

Strange quark matter nucleation and Neutron stars — Quark stars coexistence

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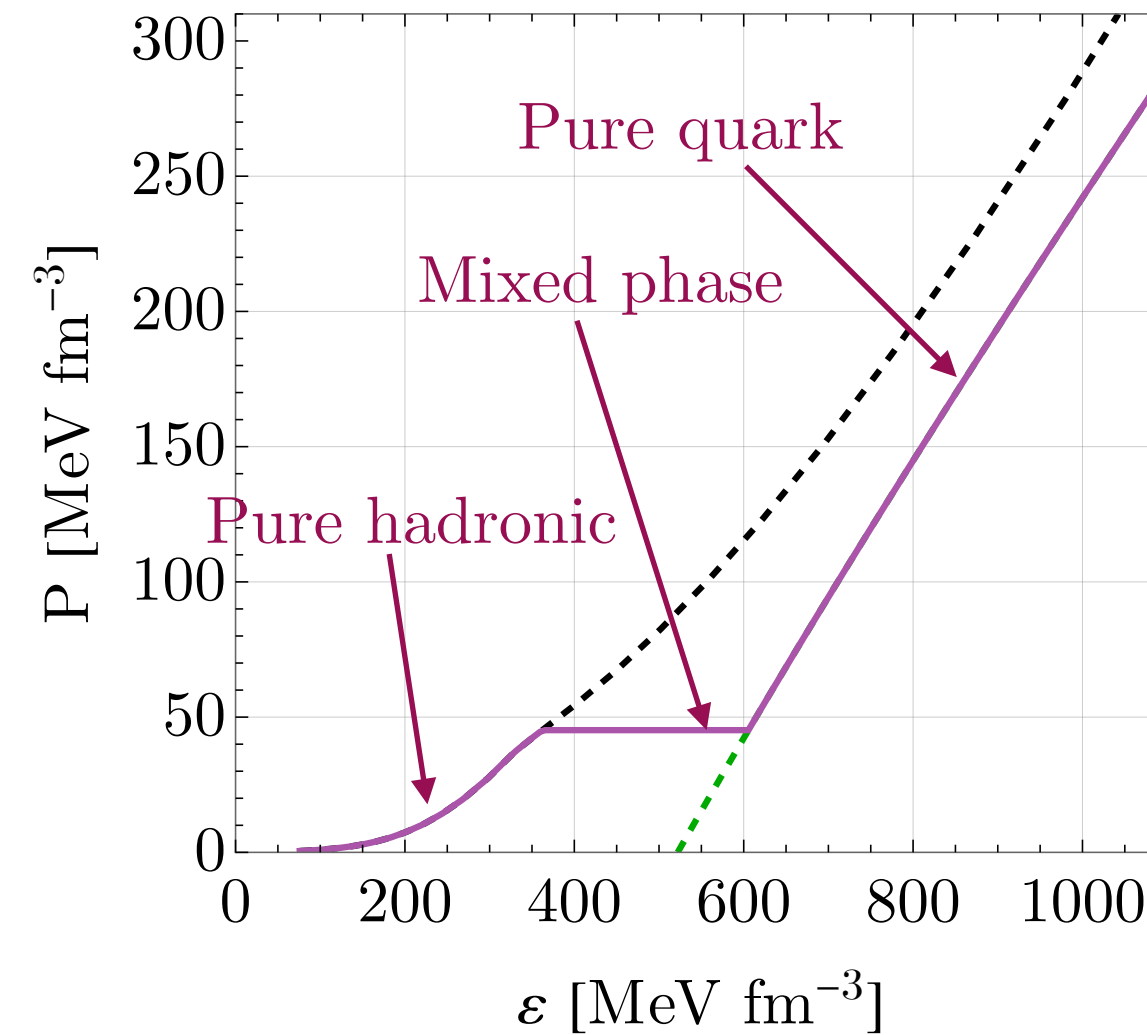
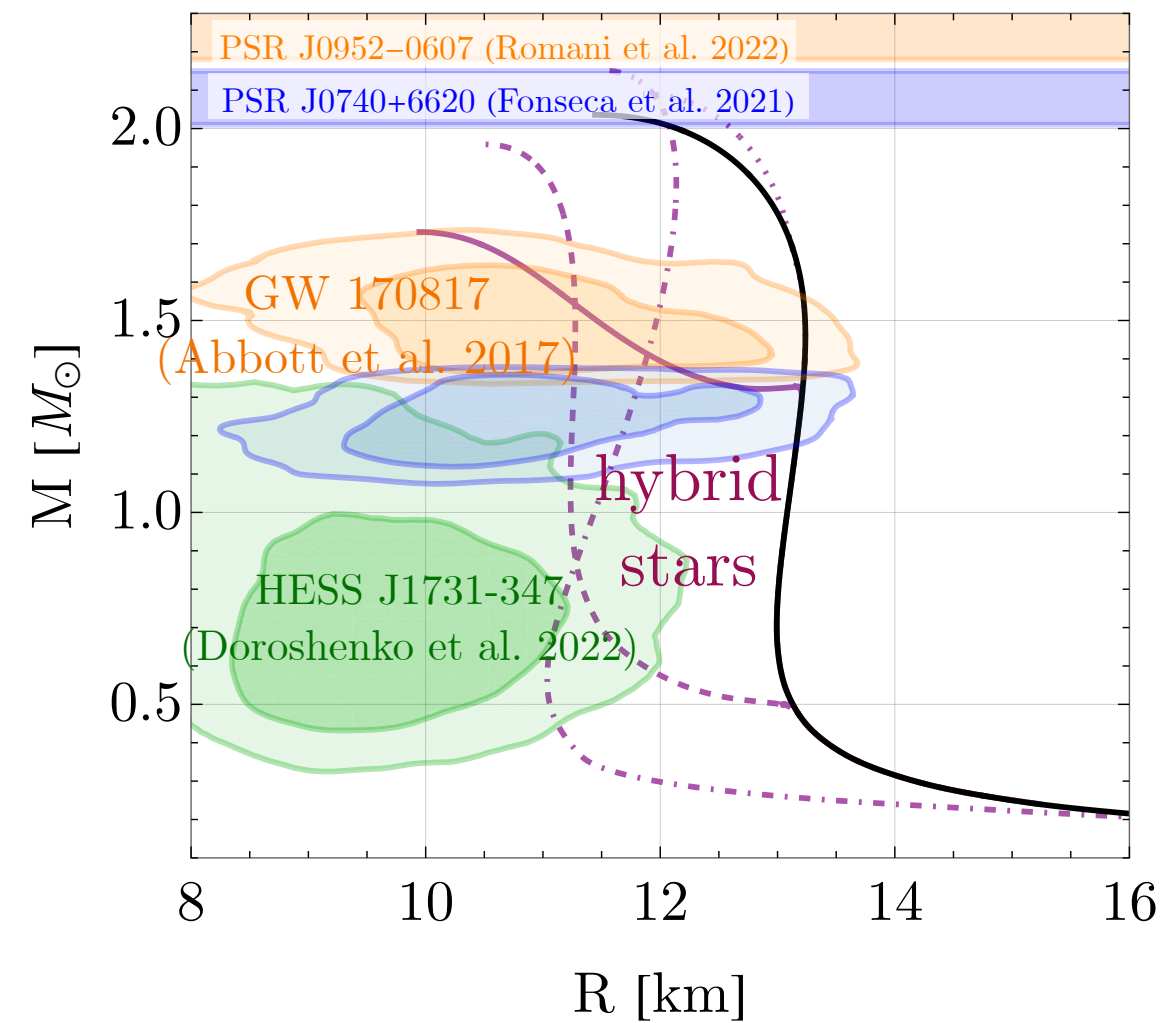


**Università
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**TNPI2025 - XX Conference on Theoretical
Nuclear Physics in Italy**



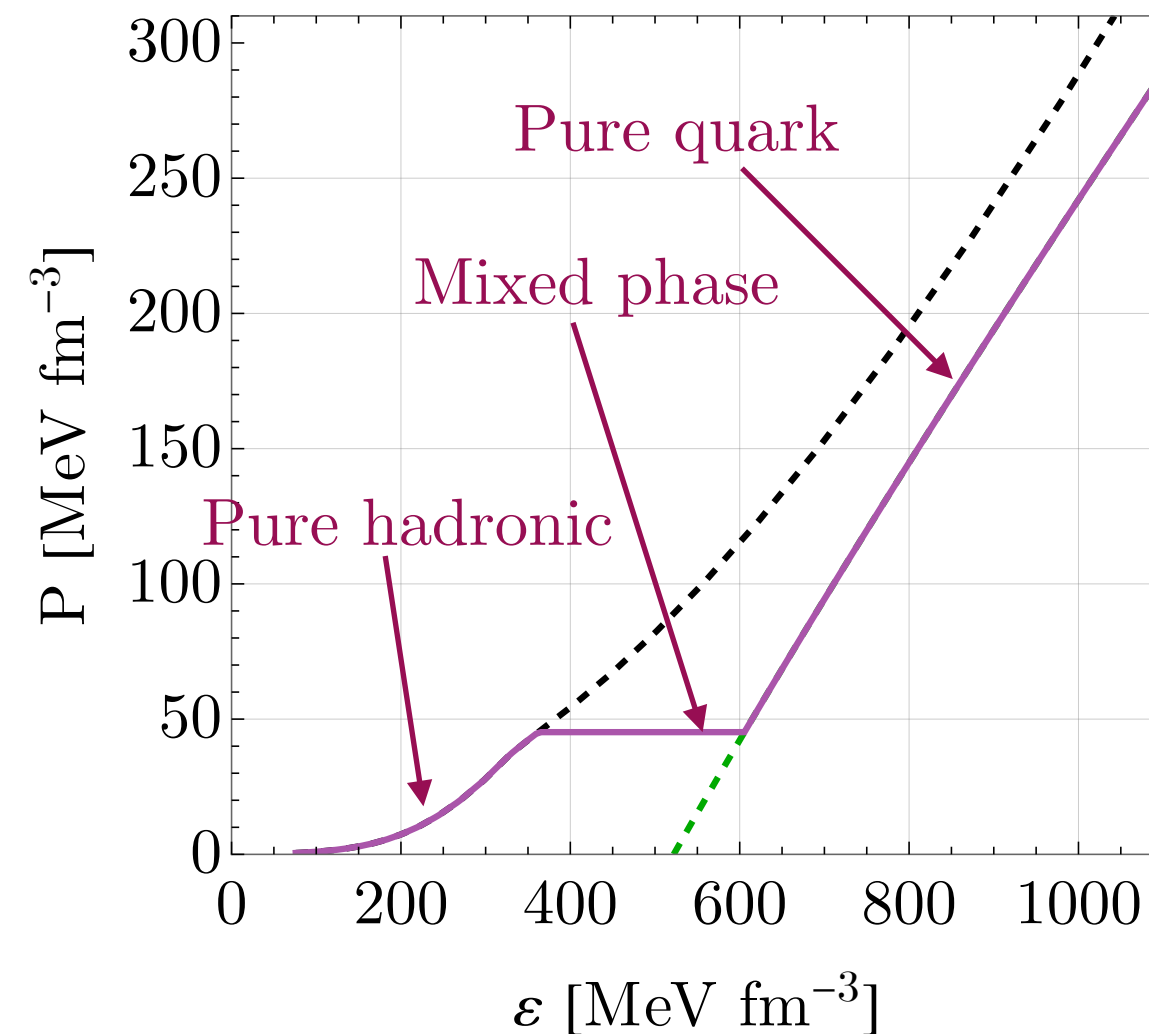
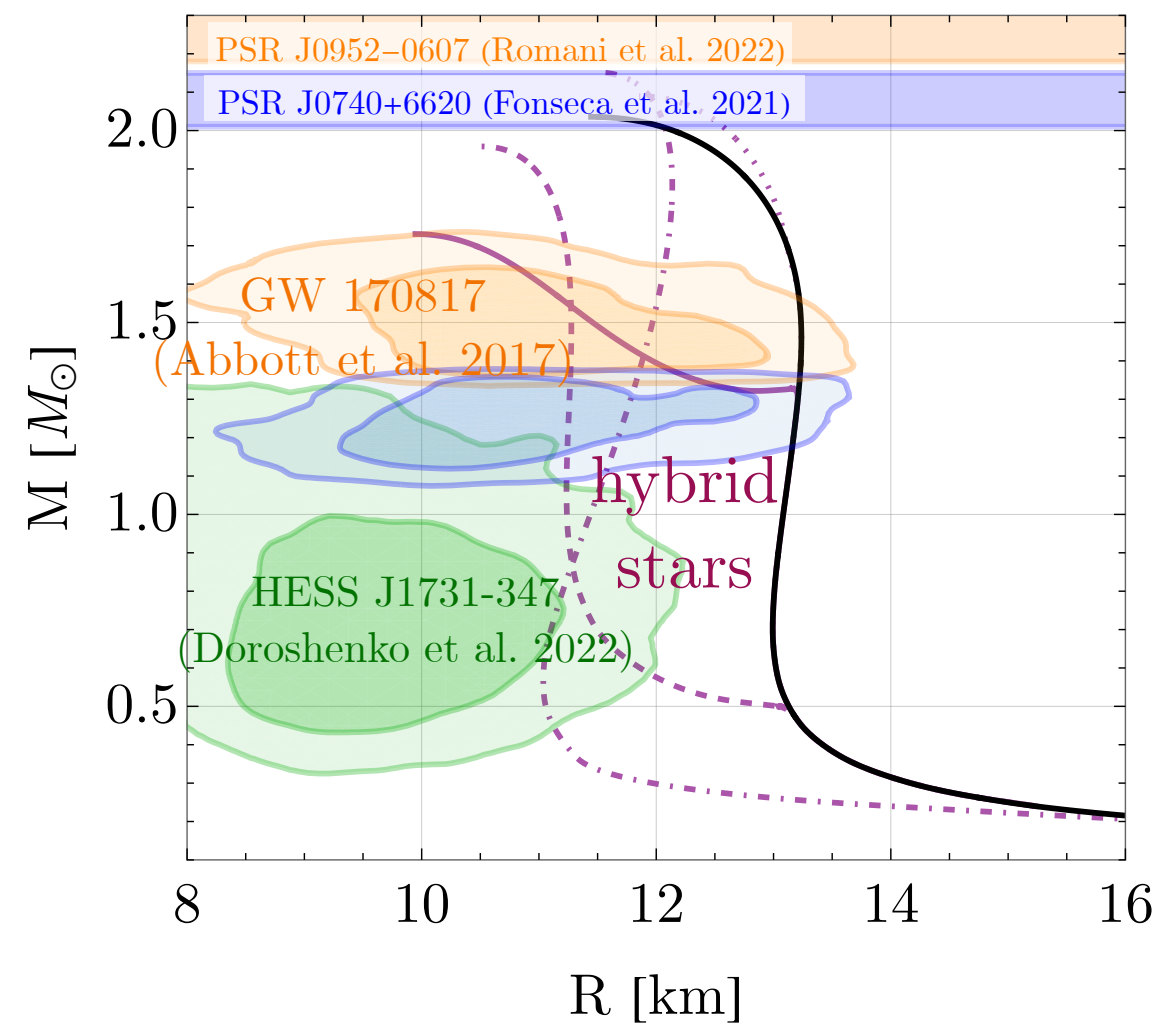
SQM in compact stars: one or two families?



One family scenario

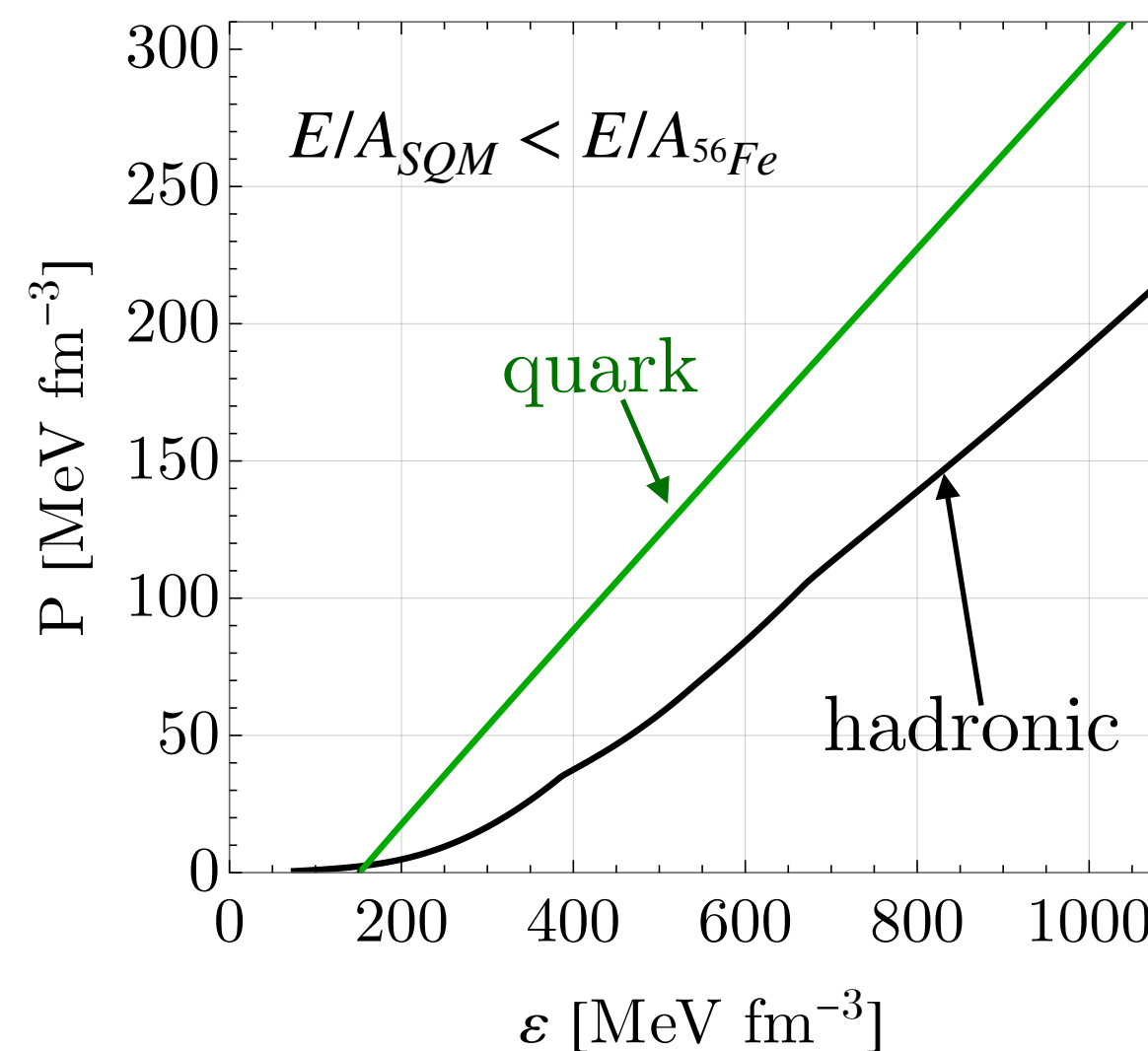
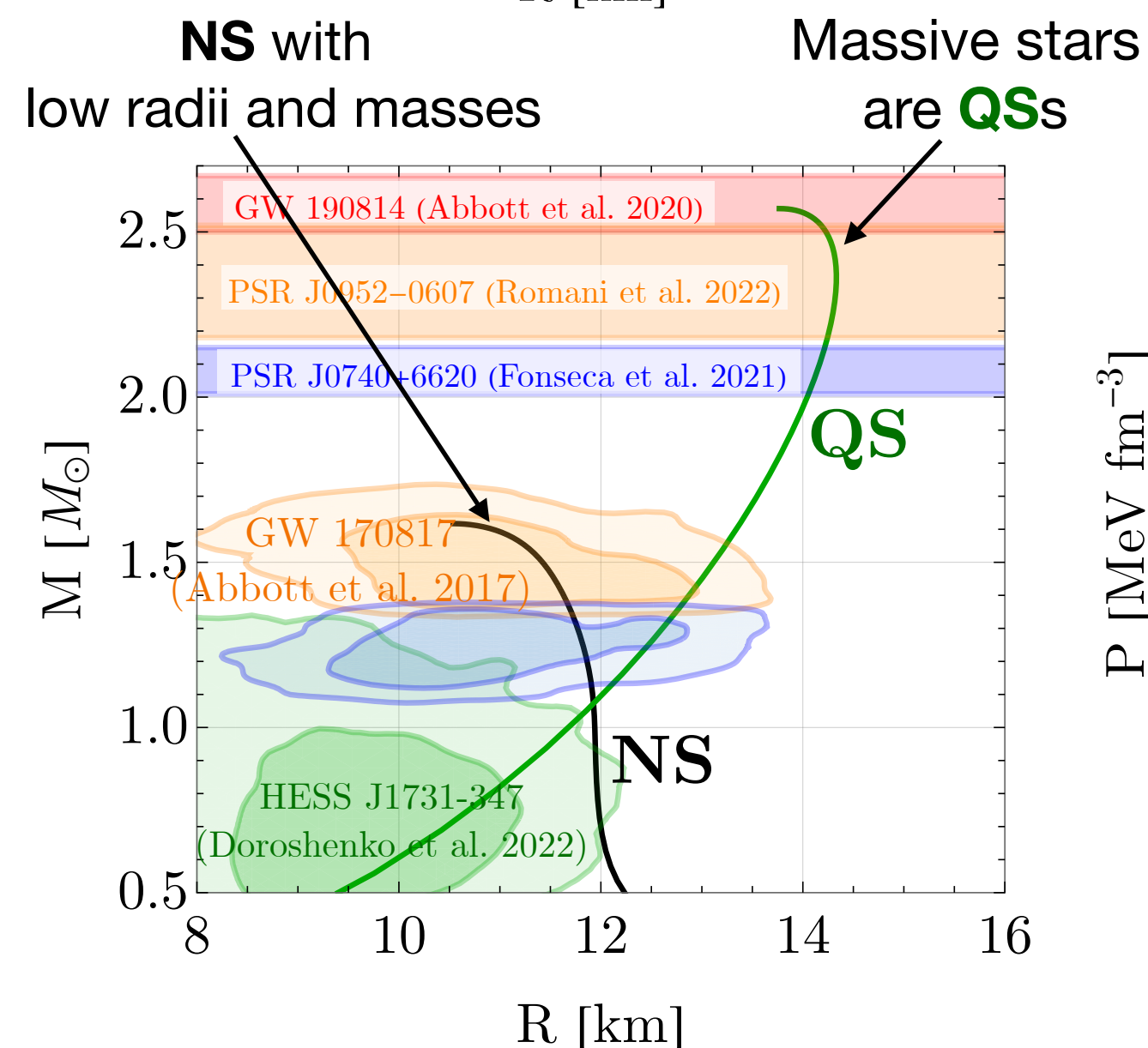
- Quarks d.o.f. expected in massive compact stars
- **Hybrid stars**: SQM in the core and hadrons in the outer part
- 1st order phase transition, crossover, quarkyonic, ...

