



CNAO2025: measurement of primary P

INFN Milano

Introduction and outline

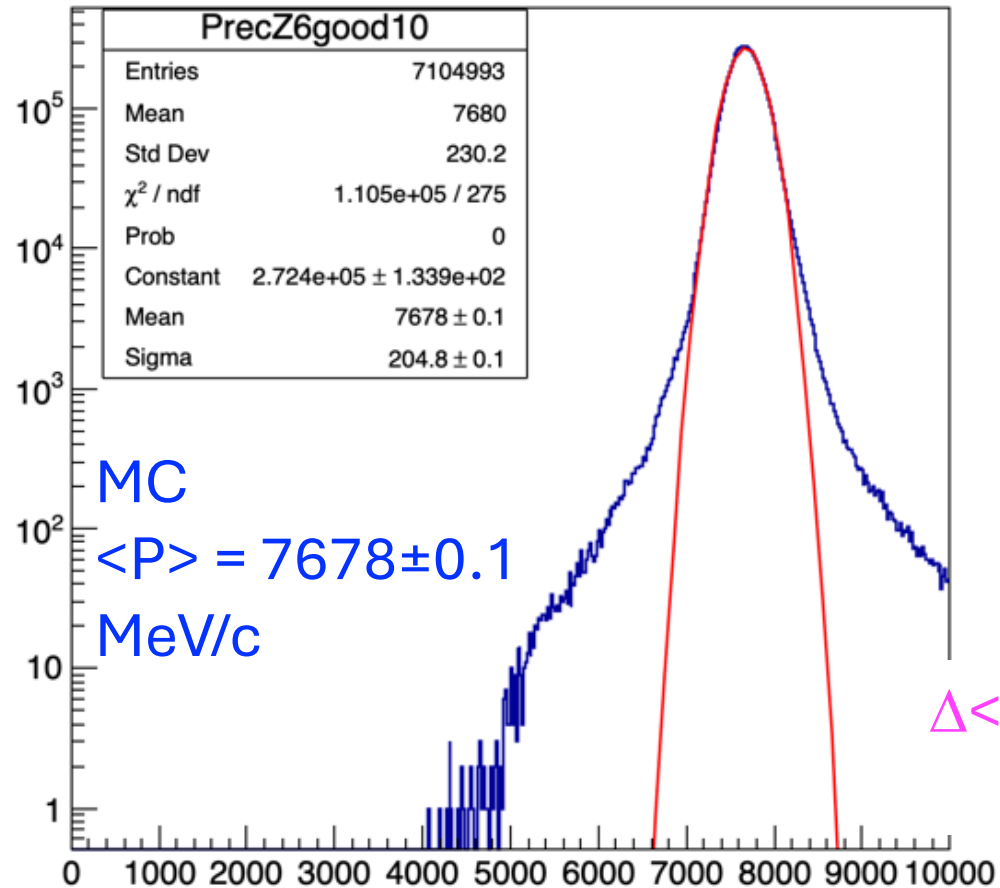
- At the last meeting we showed mass reconstruction from the combination of P and ToF for secondary fragments
- The need to correct for some P overestimation was confirmed
- The question of checking P reconstruction for the primary particles was left open. Here we present results on this subject
- Spoiler: **we might have some unexpected systematics**

1st Analysis: Runs with C target

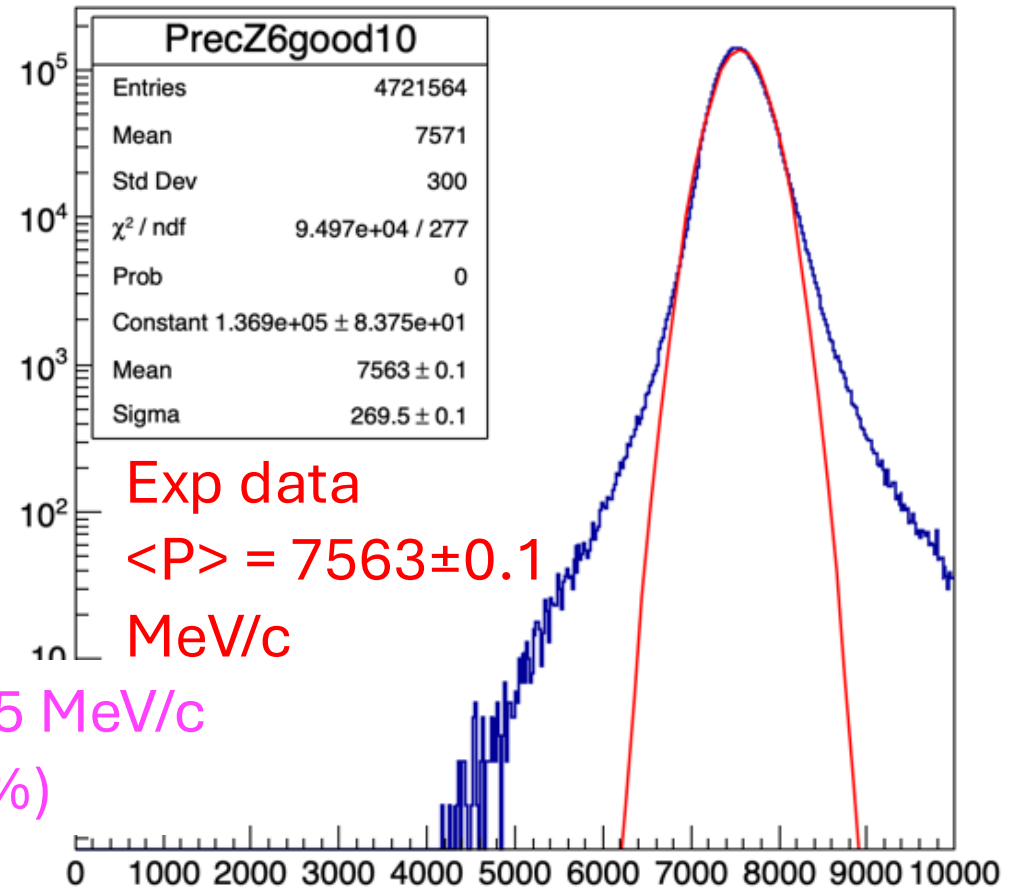
- Genfit reconstruction
- Event Selection: ≥ 1 reconstructed global track and $Z_{id} = 6$ in TW and MSD
- Tracks with ≥ 10 points
- P obtained from `glbtrck->GetTgtMomentum()` → in the case of primaries, momentum is estimated at the center of target

Data – MC comparison (C target)

