

*JENNIFER3 Kickoff Meeting*

# Study of $B^+ \rightarrow K^+ \nu \bar{\nu}$ with inclusive tag in Belle

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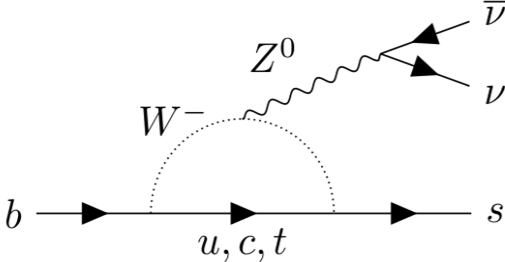
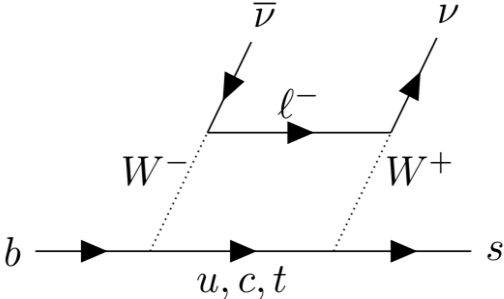
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# Introduction

- Flavour changing neutral current  $b \rightarrow s\nu\bar{\nu}$  transitions offer powerful probe of SM
  - Occur only at loop level  $\rightarrow$  highly suppressed
  - Absence of charged leptons in final state  $\rightarrow$  clean theoretical predictions
- Highly sensitive to any possible new physics contributions
  - Mediators in loops or new tree level diagrams
  - Sources of missing energy (i.e. s+DM)

SM:  $BR(B^+ \rightarrow K^+\nu\bar{\nu}) = 5.58 \pm 0.38 \times 10^{-6}$   
[\[2207.13371\]](#)

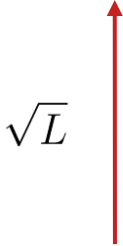


# Introduction

## Previous Belle searches:

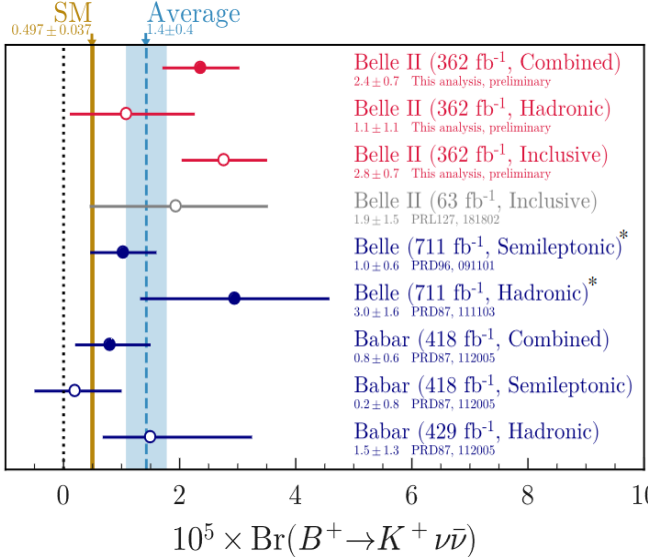
- Hadronic tagged analysis -  $BR(B^+ \rightarrow K^+ \nu \bar{\nu}) = 3.0 \pm 1.6 \times 10^{-5}$
- Semileptonic tagged analysis -  $BR(B^+ \rightarrow K^+ \nu \bar{\nu}) = 1.0 \pm 0.6 \times 10^{-5}$

Belle (**711 fb<sup>-1</sup>**)  
uncertainty:  $0.5 \times 10^{-5}$



Increase in luminosity could see comparable uncertainty to Belle semileptonic analysis

