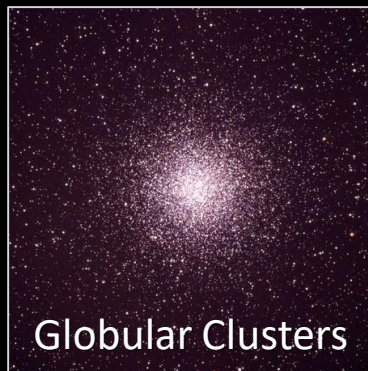




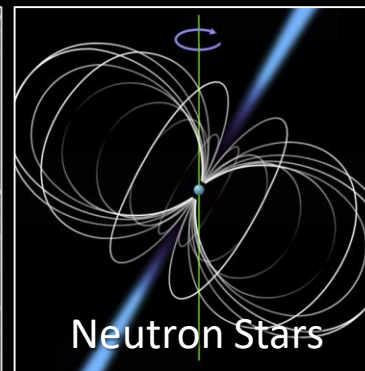
Solar Axions



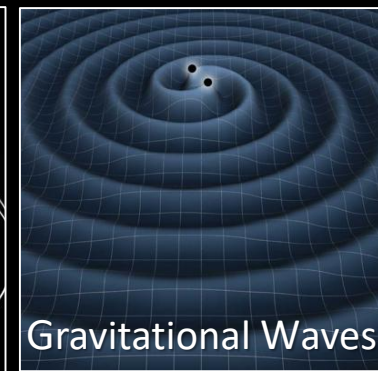
Globular Clusters



Supernova 1987A



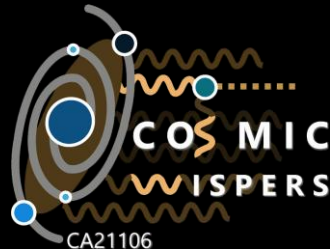
Neutron Stars



Gravitational Waves

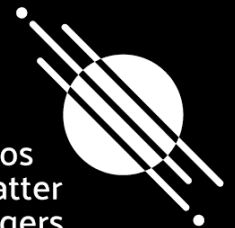
Looking at Stars Aiming for Axions

20th Patras Workshop on Axions, WIMPs and WISPs
La Laguna, Tenerife, 22 September 2025



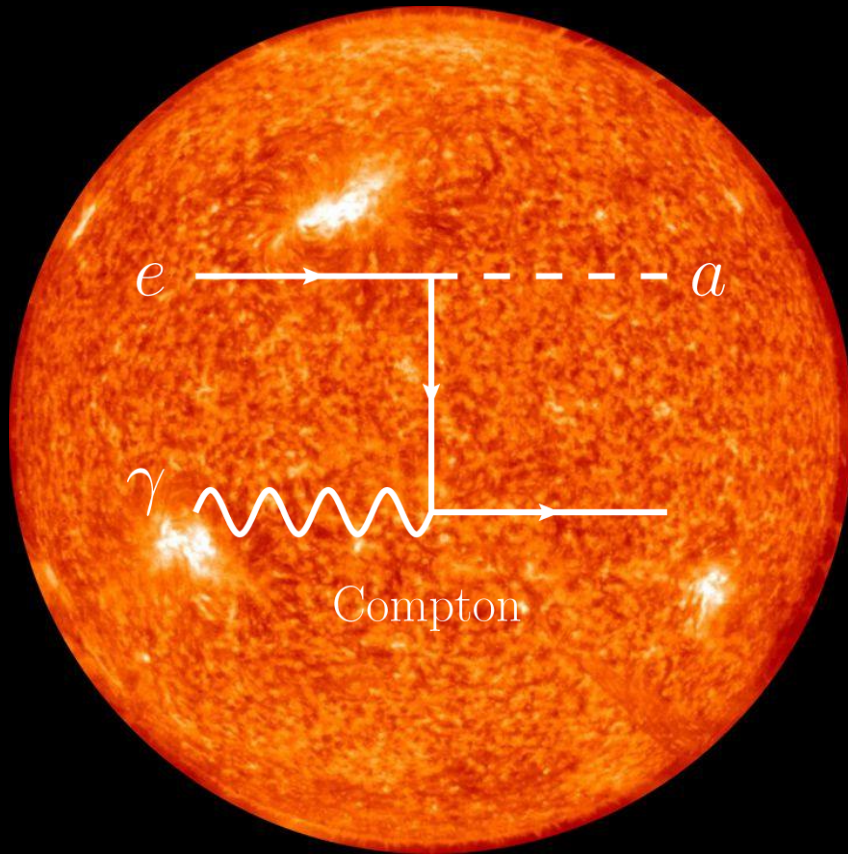
SFB 1258

Neutrinos
Dark Matter
Messengers



Georg G. Raffelt, Max-Planck-Institut für Physik, Garching

Particles and Stars



Low-mass particles are produced in stellar interiors

- **Detection opportunity (Sun or Supernovae)**
- **Backreaction on stellar properties**

→ **Neutrinos**

→ **Axions & friends**

Energy Production in Stars*

H. A. BETHE

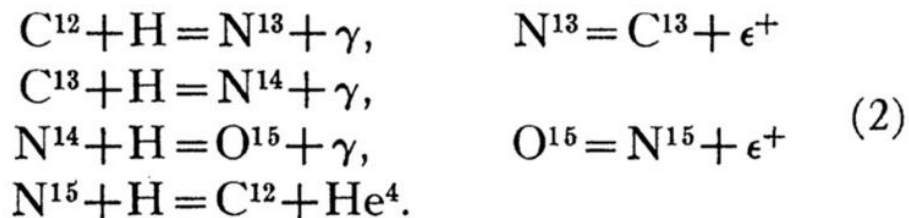
Cornell University, Ithaca, New York

(Received September 7, 1938)

The combination of four protons and two electrons can occur essentially only in two ways. The first mechanism starts with the combination of two protons to form a deuteron with positron emission, *viz.*



The deuteron is then transformed into He^4 by further capture of protons; these captures occur very rapidly compared with process (1). The second mechanism uses carbon and nitrogen as catalysts, according to the chain reaction



Hans Bethe
1906–2005



- First mention of neutrino emission from stars
- Neutrino losses discussed, although overestimated

Some Early Papers on Stellar Particle Physics

Neutrinos (since 1960s)

- Bernstein, Ruderman & Feinberg:
Electromagnetic properties of the neutrino, Phys. Rev. 132 (1963) 1227
- Gribov & Pontecorvo:
Neutrino astronomy and lepton charge, PLB 28 (1969) 493
- Cowsik:
Limits on the radiative decay of neutrinos, PRL 39 (1978) 511
- Falk & Schramm:
Limits from supernovae on neutrino radiative lifetimes, PLB 79 (1978) 511



Flavor oscillations!



Axions & light Higgs (ca 1978)

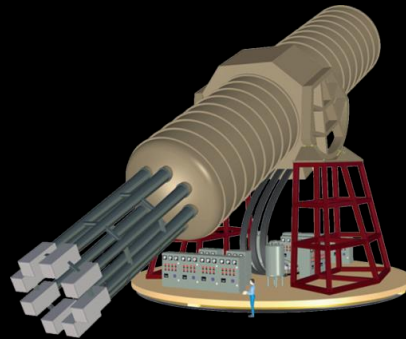
- Vysotsky, Zeldovich, Khlopov & Chechetkin:
Some astrophysical limitations on the axion mass,
Pisma Zh. Eksp. Teor. Fiz. 27 (1978) 533 [JETP Lett. 27 (1978) 502]
- Dicus, Kolb, Teplitz & Wagoner:
Astrophysical bounds on the masses of axions and Higgs particles, PRD 18 (1978) 1829
- K. O. Mikaelian: Astrophysical implications of new light Higgs bosons, PRD 18 (1978) 3605
- K. Sato: Astrophysical constraints on the axion mass and the number of quark flavors,
Prog. Theor. Phys. 60 (1978) 1942

Particles from the Sun

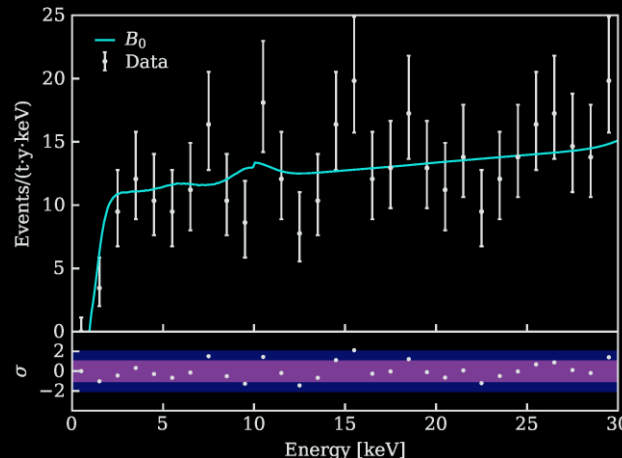


2002 Solar Neutrinos (R.Davis, M.Koshiba)

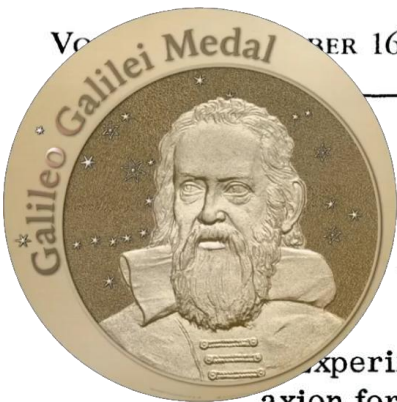
2015 Solar Nu Oscillations (A.McDonald)



Search for solar axions
with CAST and future IAXO



No excess in XENONnT
arXiv:2207.11330
Bounds on axions,
dark photons, neutrino
dipole moments



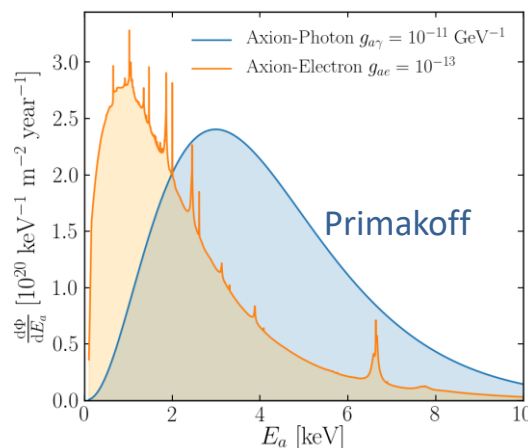
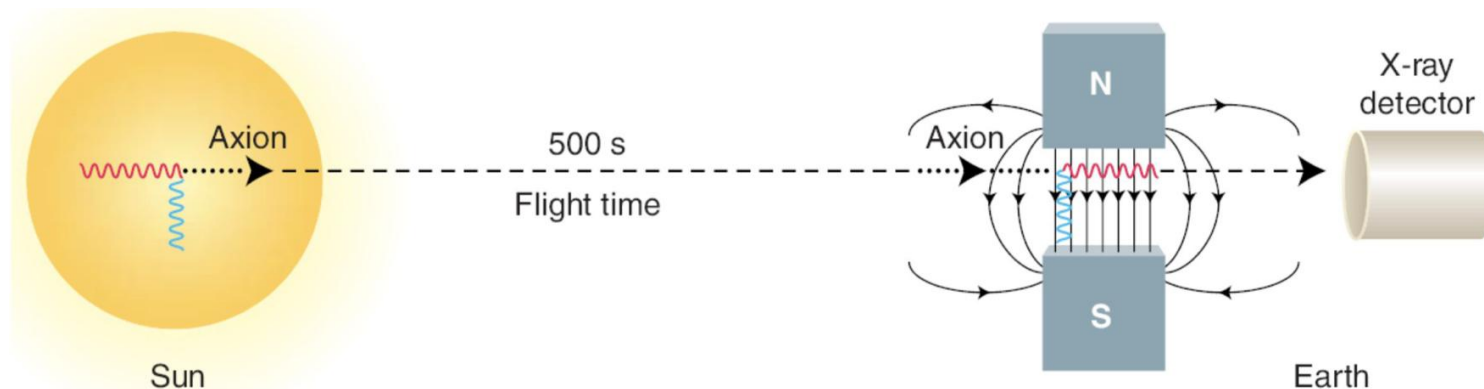
Experimental Tests of the “Invisible” Axion

P. Sikivie

Physics Department, University of Florida, Gainesville, Florida 32611

(Received 13 July 1983)

Experiments are proposed which address the question of the existence of the “invisible” axion for the whole allowed range of the axion decay constant. These experiments exploit the coupling of the axion to the electromagnetic field, axion emission by the sun, and/or the cosmological abundance and presumed clustering of axions in the halo of our galaxy.



- Large coherence length overcomes small coupling
- Axion-photon conversion in B-field similar to neutrino flavor oscillation, PRD 37 (1988) 1237
- Can be enhanced with gas filling van Bibber+ PRD 39 (1989) 2089

<https://cajohare.github.io/IAXOmass/>

Let's point a magnet
at the sun...



© Sebastian Baum

...and look for X-Rays!



Tokyo Helioscope (Sumico)

Fully steerable, 2.3 m long, 4 Tesla
Moriyama+ [hep-ex/9805026]

$$G_{\gamma\gamma} < 0.60 \times 10^{-9} \text{ GeV}^{-1}$$

See also Ohta+ [1201.4622]

Rochester-Brookhaven-FermiLab

Lazarus+ PRL 69 (1992) 2333

Few hours of data, fixed magnet

$$G_{\gamma\gamma} < 0.77 \times 10^{-8} \text{ GeV}^{-1}$$



Konstantin
Zioutas

CAST (1998–2021)

Steerable, 9.26 m long, 9 Tesla
CAST Collaboration [2406.16840]

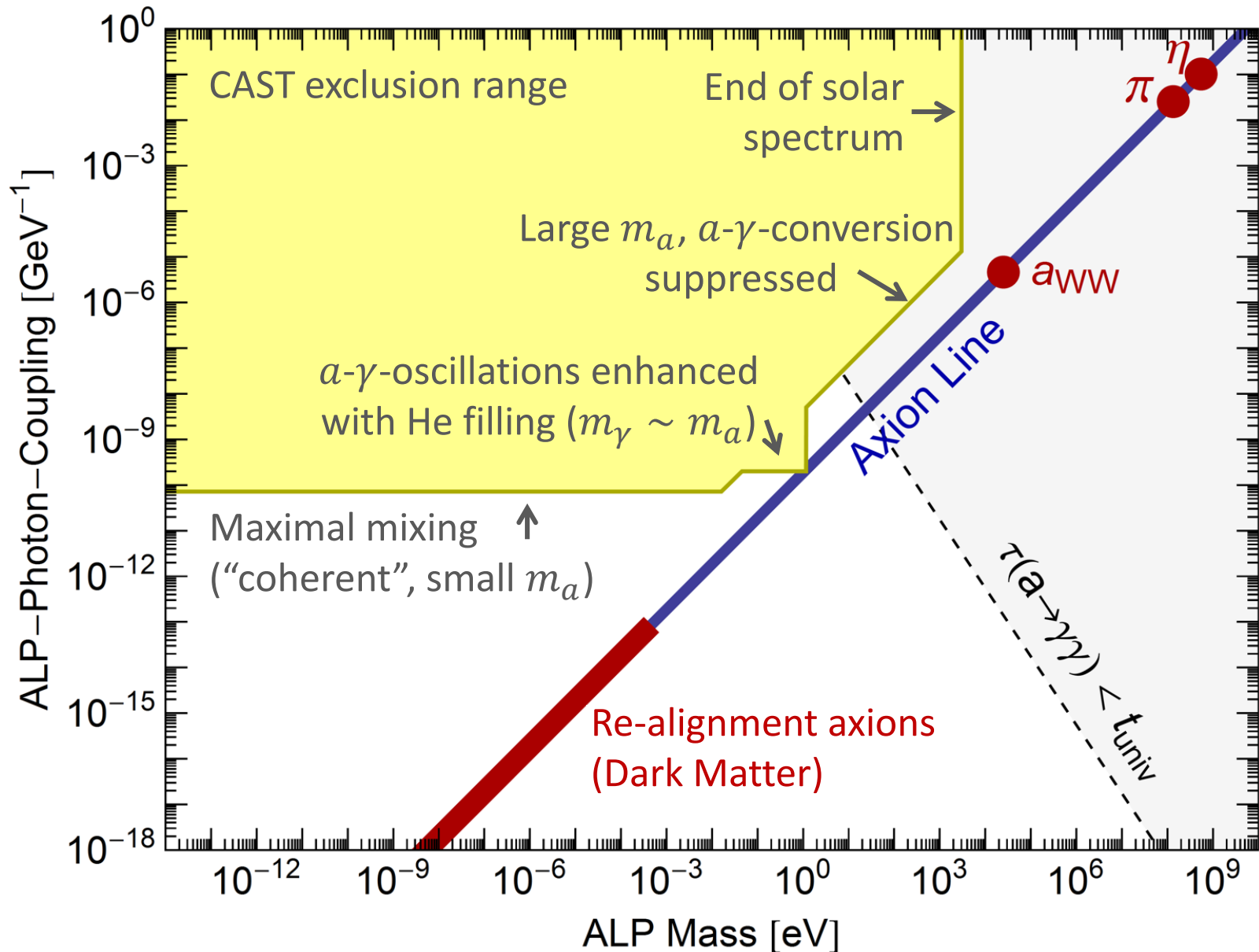
$$G_{\gamma\gamma} < 0.58 \times 10^{-10} \text{ GeV}^{-1}$$

CAST Movie on YouTube

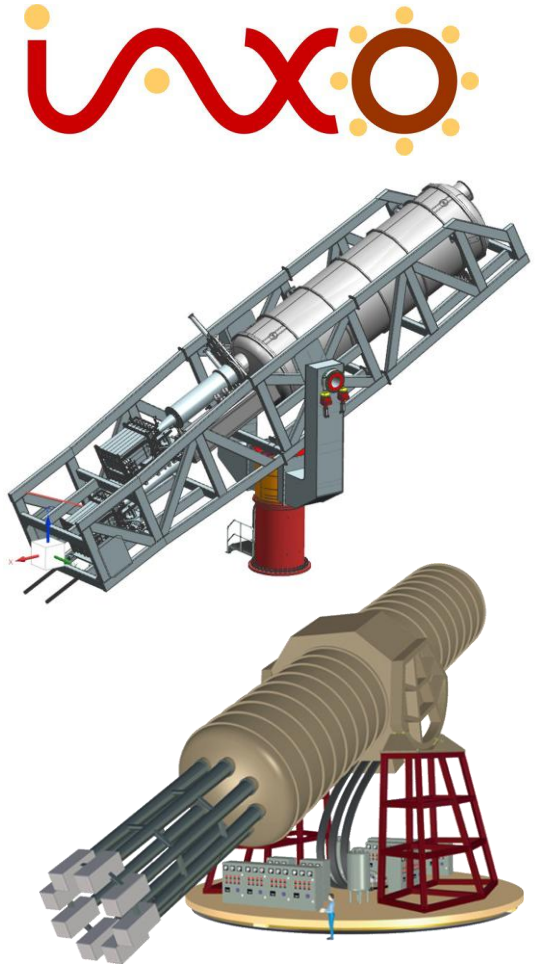
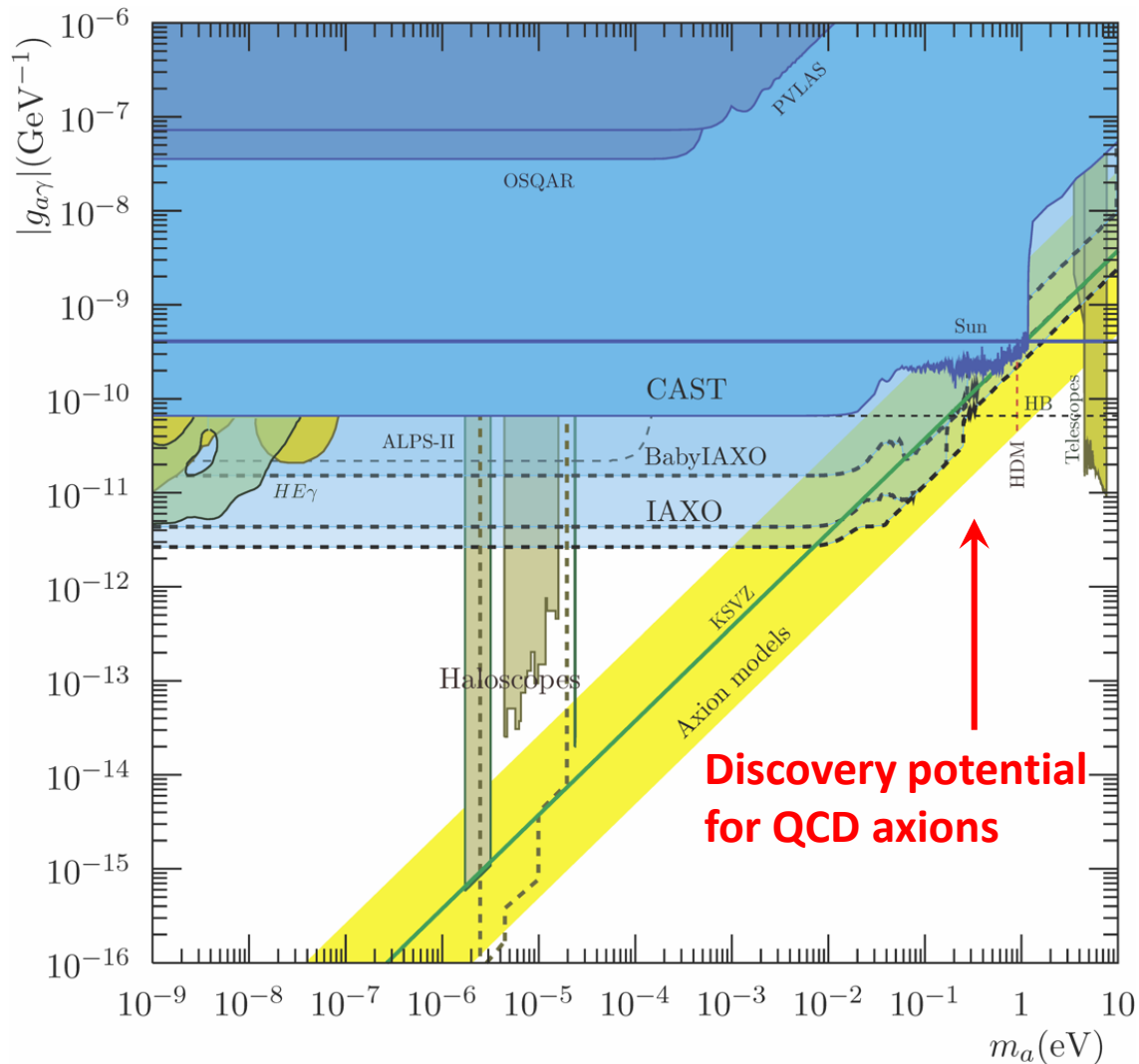
<https://youtu.be/XY2IFDXz8aQ>



Parameter Space for Axion-Like Particles (ALPs)

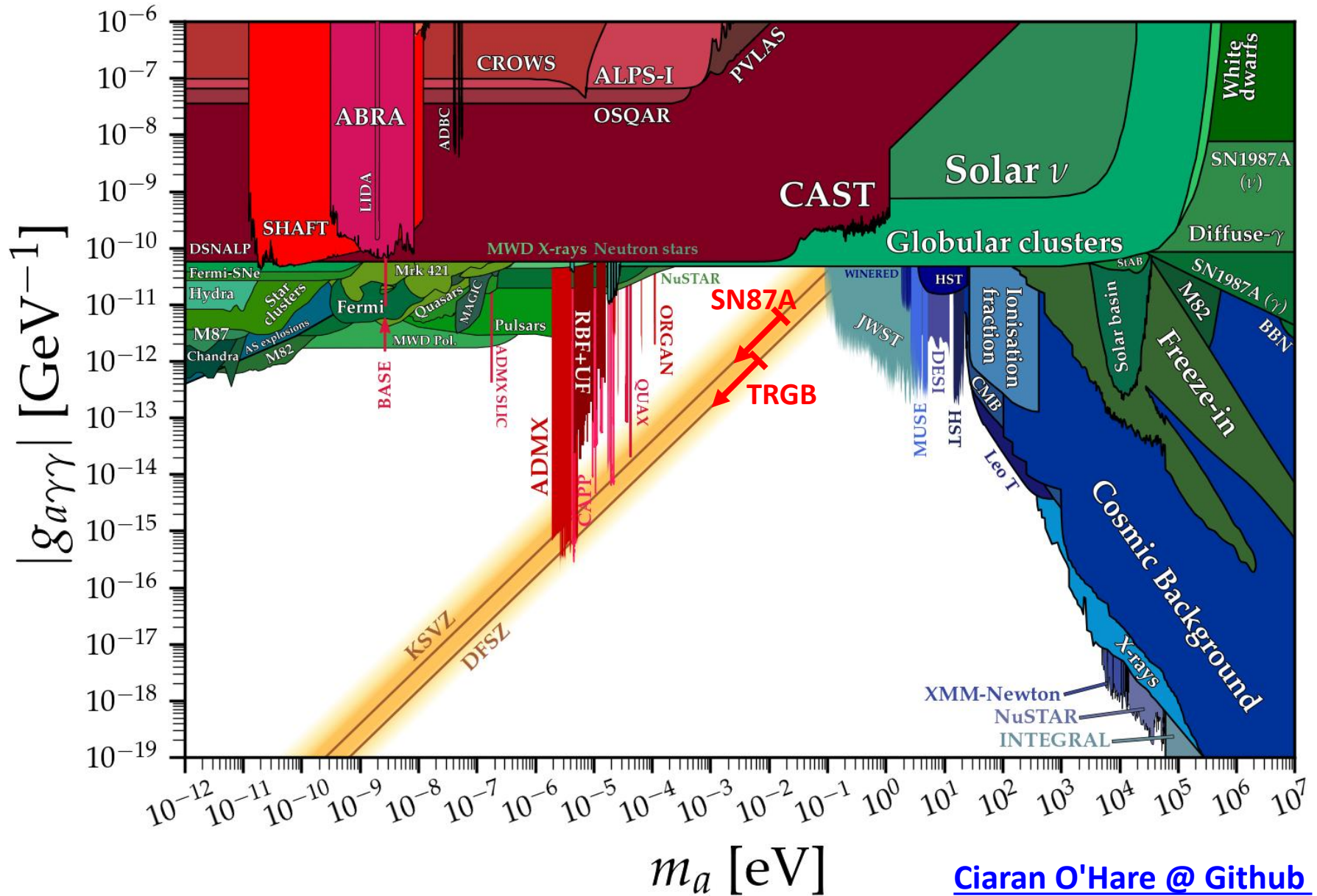


(Baby) IAXO Sensitivity Forecast



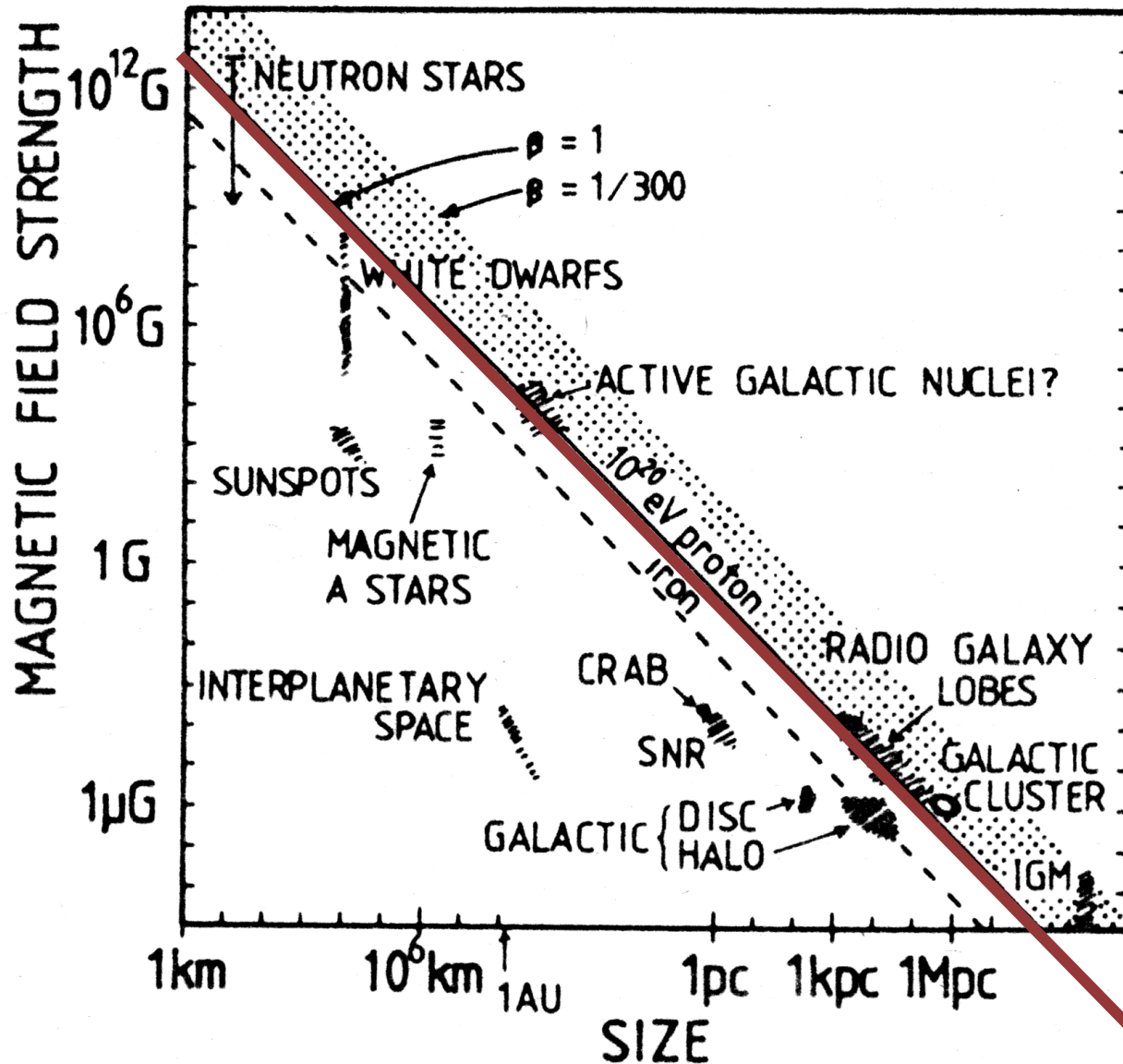
Physics potential of the International Axion Observatory (IAXO)
 JCAP 1906 (2019) 047, arXiv:1904.09155

Grand Unified ALP Scape



[Ciaran O'Hare @ Github](#)

Hillas Plot



A. M. Hillas

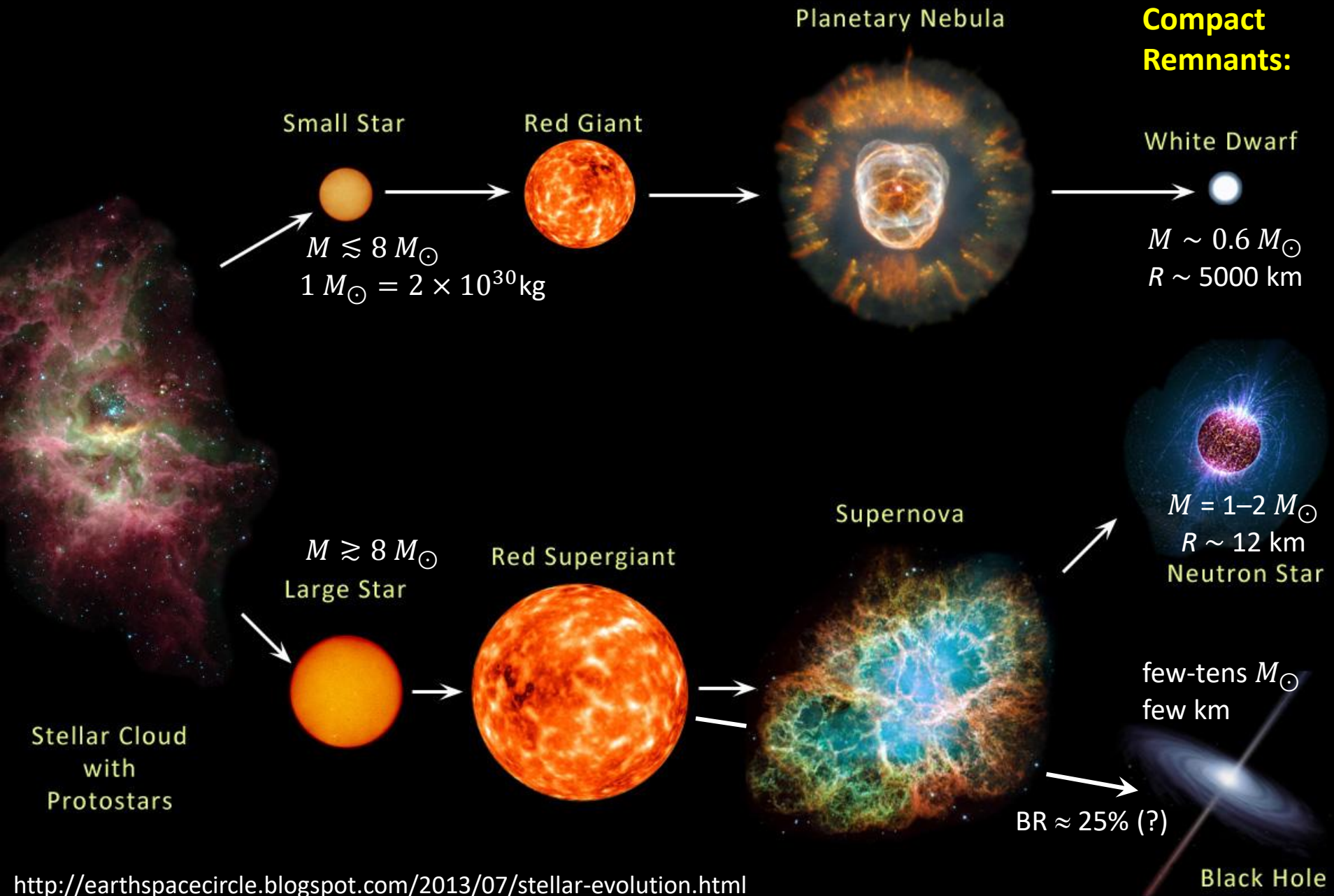
Ann. Rev. Astron. Astrophys.
22, 425 (1984)

