

Measurement of the differential distributions of $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$ decay at LHCb

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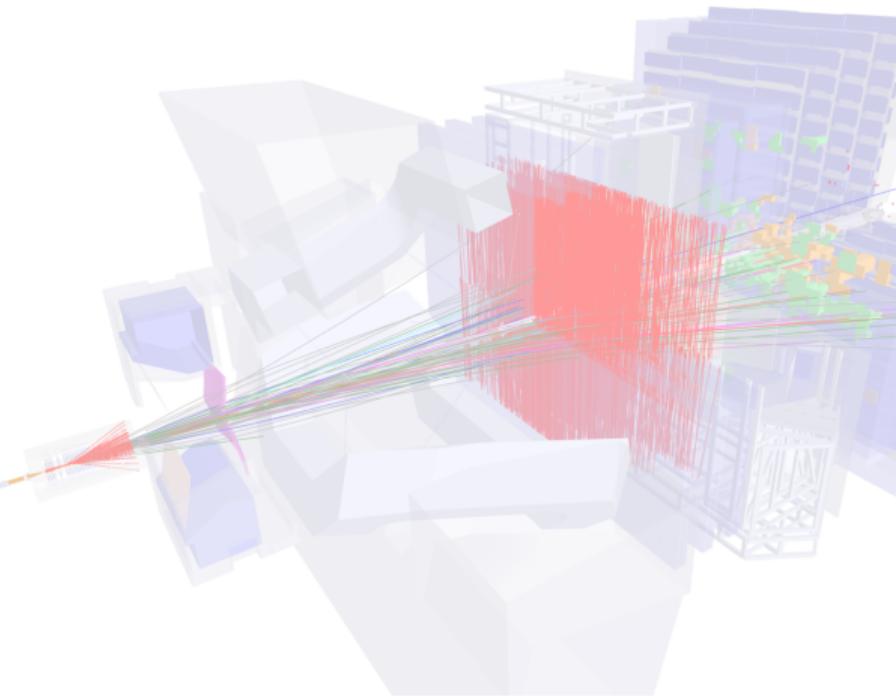
SL B decays at the junction of experiment and theory

Turin - June 13th, 2025

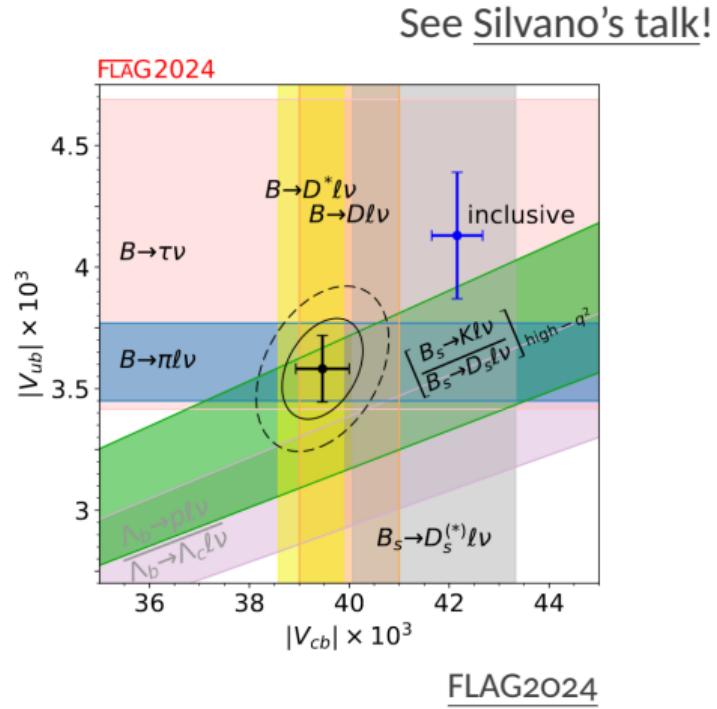
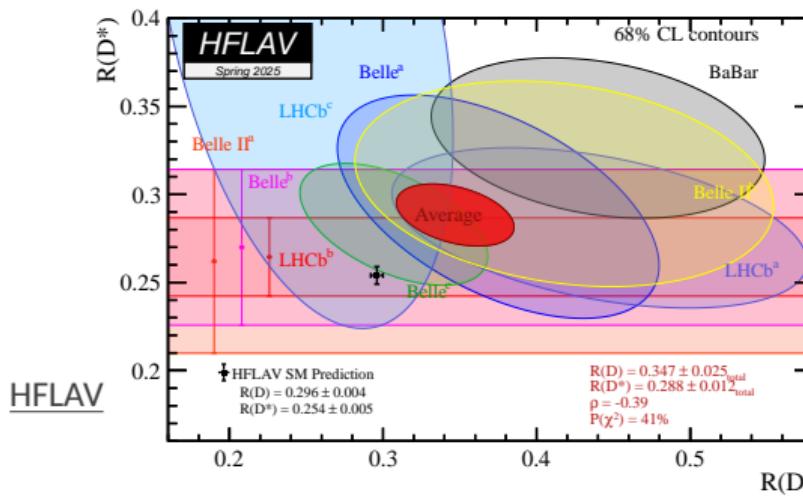


Outline

- Analysis introduction
- Event selection and background rejection
- Signal yields extraction
- Further studies
- Conclusions



We have **tensions** in inclusive/exclusive V_{ub} , V_{cb} determination and combined $\mathcal{R}(D)$ - $\mathcal{R}(D^*)$ measurement.

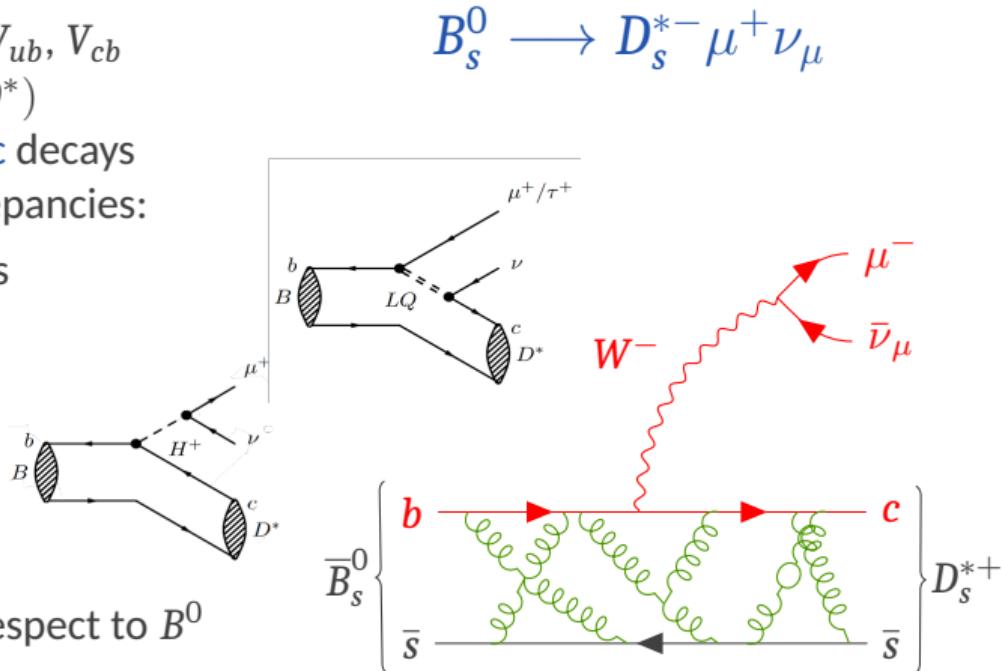


We have **tensions** in inclusive/exclusive V_{ub} , V_{cb} determination and combined $\mathcal{R}(D)$ - $\mathcal{R}(D^*)$ measurement. The study of **semileptonic** decays could help shedding light on these discrepancies:

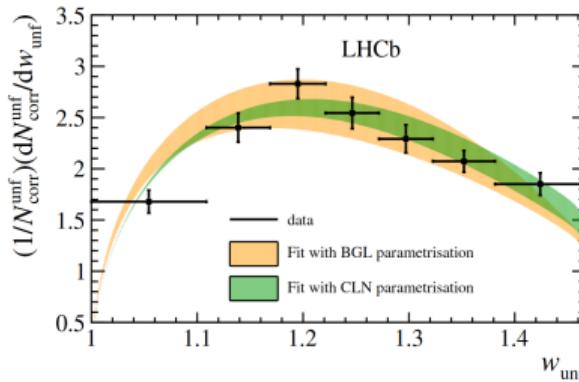
- only **one** diagram, **tree-level process**
- **EW** transition
- **QCD** interaction
- sensitivity to **New Physics**

Additionally:

- **simpler** lattice computations with respect to B^0 and B^+ (due to s quark)



- Previous analysis [JHEP12\(2020\)144](#) was published four years ago
- That was a 1-d analysis \Rightarrow this is a full angular analysis
- That used only 1.7 fb^{-1} \Rightarrow here full **Run 2** data, $\sim 5.7 \text{ fb}^{-1}$



$$w \propto -q^2 \\ \propto (p_{B_s^0} - p_{D_s^*})^2$$

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH (CERN)



CERN-EP-2020-026
LHCb-PAPER-2019-046
January 14, 2021

Measurement of the shape of the $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$ differential decay rate

arXiv:2003.08453v3 [hep-ex] 13 Jan 2021

LHCb collaboration[†]

Abstract

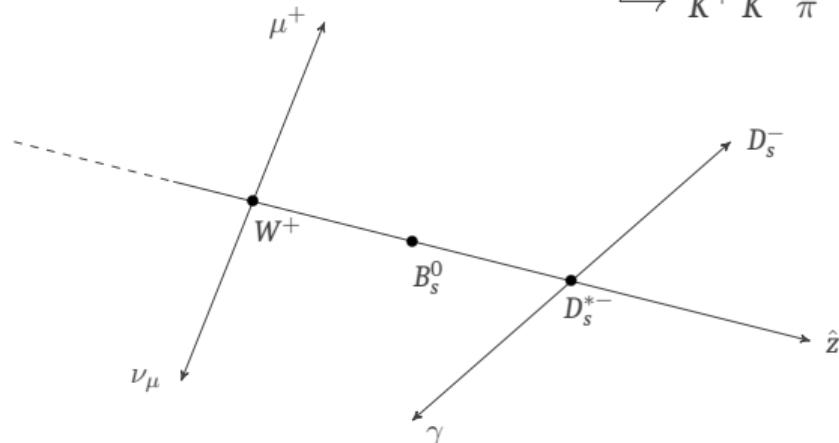
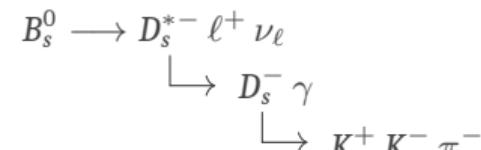
The shape of the $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$ differential decay rate is obtained as a function of the hadron recoil parameter using proton-proton collision data at a centre-of-mass energy of 13 TeV , corresponding to an integrated luminosity of 1.7 fb^{-1} collected by the LHCb detector. The $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$ decay is reconstructed through the decays $D_s^{*-} \rightarrow D_s^- \gamma$ and $D_s^- \rightarrow K^- K^+$. The differential decay rate is fitted with the Cepeda-Lokhtin-Nefkens (CLN) and Boyd-Grinstein-Lobitz (BGL) parametrisations of the form factors, and the relevant quantities for both are extracted.

