
MATTEO ROSATI - ROMA TRE UNIVERSITY, ITALY

**Learning at the Interface Between Quantum Hardware and AI:
From Data-Driven Quantum Design
to Quantum-Native Models**



Outline

ML-ENHANCED
DESIGN AND CONTROL
OF QUANTUM DEVICES

LEARNING THEORY & ALGORITHMS
FOR QUANTUM SYSTEMS

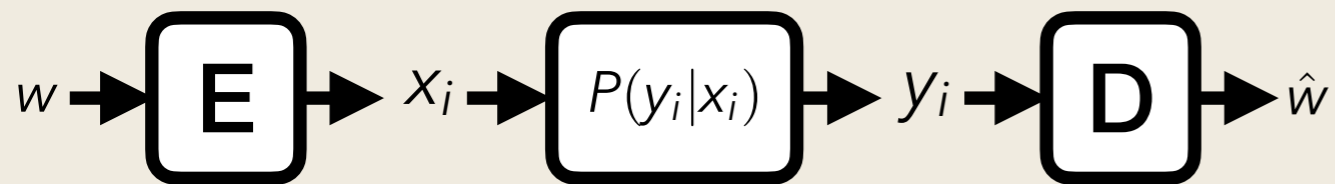
QUANTUM/AI
INTERFACE
TECHNOLOGIES

QUANTUM-ENHANCED
AI PRIMITIVES

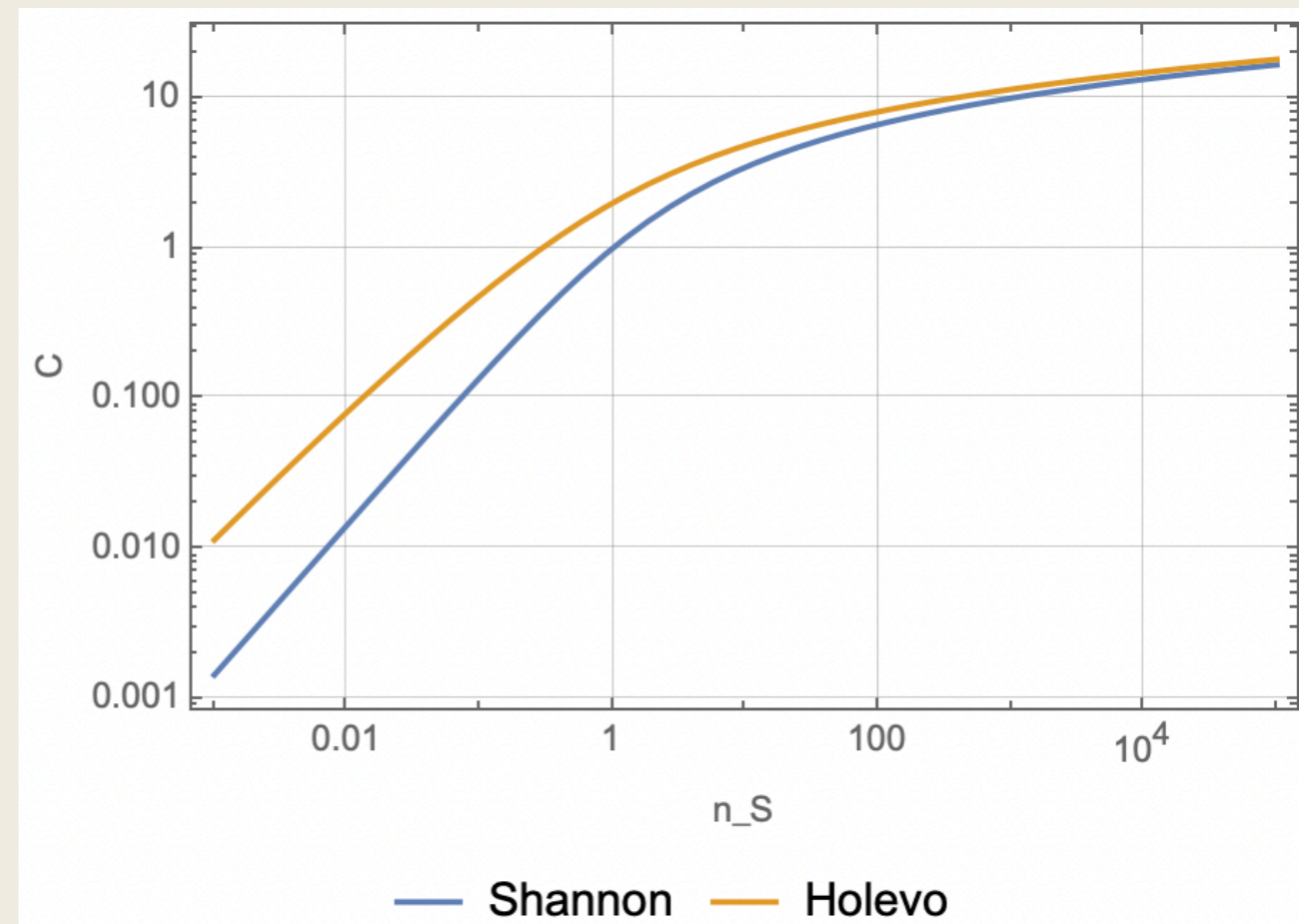
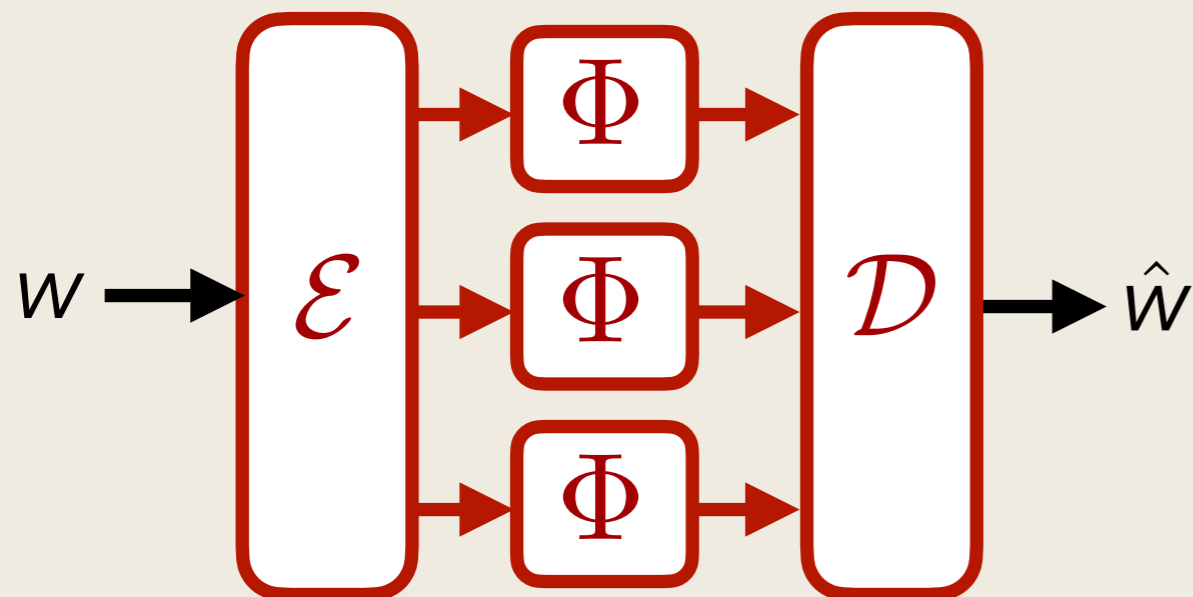
ML-enhanced control and design of quantum devices

