

Searching for New Physics in Heavy Flavours

Luca Silvestrini

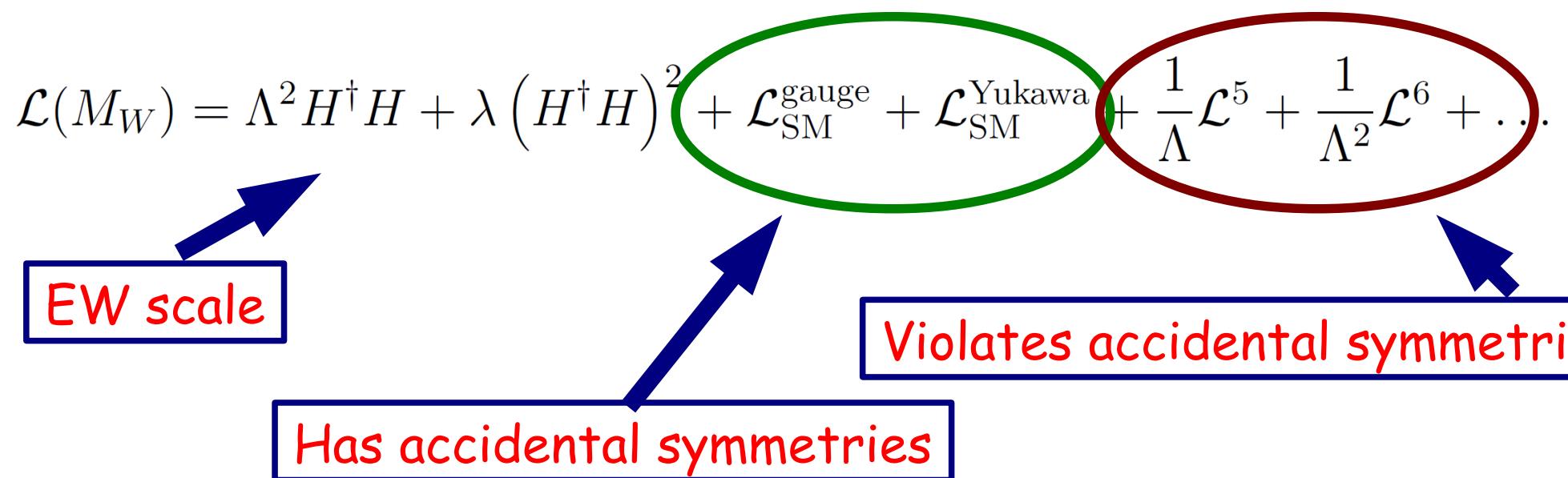
INFN, Rome



- Introduction
- Status of flavour physics in the SM
- UT beyond the SM and constraints on NP
- CP violation in Charm Physics
- Conclusions and Outlook

INTRODUCTION

The Standard Model works beautifully up to a few hundred GeV's, but it must be an effective theory valid up to a scale $\Lambda \leq M_{\text{planck}}$:



INTRODUCTION - II

Two accidental symmetries of the SM are crucial for our discussion:

- 1) Absence of tree-level flavour changing neutral currents, GIM suppression of FCNC @ the loop level
- 2) No CP violation @ tree level
⇒ Flavour physics extremely sensitive to NP!!

EXPRESS REVIEW OF THE SM

- All flavour violation from charged current coupling: CKM matrix V

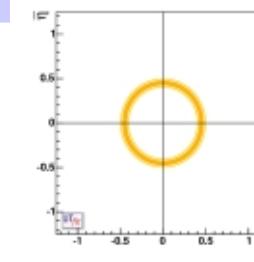
$$V_{\text{CKM}} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

- Top quark exchange dominates FCNC loops: third row (V_{tq}) determines FCNC's
 $\leftrightarrow \bar{\rho}, \bar{\eta}$, apex of the Unitarity Triangle
from $V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 1$

Flavour summarized on the $p-\eta$ plane

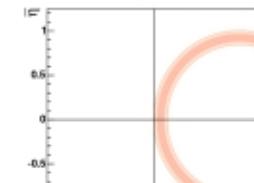
$\text{BR}(b \rightarrow u l \bar{\nu})$, $\text{BR}(B \rightarrow \pi l \bar{\nu})$

CC



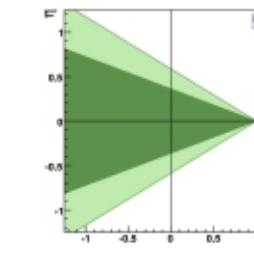
Δm_q (B_q - \bar{B}_q mass diff.)

NC



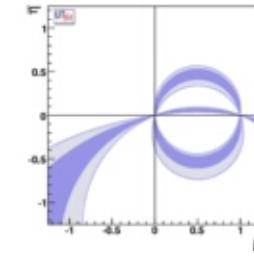
$A_{CP}(b \rightarrow c \bar{c} s)$ (J/ψ K, ...)

CC



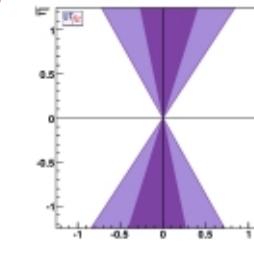
$A_{CP}(b \rightarrow s \bar{s} s, d \bar{d} s)$ (ϕ K, πK , ...)

NC



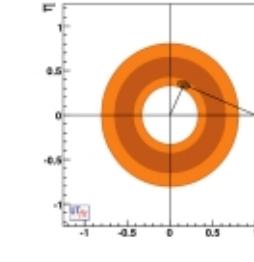
$A_{CP}(b \rightarrow d \bar{d} d, u \bar{u} d)$ ($\pi\pi$, $\rho\rho$, ...)

CC/NC



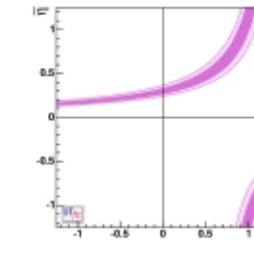
$\text{BR}(b \rightarrow \bar{c} u d, \bar{c} u s)$ (DK, ...)

CC



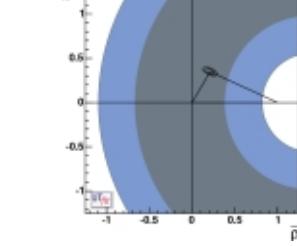
$\text{BR}(B \rightarrow \tau \bar{\nu})$

CC



$\text{BR}(B \rightarrow \rho \gamma)/\text{BR}(B \rightarrow K^* \gamma)$

NC



ε_K

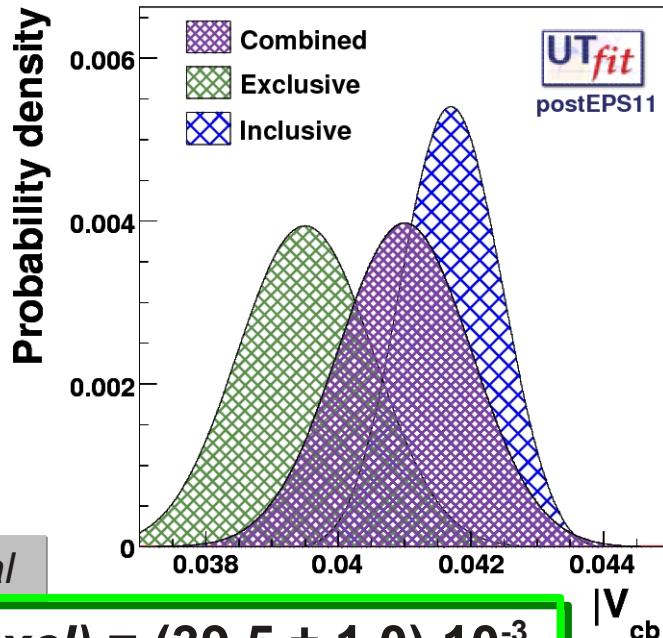
NC



$K^+ \rightarrow \pi^+ \gamma \gamma$
Frascati, 26/6/2012

NC
L. Silvestrini

SEMILEPTONIC DECAYS



Laiho et al

$$V_{cb} (\text{excl}) = (39.5 \pm 1.0) 10^{-3}$$

HFAG

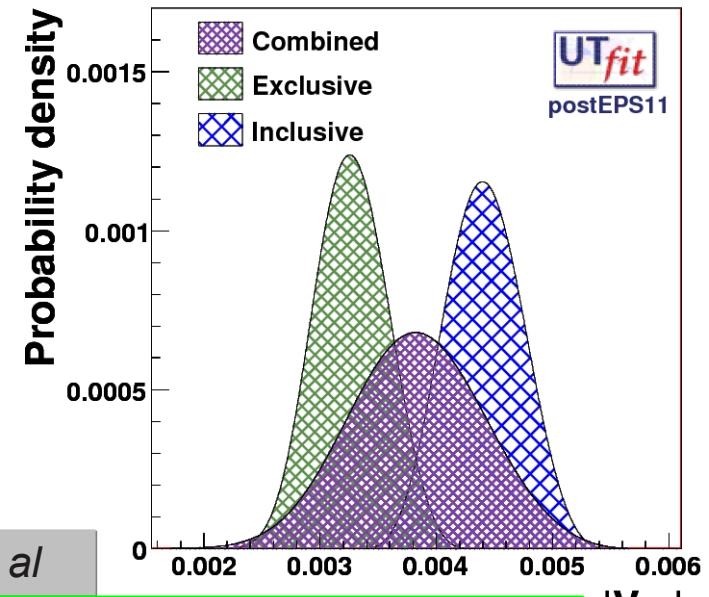
$$V_{cb} (\text{incl}) = (41.7 \pm 0.7) 10^{-3}$$

