

Description of the full q_T spectrum of low Q Drell Yan production

IV Sardinian Workshop on Spin

Lorenzo Rossi

In collaboration with S. Camarda and G. Ferrera

June 12th

Short Recap

Short Recap

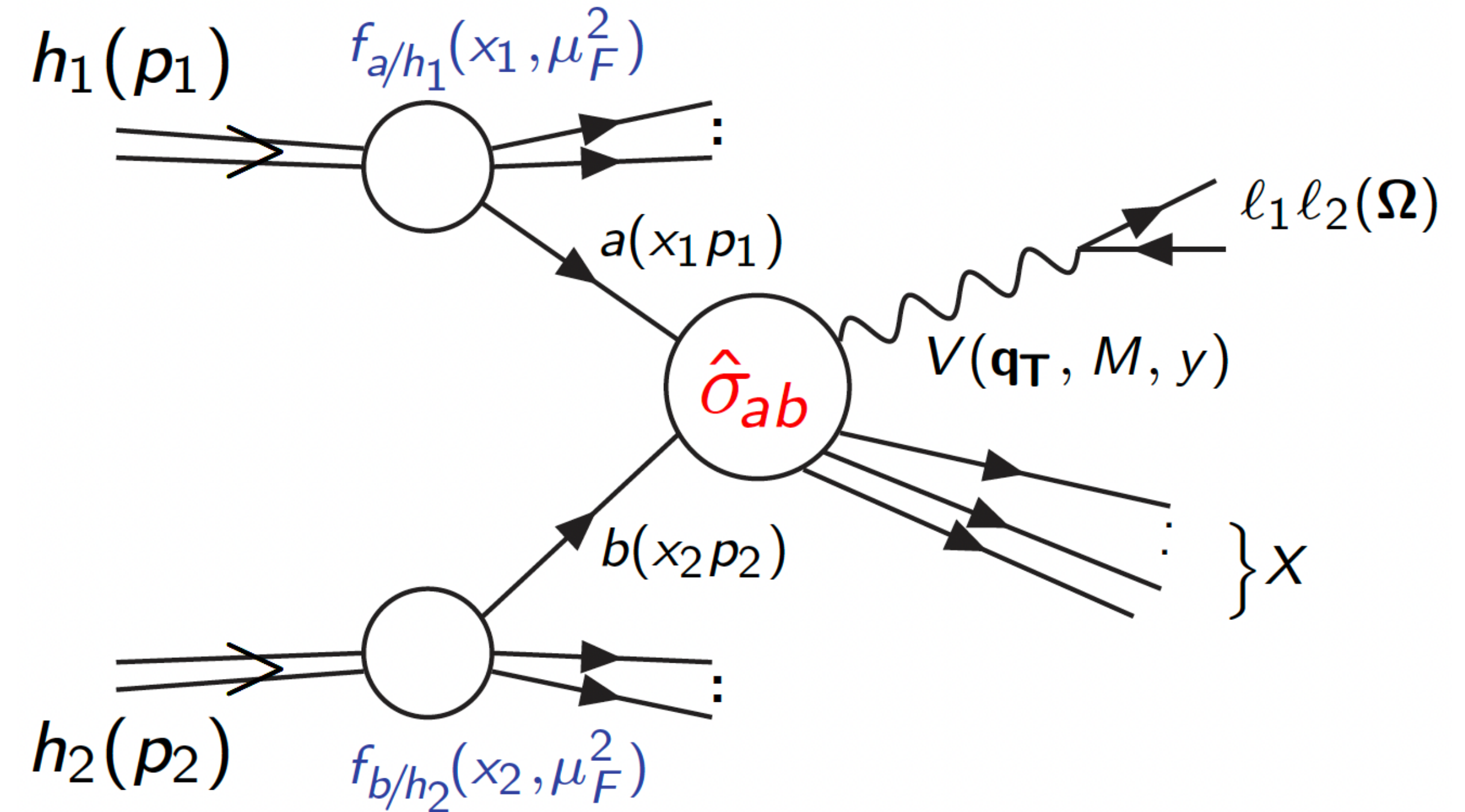
Drell Yan production

$$h_1(p_1) + h_2(p_2) \rightarrow V + X \rightarrow \ell_1 + \ell_2 + X$$

Short Recap

Drell Yan production

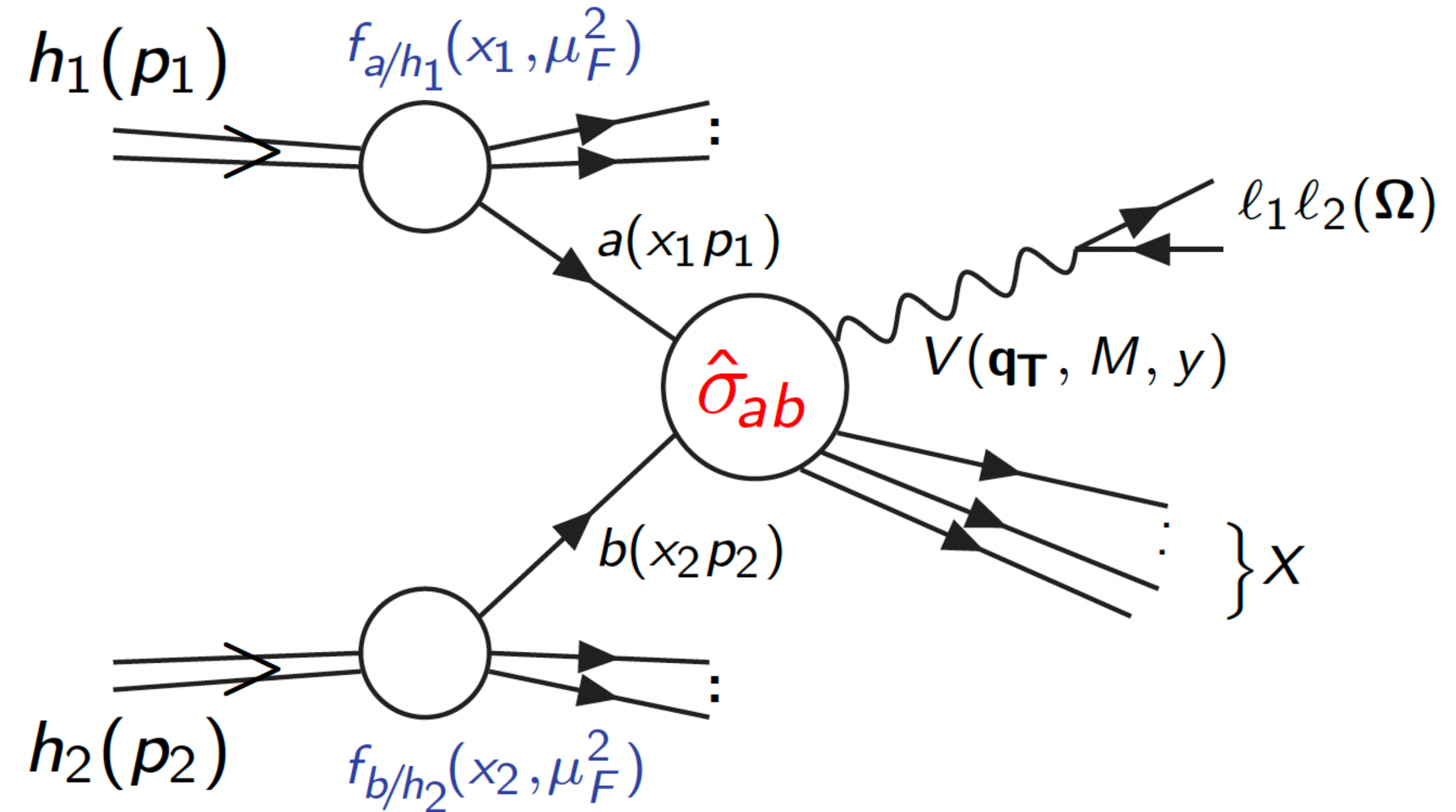
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Short Recap

Drell Yan production

$$h_1(p_1) + h_2(p_2) \rightarrow V + X \rightarrow \ell_1 + \ell_2 + X$$



$$\frac{d\sigma}{d^2\mathbf{q}_T dM^2 dy d\Omega} = \sum_{a,b} \int_0^1 dx_1 \int_0^1 dx_2 f_{a,h_1}(x_1, \mu_F^2) f_{b,h_2}(x_2, \mu_F^2) \frac{d\hat{\sigma}_{ab}}{d^2\mathbf{q}_T dM^2 d\hat{y} d\Omega}(\alpha_S(\mu_R^2), \mu_R^2, \mu_F^2)$$

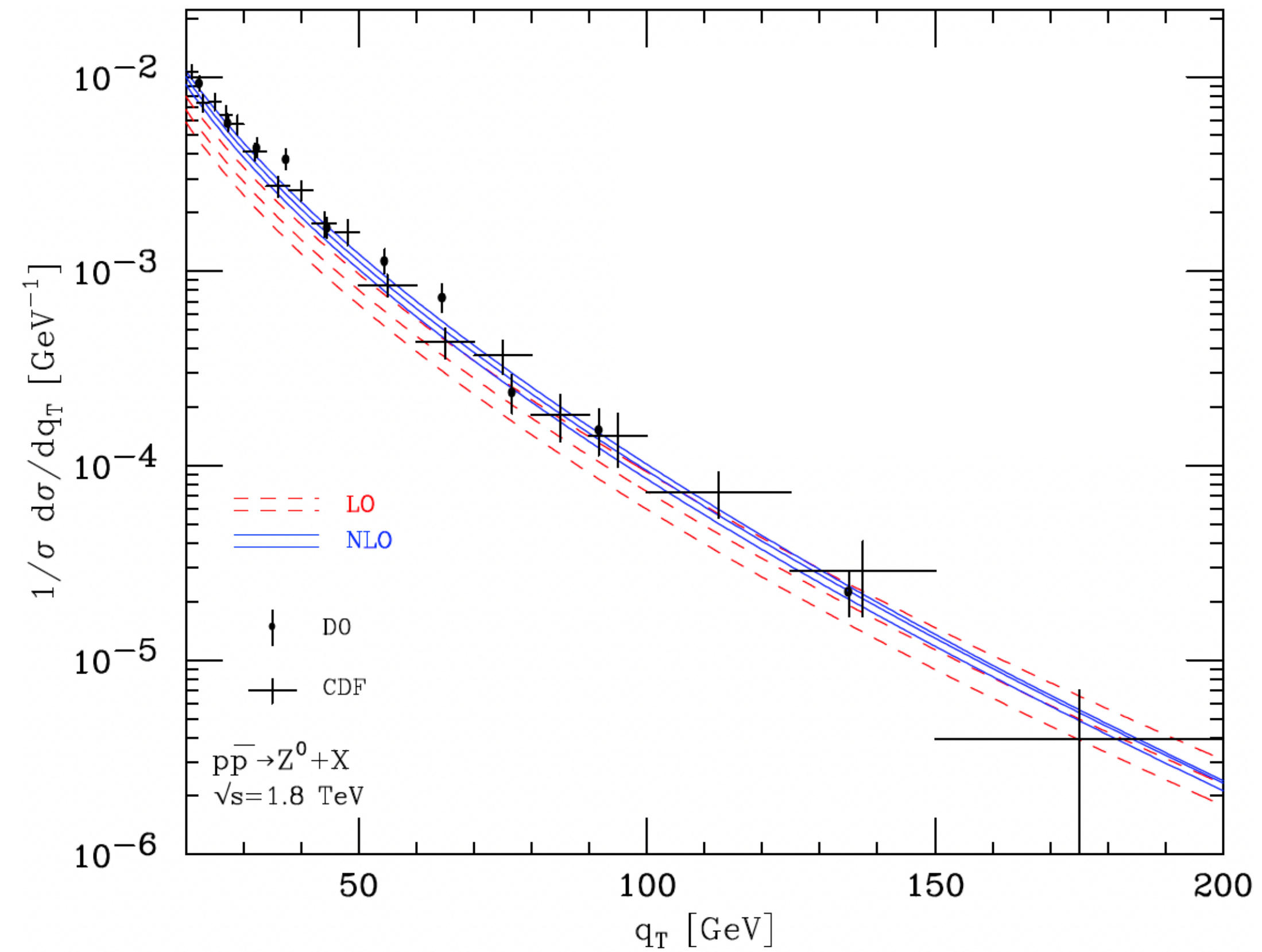
Short Recap

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Fixed order perturbative calculation only for $q_T \sim M$

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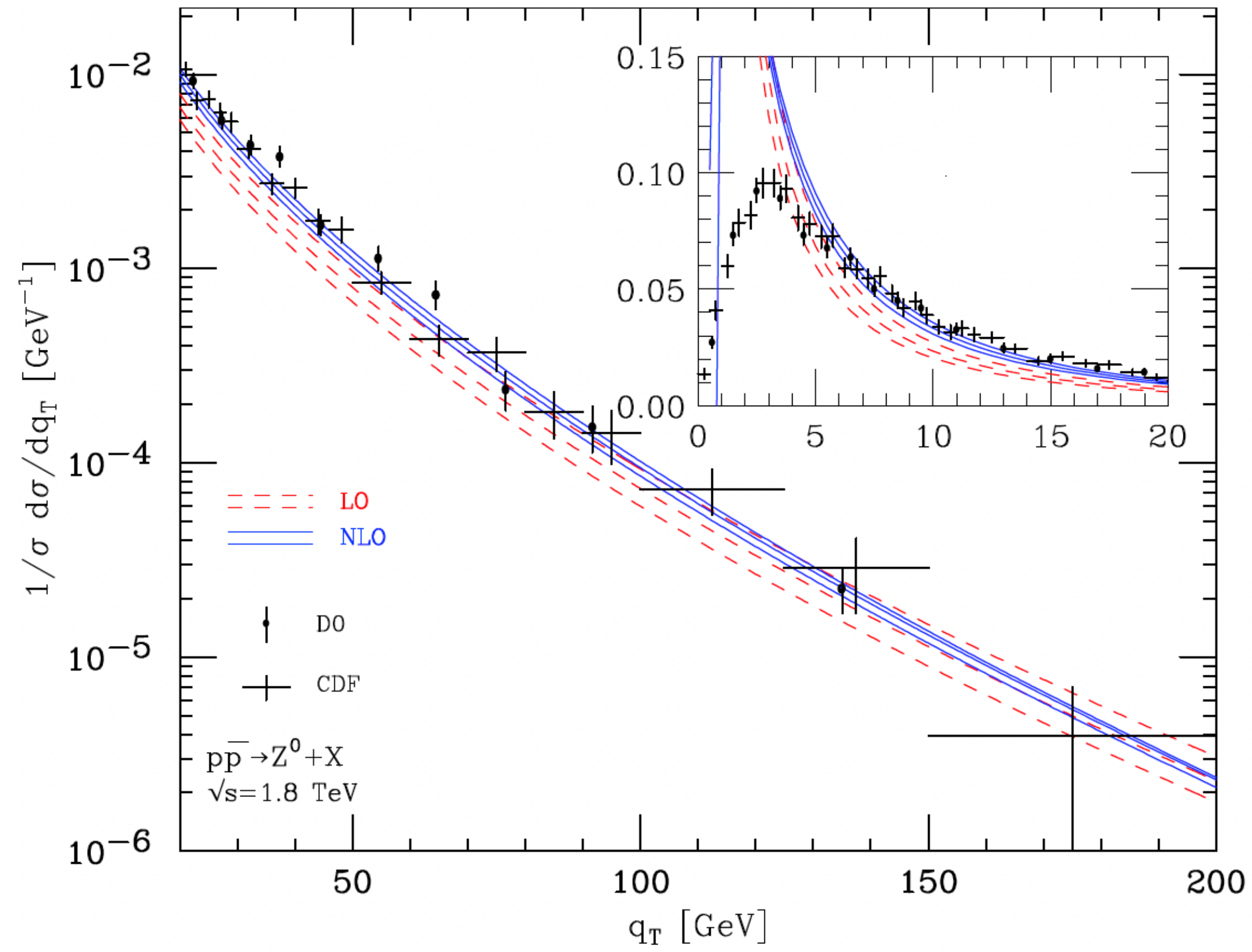
Fixed order perturbative calculation only for $q_T \sim M$



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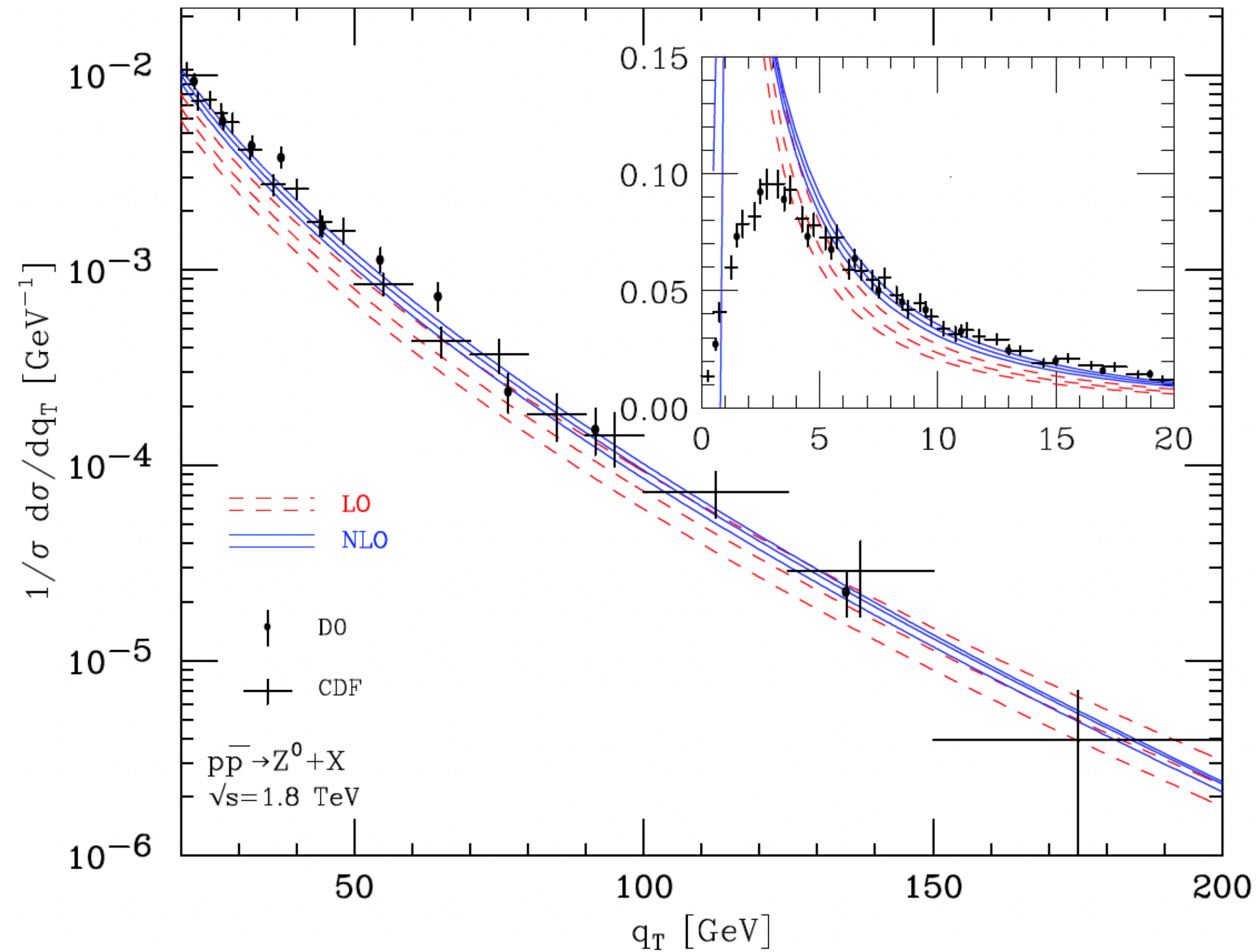
Fixed order perturbative calculation only for $q_T \sim M$

When $q_T \ll M$:



