

# STRONG COUPLING CONSTANTS OF HEAVY BARYONS WITH LIGHT MESONS IN QCD

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# Outline

- Introduction
- Interpolating Currents
- Sum Rules for Strong Coupling Constants of Heavy Baryons with Light Mesons
- Results & Conclusion

# Introduction

- $SU(3)$  classifications of heavy baryons

$$3 \times 3 = 6 + \bar{3}$$

- Ground states : 1 for  $6_F$  (two light

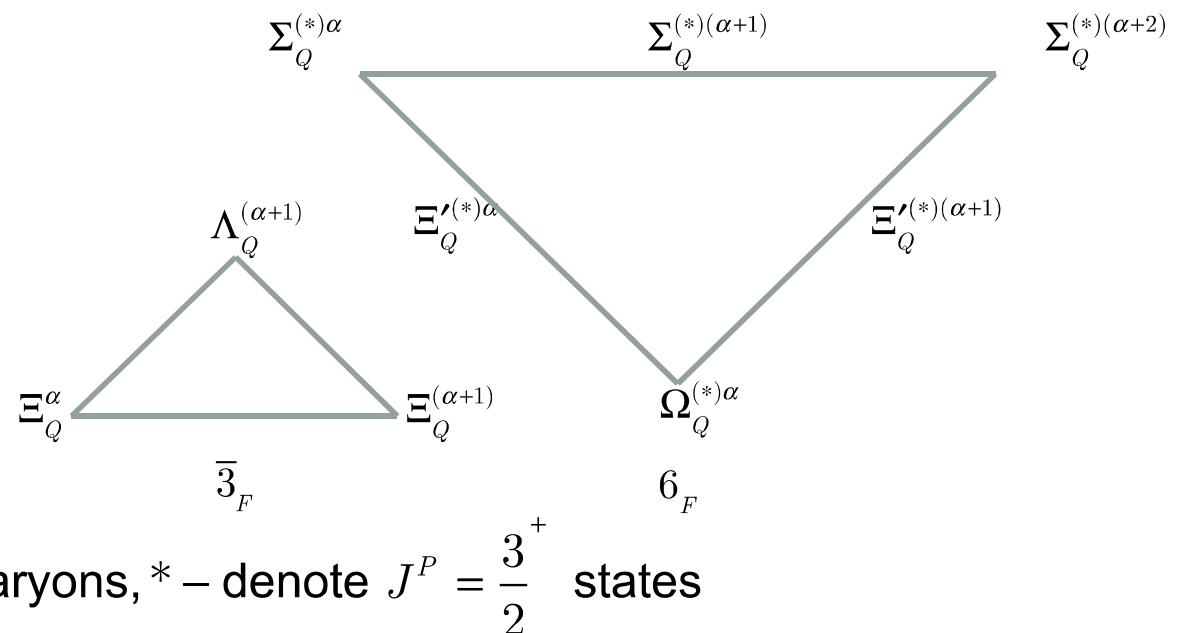
- Total spin 0 for  $\bar{3}_F$  quarks)

- $J^P = \frac{1}{2}^+$  or  $\frac{3}{2}^+ 6_F$

$$J^P = \frac{1}{2}^+ \quad \bar{3}_F$$

$\alpha, \alpha + 1, \alpha + 2$

$(\alpha = -1 \text{ or } 0)$  (Charges of baryons,  $*$  – denote  $J^P = \frac{3}{2}^+$  states



# Introduction

Exciting experimental results :

- $\frac{1}{2}^+$  and  $\frac{1}{2}^- \bar{3}_F$  states  $\Lambda_c^+, \Xi_c^+, \Xi_c^0$   
 $\Lambda_c^+(2593), \Xi_c^+(2790), \Xi_c^0(2790)$
- $\frac{1}{2}^+$  and  $\frac{3}{2}^+ 6_F$  states  $\Omega^{(*)}_c, \Sigma^{(*)}_c, \Xi^{(*)}_c$  are observed
- $\Lambda_b, \Sigma_b, \Sigma_b^*, \Xi_b^0$  and  $\Omega_b$  are observed.
- LHC B -  $\Lambda_b^*(5912), \Lambda_b^*(5920)$
- LHC (CMS)  $\Xi_b^{*0}(5945)$
- LHC - New window for Heavy Baryon Physics.

# Introduction

- A detailed theoretical study of experimental results and various weak & strong decays can provide us useful information about the quark structure of new hadrons at  $\Lambda_{had}$  ( $\rightarrow$  non-perturbative sector).
- Nonperturbative methods
- SUM RULES (STANDART OR LIGHT CONE VERSION)

# $B_Q B_Q M$ Coupling Constants in QCD

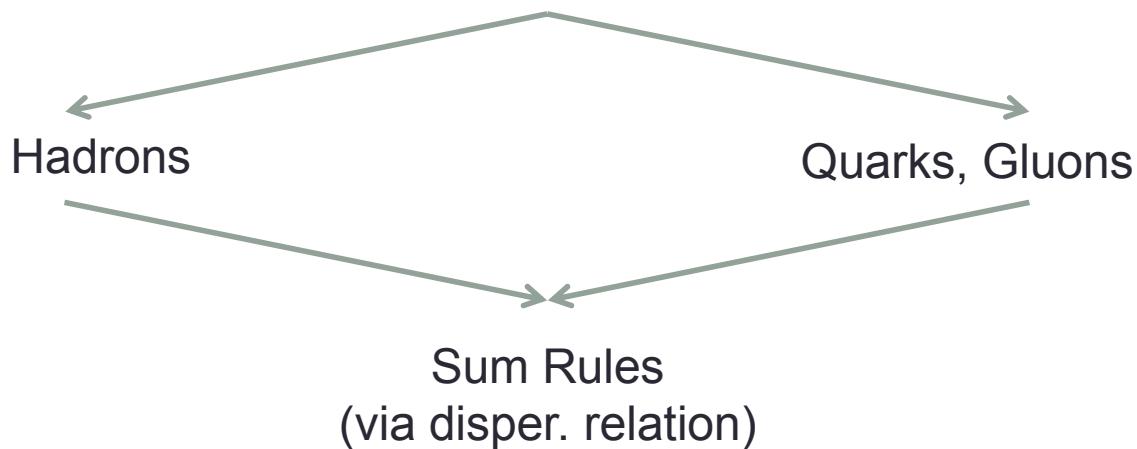
$$\Pi^{ij}_{(\mu),(\nu)} = i \int d^4x e^{ipx} \langle M(q) | \{ \eta^{(i)}_{(\mu)} \eta^{(j)}_{(\nu)} \} | 0 \rangle$$

