

# Andreas Crivellin

Albert Einstein Center for Fundamental Physics,  
Institut for Theoretical Physics,  
**Bern**



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**Right-handed effects in  $V_{ub}$  (and  $V_{cb}$ )**

# Outline:

- Right-handed  $W$ -coupling in the MSSM
- The determination of  $V_{ub}$  and  $V_{cb}$  in the presence of a right-handed  $W$ -coupling.

# Right-handed W-coupling in the MSSM

# CKM matrix

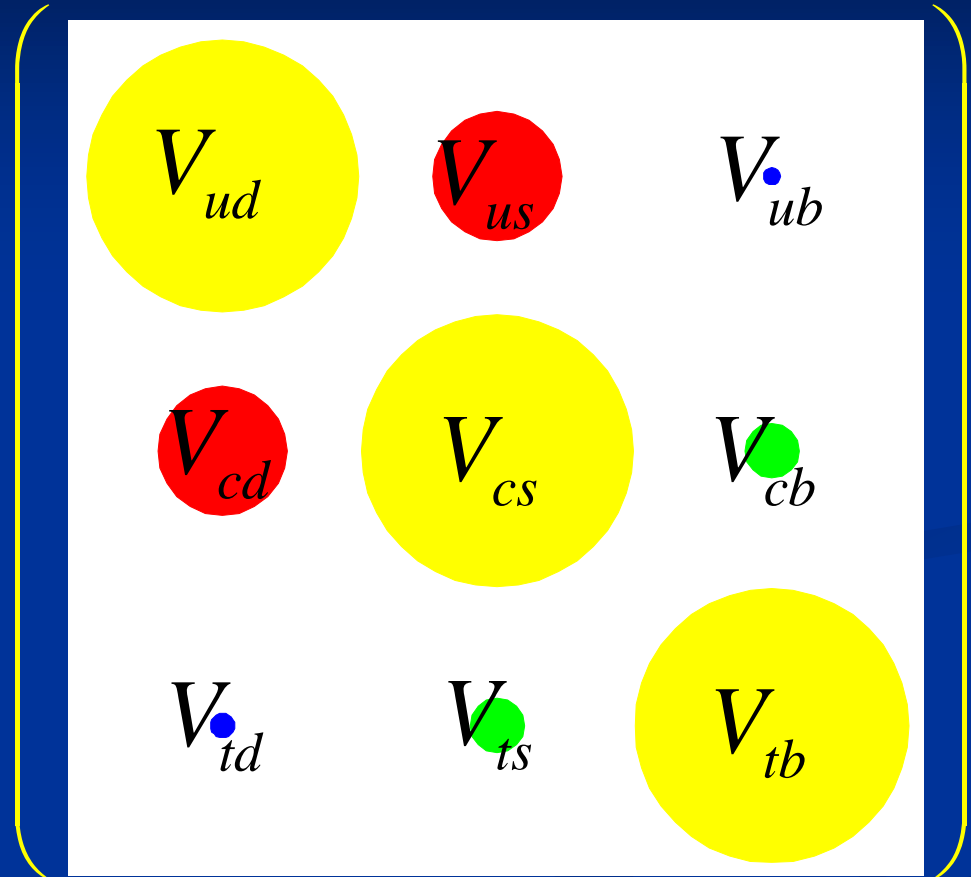
- CKM matrix is the only source of flavor and CP violation in the SM.

- No tree-level FCNCs

$$V_{\text{CKM}} =$$

- Off-diagonal CKM elements are small

➔ Flavor-violation is suppressed in the Standard Model.



# SUSY flavor (CP) problem

- The squark mass matrices are not necessarily diagonal (and real) in the same basis as the quark mass matrices.
- Especially the trilinear **A-terms** can induce dangerously large flavor-mixing (and complex phases) since they don't necessarily respect hierarchy of the SM.
- The MSSM possesses two Higgs-doublets: Flavor-changing charged and (loop-induced) neutral Higgs interactions.

 **Why is the observed flavor violation so small?**

- Possible solutions:
  - MFV D'Ambrosio, Giudice, Isidori, Strumia, 2002
  - Flavor-symmetries
  - effective SUSY, split SUSY
  - **Radiative flavor violation** F. Borzumati et al, 1999. Crivellin et al 2011.

