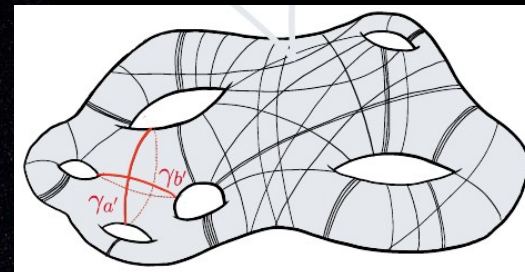
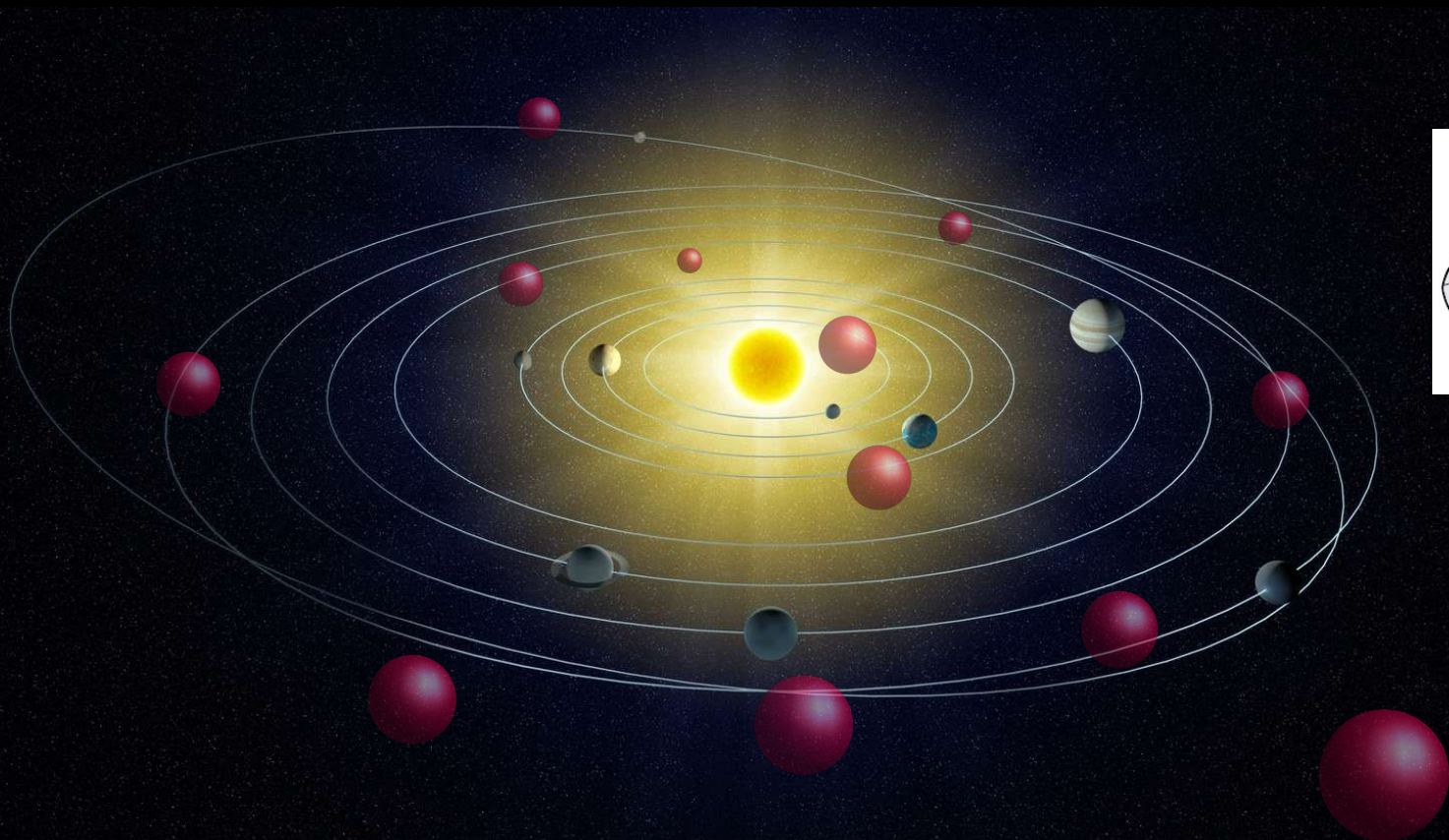


Open String Axiverse

Giovanni Villadoro
ICTP

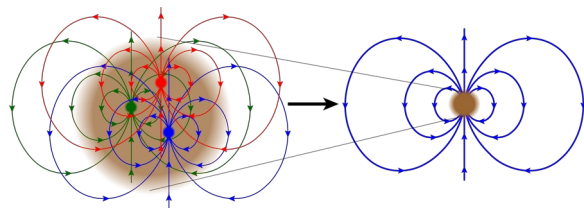


with
Rudin Petrossian-Byrne
2503.16387

The Strong CP problem

The Strong CP ~~problem~~ puzzle

No nEDM

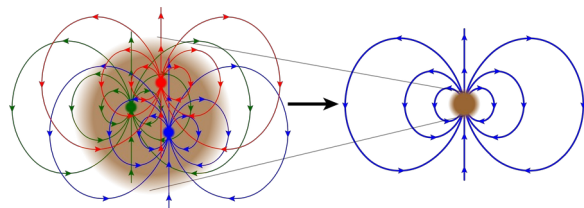


$$\theta \equiv \arg \left\{ \det (Y_u Y_d) e^{i\theta_0} \right\} \lesssim 10^{-10}$$

 $\frac{\theta_0}{32\pi^2} G\tilde{G} \in \mathcal{L}_{\text{SM}}$

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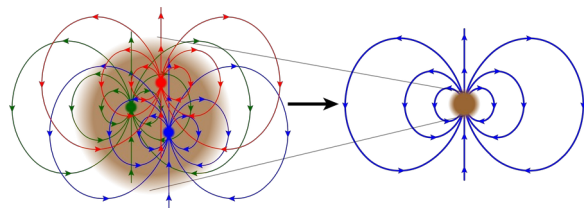
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$\searrow$
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$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2}(\partial a)^2 + \frac{a}{f_a} \frac{\alpha_s}{8\pi} G\tilde{G} + \dots \quad \Rightarrow \quad m = \frac{\chi_{\text{top}}^{1/2}}{f_a} \simeq 0.57 \text{ meV} \left(\frac{10^{10} \text{ GeV}}{f_a} \right)$$

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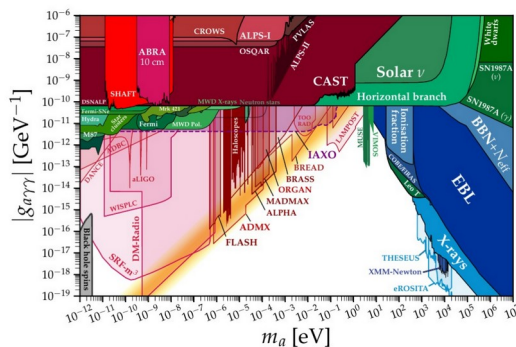
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Testable:



2203.14923

Dark Matter:



Cosmological Scenarios:

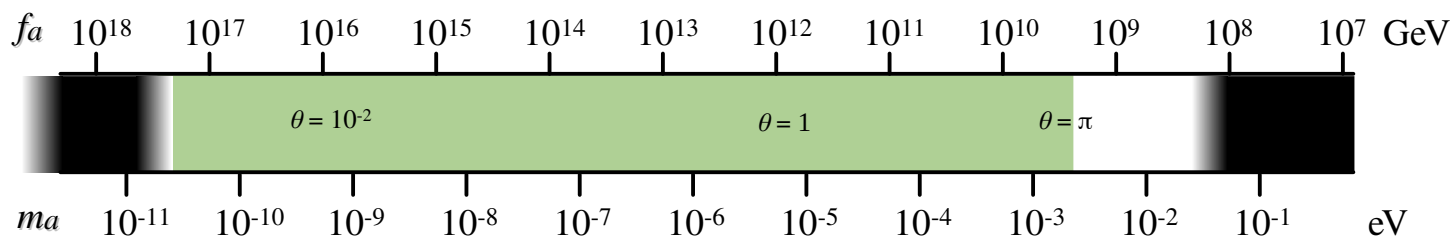
1. “pre-inflation”:
(standard misalignment)

2. “post-inflation”:
(topological defects)

Cosmological Scenarios:

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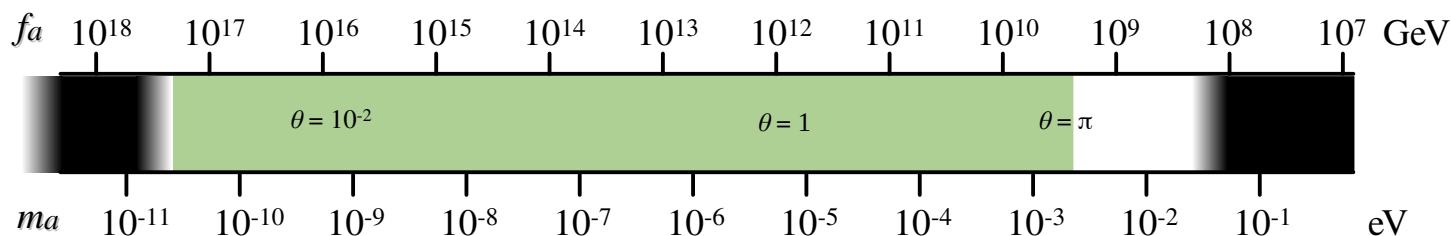


2. “post-inflation”:
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Cosmological Scenarios:

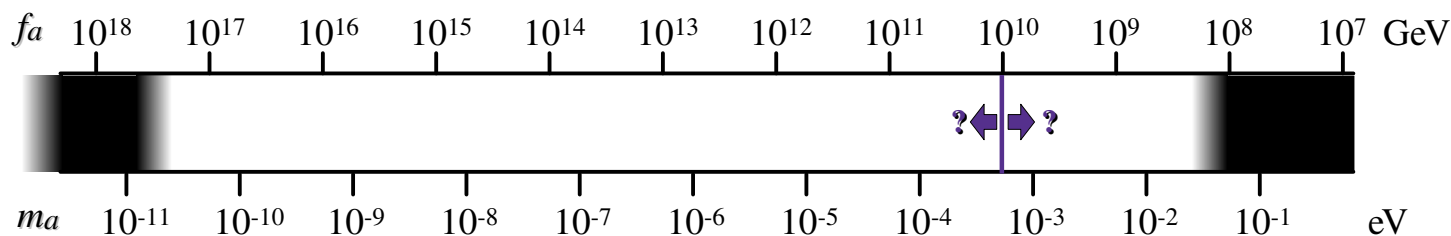
1. “pre-inflation”:
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PQ Quality:

$$V(a) = V_{\text{QCD}}(a) + V_{\text{PQ}}$$

$$\theta \lesssim 10^{-10}$$

$$\Rightarrow$$

$$V_{\text{PQ}} \lesssim 10^{-10} \chi_{\text{top}} \sim (0.2 \text{ MeV})^4$$

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Quantum Gravity $\rightarrow$ No Global Symmetries...

$$V_{\text{PQ}} \sim M_P^4 \sim 10^{78} \chi_{\text{top}}$$

Accidental PQ

$\rightarrow$ forbids PQ operators up to dim. $\sim 10 \div 40$ (for $f_a \sim 10^{10} \text{ GeV} \div \text{GUT}$)

Irreducible QG symm. breaking is non-perturbative (BH, wormholes, ...)

