



# Atom interferometry gyroscopes

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# Outline



- Atom interferometry: basic principles
- AI inertial sensors: state of the art
- The MAGIA experiment
- Performance of current AI gyroscopes
- Future of AI inertial sensors
  - transportable systems
  - new applications
  - combination with “classical” sensors

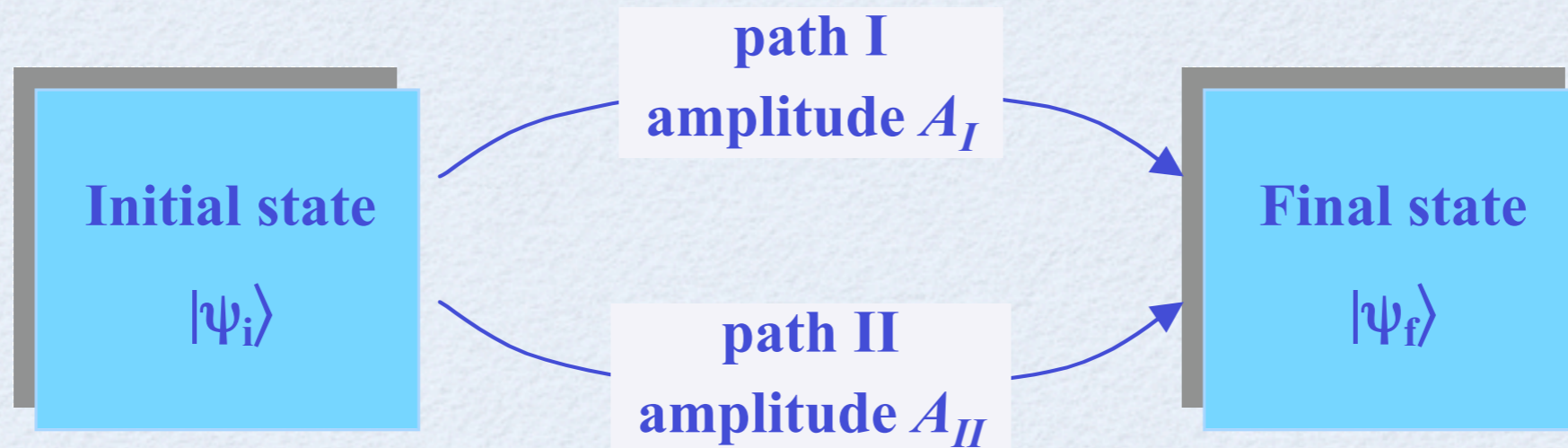




# Matter-wave interferometry



## *Quantum interference*



Interference of transition amplitudes

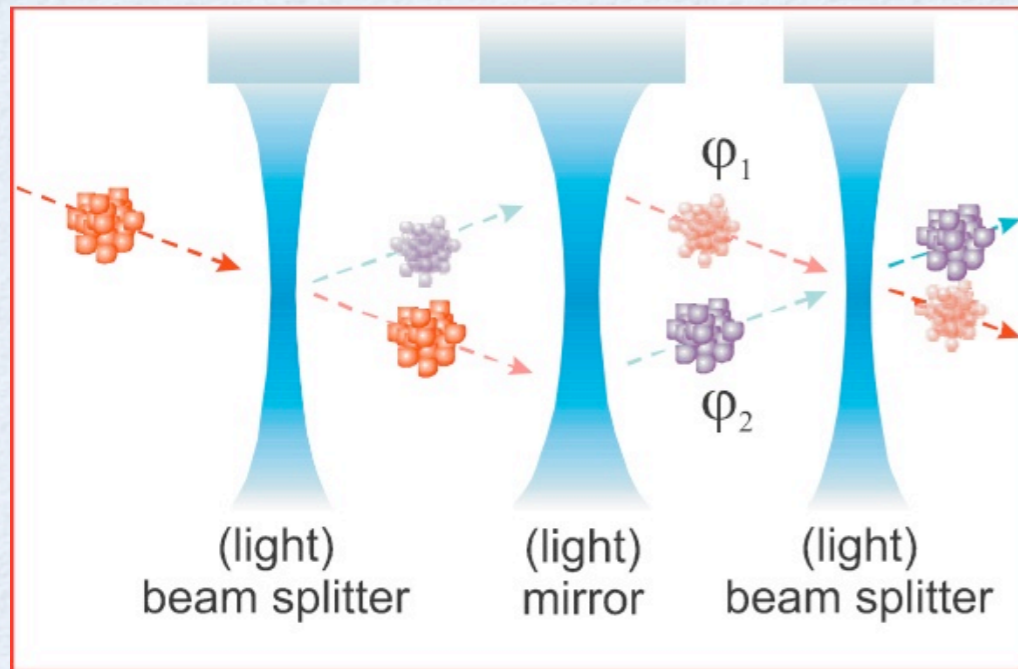
$$P(|\psi_i\rangle \rightarrow |\psi_f\rangle) = |A_I + A_{II}|^2 = |A_I|^2 + |A_{II}|^2 + 2\text{Re}(A_I A_{II}^*)$$

de Broglie wave  $\lambda_{dB} = h/mv$

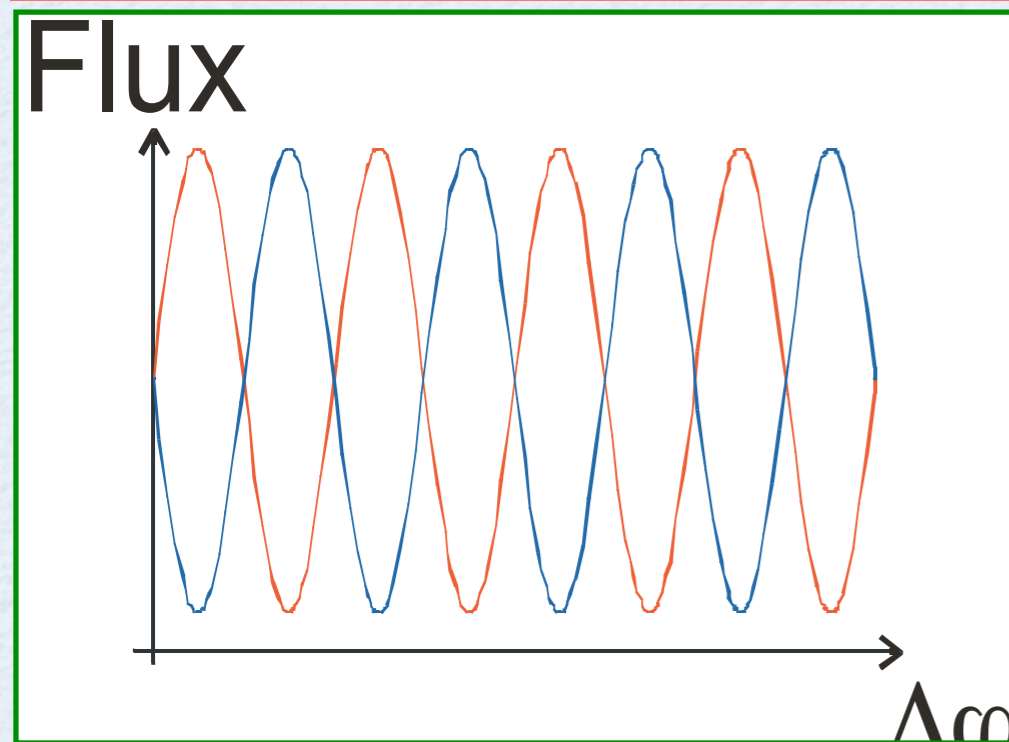
- *with electrons since 1953*
- *with neutrons since 1974*
- *with atoms since 1991*



# Atom interferometry



- atom optics
- different internal states / isotopes
- phase difference may depend on:
  - accelerations
  - rotations
  - photon recoil
  - laser phase
  - laser frequency detuning
  - electric / magnetic fields
  - interactions with atoms / molecules



atomic flux at **exit** port 1  
at **exit** port 2





# Possible applications of AI

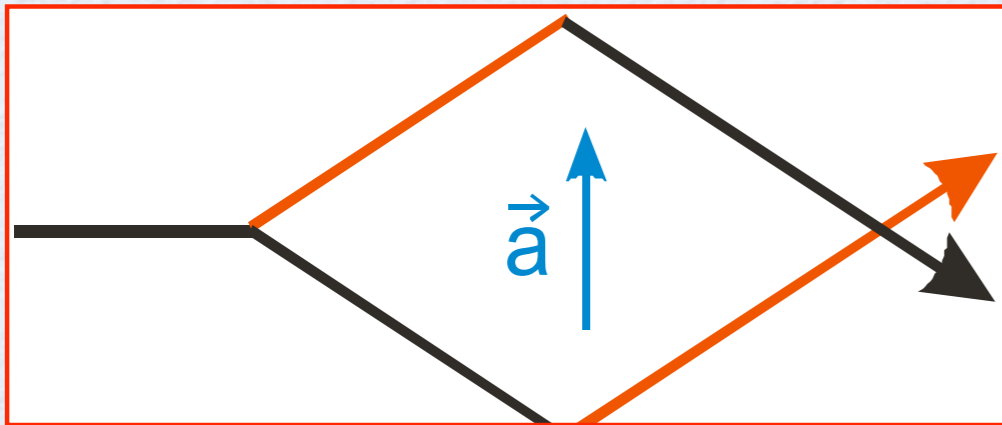


- Already achieved:
  - inertial sensing (accelerations, gravity gradients, rotations)
  - measuring fundamental constants ( $\alpha$ ,  $G$ )
- Proposed:
  - tests of GR (equiv. principle, limits on PPN parameters, Lense-Thirring, etc. )
  - GW detection
  - atom neutrality
  - testing Newton's  $1/r^2$  law at short distance
  - realization of mass unit (Watt balance)



# Matter-wave vs optical inertial sensors

## Accelerations



$$\Delta\Phi_{acc} = kT_{drift}^2 \cdot a$$

$$\frac{\Delta\phi_{mat}}{\Delta\phi_{ph}} \sim \left(\frac{c}{v_{at}}\right)^2 \approx 10^{11} \div 10^{17}$$

## Rotations



$$\Delta\Phi_{rot} = 2\pi \frac{2m_{at}}{h} A \cdot \Omega$$

$$\frac{\Delta\phi_{mat}}{\Delta\phi_{ph}} \sim \frac{m_{at}\lambda c}{h} \approx 5 \cdot 10^{11}$$

- in principle, excellent sensitivity
- good control over systematic effects
  - based on quantum matter-light interaction
  - many “knobs” to tune





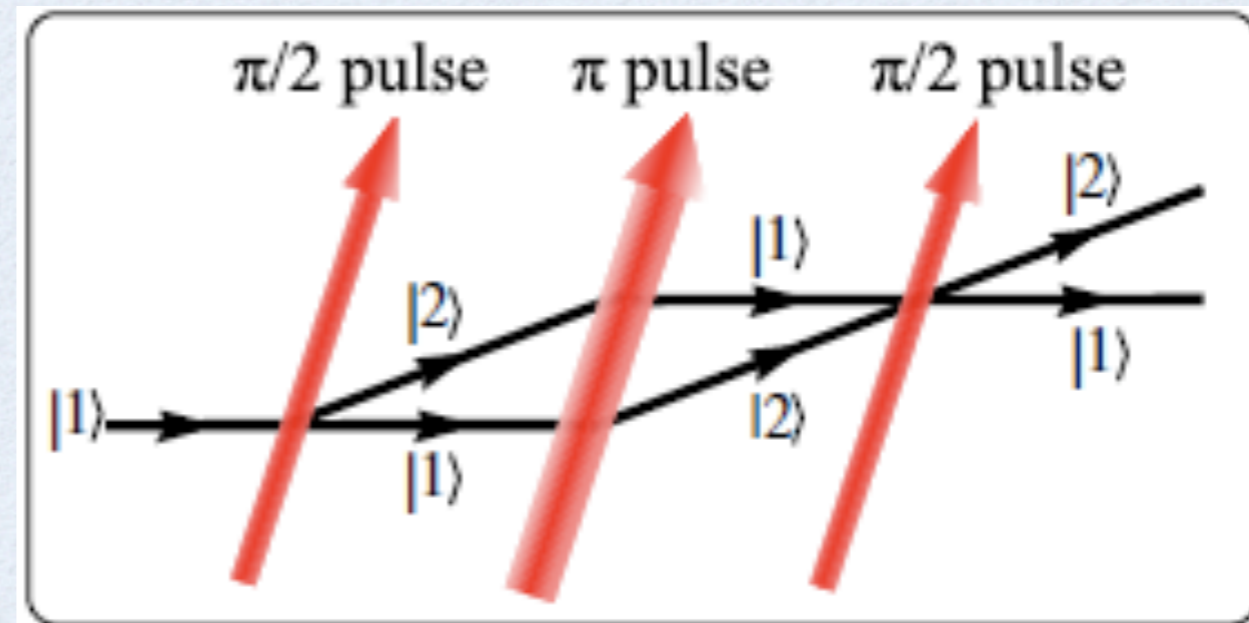
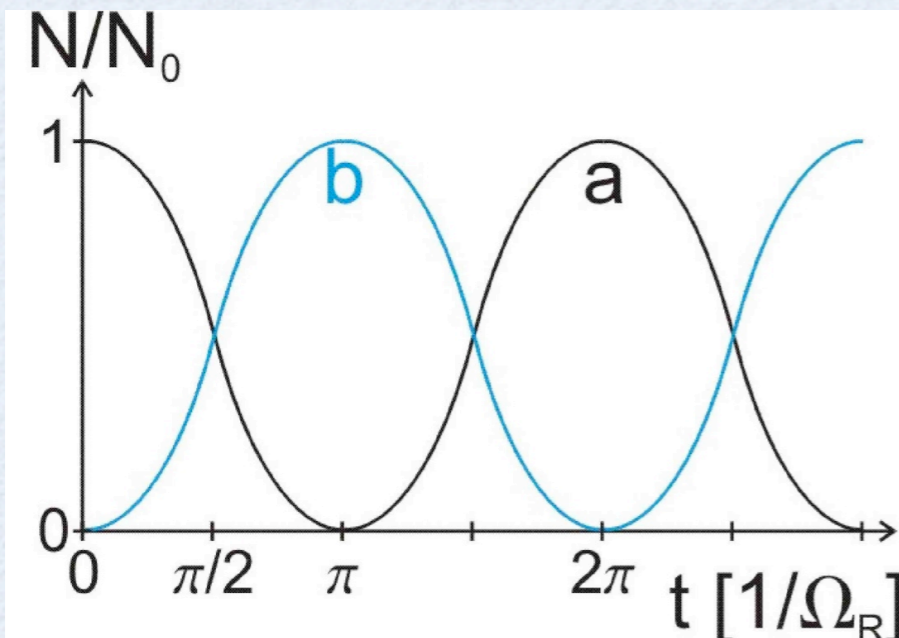
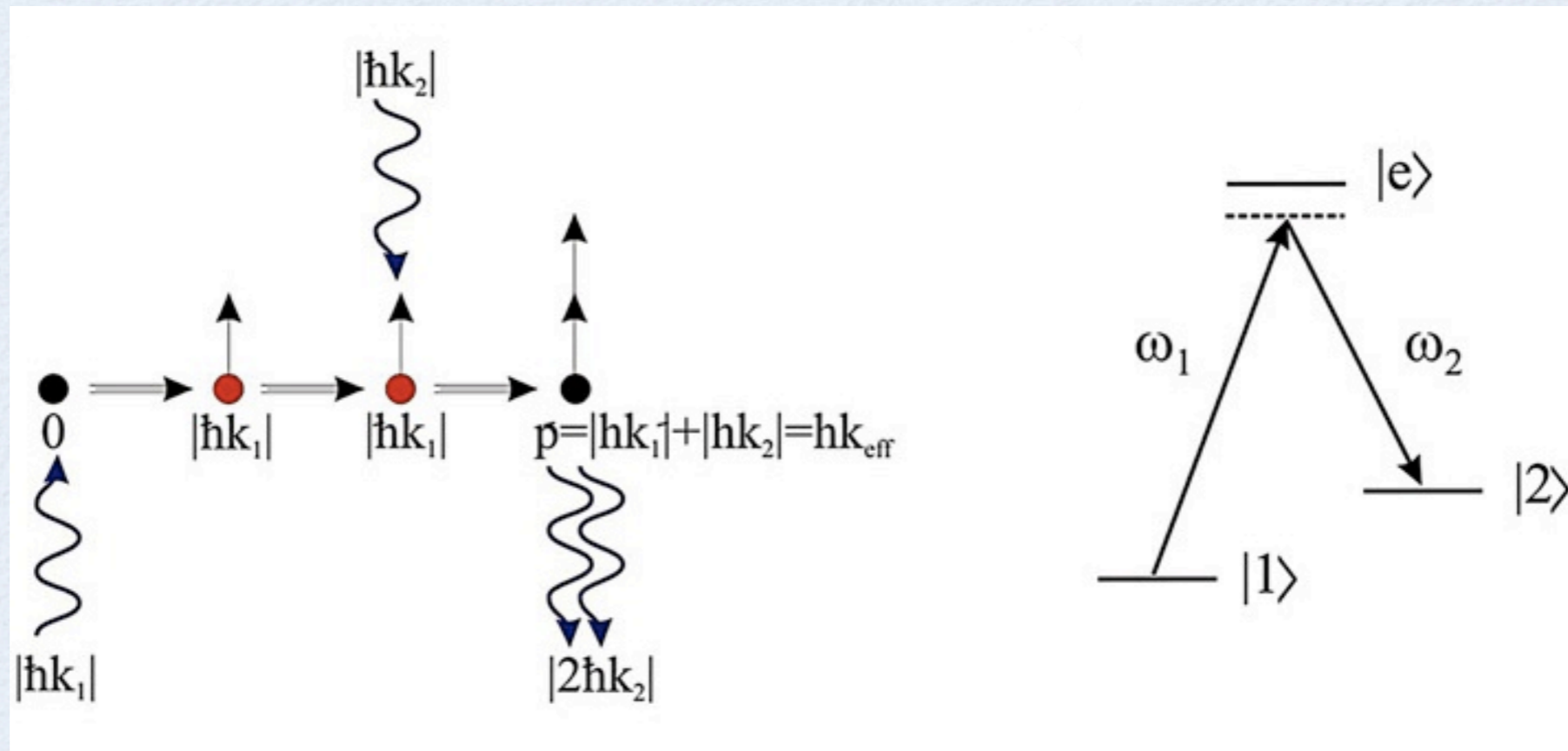
# Present limitations of AI



