### **Theory Ouverture**

# Federico Mescia

Beyond the Flavour Anomalies, April 9th, 2025

### **Theory Ouverture**

- Where do we stand?!"
- **Recent developments in flavour observables:**

 $\blacktriangleright$   $R_D - R_{D^*}$ ,  $B \rightarrow K^{(*)} \mu \mu$ , and news from  $B \rightarrow K_{VV}$  &  $K \rightarrow \pi_{VV}$ 

- What next?!
  - HL-LHC (0.3 ab<sup>-1</sup><sub>LHCb</sub>), Belle II-Upgrade … HE-LHC (27 TeV)?
  - Models of Flavour: MFV, U(2)<sup>5</sup>, Rank-1-FV and interplay with DM

### Beyond the Flavour Anomalies, April 9th, 2025

**Introduction:** Where do we stand?!

- 1. The Higgs boson has been found
  - $\rightarrow$  the SM is a d=4 renormalizable QFT
- 2. The Higgs boson is light

 $\rightarrow m_{\rm h} \sim 125 \text{ GeV} \rightarrow \text{not the heaviest SM particle}$ 

3. There is a "mass-gap" above the SM spectrum

→ no unambiguous sign of NP up to ~ 1 TeV  $\otimes$ → no clear UV cut-off where the SM fails



### Persisting pessimism...





Elegant beautiful

 $\vec{\nabla}\cdot\vec{D}=\rho$  $\vec{\nabla}\cdot\vec{B}=0$  $\vec{\nabla}\times\vec{H}=\vec{\jmath}+\frac{\partial\vec{D}}{\partial t}$  $\partial \vec{B}$  $\vec{\nabla} \times \vec{E} = \partial t$ 9. Cled Theawell

Everything is clear

Interactions are unified

nothing up to the Gravity scale

✤ adapted from G. Isidori





but not complete

e

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γ

 $e_L e_R$ 

#### Awful – che casino!



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#### Many open questions:

- ✤ All SM problems are still there
- Experimental issues:
- Baryon Asymmetry→CPV
- Neutrino Masses
- Dark Matter
- (Gravity)

- Theoretical puzzles:
- Hierarchy Problem
- Flavour Puzzle
- 3 Families
- Strong CP problem
- GUT

- Strong motivation to pursue search of New Physics at broad spectrum of energy
- Atlas/CMS/LHCb/BelleII/NA62 /BESIII/Mu2e...

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# Direct vs indirect searches?

# Let's go and discover



#### **Direct Searches for New Physics**

- Searches for new particles in the spectrum
- Direct information on the mass of NP



m<sub>ee</sub> [GeV]

# Limited by the available energy of the collider HE-LHC 2040?

### **Indirect Searches for New Physics**

#### FLAVOUR PHYSICS AS A DISCOVERY TOOL OF NEW PARTICLES

- for heavy  $M_X$ 

New particles can be detected through loops of low-energy processes



 $M_X > M_B$ : indirect probe of high-energy scale

### **Flavour Physics: window to New Physics**

Compare high-statistics measurements to high-precision SM predictions to search for the quantum effects of new particles



New intensity frontier opens up soon thanks to HL-LHC (Belle-II and BES-III upgrades)

### **Flavour Physics: window to New Physics**

For heavy  $M_{NP}$ 



★  $c_{SM} \approx 0$  enhanced sensitivities to New Particles in rare hadron transitions, for example **b** → **s II** processes at LHCb

Specific advantage at HL-LHC: huge increase in statistics

HL-LHC (NA62, KOTO, BES-III, Belle-II) good opportunity of improvement in flavor physics, covering unexplored regions of realistic NP models

### **Flavour Physics: window to New Physics**

For heavy  $M_{NP}$ 



↔  $c_{SM} \approx 0$  enhanced sensitivities to New Particles in rare hadron transitions, for example **b** → **s II** processes at LHCb

