
Review of Monte Carlo simulations and muon-induced neutrons

Marco Selvi – INFN Bologna

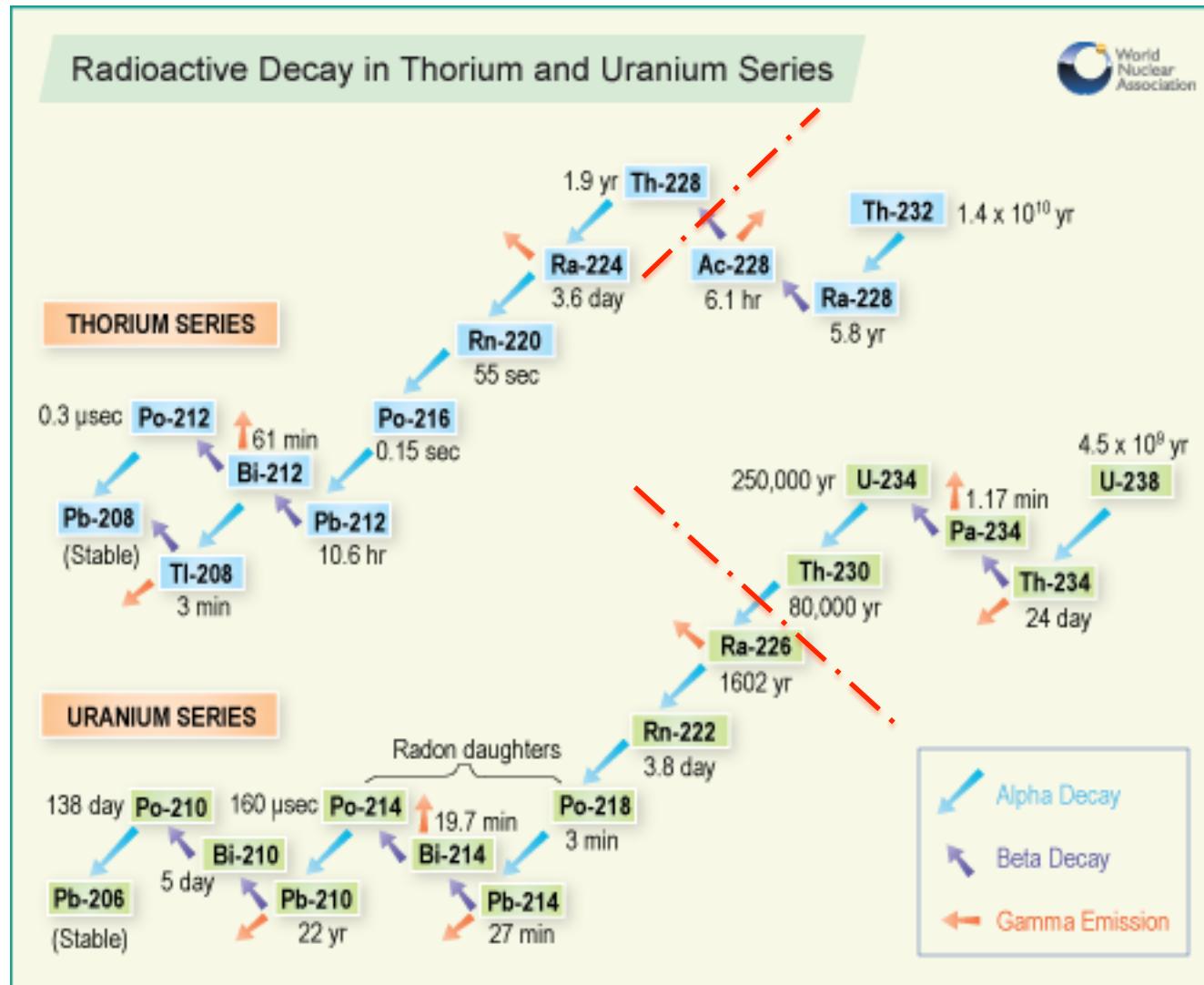
Low Radioactivity Techniques
Workshop – April, 12th 2013 - LNGS

Outline

- e.m. background:
 - Gammas, betas from radioactivity
 - Intrinsic contaminants
- Radiogenic neutrons:
 - Spontaneous fission
 - (α, n)
- Cosmogenic neutrons:
 - Muon-induced neutrons

e. m. background

U and Th chains



Radioactive decays in GEANT4

- **G4RadioactiveDecay**: process to simulate radioactive decay of nuclei
- α , β^+ , β^- decay, electron capture (EC) implemented
- Empirical and data-driven:
 - data files taken from Evaluated Nuclear Structure Data Files (ENSDF)
 - Half lives, nuclear level structure for parent and daughter nuclides, decay branching ratios, energy of decay process
- If daughter of nuclear decay is an isomer, prompt-de-excitation is done with **G4PhotonEvaporation** process

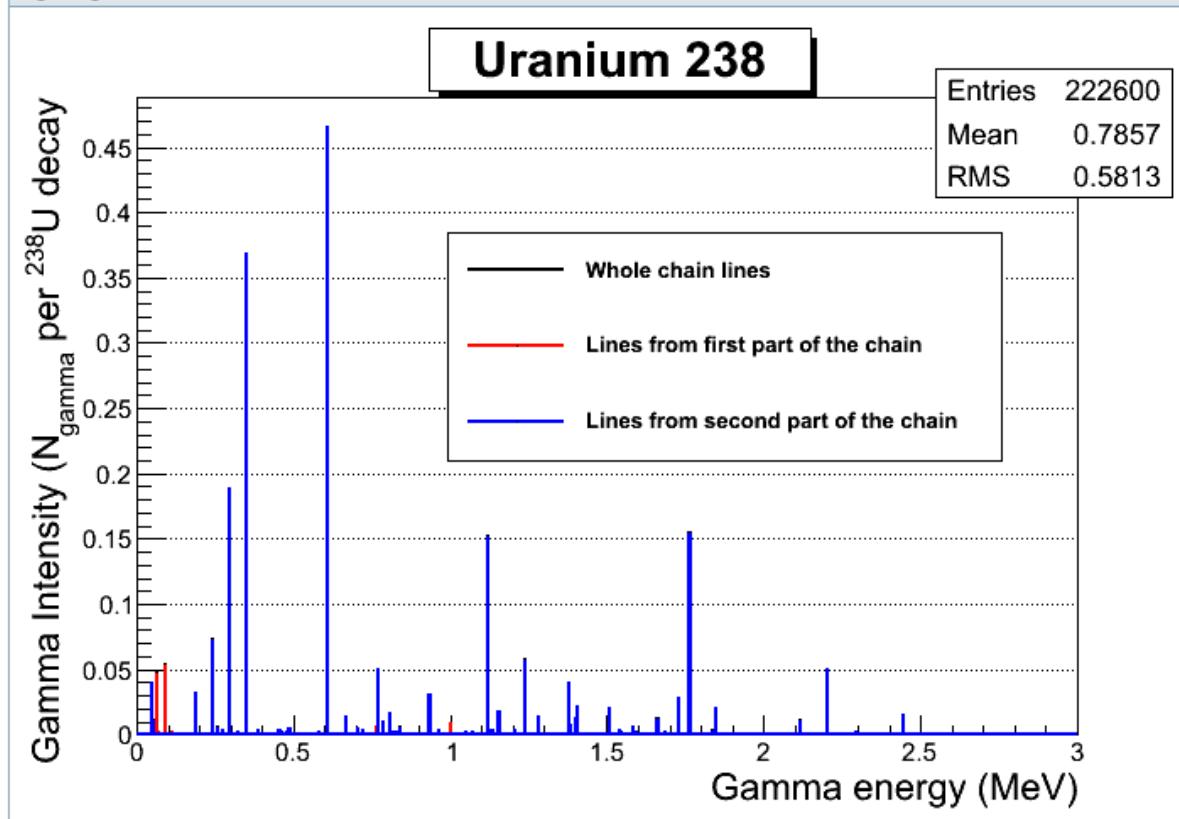
^{238}U chain

Uranium 238

Table 1: Uranium 238 chain

| Part of the chain | Gamma yield (gammas per parent decay) |
|--|---------------------------------------|
| First part: $\text{U}^{238}[0.0] \rightarrow \text{Ra}^{226}[0.0]$ | 0.14 |
| Second part: $\text{Ra}^{226}[0.0] \rightarrow \text{Pb}^{206}[0.0]$ | 2.09 |
| Whole chain: $\text{U}^{238}[0.0] \rightarrow \text{Pb}^{206}[0.0]$ | 2.23 |

Fig. 1: gamma lines from uranium 238



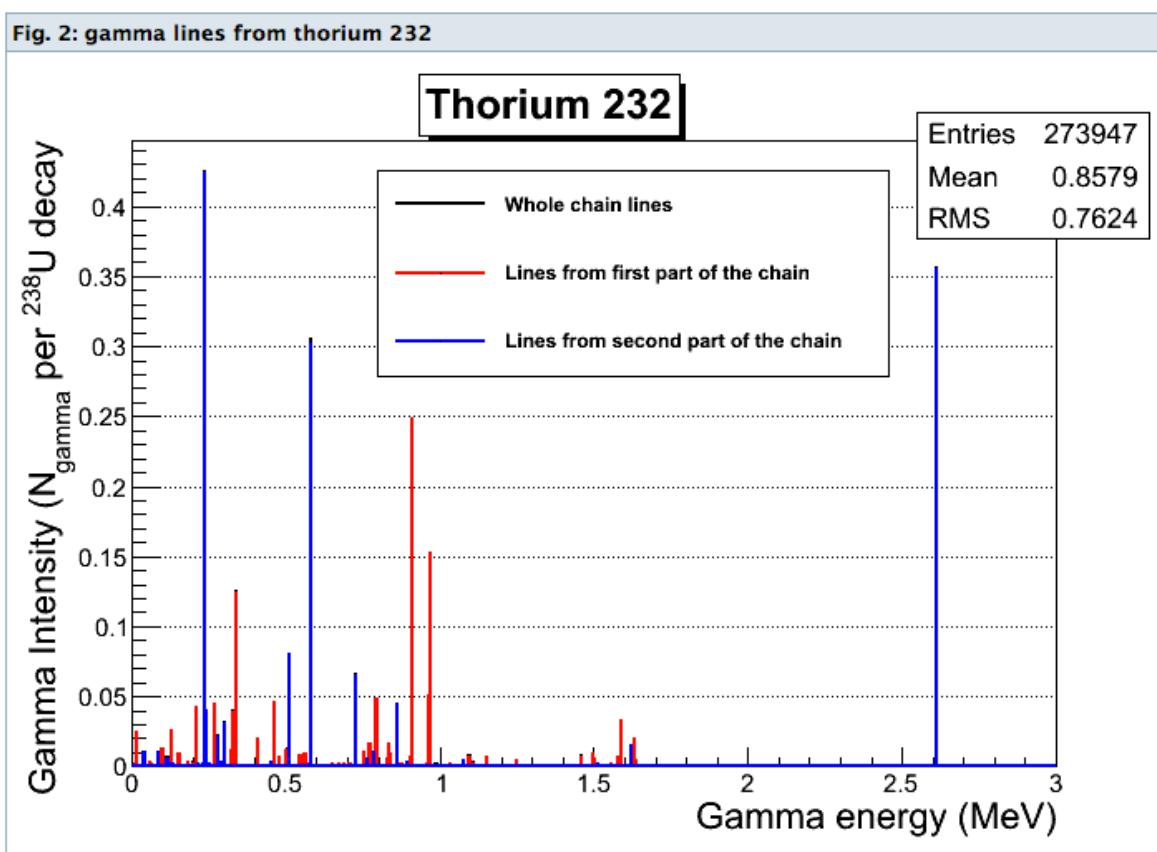
^{232}Th chain

Thorium 232

Table 2: Thorium 232 chain

| Part of the chain | Gamma yield (gammas per parent decay) |
|--|---------------------------------------|
| First part: $\text{Th}^{232}[0.0] \rightarrow \text{Th}^{228}[0.0]$ | 1.27 |
| Second part: $\text{Th}^{228}[0.0] \rightarrow \text{Pb}^{208}[0.0]$ | 1.47 |
| Whole chain: $\text{Th}^{232}[0.0] \rightarrow \text{Pb}^{208}[0.0]$ | 2.74 |