Size and B field strength
of possible sites for
particle acceleration.
Objects below the
line cannot accelerate
protons to 10^{20} eV

ALP- γ conversion

$$\frac{g_{a\gamma}}{10^{12} \text{ GeV}} BL \sim 1$$

EVOLUTION OF STARS

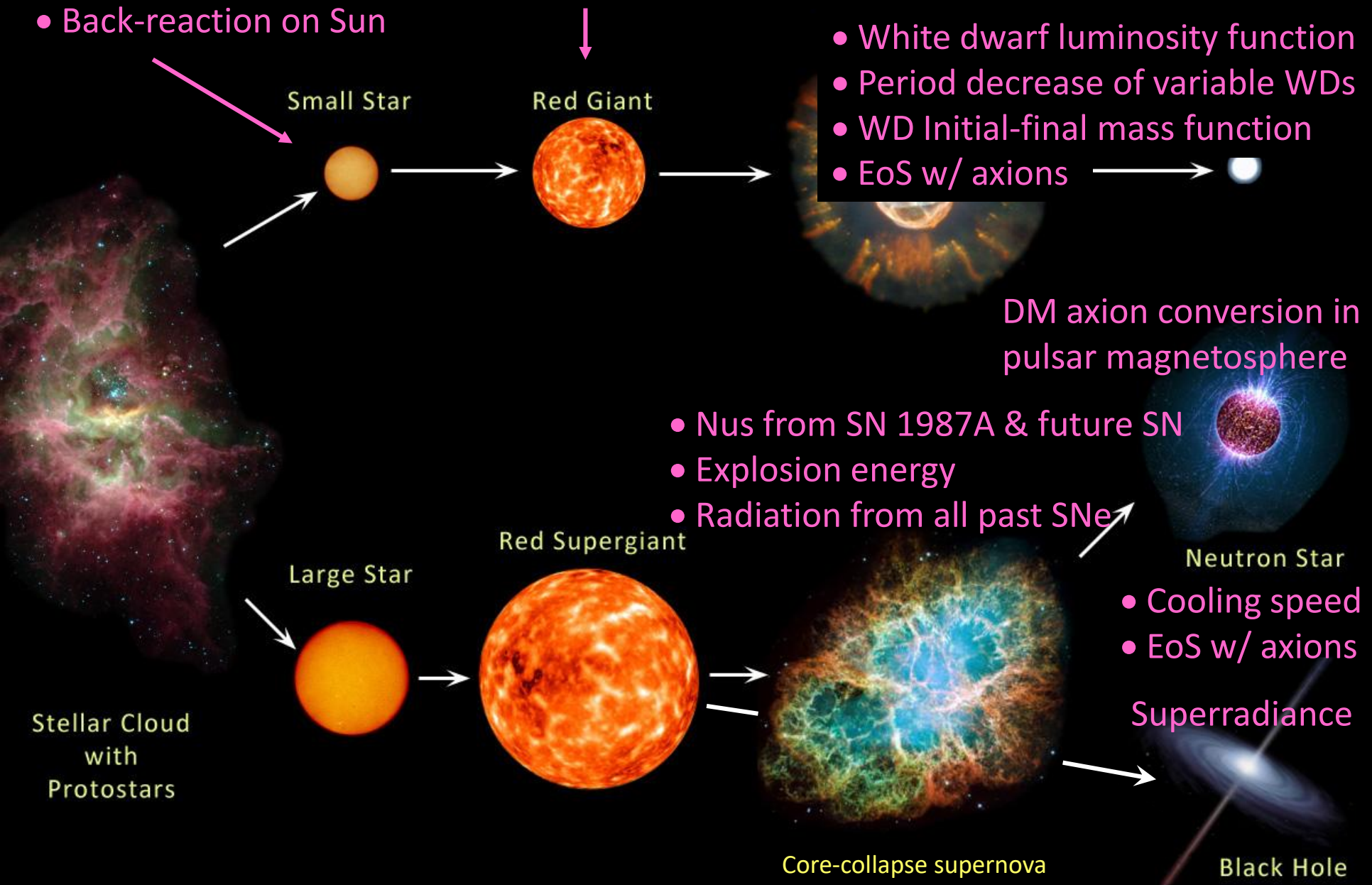


Particles from the Sun:

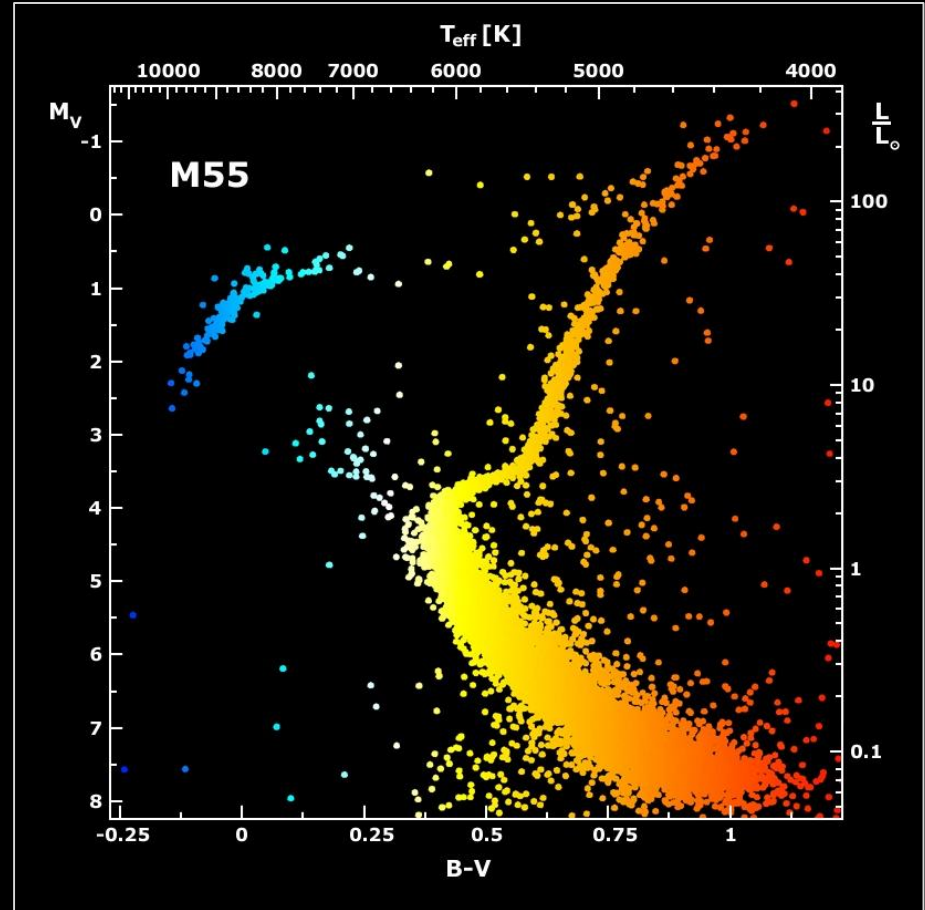
- Direct search
- Back-reaction on Sun

- Number counts in globular clusters
- Brightness of tip of red-giant branch (TRGB)

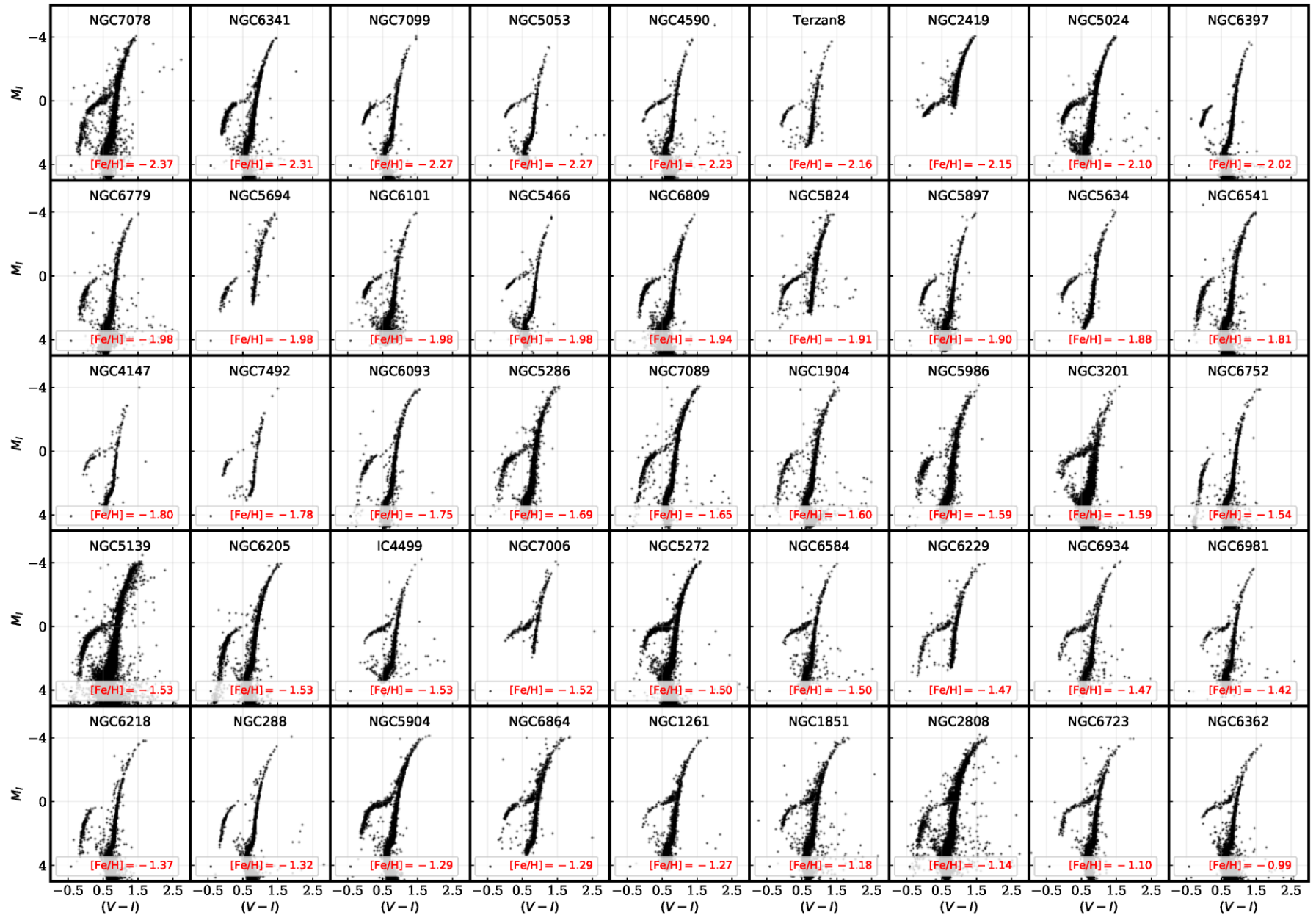
- White dwarf luminosity function
- Period decrease of variable WDs
- WD Initial-final mass function
- EoS w/ axions



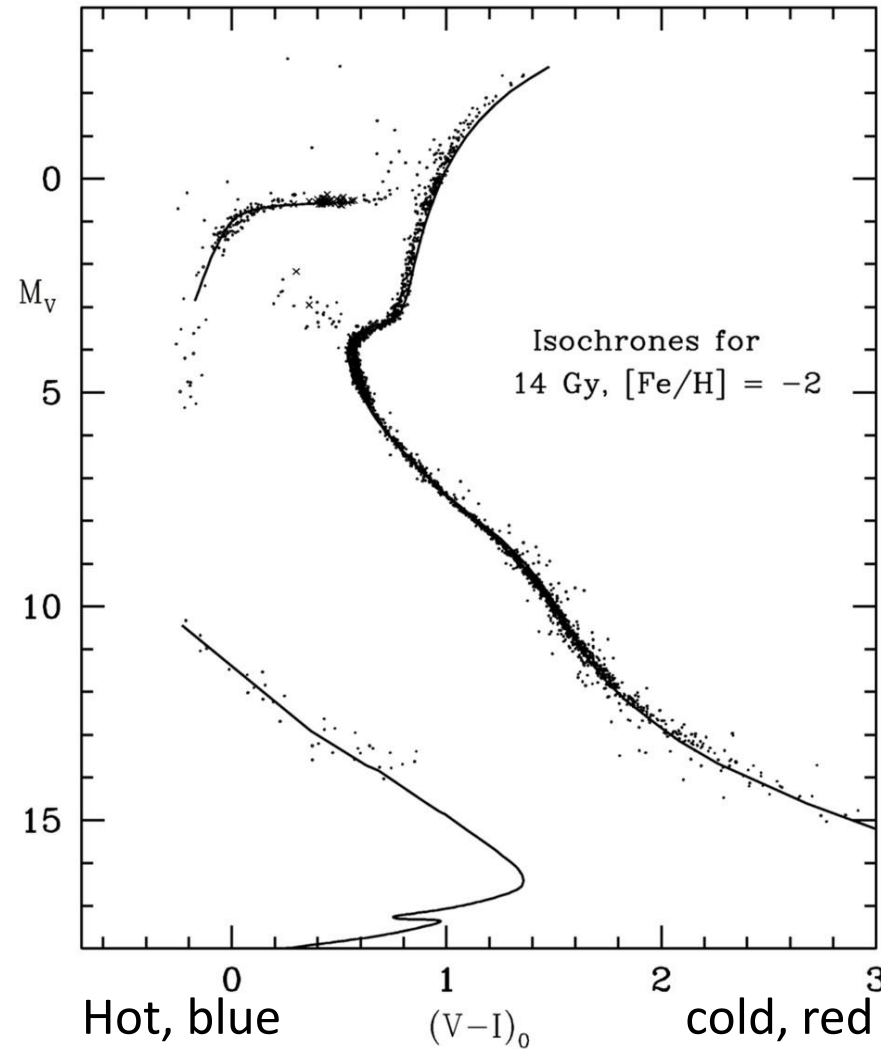
Galactic Globular Cluster M55



TRGB in 46 Globular Clusters [Cerny+ 2012.09701]

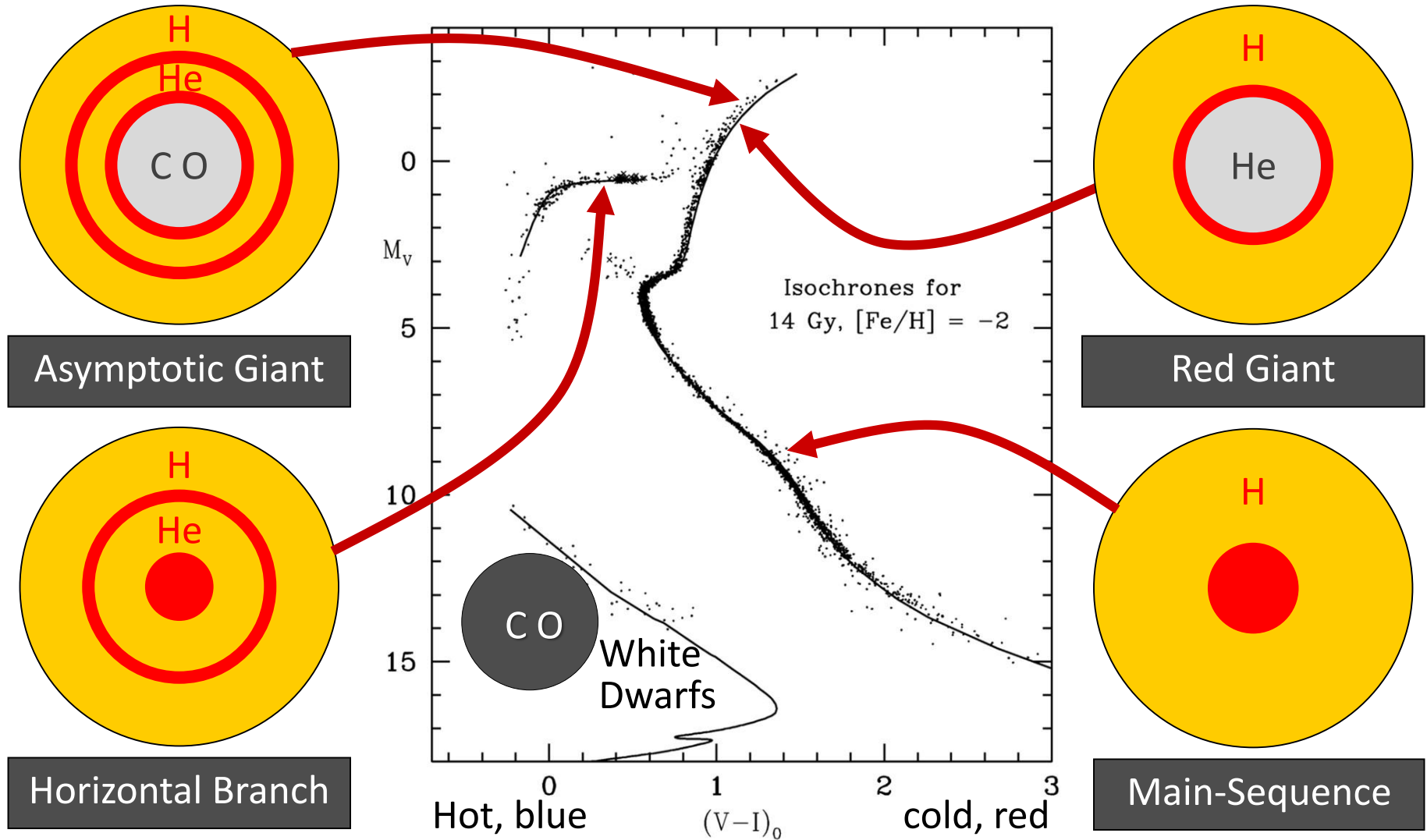


Color-Magnitude Diagram for Globular Clusters



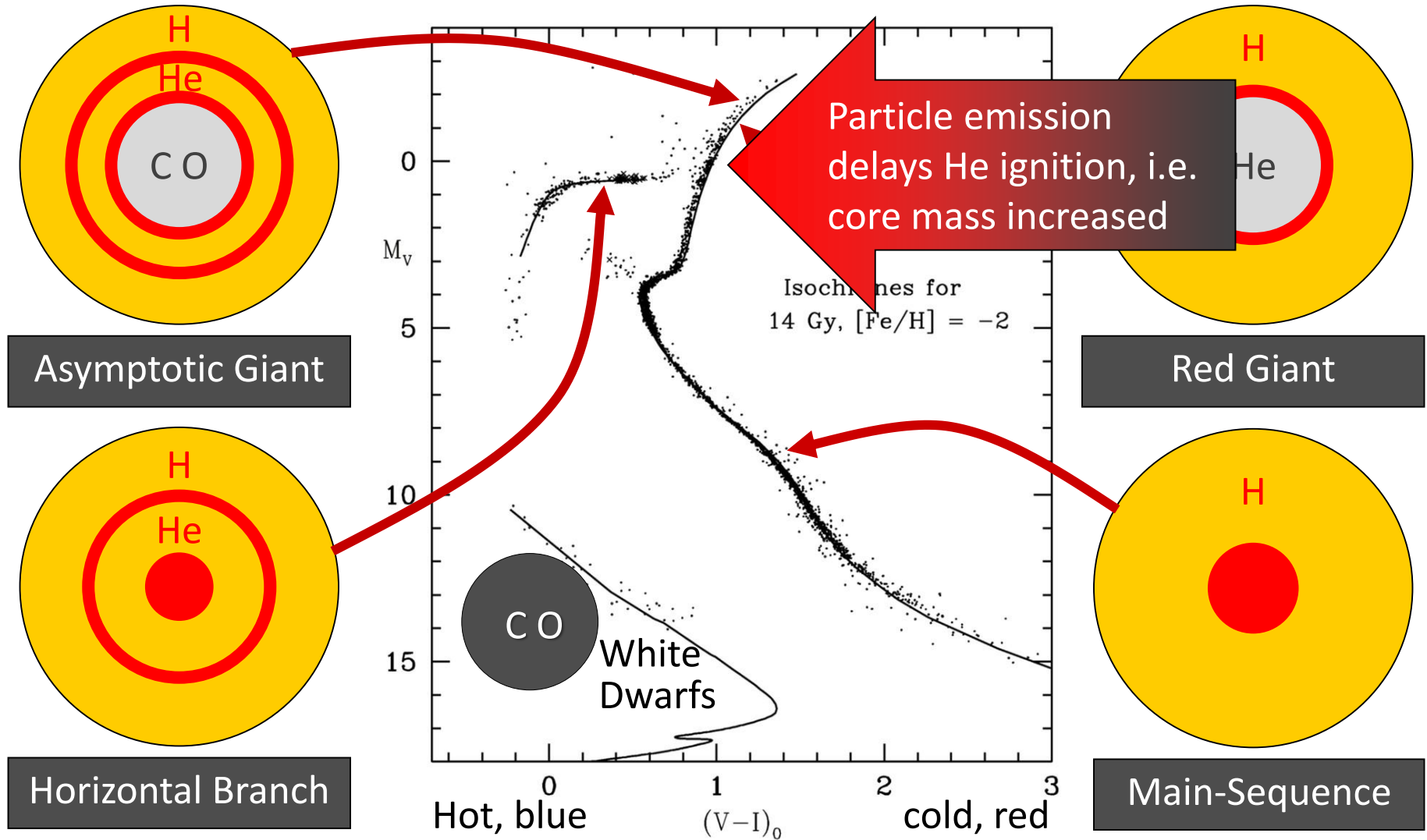
Color-magnitude diagram synthesized from several low-metallicity globular clusters and compared with theoretical isochrones (W.Harris, 2000)

Color-Magnitude Diagram for Globular Clusters



Color-magnitude diagram synthesized from several low-metallicity globular clusters and compared with theoretical isochrones (W.Harris, 2000)

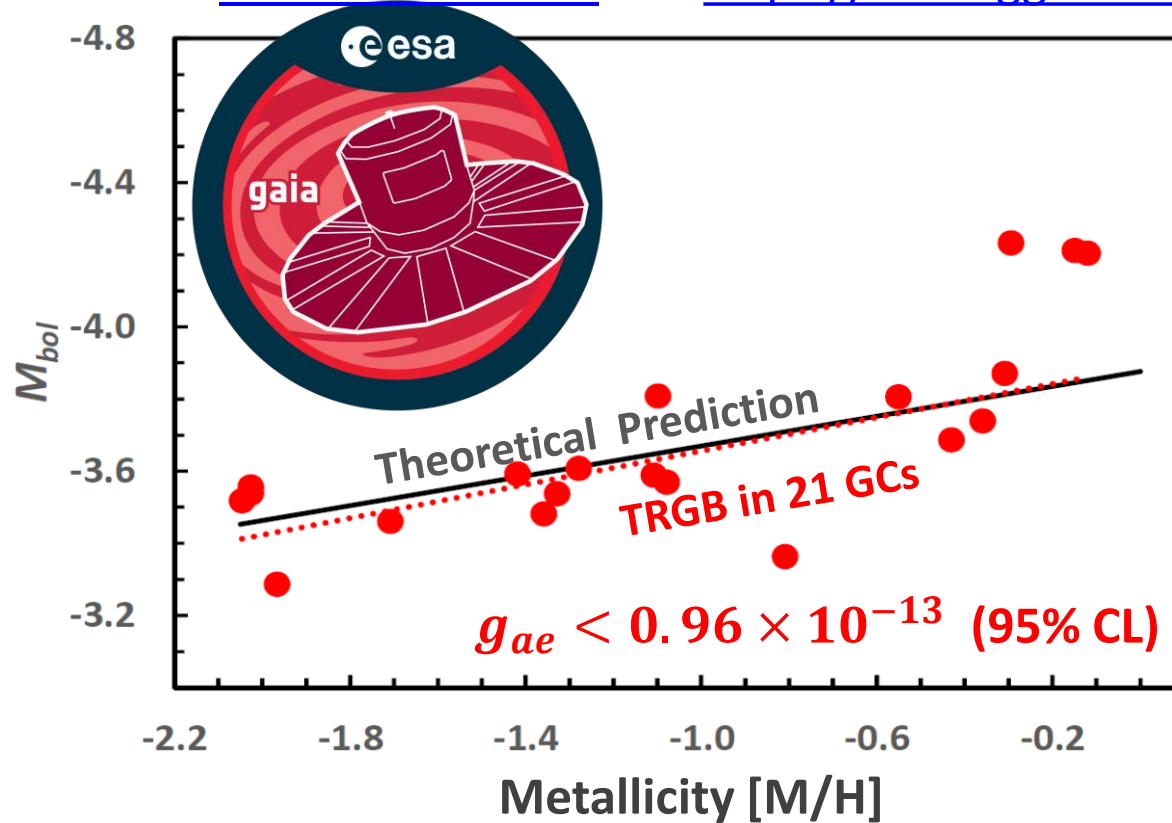
Color-Magnitude Diagram for Globular Clusters



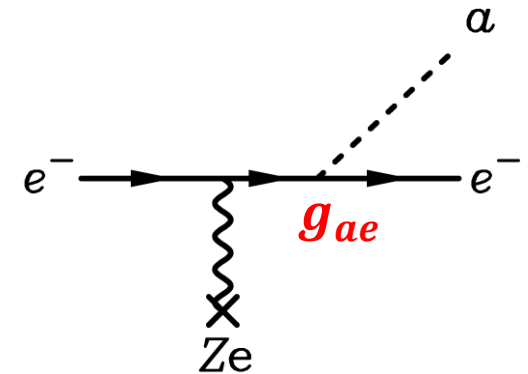
Color-magnitude diagram synthesized from several low-metallicity globular clusters and compared with theoretical isochrones (W.Harris, 2000)

New TRGB Calibration from 21 Globular Clusters

Straniero+ [arXiv:2010.03833](https://arxiv.org/abs/2010.03833) and <https://www.ggi.infn.it/talkfiles/slides/slides6554.pdf>



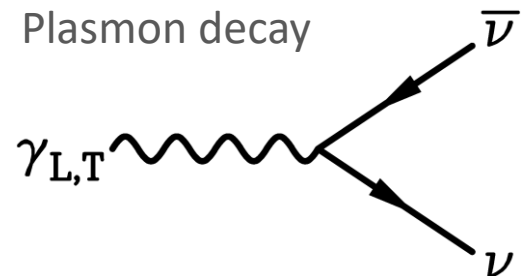
Emission of axions & friends
with direct electron coupling



Bremsstrahlung emission by
degenerate electrons

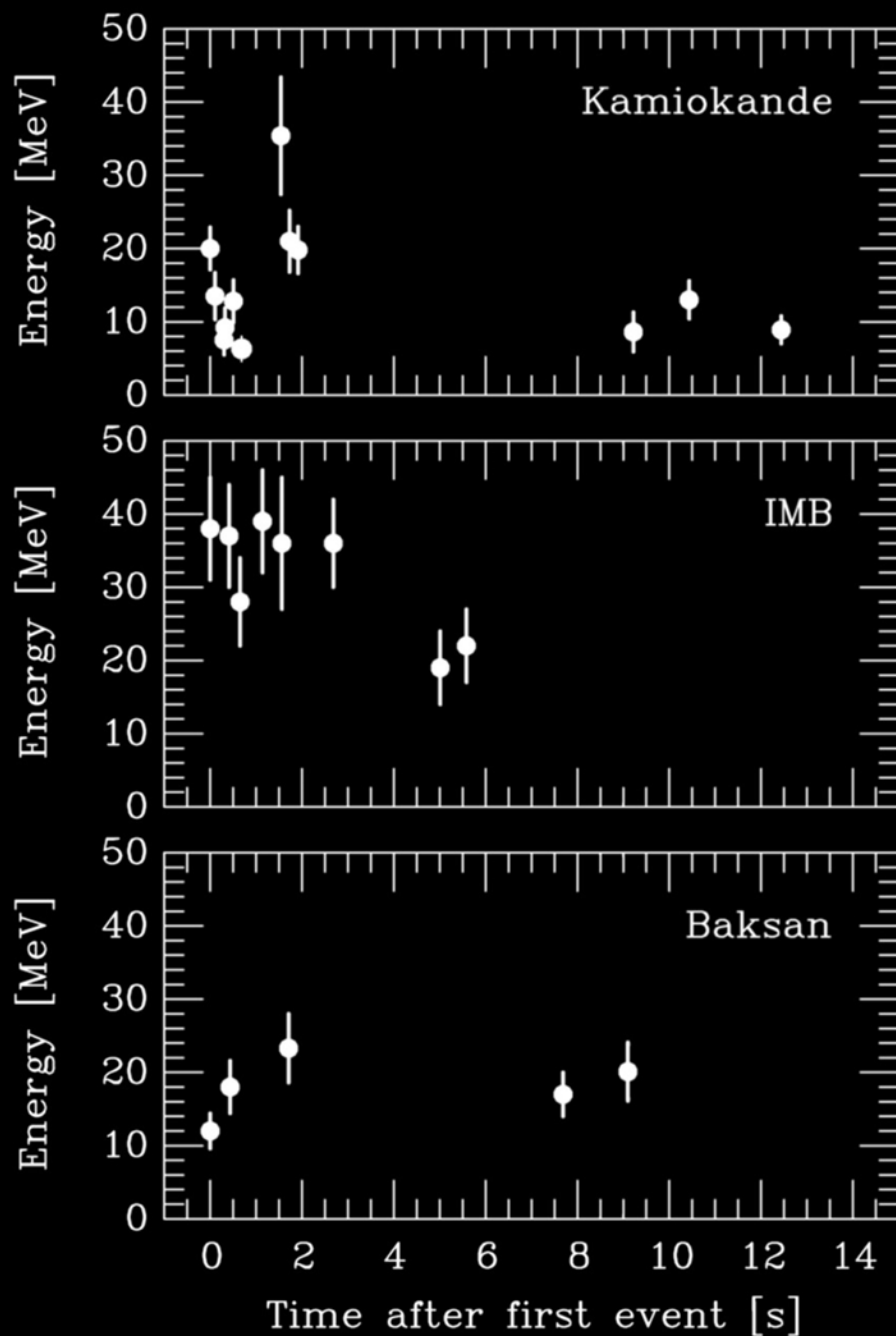
Bound for neutrino dipole moments

$$\sqrt{\sum_i |\mu_i|^2} < 0.92 \times 10^{-12} \mu_B \text{ (95\% CL)}$$

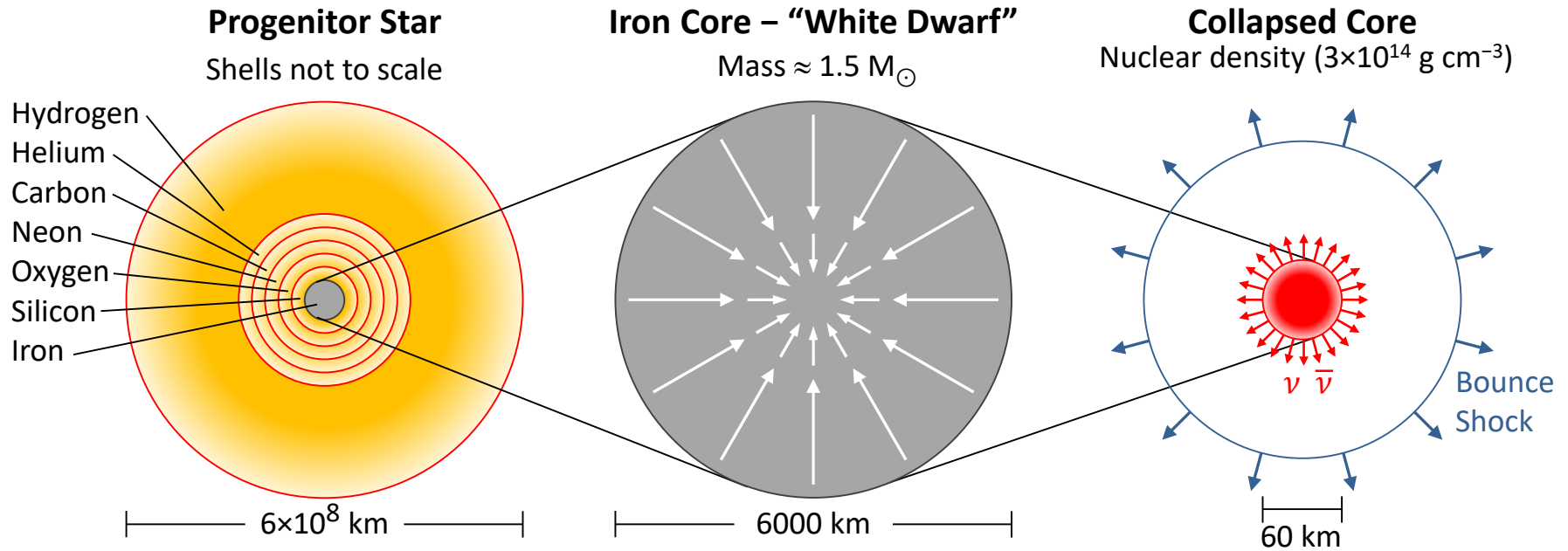


Supernova 1987A

23 February 1987



Stellar Collapse and Explosion



Gravitational binding energy

$$E_b \approx 3 \times 10^{53} \text{ erg} \approx 15\% M_{\text{SUN}} c^2$$

This shows up as

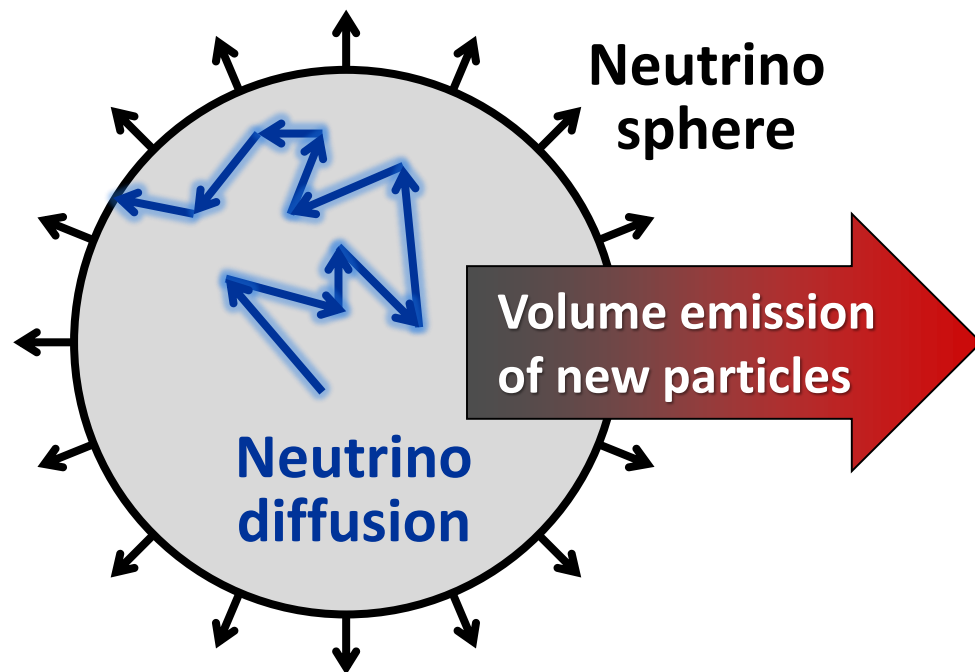
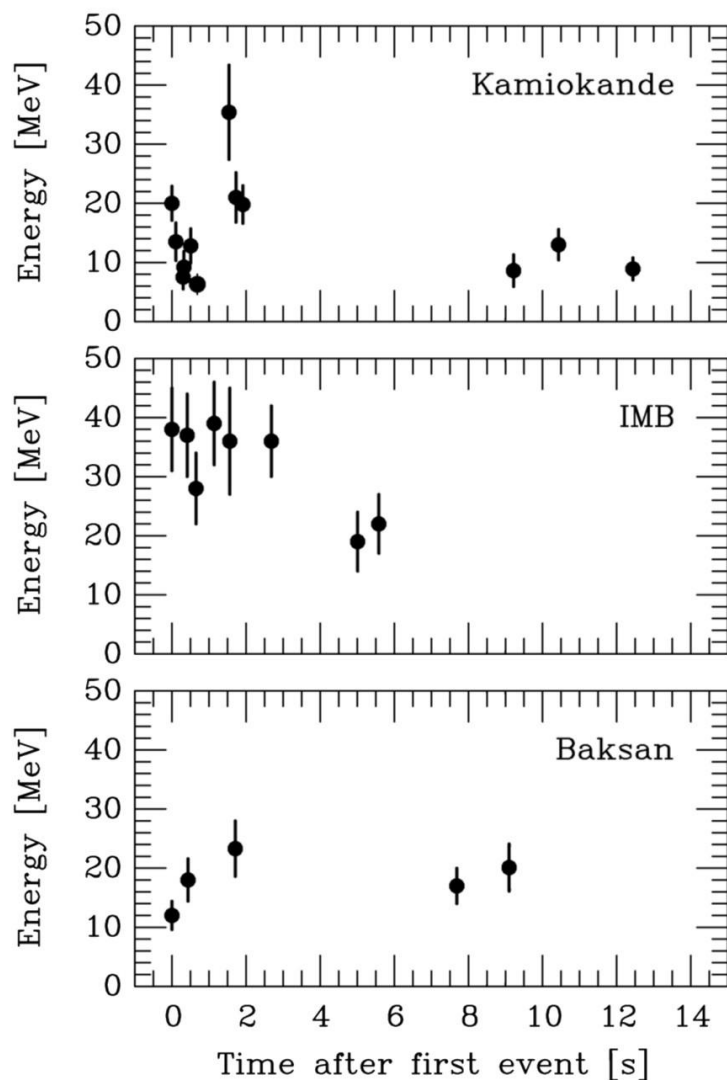
99% Neutrinos

1% Kinetic energy of explosion

0.01% Photons, outshine host galaxy

Supernova 1987A Energy-Loss Argument

SN 1987A neutrino signal

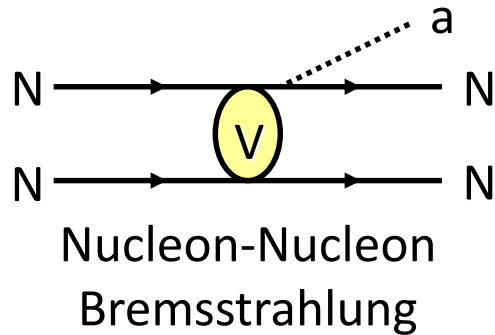


Emission of very weakly interacting particles would “steal” energy from the neutrino burst and shorten it.
(Early neutrino burst powered by accretion, not sensitive to volume energy loss.)

