

Microscopic description of fission using dynamical theories.

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Lack of theoretical prediction

Lack of theoretical prediction

- Error of order of magnitudes on the life-time
- Lack of prediction for the charge/mass distribution

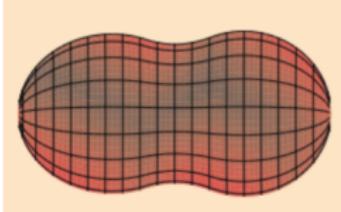
Prediction are necessary for :

- Astrophysics (r-process)
- Industrial applications, production of ions, reactors...

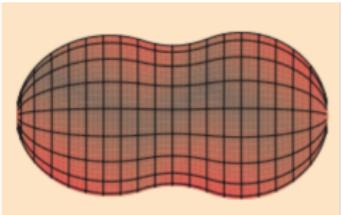
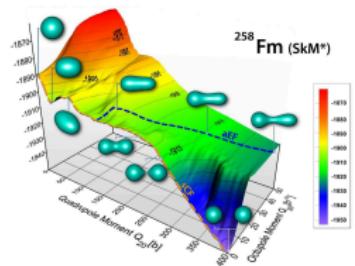
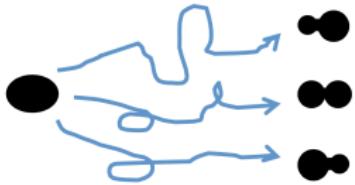
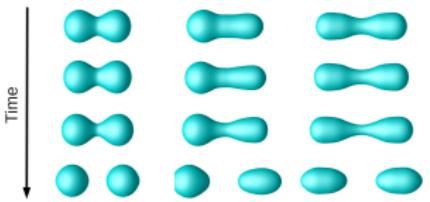
Lots of theoretical questions

- How to define the scission ?
- What are the important degrees of freedom ?
- Shell effects ?
- Effect of pairing ? Odd-even effects ?
- How the energy is split into the fragments ?
- ...

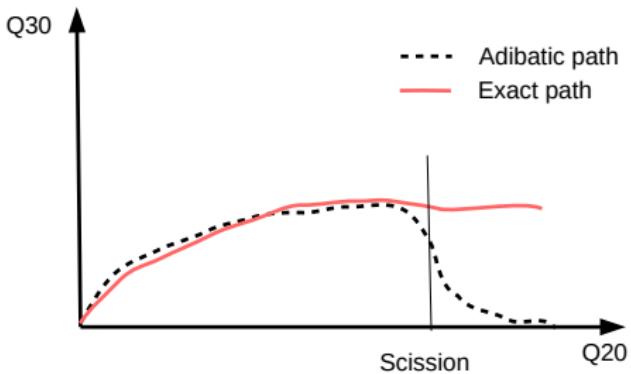
State of the art :

	Macroscopical model
Static	<p>Liquid drop with shell correction</p>  <p>P. Moller, et al., Nature 409 (2001)</p>
Dynamics	<p>Stochastic motion</p>  <p>J. Randrup, PRL 106 (2011)</p>

State of the art :

	Macroscopical model	Microscopical model
Static	<p>Liquid drop with shell correction</p> 	<p>Mean-field theory with pairing, HF+BCS or HFB</p> 
Dynamics	<p>Stochastic motion</p> 	<p>Dynamical mean-field TDHF+BCS</p> 

Adiabatic approximation



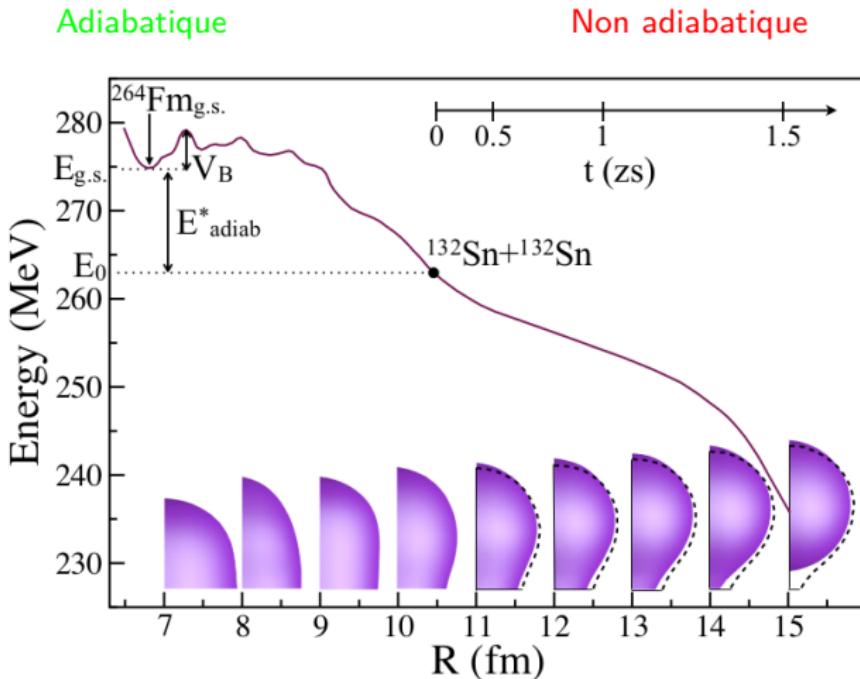
Adiabatic path

Path that minimize the energy with respect to degrees of freedom orthogonal to the elongation.