Specific advantage at HL-LHC: huge increase in statistics





Courtesy of O. Sumensari

For heavy 
$$M_{NP} = \Lambda$$
  
 $\mathcal{L}_{eff} = \mathcal{L}_{SM} + \frac{\mathcal{C}^{(5)}}{\Lambda_L} \mathcal{O}^{(5)} + \sum_i \frac{\mathcal{C}^{(6)}_i}{\Lambda^2} \mathcal{O}^{(6)}_i + \dots$ 



#### **CKM Unitarity test:** Discrepancies in 1<sup>st</sup> row/column of CKM matrix

- Deficit of first row CKM unitarity
- Tension between V<sub>us</sub> from K<sub>13</sub>
   vs K<sub>12</sub>

Both theory and experiments demands a closer scrutiny of systematic errors



$$|V_{ud}^2| + |V_{us}^2| + |V_{ub}^2| = 0.9985 \pm 0.0005,^*$$

 $|V_{ud}^2| + |V_{cd}^2| + |V_{td}^2| = 0.9970 \pm 0.0018^*$ 

see talk by S.Simula on Thursday for last updates.

- Deficit of first row CKM unitarity
- Tension between V<sub>us</sub> from K<sub>13</sub>
   vs K<sub>12</sub>
- Experiment: information to be improved

 $\left|V_{ud}^{2}\right| + \left|V_{us}^{2}\right| + \left|V_{ub}^{2}\right| = 0.9985 \pm 0.0005,$ 

# Systematic problems in $\beta$ decays measurements?



\*  $V_{ud}$ : exp. Info unclear

 Tension in neutron lifetime between beam vs bottle method (≈ 4σ)

- Deficit of first row CKM unitarity
- Tension between V<sub>us</sub> from K<sub>13</sub>
   vs K<sub>12</sub>
- Theory: radiative corrections on super-allowed β and K decays?

#### *V<sub>us</sub>*: great progress in controlling radiative corrections from Lattice QCD

- > Problem solved for  $K_{12\gamma}$  and correctly match with exp. cuts.
- >  $K_{I3}$  small phase space: soft photon from  $K_{I3\gamma}$  important for high-precision test. Lattice calculation missing!
- V<sub>ud</sub>: radiative corrections on superallowed β need further revision

Gagliardi, Garofalo, Giusti, Frezzotti, Lubicz, Martinelli, Sachrajda, Tantalo, Tarantino, Sanfilippo, Simula, 2202.03833 ..





- Deficit of first row CKM unitarity
- Tension between V<sub>us</sub> from K<sub>13</sub>
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- Experiment/Theory information to be improved
- NP example: Vector-like quarks by modified coupling to W





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$$|V_{ud}^2| + |V_{us}^2| + |V_{ub}^2| = 0.9985 \pm 0.0005,^*$$

#### M. Kirk et al. 2212.06862.

see talk by Simula on Thursday for last updates.



Some tensions between EW fit and determination of the Fermi constant

\* smallish changes from the last improvement of  $M_{W}$ , see HEPfit for EWPT

#### Unitarity Triangle results over the years (3rd family)





- CKM triangle well know now
- Huge progress thanks to Bfactories and Lattice QCD
- First step towards highprecision flavour physics
- Thanks to this improvement, we can look for NP in rare B and K decays

#### $R(D) \& R(D^*)$ Puzzle



- Discrepancy currently standing at ~ 3.1σ for the combined R(D) & R(D\*);
- Test of lepton flavour universality between heavy T leptons versus light e, µ leptons
- Clear signature of BSM couplings with the 3<sup>rd</sup> generation



Long-standing discrepancies started from BaBar, Belle, then recently LHCb

#### $R(D) \& R(D^*)$ news from Belle II



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Long-standing discrepancies started from BaBar, Belle, then recently LHCb and now seems confirmed by Belle II

### $R(D) \& R(D^*)$ theory



- Recently, developments in refining SM predictions (see talks by M.
   Bordone, M. Fedele, L. Vittorio)
- ★ Lattice QCD results for B→D form factors are satisfactory ☺
- Instead for B→D\* the situation is confusing: results with staggered do not agree with those obtained with Wilson discretization: (see talk by A. Juttner)
  - A lot of activities will be reported at this workshop
- New Physics by tree-level exchange of W', LQ, ...