Short Recap

Fixed order perturbative calculation only for $q_T \sim M$



When $q_T \ll M$:

$$\int_0^{q_T^2} d\bar{q}_T^2 \frac{d\hat{\sigma}_{q\bar{q}}}{d\bar{q}_T^2} \sim 1 + \alpha_S [c_{12} L_{q_T}^2 + c_{11} L_{q_T} + \dots] \\ + \alpha_S^2 [c_{24} L_{q_T}^4 + \dots + c_{21} L_{q_T} + \dots] + \mathcal{O}(\alpha_S^3)$$

$$\text{whit } \alpha_S^n L_{q_T}^m = \alpha_S^n \log^m \left(\frac{M^2}{q_T^2} \right) \gg 1$$

q_T resummation in QCD

q_T resummation in QCD

$$\frac{d\hat{\sigma}}{d^2\mathbf{q}_T} = \frac{d\hat{\sigma}^{(\text{res})}}{d^2\mathbf{q}_T} + \frac{d\hat{\sigma}^{(\text{fin})}}{d^2\mathbf{q}_T}$$

q_T resummation in QCD

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In impact parameter space:

$$\frac{d\hat{\sigma}^{(\text{res})}}{d^2\mathbf{q}_T} = \frac{M^2}{\hat{s}} \int \frac{d^2\mathbf{b}_T}{4\pi} e^{i\mathbf{b}_T \cdot \mathbf{q}_T} W(b, M)$$

q_T resummation in QCD

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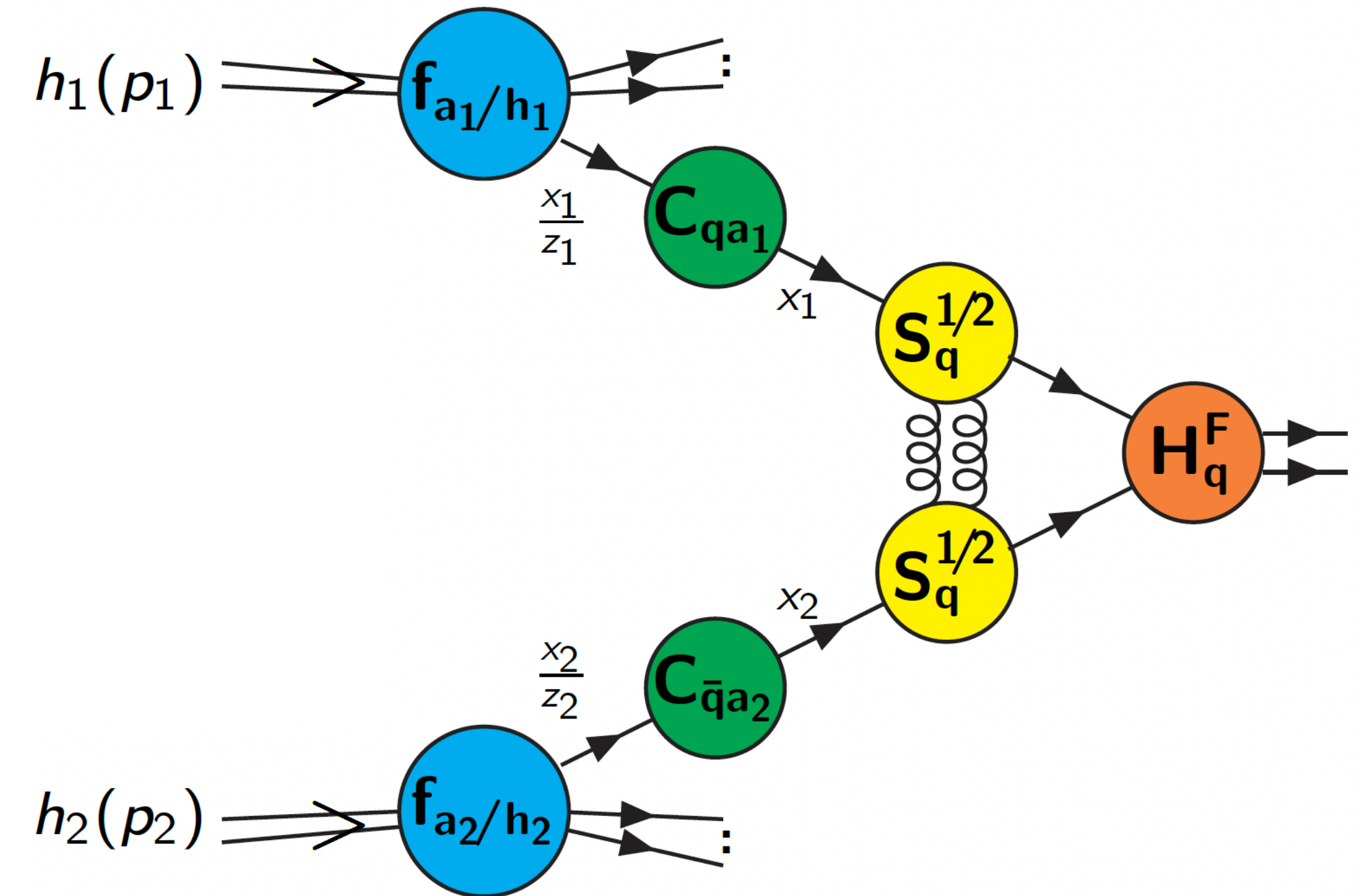
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In Mellin space:

$$W_N(b, M) = \hat{\sigma}^{(0)} H_N(\alpha_S) \times \exp\{G_N(\alpha_S, L)\}$$

Connection with CSS formalism

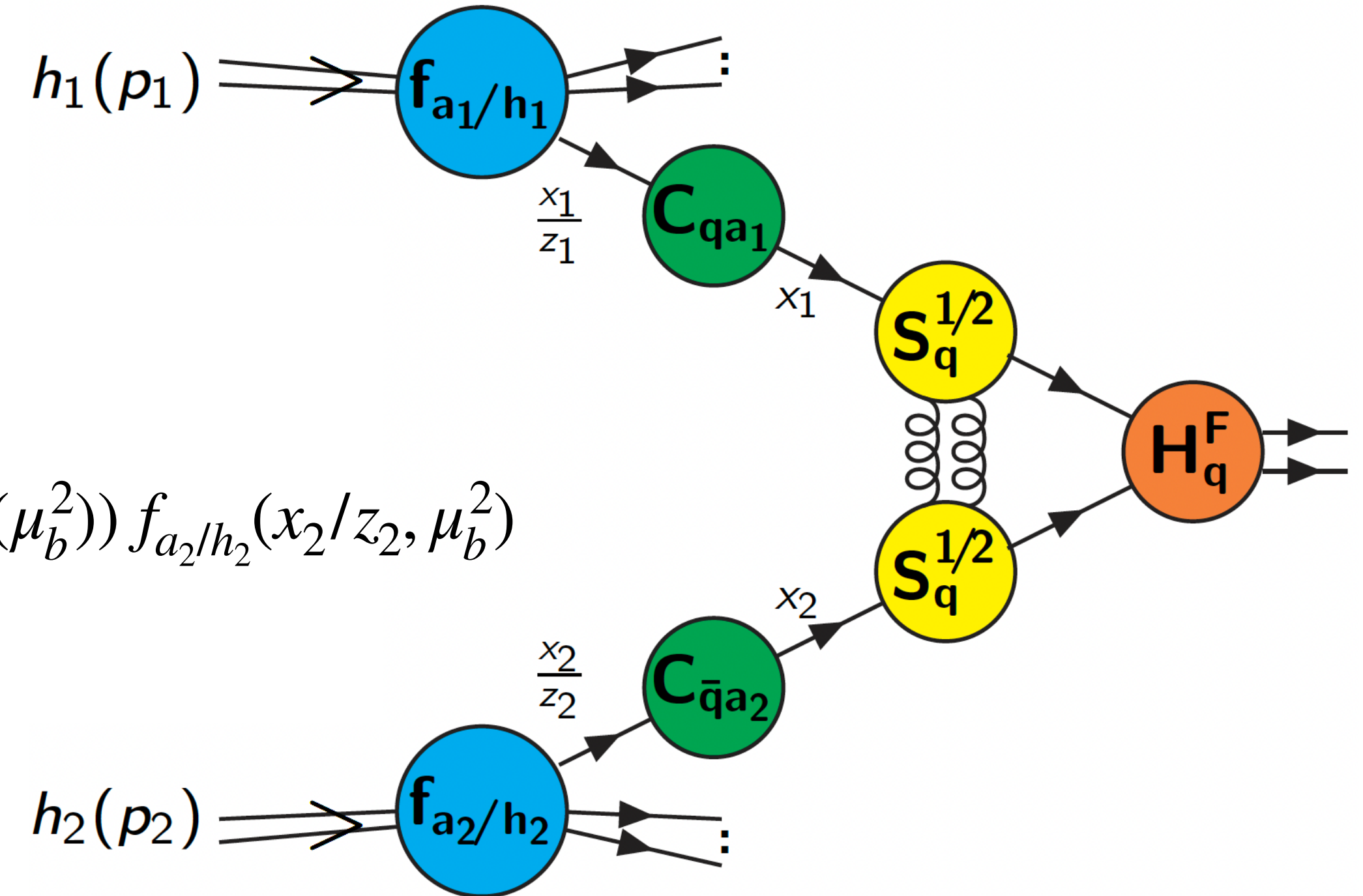
Connection with CSS formalism



Connection with CSS formalism

$$\frac{d\sigma_F^{(res)}}{dq_T^2} = \frac{M^2}{s} \sigma_{q\bar{q}}^{(0)} H_q^F(M^2) \sum_{a_1 a_2} \int \frac{d^2 \mathbf{b}_T}{2\pi} e^{i\mathbf{b}_T \cdot \mathbf{q}_T} S_q(M, b)$$

$$\times \int_{x_1}^1 \frac{dz_1}{z_1} C_{qa_1}(z_1; \alpha_s(\mu_b^2)) f_{a_1/h_1}(x_1/z_1, \mu_b^2) \int_{x_2}^2 \frac{dz_2}{z_2} C_{\bar{q}a_2}(z_2; \alpha_s(\mu_b^2)) f_{a_2/h_2}(x_2/z_2, \mu_b^2)$$



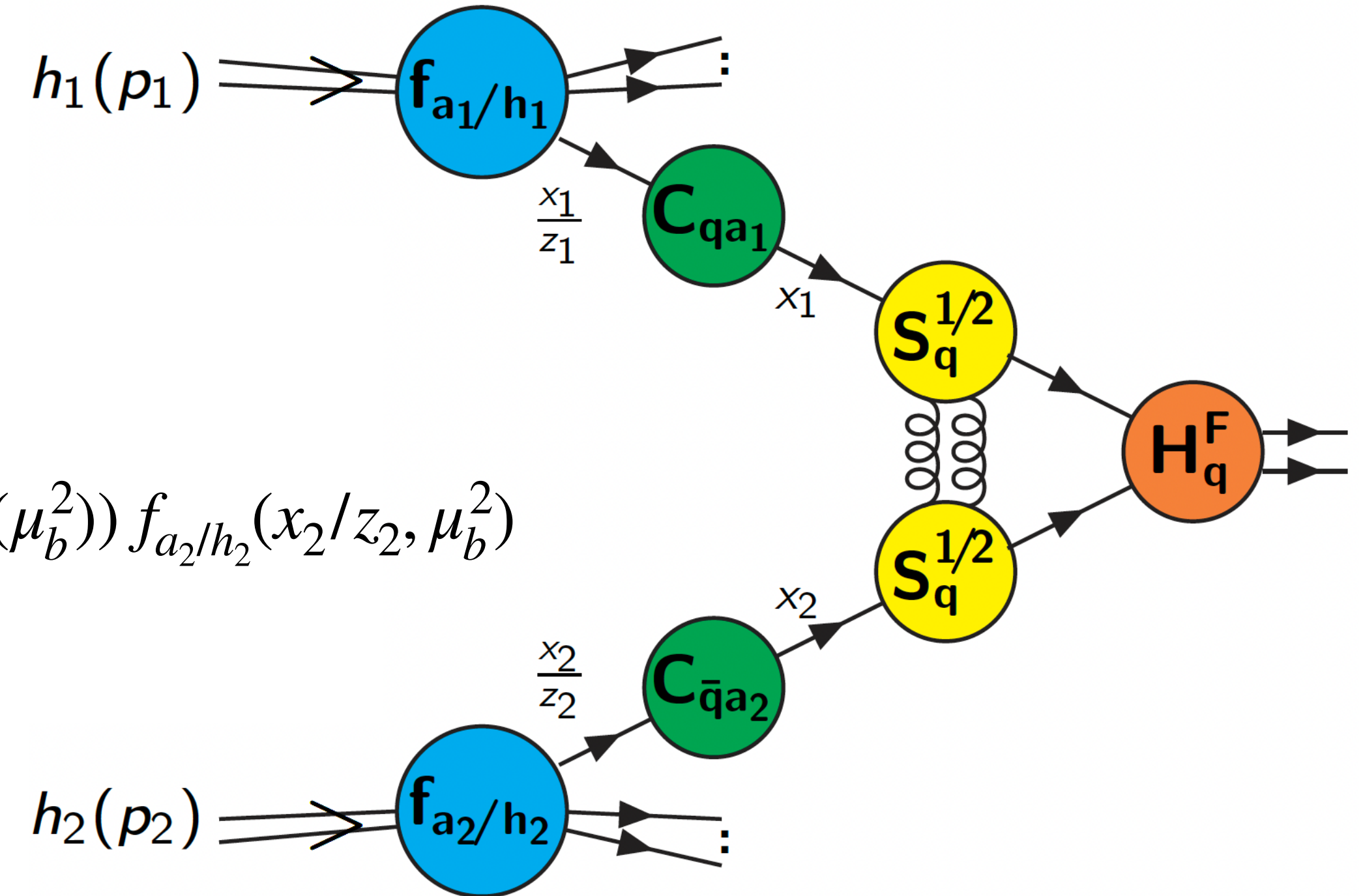
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Exactly the same expression as before



Application of q_T resummation

Application of q_T resummation



Eur.Phys.J.C 80 (2020) 3, 251

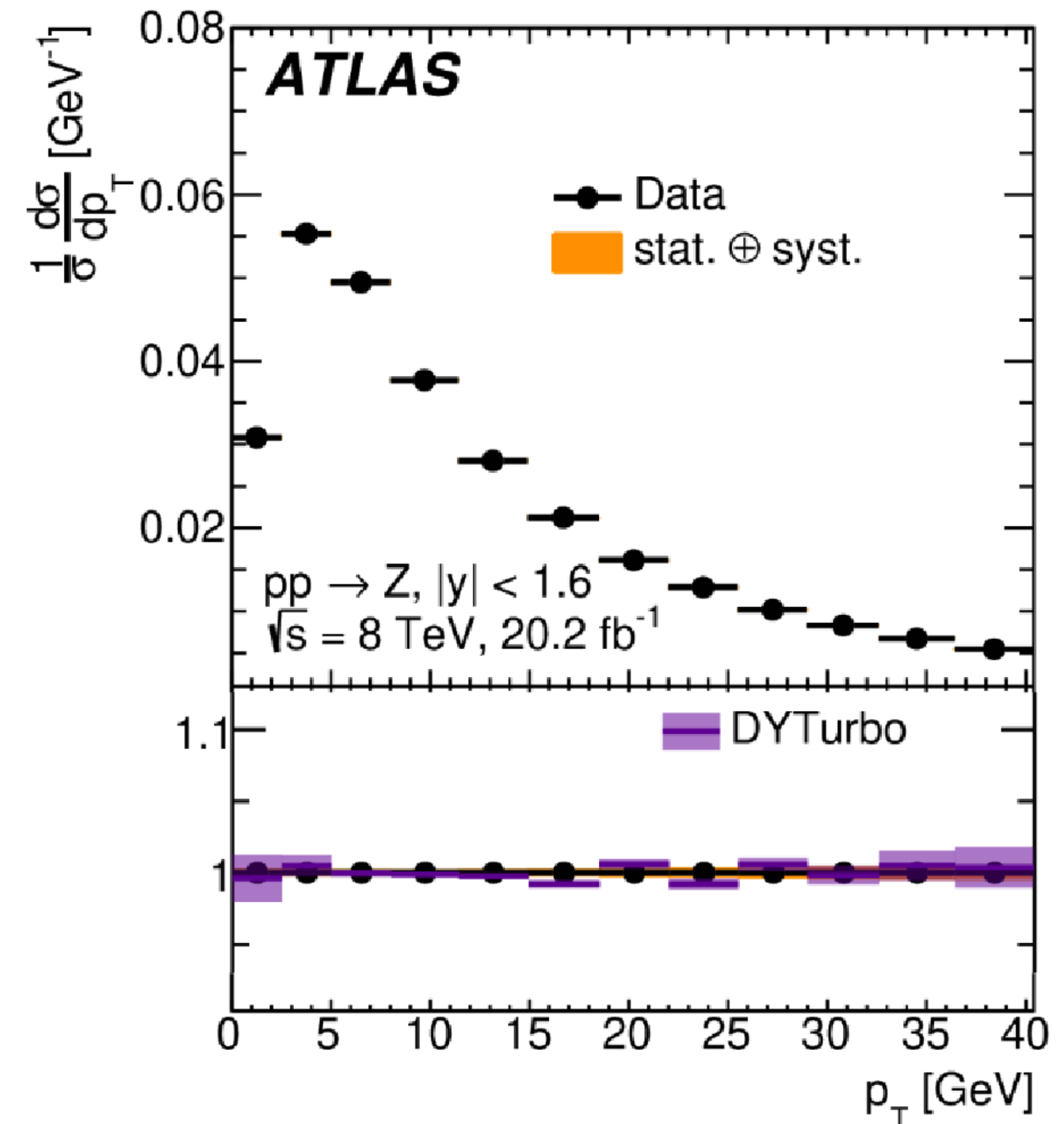
Application of q_T resummation



Eur.Phys.J.C 80 (2020) 3, 251



Study of the full q_T spectrum
of high energy data



Eur. Phys. J. C 84 (2024) 315

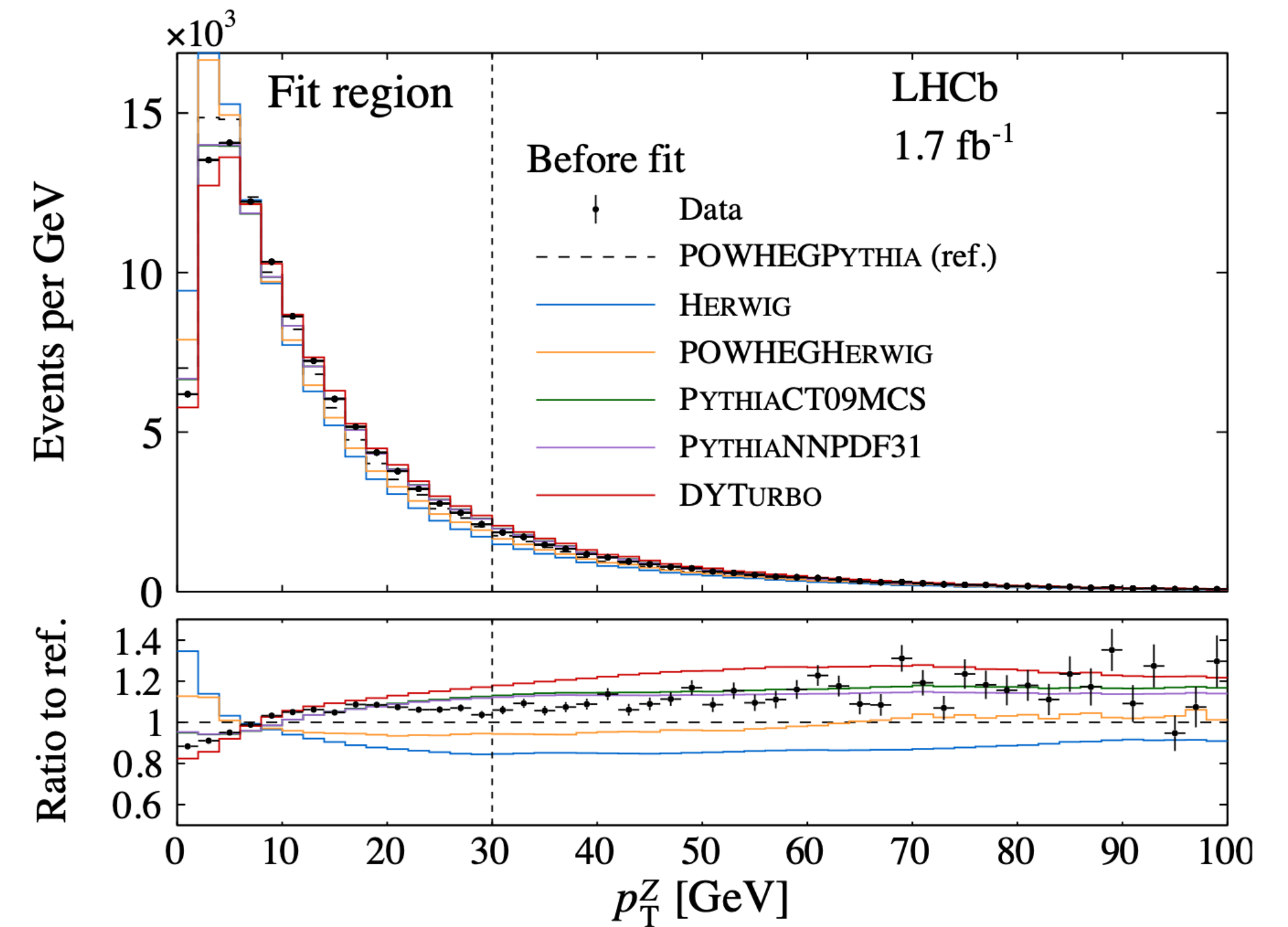
Application of q_T resummation



Eur.Phys.J.C 80 (2020) 3, 251

→ Study of the full q_T spectrum of high energy data

→ Study of the Z and $W^\pm$ boson masses



Application of q_T resummation

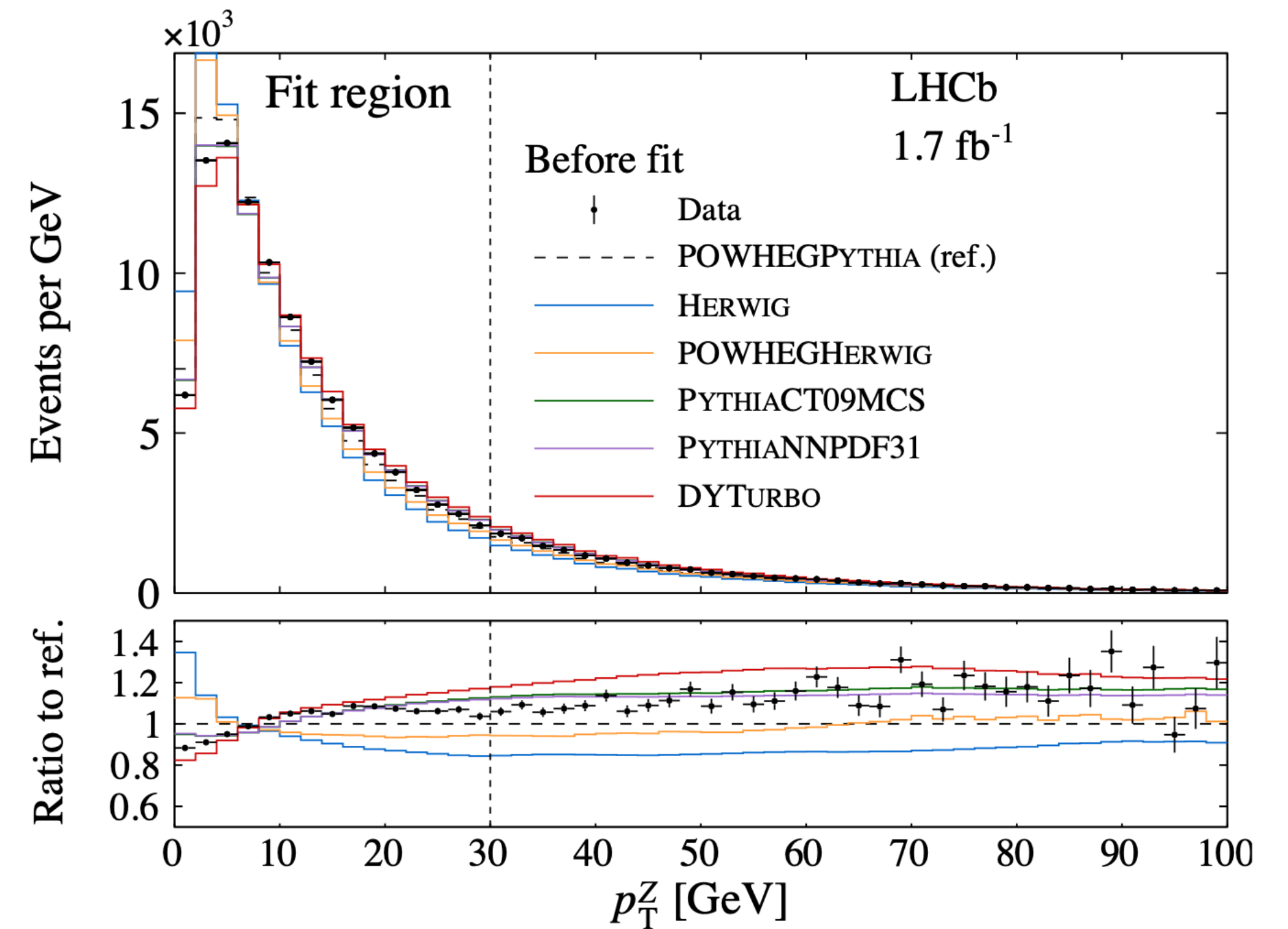


Eur.Phys.J.C 80 (2020) 3, 251

→ Study of the full q_T spectrum of high energy data

→ Study of the Z and $W^\pm$ boson masses

And at low invariant mass?



Application of q_T resummation

Application of q_T resummation

Only the resummed part...

Application of q_T resummation

Only the resummed part...