SQM in compact stars: one or two families?



One family scenario

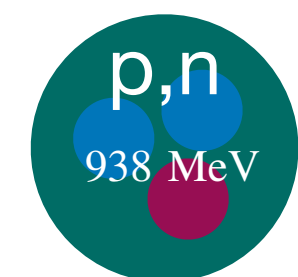
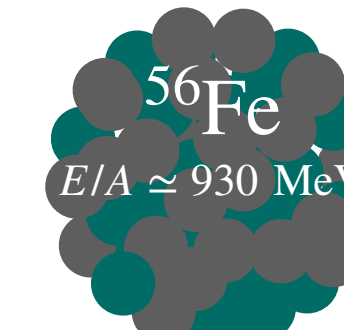
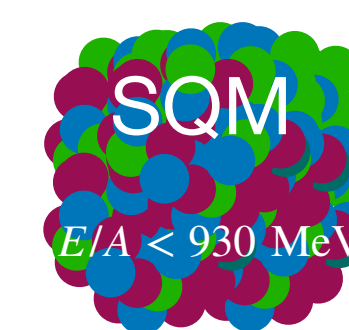
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Two families scenario

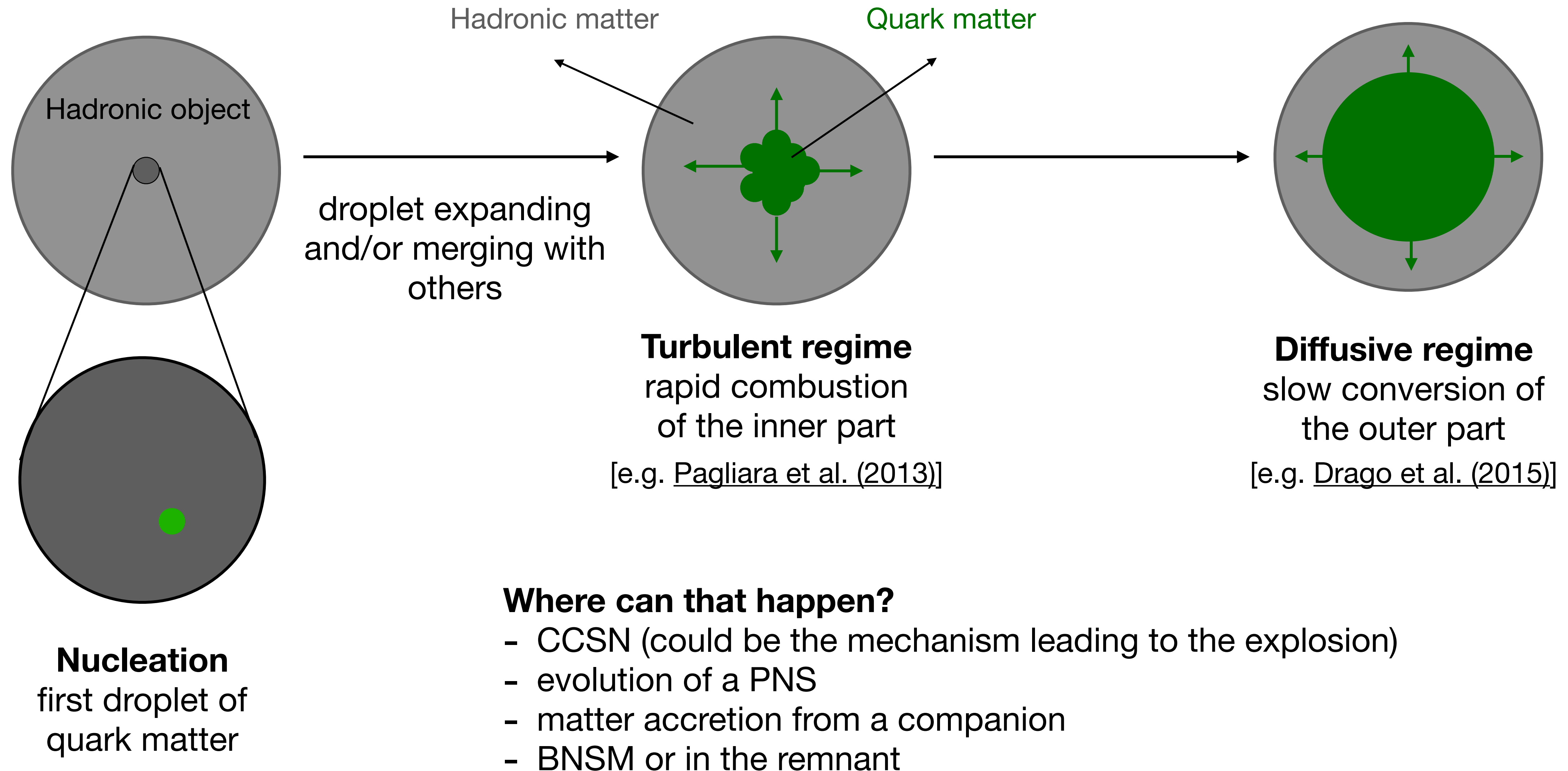
[see e.g. *Drago et al. (2016)*]

- Based on the **strange matter hypothesis** [*Witten (1984)*]

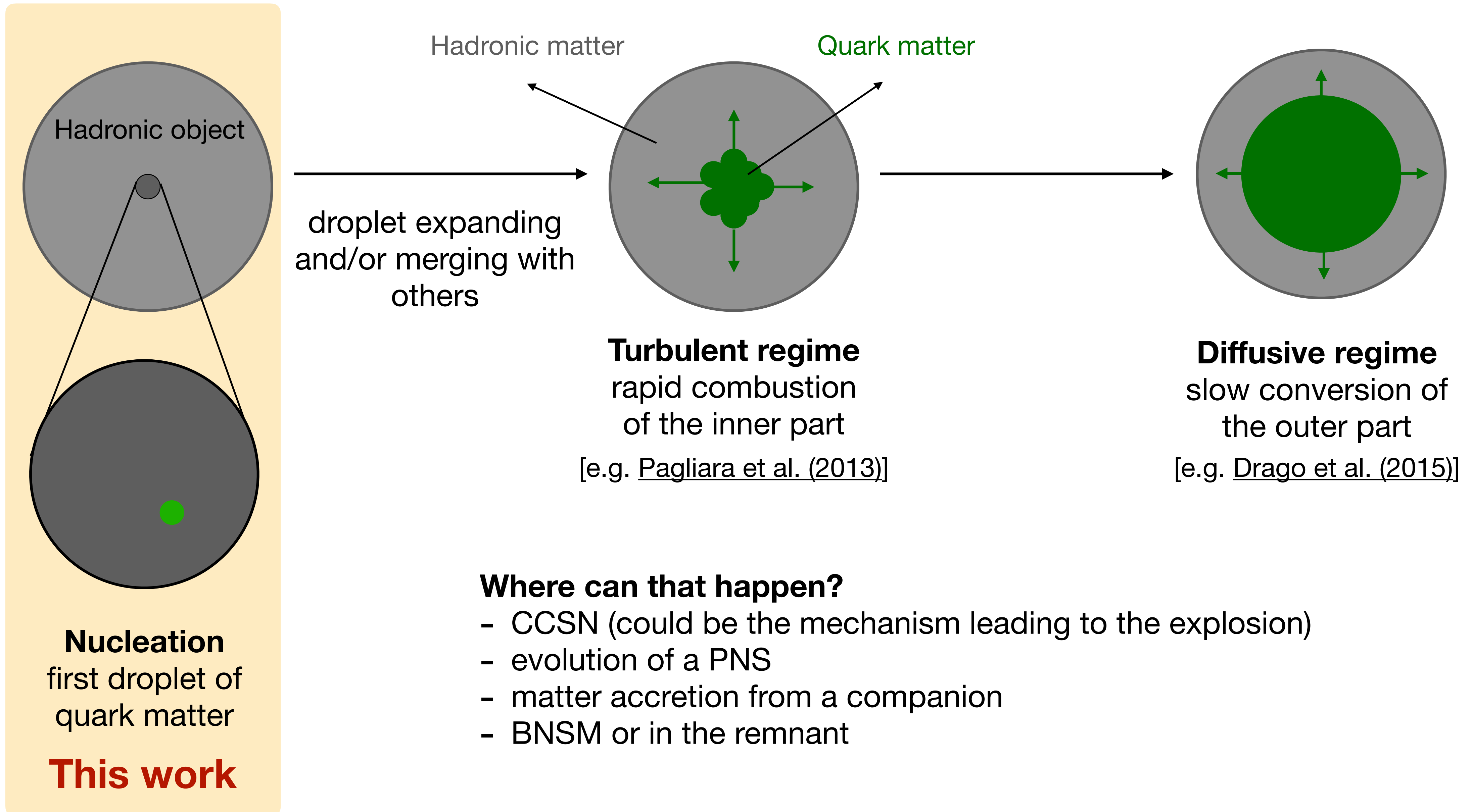


- Quark stars (QSs)** and **Neutron stars (NSs)** coexists
- Once reached deconfinement conditions, **NS** converts to **QS**

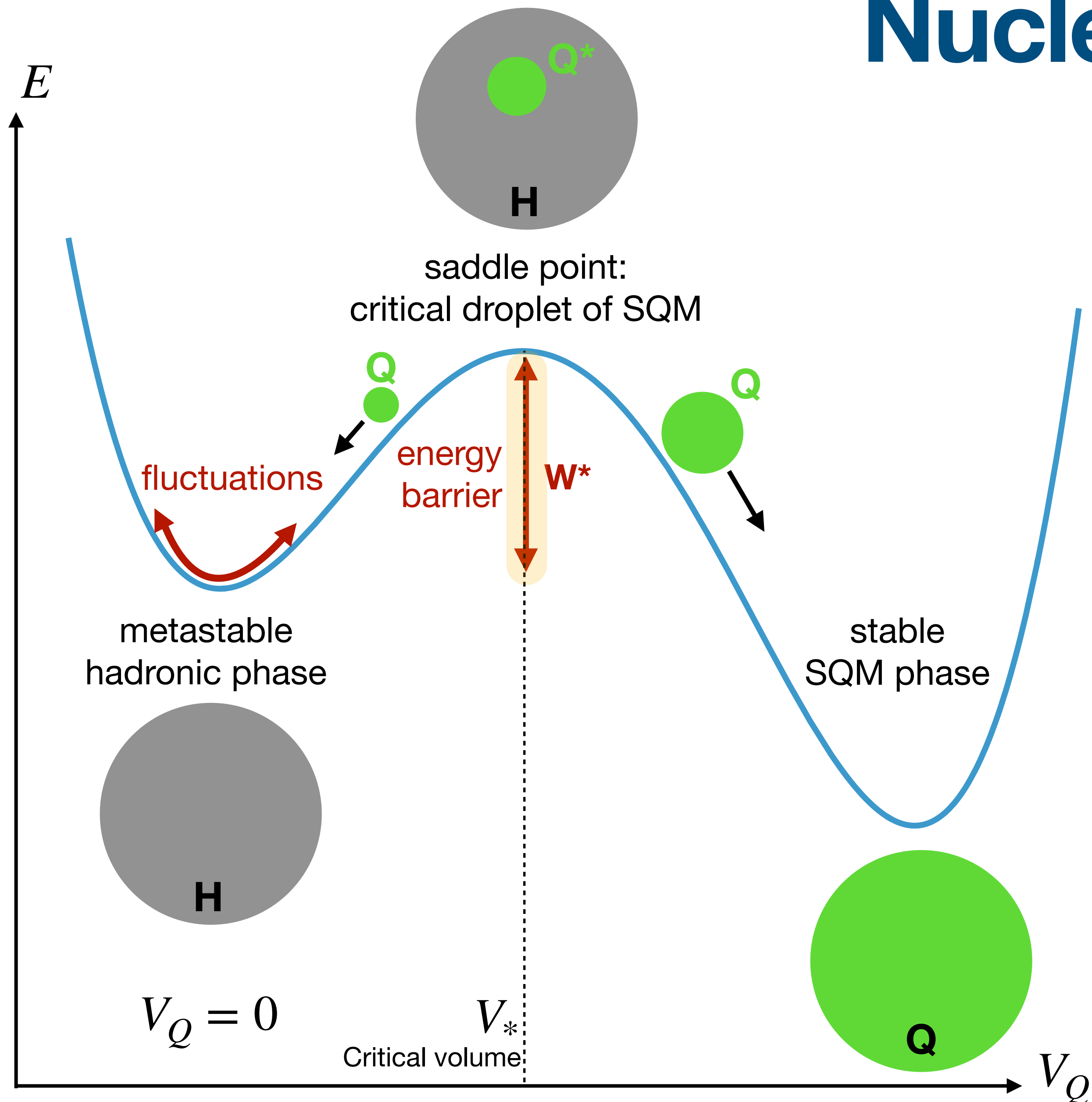
Conversion into a Quark Star



Conversion into a Quark Star



Nucleation



1st order phase transition $\Rightarrow$ surface tension

Small droplets are disfavoured

energy barrier

$$W = \underbrace{-\frac{4}{3}\pi R^3(P_{Q^*} - P_H)}_{\text{bulk energy gain (negative if H is metastable)}} + \underbrace{4\pi\sigma R^2}_{\text{surface effect (always positive)}}$$

Thermal nucleation [*Langer (1969)*]

$$\Gamma \propto e^{-\frac{W}{T}}$$

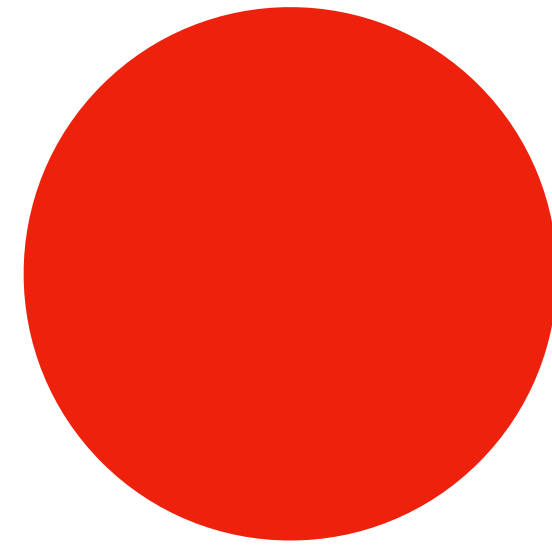
Distribution probability of a **droplet** with $R \leq R_*$ at given conditions

Quantum nucleation [*Iida (1997)*]

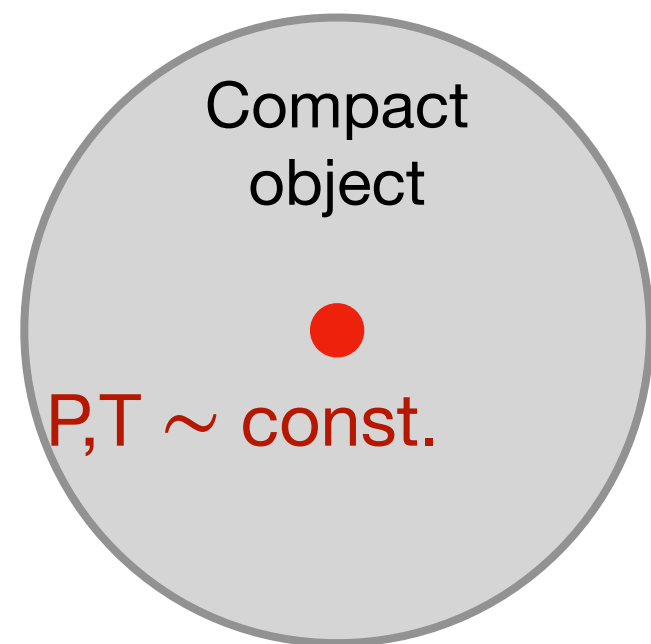
$$\Gamma \propto e^{-\frac{A(W)}{\hbar}}$$

Flavor composition can fluctuate

$$Y_i^* = \langle Y_i^H \rangle \text{ everywhere}$$



no fluctuations
of the composition

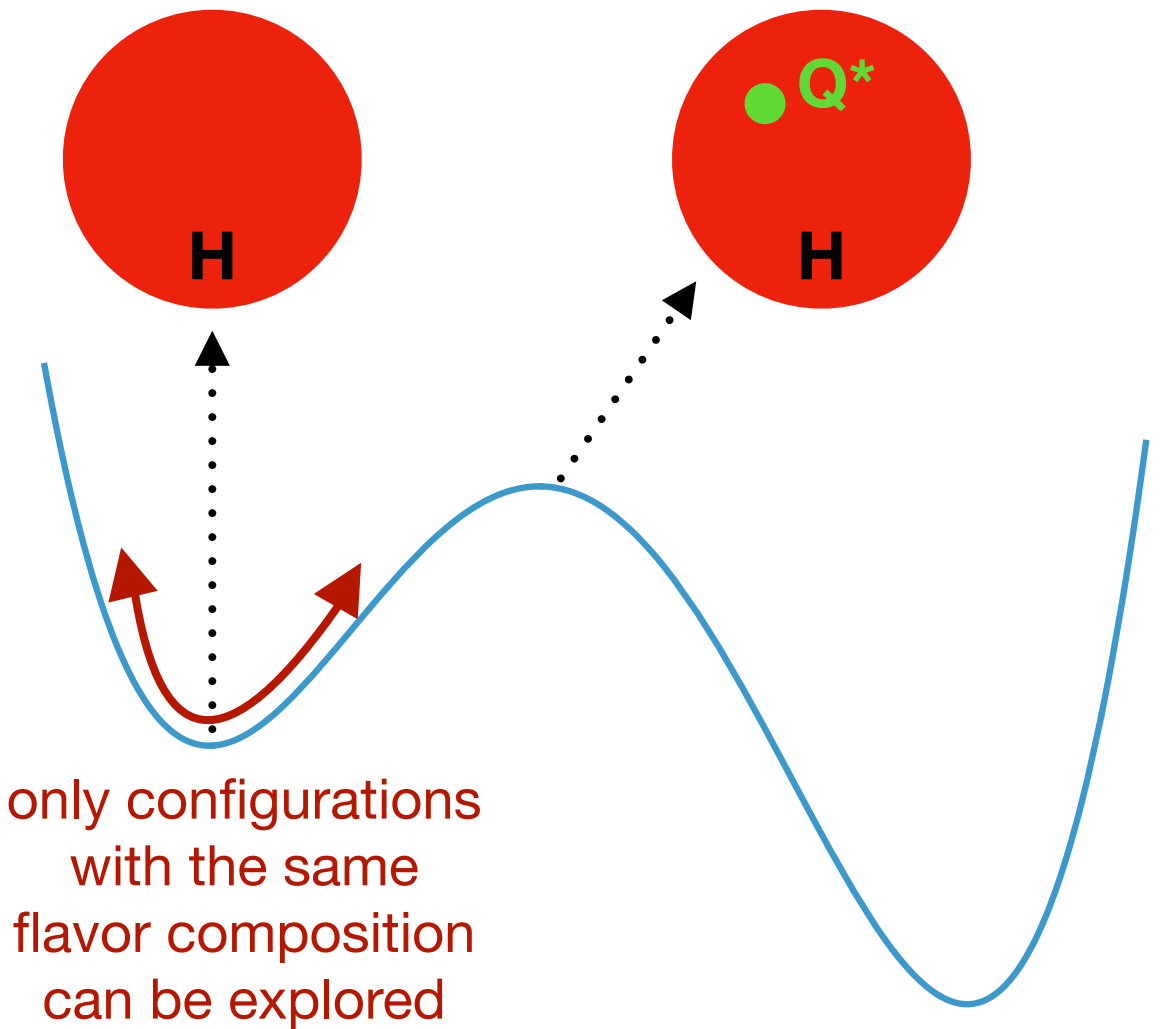


Which configurations can the system explore?

