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PIANO NAZIONALE  
DI RIPRESA E RESILIENZA

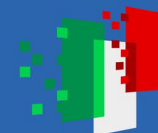
INFN  
Istituto Nazionale di Fisica Nucleare

# Hands-on Session: Examples of wavefront decomposition and curvature calculation from real measurements

**Maria Cifaldi**

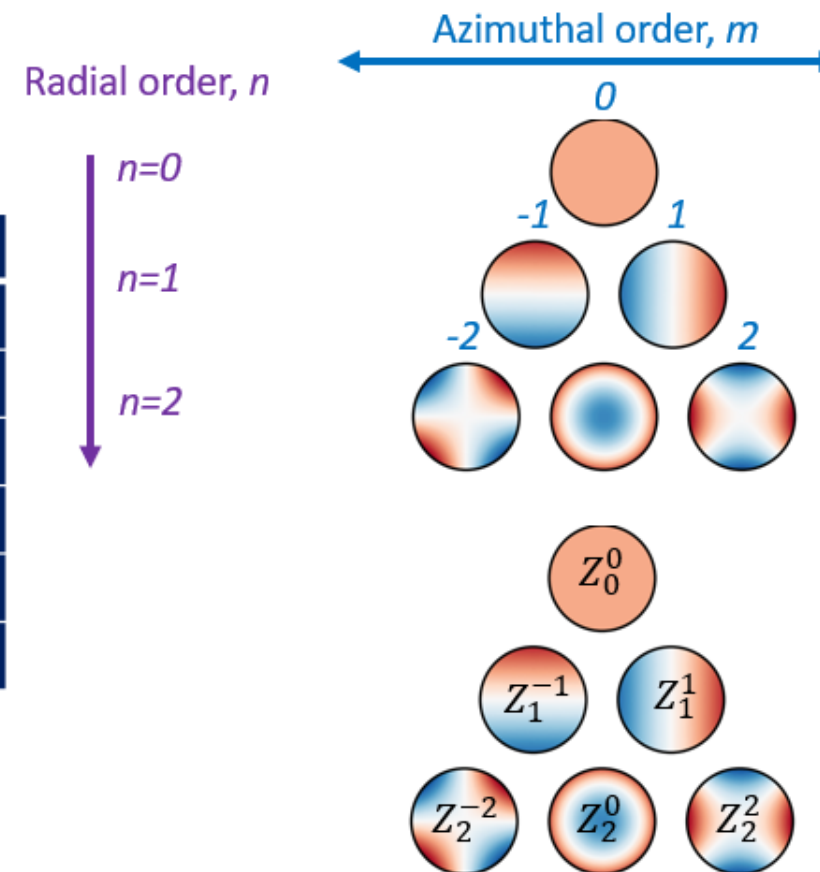
**INFN – Sezione di Roma Tor  
Vergata**

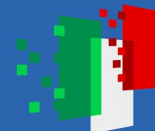




# Zernike polynomials

j	n	m	$Z_n^m$	Meaning
0	0	0	$Z_0^0$	Piston (constant term)
1	1	-1	$Z_1^{-1}$	Tilt in y-direction
2	1	1	$Z_1^1$	Tilt in x-direction
3	2	-2	$Z_2^{-2}$	Astigmatism with axis $\pm 45^\circ$
4	2	0	$Z_2^0$	Field curvature, defocus
5	2	2	$Z_2^2$	Astigmatism with axis at $0^\circ$ or $90^\circ$