- shot-noise limit to sensitivity  $\sim 1/\sqrt{\dot{N}}$ 
  - atomic flux  $\sim 10^{18} \text{ s}^{-1}$  with H ( $\sim 10^{11} \text{ s}^{-1}$  with alkali)
  - in a 1-kW laser the photon flux is  $> 10^{22} \text{ s}^{-1}$
- much lower path difference than in optical interferometers
  - better beam splitters, optical cavities
- nevertheless AI inertial sensors are already competitive
  - long term stability (bias & scale factor) and accuracy
- future developments to improve sensitivity
  - large momentum beam splitters
  - high flux atomic sources
  - sub-shot noise detection (quantum degenerate gases, etc.)
  - large size AI,  $\mu$ -gravity, ultracold atoms



# Raman pulse atom interferometer





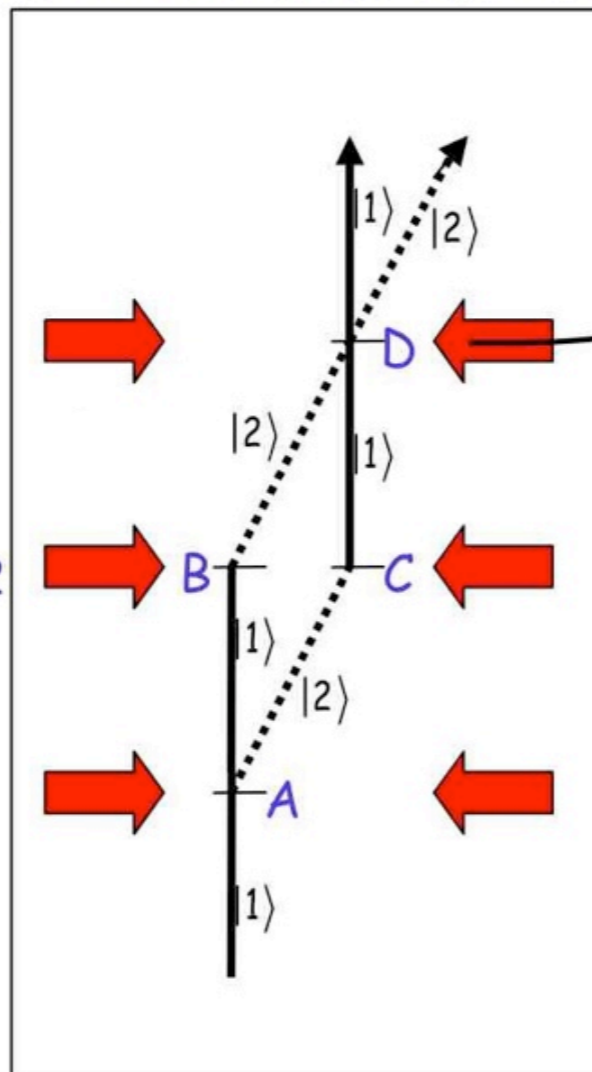


# Light-pulse AI inertial sensors



## TRANSVERSAL PULSES

- the interferometer encloses an area
- used to measure rotations (GYROSCOPES)



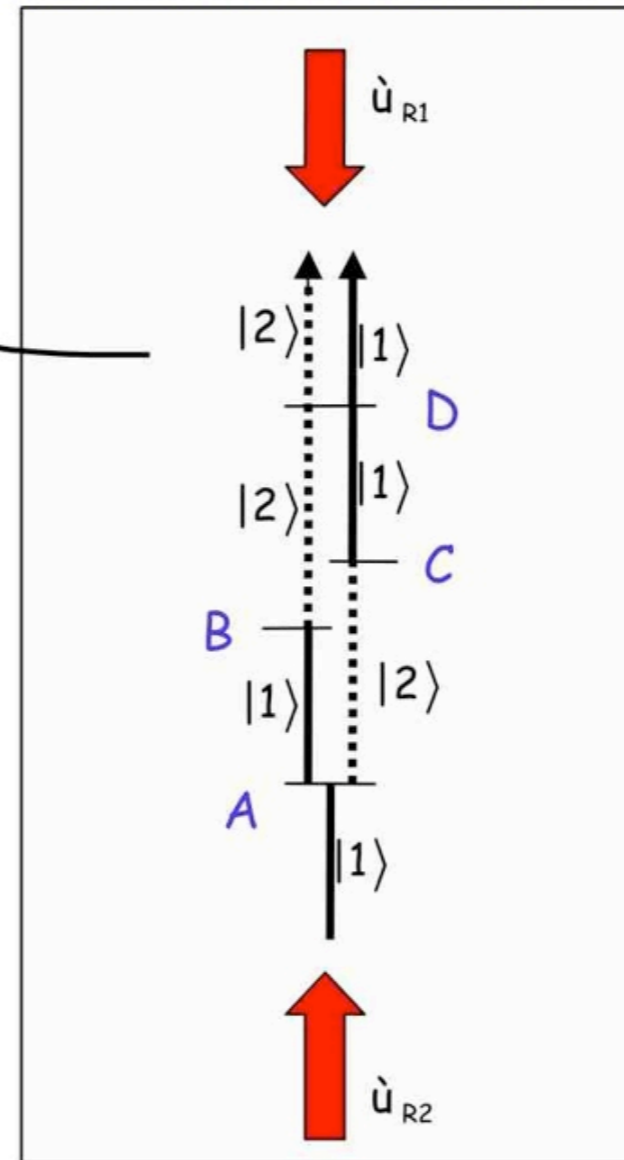
With an acceleration  $g$ ,  
the phase difference

$$\Delta\phi = 2k_{\text{eff}} \cdot (a - 2(\Omega \times v)) T^2$$

where  $k$  is the laser wavenumber and  $T$  the time interval between laser pulses

## LONGITUDINAL PULSES

- no area enclosed
- used to measure accelerations (GRAVIMETERS)

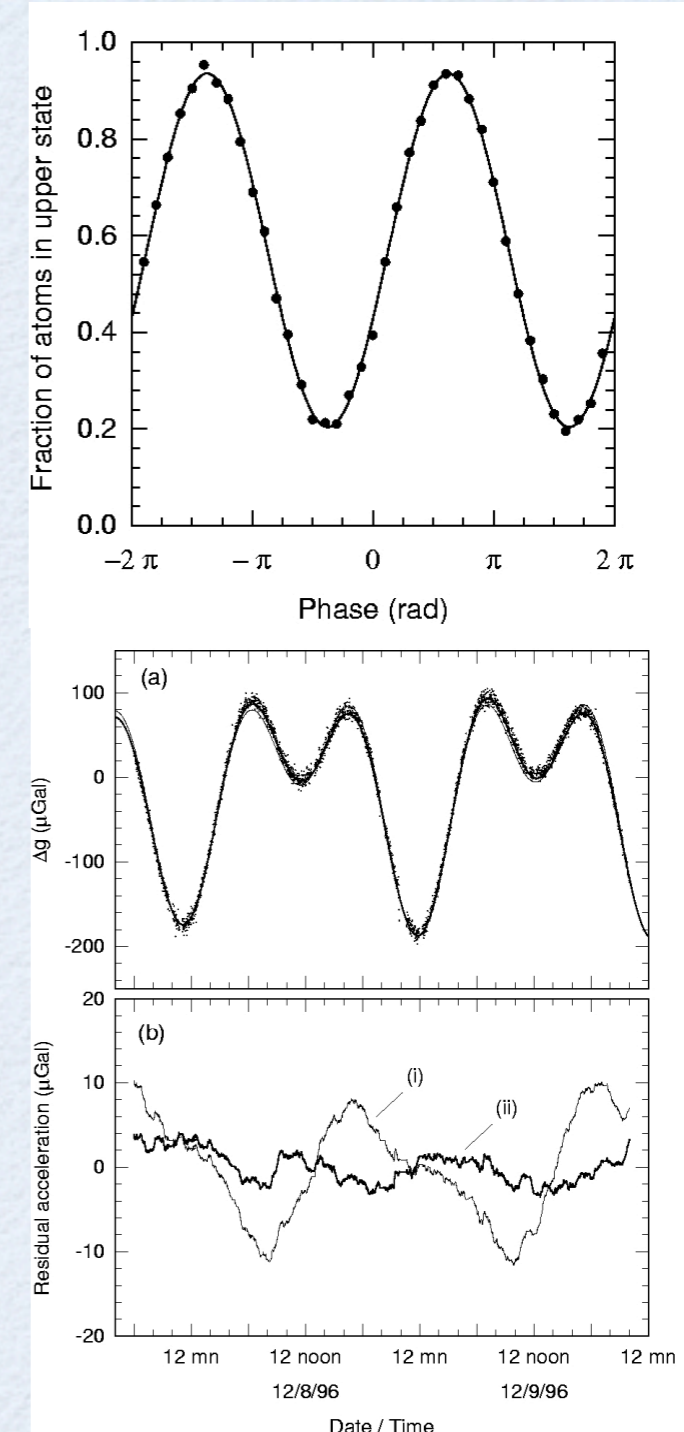
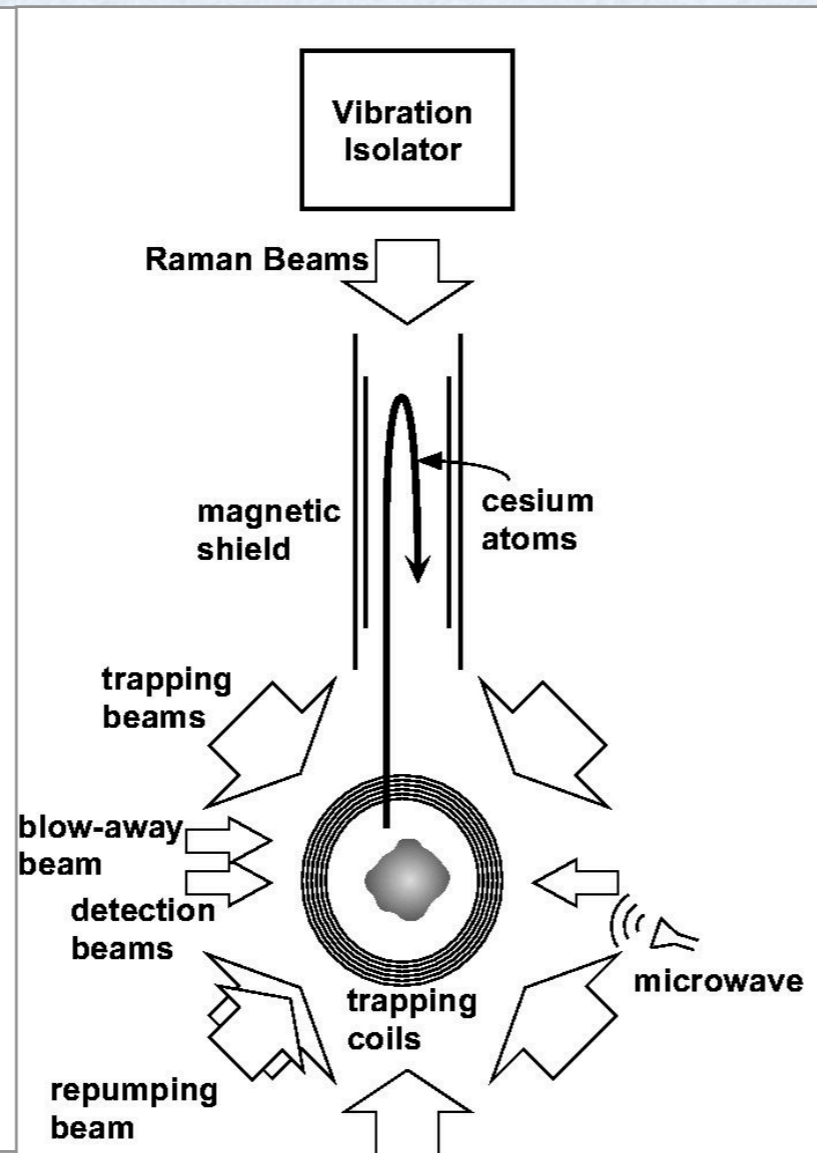
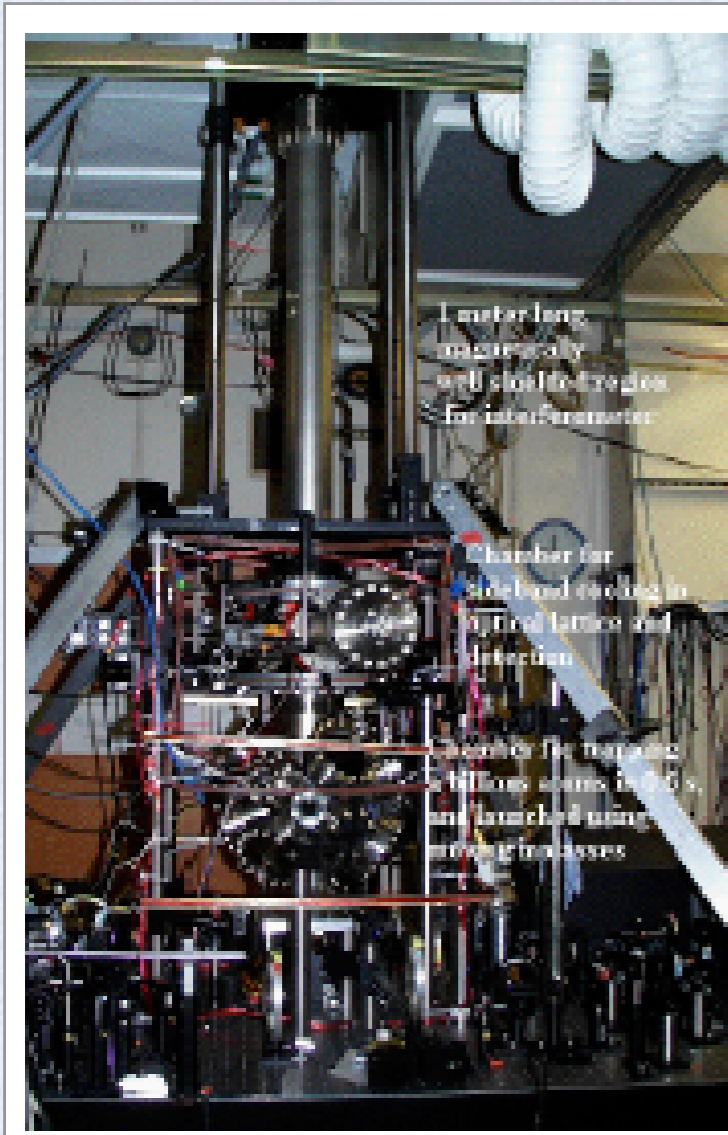


With an acceleration  $g$ ,  
the phase difference

$$\Delta\phi = k_{\text{eff}} g T^2$$

where  $k$  is the laser wavenumber and  $T$  the time interval between laser pulses

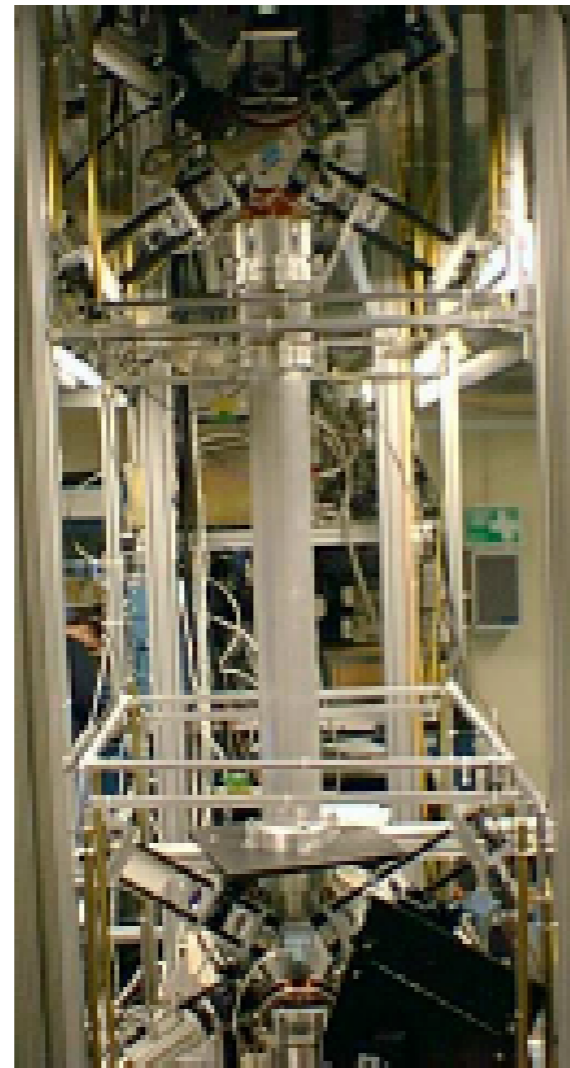




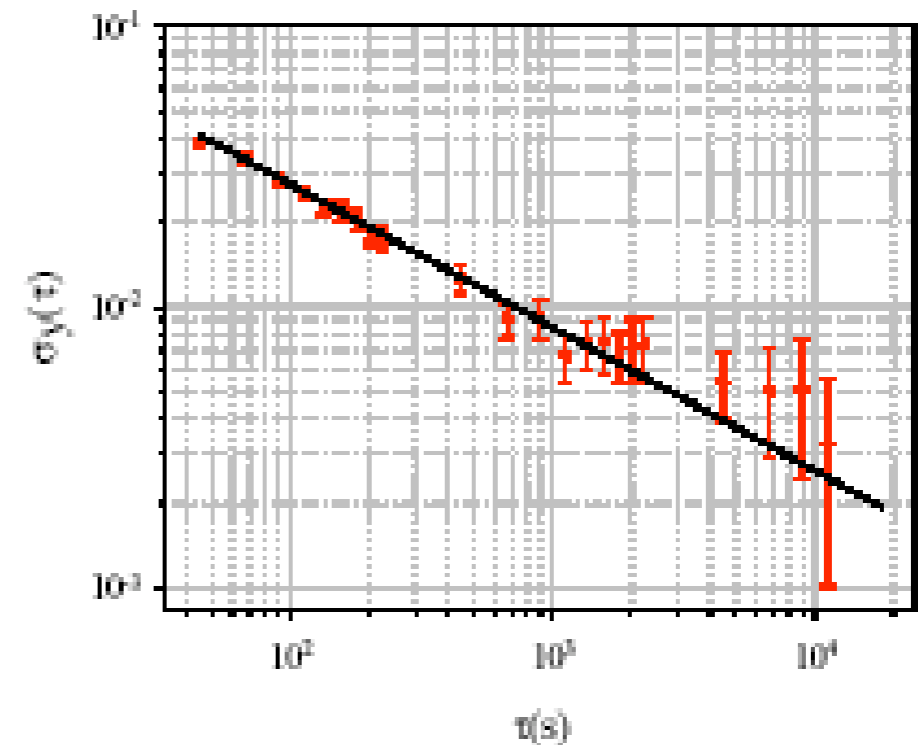
resolution:  $8 \times 10^{-9}$  g in 1 second  
 accuracy:  $\Delta g/g \leq 3 \times 10^{-9}$  limited by tidal models

