## Measurement of the $Z^{0}$ Forward-Backward Asymmetry in muon pairs with the ATLAS experiment at LHC



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## Summary

- A brief introduction to the Standard Model of particle physics.
- The ATLAS experiment at LHC.
- The Forward-Backward asymmetry $A_{F B}$ of $Z \rightarrow \mu^{+} \mu^{-}$events.
- Data sample.
- Event selection.
- Raw $A_{F B}$ measurement and unfolding procedure.
- Extraction of $\sin ^{2} \theta_{W}^{\text {eff }}$.
- The 1D fit method.
- Conclusions.


## The Standard Model and the Electroweak theory

- The Standard Model is the theory that describes matter and its interactions in terms of elementary particles.
- The electroweak theory plays an important role in the Standard Model.
- Is based on a symmetry group $\mathrm{SU}(2)_{L} \times \mathrm{U}(1)_{Y}$.
- The invariance of the Lagrangian in reached with the introduction of four bosons, $W_{i}^{\mu}$ with $i=1,2,3$ and $B^{\mu}$.
- The electroweak interactions, charged and neutral, are mediated by vector bosons that are a combination of the $\mathbf{W}^{\mu}$ and of $B^{\mu}$.

$$
W^{ \pm \mu}=\frac{1}{\sqrt{2}}\left(W_{1}^{\mu} \pm i W_{2}^{\mu}\right) \quad\binom{Z^{\mu}}{A^{\mu}}=\left(\begin{array}{cc}
\cos \theta_{W} & -\sin \theta_{W} \\
\sin \theta_{W} & \cos \theta_{W}
\end{array}\right)\binom{W_{3}^{\mu}}{B^{\mu}}
$$

- The particles $W^{+}, W^{-}$and $Z^{0}$ were discovered at CERN by the UA1 and UA2 experiments in 1983 and studied at LEP and Tevatron.
- Their mass values agree with the prediction from the SM.

$$
M_{Z}=\frac{M_{W}}{\cos \theta_{W}}
$$

## The Large Hadron Collider at CERN

- The LHC is a proton-proton collider of 27 Km circumference.
- Since March 2010 is collecting interactions at the energy of 7 TeV in the center of mass.


## CERN Accelerator Complex




- Presently an integrated luminosity of about $5 \mathrm{fb}^{-1}$ has been collected.
- Peak luminosity of $3.3 \times 10^{33} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$.

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## The ATLAS experiment

- General purpose detector to explore all proton-proton collisions.
- Main goals:
- The discovery of the Higgs Bosons.
- The discovery of physics Beyond Standard Model.

- Magnet system.
- Air-core toroidal magnets.
- Composed of different sub-detectors.
- Inner Detector. Three technologies:
- Si pixel.
- Si strips.
- Straw tubes.
- Central solenoid.
- Electromagnetic calorimeter.
- $\mathrm{Pb} / \mathrm{LAr}+\mathrm{Cu} / \mathrm{LAr}$.
- Hadronic calorimeter.
- $\mathrm{Pb} /$ Tiles.
- Muon spectrometer.
- Precision muon tracking (MDT+CSC).
- Dedicated trigger system (RPCs at $|\eta|<1.05$ and TGCs at $1.05<|\eta|<2.7$ )
Semiconductor tracker


## The Forward-Backward asymmetry $A_{F B}$ in $p p \rightarrow Z / \gamma^{*} \rightarrow \mu^{+} \mu^{-}$events

- It is due to the $V-A$ nature of the electroweak interaction.
- Neutral current coupling: $J_{Z f}=\bar{f}\left(g_{V}^{f}+g_{A}^{f} \gamma_{5}\right) f$.
- Differential cross-section:


$$
\begin{gathered}
\frac{d \sigma}{d \cos \theta}=\frac{4 \pi \alpha^{2}}{3 s}\left[\frac{3}{8} A\left(1+\cos \theta^{2}\right)+B \cos \theta\right] \\
A=Q_{l}^{2} Q_{q}^{2}+2 Q_{l} Q_{q} g_{V}^{q} g_{V}^{\prime} R e(\chi(s))+\left(g_{V}^{\prime 2}+g_{A}^{\prime 2}\right)\left(g_{V}^{q 2}+g_{A}^{q 2}\right)|\chi(s)|^{2} \quad B=\frac{3}{2} g_{A}^{q} g_{A}^{\prime}\left(Q_{l} Q_{q} R e(\chi(s))+2 g_{V}^{q} g_{V}^{\prime}|\chi(s)|^{2}\right)
\end{gathered}
$$

- the $\cos \theta$ term gives rise to the forward-backward asymmetry
$A_{F B}=\frac{\sigma_{F}-\sigma_{B}}{\sigma_{F}+\sigma_{B}}=\frac{\int_{0}^{1} \frac{d \sigma}{d \cos \theta} d \cos \theta-\int_{-1}^{0} \frac{d \sigma}{d \cos \theta} d \cos \theta}{\int_{0}^{1} \frac{d \sigma}{d \cos \theta} d \cos \theta+\int_{-1}^{0} \frac{d \sigma}{d \cos \theta} d \cos \theta}=\frac{N_{F}-N_{B}}{N_{F}+N_{B}}=\frac{3 B}{8 A}$
- Forward Event: $\cos \theta>0$. Backward Event: $\cos \theta<0$.



