

NEW FRONTIERS IN SUB-MEV DARK MATTER SEARCHES

Angelo Esposito



SAPIENZA
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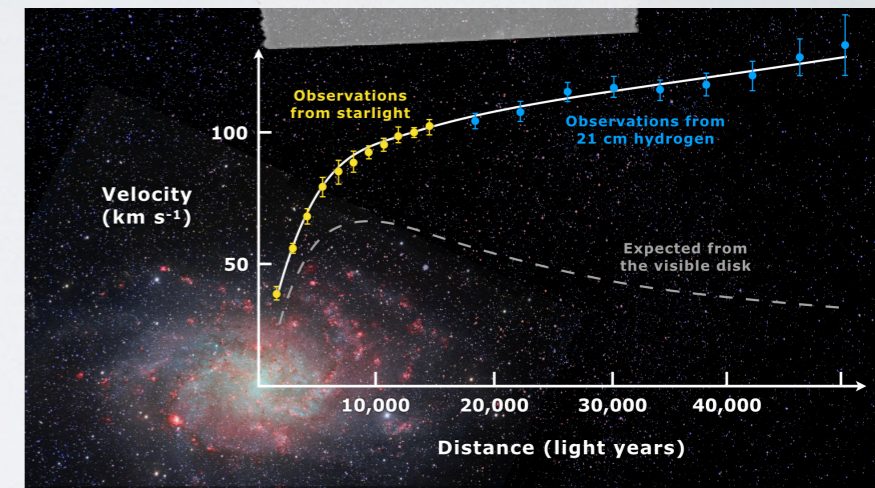
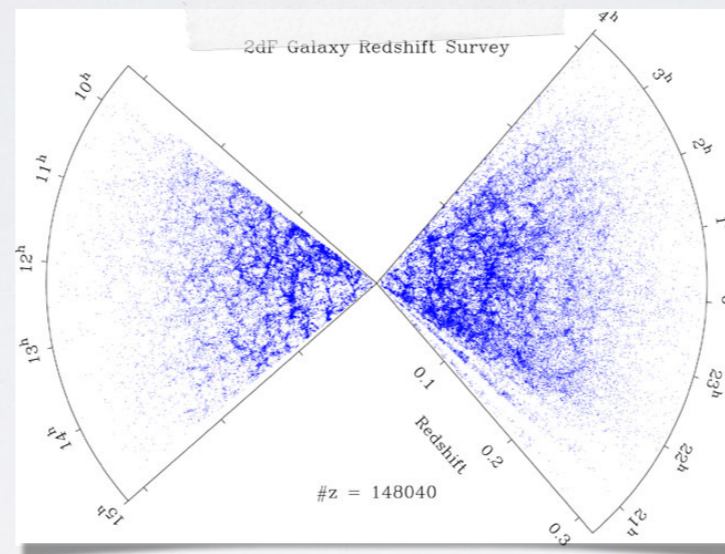
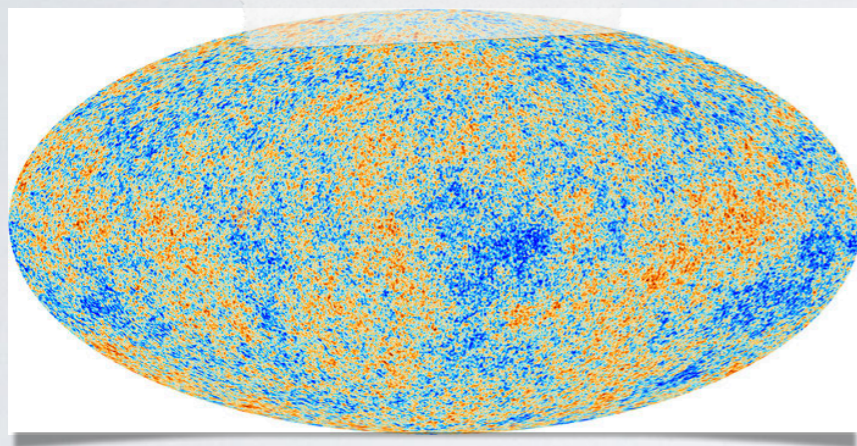
