

Diffraction 2012, Las Canarias

**Reggeometry of lepton- and
hadron-induced reactions**

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Goals and objectives

1 Reactions: DVCS: $\gamma^*p \rightarrow \gamma p$ (NB: elastic Compton, $\gamma p \rightarrow \gamma p$, is less known!), exclusive (diffractive) VMP $\gamma^*p \rightarrow Vp$ (at HERA) and elastic (diffractive) hadron scattering (*e.g.* $pp \rightarrow pp$ at ISR-LHC).

2. Measurables (observables): differential x-tion $d\sigma/dt$ and integrated in t : $\sigma_{el} = \int_{-t_{min}}^{-t_{max}} d\sigma/dt$, slope $B(s, t, Q^2)$, total x-tion σ_t (for elastic scattering only!).

3. Fitting strategy:

a) in DVCS and VMP: $d\sigma/dt$, vs. σ_{el} - which one is the "primitive" ?
Compatibility?!

b) weighting the data point? (the number of data points in pp is by an order of magnitude larger and better than in lepton-induced reactions!

c) simultaneous (multidimensional) vs. "sequent" (sequentially in each variable and/or reaction)?

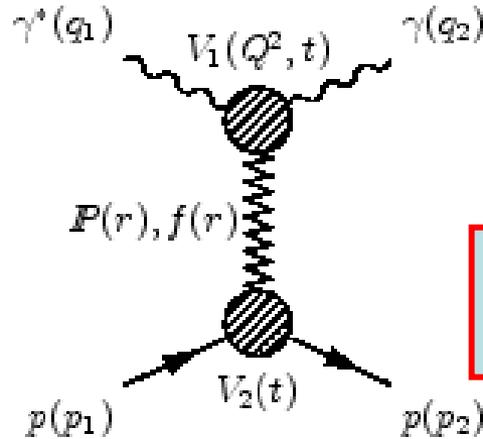
d) experientially measured bins and "symmetrization" (in DVCS and VMP).

e) the "soft" and "hard" components.

Regge-type DVCS amplitude

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$$V_1 = e^{b\beta(z)}$$

$$V_2 = e^{b\alpha(t)}$$

A new variable is introduced: $z = t - Q^2$

Applications for the model can be:

- Study of various regimes of the scattering amplitude vs Q^2, W, t (perturbative \rightarrow unperturbative QCD)
- Study of GPD_s

DVCS amplitude:
$$A(s, t, Q^2)_{\gamma^* p \rightarrow \gamma p} = -A_0 V_1(t, Q^2) V_2(t) (-is/s_0)^{\alpha(t)}$$

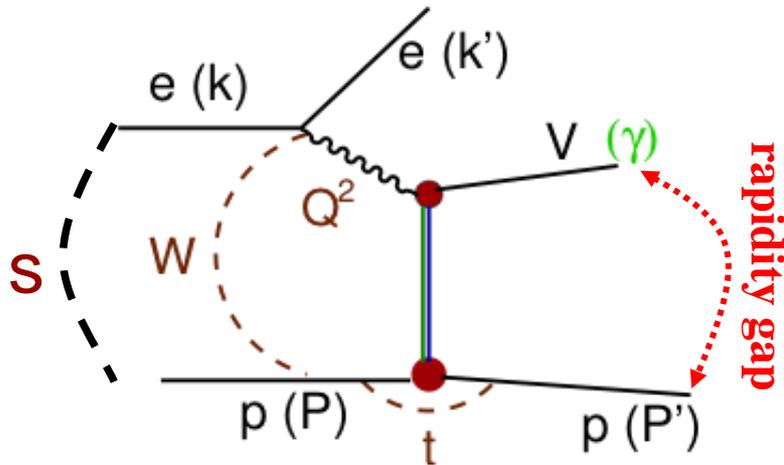
the t dependence at the vertex $pIPp$ is introduced by: $\alpha(t) = \alpha(0) - \alpha_1 \ln(1 - \alpha_2 t)$

the vertex $\gamma^*IP\gamma$ is introduced by the trajectory: $\beta(z) = \beta(0) - \beta_1 \ln(1 - \beta_2 z)$

indicating with $L = \ln(-is/s_0)$ the DVCS amplitude can be written as:

$$A(s, t, Q^2)_{\gamma^* p \rightarrow \gamma p} = -A_0 e^{b\alpha(t)} e^{b\beta(z)} (-is/s_0)^{\alpha(t)} = -A_0 e^{(b+L)\alpha(t) + b\beta(z)}$$

Exclusive diffraction



Main kinematic variables

electron-proton centre-of-mass energy:

$$s = (k + p)^2 \approx 4E_e E_p$$

photon virtuality:

$$Q^2 = -q^2 = -(k - k')^2 \approx 4E_e E_e' \sin^2 \frac{\theta}{2}$$

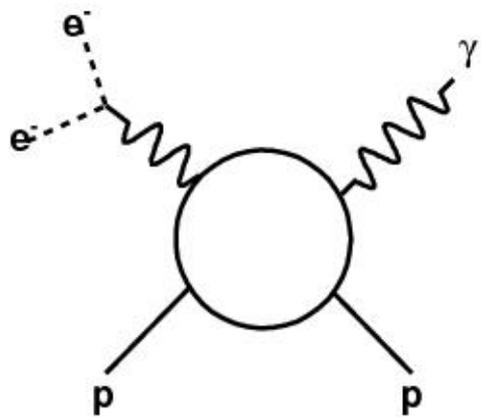
photon-proton centre-of-mass energy:

$$W^2 = (q + p)^2, \text{ where } m_p < W < \sqrt{s}$$

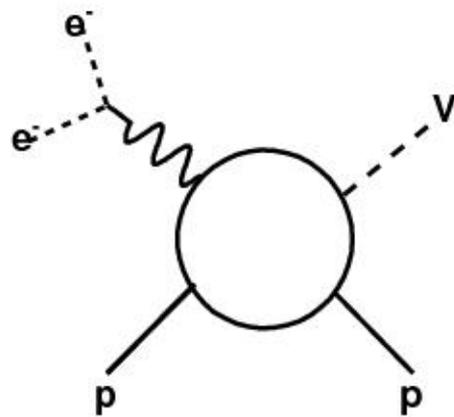
square 4-momentum at the p vertex:

$$t = (p' - p)^2$$

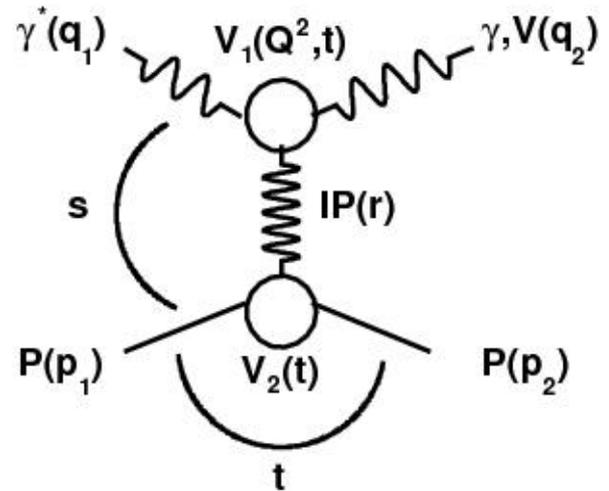
- Vector Mesons production in diffraction
- Deeply Virtual Compton Scattering



(a)



(b)



(c)

Diagrams of DVCS (a) and VMP (b) amplitudes and their Regge-factorized form (c)

Basic ideas:

How to combine s , t , and Q^2 dependencies in a binary reaction?

Reggeometry=Regge+geometry (play on words, *pun*)

1. The s - and t - dependences are related by the standard Regge-pole model:

$$A(s, t, Q^2) = \xi(t)\beta(t, M, Q^2)(s/s_0)^{\alpha(t)}$$

(see, however, item 3.);

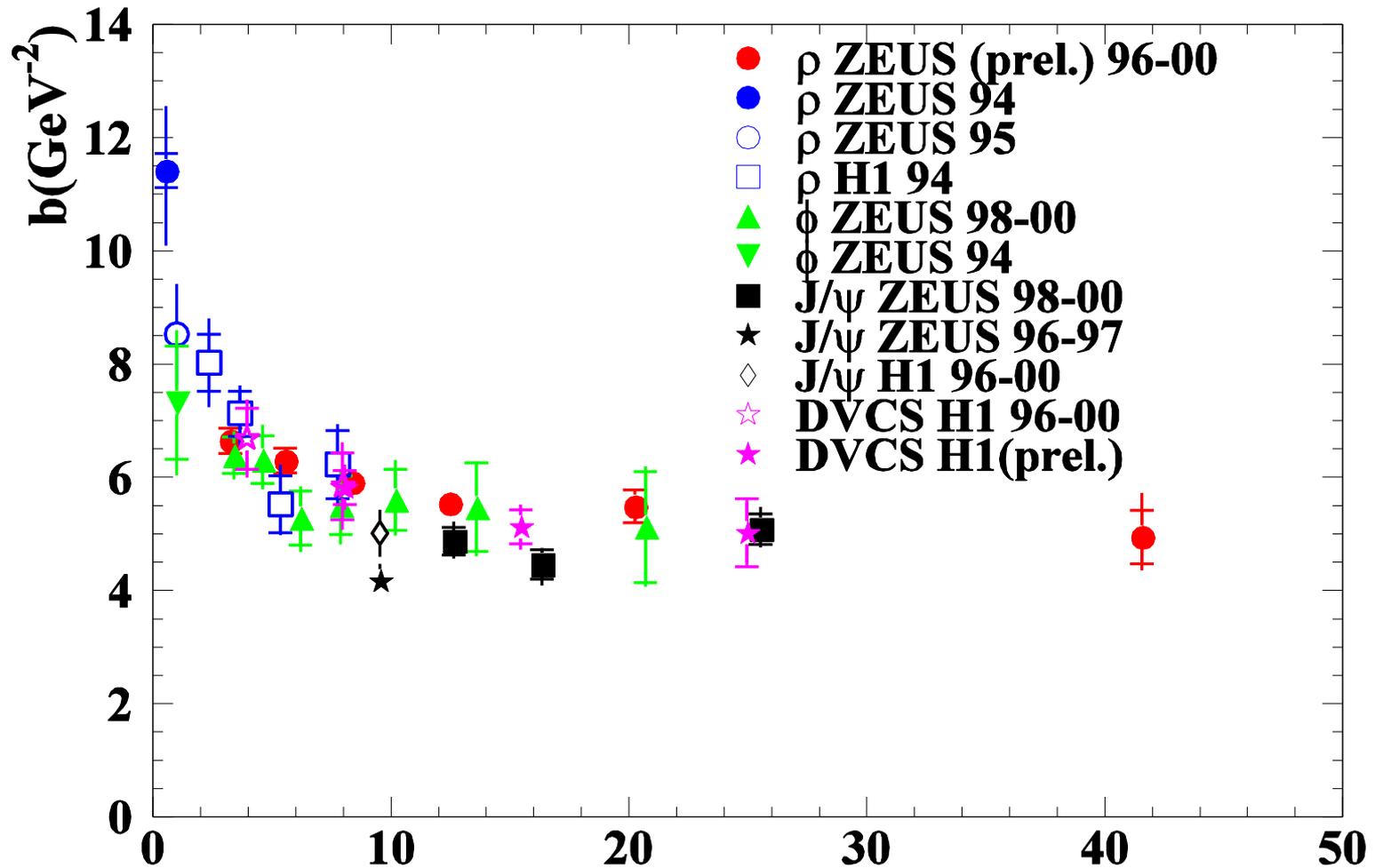
2. The t - and $\tilde{Q}^2 = Q^2 + M_V^2$ - dependences are combined by geometrical considerations: the slope is related to the masses/virtualities of the external particles (see next figure);

A rough estimates, expected to be valid both for leptons and haddrons is (to be fine-tuned!)

$$\beta(t, M, Q^2) = \exp\left[4\left(\frac{1}{M_V^2 + Q^2} + \frac{1}{2m_N^2}\right)t\right].$$

3. There is only one, universal, Pomeron, but it has two components - soft and hard, their relative weights depending on \tilde{Q}^2 .