Late-time signal most sensitive observable

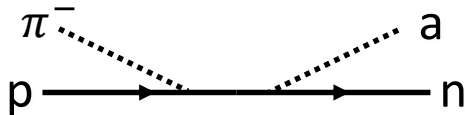
Axion Emission from a Nuclear Medium

Axion-nucleon interaction: $\mathcal{L}_{\text{int}} = \frac{c_N}{2f_a} \bar{\Psi}_N \gamma_\mu \gamma_5 \Psi_N \partial^\mu a = \frac{c_N}{2f_a} J_\mu^A \partial^\mu a$



+ ... Axial-vector interaction implies dominance of spin-dependent process

- Interaction potential (one-pion exchange OPE was often used, but too simplistic) → **Carenza+** [arXiv:1906.11844](https://arxiv.org/abs/1906.11844)
- In-medium coupling constants → **Springmann+** [arXiv:2410.10945](https://arxiv.org/abs/2410.10945)
- In-medium effective nucleon properties
- Correlation effects (static and dynamical spin-spin correlations)
- Thermal π^- contribute significantly (dominantly?) → **Carenza+** [arXiv:2010.02943](https://arxiv.org/abs/2010.02943)



Axion emission is a complicated nuclear physics problem, for several issues see **Fiorillo, Gil Muyor, Janka, Raffelt & Vitagliano**, [arXiv:2509.13322](https://arxiv.org/abs/2509.13322)

SN 1987A Axion Limits from Burst Duration

- Raffelt, Lect. Notes Phys. 741 (2008) 51 [hep-ph/0611350](#)
Burst duration calibrated by early numerical studies
“Generic” emission rates inspired by OPE rates
 $f_a \gtrsim 4 \times 10^8 \text{ GeV}$ and $m_a \lesssim 16 \text{ meV}$ (KSVZ, based on proton coupling)
- Chang, Essig & McDermott, JHEP 1809 (2018) 051 [1803.00993](#)
Various correction factors to emission rates, specific SN core models
 $f_a \gtrsim 1 \times 10^8 \text{ GeV}$ and $m_a \lesssim 60 \text{ meV}$ (KSVZ, based on proton coupling)
- Carenza, Fischer, Giannotti, Guo, Martínez-Pinedo & Mirizzi, JCAP 10 (2019) 016 & Erratum [1906.11844](#)
Beyond OPE emission rates, specific SN core models: similar to Chang et al.
 $f_a \gtrsim 4 \times 10^8 \text{ GeV}$ and $m_a \lesssim 15 \text{ meV}$ (KSVZ, based on proton coupling)
- Carenza, Fore, Giannotti, Mirizzi & Reddy [2010.02943](#)
Including thermal pions $\pi^- + p \rightarrow n + a$ (factor 3 larger emission)
 $f_a \gtrsim 5 \times 10^8 \text{ GeV}$ and $m_a \lesssim 11 \text{ meV}$ (KSVZ, based on proton coupling)
- Bar, Blum & D'Amico, **Is there a supernova bound on axions?** [1907.05020](#)
Alternative picture of SN explosion (thermonuclear event)
Observed signal not PNS cooling. SN1987A neutron star (or pulsar) not yet found.
(but see “NS 1987A in SN 1987A”, Page et al. arXiv:2004.06078)

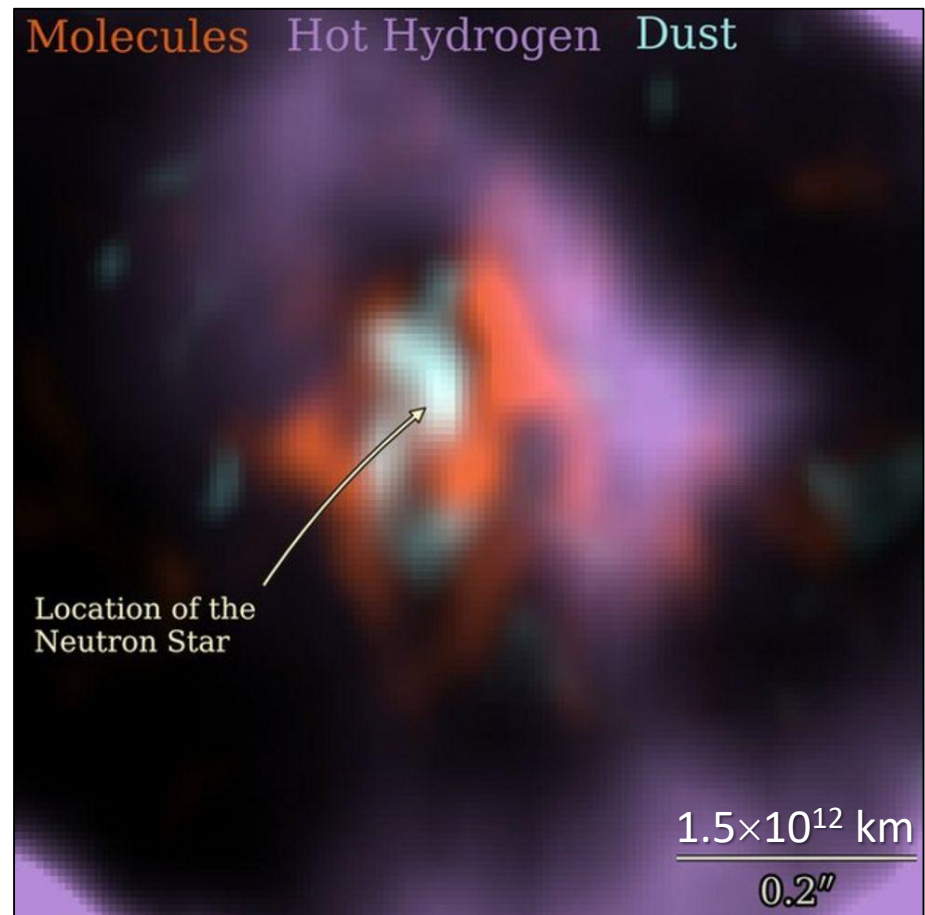
Where is the Neutron Star of SN 1987A?

No pulsar or neutron star has been seen until now (38 years later)

- Infra-red excess observed by ALMA: In “the blob” strong indication for NS
Expected position, remnant hidden by dust [Cigan+ arXiv:1910.02960]
- Most plausible model: Thermally cooling non-pulsar NS [Page+ arXiv:2004.06078]

<https://www.bbc.com/news/science-environment-50473482>

Atacama Large Millimeter/Submillimeter Array (ALMA) at ESO in Chile



SN 1987A Signal Duration Too Long?

Fiorillo+ [arXiv:2308.01403](https://arxiv.org/abs/2308.01403)

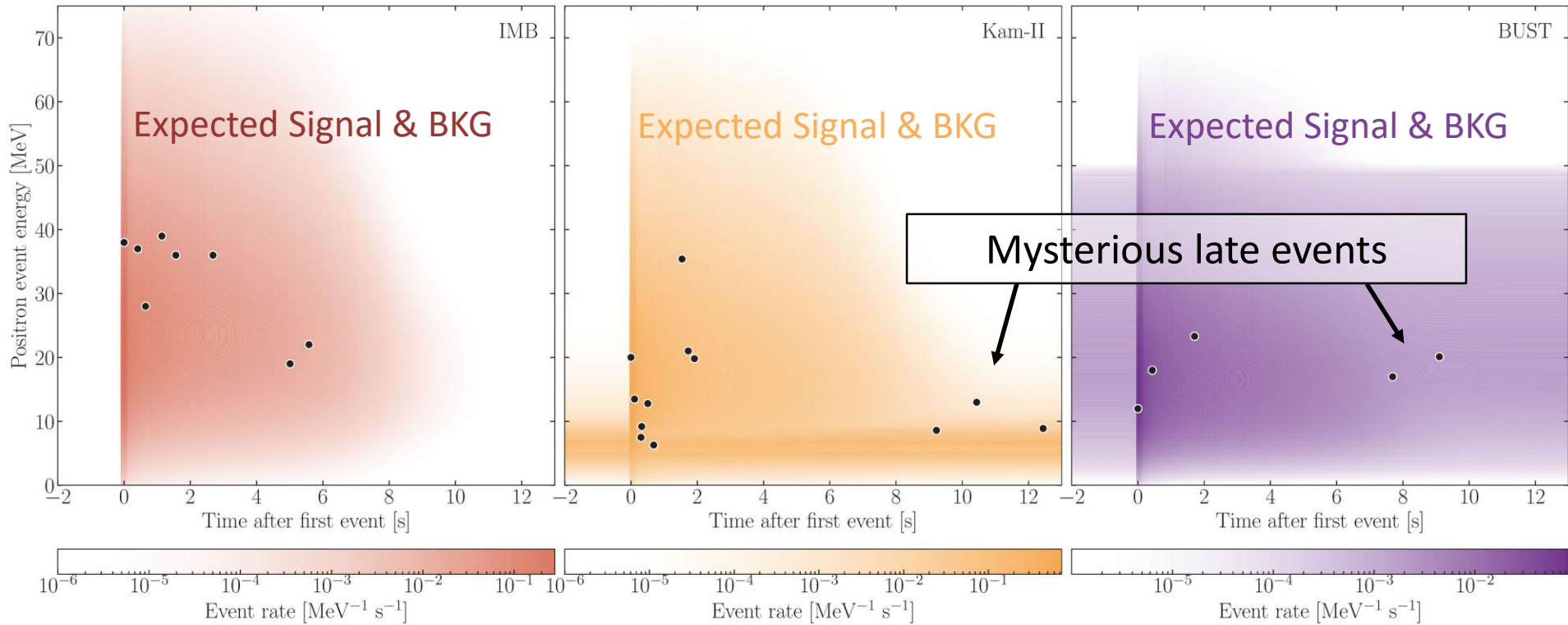
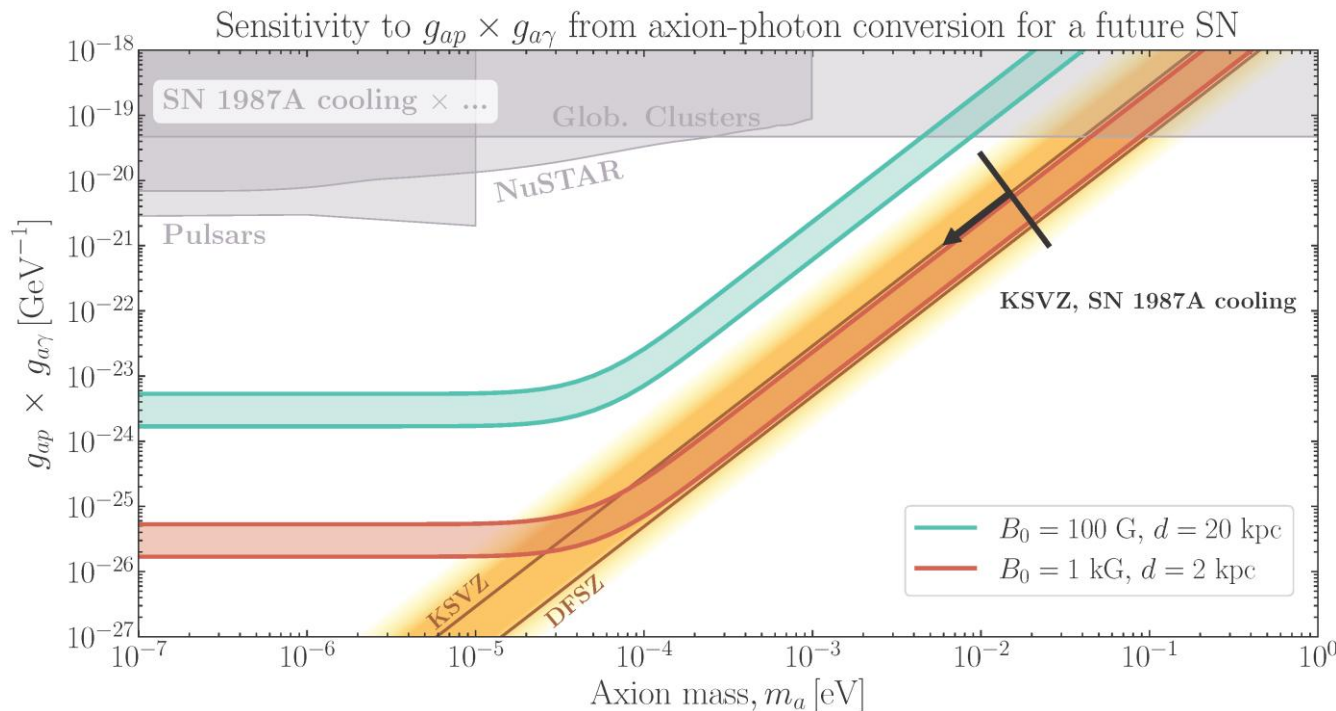
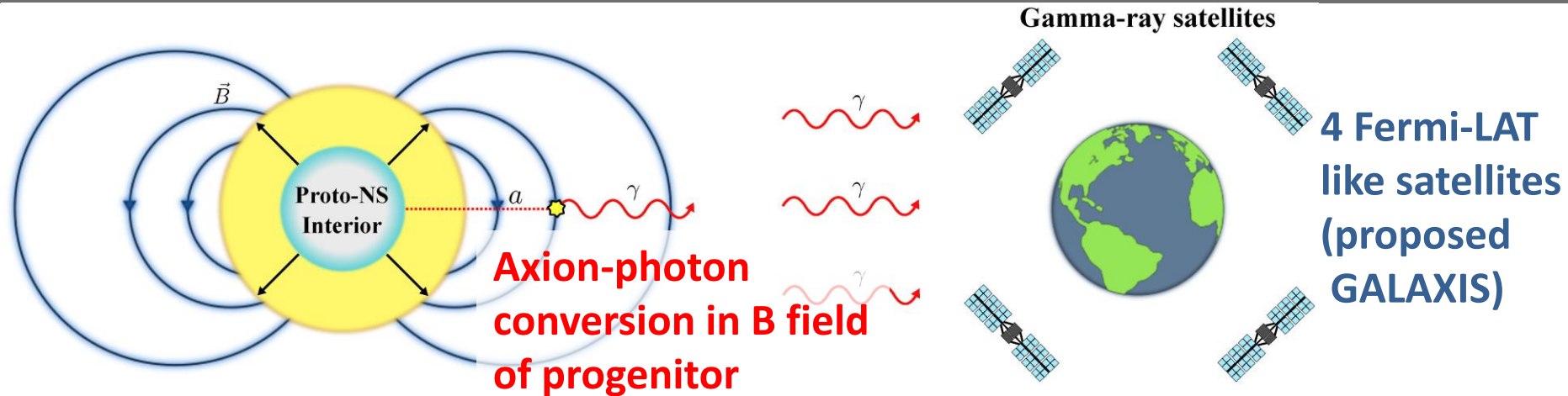


FIG. 17. Differential event distribution (signal and background) at each experiment, compared with the observations. Results are shown for model 1.44-SFHo without flavor swap; the offset time for each experiment is chosen as the best-fit value reported in Table VII.

- In a suite of Garching models (no axions), expected signal always too short (PNS convection and reduced opacities by correlations!)
- Deserves dedicated study

Detecting Axions with Next Galactic Supernova?



Manzari+
arXiv:2405.19393

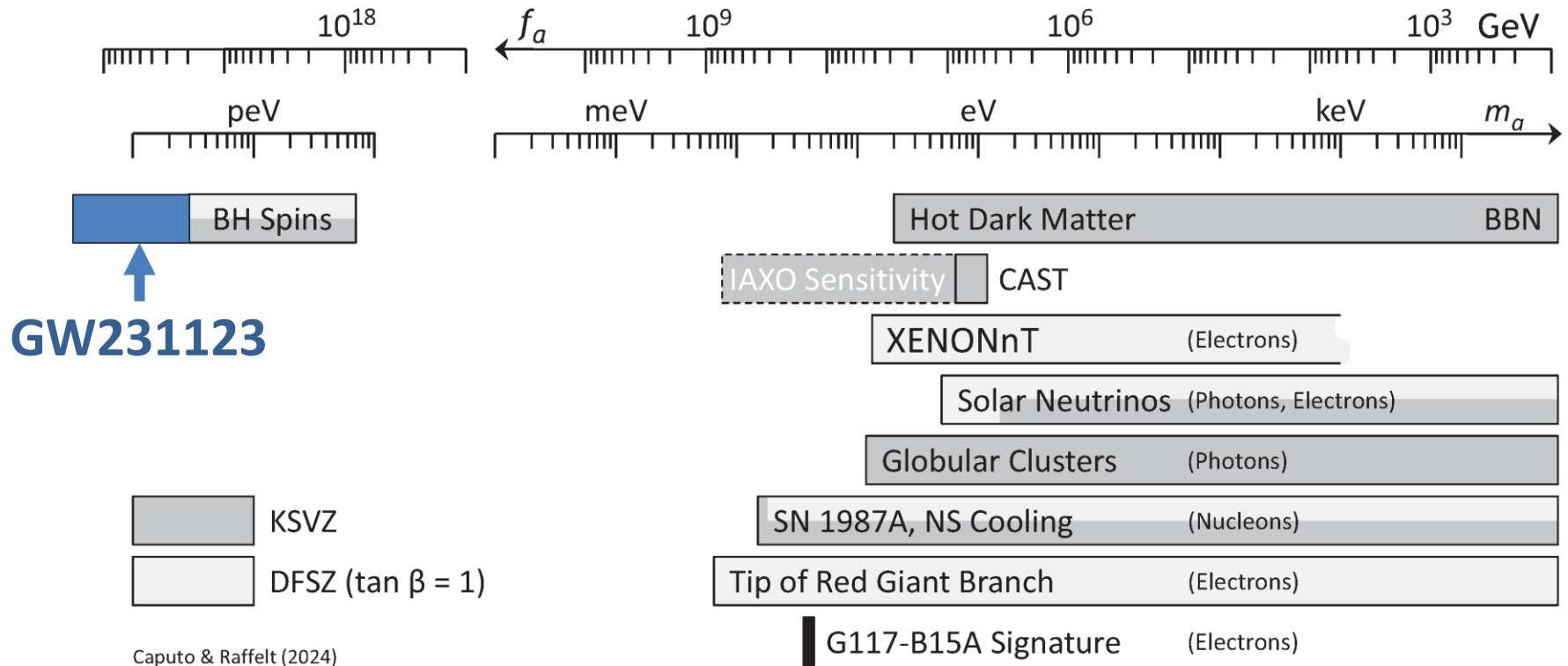
This figure:
Fiorillo, Gil Muyor,
Janka, Raffelt & Vitagliano
arXiv:2509.13322

For optimistic SN assumptions (distance, B field) QCD axion parameters reachable

Astrophysical Axion Bounds

The 2024 Edition, Caputo & Raffelt, arXiv:2401.13728, 24 Jan 2024

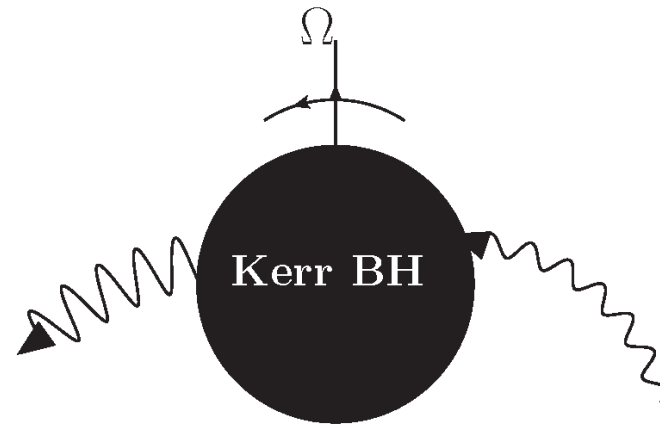
See also Carenza, Giannotti, Isern, Mirizzi & Straniero, arXiv:2411.02492



- Many improvements over the years, but overall picture the same
- Specific QCD axion signatures cannot come from cooling effects
- **Best stellar detection opportunity probably (Baby)IAXO**

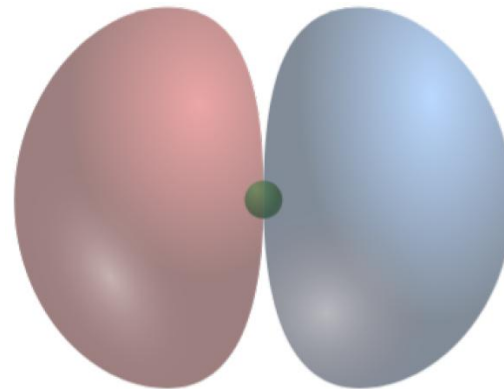
Superradiance

Extraction of rotational energy from spinning object by low-frequency modes $\omega < \Omega$ of an external bosonic field



$$m\Omega > \omega$$

- Bosons with mass get gravitationally bound
- Superradiant run-away mode
 $\phi = Y_{lm}(\theta, \phi)\psi_{lmn}(r)e^{\mathbf{r}t}$
- “Bosonic atom”
- Transitions $\rightarrow$ Gravitational waves

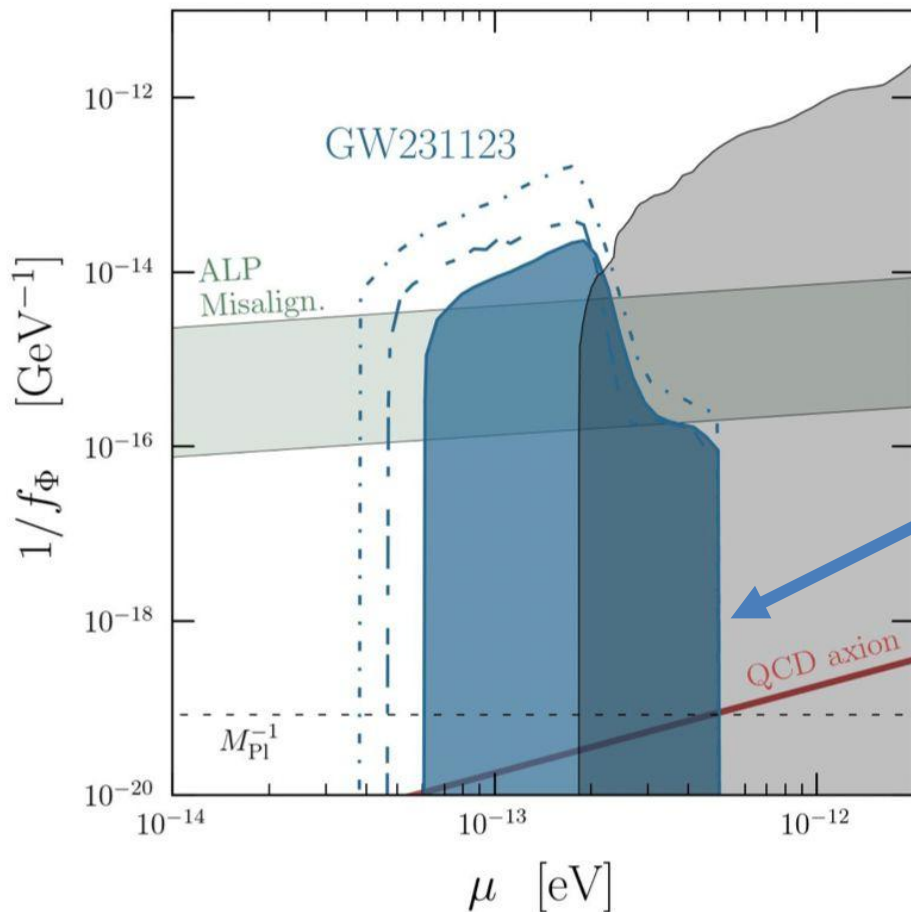


Superradiance: New Frontiers in Black Hole Physics (2020 edition)

R. Brito, V. Cardoso & P. Pani, [1501.06570v8](#) (8 Jan 2021)

BH Spins from Binary Merger GW231123

LIGO-Virgo-KAGRA observed GWs from BH-BH merger GW231123
 $137^{+22}_{-17} M_{\odot}$ and $103^{+20}_{-52} M_{\odot}$ with large spins

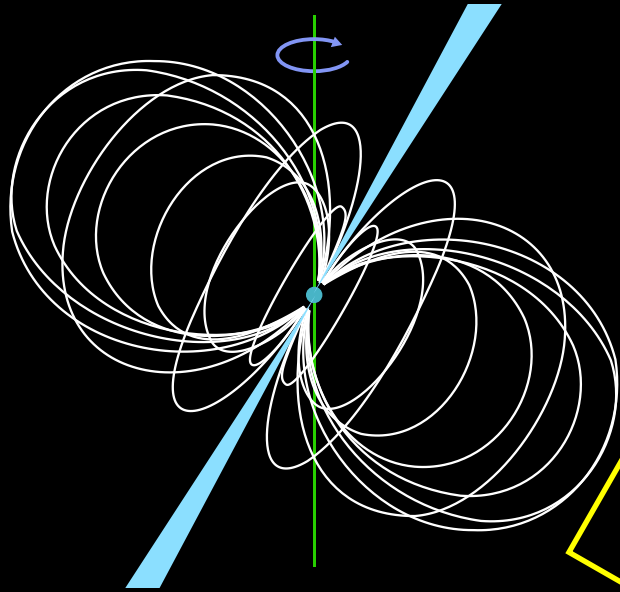


New superradiance bounds on scalar boson masses

Caputo, Franciolini & Witte
arXiv:[2507.21788](https://arxiv.org/abs/2507.21788) (29 July 2025)

Aswathi, East, Siemonsen, Sun & Jones
arXiv:[2507.20979](https://arxiv.org/abs/2507.20979) (28 July 2025)

Dark Matter Axion-Photon Conversion in Neutron Star Magnetospheres



Dark matter axions
 $m_a \sim \mu\text{eV}$, $v_a \sim 10^{-3}c$

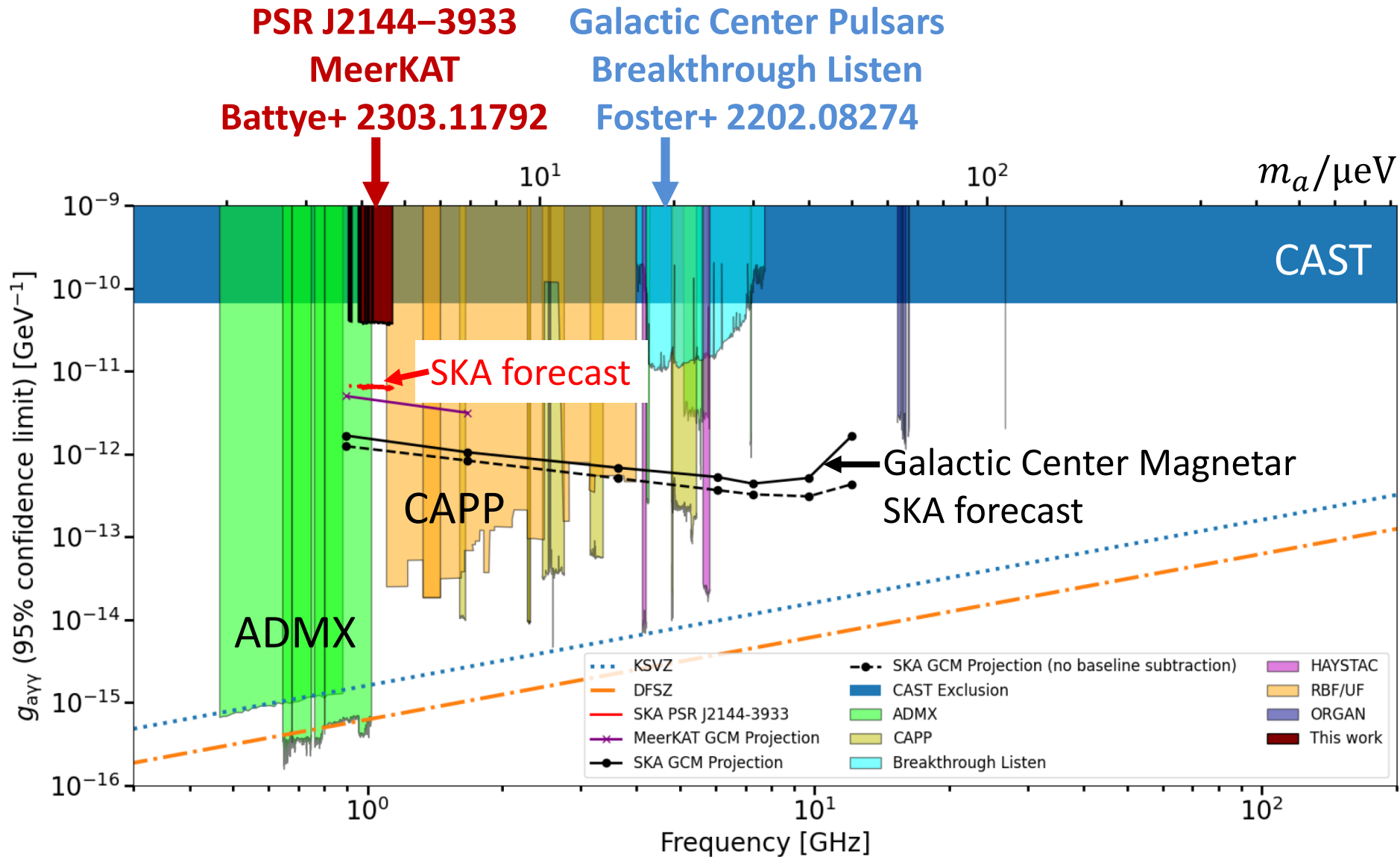
Very narrow
radio line

Axion mass and plasma frequency
Degenerate near NS surface
→ Resonant conversion

Pshirkov & Popov 2007
arXiv:0711.1264
Many papers recently



Searching for Axions with Radio Telescopes



Axion Clouds around Neutron Stars

Polar cap cascades

D.Noordhuis, A.Prabhu, S.J.Witte, A.Y.Chen,
F.Cruz & C.Weniger, [arXiv:2209.09917](https://arxiv.org/abs/2209.09917)

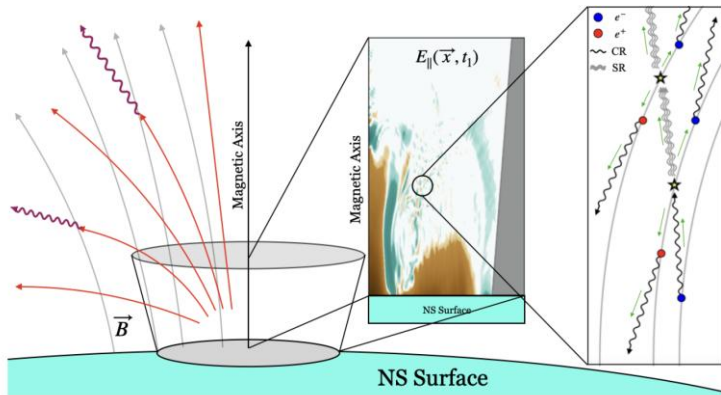
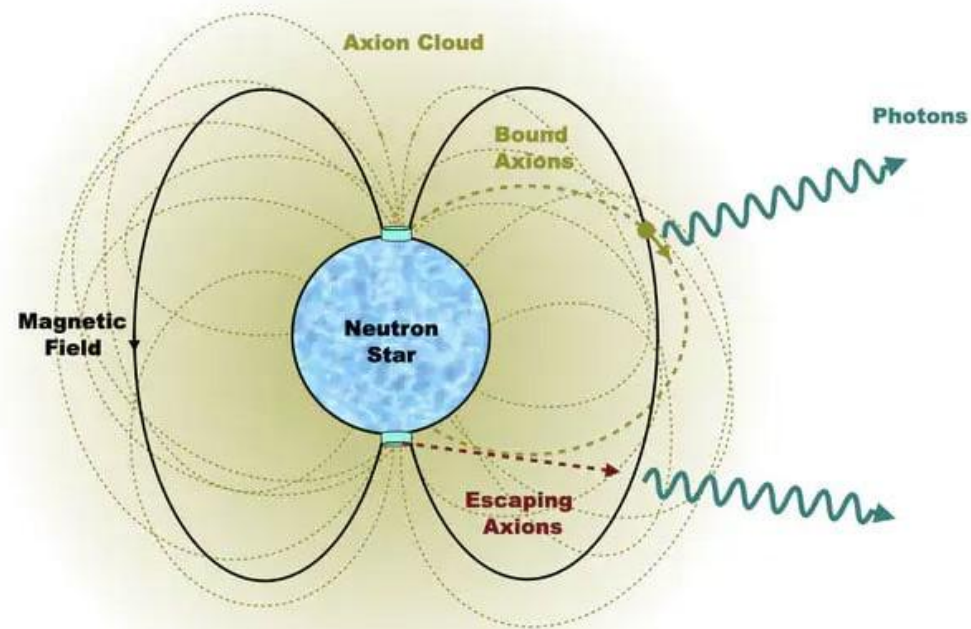


FIG. 1. Schematic figure showing axion production in neutron star vacuum gaps. The vacuum gap is depicted by a truncated cone on the neutron star surface. The left inset shows a time snapshot of $E_{\parallel}$ (as computed in the simulations of [67]), with brown/green coloring reflecting negative/positive values of $E_{\parallel}$. The right inset depicts the microphysical processes responsible for the pair cascade, with green arrows indicating the direction the cascade flows with time. Axions (red) are emitted from gap and periodically convert to photons (purple) in the presence of the neutron star's magnetic field, $\vec{B}$ (grey).