Belle II (**362 fb<sup>-1</sup>**)  
Incl. uncertainty:  $0.7 \times 10^{-5}$

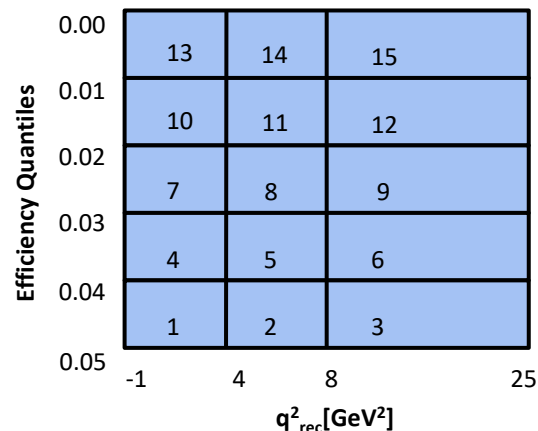
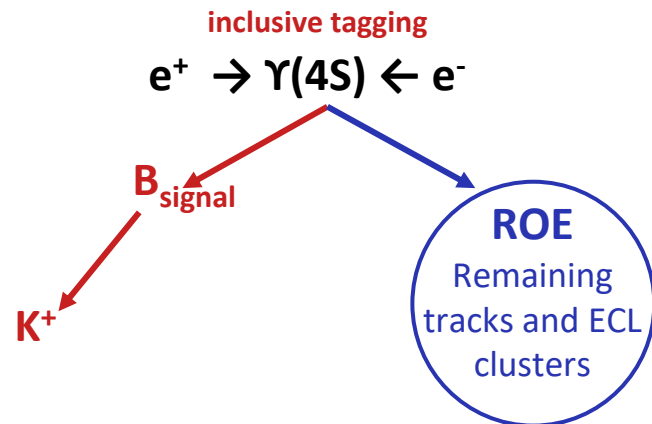


# Analysis overview

- Selection of  $B^+ \rightarrow K^+ \nu \bar{\nu}$  is challenging due to small branching fractions and missing energy from neutrinos
- Use inclusive tagging - signal Kaon + rest of event made of remaining tracks and clusters
- Main steps:
  - Selection of Kaon candidate and some basic event selection criteria
  - Background suppression with 2 BDT classifiers
  - Validation studies of signal efficiency and background modelling
  - 2D binned maximum likelihood fit for extraction of signal strength:

$$\mu = \frac{\text{Br}(B^+ \rightarrow K^+ \nu \bar{\nu})}{\text{Br}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{SM}}}$$

- On-resonance and off-resonance channels used, fit to 1% eff. Quantile vs. 3  $q^2$  bins
- Similar general analysis outline as Belle II study -> independent MC samples and validation



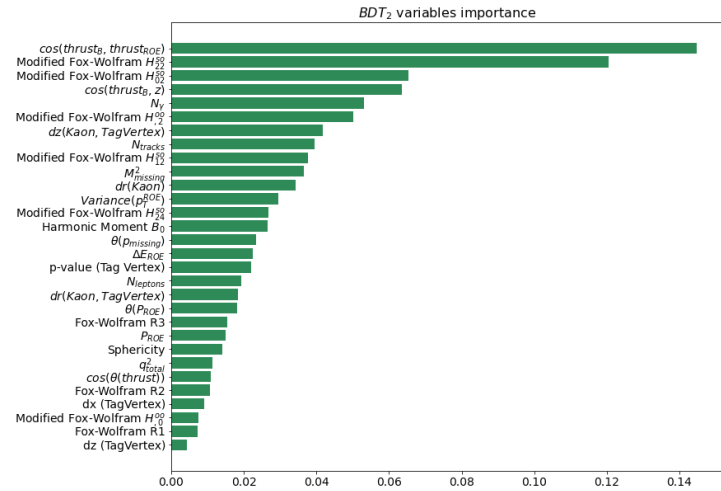
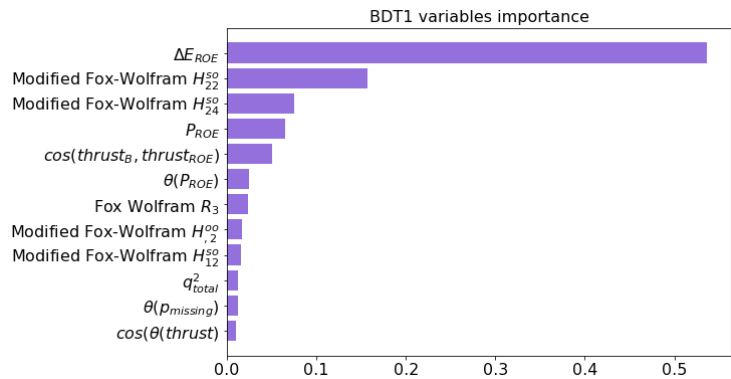
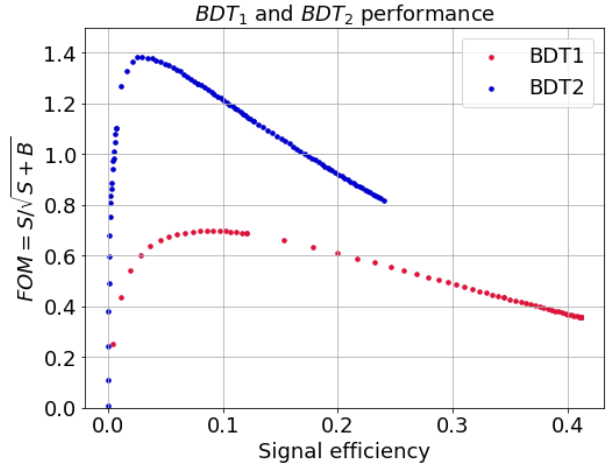
# Selection

