

Does monopole pigmy resonance exist in ^{68}Ni ?

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NN1015

June 22-26, 2015 at Catania Italy



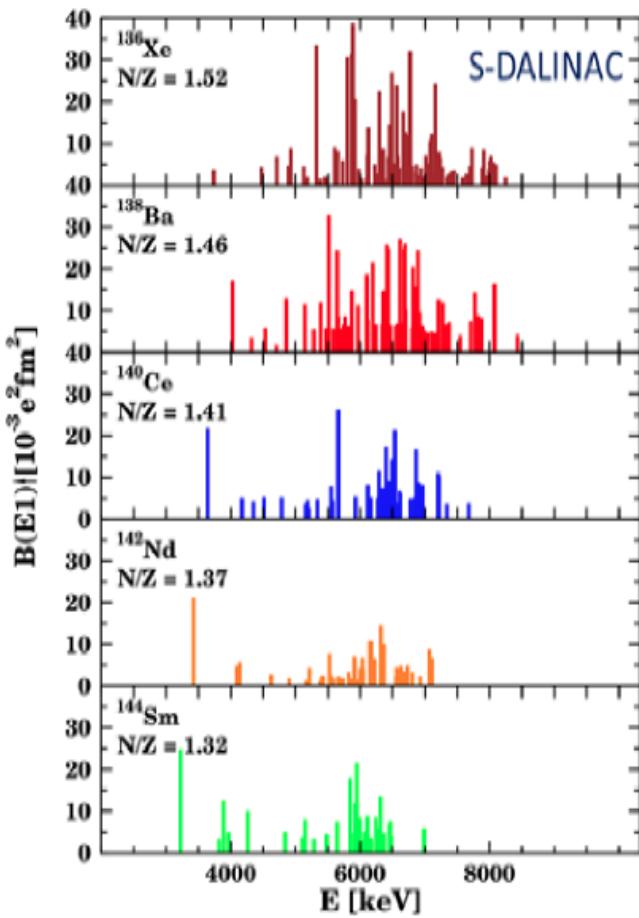
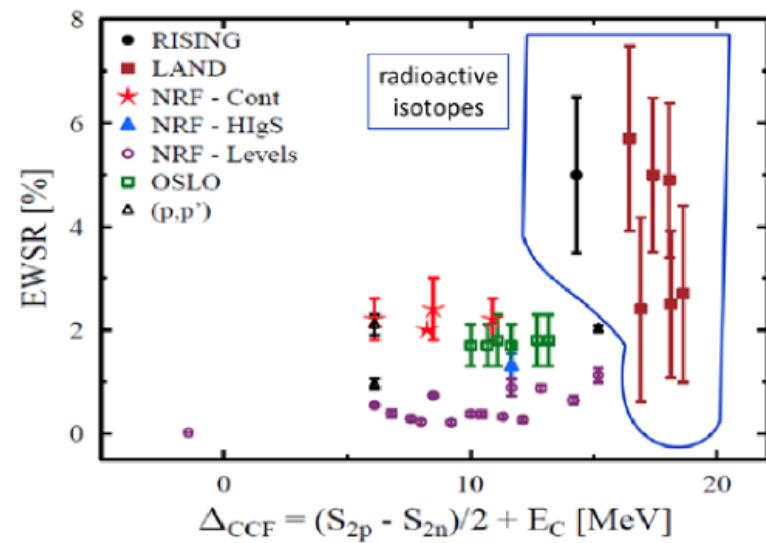


Figure 1: E1 strength distribution observed in discrete transitions to the groundstate in the stable even-even N=82 isotones (adapted from Refs. 14 and 15).

Low-energy dipole strengths may increase radiative neutron capture cross section and affect strongly r-process nucleosynthesis.

Pigmy dipole strength observed at much lower energy than IVGDR (Ex \sim 15MeV)

Pigmy dipole strength is increased in neutron-rich nuclei.
oscillation between neutron skin and core?



