Dalitz plot determination for oPs->3gamma using the J-PET detection system

# Magdalena Skurzok on behalf of the **J-PET** collaboration







Workshop on Fundamental Physics with Exotic Atoms, Frascati, 23-25.06.2025

## **Positronium decays**

#### **POSITRONIUM - the lightest purely leptonic object**





Berestetskii, E. Lifshitz, L. Pitaevskii, Relativistic Quantum Theory, Pergamon Press 1971.



$$|M|^{2} = 64(4\pi)^{3}\alpha^{3} \left[ \left( \frac{m_{e} - E_{1}}{E_{2}E_{3}} \right)^{2} + \left( \frac{m_{e} - E_{2}}{E_{1}E_{3}} \right)^{2} + \left( \frac{m_{e} - E_{3}}{E_{1}E_{2}} \right)^{2} \right]^{2}$$
 each (px,py,pz,E)  
(12 parameters)

3 Lorentz-vectors123 Masses-3Energy conserv.-1Momentum conserv.-33 Euler angles (free rotation) -3Remaining d.o.f2



$$d\sigma_{3\gamma} = \frac{8\alpha^3}{6m_e^2 v} |M|^2 dE_1 dE_2$$

3 photons,

#### 2 parameters

the complete oPs -> 3γ dynamics



presented graphically as a **Dalitz plot** - the variables on the axes represents 2 independent photon parameters, ex. angles or energies



## <u>Goal:</u>

determination, for the first time ever, the experimental Dalitz plot in an angular representation for oPs -> 3γ decay

oPs ->  $\gamma_1 \gamma_2 \gamma_3$ 





## Goal:

determination, for the first time ever, the experimental Dalitz plot in an angular representation for oPs -> 3γ decay

oPs ->  $\gamma_1 \gamma_2 \gamma_3$ 



#### <u>Goal:</u>

determination, for the first time ever, the experimental Dalitz plot in an angular representation for oPs -> 3γ decay



#### J-PET 3 layer detector at Jagiellonian University in Kraków, Poland



- 3 layers, 192 EJ-230 scintillators: 7x19x500 mm<sup>3</sup>
- 85 cm radius, 384 R9800 photomultipliers, 1536 channels
- plastic scintillators small light attenuation, large transparency
- dedicated multithreshold digital electronics (30ps time accuracy) and the novel trigger-less DAQ
- interaction time resolution  $\sim$ 250ps, angular resolution  $\sim$  1deg

[P. Moskal et al., Acta Phys. Polon. B47 (2016) 509; G. Korcyl, et al., IEEE Trans. Med. Imag. 37, 2526 (2018)]

 $\Delta I$ 

PM

PM

#### o-Ps production in J-PET with an annihilation chamber



#### o-Ps production in J-PET with an annihilation chamber



EC



- Small annihilation chamber (plastic PA6 polyamide)
- 0.7 MBq  $\beta$ + <sup>22</sup>Na source placed in the center sandwiched in XAD4 porous polymer
- data taking: 02.04.2020 01.03.2021





## o-Ps -> 3γ selection





### **Events selection**



- 2.5 ns time window for grouping hits in one event
- 6 ns time window for matching Signals on the same scintillator and different sides

1) cut on Z position for the 3 hits - only active detector region: |z|<23cm



3) cut in TOT of all 3 Hits to separate the annihilation and de excitation photon: 1<TOT<17 PMT ns DATA, cut in Energy deposition of each photon JE scatt. Α to select the annihilation candidate: 30<E<326.5 PMT keV MC mc all <u>×1</u>0<sup>3</sup> B counts E<sub>inc.</sub> 160 TOT11 Threshold 140 TOT22 120 TOT33 TOT 100 Threshold TOT TOT22 80 TOT 60 40 20 [S. Sharma, eta al., EJNMMI Phys. 7, 39 (2020)] 0<mark>.</mark> data 100 300 500 600 700 200 400 ×10<sup>6</sup> Edep [keV] counts oPs->3γ 100 2500 80 2000 60 1500 40 1000 20 500 00 0 35 50 30 40 45 5 15 20 25 10 700 14 300 500 600 100 200 400 TOT [ns] Edep [keV]

