High-precision measurement of the *W* boson mass with the CMS experiment

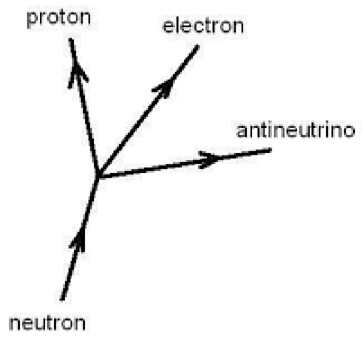
arXiv:2412.13872

Lorenzo Bianchini
Università & INFN Pisa

Towards the W boson

- **E. Fermi** (1934): a theory of β-decay

$$G_F = 1.166 \times 10^{-5}\ \text{GeV}^{-2}$$



FERMI BETA DECAY THEORY, 1934

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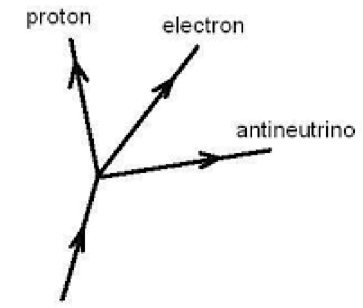

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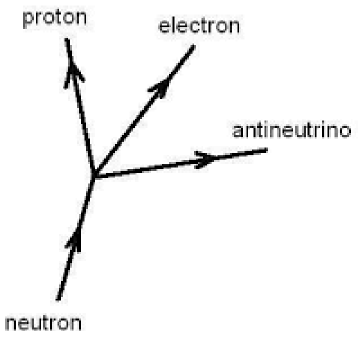

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$$\begin{cases} m_W^2 = \dfrac{\pi\ \alpha_{EM}}{\sqrt{2}G_F\ \sin^2\theta_W} \gtrsim (40\ \mathrm{GeV})^2 \\ m_Z^2 = \dfrac{\pi\ \alpha_{EM}}{\sqrt{2}G_F\ \sin^2\theta_W\ \cos^2\theta_W} \gtrsim (80\ \mathrm{GeV})^2 \end{cases}$$

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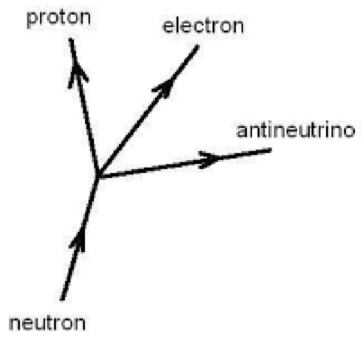

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$m_W \in [60,80]$ GeV
$m_Z \in [75,92]$ GeV

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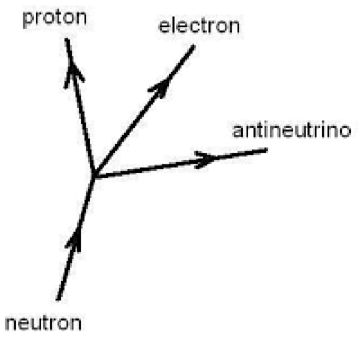

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- **C. Rubbia *et al.*** (1983): W, Z discovery ⇒ $m_W = \mathbf{80.2} \pm 1.5$ GeV, $m_Z = \mathbf{91.5} \pm 1.8$ GeV

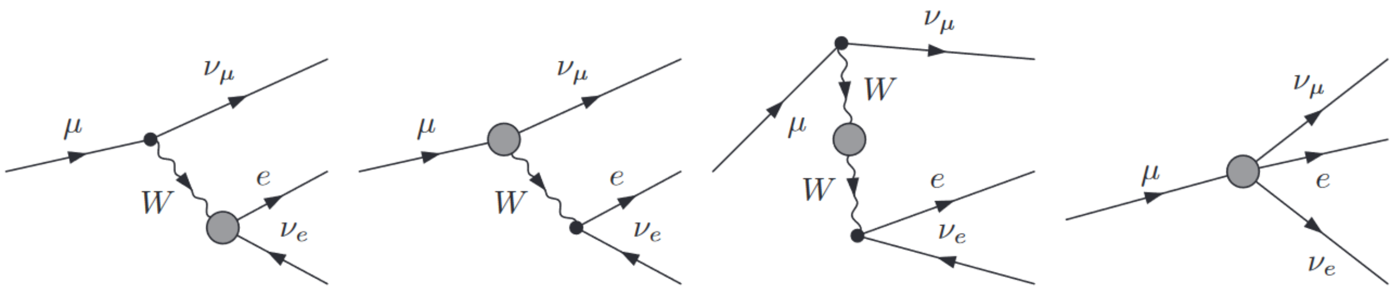
The SM prediction for m_W

$$\boldsymbol{m_W^2} = \frac{\boldsymbol{m_Z^2}}{2}\left(1 + \sqrt{1 - \frac{4\pi\, \alpha_{EM}}{\sqrt{2} G_F \boldsymbol{m_Z^2}}}\right)$$

See e.g. JHEP 05 (2015) 154
W. Hollik's talk

The SM prediction for m_W

$$m_W^2 = \frac{m_Z^2}{2}\left(1+\sqrt{1-\frac{4\pi\,\alpha_{EM}}{\sqrt{2}G_F m_Z^2}}\right) \Rightarrow \frac{m_Z^2}{2}\left(1+\sqrt{1-\frac{4\pi\,\alpha_{EM}}{\sqrt{2}G_F m_Z^2}(1+\Delta r)}\right)$$



$+\ \ldots$

$$\Delta r = -\frac{3G_F m_t^2}{8\sqrt{2}\pi^2\tan^2\theta_W} + \frac{11G_F m_W^2}{24\sqrt{2}\pi^2}\ln\frac{m_H^2}{m_W^2} + \cdots$$

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$$\begin{cases} m_Z = 911880 \pm 2.0\ \text{MeV} \\ m_H = 125.20 \pm 0.11\ \text{GeV} \\ m_t = 172.57 \pm 0.29\ \text{GeV} \end{cases}$$

Full 2 loops + QCD/EWK
@ 3,4-loops

$$m_W = \mathbf{80353 \pm 6\ MeV}$$

(75 ppm)

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BSM

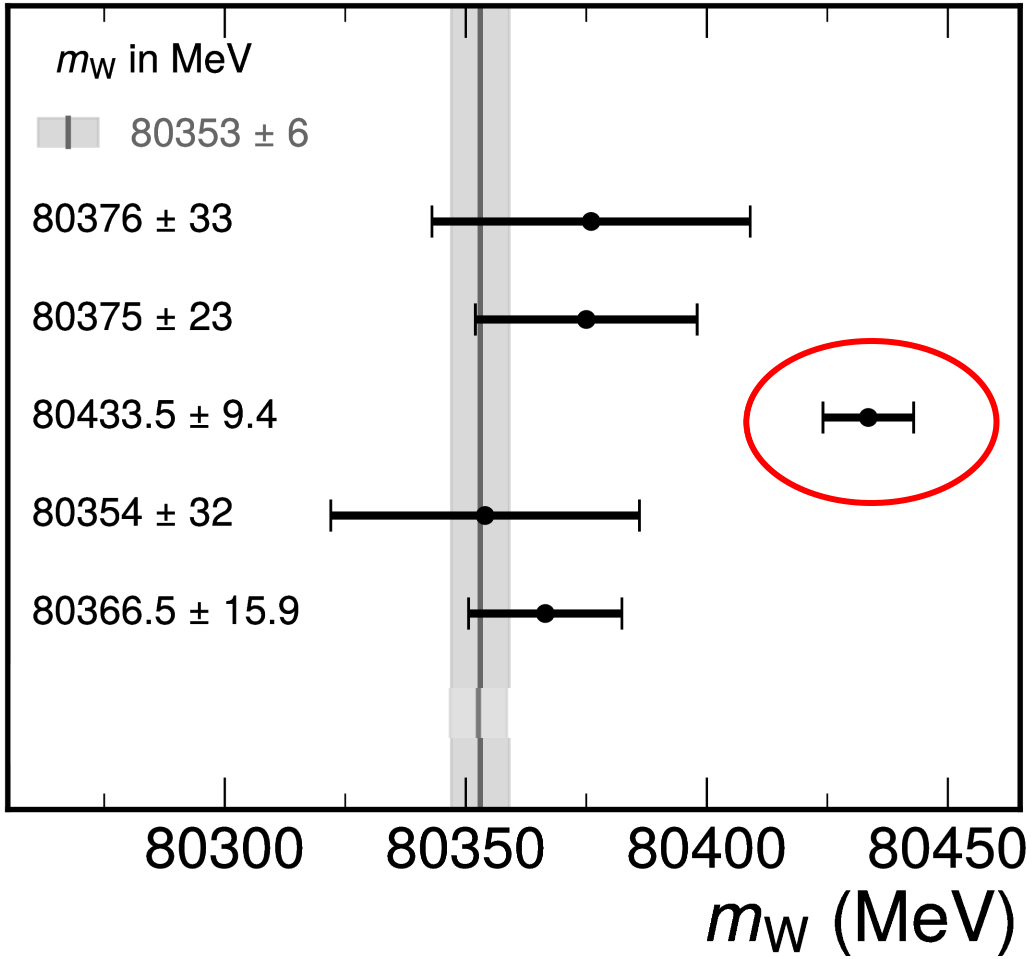
$T > \frac{1}{2}$ Higgs multiplets?

Extra $SU(2)$ doublets ?

Extra $U(1)'$?

The W mass puzzle before Sept. 17th

Electroweak fit
PRD 110 (2024) 030001
LEP combination
Phys. Rep. 532 (2013) 119
D0
PRL 108 (2012) 151804
CDF
Science 376 (2022) 6589
LHCb
JHEP 01 (2022) 036
ATLAS
arXiv:2403.15085



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  - **Inconsistent with SM** (7σ)
  - Poorly consistent with other measurements ($\sim 4\sigma$)

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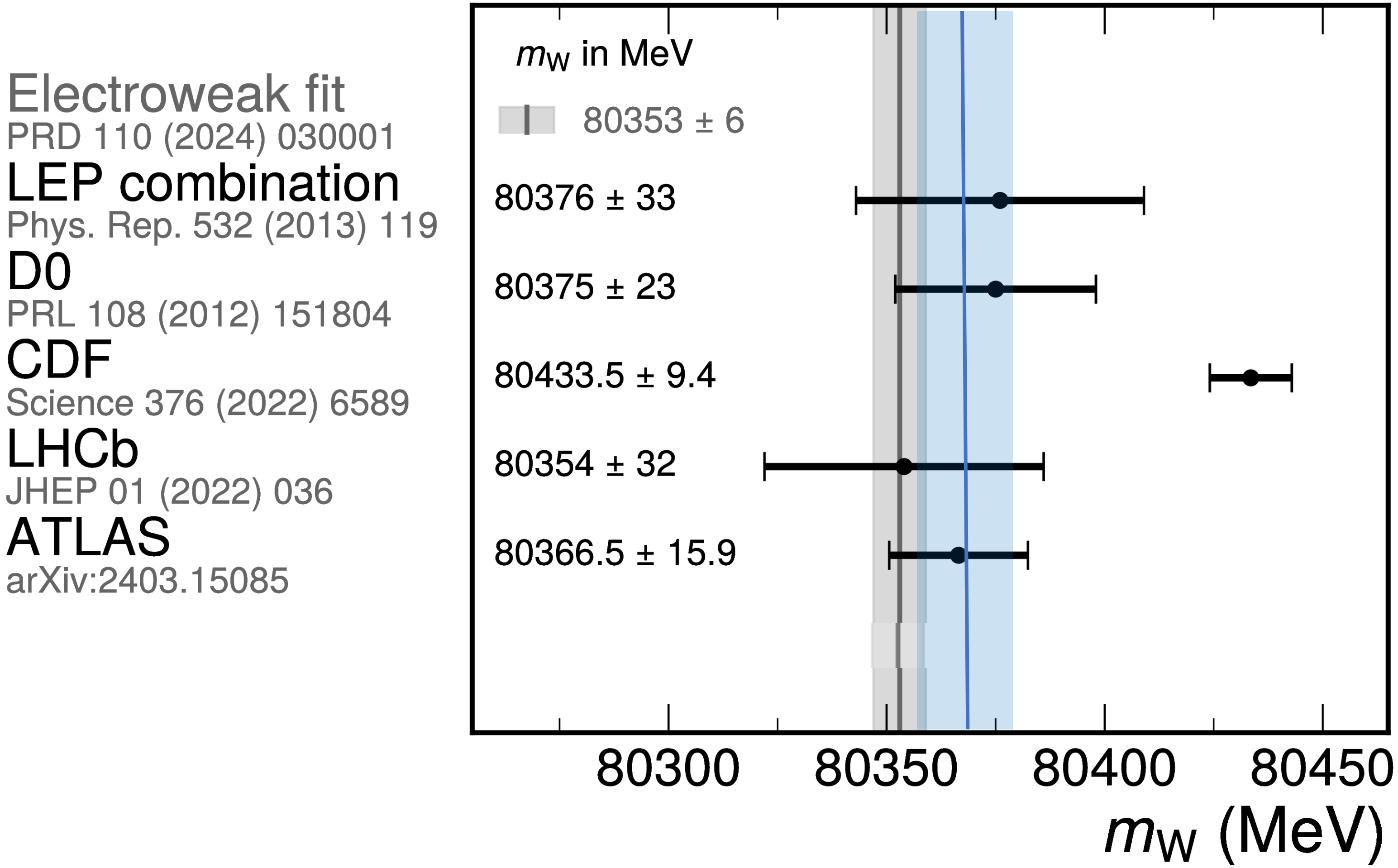

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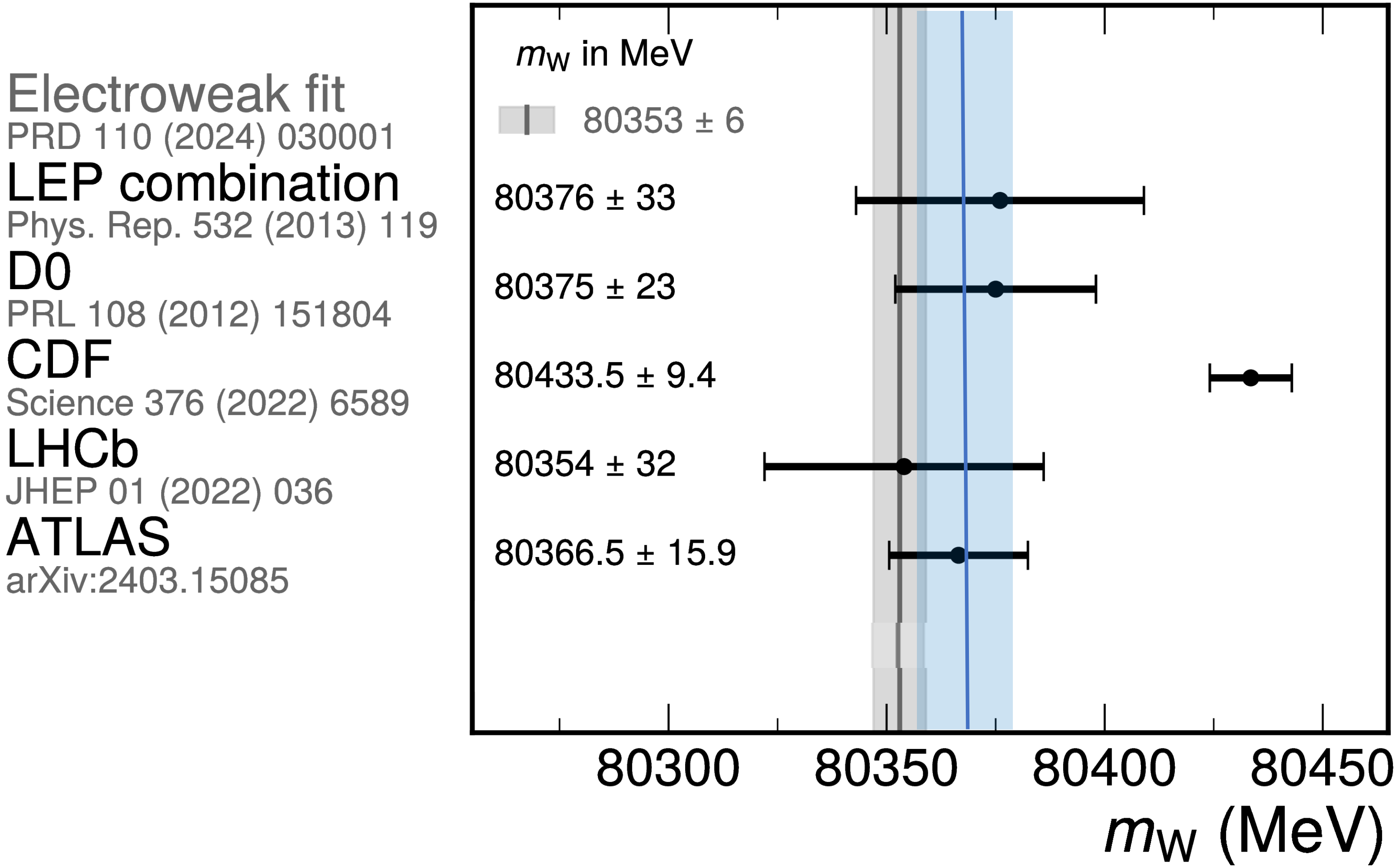

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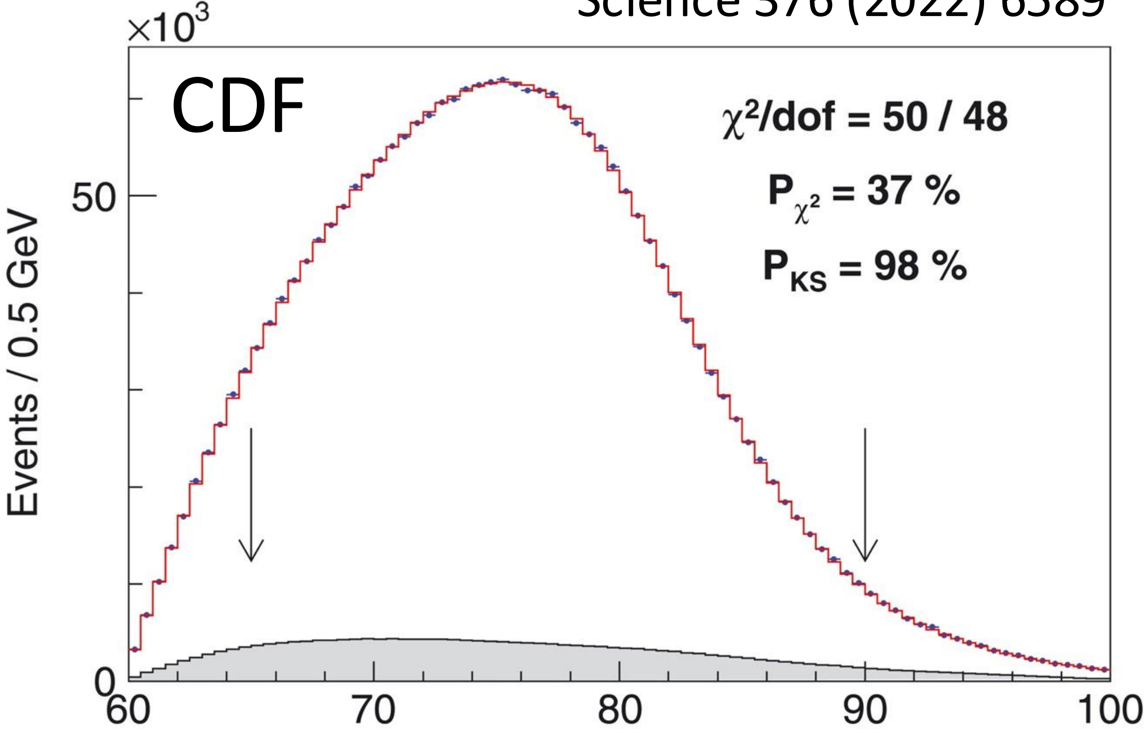
<u>CALL FOR A NEW MEASUREMENT</u>

Measuring m_W at hadron colliders

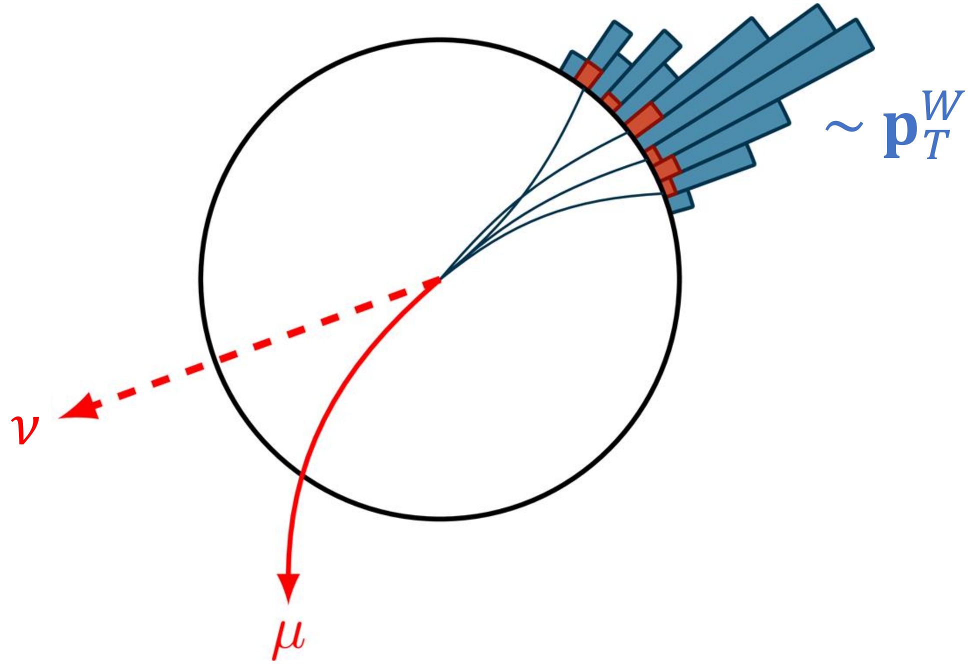
Science 376 (2022) 6589



$$m_T^{\ell\nu} = \sqrt{2(p_T^\ell|\mathbf{p}_T^\ell + \mathbf{p}_T^W| + p_T^{\ell\,2} + \mathbf{p}_T^\ell \cdot \mathbf{p}_T^W)}$$

$W \to q\bar{q}$ not feasible at the LHC

➔ focus on $W \to \ell\nu$ decay



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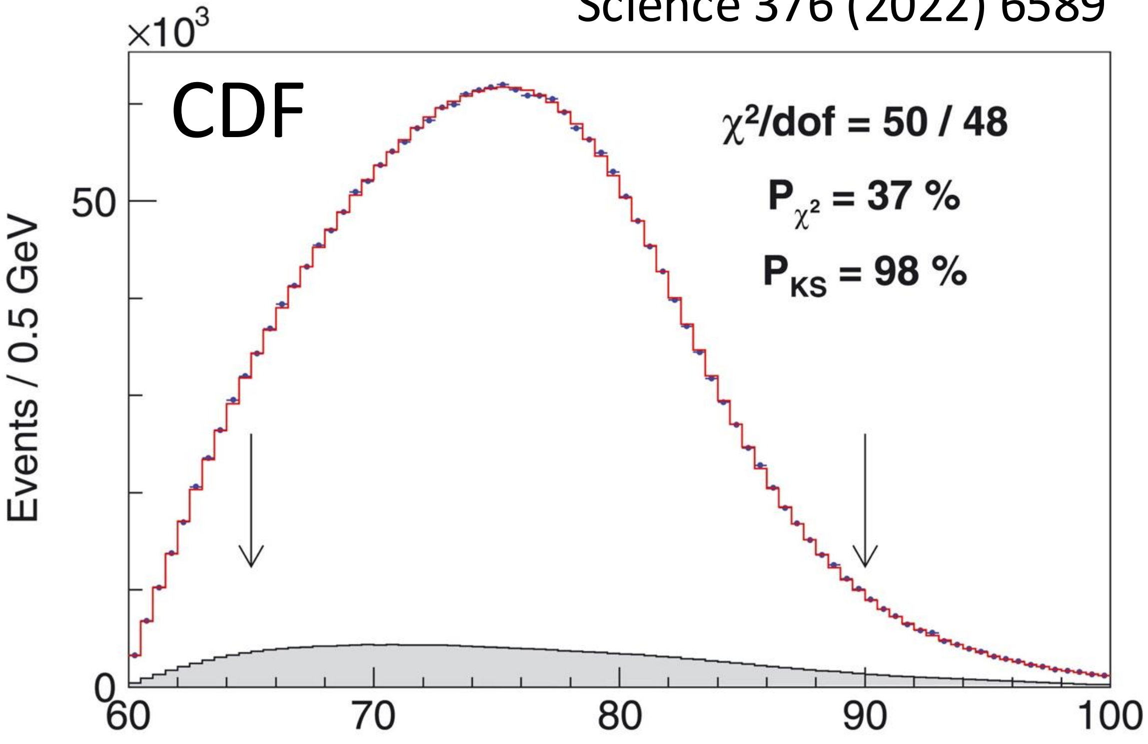

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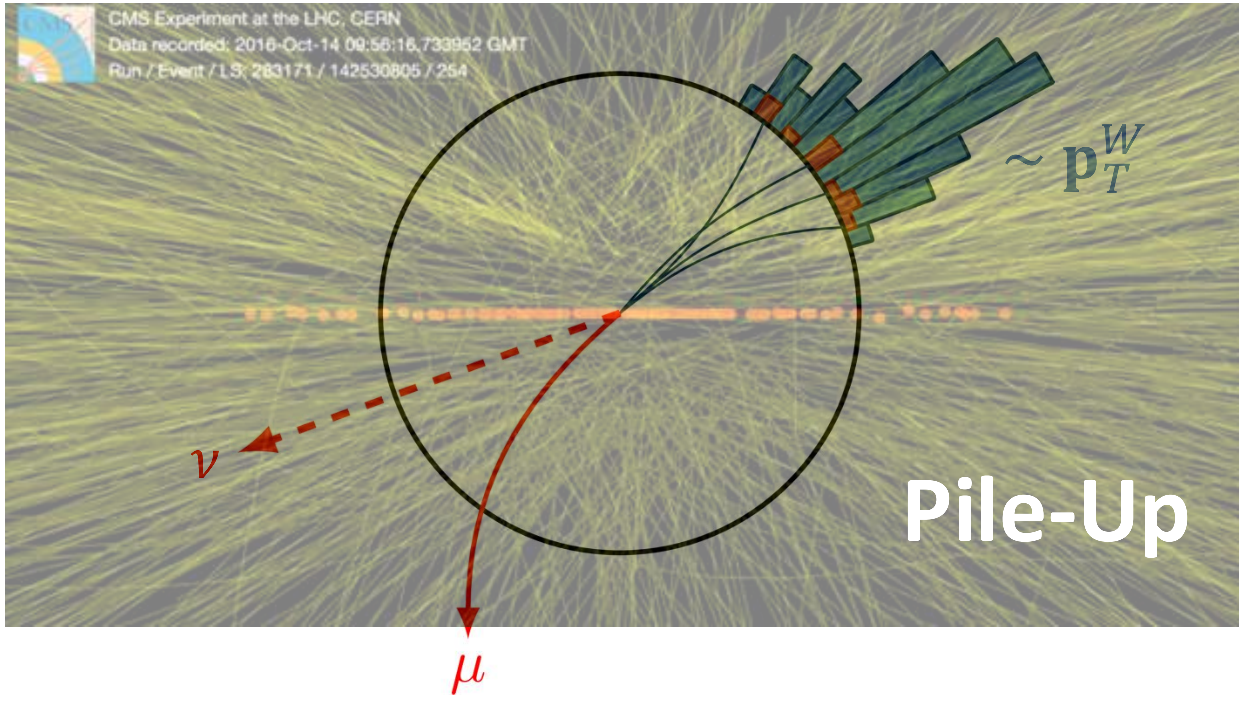

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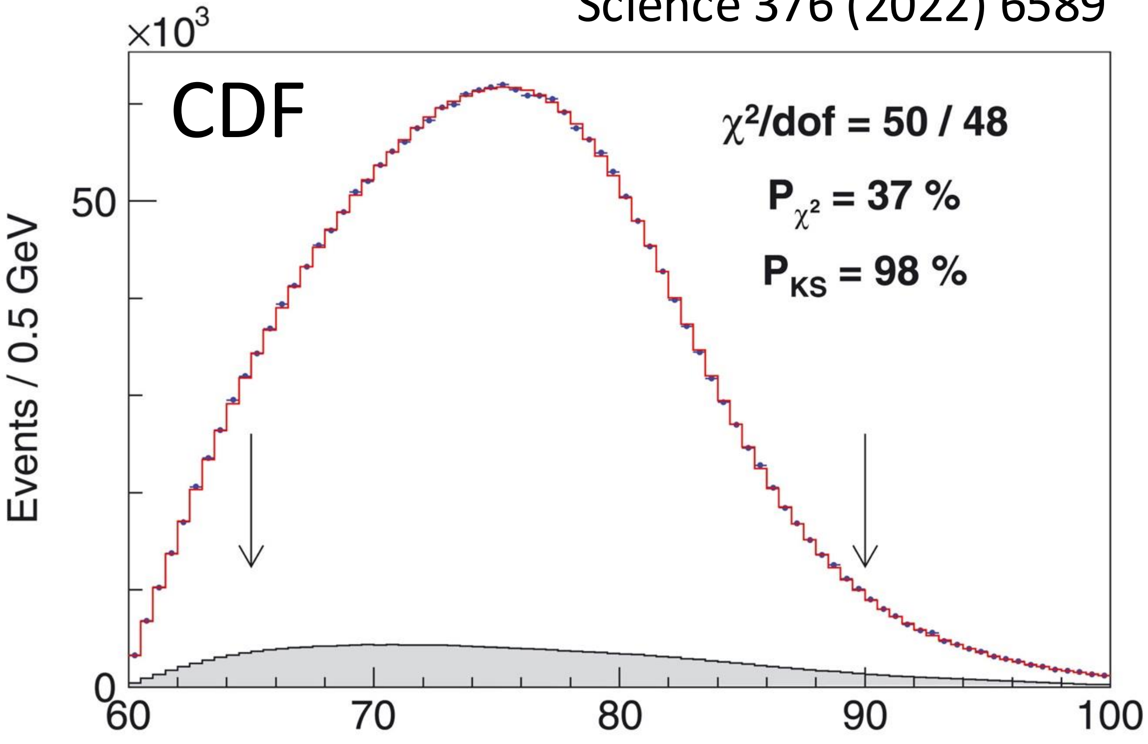
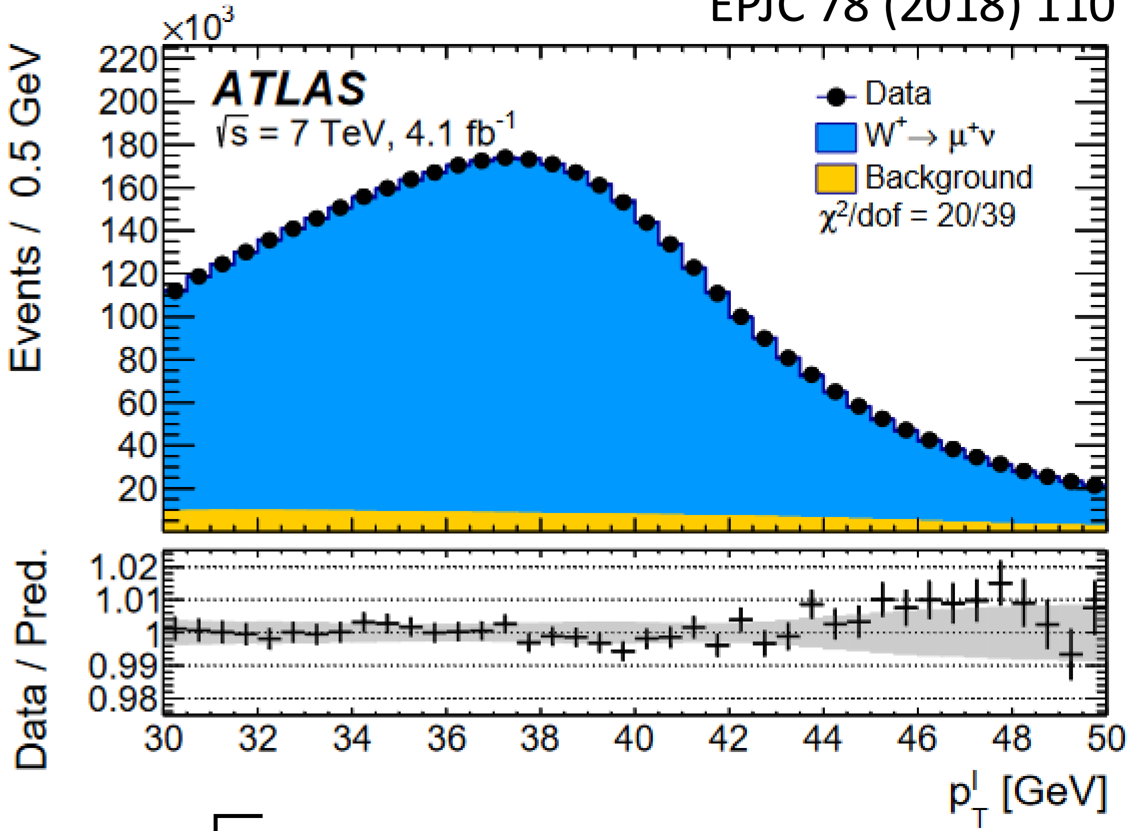