Measurement of the isoscalar monopole response in the neutron-rich nucleus ^{68}Ni

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PRL113, 032504(2014)

alpha scattering at 50A MeV in inverse kinematics with the active target MAYA at GANIL

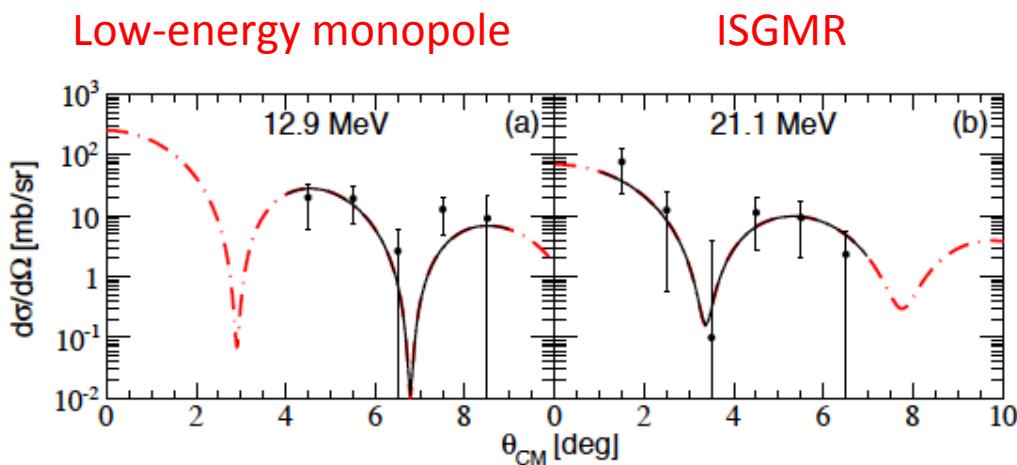
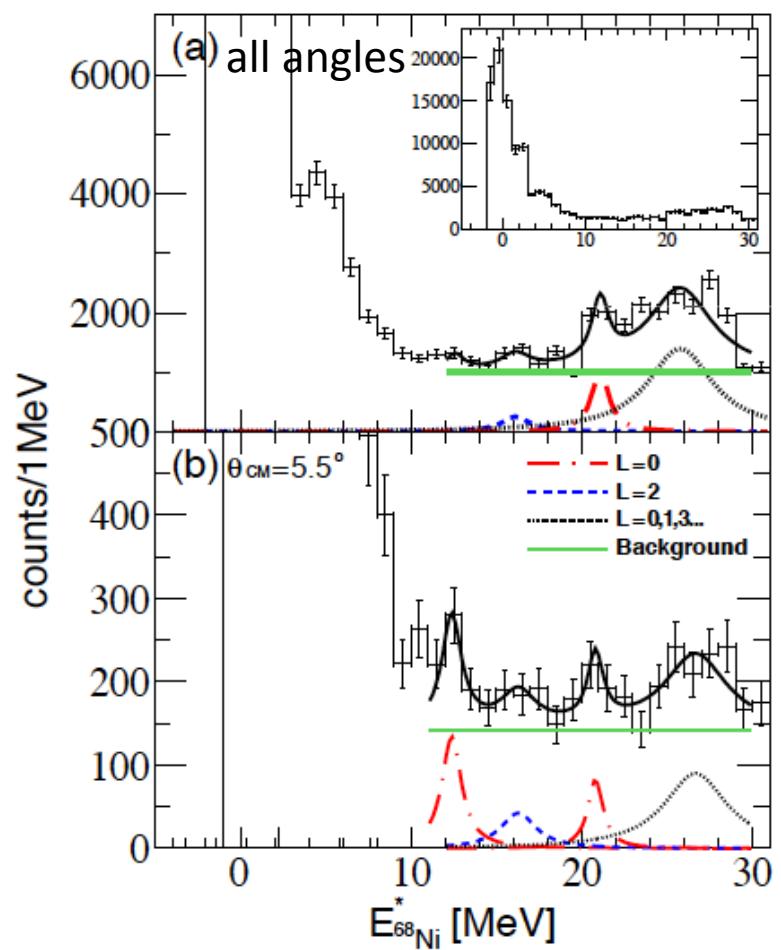


FIG. 3. (Color online) Angular distributions for the modes located at 12.9 MeV (a) and 21.1 MeV (b). The black solid line corresponds to the fit based on DWBA calculation using microscopic RPA predictions with isoscalar $L = 0$ multipolarity. These predictions are represented in red dot-dashed line.