☰ README.md



Nanga Parbat is a fitting framework aimed at the determination of the non-perturbative component of TMD distributions.

Download

You can obtain NangaParbat directly from the github repository:

<https://github.com/MapCollaboration/NangaParbat>

For the last development branch you can clone the master code:

```
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```

Application of q_T resummation

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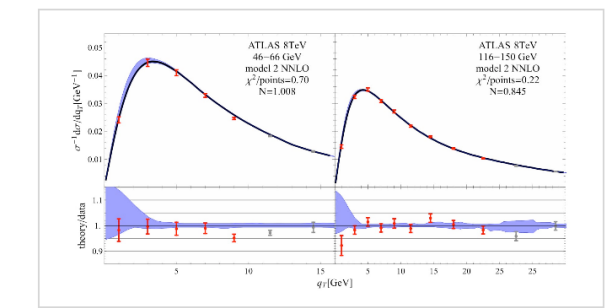
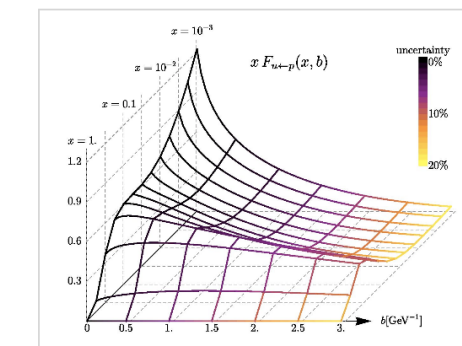
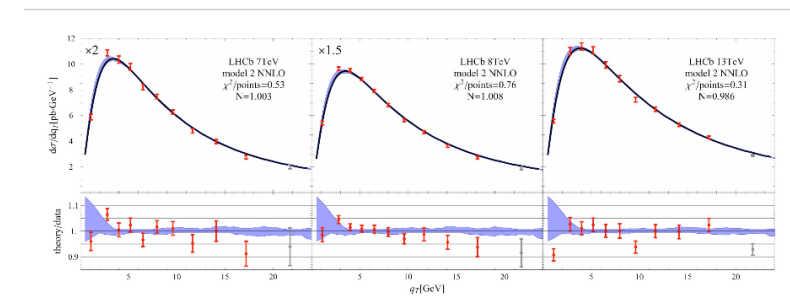
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arTeMiDe



News



12 Dec 2019: Version 2.02 released (+manual update).

23 Feb 2019: Version 1.4 released (+manual update).

21 Jan 2019: Artemide now has a [repository](#).

[Archive of older links/news.](#)

Articles, presentations & supplementary materials



[Extra pictures for the paper arXiv:1902.08474](#)

[Seminar of A.Vladimirov in Pavia 2018 on TMD evolution.](#)

[Link to the text in Inspire.](#)

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[Recent version/release can be found in repository](#)

About us & Contacts



If you have found mistakes, or have suggestions/questions, please, contact us.

Some extra materials can be found on [Alexey's web-page](#)

Alexey Vladimirov Alexey.Vladimirov@physik.uni-regensburg.de

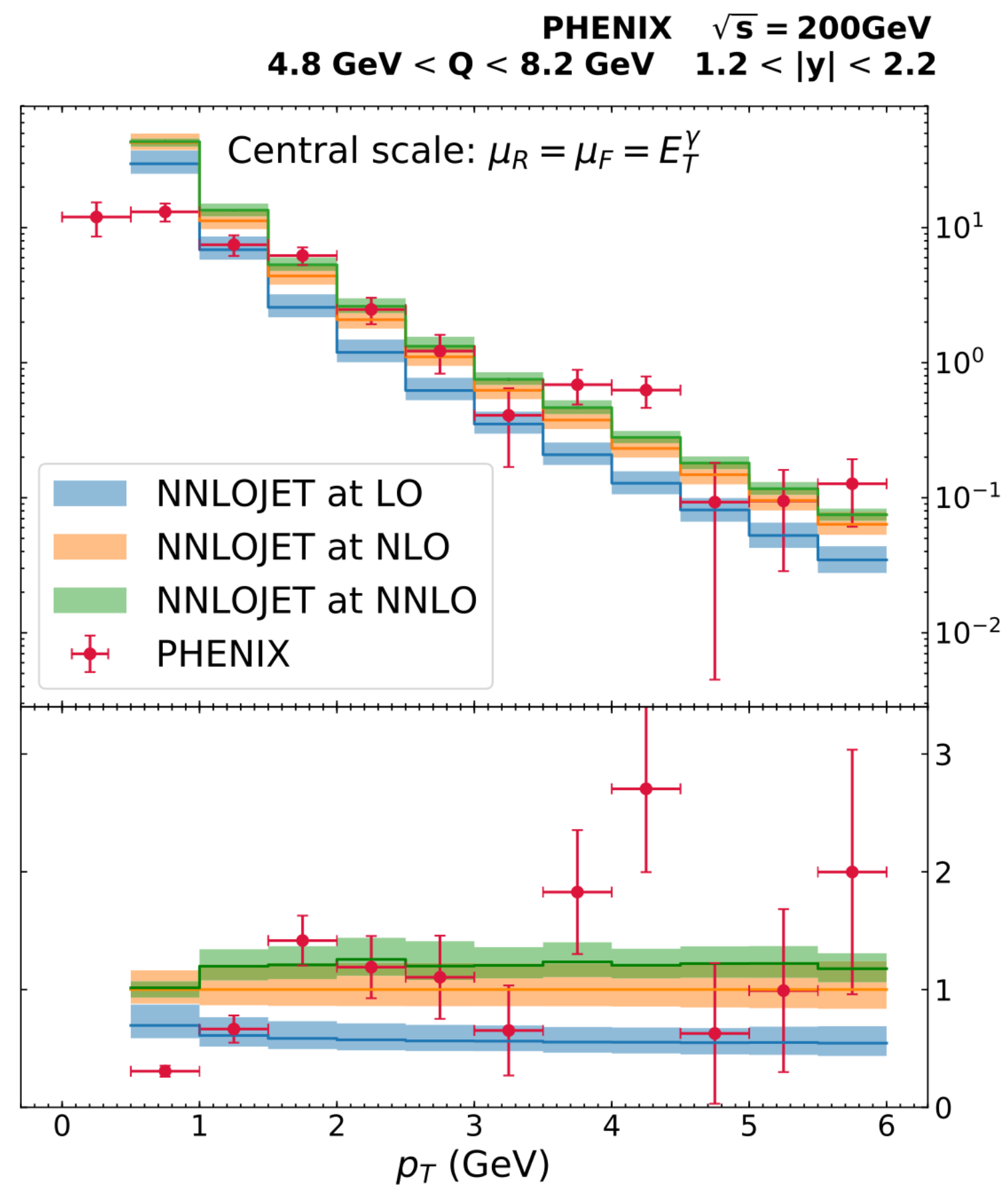
Ignazio Scimemi ignazios@fis.ucm.es

Application of q_T resummation

Or only the finite part...

Application of q_T resummation

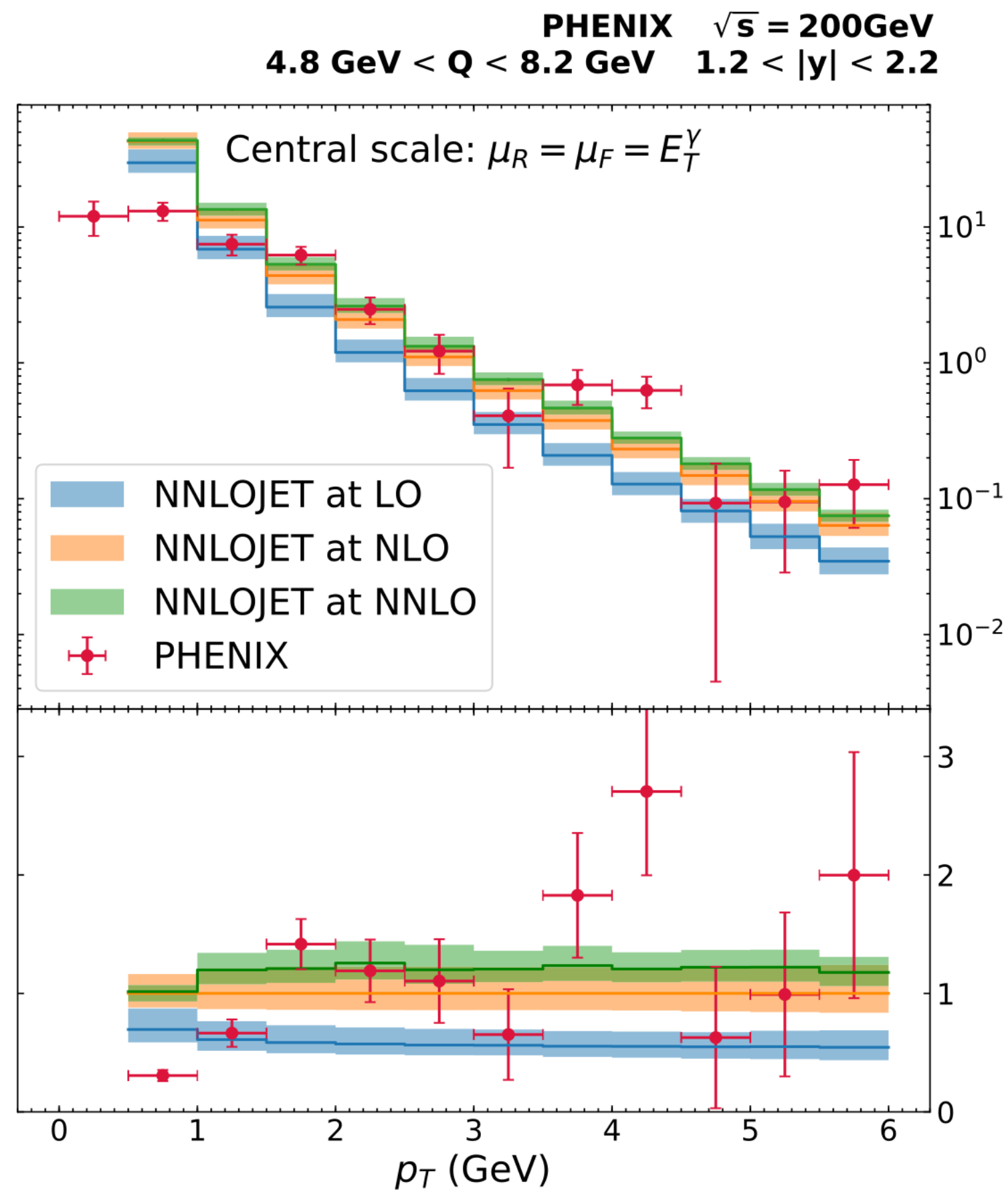