EPJC 78 (2018) 110



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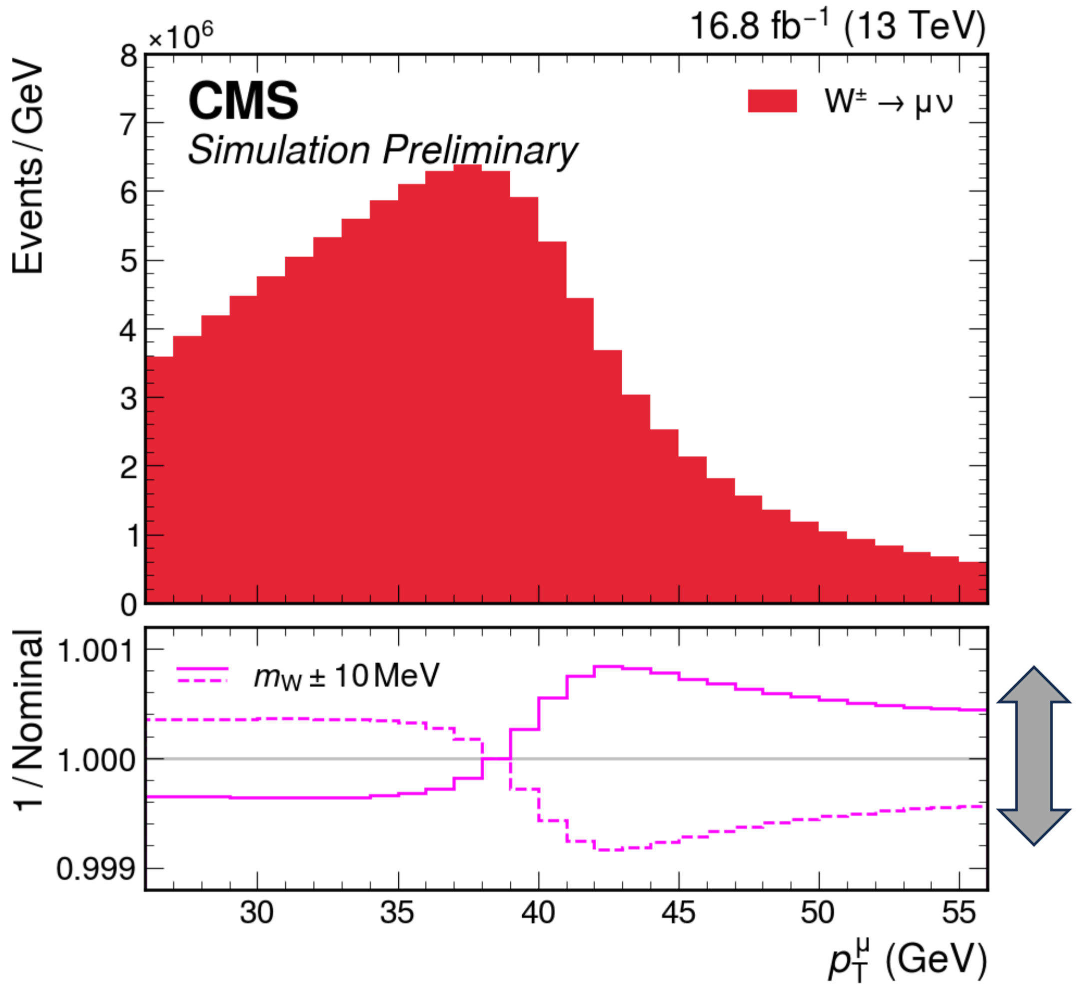
p_T^ℓ ➔

- PROS: cleaner observable
- CONS: sensitive to p_T^W **modeling**

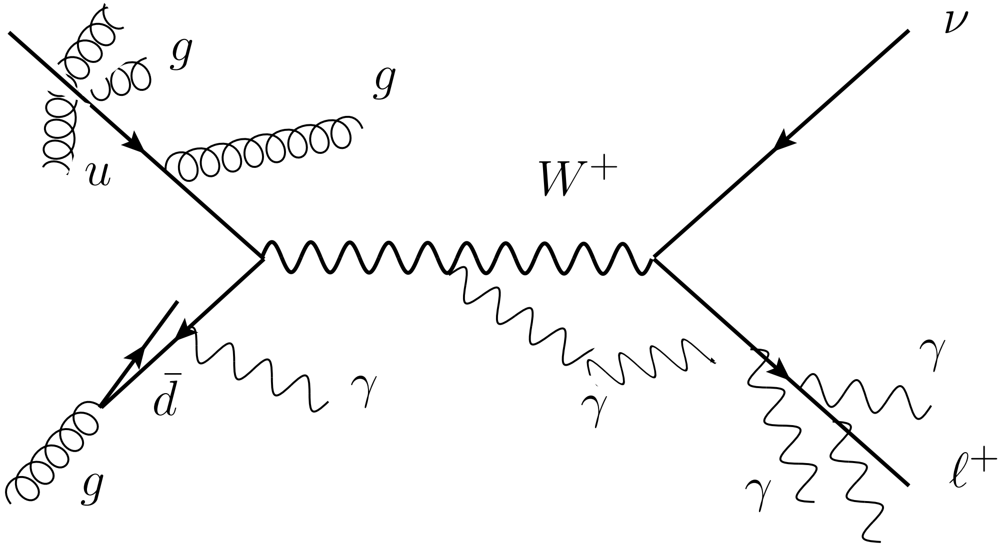
Measuring m_W at hadron colliders



$\Delta m_W = \pm 10$ MeV

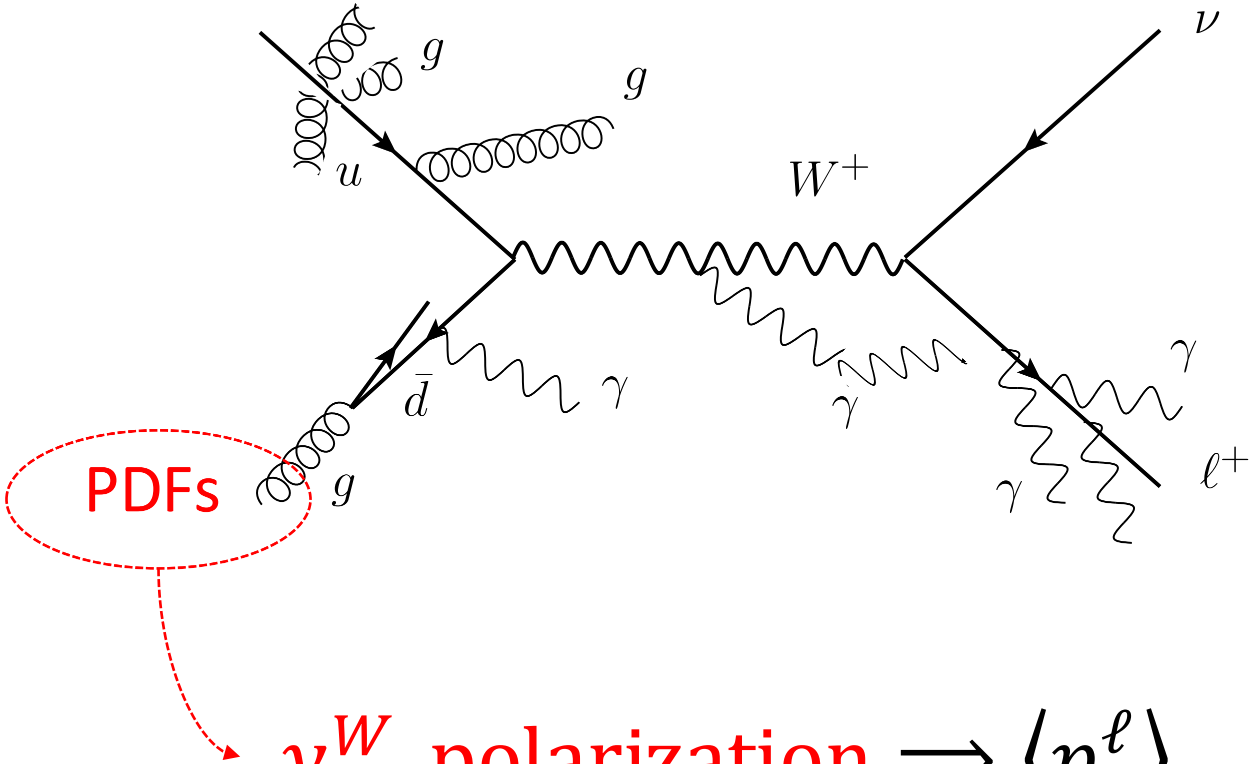
$\Longrightarrow$ **0.1% variation**

W modeling



see e.g. EPJC 77 (2017) 280

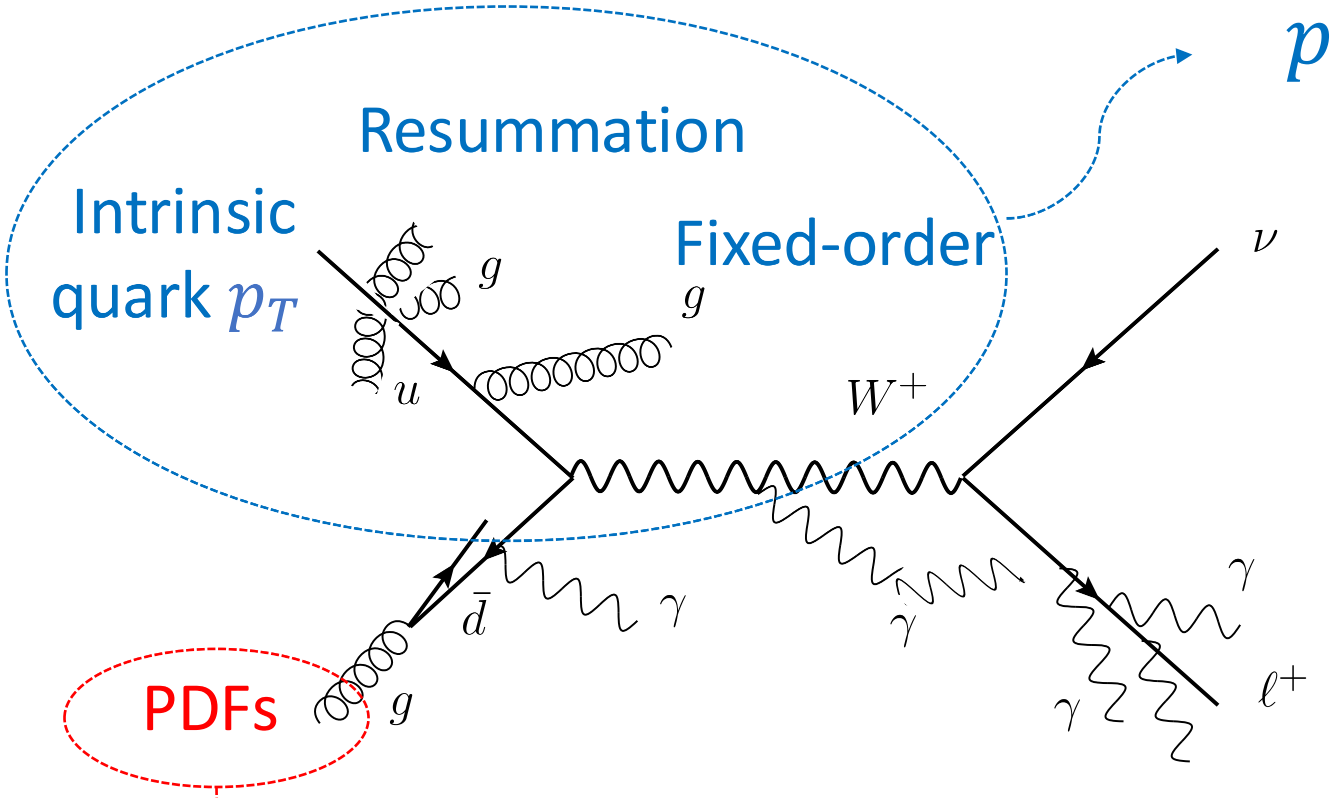
W modeling



y^W, polarization $\Longrightarrow \langle p_T^\ell \rangle$

see e.g. EPJC 77 (2017) 280

W modeling



$p_T^W \Longrightarrow p_T^\ell$

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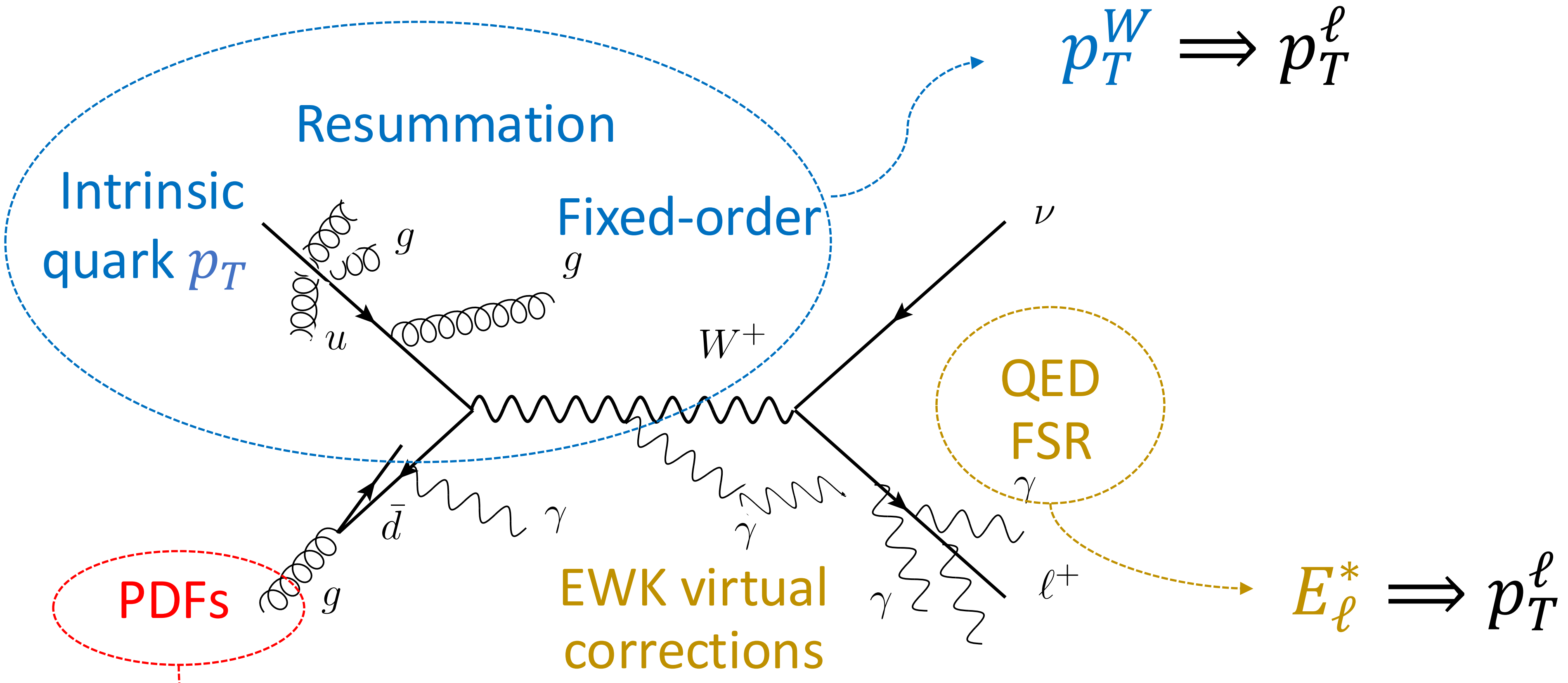

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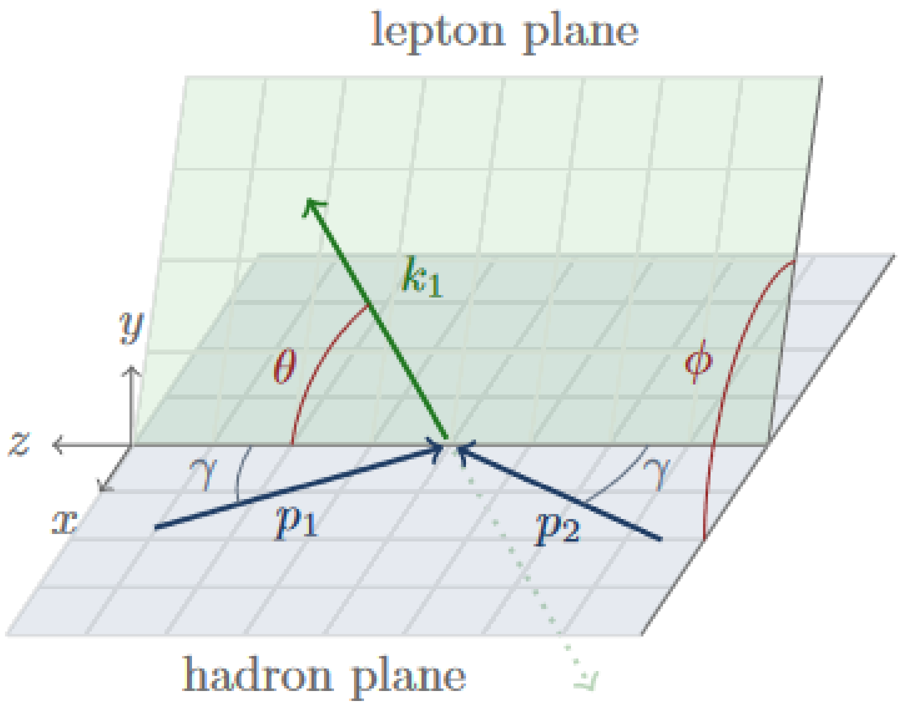
W modeling

See e.g.JHEP11 (2017) 003

$$\frac{d^6\sigma}{d\boldsymbol{\Phi}^{\ell^+}d\boldsymbol{\Phi}^{\ell^-}} \propto$$

$$\frac{d^4\sigma_{\mathrm{UL}}}{d\boldsymbol{\Phi}^V} \times \left(\sum_{i=-1}^{7} A_i(\boldsymbol{\Phi}^V) \times P_i(\theta^*, \varphi^*) \right)$$



$A_{0,\ldots,7}(p_T^W, y^W)$ → **angular coefficients**

Parton Density Functions

- Dominant systematics in the past

Eur. Phys. J. C (2010) 69: 379–397
DOI 10.1140/epjc/s10052-010-1417-0

Regular Article - Experimental Physics

$\Delta M_W \leq 10$ MeV/c^2 at the LHC: a forlorn hope?*

M.W. Krasny[1,a], F. Dydak[2], F. Fayette[1], W. Płaczek[3], A. Siódmok[1,3]

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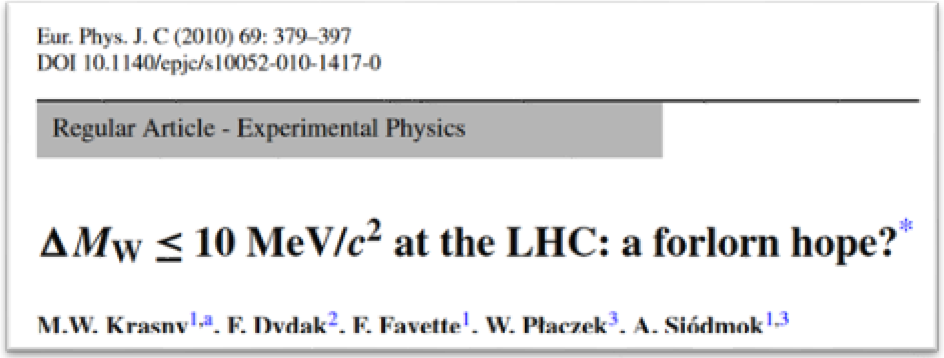

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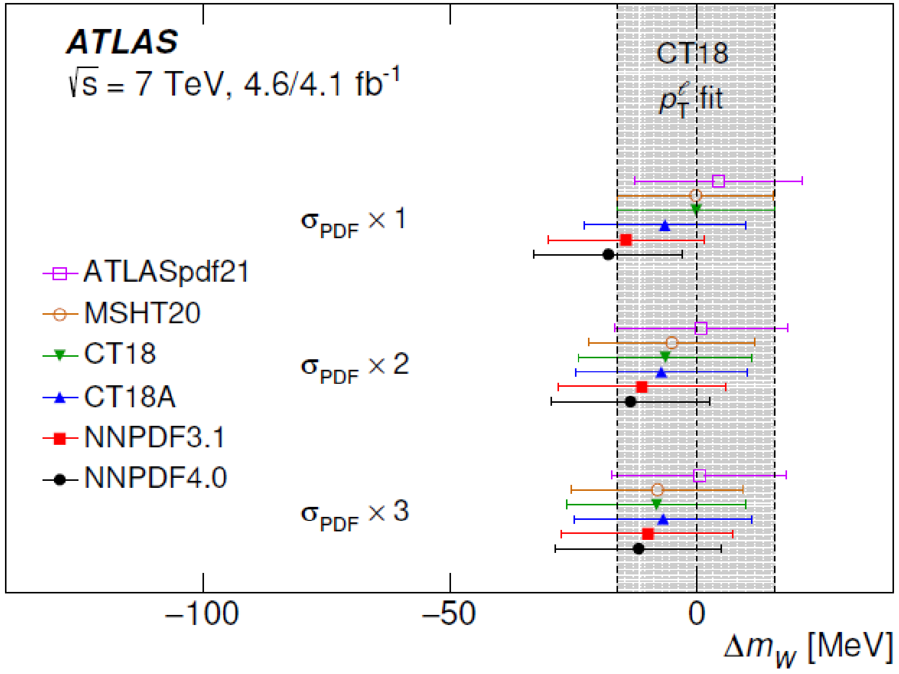

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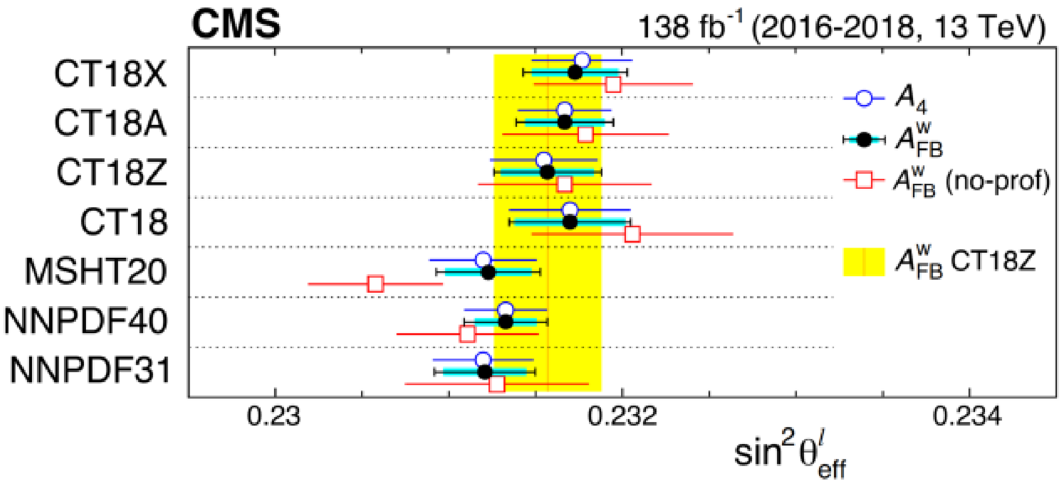

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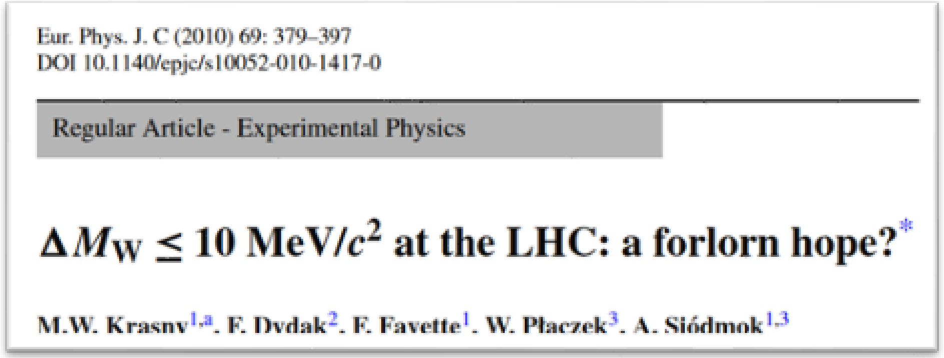
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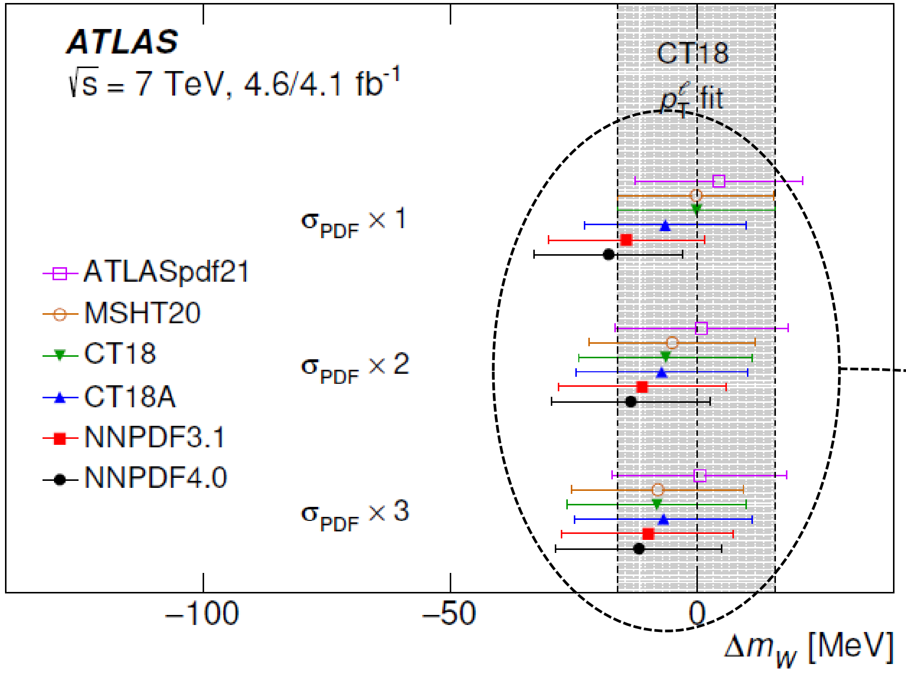

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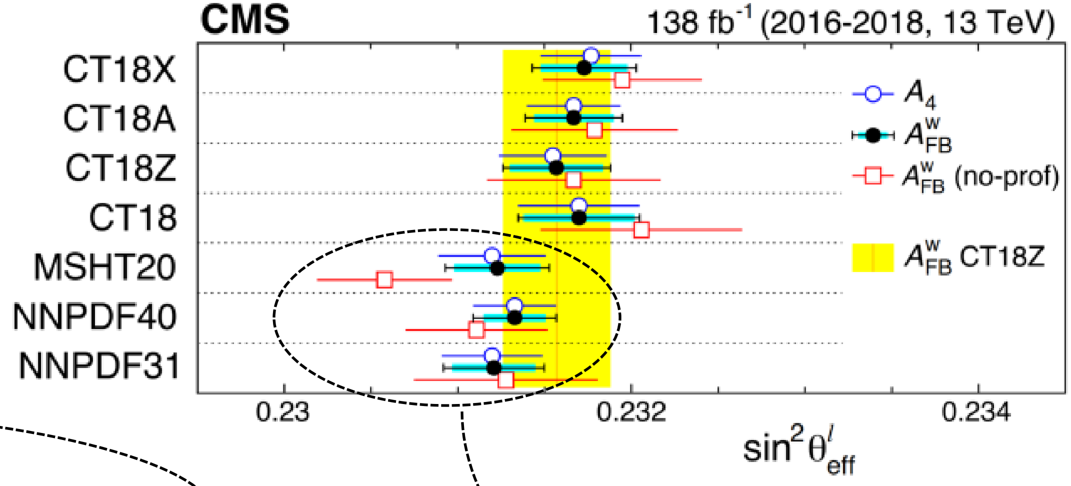

Scatter reduced by *in situ* profiling

p_T^W modeling

- Conventional wisdom:

$$\left(\frac{1}{\sigma_W}\frac{d\sigma}{dp_T^W}\right)_{\text{predicted}} = \frac{\left(\frac{1}{\sigma_W}\frac{d\sigma}{dp_T^W}\right)_{\text{MODEL}}}{\left(\frac{1}{\sigma_Z}\frac{d\sigma}{dp_T^Z}\right)_{\text{MODEL}}} \times \left(\frac{1}{\sigma_Z}\frac{d\sigma}{dp_T^Z}\right)_{\text{measured}}$$

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- <u>Rationale</u>: **RATIO** better known than **spectrum**
  - But: cancellation of μ_R/μ_F relies on **correlation scheme**

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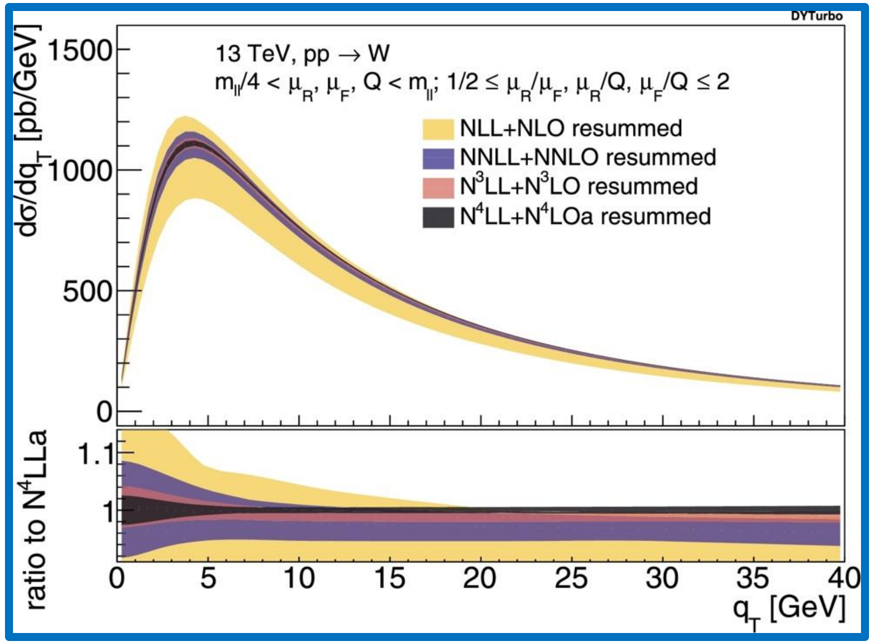
PLB 845 (2023) 138125



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- Ideal case: a single **MODEL** prediction with **properly defined uncertainties**