$\sim 1.8\sigma$ discrepancy

UTfit input value:
average à la PDG

$$V_{cb} = (41.0 \pm 1.0) 10^{-3}$$

uncertainty $\sim 2.4\%$



Laiho et al

$$V_{ub} (\text{excl}) = (3.28 \pm 0.30) 10^{-3}$$

UTfit from HFAG

$$V_{ub} (\text{incl}) = (4.40 \pm 0.31) 10^{-3}$$

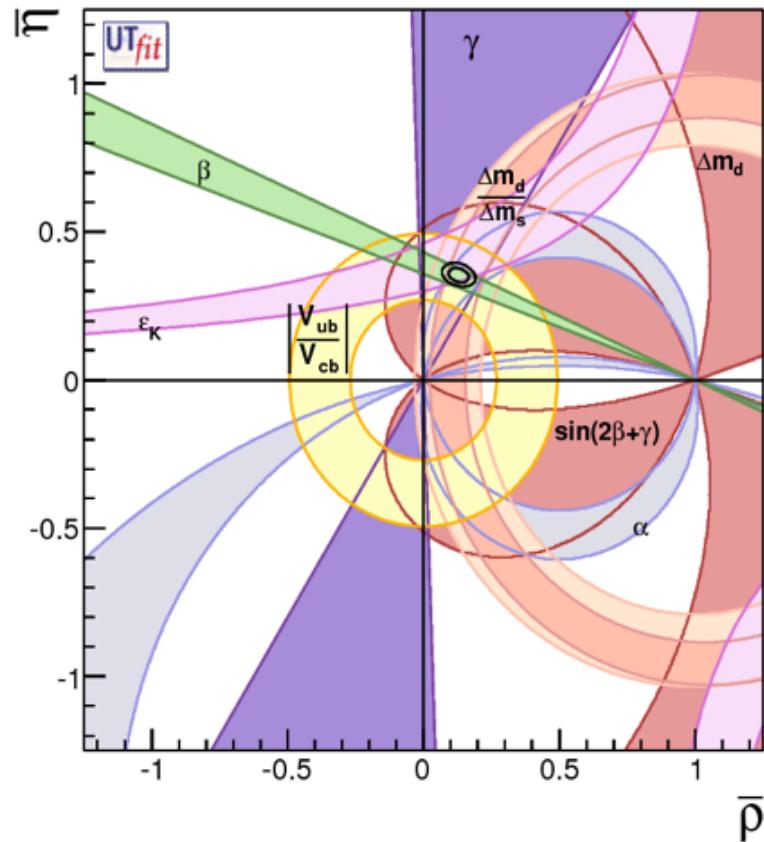
$\sim 2.6\sigma$ discrepancy

UTfit input value:
average à la PDG

$$V_{ub} = (3.82 \pm 0.56) 10^{-3}$$

uncertainty $\sim 15\%$

THE OVERALL PICTURE



$$\rho = 0.138 \pm 0.021$$

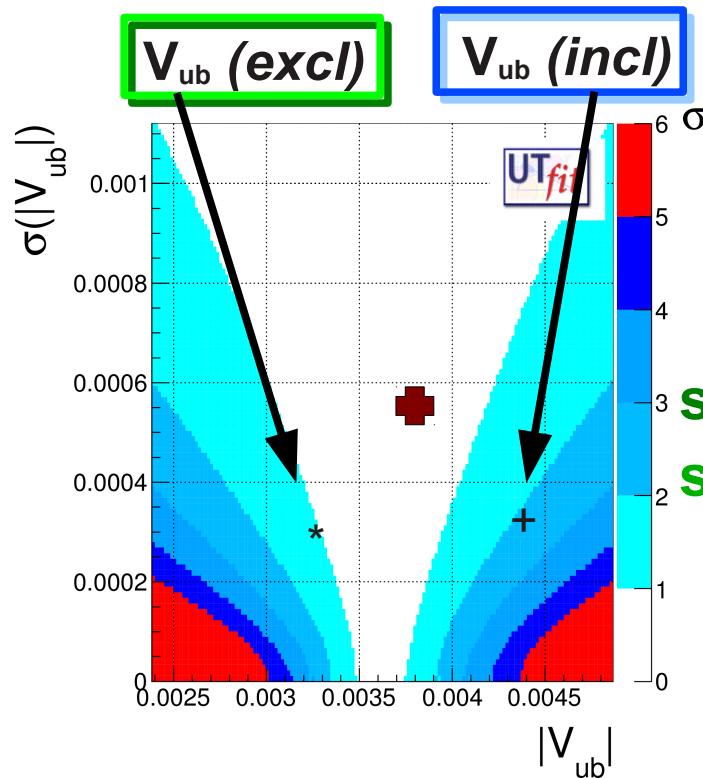
$$\eta = 0.350 \pm 0.014$$

$$A = 0.822 \pm 0.014$$

$$\lambda = 0.2254 \pm 0.0006$$

Parameter	Input value	Full fit	SM Prediction
f_{B_s}	0.233 ± 0.01	0.2303 ± 0.0058	—
f_{B_s}/f_{B_d}	1.2 ± 0.02	1.201 ± 0.018	—
B_{B_s}/B_{B_d}	1.05 ± 0.07	1.086 ± 0.051	—
B_{B_s}	0.87 ± 0.04	0.853 ± 0.036	—
B_k	0.75 ± 0.02	0.755 ± 0.02	0.847 ± 0.09
$\alpha[^{\circ}]$	91.4 ± 6.1	89.3 ± 3.0	87.9 ± 3.8
$\beta[^{\circ}]$	—	22.07 ± 0.9	26.1 ± 2.3
$\sin(2\beta)$	0.68 ± 0.023	0.697 ± 0.023	0.792 ± 0.05
$\cos(2\beta)$	0.87 ± 0.13	0.718 ± 0.022	0.616 ± 0.064
$2\beta + \gamma[^{\circ}]$	-90 ± 56 and 94 ± 52	112.8 ± 3.2	113.0 ± 3.2
$\gamma[^{\circ}]$	-103.9 ± 10.5 and 75.5 ± 10.5	68.6 ± 3.1	67.8 ± 3.2
$ \epsilon_k $	$0.00222894 \pm 1.14971 \times 10^{-5}$	$0.00222754 \pm 1.0978 \times 10^{-5}$	—
$B(B \rightarrow \tau\nu)10^{-4}$	1.64 ± 0.34	0.857 ± 0.082	0.813 ± 0.077
$J_{cp}10^{-5}$	—	3.1 ± 0.12	—
$B(B_s \rightarrow ll), 10^{-9}$	—	3.45 ± 0.27	—

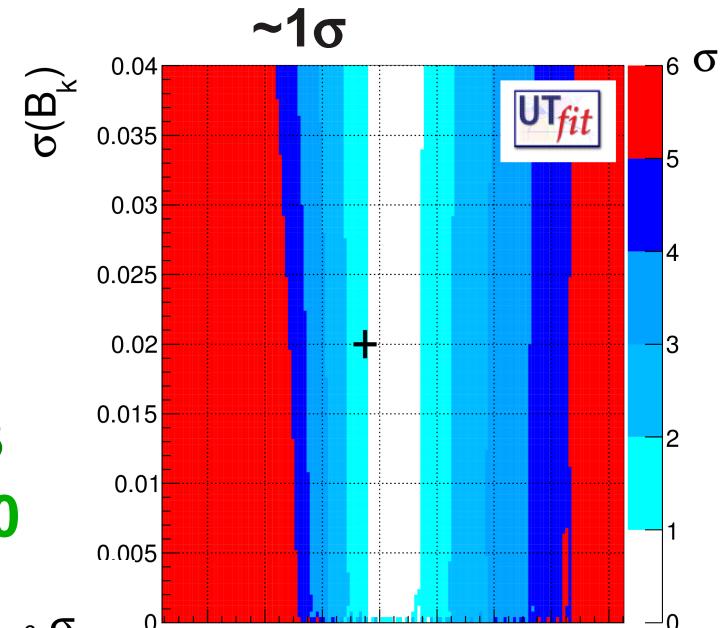
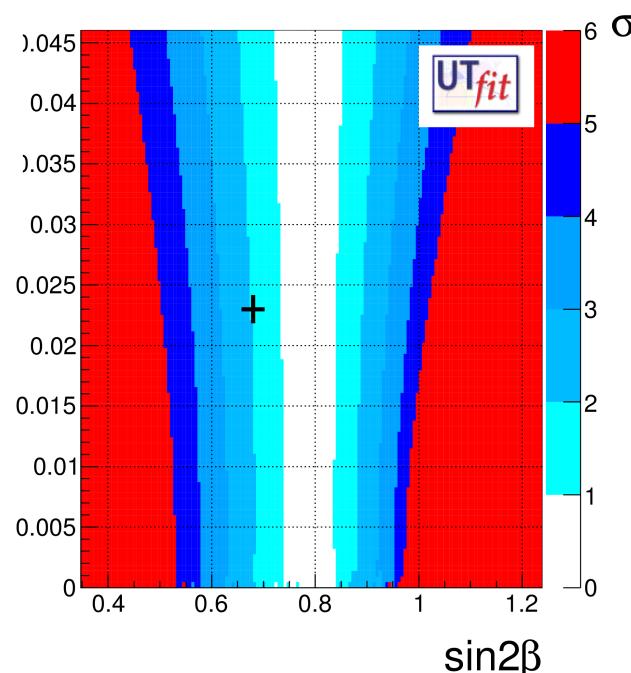
tensions



$\sim 2\sigma$

$$\sin 2\beta_{\text{exp}} = 0.680 \pm 0.023$$

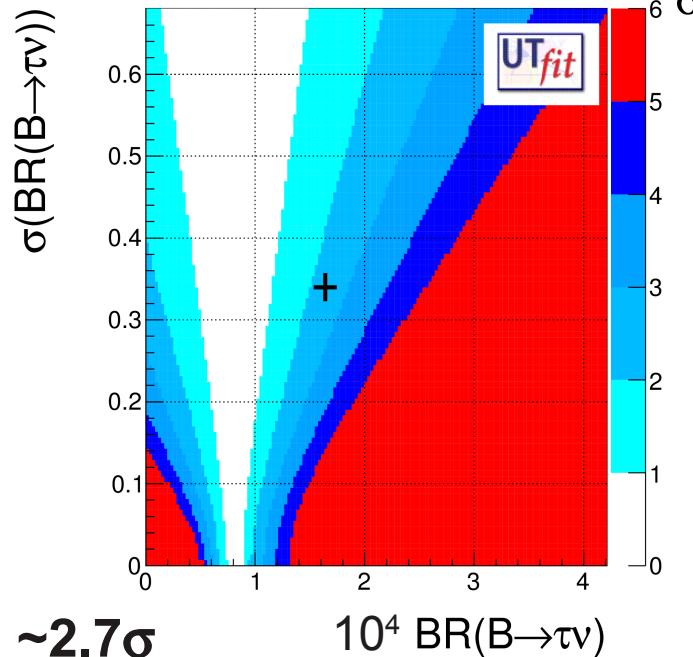
$$\sin 2\beta_{\text{UTfit}} = 0.792 \pm 0.050$$



more standard model predictions:

current HFAG world average

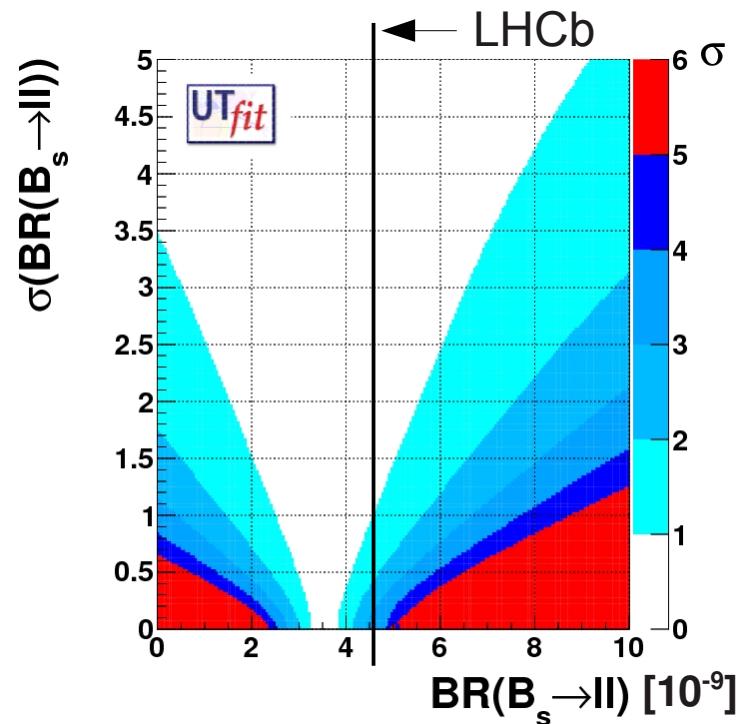
$$\text{BR}(B \rightarrow \tau\nu) = (1.67 \pm 0.30) 10^{-4}$$



$\sim 2.7\sigma$

best limit from LHCb

$$\text{BR}(B_s \rightarrow \mu\mu) < 4.5 10^{-9}$$



indirect determinations from UT

$$\text{BR}(B \rightarrow \tau\nu) = (0.82 \pm 0.08) 10^{-4}$$

$$\text{BR}(B_s \rightarrow ll) = (3.54 \pm 0.28) 10^{-9}$$

M.Bona et al, 0908.3470 [hep-ph]

(SEMI)LEPTONIC $B \rightarrow \tau$

- (Semi)leptonic $B \rightarrow \tau$ decays seem to systematically deviate from SM predictions:
 - $\text{BR}(B \rightarrow \tau\nu)$ higher than SM prediction by 2.7σ
 - $\text{BR}(B \rightarrow D\tau\nu)/\text{BR}(B \rightarrow D\nu)$ higher than SM prediction by 2σ
 - $\text{BR}(B \rightarrow D^*\tau\nu)/\text{BR}(B \rightarrow D^*\nu)$ higher than SM prediction by 2.7σ
- Deviation inconsistent with 2HDMII and simple MFV models @ large $\tan\beta$

UTfit beyond the Standard Model

1. fit simultaneously for the CKM and the NP parameters (generalized UT fit)
 - add most general NP to all sectors
 - use all available experimental info
 - find out how much room is left for NP in $\Delta F=2$ transitions
2. perform an $\Delta F=2$ EFT analysis to put bounds on the NP scale
 - consider different choices of the FV and CPV couplings

1. Parameterization of generic NP contributions to the mixing amplitudes

K mixing amplitude (2 real parameters):

$$\text{Re } A_K = C_{\Delta m_K} \text{Re } A_K^{SM} \quad \text{Im } A_K = C_\varepsilon \text{Im } A_K^{SM}$$

B_d and B_s mixing amplitudes (2+2 real parameters):

$$A_q e^{2i\Phi_q} = C_{B_q} e^{2i\Phi_{B_q}} A_q^{SM} e^{2i\Phi_q^{SM}} = \left(1 + \frac{A_q^{NP}}{A_q^{SM}} e^{2i(\Phi_q^{NP} - \Phi_q^{SM})} \right) A_q^{SM} e^{2i\Phi_q^{SM}}$$

Observables:

$$\Delta m_{q/K} = C_{B_q/\Delta m_K} (\Delta m_{q/K})^{SM} \quad \varepsilon_K = C_\varepsilon \varepsilon_K^{SM}$$

$$A_{CP}^{B_d \rightarrow J/\psi K_s} = \sin 2(\beta + \Phi_{B_d}) \quad A_{CP}^{B_s \rightarrow J/\psi \phi} \sim \sin 2(-\beta_s + \Phi_{B_s})$$

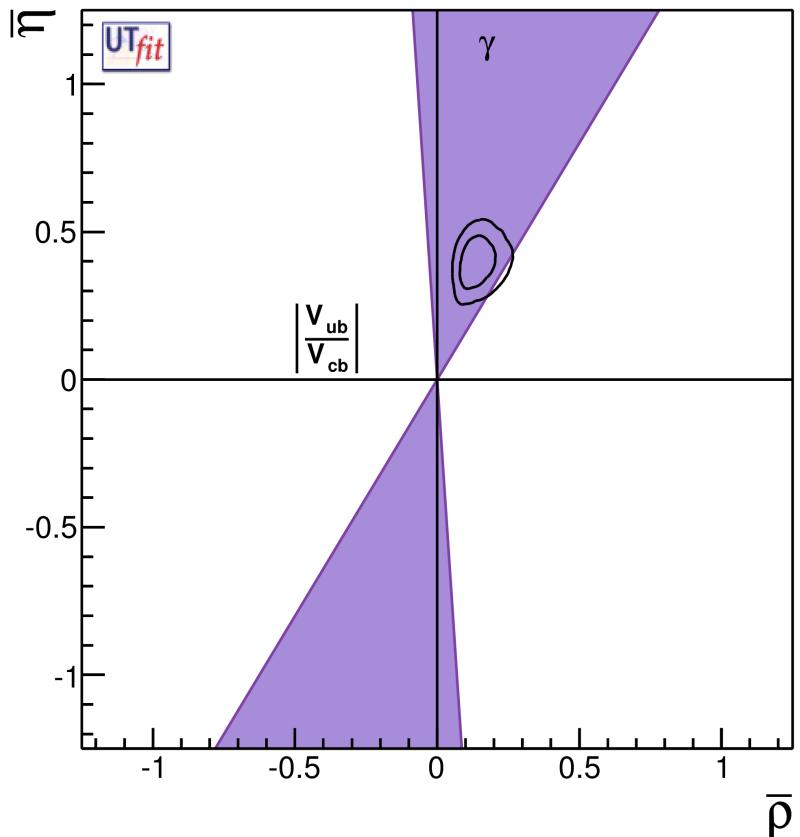
$$A_{SL}^q = \text{Im} \left(\Gamma_{12}^q / A_q \right) \quad \Delta \Gamma^q / \Delta m_q = \text{Re} \left(\Gamma_{12}^q / A_q \right)$$