- E-field extracts charges
- QED cascade
- Shuts off E-field
- Cascade stops
- ...
- Periodic E modulation
- Periodic $\vec{E} \cdot \vec{B}$
- Sources ALPs

D.Noordhuis, A.Prabhu, C.Weniger &
S.J.Witte, [arXiv:2307.11811](https://arxiv.org/abs/2307.11811)



IOP Publishing

physicsworld



ASTROPHYSICAL SEARCHES
OF DARK SECTORS WITH
RADIO WAVE OBSERVATIONS

Instituto de Astrofísica
de Canarias (IAC)

Undark

1ST W O R K S H O P

29 09 2025

03 10 2025

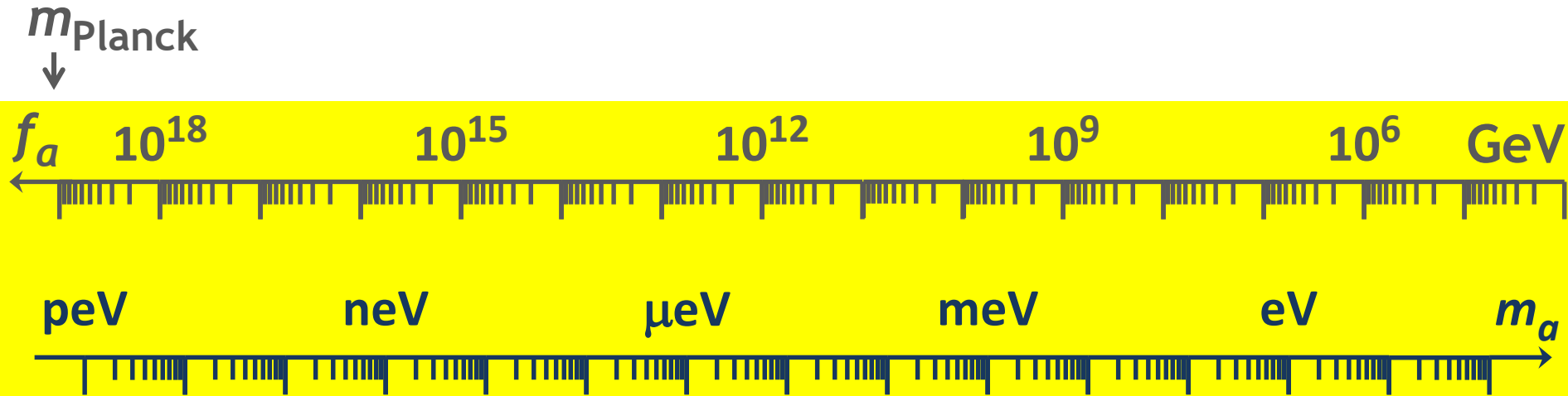


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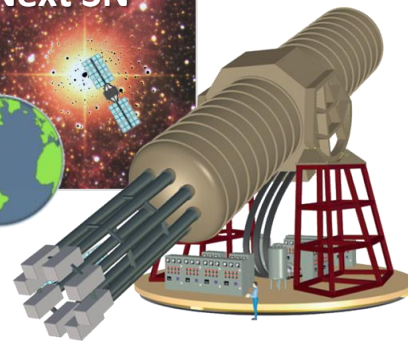
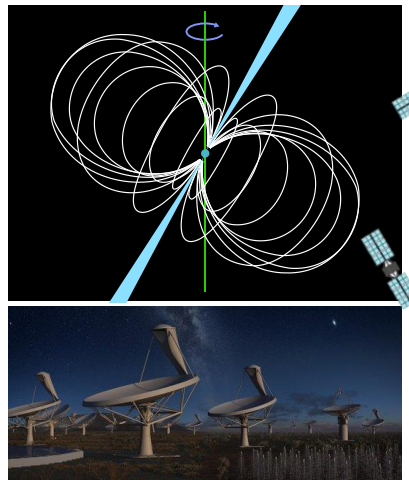
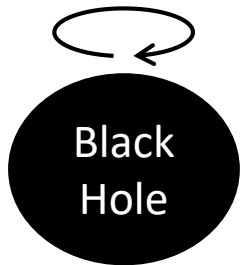
Astrophysical Axion Bounds and Opportunities



Super
Radiance

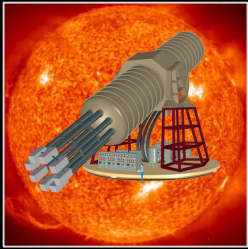
Opportunities for detection

Astrophysical Bounds
(Energy loss of stars)



IAXO Solar
Axion Telescope

Axion conversion in neutron star magnetospheres



- Best bet for systematic axion search with stars

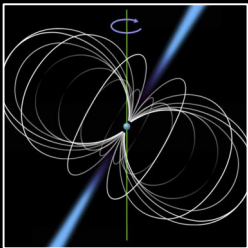


Globular clusters should be more systematically studied

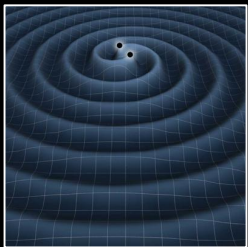
- Best bounds on electron and photon coupling
- Cooling hints inconsistent



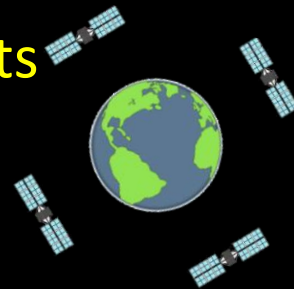
- SN1987A bounds unchanged, many refinements
- Next SN: Putting these on firm basis
- GALAXIS or IAXO detection opportunity



- Radio detection from pulsars
(DM conversion, polar-cap production)

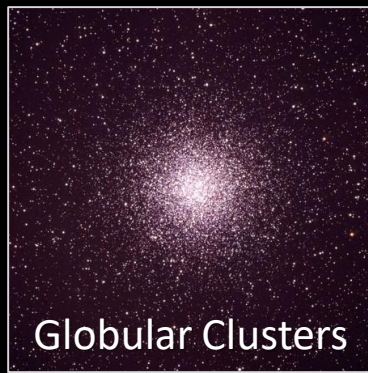


- Superradiance limits from BH spins (very small masses)
- GW signals can still show up





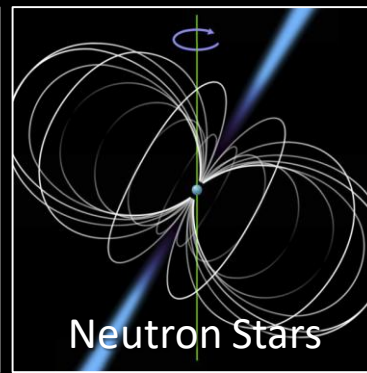
Solar Axions



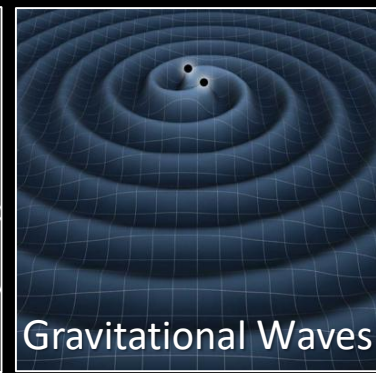
Globular Clusters



Supernova 1987A



Neutron Stars

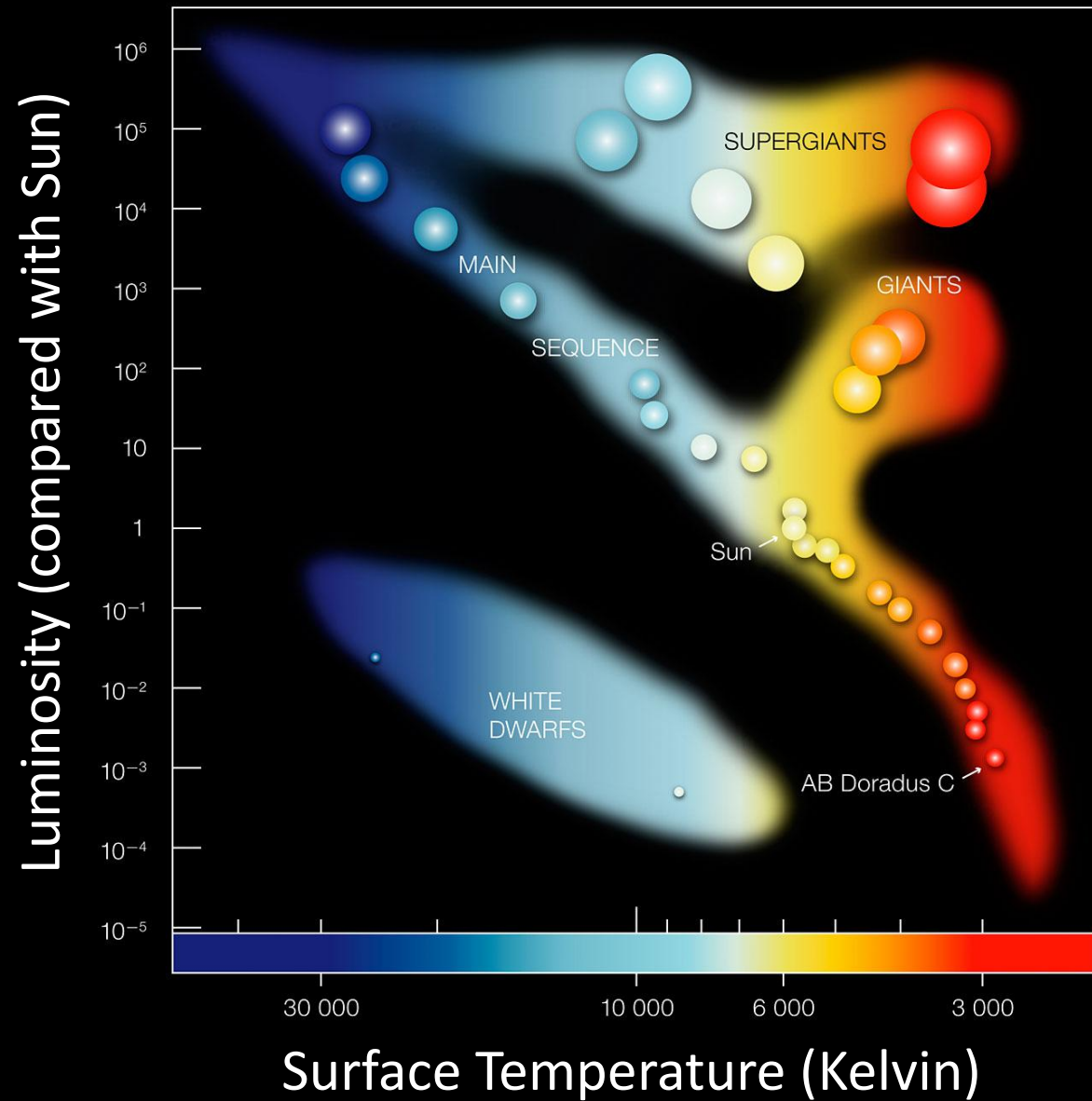


Gravitational Waves

Thanks!

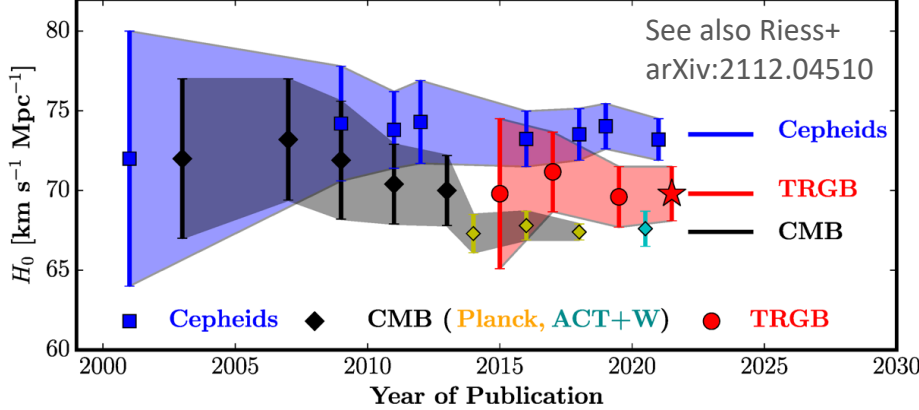
Bonus Topics

Globular Cluster Stars

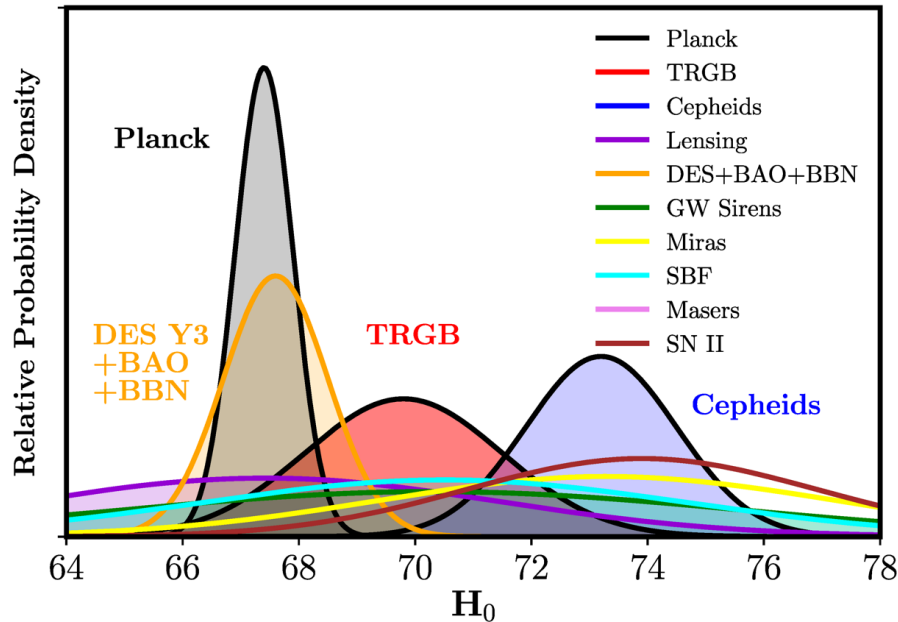


Hubble Tension

Hubble Constant Over Time



Recent Published H_0 Values



Freedman ApJ 919 (2021) 16 [2106.15656]

CMB with Planck
 Baikenhol et al. (2021), Planck 2018+SPT+ACT: 67.49 ± 0.53
 Pogosian et al. (2020), eBOSS+Planck $\Omega_m H^2$: 69.6 ± 1.8
 Aghanim et al. (2020), Planck 2018: 67.27 ± 0.60
 Aghanim et al. (2020), Planck 2018+CMB lensing: 67.36 ± 0.54
 Ade et al. (2016), Planck 2015, $H_0 = 67.27 \pm 0.66$

CMB without Planck
 Dutcher et al. (2021), SPT: 68.8 ± 1.5
 Aiola et al. (2020), ACT: 67.9 ± 1.5
 Aiola et al. (2020), WMAP9+ACT: 67.6 ± 1.1
 Zhang, Huang (2019), WMAP9+BAO: $68.36^{+0.53}_{-0.53}$
 Hinshaw et al. (2013), WMAP9: 70.0 ± 2.2

No CMB, with BBN
 D'Amico et al. (2020), BOSS DR12+BBN: 68.5 ± 2.2
 Philcox et al. (2020), P_1 +BAO+BBN: 68.5 ± 1.1
 Ivanov et al. (2020), BOSS+BBN: 67.9 ± 1.1
 Alam et al. (2020), BOSS+eBOSS+BBN: 67.35 ± 0.97

$P_1(k)$ + CMB lensing
 Philcox et al. (2020), $P_1(k)$ +CMB lensing: $70.6^{+3.0}_{-3.0}$

Cepheids – SNIa
 Riess et al. (2020), R20: 73.2 ± 1.3
 Breuval et al. (2020): 72.2 ± 2.7
 Riess et al. (2019), R19: 74.0 ± 1.4
 Camarena, Marra (2019): 75.4 ± 1.7
 Burns et al. (2018): 73.2 ± 2.3
 Dhawan, Jha, Leibundgut (2017), NIR: 72.8 ± 3.1
 Follin, Knox (2017): 73.3 ± 1.7
 Feeney, Mortlock, Dalmaso (2017): 73.2 ± 1.8
 Riess et al. (2016), R16: 73.2 ± 1.7
 Cardona, Kunz, Pettorino (2016), HPS: 73.8 ± 2.1
 Freedman et al. (2012): 74.3 ± 2.1

TRGB – SNIa
 Soltis, Casertano, Riess (2020): 72.1 ± 2.0
 Freedman et al. (2020): 69.6 ± 1.9
 Reid, Pesce, Riess (2019), SH0ES: 71.1 ± 1.9
 Freedman et al. (2019): 69.8 ± 1.9
 Yuan et al. (2019): 72.4 ± 2.0
 Jang, Lee (2017): 71.2 ± 2.5

Miras – SNIa
 Huang et al. (2019): 73.3 ± 4.0

Masers
 Pesce et al. (2020): 73.9 ± 3.0

Tully – Fisher Relation (TFR)
 Kourkchi et al. (2020): 76.0 ± 2.6
 Schombert, McGaugh, Lelli (2020): 75.1 ± 2.8

Surface Brightness Fluctuations
 Blakeslee et al. (2021) IR-SBF w/ HST: 73.3 ± 2.5
 Khetan et al. (2020) w/ LMC DEB: 71.1 ± 4.1

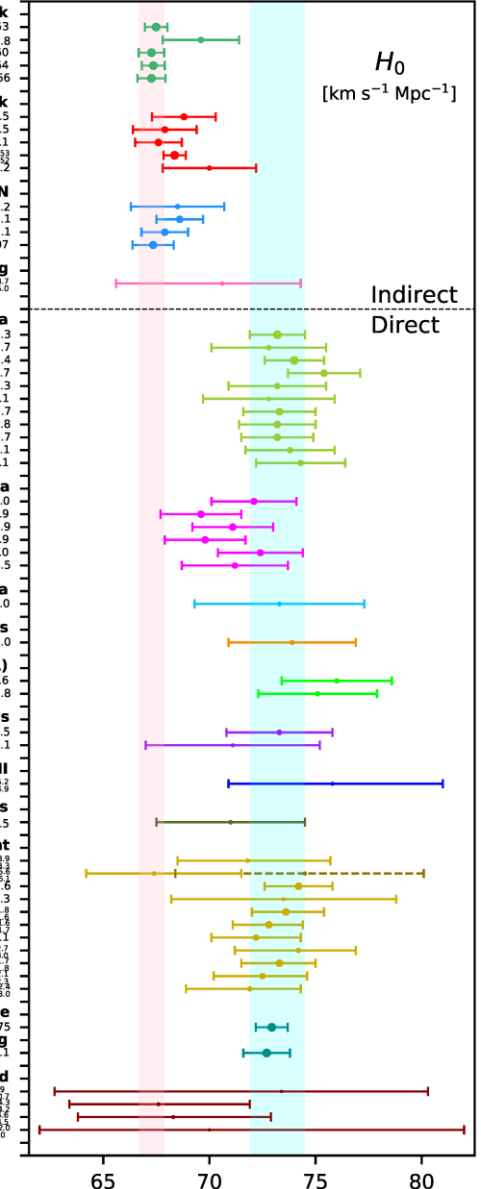
SNII
 de Jaeger et al. (2020): $75.8^{+3.3}_{-3.3}$

HII galaxies
 Fernández Arenas et al. (2018): 71.0 ± 3.5

Lensing related, mass model – dependent
 Denzel et al. (2021): $71.8^{+3.9}_{-3.9}$
 Birrer et al. (2020), TDCOSMO+SLACS: $67.4^{+4.1}_{-4.1}$, TDCOSMO: $74.5^{+5.5}_{-5.5}$
 Millon et al. (2020), TDCOSMO: 74.2 ± 1.6
 Baxter et al. (2020): 73.5 ± 5.3
 Qi et al. (2020): $73.6^{+1.8}_{-1.8}$
 Liao et al. (2020): $72.8^{+1.6}_{-1.6}$
 Liao et al. (2019): 72.2 ± 2.1
 Shajib et al. (2019), STRIDES: $74.2^{+2.0}_{-2.0}$
 Wong et al. (2019), HOLICOW 2019: $73.3^{+2.1}_{-2.1}$
 Birrer et al. (2018), HOLICOW 2018: $72.5^{+2.1}_{-2.1}$
 Bonvin et al. (2016), HOLICOW 2016: $71.9^{+2.3}_{-2.3}$

Optimistic average
 Di Valentino (2021): 72.94 ± 0.75
Ultra – conservative, no Cepheids, no lensing
 Di Valentino (2021): 72.7 ± 1.1

GW related
 Gayathri et al. (2020), GW190521+GW170817: $73.4^{+1.9}_{-1.9}$
 Mukherjee et al. (2020), GW170817+ZTF: $67.6^{+2.4}_{-2.4}$
 Mukherjee et al. (2019), GW170817+VLBI: $68.3^{+2.4}_{-2.4}$
 Abbott et al. (2017), GW170817: $70.0^{+1.9}_{-1.9}$



Di Valentino+ arXiv:2103.01183

Tip of the Red-Giant Branch in the Galaxy NGC 4258

THE ASTROPHYSICAL JOURNAL, 835:28 (17pp), 2017 January 20

JANG & LEE

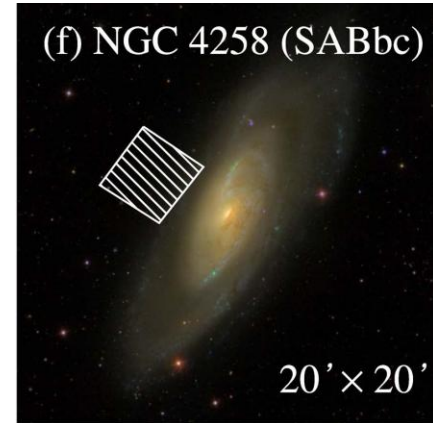
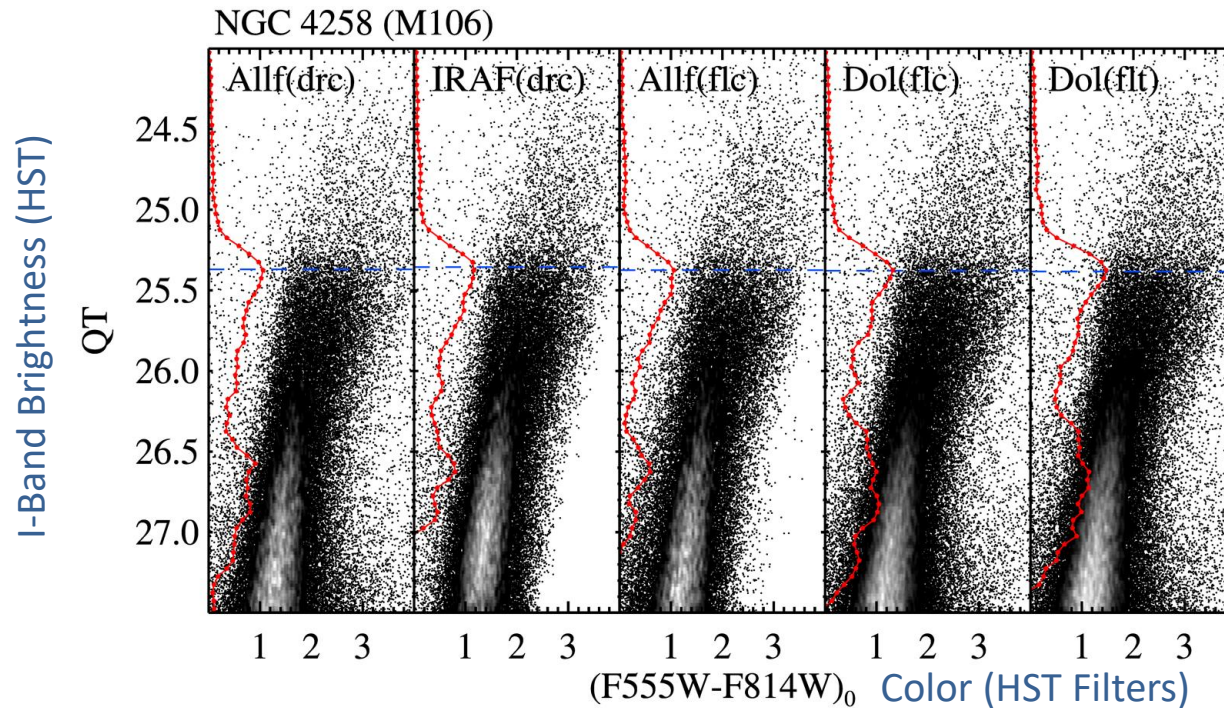


Figure 7. $QT - (F555W - F814W)_0$ CMDs of NGC 4258 from five different reduction methods : ALLFRAME on drc, IRAF/DAOPHOT on drc, ALLFRAME on flc, DOLPHOT on flc, and DOLPHOT on flt (from left to right). Edge detection responses are shown by the solid lines. Note that the estimated TRGB magnitudes (dashed lines) agree very well.