Bit transmission using quantum states

Classical Shannon system



Quantum Holevo system



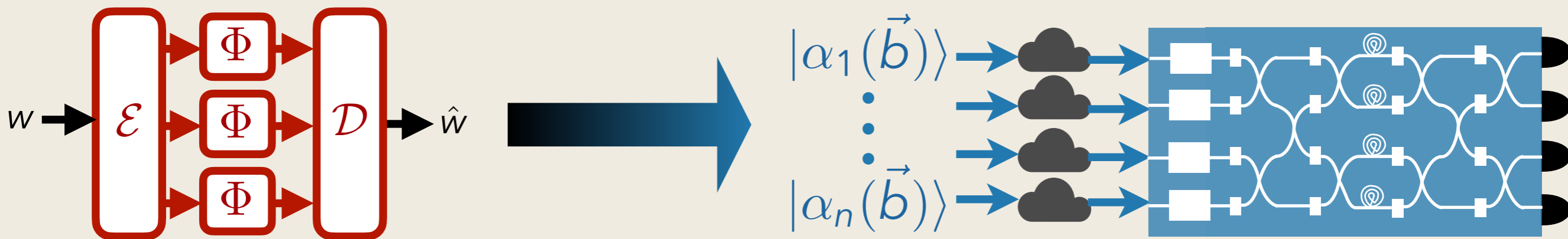
Join detection: use cases



PRACTICAL USE

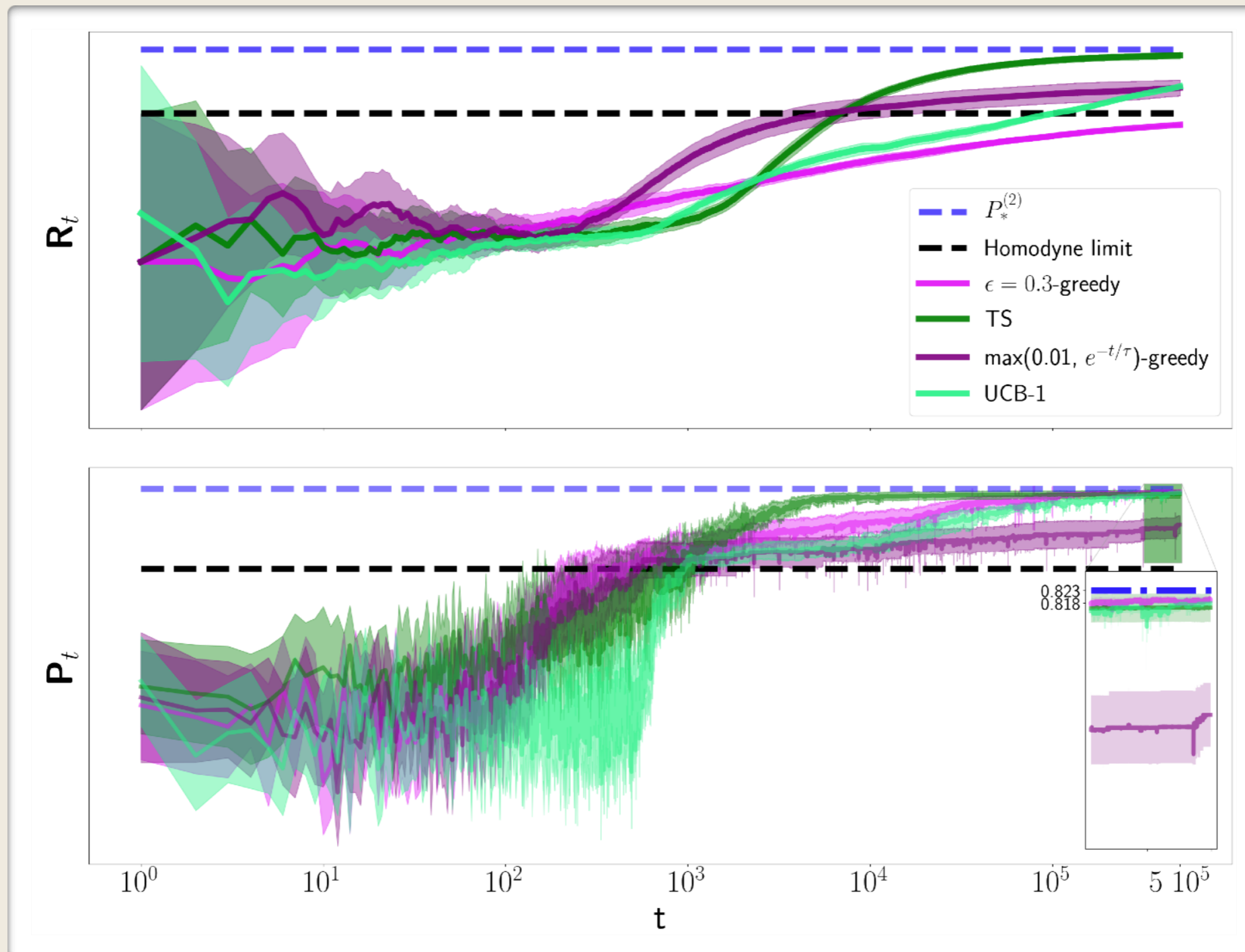
- Short-distance: constant advantage
- Long-distance: $\log(1/S)$ advantage (no amplification)
- Entanglement-assisted: infinite-fold enhancement at large noise (microwave frequencies)
- Medium-distance: ~57% energy reduction at 200Km (with amplification)