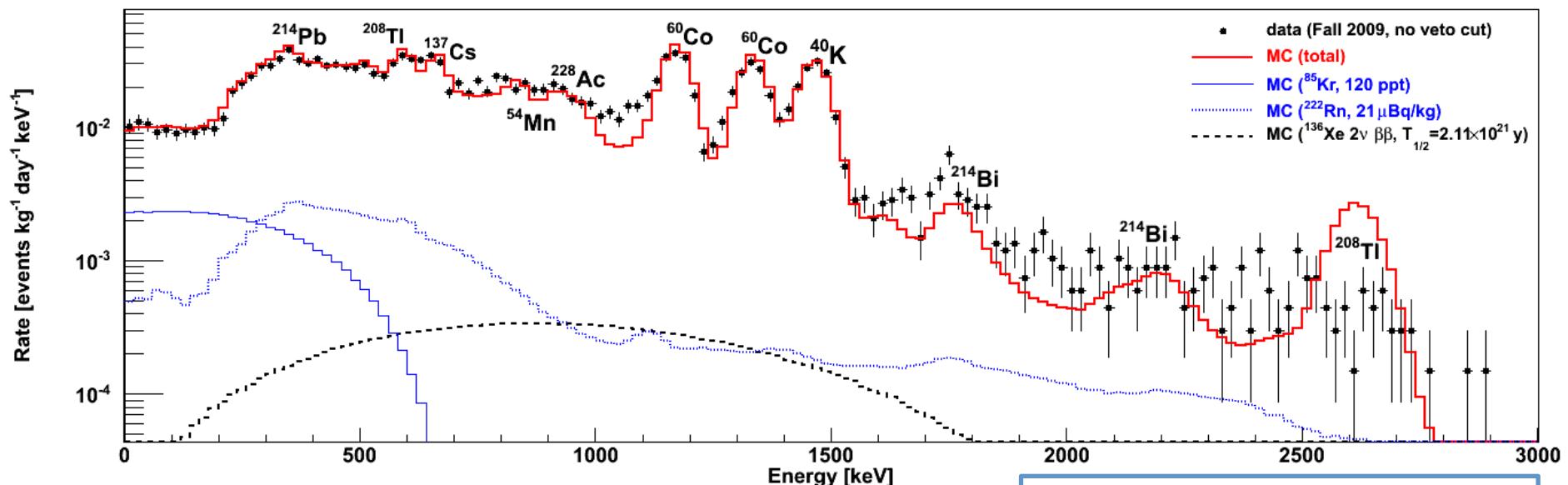
Fig. 2: gamma lines from thorium 232



MC-DATA comparison in XENON100

- Monte Carlo simulations of XENON100 e.m. background in good agreement with measured data
- Background is well understood in the full energy range

30 kg fiducial volume, single scatter, No veto cut, BEFORE S2/S1 discrimination

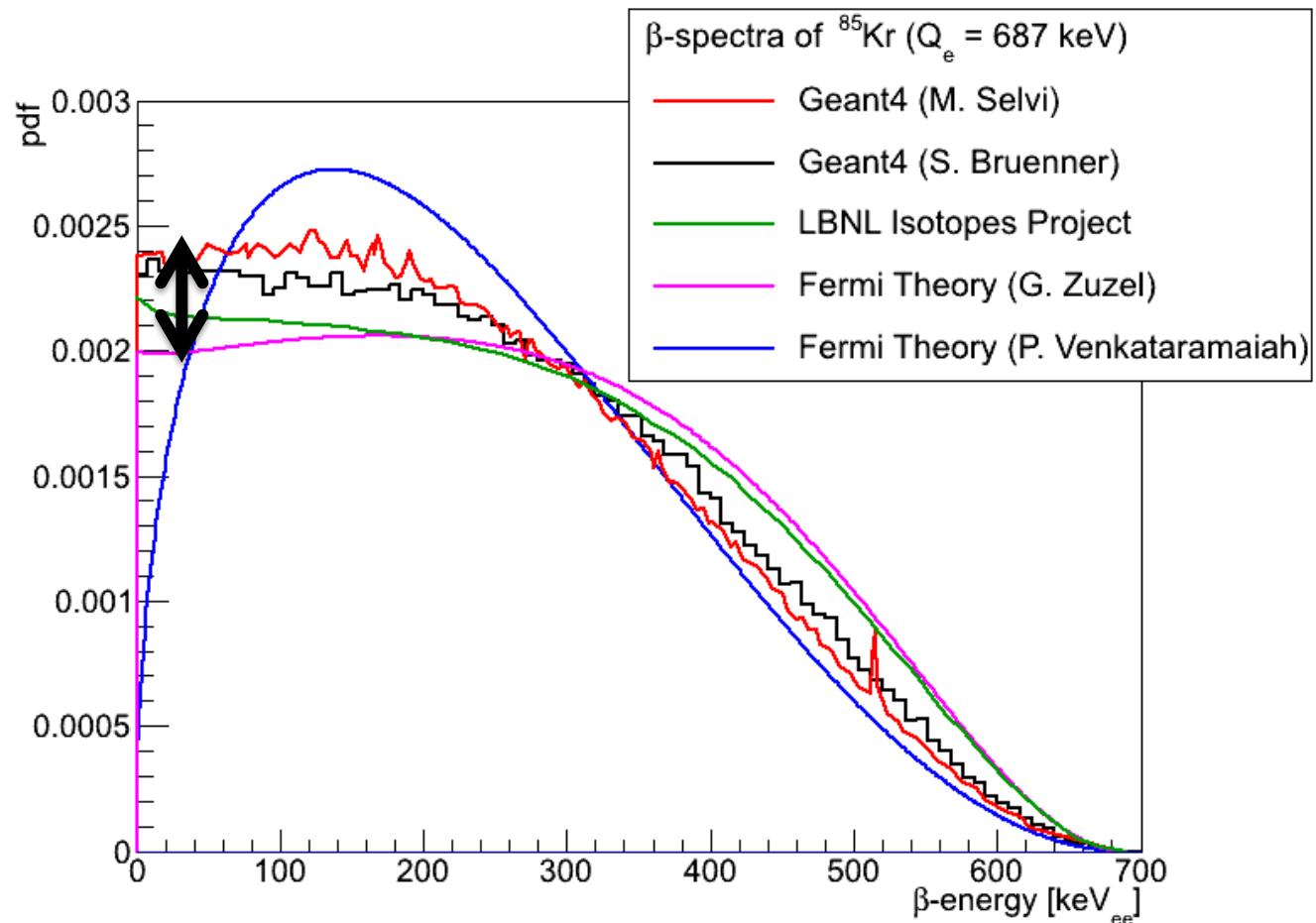


It's not a fit to the data,
we used the screened contaminations of the materials as input for the MC
simulation and superimpose with data.