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$$\text{NOTE: QCD-breaking} \rightarrow \chi_{\text{top}} \propto e^{-\frac{\#}{g_s^2}}$$

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High Quality PQ $\rightarrow$ QG is weakly coupled

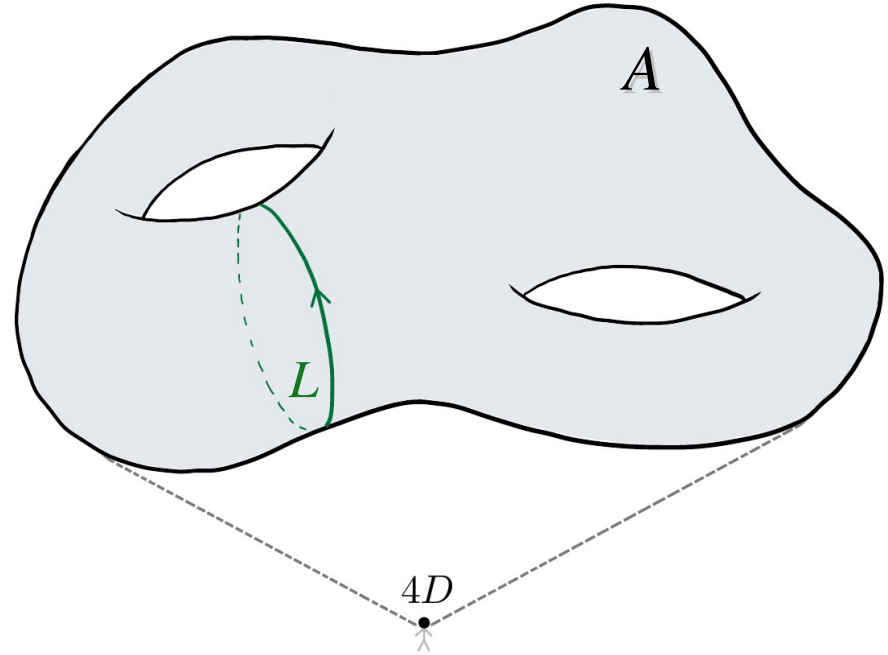
i.e. worry about PQ quality only in explicit UV completion of QG:
e.g. string theory

String Axiverse

Gauge Fields in Extra Dimensions

Choi '03

$$\frac{a}{v} = \arg \left(e^{i \oint A} \right)$$



String Axiverse

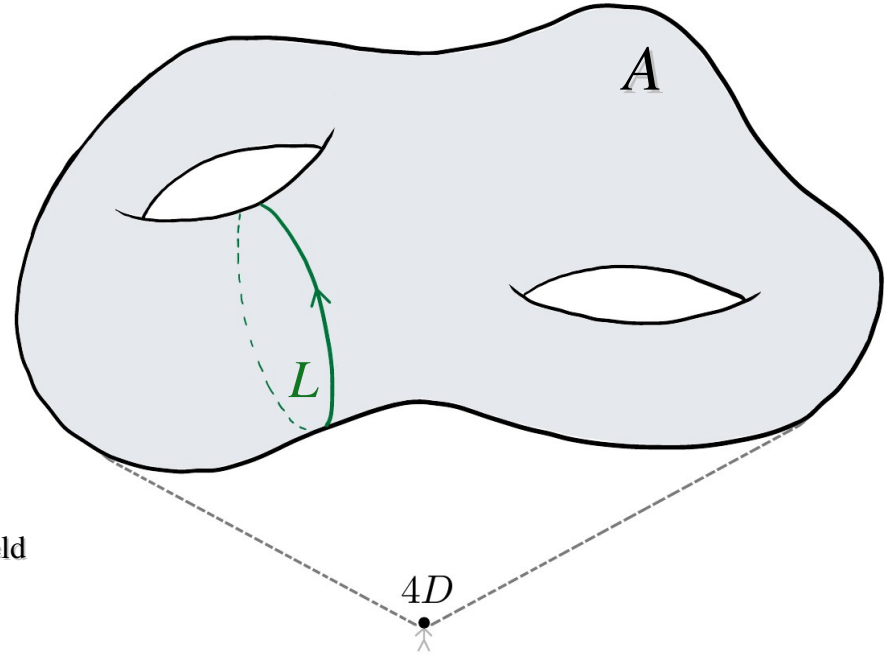
Gauge Fields in Extra Dimensions

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$$V_{PQ} \propto e^{-ML}$$


 lightest charged bulk field



String Axiverse

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In String Theory:

A = typically RR, NSNS p -forms
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 $\rightarrow M > M_s / g_s$

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$$V_{\text{PQ}} \propto e^{-\text{Vol}/g_s} \sim e^{-8\pi^2/g_4^2}$$

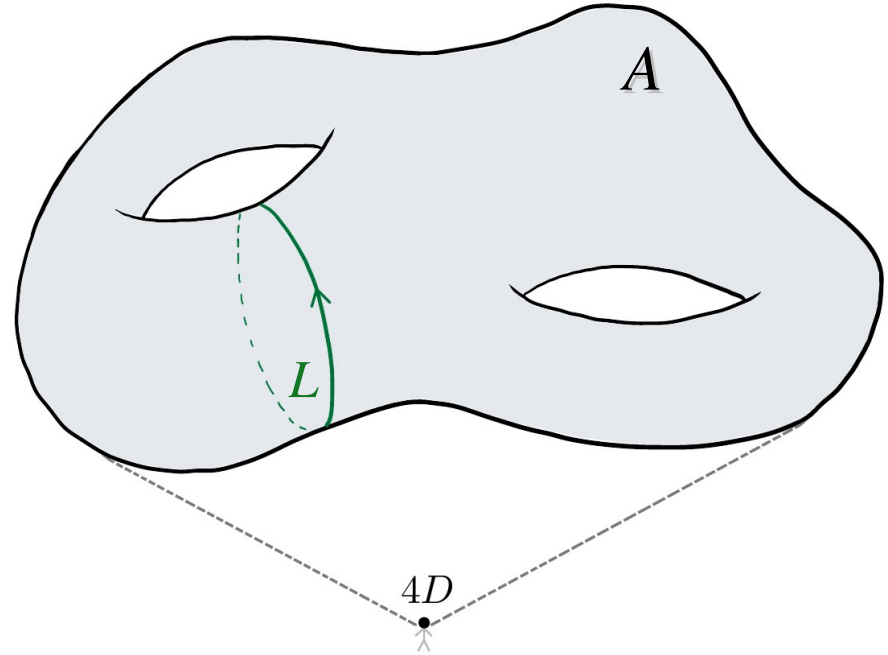
String Axiverse

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$$v > \frac{1}{L}$$



String Axiverse

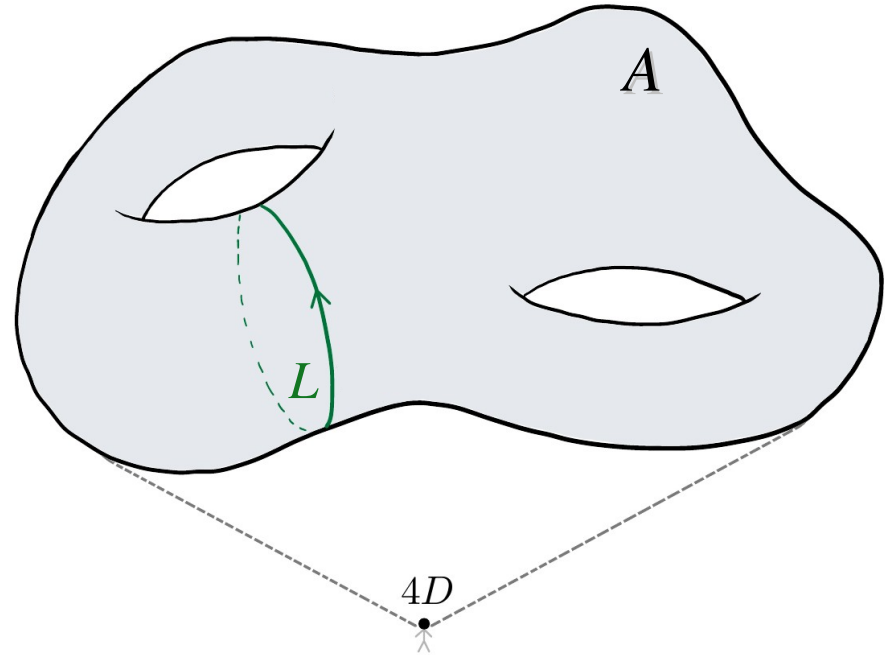
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✓ pre-inflationary and large f_a axions



String Axiverse

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Choi '03

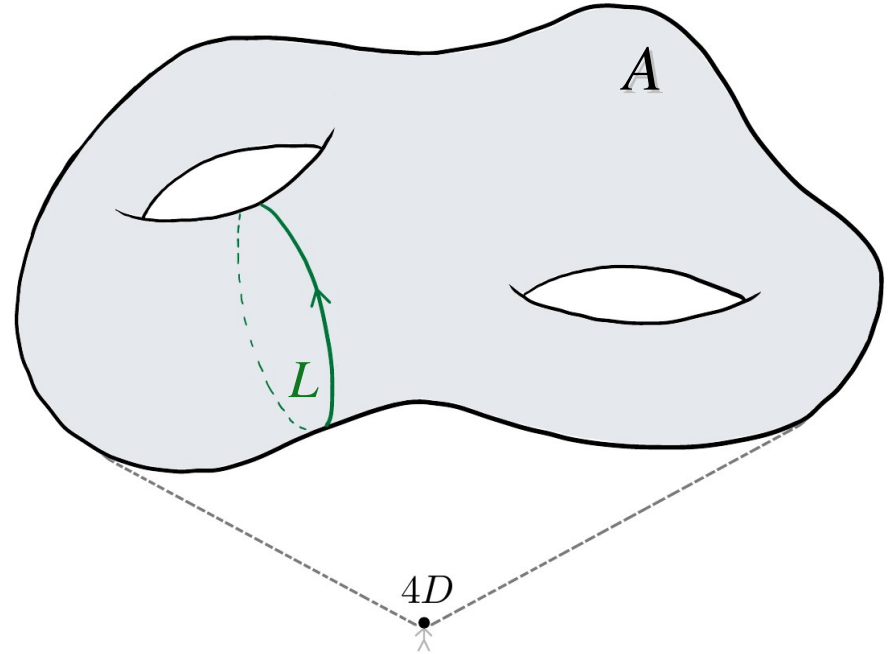
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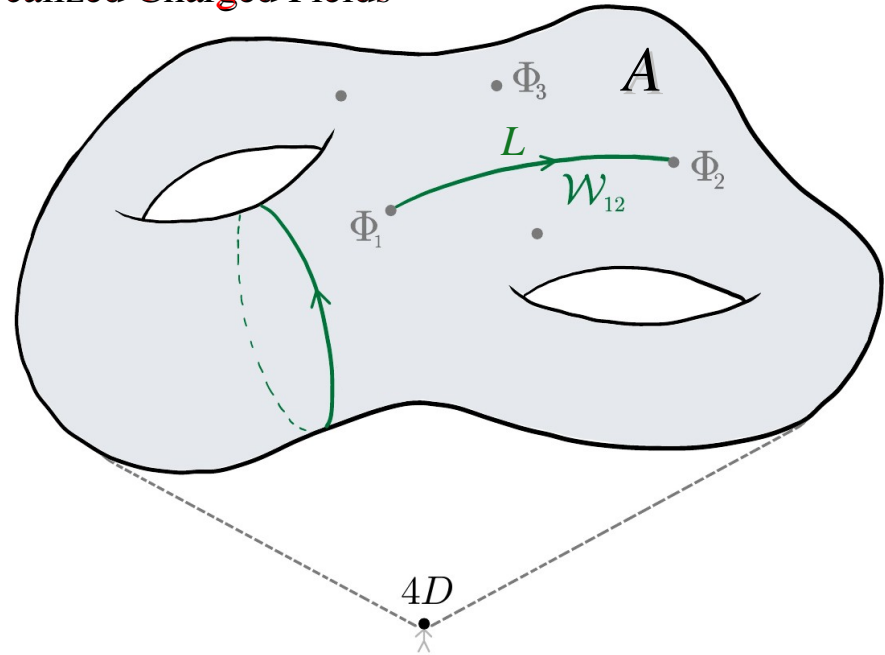
✗ post-inflationary axions

(PQ-phase restoration $\rightarrow$ D-branes after inflation...)