The quest for an optimal joint detection receiver (JDR)



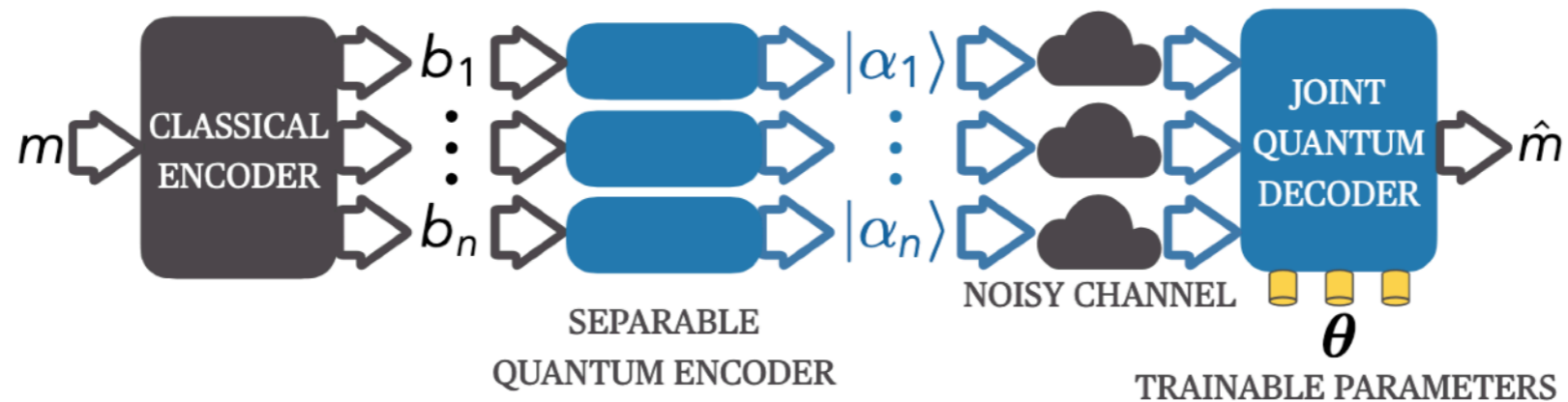
- Are there optical JDR designs for other codes, e.g., for q. advantage at higher signal power?
 - Is there a systematic way of studying them?
 - What is their performance and scalability?
 - Can optical squeezing or ancillae help?
-

Reinforcement-learning a single-symbol receiver

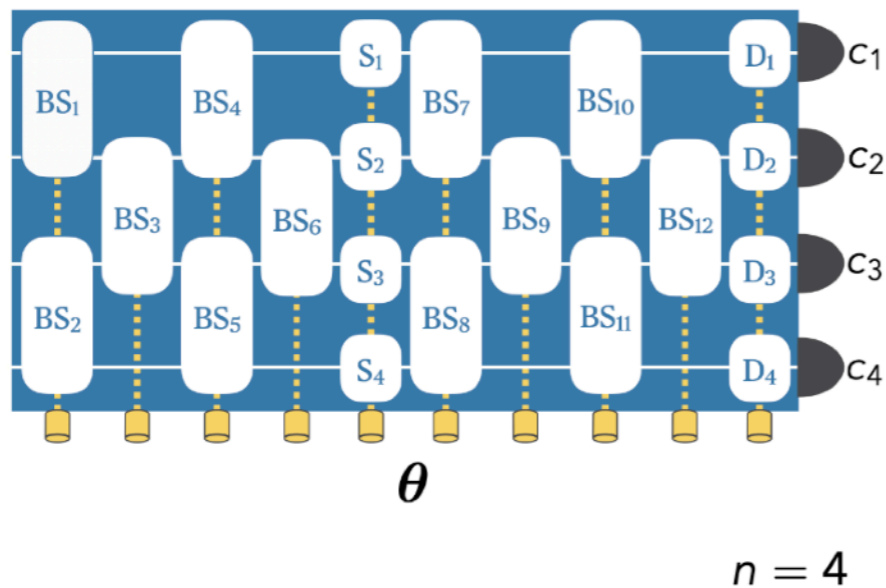


Optical JDR designs: a supervised learning approach

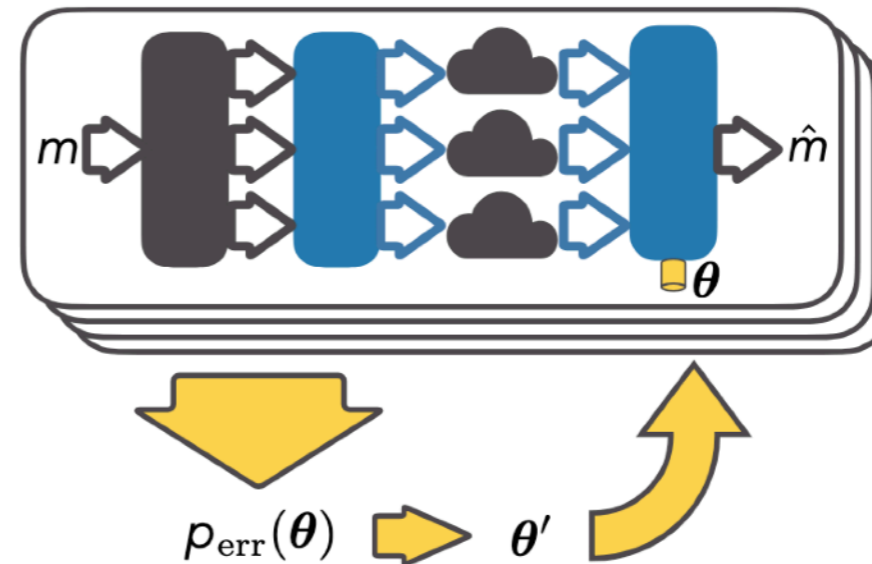
a) QUANTUM-ENHANCED BIT-TRANSMISSION SCHEME