Rec. P. Z=6



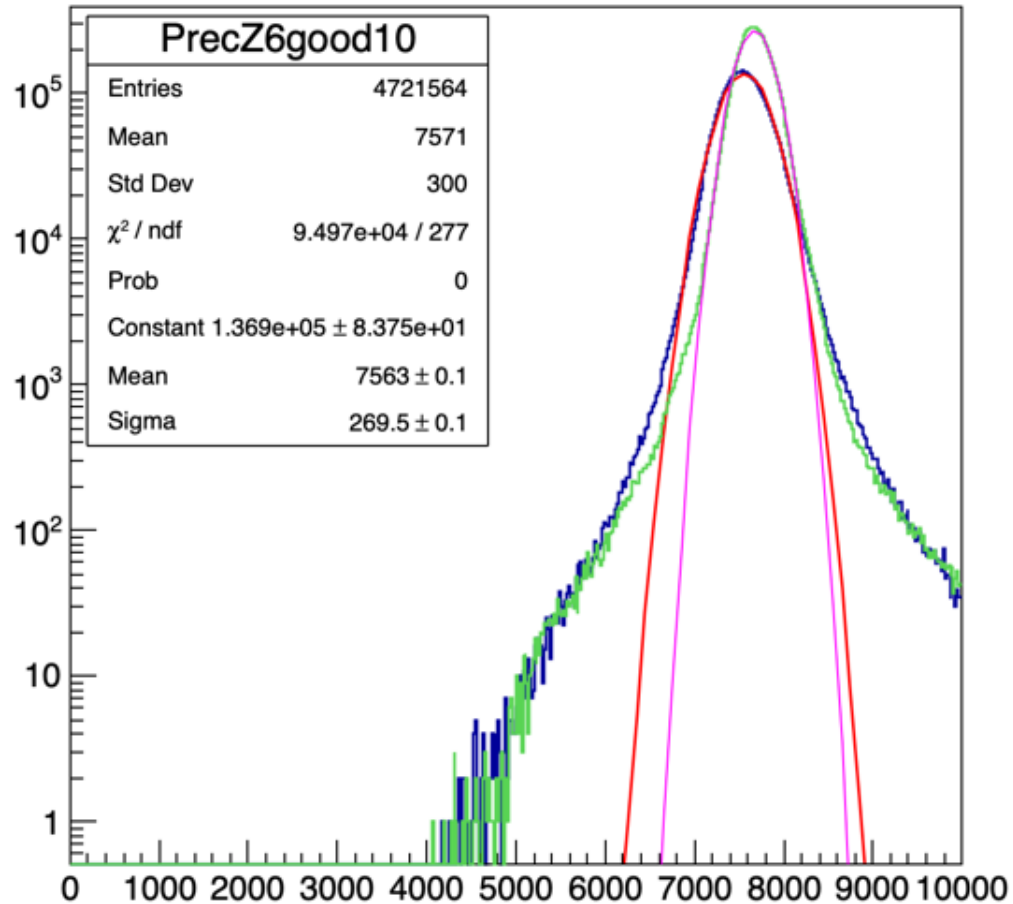
Rec. P. Z=6



$\Delta \langle P \rangle = 115 \text{ MeV/c}$
(1.5%)

We are assuming to have taken data at 200 MeV/u
(actually 200.61 MeV/u)

Rec. P. Z=6



Of course, MC follows the same assumption

Peak of Data corresponds to **193.2 MeV/u**

Peak of MC corresponds to **198.6 MeV/u**

$$\Delta E (\text{MC-Data}) = 5.4 \text{ MeV/u} \\ +2.7\%$$

(the relation between P and E is not linear)

Other observation:

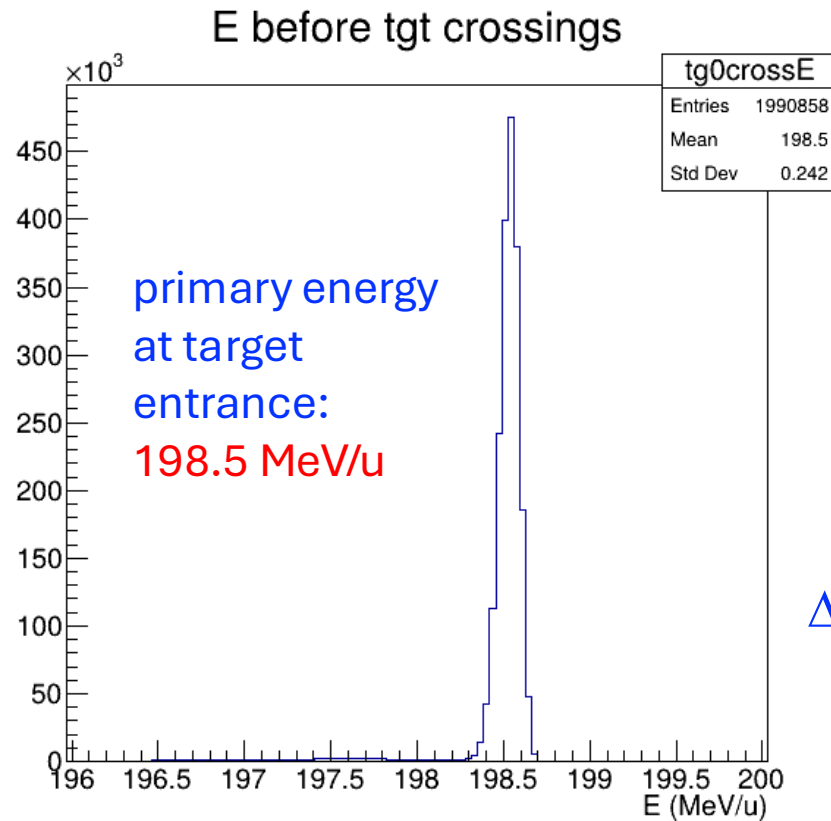
$$\sigma_P(\text{MC}) = 205 \text{ MeV/c}$$

$$\sigma_P(\text{Data}) = 270 \text{ MeV/c}$$

But in the following we shall discuss
only the ΔE issue

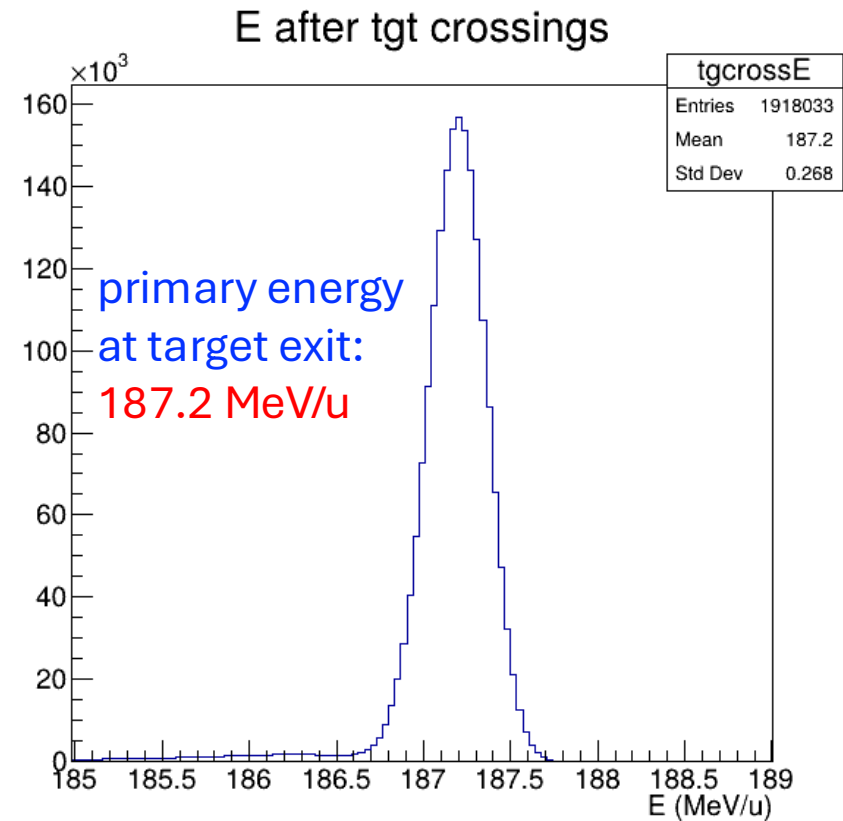
Question 1: is the MC consistent?