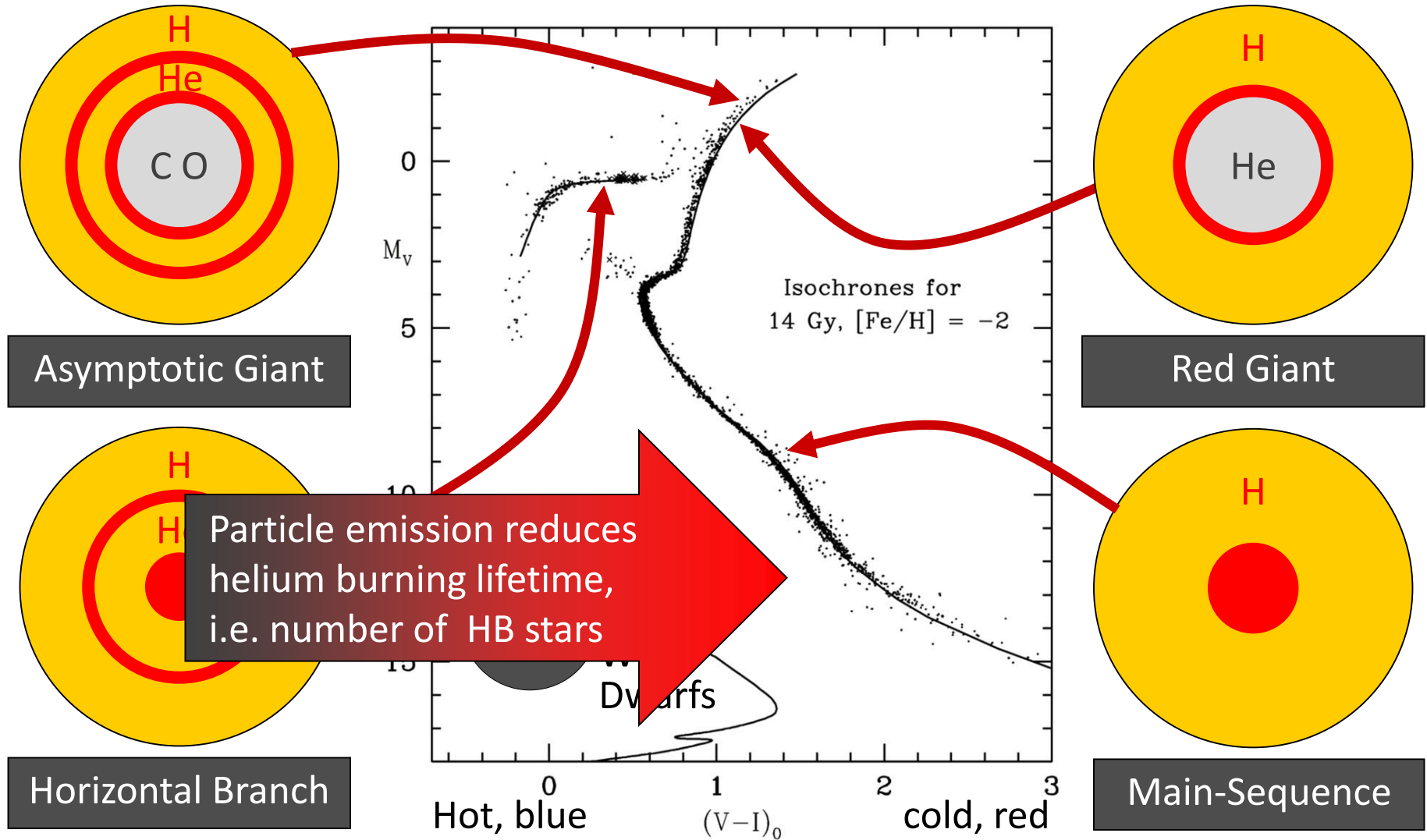
NGC 4258 hosts a water megamaser

→ **Quasi-geometric distance determination**

→ **Among the best absolute TRGB calibrations**

→ **One rung in cosmic distance ladder**

Color-Magnitude Diagram for Globular Clusters



Color-magnitude diagram synthesized from several low-metallicity globular clusters and compared with theoretical isochrones (W.Harris, 2000)

Helium Burning Lifetime: R-Method

Number ratio (“R”) of HB/RGB fixes He-burning lifetime
(if RGB not affected by new energy loss)

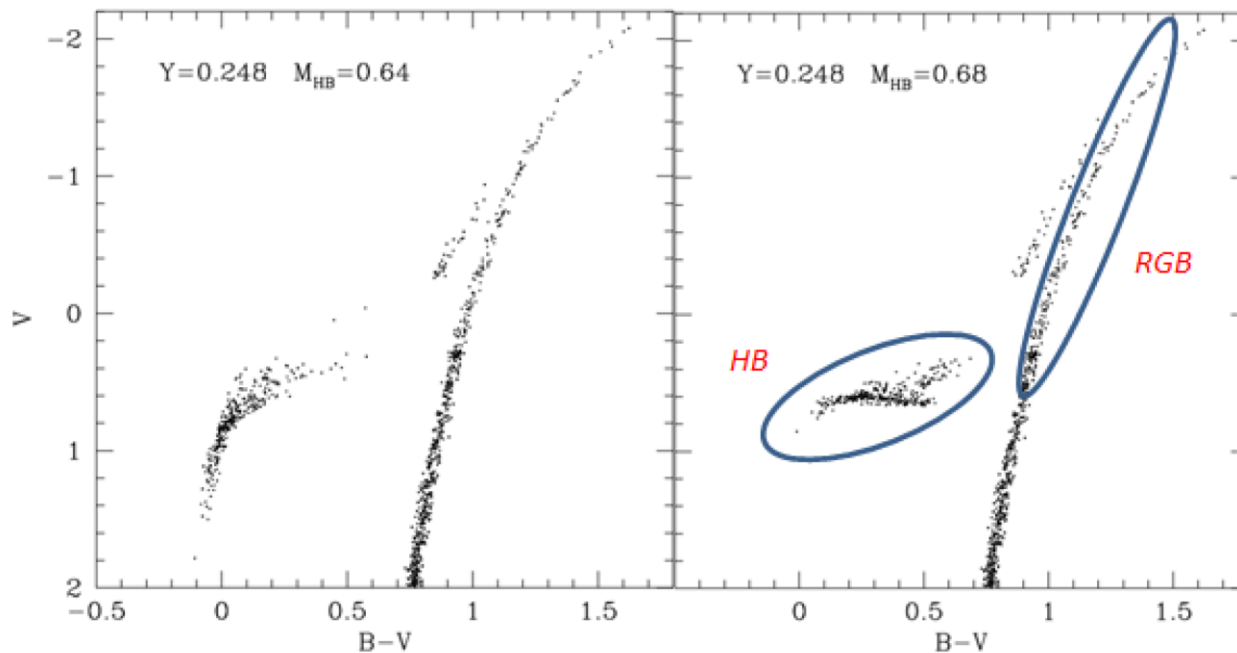
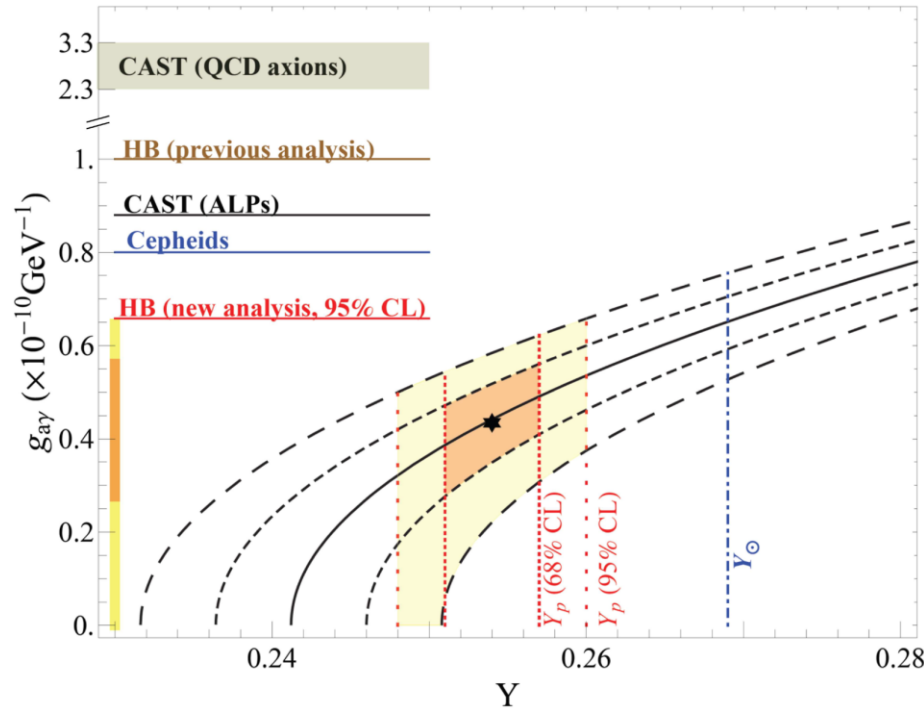


Figure 1: Example of synthetic CM diagrams. The diagram in the left panel has been obtained by assuming a stronger average mass loss rate during the RGB. As a result, the mean mass of HB stars (M_{HB}) is lower than that of the diagram in the right panel. The HB and the RGB portions used in the calculation of the R parameter are surrounded by ellipses.

Straniero, Ayala, Giannotti, Mirizzi & Domínguez,

[doi:10.3204/DESY-PROC-2015-02/straniero_oscar](https://doi.org/10.3204/DESY-PROC-2015-02/straniero_oscar)

ALP Limits from Globular Clusters



Helium abundance and energy loss rate from modern number counts HB/RGB in 39 globular clusters $R = 1.39 \pm 0.03$

$$R_{\text{th}} = 1.48 + 6.26(Y - 0.255) - 0.41g_{10}^2$$

$$g_{a\gamma} < 0.66 \times 10^{-10} \text{GeV}^{-1} \text{ (95\% CL)}$$

Same as CAST limit within 2 digits ☺

Small “cooling hint” almost certainly systematics (as usual in astrophysics)
eg nuclear reaction rates
Need more systematic exploration of systematics!

Parameter	error	Reference
$^{14}\text{N}(p, \gamma)^{15}\text{O}$	7%	[1]
$^4\text{He}(2\alpha, \gamma)^{12}\text{C}$	10%	[2]
$^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$	20%	[6]
R	1.39 ± 0.03	[4]
Y	0.255 ± 0.002	[5], [3]

Ayala, Dominguez, Giannotti, Mirizzi & Straniero, [arXiv:1406.6053](https://arxiv.org/abs/1406.6053)

[doi:10.3204/DESY-PROC-2015-02/straniero_oscar](https://doi.org/10.3204/DESY-PROC-2015-02/straniero_oscar)

Update including ALP masses: Lucente, Straniero, Carenza, Giannotti & Mirizzi, [arXiv:2203.01336](https://arxiv.org/abs/2203.01336)

HB vs. AGB Clump on Luminosity Function

Astrophysical Axion Bounds

Andrea Caputo and Georg Raffelt

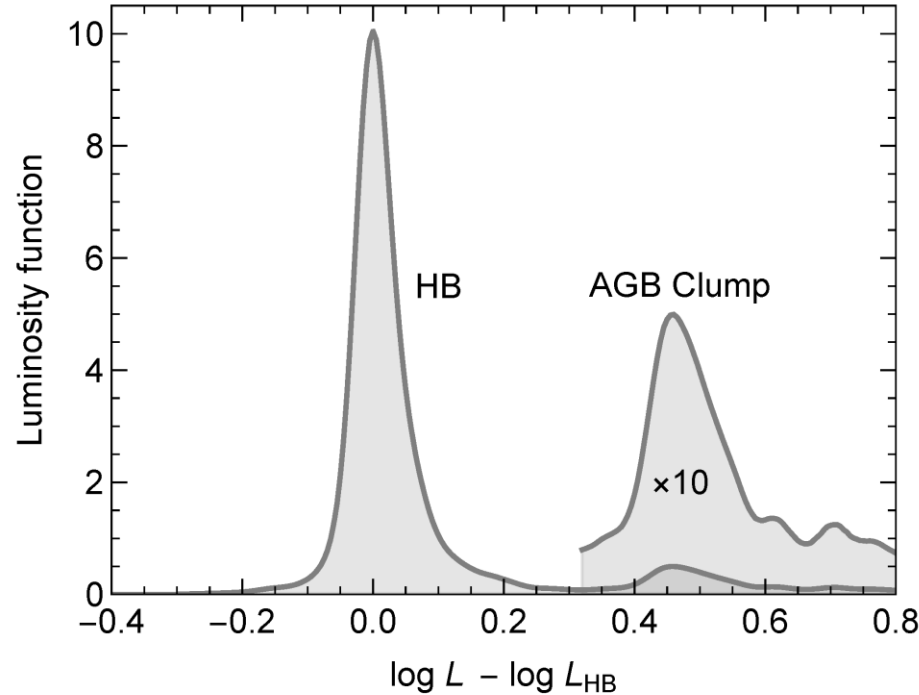


Figure 8: Empirical luminosity function, normalized to one, of the HB plus AGB stars from 14 GCs without a blue extension of the HB [212], using HST photometric data of Piotto et al. [213] and Sarajedini et al. [214]. We show a superposition of the two curves of Fig. 6 of [212], weighted with the number of stars (2414 for Sarajedini et al. and 4036 for Piotto et al.), although there is large overlap between the used clusters. Each one was aligned to its HB luminosity, defined as the maximum of the distribution. The AGB clump at $\log L - \log L_{\text{HB}} = 0.455$ sticks out as a narrow peak. The separation between HB and AGB is taken at the minimum between the peaks, and the AGB itself until $\log L - \log L_{\text{HB}} = 1$. A total of 725 AGB and 5725 HB stars went into the construction of this distribution, corresponding to $R_2 = 0.127$ for the clusters that went into this plot.

AGB/HB Counts in 48 Globular Clusters

NGC	[Fe/H]	L1	L2	Piotto et al. (2002)			Sarajedini et al. (2007)			Sandquist (2000)		
				n_{HB}	n_{AGB}	R_2	n_{HB}	n_{AGB}	R_2	n_{HB}	n_{AGB}	R_2
104	-0.72	0.078	0.068	358	53	0.148	591	82	0.139	368	38	0.103
362	-1.26	0.086	0.608	238	40	0.168	318	43	0.135	94	14	0.149
1261	-1.27	0.088	0.644	94	22	0.234	233	34	0.146	148	26	0.176
1851	-1.18	0.098	0.679	272	37	0.136	411	49	0.119	209	24	0.115
1904	-1.60	...	...	163	11	0.067	...	...	...	122	16	0.131
2419	-2.15	0.192	0.852	225	22	0.098	...	...	...	...	...	...
2808	-1.14	0.094	0.904	809	61	0.075	1200	104	0.087	247	22	0.089
4833	-1.85	0.287	0.538	94	10	0.106	...	...	...	...	...	...
5024	-2.10	0.158	0.602	224	18	0.080	360	44	0.122	302	39	0.129
5272	-1.50	0.150	0.613	...	...	...	323	40	0.124	562	65	0.116
5634	-1.88	...	...	130	15	0.115	...	...	...	...	...	...
5694	-1.98	...	...	222	26	0.117	...	...	...	56	14	0.250
5824	-1.91	...	...	463	63	0.136	...	...	...	...	...	...
5904	-1.29	0.150	0.681	162	21	0.130	280	52	0.186	555	94	0.169
5927	-0.49	0.043	0.062	201	12	0.060	...	...	...	134	20	0.149
6093	-1.75	0.464	0.447	162	31	0.191	341	51	0.150	170	39	0.229
6139	-1.65	...	...	282	35	0.124	...	...	...	114	24	0.211
6171	-1.02	0.100	0.513	...	...	...	56	10	0.179	117	29	0.248
6205	-1.53	0.527	0.441	192	20	0.104	390	48	0.123	90	12	0.133
6218	-1.47	0.561	0.299	...	...	...	82	11	0.134	91	12	0.132
6229	-1.18	...	...	278	34	0.122	...	...	...	92	19	0.207
6254	-1.26	0.588	0.260	...	...	...	157	18	0.115	69	13	0.188
6266	-1.18	...	...	446	40	0.090	...	...	...	114	18	0.158
6284	-1.26	...	...	127	16	0.126	...	...	...	...	...	...
6304	-0.45	0.062	0.060	99	8	0.081	...	...	...	...	...	...
6341	-2.31	0.261	0.542	...	...	...	245	33	0.135	140	20	0.143
6356	-0.40	...	...	362	25	0.069	...	...	...	...	...	...
6362	-0.59	0.122	0.621	38	6	0.158	...	...	...	...	...	...
6388	-0.55	0.057	0.836	1347	176	0.131	...	...	...	...	...	...
6402	-1.28	...	...	349	29	0.083	...	...	...	...	...	...
6441	-0.46	0.048	0.904	1380	154	0.112	...	...	...	...	...	...
6539	-0.63	...	...	114	15	0.132	...	...	...	...	...	...
6541	-1.81	0.563	0.347	...	...	...	248	41	0.165	...	...	...
6569	-0.76	...	...	166	30	0.181	...	...	...	...	...	...
6584	-1.50	0.102	0.558	55	8	0.145	...	...	...	...	...	...
6624	-0.44	0.077	0.085	121	9	0.074	188	20	0.106	126	30	0.238
6637	-0.64	0.078	0.065	135	25	0.185	244	43	0.176	127	21	0.165
6638	-0.95	...	...	101	28	0.277	...	...	...	...	...	...
6652	-0.81	0.073	0.080	61	5	0.082	83	9	0.108	75	20	0.267
6681	-1.62	0.558	0.334	100	9	0.090	...	...	...	82	8	0.098
6723	-1.10	0.127	0.704	102	11	0.108	194	22	0.113	101	15	0.149
6752	-1.54	0.378	0.578	...	...	...	173	20	0.116	225	13	0.058
6864	-1.29	...	...	363	69	0.190	...	...	...	55	12	0.218
6934	-1.47	0.097	0.678	149	18	0.121	99	17	0.172	...	...	...
6981	-1.42	0.142	0.570	61	7	0.115	188	36	0.191	45	10	0.222
7078	-2.37	0.174	0.713	376	48	0.128	537	57	0.106	153	23	0.150
7089	-1.65	0.150	0.790	167	18	0.108	702	100	0.142	...	...	...
7099	-2.27	0.462	0.261	89	6	0.067	...	...	...	202	11	0.054

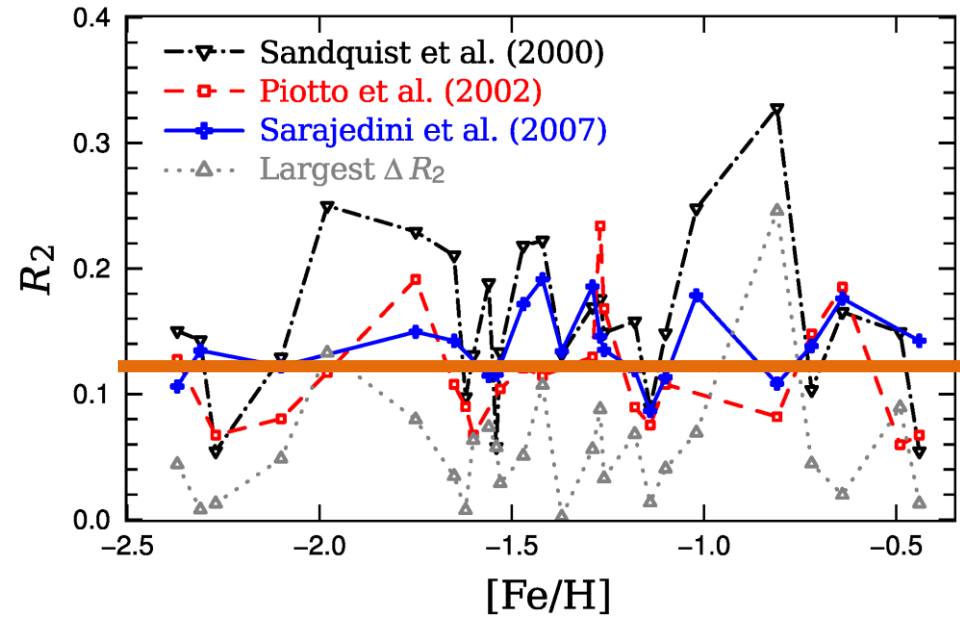


Figure 1. Comparison of R_2 for clusters shown in Table 1, limited to those with at least two different sources of photometry. The R_2 determined from the Sandquist (2000), Piotto et al. (2002), and Sarajedini et al. (2007) data are shown in black dash-dots, red dashes, and a blue solid line, respectively. The dotted grey line shows the maximum difference between R_2 determinations from different photometry.

$$R_2 = N_{\text{AGB}}/N_{\text{HB}} = 0.117 \pm 0.005$$

The treatment of mixing in core helium burning models

II. Constraints from cluster star counts

Constantino, Campbell, Lattanzio & van Duijneveldt,

[arXiv:1512.04845](https://arxiv.org/abs/1512.04845)

Predicting the Axion-Modified Ratios

M.J. Dolan, F.J. Hiskens & R.R. Volkas, [arXiv:2207.03102](https://arxiv.org/abs/2207.03102)

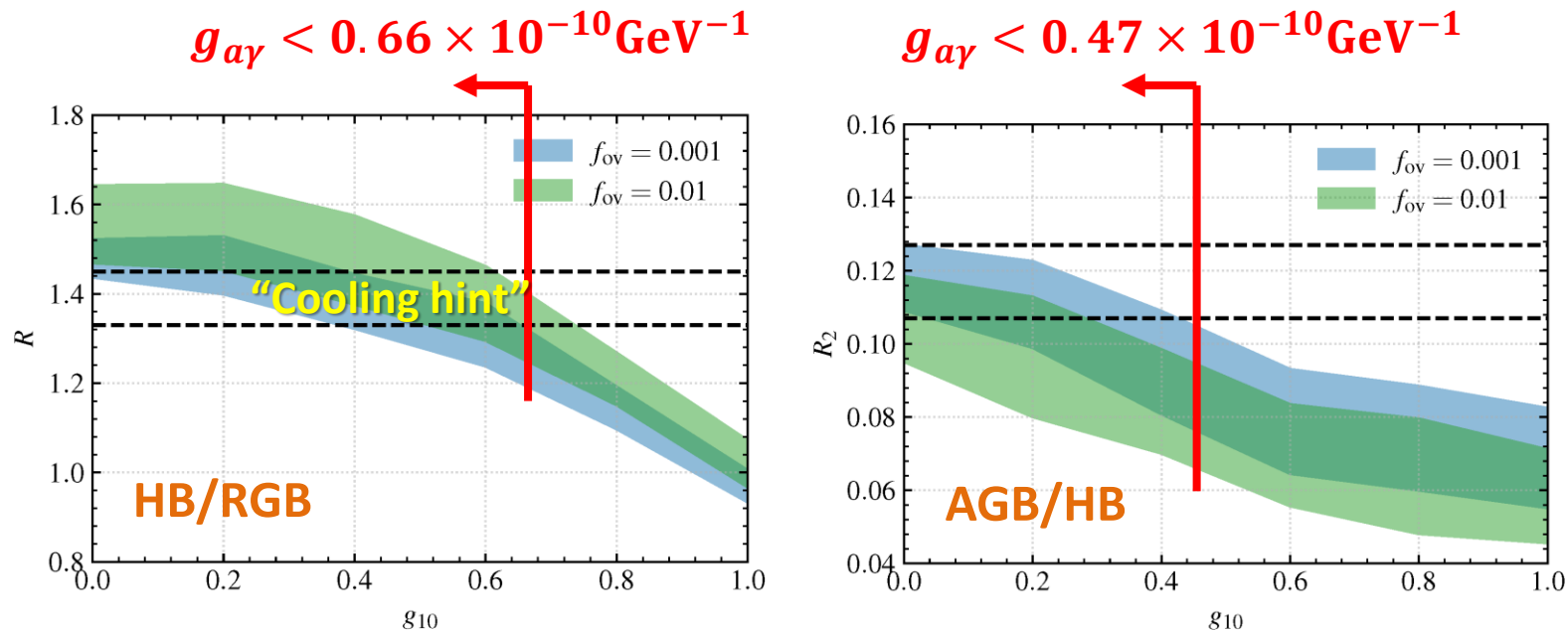
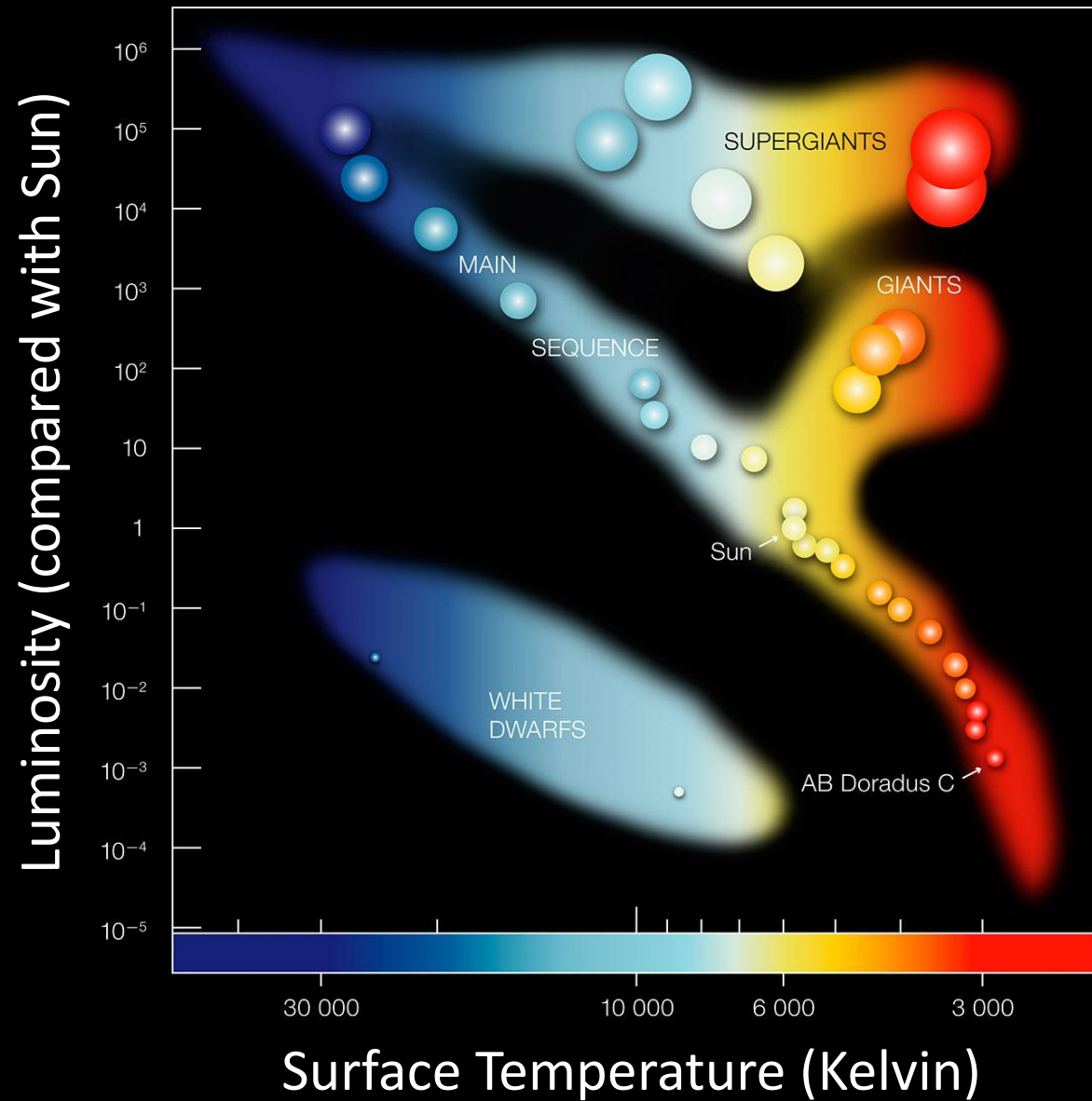


Figure 2. (Left panel): Predicted values of R as a function of g_{10} given standard convective core overshoot with $f_{\text{ov}} = 0.001$ (blue) and $f_{\text{ov}} = 0.01$ (green). The observed limit on R is indicated by the region between the dashed black lines (95% C.I.). (Right panel): The full range of R_2 values predicted as functions of g_{10} given standard overshoot with $f_{\text{ov}} = 0.001$ (blue) and $f_{\text{ov}} = 0.01$ (green). The observed limit is again shown by the dashed black lines.

Probably one should analyze GCs for all observables simultaneously using modern high-statistics (GAIA) data

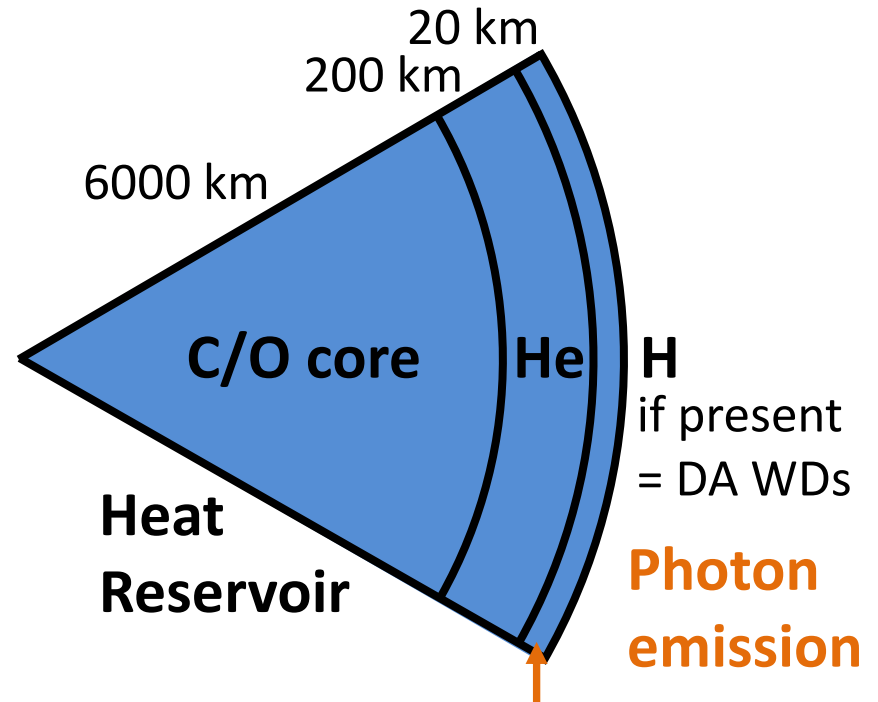
White Dwarfs



White Dwarfs

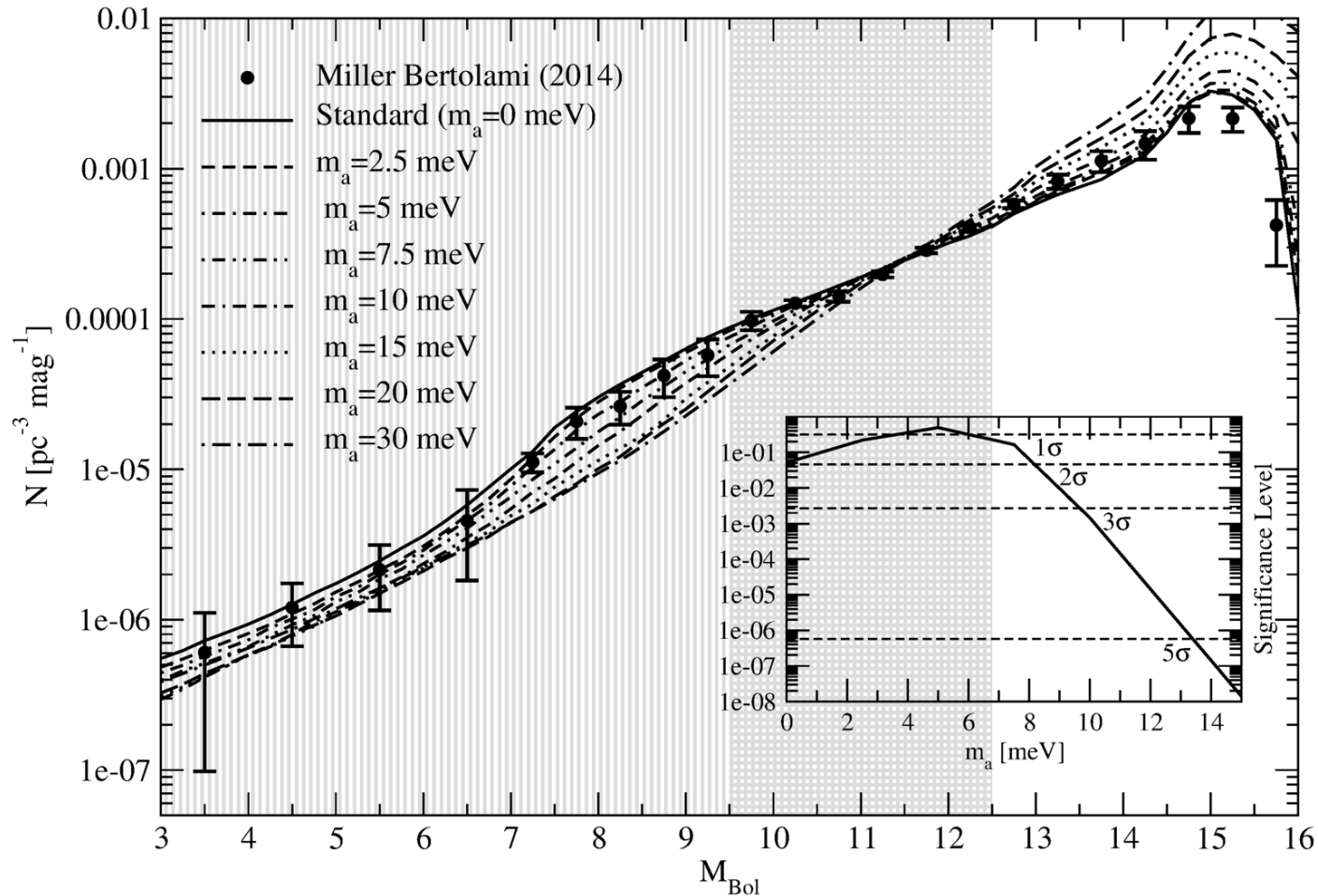


$R \simeq 6000 \text{ km}$ (Size of the Earth)
 $T_{\text{eff}} \simeq 10,000\text{--}30,000\text{K}$ (Sun 6000 K)
 $L \simeq 10^{-4}\text{--}10^{-1}L_{\odot}$
 $M \simeq 0.5\text{--}0.8M_{\odot}$
 $\rho \simeq 10^6\text{g/cm}^3$ (very degenerate)



Energy flux control
Cooling much slower for
DA type (with H layer)

Axion Bounds from WD Luminosity Function



Limits on axion-electron coupling and mass limit in DFSZ model:

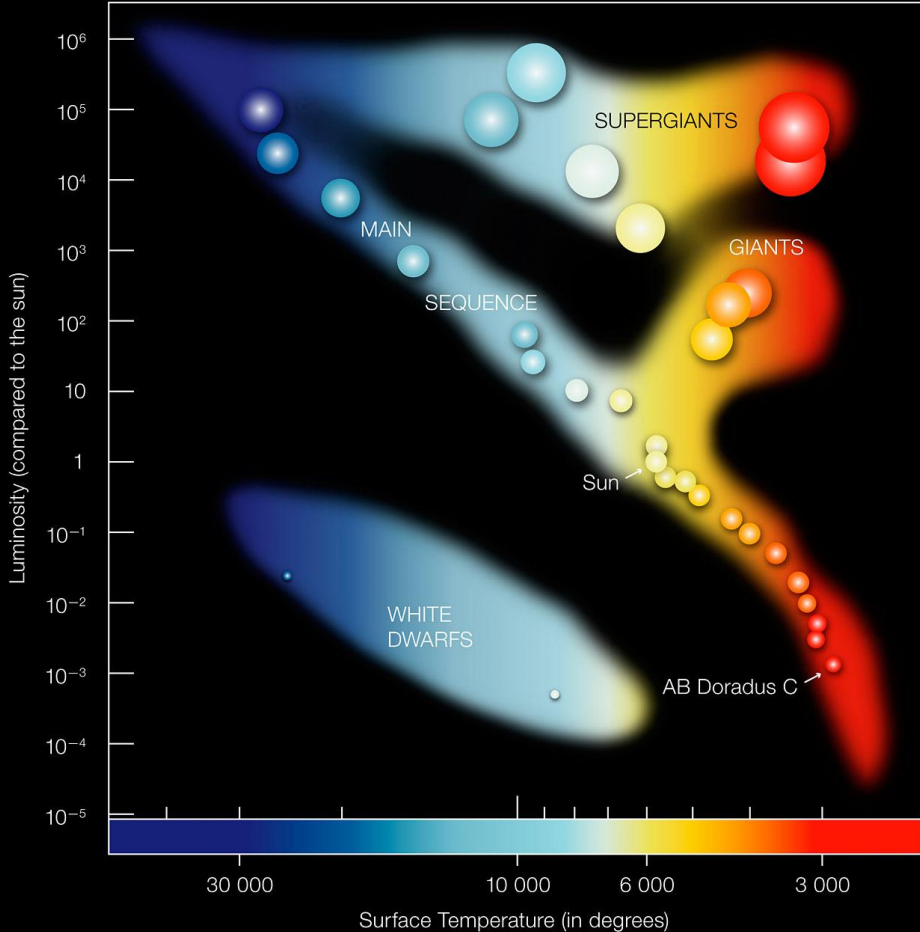
$$g_{ae} \lesssim 3 \times 10^{-13}$$

$$m_a \cos^2 \beta \lesssim 10 \text{ meV}$$

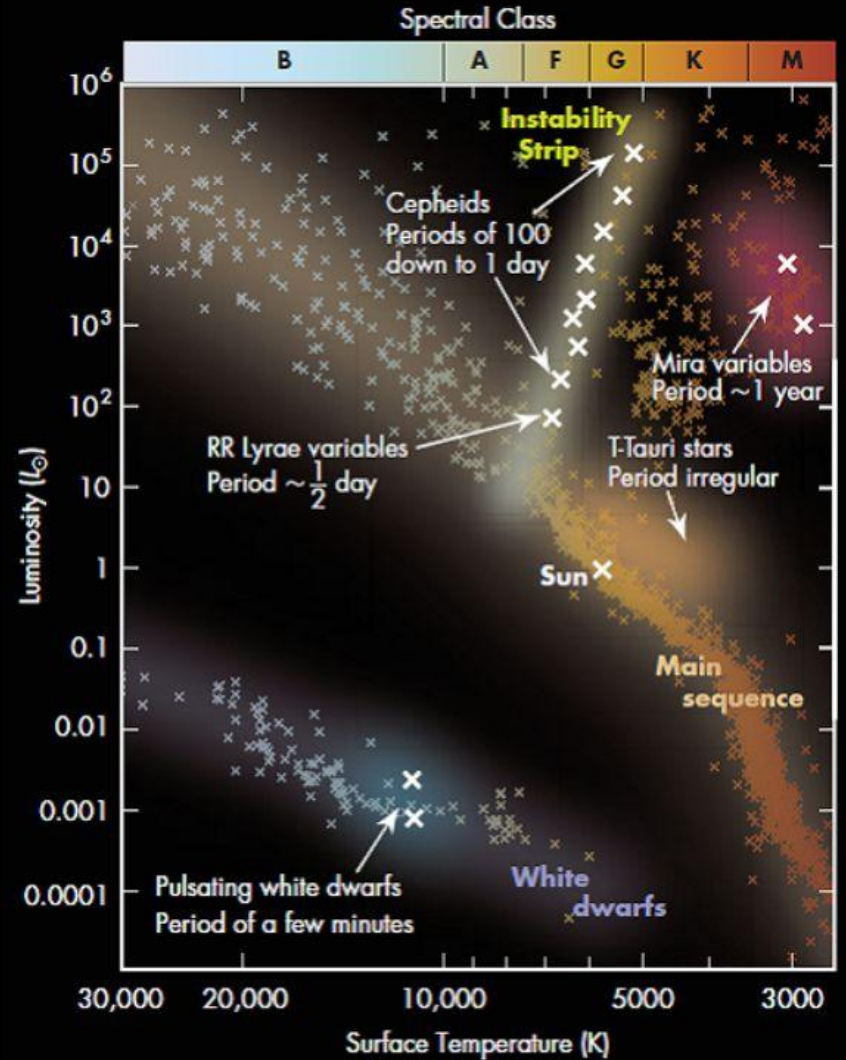
Miller Bertolami, Melendez, Althaus & Isern, [arXiv:1406.7712](https://arxiv.org/abs/1406.7712), [1410.1677](https://arxiv.org/abs/1410.1677)