UT parameters in the presence of NP

Model-independent
determination
of the CKM parameters
(no NP in tree-level decays)

$$\bar{\rho} = 0.136 \pm 0.043$$

$$\bar{\eta} = 0.397 \pm 0.054$$

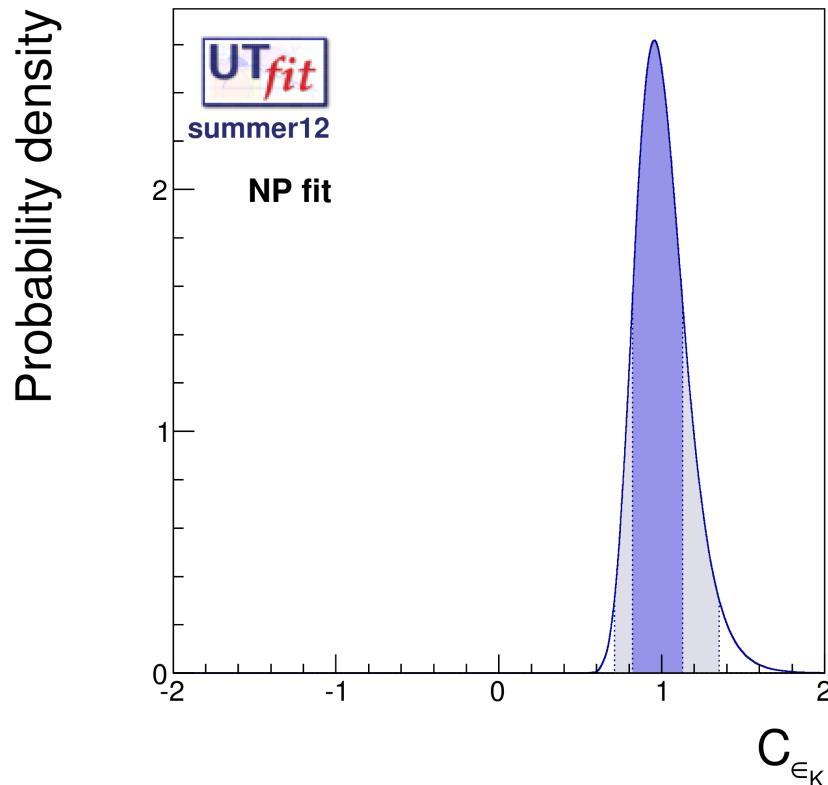


In the SM was:

$$\bar{\rho} = 0.138 \pm 0.021$$

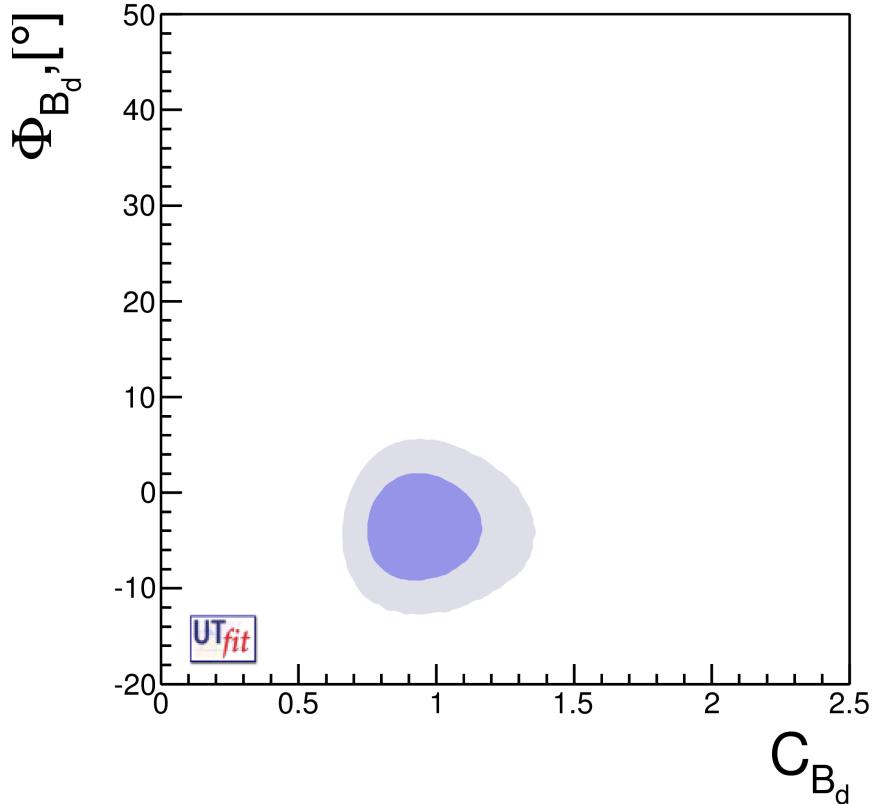
$$\bar{\eta} = 0.350 \pm 0.014$$

NP FIT RESULTS



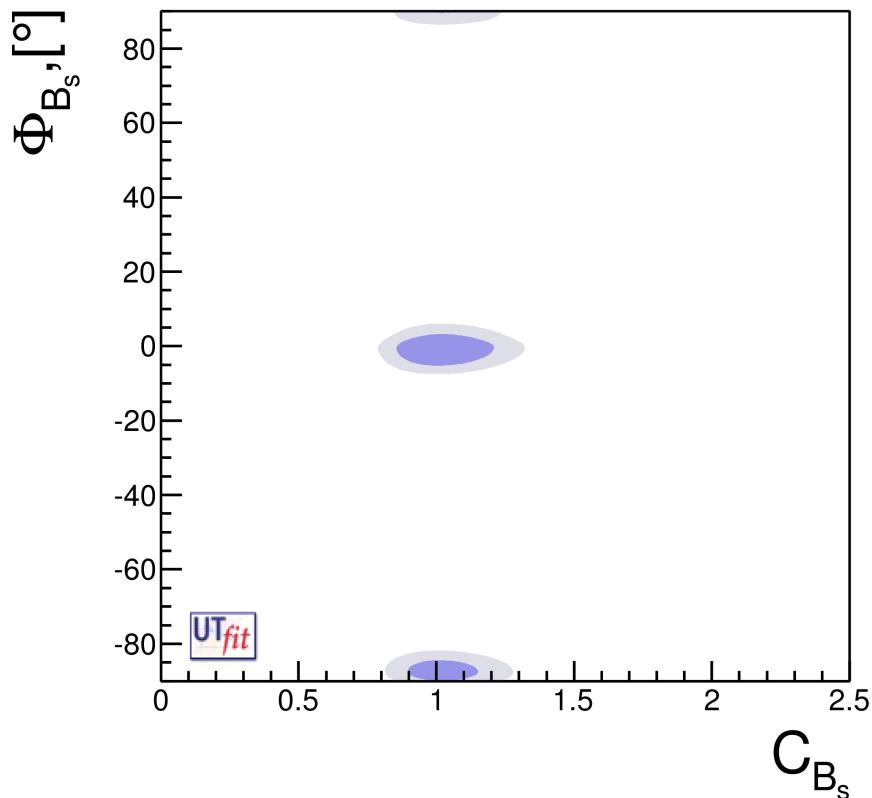
- $C_{\epsilon_K} = 0.97 \pm 0.15$
([0.70, 1.35] @ 95%
probability)

NP IN B_d MIXING



- $C_{B_d} = 0.94 \pm 0.14$
([0.70, 1.27] @ 95% probability)
- $\Phi_{B_d} = (-3.6 \pm 3.7)^\circ$
([-11, 3.7]° @ 95% probability)

NP IN B_s MIXING



- $C_{B_s} = 1.02 \pm 0.10$
([0.83,1.24] @ 95% probability)
- $\Phi_{B_s} = (-1.1 \pm 2.8)^\circ$
([-5,4.3]^\circ @ 95% probability)

The D0 dimuon asymmetry remains unexplained

A NOTE ON MEASURING β_s

- β_s is $O(\lambda^2)$, so must consider $O(\lambda^2)$ corrections to decay amplitudes, introducing unavoidable correlation with other CKM elements
- Subleading corrections can be controlled using suitable U-spin related control channels
- $B_s \rightarrow J/\Psi \phi$ is problematic since it has no simple control channels; $B_s \rightarrow KK$ look better

D- \bar{D} MIXING

- Established experimentally only in 2007
- Great experimental progress recently
- SM long distance contributions difficult to estimate, but solid prediction: no CPV in mixing
- Direct CPV possible in SCS decays (and recently observed by LHCb and CDF)

BASIC FORMULAE

- All mixing-related observables can be expressed in terms of $x = \Delta m / \Gamma$, $y = \Delta \Gamma / 2\Gamma$ and $|q/p|$, or better in terms of M_{12} , Γ_{12} and

$$\Phi_{12} = \arg(\Gamma_{12}/M_{12}):$$

$$|M_{12}| = \frac{1}{\tau_D} \sqrt{\frac{x^2 + \delta^2 y^2}{4(1 - \delta^2)}}, \quad |\Gamma_{12}| = \frac{1}{\tau_D} \sqrt{\frac{y^2 + \delta^2 x^2}{1 - \delta^2}}, \quad \sin \Phi_{12} = \frac{|\Gamma_{12}|^2 + 4|M_{12}|^2 - (x^2 + y^2)|q/p|^2/\tau_D^2}{4|M_{12}\Gamma_{12}|}$$

$$\delta = \frac{1 - |q/p|^2}{1 + |q/p|^2}, \quad \phi = \arg(q/p) = \arg(y + i\delta x), \quad A_M = \frac{|q/p|^4 - 1}{|q/p|^4 + 1}, \quad R_M = \frac{x^2 + y^2}{2}, \quad (1)$$

$$\begin{pmatrix} x'_f \\ y'_f \end{pmatrix} = \begin{pmatrix} \cos \delta_f & \sin \delta_f \\ -\sin \delta_f & \cos \delta_f \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}, \quad (x'_{\pm})_f = \left| \frac{q}{p} \right|^{\pm 1} (x'_f \cos \phi \pm y'_f \sin \phi), \quad (y'_{\pm})_f = \left| \frac{q}{p} \right|^{\pm 1} (y'_f \cos \phi \mp x'_f \sin \phi),$$

$$y_{\text{CP}} = \left(\left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) \frac{y}{2} \cos \phi - \left(\left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \frac{x}{2} \sin \phi, \quad A_{\Gamma} = \left(\left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \frac{y}{2} \cos \phi - \left(\left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) \frac{x}{2} \sin \phi,$$

$$R_D = \frac{\Gamma(D^0 \rightarrow K^+ \pi^-) + \Gamma(\bar{D}^0 \rightarrow K^- \pi^+)}{\Gamma(D^0 \rightarrow K^- \pi^+) + \Gamma(\bar{D}^0 \rightarrow K^+ \pi^-)}, \quad A_D = \frac{\Gamma(D^0 \rightarrow K^+ \pi^-) - \Gamma(\bar{D}^0 \rightarrow K^- \pi^+)}{\Gamma(D^0 \rightarrow K^+ \pi^-) + \Gamma(\bar{D}^0 \rightarrow K^- \pi^+)},$$

