

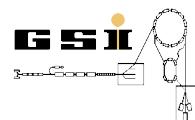


# A new approach to detect hypernuclei and isotopes in the QMD phase space distribution at relativistic energies

A. Le Fèvre<sup>1</sup>, J. Aichelin<sup>2</sup>, Ch. Hartnack<sup>2</sup> and Y. Leifels<sup>1</sup>

<sup>1</sup> *GSI Darmstadt, Germany*

<sup>2</sup> *Subatech Nantes, France*



Arnaud Le Fèvre (GSI Helmholtzzentrum für Schwerionenforschung - Darmstadt) - AsyEOS 2012 - Syracuse (Sicily)



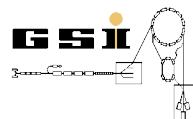
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## Motivations



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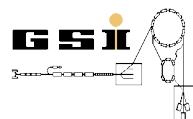
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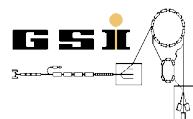
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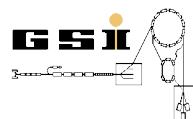
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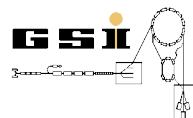
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- ❖ Having the clusters correctly formed is as important as the transport and creation of their constituents in the curse of the collisions.
- Because, apart from emitted elementary particles, they carry the only information that the experimental instruments can measure.
- ❖ Making clusters is not an easy task, because it involves, in a complex environment:
  - ▶ the fundamental nuclear properties,
  - ▶ quantum effects,
  - ▶ and variable timescales.

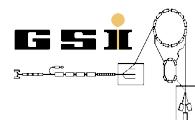


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# Simulated Annealing Clusterization Algorithm (SACA): The principles



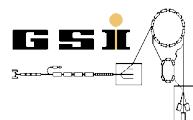
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If we want to identify fragments early, one has to use momentum space info as well as coordinate space info.



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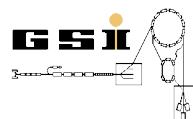
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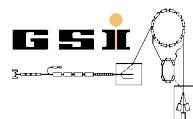


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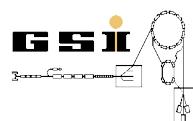
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Simulations show: Clusters chosen that way at early times are the pre-fragments of the final state clusters, because fragments are not a random collection of nucleons at the end but initial-final state correlations.



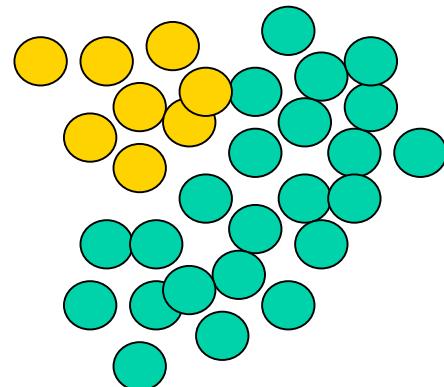


# SACA: How does this work?

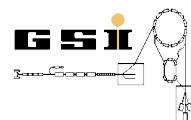
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2 steps:

- 1) Pre-select good «candidates» for fragments according to proximity criteria: real space coalescence = Minimum Spanning Tree (MST) procedure.



$$E = E_{\text{kin}}^1 + E_{\text{kin}}^2 + V^1 + V^2$$



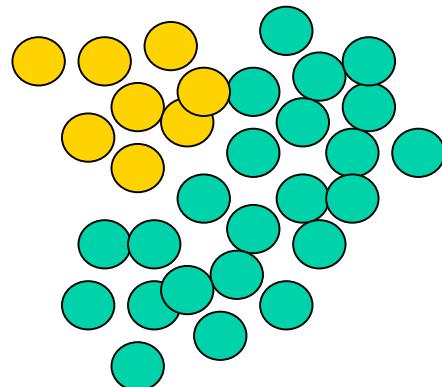


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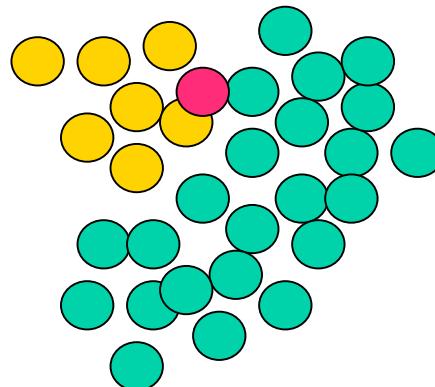
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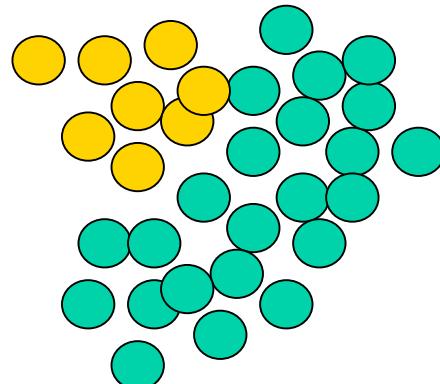


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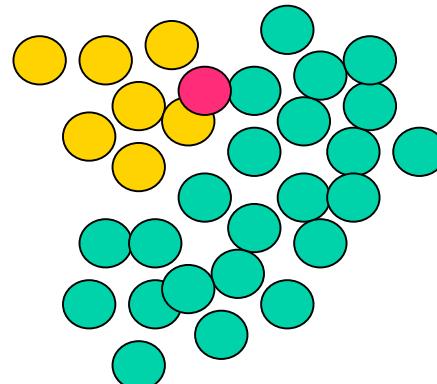
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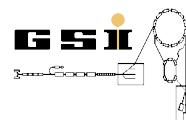
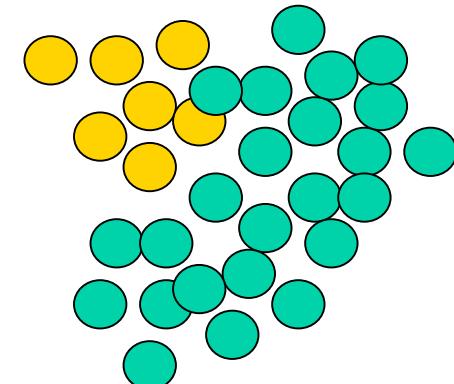
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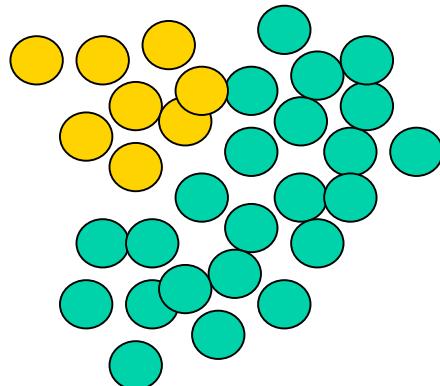


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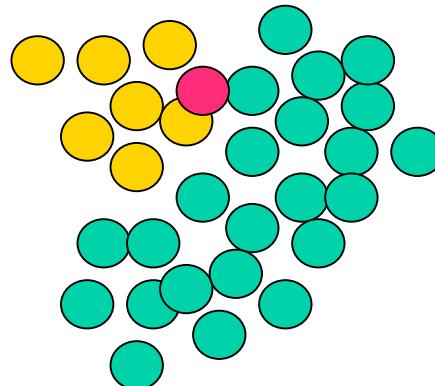
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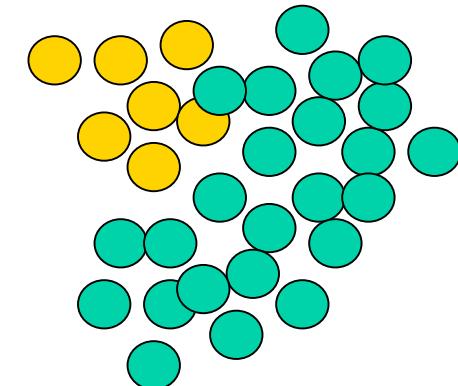


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If  $E' < E$  take the new configuration



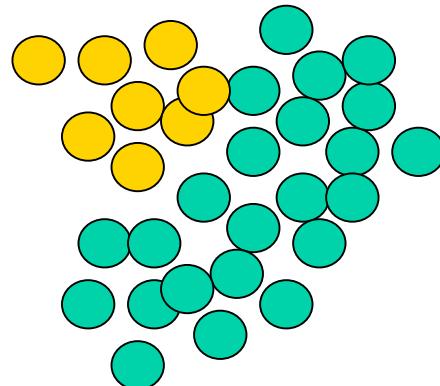


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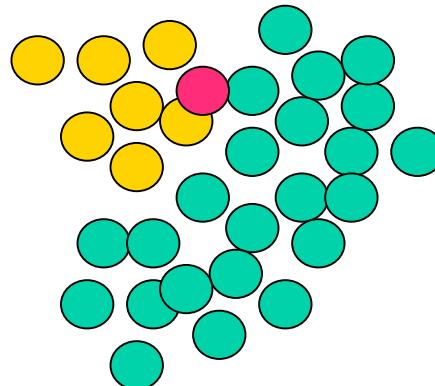
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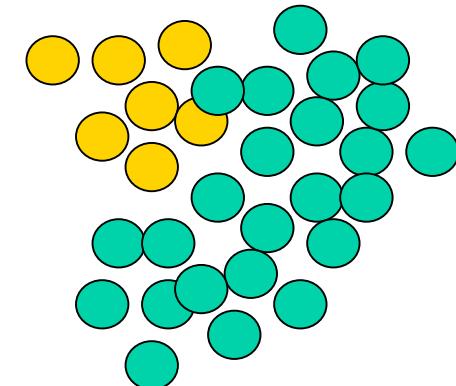
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If  $E' < E$  take the new configuration

If  $E' > E$  take the old with a probability depending on  $E' - E$

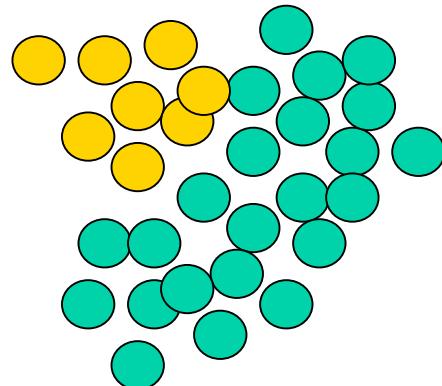


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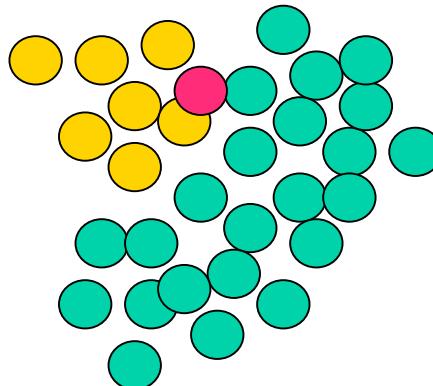
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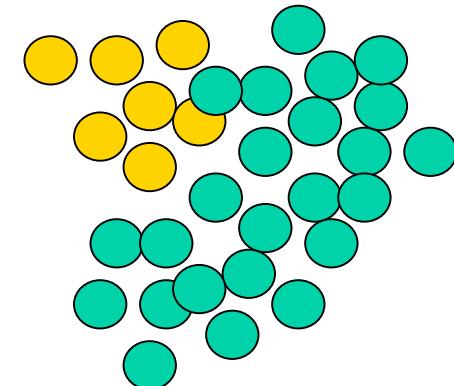
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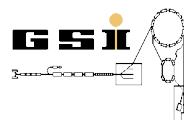
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Repeat this procedure very many times...



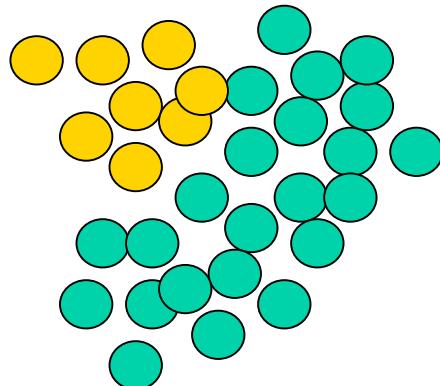


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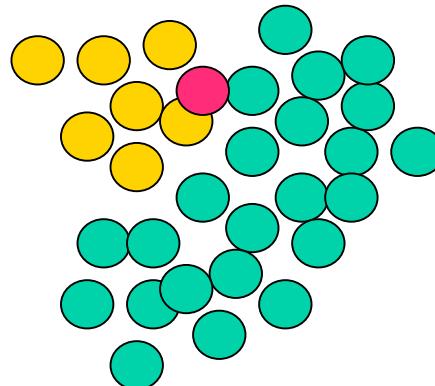
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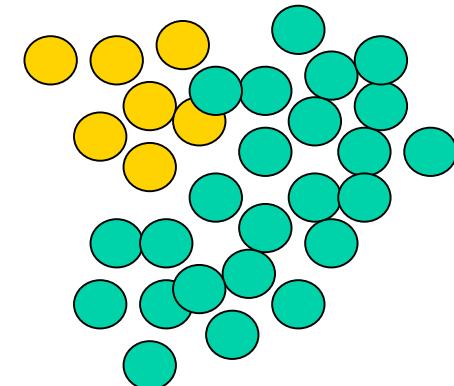
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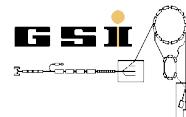
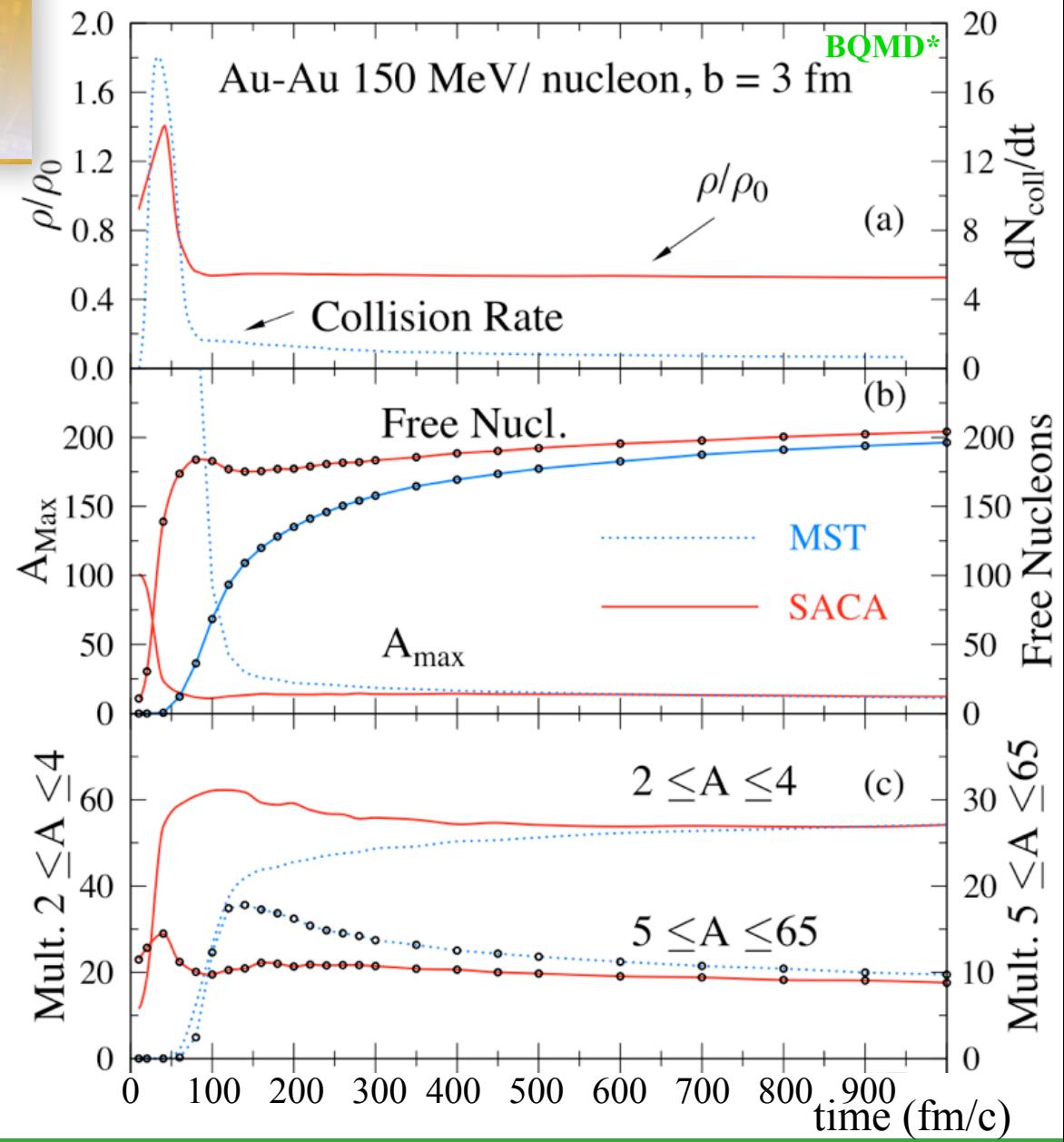
Repeat this procedure very many times...

It leads automatically to the most bound configuration.



## SACA versus coalescence (Minimum Spanning Tree)

\* P.B. Gossiaux, R. Puri, Ch. Hartnack, J. Aichelin,  
Nuclear Physics A 619 (1997) 379-390