Open String Axiverse:

Gauge Fields in Extra Dimensions + **Localized Charged Fields**

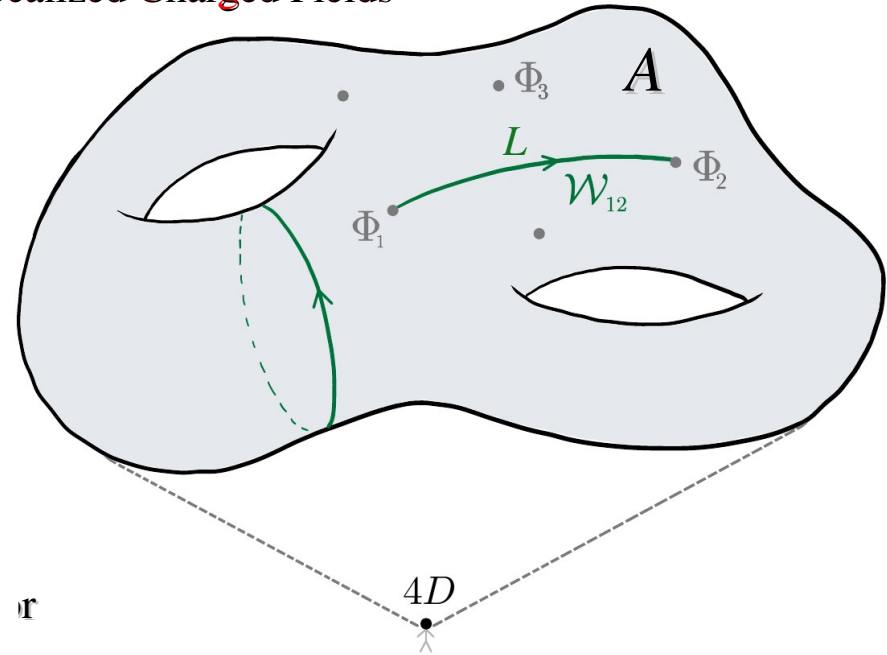


Open String Axiverse:

Gauge Fields in Extra Dimensions + **Localized Charged Fields**

$$\mathcal{W} = \Phi_+ e^{i \int_{y_+}^{y_-} A} \Phi_-$$

$$\text{gauge invariant: } \begin{cases} A \rightarrow A + \partial \Lambda \\ \Phi_{\pm} \rightarrow e^{\pm i \Lambda} \Phi_{\pm} \end{cases}$$



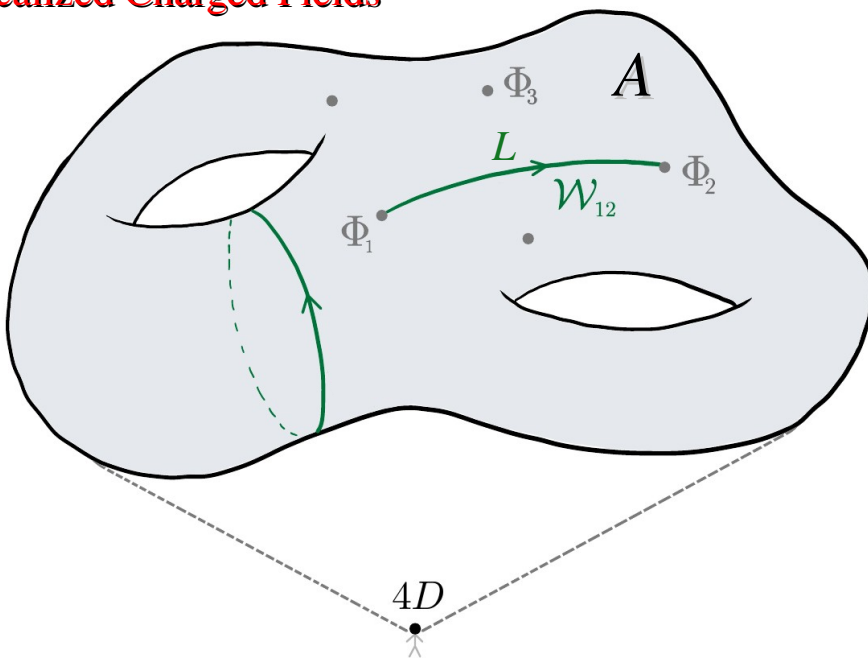
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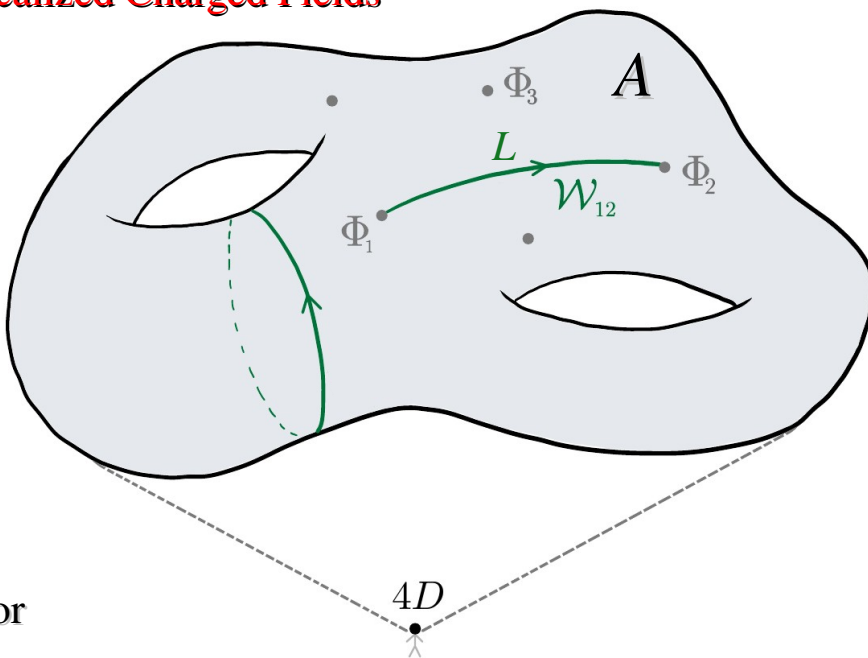
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Locally PQ = gauge transf.

→ no local PQ charged gauge inv. operator



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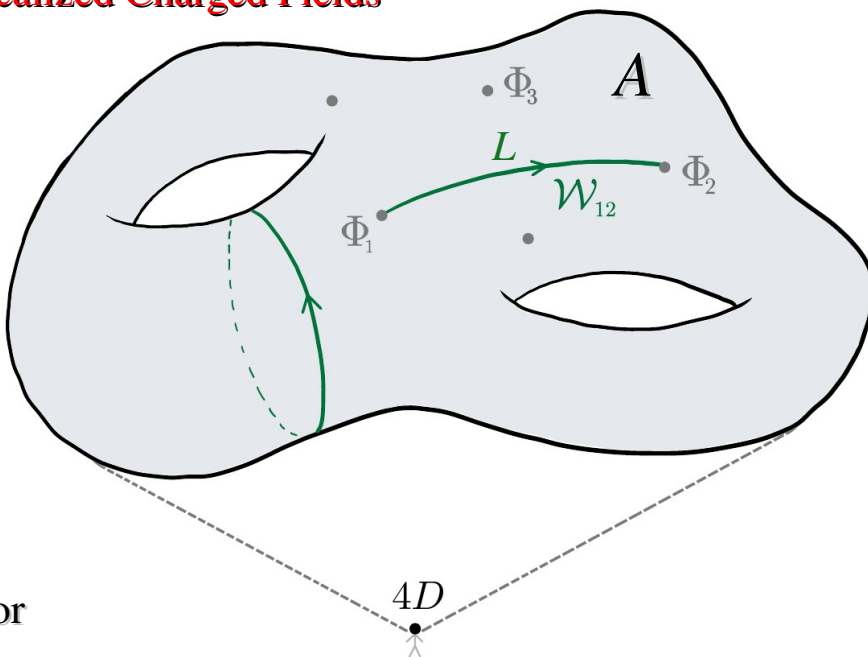
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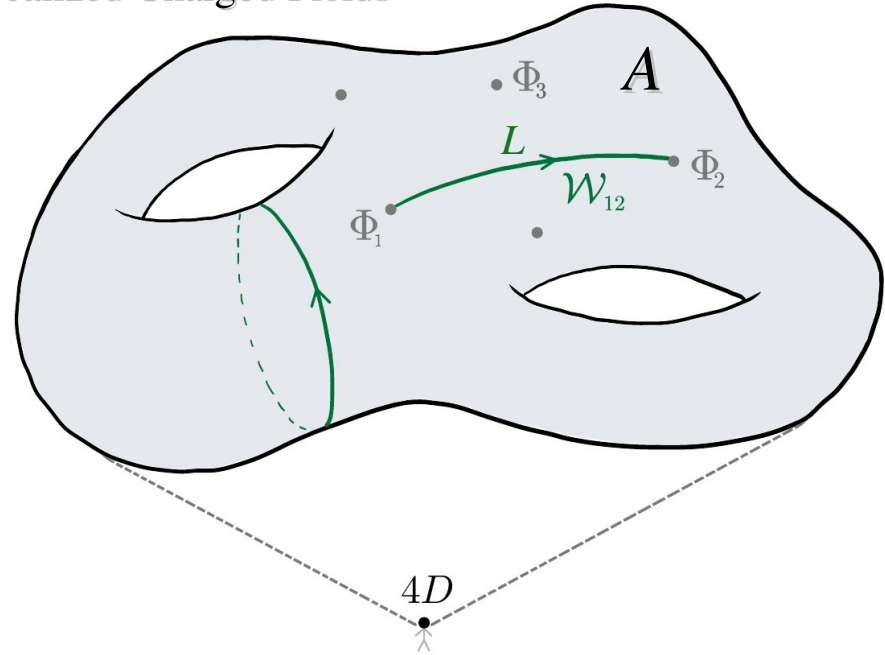
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Open String Axiverse:

Gauge Fields in Extra Dimensions + Localized Charged Fields

– With N localized fields $\rightarrow N - 1$ global U(1)s



Open String Axiverse:

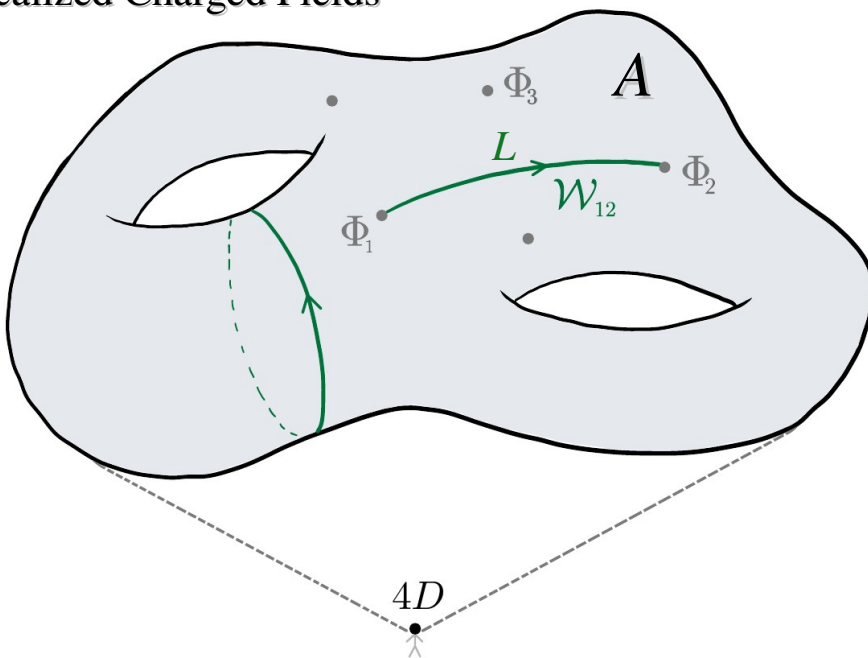
Gauge Fields in Extra Dimensions + Localized Charged Fields

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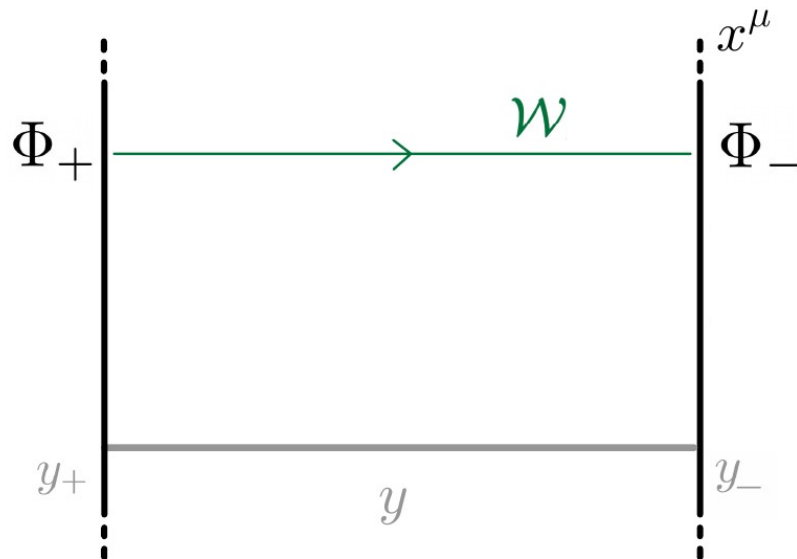
– PQ is linearly realized in 4D:

$$\frac{a}{v} = \arg \left(\Phi_+ e^{i \int_{y_+}^{y_-} A} \Phi_- \right)$$

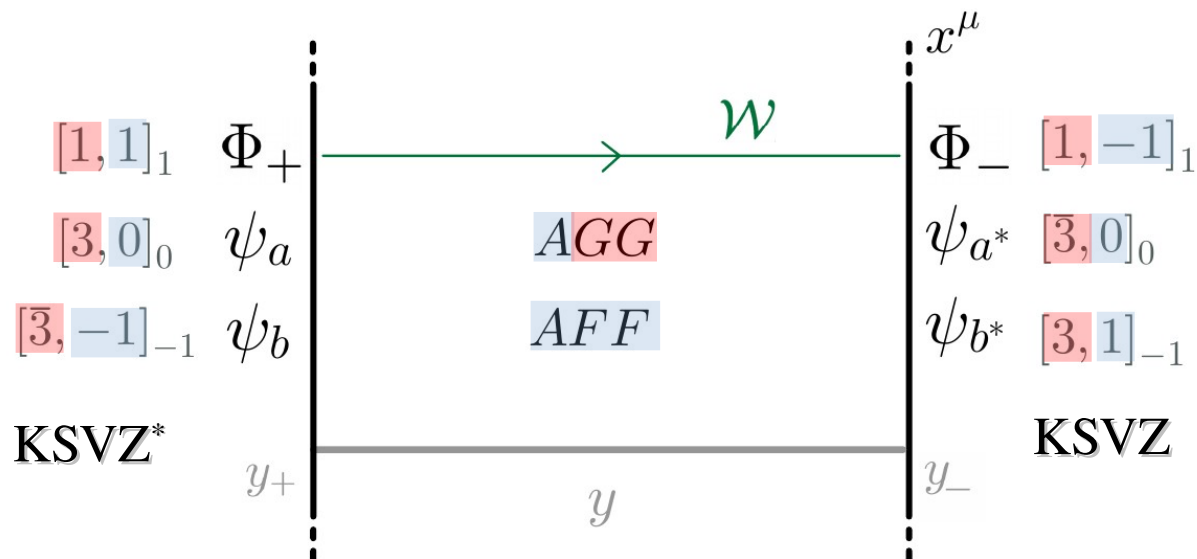
$$v \ll \frac{1}{L} \quad \text{if} \quad \min \langle \Phi_{\pm} \rangle \ll \frac{1}{L}$$



A 5D toy model:

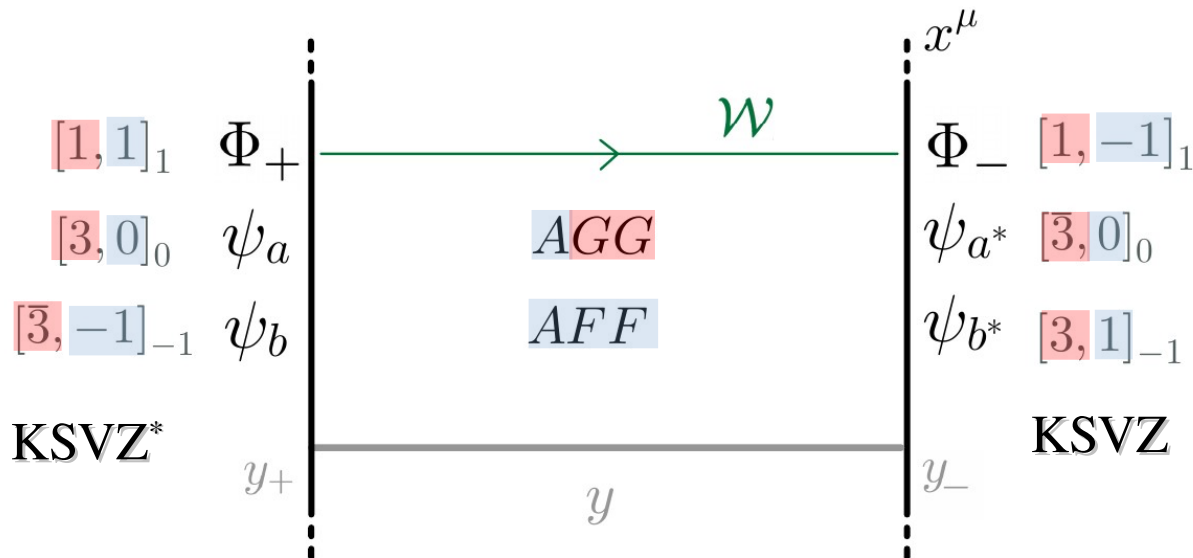


A 5D toy model:



Kim '79,
Shifman, Vainshtein, Zakharov '80

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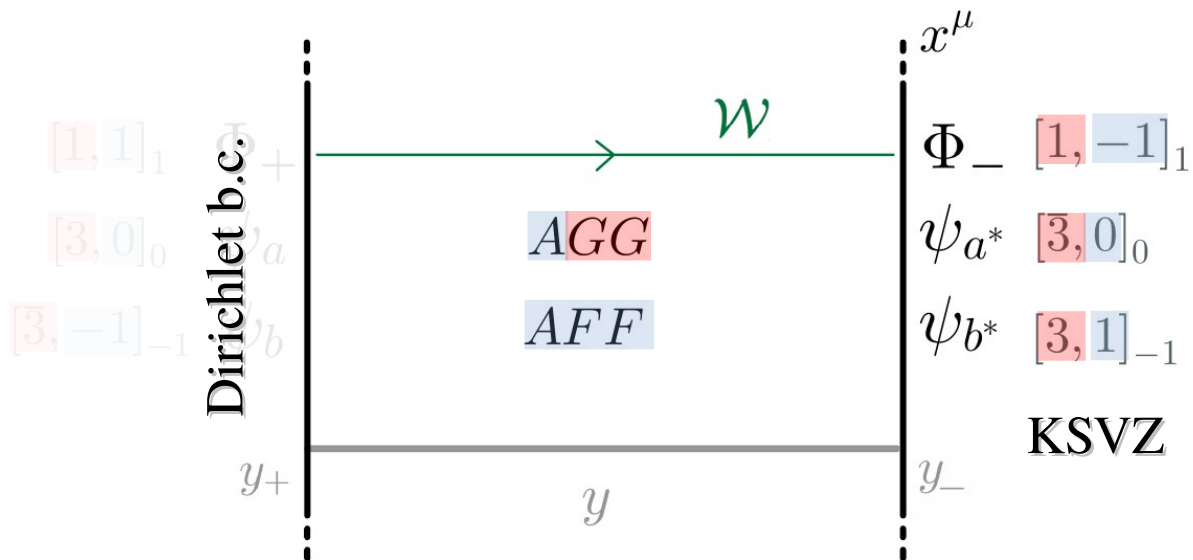


Kim '79,
Shifman, Vainshtein, Zakharov '80

- In the limit $v_- \ll (v_+, 1/L)$ minimal ($N_{\text{DW}} = 1$) KSVZ model recovered:
- L can be small so that all 4D KSVZ extensions work as usual: SUSY, GUT, exotics, ...

A 5D toy model:

NOTE: in the limit $v_+ \rightarrow \infty$



KK lifting of symmetries

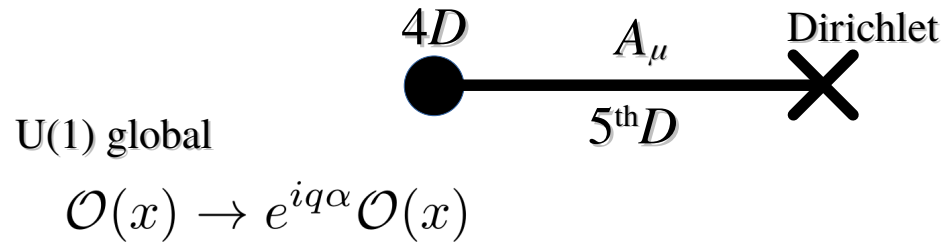
$4D$



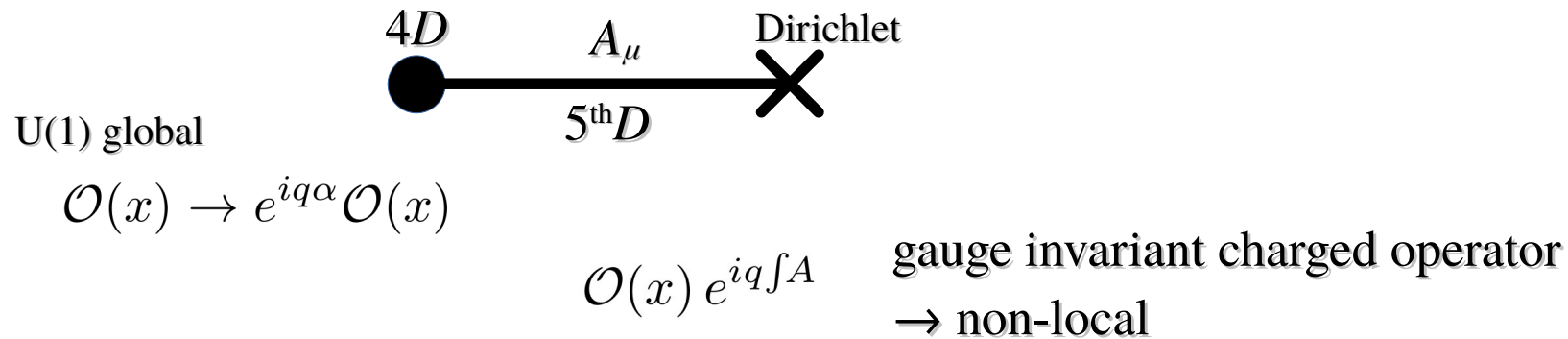
U(1) global

$$\mathcal{O}(x) \rightarrow e^{iq\alpha} \mathcal{O}(x)$$

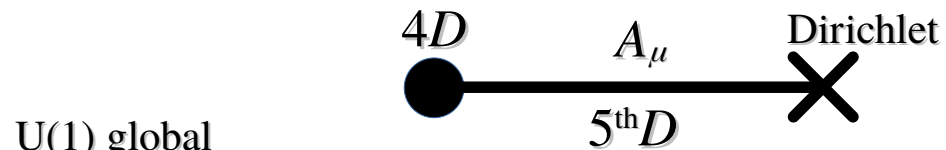
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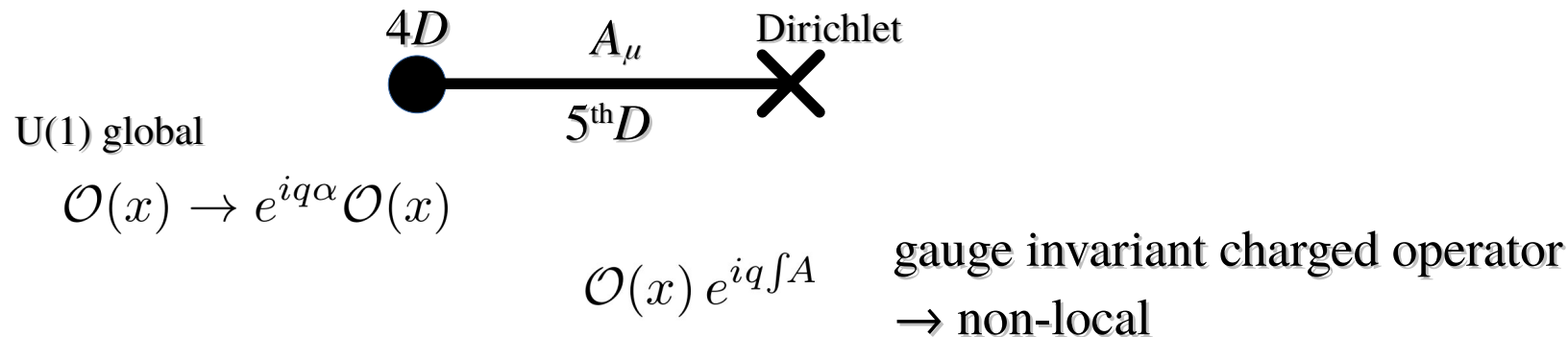
$$\mathcal{O}(x) \rightarrow e^{iq\alpha} \mathcal{O}(x)$$

$$\mathcal{O}(x) e^{iq\int A}$$

gauge invariant charged operator
 $\rightarrow$ non-local

$$\text{Breaking} \rightarrow e^{-ML}$$

KK lifting of symmetries

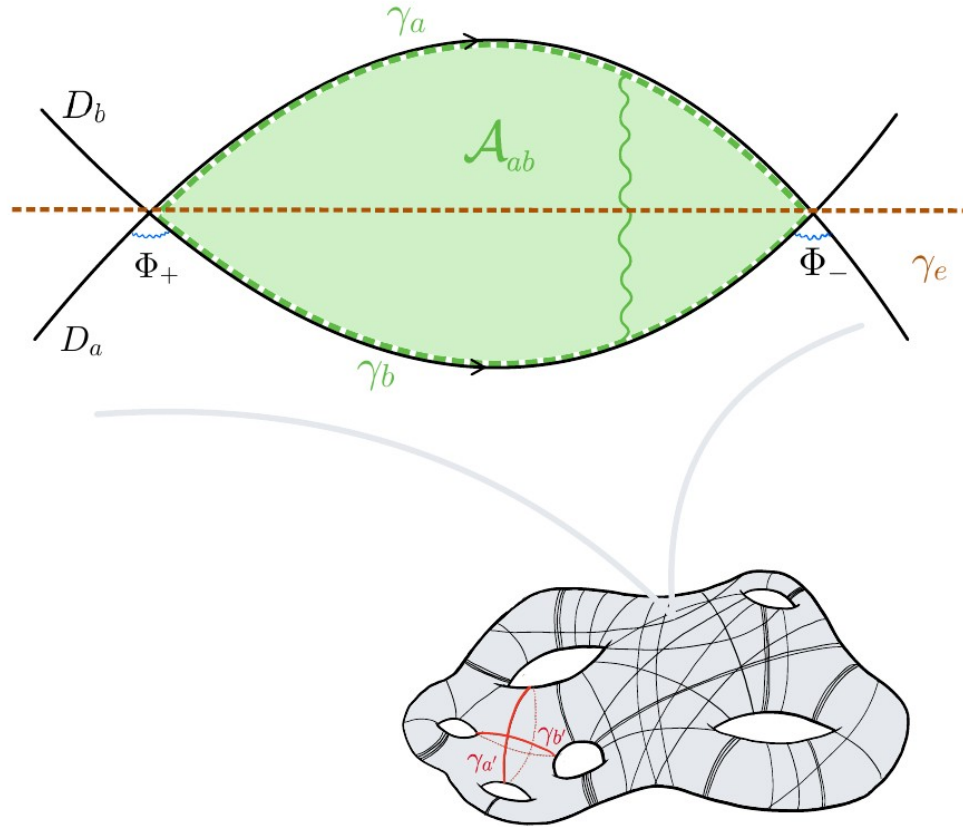


Breaking $\rightarrow e^{-ML}$

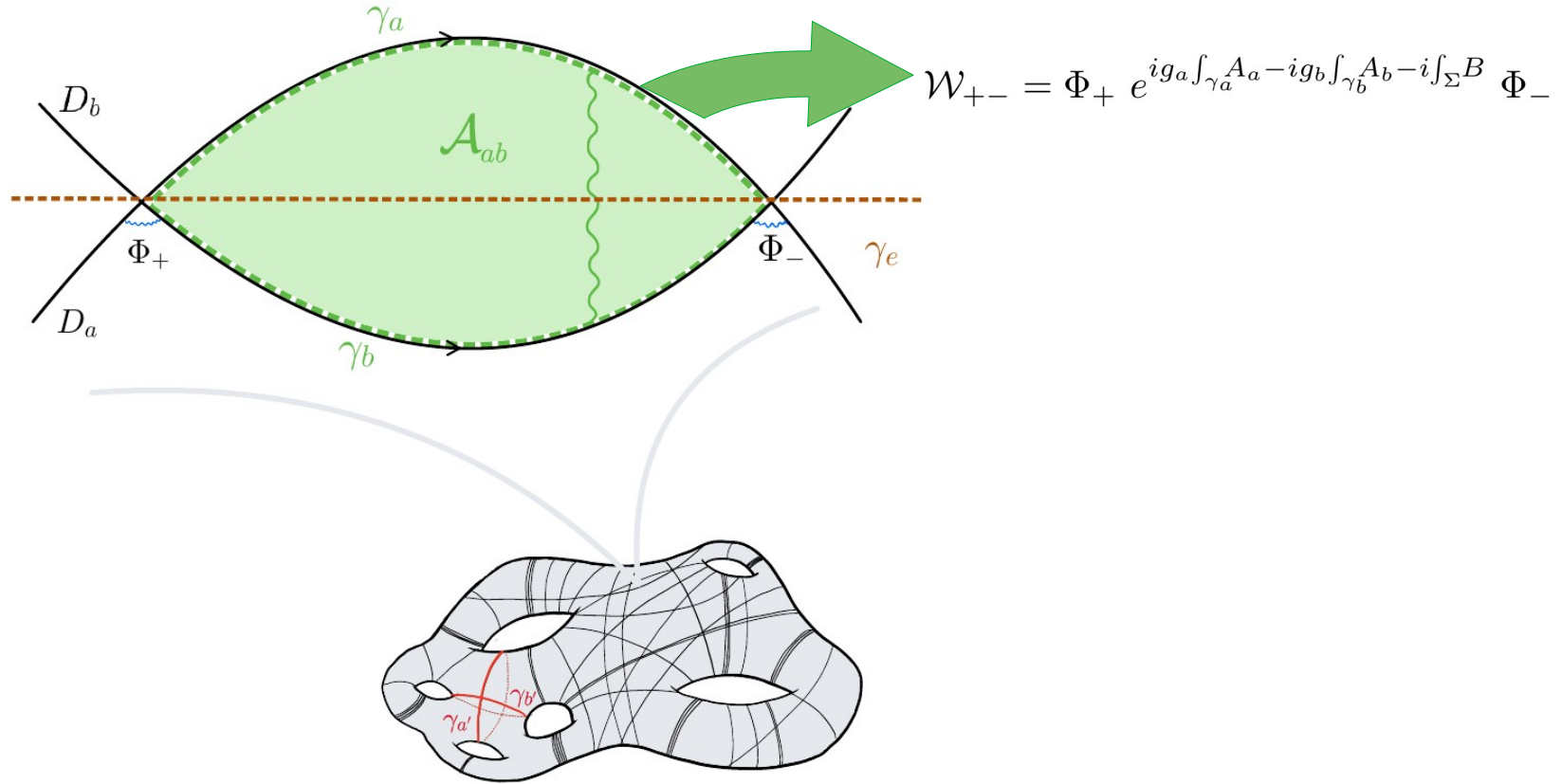
NOTE:

in 4D the global symmetry is not *accidental* but exponentially good

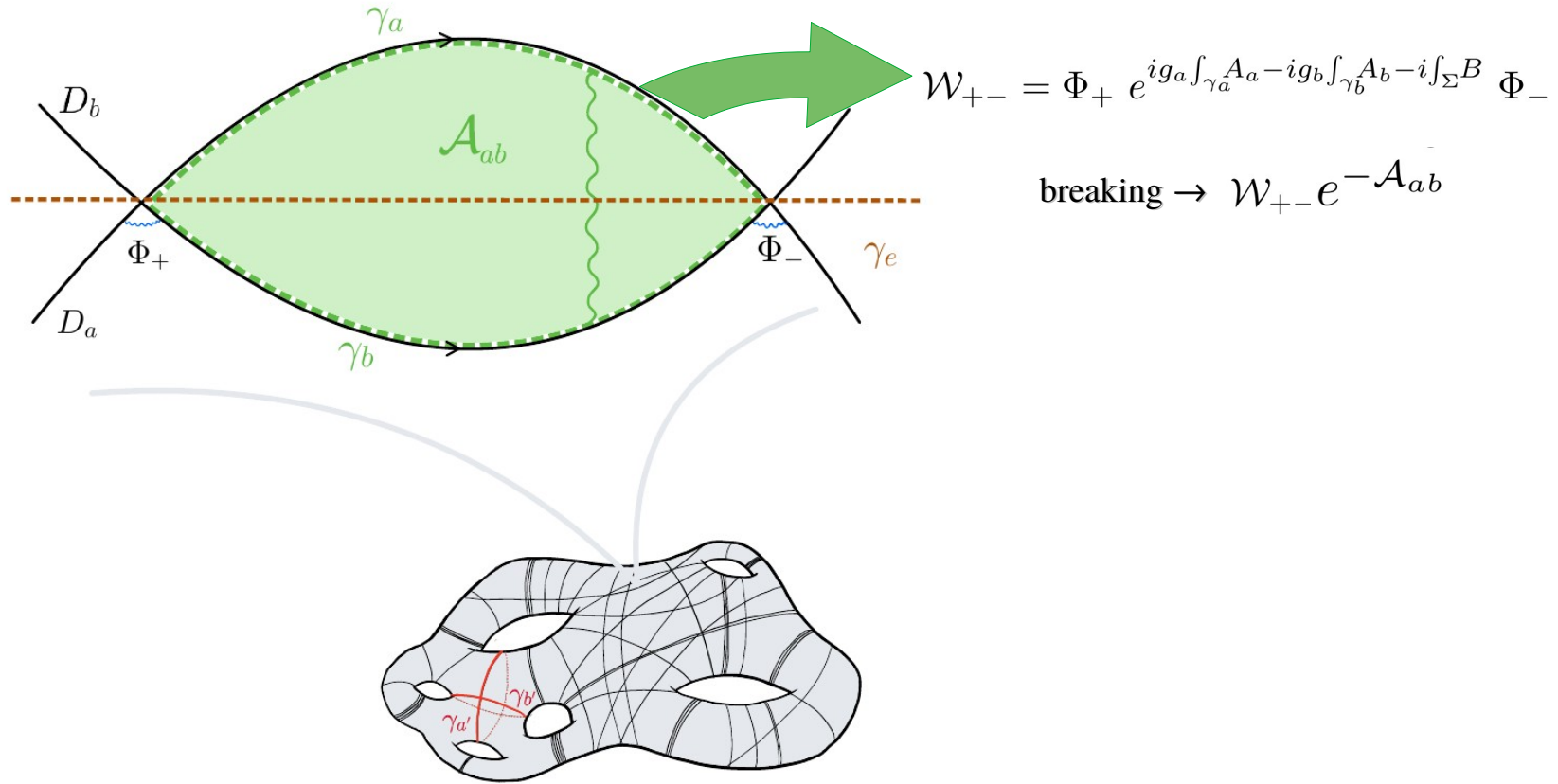
A simple string theory embedding



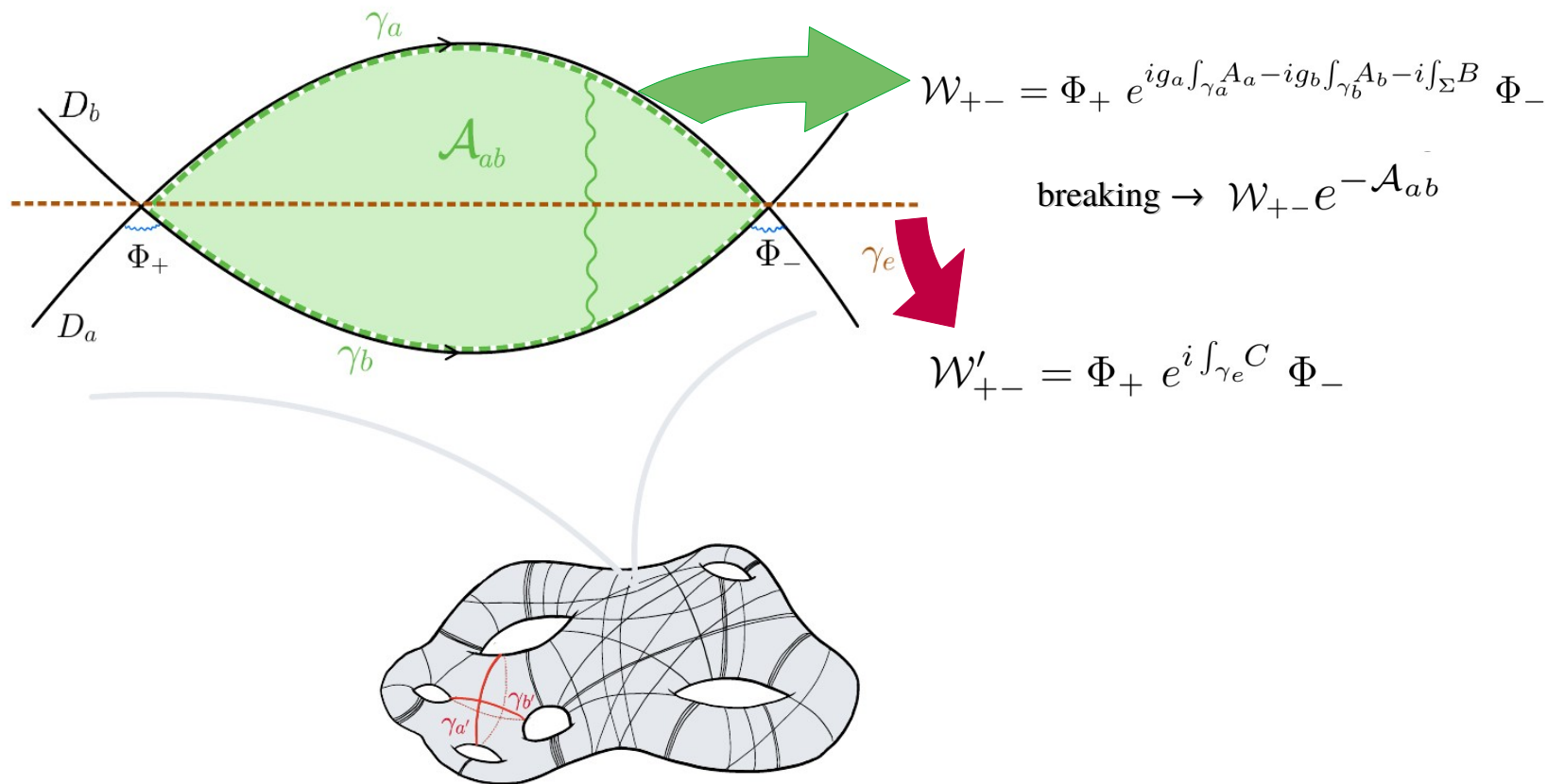
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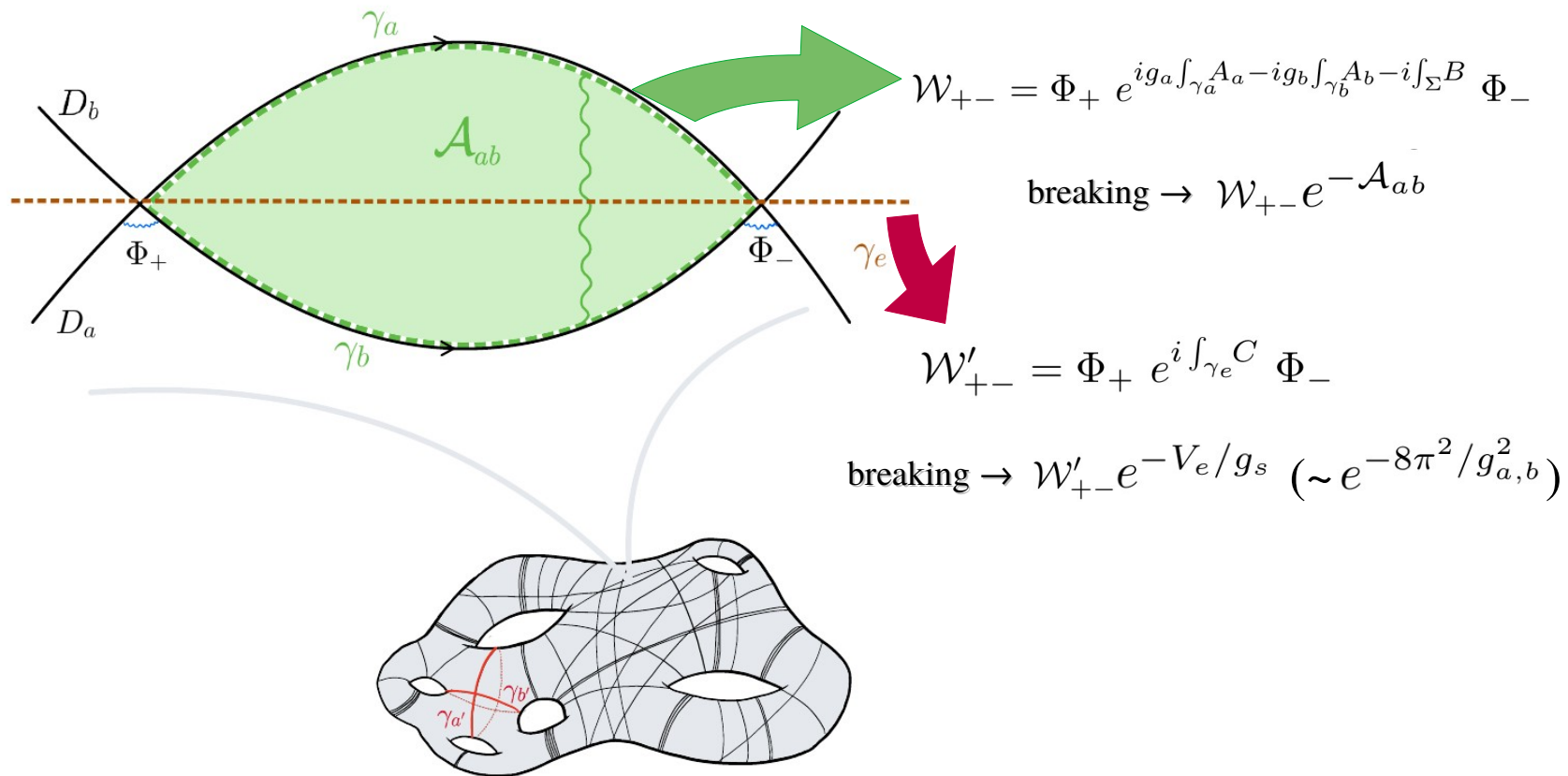
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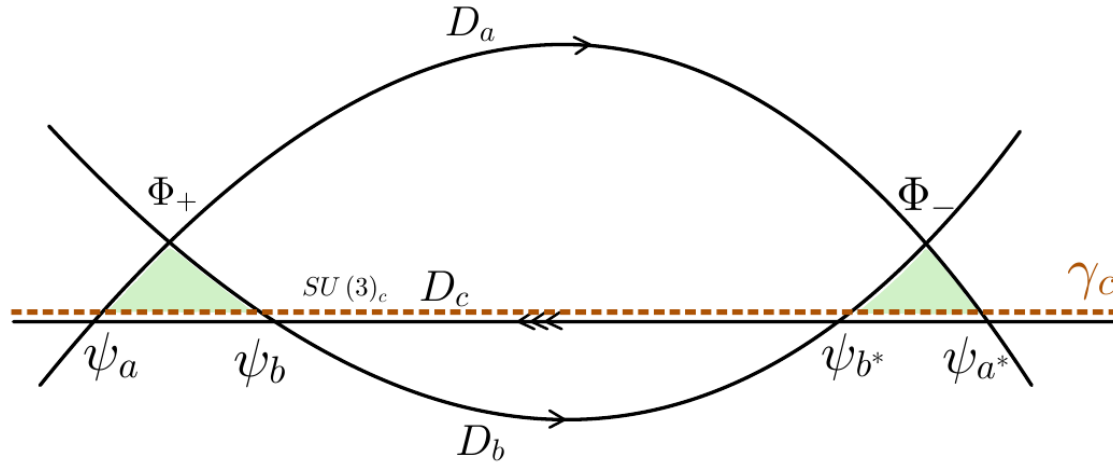
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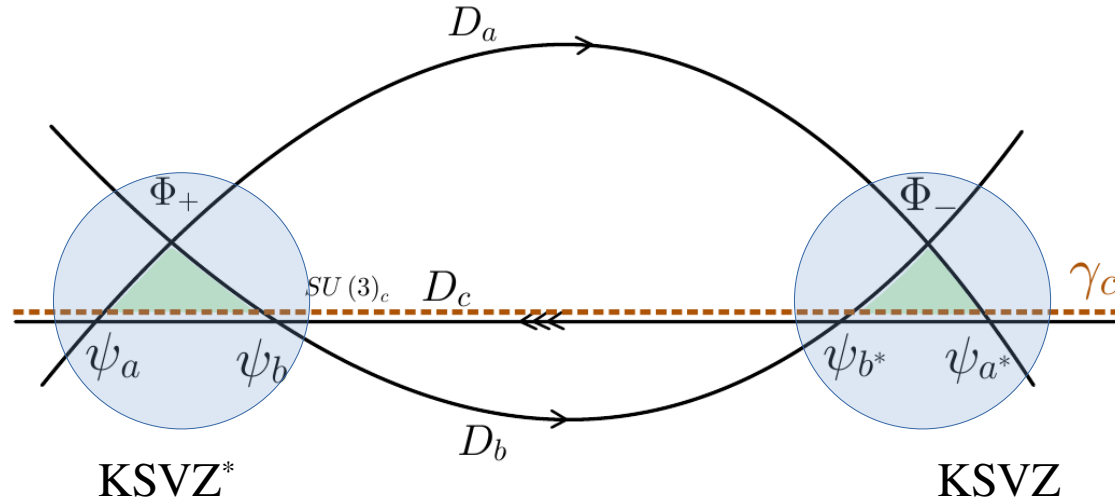
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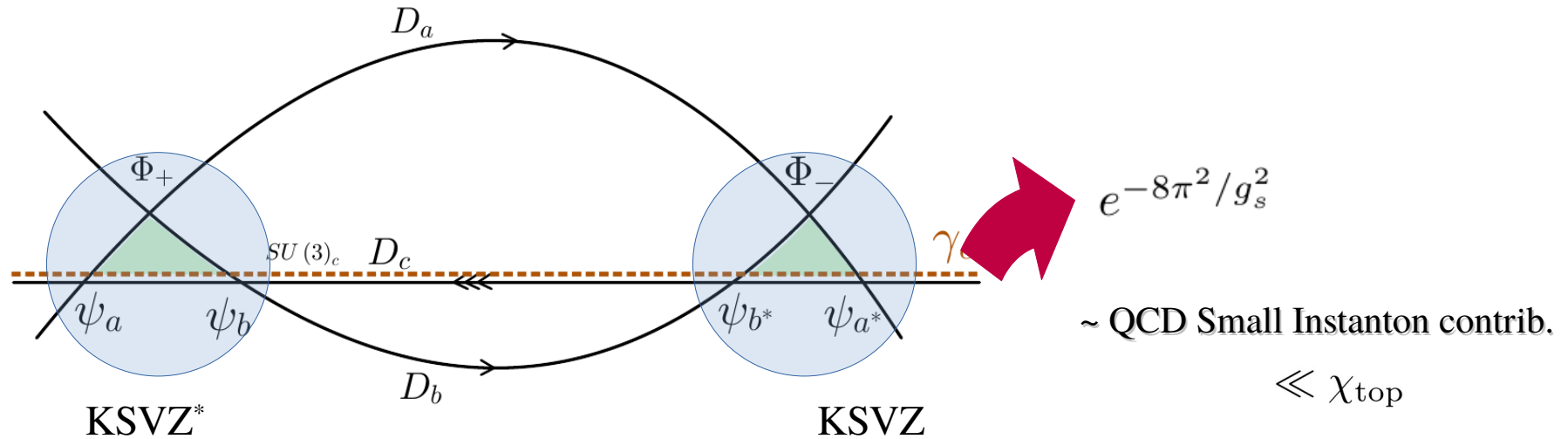
A simple string theory embedding of minimal KSVZ