Phys. Rev. D83: 082001, 2011

^{85}Kr beta spectrum

Uncertainty in
the low energy
region :
about 20 %

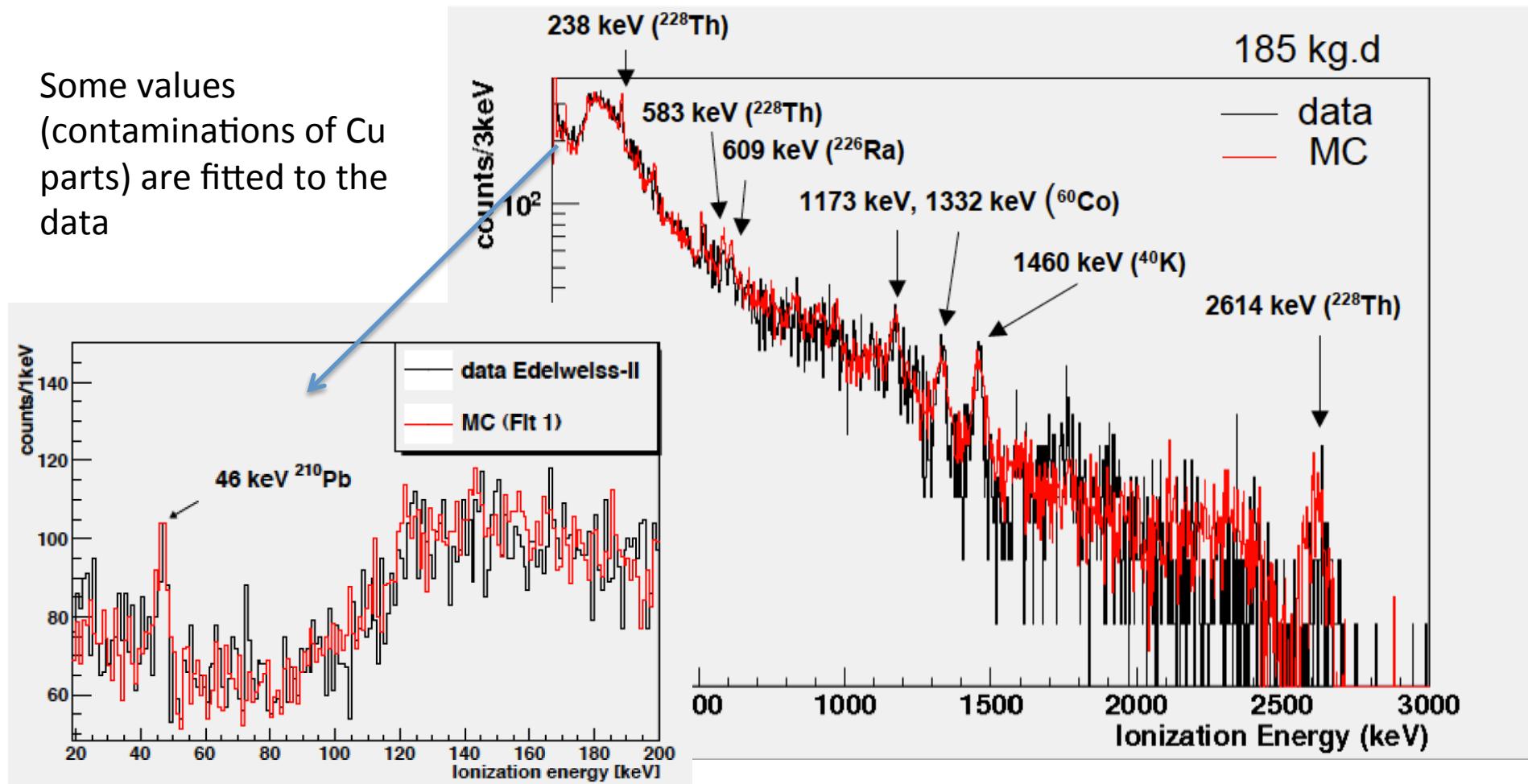


Plot by S. Lindemann - MPIK

MC-DATA comparison in EDELWEISS-II

The decays of ^{226}Ra , ^{228}Ra , ^{60}Co , ^{40}K , ^{54}Mn and ^{210}Pb were simulated in the detector casings, the copper plates at 10 mK, the bars supporting the plates, the screen and plate at 10 mK, cryostat, the dilution chamber, 1K connectors, the coaxial cables and the lead shielding

Some values
(contaminations of Cu
parts) are fitted to the
data



Radiogenic neutrons

Radiogenic neutrons

- SOURCES-4A (modified version – Sheffield group):
Wilson et al. Sources4A. Technical Report,
LA-13639-MS (1999);
Tomasello et al., NIMA 595 (2008) 431.
Cross-sections from EMPIRE.
- Zhang-Mei-Hime code
NIM A606, 651 (2009)
<http://neutronyield.usd.edu>
Cross-sections from TALYS.

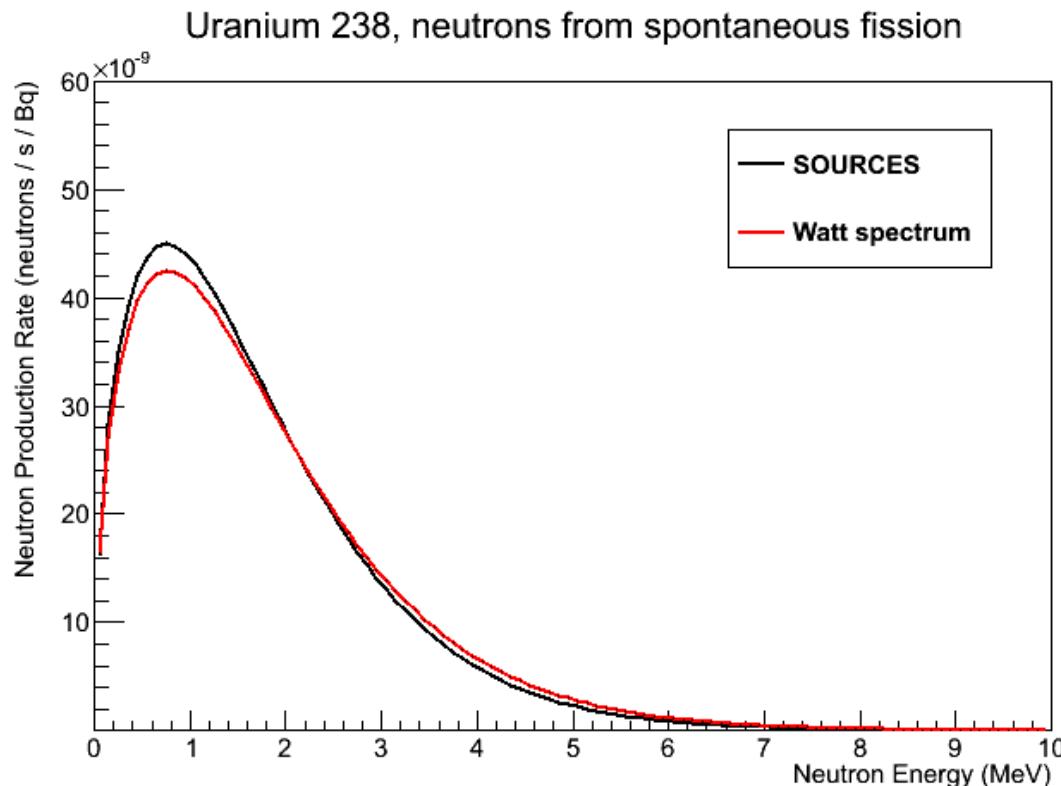
Neutrons from spontaneous fission

Watt's spectrum: $N(E) = C * e^{(-E/a)} * \sinh(\sqrt{b*E})$

with $a = 0.7124 \text{ MeV}$, $b = 5.6405 \text{ MeV}^{-1}$.

C is the normalization factor.

H. Wulandari et al., Astrop. Phys. 22 313 (2004).



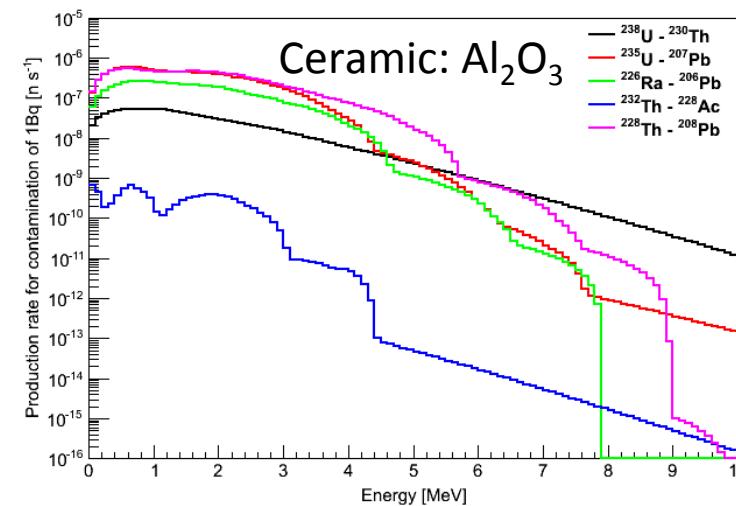
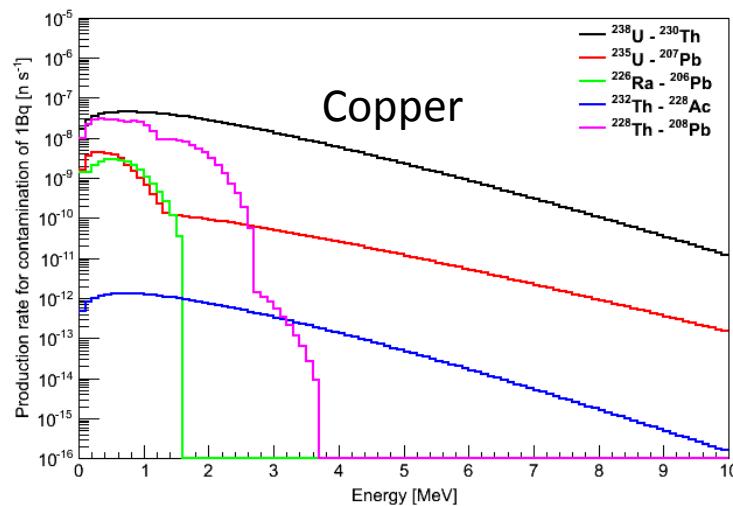
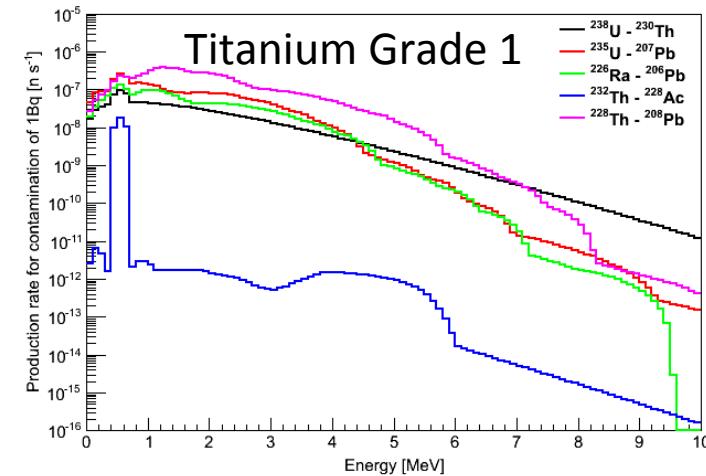
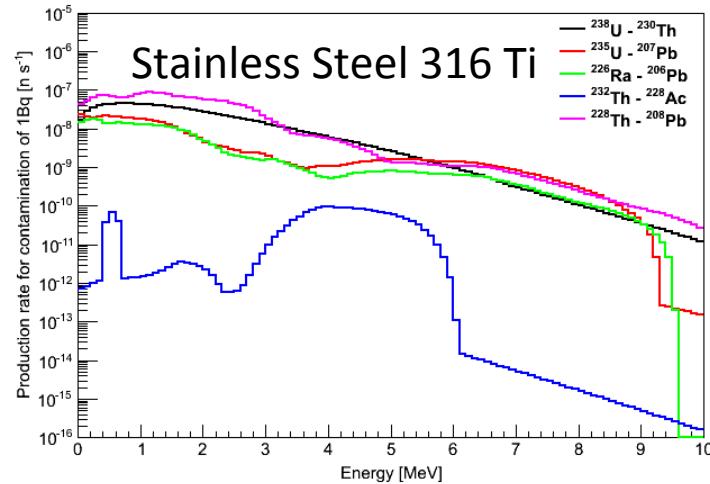
1 kg of Uranium
emits 13.53 n/s
(taken from
<http://www.wise-uranium.org/ranc.html>),
 $\rightarrow 1.1 \cdot 10^{-6} \text{ n/s} @ 1 \text{ Bq}$
independent from the material

