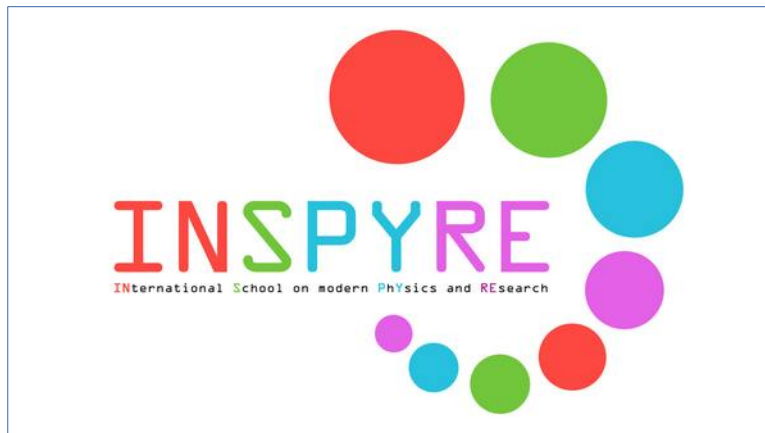




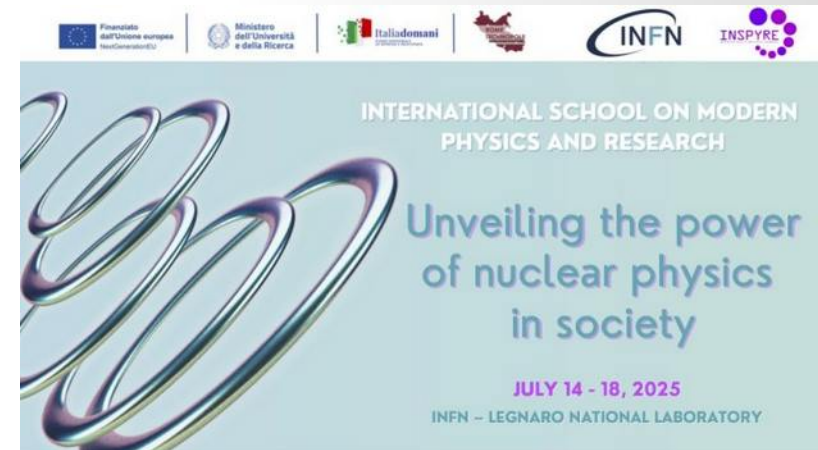
# “New aspects and properties of atomic nuclei using reactions with radioactive beams”

A contribution to the  
Inspyre 2025 School INFN LNL, Legnaro

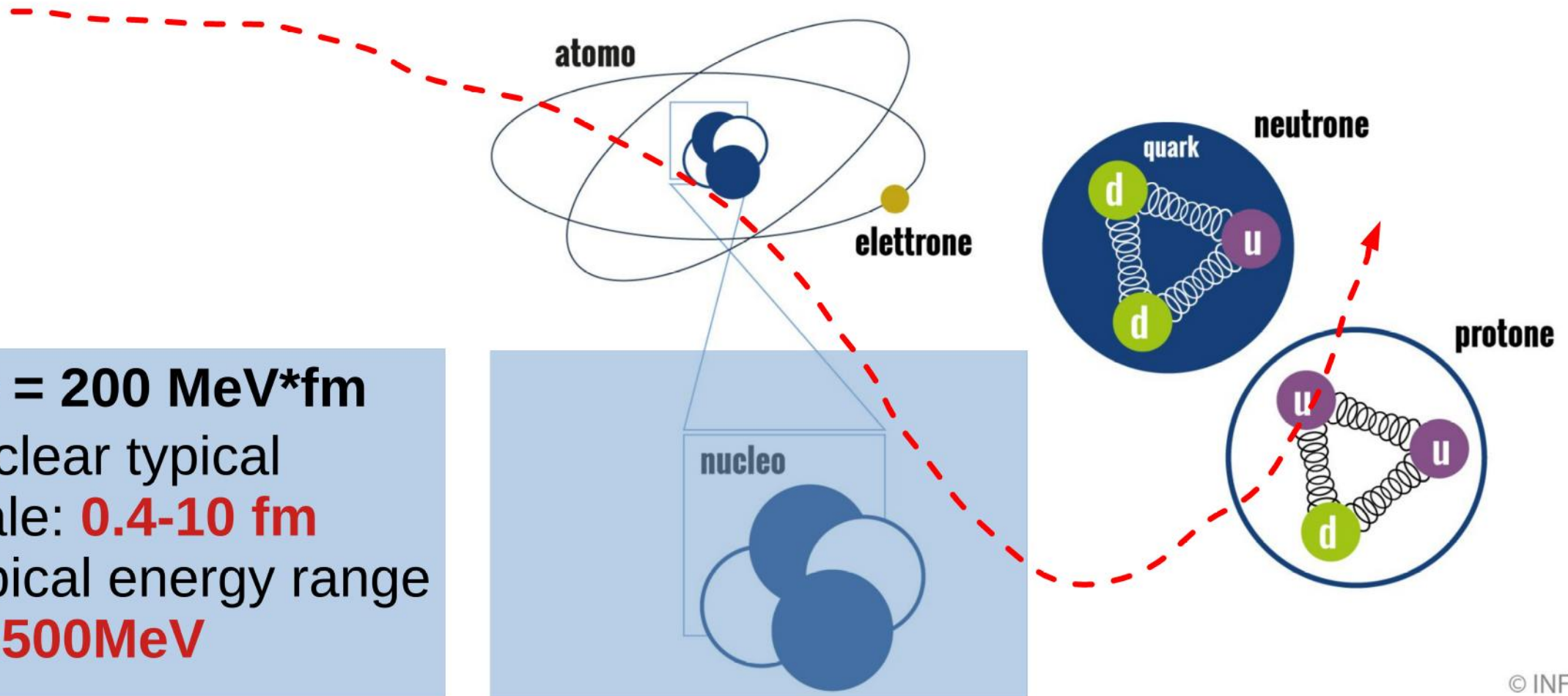
July 15-18 2025



Giovanni Casini  
INFN Sezione di Firenze



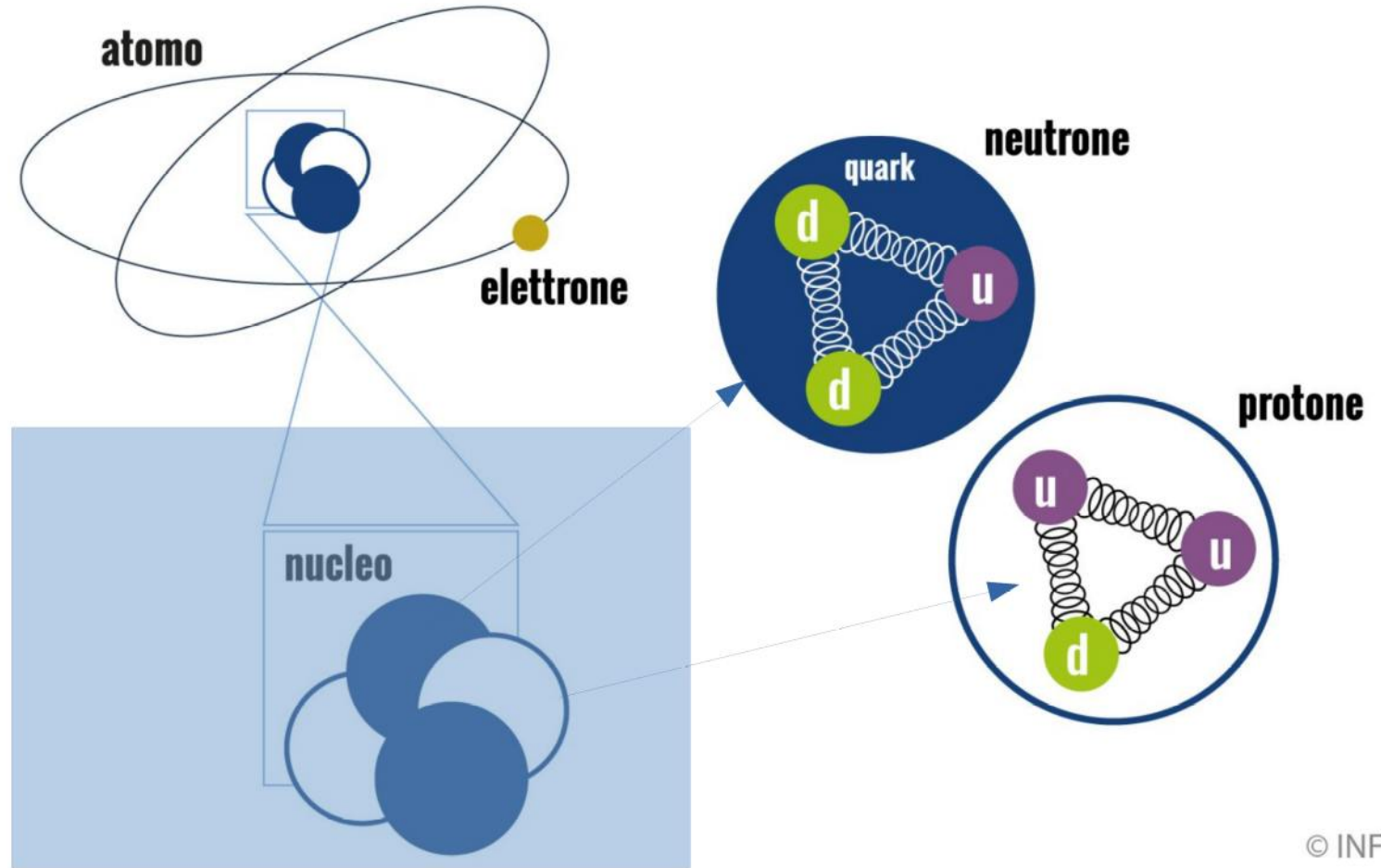
# “New aspects and properties of atomic nuclei using reactions with radioactive beams”



$\hbar c = 200 \text{ MeV} \cdot \text{fm}$   
Nuclear typical scale: **0.4-10 fm**  
Typical energy range **20-500 MeV**



# “New aspects and properties of atomic nuclei using reactions with radioactive beams”



**Last 40 years  
(anniversary!) of  
studies changed and  
are changing the  
nuclear Physics  
textbooks**

# An adventure in a Canyon region

Grand Canyon, USA



Jebel Shams Canyon, OMAN



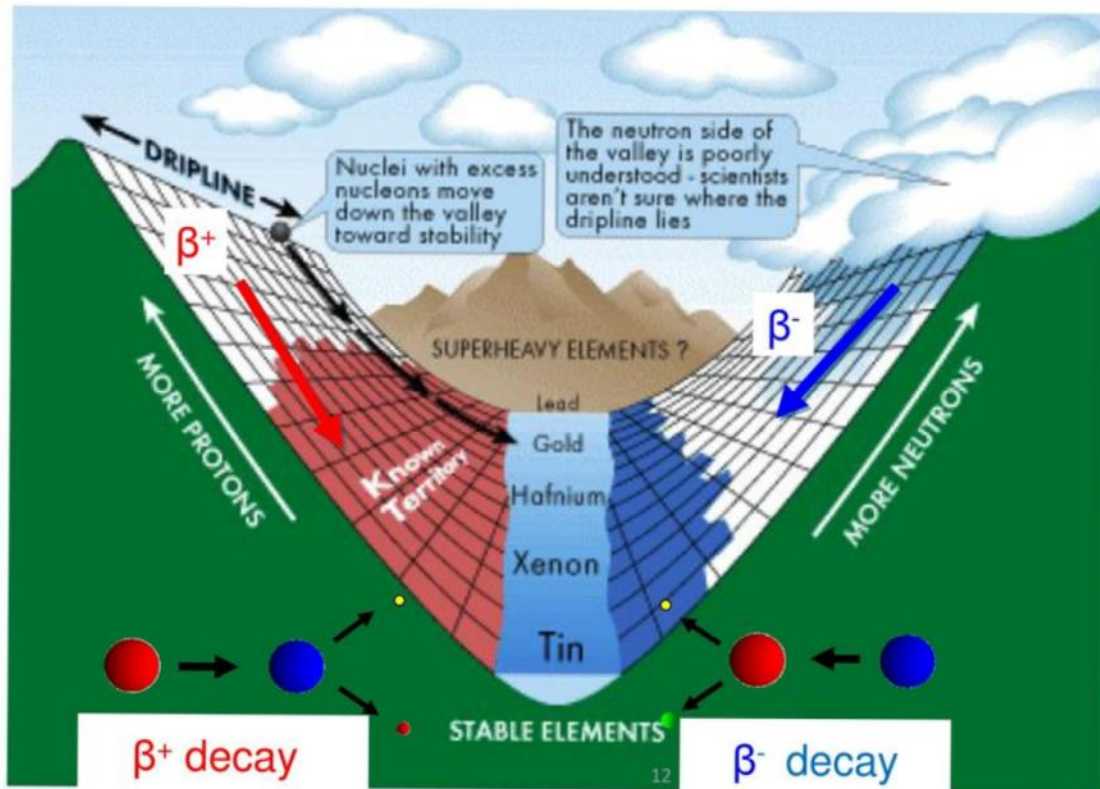
From an old conversation with my colleague Nanni Pollarolo

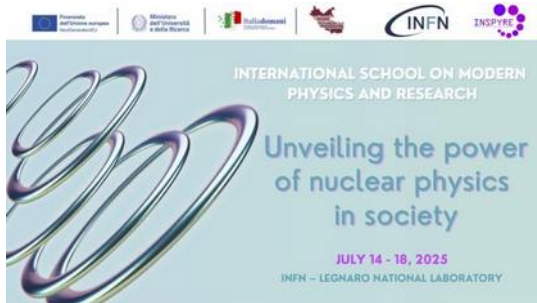


# The nuclear Canyon: the action of the nuclear potential

## Valley of stability

Jebel Shams Canyon, OMAN



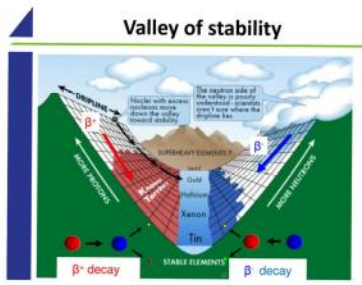


# Summary

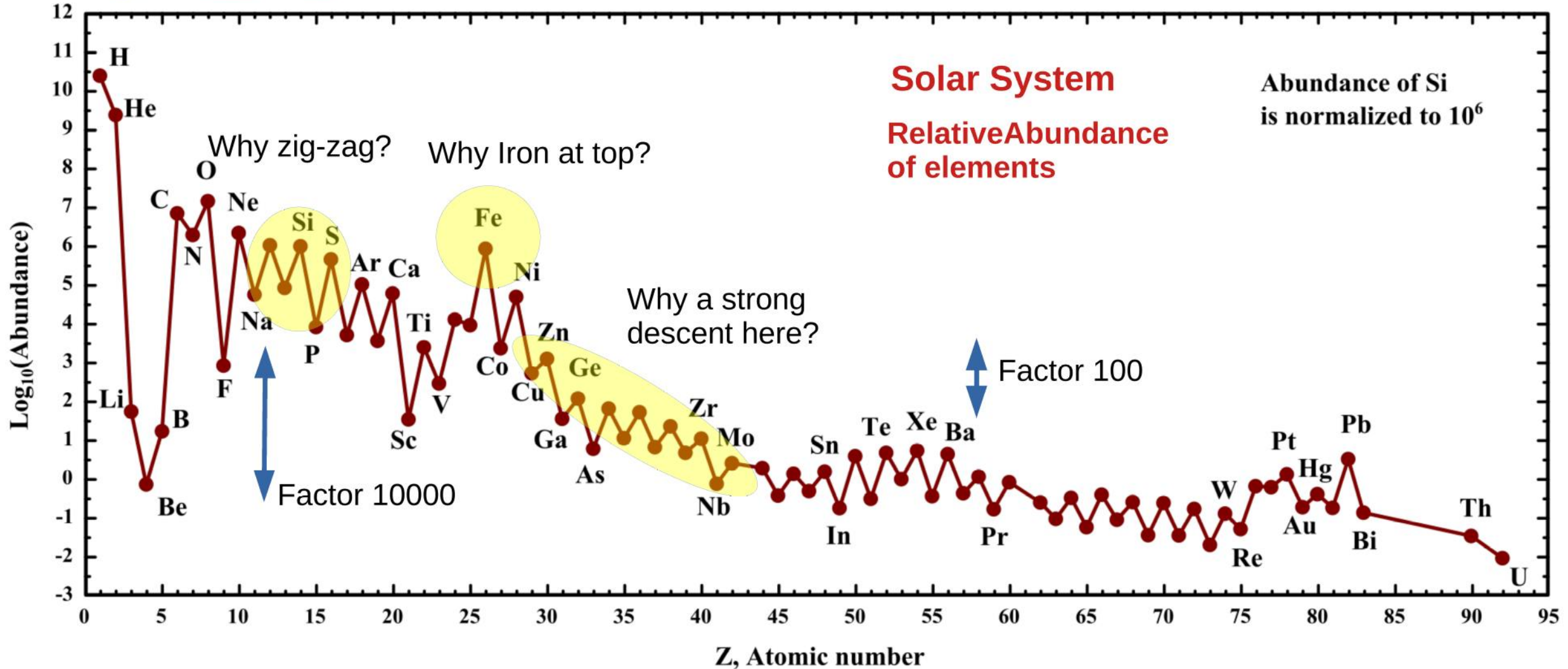
- 1900-1980 Nuclear physics, down in the canyon (stability)
- Where/How Nature explores the whole landscape
- 1980-now: exotic beam facilities and the journey far from stability
- Physics cases, fascinating nuclei







# Masses, bonds, stability, abundances



# Nuclear mass $m$ and binding energy

$$m = Zm_p + Nm_n - \frac{E_B}{c^2}$$

final total mass = mass of components - Binding energy ( $E_B$ )

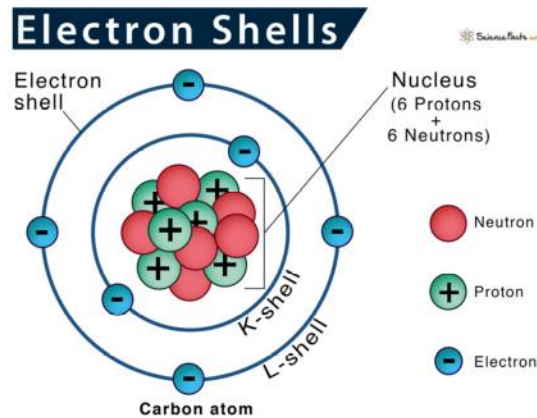
- Equivalence  $mc^2=E$
- “To bind” means transforming part of the mass in energy.
- Binding energy and mass excess (change of sign plus-minus)
- Valid for every bound systems in nature

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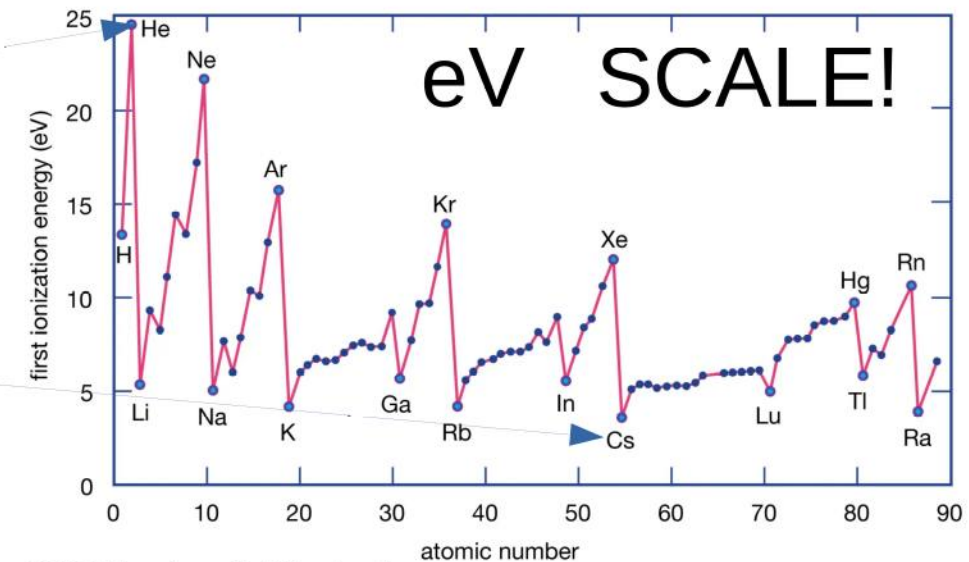
- Equivalence  $mc^2=E$
- “To bind” means transforming part of the mass in energy.
- Binding energy and mass excess (change of sign plus-minus)
- Valid for every bound systems in nature



Noble elements: last electrons deeply bound

Alcaline elements: last electron almost free

**EXAMPLE: ATOMIC SYSTEMS and the world of CHEMISTRY**



# Nuclear mass $m$ and binding energy

$$m = Zm_p + Nm_n - \frac{E_B}{c^2}$$

final total mass = mass of components - Binding energy ( $E_B$ )

- Equivalence  $mc^2=E$
- “To bind” means transforming part of the mass in energy.
- Binding energy and mass excess (change of sign plus-minus)
- Valid for every bound systems in nature

Various contributions of the nuclear potential produce the binding energy and thus the nuclear masses:

$$E_B = a_V A - a_S A^{2/3} - a_C \frac{Z(Z-1)}{A^{1/3}} - a_A \frac{(A-2Z)^2}{A} + \delta(A, Z)$$

volume

+

surface

-

Electric energy  
(Coulomb potential)

-

Symmetry energy  
(neutron-proton symmetry)

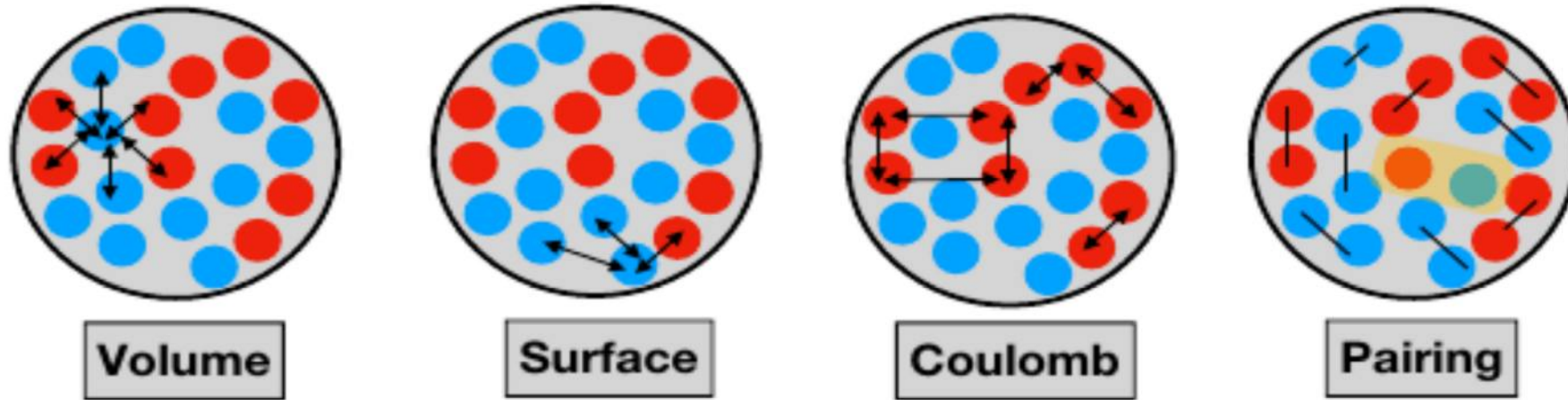
-

Pairing term

+



# Nuclear mass $m$ and binding energy



Many contributions of the nuclear potential produce the binding energy and thus the nuclear masses:

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volume

+

surface

-

Electric  
(Coulomb potential)

-

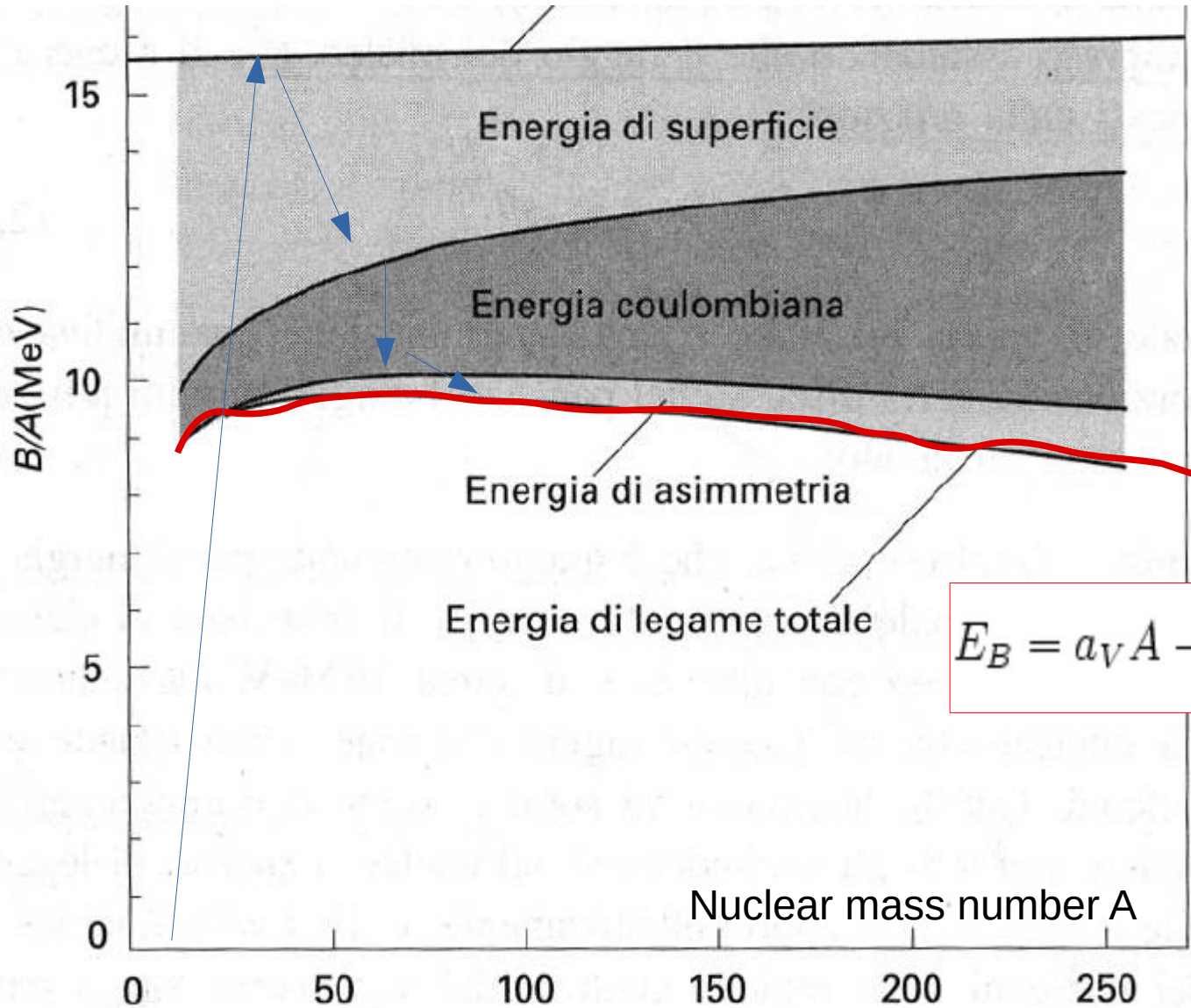
Symmetry energy  
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-

Pairing term

+/-

# Various contributions to $E_B$ (or $B/A$ , MeV scale)

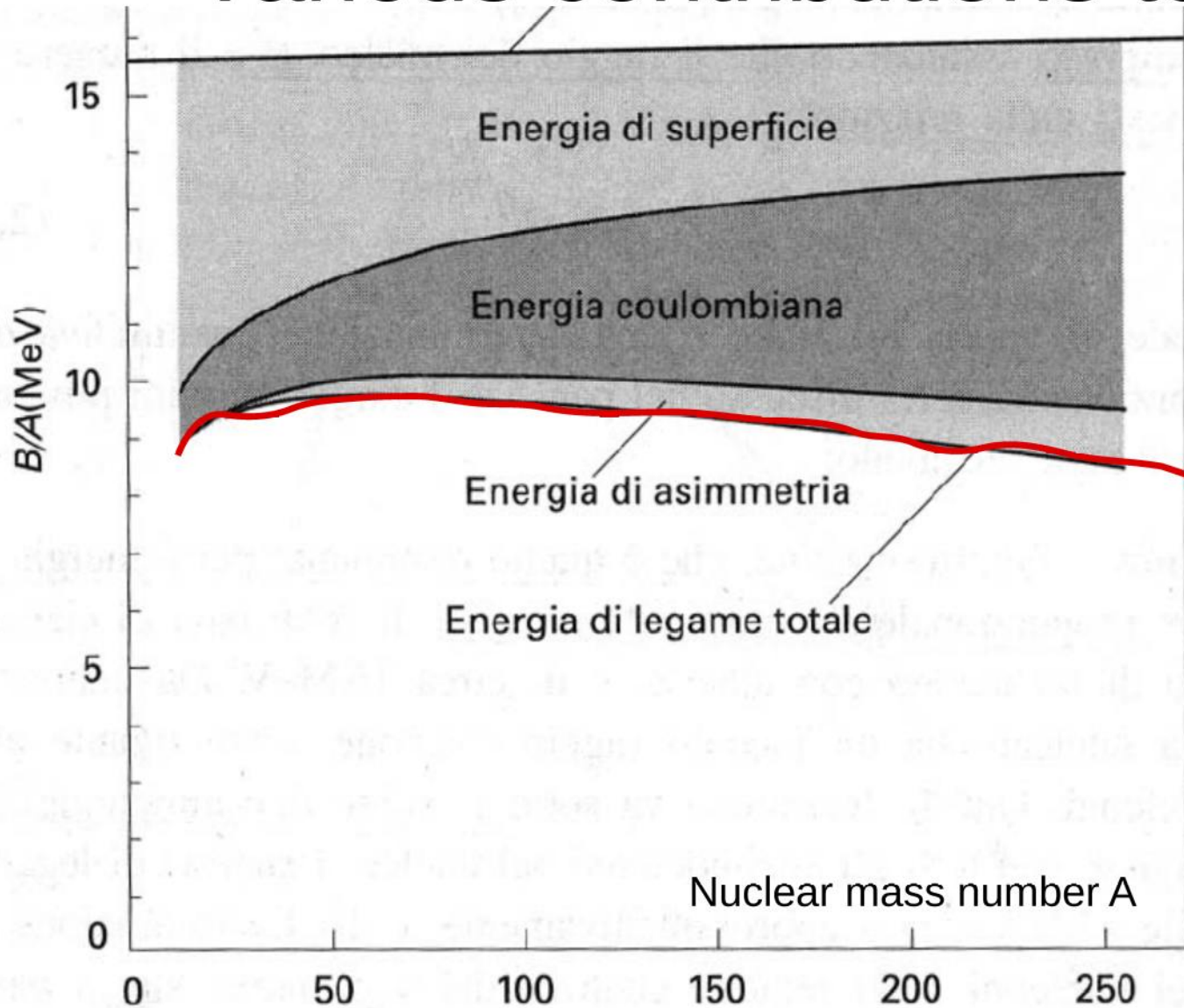


**90 years of predictions**  
 Semi-empirical nuclear mass  
 formula  
 Von Weizsäcker, 1935

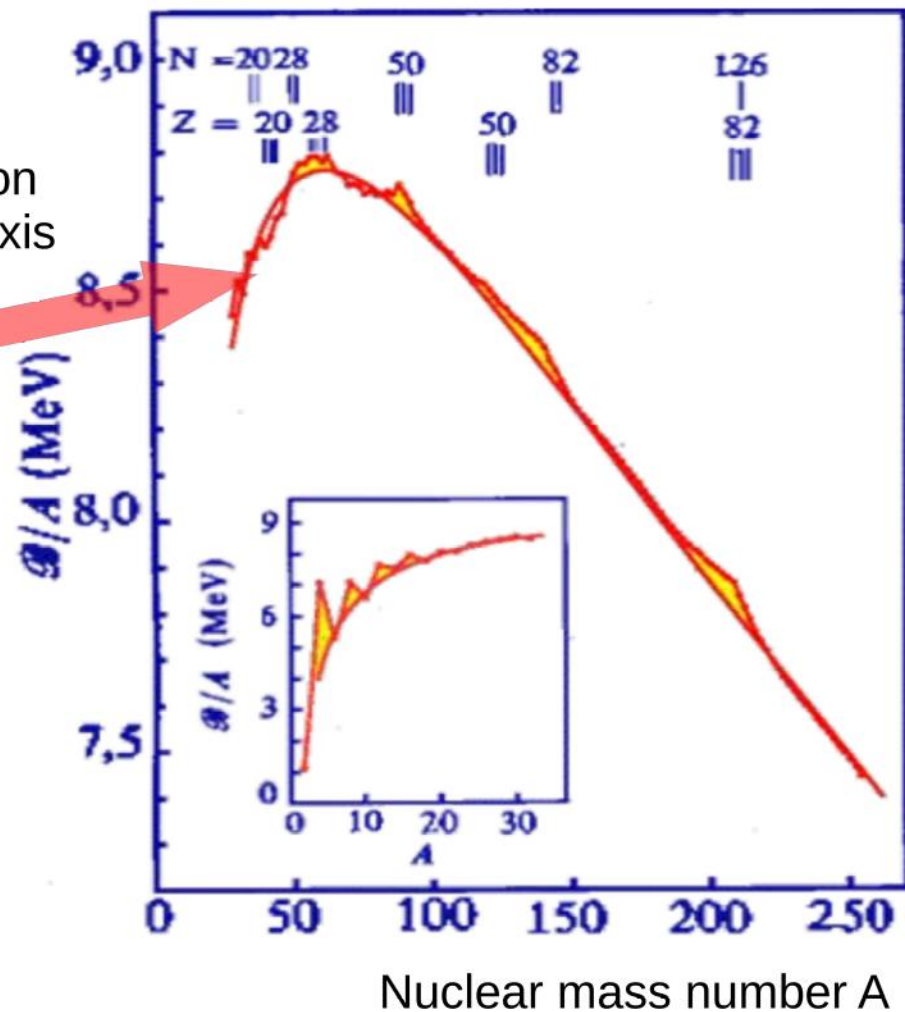
$$E_B = a_V A - a_S A^{2/3} - a_C \frac{Z(Z-1)}{A^{1/3}} - a_A \frac{(A-2Z)^2}{A} + \delta(A, Z)$$

$$\delta(A, Z) = \begin{cases} +\delta_0 & Z, N \text{ even (A even)} \\ 0 & A \text{ odd} \\ -\delta_0 & Z, N \text{ odd (A even)} \end{cases} \quad \delta_0 = \frac{a_P}{A^{1/2}}$$

