



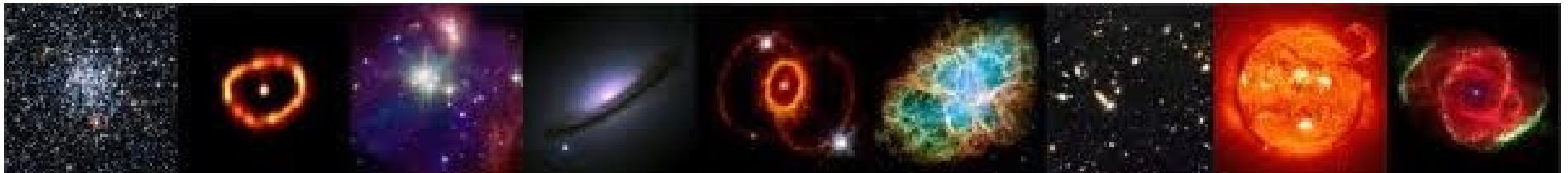
ALEXIS DIAZ-TORRES

European Centre for Theoretical
Studies in Nuclear Physics and
Related Areas

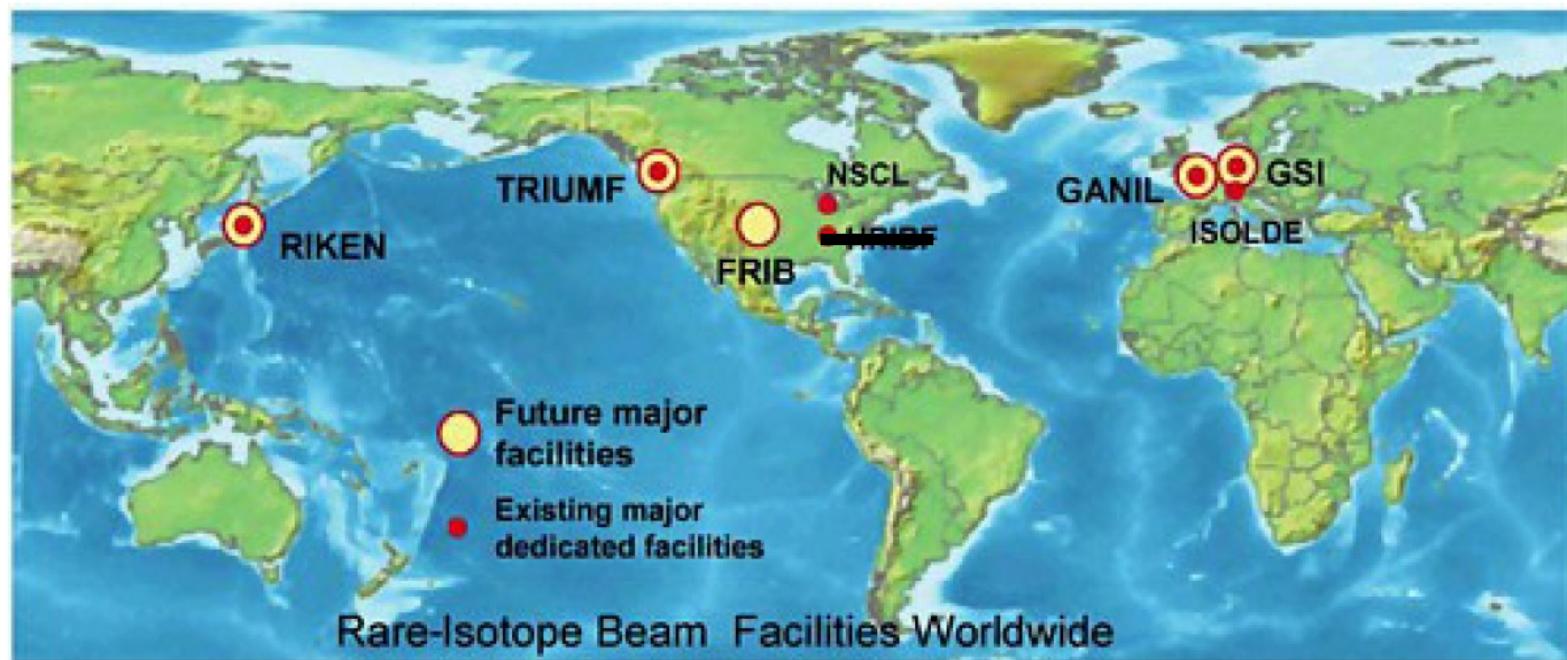


Trento, Italy

Why am I interested in the physics of nuclear reactions?



- ★ The physics of low-energy nuclear reactions is crucial for understanding energy production and nucleosynthesis in the Universe



- ★ Nuclear reactions are the primary probe of the New Physics

Quantifying low-energy fusion dynamics of weakly bound nuclei

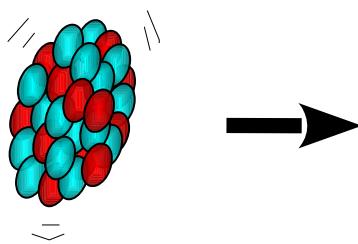
- A Time Dependent Perspective -



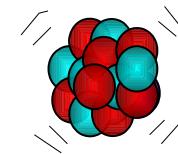
What I will tell you next

- ★ Issue & Important Concepts
- ★ Classical & Quantum Dynamical Models
- ★ Summary & Outlook

What's the issue I'd like to understand and quantify?