Continuum coupling is properly accommodated in the response function (coordinate space solutions)

Unperturbed Green's function

$$G^{(0)}(\vec{r}, \vec{r}'; \omega) = \sum_{i \in \text{occupied}} \varphi_i^*(\vec{r}) \left\langle \vec{r} \left| \frac{1}{\omega + i\eta - h_0 + \varepsilon_i} - \frac{1}{\omega - i\eta + h_0 + \varepsilon_i} \right| \vec{r}' \right\rangle \varphi_i(\vec{r}')$$

where $\varphi_i(\vec{r})$ and ε_i are the HF single particle wave function and energy

$$h_0 \varphi_i(\vec{r}) = \varepsilon_i \varphi_i(\vec{r})$$

RPA Green's function is given by

$$G^{\text{RPA}} = G^{(0)} + G^{(0)} \frac{\delta v}{\delta \rho} G^{\text{RPA}} = (1 - G^{(0)} \frac{\delta v}{\delta \rho})^{-1} G^{(0)}$$

Strength function

$$S(E) = \sum_n \left| \left\langle n | f(\vec{r}) | 0 \right\rangle \right|^2 \delta(E_n - E_0 - E)$$

$$= \frac{1}{\pi} \int d\vec{r}_1 \int d\vec{r}_2 f^*(\vec{r}_1) \text{Im}\{G(\vec{r}_1, \vec{r}_2; \omega)\} f(\vec{r}_2)$$

$$f(r) = \frac{1}{\sqrt{4\pi}} \sum_i r_i^2 \text{ for isoscalar monopole strength.}$$

The inverse operator equation can be solved as

$$\left\langle \vec{r} \left| \frac{1}{h_0 - \varepsilon_i \pm \omega - i\eta} \right| \vec{r}' \right\rangle = \sum_{lm} Y_{lm}^*(\hat{r}, \sigma) Y_{lm}(\hat{r}', \sigma) g_{lj}(r, r')$$

where

$$g_{lj}(r, r') = -\frac{2m^*(r)}{\hbar^2} \frac{1}{W(u, v)} u(r_<)v(r_>) \quad \begin{cases} r_< = r, r_> = r' \text{ if } r < r' \\ r_< = r', r_> = r \text{ if } r \geq r' \end{cases}$$

and

$$(h_0 - \varepsilon_i \pm \omega) \begin{pmatrix} u \\ v \end{pmatrix} = 0$$

where u (v) is the regular (irregular) solution at the origin and u (v) behaves like a standing (outgoing) wave at infinity.

Continuum coupling is properly accommodated in the response function (coordinate space solutions)

Questions and Answers

1) Sharp resonance with the width of 1MeV exists for the monopole response near the threshold?