Published in JHEP 12 (2020) 144

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[†]Authors are listed at the end of this paper.

The analysis aims to measure the **differential decay rate** in the space given by the variables that describe the decay kinematics:

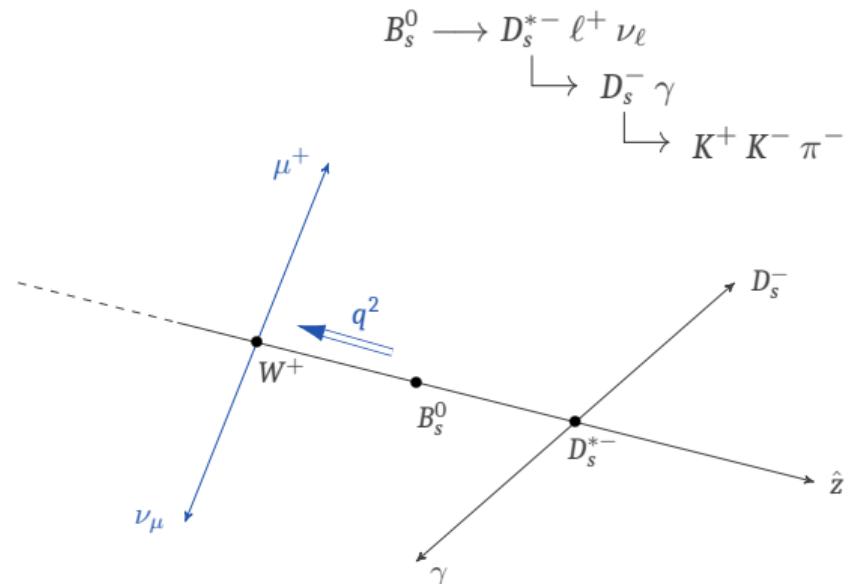


$$\hat{z} = \vec{p}_{D_s^*} / |\vec{p}_{D_s^*}|$$

The analysis aims to measure the **differential decay rate** in the space given by the variables that describe the decay kinematics:

$$q^2$$

$$q^2 = (p_{B_s^0} - p_{D_s^{*-}})^2$$



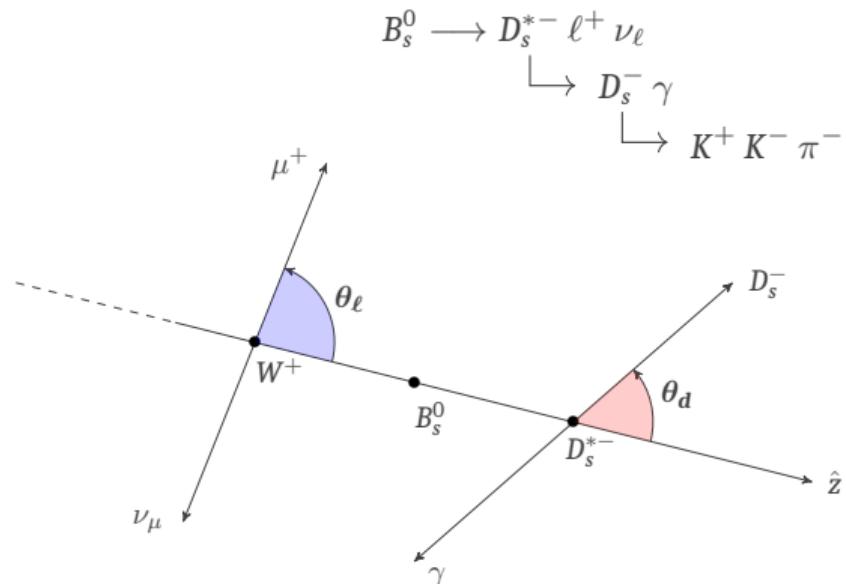
$$\hat{\mathbf{z}} = \vec{p}_{D_s^{*-}} / |\vec{p}_{D_s^{*-}}|$$

The analysis aims to measure the **differential decay rate** in the space given by the variables that describe the decay kinematics:

$$q^2 \quad \theta_\ell \quad \theta_d$$

$$q^2 = (p_{B_s^0} - p_{D_s^{*-}})^2$$

θ_ℓ and θ_d are helicity angles



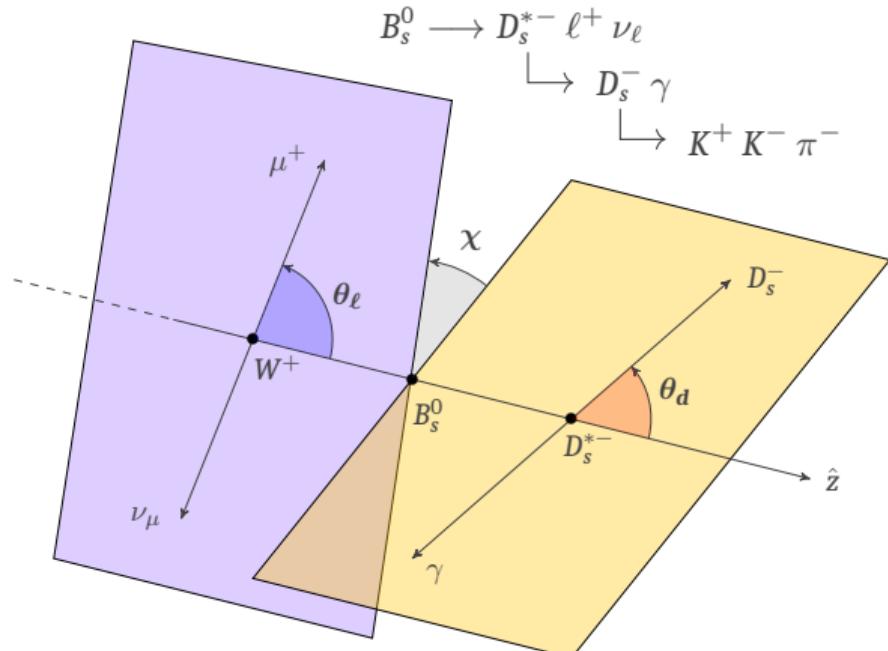
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The analysis aims to measure the **differential decay rate** in the space given by the variables that describe the decay kinematics:

$$q^2 \quad \theta_\ell \quad \theta_d \quad \chi$$

$$q^2 = (p_{B_s^0} - p_{D_s^*})^2$$

θ_ℓ and θ_d are helicity angles
 χ angle between decay planes



$$\hat{z} = \vec{p}_{D_s^*} / |\vec{p}_{D_s^*}|$$



The differential decay width

Analysis introduction

LHCb
FHCb

$$\frac{d\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_d d\chi} \propto \sum_i I_i(q^2) \Xi_i(\theta_\ell, \theta_d, \chi)$$

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- $I_i(q^2)$ functions encode the hadronic interaction: we use CLN and BGL¹ models to parametrise their expressions, or fit them with a model-independent approach

¹Caprini-Lellouch-Neubert and Boyd-Grinstein-Lebed

$$\frac{d\Gamma}{dq^2 d \cos \theta_\ell d \cos \theta_d d\chi} \propto \sum_i I_i(q^2) \Xi_i(\theta_\ell, \theta_d, \chi)$$

- $I_i(q^2)$ functions encode the hadronic interaction: we use CLN and BGL¹ models to parametrise their expressions, or fit them with a model-independent approach
 - * Modifying the $I_i(q^2)$ functions and considering a New Physics coupling constant ϵ_{NP} , different structures for NP can be implemented:

$$I_i(q^2) \implies I_i(q^2, \epsilon_{NP})$$

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- $\Xi_i(\theta_\ell, \theta_d, \chi)$ are known functions of the angular variables

¹Caprini-Lellouch-Neubert and Boyd-Grinstein-Lebed

Events selection :

- $D_s^\pm \rightarrow K^+ K^- \pi^\pm$ selection, ϕ and K^* resonances
- $D_s^* \rightarrow D_s \gamma$ reconstruction, soft γ selection
- charge of the identified muon **opposite** to that of D_s^*
- **muon** trigger lines
 - ★ mu_L0MuonDecision_TOS
 - ★ mu_Hlt1TrackMuonDecision_TOS
 - ★ Bs_0_Hlt2XcMuXForTauB2XcMuDecision_TOS
- cuts on muon $p_\mu^T > 1.2$ GeV and $\text{PID}_\mu > 2$

Particle	Variable	Cut
π^\pm, K^\pm	p_T	> 200 MeV
	p	> 5 GeV
	χ_{IP}^2	> 9
π^\pm	$\text{DLL}_{K\pi}$	< 4
K^\pm	$\text{DLL}_{K\pi}$	> 2
D_s^+	$m_{D_s^+}$	(1920, 2010) MeV
	Min of daughters p_T	> 800 MeV
	Sum of daughters p_T	> 2500 MeV
	$D_s^+ \min p_T$	> 2000 GeV
	Distance of closest approach	< 0.1 mm
	Vertex displacement	$\text{VD}\chi^2 > 25$
	Vertex fit χ^2	< 10
	Direction angle	> 0.999
	$m_{D_s^+ \mu^-}$	< 10.5 GeV
B_s^0	Distance of closest approach	< 0.5 mm
	Vertex displacement	$\text{VD}\chi^2 > 50$
	Vertex fit χ^2	< 15
	Direction angle	> 0.999

We consider several background channels, which are rejected with:

- $s\mathcal{P}lot$ to evaluate and subtract combinatorial background for the photon emitted by D_s^*
- cut on dedicated variable to suppress the doubly-charmed decays ($H_b \rightarrow D_s^* H_c$)