$b(Q^2+M^2) - VM$



Magic formula : $\langle r^2 \rangle = b \cdot \hbar c$

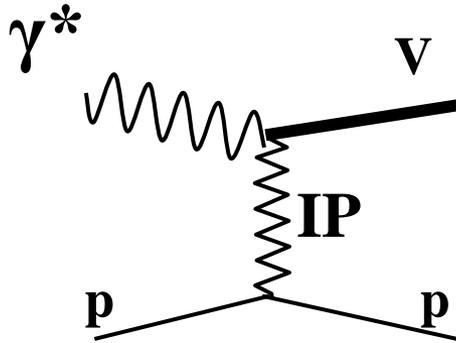
$r_{glue} = 0.56 \text{ fm}$

$r_{proton} = 0.8 \text{ fm}$

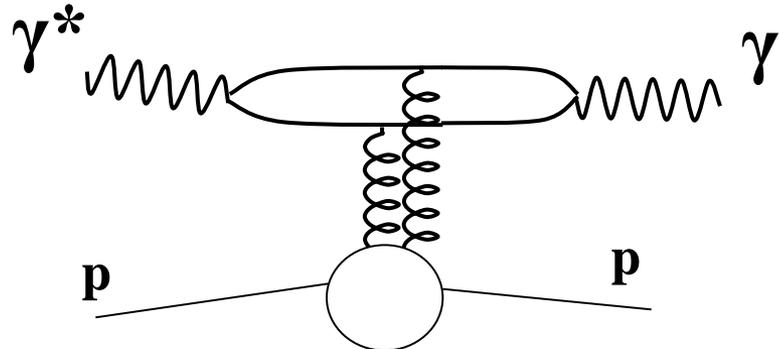
$Q^2+M^2(\text{GeV}^2)$

Deeply Virtual Compton Scattering

VM ($\rho, \omega, \varphi, J/\psi, Y$)



DVCS (γ)



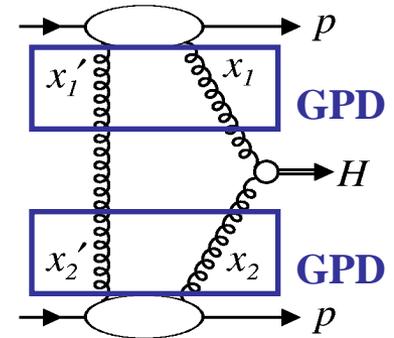
Scale: $Q^2 + M^2$



Q^2

DVCS properties:

- Similar to VM production, but γ instead of VM in the final state
- No VM wave-function involved
- Important to determine Generalized Parton Distributions sensible to the correlations in the proton
- GPD_s are an ingredient for estimating diffractive cross sections at the LHC



Pomeron Trajectory

Regge-type: $\frac{d\sigma}{dt}(W) = \exp(b_0 t) W^{2[2\alpha_{IP}(t)+2]}$

First measured in h-h scattering



Soft Pomeron values

$$\alpha(0) \approx 1.09$$

$$\alpha' \approx 0.25$$

Linear Pomeron trajectory

$$\alpha(t) = \alpha(0) + \alpha'(t)t$$

$\alpha(0)$ and α' are fundamental parameters to represent the basic features of strong interactions

$\alpha(0)$: determines the energy dependence of the diff. Cross section

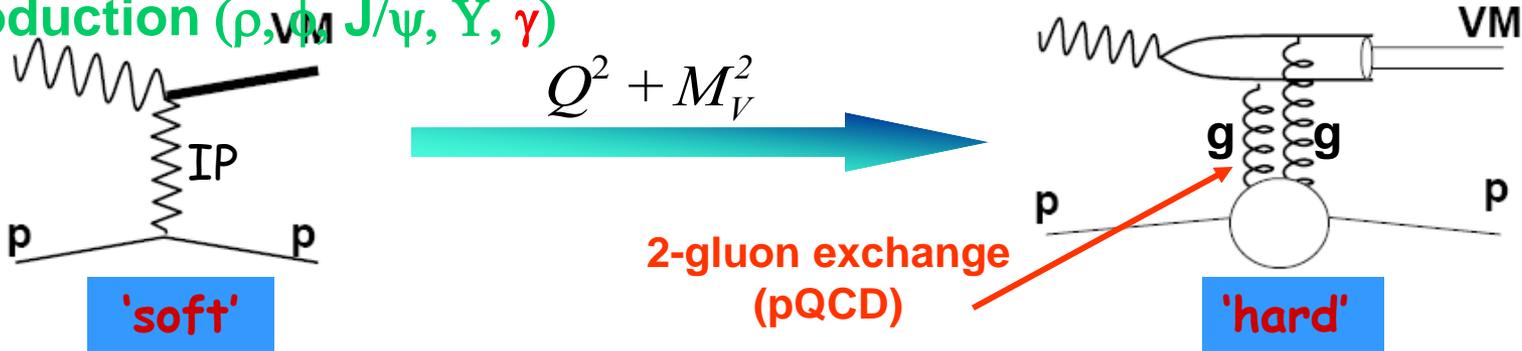
$$\frac{d\sigma}{dt} \propto \exp(b_0 t) W^{4\alpha(t)-4} = W^{4\underline{\alpha(0)}-4} \cdot \exp(bt); \quad b = b_0 + 4\underline{\alpha'} \ln(W)$$

α' : determines the energy dependence of the transverse extension system

Diffraction: soft -> hard

Vector Meson

production ($\rho, \phi, J/\psi, Y, \gamma$)



Gluon density in the proton

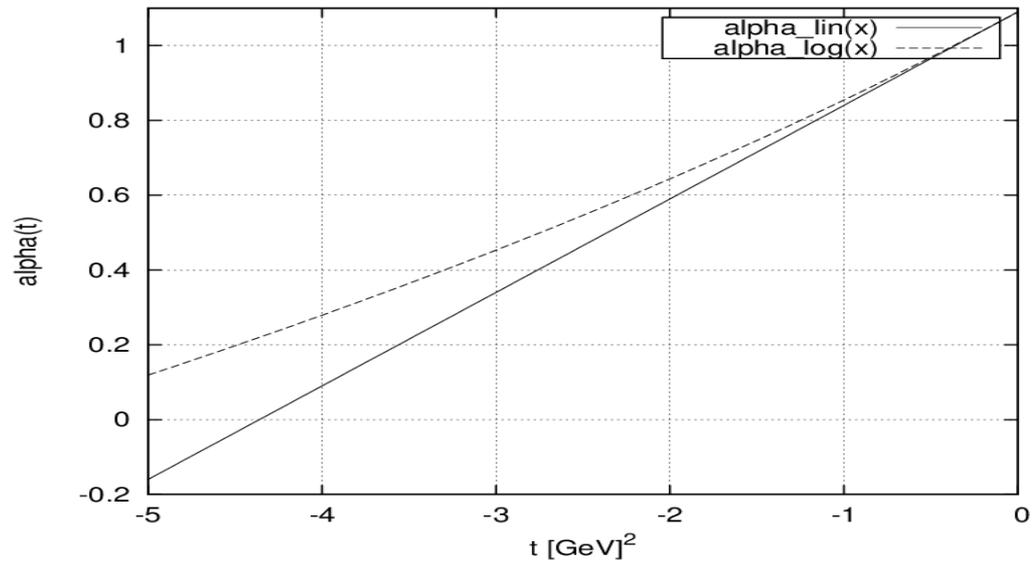
Cross section proportional to probability of finding 2 gluons in the proton

$$\begin{cases} \sigma \propto [x g(x, \mu^2)]^2 \\ \mu^2 \propto (Q^2 + M_V^2) \end{cases}$$

$\sigma(W) \propto W^\delta \Rightarrow \delta$ increases from soft (~ 0.2 , "soft Pomeron") to hard (~ 0.8 , "hard Pomeron")

$\frac{d\sigma}{dt} \propto e^{-b|t|} \Rightarrow b$ decreases from soft ($\sim 10 \text{ GeV}^{-2}$) to hard ($\sim 4-5 \text{ GeV}^{-2}$)

alpha-lin=1.09+0.25 t and alpha-log=1.09-2*ln(1-0.125 t) vs t



$$\begin{aligned}
A(s, t, Q^2, M_v^2) &= \frac{\tilde{A}_s}{\left(1 + \frac{\tilde{Q}^2}{Q_s^2}\right)^{n_s}} e^{-i\frac{\pi}{2}\alpha_s(t)} \left(\frac{s}{s_{0s}}\right)^{\alpha_s(t)} e^{2\left(\frac{a_s}{Q^2} + \frac{b_s}{2m_p^2}\right)t} \\
&+ \frac{\tilde{A}_h \left(\frac{\tilde{Q}^2}{Q_h^2}\right)}{\left(1 + \frac{\tilde{Q}^2}{Q_h^2}\right)^{n_h+1}} e^{-i\frac{\pi}{2}\alpha_h(t)} \left(\frac{s}{s_{0h}}\right)^{\alpha_h(t)} e^{2\left(\frac{a_h}{Q^2} + \frac{b_h}{2m_p^2}\right)t}
\end{aligned}$$

$$\frac{d\sigma_{el}}{d|t|} = H_s^2 e^{2L_s(\alpha_s(t)-1)+g_s t} + H_h^2 e^{2L_h(\alpha_h(t)-1)+g_h t} \\ + 2H_s H_h e^{L_s(\alpha_s(t)-1)+L_h(\alpha_h(t)-1)+(g_s+g_h)t} \cos\left(\frac{\pi}{2}(\alpha_s(t) - \alpha_h(t))\right)$$