Relative motion

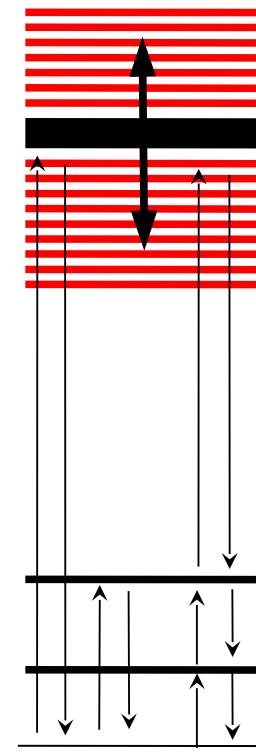


SCALES

Energy: MeV = 10^6 eV

Length: fm = 10^{-15} m

Collision Time: 10^{-20} - 10^{-22} s

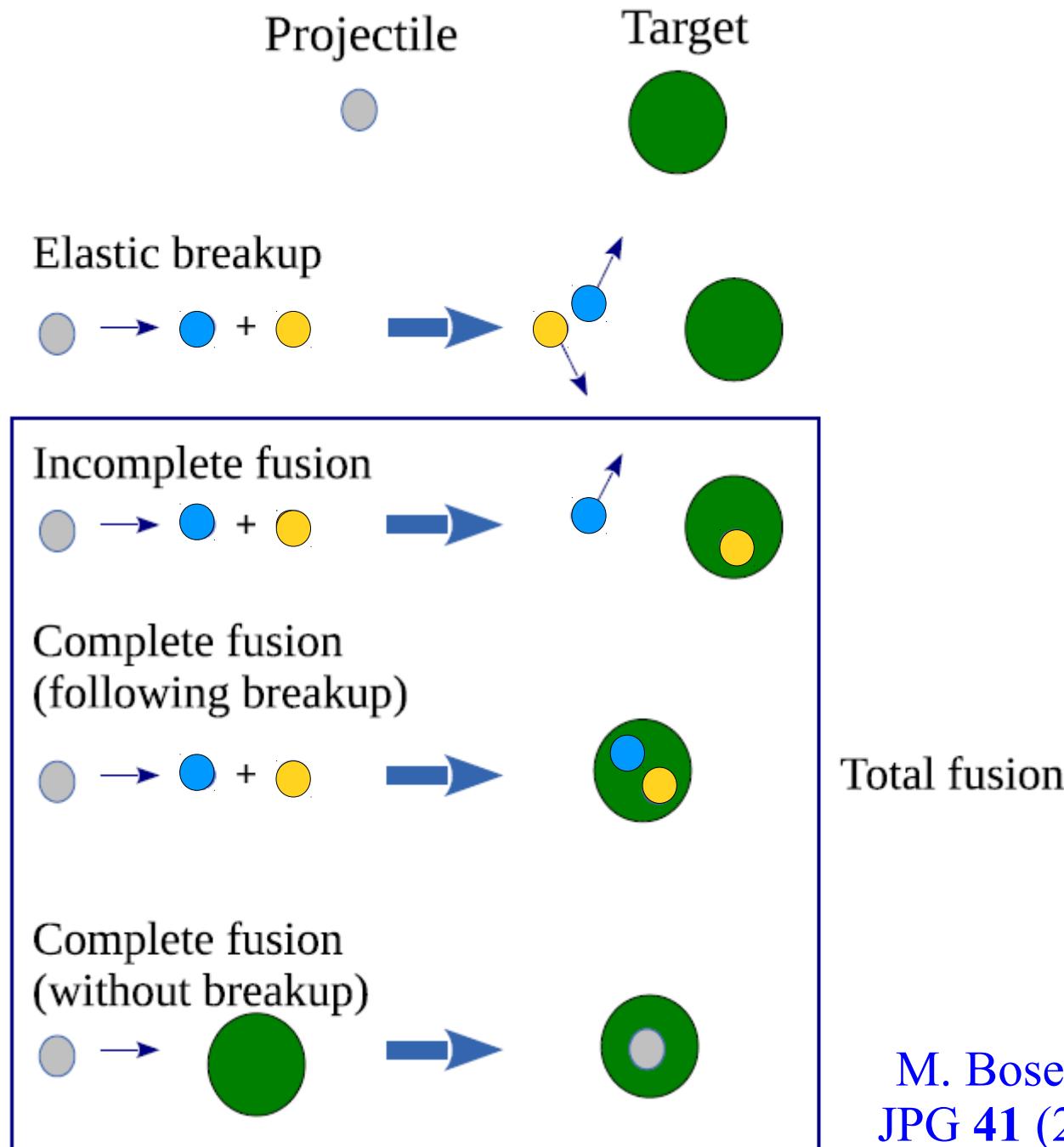


|3>
| I_k >
|2>
|1>
|0>

Intrinsic
quantum states

Strong interplay of nuclear structure and reaction dynamics
determines reaction outcomes (cross sections)

Unified description of low-energy reaction processes?



Some examples of low-energy models in the last 15 years

Classical

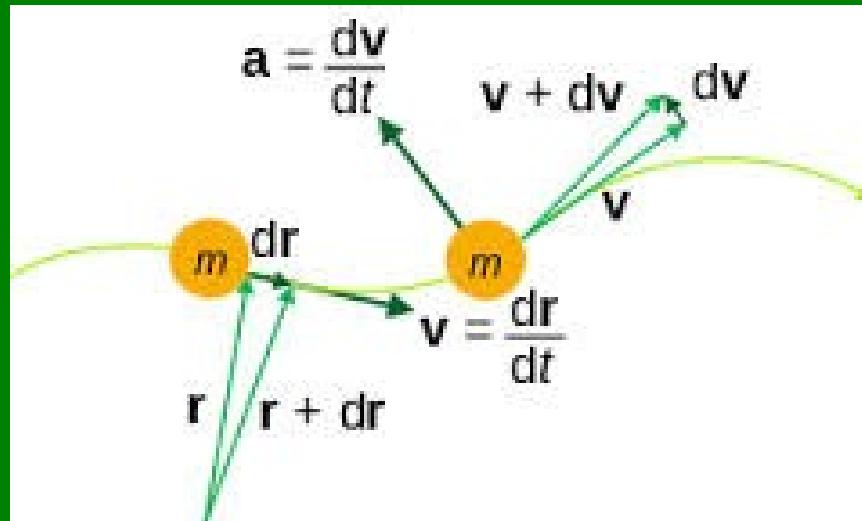
AD-T, Hinde, Tostevin, Dasgupta & Gasques, PRL **98** (2007) 152701
Hagino, Dasgupta & Hinde, NPA **738** (2004) 475c

Mixed Quantum-Classical

Marta, Canto & Donangelo, PRC **89** (2014) 034625; PRC **73** (2005) 034608
Baye, Capel & Melezlik, NPA **722** (2003) 328c
Esbensen & Bertsch, NPA **706** (2002) 383
Yokimoto, Typel *et al.*, PRC **63** (2001) 035801

Quantum Mechanical

Descouvemont, Druet, Canto & Hussein, PRC **91** (2015) 024606
Lubian, Correa, Canto, Gomez-Camacho, Gomes *et al.*, PRC **79** (2009) 285
Rodriguez-Gallardo, Moro *et al.*, PRC **80** (2009) 051601
Ito, Yabana, Nakatsukasa & Ueda, PLB **637** (2006) 53
AD-T, Thompson & Beck, PRC **68** (2003) 044607; PRC **65** (2002) 024606
Tostevin, Nunes & Thompson, PRC **63** (2001) 024617
Hagino, Vitturi, Dasso & Lenzi, PRC **61** (2000) 037602



Classical Trajectory Monte Carlo Method

- After breakup, interaction among fragments is crucial
- Useful for interpreting particle-gamma coincidence data
- Breakup triggered by transfer enriches the fusion scenario

See e.g., R. E. Olson, CTMC techniques, in Springer Handbook of Atomic, Molecular & Optical Physics (2006) pp. 869-874

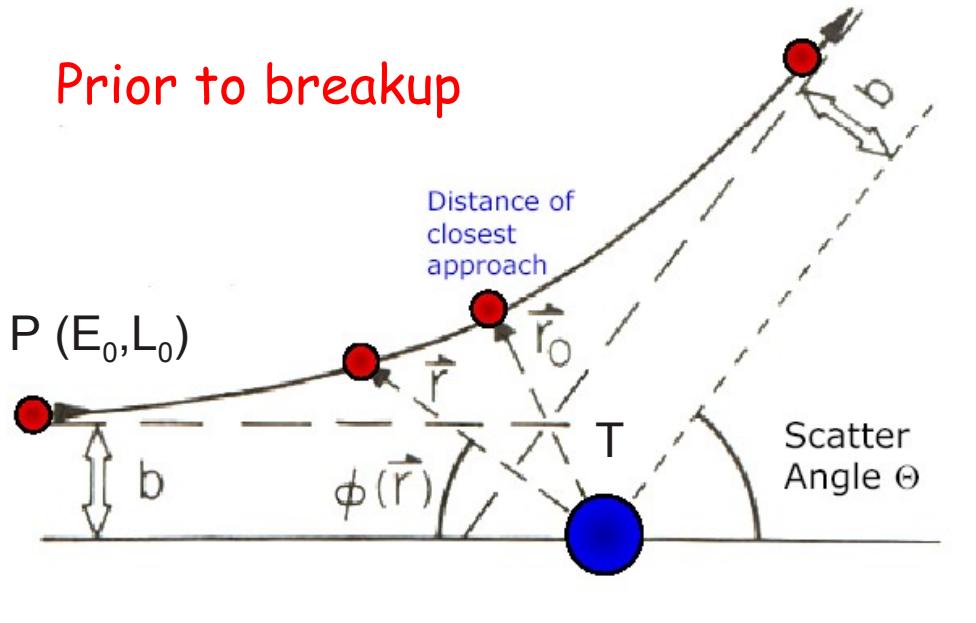
Classical Dynamical Model

AD-T, Hinde, Tostevin, Dasgupta & Gasques, PRL 98 (2007) 152701

AD-T, CPC 182 (2011) 1100 (PLATYPUS code)