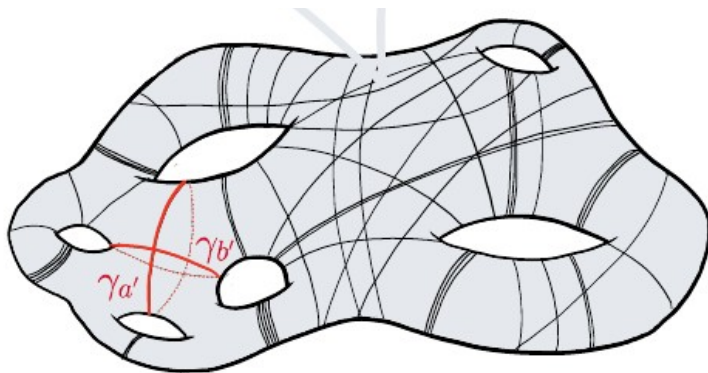
A simple string theory embedding of minimal KSVZ



A simple string theory embedding of minimal KSVZ



Open String Axiverse



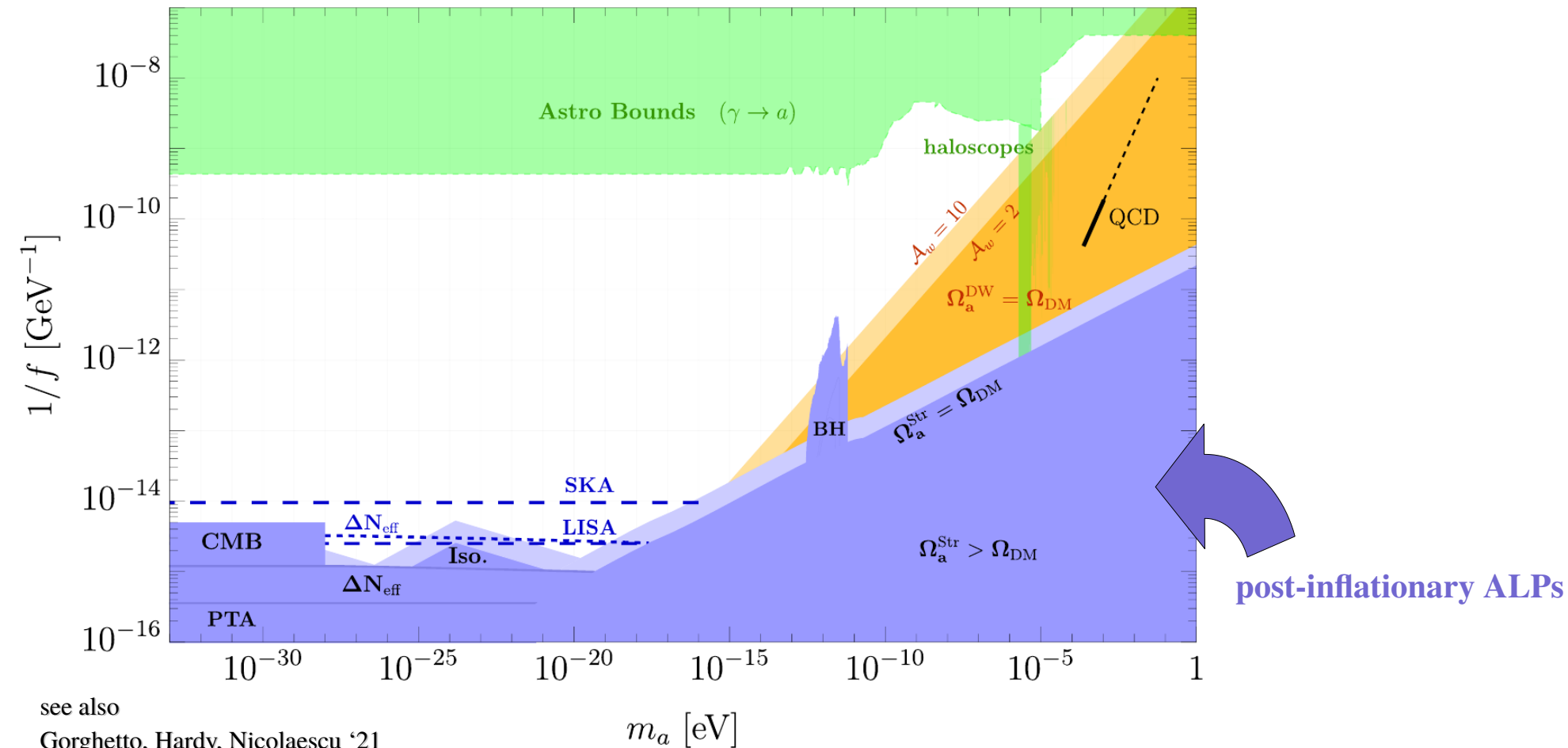
In realistic compactifications branes have multiple intersections

→ potentially multiple post-inflationary ALPs

see e.g. works of:

Allahverdi, Berenstein, Cicoli, Diaz, Dutta, Guidetti, Honecker, Klevers, Krippendorff, Mayrhofer, Perkin, Quevedo, Rummel, Sinha, Staessens, Valandro ...