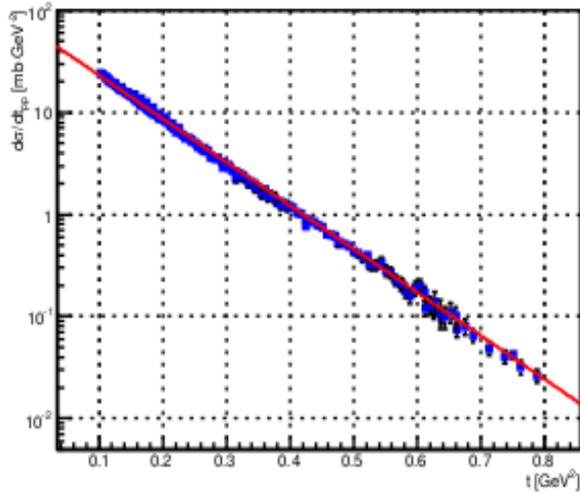
$$H_s = \frac{A_s}{\left(1 + \frac{\widetilde{Q}^2}{Q_s^2}\right)^{n_s}} \quad H_h = \frac{A_h \left(\frac{\widetilde{Q}^2}{Q_h^2}\right)}{\left(1 + \frac{\widetilde{Q}^2}{Q_h^2}\right)^{n_h+1}}$$

$$L_s = \ln \left(\frac{s}{s_{0s}} \right) \quad g_s = 2 \left(\frac{a_s}{\widetilde{Q}^2} + \frac{b_s}{2m_p^2} \right) \quad \alpha_s(t) = \alpha_{0s} + \alpha'_s t$$

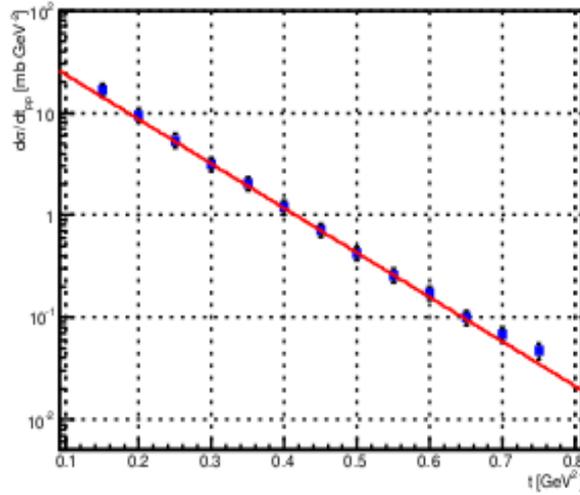
$$L_h = \ln \left(\frac{s}{s_{0h}} \right) \quad g_h = 2 \left(\frac{a_h}{\widetilde{Q}^2} + \frac{b_h}{2m_p^2} \right) \quad \alpha_h(t) = \alpha_{0h} + \alpha'_h t$$

pp

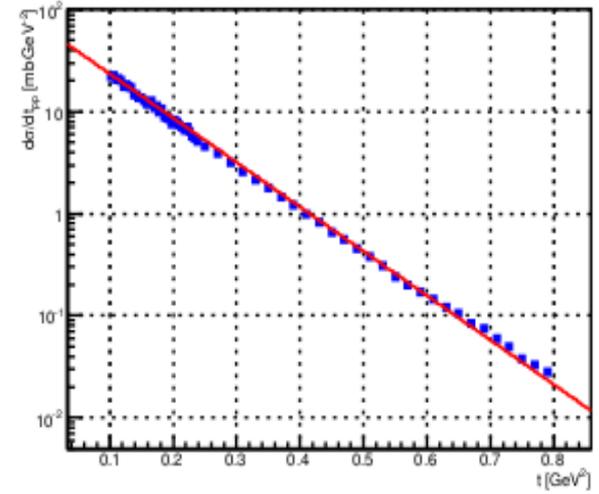
" $d\sigma/dt_{pp}(W,t)$ "|W 19.42 [GeV]



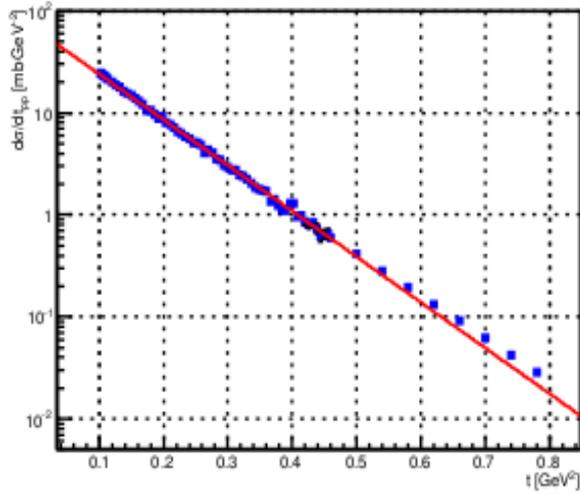
" $d\sigma/dt_{pp}(W,t)$ "|W 23.45 [GeV]



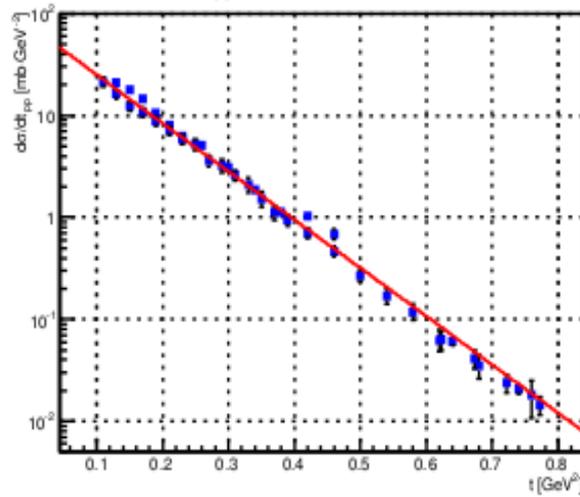
" $d\sigma/dt_{pp}(W,t)$ "|W 23.51 [GeV]



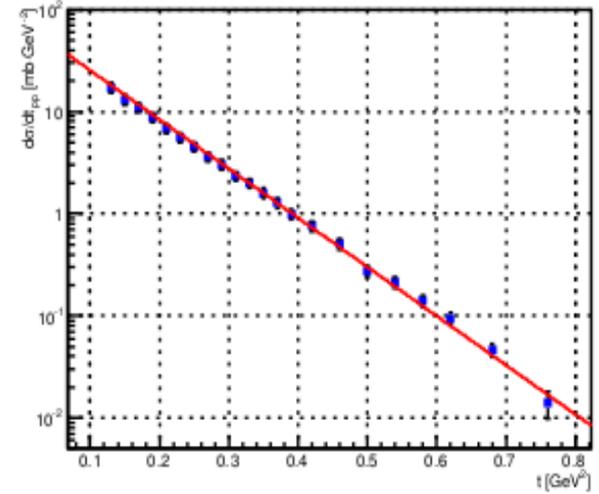
" $d\sigma/dt_{pp}(W,t)$ "|W 30.70 [GeV]



" $d\sigma/dt_{pp}(W,t)$ "|W 53.02 [GeV]

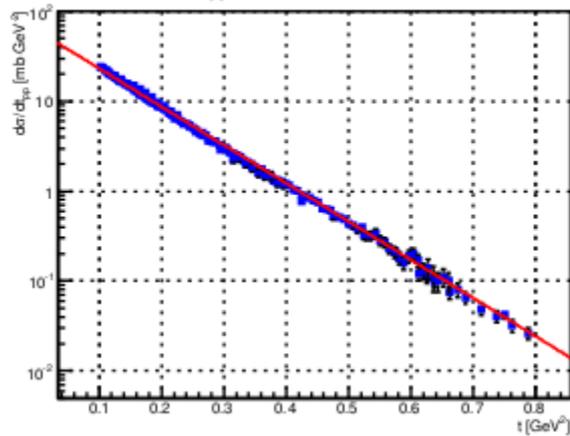


" $d\sigma/dt_{pp}(W,t)$ "|W 62.01 [GeV]

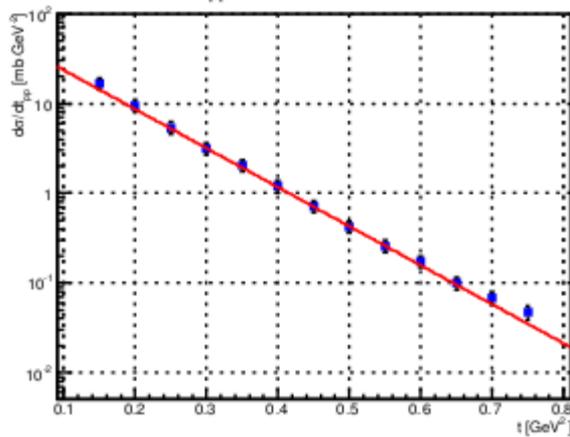


pp

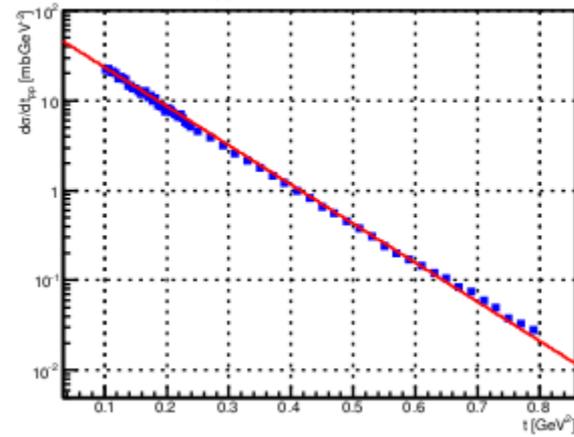
" $d\sigma/dt_{pp}(W,t)$ "|W 19.42 [GeV]



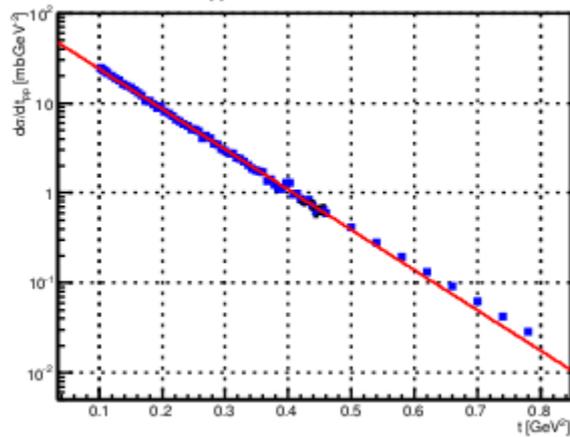
" $d\sigma/dt_{pp}(W,t)$ "|W 23.45 [GeV]



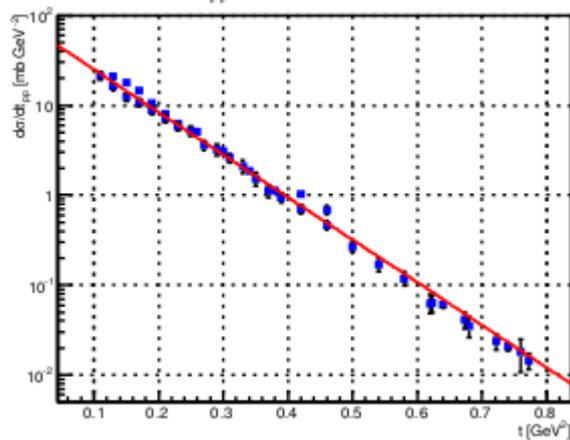
" $d\sigma/dt_{pp}(W,t)$ "|W 23.51 [GeV]