TDHF or TDHF+BCS

All the degrees of freedom are taken into account

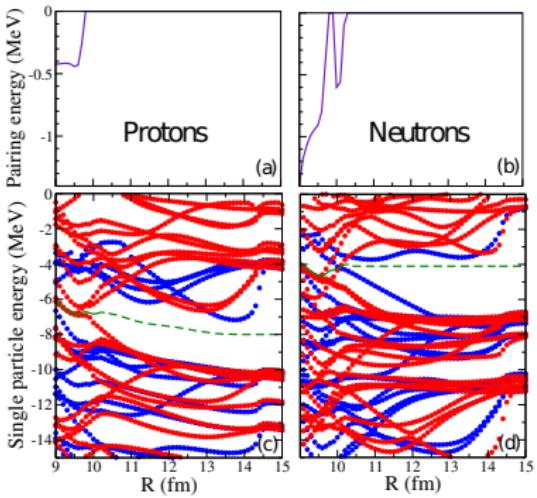
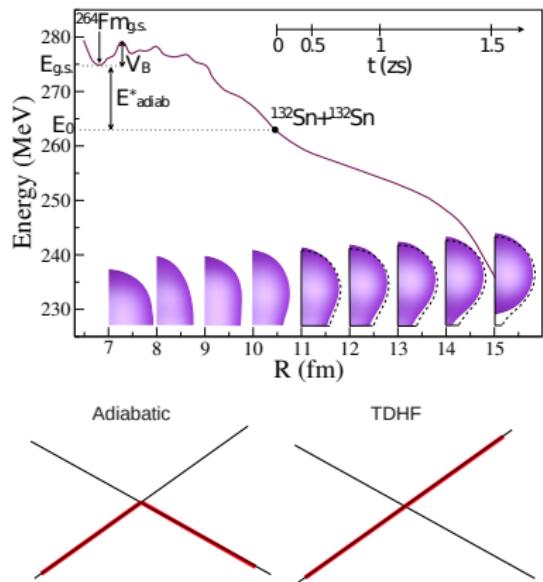
TDHF calculation, fission of ^{264}Fm



C. Simenel and A. S. Umar, Phys. Rev. C 89, 031601(R), 2014

The adiabaticity approximation is assumed for the barrier crossing but is known to break down before scission.

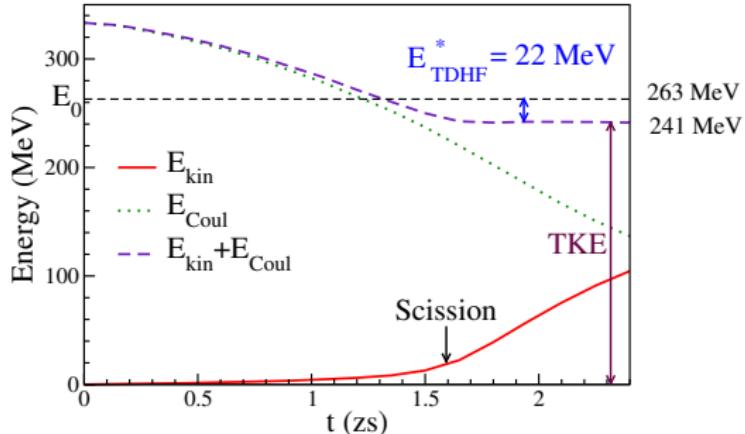
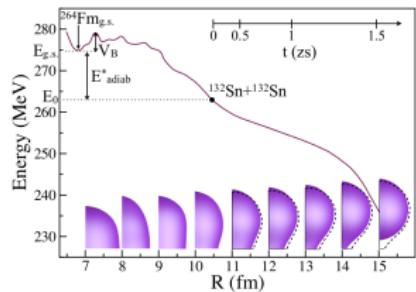
TDHF calculation, fission of ^{264}Fm



C. Simenel and A. S. Umar, Phys. Rev. C 89, 031601(R), 2014

The adiabaticity is not assumed in the TDHF evolution

TDHF calculation, fission of ^{264}Fm



C. Simenel and A. S. Umar, Phys. Rev. C 89, 031601(R), 2014

Conclusion

Total Kinetic energy = 241 MeV

Excitation energy = $E^*_{\text{adiabatic}} + E^*_{\text{TDHF}} = 34$ MeV

Mean-field theory with pairing

TDHF

- Independent particle
- Initialisation : $\hat{h}_{MF} |\phi_i\rangle = \epsilon_i |\phi_i\rangle$
- Evolution :
 $i\hbar \frac{d\rho}{dt} = [h_{MF}, \rho]$

TDHFB

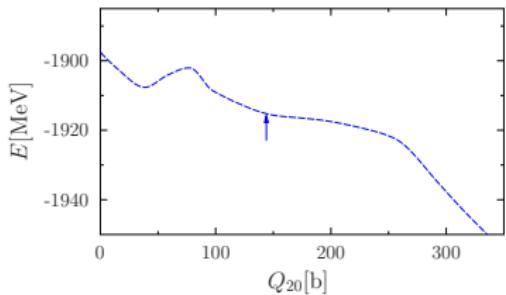
- Pairing correlation
- Quasi-particles : $|\omega_\alpha\rangle = \begin{pmatrix} u_\alpha \\ v_\alpha \end{pmatrix}$
- Evolution :
 $i\hbar \frac{d|\omega_\alpha\rangle}{dt} = \begin{pmatrix} h & \Delta \\ -\Delta^* & -h^* \end{pmatrix} |\omega_\alpha\rangle$