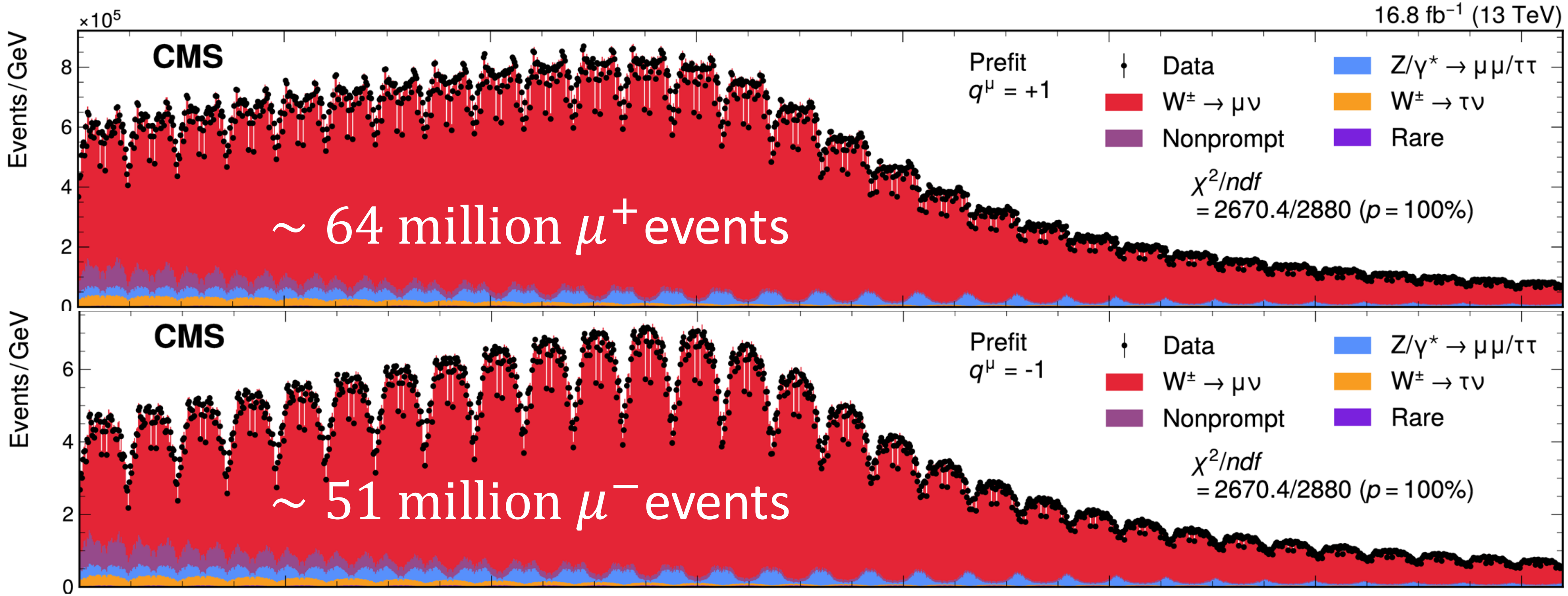
The CMS paradigm

arXiv:2412.13872

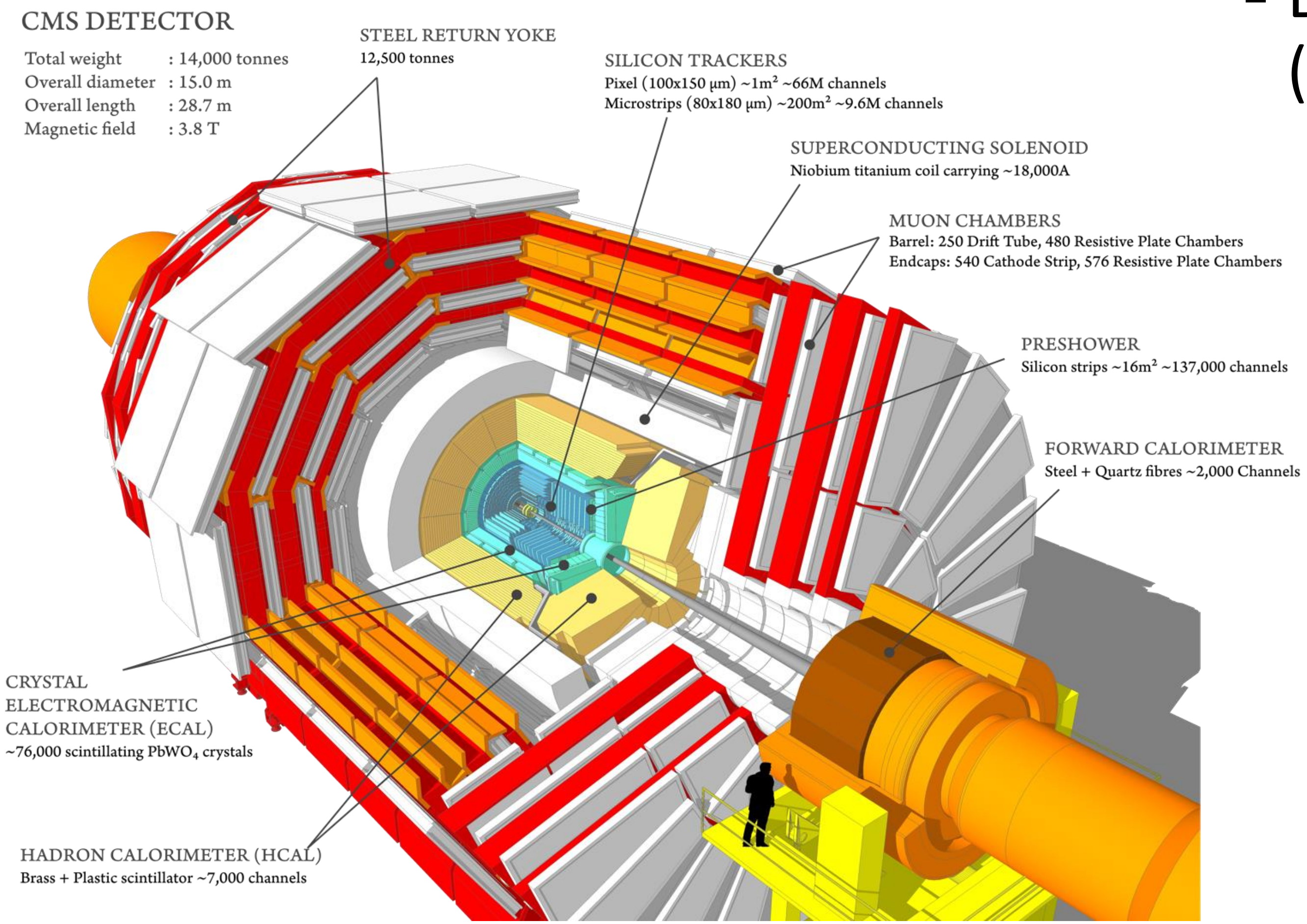
Z for validation only	State-of-the-art theo. calculations	*In situ* constraint

Large samples, high-granularity

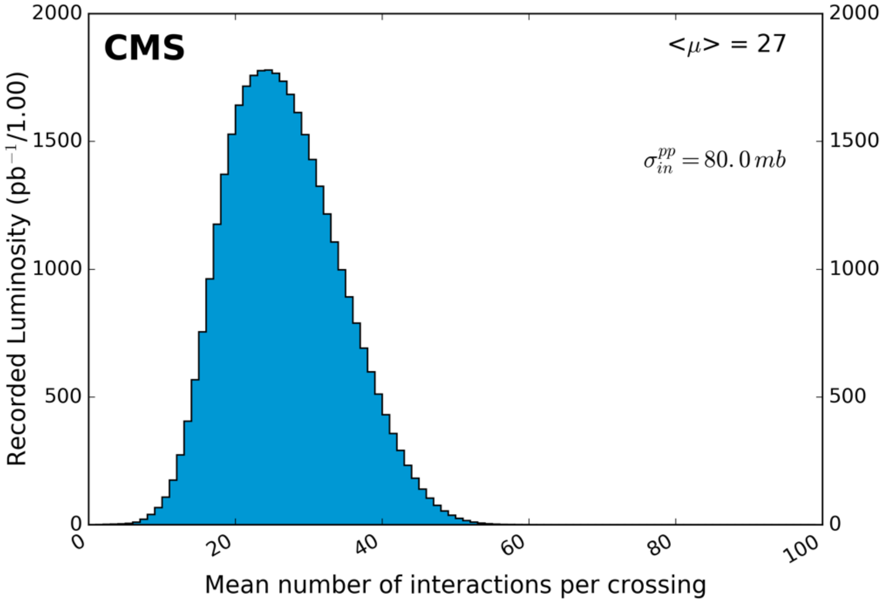
- Large samples → high pile-up → analyze **muon momentum only**
- Granularity → **finely grained 3D-space** $(p_T^\mu \times \eta^\mu \times q^\mu)$ → **2880 bins**
  - $p_T^\mu \in [26,56]$ GeV, $|\eta^\mu| < 2.4$, $q^\mu = \pm 1$



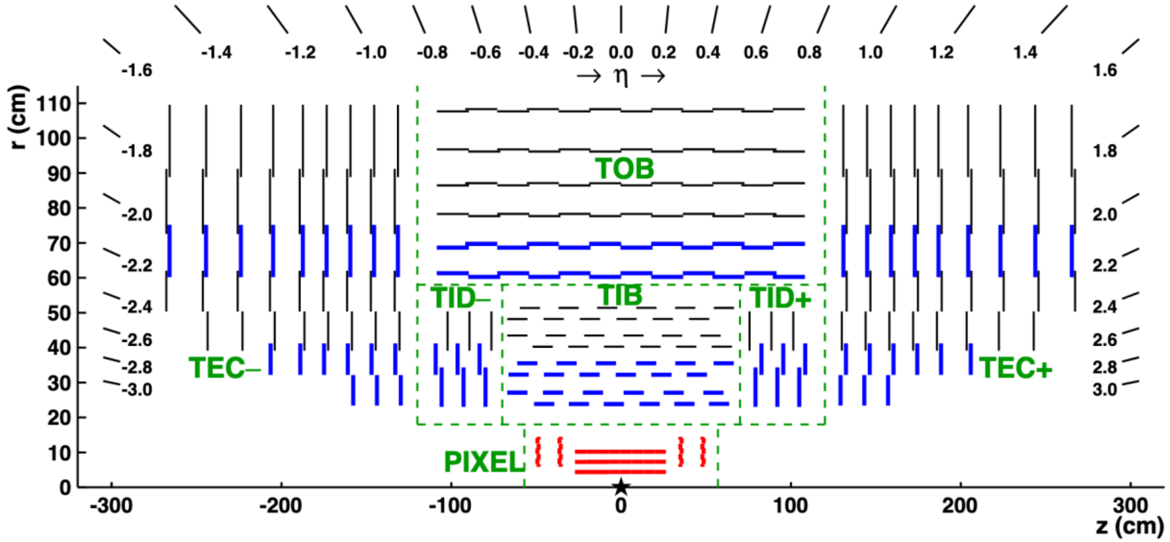
The CMS detector



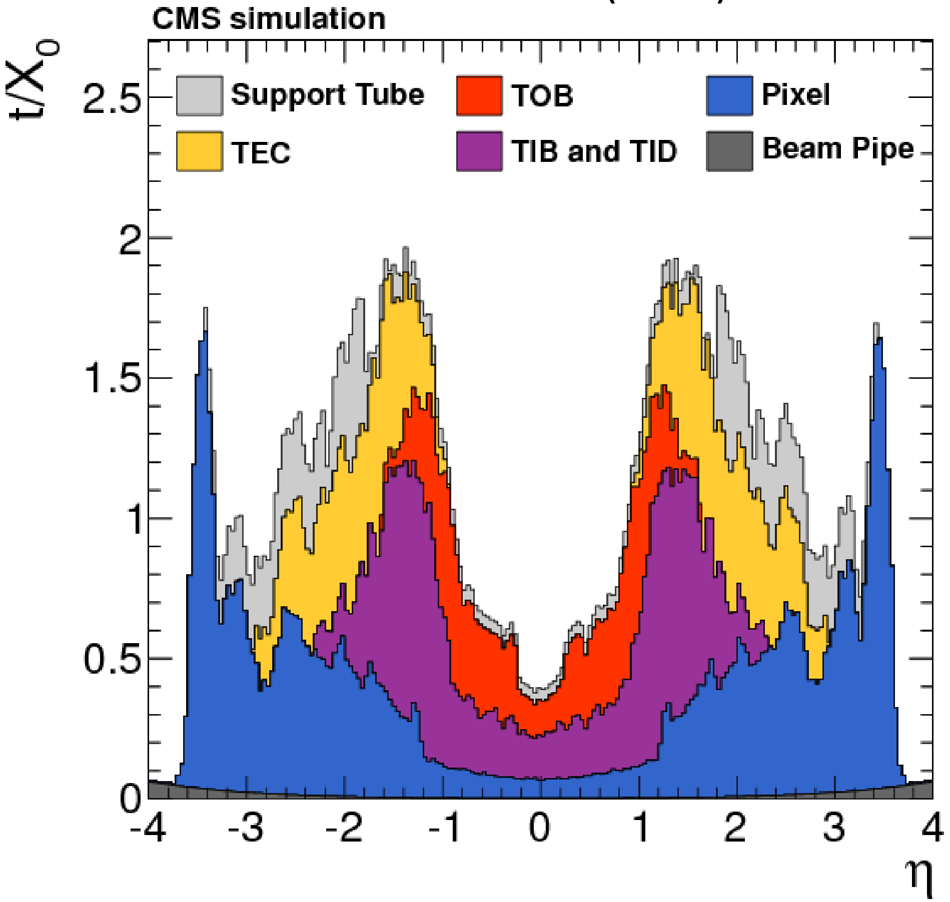
- Data from a **subset** $(\sim 10\%)$ **of Run2** $(L = 16.8\ \mathrm{fb}^{-1})$
  - Average pile-up: $\langle \mu \rangle = 25$



The CMS tracker



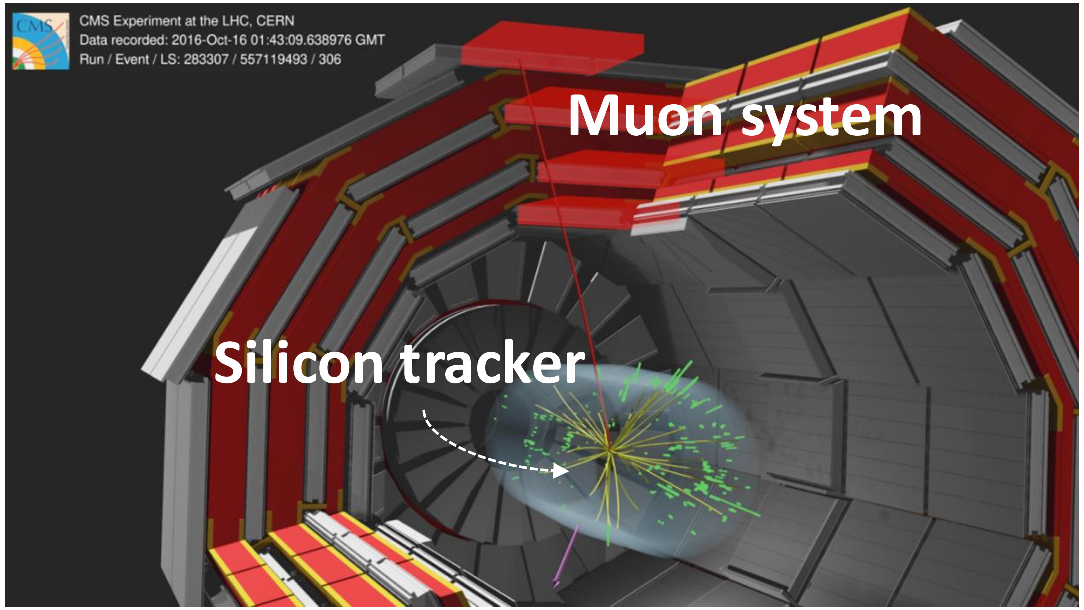
JINST 9 (2014) P10009



- Fully **silicon-based**
  - Up to 17 points per track ($9 \div 50\ \mu m$ resolutions)
- Up to **2 radiation lengths**
  - with some implications on resolution/energy loss

Muons in CMS

- Two-stage reconstruction
  - **Muon system** → trigger and ID
  - **Silicon Tracker** → 3-momentum at the IP



Muons in CMS

- Two-stage reconstruction
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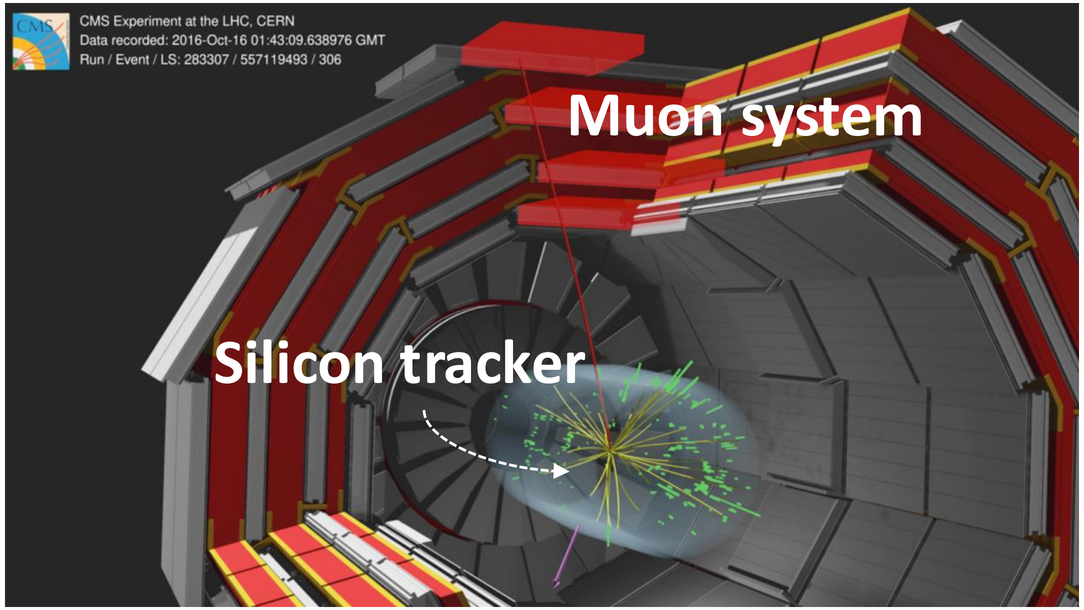
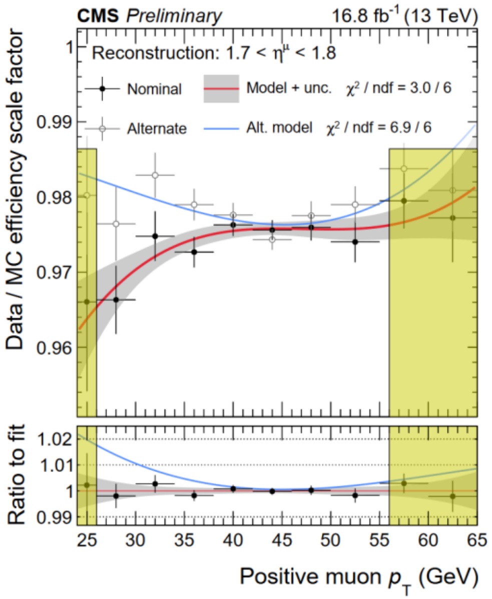
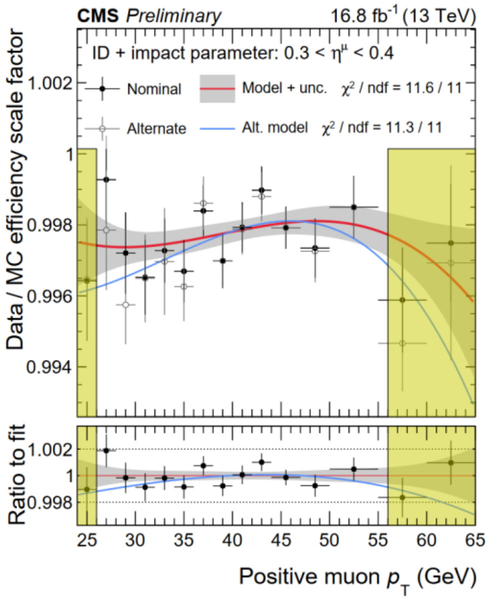
- Efficiencies calibrated on $\boldsymbol{Z \to \mu\mu}$
  - Uncertainties propagated through $O(3{,}000)$ nuisance parameters

Impact on m_W → ~3 MeV



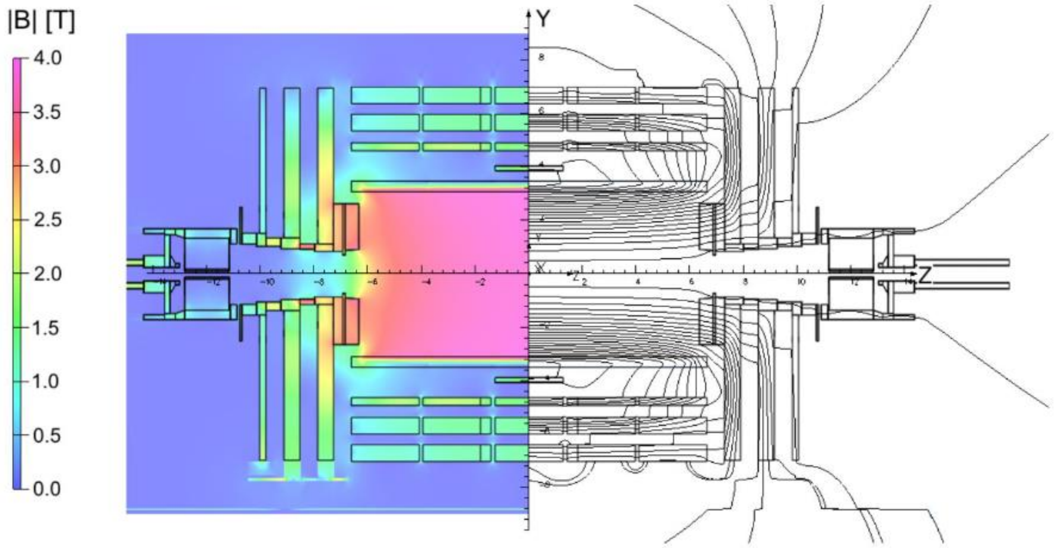




Magnetic field

JINST 5:T03021,2010
Symmetry 14 (2022) 169

- *B*-field in tracker volume was **measured**
    1. at the **surface**,
    2. with **empty coil**,
    3. with Hall probes calibrated to $\mathbf{3 \times 10^{-4}}$,
    4. $\frac{\Delta \boldsymbol{B}}{\boldsymbol{B}} = \mathbf{-8 \times 10^{-4}}$ between map and *in situ* NMR survey



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JINST 5:T03021,2010
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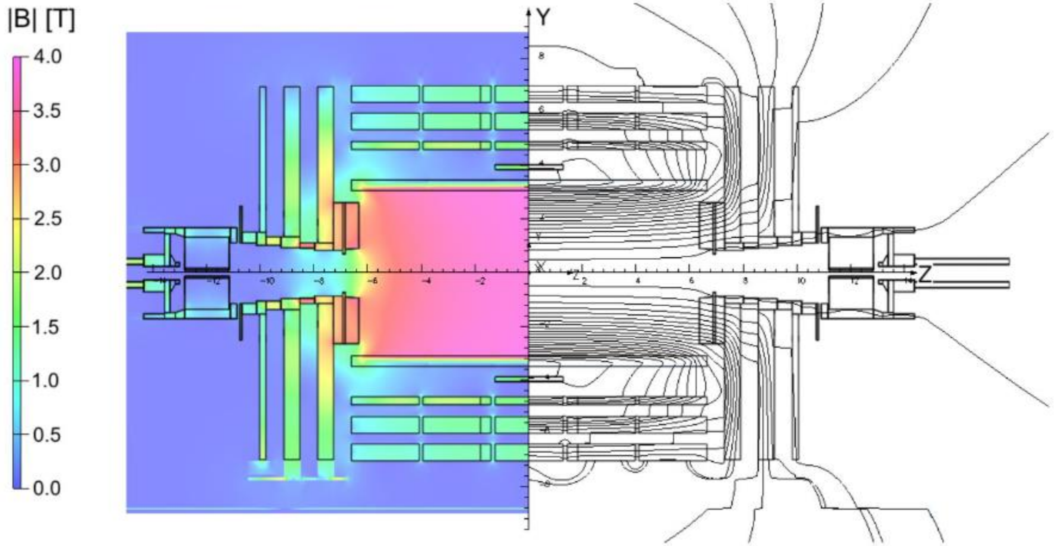


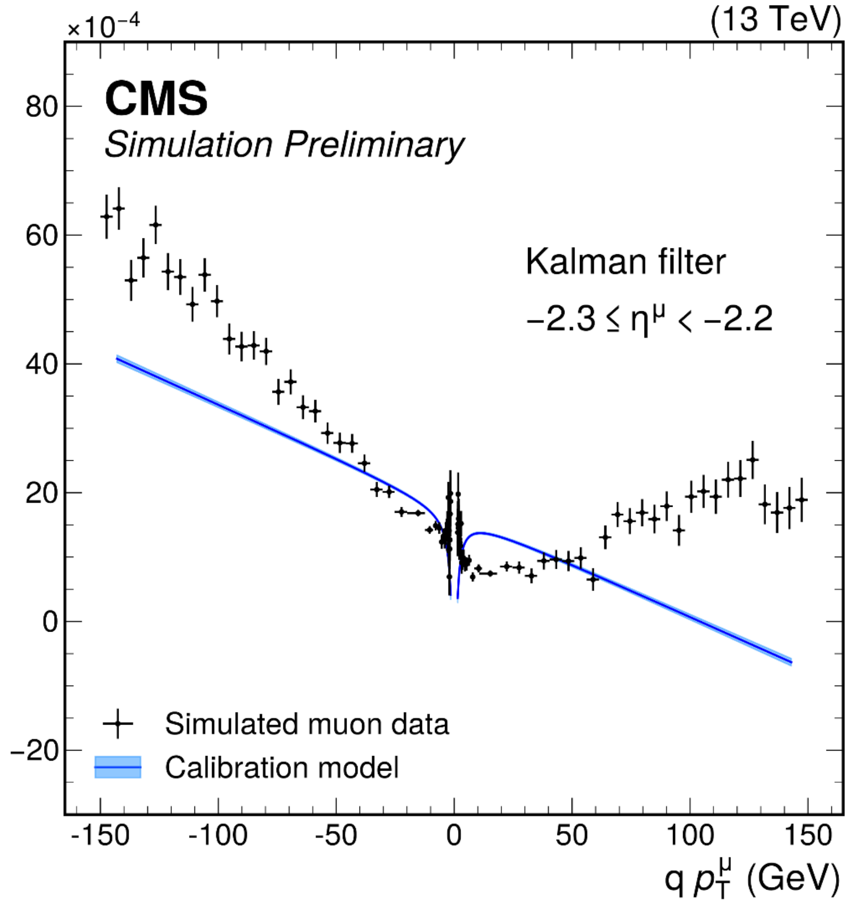
A priori knowledge of *B*-field: $\sim\mathbf{10^{-3}}$
(in excess of our **target** $\mathbf{10^{-4}}$)

NEED FOR *IN SITU* SCALE CALIBRATION

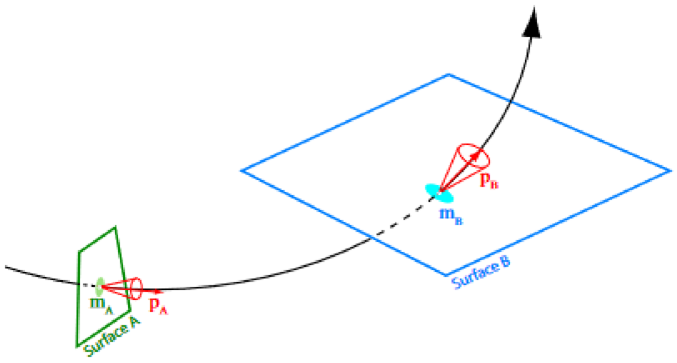
Muon momentum scale

- <u>Observation</u>: **up to 1% bias in scale** in **ideal simulation** (not expected/understood)

$$\left\langle \frac{p_T^{\text{reco}}}{p_T^{\text{gen}}} \right\rangle - 1$$

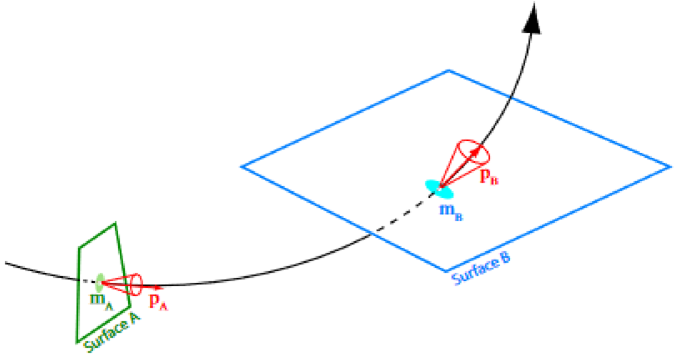


Muon momentum scale



1. **Fixes to default CMS reconstruction**
   - ✓ **Tuning** of parameters in GEANT4 simulation
   - ✓ **Track re-fit** with improved treatment of *B*-field and material

Muon momentum scale



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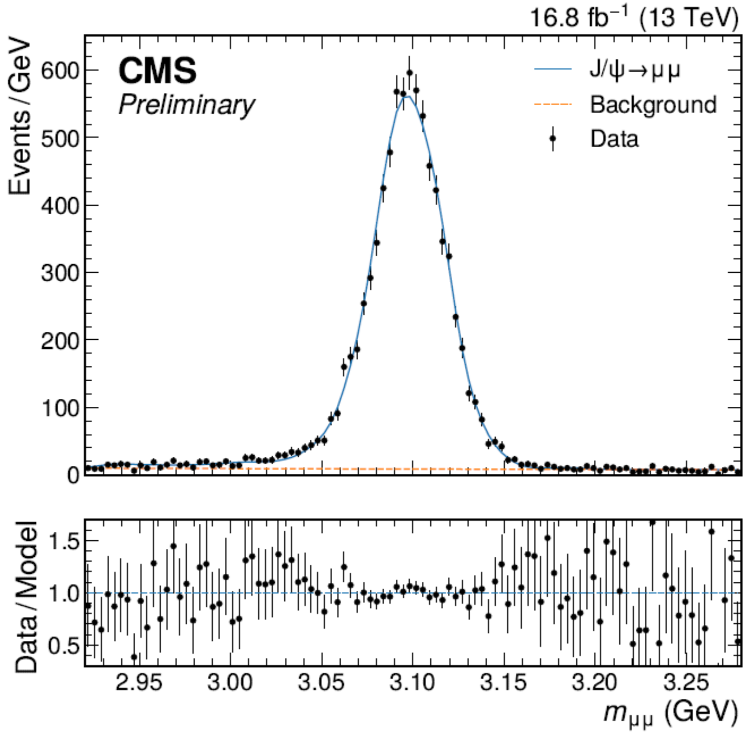


