

Seeking New Physics with the
 $\pi \rightarrow e \nu$ Branching Ratio

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Overview of Light Particle Rare Decay Experiments

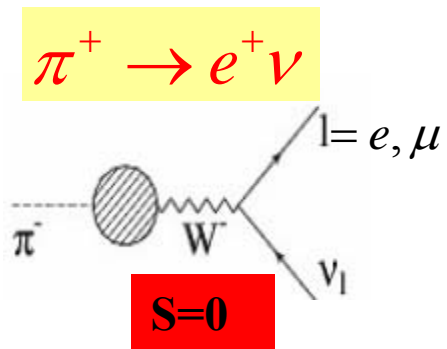
State of the art: single event sensitivity, 10^{-12}

<p>Exotic Searches <i>New physics if seen; SM effects are negligible.</i></p>	<p>$K_L^0 \rightarrow \mu e$ LFV $\mu \rightarrow e\gamma$ LFV $\mu^- N \rightarrow e^- N$ LFV $K^+ \rightarrow \pi^+ f$ "Axions"</p>
<p>SM Parameters and BSM Physics <i>New physics if deviations from well-calculated SM predictions occur.</i></p>	<p>$\frac{\pi^+(K^+) \rightarrow e^+ \nu}{\pi^+(K^+) \rightarrow \mu^+ \nu}$ Universality $\pi^+ \rightarrow \pi^0 e \nu$ V_{ud} $K_L^0 \rightarrow \mu^+ \mu^-$ V_{td} $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ V_{td} $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ CP violation</p>
<p>Low Energy QCD Chiral Perturbation Theory</p>	<p>Radiative decays $K_L^0 \rightarrow ee$</p>

$e - \mu - \tau$ Lepton Universality

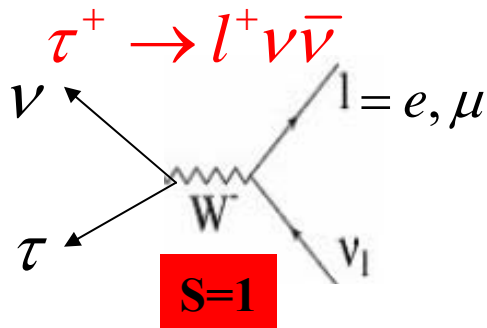
Standard Model: e, μ, τ have identical electroweak gauge interactions.

Differ only in mass and coupling to Higgs boson.



$$R_{e/\mu}^0 \equiv \frac{\Gamma(\pi^+ \rightarrow e^+ \nu)}{\Gamma(\pi^+ \rightarrow \mu^+ \nu)} = \frac{m_e^2}{m_\mu^2} \frac{\left(1 - \frac{m_e^2}{m_\pi^2}\right)}{\left(1 - \frac{m_\mu^2}{m_\pi^2}\right)} = 1.284 \times 10^{-4}$$

Independent of f_π, V_{ud} .



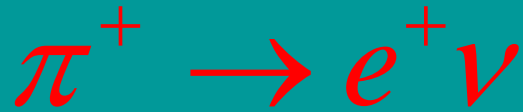
$$R_{e/\mu}^\tau = \left(1 - \frac{8m_\mu^2}{m_\tau^2} \dots\right) = 1.0282$$

Unless... new physics does not respect universality.

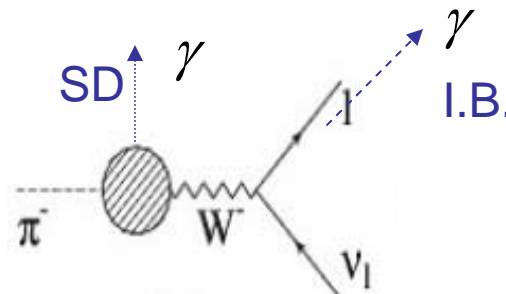
Universality Tests

Mode	g_e/g_μ
$\pi \rightarrow e\nu / \pi \rightarrow \mu\nu$	0.9983 ± 0.0015
$K \rightarrow e\nu / K \rightarrow \mu\nu$	1.012 ± 0.010
$\tau \rightarrow e\nu\nu / \tau \rightarrow \mu\nu\nu$	0.9999 ± 0.0021
ν_e/ν_μ scattering	1.10 ± 0.05
W decays	0.999 ± 0.011
$K^{+0} \rightarrow \pi e\nu / K^{+0} \rightarrow \pi\mu\nu$	$1.0018 \pm 0.0025^*$

*M. Moulson, Flavinet Mini-workshop, Frascati 2007



Radiative Corrections; Inner Bremsstrahlung, and Structure-Dependent Radiation:



$$\Gamma(\pi \rightarrow l \bar{\nu}_l(\gamma)) = \frac{G_\mu^2 |V_{ud}|^2}{8\pi} f_\pi^2 m_\pi m_l^2 \left[1 - \frac{m_l^2}{m_\pi^2} \right]^2 \left[1 + \frac{2\alpha}{\pi} \ln \left[\frac{m_Z}{m_\rho} \right] \right] \gamma$$

$$\times \left[1 - \frac{\alpha}{\pi} \left\{ \frac{3}{2} \ln \left[\frac{m_\rho}{m_\pi} \right] + C_1 + C_2 \frac{m_l^2}{m_\rho^2} \ln \frac{m_\rho^2}{m_l^2} + C_3 \frac{m_l^2}{m_\rho^2} + \dots \right\} \right] \left[1 + \frac{\alpha}{\pi} F(x) \right]$$

[+ π Structure-dependent $\pi^+ \rightarrow e^+ \nu \gamma$ terms] -4% for $l=e$

where $G_\mu = 1.16637(1) \times 10^{-5} \text{ GeV}^{-2}$, $V_{ud} = 0.9738$

But, most factors cancel in the ratio

$$R_{e/\mu}^{th} = \frac{\Gamma(\pi \rightarrow e\nu + \pi \rightarrow e\nu\gamma)}{\Gamma(\pi \rightarrow \mu\nu + \pi \rightarrow \mu\nu\gamma)}$$

$$R_{e/\mu}^{th} = R_{e/\mu}^0 \left\{ 1 + \frac{\alpha}{\pi} \left[F\left(\frac{m_e}{m_\pi}\right) - F\left(\frac{m_\mu}{m_\pi}\right) + C_2 \frac{m_\mu^2}{m_\rho^2} \ln \frac{m_\rho^2}{m_\mu^2} + C_3 \frac{m_\mu^2}{m_\rho^2} \right] (+SD_\pi) \right\}$$

8×10^{-8}

F : kinematic factors

$C_2 = 3.1$ (Terent'ev)

C_3 : Small but
Model dependent
Marciano : 0 ± 10

Pure Structure Dependent (SD) $\pi \rightarrow e\nu\gamma$ corrections are not helicity suppressed but are small and known for π decay:



$$R_{e/\mu}^{th} = (1.2353 \pm 0.0004) \times 10^{-4}$$

Marciano $\rightarrow \pm 0.0001?$

V. Cirigliano (TBA*)

Possibly the most accurately calculated decay process involving hadrons .



$$R_{K \rightarrow e/\mu}^{th} = (2.472 \pm 0.001^*) \times 10^{-5}$$

Helicity suppression 5x $\pi^+ \rightarrow e^+ \nu$

Finkemeier(1995)

Structure dependent radiation not included.

Experiments

$$\pi \rightarrow e\nu$$

$$R_{e/\mu}^{\text{exp}\pi} (\pm 0.4\%)$$

$$1.2265(34)(44) \times 10^{-4} \text{ TRIUMF (1992)}$$

$$1.2346(35)(36) \times 10^{-4} \text{ PSI (1993)}$$

$$R_{e/\mu}^{\text{th}} - R_{e/\mu}^{\text{exp}} = 43(37) \times 10^{-8}$$

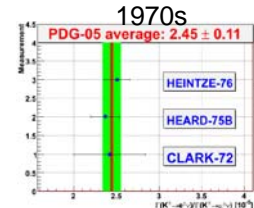
Two new $\pi \rightarrow e\nu$ experiments.
Goals: $\pm (5) \times 10^{-8}$ (0.05%)

$$K \rightarrow e\nu / K \rightarrow \mu\nu$$

$$R_{e/\mu}^{\text{exp}K} (\pm 2\%)$$

$$2.45(11) \times 10^{-5}$$

$$2.416(43)(24) \times 10^{-5} \text{ CERN(2006)}$$



$$R_{e/\mu}^{\text{th}} - R_{e/\mu}^{\text{exp}} = 56(46) \times 10^{-8}$$

KLOE: Stay tuned \rightarrow (1-2%?);
New $K \rightarrow e\nu$ experiment at CERN.
Goal: $\pm (10) \times 10^{-8}$ (0.3%)

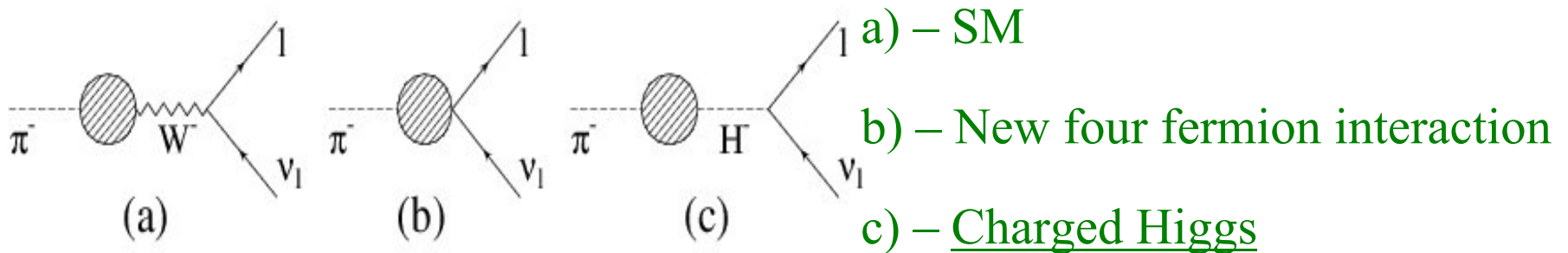
$$\pi^+ \rightarrow e^+ \nu$$

Beyond the Standard Model

High Sensitivity to New **Pseudoscalar** Interactions which are not helicity suppressed.

PS contribution comes as interference term with the axial-vector (dominant) term.

