# The Tracking Code RF-Track v2.3.1

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- 1. Introduction and highlights
- 2. Beam models
- 3. Beamline elements
- 4. Collective effects
- 5. Examples of applications
- 6. Summary and future developments

# Introduction and highlights

# Motivation for developing RF-Track: the TULIP project

A linac for hadron therapy featuring high-gradient S-band backward travelling-wave structures



S. Benedetti, A. Grudiev, and A. Latina, "High gradient linac for proton therapy", Phys. Rev. Accel. Beams 20, 040101 [2017]

# **RF-Track requisites and highlights**

- $\bullet\,$  It handles  $\mathbb{C}omplex\; 3D$  field maps of oscillating RF electromagnetic fields:
  - Standing-wave; Backward  $\ll$  and Forward  $\gg$  travelling-wave fields
  - Static electric and magnetic fields
  - Robust interpolation algorithms
- It can simulate particles with any mass and charge
  - No approximations, like  $\beta \simeq 1$  or  $\gamma \gg 1$ , are made
  - It is used to simulate: protons, ions, electrons, positrons, photons, muons, ... from creation to ultra-relativistic
  - It implements photocathodes
  - It can simulate mixed-species beams
- Implements high-order adaptive integration algorithms
  - Can do back-tracking
- Implements several collective effects
- It's modular, flexible, and fast

# **RF-Track: minimalistic and physics-oriented**

RF-Track is a module that can be used through **two different user interfaces**: one in **Octave** and one in **Python**. Written in **parallel** and **optimised** C++, RF-Track focuses solely on accelerator simulation:

- Flexible accelerator description and beam models
- Accurate integration of the equations of motion
- Robust field map interpolation
- Collective effects
- Easy implementation of imperfections and correction algorithms

For *"all the rest"* (ODE solvers, random number generation, special functions, ...), it relies on two robust and well-known open-source libraries:

- <u>GSL</u>, "Gnu Scientific Library", provides a wide range of mathematical routines such as high-quality random number generators, ODE integrators, linear algebra, and much more
- <u>FFTW</u>, "Fastest Fourier Transform in the West", arguably the fastest free library to compute discrete Fourier transforms

# **Beam models**

## Two beam models: tracking in space and in time

RF-Track implements two beam models:

- 1. Beam moving in space: Bunch6d()
  - All particles have the same S position
  - The equations of motion are integrated in  $dS: S \rightarrow S + dS$  (moves the bunch element by element)

(x [mm], x' [mrad], y [mm], y' [mrad], t [mm/c], P [MeV/c])

- 2. Beam moving in time: Bunch6dT()
  - All particles are considered at same time t
  - The equations of motion are integrated in dt:  $t \rightarrow t + dt$
  - Particles can have  $P_z < 0$  or even  $P_z = 0$ : particles can move backward

(X [mm], P<sub>x</sub> [MeV/c], Y [mm], P<sub>y</sub> [MeV/c], Z [mm], P<sub>z</sub> [MeV/c])

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(X [mm], P<sub>x</sub> [MeV/c], Y [mm], P<sub>y</sub> [MeV/c], Z [mm], P<sub>z</sub> [MeV/c])

For each macro particle also considers

m : mass [MeV/c<sup>2</sup>], Q : charge [ $e^+$ ]

N : nb of particles / macroparticle,  $t_0$  : creation time<sup>(\*)</sup>

au: lifetime [NEW!]

(\*) only for beams moving in time.

#### RF-Track can simulate multi-species beams and the creation and decay of particles.

# **Bunch creation**

Particle bunches can be created in multiple ways:

- 1. From arbitrary distributions, directly importing the phase space
- 2. From a set of Twiss parameters
- From a Photocathode simulation similar to ASTRA's "Generator" 1D distributions: 'gaussian', 'uniform', 'plateau', 'parabola' 2D distributions: 'radial-uniform', 'radial-pleateau', 'radial-gaussian', 'radial-parabola'

3D distributions: 'ellipsoid', 'isotropic', 'fermi-dirac'





Since version 2.3.0, it is possible to create multi-bunch beams.

Example of multi-bunch beam definition:

```
% Define a bunch
mass = electronmass;
charge = 1 * nC;
q = -1;
bunch = Bunch6d(mass, charge, q, phase_space);
% Define the train structure
num_of_bunches = 30; % train length
bunch_spacing = 1/3 * ns; % bunch spacing
% Define a beam
B0 = Beam(bunch, bunch_spacing, num_of_bunches);
```

A native multi-bunch implementation ease and speed up the computation of bunch-to-bunch collective effects.

