

Work Fluctuations for Active Particles: singularities, dynamical phase transitions and big jumps

Wednesday, 21 May 2025 16:55 (15 minutes)

Active Particles are physical entities able to transform energy from the environment or internal reservoirs into directed self-propelled motion. From a theoretical standpoint, in recent years this class of systems generated great interest in statistical mechanics due to the display of intriguing new properties as motility-induced phase separation [1], an inherent out of equilibrium character [2] and the occurrence of singularities in distributions of integrated observables. The latter are in turn associated to Dynamical Phase Transitions (DPTs) [3], i.e. changes in the dynamical behavior of the system in different fluctuation regimes separated by singularities. In this respect, Active Work, i.e. the work performed by the self-propulsion force, emerged as a key observable to monitor in active systems as at the same time it quantifies how efficiently energy is transformed into self-propulsion [4], it is strictly related to entropy production [2] and its singular distribution signals DPTs [5].

In this talk we will present a summary of our results on this subject. After briefly reviewing the case of a single free Active Ornstein-Uhlenbeck Particle (AOUP) from [4], in which DPTs do not occur, we will consider the case of a single AOUP under the effect of a confining harmonic potential from [6]. The simple but non-trivial framework of a single particle allowed us to tackle the problem analytically for both stationary and generic uncorrelated initial states. In particular, we adopted the general Large Deviations approach we developed in [7] for quadratic functionals of Gauss-Markov chains. Our results showed that harmonic confinement can indeed induce singularities in the Active Work Rate Function, with linear tails at large positive and negative values appearing for sufficiently large self-propulsion force, harmonic confinement and/or initial values. In addition, by looking at the system trajectories, we discovered these singularities to be associated to DPTs, which in turn are originated by concentrated large values, or big jumps, in the displacement and the self-propulsion force at the initial or ending points of trajectories. In order to show that these big jumps represent a general mechanism for Brownian particles, we will show that analogous results are obtained also for the work injected by the random noise on a passive underdamped Brownian particle studied in [8]. Overall, our results provide a connection between DPTs and a condensation-like physical mechanism and clarify the relevance of boundary terms in the problem at hand.

- [1] Motility-Induced Phase Separation, M. E. Cates and J. Tailleur, Annual Review of Condensed Matter Physics (6) 2015
- [2] Irreversibility and Biased Ensembles in Active Matter: Insights from Stochastic Thermodynamics, E. Fodor, R. L. Jack, and M. E. Cates, Annual Review of Condensed Matter Physics (13) 2022
- [3] A first-order dynamical transition in the displacement distribution of a driven run-and-tumble particle, G. Gradenigo and S. N. Majumdar, Journal of Statistical Mechanics: Theory and Experiment (5) 2019
- [4] Work fluctuations in the active Ornstein-Uhlenbeck particle model, M. Semeraro, A. Suma, I. Petrelli, F. Cagnetta, and G. Gonnella, Journal of Statistical Mechanics: Theory and Experiment (12) 2021
- [5] Large fluctuations and dynamic phase transition in a system of self-propelled particles, F. Cagnetta, F. Corberi, G. Gonnella, and A. Suma, Physical review letters (119) 2017
- [6] Work Fluctuations for a Harmonically Confined Active Ornstein-Uhlenbeck Particle, M. Semeraro, G. Gonnella, A. Suma, and M. Zamparo, Physical Review Letters (131) 2023
- [7] Large deviations for quadratic functionals of stable Gauss-Markov chains and entropy production, M. Zamparo and M. Semeraro, Journal of Mathematical Physics (64) 2023
- [8] Work fluctuations for a confined Brownian particle: the role of initial conditions, G. B. Carollo, M. Semeraro, G. Gonnella and M. Zamparo, Journal of Physics A: Mathematical and Theoretical (43) 2023

Primary authors: Dr SEMERARO, Massimiliano (Università di Bari and INFN Bari); Dr SUMA, Antonio (Università di Bari and INFN Bari); Dr ZAMPARO, Marco (Università del Piemonte Orientale); Prof. GONNELLA, Giuseppe (Università di Bari and INFN Bari)

Presenter: Dr SEMERARO, Massimiliano (Università di Bari and INFN Bari)

Session Classification: Applied theory