# Various contributions to $E_B$ (or $B/A$ , MeV scale)

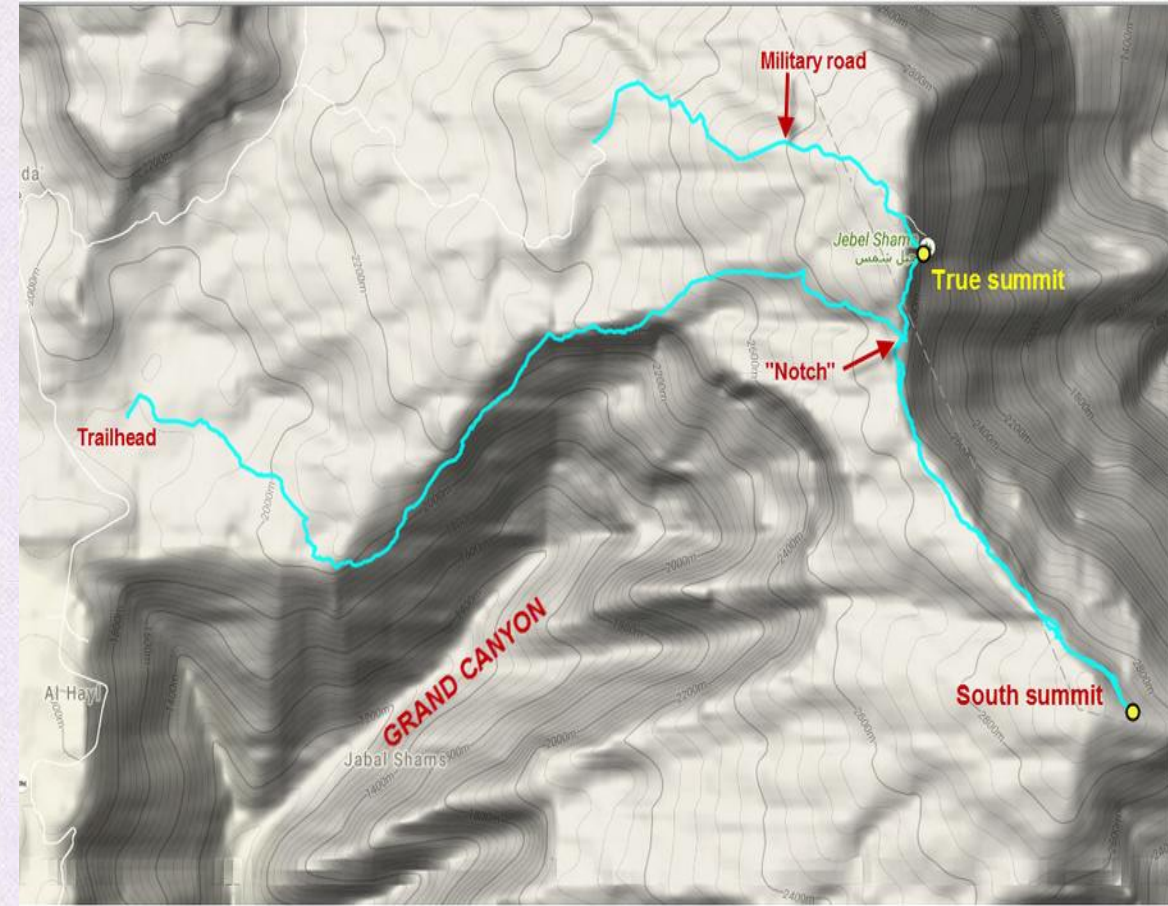
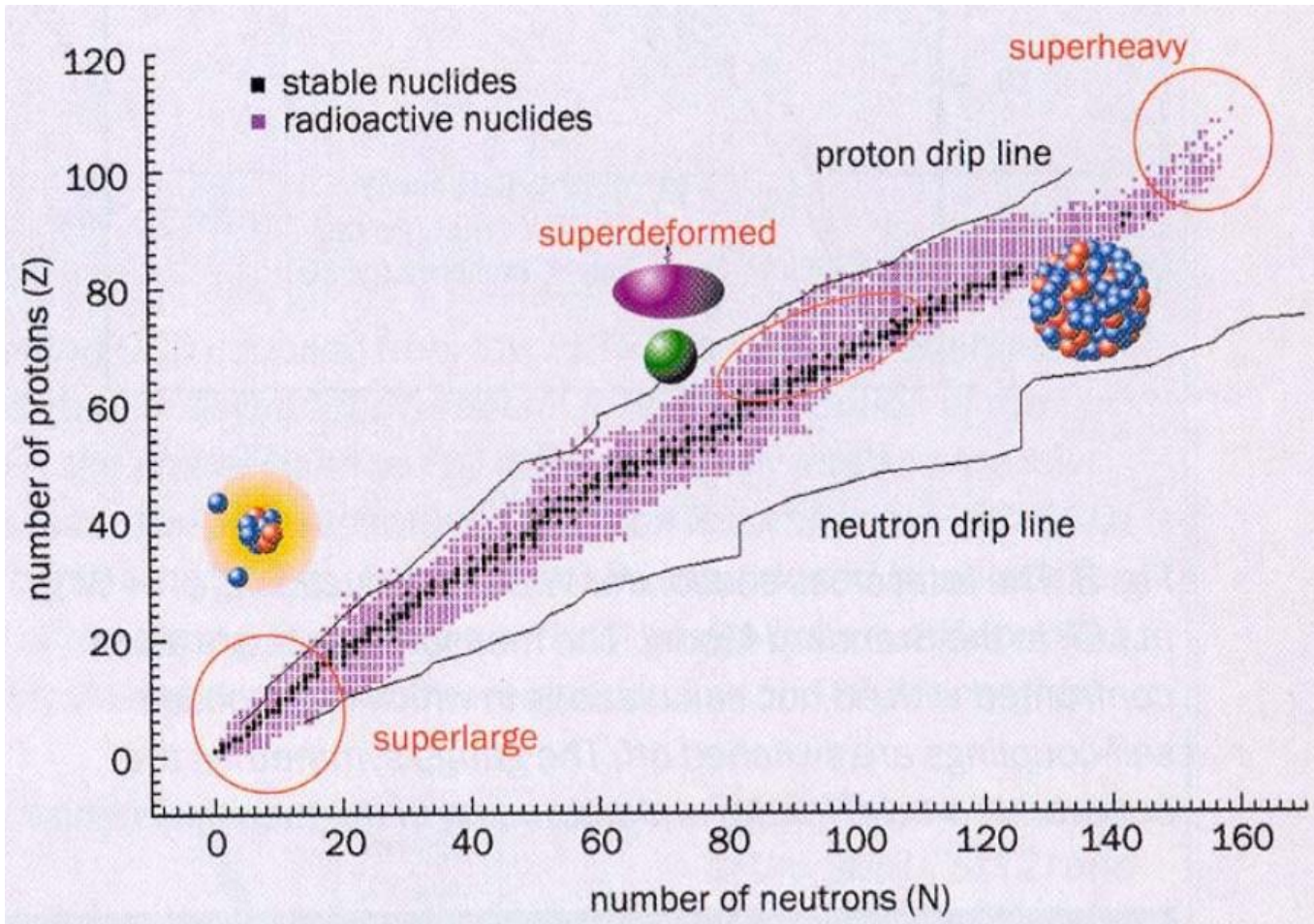


Zoom on the Y-axis





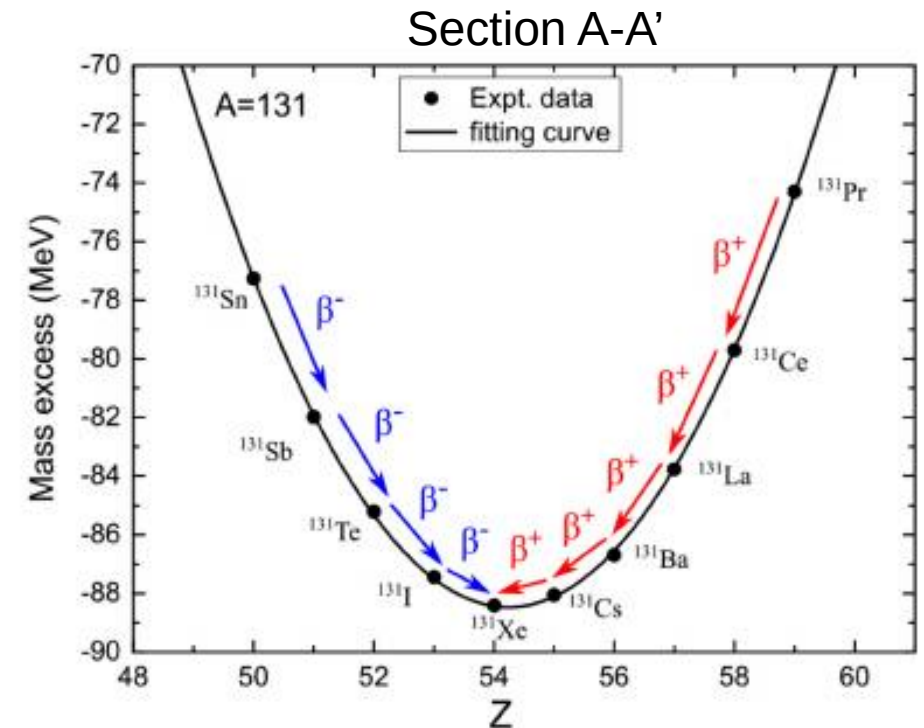
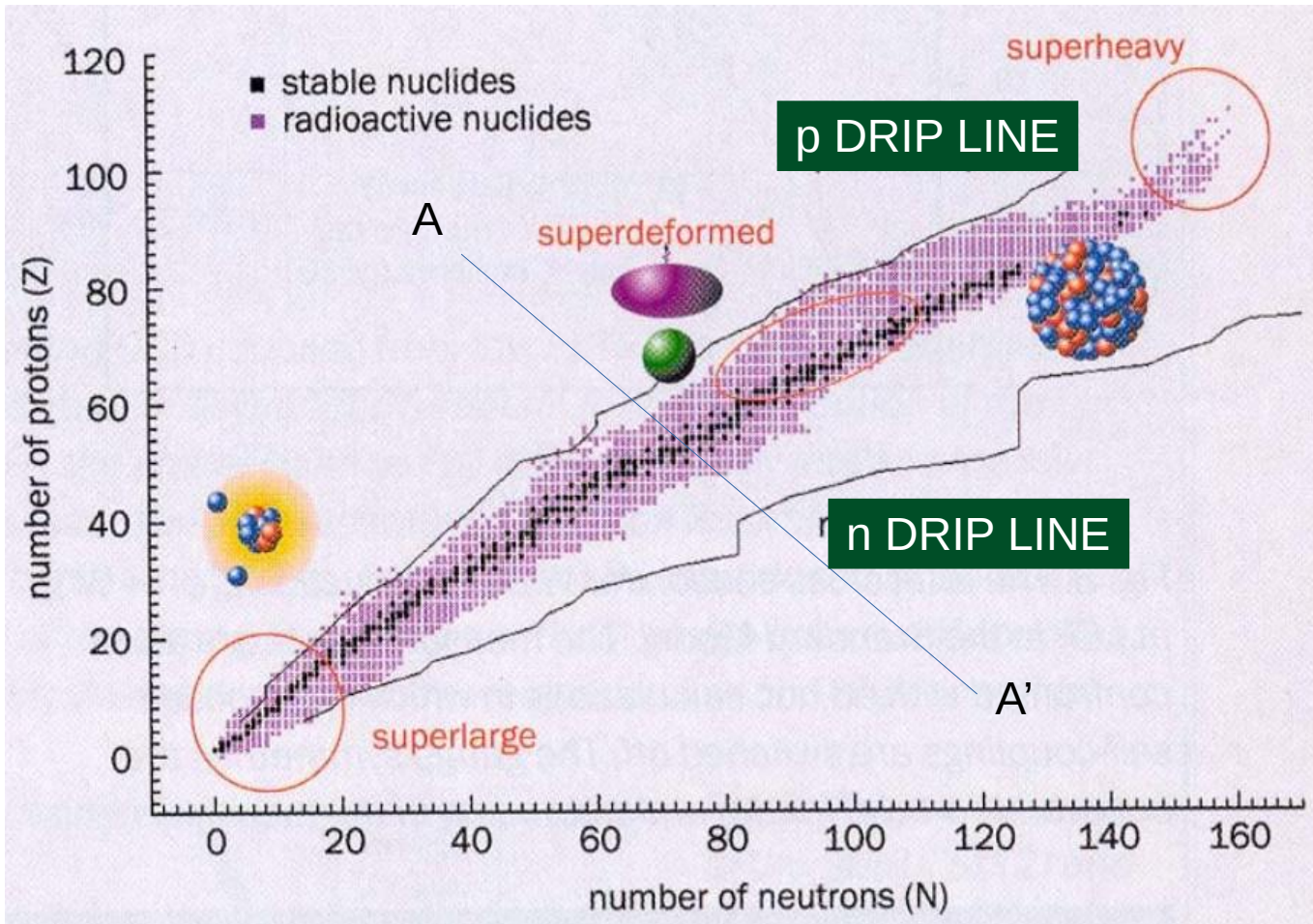
# Stronger bonds, larger stability: the canyon



The interplay of the various nuclear potential terms produces a narrow region in the bidimensional map  $Z$  vs  $A$  (Chart of Segré), where most nuclei are located: this is the **VALLEY of (nuclear) STABILITY (where about 300 nuclides are sitting)**



# Stronger bonds, larger stability



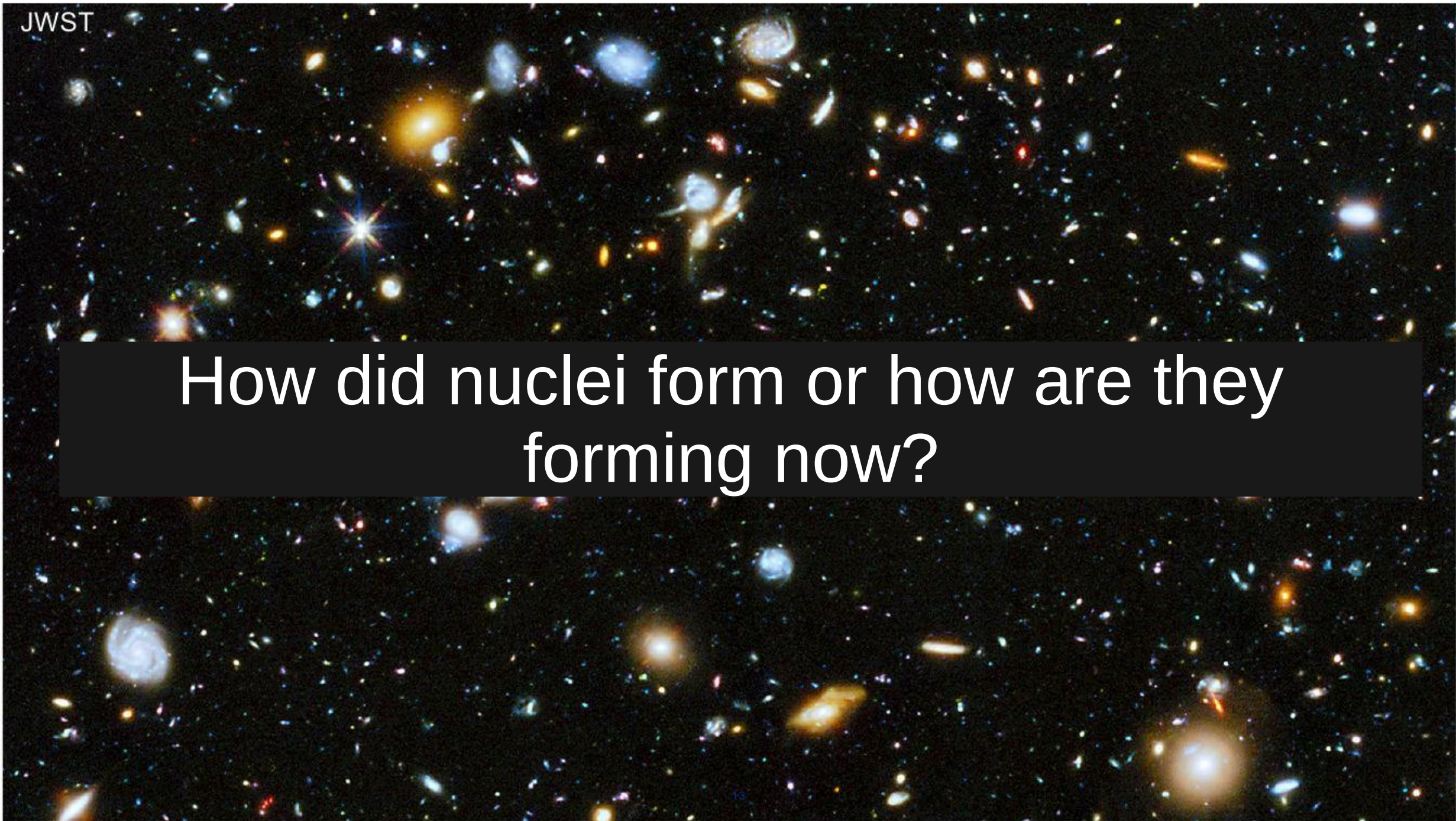
The interplay of the various nuclear potential terms produces a narrow region, in the bidimensional map Z vs A (Chart of Segré), where most nuclei are located: this is the **VALLEY of (nuclear) STABILITY**

**Drip lines:** are the tops of the canyon, at both sides, where separation energy for p and n goes to zero.



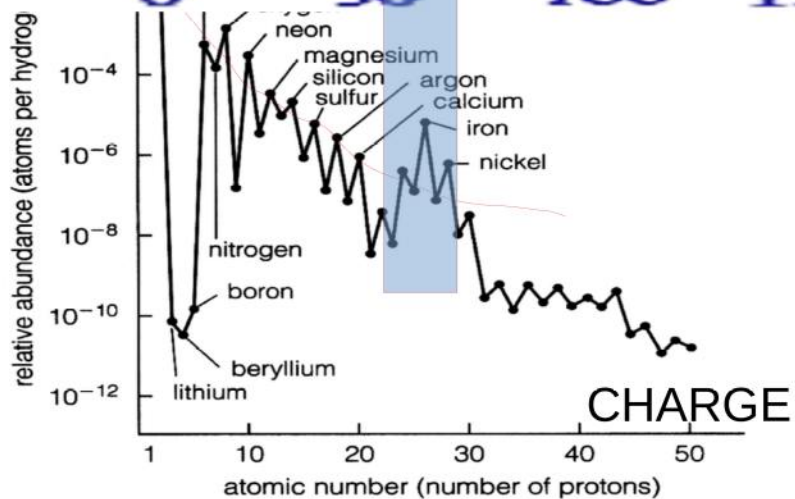
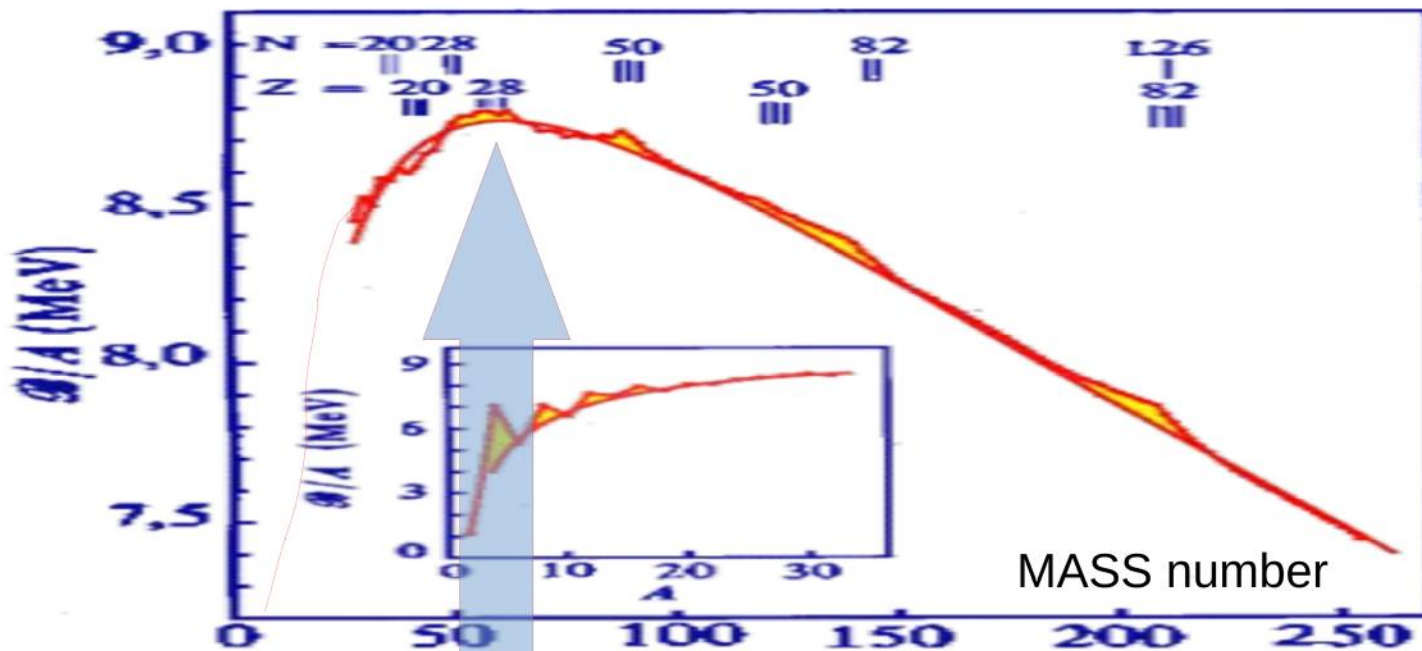
JWST

How did nuclei form or how are they forming now?

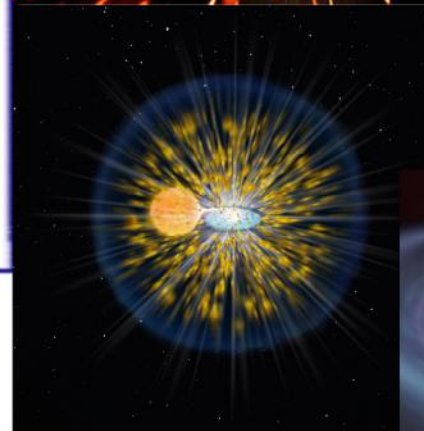




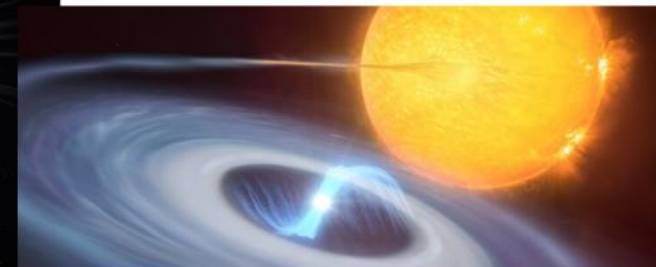
# Bonds, sources, abundances



Cosmological origin  
**BIG BANG**



Astrophysical origin  
**Novae, micronovae, ...**

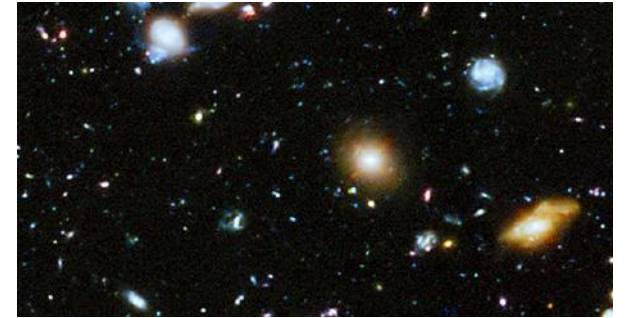


Of course in the observed abundances there play a strong role also the **production sites and production sources**.

You may have a possible stability region never accessed or rarely reached and v.v. less bound systems very abundantly produced

# How did nuclei form or how are they forming, now ?

## Nucleosynthesis



- Cosmological origin: BIG BANG
- Stellar main sequence (p-p chain, basically is fusion of  $4^*H$  into  $4He$ )
- Stars (old and/or heavy) from  $He+He+He$  to  $^{12}C$  and over ( $^{16}O, ^{20}Ne...$ )
- Stars: Neutron “candles” at a certain stellar life phase; the slow process
- Stars: Final (explosive) phases; the rapid process
- Giant explosions or collisions: micronovae, novae, black hole mergers or other pair collapses



# How did nuclei form or how are they forming, now ?

## **Nucleosynthesis**

- Cosmological origin: BIG BANG
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- Stars: Final (explosive) phases; the rapid process
- Giant explosions or collisions: micronovae, novae, Black hole mergers or other pair collapses
- **And in laboratories? Can we do something similar on Earth?**



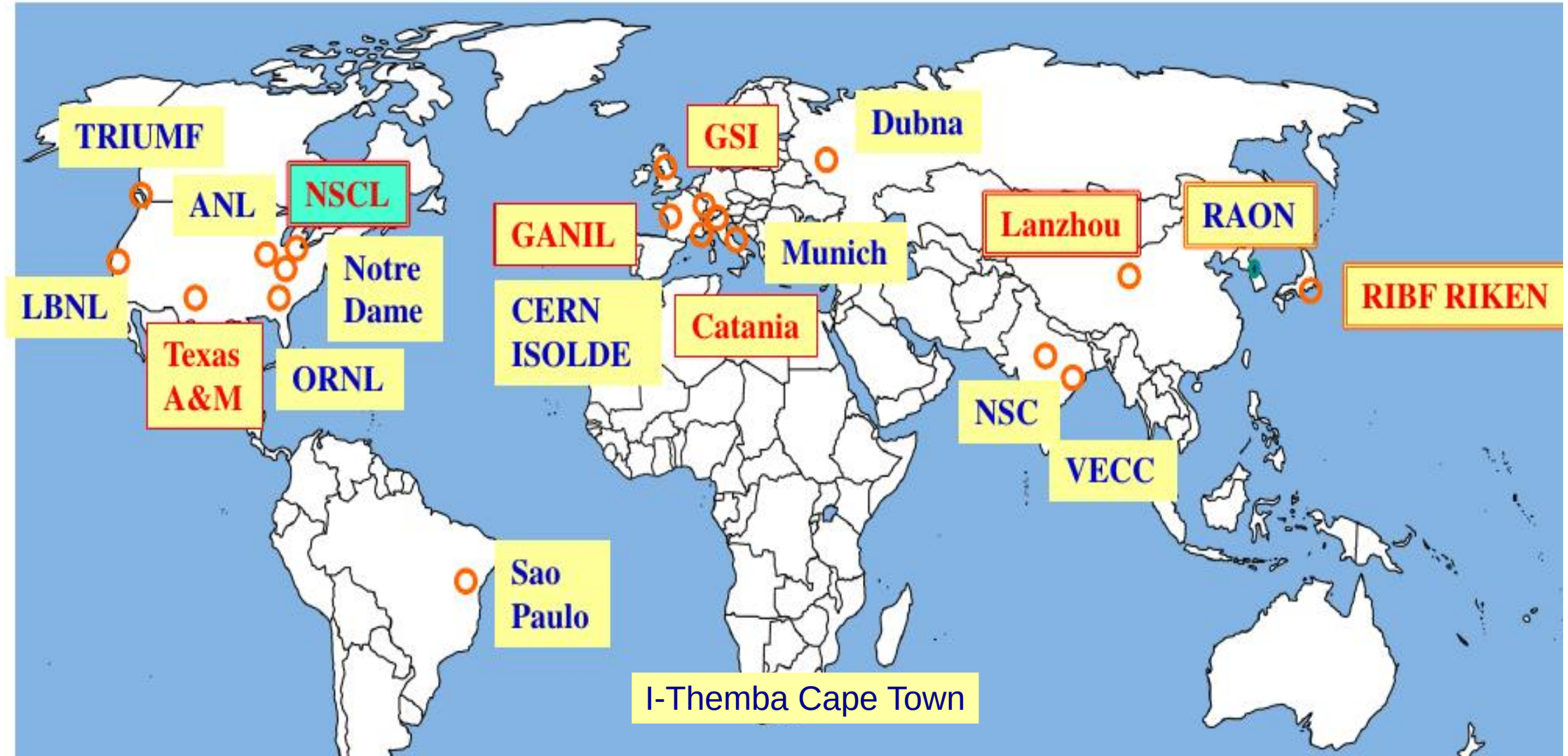
# Going to the analogy: how to climb the Canyon sides?