1. **BDT<sub>1</sub>**

- a. Trained on sampled 5% of available generic MC (continuum, BBbar, low-multiplicity samples) and dedicated signal sample
- b. 12 input variables - main separation power from ROE  $\Delta E$ , roe P and Fox-Wolfram  $H_{m,2}$
- c. Cuts out large bulk of clear backgrounds (continuum processes)

1. **BDT<sub>2</sub>**

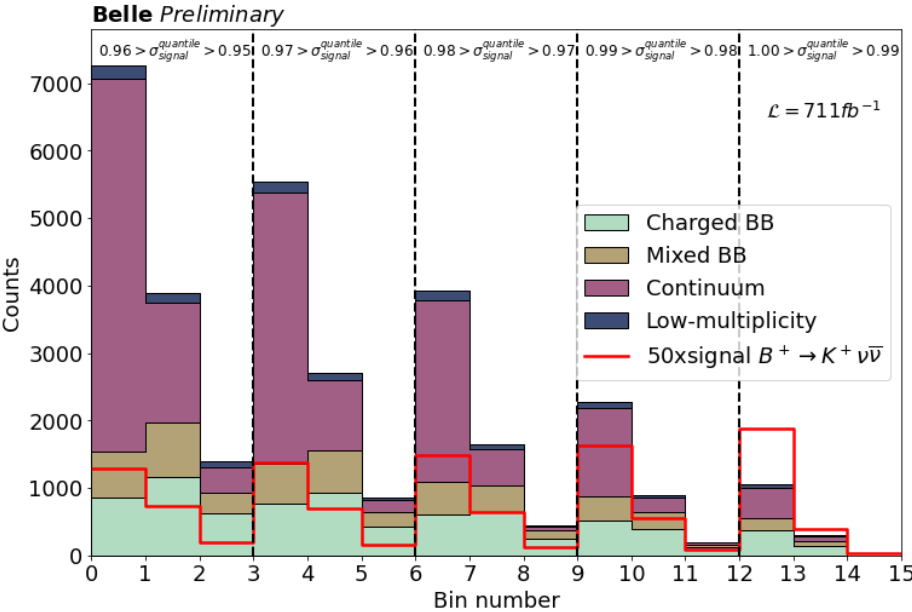
- a. Same 12 variables + 18 more
- b. Much stronger signal selection ability - highest purity region selected for fitting
- c. Trained on sampled 10% of generic MC after BDT1 (continuum, BBbar, low-multiplicity samples) and dedicated signal sample



# Background composition

- Large amount of continuum in less sensitive bins
- In  $B\bar{B}$ :  $\mathbf{B} \rightarrow \mathbf{D}^{(*)} \nu$  backgrounds most dominant in 5% signal efficiency region, affected by  $D \rightarrow K_L^0$  mismodelling in MC
- $\mathbf{B}^+ \rightarrow \mathbf{K}^+ \mathbf{K}^0 \mathbf{K}^0$  and  $\mathbf{B}^+ \rightarrow \mathbf{K}^+ \mathbf{nn}$  - modelled in generic MC according to phase-space assumptions, corrections for branching fractions are then applied

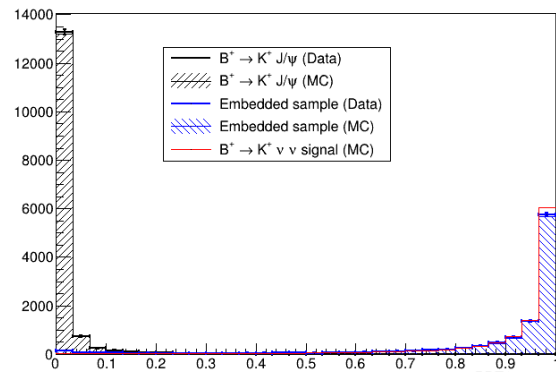
Decay	Fraction, %
1. $B^+ \rightarrow \bar{D}^0 \mu^+ \nu_\mu$	10.3914
2. $B^+ \rightarrow \bar{D}^0 e^+ \nu_e$	7.9187
3. $B^+ \rightarrow \bar{D}^*(2007)^0 \mu^+ \nu_\mu$	5.2443
4. $B^+ \rightarrow \bar{D}^*(2007)^0 e^+ \nu_e$	3.8254
5. $B^+ \rightarrow \bar{D}^0 K^+$	3.705
6. $B^+ \rightarrow \bar{D}^0 \pi^+$	3.1702
7. $B^+ \rightarrow \bar{D}^*(2007)^0 K^+$	2.34
8. $B^+ \rightarrow \bar{D}^*(2007)^0 \pi^+$	2.1714
9. $B^+ \rightarrow \rho(770)^+ \bar{D}^0$	1.7037
10. $B^+ \rightarrow \bar{D}^*(2007)^0 \rho(770)^+$	0.952



