

Constraints on dependence of the symmetry energy from elliptic flow data

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Overview

- **Introduction & Motivation**
- **HIC Model**
- **In-medium effects**
- **Flow observables**
- **Summary & Outlook**

Introduction

Equation of State (EoS) of Nuclear Matter:

$$E(\rho) = E(\rho_0) + \frac{K}{18} \frac{(\rho - \rho_0)^2}{\rho_0^2}$$

$$P = \rho^2 \frac{\partial E(\rho)}{\partial \rho} \quad K = 9 \frac{\partial P}{\partial \rho}$$

Sources

- finite nuclei $\rho/\rho_0 \leq 1$
- heavy – ions $\rho/\rho_0 \leq 3$
- neutron stars $\rho/\rho_0 \leq 10$

Relevance:

- structure of neutron star cores
- astrophysical processes like supernova explosions

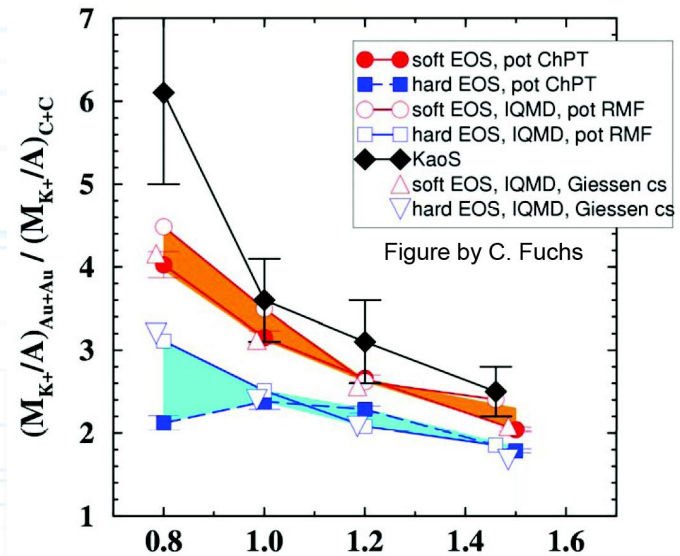
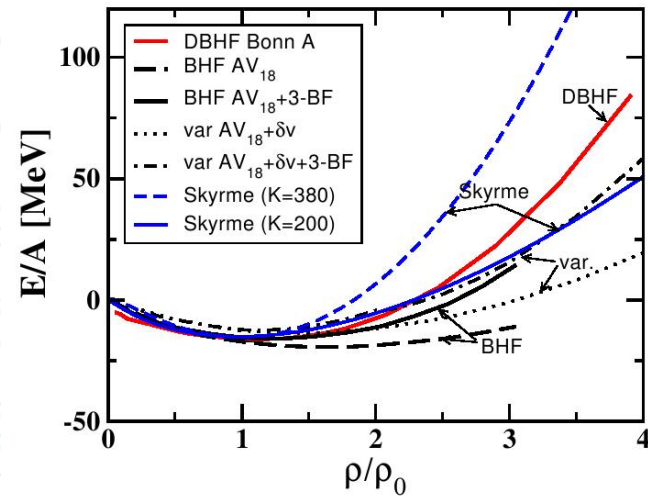


Figure by C. Fuchs

C. Fuchs et al. PRL 86, 1974 (2001)
 C. Hartnack et. al. PRL 96, 012302(2006)

Symmetry Energy

EoS of Asymmetric Nuclear Matter

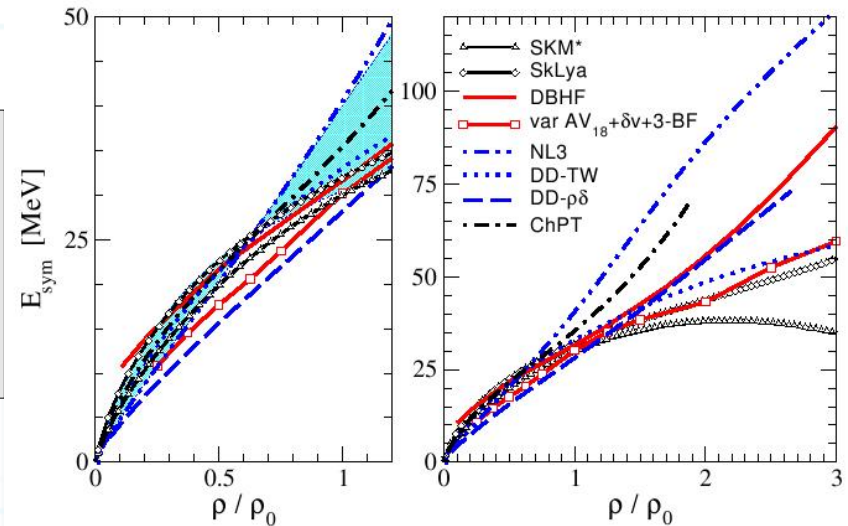
$$E(\rho, \beta) = E(\rho, \beta=0) + S(\rho)\beta^2 \quad \beta = \frac{\rho_n - \rho_p}{\rho}$$

$$S(\rho) = S(\rho_0) + \frac{L}{3} \frac{\rho - \rho_0}{\rho_0} + \frac{K_{sym}}{18} \frac{(\rho - \rho_0)^2}{\rho_0^2}$$

Theoretical estimates of L and K

B.A. Li *et al.* *Int.J.Mod.Phys. E7*, 147 (1998)

| Force | Paris | SKM* | SI' | SIH | DHF (b) | DHF (e) |
|-----------|-------|--------|--------|--------|---------|---------|
| L | 68.8 | 45.78 | 35.34 | 9.91 | 132 | 138 |
| K_{sym} | 37.56 | -155.9 | -259.1 | -393.7 | 466 | 276 |



Experimental results:

isospin diffusion/neutronskin thickness
of Pb: $L \approx 65$ MeV [B.A. Li *et al.* PRC 72,064611 \(2005\)](#)

giant monopole resonances:
 $K_{sym} = -566 \pm 1350$ MeV; 34 ± 159 MeV
[S. Shlomo *et al.* PRC 47, 529 \(1993\)](#)

Neutron Stars

equilibrium w.r.t. weak interactions

$$\frac{\partial E}{\partial \beta}(\rho, \beta) + \frac{\partial E_L}{\partial \beta}(\beta) = 0$$