Effect is proportional to $1/\Lambda^2$ where Λ is the mass of the hypothetical particle.



$$1 - \frac{R_{e/\mu}^{New}}{R_{e/\mu}^{SM}} \sim \mp \frac{\sqrt{2}\pi}{G_\mu} \frac{1}{\Lambda_{eP}^2} \frac{m_\pi^2}{m_e(m_d + m_u)} \sim \left(\frac{1\text{TeV}}{\Lambda_{eP}}\right)^2 \times 10^3$$

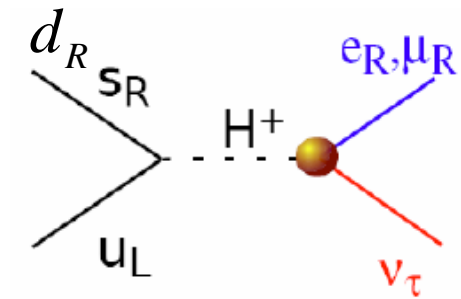
0.05 % Measurement $\rightarrow \Lambda_{eP} > 1000 \text{ TeV}$

Charged Higgs mass $m_{H^\pm} \sim 200 \text{ TeV}$ probed.

Charged Higgs and Lepton Flavor Violation

Masiero, Paradisi, Petronzio (2006)

The unobserved neutrino involved in $\pi^+ / K^+ \rightarrow e^+ \nu$ decay may be ν_e, ν_μ , or ν_τ



Low Energy SUSY (with R parity*); Large $\tan \beta$.

$$\mathbf{R}_{e/\mu}^{NP} = \mathbf{R}_{e/\mu}^{SM} \left(1 + \Delta r_{NP}^{e/\mu} \right)$$

Current (Future) Experiments:

$$\left| \Delta r_{\pi}^{e/\mu} \right| < 0.004 \quad (0.0003)$$

$$\left| \Delta r_{K}^{e/\mu} \right| < 0.06 \quad (0.005)$$

*R Parity (MSSM): $\mathbf{R} = (-1)^{3\mathbf{B} + \mathbf{L} + 2\mathbf{S}}$

i) FCNC $M \rightarrow l\nu_l$; $\Delta r_{NP}^{e/\mu} < 10^{-6}$

ii) **Lepton Flavor Violation** $M \rightarrow l_i\nu_k$; $i(=e, \mu), \neq k(=\tau)$.

$$\Delta r_{SUSY}^{e/\mu} = \left(\frac{m_P}{m_H}\right)^4 \left(\frac{m_\tau}{m_e}\right)^2 \Delta_P^{31} \tan^6 \beta \quad P = \pi, K$$
$$\leq O_K(0.01), O_\pi(0.0003);$$

For $\Delta_P^{31} \sim 5 \cdot 10^{-4}$, $\tan \beta \sim 40$

Effects (optimistically!) in range of planned experiments.

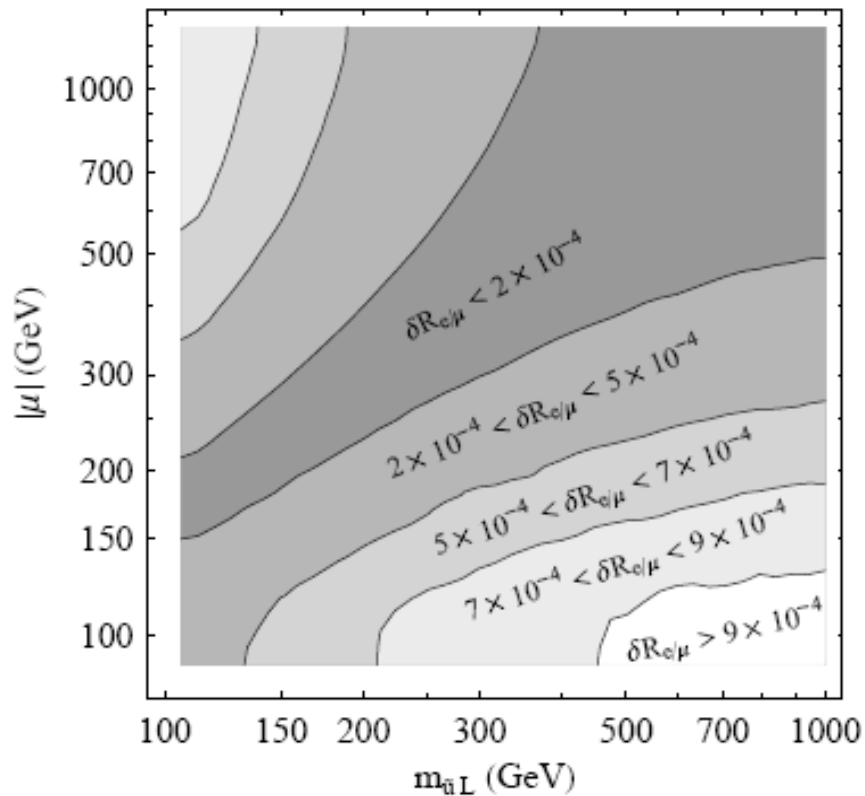
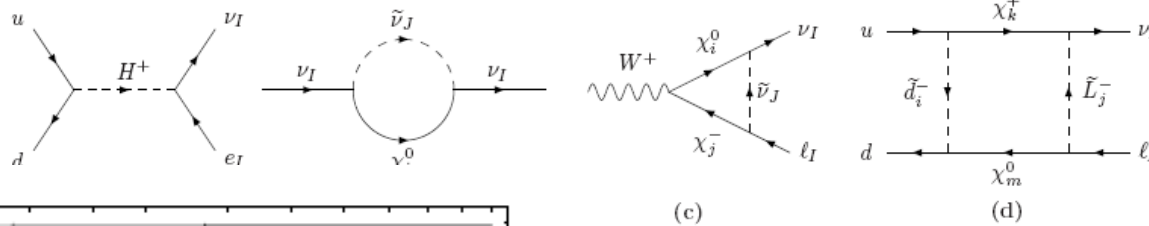
For the parameters above $R(\tau \rightarrow \mu\gamma) \sim 10^{-10}$;

(Present experiment (Babar/Belle) $R(\tau \rightarrow \mu/e\gamma) < 10^{-7}$.)

Larger effects in $B \rightarrow l\nu$, beyond reach of current experiments.

$\pi^+ \rightarrow e^+ \nu$ Sensitive to R-Parity Violating MSSM

Ramsey-Musolf, Su, Tulin (2007)



μ vs. $m_{\tilde{u}_L}$
 μ : Higgsino mass parameter
 $m_{\tilde{u}_L}$: Mass of \tilde{u}_L

Scalar Interactions:

$\pi \rightarrow e\nu$ vs. Super-allowed β Decay

$$\left\{ \begin{array}{l} CKM \text{ Unitarity: } |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9992(10) \\ R_{e/\mu} = \frac{\Gamma(\pi^+ \rightarrow e^+\nu)}{\Gamma(\pi^+ \rightarrow \mu^+\nu)} = 1.231(4) \times 10^{-4} \text{ (now } \rightarrow < 0.1\%) \end{array} \right\} 0.1\% \text{ Precision}$$

Constraining new Physics?

Direct Constraints

$$R_{e/\mu} : \quad \Lambda_A \sim 20 \text{ TeV}, \quad \Lambda_P \sim 1000 \text{ TeV} (!) \quad SM : \frac{G_\mu}{\sqrt{2}} \sim \frac{\pi}{2\Lambda_{SM}^2}; \quad \Lambda_{SM} \sim 440 \text{ GeV}$$

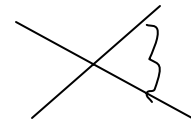
$$\text{Unitarity:} \quad \Lambda_V \sim 20 \text{ TeV}, \quad \Lambda_S \sim 12 \text{ TeV}$$

Induced Current Constraints

$$R_{e/\mu} : \quad \Lambda_V \sim 2 \text{ TeV}, \quad \Lambda_S \sim 60 \text{ TeV} (!)$$

$$\text{Unitarity:} \quad \Lambda_A \sim 2 \text{ TeV}$$

Loops

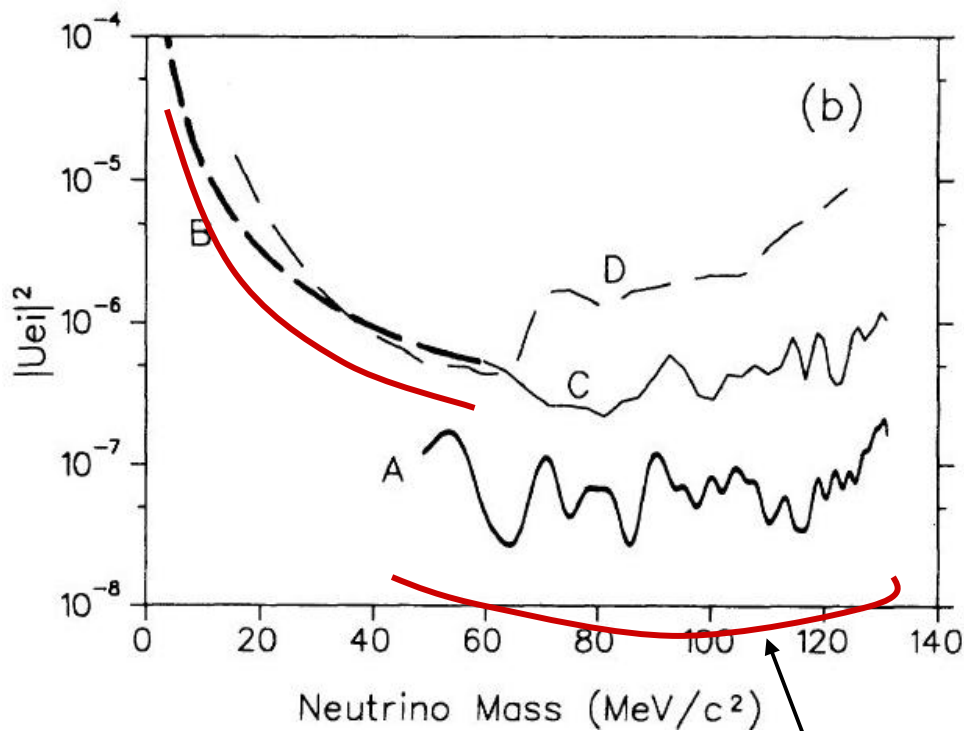


**e.g. A induces V
P induces S**

$$\pi / K^+ \rightarrow e^+ \nu$$

Other BSM Physics :

Heavy ν



expected

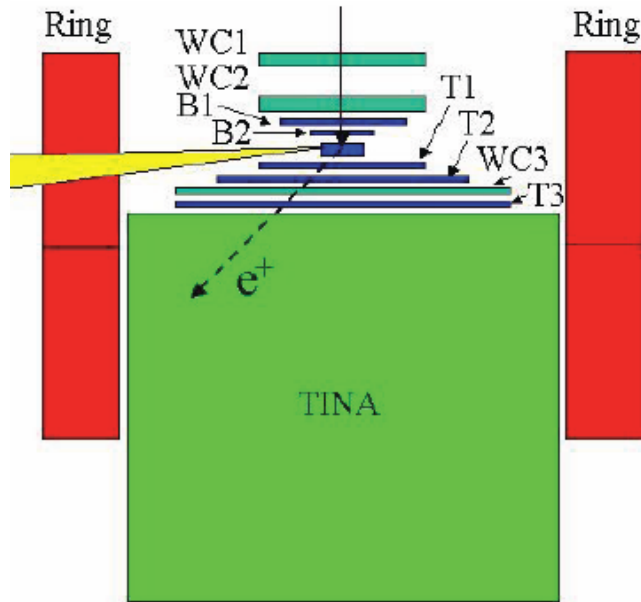
SM extensions:

- Leptoquarks
- Excited gauge bosons
- Compositeness
- R-parity violating SUSY*
- Extra dimensions
- ν Mass from QCD cond. (Davoudias, Everett (2006))
- LFV (Isidori, Paradisi (2006))

New $\pi^+ \rightarrow e^+ \nu$ Experiments

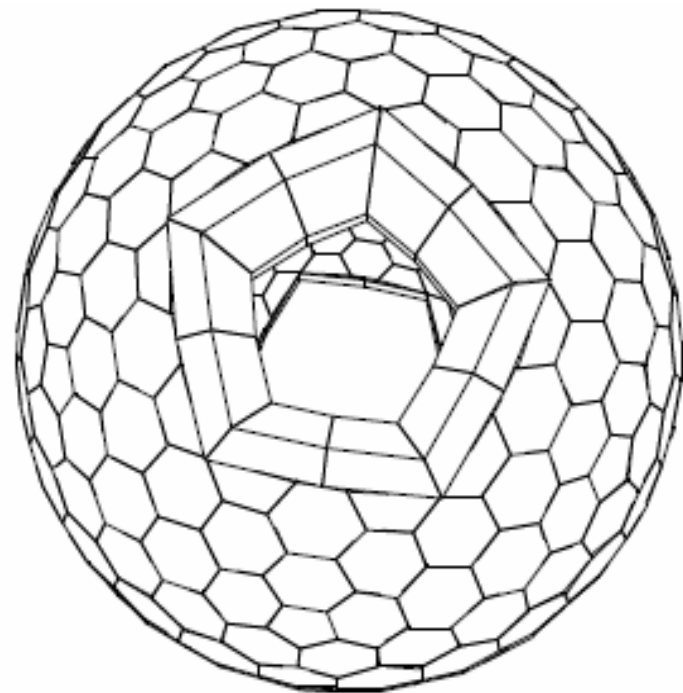
Precision Goals for $R_{e/\mu}^{\text{exp}\pi} : < 0.1\%$

TRIUMF PIENU



ASU, BNL, Osaka, TRIUMF, UBC, VPI

PSI PIBETA Spectrometer

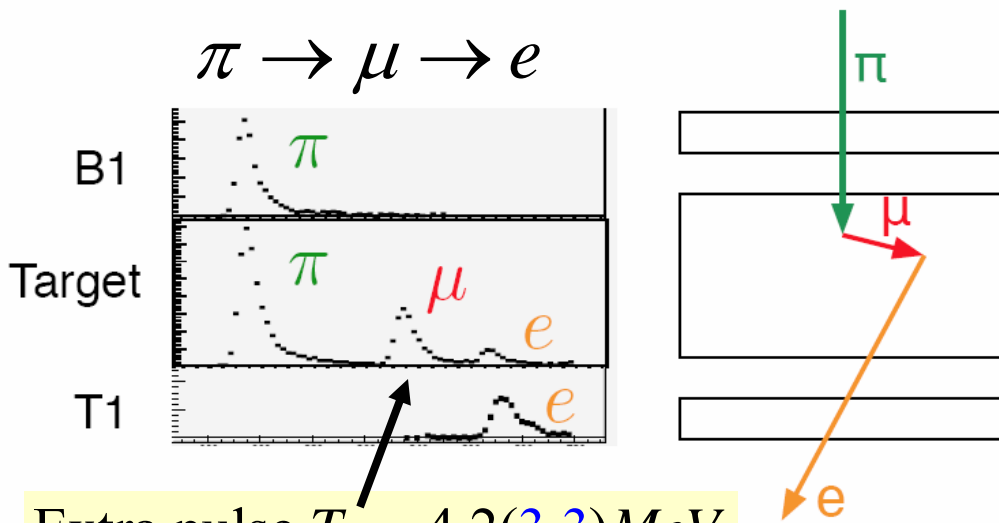
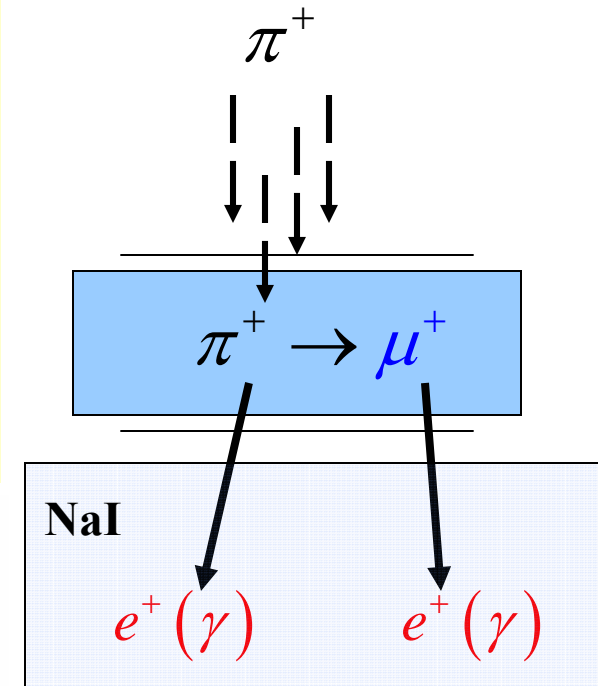


INS (Pol.), IHEP, JINR,
PSI, RBI, Virginia, Zurich



Experiment Concepts

Low Momentum π Beam at $p=75$ MeV/c.
 π s lose energy and stop in a target of plastic scintillator. Scintillation detectors viewed by photo-multiplier tubes and all signals are digitized at 500 MHz.



Extra pulse $T_\mu = 4.2(3.3)MeV$
for $\pi \rightarrow \mu \rightarrow e$ only.

$$\tau_\pi = 26ns, \tau_\mu = 2200ns$$

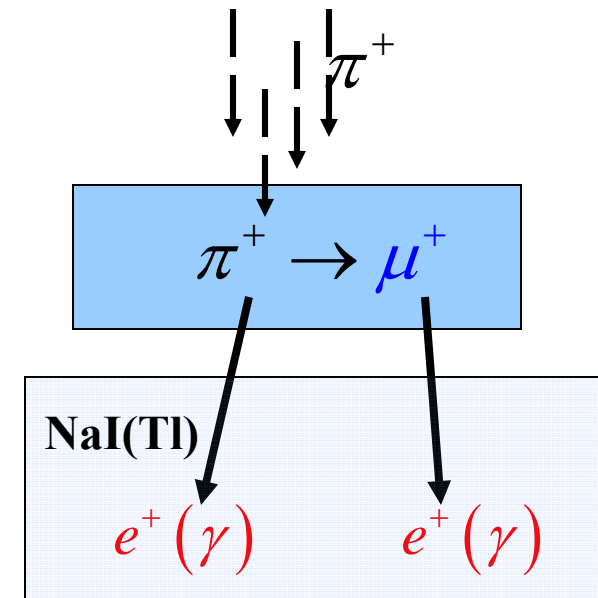
Measure positron energies in a NaI(Tl) crystal spectrometer (no magnetic field!):

$$\left[\pi^+ \rightarrow e^+ \nu \right] \quad P_e = 70 \text{ MeV} / c$$

$$\left[\pi^+ \rightarrow \mu^+ \nu \right] \quad P_\mu = 30 \text{ MeV} / c$$

$$T_\mu = 4.2 \text{ MeV}, \quad R_\mu = 1.4 \text{ mm}$$

$$\left[\mu \rightarrow e^+ \nu \bar{\nu} \right] \quad P_e = 0 - 53 \text{ MeV}$$

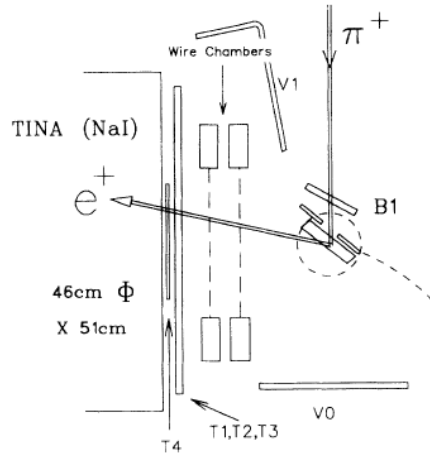


Electrons have fairly uniform interactions over the range P[1-70 MeV]:

Systematic effects cancel (to 1st order) in the ratio $\frac{\Gamma(\pi \rightarrow e)}{\Gamma(\pi \rightarrow \mu \rightarrow e)}$

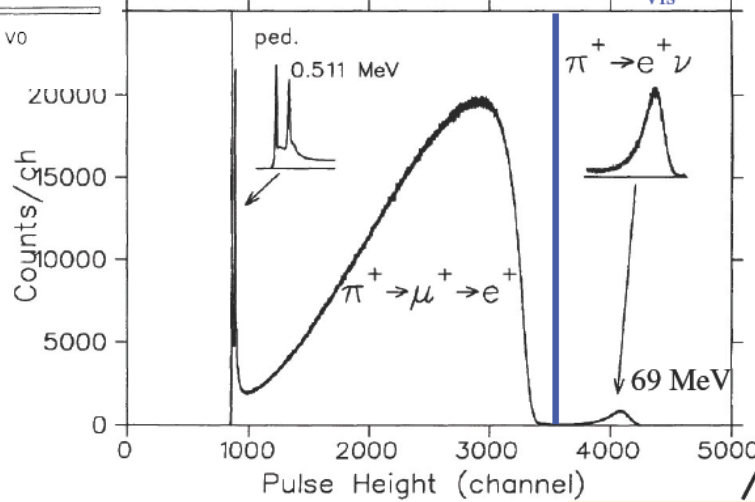
e.g. solid angle, Multiple Coulomb Scattering, $\frac{dE}{dx}$, annihilation, bremsstrahlung, timing.

N.B.: When aiming for high precision: must rely on measurements for corrections rather than simulations whenever possible!