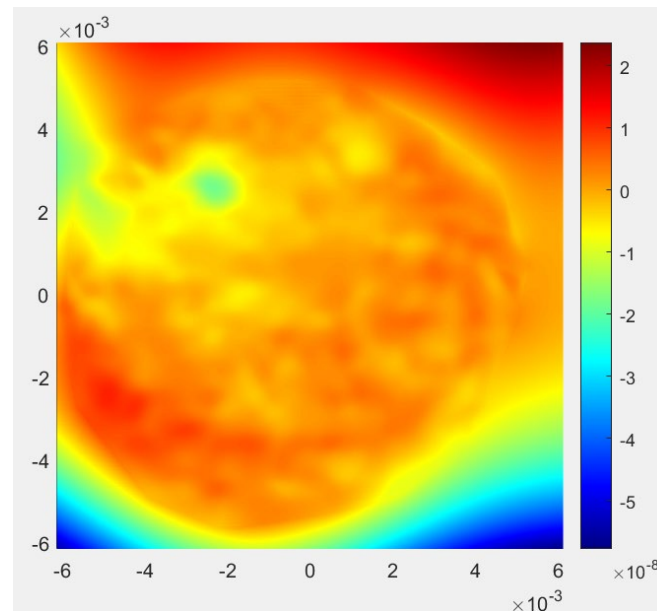




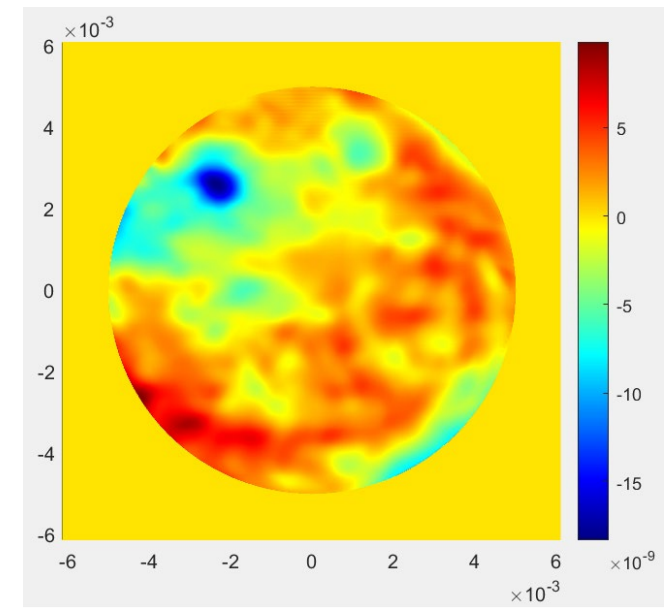
## Zernike polynomials and subtraction

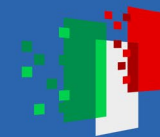
- 1) Zernike polynomials decomposition of the WF
- 2) 2D polynomial fit with  
 $y(r) = a \cdot r^2 + b \cdot x + c \cdot y + d$