b) PHOTONIC DECODER CIRCUIT

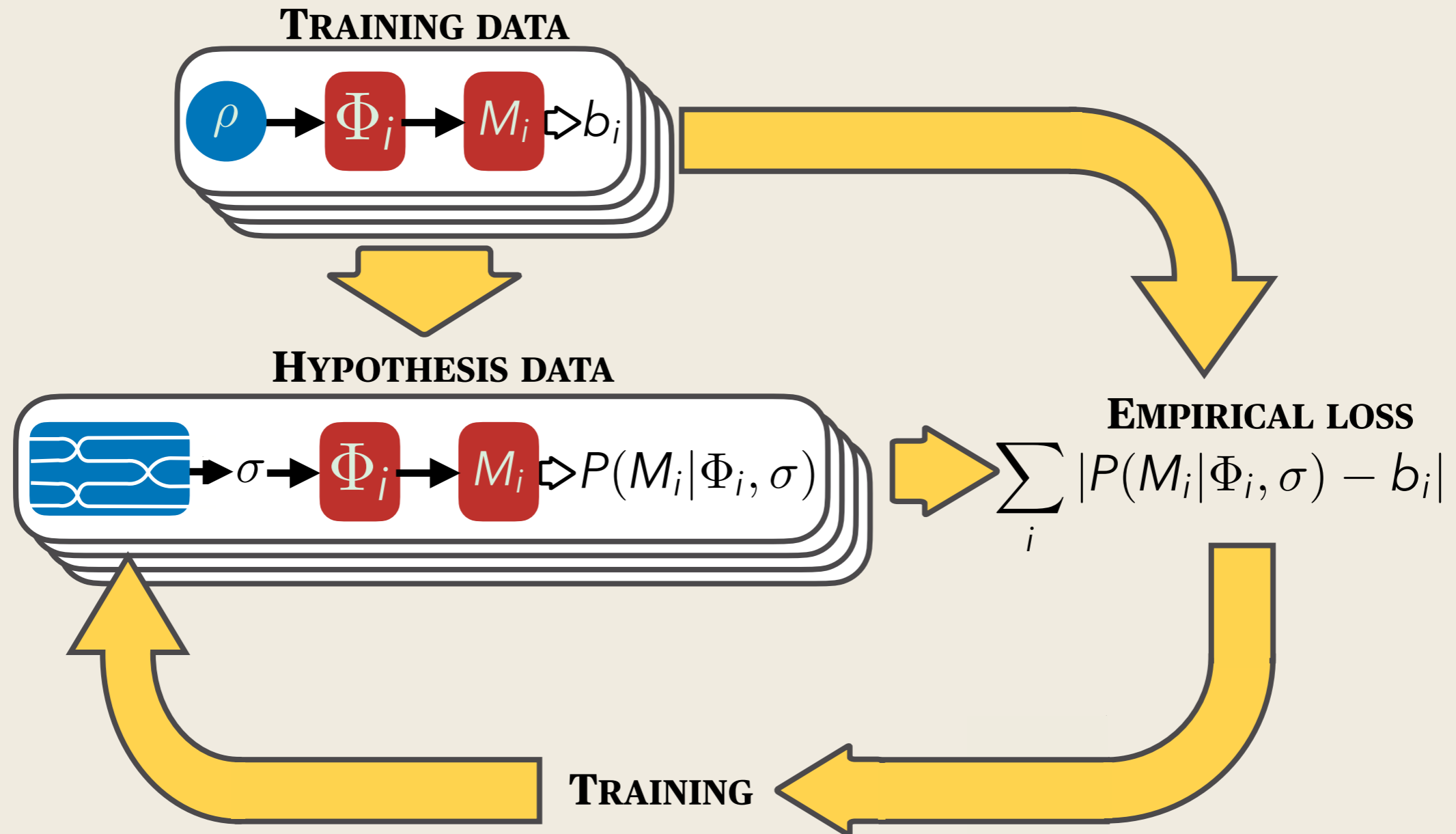


c) TRAINING PROCESS

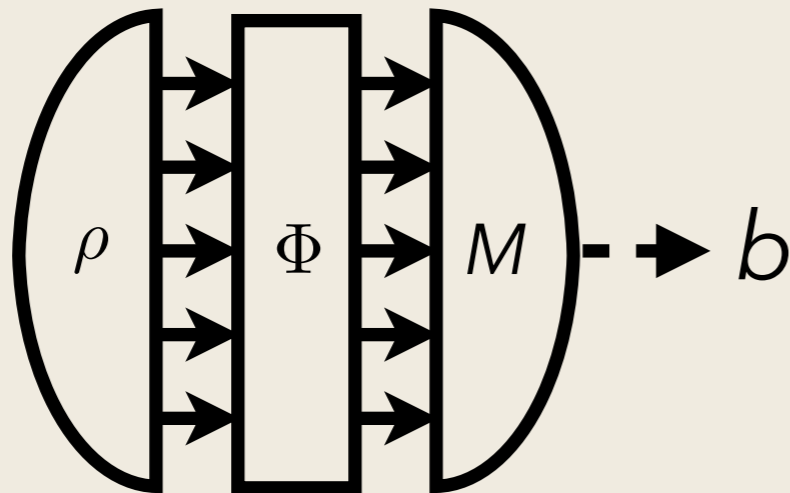


Learning theory & algorithms for quantum systems

Learning probability distributions generated by bosonic circuits



Gaussian and non-Gaussian circuits



$b = 1$ "accept"
with probability

$$P(M|\Phi, \rho) = \text{Tr}[M \cdot \Phi(\rho)]$$

Gaussian

$$P(M|\Phi, \rho) = \mathcal{G}_{\mathbf{m}_{\text{out}}, V_{\text{out}} + V'}(\mathbf{m}')$$

Gaussian plus
photodetection

$$P(M|\Phi, \rho) = \mathcal{G}_{\mathbf{m}_{\text{out}}, V_{\text{out}} + V'}(\mathbf{m}') \cdot H_{\mathbf{k}}^{(\tilde{V})}(\tilde{\mathbf{m}})$$

Non-Gaussian
(complex sum of
complex-valued
Gaussian Wigner f.)

$$P(M|\Phi, \rho) = \sum_i c_i \mathcal{G}_{\mathbf{m}_{i,\text{out}}, V_{i,\text{out}} + V'_i}(\mathbf{m}'_i)$$