- Fragmentation in flight
- ISOL (isotope separation on line)
- Where in the world
- A matter of final energy, purity, precision
- Low energy: nuclear structure
- High energy: Equation Of State and nuclei at extreme environments
- *Relativistic energy (back to Big Bang and up to nucleon structure)*
- **SPES** at LNL (Legnaro)

Radioactive ion beam (RIB) facilities

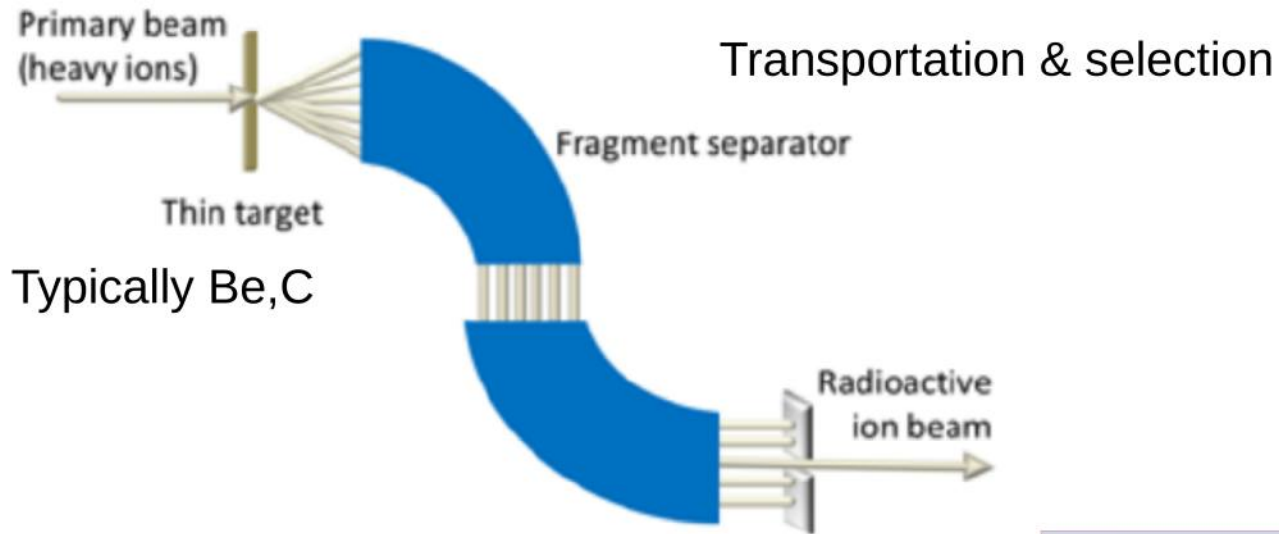
**you are here!**

# RIB labs in the world



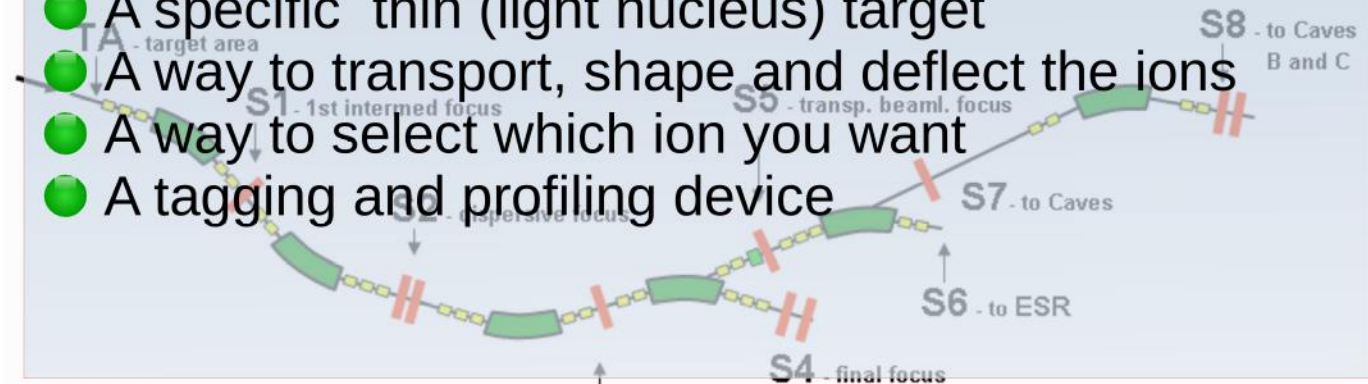
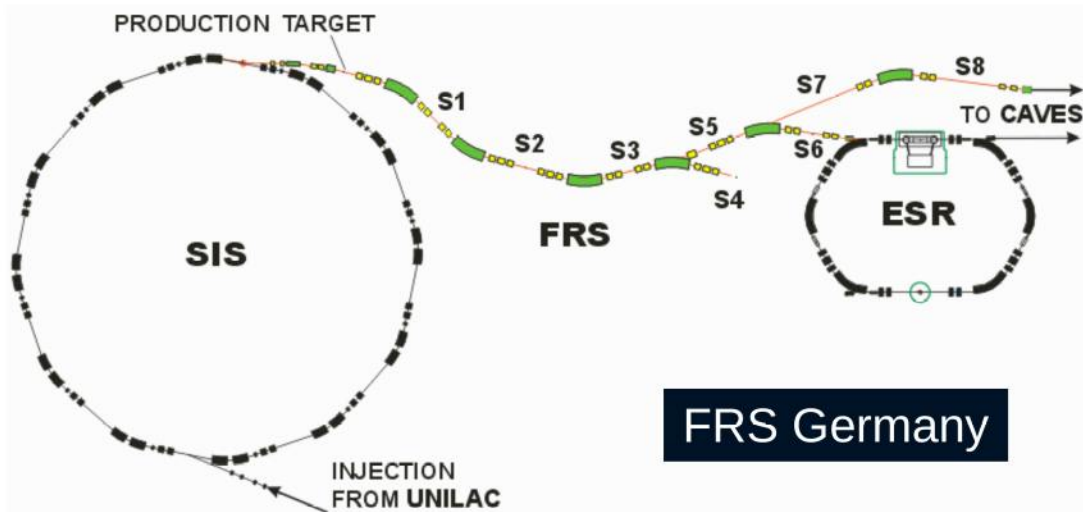


# IN-FLIGHT (IF) Technique



## Ingredients for a well performing IF beam lab

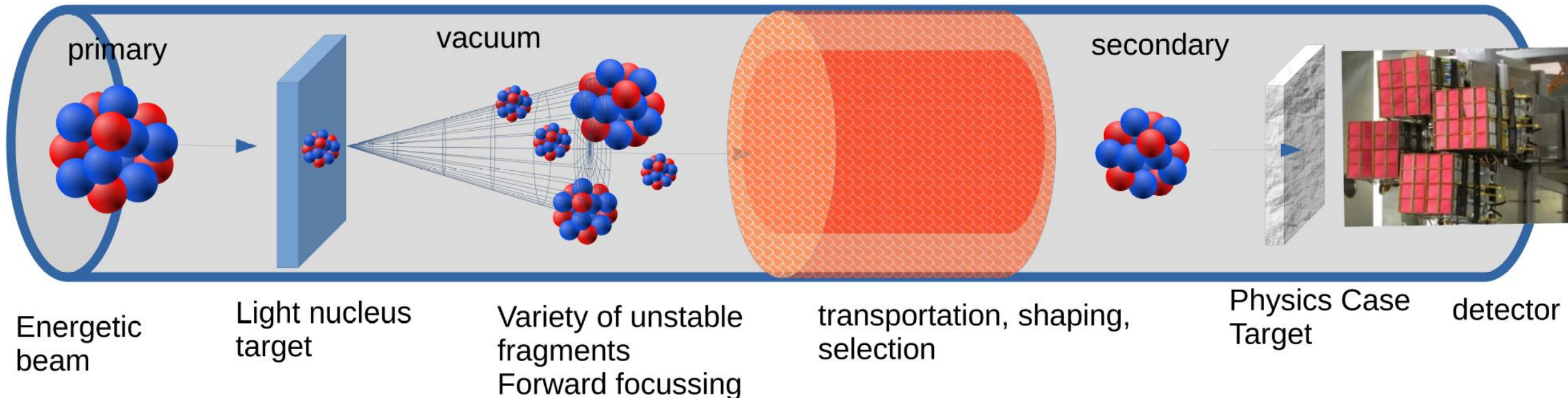
- An injecting accelerator, powerful
- A specific thin (light nucleus) target
- A way to transport, shape and deflect the ions
- A way to select which ion you want
- A tagging and profiling device



# IN-FLIGHT (IF) Technique

## Ingredients for a well performing IF beam lab

- An injecting accelerator, powerful
- A specific thin (light nucleus) target
- A way to transport, shape and deflect the ions
- A way to select which ion you want
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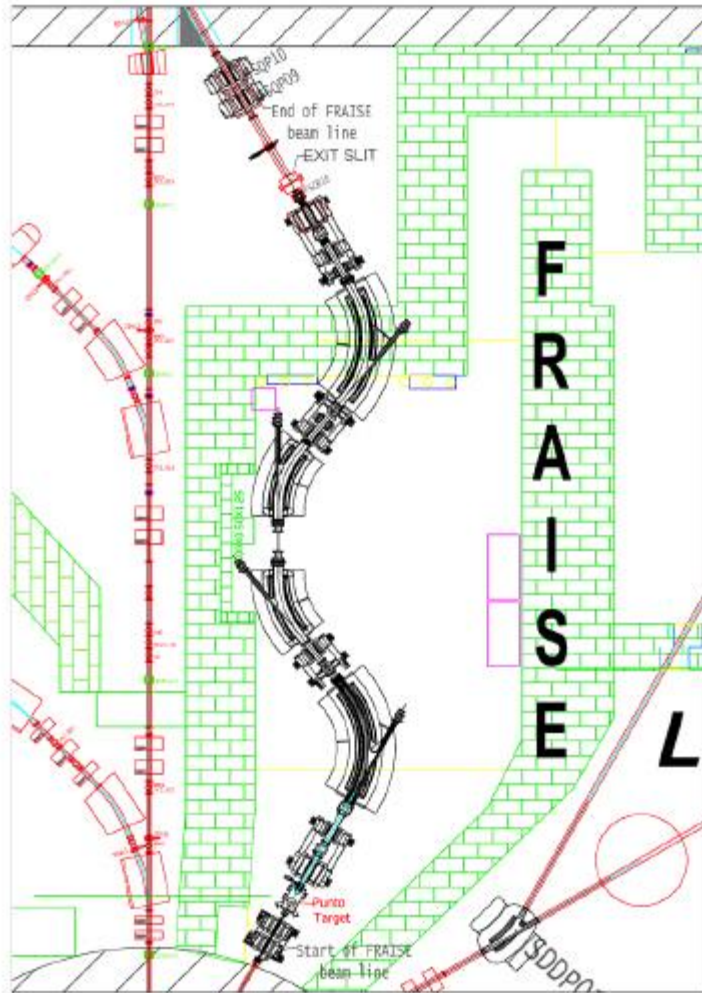




# IN-FLIGHT Technique

Driver: Superconducting Cyclotron (upgraded to 10kW)  
 Primary Ions: from C to Ar  
 Production Target: Be,C (max power 2-3kW)

In ITALY  
**FRAISE** Fragment IN-flight Separator  
 @ LNS, INFN Catania



$^{12}\text{C}^{6+}$  @ 60 AMeV  $^{18}\text{O}^{8+}$  @ 70 AMeV  $^{20}\text{Ne}^{10+}$  @ 70 AMeV  
 on 1-2mm  $^9\text{Be}$  target

				$^{17}\text{Ne}$ 8.7E5 53	$^{18}\text{Ne}$ 3.1E7 51	$^{19}\text{Ne}$ 6.0E8 52	$^{20}\text{Ne}$	$^{21}\text{Ne}$	$^{22}\text{Ne}$	$^{23}\text{Ne}$
	Proton rich				$^{17}\text{F}$ 1.7E8 50	$^{18}\text{F}$	$^{19}\text{F}$	$^{20}\text{F}$ 9.5E6 55	$^{21}\text{F}$	$^{22}\text{F}$
		$^{13}\text{O}$ 7.2E4 54	$^{14}\text{O}$ 1.4E6 40	$^{15}\text{O}$ 2.8E7 54	$^{16}\text{O}$	$^{17}\text{O}$	$^{18}\text{O}$	$^{19}\text{O}$ 4.4E6 50	$^{20}\text{O}$	$^{21}\text{O}$
		$^{12}\text{N}$ 1.2E6 49	$^{13}\text{N}$ 2.3E7 50	$^{14}\text{N}$	$^{15}\text{N}$	$^{16}\text{N}$ 6.9E8 53	$^{17}\text{N}$ 3.2E8 57	$^{18}\text{N}$ 3.7E6 57	neutron rich	
$^9\text{C}$ 4.0E5 45	$^{10}\text{C}$ 1.1E7 43	$^{11}\text{C}$ 2.2E8 44	$^{12}\text{C}$	$^{13}\text{C}$	$^{14}\text{C}$ 1.1E8 59	$^{15}\text{C}$ 4.0E7 59	$^{16}\text{C}$ 1.4E7 60	$^{17}\text{C}$ 1.2E5 58	$^{18}\text{C}$ 4.8E2 55	$^{19}\text{C}$
$^8\text{B}$ 3.1E6 42		$^{10}\text{B}$	$^{11}\text{B}$	$^{12}\text{B}$ 2.6E7 57	$^{13}\text{B}$ 7.5E6 58	$^{14}\text{B}$ 1.4E6 60	$^{15}\text{B}$ 2.6E5 51		$^{17}\text{B}$	
$^7\text{Be}$ 1.5E7 43		$^9\text{Be}$	$^{10}\text{Be}$ 1.6E7 50	$^{11}\text{Be}$ 1.5E6 58	$^{12}\text{Be}$ 2.8E5 60		$^{14}\text{Be}$ 3.0E3 63			
$^6\text{Li}$	$^7\text{Li}$	$^8\text{Li}$ 4.2E6 50	$^9\text{Li}$ 8.9E5 51		$^{11}\text{Li}$ 3.3E3 60					
	$^6\text{He}$ 2.1E6 51		$^8\text{He}$ 1.8E4 51							

EXPECTED  
 (calculations)

# IN-FLIGHT Technique



@ASG Superconductors, Italy

Superconducting magnet for SFS

## FEATURES

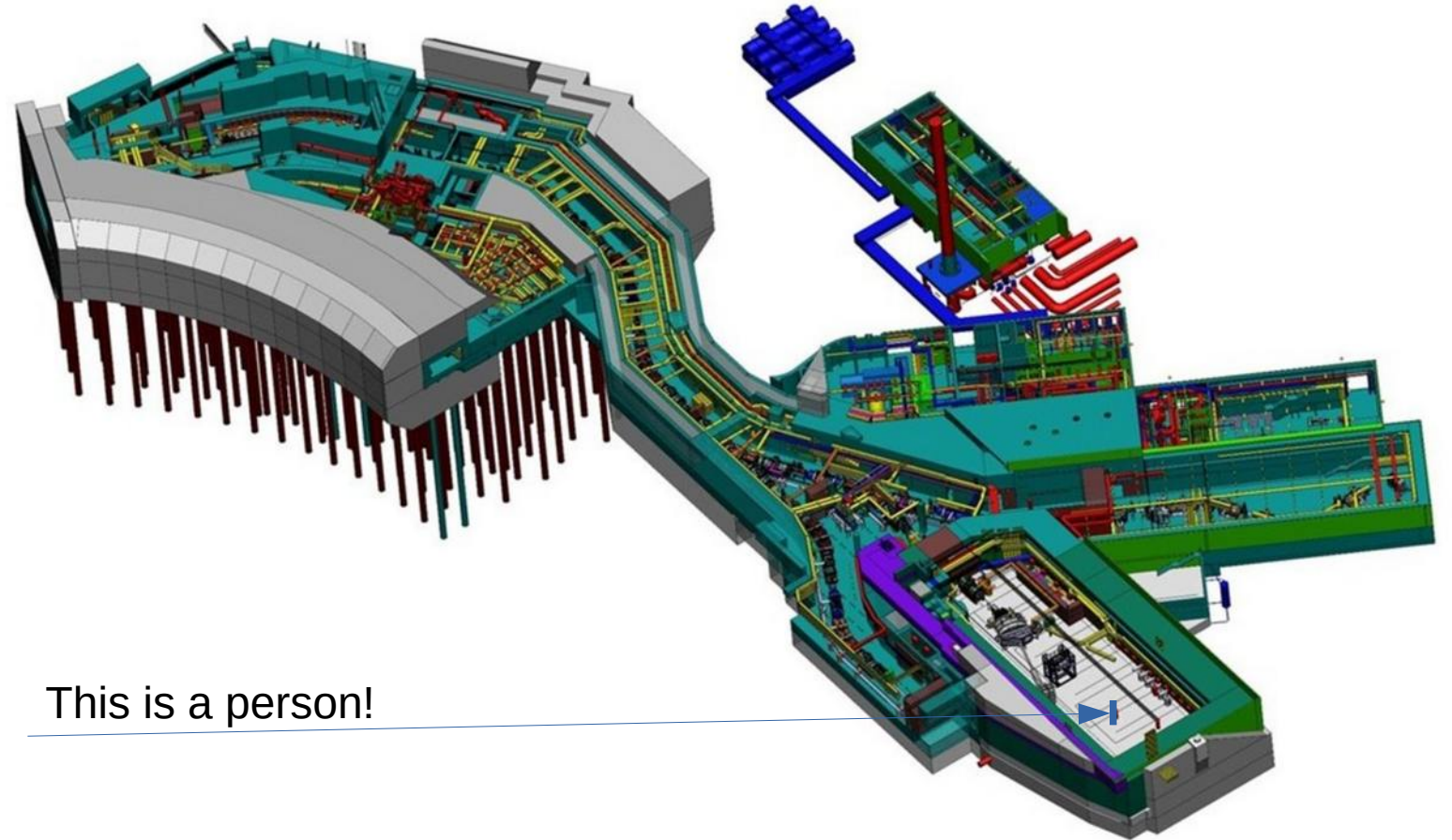
Intensities up to **1000 billions per second**

Elements from **p – U**

Energies up to **1.5 GeV/nucleon**

## SFS

Super Fragment Separator @ GSI



This is a person!

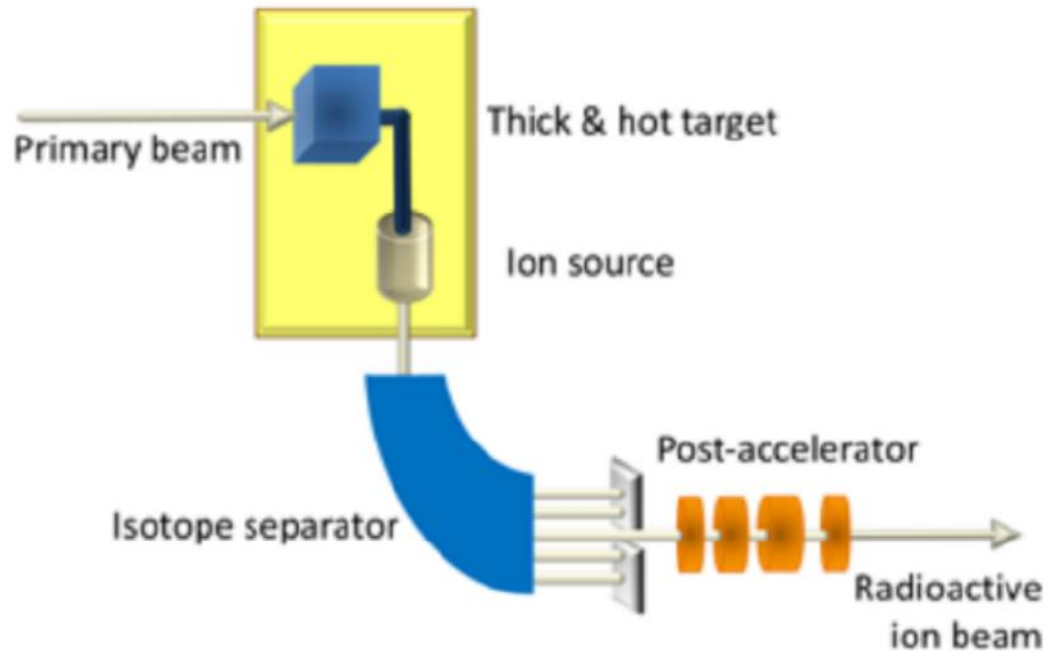
@DMU-GSI, @FSB-FAIR

## A GIANT IN GERMANY



# ISOL TECHNIQUE

## isotope separation on line

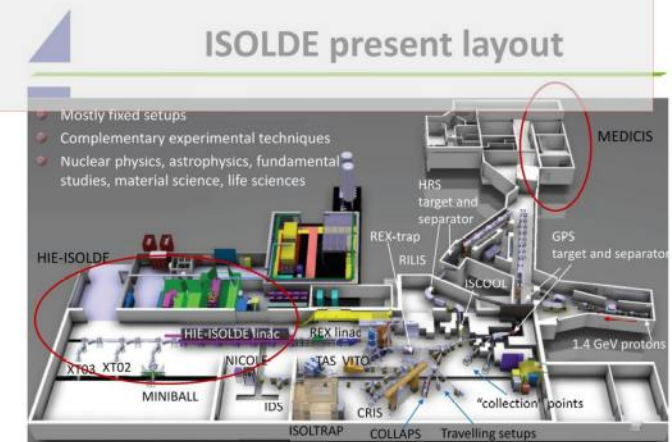


### Ingredients for a performing exotic beam lab

- An injecting accelerator, powerful
- A special 'robust' target
- A way to extract formed produced (slow) nuclei (atomic form)
- A way to give charge to atoms (getting ions)
- A way to select which ion you want
- A post-accelerator to achieve useful energy for physics
- All above, very quick!

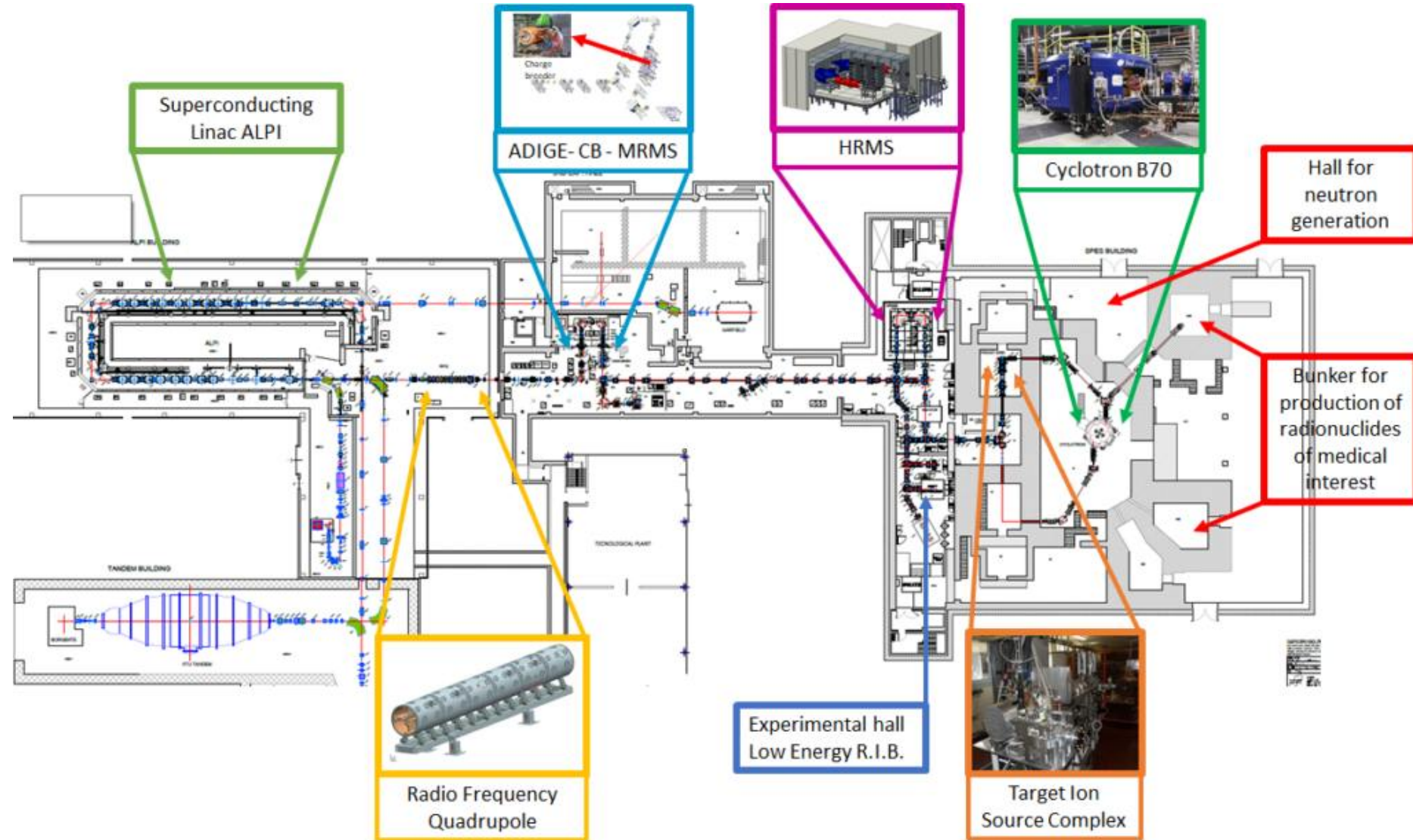
Among various examples:

Historical Facility, great expertise: ISOLDE, CERN  
Then also Triumf (Canada)  
In progress: **SPES, here at LNL**

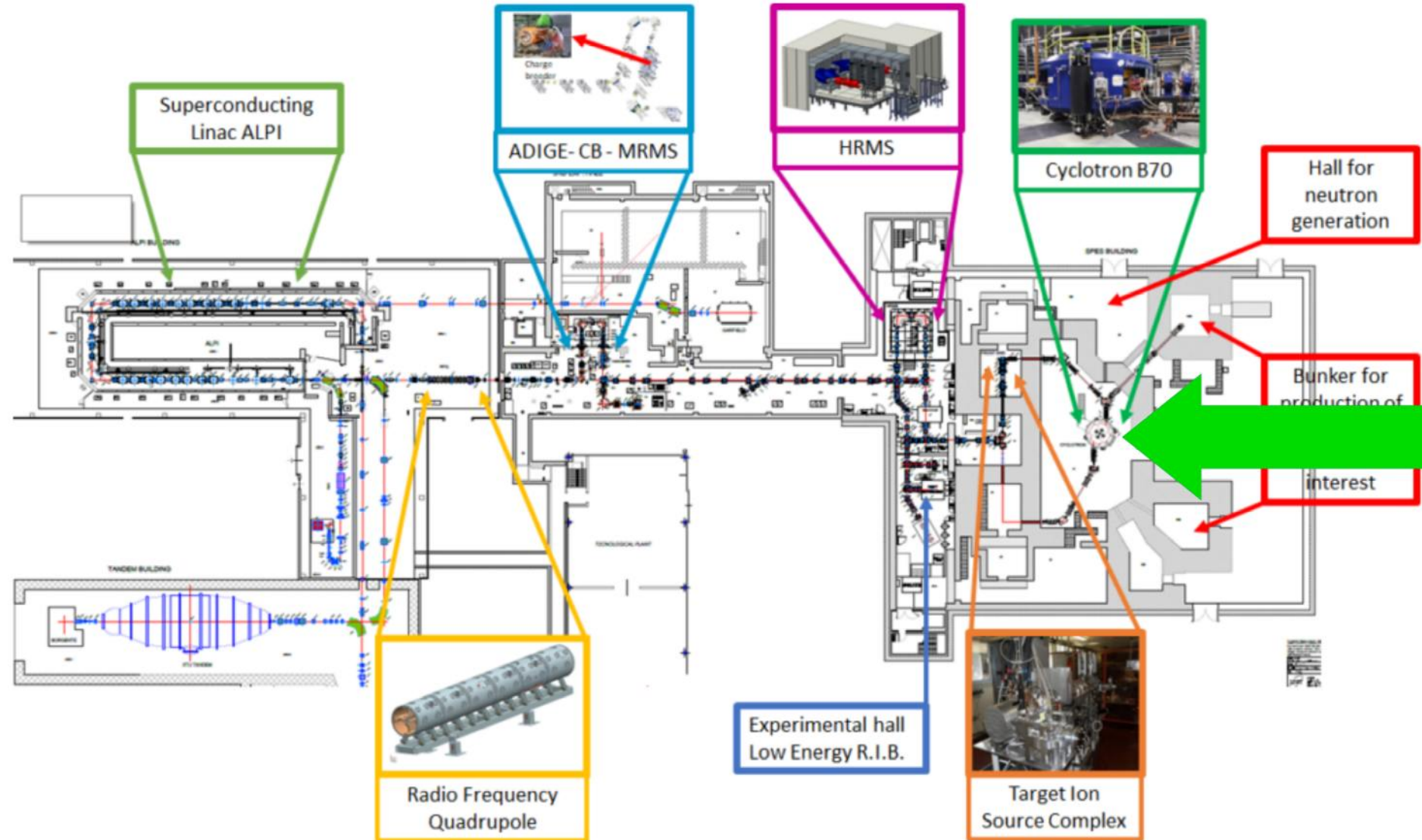




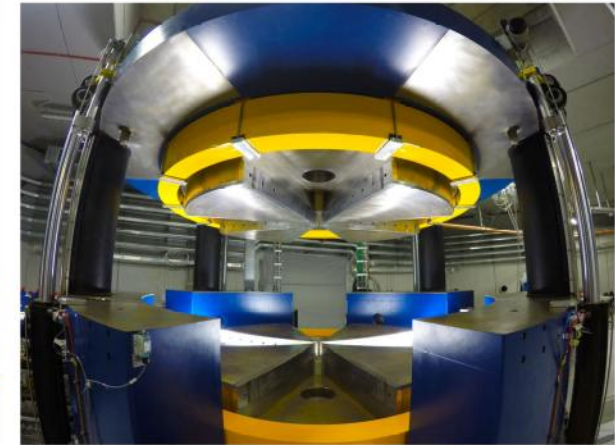
# The italian ISOL laboratory: SPES at LNL



# The italian ISOL laboratory: SPES at LNL



All starts here



**B70 cyclotron**  
150 tons  
Proton beams up to 0.75mA  
Energy 20-70 MeV  
Max power 52kW



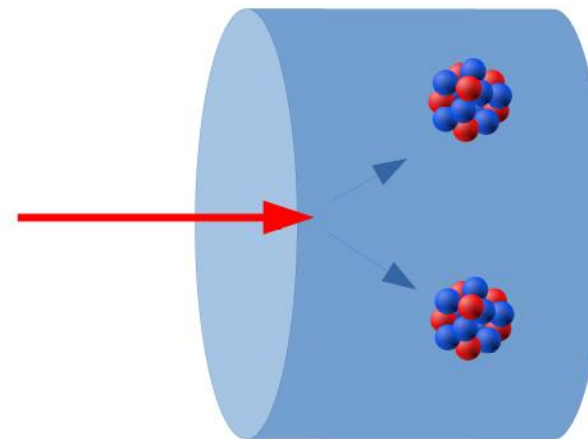
# The Target Ion Source (TIS) at SPES

From the cyclotron  
Proton beam

Up to  
some  $10^{15}$  pps



Sliced target (disks of e.g. SiC, BeC,  
Ucx, refractory compounds)



UCx

The exotic slow  
fragments soon  
stop within the disk

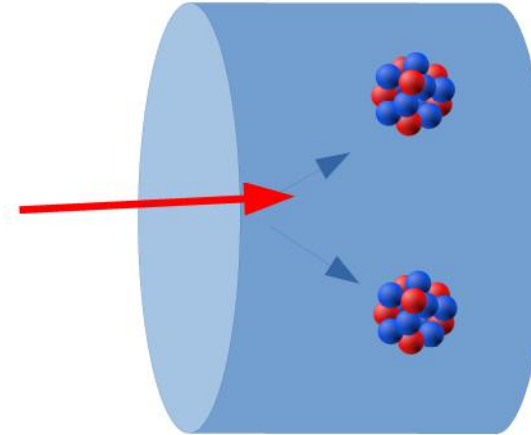
We must extract  
them!

# The Target Ion Source (TIS) at SPES

Proton beam



Sliced target (disks of e.g. SiC, BeC, Ucx, refractory compounds)

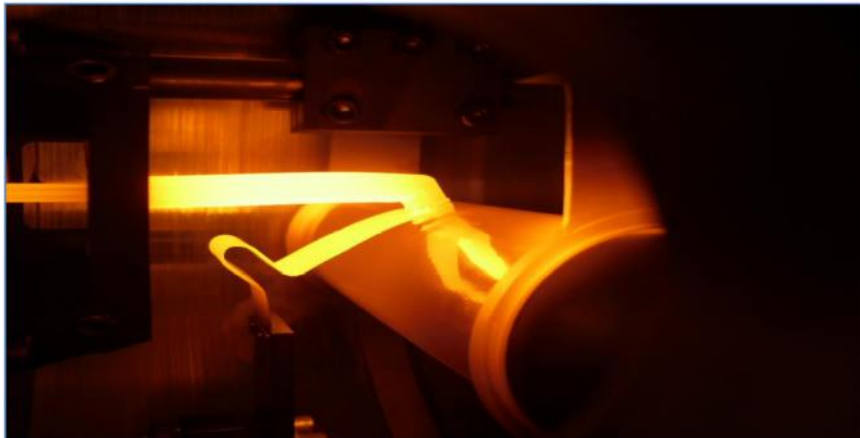


The exotic fragments quickly stop within the disk

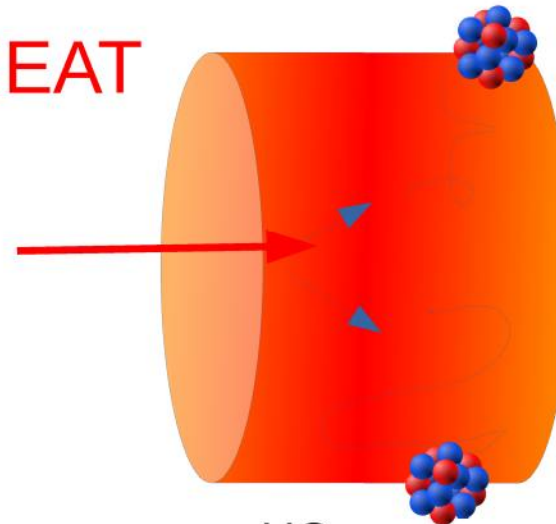
We must extract them!