For extensions and review see: Isern, [arXiv:2002.08069](https://arxiv.org/abs/2002.08069)

Pulsating Stars

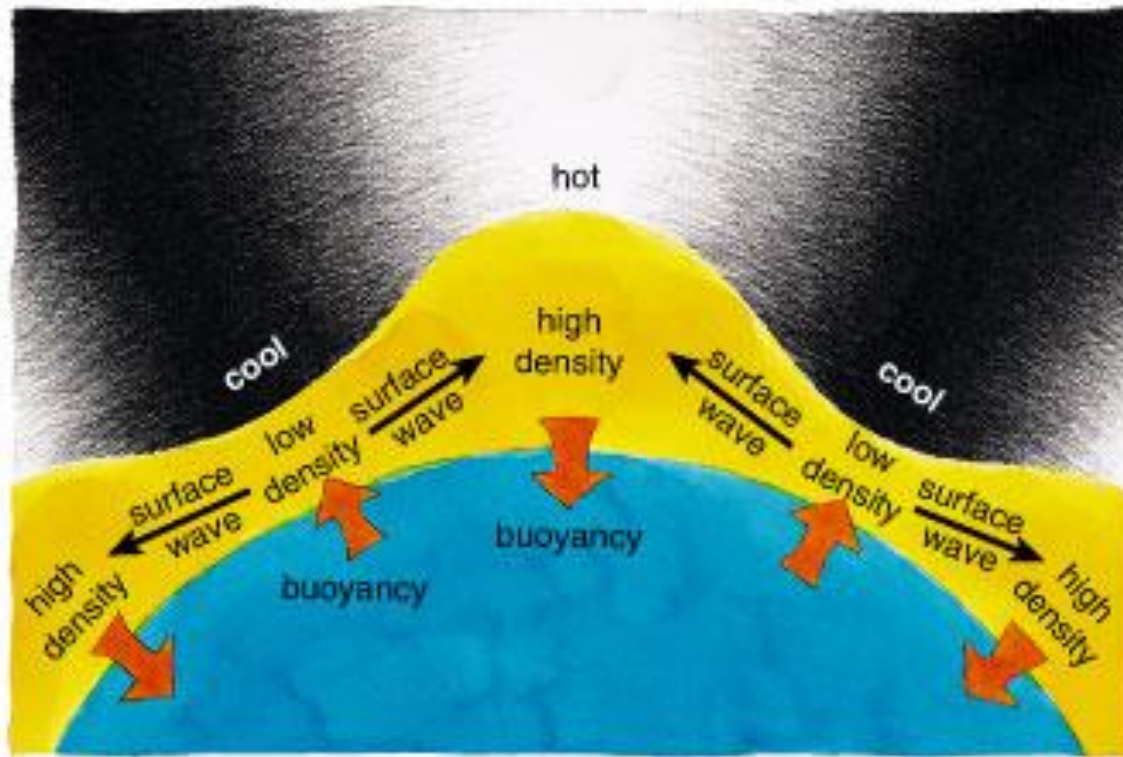


<https://www.eso.org/public/images/eso0728c/>



<https://scienceatyourdoorstep.com/2021/01/04/what-are-variable-stars/>

Non-Radial g-Modes



From a talk by J. Isern

$$\frac{d \log \Pi}{dt} \propto - \frac{d \log T}{dt}$$

- Long period waves (100 – 1000 s)
- Gravity is the restoring force

- Period decreases as the star cools
- Characteristic rate 10^{-15} s/s
- Measures cooling speed of a single star

Pulsating White Dwarf G117–B15A

Kepler+ ApJ 254 (1982) 676

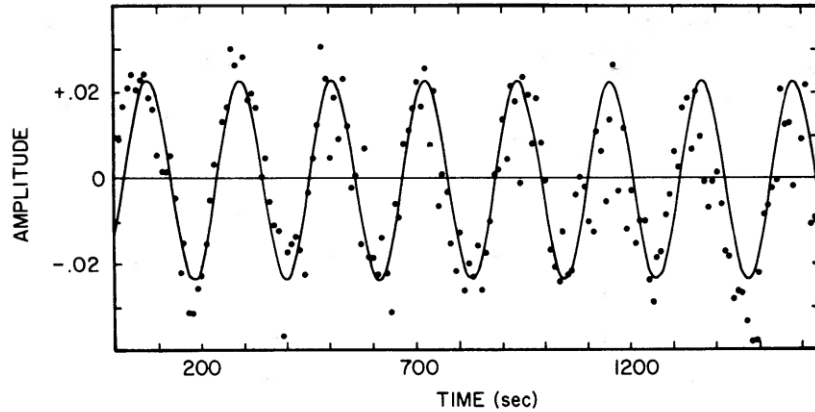


FIG. 1.—A portion of the light curve of G117–B15A in unfiltered light during run 2075. The light curve has been normalized so that the time-averaged brightness of G117–B15A is equal to 1.00, and then 1.00 has been subtracted from the light curve. The solid line is a sine curve with a period of 215.19 s and a semi-amplitude of 0.022 mag.

$$D = 57.5 \pm 0.1 \text{ pc}$$

$$T = 12,400 \text{ K}$$

$$M = 0.69 M_{\odot}$$

$$\text{Period } 215.2 \text{ s}$$

Kepler+ ApJ 906 (2021) 7

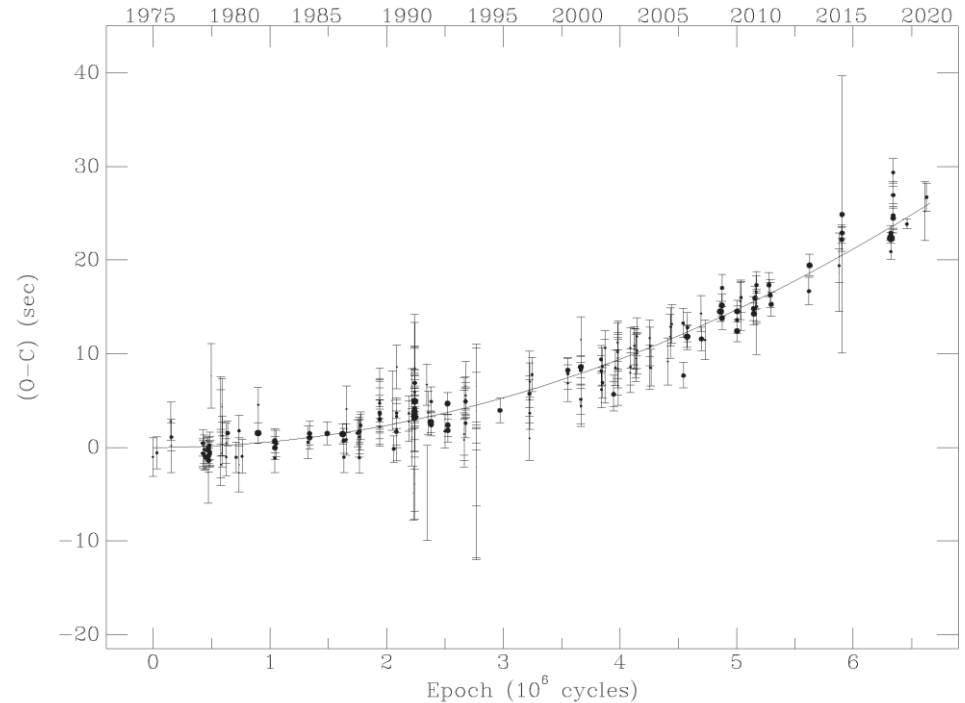


Figure 1. ($O - C$): observed minus calculated times of maxima for the 215 s pulsation of G 117-B15A. The size of each point is proportional to its weight, i.e., inversely proportional to the uncertainty in the time of maxima squared. We show $\pm 1\sigma$ error bars for each point, and the line shows our best-fit parabola to the data. The fact that the line does not overlap these error bars is a demonstration that they are underestimated. Note that as the period of pulsation is 215.1973882 s, the observed total change in phase is only 50 deg.

“Most stable optical clock”, slipped by 26 s (of 215.2 s period) in 45 years

$$\dot{P}/P = (5.12 \pm 0.82) \times 10^{-15} \text{ s/s}$$

G117–B15A Period Decrease: Hint for Axion Cooling?

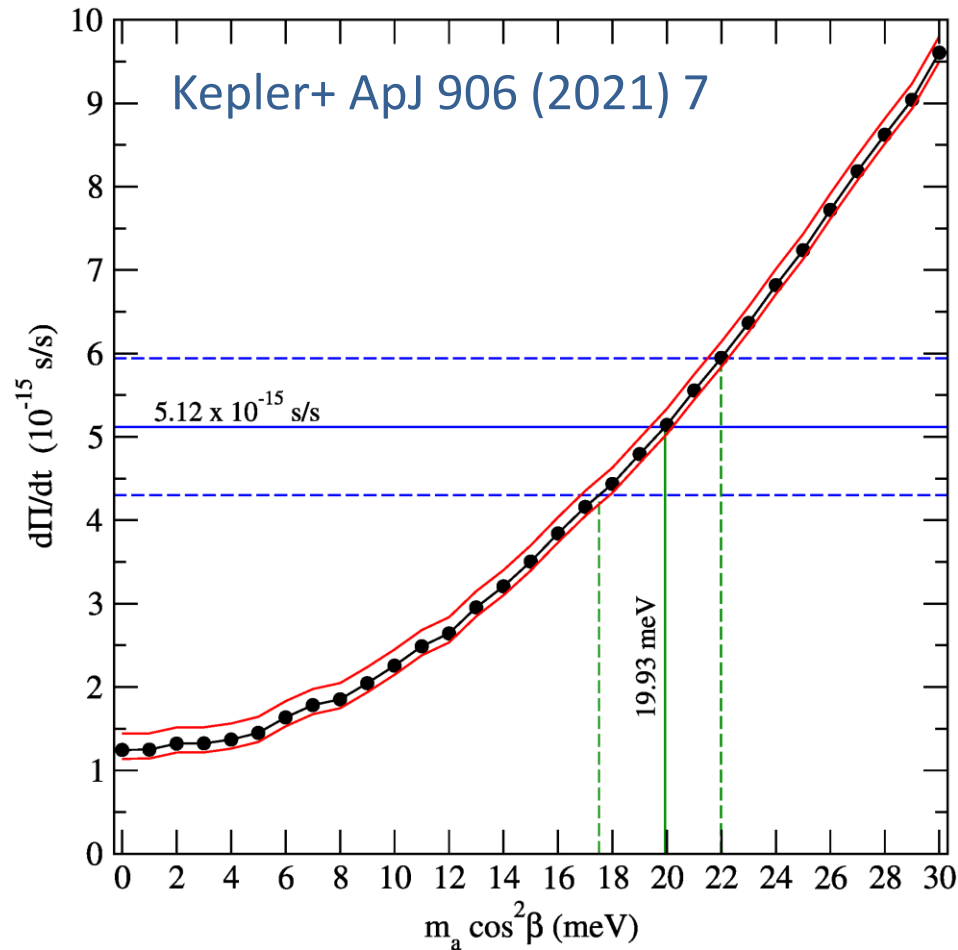
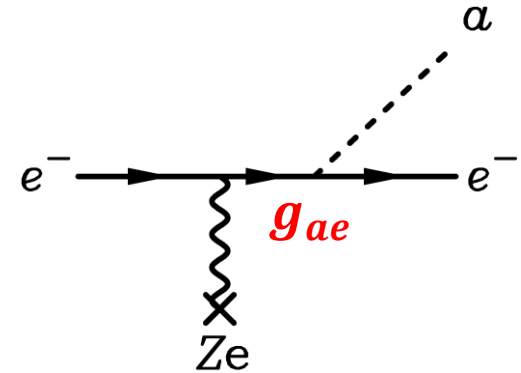


Figure 2. The rate of period change for the mode with $\ell = 1$ and $k = 2$, corresponding to a period of ~ 215 s in terms of the axion mass (black circles). Dashed lines represent the uncertainties in the value in the observed $\dot{P}$ and the axion mass, while the red curves represent the internal uncertainties in $\dot{P}$ due to modeling.

$$\dot{P}/P = (5.12 \pm 0.82) \times 10^{-15} \text{ s/s}$$

Emission of axions & friends
with direct electron coupling



Bremsstrahlung emission by
degenerate electrons

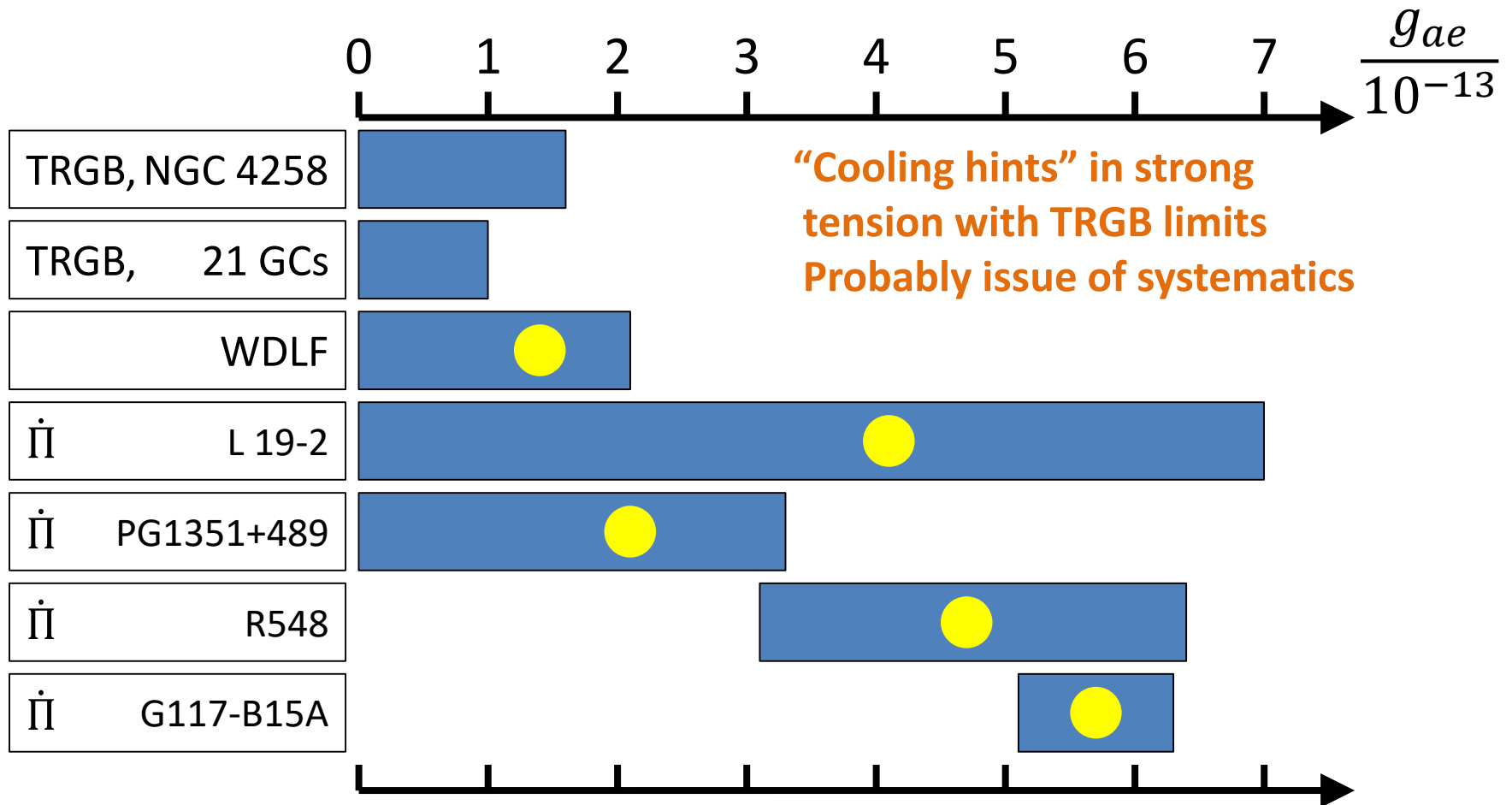
Case of DFSZ Axion

$$g_{ae} = 0.28 \times 10^{-13} \frac{m_a \cos^2 \beta}{\text{meV}}$$

Nominal cooling signal

$$g_{ae} = (5.7 \pm 0.6) \times 10^{-13}$$

White-Dwarf Bounds on Axion-Electron Coupling



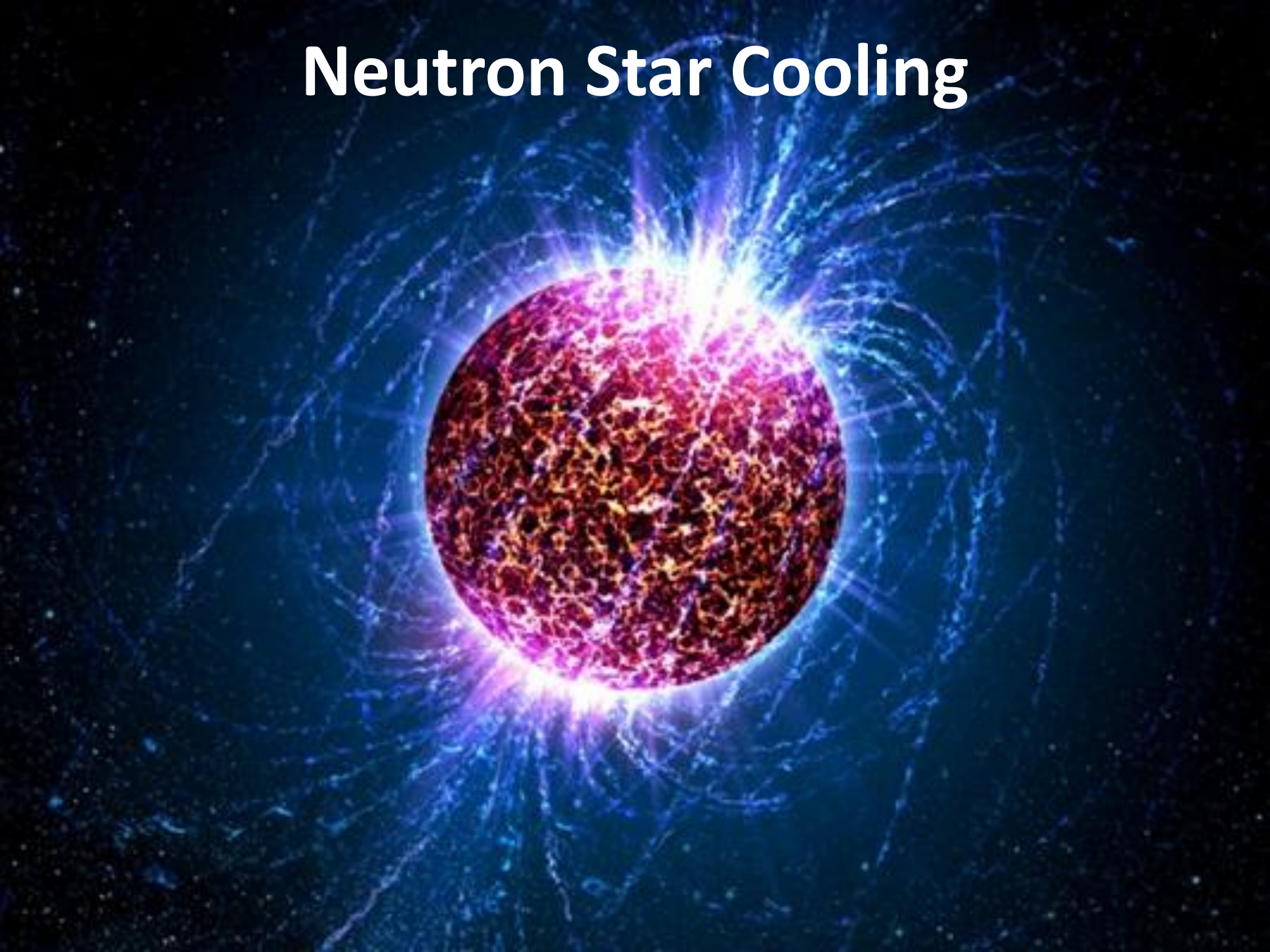
White Dwarfs as Physics Laboratories: Lights and Shadows, [arXiv:2202.02052](https://arxiv.org/abs/2202.02052)

J. Isern, S. Torres & A. Rebassa-Mansergas

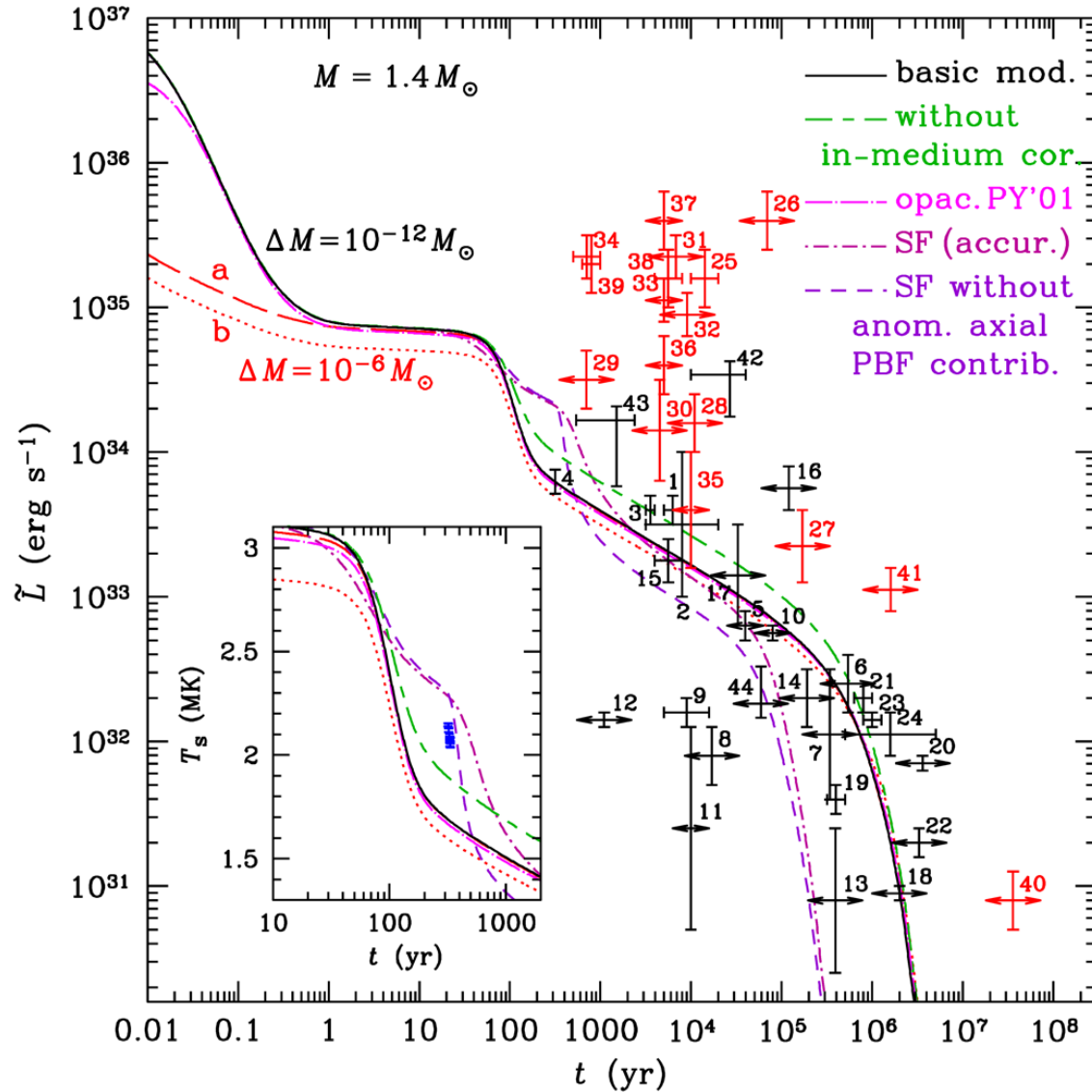
Stellar Evolution Confronts Axion Models, [arXiv:2109.10368](https://arxiv.org/abs/2109.10368)

L. Di Luzio, M. Fedele, M. Giannotti, F. Mescia & E. Nardi

Neutron Star Cooling



Neutron Star Cooling



Potekhin & Chabrier: Magnetic neutron star cooling and microphysics [1711.07662]

Cooling Simulations of Five Neutron Stars

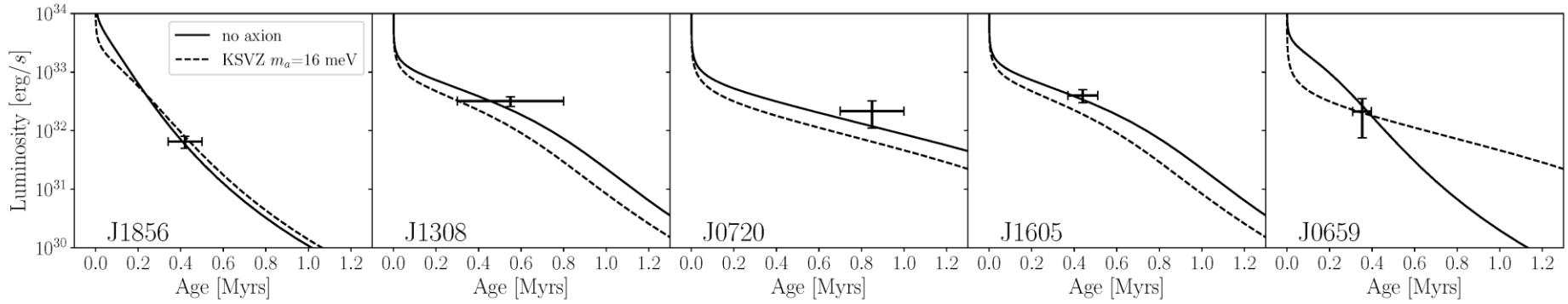
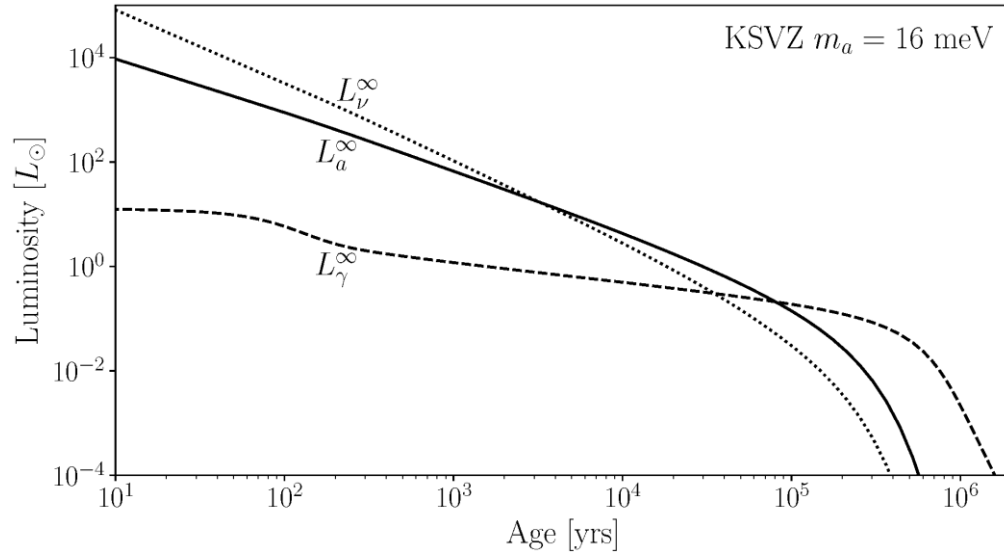


Figure 1. The luminosity and age data for each of the NSs considered in this work (see Tab. I). We show the best-fit cooling curves computed in this work for each of these NSs under the null hypothesis and with the axion mass fixed to $m_a = 16 \text{ meV}$, which is our 95% upper limit on the QCD axion mass in the context of the KSVZ model.