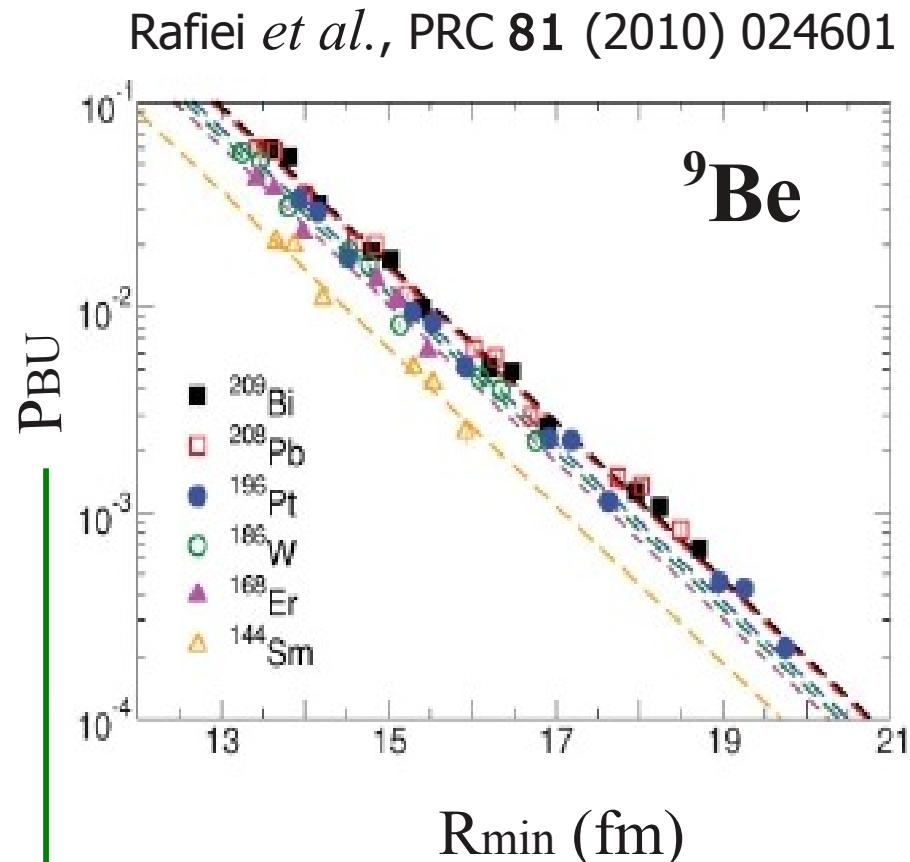


Prior to breakup



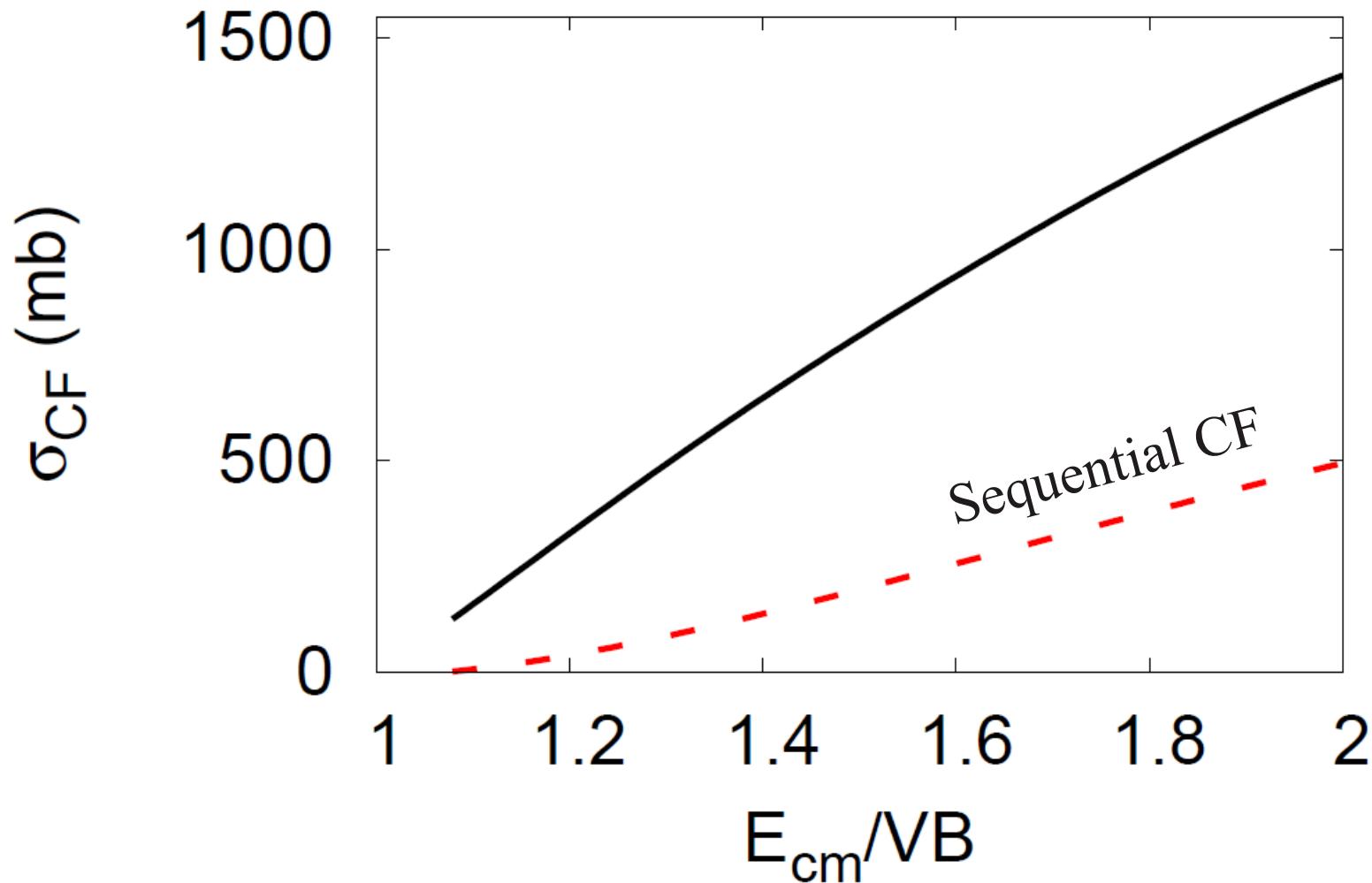
Main Ingredient :

$P_{BU}^L(R)dR$ probability of breakup
on the interval $R + dR$



$$P_{BU}(R_{min}) = 2 \int_{R_{min}}^{\infty} P_{BU}^L(R) dR = A \exp(-\alpha R_{min})$$