- Signal efficiency validation
  - Embedded  $B^+ \rightarrow K^+ J/\psi (\mu^+ \mu^-)$
- Background modelling validation
  - Continuum
    - Off-resonance
  - On-resonance side-band
    - Away from signal region ( $BDT_2 < 0.9$ )
  - $B \rightarrow D(*) \rightarrow K_L^0$  decays
    - PID sidebands - both pion and lepton
  - Others - modelling of BF
    - $B \rightarrow K^+ n n$
    - $B \rightarrow K^+ K^0 K^0$
- PID and neutral reconstruction validation
  - pion  $\rightarrow$  kaon fakes
    - dedicated  $B \rightarrow h D(K\pi)$  sample
  - Others
    - $\phi(K_s^0 K_L^0) \gamma - K_L$  efficiency checks

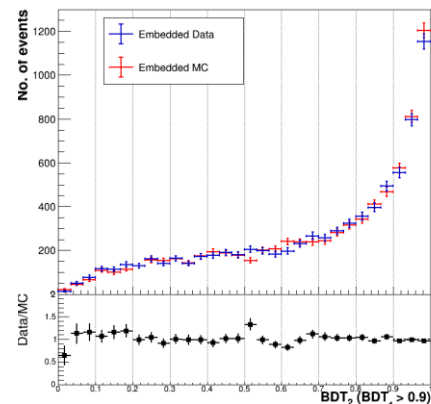
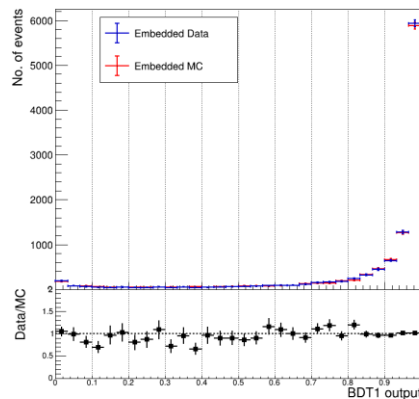
# Signal embedding: $B^+ \rightarrow K^+ J/\psi(\mu^+ \mu^-)$

- $B^+ \rightarrow K^+ J/\psi(\mu^+ \mu^-)$  sample  $\rightarrow$  remove  $J/\psi(\mu^+ \mu^-)$   
 $\rightarrow$  add kaon from  $B^+ \rightarrow K^+ \nu \bar{\nu}$  signal MC (“signal embedding”)
- Good agreement between embedded MC and embedded data



Selection efficiency in the signal region for the embedded data and MC samples

Sample	Efficiency
Data	0.0622 +/- 0.0020
MC	0.0633 +/- 0.0020
<b>Ratio</b>	<b>0.9833 +/- 0.0443</b>



The data-MC comparison of BDT1 (left) and BDT2 (right) outputs

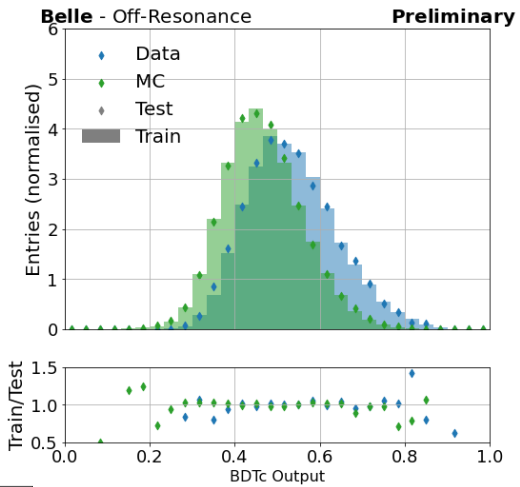
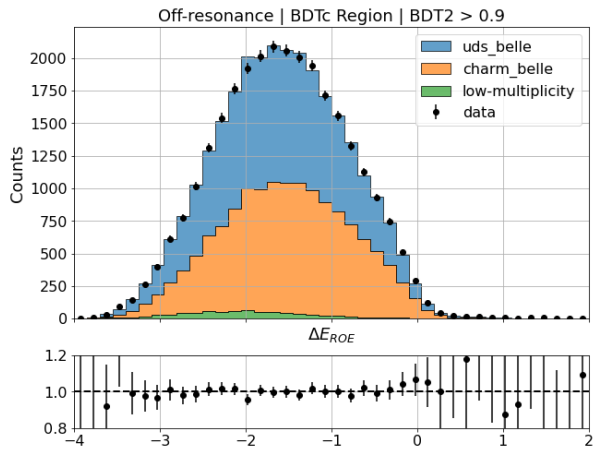
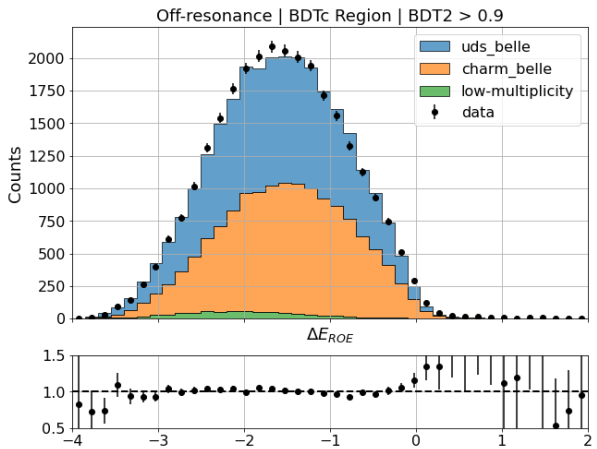