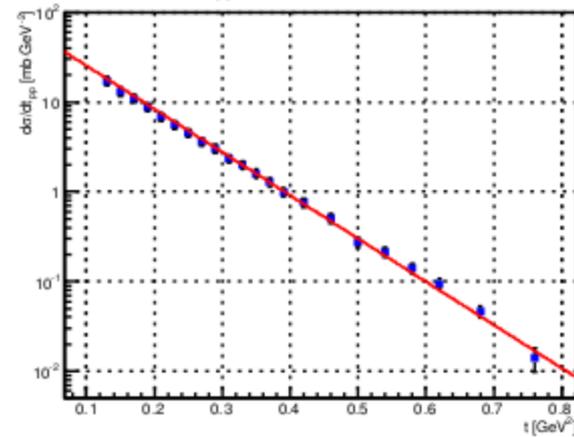
" $d\sigma/dt_{pp}(W,t)$ "|W 30.70 [GeV]



" $d\sigma/dt_{pp}(W,t)$ "|W 53.02 [GeV]

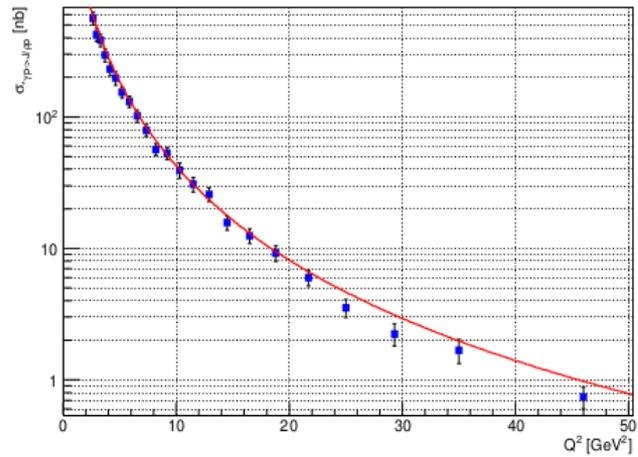


" $d\sigma/dt_{pp}(W,t)$ "|W 62.01 [GeV]

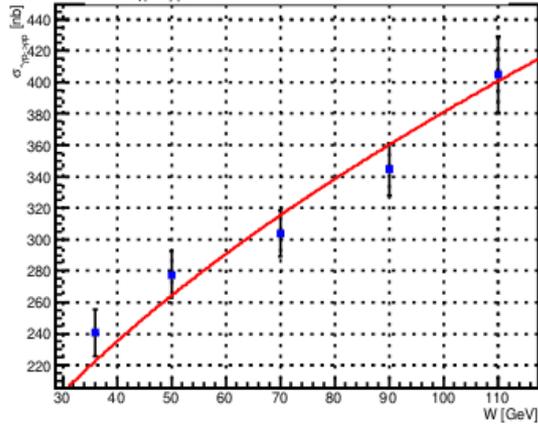


rho0(1)

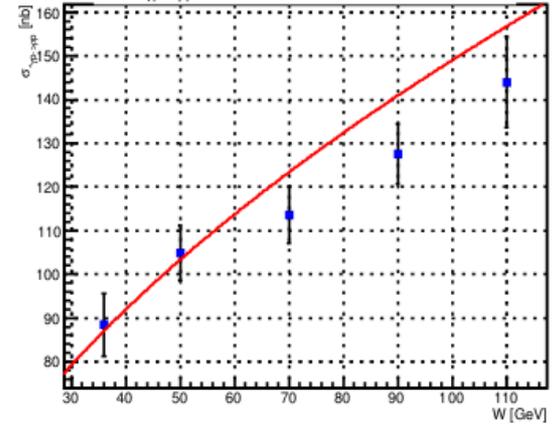
" $\sigma_{\gamma p \rightarrow \rho p}$ #h3 2009"|W 75.00 [GeV]



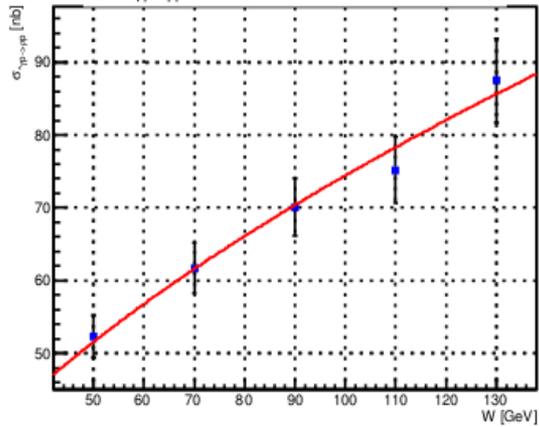
" $\sigma_{\gamma p \rightarrow \rho p}$ #z6 2007"|Q² 3.70 [GeV²]



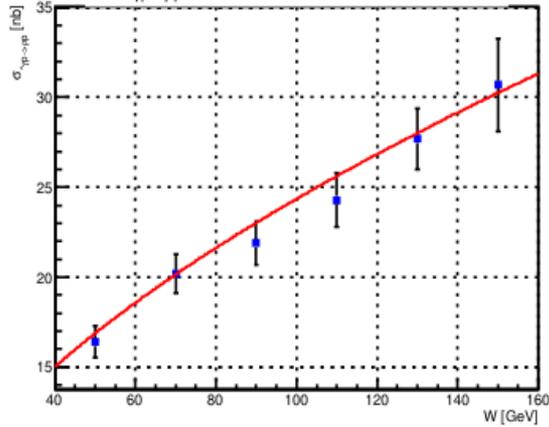
" $\sigma_{\gamma p \rightarrow \rho p}$ #z6 2007"|Q² 6.00 [GeV²]



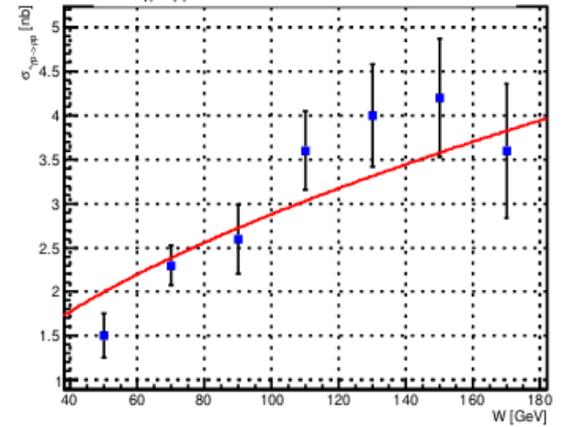
" $\sigma_{\gamma p \rightarrow \rho p}$ #z6 2007"|Q² 8.30 [GeV²]



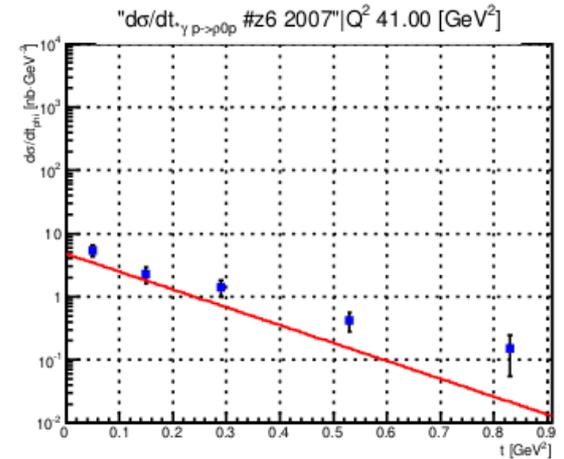
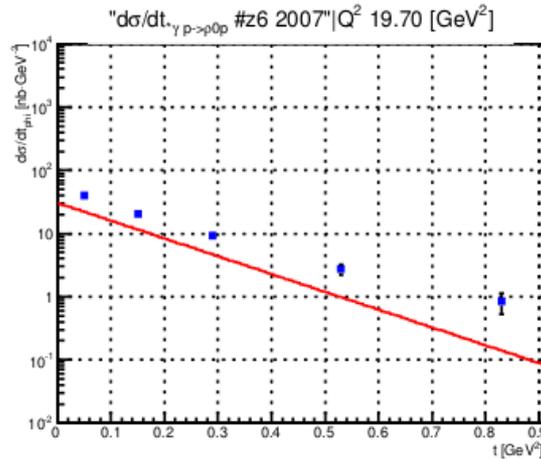
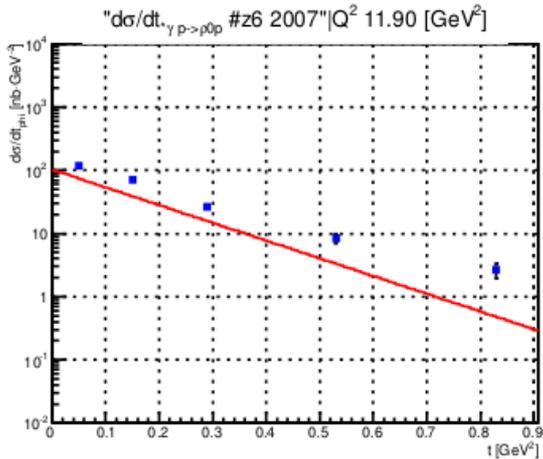
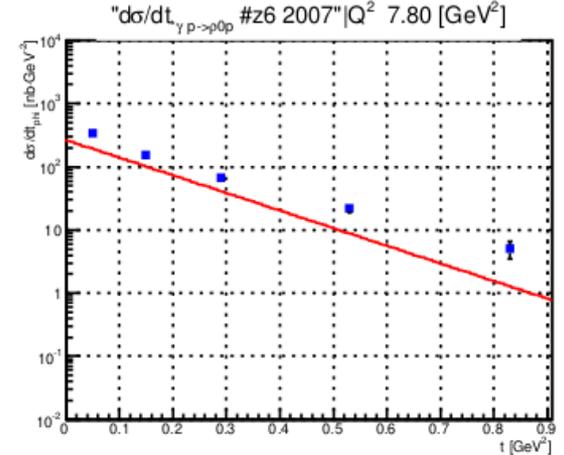
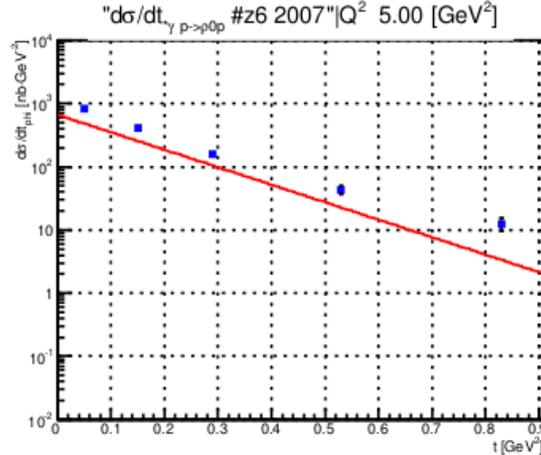
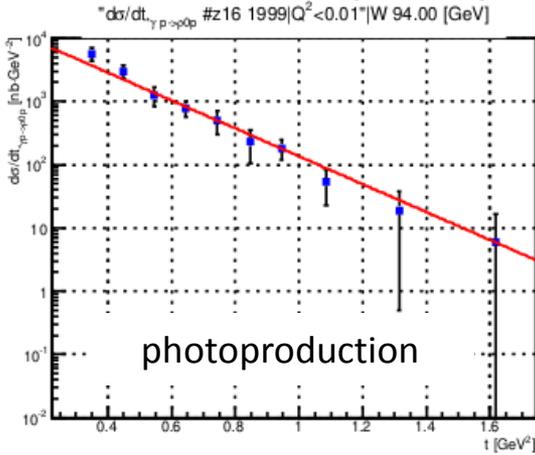
" $\sigma_{\gamma p \rightarrow \rho p}$ #z6 2007"|Q² 13.50 [GeV²]