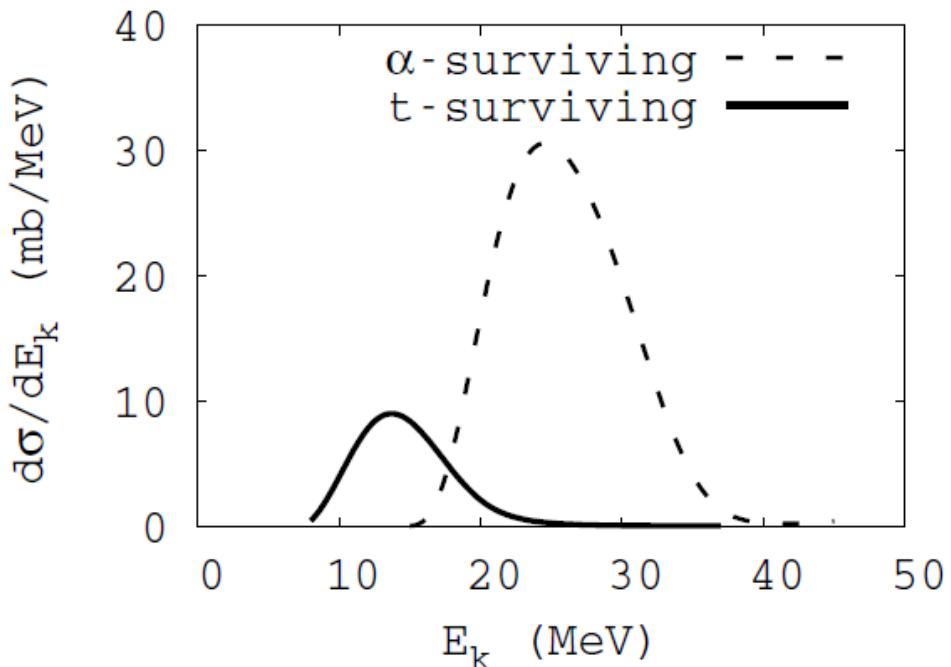
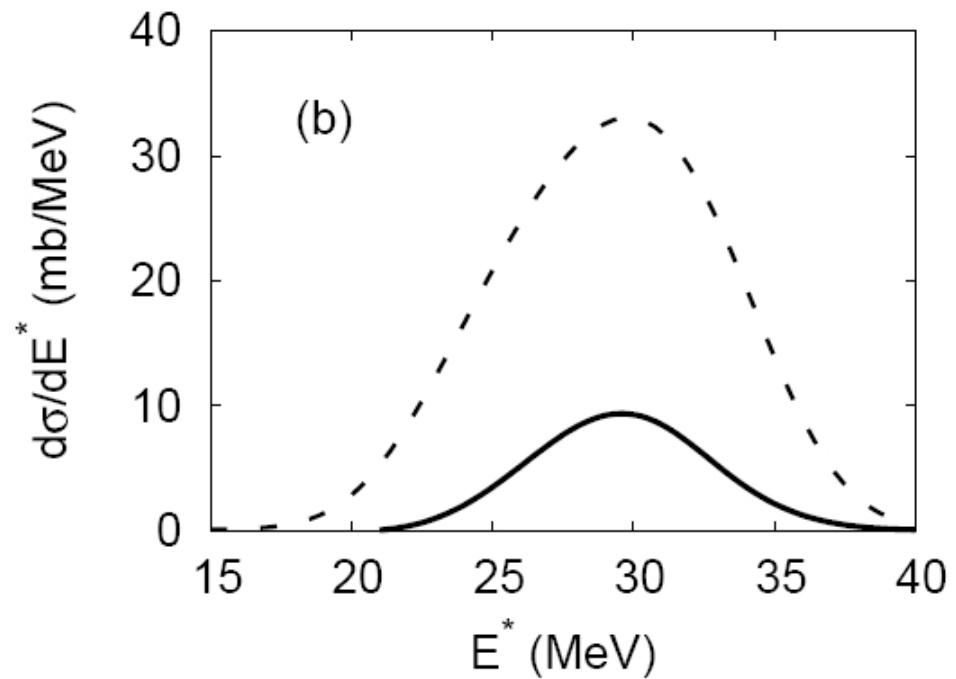
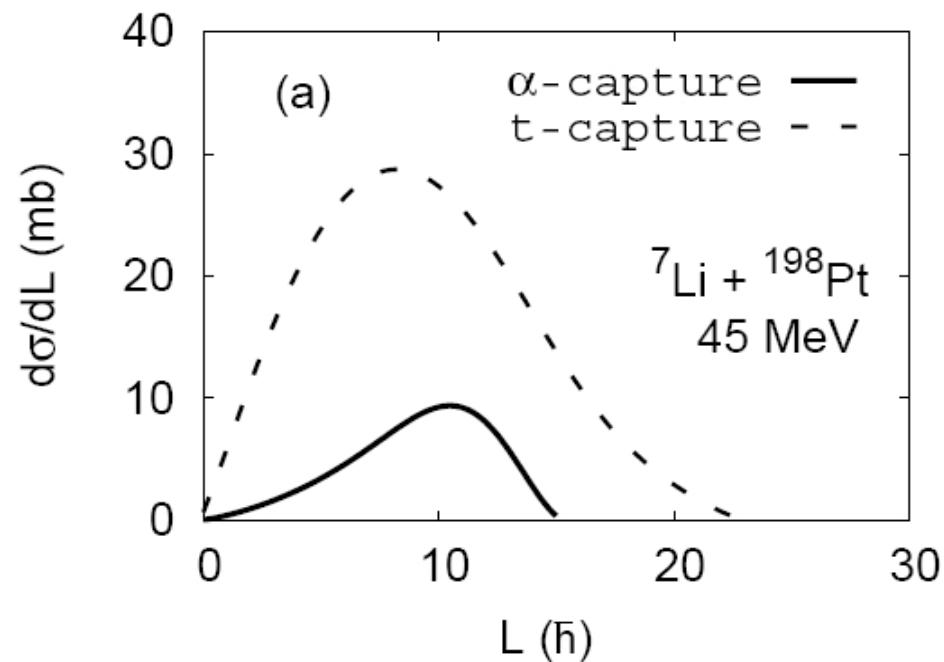
Complete fusion of ${}^7\text{Li} + {}^{198}\text{Pt}$ at above-barrier energy



Sequential CF becomes substantial as energy increases

See e.g., Dasgupta *et al.*, PRC **66** (2002) 041602 (R), for ${}^6,{}^7\text{Li} + {}^{209}\text{Bi}$

Incomplete fusion of ${}^7\text{Li} + {}^{198}\text{Pt}$ at above-barrier energy

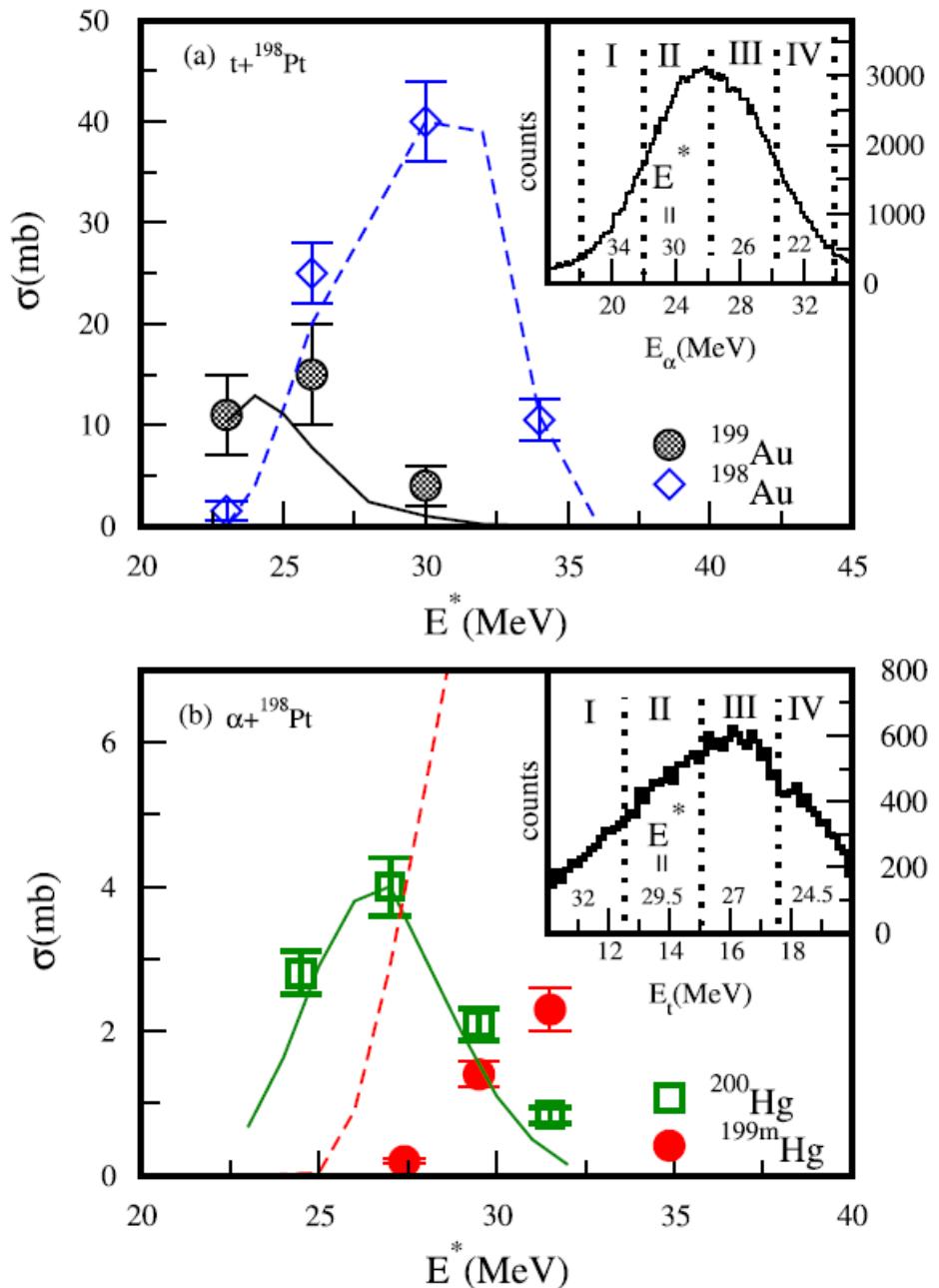


PLATYPUS code

AD-T, CPC 182 (2011) 1100

Useful for planning & interpreting
particle-gamma-coincidence
measurements

Incomplete fusion measurements vs. **Platypus+PACE** calculations: E* and spin distribution from **Platypus** fed to evaporation code **PACE**