A. Peters, K.Y. Chung and S. Chu, *Nature* **400**, 849 (1999)  
 H. Müller et al., *Phys. Rev. Lett* **100**, 031101 (2008)





1.4 m



Demonstrated differential acceleration sensitivity:

$$4 \times 10^{-9} \text{ g/Hz}^{1/2}$$

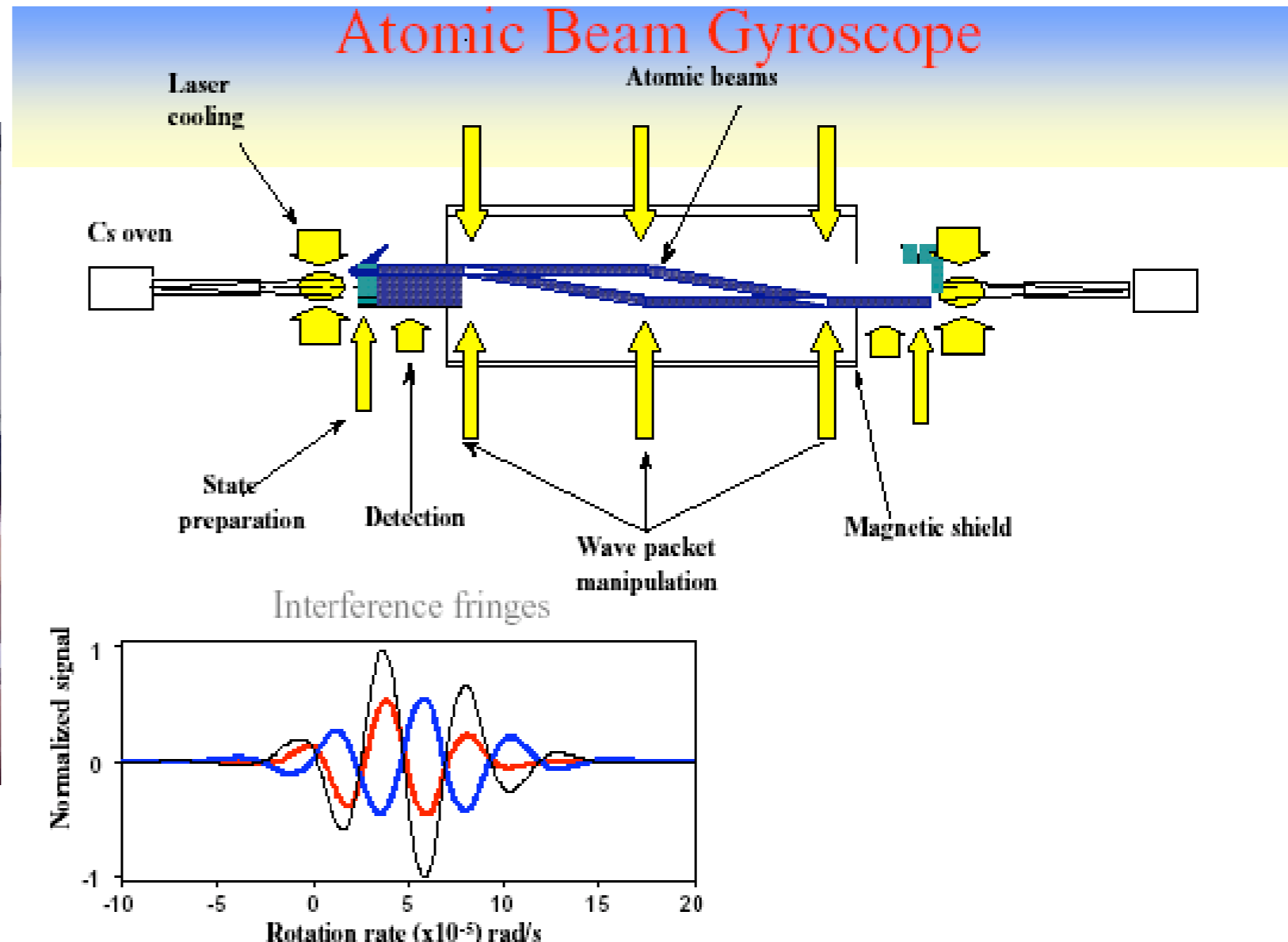
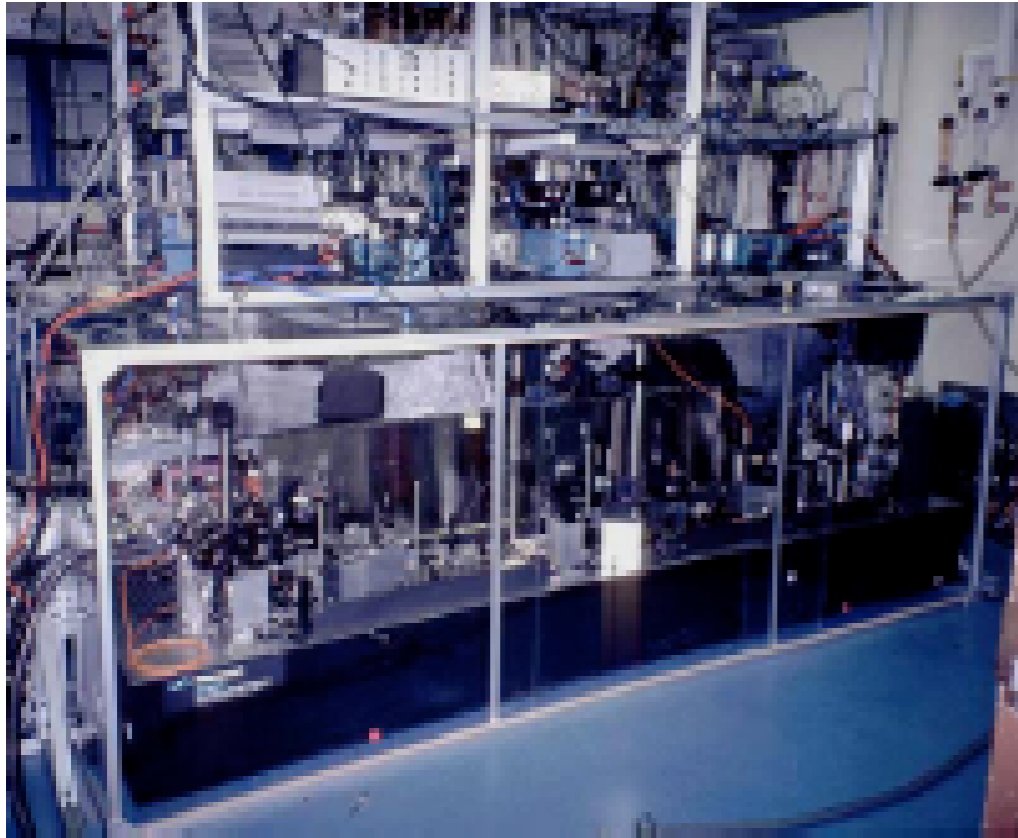
( $2.8 \times 10^{-9} \text{ g/Hz}^{1/2}$  per accelerometer)

*limited by QPN*

*Distinguish gravity induced accelerations from those due to platform motion with differential acceleration measurements.*

J. M. McGuirk et al., Phys. Rev. A 65, 033608 (2002)





sensitivity:  $6 \times 10^{-10} \text{ rad} \cdot \text{s}^{-1} \sqrt{\text{Hz}}$

scale factor stability  $< 5 \text{ ppm}$

bias stability  $< 70 \mu\text{deg/h}$

T.L. Gustavson, A. Landragin and M.A. Kasevich, *Class. Quantum Grav.* **17**, 2385 (2000)

D. S. Durfee, Y. K. Shaham, M.A. Kasevich, *Phys. Rev. Lett.* **97**, 240801 (2006)

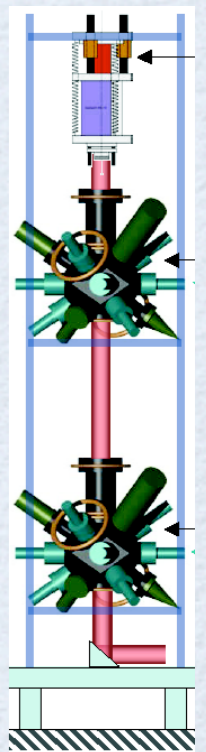
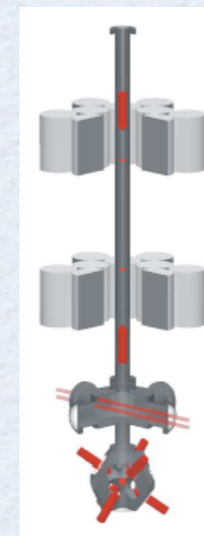
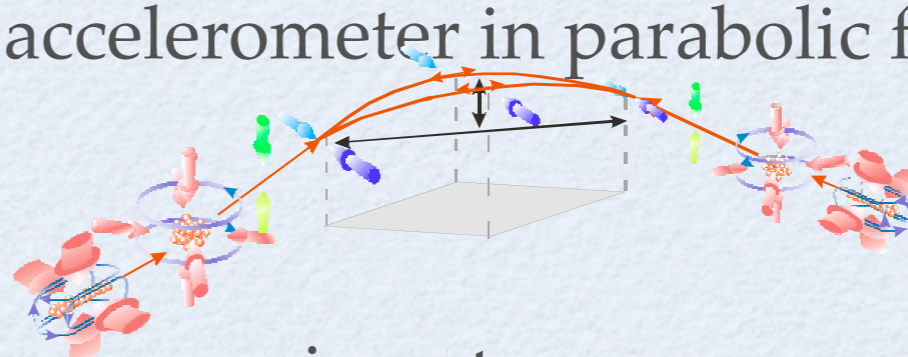
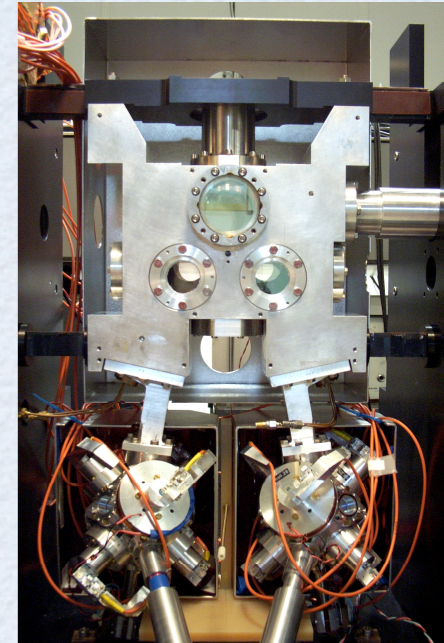
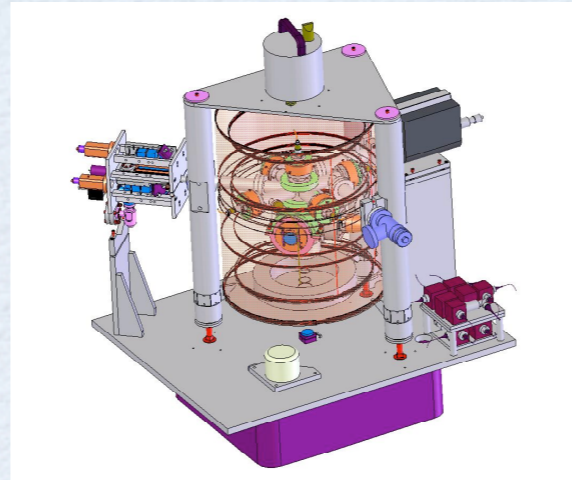




# Other AI sensors



- SYRTE (FR)
  - absolute gravimeter
  - gyroscope
  - six-axis inertial sensor
  - I.C.E. AI differential accelerometer in parabolic flight
- IQO (D)
  - CASI gyroscope
  - QUANTUS drop-tower experiment
- JPL (USA)
  - gradiometer
- STANFORD (U.S.A)
  - transportable multi-axis sensors
- MAGIA (IT)



Atom interferometry gyroscopes



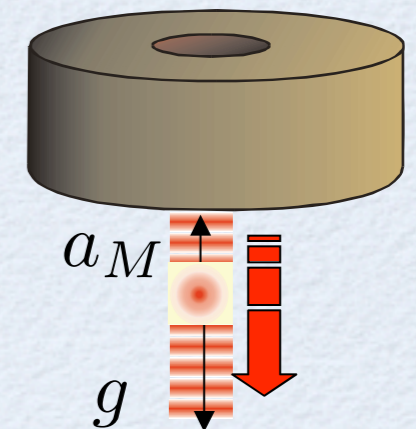


# MAGIA



## *Misura Accurata di $G$ mediante Interferometria Atomica*

- Measure  $g$  by atom interferometry
- Add source masses
- Measure change of  $g$