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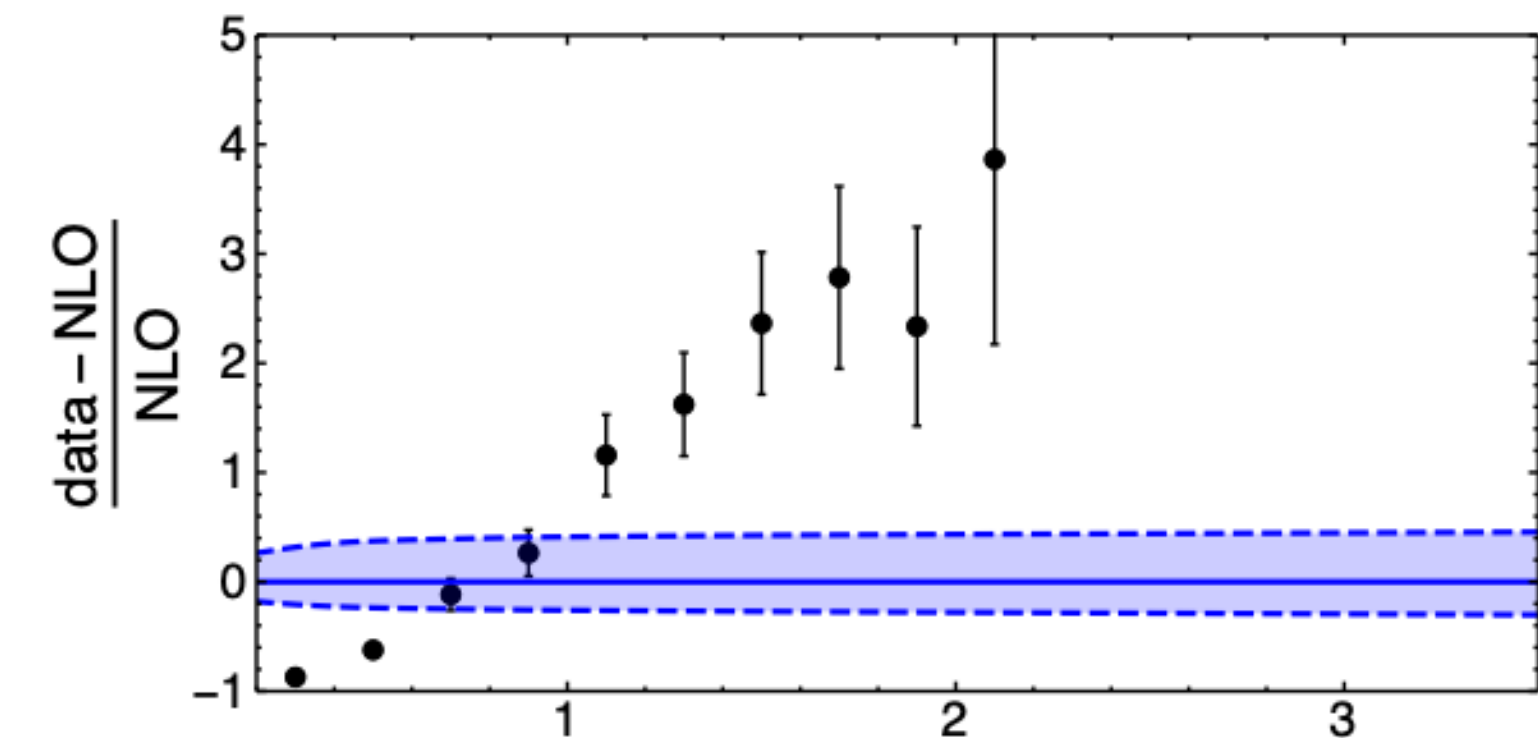
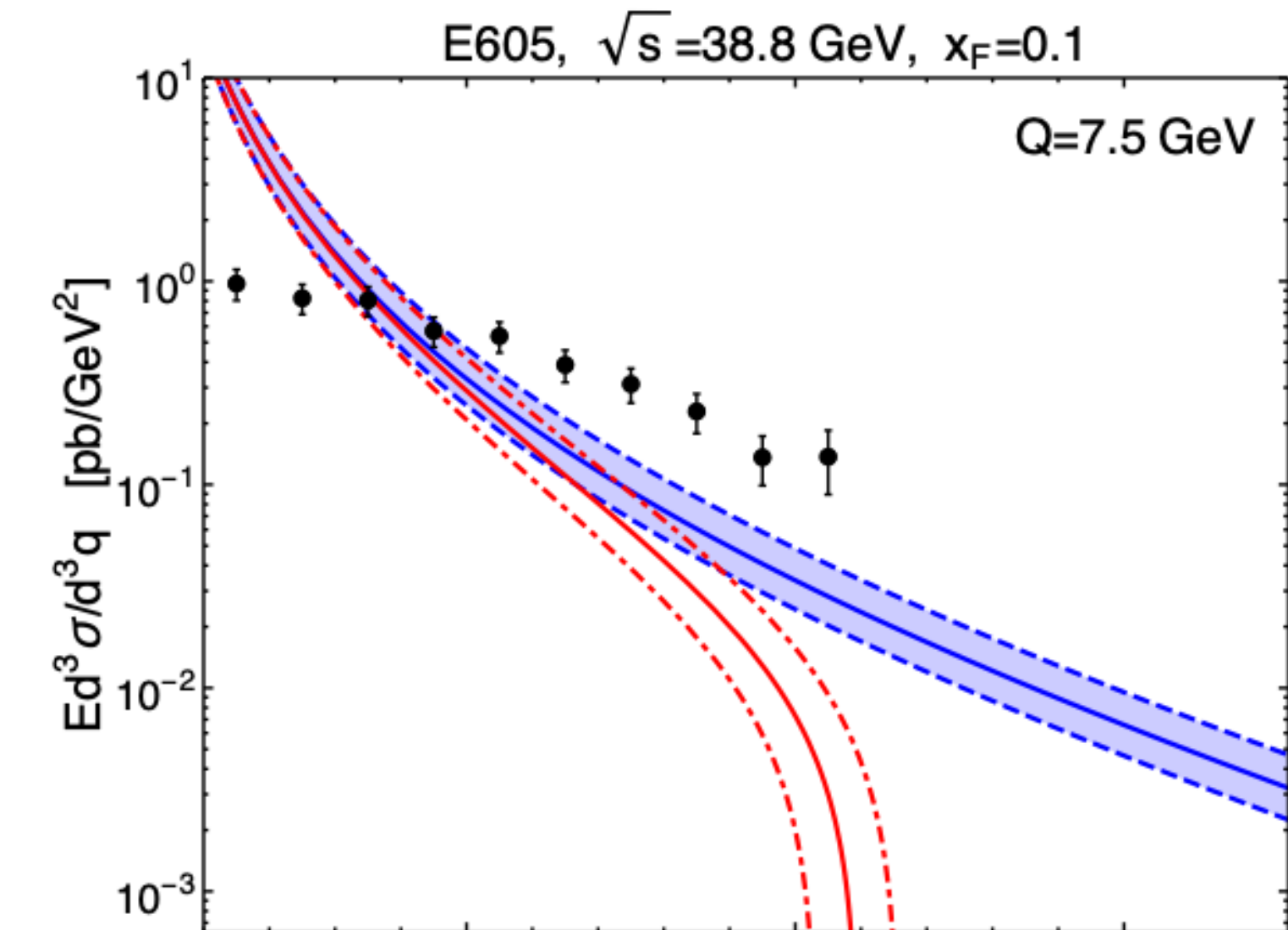
Physics Letters B 829 (2022) 137111

Application of q_T resummation

Or only the finite part...



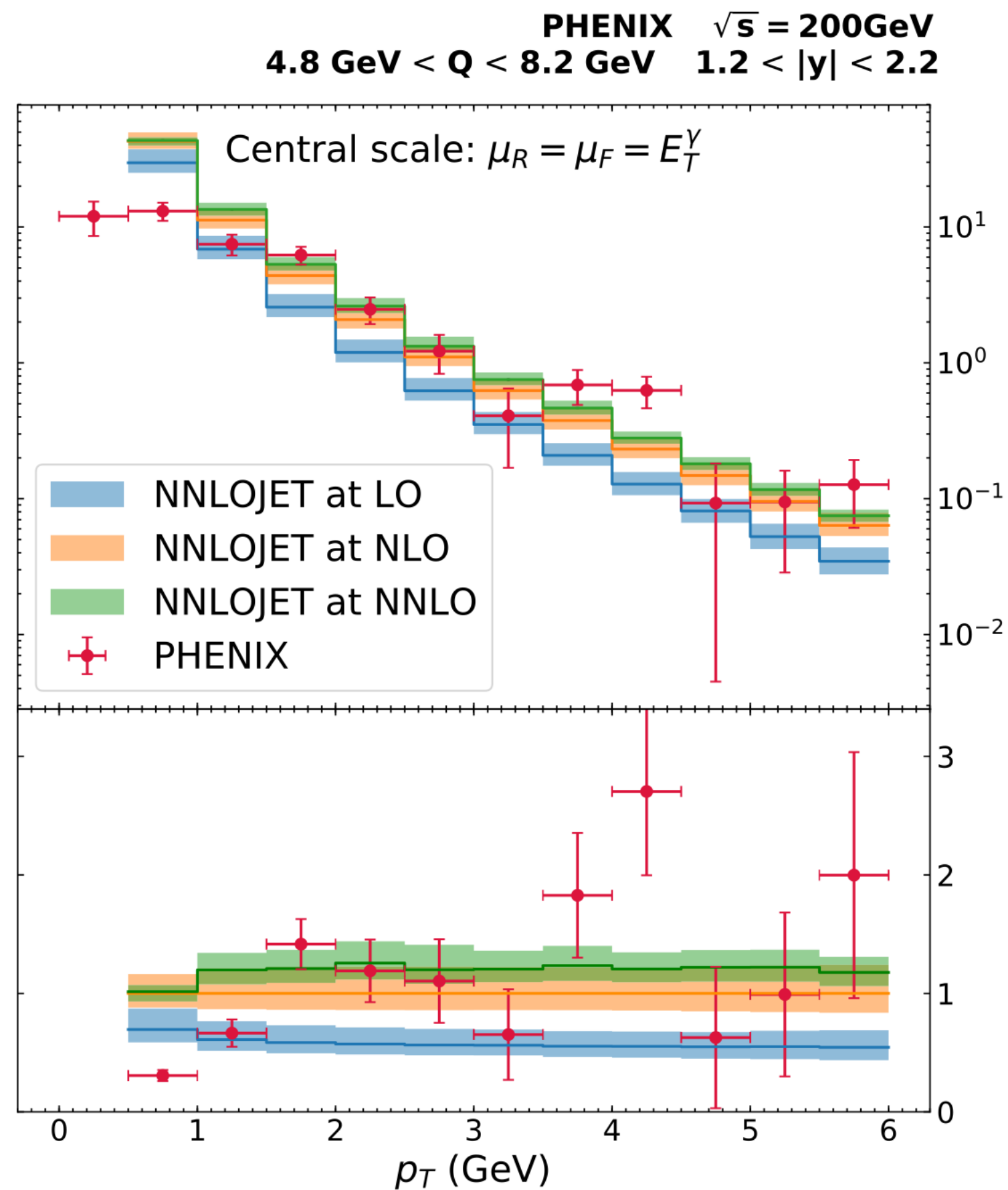
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Phys.Rev.D 100 (2019) 1, 014018

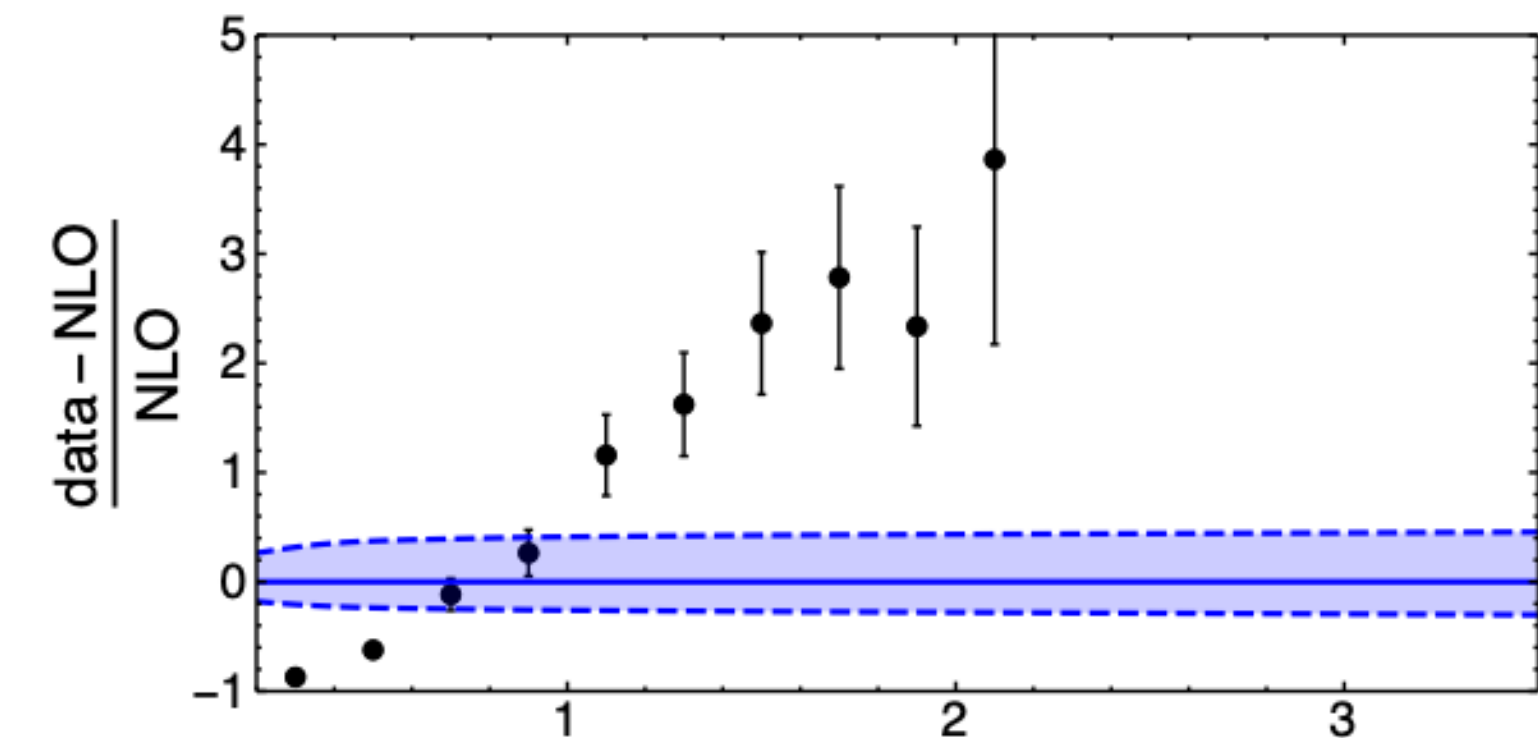
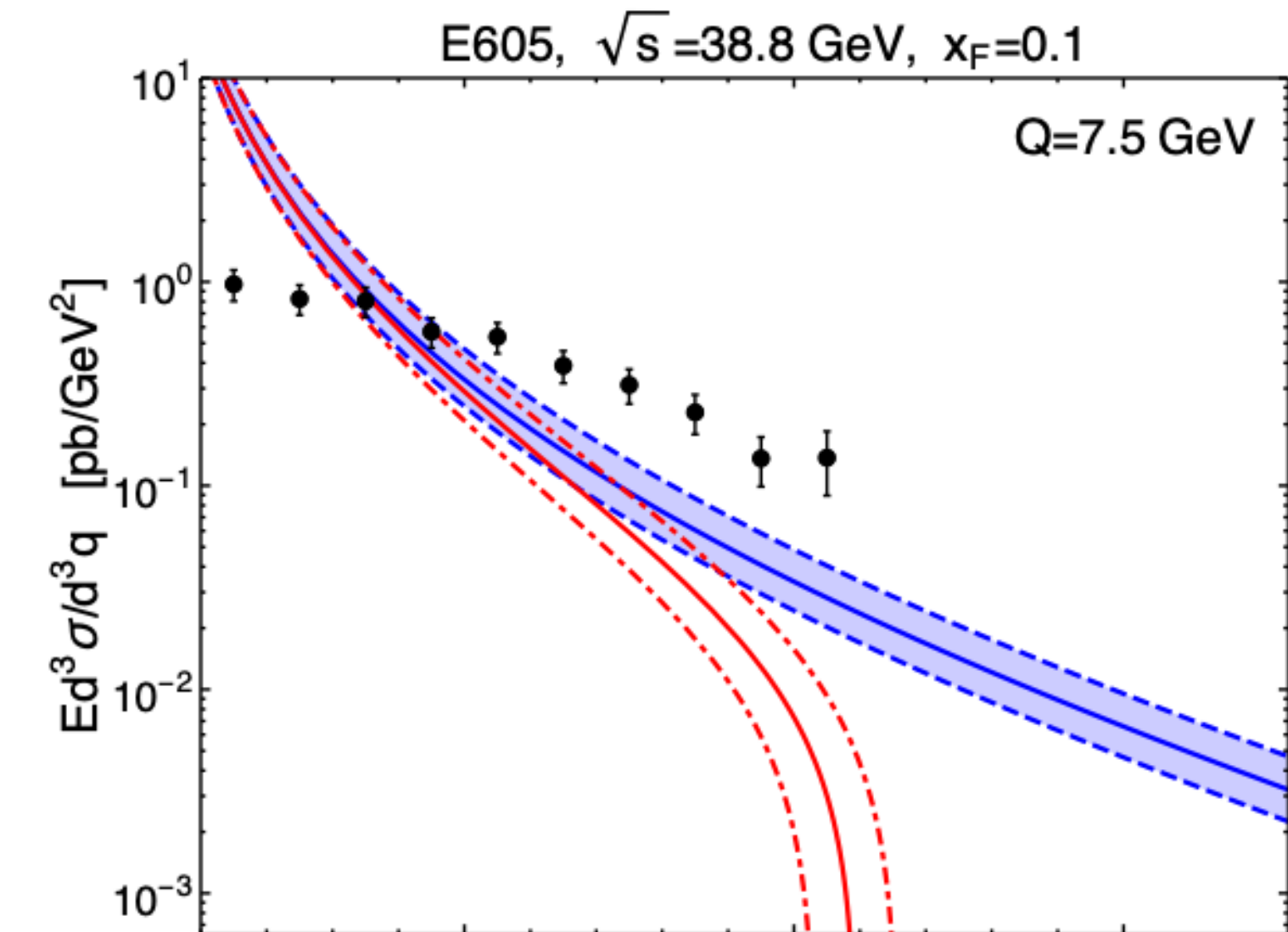
Application of q_T resummation

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Physics Letters B 829 (2022) 137111

*Problem in the
description of
the data*

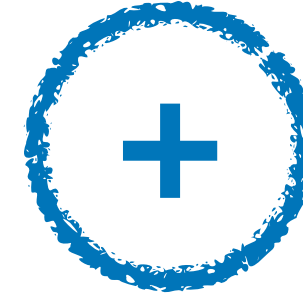


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Study of low invariant mass data

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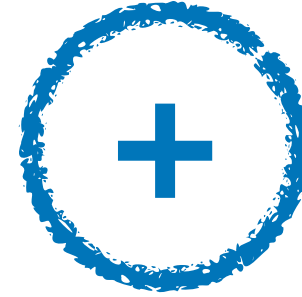
Finite part



Resummed part

Study of low invariant mass data

Finite part

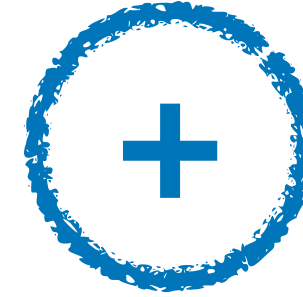


Resummed part

- N^4LL perturbative accuracy, i.e. up to $\exp(\sim \alpha_s^n L^{n-3})$

Study of low invariant mass data

Finite part

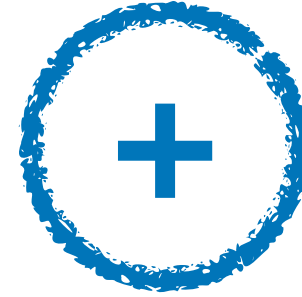


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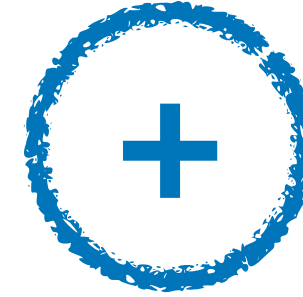


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→ Now implemented in DYTurbo

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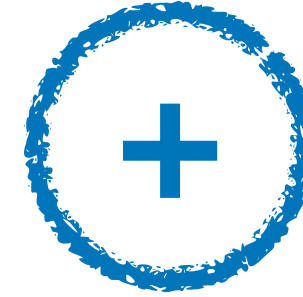


Benchmark with MCFM

*Phys.Rev.D 107 (2023) 1,
L011506*

Study of low invariant mass data

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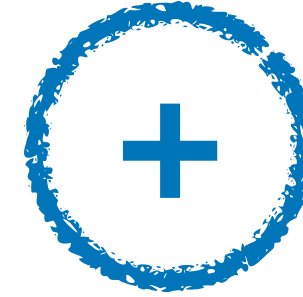