 $\frac{\Lambda_{NP}}{g_{NP}} = a \text{ few TeV}$ 

 $\int \mathcal{L} dt = 365 fb^{-1}$ Moriond 2025 0.45 Belle II had, tag + SM [2-8] 2024 [22] This work 39.3% CI SM exp.  $\mathcal{R}(X_{\tau/l})$ This work 68.3% CI --- Belle II had. R(X<sub>t/l</sub>) [23] 0.40 World average HFLAV 2024 [24] 0.35 R(D\*) 20.30 0.25 0.20 0.20 0.25 0.30 0.35 0.40 0.45 0.50 0.55  $\mathcal{R}(D)$ 

Di Luzio & Nardecchia, 1706.01868

 $B \rightarrow K^{(*)} \mu \mu \& B_s \rightarrow \phi \mu \mu$ 

- 4σ deficit in Br using LCSR
   helped by Lattice QCD\*
- Test of NP in angular observables, P'<sub>5</sub>?

#### see talk by Quim Matias







Br's ~ 20% below the SM expectations!!?

♦  $B_s \rightarrow \mu\mu$  is now SM-like, C<sub>10</sub>~0

•  $R_{K}, R_{K^*} \& R_{\phi} \sim 1$  toward LFU NP

Good fit with

 $C_{9}^{U}$  $C_{9}^{U}, C_{10}^{U}$ 



# Global fit pointing to $5\sigma$ or $7\sigma$ deviation w.r.t the SM, depending on the choice of hadronic input.

#### Capdevila, Crivellin and Matias, 2309.01311

Gubernari, Reboud, van Dyk, Virto, 2206.03797 Hurth, Mahmoudi and Neshatpour 2310.05585

♦  $B_s \rightarrow \mu\mu$  is now SM-like, C<sub>10</sub>~0

- ♦  $R_{K}, R_{K^*} \& R_{\phi} \sim 1$  toward LFU NP
- Good fit with

#### **Open question:**

Local or non-local hadronic matrix elements (charm-loops)

local matrix elements
 have not been computed
 on lattice recently:
 heavily dominated by
 LCSR. ?!

#### Hadronic inputs - hot issues for discussions at all workshops



♦  $B_s \rightarrow \mu\mu$  is now SM-like, C<sub>10</sub>~0

•  $R_{K}, R_{K^*} \& R_{\phi} \sim 1$  toward LFU NP

Good fit with

**Open question:** charm-loops?

# Hadronic inputs - hot issues for discussions at all workshops



$$\frac{h_{\lambda}}{m^2}(q^2) = \frac{\epsilon^*_{\mu}(\lambda)}{m^2_B} \int d^4x e^{iqx} \langle \bar{K}^* | T\{j^{\mu}_{\rm em}(x) \mathcal{H}^{\rm had}_{\rm eff}(0)\} | \bar{B} \rangle$$



see talk by A. Tinari

# Hadronic inputs - hot issues for discussions at all workshops

- ♦  $B_s \rightarrow \mu\mu$  is now SM-like, C<sub>10</sub>~0
- $R_{K}, R_{K^*} \& R_{\phi} \sim 1$  toward LFU NP
- Good fit with
- **Open question:** charm-loops?
- M. Ciuchini, M. Fedele, E. Franco, M. Valli, L. Silvestrini, 2212.10516

$$\begin{split} H_V^- \propto & \frac{m_B^2}{q^2} \left[ \frac{2m_b}{m_B} \left( C_7^{\rm SM} + h_-^{(0)} \right) \widetilde{T}_{L-} - 16\pi^2 h_-^{(2)} q^4 \right] \\ &+ \left( C_9^{\rm SM} + h_-^{(1)} \right) \widetilde{V}_{L-} \,, \end{split}$$