Neutron production with SOURCES

Table 1: Neutron production rate due to (α, n) and spontaneous fission reactions calculated with SOURCES-4A. Included is the systematic unc

| Material | Neutron production for contamination of 1Bq [$n \cdot s^{-1}$] | | | | |
|---|--|------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|
| | $^{238}\text{U} - ^{230}\text{Th}$ | $^{235}\text{U} - ^{207}\text{Pb}$ | $^{226}\text{Ra} - ^{206}\text{Pb}$ | $^{232}\text{Th} - ^{228}\text{Ac}$ | $^{228}\text{Th} - ^{208}\text{Pb}$ |
| stainless steel 316Ti | $(1.1 \pm 0.2) \cdot 10^{-6}$ | $(4.1 \pm 0.7) \cdot 10^{-7}$ | $(3.1 \pm 0.5) \cdot 10^{-7}$ | $(1.8 \pm 0.3) \cdot 10^{-9}$ | $(2.0 \pm 0.3) \cdot 10^{-6}$ |
| stainless steel 304L | $(1.1 \pm 0.2) \cdot 10^{-6}$ | $(3.4 \pm 0.6) \cdot 10^{-7}$ | $(2.8 \pm 0.5) \cdot 10^{-7}$ | $(4.9 \pm 0.8) \cdot 10^{-11}$ | $(2.0 \pm 0.3) \cdot 10^{-6}$ |
| titanium | $(1.2 \pm 0.2) \cdot 10^{-6}$ | $(3.3 \pm 0.6) \cdot 10^{-6}$ | $(2.0 \pm 0.3) \cdot 10^{-6}$ | $(3.8 \pm 0.7) \cdot 10^{-8}$ | $(7.7 \pm 1.3) \cdot 10^{-6}$ |
| copper | $(1.1 \pm 0.2) \cdot 10^{-6}$ | $(3.3 \pm 0.6) \cdot 10^{-8}$ | $(2.5 \pm 0.4) \cdot 10^{-8}$ | $(3.0 \pm 0.5) \cdot 10^{-11}$ | $(3.6 \pm 0.6) \cdot 10^{-7}$ |
| PTFE | $(7.4 \pm 1.3) \cdot 10^{-6}$ | $(1.3 \pm 0.2) \cdot 10^{-4}$ | $(5.5 \pm 0.9) \cdot 10^{-5}$ | $(7.3 \pm 1.2) \cdot 10^{-7}$ | $(1.0 \pm 0.2) \cdot 10^{-4}$ |
| Cirlex | $(1.3 \pm 0.2) \cdot 10^{-6}$ | $(2.2 \pm 0.4) \cdot 10^{-6}$ | $(3.5 \pm 0.6) \cdot 10^{-6}$ | $(4.1 \pm 0.7) \cdot 10^{-8}$ | $(2.4 \pm 0.4) \cdot 10^{-6}$ |
| Kovar | $(1.1 \pm 0.2) \cdot 10^{-6}$ | $(1.3 \pm 0.2) \cdot 10^{-7}$ | $(1.2 \pm 0.2) \cdot 10^{-7}$ | $(3.0 \pm 0.5) \cdot 10^{-11}$ | $(1.0 \pm 0.2) \cdot 10^{-6}$ |
| quartz (fused silica, SiO_2) | $(1.2 \pm 0.2) \cdot 10^{-6}$ | $(1.9 \pm 0.3) \cdot 10^{-6}$ | $(8.8 \pm 1.5) \cdot 10^{-7}$ | $(6.8 \pm 1.2) \cdot 10^{-9}$ | $(1.9 \pm 0.3) \cdot 10^{-6}$ |
| ceramics, aluminum oxide (Al_2O_3) | $(1.2 \pm 0.2) \cdot 10^{-6}$ | $(1.3 \pm 0.2) \cdot 10^{-5}$ | $(6.0 \pm 1.0) \cdot 10^{-6}$ | $(9.2 \pm 1.6) \cdot 10^{-9}$ | $(1.4 \pm 0.2) \cdot 10^{-5}$ |
| ceramics, titanium oxide (Ti_2O_3) | $(1.2 \pm 0.2) \cdot 10^{-6}$ | $(1.8 \pm 0.3) \cdot 10^{-6}$ | $(1.1 \pm 0.2) \cdot 10^{-6}$ | $(2.1 \pm 0.4) \cdot 10^{-8}$ | $(3.9 \pm 0.7) \cdot 10^{-6}$ |
| polyethylene (C_2H_4) | $(1.2 \pm 0.2) \cdot 10^{-6}$ | $(1.6 \pm 0.3) \cdot 10^{-6}$ | $(7.5 \pm 1.3) \cdot 10^{-7}$ | $(3.1 \pm 0.5) \cdot 10^{-8}$ | $(1.4 \pm 0.2) \cdot 10^{-6}$ |
| PEN (polyethylene naphtalate, $[\text{C}_{14}\text{H}_{12}\text{O}_4 \cdot \text{C}_2\text{H}_6\text{O}_2]_n$) | $(1.3 \pm 0.2) \cdot 10^{-6}$ | $(2.0 \pm 0.3) \cdot 10^{-6}$ | $(9.4 \pm 1.6) \cdot 10^{-7}$ | $(3.7 \pm 0.6) \cdot 10^{-8}$ | $(1.7 \pm 0.3) \cdot 10^{-6}$ |
| PMMA, acrylic plastic (polymethyl methacrylate, $[\text{C}_5\text{H}_8\text{O}_2]_n$) | $(1.3 \pm 0.2) \cdot 10^{-6}$ | $(1.8 \pm 0.3) \cdot 10^{-6}$ | $(8.8 \pm 1.5) \cdot 10^{-7}$ | $(3.5 \pm 0.6) \cdot 10^{-8}$ | $(1.6 \pm 0.3) \cdot 10^{-6}$ |
| PEEK (polyether ether kethone, $[\text{OC}_6\text{H}_4\text{OC}_6\text{H}_4\text{COC}_6\text{H}_4]_n$) | $(1.3 \pm 0.2) \cdot 10^{-6}$ | $(2.4 \pm 0.4) \cdot 10^{-6}$ | $(1.1 \pm 0.2) \cdot 10^{-6}$ | $(4.6 \pm 0.8) \cdot 10^{-8}$ | $(2.1 \pm 0.4) \cdot 10^{-6}$ |
| LNGS concrete | $(1.2 \pm 0.2) \cdot 10^{-6}$ | $(1.5 \pm 0.3) \cdot 10^{-6}$ | $(7.1 \pm 1.2) \cdot 10^{-7}$ | $(7.8 \pm 1.3) \cdot 10^{-9}$ | $(1.5 \pm 0.3) \cdot 10^{-6}$ |

Neutron production with SOURCES



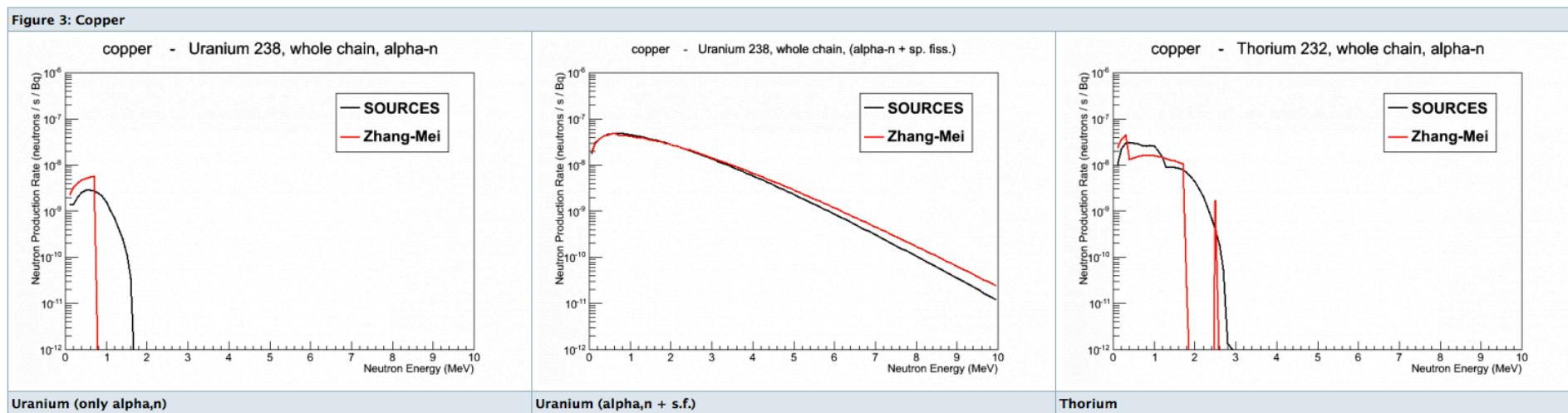
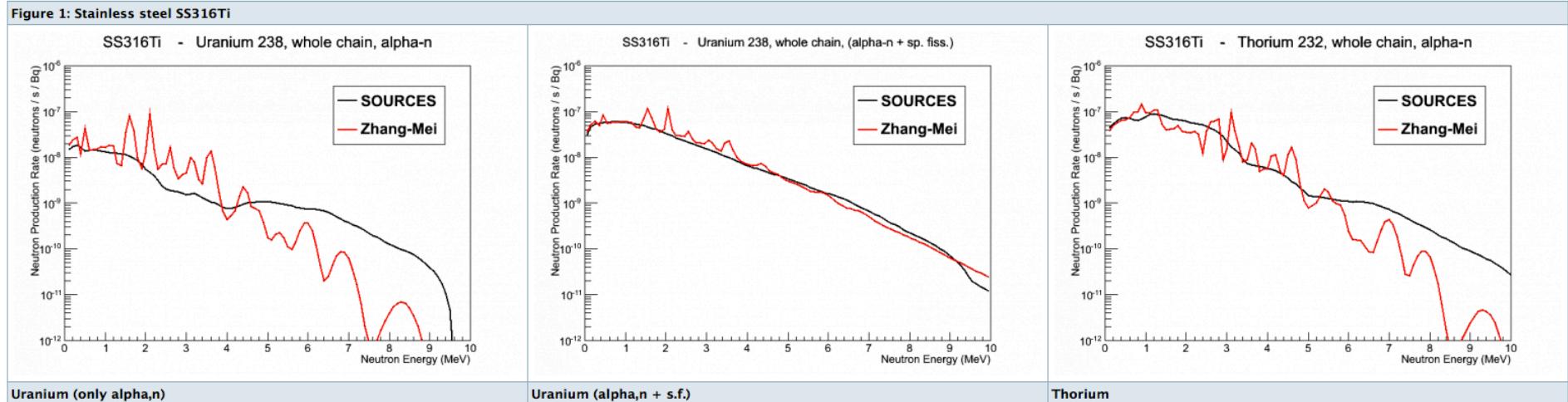
Cross checks of (alpha,n) neutrons

Comparison of the neutrons produced by (alpha,n) interactions between **SOURCES** and the code by [Zhang, Mei and Hime](#).