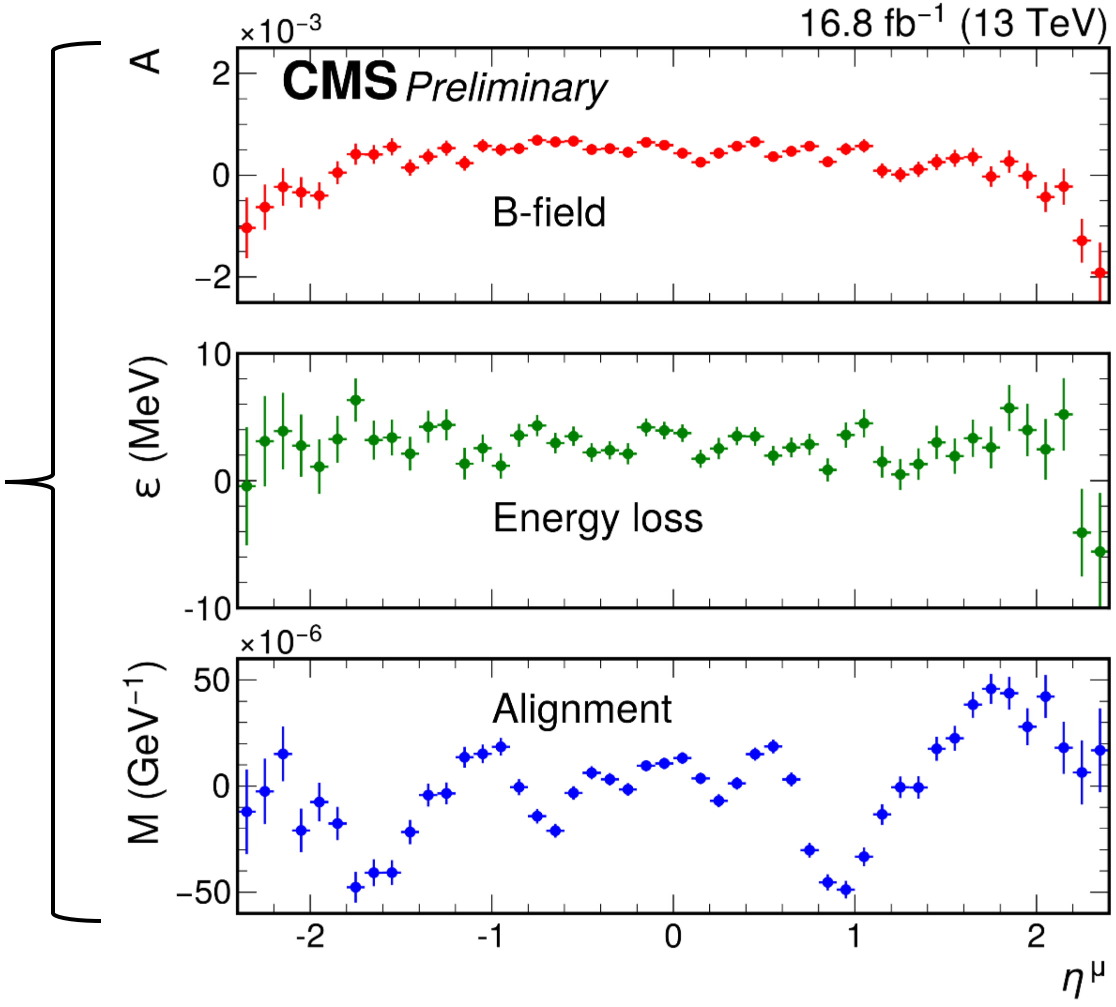
2. **Calibration on $\mathrm{J}/\Psi \to \mu\mu$** $\left(\frac{\Delta m_{\mathrm{J}/\Psi}}{m_{\mathrm{J}/\Psi}} \sim 10^{-6}\right)$
   - ✓ **Global alignment** of tracker (+ *B*-field + material)
   - ✓ Fit residual scale bias with **parametric model**:

$$\left(\frac{p_T^{\mathrm{corr}}}{p_T}\right)_{\pm} = 1 + A_{i\eta} - \frac{\varepsilon_{i\eta}}{p_T} \pm M_{i\eta} p_T$$

Parametrized scale corrections

***B*-field** and **material** corrections consistent with their *a priori* knowledge

$$\left(\frac{p_T^{\text{corr}}}{p_T}\right)_{\pm} = 1 + A_{i\eta} - \frac{\varepsilon_{i\eta}}{p_T} \pm M_{i\eta} p_T$$



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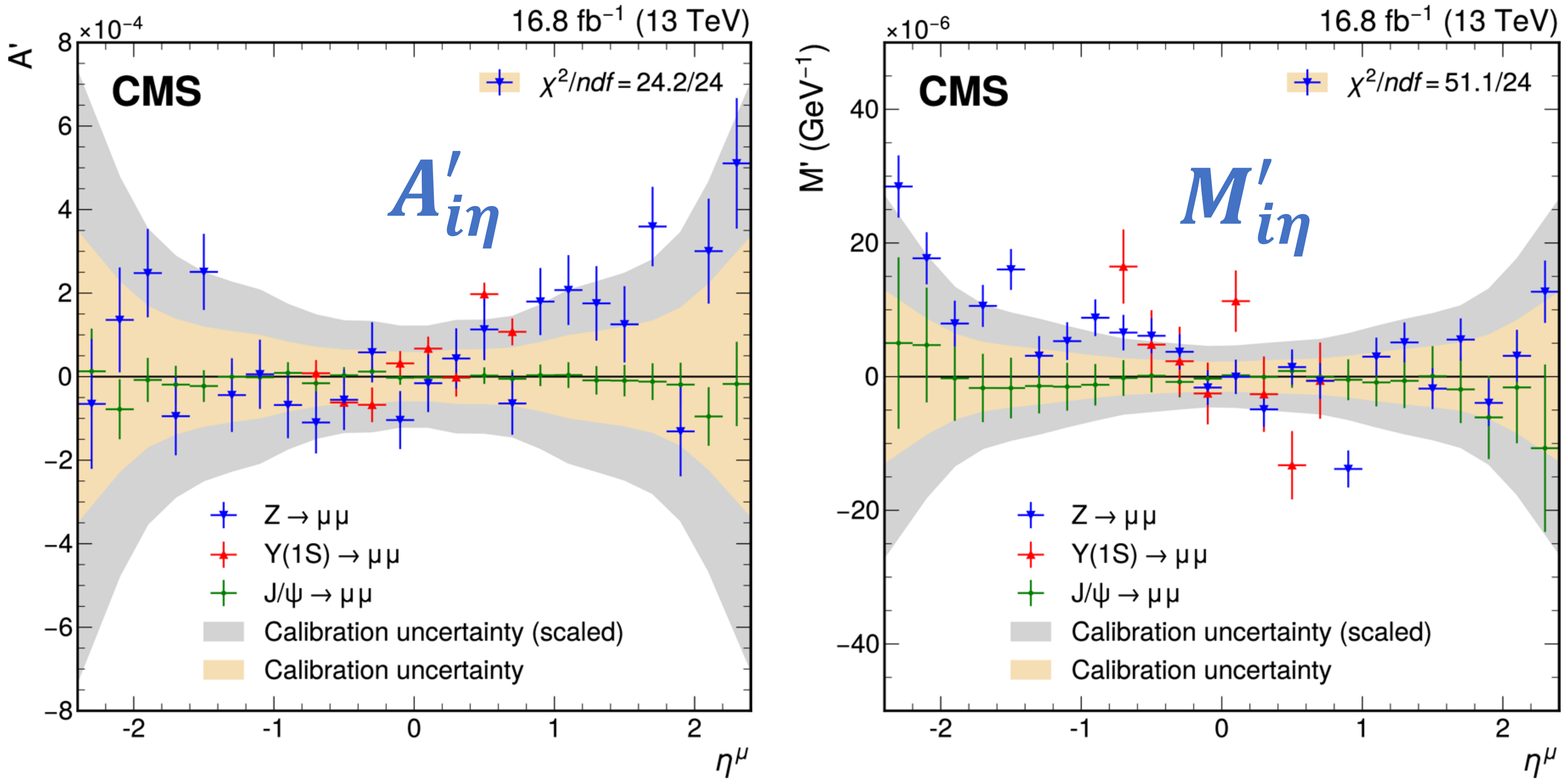

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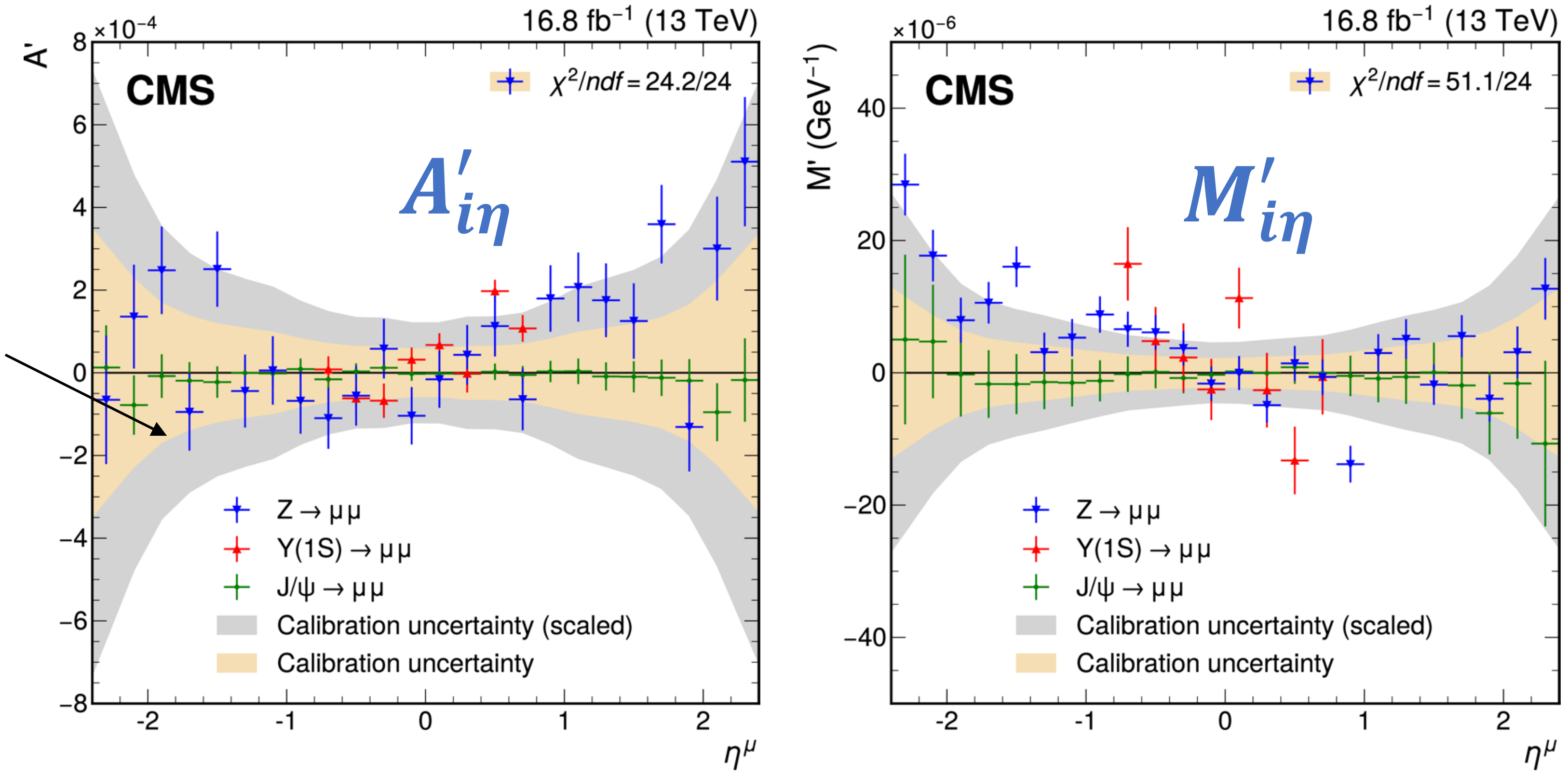
σ_{stat}



Should be ~ 0 within σ_{stat} for *ideal* calibration

Validation: Z-closure

- **J/Ψ-based calibrations** are applied to muons from $\boldsymbol{Z \to \mu\mu}$ decays
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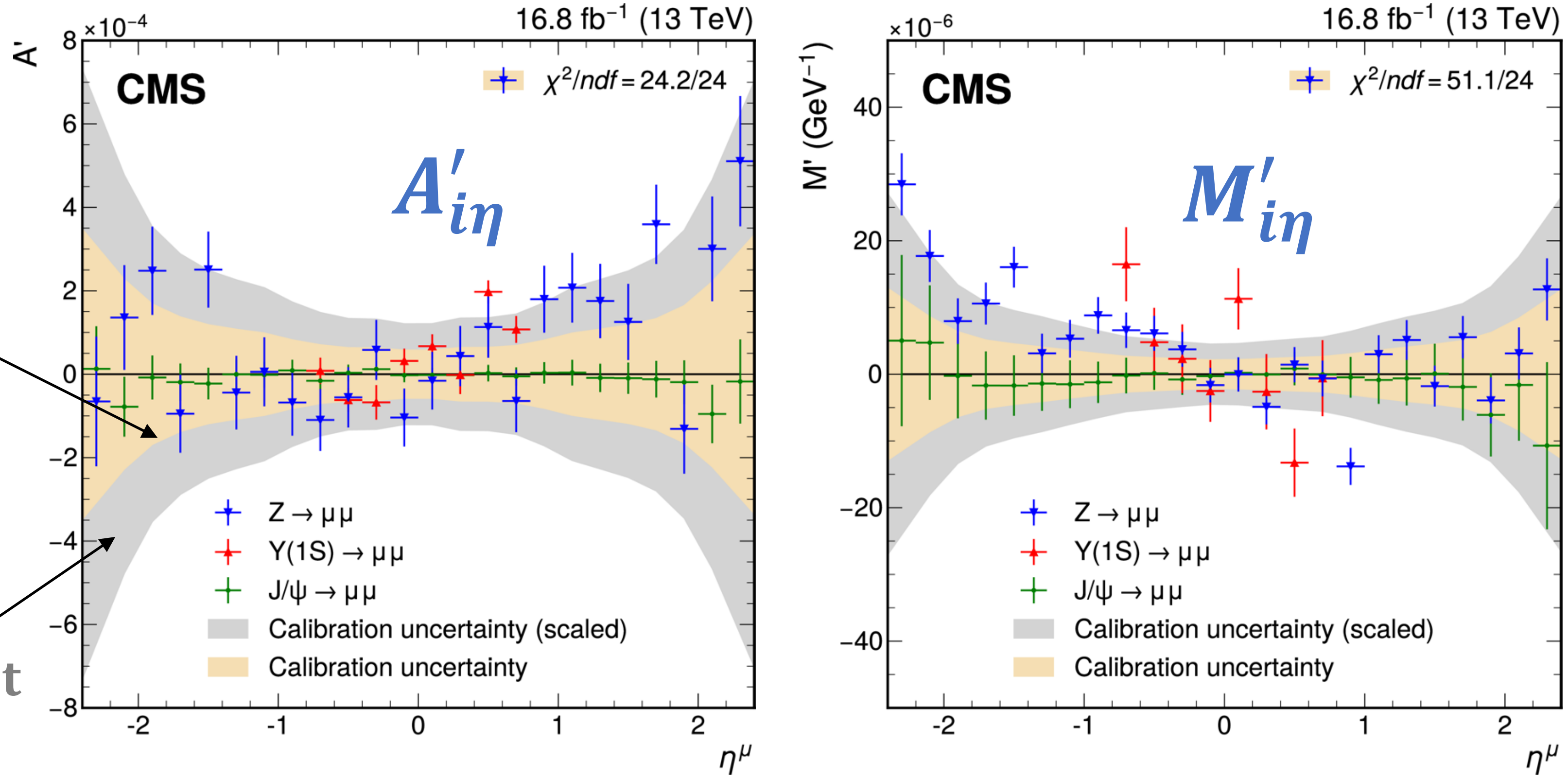
σ_{stat}

$2.1 \times \sigma_{\mathrm{stat}}$



Should be ~ 0 within σ_{stat} for *ideal* calibration

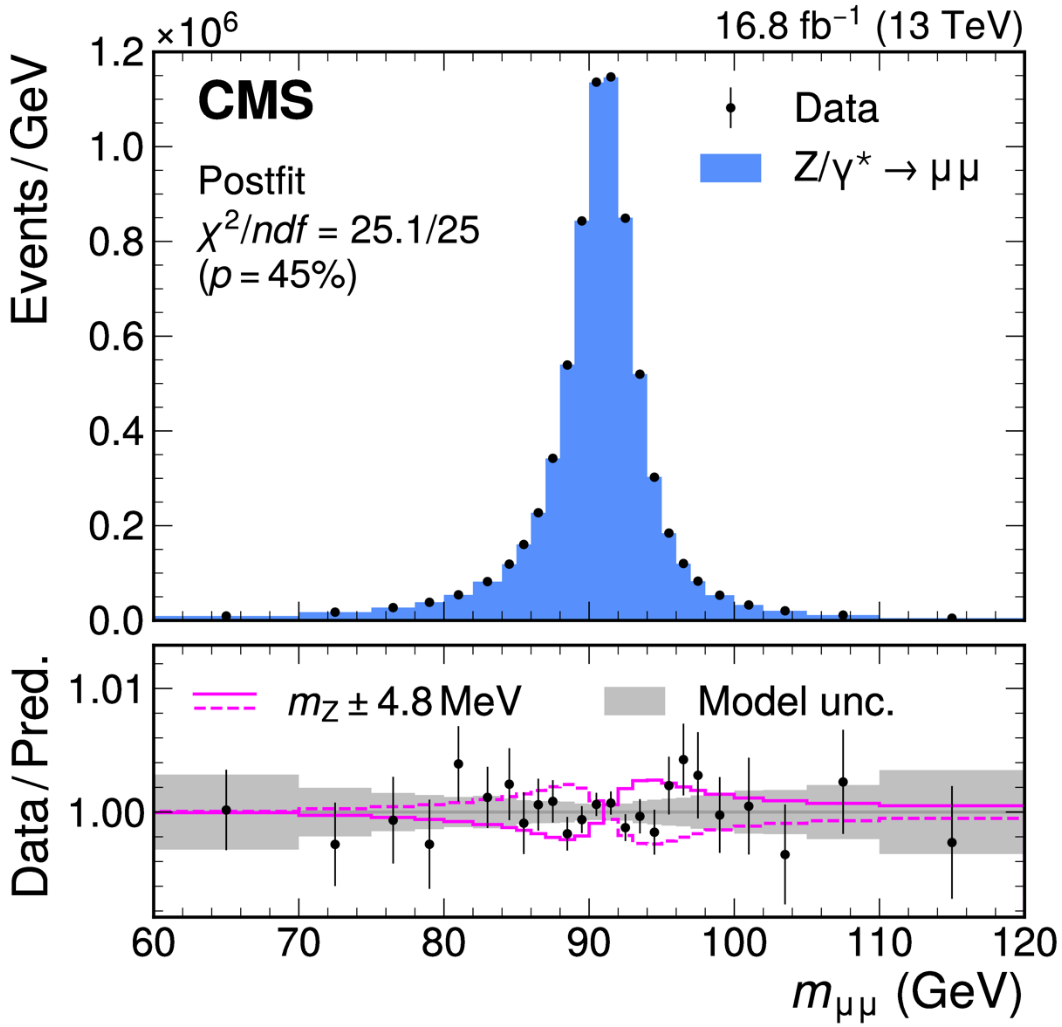
$\mathbf{2.1}$ = smallest **inflation factor** such that $\chi^2/ndof = 1$

Uncertainties & closure test

- Uncertainties on **momentum scale**:
  - $(\mathbf{2.1}\ \times)\ \boldsymbol{\sigma}_{\mathbf{stat}}$ from J/Ψ
  - $\boldsymbol{\sigma}_{\mathbf{stat}}$ from $\mathrm{Z-closure}$
  - $\Delta \boldsymbol{m}_{\boldsymbol{Z}}^{\mathbf{LEP}}$

Impact on $\boldsymbol{m}_{\boldsymbol{W}}$ → $\mathbf{4.8}$ MeV

Uncertainties & closure test



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Impact on $\boldsymbol{m_W}$ → $\mathbf{4.8}$ MeV

- Validation by fitting $\left(m^{\mu\mu}, \eta^{\mu-\mathrm{fwd}}\right)$ spectrum:

$$m_Z - m_Z^{\mathrm{PDG}} = -2.2 \pm 4.8\ \mathrm{MeV}$$
$$= -2.2 \pm 1.0\ (\mathrm{stat}) \pm 4.7\ (\mathrm{syst})\ \mathrm{MeV}$$

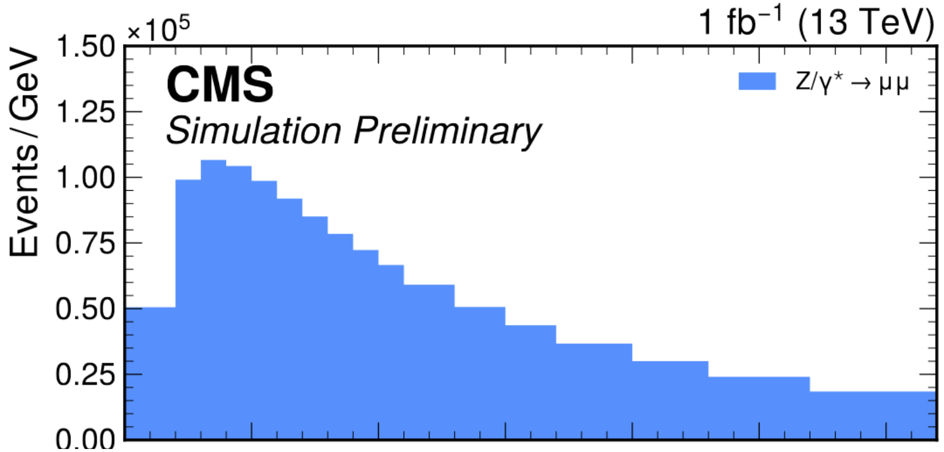
(not yet an independent measurement of $\boldsymbol{m_Z}$)

W and Z modeling: p_T^V

EPJ+ 136 (2021) 214 F. Tackman's slides

JHEP07(2022)129 G. Marinelli's slides

arXiv:2411.16004 arXiv:2411.18606



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$$p_T \frac{d\sigma}{dp_T} = \left[H \times B_a \otimes B_b \otimes S \right](\alpha_S, L \equiv \ln p_T/m_Z) + \mathcal{O}\left(\frac{p_T^2}{m_Z^2}\right)$$

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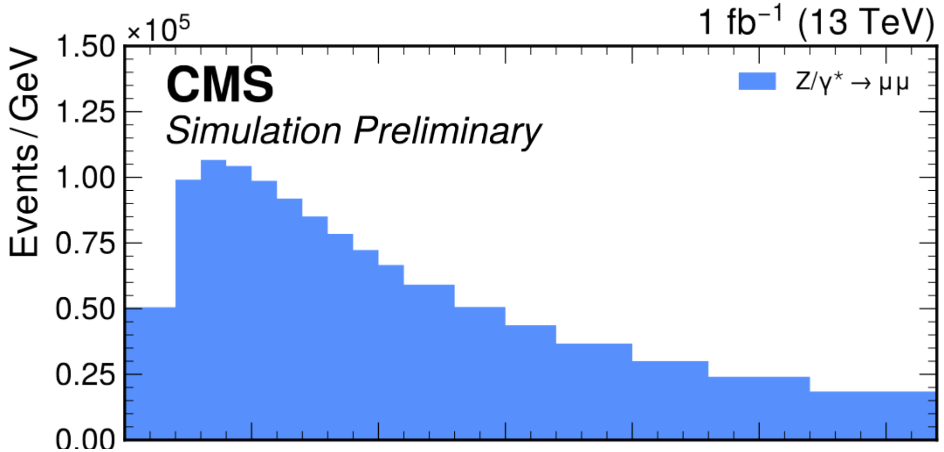

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$$F(\alpha_S, L) = F(\alpha_S) \exp \int_0^L dL' \{ \Gamma[\alpha_S(L')] L' + \gamma_F [\alpha_S(L')] \}$$

boundary conditions — anomalous dimensions

W and Z modeling: p_T^V

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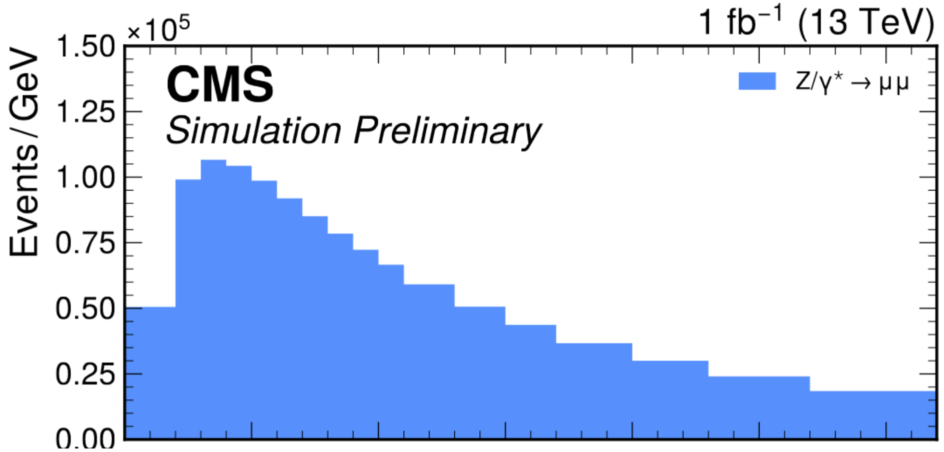
boundary conditions anomalous dimensions

$$f^{\rm pred}(\alpha) = f_0 + \alpha f_1 + \alpha^2 f_2 + \alpha^3 f_3(\theta_3) + \mathcal{O}(\alpha_S^4)$$



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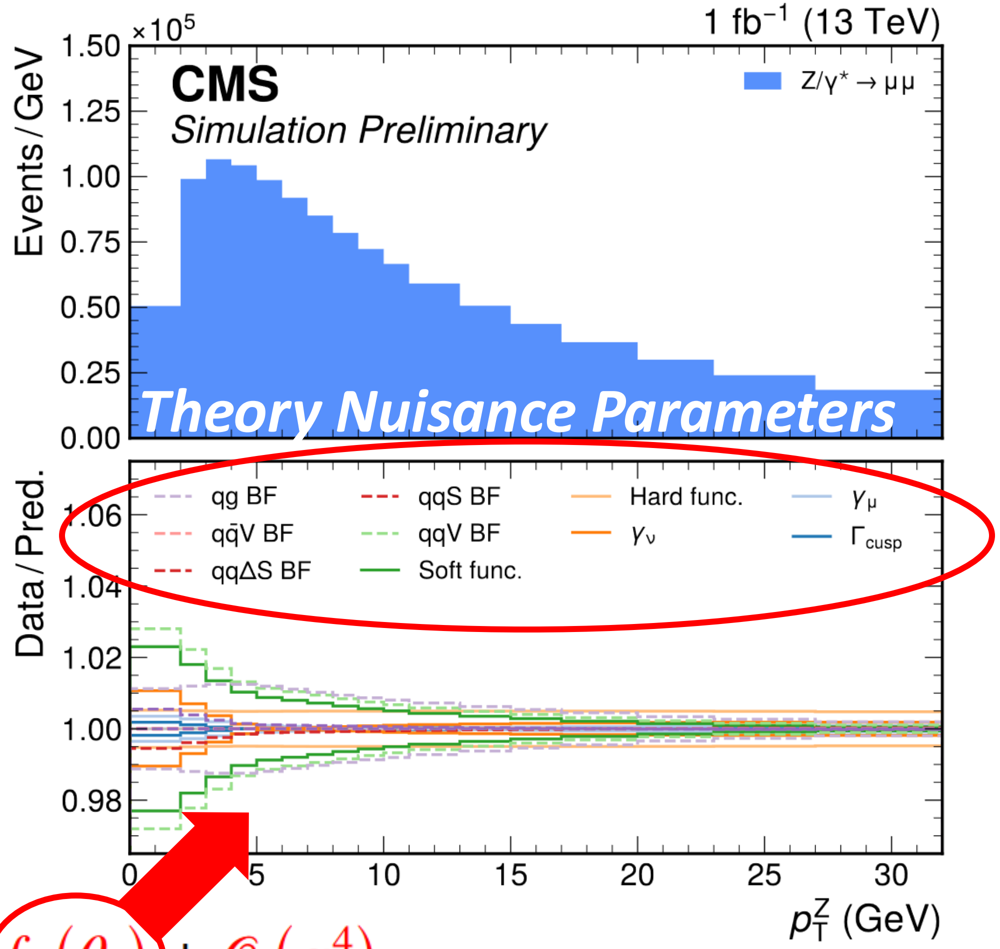

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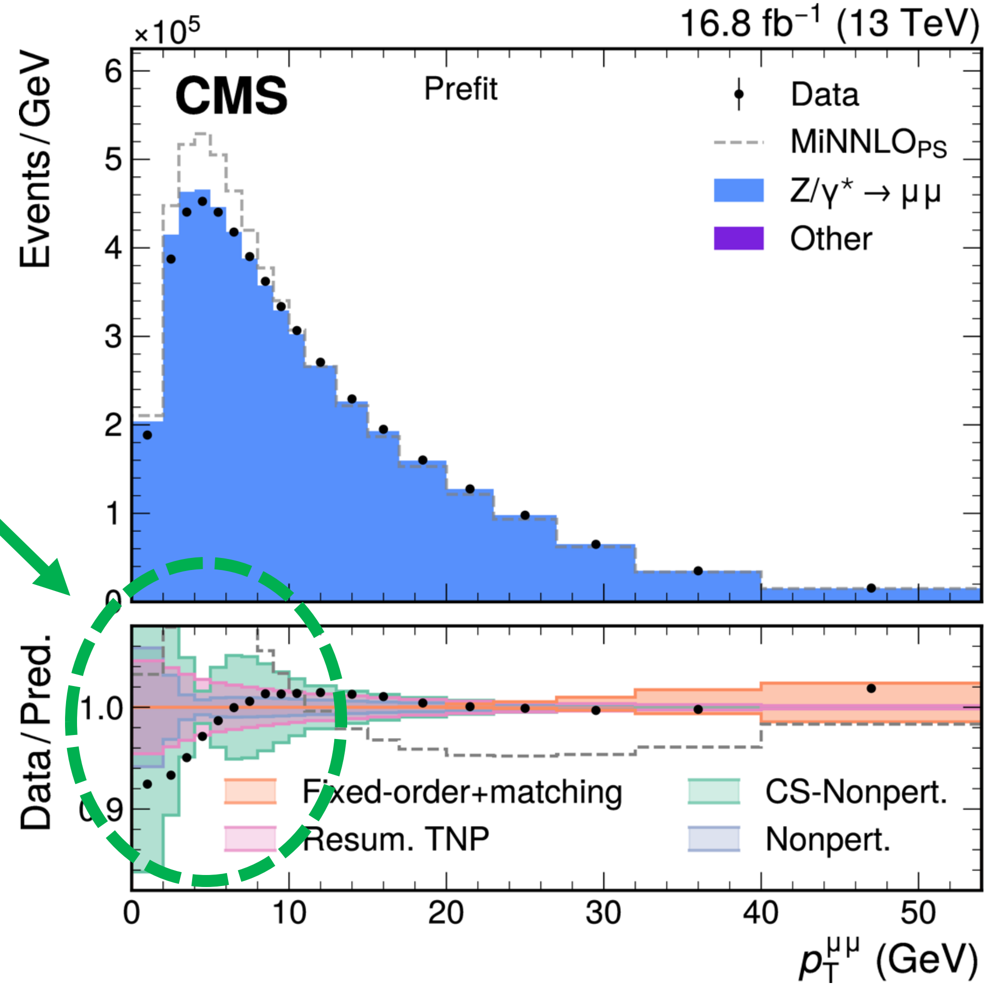