Nucleation is due to **strong interactions**
strong timescale $\ll$ weak timescale

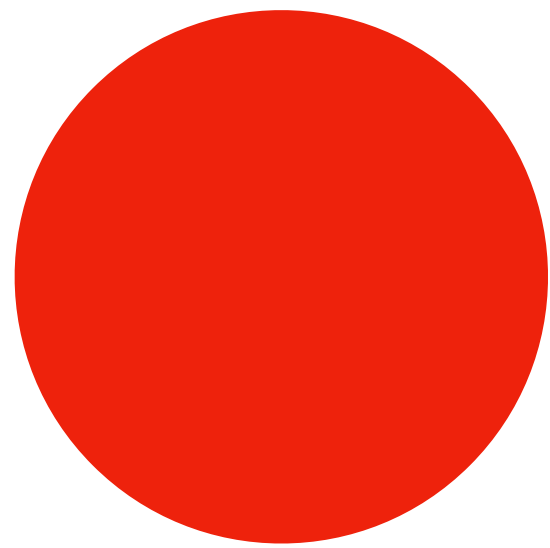
↓
Conserved flavors
...locally?

$$\{Y_i^{Q*}\} = \{Y_i^*\}$$

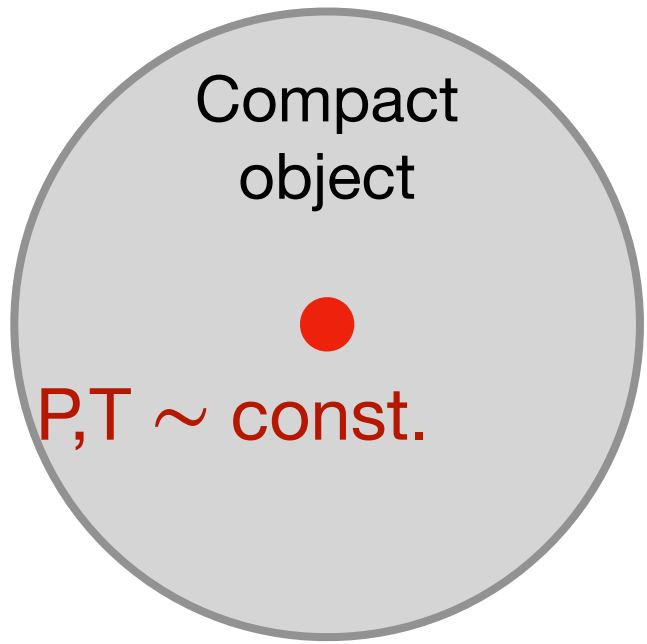


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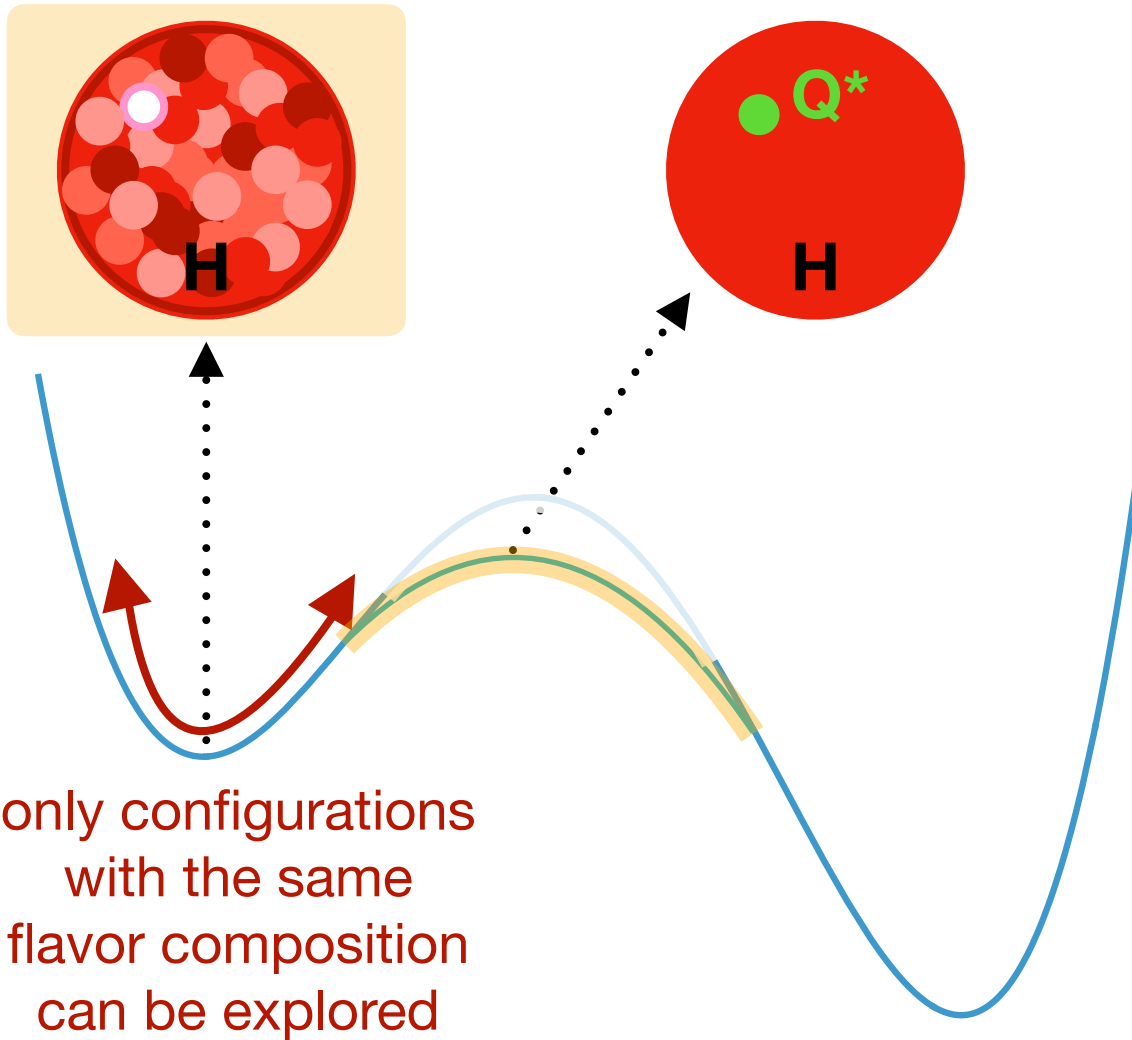


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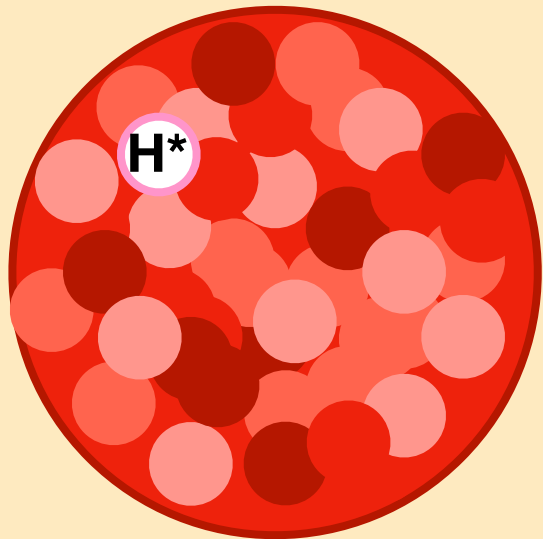
↓
Conserved flavors
...locally?

$$\{Y_i^{Q*}\} = \{Y_i^*\}$$



[Guerrini et al. (2024)]

locally $Y_i^* \neq \langle Y_i^H \rangle$



thermal fluctuations
of the composition

Key idea:

at $T \neq 0$ the hadronic **composition fluctuates** around the average values $\langle Y_i^H \rangle$
the nucleation is a **local process**

↓
Nucleation could happen in a subsystem H^* in which
the local composition $Y_i^* \neq \langle Y_i^H \rangle$ makes nucleation easier

$$\Gamma \propto \underbrace{\exp \left[-\frac{W_{H \rightarrow H^*}}{T} \right]}_{\text{probability of a subsystem } H^*} \underbrace{\exp \left[-\frac{W_{H^* \rightarrow Q^*}}{T} \right]}_{\text{nucleation probability in a subsystem } H^*}$$

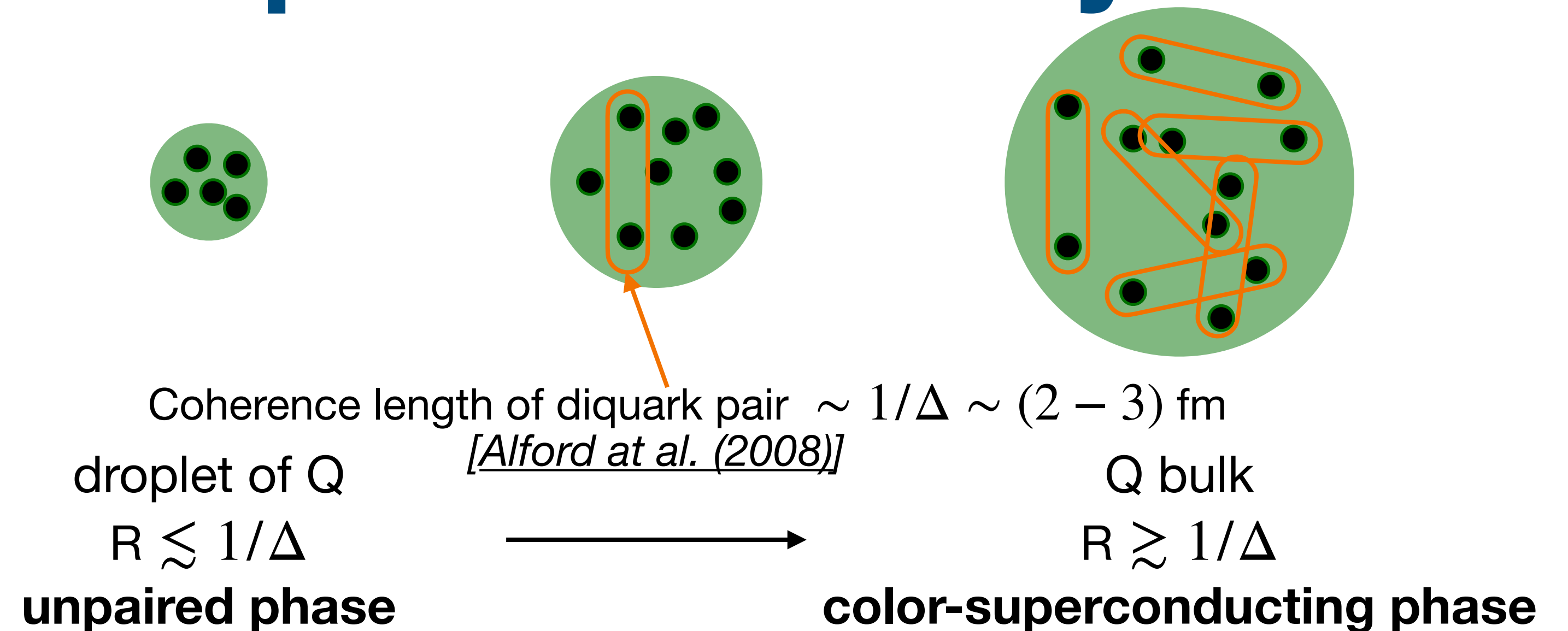
Role of color-superconductivity

- to reach $\sim (2.2 - 2.5) M_{\odot}$ we need **superconducting** quark matter (e.g. **CFL**)

[e.g. *Bombaci et al. (2021)*, *Blaschke et al. (2023)*]

- gaps could **vanish** in very **small systems** (as critical quark droplet is)

[e.g. *Amore et al. (2002) PRD*]



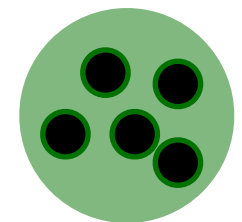
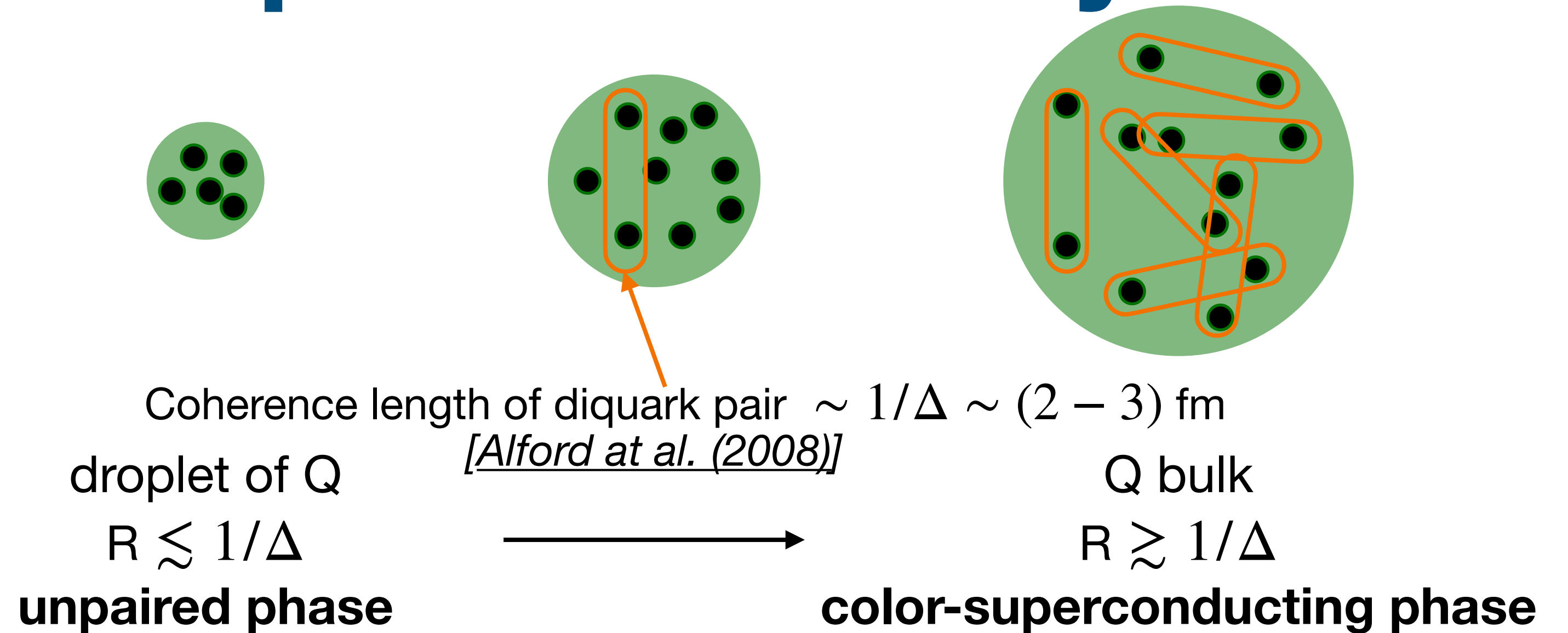
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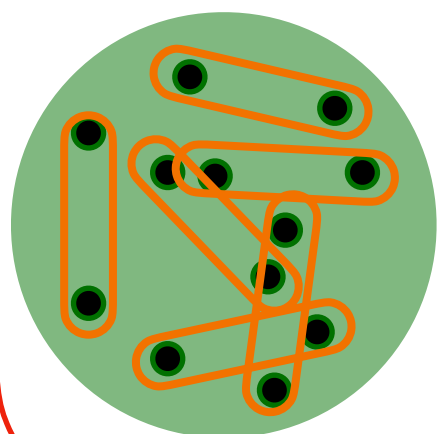
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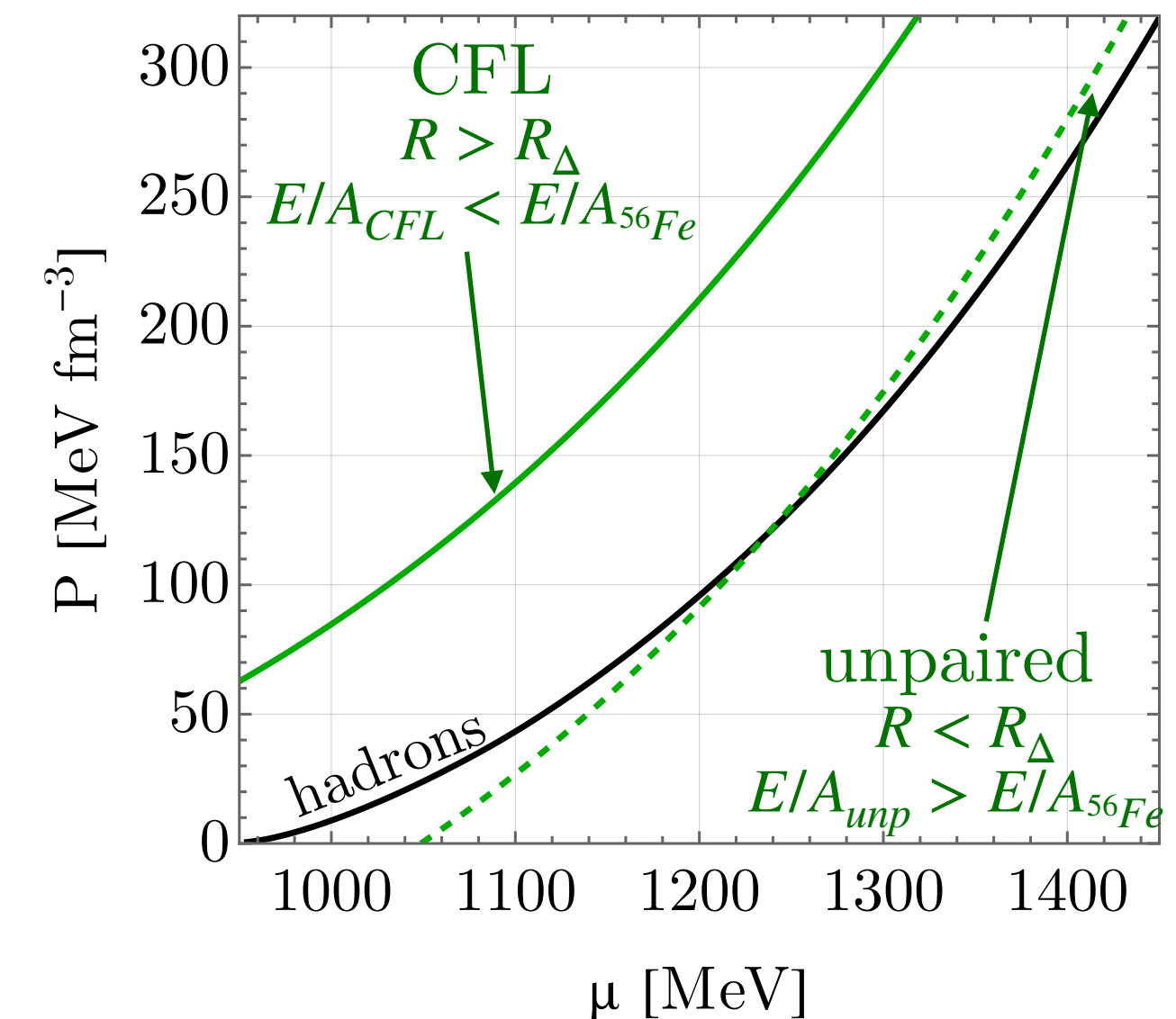
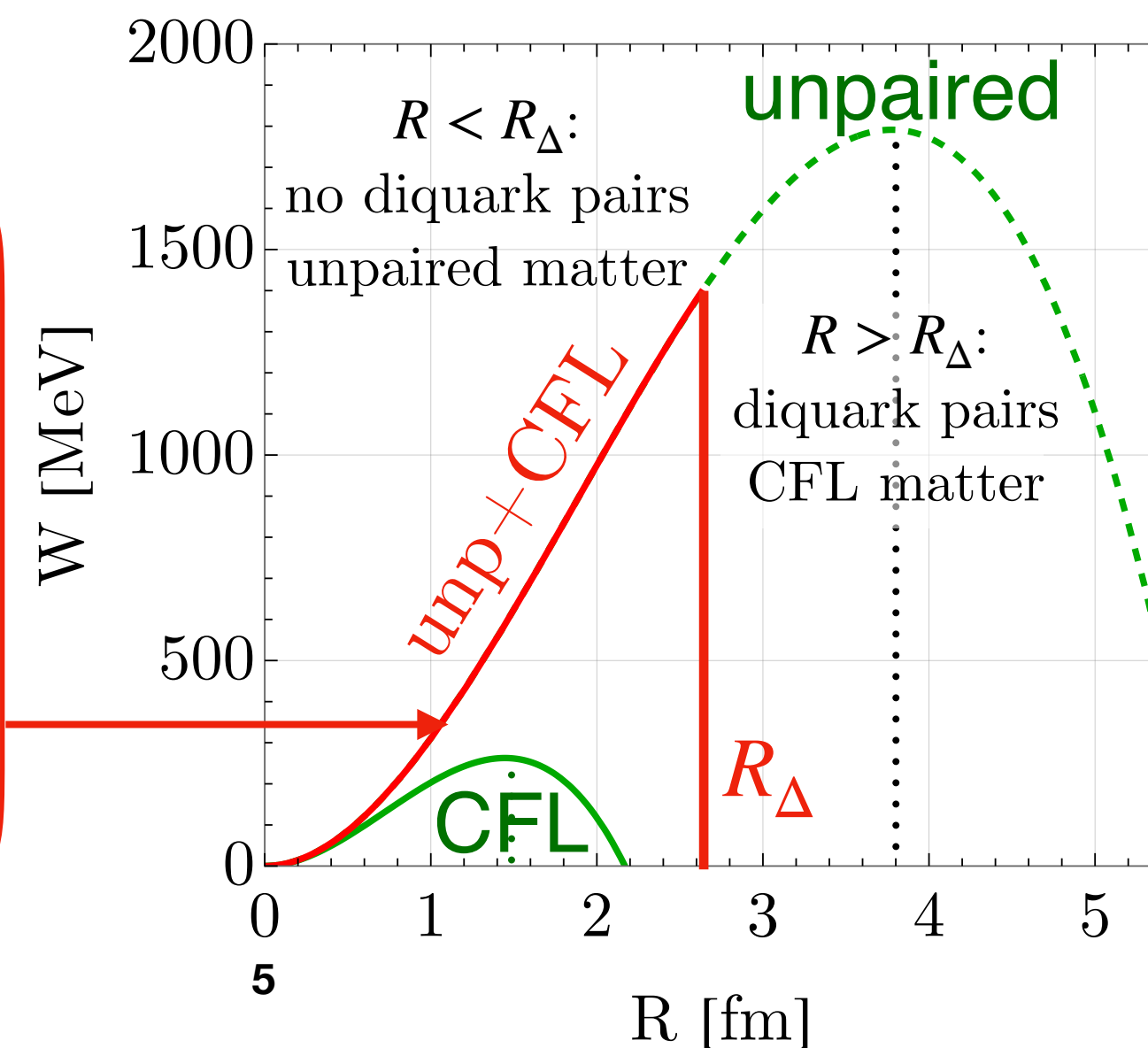
[e.g. *Amore et al. (2002) PRD*]