| Material | U238 (only alpha,n) | | | | U238 (alpha,n + s.f.) | | | | Th232 | | | |
|----------|---------------------|-----------|--------|----------|-----------------------|---------|----------|-----------|--------|---------|-----------|--------|
| | SOURCES | Zhang-Mei | Diff % | SOURCES | Zhang-Mei | Diff % | SOURCES | Zhang-Mei | Diff % | SOURCES | Zhang-Mei | Diff % |
| SS316Ti | 3.16e-07 | 6.57e-07 | -70.1% | 1.42e-06 | 1.75e-06 | -21% | 1.98e-06 | 2.05e-06 | -3.49% | | | |
| TiGrade1 | 2.14e-06 | 3.58e-06 | -50.5% | 3.24e-06 | 4.67e-06 | -36.3% | 7.7e-06 | 6.76e-06 | 12.9% | | | |
| copper | 2.46e-08 | 3.06e-08 | -21.6% | 1.12e-06 | 1.13e-06 | -0.294% | 3.56e-07 | 3.01e-07 | 16.6% | | | |
| PTFE | 6.09e-05 | 5.91e-05 | 2.88% | 6.2e-05 | 6.02e-05 | 2.84% | 0.000104 | 6.06e-05 | 52.9% | | | |
| Al2O3 | 6.17e-06 | 6.94e-06 | -11.6% | 7.28e-06 | 8.03e-06 | -9.87% | 1.39e-05 | 8.59e-06 | 47.1% | | | |
| Ti2O3 | 1.17e-06 | 2.51e-06 | -72.8% | 2.27e-06 | 3.6e-06 | -45.3% | 3.89e-06 | 4.62e-06 | -17.3% | | | |
| Poly | 8.83e-07 | 8.31e-07 | 6.09% | 1.99e-06 | 1.93e-06 | 3.06% | 1.39e-06 | 7.56e-07 | 59.3% | | | |

The total neutron yields are [within a factor 2](#).

Cross checks of (alpha,n) neutrons



Cross checks of (alpha,n) neutrons

Figure 5: Ceramic (Al₂O₃)

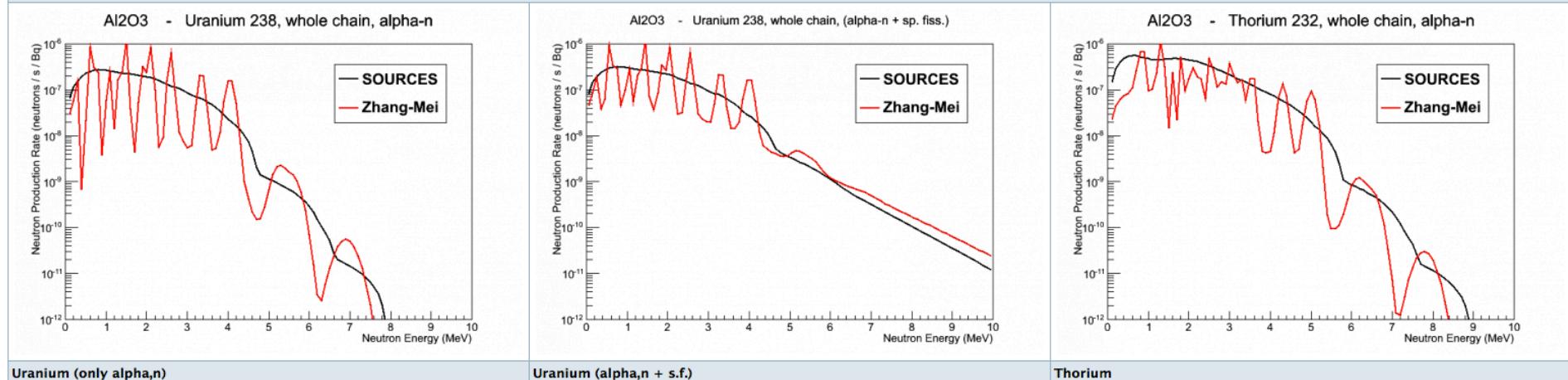
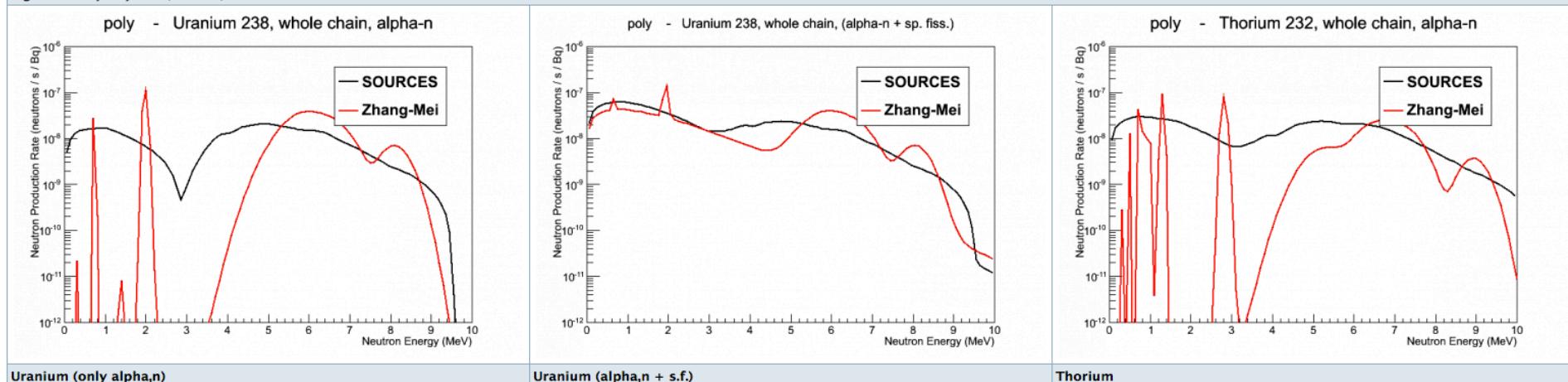


Figure 7: Polyethylene (C_nH_{2n})



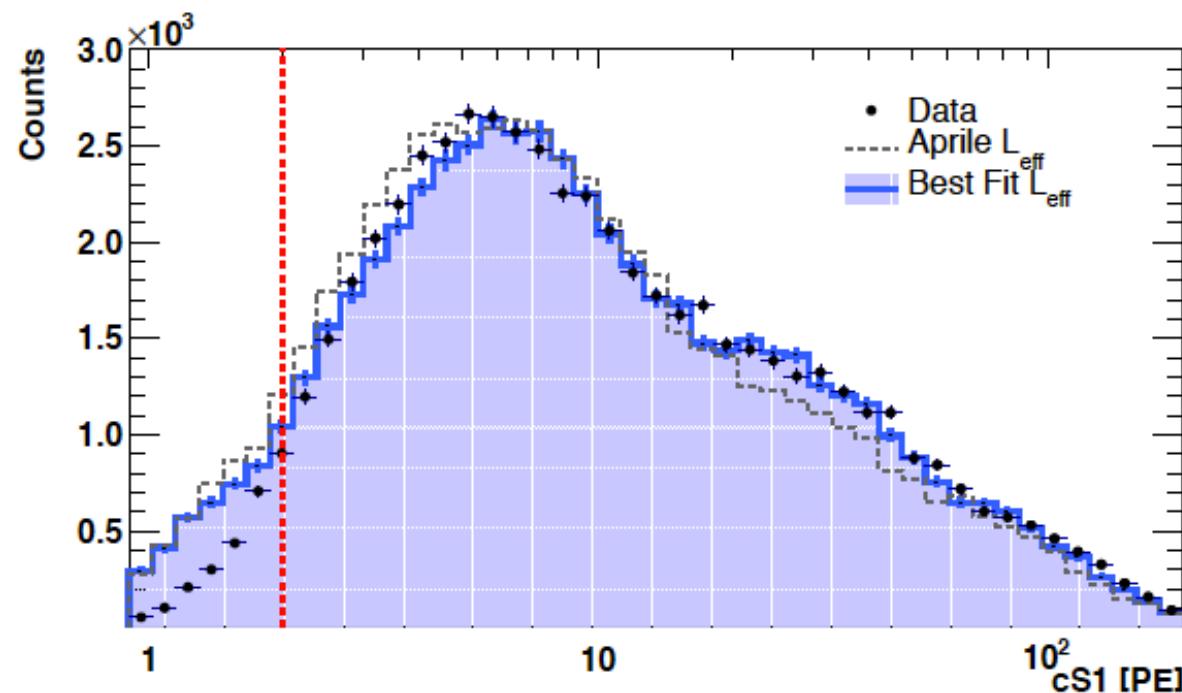
Neutron propagation and interaction

Response of the XENON100 Dark Matter Detector to Nuclear Recoils – arXiv:1304.1427

Neutrons from AmBe calibration source.

Comparison between data and the GEANT4 simulation shows a good agreement.

