

# Dilaton Phase Transitions and Axion Relic Pockets

M.C. David Marsh  
Stockholm University



20th Patras workshop on axions, WIMPs and WISPs

22 September, 2025



# Dilaton Phase Transitions and Axion Relic Pockets

*With*

Charalampos Nikolis,  
Aleksandr Chatrchyan,  
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Oksana Iarygina,  
Pierluca Carenza,  
Wafa Khater



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A gauge theory has two parameters – quantum gravity has none

$$\mathcal{L} = -\frac{1}{2g^2} \text{Tr} (F_{\mu\nu} F^{\mu\nu}) + \frac{\theta}{16\pi^2} \text{Tr} (F_{\mu\nu} \tilde{F}^{\mu\nu})$$

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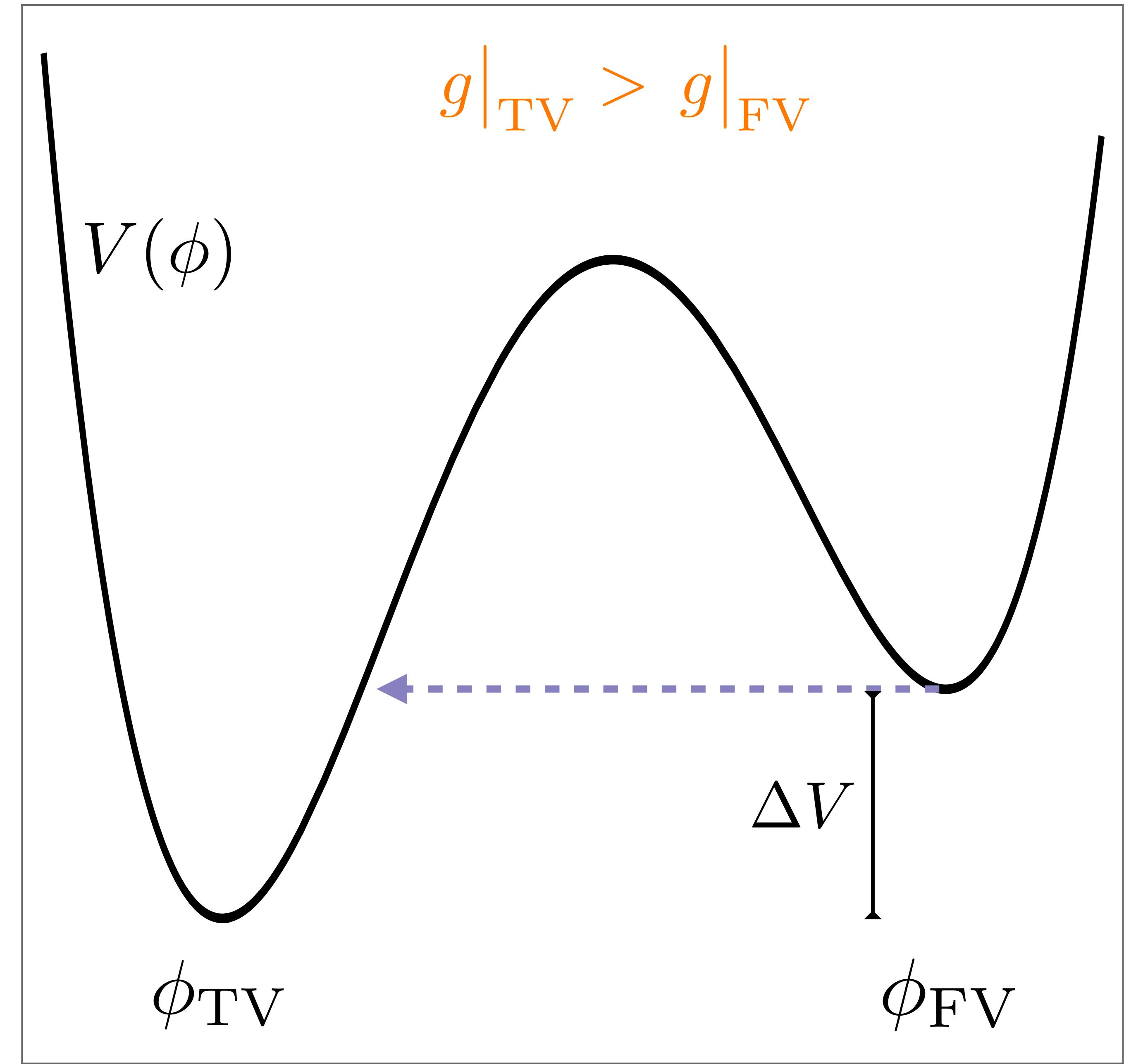
$$\mathcal{L} = -\frac{1}{2} f(\phi) \text{Tr} (F_{\mu\nu} F^{\mu\nu}) + \frac{a}{16\pi^2 f_a} \text{Tr} \left( F_{\mu\nu} \tilde{F}^{\mu\nu} \right)$$

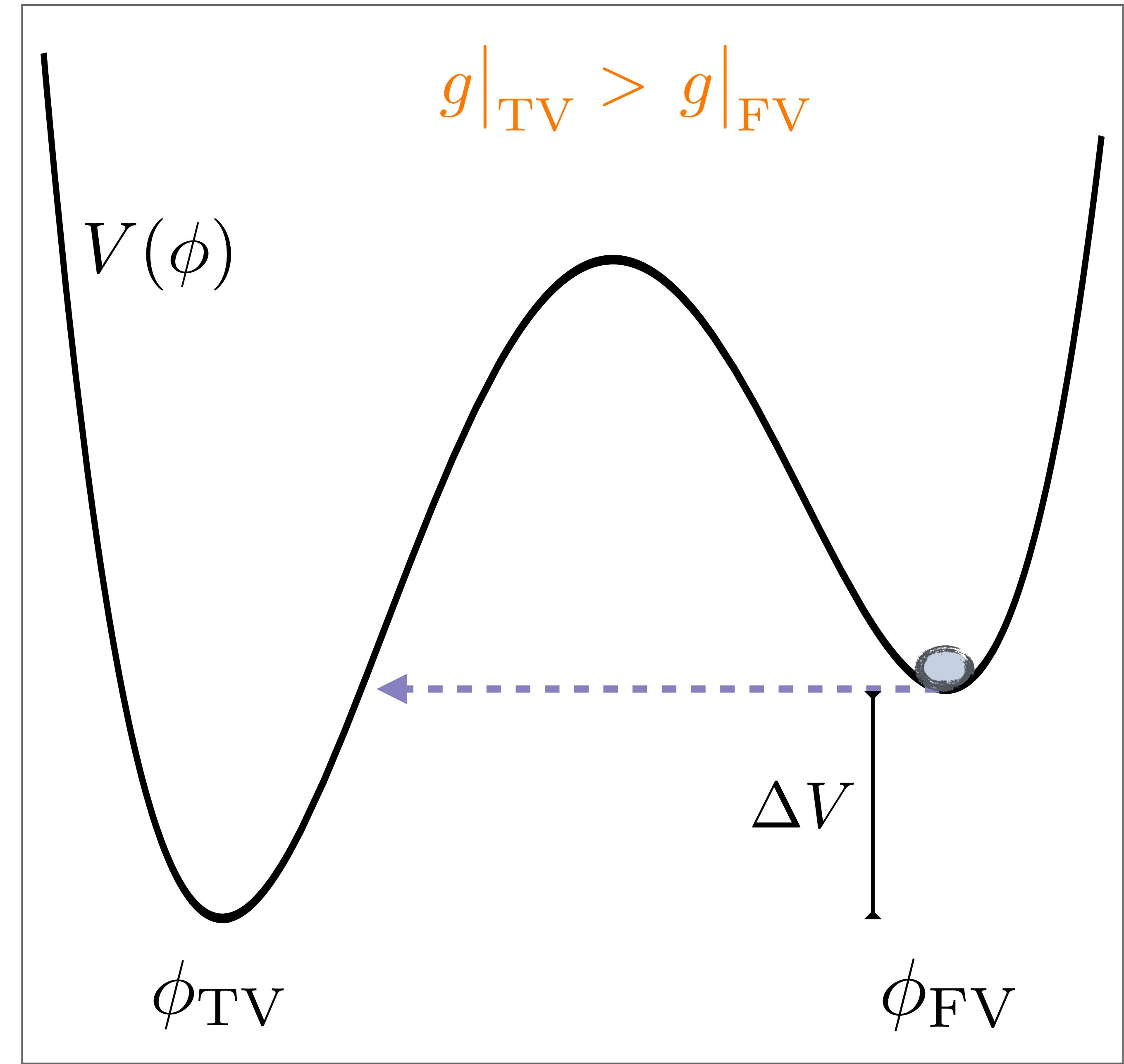
$\phi$  : 'dilaton'

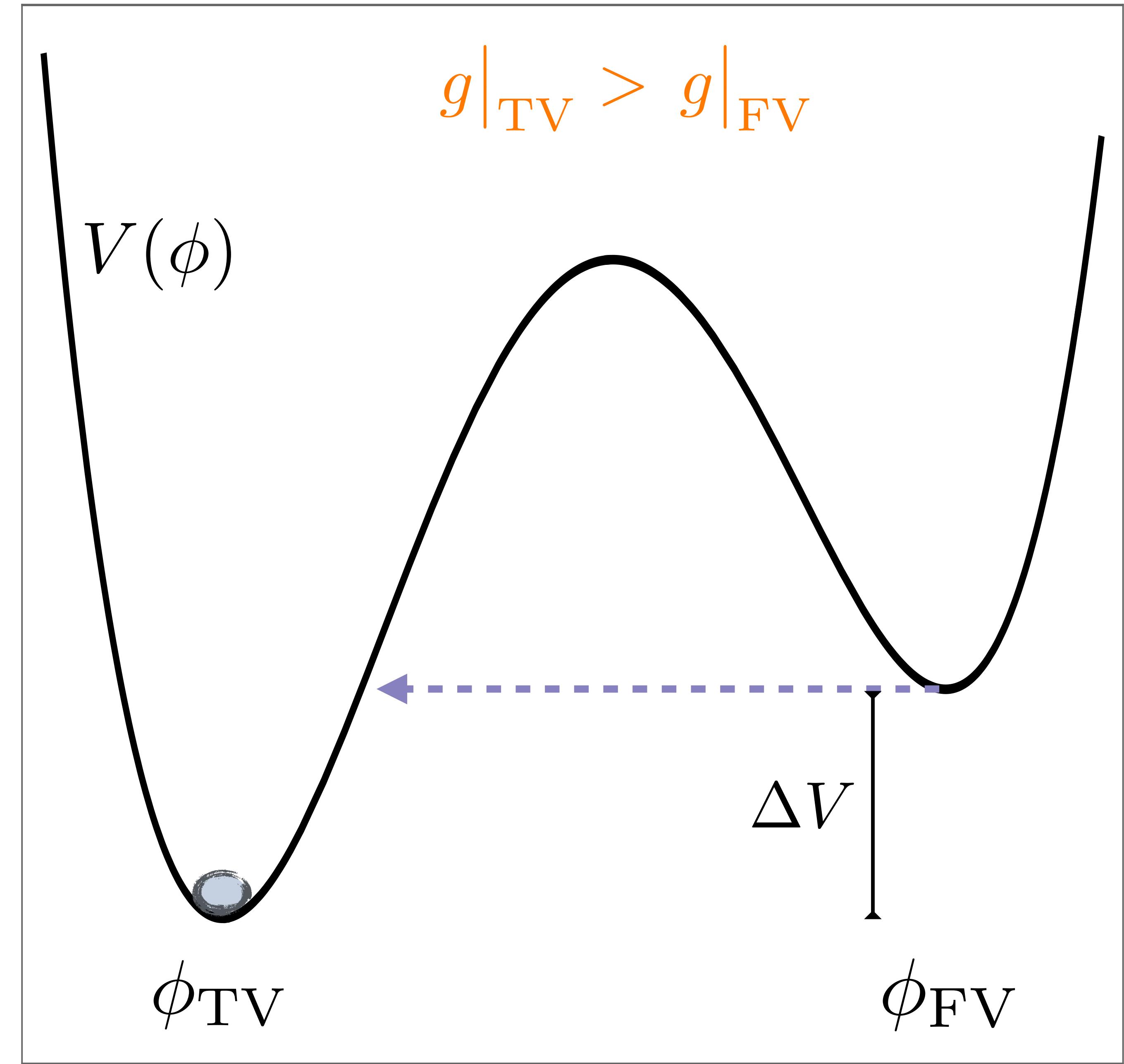
$$\langle f(\phi) \rangle = \frac{1}{g^2} \Big|_{\text{UV}}$$

$a$  : axion

$$\langle a/f_a \rangle = \theta$$





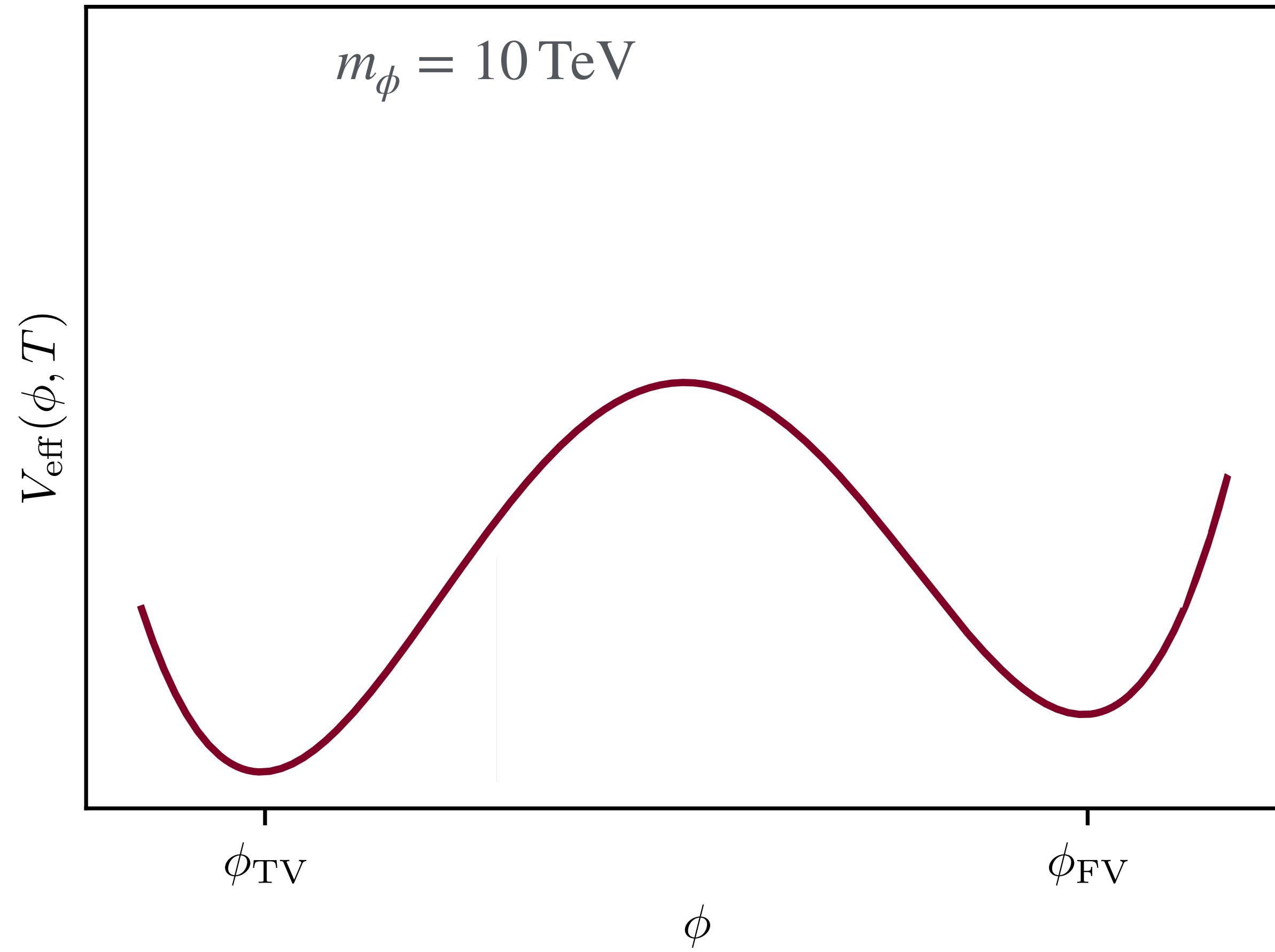


# Part I: the QCD dilaton

$$\mathcal{L} = -\frac{1}{2}f(\phi) \operatorname{tr}\left(G_{\mu\nu}G^{\mu\nu}\right) + \sum_i \bar{q}_i \left(i\not\nabla - m_i\right) q_i + \frac{1}{2}(\partial\phi)^2 - V_0(\phi)$$

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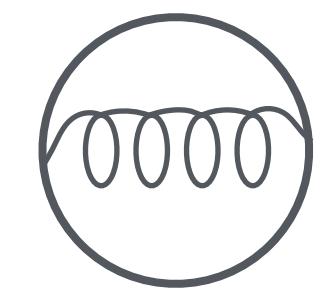
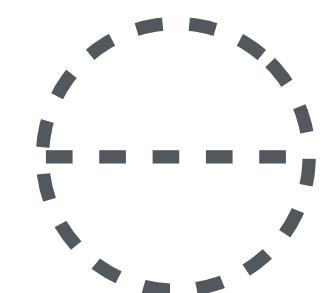


$$V_{\text{eff}} = V_0 + V_T + V_{\mathcal{P}}$$

$V_0$  = tilted double well

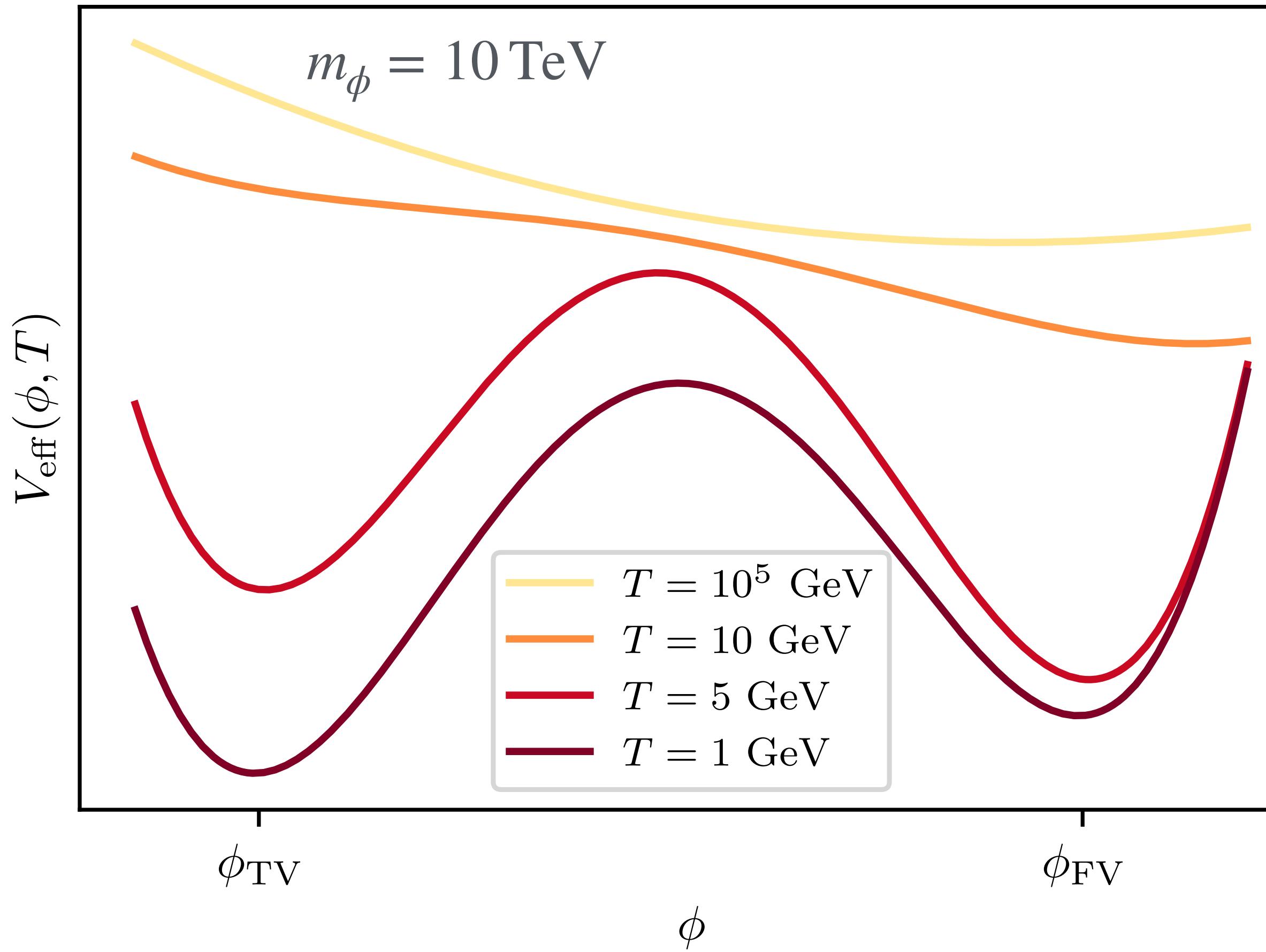
$$V_T = \frac{T^4}{2\pi^2} J_B\left(\frac{m_\phi^2(\phi)}{T^2}\right)$$

$$V_{\mathcal{P}} = -\frac{8\pi^2 T^4}{45} \left( \frac{17}{3} - \frac{235}{16} \alpha_s + \mathcal{O}(\alpha_s^{3/2}) \right)$$



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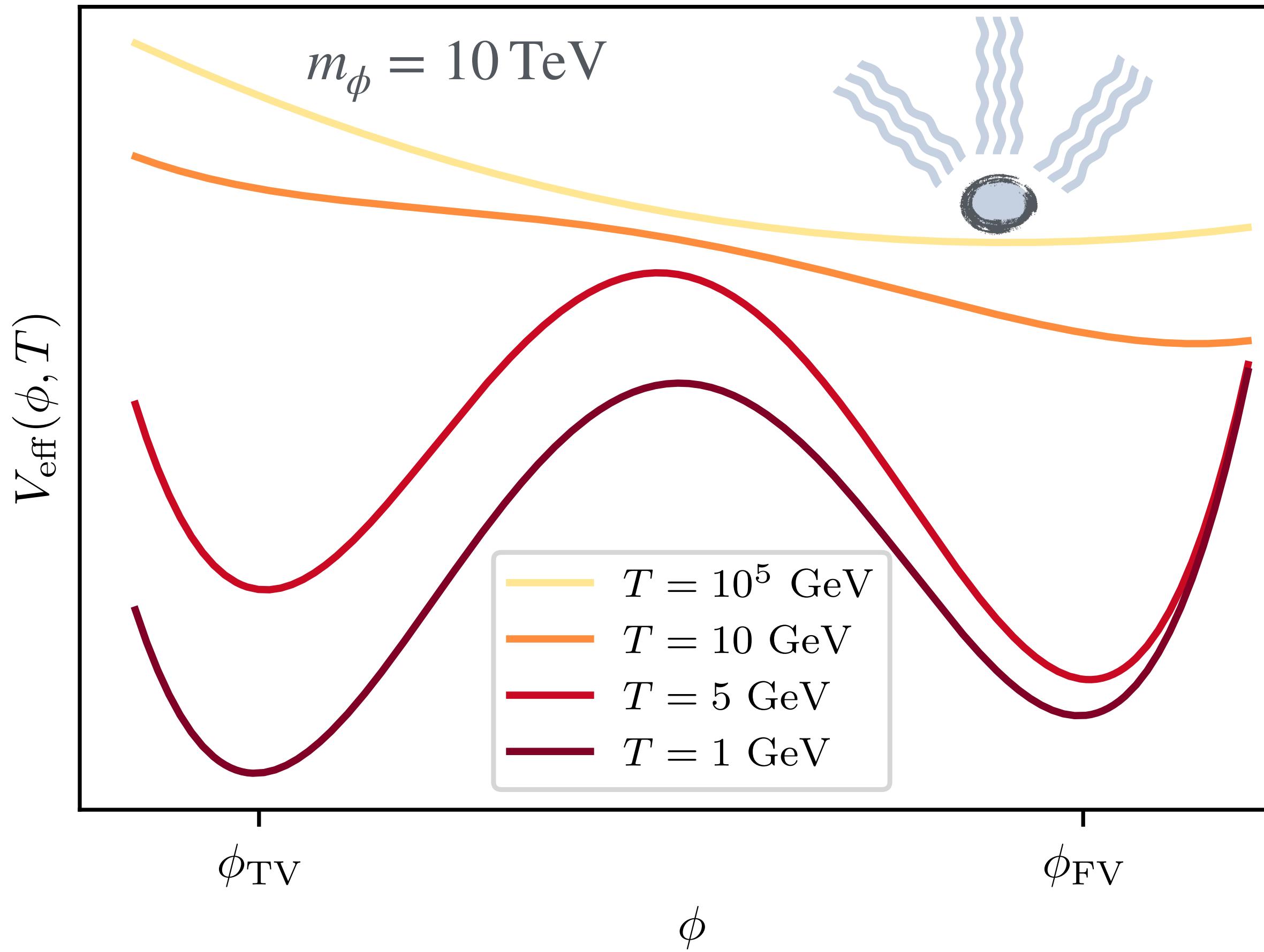
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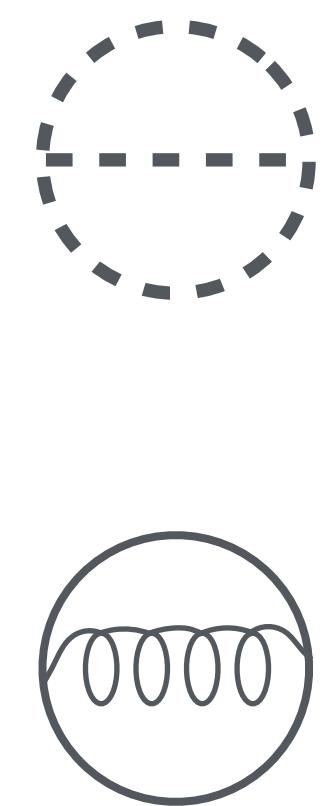