Energy and Time spectra

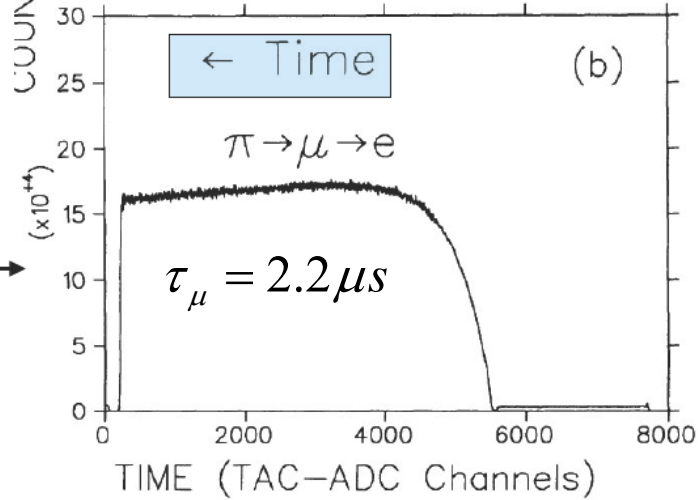
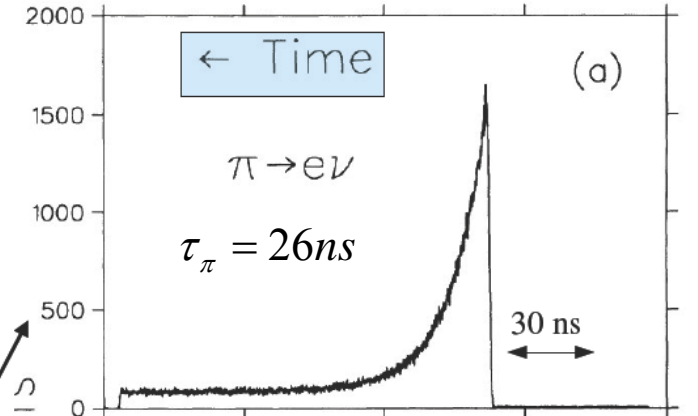
Separate events by Energy: ($E_{vis} \sim 52 \text{ MeV}$)



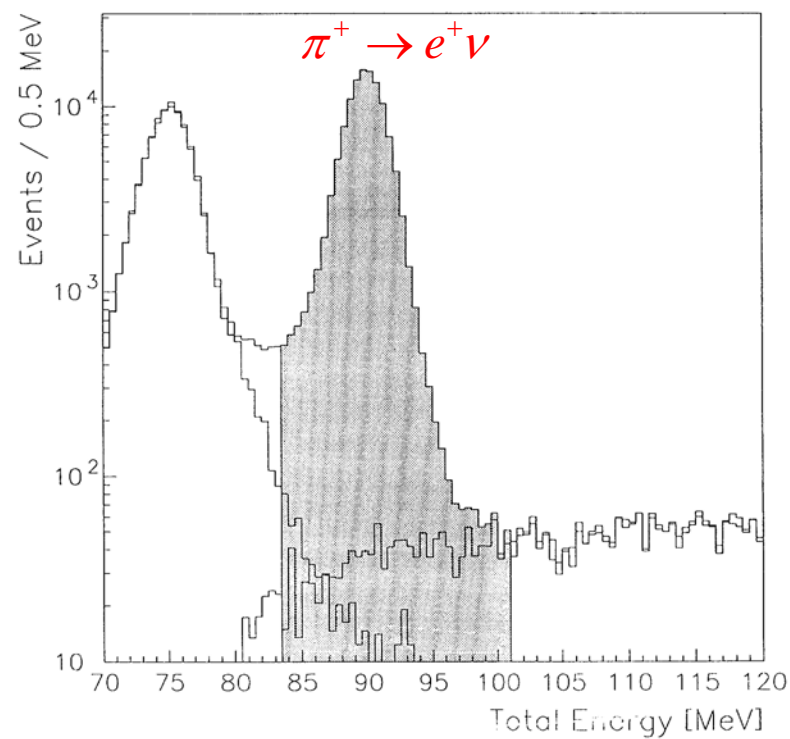
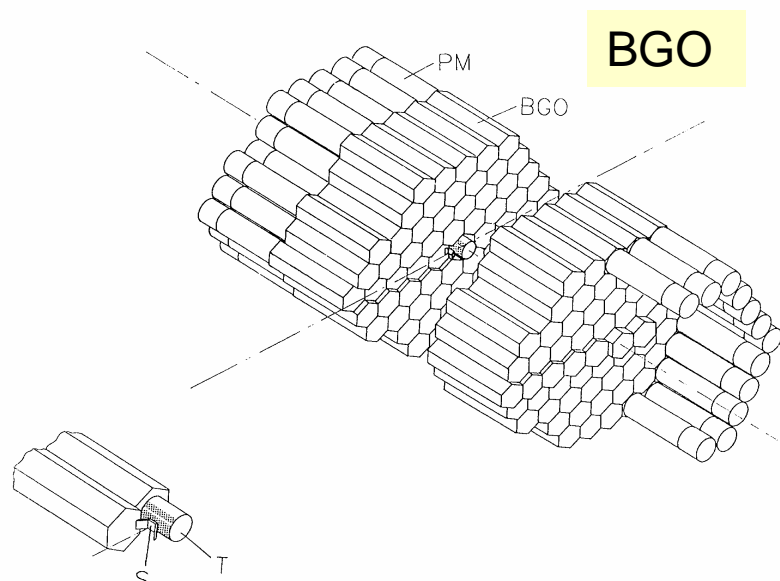
$\pi-\mu-e$ region

$\pi \rightarrow e \nu$

Fit both spectra simultaneously and obtain the ratio.



Previous PSI experiment: C. Czapek et al. 1993



Energy resolution 1.7% at 90 MeV

Total Energy (including target)

Previous PSI experiment: C. Czapek et al. 1993

TABLE I. Main corrections and systematic errors of our final result for the branching ratio for the rare decay $\pi \rightarrow e\nu(\gamma)$.

Process	Correction (%)	Error (%)
Electromagnetic losses	+1.64	0.09
Photonuclear reactions	+0.95	0.19
$\pi \rightarrow e\nu\gamma$ events with $E_{\text{total}} > 101$ MeV	+0.04	0.02
Uncertainty of the energy calibration	0.0	0.08
$\pi \rightarrow e\nu$ self-veto in anticounter	+0.03	0.02
Time measurement difference for e and μ	-0.08	0.03
Pulse-shape difference for e and μ	0.0	0.03
Efficiency of e^+ detection in target	+0.15	0.01
Subtraction of radiative μ decay background	-0.45	0.17
Subtraction of pion reaction background	-1.13	0.06



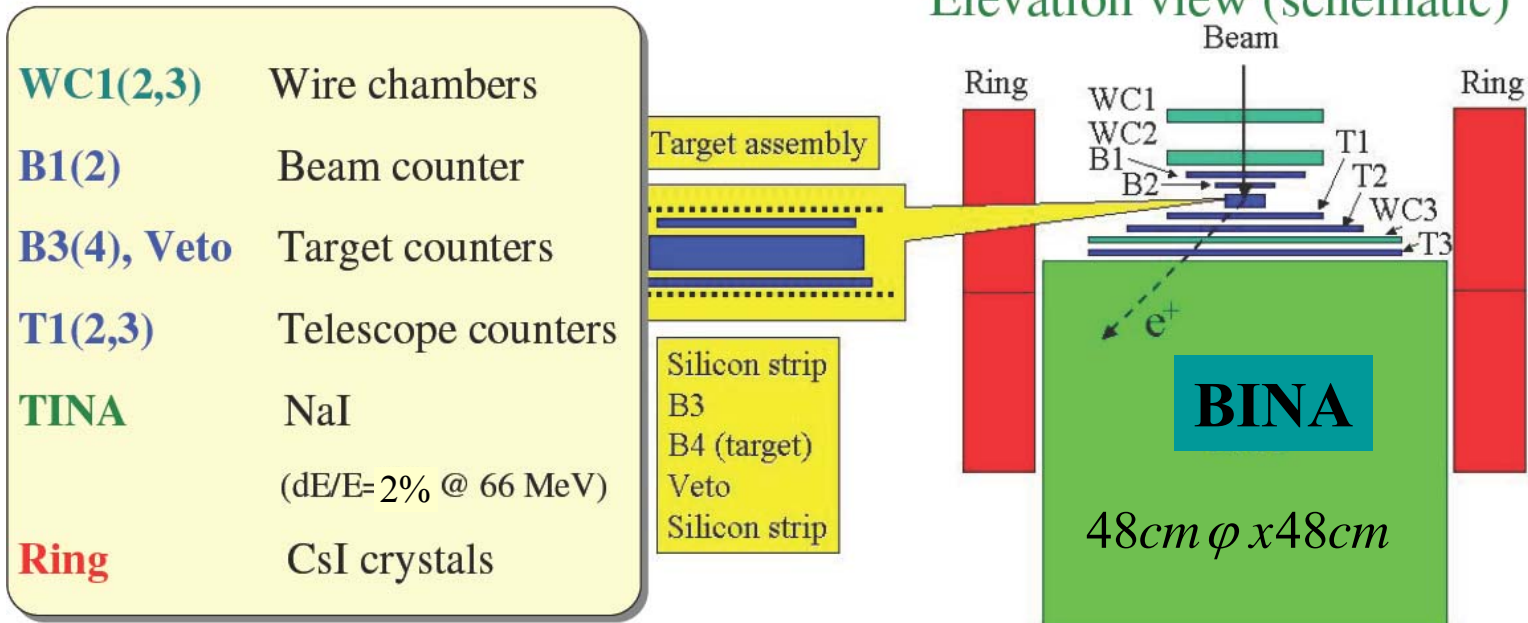
**M. Aoki, M. Blecher, D. Bryman, J. Comfort,
P. Gumplinger, S. Kettell, T. Krupovnickas,
Y. Kuno, L. Kurchaninov, L. Littenberg, W.
Marciano, G. Marshall, T. Numao, A. Olin,
R. Poutissou, M. Ramsey-Musolf, F. Retiere,
A. Sher, V. Selivanov, B. Walker, K. Yamada**

Canada-Japan-Russia-US

***Arizona State University, BNL, Caltech,
Kurchantov Institute, Osaka University,
TRIUMF, University of BC, Virginia
Polytechnic Institute and State University***

TRIUMF PIENU Experiment

Precision goal: $<0.05\%$



Solid angle: 25% (2.9%)

π^+ rate: $\sim 70\text{kHz}$ (100kHz)