Channels

$$B_s^0 \rightarrow D_s^{*-} \tau^+ \nu_\tau$$

$$B_s^0 \rightarrow D_{s1} \mu \nu_\mu$$

$$B_s^0 \rightarrow D_{s1} \tau \nu_\tau$$

$$B^0 \rightarrow D_s^{*+} D^{(*)-}$$

$$B_s^0 \rightarrow D_s^{*+} D_s^{(*)-}$$

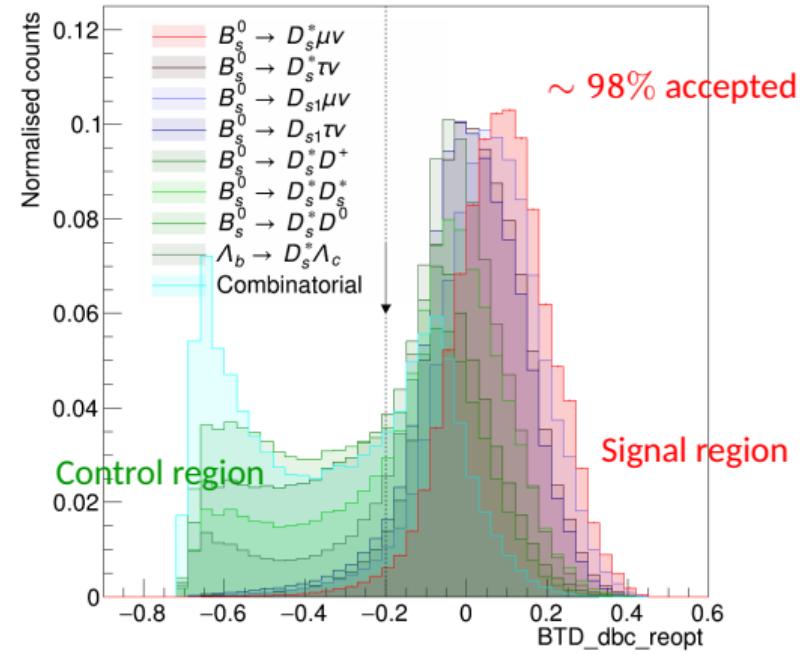
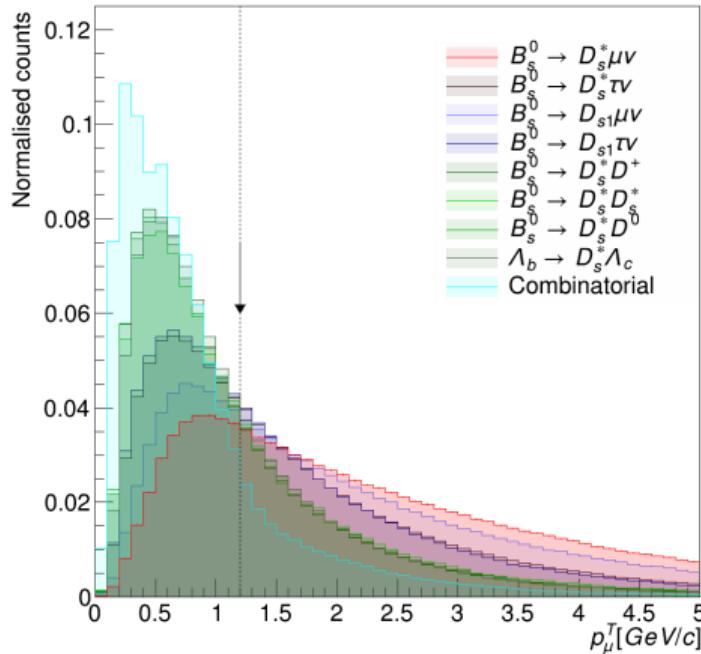
$$B^+ \rightarrow D_s^{*+} \bar{D}^{*0}$$

$$\Lambda_b \rightarrow D_s^{*-} \Lambda_c^{(*)+}$$

Combinatorial + misID

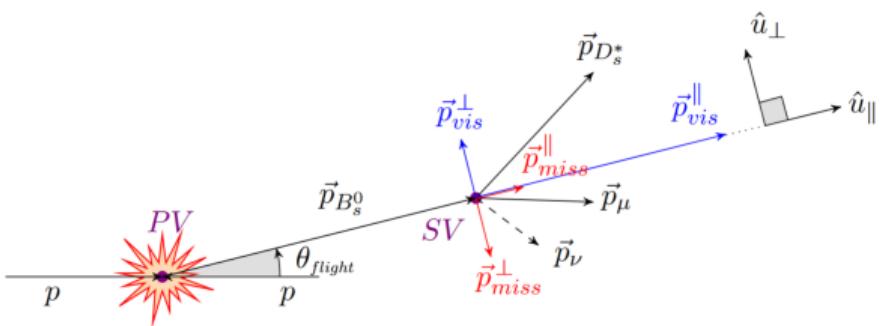
Background rejection: cuts examples

Event selection and background rejection



Experimental challenge: kinematics reconstruction

Event selection and background rejection

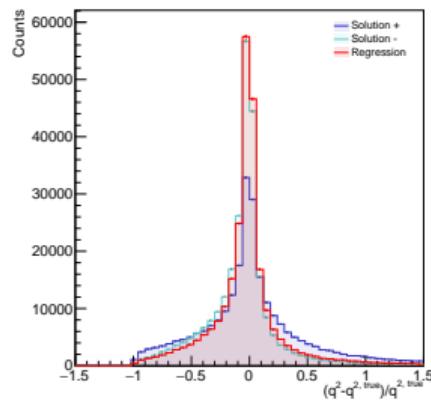


We assume there is only one missing particle in the final state and that $m_{B_s^0}$ is known (see [JHEP02\(2017\)021](#))

$$\Rightarrow \text{Two fold ambiguity, } p_\pm = p_{\text{vis}}^\parallel - a \pm \sqrt{r}$$

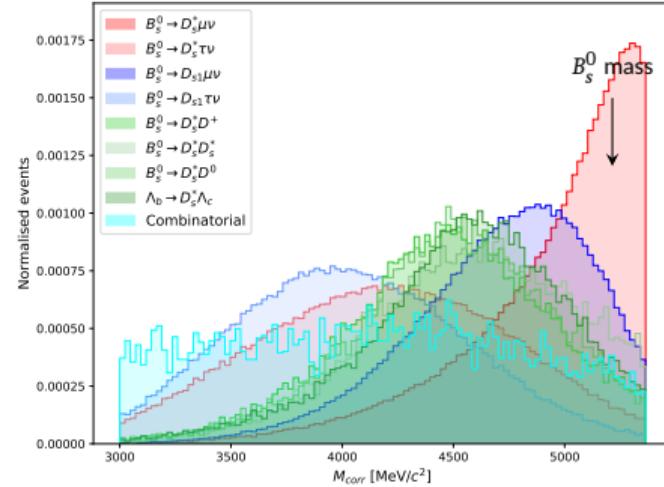
Regression algorithm gives a rough estimate of $p_{B_s^0}$, we resolve the ambiguity using

$$\Delta_\pm = (p_{\text{reg}} - p_\pm)$$



Extract signal yields using

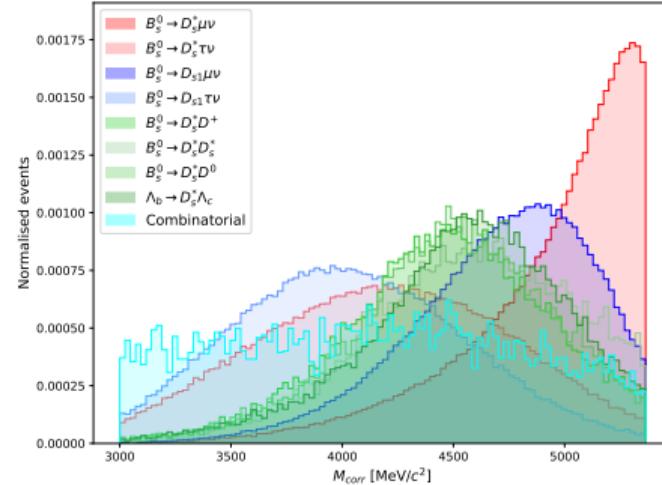
$$M_{corr} = \sqrt{m_{D_s^* \mu}^2 + |p_{miss}^\perp|^2 + |p_{miss}^\perp|}$$



Extract signal yields using

$$M_{corr} = \sqrt{m_{D_s^* \mu}^2 + |\vec{p}_{miss}^\perp|^2} + |\vec{p}_{miss}^\perp|$$

Template binned fit over 4-d space,
extrapolation in three steps:



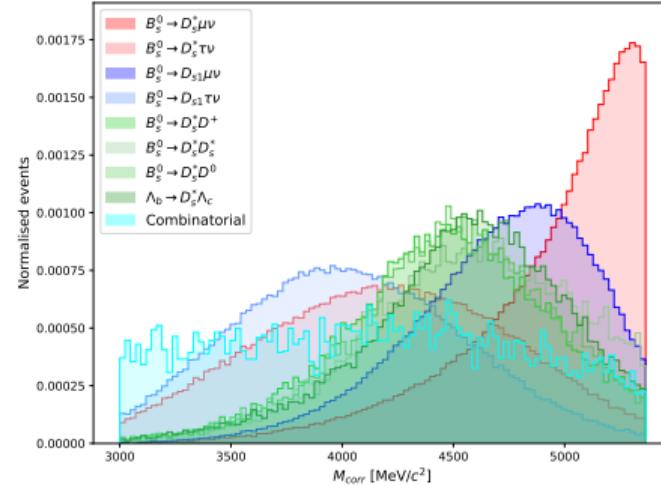
Variable	Bin Edges						Bins	
q^2 [GeV 2]	0.	1.83	3.67	5.5	7.33	9.17	11.	6
$\cos \theta_\ell$	-1.	-0.5	0.	1.				3
$\cos \theta_d$	-1.	-0.5	0.	1				3
χ [rad]	0.	1.26	2.51	3.77	5.03	6.28		5

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- preliminary fit in the control region to constrain backgrounds