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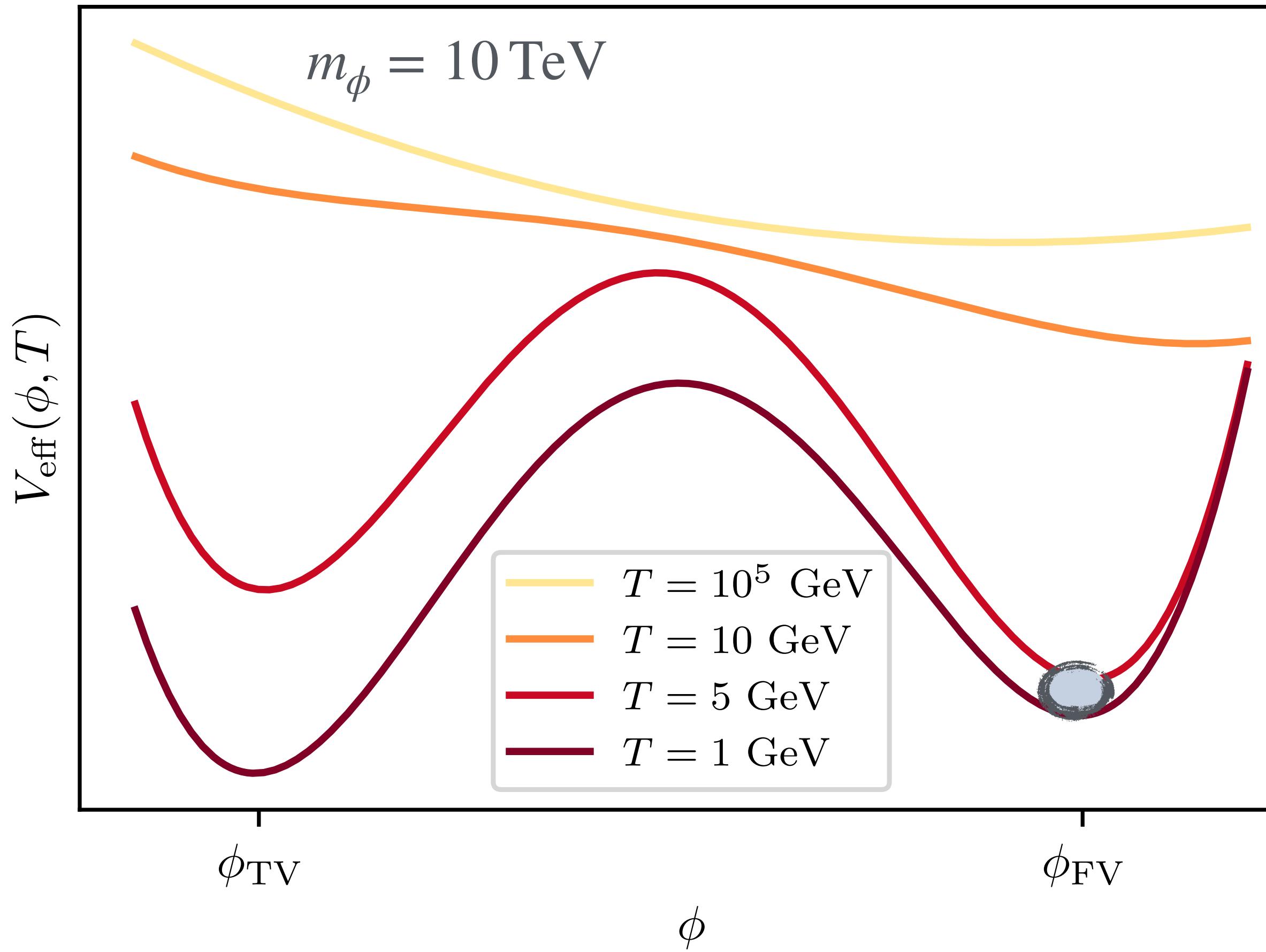
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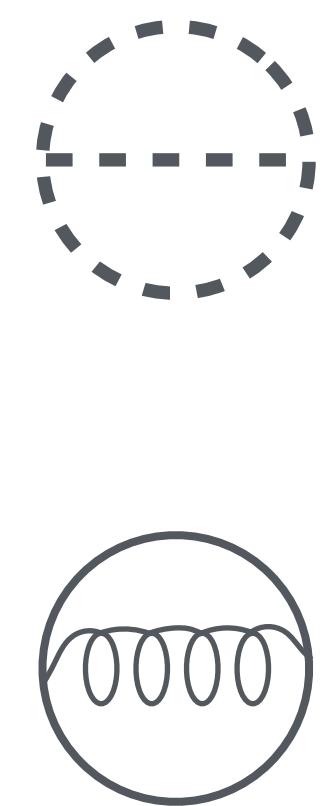


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# Big Bang Cosmology of the first micro-second

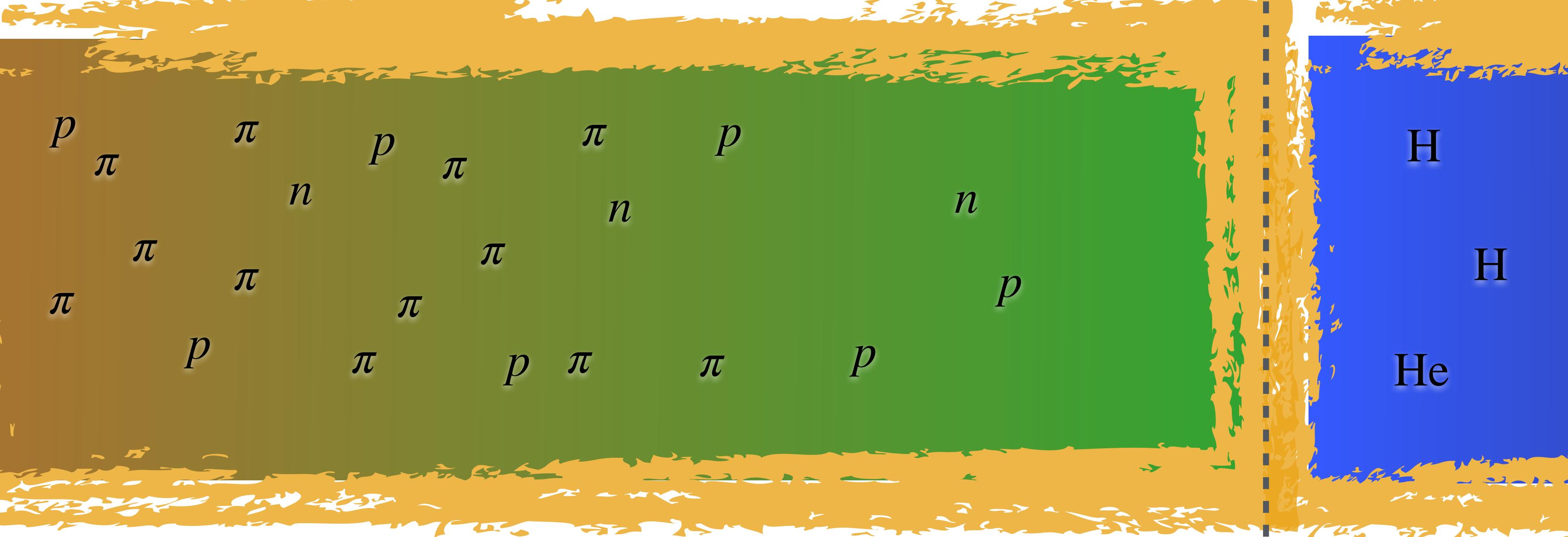
## Quark-Gluon Plasma

$$\alpha_s < 1$$
$$\langle \bar{q}q \rangle = 0$$



## Hadron Gas

$$\alpha_s \gtrsim 1$$
$$\langle \bar{q}q \rangle \neq 0$$



## Big Bang Nucleosynthesis



$T$  [MeV]

200

100

10

1

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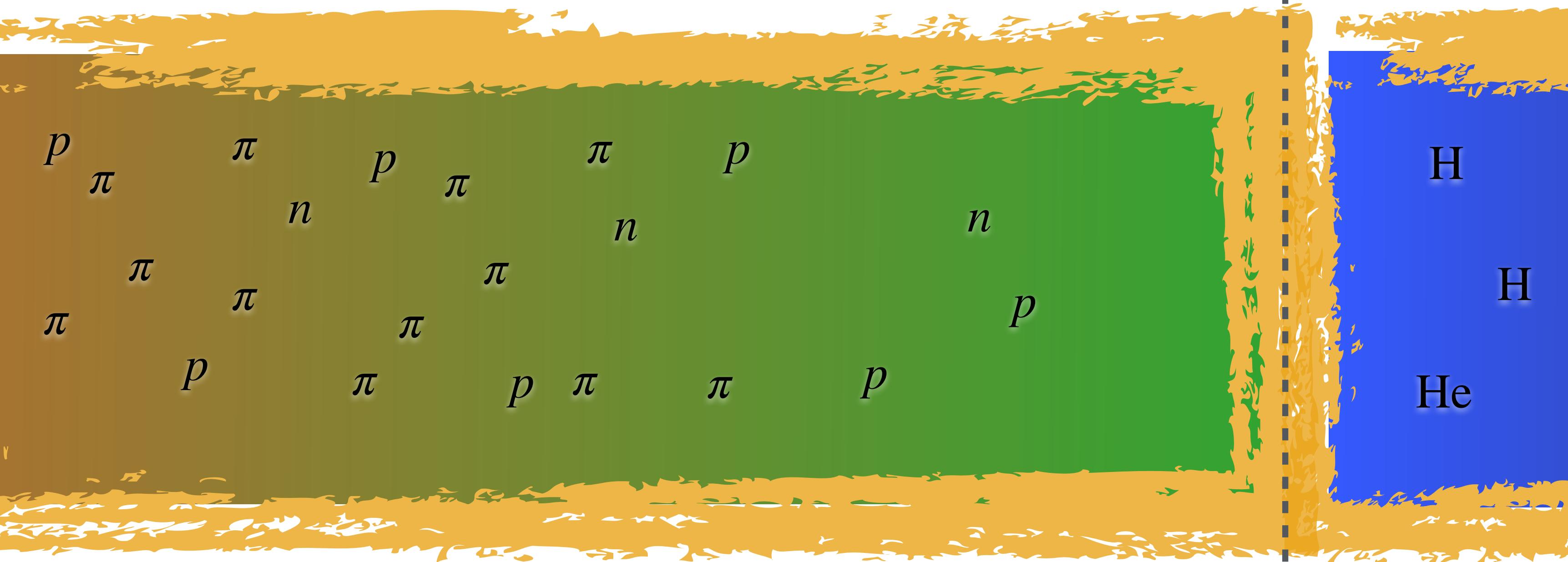
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Cross-over  
in SM

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## Big Bang Nucleosynthesis



$$\phi = \phi_{\text{TV}} ? \quad \phi = \phi_{\text{FV}} ?$$

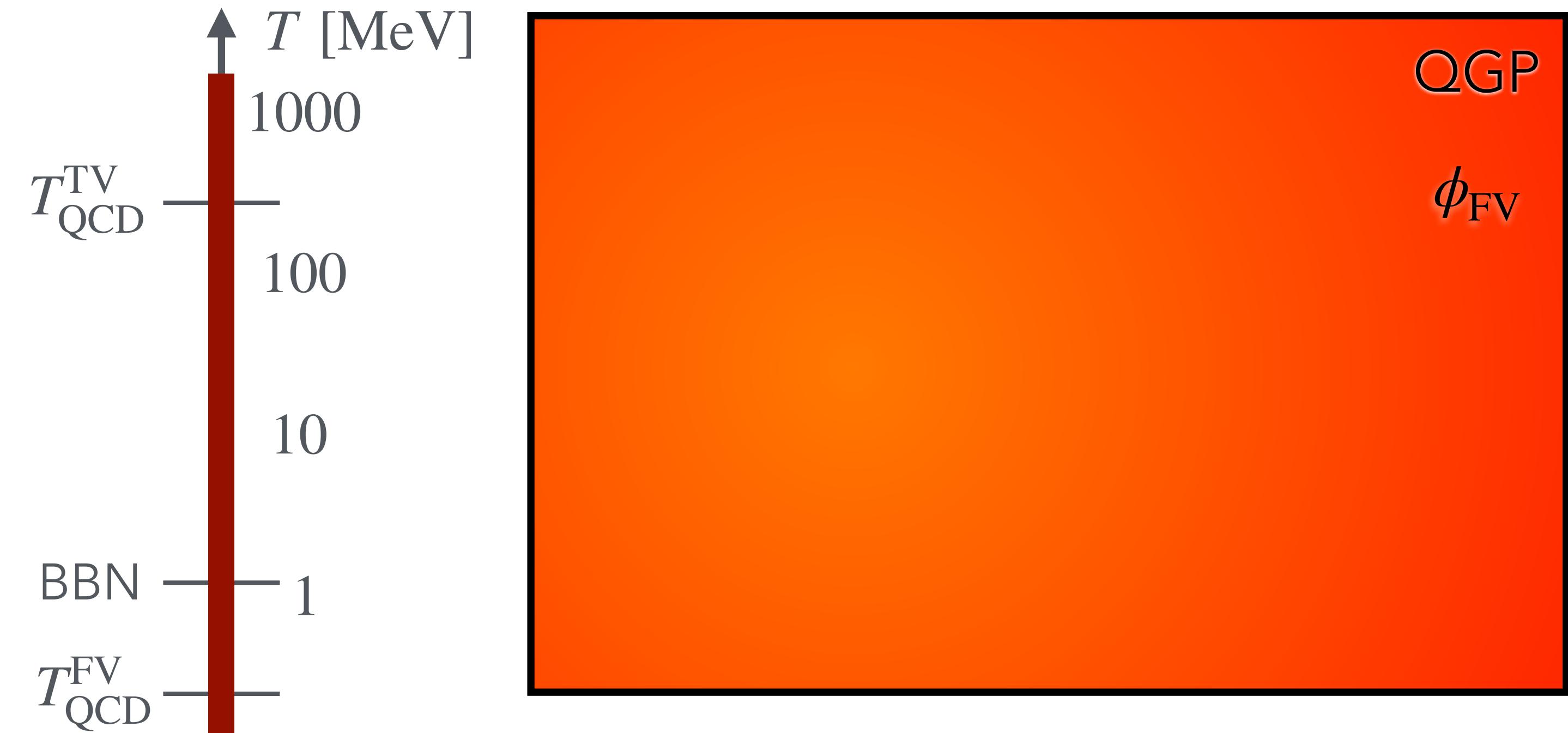
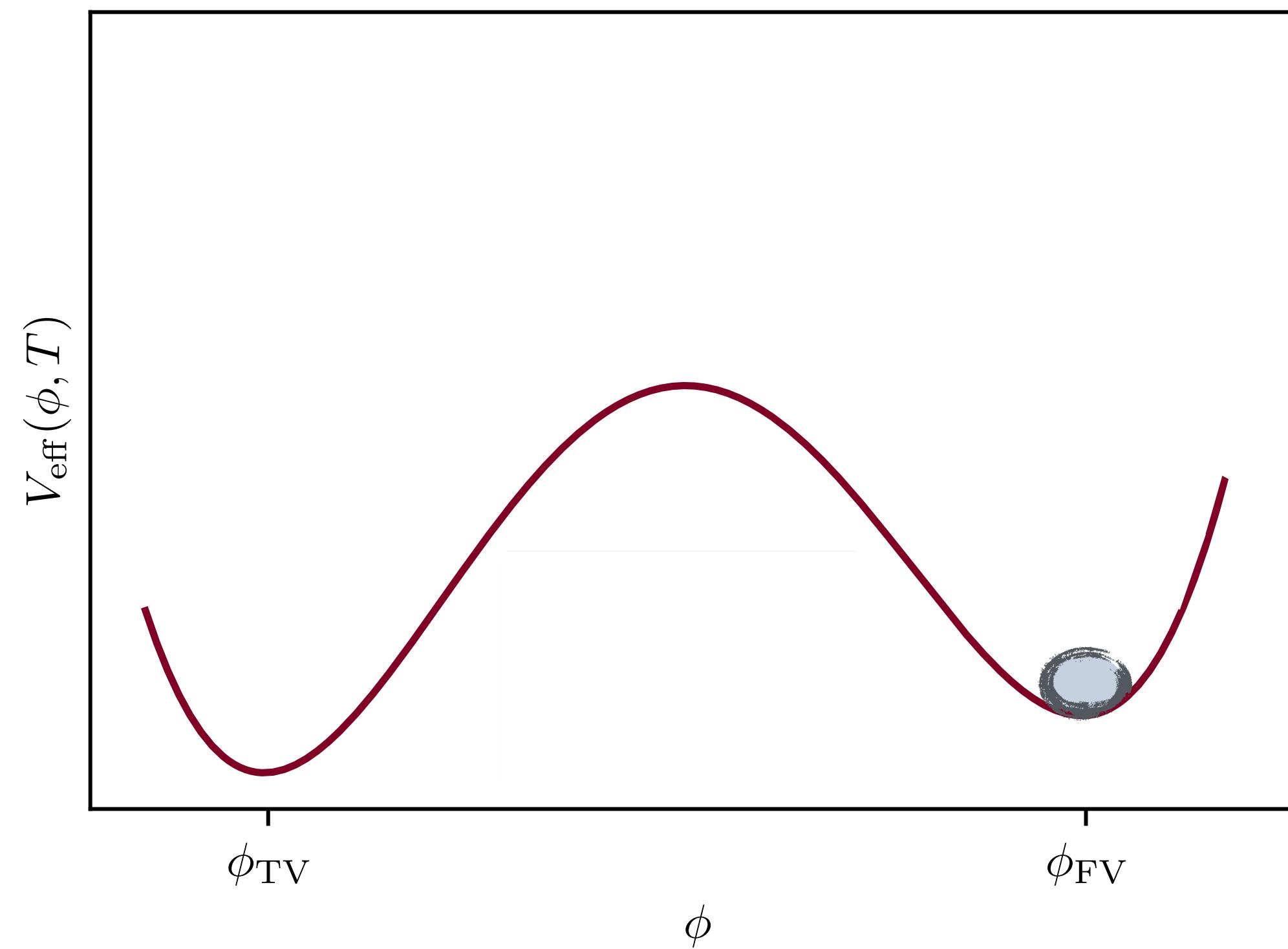
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# A dilton-induced first-order QCD Phase Transition

Dimensional transmutation:

$$\Lambda_{\text{QCD}} = \mu \exp \left[ -\frac{8\pi^2}{\beta_0 g_3^2(\mu)} \right] \quad \left( \beta_0 = 11 - \frac{2}{3} N_f \right)$$

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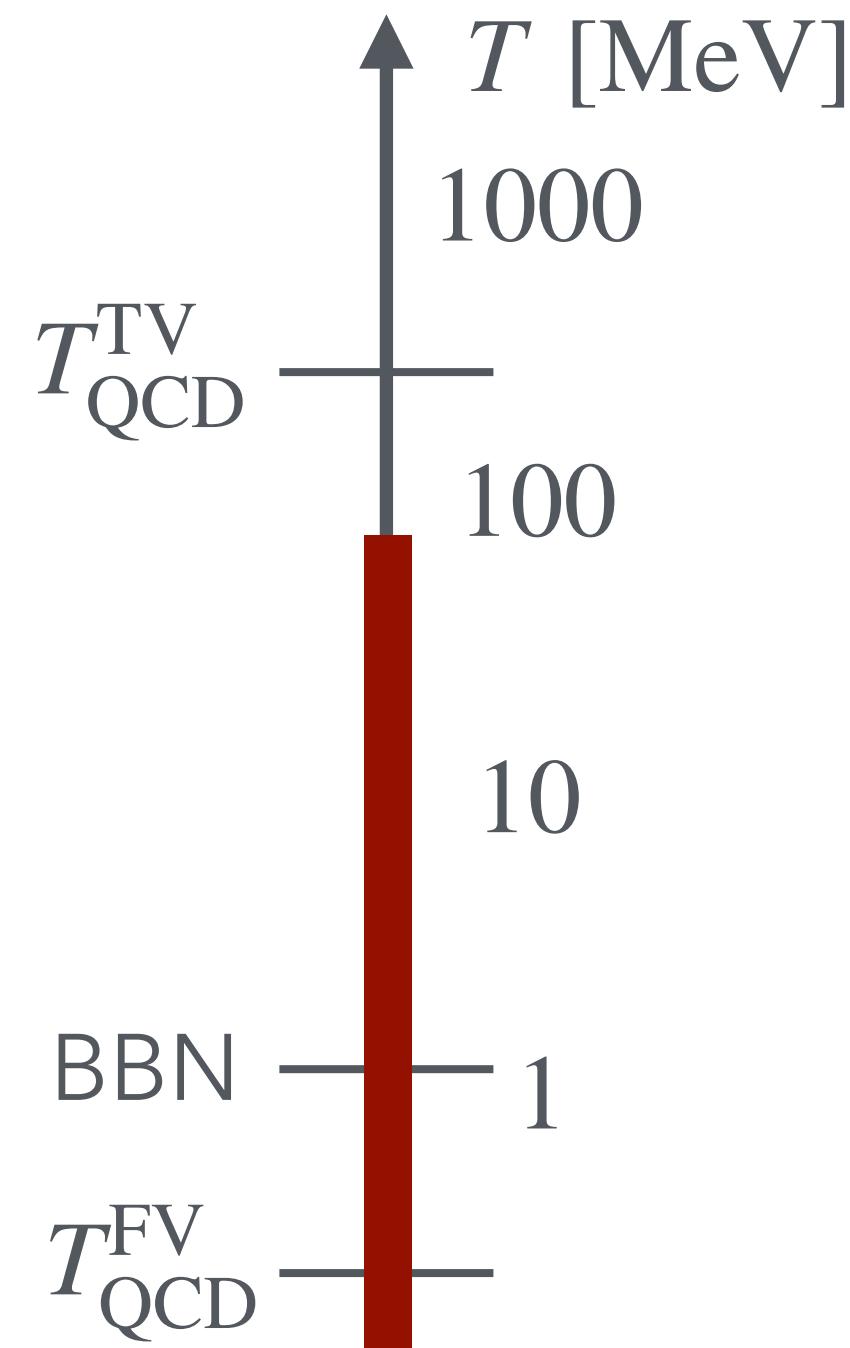
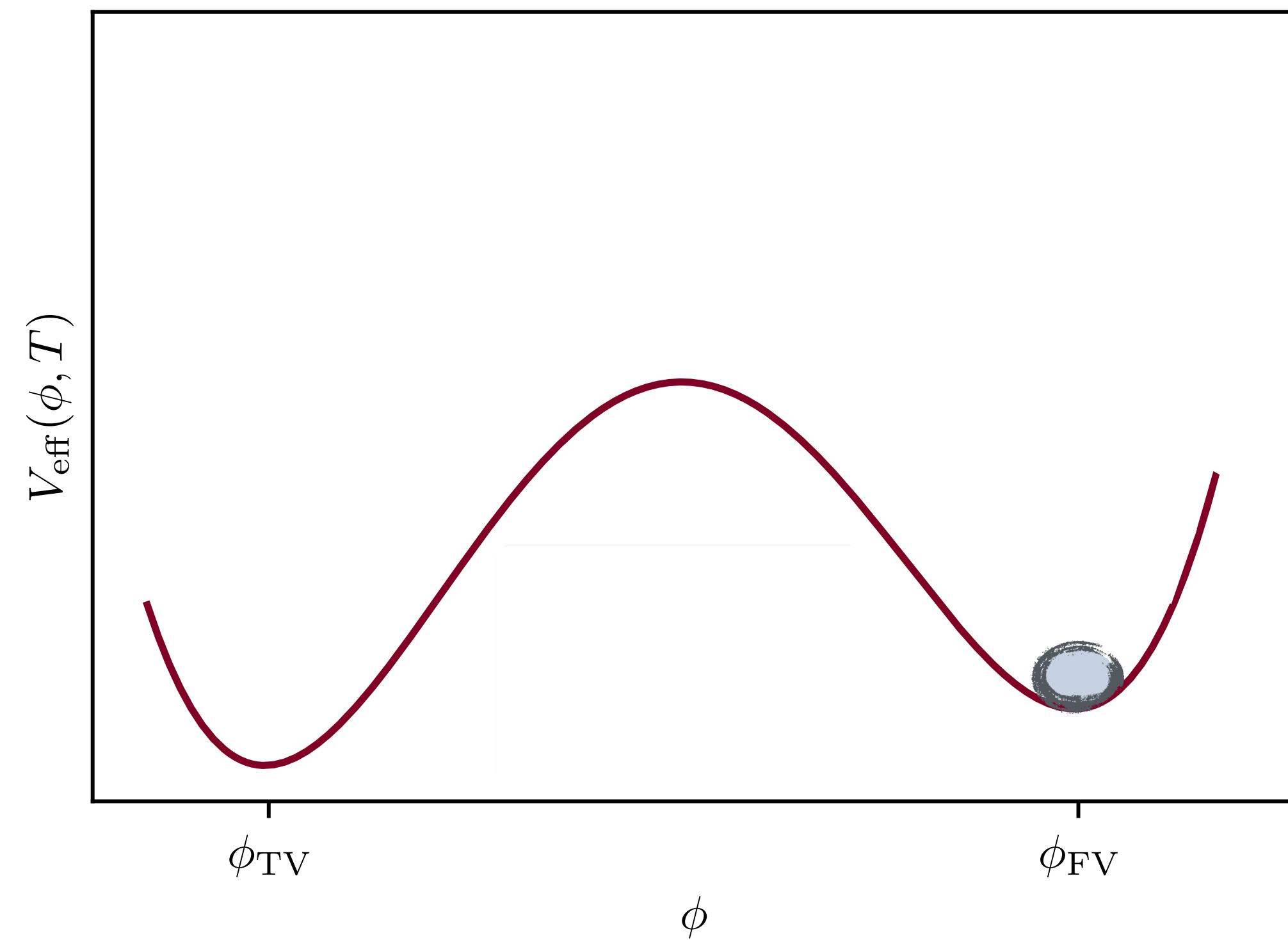