# Off-resonance control sample

- Slight mismodelling of continuum data/MC after BDT1 is observed in off-resonance control sample
- A dedicated BDT (called BDTc) is trained to correct for **shape** disagreement
- MC events are assigned weight according to the output of BDTc as:

$$w = \frac{p}{1 - p}$$

- Improved data/MC agreement with the BDTc reweighting applied



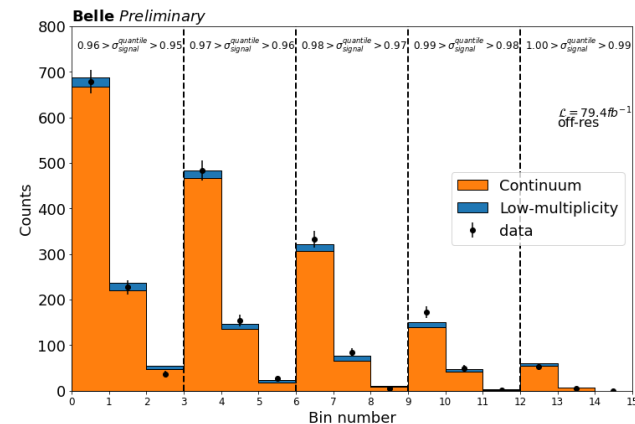
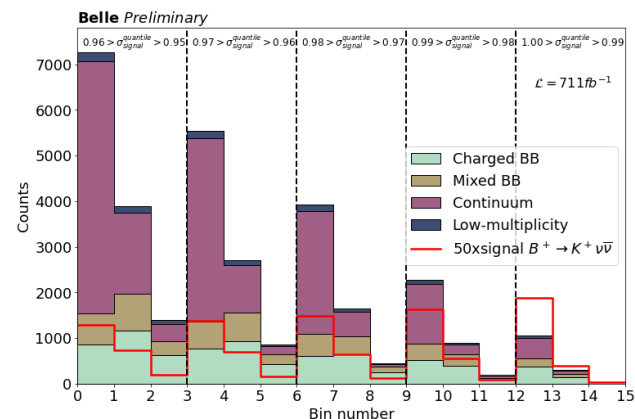
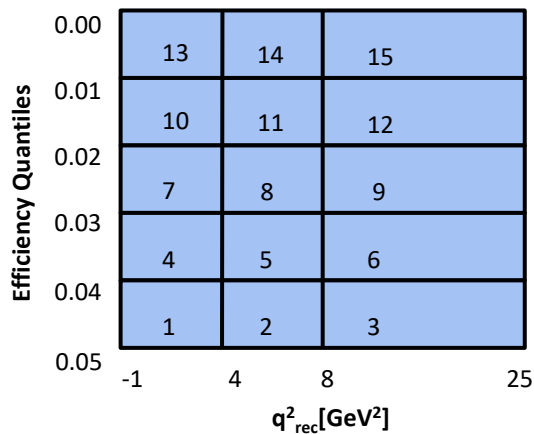
# Signal extraction

- Simultaneous binned maximum likelihood fit of 15 bins  $\eta(\text{BDT}_2) \times q^2_{\text{rec}}$  with both on-resonance and off-resonance channels - template fit in pyhf