TDHF+BCS

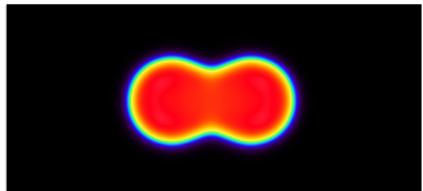
- Based on TDHFB with the approximation : $\Delta_{ij} = \delta_{ij}\Delta_i$
- Evolution :
 $i\hbar \frac{d\phi_i}{dt} = (\hat{h}_{MF} - \epsilon_i)\phi_i$
 $i\hbar \frac{dn_i}{dt} = \Delta_i^* \kappa_i - \Delta_i \kappa_i^*$
 $i\hbar \frac{d\kappa_i}{dt} = \kappa_i(\epsilon_i - \epsilon_{\bar{i}}) + \Delta_i(2n_i - 1)$

Why does we need pairing ?

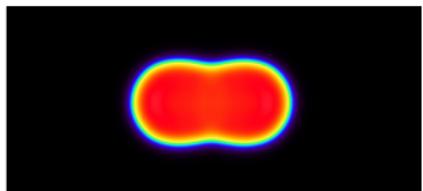
Fission barrier : ^{258}Fm



TDHF



TDHF+BCS

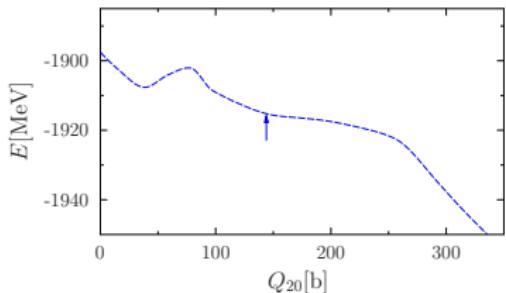


G. Scamps, C. Simenel, D. Lacroix, arXiv :1501.03592 [nucl-th]

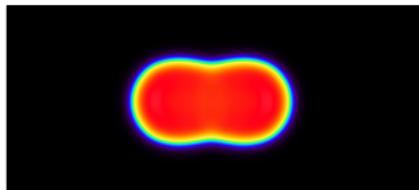
Why does we need pairing ?

TDHF

Fission barrier : ^{258}Fm



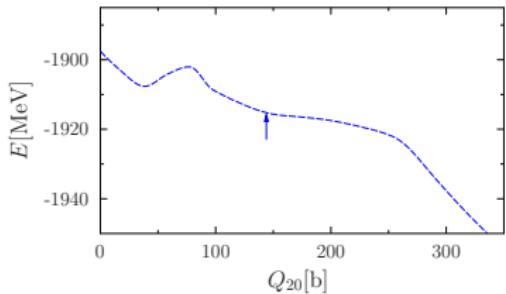
TDHF+BCS



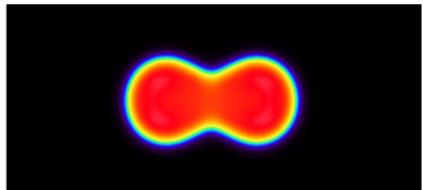
G. Scamps, C. Simenel, D. Lacroix, arXiv :1501.03592 [nucl-th]

Why does we need pairing ?

Fission barrier : ^{258}Fm



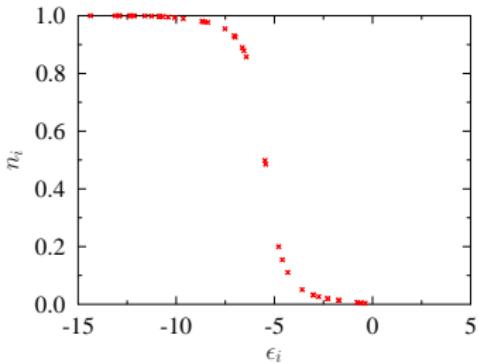
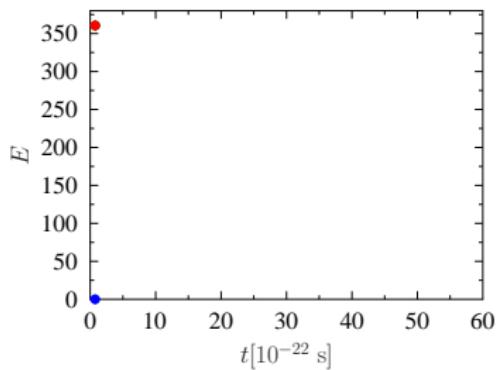
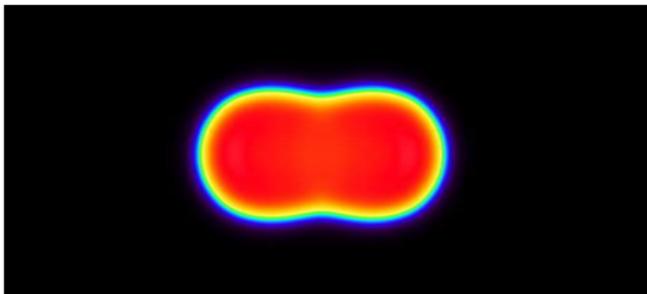
TDHF