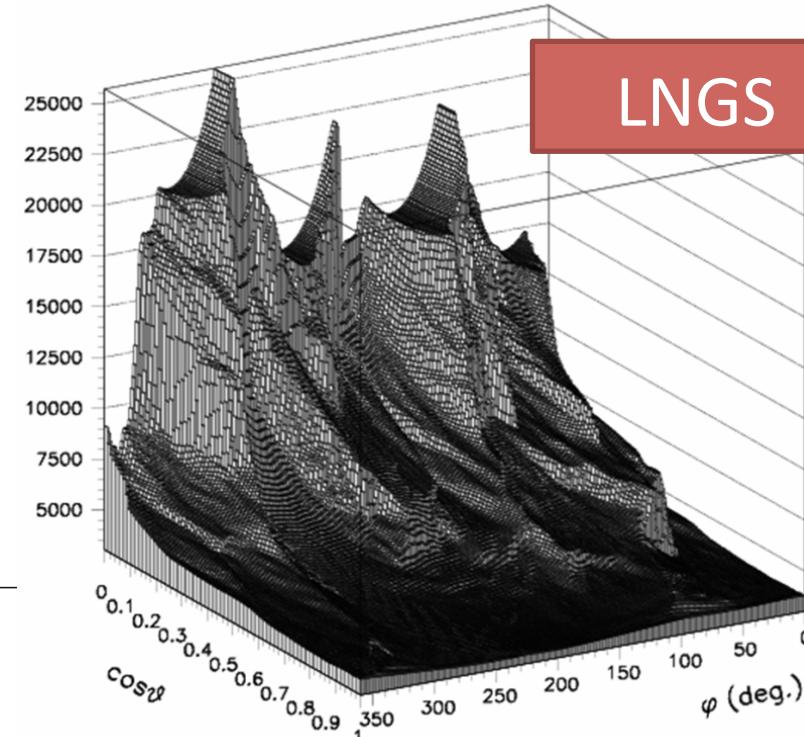
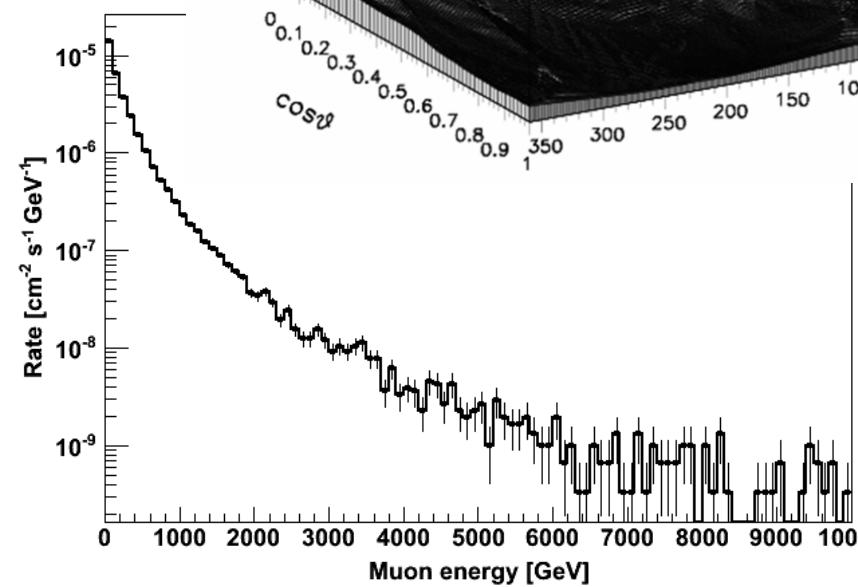
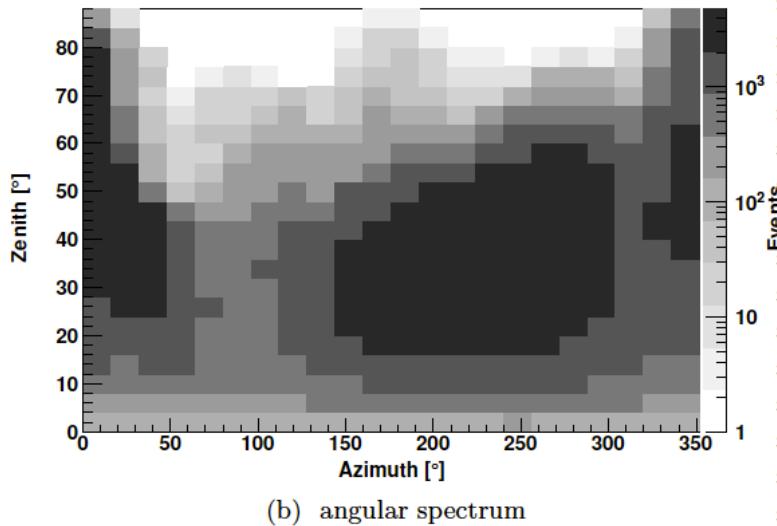
“HP” physics list was used for neutron propagation and interaction, using the ENDF/B-VI/B-VII databases provided in the data files G4NDL 3.13.



Muon-induced neutrons

Ingredients

- Muon flux, energy spectrum and angular distribution (site dependent)
→ MUSIC, MUSUN
V. Kudryavtsev, Comp. Phys. Comm. 180 (2009) 339

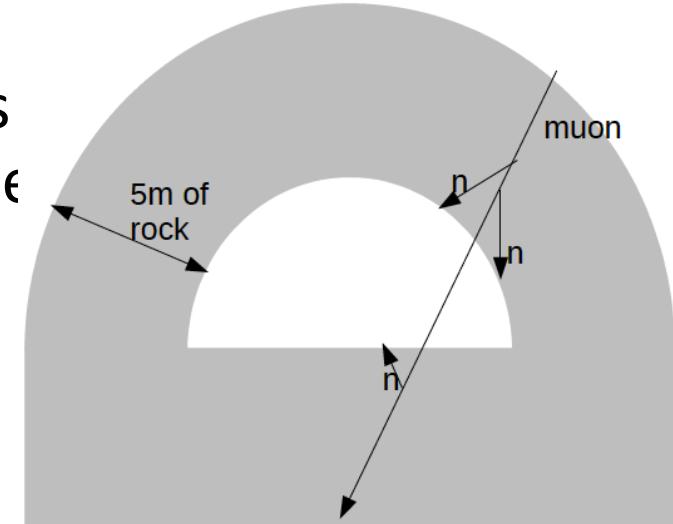


Ingredients

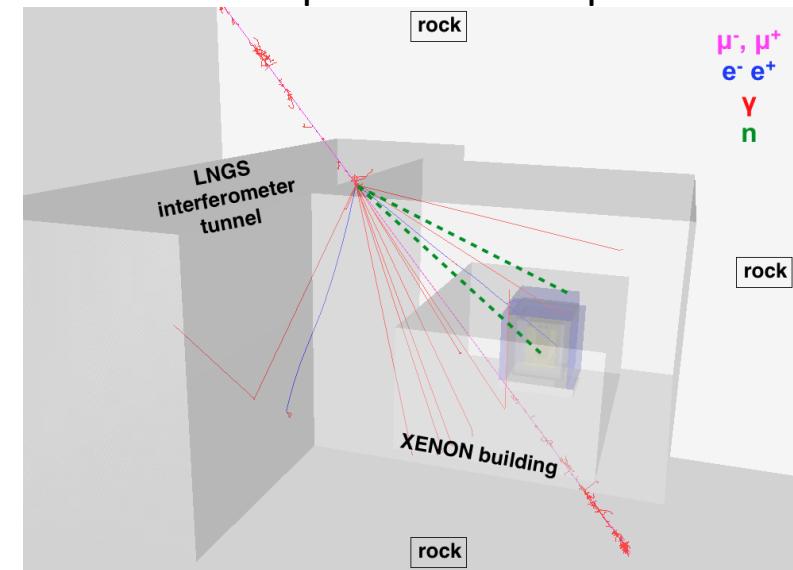
- Put a few meters of rock thickness around the hall to fully develop the muon-induced showers.

- Rock composition

| Element | Percentage in weight | |
|---------|----------------------|------|
| | LNGS | LSM |
| H | 0 | 1 |
| C | 12 | 5.94 |
| O | 51 | 49.4 |
| Na | 0 | 0.44 |
| Mg | 8.4 | 0.84 |
| Al | 0.6 | 2.58 |
| Si | 1 | 6.93 |
| P | 0 | 0.06 |
| K | 0 | 0.21 |
| Ca | 27 | 30.6 |
| Ti | 0 | 0.07 |
| Mn | 0 | 0.03 |
| Fe | 0 | 1.9 |