$i = 1, j = 1$    6 - 6

$i = 1, j = 2$    6 -  $\bar{3}$

$i = 2, j = 2$    Antitriplet - antitriplet

- $\Pi$  – two different representations



# Interpolating Currents

$$\eta^{(s)} = -\frac{1}{\sqrt{2}} \epsilon^{abc} \left\{ (q_1^{aT} c Q^b) \gamma_5 q_2^c - (Q^{aT} c q_2^b) \gamma_5 q_1^c + \beta \left[ (q_1^{aT} c \gamma_5 Q^b) q_2^c - (Q^{aT} c \gamma_5 q_2^b) q_1^c \right] \right\}$$

$$\eta^{(a)} = \frac{1}{\sqrt{6}} \epsilon^{abc} \left\{ 2(q_1^{aT} C q_2^b) \gamma_5 Q^c + (q_1^{aT} C Q^b) \gamma_5 q_2^c + (Q^{aT} C q_2^b) \gamma_5 q_1^c + \beta \left[ 2(q_1^{aT} C \gamma_5 q_2^b) Q^c + (q_1^{aT} C \gamma_5 Q^b) q_2^c + (Q^{aT} C \gamma_5 q_2^b) q_1^c \right] \right\}$$

$\eta^{(s)}$  is symmetric  $q_1 \leftrightarrow q_2$

$\eta^{(a)}$  is antisymmetric  $q_1 \leftrightarrow q_2$

# Interpolating Currents

	$q_1$	$q_2$
$\Sigma_{b(c)}^{+(++)}$	$u$	$u$
$\Sigma_{b(c)}^{0(+)}$	$u$	$d$
$\Sigma_{b(c)}^{-(0)}$	$d$	$d$
$\Xi_{b(c)}^{\prime-(0)}$	$d$	$s$
$\Xi_{b(c)}^{\prime0(+)}$	$u$	$s$
$\Omega_{b(c)}^{-(0)}$	$s$	$s$
$\Lambda_{b(c)}^{0(+)}$	$u$	$d$
$\Xi_{b(c)}^{-(0)}$	$d$	$s$
$\Xi_{b(c)}^{0(+)}$	$u$	$s$

# Interpolating Currents

$$\eta_\mu = A \epsilon^{abc} \left\{ (q_1^{aT} C \gamma_\mu q_2^b) Q^c + (q_2^{aT} C \gamma_\mu Q^b) q_2^c + (Q^{aT} C \gamma_\mu q_1^b) q_2^c \right\}$$

	$q_1$	$q_2$	$A$
$\Sigma_{b(c)}^{*+(++)}$	$u$	$u$	$1/\sqrt{3}$
$\Sigma_{b(c)}^{*0(+)}$	$u$	$d$	$\sqrt{2}/\sqrt{3}$
$\Sigma_{b(c)}^{*-0(0)}$	$d$	$d$	$1/\sqrt{3}$
$\Xi_{b(c)}^{*0(+)}$	$u$	$s$	$\sqrt{2}/\sqrt{3}$
$\Xi_{b(c)}^{*-0(0)}$	$d$	$s$	$\sqrt{2}/\sqrt{3}$
$\Omega_{b(c)}^{*-0(0)}$	$s$	$s$	$1/\sqrt{3}$

# Relations Between Invariant Functions

SSP:

$$\Pi^{\Sigma_b^0 \rightarrow \Sigma_b^0 \pi^0} = g_{\pi uu} \Pi_1^{(1)}(u, d, b) + g_{\pi dd} \Pi_1'^{(1)}(u, d, b) + g_{\pi bb} \Pi_2^{(1)}(u, d, b)$$

$$J_{\pi^0} = \sum g_{\pi qq} \bar{q} \gamma_5 q$$

$$\Rightarrow g_{\pi uu} = -g_{\pi dd} = \frac{1}{\sqrt{2}}, \quad g_{\pi bb} = 0$$

$$\Pi_1'^{(1)}(u, d, b) = \Pi_1^{(1)}(d, u, b)$$

$$\Pi^{\Sigma_b^0 \rightarrow \Sigma_b^0 \pi^0} = \frac{1}{\sqrt{2}} \left[ \Pi_1^{(1)}(u, d, b) - \Pi_1^{(1)}(d, u, b) \right]$$

$$\text{In } SU(2) \text{ limit } \Pi^{\Sigma_b^0 \rightarrow \Sigma_b^0 \pi^0} = 0$$

# Relations Between Invariant Functions

- For  $\Sigma_b^+ \rightarrow \Sigma_b^+ \pi^0$  can be obtained from

$$\Sigma_b^0 \rightarrow \Sigma_b^0 \pi^0 : d \rightarrow u \text{ and } \Sigma_b^0 = -\sqrt{2} \Sigma_b^+$$

$$\downarrow 4 \Pi_1^{(1)}(u, d, b) = -2 \langle uu | \Sigma^+ \Sigma^+ | 0 \rangle$$

$\Sigma^+$  cont.  $2u \rightarrow 4$  ways for rad.  $\pi^0$  from  $u$

$$\Pi^{\Sigma_b^+ \rightarrow \Sigma_b^+ \pi^0} = \sqrt{2} \Pi_1^{(1)}(u, u, b)$$

- $\Xi_b'^{-(0)} \rightarrow \Xi_b'^{-(0)} \pi^0$

From  $\Sigma_b^0 \rightarrow \Sigma_b^0 \pi^0 : \Xi_b'^0 = \Sigma_b^0(d \rightarrow s), \Xi_b'^- = \Sigma_b^0(u \rightarrow s)$

$$\Pi^{\Xi_b'^0 \rightarrow \Xi_b'^0 \pi^0} = \frac{1}{\sqrt{2}} \Pi_1^{(1)}(u, s, b)$$

$$\Pi^{\Xi_b'^- \rightarrow \Xi_b'^- \pi^0} = -\frac{1}{\sqrt{2}} \Pi_1^{(1)}(d, s, b)$$