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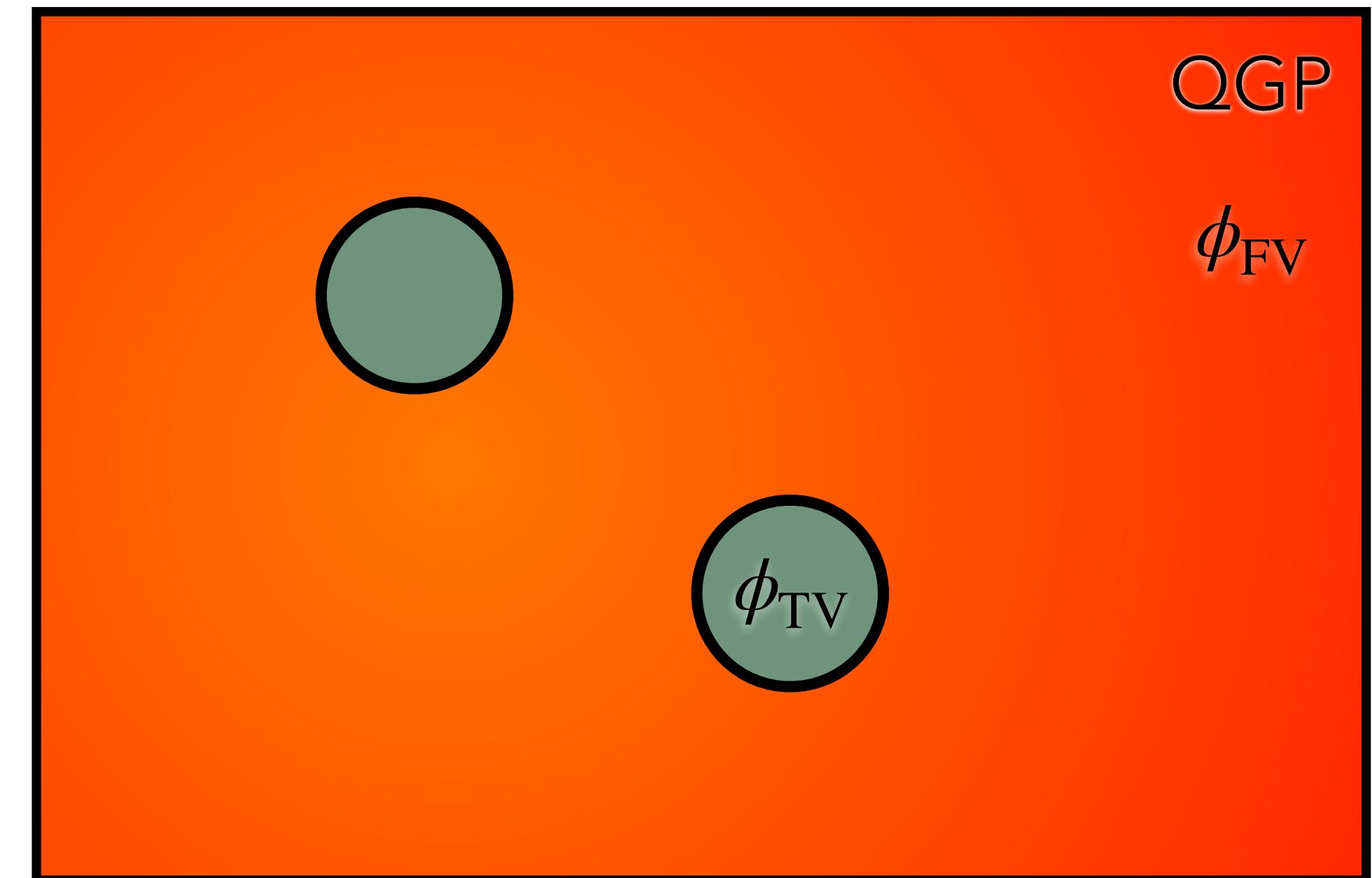
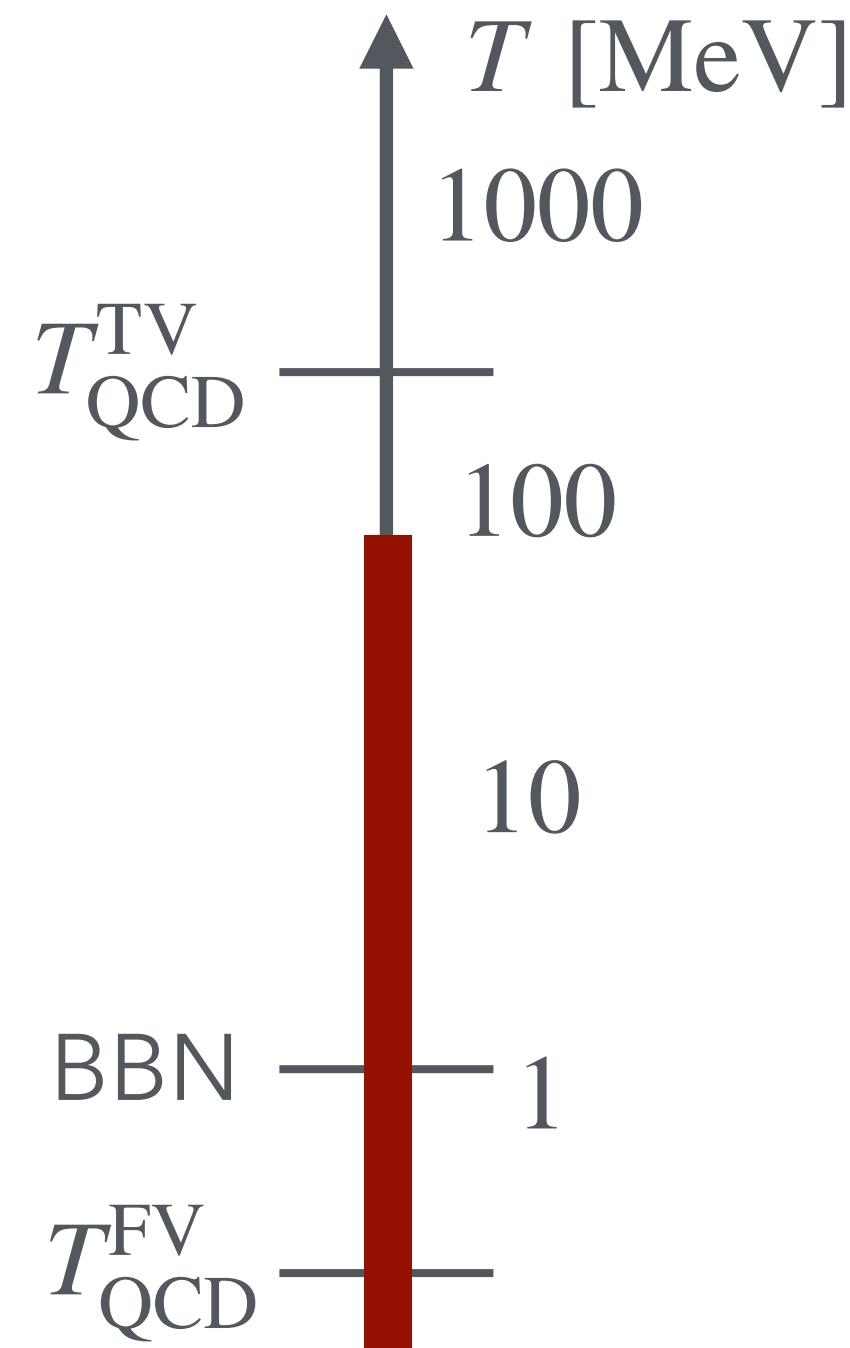
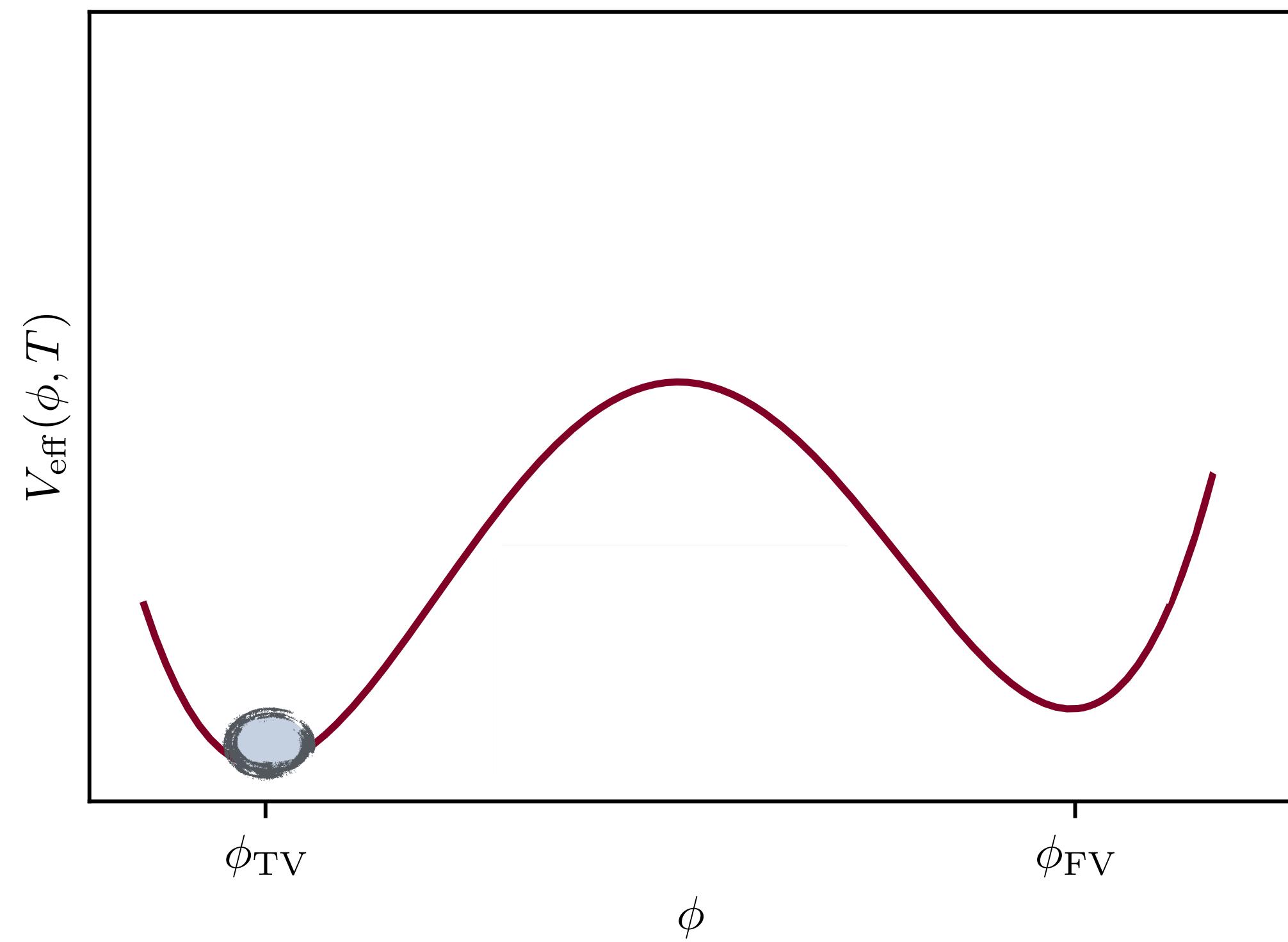


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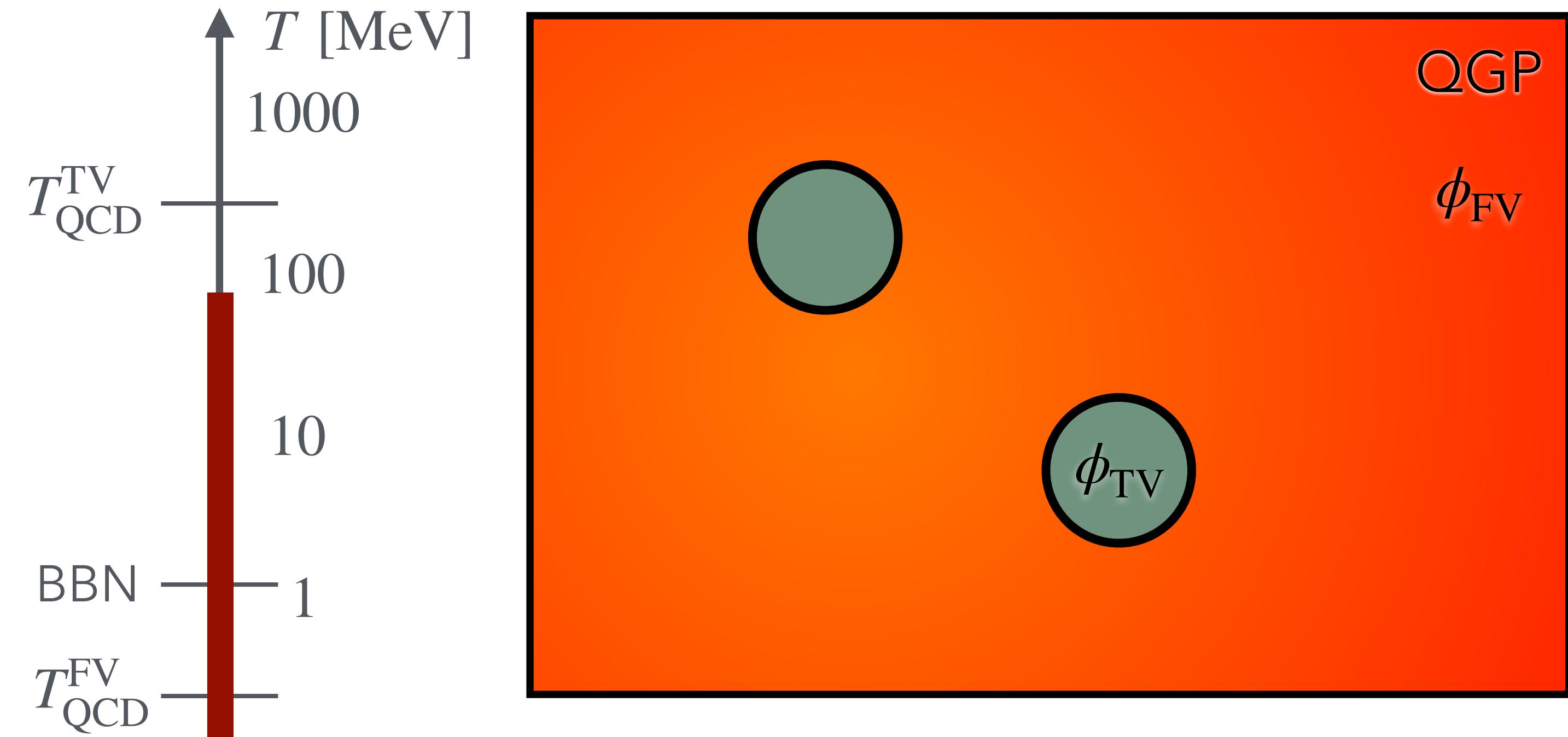
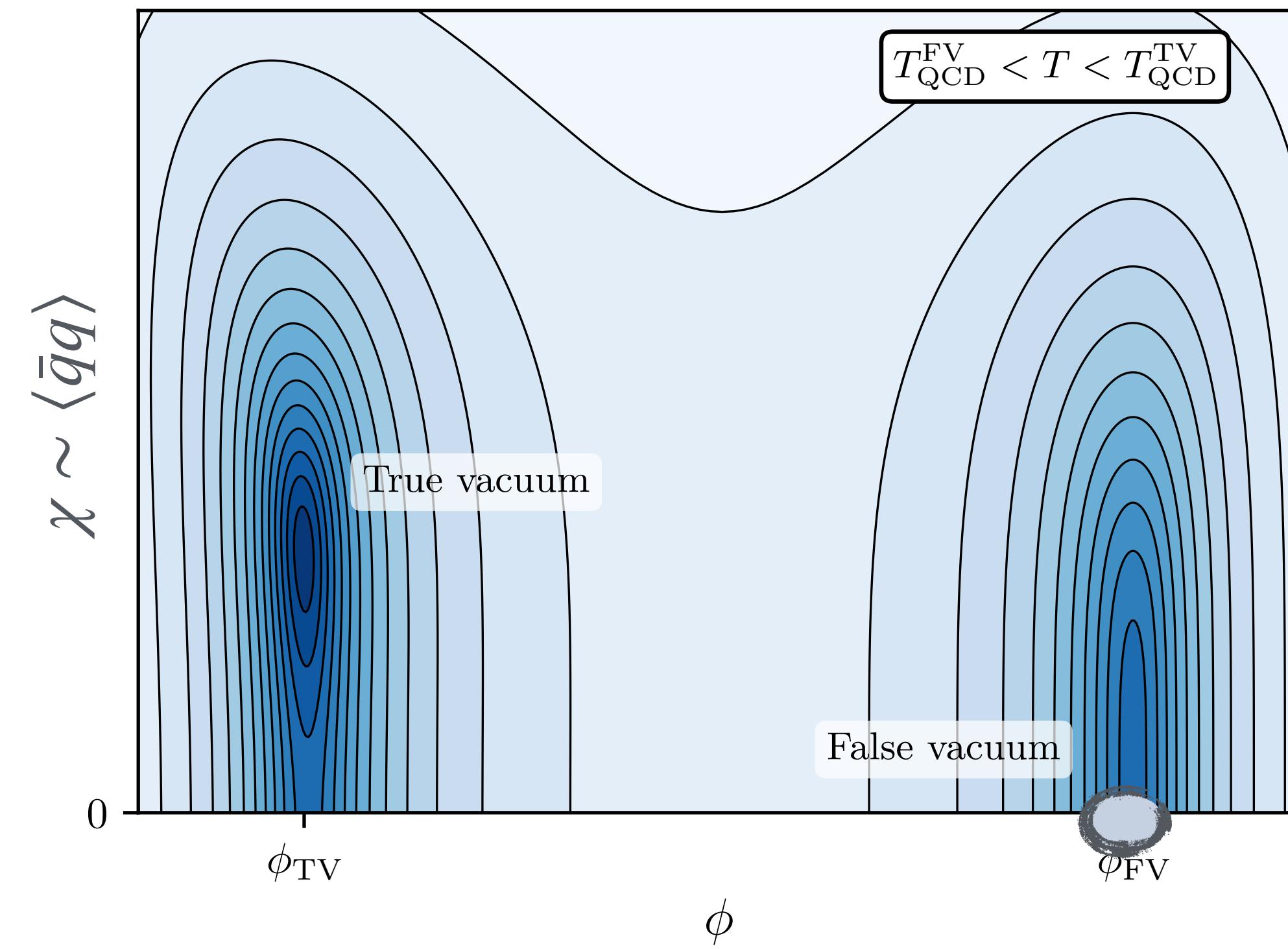


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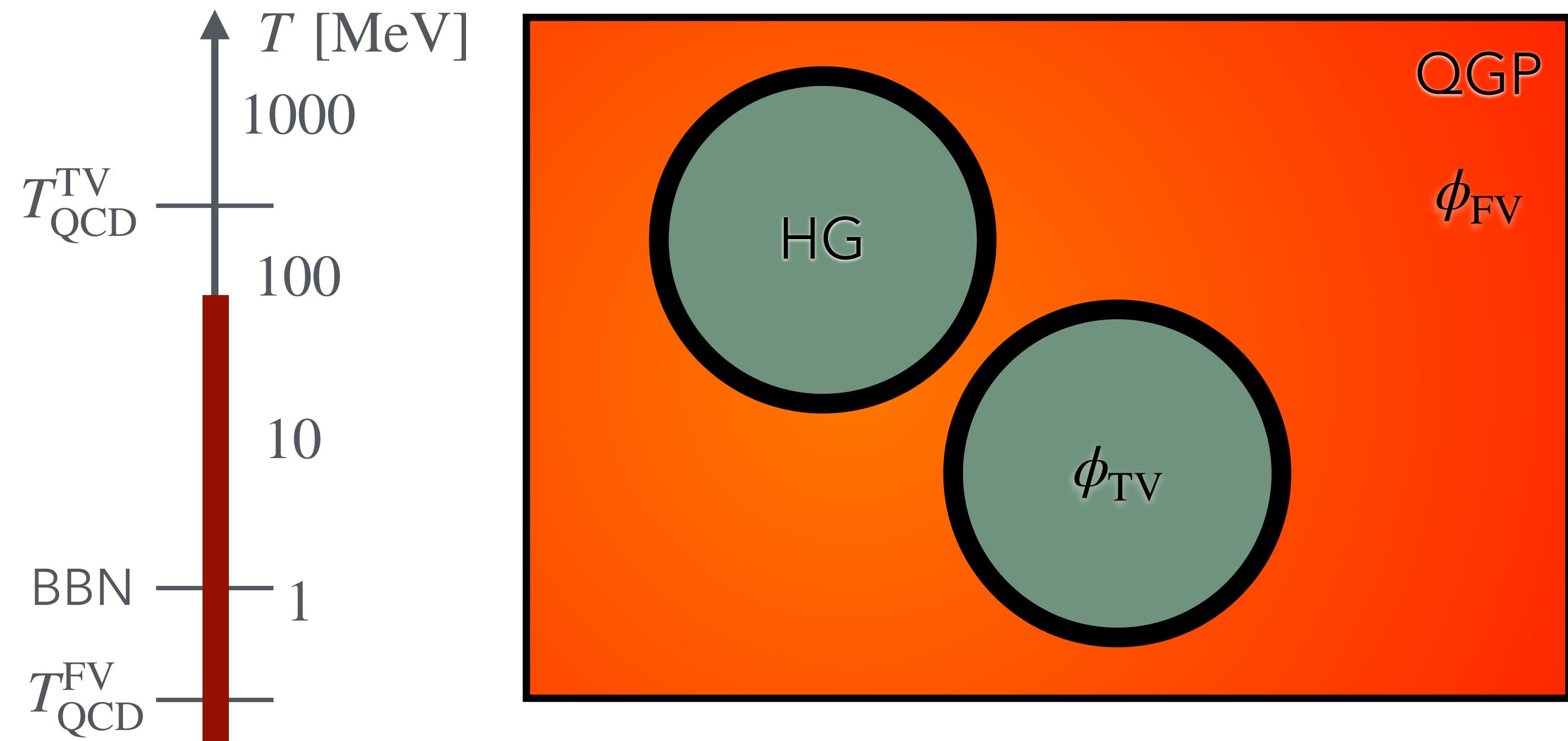
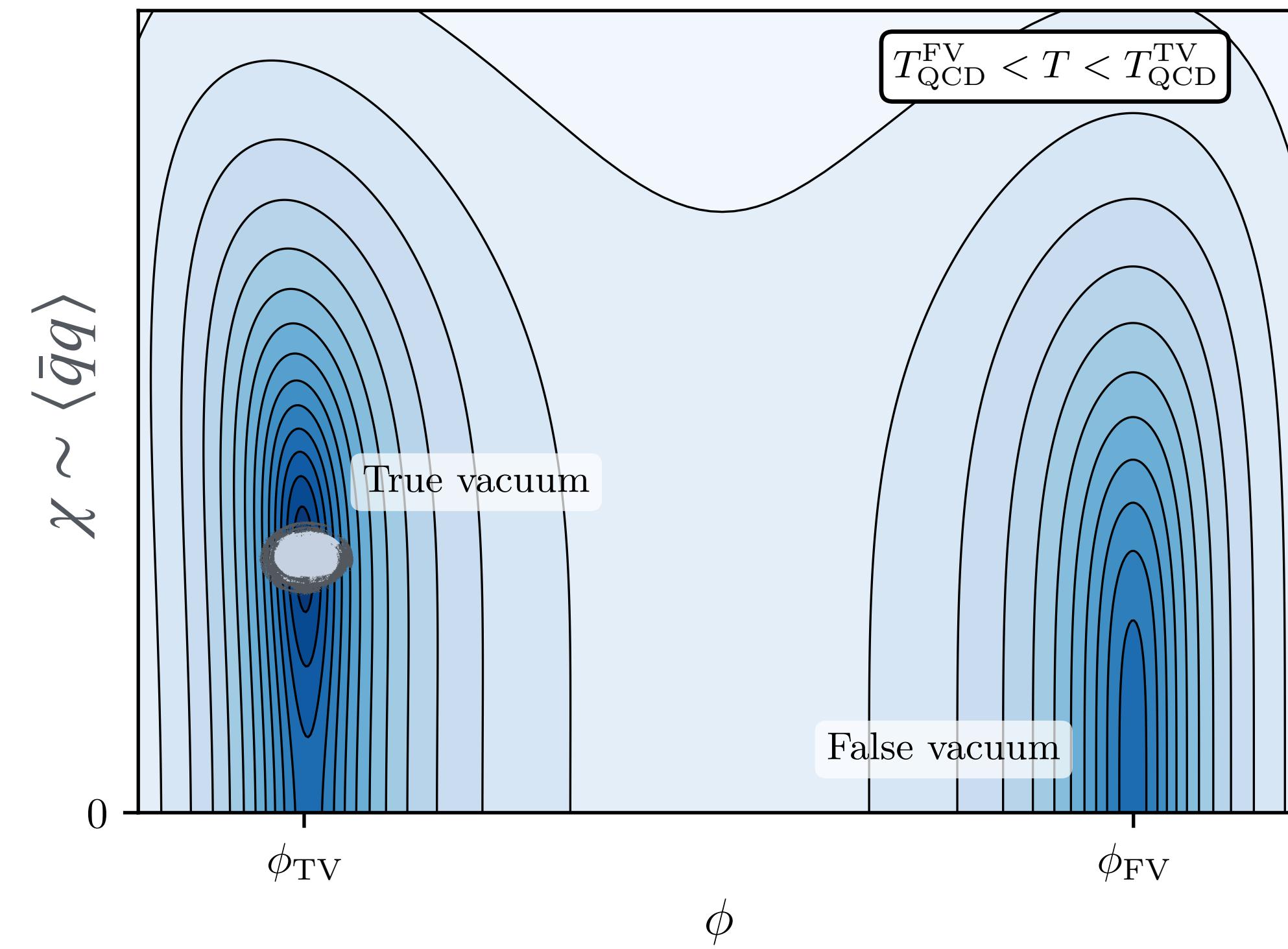