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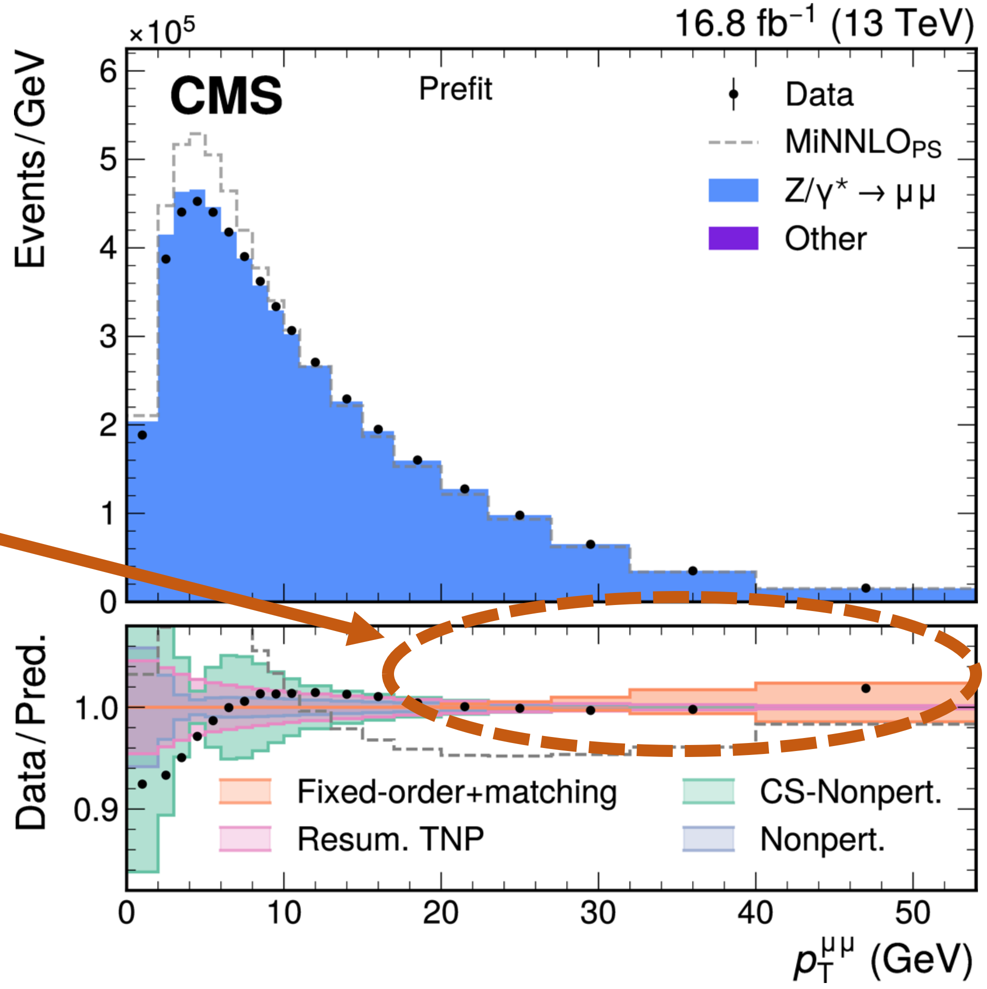
  - Variations μ_R/μ_F scale and transition-point



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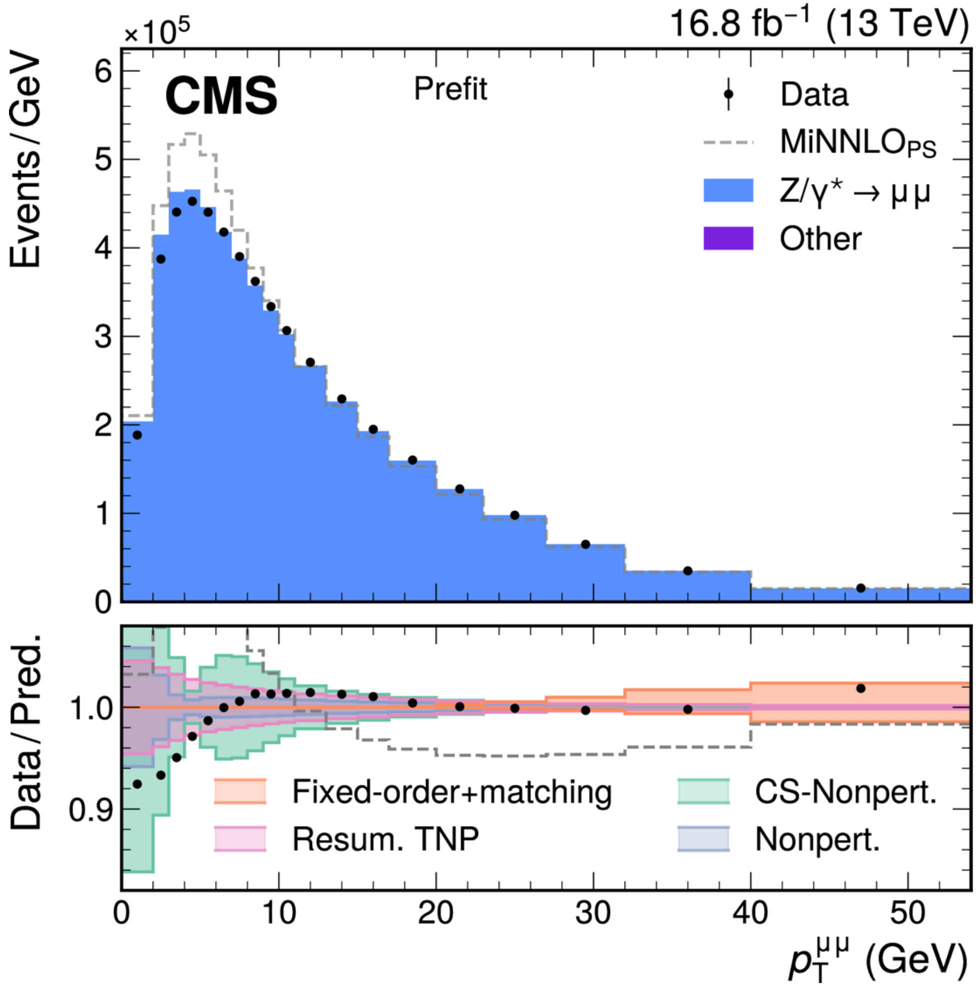
- **b/c quark-masses** (→ MSHT20)
  - variation of heavy quark thresholds in PDFs

TOTAL Impact on m_W → ~2 MeV



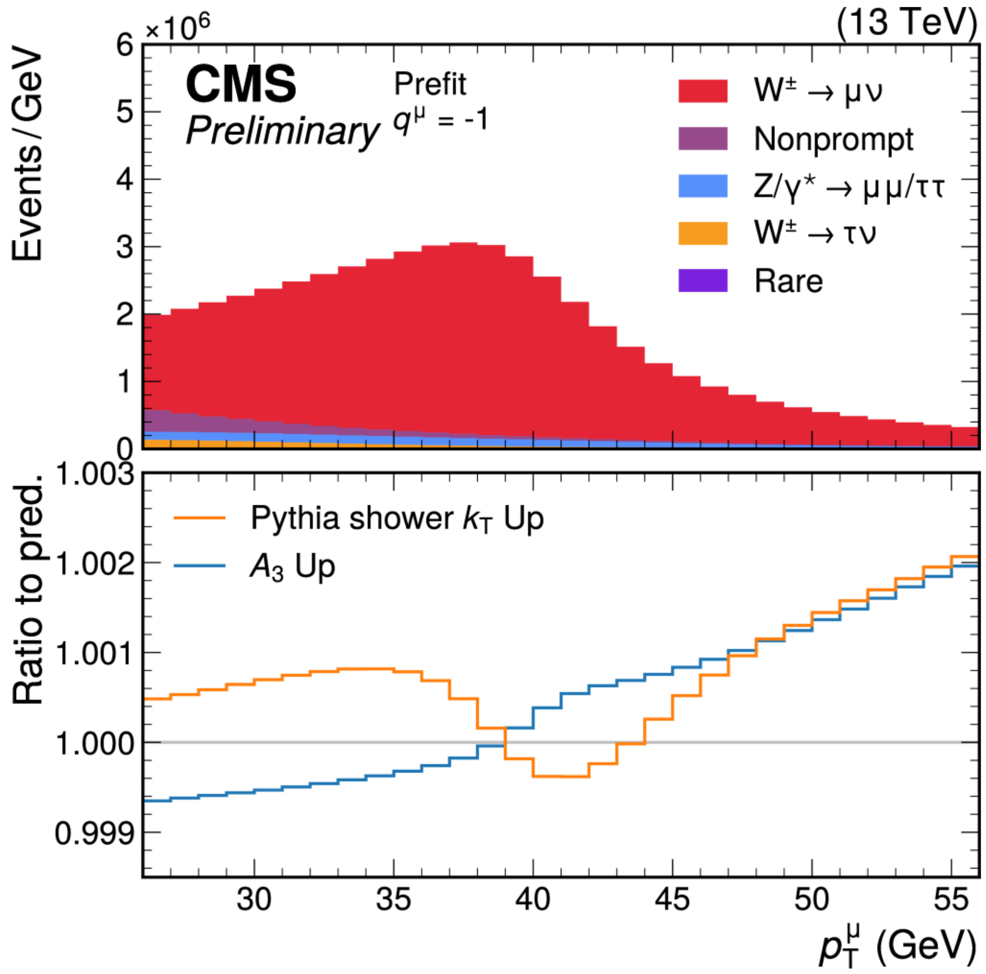
W and Z modeling: $\boldsymbol{A_i}$

- **Angular coefficients** (→ MiNNLO$_{PS}$ @NLO)
  - Envelope of 7-point scale variations in bins of p_T^V
  - Full difference

    MiNNLO$_{PS}$ *vs*. **MiNNLO$_{PS}$ + PYTHIA**

    (due to PYTHIA parton shower/intrinsic k_T)

Impact on m_W → $\sim$3.3 MeV



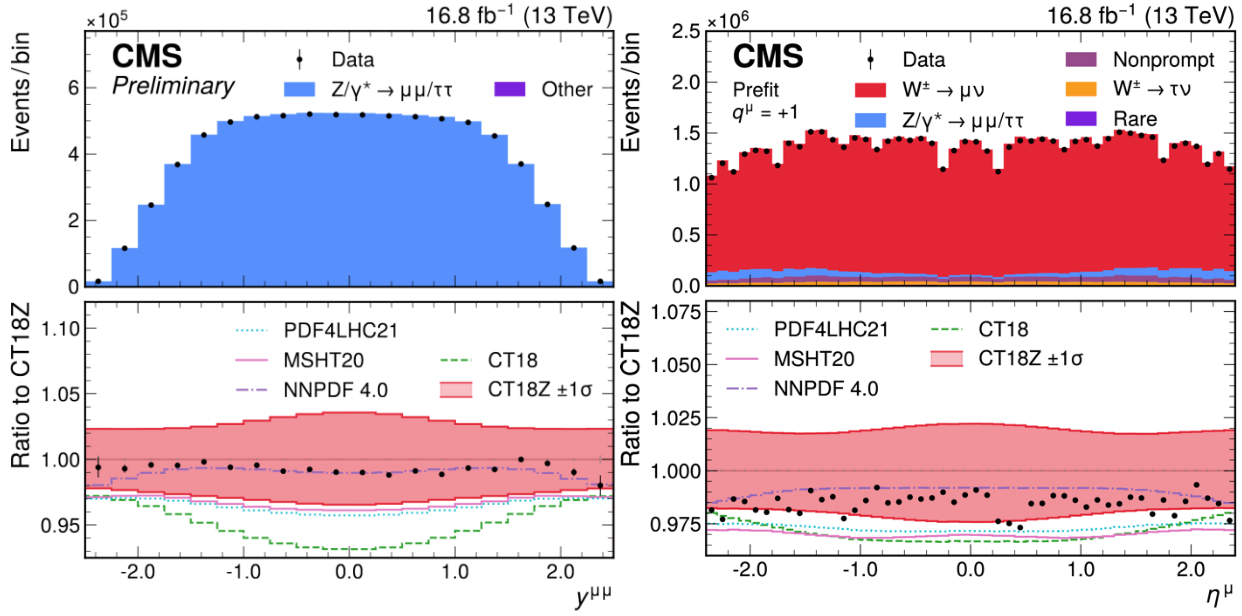
PDFs

REMINDER: **PDFs are profiled *in situ***

- We chose **CT18Z** as nominal PDF set because:
  - good **pre-fit agreement on y^Z, η^ℓ**
  - relatively **large** uncertainty
  - it **covers** alternate PDF sets, i.e.

$$|m_W^{\text{alt.PDF}} - m_W^{\text{nom. PDF}}| \leq \sigma_{\text{nom. PDF}}$$

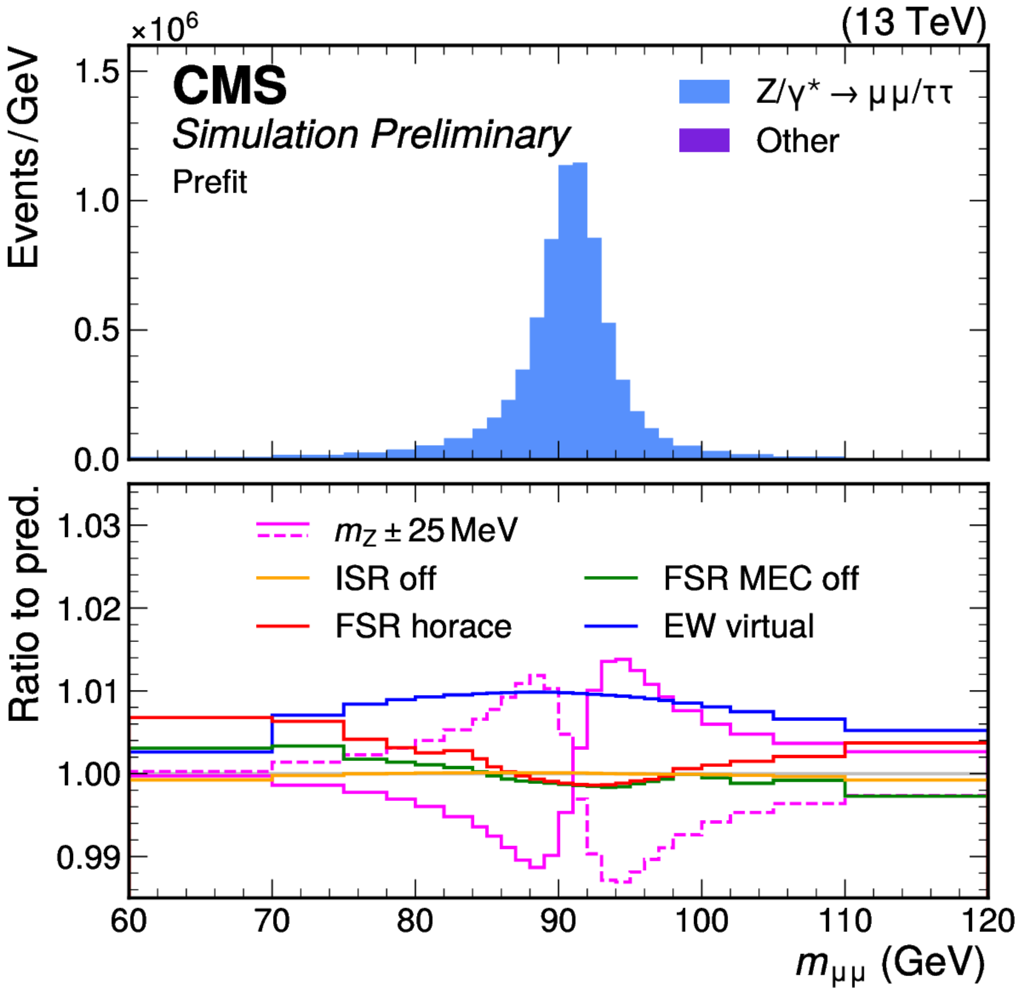
Impact on m_W → 4.4 MeV



PDF set	Scale factor	Impact in m_W (MeV) Original σ_{PDF}	Scaled σ_{PDF}
CT18Z	–	4.4	
CT18	–	4.6	
PDF4LHC21	–	4.1	
MSHT20	1.5	4.3	5.1
MSHT20aN3LO	1.5	4.2	4.9
NNPDF3.1	3.0	3.2	5.3
NNPDF4.0	5.0	2.4	6.0

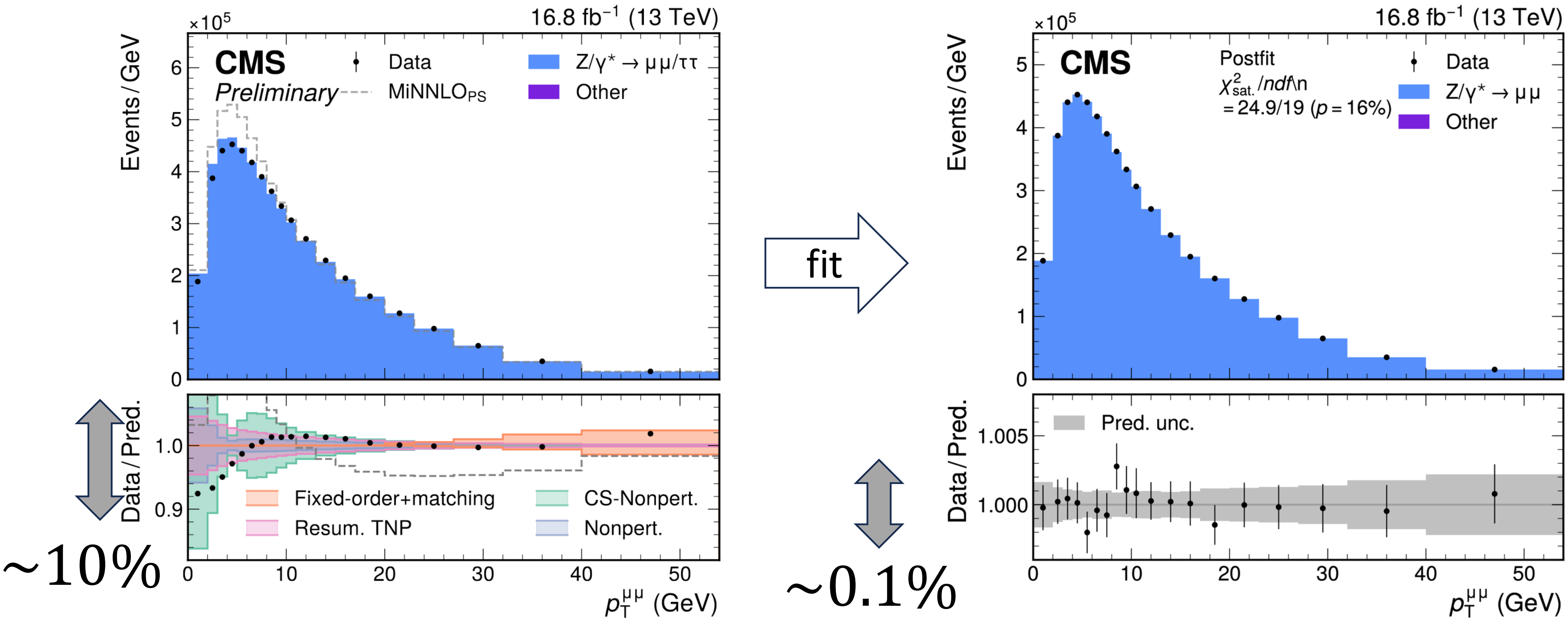
EWK uncertainties

- **FSR** (→ PHOTOS++ @LL+MEC)
  - uncertainty from switching on/off the MEC and from full difference with HORACE
- **ISR** (→ PYTHIA8 @LL)
  - uncertainty from switching on/off
- **Virtual EWK** (→ not included in nominal MC)
  - External calculations from:
    - RENESANCE (for W)
    - POWHEG-BOX-V2 (for Z)
  - NLO/LO ratio taken as a systematic



Impact on m_W → 1.9 MeV

Model validation: $(p_T^{\mu\mu}, y^{\mu\mu})$ spectrum



Model validation: W-like

- PROOF OF PRINCIPLE: measure m_Z via a $(\boldsymbol{p_T^{\mu}}, \boldsymbol{\eta^{\mu}}, \boldsymbol{q^{\mu}})$ **fit**

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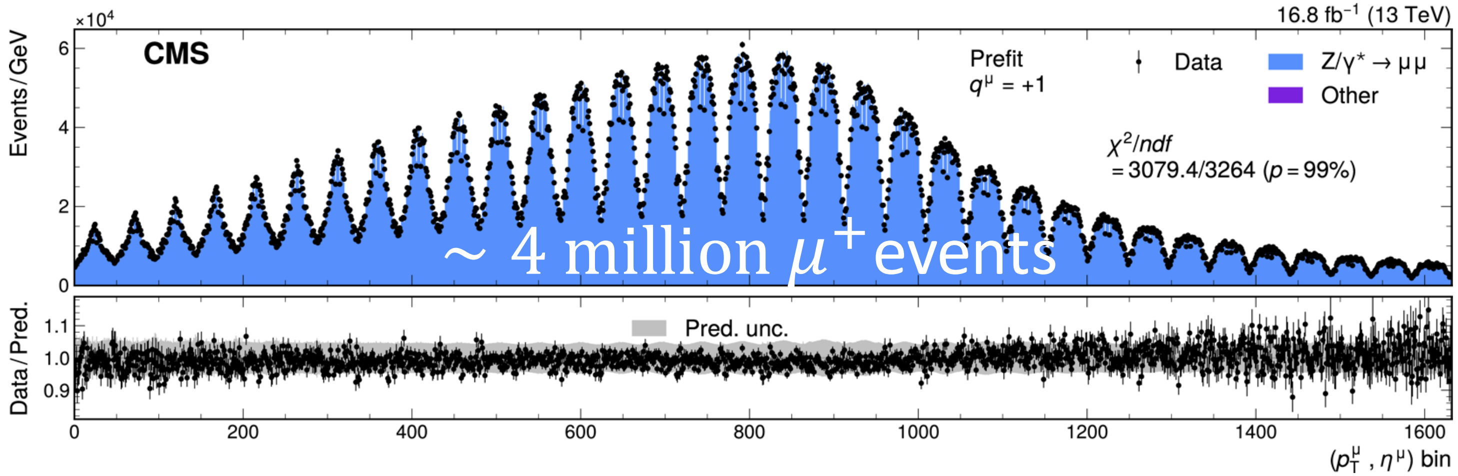
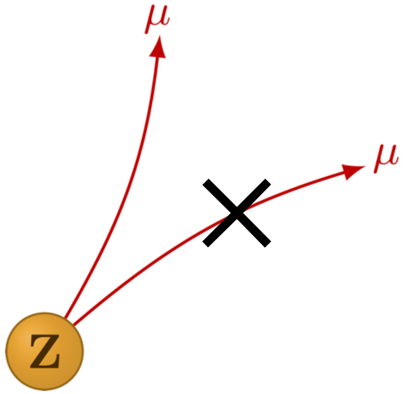
$\boldsymbol{\mu^+}$ in **even-numbered** events





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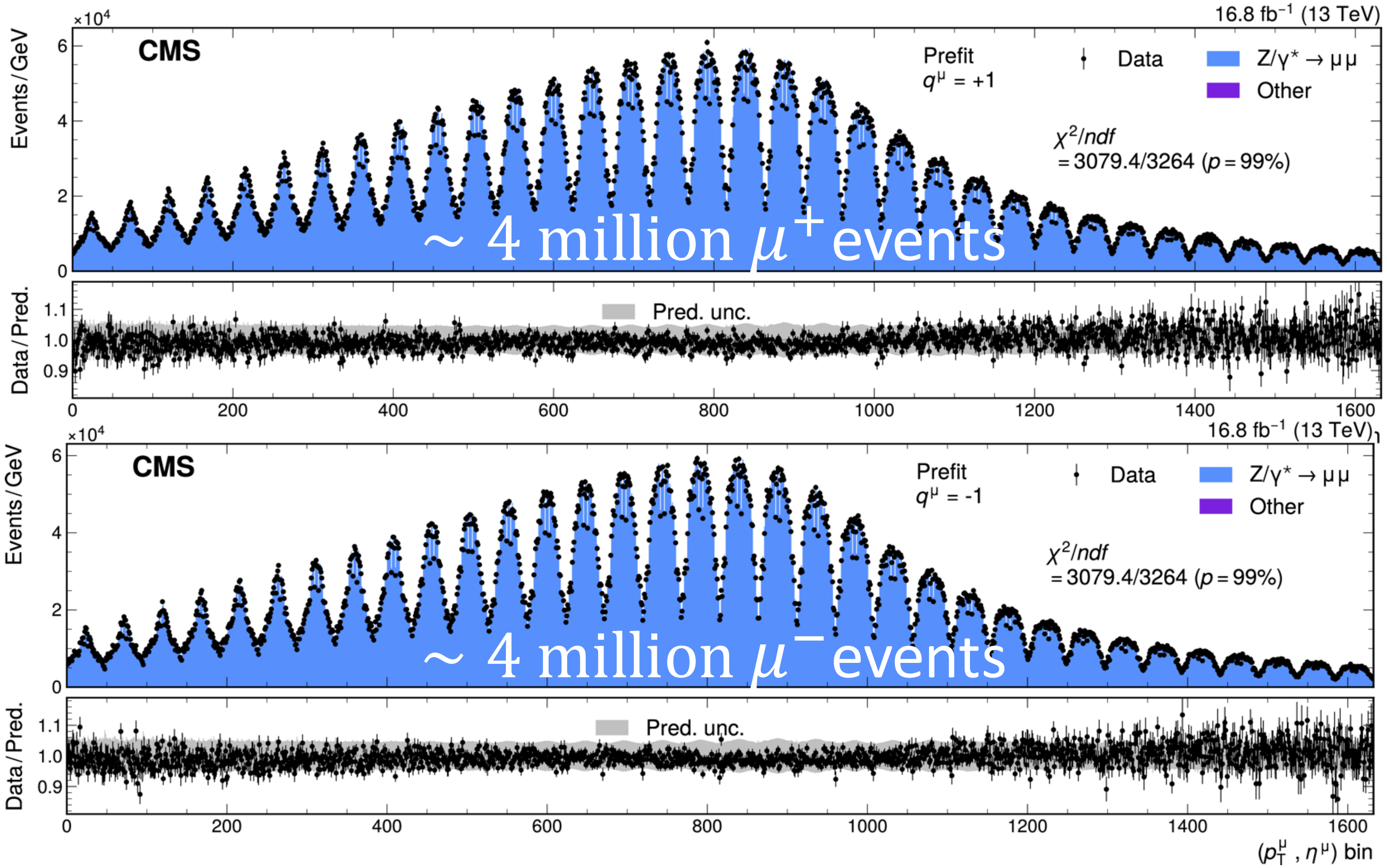
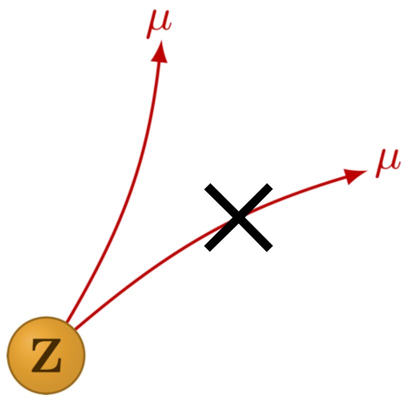
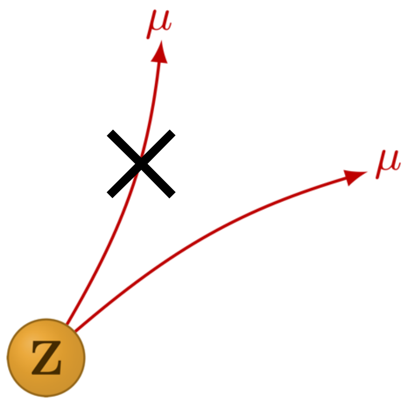
$\boldsymbol{\mu^+}$ in **even-numbered** events

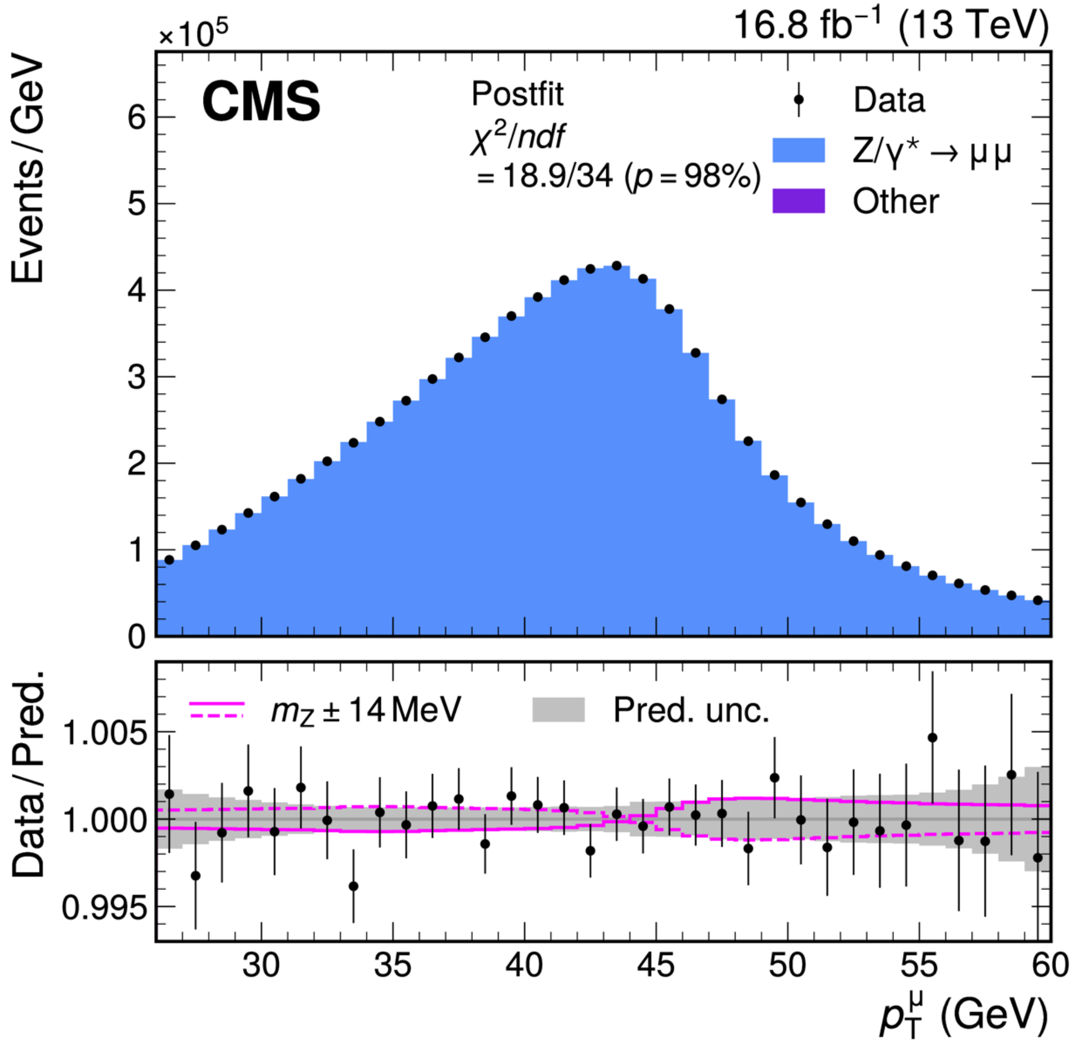
$\boldsymbol{\mu^-}$ in **odd-numbered** events



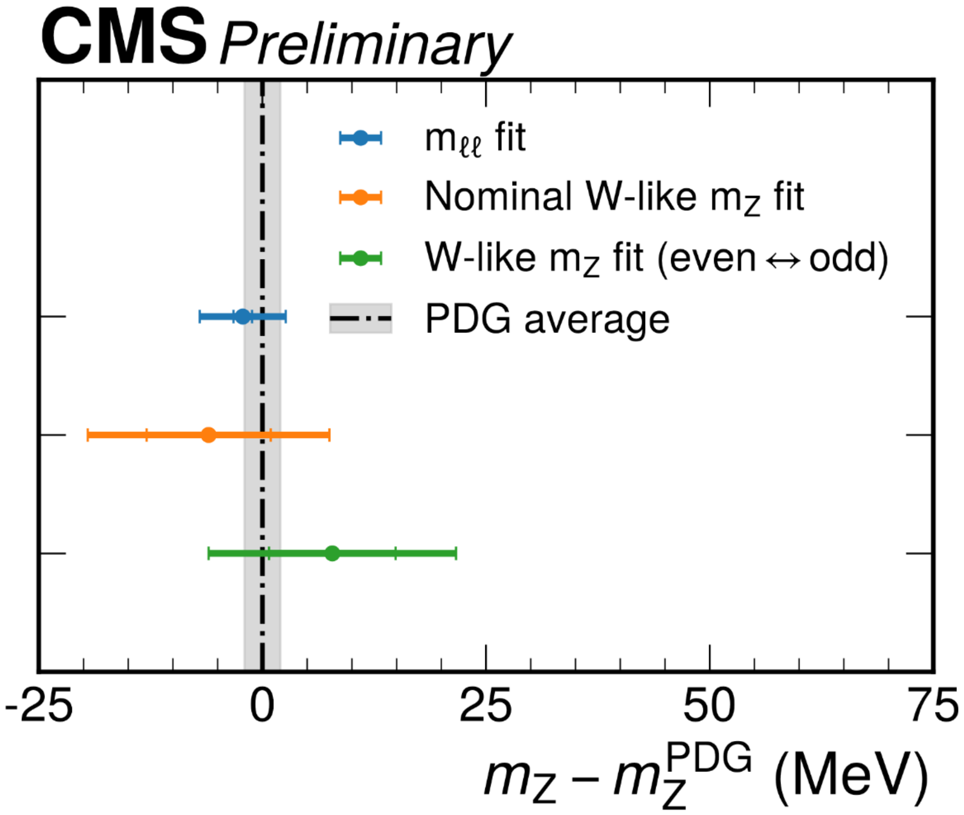




W-like: results



- Total uncertainty on m_Z is **13.5 MeV**
  - Muon scale (5.6), A_i (4.9), muon eff. (3.8)