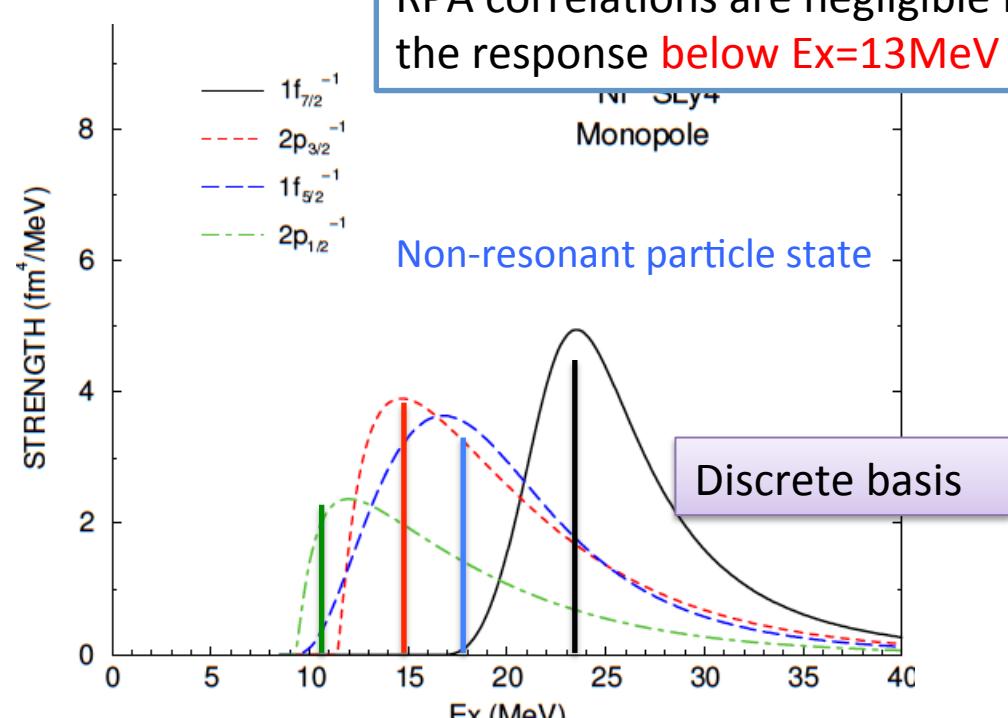
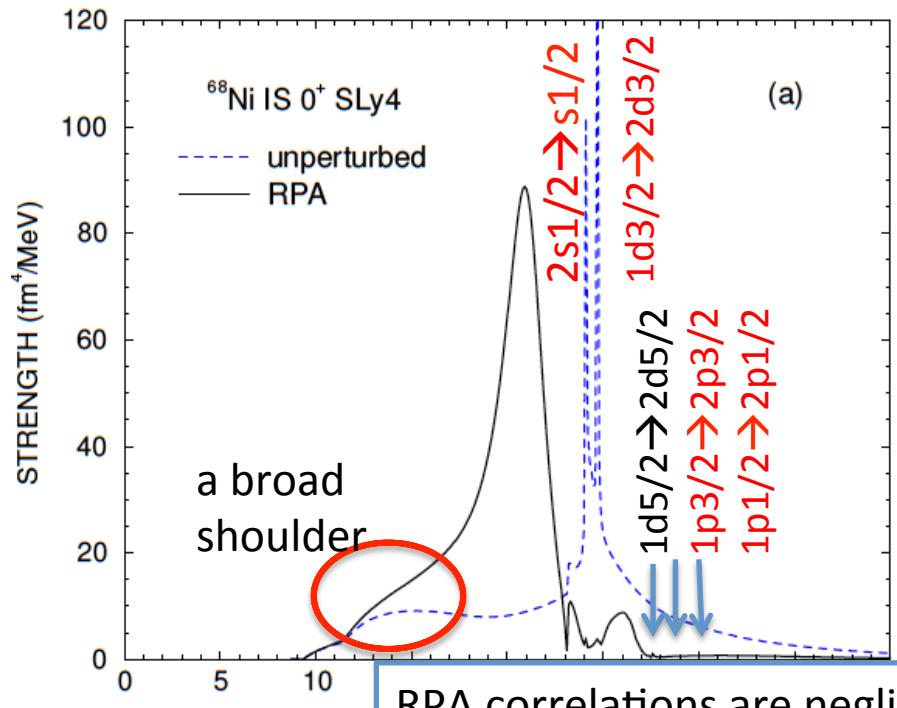
The answer is **NO!**

2) Spin-orbit splitting of the states near the threshold will be disappeared ?
(E. Yuksel et al., Eur. Phys. J. A49, 124(2013))

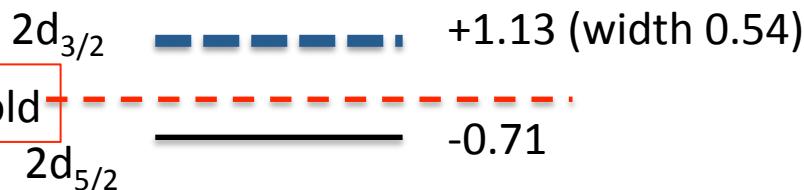
The answer is **NO!**

3) Threshold strength proportional to $(E-E_{\text{threshold}})^{l+1/2}$ appears in neutron-rich nuclei.