# Squark mass matrix

$$M_{\tilde{q}}^2 = \begin{pmatrix} M_{LL}^{\tilde{q}2} & \Delta^{\tilde{q}LR} \\ \Delta^{\tilde{q}LR\dagger} & M_{RR}^{\tilde{q}2} \end{pmatrix}$$

hermitian:  $\longrightarrow W^{\tilde{q}\dagger} M_{\tilde{q}}^2 W^{\tilde{q}} = M_{\tilde{q}}^{2(D)}$

$M_{LL,RR}^{\tilde{q}2}$  involves only bilinear terms (in the decoupling limit)

The chirality-changing elements are proportional to a vev

$$\Delta_{ij}^{dLR} = -v_d \left( \mu \tan(\beta) Y_i^{d(0)} \delta_{ij} + A_{ij}^d \right)$$

$$\tan(\beta) = \frac{v_u}{v_d}$$

$$\Delta_{ij}^{uLR} = -v_u \left( \mu \cot(\beta) Y_i^{u(0)} \delta_{ij} + A_{ij}^u \right)$$

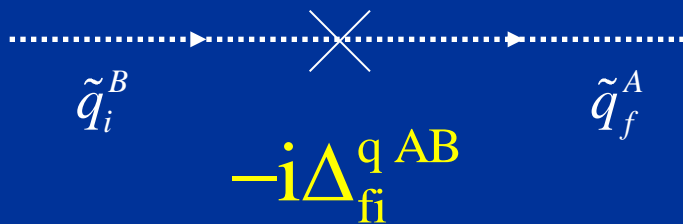
# Mass insertion approximation

(L.J. Hall, V.A. Kostelecky and S. Raby, Nucl. Phys. B 267 (1986) 415.)

- Useful to visualize flavor-changes in the squark sector

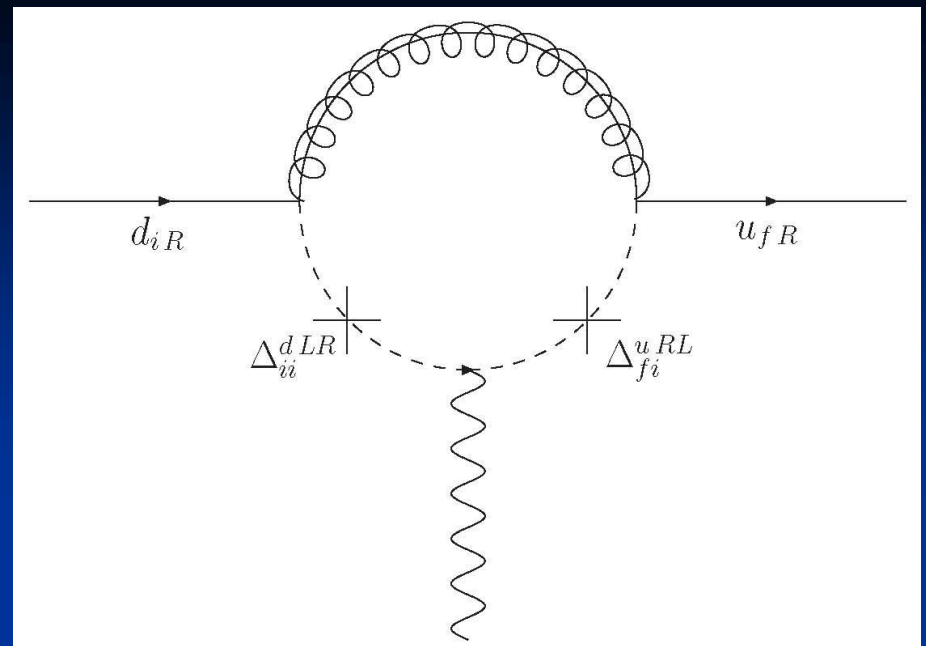
$\Delta_{ij}^{q AB}$  off-diagonal element of the squark mass matrix