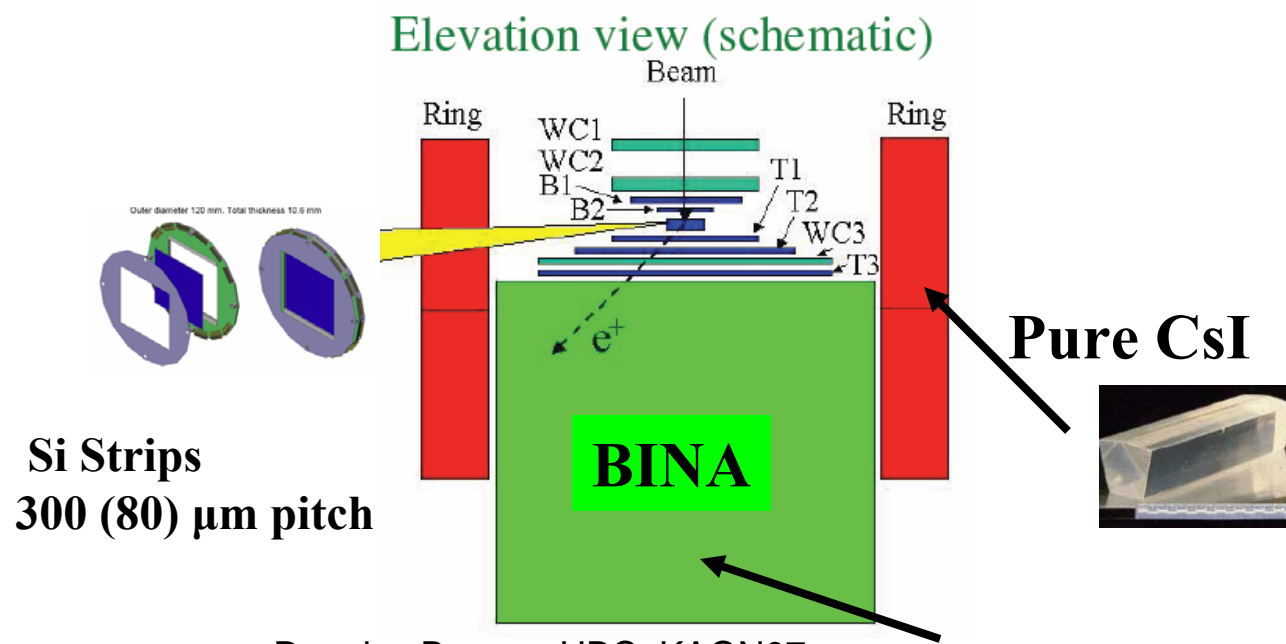
Tina rate: $\sim 40\text{kHz}$ (30kHz)

Trigger rate: $\sim 1\text{kHz}$

Statistics: $\sim 5 \times 10^6 \pi \rightarrow e\nu$ ($\times 30$ E248)

Equipment

- **Single crystal NaI(Tl) detector (BNL)**
Energy resolution <2% (RMS) at 70 MeV
- **E949 Pure CsI crystal collar**
- **500 MHz digitizers**
- **Silicon strip and drift chamber tracking**



Douglas Bryman UBC KAON07

48 cm dia. x 48 cm ~19 X0²³

Tail correction

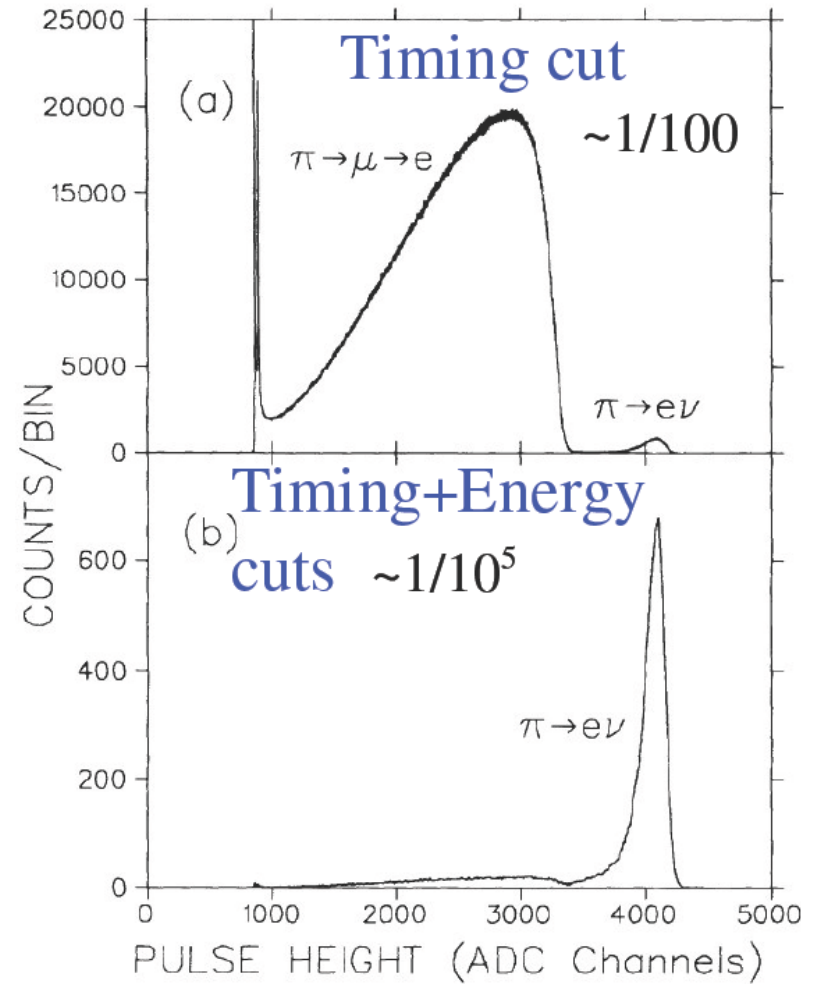
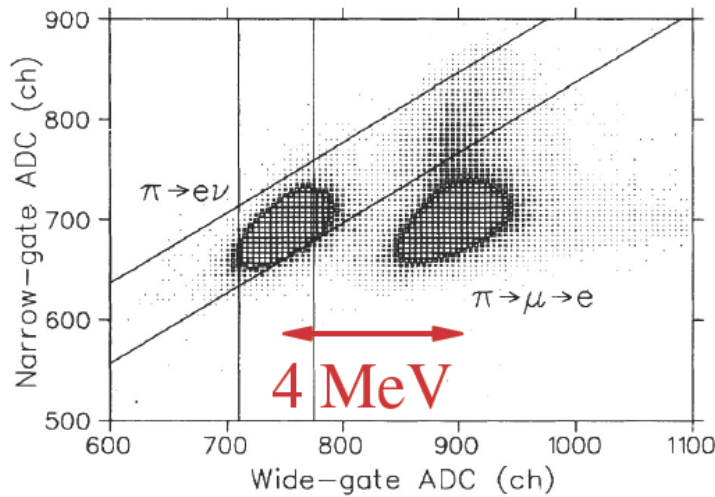
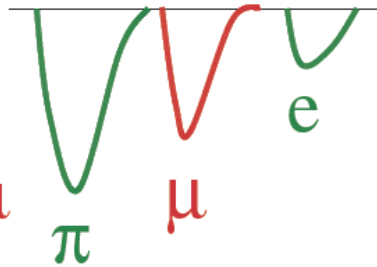
(the main source of systematics)