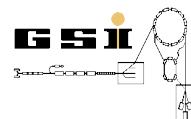
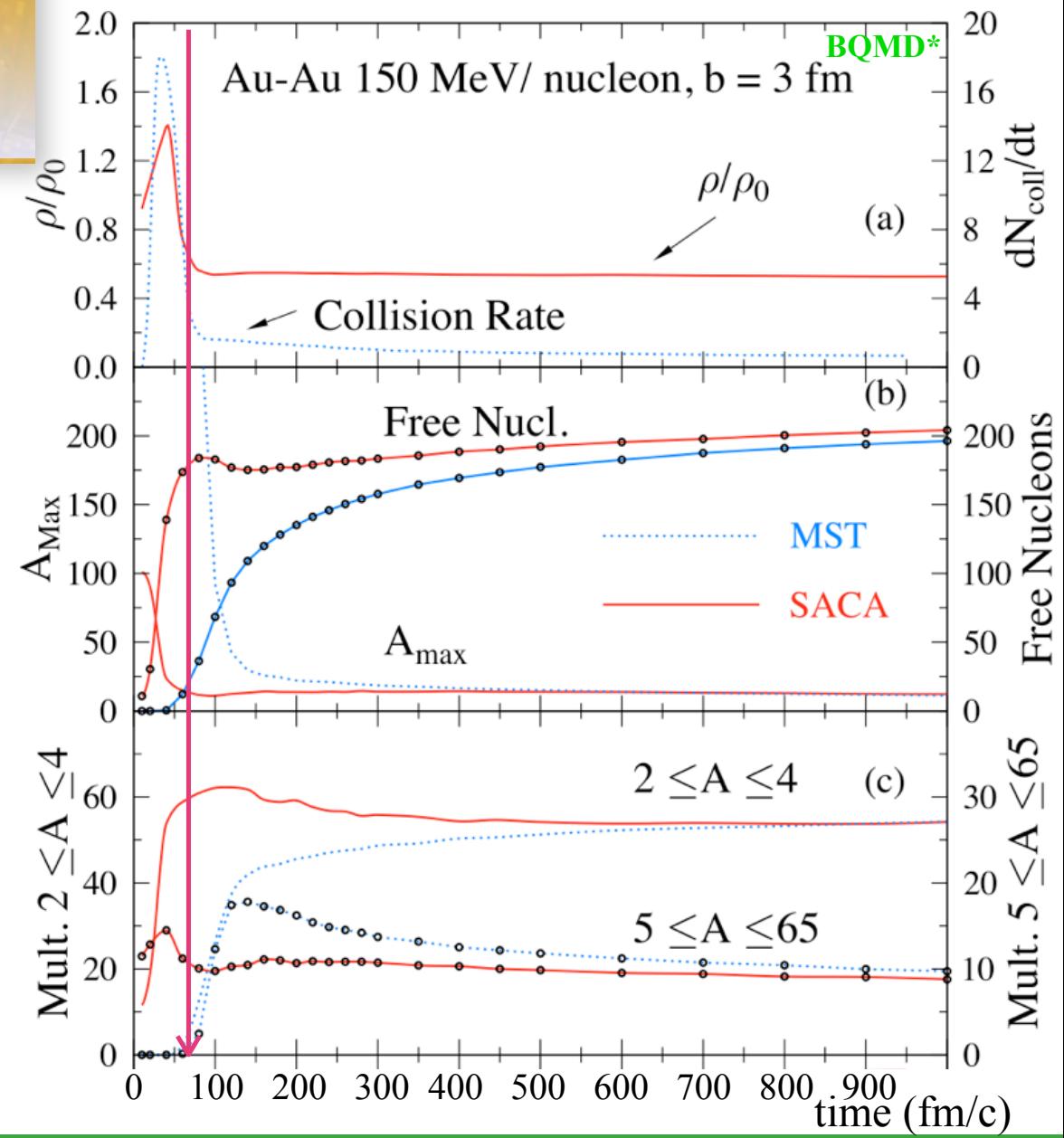
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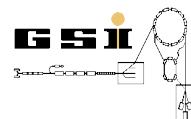
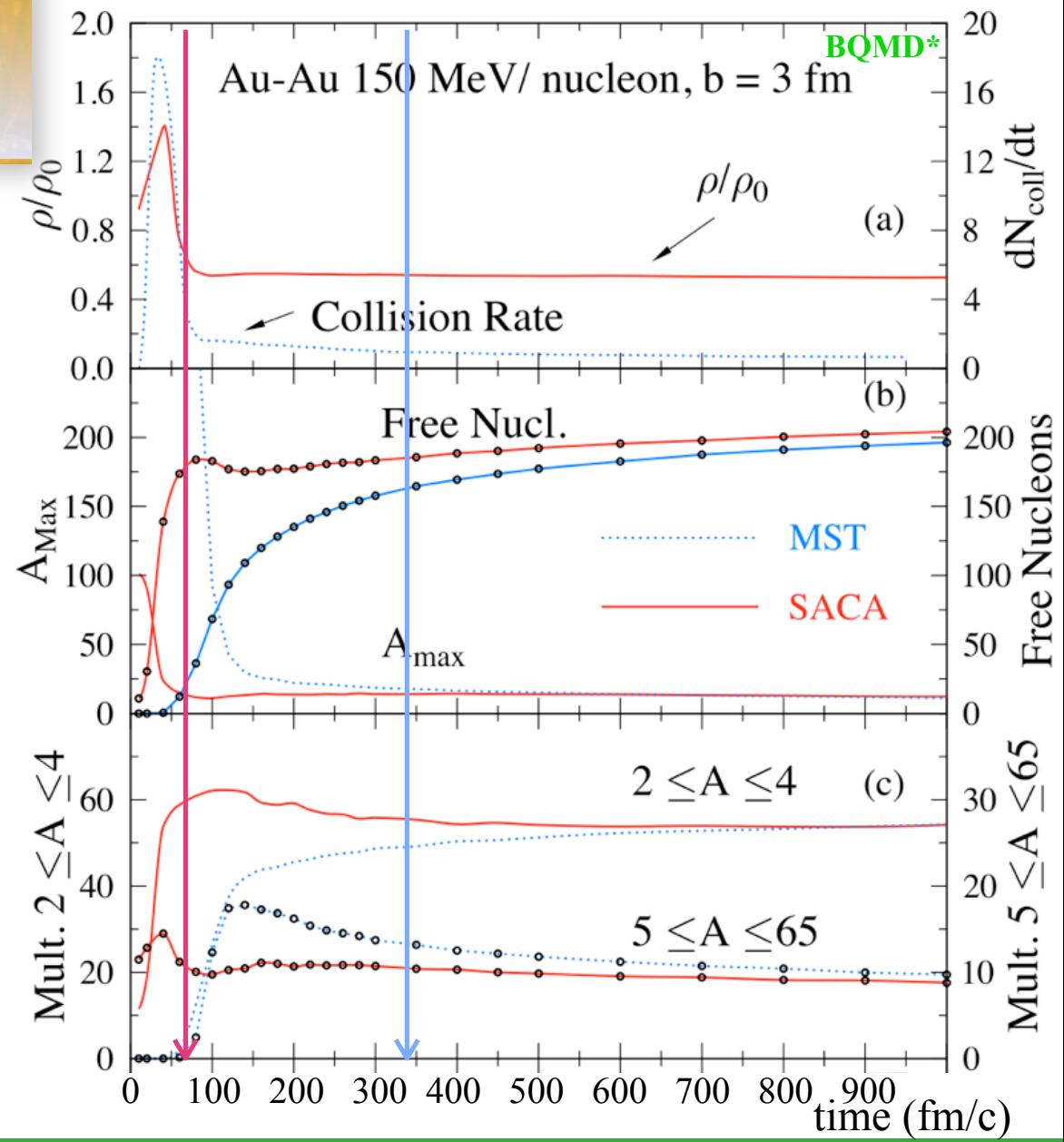
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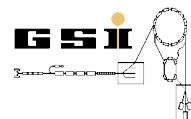
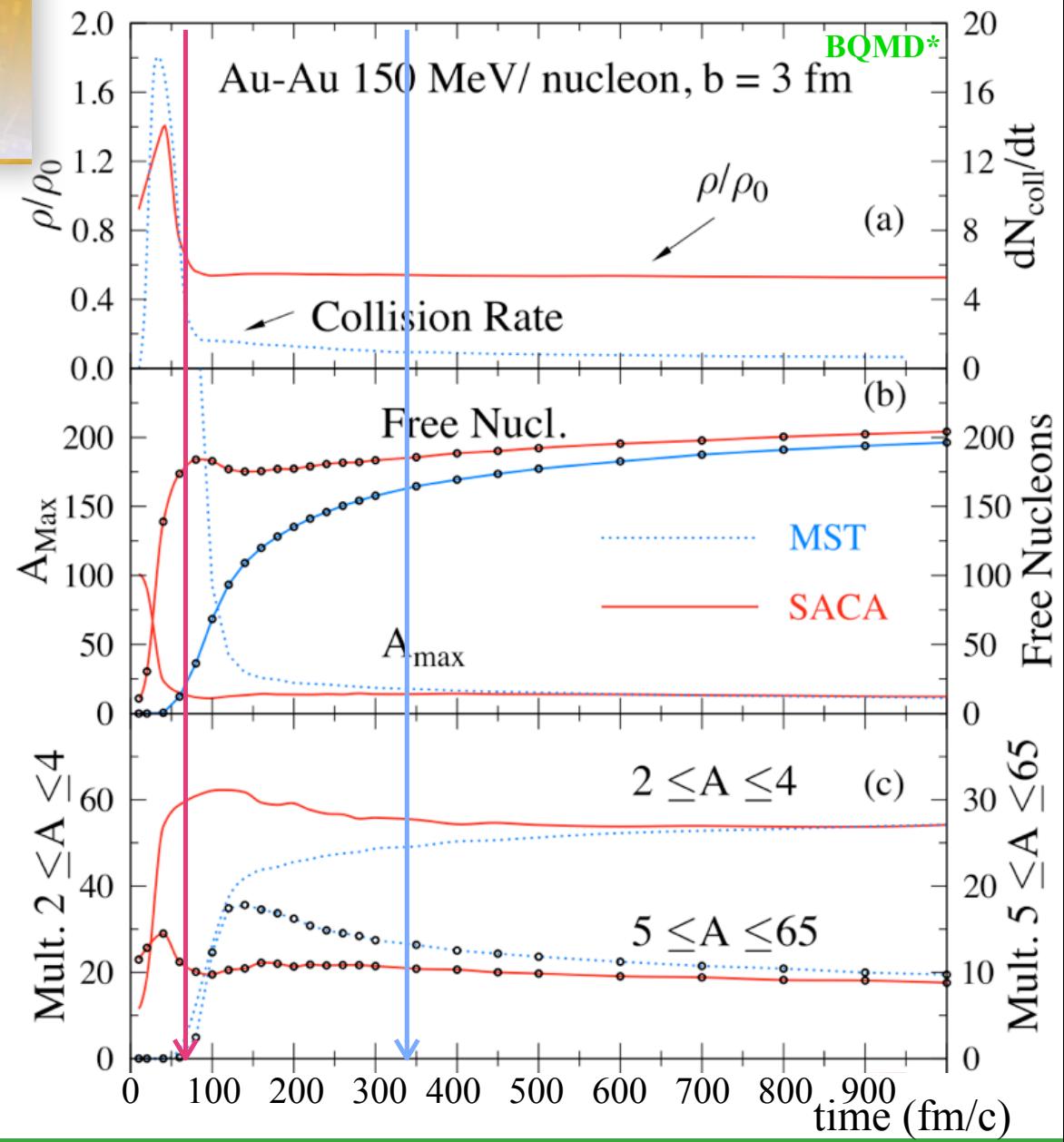
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Unlike SACA, MST is not able to describe the early formation of fragments.

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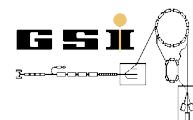
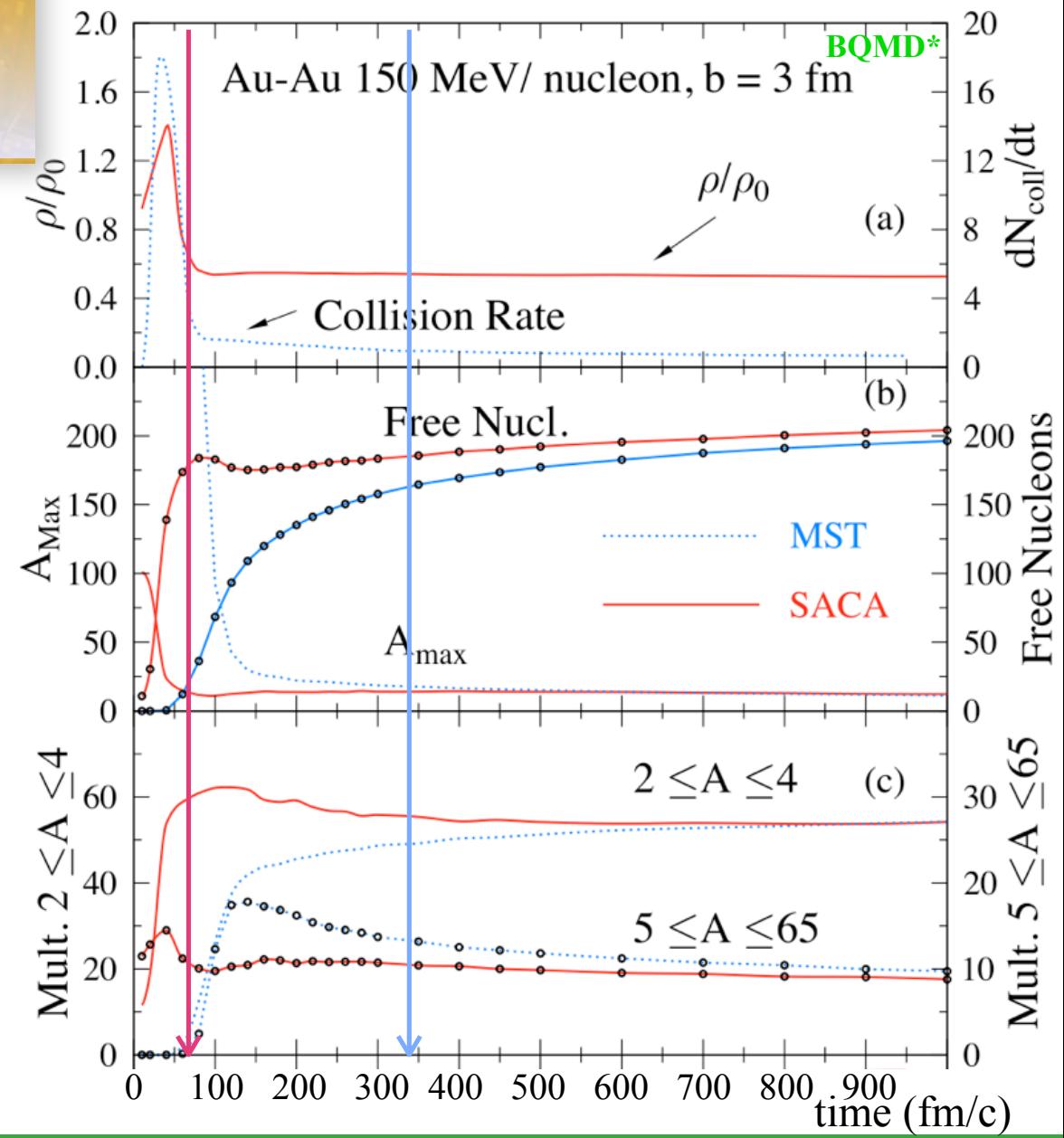


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→ With MST, one has to consider necessarily later times (typically 200-400 fm/c), where the dynamical conditions are no longer the same.

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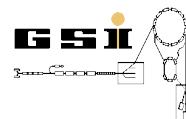
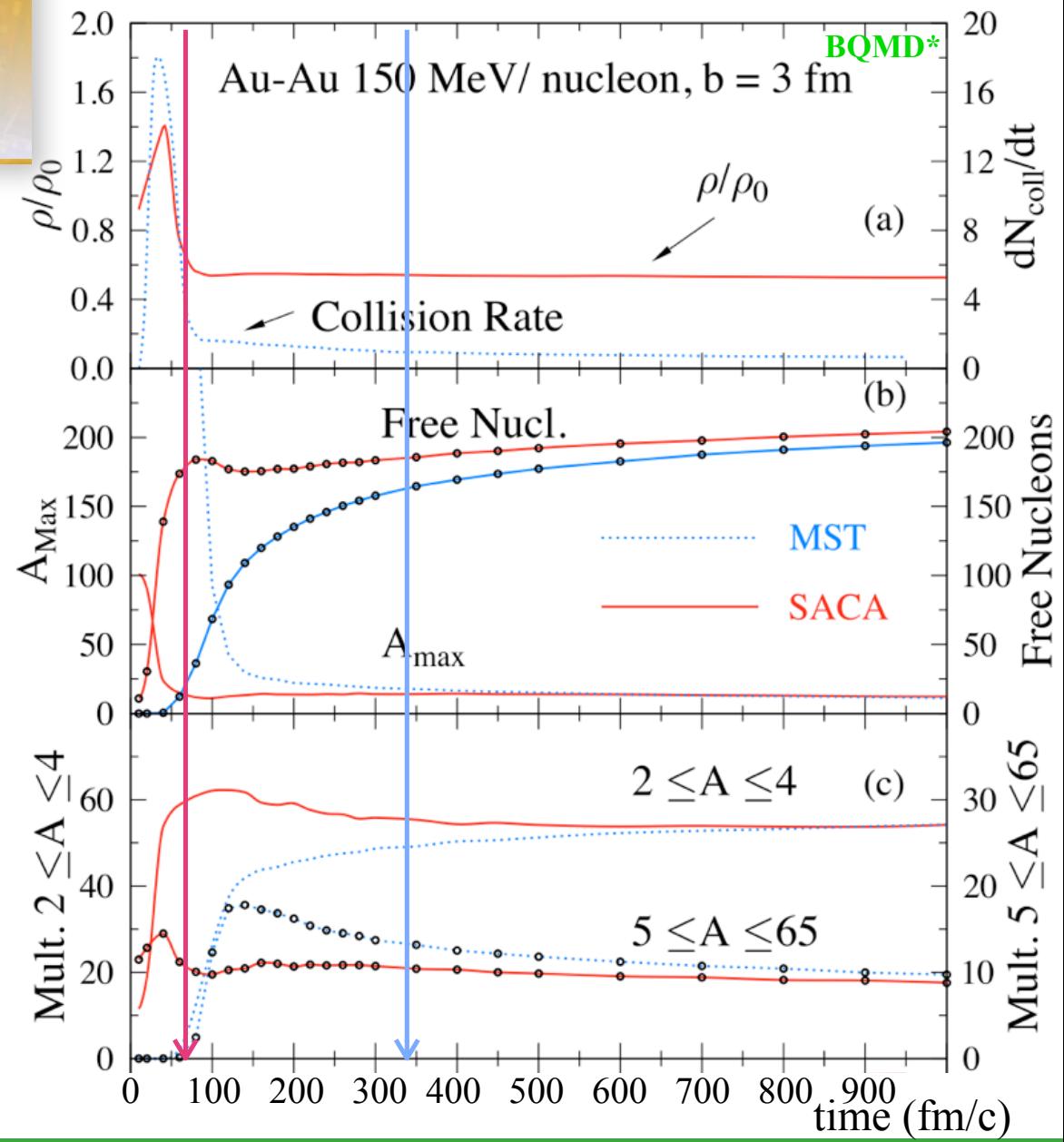


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- With MST, one has to consider necessarily later times (typically 200-400 fm/c), where the dynamical conditions are no longer the same.
- Advantage of SACA : the fragment partitions can reflect the early dynamical conditions (Coulomb, density, flow details, strangeness...).

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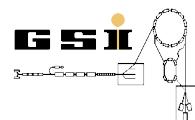




## Toward the isotope yields... IQMD + new SACA

SACA is applied here on the IQMD transport model\* calculations

\*C. Hartnack *et al.*, Eur. Phys. J. A1, 151(1998).



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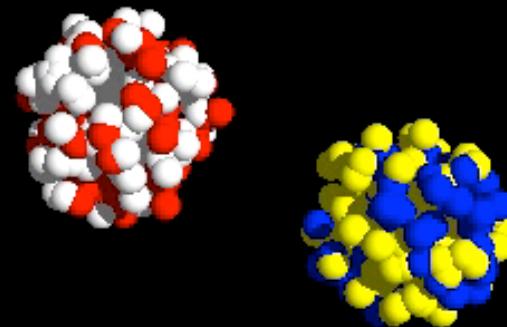


## Toward the isotope yields... IQMD + new SACA

SACA is applied here on the IQMD transport model\* calculations

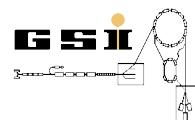
\*C. Hartnack *et al.*, Eur. Phys. J. A1, 151(1998).

Au+Au at 100 A.MeV - b=7 fm



## An example of complex system accurately measured

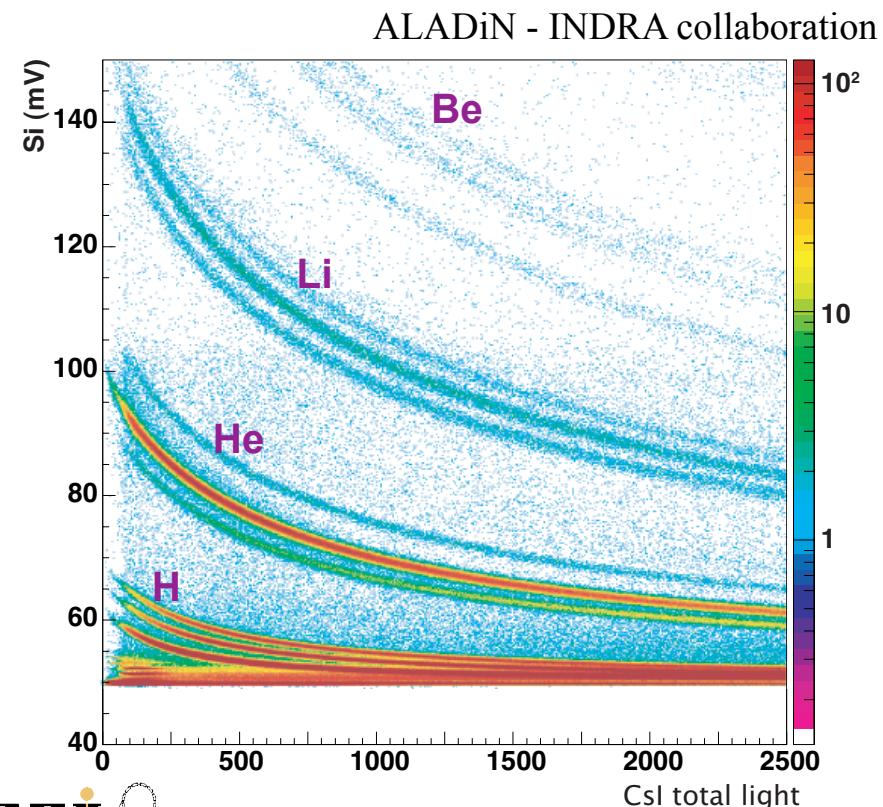
Large Z range of measured isotopes,  
large flow, high excitation energy.



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# An example of complex system accurately measured

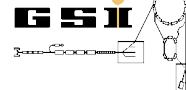
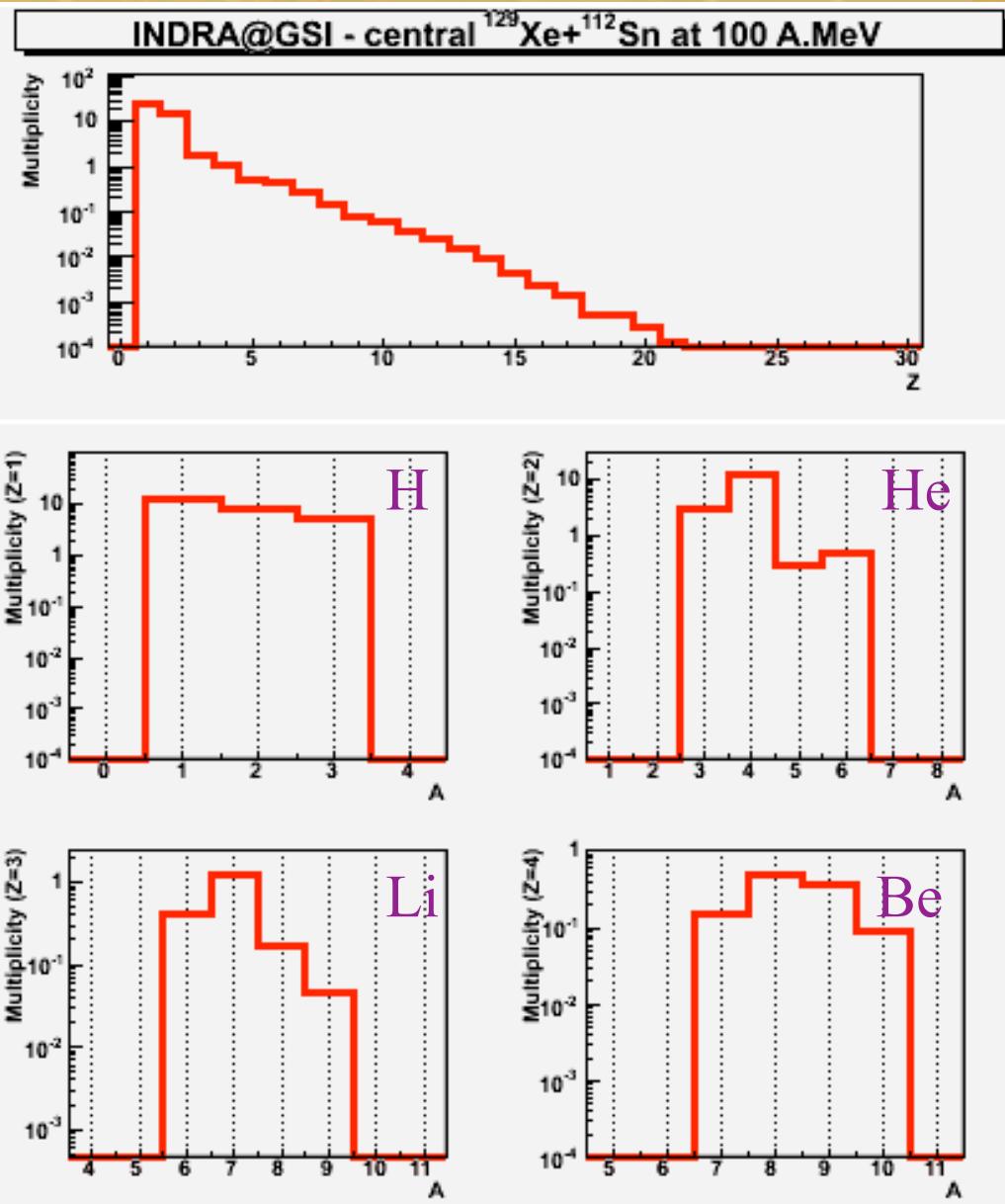
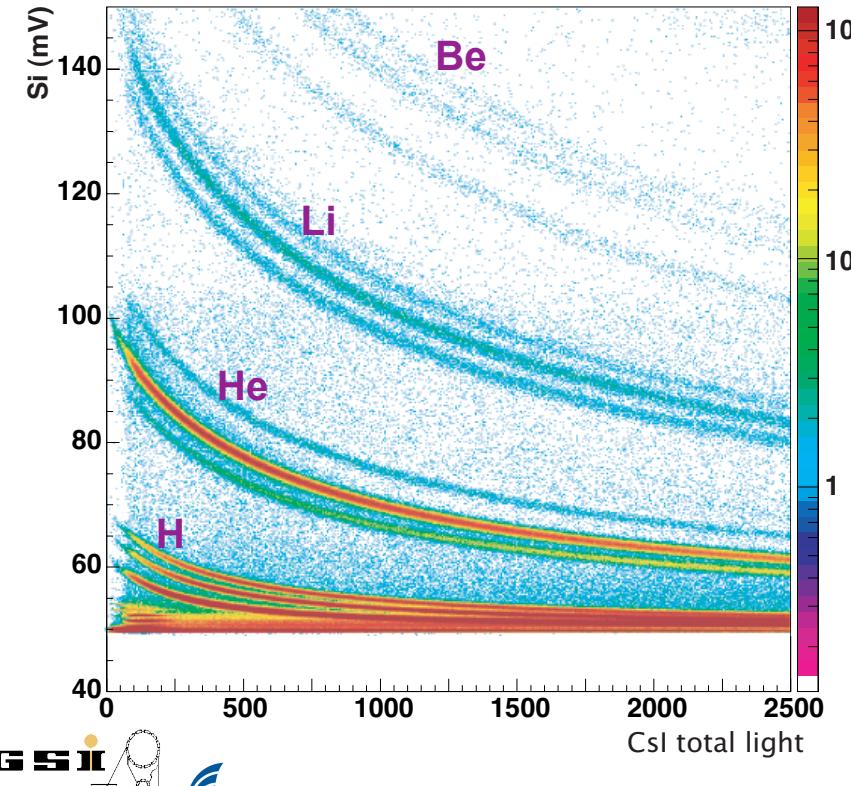
Large Z range of measured isotopes,  
large flow, high excitation energy.