- $q = u, d$
- $i, j$  flavor indices 1,2,3
- $A, B$  chiralities L,R



$$\delta_{fi}^{q AB} = \frac{\Delta_{fi}^{q AB} V}{\tilde{m}_{\tilde{q}}^2}$$

# Genuine vertex-correction



$$-i\Lambda_{u_f d_i}^{W \tilde{g}} = \frac{g_2}{\sqrt{2}} \frac{i\alpha_s}{3\pi} \gamma^\mu \sum_{s,t=1}^6 \sum_{j,k=1}^3 \left( W_{fs}^{\tilde{u}} W_{ks}^{\tilde{u}*} V_{kj}^{CKM} W_{jt}^{\tilde{d}} W_{it}^{\tilde{d}*} P_L + W_{f+3,s}^{\tilde{u}} W_{ks}^{\tilde{u}*} V_{kj}^{CKM} W_{jt}^{\tilde{d}} W_{i+3,t}^{\tilde{d}*} P_R \right) C_2(m_{\tilde{u}_s}, m_{\tilde{d}_t}, m_{\tilde{g}})$$

- Corrections to the left-handed coupling suppressed because the hermitian part of the WFR cancels with the genuine vertex correction.
- Right-handed coupling not suppressed!

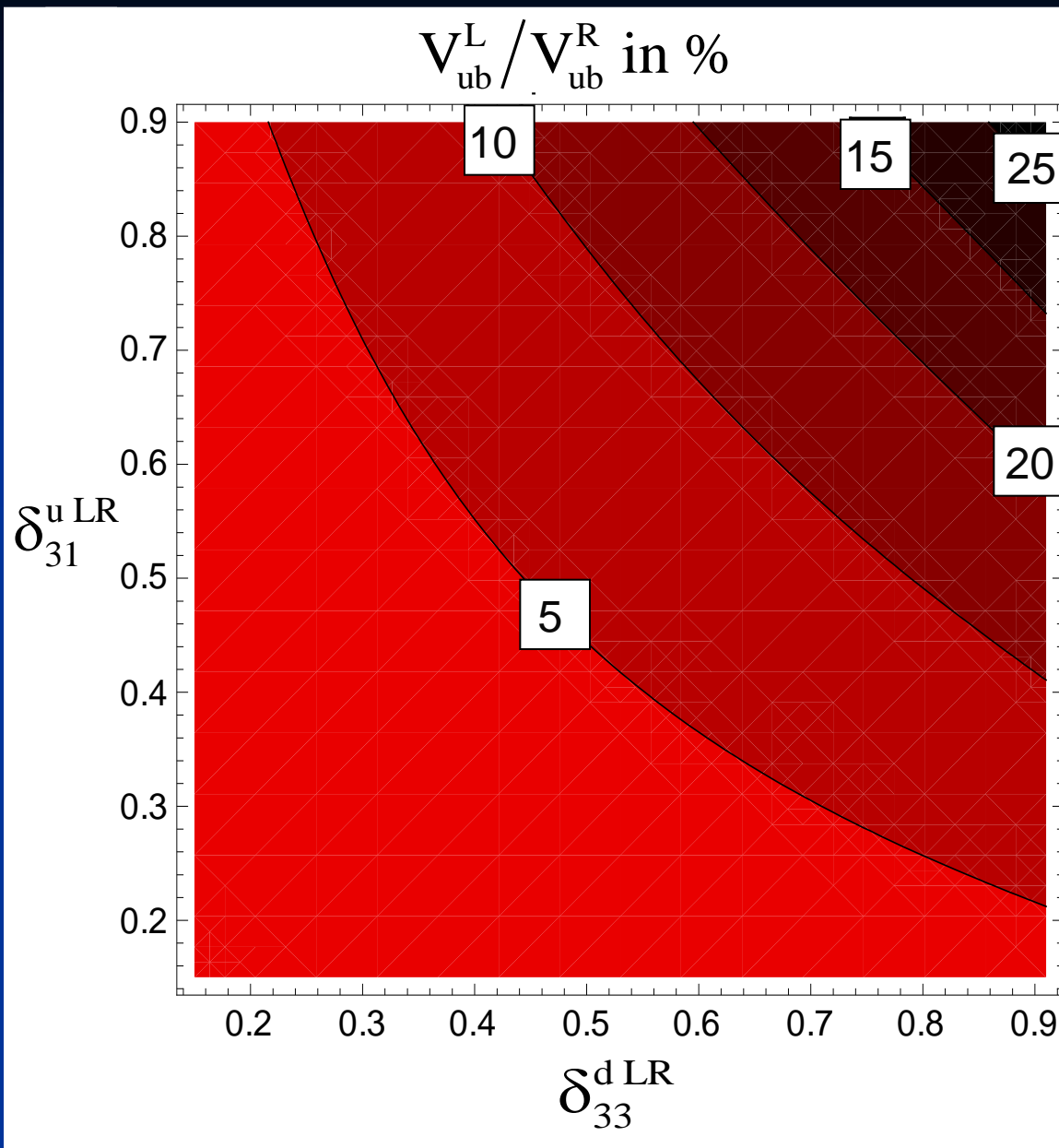


# Where are SUSY effects possible?

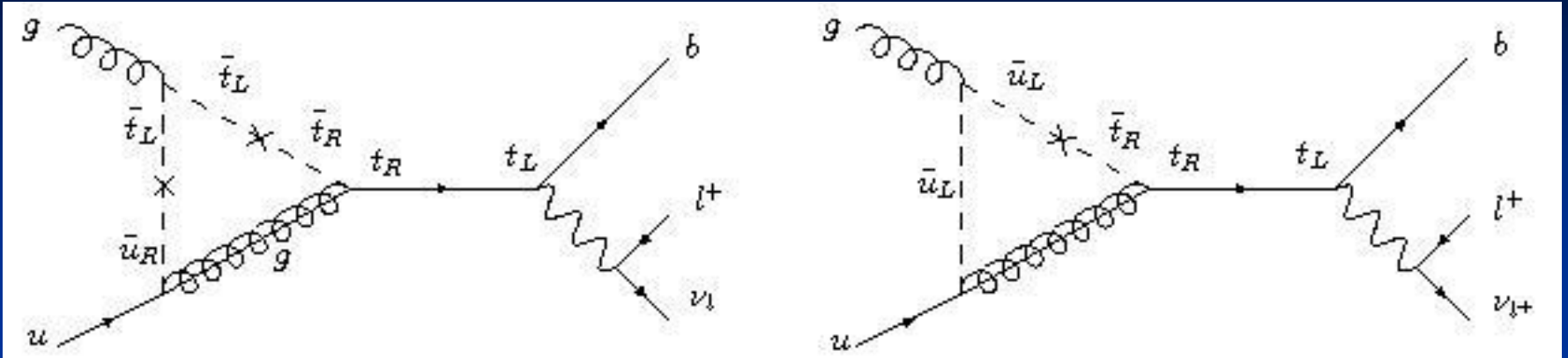
- $\delta_{fi}^{d LR/RL}$  strongly constrained from FCNC processes.
  - $\delta_{13,23}^{u LR}$  less constrained from FCNCs ( $B \rightarrow K^* l^+ l^-$ )
  - $\delta_{12,21}^{u LR,LL,RR}$  constrained from D mixing
  - $\delta_{13,23}^{u RL}$  unconstrained from FCNCs
  - Large  $\delta_{33}^{d LR}$  possible if  $A^b$  or  $\tan(\beta)$  is large.
  - $V_{ud}, V_{us}, V_{cd}, V_{cs}$  are too large for observable effects
- ➔ Only  $V_{ub}, V_{cb}$  can be affected by SUSY effects.