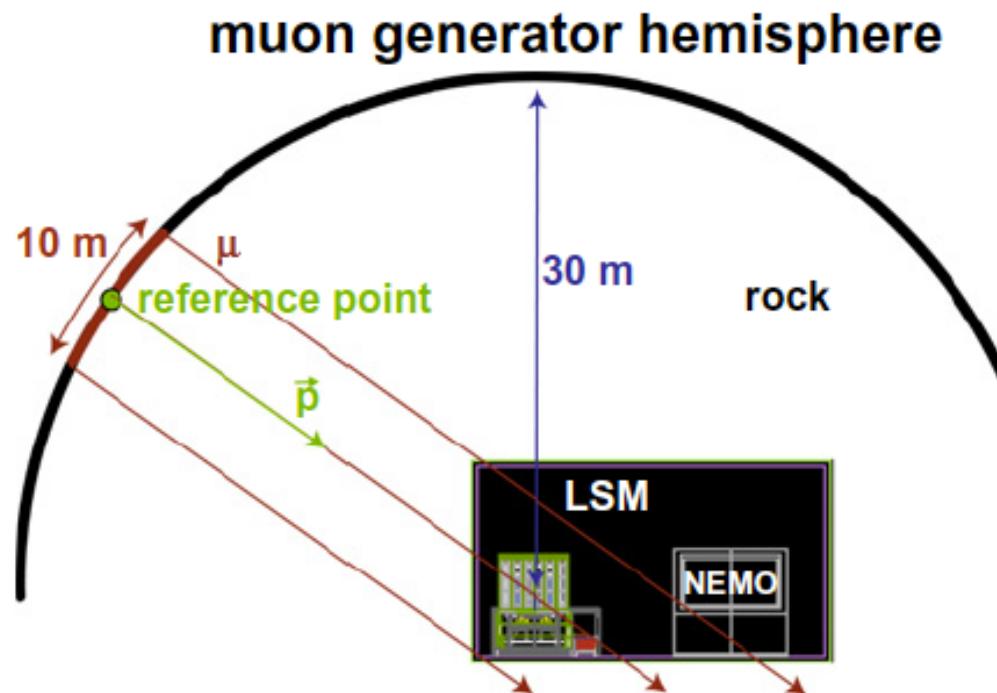


- Detailed description of the experimental hall



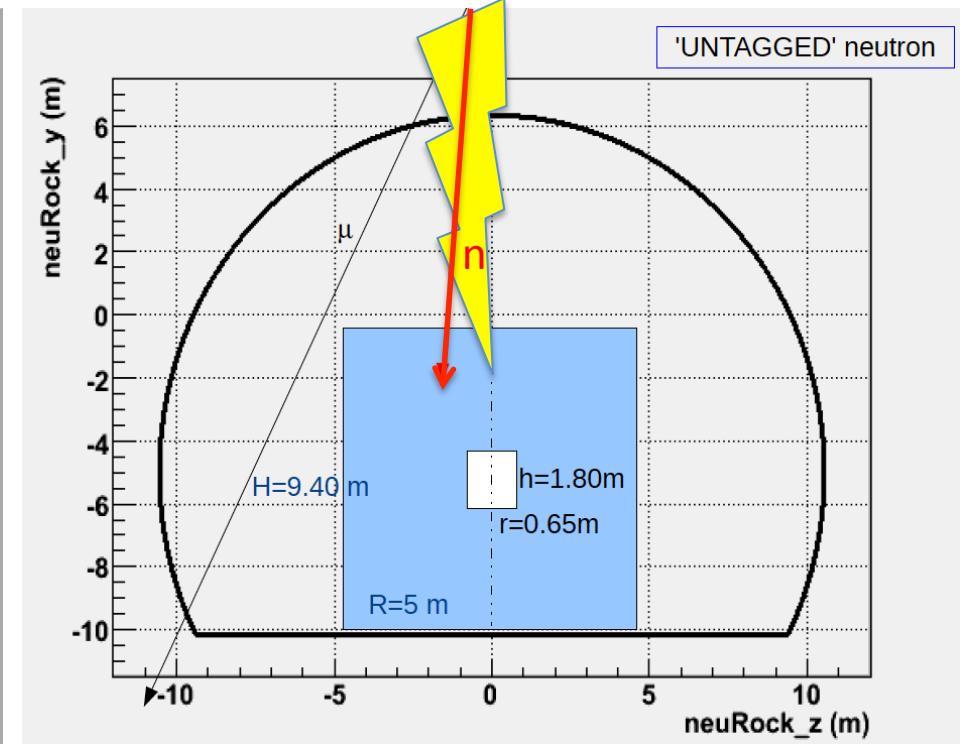
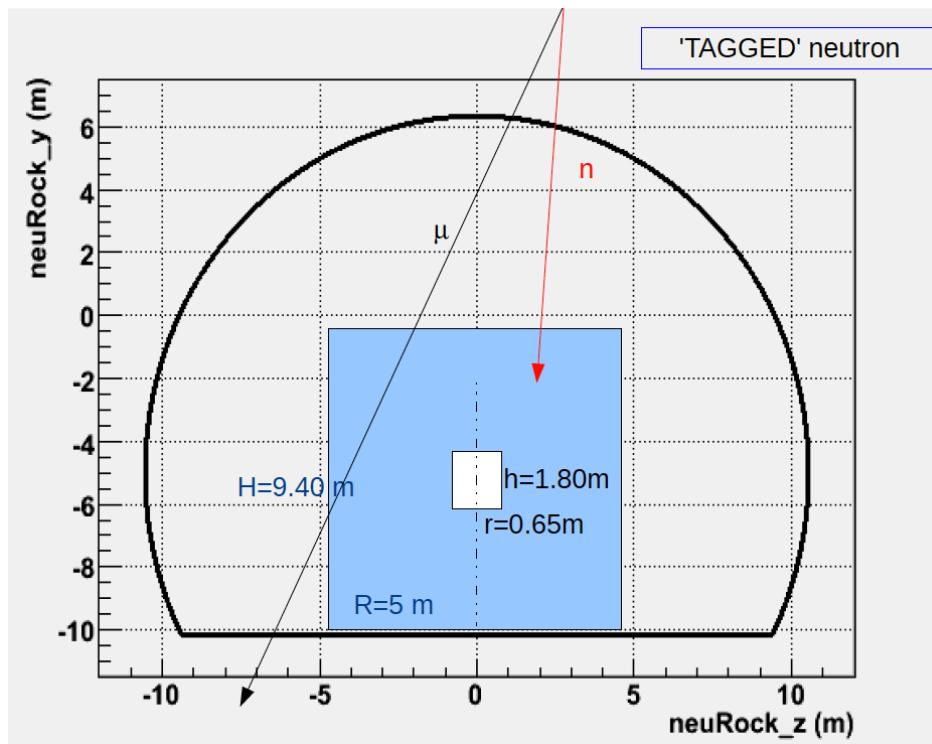
Ingredients

- Generate muons over a large area: radius up to 10-30 meters from the experimental site



Ingredients

- Propagate all the secondary particles , not just the neutrons (in particular for active veto)



Neutron flux underground

100M muons were generated with [GEANT4 9.3 \(physics list QGSP_BIC_HP\)](#) with the proper energy and angular distribution at LNGS. They were sampled over a large area: a circle with 30m radius, corresponding to about 1250 days at Gran Sasso.

Muons are propagated through the LNGS rock, all the neutrons produced by direct spallation, e.m. and hadronic cascades are followed and their entrance point and momentum at the hall surface is recorded.

The total flux from the MC is:

$$E_n > 10 \text{ MeV}: 1.3 \cdot 10^{-10} (\text{cm}^2 \text{ s})^{-1}$$

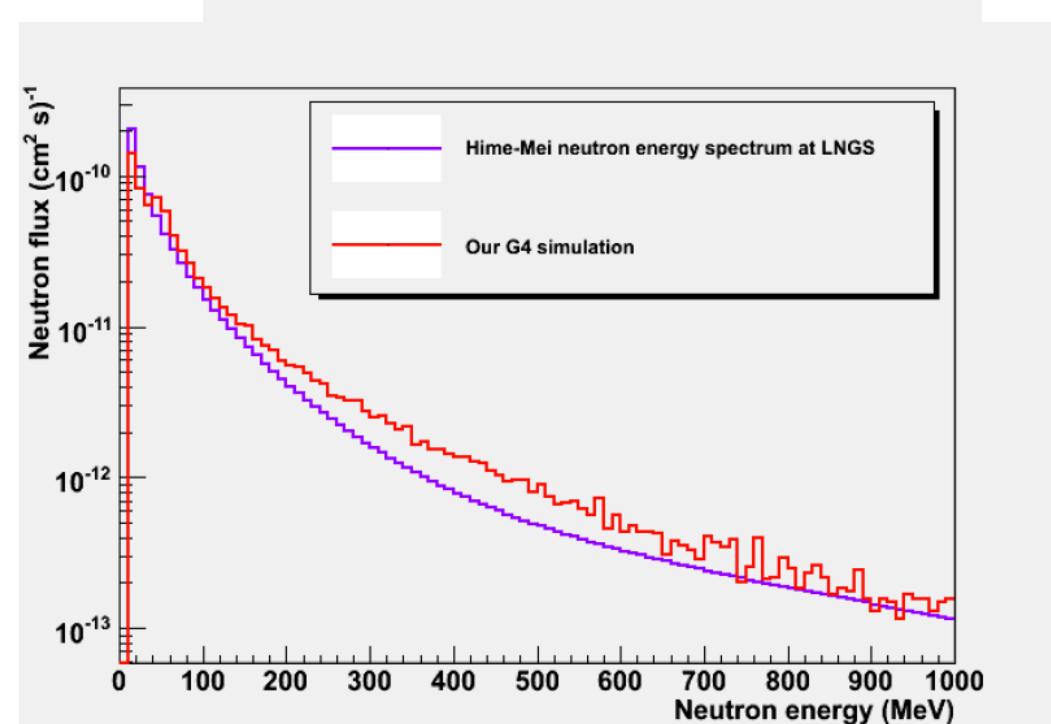
$$E_n > 100 \text{ MeV}: 3.7 \cdot 10^{-11} (\text{cm}^2 \text{ s})^{-1}$$

FLUKA (+some “doping”) simulation:

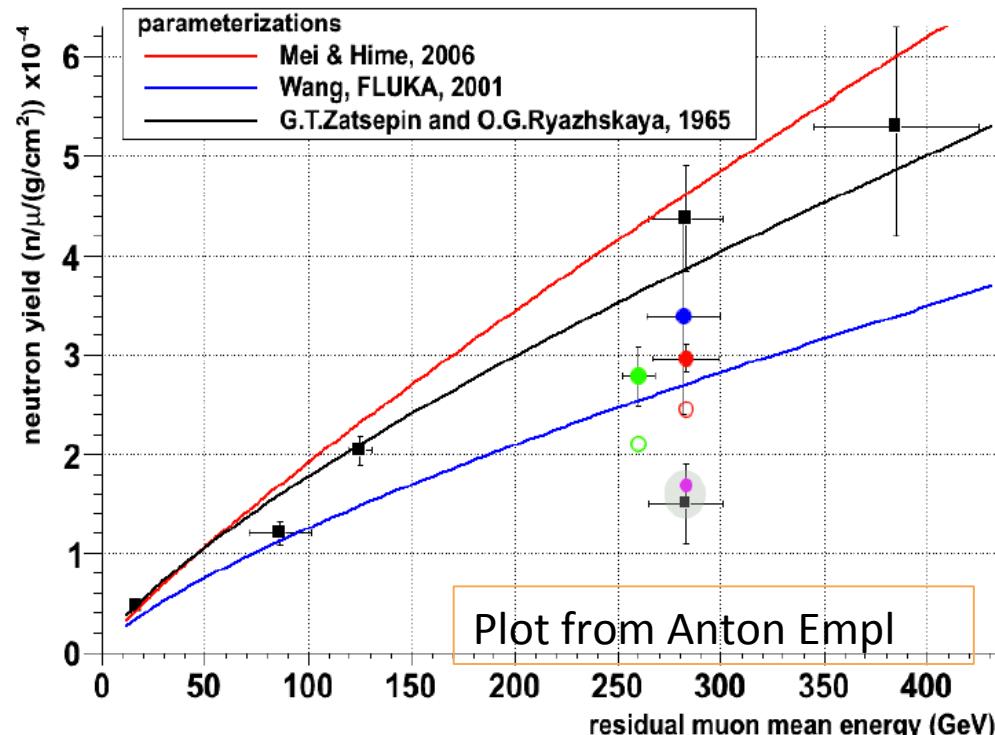
Mei and Hime, Phys. Rev. D 73, 053004 (2006):

$$E_n > 10 \text{ MeV}: 7.3 \cdot 10^{-10} (\text{cm}^2 \text{ s})^{-1}$$

About 6 times higher !



n-yield in liquid scint. : data vs FLUKA



solid black symbols: Malgin and Ryazhskaya, Yad. Fiz. 71, 1800 (2008)
Phys. At. Nuclei 71, 1769 (2008)

Measurements made by physicists of the Laboratory of Electron Methods for Neutrino Detection, Inst. for Nuclear Research, Moscow and by members of the LSD and LVD collaborations. The black line is not a fit to the data but an early prediction.

See also N. Agafonova, A. Malgin arXiv:1304.0919
Universal formula for the muon-induced neutron yield

Solid blue symbol:
PhD R. Persiani, Bologna (2011)
Presentation at AARM meeting (2012)
Recent result from LVD

Solid and open green symbols:
Phys. Rev. C 81, 025807 (2010)
Results from KamLAND on cosmogenic neutron and isotope production. The open symbol corresponds to results from a FLUKA simulation.

Solid and open red symbols:
PhD A. Chavarria, Princeton (2012)
A first result from Borexino on the neutron yield. The open symbol corresponds to the FLUKA predicted yield - however, note slides on ^{11}C production.