## The Collins-Soper reference frame

- Consider the incoming quark. There are two possibilities


## No transverse momentum


$\Downarrow$
$\theta$ is determined unambiguously from the four-momenta of the leptons.
$\theta$ is the angle that the lepton makes with the proton beam in the center-of- mass frame of the lepton pair.

## Significant transverse momentum


exists an ambiguity in the four-momenta of the incoming quarks in the frame of the dilepton pair.

$$
\Downarrow
$$

The Collins-Soper formalism: the polar axis is defined as the bisector of the proton beam momentum and the negative of the anti-proton beam momentum when they are boosted into the center-of-mass frame of the dilepton pair.

$$
\cos \theta^{*}=\frac{2}{Q \sqrt{Q^{2}+Q_{T}^{2}}}\left(P_{1}^{+} P_{2}^{-}-P_{1}^{-} P_{2}^{+}\right)
$$

## $\sin ^{2} \theta_{W}^{e f f}$ measurement from $A_{F B}$

$$
\begin{gathered}
A_{F B}=\frac{3 B}{8 A} \\
A=Q_{I}^{2} Q_{q}^{2}+2 Q_{I} Q_{q} g_{V}^{q} g_{V}^{\prime} \operatorname{Re}(\chi(s))+\left(g_{V}^{\prime 2}+g_{A}^{\prime 2}\right)\left(g_{V}^{q 2}+g_{A}^{q 2}\right)|\chi(s)|^{2} \\
B=\frac{3}{2} g_{A}^{q} g_{A}^{\prime}\left(Q_{I} Q_{q} \operatorname{Re}(\chi(s))+2 g_{V}^{q} g_{V}^{\prime}|\chi(s)|^{2}\right) \\
\frac{g_{V}^{f}}{g_{A}^{f}}=1-\frac{2 Q_{f}}{l_{f}^{3}} \sin ^{2} \theta_{W}^{e f f}
\end{gathered}
$$

- $A_{F B}$ directly related with the value of the $\sin ^{2} \theta_{W}^{e f f}$.


## Data and Monte Carlo samples

MC statistic used

| Channel | Number of Events | Cross Section (nb) |
| :---: | :---: | :---: |
| $Z \rightarrow \mu \mu$ | 4999129 | 0.85525 |
| $Z \rightarrow \tau \tau$ | 1998042 | 0.854 |
| $W \rightarrow \mu \nu$ | 6965567 | 8.9379 |
| $W \rightarrow \tau \nu$ | 998368 | 8.9291 |
| $W W \rightarrow l l \nu \nu$ | 1399724 | 0.000505 |
| $W^{+} Z \rightarrow l \nu l l$ | 24995 | 0.011126 |
| $W^{+} Z \rightarrow l \nu q q$ | 24989 | 0.011231 |
| $W^{-} Z \rightarrow l \nu l l$ | 99972 | 0.0060414 |
| $W^{-} Z \rightarrow l \nu q q$ | 24993 | 0.0060842 |
| $Z Z \rightarrow l l q q$ | 24990 | 0.0056683 |
| $Z Z \rightarrow l l l l$ | 99982 | 0.0056757 |
| $Z Z \rightarrow l l \nu \nu$ | 99978 | 0.0056702 |
| $c c$ | 1499511 | 28.0305 |
| $b b$ | 4482783 | 72.6217 |
| $t t$ | 998771 | 0.1458 |

## $Z / \gamma^{*} \rightarrow \mu^{+} \mu^{-}$event selection

- Single muon trigger.

$$
p_{T}^{\mu}>18 \mathrm{GeV}
$$

- Vertex:
$\begin{array}{ll} & N_{\text {tracks }}>3 . \\ & z_{\text {vertex }}<150 \mathrm{~mm} .\end{array}$
- Preselection:

○ $p_{T}>20 \mathrm{GeV}$.
O Muon reconstructed using both ID and MS.

- $\eta<2.4$.
- $\left(z_{0}-z_{\text {vertex }}\right)<10 \mathrm{~mm}$.
- Isolation:

○ $\frac{\sum p_{T}}{p_{T}^{\mu}}<0.2$ in a cone of

$$
\Delta R<0.4
$$

- Opposite charge.
- $Z$ mass window:

○ $66<M_{\mu \mu}<110 \mathrm{GeV}$.