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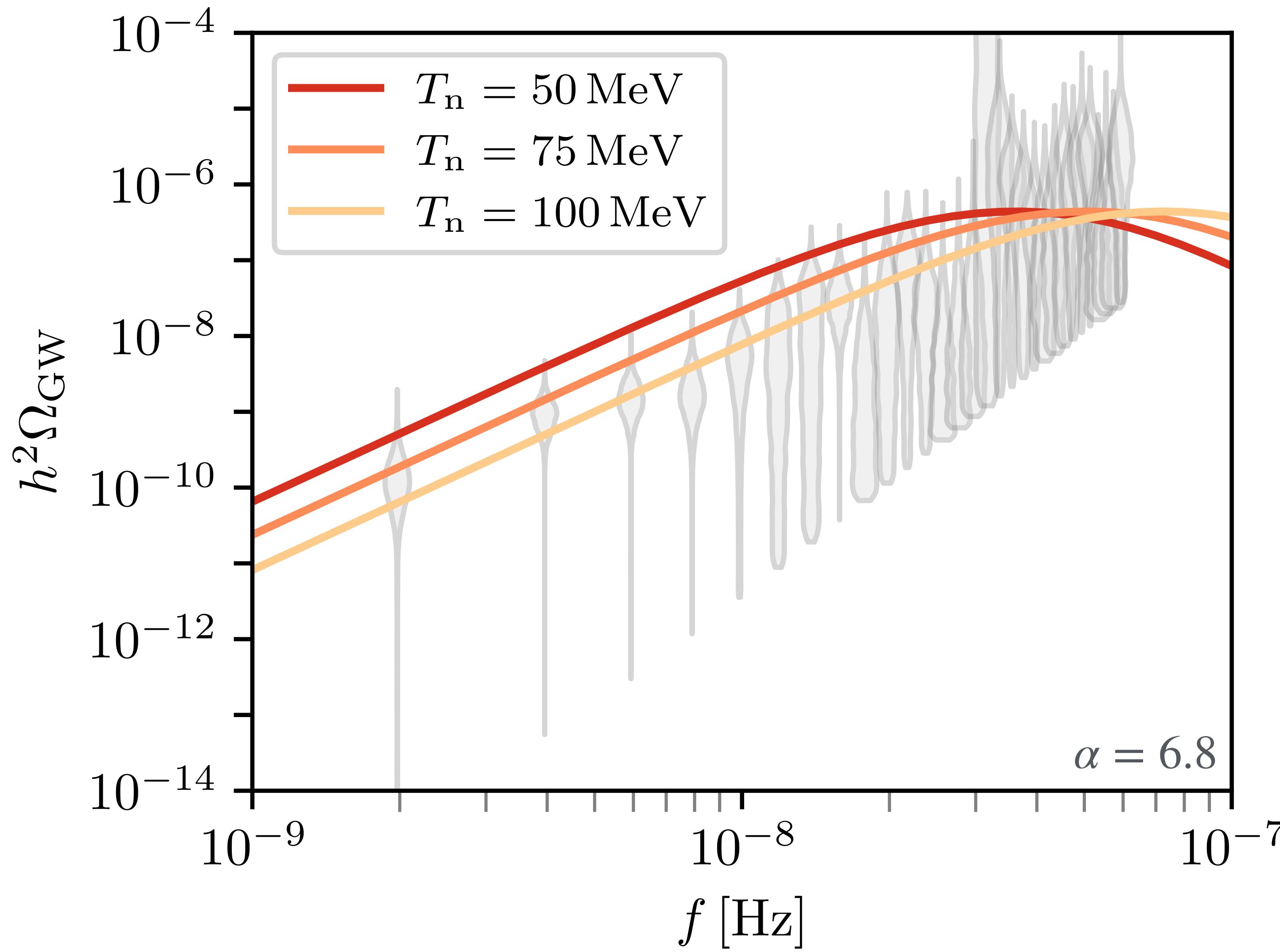
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# Gravitational Wave Spectrum



Bubble walls expand as detonations;  
QGP exerts pressure, but  
terminal velocity is relativistic.

Sound waves produce GWs.

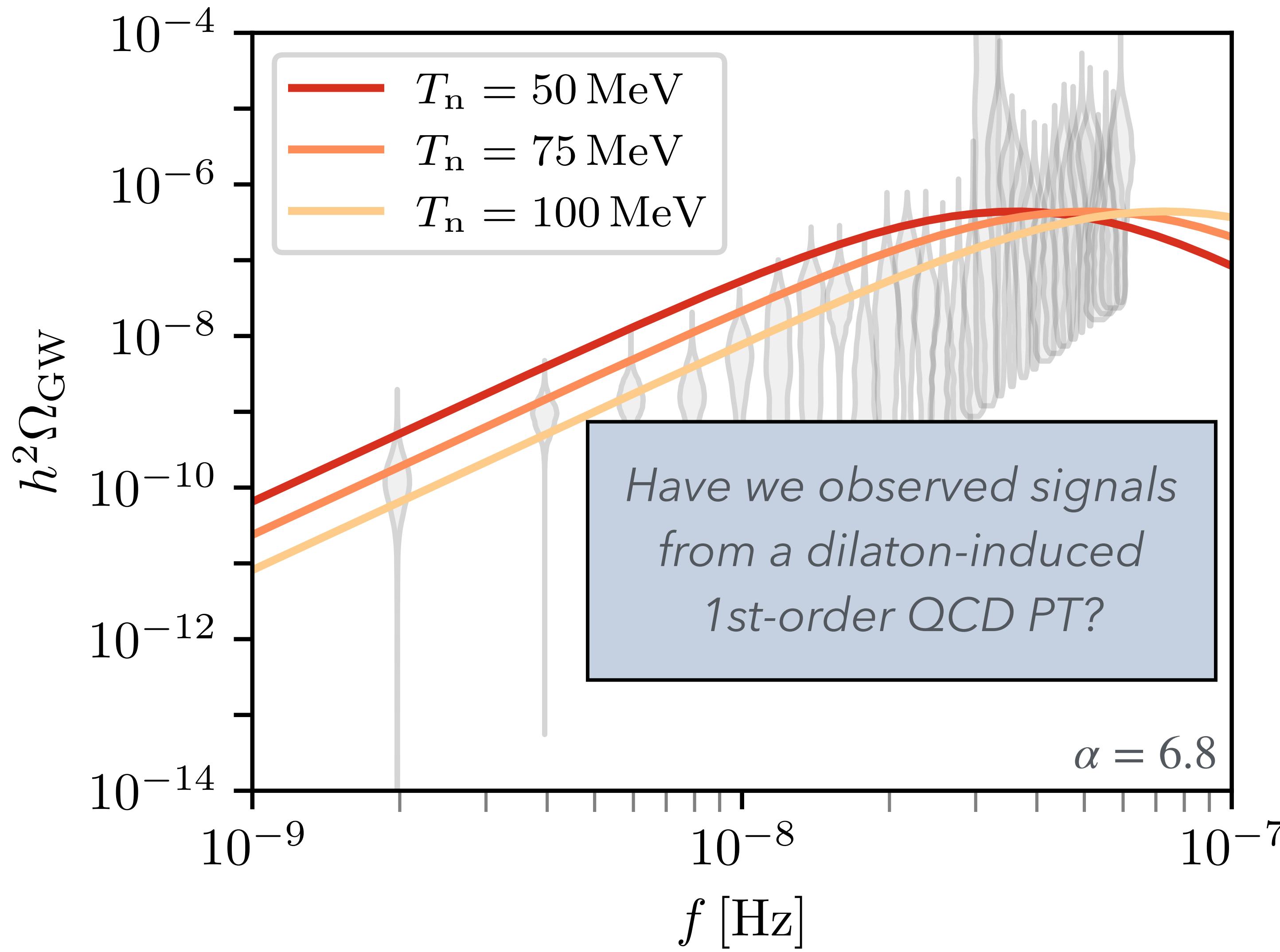
Curiously, the amplitude and spectrum  
match the nHz GW background reported  
by Pulsar Timing Arrays (PTAs).

Parameters:

$$0 < \alpha = \Delta V / \rho_{\text{rad}} \lesssim 20, 8 \geq \beta / H \geq 3$$

$$f_{\text{peak}} \simeq 17 \text{ nHz} \frac{\beta}{H} \frac{T_n}{100 \text{ MeV}}$$

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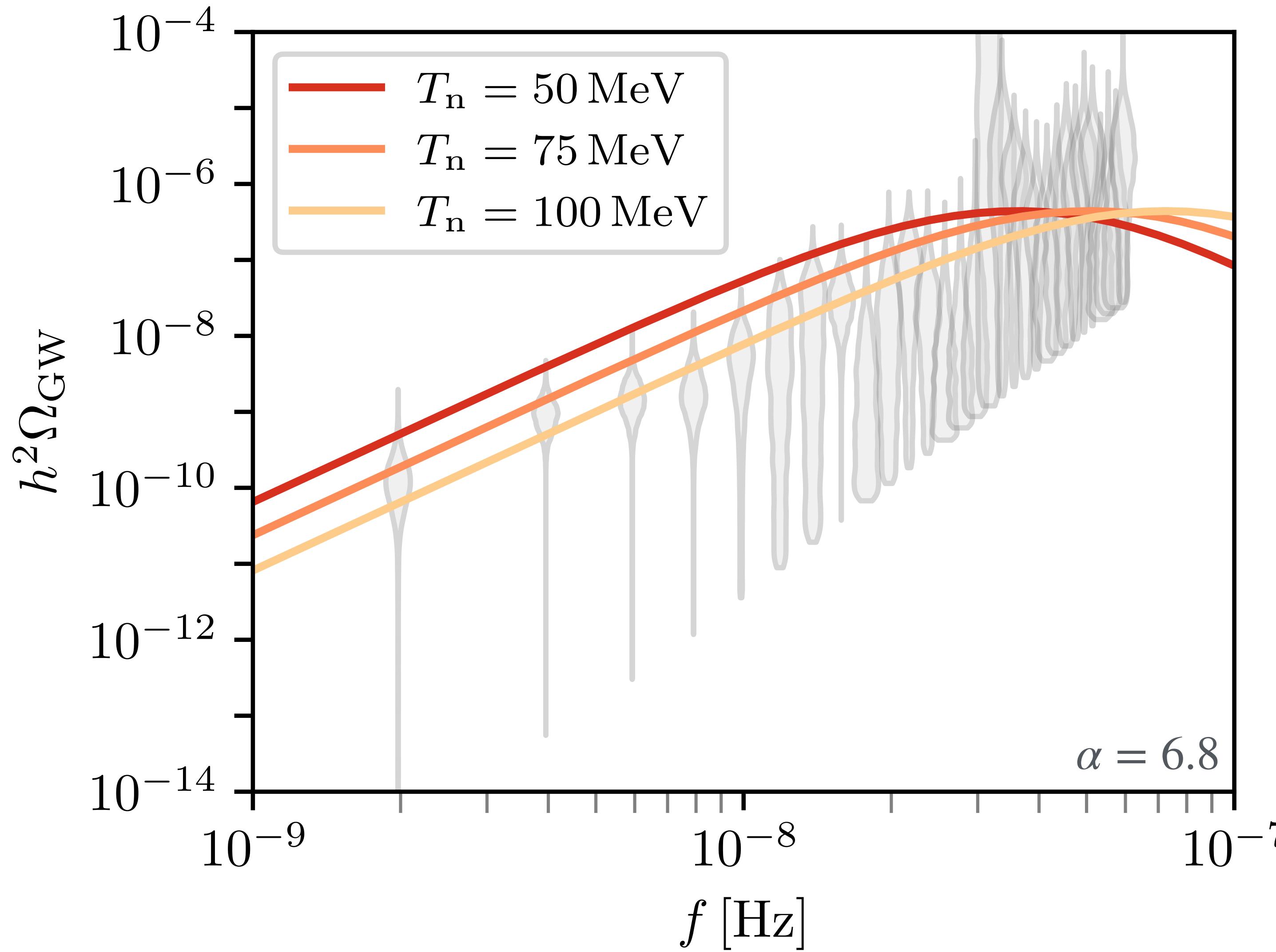
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# Gravitational Wave Spectrum



## Testable:

Dilaton is probed at colliders through dijet resonances.

Probed cosmologically through inhomogeneous BBN.

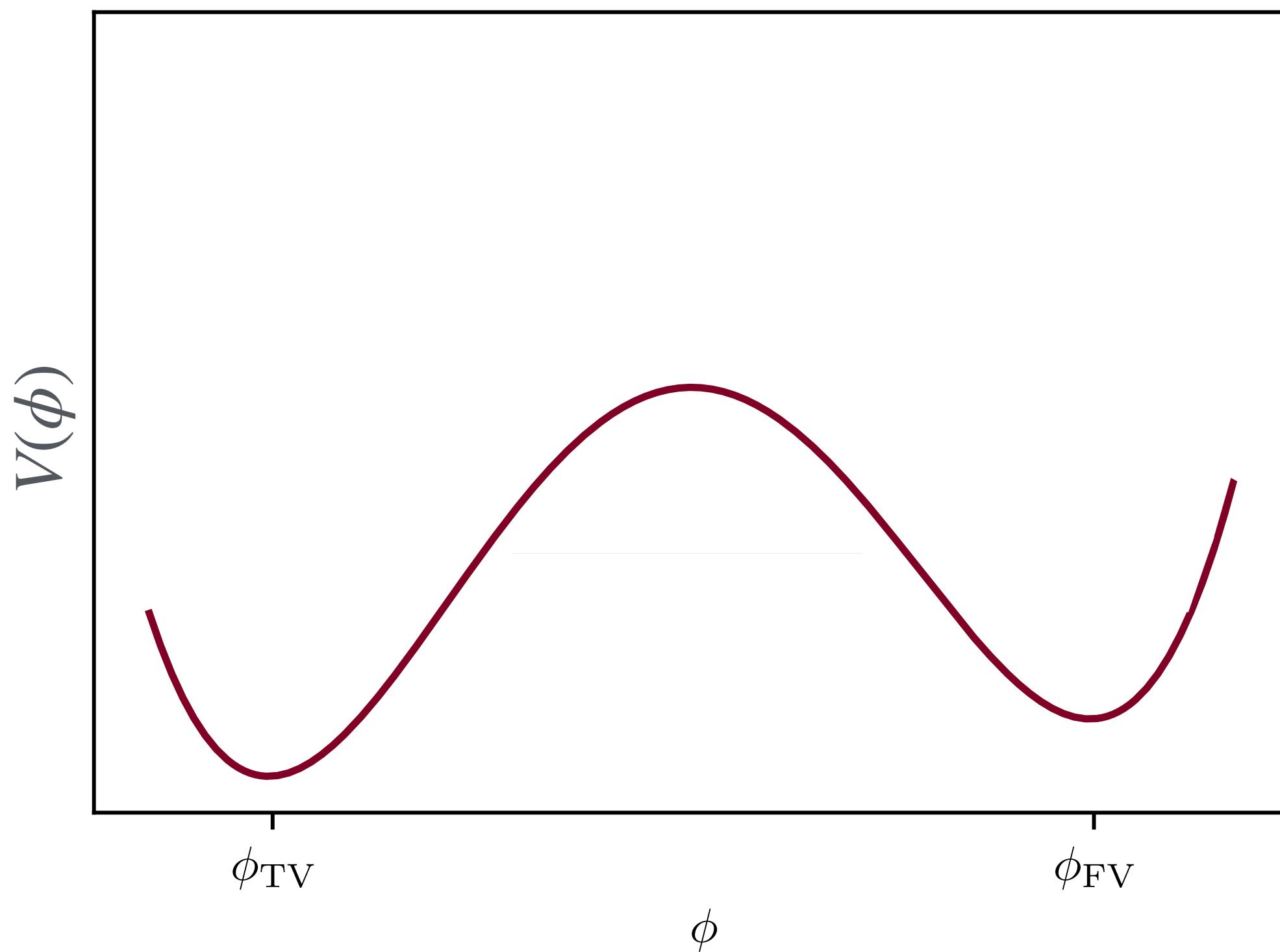
The GW signal should reach  $5\sigma$  with the upcoming IPTA DR3.

## Part II: dilatons and axions

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Hidden sector  
confining gauge theory

Initial seed density of  
axions present (e.g. from  
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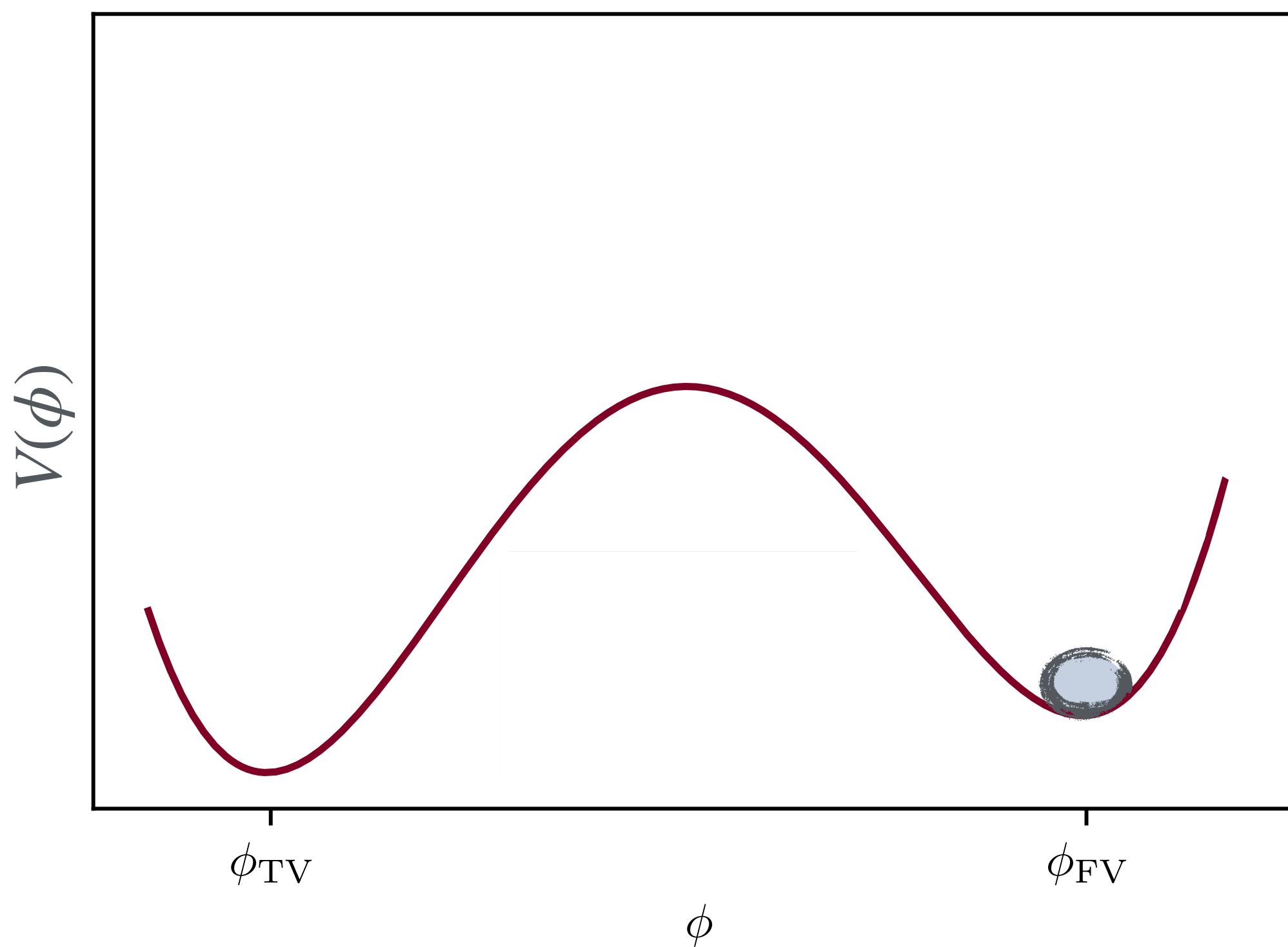


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The axion potential is exponentially sensitive to  $\phi$ .

$$V(\phi, a) = M^4 e^{-S(\phi)} \left( 1 - \cos \left( \frac{a}{f_a} \right) \right)$$

$$m_a^2 \Big|_{\text{TV}} = m_a^2 \Big|_{\text{FV}} \exp \left( S_{\text{FV}} \cdot \frac{|\Delta f|}{f_{\text{FV}}} \right)$$

Often  $\mathcal{O}(100 - 1000)$

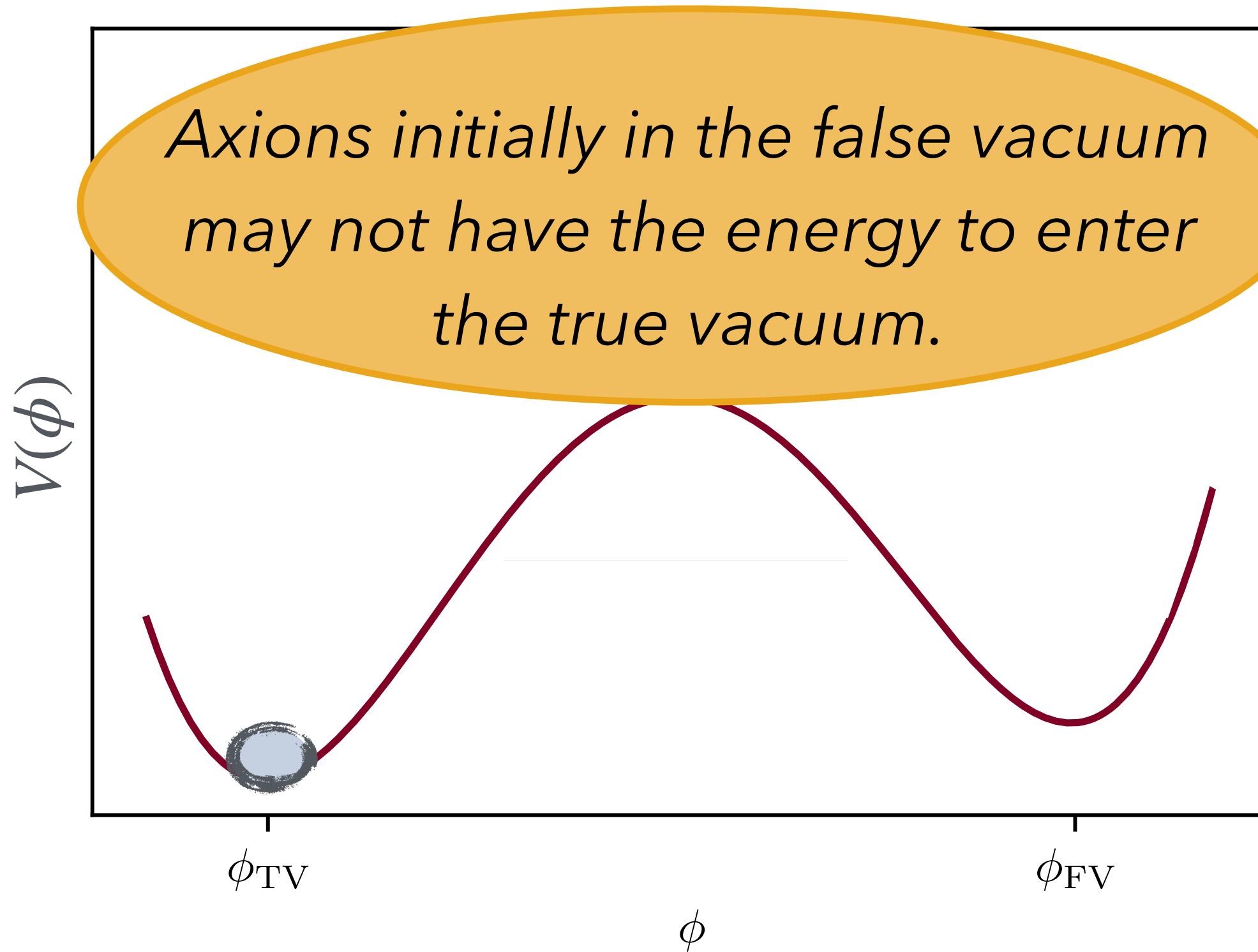
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Axions initially in the false vacuum  
may not have the energy to enter  
the true vacuum.