$R < R_{\Delta} = 1/\Delta(T)$: **unpaired matter**
non absolutely stable



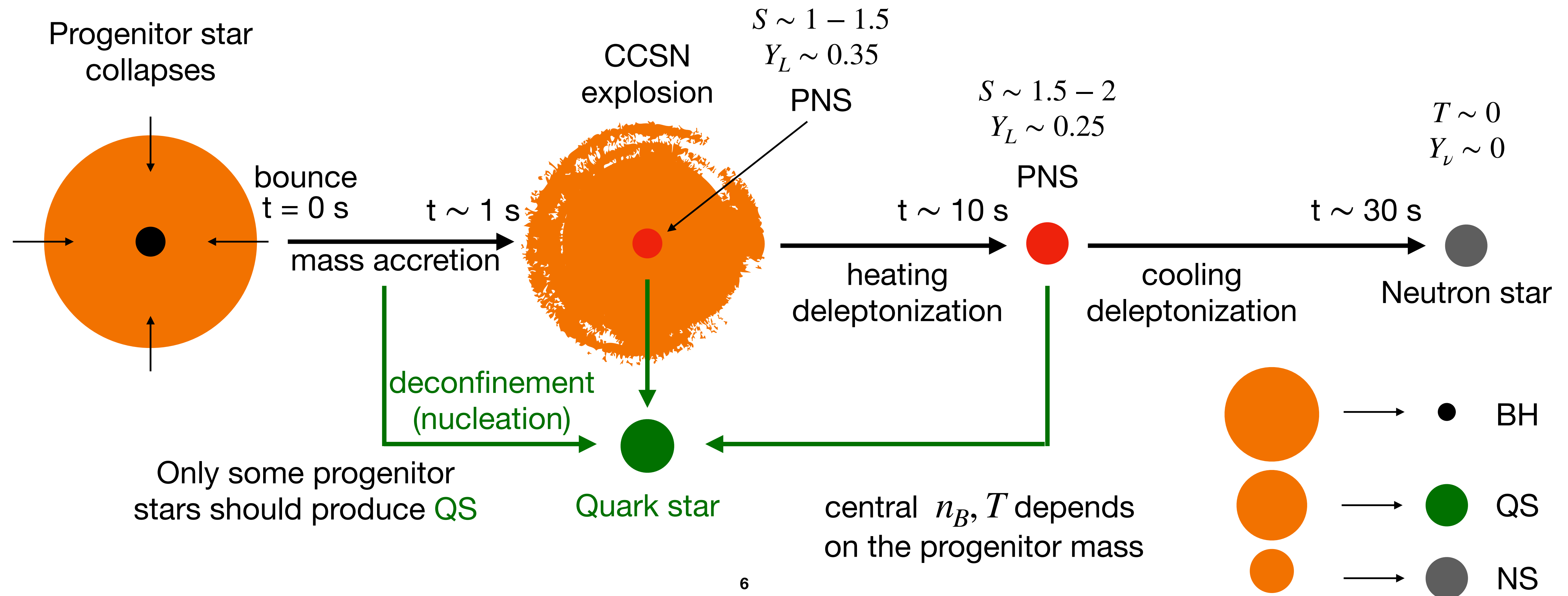
$R > R_{\Delta} = 1/\Delta(T)$: **CFL matter**
absolutely stable



Evolution of PNSs

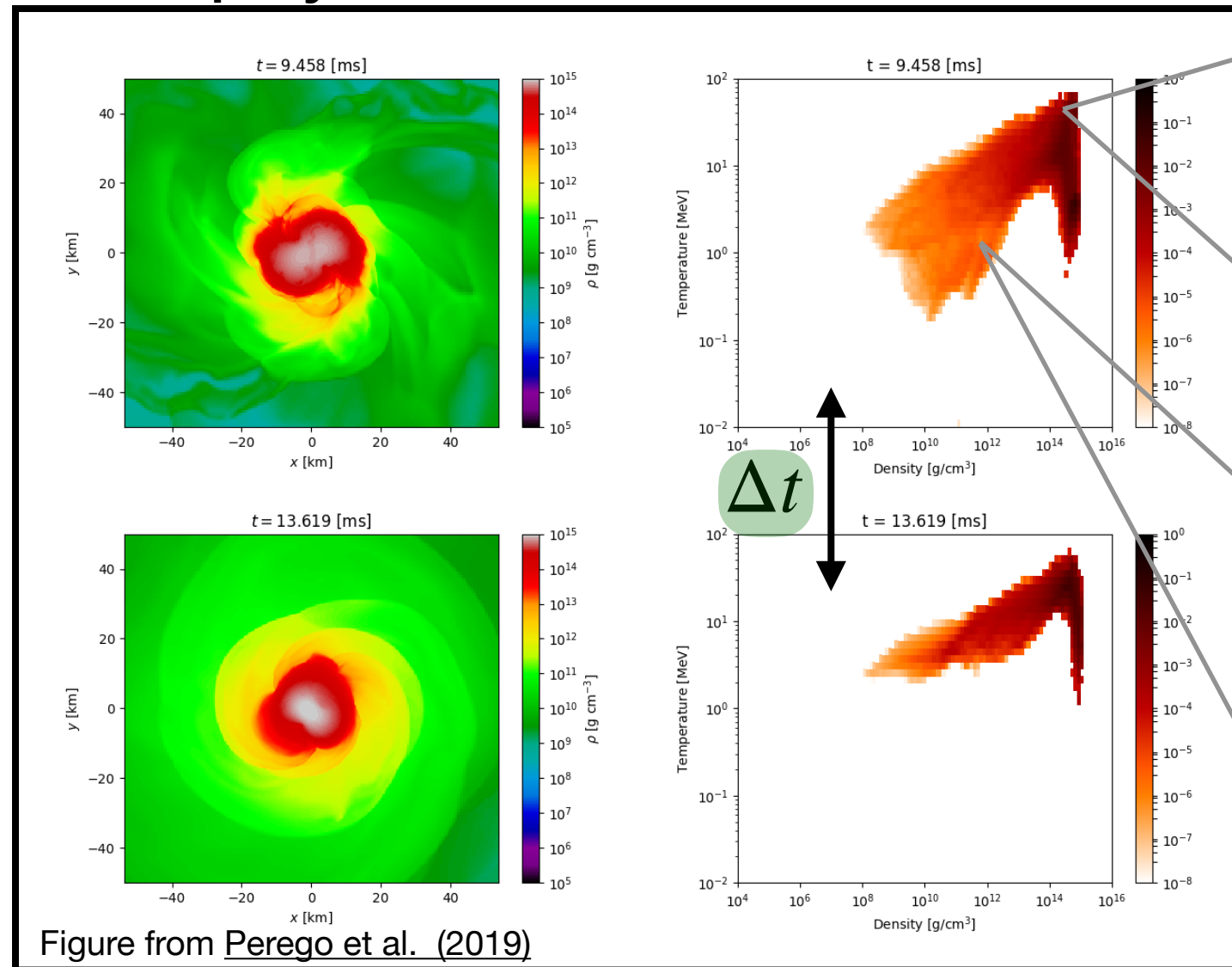
Constraints:

- i. EOS for SQM must have a **maximum mass configuration** $M \gtrsim (2.2 - 2.6) M_{\odot}$
- ii. Some ordinary **neutron stars must survive** the evolution process (namely, **nucleation only at large enough n_B, T**)

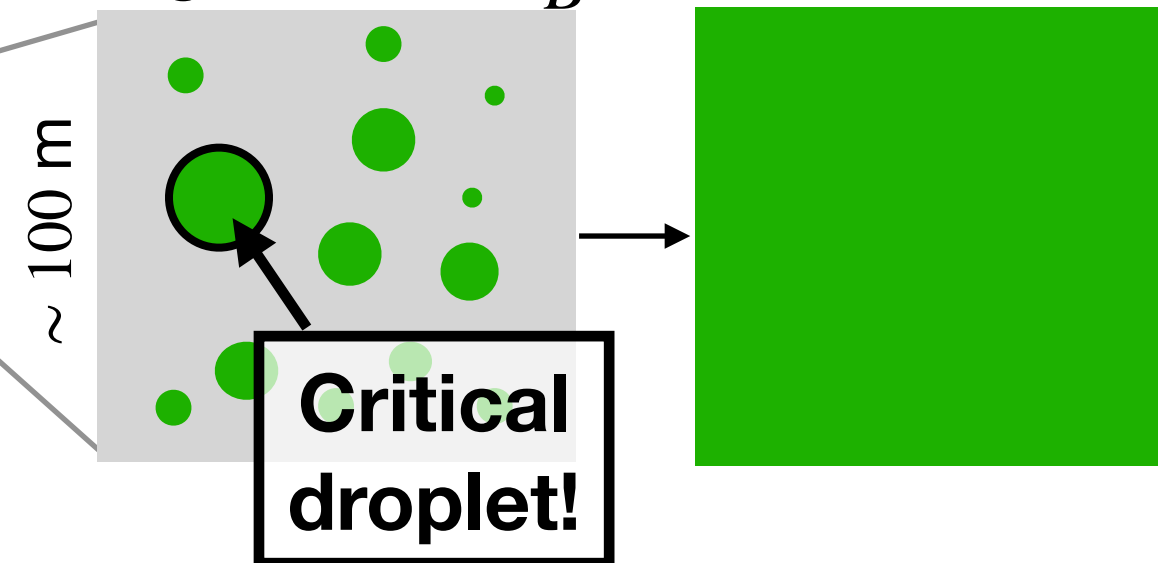


Nucleation in astrophysical systems

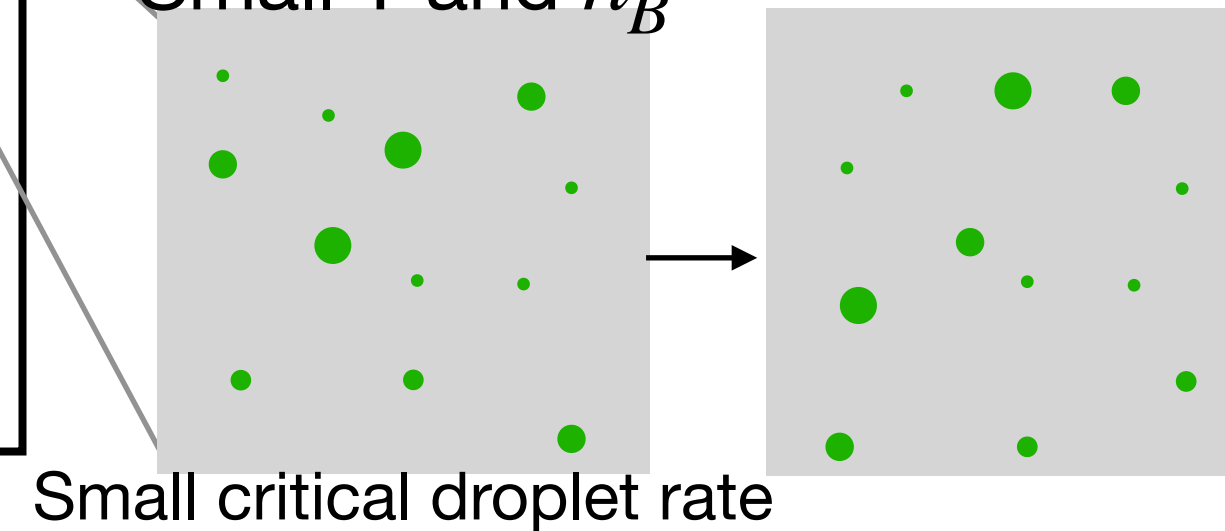
Astrophysical simulation



High T and n_B



Small T and n_B



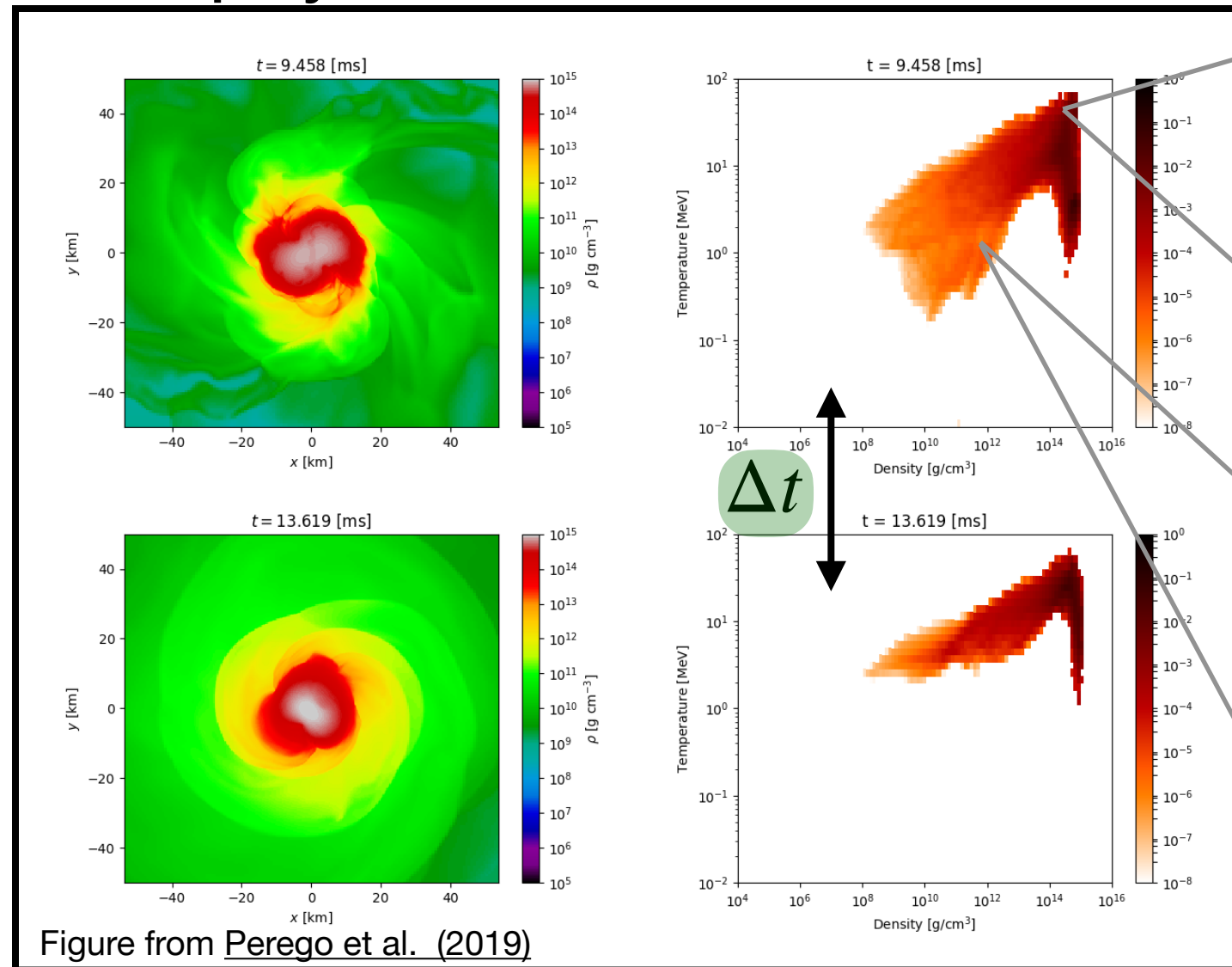
Simulation output: n_B, Y_e, T
in each space-cell and
in each time-step

$$\sum_{\text{every cell}} \sum_{\text{every time}} V_{\text{cell}} \Delta t \Gamma(n_B^H, Y_e, T) \geq 1$$

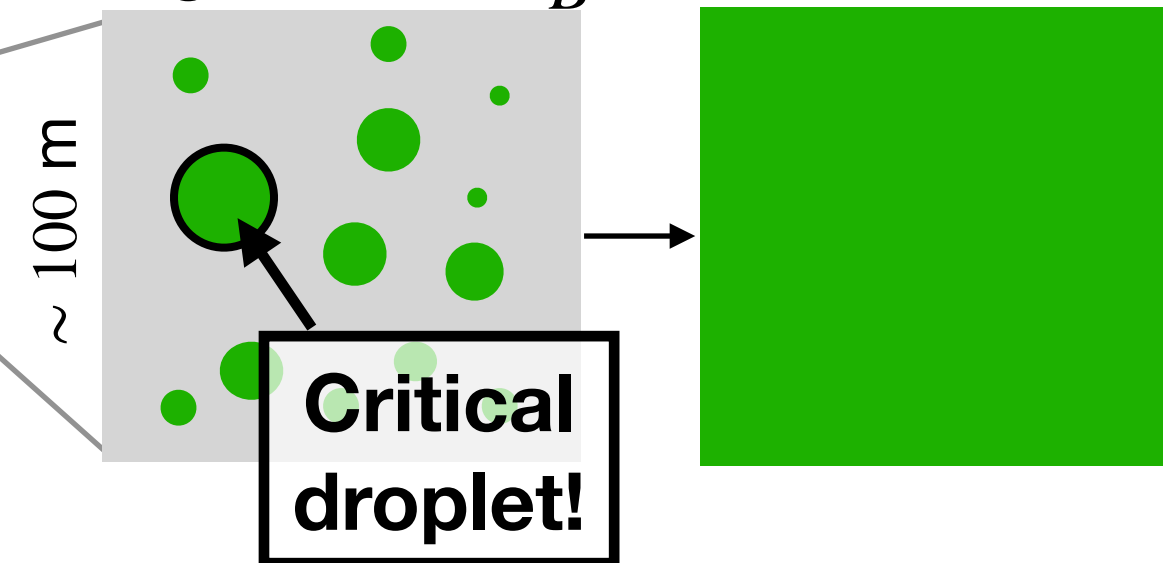
Nucleation rate

Nucleation in astrophysical systems

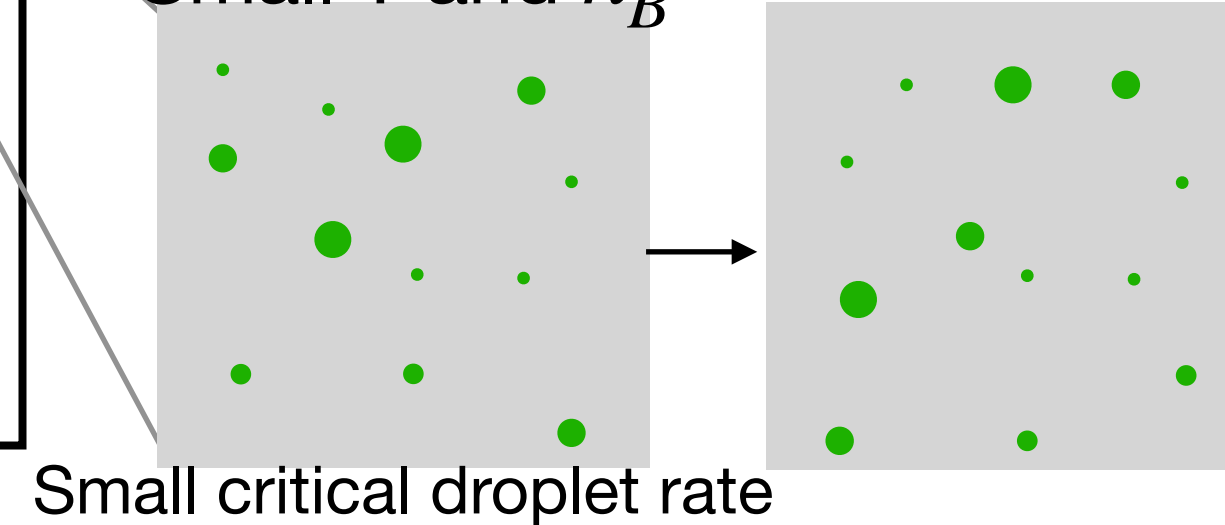
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High T and n_B