# An example of complex system accurately measured

Large Z range of measured isotopes,  
large flow, high excitation energy.

ALADiN - INDRA collaboration

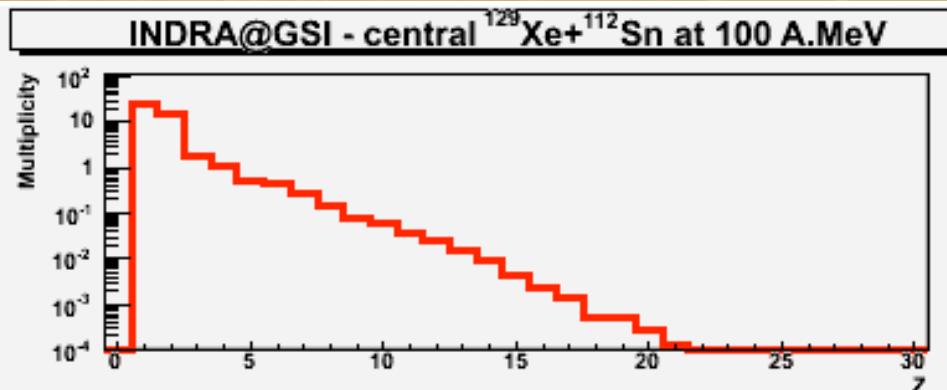


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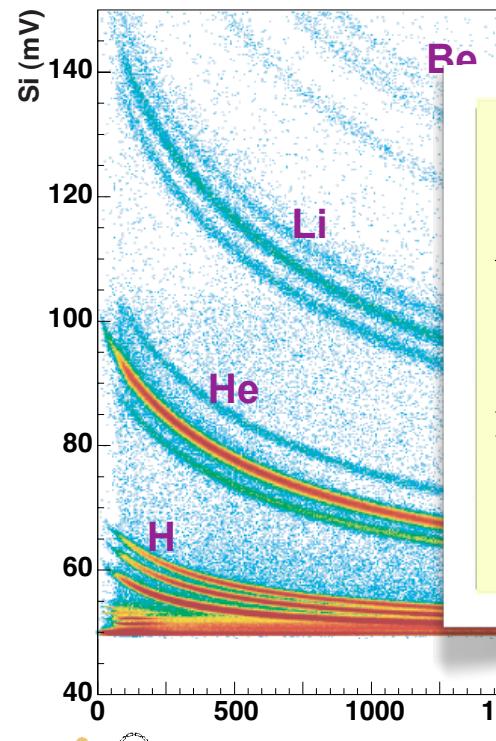
Arnaud Le Fèvre (GSI Helmholtzzentrum für Schwerionenforschung - Darmstadt) - AsyEOS 2012 - Syracuse (Sicily)

# An example of complex system accurately measured

Large Z range of measured isotopes,  
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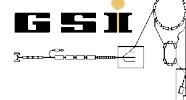
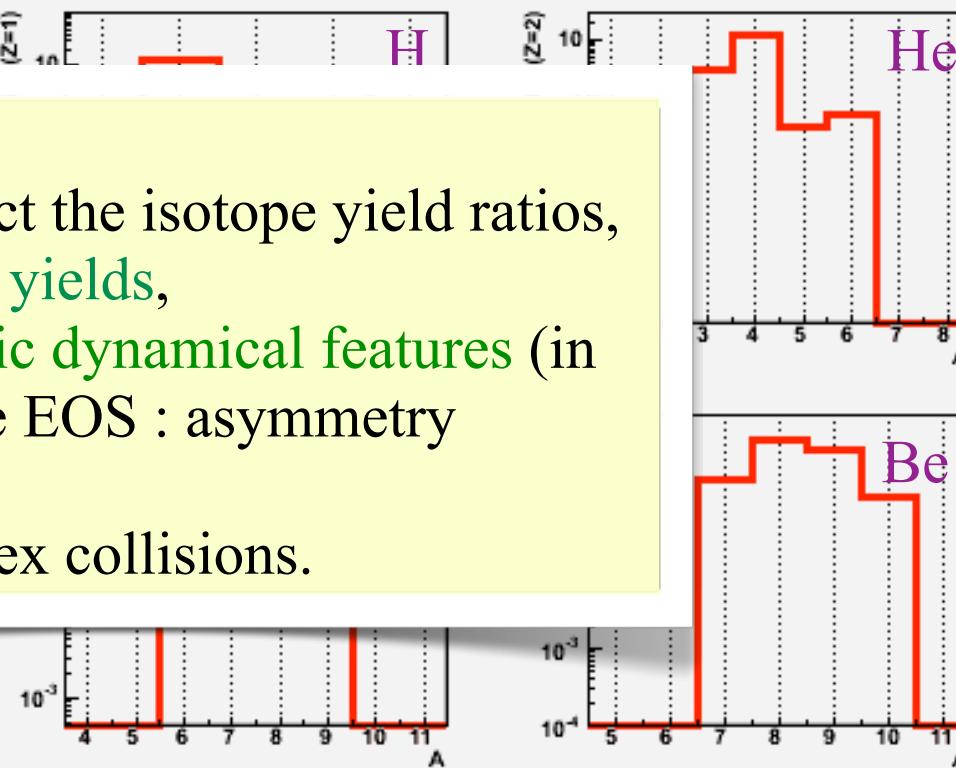


ALADiN - INDRA collaboration



## Our goals:

- not only predict the isotope yield ratios,  
but the **absolute yields**,
- and the **isotopic dynamical features** (in  
relation with the EOS : asymmetry  
energy, ...),
- in such complex collisions.



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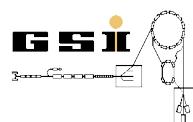
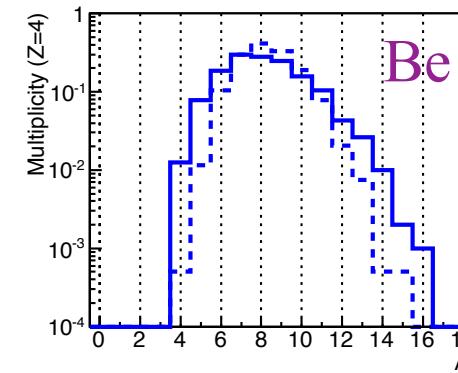
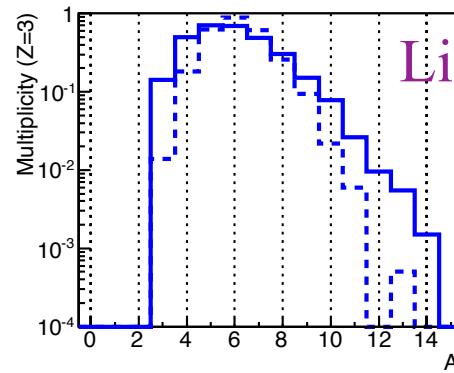
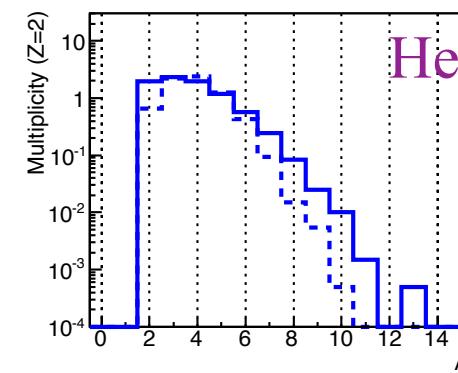
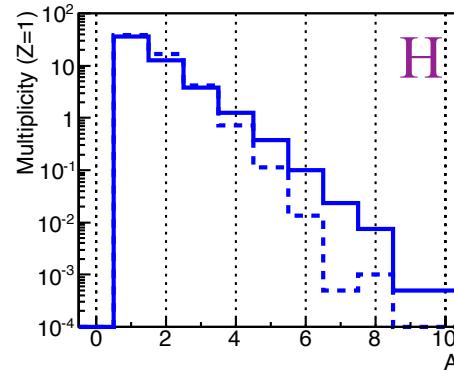
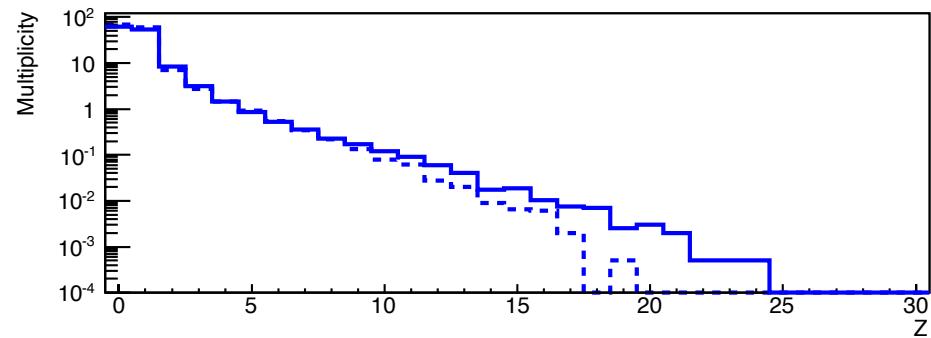
# SACA versus coalescence (Minimum Spanning Tree)

IQMD  $^{136}\text{Xe} + ^{112}\text{Sn}$  at 100 A.MeV,  $b=1$  fm,  $t_{\text{SACA}} = 60$  fm/c

SACA version:

----- MST only (200 fm/c)

—  $E_{\text{asy}}=0$ , no pairing



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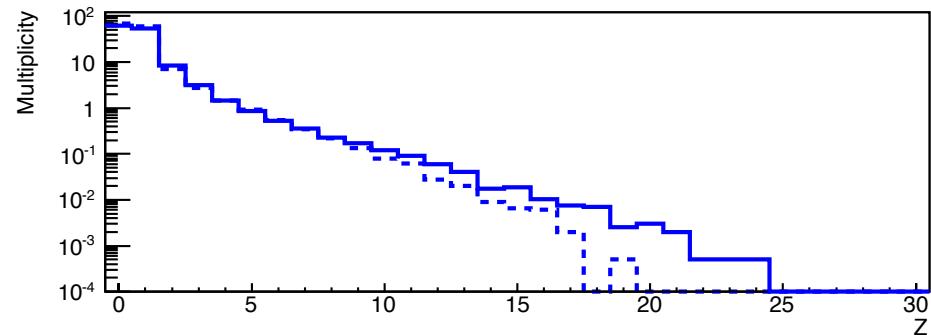
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IQMD  $^{136}\text{Xe} + ^{112}\text{Sn}$  at 100 A.MeV,  $b=1$  fm,  $t_{\text{SACA}} = 60$  fm/c

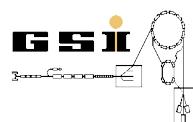
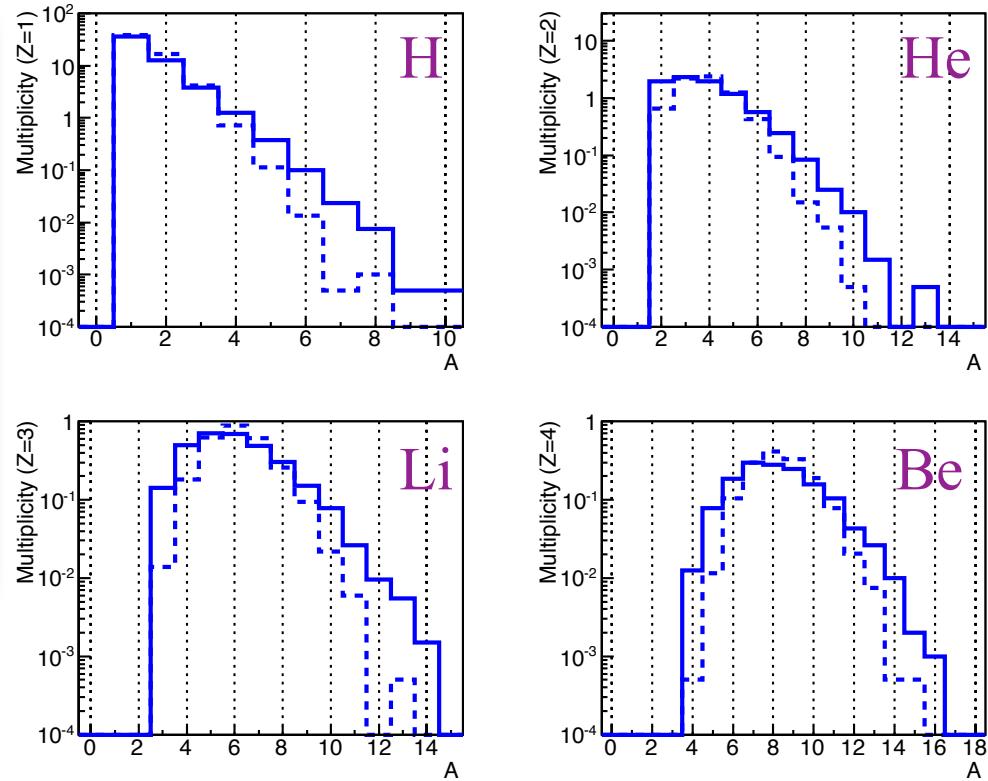
SACA version:

- MST only (200 fm/c)
- $E_{\text{asy}}=0$ , no pairing



At this stage, SACA contains as ingredients of the potential making the binding energy of the clusters :

- ① volume component:  
**mean field (Skyrme, dominant)**
- ② correction of surface effects:  
**Yukawa**



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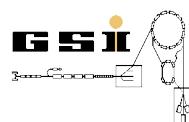
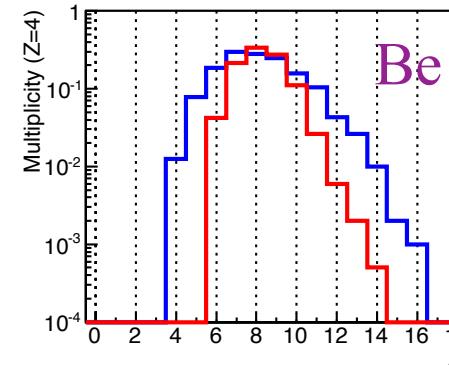
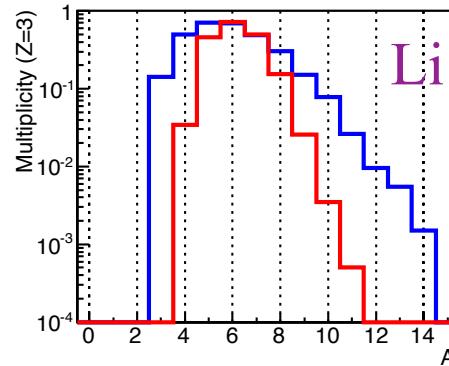
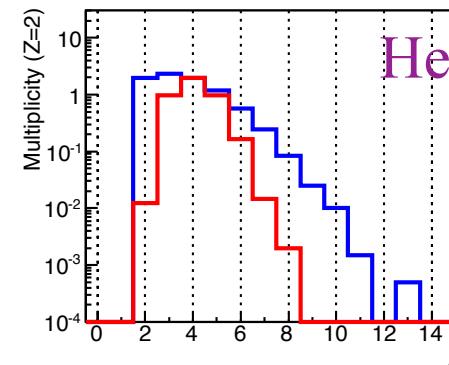
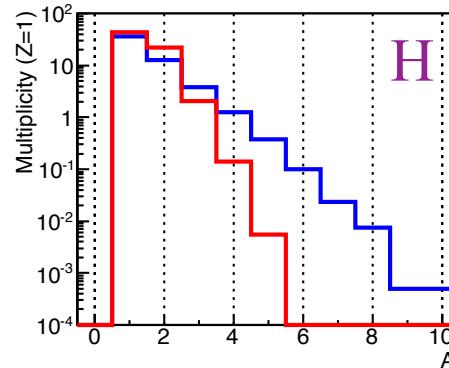
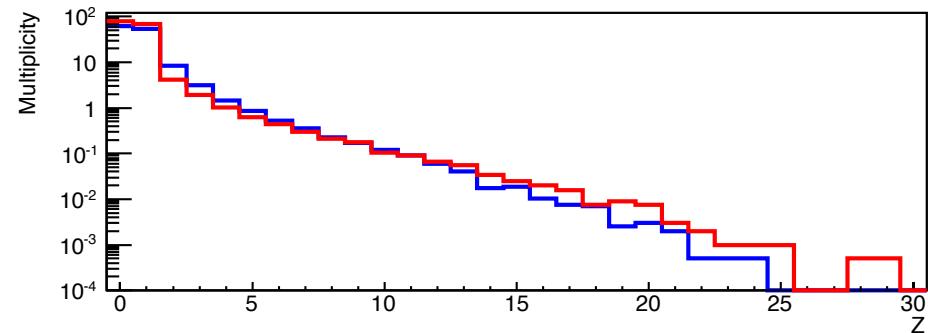
# SACA with asymmetry energy

IQMD  $^{136}\text{Xe} + ^{112}\text{Sn}$  at 100 A.MeV,  $b=1$  fm,  $t_{\text{SACA}} = 60$  fm/c

SACA version:

—  $E_{\text{asy}}=0$ , no pairing

—  $E_{\text{asy}}=32$  MeV ( $\gamma=1$ ), no pairing



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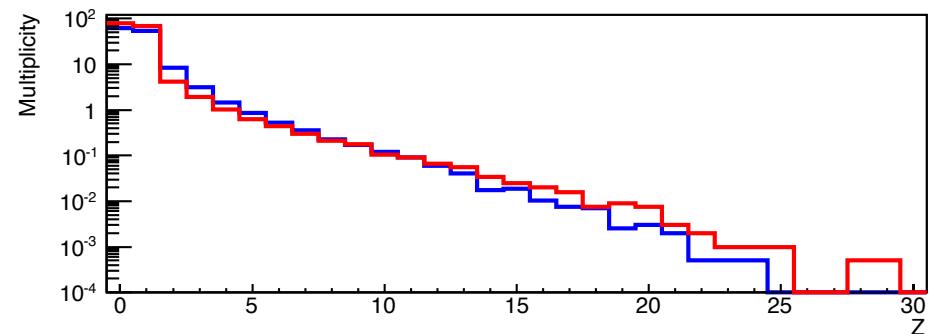
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# SACA with asymmetry energy

IQMD  $^{136}\text{Xe} + ^{112}\text{Sn}$  at 100 A.MeV,  $b=1$  fm,  $t_{\text{SACA}} = 60$  fm/c

SACA version:

- $E_{\text{asy}}=0$ , no pairing
- $E_{\text{asy}}=32$  MeV ( $\gamma=1$ ), no pairing

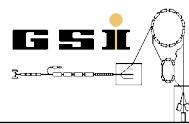
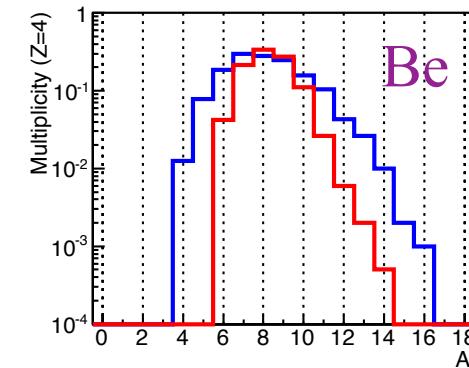
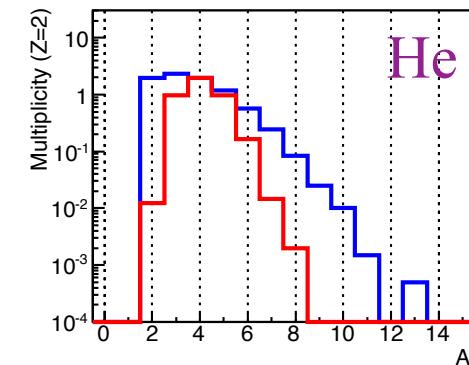
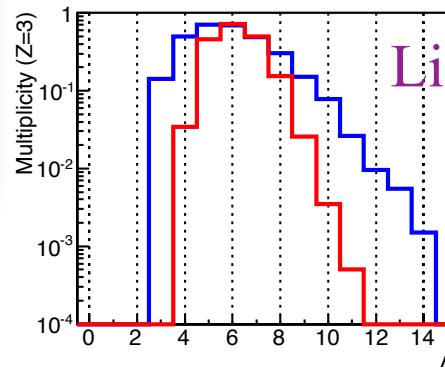
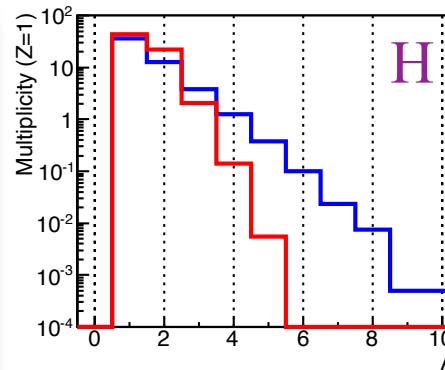


Here,  
in IQMD and SACA, we adopt the  
following asymmetry energy  
parametrisation:

$$E_{\text{asy}} = E_0 \cdot (\langle \rho_B \rangle / \rho_0)^{(\gamma-1)} \cdot (\langle \rho_n \rangle - \langle \rho_p \rangle) / \langle \rho_B \rangle$$

with  $E_0 = 32$  MeV,  $\gamma = 1$  («stiff»)

- Z and A yields not strongly modified
- Isotope yields shrink onto the N=Z line
- Still not fully realistic: shell, odd-even effects (pairing) still absent.