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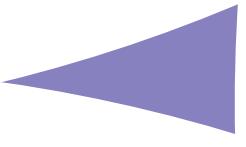
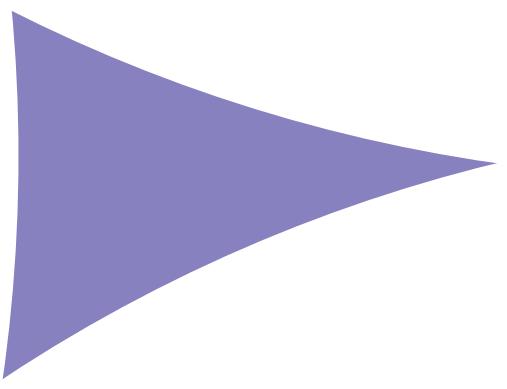
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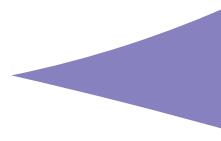
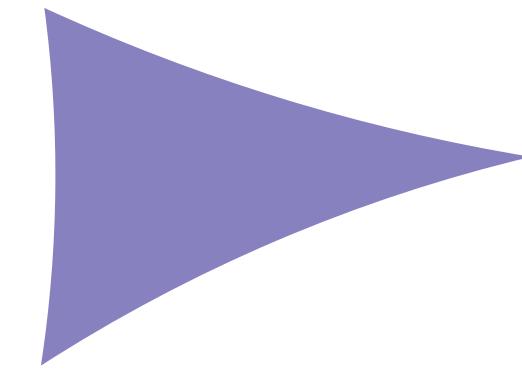
$$\phi_{\mathrm{FV}}$$

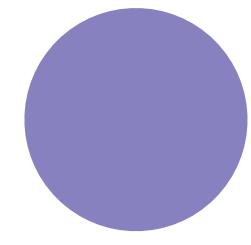
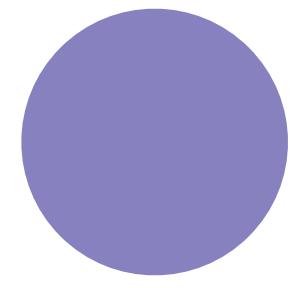
$$n_a \neq 0$$

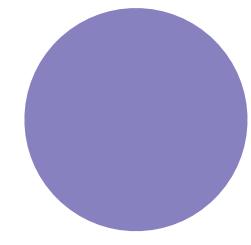
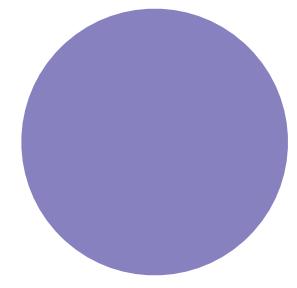
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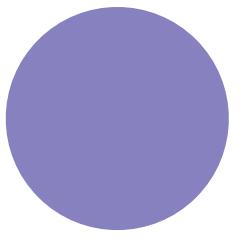


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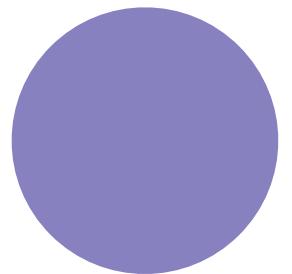


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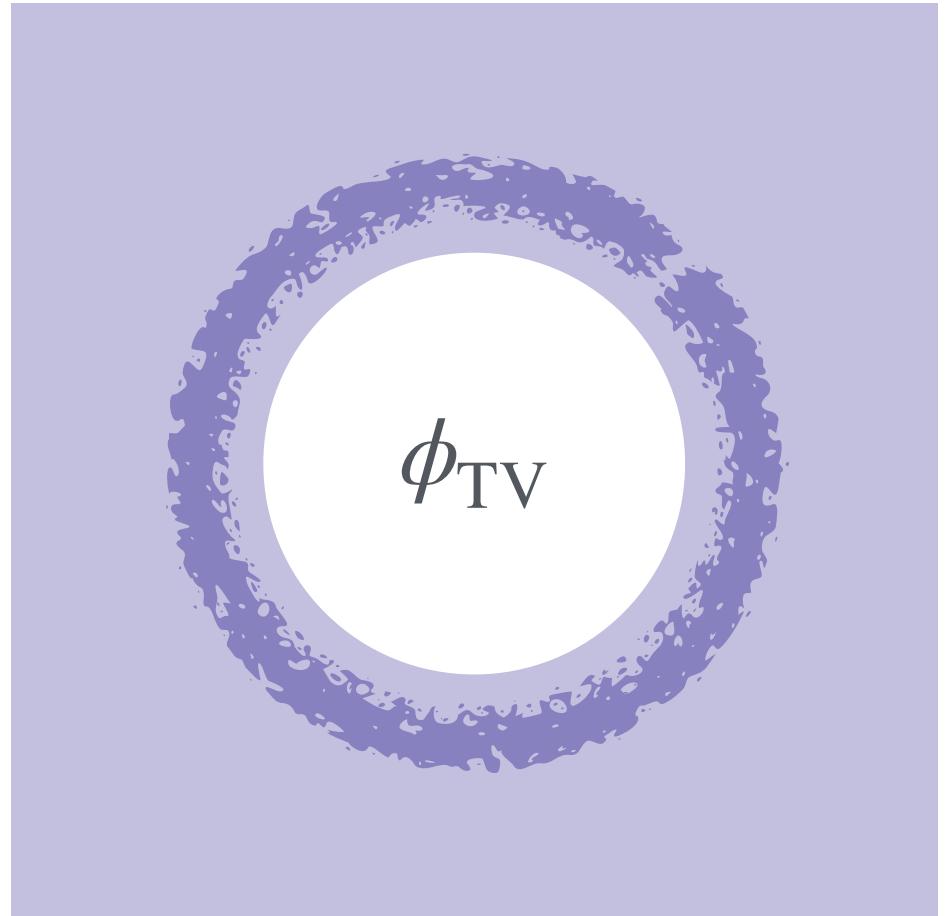
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Axion Relic Pockets



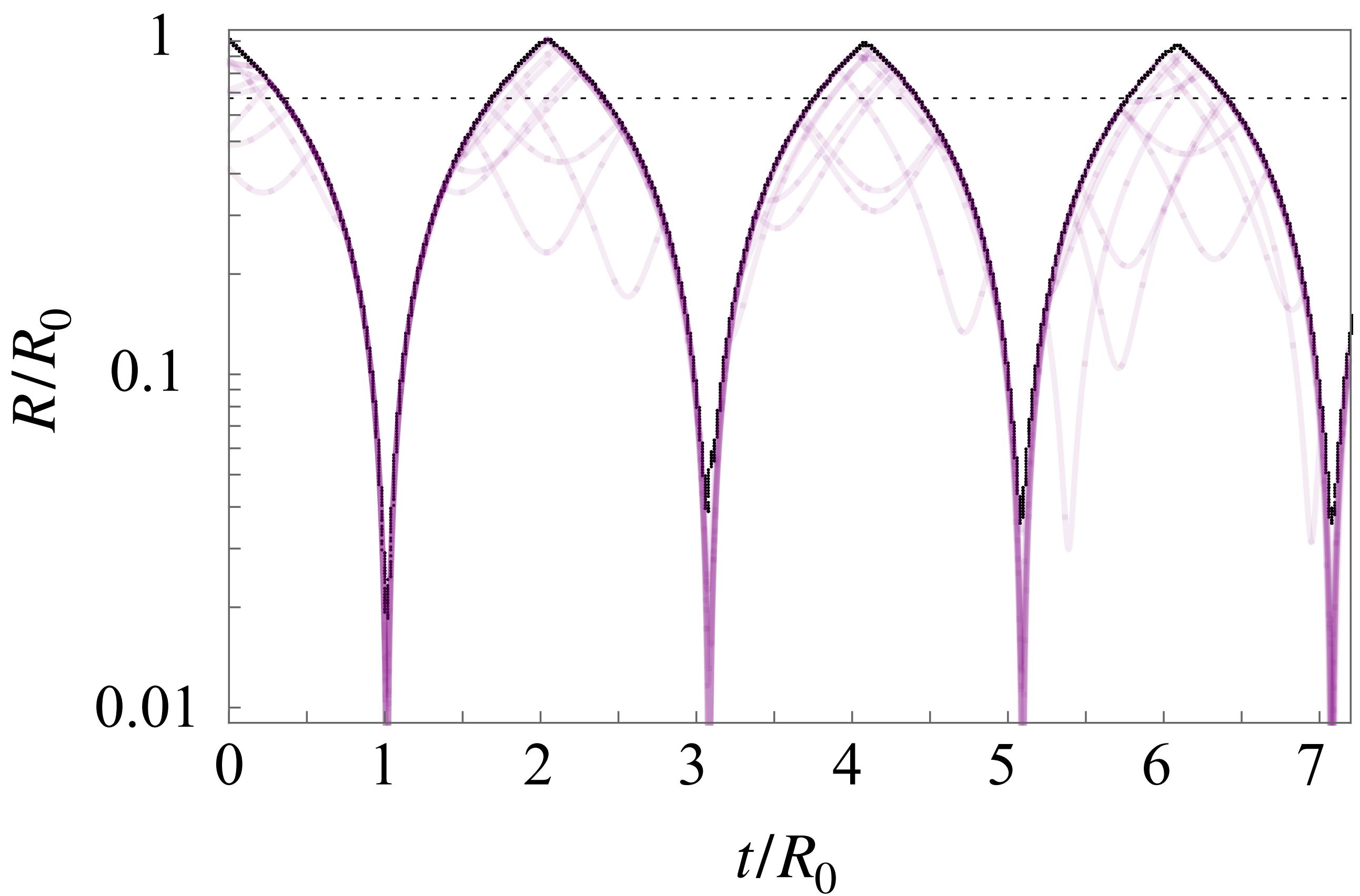
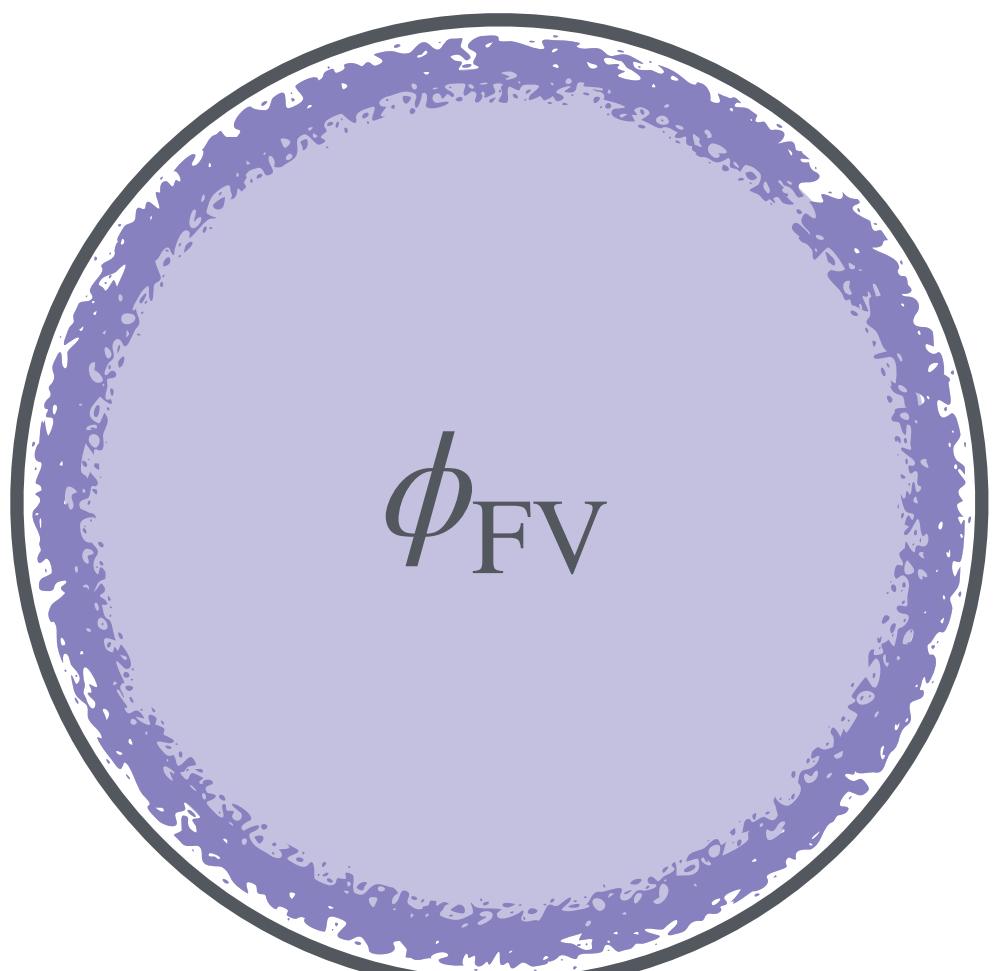
# Pressure from axions on wall

Initial axion pressure is negligible, but grows like  $\Delta p \sim \gamma_w^2$ .



Colliding bubbles are highly relativistic:  $\gamma_w \sim R_H/R_c$

N-body simulations of spherical pockets show that they pulsate with a period  $2R_0 \approx 2R_H$ .



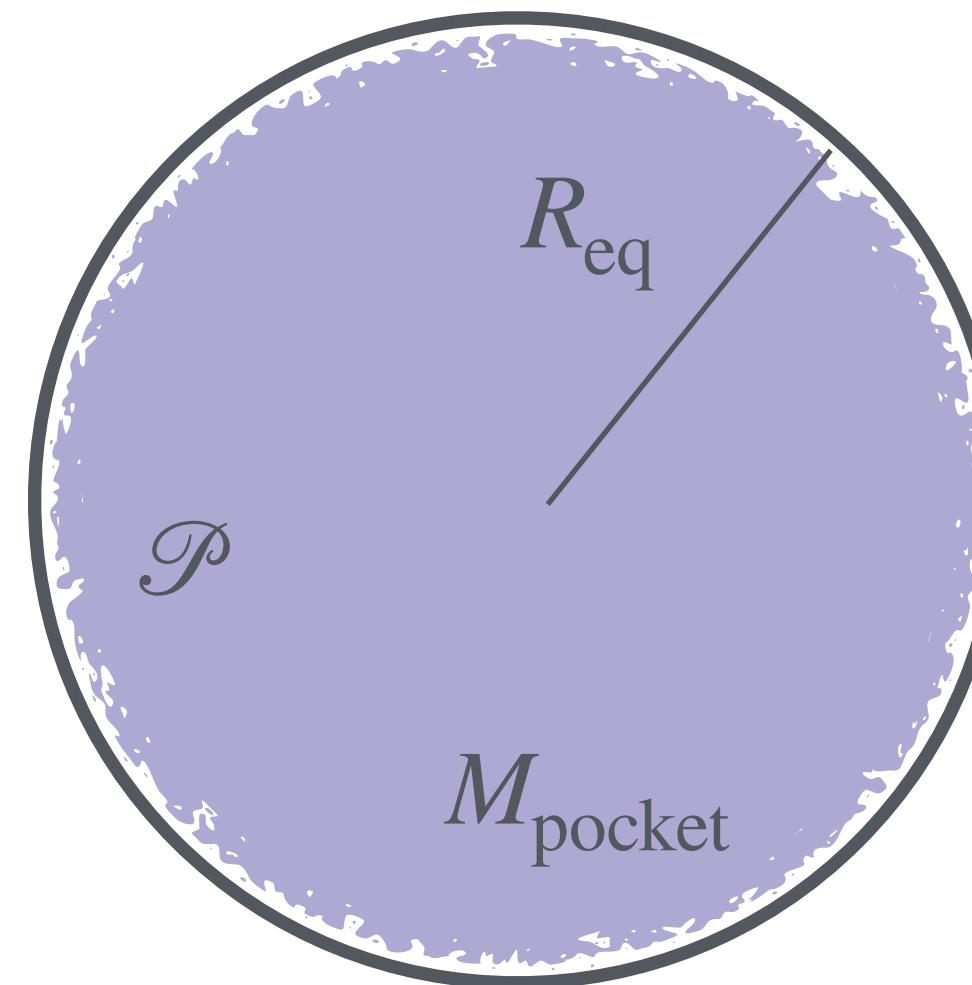
# Equilibrium properties

**Model independently:**

$$R_{\text{eq}} = \mathcal{O}(1) \times R_H$$

$$\mathcal{P} \approx \Delta V$$

$$M_{\text{pocket}} \approx (\Delta V + 3\mathcal{P}) \text{ Vol}_{\text{eq}}$$



**Axion gas temperature** (thermal):

$$T_{\text{eq}} \sim 5 \text{ GeV} \left( \frac{T_t}{\text{TeV}} \right)^{3/4}$$

If gas *thermalises*, all properties become independent of initial axion abundance.

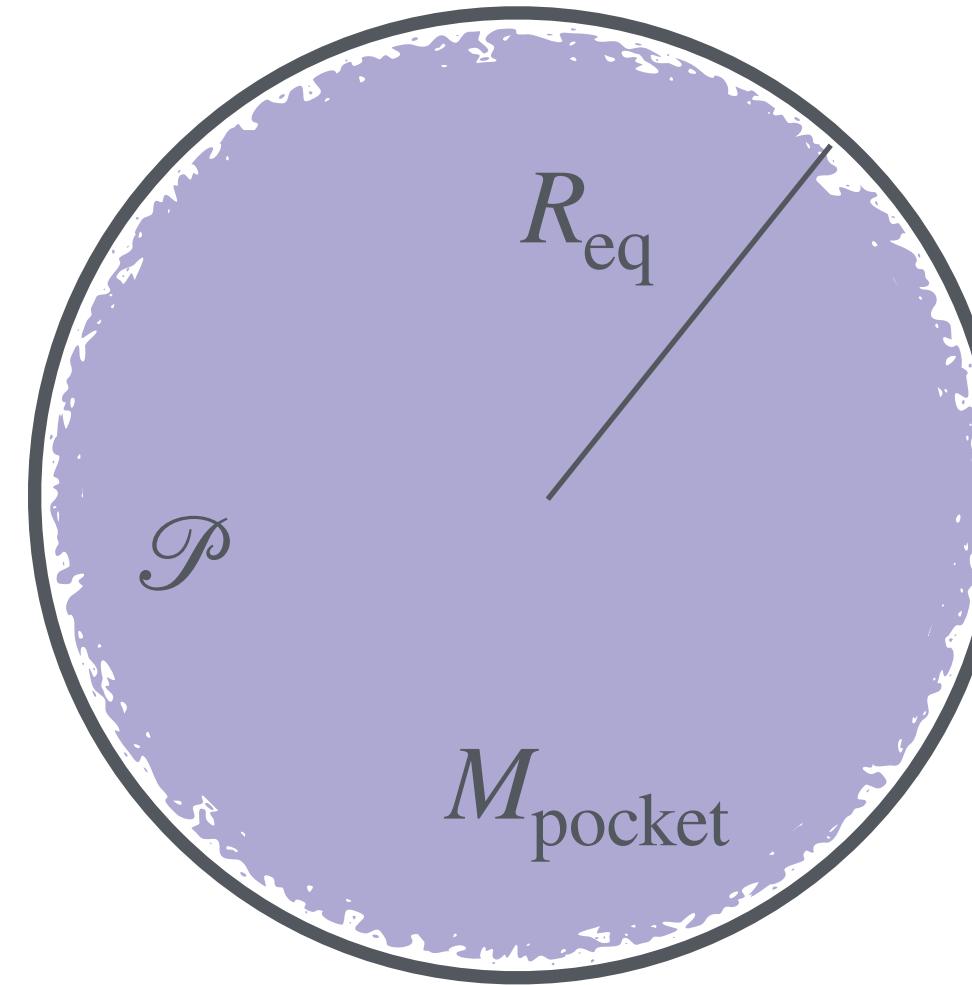
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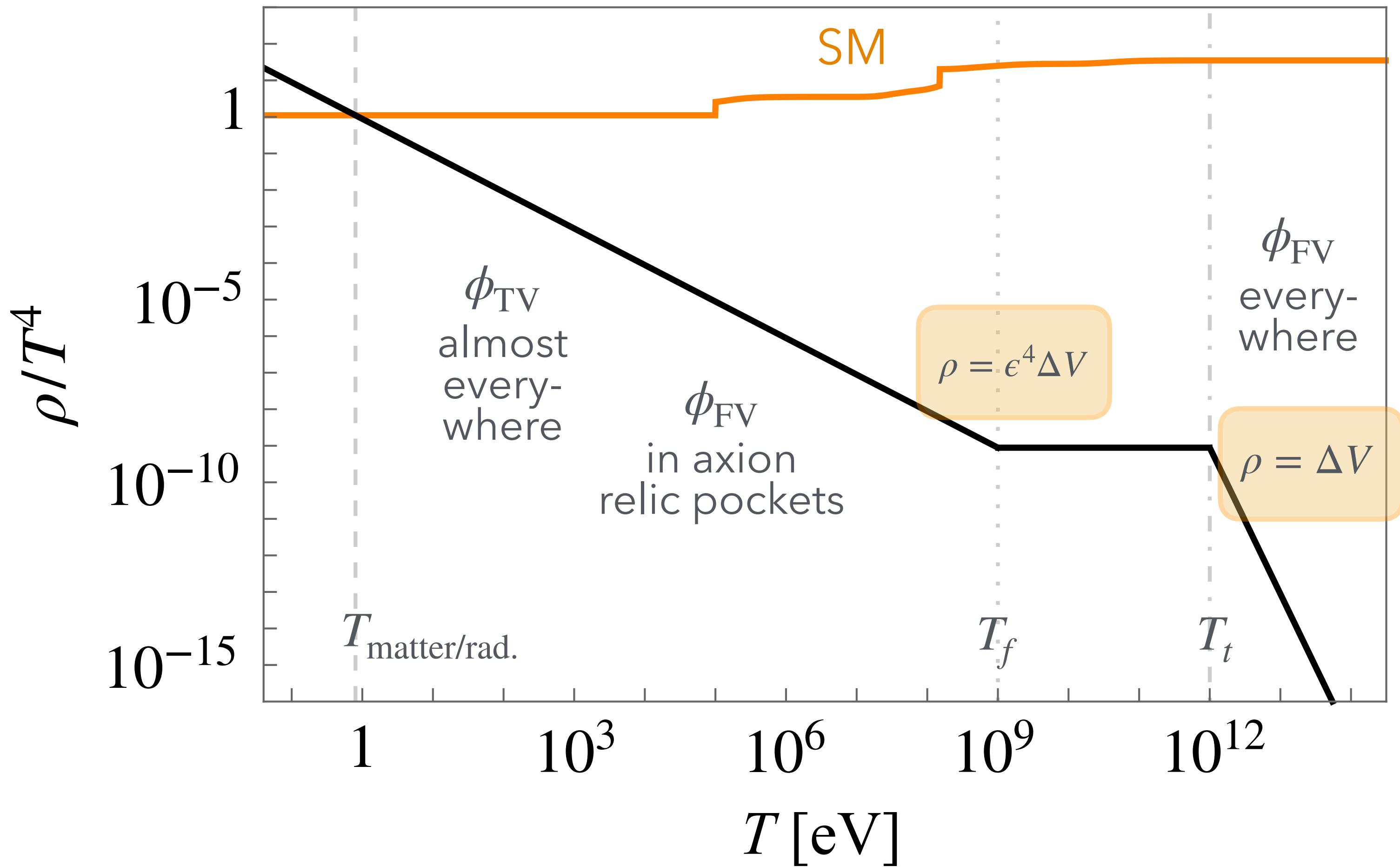


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# Axion Relic Pocket Cosmology



The pockets can (rather easily) be cosmologically stable.

Axion relic pockets can comprise all of dark matter.