#### Looking for complementary $b \rightarrow s$ modes

$$B_s \rightarrow \mu^+ \mu^- \gamma$$
 at large  $q^2$  from lattice QCD

#### Breakthrough from Lattice QCD

Frezzotti, Gagliardi, Lubicz, Martinelli, Sachrajda, Sanfilippo, Simula, Tantalo 2402.03262





#### G. GAGLIARDI

 Comparison with current LHCb upper-bound for  $x_{\gamma}^{cut} \sim 0.166$ .

  $\mathcal{B}_{SD}^{LHCb}(0.166) < 2 \times 10^{-9}$ ,
  $\mathcal{B}_{SD}(0.166) = 6.9(9) \times 10^{-11}$ 

 $B_s \rightarrow \mu\mu\gamma$  @ high-q2: same short-distance effects as those in  $B \rightarrow K^{(*)} \ell\ell$ but long-distance contributions are expected to be rather small

#### Looking for complementary $b \rightarrow s$ modes

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 $\mathcal{B}_{SD}^{LHCb}(0.166) < 2 \times 10^{-9}$ ,  $\mathcal{B}_{SD}(0.166) = 6.9(9) \times 10^{-11}$ 

Is there a way to use the Hansen-Lupo-Tantalo method to estimate the contribution of cc to C<sub>9</sub>? (see talk by C. Sacrajada, G. Gagliardi)

#### see talk by L. Allwicher

• First experimental evidence of  $B \rightarrow K \nu \nu!$ 

 $B \rightarrow K^{(*)} \nu \nu$  from Belle II

- extremely theoretically clean probe of BSM:
  - they are significantly suppressed in SM
  - Iong-distance contributions are generally sub-leading



#### 1. NP assumed to be heavy



$$\mathcal{L}_{\rm LEFT}^{\rm NP} = \sum_{ij\alpha\beta} \left[ L_L^{ij\alpha\beta} (\bar{d}_L^i \gamma_\mu d_L^j) (\bar{\nu}_L^\alpha \gamma^\mu \nu_L^\beta) + L_R^{ij\alpha\beta} (\bar{d}_R^i \gamma_\mu d_R^j) (\bar{\nu}_L^\alpha \gamma^\mu \nu_L^\beta) \right]$$



Marzocca, Nardecchia, Toni, Stanzione 2404.06533 **Allwicher**, Becirevic, Piazza, Sumensari 2309.02246 Becirevic, Fajfer, Kosnik, Pavicic 2419.23257 **Allwicher**, Becirevic, Piazza, Sumensari 2309.02246 Allwicher, Bordone, Isidori, Piazza and Stanzione, 2410.21444



- First experimental evidence of  $B \rightarrow K \nu \nu!$
- extremely theoretically clean probe of BSM:
  - they are significantly suppressed in SM
  - long-distance contributions are generally sub-leading

#### 2. NP assumed to be light

hint of new invisible particles: fermions or bosons

 $B \rightarrow K E_{\text{miss}}$ 

 $10^5 \times \text{Br}(B^+ \rightarrow K^+ \nu \bar{\nu})$ 



Bolton, Fajfer, Kamenik, Novoa-Brunet 2503.19025 Altmannshofer et al. '23

Good fit to Belle-II data too, since the excess is mostly localized

> m<sub>ψ</sub>~ 0.6 GeV m<sub>v/φ</sub>~ 2.1 GeV



$$\frac{\mathcal{B}(K^+ \to \pi^+ \nu \bar{\nu})_{exp}}{\mathcal{B}(K^+ \to \pi^+ \nu \bar{\nu})_{SM}} = 1.65 + 0.30$$

$$M652$$
Solution between the SM at 1.7 or

Compatible v

- theoretically clean ۲
- significant improvements expected in the next years: Belle II will measure  $B \to K \nu \bar{\nu}$  @ 10%, and NA62  $K \to \pi \nu \bar{\nu}$  @ 15%
- sensitive to a limited number of EFT operators:  $C_{\ell a}^{(3)[3333]}$ ,  $C_{\ell a}^{(1)[3333]}$
- the present central values exceed the corresponding SM predictions
- Sensitive to 3<sup>rd</sup> generation NP ٠