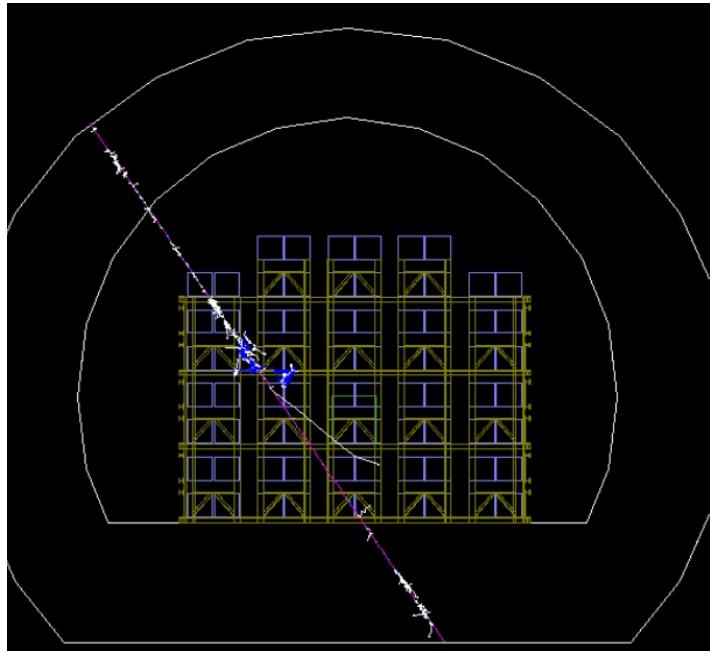
Gray shaded:
Early results (1999) reported from LVD (black) and CTF (purple symbol).

FLUKA vs GEANT4



... see A. Villano talk in a while :
**A Comprehensive Comparison for Simulations of
Cosmic Ray Muons Underground**

LVD



The MC also tells us that 80% of the neutrons are produced in the iron of the support structure:

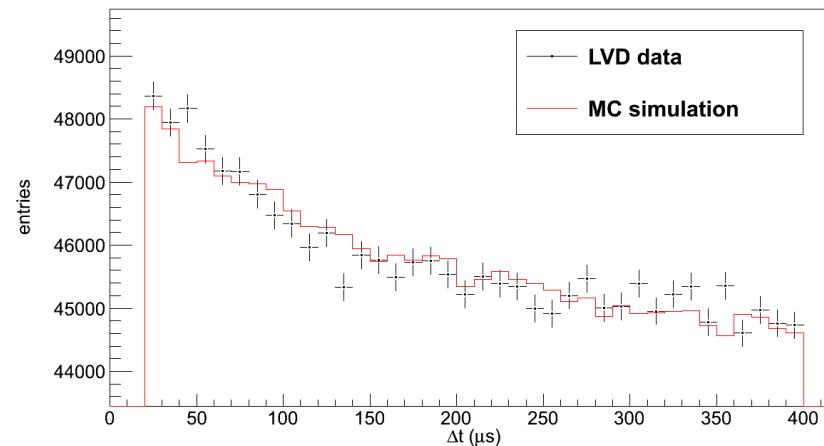
$$Y_{LS} = (2.9 \pm 0.6) \times 10^{-4} \text{ n}/(\text{g/cm}^2)$$

$$Y_{Fe} = (1.5 \pm 0.3) \times 10^{-3} \text{ n}/(\text{g/cm}^2)$$

Monte Carlo simulation done in GEANT4 9.3, with the QGSP_BIC_HP physics list.

Background evaluation independent from the muon-correlated data.

Agreement with the experimental data increasing the MC by a factor 1.4.

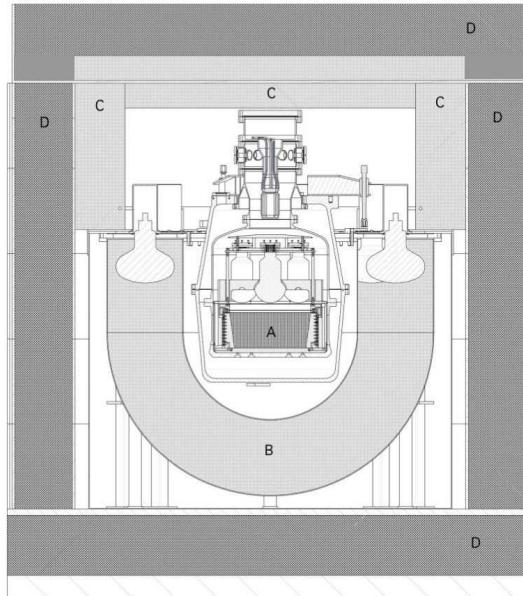


More details in Rino Persiani's poster:
Measurement of the neutron yield induced by muons in liquid scintillator and iron at LNGS with LVD experiment

ZEPLIN II and III

ZEPLIN-II measurement: [Astrop. Phys. 29 \(2008\) 471](#)

Details of the MC simulation: [Astrop. Phys. 31 \(2009\) 366](#)



Neutrons detected via their capture in Gd-loaded liquid scintillator detector

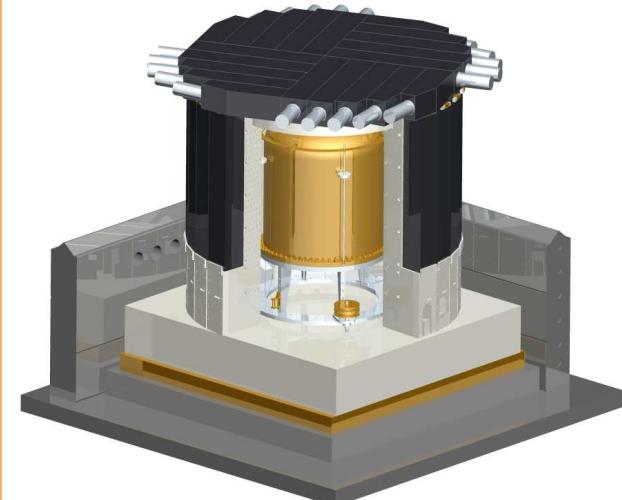
MC simulation developed in GEANT4 8.2,
with a custom physics list

Wait for Lea Reichhart's talk
about the results of ZEPLIN-III

Neutron production mainly in the lead of the shield:

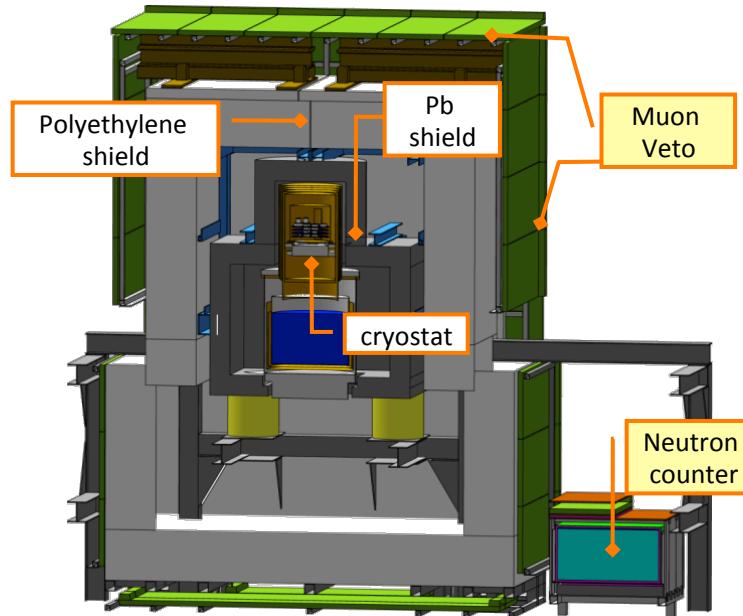
- DATA: $0.079 \pm 0.003 \text{ n}/\mu$
- MC: $0.143 \pm 0.010 \text{ n}/\mu$

MC simulation is a factor **1.8 higher**
than the DATA



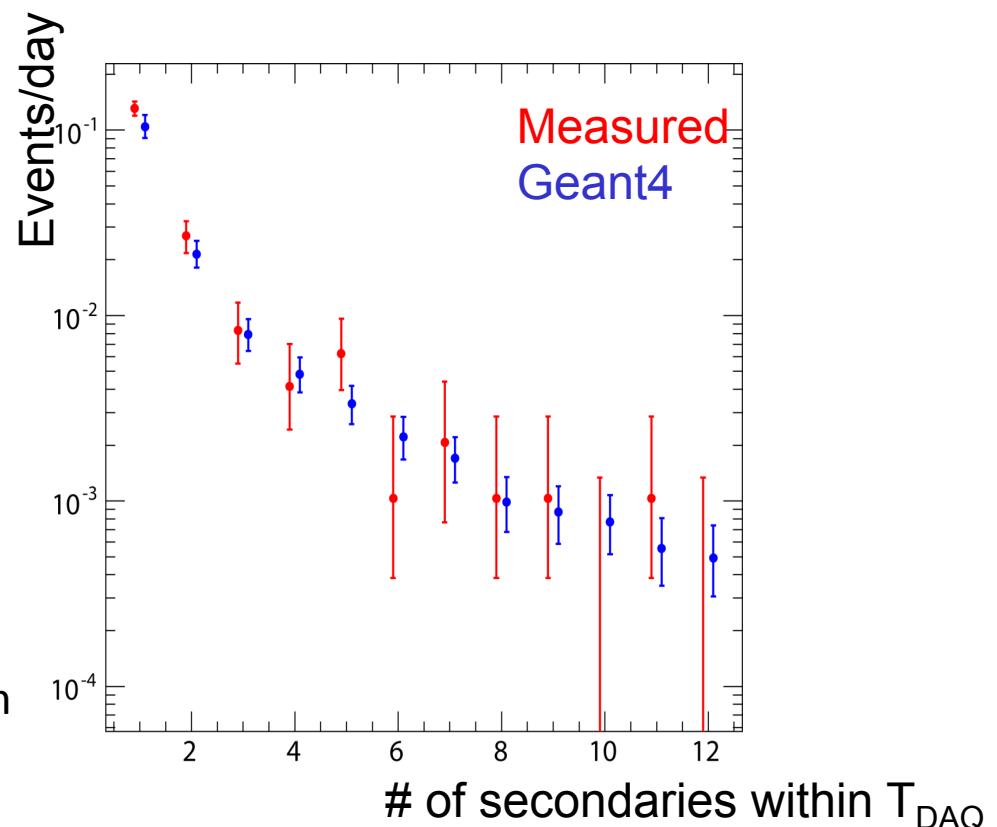
EDELWEISS – Gd Neutron counter

Muon-veto performance in
Astrop. Phys. 44 (2013) 28–39



- Geant4 9.2p01
- Physics list is based on QGSP_BIC_HP
- Detailed 3D geometry of the setup
- Custom Gd neutron capture spectrum
- Same cuts as in the measurement, ...
⇒ Agreement within 20%

See V. Kozlov poster:
Measurement and modeling of muon-induced neutrons in LSM in application for direct Dark Matter searches



Conclusions

- MC simulations of e.m. backgrounds can reproduce the experimental data with a very high precision level.
- Radiogenic neutrons: comparison between two independent codes show results compatible inside a factor 2
- Muon-induced neutrons:
 - more experiment are doing measurements interpreted with detailed Monte Carlo simulations,
 - uncertainties still quite large, but the discrepancy is decreasing (inside a factor 2)
 - GEANT4: variations in the neutron yield modifying the code version or the physics list

Thanks !