#### 4) cut on distance between annihilation plane and the source: d<5cm



#### 5) cut on emission time difference between the third and first hit: t<1.5ns



#### 6) cut on the sum of two smallest angles of oPs decaying into $3\gamma$ : sum $\geq$ 190 deg



#### 6) cut on the sum of two smallest angles of oPs decaying into $3\gamma$ : sum $\geq$ 190 deg





# fit to data





cleaned data



# Summary

- experimental Dalitz Plot determined for the first time ever for oPs -> 3γ decay with J-PET scanner
- The precision experimental investigations of the positronium decays are crucial in particular for a sensitive probe of QED and the tests of fundamental symmetries
- the Dalitz Plot investigation for allowed and forbidden Ps-> 3γ decays -> comment on C symmetry

# **Grazie per l'attenzione!**



## Positronium



## **MC contributions**

# MC all: all simulation MC oPs: signal: 3 hits associated to oPs coming from the same vertex GenGammaMultiplicity<sub>i i k</sub>==3 && vtxIndex<sub>i</sub> = vtxIndex<sub>i</sub> = vtxIndex<sub>k</sub> MC oPs<sub>Mis</sub>: mis-reconstructed oPs: 3 hits associated to oPs, but at least one is scattered GenGammaMultiplicity<sub>i,i</sub>==3 && GenGammaMultiplicity<sub>k</sub>==103 (1 scattered) GenGammaMultiplicity<sup>\*\*</sup><sub>i,j,k</sub>==103 (2 scattered) GenGammaMultiplicity<sup>\*\*</sup><sub>i,j,k</sub>==103 (3 scattered)

MC background = all MC - oPs - oPs

$$|M|^{2} = 64(4\pi)^{3}\alpha^{3} \left[ \left( \frac{m_{e} - E_{1}}{E_{2}E_{3}} \right)^{2} + \left( \frac{m_{e} - E_{2}}{E_{1}E_{3}} \right)^{2} + \left( \frac{m_{e} - E_{3}}{E_{1}E_{2}} \right)^{2} \right]^{3}$$

$$3 \text{ photons,}$$
each (px,py,pz,E)
$$12 \text{ parameters}$$

$$d\sigma_{3\gamma} = \frac{8\alpha^3}{6m_e^2 v} |M|^2 dE_1 dE_2$$

$$V|\Psi(0)|^2 = \frac{m^3 \alpha^3}{8\pi}$$
electron positron flux density relative velocity
$$\Gamma_{LO} = 7.21117 \ \mu s^{-1}$$
Averaging the cross-section over initial spin states three from four possible positronium spin states undergo 3\gamma annihilation
$$\int_{120}^{180} \frac{180}{\theta_{12}} d\sigma_{3\gamma} v |\Psi(0)|^2$$

### O(alpha) correction



FIG. 2. Graphs contributing to the ortho-Ps decay amplitudes through order  $\alpha$ . They are the (a) self-energy, (b) outer vertex, (c) inner vertex, (d) double vertex, (e) ladder, and (f) annihilation contributions. The wave function factors are implicit in these graphs.

$$\Gamma_1 = \frac{m\alpha^7}{36\pi^2} \int_0^1 dx_1 \int_{1-x_1}^1 dx_2 \frac{1}{x_1 x_2 x_3} \{F(x_1, x_3) + \text{permutations}\}$$

### O(alpha) correction

$$F(x_1, x_3) = g_0(x_1, x_3) + \sum_{i=1}^{5} g_i(x_1, x_3) h_i(x_1)$$

7

+ 
$$\sum_{i=6}^{7} g_i(x_1, x_3) h_i(x_1, x_3)$$
.

