

AI-Enhanced BEGe Detectors for Low-Energy X-ray Collapse Model Test

Simone Manti INFN-LNF, Frascati (Italy) on behalf of the VIP-2 collaboration

Content

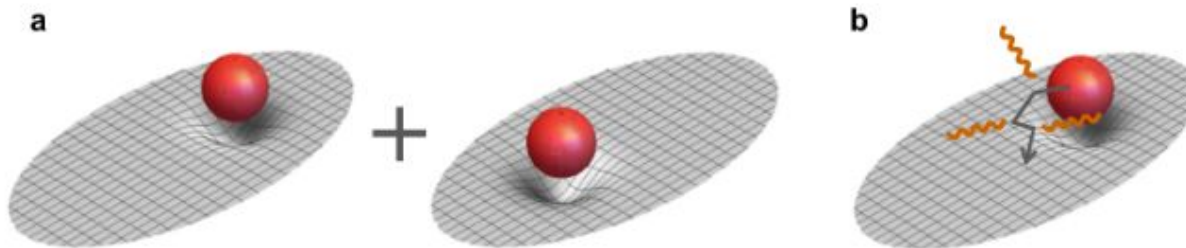
- **Testing Collapse Models through Spontaneous Emission**
- **Emission Rate in the Low-Energy Regime:**
 - **Rate Calculations and Cancellation Effects**
 - **AI-assisted BEGe detector for low-energy analysis**

Content

- **Testing Collapse Models through Spontaneous Emission**
- **Emission Rate in the Low-Energy Regime:**
 - **Rate Calculations and Cancellation Effects**
 - **AI-assisted BEGe detector for low-energy analysis**

The Measurement Problem and Collapse Models

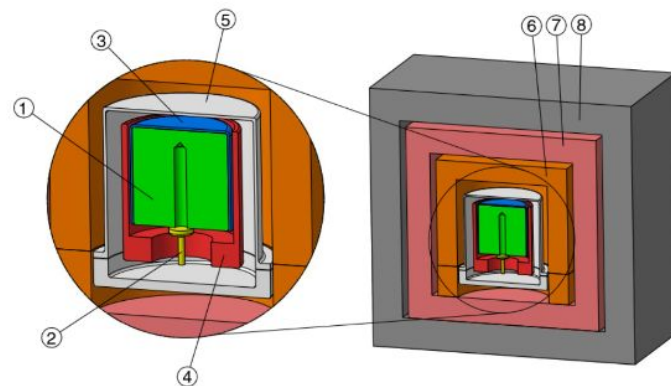
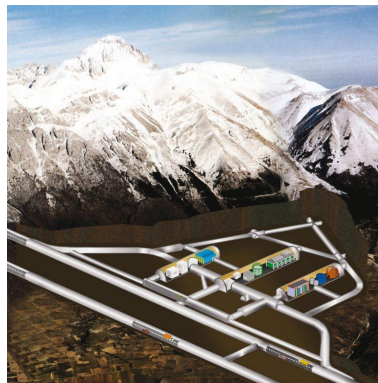
- **Quantum Mechanics:** Allows precise predictions, but superposition principle is not observed in macroscopic systems.
- **Collapse Models:** Propose that quantum mechanics' linearity breaks down at a certain scale to solve the measurement problem (GRW, DP, CSL, Károlyházy,...)
 - **Continuous Spontaneous Localization (CSL)**
 - **Diósi-Penrose (DP)**



How to test Collapse Models?

- Unavoidable side effect of the **Stochastic Collapse Dynamics**: Brownian-like diffusion of the system in space
- **Charged particles** emit spontaneous radiation. We search for spontaneous radiation emission from a germanium crystal and the surrounding materials in the experimental apparatus.