" $\sigma_{\gamma p \rightarrow \rho p}$ #z6 2007"|Q² 32.00 [GeV²]



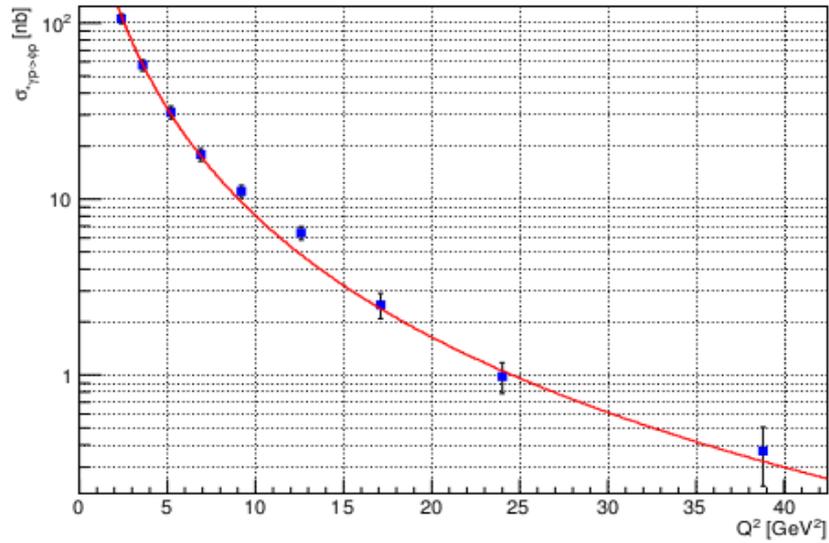
rho0 (2)



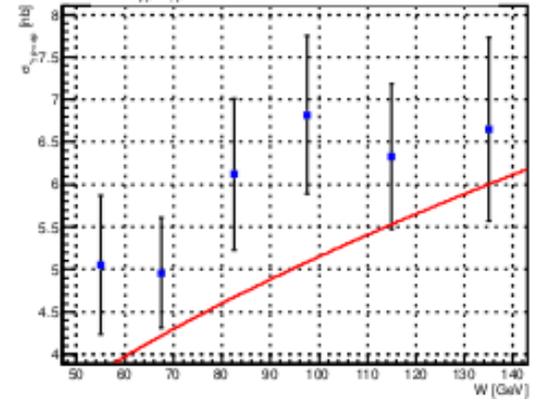
ZEUS 2007, $W = 90\text{GeV}^2$, electroproduction

phi (1)

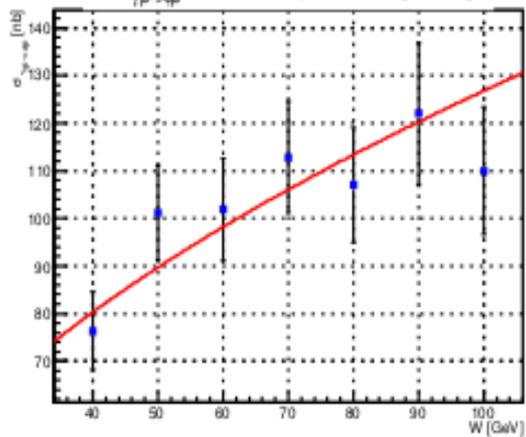
" $\sigma_{\gamma p \rightarrow \phi p}$ #z8 2005"|W 75.00 [GeV]



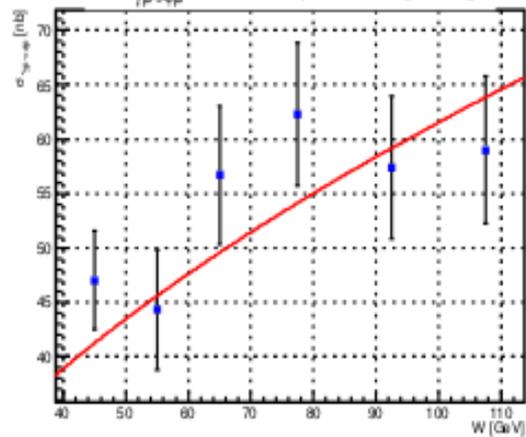
" $\sigma_{\gamma p \rightarrow \phi p}$ #z8 2005"| Q^2 13.00 [GeV^2]



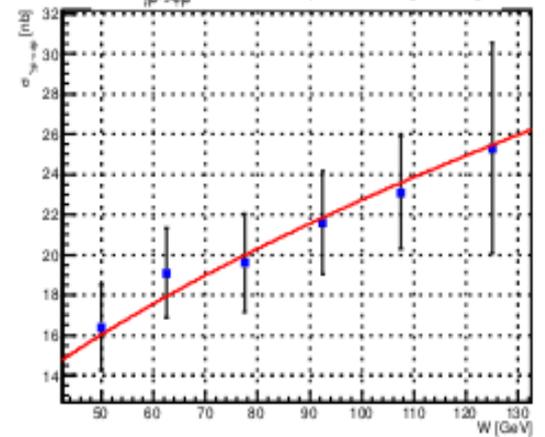
" $\sigma_{\gamma p \rightarrow \phi p}$ #z8 2005"| Q^2 2.40 [GeV^2]



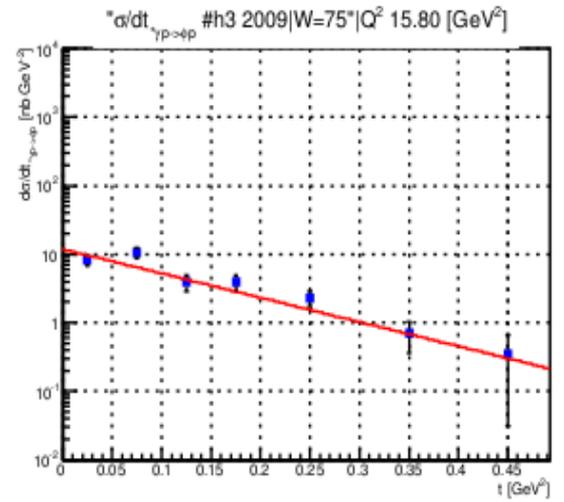
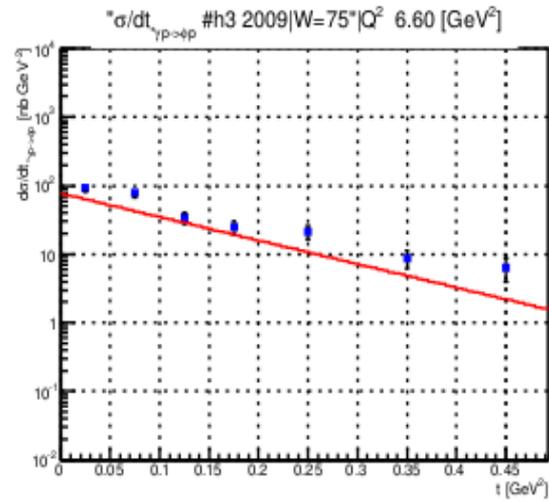
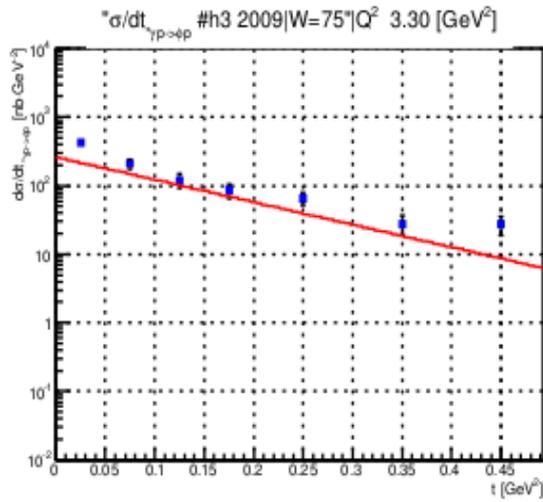
" $\sigma_{\gamma p \rightarrow \phi p}$ #z8 2005"| Q^2 3.80 [GeV^2]



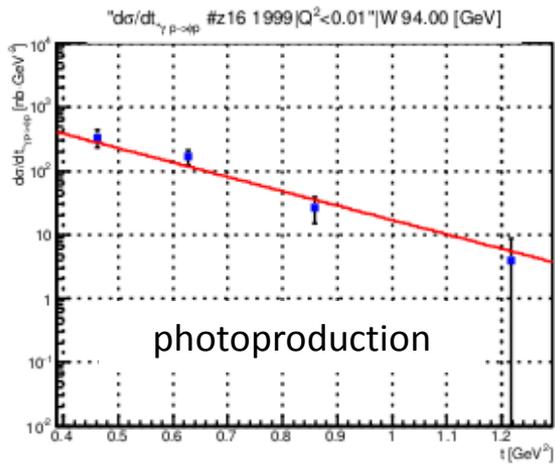
" $\sigma_{\gamma p \rightarrow \phi p}$ #z8 2005"| Q^2 6.50 [GeV^2]



phi (2)