The answer is **YES!**

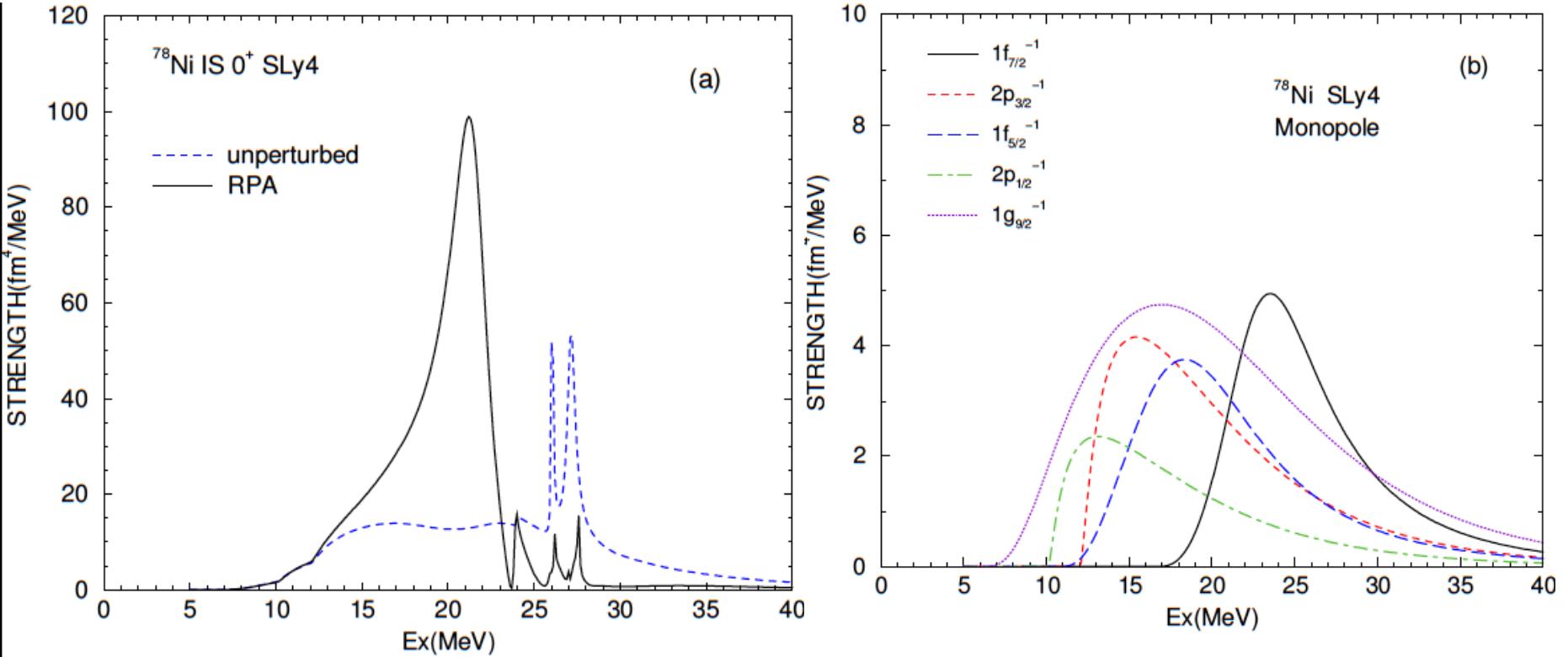


Red: proton p-h configuration
 Black: neutron p-h configuration
 There is no unperturbed p-h states **below** $\text{Ex}=20\text{MeV}$, in which particle is either a bound or resonant state