<http://www.fi.infn.it/sezione/esperimenti/MAGIA/home.html>

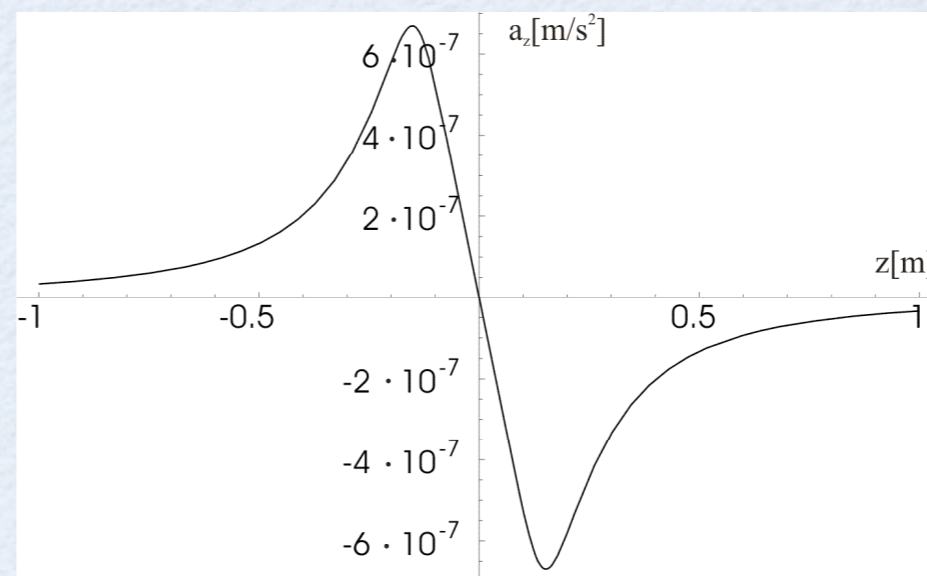
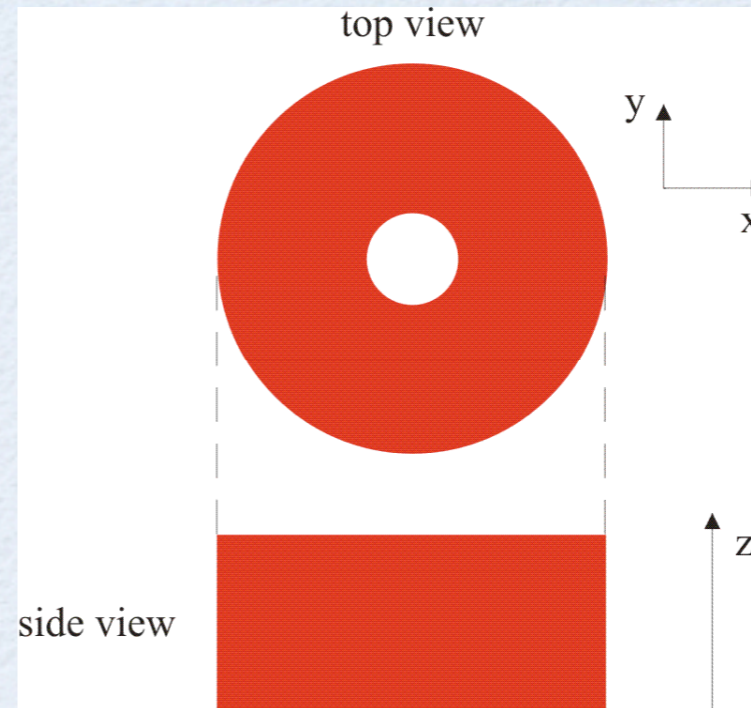
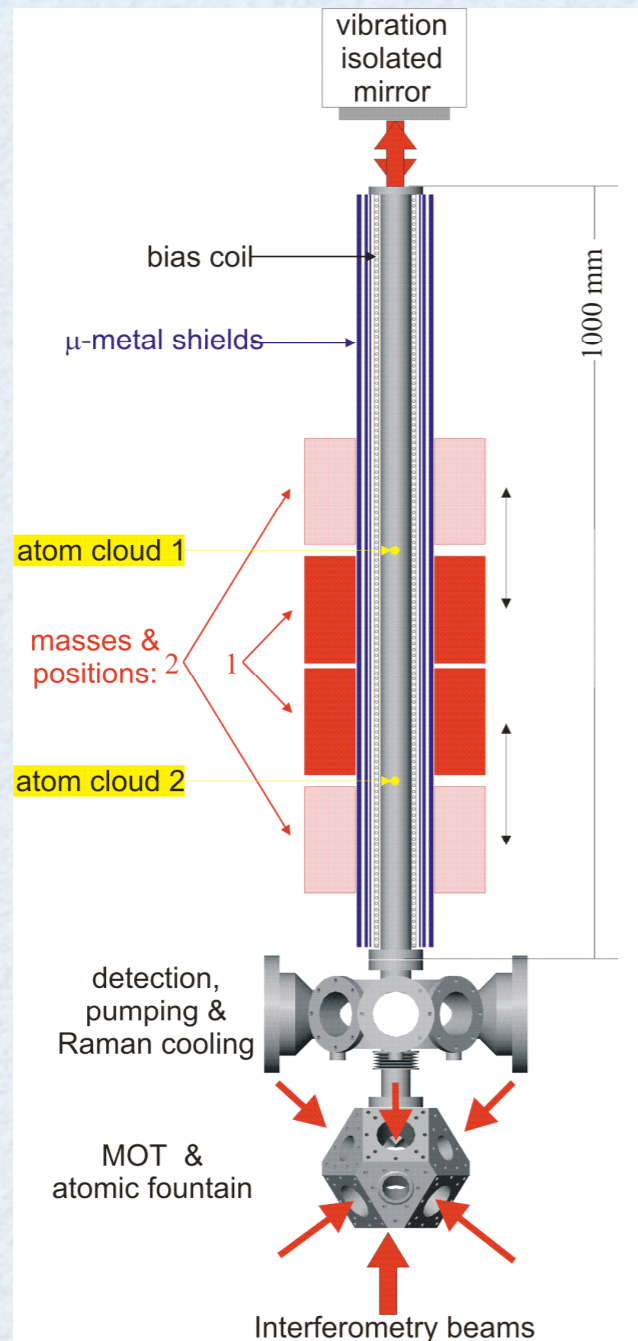




# Using atomic probes

- Point-like test masses in free fall
- virtually insensitive to stray fields
- well known and reproducible properties
- different states, isotopes
- precision measurements by atom interferometry





500 Kg tungsten mass

Peak mass acceleration  $a_g \sim 10^{-7} g$

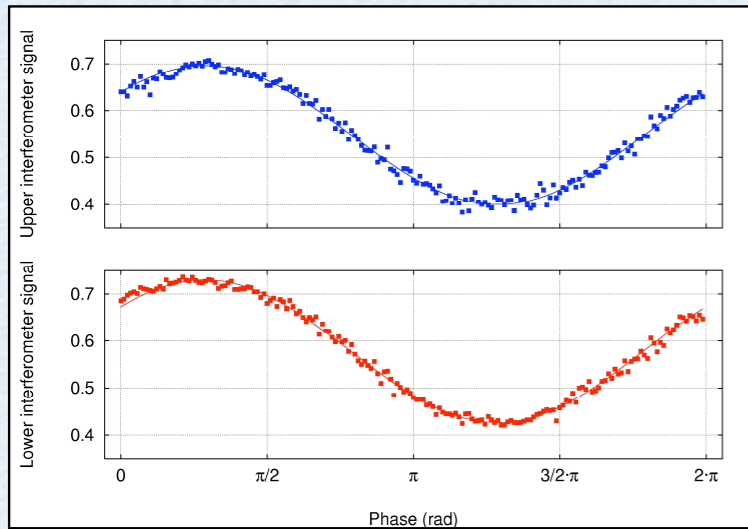
10000 shots  $\rightarrow \Delta G/G \sim 10^{-4}$

Sensitivity  $10^{-9} g/\text{shot}$   
 one shot  $\rightarrow \Delta G/G \sim 10^{-2}$



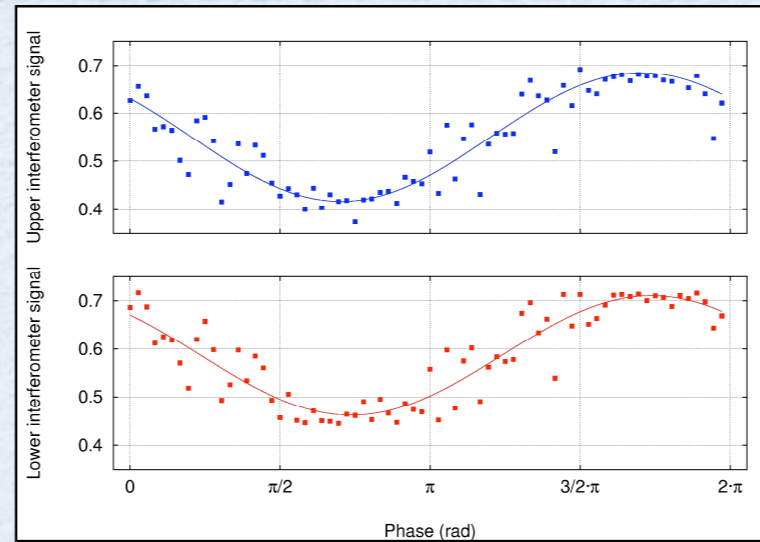


# Differential gravity measurement



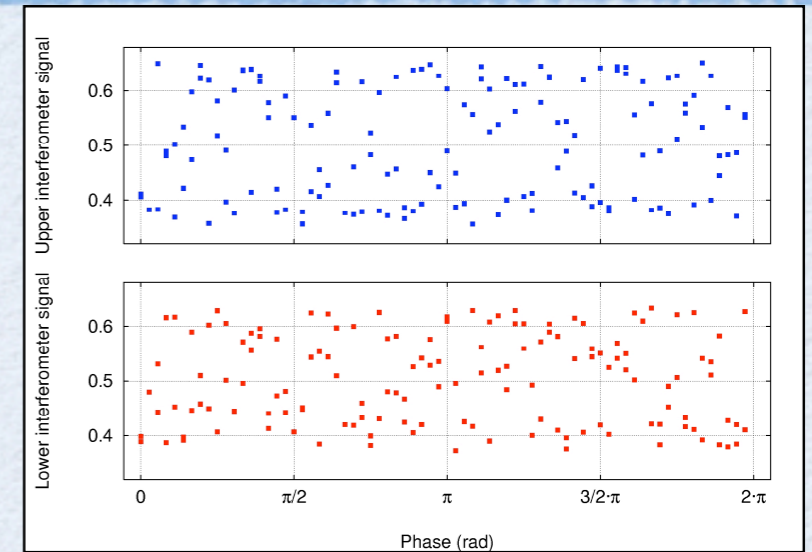
$T=5$  ms

resol. =  $2.3 \times 10^{-5}$  g/shot



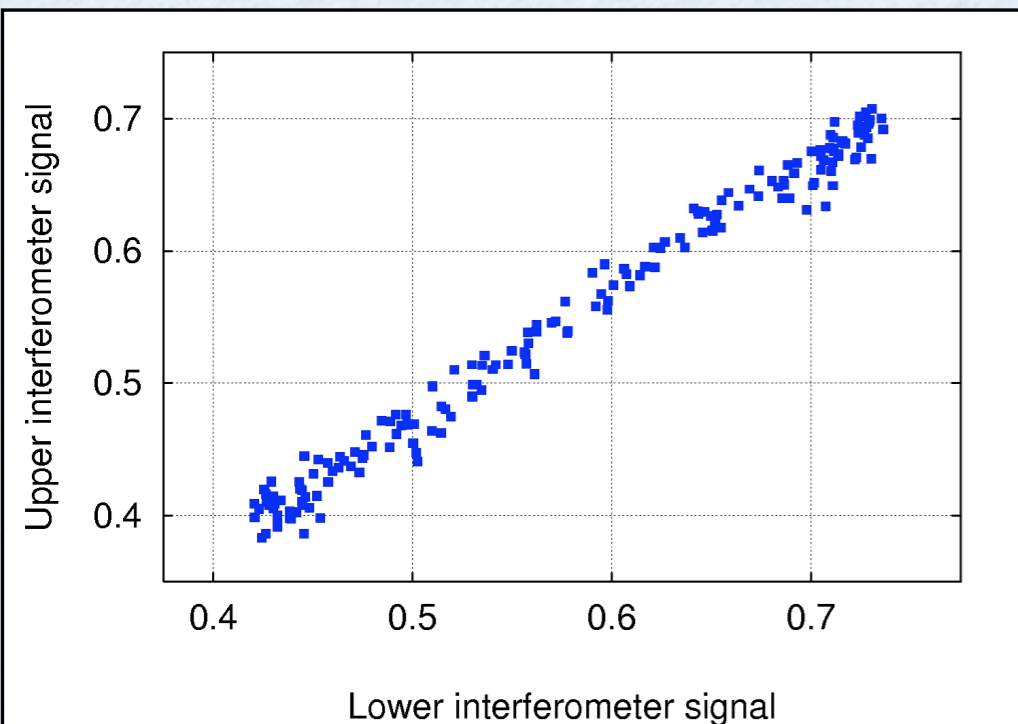
$T=50$  ms

resol. =  $1.0 \times 10^{-6}$  g/shot

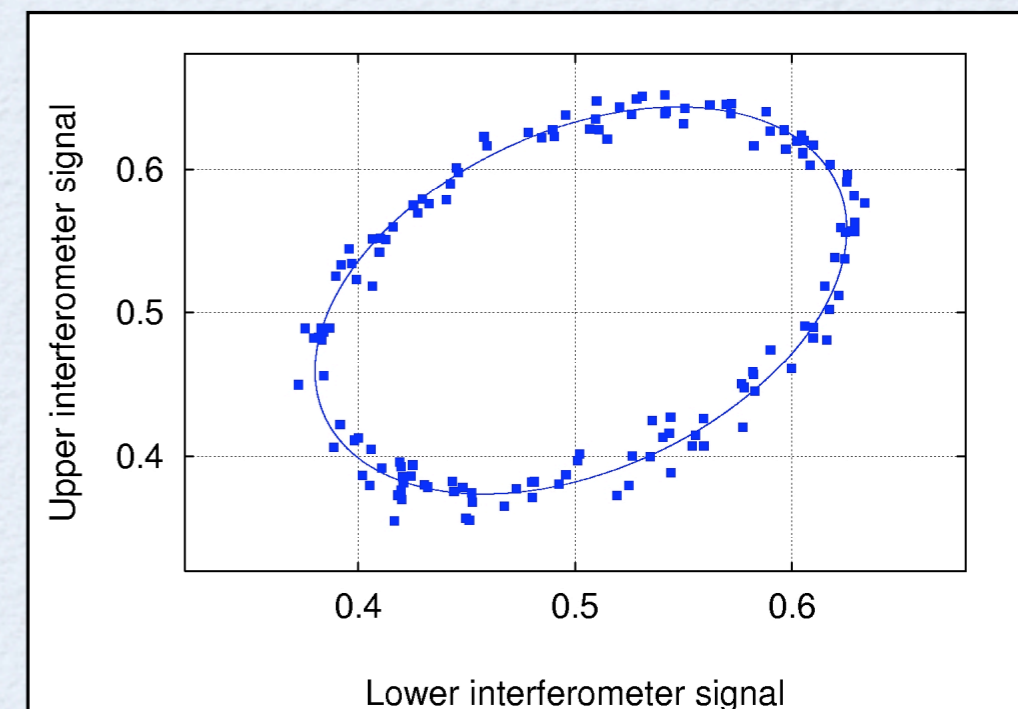


$T=150$  ms

resol. =  $3.2 \times 10^{-8}$  g/shot



$$\Delta\Phi = k_e g T^2$$



G. T. Foster et al., Opt. Lett **27**, 951 (2002)

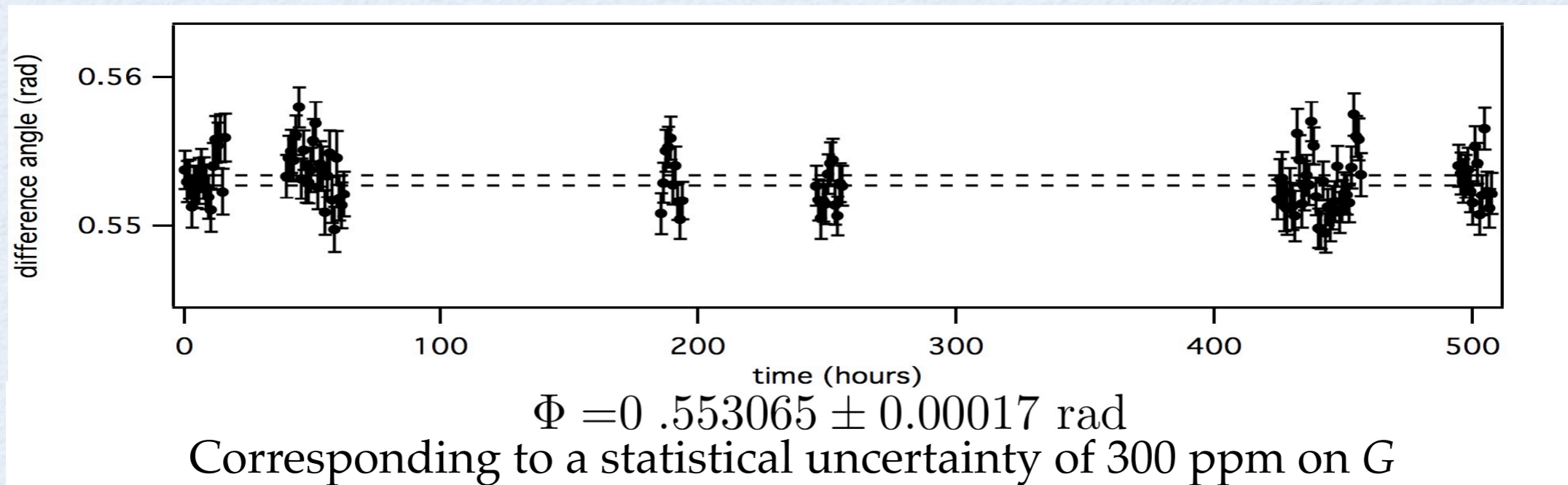




# Test of G measure & long term stability

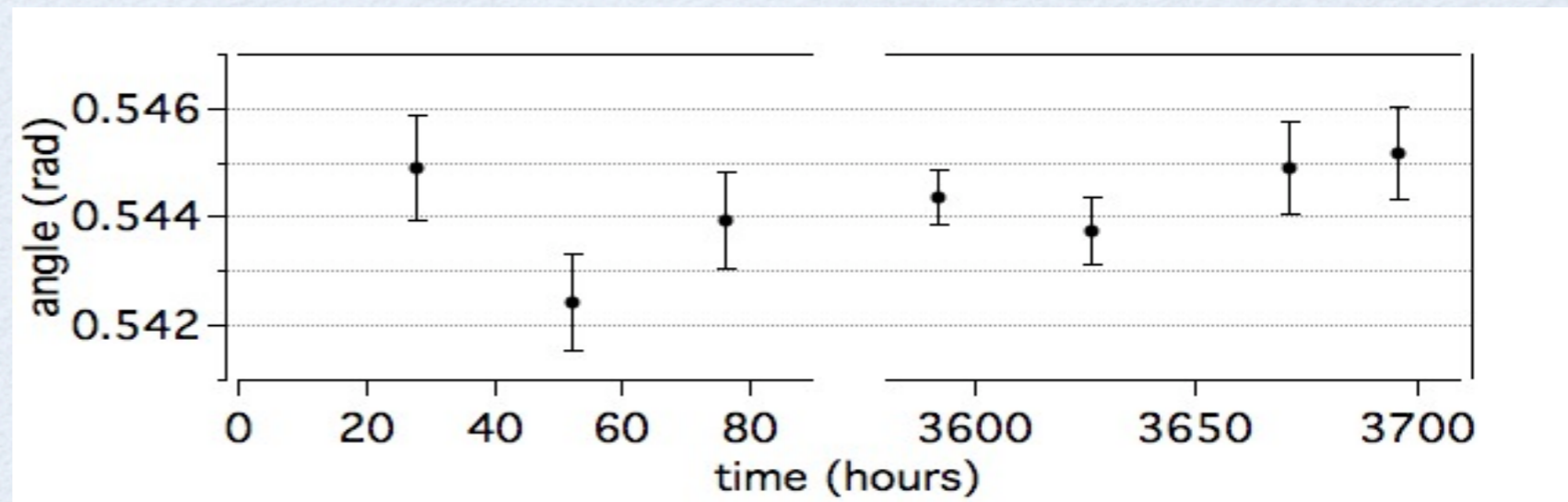


First G measurement with 1500 ppm precision,  
*G. Lamporesi et al., Phys. Rev. Lett* **100**, 050801 (2008)