$$\begin{split} g_2(x_1,x_3) &= \frac{2}{3x_1^{3}\overline{x}_1x_3} \{-48x^{10} + 180x^{20} - 276x^{30} + 228x^{40} \\ &- 108x^{50} + 24x^{60} + 48x^{01} - 48x^{11} - 144x^{51} \\ &+ 244x^{41} - 106x^{51} + 2x^{61} + 4x^{71} - 96x^{02} + 156x^{12} \\ &- 108x^{22} + 168x^{32} - 132x^{42} + 7x^{52} + 6x^{62} \\ &+ 48x^{03} - 60x^{13} - 36x^{23} + 42x^{33} + 9x^{43} - 6x^{53} \\ &+ 6x^{34} - 4x^{44}\}. \end{split}$$

$$\begin{array}{c} g_{3}(x_{1},x_{3})=\frac{4}{x_{1}^{2}(x_{1}-x_{3})x_{3}}\{-2x^{20}-2x^{40}-4x^{60}+5x^{11}-6x^{21}\\ &+14x^{31}-4x^{41}+18x^{51}-x^{61}-4x^{02}-2x^{12}+4x^{22}\\ &-2x^{32}-26x^{42}-x^{52}+8x^{03}-7x^{13}-2x^{23}+12x^{33}\\ &+2x^{43}-4x^{04}+4x^{14}\}, \end{array}$$

$$g_4(x_1, x_3) = \frac{8}{x_1^2} \{-4 + 7x^{10} - 7x^{20} + 12x^{30} - 10x^{40} + 2x^{50} + 8x^{01} \\ - 10x^{11} + 3x^{21} - 3x^{31} + 2x^{41} - 4x^{02} + 3x^{12} + 2x^{22} \\ + x^{32}\}, \qquad (A5e)$$

$$g_5(x_1, x_3) = \frac{2\overline{x}_1}{x_1} \{8 - 34x^{10} + 29x^{20} - 4x^{30} + 6x^{11} + 8x^{02} - 4x^{12}\},$$
 (A51)

$$\begin{split} & = g_6(x_1,x_3) = \frac{1}{x_1 \overline{x}_2 x_3} \{ 16 - 76x^{10} + 136x^{20} - 124x^{30} + 64x^{40} \\ & - 16x^{50} - 60x^{01} + 272x^{11} - 424x^{21} + 294x^{31} \\ & - 104x^{41} + 22x^{51} + 92x^{02} - 392x^{12} + 484x^{22} \\ & - 187x^{32} + 13x^{42} + 2x^{52} - 76x^{03} + 294x^{13} - 259x^{23} \\ & + 30x^{33} + 3x^{43} + 36x^{64} - 120x^{14} + 61x^{24} + 3x^{34} \\ & - 8x^{05} + 22x^{15} + 2x^{25} \}, \end{split}$$

$$\begin{split} g_7(x_1,x_3) &= \frac{1}{\bar{x}_2} \{ 16 - 48x^{10} + 46x^{20} - 12x^{30} - 2x^{40} - 48x^{01} \\ &\quad + 60x^{11} + 9x^{21} - 31x^{31} + 10x^{41} + 46x^{02} + 9x^{12} \end{split}$$

 $+ 60x^{11} + 9x^{21} - 31x^{31} + 10x^{41} + 46x^{02} + 9x^{12}$  $- 42x^{22} + 11x^{32} - 12x^{03} - 31x^{13} + 11x^{23} - 2x^{04}$ 

(A5h)

# The g functions

The g functions are given in terms of  $x^{mn} = x_1^m x_3^n$  and  $\overline{x}_2 = x_1 + x_3 - 1$  as

$$g_{0}(x_{1}, x_{3}) = \frac{1}{9x_{1}\bar{x}_{1}(1 - 2x_{1})x_{3}\bar{x}_{3}(1 - 2x_{3})} \{-180 + 2196x^{10} - 4968x^{20} + 5292x^{30} - 2664x^{40} + 504x^{50} - 5848x^{11} + 22639x^{21} - 20280x^{31} + 8405x^{41} - 1240x^{51} - 24x^{61} - 17551x^{22} + 22982x^{32} - 5857x^{42} + 264x^{52} + 48x^{62} - 3776x^{33} - 878x^{43} + 400x^{53} + 536x^{44}\},$$
(A5a)

$$g_{1}(x_{1},x_{3}) = \frac{4}{x_{1}^{2}(1-2x_{1})^{2}(x_{1}-x_{3})x_{3}} \{2x^{20}-13x^{30}+35x^{40} - 36x^{50}+8x^{60}+4x^{70}+9x^{11}-59x^{21}+149x^{31} - 210x^{41}+162x^{51}-51x^{61}+x^{71}-4x^{02}+3x^{12} + 55x^{22}-126x^{32}+104x^{42}-39x^{52}+x^{62}+8x^{03} - 26x^{13}+7x^{23}+22x^{33}+2x^{43}-2x^{53}-4x^{04} + 14x^{14}-8x^{24}-8x^{34}\},$$
(A5b)

G. S. Adkins, Analytic evaluation of the amplitudes for orthopositronium decay to three photons to one-loop order + 10x<sup>14</sup>}.