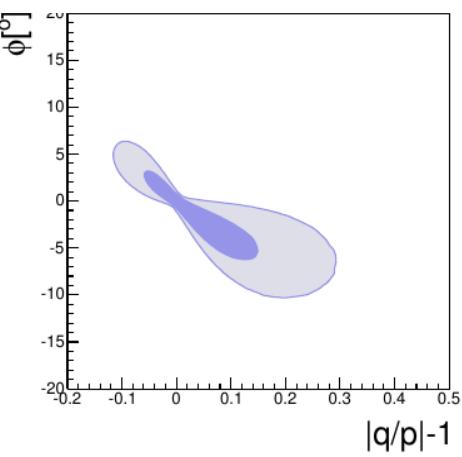
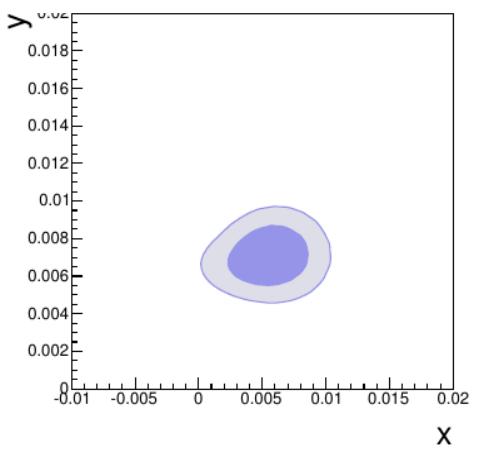
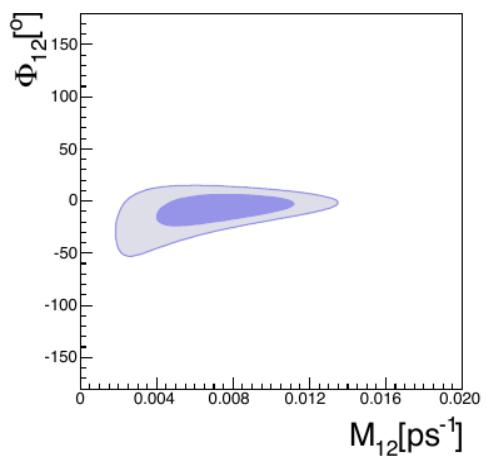
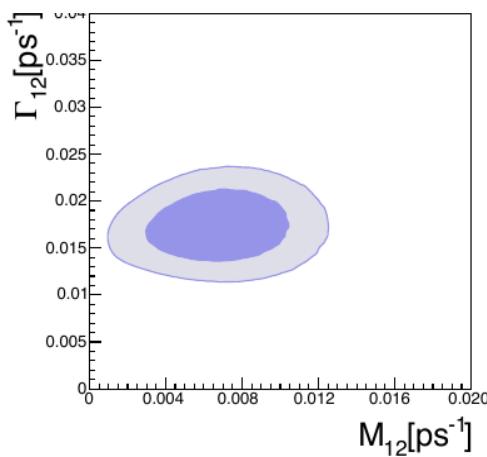
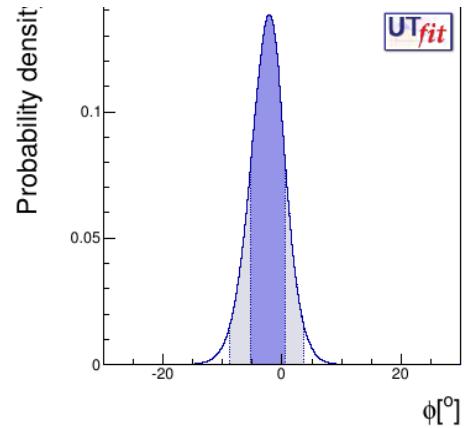
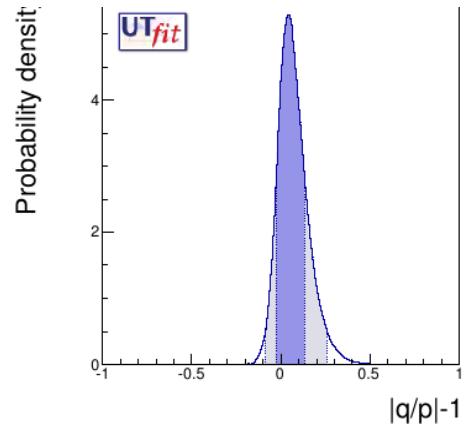
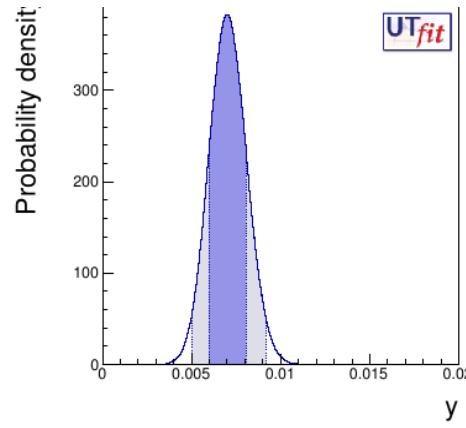
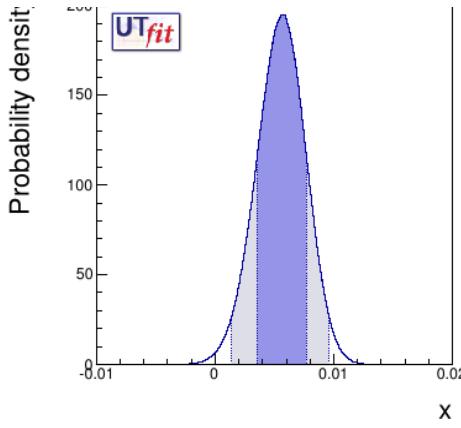
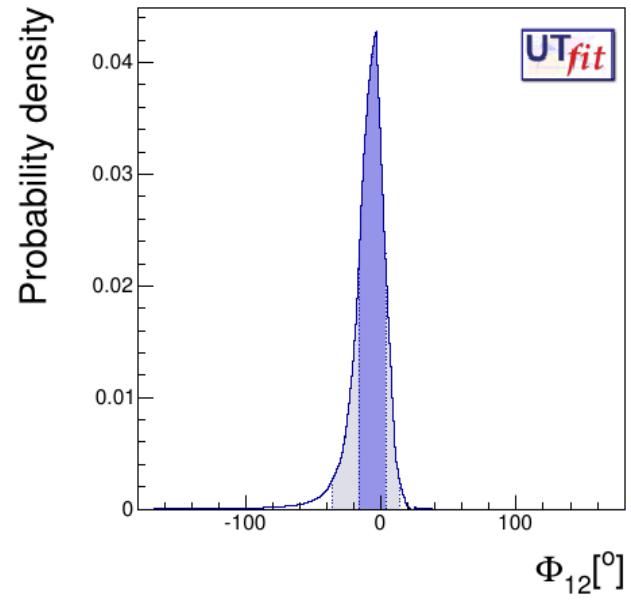
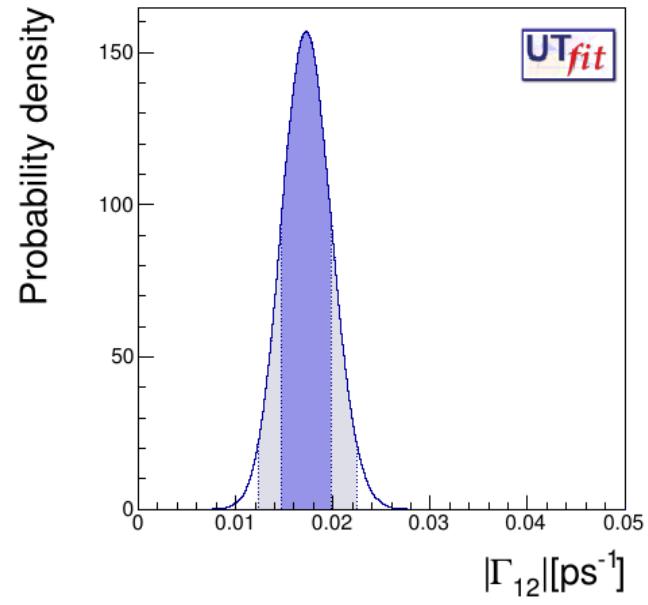
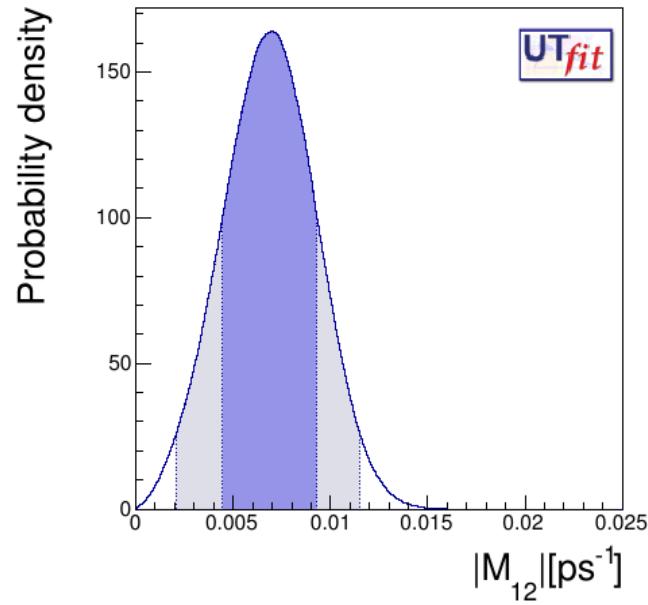
Experimental input from B-factories, CLEO-C, TeVatron and LHCb

Observable	Value	Correlation Coeff.				Reference
y_{CP}	$(0.866 \pm 0.155)\%$					[2] [17] [25]
A_Γ	$(0.022 \pm 0.161)\%$					[2] [20] [23] [26]
x	$(0.811 \pm 0.334)\%$	1	-0.007	-0.255α	0.216	[3]
y	$(0.309 \pm 0.281)\%$	-0.007	1	-0.019α	-0.280	[3]
$ q/p $	$(0.95 \pm 0.22 \pm 0.10)\%$	-0.255α	-0.019α	1	-0.128α	[3]
ϕ	$(-0.035 \pm 0.19 \pm 0.09)$	0.216	-0.280	-0.128α	1	[3]
x	$(0.16 \pm 0.23 \pm 0.12 \pm 0.08)\%$	1	0.0615			
y	$(0.57 \pm 0.20 \pm 0.13 \pm 0.07)\%$	0.0615	1			
R_M	$(0.0130 \pm 0.0269)\%$					[28] [32]
$(x'_+)_K\pi\pi^0$	$(2.48 \pm 0.59 \pm 0.39)\%$	1	-0.69			
$(y'_+)_K\pi\pi^0$	$(-0.07 \pm 0.65 \pm 0.50)\%$	-0.69	1			
$(x'_-)_K\pi\pi^0$	$(3.50 \pm 0.78 \pm 0.65)\%$	1	-0.66			
$(y'_-)_K\pi\pi^0$	$(-0.82 \pm 0.68 \pm 0.41)\%$	-0.66	1			
x^2	$(0.1549 \pm 0.2223)\%$	1	-0.6217	-0.00224	0.3698	0.01567
y	$(2.997 \pm 2.293)\%$	-0.6217	1	0.00414	-0.5756	-0.0243
R_D	$(0.4118 \pm 0.0948)\%$	-0.00224	0.00414	1	0.0035	0.00978
$2\sqrt{R_D} \cos \delta_{K\pi}$	$(12.64 \pm 2.86)\%$	0.3698	-0.5756	0.0035	1	0.0471
$2\sqrt{R_D} \sin \delta_{K\pi}$	$(-0.5242 \pm 6.426)\%$	0.01567	-0.0243	0.00978	0.0471	1
R_D	$(0.3030 \pm 0.0189)\%$	1	0.77	-0.87		
$(x'_+)_K\pi^2$	$(-0.024 \pm 0.052)\%$	0.77	1	-0.94		
$(y'_+)_K\pi$	$(0.98 \pm 0.78)\%$	-0.87	-0.94	1		
A_D	$(-2.1 \pm 5.4)\%$	1	0.77	-0.87		
$(x'_-)_K\pi^2$	$(-0.020 \pm 0.050)\%$	0.77	1	-0.94		
$(y'_-)_K\pi$	$(0.96 \pm 0.75)\%$	-0.87	-0.94	1		
R_D	$(0.364 \pm 0.018)\%$	1	0.655	-0.834		
$(x'_+)_K\pi^2$	$(0.032 \pm 0.037)\%$	0.655	1	-0.909		
$(y'_+)_K\pi$	$(-0.12 \pm 0.58)\%$	-0.834	-0.909	1		
A_D	$(2.3 \pm 4.7)\%$	1	0.655	-0.834		
$(x'_-)_K\pi^2$	$(0.006 \pm 0.034)\%$	0.655	1	-0.909		
$(y'_-)_K\pi$	$(0.20 \pm 0.54)\%$	-0.834	-0.909	1		
CP asymmetry	Value	$\Delta \langle t \rangle / \tau_{D^0}$				Reference
$A_{CP}(D^0 \rightarrow K^+ K^-)$	$(-0.24 \pm 0.24)\%$					[36] [37]
$A_{CP}(D^0 \rightarrow \pi^+ \pi^-)$	$(0.11 \pm 0.39)\%$					[36] [37]
ΔA_{CP}	$(-0.82 \pm 0.21 \pm 0.11)\%$	$(9.83 \pm 0.22 \pm 0.19)\%$				[9]
ΔA_{CP}	$(-0.62 \pm 0.21 \pm 0.10)\%$	$(26 \pm 1)\%$				[10]

FIT RESULTS

parameter	result @ 68% prob.	95% prob. range
$ M_{12} $ [1/ps]	$(6.9 \pm 2.4) \cdot 10^{-3}$	$[2.1, 11.5] \cdot 10^{-3}$
$ \Gamma_{12} $ [1/ps]	$(17.2 \pm 2.5) \cdot 10^{-3}$	$[12.3, 22.4] \cdot 10^{-3}$
Φ_{12} [°]	(-6 ± 9)	$[-37, 13]$
x	$(5.6 \pm 2.0) \cdot 10^{-3}$	$[1.4, 9.6] \cdot 10^{-3}$
y	$(7.0 \pm 1.0) \cdot 10^{-3}$	$[5.0, 9.1] \cdot 10^{-3}$
$ q/p - 1$	$(5.3 \pm 7.7) \cdot 10^{-2}$	$[-8.5, 25.6] \cdot 10^{-2}$
ϕ [°]	(-2.4 ± 2.9)	$[-8.8, 3.7]$
A_Γ	$(0.7 \pm 0.8) \cdot 10^{-3}$	$[-0.9, 2.3] \cdot 10^{-3}$
A_M	$(11 \pm 14) \cdot 10^{-2}$	$[-15, 44] \cdot 10^{-2}$
R_M	$(4.0 \pm 1.4) \cdot 10^{-5}$	$[1.7, 7.2] \cdot 10^{-5}$
R_D	$(3.27 \pm 0.08) \cdot 10^{-3}$	$[3.10, 3.44] \cdot 10^{-3}$
$\delta_{K\pi}$ [°]	(18 ± 12)	$[-14, 40]$
$\delta_{K\pi\pi^0}$ [°]	(31 ± 20)	$[-11, 73]$
$a_{\text{CP}}^{\text{dir}}(D^0 \rightarrow K^+ K^-)$	$(-2.6 \pm 2.2) \cdot 10^{-3}$	$[-7.1, 1.9] \cdot 10^{-3}$
$a_{\text{CP}}^{\text{dir}}(D^0 \rightarrow \pi^+ \pi^-)$	$(4.1 \pm 2.4) \cdot 10^{-3}$	$[-0.8, 9.0] \cdot 10^{-3}$
$\Delta a_{\text{CP}}^{\text{dir}}$	$(6.6 \pm 1.6) \cdot 10^{-3}$	$[-9.8, 3.5] \cdot 10^{-3}$

TABLE II. Results of the fit to D mixing data. $\Delta a_{\text{CP}}^{\text{dir}} = a_{\text{CP}}^{\text{dir}}(D^0 \rightarrow K^+ K^-) - a_{\text{CP}}^{\text{dir}}(D^0 \rightarrow \pi^+ \pi^-)$.