Starting from the assumed energy value in the beam pipe (200.61 MeV/u)



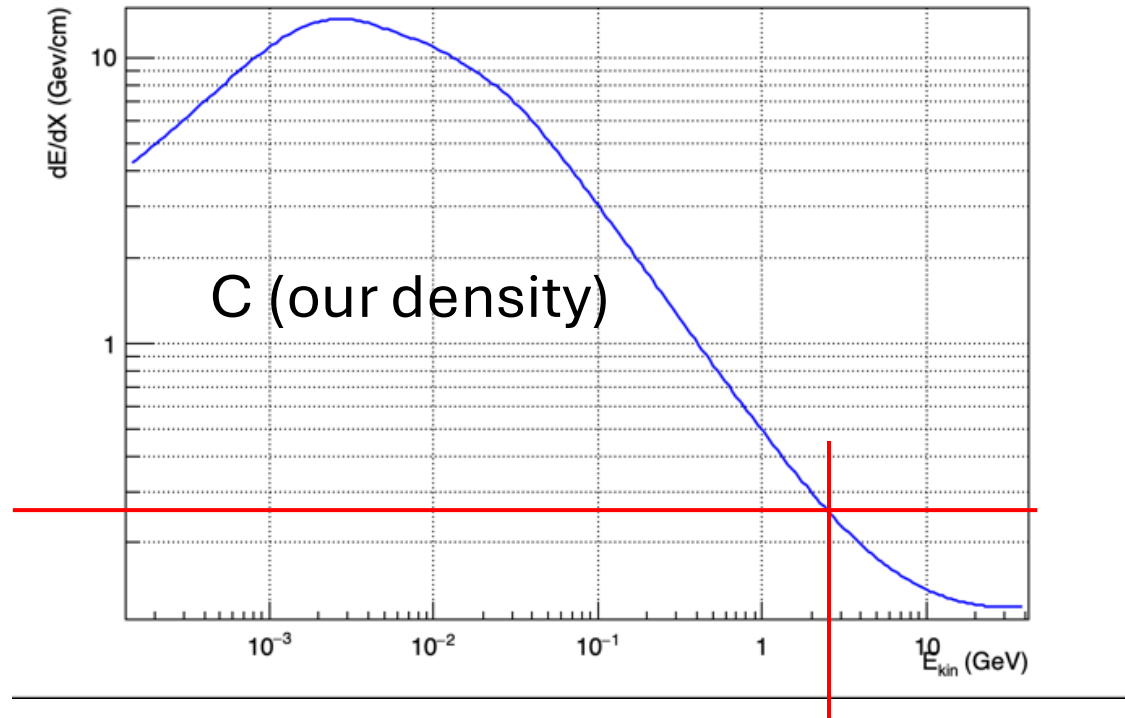
MC truth

$\Delta E = 11.3 \text{ MeV/u}$



At target center → E = 192.9 MeV/u

dE/dx vs total E_{kin} for ¹²C in C



At 200 MeV/u (2400 MeV): $dE/dx \sim 266$ MeV (total)/cm = 26.6 MeV/mm \sim 2.2 MeV/u/mm

→ Energy loss in target is consistent

→ Energy at target center ~ 192.8 MeV/u → $P \sim 7553.9$ MeV/c

→ $E_{rec} = 198.6$ MeV/u, $P_{rec} = 7678$ MeV/c, but we already know (from previous analyses) that Rec. P is overestimated by 1 - 2%

→ the MC reconstruction is consistent

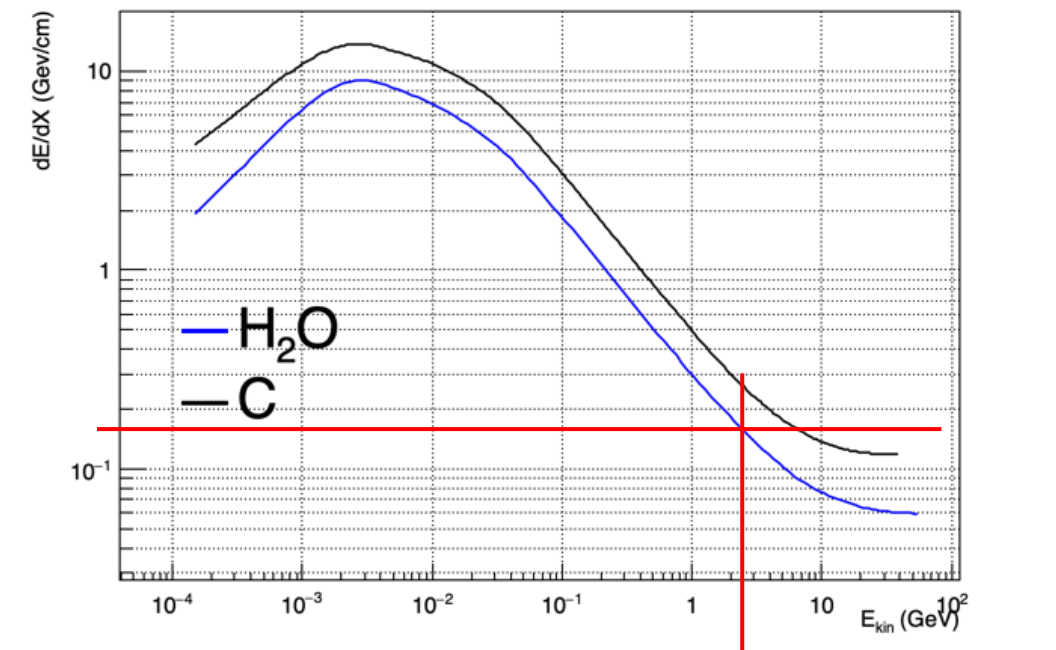
Question 2: is the MC input energy assumption correct?