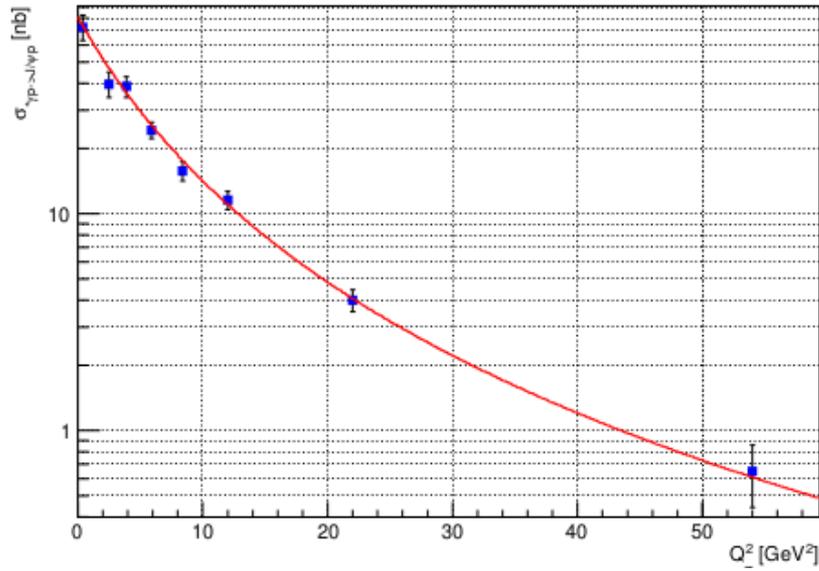


electroproduction

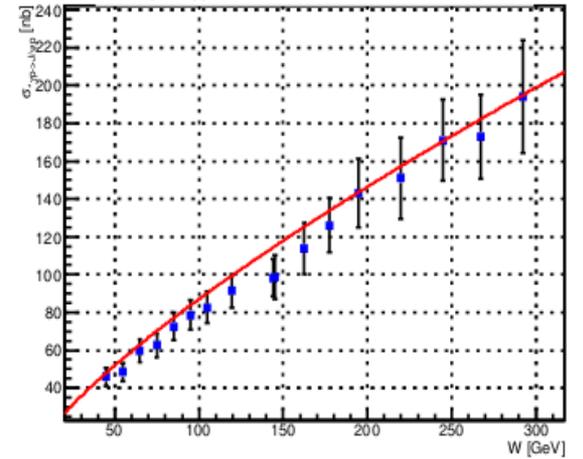


J/psi (1)

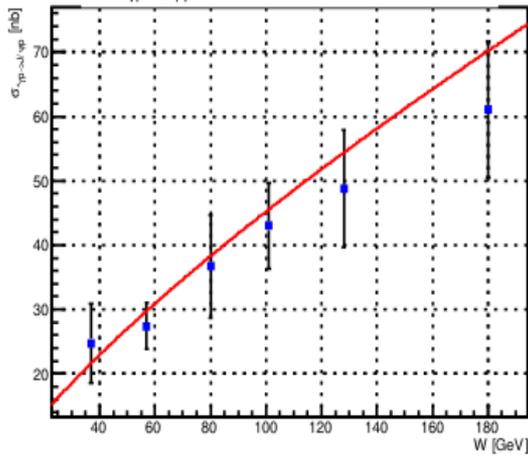
" $\sigma_{\gamma p \rightarrow J/\psi p}$ #z9 2004" | W 90.00 [GeV]



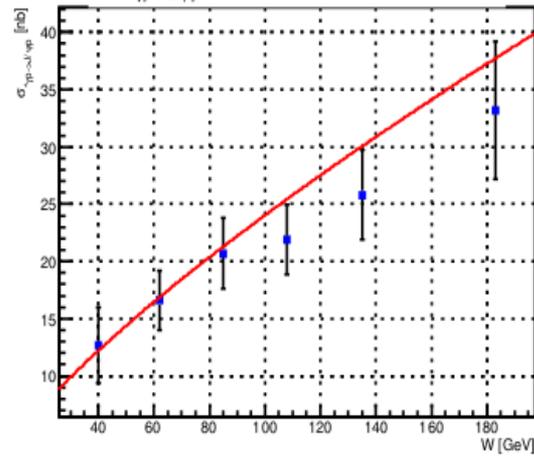
" $\sigma_{\gamma p \rightarrow J/\psi p}$ #h6 2005" | Q^2 0.05 [GeV^2]



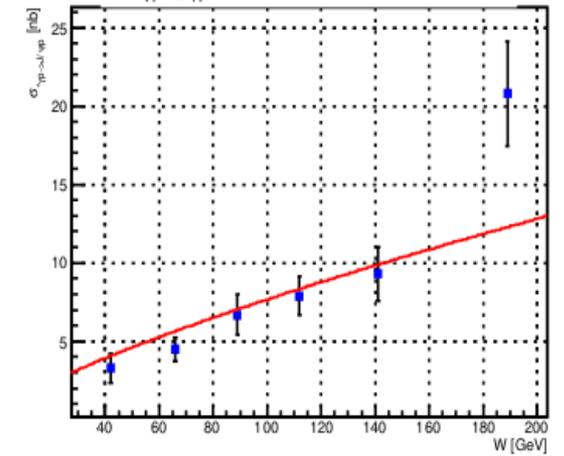
" $\sigma_{\gamma p \rightarrow J/\psi p}$ #z9 2004" | Q^2 3.10 [GeV^2]



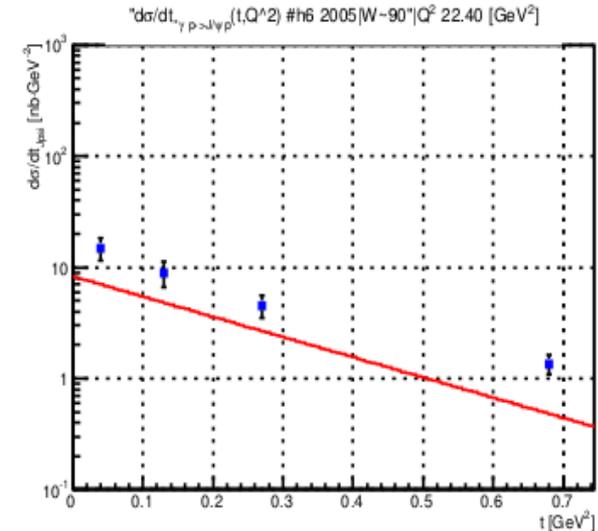
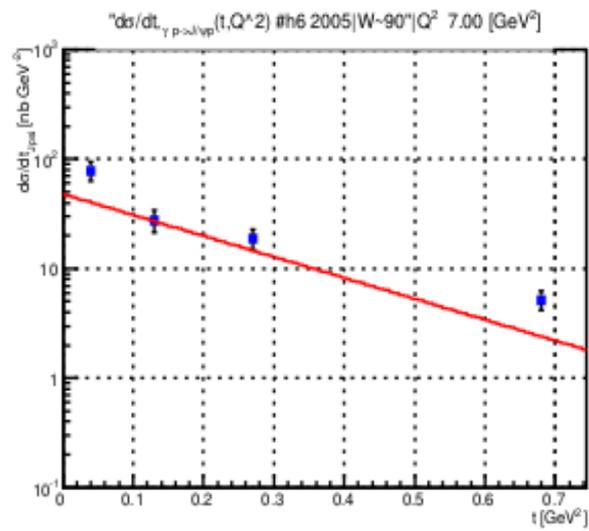
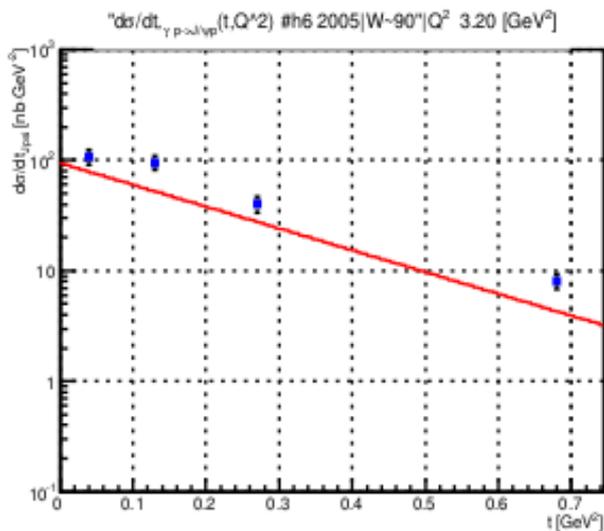
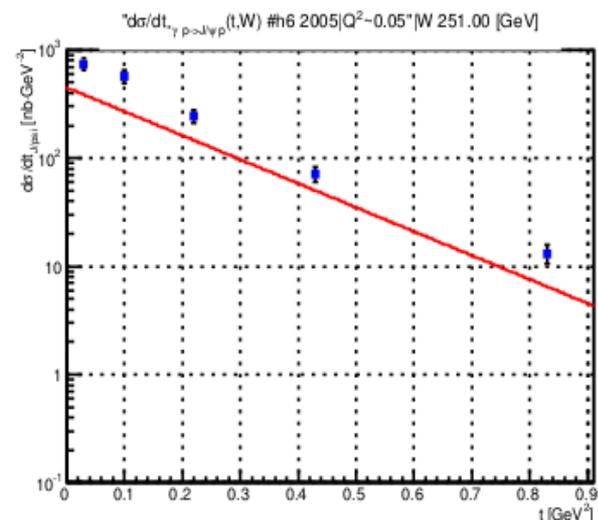
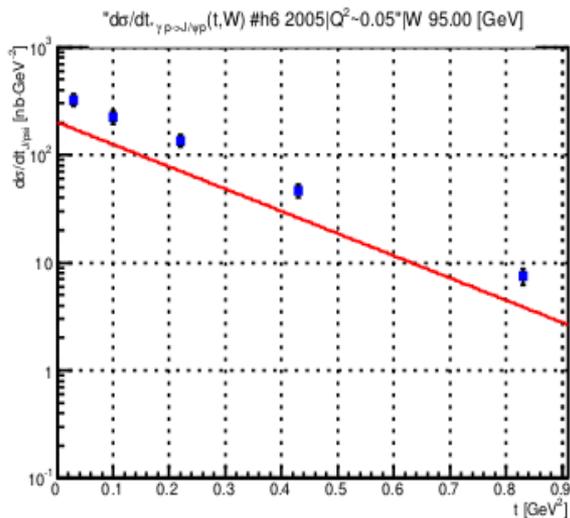
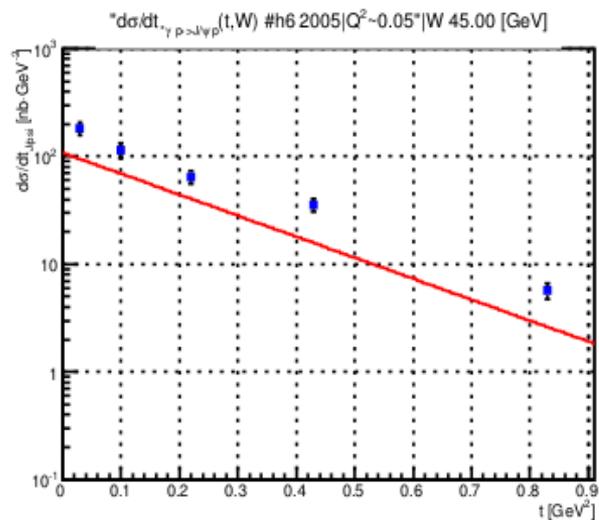
" $\sigma_{\gamma p \rightarrow J/\psi p}$ #z9 2004" | Q^2 6.80 [GeV^2]



" $\sigma_{\gamma p \rightarrow J/\psi p}$ #z9 2004" | Q^2 16.00 [GeV^2]

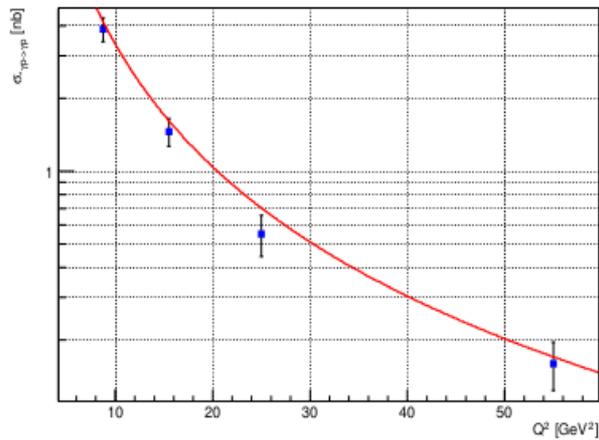


J/psi (2)