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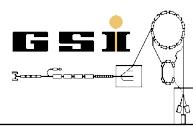
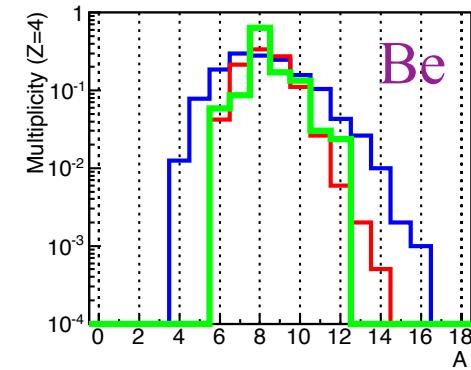
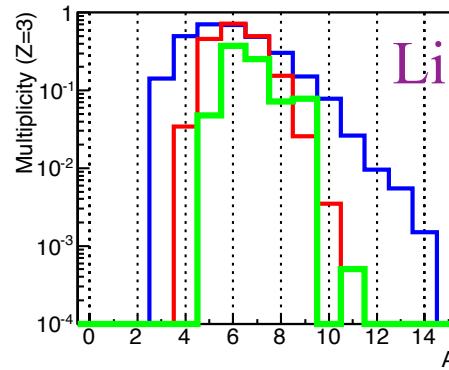
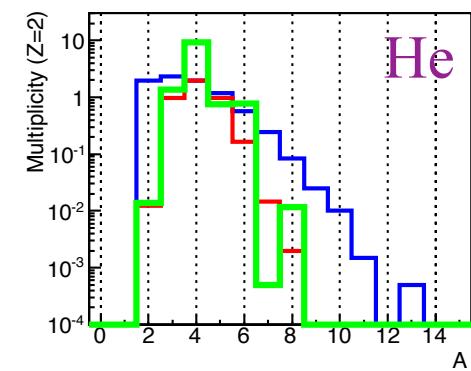
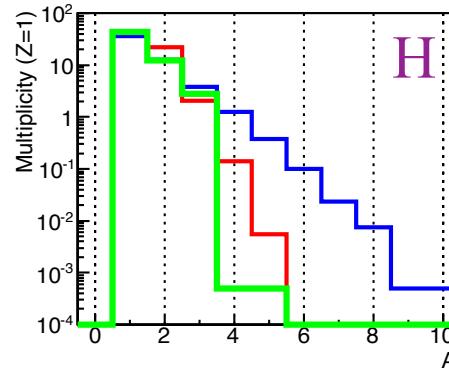
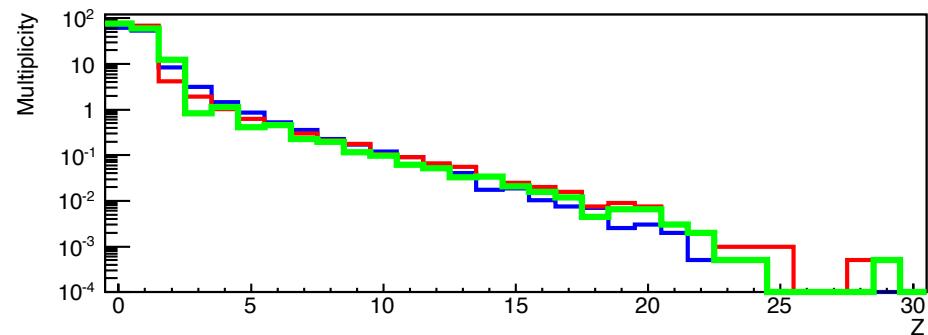
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# SACA with asymmetry energy and pairing

INDRA@GSI - central  $^{129}\text{Xe} + ^{112}\text{Sn}$  at 100 A.MeV

SACA version:

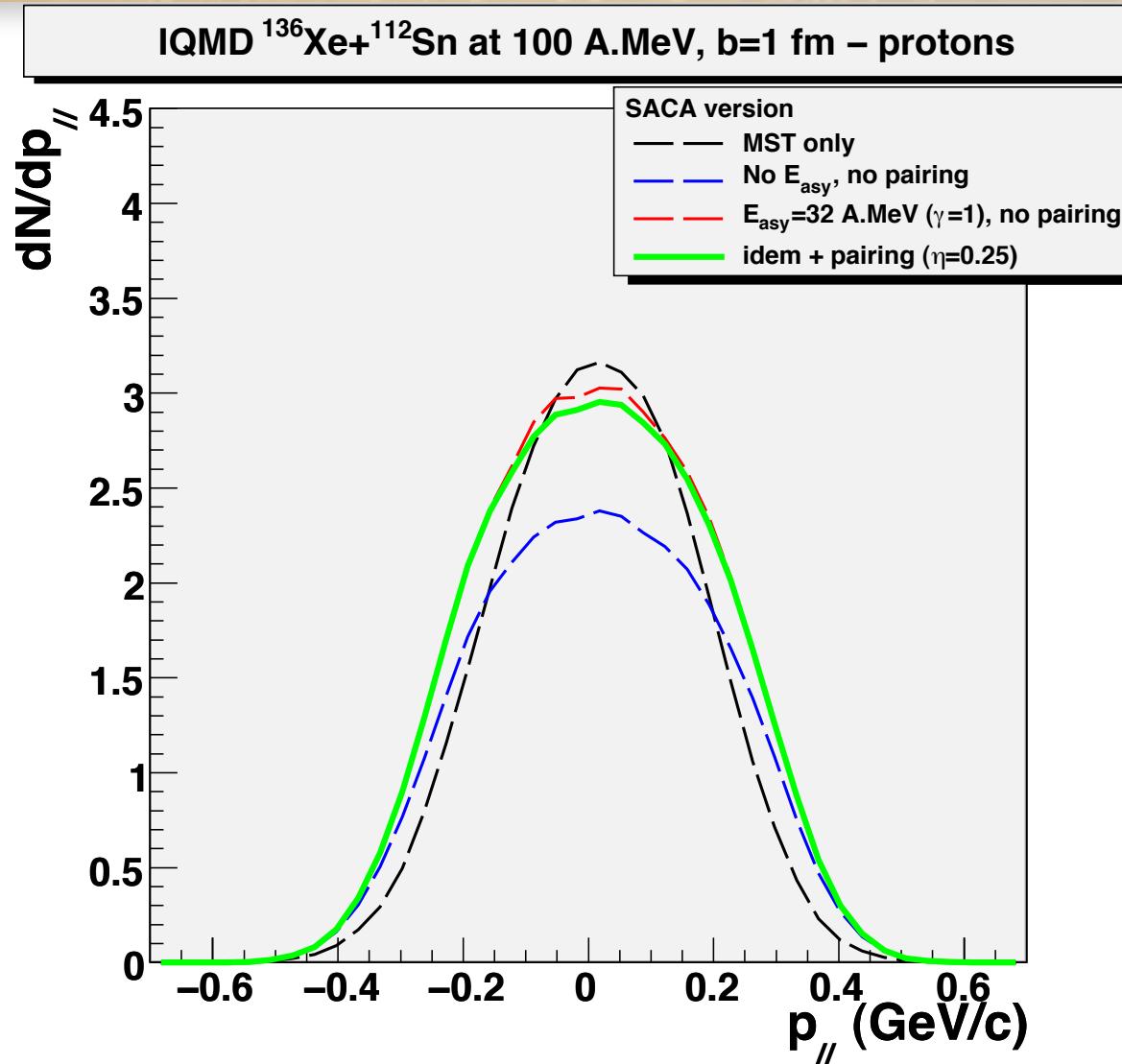
- E<sub>asy</sub>=0, no pairing
- E<sub>asy</sub>=32 MeV ( $\gamma=1$ ), no pairing
- E<sub>asy</sub>=32 MeV ( $\gamma=1$ ) +  $\eta_{\text{pairing}} = 0.25$



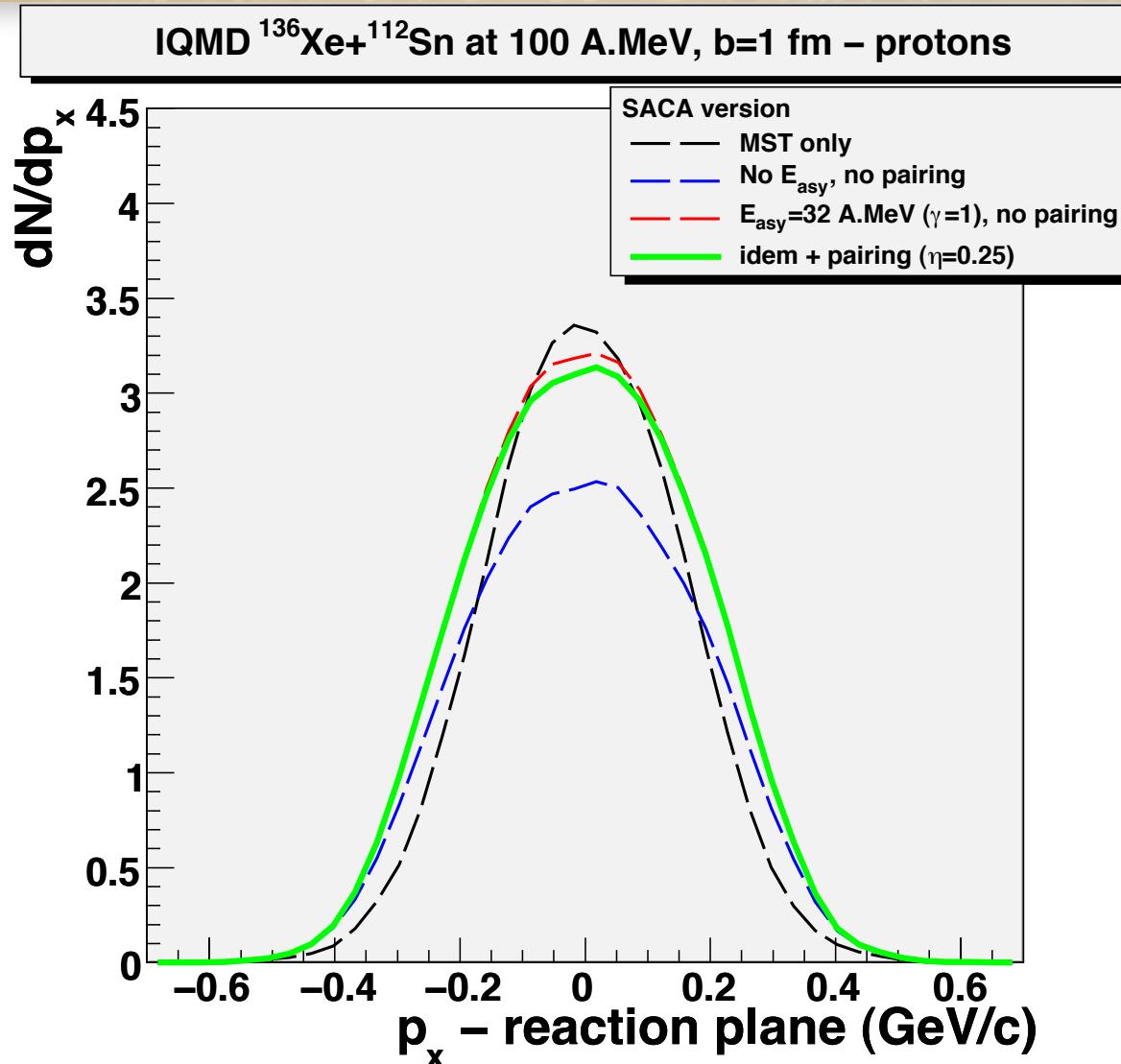
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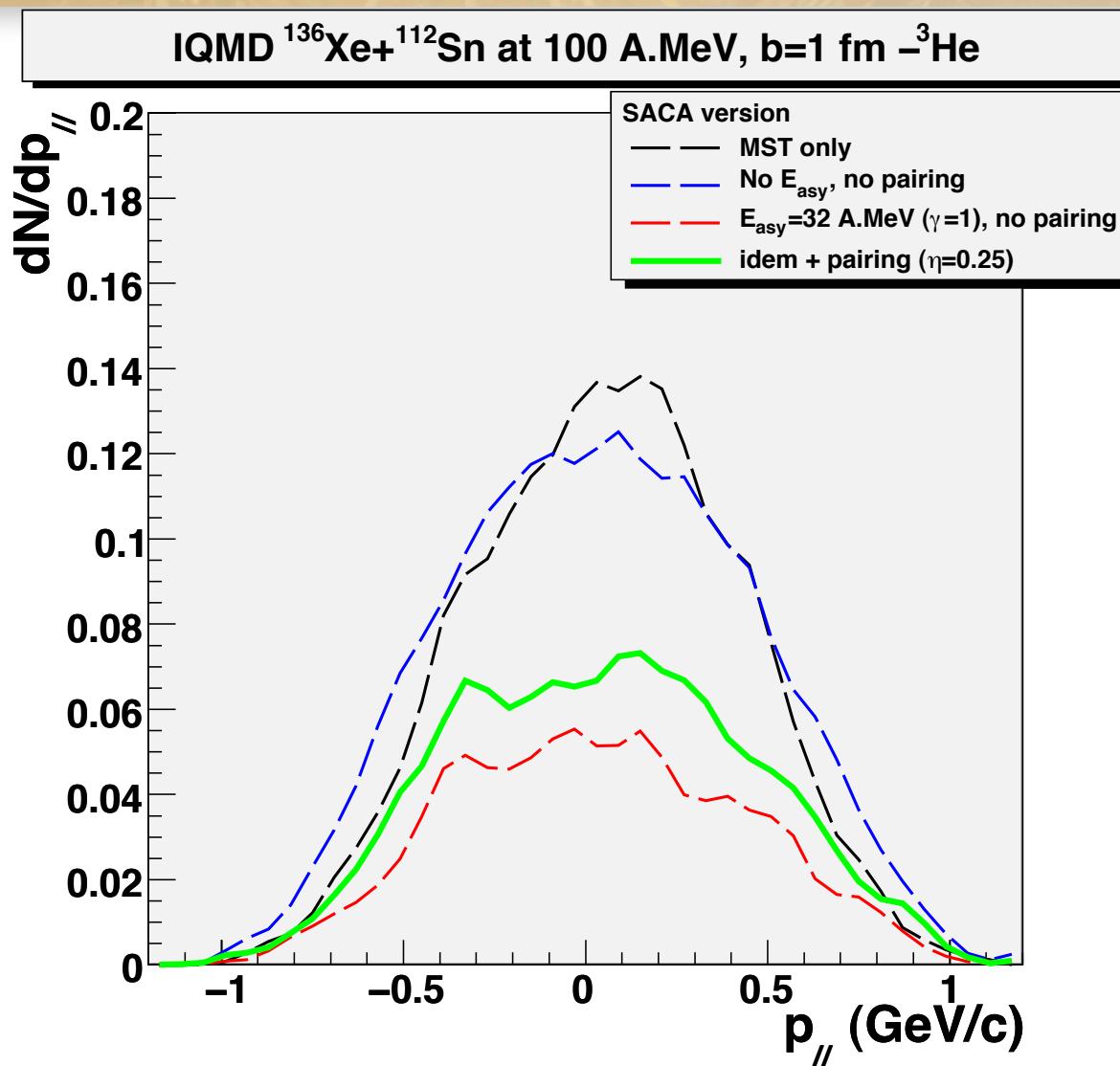
# How the dynamical patterns of isotopes are affected



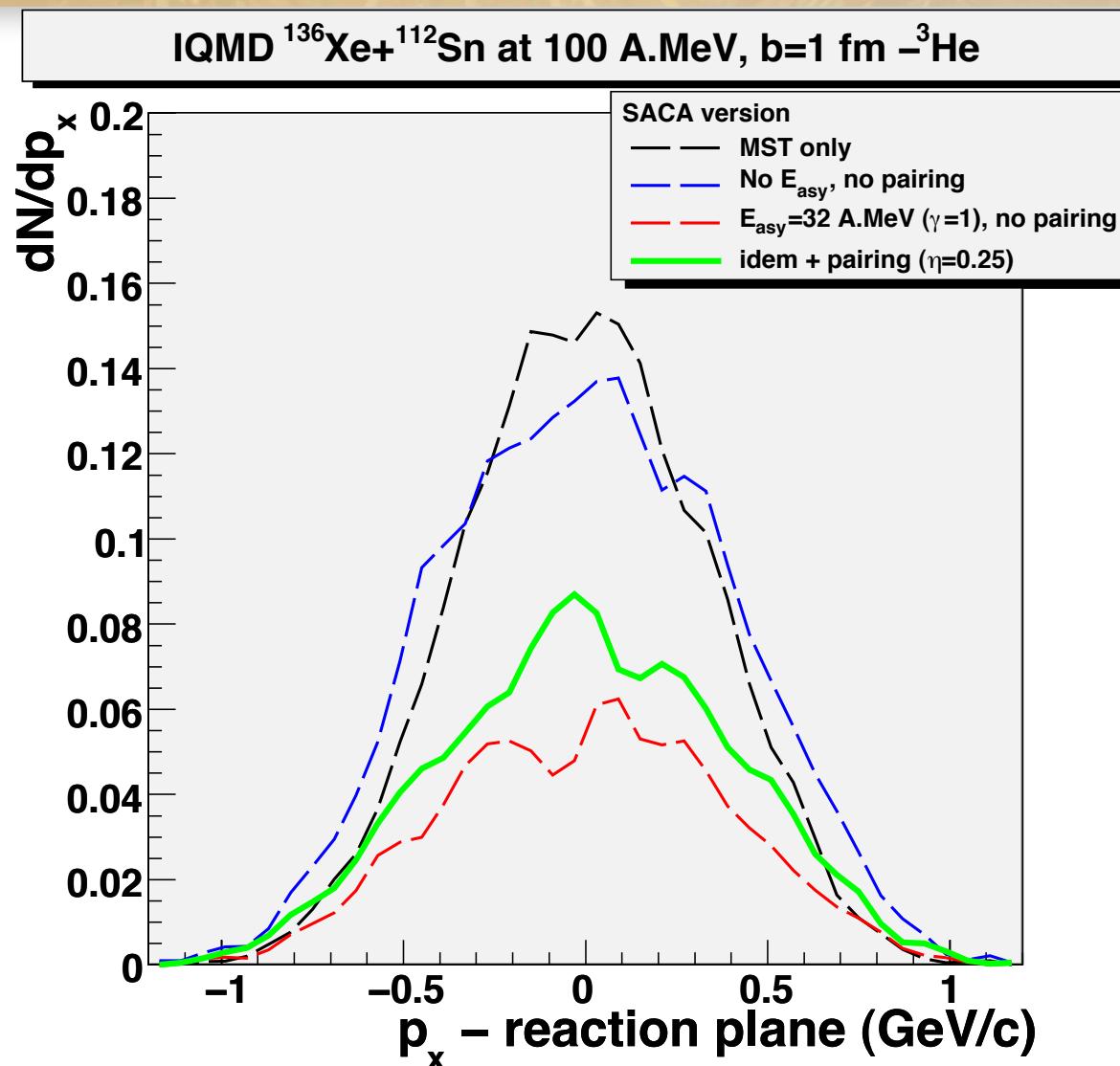
# How the dynamical patterns of isotopes are affected