$\pi \rightarrow e \nu$

$\Gamma \pi + \Delta E e$

$\pi \rightarrow \mu \rightarrow e$

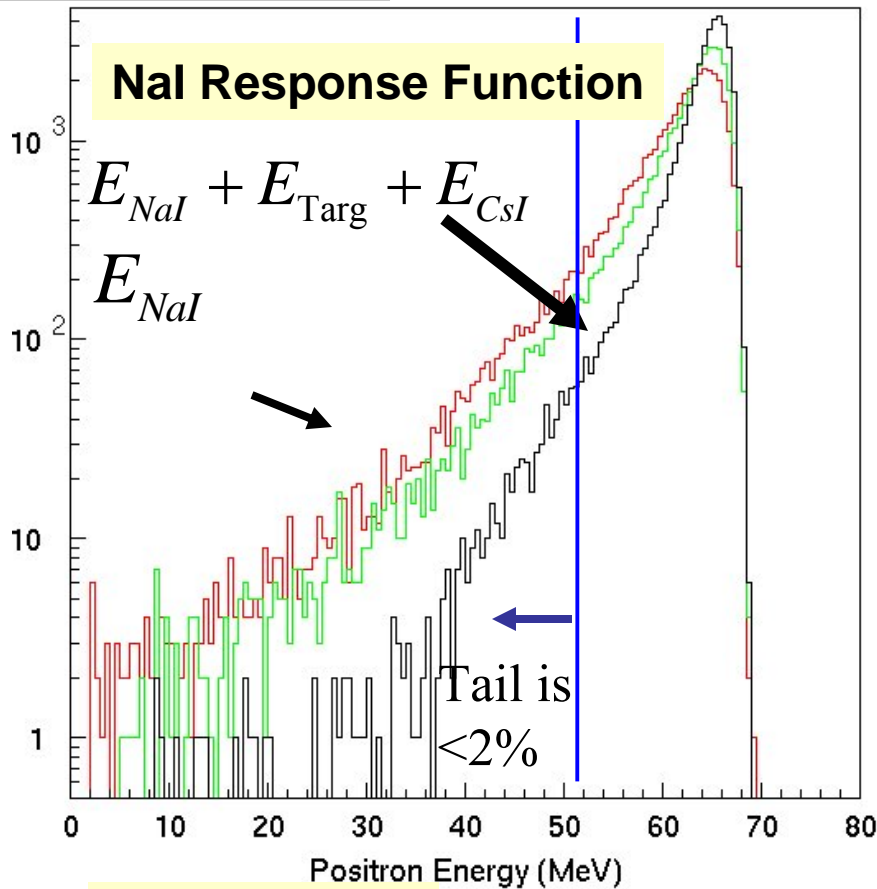
$\Gamma \pi + \Delta E e + E \mu$



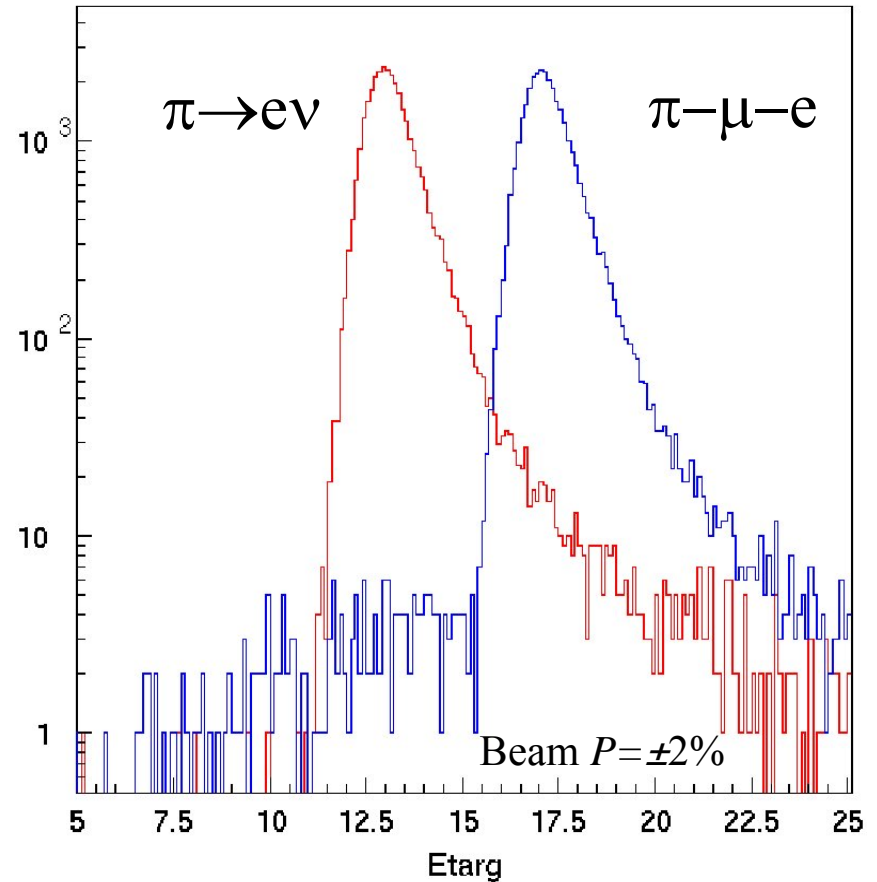
Resolution and NaI Tail

Simulations for PIENU Experiment

$\pi \rightarrow e\nu$ events



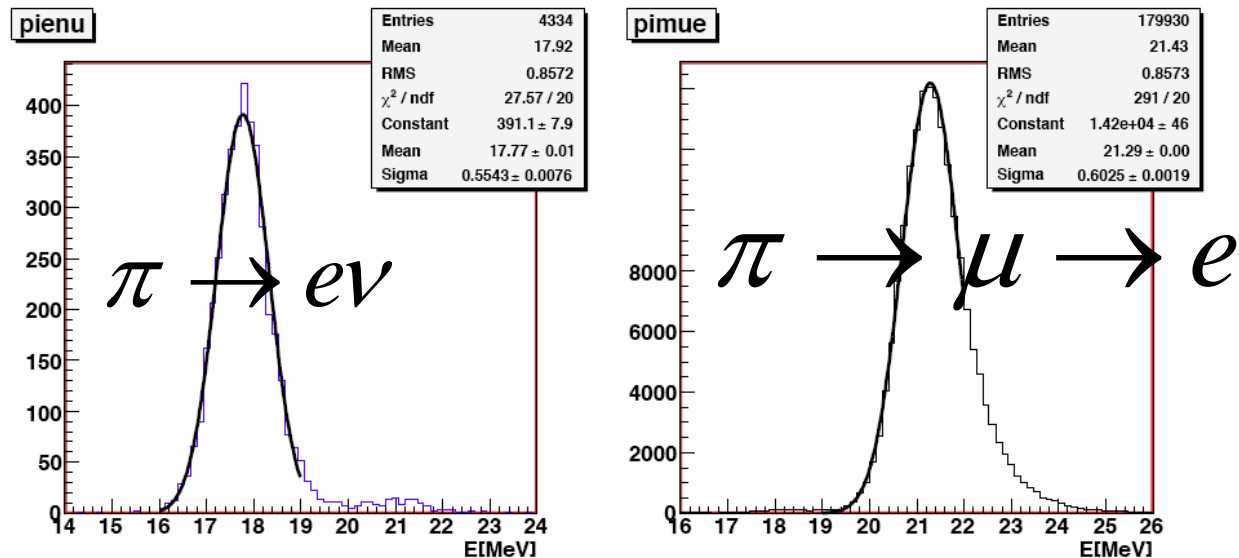
NaI(Tl) Energy



Target energy

Beam Test Data

total energy deposit in
the target




Good separation in the target $dE/E \sim 3\%$

Expected Uncertainties


Largest systematics come from:

Low energy tail ($\pi \rightarrow e\nu$)
0.03%


Britton et al. : 0.25% Uncertainty of the correction - limited by statistics & contamination by in-flight pion decays

 PI E NU Better dE/dx in target (x2) and smaller statistical uncertainty (x5):

Energy dependent Acceptance difference 0.03%

 PI E NU Larger solid angle x5, geometry:

Uncertainties Summary

Sources	Britton et al. 1993	 PI E NU
Statistical error	0.0028	0.0005
Low energy tail ($\pi \rightarrow e\nu$)	0.0025	0.0003
Acceptance differences	0.0011	0.0003
Pion lifetime	0.0009	0.0002
Others (time calibration, etc.)	0.0011	0.0003
Expected systematic error	0.0031	0.0006

PIENU Experiment Plan

- 2006/7: Beam Tests
- 2007: Assembly
- 2008-2009 Data runs
- 2008-10 Analysis/publications

Students, Postdocs: Interested? See me later!

Detector build-up

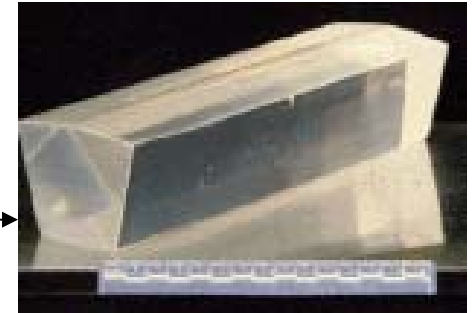
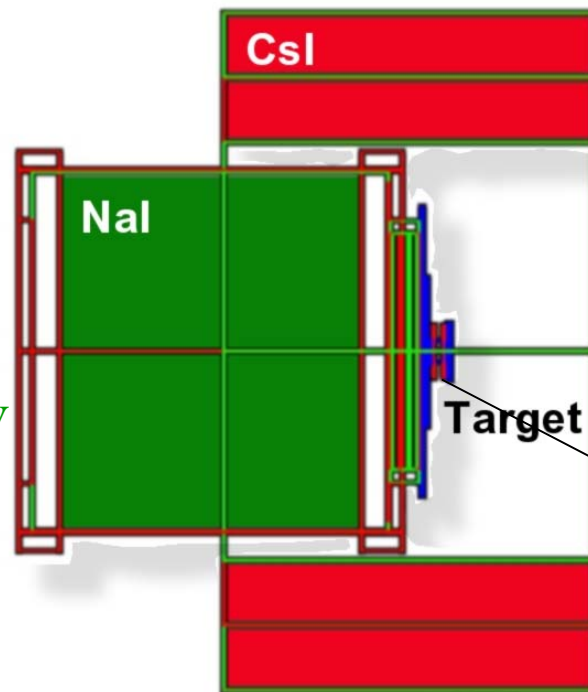
Brookhaven NaI crystal
(BINA)

Radius=24 cm

Length = 48 cm(19 X_0)

Energy resolution:

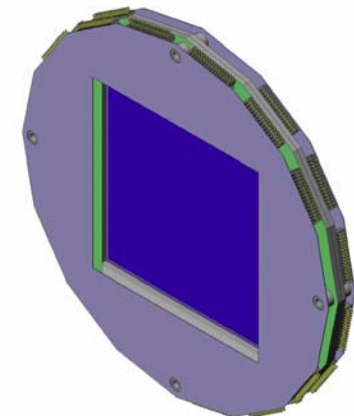
~<2% (FWHM) at 70 MeV



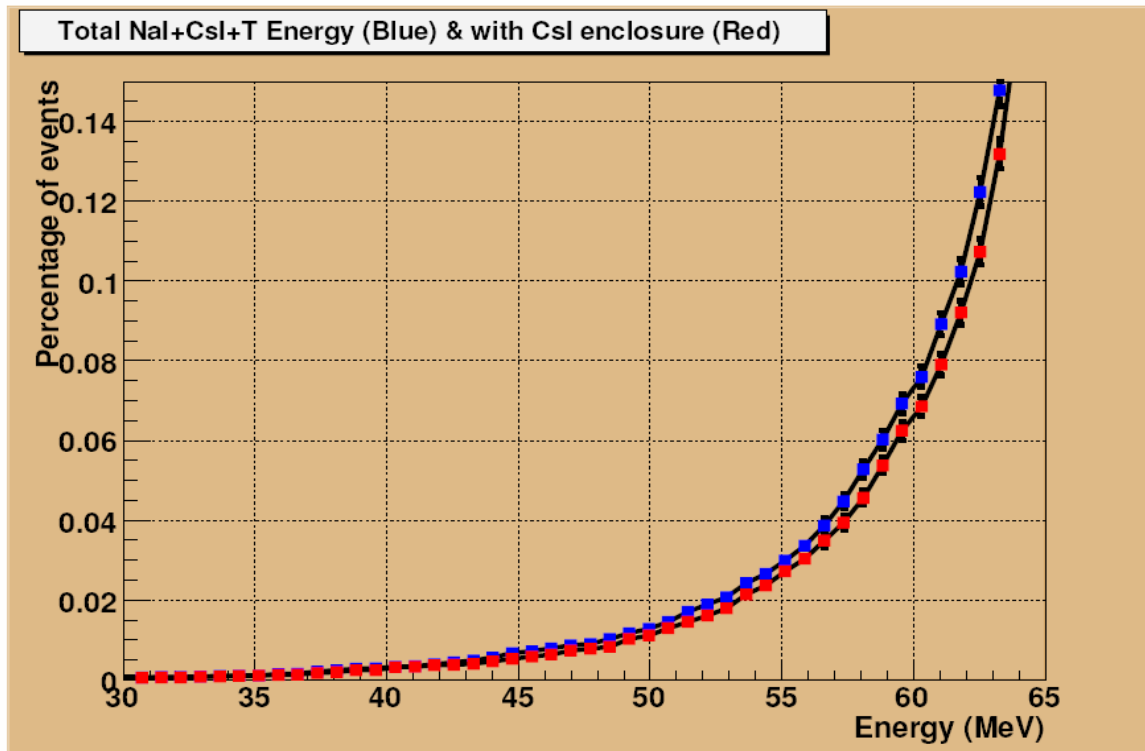
Pure CsI crystals

π Beam

Si Strips
300 (80) μm pitch



To reach 0.05% precision, everything must be studied/known to 0.01%:
GEANT3 & 4 MC Studies Example:
Dead material and Gaps between crystals