 $\Gamma = 7.0401 \pm 0.0007 \times 10^6 \,\mathrm{s}^{-1}$ 

best published experimental result



## ANALYSIS

determination, for the first time ever, of the experimental Dalitz plot in an angular representation for oPs  $\rightarrow$  3 $\gamma$  decay

## **Experimental Data - Big Barrel:**

#### RUN11

- 02.04.2020 01.03.2021
- small annihilation chamber (PA6 material)
- <sup>22</sup>Na source activity 0.702 MBg
- thresholds: 30, 80, 190, 300 mV

#### Analysed data:

- **484978** hld files -> 950~TB
- 40 million o-Ps -> 3g signal events identified
- -> about 91% of data in RUN11
  - "EventFinder EventTime float":2500.0 (2.5 [ns]) time window for grouping hits in one event
  - "HitFinder ABTimeDiff float":6000.0 (6 [ns]) time window for matching Signals on the same scintillator and different sides

# **MC Simulations**

1.564\*10<sup>11</sup> events generated (with frame)

J-PET Report 2020 J-PET Monte Carlo simulations in Geant4 toolkit User Manual for version 4.0





- "GeantParser ZPositionSmearingPara meters std::vector<double>":[3.0] [cm]
- "GeantParser TimeSmearingParameter s std::vector<double>":[225.0] [ps]

## userParams

### Data:

- preselected data /mnt/jpet/Preselection/Run11/data
  - "TimeWindowCreator\_MinTime\_float":-20000.0 (-20 [ns])
  - "SignalFinder\_EdgeMaxTime\_float":3000.0 (3 [ns]) time window for matching Signal Channels on Leading Edge
  - "SignalFinder\_LeadTrailMaxTime\_float":23000.0 (23 [ns])

time window for matching Signal Channels on the same thresholds from Leading and Trailing edge

- "HitFinder\_ABTimeDiff\_float":6000.0 (6 [ns]) time window for matching Signals on the same scintillator and different sides
- "EventFinder\_EventTime\_float":2500.0 (2.5 [ns]) time window for grouping hits in one event

### **MC Simulations**

- "GeantParser\_MinTimeWindow\_double":-20000000
   .0 (-20 [ns])
- "EventFinder\_EventTime\_float":2500.0 (2.5 [ns])
- "GeantParser\_SourceActivity\_double":1.1 [MBq]
- "GeantParser\_EnergyThreshold\_double":30.0 [keV]
- "GeantParser\_ZPositionSmearingParameters\_std::v ector<double>":[3.0] [cm]
- "GeantParser\_TimeSmearingParameters\_std::vecto r<double>":[225.0] [ps]

#### 4) cut on distance between annihilation plane and the source: d<5cm



# Goal of the analysis



$$d\Gamma_T^{3\gamma} = \frac{8\alpha\Gamma_s^{2\gamma}}{3\alpha^2 (2\pi)^4} (\omega_1\omega_2\omega_3)^{-1} \sum_{1\to 2\to 3} \omega_i^2 \left(\frac{1}{2} - \omega_i\right)^2 d\theta_{12} d\theta_{13} d\Omega_1 d\varphi_1,$$
  
$$\Gamma_T^{3\gamma} = \frac{4\alpha\Gamma_s^{2\gamma}}{3\pi^2} \int_0^{1/2} d\omega \int_{1/2-\omega_1}^{1/2} \sum_{1\to 2\to 3} \left(\frac{1}{2} - \omega_1\right)^2 / (\omega_2\omega_3)^2 d\omega_2 \approx 0.898 \cdot 10^{-3} g^2 \Gamma_s^{2\gamma}$$

Raffaele Del Grande

### **Events selection**

#### 5) cut on emission time difference between the third and first hit: t<1.5ns



34

3

3.5

t<sub>hit1</sub>-t<sub>hit3</sub> [ns]