2. EFT analysis of $\Delta F=2$ transitions

The mixing amplitudes $A_q e^{2i\Phi_q} = \langle \bar{M}_q | H_{eff}^{\Delta F=2} | M_q \rangle$

$$H_{eff}^{\Delta B=2} = \sum_{i=1}^5 C_i(\mu) Q_i(\mu) + \sum_{i=1}^3 \tilde{C}_i(\mu) \tilde{Q}_i(\mu)$$

$$Q_1 = \bar{q}_L^\alpha \gamma_\mu b_L^\alpha \bar{q}_L^\beta \gamma^\mu b_L^\beta \quad (\text{SM/MFV})$$

$$Q_2 = \bar{q}_R^\alpha b_L^\alpha \bar{q}_R^\beta b_L^\beta$$

$$Q_4 = \bar{q}_R^\alpha b_L^\alpha \bar{q}_L^\beta b_R^\beta$$

$$\tilde{Q}_1 = \bar{q}_R^\alpha \gamma_\mu b_R^\alpha \bar{q}_R^\beta \gamma^\mu b_R^\beta$$

$$\tilde{Q}_2 = \bar{q}_L^\alpha b_R^\alpha \bar{q}_L^\beta b_R^\beta$$

$$Q_3 = \bar{q}_R^\alpha b_L^\beta \bar{q}_R^\beta b_L^\alpha$$

$$Q_5 = \bar{q}_R^\alpha b_L^\beta \bar{q}_L^\beta b_R^\alpha$$

$$\tilde{Q}_3 = \bar{q}_L^\alpha b_R^\beta \bar{q}_L^\beta b_R^\alpha$$

7 new operators beyond MFV involving quarks with different chiralities

H_{eff} can be recast in terms of
the $C_i(\Lambda)$ computed at the NP scale

- $C_i(\Lambda)$ can be extracted from the data (one by one)
- the associated NP scale Λ can be defined from

$$C_i(\Lambda) = \frac{LF_i}{\Lambda^2}$$

tree/strong interact. NP: $L \sim 1$
perturbative NP: $L \sim a_s^{-2}, a_w^{-2}$

Flavour structures:

MFV

- $F_1 = F_{SM} \sim (V_{tq} V_{tb}^*)^2$
- $F_{i \neq 1} = 0$

next-to-MFV

- $|F_{il}| \sim F_{SM}$
- arbitrary phases

generic

- $|F_{il}| \sim 1$
- arbitrary phases

present lower bound on the NP scale for
 $L=1$ and $F_i = 1$:

from ε_K : $4.9 \cdot 10^5$ TeV

from D mixing: $1.3 \cdot 10^4$ TeV

from B_d mixing: $3 \cdot 10^3$ TeV

from B_s mixing: $8 \cdot 10^2$ TeV

- * $\Delta F=2$ chirality-flipping operators are RG enhanced and thus probe larger NP scales
- * when these operators are allowed, the NP scale is easily pushed beyond the LHC reach
- * suppression of the $1 \leftrightarrow 2$ transitions strongly weakens the lower bounds

DIRECT CPV IN CHARM DECAYS

- Some basic facts known for a long time:
 - 1) To obtain a good description of SCS D BR's need:
 - final state interactions and corrections to factorization
 - sizable SU(3) breaking
 - 2) The SM expectation for direct CPV is $\lesssim 10^{-3}$

See for example Buccella et al. '95

EXPERIMENTAL STATUS

- Very recently, LHCb and CDF provided evidence of $\Delta A_{CP} = A_{CP}(K^+K^-) - A_{CP}(\pi^+\pi^-)$
- Combining LHCb, CDF and B-factories:

$$a_{CP}^{\text{dir}}(D^0 \rightarrow K^+K^-) \quad (-2.6 \pm 2.2) \cdot 10^{-3} \quad [-7.1, 1.9] \cdot 10^{-3}$$

$$a_{CP}^{\text{dir}}(D^0 \rightarrow \pi^+\pi^-) \quad (4.1 \pm 2.4) \cdot 10^{-3} \quad [-0.8, 9.0] \cdot 10^{-3}$$

$$\Delta a_{CP}^{\text{dir}} \quad (6.6 \pm 1.6) \cdot 10^{-3} \quad [-9.8, 3.5] \cdot 10^{-3}$$

well above the 10^{-3} barrier...

THEORY QUESTIONS

- Can we envisage a mechanism to enhance the SM prediction for CPV by one order of magnitude to reproduce the exp result?

Brod, Kagan & Zupan '11; Pirtskhalava & Uttayarat '11;
Bhattacharya, Gronau & Rosner '12; Cheng & Chiang '12;
Brod, Grossman, Kagan & Zupan '12

- Can anything analogous to the $\Delta I = 1/2$ rule take place in SCS charm decays?

Golden & Grinstein, '89

ISOSPIN & UNITARITY

- Let us start from the basic knowledge:
 - SU(3) breaking is large \Rightarrow use only isospin
 - corrections to factorization are large \Rightarrow use a general parameterization
 - final state interactions are important \Rightarrow implement unitarity & external info on rescattering

Franco, Mishima & LS '12

ISOSPIN AMPLITUDES

$$A(D^+ \rightarrow \pi^+ \pi^0) = \frac{\sqrt{3}}{2} \mathcal{A}_2^\pi ,$$

$r_{CKM} = 6.4 \cdot 10^{-4}$

$$A(D^0 \rightarrow \pi^+ \pi^-) = \frac{\mathcal{A}_2^\pi - \sqrt{2}(\mathcal{A}_0^\pi + ir_{CKM}\mathcal{B}_0^\pi)}{\sqrt{6}} ,$$

$$A(D^0 \rightarrow \pi^0 \pi^0) = \frac{\sqrt{2}\mathcal{A}_2^\pi + \mathcal{A}_0^\pi + ir_{CKM}\mathcal{B}_0^\pi}{\sqrt{3}} ,$$

A CP-even
B CP-odd

$$A(D^+ \rightarrow K^+ \bar{K}^0) = \frac{\mathcal{A}_{13}^K}{2} + \mathcal{A}_{11}^K + ir_{CKM}\mathcal{B}_{11}^K ,$$

$$A(D^0 \rightarrow K^+ K^-) = \frac{-\mathcal{A}_{13}^K + \mathcal{A}_{11}^K - \mathcal{A}_0^K + ir_{CKM}\mathcal{B}_{11}^K - ir_{CKM}\mathcal{B}_0^K}{2} ,$$

$$A(D^0 \rightarrow K^0 \bar{K}^0) = \frac{-\mathcal{A}_{13}^K + \mathcal{A}_{11}^K + \mathcal{A}_0^K + ir_{CKM}\mathcal{B}_{11}^K + ir_{CKM}\mathcal{B}_0^K}{2} .$$

NUMERICAL RESULTS FROM BR's

$$|\mathcal{A}_2^\pi| = (3.08 \pm 0.08) \times 10^{-7} \text{ GeV},$$

$$|\mathcal{A}_0^\pi| = (7.6 \pm 0.1) \times 10^{-7} \text{ GeV},$$

$$\arg(\mathcal{A}_2^\pi / \mathcal{A}_0^\pi) = (\pm 93 \pm 3)^\circ.$$

No $\Delta I=1/2$ rule for D decays, large strong phases

$$|\mathcal{A}_{13}^K - \mathcal{A}_{11}^K - \mathcal{A}_0^K| = (5.0 \pm 0.4) \times 10^{-7} \text{ GeV}$$

Should vanish in the SU(3) limit, but is O(1)!!

UNITARITY CONSTRAINTS

$$S = \left(\begin{array}{c|cccc} D \rightarrow D & D \rightarrow \pi\pi & D \rightarrow KK & \cdots \\ \hline \pi\pi \rightarrow D & \pi\pi \rightarrow \pi\pi & \pi\pi \rightarrow KK & \cdots \\ KK \rightarrow D & KK \rightarrow \pi\pi & KK \rightarrow KK & \cdots \\ \vdots & \vdots & \vdots & \ddots \end{array} \right) \equiv \left(\begin{array}{cc} 1 & -i(T)^T \\ -i \text{CP}(T) & S_S \end{array} \right)$$

implies

$$T^R = S_S(T^R)^*, \quad T^I = S_S(T^I)^*$$

Elastic case: $S = e^{2i\delta} \Rightarrow$ Watson theorem:

$$T^R = |T^R|e^{i\delta}, \quad T^I = |T^I|e^{i\delta}$$

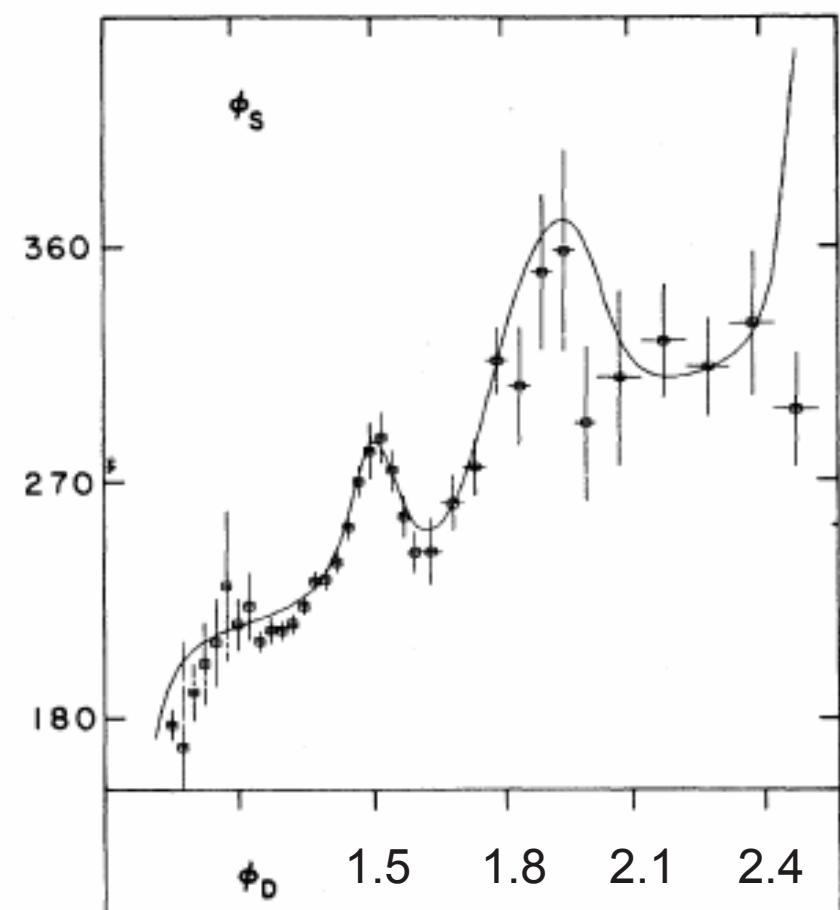
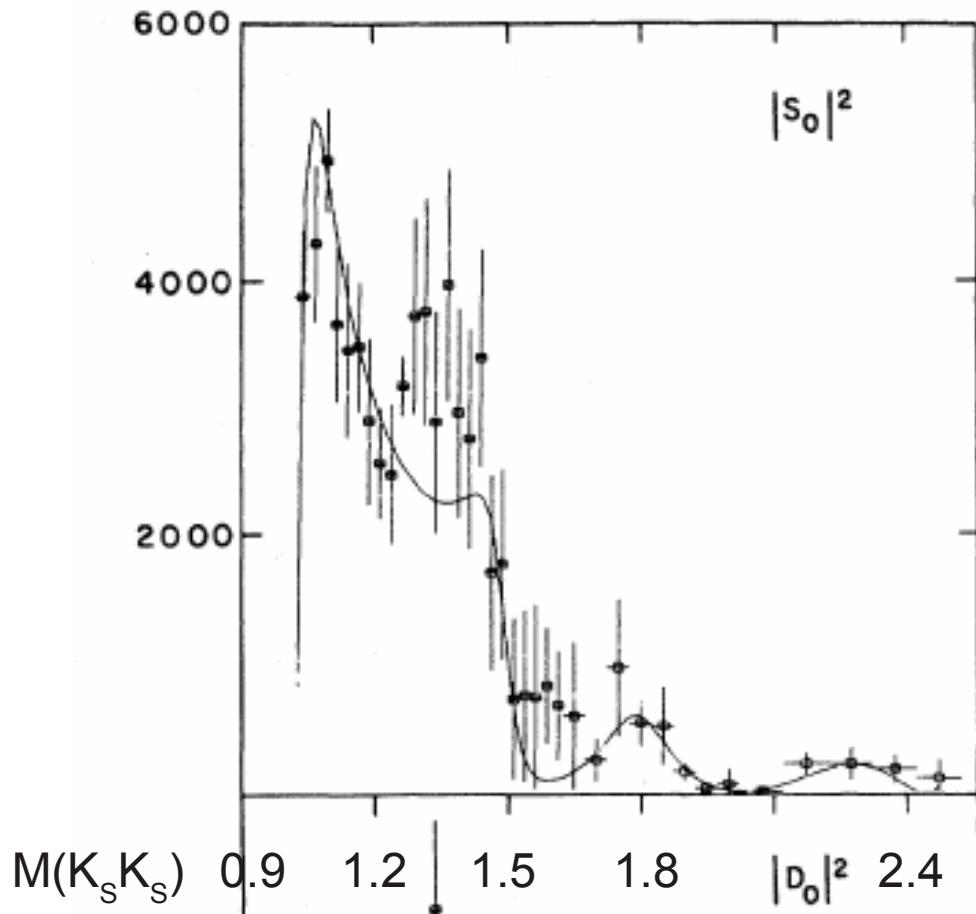
2-CHANNEL UNITARITY

$$\begin{pmatrix} \mathcal{A}_0^\pi \\ \mathcal{A}_0^K \end{pmatrix} = \begin{pmatrix} \eta e^{2i\delta_1} & \pm i\sqrt{1-\eta^2} e^{i(\delta_1+\delta_2)} \\ \pm i\sqrt{1-\eta^2} e^{i(\delta_1+\delta_2)} & \eta e^{2i\delta_2} \end{pmatrix} \begin{pmatrix} (\mathcal{A}_0^\pi)^* \\ (\mathcal{A}_0^K)^* \end{pmatrix}$$

Obtain constraints on magnitudes and phases of amplitudes

For η close to 1, magnitudes almost unconstrained but phases close to δ_1 and δ_2

Is the 2-channel S-matrix unitary at the D mass?