- $1.282 \mathrm{M} Z / \gamma^{*}$ candidates found in data sample.
$\mathrm{Z} / \boldsymbol{\gamma}^{*} \rightarrow \mu^{+} \mu^{-}$invariant mass distribution

$\mathrm{Z} / \boldsymbol{\gamma}^{\boldsymbol{*}} \rightarrow \boldsymbol{\mu}^{+} \boldsymbol{\mu}^{-}$rapidity distribution



## Raw $A_{F B}$ measurement

- Divide the mass spectrum in bins.
- In each bin count the number of forward and backward events.
- Subtract the number of forward and backward events due to the background estimated by MC.
- Compute the raw $A_{F B}$ value using the relation:

$$
A_{F B}=\frac{N^{F}-N^{B}}{N^{F}+N^{B}}
$$



## Unfolding of the $A_{F B}$ distribution.

- Two effects to be taken into account:
- $Z$ Mass migration.

O Final state radiation (FSR) of muons and detector resolution.

- Dilution.

O Lack of knowledge on which of the beam contributes with a quark to the interaction.

- Corrections are applied by means of response matrices.
- Matrices are built using Monte Carlo truth information.
- After the unfolding perfect agreement with Standard Model prediction.

O A deviation from SM could be a signal for new physics.

## Unfolded $\mathrm{A}_{\text {FB }}$ distribution



## Extraction of $\sin ^{2} \theta_{W}^{\text {eff }}$

- We use an expansion of $A_{F B}$ around the $Z$ pole in terms of the center-of-mass energy $s$.

$$
A_{F B}(s) \simeq A_{F B}\left(m_{Z}^{2}\right)+\frac{\left(s-m_{Z}^{2}\right)}{s} \frac{3 \pi \alpha(s)}{\sqrt{2} G_{F} m_{Z}^{2}} \frac{2 Q_{q} Q_{f} g_{A q} g_{A \mu}}{\left(g_{V q}^{2}+g_{A q}^{2}\right)\left(g_{V \mu}^{2}+g_{A \mu}^{2}\right)} \quad \frac{g_{V}^{f}}{g_{A}^{f}}=1-\frac{2 Q_{f}}{l_{f}^{3}} \sin ^{2} \theta_{W}^{e f f}
$$

- To extract $\sin ^{2} \theta_{W}^{\text {eff }}$ fit the $A_{F B}$ vs. $M_{\mu \mu}$ distribution with the expression:

$$
\begin{align*}
& A_{F B}(s) \simeq A_{F B}\left(m_{Z}^{2}\right)+\frac{s-m_{Z}^{2}}{s} \frac{3 \pi \alpha(s)}{\sqrt{2} G_{F} m_{Z}^{2}}  \tag{1}\\
& \cdot\left[\frac{2\left(x_{u}+x_{c}+x_{t}\right)}{1+\left(1-\frac{8}{3} \sin ^{2} \theta_{W}^{e f f}\right)^{2}}+\frac{x_{d}+x_{s}+x_{b}}{1+\left(1-\frac{4}{3} \sin ^{2} \theta_{W}^{e f f}\right)^{2}}\right] \cdot\left[\frac{1}{1+\left(1-4 \sin ^{2} \theta_{W}^{e f f}\right)^{2}}\right]
\end{align*}
$$

- A logarithmic expansion is used for the running of the electromagnetic coupling.

$$
\alpha(s)=\frac{\alpha}{1-\Delta \alpha-\frac{\alpha}{3 \pi} \frac{38}{9} \log \frac{s}{m_{Z}^{2}}}
$$

## $\sin ^{2} \theta_{W}^{\text {eff }}$ measurement

- The mass range chosen to perform the fit is 88.5 $<M_{\mu \mu}<94.5 \mathrm{GeV}$.
- Need to fit the fully unfolded $A_{F B}$ vs. $M_{\mu \mu}$ distribution.
- Results in agreement with Pythia Monte Carlo prediction.

Pythia Monte Carlo prediction

$m_{\mu \mu}$

| $\sin ^{2} \theta_{W}^{\text {eff }}$ | $x_{u}+x_{c}+x_{t}$ | $x_{d}+x_{s}+x_{b}$ |
| :---: | :---: | :---: |
| 0.232 | 0.430 | 0.570 |

$$
\sin ^{2} \theta_{\mathrm{W}}^{\text {eff }} \text { measurement }
$$

| $\sin ^{2} \theta_{\mathrm{W}}^{\text {eff }}$ | $\sin ^{2} \theta_{\mathrm{W}}^{\text {eff }}$ PDG value | $\mathrm{x}_{\mathbf{u}}+\mathrm{x}_{\mathbf{c}}+\mathrm{x}_{\mathbf{t}}$ | $\mathrm{x}_{\mathbf{d}}+\mathrm{x}_{\mathbf{s}}+\mathrm{x}_{\mathbf{b}}$ | $\boldsymbol{\Delta} \boldsymbol{\alpha}$ |
| :---: | :---: | :---: | :---: | :---: |
| $0.23200 \pm 0.00043$ (stat.) | $0.23153 \pm 0.00016$ | $0.3131 \pm 0.0095$ (stat.) | $0.471 \pm 0.011$ (stat.) | $0.020 \pm 0.013$ (stat.) |