# Relations Between Invariant Functions

- For charged pion

$$\langle \bar{d}d | \Sigma_b^0 \bar{\Sigma}_b^0 | 0 \rangle$$

$d$  from  $\Sigma_b$ ,  $\bar{d}$  from  $\bar{\Sigma}_b^0$  form  $\bar{d}d$  final state  $u,b$ , spectators

$$\langle \bar{u}d | \Sigma_b^+ \bar{\Sigma}_b^0 | 0 \rangle \sim \langle dd | \Sigma_b^0 \bar{\Sigma}_b^0 | 0 \rangle$$

Calculations :

$$\begin{aligned} \Pi^{\Sigma_b^0 \rightarrow \Sigma_b^+ \pi^-} &= \langle \bar{u}d | \Sigma_b^+ \bar{\Sigma}_b^0 | 0 \rangle = -\sqrt{2} \langle \bar{d}d | \Sigma_b^0 \bar{\Sigma}_b^0 | 0 \rangle \\ &= -\sqrt{2} \Pi_1^{(1)}(d, u, b) \end{aligned}$$

$$u \leftrightarrow d$$

$$\Pi^{\Sigma_b^0 \rightarrow \Sigma_b^- \pi^+} = \sqrt{2} \langle u\bar{u} | \Sigma_b^0 \bar{\Sigma}_b^0 | 0 \rangle = \Pi_1^{(1)}(u, d, b)$$

## Relations Between Invariant Functions

Similar arguments holds for all  
SSP, SAP, AAP, SSV, SAV, AAV

transitions:

- Main results: All these transitions (with P, V) can be represented in terms of only one invariant function for each class.
- Relations among the invariant functions are structure independent, but their explicit forms are structure dependent.

# $B_Q B_Q M$ Coupling Constants in QCD

$$\Pi^{ij}_{(\mu),(\nu)} = \frac{\langle 0 | \eta^{(i)}_{(\mu)} | B_2(p) \rangle \langle B_2(p) M(q) | B_1(p+q) \rangle \langle B_1(p+q) | \bar{\eta}_\nu^j | 0 \rangle}{\left( p^2 - m_2^2 \right) \left[ (p+q)^2 - m_1^2 \right]}$$

+ ...

## Matrix Elements

$$\langle 0 | \eta^{(i)}_{(\mu)} | B_2(p) \rangle = \lambda^i u_{(\mu)}(p)$$

$$\langle B_1(p+q) | \bar{\eta}_\nu^j | 0 \rangle = \lambda^j \bar{u}(p+q)$$

$$\langle B_2(p) M(q) | B_1(p+q) \rangle =$$

# $B_Q B_Q M$ Coupling Constants in QCD

$$= g \bar{u}(p) i \gamma_5 u(p+q) \quad \text{spin } 1/2 \text{ spin } 1/2 P$$

$$\bar{u}(p) \left[ f_1 \gamma_\mu - i \frac{\sigma_{\mu\nu} q^\nu}{m_1 + m_2} f_2 \right] u(p+q) \varepsilon^\mu \text{1/2} \rightarrow \text{1/2} V$$

↓                    ↓  
charge              magnetic formfactors

$$g \bar{u}(p) u_\alpha(p+q) q^\alpha \text{ 3/2} \rightarrow \text{1/2} P$$

$$\begin{aligned} & \bar{u}(p) \{ g_1 (q_\alpha \not{q} - \varepsilon_\alpha \not{q}) \gamma_5 + g_2 ((p \varepsilon) q_\alpha - P q \varepsilon_\alpha) \gamma_5 + \\ & g_3 ((q \varepsilon) q_\alpha - q^2 \varepsilon_\alpha) \gamma_5 \} u_\alpha(p+q) \text{ 3/2} \rightarrow \text{1/2} V \end{aligned}$$

# $B_Q \bar{B}_Q M$ Coupling Constants in QCD

$$g\bar{u}_\alpha(p)i\gamma_5 u_\alpha(p+q) \quad 3/2 \rightarrow 3/2P$$

$$\begin{aligned} \bar{u}_\alpha(p) & \left\{ g^{\alpha\beta} \left[ \not{g}_1 + 2p\varepsilon \frac{g_2}{m_1 + m_2} \right] + \right. \\ & \left. \frac{q^\alpha q^\beta}{(m_1 + m_2)^2} \left[ \not{g}_3 + 2p\varepsilon \frac{g_4}{m_1 + m_2} \right] \right\} u^\beta(p+q) \end{aligned}$$

$$3/2 \rightarrow 3/2V$$

## $B_Q B_Q M$ Coupling Constants in QCD

Two problems (in participation of spin 3/2 baryons)

- The spin 1/2 states also contribute to the matrix element

$$\langle 0 | \eta_\mu | B(1/2) \rangle = A \left( \gamma_\mu - \frac{4}{m} p_\mu \right) u(p)$$

i.e.  $\eta_\mu$  – couples to both spin 3/2 and spin 1/2

- Not all structures are independent.

# $B_Q B_Q M$ Coupling Constants in QCD

Solution: Ordering Dirac Matrices!

- ln  $\frac{3}{2} \rightarrow \frac{1}{2} P$       Ordering  $q p \gamma_\mu$  ( $q q_\mu$  structure is chosen)
- $\frac{3}{2} \rightarrow \frac{1}{2} V$       Ordering  $\underline{\gamma_\mu \not{q} p \gamma_5}$ 
  - $\not{p} \gamma_5 q_\mu$  for  $g_1$
  - $\not{q} p (p \epsilon)$        $g_2$
  - $q^2 \not{q} p \epsilon_\mu \gamma_5$        $g_3$

# $B_Q B_Q M$ Coupling Constants in QCD

$$\frac{3}{2} \rightarrow \frac{3}{2} P \quad \gamma_\mu p q \gamma_\nu \gamma_5$$

$$g_{\mu\nu} p q \gamma_5$$

$$\frac{3}{2} \rightarrow \frac{3}{2} V \quad \gamma_\mu \not{q} \not{p} \gamma_\nu$$