Etkin et al. '82

S_{12} has small amplitude and small phase.

Is this compatible with measured S_{11} ?

Unfortunately, πN
 scattering
 alone is ambiguous;
 different
 fits corresponding
 to discrete
 ambiguities yield
 widely
 different results
 close to the
 D mass. 2- and 3-
 channel unitarity
 possible.

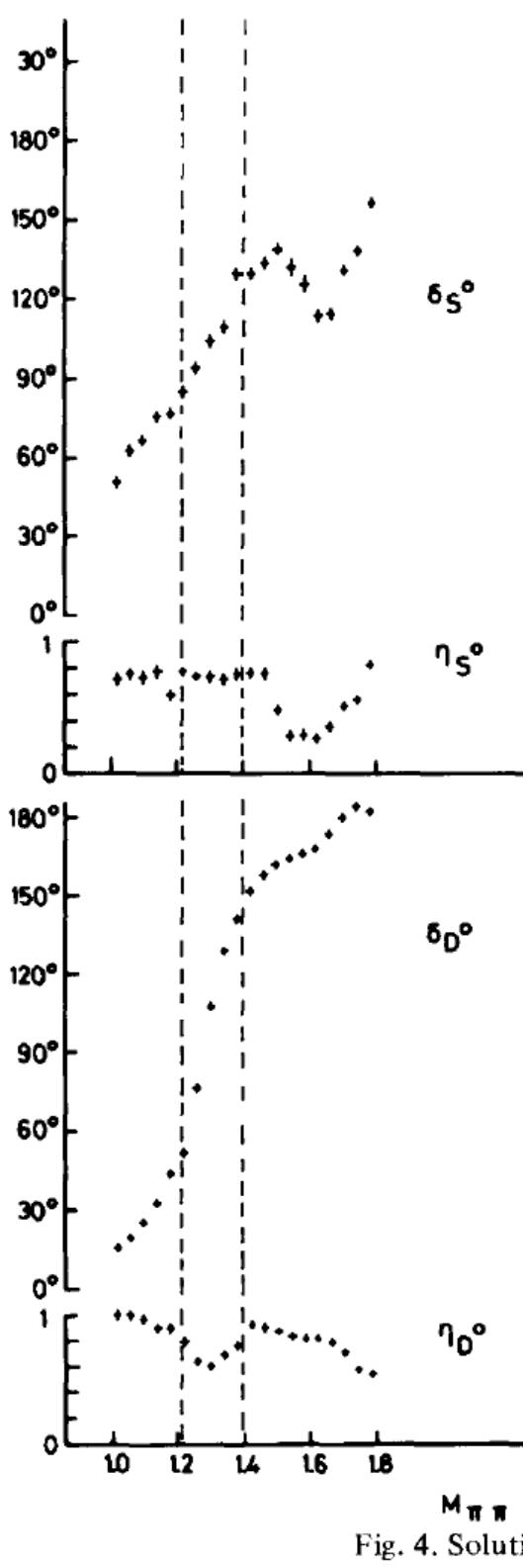


Fig. 4. Soluti

Hyams et al. '73

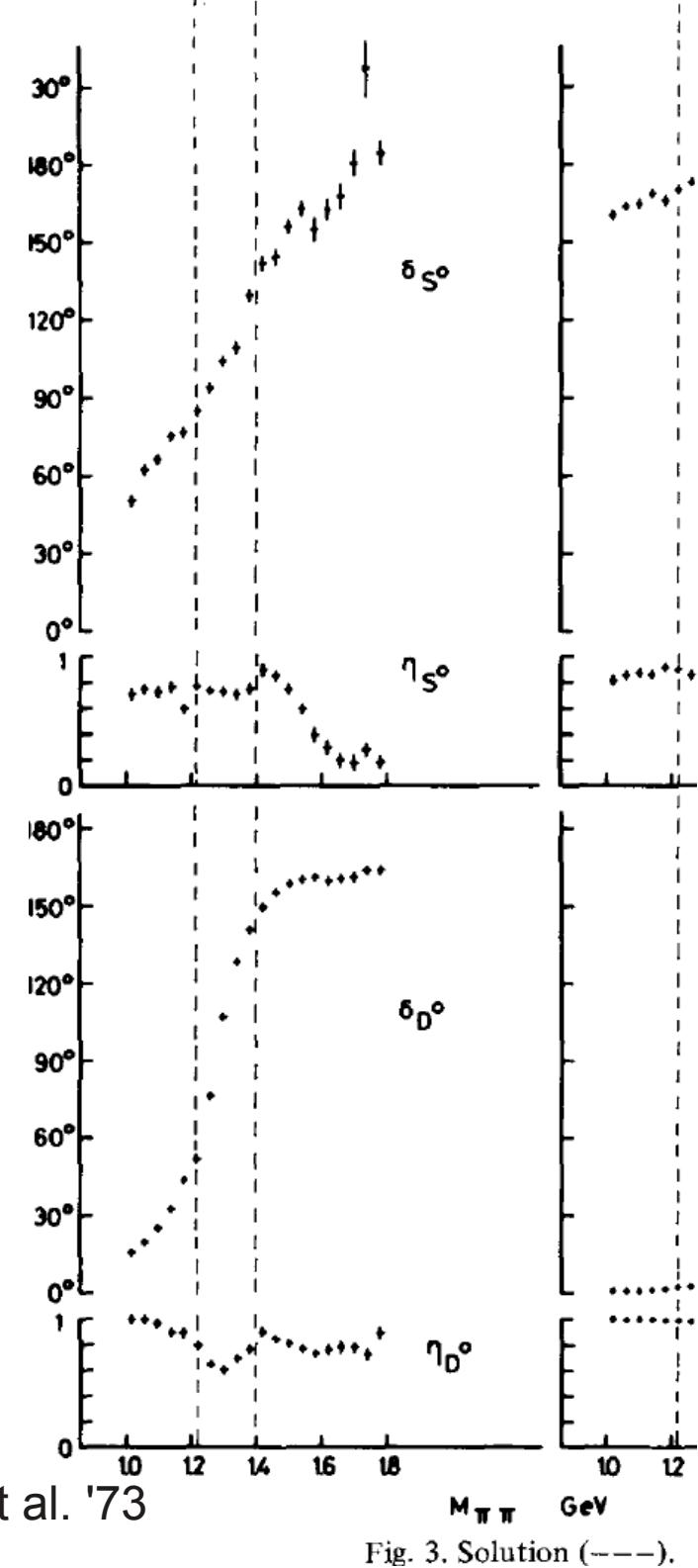


Fig. 3. Solution (---).

CP ASYMMETRIES

- One can study the CP asymmetries as a function of the upper bound on the size of CPV contributions in the two- and three-channel scenarios. We write

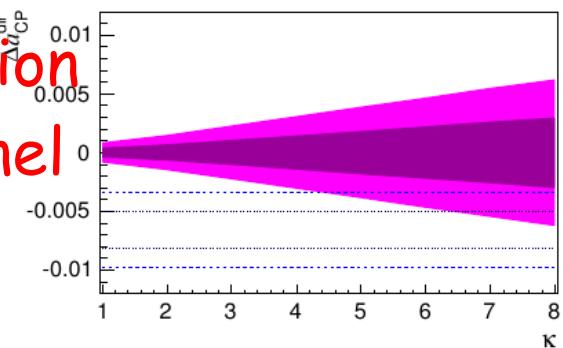
$$|\mathcal{B}_0^\pi| < \kappa |\mathcal{A}_0^\pi|,$$

$$|\mathcal{B}_0^K - \mathcal{A}_0^K| < \kappa |\mathcal{A}_0^K|,$$

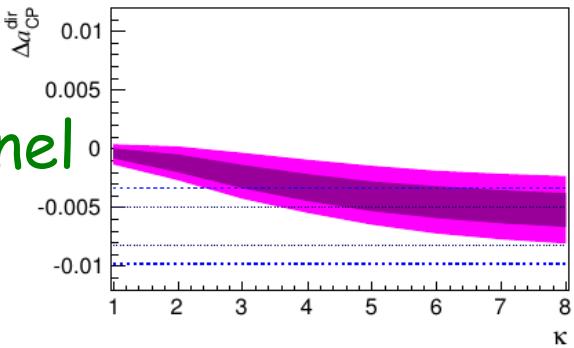
$$|\mathcal{B}_{11}^K - (\mathcal{A}_{11}^K - \mathcal{A}_{13}^K)| < \kappa |\mathcal{A}_{11}^K - \mathcal{A}_{13}^K|,$$

and consider predictions and fit results for CP asymmetries

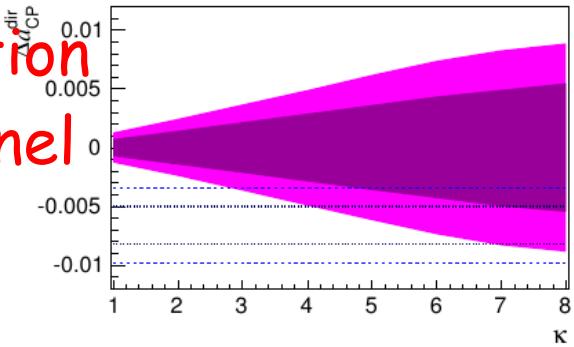
Prediction
2-channel



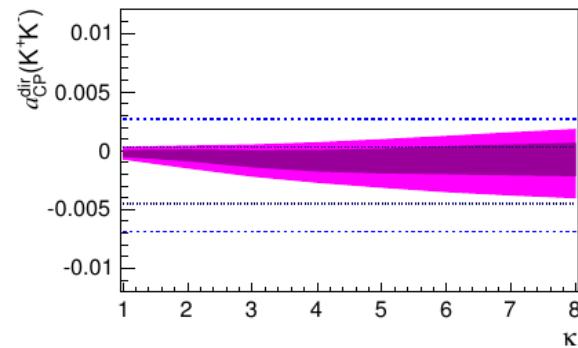
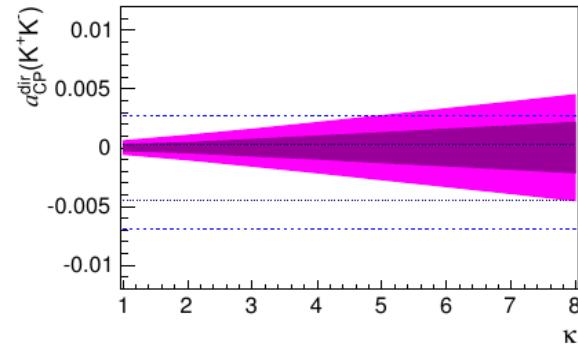
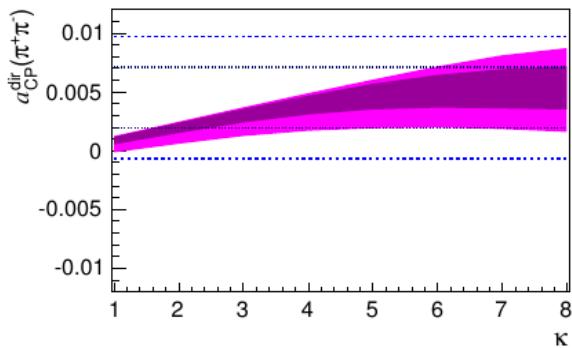
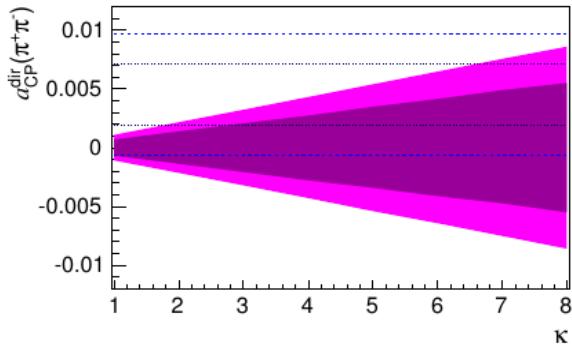
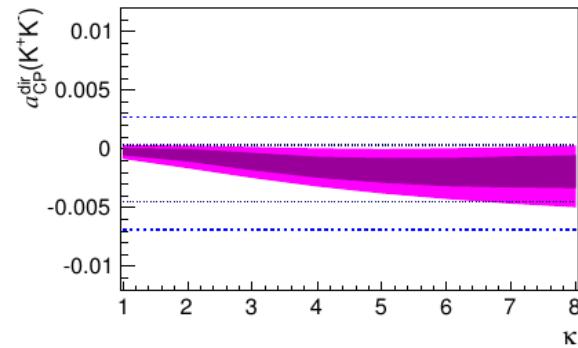
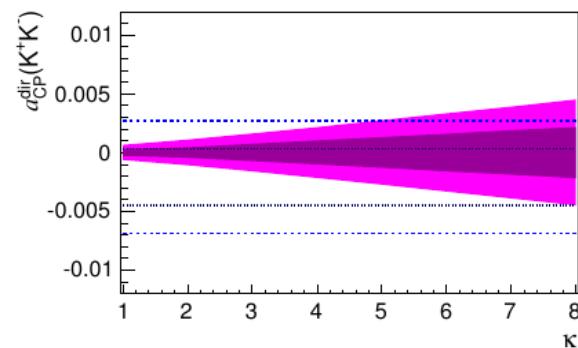
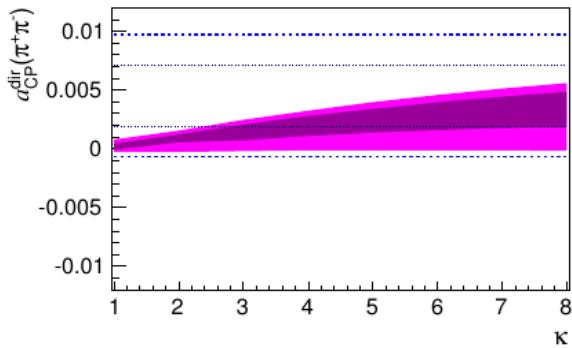
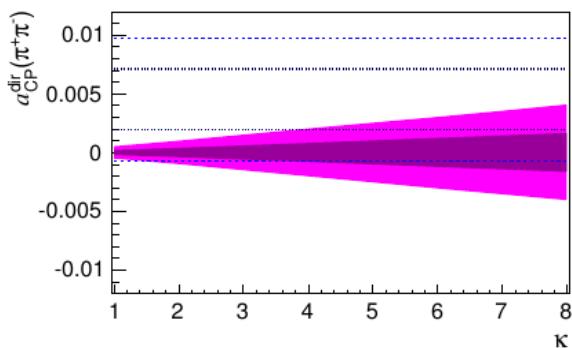
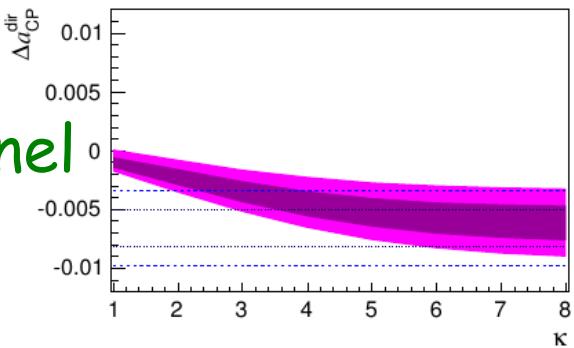
Fit
2-channel