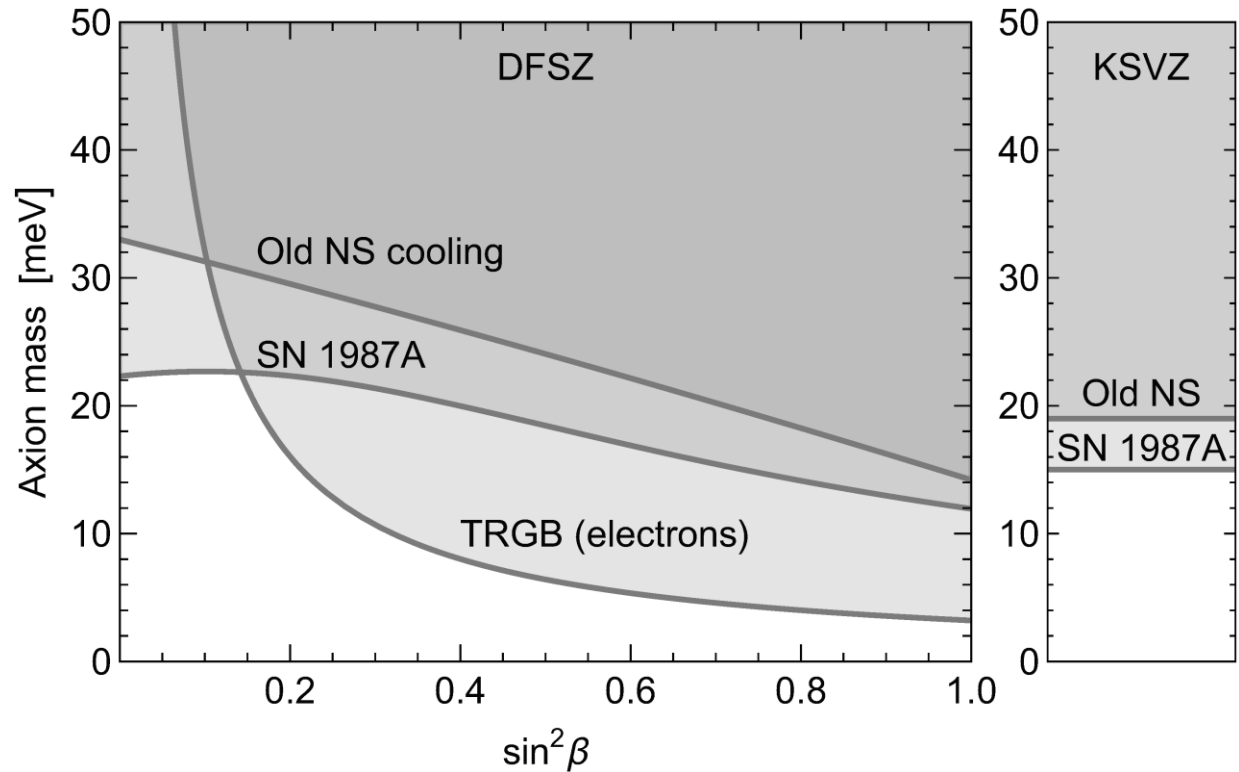


Cooling of J1605 with KSVZ axions,
BSk22 EOS, SBF-0-0 superfluidity
model, $M_{\text{NS}} = 1.0 M_\odot$

Upper Limit on the QCD Axion Mass from Isolated Neutron Star Cooling
Buschmann, Dessert, Foster, Long & Safdi, [2111.09892](#)

Neutron-Star Cooling Bounds

Caputo & Raffelt, arXiv:2401.13728



DFSZ Axions

$$\mathcal{L}_{af} = C_f \bar{\Psi}_f \gamma^\mu \gamma_5 \Psi_f \frac{\partial_\mu a}{2f_a}$$

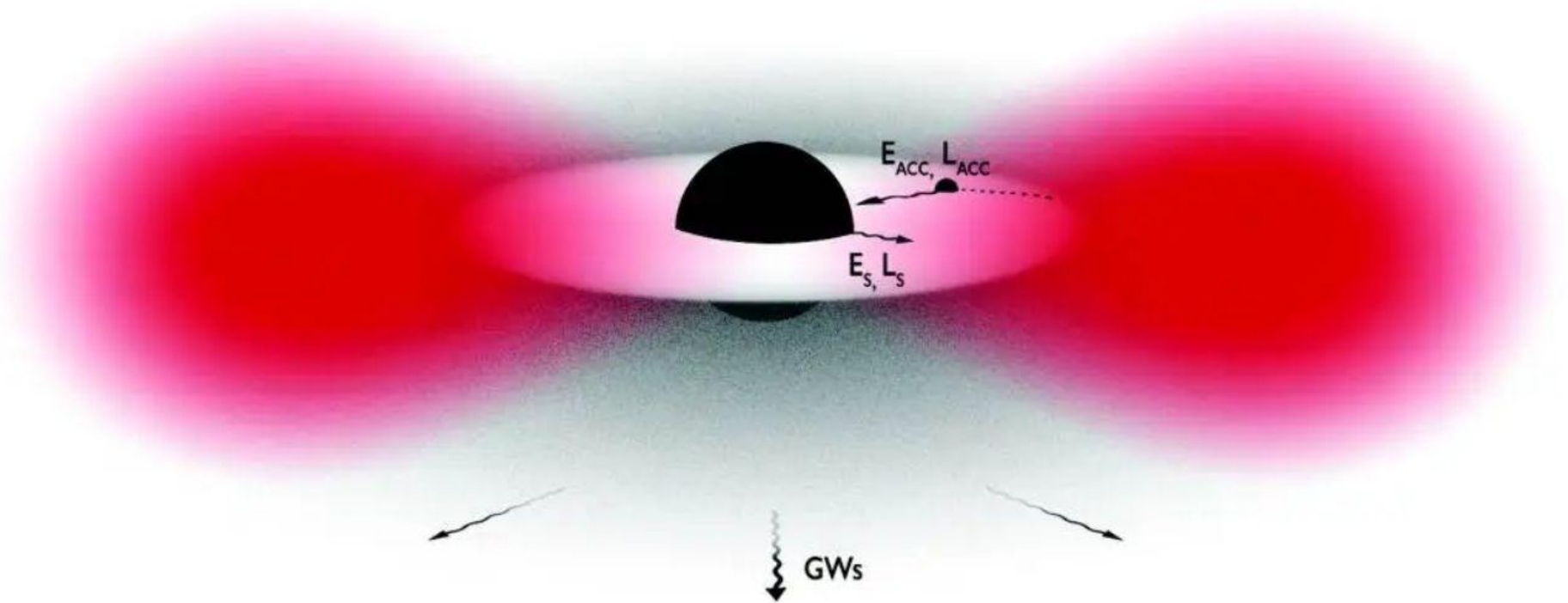
$$C_n = -0.160 \pm 0.025 + 0.414 \cos^2 \beta$$

$$C_p = -0.182 \pm 0.025 - 0.435 \cos^2 \beta$$

$$C_e = \frac{1}{3} \cos^2 \beta$$

**Upper Limit on the QCD Axion Mass
from Isolated Neutron Star Cooling**
Buschmann, Dessert, Foster, Long & Safdi,
arXiv:2111.09892

Superradiance

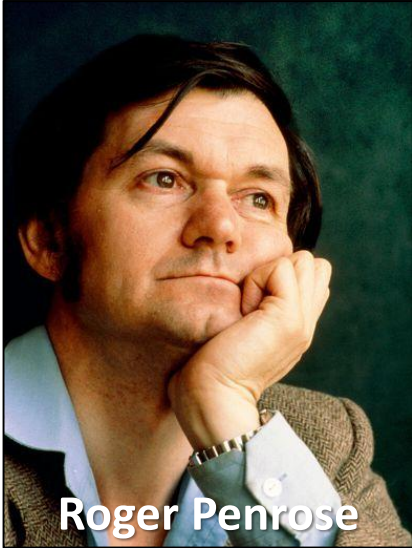


© a.s./grit

Superradiance: New Frontiers in Black Hole Physics (2020 edition)

R. Brito, V. Cardoso & P. Pani, [1501.06570v8](#) (8 Jan 2021)

Rotational Superradiance



Roger Penrose

Gravitational Collapse: The Role of General Relativity

Riv. Nuovo Cim., Num. Spez. 1 (1969) 257

Reprinted in [Gen. Rel. Grav. 34 \(2002\) 1141](#)



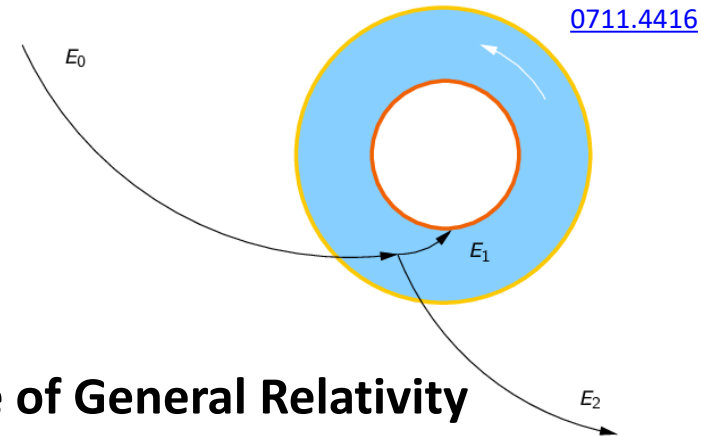
Yakov B. Zeldovich

Generation of Waves by a Rotating Body

[JETP Lett. 14 \(1971\) 180](#)

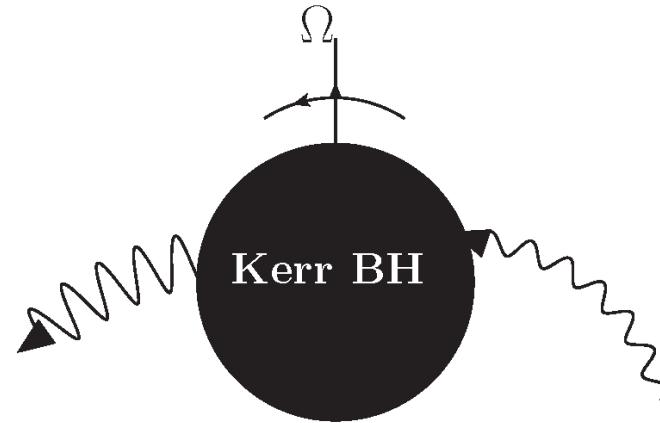
Amplification of Cylindrical Electromagnetic Waves Reflected from a Rotating Body

[Zh. Eksp. Teor. Fiz. 62 \(1972\) 2076](#)



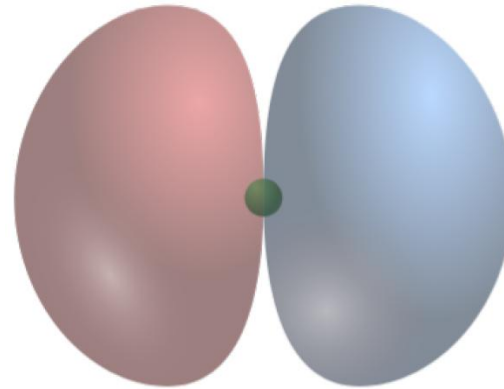
Superradiance

Extraction of rotational energy from spinning object by low-frequency modes $\omega < \Omega$ of an external bosonic field



$$m\Omega > \omega$$

- Bosons with mass get gravitationally bound
- Superradiant run-away mode
 $\phi = Y_{lm}(\theta, \phi)\psi_{lmn}(r)e^{\mathbf{r}t}$
- “Bosonic atom”
- Transitions $\rightarrow$ Gravitational waves



Superradiance: New Frontiers in Black Hole Physics (2020 edition)

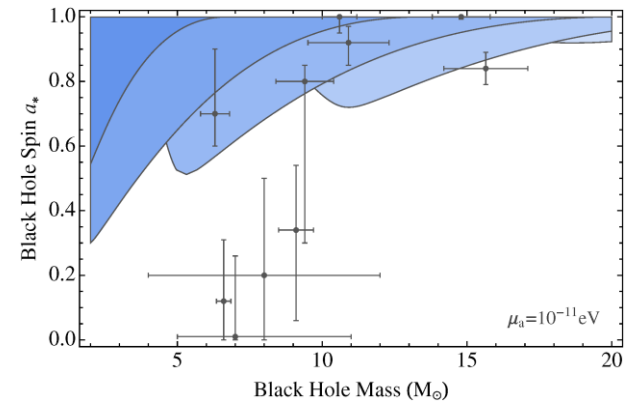
R. Brito, V. Cardoso & P. Pani, [1501.06570v8](#) (8 Jan 2021)

Signatures

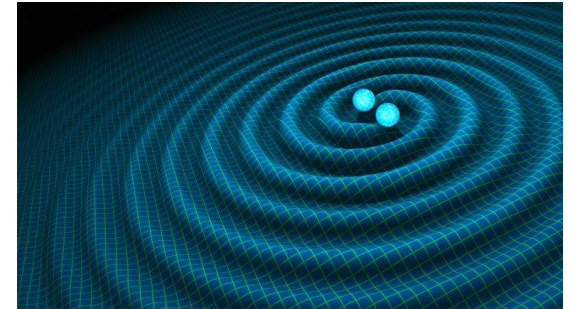
- **Constraints on light particles from BH spin**

Exploring the string axiverse with precision black hole physics
Arvanitaki & Dubovsky, [1004.3558](#)

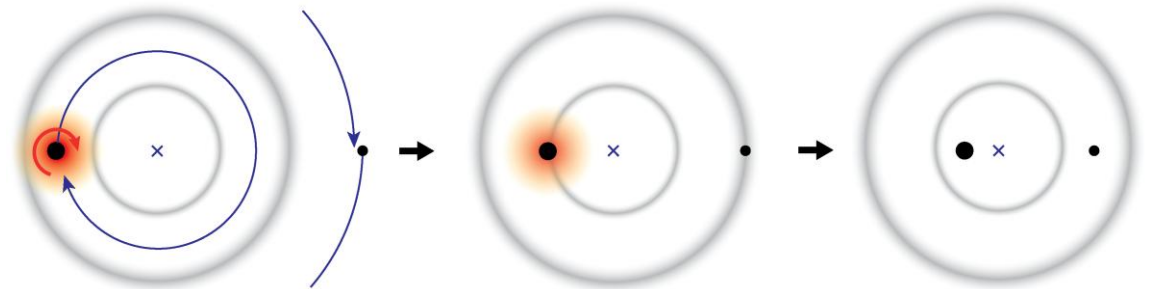
Discovering the QCD axion with black holes and gravitational waves, Arvanitaki, Baryakhtar & Huang, [1411.2263](#)



- **Gravitational waves from “atomic transitions”**

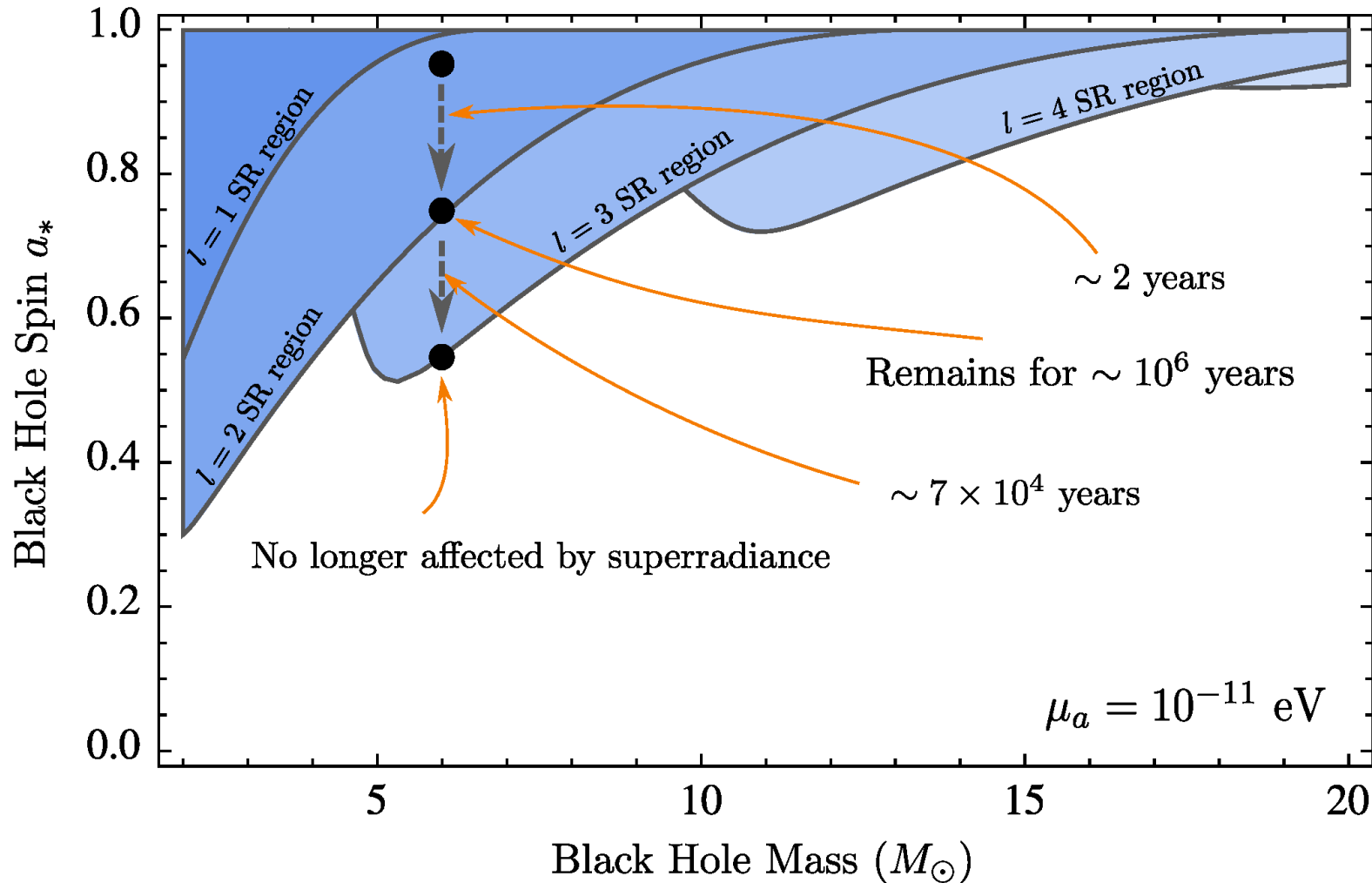


- **Effects on binaries**



Probing Ultralight Bosons with Binary Black Holes
Baumann, Chia & Porto, [1804.03208](#)

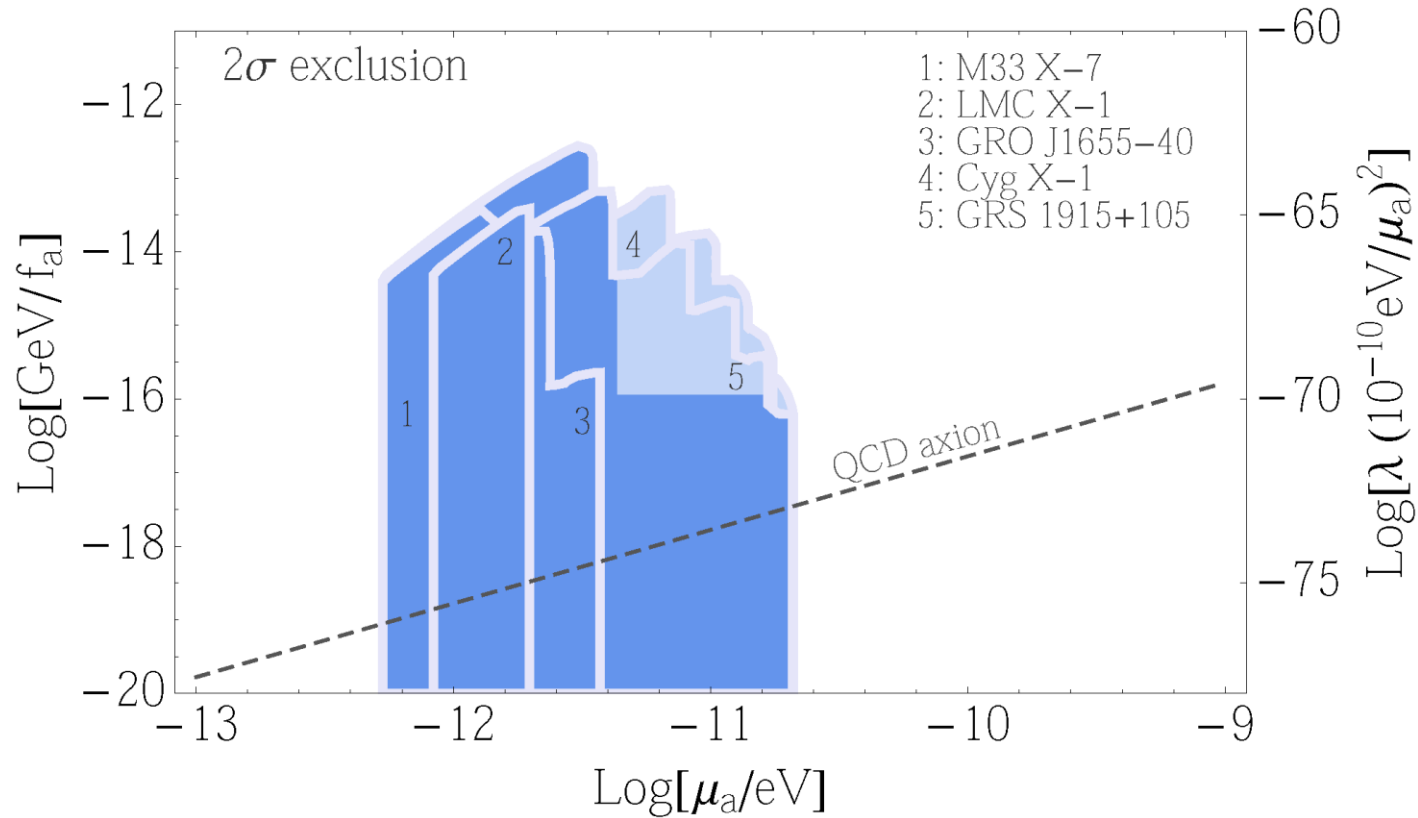
Impact on Black Hole Spins



Discovering the QCD axion with black holes and gravitational waves

Arvanitaki, Baryakhtar & Huang, [1411.2263](#)

Constraints from Black Hole Spins

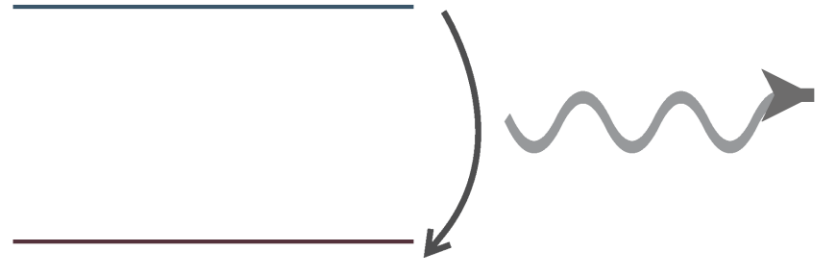


#	Object	Mass ($M_\odot$)	Spin	Age (yrs)	Period (days)	$M_{\text{comp. star}}$ ($M_\odot$)	$\dot{M}/\dot{M}_E$
1	M33 X-7	15.65 ± 1.45	$0.84^{+0.10}_{-0.10}$ [51]	3×10^6 [52]	3.4530 [53]	$\gtrsim 20$ [53]	$\gtrsim 0.1$ [53]
2	LMC X-1	10.91 ± 1.4	$0.92^{+0.06}_{-0.18}$ [54]	5×10^6 [52]	3.9092 [55]	31.79 ± 3.48 [55]	0.16 [55]
3	GRO J1655-40	6.3 ± 0.5	$0.72^{+0.16}_{-0.24}$ [51]	3.4×10^8 [56]	2.622 [56]	2.3 - 4 [56]	$\lesssim 0.25$ [57]
4	Cyg X-1	14.8 ± 1.0	> 0.99 [58]	4.8×10^6 [59]	5.599829 [52]	17.8 [52]	0.02 [52]
5	GRS1915+105	10.1 ± 0.6	> 0.95 [51, 60]	4×10^9 [61]	33.85 [62]	0.47 ± 0.27 [62]	$\gtrsim 1$ [62].

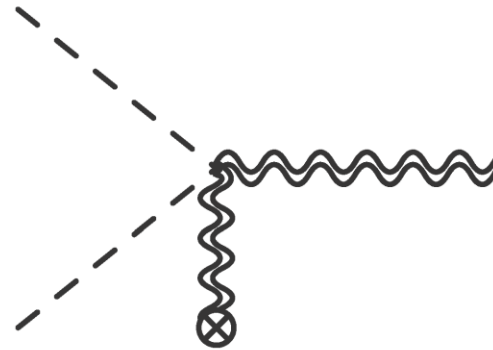
Arvanitaki, Baryakhtar & Huang, [1411.2263](#)

Gravitational Wave Signals

- Transitions between levels



- Annihilations to gravitons



Arvanitaki, Baryakhtar, Dimopoulos, Dubovsky & Lasenby, arXiv:1604.03958

Direct Constraints on the Ultralight Boson Mass from Searches of Continuous Gravitational Waves

C. Palomba¹, S. D'Antonio², P. Astone¹, S. Frasca^{3,1}, G. Intini^{3,1}, I. La Rosa⁴, P. Leaci^{3,1}, S. Mastrogiovanni⁵, A. L. Miller^{3,1,6}, F. Muciaccia³, O. J. Piccinni^{3,1}, L. Rei⁷, and F. Simula¹

Superradiance limits from LIGO O2 all-sky search for periodic GWs

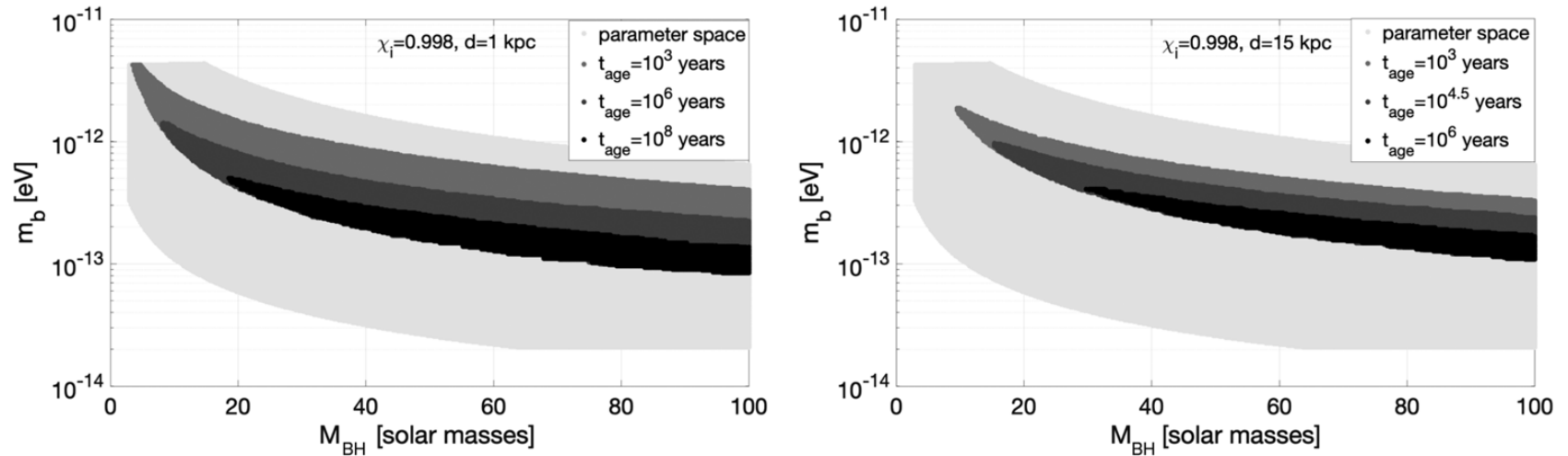


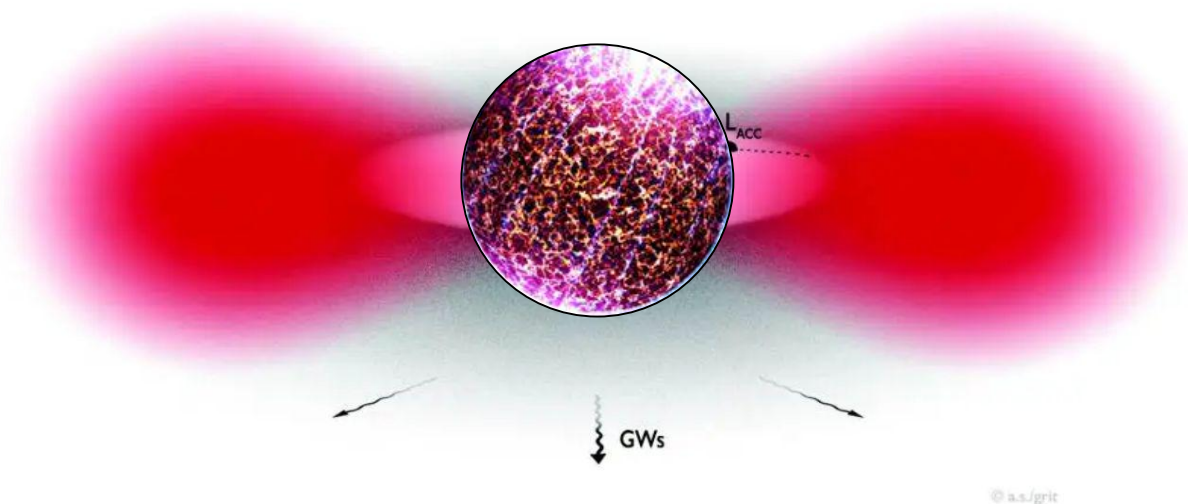
FIG. 2. 95% C.L. exclusion regions in the plane $m_b - M_{\text{BH}}$ assuming a maximum distance $d = 1$ kpc (left plot) and $d = 15$ kpc (right plot), a black hole initial adimensional spin $\chi_i = 0.998$, and three possible values for t_{age} : 10^3 , 10^6 , 10^8 yr (left plot) and 10^3 , $10^{4.5}$, 10^6 yr (right plot). The larger light gray area is the accessible parameter space. As expected, the extension of the excluded region decreases for increasing t_{age} (corresponding to darker color).

See also:

Search for ultralight bosons in Cygnus X-1 with Advanced LIGO, arXiv:1909.11267

Superradiance in Neutron Stars

- Crucial issue is absorption of bosons within neutron star
- Not enough absorption for axions in nuclear matter?



Superradiance in rotating stars and pulsar-timing constraints on dark photons

V.Cardoso, P.Pani & T.-T.Yu, [1704.06151](#)

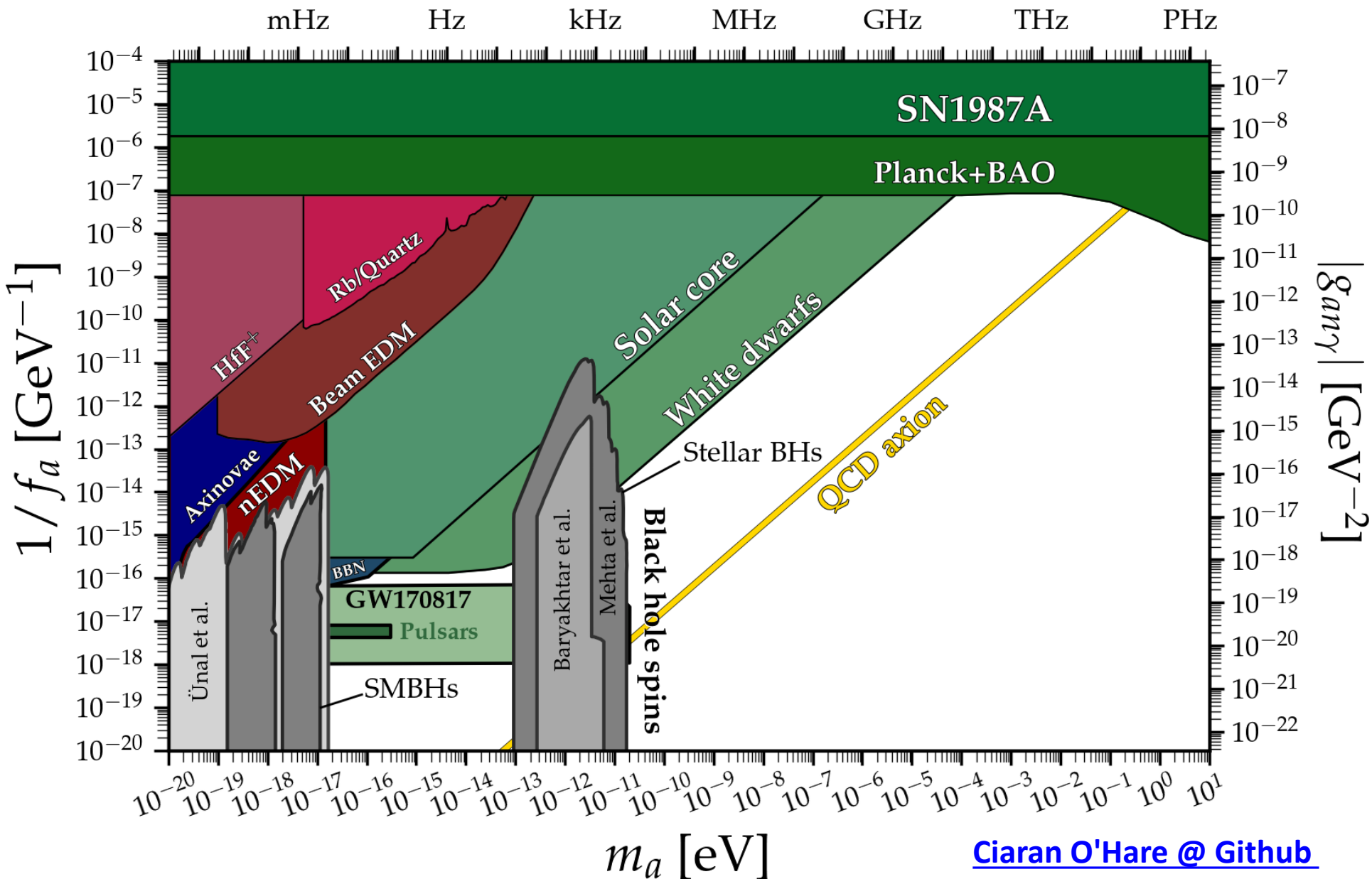
Axion superradiance in rotating neutron stars

F.V.Day & J.I.McDonald, [1904.08341](#)

Superradiance in stars: non-equilibrium approach to damping of fields in stellar media

F.Chadha-Day, B.Garbrecht & J.I.McDonald, [2207.07662](#)

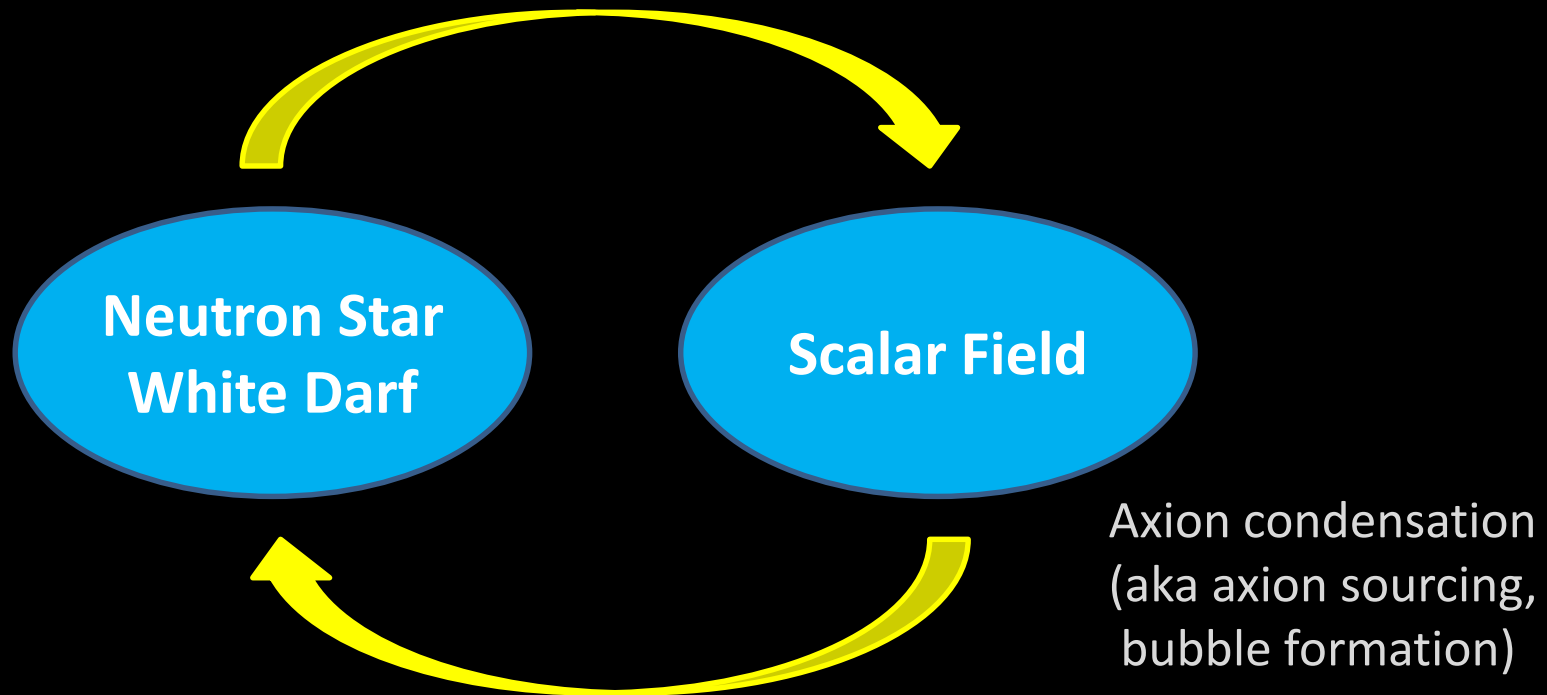
Peccei-Quinn Scale vs. Axion Mass



[Ciaran O'Hare @ Github](#)