# Two tracking environments

#### Lattice: for space integration

- A list of elements
- Tracks the particles element by element, along the longitudinal direction
- Elements can be arbitrarily misaligned

#### Volume: for time integration

- A portion of 3D space
- Elements can be placed anywhere
- Element misalignment via Euler angles (pitch, yaw, roll)
- Allows element overlap
- Allows creation of particles
- Can simulate cathodes and field emission
- Includes cathode mirror charges





# Lattice and Volume

Lattice and Volume can be used together or separately. Example: a photoinjector



Typically, Volume (time integration) is suitable for space-charge dominated regimes, whereas Lattice (space integration) is suitable for ultra-relativistic regions of the machine.

Notice that Volumes can be inserted in a Lattice, and Lattices can be placed in a Volume.

#### Volume as a Lattice element

Example of field map:



#### Volume as a Lattice element

Boundaries of a Volume:



#### The boundaries of a Volume can have any orientation in space.

#### Volume as a Lattice element

Boundaries of a Volume:



#### A Volume can be sandwiched between two Lattices.

## Example of Volume (Octave)

#### RF\_Track;

```
L = 0; % length [m]
B = 1; % field at the center of the coil [T]
R = 0.2; % coil radius [m]
Cm = Coil(L, -B, R);
Cp = Coil(L, +B, R);
V = Volume():
V.add(Cm, 0, 0, -0.5, 'center');
V.add(Cp, 0, 0, 0.5, 'center');
figure(1)
Za = linspace(-1e3, +1e3, 1000); % mm
[E,B] = V.get_field(0, 0, Za, 0);
plot(Za, B(:,3));
xlabel('S [mm]'):
ylabel('B_z [T]');
```





## Example of Lattice (Octave)

```
% load RF-Track
RF_Track:
% create a bunch from phase-space matrix
B0 = Bunch6d(electronmass, 200 * pC, -1, phase_space_matrix);
% create a lattice (1 FODO cell)
Lq = 0.4; \% m
Ld = 0.6; \% m
G = 1.2; % T/m
FODO = Lattice();
FODO.append (Ouadrupole (La, G)):
FODO.append (Drift (Ld));
FODO.append (Quadrupole (Lq, -G));
FODO.append (Drift (Ld)):
% track the beam
B1 = FODO.track(B0);
% plot the phase space
T1 = B1.aet_phase_space("%x %xp %v %vp");
scatter (T1(:,1), T1(:,2), "*");
xlabel ("x [mm]");
vlabel ("x' [mrad]"):
```

# **Beamline elements**

## Overview of the beamline elements

- 1. Standard set of matrix-based symplectic elements:
  - Sector bend
  - Quadrupole
  - **Drift** (with an optional constant electric and magnetic fields, can be used to simulate e.g., rectangular bends)

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- 2. Field maps (see next slides)
- 3. Special elements:
  - Absorber (predefined materials: air, water, beryllium, lithium, tungsten, ... )
  - 3D analytic fields: Coil and Solenoid, Undulator, Standing-wave and Traveling-wave structures, Adiabatic matching devices, Toroidal Harmonics
  - LaserBeam for Inverse Compton Scattering simulations
  - Electron Cooler
  - **Transfer Line**: tracks through an arbitrary lattice given in form of Twiss table (phase advances, momentum compaction, 1<sup>st</sup> and 2<sup>nd</sup> order chromaticity are considered)
  - Screens: to capture the phase space at any point with any orientation in space

In field maps and analytic fields, RF-Track integrates the equations of motion numerically:

- The default is: "leapfrog":
  - \* super fast, second-order accurate
- "analytic" algorithm:
  - \* integration assuming a locally-constant EM field
- Higher-order, adaptive algorithms provided by GSL:
  - \*"**rk2**" Runge-Kutta (2, 3)
- \*"**rkck**" Runge-Kutta Cash-Karp (4, 5)
  - \*"**rk4**" 4th order Runge-Kutta \*"**rk8pd**" Runge-Kutta Prince-Dormand (8, 9)
  - \*"rkf45" Runge-Kutta-Fehlberg (4, 5) \*"msadams" multistep Adams in Nordsieck form (order varies dynamically between 1 and 12)

#### (backtracking is possible)

In Lattice, a Solenoid is a standard **symplectic transfer matrix**. In Volume, a Solenoid is the three-dimensional field generated by an **arbitrary number of thin sheets of current**:



Solenoid field computed by RF-Track.

#### [ Plot courtesy of Bernd Michael Stechauner, CERN ]

# The element Undulator

A symplectic implementation of an Undulator, using a 3D field.

```
U = Undulator (lperiod, K, nperiods, kx2=0);
```



Undulator field and single-partcle trajectories as computed by RF-Track.