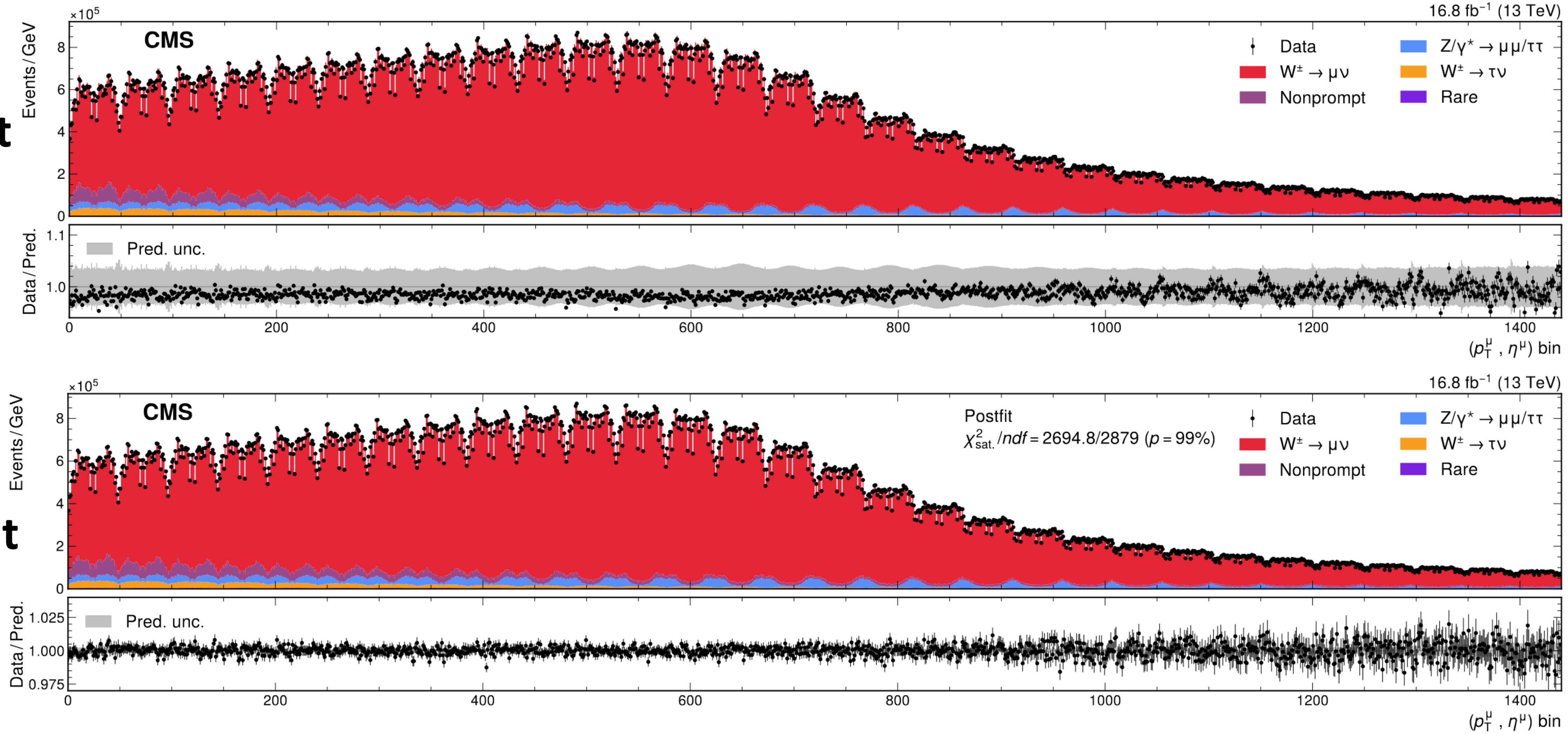


Moving to the W

$4{,}858$ **nuisance parameters**
(with Gaussian constraints)

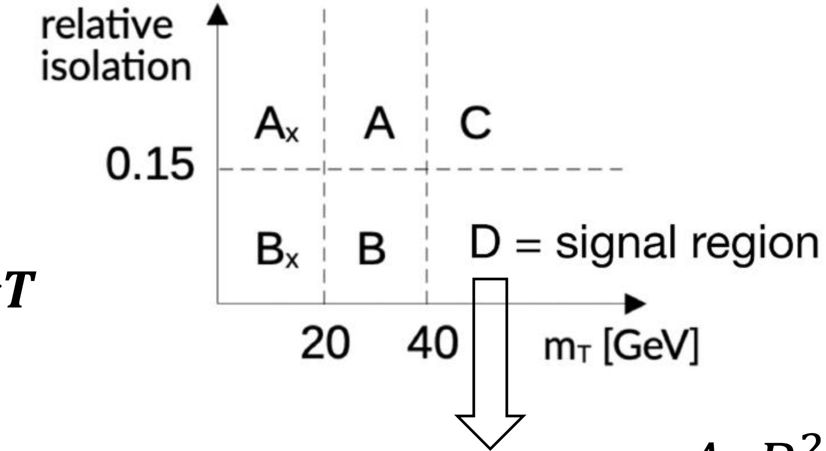
Pre-fit

Post-fit

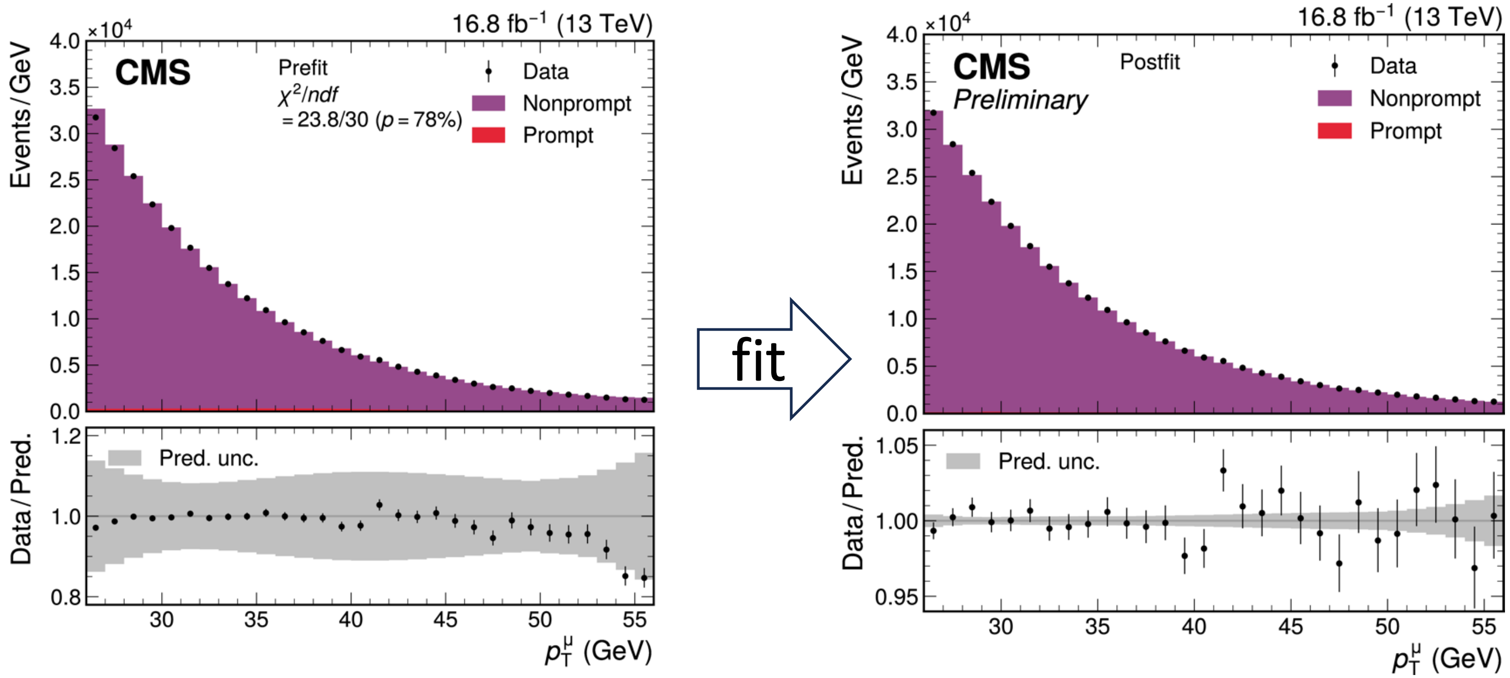


Non-prompt background

- Mostly muons from $\boldsymbol{B/C}$ **hadron decay**
- "Extended-ABCD" method based on **isolation** : $\boldsymbol{m_T}$
  - Validated on MC simulation and data sidebands



$$D = C \cdot \frac{A_x B^2}{A_x A^2}$$

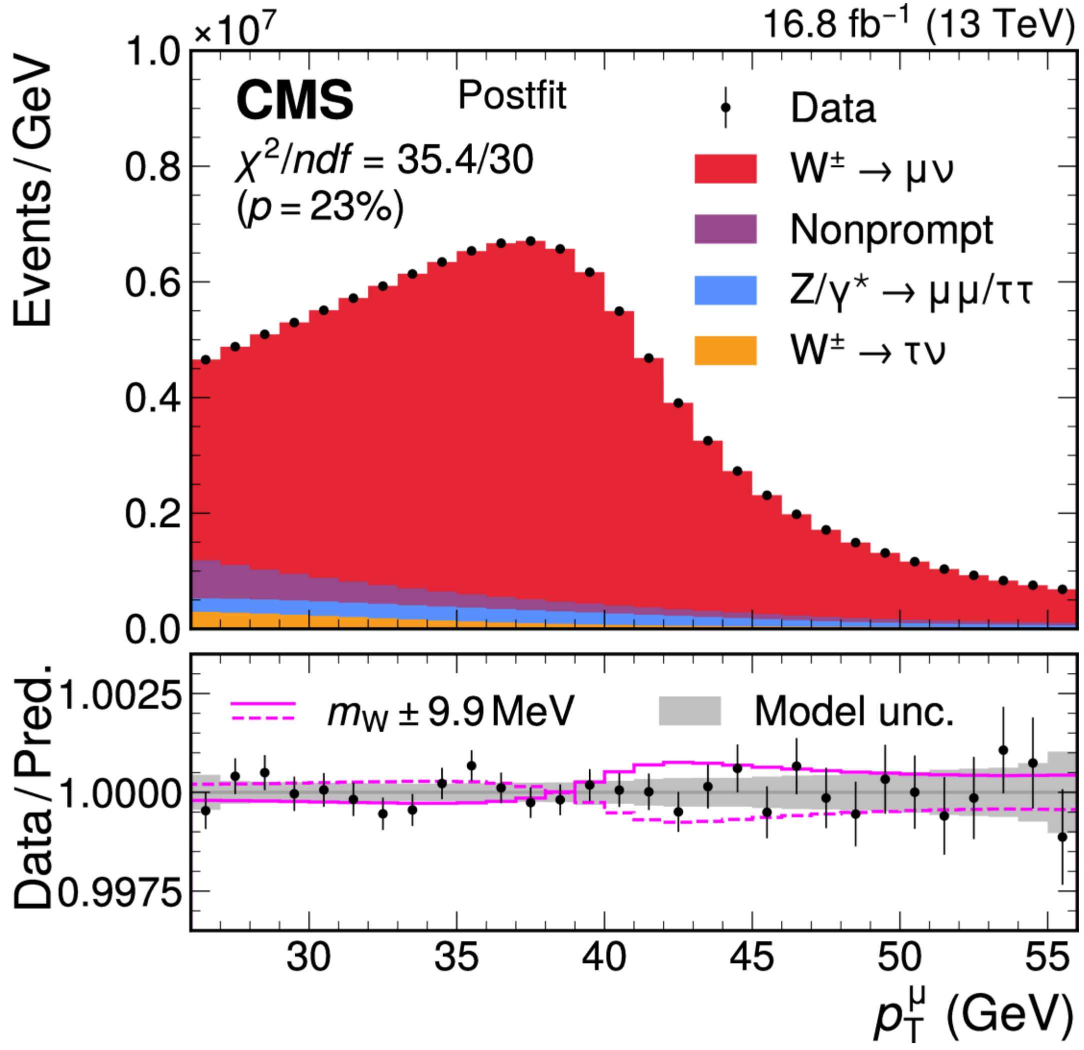


Enforcing analytic p_T spectrum:

$$f_i(p_T) \propto e^{-(a_i p_T^3 + b_i p_T^2 + c_i p_T)}$$

Impact on m_W → ~3 MeV

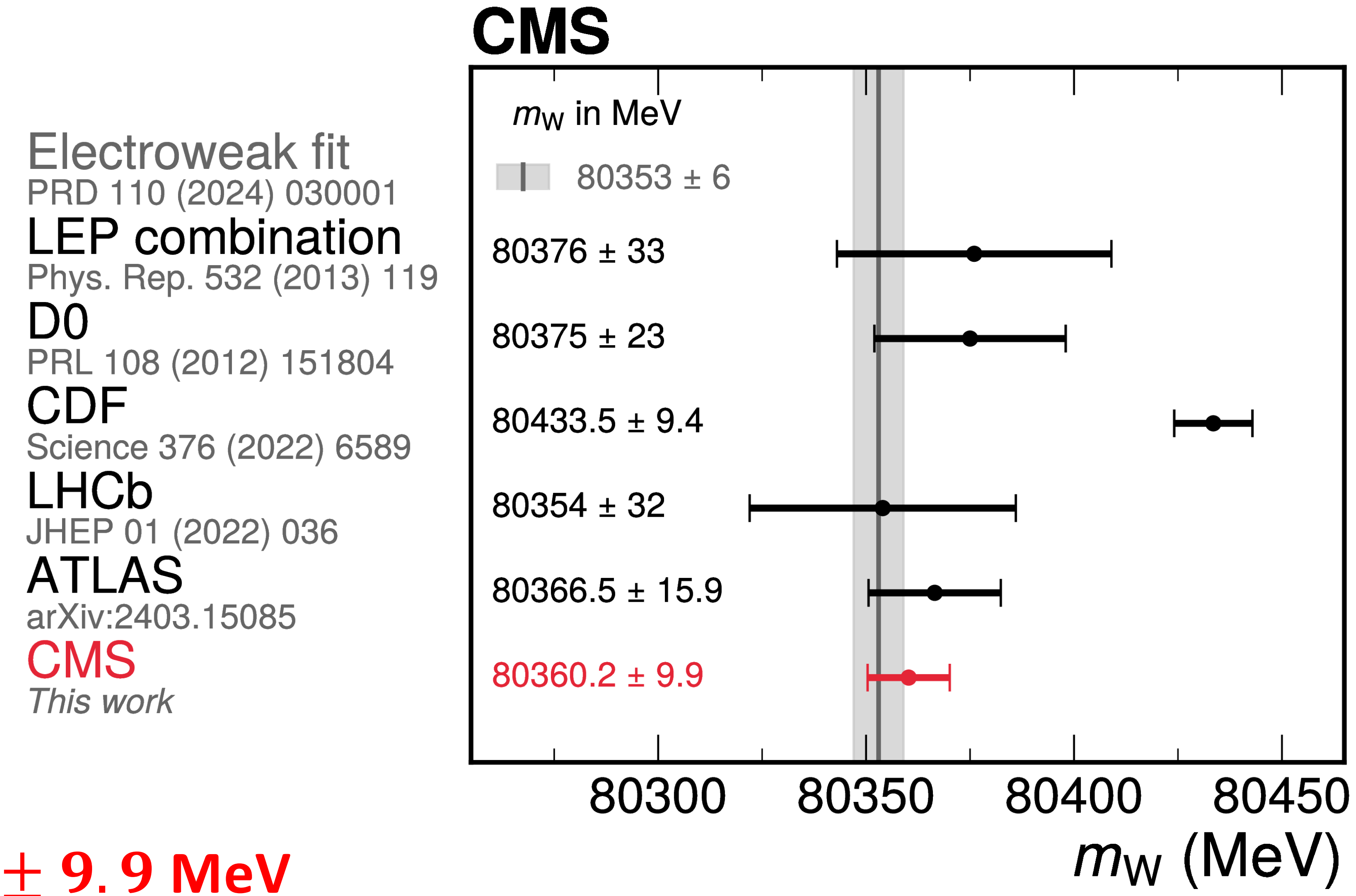
Unblinding the W fit



- Total uncertainty on m_W is **9.9 MeV**
  - m_W **blinded** until all check completed

Source of uncertainty	Nominal in m_Z	Nominal in m_W
Muon momentum scale	5.6	4.8
Muon reco. efficiency	3.8	3.0
W and Z angular coeffs.	4.9	3.3
Higher-order EW	2.2	2.0
p_T^V modeling	1.7	2.0
PDF	2.4	4.4
Nonprompt background	–	3.2
Integrated luminosity	0.3	0.1
MC sample size	2.5	1.5
Data sample size	6.9	2.4
Total uncertainty	13.5	9.9

Results



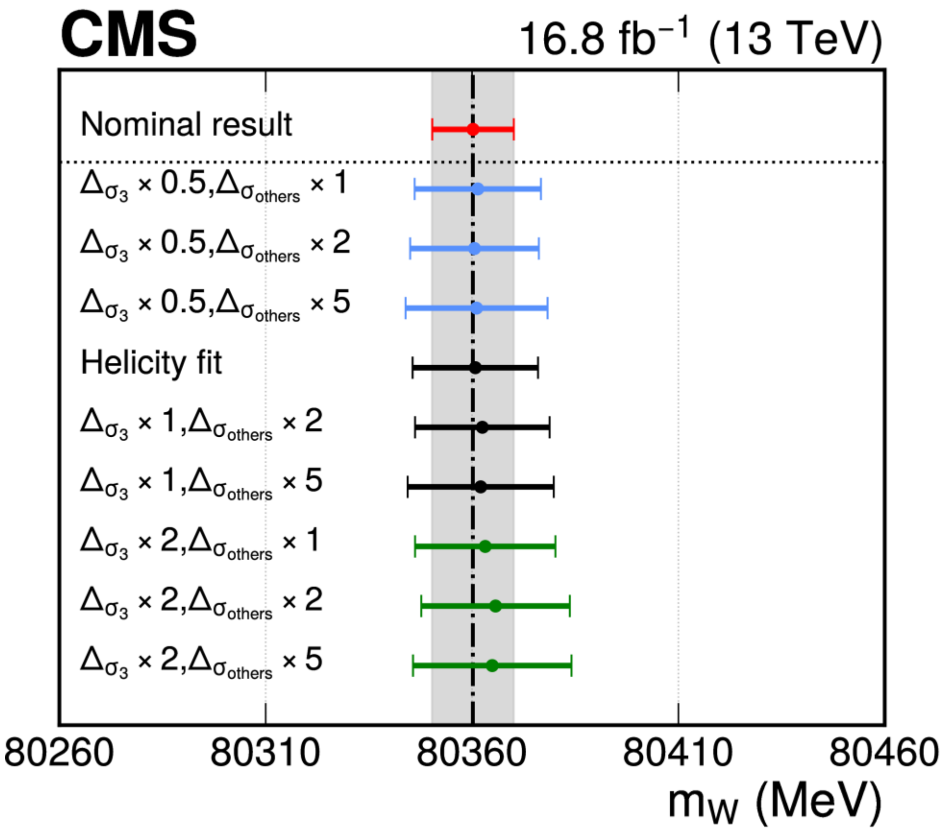
$$m_W^{\mathrm{CMS}} = 80360.2 \pm 9.9\ \mathrm{MeV}$$

Test of model dependence

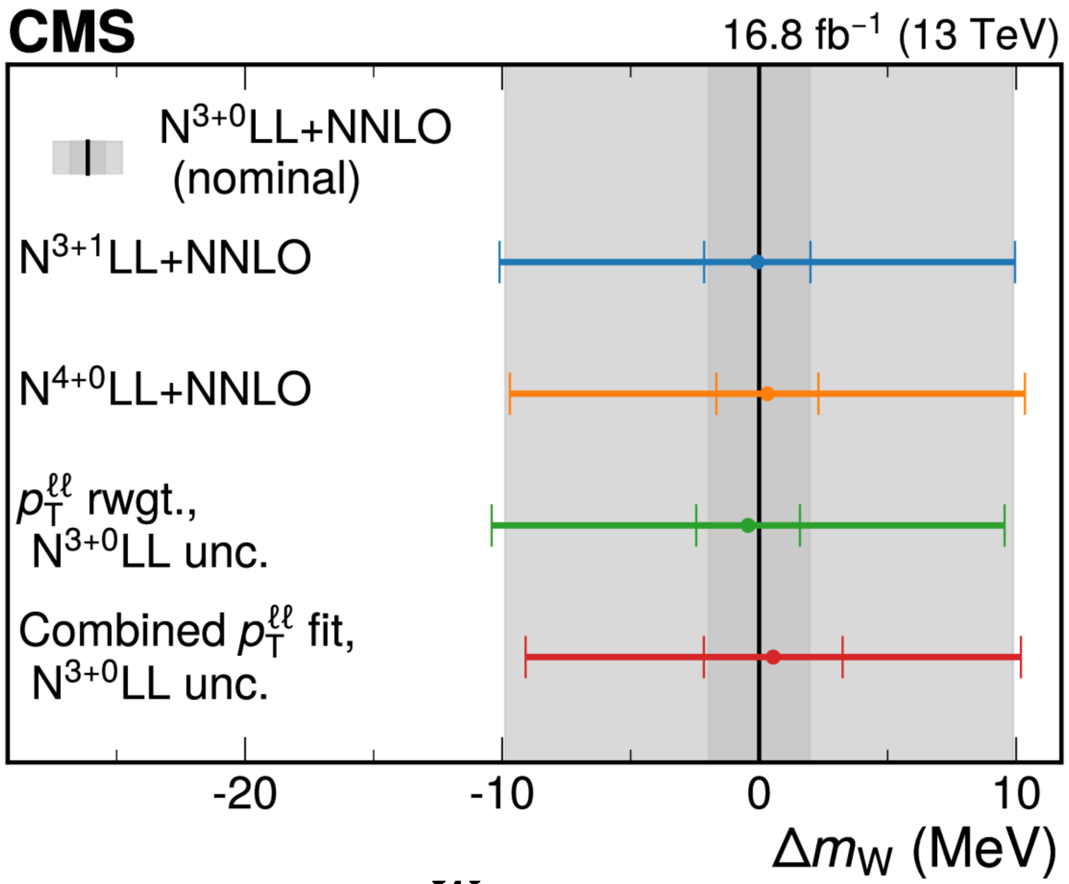
- Assigning additional priors on **helicity cross sections** $\boldsymbol{\sigma_i \equiv \sigma_{\mathrm{UL}} \times A_i}$

- **Stability of** $\boldsymbol{m_W}$ tested for increasingly looser priors

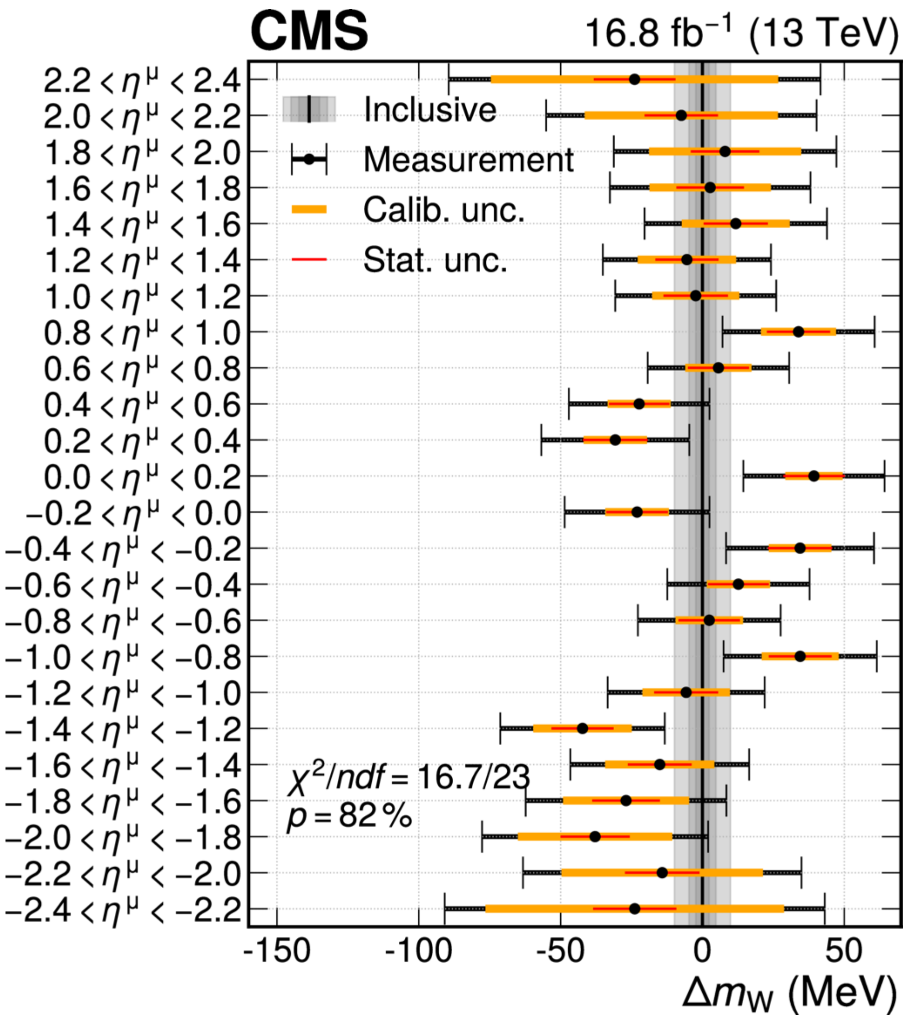
  → no evidence for tensions/trends



Test of model dependence



→ Different p_T^W **uncertainty models**

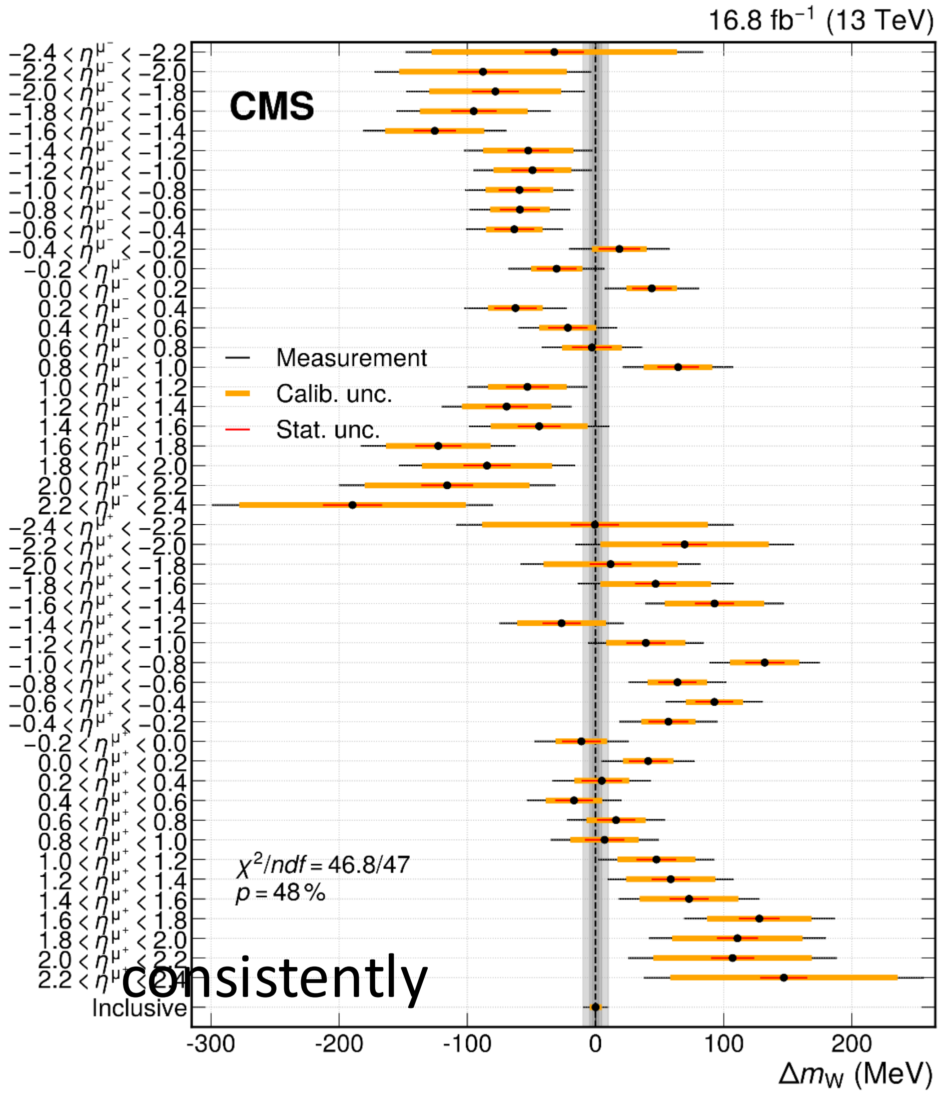


→ Different **detector** regions

Charge asymmetry

- $\boldsymbol{m_{W^+} - m_{W^-} = 57 \pm 30}$ **MeV** (p-value = 6%)
  - Correlation with **avg. mass** ~ 0.02

Source of uncertainty	Global impact (MeV) in $m_{Z^+} - m_{Z^-}$	in m_Z	in $m_{W^+} - m_{W^-}$	in m_W
Muon momentum scale	21.2	5.3	20.0	4.4
Muon reco. efficiency	6.5	3.0	5.8	2.3
W and Z angular coeffs.	13.9	4.5	13.7	3.0
Higher-order EW	0.2	2.2	1.5	1.9
p_T^V modeling	0.4	1.0	2.7	0.8
PDF	0.7	1.9	4.2	2.8
Nonprompt background	–	–	4.8	1.7
Integrated luminosity	< 0.1	0.2	0.1	0.1
MC sample size	6.4	3.6	8.4	3.8
Data sample size	18.1	10.1	13.4	6.0
Total uncertainty	32.5	13.5	30.3	9.9



consistently

- Likely, a combination of alignment/theory NP's shifted by $\sim 1\sigma$ from their prior
  - No significant bias on **average** $\boldsymbol{m_W}$ even for generous shifts of pre-fit NP