**Support material
in gaps between
crystals: <10%
effect, known to
<1% precision.**

Beam Test data: KEK 500 MHz Digitizers

Pulse fitting

Fitting as a single pulse

Fitting function

2 free parameters A, T_1

$$V = A1F(t+T1)$$

for $B1, B2, T1, T2$

Fitting as a double pulse

Fitting function

4 free parameters A_i, T_i $i=1,2$

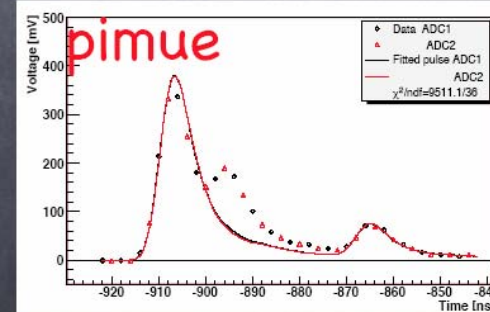
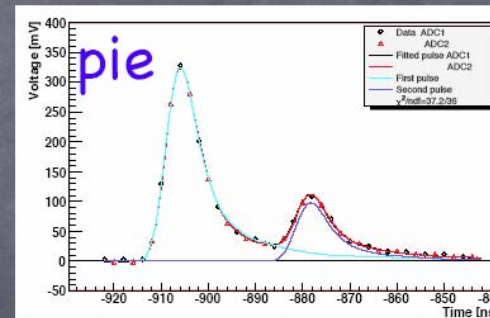
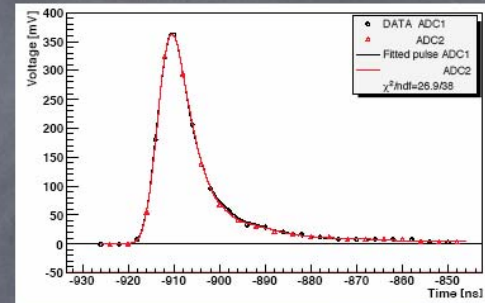
$$V = A1F(t+T1) + A2F(t+T2)$$

for Target

pie \rightarrow correct assumption

pimue \rightarrow incorrect assumption

χ^2 and parameters obtained from fitting is useful for identification of the decay-mode



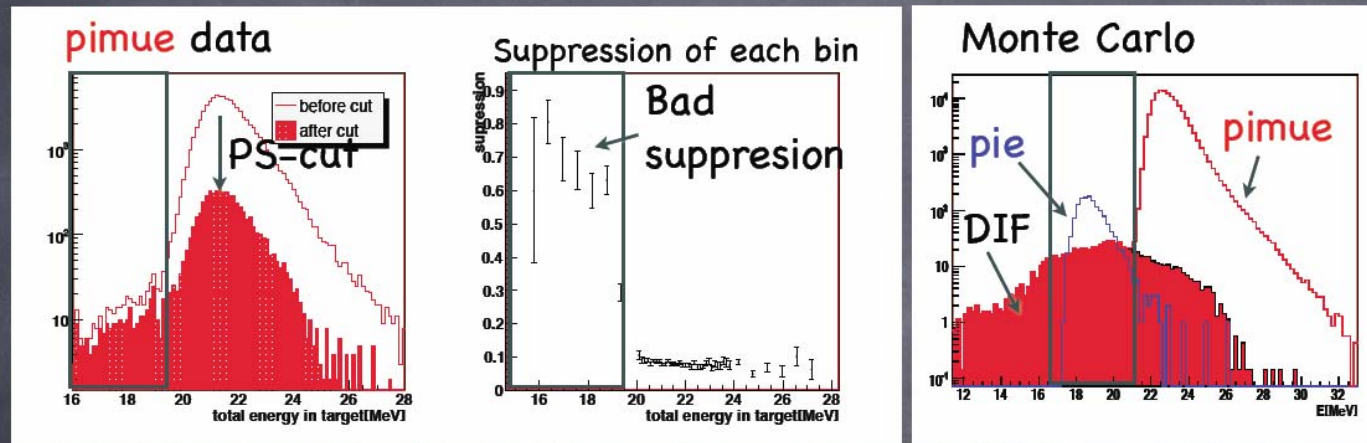
Tail Correction Background source: π Decays-in-Flight

Correlation between E_{total} and PS-cut

Horizontal axis: E_{total} In Target

Pulse Shape

Beam Test data:

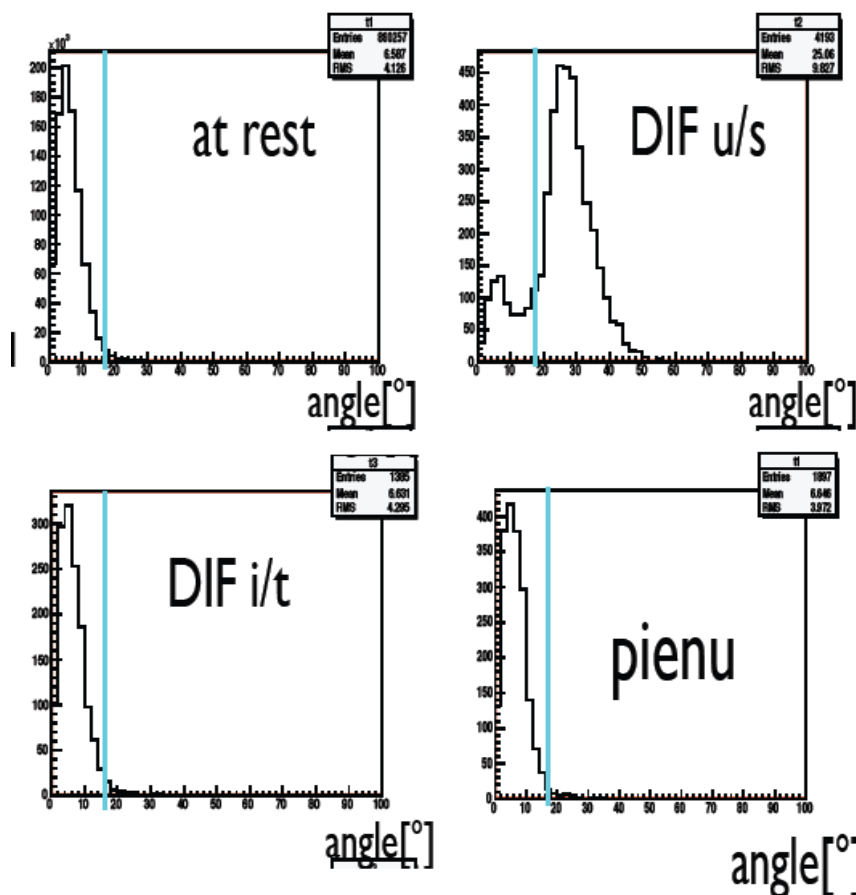
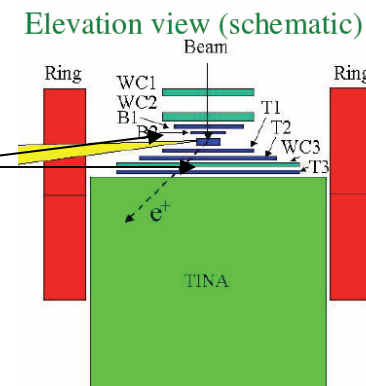


$E_{\text{total}} < 20 \text{ MeV}$: Suppression of PS-cut is weak

DIF is dominant

Si Strip and WC tracking suppress decays-in-flight

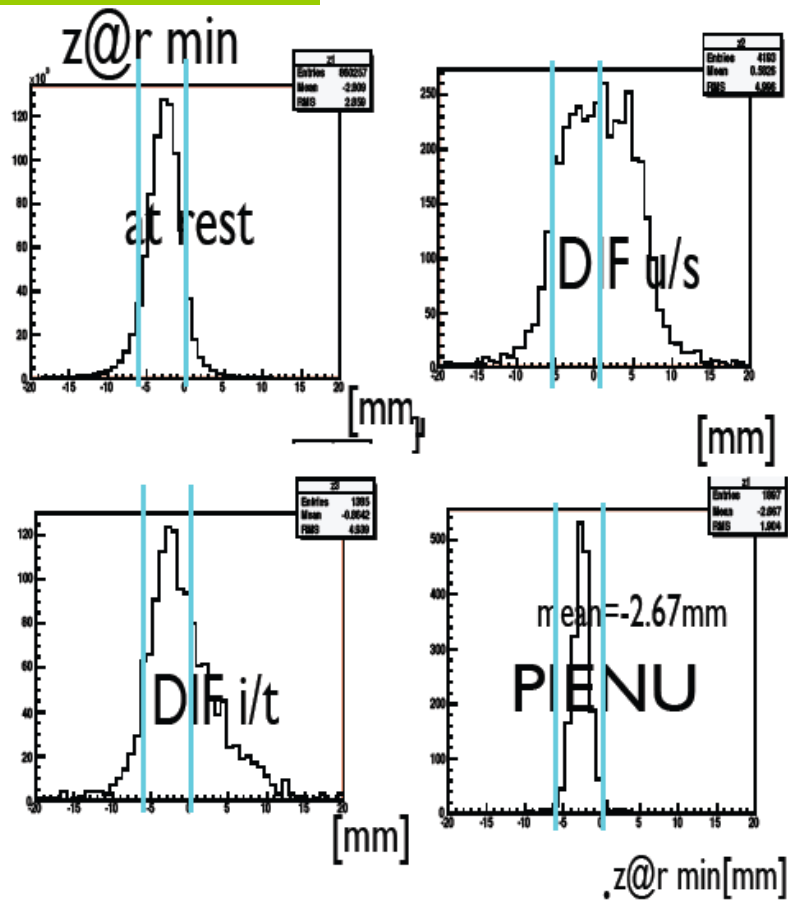
MC simulations



Measuring the angle between the incident beam pion (using Wire Chambers) and the charged particle entering the target (using Silicon Strip detectors) reduces decays-in-flight
(Factor ~8)

SS and WC tracking suppress decays-in-flight

MC simulations



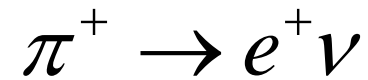
Tracking to determine the stop/decay vertex suppresses decays-in-flight further.