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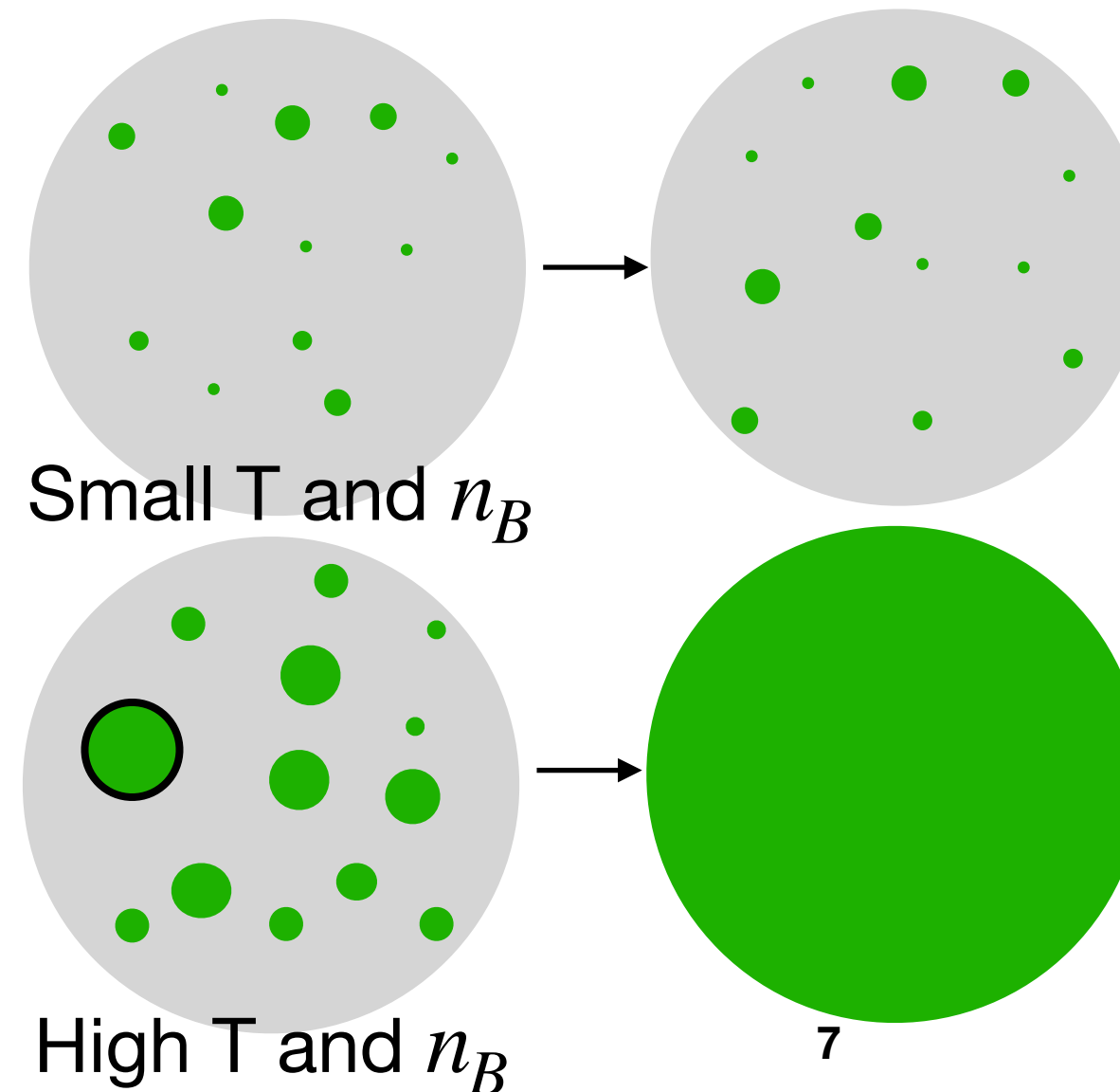
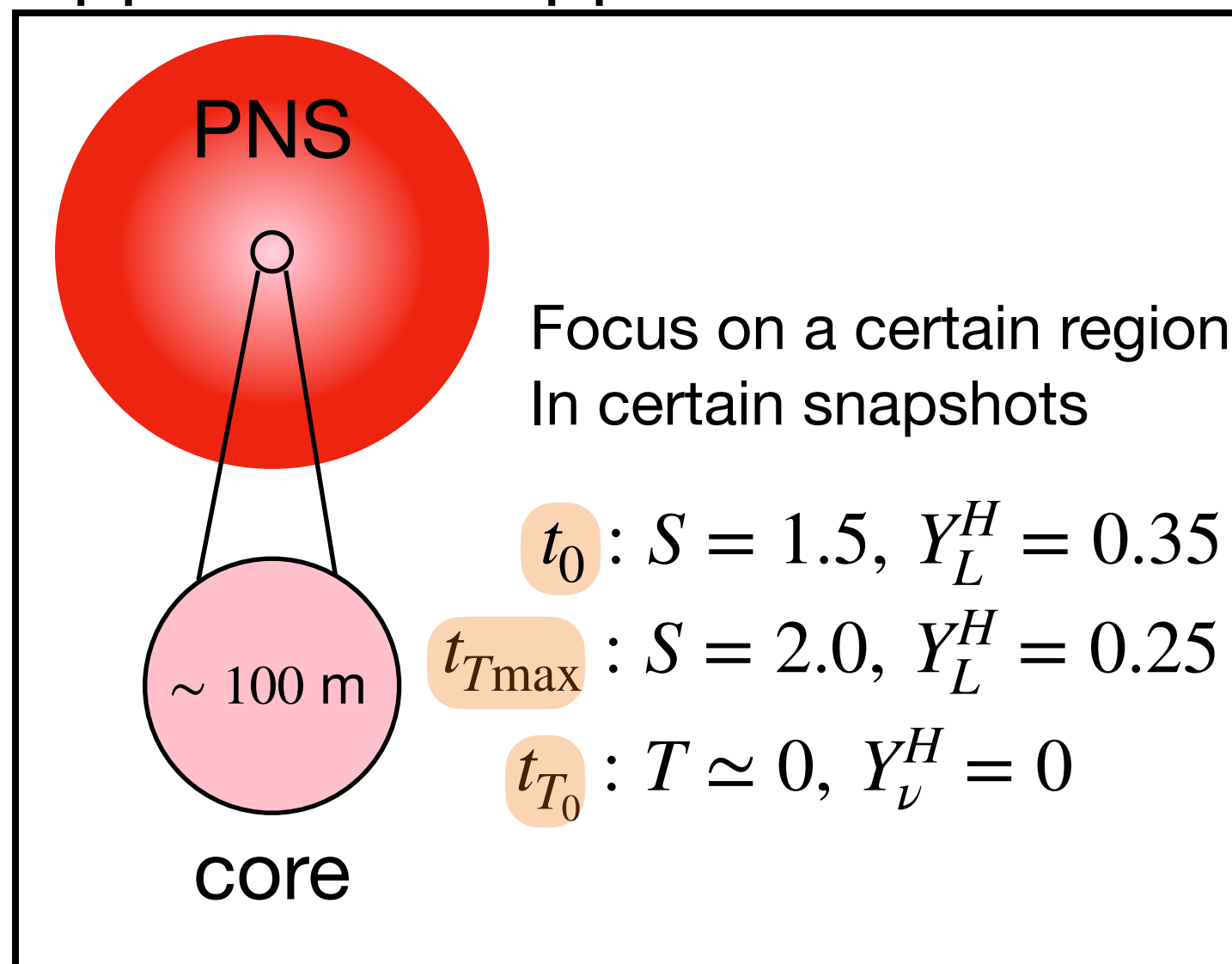


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Nucleation rate

Approximate approach

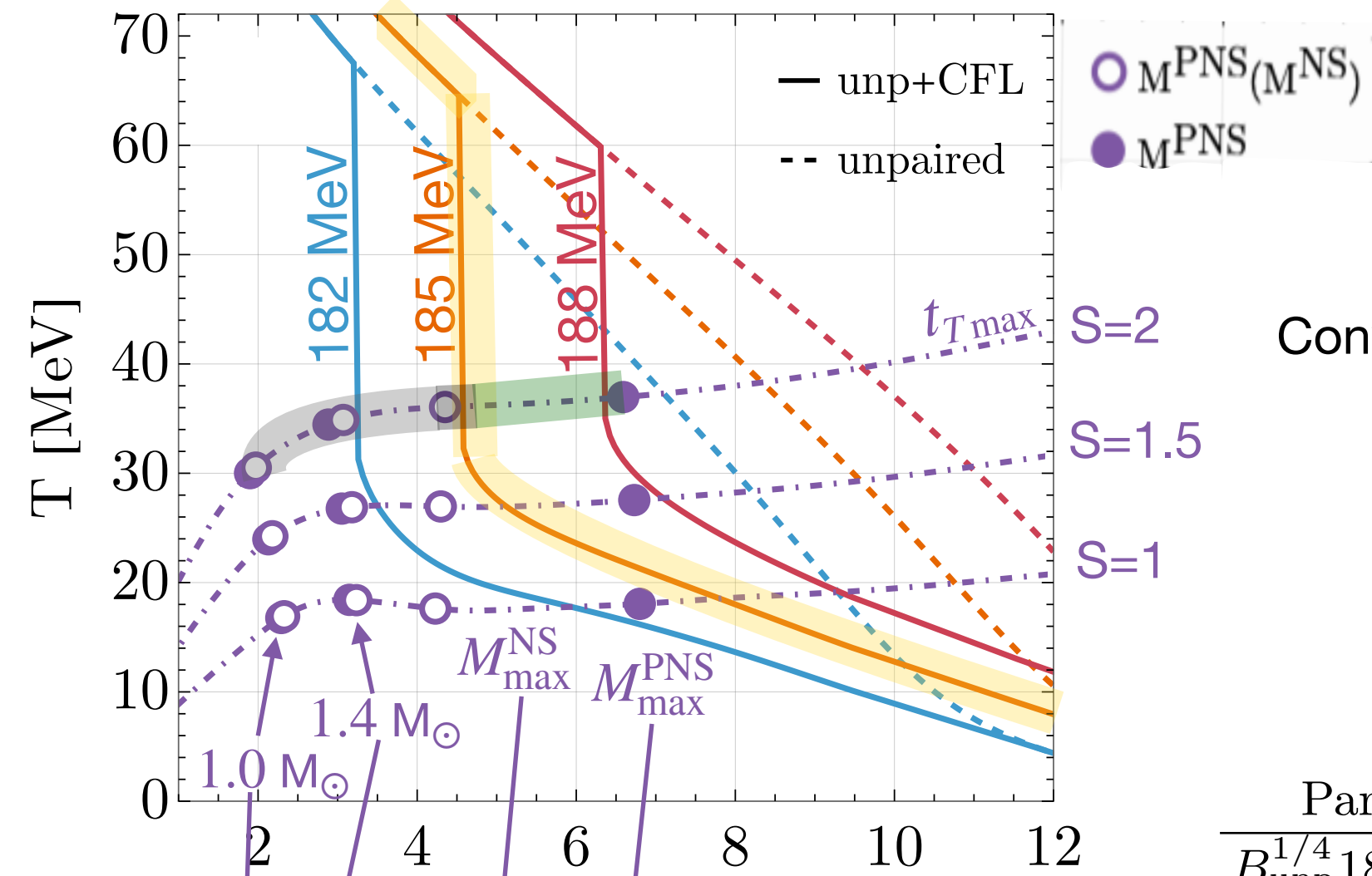


We have some snapshots with fixed Y_L, S
 n_B fixed as central density of a given M^{PNS}

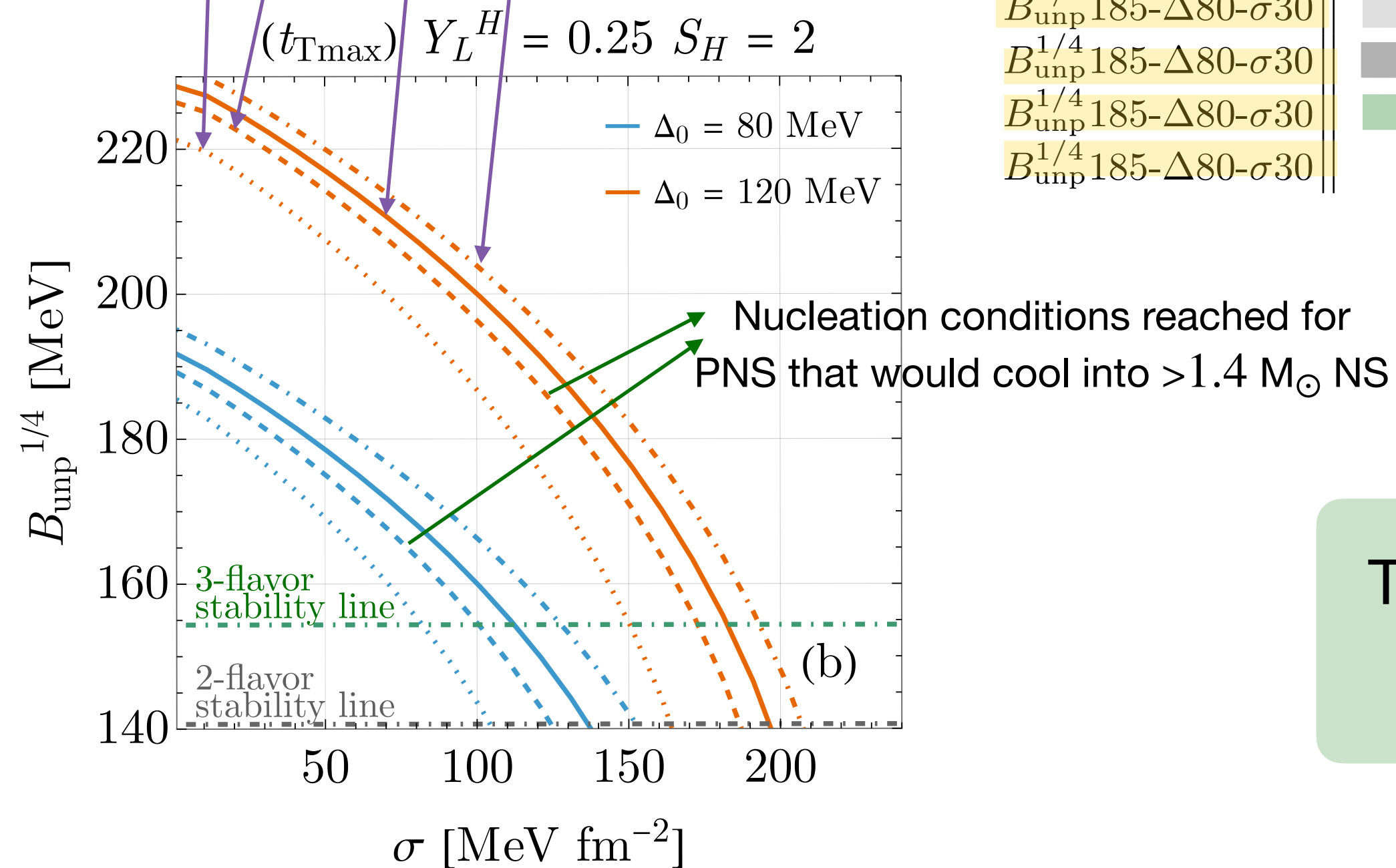
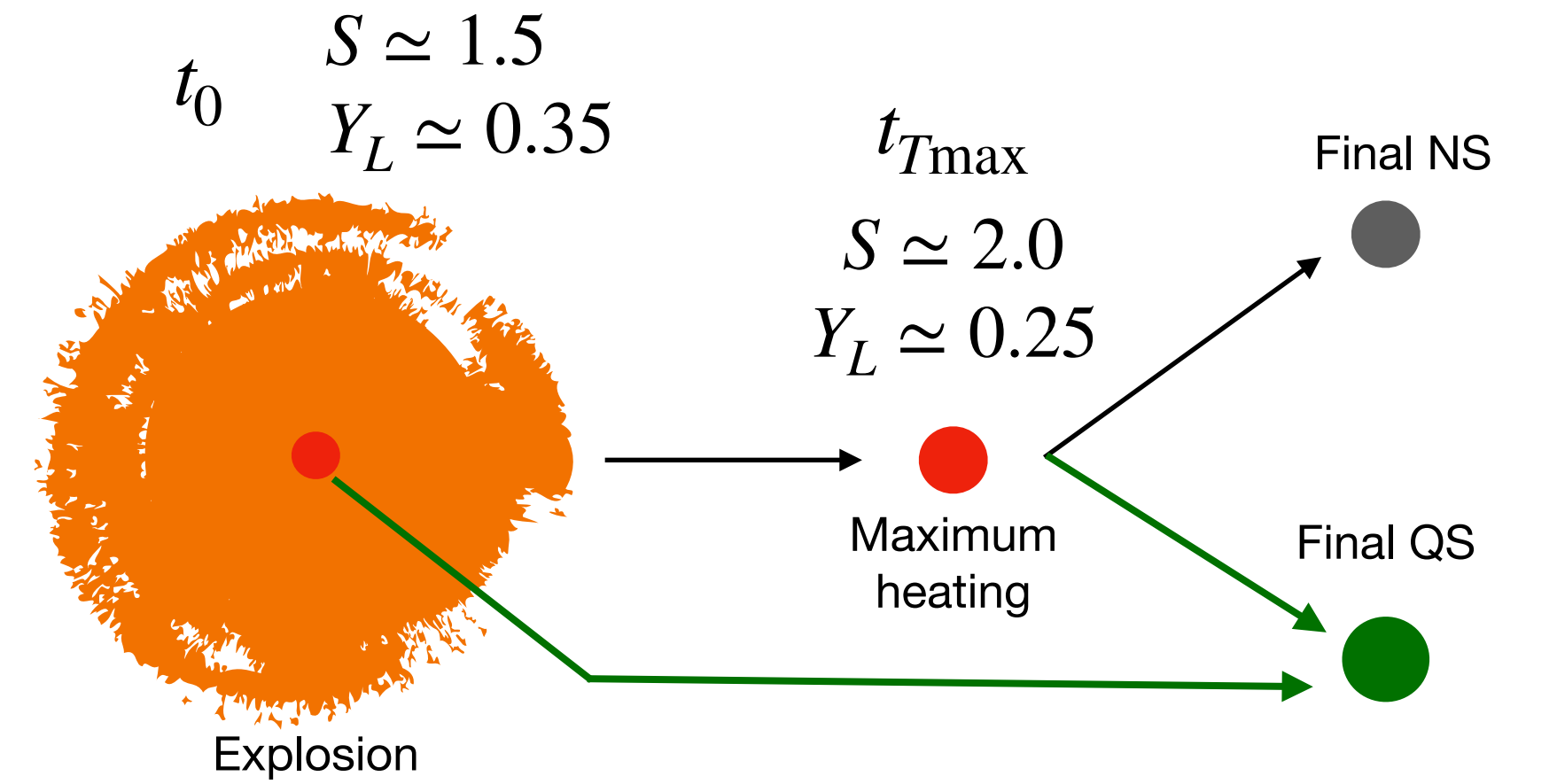
$$[V_{\text{core}} \Gamma(n_B^H, Y_e, T)]^{-1} \equiv \tau_{\text{nuc}} \leq \tau_{\text{dyn}}$$

Typical time after which a
critical droplet
is statistically expected

nucleating conditions at $Y_L^H = 0.25$



Conversion for all the $n_B^H > \text{nucleating line}$



Parameters	PNS at t_0				PNS at $t_{T_{\text{max}}}$			Remnant		
	M^{PNS} [$M_{\odot}$]	M_B^{PNS} [$M_{\odot}$]	$n_{B,c}^H$ [n_0]	$Y_{S,c}^H$	M^{PNS} [$M_{\odot}$]	$n_{B,c}^H$ [n_0]	$Y_{S,c}^H$	remnant	M [$M_{\odot}$]	E_{conv} [$\times 10^{53}$ erg]
$B_{\text{unp}}^{1/4} 182-\Delta 80-\sigma 30$	1.40	1.48	2.85	0.02	1.39	2.87	0.04	NS	1.34	-
$B_{\text{unp}}^{1/4} 182-\Delta 80-\sigma 30$	1.60	1.72	3.53	0.05	1.59	3.70	0.11	QS	1.32	4.98
$B_{\text{unp}}^{1/4} 182-\Delta 80-\sigma 30$	1.80	1.97	5.40	0.31	-	-	-	QS	1.49	7.22
$B_{\text{unp}}^{1/4} 185-\Delta 80-\sigma 30$	1.60	1.72	3.53	0.05	1.59	3.70	0.11	NS	1.53	-
$B_{\text{unp}}^{1/4} 185-\Delta 80-\sigma 30$	1.70	1.84	4.08	0.10	1.69	4.48	0.20	BH	-	-
$B_{\text{unp}}^{1/4} 185-\Delta 80-\sigma 30$	1.75	1.90	4.52	0.16	1.74	5.31	0.33	QS	1.45	5.32
$B_{\text{unp}}^{1/4} 185-\Delta 80-\sigma 30$	1.80	1.97	5.40	0.31	-	-	-	BH	-	-

Conversion energy
GRB after CCSN?
other phenomenology?

Coexistence of QS-NS

There exists a parameter space in which some PNSs will not convert into QSs but instead cool down into NS.

Summary and conclusions

Any other questions
or suggestions?
mirco.guerrini@unife.it

Background

- **Two families** of compact objects may exist if the **Witten hypothesis** is correct (absolute stability of SQM in bulk)
- **Nucleation** is key for understanding under which conditions ordinary **NS** can **convert** into **QS**

Method

- We added the contribution of **thermal fluctuations of the composition** in computing the nucleation time
- We propose a framework for **color-superconductivity in nucleation**:
 1. CFL is absolutely stable; unpaired matter is not
 2. diquark pairs form only in systems large enough (unpaired in $R < 1/\Delta$, CFL in $R > 1/\Delta$)

Goal: testing the possible coexistence of NSs and Qs: Can at least some NSs survive the PNS evolution?

Results: a parameters space for the two-families scenario exists

Outlooks

- Use more sophisticated EOSs for the quark phase and estimate surface tension
- How to include those **finite-size effects in simulations**?
- Complete study of related phenomenology (e.g., deconfinement-driven CCSN with two families scenario? Accretion?)