UCx

Use of HEAT



Strong heating at  $T=2000-2200^{\circ}\text{C}$

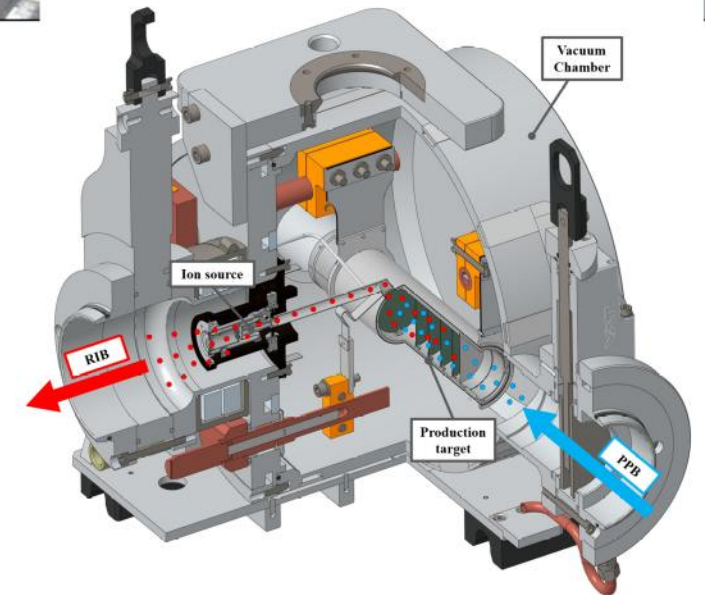
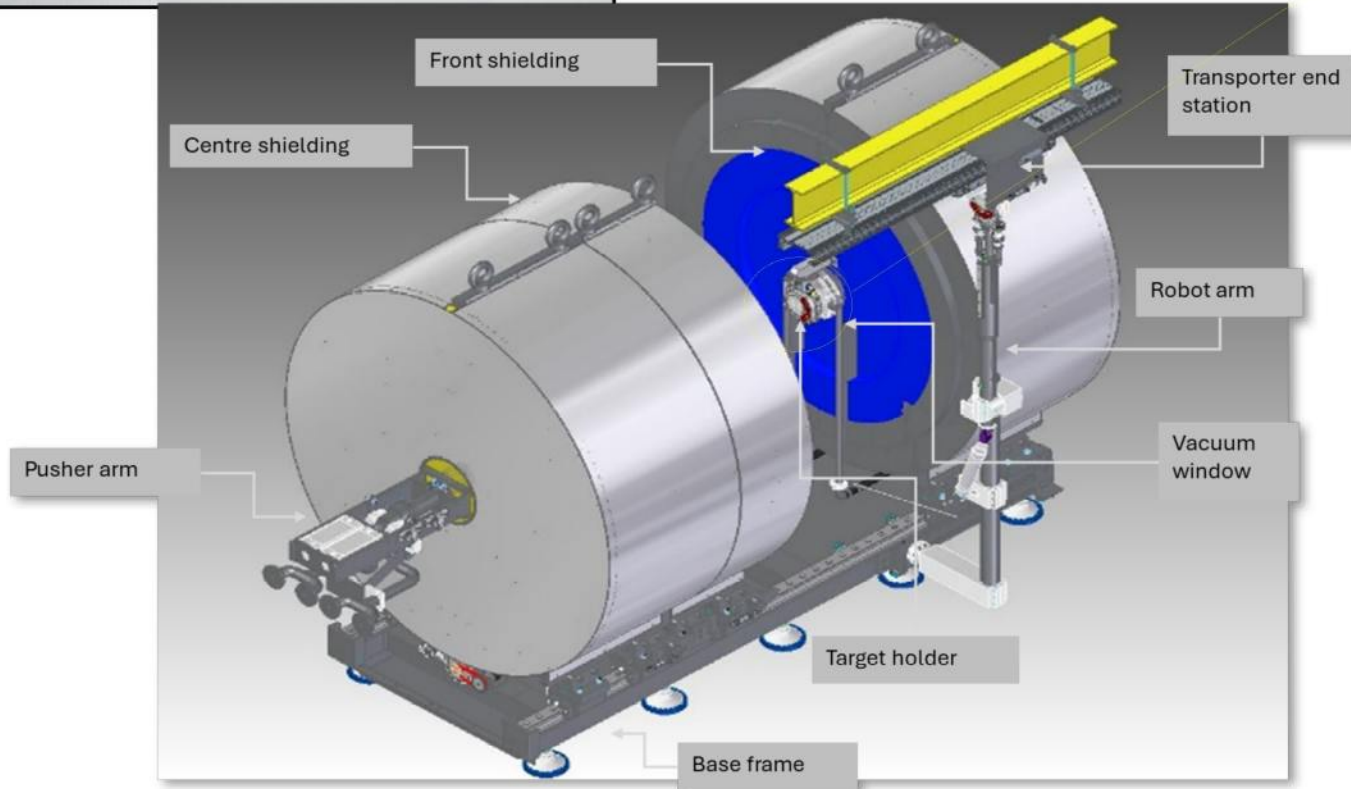
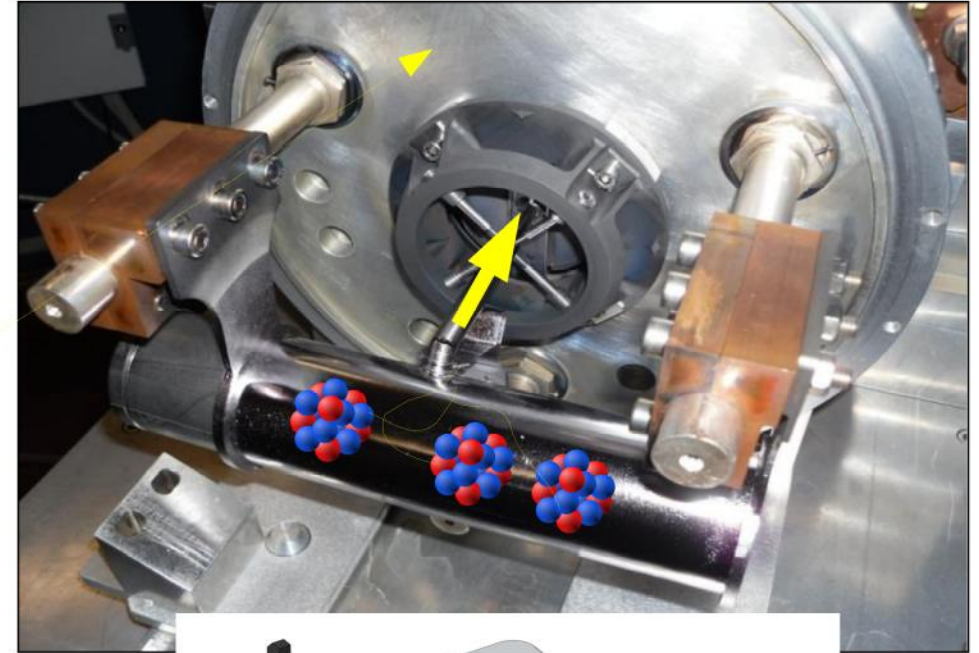
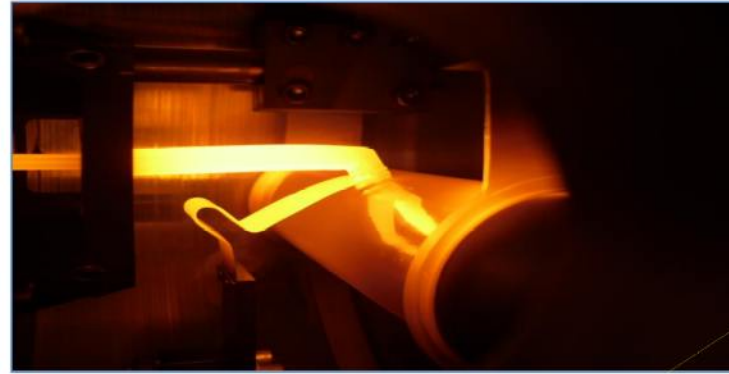


The unstable species **effuse** out of the target disk (with a certain efficiency, of course)

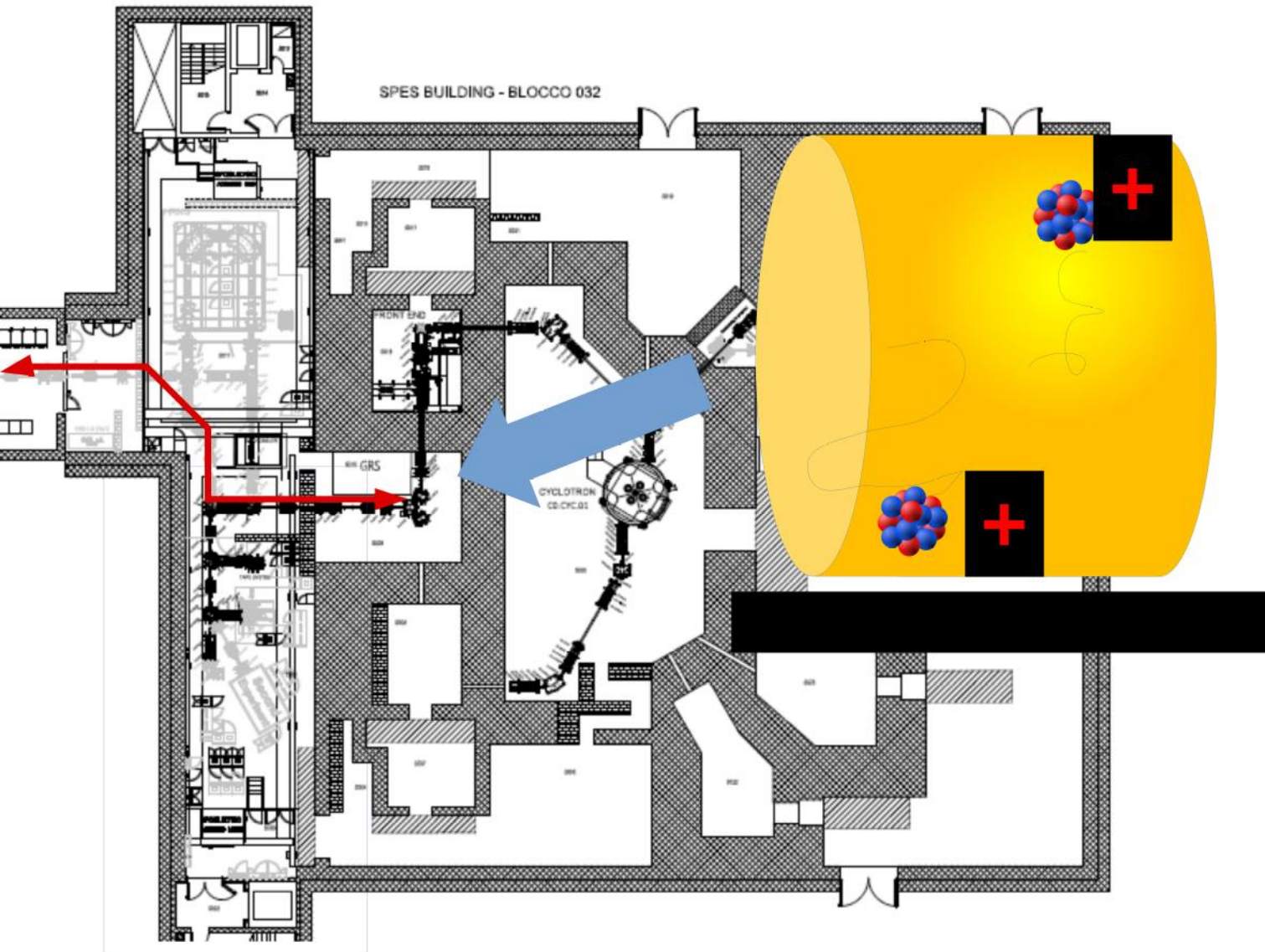
UCx



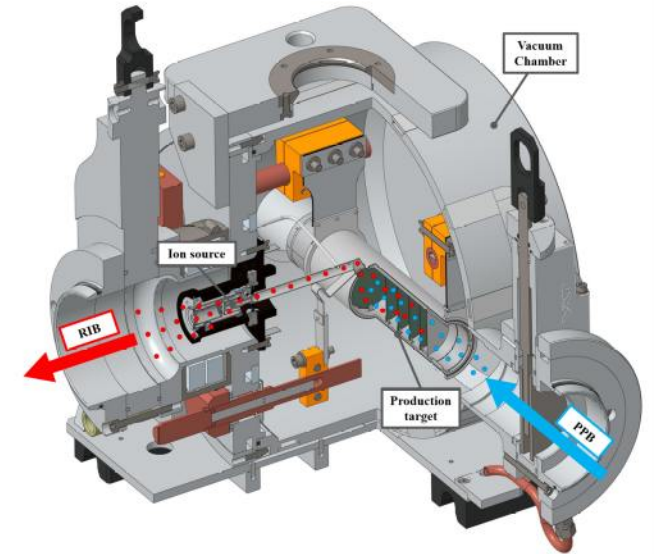
# The Target Ion Source (TIS) at SPES



# From atoms to ions, from slow to fast ions



Low Energy RIB area



After the **extraction** from the target, in fractions of second, **ions** must be produced (1+), must be preliminarily **accelerated** (with static HV), then **enriched** in charge (Charge Breeder) and **accelerated** more with specific RadioFrequency sections. Also the **isotope separation** must be done with efficient spectrometers



# Which are the most intriguing physics subjects?

Nuclear geography: interplay of energies and potentials (typical of all physical systems)

- Nuclear radius: a clear cut definition?
  - Atomic nuclei become nuclear atoms...
  - Nuclei: not only single protons and neutrons
  - Weakly bound systems and their wonderful periphery
  - Strange radioactivity modes
  - Shapes: not only spherical droplets
  - From old Magic to new Magic
  - ...and much more; if you're curious, please follow Nuclear Physics Academic courses!
- To stimulate your curiosity

# What is the nuclear radius?

Till the '80s there was consensus about the “macroscopic” nucleus description in terms of a **drop of incompressible liquid** with **constant density**. This implies that the radius  $R$  of the nucleus **weakly** increases with its mass  $m$ .

$$V = \left(\frac{4}{3}\right) \pi R^3$$

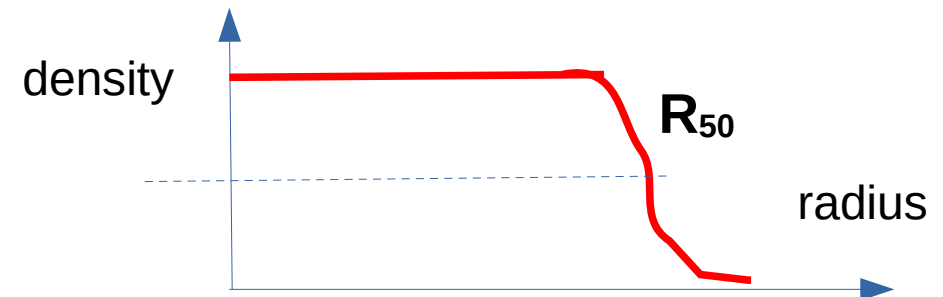
$$m = \rho V ; \rho = \text{constant (incompressible liquid drop)}$$

From these formulas, it simply follows:

$$R = a m^{(1/3)} = r_0 A^{(1/3)} \quad \text{Where } r_0 \text{ is a 'constant' in (fm) and } A \text{ is the mass number. Typically } r_0 = 1.2 \text{ fm}$$

**But: *Natura non facit saltus!*** Experiments using electron diffusion on nuclei revealed some diffuseness, i.e. some **surface detail**:

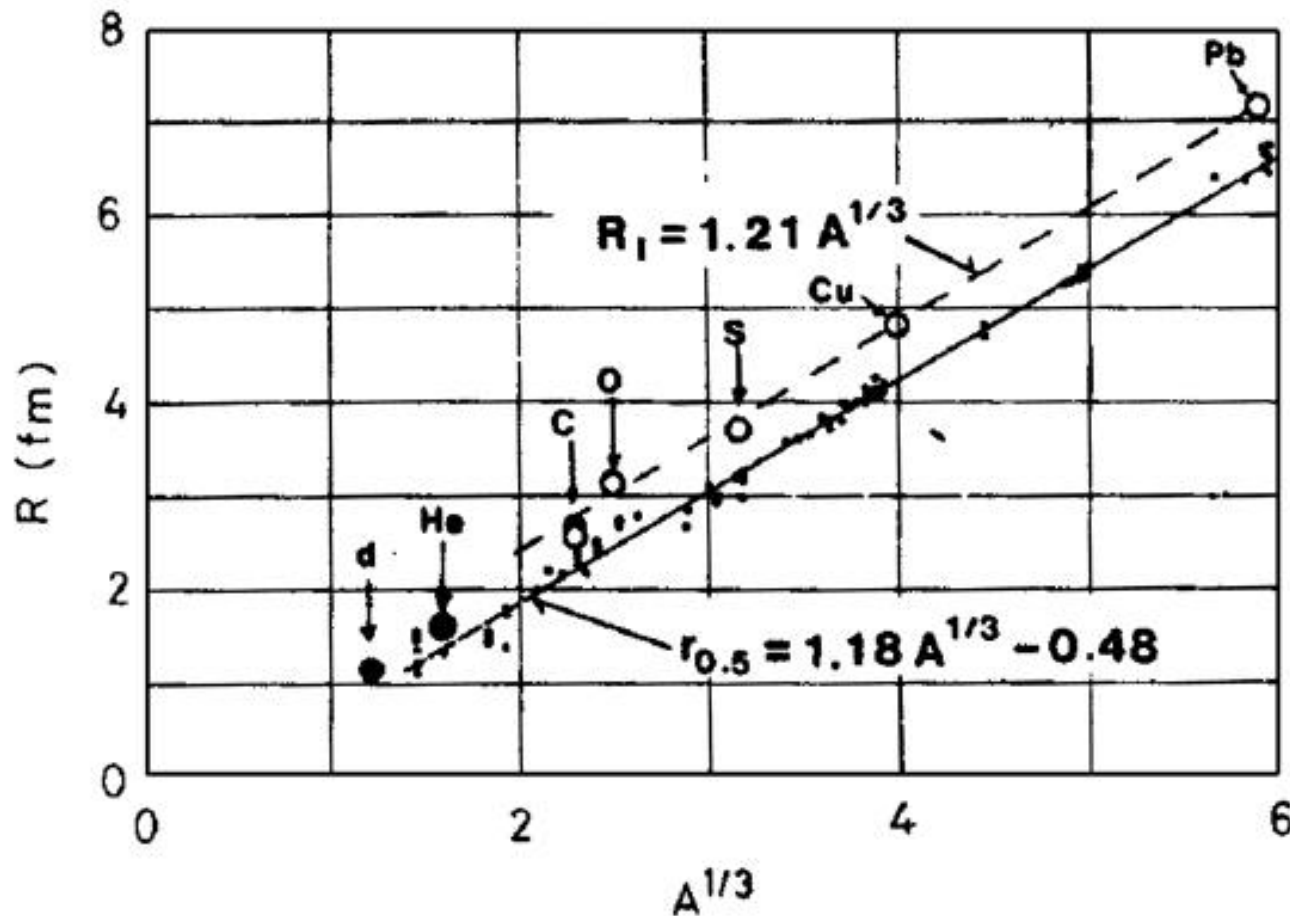
$$R_{50} = r_0 A^{(1/3)} - \delta$$



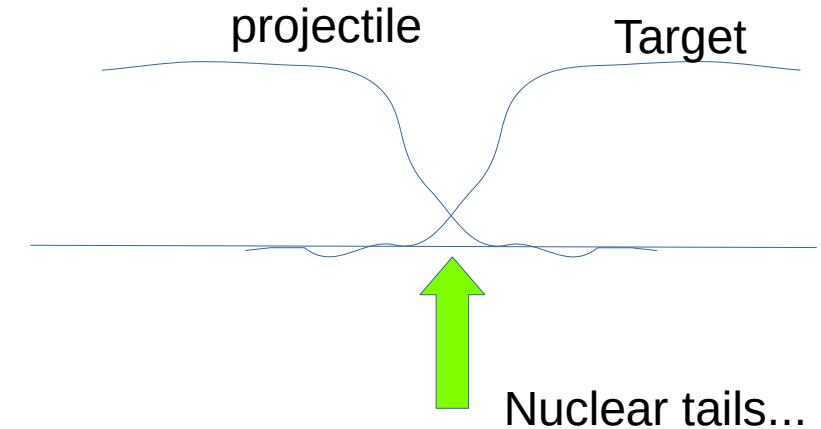


# What is the nuclear radius?

Measurements of cross sections in reactions with stable nuclei put in evidence small surface effects (diffuseness); **however**, the main view/description of the nuclear droplets was retained.



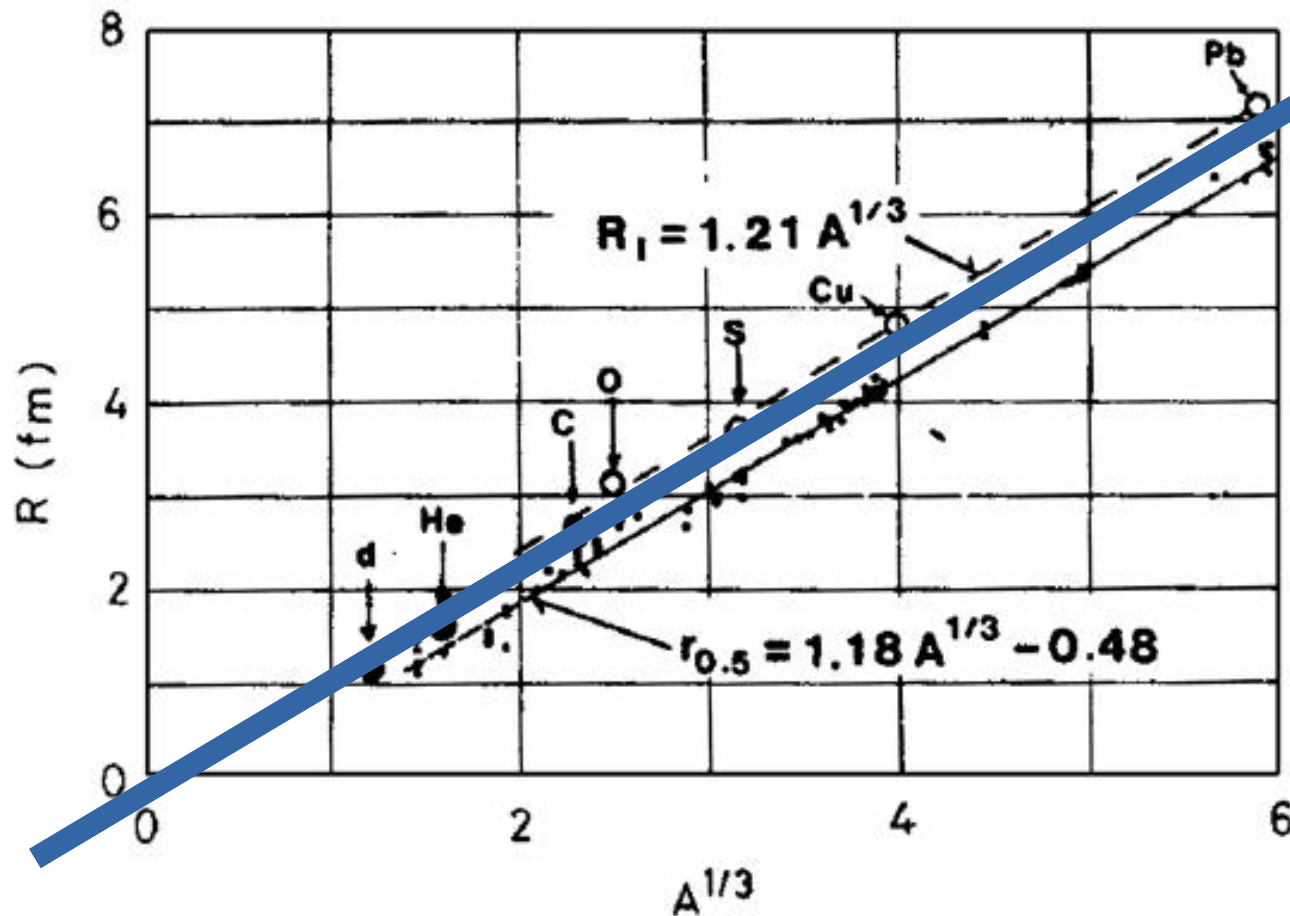
$$R = r'_0 A^{(1/3)}$$



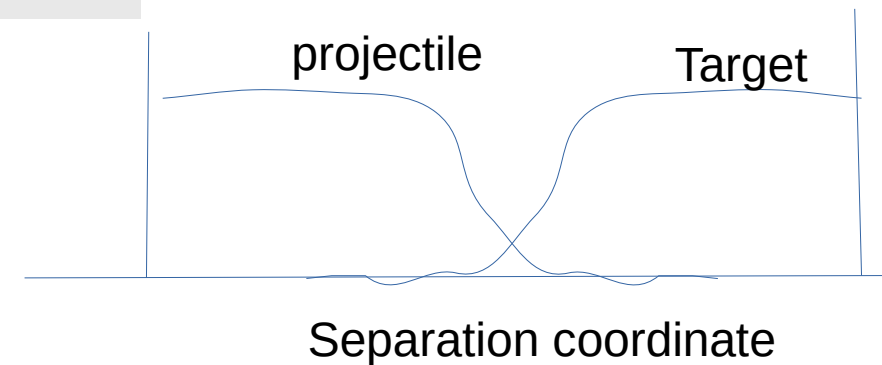
$$R_{50} = r_0 A^{(1/3)} - \delta$$

# What is the nuclear radius?

Measurements of cross sections in reactions with stable nuclei put in evidence small surface effects (diffuseness); **however**, the main view/description of the nuclear droplets was retained.



$$R = r_0' A^{(1/3)}$$



$$R_{50} = r_0 A^{(1/3)} - \delta$$



# The discovery of halo in nuclei

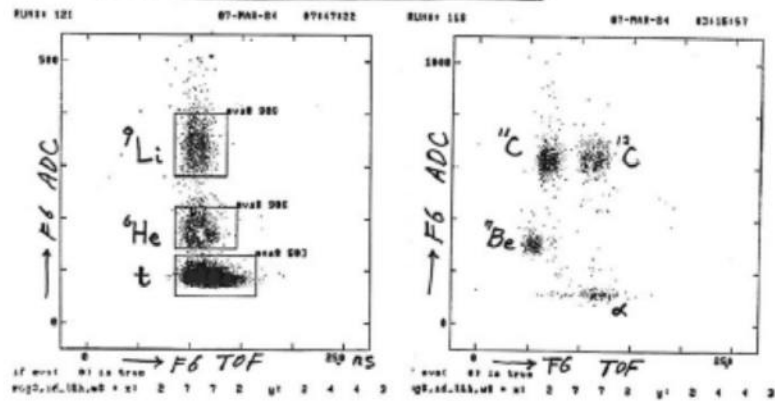
March 7, 1984

HOT!!

News from LBL.

We have got unstable nuclear  
Beams.

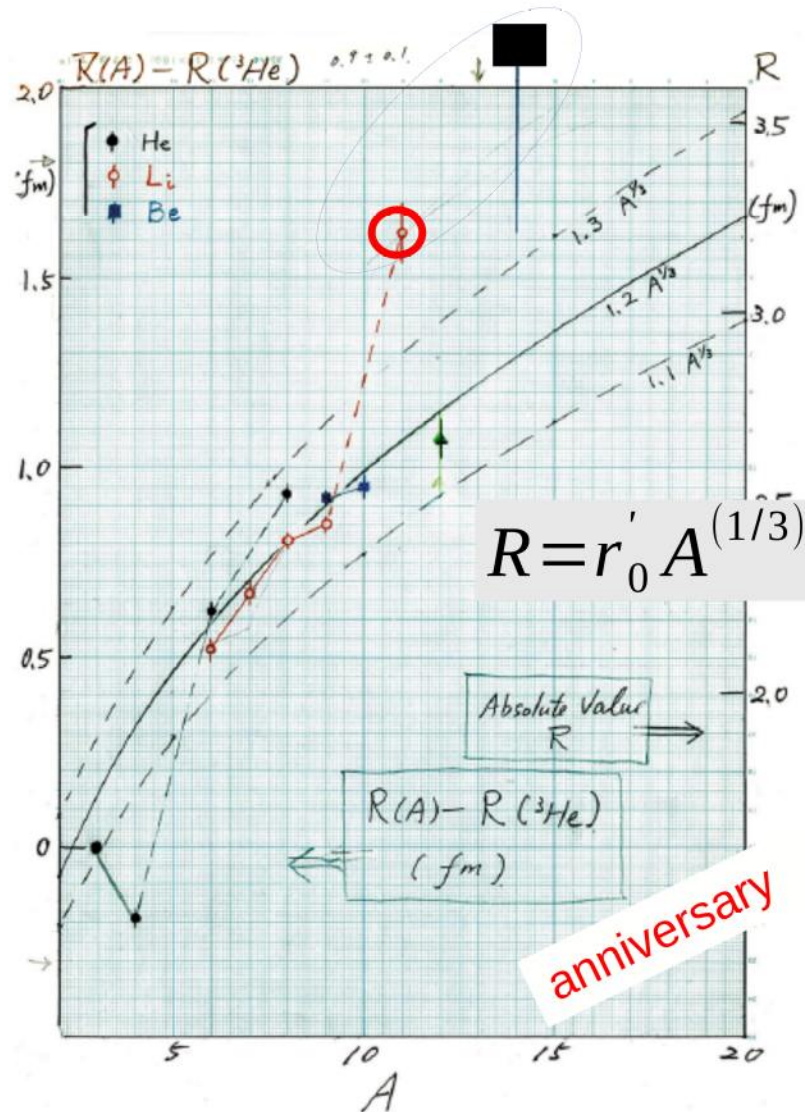
$^{12}\text{C}$  beam of  $\sim 800 \text{ A}\cdot\text{MeV}$



K. Nagai, Y. Yamahata, O. Hashimoto, et al.

This paradigm was dramatically changed with the advent of the first **unstable beams**. First attempts at the LBL, USA (early 80s)

The strange radii of  **$^{11}\text{Li}$**  and  **$^{14}\text{Be}$**



# An unexpected variety of configurations

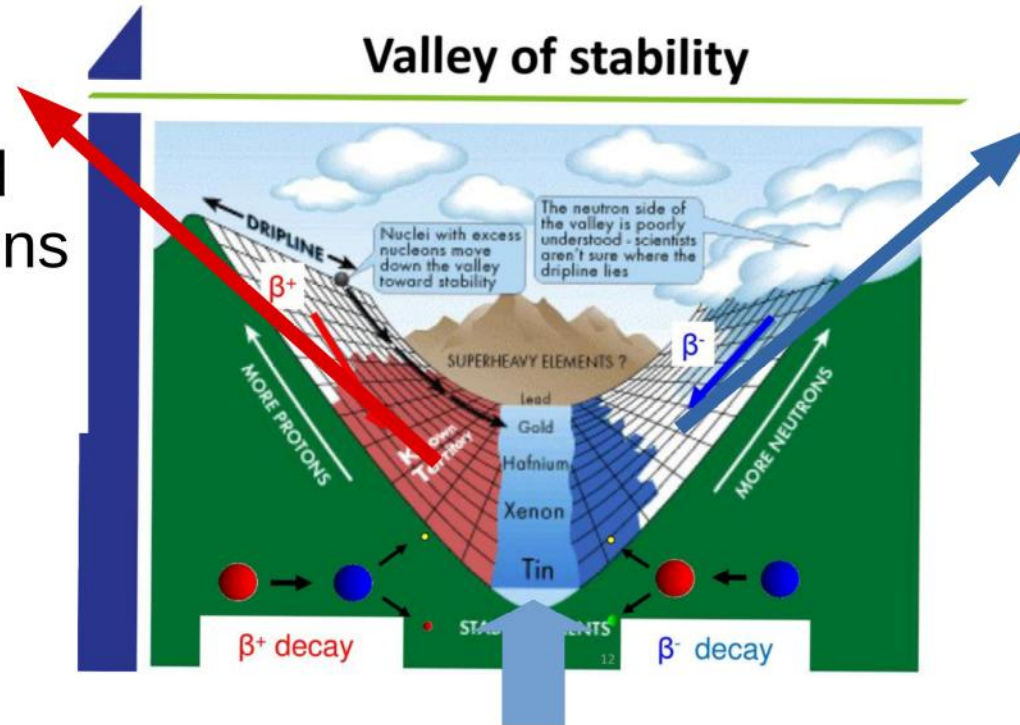
- Mass scaling not fully valid!
- Radius also depends on the isospin degree of freedom, i.e. the difference in neutron  $N$  and proton  $Z$  numbers
- Isobars (same  $A$ ) with different ratios  $N/Z$  have not same radius.