TDHF+BCS

G. Scamps, C. Simenel, D. Lacroix, arXiv :1501.03592 [nucl-th]

Influence of pairing on fission process



Influence of pairing on fission process

^{258}Fm : Experimental results

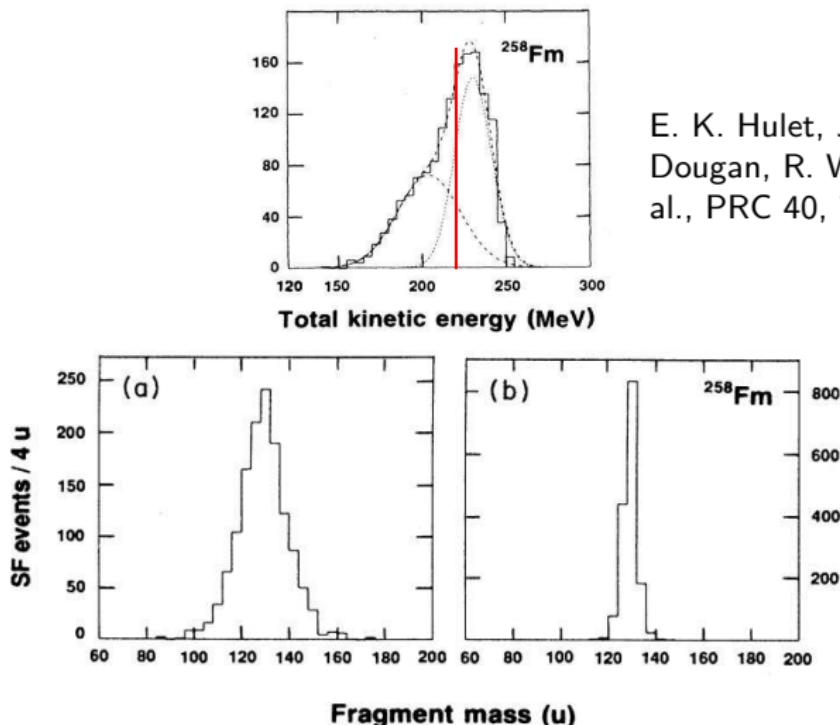


FIG. 8. Mass distributions obtained by sorting fission events according to their total kinetic energies: (a) for events with TKE's < 220 MeV and (b) for those with TKE's ≥ 220 MeV.

^{258}Fm : Bimodal or trimodal fission ?

3 possible modes

- Symmetric compact fragment



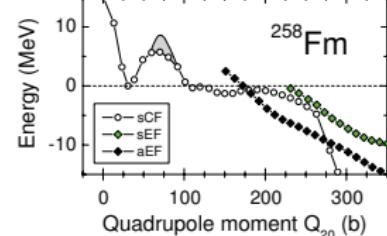
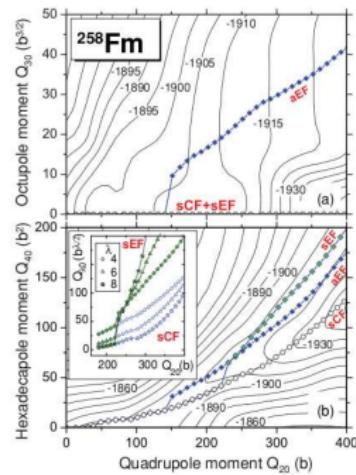
- Asymmetric elongated fragment



- Symmetric elongated fragment



Constraint HF+BCS calculations (SkM*)



A. Staszczak, A. Baran, J. Dobaczewski, and W. Nazarewicz,
PRC 80, 014309 (2009)

^{258}Fm : TDHF+BCS results

3 possible modes

- Symmetric compact fragment



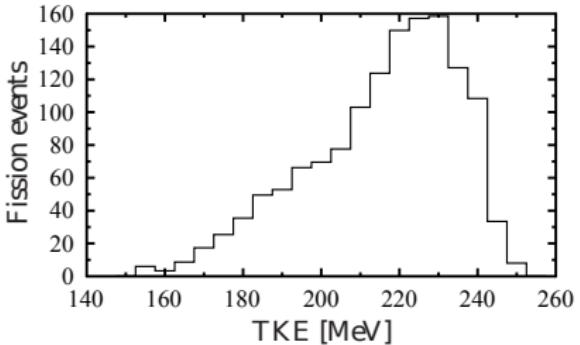
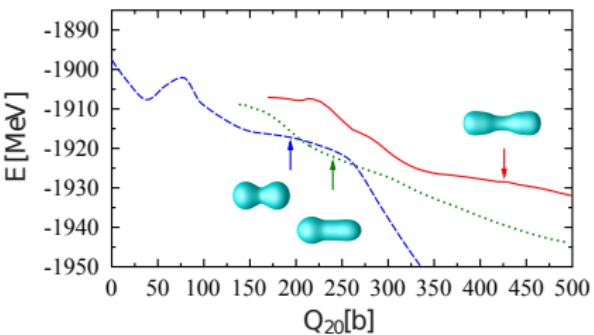
- Asymmetric elongated fragment