## **ANALYSIS**

## **Experimental Data:**

#### <u>RUN11</u>

- 02.04.2020 01.03.2021
- small annihilation chamber (PA6 material)
- <sup>22</sup>Na source activity 0.702 MBq
- thresholds: 30, 80, 190, 300 mV

#### Analysed data:

- tapes 186-200, 239 127057 .hld files
- -> about 20% of data in RUN11 (616708 files), 42 days

## **MC Simulations**

- oPs ->  $3\gamma$  8.49\*10<sup>9</sup> events generated
- pPs ->  $3\gamma$  10<sup>9</sup> events generated

J-PET Report 2020 *J-PET Monte Carlo simulations in Geant4* toolkit User Manual for version 4.0

#### P. Mills, S. Berko, Phys. Rev. Lett. 18, 420 (1967)



#### correcting MC with Edep efficiency



determined by Sushil Sharma, more details in:

https://koza.if.uj.edu.pl/petwiki/images/b/b5/AnalysisStatus\_210120201.pdf https://koza.if.uj.edu.pl/petwiki/images/5/52/EfficiencyOfJPet.pdf

## **Dalitz Plots Energy**









oPs mis





## **Charge Conjugation Symmetry Test**

• experimental tests of C-symmetry in Ps decays

 $\begin{array}{ll} \mathrm{BR}(\mathrm{o}\text{-}\mathrm{Ps} \rightarrow 4\gamma/\mathrm{o}\text{-}\mathrm{Ps} \rightarrow 3\gamma) &< 2.6 \times 10^{-6} & \mathrm{at} & 90\% \ \mathrm{C.L.} \end{array} \tag{I] J. Yang eta al., Phys. Rev. A 54, 1952 (1996)} \\ & \text{the best limit for p-Ps -> 3y} \\ \mathrm{BR}(\mathrm{p}\text{-}\mathrm{Ps} \rightarrow 3\gamma/\mathrm{p}\text{-}\mathrm{Ps} \rightarrow 2\gamma) &< 2.8 \times 10^{-6} & \mathrm{at} & 68\% \ \mathrm{C.L.} \end{aligned} \tag{I] J. Yang eta al., Phys. Rev. A 54, 1952 (1996)} \\ & \text{the best limit for p-Ps -> 3y} \\ \mathrm{BR}(\mathrm{p}\text{-}\mathrm{Ps} \rightarrow 3\gamma/\mathrm{p}\text{-}\mathrm{Ps} \rightarrow 2\gamma) &< 2.7 \times 10^{-7} & \mathrm{at} & 90\% \ \mathrm{C.L.} \end{aligned}$ 



- >  $Cu^{64}$  source (in gas chamber)
- 6 Nal(TI) scintillators, multiple coinc. electronics
- NO quenching to suppress o-Ps-3γ
  - the C forbidden p-Ps->3γ decay separated from the allowed o-Ps->3γ decay by studying angular distribution of 3 photons:
    - symmetric configuration (120°,120°,120°)
    - 60°,150°,150°
    - 90°,120°,150°

$$\begin{split} E_{1} &= -2m_{e}c^{2} \frac{-\cos\theta_{13} + \cos\theta_{12}\cos\theta_{23}}{(-1 + \cos\theta_{12})(1 + \cos\theta_{12} - \cos\theta_{13} - \cos\theta_{23})} = \omega_{1} \\ E_{2} &= -2m_{e}c^{2} \frac{\cos\theta_{12}\cos\theta_{13} - \cos\theta_{23}}{(-1 + \cos\theta_{12})(1 + \cos\theta_{12} - \cos\theta_{13} - \cos\theta_{23})} = \omega_{2} \\ E_{3} &= 2m_{e}c^{2} \frac{1 + \cos\theta_{12}}{(1 + \cos\theta_{12} - \cos\theta_{13} - \cos\theta_{23})} = \omega_{3} \end{split}$$