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## $\sin ^{2} \theta_{W}^{\text {eff }}$ systematics

- Also studied some systematic errors.
- Use of different PDF sets $\Delta \sin ^{2} \theta_{\mathrm{W}}^{\text {eff }}=\mathbf{0 . 0 0 0 3}$
- Use of different unfolding algorithm $\Delta \boldsymbol{\operatorname { s i n }}^{2} \theta_{\mathrm{W}}^{\text {eff }}=\mathbf{0 . 0 0 4 2}$
- Other systematic error studies are ongoing

$$
\sin ^{2} \theta_{\mathrm{W}}^{\mathrm{eff}}=0.2320 \pm 0.0045 \text { (sys.) } \pm 0.0004 \text { (stat.) }
$$

## Conclusions

The ATLAS experiment at LHC is collecting proton-proton collisions at 7 TeV and successfully remeasuring SM processes

- Analyzed $\sim 1.3 \mathrm{M} \mathrm{Z} \rightarrow \mu \mu$ events collected in 2010-2011 and measured the $A_{F B}$
- This is an important test to search for new physics BSM
- From the $A_{F B}$ extracted, at the $Z$ pole, a preliminary measurement of the $\sin ^{2} \theta_{W}^{e f f}$.
- Result in agreement with the SM expectation and precision measurement at Tevatron
- Some systematics studies already done.
- Goal is to produce a paper in February.


## Backup slides

## $A_{F B}$ expansion

- On the $Z$ pole

$$
A_{F B}=\frac{3}{4} \mathcal{A}_{q} \mathcal{A}_{\mu} \quad \mathcal{A}_{q, \mu}=\frac{2 \frac{g_{V}^{q, \mu}}{g_{A}^{q, \mu}}}{1+\left(\frac{g_{V}^{q, \mu}}{g_{A}^{q, \mu}}\right)^{2}}
$$

- For a pp collider

$$
A_{F B}=\sum_{q=u, d, s, c, t, b} x^{q} A_{F B}^{q} \quad x^{q}=\frac{N_{q}^{+}+N_{q}^{-}}{N^{+}+N^{-}} \quad A_{F B}^{q}=\frac{N_{q}^{+}-N_{q}^{-}}{N_{q}^{+}+N_{q}^{-}}
$$

$\Downarrow$

$$
A_{F B}=\frac{3}{4}\left[\frac{2\left(1-\frac{8}{3} \sin ^{2} \theta_{W}^{\text {eff }}\right)}{1+\left(1-\frac{8}{3} \sin ^{2} \theta_{W}^{e f f}\right)^{2}} \cdot\left(x_{u}+x_{c}+x_{t}\right)+\frac{2\left(1-\frac{4}{3} \sin ^{2} \theta_{W}^{\text {eff }}\right)}{1+\left(1-\frac{4}{3} \sin ^{2} \theta_{W}^{e f f}\right)^{2}} \cdot\left(x_{d}+x_{s}+x_{b}\right)\right] \frac{2\left(1-4 \sin ^{2} \theta_{W}^{\text {eff }}\right)}{1+\left(1-4 \sin ^{2} \theta_{W}^{\text {eff }}\right)^{2}}
$$

## Monte Carlo closure test (1D fit)

- The mass range chosen to perform the fit is $82<M_{\mu \mu}<97.5 \mathrm{GeV}$.
- Need to fit the fully unfolded $A_{F B}$ vs. $M_{\mu \mu}$ distribution.
- Results in agreement with Pythia true values.

|  | Fit Results(Monte Carlo truth) |  |  |
| :---: | :---: | :---: | :---: |
| $\sin ^{2} \theta_{\mathrm{W}}^{\text {eff }}$ | $\mathrm{x}_{\mathrm{u}}+\mathrm{x}_{\mathbf{c}}+\mathrm{x}_{\mathbf{t}}$ | $\mathrm{x}_{\mathbf{d}}+\mathrm{x}_{\mathbf{s}}+\mathrm{x}_{\mathbf{b}}$ | $\mathbf{b}$ |
| $0.2328 \pm 0.0033$ | $0.31 \pm 0.24$ | $0.50 \pm 0.12$ | $0.00497 \pm 0.00088$ |