Results: sample complexity

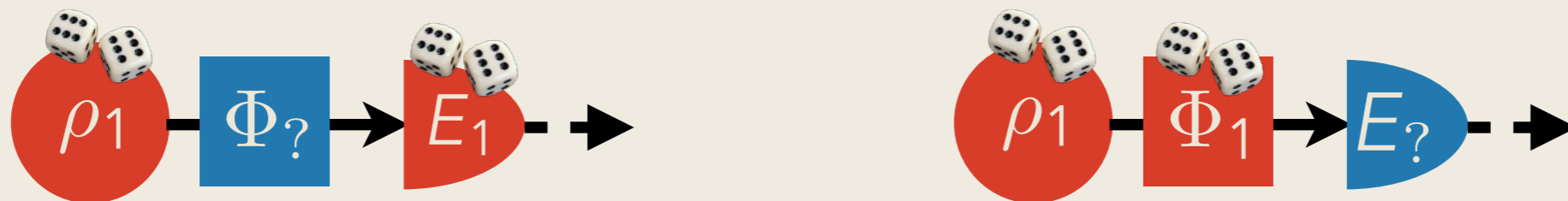
We obtain efficient learnability for k -mode circuits:

Gaussian $n = O(\epsilon^{-2}k^2)$

Gaussian plus photodetection $n = O(\epsilon^{-2}k^2 \log N)$

Non-Gaussian $n = O(\epsilon^{-4}k^2B^2)$

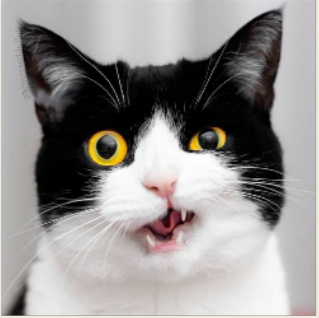
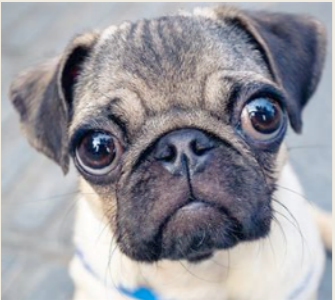
Similar scaling: learning channels / measurements



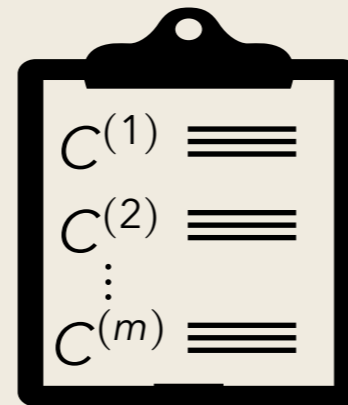
Classical Statistical Learning Theory

POSSIBLE EXPLANATIONS

OBSERVATIONS

classical "input" x	classical "label" y
	cat
	dog

theoretical
model

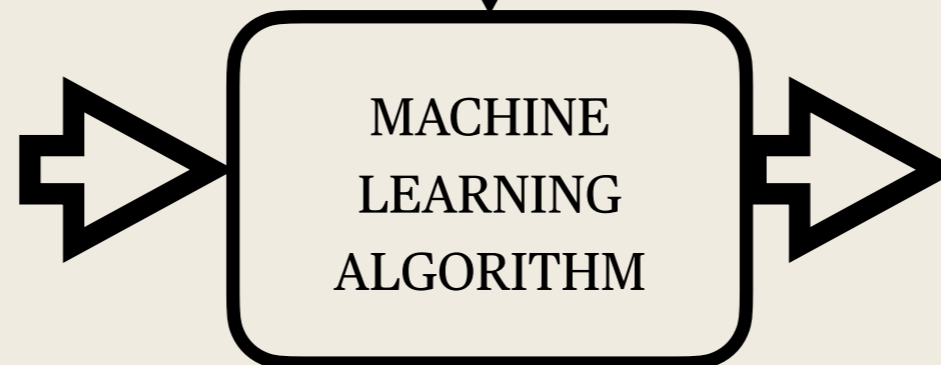


Learning a
deterministic
function

$$y = f(x)$$

**BEST
EXPLANATION**





C_{op}



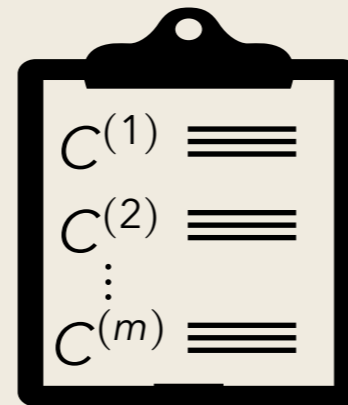
Classical Statistical Learning Theory

POSSIBLE EXPLANATIONS

OBSERVATIONS

classical "context" x	classical "signal" y
	
	

theoretical model

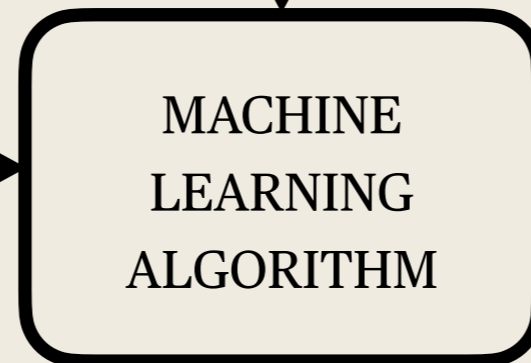


Learning a probabilistic relation

$$p(y|x)$$

BEST EXPLANATION





$$C_{op}$$



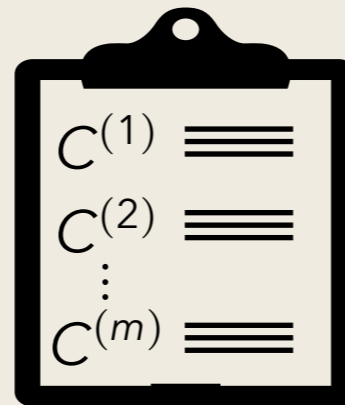
Quantum Statistical Learning Theory

POSSIBLE EXPLANATIONS

OBSERVATIONS

classical "signal"	quantum "signal"
x	ρ
	
	