$^7\text{Li} + ^{198}\text{Pt}$ @ 45 MeV

triton - fusion

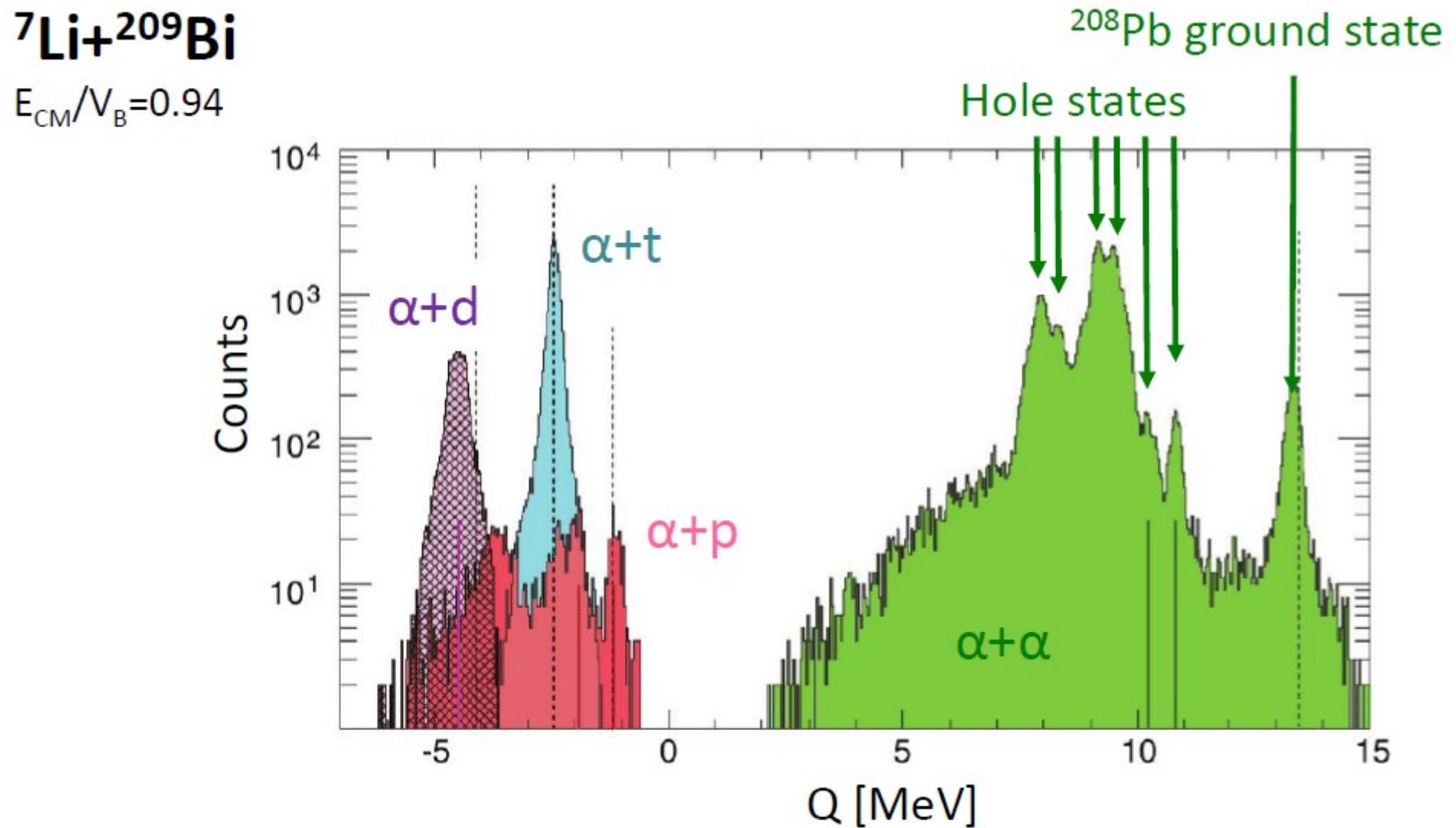
α gated γ spectra
 $t + ^{198}\text{Pt} : ^{201}\text{Au}^*$

α - fusion

t gated γ spectra
 $\alpha + ^{198}\text{Pt} : ^{202}\text{Hg}^*$

Shrivastava, Navin, AD-T *et al.*,
PLB 718 (2013) 931

Q-value spectrum in sub-barrier breakup of ${}^7\text{Li}$ on ${}^{209}\text{Bi}$



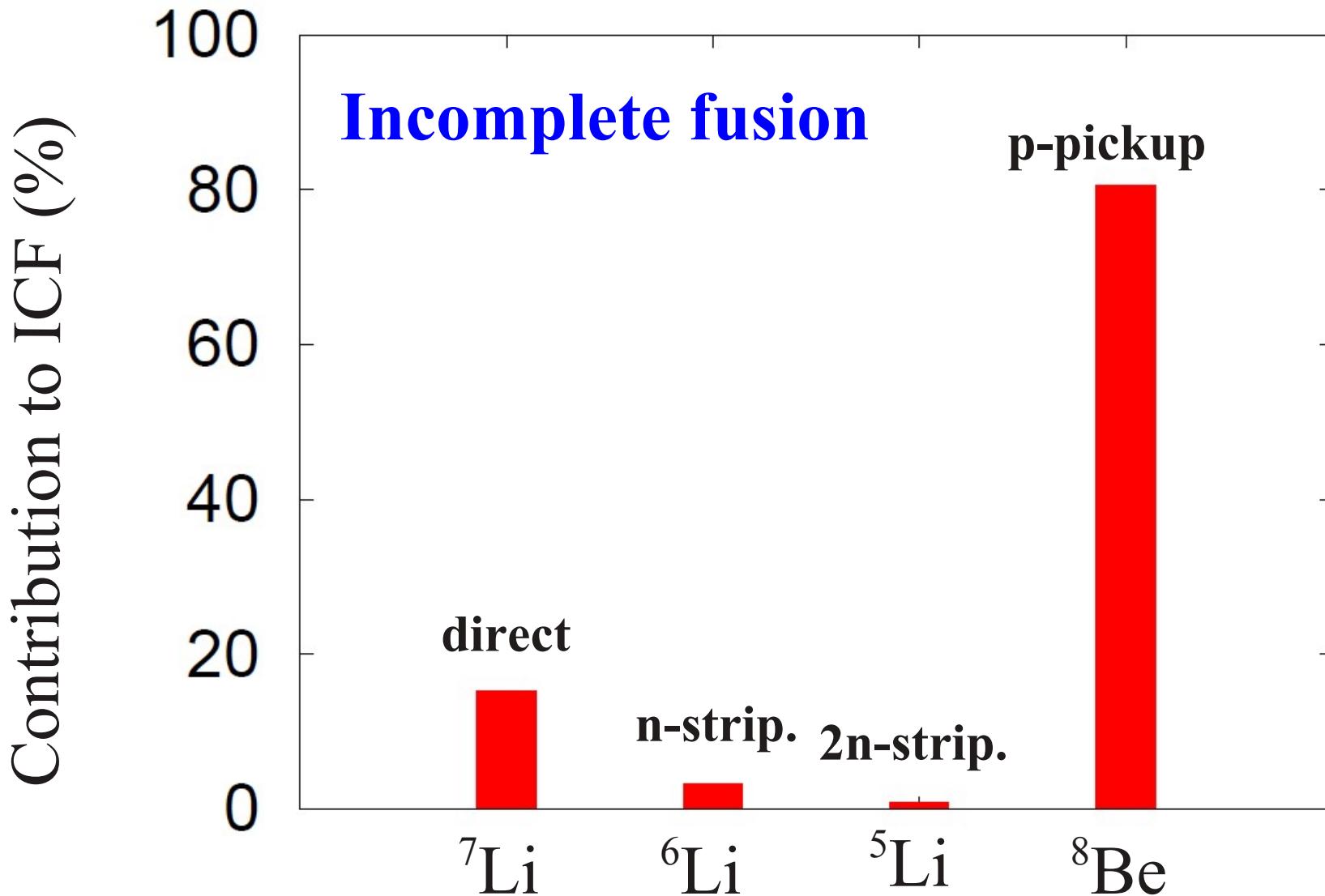
Luong *et al.*, Phys. Rev. C 88, 034609 (2013)

Courtesy of Ed Simpson (ANU)