F. Sorrentino et al., *New J. Phys.* **12**, 095009 (2010)

Comparison between two runs  
in December 2009 and May 2010





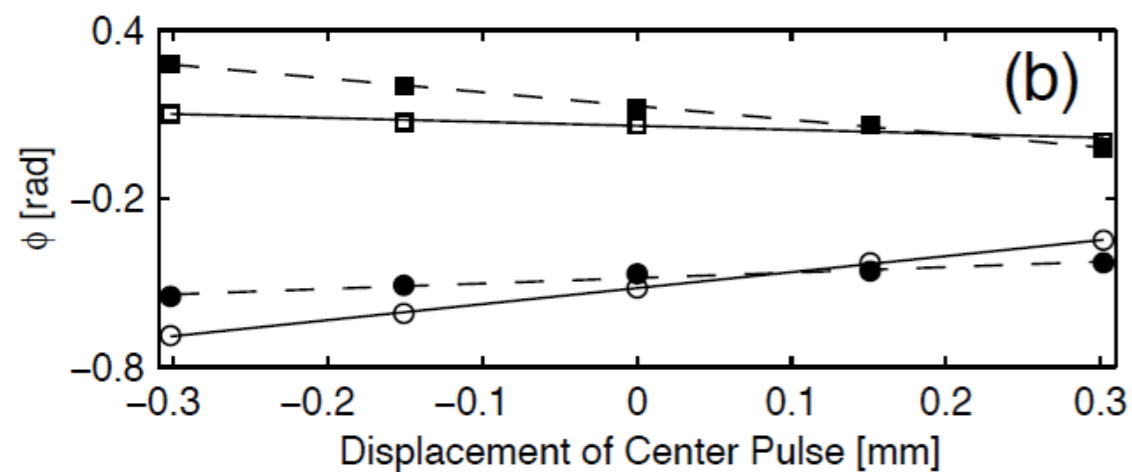
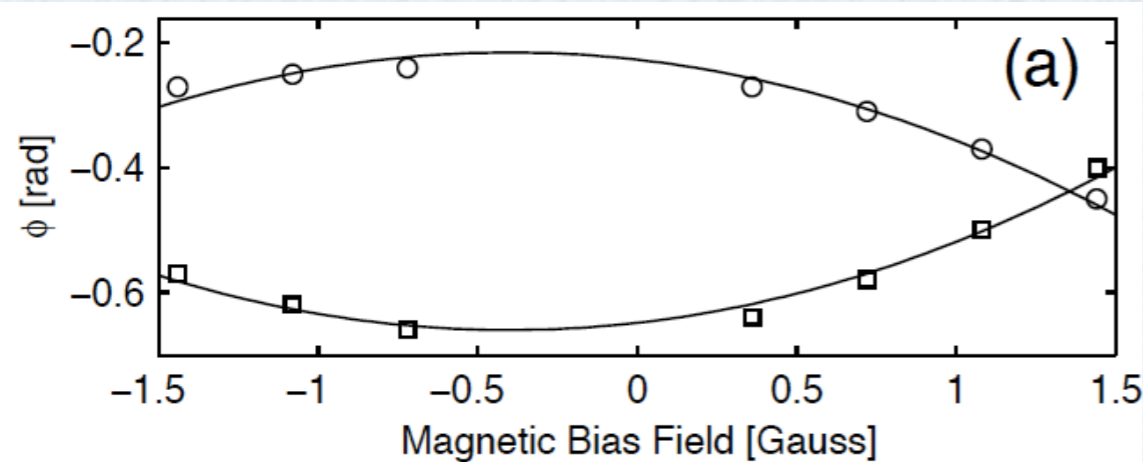


# AI gyroscopes: long term stability



- Area reversal
- correlations removal

D. S. Durfee, Y. K. Shaham, M.A. Kasevich,  
*Phys. Rev. Lett.* **97**, 240801 (2006)

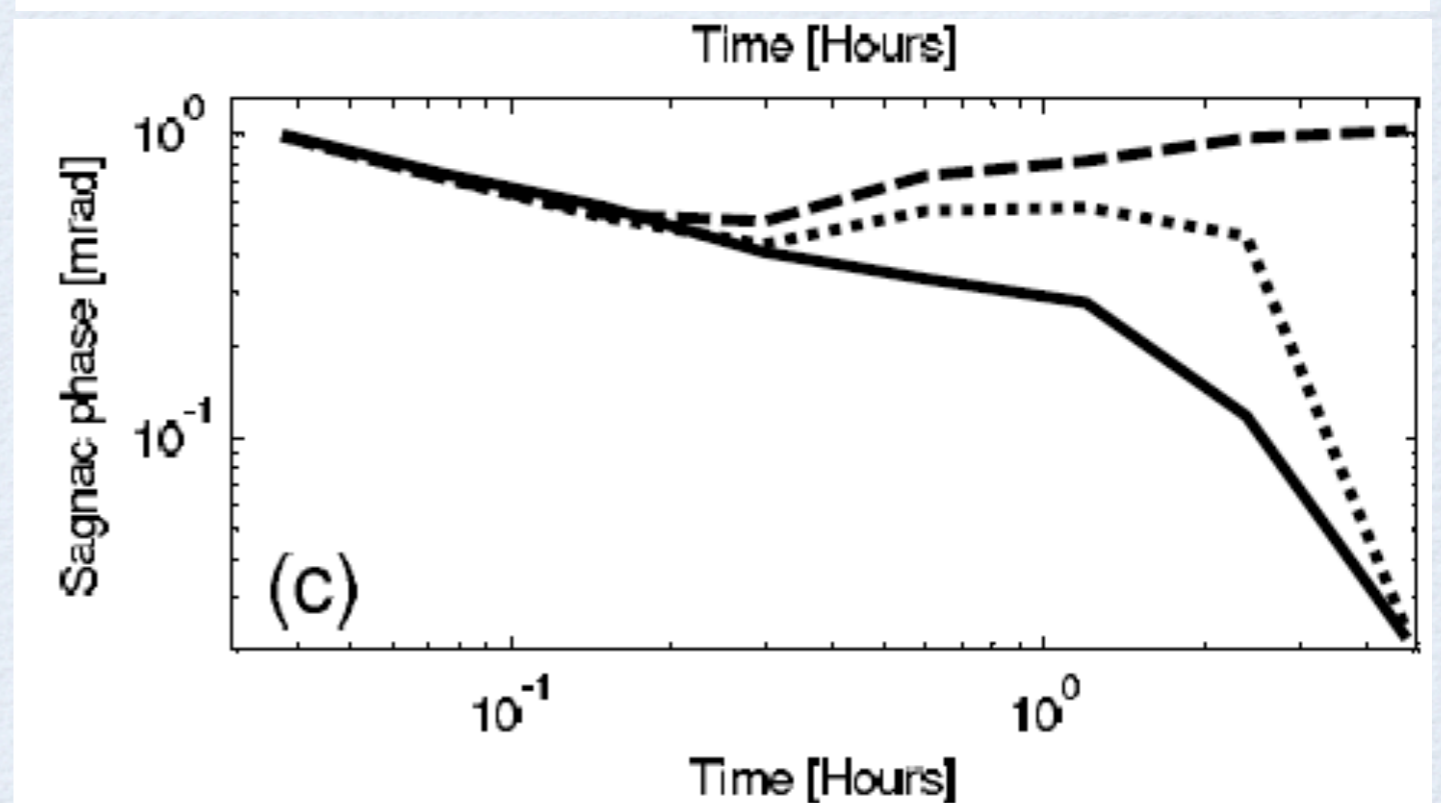
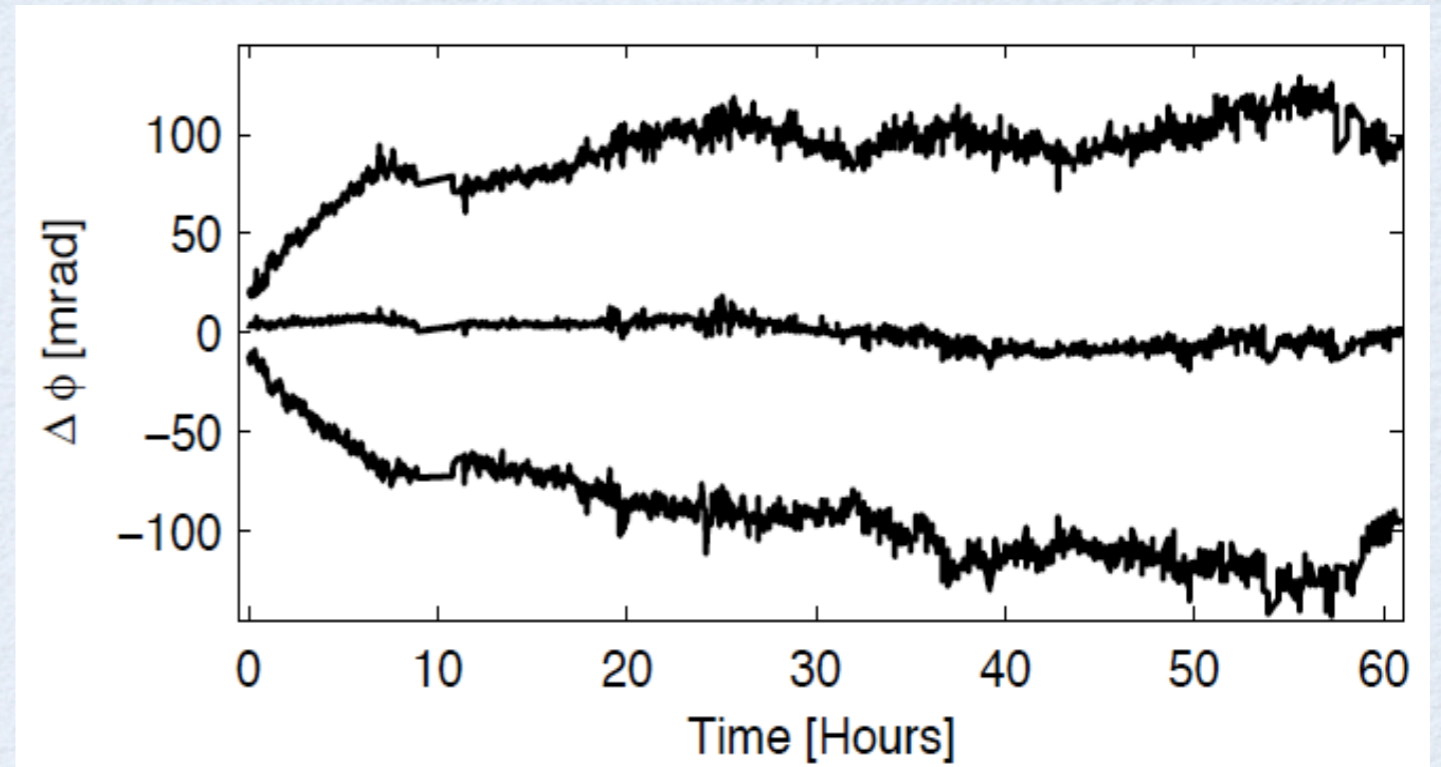


sensitivity:  $6 \times 10^{-10} \text{ rad} \cdot \text{s}^{-1} \sqrt{\text{Hz}}$

scale factor stability  $< 5 \text{ ppm}$

bias stability  $< 70 \mu\text{deg/h}$

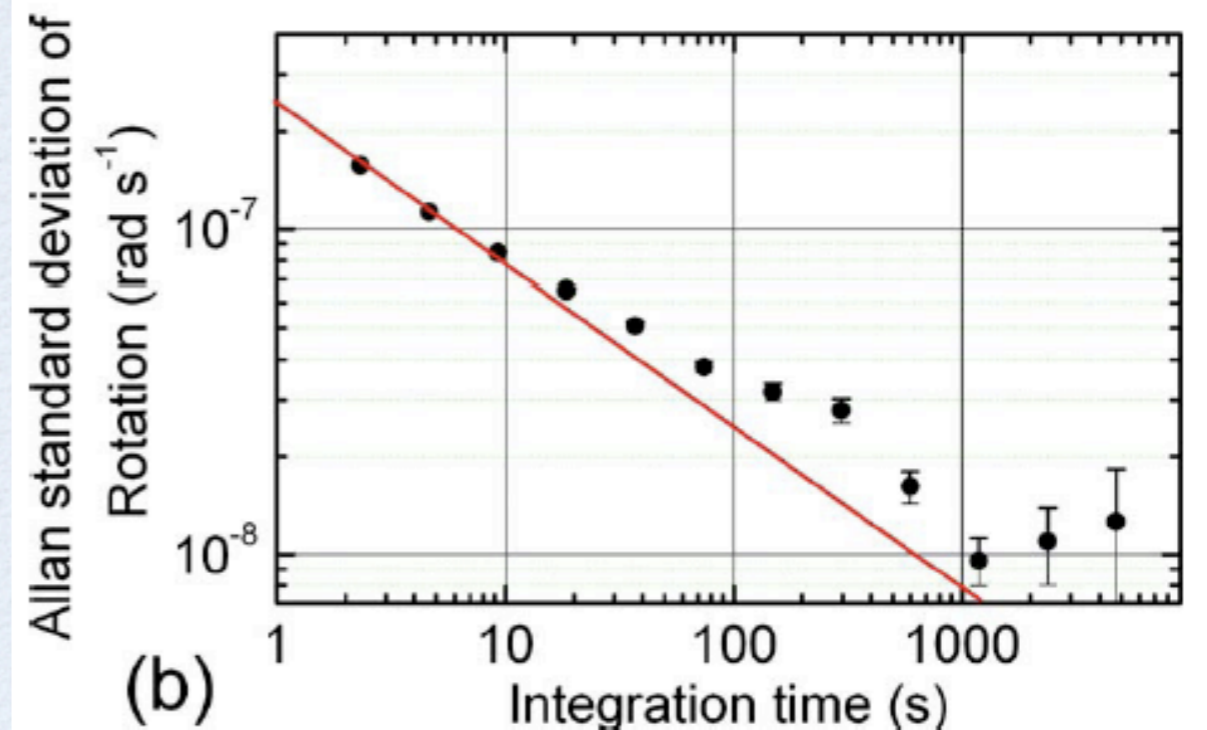
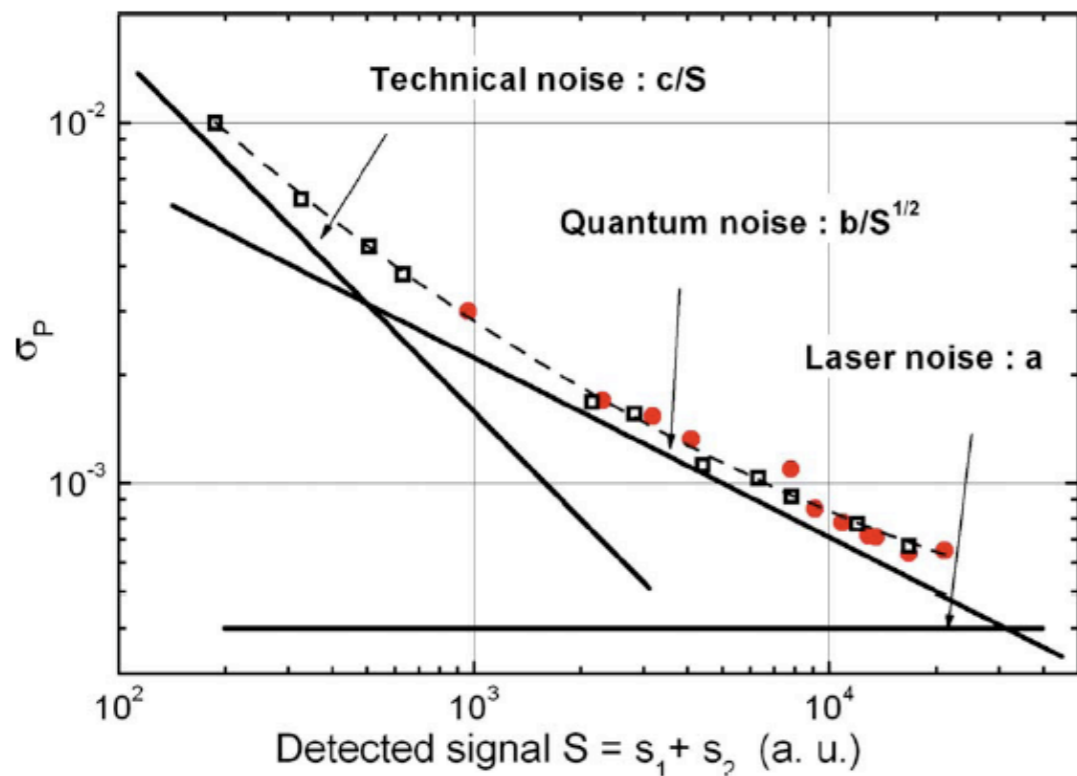
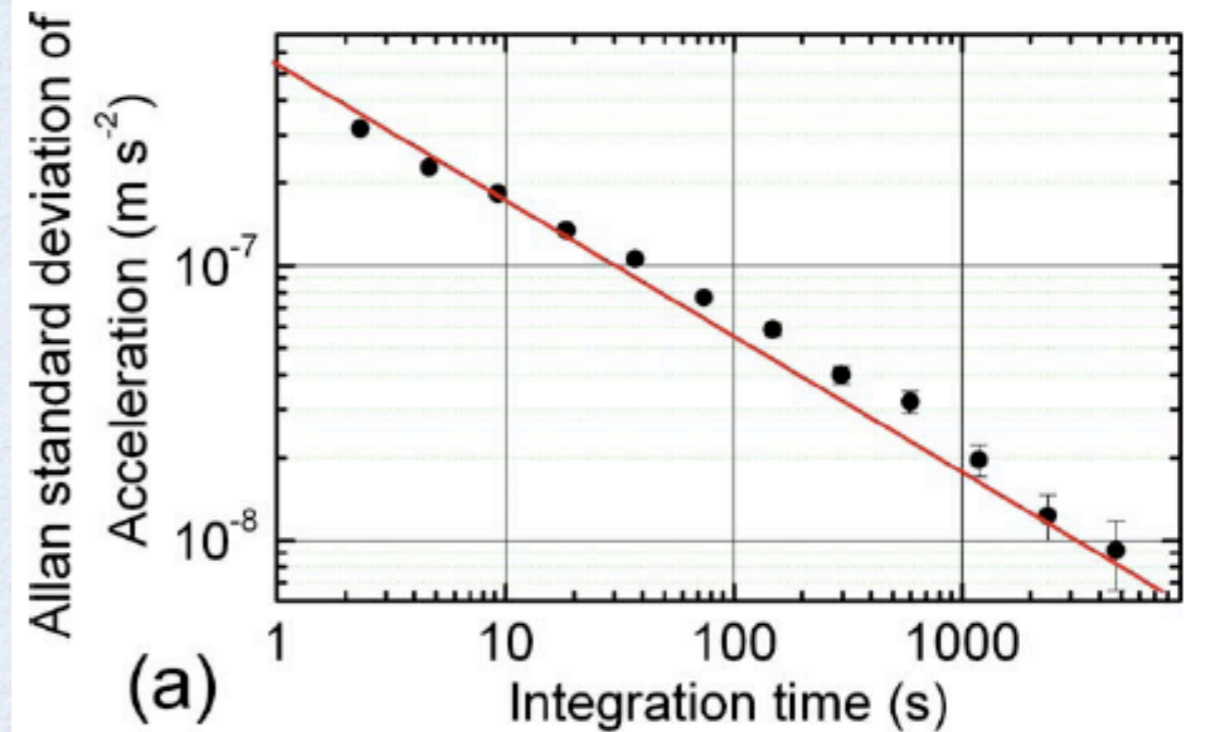
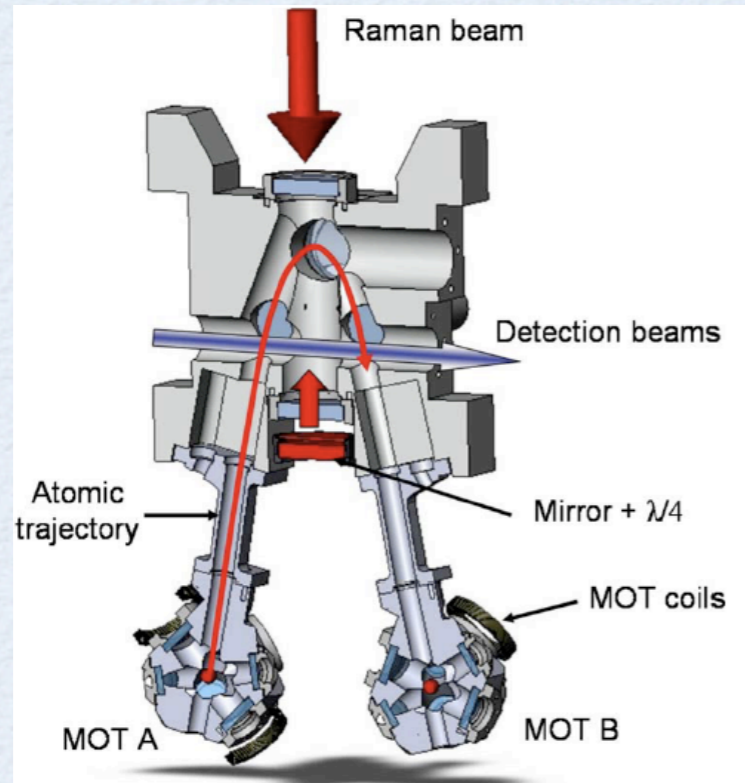
F. Sorrentino, LNL 19/12/11