Istituto Nazionale di Fisica Nucleare

“The low-energy frontier of particle physics”, LNF Feb. 11th 2025

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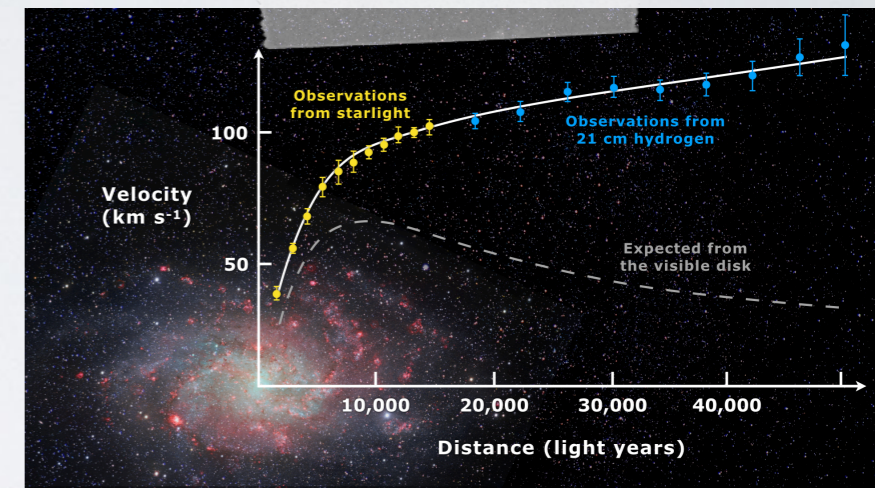
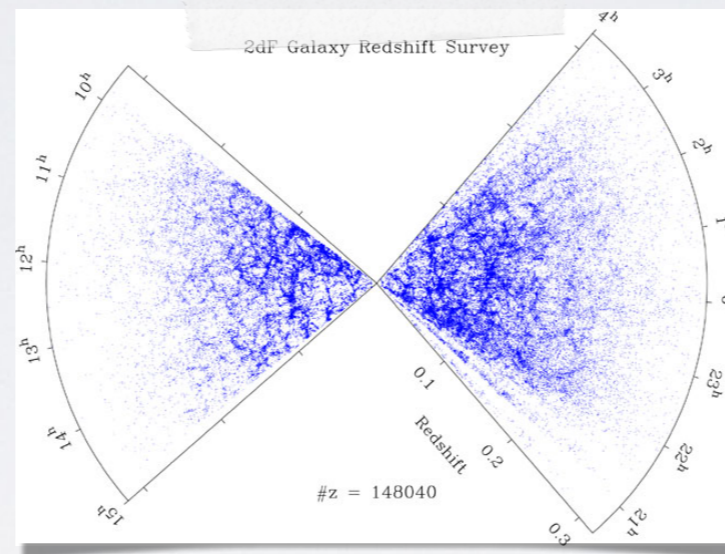