# Largest SUSY effect in $V_{ub}$ possible.

Effect in  
 $V_{cb} \approx 10\%$   
compared  
to  $V_{ub}$



# Enhancement of Single-Top Production

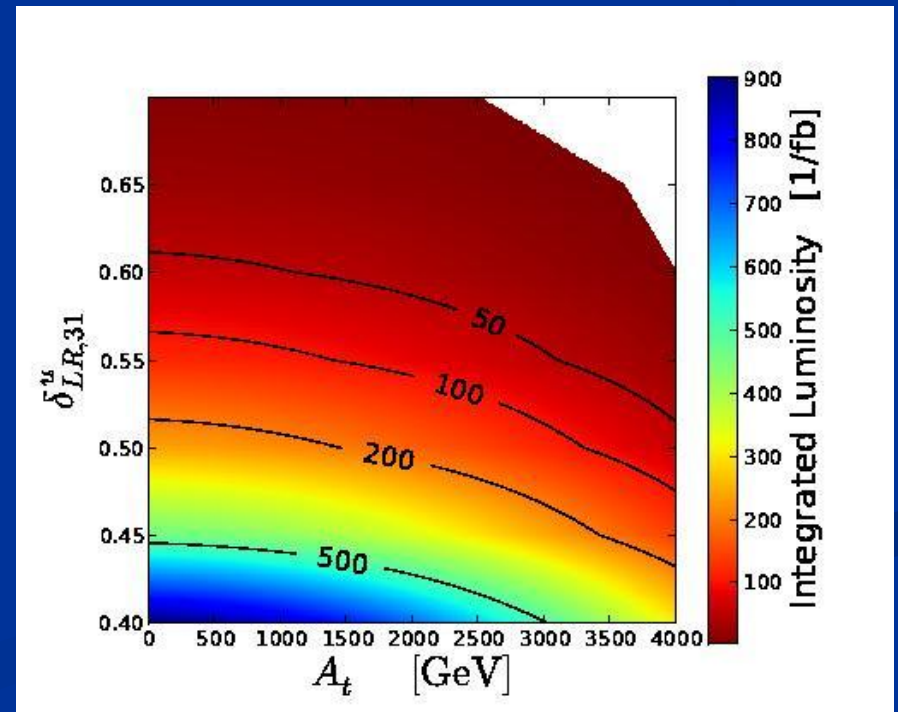


Feynman diagrams  
contributing to single-top  
production

Integrated luminosity  
necessary to discover  
single tops



Plehn, Rauch, Spannowski: 0906.1803



# Right-handed W-coupling and the determination of $V_{ub}$ and $V_{cb}$

# Motivation for a right-handed $W$ coupling

- 2.2  $\sigma$  discrepancy between the inclusive and exclusive determination of  $V_{cb}$
- 2.5 - 2.8  $\sigma$  deviation from the SM expectation in  $B \rightarrow \tau \nu$  *UTfit, CKMfitter*
- Tree-level processes. Commonly believed to be free of NP. (Charged Higgs contribution to  $B \rightarrow \tau \nu$  is destructive.)

➔ Notoriously difficult to explain the deviations from the SM

# Effective field theory

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \sum_i C_i Q_i^{(5)} + \frac{1}{\Lambda^2} \sum_i C_i Q_i^{(6)} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right)$$

Buchmüller, Wyler Nucl. Phys. B268 (1986)

- $O^{(5)}$  gives rise to neutrino masses
- Focus on the dimension 6 operator

$$Q_{\text{RR}} = \bar{u}_f \gamma^\mu P_R d_i \left( \tilde{\phi}^\dagger i D_\mu \phi \right)$$

which generates the anomalous W couplings

$$-i \frac{g_W}{\sqrt{2}} \gamma^\mu \left( P_L V_{fi}^L + P_R V_{fi}^R \right)$$

# Possible size of $V^R$

- $V_{tb}^R$  strongly constrained from  $b \rightarrow s\gamma$   
Misiak et. al. 0802.1413
- $V_{ts}^R$  ( $V_{td}^R$ ) also constrained from  $b \rightarrow s\gamma$  ( $b \rightarrow d\gamma$ )  
A.C. Lorenzo Mercolli arXiv:1106.5499
- No large effect for the first two generations possible because the CKM elements are big and the chirality violation is small.
- Sizable effects possible in  $V_{ub}^R$  and  $V_{cb}^R$  possible

