



Istituto Nazionale di Fisica Nucleare  
LABORATORI NAZIONALI DI LEGNARO



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# Image-based cell dosimetry using Geant4

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Image of cells (LNCaPs)

Development of a geometric model

Simulations with Geant4

Determination of absorbed dose and of survival fraction in a culture irradiated with Ag-111



# Work flow

## Phase I: study of the image

Radii of each cell and their respective probability (PDF)

Mean radius of each cell

Mean radius and std deviation of the image

## Phase II: geometric model

Modeling cells with wedges

Simulations with Geant4 calculating the S-values for different shapes

Interpolating S-value's curves

## Phase III: generation of 10000 cells

Lognormal distribution of mean radii

Association of each bin of the lognormal to a PDF (from phase I)

## Phase IV: dose and survival fraction

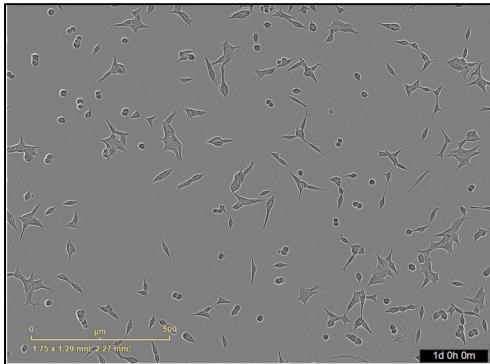
S-values in the nucleus from interpolating curves and PDFs

Activity assigned randomly to each cell using another lognormal distribution

Average cumulated dose and survival fraction

# Phase I: image analysis with ImageJ

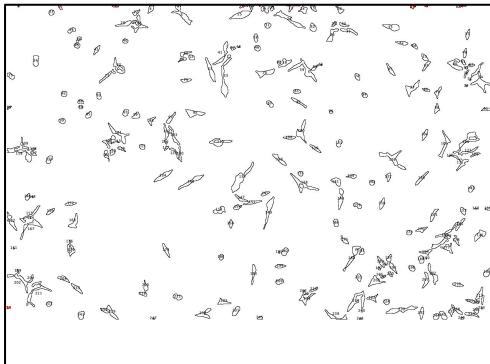
1)



2)



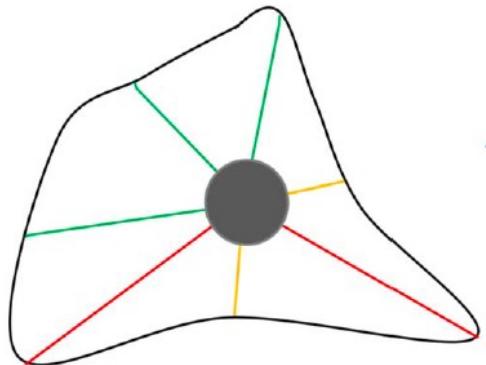
3)



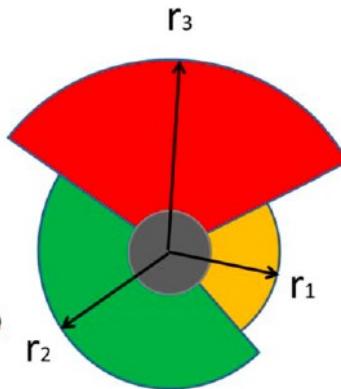
4)

```
Cellula numero 1
r_ 1 = 1.6866 p_ 1 = 0.08333
r_ 2 = 1.9159 p_ 2 = 0.08333
r_ 3 = 2.1452 p_ 3 = 0.08333
r_ 4 = 2.3744 p_ 4 = 0.08333
r_ 5 = 2.6037 p_ 5 = 0
r_ 6 = 2.833 p_ 6 = 0
r_ 7 = 3.0622 p_ 7 = 0.25
r_ 8 = 3.2915 p_ 8 = 0.1667
r_ 9 = 3.5208 p_ 9 = 0.1667
r_ 10 = 3.75 p_ 10 = 0.08333
Mean radius [um]= 2.8809 Dev std [um]= 0.6332
*****
```