Atom interferometry gyroscopes

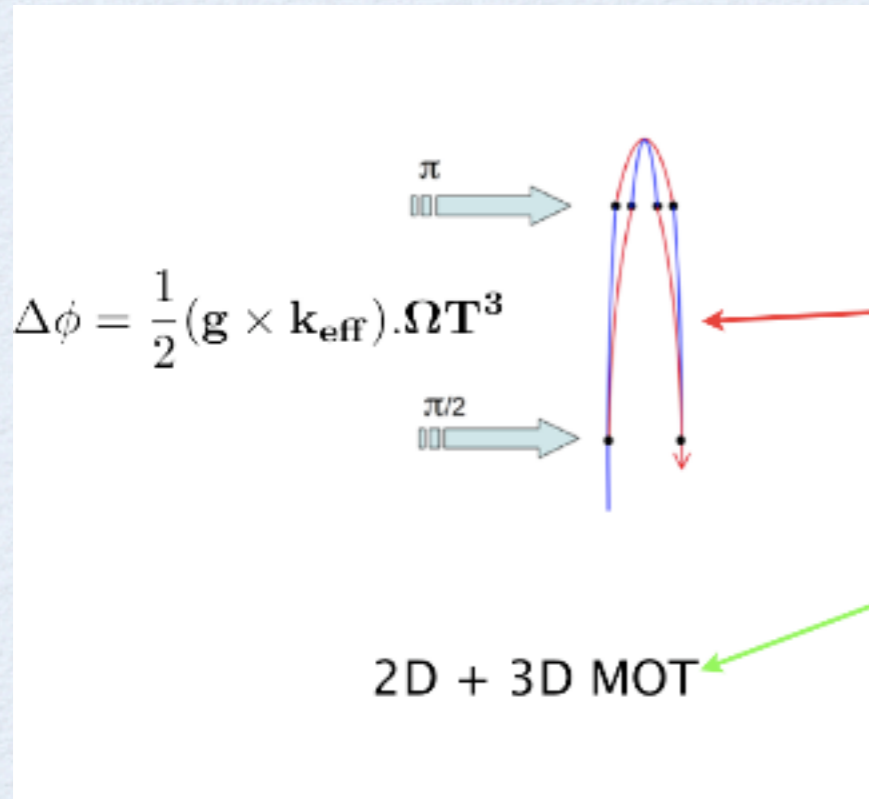
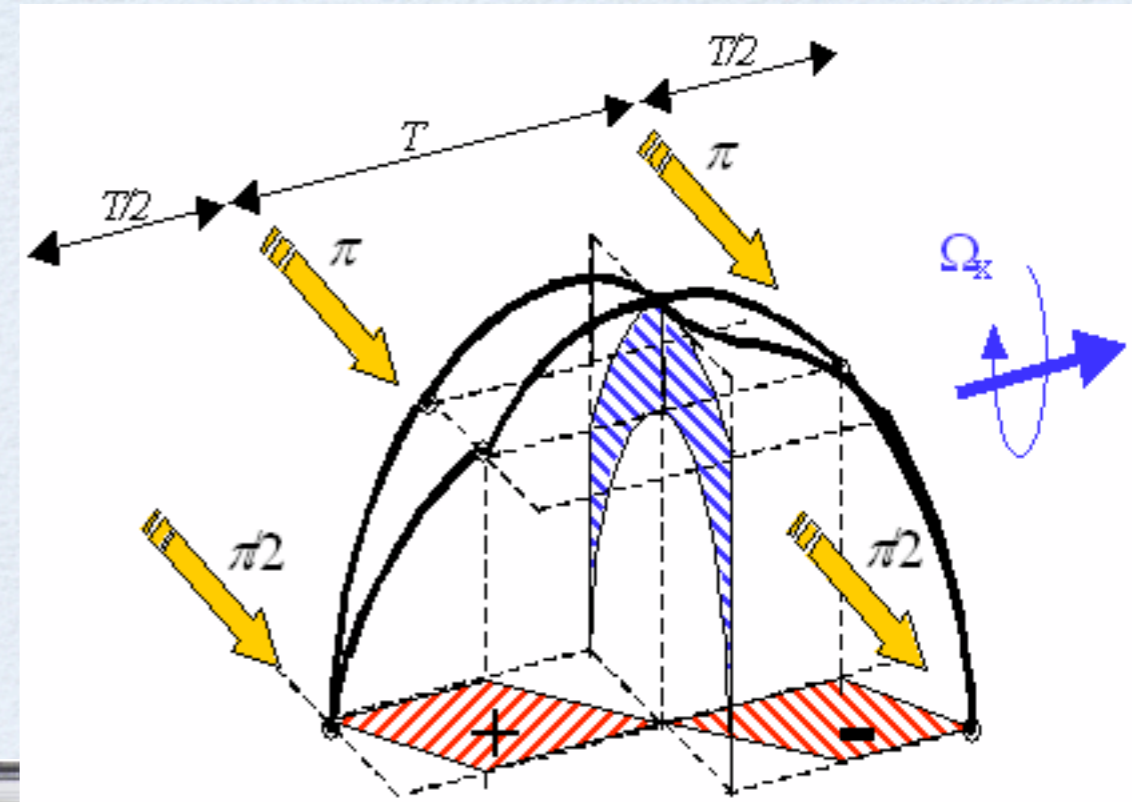


# Cold atoms gyroscope (SYRTE)





- Vertical fountain
- four Raman pulses
- no acceleration sensitivity
- large area (11 cm<sup>2</sup>)







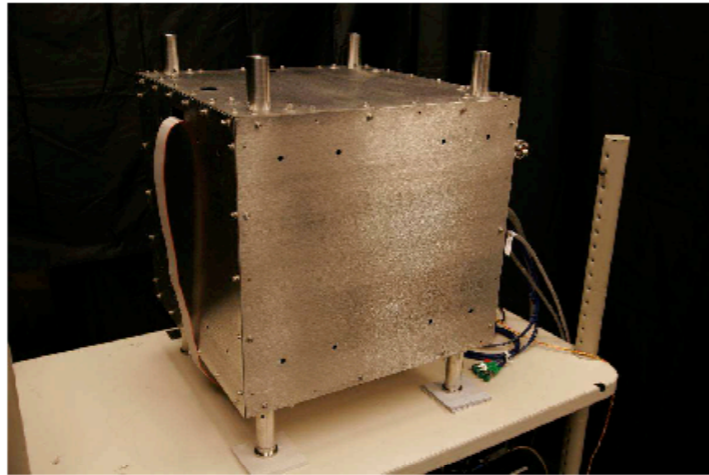
# Future of AI inertial sensors



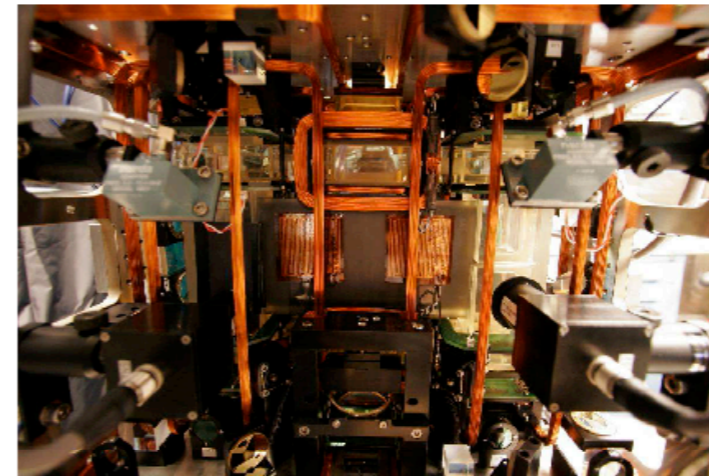
- Compact and transportable system without performance degradation
  - ground applications (geophysics)
  - space applications (satellite geodesy, inertial navigation, tests of fundamental physics):  $\Delta\phi = kgT^2$
- Novel schemes to improve sensitivity / accuracy
  - high-momentum beam splitters
  - coherent / squeezed atomic states to surpass QPN detection
  - large size AI
- New applications
  - GW, quantum gravity, etc.



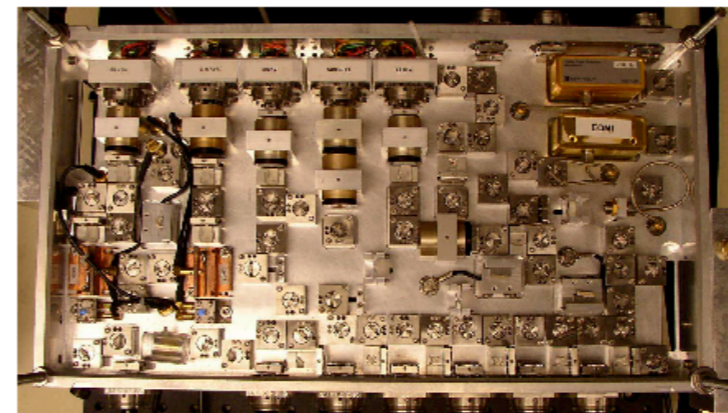
## Compact gravity gradiometer/gyroscope/accelerometer



Multi-function sensor measures gravity gradient, rotation and linear acceleration along a single input axis.



Interior view



Laser system



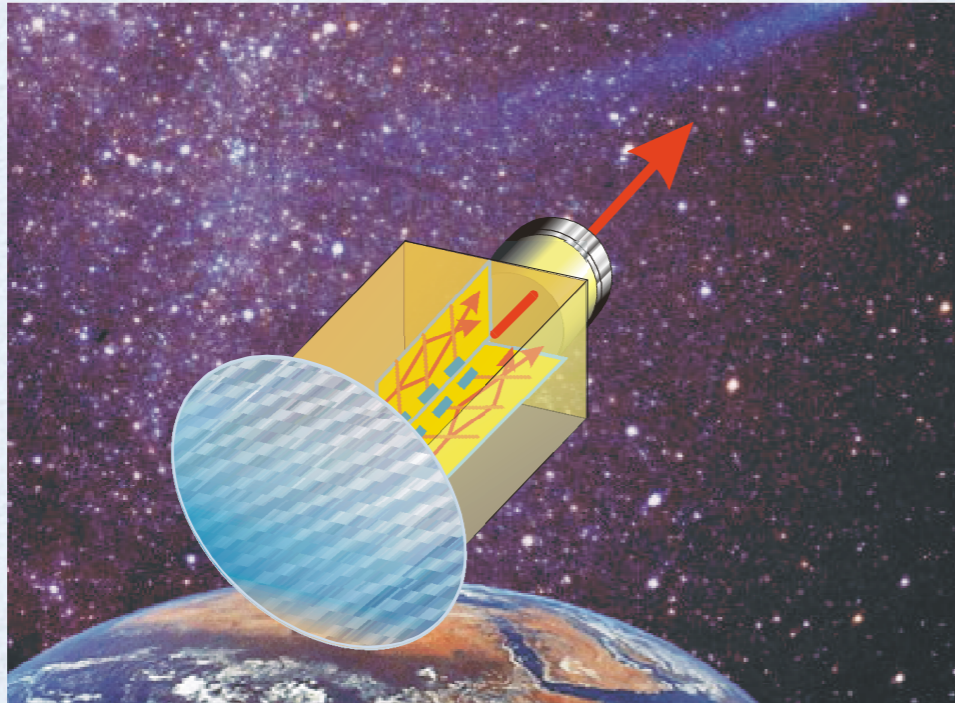
STANFORD UNIVERSITY

from M. Kasevich, Talk at the International Workshop on Advances in Precision Tests and Experimental Gravitation in Space, Firenze, September 2006





# The HYPER project



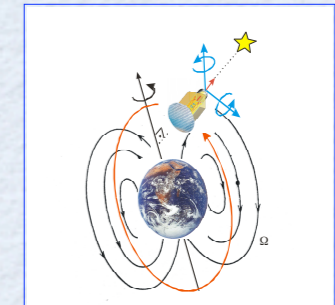
Differential measurement between two atom gyroscopes and a star tracker orbiting around the Earth

Resolution:  $3 \times 10^{-12} \text{ rad/s} / \sqrt{\text{Hz}}$

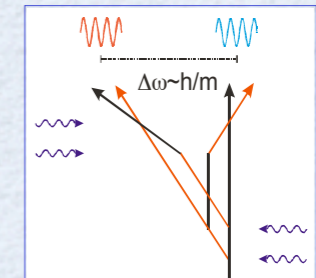


- Expected Overall Performance:  $3 \times 10^{-16} \text{ rad/s}$  over one year of integration i.e. a S/N~100 at twice the orbital frequency

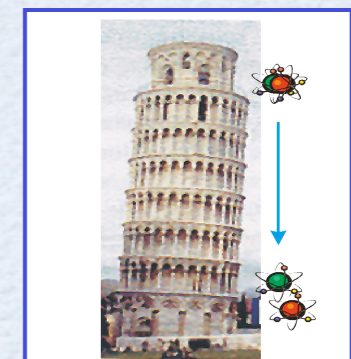
Mapping Lense-Thirring effect close to the Earth



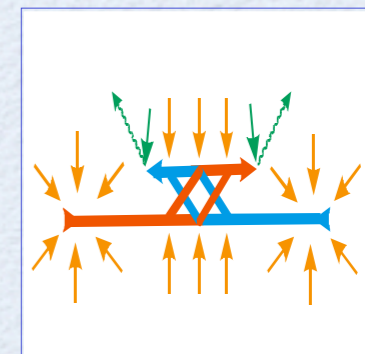
Improving knowledge of fine-structure constant