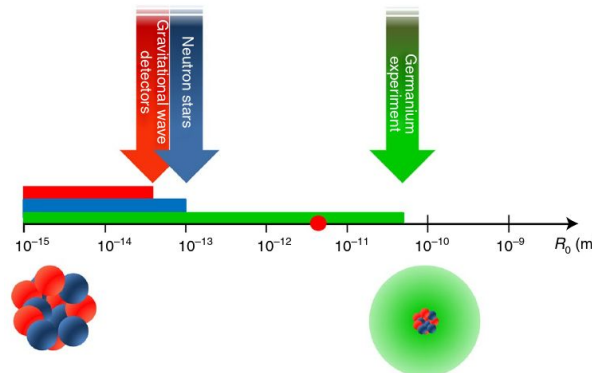
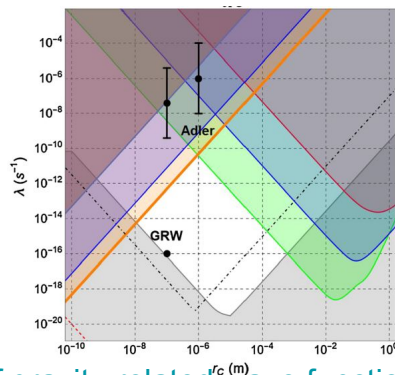
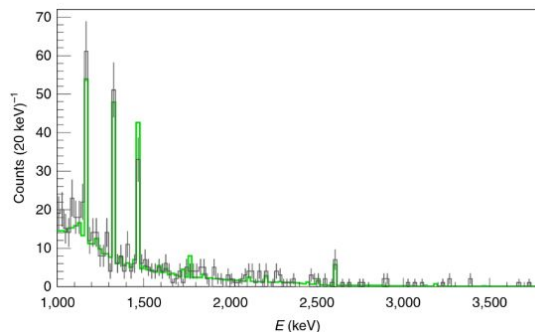
Gran Sasso
environment (LNGS)
low-background
enhanced sensitivity
3600 m w.e.



How to test Collapse Models?

Strategy:

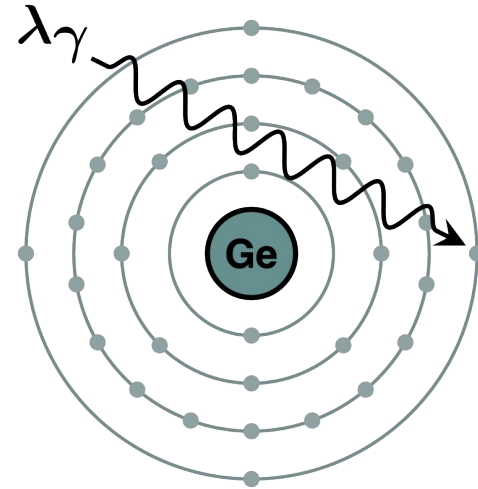
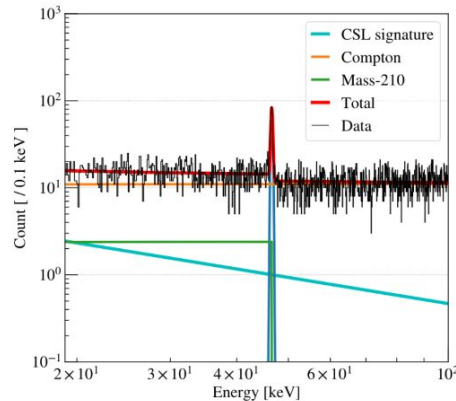
- **Simulate the background** from all the known emission processes
- Perform a **Bayesian inference** of the residual spectrum with the theoretical prediction
- Extract the **PDF** of the **Model Parameters**
- **Bound the Parameters**



[Donadi, Sandro, et al. "Underground test of gravity-related Wave function collapse." *Nature Physics* 17.1 \(2021\): 74-78.](#)

Testing Emission Rate at Low-Energy

- Theoretical spectrum follows a $\sim 1/E$ dependence, implying a **diverging rate at low energies**
- **Low-Energy Region** is the most promising to observe or constrain collapse-induced radiation and discriminate different models



[Arnquist, I. J., et al. *Physical Review Letters* 129.8 \(2022\): 080401.](#)

Content

- **Testing Collapse Models through Spontaneous Emission**
- **Emission Rate in the Low-Energy Regime:**
 - **Rate Calculations and Cancellation Effects**
 - **AI-assisted BEGe detector for low-energy analysis**

Content

- **Testing Collapse Models through Spontaneous Emission**
- **Emission Rate in the Low-Energy Regime:**
 - **Rate Calculations and Cancellation Effects**
 - **AI-assisted BEGe detector for low-energy analysis**

Atomic Structure Effects on the Emission Rate at Low-Energy

- Dissipative dynamics of collapse models is described by a master equation:

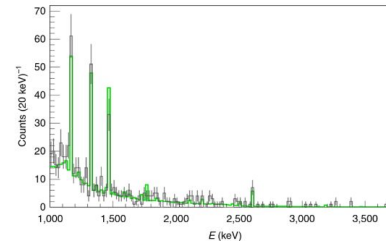
$$\frac{d\hat{\rho}}{dt} = -\frac{i}{\hbar}[\hat{H}, \hat{\rho}] - \frac{1}{2\hbar^2} \int d^3r d^3r' \mathcal{D}(\mathbf{r} - \mathbf{r}') [\hat{\rho}(\mathbf{r}), [\hat{\rho}(\mathbf{r}'), \hat{\rho}]] \quad \hat{\rho}(r) = \sum_{\ell=1}^n m_{\ell} \sum_s a_{\ell}^{\dagger}(r, s) a_{\ell}(r, s)$$