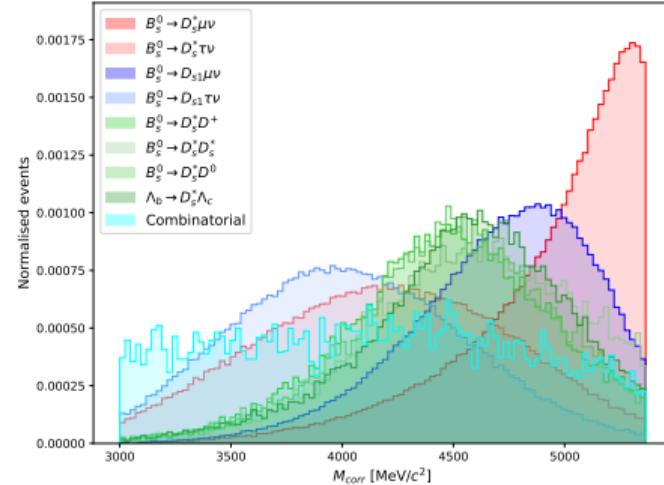
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Template binned fit over 4-d space,
extrapolation in three steps:

- preliminary fit in the control region to constrain backgrounds
- simultaneous fit over q^2 bins, integrating the angles



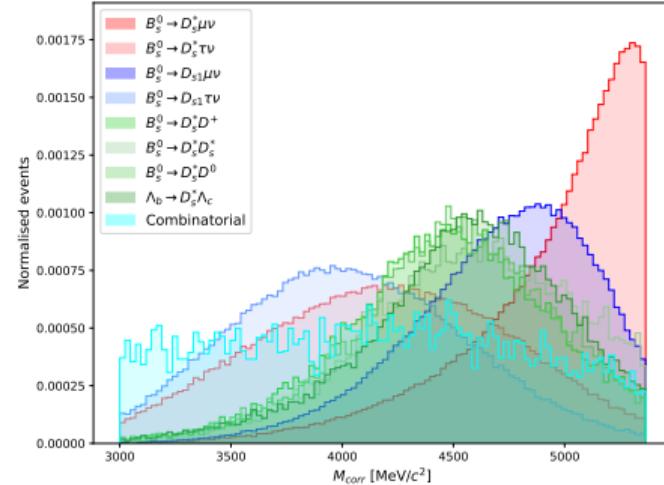
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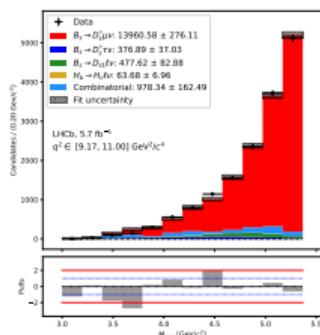
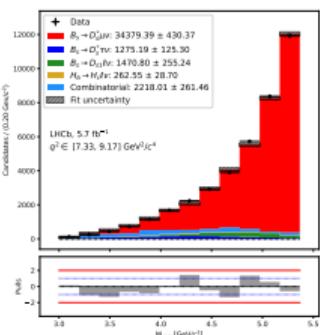
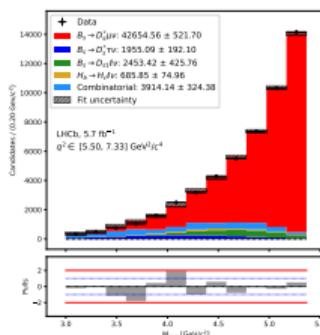
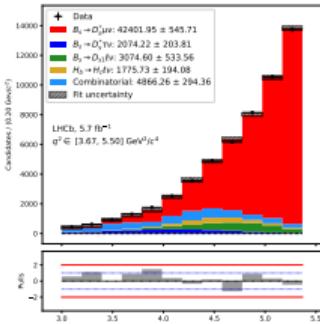
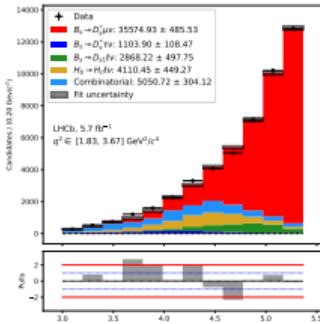
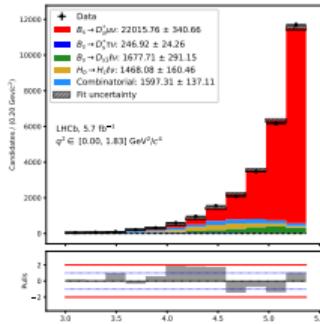
- preliminary fit in the control region to constrain backgrounds
- simultaneous fit over q^2 bins, integrating the angles
- second fit over all bins, fixing background templates



Variable	Bin Edges						Bins	
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The M_{corr} fit: q^2 results in the signal region

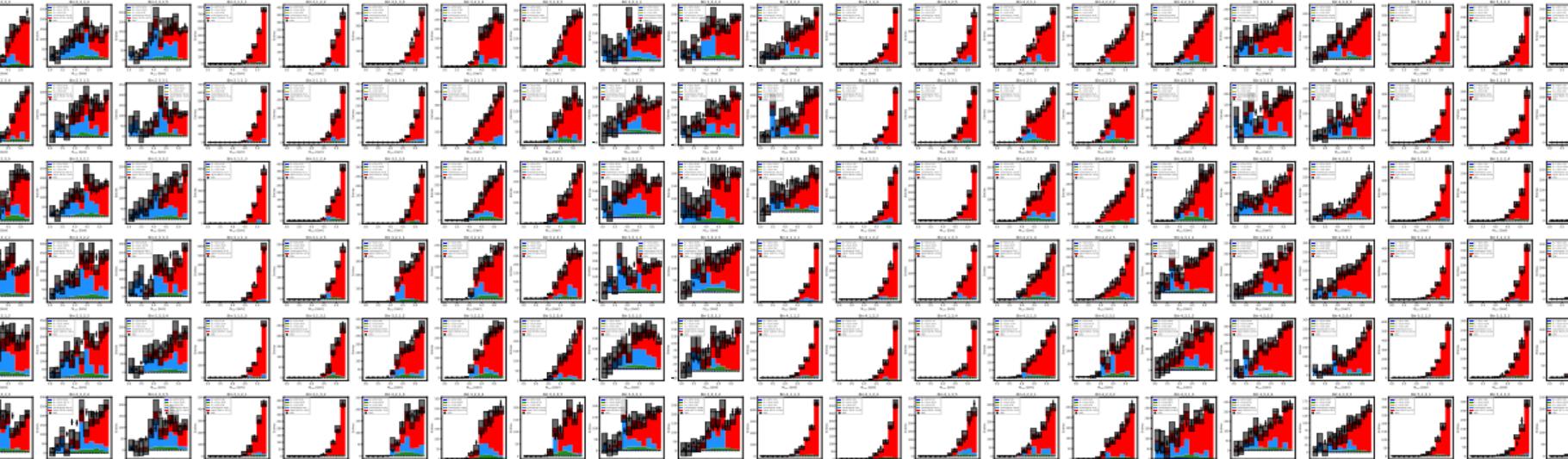
Signal yields extraction



$q^2 [\text{GeV}^2/\text{c}^4]$	Signal [%]
[0, 1.83]	82
[1.83, 3.67]	73
[3.67, 5.50]	81
[5.50, 7.33]	83
[7.33, 9.17]	87
[9.17, 11]	88

The M_{corr} fit: examples

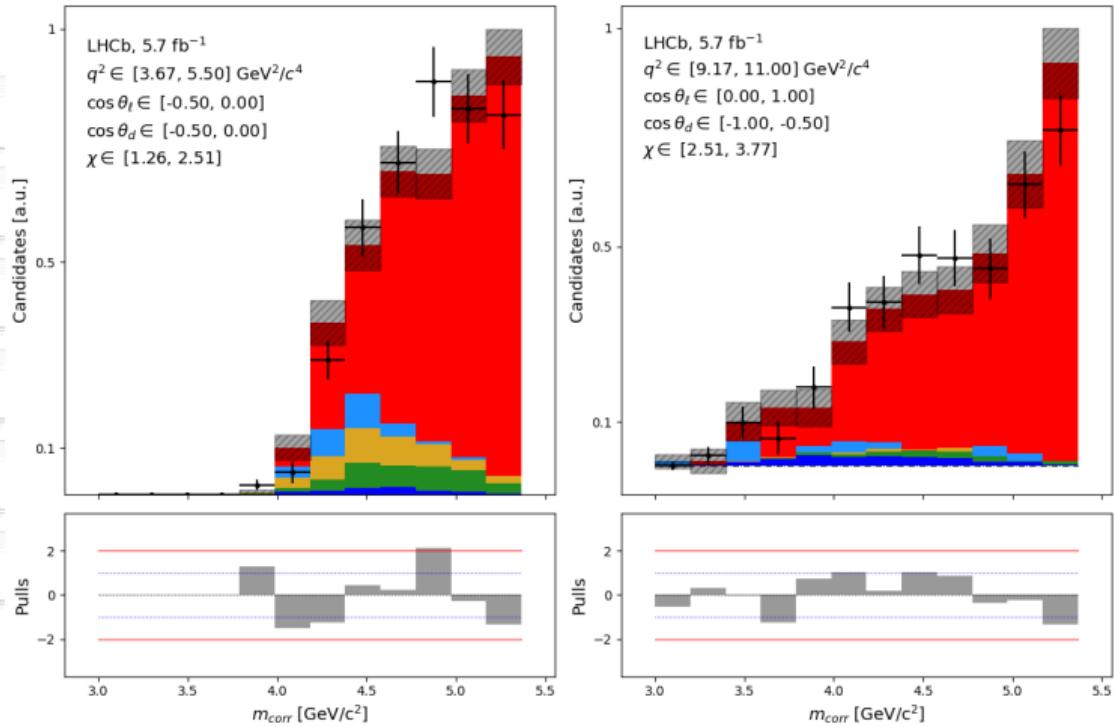
Signal yields extraction



Well, it's impossible to visualize them all...