Testing EP with microscopic bodies



Atomic gyroscope control of a satellite



ESA-SCI (2000) 10  
July 2000

<http://sci.esa.int/home/hyper/index.cfm>





# Space Atom Interferometers

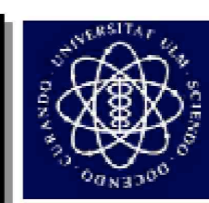
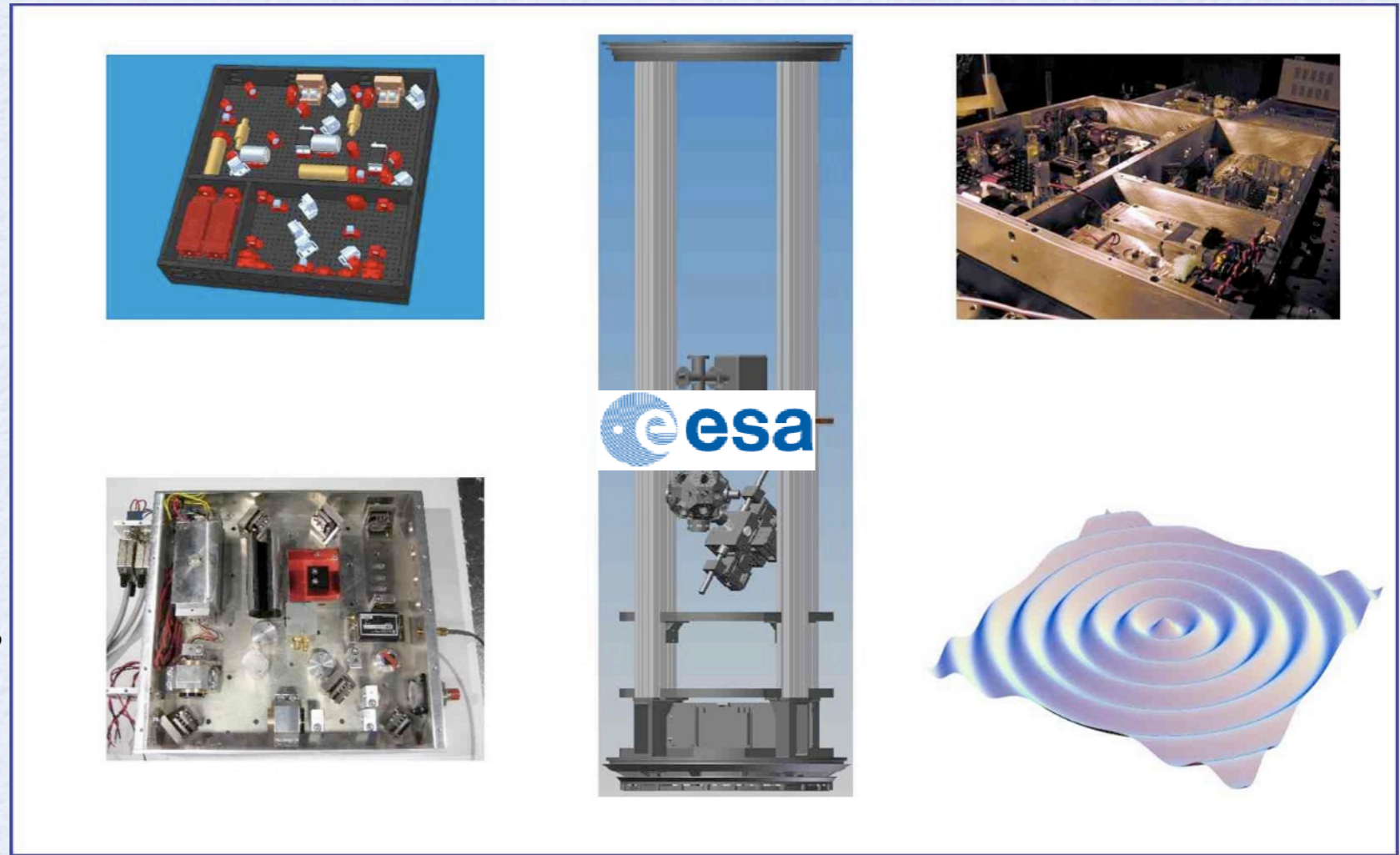


Sensitivity of AI interferometry sensors scale as the square of T  
 In microgravity possible sensitivity  $\sim 10^{-13}$  m/s<sup>2</sup> @ 1 s or better

Main goals:

- ground demonstrator to test technology readiness of atom interferometry sensors for space applications
- Investigation of novel schemes based on quantum degenerate gases

Space-based geodesy, inertial navigation, fundamental physics







# The SAI project



Pre-Phase-A project

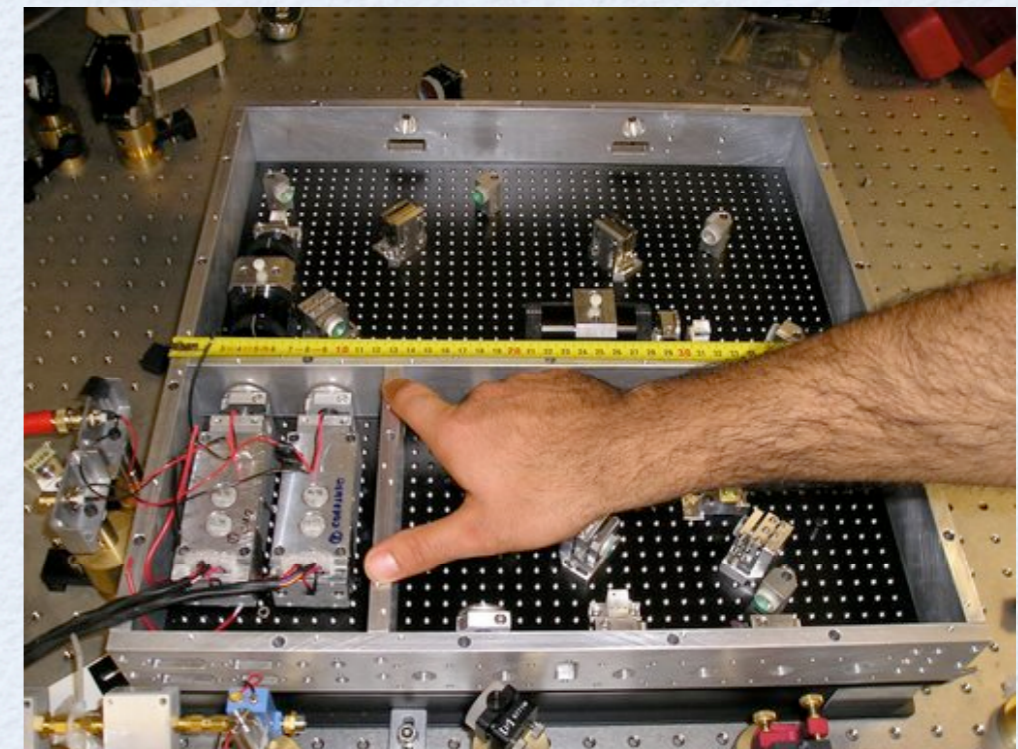
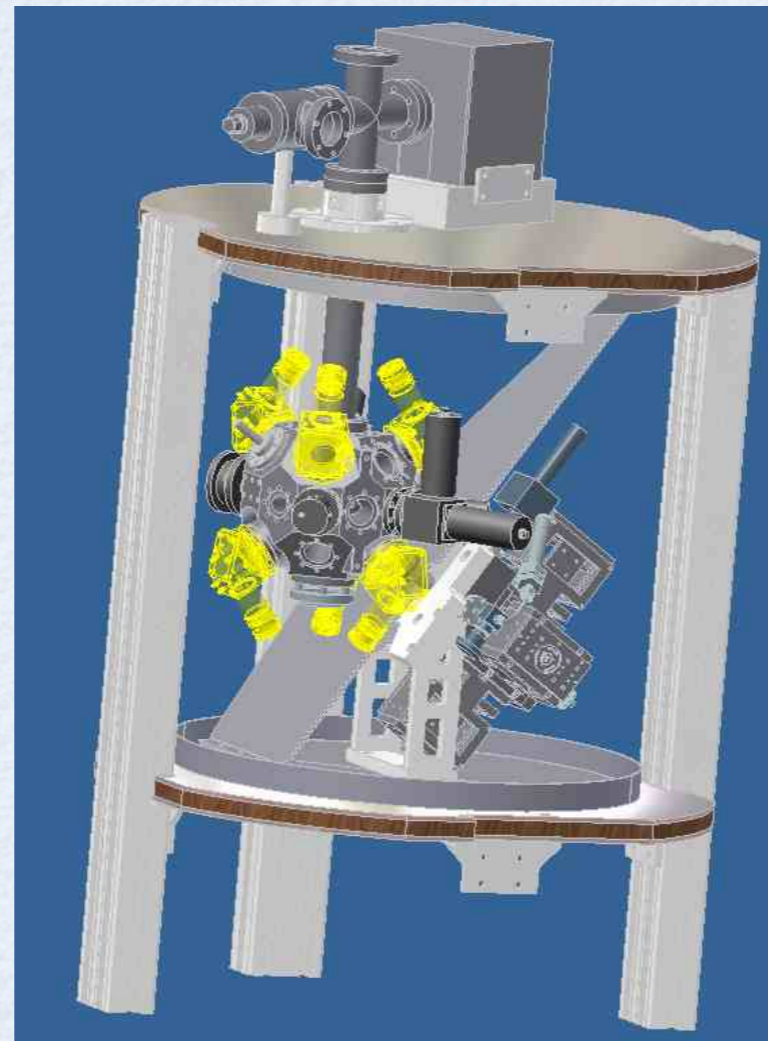
ESA contract n. 20578/07/NL/VJ  
AO-2004-064/082

Contract officer: Dr. L. Cacciapuoti

Project coordinator: Prof. G. M. Tino  
Dipartimento di Fisica and LENS  
Università di Firenze, Italy

SAI team:

Dipartimento di Fisica, Università di Firenze  
Institut für Quantenoptik, Universität Hannover  
Universität Hamburg  
Humboldt-Universität zu Berlin  
SYRTE, Observatoire de Paris  
LENS, Firenze  
Universität Ulm  
ZARM, University of Bremen



F. Sorrentino et al., *A compact atom interferometer for future space missions*,  
*Microgravity Sci. Technol.* **22**, 551 (2010)

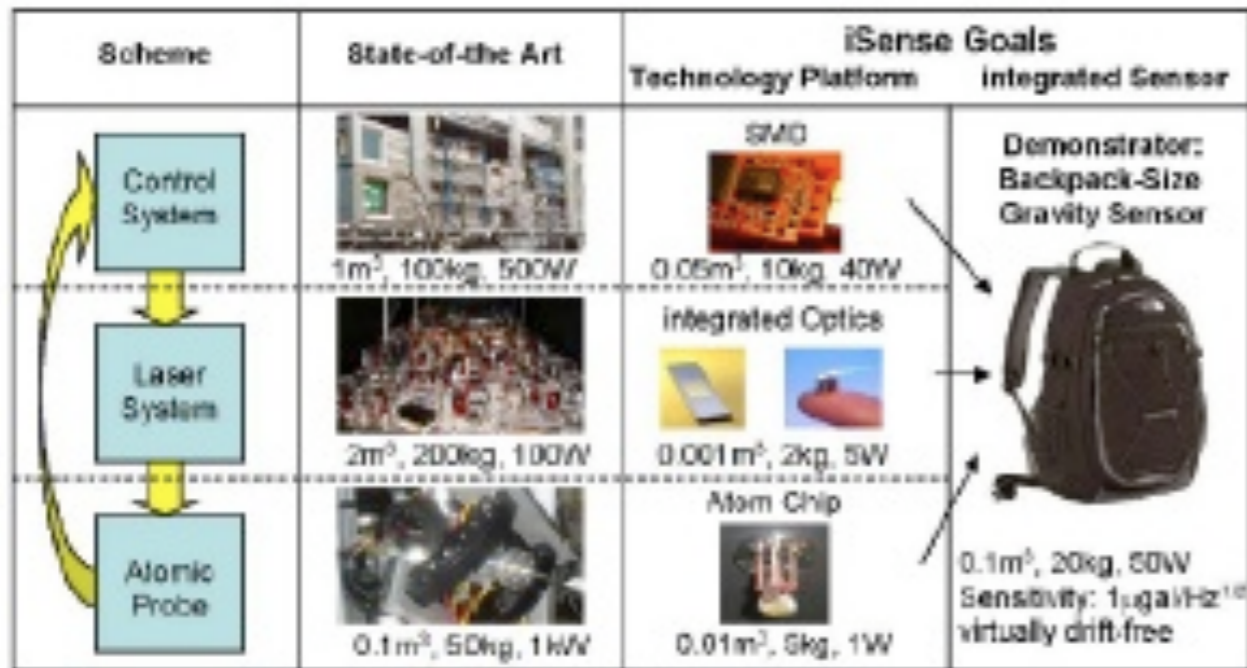




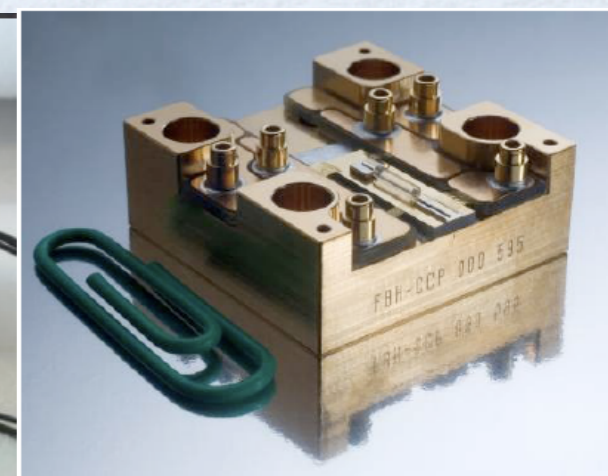
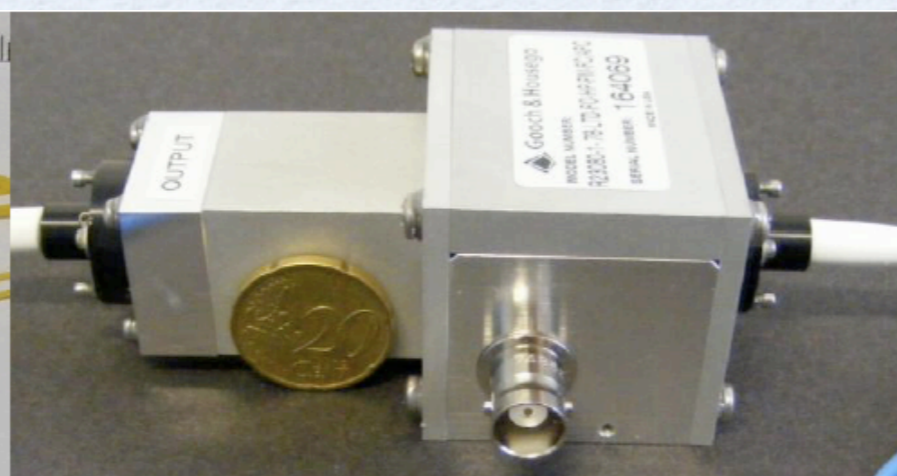
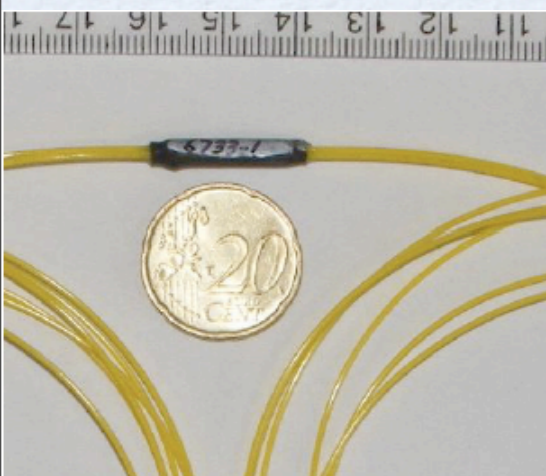
# The iSense project



## 7th Framework Programme - Theme 3 "Information and Communication Technologies" Call identifier: FP7-ICT-2009- C FET-Open