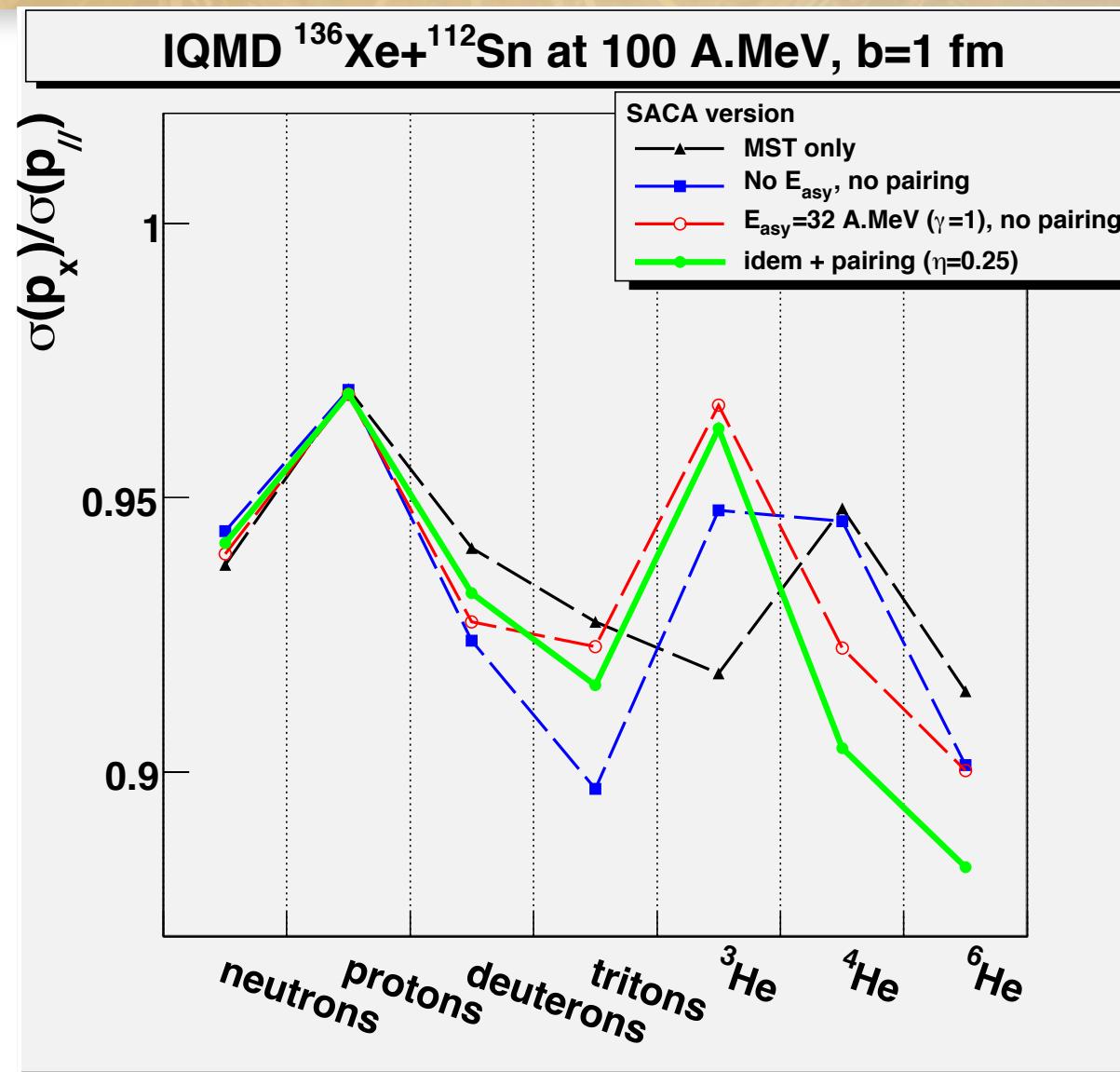
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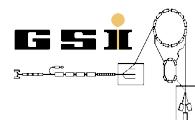
# How the dynamical patterns of isotopes are affected





## Excitation energy of the primary fragments

$$E^* = E_{g.s.} - E_{\text{bind}}$$



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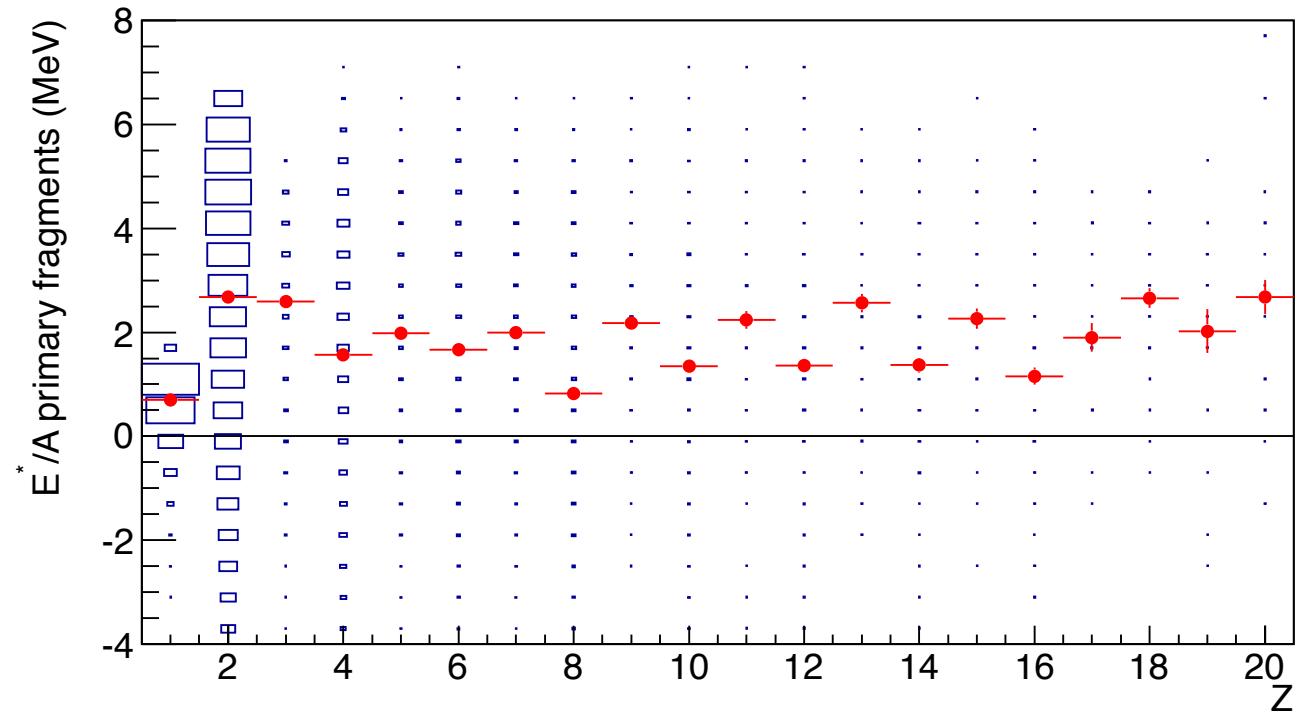
Arnaud Le Fèvre (GSI Helmholtzzentrum für Schwerionenforschung - Darmstadt) - AsyEOS 2012 - Syracuse (Sicily)



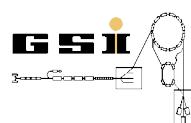
## Excitation energy of the primary fragments

$$E^* = E_{g.s.} - E_{bind}$$

IQMD+SACA  $^{129}\text{Xe} + ^{124}\text{Sn}$  at 100 A.MeV -  $b < 0.2 b_0$  fm (central)



On Average, 2 A.MeV of excitation energy. Corresponds to findings of S. Hudan et al. (INDRA collaboration), PRC 67, 064613 (2003).  
=> secondary decay (GEMINI) justified here.



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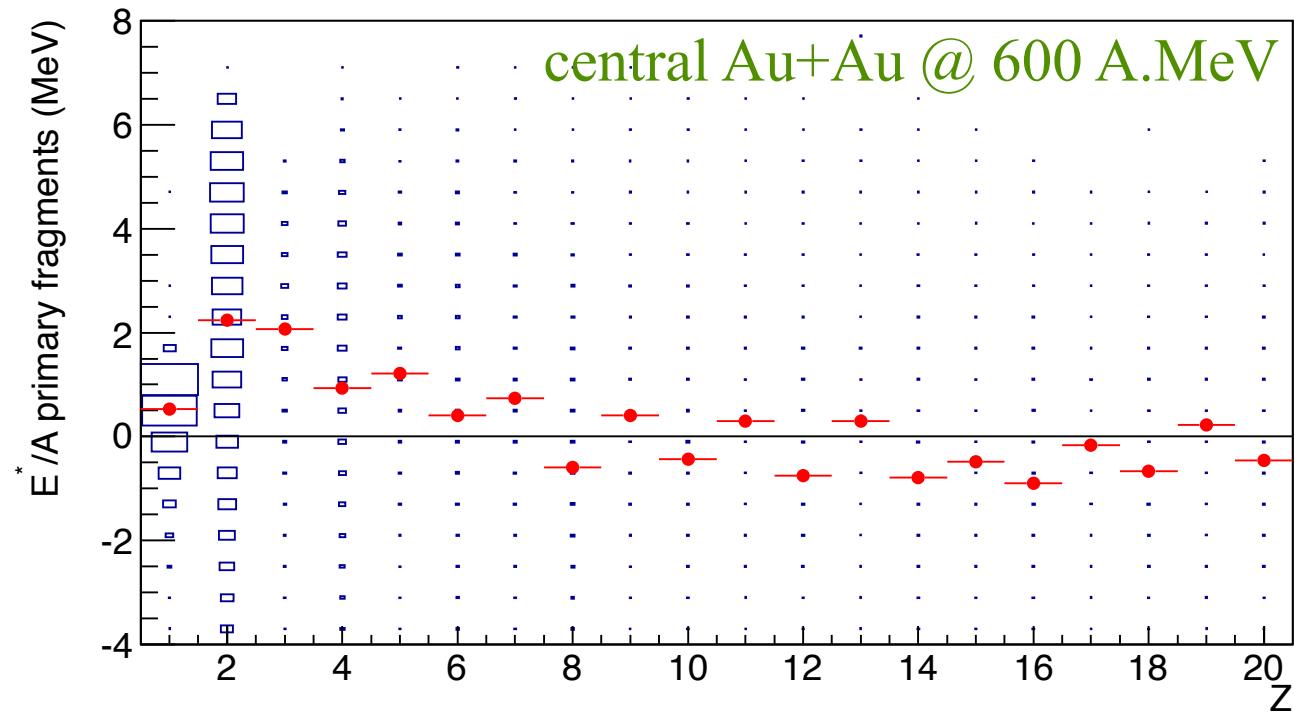
Arnaud Le Fèvre (GSI Helmholtzzentrum für Schwerionenforschung - Darmstadt) - AsyEOS 2012 - Syracuse (Sicily)



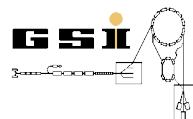
## Excitation energy of the primary fragments

$$E^* = E_{\text{g.s.}} - E_{\text{bind}}$$

IQMD+SACA  $^{197}\text{Au} + ^{197}\text{Au}$  at 600 A.MeV -  $b < 0.2 b_0$  fm (central)



At relativistic energies, in the participant-spectator regime, heavy primary clusters are produced colder on average.



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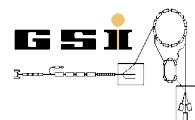
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## What can we learn from the isotope yields regarding the asymmetry energy?

Mean radius of primary clusters

IQMD+SACA



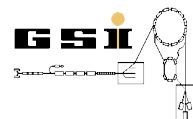
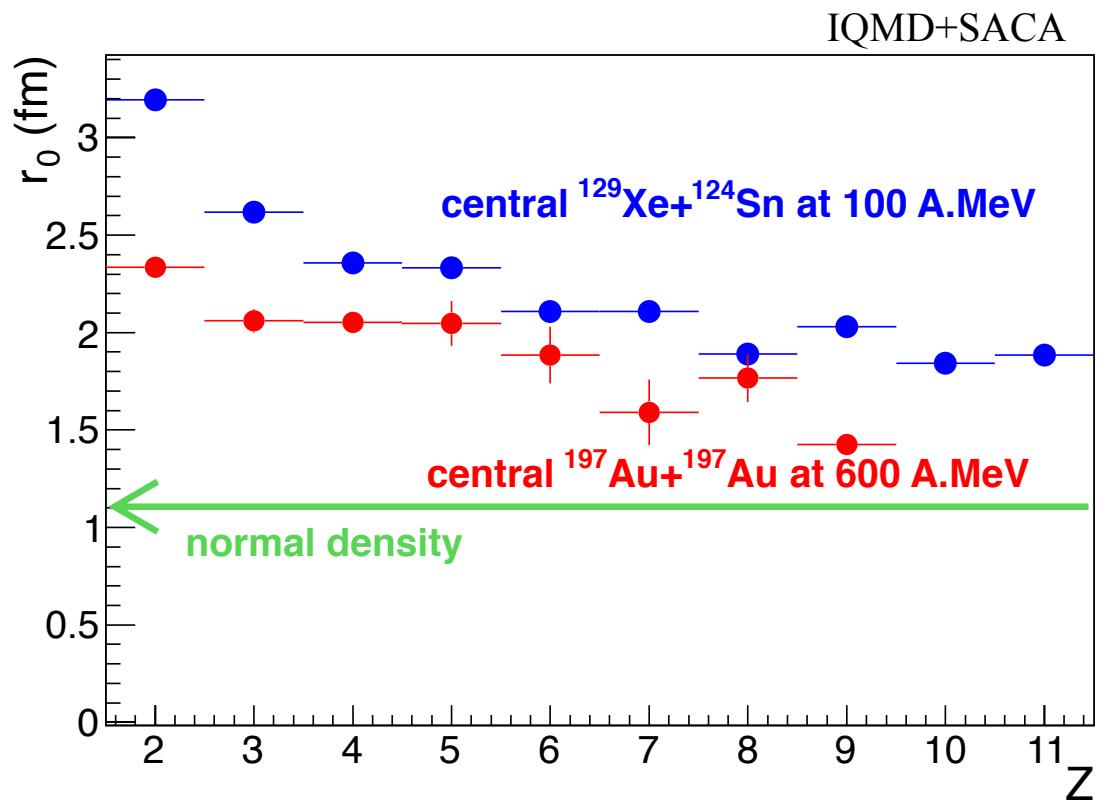
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## What can we learn from the isotope yields regarding the asymmetry energy?

Mean radius of primary clusters



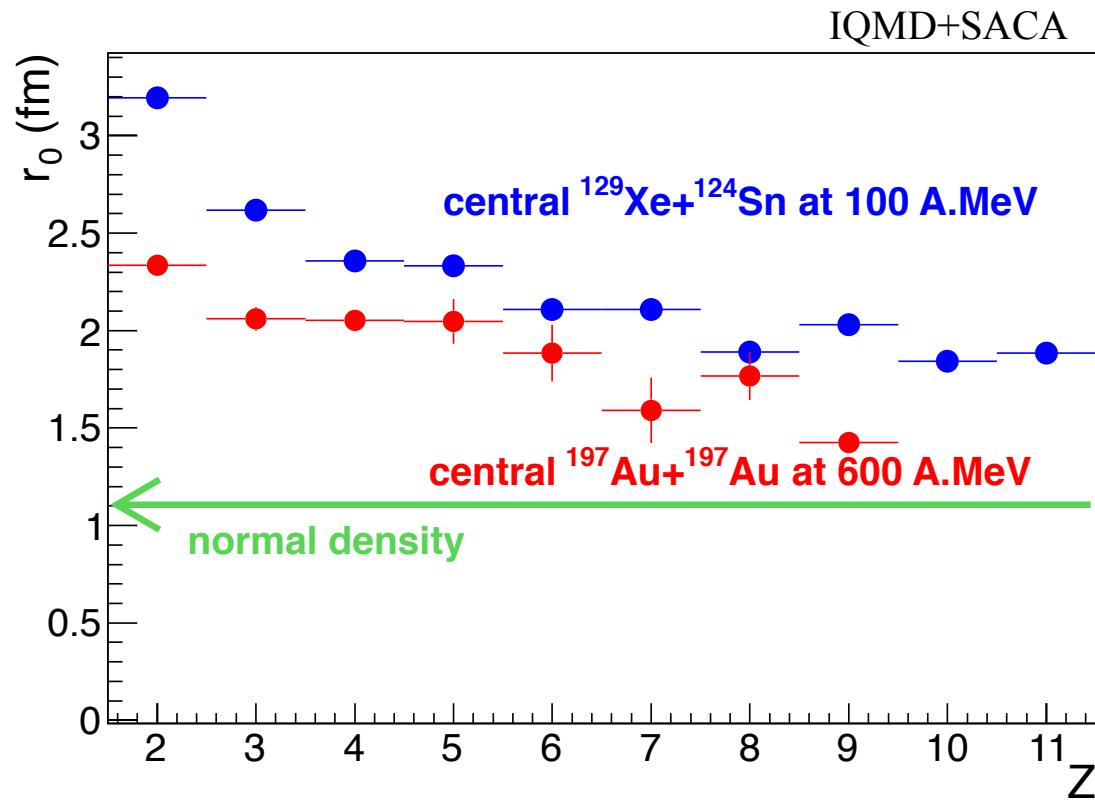
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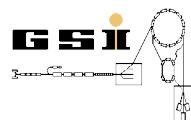


## What can we learn from the isotope yields regarding the asymmetry energy?

Mean radius of primary clusters



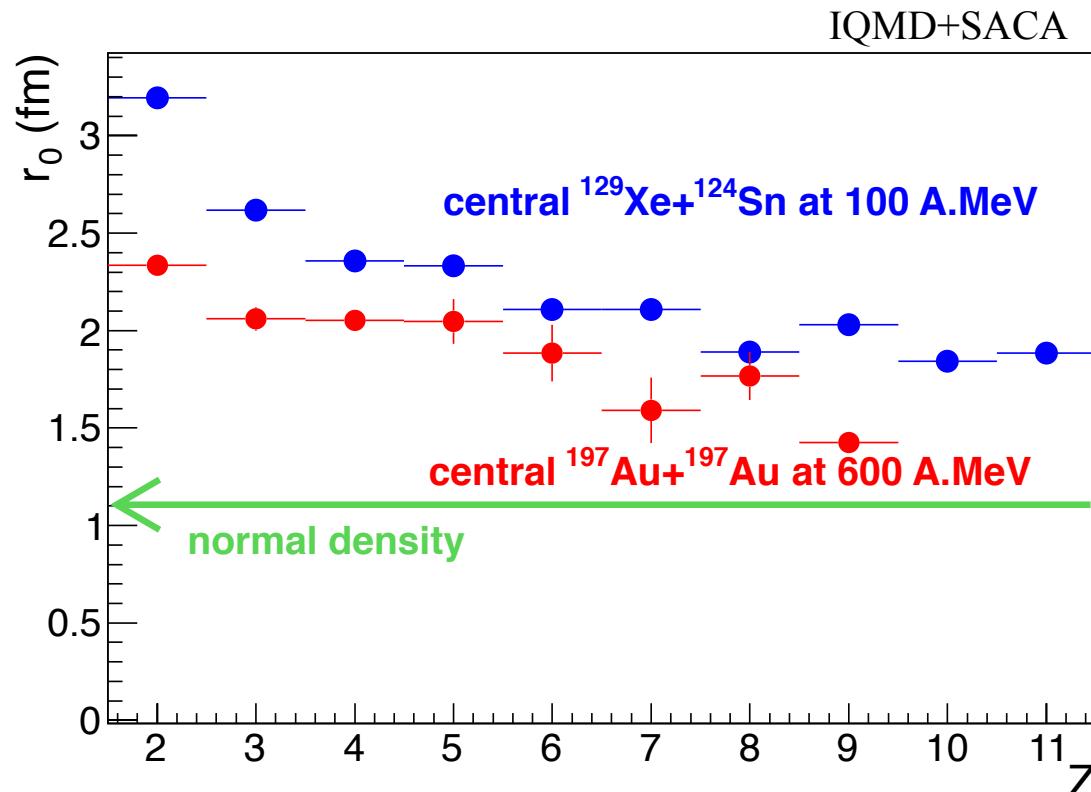
Though the medium is dense at this early stage, the dense clusters are disfavoured, because they would correspond to nucleons flowing against each other, hence with too high relative momenta to make a cluster.





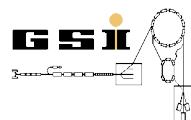
## What can we learn from the isotope yields regarding the asymmetry energy?

Mean radius of primary clusters



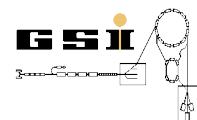
Though the medium is dense at this early stage, the dense clusters are disfavoured, because they would correspond to nucleons flowing against each other, hence with too high relative momenta to make a cluster.

$\Rightarrow$  The isotope yields can only inform on the low density dependence on the asymmetry energy.