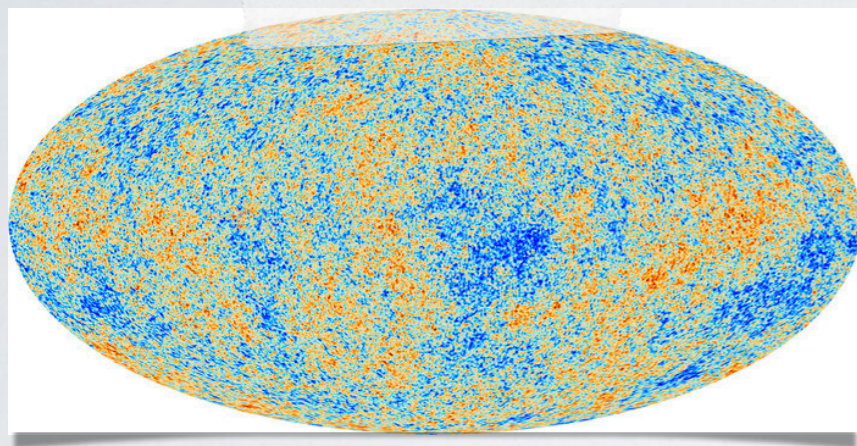
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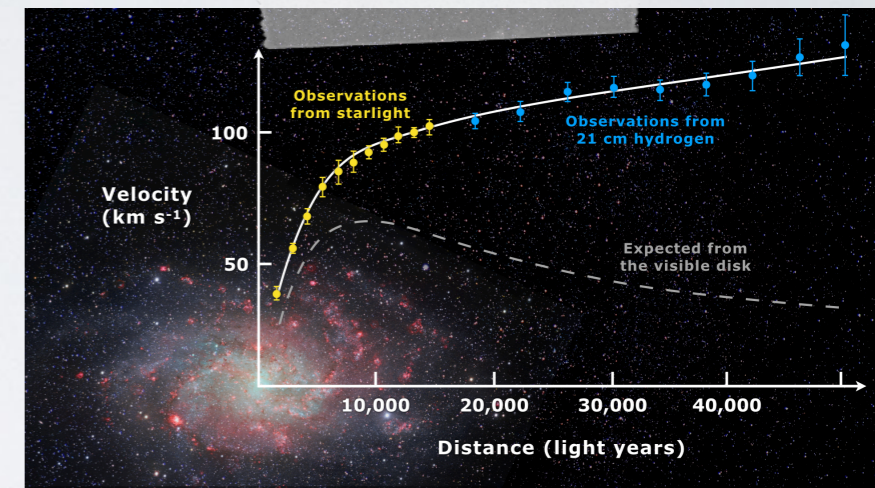
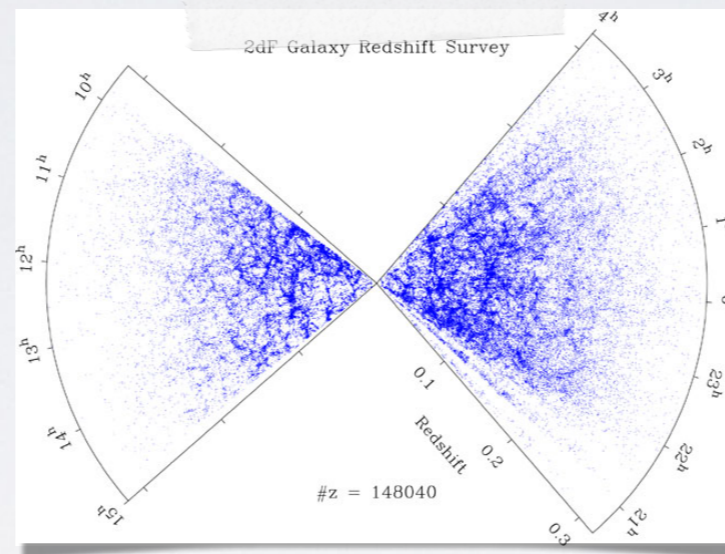
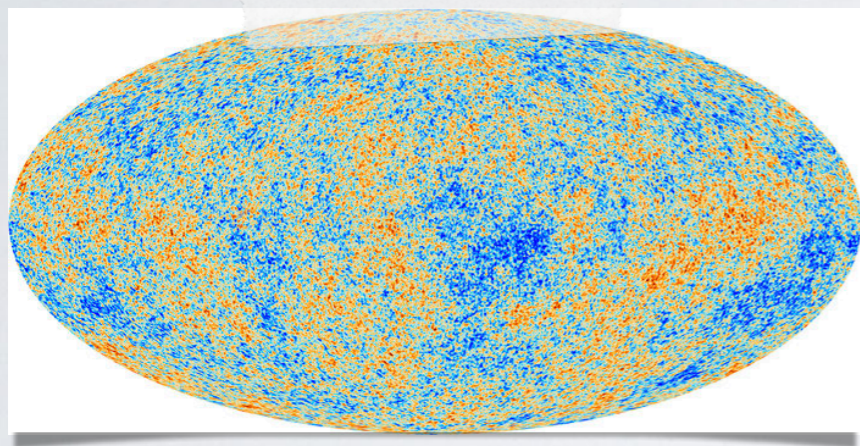
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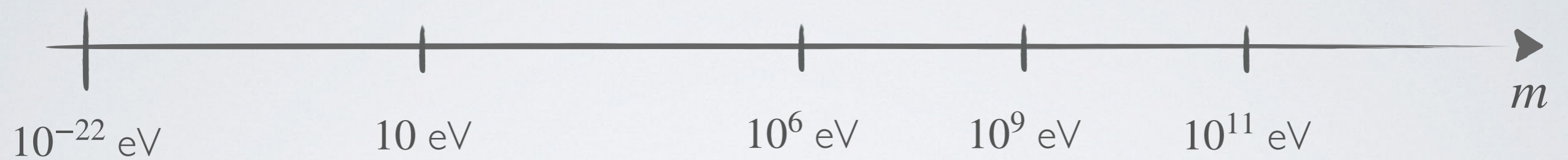