Total suppression factor ~ 30

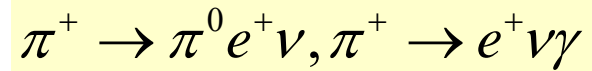
PEN at PSI

Precision Goal: 0.05%

PI Beta Spectrometer: 12 X0 pure CsI

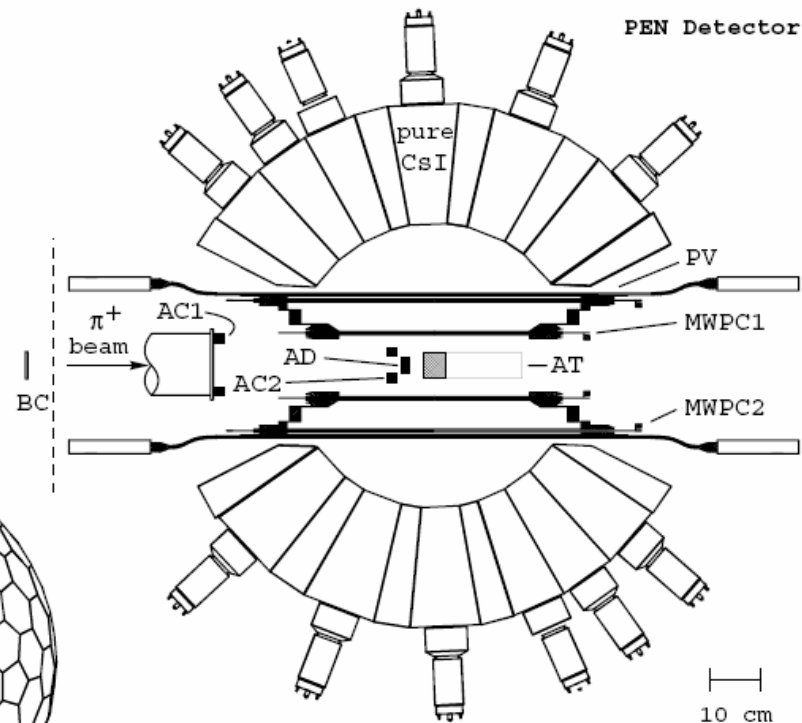
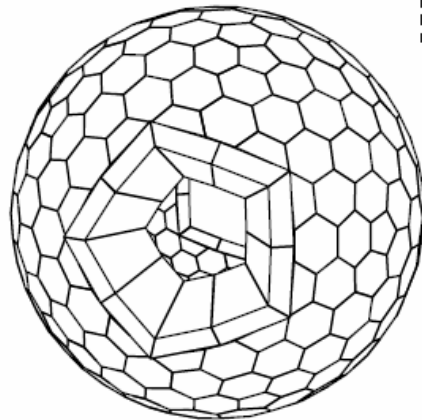


Previously measured



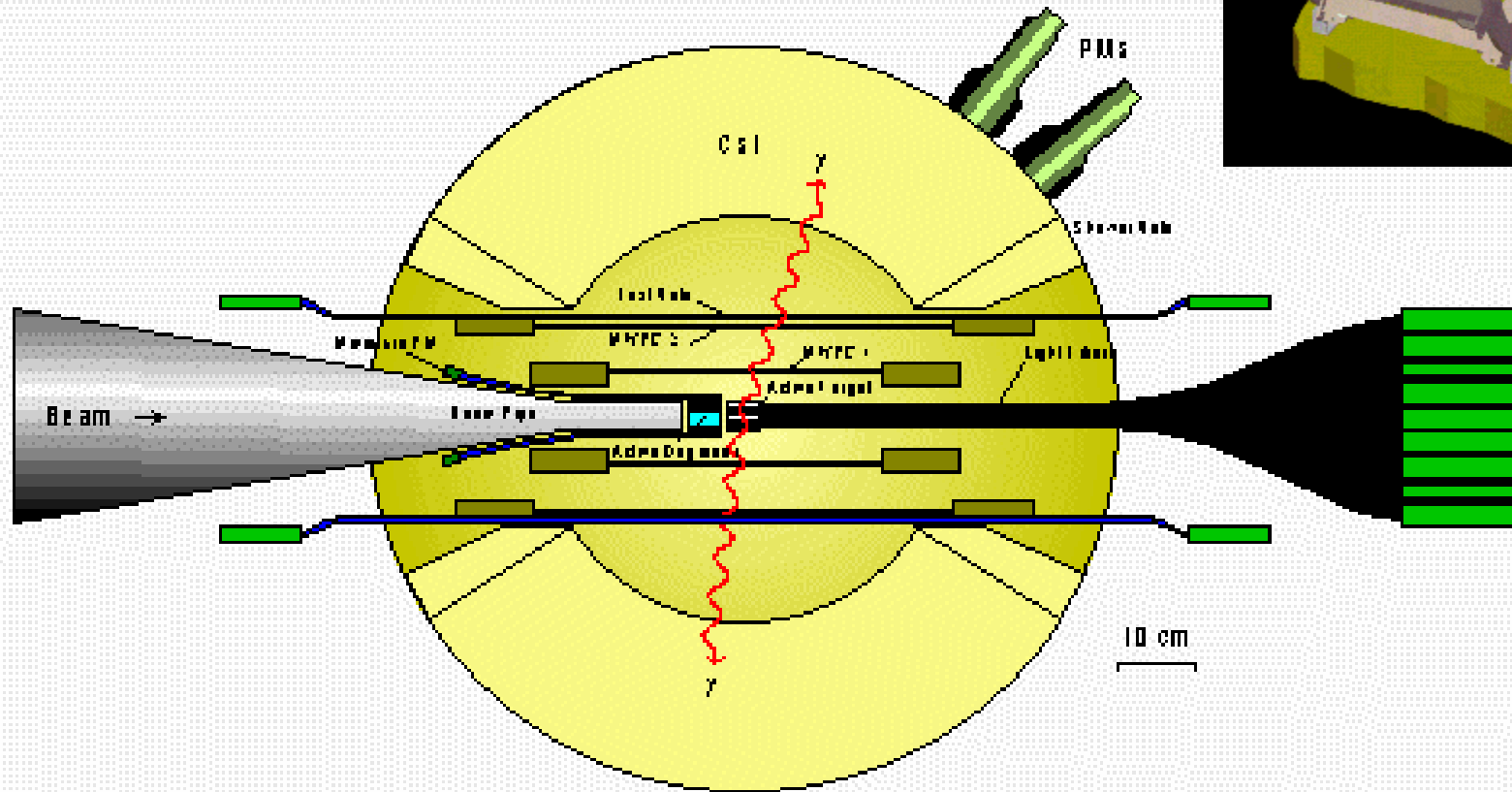
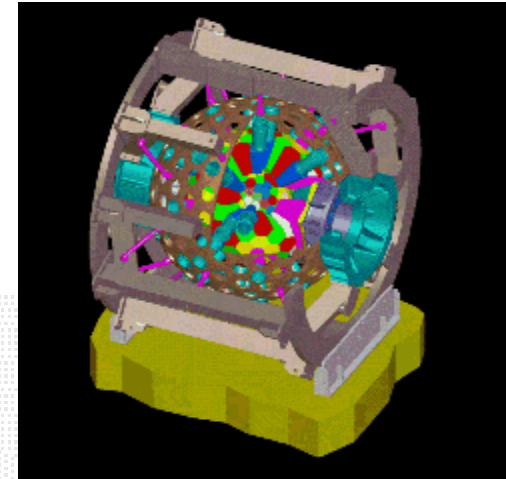
The PEN Experiment:

- stopped π^+ beam
- active target
- 240-det. CsI(pure) calorimeter
- central tracking
- digitized waveforms



Detector schematic cross section

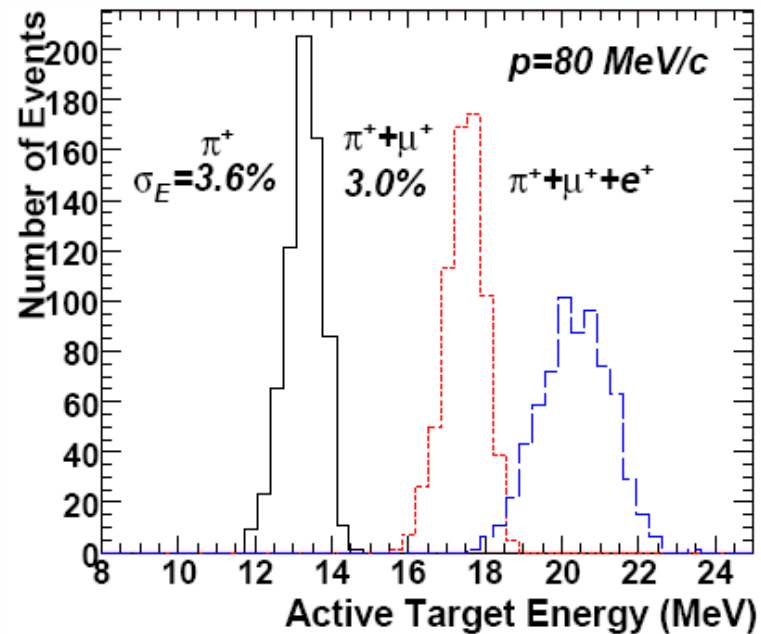
PSI π - β Target Arrangement



PEN Active Target
 detector energy resolution

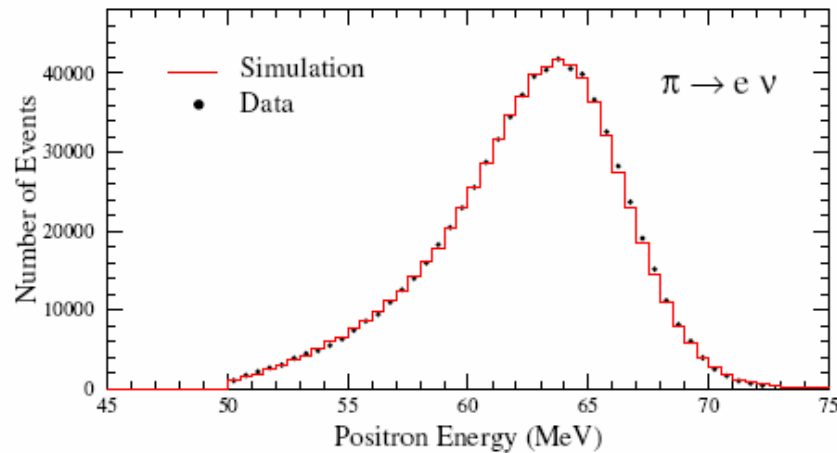
- stopped pion signal
- stopped pion with
 $\pi \rightarrow \mu\nu$
- stopped pion with
 $\pi \rightarrow \mu \rightarrow e$

[From 2006 PEN test run]



Calorimeter energy
 resolution for $\pi^+ \rightarrow e^+\nu$
 after subtraction of late
 decay events.

[From 2004 PIBETA run]



12.8% FWHM at 66 MeV

Summary

High precision studies of the $\frac{\pi / K \rightarrow e\nu}{\pi / K \rightarrow \mu\nu}$ branching ratios offer unique, clean access to new short distance effects and high mass scales that are complementary to studies at the LHC.

New Physics Sensitivity

- $\frac{\pi \rightarrow e\nu}{\pi \rightarrow \mu\nu}$
- $\frac{K \rightarrow e\nu}{K \rightarrow \mu\nu}$



PSI-PEN

CERN NA48/3

KLOE

$$\frac{1}{M_H^2} \text{ with } M_H \leq 1000 \text{ TeV}$$