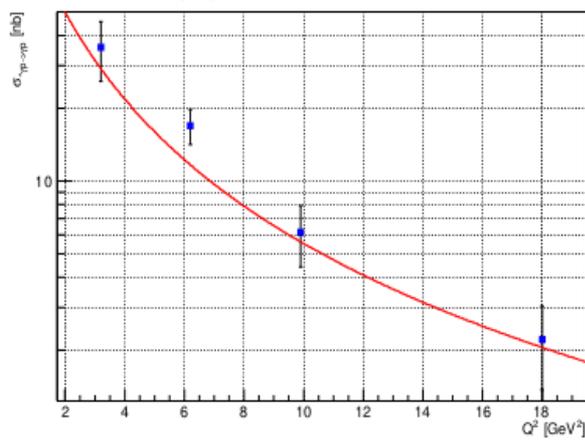


DVCS (1)

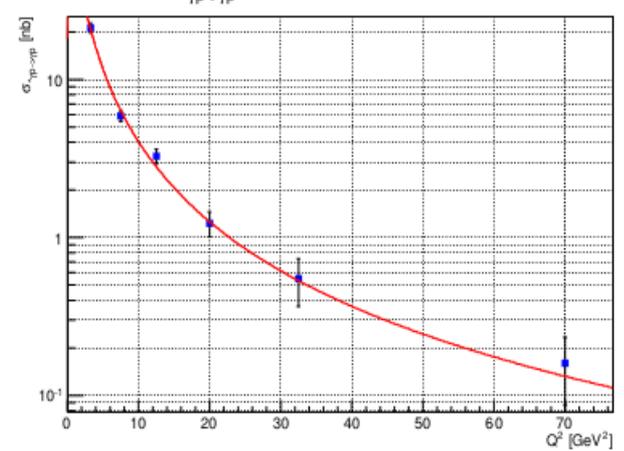
" $\sigma_{\gamma p \rightarrow \gamma p}$ #h2 2009" | W 82.00 [GeV]



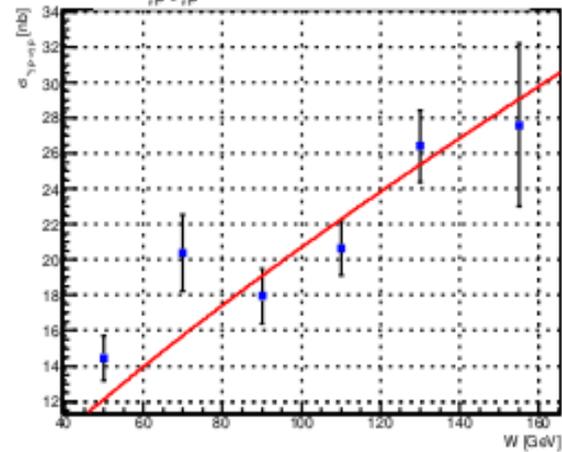
" $\sigma_{\gamma p \rightarrow \gamma p}$ #z5 2008" | W 155.00 [GeV]



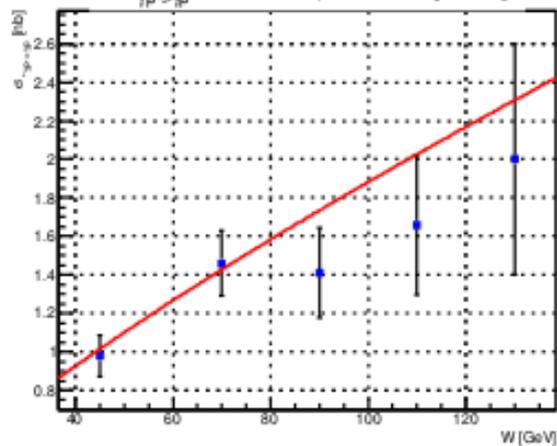
" $\sigma_{\gamma p \rightarrow \gamma p}$ #z5 2008" | W 104.00 [GeV]



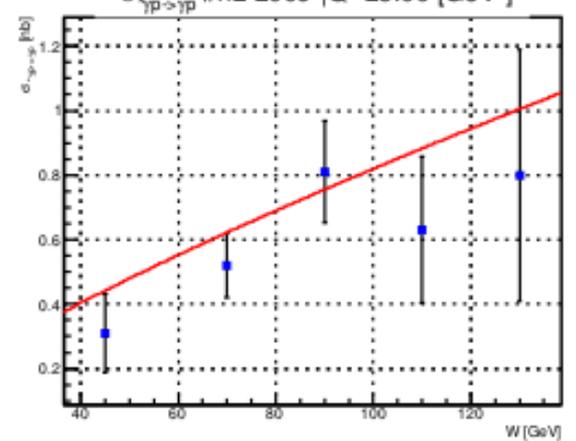
" $\sigma_{\gamma p \rightarrow \gamma p}$ #z5 2008" | Q² 3.20 [GeV²]



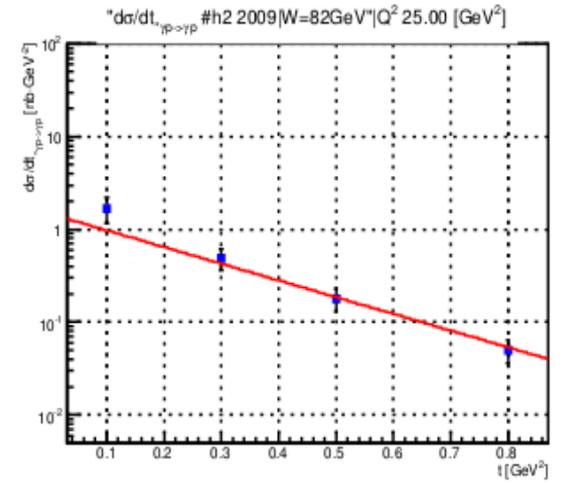
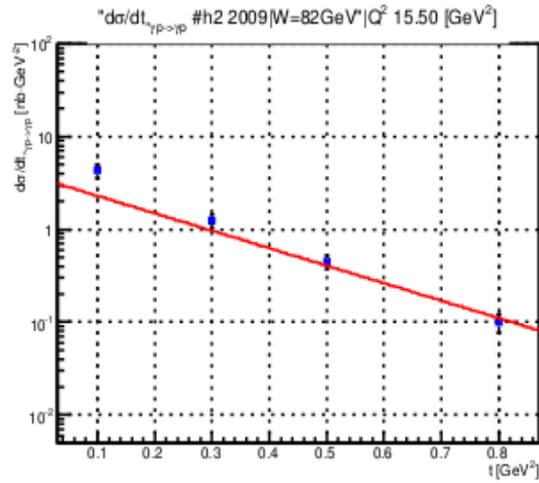
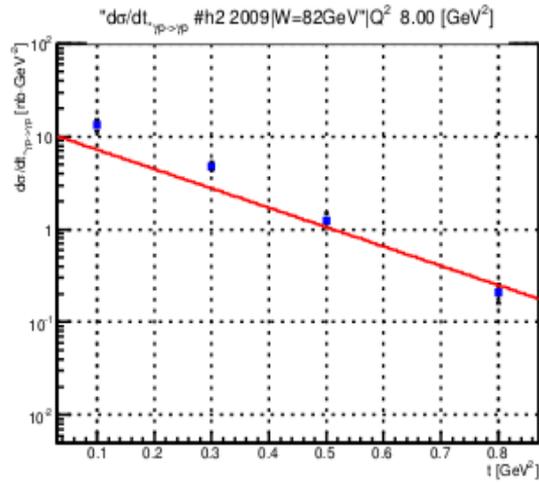
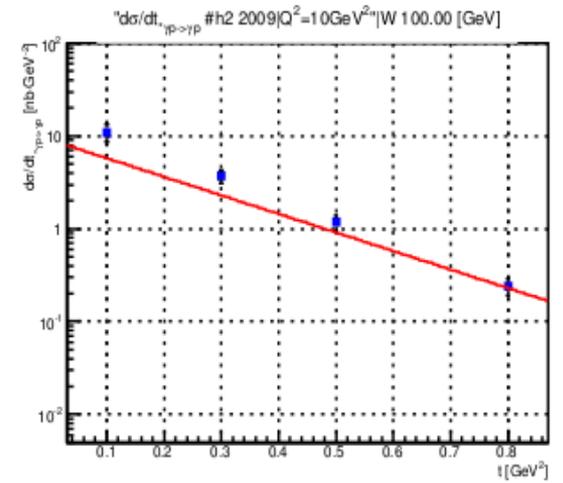
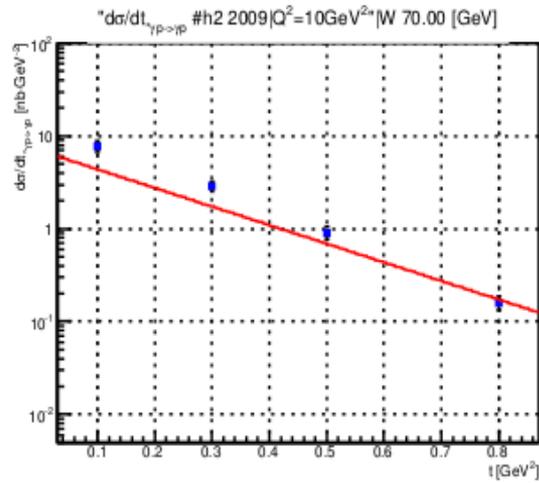
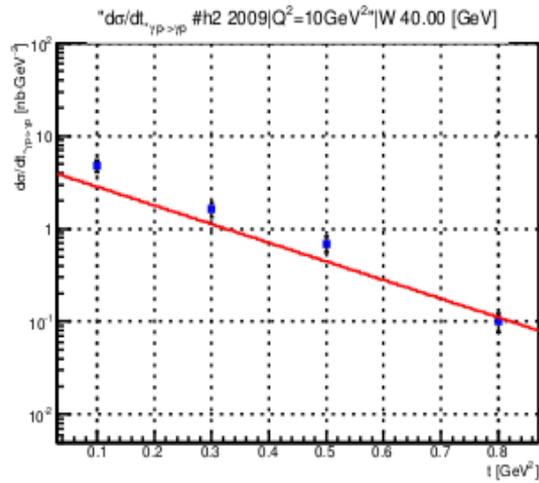
" $\sigma_{\gamma p \rightarrow \gamma p}$ #h2 2009" | Q² 15.50 [GeV²]



" $\sigma_{\gamma p \rightarrow \gamma p}$ #h2 2009" | Q² 25.00 [GeV²]



DVCS (2)