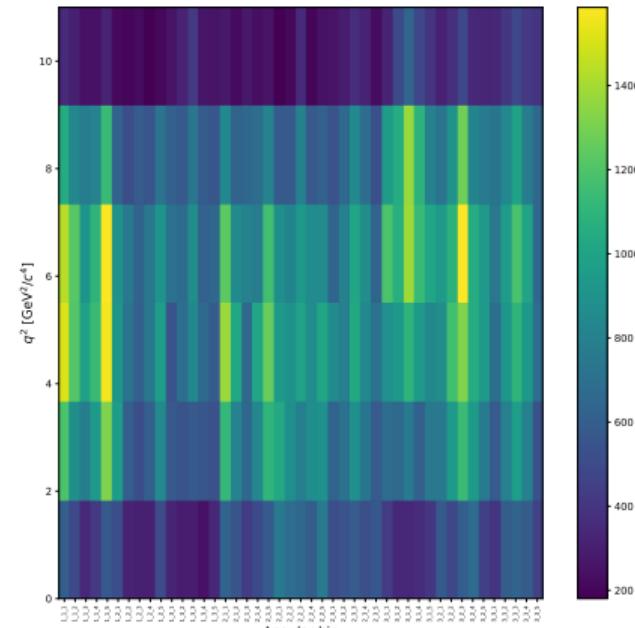
The M_{corr} fit: examples

Signal yields extraction



Once we extract the signal yield distribution, we can:

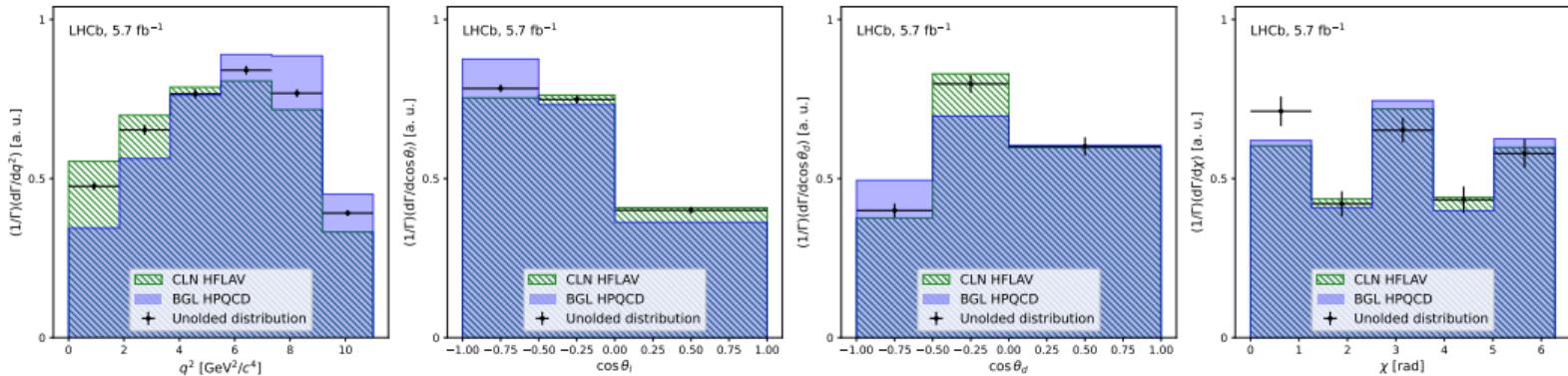
- Unfold the distribution with **migration matrix + efficiency vector** to account for detector effects
- Compare the unfolded distribution with **theory/other experiments**
- Use the unfolded distribution to perform a **model-independent** fit to extract $I_i(q^2)$ functions



Angular bin: $\cos \theta_\ell - \cos \theta_d - \chi$

Unfolded distributions vs predictions

Further studies



- Models used: HFLAV averages for CLN, HPQCD predictions for BGL
- Visible tension in some bins
- Something similar was observed comparing Belle data with HPQCD predictions, but with different binning and with $B^0 \rightarrow D^*$

Folded fit

$$\chi^2 = \left(\vec{N}^{\text{meas}} - \vec{N}^{\text{pred}} \right)^T \frac{1}{C(N^{\text{meas}})} \left(\vec{N}^{\text{meas}} - \vec{N}^{\text{pred}} \right)$$

where

$$N_i^{\text{pred}} = k \cdot \sum_{j=1}^t m_{ij} \cdot (\Delta\Gamma(\vec{p}) \cdot \mathcal{E})_j \quad (\Delta\Gamma(\vec{p}) \cdot \mathcal{E})_j = \Delta\Gamma_j(\vec{p}) \cdot \mathcal{E}_j$$

$\Delta\Gamma$ = expected yields distribution \vec{p} = CLN/BGL parameters

Unfolded fit

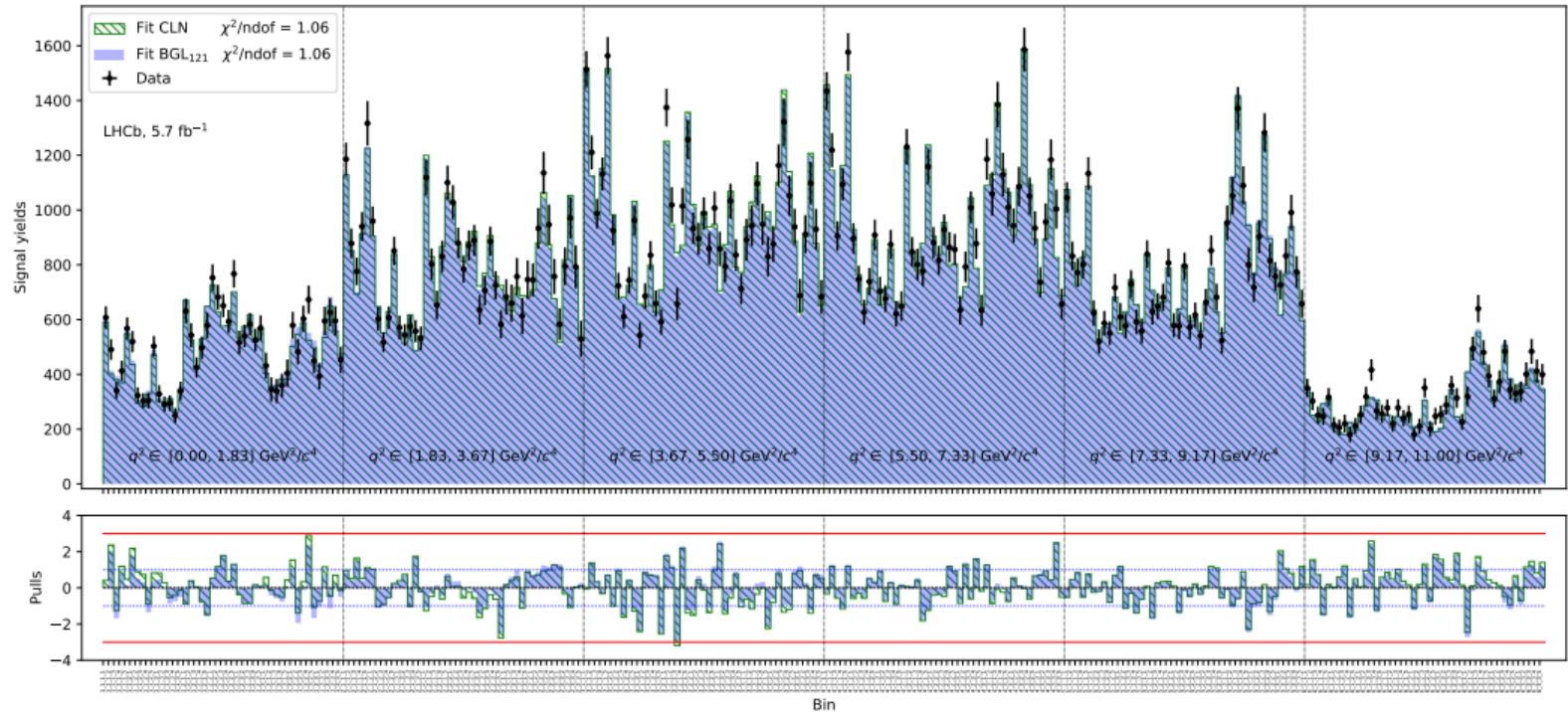
$$\chi^2 = \left(\vec{N}^{\text{unf}} / \mathcal{E} - k \cdot \Delta\Gamma(\vec{p}) \right)^T \frac{1}{C(N^{\text{unf}})} \left(\vec{N}^{\text{unf}} / \mathcal{E} - k \cdot \Delta\Gamma(\vec{p}) \right)$$