# Phase II: geometric model

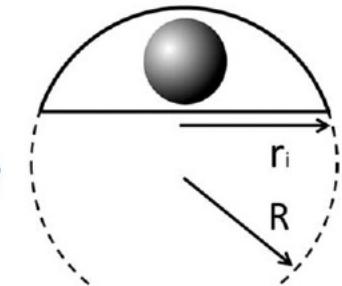
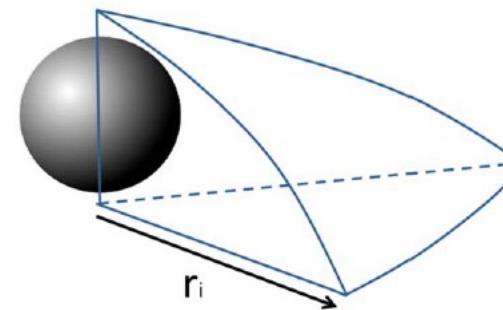


A 3-bin histogram representation



In 3 dimensions

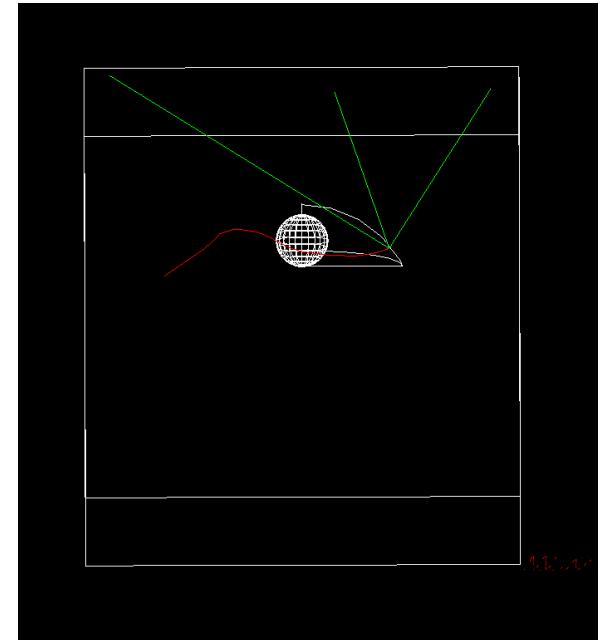
Spherical cap representation of wedge



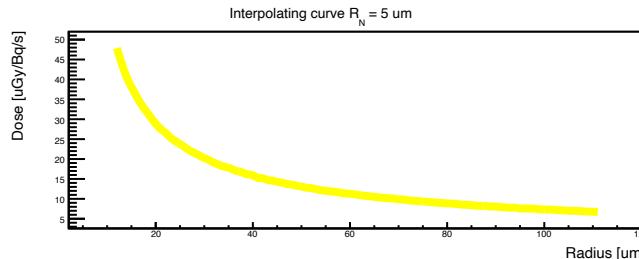
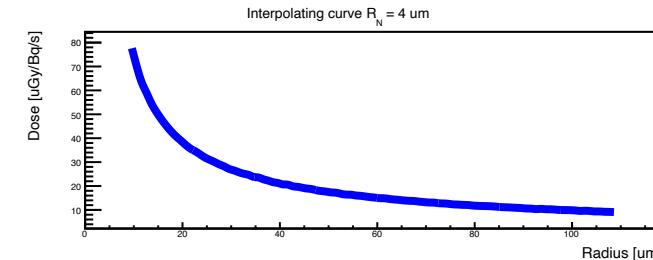
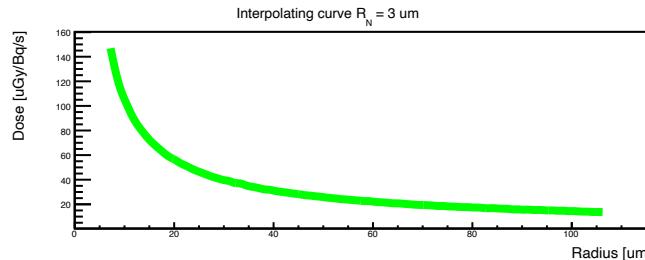
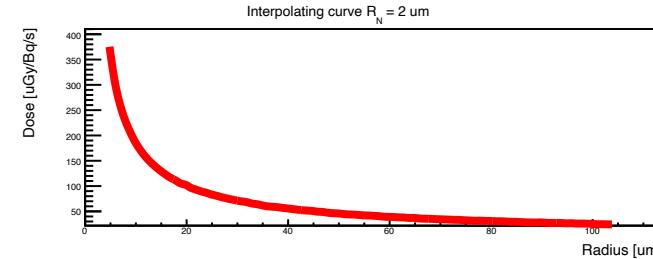
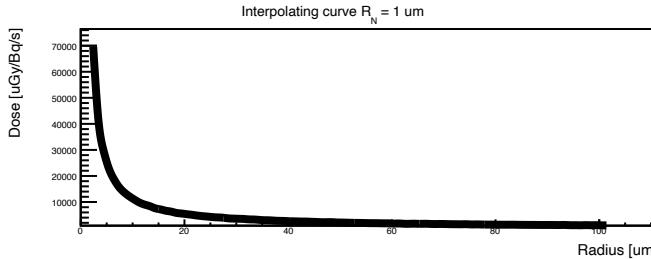
# Simulations with