# Asymmetry energy influence versus system energy



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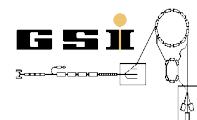
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# Asymmetry energy influence versus system energy

*W. Reisdorf and the FOPI Collaboration*

*Nuclear Physics A 848 (2010) 366–427*



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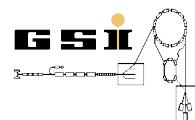
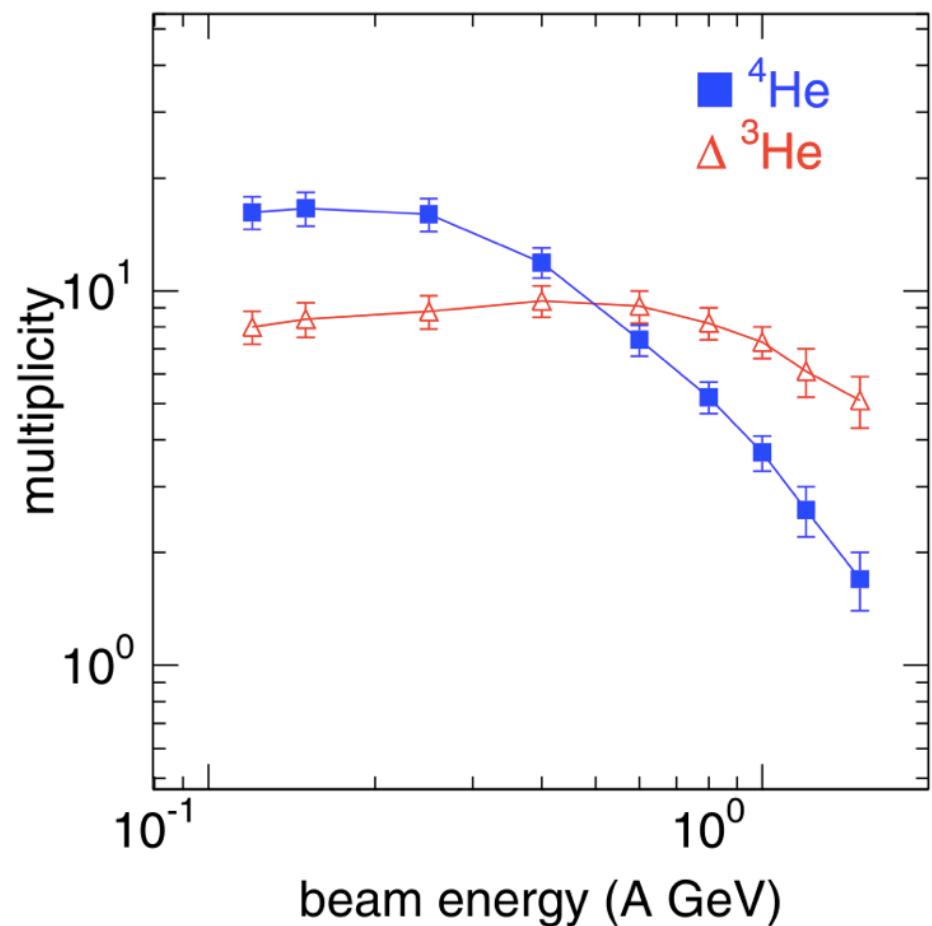


# Asymmetry energy influence versus system energy

*W. Reisdorf and the FOPI Collaboration*

*Nuclear Physics A 848 (2010) 366–427*

Au+Au  $b_0 < 0.15$



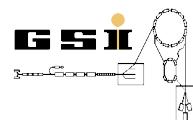
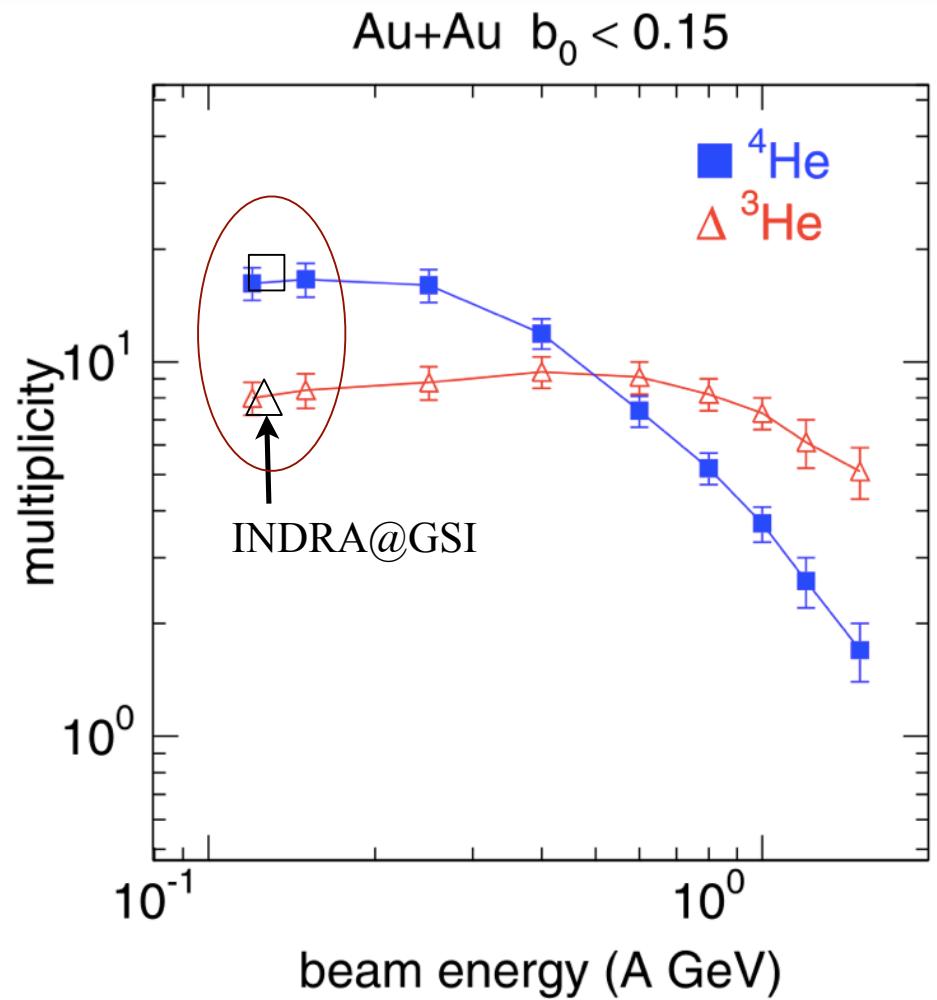
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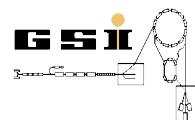
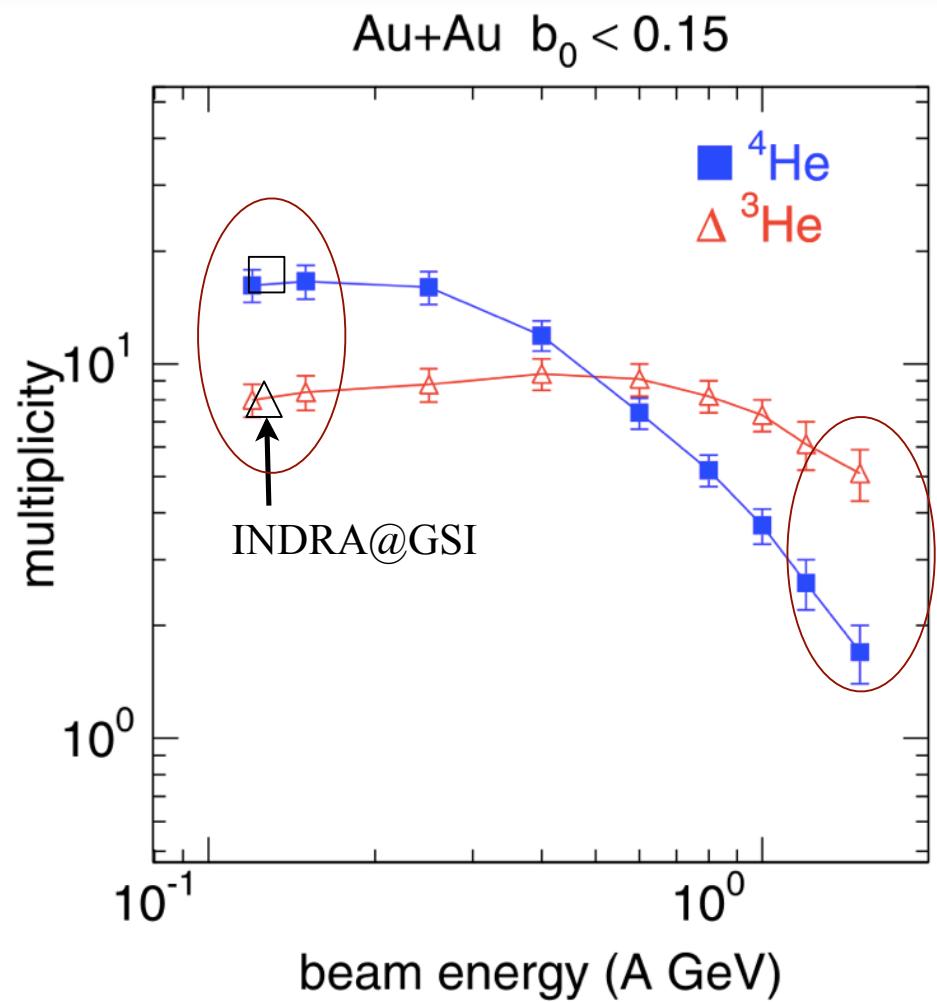
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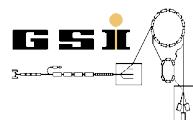
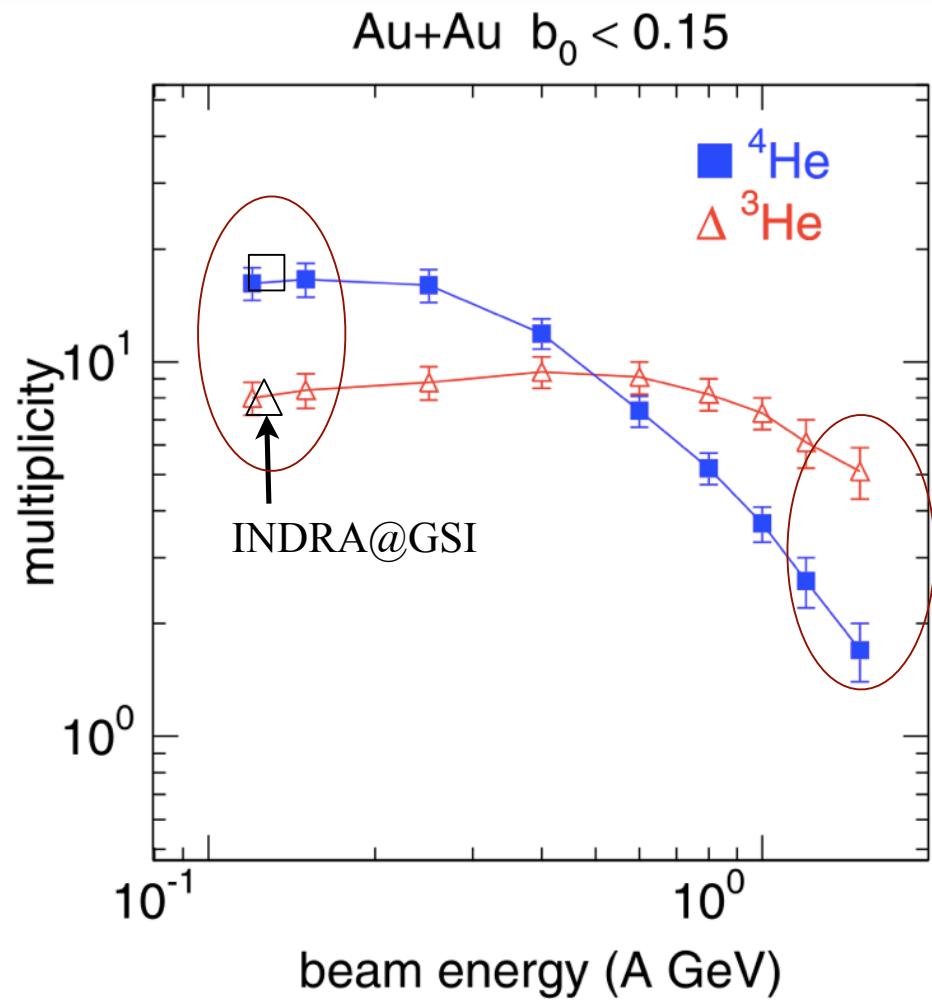


# Asymmetry energy influence versus system energy

*W. Reisdorf and the FOPI Collaboration*

*Nuclear Physics A 848 (2010) 366–427*

=> At high energy, the asymmetry energy effect on clusters seems to vanish. Timescale effect? Non-linear dependence on the density?

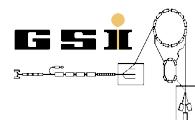
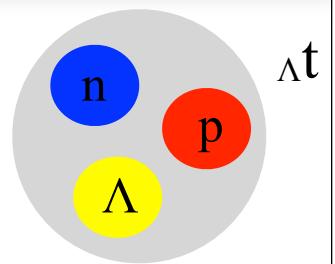


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## Another application of SACA : hypernuclei production



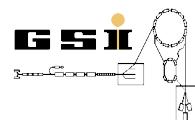
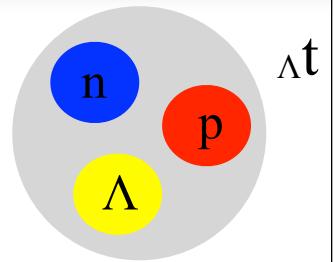
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## Another application of SACA : hypernuclei production

A hypernucleus is a nucleus which contains at least one hyperon ( $\Lambda(uds)$ , ...) in addition to nucleons.



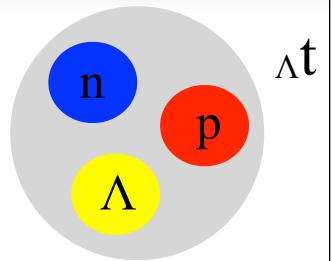
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Extending SACA for clusterising hadrons with hyperons (lambdas,...) for making **hypernuclei** is straightforward:

- ❖ one replaces  $V_{n-p}$  by  $V_{\Lambda-p}$  and  $V_{n-n}$  by  $V_{\Lambda-n}$
- ❖ and applies with these modifications the SACA algorithm.

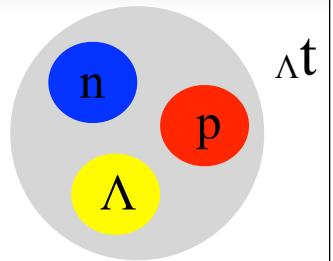
If in a final fragment there is a lambda, a hypernucleus should be created.

As a first approach, we have adopted  $V_{\Lambda-N} = 2/3 V_{n-N}$  ; further refinements are possible.



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Many ways of producing lambdas:  $K N \rightarrow \Lambda \pi$ ,  $\pi^+ n \rightarrow \Lambda K^+$ ,  $\pi^- p \rightarrow \Lambda K_0$ ,  $p p \rightarrow \Lambda X$   
⇒ influence of the EOS, in medium-properties, etc.



## Another application of SACA : hypernuclei production

IQMD+SACA

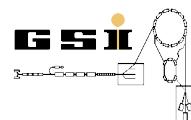
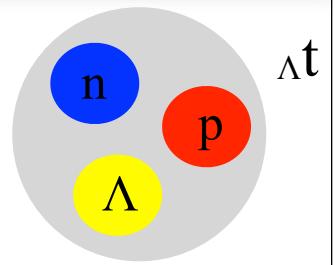
$^{58}\text{Ni} + ^{58}\text{Ni}$

at

1.91 A.GeV

( $b < 6 \text{ fm}$ ) -

$t_{\text{cluster}} = 20 \text{ fm/c}$



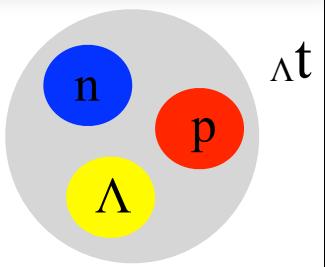
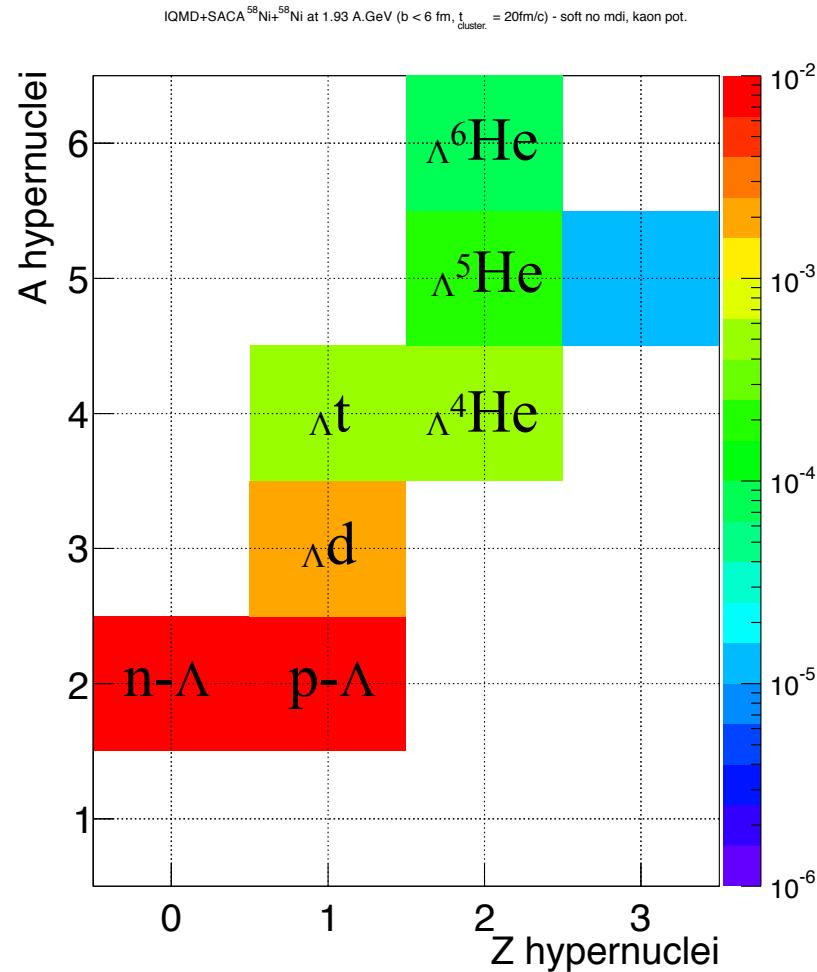
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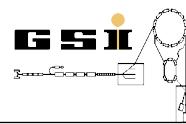


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Soft EOS  
no m.d.i.  
with Kaon pot.



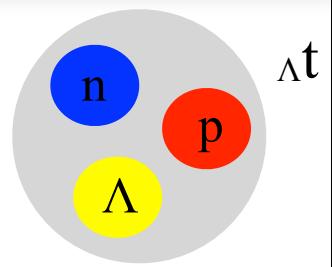
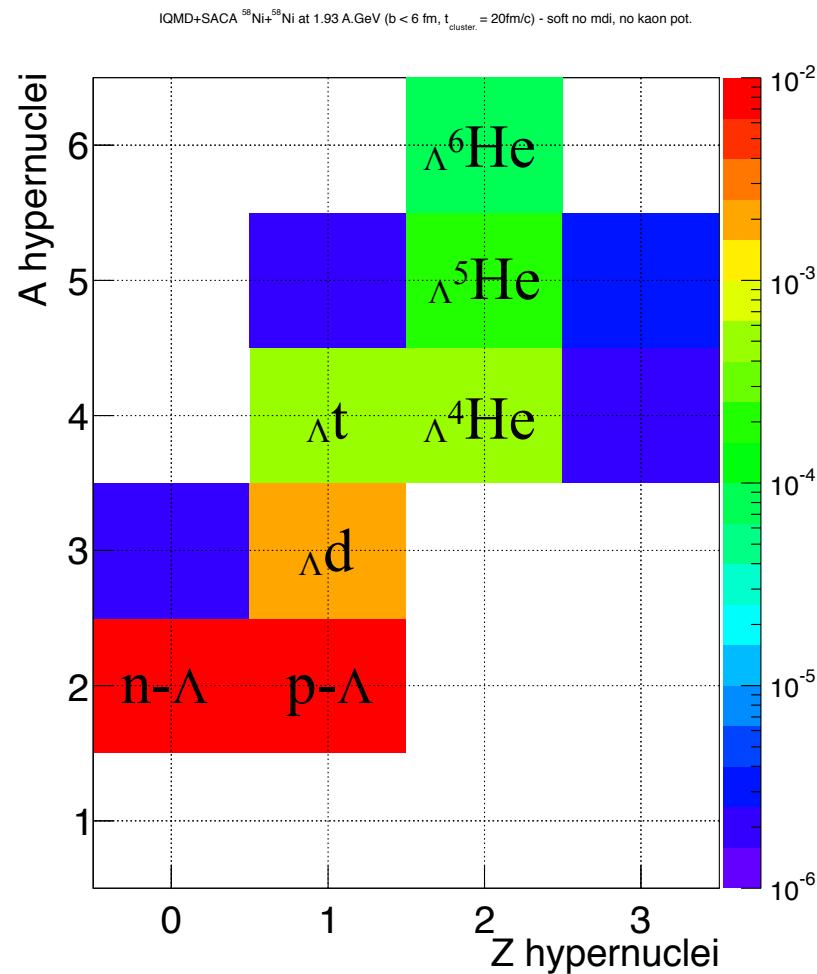
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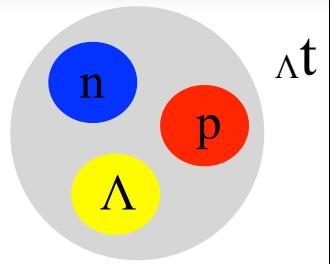
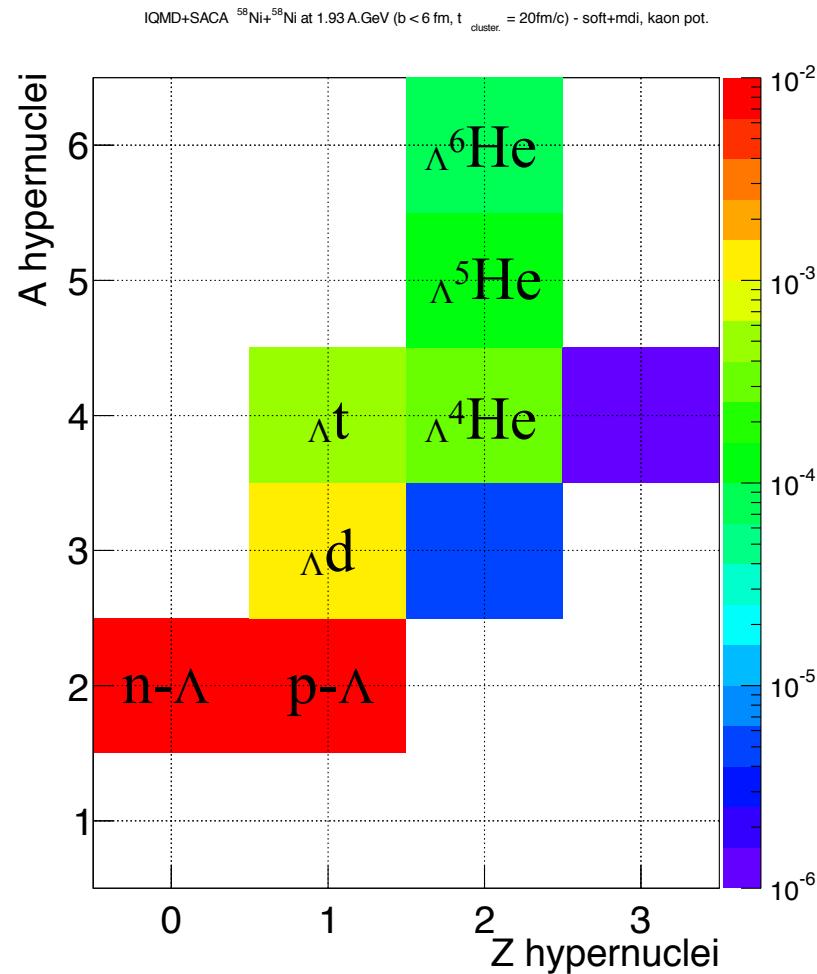
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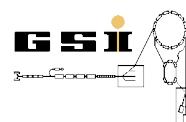


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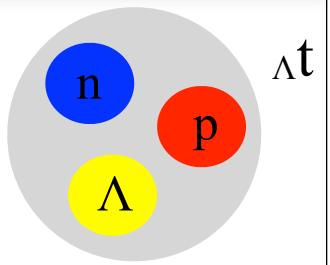
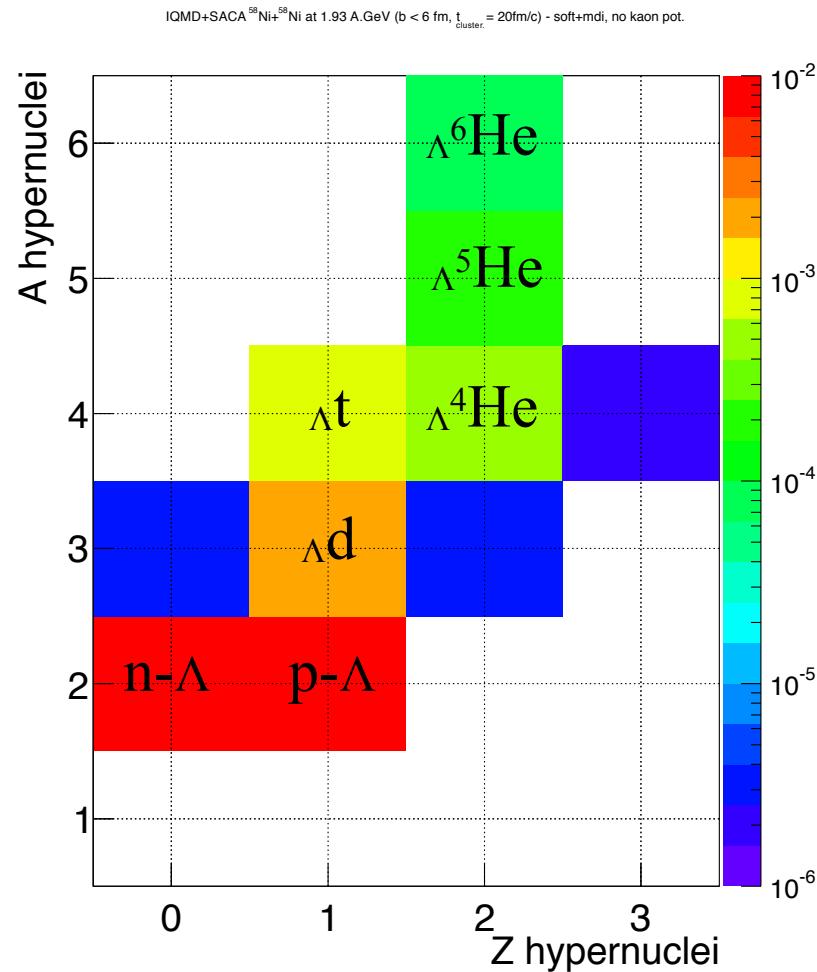
Soft EOS  
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with Kaon pot.