- The **spontaneous emission rate** is given by:

$$\frac{d\Gamma}{dE} \sim \frac{1}{E} \sum_{ij} q_i q_j \frac{\sin(kr_{ij})}{kr_{ij}} (-\nabla^2 D(r, \omega)) \quad -\nabla^2 D(r, \omega) = \begin{cases} \frac{\hbar G}{2\sqrt{\pi}\sigma^3} e^{-r_{ij}^2/4\sigma^2} & \text{(DP)} \\ \frac{6\hbar^2\lambda}{4m_0^2\sigma^3} \left(1 - \frac{r_{ij}^2}{6\sigma^2}\right) e^{-r_{ij}^2/4\sigma^2} & \text{(CSL)} \end{cases}$$

- For **Radiation Wavelengths** larger than **Interatomic Distances**, the rate simplifies to:

$$\frac{d\Gamma}{dE} \sim \frac{1}{E} (N_p^2 + N_e)$$



[Donadi, Sandro, et al. "Underground test of gravity-related wave function collapse." *Nature Physics* 17.1 \(2021\): 74-78.](#)

Low energy limit: Semiclassical Approximation

$$\frac{d\Gamma}{dE} \sim \frac{1}{E} \sum_{ij} q_i q_j \frac{\sin(kr_{ij})}{kr_{ij}} (-\nabla^2 D(r, \omega))$$

- Proton-Proton term:**

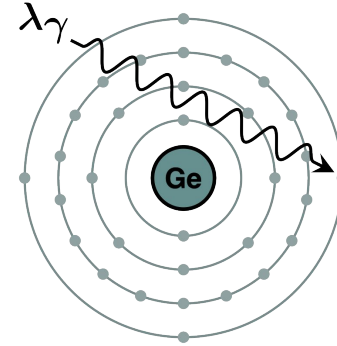
$$|\mathbf{r}_{ip} - \mathbf{r}_{jp}| / \lambda_\gamma \ll 1 \quad (\mathbf{r}_{ip} - \mathbf{r}_{jp})^2 / r_C^2 \ll 1$$

- Proton-Electron term:**

$$|\mathbf{r}_{ip} - \mathbf{r}_{je}^{(o)}| = \langle \mathbf{r}_{je}^{(o)} \rangle = \rho_o$$

- Electron-Electron term:**

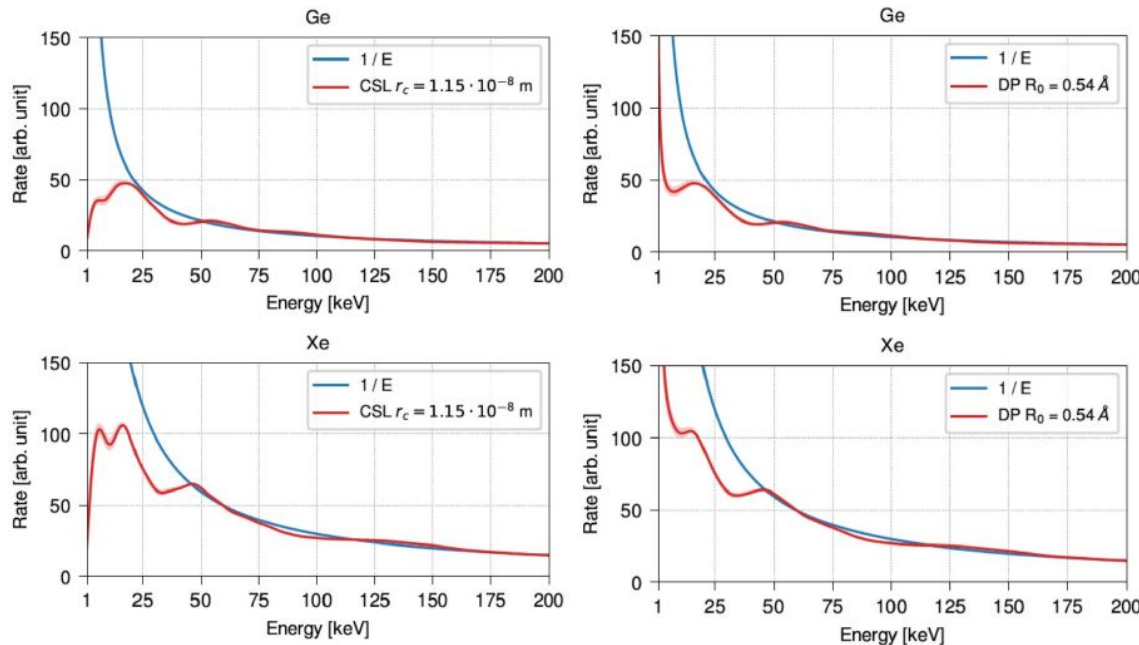
$$\begin{cases} |\mathbf{r}_{ie}^{(o)} - \mathbf{r}_{je}^{(o')}| = \langle \mathbf{r}_{ie}^{(o)} - \mathbf{r}_{je}^{(o')} \rangle = \alpha \rho_o & \text{if } o = o' \\ |\mathbf{r}_{ie}^{(o)} - \mathbf{r}_{je}^{(o')}| = \langle \mathbf{r}_{ie}^{(o)} - \mathbf{r}_{je}^{(o')} \rangle = (1 - \beta) |\rho_o - \rho_{o'}| & \text{if } o \neq o' \end{cases}$$