- Simulations of this geometry changing the radius of the sphere and of the nucleus
- Calculation of the S-value for 100 radii and 5 radii of the nucleus

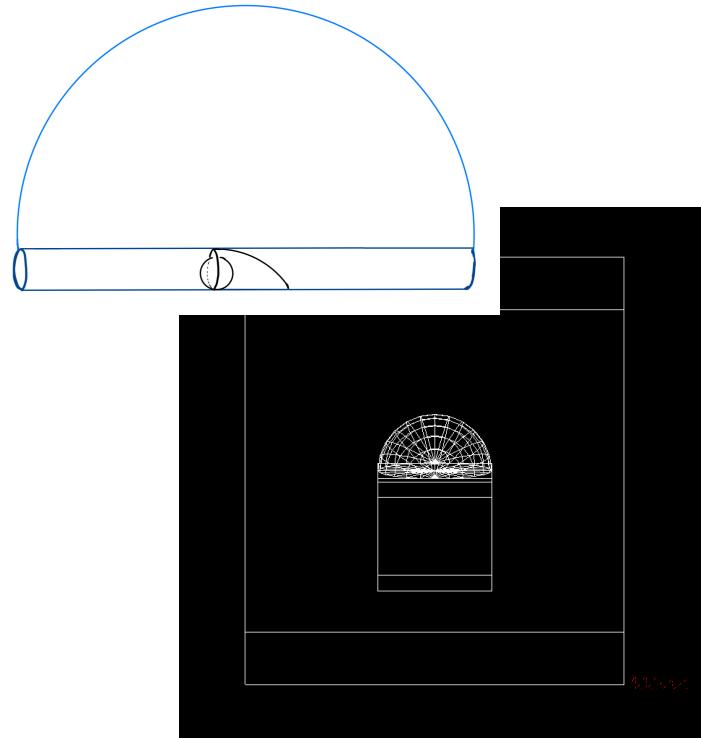


# S-values curves



Source: membrane  
Target: nucleus

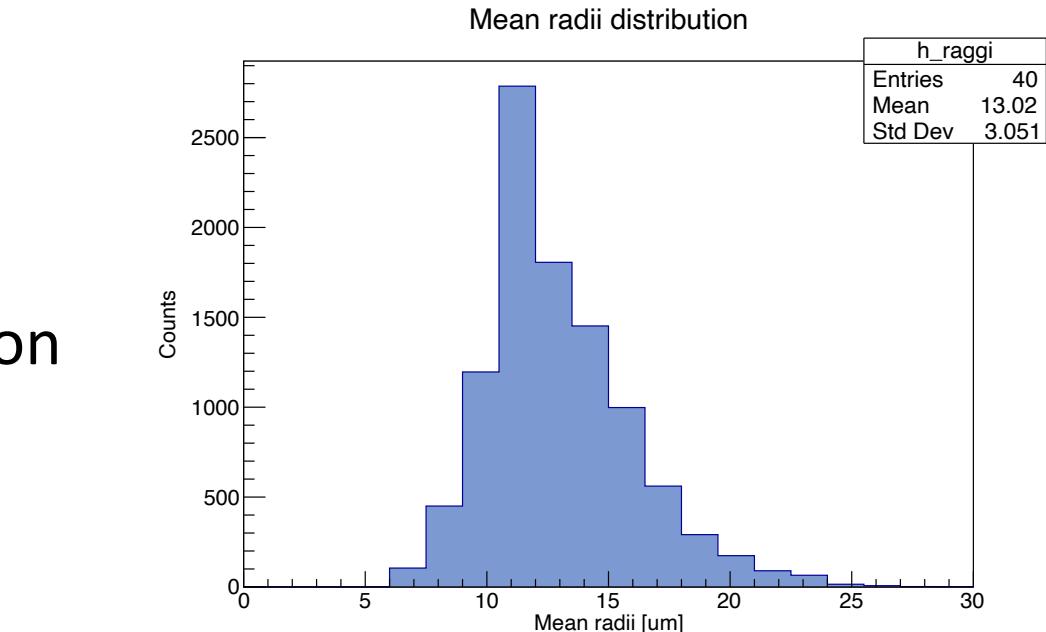
- Emisphere (water) of radius 3 mm
- Cylinder (water) of height  $\sim 15 \mu\text{m}$
- Box (polystyrene) of height 1 mm
- Box (steel) of height 5 mm