Allwicher, Bordone, Isidori, Piazza and Stanzione, 2410.21444



#### HL-LHC tasks: Is there a hierarchy of NP flavour?

With O(1) NP couplings, bounds on **flavour-violating** operators point to **huge scales higher than 10<sup>4</sup> TeV** 

However, hierarchical structures are already present in the SM

 $c_{ij} = 1$  is unnatural due to  $Y_u$  and  $Y_d$ 

With SM inspired assumptions about the NP flavour structure (Λ<10 TeV) MFV vs U(2)<sup>5</sup> vs Rank-1 FV?

 $\Lambda \sim 10 \text{ TeV}, \quad \Lambda \sim 1 \text{ TeV}, \quad \Lambda \sim 1\text{--}10 \text{ TeV}$ 



### MFV vs U(2)<sup>5</sup> vs Rank-1 FV?

Flavour could just be an accidental symmetry from more fundamental interactions: nothing forbids it to be badly violated in the UV.

I. MFV= U(3)<sup>5</sup> flavour breaking

*Flavour violations* =  $a Y_{1=2=3}$ 

D'Ambrosio, Giudice, Isidori, Strumia, hep-ph/0207036

Glioti, Rattazzi, Ricci and Vecchi, 2402.09503.

> one d.o.f
 > Λ ~ 10 TeV

$$\bigvee_{U/A^{-}}\begin{pmatrix} & & & & & \\ & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & & \\ & & & &$$

• For new physics interactions, e.g.  $\mathcal{L}_{\mathrm{NP}} = C_{ij}(\overline{u}_{Ri}\gamma^{\mu}u_{Rj})\mathcal{O}_{\mu}$ 

 $\rightarrow C_{ij} = c_0 \,\delta_{ij} + \epsilon \,c_1 (Y_u^{\dagger} Y_u)_{ij} + \epsilon^2 \left[ c_2 (Y_u^{\dagger} Y_u Y_u^{\dagger} Y_u)_{ij} + c_2' (Y_u^{\dagger} Y_d Y_d^{\dagger} Y_u)_{ij} \right] + \dots$ 

### MFV vs <u>U(2)<sup>5</sup></u>vs Rank-1 FV?

Flavour could just be an accidental symmetry from more fundamental interactions: nothing forbids it to be badly violated in the UV.
Marzia

II. U(2)<sup>5</sup> flavour breaking

Flavour violations =  $a Y_{1=2} + \varepsilon \tilde{Y}_3$ 

- > 3<sup>rd</sup> familiy special!
- two d.o.f
- ≻ Λ ~ 1 TeV
- > Higgs mostly coupled to 3rd gen

(could have escaped at Atlas/CMS)

$$\gamma_{U,N} = \Im_{t_{15}} \begin{pmatrix} \gamma_{1=2} & \widehat{\gamma}_{3} \\ 0 & 1 \end{pmatrix}$$

Bordone, Isidori, Trifinopoulos, 1705.10729 Allwicher, Cornella, Isidori and Stefanek, 2311.00020

### MFV vs U(2)<sup>5</sup> vs <u>Rank-1 FV</u>?

#### III. Rank-1 flavour breaking;

New Physics coupled linearly to SM quarks,  $\lambda_i \bar{q}^i \mathcal{O}_{\mathrm{NP}}$ 