K. Saito et al. arXiv:1207.1554

Pure Nucleonic NS

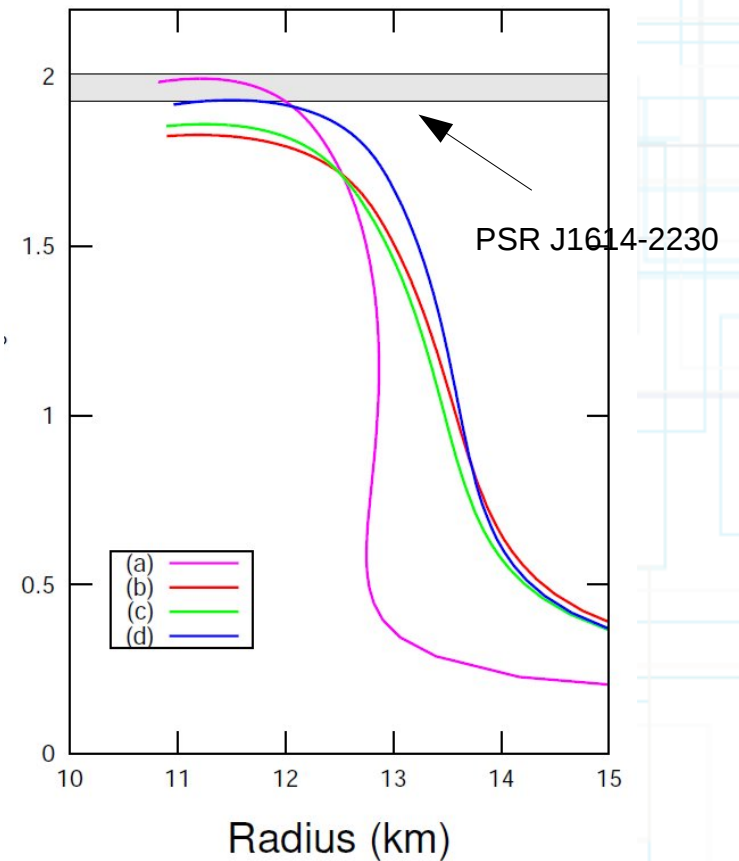
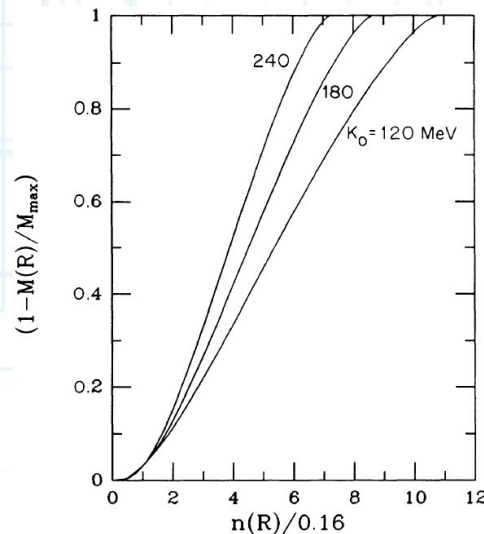
$S(\rho)$ determines how β depends on density

maximum mass scales like $K^{1/2}$

$S(\rho)$ bigger impact for softer K

M. Prakash et al. PRL 61, 2518 (1988)

| $F(u)$ | K_0 (MeV) | M_{\max}/M_{\odot} | R (km) |
|--------------------|----------------|----------------------|-------------|
| u | 120 | 1.458(1.70) | 9.114 |
| | 180 | 1.722(1.90) | 9.879 |
| | 240 | 1.935(2.07) | 10.57 |
| $\frac{2u^2}{1+u}$ | 120 | 1.470(1.95) | 9.895 |
| | 180 | 1.738(2.10) | 10.318 |
| | 240 | 1.952(2.24) | 10.933 |
| \sqrt{u} | 120 | 1.404(1.45) | 8.435 |
| | 180 | 1.679(1.71) | 9.324 |
| | 240 | 1.895(1.92) | 10.112 |



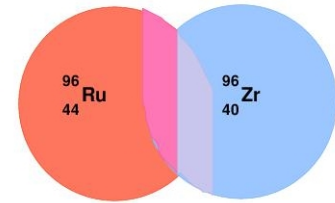
Motivation: FOPI/FOPI-LAND Experiments

FOPI Collaboration: p and charged mass fragments
in the 0.150 – 1.5 AGeV energy range

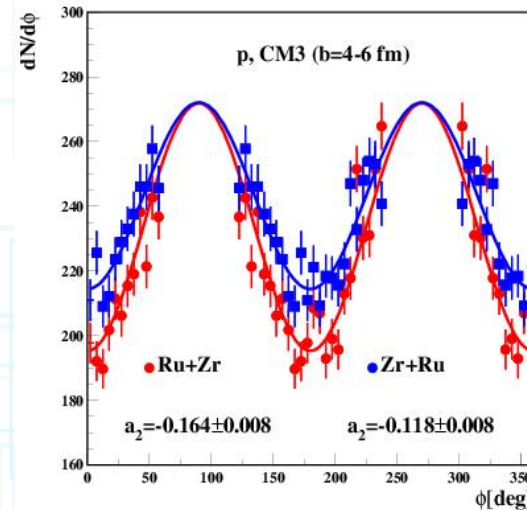
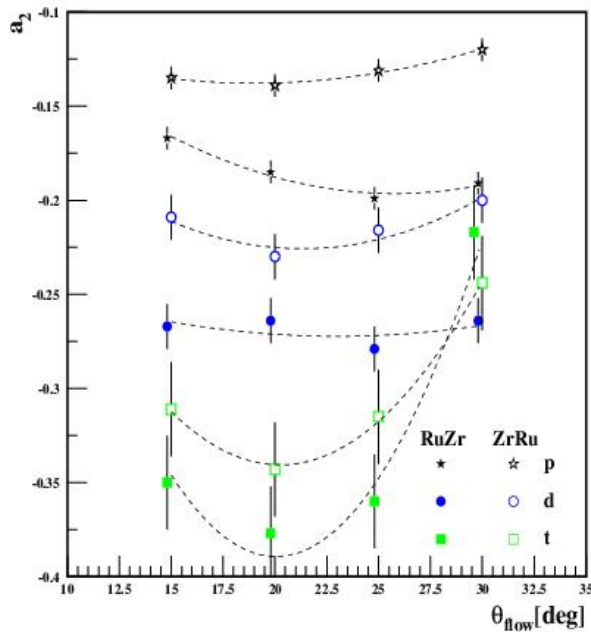
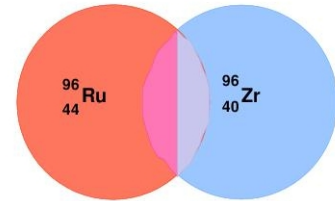
Rami et al., PRL 84,1120;
Hong et al., PRC 66, 034901; A. Andronic et al. NPA 679,765 (2001)

FOPI LAND: n, p and light mass fragments

Y. Leifels et al. PRL 71, 963 (1993); D. Lambrecht Z.Phys. 350,115 (1994)



N/Z 1.18 1.25 | 1.32 1.4

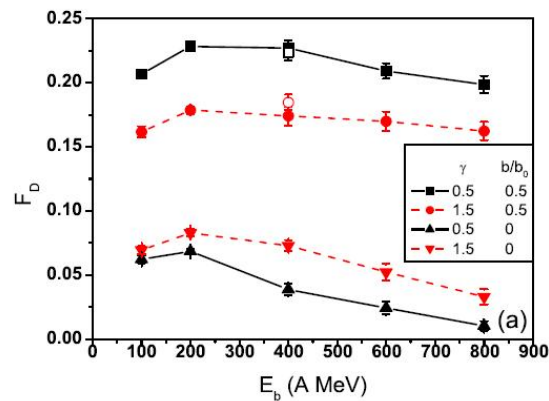
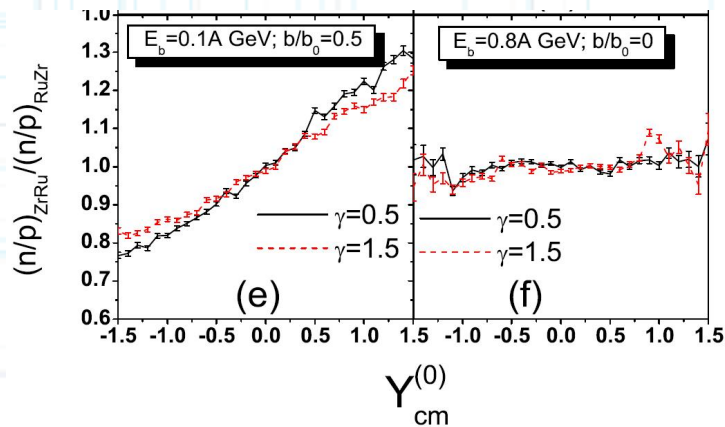