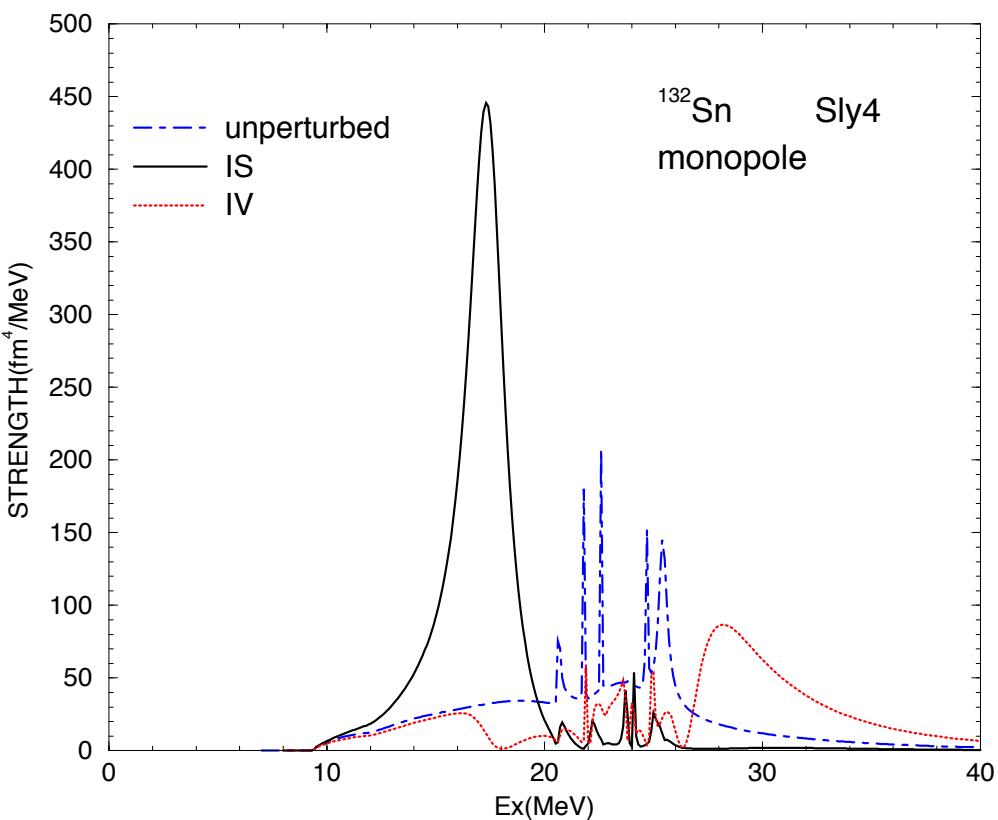


$1f_{5/2}$	-8.92 (exp.-7.79)
$2p_{1/2}$	-9.25
$2p_{3/2}$	-11.39
$1f_{7/2}$	-16.45