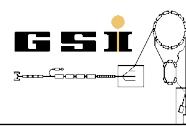


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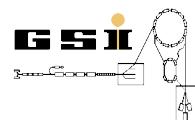
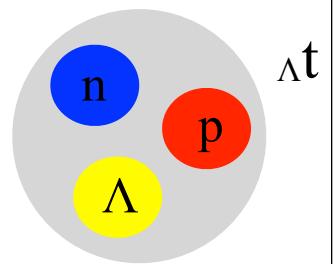


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## Strong phase space constraints

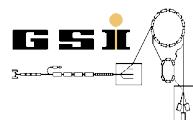
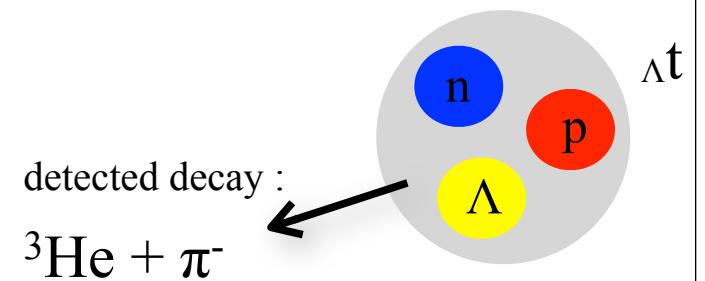


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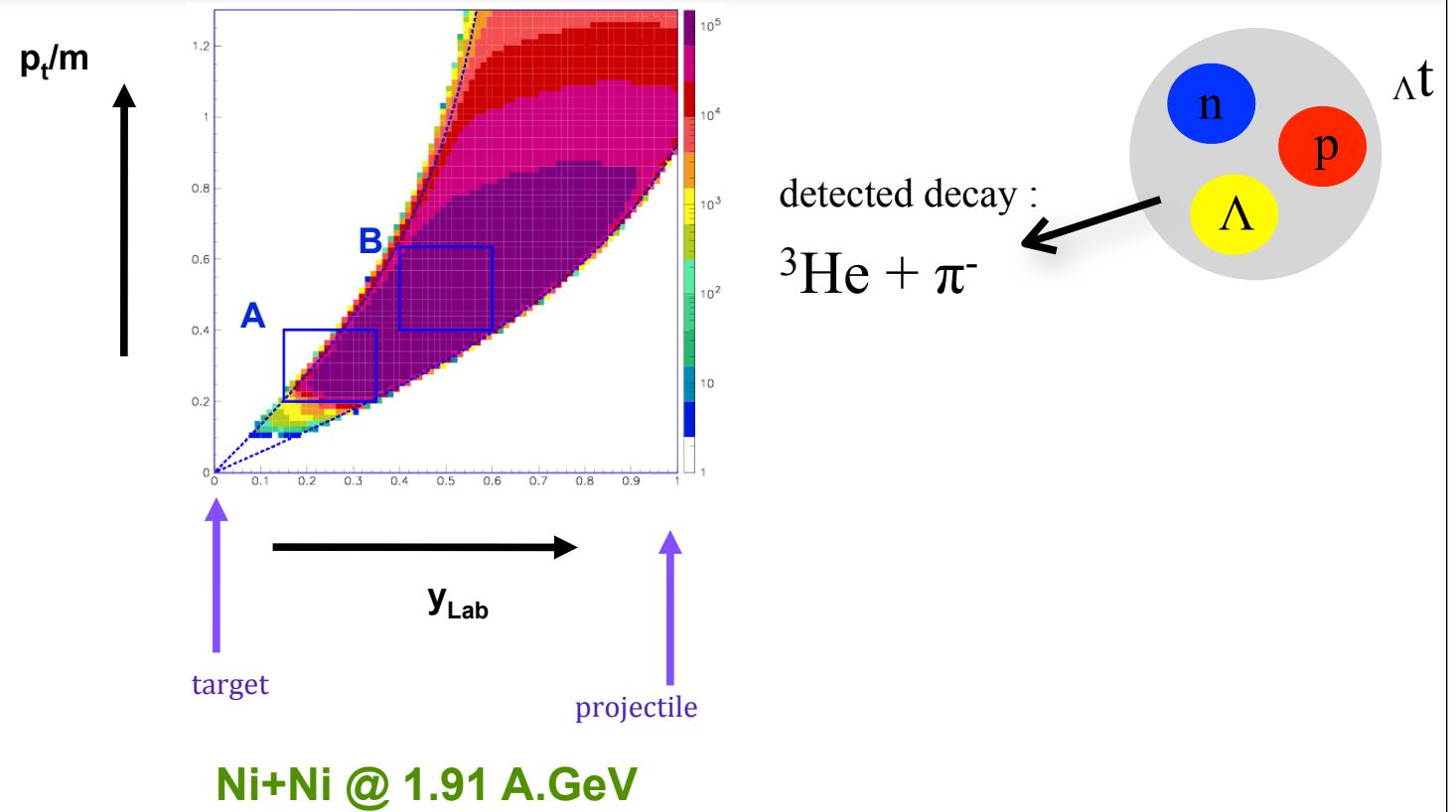
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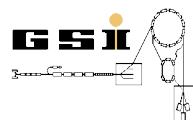


## Strong phase space constraints

FOPI Coll.  
Y. Zhang, Heidelberg



Preliminary



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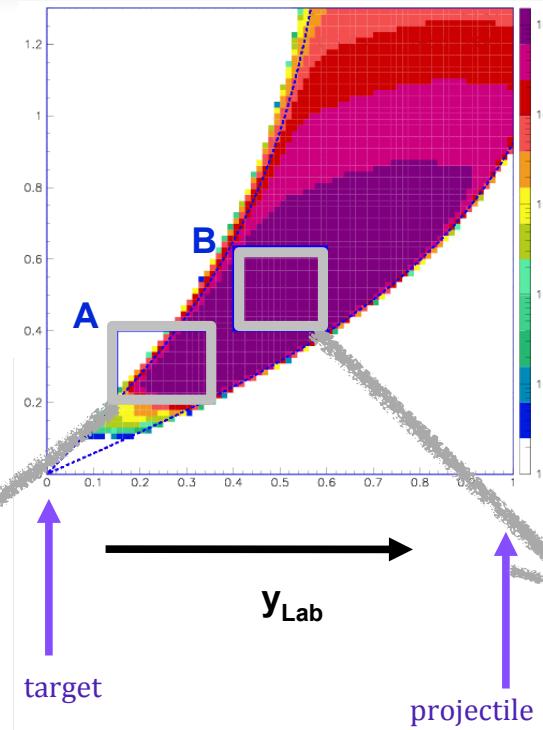
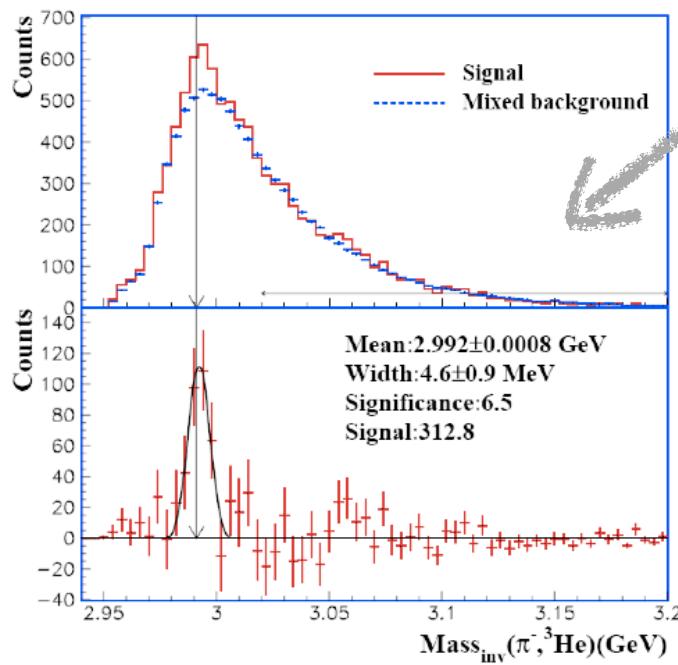
Arnaud Le Fèvre (GSI Helmholtzzentrum für Schwerionenforschung - Darmstadt) - AsyEOS 2012 - Syracuse (Sicily)



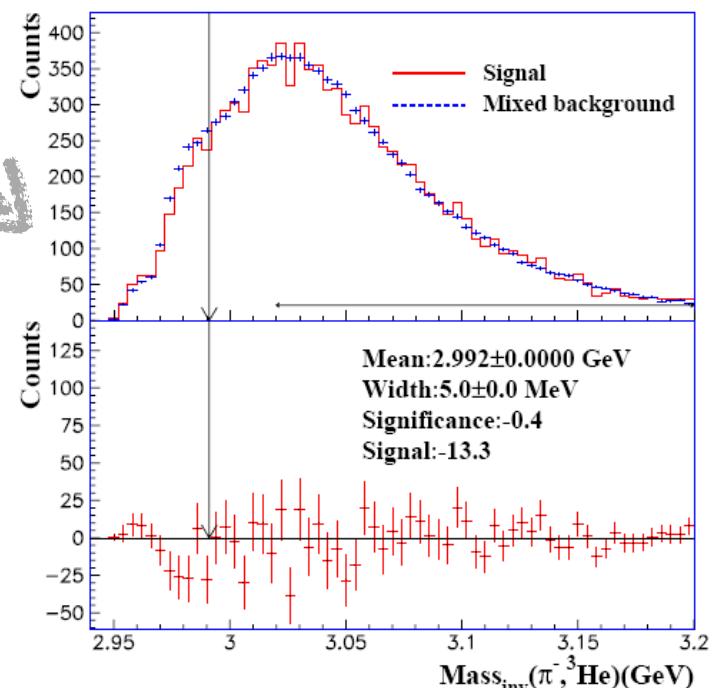
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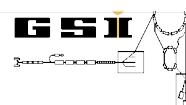
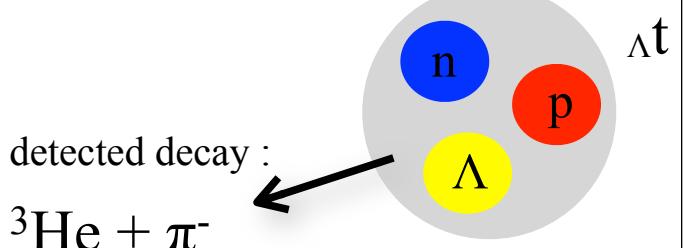
Excess over combinatorial background only in region A



Ni+Ni @ 1.91 A.GeV



Preliminary



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## Strong phase space constraints

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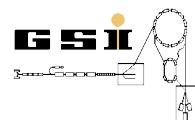
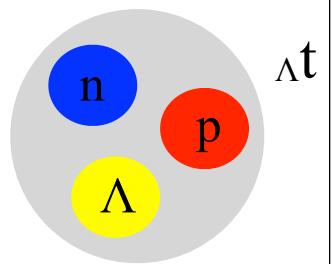
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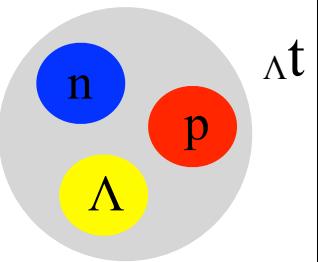
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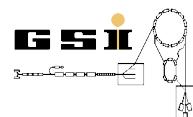
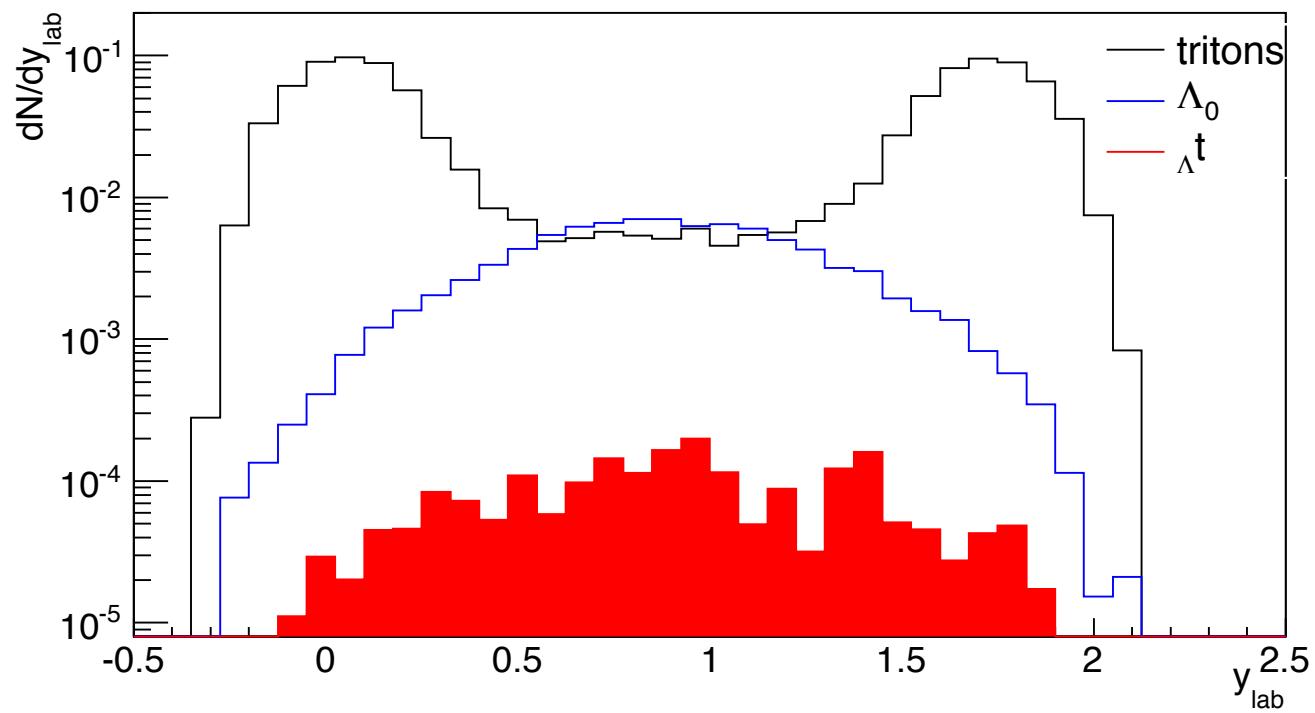


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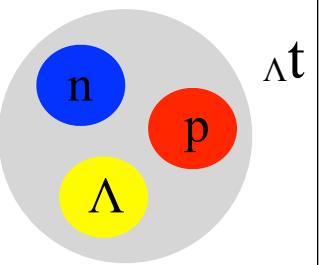
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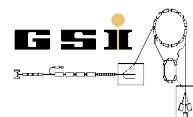
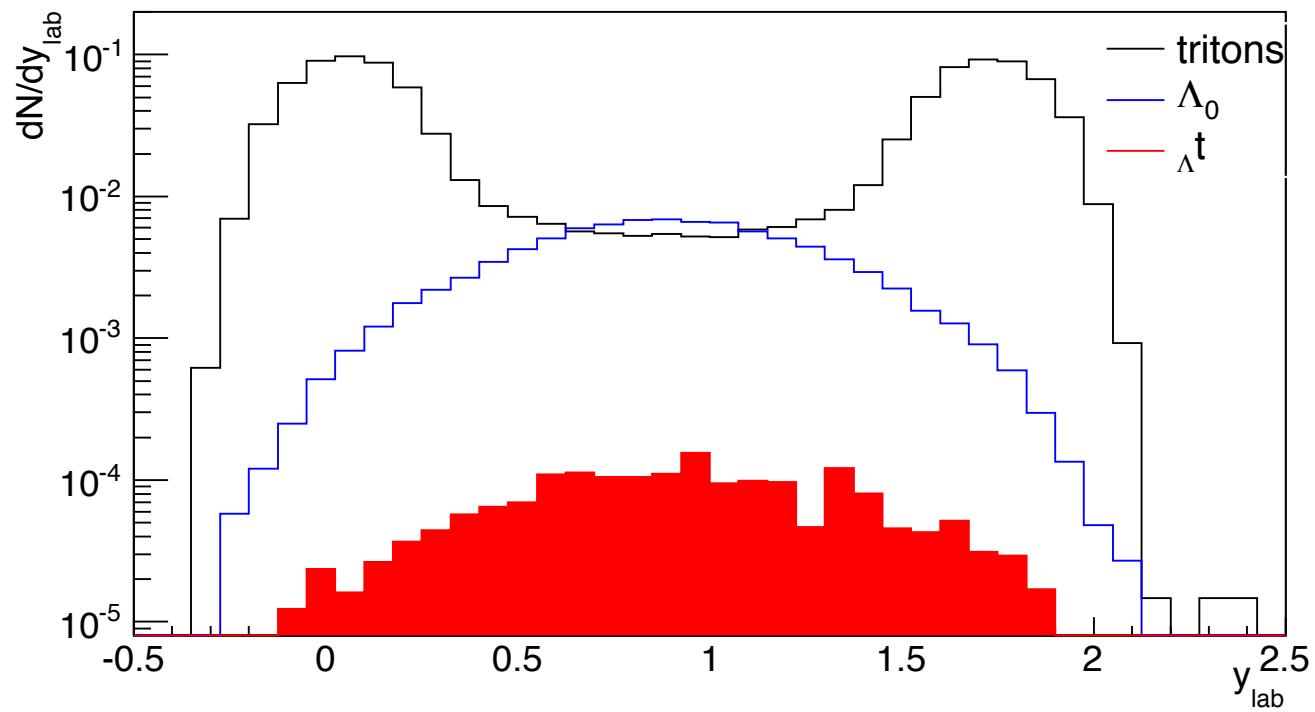


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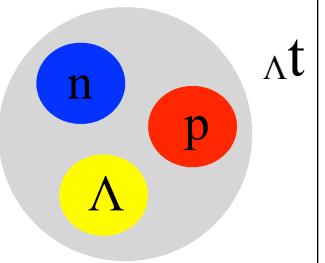
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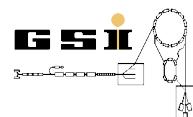
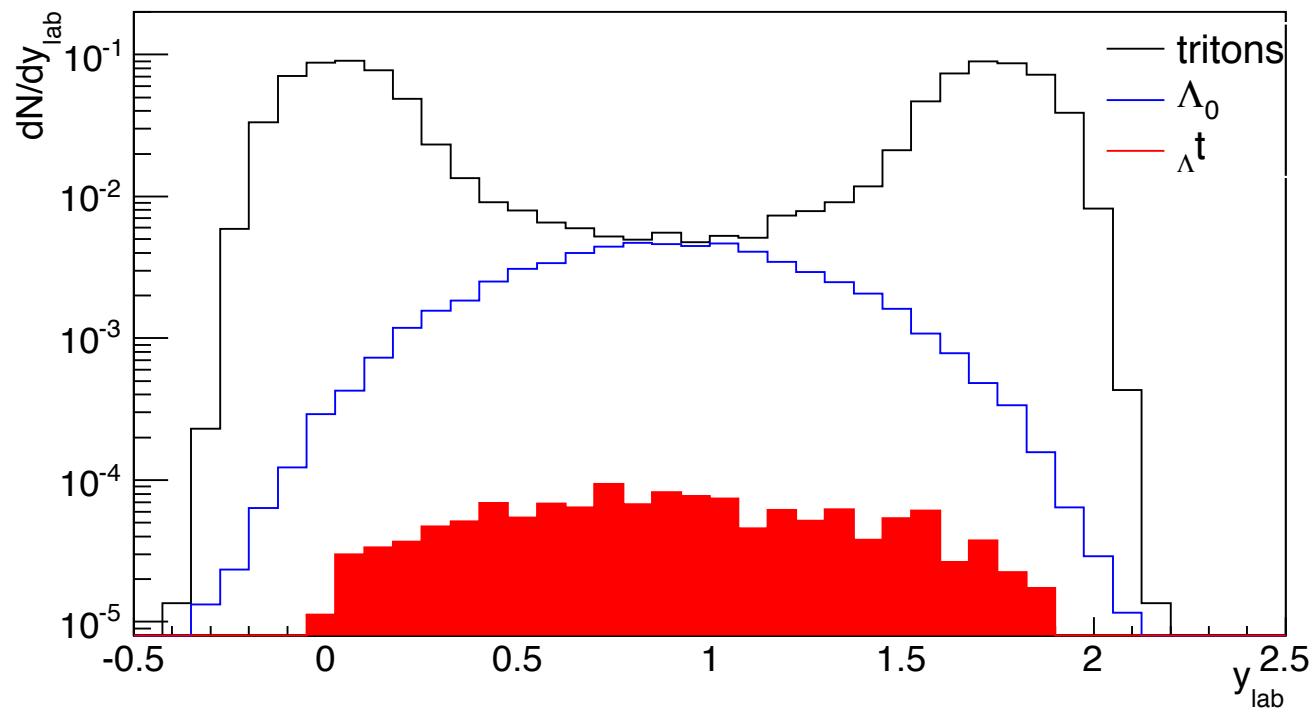