#### **Field maps**

RF-Track can import several types of oscillating RF field maps, which are interpolated linearly or cubically

- 1D field maps (on-axis field)
  - It uses Maxwell's equations to reconstruct the 3D fields off-axis, assuming cylindrical symmetry
- 2D field maps: given a field on a plane, applies cylindrical symmetry
- 3D field maps of oscillating electro-magnetic fields
  - Accepts 3D meshes of complex numbers
  - Accepts quarter field maps and automatically performs mirroring
  - For RF fields, allows specifying the input power supplied to the structure
  - Treats "NaN" in the field map as walls for accurate 3D loss maps

It also provides elements dedicated to StaticElectric and StaticMagnetic field maps

• They ensure curl-free (electric) and divergence-free (magnetic) interpolation of the field

#### Field maps of magnetic elements

Static\_Magnetic\_FieldMap corrects any input field map (whether measured or computed), and makes it physically correct. This ensures symplecticity



Magnetic chicane for the FCC-ee's positron source.

[ Field map courtesy of Riccardo Zennaro (PSI); Plots courtesy of Yuting Wang, IJCLab ]

#### The element LaserBeam and Inverse Compton Scattering

A collision with a LaserBeam can be added to any Lattice, using the element "LaserBeam":

```
X angle = 2: \% deg. crossing angle
                                                                                dN / dE' [10<sup>6</sup> ph / (keV bx)]
0.0
0.0
0.0
nX = sind(180-X_angle);
nZ = cosd(180-X anale):
%% Define laser-beam IP region
FP = LaserBeam(); % ICS interaction point
FP.pulse_energy = 28; % mJ, laser pulse energy
                                                                                    0
                                                                                          10
FP.pulse length = 5: \% ps. laser pulse length
FP.wavelenath = 1030; % nm, laser wavelenath
FP.set direction (nX, 0, nZ): % laser incoming direction
FP.lenath = IP lenath:
                                                                                   0.3
FP.set_IP_position (IP_length): % m
                                                                                   0.2
FP.R = 0.035; % mm, laser rms radius at waist, Gaussian profile
                                                                                   0.1
FP.M2 = 1.1: \%
                                                                                ۲ [mm]
                                                                                   0
```



The **photons** are added to the bunch and **transported** through the beam line.

## **Element hierarchy**





Collective and Single-particle effects

# Overview of the collective and single-particle effects

#### Collective effects:

- Space-charge, full 3D, Particle-in-Cell (FFT) or P2P
  - Full computation of electric and magnetic effects
  - Beam-beam effects are automatically included
  - Optionally considers mirror charges at cathode
- Short-range wakefields:
  - Karl Bane's approximation
  - 1D user-defined spline, longitudinal monopole or transverse dipole
- Two models of Long-range wakefields:
  - 1. Sum of damped oscillators. Takes modes: frequency, amplitude, and Q factor
  - 2. 1D user-defined spline, longitudinal monopole or transverse dipole
- Self-consistent Beam loading effect in TW and SW structures
  - Given: R/Q, group velocity, and Q factors along the structure, computes the beam loaded fields

Single-particle effects:

- Incoherent Synchrotron Radiation (from any fields)
- Magnetic multipole kicks for imperfection studies
- Multiple Coulomb Scattering (recently updated)

# Space-charge effects (1/4)

Benchmark against ASTRA:

#### Simulation of the CLEAR photoinjector:

- Q = 600 pC
- Gun, Ez = 100 MV/m, f = 3 GHz
- Peak energy phase for the reference particle
- Solenoid, Bz = 0.25 T ON | **OFF**
- Space-charge ON | OFF

50'000 macro particles



Solenoid OFF – Space-charge OFF

# Space-charge effects (2/4)

Benchmark against ASTRA:

#### Simulation of the CLEAR photoinjector:

- Q = 600 pC
- Gun, Ez = 100 MV/m, f = 3 GHz
- Peak energy phase for the reference particle
- Solenoid, Bz = 0.25 T ON | **OFF**
- Space-charge
   ON | OFF

50'000 macro particles



# Space-charge effects (3/4)

Benchmark against ASTRA:

#### Simulation of the CLEAR photoinjector:

- Q = 600 pC
- Gun, Ez = 100 MV/m, f = 3 GHz
- Peak energy phase for the reference particle
- Solenoid, Bz = 0.25 T **ON** | OFF
- Space-charge
   ON | OFF

50'000 macro particles



Solenoid ON – Space-charge ON

# DC gun

#### Electrostatic Gun (Astra, GPT, RFT)

Ez = -1 MV/m B = realistic solenoid, B max = 0.25 T No SC



#### Beam loading in standing-wave structures

Beam-loading effects have also been computed in standing-wave structures.

Follow the example of the photoinjector of the CLEAR test facility at CERN. The plots show the beam-induced energy loss of a train of 150 bunches with 1.5 GHz bunch-spacing, as a function of the bunch charge.