- Symmetric elongated fragment



Sly4d



^{258}Fm : TDHF+BCS results

3 possible modes

- Symmetric compact fragment

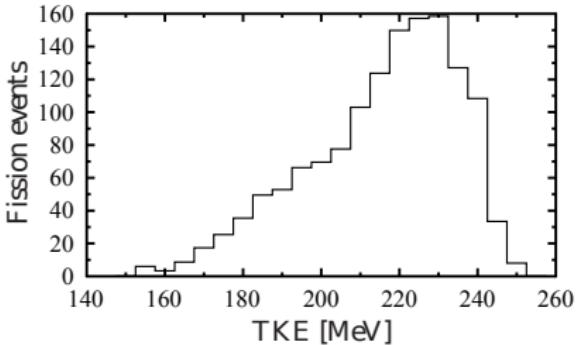
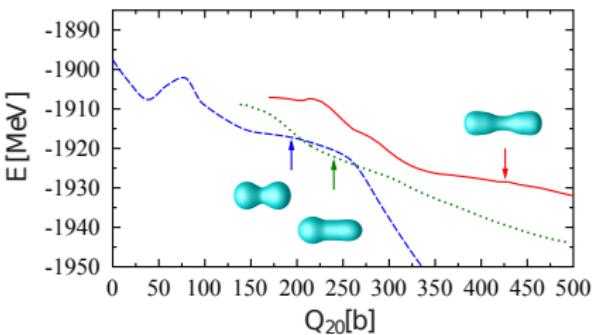


- Asymmetric elongated fragment



- Symmetric elongated fragment

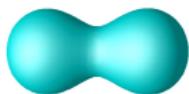
Sly4d



^{258}Fm : TDHF+BCS results

3 possible modes

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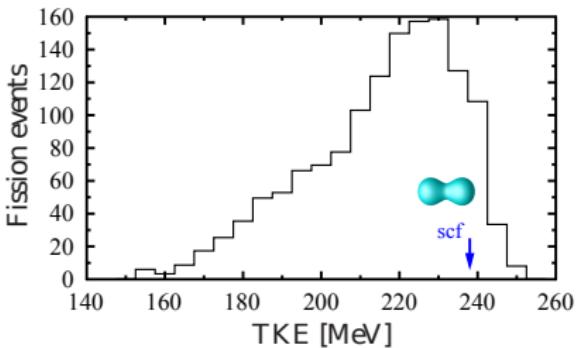
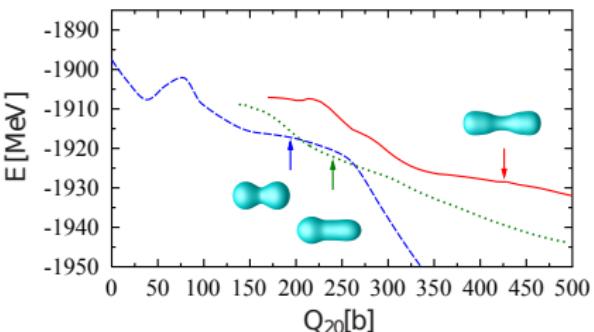
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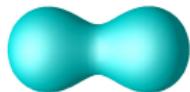
Sly4d



^{258}Fm : TDHF+BCS results

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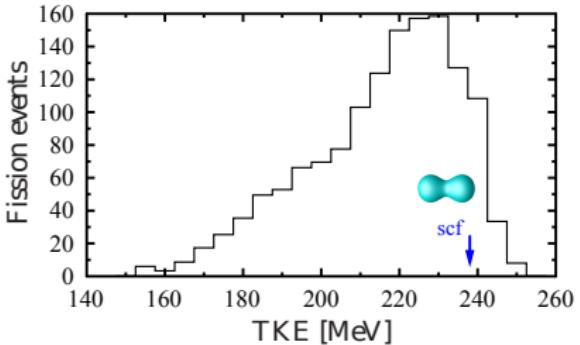
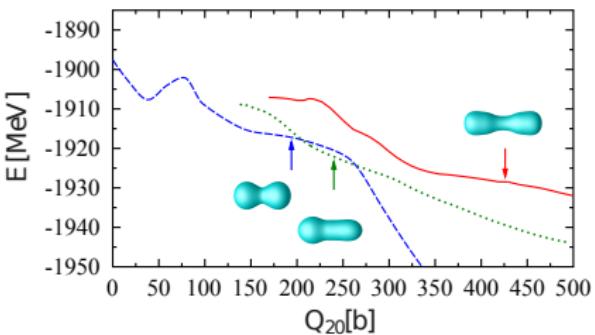


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Sly4d



^{258}Fm : TDHF+BCS results

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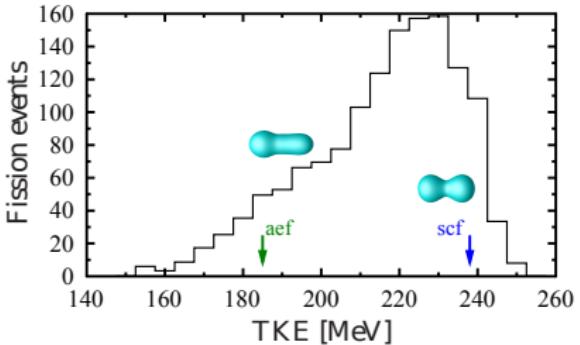
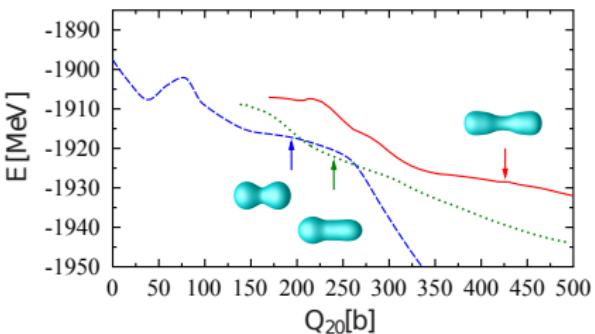
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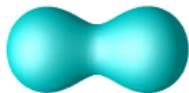
Sly4d