$$g_{\mu\nu} q \not{e} p \quad g_1 + \frac{g_2 m_2}{m_1 + m_2}$$

$$q_\mu q_\nu \not{e} \not{q} \not{p} \quad \frac{g_2}{m_1 + m_2}$$

$$2 \not{e} p q_\mu q_\nu \not{q} \not{p} \quad \frac{g_3}{(m_1 + m_2)^2}$$

# Results

<u>SSP</u>	<u>Bottom Baryons</u>	<u>Charmed Baryons</u>
$g^{\Xi_Q^{10(+)} \rightarrow \Xi_Q^{10(+)} \pi^0}$	$9 \pm 3$	$4 \pm 1.4$
$g^{\Sigma_Q^{0(+)} \rightarrow \Sigma_Q^{-(0)} \pi^+}$	$17 \pm 6$	$8 \pm 2.8$
$g^{\Xi_Q^{10(+)} \rightarrow \Sigma_Q^{+(++)} K^-}$	$19 \pm 6.7$	$9 \pm 3.4$
$g^{\Omega_Q^{-(0)} \rightarrow \Xi_Q^{10(+)} K^-}$	$21 \pm 6.8$	$9 \pm 3.4$
<u>SAP</u>		
$g^{\Xi_Q^{10(+)} \rightarrow \Xi_Q^{10(+)} \pi^0}$	$7.5 \pm 2.6$	$3.1 \pm 1.1$
$g^{\Sigma_Q^{-(0)} \rightarrow \Lambda_Q^{0(+)} \pi^-}$	$15 \pm 4.9$	$6.5 \pm 2.4$
$g^{\Sigma_Q^{0(+)} \rightarrow \Xi_Q^{0(+)} \bar{K}^0}$	$11.5 \pm 3.9$	$5.0 \pm 1.7$
$g^{\Xi_Q^{10(+)} \rightarrow \Xi_Q^{-(+)} K^+}$	$12 \pm 4.3$	$4.5 \pm 1.6$
<u>AAP</u>		
$g^{\Xi_Q^{0(+)} \rightarrow \Xi_Q^{0(+)} \pi^0}$	$1 \pm 0.3$	$0.7 \pm 0.22$
$g^{\Xi_Q^{-(0)} \rightarrow \Lambda_Q^{0(+)} K^-}$	$1.5 \pm 0.5$	$0.9 \pm 0.3$
$g^{\Xi_Q^{0(+)} \rightarrow \Xi_Q^{0(+)} \eta_1}$	$0.6 \pm 0.2$	$0.07 \pm 0.02$
$g^{\Lambda_Q^{0(+)} \rightarrow \Lambda_Q^{0(+)} \eta_1}$	$1 \pm 0.3$	$0.75 \pm 0.24$

$f_1^{\text{channel}}$	Bottom Baryons		$f_1^{\text{channel}}$	Charmed Baryons	
	General current	Ioffe current		General current	Ioffe current
$f_1^{\Xi_b'^0 \rightarrow \Xi_b'^0 \rho^0}$	$2.2 \pm 0.7$	$2.0 \pm 0.7$	$f_1^{\Xi_c'^+ \rightarrow \Xi_c'^+ \rho^0}$	$2.5 \pm 0.8$	$5.0 \pm 1.7$
$f_1^{\Sigma_b^0 \rightarrow \Sigma_b^- \rho^+}$	$4.5 \pm 1.5$	$3.4 \pm 1.1$	$f_1^{\Sigma_c^+ \rightarrow \Sigma_c^0 \rho^+}$	$4.0 \pm 1.3$	$3.4 \pm 1.1$
$f_1^{\Xi_b'^0 \rightarrow \Sigma_b^+ K^{*-}}$	$6.0 \pm 2.0$	$3.9 \pm 1.3$	$f_1^{\Xi_c'^+ \rightarrow \Sigma_c^+ K^{*-}}$	$5.0 \pm 1.7$	$3.8 \pm 1.3$
$f_1^{\Omega_b^- \rightarrow \Xi_b'^0 \bar{K}^{*-}}$	$6.0 \pm 2.0$	$4.8 \pm 1.6$	$f_1^{\Omega_c^0 \rightarrow \Xi_c^+ \bar{K}^{*-}}$	$7.0 \pm 2.0$	$14.0 \pm 5.0$
$f_1^{\Sigma_b^+ \rightarrow \Sigma_b^+ \omega}$	$4.0 \pm 1.3$	$3.0 \pm 1.0$	$f_1^{\Sigma_c^{++} \rightarrow \Sigma_c^+ \omega}$	$3.5 \pm 1.2$	$3.0 \pm 1.0$
$f_1^{\Xi_b'^0 \rightarrow \Xi_b'^0 \omega}$	$2.1 \pm 0.7$	$1.7 \pm 0.6$	$f_1^{\Xi_c'^+ \rightarrow \Xi_c'^+ \omega}$	$2.4 \pm 0.8$	$4.9 \pm 1.6$
$f_1^{\Xi_b'^0 \rightarrow \Xi_b'^0 \phi}$	$5.0 \pm 1.7$	$2.6 \pm 0.9$	$f_1^{\Xi_c'^+ \rightarrow \Xi_c'^+ \phi}$	$4.0 \pm 1.3$	$2.5 \pm 0.8$
$f_1^{\Omega_b^- \rightarrow \Omega_b^- \phi}$	$10.0 \pm 3.4$	$7.0 \pm 2.4$	$f_1^{\Omega_c^0 \rightarrow \Omega_c^0 \phi}$	$11.0 \pm 4.0$	$23.0 \pm 8.0$

The values of the strong coupling constants  $f_1$  for the transitions among the sextet–sextet heavy baryons with vector mesons.

$f_1^{\text{channel}}$	Bottom Baryons		$f_1^{\text{channel}}$	Charmed Baryons	
	General current	Ioffe current		General current	Ioffe current
$f_1^{\Xi_b'^0 \rightarrow \Xi_b^0 \rho^0}$	$1.4 \pm 0.5$	$0.6 \pm 0.2$	$f_1^{\Xi_c'^+ \rightarrow \Xi_c^+ \rho^0}$	$1.5 \pm 0.5$	$0.7 \pm 0.2$
$f_1^{\Xi_b'^0 \rightarrow \Xi_b^- K^{*+}}$	$2.5 \pm 0.8$	$1.3 \pm 0.4$	$f_1^{\Xi_c'^+ \rightarrow \Xi_c^0 K^{*+}}$	$2.3 \pm 0.8$	$1.2 \pm 0.4$
$f_1^{\Sigma_b^- \rightarrow \Lambda_b^0 \rho^-}$	$2.8 \pm 0.9$	$0.8 \pm 0.3$	$f_1^{\Sigma_c^0 \rightarrow \Lambda_c^+ \rho^-}$	$2.6 \pm 0.9$	$0.6 \pm 0.2$
$f_1^{\Sigma_b^0 \rightarrow \Xi_b^0 \bar{K}^{*0}}$	$2.6 \pm 0.8$	$1.5 \pm 0.5$	$f_1^{\Sigma_c^+ \rightarrow \Xi_c^+ \bar{K}^{*0}}$	$2.2 \pm 0.7$	$0.8 \pm 0.3$
$f_1^{\Omega_b^- \rightarrow \Xi_b^- \bar{K}^{*0}}$	$3.5 \pm 1.2$	$2.0 \pm 0.6$	$f_1^{\Omega_c^0 \rightarrow \Xi_c^0 \bar{K}^{*0}}$	$3.3 \pm 1.1$	$1.7 \pm 0.6$
$f_1^{\Xi_b'^0 \rightarrow \Xi_b^- \omega}$	$1.3 \pm 0.4$	$0.5 \pm 0.2$	$f_1^{\Xi_c'^+ \rightarrow \Xi_c^0 \omega}$	$1.2 \pm 0.4$	$1.1 \pm 0.4$
$f_1^{\Xi_b'^0 \rightarrow \Xi_b^0 \phi}$	$2.6 \pm 0.9$	$2.0 \pm 0.7$	$f_1^{\Xi_c'^+ \rightarrow \Xi_c^+ \phi}$	$2.1 \pm 0.7$	$1.4 \pm 0.5$