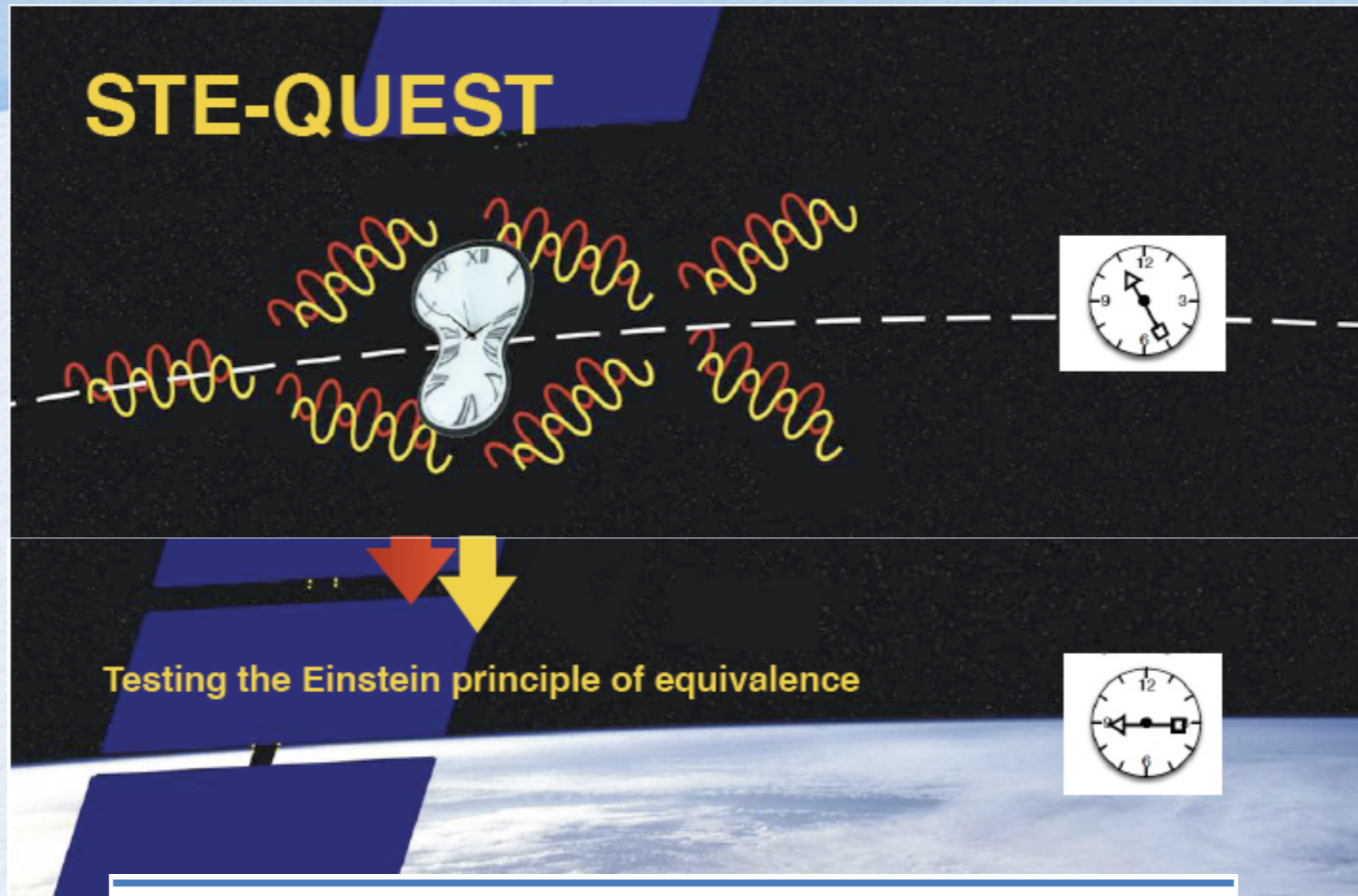
Participant no. *	Participant organisation name	Part. short name	Country
1 (Coordinator)	The University of Birmingham	Bham	UK
2	QinetiQ	QinetiQ	UK
3	University of Hamburg	UHH	D
4	Centre National de la Recherche Scientifique <sup>1</sup>	CNRS	F
5	University of Florence	UNIFI	I
6	Leibniz University Hannover	LUH	D
7	Institute for quantum optics and quantum information - Austrian Academy of Sciences	IQOQI-OEAW	A
8	Ferdinand-Braun-Institut für Höchstfrequenztechnik im Forschungsverbund Berlin e.V.	FBH	D
9	University of Nottingham	Nham	UK







# ESA Cosmic Vision: STE-QUEST





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PHYSICAL REVIEW LETTERS

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## Atom Interferometers with Scalable Enclosed Area

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Bloch oscillations (i.e., coherent acceleration of matter waves by an optical lattice) and Bragg diffraction are integrated into light-pulse atom interferometers with large momentum splitting between the interferometer arms, and hence enhanced sensitivity. Simultaneous acceleration of both arms in the same internal states suppresses systematic effects, and simultaneously running a pair of interferometers suppresses the effect of vibrations. Ramsey-Bordé interferometers using four such Bloch-Bragg-Bloch beam splitters exhibit 15% contrast at  $24\hbar k$  splitting, the largest so far ( $\hbar k$  is the photon momentum); single beam splitters achieve  $88\hbar k$ . The prospects for reaching 100 s of  $\hbar k$  and applications such as gravitational wave sensors are discussed.

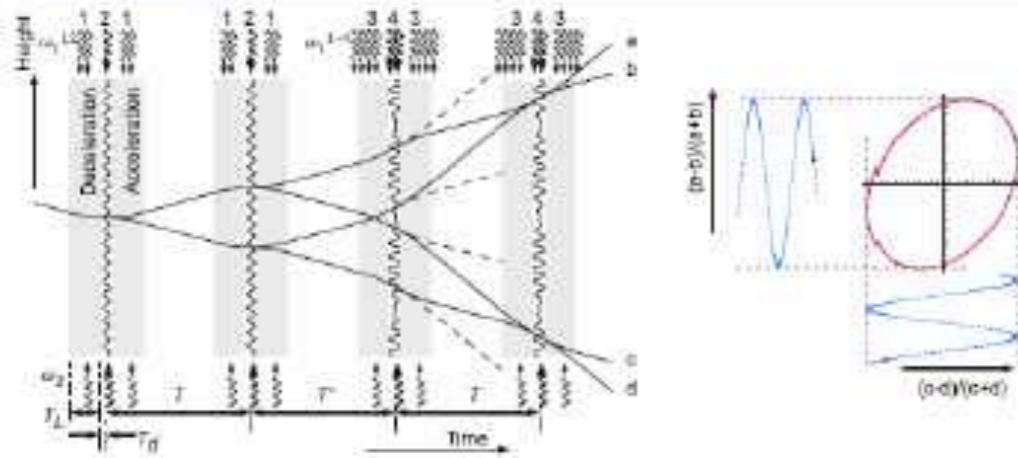
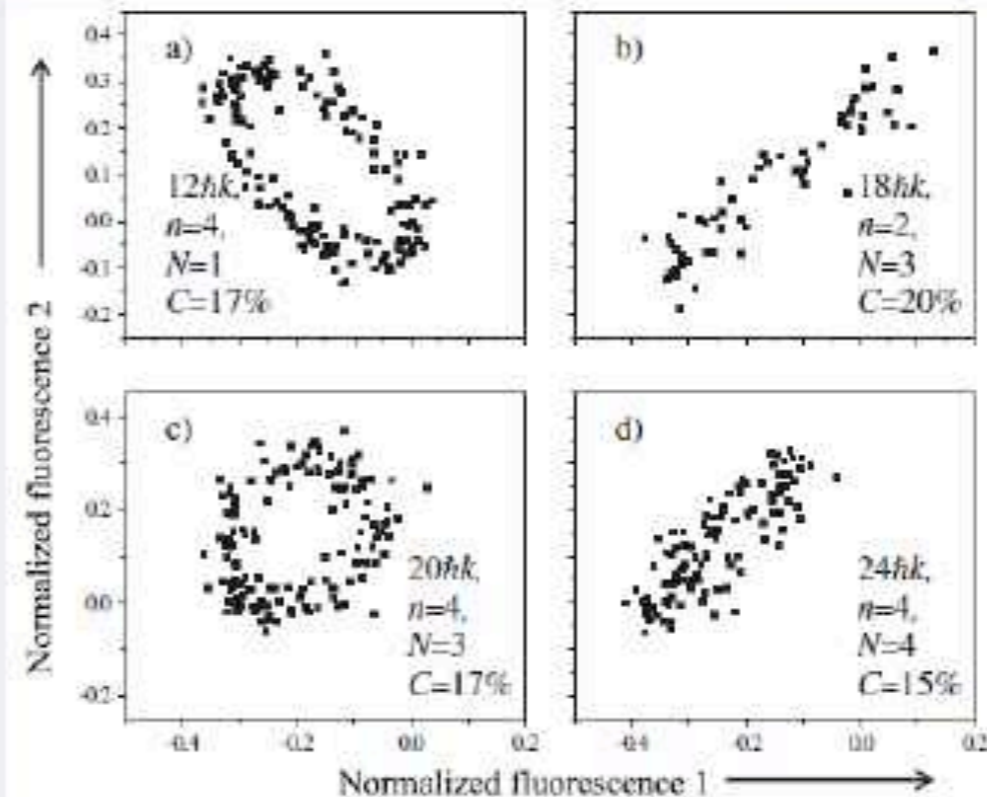


FIG. 1 (color online). Left: space-time diagram of simultaneous conjugate Ramsey-Bordé BBB-interferometers. 1: Dual optical lattice; 2: single Bragg beam splitter; 3: quadruple optical lattice; 4: dual Bragg beam splitter; (a)–(d): outputs. The dashed lines indicate trajectories that do not interfere. Right: plotting the outputs of the interferometers versus one another draws an ellipse.



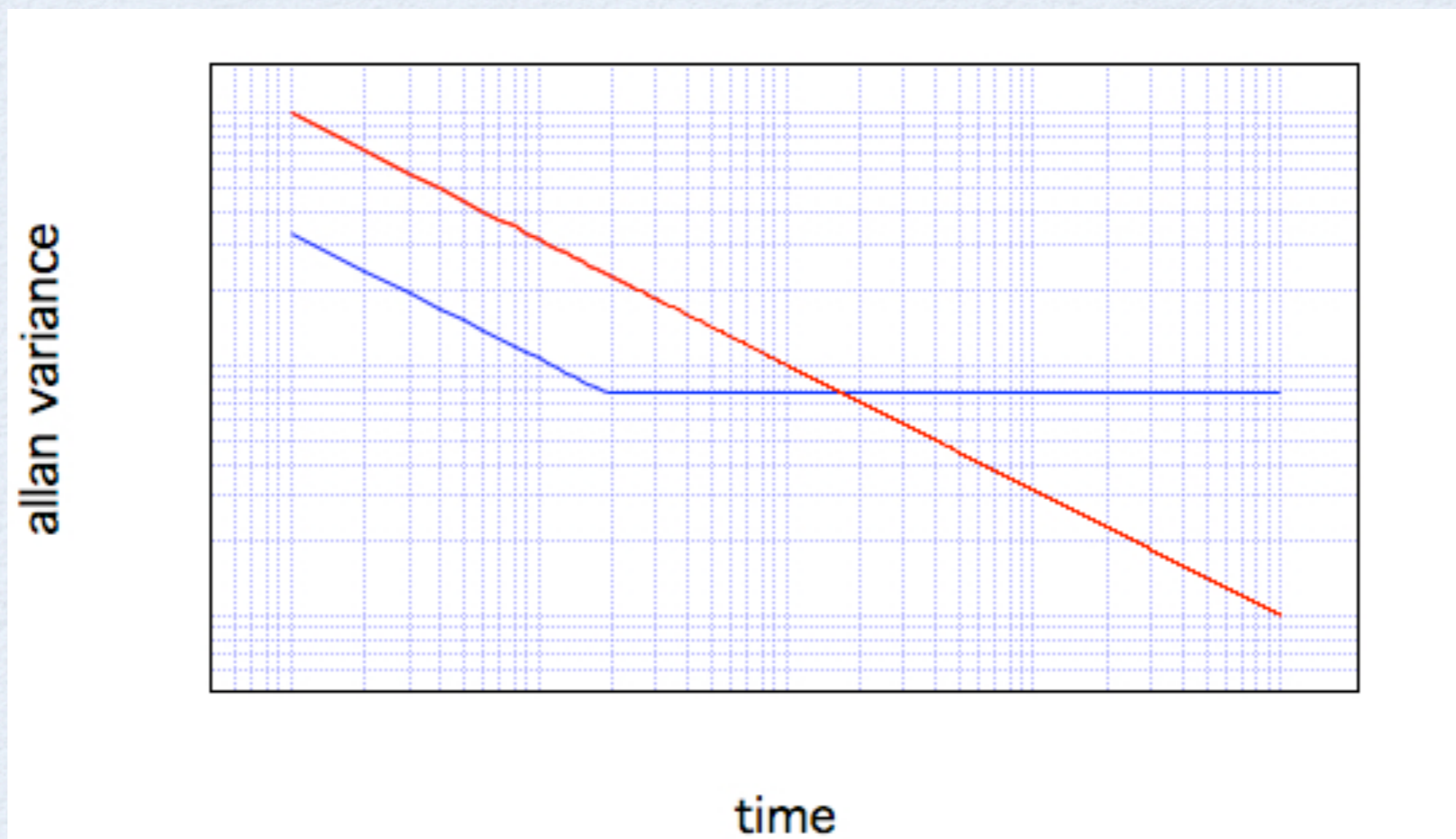




# Combination of atom & optical gyros



- Combination of optimal detection bands
- Tests of quantum gravity







# Red-shift measure with atomic probes



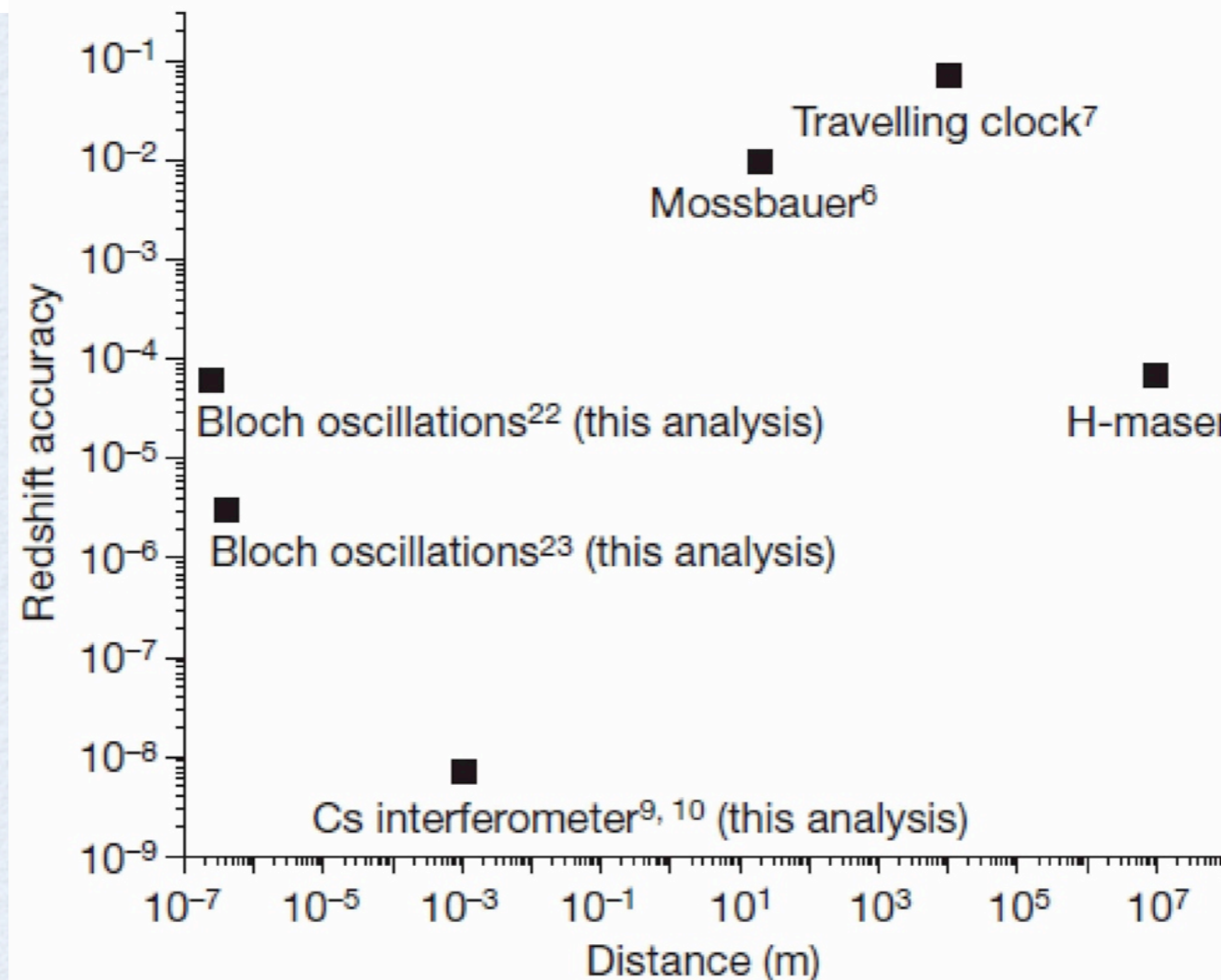
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LETTERS

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## A precision measurement of the gravitational redshift by the interference of matter waves

Holger Müller<sup>1,2</sup>, Achim Peters<sup>3</sup> & Steven Chu<sup>1,2,4</sup>







# Conclusions



- Novel quantum inertial sensors have been developed using ultracold atoms and atom optics
- Particularly promising for long term stability and accuracy
  - MAGIA:  $G$  measured at  $10^{-3}$  level, new measurement at  $10^{-4}$  in progress
  - highly sensitive gyroscopes with thermal atoms, improved devices based on ultracold atoms under development
- Transportable systems have been already demonstrated, space-compatible ones are being developed
- Expected large improvements in next future, exp. in microgravity
- Combination/ comparison with classical sensors may give rise to new schemes for applications of tests of fundamental physics





# Our team



## *G.M. Tino team members*

Nicola Poli                      Researcher, Università di Firenze  
Fiodor Sorrentino              Post-doc, CNR and Università di Firenze  
Yu-Hung Lien                  Post-doc, Università di Firenze/ICTP  
Antonio Giorgini              Post-doc, LENS  
Marco Tarallo                 Post-doc, LENS  
Fu-Yuan Wang                 Post-doc, Università di Firenze/ICTP  
Marco Schioppo                PhD student, Università di Firenze  
Gabriele Rosi                 PhD student, Università di Pisa  
Denis Sutyrin                 PhD student, Università di Pisa  
  
Luigi Cacciapuoti              Long term guest, ESA-Noordwijk  
Marella de Angelis            Long term guest, CNR  
Marco Prevedelli              Long term guest, Università di Bologna

## *Previous members and visitors*

Andrea Alberti, PhD student  
Andrea Bertoldi, Post-doc  
Sergei Chepurov, Institute of Laser Physics, Novosibirsk, visitor  
Robert Drullinger, NIST, Long term guest  
Marco Fattori, PhD student  
Gabriele Ferrari, Researcher, INFN/CNR  
Vladyslav Ivanov, Post-doc  
Marion Jacquy, Post-doc  
Giacomo Lamporesi, PhD student  
Chris Oates, NIST, visitor  
Torsten Petelski, PhD student  
Juergen Stuhler, Post-doc

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- ✓ Agenzia Spaziale Italiana (ASI)
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<http://coldatoms.lens.unifi.it/>