^{258}Fm : TDHF+BCS results

3 possible modes

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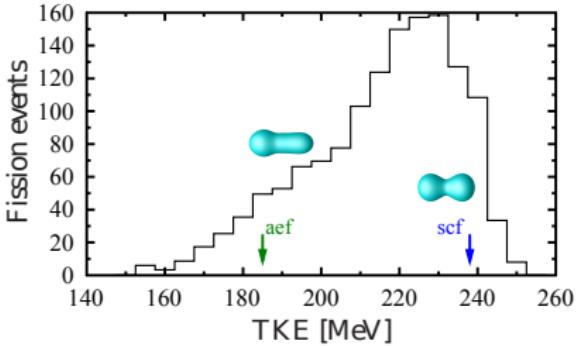
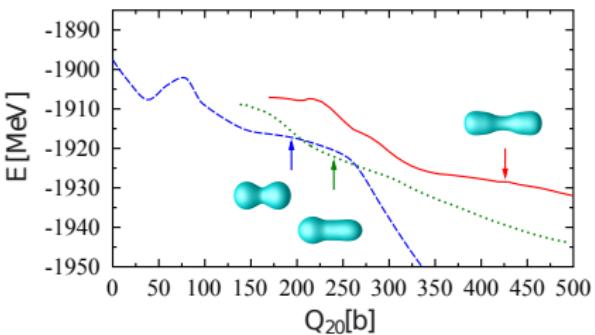


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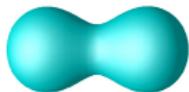
Sly4d



^{258}Fm : TDHF+BCS results

3 possible modes

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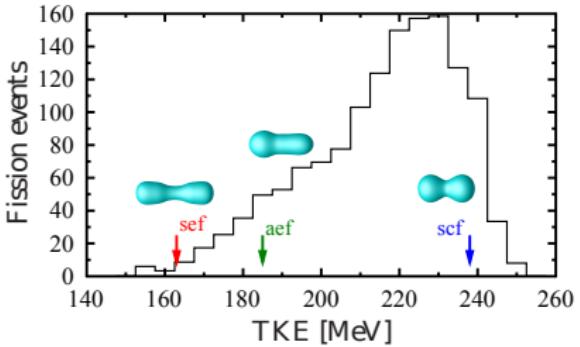
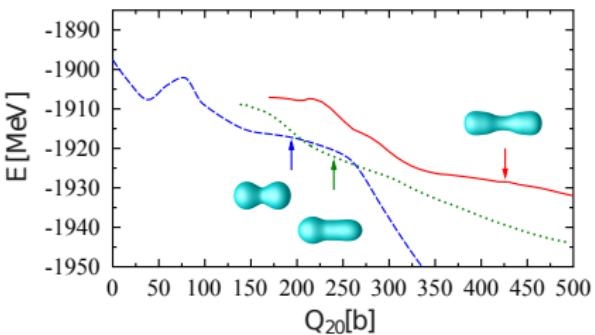
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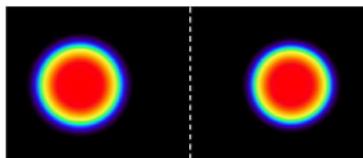


Sly4d



Distribution of number of particles

Projection technique

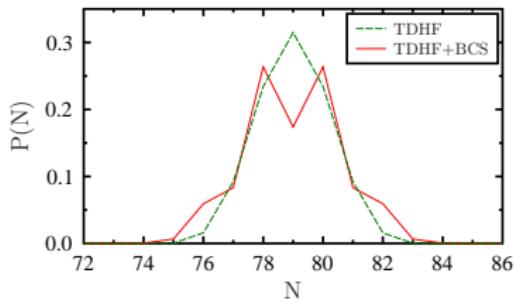


Proba (N part. on the left) = $\langle \Psi | \hat{P}_{\text{left}}(N) | \Psi \rangle$

TDHF : C. Simenel, PRL 105 (2010)

TDHF+BCS : G. Scamps and D. Lacroix, PRC 87, 014605 (2013)

Results

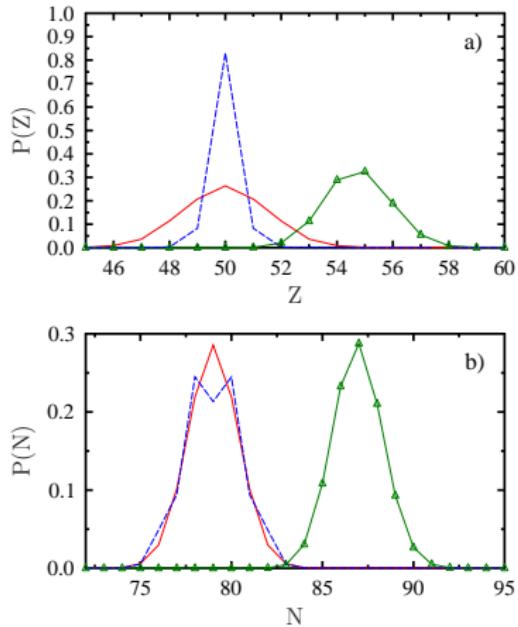


Conclusion

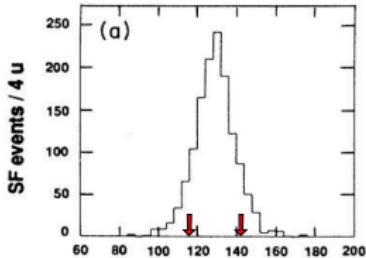
Reproduction of the odd-even effect
with TDHF+BCS