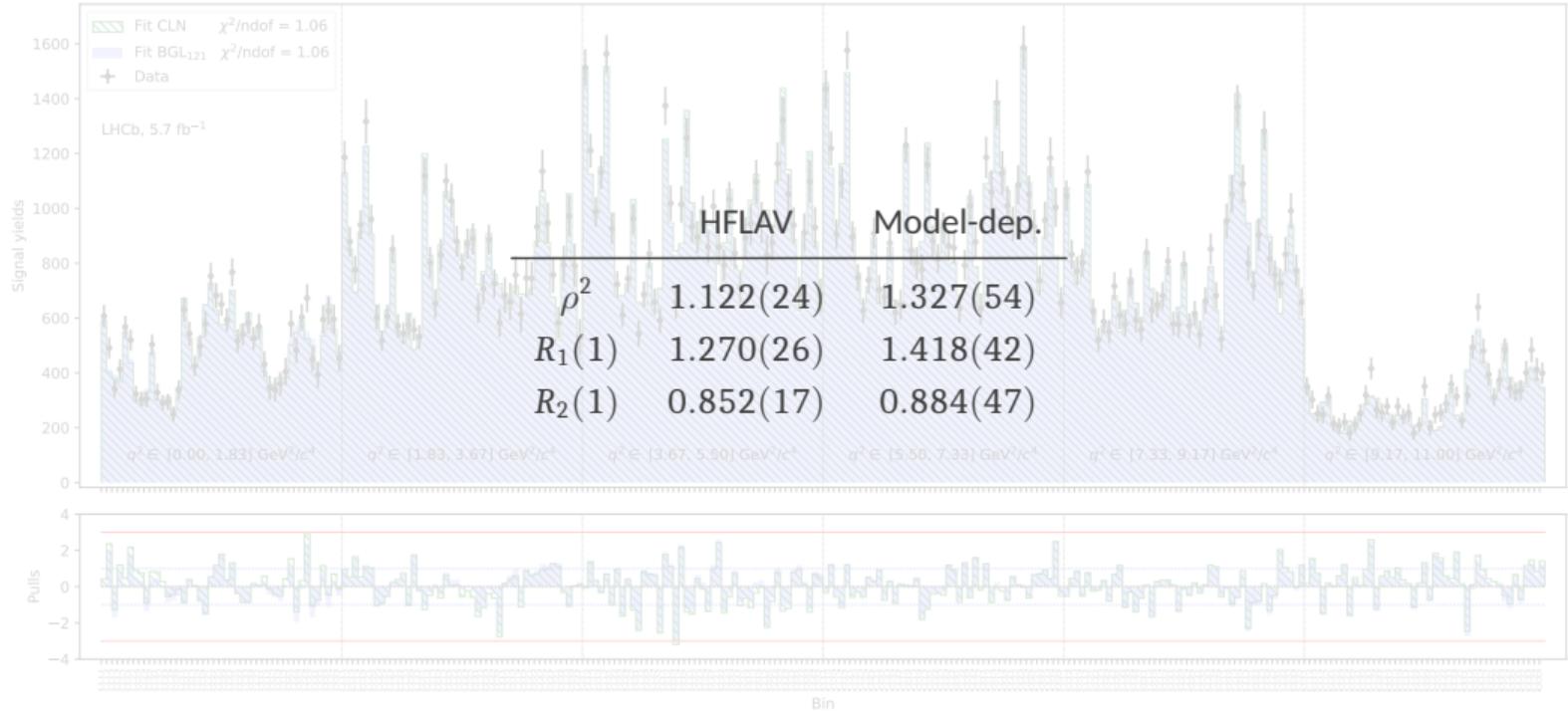
where

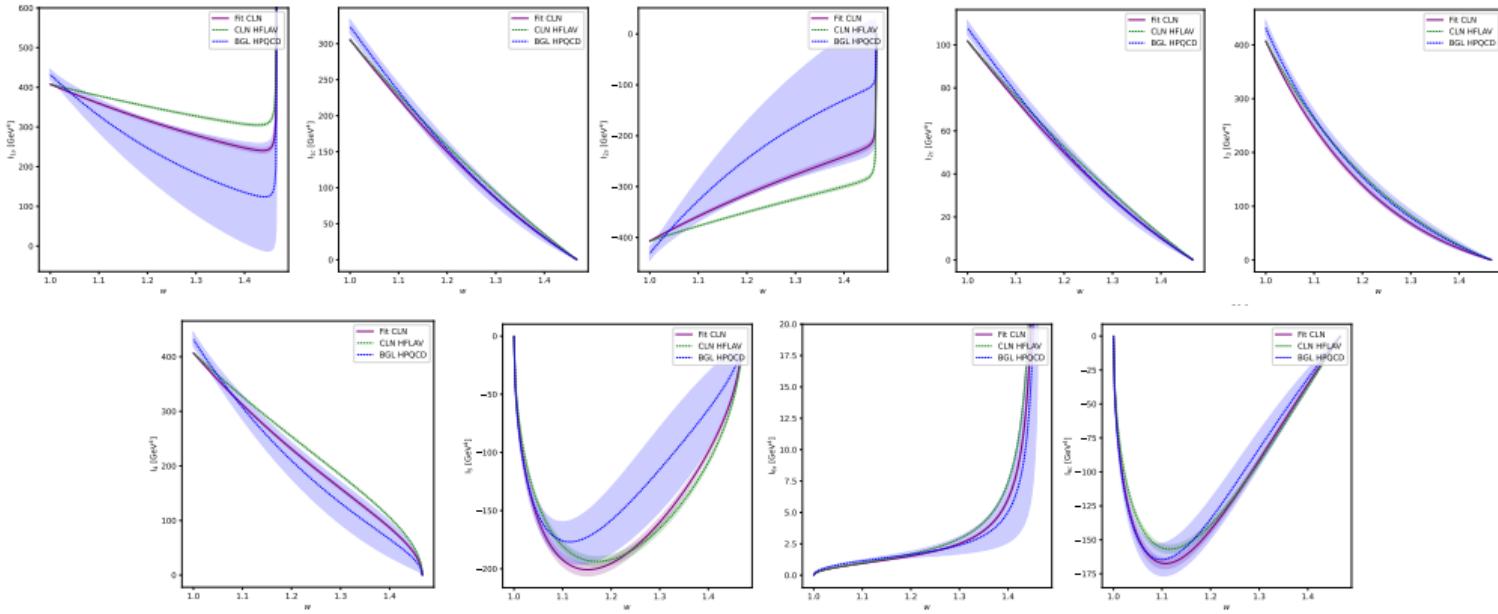
\vec{N}^{unf} is obtained using Bayesian unfolding

CLN and BGL from differential distribution

Further studies







We can explicitly fit the $I_i(q^2)$ functions integrated over the q^2 bins, without any assumption on the hadronic model:

$$N_{\textcolor{green}{k}, \textcolor{red}{p}, \textcolor{red}{q}, \textcolor{red}{r}}^{\text{pred}} = \int_{\Delta q_k^2} \int_{\Delta \cos \theta_{\ell \textcolor{red}{p}}} \int_{\Delta \cos \theta_{d \textcolor{red}{q}}} \int_{\Delta \chi \textcolor{red}{r}} \frac{d\Gamma}{dq^2 d \cos \theta_\ell d \cos \theta_d d\chi} dq^2 d \cos \theta_\ell d \cos \theta_d d\chi$$

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 N_{\textcolor{green}{k}, \textcolor{red}{p}, \textcolor{red}{q}, \textcolor{red}{r}}^{\text{pred}} &= \int_{\Delta q_k^2} \int_{\Delta \cos \theta_{\ell_p}} \int_{\Delta \cos \theta_{d_q}} \int_{\Delta \chi_r} \frac{d\Gamma}{dq^2 d \cos \theta_\ell d \cos \theta_d d\chi} dq^2 \overbrace{d \cos \theta_\ell d \cos \theta_d d\chi}^{d\Omega} \\
 &\propto \sum_i \int_{\Delta q_k^2} \left(1 - m_\mu^2/q^2\right)^2 |\vec{p}_{D_s^*}(q^2)| I_i(q^2) dq^2 \cdot \int_{\Delta \Omega_l} \Xi_i(\theta_\ell, \theta_d, \chi) d\Omega
 \end{aligned}$$

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$$\begin{aligned}
 N_{\text{pred}}^{\text{pred}} &= \int_{\Delta q_k^2} \int_{\Delta \cos \theta_{\ell p}} \int_{\Delta \cos \theta_{d q}} \int_{\Delta \chi_r} \frac{d\Gamma}{dq^2 d \cos \theta_{\ell} d \cos \theta_d d\chi} dq^2 \overbrace{d \cos \theta_{\ell} d \cos \theta_d d\chi}^{d\Omega} \\
 &\propto \sum_i \int_{\Delta q_k^2} \left(1 - m_{\mu}^2/q^2\right)^2 |\vec{p}_{D_s^*}(q^2)| I_i(q^2) dq^2 \cdot \int_{\Delta \Omega_l} \Xi_i(\theta_{\ell}, \theta_d, \chi) d\Omega \\
 &\propto \sum_i J_{i,k}(q^2) \cdot \zeta_{i,l}(\theta_{\ell}, \theta_d, \chi)
 \end{aligned}$$

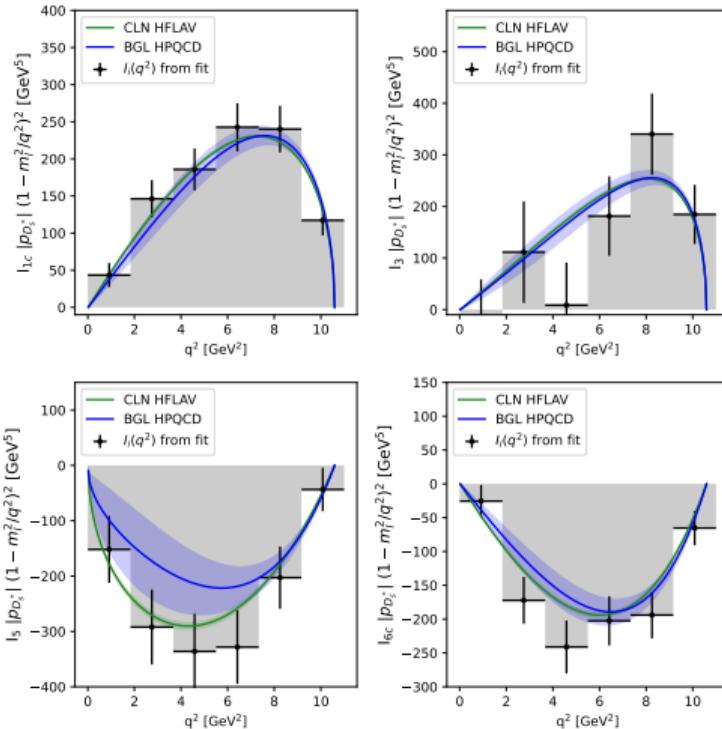
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q^2 bins $I_i(q^2)$ functions

where $\zeta_{i,l}(\theta_{\ell}, \theta_d, \chi)$ are analytically computable. We have $\sim 6 \times 10$ free parameters. After the fit we can extract CLN/BGL parameters from the $J_i(q^2)$ shapes.

Model-independent $I_i(q^2)$ determination

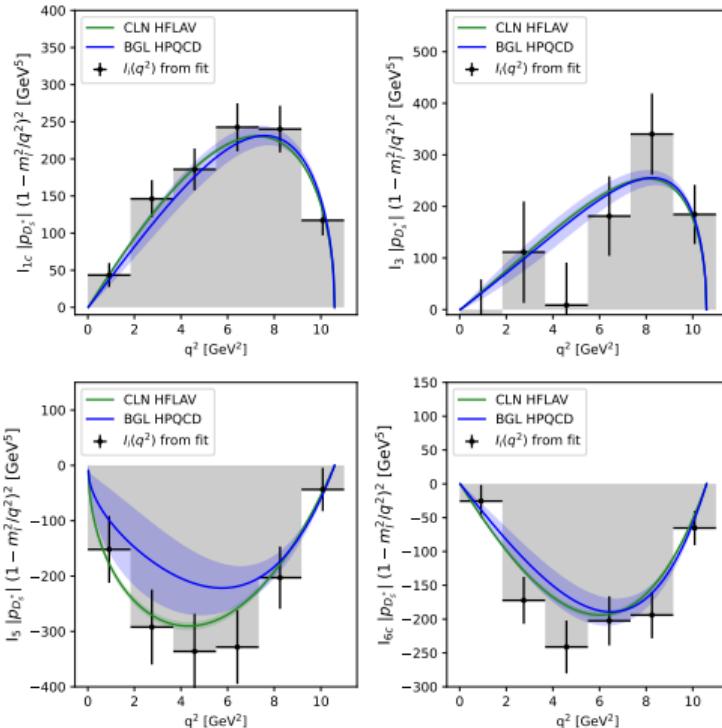
Further studies



$$\begin{aligned} \frac{d\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_d d\chi} &= \mathcal{K}(q^2) \sum_i I_i(q^2) \Xi_i(\theta_\ell, \theta_d, \chi) \\ &\propto \left[I_{1s} \sin^2 \theta_d + I_{1c} (3 + \cos 2\theta_d) + I_{2s} \sin^2 \theta_d \cos 2\theta_\ell \right. \\ &\quad + I_{2c} (3 + \cos 2\theta_d) \cos 2\theta_\ell + I_3 \sin^2 \theta_d \sin^2 \theta_\ell \cos 2\chi \\ &\quad + I_4 \sin 2\theta_d \sin 2\theta_\ell \cos \chi + I_5 \sin 2\theta_d \sin \theta_\ell \cos \chi \\ &\quad + I_{6s} \sin^2 \theta_d \cos \theta_\ell + I_{6c} (3 + \cos 2\theta_d) \cos \theta_\ell \\ &\quad \left. + I_7 \sin 2\theta_d \sin \theta_\ell \sin \chi + I_8 \sin 2\theta_d \sin 2\theta_\ell \sin \chi \right. \\ &\quad \left. + I_9 \sin^2 \theta_d \sin^2 \theta_\ell \sin 2\chi \right] \end{aligned}$$