Warning: at present we are not considering the C-fiber window at beam exit of the beam pipe

C-fiber window estimated to be equivalent to ~ 1 mm H_2O

(M. Pullia, private communication)

dE/dx vs total E_{kin} of ^{12}C in C and H_2O



At 200 MeV/u (2400 MeV): $dE/dx \sim 160$ MeV (total)/cm = 16 MeV/mm ~ 1.3 (MeV/u)/mm
 \rightarrow this is not enough to reconcile MC and data (you would need ~ 196 MeV/u at the entrance of ST and ~ 194.6 MeV at Target entrance)

Something more about the energy assumption

From CNAO ^{12}C beam library

Energy (MeV/u)	mm H_2O
195.18	80
197.91	82
200.61	84
203.29	86
205.95	88

A step of Bragg peak position of 2 mm corresponds to a change of energy of the order of ~ 2.7 MeV/u



Our nominal energy at CNAO2025



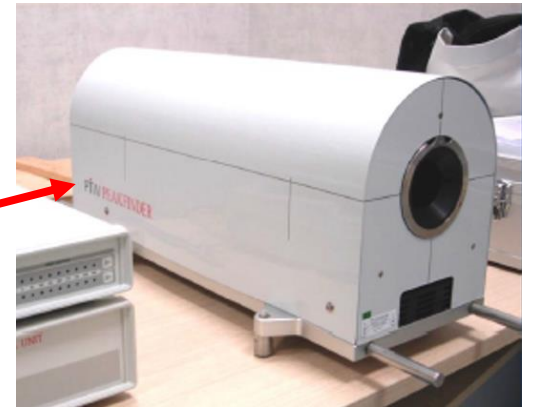
These values are supposed to be the energy in the beam pipe



According to the convention used at CNAO, this number represents the position of Bragg Peak

→ Bragg Peak position in Water is what was actually measured during the commissioning

Bragg Peak measurement at CNAO



At CNAO, to measure the Bragg peak, a PTW "peak finder" is used. It measures the ratio between an entrance chamber and a depth chamber in a "water column" (variable position with excellent resolution in the order of 10 microns)

- The peak finder is placed at the isocenter.
- **Dose delivery is in and with carbon, ripple filters are inserted.**

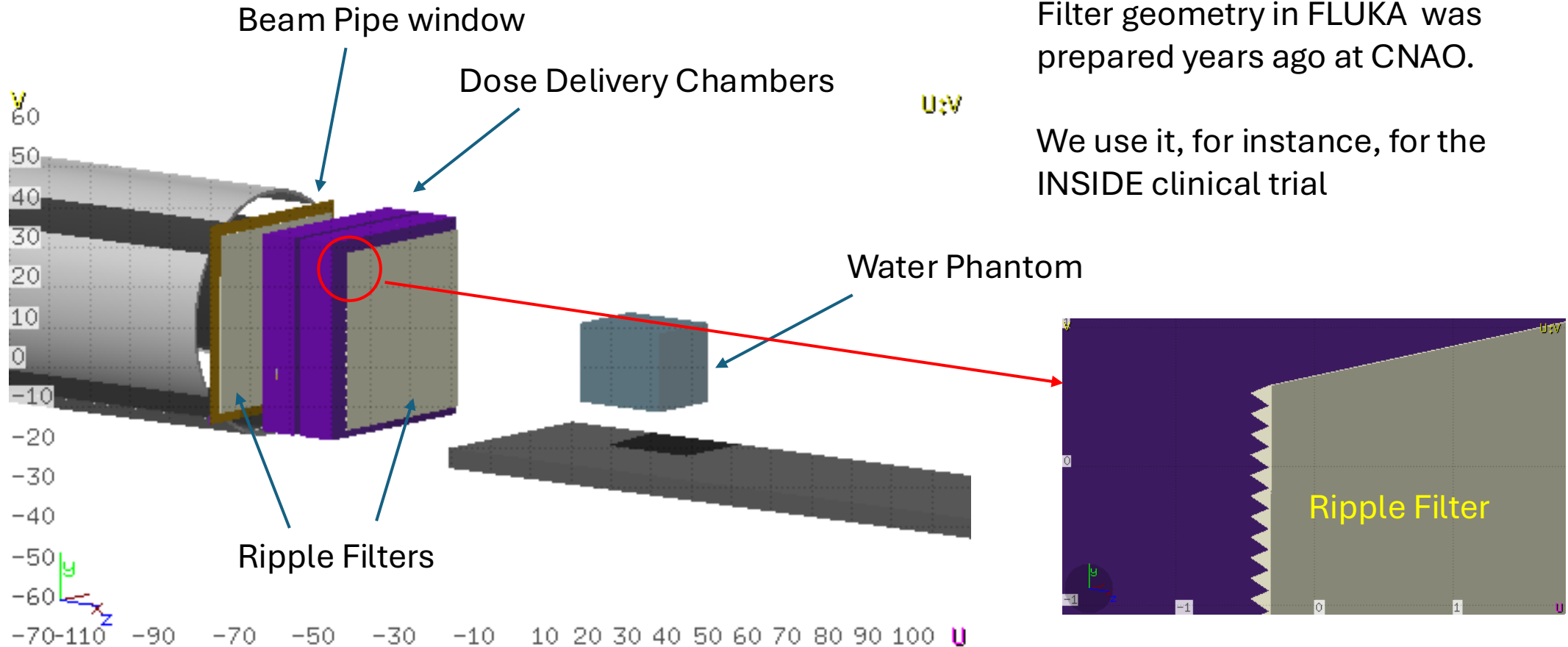
In FOOT we do not have Dose Delivery chambers and Ripple Filters

The measured peak position is then set back by ~ 3 mm to compensate the effect of Dose Delivery with ripple filters

For example: if you send a "30 mm" beam, the peak position is found at 27 mm depth. Without it, it would be 30 mm.

(M. Pullia, private communication)

Simulation check: geometry

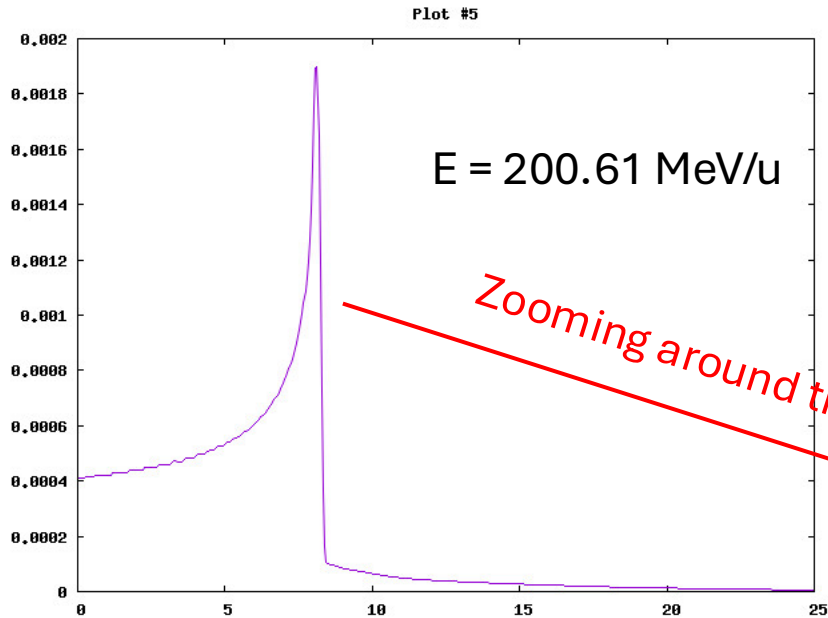


The Dose Delivery and Ripple Filter geometry in FLUKA was prepared years ago at CNAO.