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Benchmark with MCFM Phys.Rev.D 107 (2023) 1, L011506

Benchmark with inclusive
 N^3LO cross section JHEP 12 (2022) 066

Study of low invariant mass data

Finite part

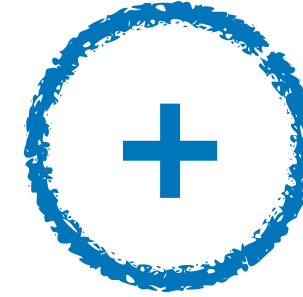


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Study of low invariant mass data

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- LL mixed QCD-QED accuracy, i.e. up to $\exp(\sim \alpha_S^n \alpha_{em}^n L^{2n})$ JHEP 07 (2023) 104

Study of low invariant mass data

Study of low invariant mass data

Experiment	Observable	$\sqrt{s}$ [GeV]	Q [GeV]	y or x_F
E605	$Ed^3\sigma/d^3\mathbf{q}$	38.8	7 - 18	$x_F = 0.1$
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E288 300 GeV	$Ed^3\sigma/d^3\mathbf{q}$	23.8	4 - 12	$y = 0.21$
E288 400 GeV	$Ed^3\sigma/d^3\mathbf{q}$	27.4	5 - 14	$y = 0.03$
ATLAS 8 TeV on-peak	$(1/\sigma)d\sigma/d \mathbf{q}_T $	8000	66 - 116	$ y < 0.4$ $0.4 < y < 0.8$ $0.8 < y < 1.2$ $1.2 < y < 1.6$ $1.6 < y < 2$ $2 < y < 2.4$
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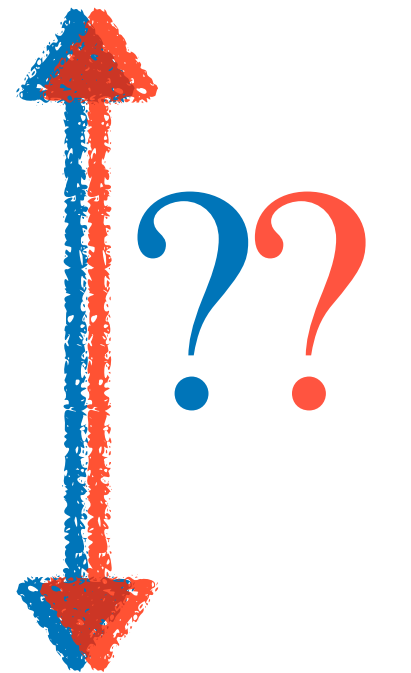
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**Already well
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**Already well
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Study of low invariant mass data

Study of low invariant mass data

Some stuff...

Study of low invariant mass data

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- Landau pole:

Study of low invariant mass data

Some stuff...

- Landau pole:

b_T 