# Phase III: generation of 10000 cells

- 10000 cells of different mean radii
- Lognormal distribution
- Each bin of the distribution is associated with a PDF

```
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r_ 1 = 1.6866 p_ 1 = 0.08333
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```



# Phase IV: S-value calculation

$$D_{tot} = \sum_{r_i}^{\#bins} D(m \rightarrow n) (r_i) \cdot p_i + D(cy \rightarrow n)(r_i) \cdot p_i$$

# Phase IV: S-value calculation

$$D_{tot} = \sum_{r_i}^{\#bins} [D(m \rightarrow n)(r_i) \cdot p_i + D(cy \rightarrow n)(r_i) \cdot p_i]$$


S-value from the interpolating curves:

- source: membrane
- target: nucleus

# Phase IV: S-value calculation

$$D_{tot} = \sum_{r_i}^{\#bins} D(m \rightarrow n)(r_i) \cdot p_i + \boxed{D(cy \rightarrow n)(r_i)} \cdot p_i$$



S-value from the interpolating curves:

- source: cytoplasm
- target: nucleus

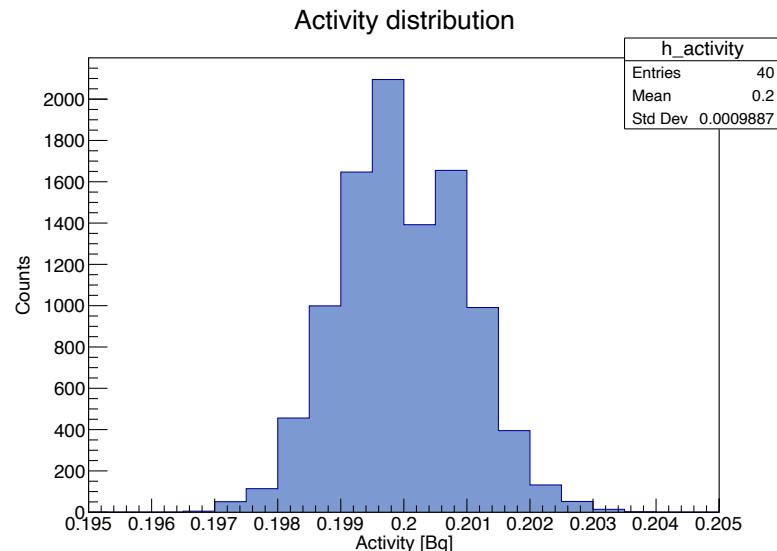
# Phase IV: S-value calculation

$$D_{tot} = \sum_{r_i}^{\#bins} D(m \rightarrow n)(r_i) \cdot p_i + D(cy \rightarrow n)(r_i) \cdot p_i$$



Probability of the radius  $r_i$

- The activity is assigned randomly to each cell using a lognormal distribution

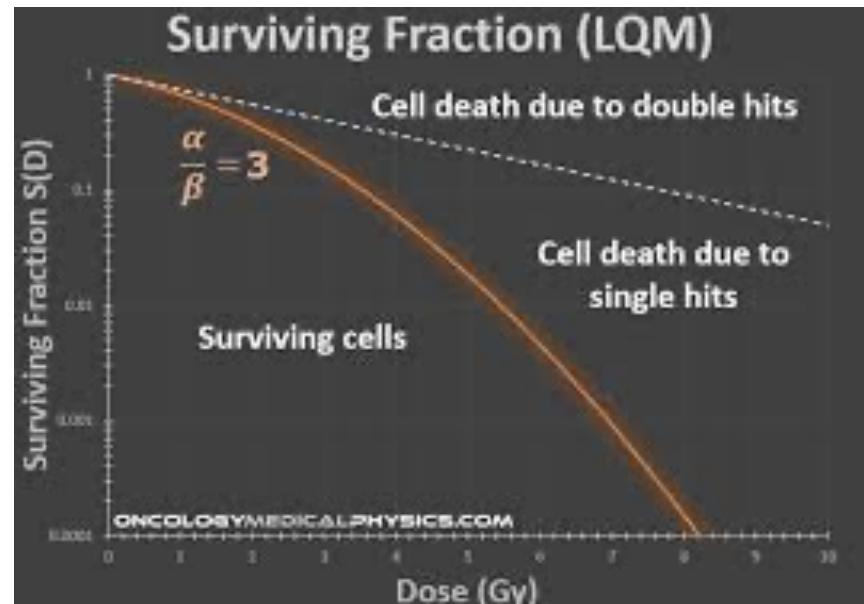


## Hypothesis

- Applied activity: 100 kBq
- Uptake: 2%
- In the cytoplasm: 60%
- In the membrane: 40%

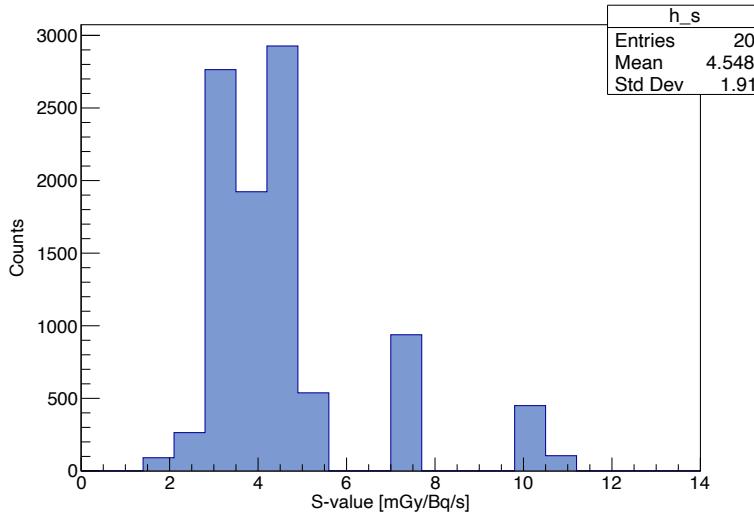
# Cell survival probability

- LQ model:  $P = e^{-\alpha D - \beta D^2}$
- A cell is alive if  $\xi < P$ , for  $\xi \in [0, 1]$
- Average survival probability:  
 $N_{alive}/N_{cells}$

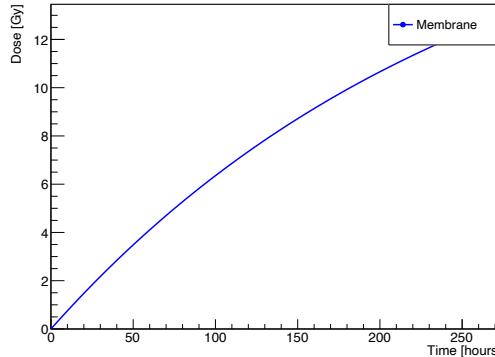


# First results

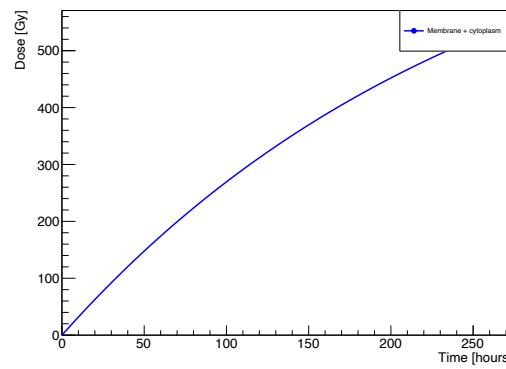