Original WF



Piston, Tilt X, Tilt Y, Curv subtracted



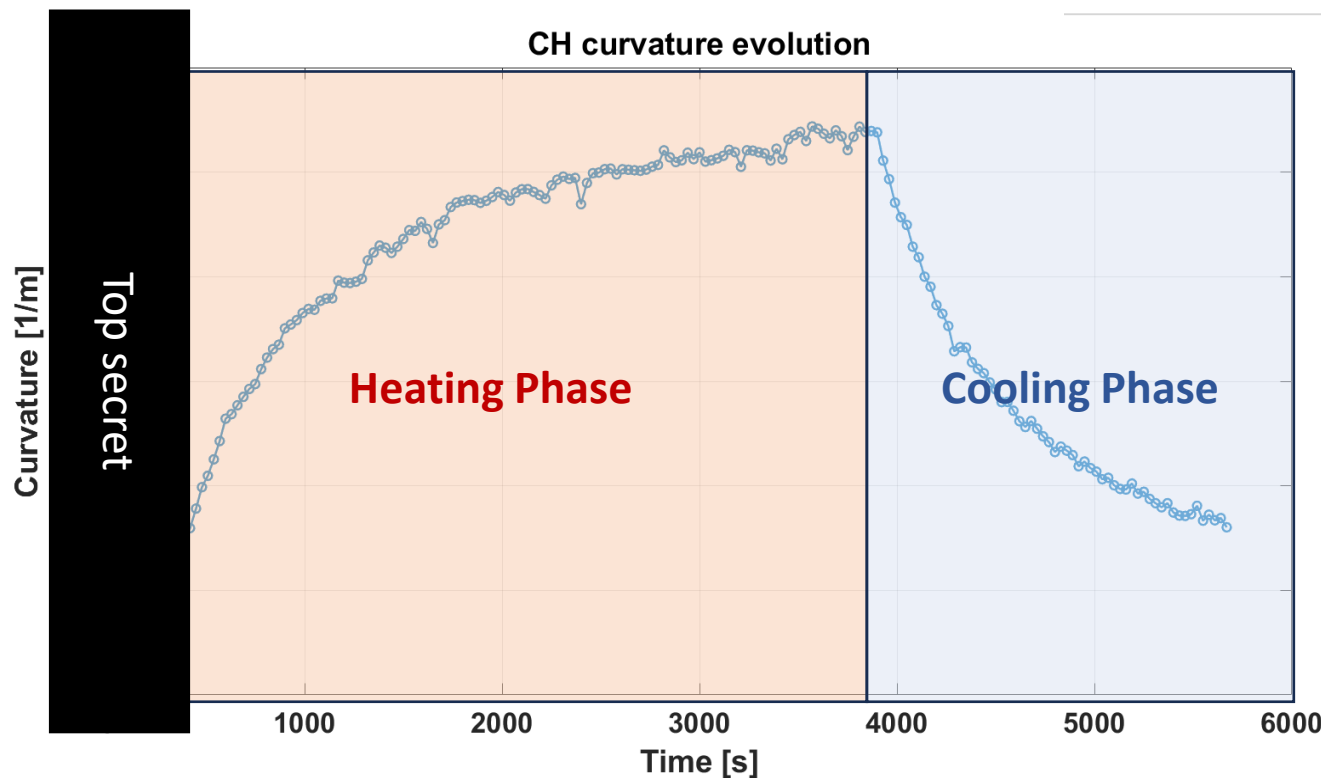


# Measure parameters

## Adv-TCS (CO2 laser projector)

lorenzini, nardecchia, menzione - 18:36 Wednesday 22 February 2023 (58989)

### NI CH, DAS and RH alignment checks--measurements and results



**Goal of the measurements:** Alignment checks

# total WF: 190

Time sleep: 30 s

CH power injected: 120mW

**How to perform an HWS measurement:**

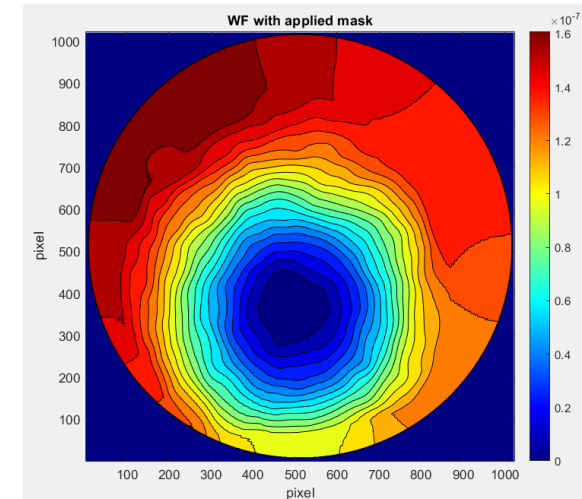
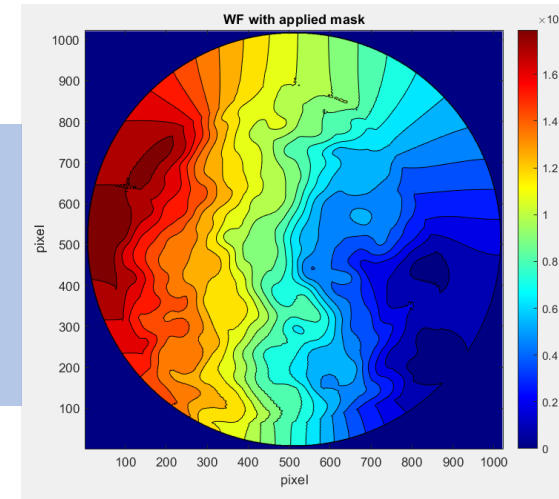
- dark WF
- Reference WF
- Live WFs with a determined sleep time





## Goal of the session:

1. WF analysis with Zernike polynomials decomposition
2. Extraction of the Curvature coefficient
3. Computation of the tau value



$$y(x) = a \cdot \exp\left(-\frac{x - x_0}{\tau}\right) + c$$

plot Time vs Curvature

MATLAB: Curve Fitting

EXCEL

**If we have time:**

Gaussian weighted RMS and  
determination of center coordinates

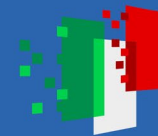
All the material is collected at the [link](#)

**MATLAB script:**

*WF\_analysis\_Zernike\_HANDSON.m*

**Data folder:**

*wavefront*



## Gaussian Weighted RMS

Used to quantify the deviation from an ideal wavefront surface

$$RMS = \sqrt{\sigma_g^2} = \sqrt{\frac{\sum_{m,n} G(x_m, y_m) [h(x_m, y_m) - h_g]^2}{\sum_{m,n} G(x_m, y_m)}}$$

Wavefront distortion

ITF normalized beam  
intensity

$$G(x_m, y_m) = \frac{2}{\pi W_{YAG}^2} e^{-2(x_m^2 + y_m^2)/W_{YAG}^2}$$

$$h_g = \frac{\sum_{m,n} G(x_m, y_m) h(x_m, y_m)}{\sum_{m,n} G(x_m, y_m)}$$