M. Petrovici et al. (FOPI) preliminary/
unpublished

Observables

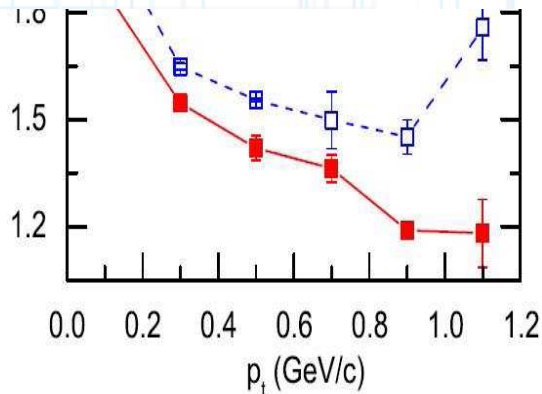
symmetry potential has opposite sign for neutrons (repulsive) and protons (attractive)

slope of double neutron to proton ratio $(n/p)_{AB}/(n/p)_{BA}$ Li, Li, Stoecker PRC 73, 051601(2006)

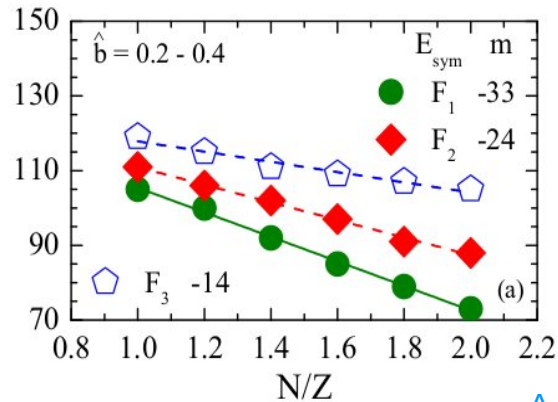


$$S(u) = S_0 u^\gamma \quad u = \rho / \rho_0$$

neutron/proton ratio at midrapidity



balance energy of transverse flow



$$\langle p_x^{dir} \rangle = \frac{1}{N} \sum_1^N \text{sign}(y_i) p_x(i)$$

Yong, Li, Chen PLB 650, 344 (2007)

A. Sood, PRC 84, 014611 (2011)

Transport Model

Quantum Molecular Dynamics (QMD):

Monte Carlo cascade + Mean field + Pauli-blocking+ in medium cross section

all 4* resonances below 2 GeV - 10 Δ^* and 11 N^*

baryon-baryon collisions:

all elastic channels

inelastic channels $NN \rightarrow NN^*$, $NN \rightarrow N\Delta$, $NN \rightarrow \Delta N^*$, $NN \rightarrow \Delta\Delta^*$, $NR \rightarrow NR'$

pion-absorption \Leftrightarrow resonance-decay channels: $\Delta \leftrightarrow N\pi$, $\Delta^* \leftrightarrow \Delta\pi$, $N^* \leftrightarrow N\pi$

meson production/absorption: $\eta(547)$, $\rho(770)$, $\omega(782)$, $\eta'(958)$, $f_0(980)$, $a_0(980)$, $\Phi(1020)$

applied to study:

- dilepton emission in HIC: [K.Shekter, PRC 68, 014904 \(2004\)](#); [D. Cozma, PLB640,170 \(2006\)](#);
[E.Santini PRC78,03410 \(2008\)](#)
- EoS of symmetric nuclear matter: [C. Fuchs, PRL86, 1974](#); [Z.Wang NPA645,177](#)
- In-medium effects and HIC dynamics: [C. Fuchs, NPA 626,987](#); [U. Maheswari NPA 628,669](#)

Isospin dependence of EoS

EoS of isospin asymmetric nuclear mater: [Das, Das Gupta, Gale, Li PRC67, 034611 \(2003\)](#)

$$U(\rho, \beta, p, \tau, x) = A_u(x) \frac{\rho_{\tau'}}{\rho_0} + A_l(x) \frac{\rho_{\tau}}{\rho_0} + B(\rho/\rho_0)^{\sigma} (1 - x\beta^2) - 8\tau x \frac{B}{\sigma + 1} \frac{\rho^{\sigma-1}}{\rho_0^{\sigma}} \beta \rho_{\tau'}$$

$$+ \frac{2C_{\tau\tau}}{\rho_0} \int d^3p' \frac{f_{\tau}(\vec{r}, \vec{p}')}{1 + (\vec{p} - \vec{p}')^2/\Lambda^2} + \frac{2C_{\tau\tau'}}{\rho_0} \int d^3p' \frac{f_{\tau'}(\vec{r}, \vec{p}')}{1 + (\vec{p} - \vec{p}')^2/\Lambda^2}$$

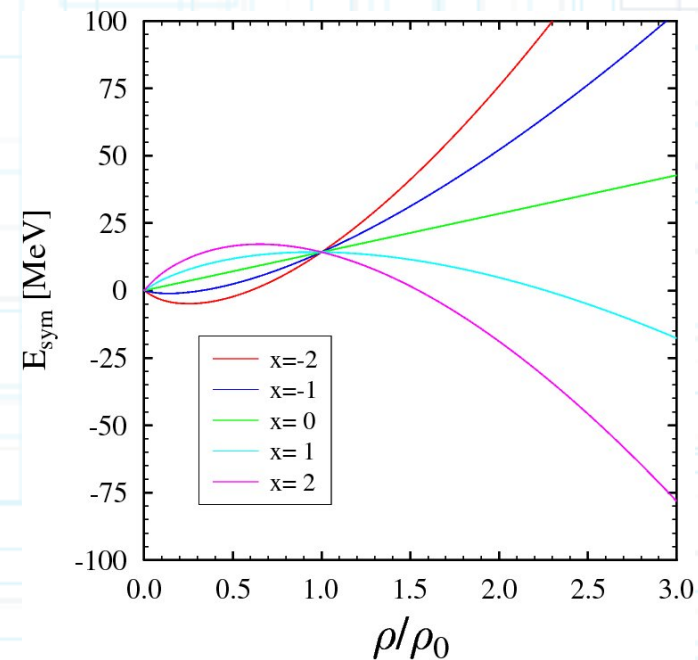
nucleons and resonances propagate in an isospin dependent mean field