The diffuseness is **not almost equal** in all nuclei. The spatial distributions of neutrons and protons, similar for stable nuclei, may differ far from the *Canyon valley*; their separation energies can change a lot, accordingly, for protons and neutrons

If you climb this side

- protons loosely bound
- Extended p-distributions
- large radii
- Short lifetimes

“Only” this?



If you climb this side

- Neutrons loosely bound
- Extended n-distributions
- Very large radii
- Short lifetimes

“Only” this?

$n, p$  similar binding energies

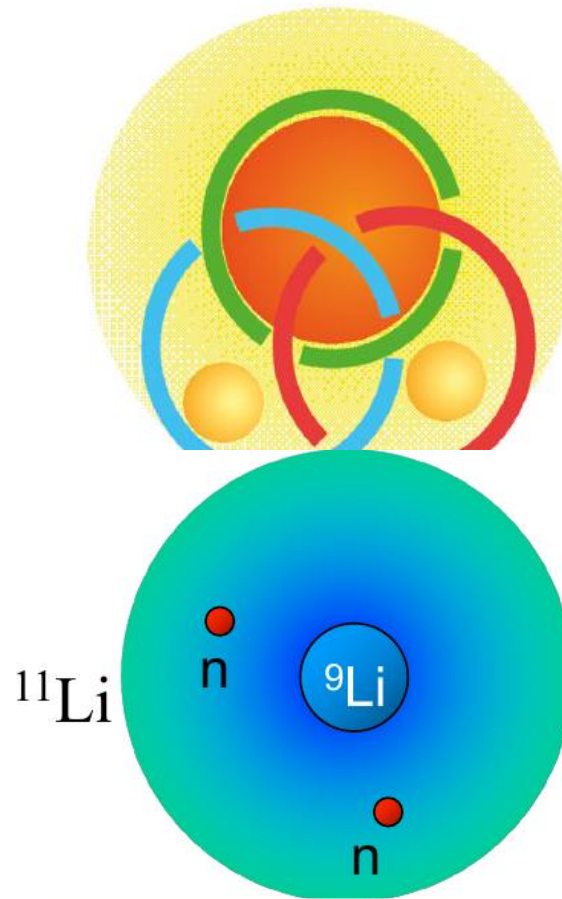


# An unexpected variety of configurations

Other phenomena have been put in evidence and are currently under study using reactions with exotic beams. The **drip lines** have been reached with these investigations **for the light systems** because they are closer to the Valley.

Examples of new nuclear phenomena

- ⊗ Only in three guys together, we survive!
- ⊗ Neutrons as electrons in molecules
- ⊗ Not only halos but also Neutron skins
- ⊗ Towards the Equation of State of nuclei and neutron stars
- ⊗ The world of clusters



$^9\text{Li} + \text{neutron}$  doesn't exist

2-neutron pair doesn't exist

$^9\text{Li} + 2\text{n}$  **does exist, it's  $^{11}\text{Li}$**

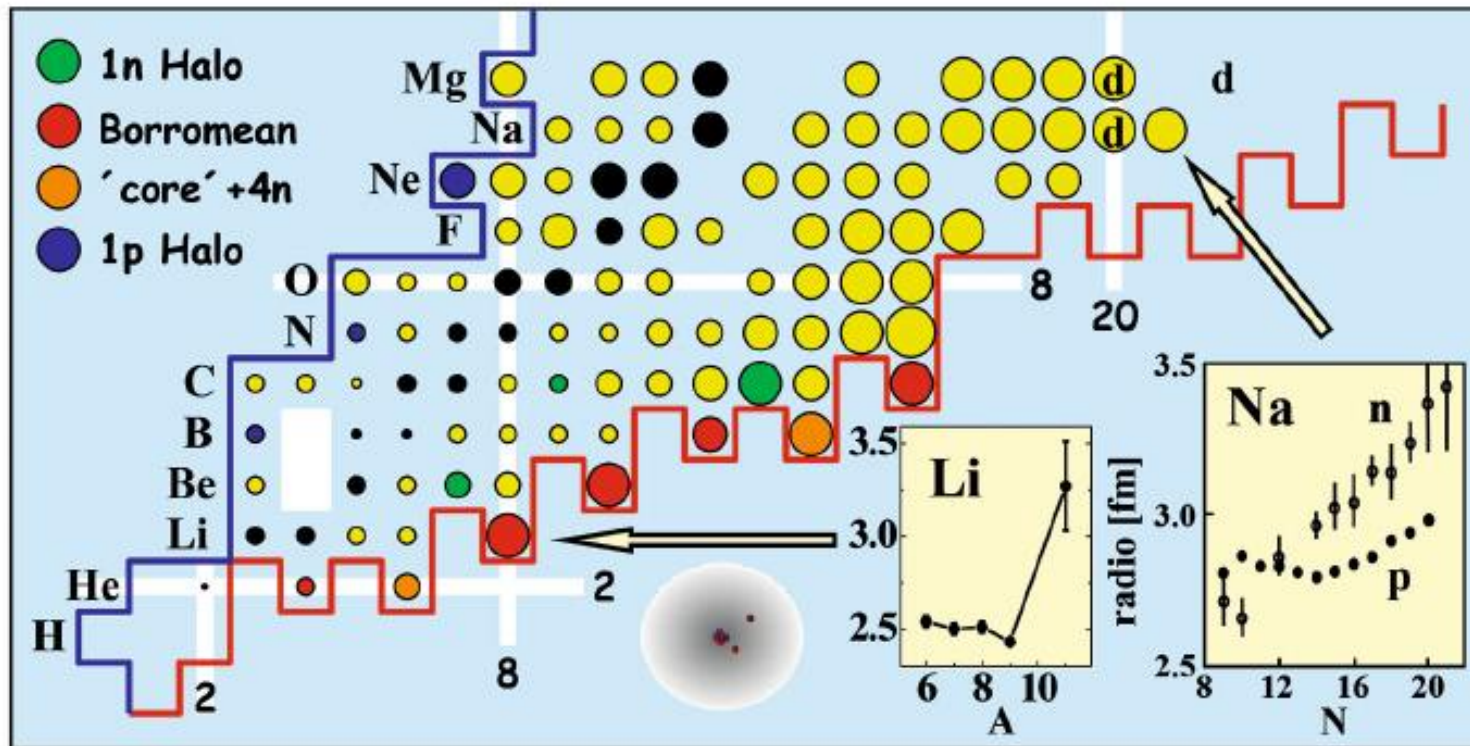
Rare quantum case of a system bound via three-body correlations



Borromean nuclei  
(from araldic logo)

# An unexpected variety of configurations

Other phenomena have been put in evidence and are currently under study using reactions with exotic beams. The **drip lines** have been reached with these investigations **for the light systems** because they are closer to the Valley.



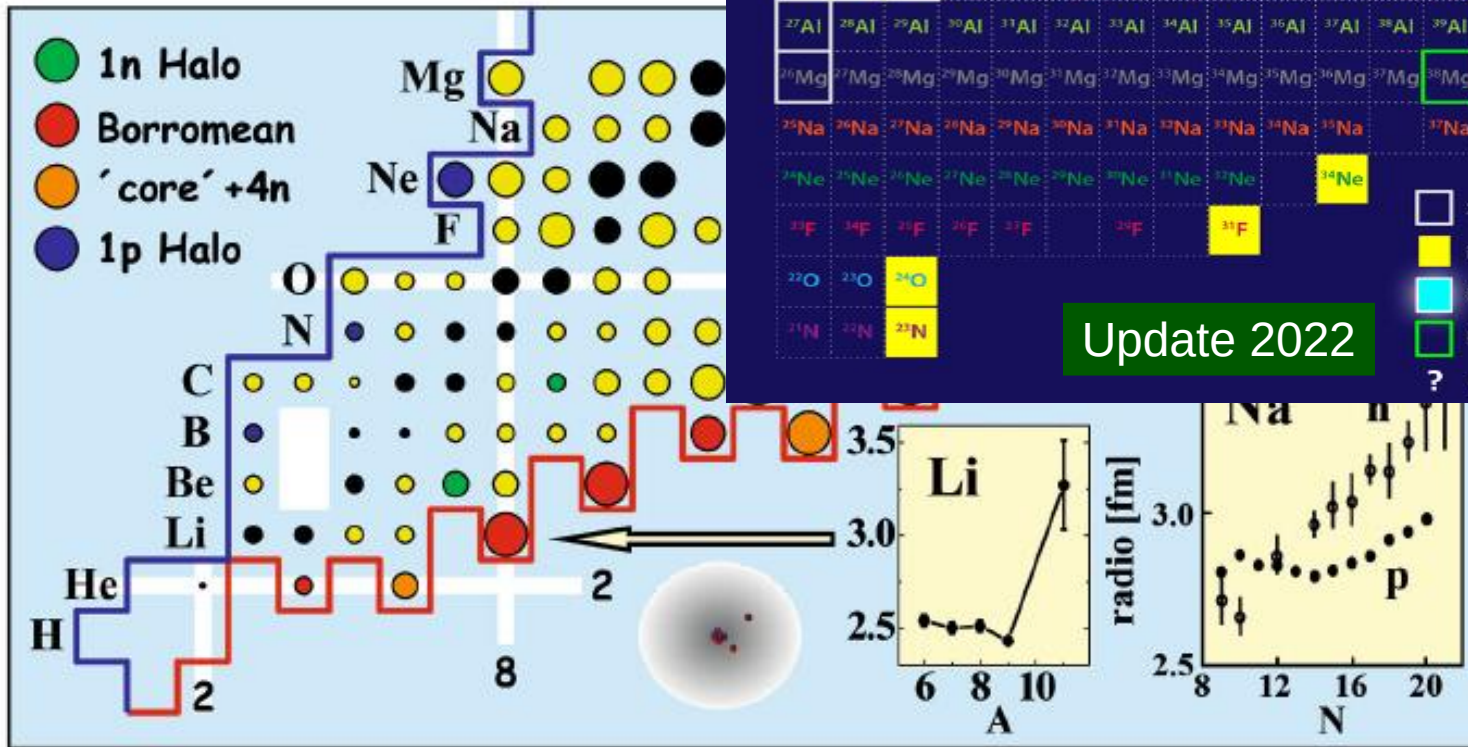
- ★ Several Borromean nuclei (e.g.  ${}^6\text{He}$ ,  ${}^{14}\text{Be}$ ,  ${}^{22}\text{C}$ )
- ★ Some single-neutron halo nuclei (e.g.  ${}^{11}\text{Be}$ ,  ${}^{19}\text{C}$ )
- ★ Some 4n correlations ( ${}^{19}\text{B}$ )
- ★ Rare cases of proton halo (e.g.  ${}^{17}\text{Ne}$ )
- ★ The strange case of  ${}^{24}\text{O}$  and  ${}^{31}\text{F}$  limiting species

2015: n-drip line was reached up to  $Z=11$  (Sodium)

**What next?**

# An unexpected variety of configurations

Other phenomena have been put in evidence and are currently under study using reactions with exotic beams. The **drip lines** have been reached because they are closer to the Valley.



- ★ Borromean nuclei (6He, 14Be, 22C)
- ★ single-neutron halo (e.g. 11Be, 19C)
- ★ 4n correlations (19B)
- ★ Rare cases of proton halo (e.g. 17Ne)
- ★ The strange case of 24O and 31F border guys

2015: n-drip line was reached up to Z=11 (Sodium)

**What next?**



# An unexpected variety: clusters

Archaeologists are careful when they suspect that some nice hidden structure and configuration can emerge from the gross region they excavate.

Similarly, nuclear physicists for many decades were supposing that in some nuclei the wave function may have contribution from **cluster configurations (i.e. groups of strictly correlated nucleons in the medium)**

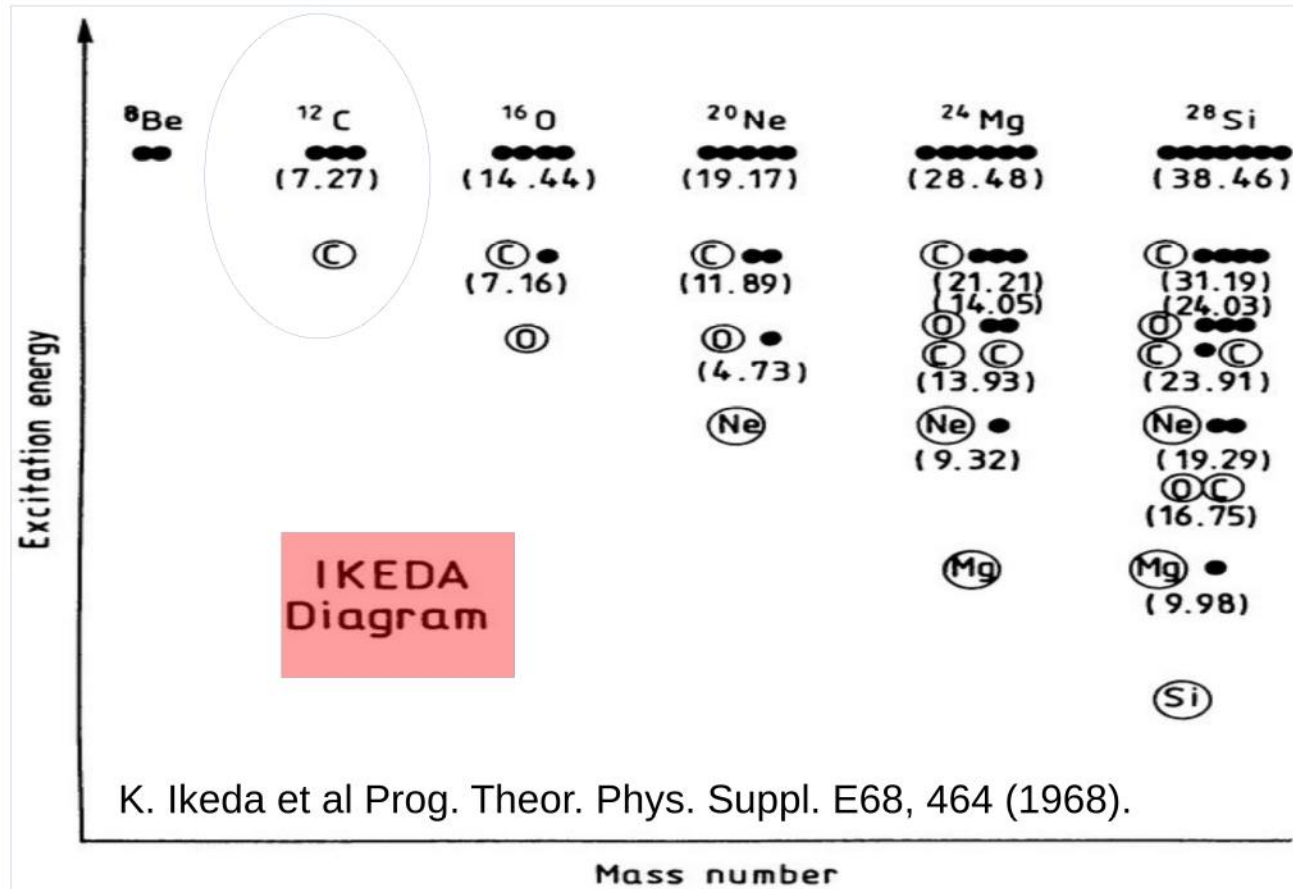
In particular, (due to their high binding energy) nucleon quartettos of **alpha-particles** were expected.

As in archaeology discovery, the underlying structure can manifest when the nucleus is *gently* excited just close to the separation energy (at the **threshold**)



# An unexpected variety

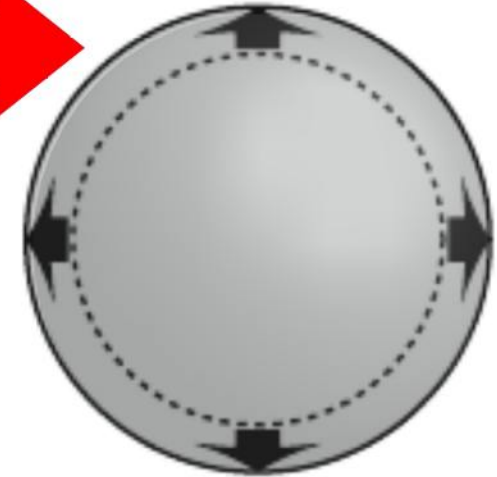
60 years ago, it was proposed that in  $N=Z$  nuclei, a hidden structure made of alpha particles could be evidenced when light (stable) nuclei are excited close to the separation energy



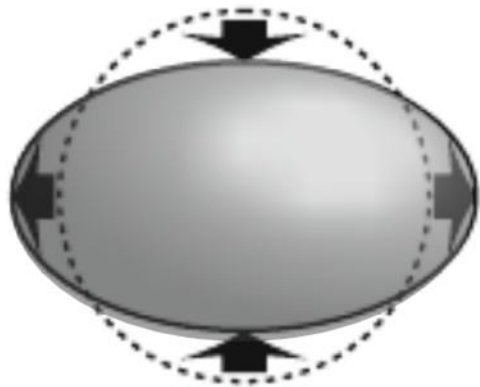
# An unexpected variety

Nuclei don't like to change density (incompressible to a large extent) so that other modes are excited when you start to put energy

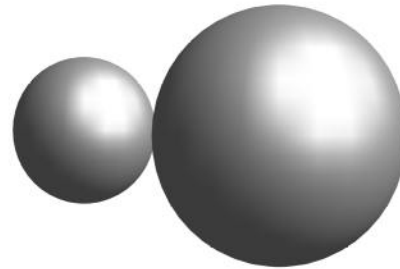
unfavourable



Shape oscillations are more favoured and also cluster formation because **they both don't change the density**



Shape oscillation



clustering



favourable



# An unexpected variety

The saturation property of nuclei at the drip lines breaks up and many associated features change a lot. Thus the cluster structures, when “*climbing the canyon*”, can reveal unexpected phenomena

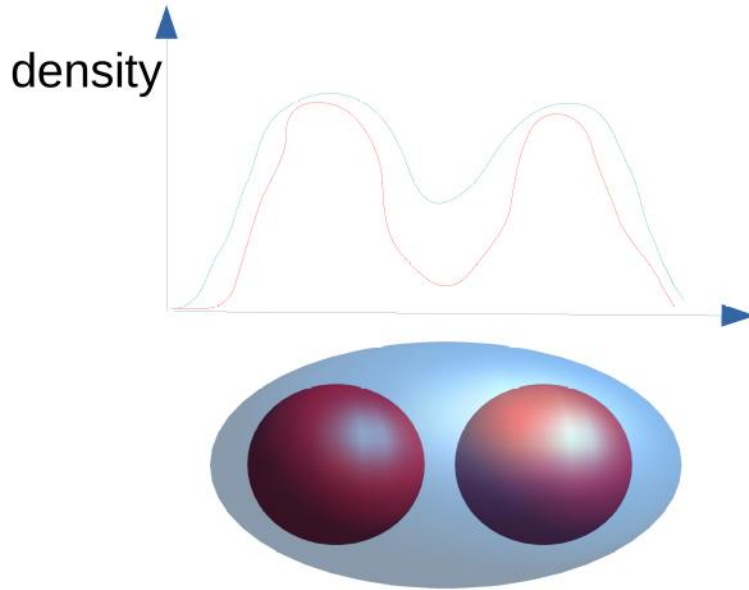
Consider a very neutron rich nucleus:  
does this unbalance favour or disfavour  
clustering?



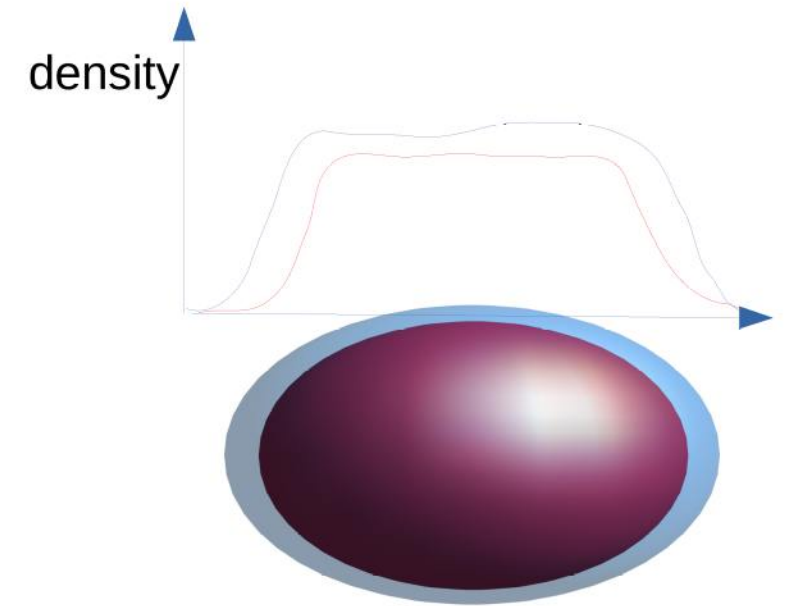
# An unexpected variety

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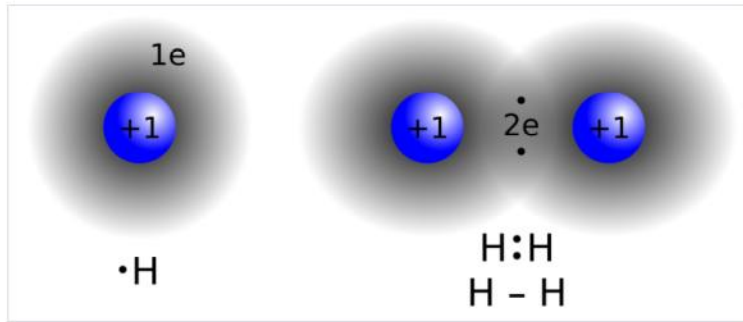
Clustering **favoured** because the  
symmetry Energy is *locally* reduced



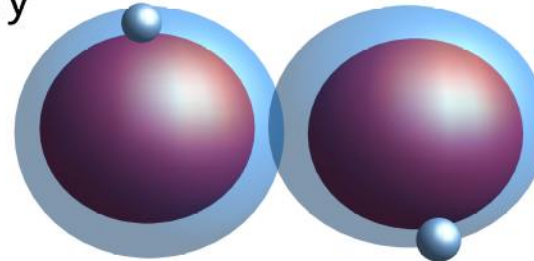
Clustering **disfavoured**  
because the symmetry  
Energy is *globally* reduced

# An unexpected variety

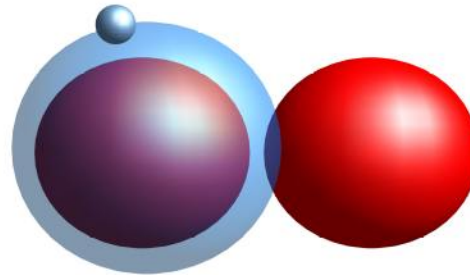
Also the **shell structure** of nuclei, due to their quantum nature, comes to play and changes with strong p-n unbalance; the shells are built in a non spherical well



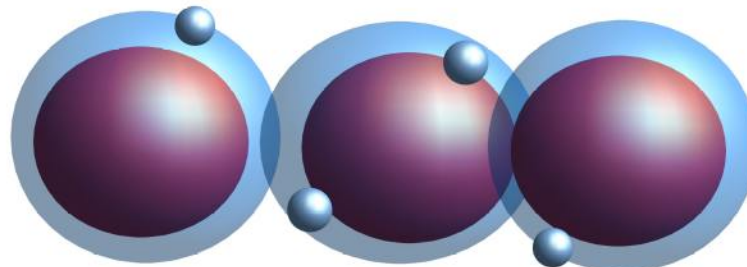
Remind chemistry



Molecular configuration with a kind of **covalent** bond



Atomic configuration with a kind of **ionic** bond



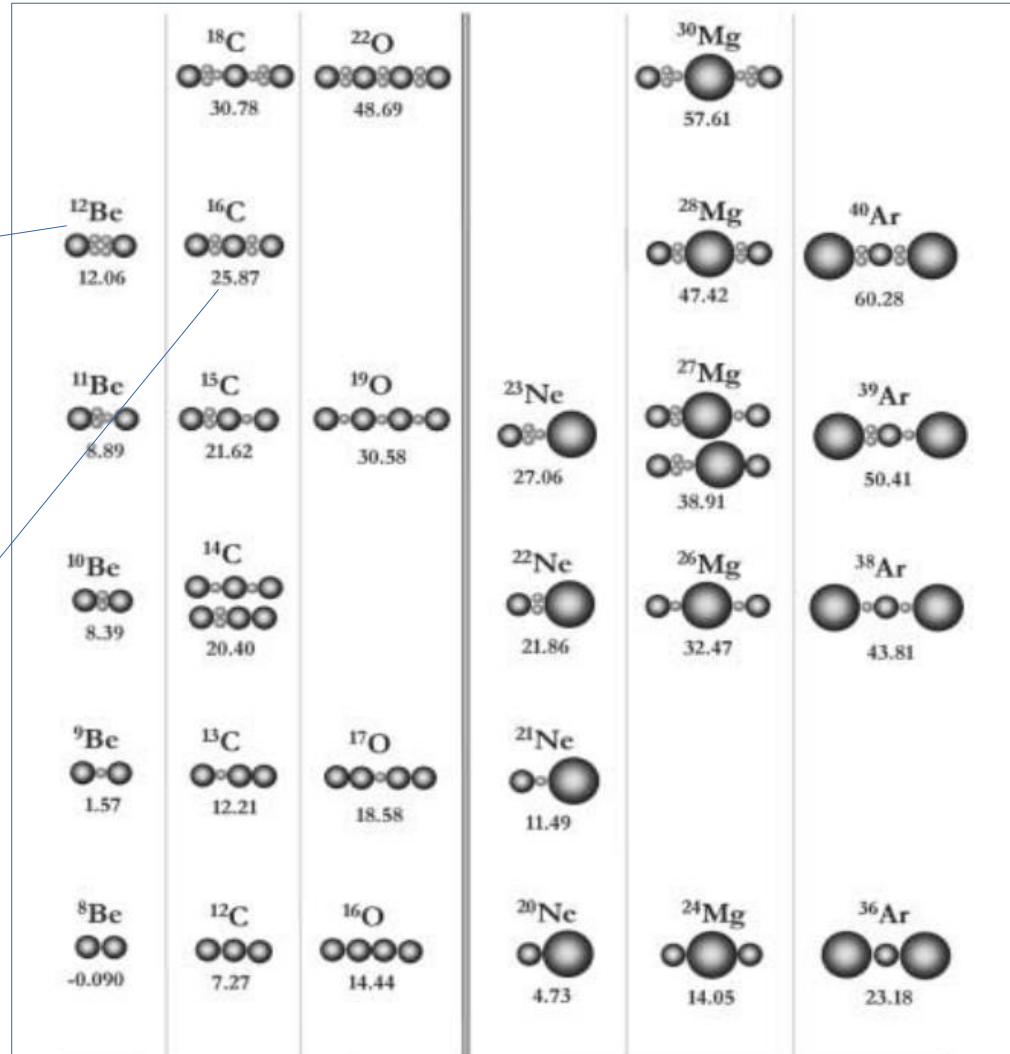
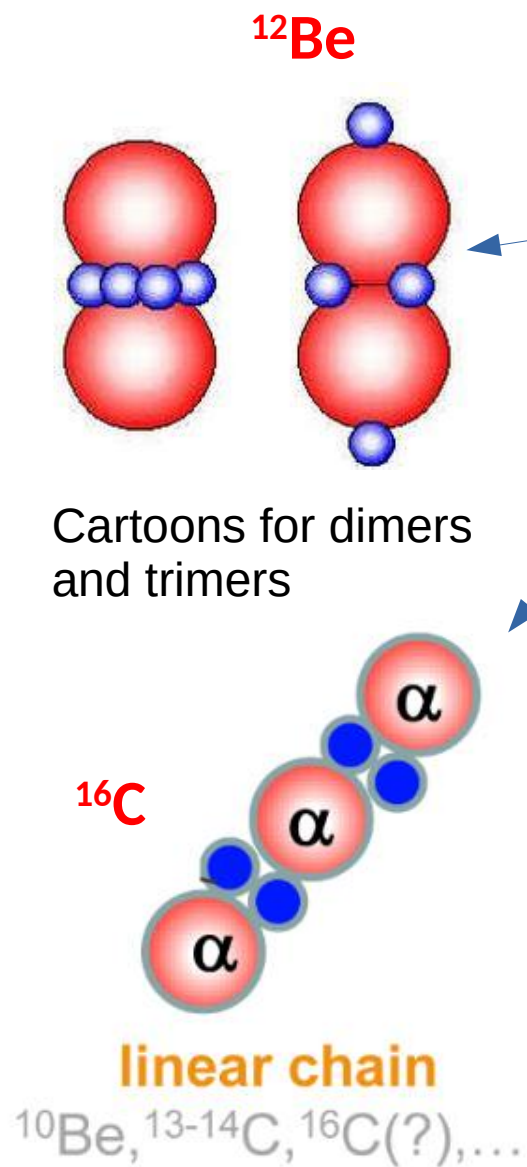
Peculiar configurations allowed by the excess nucleons acting as valence electrons

Configurations appear looking like atomic or molecular systems where **valence hadrons are exchanged or shared to establish the (weak) bond**

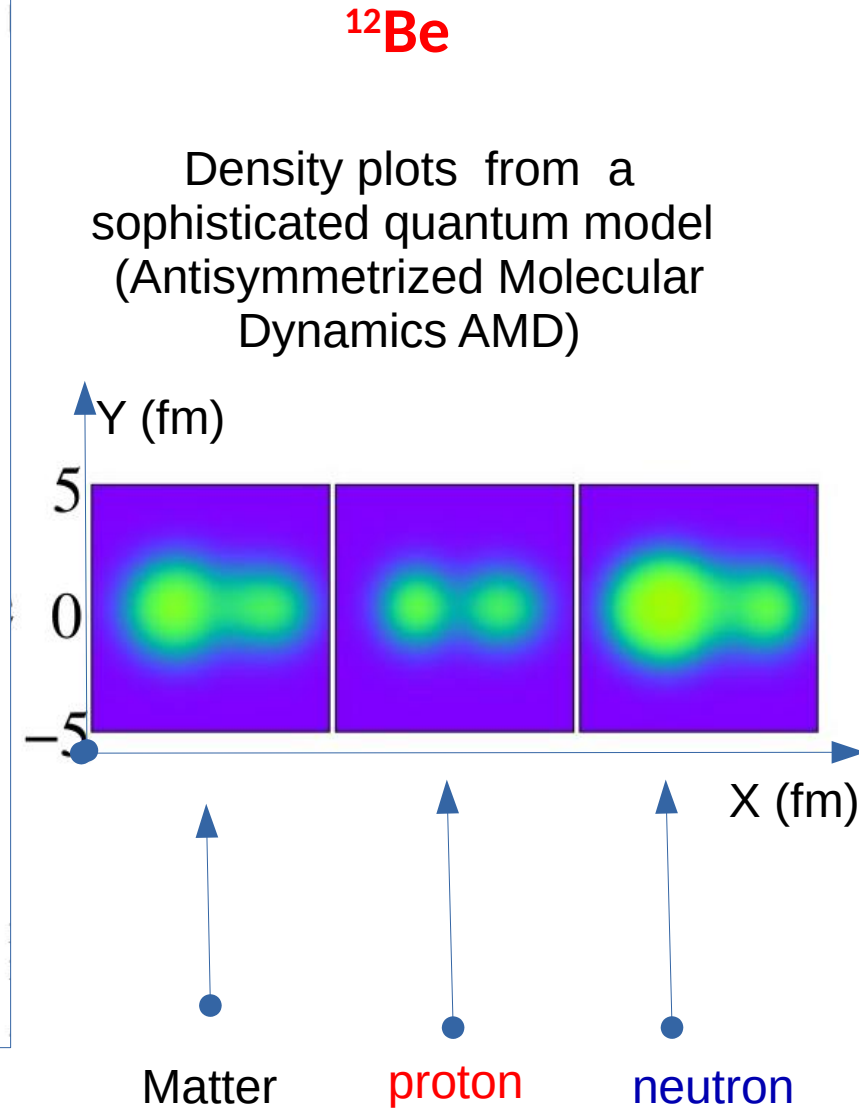
Many shapes manifest for exotic nuclides that cannot exist in stable species