state nl	occupation	eigenvalue [Hartree]	[eV]	<r> [Bohr]
1s	2.000	-396.251380	-10782.54926	0.048
2s	2.000	-49.051315	-1334.75427	0.214
2p	6.000	-43.720357	-1189.69150	0.185
3s	2.000	-5.960689	-162.19862	0.636
3p	6.000	-4.194670	-114.14278	0.653
3d	10.000	-1.117153	-30.39929	0.733
4s	2.000	-0.426445	-11.60415	2.142
4p	2.000	-0.149906	-4.07915	2.883

[Piscicchia, Kristian, et al. *Physical Review Letters* 132.25 \(2024\): 250203.](#)

Low energy limit: Semiclassical Approximation



- Differences compared to the **$\sim 1/E$ behaviour!**
- **Different model** (CSL and DP) exhibits **different behaviour** as function of the energy
- **Atomic Cancellation** effect in **CSL** at low energies
- Scheme recently used by **XENON** experiment

[Aprile, E., et al. "Challenging Spontaneous Quantum Collapse with XENONnT." *arXiv preprint arXiv:2506.05507* \(2025\).](#)

[Piscicchia, Kristian, et al. *Physical Review Letters* 132.25 \(2024\): 250203.](#)

Low energy limit: Radial Distribution Functions (RDFs)

Including realistic Radial Distribution in the Emission Rate formula:

$$\frac{d\Gamma}{dE} \sim \frac{1}{E} \sum_{ij} q_i q_j \frac{\sin(kr_{ij})}{kr_{ij}} (-\nabla^2 D(r, \omega))$$

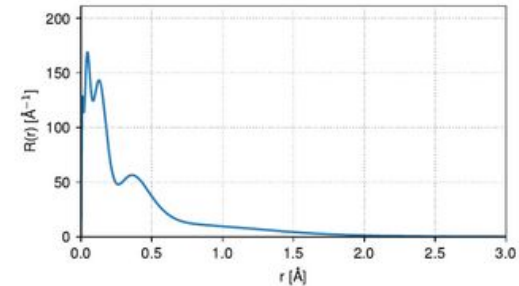
Evaluating the sum with:

$$\frac{d\Gamma}{dE} = \frac{1}{E} \sum_{ij} q_i q_j \int_0^\infty dr P_{ij}(r) \frac{\sin(kr)}{kr} f(r) (-\nabla^2 D(r, \omega))$$

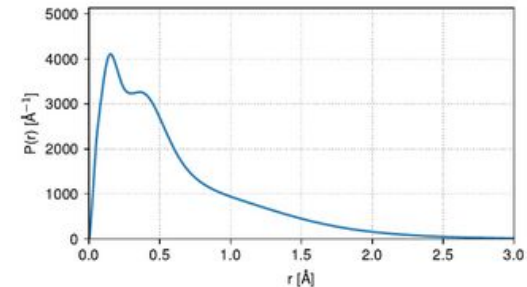
$$P_{ij}(r)dr$$

**Probability to find emitters i and j
at distance r!**

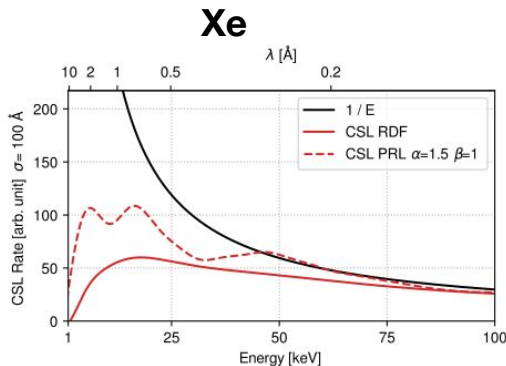
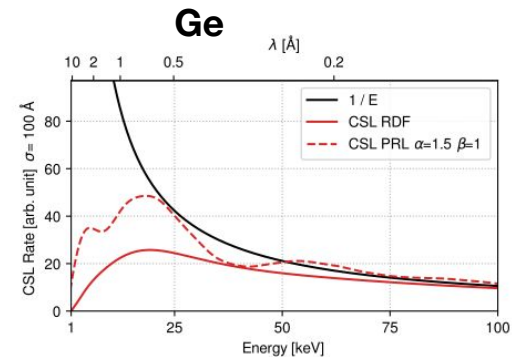
Proton-Electron RDF