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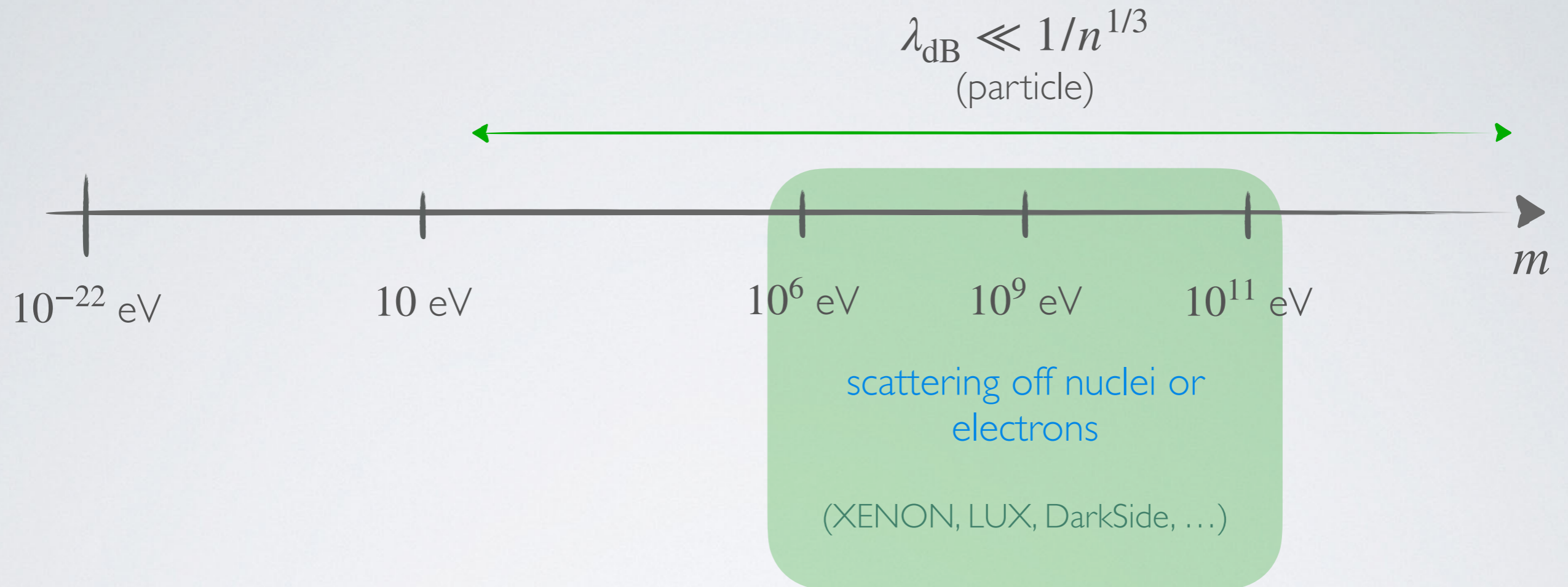
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- However... huge possible mass range → detection techniques vary widely depending on the dark matter mass