The values of the strong coupling constants  $f_1$  for the transitions among the sextet-antitriplet heavy baryons with vector mesons.

$f_1^{\text{channel}}$	Bottom Baryons		$f_1^{\text{channel}}$	Charmed Baryons	
	General current	Ioffe current		General current	Ioffe current
$f_1^{\Xi_b^0 \rightarrow \Xi_b^0 \rho^0}$	$3.1 \pm 1.1$	$2.5 \pm 0.8$	$f_1^{\Xi_c^+ \rightarrow \Xi_c^+ \rho^0}$	$6.0 \pm 2.0$	$1.5 \pm 0.5$
$f_1^{\Xi_b^- \rightarrow \Lambda_b^0 K^{*-}}$	$5.0 \pm 1.7$	$4.6 \pm 1.5$	$f_1^{\Xi_c^0 \rightarrow \Lambda_c^+ K^{*-}}$	$4.6 \pm 1.5$	$4.1 \pm 1.4$
$f_1^{\Xi_b^0 \rightarrow \Xi_b^0 \omega}$	$2.8 \pm 0.9$	$2.3 \pm 0.8$	$f_1^{\Xi_c^+ \rightarrow \Xi_c^+ \omega}$	$5.5 \pm 1.8$	$1.2 \pm 0.4$
$f_1^{\Lambda_b^0 \rightarrow \Lambda_b^0 \omega}$	$5.2 \pm 1.7$	$4.6 \pm 1.5$	$f_1^{\Lambda_c^+ \rightarrow \Lambda_c^+ \omega}$	$4.9 \pm 1.6$	$4.3 \pm 1.4$
$f_1^{\Lambda_b^0 \rightarrow \Lambda_b^0 \phi}$	$5.0 \pm 1.7$	$4.7 \pm 1.6$	$f_1^{\Lambda_c^+ \rightarrow \Lambda_c^+ \phi}$	$4.6 \pm 1.5$	$4.1 \pm 1.4$

The values of the strong coupling constants  $f_1$  for the transitions among the ant triplet-antitriplet heavy baryons with vector mesons.

$f_2^{\text{channel}}$	Bottom Baryons		$f_2^{\text{channel}}$	Charmed Baryons	
	General current	Ioffe current		General current	Ioffe current
$f_2^{\Xi_b'^0 \rightarrow \Xi_b'^0 \rho^0}$	$30.0 \pm 10.0$	$39.0 \pm 13.0$	$f_2^{\Xi_c'^+ \rightarrow \Xi_c'^+ \rho^0}$	$16.0 \pm 5.2$	$18.0 \pm 6.0$
$f_2^{\Sigma_b^0 \rightarrow \Sigma_b^- \rho^+}$	$55.0 \pm 18.0$	$72.0 \pm 24.0$	$f_2^{\Sigma_c^+ \rightarrow \Sigma_c^0 \rho^+}$	$27.0 \pm 9.0$	$33.0 \pm 11.0$
$f_2^{\Xi_b'^0 \rightarrow \Sigma_b^+ K^{*-}}$	$60.0 \pm 20.0$	$80.0 \pm 27.0$	$f_2^{\Xi_c'^+ \rightarrow \Sigma_c^+ K^{*-}}$	$30.0 \pm 10.0$	$36.0 \pm 12.0$
$f_2^{\Omega_b^- \rightarrow \Xi_b'^0 \bar{K}^{*-}}$	$70.0 \pm 23.0$	$88.0 \pm 29.0$	$f_2^{\Omega_c^0 \rightarrow \Xi_c^+ \bar{K}^{*-}}$	$35.0 \pm 12.0$	$41.0 \pm 14.0$
$f_2^{\Sigma_b^+ \rightarrow \Sigma_b^+ \omega}$	$50.0 \pm 17.0$	$64.0 \pm 21.0$	$f_2^{\Sigma_c^{++} \rightarrow \Sigma_c^{++} \omega}$	$24.0 \pm 8.0$	$29.0 \pm 9.5$
$f_2^{\Xi_b'^0 \rightarrow \Xi_b'^0 \omega}$	$27.0 \pm 9.0$	$34.0 \pm 11.0$	$f_2^{\Xi_c'^+ \rightarrow \Xi_c'^+ \omega}$	$15.0 \pm 5.0$	$16.0 \pm 6.3$
$f_2^{\Xi_b'^0 \rightarrow \Xi_b'^0 \phi}$	$45.0 \pm 15.0$	$57.0 \pm 19.0$	$f_2^{\Xi_c'^+ \rightarrow \Xi_c'^+ \phi}$	$21.0 \pm 7.0$	$26.0 \pm 8.6$
$f_2^{\Omega_b^- \rightarrow \Omega_b^- \phi}$	$95.0 \pm 32.0$	$125.0 \pm 42.0$	$f_2^{\Omega_c^0 \rightarrow \Omega_c^0 \phi}$	$52.0 \pm 17.0$	$60.0 \pm 20.0$

The values of the strong coupling constants of  $f_2$  for the transitions among the sextet-sextet heavy baryons with vector mesons