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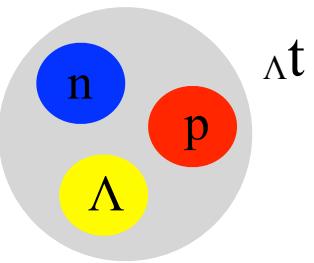
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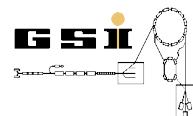
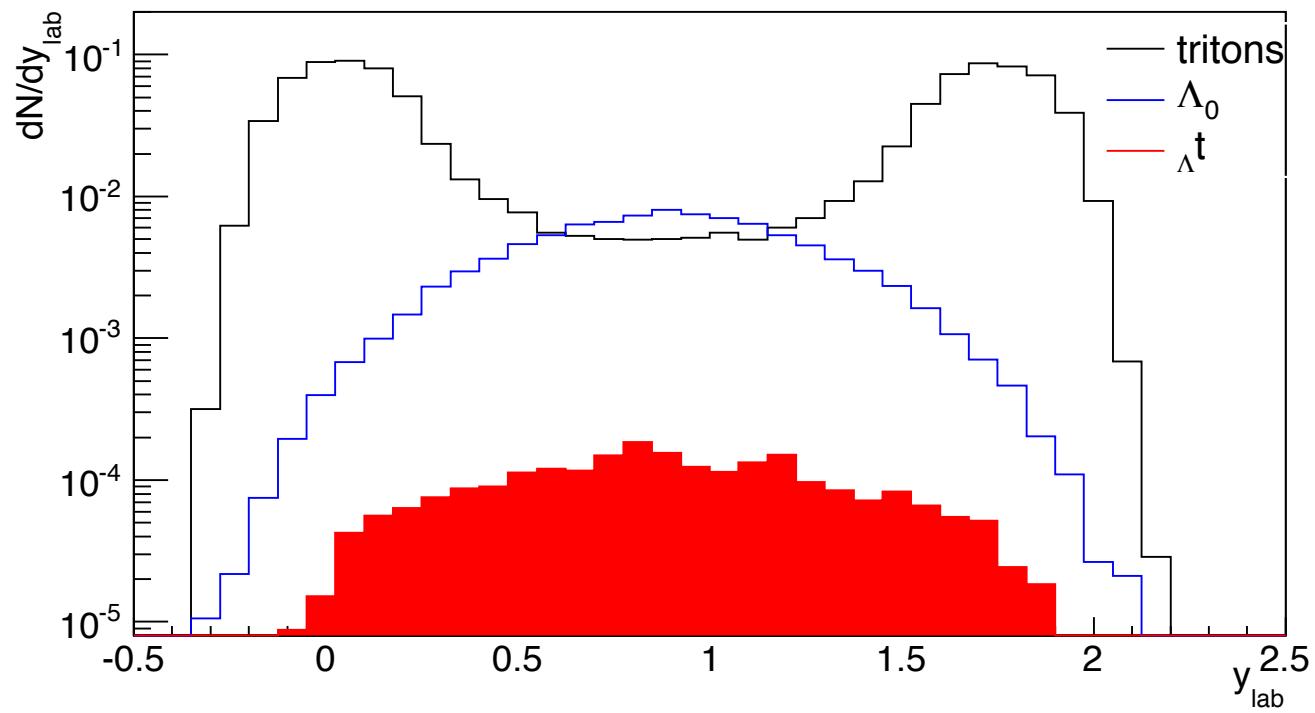


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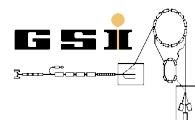
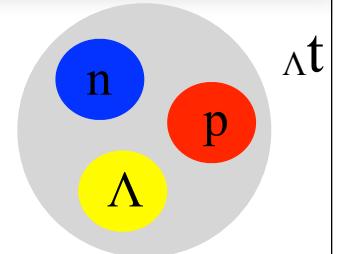
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IQMD+SACA  
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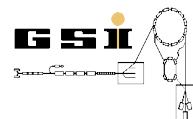
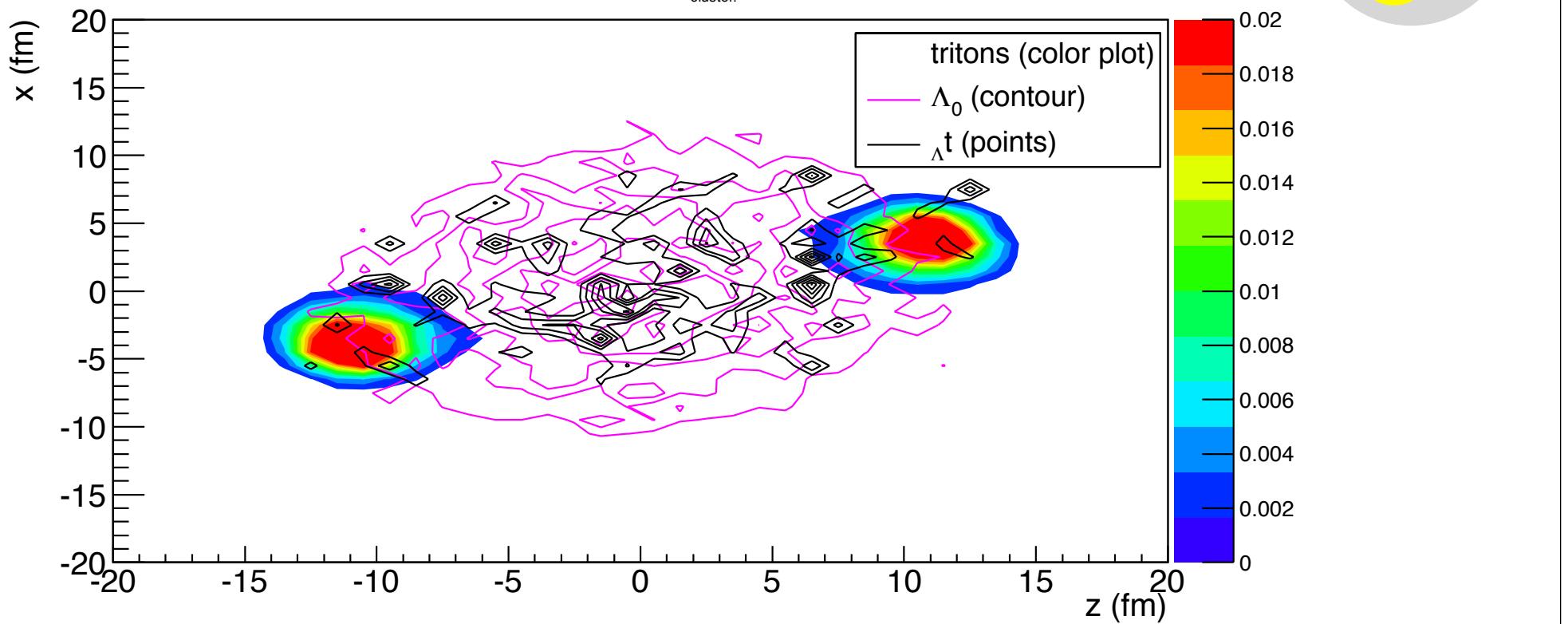
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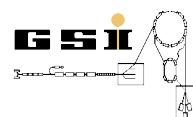
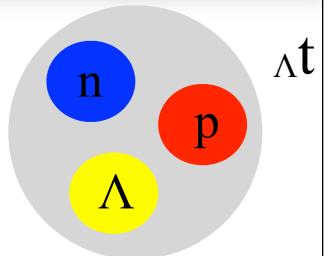
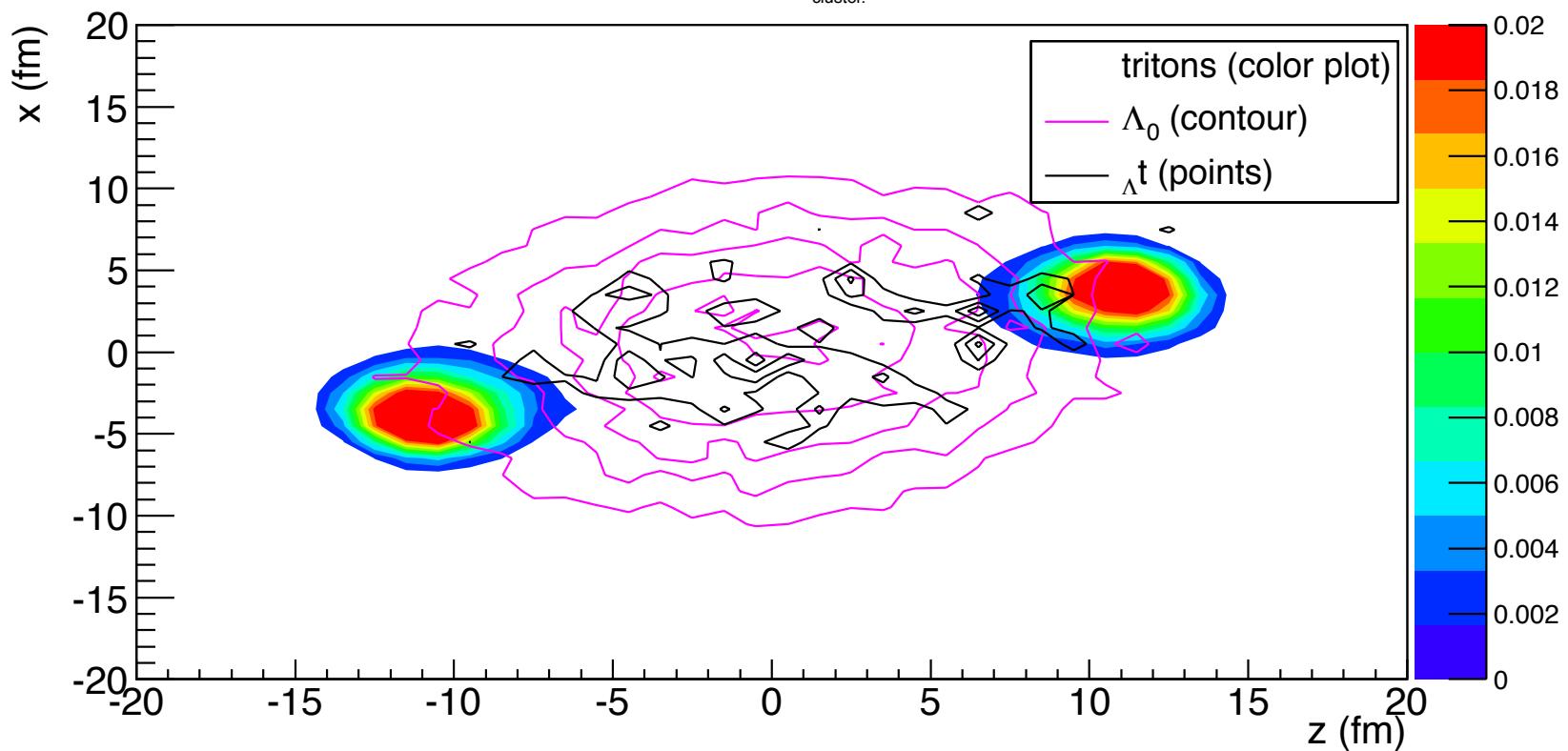
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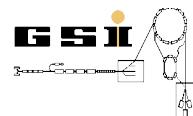
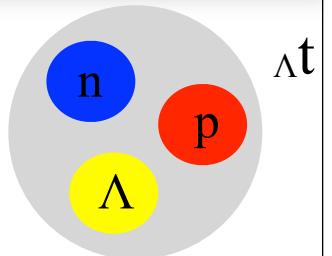
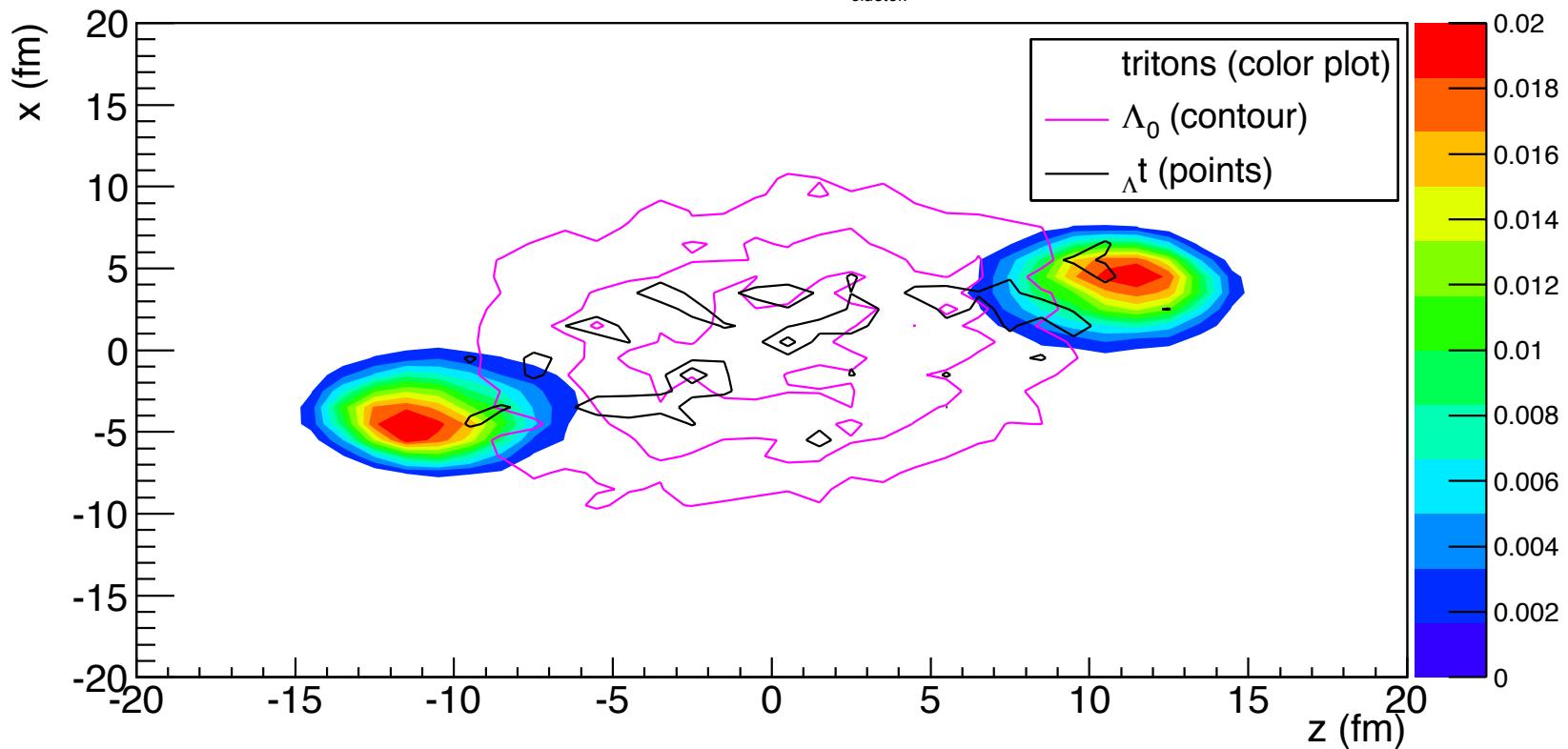
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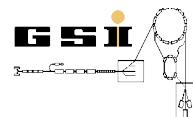
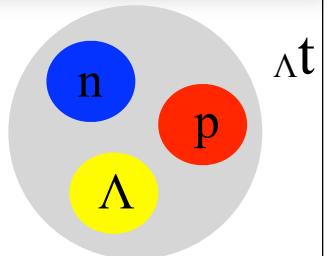
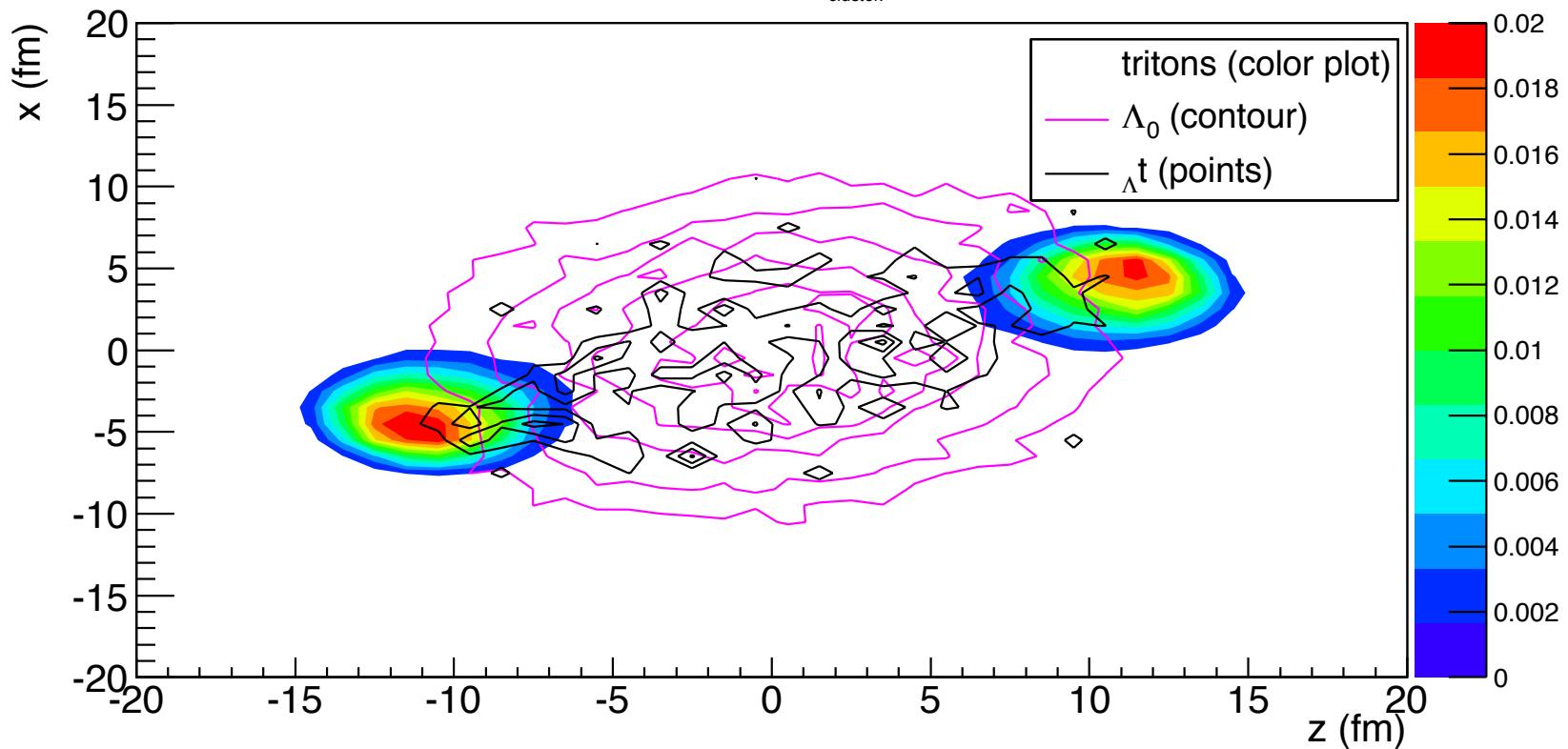
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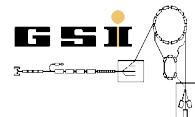


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# Summary and perspectives



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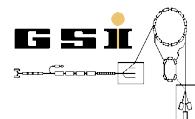
Arnaud Le Fèvre (GSI Helmholtzzentrum für Schwerionenforschung - Darmstadt) - AsyEOS 2012 - Syracuse (Sicily)



## Summary and perspectives

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- ❖ Supplying SACA with a more precise description of nuclei binding energy at abnormal density allows promising, realistic predictions of absolute isotope yields, and hypernuclei.
- ❖ The asymmetry energy has a strong influence on the anisotropy (apparent stopping power) for some isotopes ( $^3\text{He}$ ,  $^4\text{He}$ , ...).
- ❖ Within this model, isotope yields cannot inform on the high density dependence of the asymmetry energy.  $\Rightarrow$  better look at n / p,  $\text{K}^+ / \text{K}^-$ ,  $\pi^+ / \pi^-$  yields/flows for that purpose.



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## Further developments:

After processing SACA, proceed:

- ❖ further decay of primary unstable isotopes like  $^8\text{Be}$ ,  $^5\text{He}$ , etc., which lifetime do not allow to detect them still bound in the detectors,
- ❖ allow early  $^3\text{He} + n \rightarrow ^4\text{He}$  according to its particularly high cross-section.
- ❖ secondary decay (evaporation code like GEMINI) of still excited clusters. Particularly relevant at intermediate energies ( $E_{beam}$  100 A.MeV down to the Fermi regime)
- ❖ for hypernuclei formation, refine lambda-N potential in SACA or EOS/Kaon potential in IQMD in order to predict reasonably the measured cross-sections, and momentum distributions, which are very constraining.