Electron-Electron RDF

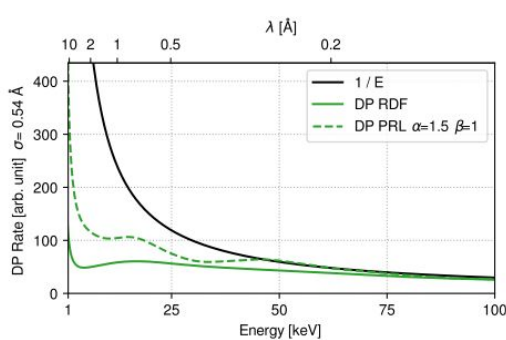
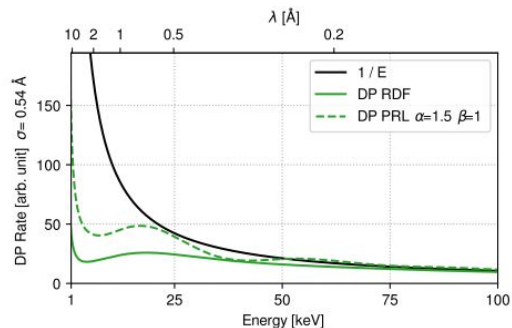


Low energy limit: Radial Distribution Functions



- Recovering former results with RDF:

- Difference $\sim 1/E$
- Model dependence
- Cancellation effects



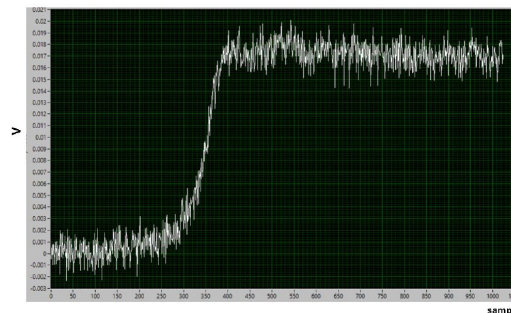
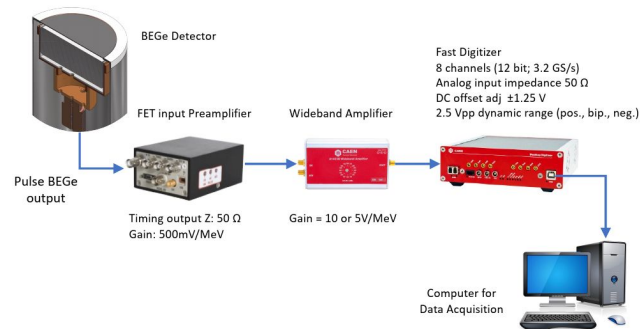
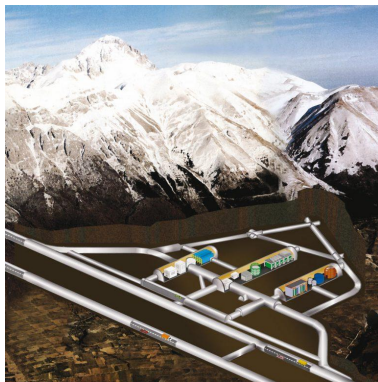
- Smoother rates due to realistic emitters radial density
- Paper in preparation!

Content

- **Testing Collapse Models through Spontaneous Emission**
- **Emission Rate in the Low-Energy Regime:**
 - **Rate Calculations and Cancellation Effects**
 - **AI-assisted BEGe detector for low-energy analysis**