$g$ channel	Bottom Baryons		$g$ channel	Charmed Baryons	
	General current	Ioffe current		General current	Ioffe current
$g^{\Xi_b^{*0} \rightarrow \Xi_b' \pi^0}$	$2.0 \pm 0.4$	$1.6 \pm 0.4$	$g^{\Xi_c^{*+} \rightarrow \Xi_c' \pi^0}$	$2.1 \pm 0.3$	$2.3 \pm 0.4$
$g^{\Sigma_b^{*0} \rightarrow \Sigma_b^- \pi^+}$	$3.7 \pm 0.6$	$3.5 \pm 0.5$	$g^{\Sigma_c^{*+} \rightarrow \Sigma_c^0 \pi^+}$	$4.2 \pm 0.5$	$4.3 \pm 0.4$
$g^{\Xi_b^{*0} \rightarrow \Sigma_b^+ K^-}$	$4.8 \pm 1.0$	$2.6 \pm 0.5$	$g^{\Xi_c^{*+} \rightarrow \Sigma_c^+ K^-}$	$4.5 \pm 0.5$	$3.9 \pm 0.4$
$g^{\Omega_b^{*-} \rightarrow \Xi_b' K^-}$	$5.0 \pm 1.4$	$2.5 \pm 0.4$	$g^{\Omega_c^{*0} \rightarrow \Xi_c' K^-}$	$4.3 \pm 0.5$	$4.5 \pm 0.4$
$g^{\Sigma_b^{*+} \rightarrow \Sigma_b^+ \eta_1}$	$2.9 \pm 0.7$	$2.0 \pm 0.4$	$g^{\Sigma_c^{*++} \rightarrow \Sigma_c^{++} \eta_1}$	$2.9 \pm 0.4$	$2.7 \pm 0.4$
$g^{\Xi_b^{*0} \rightarrow \Xi_b' \eta_1}$	$1.3 \pm 0.3$	$0.9 \pm 0.3$	$g^{\Xi_c^{*+} \rightarrow \Xi_c' \eta_1}$	$1.5 \pm 0.3$	$1.0 \pm 0.2$
$g^{\Omega_b^{*-} \rightarrow \Omega_b^- \eta_1}$	$5.8 \pm 1.6$	$3.6 \pm 0.6$	$g^{\Omega_c^{*0} \rightarrow \Omega_c^0 \eta_1}$	$5.9 \pm 0.8$	$5.8 \pm 0.4$

Values of the strong coupling constants  $g$  in  $\text{GeV}^{-1}$  for the transitions among the sextet spin -3/2 and sextet spin -1/2 heavy baryons with pseudoscalar mesons

$g$ channel	Bottom Baryons		$g$ channel	Charmed Baryons	
	General current	Ioffe current		General current	Ioffe current
$g^{\Xi_b^{*0} \rightarrow \Xi_b^0 \pi^0}$	$3.0 \pm 0.6$	$1.4 \pm 0.3$	$g^{\Xi_c^{*+} \rightarrow \Xi_c^+ \pi^0}$	$3.5 \pm 0.5$	$2.0 \pm 0.3$
$g^{\Sigma_b^{*-} \rightarrow \Lambda_b^0 \pi^-}$	$6.0 \pm 1.1$	$2.5 \pm 0.5$	$g^{\Sigma_c^{*0} \rightarrow \Lambda_c^+ \pi^-}$	$7.8 \pm 1.0$	$3.9 \pm 0.6$
$g^{\Sigma_b^{*0} \rightarrow \Xi_b^0 \bar{K}^0}$	$3.7 \pm 0.5$	$2.0 \pm 0.5$	$g^{\Sigma_c^{*+} \rightarrow \Xi_c^+ \bar{K}^0}$	$5.0 \pm 1.0$	$3.1 \pm 0.4$
$g^{\Omega_b^{*-} \rightarrow \Xi_b^- \bar{K}^0}$	$5.0 \pm 0.8$	$2.6 \pm 0.4$	$g^{\Omega_c^{*0} \rightarrow \Xi_c^0 \bar{K}^0}$	$6.2 \pm 1.5$	$4.1 \pm 0.5$
$g^{\Xi_b^{*0} \rightarrow \Xi_b^- K^+}$	$3.6 \pm 0.5$	$1.9 \pm 0.6$	$g^{\Xi_c^{*+} \rightarrow \Xi_c^0 K^+}$	$4.4 \pm 0.8$	$3.0 \pm 0.4$
$g^{\Xi_b^{*0} \rightarrow \Xi_b^0 \eta_1}$	$5.4 \pm 1.0$	$2.5 \pm 0.4$	$g^{\Xi_c^{*+} \rightarrow \Xi_c^+ \eta_1}$	$6.9 \pm 1.5$	$4.0 \pm 0.5$

Values of the strong coupling constants  $g$  in  $\text{GeV}^{-1}$  for the transitions among the sextet spin -3/2 and anti-triplet -1/2 heavy baryons with pseudoscalar mesons

	Our work	CQM	LFQM	RQM	NRQM	Experiment
$\Gamma(\Sigma_c^{*++} \rightarrow \Lambda_c^+ \pi^+)$	$14.6 \pm 3.8$	20	12.84	$21.90 \pm 0.87$	$17.52 \pm 0.74$	$14.9 \pm 1.9$
$\Gamma(\Sigma_c^{*+} \rightarrow \Lambda_c^+ \pi^0)$	$14.6 \pm 3.8$	20	—	—	—	$< 17$
$\Gamma(\Sigma_c^{*0} \rightarrow \Lambda_c^0 \pi^0)$	$14.6 \pm 3.8$	20	12.40	$21.20 \pm 0.81$	$16.90 \pm 0.71$	$16.1 \pm 2.1$
$\Gamma(\Xi_c^{*+} \rightarrow \Xi_c^0 \pi^+)$	$2.8 \pm 0.9$	—	1.12	$1.78 \pm 0.33$	—	$< 3.1$
$\Gamma(\Xi_c^{*+} \rightarrow \Xi_c^+ \pi^0)$	$1.4 \pm 0.4$	—	0.69	$1.26 \pm 0.17$	—	$< 3.1$
$\Gamma(\Xi_c^{*0} \rightarrow \Xi_c^+ \pi^-)$	$2.8 \pm 0.9$	—	1.16	$2.11 \pm 0.29$	—	$< 5.5$
$\Gamma(\Xi_c^{*0} \rightarrow \Xi_c^0 \pi^0)$	$1.4 \pm 0.4$	—	0.72	$1.01 \pm 0.15$	—	$< 5.5$