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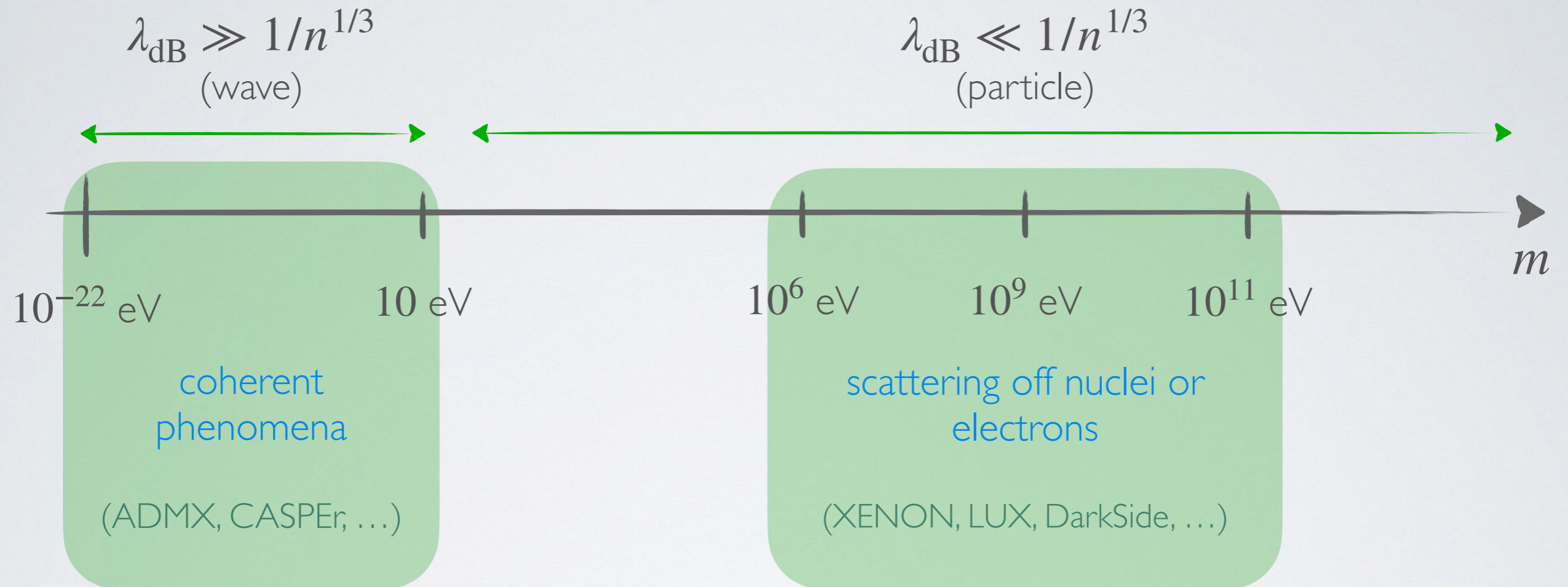
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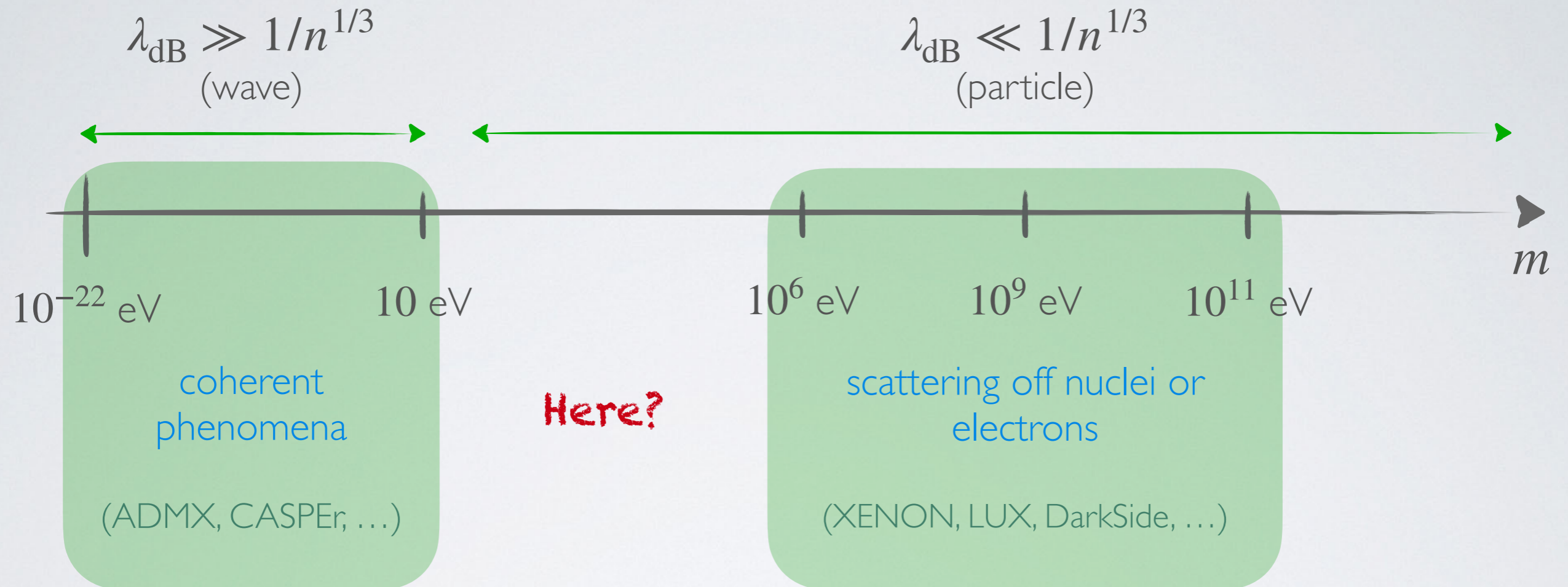