Axions and Stellar Structure

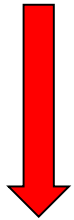
Coupled systems are coupled:
Stars destabilize axions, axions destabilize stars



Axion Potential in Vacuum

Non-perturbative effects
generate Λ_{QCD}

UV $\frac{g_s^2}{32\pi^2} \frac{\phi}{f_a} G\tilde{G}$

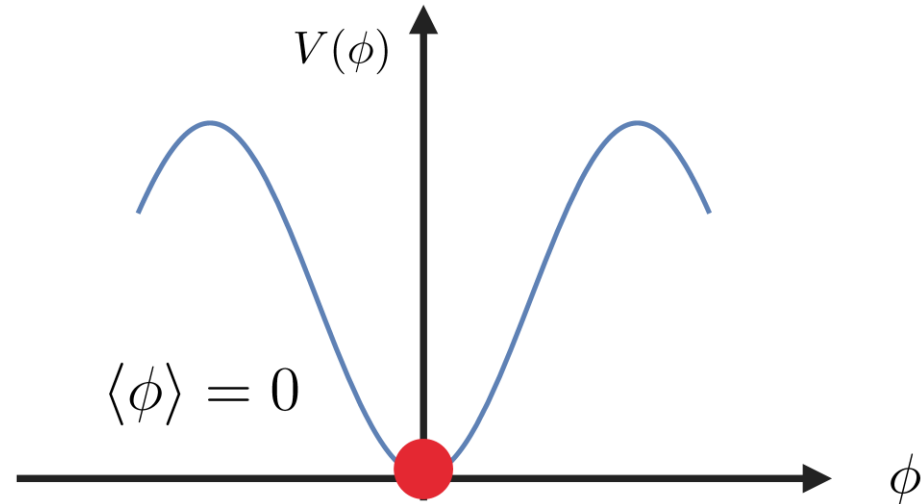


IR

$$V(\phi) = -m_\pi^2 f_\pi^2 \sqrt{1 - \frac{4m_u m_d}{(m_u + m_d)^2} \sin^2 \left(\frac{\phi}{2f_a} \right)}$$

$$\simeq - \underbrace{\frac{m_\pi^2 f_\pi^2}{4}}_{m_a^2 f_a^2} \left[\cos \left(\frac{\phi}{f_a} \right) - 1 \right]$$

$2\pi f_a$ periodic potential



Axion Potential in Dense Medium

Nuclear chiral perturbation theory with QCD axion

$$\mathcal{L}_{\text{chiral}} = \text{Tr}[U M_q e^{i\phi/f_a} + \text{h.c.}] \bar{N}N + \dots$$

Leads to **non-derivative nucleon couplings**

$$\mathcal{L} \supset - \left[m_N + \sigma_{\pi N} \left(\cos \frac{\phi}{f_a} - 1 \right) \right] \bar{N}N \quad \sigma_{\pi N} \simeq 50 \text{ MeV}$$

For nonvanishing nucleon density $n_N = \langle \bar{N}N \rangle$ **an axion potential**

$$V(\phi) = - \frac{m_\pi^2 f_\pi^2}{4} \left(1 - \underbrace{\frac{4\sigma_{\pi N} n_N}{m_\pi^2 f_\pi^2}} \right) \left(\cos \frac{\phi}{f_a} - 1 \right)$$

$\mathcal{O}(1)$ at nuclear density

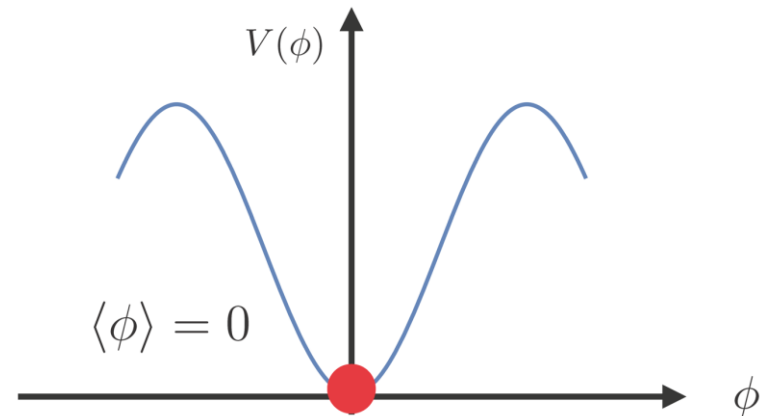
Hook & Huang [1708.08464](#), Balkin+ [2105.13354](#)

Light QCD Axions at Finite Density

$$V(\phi) = -\frac{m_\pi^2 f_\pi^2}{4} \left(\epsilon - \frac{4\sigma_{\pi N} n_N}{m_\pi^2 f_\pi^2} \right) \left(\cos \frac{\phi}{f_a} - 1 \right)$$

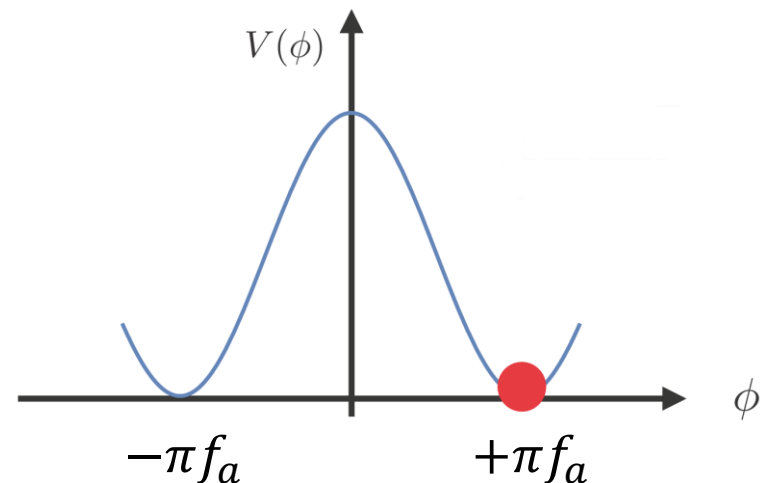
Axions with smaller mass

$$n < n_c = \epsilon \underbrace{\frac{m_\pi^2 f_\pi^2}{4\sigma_{\pi N}}}_{(2.1 \text{ fm})^{-3}}$$



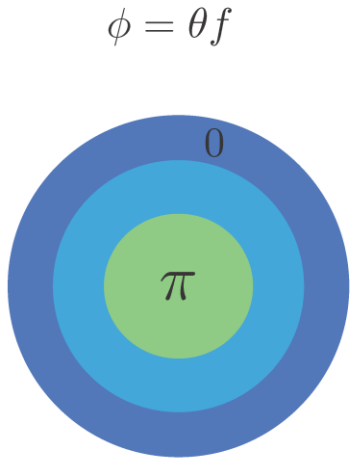
New minima appear at large density

$$n > n_c = \epsilon \frac{m_\pi^2 f_\pi^2}{4\sigma_{\pi N}}$$

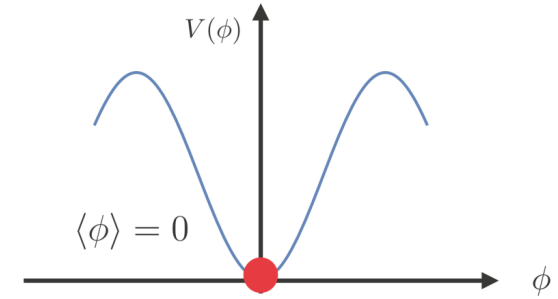
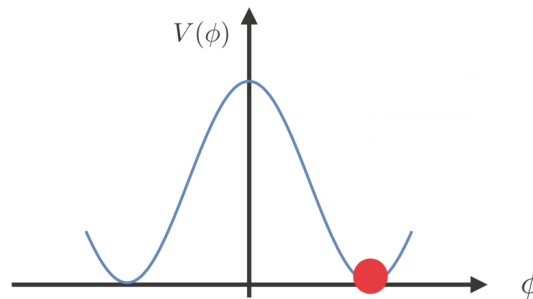
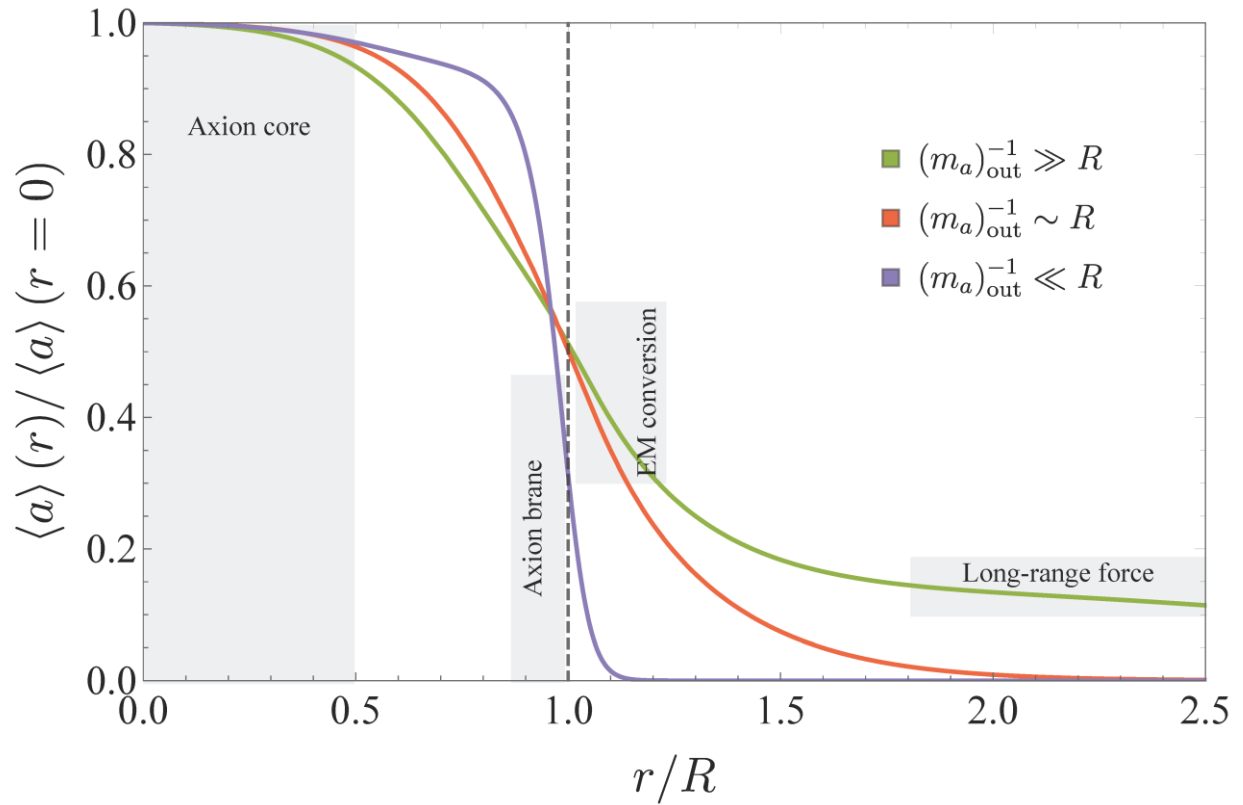


Hook & Huang [1708.08464](#), Balkin+ [2105.13354](#)

Axion Profile of a Neutron Star

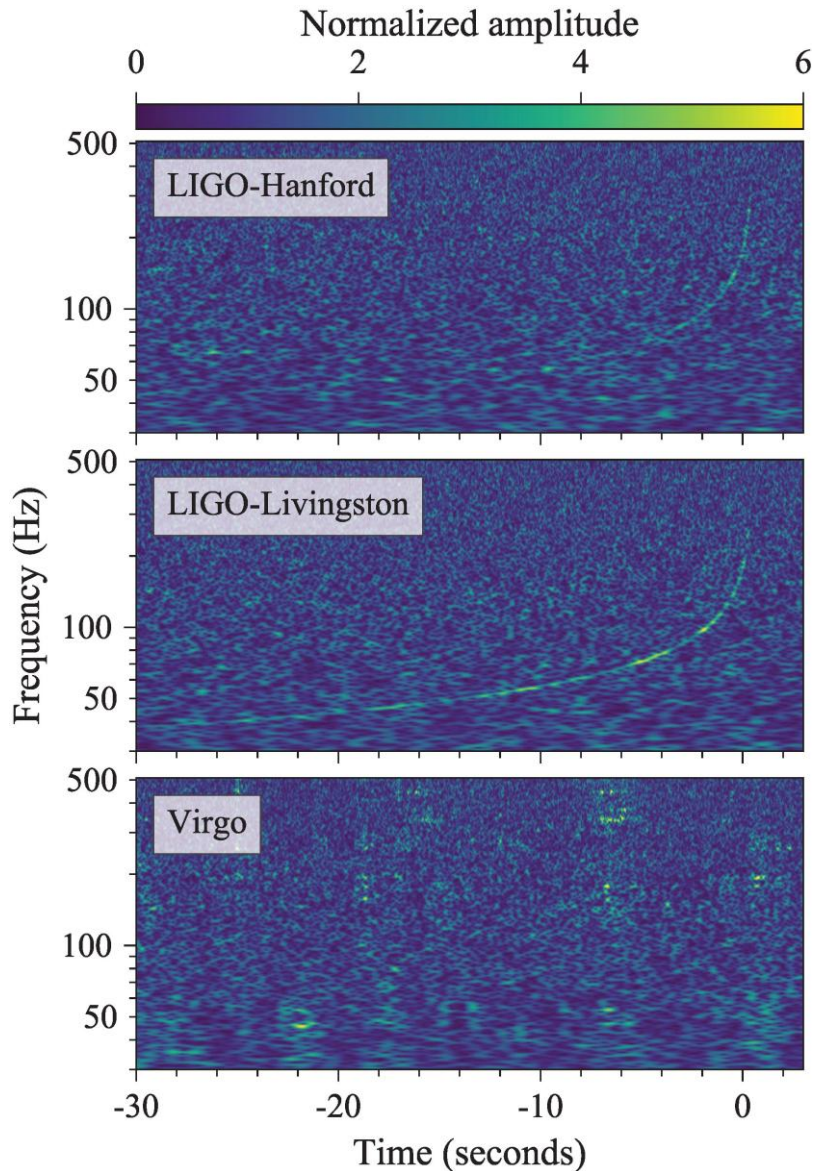


Nucleon mass shifted
 $m_N \rightarrow m_N - \sigma_{\pi N}$

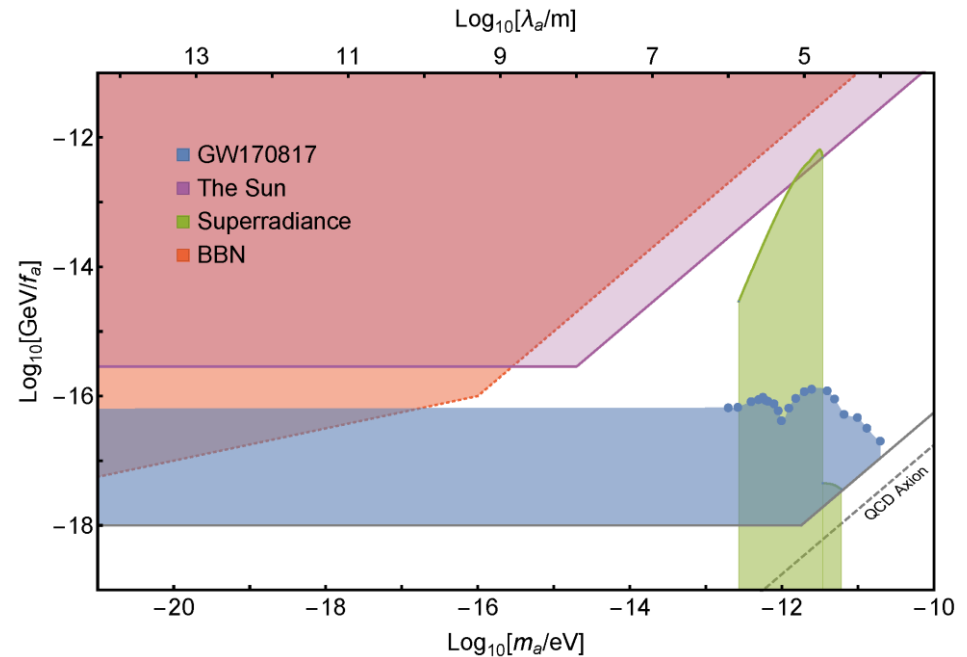


Hook & Huang [1708.08464](#)
 Balkin+ [2105.13354](#)

Binary Neutron Star Merger GW 170817



LIGO & Virgo, [1710.05832](#)



**First Constraints on Nuclear Coupling of
Axionlike Particles from the Binary Neutron
Star Gravitational Wave Event GW 170817**

J.Zhang+, [2105.13963](#)

Changed Equation of State (EoS)

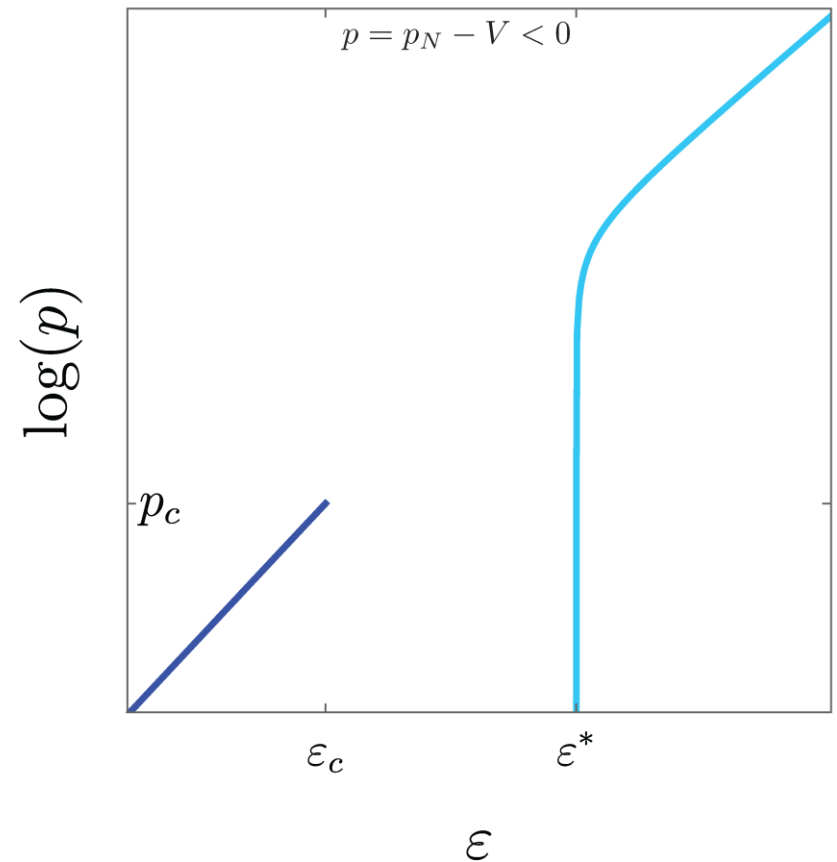
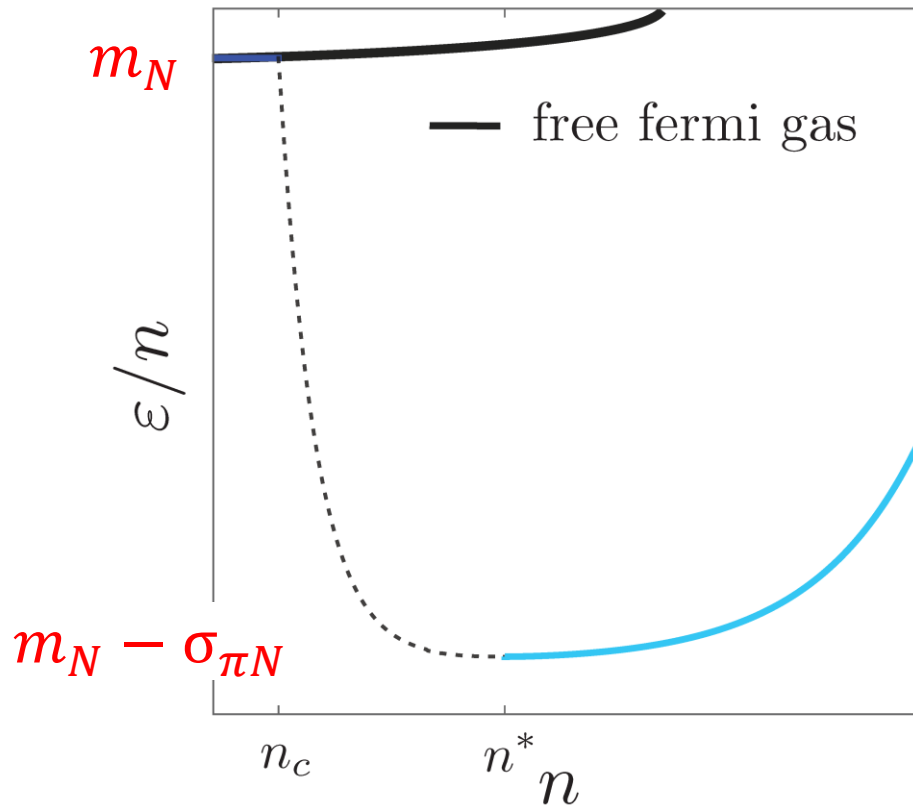
Energy/nucleon

Pressure

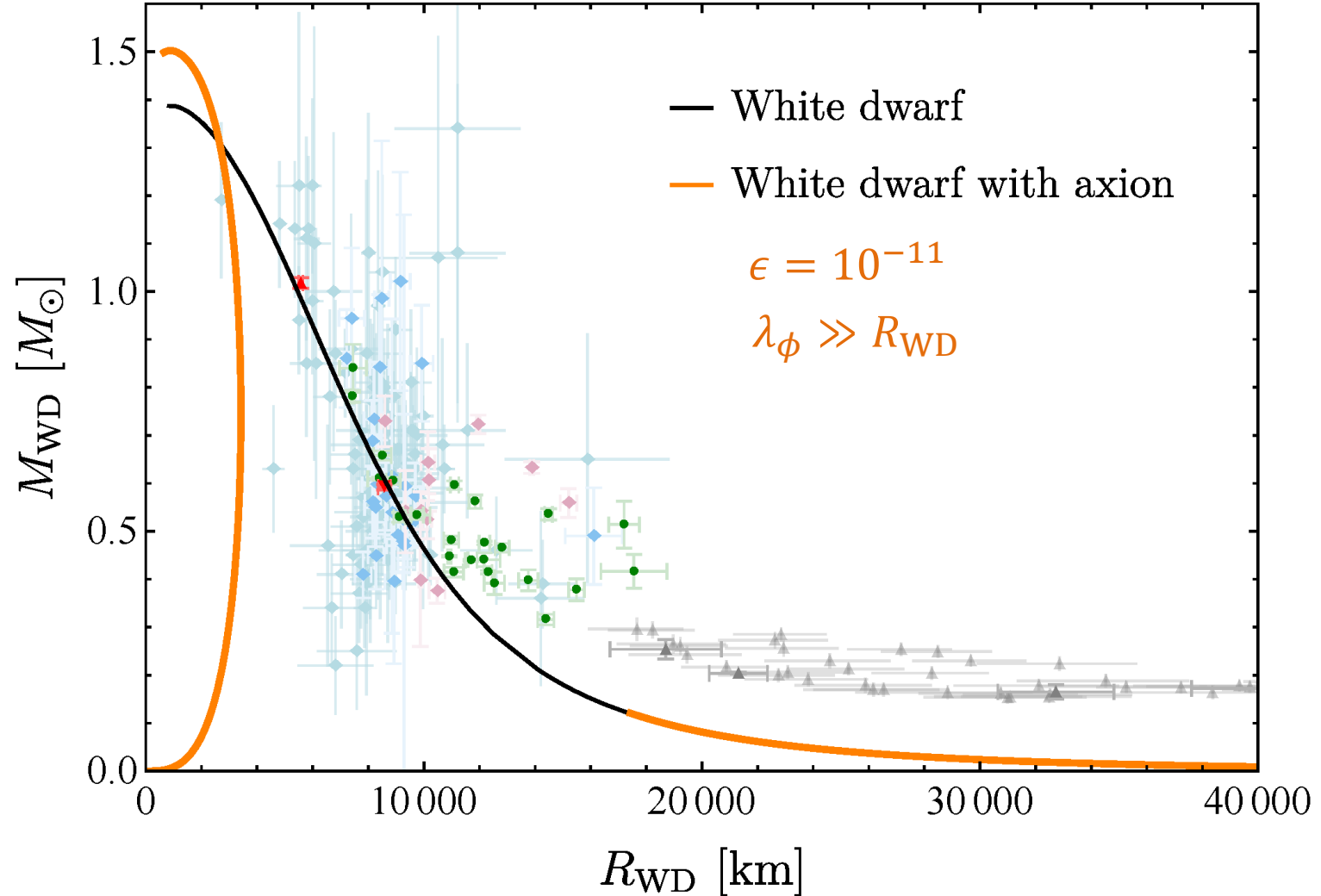
— metastable ($\phi = 0$)

.... unstable

— stable ($\phi = \pi f$)

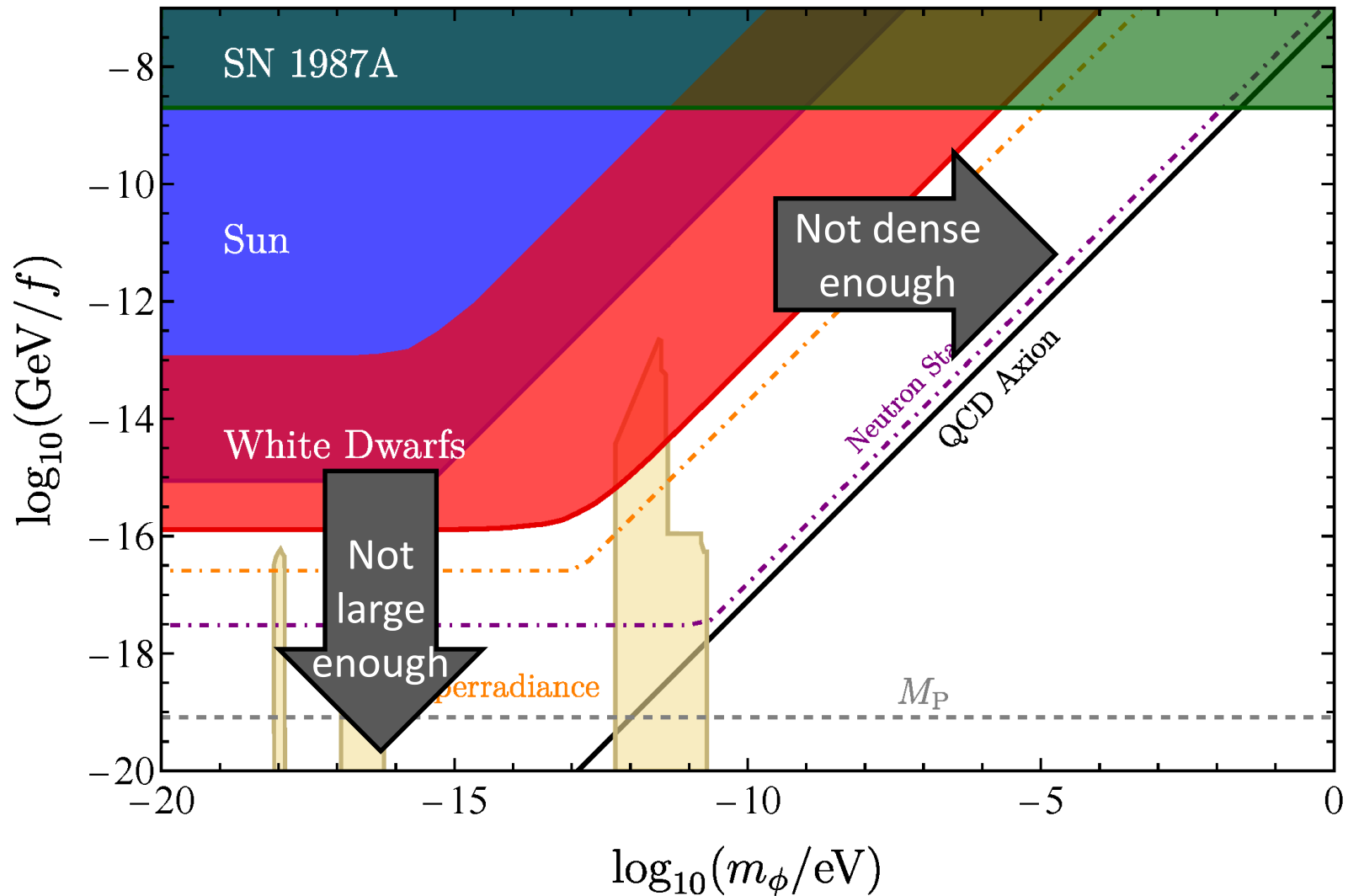


White-Dwarf Mass-Radius Relation



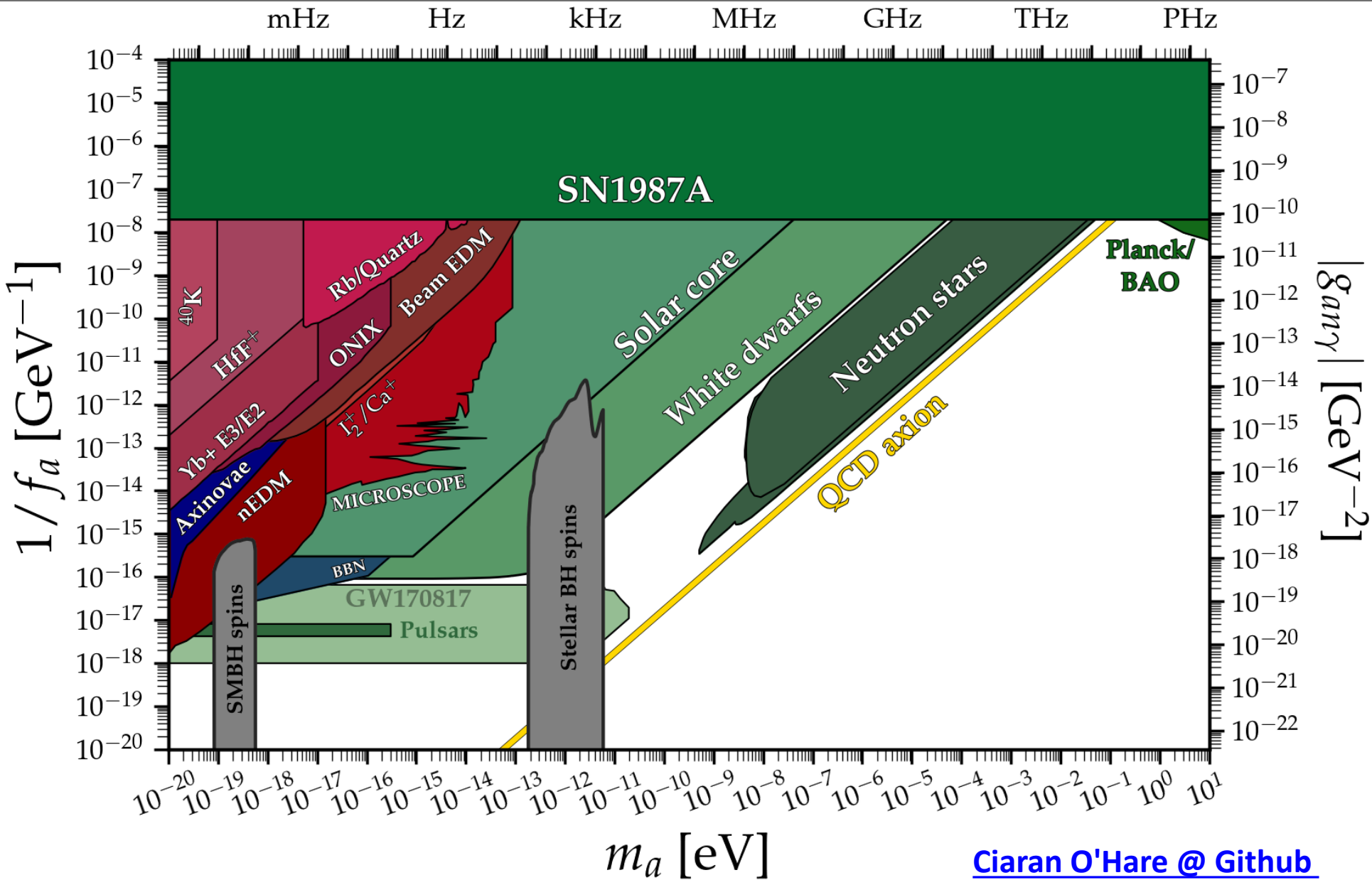
R. Balkin, J. Serra, K. Springmann, S. Stelzl & A. Weiler, [2211.02661](#)

Axion Bounds from Stellar Structure



R. Balkin, J. Serra, K. Springmann, S. Stelzl & A. Weiler, [2211.02661](#)

Peccei-Quinn Scale vs. Axion Mass



[Ciaran O'Hare @ Github](#)