theoretical
model

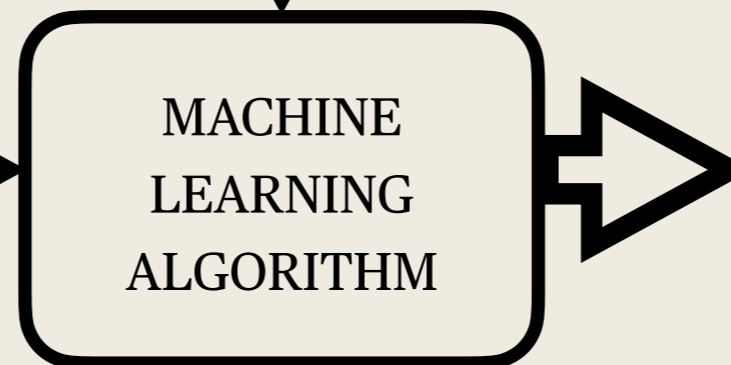


Learning a
classical-quantum
channel

$$\rho(x)$$

**BEST
EXPLANATION**

$$C_{op}$$



Learning Classical-Quantum Channels

Target (c-q function) $\rho? : \mathcal{X} \rightarrow \mathcal{D}(\mathcal{H})$

Hypothesis class $\mathcal{C} = \{\sigma : \mathcal{X} \rightarrow \mathcal{D}(\mathcal{H})\}$

given samples $(x_i, \rho?(x_i)) \quad i = 1, \dots, n \quad x_i \sim \mathcal{D}$

find a **good** candidate

$$O \in \mathcal{C} : \hat{R}(O) - \eta \inf_{O' \in \mathcal{C}} R(O') \leq \epsilon \text{ w.h.p.}$$

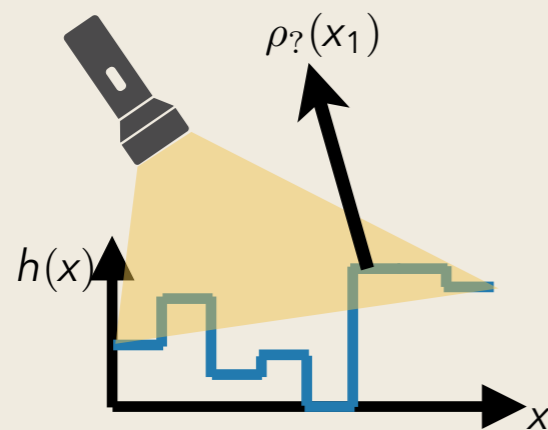
- **Theorem:** a sufficient condition for learnability of classical-quantum processes is

$$\lim_{n \rightarrow \infty} \frac{\log^2 \gamma(n, \epsilon, \mathcal{C})}{n} = 0$$

Applications

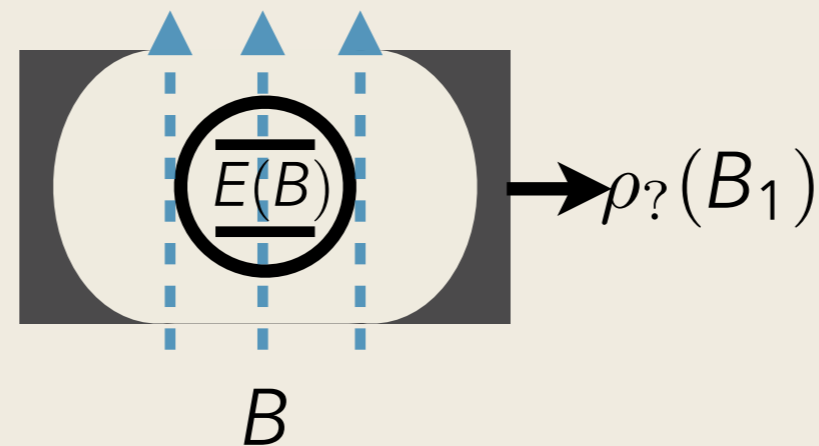
Approximate an unknown quantum process from "noisy" or "random" samples:

- Quantum imaging



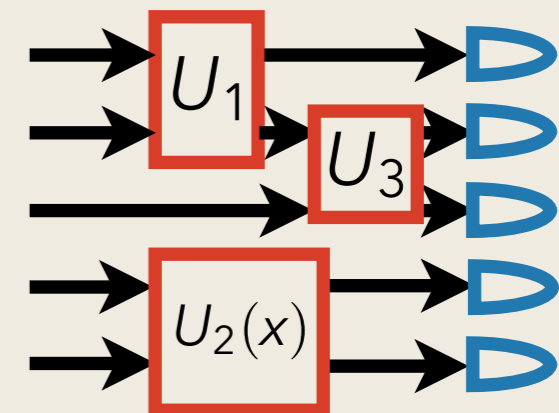
Learn the **optical depth** as a function of the **position**

- Hamiltonian learning



Learn the **excited state energy** as a function of the **magnetic field**

- Circuit compilation

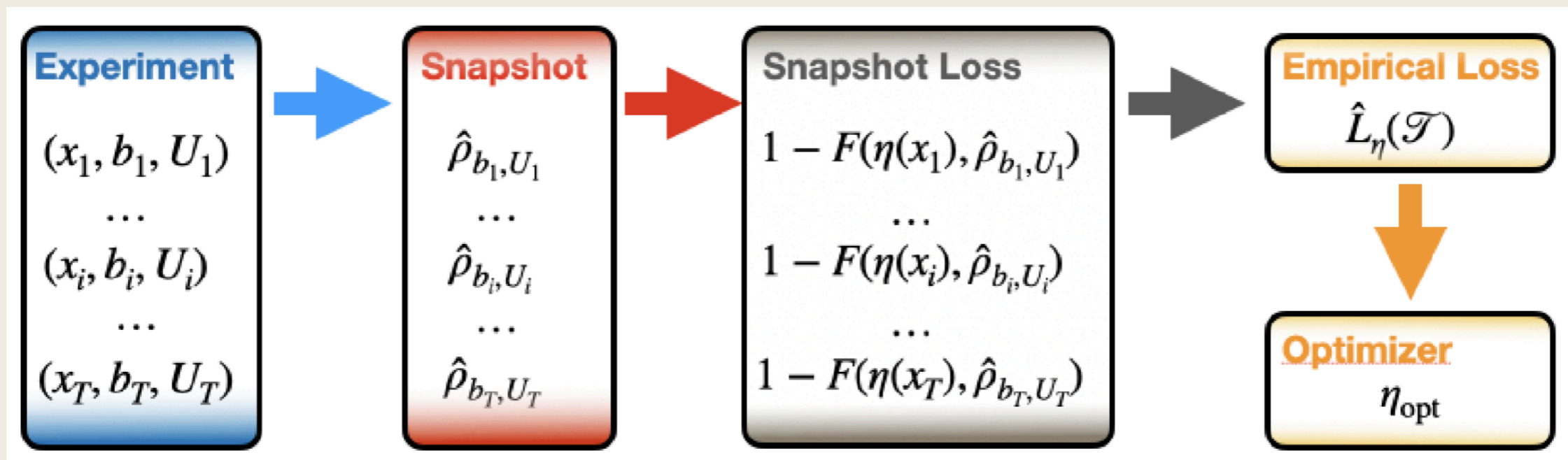


Learn **circuit** as a function of the **classical encoding parameters**

Photon-starved polarimetry with functional classical shadows

Reconstruct a polarimetric profile, i.e., qubit angles as a function of wavelength, from standard measurements