Prediction
3-channel



Fit
3-channel



CONCLUSIONS FROM UNITARITY

- The prediction does not reach the exp value within 2σ even for $\kappa=8$ in the 2-channel case
- Without unitarity constraints, the prediction reaches the exp value at the 2σ level for $\kappa>5$, but even for $\kappa=8$ it is still 1σ below
- How large can κ be?
 - translate fit results into RGI parameters
 - compare with K and B

FROM ISOSPIN AMPLITUDES TO RGI PARAMETERS

- The BR fit results can be translated into results for RGI parameters (aka topologies). Neglecting for simplicity $O(1/N_c^2)$ terms:

$$E_1(\pi) + E_2(\pi) = (1.72 \pm 0.04) \times 10^{-6} e^{i\delta} \text{ GeV},$$

$$E_1(\pi) + A_2(\pi) - P_1^{\text{GIM}}(\pi) = (2.10 \pm 0.02) \times 10^{-6} e^{i(\delta \pm (71 \pm 3)^\circ)} \text{ GeV},$$

$$E_2(\pi) - A_2(\pi) + P_1^{\text{GIM}}(\pi) = (2.25 \pm 0.07) \times 10^{-6} e^{i(\delta \mp (62 \pm 2)^\circ)} \text{ GeV}$$

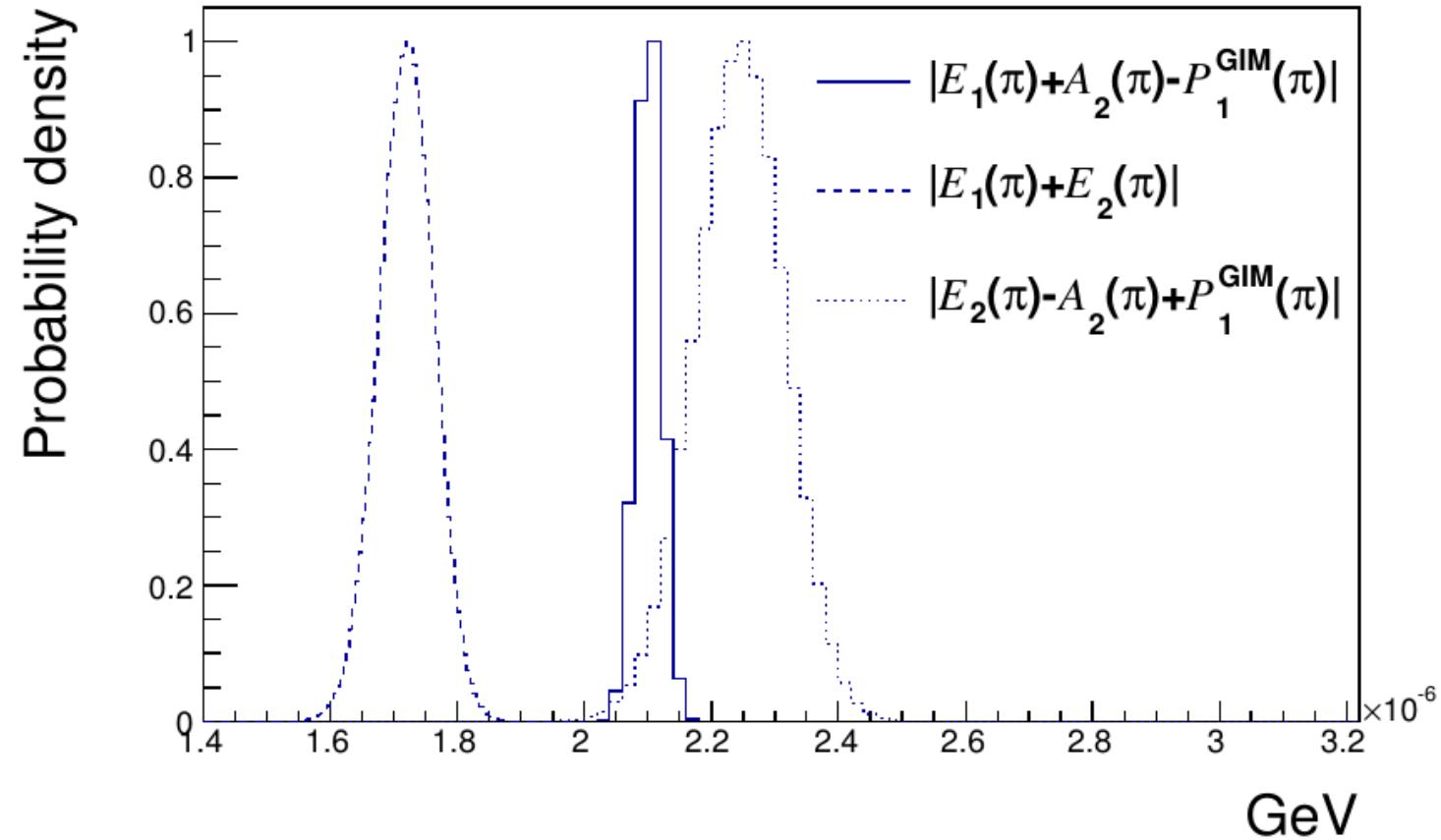
- E_1 does not dominate the amplitudes \Rightarrow we are away from the infinite mass limit
- All amplitudes of same size, w. large phases

THE MEANING OF κ

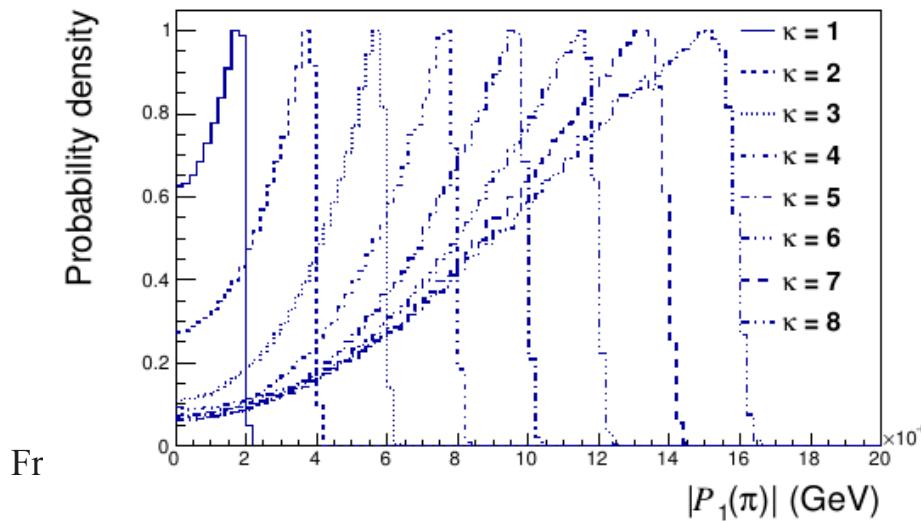
- The condition $|\mathcal{B}_0^\pi| < \kappa |\mathcal{A}_0^\pi|$, means

$$|P_1(\pi)| \leq \kappa \left| \frac{2}{3}E_1(\pi) - \frac{1}{3}E_2(\pi) + A_2(\pi) - P_1^{\text{GIM}}(\pi) \right|$$

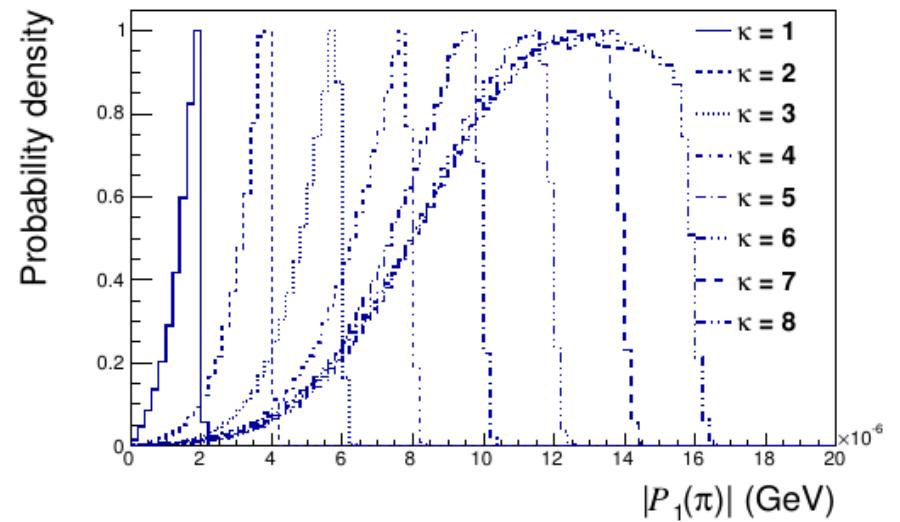
- κ is the ratio of $|P_1|$ over all other topologies
- Notice that $P_1 \sim P_b - P_s$ while $P_1^{\text{GIM}} \sim P_d - P_s$
- How large should $|P_1|$ be to reproduce $\Delta a_{CP}^{\text{dir}}$?



2-channel



3-channel



DYNAMICAL ARGUMENTS

- The amplitudes for K, D and $B \rightarrow \pi\pi$ are formally the same, with the obvious flavour and CKM replacements.
- In the Kaon system, one has

$$(P_u - P_c) \sim 3 (P_+ - P_c) \sim 25 (E_1 + E_2)$$

- No enhancement expected for P_u (will be checked on the lattice soon), while P_c and P_+ generate local operators with chirally enhanced matrix elements (SVZ)

DYNAMICAL ARGUMENTS II

- In charm decays, no chiral enhancement is present, so that one expects

$$|P_1| = |P_b - P_s| \leq |E_1|, |E_2|, |A_1|, |A_2|, |P_1^{\text{GIM}}|$$

i.e. $\kappa \leq 1$.

- In B decays one is much closer to the infinite mass limit so that $|E_1|$ and $|E_2|$ dominate, with all other contractions power suppressed.