We use it, for instance, for the INSIDE clinical trial

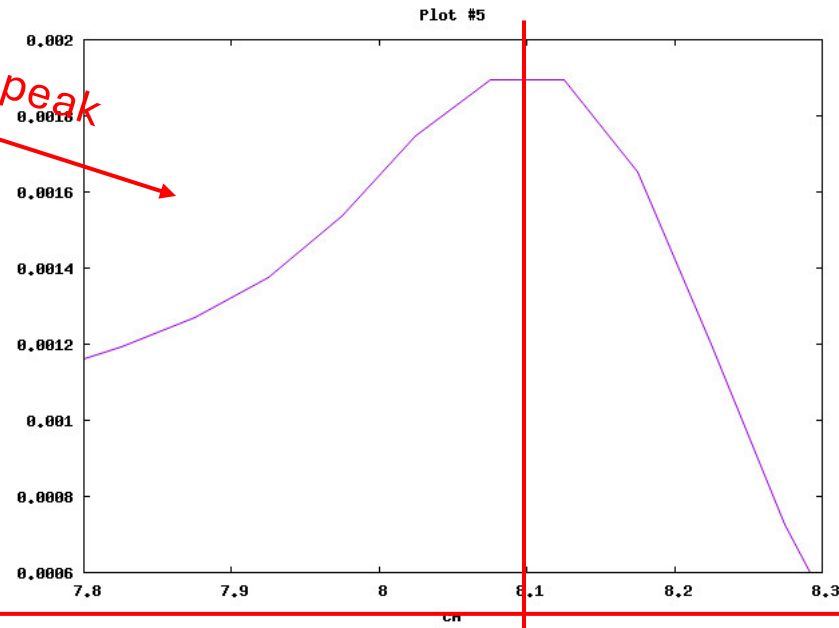
We use as energy inside the vacuum pipe the 200.61 MeV/u value

Simulation check: results



Bragg Peak location predicted at **81 mm**

→ by adding 3 mm you get the expected **84 mm**



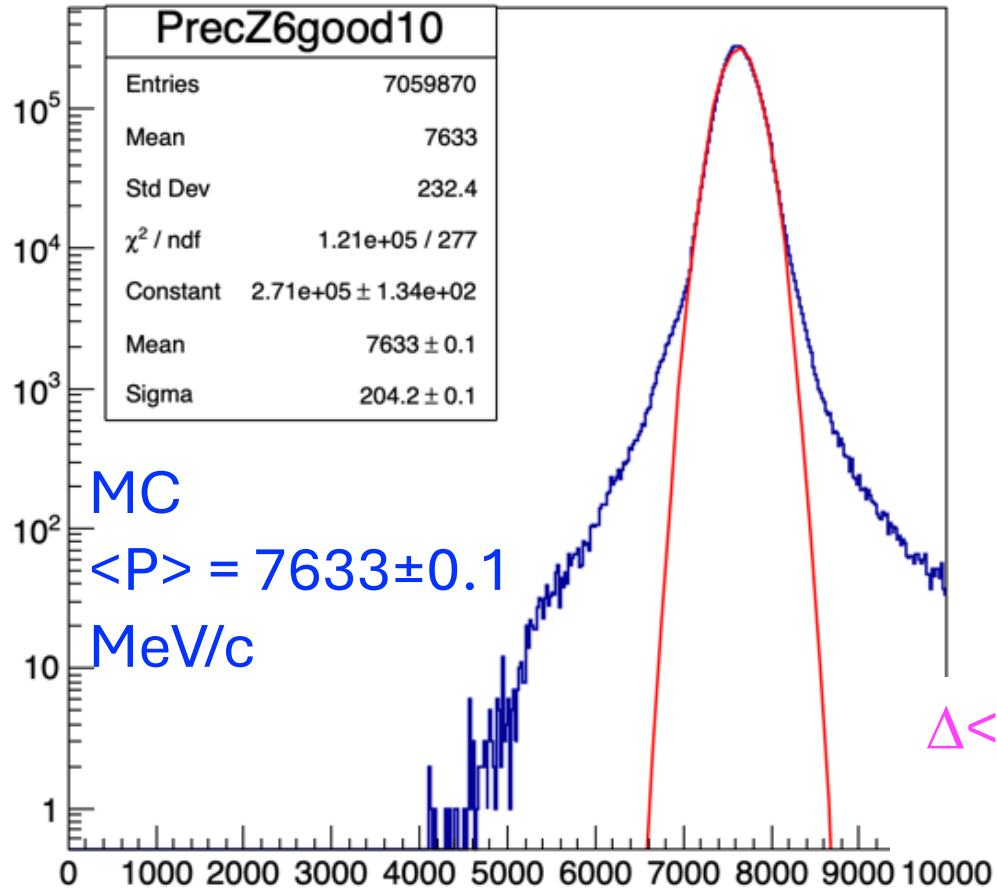
→ Therefore it is correct to assume that the input energy is the value to be used inside the beam pipe

2nd Analysis: Runs with C₂H₄ target

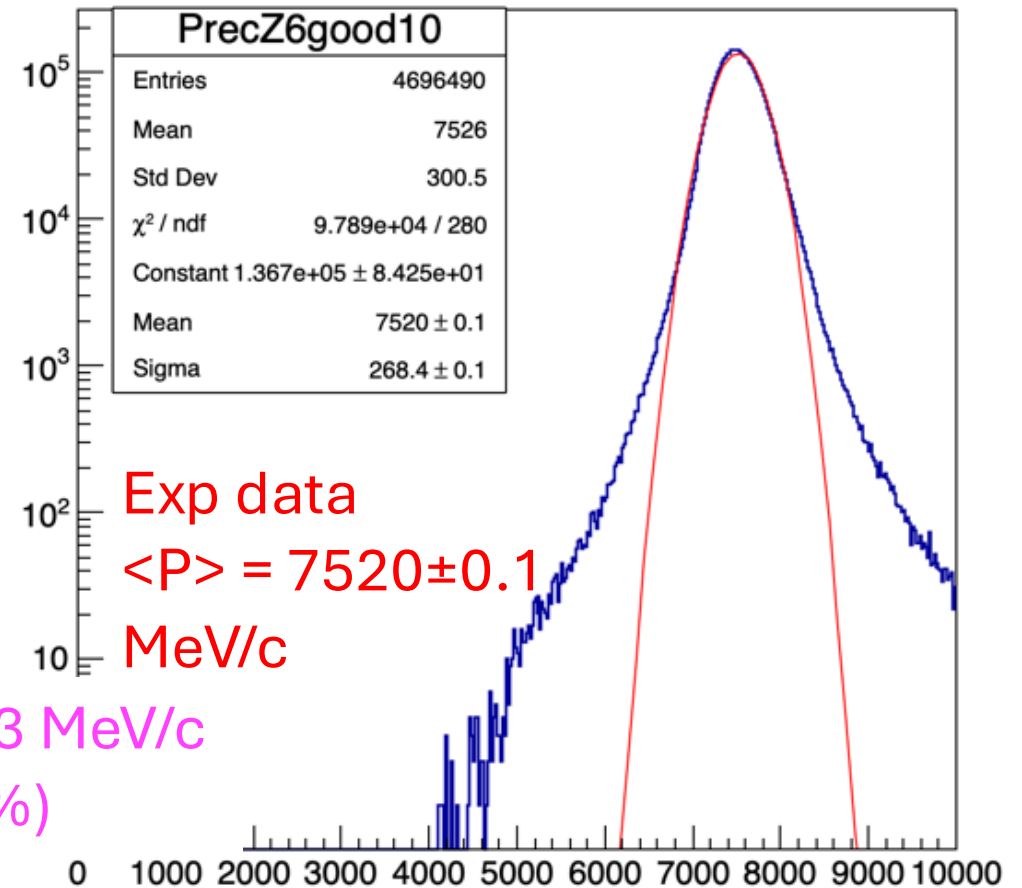
- Exactly the same selection cuts and procedure as for the C target case

