



#### Multiwavelength modelling

Lea Heckmann









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→ Steady state (typically a broken power law) or time evolving particle distribution







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#### Radiation mechanisms

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- Power law of e (index p)  $\rightarrow$  power law of photons ( $\Gamma$ )

 $\Gamma = \frac{p-1}{2}$ 



electron



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Upscattering of low-energy photons
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- Photon target fields:
  - Synchrotron photons (SSC)
  - Cosmic microwave background
  - AGN components: Dusty torus, Accretion disk, broad line region



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• Power 
$$P_{IC} = \frac{4}{3} c \sigma_T \beta^2 \gamma^2 U_{rad}$$



#### Inverse Compton emission

• Thomson regime

 $h v \ll m_e c^2$ 

 Klein Nishina regime decreases scattering cross section



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- Klein Nishina regime decreases scattering cross section
- Energy gain:  $\Delta v \sim y^2$  Thomson  $\Delta v \sim y$  Klein Nishina

• Cooling time scale:  

$$t_{cool} \sim \frac{1}{\gamma U_{rad} F_{KN}}$$
 $F_{KN} \ll 1$ 
Thomson
Klein Nishina



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Credit: http://chandra.harvard.edu/resources/illustrations/x-raysLight.html

• Cooling time scale:

$$\Delta v \sim \gamma^{2}$$
  
 $\Delta v \sim \gamma$  Klein Nishina

$$F_{_{K\!N}}\!pprox\!1$$
 Thomson  
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• Spectral index:

$$\Gamma_{IC} \sim \Gamma_{syn}$$

 $t_{cool} \sim \frac{1}{\gamma U_{rad} F_{KN}}$ 

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Bremsstrahlung

Acceleration of electrons in the Coloumbfield of nuclei
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Acceleration of electrons in the Coloumbfield of nuclei
 → Emission of high-energy photons (X-rays/gamma)



- Power:  $P \sim Z^2 N v$  (non-relativistic) different for relativistic or thermal cases but always proportional to Z
- Cooling time:



#### Leptonic models



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[ erg cm<sup>2</sup> s<sup>-1</sup>]

Energy flux v F<sub>v</sub>

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Proton-proton

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- Main channels:

$$\begin{array}{rcl} p+p & \rightarrow & p+p+\pi^0 \\ p+p & \rightarrow & p+n+\pi^+ \\ p+p & \rightarrow & p+p+\pi^++\pi^- ... \end{array}$$

$$\begin{aligned} \pi^0 &\to & \gamma + \gamma \\ \pi^+ &\to & \mu^+ + \nu_\mu \quad \text{and} \quad \mu^+ \to e^+ + \bar{\nu}_\mu + \nu_e \\ \pi^- &\to & \mu^- + \bar{\nu}_\mu \quad \text{and} \quad \mu^- \to e^- + \nu_\mu + \bar{\nu}_e \end{aligned}$$

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• π<sup>o</sup> decay shows up in gamma-rays



Credit: https://libgamera.github.io/GAMERA/docs/radiation\_modeling.html

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#### Proton-photon

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• Produced electrons and photons subsequently develop cascades

(Lepto)-hadronic models

AGNs









# Propagation: boosting, absorption,...

Doppler boosting

- Enhances the flux when structures move relativistically towards us at an angle  $\theta$  (e.g. AGN jets):



Credit: https://www.mpi-hd.mpg.de/HESS/pages/home/som/2018/04/

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- Synchrotron self-absorption (radio)
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<u>Absorption and extinction:</u>

- Synchrotron self-absorption (radio)
- Interstellar extinction (IR UV)
- Interstellar medium grain absorption (X-rays)
- Gamma-gamma absorption (gamma rays)
  - Extragalactic background light
  - Internal photon fields, e.g. accretion disk photons





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### Public tools

#### <u>Python based/interface:</u>

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- Jetset
- Agnpy
- AM3
- FLAREMODEL
- ....

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Overview paper of some public codes:

 Galaxies 2022, 10(4), 85; https://doi.org/10.3390/galaxies10040085

Hadronic code comparison paper:

• arXiv:2411.14218

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- Input: steady-state particle distributions



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  - MCMC
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  - But only independent zones (no interaction)
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(b) CTA 102

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Credit: ApJ 950 28 (2023)



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    - Currently mostly done on flux points (SEDs)
    - Better to do it on count data (dl3) itself → Gammapy https://github.com/mireianievas/gammapy\_mwl\_workflow

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