Beam parameter (end of linac)	Value range
Energy	60 - 220 MeV
Bunch charge	0.01 - 1.5 nC
Normalized emittances	3 um for 0.05 nC per bunch 20 um for 0.4 nC per bunch (in both planes)
Bunch length	~100 um - 1.2 mm
Relative energy spread	< 0.2 % rms (< 1 MeV FWHM)
Repetition rate	0.8 - 10 Hz
Number of micro-bunches in train	1 - 150
Micro-bunch spacing	1.5 or 3.0 GHz



# (A) Experimental measurements(B) RF-Track simulation

J. H. Olivares et al., "Implementation of the beam-loading effect in the tracking code RF-track based on a power-diffusive model", Frontiers in Physics, 2024

## Beam loading in traveling-wave structures

A **power diffusive model** computes beam loaded field in an RF structure. Both **transient** and **steady state** can be computed. Beam-loading **compensation** schemes can be computed.

Usage example:

```
%% Transient Beam loading
BL = BeamLoading (Ncells, freq, phaseadvance, QQ, R_Q, VG);
%% RF-element from field map
TWS = RF_FieldMap_1d_CINT ( Ez, hz, L, freq, +1 );
TWS.set_Odeint_algorithm( "rk2" );
TWS.set_P_map( Pmap );
TWS.set_P_actual( Pactual );
TWS.add_collective_effect ( BL );
TWS.set_cfx_nsteps ( 20 );
```

The plots show beam loading effects in a CLIC accelerator structure with a beam of  $352 \times 600 \text{ pC}$  bunches with a 2 GHz bunch spacing.



# **Examples of applications**

RF-Track is currently used for the design, optimisation, and simulation of:

- Medical applications (**DEFT facility**, collaboration CERN, CHUV, THERYQ), the **CLIC** and **FCC-ee positron sources** (CERN, IJCLab, PSI) and **FCC-ee pre-injector linacs** (CERN, PSI)

- Linac4 (CERN), Inverse-Compton Scattering sources (CERN, IJCLab, INFN Ferrara, Korea University), and the Cooling channel of a future Muon Collider (CERN), etc.

I'll show two examples:

- 1. CLIC and FCC-ee positron sources
- 2. ADAM's RFQ
- 3. Linac4  $H^-$  source at CERN
- 4. Cooling channel for a future muon collider

# 1. CLIC positron source

#### Start-to-end optimisation of the CLIC positron source



- · More realistic simulations than any previous studies
- Start-to-end optimisation with higher positron yield than any previous studies ~1.8 @ 380 GeV (~2.4 @ 3 TeV)

#### Work by Yongke Zhao (CERN)

## 2. The RFQ of the ADAM linear accelerator for proton therapy

«LIGHT is a normal conducting 230 MeV medical proton linear accelerator being constructed by ADAM.

For the commissioning, RFQ beam dynamics simulations were performed with RF-Track by simulating the particles through the 3D field map.»



Figure 1: Layout of the LIGHT structures during the beam commissioning at 5 MeV.



Figure 7: Horizontal phase space plots of the RFQ input beam when steered in the negative and positive x directions (first row), expected (second row) and the measured (third row) phase space plots after the RFQ for each case.

V. Dimov et al., "Beam commissioning of the 750 MHz proton RFQ for the LIGHT prototype", IPAC2018, Vancouver, BC, Canada, TUPAF002

Preliminary results of the simulation of the Linac4 source:  $H^-$  ions are generated by ionising hydrogen gas, utilising plasma confinement, cesium injection for enhanced ion production, and electrostatic fields for extraction.

The ions are then accelerated in the Linac4 before being stripped of their electrons at 160 MeV to form protons.

- In this case, 5 eV H<sup>-</sup> are simulated
- Simultaneous simulation of ions and electrons possible



Credits: Bernd Stechauner (CERN)



This simulation includes: 3D solenoids, standing-wave structures, absorbers – overlapping. 35/37 A. Latina – The tracking code RF-Track, LNF-INFN, November 2024

# Summary and future developments

#### RF-Track:

- Minimalistic, parallel, fast implements several collective effects
- Friendly and flexible, it uses Octave and Python as user interfaces
- Ideal for nontrivial optimisations and numerical experimentations
- Currently used to design and optimise: FCC-ee pre-injectors, CLIC and FCC-ee positron sources, muon cooling channel, RFQ, Linac4, ICS sources, medical accelerators...

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#### Next steps:

- Add Intra-beam scattering (IN TESTING PHASE), 3D Coherent synchrotron radiation (ASAP)
- Interface to SUPERFISH and CST Studio (done)

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#### Pre-compiled binaries and more up-to-date documentation are available here:

• https://gitlab.cern.ch/rf-track

Python users can use:

• pip install RF\_Track

# Thank you for your attention!



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