Data – MC comparison (C₂H₄ target)

Rec. P. Z=6

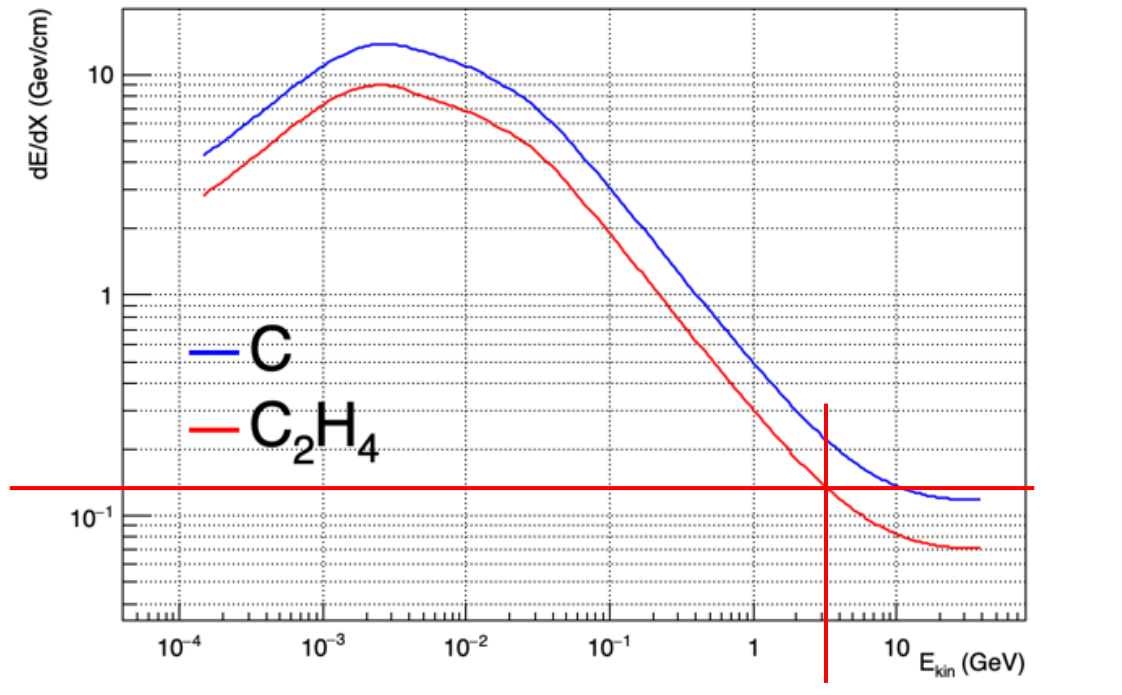


Rec. P. Z=6



$\Delta \langle P \rangle = 113 \text{ MeV/c}$
(1.5%)

dE/dx vs total E_{kin} of ¹²C in C and C₂H₄



At 200 MeV/u (2400 MeV): $dE/dx \sim 162$ MeV (total)/cm = 16.2 MeV/mm ~ 1.35 (MeV/u)/mm
very similar to H₂O, but target is thicker by a factor of 2

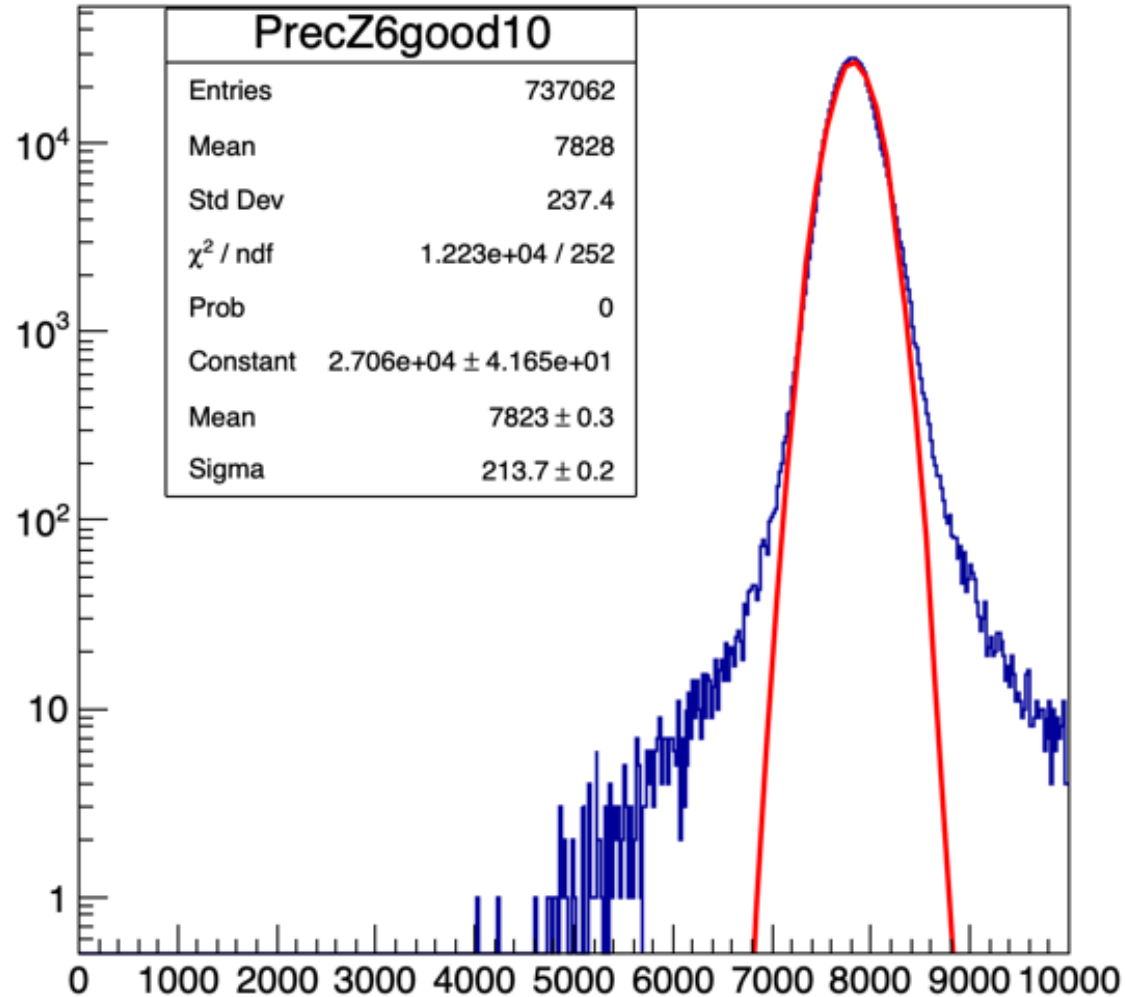
→ Energy at target center is now ~ 191.6 MeV/u → $P \sim 7528$ MeV/c
(slightly lower than for C target). → Reconstruction overestimated by 1.4%

→ Both MC and exp. data appear to scale with target \sim in agreement with expectations

3rd Analysis: Runs with no target

- Only 4 runs to be considered safe: 8017, 8018, 8019, 8020, ~128600 triggers
- Exactly the same selection cuts and procedure as for the C target case