$$U_{asym}(n^*) = U_{asym}(\Delta^0) = U_{asym}^n$$

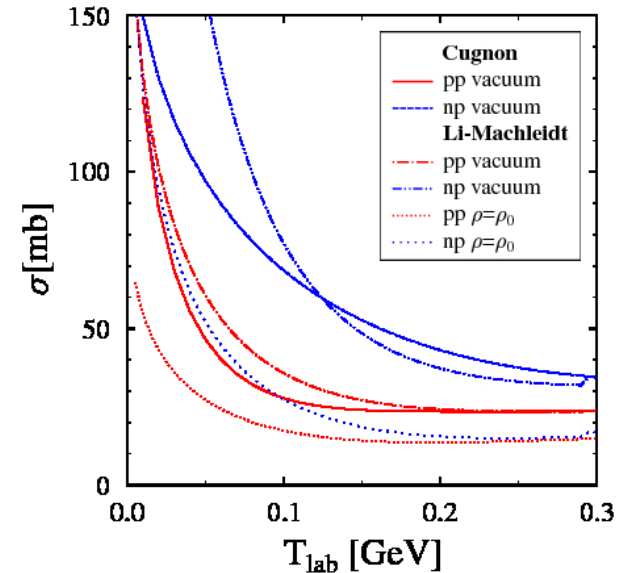
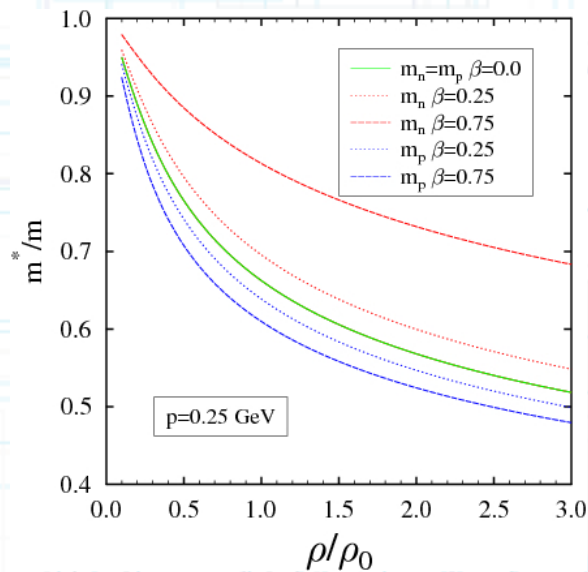
$$U_{asym}(p^*) = U_{asym}(\Delta^+) = U_{asym}^p$$

$$U_{asym}(\Delta^{++}) = 2U_{asym}^p - U_{asym}^n$$

$$U_{asym}(\Delta^-) = 2U_{asym}^n - U_{asym}^p$$



Isospin/Density Dep. Cross-Sections



Isospin asymmetry dependence of NN cross-sections

Li, Machleidt PRC 48, 1702 (1993)
Li, Machleidt PRC 49, 566 (1994)

$$\sigma_{NN}(\rho, \beta) = \sigma_{NN}(\rho, \beta = 0) \frac{m_1(\rho, \beta) m_2(\rho, \beta)}{m_1(\rho, \beta = 0) m_2(\rho, \beta = 0)}$$

Density/Isospin asymmetry dependence of NN cross-sections above pion production threshold

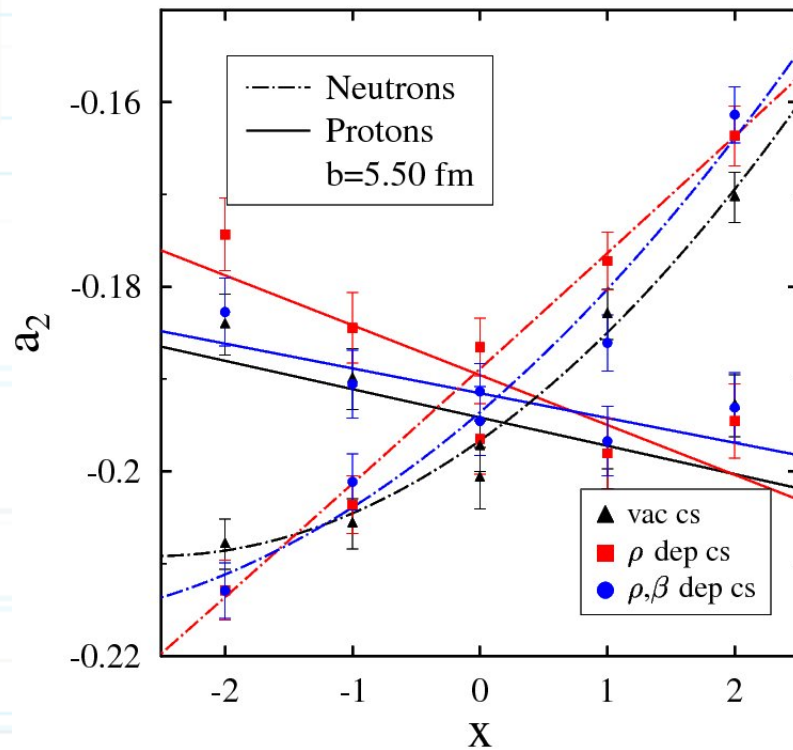
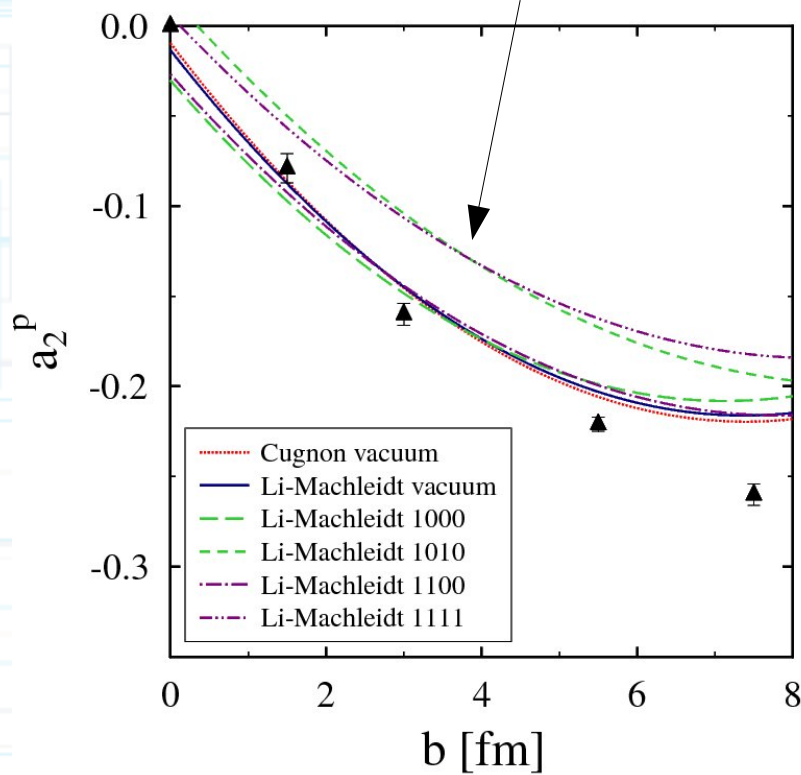
$$\sigma_{NN}(\rho, \beta) = \sigma_{NN}(\rho = 0, \beta = 0) \frac{m_1(\rho, \beta) m_2(\rho, \beta)}{m_N^2}$$

Elliptic Flow

$$\frac{dN}{d\phi} \sim 1 + a_1 \cos \phi + a_2 \cos 2\phi$$

$$a_2 = 2v_2$$

ρ, β dependence of cross-sections above pion production threshold **important !!!**