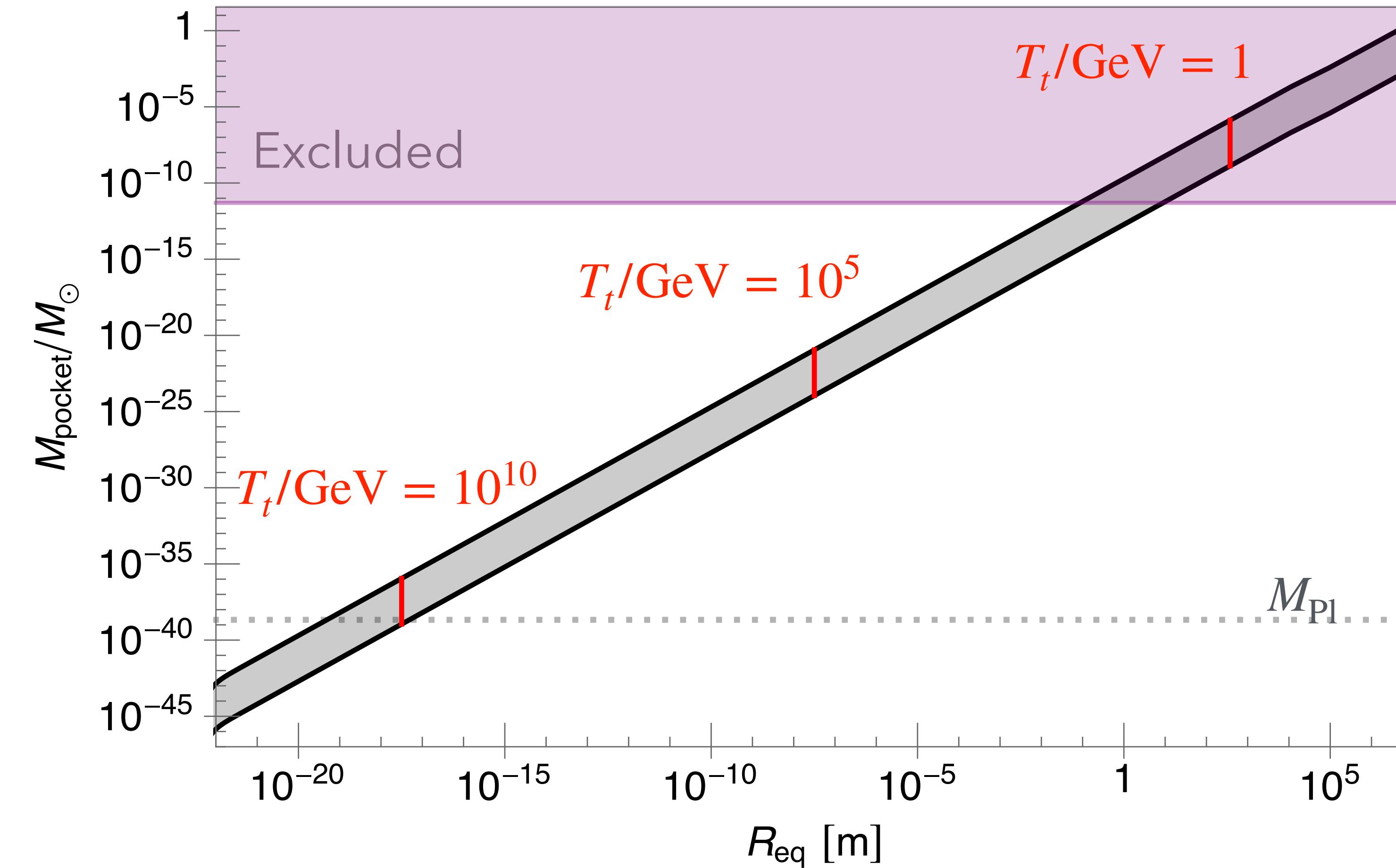
$$\left. \Delta V \right|_{\text{DM}} \simeq 20 \text{ GeV}^4 \epsilon^{-4} \left( \frac{T_t}{\text{TeV}} \right)^3$$

Transition must (naively) happen between inflation and matter/rad. equality:

$$1 \text{ eV} \lesssim T_t \lesssim 10^{16} \text{ GeV}$$

# Mass v. Radius

Single-parameter solution, but with a broad range.



A priori, radius may run from point-like to galactic.

Microlensing constraints:  $T_t \gtrsim 13 \text{ GeV}$ .

Viable range:

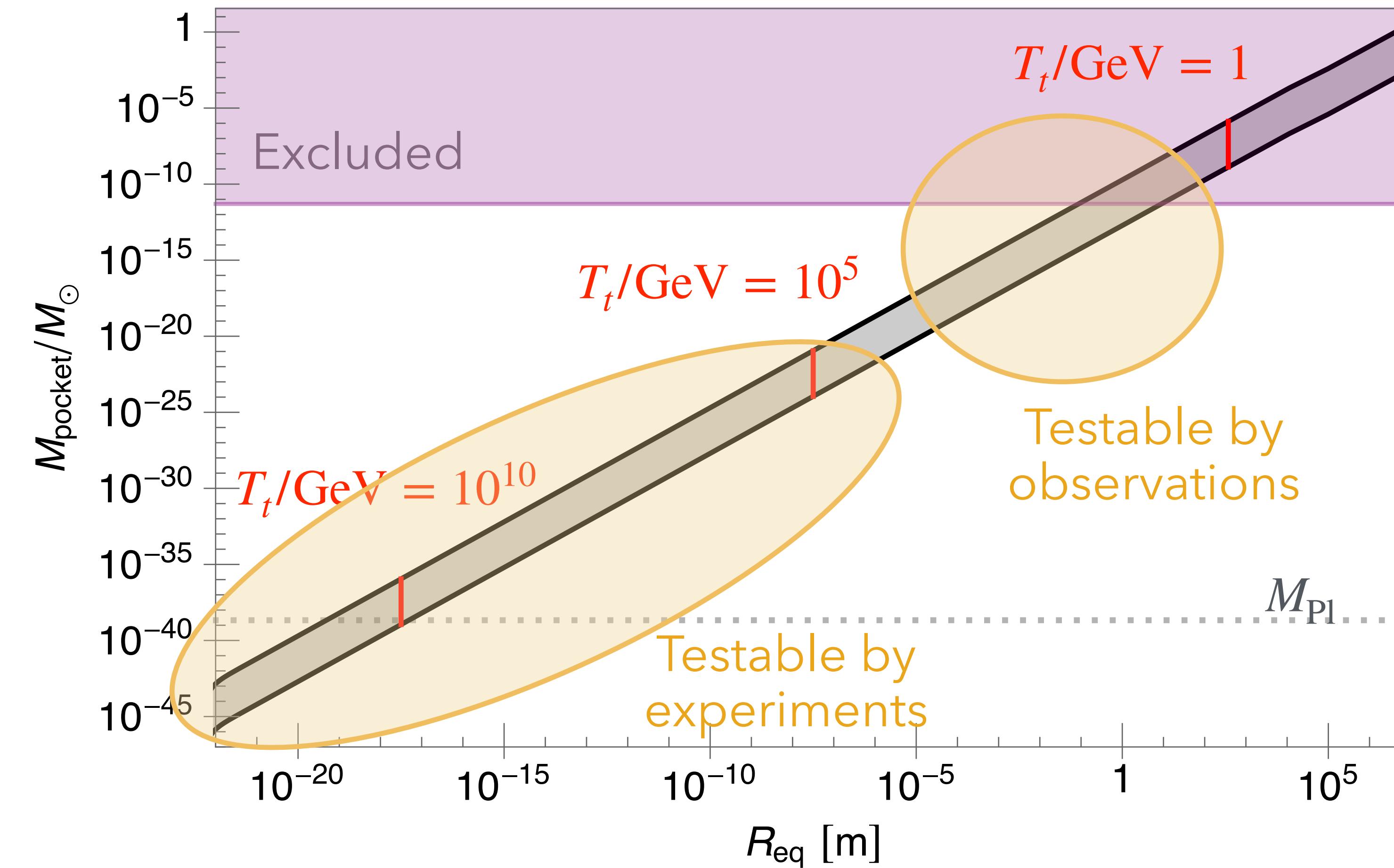
$$10^{10} \text{ GeV} < M_{\text{pocket}} \lesssim 5 \cdot 10^{-12} M_{\odot}$$

$$10^{-25} \text{ m} \lesssim R_{\text{pocket}} \lesssim 20 \text{ cm}$$

$$10^{10} \text{ GeV} \gtrsim T_{\text{eq}} \gtrsim 5 \text{ GeV}$$

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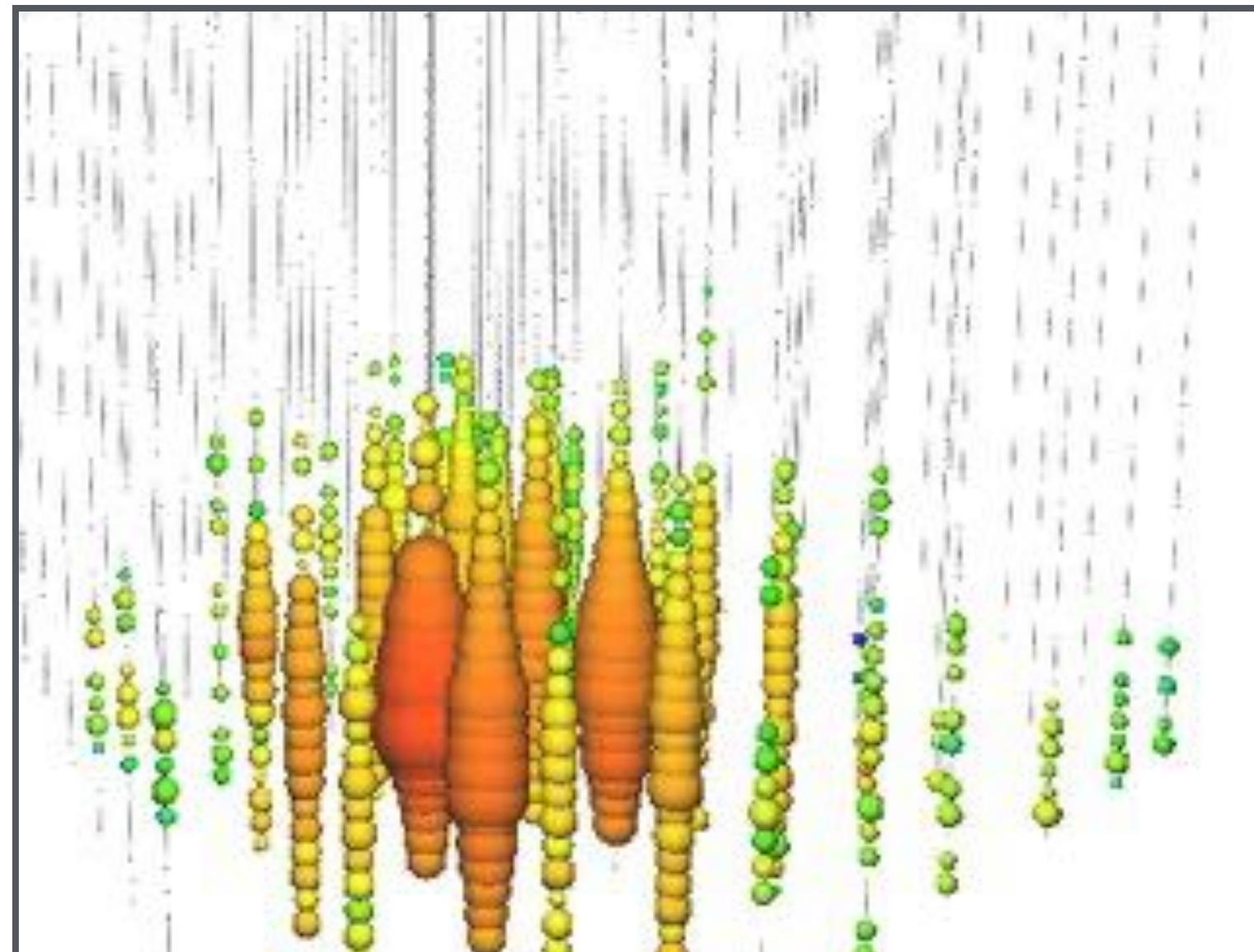
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# Terrestrial Axion Relic Pockets searches

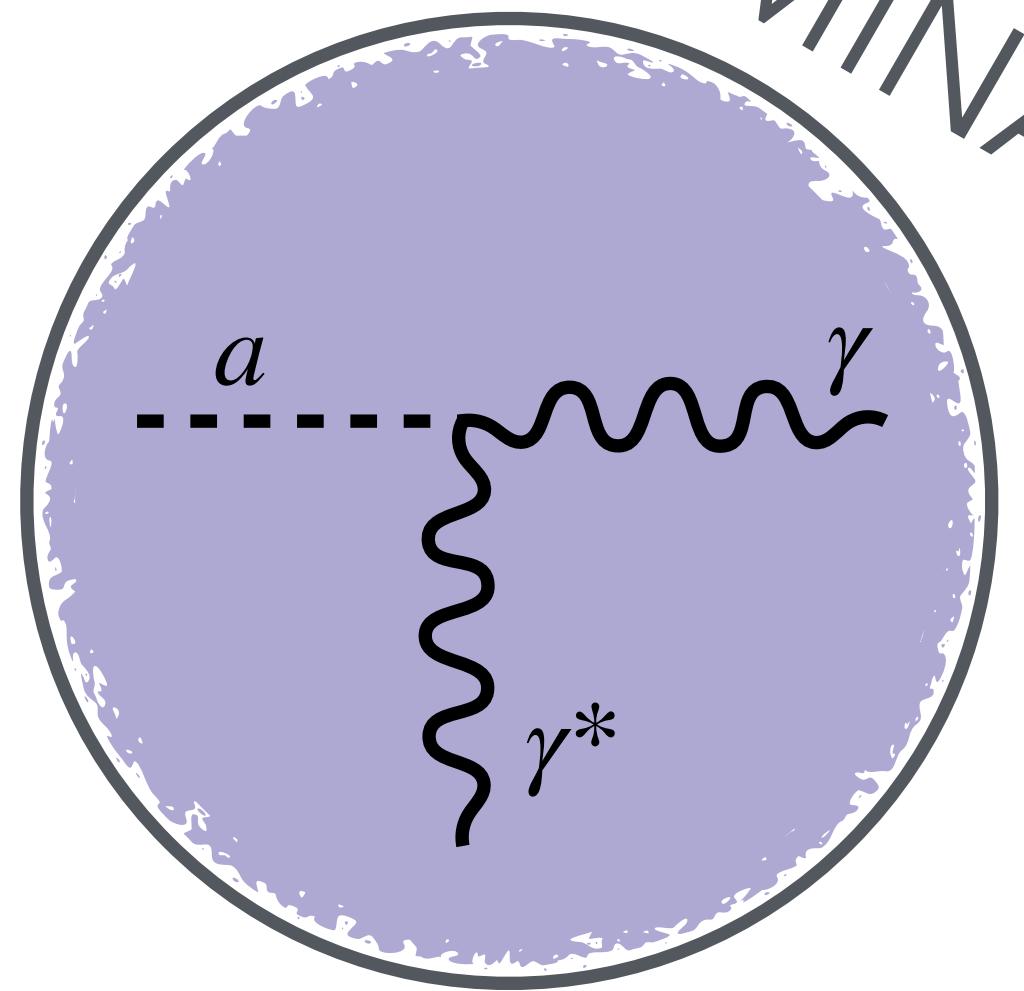
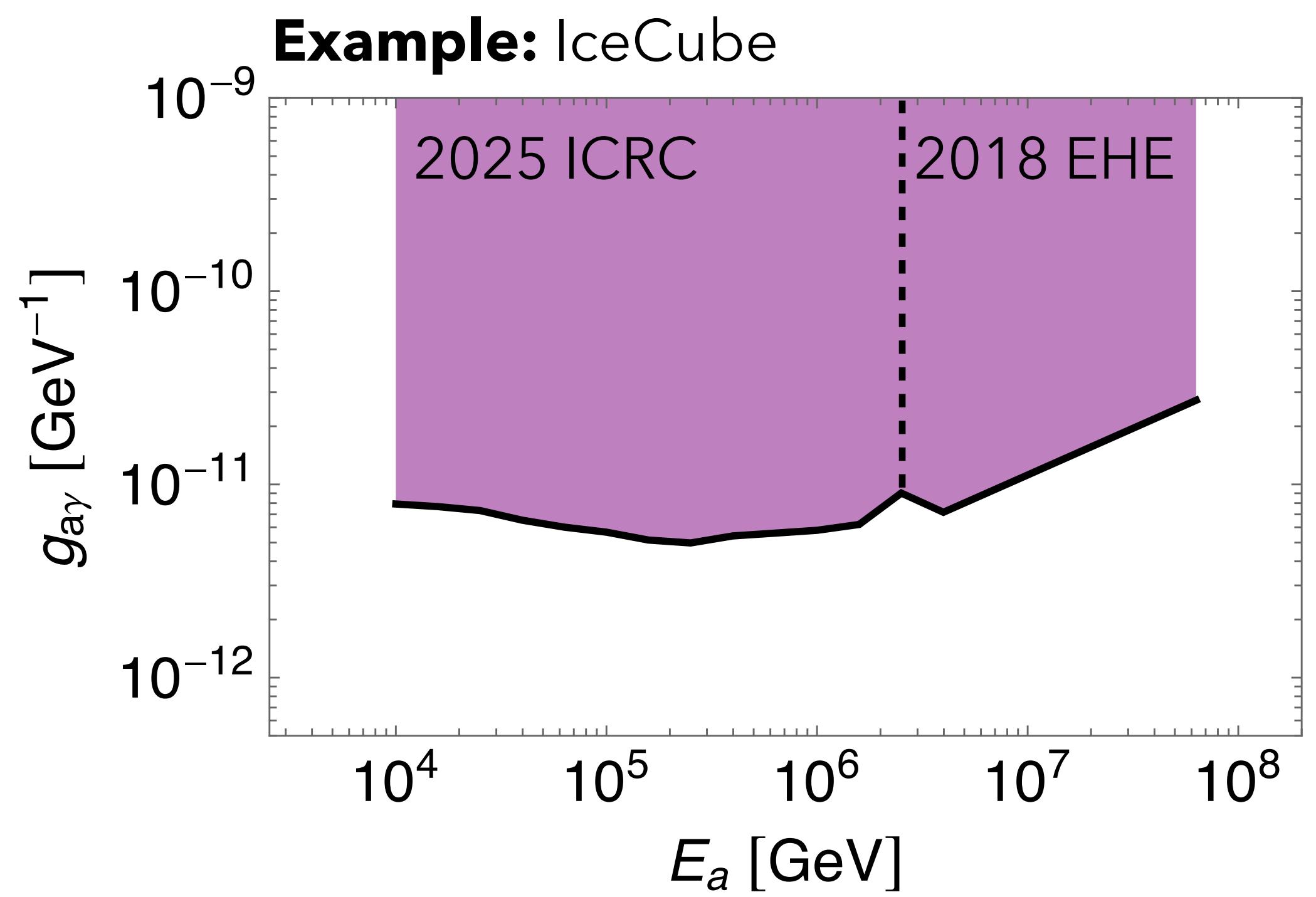
Event rate (single-axion processes):

$$\dot{N}_{\text{event}} = \frac{3}{4} \frac{\sigma}{E_a} \rho_{\text{DM}} N_{\text{target}}$$



**Smoking gun:** high-energy upward-going cascades.

# targets (e.g. atoms)  
in detector



PRELIMINARY

# Summary

**Dilatons and axions** are both highly motivated by high-energy physics.

Cosmic dilaton phase transitions can lead to:

- **1st order QCD PT:** with GW signals curiously close to those reported by PTAs.
- **Axion relic pockets:** a dark matter theory with phenomenology distinct from existing paradigms.

*Thanks for your attention!*



Extra slides



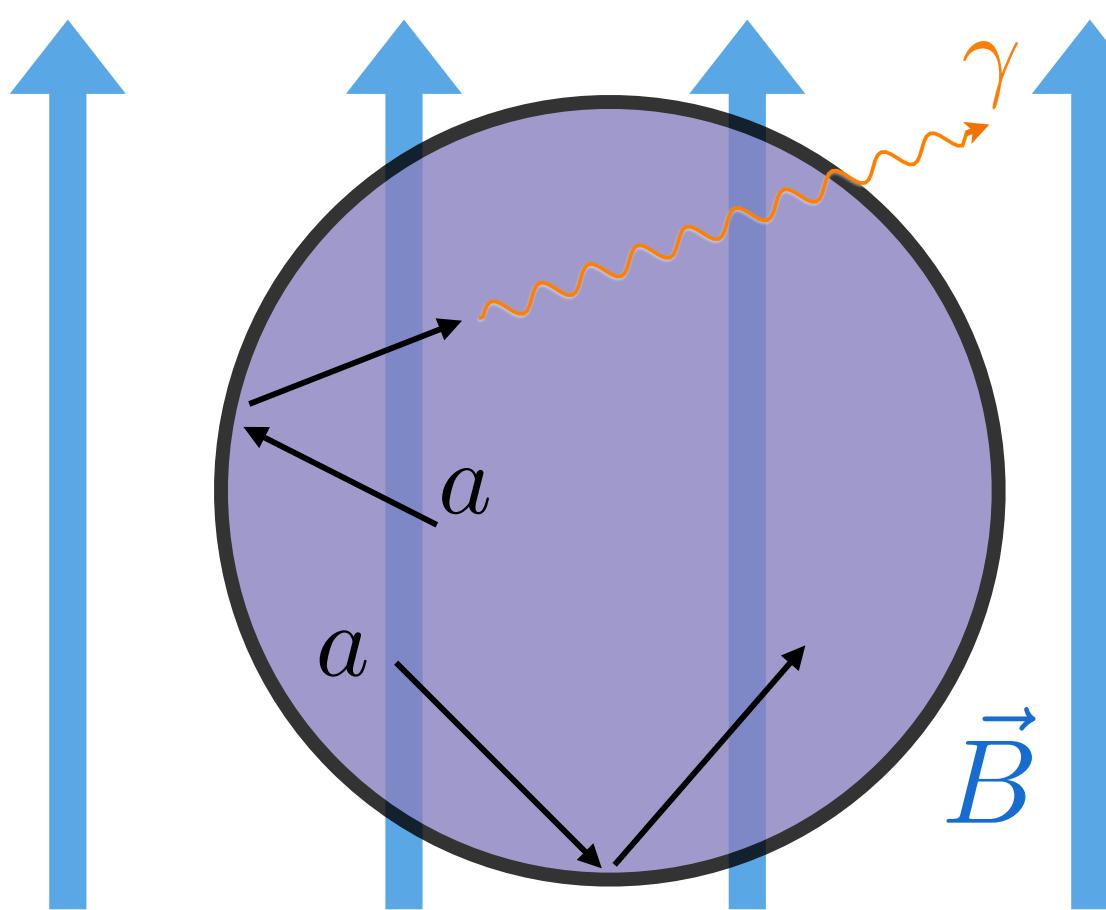
# Pocket stability

Since  $R_{\text{eq}} \gg R_c$ , bubble formation doesn't stop. However, TV bubbles collapse due to gas pressure.

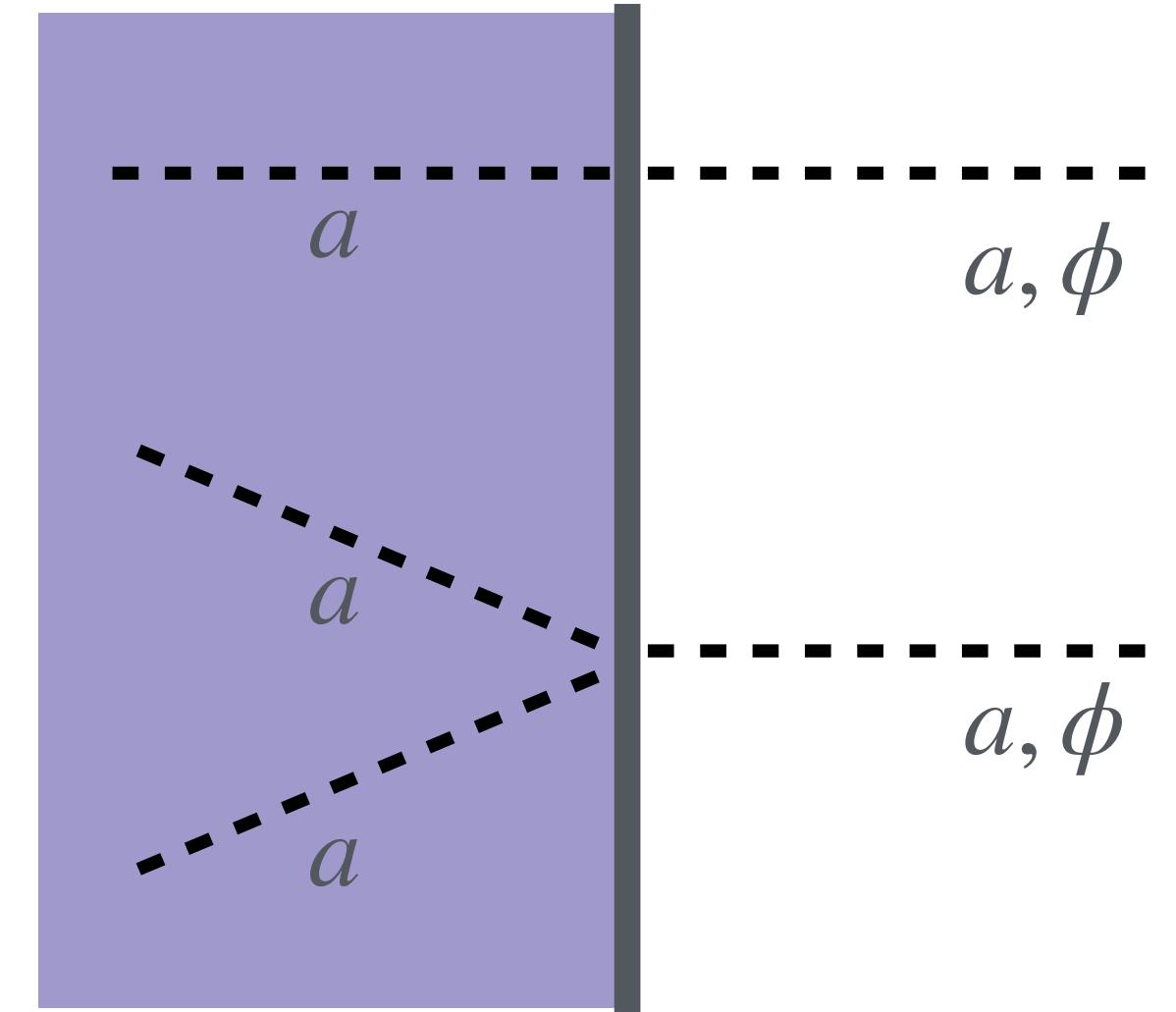
Too dilute to collapse into black holes.