# An unexpected variety

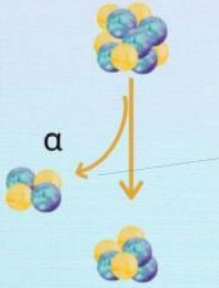


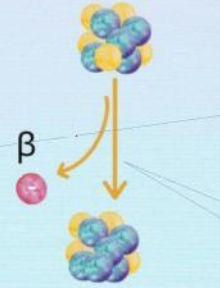
A proposed new IKEDA diagram

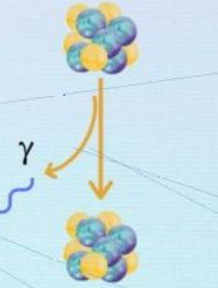


# New radioactivity modes

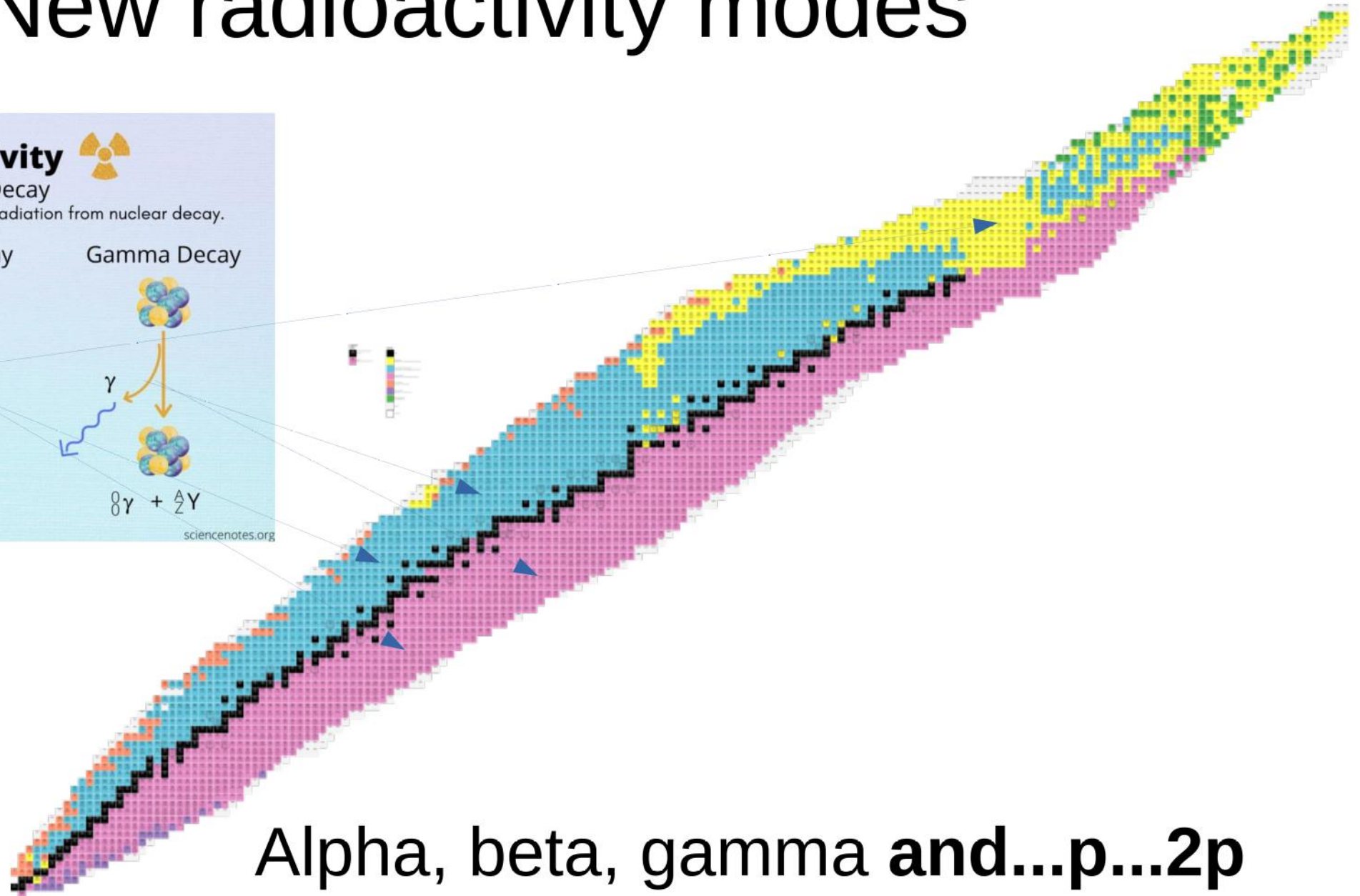
**Radioactivity**  
Radioactive Decay  
Radioactivity is the emission of ionizing radiation from nuclear decay.

**Alpha Decay**  
  
 ${}^4_2\text{He} + {}^{A-4}_{Z-2}\text{Y}$

**Beta Decay**  
  
 ${}^0_{-1}\text{e} + {}^A_{Z+1}\text{Y}$

**Gamma Decay**  
  
 $\gamma + {}^A_Z\text{Y}$

sciencenotes.org



Alpha, beta, gamma and...p...2p

# New radioactivity modes

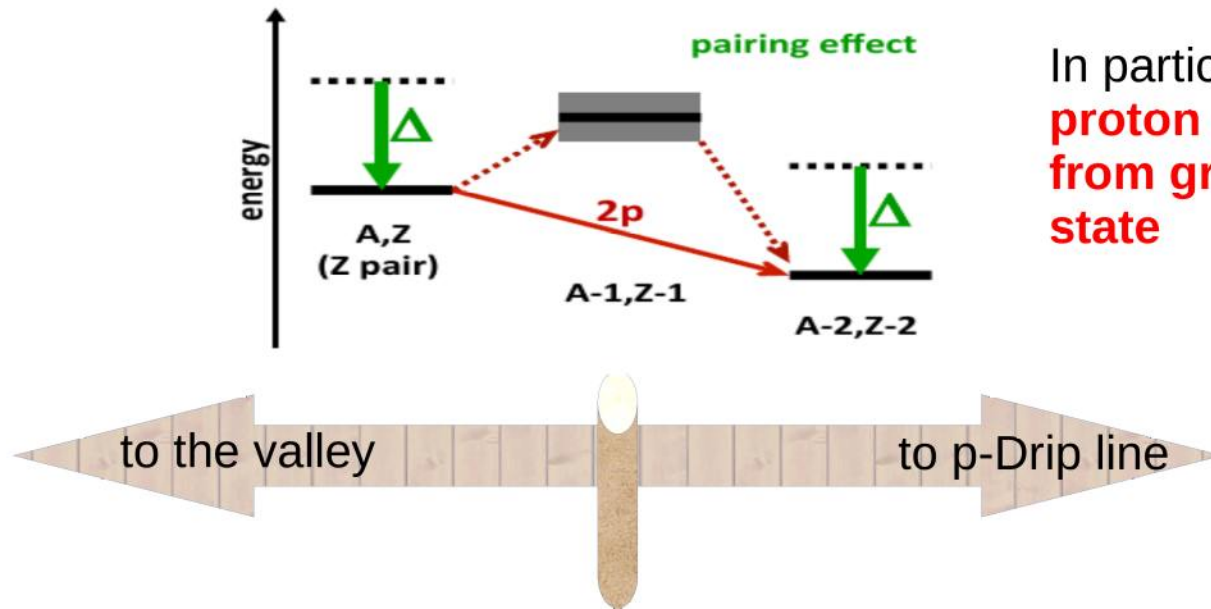
- Close to the p-drip line the proton excess is high and the instability grows
- nuclei can decay from ground state via one-proton (if odd-Z) or two-proton emission (if even-Z)

## 1 proton decay

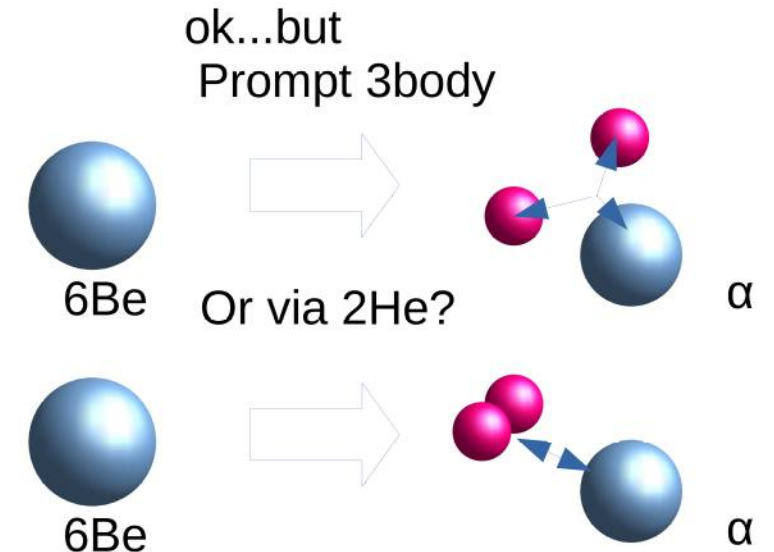
Already **observed the first time at GSI in 1980** via fusion reaction with stable beams (fusion reactions with **stable** beam-target pair typically produce nuclei toward the p-rich side of the valley)

## 2 proton decay

difficult experiments but feasible without radioactive beams. The latter, however, allow for a deeper investigation towards the p-drip region and to access very exotic decay.



In particular **2-proton decay from ground state**





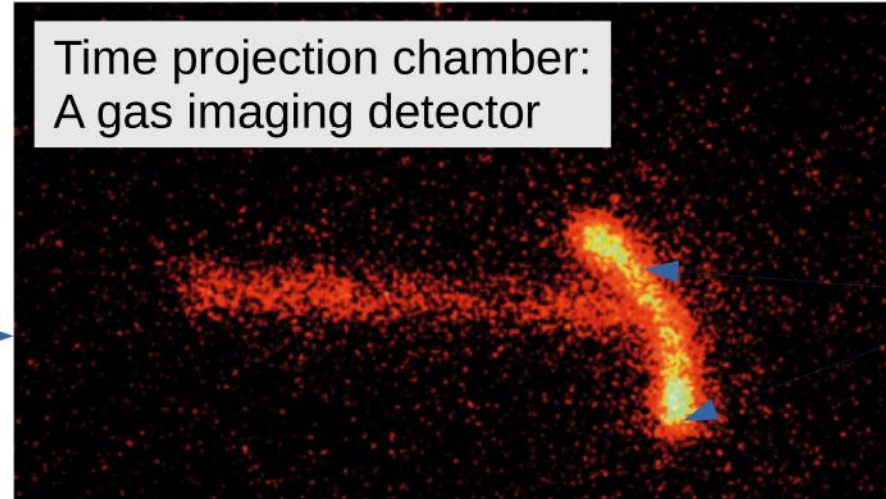
# New radioactivity modes

2 proton from the ground state: expected when the binding energy of a proton pair is less than that of one proton. This can occur for nuclei close to the drip line

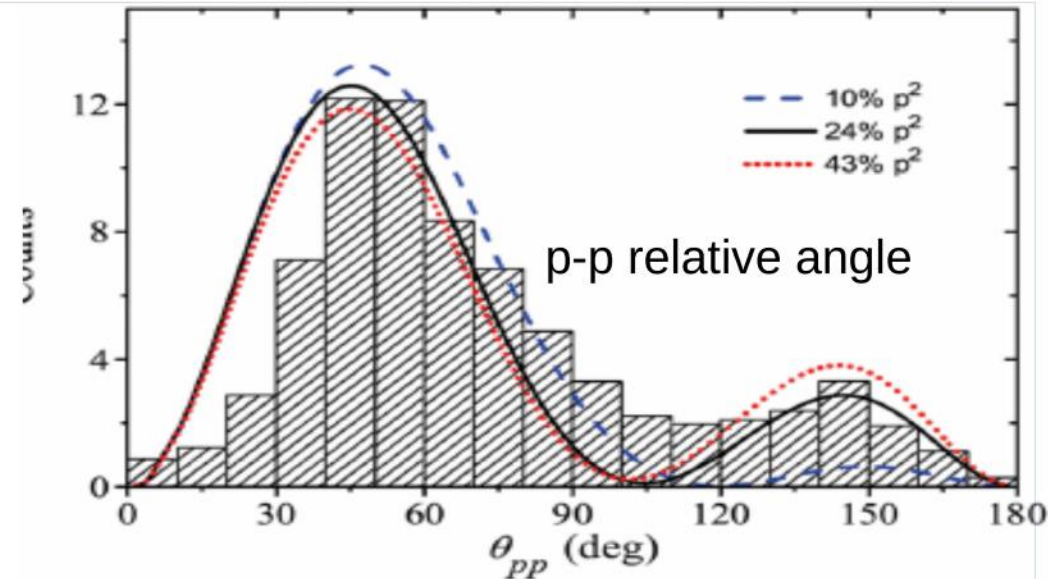
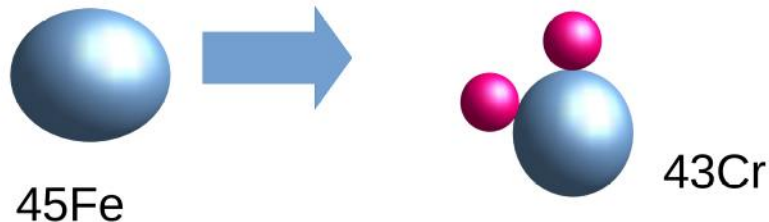
First observation of a correlated two-proton decay from g.s.  
**2002 at GANIL**

TPC photographs of the 2p decay from g.s. of  $^{45}\text{Fe}$  taken in **2007 at MSU**

$^{45}\text{Fe}$  ion  
26 protons  
19 neutrons  
 $T_{1/2}=2.6\text{ms}$



Angular correlation demonstrate it's **direct 3 body** decay!

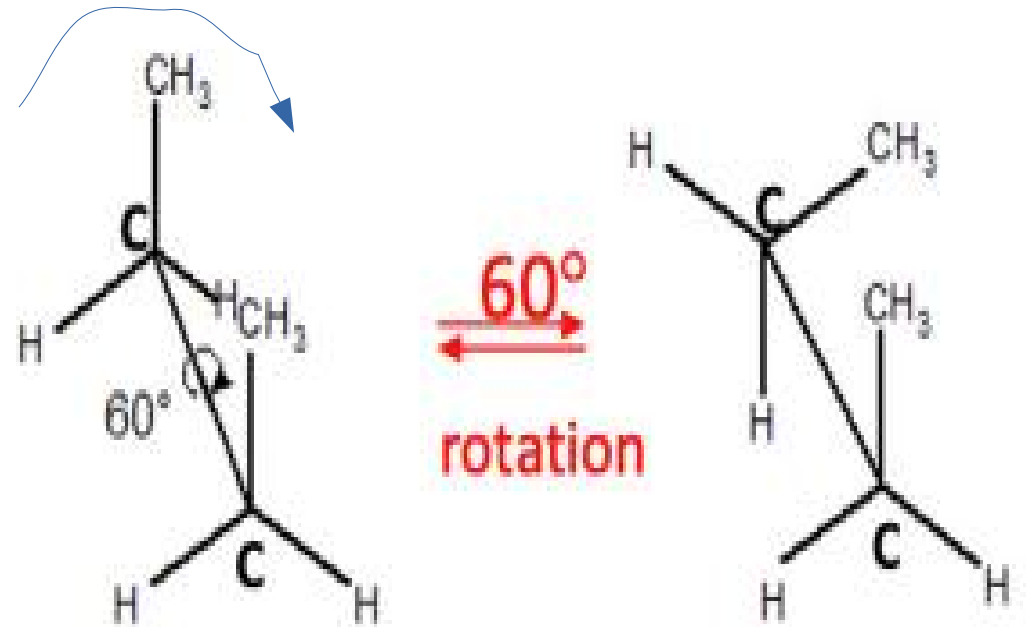


# Shape Coexistence

one chemistry, various shapes

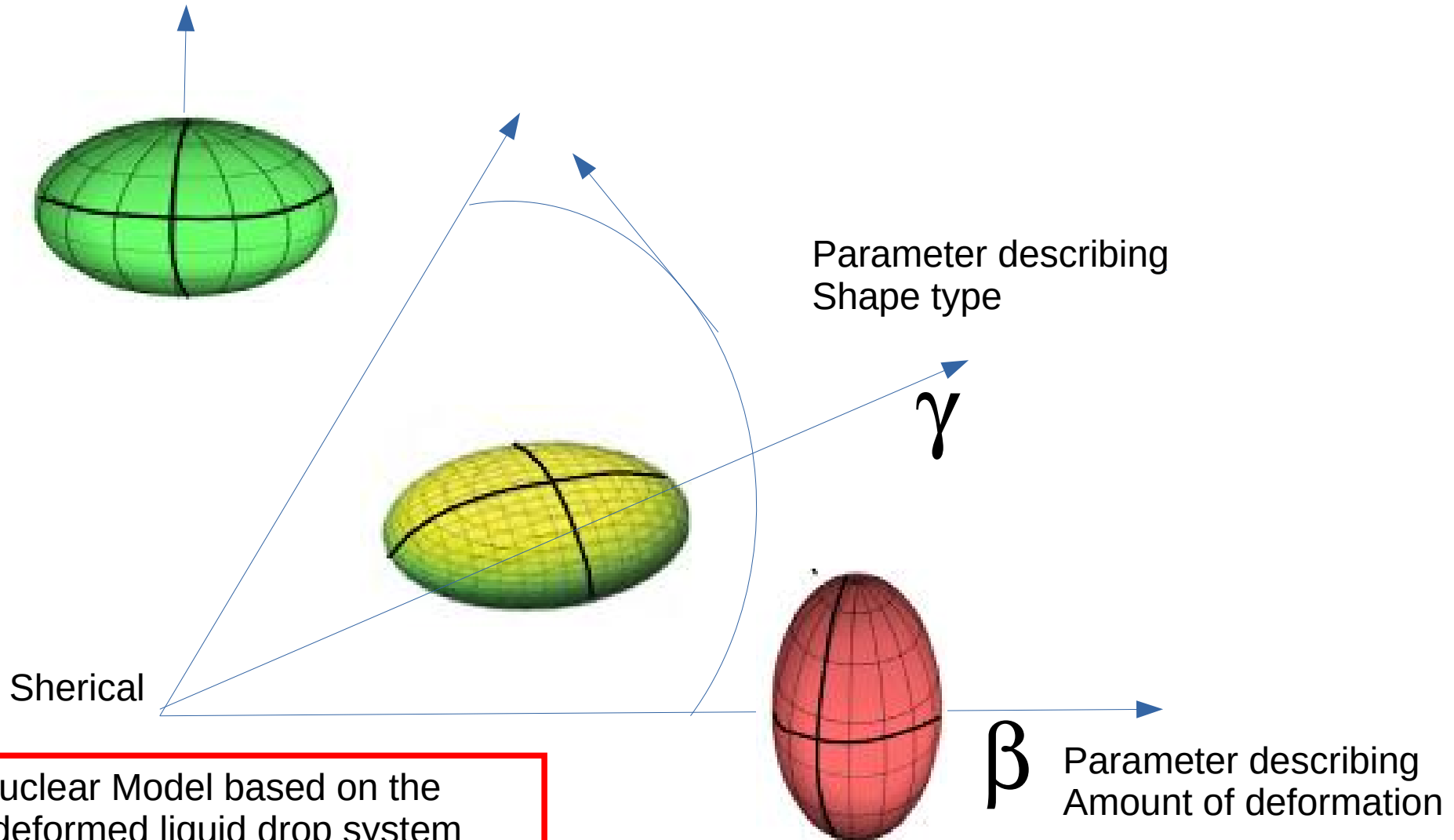
Quantum system phenomenon:  
The system can assume various shapes (rearrangements of the constituents) having close energetic levels. The constituents can be arranged differently

Again in analogy with chemistry



MOLECULES, ISOMERS

# Nuclear Shape in two parameters (for the class of quadrupole deformation)



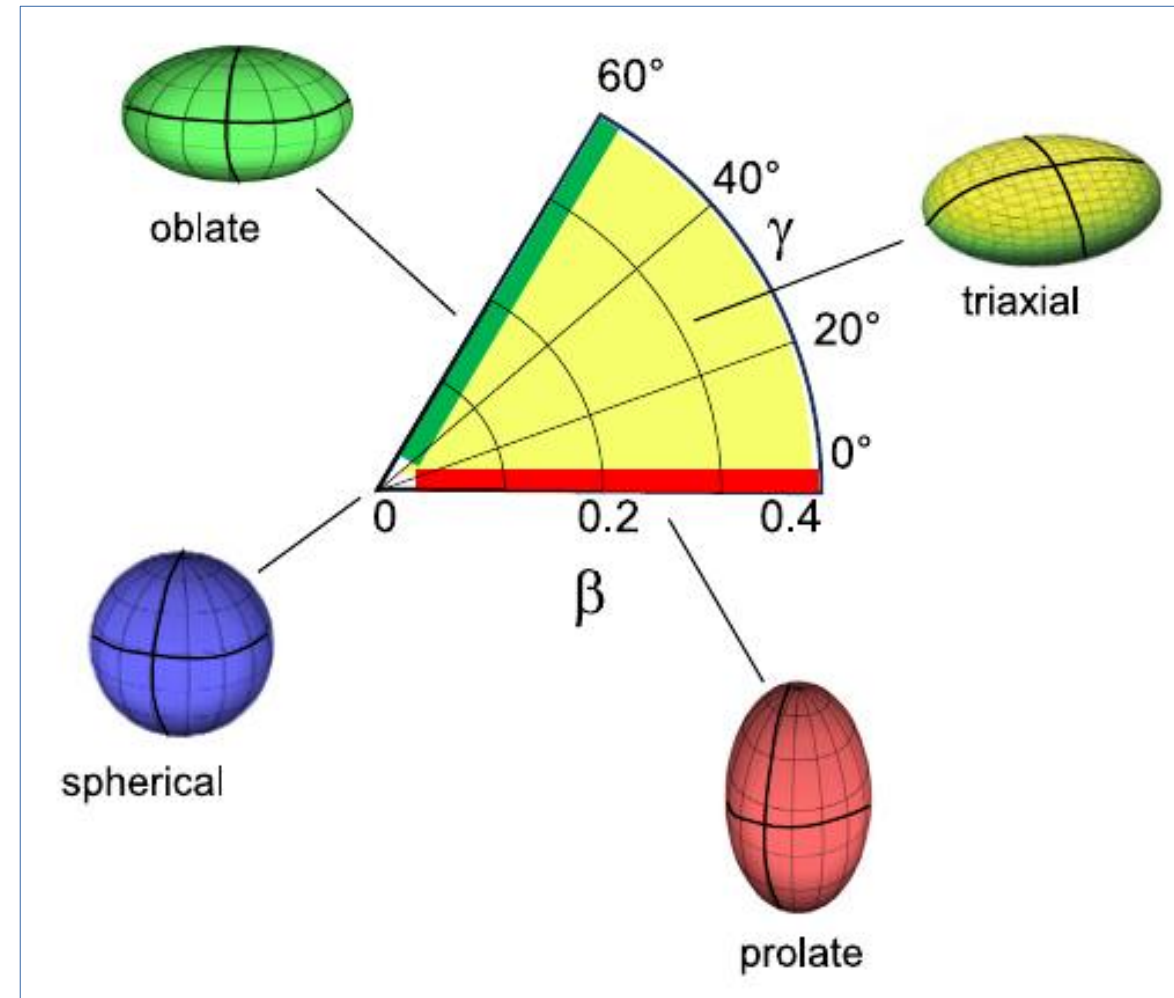
Semiclassical nuclear Model based on the analogy with a deformed liquid drop system



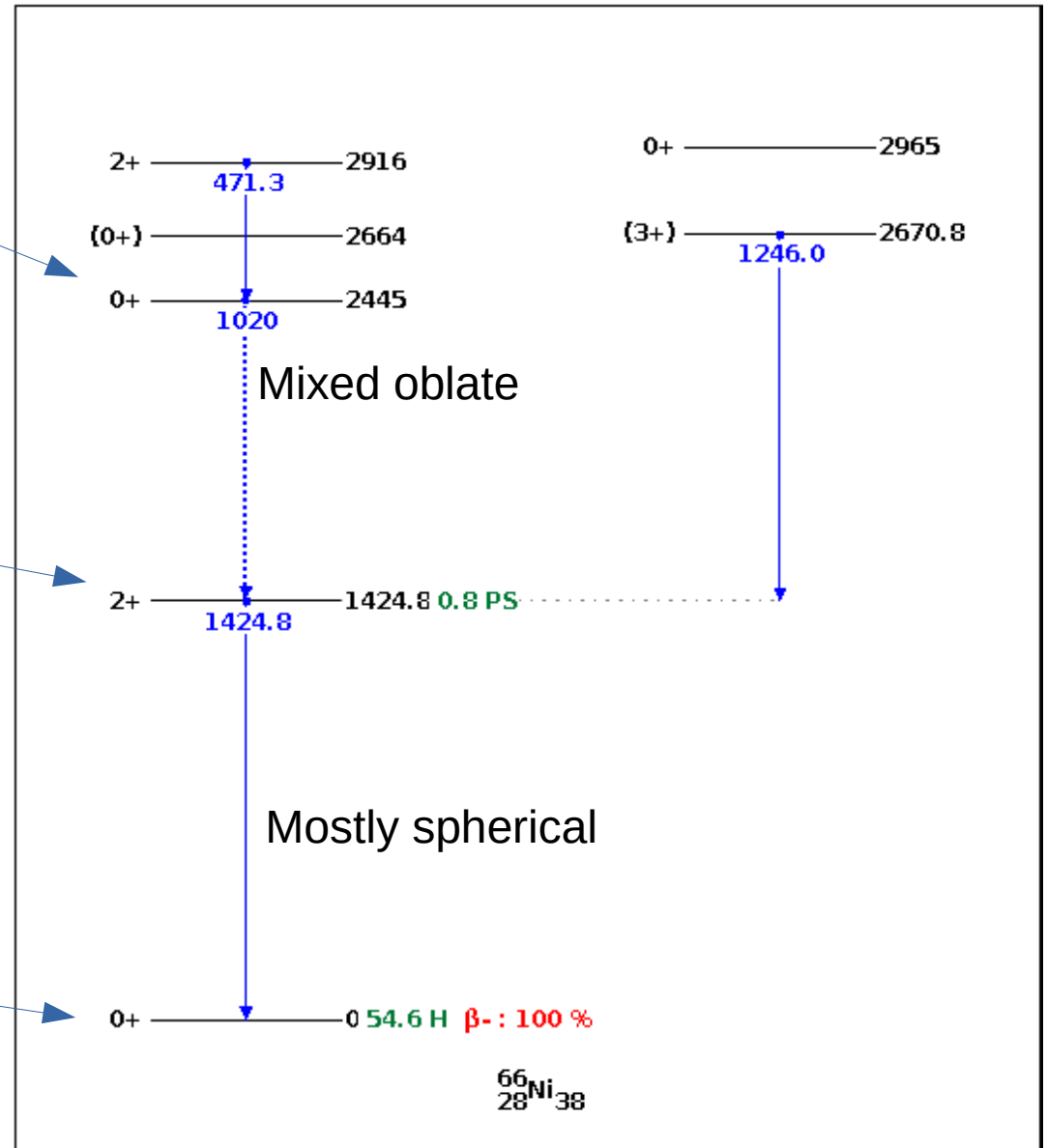
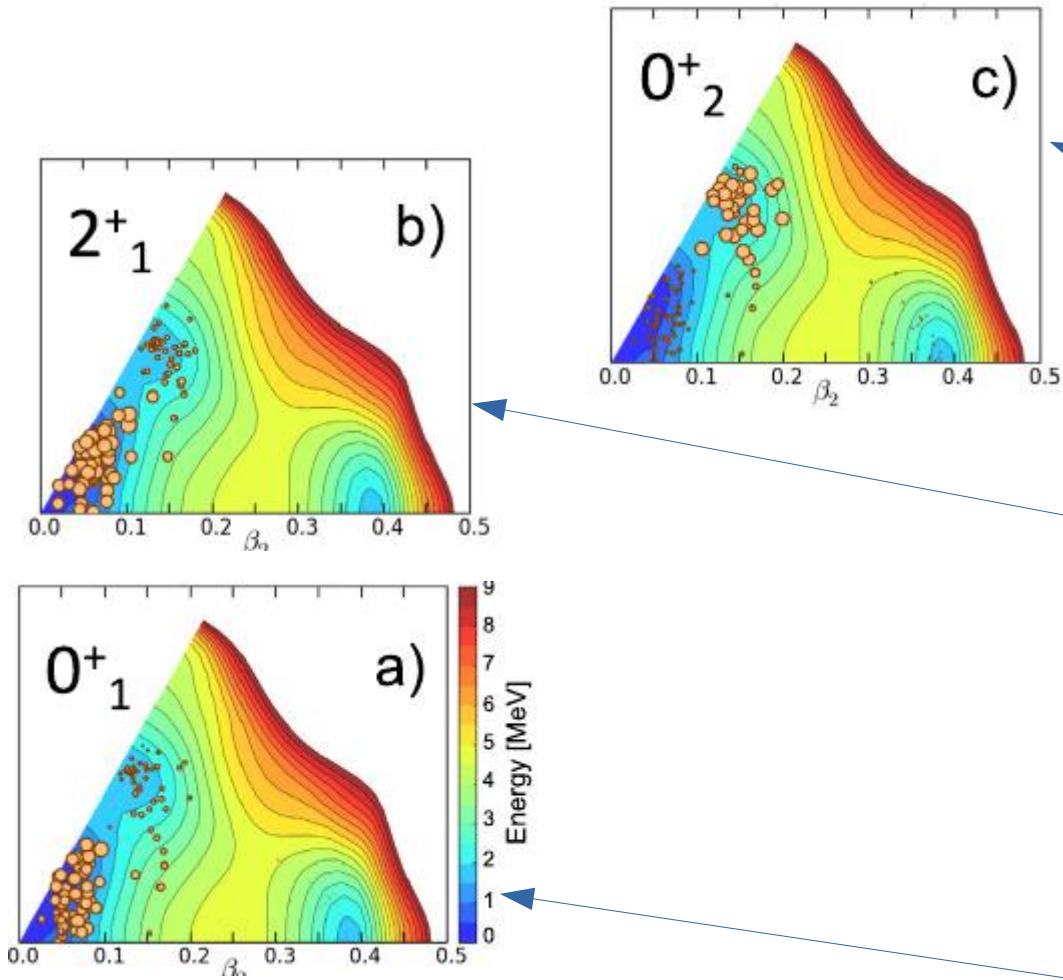
# Shape Coexistence in nuclei the discovery in the '70s

At ISOLDE-CERN, the study of neutron deficient **Hg and Pb** isotopes, showed this new facet of nuclear structure

Similarly, **Kr isotopes** were soon found to present almost *degenerate* (i.e. same energy) prolate and oblate configurations