Comparing with ATLAS p_T^{μ}-only fit

arXiv:2403.15085

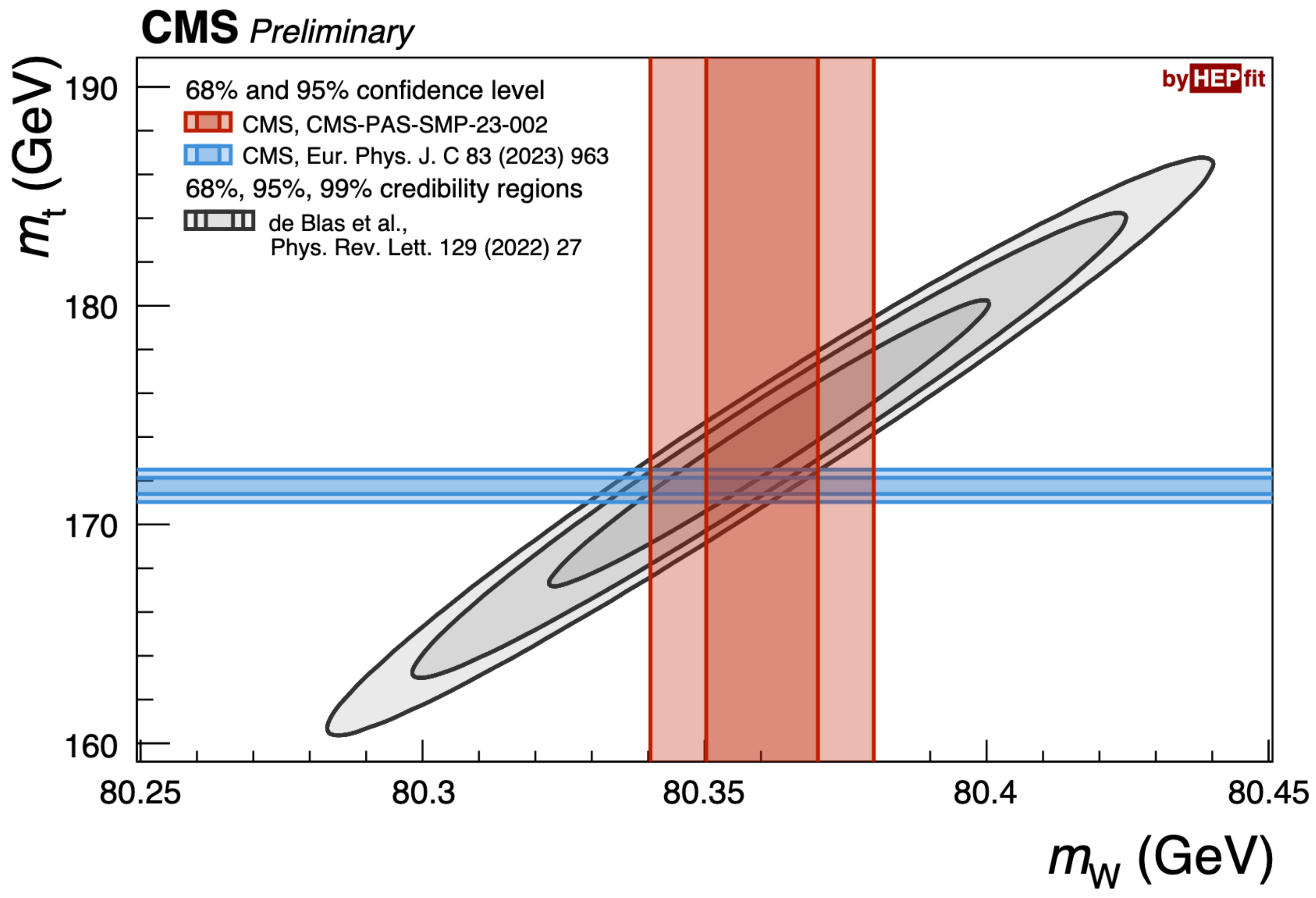
Unc. [MeV]	Total	Stat.	Syst.	PDF	A_i	Backg.	EW	e	μ	u_T	Lumi	Γ_W	PS
p_T^{ℓ}	16.2	11.1	11.8	4.9	3.5	1.7	5.6	5.9	5.4	0.9	1.1	0.1	1.5

For “global” impacts see arXiv:2307.04007

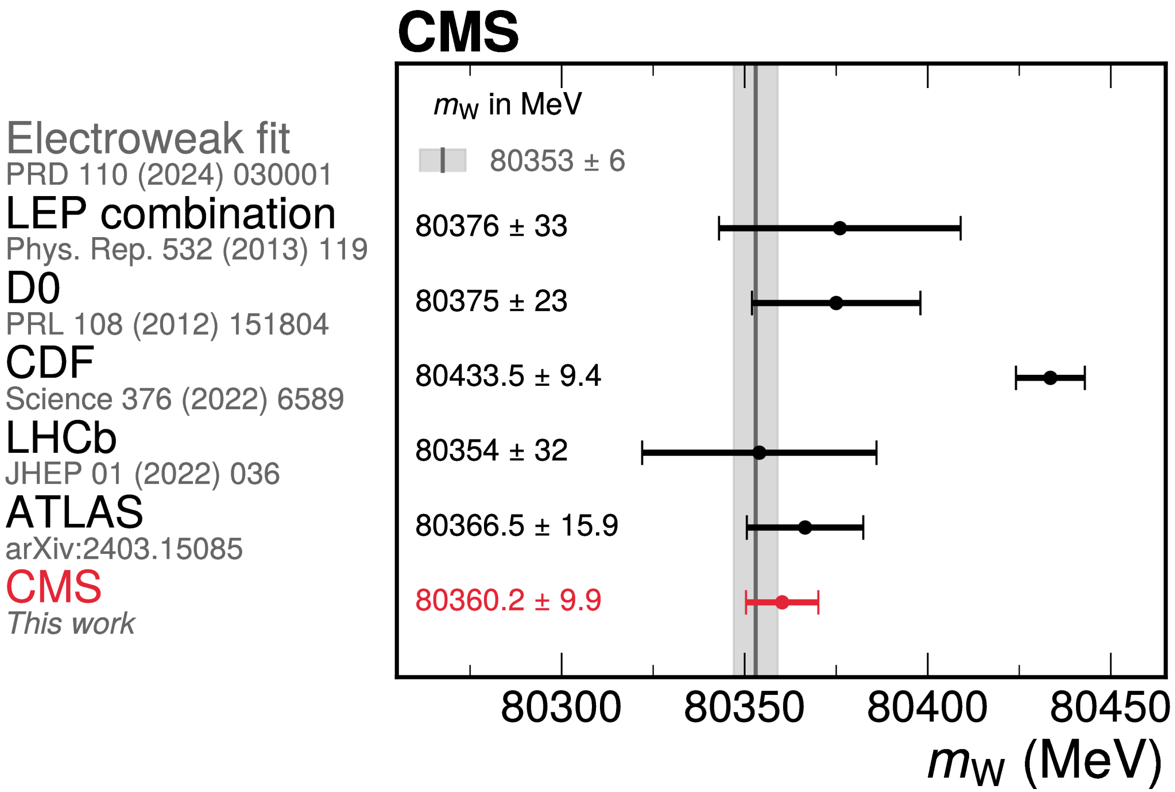
Source of uncertainty	Impact (MeV) Nominal in m_Z	Nominal in m_W	Global in m_Z	Global in m_W
Muon momentum scale	5.6	4.8	5.3	4.4
Muon reco. efficiency	3.8	3.0	3.0	2.3
W and Z angular coeffs.	4.9	3.3	4.5	3.0
Higher-order EW	2.2	2.0	2.2	1.9
p_T^V modeling	1.7	2.0	1.0	0.8
PDF	2.4	4.4	1.9	2.8
Nonprompt background	–	3.2	–	1.7
Integrated luminosity	0.3	0.1	0.2	0.1
MC sample size	2.5	1.5	3.6	3.8
Data sample size	6.9	2.4	10.1	6.0
Total uncertainty	13.5	9.9	13.5	9.9

CMS-PAS-SMP-23-002

The EWK fit and direct CMS (m_{t}, m_W)



Conclusions



- **First measurement** of m_W by CMS
  - **Most precise** measurement at the LHC
  - Approaching the precision of CDF
- Good **agreement with the SM** prediction and with the PDG average
- The **first in a line** of new precision EWK measurements by CMS

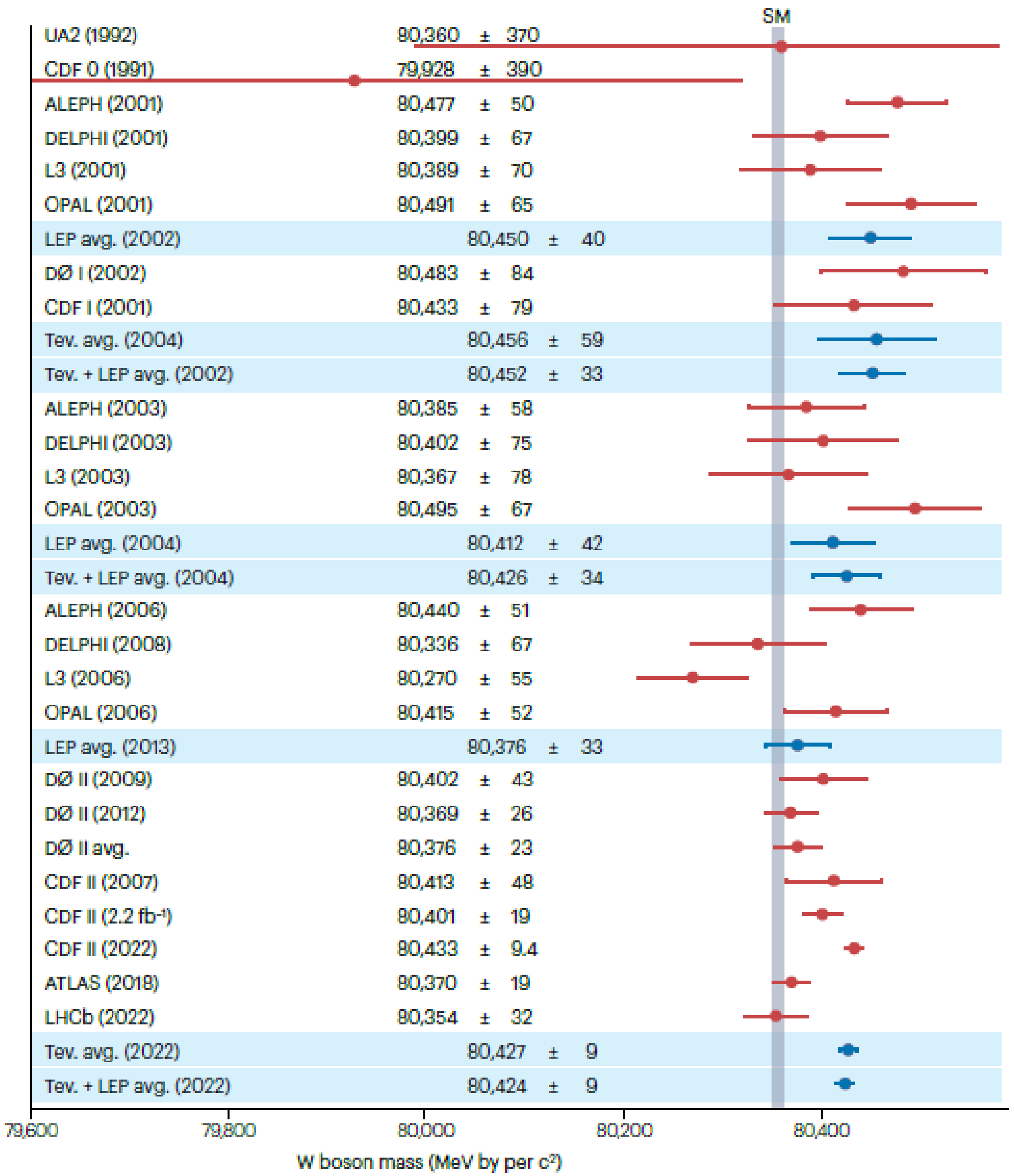
Grazie per l’attenzione!

Backup

Nature Reviews Physics **6** (2024) 180

~500 MeV

~10 MeV



+2 new results in 2024

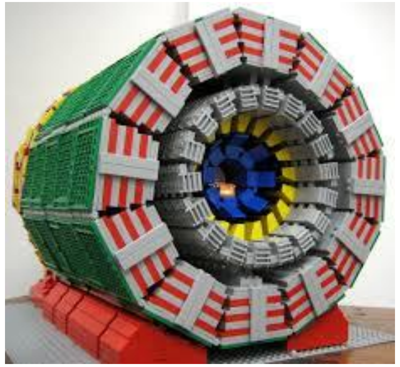
Measuring m_W at hadron colliders

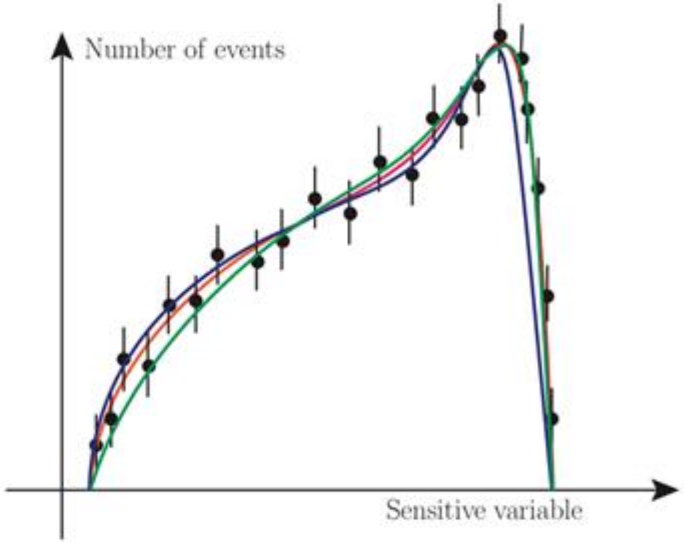
MC simulation

$pp \to W^{\pm} + X$

$\hookrightarrow \ell^{\pm} + \nu_{\ell}$

$\otimes$

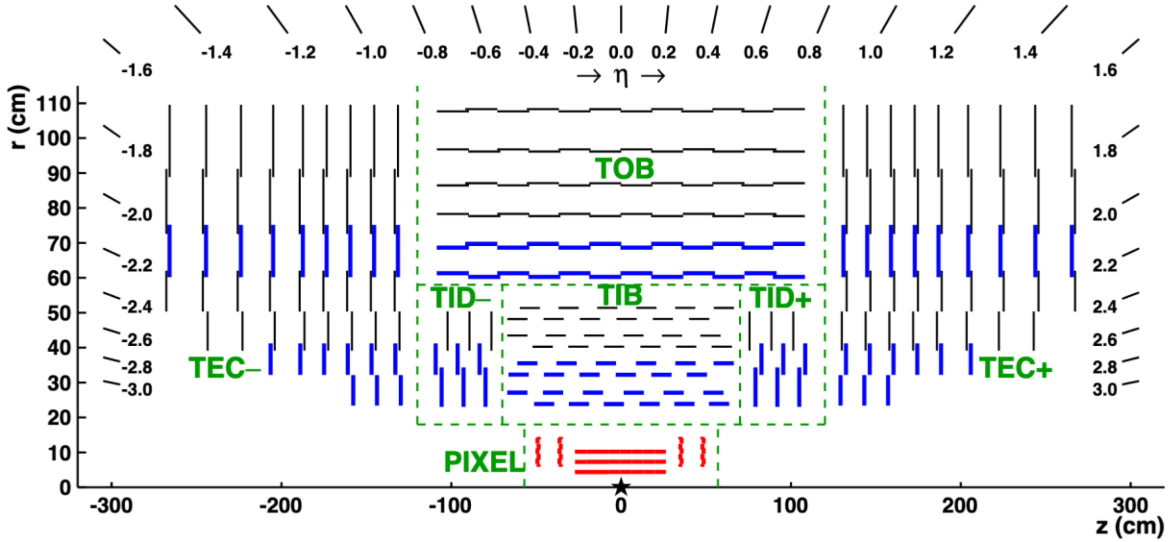




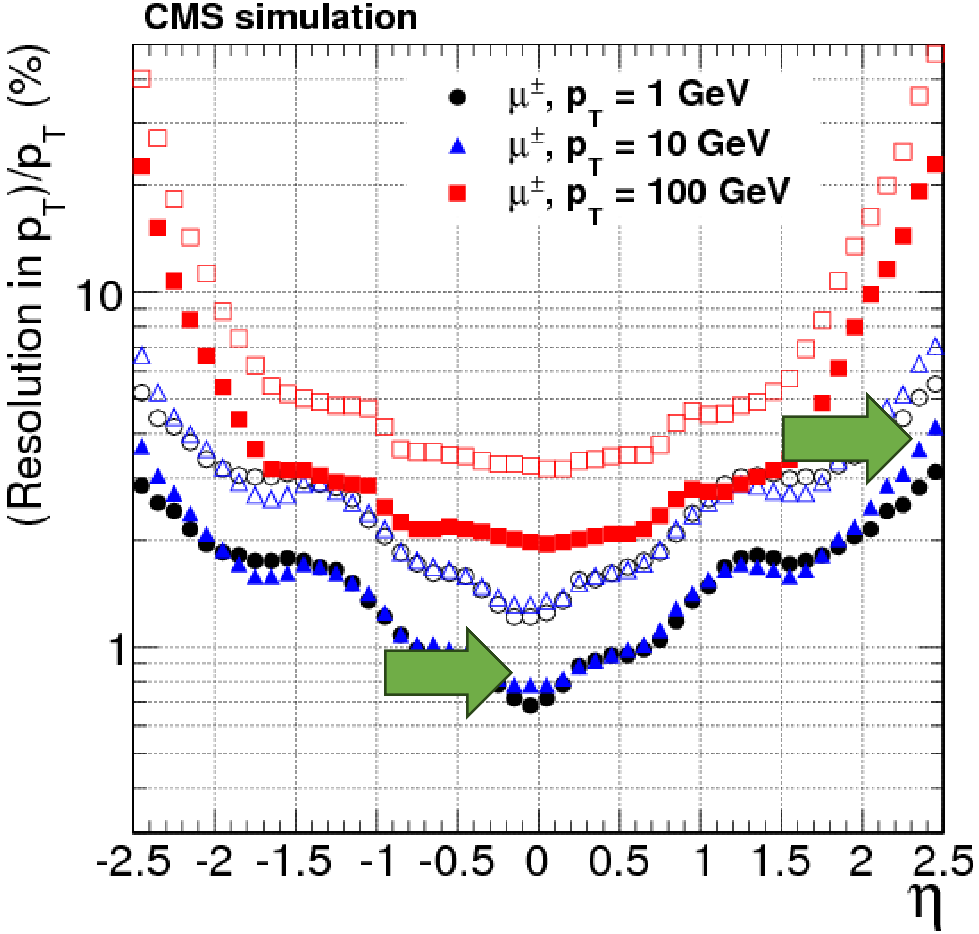
1) Build MC **templates** of $\frac{d\sigma}{dp_T^{\ell}}(p_T^{\ell} \mid \boldsymbol{m_W})$

2) Find $\hat{\boldsymbol{m}}_{\boldsymbol{W}}$ that **best fits** to the data

The CMS tracker



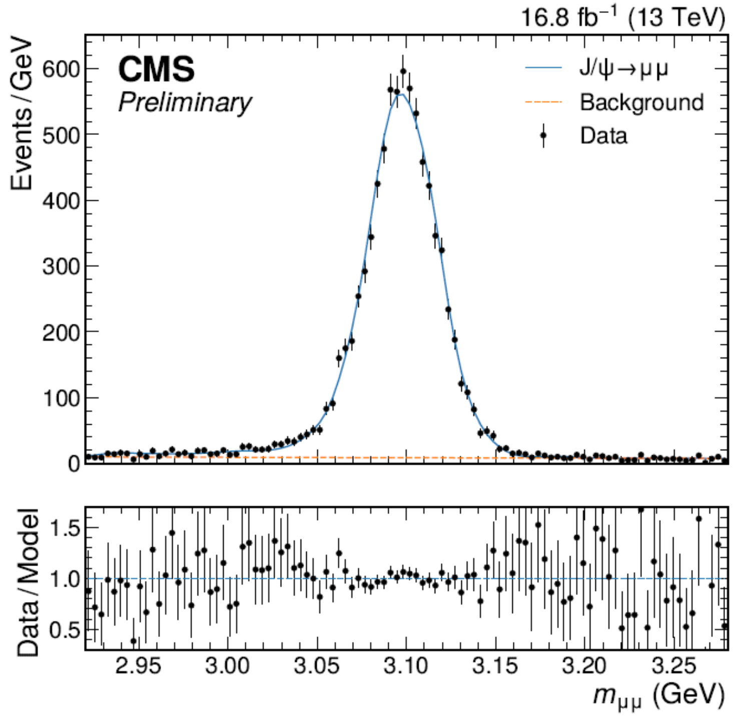
JINST 9 (2014) P10009



- Fully silicon-based
- Up to 17 points per track ($9 \div 50\ \mu m$ resolutions)
- Up to **2 radiation lengths**
  - p_T^μ resolution from multiple scattering: $\mathbf{1} \div \mathbf{3}\%$

Muon momentum scale: workflow

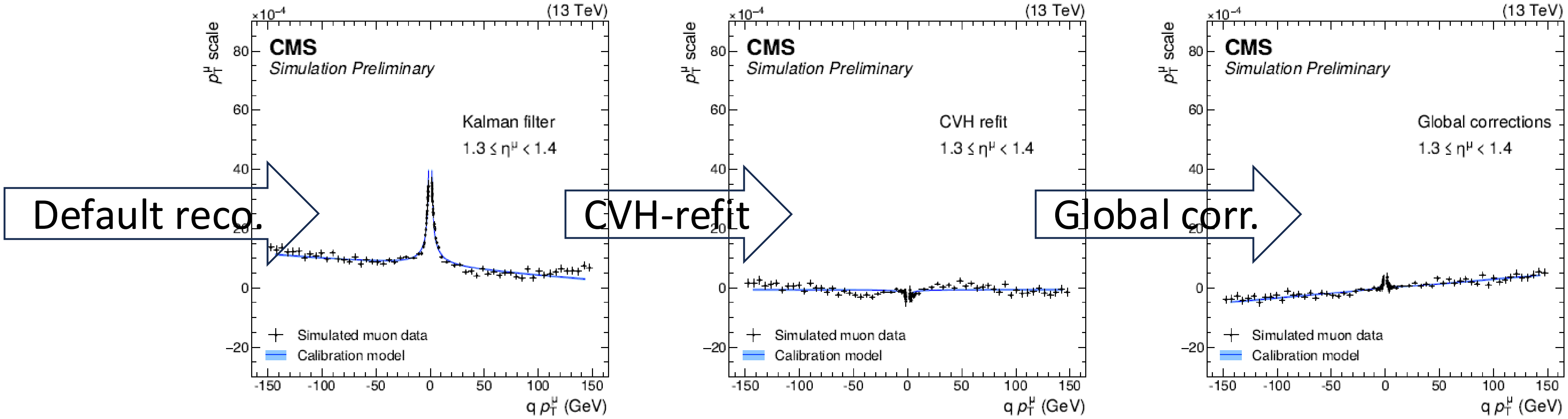
1. **Tuning** of parameters in CMS simulation.
2. **Track re-fit** with improved B-field/material treatment in track propagation.
3. **Module-level correction** of alignment, B-field, and material by minimizing $J/\Psi \rightarrow \mu\mu$ track residuals.
   - → Scale in ideal MC is **now unity** within a few 10^{-5}
   - → Residual mis-modeling can be **parametrized** as:



$$\left(\frac{\delta p_T}{p_T}\right)_{\pm} = A_{i\eta} - \frac{\varepsilon_{i\eta}}{p_T} \pm M_{i\eta} p_T$$

4. $(A_{i\eta}, \varepsilon_{i\eta}, M_{i\eta})$ from likelihood fits to $\mathbf{J/\Psi}$ **mass** binned in $(p_T^+, \eta^+, p_T^-, \eta^-)$

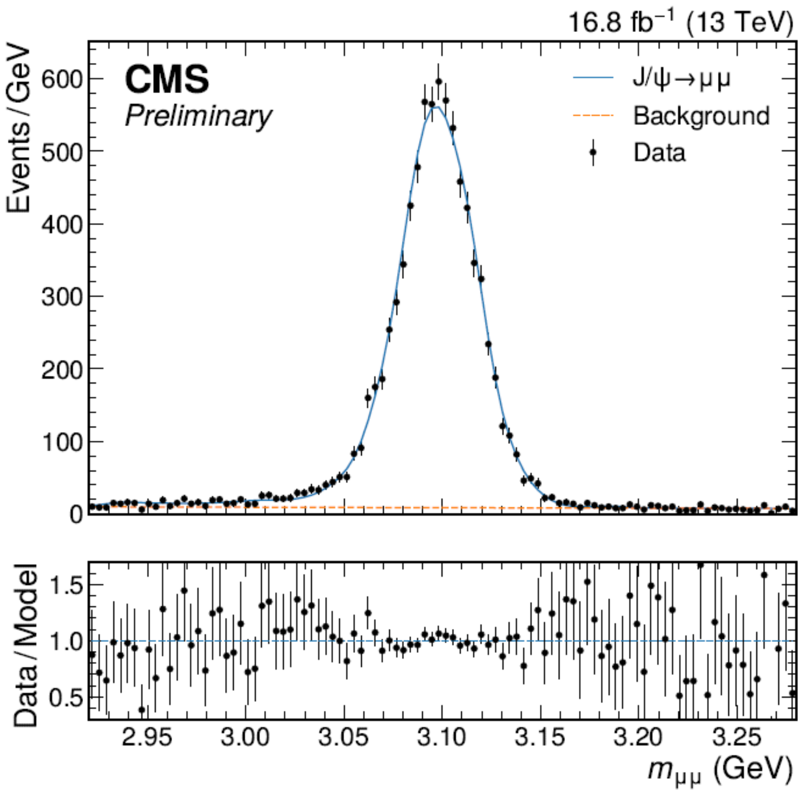
Muon momentum scale



Muon momentum scale

4. **Removal of residual data/MC scale bias** using J/Ψ events in a fine-grained 4D space $(p_T^+, \eta^+, p_T^-, \eta^-)$

$O(10{,}000)$
Mass spectra



- Fit a **scale shift $\boldsymbol{\Sigma}$** in each 4D bin
- Finally, do a χ^2 fit of $(A_\eta, \varepsilon_\eta, M_\eta)$ from all bins

$$\sum_{ijkl} \frac{\left(\Sigma_{ijkl}^2 - \left(A_j - \frac{\varepsilon_j}{p_{T,i}} + M_j p_{T,i}\right)\left(A_l - \frac{\varepsilon_l}{p_{T,k}} + M_l p_{T,k}\right)\right)^2}{\mathrm{Var}\left[\Sigma_{ijkl}^2\right]}$$

Impact on m_W

Source of uncertainty	Nuisance parameters	Uncertainty in m_W (MeV)
J/ψ calibration stat. (scaled $\times 2.1$)	144	3.7
Z closure stat.	48	1.0
Z closure (LEP measurement)	1	1.7
Resolution stat. (scaled $\times 10$)	72	1.4
Pixel multiplicity	49	0.7
Total	314	4.8

PDF

- Fitting simultaneously eta_mu and yZ

PDF set	Nominal fit		Without PDF+α_s unc.		Without theory unc.	
	χ^2/ndf	p-val. (%)	χ^2/ndf	p-val. (%)	χ^2/ndf	p-val. (%)
CT18Z	100.7/116	84	125.3/116	26	103.8/116	78
CT18	100.7/116	84	153.2/116	1.0	105.7/116	74
PDF4LHC21	97.7/116	89	105.5/116	75	104.1/116	78
MSHT20	97.0/116	90	107.4/116	70	98.8/116	87
MSHT20aN3LO	99.0/116	87	122.8/116	31	101.9/116	82
NNPDF3.1	99.1/116	87	105.5/116	75	115.0/116	51
NNPDF4.0	99.7/116	86	104.3/116	77	116.7/116	46

Further checks

Configuration	$m_W^+ - m_W^-$ (MeV)	Δm_W (MeV)
nominal	57 ± 30	0
Alignment $\sim$1 sigma up	38 ± 30	< 0.1
LHE A_i as nominal	48 ± 30	-0.5
A_3 one sigma down	49 ± 30	0.4
Alignment and A_i shifted as above	21 ± 30	0.1
Alignment $\sim$ 3 sigma up	-5 ± 30	0.6

Configuration	Δm_W in MeV	Auxiliary parameter
$26 < p_T < 52$ GeV	-0.75 ± 10.03	—
$30 < p_T < 56$ GeV	-1.11 ± 11.05	—
$30 < p_T < 52$ GeV	-2.15 ± 11.17	—
W floating	-0.47 ± 9.98	$\mu_W = 0.979 \pm 0.026$
Alt. veto efficiency	0.05 ± 9.88	—
Hybrid smoothing	-1.58 ± 9.88	—
Charge difference	0.34 ± 9.89	$m_W^{diff.} = 56.96 \pm 30.30$ MeV
η sign difference	-0.01 ± 9.88	$m_W^{diff.} = 5.8 \pm 12.4$ MeV
$\lvert\eta\rvert$range difference	-0.61 ± 9.90	$m_W^{diff.} = 15.3 \pm 14.7$ MeV

Fit model

- m_W extracted from binned maximum-likelihood fit
  - Systematic uncertainties → **nuisance parameters (NP)** with Gaussian constraints
- RDataFrame → multi-dimensional Boost Histogram's
  - Nominal × **systematic variations**
- Likelihood calculation and minimization based on Tensorflow library

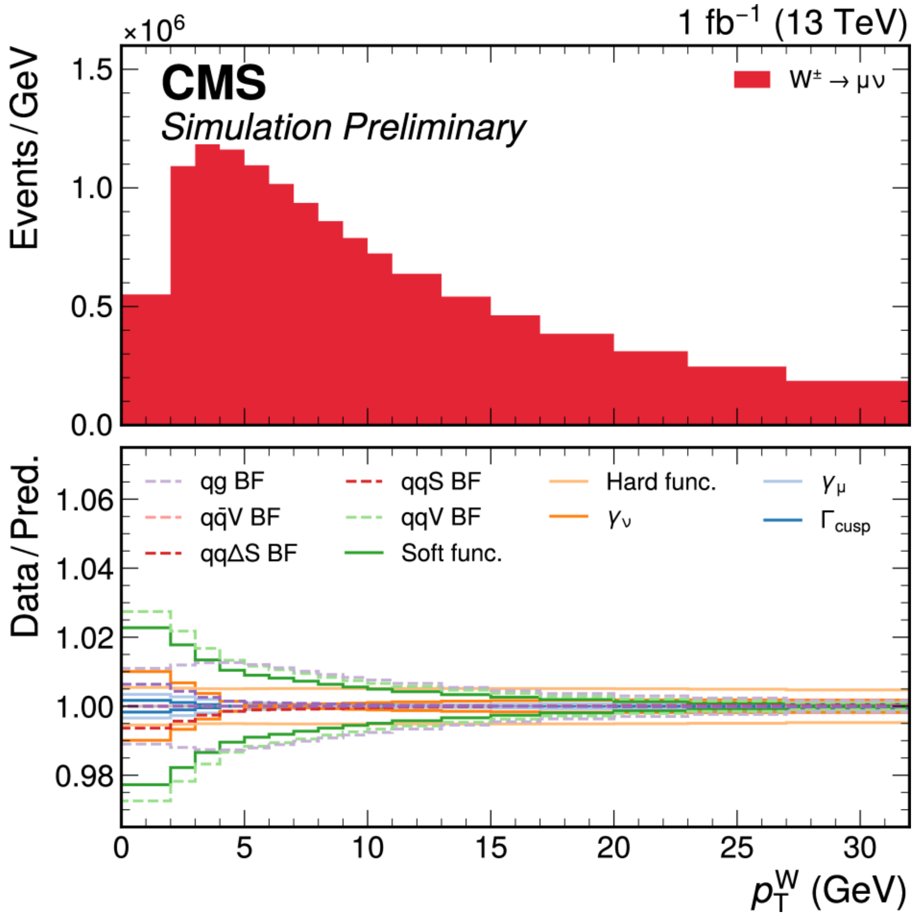
ROOT Data Analysis Framework → Boost Histogram → Tensorflow