Experimental data (FOPI): A. Andronic et al. Nucl. Phys. A 679, 765 (2001)

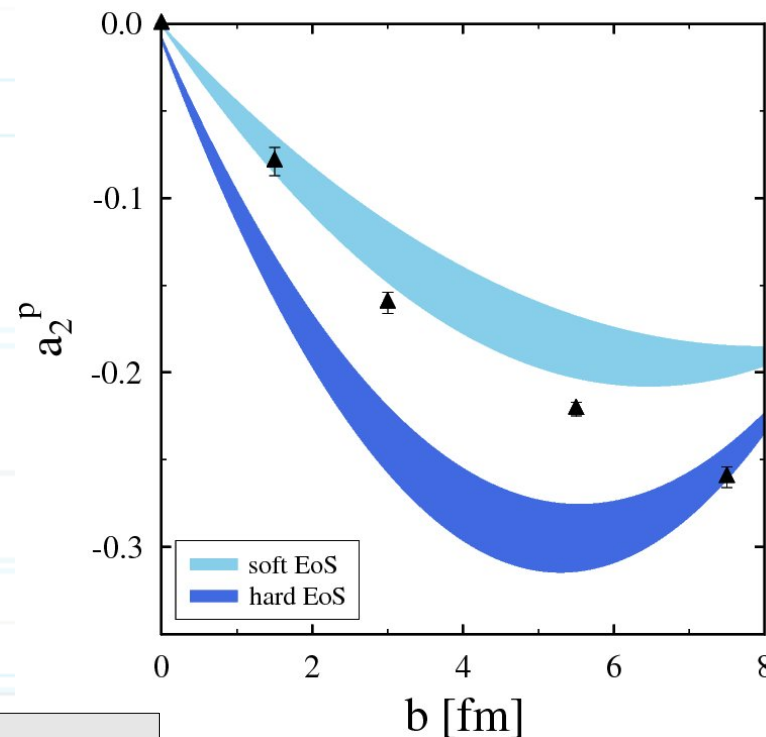
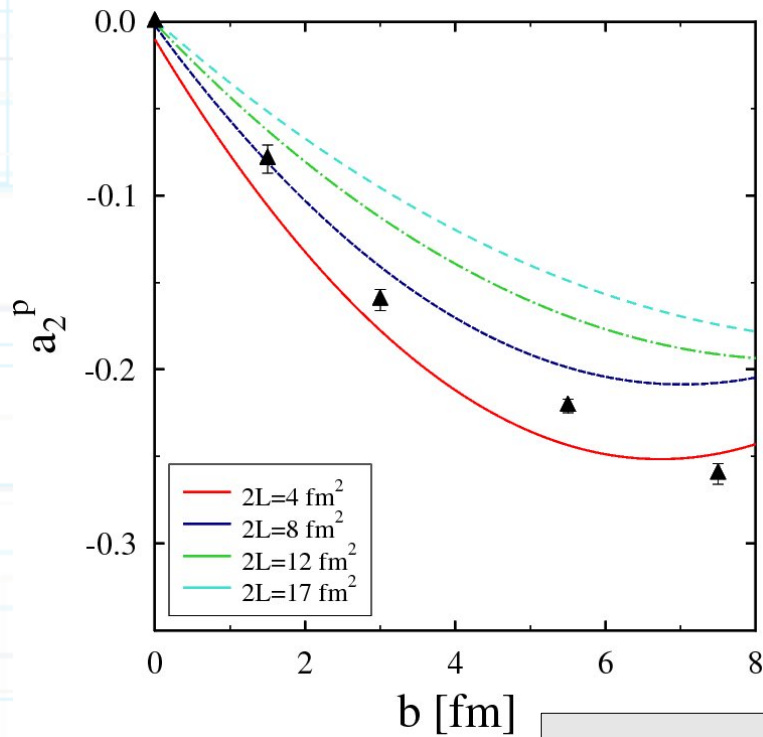
Model dependence of a_2^p

spread of the wave packet: L

$$\Psi(\vec{r}, \vec{p}, t) \sim \exp(-(\vec{x} - \vec{r})^2/L) \exp(i\vec{x} \vec{p})$$

$$f_i(\vec{r}, \vec{p}, t) \sim \exp(-(\vec{r} - \vec{r}_i)^2/2L) \exp(-(\vec{p} - \vec{p}_i)^2 L/2)$$

stability of heavy nuclei: $2L=8 \text{ fm}^2$
 C. Hartnack et al. Eur.Phys.J.A1,151 (1998)



stiffness of EoS

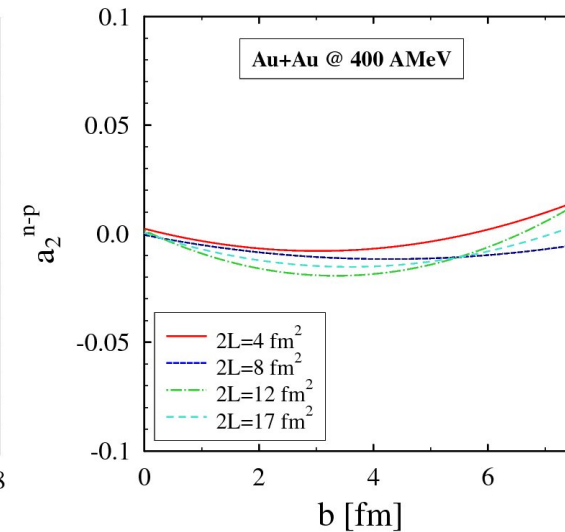
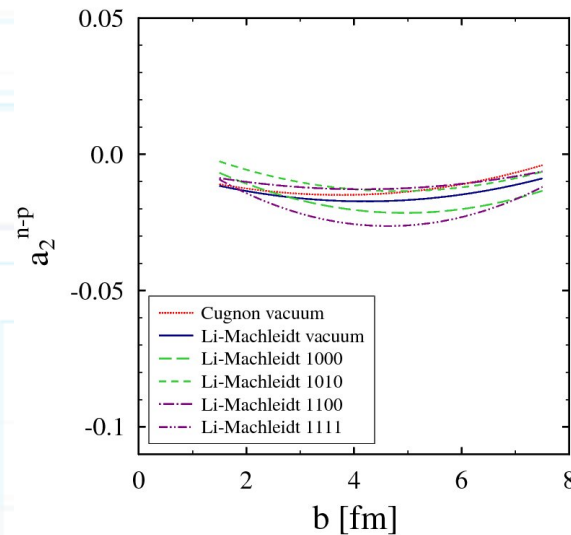
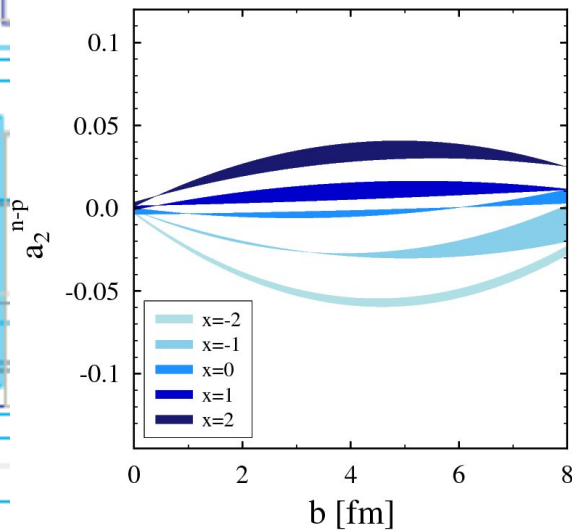
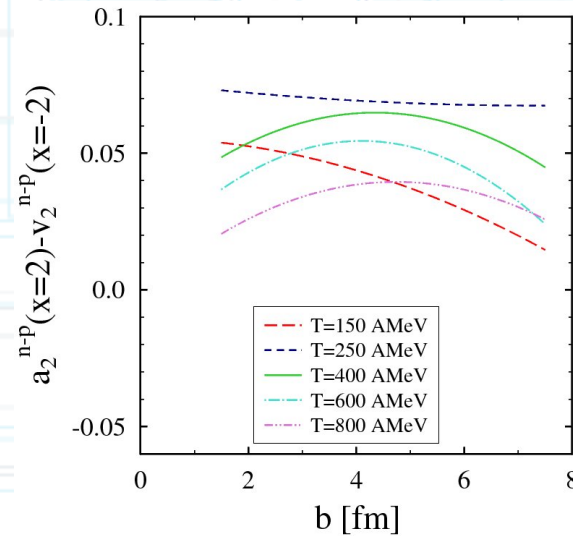
$$E(\rho) = E(\rho_0) + \frac{K}{18} \frac{(\rho - \rho_0)^2}{\rho_0^2}$$