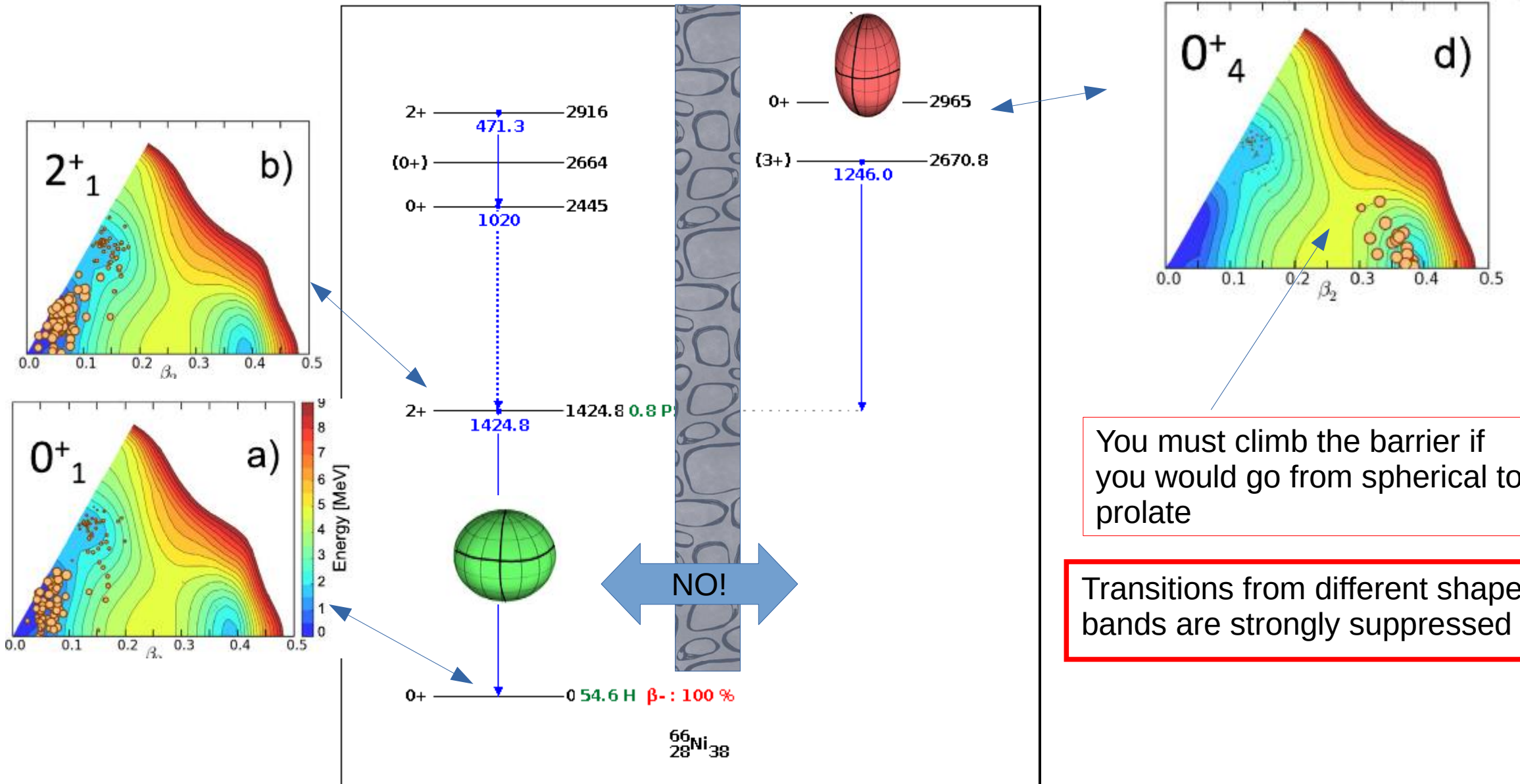


# The example of $^{66}_{28}\text{Ni}$ (unstable)



At the ground state an almost spherical shape energy band is found

# The example of $^{66}\text{Ni}$ (unstable)



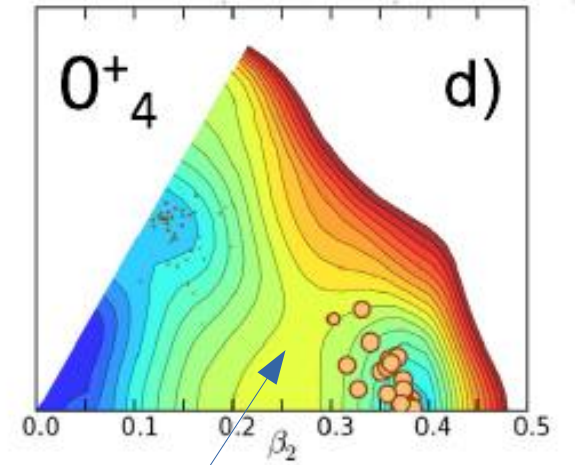
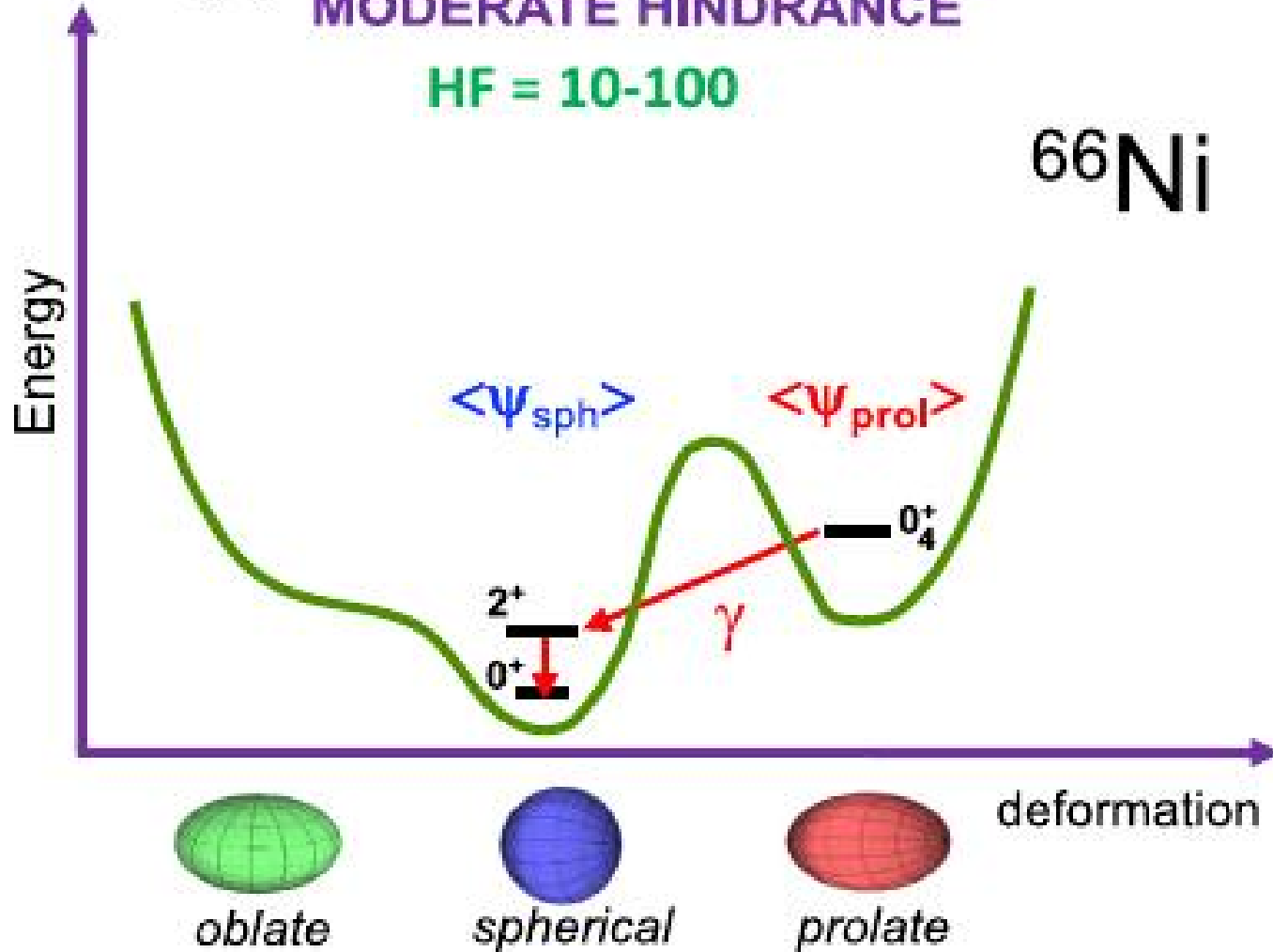


# The example of $^{66}\text{Ni}$ (unstable)

(c) MEDIUM BARRIER and MODERATE HINDRANCE

HF = 10-100

$^{66}\text{Ni}$

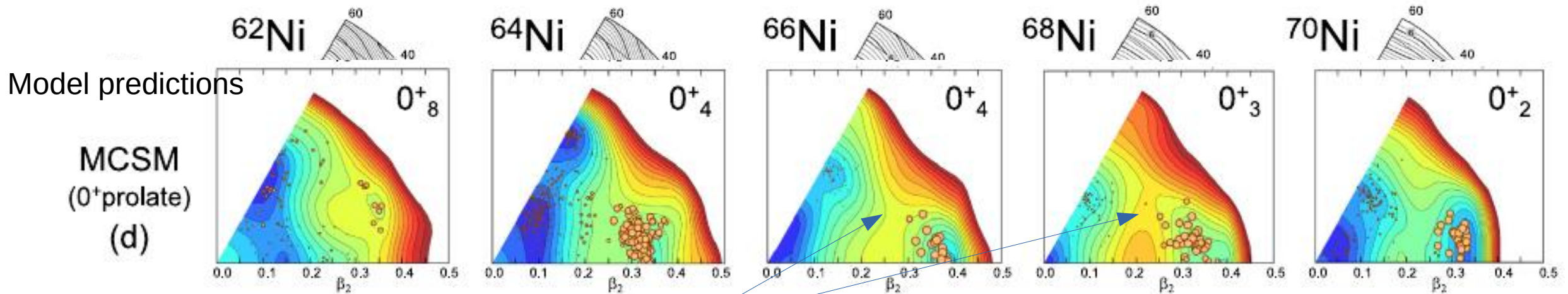
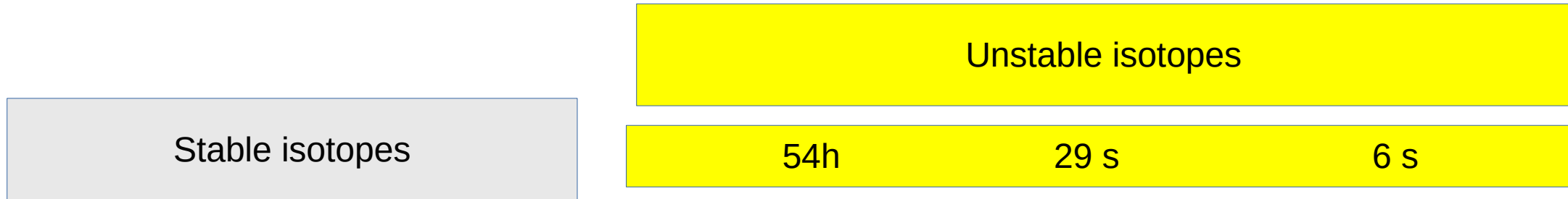


You must climb the barrier if you would go from spherical to prolate

Transitions from different shape bands are strongly suppressed

# A very rich information exploring the “canyon” slope

Even-even  
 **${}_{28}\text{Ni}$  chain**

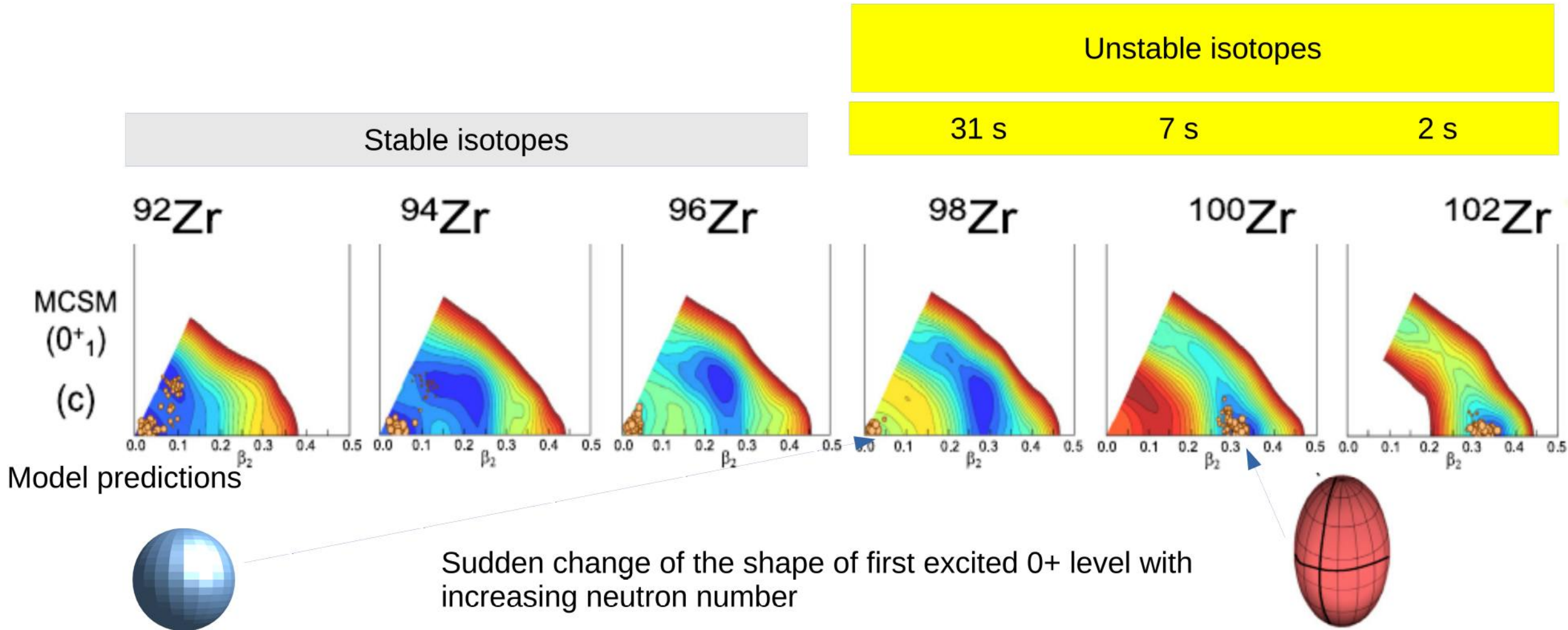


Developping the barrier in deformed excited  $0^+$  band

(MCSM = MonteCarlo Shell Model)

# A very rich information exploring the “canyon” slopes

Even-even  
 **$^{40}\text{Zr}$  chain**





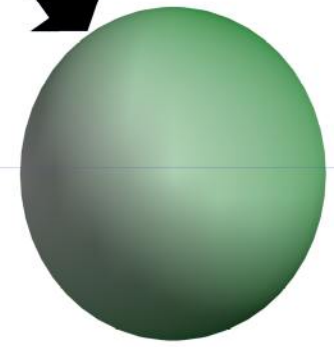
# Coulomb Excitation: nuclear electric fields to gently excite nuclei

An excellent experimental technique also for **SPES**

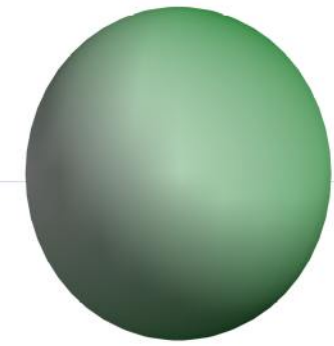
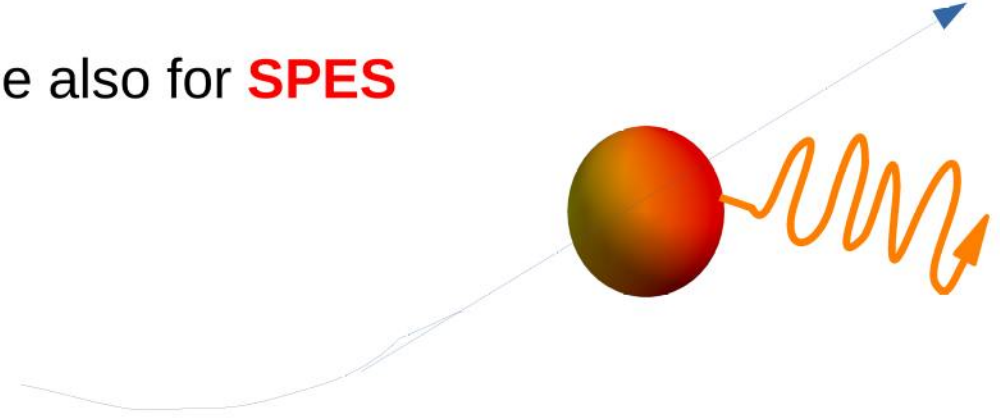
Projectile nucleus



Target nucleus



Far distance:  
Coulomb interaction only

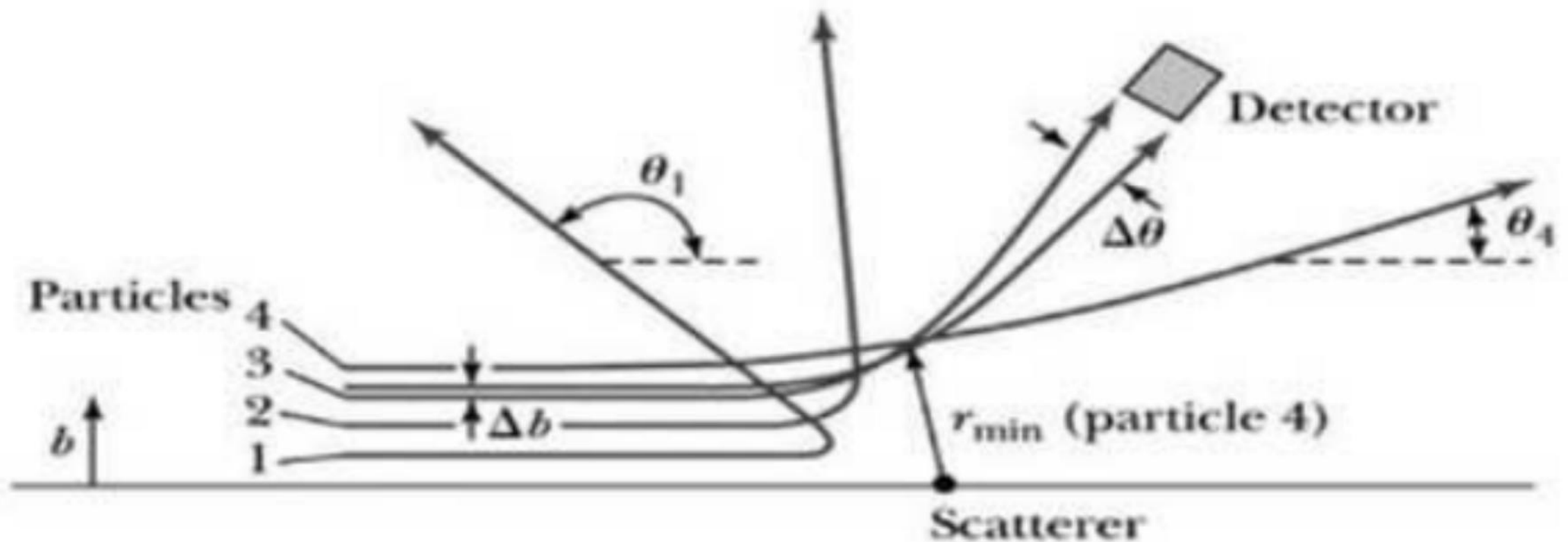


Time line



The nucleus is not a point like charge but a complex system  
It gets excited and one studies its decay to ground state

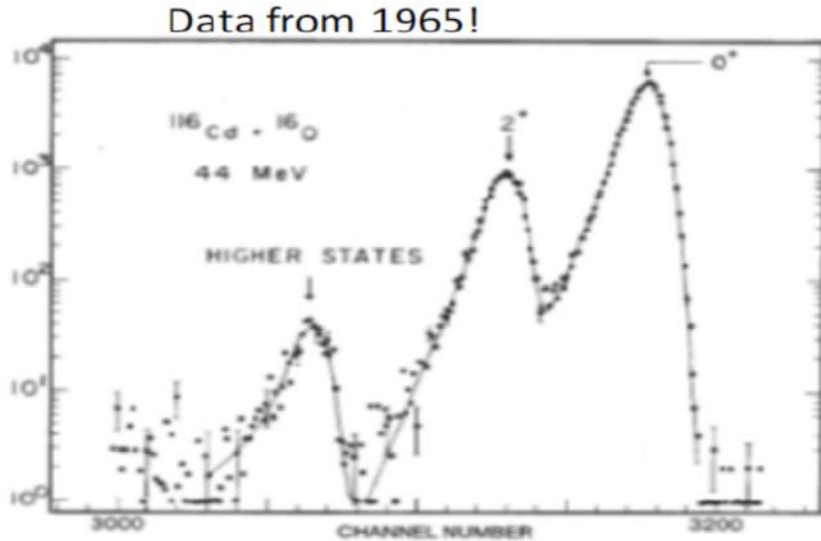
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Far distance:  
Coulomb interaction only

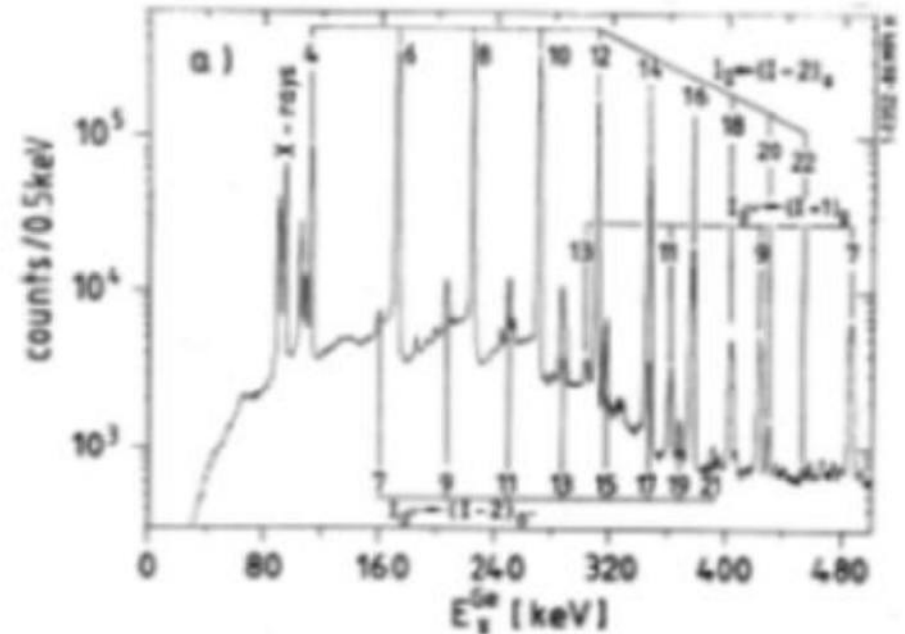
The projectile is not a point like charge but a complex system  
It gets excited and one studies its decay to ground state

# Coulomb Excitation with stable light beams



- First experiments ('60)
- light (and stable) ion beams
- Spectrometers
- no gamma-detectors

- Experiments from the '70s
- Also Germanium gamma-detectors
- excellent gamma-E resolution
- unprecedented details of nuclear structure





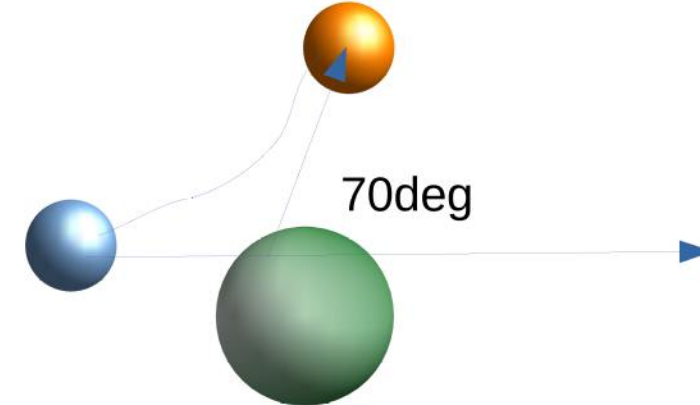
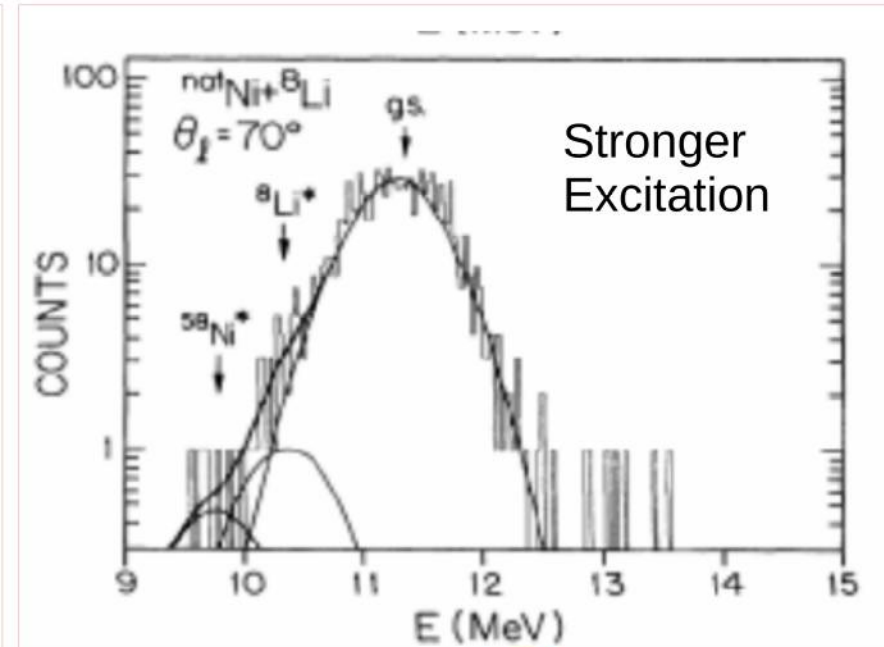
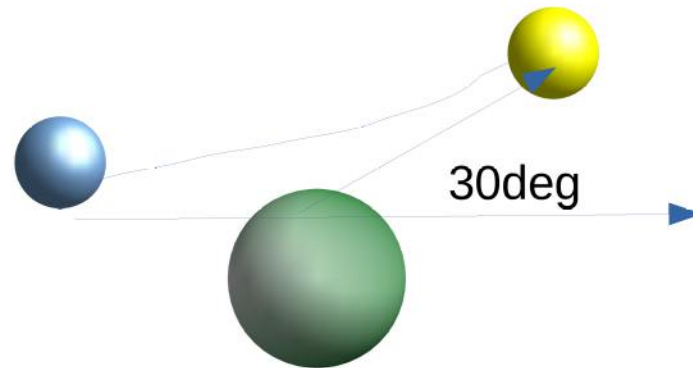
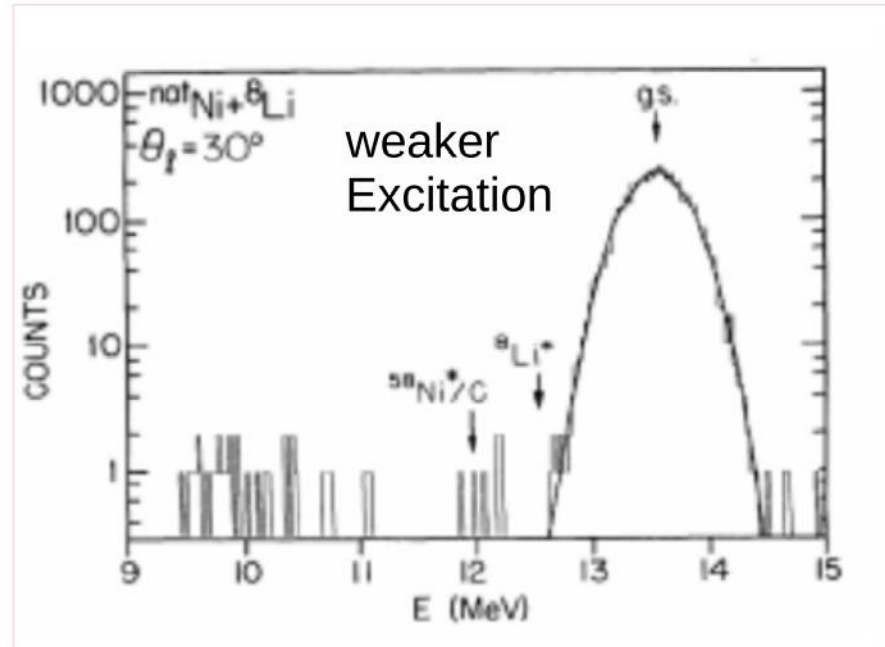
# Coulomb Excitation

## 1991: first experiment with unstable ions

J.A. Brown  
FIRST EXPERIMENT WITH a  
Radioactive beam (USA)  
8Li from n-pickup of 7Li on a  
thick Be target

**$^8\text{Li} + \text{natNi}$  at 15 MeV**

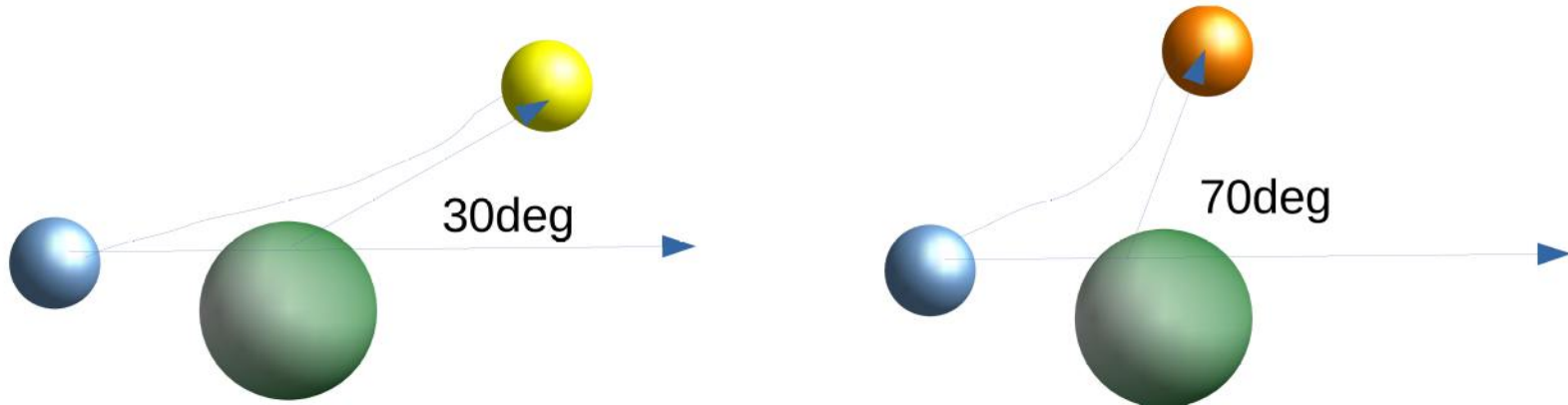
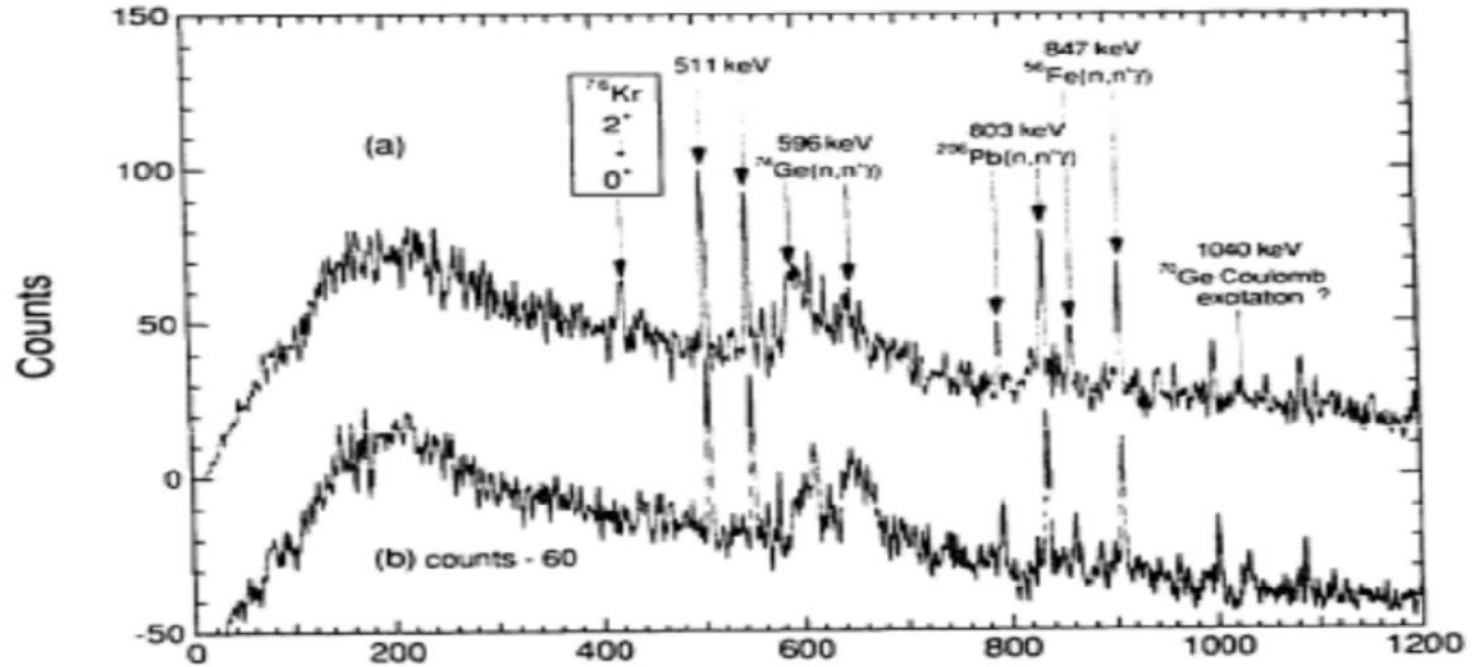
- T1/2 for 8Li=870 ms
- NO GAMMA DETECTOR
- ONLY DEFLECTED Lithium was detected