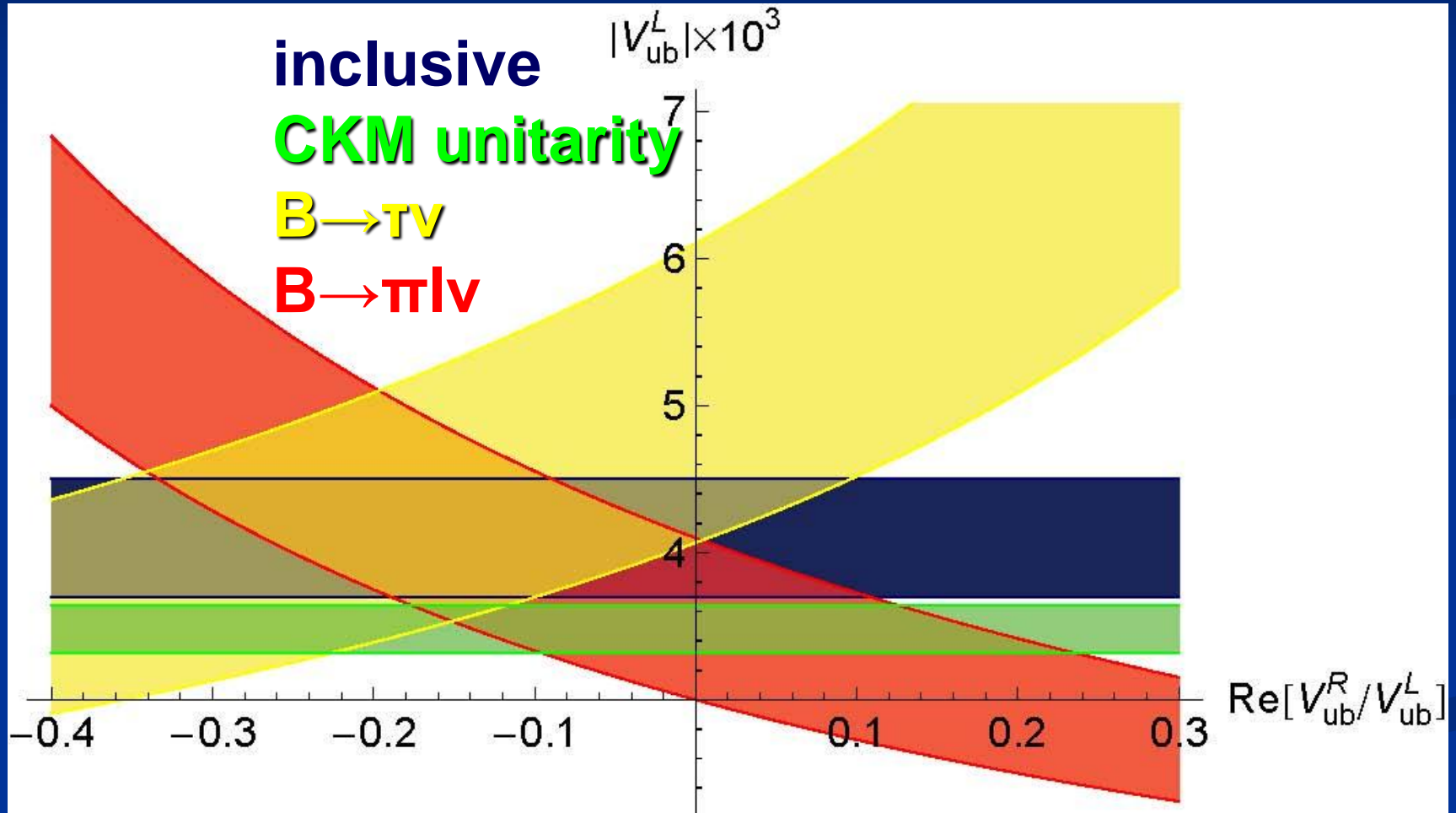
# Right-handed W coupling in exclusive and inclusive B decays