- Measure signal strength

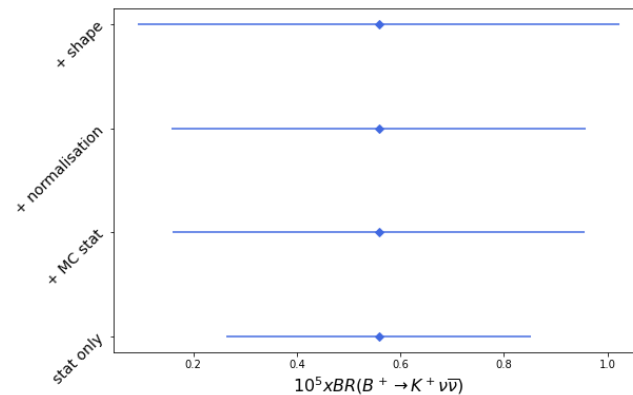
$$\mu = \frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})}{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{SM}}$$

- Systematic uncertainties included as nuisance parameters - correlations between off-resonance channel and continuum samples in on-resonance channel



# Systematic uncertainties

Source	MC Correction	$N_{nuis.param.}$	Uncertainty Size
$B\bar{B}$ norm.	-	1 Global	70%
Leading $B\bar{B}$ backgrounds	-	10, Shape	$\mathcal{O}(1\%)$
$B \rightarrow D^{(*)}$ modelling	-	10, Shape	50%
$B^+ \rightarrow K^+ n\bar{n}$ modelling	bin-dependent	1, Shape	100%
$B \rightarrow (D \rightarrow K_L^0)$ modelling	+35%	1, Shape	10%
Signal FF	bin-dependent	1, Shape	6-18%
Continuum norm	-	1 Global	70%
Continuum shape	-	1, Shape	2%
Low-multi norm	-	1 Global	70%
Low-multi shape	-	1, Shape	2%
$B^+ \rightarrow K^+ K^0 \bar{K}^0$ shape	bin-dependent	1, Shape	2%
$K_L^0$ efficiency	+10%	1 Global	10%
Luminosity	-	1 Global	TBD
particle ID	bin-dependent	1 Global	TBD
Tracking	-	1 Global	0.35%
MC statistics	-	90, Shape	-



Current total uncertainty estimation (preliminary):  
 **$BF=0.504 \pm 0.47 \times 10^{-5}$**