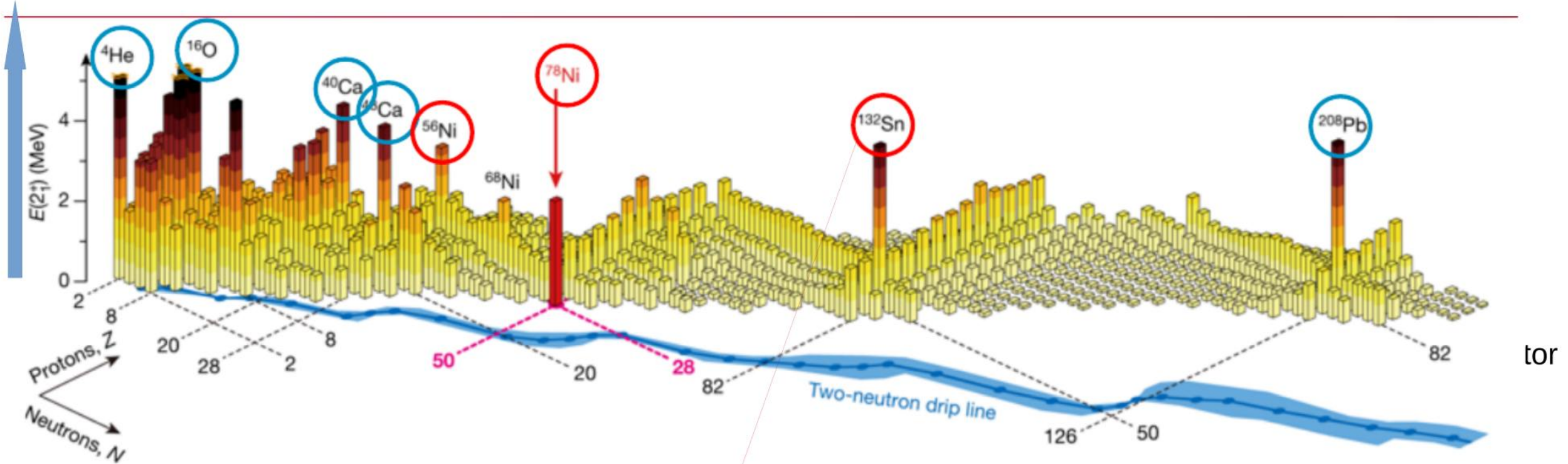
# Coulomb excitation: 1992: exotic beams, gamma and particle detectors

M.Oshima  
FIRST EXPERIMENT WITH a  
Radioactive beam AND GAMMA  
DETECTOR (JAPAN)

$^{76}\text{Kr}$  from 3n-stripping of  $^{70}\text{Ge}$  on a  
thick Be target



# Coulomb excitation: a strong method to explore the canyon



- For double-magic nuclei the gap of the 2+ excited state and g.s. is large
- nuclei are in this case spherical
- BUT:
- Is this still valid towards the n-drip line?
- The 'reference' case of **132Sn** (also at SPES)

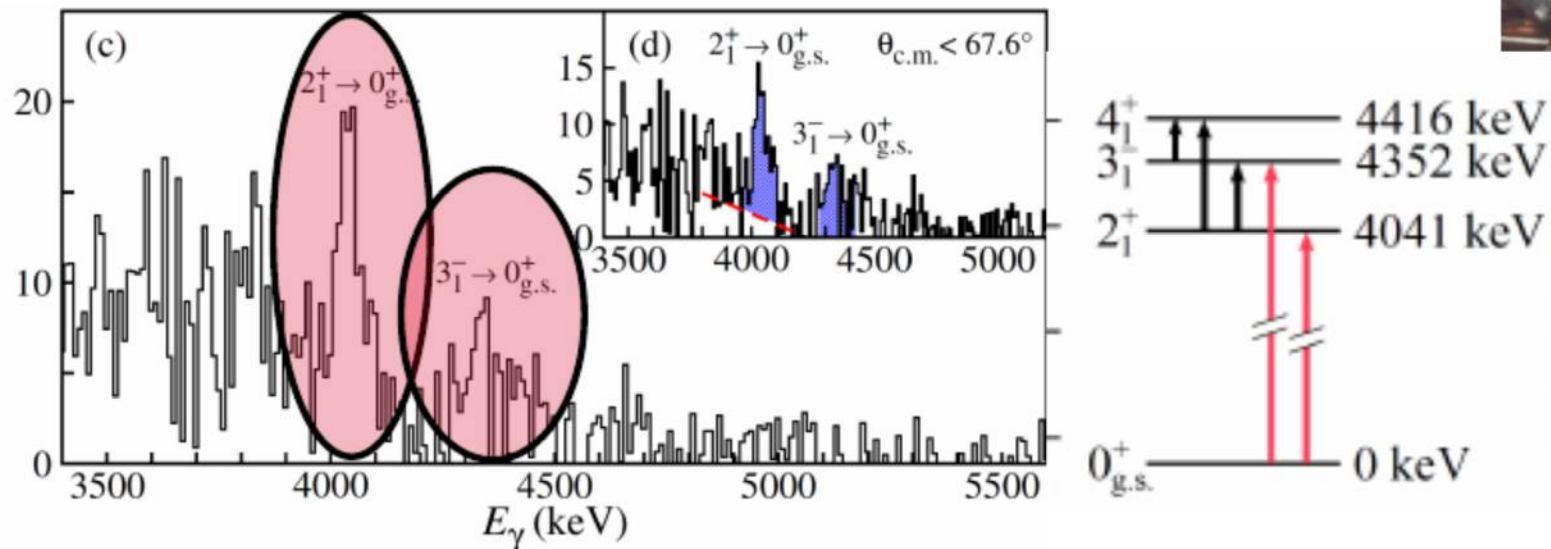


# The reference case of $^{132}\text{Sn}$ (also at SPES)

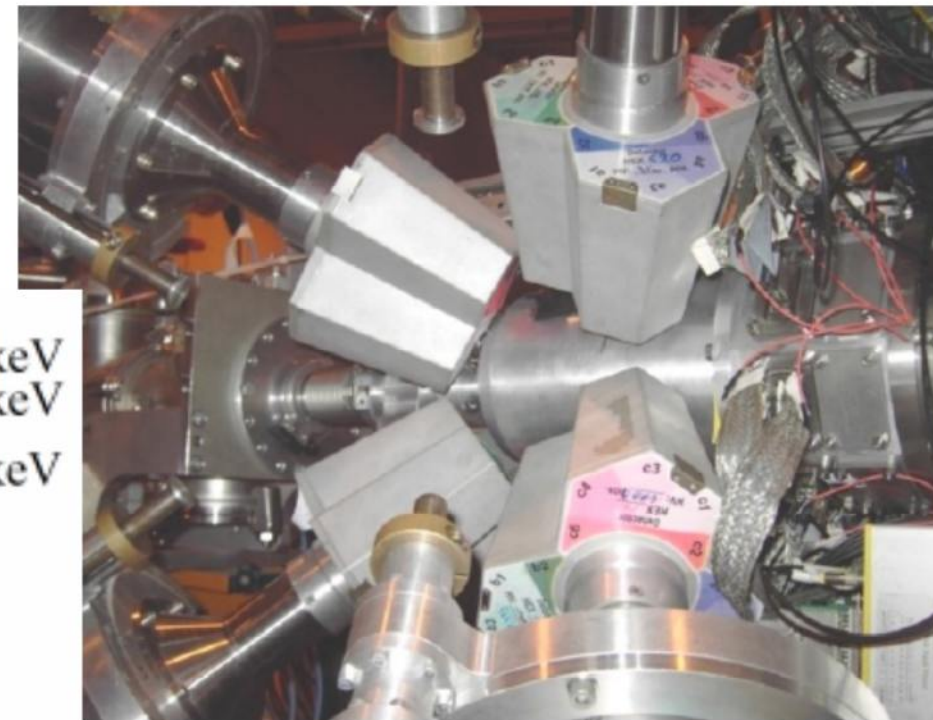
- First study at ISOLDE with the MINIBALL array
- Very good experiment published in 2018

Low energy Coulomb excitation

$^{206}\text{Pb} + ^{132}\text{Sn}^{31+}$  (@ 5.49 MeV/u)



MINIBALL Gamma detector @ CERN



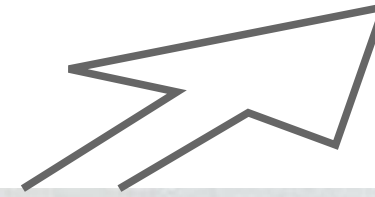
- First determination of the lowest energy level of  $^{132}\text{Sn}$
- Comparison with Shell model advanced calculations
- Strong hint to confirm the spherical shape
- Still low statistics
- Rather big background of contaminants

A top-10 physics case for the **SPES** facility promising high-rate and high-purity  $^{132}\text{Sn}$  beam at right energy

# Some References and credits

- 1 Kosai Tanabe and Kazuko Sugawara-Tanabe  
*Top-on-top mechanism and the electromagnetic transitions for the triaxial strongly deformed bands in odd mass nuclei*
- 2 Tommaso Marchi, INFN LNL  
*Presentation of the LNL delegation at PSI, Suisse, july 2025*
- 3 Marco Rocchini, INFN FI  
*Presentation of the Gr3 nuclear phys group, CdS Firenze, june 2025*
- 4 Andrea Jungclaus  
*Single particle versus collectivity, shapes of exotic nuclei <https://link.springer.com/article/10.1140/epjp/i2016-16059-9>*
- 5 Isaho Tanihata  
*Nuclear Physics with RIB's: How it all started <https://link.springer.com/article/10.1140/epjp/i2016-16090-x>*
- 6 N.S. Martorana 2023 *J. Phys.: Conf. Ser.* 2586 012149
- 7 P. Russotto 2024
- 8 W. Korten – AGATA – The Advanced Gamma Tracking Array - CPAN Days october 2019
- 9 W. Von Oertzen *Eur. Phys. J. A* 11, 403–411 (2001)
- 10 M. Kimura *Eur. Phys. J. A* (2016) 52: 373
- 11 Y. Blumenfeld *Physics* 15 177 2022

# Conclusions



Heavy and SuperHeavy nuclei



C.D. Friedrich

Unknown regions for Young researchers

Proton drip line

Valley of Stability

Neutron Drip line

Light nuclei





# The discovery of halo in nuclei

- $^{11}\text{Li}$
- Dimensions
- Weakly bound systems
- Diffuse surfaces
- New collective modes
- Strange shapes (not only spherical: pear, chain, bubble, coexistence)
- Exotic radioactivity e.g. proton decay!
- New magic numbers
- From 'normal' collective modes to exotic modes
- Pigmy
- Dynamical dipole

# Coulomb excitation: electric fields to gently excite nuclei

J.A. Brown 1991  
FIRST EXPERIMENT WITH a  
Radioactive beam (USA)  
8Li from n-pickup of 7Li on a  
thick Be target

8Li+Ni at 15MeV

Strong actual interest: perfect technique for ISOL  
laboratories

ISOL: low energy beams

ISOL: pure beam species (low contamination)

ISOL: suitable beam (even low) currents, CE has large cross sections

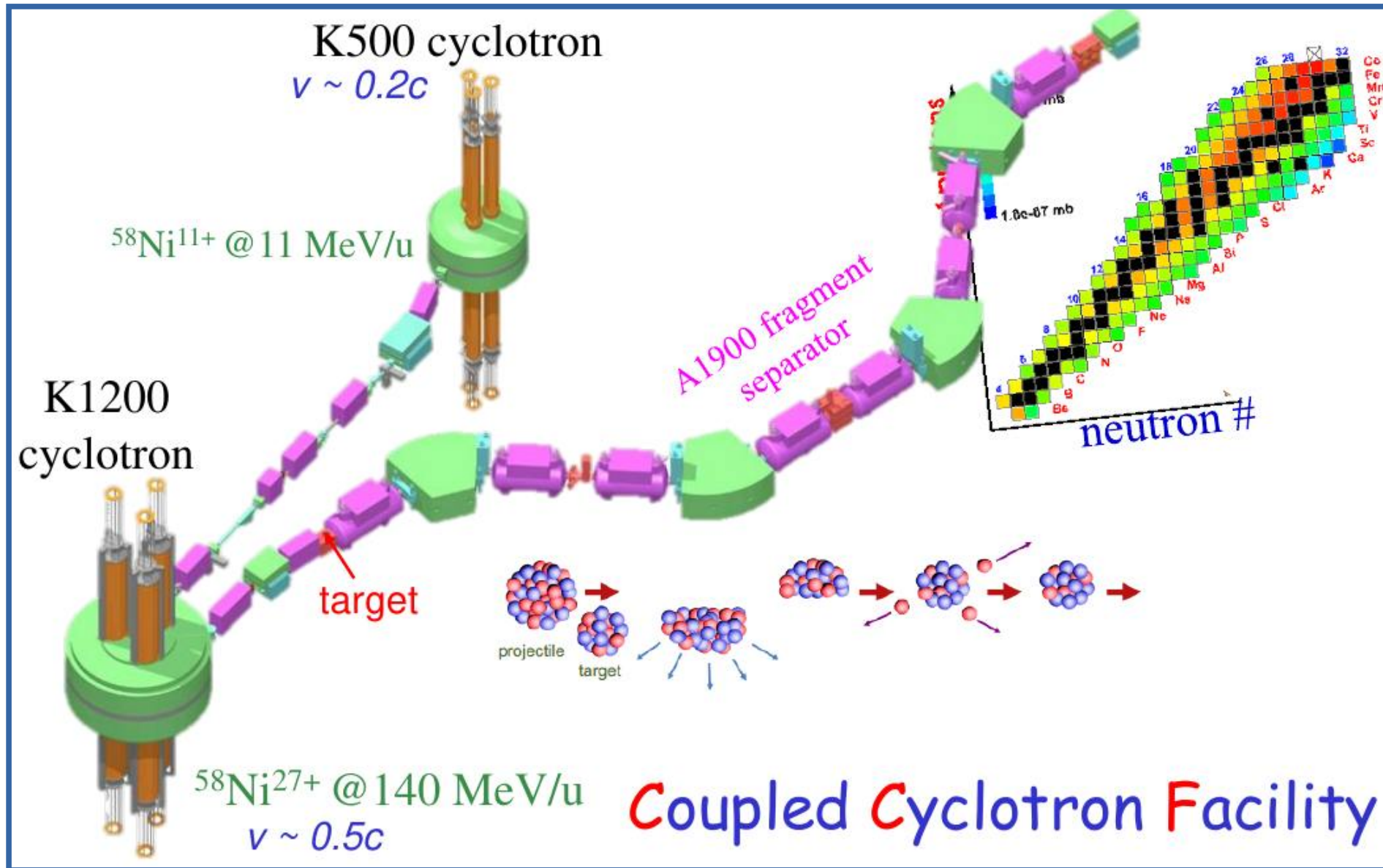
OPTIMUM experimental conditions to investigate more the nuclear structure far  
from the stability line (“climb the canyon cliff”)

OF COURSE:

The more you climb the more you suffer! (low statistics, large isotopic  
contaminations, less robust complementary information)

Collectivity in nuclei  
Shape coexistence

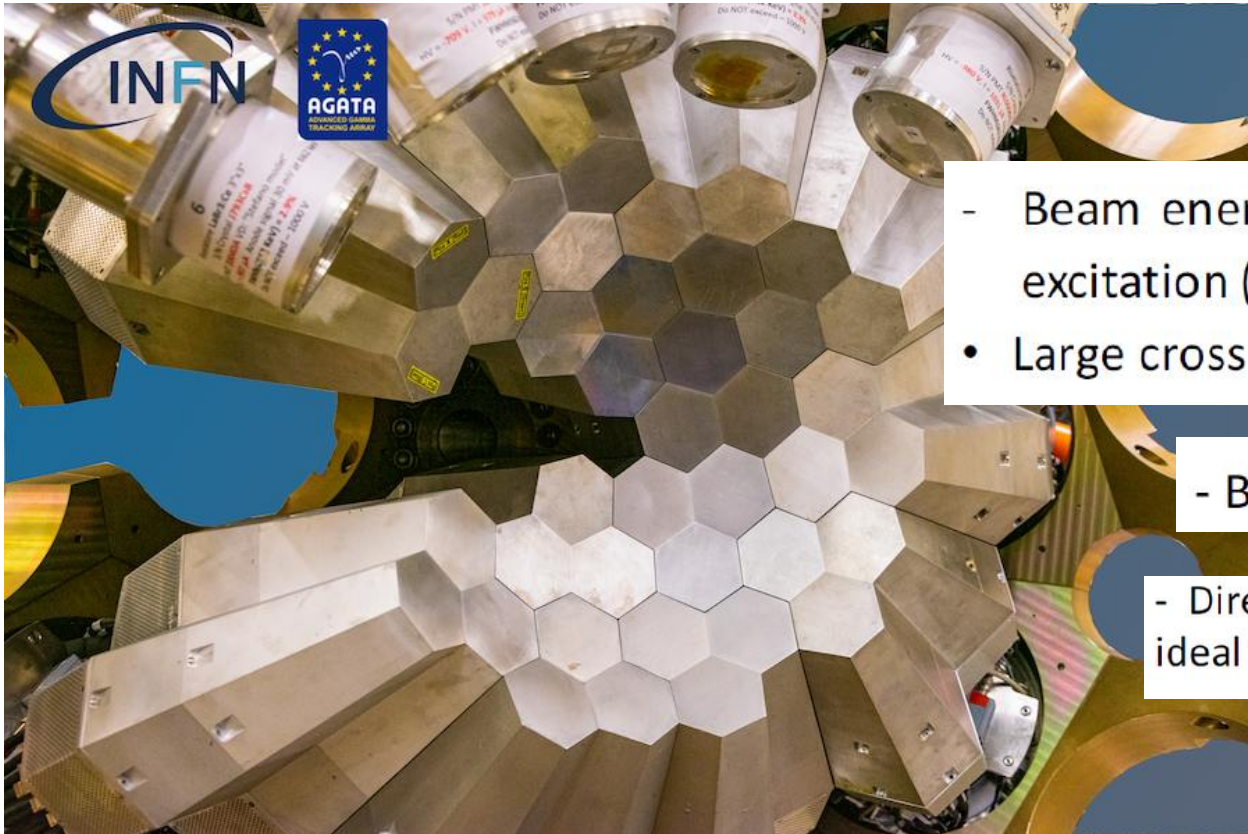
# Example of IF facility NSCL (USA)



Se serve vedi  
Btsang nella  
cartella talk  
nusym15  
DeAngelis  
vitainfn/csn3/2017  
Prete  
vitainfn/cns3/  
Ins2017



# Gamma side

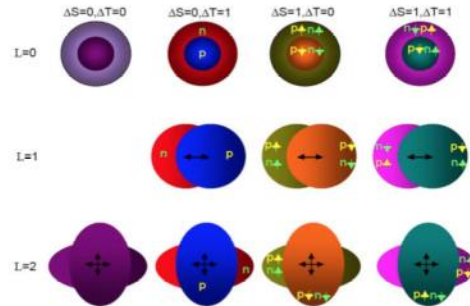


Coulomb excitation  
Vedi indico page feb 2025, Firenze

- Beam energies available at ISOL facilities perfect for Coulomb excitation (2-5 MeV/A)
- Large cross sections (excitation of  $2^+_1 \sim$  barns)
- B(E2) transition probabilities – measure of collectivity
- Direct measurement of quadrupole moment including sign – ideal tool to study shapes and shape coexistence

# GMR study: Physics Motivation

## Giant Resonances in Exotic Nuclei



**Constrain the Nuclear Matter Equation of State**

Investigation of the GMR

$$E_{GMR} = \hbar \sqrt{\frac{K_A}{m \langle r^2 \rangle}}$$

its energy is directly related to the compressibility of nuclear matter ( $K_\infty$ )

$$K_A = K_\infty + K_{surf} A^{-1/3} + K_\tau \delta^2 + K_{Coul} \frac{Z^2}{A^{4/3}}$$

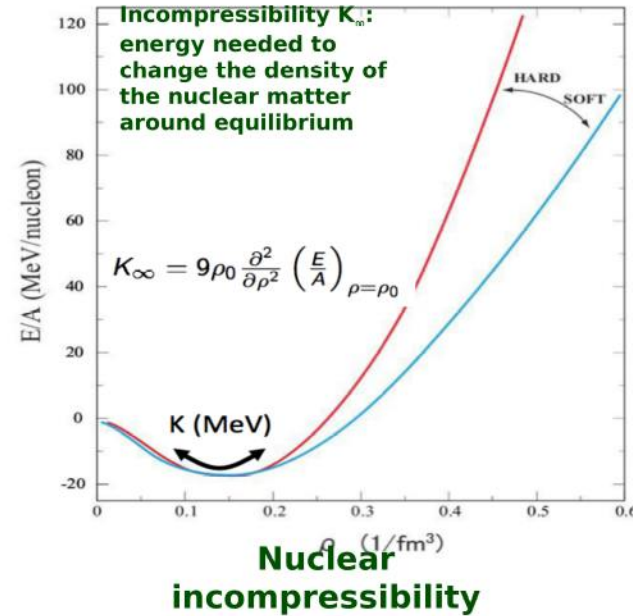
$K_\infty$  → Nucleus (mass A)  
 $K_\infty$  → Nuclear Matter

Isospin Dependence  
 $K_\tau = -500 \pm 100$  MeV  
 T. Li, UFGarg et al., Phys. Rev. C 81, 034309 (2010)

$K_\infty = 240 \pm 10$  MeV

J. Li, G. Colò and J. Meng, Phys. Rev. C 78, 061304 (2008)

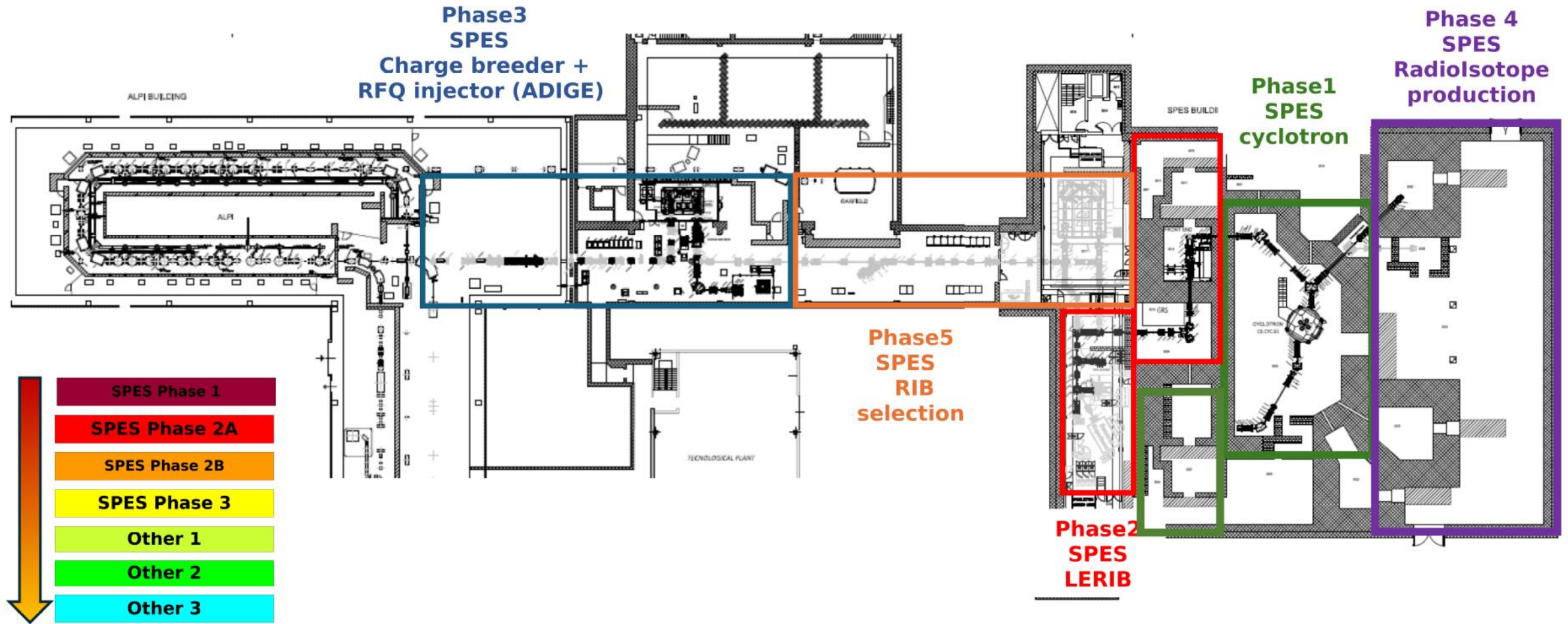
Part of this uncertainty is due to our poor knowledge of the Isospin dependence  $K_\tau$



**Nuclear incompressibility**



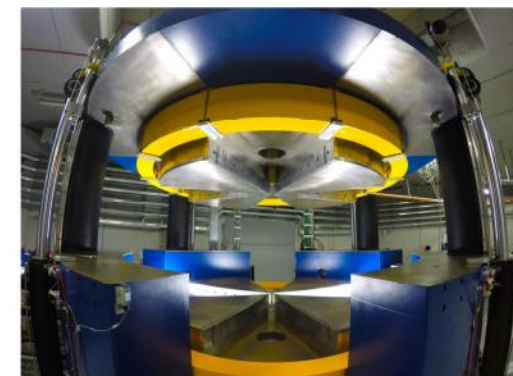
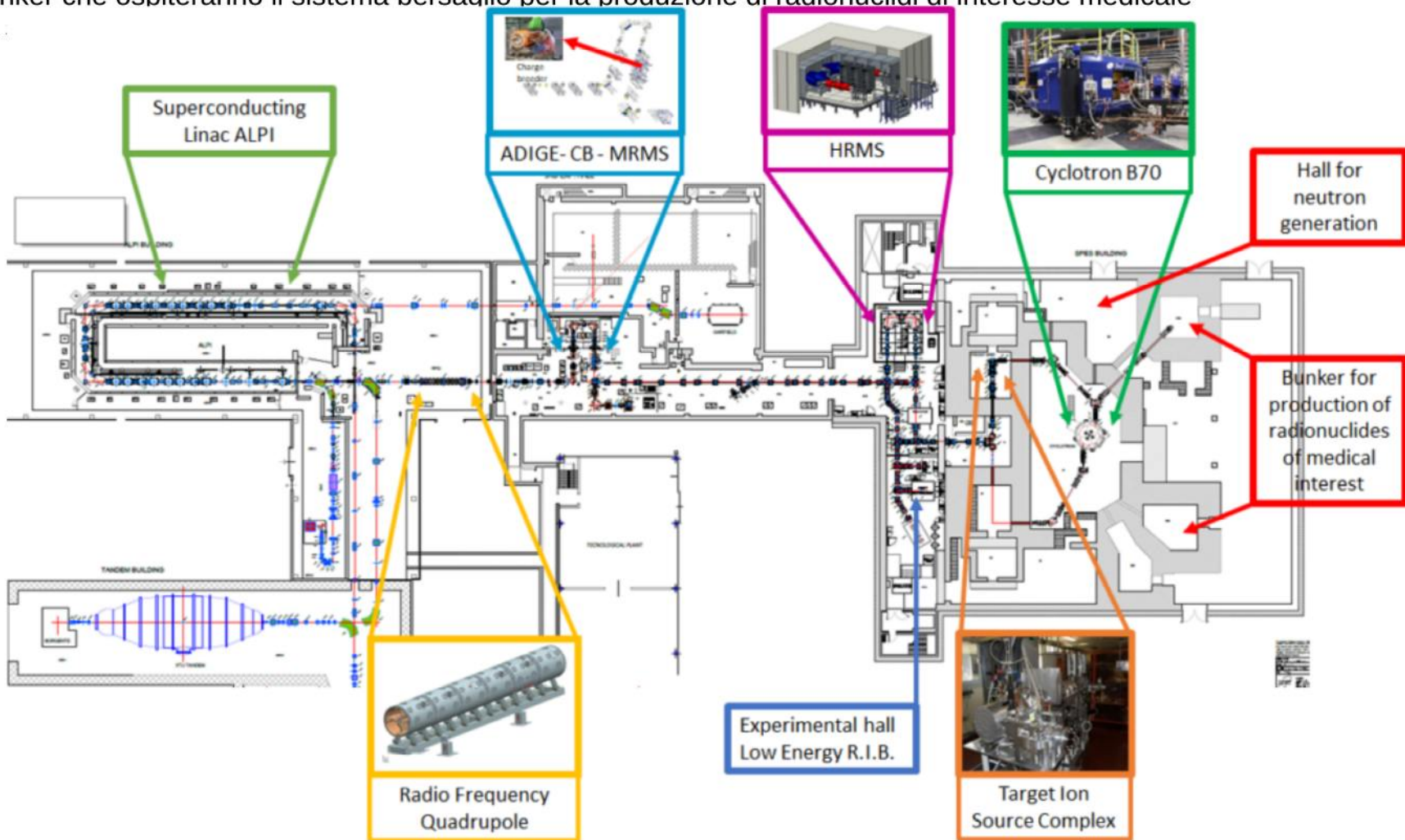
# SPES - Phased Approach





la sala sperimentale per gli esperimenti con fasci di ioni radioattivi non riaccelerati (Low Energy R.I.B.)  
 lo Spettrometro di massa ad Alta Risoluzione HRMS per la separazione di massa dei fasci di ioni radioattivi  
 il rivelatore ADIGE, che comprende lo Spettrometro di massa a Media Risoluzione MRMS e il Charge Breeder  
 per l'aumento dello stato di carica  
 i fasci di ioni radioattivi  
 l'RFQ (Radio Frequency Quadrupole) per la preaccelerazione dei fasci di ioni radioattivi  
 l'acceleratore lineare superconduttivo ALPI per l'accelerazione dei fasci di ioni radioattivi  
 i bunker che ospiteranno il sistema bersaglio per la produzione di radionuclidi di interesse medicale

# SPES, LNL



B70 cyclotron  
 150 tons  
 Proton beams up to 0.75mA  
 Energy 20-70 MeV  
 Max power 52kW

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# Coulomb excitation: still a stimulating method

J.Henderson and others PRL 2025

The strange case of lead ( $^{208}\text{Pb}$ ) which is the heaviest DM nucleus  
Confirmed shape deformation (prolate dominant) in double-magic nuclei  
No model reproduces this so strong behaviour  
Why unexpected? Because magic nuclei (and more double magic one) are particularly stable and supposed to be spherical