Flavour violations = 
$$a \hat{n}_i \hat{n}_j$$
Five d.o.f $\wedge$  - 1-10 TeV $\hat{n}_i = \begin{pmatrix} \hat{n}_{1st} \\ \hat{n}_{2nd} \\ \hat{n}_{3rd} \end{pmatrix} = \begin{pmatrix} e^{i\alpha_{db}} \sin \theta \cos \phi \\ e^{i\alpha_{sb}} \sin \theta \sin \phi \\ \cos \theta \end{pmatrix}$ 

NP couples along a specific direction,  $\hat{n}$  in the U(3)\_q quark flavor space

Marzocca, Nardecchia, Toni, Stanzione, 2404.06533

### MFV and DM

#### **NO-anomalies: No panic!**

#### All interactions respect the MFV pattern

MFV hypothesis  $\rightarrow$  Stability of flavored dark matter

| $SU(3)_Q 	imes SU(3)_{u_R} 	imes SU(3)_{d_R}$                                                            | Stable? |
|----------------------------------------------------------------------------------------------------------|---------|
| (1, 1, 1)                                                                                                |         |
| ( <b>3</b> , <b>1</b> , <b>1</b> ),( <b>1</b> , <b>3</b> , <b>1</b> ),( <b>1</b> , <b>1</b> , <b>3</b> ) | Yes     |
| $(ar{3},1,1),(1,ar{3},1),(1,1,ar{3})$                                                                    | Yes     |
| $({f 6},{f 1},{f 1}),({f 1},{f 6},{f 1}),({f 1},{f 1},{f 6})$                                            | Yes     |
| ( <b>3</b> , <b>3</b> , <b>1</b> ),( <b>3</b> , <b>1</b> , <b>3</b> ),( <b>1</b> , <b>3</b> , <b>3</b> ) |         |
| $(ar{6}, 1, 1),(1, ar{6}, 1),(1, 1, ar{6})$                                                              | Ves     |
| $(ar{3},ar{3},1),(ar{3},1,ar{3}),(1,ar{3},ar{3})$                                                        | 105     |

 $(n_{\chi} - m_{\chi}) \mod 3 \neq 0$ 

- Applied for any spin and EW representation of  $\chi$
- Only the lightest flavored particle is stable

Batell, Pradler, Spannowsky, 1105.1781 Lopez-Honorez and L. Merlo,1303.1087 F.M., Okawa, Keyun Wu 2408.16812

 $\chi \sim (n_{q_L}, m_{q_L}) \times (n_{u_R}, m_{u_R}) \times (n_{d_R}, m_{d_R})$ 

$$m_\chi = m_{q_L} + m_{u_R} + m_{d_R}$$
  
 $n_\chi = n_{q_L} + n_{u_R} + n_{d_R}$ 

stability condition

### DM and Flavour Physics (MFV)

A gauge singlet scalar  $S \sim (\mathbf{1}, \mathbf{3}, \mathbf{1})$ 



- Compatible with all direct and indirect searches
- $\ \ \square \ \ \tau_{S_i} > \tau_U \ \rightarrow \mathsf{DM}$
- □  $\tau_{S_i} < \tau_U$  → not DM and have to decay prior to the BBN (we require  $\tau_{S_i} < 1$  sec in that case)
- DM are composed of two or three components in the white region

F.M., Okawa, Keyun Wu 2408.16812

### What next?!:

### What next?!:



Plenty of new experiments on the next 10 years. <u>Ora et Labora.</u> (LHCb, Belle-II, BES-III, NA62, KOTO, EDM, g-2, Mu2e, Legend-1000)

**Proposed Future Running** 

Data Taking

(Approved Experiments)



# Conclusions

#### Intensity frontier:

Potential discovery of new d.o.f beyond the reach of direct productions, ATLAS/CMS

#### *⊗* Hadronic uncertainties:

QCD strong to kill – PIANO PIANO!