CONCLUSIONS

- The SM UTA has reached high precision and redundancy, allowing to test the SM and search for NP
- Overall picture consistent with the SM, with nonstandard CPV in $\Delta F=2$ possible at the few degrees level in all sectors
- Stringent bounds on the NP scale from $\Delta F=2$ processes

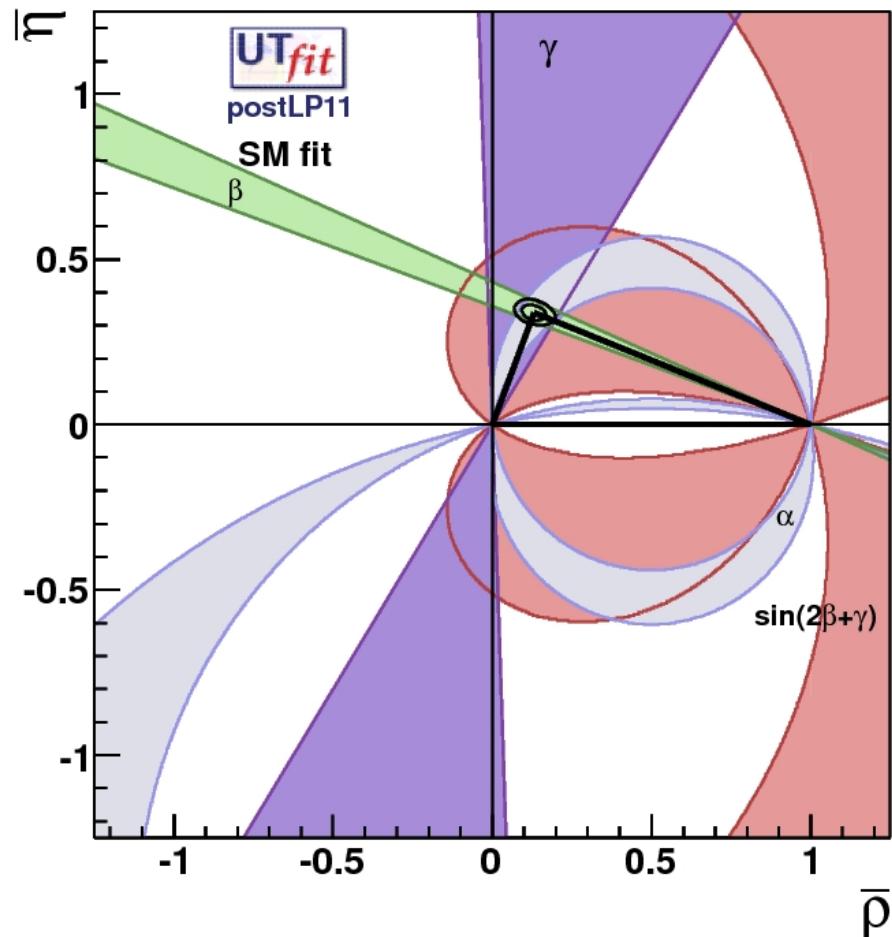
CONCLUSIONS II

- However, looking more closely there are several (unexpected) deviations from the SM at the $2\text{-}3\sigma$ level: $\sin 2\beta$, $B \rightarrow (D^{(*)})\tau\nu$, $\Delta A_{CP}, \dots$
- These deviations are not easily accommodated in simple NP models
- Direct searches are also telling us that simple NP models are unnatural
- Wait for more hints in the very near future!

BACKUP SLIDES

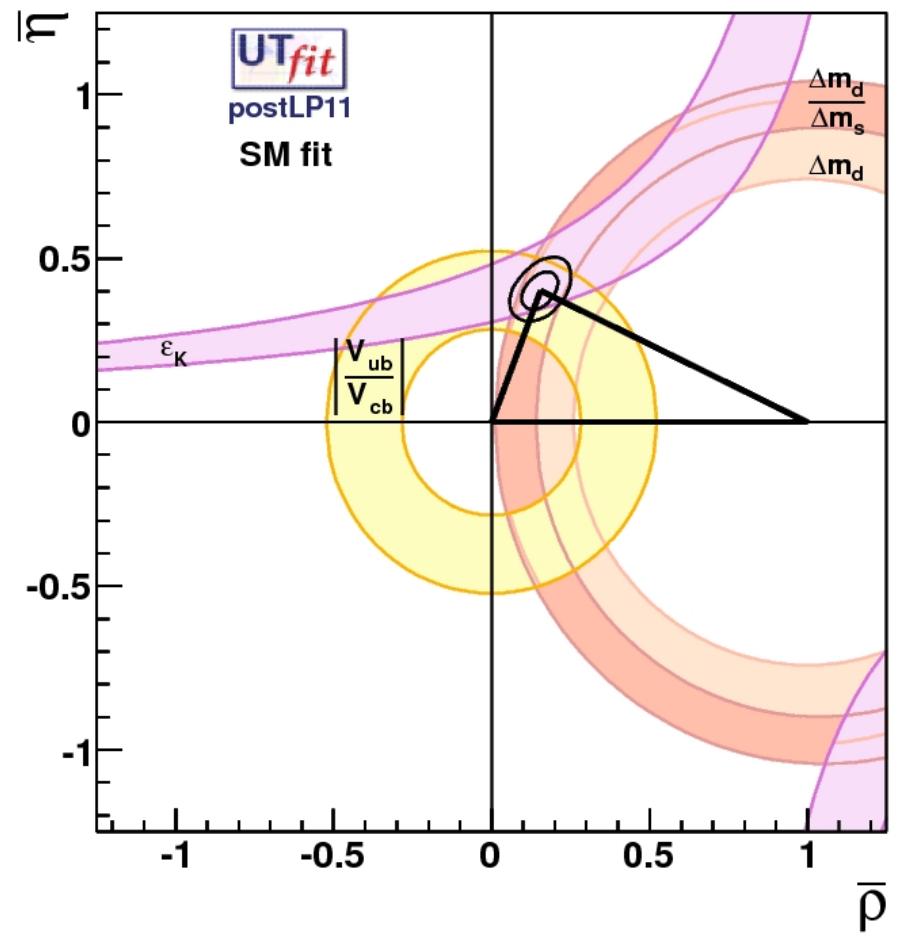
angles vs the others

levels @
95% Prob



$$\bar{\rho} = 0.130 \pm 0.027$$

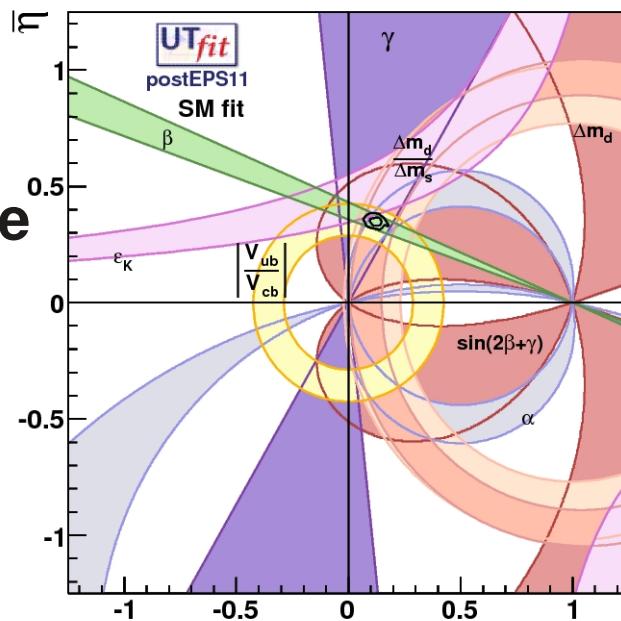
$$\bar{\eta} = 0.338 \pm 0.016$$



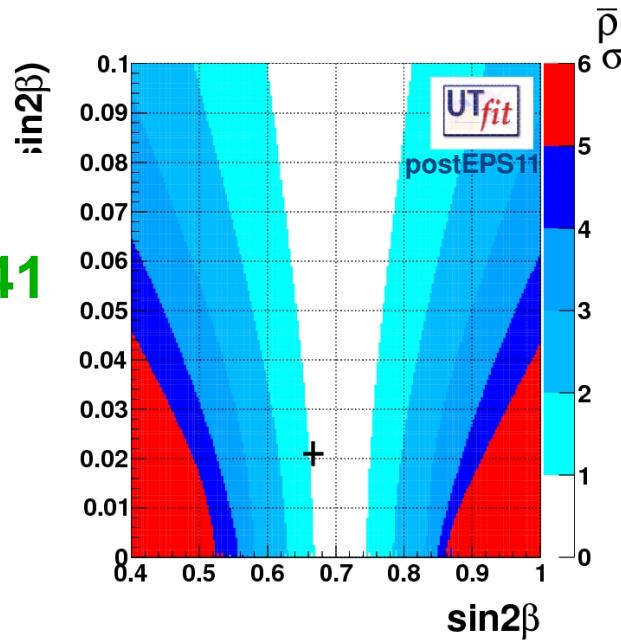
$$\bar{\rho} = 0.154 \pm 0.038$$

$$\bar{\eta} = 0.400 \pm 0.038$$

only
exclusive
values

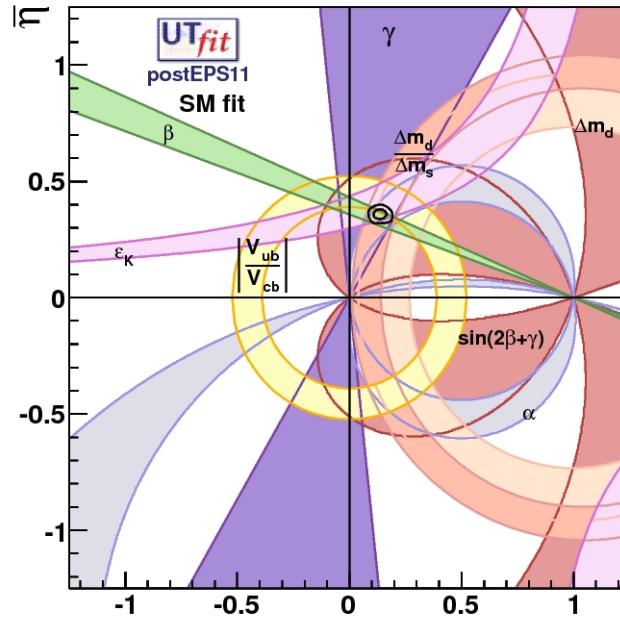


$$\sin 2\beta_{\text{UTfit}} = 0.706 \pm 0.041 \sim 0.8\sigma$$



$$\sin 2\beta_{\text{UTfit}} = 0.76 \pm 0.10 \rightarrow \text{no semileptonic}$$

only
inclusive
values



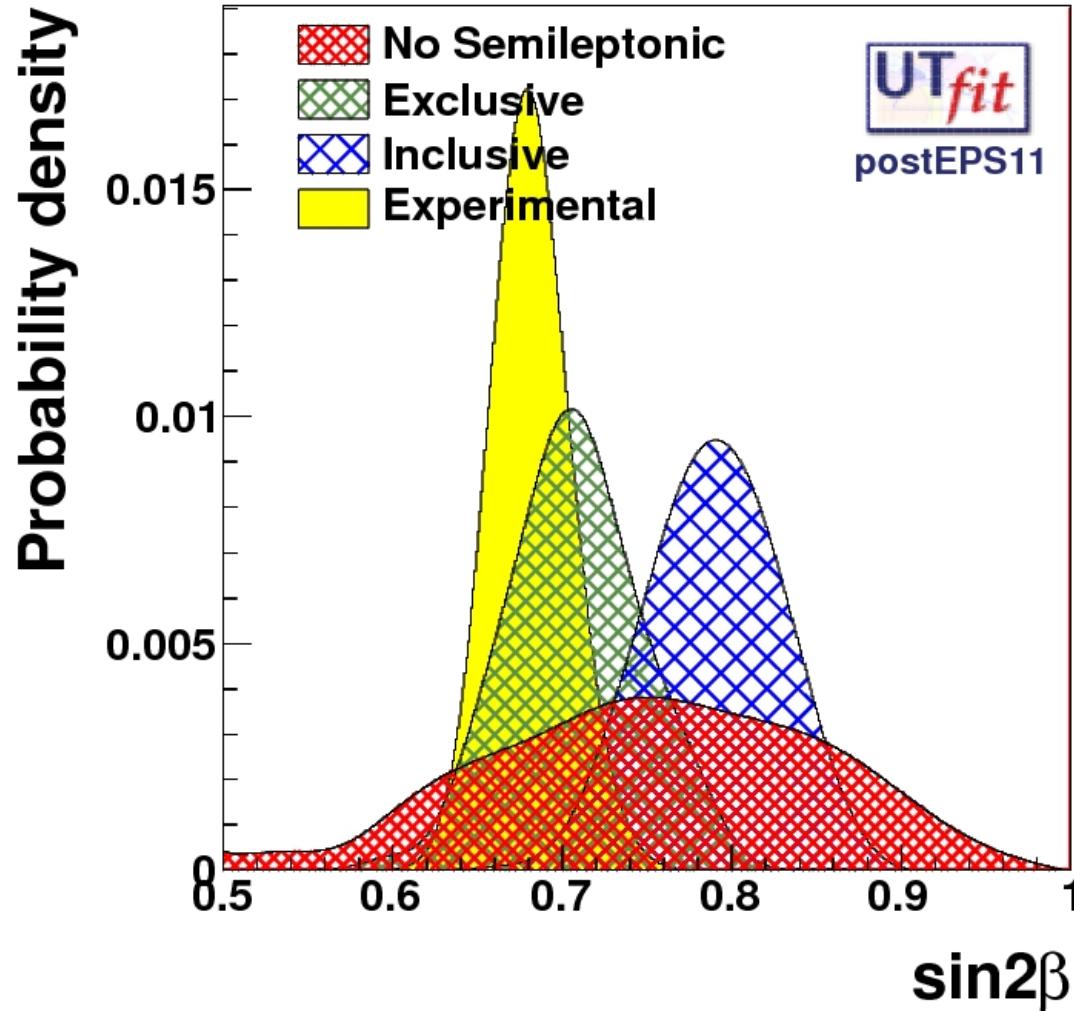
$$\sin 2\beta_{\text{UTfit}} = 0.791 \pm 0.041 \sim 2.6\sigma$$

inclusives vs exclusives

only
exclusive
values

$$\sin 2\beta_{\text{UTfit}} = 0.706 \pm 0.041$$

$\sim 0.8\sigma$



only
inclusive
values

$$\sin 2\beta_{\text{UTfit}} = 0.791 \pm 0.041$$

$\sim 2.6\sigma$

$$\sin 2\beta_{\text{UTfit}} = 0.76 \pm 0.10 \rightarrow \text{no semileptonic}$$

L. Silvestrini
 $\sim 0.9\sigma$