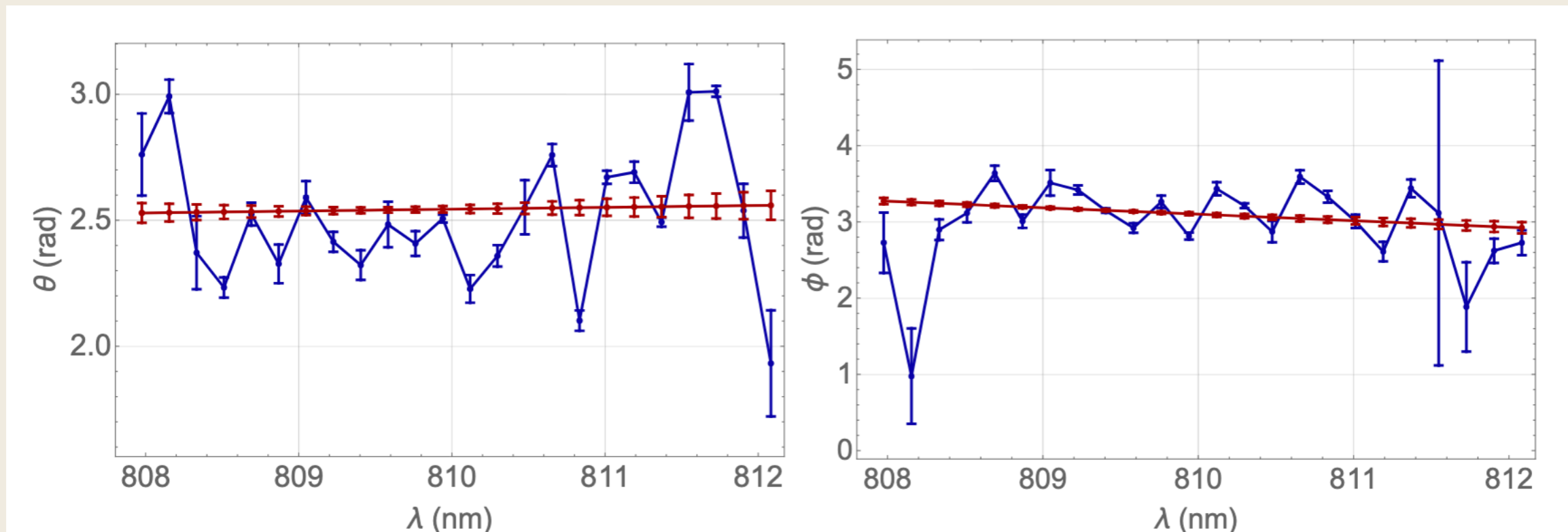
$$\mathcal{C} = \left\{ |\eta(x)\rangle = \cos \frac{\theta(x)}{2} |H\rangle + e^{i\phi(x)} \sin \frac{\theta(x)}{2} |V\rangle \right\}$$



Photon-starved polarimetry with functional classical shadows

Reconstruct a polarimetric profile, i.e., qubit angles as a function of wavelength, from standard measurements

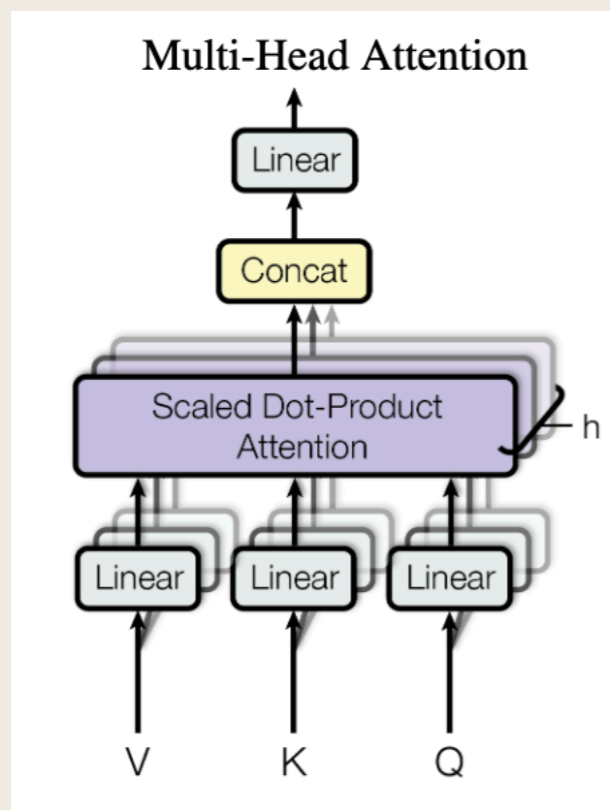
$$\mathcal{C} = \left\{ |\eta(x)\rangle = \cos \frac{\theta(x)}{2} |H\rangle + e^{i\phi(x)} \sin \frac{\theta(x)}{2} |V\rangle \right\}$$