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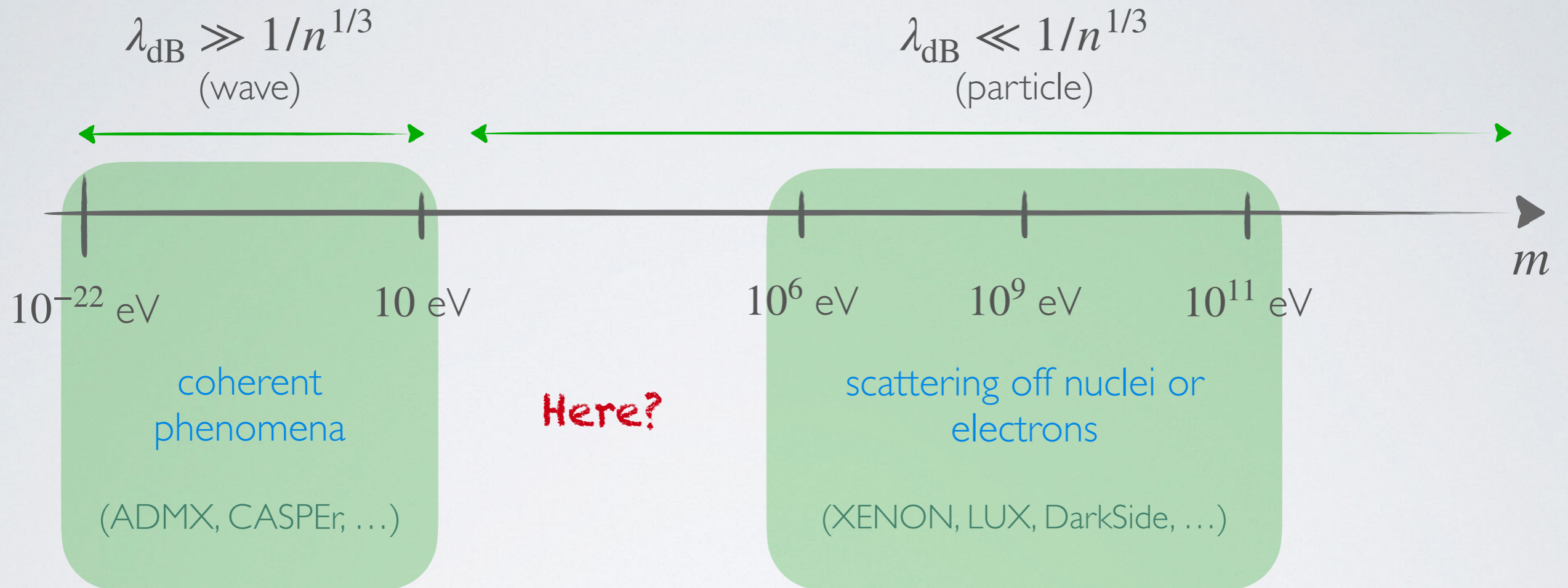
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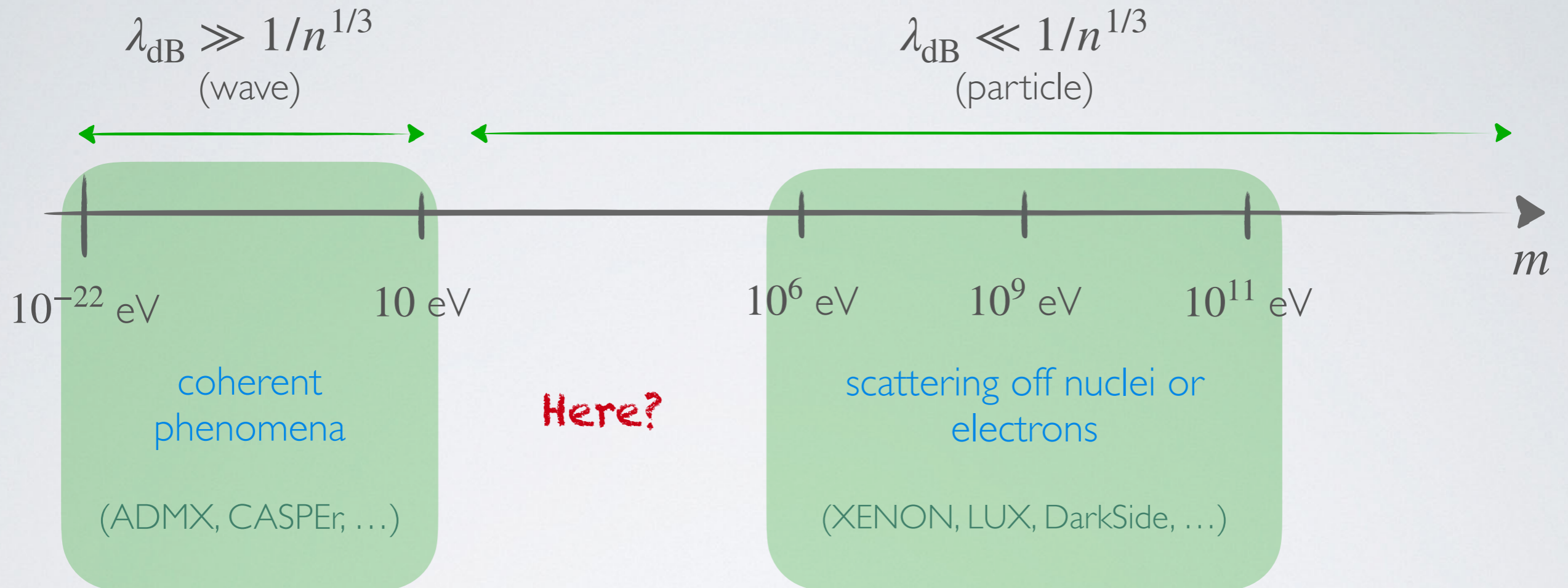


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- Need **new materials and/or observables**