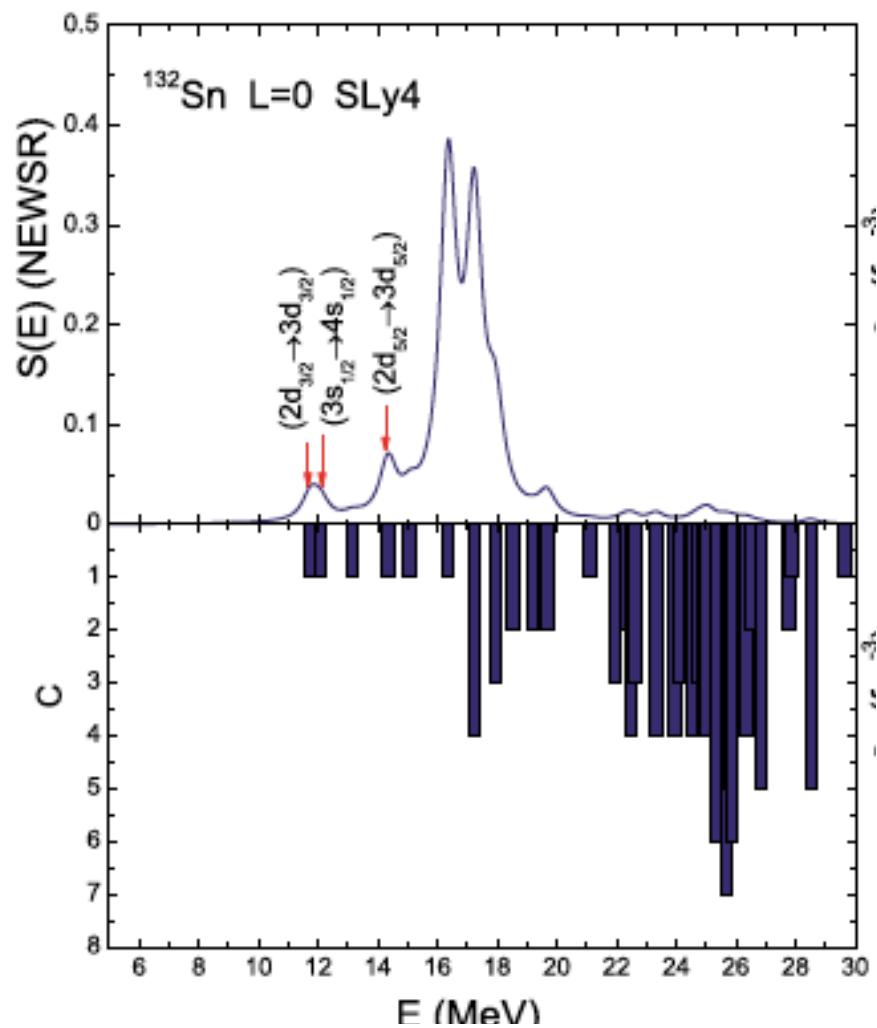
^{68}Ni neutrons



The continuum response of ^{78}Ni is the same as ^{68}Ni ,
except $1g_{9/2} \rightarrow$ continuum

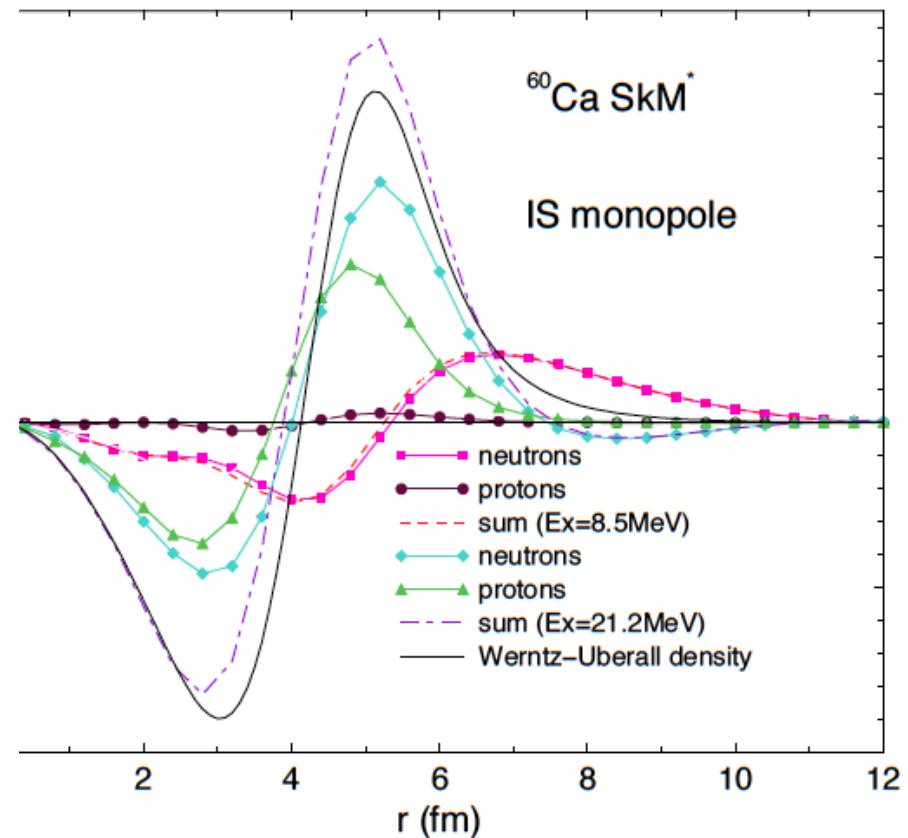
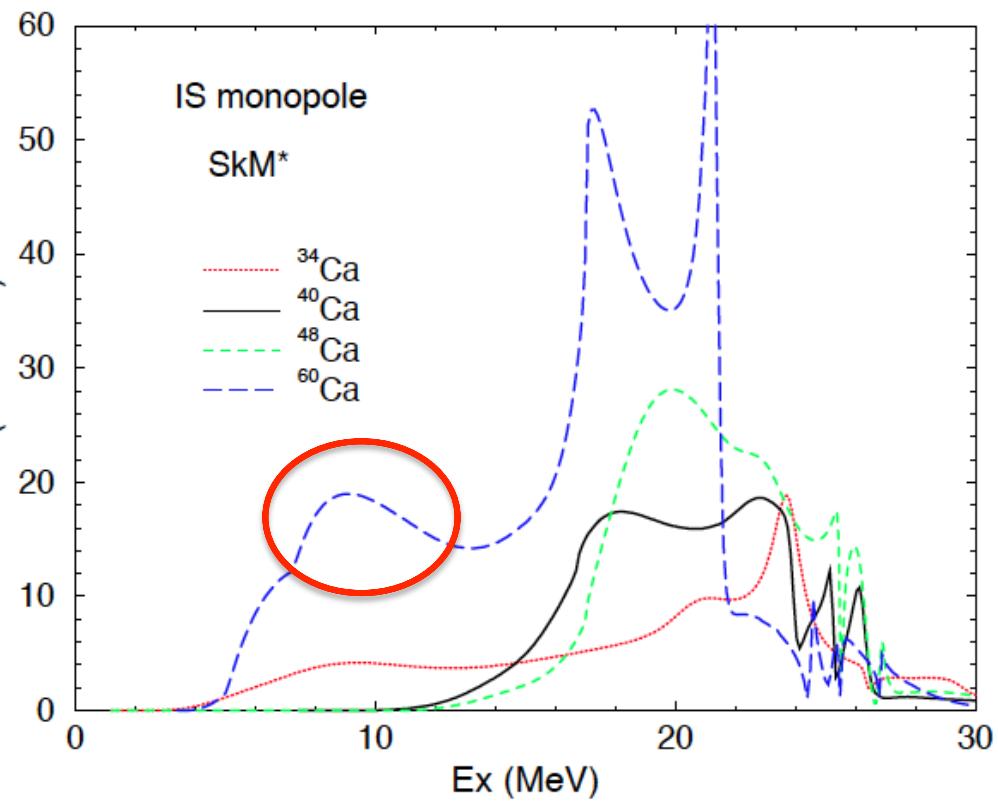