$$b_{\star}(b_T) = \frac{b_T}{\sqrt{1 + \frac{b_T^2}{b_{\max}^2}}} \quad \text{Nucl.Phys.B250 (1985)199}$$

Study of low invariant mass data

Some stuff...

- Landau pole: $b_T \longrightarrow$
(We tried also the minimal prescription)

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Study of low invariant mass data

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Study of low invariant mass data

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 $\downarrow$
 $\exp\{\alpha_s^n \tilde{L}^k\} \Big|_{b_T=0} = 1$

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$\downarrow$

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$\longleftarrow$

$\int_0^\infty d^2 \mathbf{q}_T \frac{d\sigma}{d^2 \mathbf{q}_T} = \sigma^{tot}$

Study of low invariant mass data

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Other stuff...

Study of low invariant mass data

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Study of low invariant mass data

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Phys.Rev.D 91 (2015) 7, 074020

Study of low invariant mass data

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**4 non-perturbative
parameters**

Study of low invariant mass data

Study of low invariant mass data



Eur.Phys.J.C 80 (2020) 3, 251

Study of low invariant mass data



Eur.Phys.J.C 80 (2020) 3, 251



Study of low invariant mass data



Eur.Phys.J.C 80 (2020) 3, 251



arxiv:2206.12465

- Fit at central scale $\mu_F = \mu_R = \mu_Q = M$

Study of low invariant mass data



Eur.Phys.J.C 80 (2020) 3, 251



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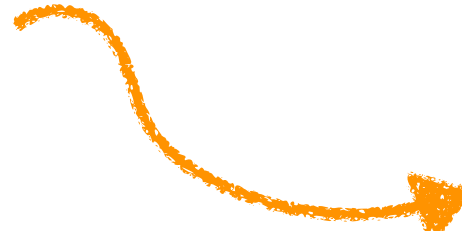