$K=210 \text{ MeV}$ (soft) / 380 MeV (stiff)

Neutron-Proton EF difference

Mean field potential:

- 2,3 - body contact Skyrme
- + empiric momentum dependent part
(Hartnack & Aichelin, Phys. Rev. C 49, 2801 (1994))
- Gogny inspired isovector part
(C.B. Das et al., Phys. Rev. C 67, 034611-1 (2003))

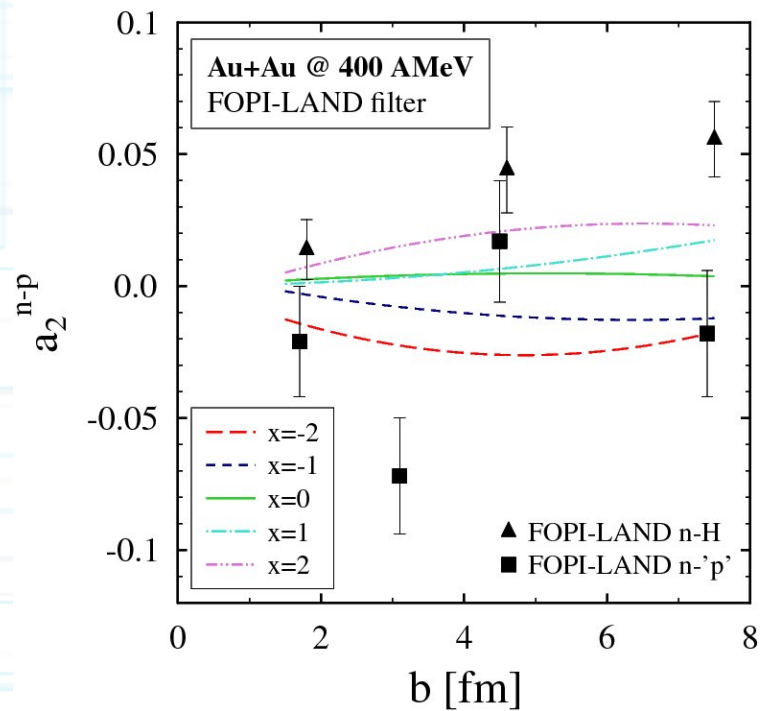


FOPI-LAND

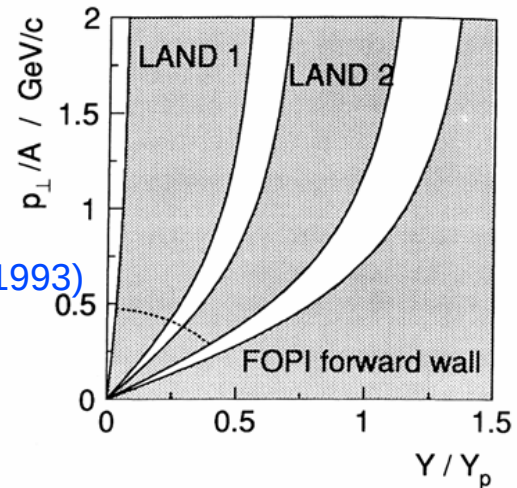
first detection of neutron squeeze-out

Y. Leifels et al. PRL 71, 963 (1993)

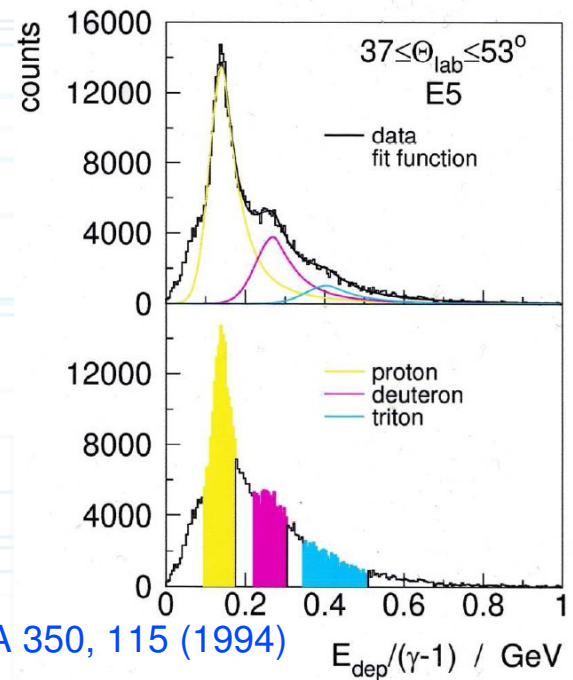
M.D. Cozma, PLB 700, 139 (2011)



D. Lambrecht et al., ZPA 350, 115 (1994)



400 A MeV Au+Au



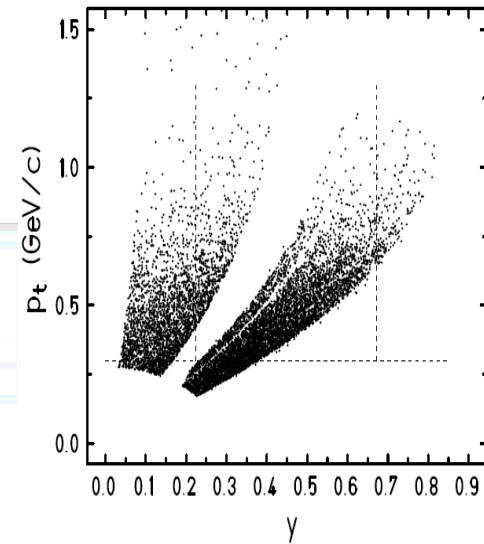
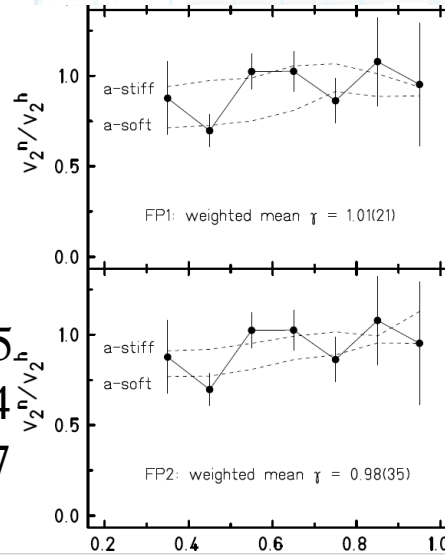
New FOPI-LAND data