Model-independent $I_i(q^2)$ determination

Further studies

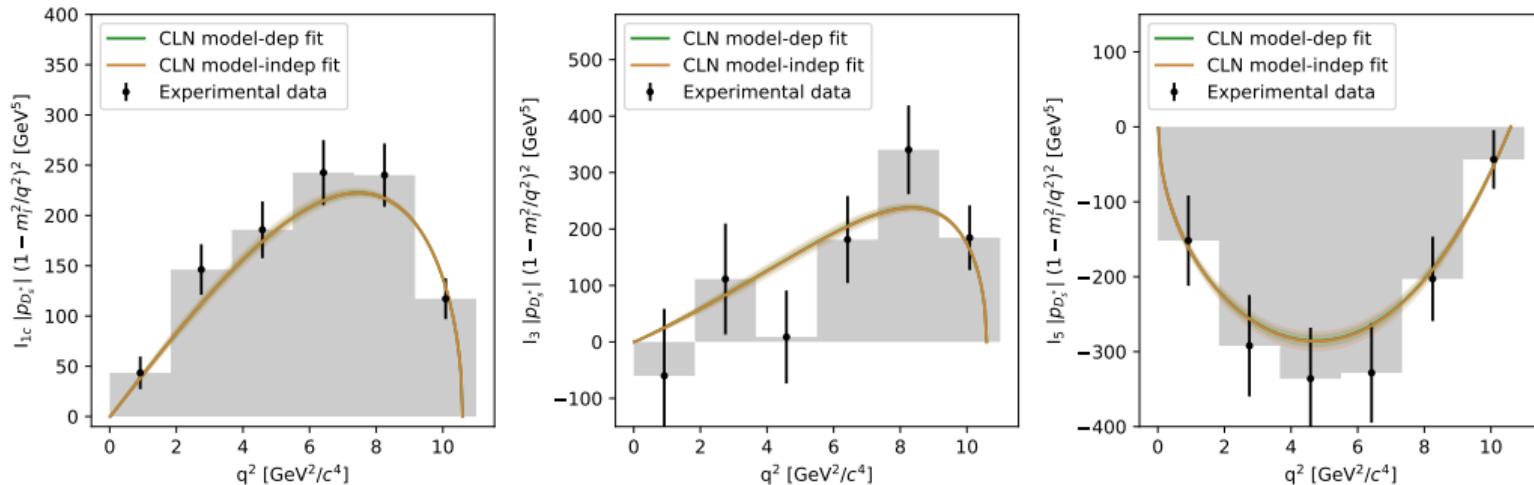


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We could extract information about NP,
because we expect some $I_i(q^2)$ functions
to be zero in SM picture

CLN and BGL from fitted $I_i(q^2)$ functions

Further studies

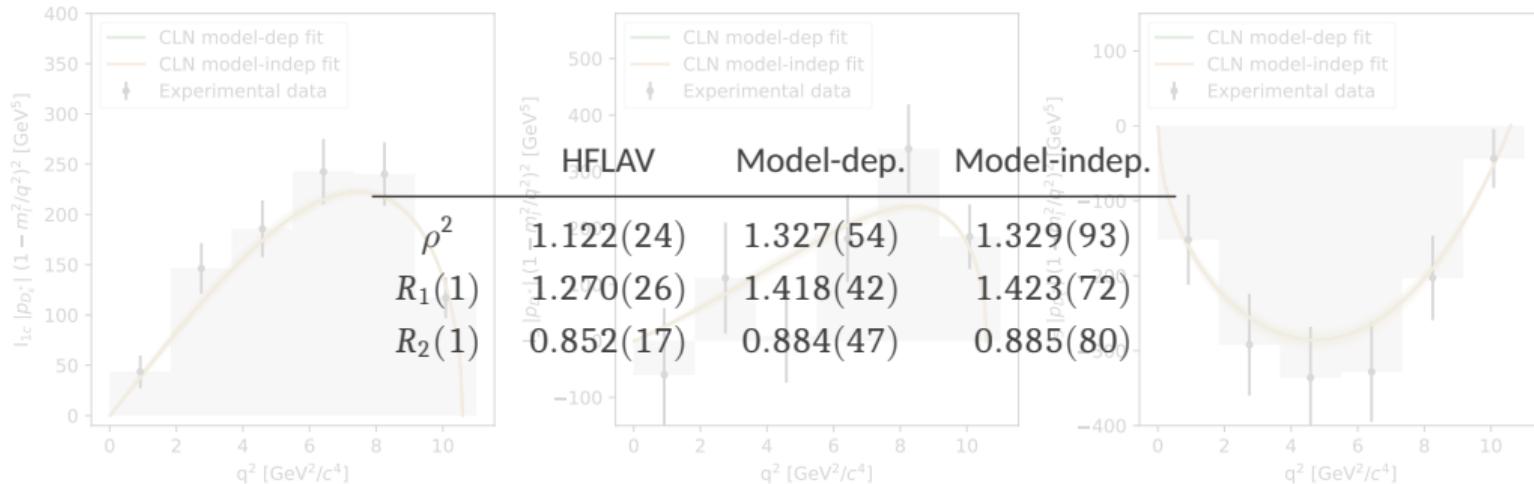


Where:

- Model-dependent shape = CLN/BGL parameters from differential distribution
- Model-independent shape = CLN/BGL parameters from the fitted integrals

CLN and BGL from fitted $I_i(q^2)$ functions

Further studies



Where:

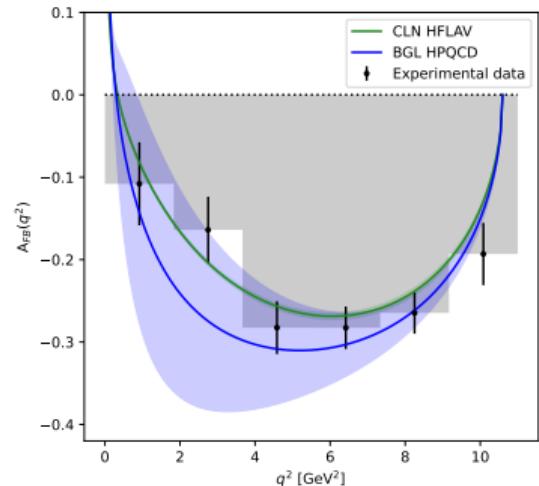
- Model-dependent shape = CLN/BGL parameters from differential distribution
- Model-independent shape = CLN/BGL parameters from the fitted integrals

We can build several observables to evaluate the contribution of New Physics interaction, for instance the forward-backward asymmetry:

$$\begin{aligned} A_{FB}(q^2) &= \left[\int_0^1 \frac{d^2\Gamma}{dq^2 d\cos\theta_\ell} d\cos\theta_\ell - \int_{-1}^0 \frac{d^2\Gamma}{dq^2 d\cos\theta_\ell} d\cos\theta_\ell \right] / \frac{d\Gamma}{dq^2} \\ &= \frac{3(I_{6s} + 4I_{6c})}{6I_{1s} + 24I_{1c} - 2I_{2s} - 8I_{2c}} \end{aligned}$$



Compute the asymmetry for each q^2 bin using the fitted $I_i(q^2)$ values

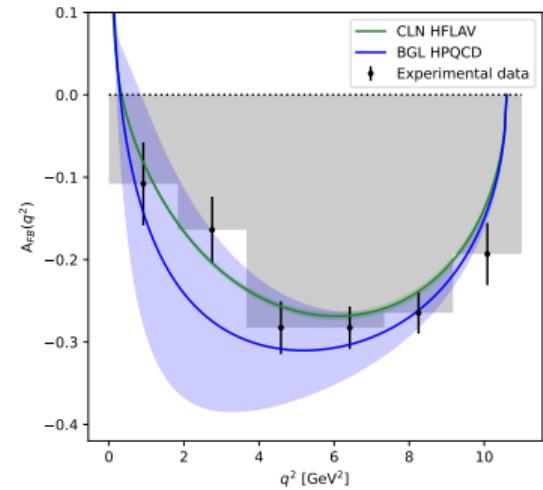


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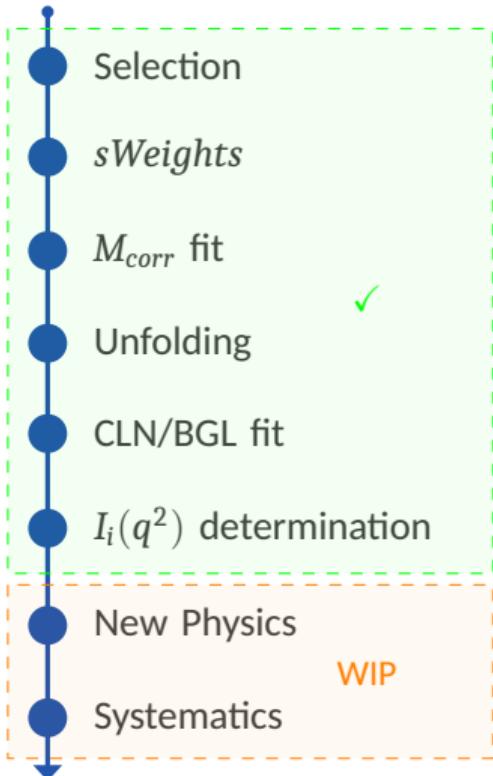