Lewicki++ 2022

If  $m_a|_{\text{TV}}$  and  $m_\phi|_{\text{TV}}$  are sufficiently large ( $\gg T_{\text{eq}}$ ), then axions can't escape by scattering through wall.



Interactions with Standard Model typically harmless for stability, but can give interesting signals.



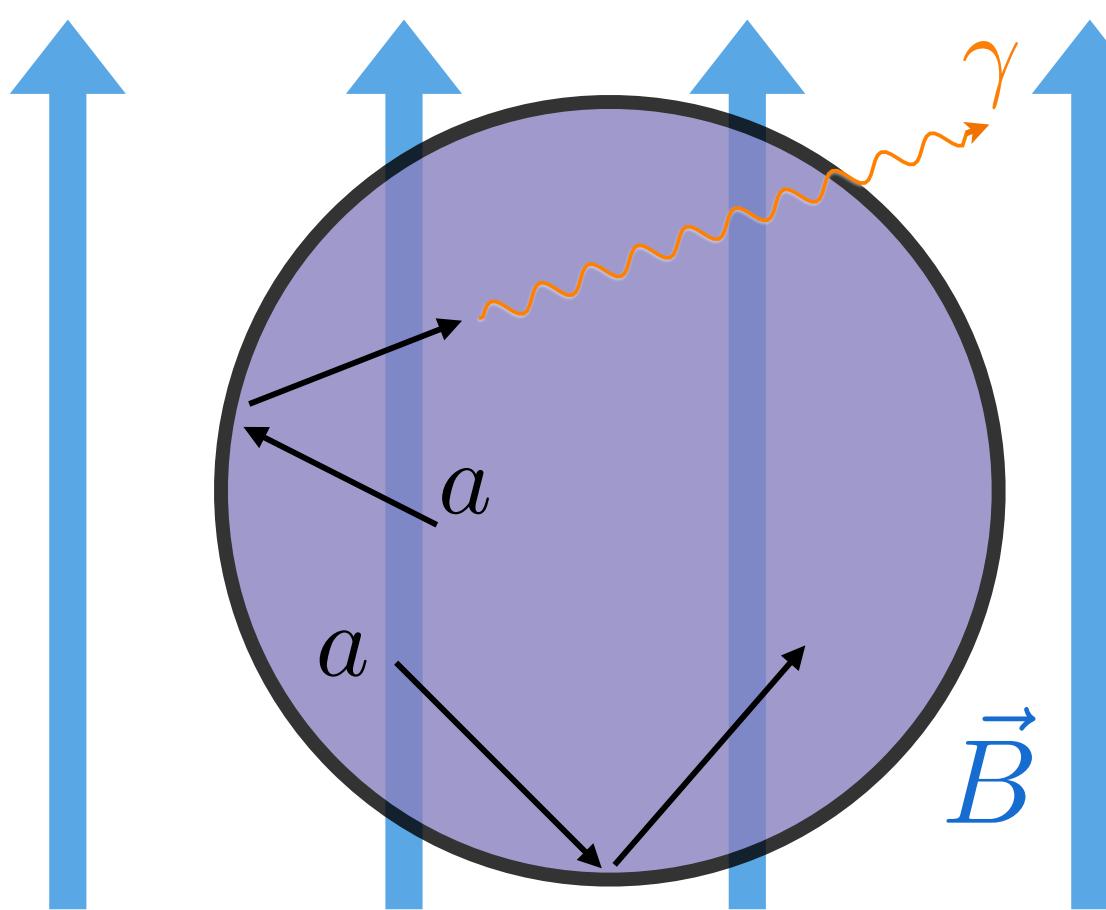
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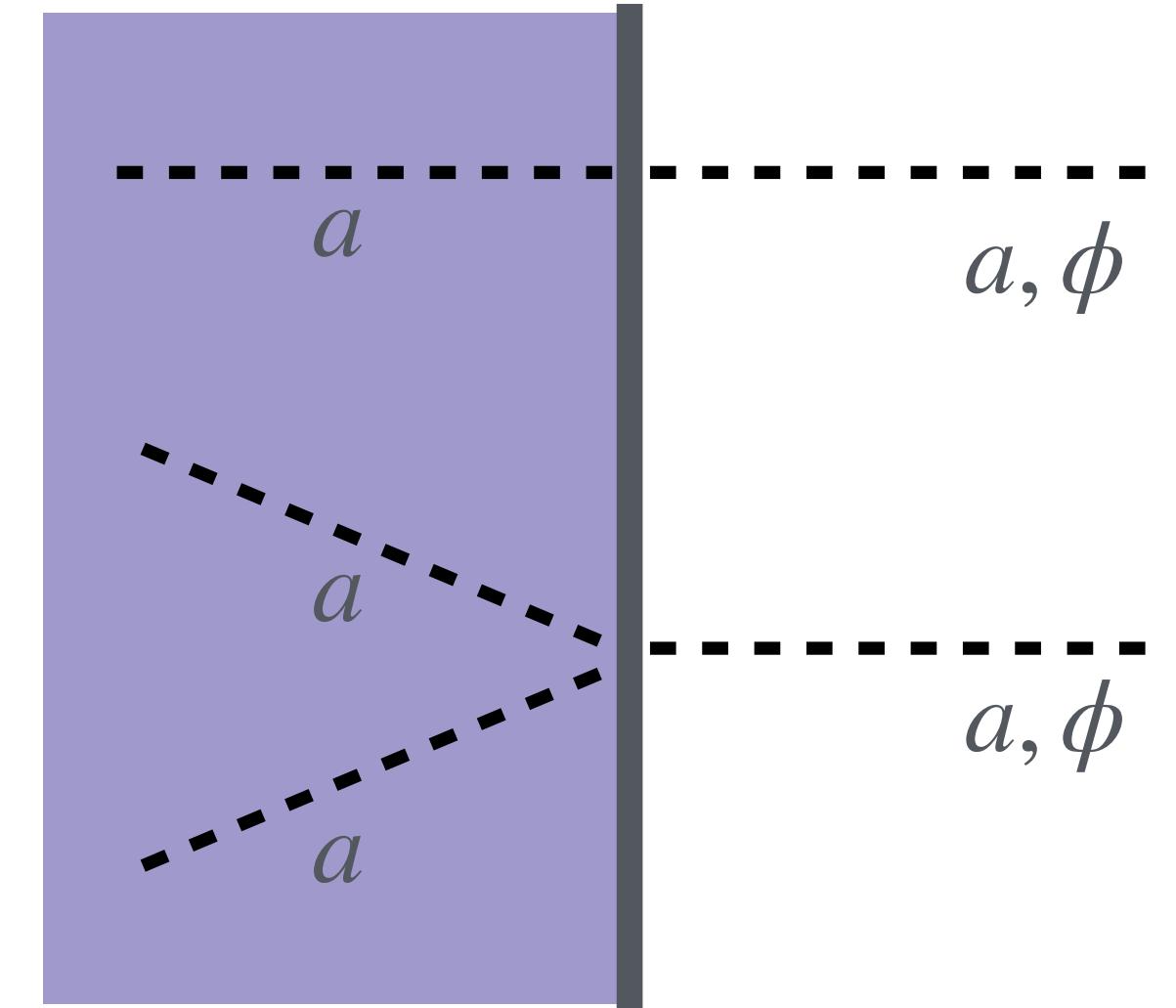
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# Equilibrium properties

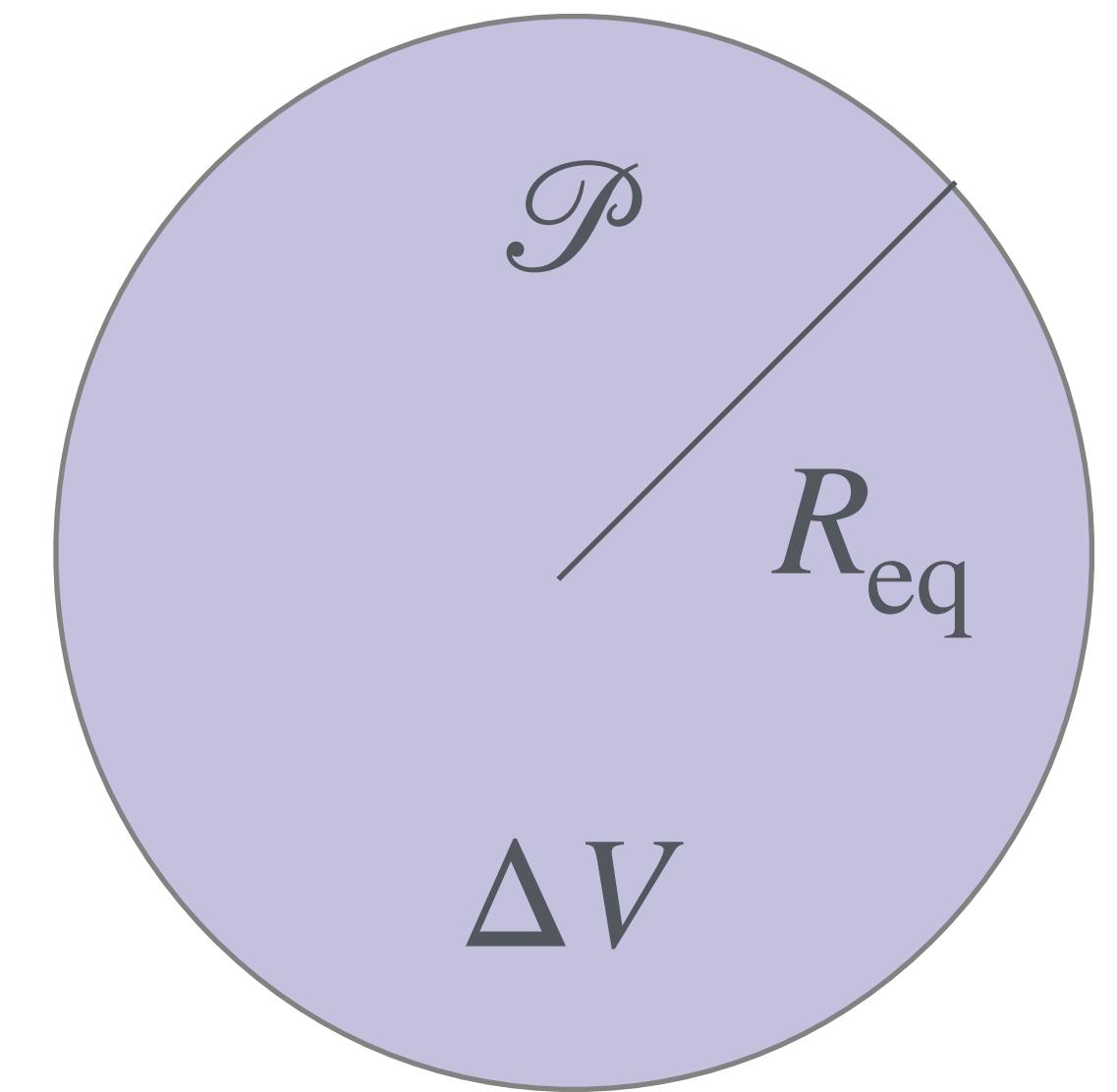
$$\dot{R} = \ddot{R} = 0$$

Spherical EoM:

$$\ddot{R} + \frac{2(1 - \dot{R}^2)}{R} = -\frac{3(1 - \dot{R}^2)^{3/2}}{R_c} \left( 1 - \frac{\mathcal{P}}{\Delta V} \right)$$

Equilibrium radius:

$$R_{\text{eq}} = \frac{2}{3} \frac{R_c}{\mathcal{P}/\Delta V - 1}$$



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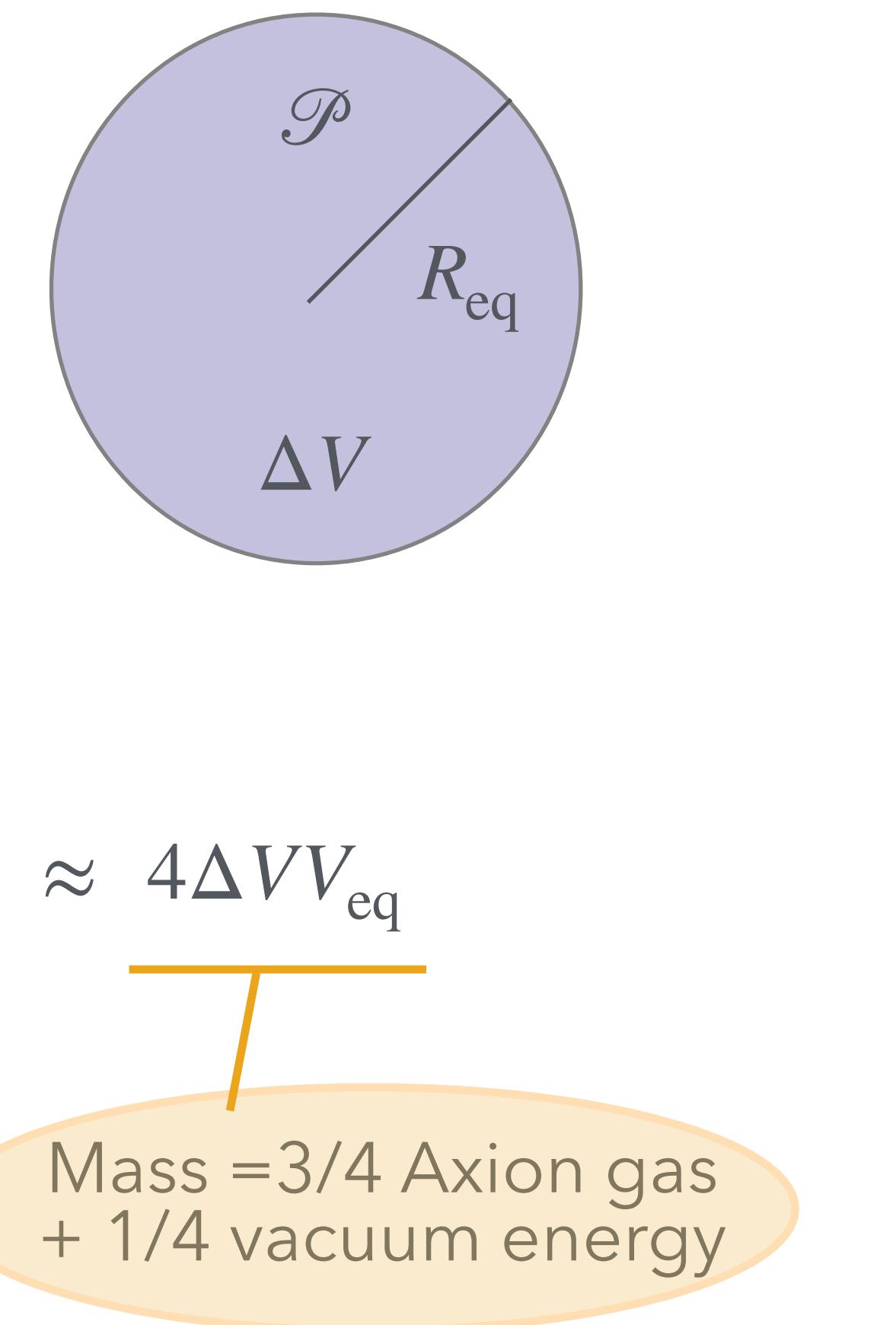
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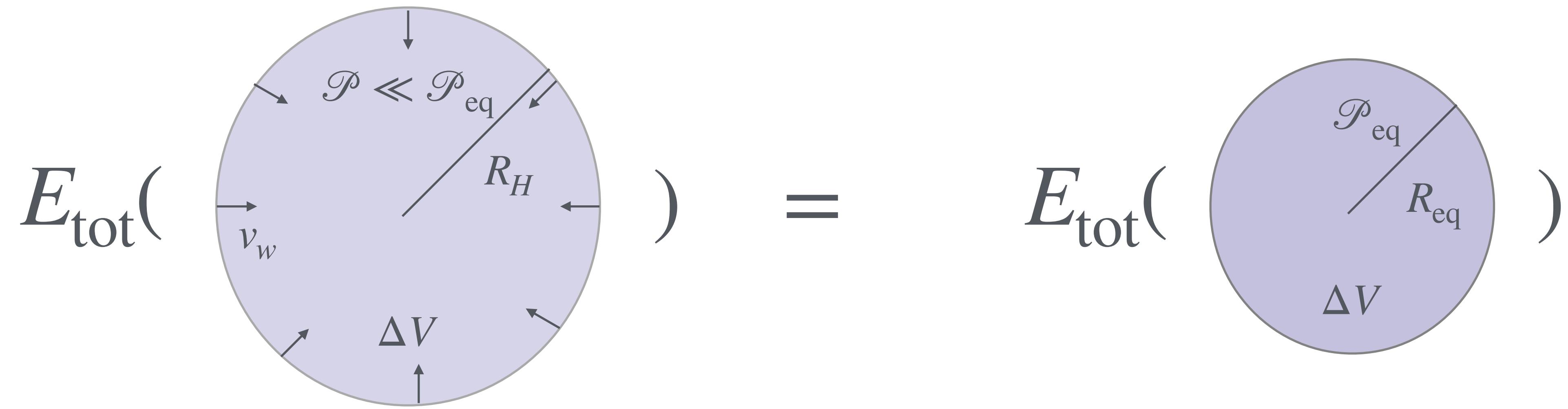
$$R_{\text{eq}} = \frac{2}{3} \frac{R_c}{\mathcal{P}/\Delta V - 1}$$

Equilibrium mass:

$$M_{\text{pocket}} = \sigma A_{\text{eq}} + (\Delta V + 3\mathcal{P}) V_{\text{eq}} = \Delta V V_{\text{eq}} \left( 4 + \frac{R_c}{R_{\text{eq}}} \right) \approx 4 \Delta V V_{\text{eq}}$$



# Energy conservation



**Model independently:**

$$R_{\text{eq}} = \mathcal{O}(1) \times R_H$$

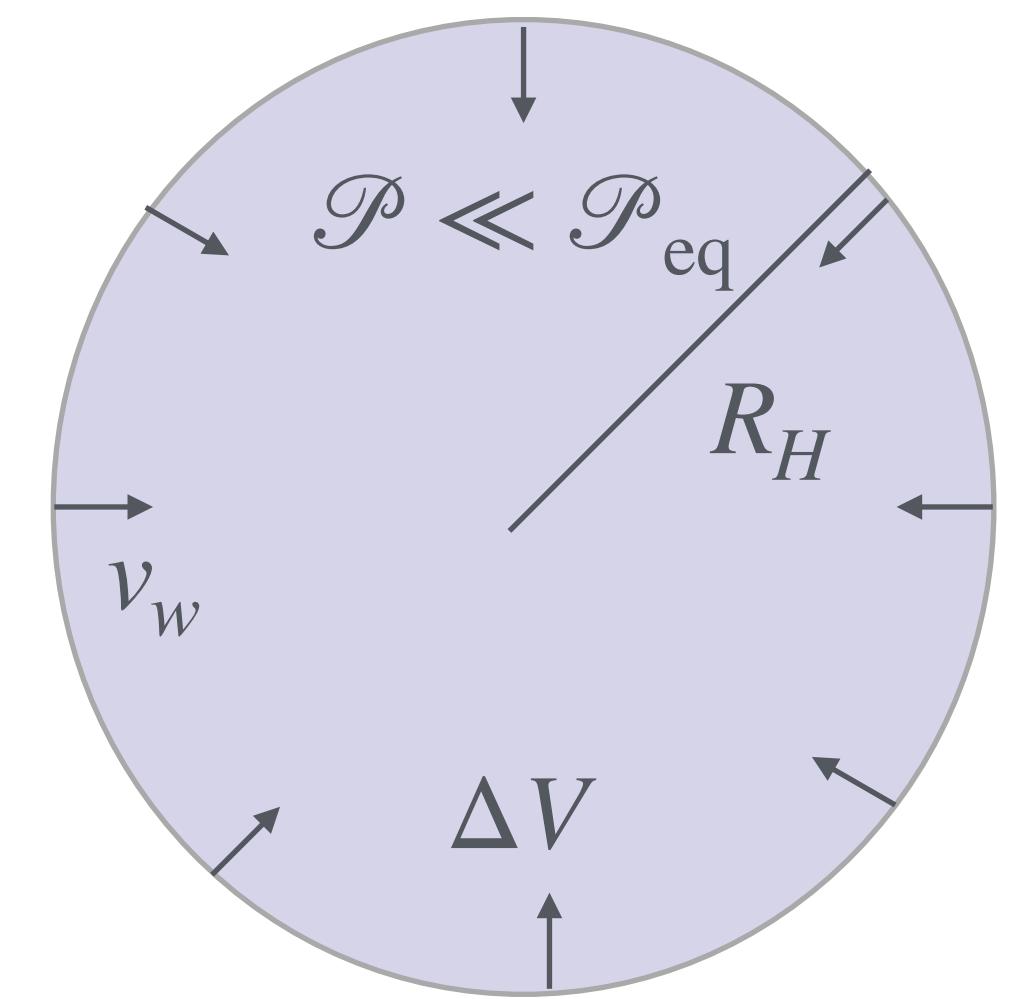
$$\mathcal{P}_{\text{eq}} = \Delta V (1 + \text{small})$$

$$M_{\text{pocket}} \approx (\Delta V + 3\mathcal{P}) V_{\text{eq}} = 4\Delta V V_{\text{eq}}$$

**Axion gas temperature (thermal):**

$$T_{\text{eq}} \sim 5 \text{ GeV} \left( \frac{T_t}{\text{TeV}} \right)^{3/4}$$

If gas *thermalises*, all properties become independent of initial axion abundance.