S-value distribution



Average cumulated dose per cell nucleus

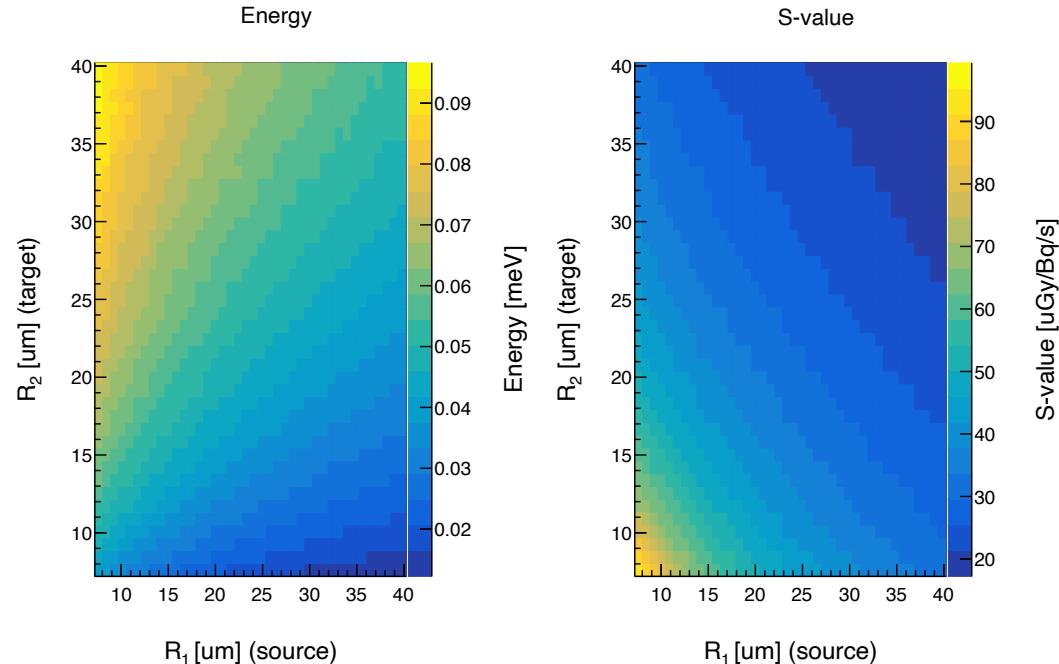
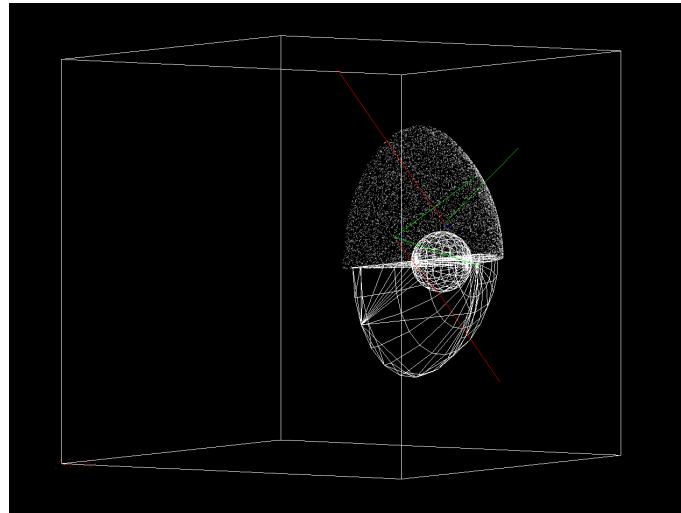


Average cumulated dose per cell nucleus



- Great dose released in the nucleus from the cytoplasm
- Average surviving fraction after 4 days:  
~0 %

- Two wedges: one is the source, the other is the target



# Conclusions: what's next?

- Predictions on how the cumulated dose and the surviving fraction change with the applied activity
- Predictions on how the cumulated dose and the surviving fraction change with the uptake
- Compare the results with experimental data from the next experiment in May
- Implementing angular extension in the study of the target cytoplasm
- Therapy simulations with Geant4-DNA with Lu-177 in collaboration with Brescia hospital.

**Thanks for your attention!**