P. Russotto et al. PLB 697, 471 (2011)

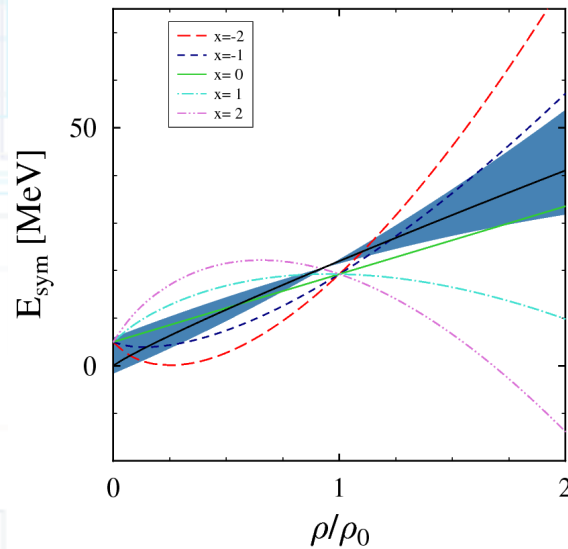
$$E_{\text{sym}} = 22(\rho/\rho_0)^\gamma + 12(\rho/\rho_0)^{2/3} \text{ MeV}$$

clustering algorithm – good
Z=1 reproduction

$$\begin{aligned} v_2^n/v_2^h & \quad \gamma = 1.01 \pm 0.21 / 0.98 \pm 0.35 \\ 5.5 < b < 7.5 & \quad \gamma = 0.58 \pm 0.27 / 0.35 \pm 0.44 \\ v_2^n/v_2^p & \quad \gamma = 0.99 \pm 0.28 / 0.85 \pm 0.47 \end{aligned}$$

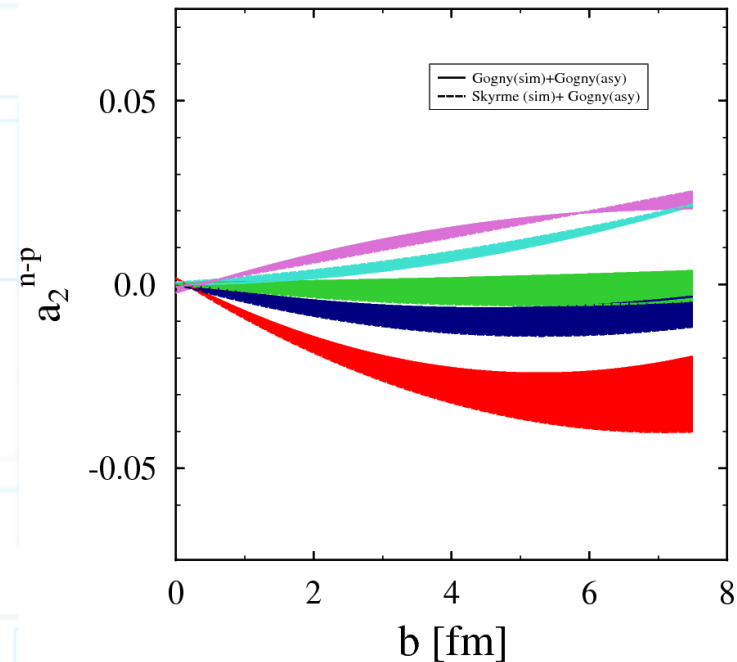
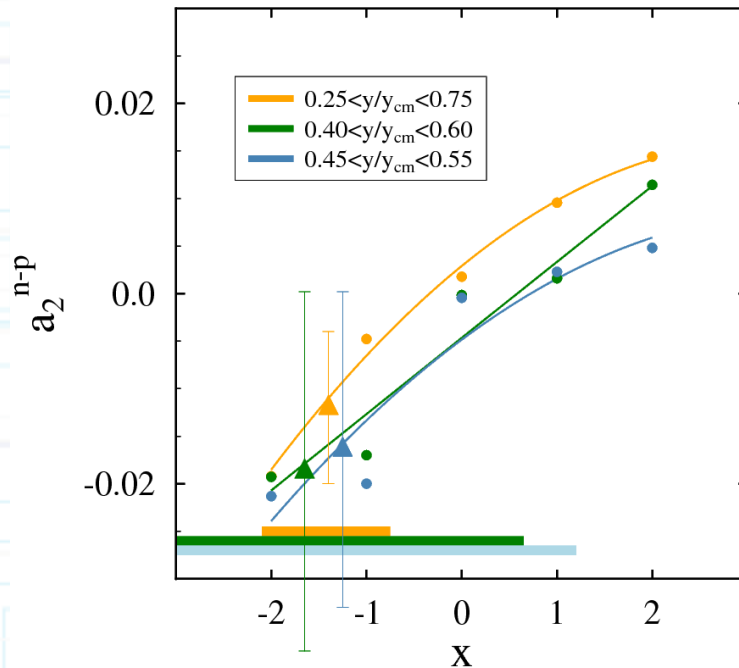


$$\gamma = 0.9 \pm 0.4$$



New FOPI-LAND data

experimental data: FOPI-LAND preliminary (W. Trautmann et al.)



see also [L.Zhang et.al nucl-th 12031724](#)

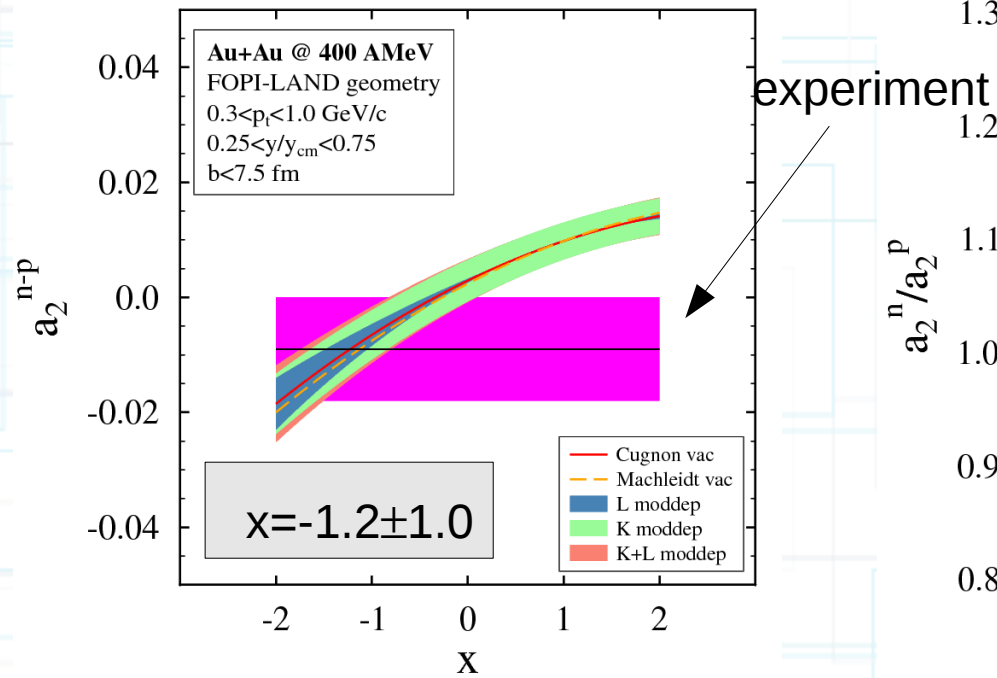
rather **poor reproduction** of **new FOPI-LAND** a_2^n and a_2^p values

extra model dependence ? (momentum dependent part of symmetric EoS)