Breakup triggered by transfer affects above-barrier fusion

Example: ${}^7\text{Li} + {}^{209}\text{Bi}$ @ Ecm/VB = 1.2

PRELIMINARY RESULTS FROM PLATYPUS



In collaboration with H. Luong



Time-Dependent Wave-Packet Dynamics

Useful for understanding sub-Coulomb fusion data

In collaboration with Maddalena Boselli,
PhD student at the ECT*



Time-Dependent Wave-Packet Dynamics

D.J. Tannor, *Quantum Mechanics in a Time-Dependent Perspective*, USB, 2007

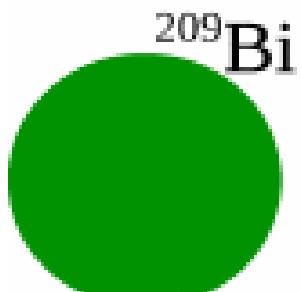
Yabana, Prog. Theor. Phys. **97** (1997) 437

Schneider & Wolter, Z. Phys. A **339** (1991) 177

- **Preparation** of the initial state $\Psi(t = 0)$.
- **Time propagation**, $\Psi(0) \rightarrow \Psi(t)$, guided by the evolution operator, $\exp(-i \hat{H} t/\hbar)$, where \hat{H} is the total Hamiltonian.
- **Analysis:** calculation of **cross sections** from the time-dependent wave function.