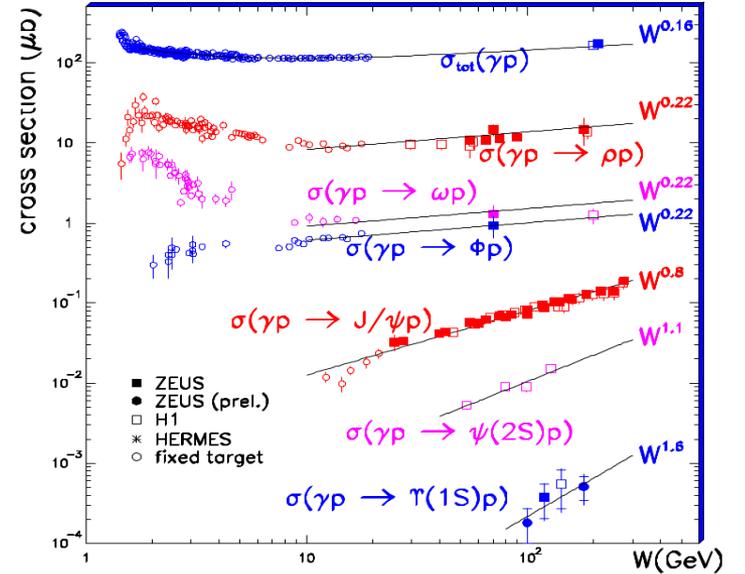


| | A_s | \widetilde{Q}_s^2 | n_s | α_{0s} | α'_s | a_s | b_s | $\widetilde{\chi}^2$ |
|----------------|-----------------|---------------------|-----------------|-----------------|-------------------|-------------------|-----------------|----------------------|
| pp | 5.9 ± 5.7 | *** | 0.00 | 1.05 ± 0.14 | 0.276 ± 0.474 | 2.877 ± 2.837 | 0.00 | 1.52 |
| ρ^0 | 59.5 ± 29.3 | 1.33 | 1.35 ± 0.05 | 1.15 ± 0.06 | 0.15 | -0.22 | 1.69 | 6.56 |
| ϕ | 31.8 ± 35.3 | 1.30 | 1.32 ± 0.10 | 1.14 ± 0.12 | 0.15 | -0.85 ± 1.60 | 2.51 ± 2.67 | 3.81 |
| J/ψ | 34.2 ± 19.0 | 1.4 ± 0.7 | 1.39 ± 0.13 | 1.21 ± 0.05 | 0.09 | 1.90 | 1.03 | 4.50 |
| $\Upsilon(1S)$ | 37 ± 101 | 0.9 ± 1.7 | 1.53 ± 0.55 | 1.29 ± 0.26 | 0.01 ± 0.6 | 1.90 | 1.03 | 1.28 |
| $DVCS$ | 9.7 ± 9.0 | 0.45 ± 0.5 | 0.94 ± 0.24 | 1.19 ± 0.09 | -0.007 ± 0.3 | 1.94 ± 4.65 | 1.74 ± 2.28 | 1.75 |

Table 1. Fitting results

| | δ | α_{0s} | $\alpha_{0s}(fit)$ | α'_s |
|----------------|----------|---------------|--------------------|-------------------|
| pp | | 1.08(DL) | 1.05 ± 0.14 | 0.276 ± 0.474 |
| ρ^0 | 0.22 | 1.055 | 1.15 ± 0.06 | 0.15 |
| ϕ | 0.22 | 1.055 | 1.14 ± 0.12 | 0.15 |
| J/ψ | 0.8 | 1.2 | 1.21 ± 0.05 | 0.09 |
| $\Upsilon(1S)$ | 1.6 | 1.4 | 1.29 ± 0.26 | 0.01 ± 0.6 |
| $DVCS$ | 0.54 | 1.135 | 1.19 ± 0.09 | -0.007 ± 0.3 |

Table 2. $\alpha(0)$, α'



(a) The W dependence of the cross section for exclusive VM photoproduction together with the total photoproduction cross section. Lines are the result of a W^δ fit to the data at high W -energy values.

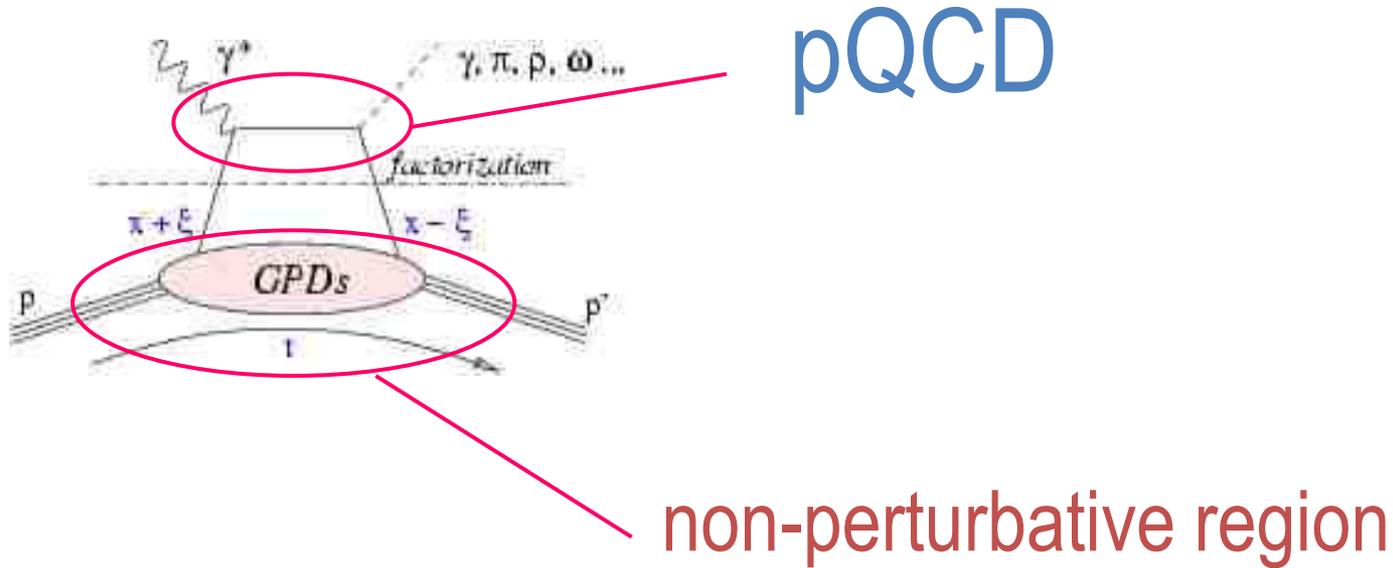
Parameter s_{0s} for simplicity is also fixed $s_{0s} = 1$.

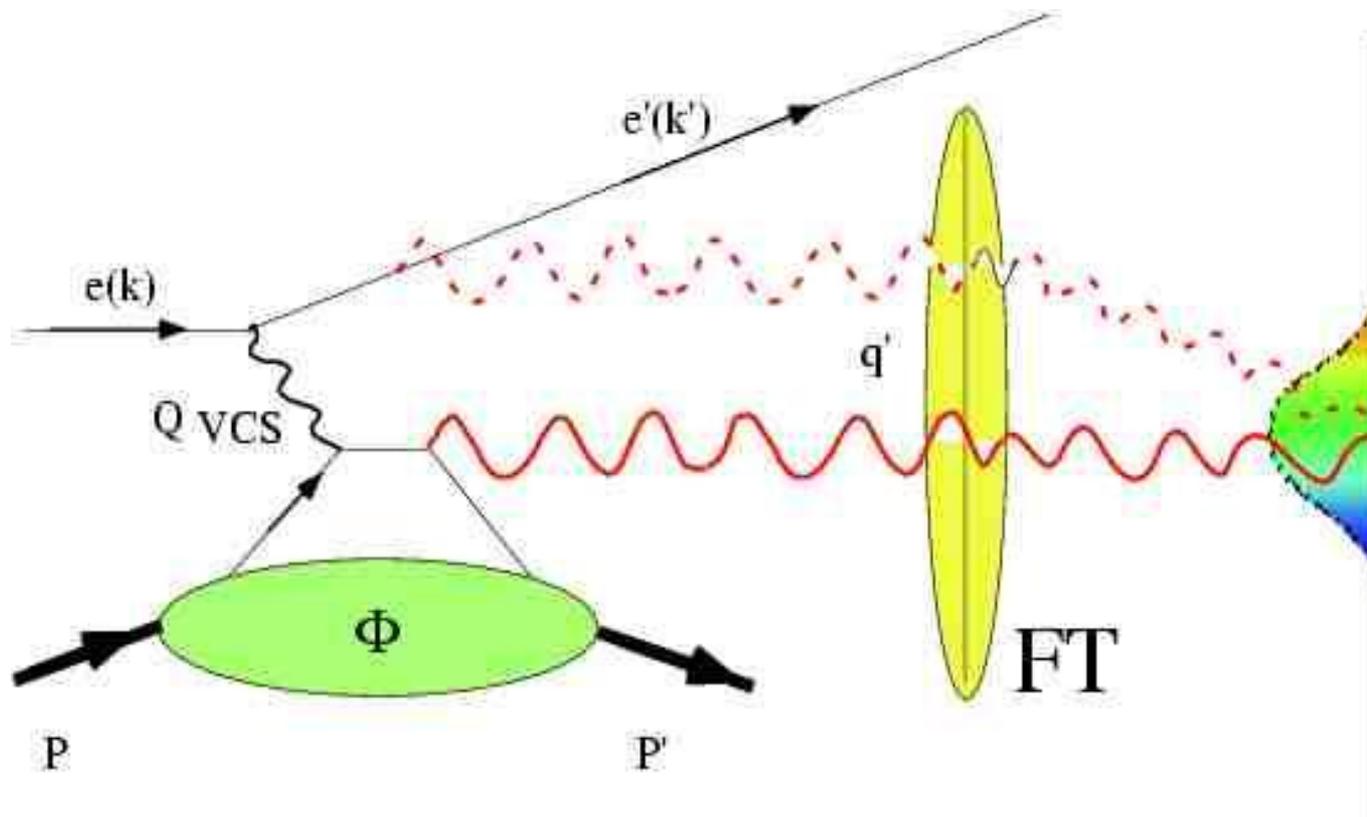
* Parameters that doesn't have errors in table[1] were fixed at fitting stage.

Conclusions and prospects:

1. There is one, unique Pomeron, but it may have many components (e.d. “soft” and “hard”).
 2. Regge trajectories are non-linear.
1. DVCS and VMP – a tool to access to GPD (below):

QCD-factorized form of a DVCS scattering amplitude

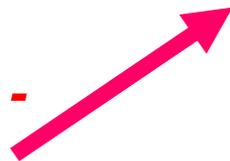




GPDs cannot be measured directly,
instead they appear as convolution integrals,
difficult to be inverted !

$$A(\xi, \eta, t) \sim \int_{-1}^1 dx \frac{GPD(x, \eta, t)}{x - \xi + i\varepsilon}$$

*We need clues from
phenomenological models -
Regge behaviour, t-
factorization etc.*



$$\sigma_{tot} \sim \Im m A,$$

$$\frac{d\sigma}{dt} \sim |A|^2$$

“Handbag”