Compute the asymmetry for each q^2 bin using the fitted $I_i(q^2)$ values



Use the basis $\eta, \eta', \delta, \epsilon, \epsilon'$
[arXiv:2104.02094](https://arxiv.org/abs/2104.02094)

- Semileptonic decays are a powerful tool to test Standard Model
- This work will lead to the **first** measurement of $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$ differential distributions
- It is possible to directly test **different New Physics scenarios**, with both a model-dependent and a model-independent approach



Measurement of the differential distributions of $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$ decay at LHCb

Thank you for listening!

arXiv:1801.10468

$$\frac{d\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_d d\chi} = \mathcal{K}(q^2) \sum_i I_i(q^2) \Xi_i(\theta_\ell, \theta_d, \chi)$$

$I_i(q^2) = I_i(q^2; H_0, H_\pm, H_t)$
 and H_i are written using
 CLN/BGL models

$$\begin{aligned}
 &= \mathcal{N}_\gamma |\vec{p}_{D_s^*}(q^2)| \left(1 - \frac{m_\mu^2}{q^2}\right)^2 \cdot \left[I_{1s} \sin^2 \theta_d + I_{1c} (3 + \cos 2\theta_d) \right. \\
 &\quad + I_{2s} \sin^2 \theta_d \cos 2\theta_\ell + I_{2c} (3 + \cos 2\theta_d) \cos 2\theta_\ell \\
 &\quad + I_3 \sin^2 \theta_d \sin^2 \theta_\ell \cos 2\chi + I_4 \sin 2\theta_d \sin 2\theta_\ell \cos \chi + I_5 \sin 2\theta_d \sin \theta_\ell \cos \chi \\
 &\quad + I_{6s} \sin^2 \theta_d \cos \theta_\ell + I_{6c} (3 + \cos 2\theta_d) \cos \theta_\ell \\
 &\quad \left. + I_7 \sin 2\theta_d \sin \theta_\ell \sin \chi + I_8 \sin 2\theta_d \sin 2\theta_\ell \sin \chi + I_9 \sin^2 \theta_d \sin^2 \theta_\ell \sin 2\chi \right]
 \end{aligned}$$

zero in SM

zero in SM and tensor model

$$\mathcal{N}_\gamma = \frac{3G_F^2 |V_{cb}|^2 \mathcal{B}(D_s^* \rightarrow D_s \gamma)}{128(2\pi)^4 m_{B_s^0}^2}$$

$$|\vec{p}_{D_s^*}(q^2)| = \frac{\lambda^{1/2}(m_{B_s^0}^2, m_{D_s^*}^2, q^2)}{2\sqrt{q^2}}$$

$$\lambda(x, y, z) = x^2 + y^2 + z^2 - 2xy - 2xz - 2yz$$

$$H_0 = \frac{(m_{B_s^0} + m_{D_s^*})^2 \lambda^{1/2} (m_{B_s^0}^2, m_{D_s^*}^2, q^2) \mathbf{A}_1(q^2) - \lambda (m_{B_s^0}^2, m_{D_s^*}^2, q^2) \mathbf{A}_2(q^2)}{2m_{D_s^*}(m_{B_s^0} + m_{D_s^*})\sqrt{q^2}}$$

$$H_{\pm} = \frac{(m_{B_s^0} + m_{D_s^*})^2 \mathbf{A}_1(q^2) 4\lambda^{1/2} (m_{B_s^0}^2, m_{D_s^*}^2, q^2) \mathbf{V}(q^2)}{m_{B_s^0} + m_{D_s^*}}$$

$$H_t = -\frac{\lambda^{1/2} (m_{B_s^0}^2, m_{D_s^*}^2, q^2)}{\sqrt{q^2}} \mathbf{A}_0(q^2) \quad w = \frac{m_{B_s^0}^2 + m_{D_s^*}^2 - q^2}{2m_{B_s^0}m_{D_s^*}}$$

$$V(w) = \frac{R_1(w)}{R^*} h_{A_1}(w)$$

$$A_0(w) = \frac{R_0(w)}{R^*} h_{A_1}(w)$$

$$A_1(w) = \frac{w+1}{2} R^* h_{A_1}(w)$$

$$A_2(w) = \frac{R_2(w)}{R^*} h_{A_1}(w)$$

$$\begin{aligned} h_{A_1}(w) &= h_{A_1}(1)[1 - 8\rho^2 z(w) + (53\rho^2 - 15)z(w)^2 \\ &\quad - (231\rho^2 - 91)z(w)^3] \end{aligned}$$

$$R_1(w) = R_1(1) - 0.12(w-1) + 0.05(w-1)^2$$

$$R_2(w) = R_2(1) + 0.11(w-1) - 0.06(w-1)^2$$

$$H_0(w) = \frac{\mathcal{F}_1(w)}{\sqrt{q^2}}$$

$$H_{\pm}(w) = \textcolor{red}{f(w)} 4m_{B_s^0} m_{D_s^*} \sqrt{w^2 - 1} \textcolor{red}{g(w)}$$

$$z(w) = \frac{\sqrt{w+1} - \sqrt{2}}{\sqrt{w-1} + \sqrt{2}}$$

$$H_t(w) = m_{B_s^0} \frac{\sqrt{r}(1+r)\sqrt{w^2-1}}{\sqrt{1+r^2-2wr}} \mathcal{F}_2(w)$$

$f(z) = \frac{1}{P_{1+}(z)\phi_f(z)} \sum_{n=0}^N \textcolor{blue}{a_n^f} z^n$	$\mathcal{F}_1(z) = \frac{1}{P_{1+}(z)\phi_{\mathcal{F}_1}(z)} \sum_{n=0}^N \textcolor{blue}{a_n^{\mathcal{F}_1}} z^n$
$g(z) = \frac{1}{P_{1-}(z)\phi_g(z)} \sum_{n=0}^N \textcolor{blue}{a_n^g} z^n$	$\mathcal{F}_2(z) = \frac{\sqrt{r}}{(1+r)P_{0-}(z)\phi_{\mathcal{F}_2}(z)} \sum_{n=0}^N \textcolor{blue}{a_n^{\mathcal{F}_2}} z^n$

$$H'_{eff} = H_{eff}^{\text{SM}} + \frac{G_F}{\sqrt{2}} V_{cb} \left[\epsilon_T^\ell \bar{c} \sigma_{\mu\nu} (1 - \gamma_5) b \bar{\ell} \sigma^{\mu\nu} (1 - \gamma_5) \nu_\ell + h.c. \right] \quad \sigma^{\mu\nu} = \frac{i}{2} [\gamma^\mu, \gamma^\nu]$$

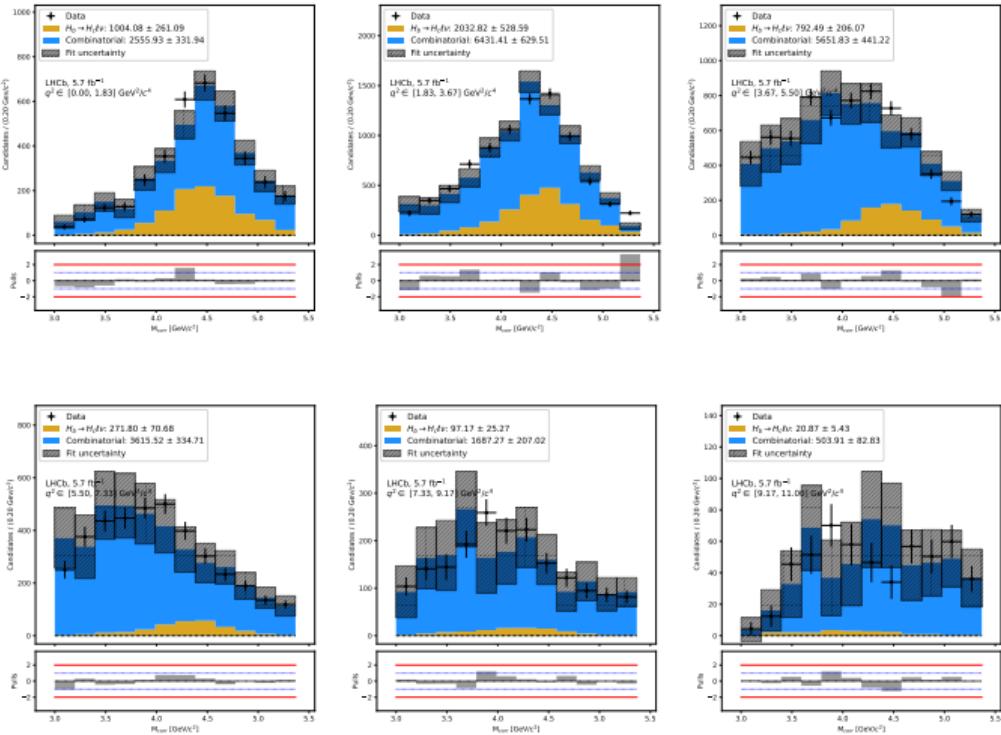
$$\mathcal{A}(B_s^0 \rightarrow D_s^* \ell \nu_\ell) = \frac{G_F}{\sqrt{2}} V_{cb} \left[H_\mu^{\text{SM}} L^{\mu, \text{SM}} + \epsilon_T^\ell H_{\mu\nu}^{\text{NP}} L^{\mu\nu, \text{NP}} \right]$$

$$H_m^j = \langle D_s^*(p_{D_s^*}, \epsilon_m) | \bar{c} \mathcal{O}^j (1 - \gamma_5) b | B_s^0(p_{B_s^0}) \rangle \quad L^j = \bar{\ell} \mathcal{O}^j (1 - \gamma_5) \nu_\ell$$

$$\Rightarrow \quad H_m^{\text{NP}} = H_m^{\text{NP}}(\textcolor{blue}{T}_0, \textcolor{blue}{T}_1, \textcolor{blue}{T}_2) \quad I_j^{\text{NP}} = I_j^{\text{NP}}(H_m^{\text{NP}})$$

Fit in the control region

Backup



Preliminary in the control region
 $\text{BDT}_{\text{dbc_reopt}} < -0.2$, that is
 combinatorial and doubly
 charmed enriched

- use results from this fit to constrain these components

arXiv:2304.03137

