Hunting axion dark matter with anti-ferromagnets

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based on 2411.09761, 2411.11971 with Angelo Esposito and Shashin Pavaskar

Cortona, May 20th 2025

QCD axion

• The QCD axion is a very well motivated BSM particle.



• Explains the smallness of θ and can constitute DM in our Universe V(a)

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• How can we describe collective excitations in antiferromagnets?

Collective excitations à la HEP

All phases of matter spontaneously break spacetime and internal symmetries



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• At low energies, the system can be described by an EFT of Goldstones, organized in a derivative expansion

$$\mathscr{L}_{\mathrm{EFT}}(\pi,\partial\pi)\simeq\sum_{n,m}g_{n,m}(\pi,\partial\pi)\partial^n\pi^m$$



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• Similarly to the non-linear σ model, we can parametrize the fluctuations around the vacuum as [Esposito, Pavaskar, PRD 2023 - 2210.13516]

$$\hat{\boldsymbol{n}}_{I}(\boldsymbol{x},t) = \begin{bmatrix} e^{iJ_{1}\theta^{1}(\boldsymbol{x},t) + iJ_{2}\theta^{2}(\boldsymbol{x},t)} \hat{\boldsymbol{x}} \end{bmatrix}_{I} \xrightarrow{SO(3)_{\text{int}}} R^{J}_{I} \cdot \hat{\boldsymbol{n}}_{J}(\boldsymbol{x},t), \quad \sum_{I} (\hat{\boldsymbol{n}}_{I})^{2} = 1$$
magnon fields

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magnon fields

• At the lowest order in the derivative expansion, the most general Lagrangian density invariant under the internal SO(3)

$$\mathscr{L}_{0} = \frac{c_{1}}{2} \left[\partial_{t} \hat{n}^{I} \partial_{t} \hat{n}_{I} - v_{\theta}^{2} \left(\nabla_{i} \hat{n}^{I} \right) \left(\nabla_{i} \hat{n}_{I} \right) \right] \equiv \frac{c_{1}}{2} \left[(\partial_{t} \hat{n})^{2} - v_{\theta}^{2} (\nabla_{i} \hat{n})^{2} \right]$$

$$v_{\theta} \text{ from dispersion relations}$$

$$c_{1} \text{ from nuclear scattering}$$

$$\sigma_{n} \propto c_{1}$$

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- The gap depends on
 - * Crystalline structure (anisotropies λ)
 - \diamond External *magnetic* fields **B**

$\Delta = \Delta(\lambda, B)$







Magnons full EFT

• For small magnetic fields, i.e. $B < B_{s.f.}$, then [PGC, Esposito, Pavaskar, 2411.09761, 2411.11971]

$$\hat{\boldsymbol{n}}_{I}(\boldsymbol{x},t) = \left[\exp\left(iS_{a}\theta^{a}\right)\hat{\boldsymbol{z}}\right]_{I}$$
$$\mathscr{L}_{\text{EFT}} = \frac{c_{1}}{2}\left[\left(\dot{\theta}^{a} - \mu B\epsilon^{ab}\theta^{b}\right)^{2} - v_{\theta}^{2}(\nabla\theta^{a})^{2} - 2\lambda_{z}(\theta^{a})^{2} - 2\lambda_{x}\delta^{a2}\delta^{b2}\theta^{a}\theta^{b} + \mathcal{O}(\theta^{4})\right]$$
$$a, b = 1,2$$

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• Computing the spectrum of \mathscr{L}_{EFT} one finds two modes:







• NR limit + selection of the right d.o.f.

[PGC, Esposito, Pavaskar, 2411.11971]

$$\mathscr{L}_{a} \supset \frac{g_{aee}}{2m_{e}} \partial_{\mu} a \ \overline{e} \gamma^{\mu} \gamma_{5} e \xrightarrow{\text{NR}} \frac{g_{aee}}{m_{e}} \nabla a \cdot \left(e_{\text{nr}}^{\dagger} \frac{\boldsymbol{\sigma}}{2} e_{\text{nr}} \right) \xrightarrow{\text{IR}} \frac{g_{aee}}{m_{e}} \overrightarrow{\nabla} a \cdot \overrightarrow{s}$$

 $\vec{s}(\theta)$ spin density

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 The spin density is easily computed as the SO(3) Noether current in the EFT

$$s^{I} = c_{1} \Big[\Big(\partial_{t} \hat{\boldsymbol{n}} \times \hat{\boldsymbol{n}} \Big)^{I} + \mu (\boldsymbol{B} \cdot \hat{\boldsymbol{n}}) \, \hat{\boldsymbol{n}}^{I} \Big] \simeq c_{1} \Big[\delta^{Ia} \Big(\dot{\theta}^{a} - \mu B \epsilon^{ab} \theta^{b} \Big) - \delta^{I3} \theta^{a} \Big(\epsilon^{ab} \dot{\theta}^{b} + \gamma B \theta^{a} \Big) + \dots \Big]$$

1Kg year exposure



$$R(\hat{\mathbf{v}}_{e}) = \frac{\rho_{a}}{\rho_{T} m_{a}} \int d^{3}v f(|\vec{\mathbf{v}} + \vec{\mathbf{v}}_{e}|) \Gamma(\vec{\mathbf{v}})$$

1Kg year exposure





Directional system



Directional system

Efficient strategy to discriminate between signal and background ~300 % directionality

Observables?





Observables?











- How to enhance this tiny signal?
 - ★ SQUID?
 - ★ Magnetic Haloscope?

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Thank you for the attention!