# Solution of equation can be presented as:

In the **CM frame**, E of gamma quanta from PS annihilation can be expressed as a function of angles Momentum entry corrections  $\theta_{12}, \theta_{23}, \theta_{13}$ 

relation between Theta's and energy calculated

 $w_1 + w_2 + w_3 = 2m$   $m = 511 \ keV$  $0 \le \theta_{12}, \theta_{23}, \theta_{13} \le 180^\circ$ 

$$\theta_{12} = \cos^{-1} \left( \frac{p_3^2 - p_1^2 - p_2^2}{2p_1 p_2} \right)$$
  
$$\theta_{23} = \cos^{-1} \left( \frac{p_1^2 - p_2^2 - p_3^2}{2p_2 p_3} \right)$$
  
$$\theta_{31} = \cos^{-1} \left( \frac{p_2^2 - p_1^2 - p_3^2}{2p_1 p_3} \right)$$

$$d\sigma_{3\gamma} = \frac{(2\pi)^2 |M_{fi}|^2}{4I} \delta\left(k_1 + k_2 + k_3\right) \delta\left(\omega_1 + \omega_2 + \omega_3 - 2m\right) \frac{d^3k_1 d^3k_2 d^3k_3}{(2\pi)^9 2\omega_1 2\omega_2 2\omega_3}$$

amplitude can be calculated as:

$$\sum_{polarisation} |M_{fi}| = 64 \left(4\pi\right)^3 e^6 \left[ \left(\frac{m-\omega_1}{\omega_2\omega_3}\right)^2 + \left(\frac{m-\omega_2}{\omega_1\omega_3}\right)^2 + \left(\frac{m-\omega_3}{\omega_1\omega_2}\right)^2 \right]$$

the resulting differential cross-section for annihilation of photons having specified energies

$$d\sigma_{3\gamma} = \frac{1}{6} \frac{8e^6}{vm^2} \left[ \left( \frac{m - \omega_1}{\omega_2 \omega_3} \right)^2 + \left( \frac{m - \omega_2}{\omega_1 \omega_3} \right)^2 + \left( \frac{m - \omega_3}{\omega_1 \omega_2} \right)^2 \right] d\omega_1 d\omega_2$$

$$\sigma_{3\gamma} = \frac{8e^6}{6vm^2} \cdot 3\int_0^m \int_{m-\omega_1}^m \sum_{1\to 2\to 3} \left(\frac{m-\omega_1}{\omega_2\omega_3}\right)^2 d\omega_1 d\omega_2$$

J-PET Report 2020 J-PET Monte Carlo simulations in Geant4 toolkit User Manual for version 4.0

amplitude can be calculated as:

$$\sum_{polarisation} |M_{fi}| = 64 (4\pi)^3 e^6 \left[ \left( \frac{m - \omega_1}{\omega_2 \omega_3} \right)^2 + \left( \frac{m - \omega_2}{\omega_1 \omega_3} \right)^2 + \left( \frac{m - \omega_3}{\omega_1 \omega_2} \right)^2 \right]$$

$$\sum_{polarisation} |M_{fi}| = 64 (4\pi)^3 e^6 \left[ \left( \frac{m - \omega_1}{\omega_2 \omega_3} \right)^2 + \left( \frac{m - \omega_2}{\omega_1 \omega_3} \right)^2 + \left( \frac{m - \omega_3}{\omega_1 \omega_2} \right)^2 \right]$$

$$\sum_{k_r, k_2} |k_r, k_2| = \frac{m_1 + \omega_2}{\omega_1 \omega_2} d\omega_1 + 2\pi \omega_2^2 \frac{d(\cos \theta_1 - \omega_2)}{d(\cos \theta_1 - \omega_2)} d\omega_2$$

$$d(\cos \theta_{12}) = \frac{\omega_3}{\omega_1 \omega_2} d\omega_3 \quad \omega_3 = \sqrt{\omega_1^2 + \omega_2^2 + 2\omega_1 \omega_2 \cos \theta_{12}} d\omega_3$$

to ged rid of  $\delta(\omega)$  - integrate over  $d^3\omega_3$ 

the resulting differential cross-section for annihilation of photons having specified energies

$$d\sigma_{3\gamma} = \frac{1}{6} \frac{8e^6}{vm^2} \left[ \left( \frac{m - \omega_1}{\omega_2 \omega_3} \right)^2 + \left( \frac{m - \omega_2}{\omega_1 \omega_3} \right)^2 + \left( \frac{m - \omega_3}{\omega_1 \omega_2} \right)^2 \right] d\omega_1 d\omega_2$$