*\* off-resonance check*

*\* pionID and muonID sidebands checks*

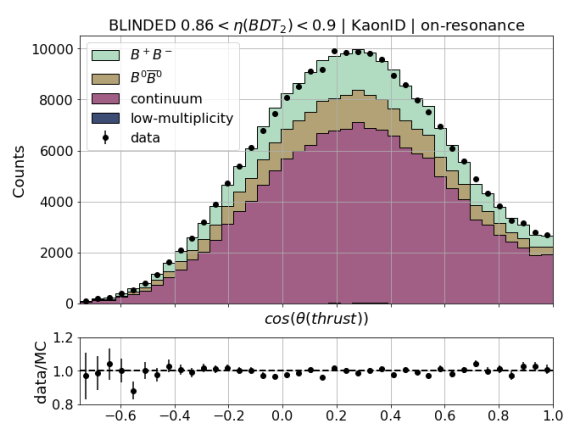
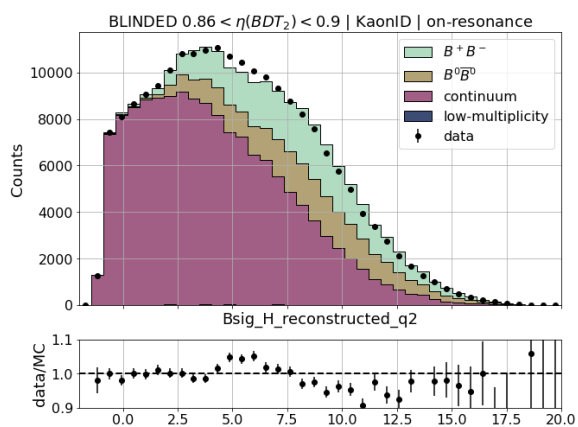
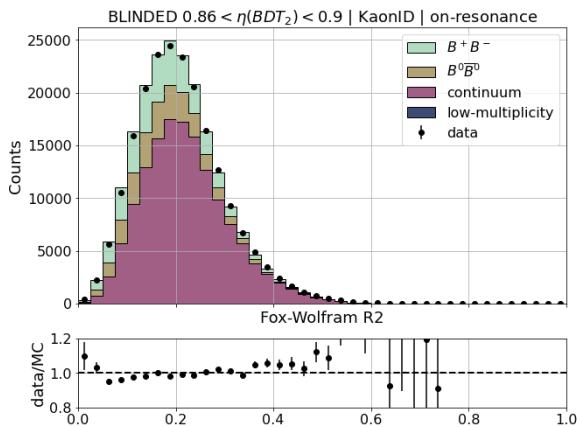
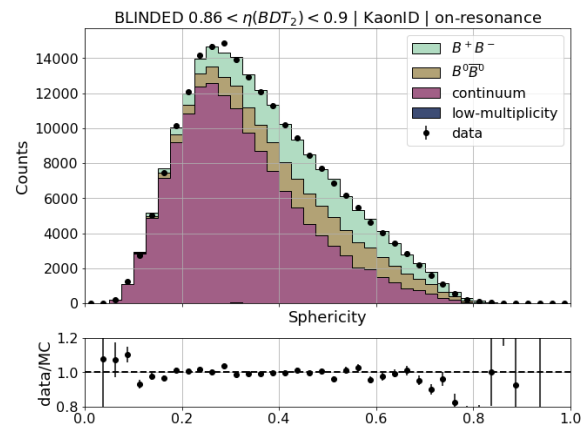
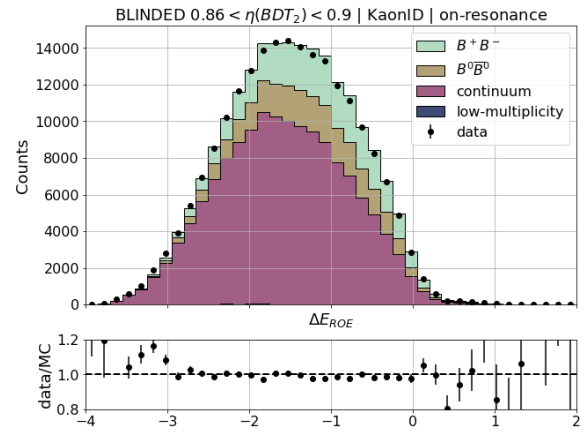
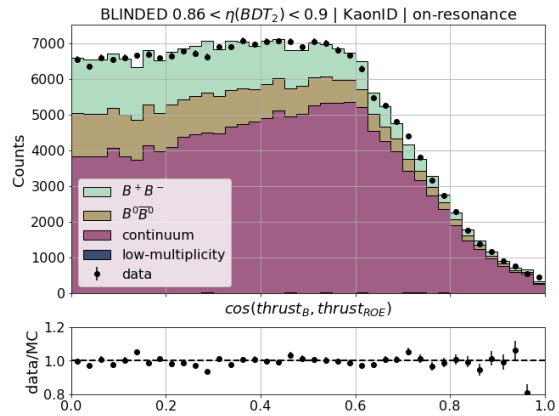
*\* reweighting according to Babar studies*