One-Dimensional Toy Model

TARGET



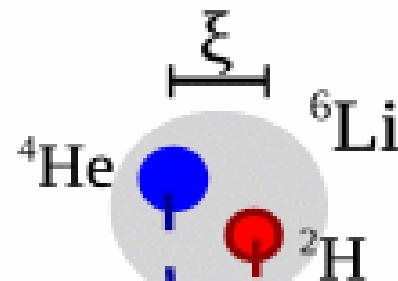
10

x GM

2

x

PROJECTILE



1

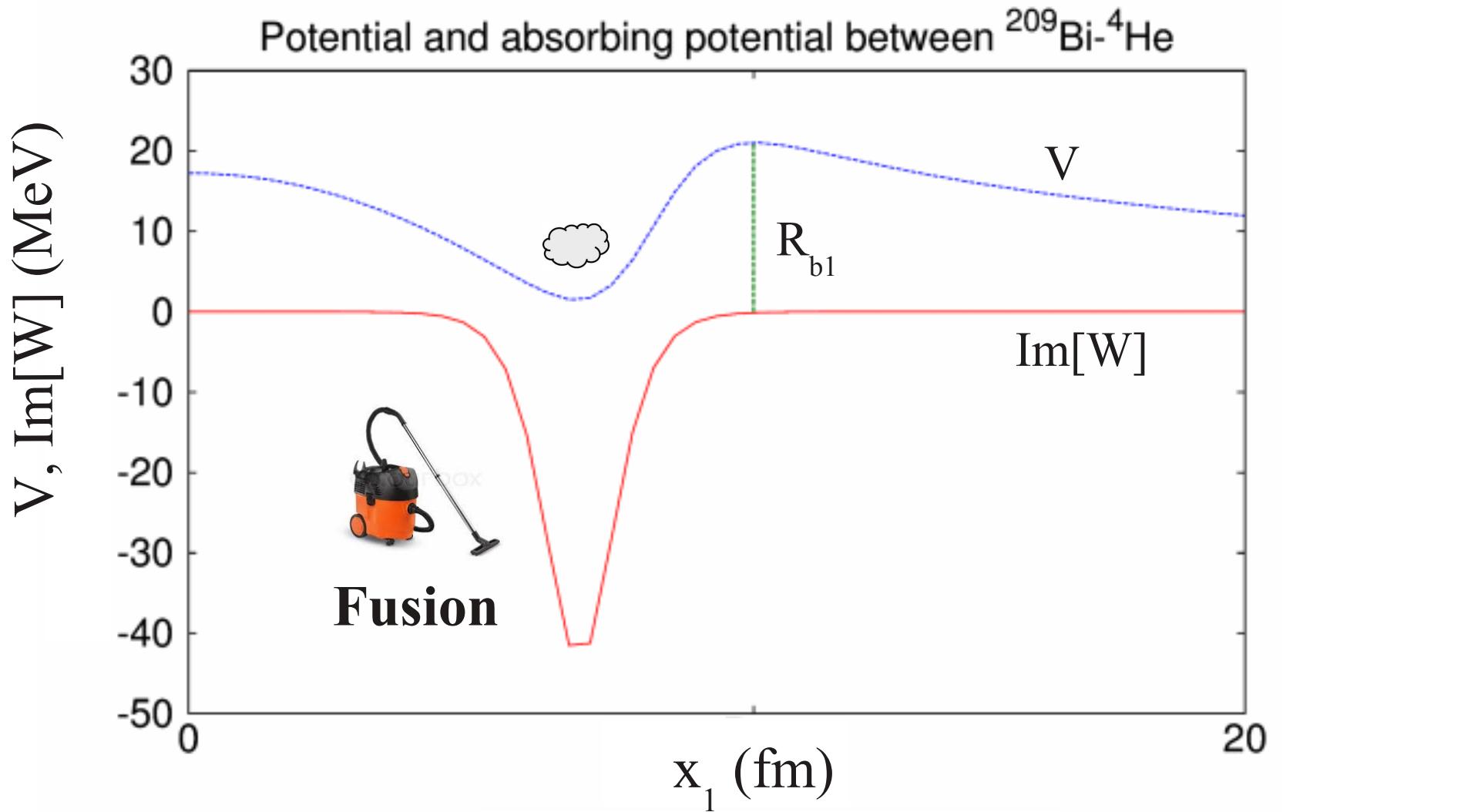
$$x_2 = x_{CM} + b \xi$$

$$x_1 = x_{CM} - a \xi$$

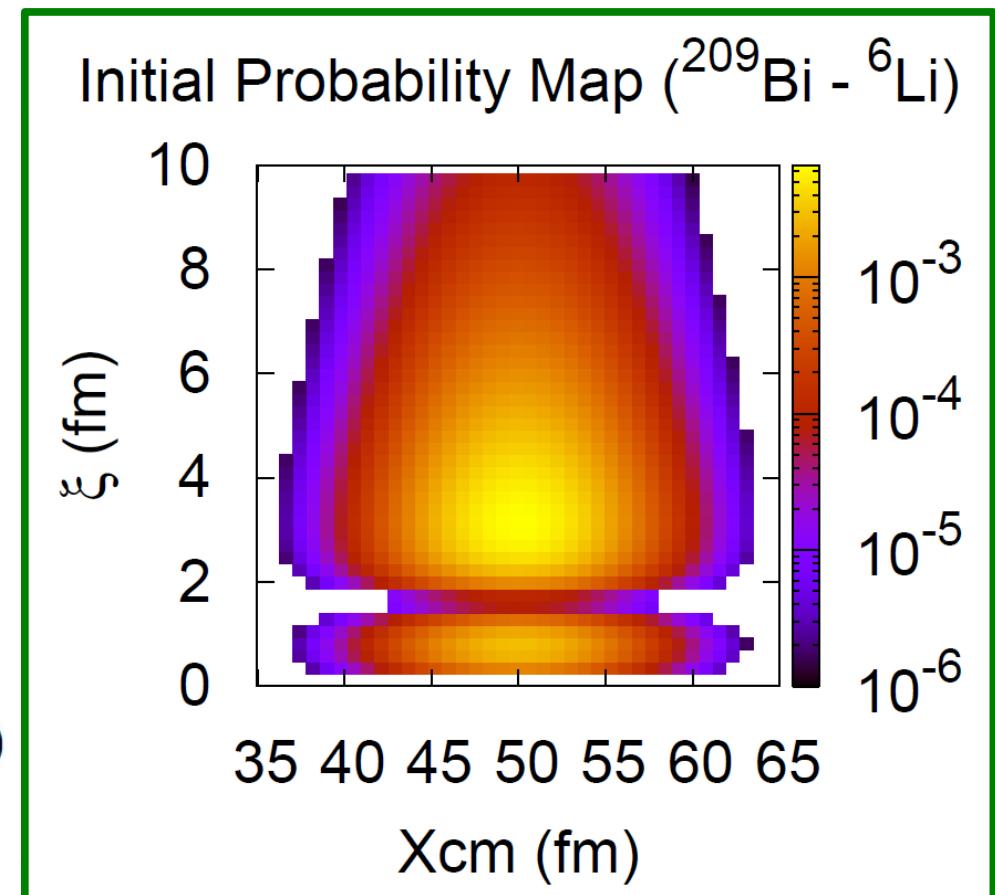
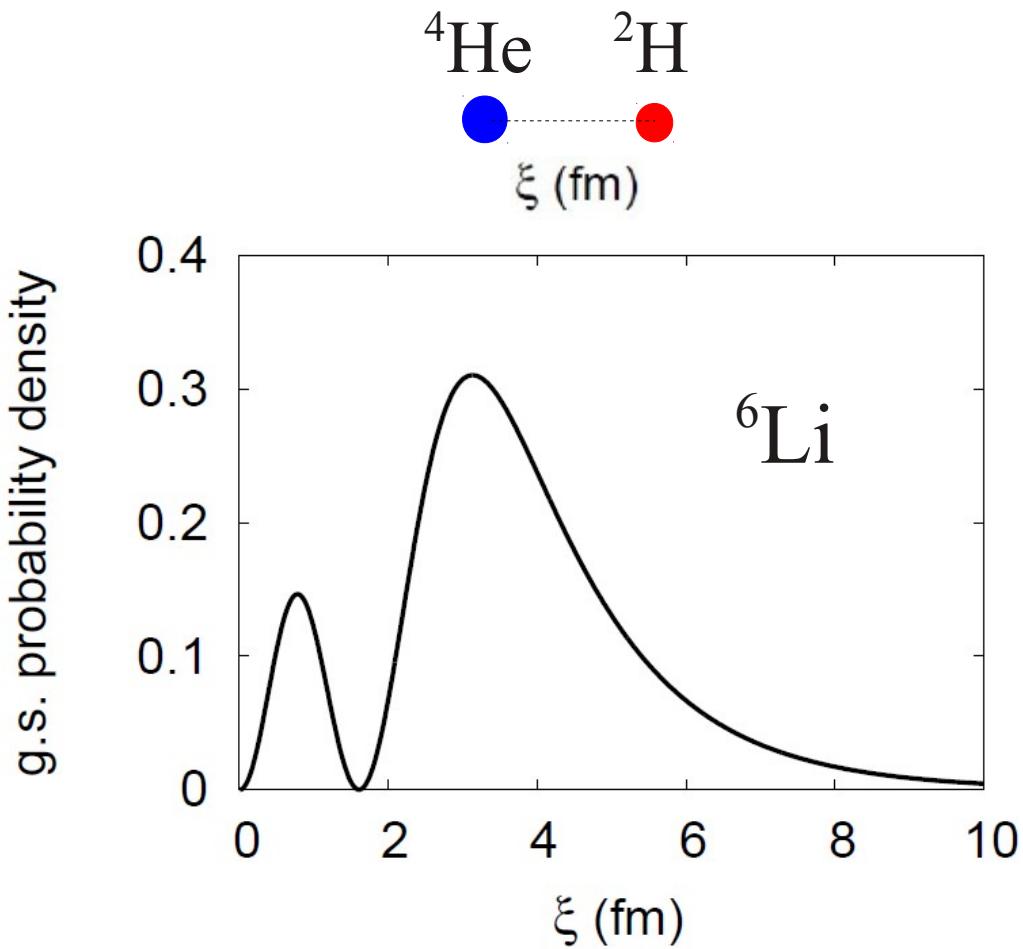
$$H = \frac{P_{x_{CM}}^2}{2M_{T12}} + \frac{P_\xi^2}{2m_{12}} + U_{12}(\xi) + V_{T1}(x_{CM} - a\xi) + V_{T2}(x_{CM} + b\xi)$$

Describing Fusion

- ◆ To simulate fusion (**irreversibility**):
acting inside the Coulomb barrier $-iW_{T1}(x_1)$ & $-iW_{T2}(x_2)$



Preparing the Initial State



Time Propagation

R. Kosloff, Ann. Rev. Phys. Chem. **45** (1994) 145

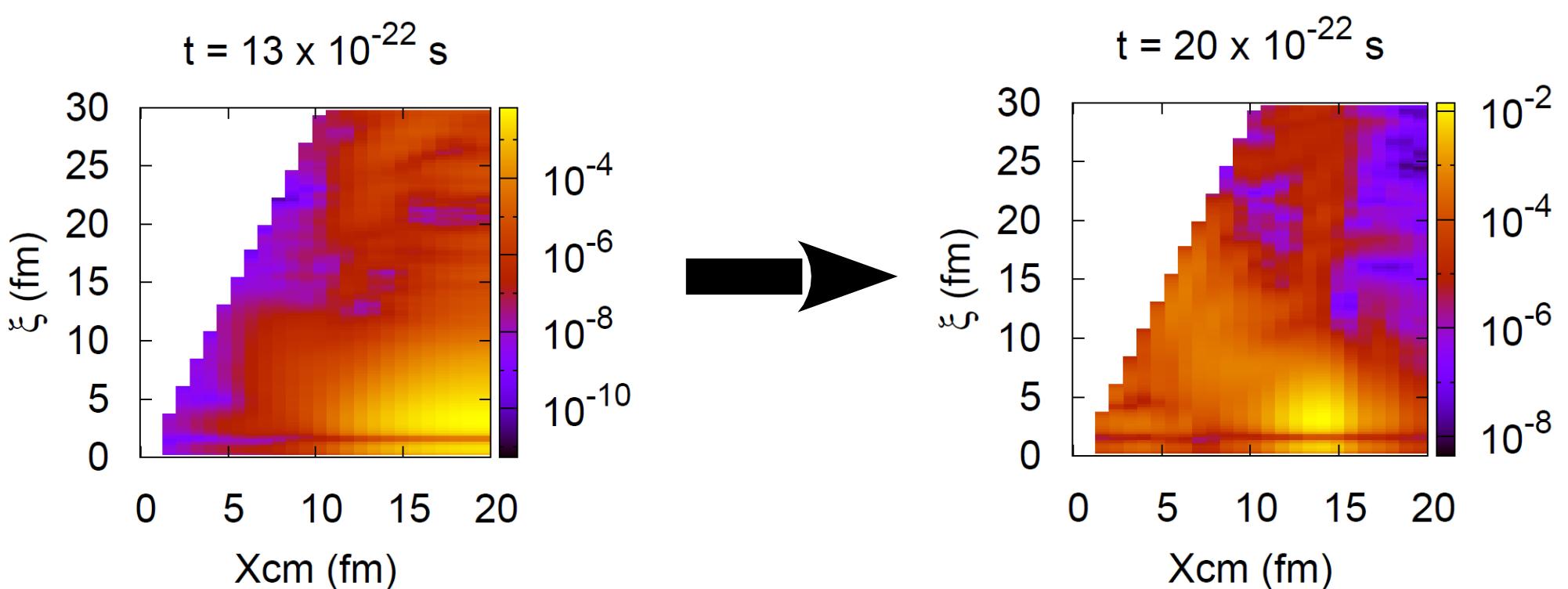
$$\Psi(t + \Delta t) = \exp\left(-i\frac{\hat{H} \Delta t}{\hbar}\right) \Psi(t)$$

$$\exp\left(-i\frac{\hat{H} \Delta t}{\hbar}\right) \approx \sum_n a_n Q_n(\hat{H}_{norm})$$

$$\hat{H}_{norm} = \frac{(\bar{H} \hat{1} - \hat{H})}{\Delta H}$$

The Chebyshev Propagator

$$a_n = i^n (2 - \delta_{n0}) \exp\left(-i\frac{\bar{H} \Delta t}{\hbar}\right) J_n\left(\frac{\Delta H \Delta t}{\hbar}\right)$$