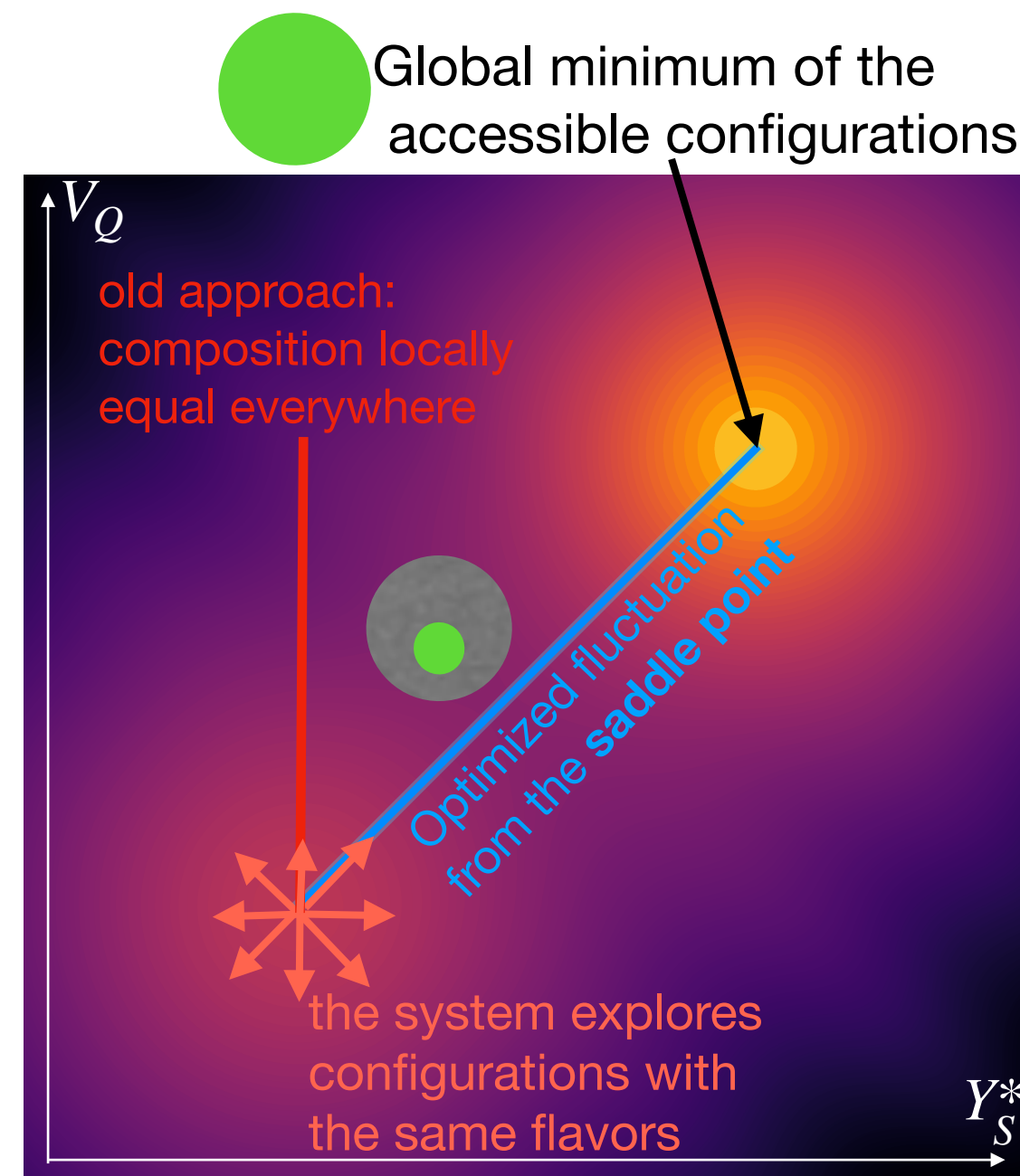
Backup

Fluctuations and nucleation

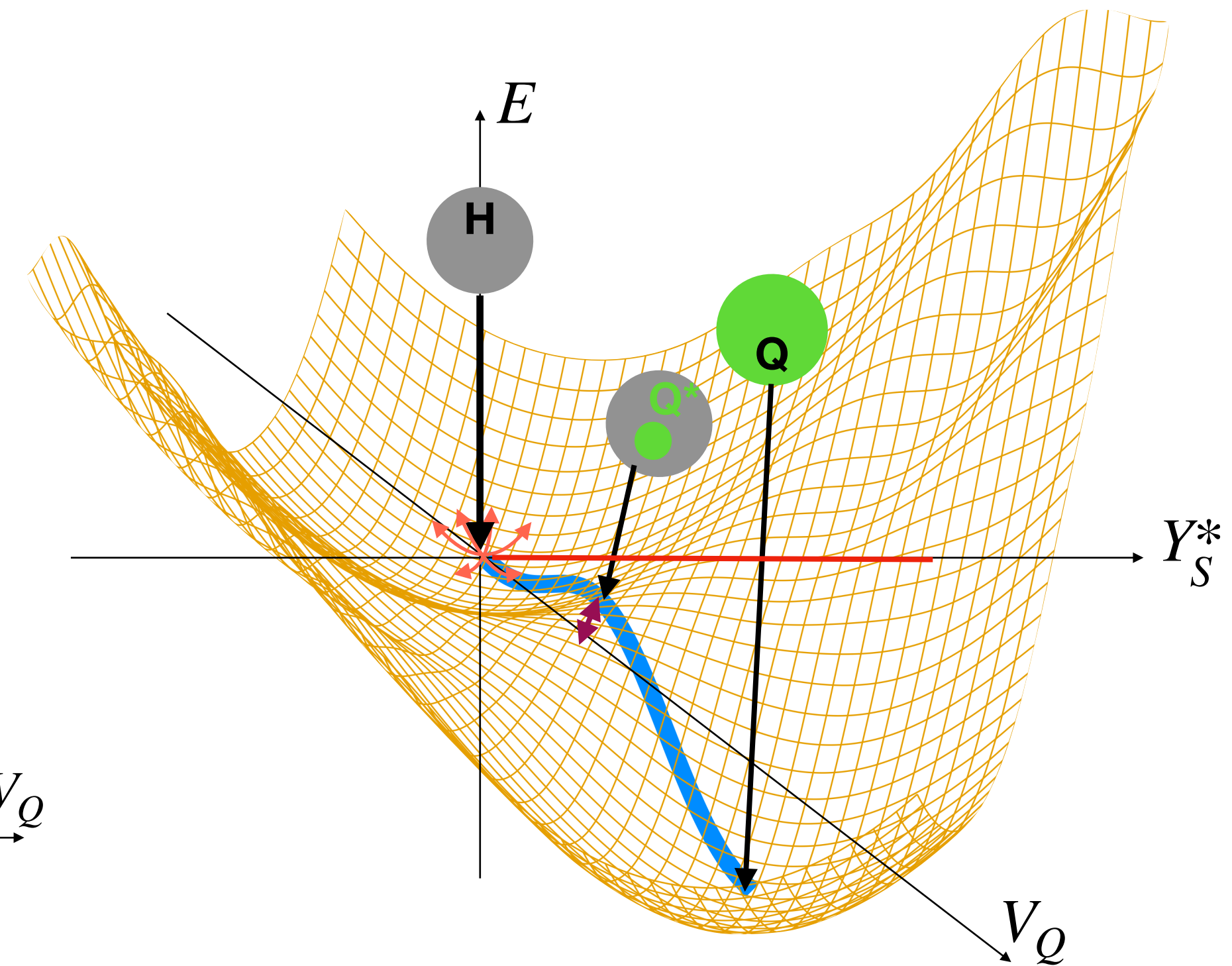
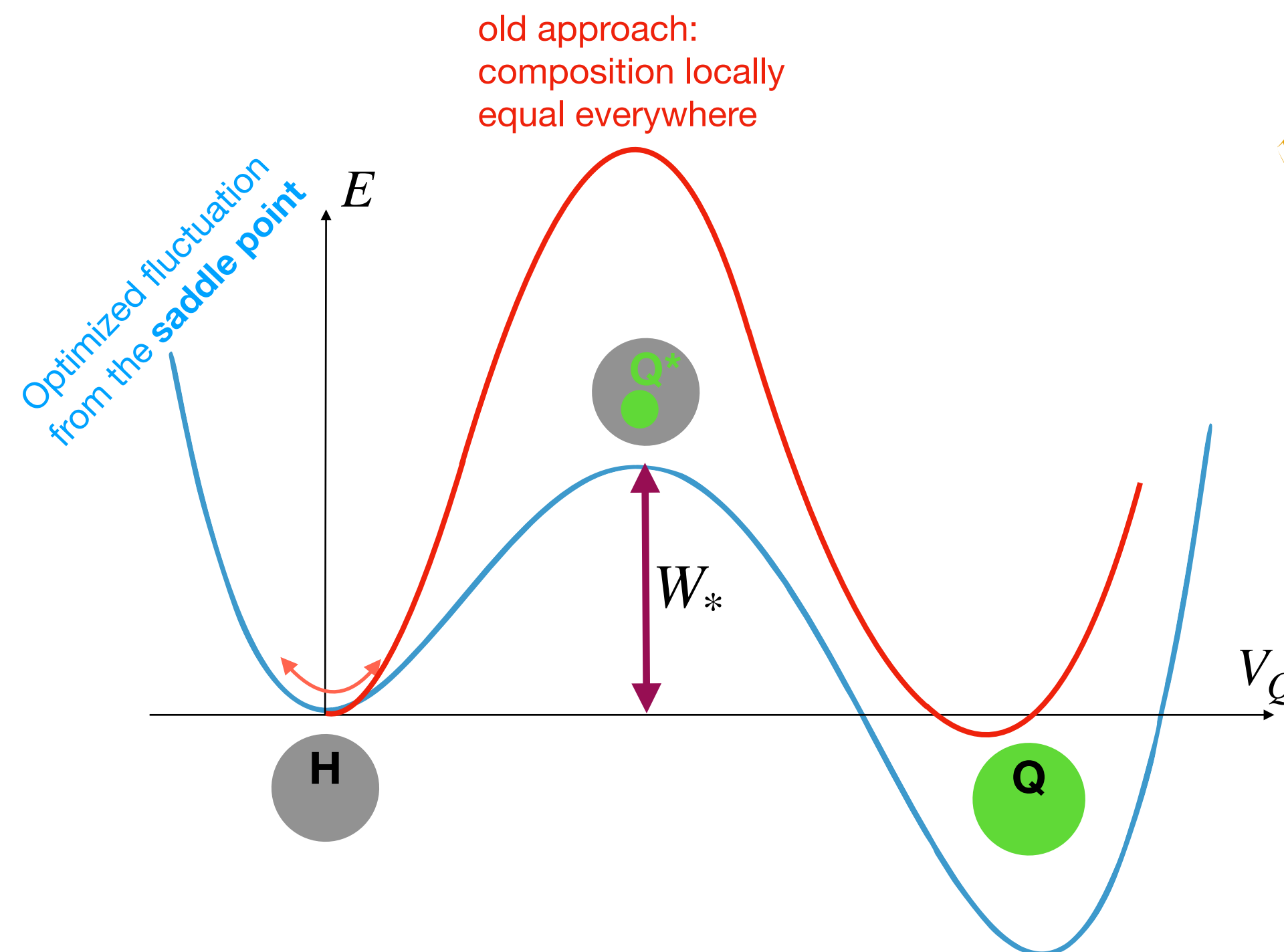
$\propto e^{-\frac{W}{T}}$
Configurations with high W are negligible

$$\min_{n_B^{Q*}, \{Y_i^*\}, T_{Q*}} \left[W(R, n_B^{Q*}, \{Y_i^*\}, T_{Q*}, n_B^H, \{Y_i^H\}, T) \right] \rightarrow W(R, n_B^H, \{Y_i\}, T)$$

$$\max_R \left[W(R, n_B^H, \{Y_i^H\}, T) \right] = W(R_*, n_B^H, \{Y_i^H\}, T) \equiv W_*$$

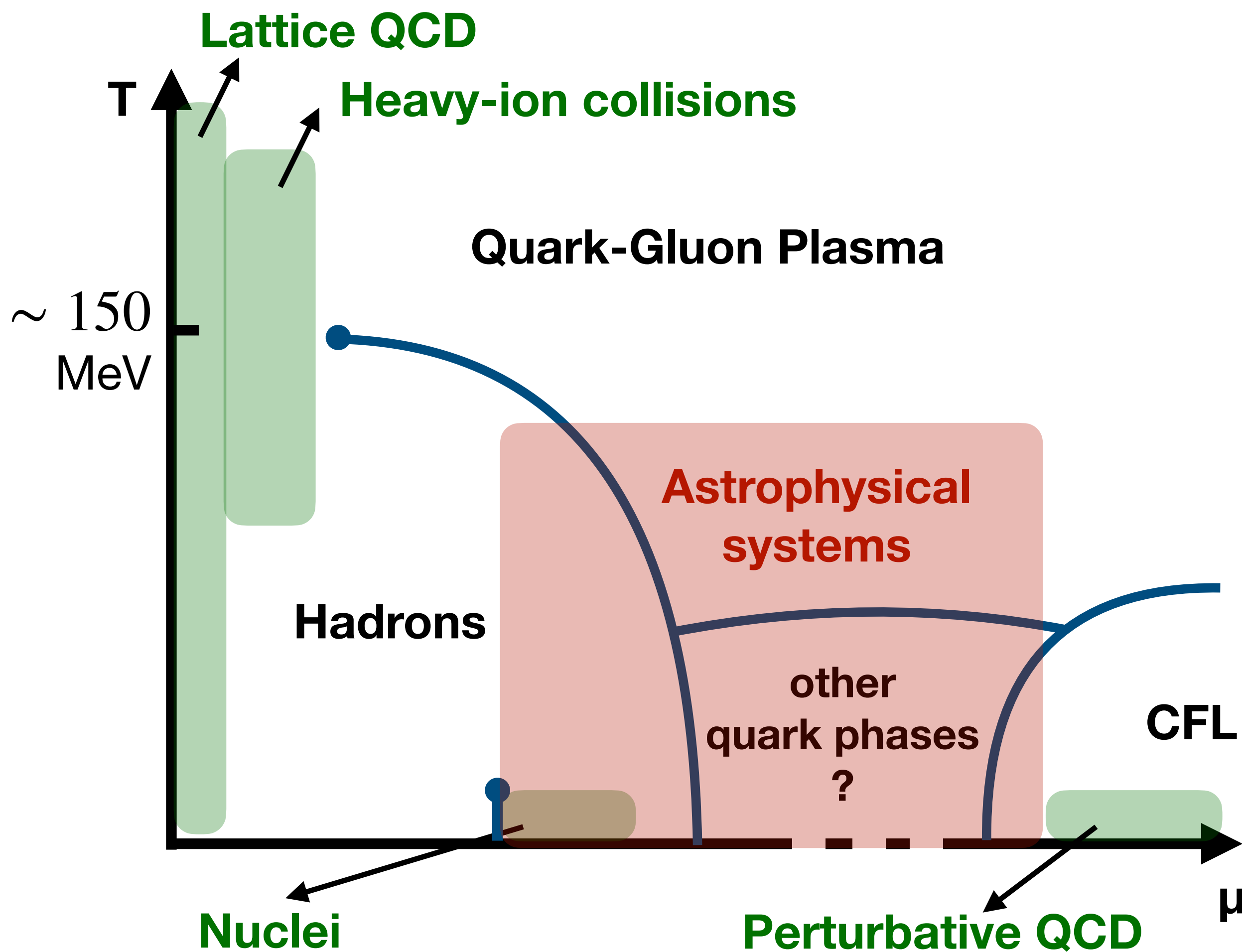


Local minimum:
The entire system is in the **H phase** ($V_Q = 0$)
with the composition locally equal everywhere



3D representation of a N-D
plot of the **energy** of the system
as a function of all the **variables**

QCD phase diagram



- the high-density regime is poorly known
- quarks d.o.f. expected at $n_B \sim \text{few } n_0$
- extreme densities are reached in astrophysical phenomena related to **compact objects**

Astrophysical systems

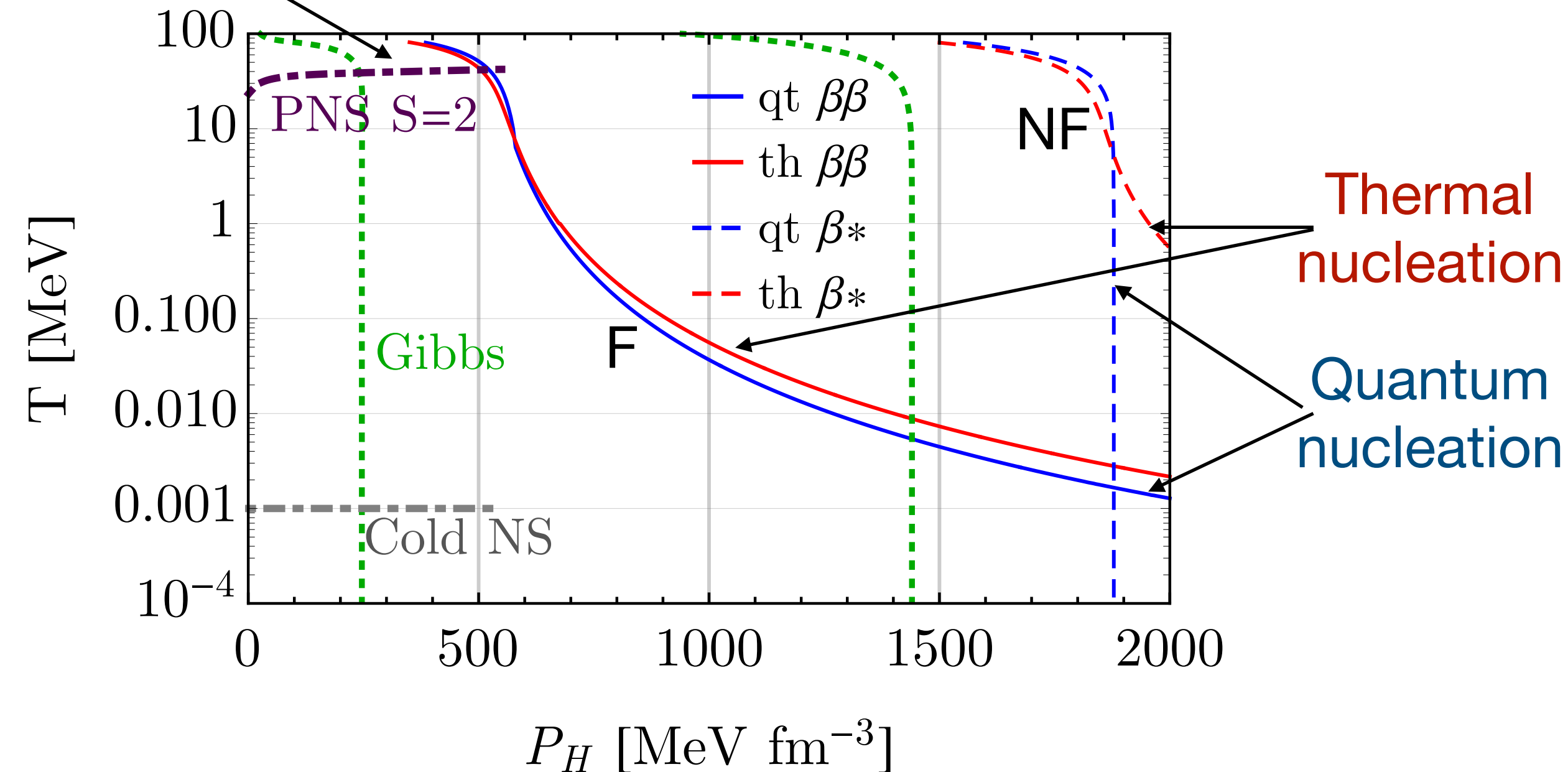
	n_B/n_0	T [MeV]	Y_e
Isolated NS	$10^{-8} - 8$	~ 0	0.01-0.3
Core Collapse Supernovae (CCSN)	$10^{-8} - 8$	$0 - 50$	0.25-0.55
Proto NS (PNS)	$10^{-8} - 8$	$0 - 50$	0.01-0.3
Binary NS Mergers (BNSM)	$10^{-8} - 8$	$0 - 100$	0.01-0.6

Results: two flavors case

[Guerrini et al. (2024)]

PNS after deleptonization

$$\sigma = 30 \text{ MeV fm}^{-2}$$



Effect of thermal fluctuation (F) in the hadronic composition

$T \gtrsim 10 \text{ MeV}$:

- nucleation at lower P than no fluc. (NF) case
- most massive PSNs could nucleate

$1 \text{ keV} \lesssim T \lesssim 10 \text{ MeV}$:

- nucleation at lower P than NF case
- PSNs can not nucleate

$T \lesssim 1 \text{ keV}$:

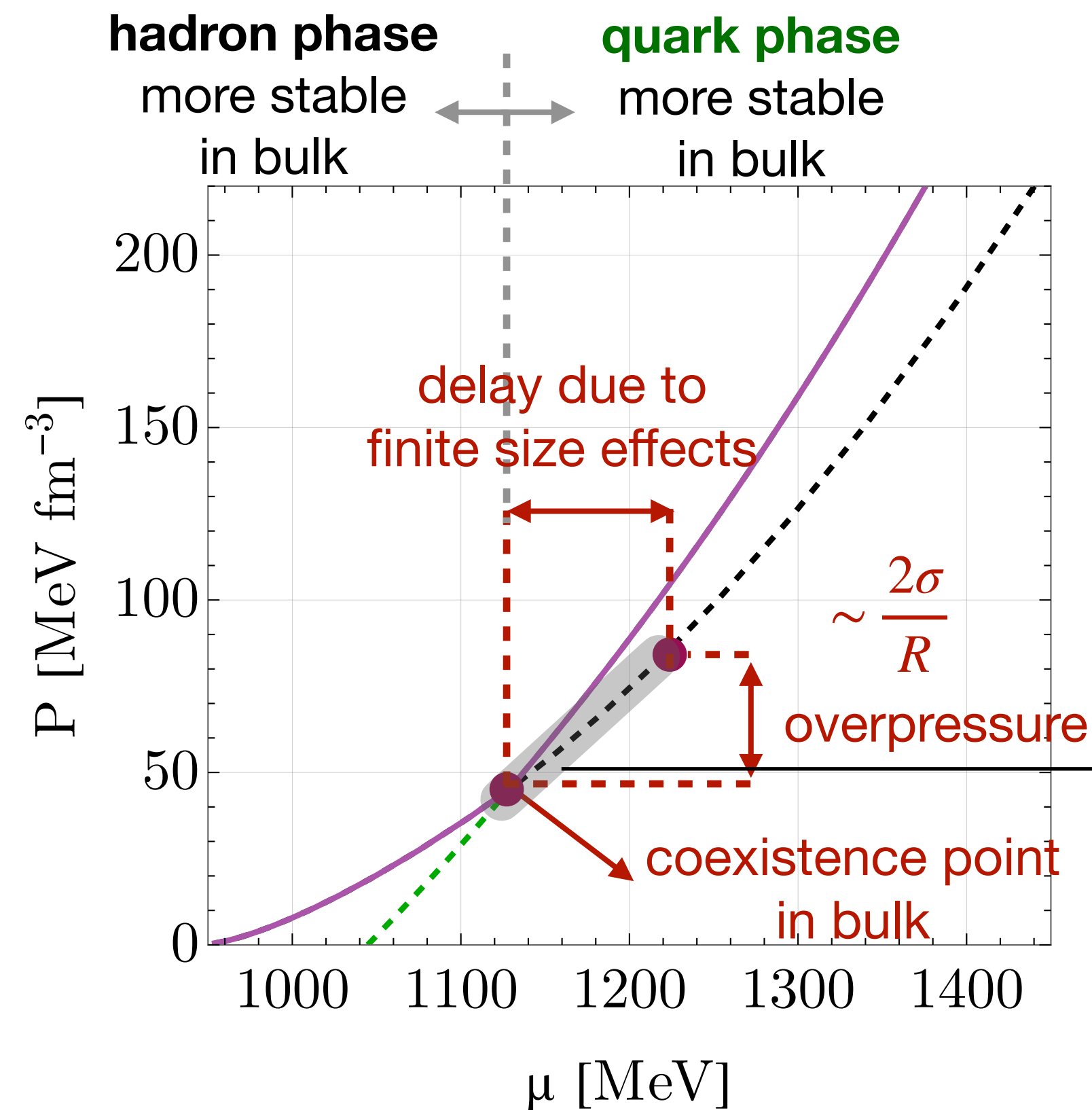
- negligible contribution

P and T at which the typical nucleation time is $\sim 1 \text{ s}$

Take home message:

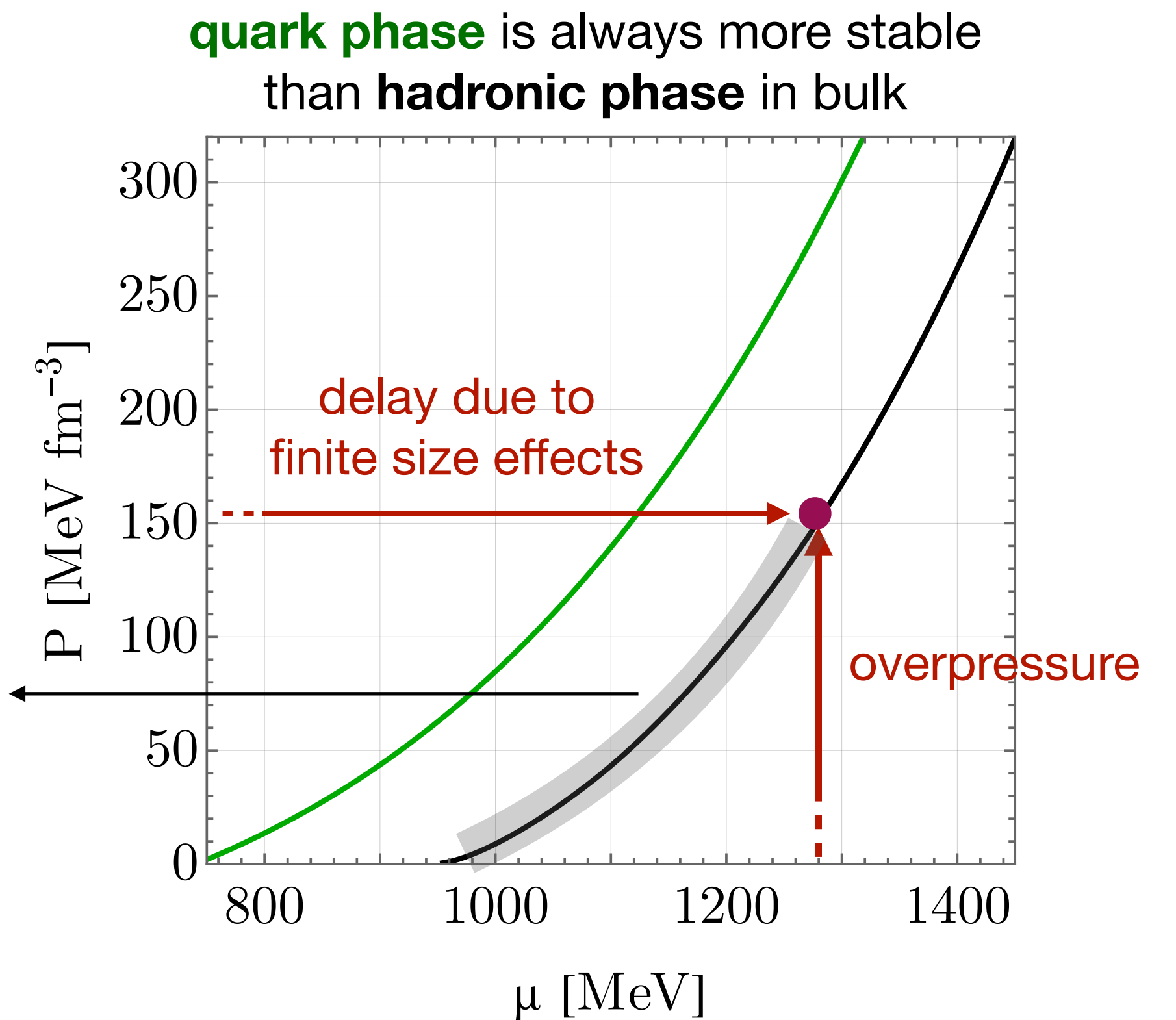
composition fluctuations lead to a much faster nucleation (i.e. deconfinement can start at lower P) in compact objects at intermediate and high temperature

Nucleation in compact stars



One family scenario (hybrid stars)

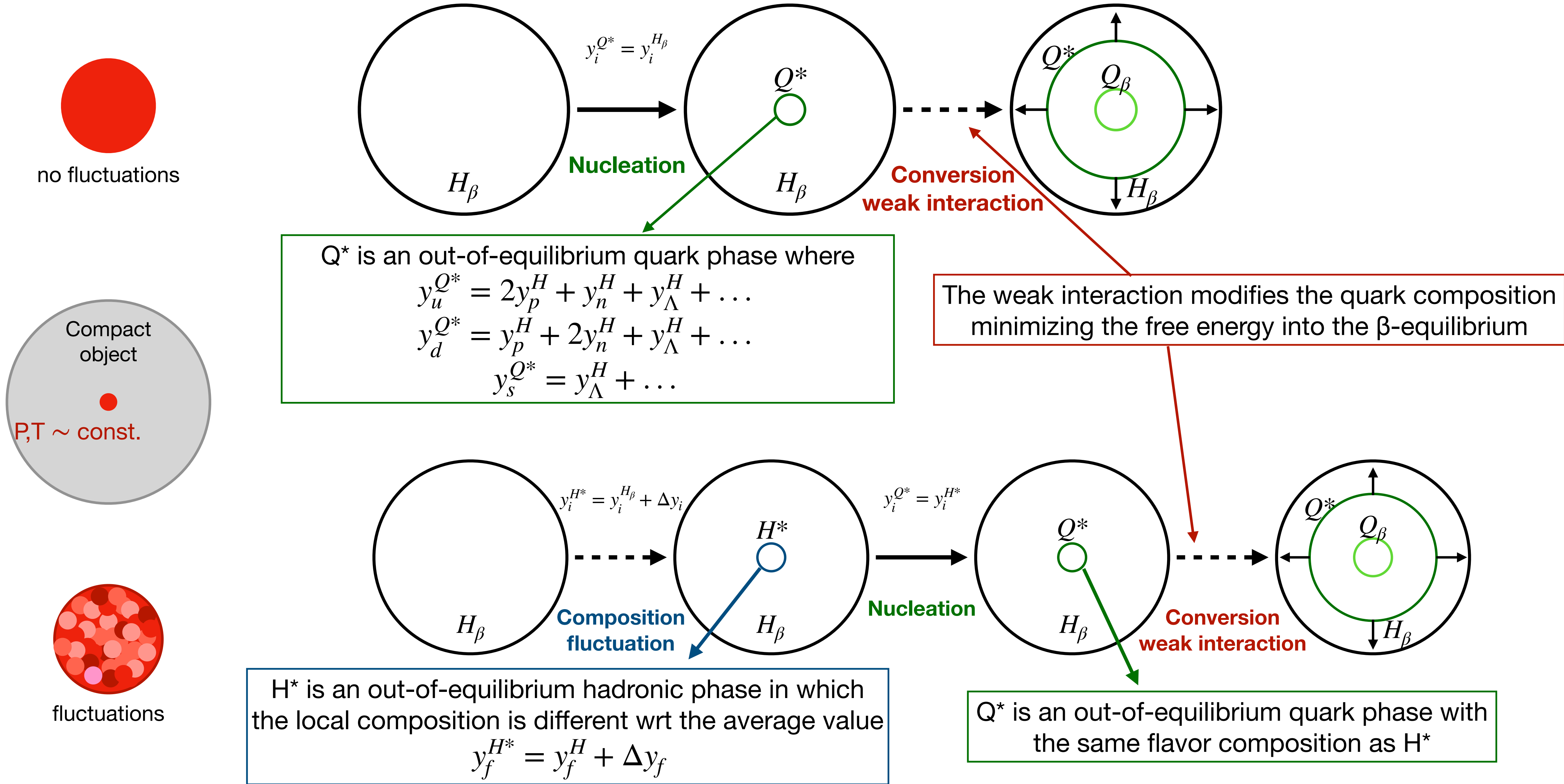
leads to a **delay** in the phase transition with respect to the bulk mixed phase onset



Two families scenario (neutron and quark stars)

is the only mechanism that prevents the decay of ordinary matter into SQM

Nucleation: calculations setup



Backup: nucleation

$$\Gamma = \Gamma_0 e^{-W/T} \quad R_* = \frac{2\sigma}{P_{Q*} - P_H} \quad W = \frac{16}{3} \pi \frac{\sigma^3}{(P_{Q*} - P_H)^2}.$$

$$\tau = \frac{1}{V\Gamma} \quad W = -\frac{4}{3} \pi R_*^3 [P_{Q*} - P_H] + 4\pi\sigma R_*^2.$$

$$\begin{aligned} W_1 &= \sum_{i=B,C,S,e} N_i^* (\mu_i^{H*} - \mu_i^H) \\ &= \frac{4}{3} \pi R_*^3 n_B^{Q*} \sum_{i=B,C,S,e} Y_i^* (\mu_i^{H*} - \mu_i^H) \end{aligned}$$

$$\begin{aligned} \mu_B^Q(n_B^{Q*}, \{Y_i^{Q*}\}, T) &= \mu_B^H(n_B^H, \{Y_i^H\}, T) \\ \mu_C^Q(n_B^{Q*}, \{Y_i^{Q*}\}, T) + \mu_e^Q(n_B^{Q*}, Y_e^{Q*}, T) &= \mu_C^H(n_B^H, \{Y_i^H\}, T) + \mu_e^H(n_B^H, Y_e^H, T) \\ \mu_S^Q(n_B^{Q*}, \{Y_i^{Q*}\}, T) &= \mu_S^H(n_B^H, \{Y_i^H\}, T) \\ \mu_\nu^Q(n_B^{Q*}, Y_{\nu_e}^{Q*}, T) &= \mu_\nu^H(n_B^H, Y_{\nu_e}^H, T) \\ Y_C^{Q*} - Y_e^{Q*} &= 0. \end{aligned}$$

Backup: CFL+unp

$$P_Q(n_B^Q, \{Y_i^Q\}, T, R) = \begin{cases} P_{Qunp}(n_B^Q, \{Y_i^Q\}, T) & \text{if } R \leq R_\Delta \\ P_{QCFL}(n_B^Q, T) & \text{if } R > R_\Delta \end{cases}$$

$$R_*(n_B^H, \{Y_i^H\}, T) = \begin{cases} R_{unp*}(n_B^H, \{Y_i^H\}, T) & \text{if } R_{unp*}(n_B^H, \{Y_i^H\}, T) \leq R_\Delta \\ \max[R_\Delta, R_{CFL*}(n_B^H, T)] & \text{if } R_{unp*}(n_B^H, \{Y_i^H\}, T) > R_\Delta \end{cases}$$

$$\Delta(T) = \Theta(T_c - T) \Delta_0 \sqrt{1 - \frac{T}{T_c}}$$

$$T_c \simeq 2^{1/3} 0.57 \Delta_0$$

Schmitt (2010) Lec. Not. Phys

Backup: three flavors EOSs

$$P_q(\mu_i, T, m_i, \alpha_s = 0) = \frac{6}{2\pi^2} \frac{1}{3} \int_0^{+\infty} \frac{k^4}{E(k, m_i)} [\mathbf{f}(k, \mu_i, T, m_i) + \mathbf{f}(k, -\mu_i, T, m_i)] dk$$

$$P_i^Q(\mu_i, T) = P_q(\mu_i, T, m_i, \alpha_s = 0) - \frac{5\pi\alpha_s}{18} T^4 - \frac{2\alpha_s}{\pi} \left(\frac{1}{2} T^2 \mu_i^2 + \frac{1}{4\pi^2} \mu_i^4 \right)$$