## Energy conservation

Consider the (spherical) pocket just as it was formed

$$E_{\text{tot}} = \frac{\gamma(t_{\text{coll}})\sigma A_H}{T} + \Delta V V_H + E_{\text{gas}}^{(0)} \approx (1 + \alpha) \Delta V V_H$$

$\equiv \alpha \frac{R_H}{R_c}$ 
 $\ll \Delta V V_H$

**Energy conservation:**  $E_{\text{tot}} = M_{\text{pocket}} \approx 4\Delta V V_{\text{eq}}$

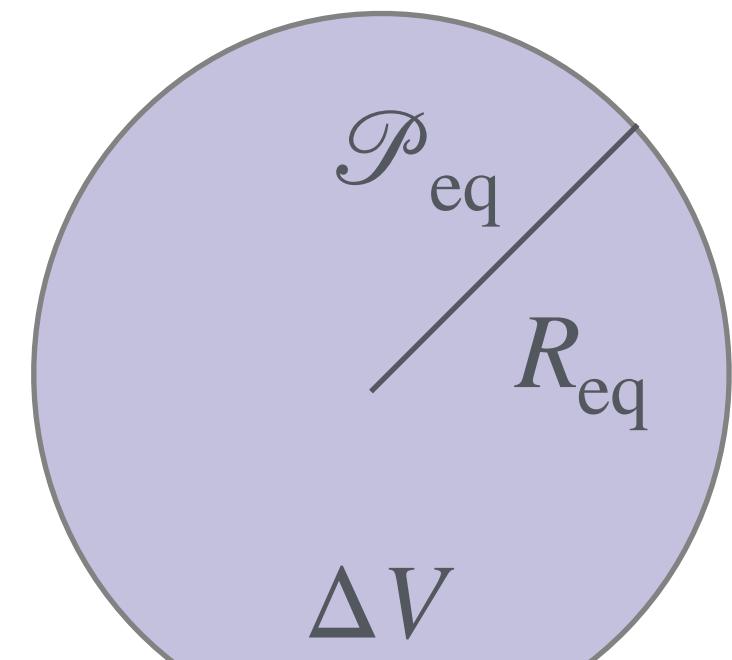
$$R_{\text{eq}} = \left( \frac{1 + \alpha}{4} \right)^{1/3} R_H$$

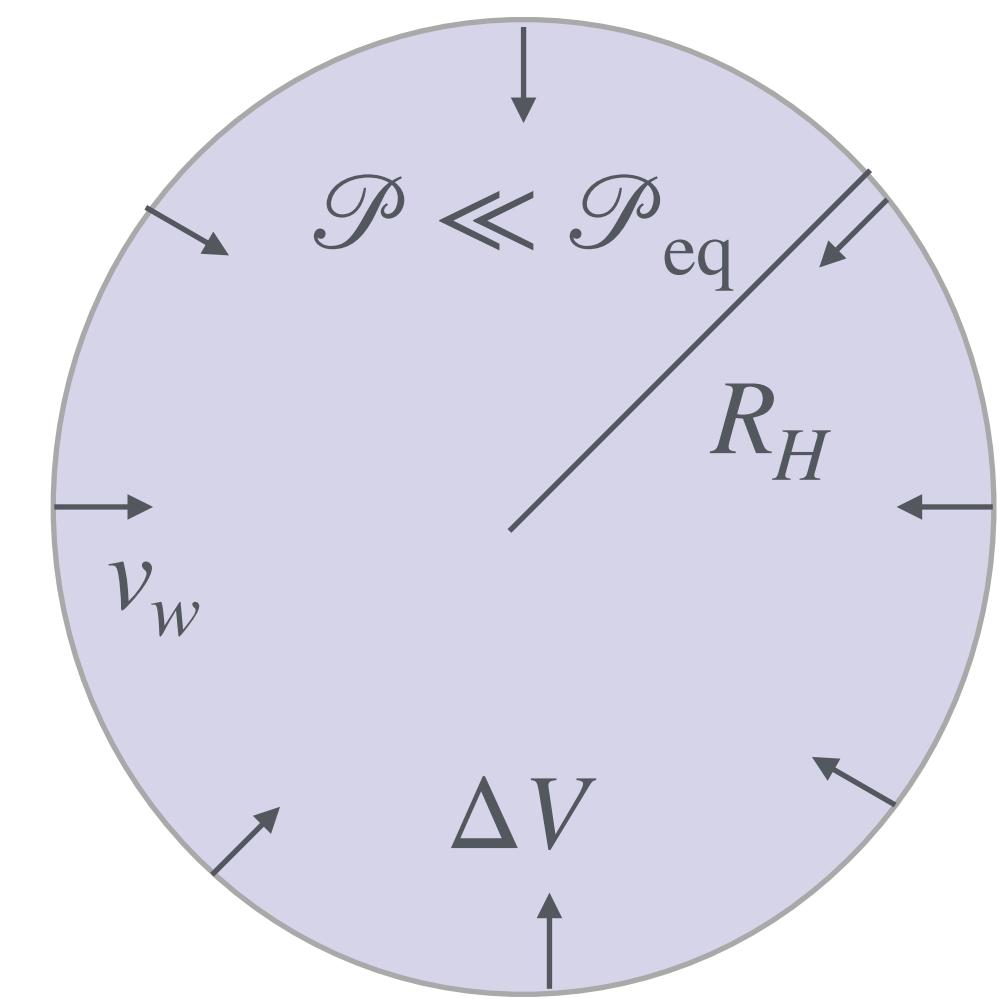
Pocket radius  $\sim$  Hubble radius at time of creation

**Gas pressure:**

$$\mathcal{P}_{\text{eq}} = \Delta V (1 + \mathcal{O}(R_c/R_H))$$

**Axion gas temperature (thermal):**





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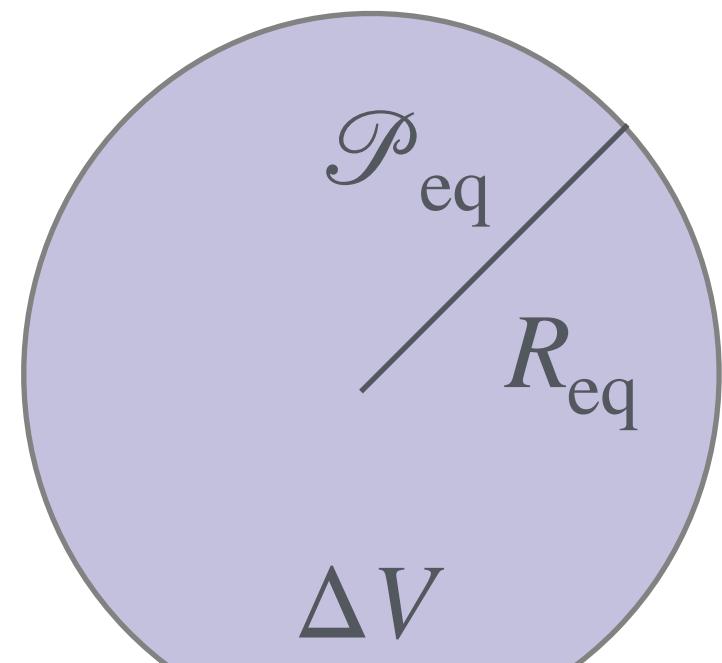
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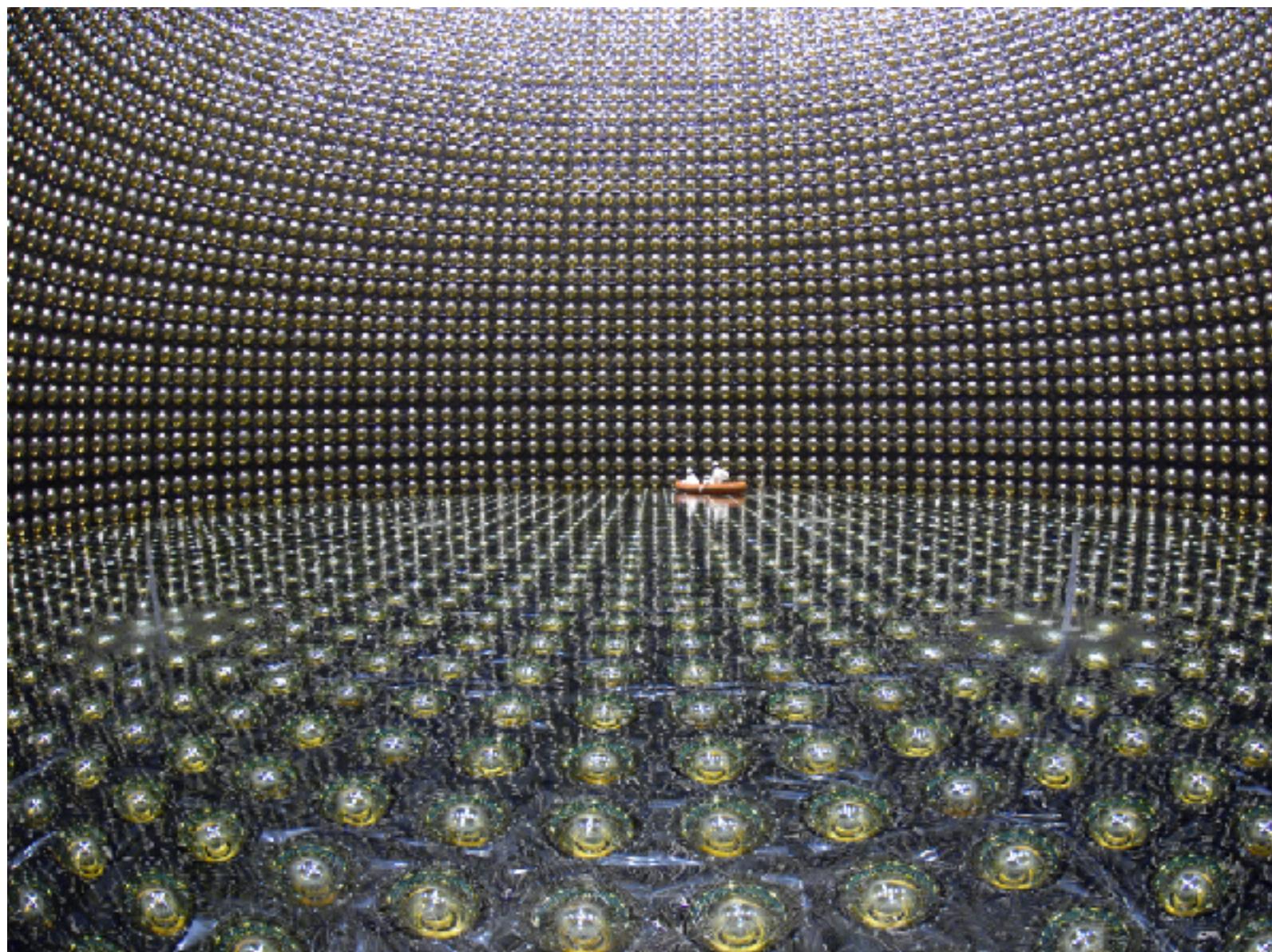
# Laboratory searches for Axion Relic Pockets

**Encounter rate:**

$$\Gamma_{\text{encounter}} \sim n_{\text{pocket}} \sigma v_{\text{pocket}} = 10^{-6} \epsilon \text{ year}^{-1} \left( \frac{R}{R_{\oplus}} \right)^2 \left( \frac{T_t}{\text{TeV}} \right)^3$$

For  $T_t \gtrsim 10^{12} \text{ GeV}$ , a detector volume of  $1 \text{ m}^3$  would encounter 1 pocket/second.

Gas temperature  $\sim 10^{10} \text{ GeV}$ , and #axions/pocket  $\sim 10^5$ .



Super-Kamiokande



XENONnT



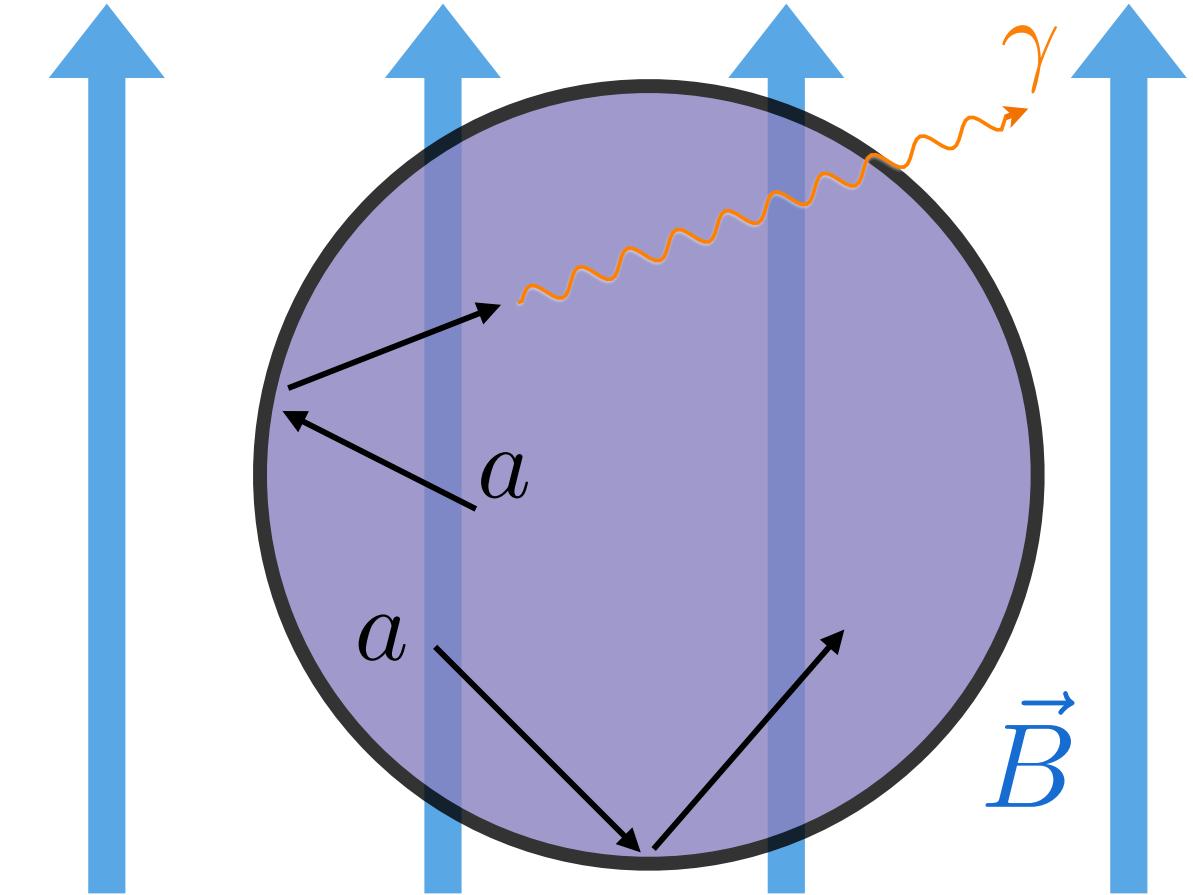
LHAASO, WCDA

# Astronomical searches for Axion Relic Pockets

## Axion-photon conversion rate:

$$\left| \frac{dN_{a\text{ pocket}}}{dt} \right| = \Gamma_{a \rightarrow \gamma} N_{a\text{ pocket}} = 200 \text{ s}^{-1} \epsilon^{-3/4} \left( \frac{g_{a\gamma}}{10^{-10} \text{ GeV}^{-1}} \right)^2 \left( \frac{B}{\mu\text{G}} \right)^2 \left( \frac{\text{TeV}}{T_t} \right)^{23/4}$$

Rate is small enough for relic pockets to be long-lived.



Number flux is greatly enhanced at low temperatures. E.g., for  $T_t = 15 \text{ GeV}$  and  $B_\perp = 15 \text{ G}$ ,

$$\left| \frac{dN_{a\text{ pocket}}}{dt} \right| \sim 10^{37} \text{ s}^{-1} \left( \frac{g_{a\gamma}}{10^{-10} \text{ GeV}^{-1}} \right)^2$$

with photon energy set by  $T_{\text{eq}} \sim 230 \text{ MeV}$ .

Moderate-to-highly magnetised regions (e.g. magnetars with  $B \sim 10^{15} \text{ G}$ ) may generate observable, characteristic signals.

# Theory requirements

**Initial axion population particle-like:**

$$m_a \Big|_{\text{FV}} \gtrsim 3H(T_t)$$

if produced by misalignment mech.  
no restriction if seed is dark radiation

**Reflective boundary condition:**

$$m_a \Big|_{\text{TV}} > E_a$$

**Required field displacement:**

$$\frac{|\Delta\phi|}{\phi_{\text{FV}}} \gtrsim 0.1 - 0.5$$

for  $S_{\text{FV}} \sim \mathcal{O}(100)$

**Dilaton potential:**

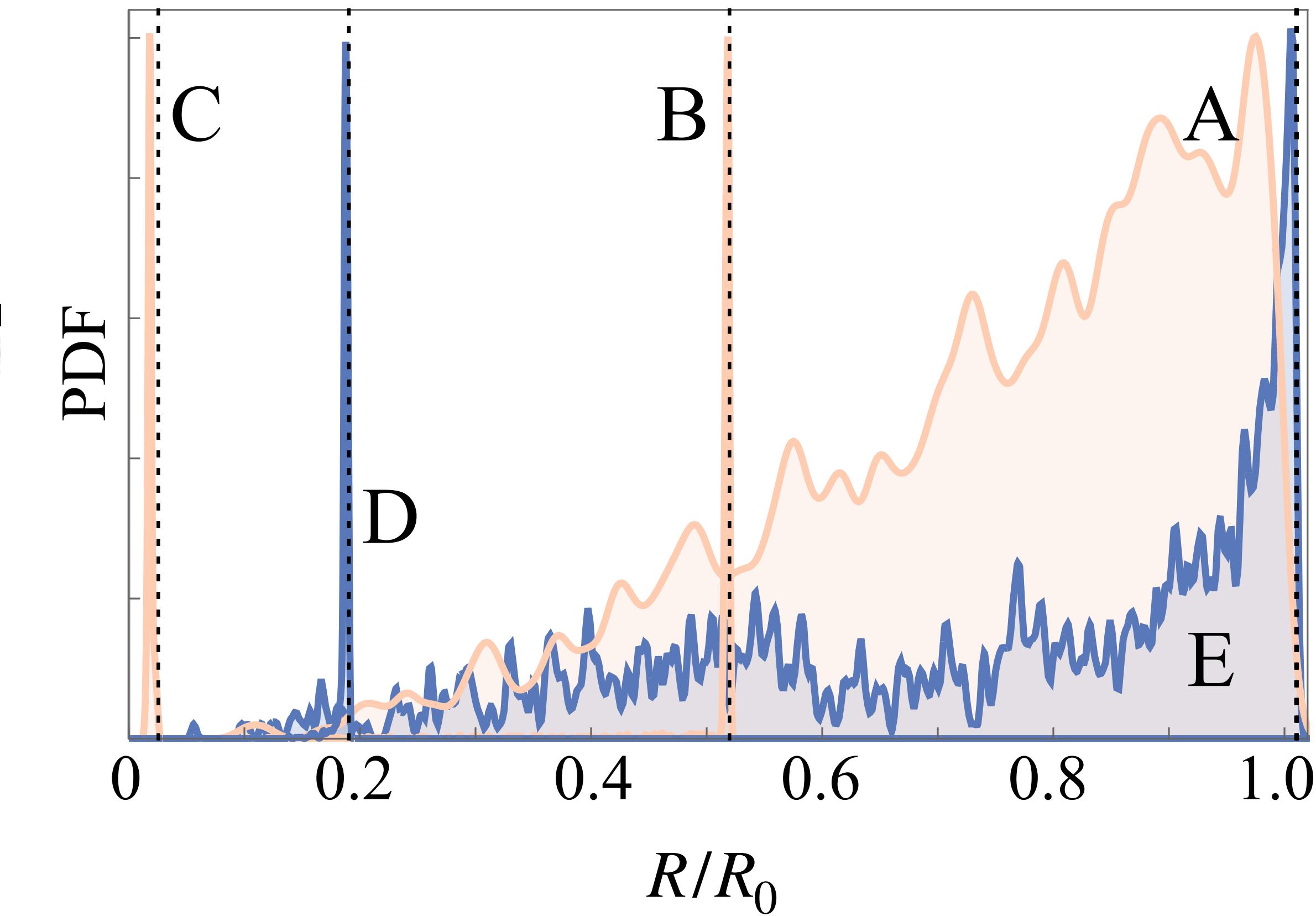
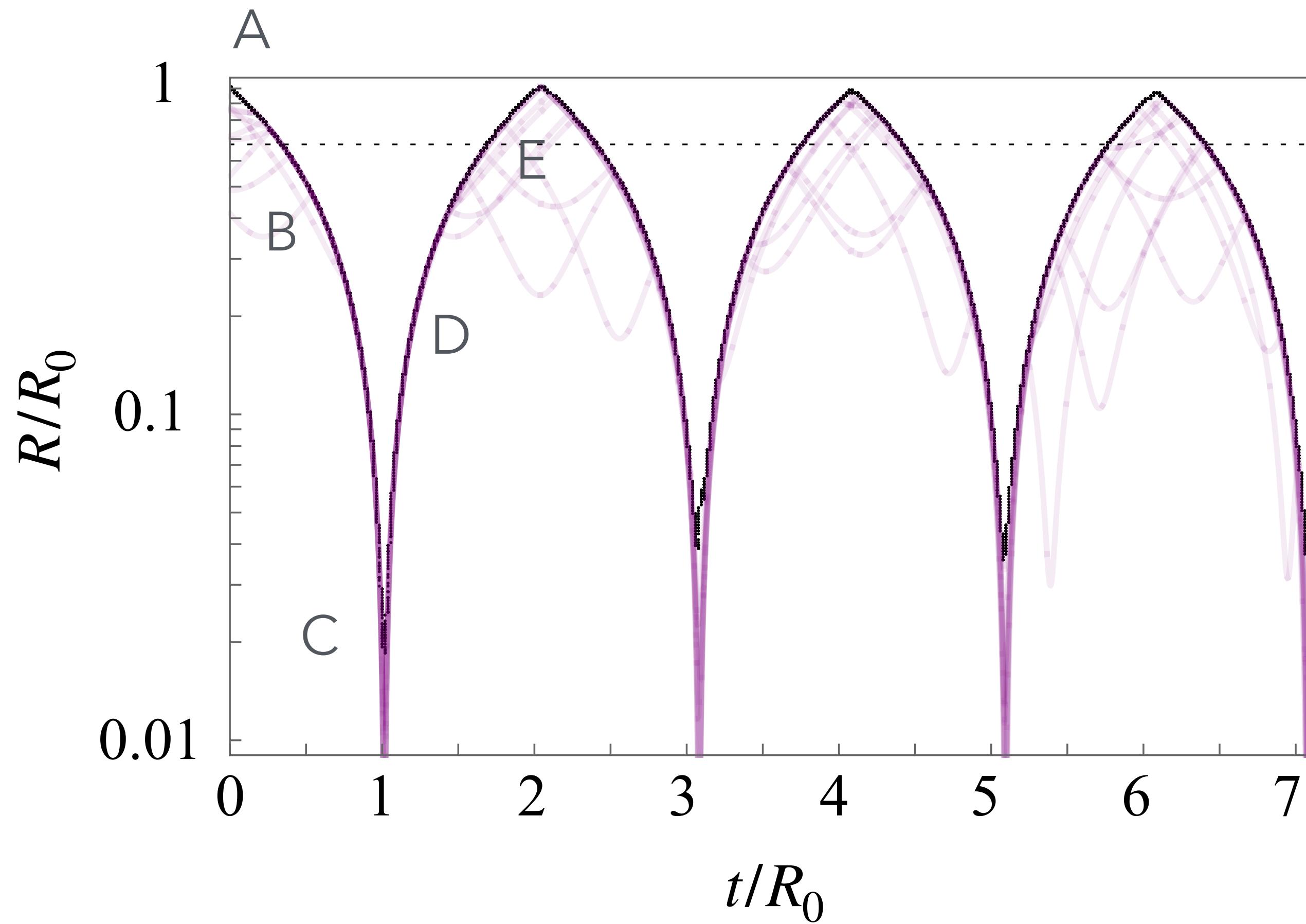
$V_{\text{dil}}(\phi)$  should support a quantum phase transition during radiation domination.

$m_\phi \gg E_a$  in both phases, in simplest case.

Couplings to the Standard Model can make  $\phi$  unstable.

# Pulsating pockets

$$\begin{cases} N_{\text{particles}} & = 1,000 \\ \dot{R}(0) & = -0.999 \\ R_0/R_c & = 100 \end{cases}$$



Radial oscillations for some time.

# Context: Previous work

**Transient false-vacuum pockets** ("droplets")

are observed in more general PT's, even without large mass hierarchy.

Weir++ 2019

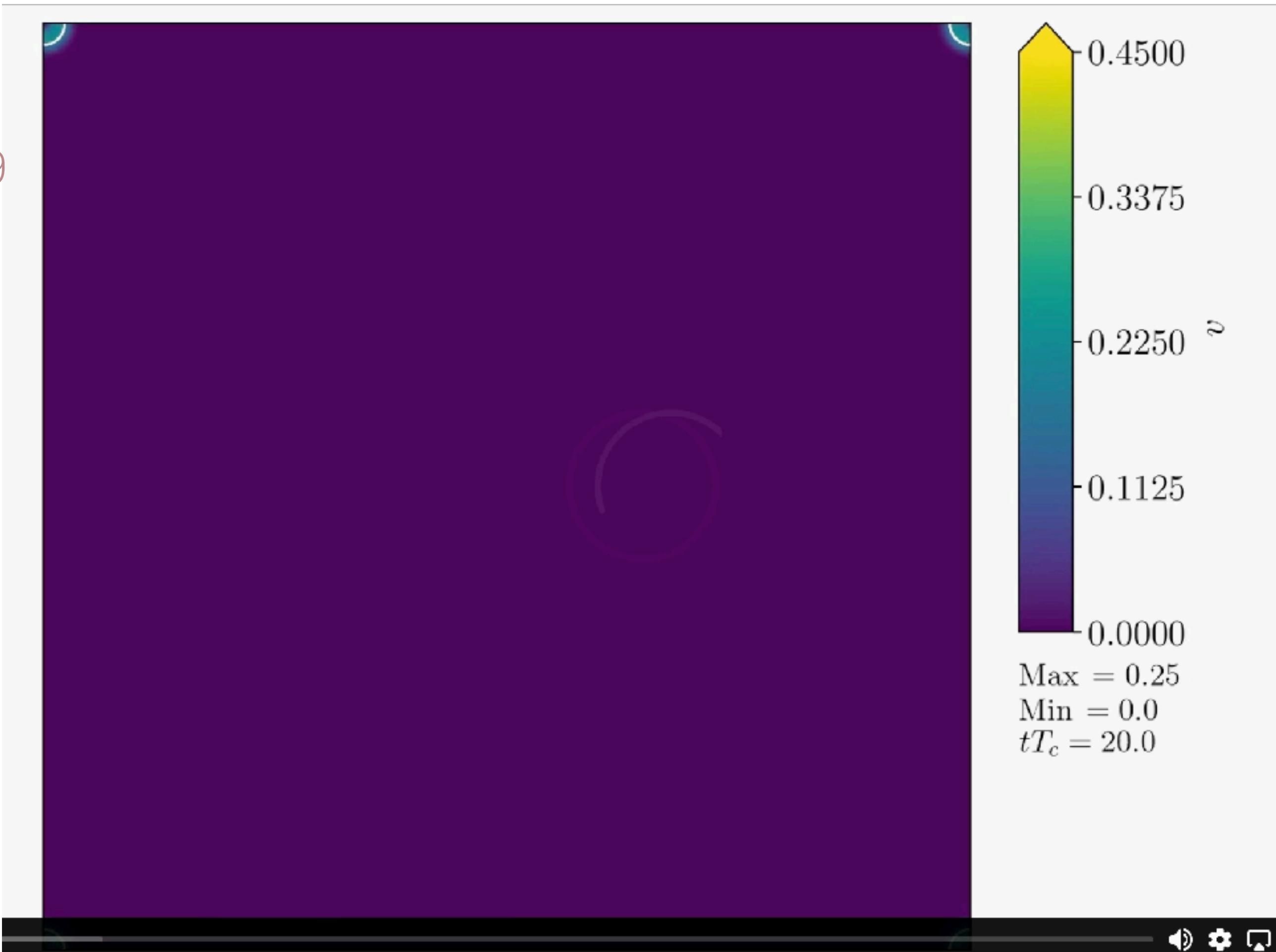
**Quark nuggets** are pockets that could have formed if the QCD phase transition was first order and "strange quark matter" is the true ground state of baryonic matter.

Witten '84

**Generalisations:** Axion Quark Nuggets, Dark Quark Nuggets, Fermi balls, Thermal balls

**See talk by Ariel Zhitnitsky this afternoon.**

Zhitnitsky 2002; Bai 2018; Gross++ 2021;  
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