Distribution of number of particles

Results



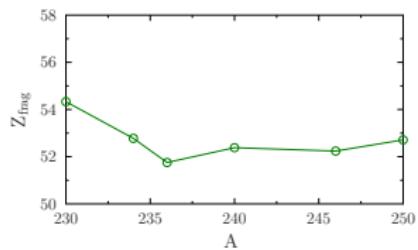
Experimental data



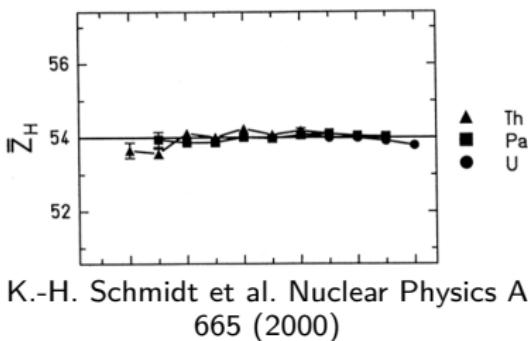
Systematic comparison for actinide

Comparison with experimental data

TDHF+BCS results for ^{230}Th , ^{234}U ,
 ^{236}U , ^{240}Pu , ^{246}Cm , ^{250}Cf



Experimental data



K.-H. Schmidt et al. Nuclear Physics A 665 (2000)

Conclusion

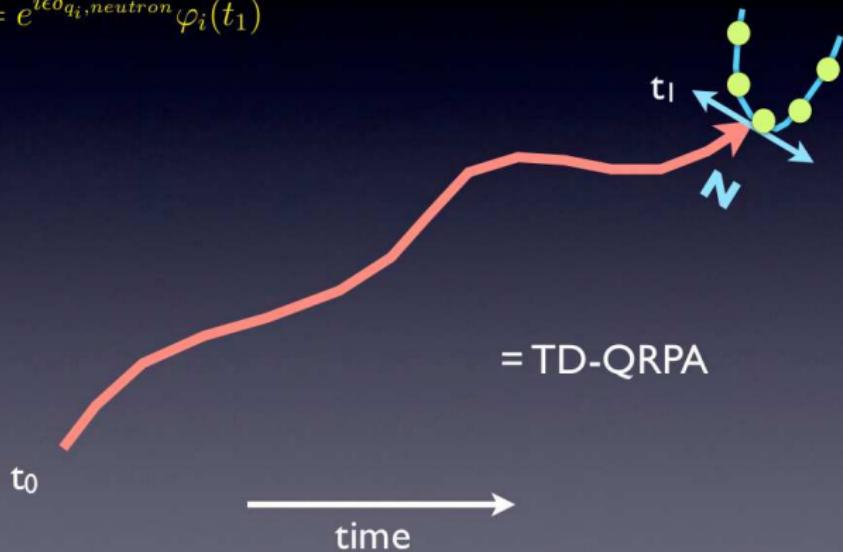
→ Good reproduction of the $Z \approx 54$ "magic" number