MC



$\langle P \rangle = 7823 \pm 0.3 \text{ MeV}/c$

$E = 205.5 \text{ MeV}/u$

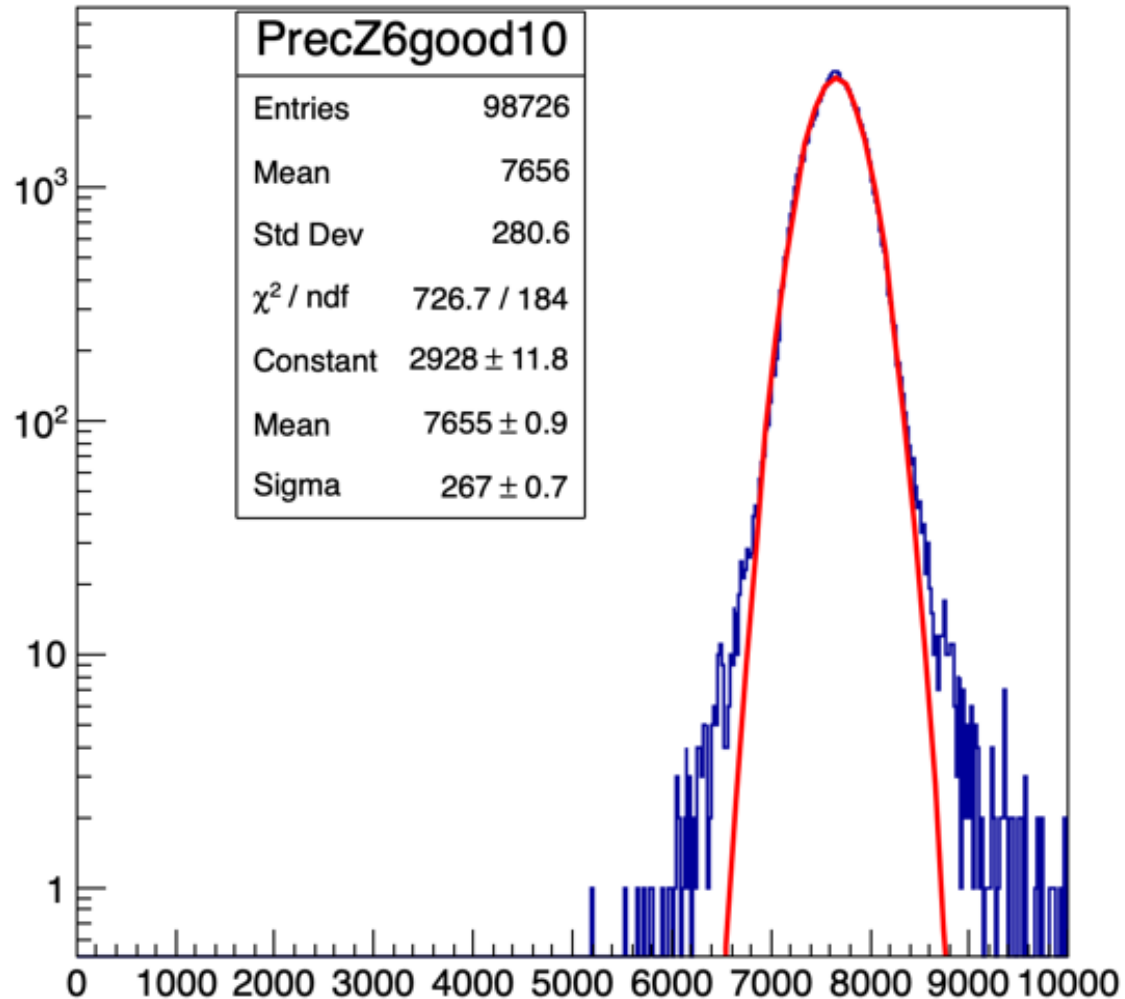
Obviously too high!
(MC truth = 198.5 MeV/u)

~199.7 MeV/u after correction for
possible P overestimation by 1.6%

~198.2 MeV/u after correction for
possible P overestimation by 2%

Much closer to MC truth

Exp. data



$\langle P \rangle = 7655 \pm 0.9 \text{ MeV}/c$

$E = 197.5 \text{ MeV}/u$

Assuming the same correction for P overestimation as in MC, we get **$\sim 192 \text{ MeV}/u$**

Again, it is too low ($\sim 6.5 \text{ MeV}/u$)

Material budget along primary tracks (C target)

From Beam Exit to Target	1.15 mm H ₂ O	<i>Even primary tracks may cross either 1 or 2 IT ladders</i>
From Target to VT:	8.72	
From VT to IT:	0.9	
From IT to MSD:	1.07 / 1.75	
From MSD to TW:	3.28	

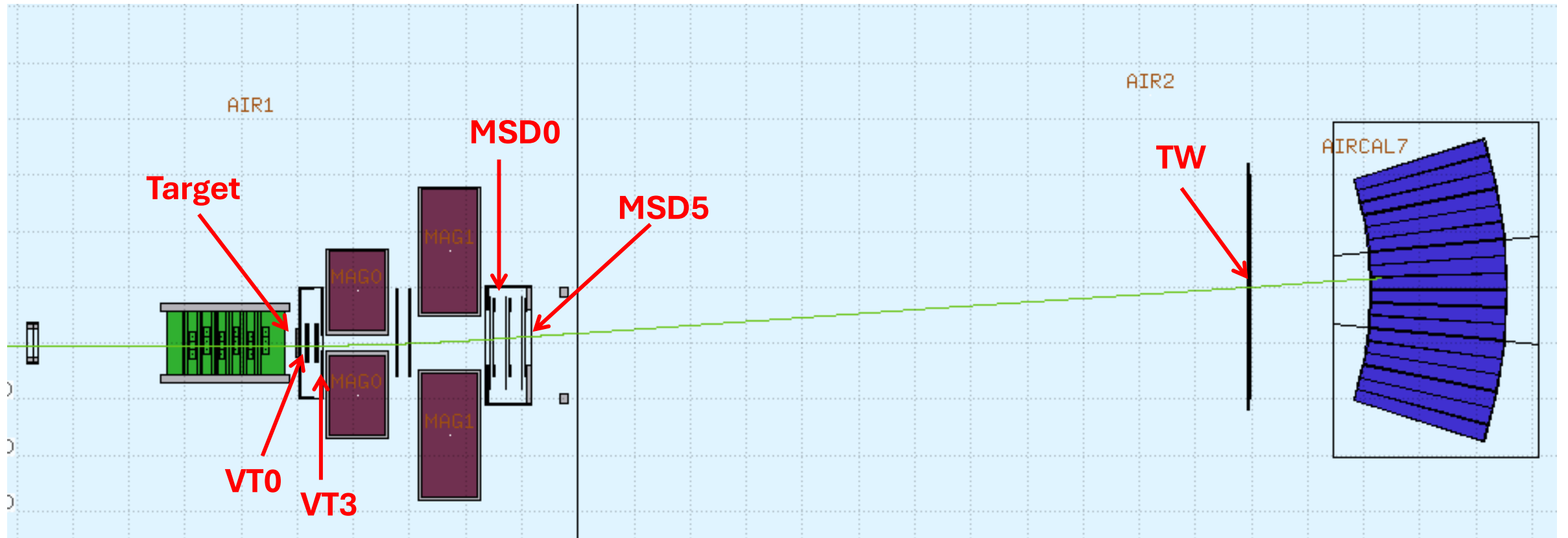
Total: **15.1 / 15.8 mm H₂O**

In order to reconcile MC and Data we need an additional thickness of **~4.2 mm H₂O** in the total material budget (**+27 - 28% !!**).