Open String Axiverse Phenomenology

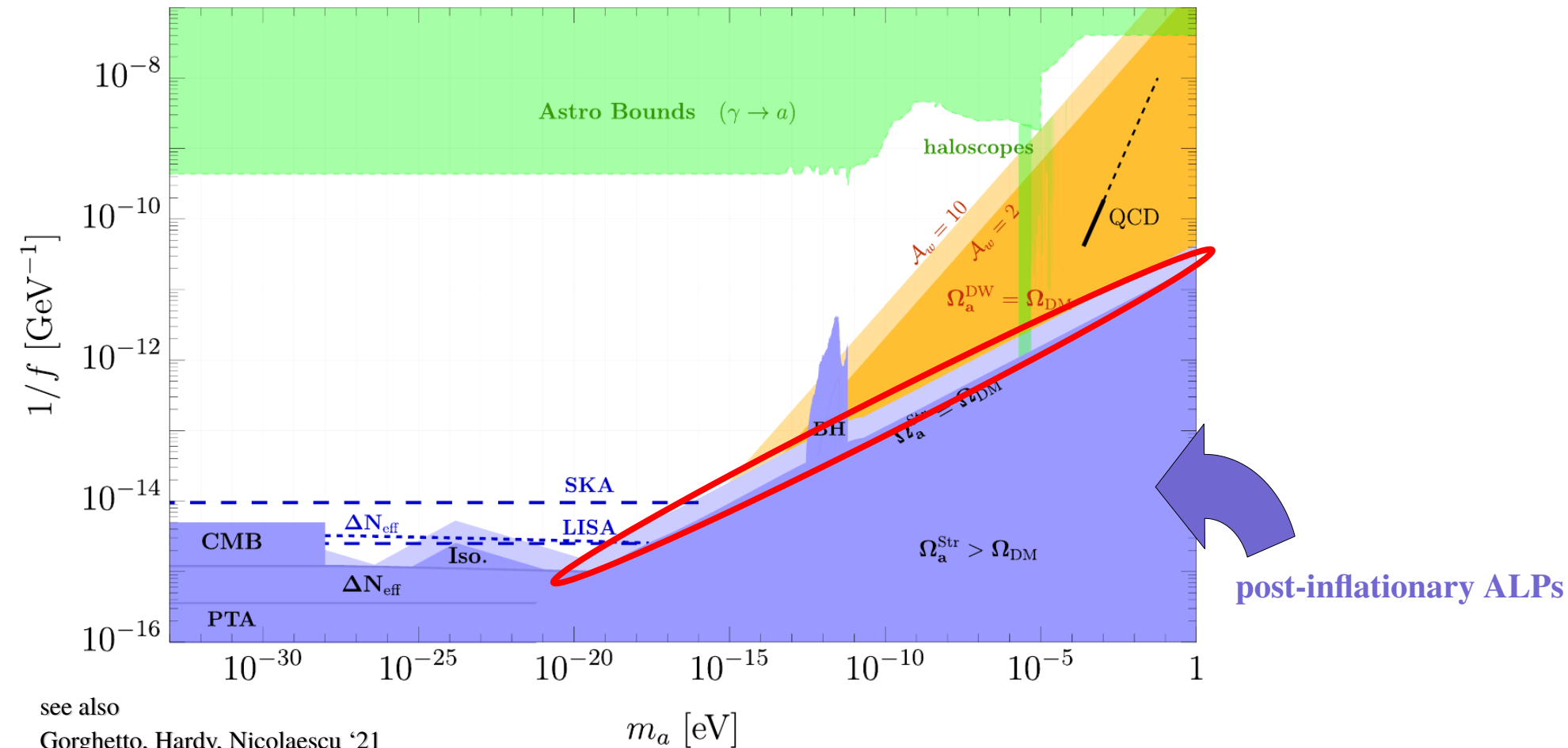


see also

Gorghetto, Hardy, Nicolaescu '21

Gorghetto, Hardy '22

Open String Axiverse Phenomenology

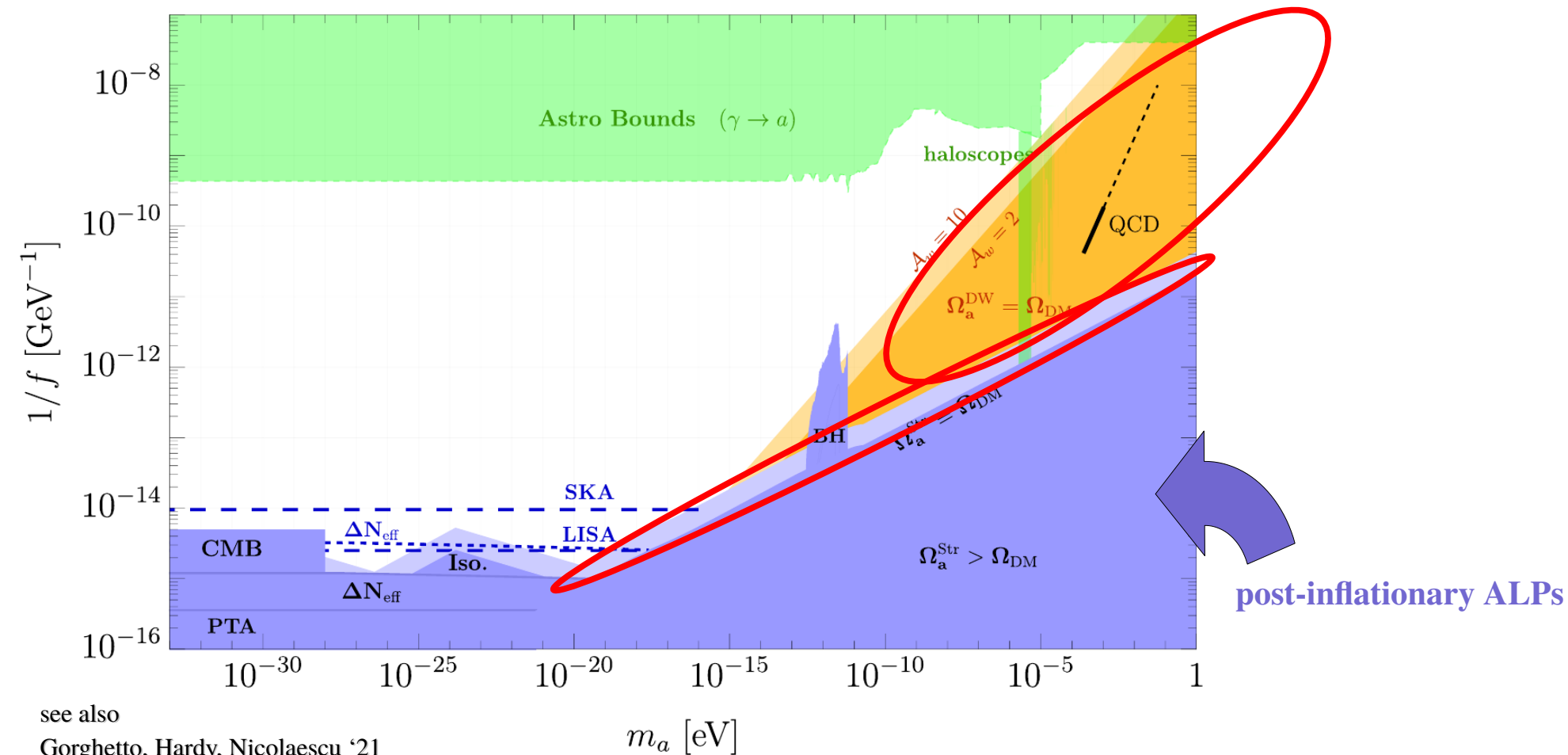


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Open String Axiverse Phenomenology

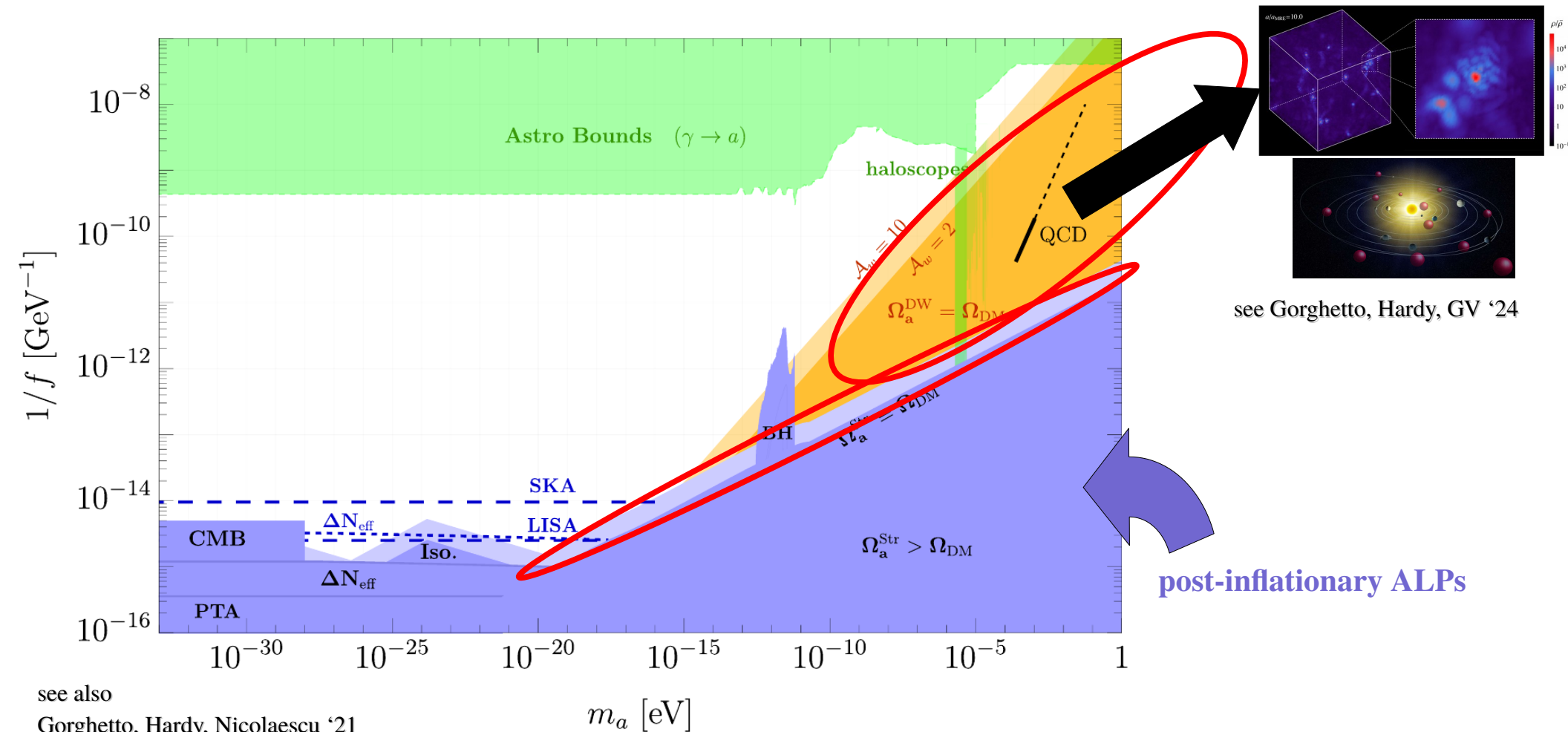


see also

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Open String Axiverse Phenomenology



see Gorghetto, Hardy, GV '24

post-inflationary ALPs

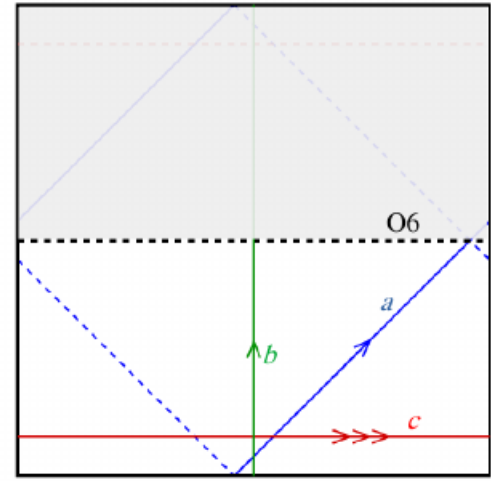
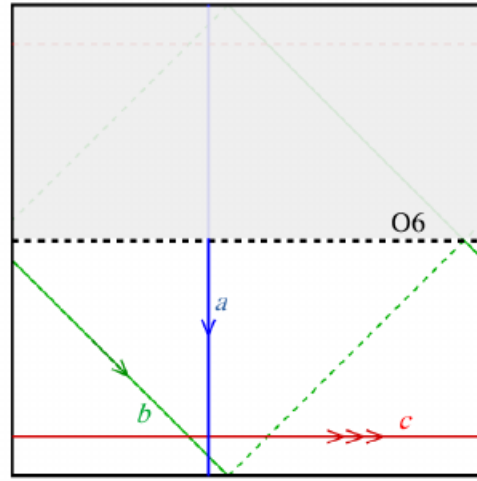
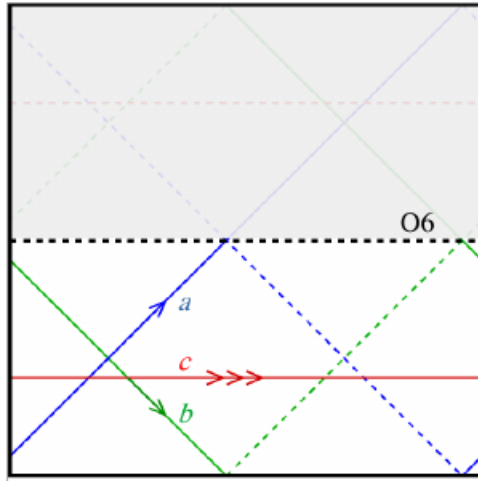
see also
Gorghetto, Hardy, Nicolaescu '21
Gorghetto, Hardy '22

Executive Conclusions

1. No problem between Quantum Gravity and HQ Symmetries
2. No fundamental obstruction to post-inflation QCD axions/ALPs
3. In fact it's generic → “open string axiverse”
4. New phenomenological opportunities

Thank You!

Back up



Example: SUSY cycles on T^6 compatible with (approx.) SUSY moduli stabilization