Continuum RPA: no smearing.



E. Yuksel et al., Eur.Phys.J. A49, 124(2013)
RPA with discretized basis with smearing the strength

I. Hamamoto, H. Sagawa and X. Z. Zhang
 Phys. Rev. C56, 3121(1997)



A broad bump appears as an oscillation of neutron skim against the core in ^{60}Ca .

Summary

- 1) Threshold continuum strength as a broad shoulder appears the monopole response less than $E_x=15\text{MeV}$ in a neutron-rich nucleus ^{68}Ni .
- 2) No resonance state appears below $E_x < 20\text{MeV}$.
- 3) Spin-orbit splitting should be discussed using resonance states.
- 4) Theoretically the proper treatment of the continuum effect is extremely important for the monopole excitations in neutron-rich nuclei.
- 5) To measure the cross sections **at the forward angles** is desperately needed to assign the monopole strength and excluding other multipoles.

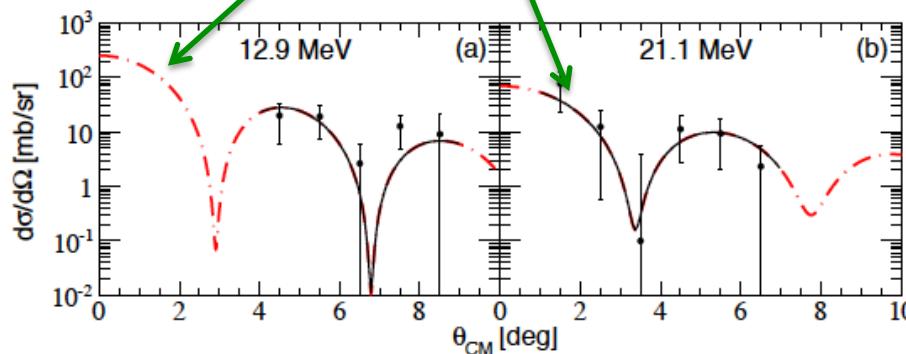


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