Strong one-pion decay rates. Here the short keys stands for : (CQM) Constituent Quark Model, (LFQM) Light-Front Quark Model, (RQM) Relativistic Quark Model, (NRQM) Non-Relativistic Quark Model. The results are presented in units of MeV.

transition	$g_1$	$g_1^{Ioffe}$	$g_2$	$g_2^{Ioffe}$	$g_3$	$g_3^{Ioffe}$	NRQM
$\Sigma_b^{*0} \rightarrow \Sigma_b^- \rho^+$	$4.2 \pm 1.0$	$4.6 \pm 1.2$	$0.7 \pm 0.2$	$0.7 \pm 0.2$	$84 \pm 20$	$90 \pm 23$	$(2/3)c$
$\Sigma_b^{*+} \rightarrow \Sigma_b^+ \omega$	$3.8 \pm 1.1$	$4.2 \pm 1.1$	$0.6 \pm 0.2$	$0.7 \pm 0.2$	$70 \pm 20$	$74 \pm 21$	$(2/3)c$
$\Sigma_b^{*-} \rightarrow \Lambda_b \rho^-$	$8.0 \pm 2.1$	$8.4 \pm 1.4$	$0.7 \pm 0.2$	$0.8 \pm 0.2$	$148 \pm 38$	$154 \pm 26$	$(2/\sqrt{3})c$
$\Sigma_b^{*+} \rightarrow \Xi_b'^0 K^{*+}$	$4.6 \pm 1.4$	$5.2 \pm 1.3$	$0.9 \pm 0.3$	$1.2 \pm 0.4$	$64 \pm 18$	$70 \pm 18$	$(2/3)c$
$\Sigma_b^{*0} \rightarrow \Xi_b^0 K^{*0}$	$6.4 \pm 1.7$	$6.8 \pm 1.2$	$0.9 \pm 0.2$	$1.1 \pm 0.2$	$87 \pm 20$	$88 \pm 15$	$(\sqrt{2/3})c$
$\Xi_b^{*0} \rightarrow \Xi_b'^0 \rho^0$	$2.4 \pm 0.7$	$2.7 \pm 0.7$	$0.4 \pm 0.1$	$0.4 \pm 0.1$	$48 \pm 10$	$52 \pm 14$	$(1/3)c$
$\Xi_b^{*0} \rightarrow \Xi_b'^0 \omega$	$2.4 \pm 0.5$	$2.4 \pm 0.6$	$0.4 \pm 0.1$	$0.3 \pm 0.1$	$40 \pm 10$	$42 \pm 12$	$(1/3)c$
$\Xi_b^{*0} \rightarrow \Xi_b'^0 \phi$	$3.2 \pm 1.0$	$3.6 \pm 1.0$	$0.3 \pm 0.1$	$0.4 \pm 0.1$	$35 \pm 11$	$39 \pm 12$	$(\sqrt{2}/3)c$
$\Xi_b^{*0} \rightarrow \Sigma_b^+ K^{*-}$	$4.7 \pm 1.4$	$4.9 \pm 1.4$	$1.0 \pm 0.3$	$1.2 \pm 0.4$	$64 \pm 16$	$66 \pm 16$	$(2/3)c$
$\Xi_b^{*0} \rightarrow \Omega_b^- K^{*+}$	$5.3 \pm 1.6$	$5.9 \pm 1.7$	$1.0 \pm 0.2$	$1.3 \pm 0.3$	$74 \pm 21$	$83 \pm 20$	$(2/3)c$
$\Xi_b^{*0} \rightarrow \Xi_b^0 \rho^0$	$4.3 \pm 1.1$	$4.4 \pm 0.8$	$0.4 \pm 0.1$	$0.4 \pm 0.1$	$82 \pm 20$	$84 \pm 16$	$(1/\sqrt{3})c$
$\Xi_b^{*0} \rightarrow \Xi_b^0 \omega$	$4.3 \pm 1.1$	$4.4 \pm 0.8$	$0.4 \pm 0.1$	$0.4 \pm 0.1$	$82 \pm 20$	$84 \pm 16$	$(1/\sqrt{3})c$
$\Xi_b^{*0} \rightarrow \Xi_b^0 \phi$	$5.9 \pm 1.6$	$6.4 \pm 1.1$	$0.7 \pm 0.2$	$0.7 \pm 0.2$	$65 \pm 17$	$69 \pm 12$	$(\sqrt{2}/3)c$
$\Xi_b^{*0} \rightarrow \Lambda_b \bar{K}^{*0}$	$6.3 \pm 1.7$	$6.6 \pm 1.0$	$0.5 \pm 0.1$	$0.6 \pm 0.2$	$86 \pm 20$	$88 \pm 15$	$(\sqrt{2}/3)c$
$\Omega_b^{*-} \rightarrow \Omega_b^- \phi$	$7.2 \pm 1.8$	$8.2 \pm 2.2$	$1.0 \pm 0.2$	$1.2 \pm 0.3$	$85 \pm 15$	$90 \pm 25$	$(2\sqrt{2}/3)c$
$\Omega_b^{*-} \rightarrow \Xi_b'^0 K^{*-}$	$5.3 \pm 1.5$	$5.8 \pm 1.6$	$1.0 \pm 0.3$	$1.2 \pm 0.4$	$74 \pm 18$	$77 \pm 15$	$(2/3)c$
$\Omega_b^{*-} \rightarrow \Xi_b^- \bar{K}^{*0}$	$9.7 \pm 2.5$	$10.0 \pm 2.0$	$1.3 \pm 0.3$	$1.5 \pm 0.3$	$136 \pm 31$	$133 \pm 25$	$(2/\sqrt{3})c$

The absolute values of the coupling constants  $g_{1,2,3}$  for transitions of b-baryons.  
The couplings,  $g_1$ ,  $g_2$ , and  $g_3$  are in  $\text{GeV}^{-1}$ ,  $\text{GeV}^{-2}$  and  $\text{GeV}^{-2}$  respectively.