Numerical application of the BV prescription

standard forward TDHF

neutron fluctuations at t_1

$$\varphi_i(t_1, \epsilon) = e^{i\epsilon\delta_{q_i, neutron}} \varphi_i(t_1)$$



Numerical application of the BV prescription

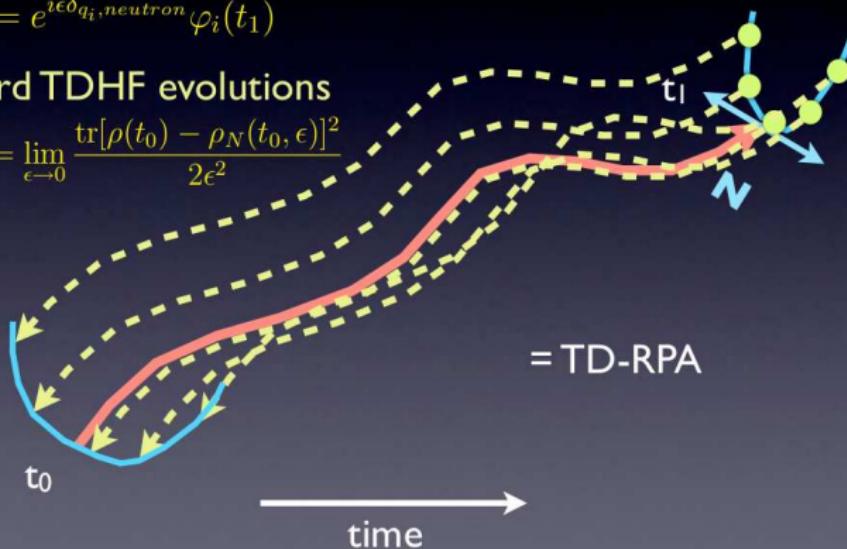
standard forward TDHF

neutron fluctuations at t_1

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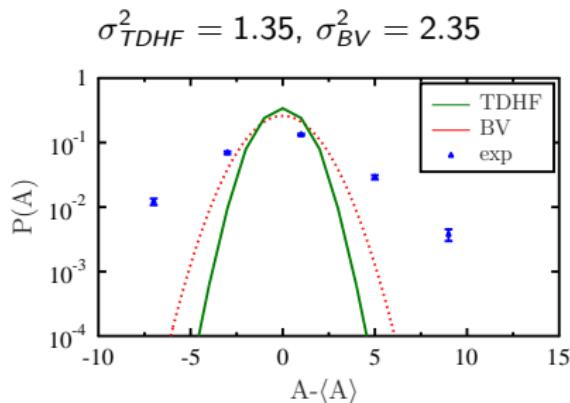
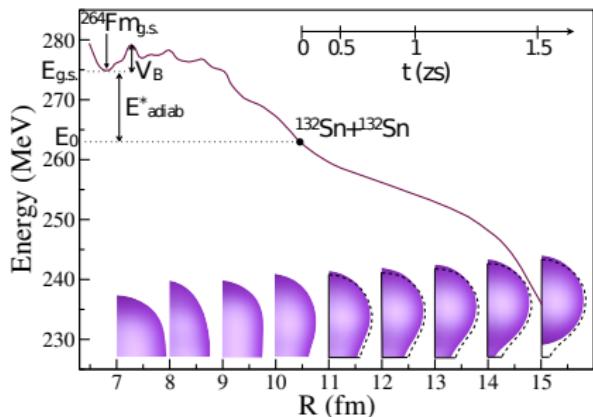
backward TDHF evolutions

$$\sigma_{NN}^2(t_1) = \lim_{\epsilon \rightarrow 0} \frac{\text{tr}[\rho(t_0) - \rho_N(t_0, \epsilon)]^2}{2\epsilon^2}$$



TDHF with Balian-Vénéroni variational principle

Results



Conclusion

BV provides the fluctuations for the scission process
Need initial fluctuations (second part of the talk)

Conclusion TDHF+BCS

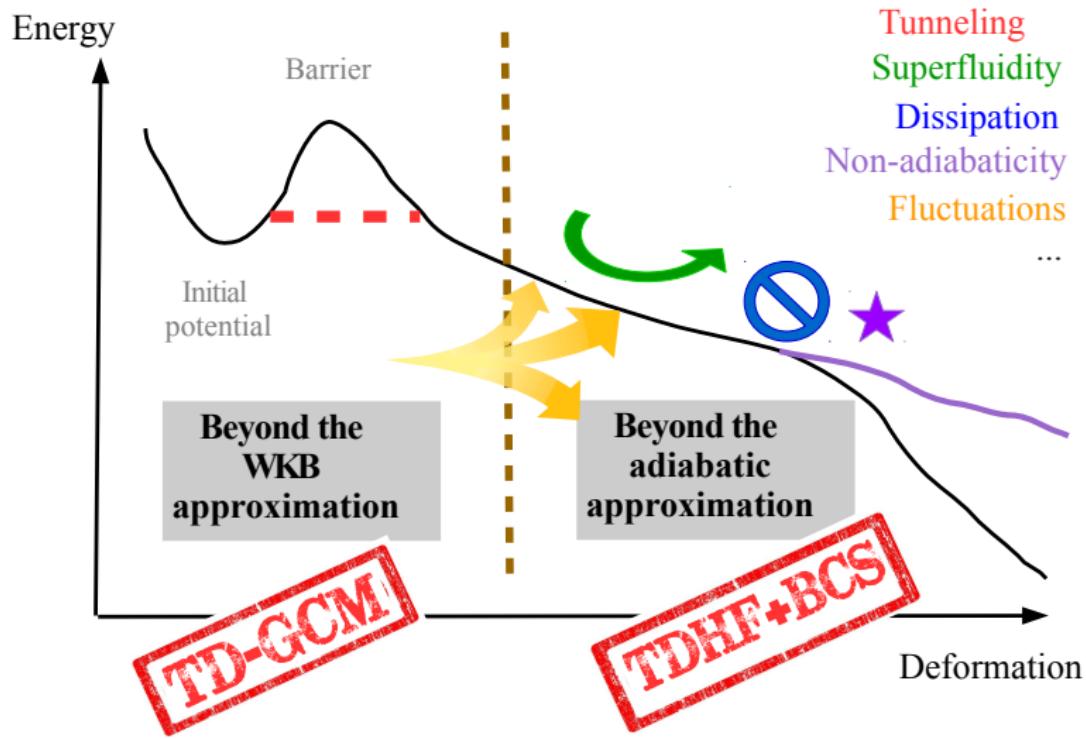
Conclusion

- Good reproduction of the total kinetic energy
- Important effect of pairing on fission process (J. W. Negele, et al. (1978))
- Reproduction of the even-odd effects
- Reproduction of the $Z \approx 54$ behavior
- Fluctuation obtained with Balian-Vénéroni method (for TDHF)

Prospects

- Finite temperature calculation
- Description of the evaporation
- Study of the collective excitation after the scission

Outlooks



Thank you