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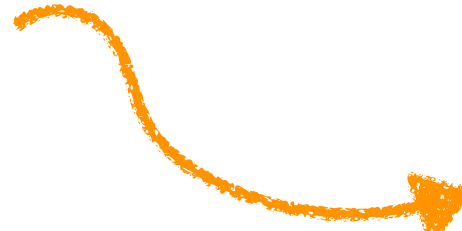


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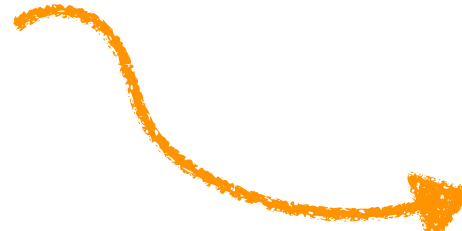


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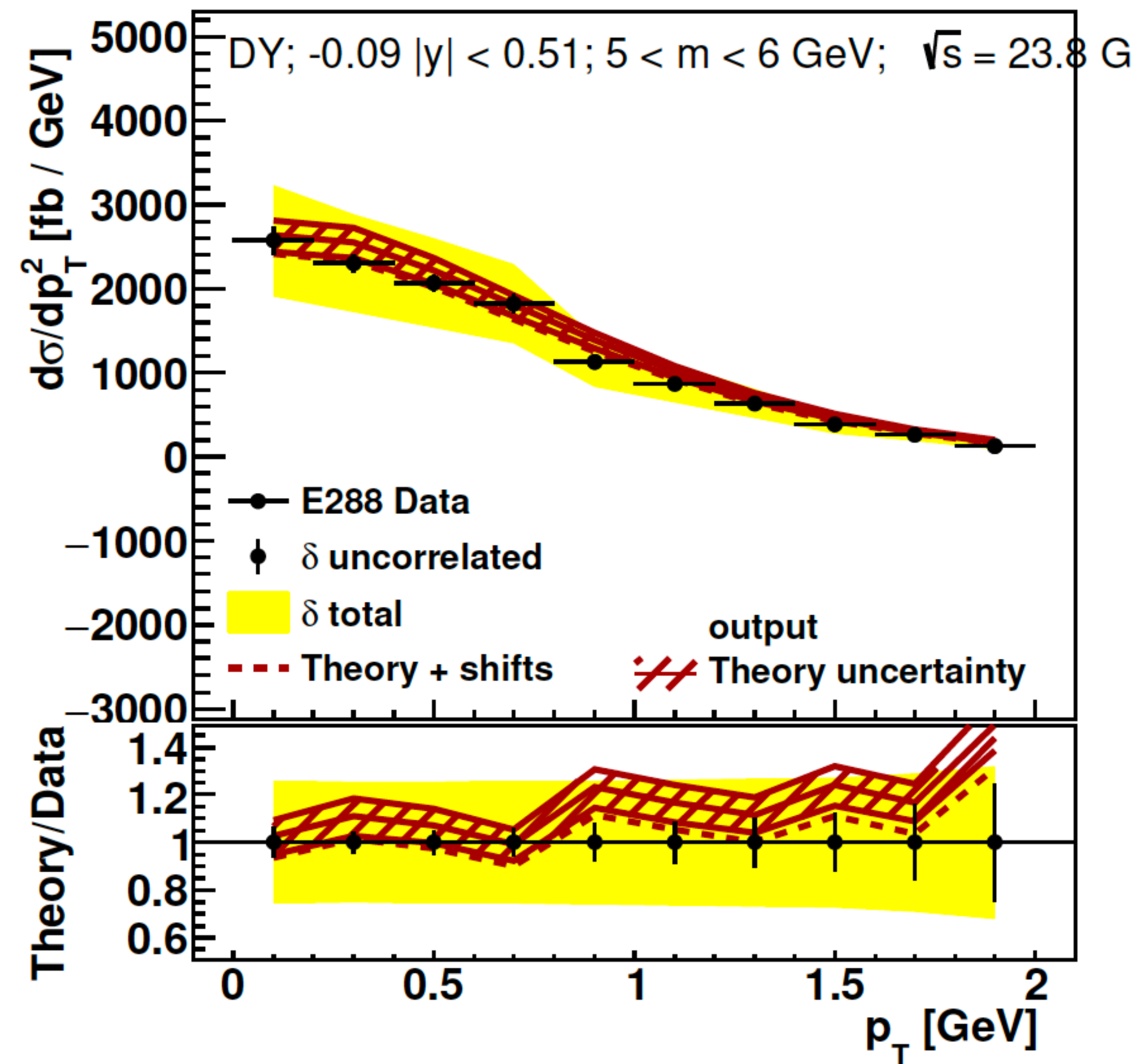
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We have high- q_T data!

Study of low invariant mass data

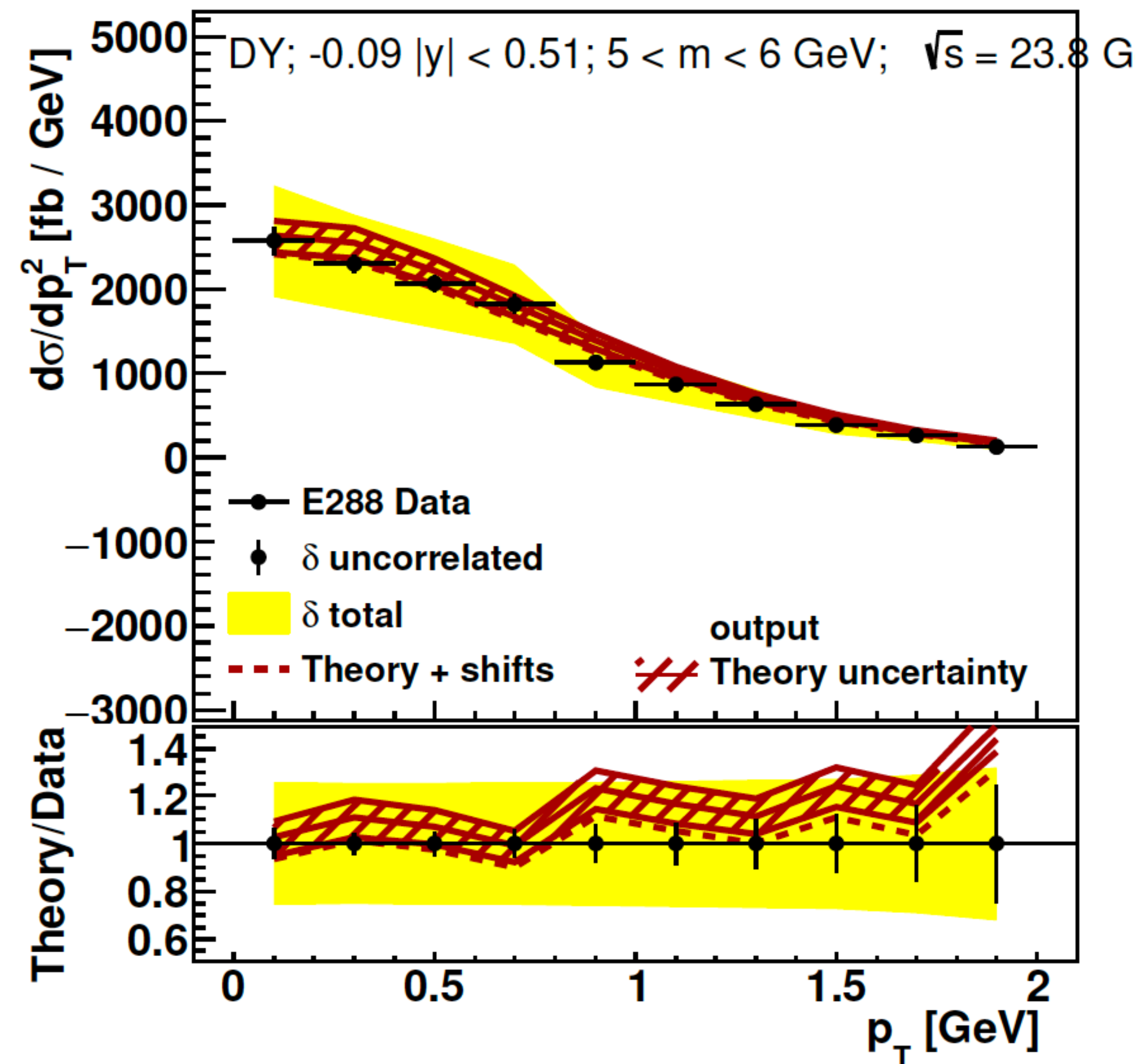
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E288 300 GeV, $5 < Q < 6$



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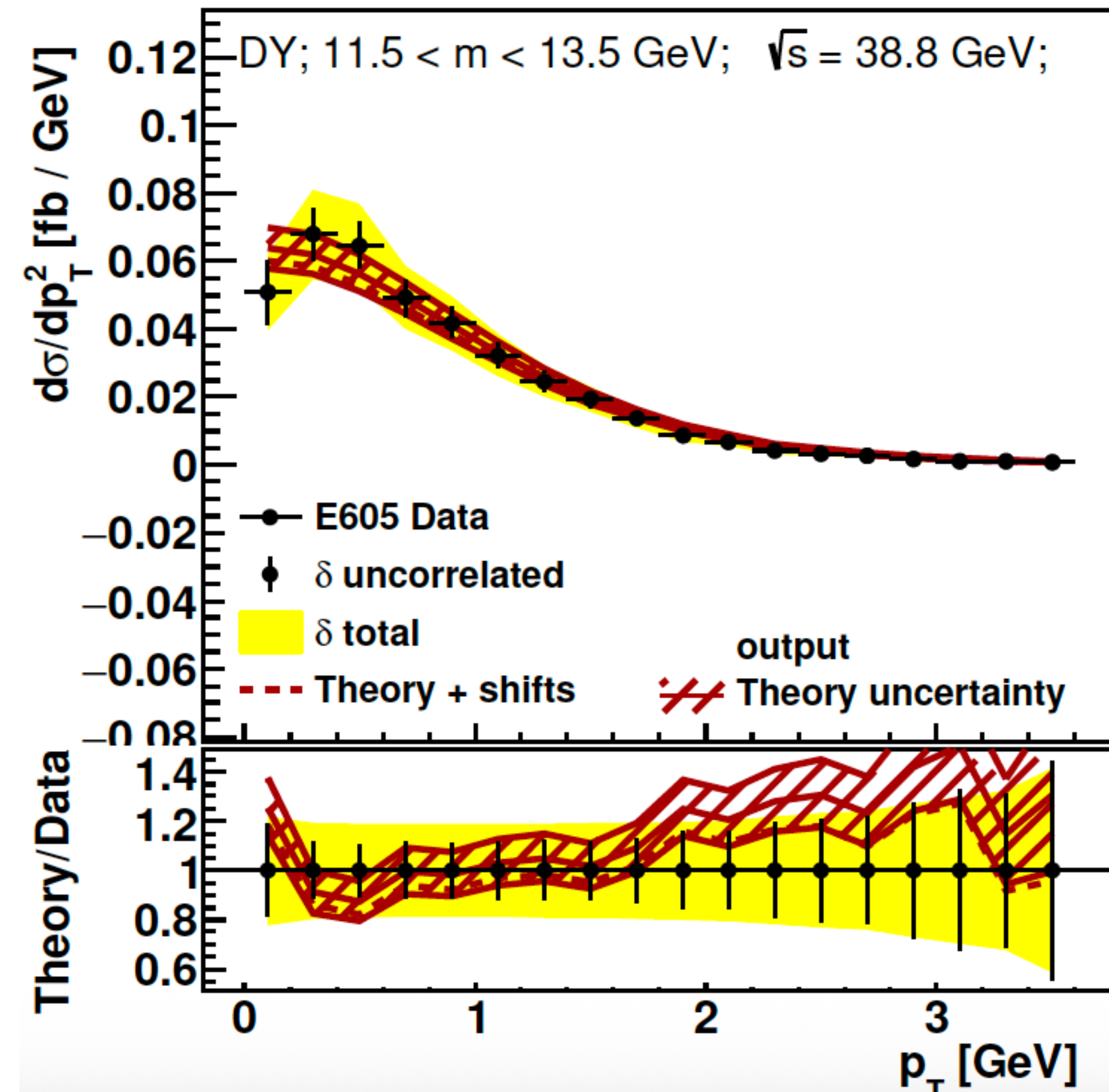
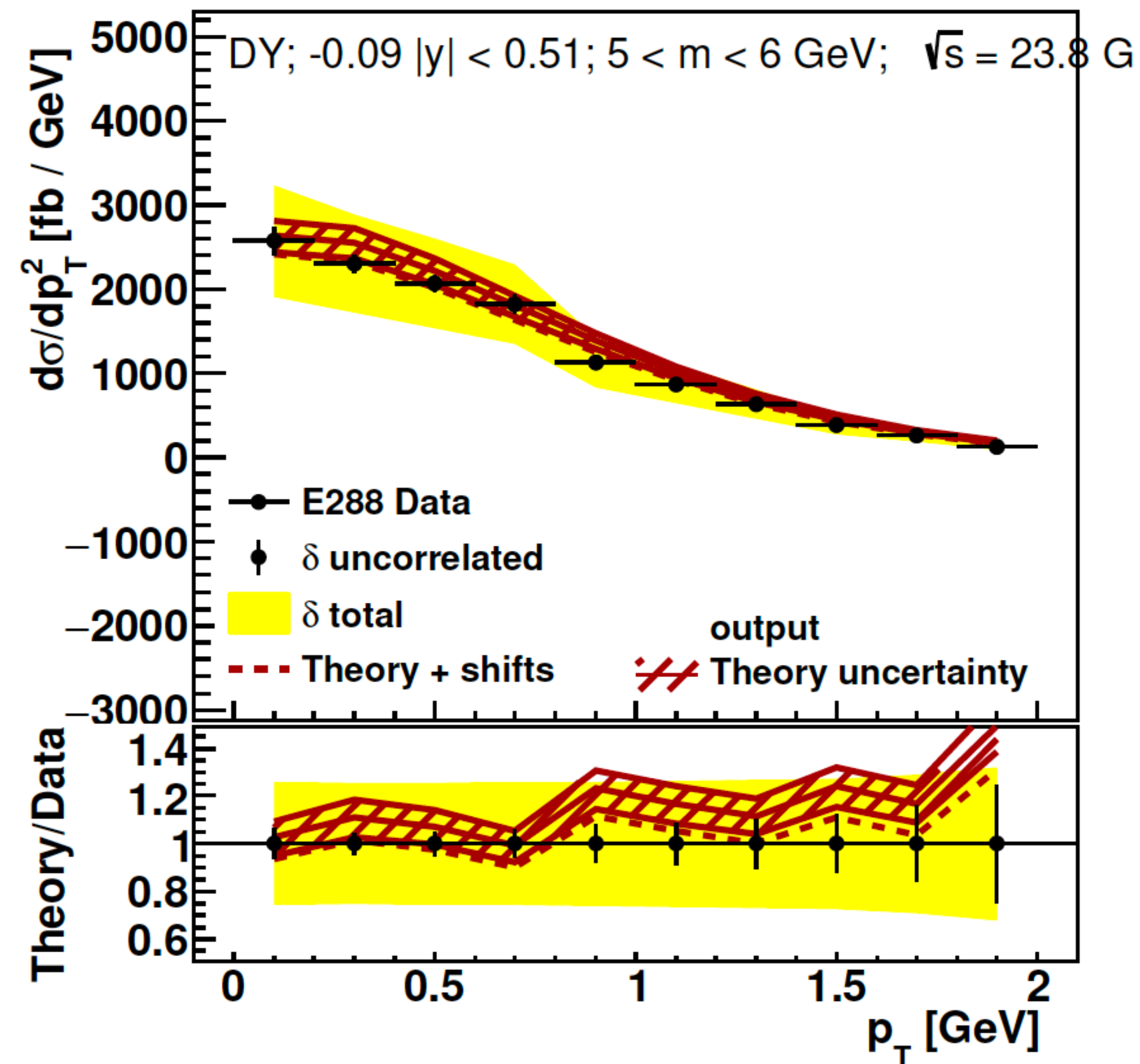


$$\chi^2/N_{data} = 1.05$$

Study of low invariant mass data

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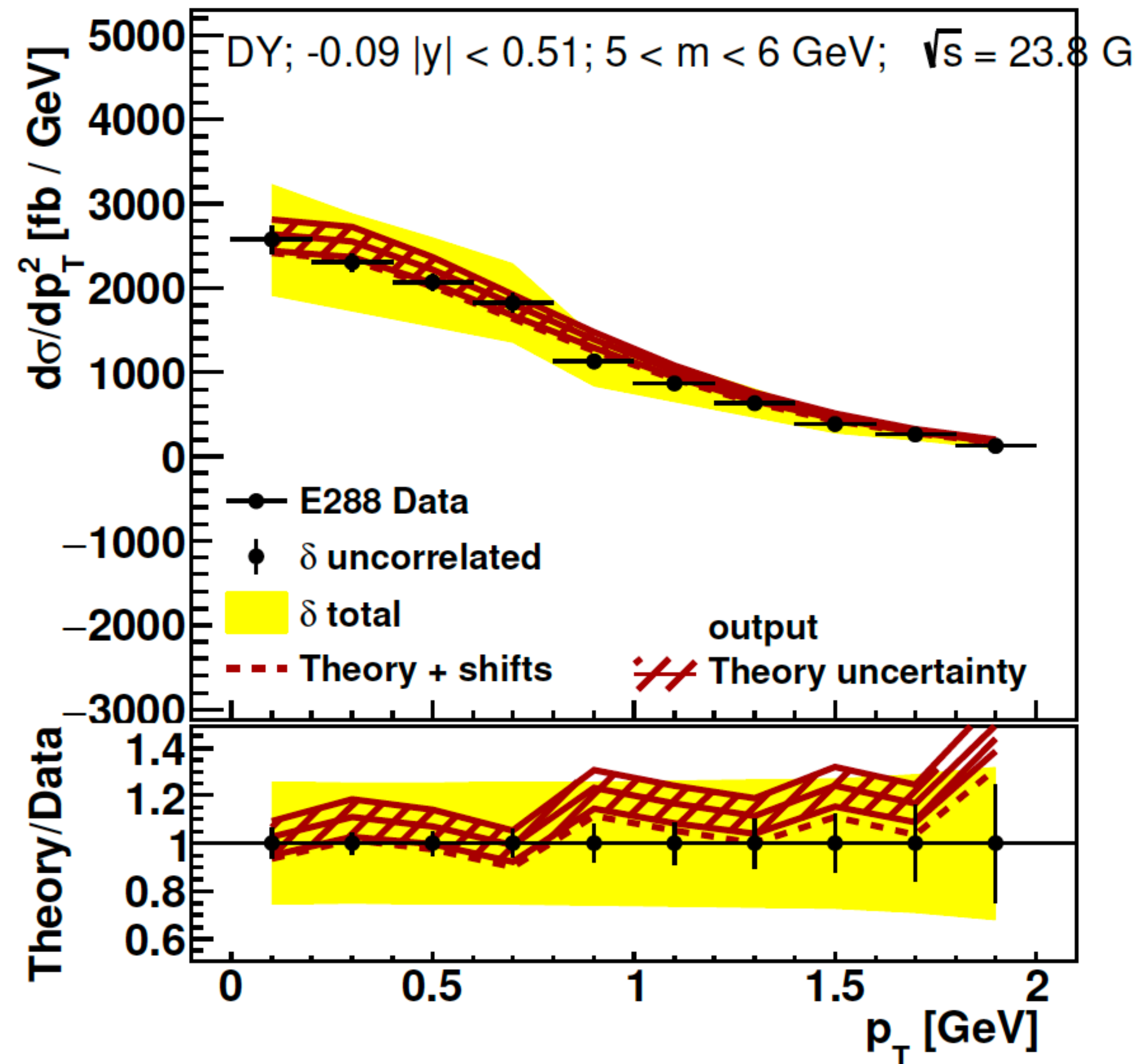
E605, $11.5 < Q < 13.5$



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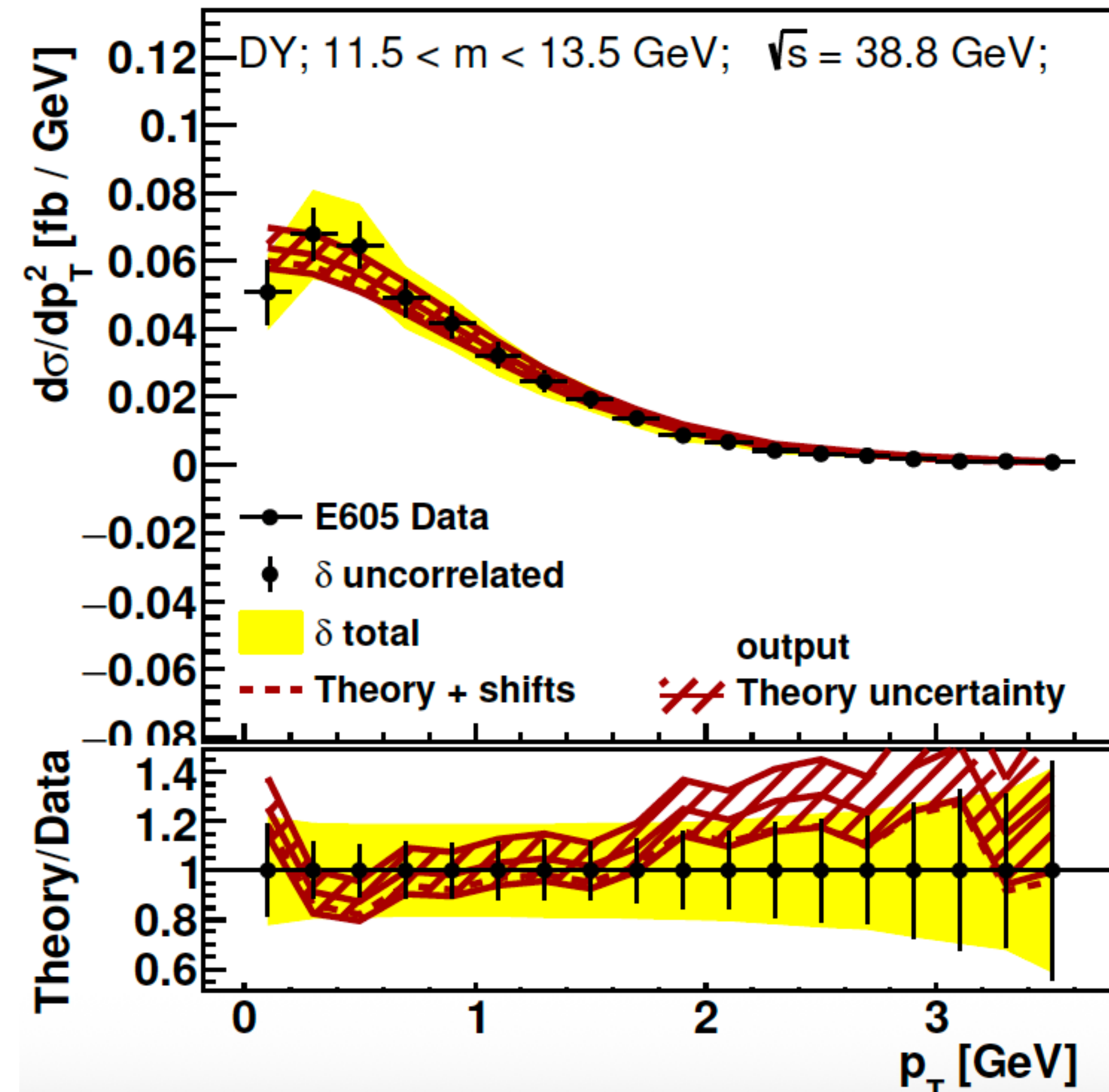
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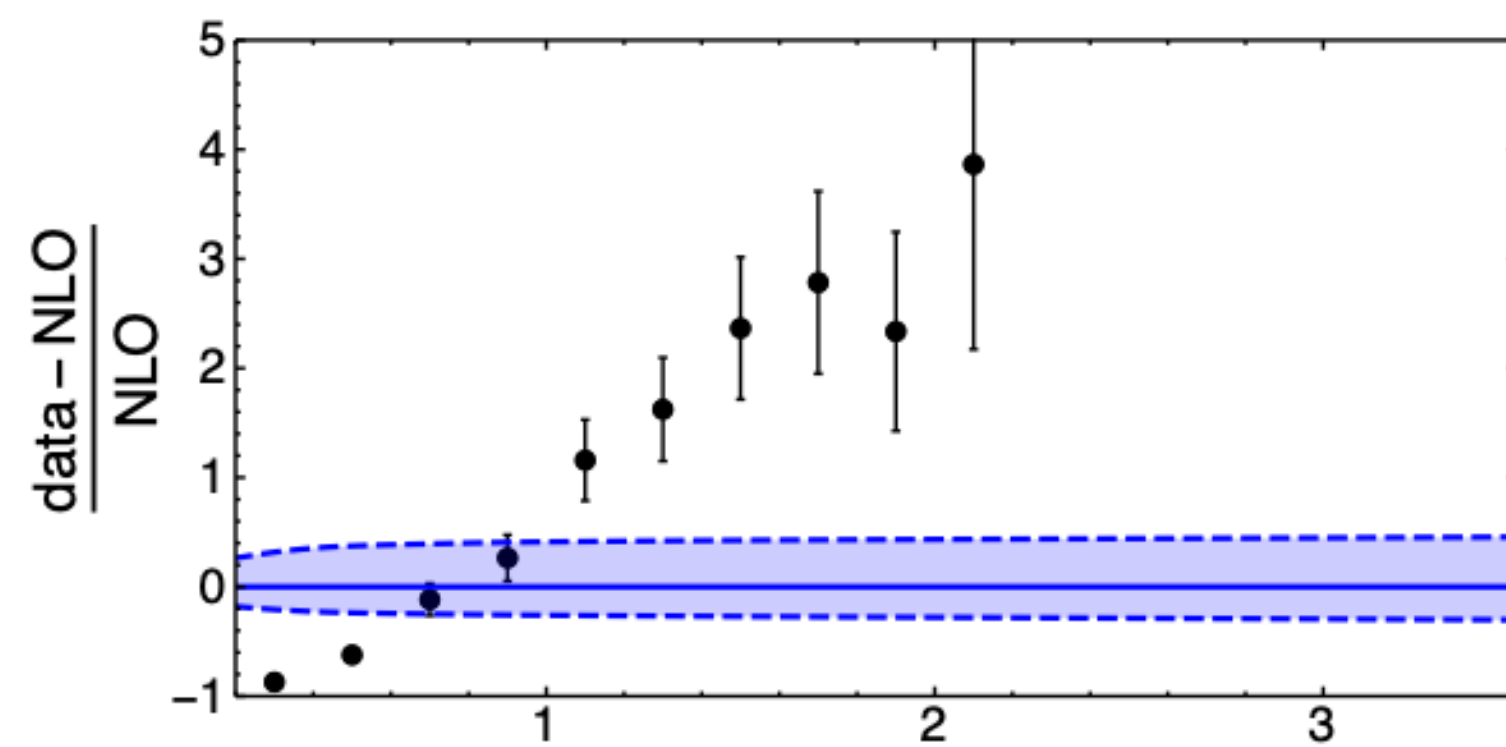
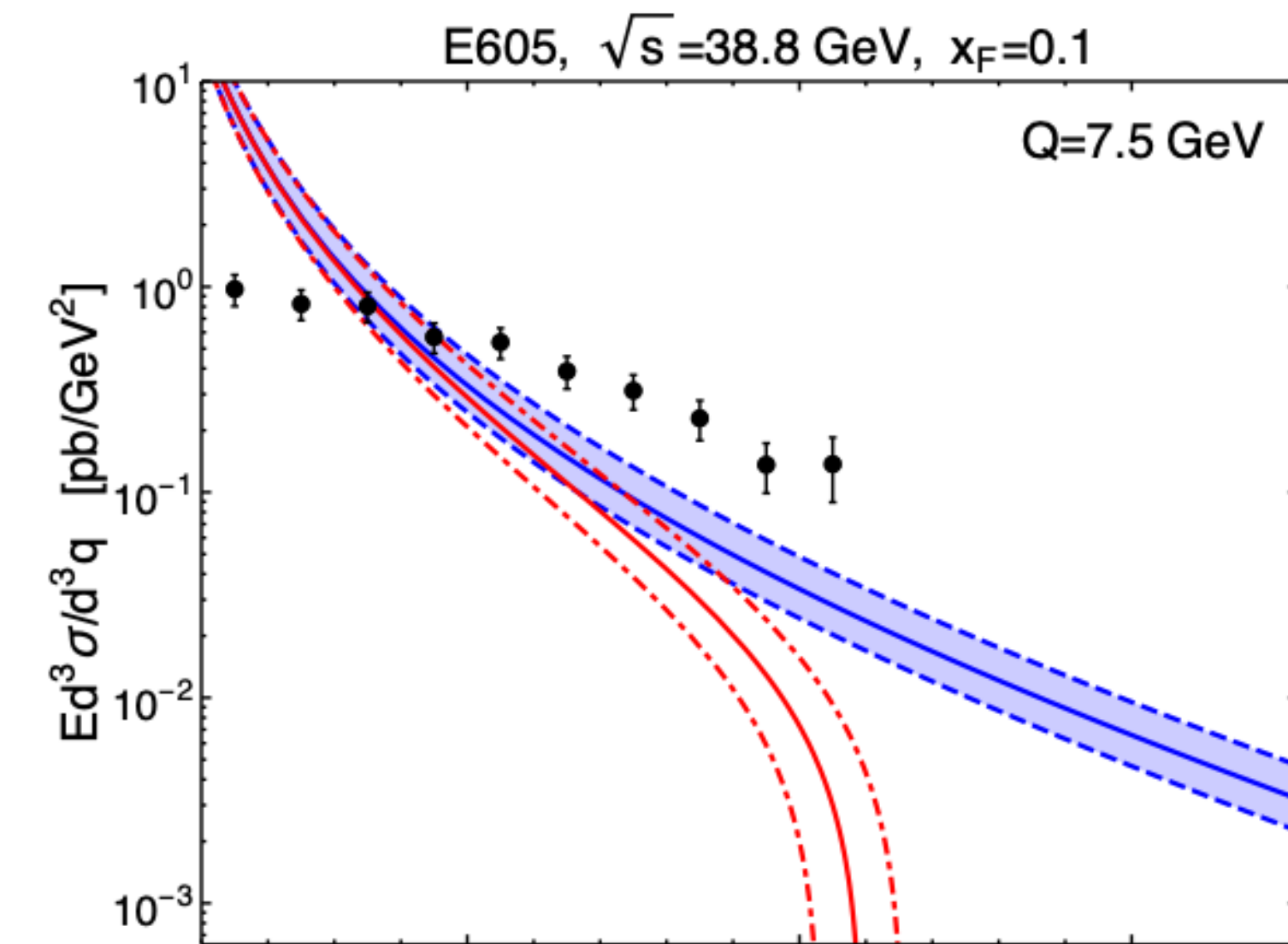
E605, $11.5 < Q < 13.5$



$$\chi^2/N_{data} = 0.79$$

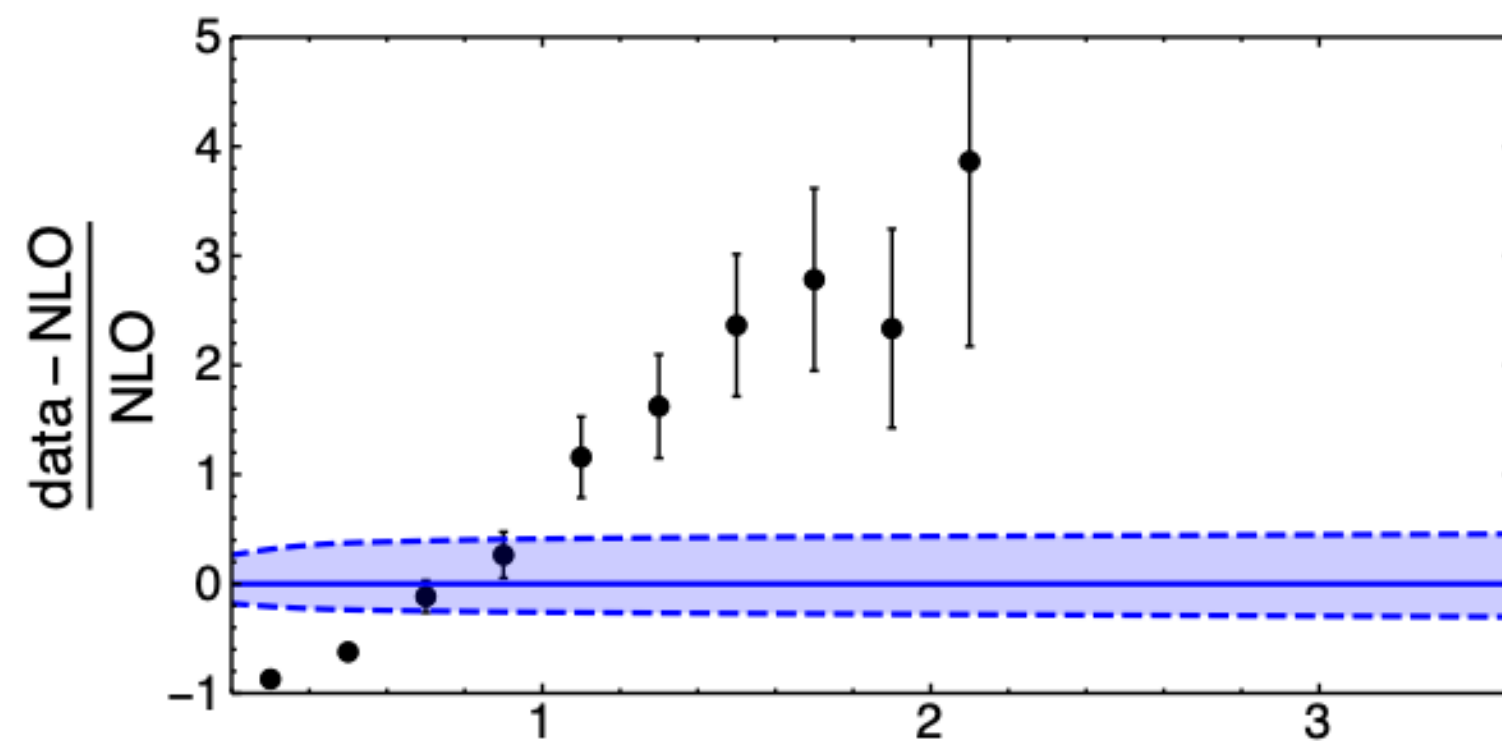
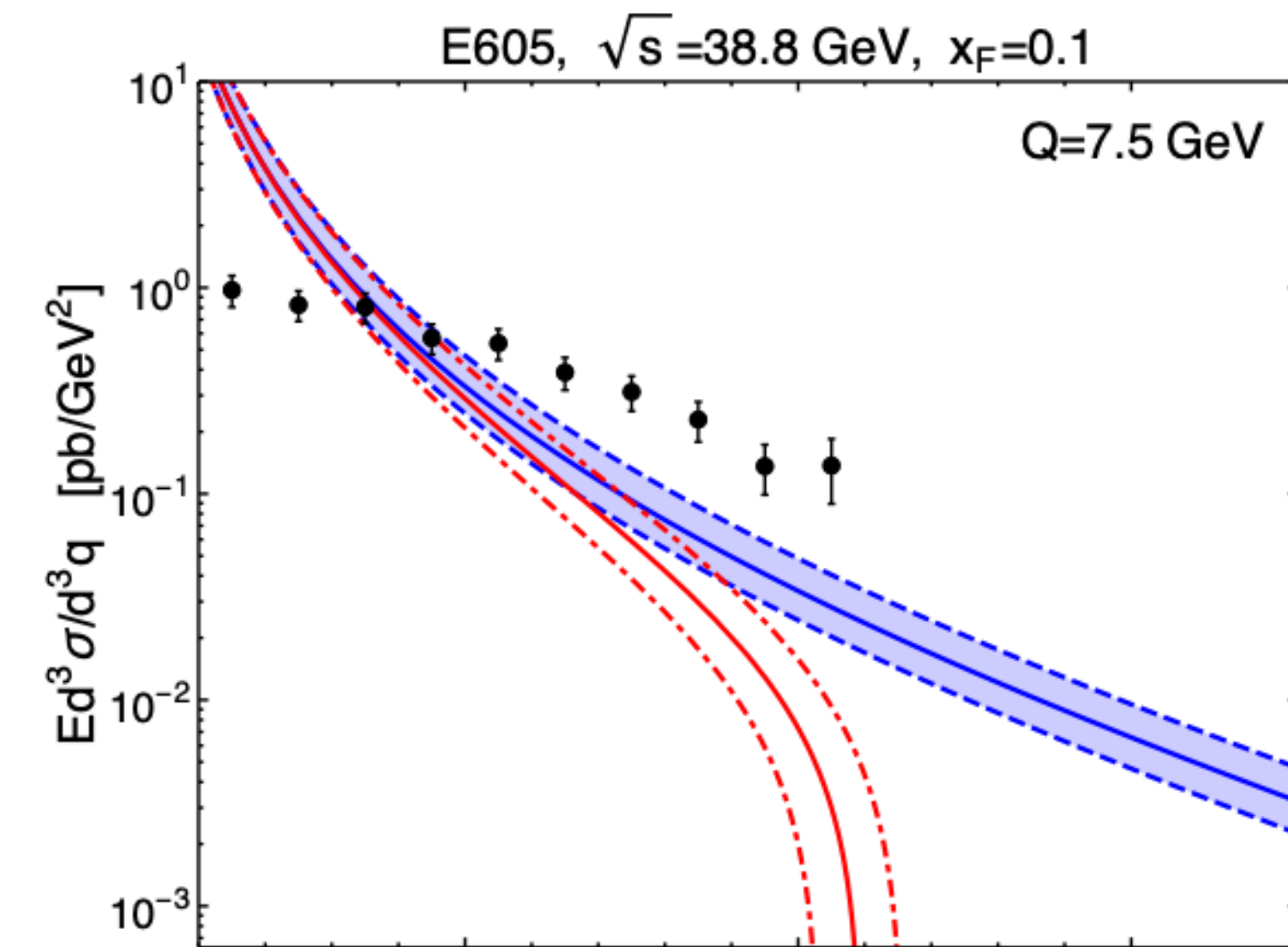
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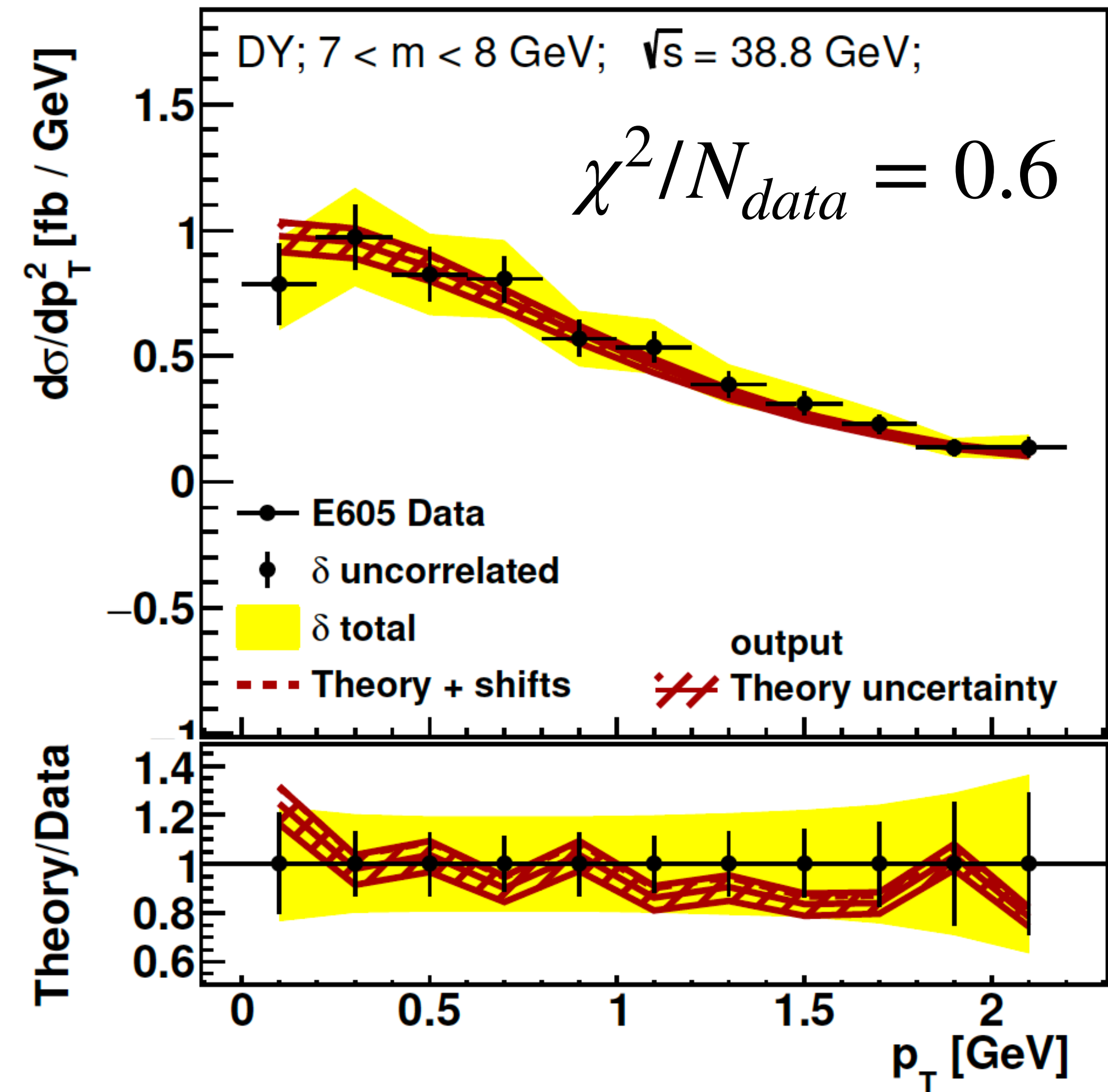


Phys.Rev.D 100 (2019) 1, 014018

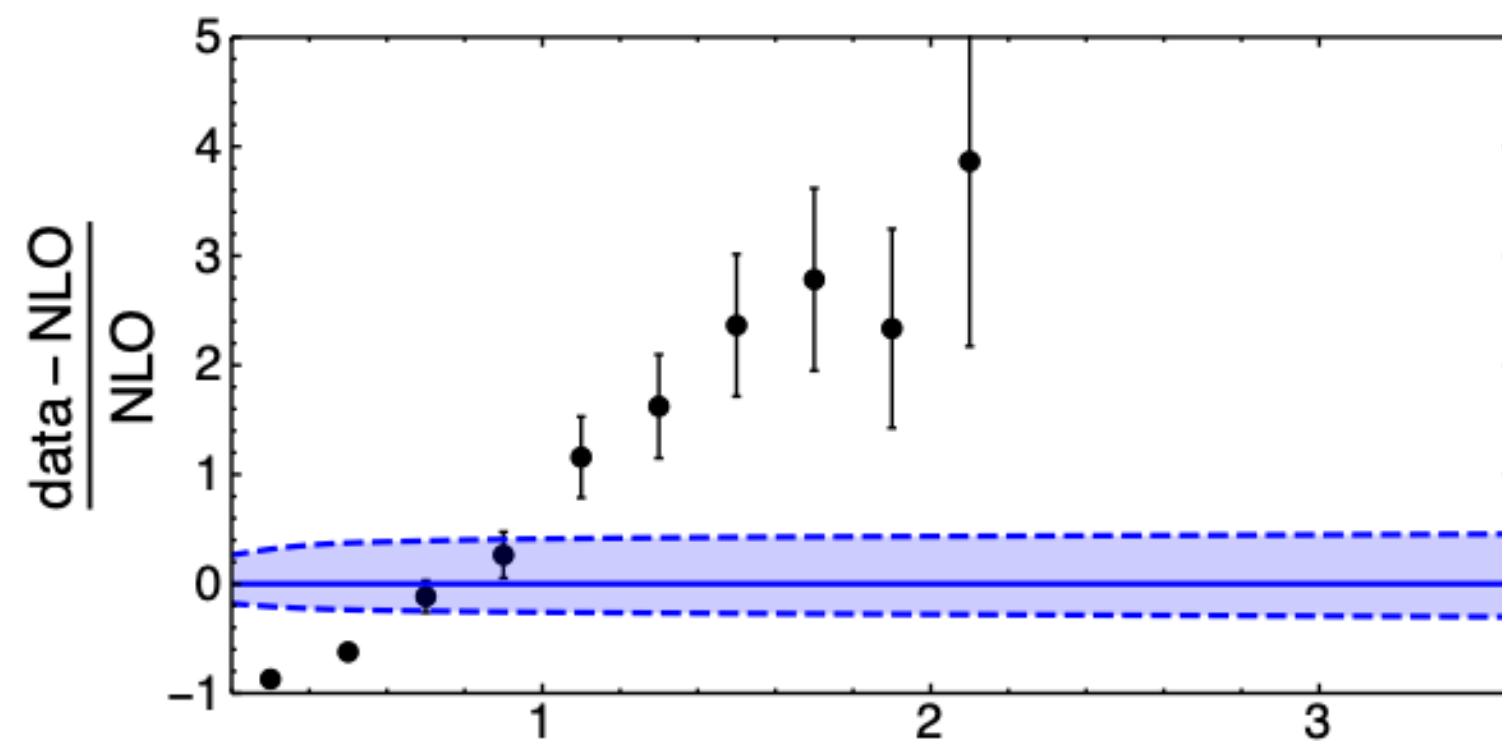
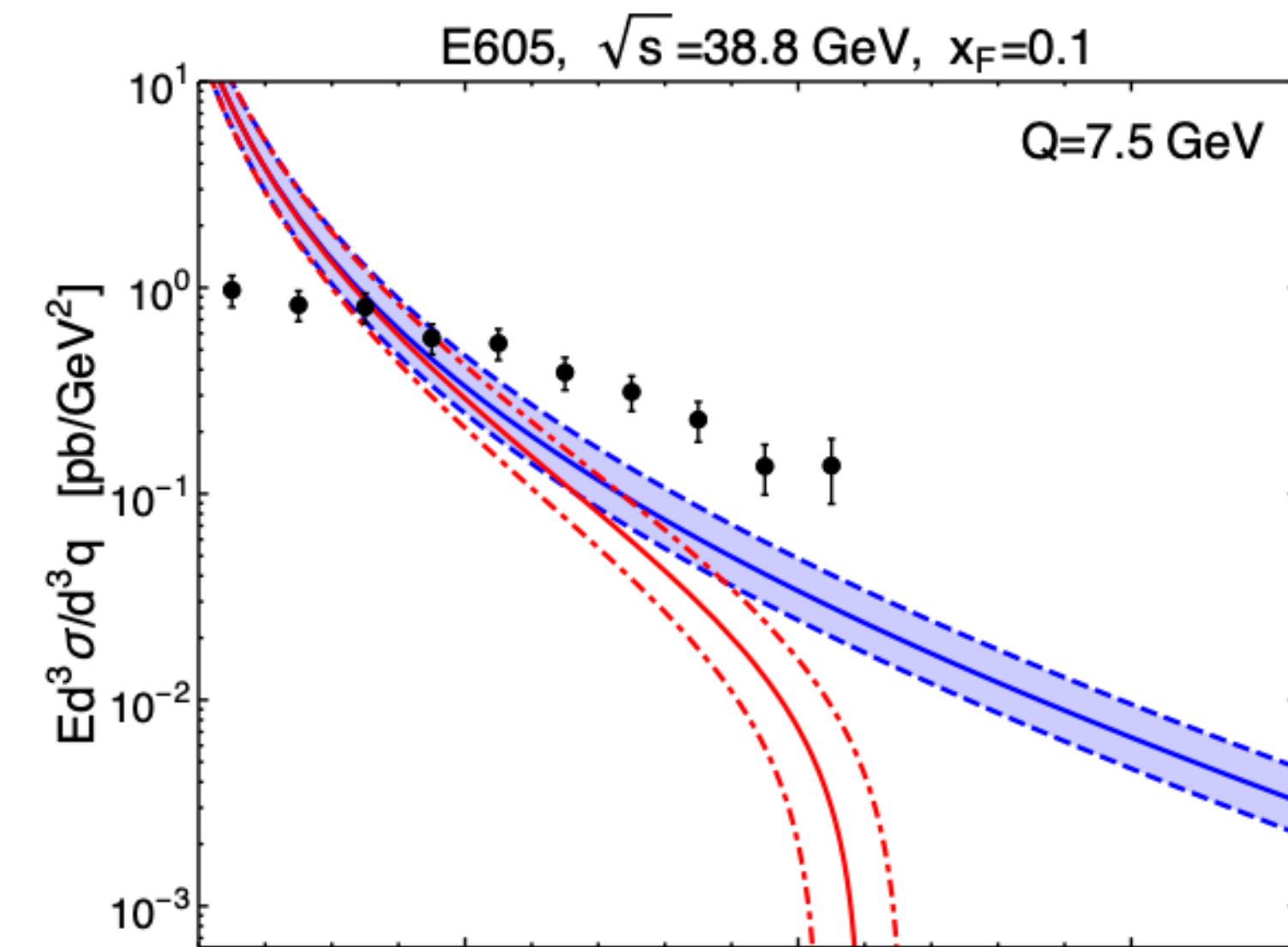
Study of low invariant mass data



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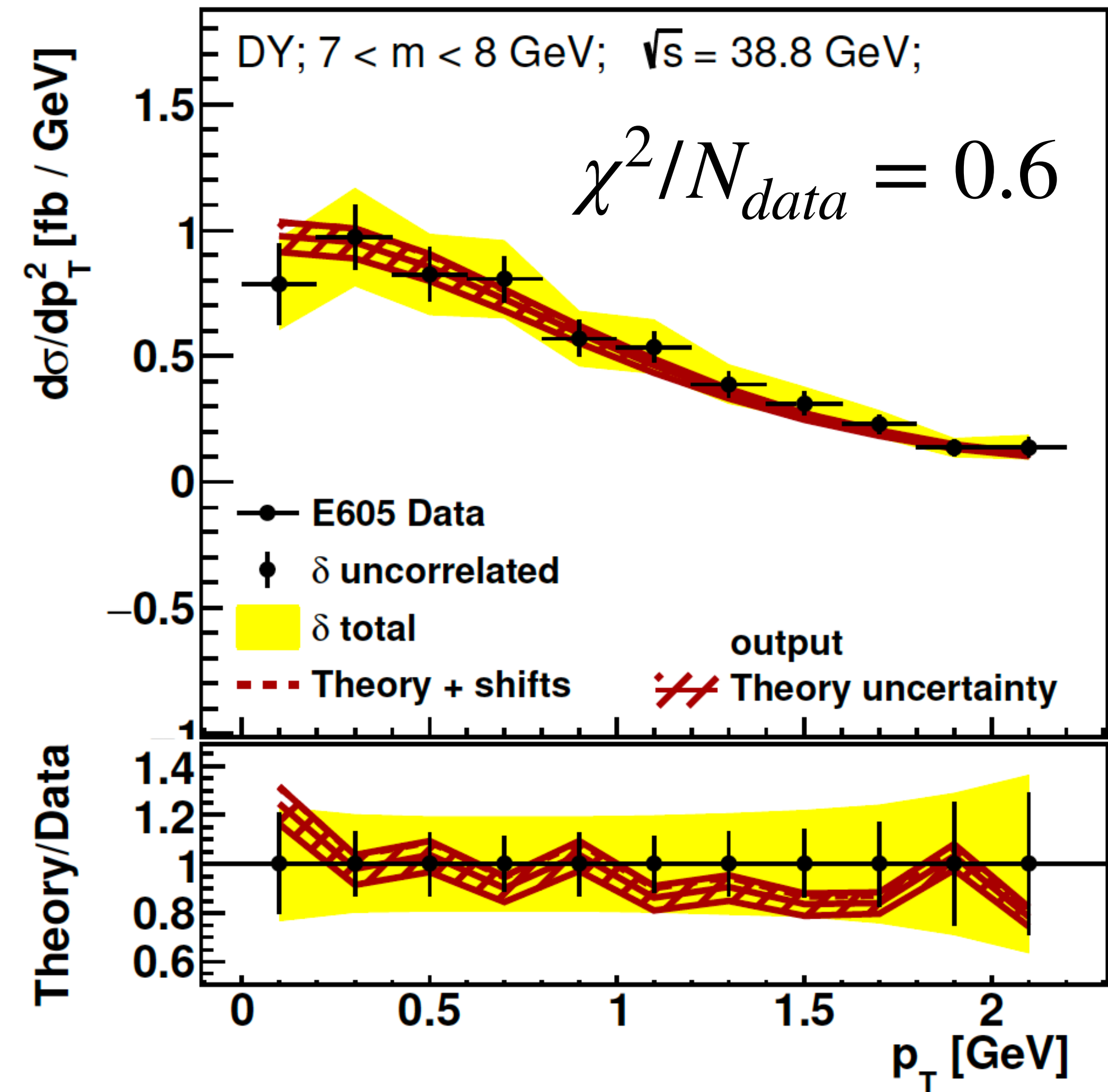


Study of low invariant mass data