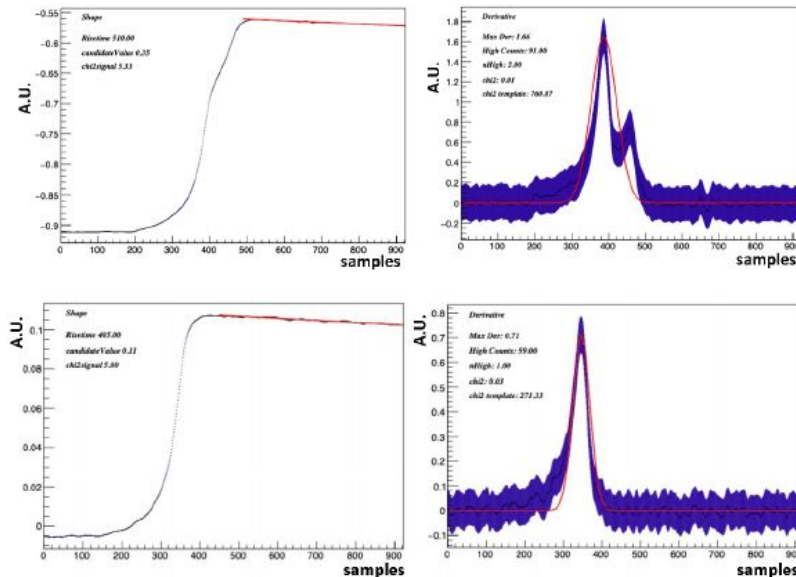
BEGe Detector Emission Rate Measurement at LNGS

- BEGe detector at the *Laboratori Nazionali del Gran Sasso (LNGS)*
- Spectrum obtained from Waveform acquisition optimized for **Low-Energy (< 20 keV)** events



[Piscicchia, Kristian, et al. "Optimization of a BEGe Detector Setup for Testing Quantum Foundations in the Underground LNGS Laboratory." *Condensed Matter* 9.2 \(2024\): 22.](#)

Pulse Shape Analysis of BEGe 2021 Waveforms



Ad-Hoc **Pulse Shape Analysis (PSA)** on 2021 Data Acquisition

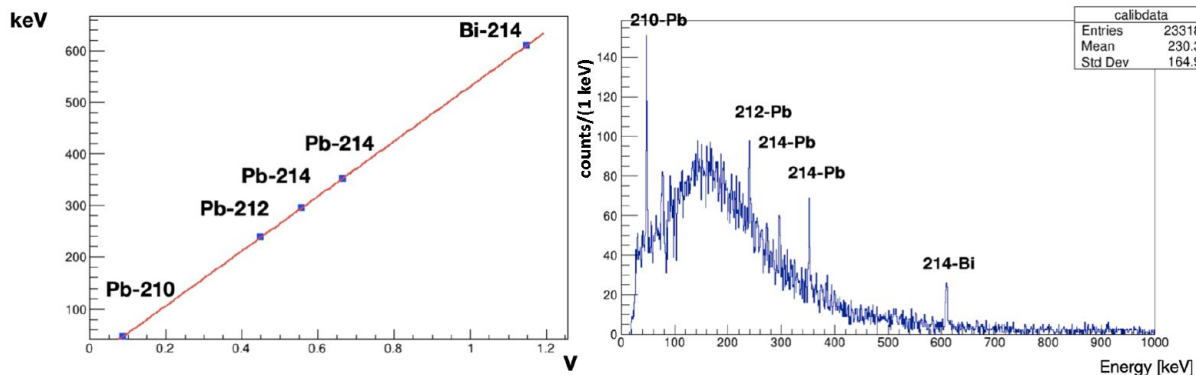
The **PSA** was performed using custom selection criteria:

1. **χ^2 -score** from a template-fit to quantify waveform shape agreement.
2. **Number of peaks** identified in the pulse derivative to distinguish multi-site events.
3. **Mean amplitude** at the **start and end** of the waveform to detect slow-rise or flat-top events.

[Piscicchia, Kristian, et al. "Optimization of a BEGe Detector Setup for Testing Quantum Foundations in the Underground LNGS Laboratory." *Condensed Matter* 9.2 \(2024\): 22.](#)

Minimum Energy Threshold for BEGe with PSA

- Validation performed on **2021 spectrum** in the 20–1000 keV range
- Energy calibration using **Pb and Bi reference peaks** (linear response)
 - **Low-energy sensitivity: ~20 keV**
 - **High resolution: 2 keV @ 100 keV**
 - **Linear calibration with Pb/Bi peaks**

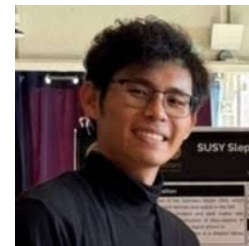


[Piscicchia, Kristian, et al. "Optimization of a BEGe Detector Setup for Testing Quantum Foundations in the Underground LNGS Laboratory." *Condensed Matter* 9.2 \(2024\): 22.](#)