Quantum-enhanced AI primitives

A Quantum Transformer Architecture

- Classical self-attention: non-linear processing of inputs



$\mathbf{X}_1, \dots, \mathbf{X}_j$



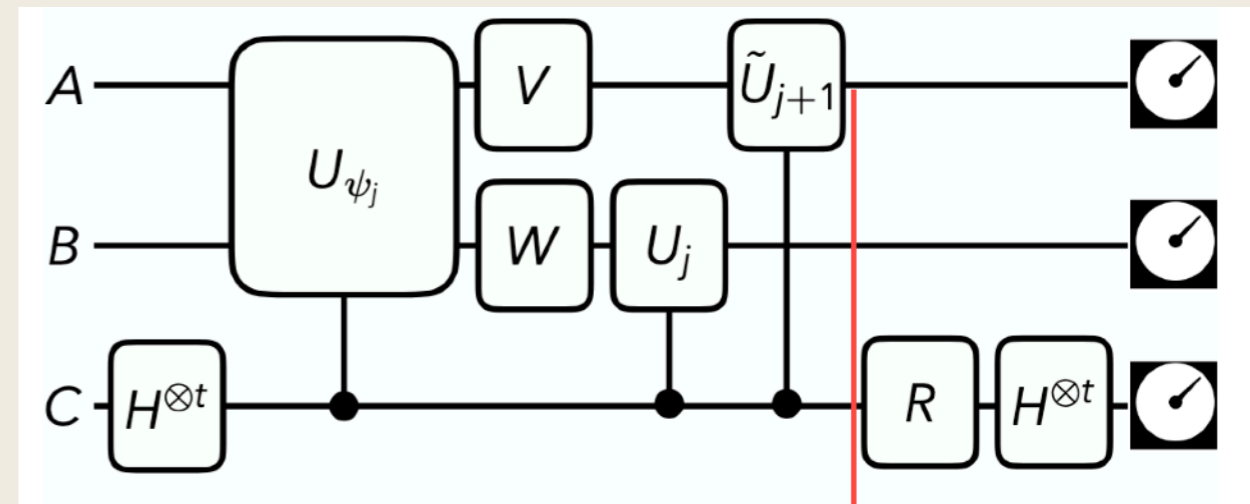
$$\mathbf{z}_j = \sum_{i=1}^j \text{softmax} \left(\frac{\mathbf{q}_j \cdot \mathbf{k}_i}{\sqrt{d_K}} \right) \mathbf{v}_i,$$

$$\tilde{\mathbf{z}}_j \propto \sum_{i=1}^j (\mathbf{x}_j \mathbf{Q}^T \mathbf{K} \mathbf{x}_i) \mathbf{V} \mathbf{x}_i,$$

A Variational Quantum Transformer Architecture

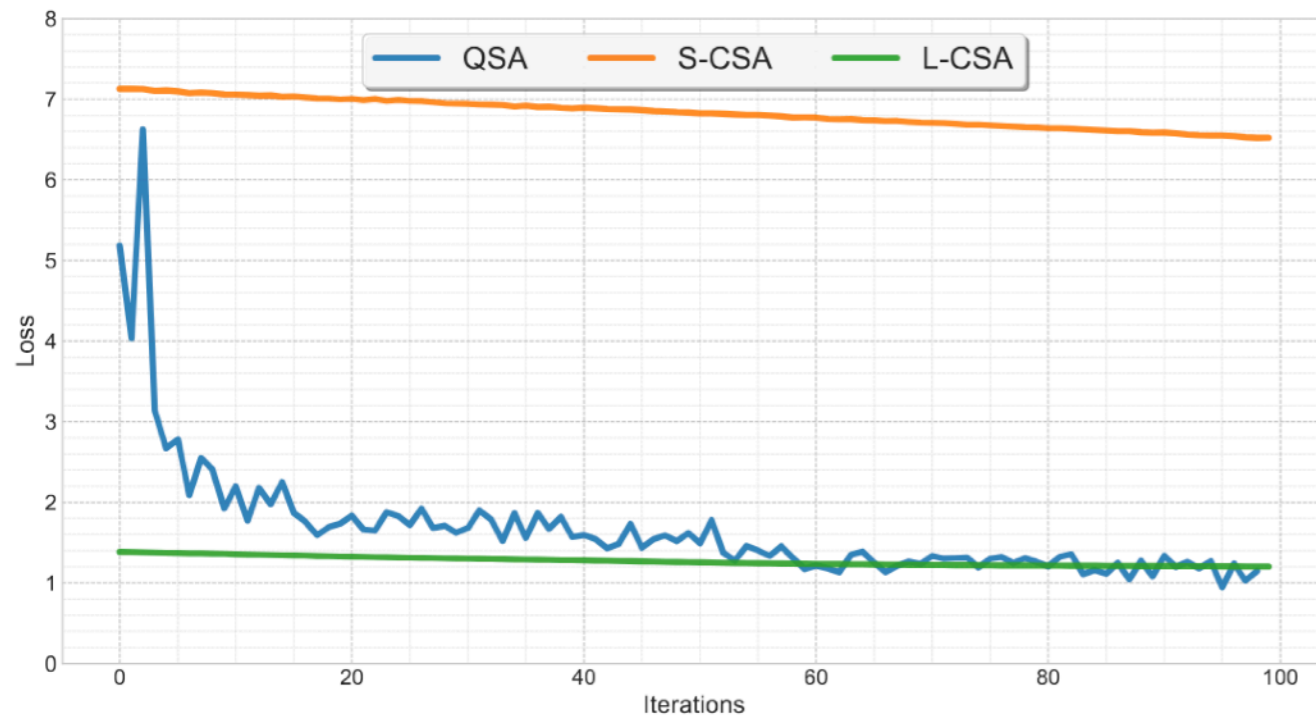
- Quantum self-attention:
 - inputs data three times
 - variational unitary action
 - processes multiple words in coherent superposition
 - outputs Renyi cross-entropy loss as a Pauli observable's expectation

$$\mathcal{L}_{\frac{1}{2}}(p) = -2 \log \left| \sum_{j=1}^T \sqrt{p_{j+1}} \right|$$



$$\propto \sum_{j=1}^T \langle \tilde{\mathbf{x}}_{j+1} | \tilde{\mathbf{z}}_j \rangle |j\rangle_C.$$

A Quantum Transformer Architecture



Classical sequence prediction

(my, dog, is, black)

Quantum sequence prediction

$(|\psi_0\rangle, e^{-iH}|\psi_0\rangle, e^{-i2H}|\psi_0\rangle, e^{-i3H}|\psi_0\rangle)$

$$H_{TFIM} = \sum_i h_i X_i + \sum_{i<j} J_{ij} Z_i Z_j$$

- Complexity: QSA beats CSA for long sequences
 $\tilde{O}(Td^2)$ vs. $O(T^2d)$

Conclusions

- ML can calibrate and optimize quantum devices
 - A learning approach replaces tomography with sample-efficient estimation of targeted quantum system properties
 - Efficient mid-term Quantum LLM design
-