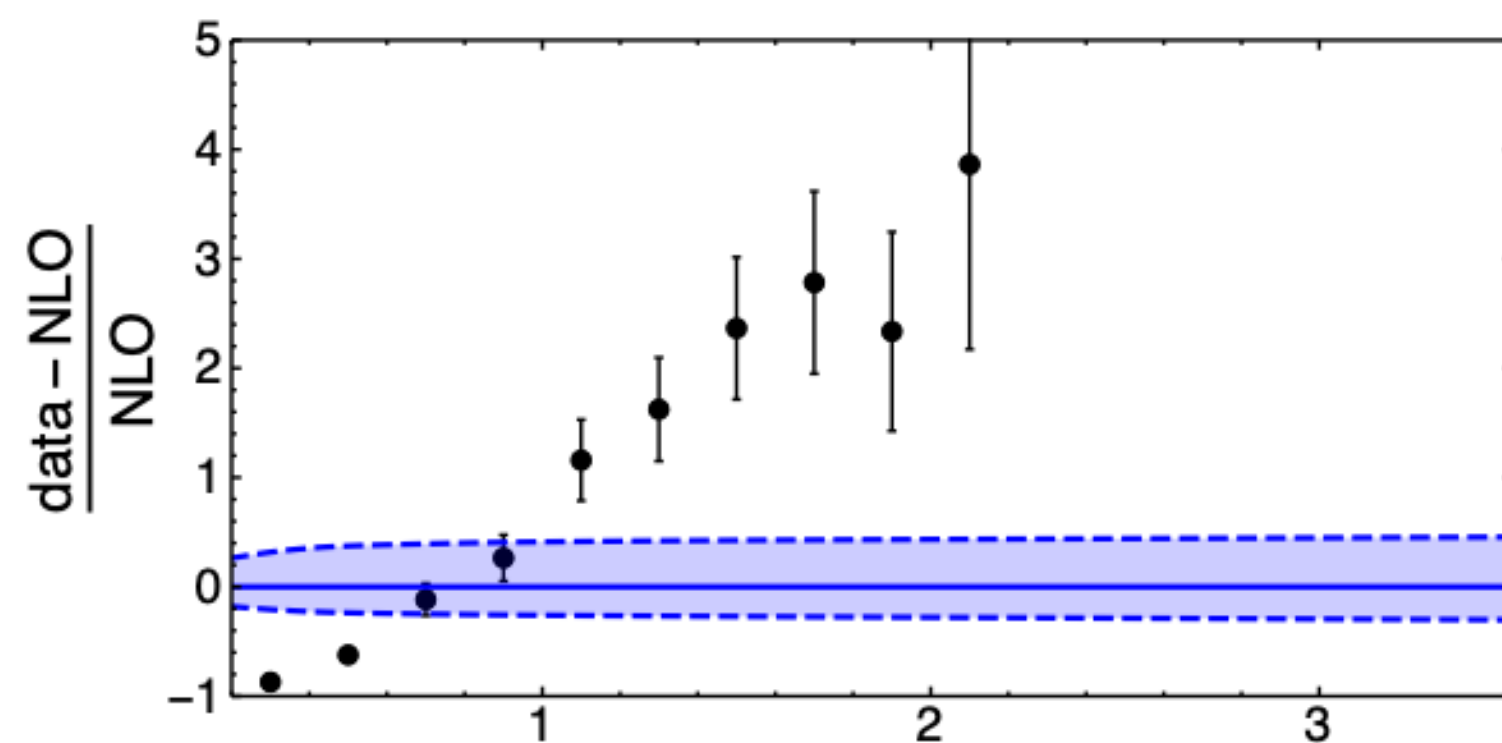
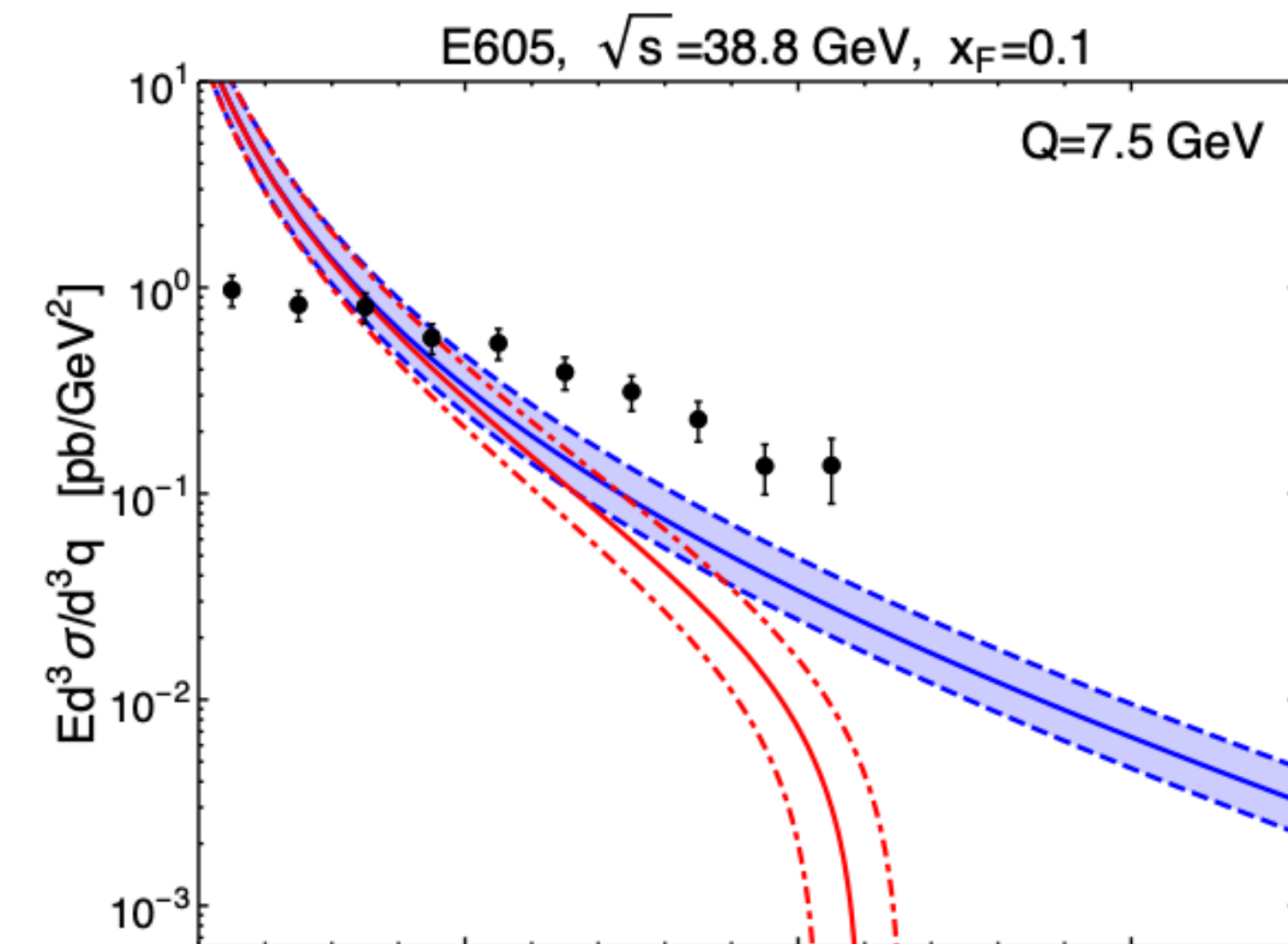


Phys.Rev.D 100 (2019) 1, 014018

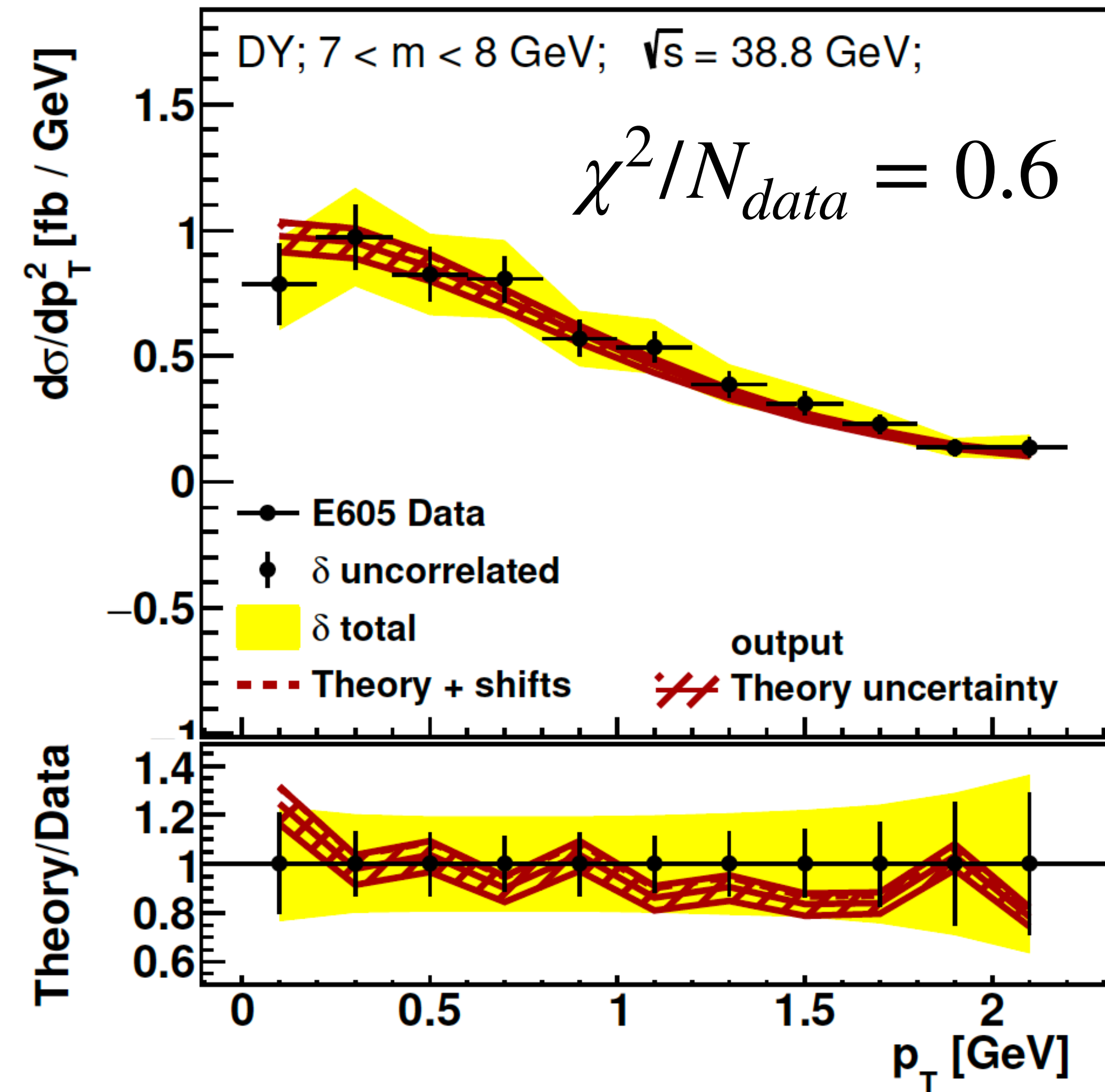
Starting point



Study of low invariant mass data



Phys.Rev.D 100 (2019) 1, 014018



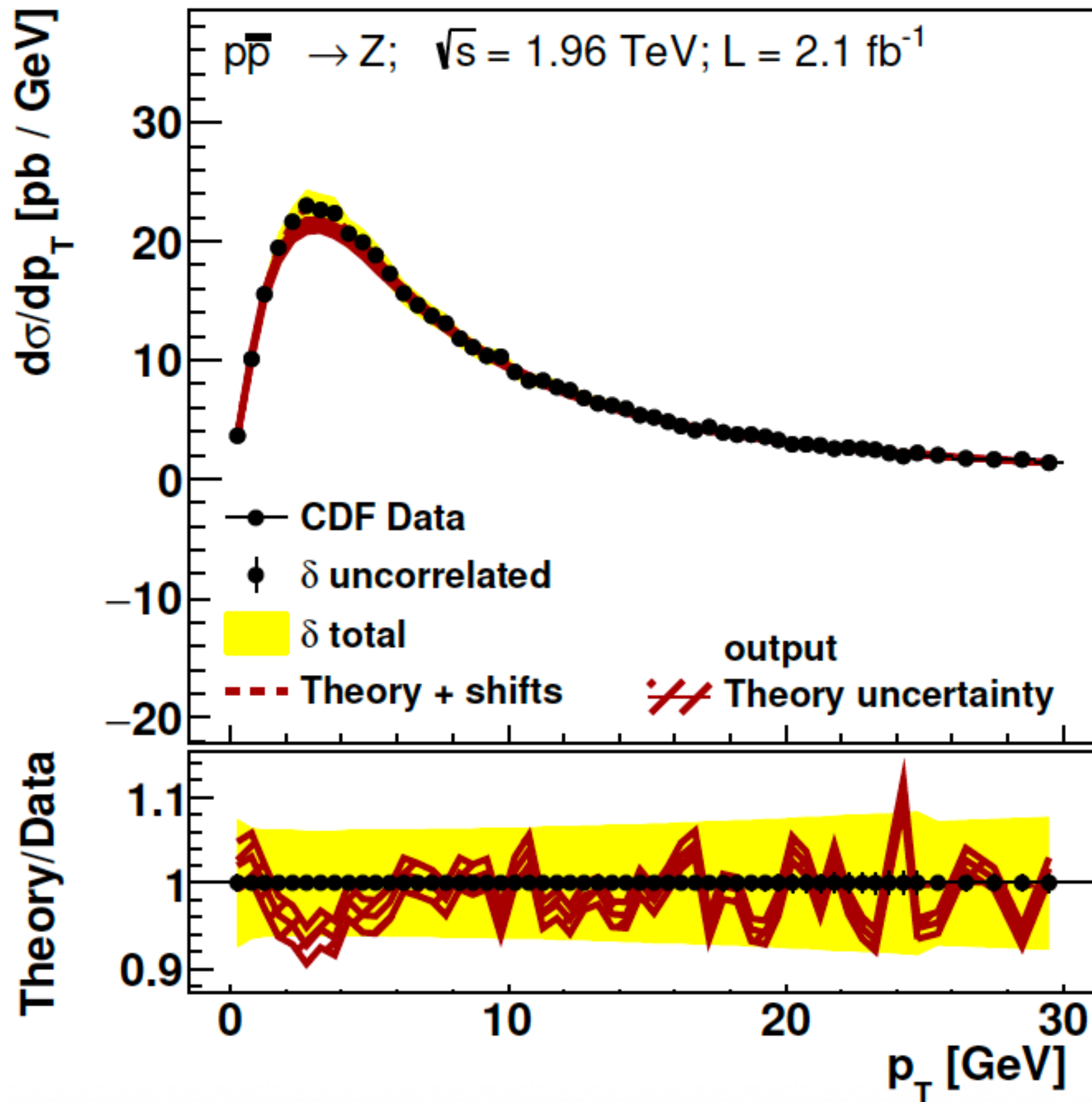
Starting point



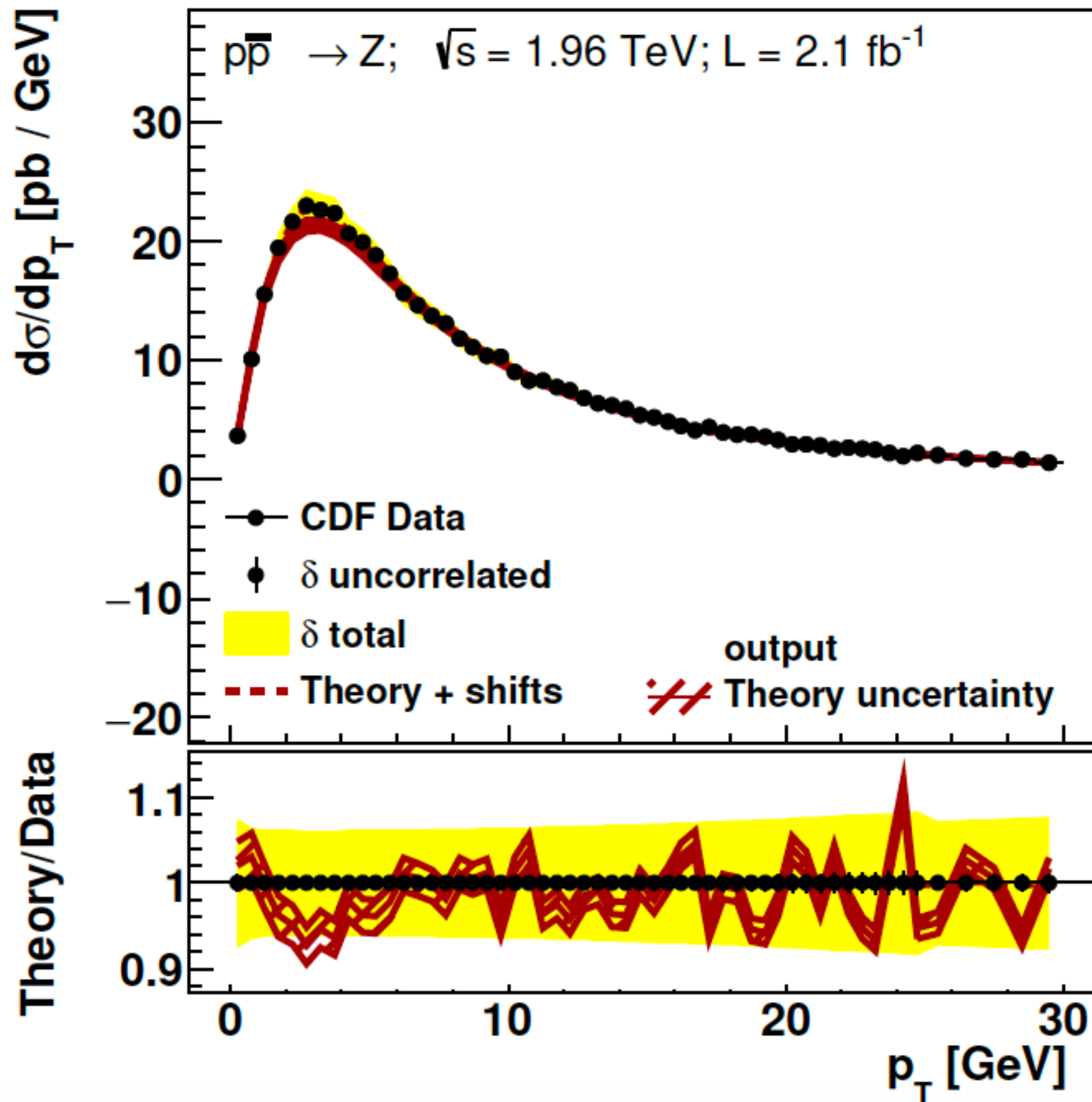
Arrival point

Study of low invariant mass data

Study of low invariant mass data



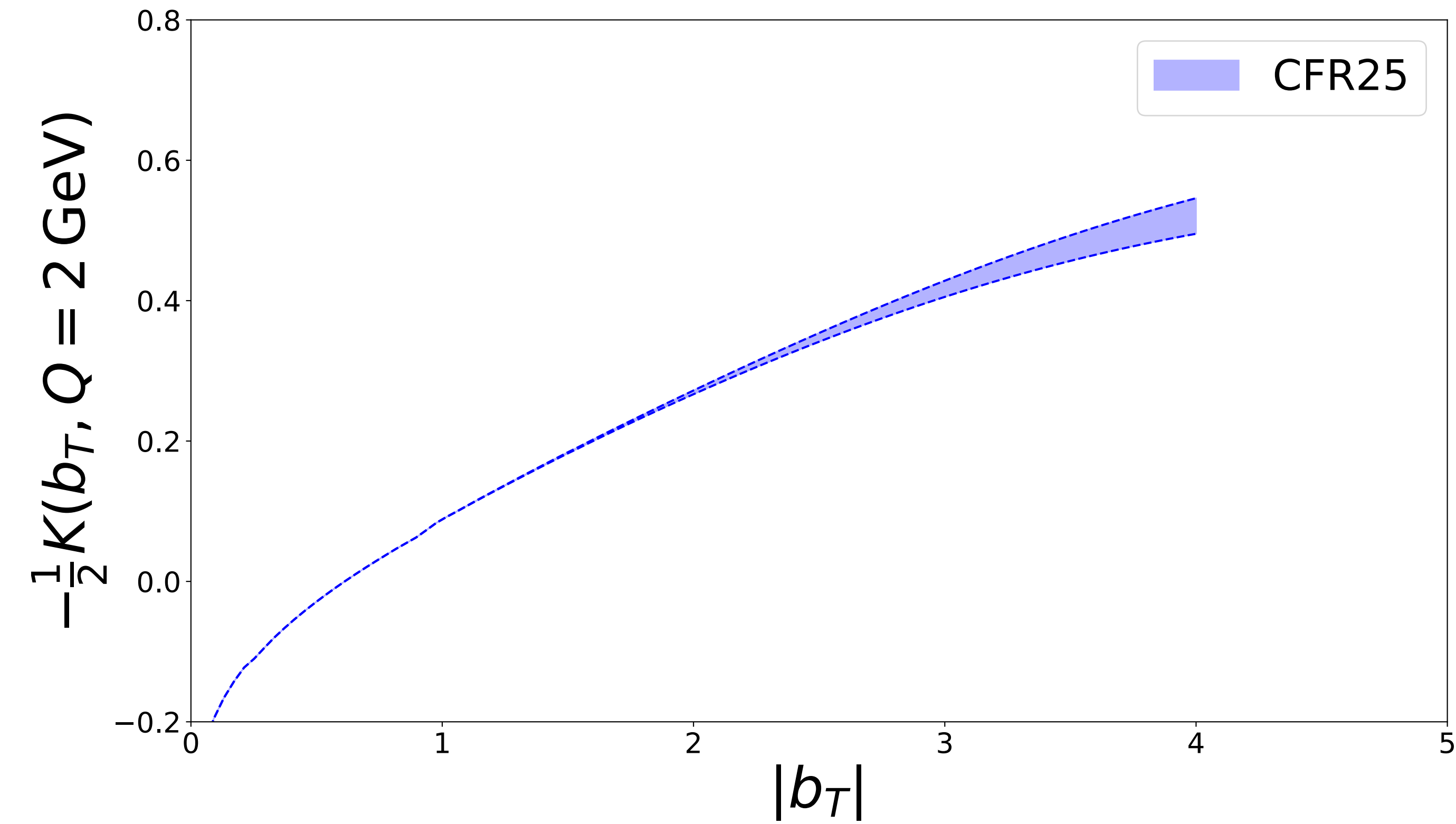
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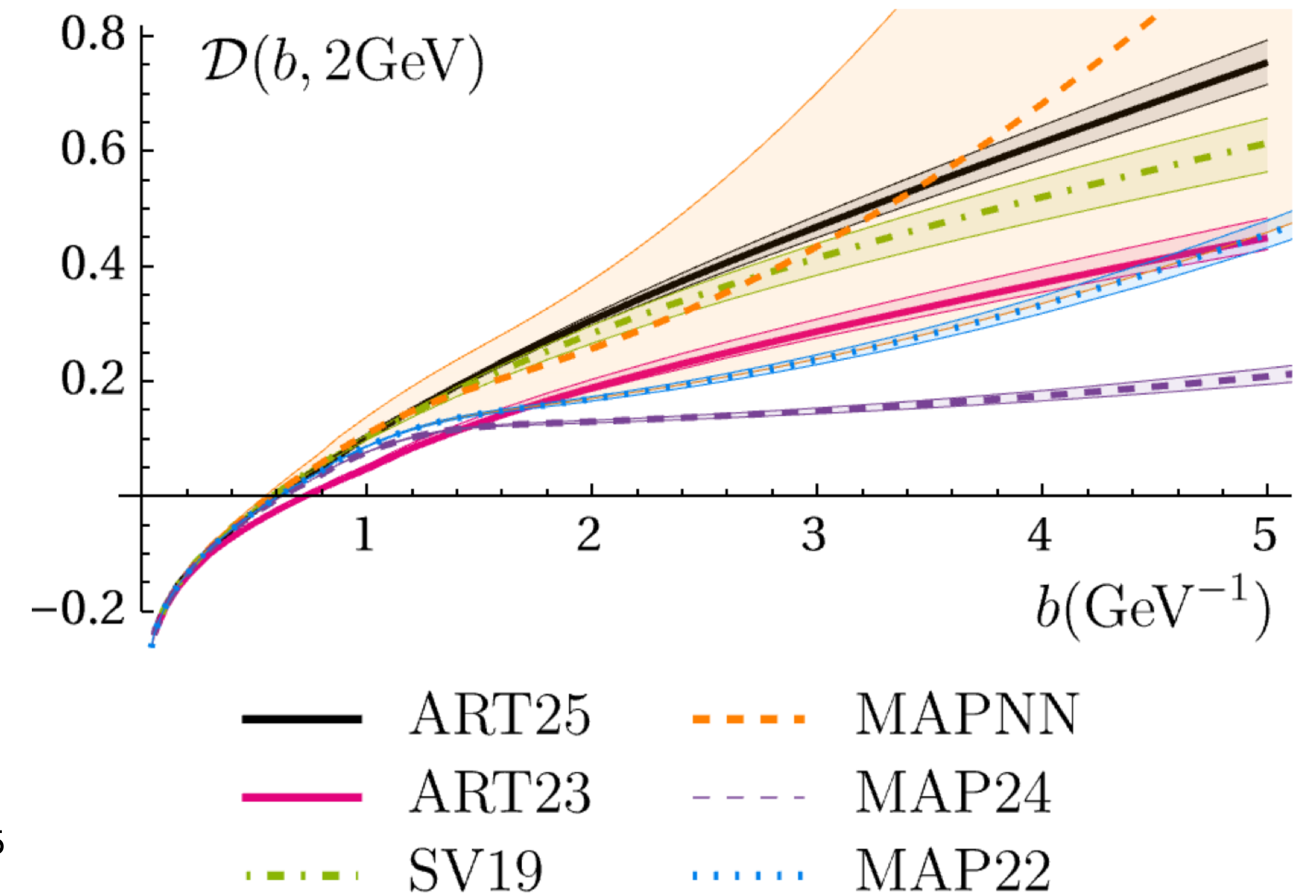
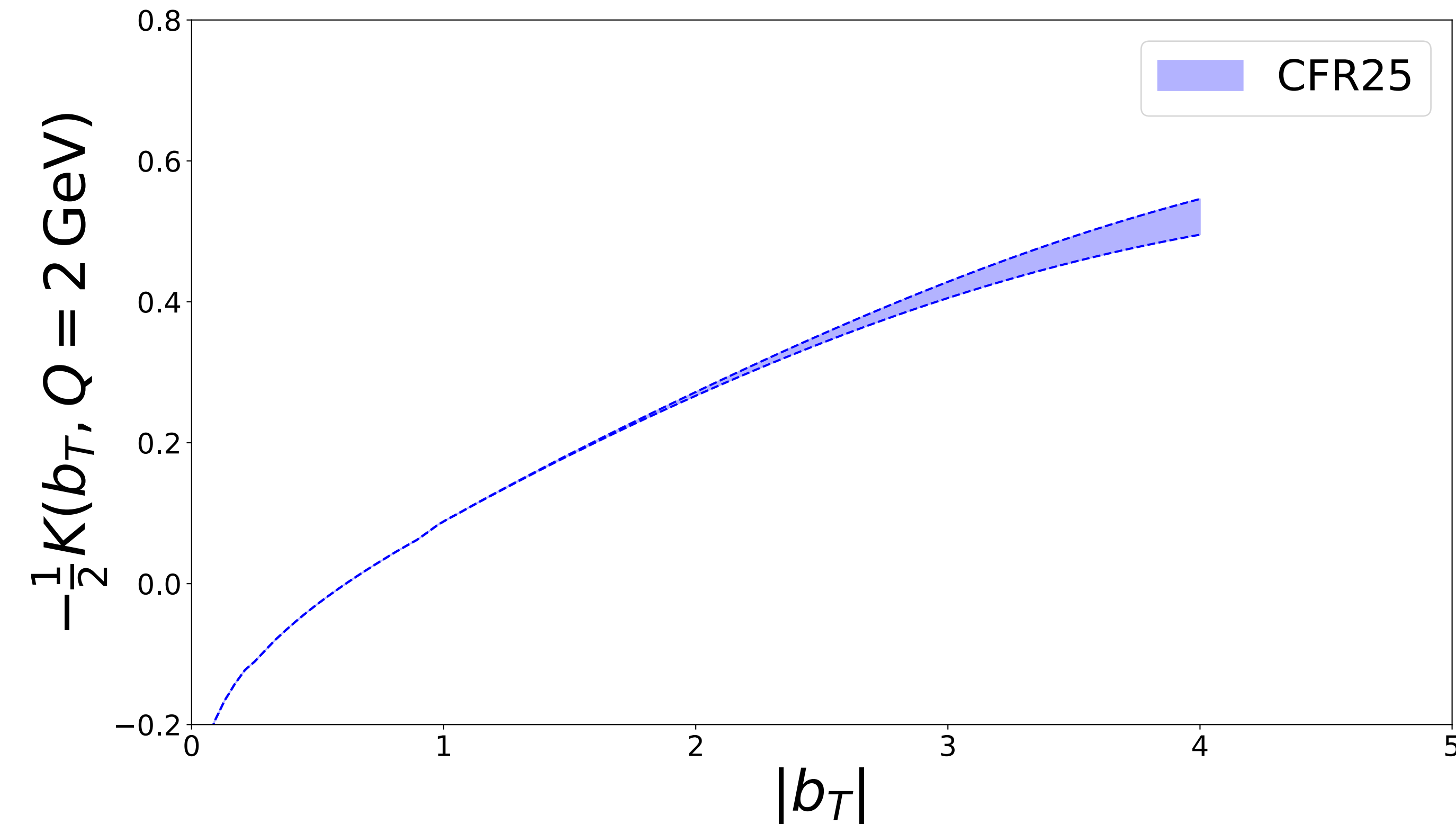
*High invariant mass data
remain well described*

Extracted Collins Soper Kernel

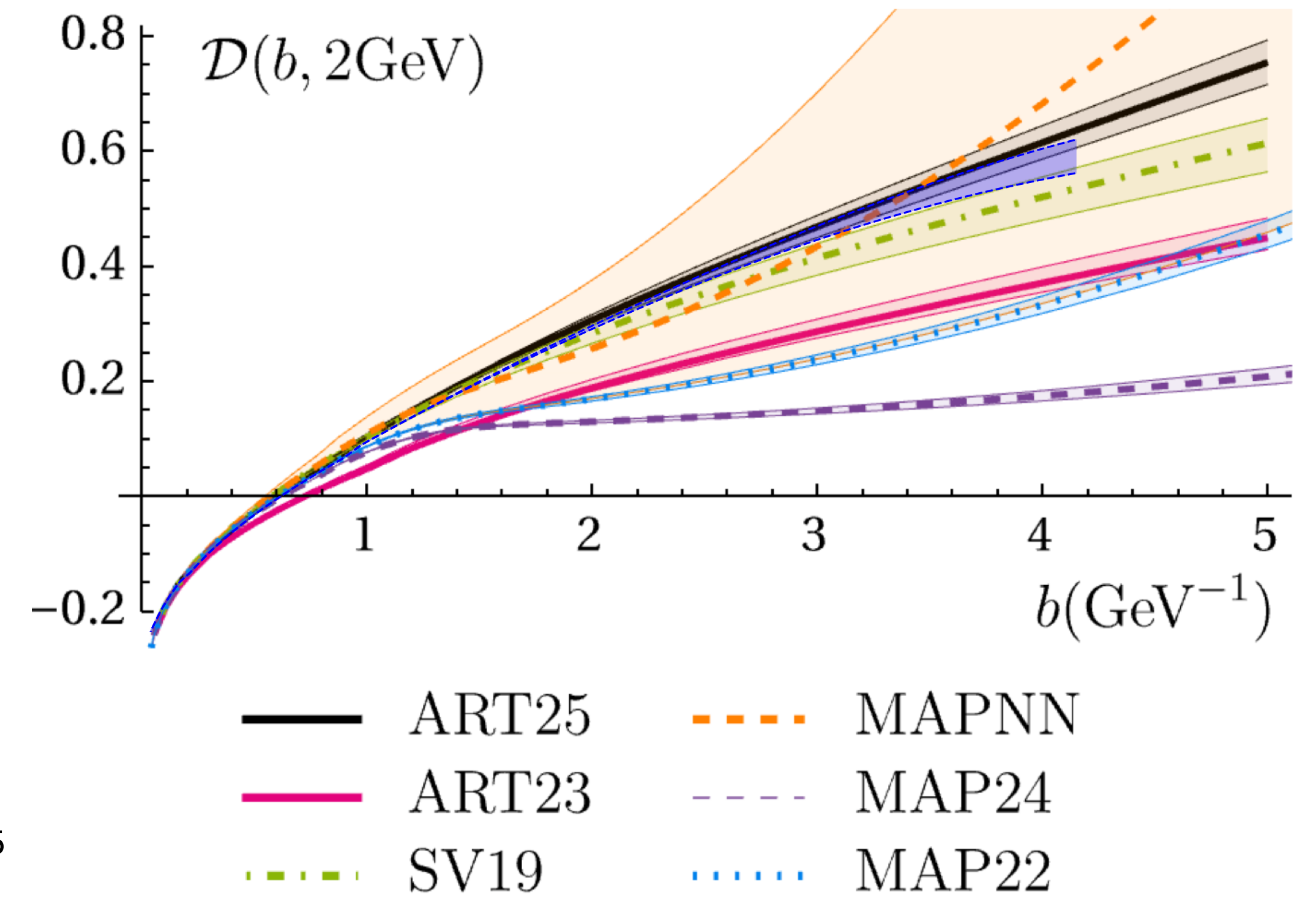
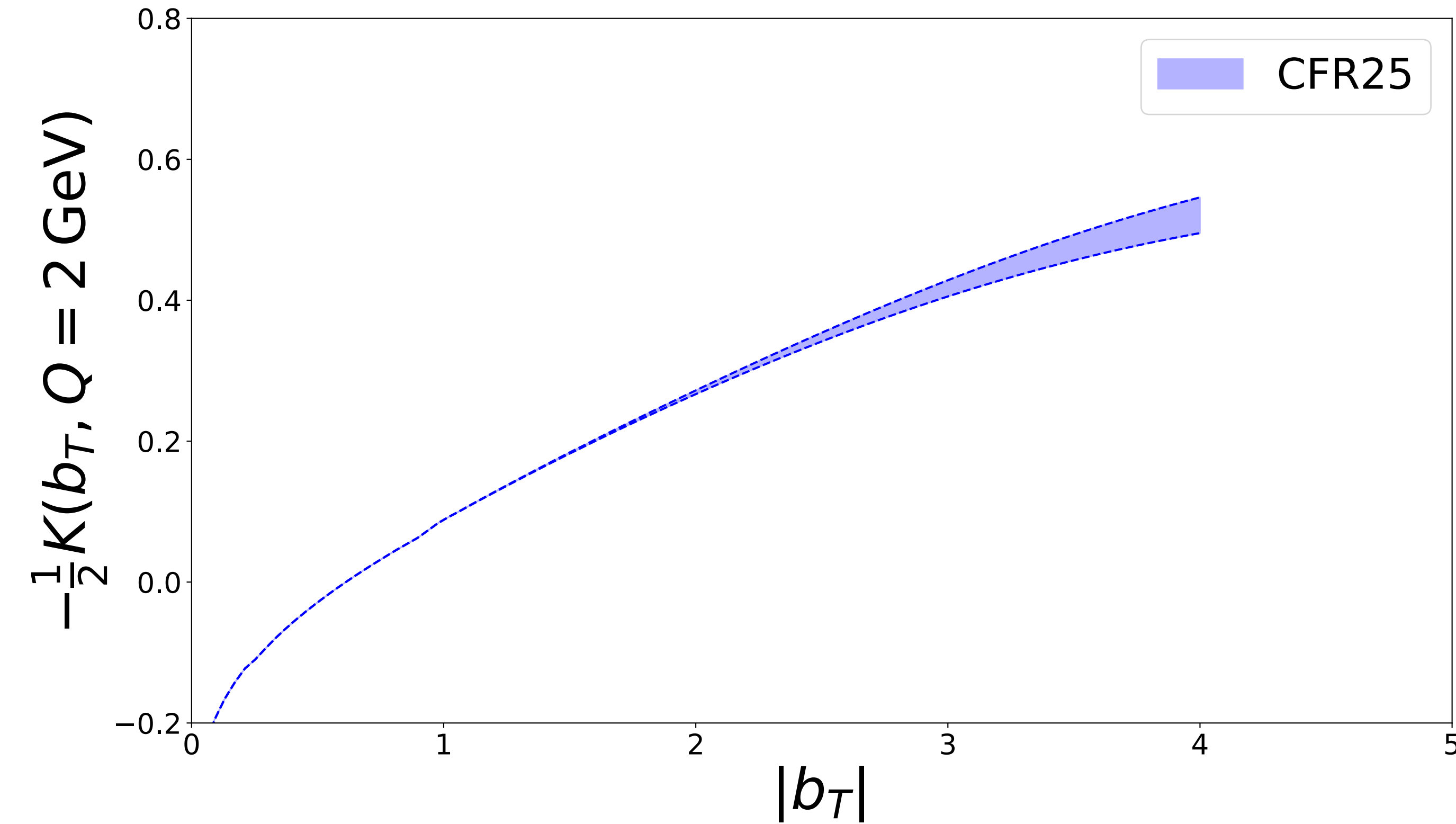
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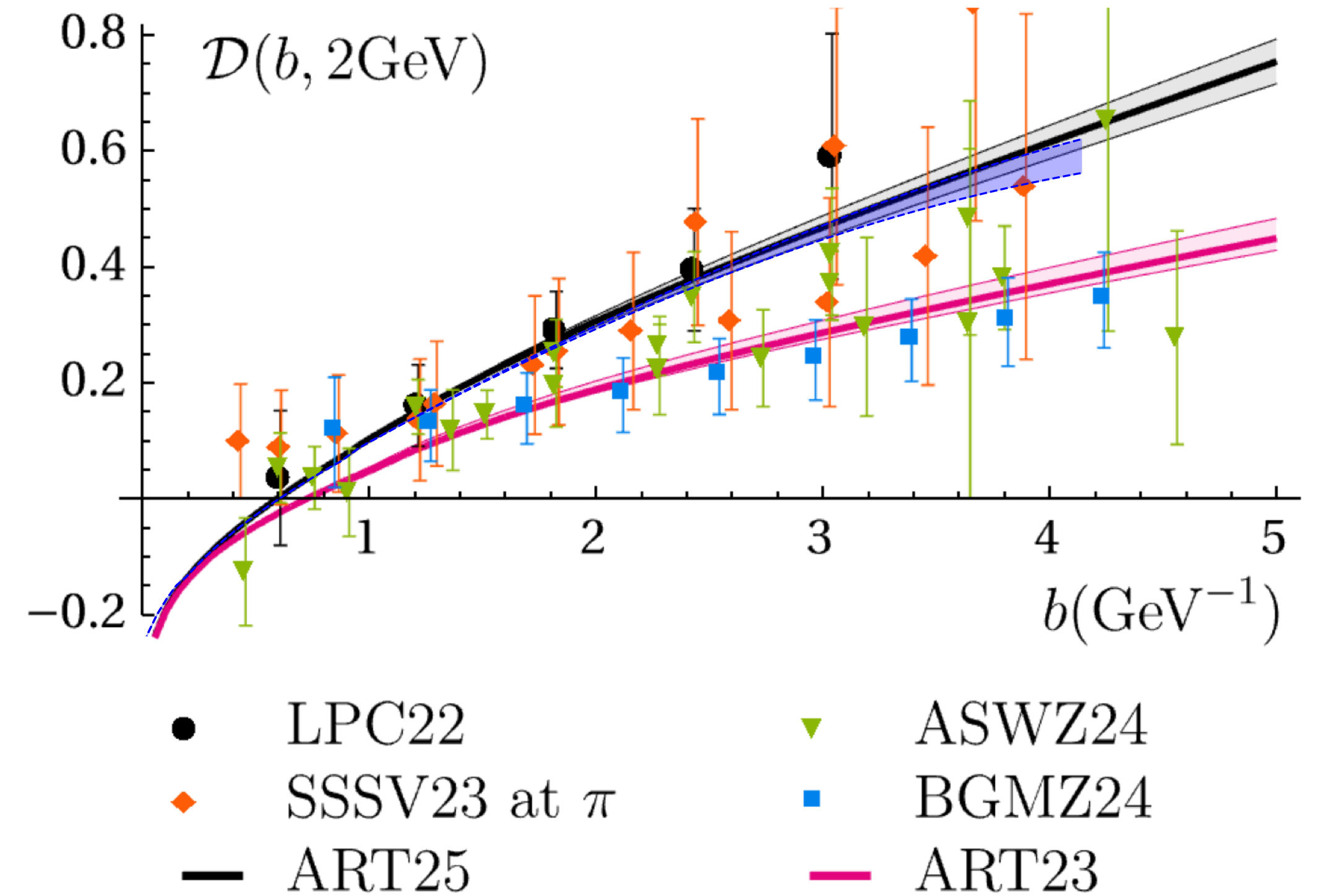
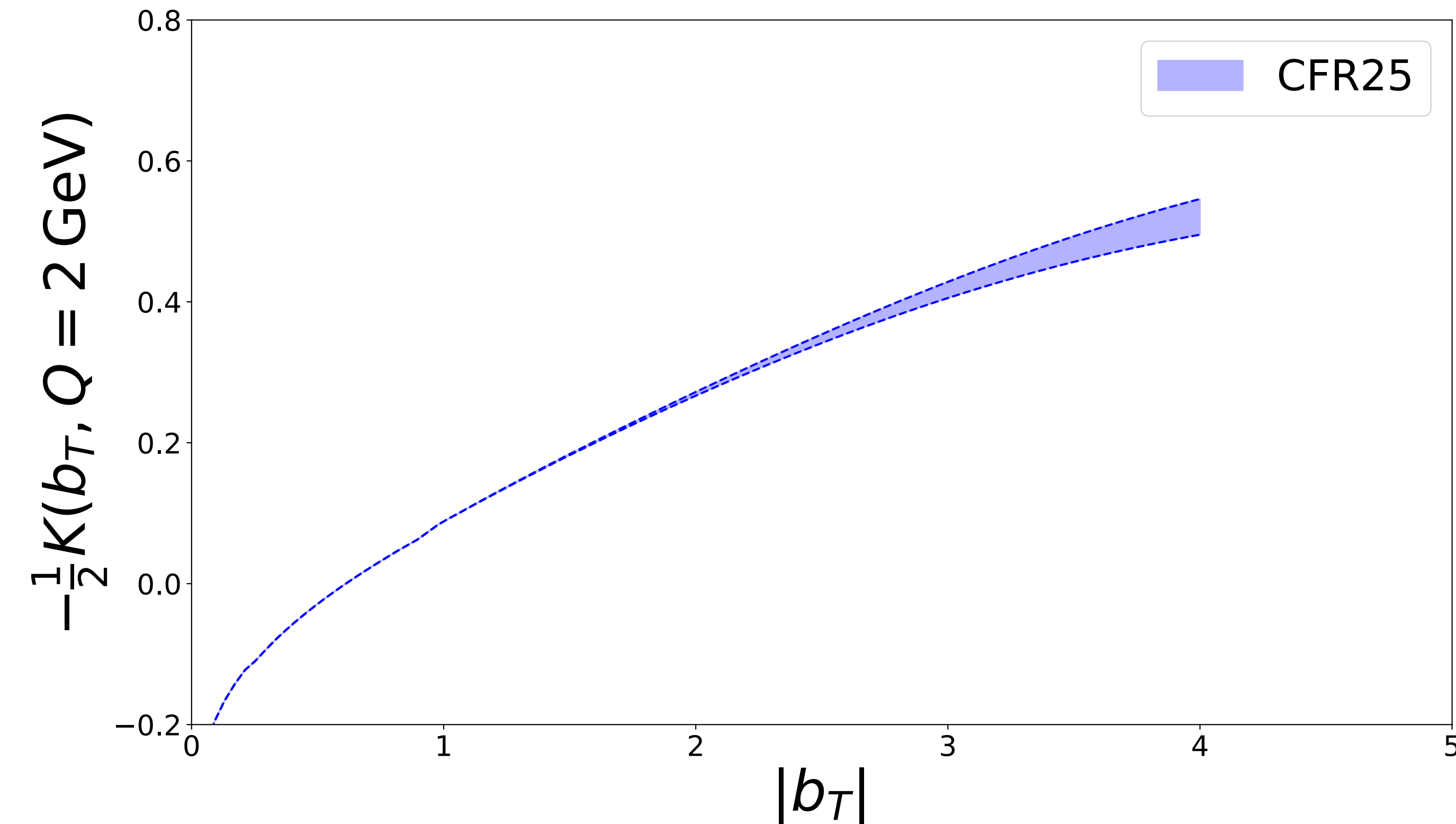
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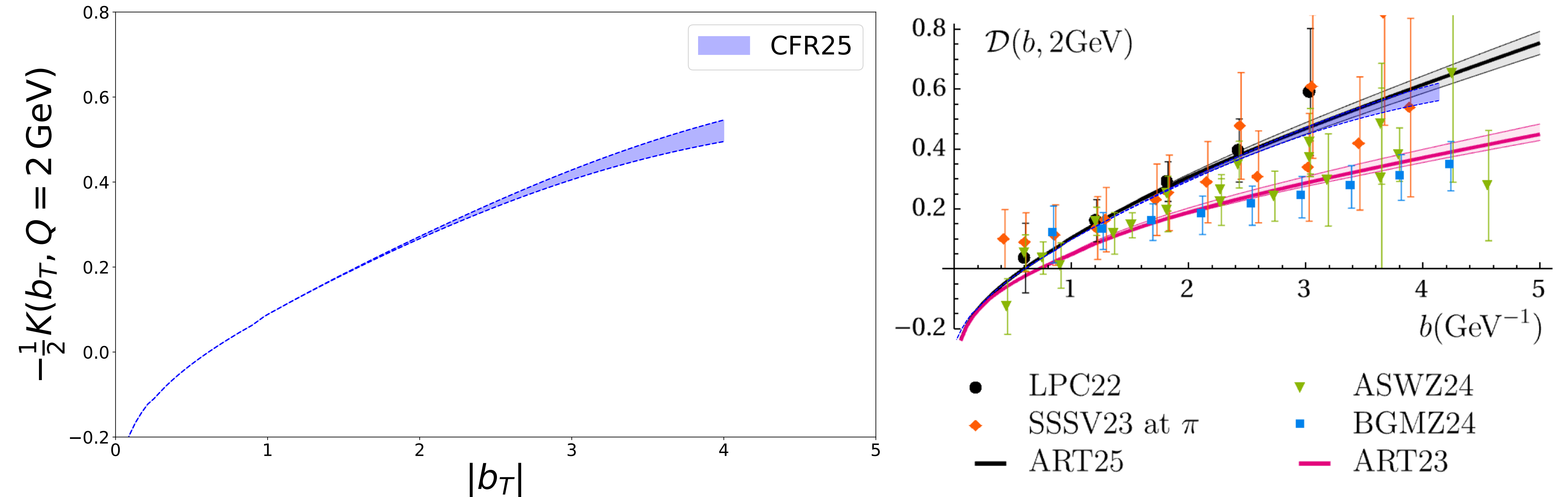
Extracted Collins Soper Kernel



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We are working on the choice of the non perturbative (hyper)parameters...

Conclusions and outlook

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- Study of the available data-sets

Resummation, Evolution, Factorization 2025

13–17 Oct 2025
Physics Department, Milan University
Europe/Rome timezone



Overview

Workshop venue

Registration

Registration #2: fee
payment

Call for Abstracts

Participant List

Timetable

Accommodation

Workshop dinner
(Wednesday 15/10)

Videoconference
information

Contact