*\* q2 distribution reweighted according to theory prediction*

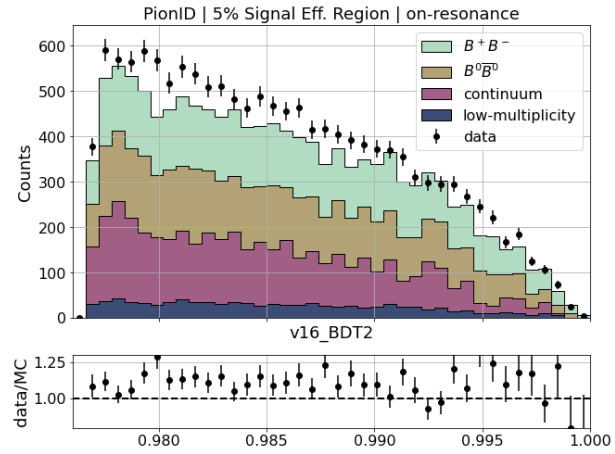
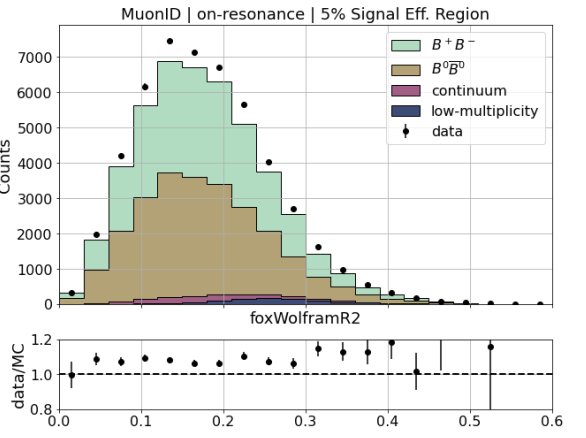
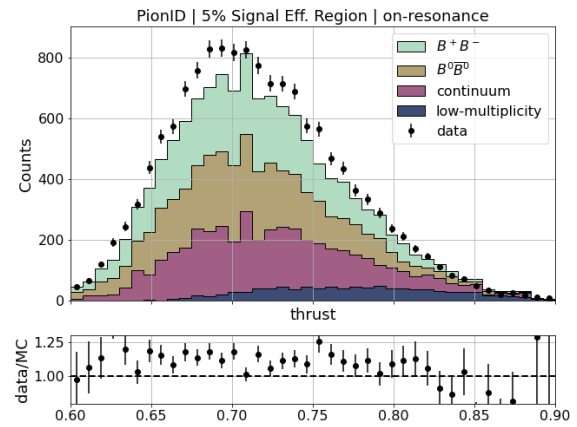
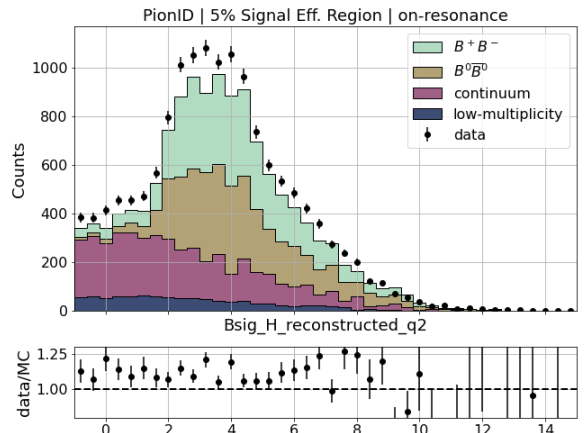
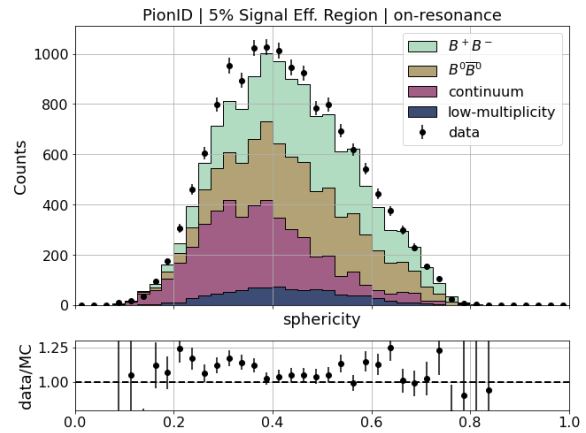
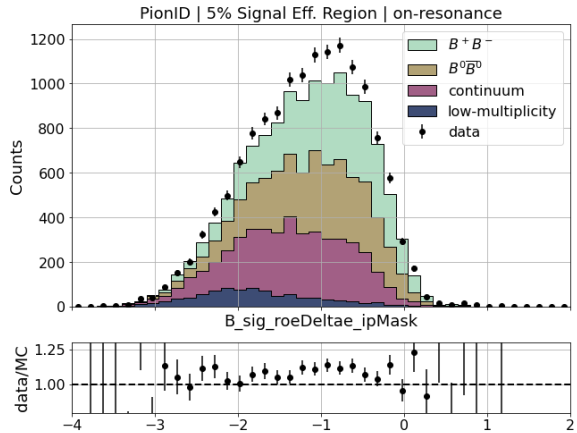
- Inclusive analysis of  $B^+ \rightarrow K^+ \nu \bar{\nu}$  decays using full 711 fb<sup>-1</sup> Belle data:
  - Preliminary sensitivity comparable to Belle II inclusive tag
  - Selection and signal region optimisation completed
  - Background suppression using two consecutive BDTs
  - Extensive validations studies completed
    - Corrections determined from off-resonance sideband checks
    - Signal efficiency validated using embedded sample
    - Good agreement in on-resonance sideband (BDT<sub>2</sub> < 0.9)
    - $D \rightarrow K_L^0$  scaling determined from pion and muon sideband checks
  - Simultaneous binned 2D maximum likelihood fit of on-resonance and off-resonance samples for extraction of  $B^+ \rightarrow K^+ \nu \bar{\nu}$  signal strength
  - Ongoing work to finalize all systematic sources in template fit
- **Aiming for summer conferences 2025**

# Backup

# On-resonance sideband



# PionID sideband - on-resonance



## Fit to determine D->K0L scaling

-----	-----	-----
mu	1.39236	0.0627678
bkg_norm	0.069394	0.992569
cont_norm	0.0773284	0.0901136
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In fit:

***variable used -  $q^2$***

mu - parameter of interest

other B bkg normalisation - vary by 1%

continuum normalisation - vary by 50%