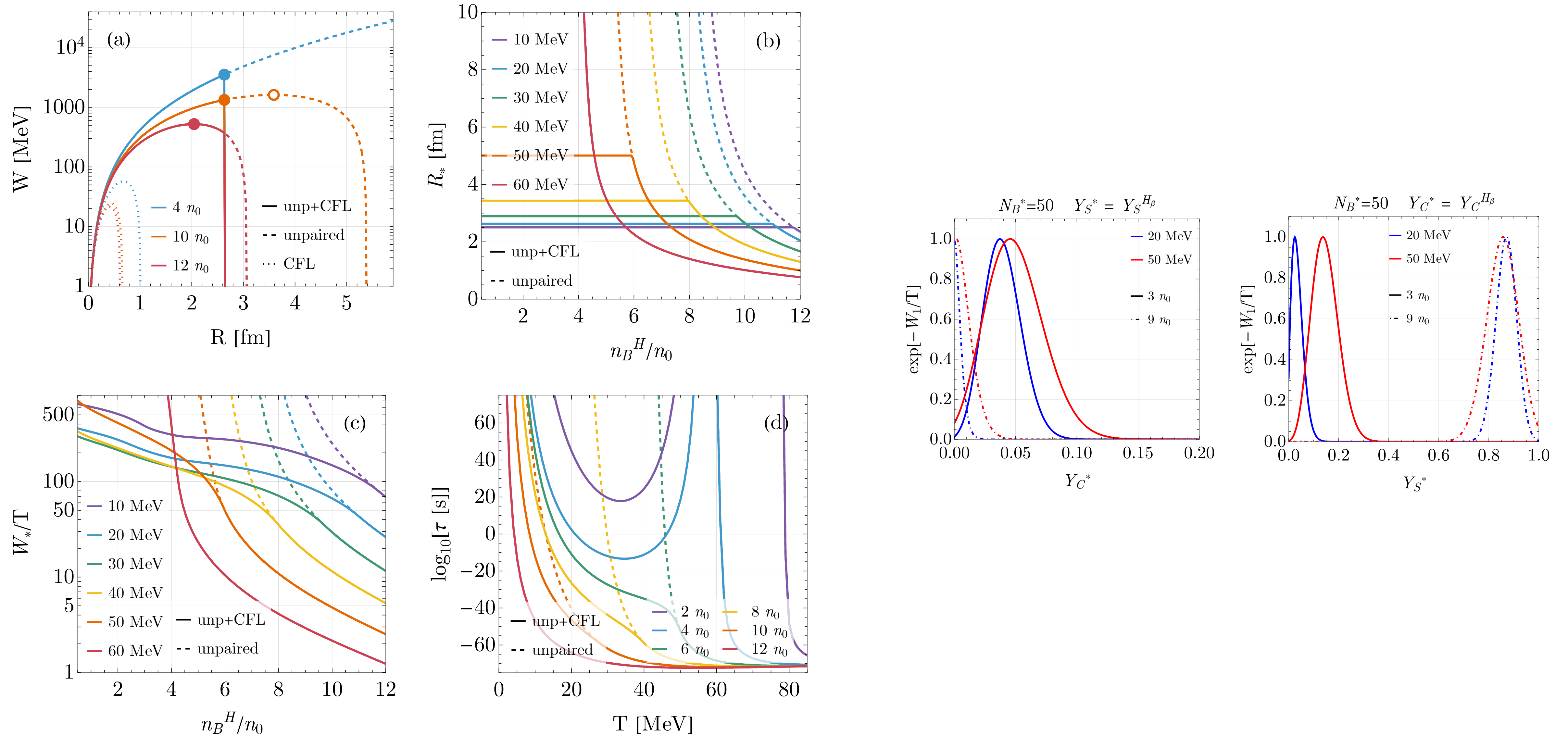
Fischer et al. (2011) ApJ

$$\Delta(T) = \Theta(T_c - T) \Delta_0 \sqrt{1 - \frac{T}{T_c}}$$

$$T_c \simeq 2^{1/3} 0.57 \Delta_0$$

Schmitt (2010) Lec. Not. Phys

Backup: more on three flavors



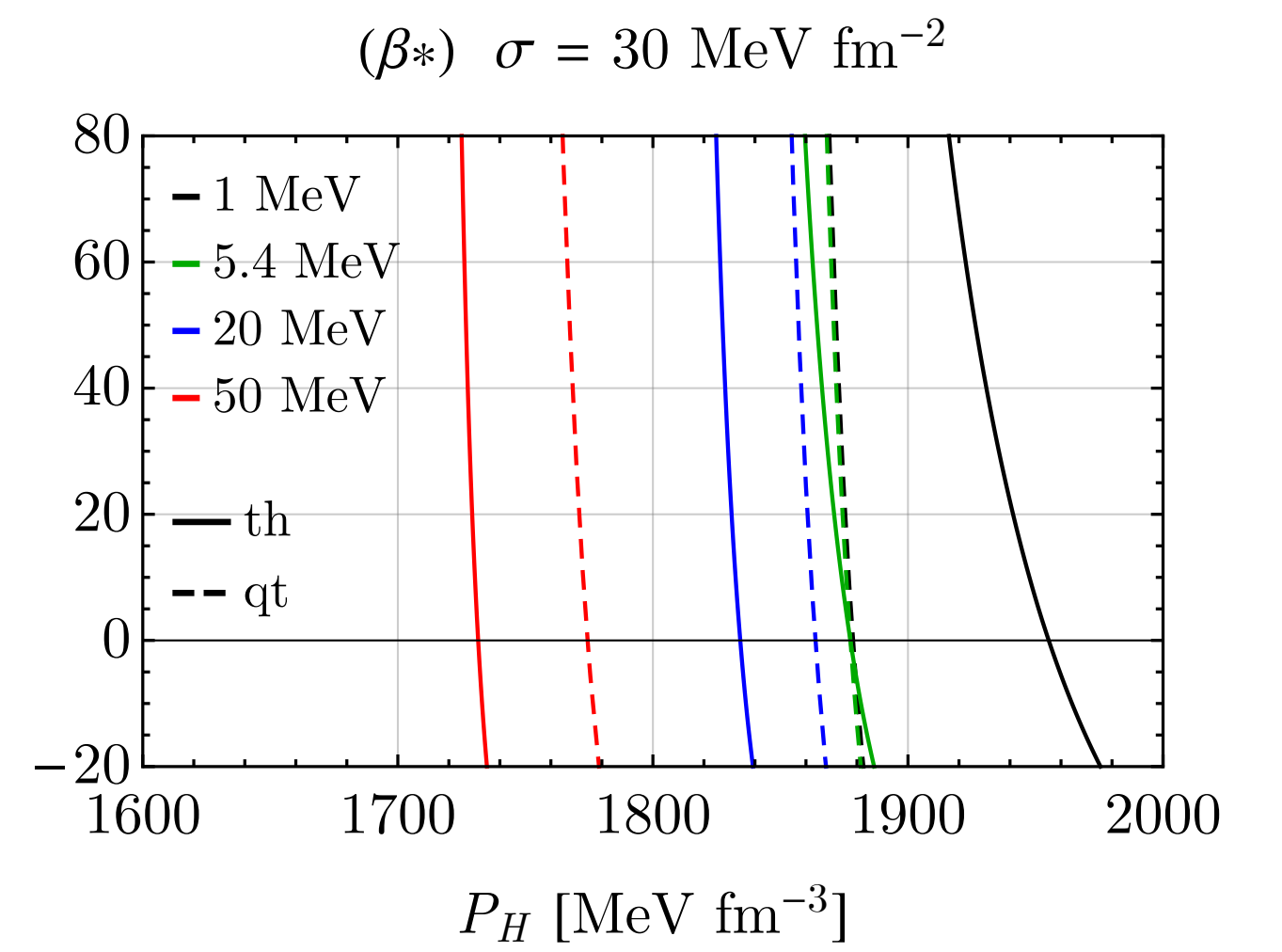
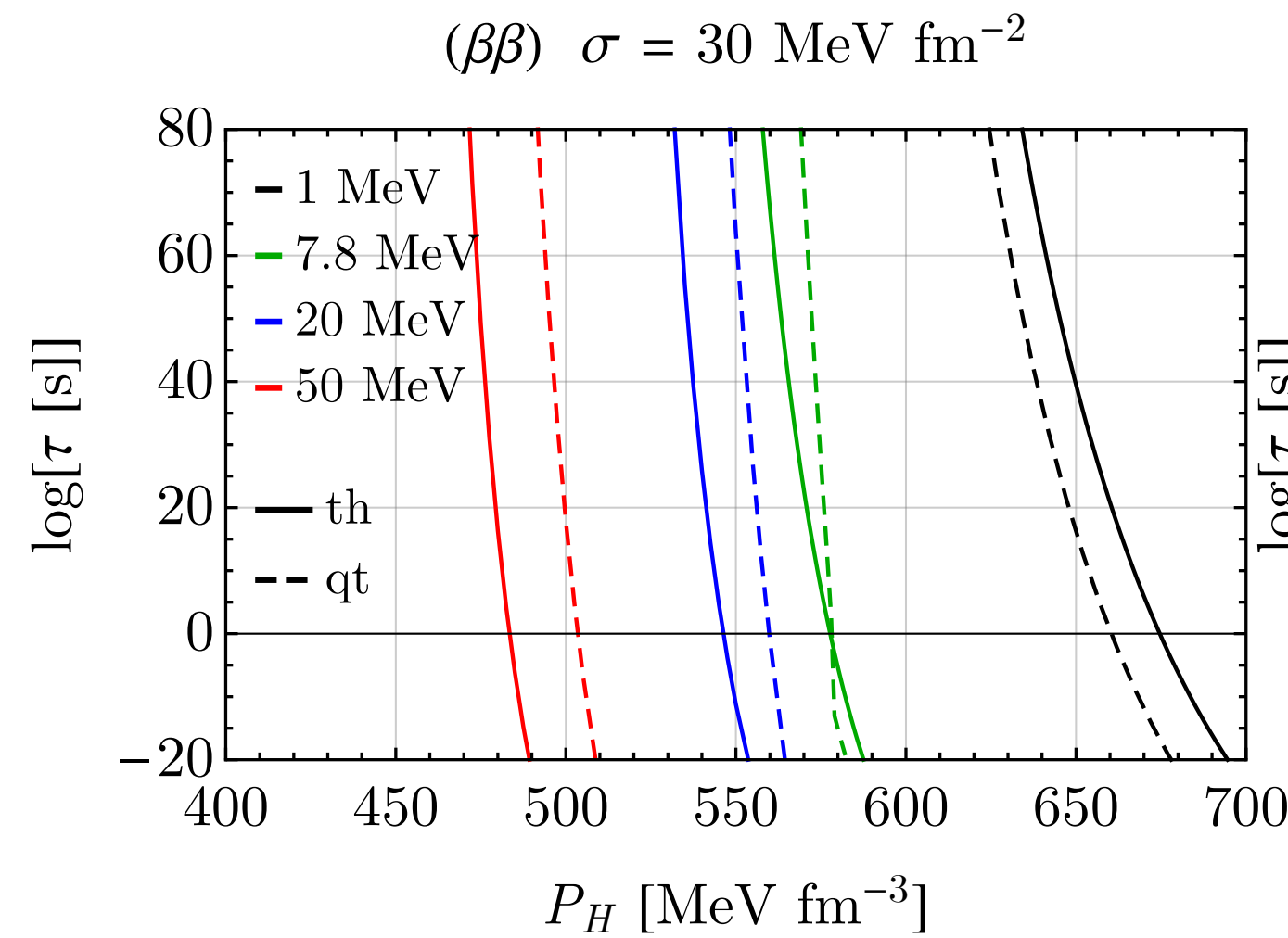
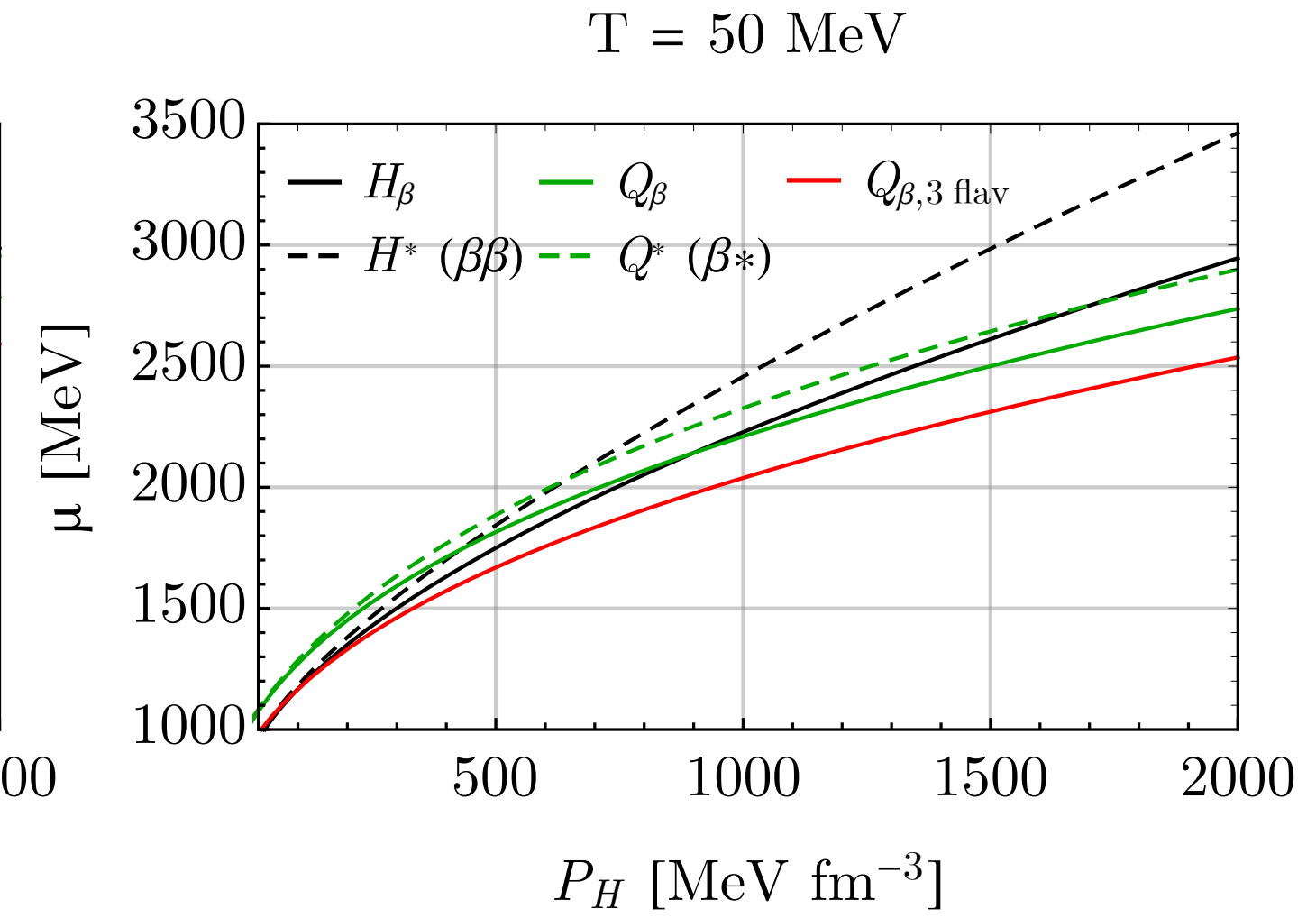
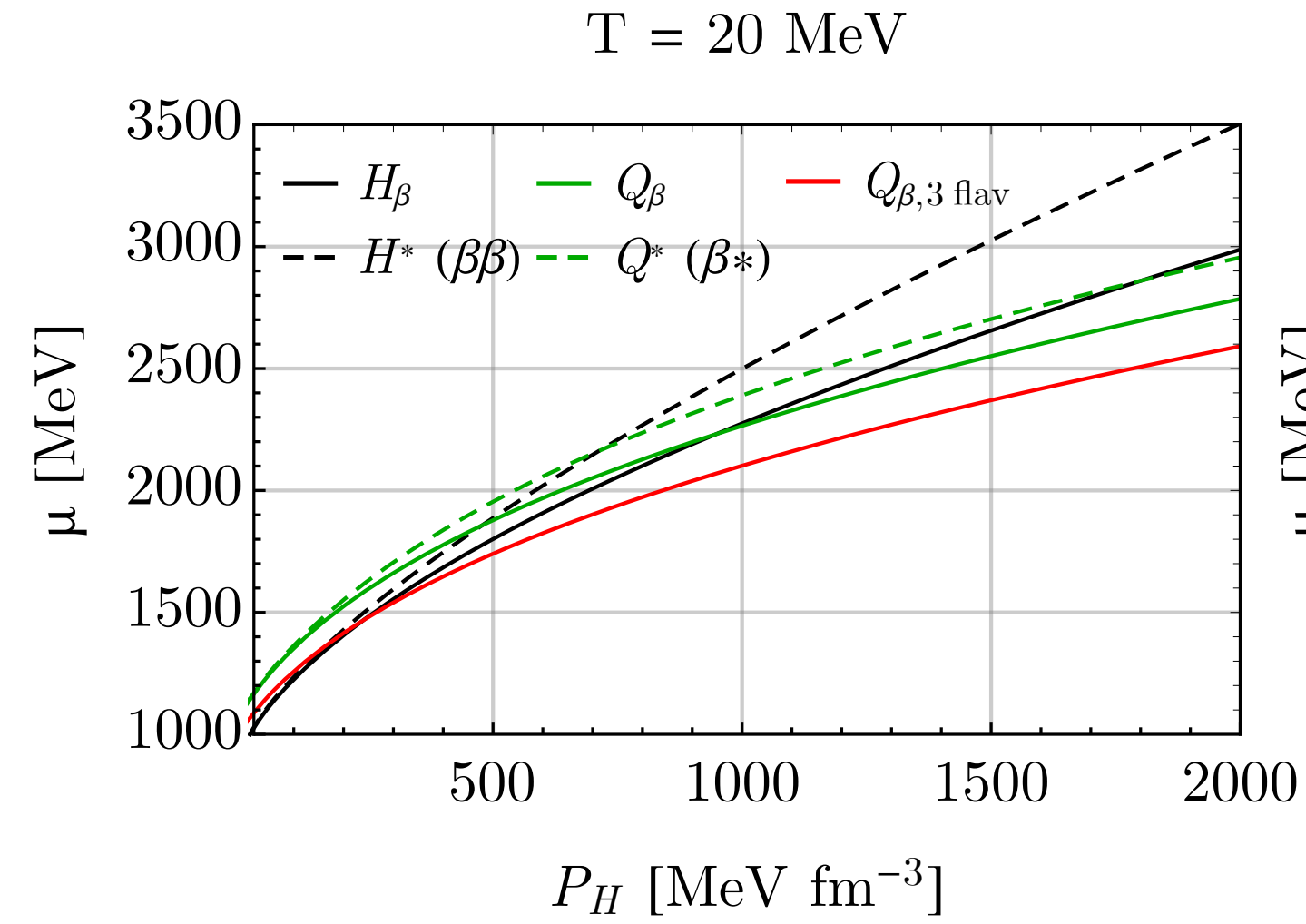
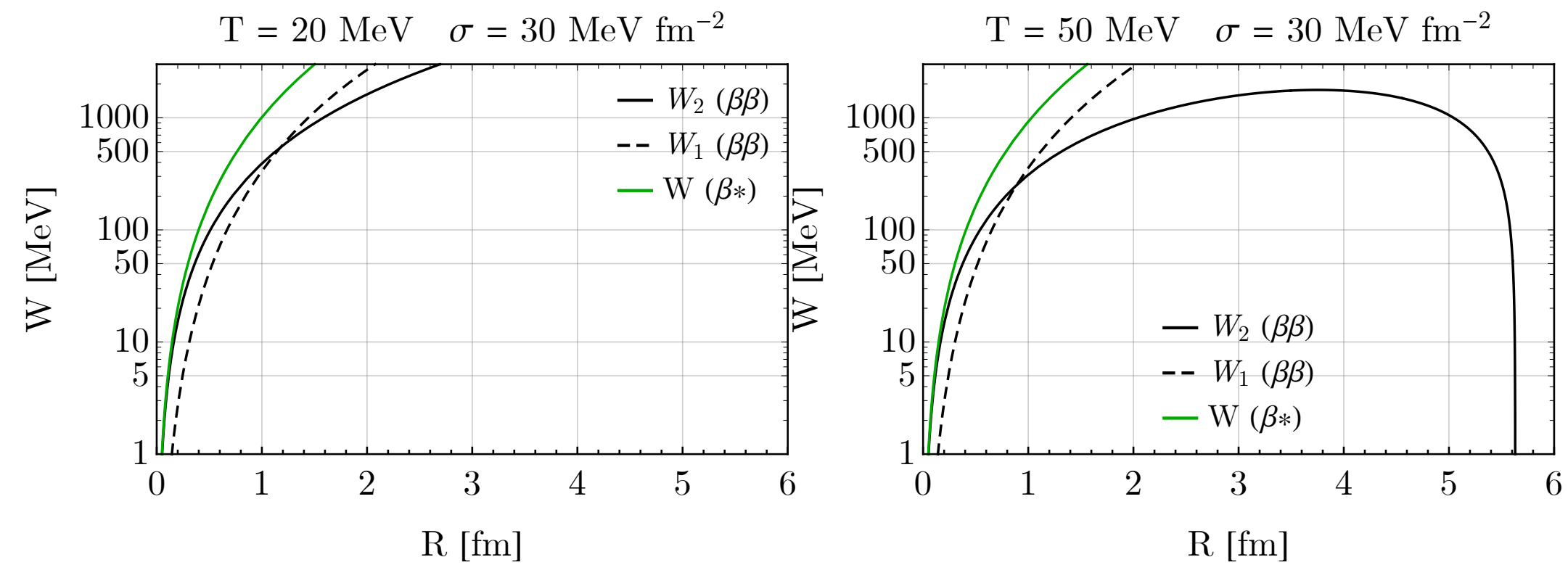
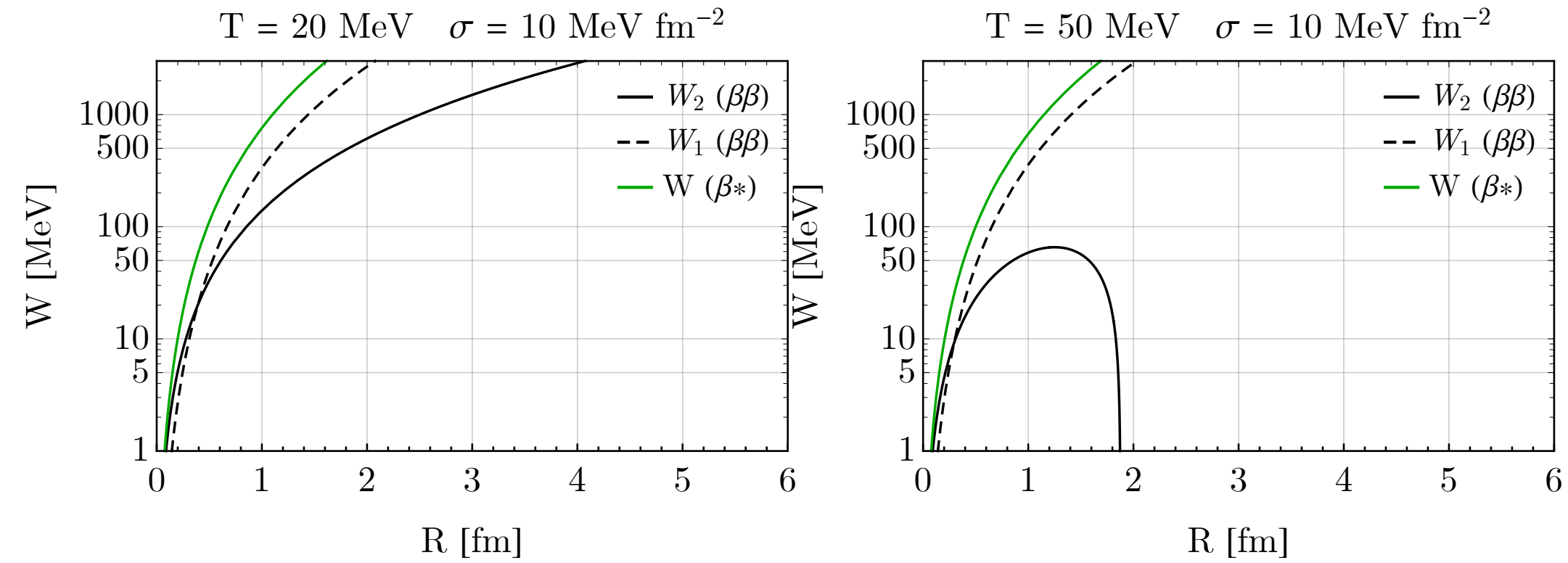
Backup: more on two flavors

$$\begin{aligned} W_1 &= n_{B,Q^*} V_{Q^*} \sum_i y_i^{H^*} \left(\mu_i^{H_\beta} - \mu_i^{H^*} \right) \\ &= n_{B,Q^*} \frac{4}{3} \pi R^3 \sum_i y_i^{H^*} \left(\mu_i^{H_\beta} - \mu_i^{H^*} \right). \end{aligned}$$

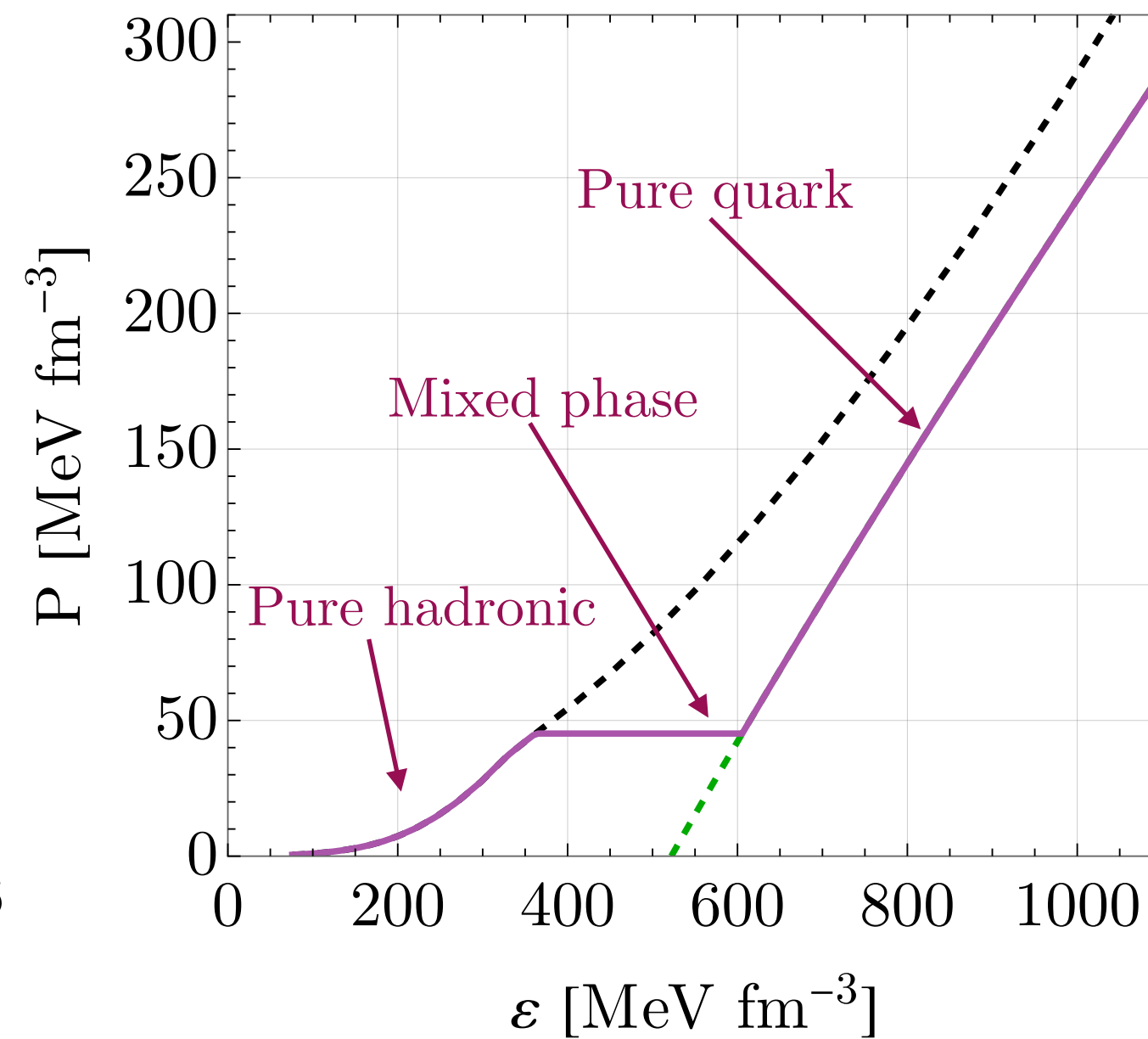
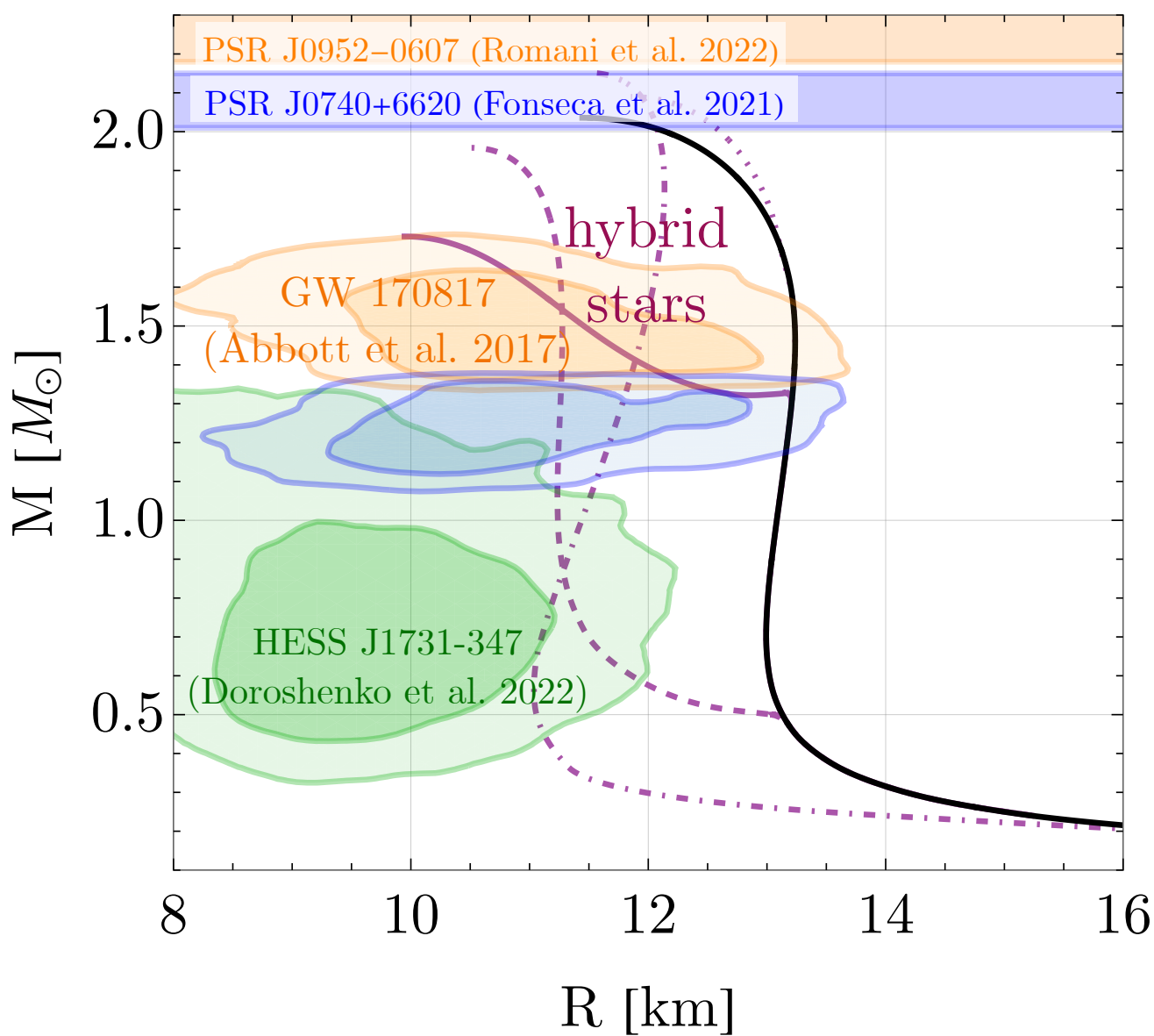
$$W_2 = \frac{4}{3} \pi R^3 n_{B,Q^*} (\mu_{Q^*} - \mu_{H^*}) + 4\pi\sigma R^2.$$

$$\tau^{th}(P_H, \{\Delta y_i\}, T) = \left[V_{nuc} \frac{\kappa}{2\pi} \Omega_0 \mathcal{P}_1^{th} \mathcal{P}_2^{th} \right]^{-1}$$

Backup: more on two flavors results



SQM in compact stars: one or two families?



[Constantinou et al. 2024]
(soon at finite temperature)

One family scenario

- deconfined quarks d.o.f. expected in massive compact stars
- hybrid stars**: SQM in the core and hadrons in the outer part
- 1st order phase transition, crossover, quarkyonic, ...

Maxwell C., Gibbs C., **mixed approach**