Where?

We can check the evolution of P along the tracks

P evaluated at different depths



Test on C target:

$\langle P \rangle$ from gaussian fit at each position (MeV/c)

	MC		DATA		MC - DATA	
	P (MeV/c)	E (MeV/u)	P (MeV/c)	E (MeV/u)	ΔP (MeV/c)	ΔE (MeV/u)
Target	7678.0	198.6	7563.0	193.2	115.0	5.4
VT0	7558.0	193.0	7439.0	187.5	119.0	5.5
VT3	7547.0	192.5	7430.0	187.1	117.0	5.4
MSD0	7526.0	191.5	7407.0	186.0	119.0	5.5
MSD5	7481.0	189.4	7360.0	183.8	121.0	5.6
TW	7388.0	185.1	7264.0	179.5	124.0	5.7

Fit error on P is always of the order 0.1 MeV/c

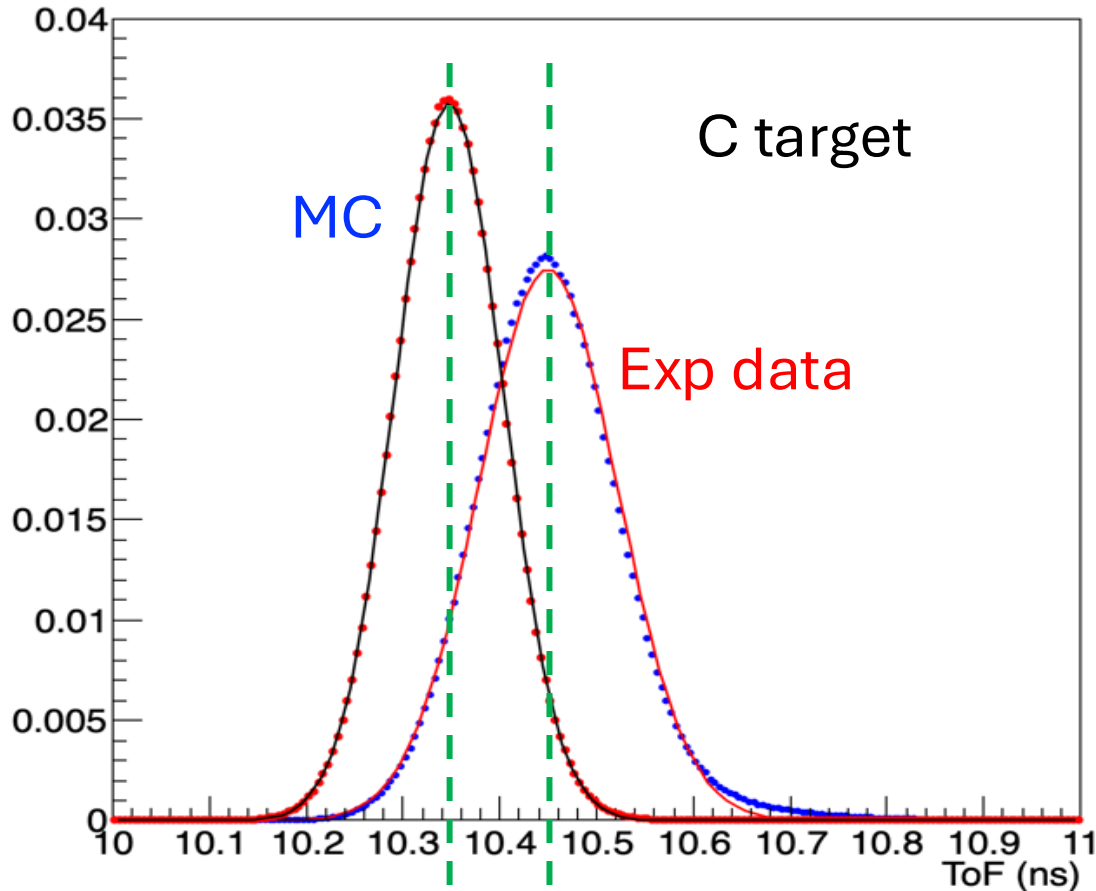
Apart from small variations of the order of few MeV/c ($\sim 1\%$)

$\Delta P(\text{MC-Data})$ is \sim constant along the track

→ Tracks see the \sim same material budget in both MC and Data

A last P-independent check: ToF comparison

ToF for Z=6



Gaussian fits

MC: $\langle \text{ToF} \rangle = 10.3474 \pm 2e-05 \text{ ns}$

Data: $\langle \text{ToF} \rangle = 10.4497 \pm 3e-05 \text{ ns}$

$\Delta \langle \text{ToF} \rangle = 0.102 \text{ ns}$

This could perfectly compatible with:

1) **a difference in kinetic energy of $\sim 5.5 \text{ MeV/u}$**

OR

2) **a mismatch, or error, in TW distance of $\sim 2 \text{ cm}$**

**But ToF is not yet calibrated in CNAO2025:
there is still the 2024 calibration**

Warning: there might be also some circularity

The ToF we are considering in analysis is:

$$\text{ToF}(\text{TW} - \text{SC}) - \text{ToF}(\text{Target} - \text{SC})$$

ToF(Target – SC) is not measured, it is calculated on the basis of the assumption on initial energy

At present, in both MC and Data analysis we were using:

$$\text{ToF}(\text{Target-SC}) = 47.15 \text{ cm} / \beta(E=200.61 \text{ MeV/u}) c \sim 2.767 \text{ ns}$$

A difference of 5 MeV/u would imply a correction of the order of ~ 0.03 ns

Summary and conclusions(?)

- There is a difference of $\sim 1.5\%$ in the value of P reconstruction between MC and data *Is this important?*
- An independent ToF measurement could confirm this, but geometry has to be double checked and calibration for CNAO2025 has to be completed
- MC is demonstrated to be self-consistent (*although this does not necessarily mean that FOOT simulation is correct*)
- The choice of input energy inside the beam pipe turned out to be consistent with CNAO measurements and assumptions
- Reconstruction scales consistently with target properties on both MC and Data
- P evolves \sim in the same way along the track both in MC and Data: we have the material budget under control
- At present we remain with no explanation, *unless..*

Hypotheses and questions for discussion

Assuming that SHOE reconstruction behaves exactly in the same way for MC and Data:

But this would be quite a big thickness!

1. We are missing some material (~ 4.2 mm H_2O) of in the description of FOOT upstream of the target (1 mm H_2O can be accounted by the beam window)
2. OR there is some subtle problem with the magnetic field (*Yun suggests also the possible role of alignment of the magnetic system*). An independent ToF comparison could exclude this problem, after calibration and geometry check
3. OR could this be due to some wrong parameter in geometry? Or a difference in geometry between MC and reconstruction?
4. OR for some unknown reason, the beam energy is not what it's supposed to be (lower by $\sim 5 - 6$ MeV/u)
5. OR???