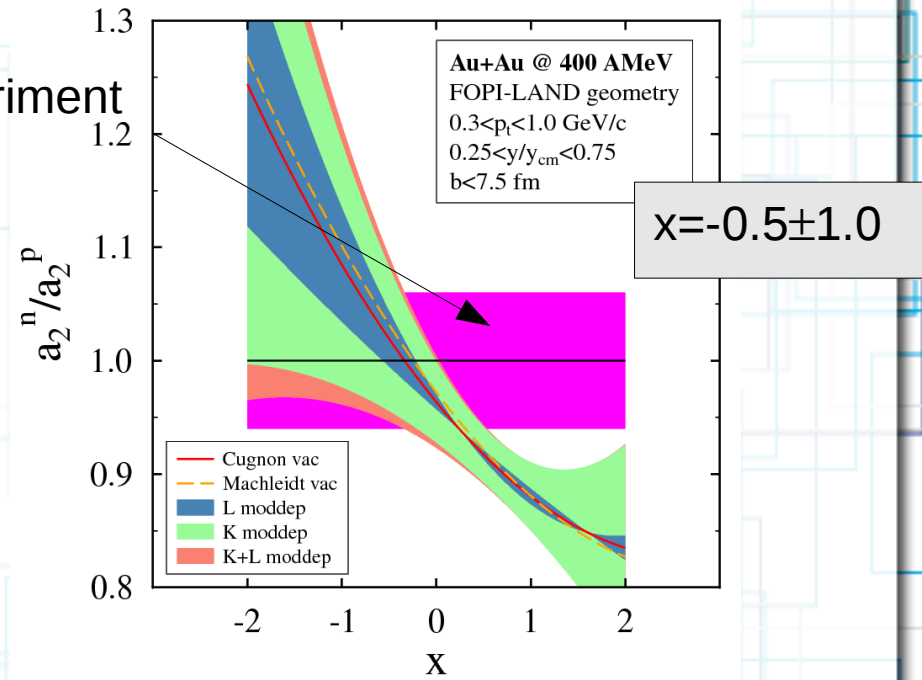
some differences between old/new FOPI LAND data sets

EF ratios vs. differences

flow difference



flow ratio



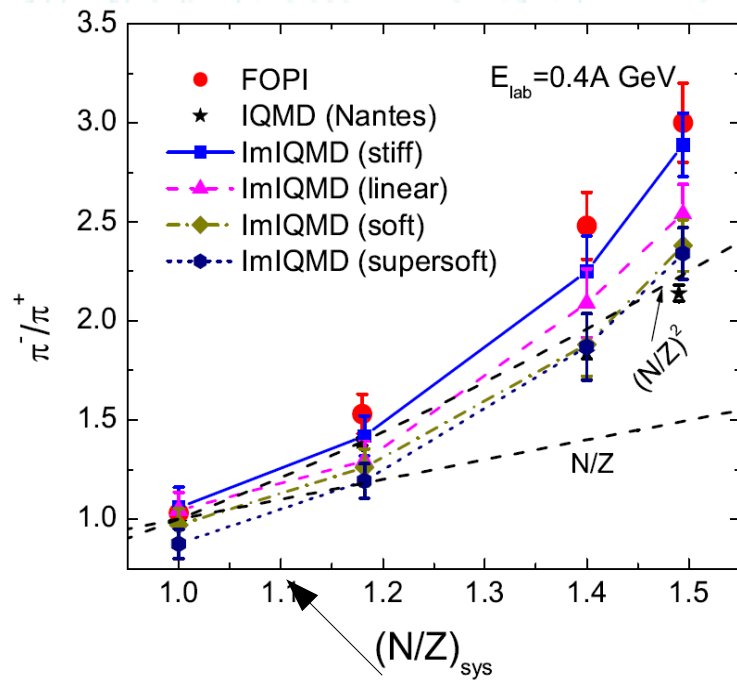
experimental data: FOPI-LAND preliminary (W. Trautmann et al.)

Constraints from other observables

$$\pi^-/\pi^+ = (5N^2 + NZ) / (5Z^2 + NZ)$$

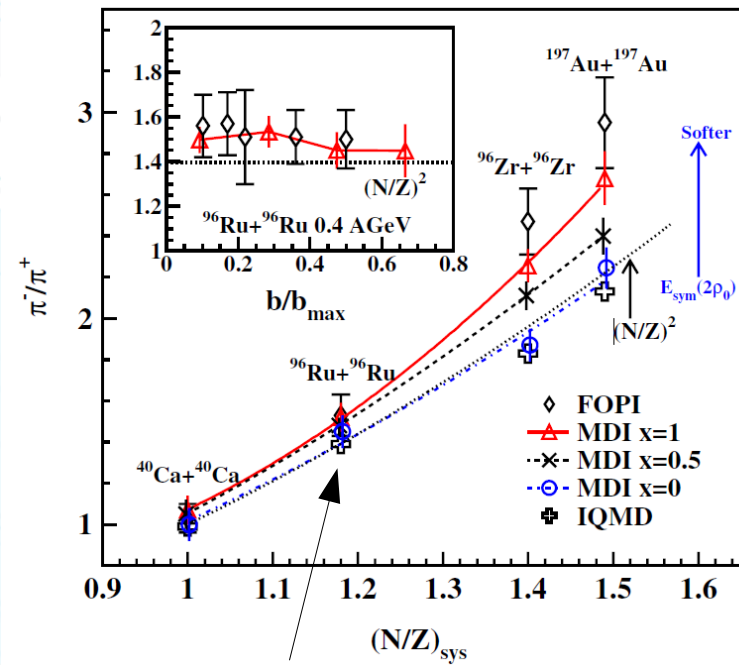
Z.-Q. Feng et al., PLB 683, 140, (2010)

Z. Xiao et al. PRL 102,062502, (2009)



IQMD

$$S(u) = S_0 u^\gamma$$



IBUU

Gogny force

Summary & Outlook

symmetry energy – important for describing astrophysical related phenomena/quantities

CAN be constrained at suprasaturation densities - heavy-ion related observables

elliptic flow observables – suppressed dependence to certain model parameters (K, L, cs)

some model dependence still present – differences vs ratios

OUTLOOK:

- study left over model dependence
- mitigate differences w.r.t other observables (pion ratios)
- how about light mass fragments?

$$x = -0.8 \pm 0.5$$