**V = measured CKM element**

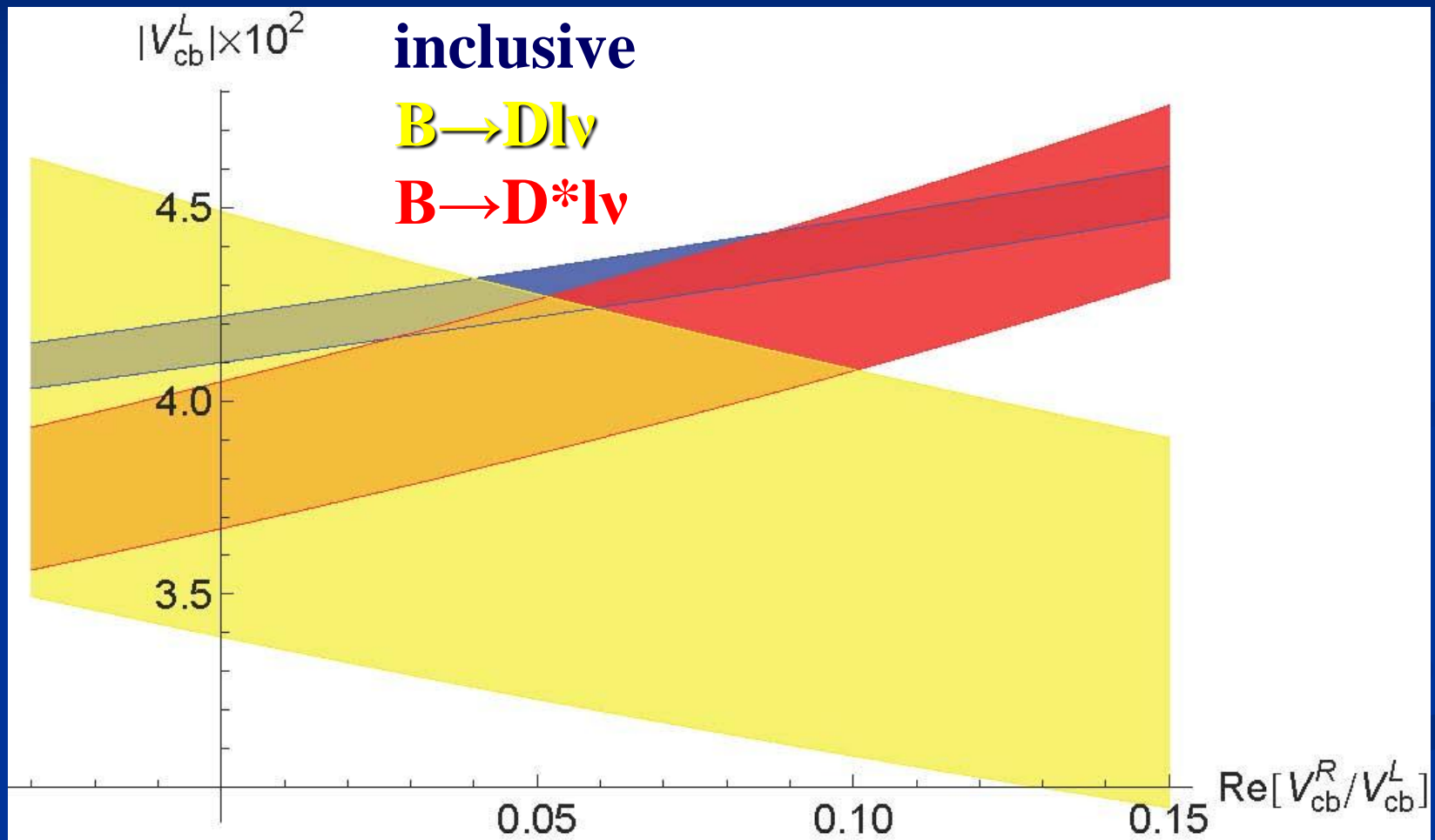
- Exclusive leptonic B decays:  $\sim |\gamma^\mu \gamma^5|^2$   
➔  $V^L = V + V^R$
- Exclusive semi-leptonic B decays to pseudo-scalar mesons  $\sim |\gamma^\mu|^2$   
➔  $V^L = V - V^R$
- Exclusive semi-leptonic B decays to vector mesons  $\sim |\gamma^\mu \gamma^5|^2$  **at  $\omega=1$**   
➔  $V^L = V + V^R$
- Inclusive  $B \rightarrow u$  decay  $\sim |1 + \gamma^\mu \gamma^5|^2 + |1 - \gamma^\mu \gamma^5|^2$   
➔  $V^L \approx V$
- Inclusive  $B \rightarrow c$  decay receive correction proportional to  $m_c/m_b$   
Dassinger, Feger, Mannel: Complete Michel Parameter Analysis of inclusive semileptonic  $b \rightarrow c$  transition  
➔  $V^L = V + 0.56 V^R$



# Effects of a right-handed W-coupling on $V_{ub}$



# Effects of a right-handed W-coupling on $V_{cb}$



# Conclusions

- The MSSM can generate such a sizeable right-handed  $W$ -coupling
- A right-handed  $W$ -coupling changes the determination of the CKM elements.
- A right-handed  $W$ -coupling can enhance  $B \rightarrow \tau \nu$  and solve the  $V_{ub}$  problem