	Bottom Baryons		Charmed Baryons
$g^{\Xi_b^{*0} \rightarrow \Xi_b^{*0} \pi^0}$	$41 \pm 9$ ( $4.0 \pm 0.5$ )	$g^{\Xi_c^{*+} \rightarrow \Xi_c^{*+} \pi^0}$	$22 \pm 6$ ( $5.3 \pm 0.6$ )
$g^{\Sigma_b^{*0} \rightarrow \Sigma_b^{*-} \pi^+}$	$75 \pm 15$ ( $8.0 \pm 0.7$ )	$g^{\Sigma_c^{*+} \rightarrow \Sigma_c^{*0} \pi^+}$	$42 \pm 10$ ( $11.0 \pm 0.7$ )
$g^{\Xi_b^{*0} \rightarrow \Sigma_b^{*+} K^-}$	$65 \pm 14$ ( $7.8 \pm 0.8$ )	$g^{\Xi_c^{*+} \rightarrow \Sigma_c^{*++} K^-}$	$37 \pm 8$ ( $10.2 \pm 0.6$ )
$g^{\Omega_b^{*-} \rightarrow \Xi_b^{*0} K^-}$	$73 \pm 16$ ( $8.0 \pm 0.8$ )	$g^{\Omega_c^{*0} \rightarrow \Xi_c^{*+} K^-}$	$37 \pm 9$ ( $9.8 \pm 0.8$ )
$g^{\Sigma_b^{*+} \rightarrow \Sigma_b^{*+} \eta_8}$	$45 \pm 10$ ( $5.8 \pm 0.6$ )	$g^{\Sigma_c^{*++} \rightarrow \Sigma_c^{*++} \eta_8}$	$25 \pm 6$ ( $7.8 \pm 0.6$ )
$g^{\Xi_b^{*0} \rightarrow \Xi_b^{*0} \eta_8}$	$19 \pm 4$ ( $2.7 \pm 0.3$ )	$g^{\Xi_c^{*+} \rightarrow \Xi_c^{*+} \eta_8}$	$11.5 \pm 1.8$ ( $3.2 \pm 0.4$ )
$g^{\Omega_b^{*-} \rightarrow \Omega_b^{*-} \eta_8}$	$95 \pm 22$ ( $11.5 \pm 1.8$ )	$g^{\Omega_c^{*0} \rightarrow \Omega_c^{*0} \eta_8}$	$52 \pm 10$ ( $13.6 \pm 0.7$ )

The values of the strong coupling constants for the transitions among the heavy spin -3/2 baryons with pseudoscalar mesons.

transition	$g_1$	$g_2$	$g_3$	$g_4$
$\Xi_b^{*0} \rightarrow \Xi_b^{*0} \rho^0$	$9 \pm 1$	$19 \pm 2$	$50 \pm 5$	$15 \pm 2$
$\Sigma_b^{*0} \rightarrow \Sigma_b^{*-} \rho^+$	$18 \pm 2$	$36 \pm 4$	$100 \pm 20$	$27 \pm 3$
$\Xi_b^{*0} \rightarrow \Sigma_b^{*+} K^{*-}$	$30 \pm 5$	$40 \pm 4$	$110 \pm 15$	$28 \pm 3$
$\Omega_b^{*-} \rightarrow \Xi_b^{*0} K^{*-}$	$30 \pm 5$	$41 \pm 4$	$110 \pm 20$	$28 \pm 3$
$\Sigma_b^{*+} \rightarrow \Xi_b^{*0} K^{*+}$	$30 \pm 5$	$40 \pm 4$	$100 \pm 20$	$28 \pm 3$
$\Xi_b^{*0} \rightarrow \Omega_b^{*-} K^{*+}$	$35 \pm 5$	$42 \pm 5$	$100 \pm 20$	$28 \pm 3$
$\Sigma_b^{*+} \rightarrow \Sigma_b^{*+} \omega$	$16 \pm 2$	$32 \pm 3$	$90 \pm 10$	$24 \pm 4$
$\Xi_b^{*0} \rightarrow \Xi_b^{*0} \omega$	$10 \pm 2$	$17 \pm 2$	$45 \pm 5$	$13 \pm 2$
$\Xi_b^{*0} \rightarrow \Xi_b^{*0} \phi$	$17 \pm 2$	$25 \pm 3$	$85 \pm 10$	$25 \pm 5$
$\Omega_b^{*-} \rightarrow \Omega_b^{*-} \phi$	$40 \pm 5$	$50 \pm 6$	$140 \pm 20$	$50 \pm 10$

Coupling constants of the light vector mesons with heavy spin -3/2 baryons containing b quark

transition	$g_1$	$g_2$	$g_3$	$g_4$
$\Xi_c^{*+} \rightarrow \Xi_c^{*+} \rho^0$	$8\pm 1$	$13\pm 1$	$27\pm 3$	$16\pm 2$
$\Sigma_c^{*+} \rightarrow \Sigma_c^{*0} \rho^+$	$15\pm 1$	$18\pm 1$	$45\pm 5$	$10\pm 2$
$\Xi_c^{*+} \rightarrow \Sigma_c^{*++} K^{*-}$	$29\pm 2$	$19\pm 1$	$50\pm 10$	$13\pm 2$
$\Omega_c^{*0} \rightarrow \Xi_c^{*+} K^{*-}$	$18\pm 2$	$26\pm 4$	$50\pm 10$	$30\pm 4$
$\Sigma_c^{*++} \rightarrow \Xi_c^{*+} K^{*+}$	$27\pm 4$	$19\pm 1$	$50\pm 10$	$13\pm 2$
$\Xi_c^{*+} \rightarrow \Omega_c^{*0} K^{*+}$	$21\pm 6$	$27\pm 2$	$52\pm 10$	$31\pm 4$
$\Sigma_c^{*++} \rightarrow \Sigma_c^{*++} \omega$	$13\pm 2$	$16\pm 2$	$40\pm 5$	$9\pm 2$
$\Xi_c^{*+} \rightarrow \Xi_c^{*+} \omega$	$10\pm 2$	$11\pm 2$	$23\pm 3$	$17\pm 3$
$\Xi_c^{*+} \rightarrow \Xi_c^{*+} \phi$	$13\pm 2$	$12\pm 1$	$38\pm 5$	$9\pm 2$
$\Omega_c^{*0} \rightarrow \Omega_c^{*0} \phi$	$36\pm 6$	$35\pm 5$	$80\pm 10$	$45\pm 5$

Coupling constants of the light vector mesons with heavy spin -3/2 baryons containing c quark

# Conclusion

- Using the symmetry arguments it is shown that all SSM, SAM, and AAM transitions are described by only one universal function for each class of transition for any Lorentz structure.
- Violation of SU(3) does not produce any new structure in addition than that one existing in SU(3) symmetry case.
- Relations between invariant functions are structure independent, while their explicit expressions are structure dependent.