#### • $R_D$ and $b \rightarrow s \mu \mu$ :

Theory and exp. progress is needed to solve this issue: new Exp. and LQCD data will be essential.

#### **\*** $B \rightarrow K$ vv and $K \rightarrow \pi vv$ :

Better data are expected soon from NA62 and Belle II.

#### Model Building:

new ideas to tackle and correlate other open questions

Força, Equilibri, Valor i Seny





Força, Equilibri, Valor i Seny

# Bon voyage to Beyond Flavour Anomalies

## **HL-LHC**

BELLEI

# **BSM** is awaiting

### Flavour Thysics: window to New Thysics

#### HL-LHC hints; "NP flavour to be or not to be hierarchical"?



### **Flavour Shysics:** NP in the 3rd generation



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 $U(2)^5 \equiv U(2)_q \times U(2)_u \times U(2)_d \times U(2)_\ell \times U(2)_e$ 



Allwicher, Cornella, Isidori and Stefanek 2311.00020

| Observable                                                                       | Current LHCb                    | LHCb 2025                    | Belle II                             | Upgrade II                   |
|----------------------------------------------------------------------------------|---------------------------------|------------------------------|--------------------------------------|------------------------------|
| EW Penguins                                                                      |                                 |                              |                                      | 10                           |
| $\frac{1}{R_{V}} (1 < q^{2} < 6 \mathrm{GeV}^{2} c^{4})$                         | 0.1 [274]                       | 0.025                        | 0.036                                | 0.007                        |
| $B_{K^*}$ $(1 < q^2 < 6 {\rm GeV}^2 c^4)$                                        | 0.1 [275]                       | 0.031                        | 0.032                                | 0.008                        |
| $R_{\phi}, R_{pK}, R_{\pi}$                                                      | -                               | 0.08, 0.06, 0.18             | -                                    | 0.02,0.02,0.05               |
| CKM tests                                                                        |                                 |                              |                                      |                              |
| $\gamma$ , with $B^0 \rightarrow D^+ K^-$                                        | $\binom{+17}{22}^{\circ}$ [136] | 4°                           | -                                    | 1°                           |
| $\gamma$ , all modes                                                             | 3° [167]                        | $1.5^{\circ}$                | $1.5^{\circ}$                        | $0.35^{\circ}$               |
| $\sin 2\beta$ , with $B^0 \to J/\psi K_c^0$                                      | 0.013 609                       | 0.011                        | 0.005                                | 0.003                        |
| $\phi_{\rm ev}$ with $B^0 \to J/\psi\phi$                                        | 20 mrad 44                      | 14 mrad                      | -                                    | 4 mrad                       |
| $\phi_s$ , with $B_s^0 \to D_s^+ D_s^-$                                          | 170 mrad 49                     | 35 mrad                      | -                                    | 9 mrad                       |
| $\phi^{s\bar{s}s}_{s}$ , with $B^0_{s} \to \phi\phi$                             | 154 mrad 94                     | 39 mrad                      | -                                    | 11 mrad                      |
| $a_{-1}^s$                                                                       | $33 \times 10^{-4}$ [211]       | $10 	imes 10^{-4}$           | -                                    | $3	imes 10^{-4}$             |
| $ V_{ub} / V_{cb} $                                                              | 6% 201                          | 3%                           | 1%                                   | 1%                           |
| $B^0_*, B^0 { ightarrow} \mu^+ \mu^-$                                            |                                 |                              |                                      |                              |
| $\overline{\mathcal{B}(B^0 \to \mu^+ \mu^-)}/\mathcal{B}(B^0_c \to \mu^+ \mu^-)$ | 90% [264]                       | 34%                          | -                                    | 10%                          |
| $\tau_{R^0 \rightarrow u^+ u^-}$                                                 | 22% [264]                       | 8%                           | -                                    | 2%                           |
| $S_{\mu\mu}^{\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $                             | <u> </u>                        | -                            | -                                    | 0.2                          |
| $b  ightarrow c \ell^- \bar{ u_l} 	ext{ LUV studies}$                            |                                 |                              |                                      |                              |
| $\overline{R(D^*)}$                                                              | 0.026 [215, 217]                | 0.0072                       | 0.005                                | 0.002                        |
| $R(J/\psi)$                                                                      | 0.24 [220]                      | 0.071                        | -                                    | 0.02                         |
| Charm                                                                            |                                 |                              |                                      |                              |
| $\Delta A_{CP}(KK - \pi\pi)$                                                     | $2.9 \times 10^{-4}$ [613]      | $1.7 	imes 10^{-4}$          | $5.4 	imes 10^{-4}$                  | $3.0	imes10^{-5}$            |
| $A_{\Gamma} \ (\approx x \sin \phi)$                                             | $2.8 \times 10^{-4}$ [240]      | $4.3 	imes 10^{-5}$          | $3.5 	imes 10^{-4}$                  | $1.0 \times 10^{-5}$         |
| $x\sin\phi$ from $D^0 \to K^+\pi^-$                                              | $13 	imes 10^{-4}$ [228]        | $3.2 	imes 10^{-4}$          | $4.6 	imes 10^{-4}$                  | $8.0	imes10^{-5}$            |
| $x\sin\phi$ from multibody decays                                                | _                               | $(K3\pi) 4.0 \times 10^{-5}$ | $(K_{ m S}^0\pi\pi)~1.2	imes10^{-4}$ | $(K3\pi)  8.0 	imes 10^{-6}$ |