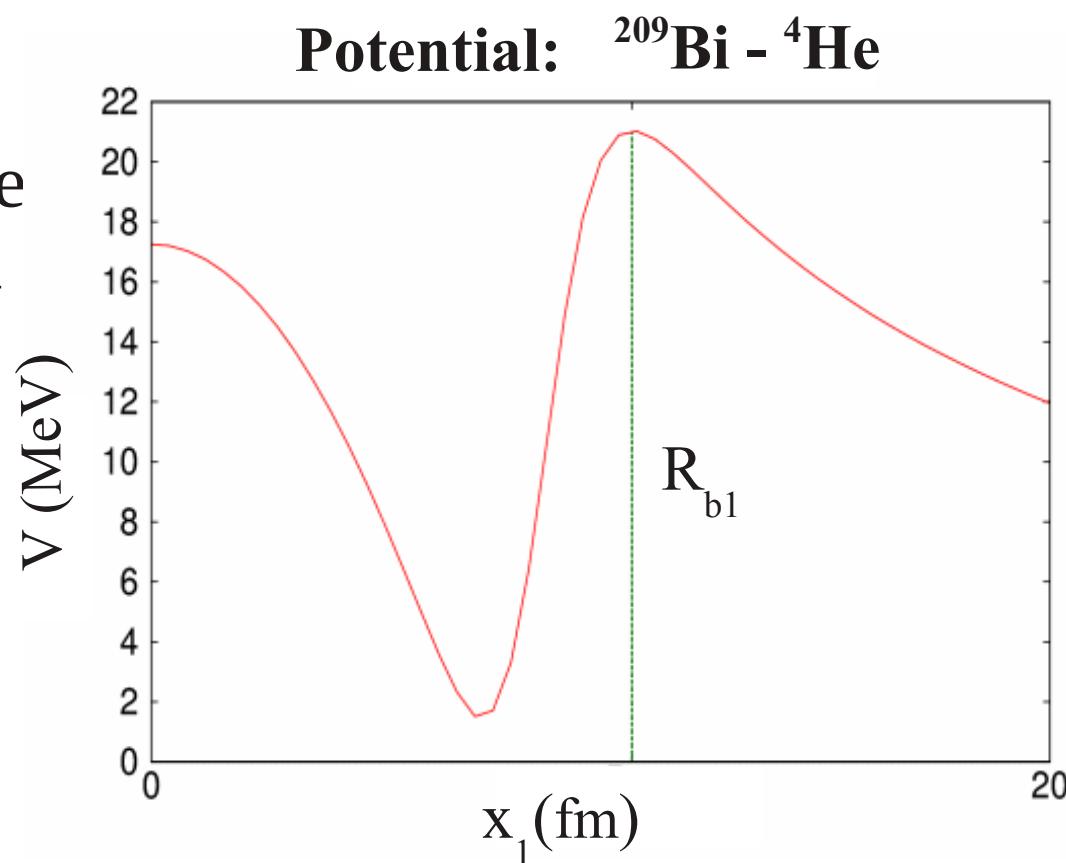
Slicing the Wave Function: A Novel Idea

- ◆ Projection operator acting on the position x_i of the fragment relative to the target
(Heaviside function)

$$P_i = \Theta(R_{bi} - x_i)$$
$$Q_i = 1 - P_i$$



- ◆ Act with $(P_1+Q_1)(P_2+Q_2)=1$ on the wave function:



	CAPTURED	NON CAPTURED
CF	● ●	
ICF	●	●

$$\tilde{\Psi}(x_1, x_2, t) = (P_1 P_2 + P_1 Q_2 + Q_1 P_2 + Q_1 Q_2) \tilde{\Psi}(x_1, x_2, t) = \Psi_{CF} + \Psi_{ICF} + \Psi_{SCATT}$$

Below the equation, there are three horizontal bars: a red bar, a blue bar, and a green bar, representing the different components of the wave function.

Analysis of the Wave Function

Power Spectrum of the Wave Function

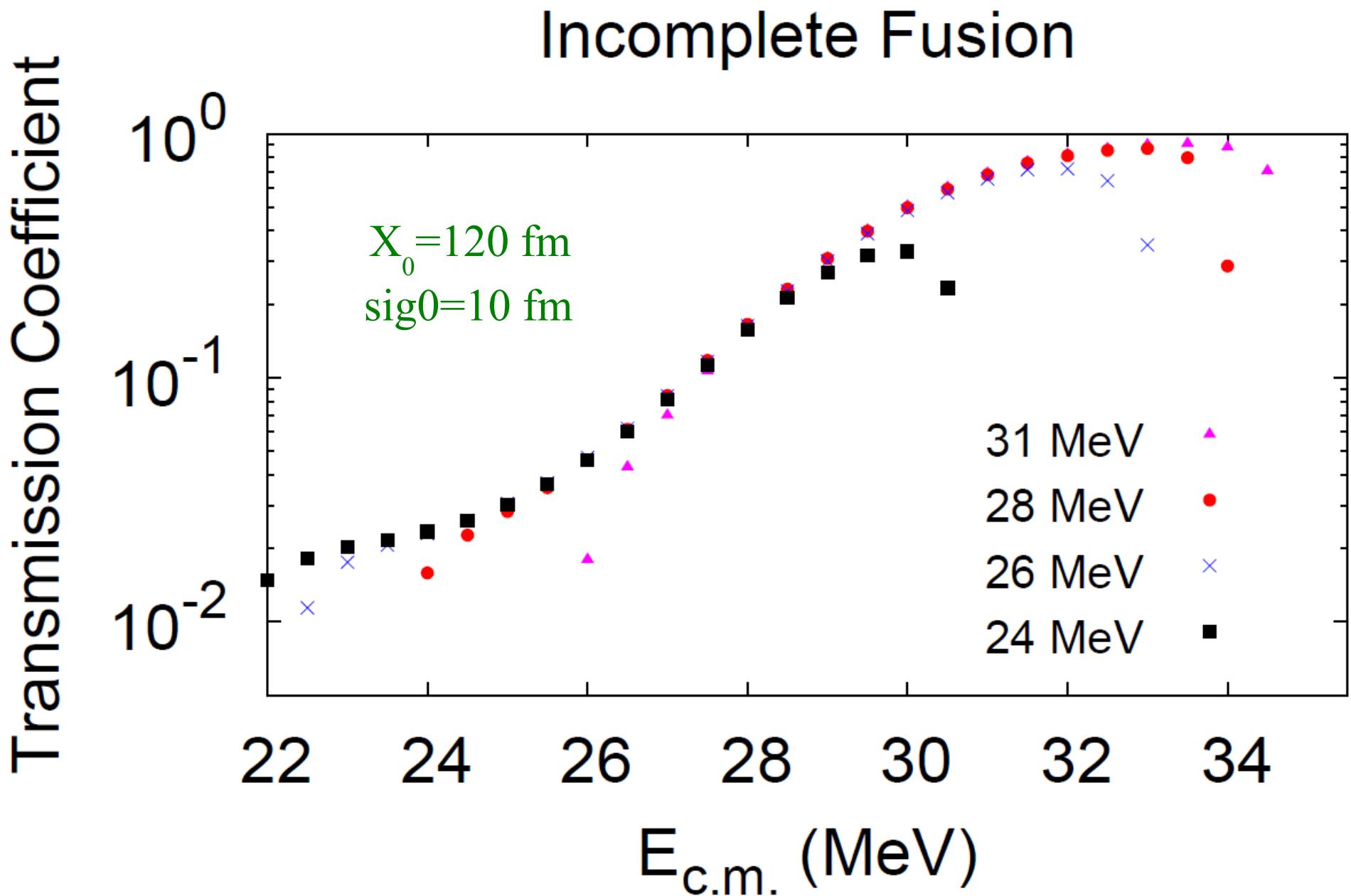
$$\mathcal{P}(E) = \langle \Psi(t) | \underbrace{\delta(E - \hat{H})}_{\text{Energy Projector}} | \Psi(t) \rangle$$

Reflection & Transmission Coefficients

$$\mathcal{R}(E) = \frac{\mathcal{P}^{final}(E)}{\mathcal{P}^{initial}(E)}$$

$$T(E) = 1 - \mathcal{R}(E)$$

Example





Summary

- ★ **The time-dependent perspective** is useful for understanding and quantifying low-energy reaction dynamics of exotic nuclei.
- ★ **PLATYPUS** is a powerful tool for planning and interpreting (fusion & breakup) measurements, which allow its fine tuning.



AD-T, CPC **182** (2011) 1100

Outlook

- ★ A **quantum dynamical 3D-model** is being developed.

Maddalena Boselli & AD-T, JPG **41** (2014) 094001



Understanding the breakup mechanisms and their impact on unambiguously separated CF & ICF processes could make for further progress in the field.