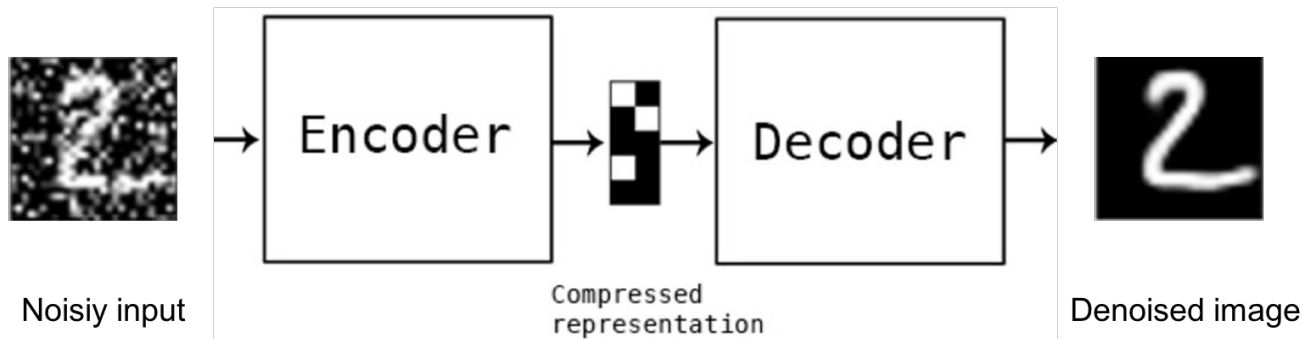
Improving and Automating PSA with Machine Learning

Using a Denoising Autoencoder (DAE) for Pulse Shape Analysis

- Enhance waveform quality and automate feature extraction
- **Approach:**
 - **Denoise** waveforms using a trained **Autoencoder**
 - **Extract features** to build a **Labeled Dataset** for *normal* and *anomalous* events.

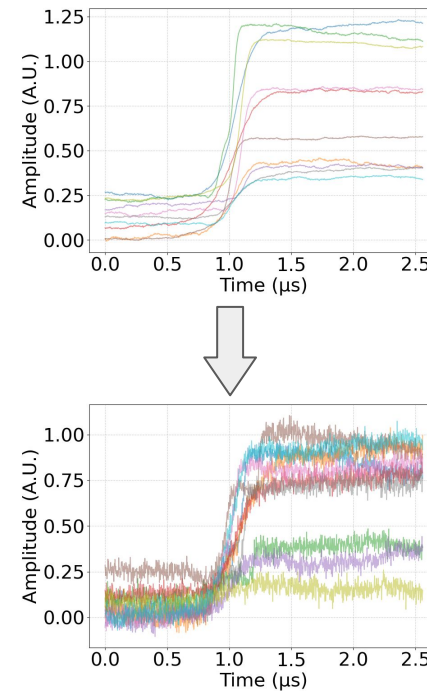
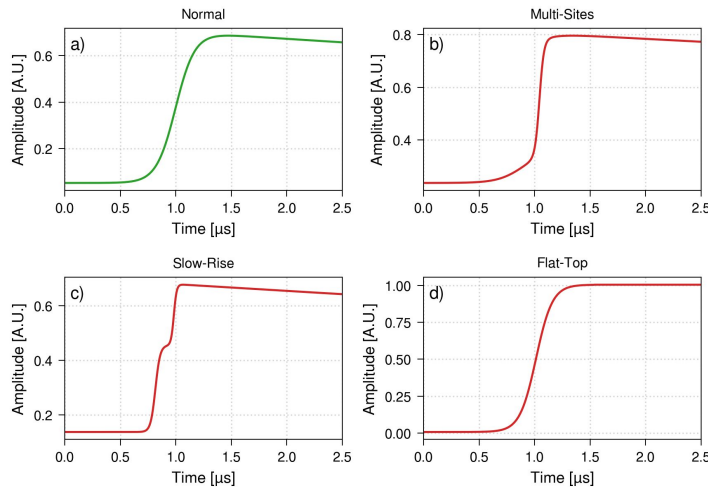