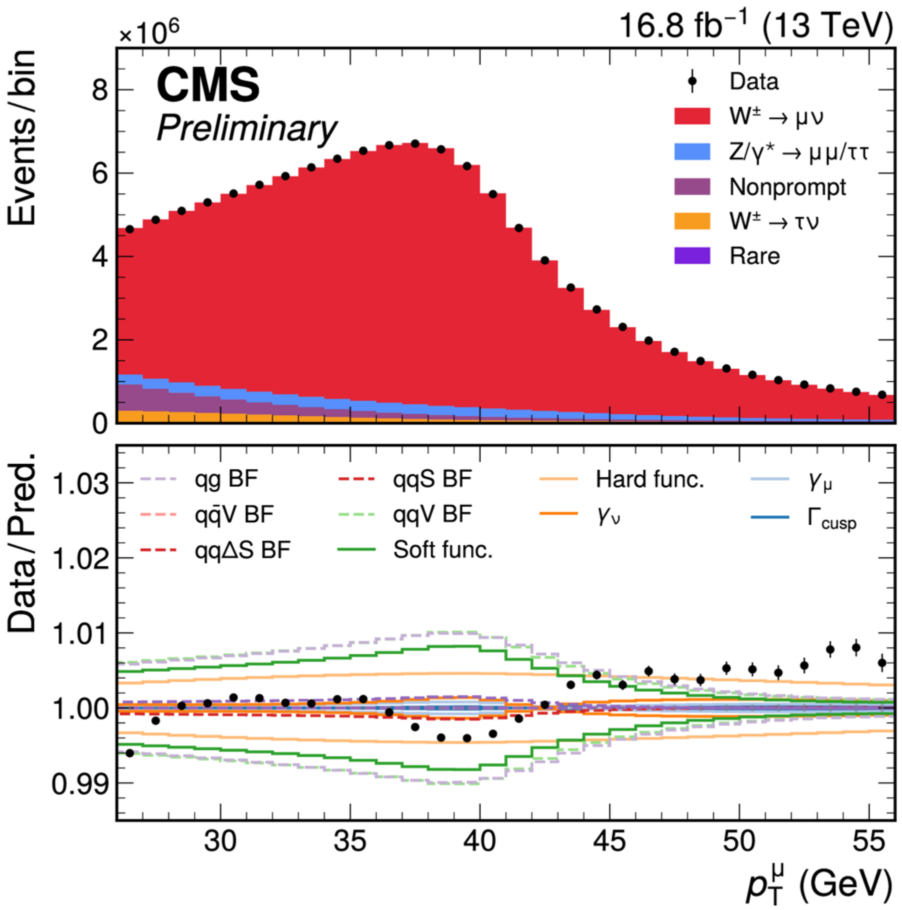
D. Walter's slides

<table>
<tr><th>Systematic uncertainties</th><th>W-like m_Z</th><th>m_W</th></tr>
<tr><td>Muon efficiency</td><td>3127</td><td>3658</td></tr>
<tr><td>Muon eff. veto</td><td>–</td><td>531</td></tr>
<tr><td>Muon eff. syst.</td><td colspan="2">343</td></tr>
<tr><td>Muon eff. stat.</td><td colspan="2">2784</td></tr>
<tr><td>Nonprompt background</td><td>–</td><td>387</td></tr>
<tr><td>Prompt background</td><td>2</td><td>3</td></tr>
<tr><td>Muon momentum scale</td><td colspan="2">338</td></tr>
<tr><td>L1 prefire</td><td colspan="2">14</td></tr>
<tr><td>Luminosity</td><td colspan="2">1</td></tr>
<tr><td>PDF (CT18Z)</td><td colspan="2">60</td></tr>
<tr><td>Angular coefficients</td><td>177</td><td>353</td></tr>
<tr><td>W MiNNLO$_{PS}$ μ_F, μ_R</td><td>–</td><td>176</td></tr>
<tr><td>Z MiNNLO$_{PS}$ μ_F, μ_R</td><td colspan="2">176</td></tr>
<tr><td>PYTHIA shower k_T</td><td colspan="2">1</td></tr>
<tr><td>p_T^V modeling</td><td>22</td><td>32</td></tr>
<tr><td>Nonperturbative</td><td>4</td><td>10</td></tr>
<tr><td>Perturbative</td><td>4</td><td>8</td></tr>
<tr><td>Theory nuisance parameters</td><td colspan="2">10</td></tr>
<tr><td>c, b quark mass</td><td colspan="2">4</td></tr>
<tr><td>Higher-order EW</td><td>6</td><td>7</td></tr>
<tr><td>Z width</td><td colspan="2">1</td></tr>
<tr><td>Z mass</td><td colspan="2">1</td></tr>
<tr><td>W width</td><td>–</td><td>1</td></tr>
<tr><td>W mass</td><td>–</td><td>1</td></tr>
<tr><td>$\sin^2 \theta_W$</td><td colspan="2">1</td></tr>
<tr><td>Total</td><td>3750</td><td>4859</td></tr>
</table>

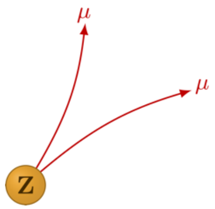
TNP

F. Tackman's slides

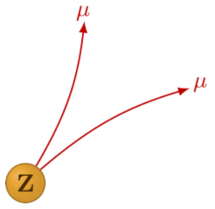




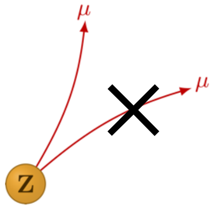
W-like: p_T^Z modeling



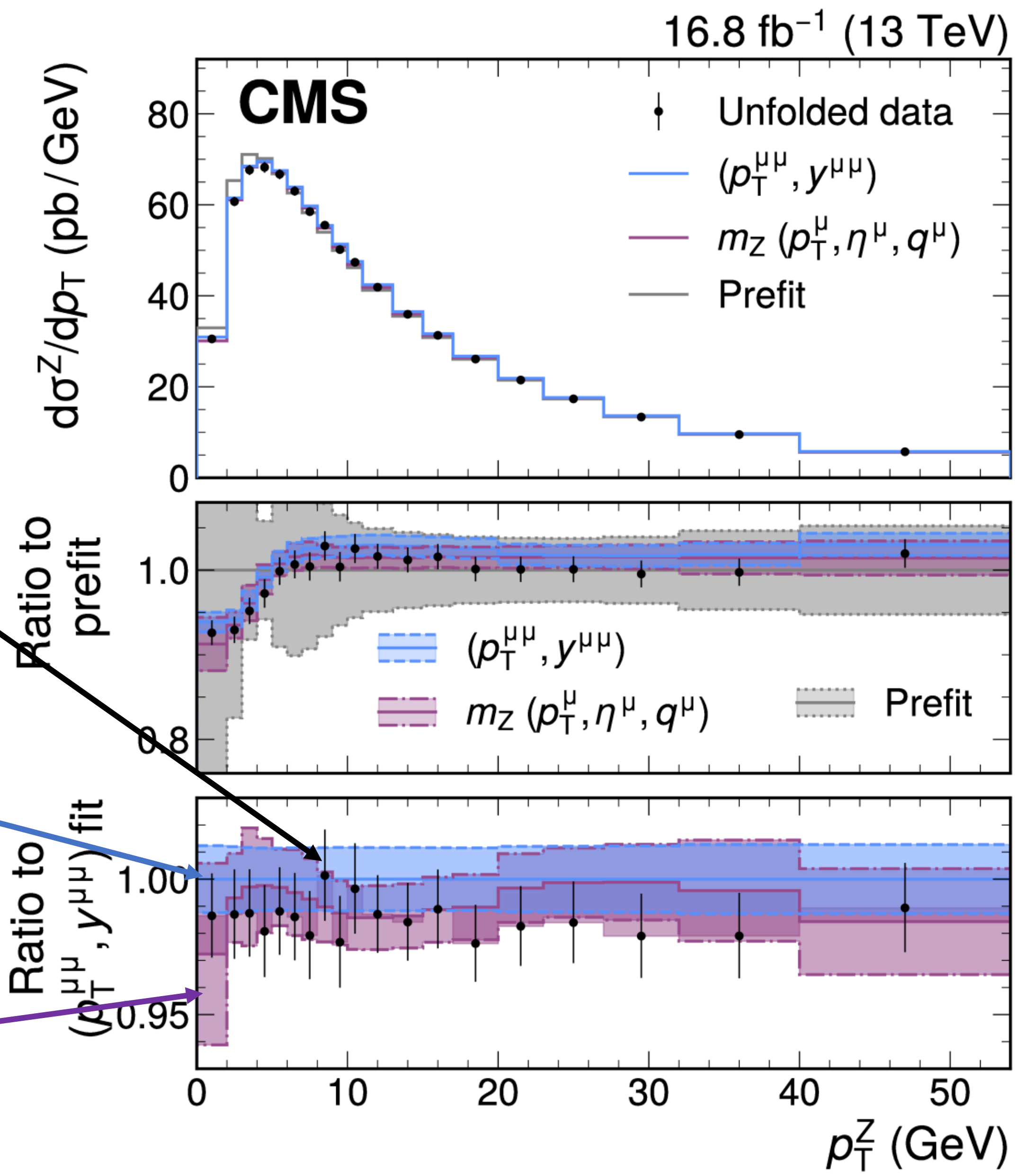
$$f_{\text{unfold}} = U^{-1}_{\text{reco|gen}}\, f_{\text{reco}}$$



$$f_{\text{model}}(p_T^Z \mid \theta_{(p_T^{\mu\mu}, y^{\mu\mu})})$$



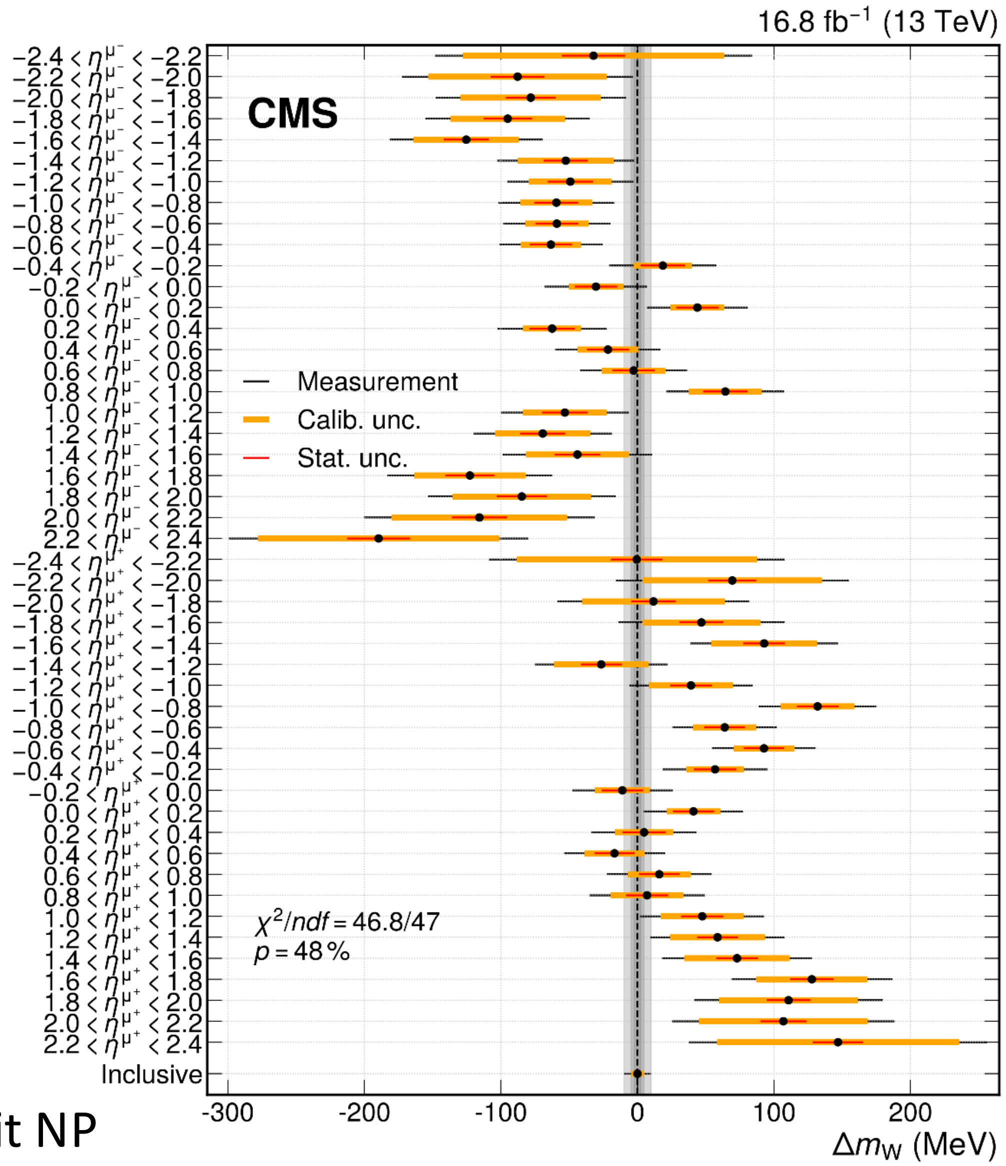
$$f_{\text{model}}(p_T^Z \mid \theta_{(q^{\mu}, p_T^{\mu}, \eta^{\mu})})$$



Charge asymmetry

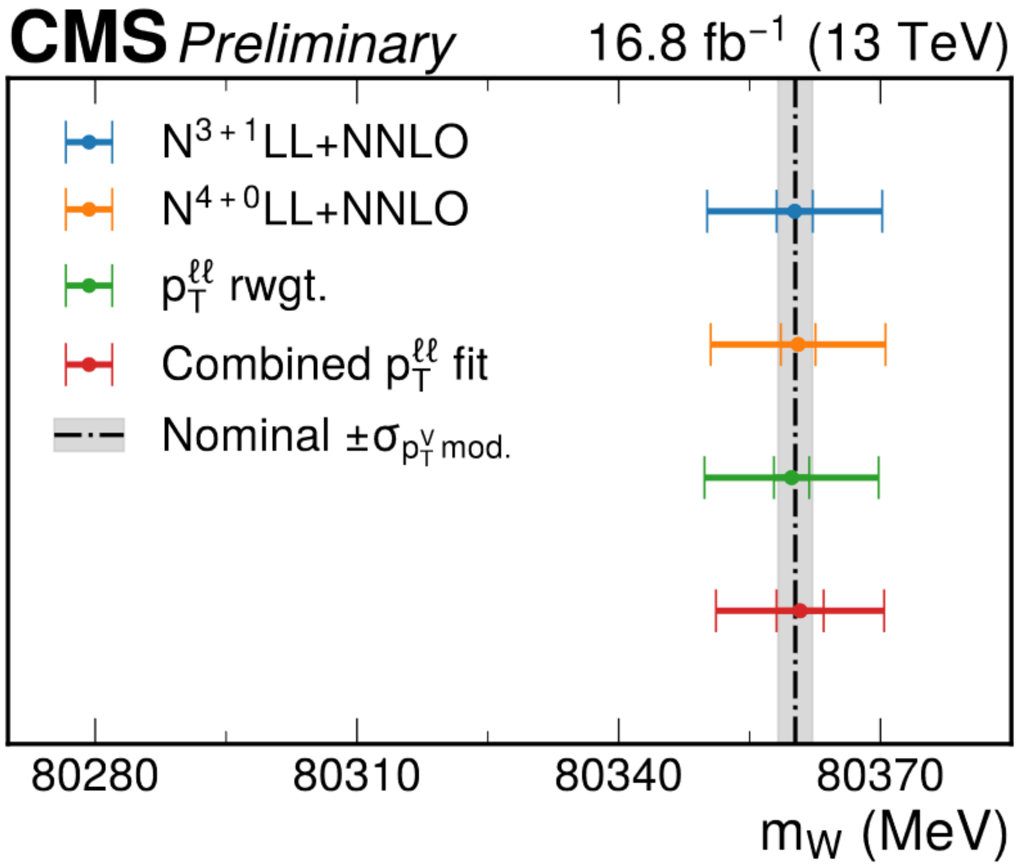
- $m_{W^+} - m_{W^-} = 57 \pm 30$ MeV
  - p-value = 6%

Source of uncertainty	Global impact (MeV)			
	in $m_{Z^+} - m_{Z^-}$	in m_Z	in $m_{W^+} - m_{W^-}$	in m_W
Muon momentum scale	21.2	5.3	20.0	4.4
Muon reco. efficiency	6.5	3.0	5.8	2.3
W and Z angular coeffs.	13.9	4.5	13.7	3.0
Higher-order EW	0.2	2.2	1.5	1.9
p_T^V modeling	0.4	1.0	2.7	0.8
PDF	0.7	1.9	4.2	2.8
Nonprompt background	–	–	4.8	1.7
Integrated luminosity	< 0.1	0.2	0.1	0.1
MC sample size	6.4	3.6	8.4	3.8
Data sample size	18.1	10.1	13.4	6.0
Total uncertainty	32.5	13.5	30.3	9.9

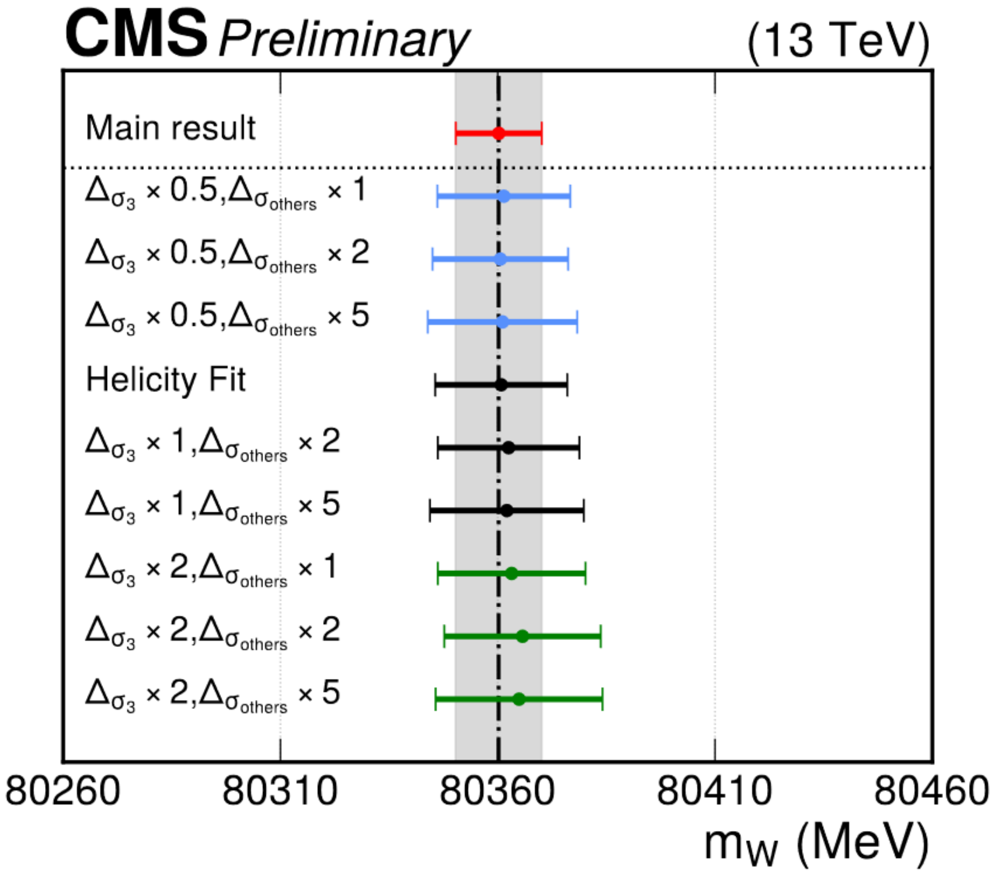


- Likely, a combination of alignment/theory nuisances consistently pulled by $\sim 1\sigma$
  - no significant shift in m_W even for generous shifts of pre-fit NP

Test of model dependence

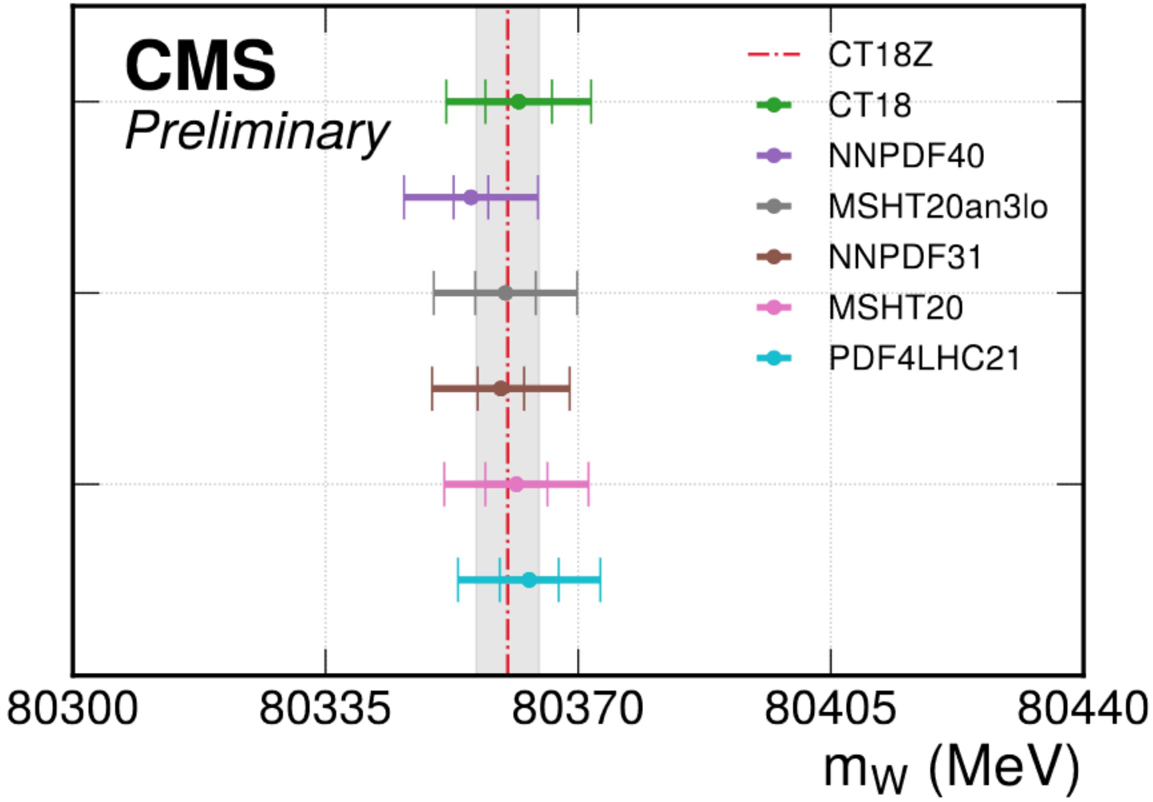


Different p_T^V uncertainty models



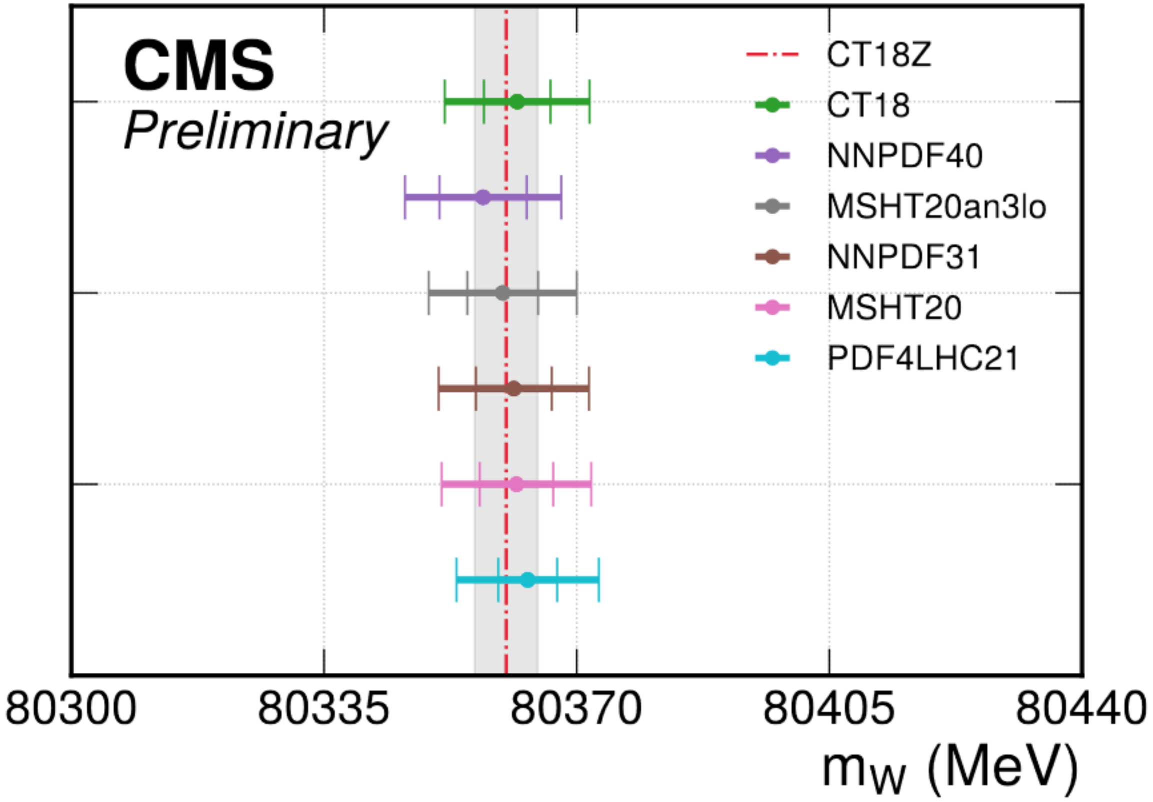
"Helicity fit": loose priors on $\sigma_{\mathrm{UL},0,..,4}$

PDF dependence



WITHOUT INFLATION

Spread of central values within the uncertainty of **nominal PDF set**



WITH INFLATION

Spread of central values within the uncertainty of **any PDF sets**

Comparison w/ ATLAS & CDF-II

- To enable one-to-one comparison with ATLAS, use ”global” impacts

arXiv:2307.04007

Unc. [MeV]	Total	Stat.	Syst.	PDF	A_i	Backg.	EW	e	μ	u_T	Lumi	Γ_W	PS
p_T^ℓ	16.2	11.1	11.8	4.9	3.5	1.7	5.6	5.9	5.4	0.9	1.1	0.1	1.5

Source of uncertainty	Impact (MeV) Nominal		Global	
	in m_Z	in m_W	in m_Z	in m_W
Muon momentum scale	5.6	4.8	5.3	4.4
Muon reco. efficiency	3.8	3.0	3.0	2.3
W and Z angular coeffs.	4.9	3.3	4.5	3.0
Higher-order EW	2.2	2.0	2.2	1.9
p_T^V modeling	1.7	2.0	1.0	0.8
PDF	2.4	4.4	1.9	2.8
Nonprompt background	–	3.2	–	1.7
Integrated luminosity	0.3	0.1	0.2	0.1
MC sample size	2.5	1.5	3.6	3.8
Data sample size	6.9	2.4	10.1	6.0
Total uncertainty	13.5	9.9	13.5	9.9

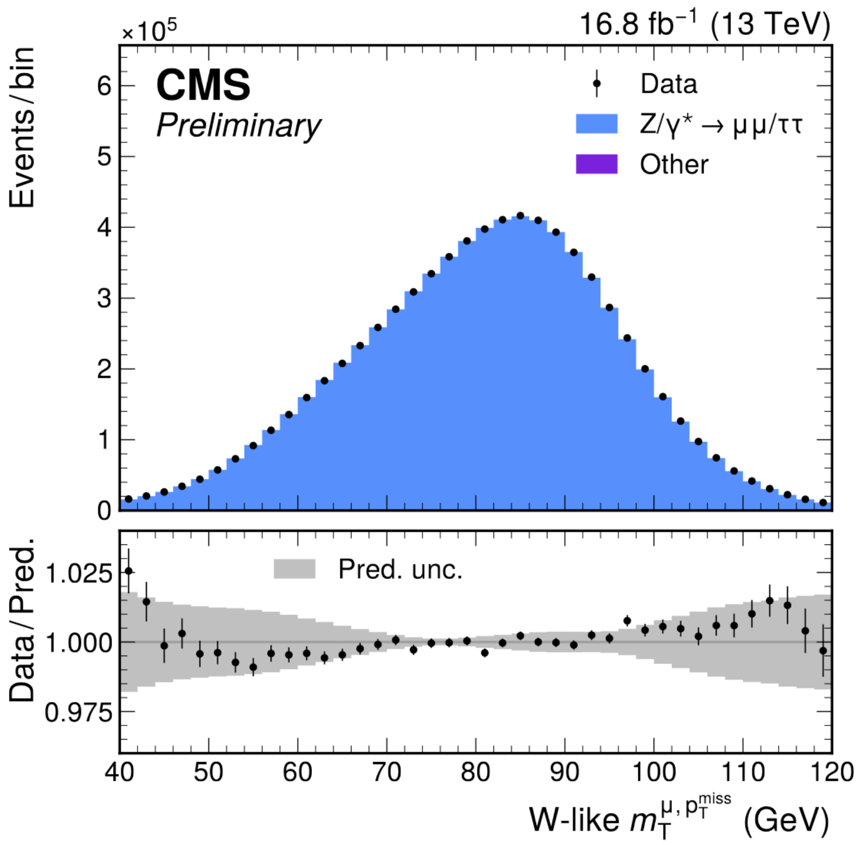
Source	Uncertainty (MeV)
Lepton energy scale	3.0
Lepton energy resolution	1.2
Recoil energy scale	1.2
Recoil energy resolution	1.8
Lepton efficiency	0.4
Lepton removal	1.2
Backgrounds	3.3
p_T^Z model	1.8
p_T^W/p_T^Z model	1.3
Parton distributions	3.9
QED radiation	2.7
W boson statistics	6.4
Total	9.4

arXiv:2403.15085

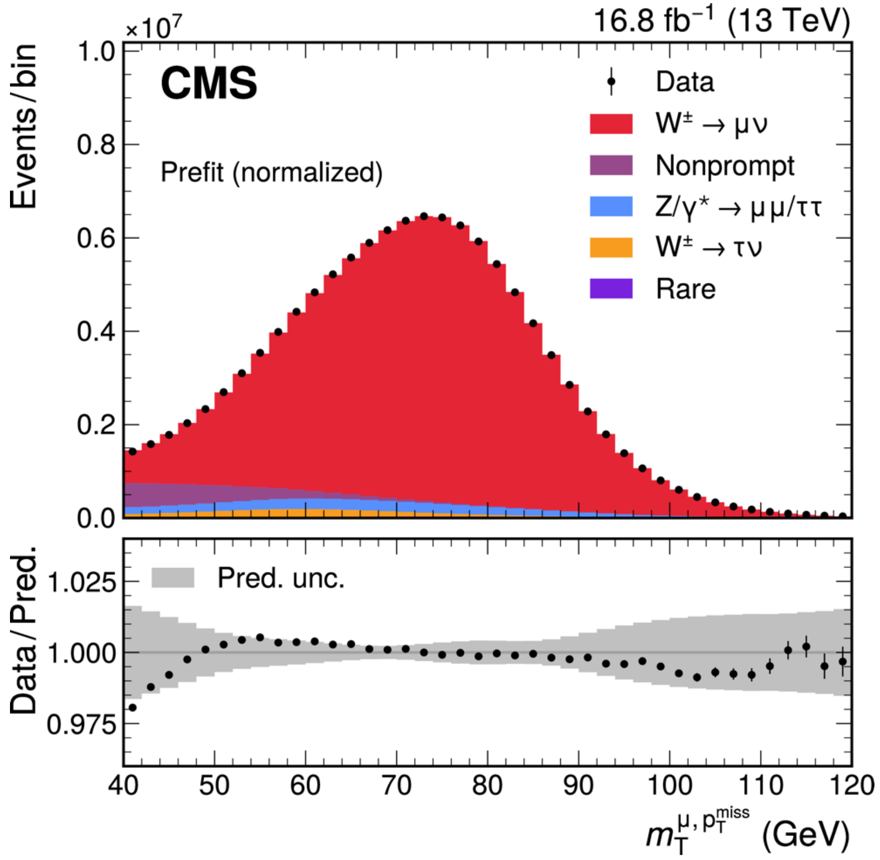
CMS-PAS-SMP-23-002

Science 376 (2022) 6589

Recoil



16.8 fb⁻¹ (13 TeV)
×10⁵
CMS
Preliminary
Data
Z/γ* → μμ/ττ
Other
Events/bin
Pred. unc.
Data/Pred.
W-like $m_T^{\mu, p_T^{miss}}$ (GeV)



16.8 fb⁻¹ (13 TeV)
×10⁷
CMS
Prefit (normalized)
Data
W± → μν
Nonprompt
Z/γ* → μμ/ττ
W± → τν
Rare
Events/bin
Pred. unc.
Data/Pred.
$m_T^{\mu, p_T^{miss}}$ (GeV)