#### Long story short

- 1) The contribution is dominated by the charm loops due to  $O_{1c}$  and  $O_{2c}$
- 2) The contribution mimics new physics by shifting  $C_9$





|                                              | AC  | RVV2 | AKM | $\delta LL$ | FBMSSM | LHT | RS  |
|----------------------------------------------|-----|------|-----|-------------|--------|-----|-----|
| $D^0 - \bar{D}^0$                            | *** | *    | *   | *           | *      | *** | ?   |
| $\epsilon_K$                                 | *   | ***  | *** | *           | *      | **  | *** |
| $S_{\psi\phi}$                               | *** | ***  | *** | *           | *      | *** | *** |
| $S_{\phi K_S}$                               | *** | **   | *   | ***         | ***    | *   | ?   |
| $A_{\rm CP} \left( B \to X_s \gamma \right)$ | *   | *    | *   | ***         | ***    | *   | ?   |
| $A_{7,8}(B \to K^* \mu^+ \mu^-)$             | *   | *    | *   | ***         | ***    | **  | ?   |
| $A_9(B \to K^* \mu^+ \mu^-)$                 | *   | *    | *   | *           | *      | *   | ?   |
| $B \to K^{(*)} \nu \bar{\nu}$                | *   | *    | *   | *           | *      | *   | *   |
| $B_s \rightarrow \mu^+ \mu^-$                | *** | ***  | *** | ***         | ***    | *   | *   |
| $K^+ \to \pi^+ \nu \bar{\nu}$                | *   | *    | *   | *           | *      | *** | *** |
| $K_L \to \pi^0 \nu \bar{\nu}$                | *   | *    | *   | *           | *      | *** | *** |
| $\mu \rightarrow e \gamma$                   | *** | ***  | *** | ***         | ***    | *** | *** |
| $\tau \to \mu \gamma$                        | *** | ***  | *   | ***         | ***    | *** | *** |
| $\mu + N \rightarrow e + N$                  | *** | ***  | *** | ***         | ***    | *** | *** |
| $d_n$                                        | *** | ***  | *** | **          | ***    | *   | *** |
| $d_e$                                        | *** | ***  | **  | *           | ***    | *   | *** |
| $(g-2)_{\mu}$                                | *** | ***  | **  | ***         | ***    | *   | ?   |

#### ★★★ large effects

 $\star$ 

- ★★ visible but small effects
  - unobservable effects