Jason Yip



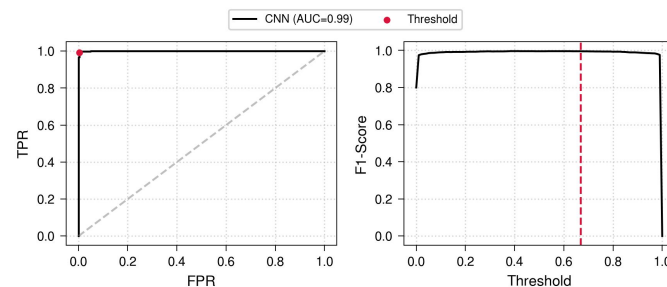
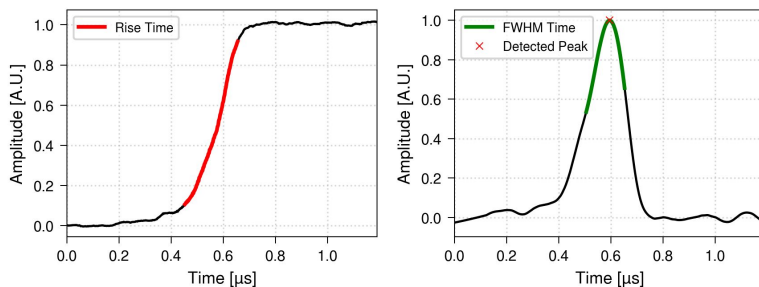
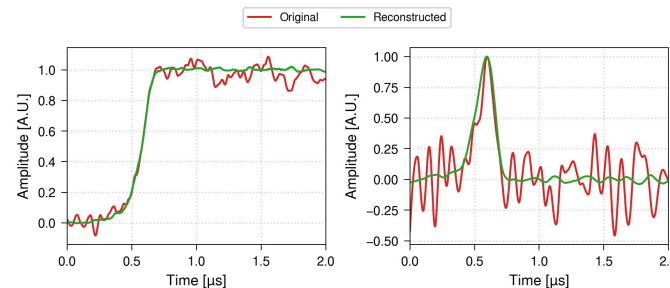
Training the DAE on a Synthetic Dataset

- Synthetic waveforms generated for **Normal**, **Multi-site**, **Slow-rise**, and **Flat-top** events
- Provide controlled inputs for **DAE training and validation**
- Enable robust feature learning before applying to real data



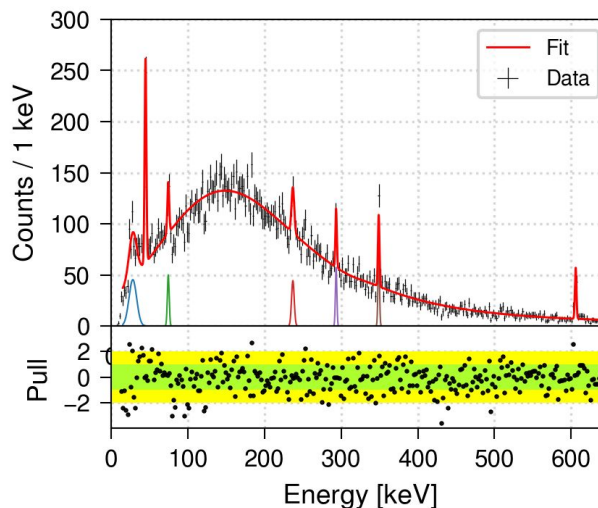
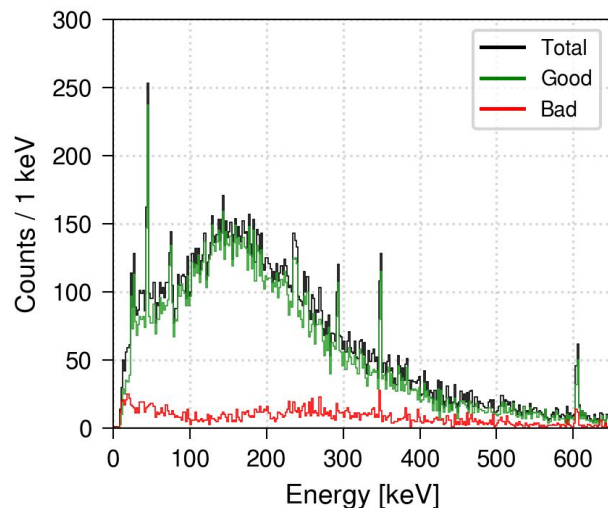
Using DAE on Real BEGe Waveforms

- **Cleaning real BEGe waveforms** with the Denoising Autoencoder (DAE), compared to a **parameter-based filter** (e.g., *Savitzky–Golay*).
- **Extracting features** from denoised signals to build a **labeled waveform dataset**.
- **Attaching a classifier** (e.g., CNN) to distinguish **normal** from **anomalous** events.



Building Spectrum from DAE Event Selection

- **Spectrum reconstruction** from waveform amplitudes using a **trapezoidal filter**
- **Performance improvement** compared to manual PSA



- $E_{\min} \sim 10 \text{ keV}$
- $\text{FWHM} \sim 1 \text{ keV@100 keV}$
- S / B improved by 20% over manual PSA

Conclusion

- **Testing Collapse Models through Spontaneous Emission**
- **Emission Rate in the Low-Energy Regime:**
 - **Rate Calculations and Cancellation Effects**
 - **AI-assisted BEGe detector for low-energy analysis**

Conclusion

- **Testing Collapse Models through Spontaneous Emission**
- **Emission Rate in the Low-Energy Regime:**
 - **Rate Calculations and Cancellation Effects**
 - **AI-assisted BEGe detector for low-energy analysis**

Thank you for your Attention!