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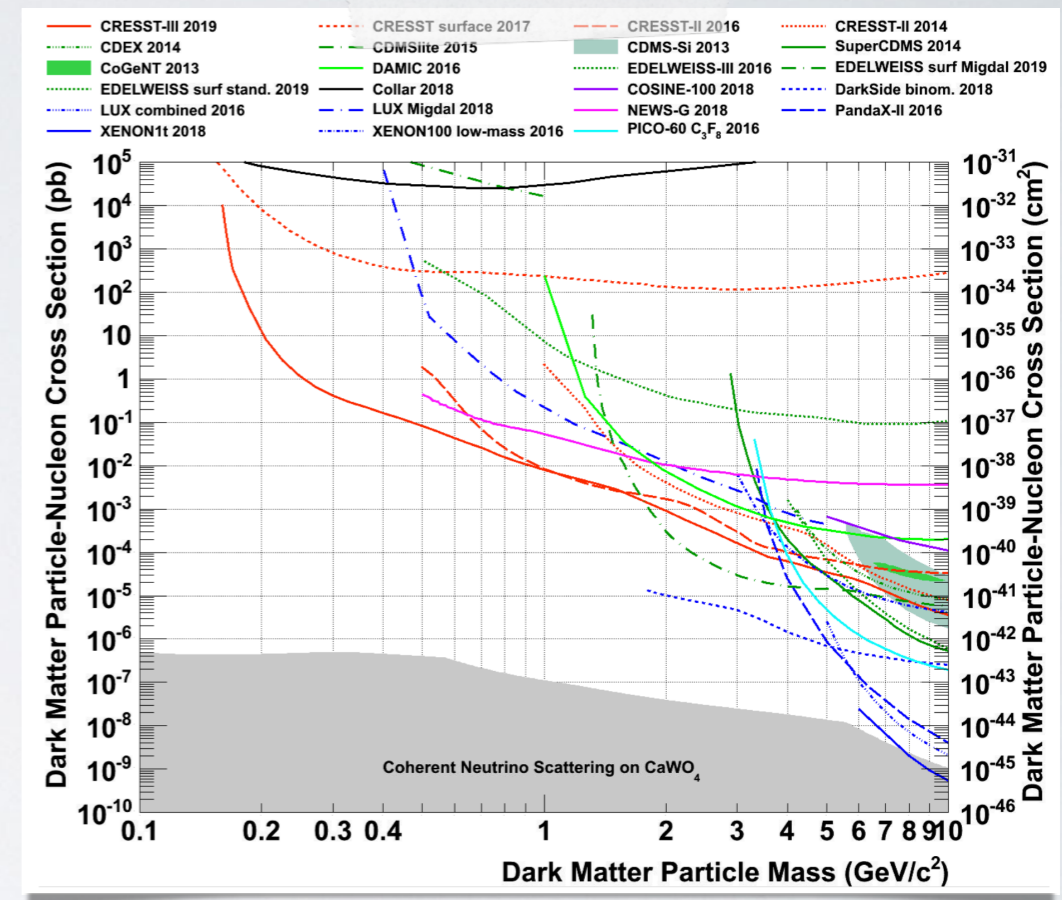
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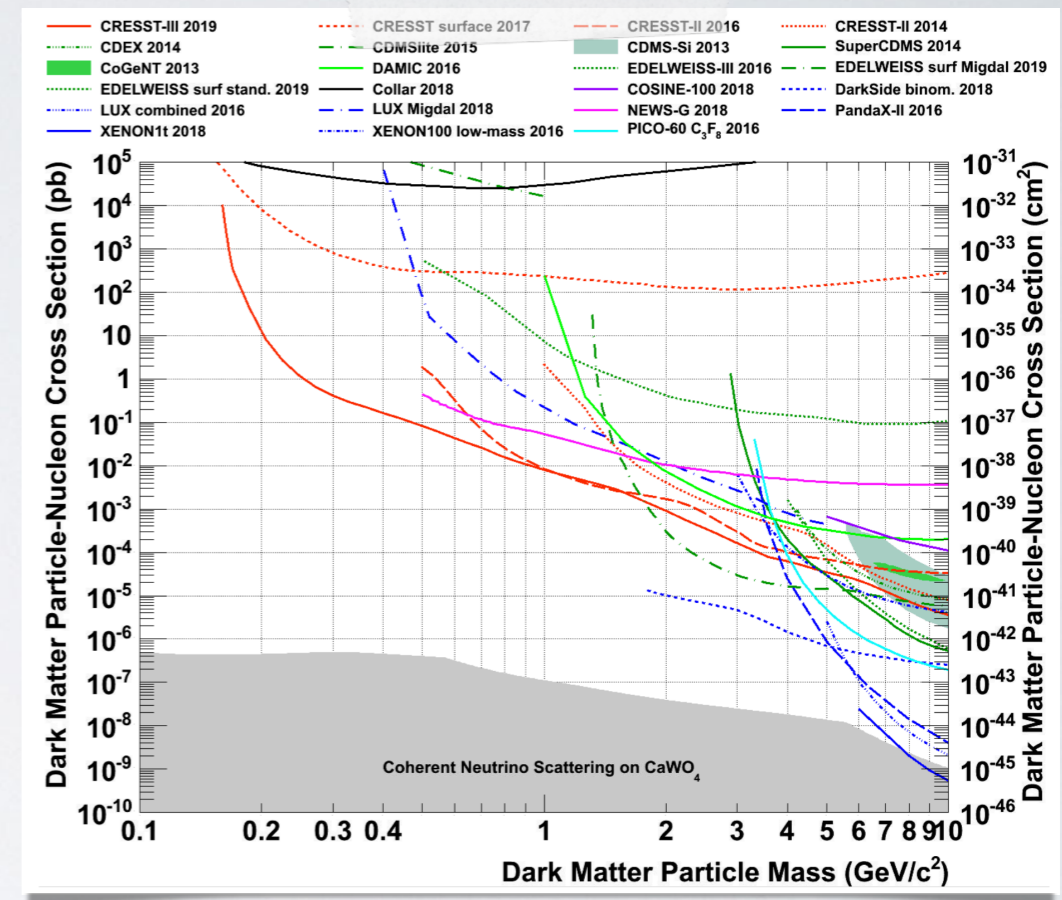
[CRESST – PRD 2019, 1904.00498]

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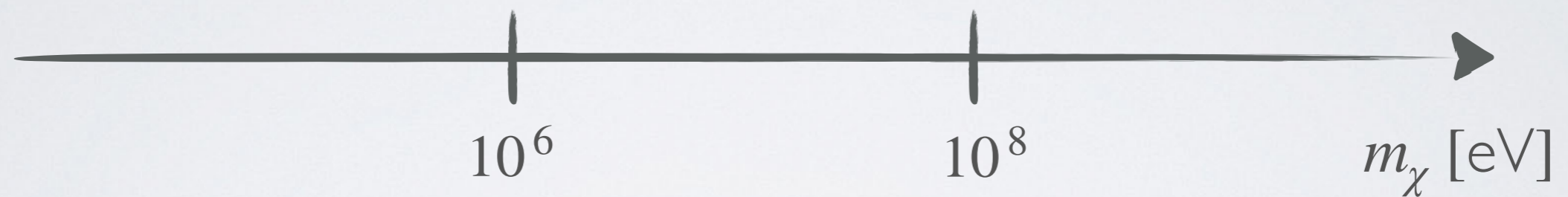
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- To evade this we must look into inelastic processes → one possibility are collective excitations

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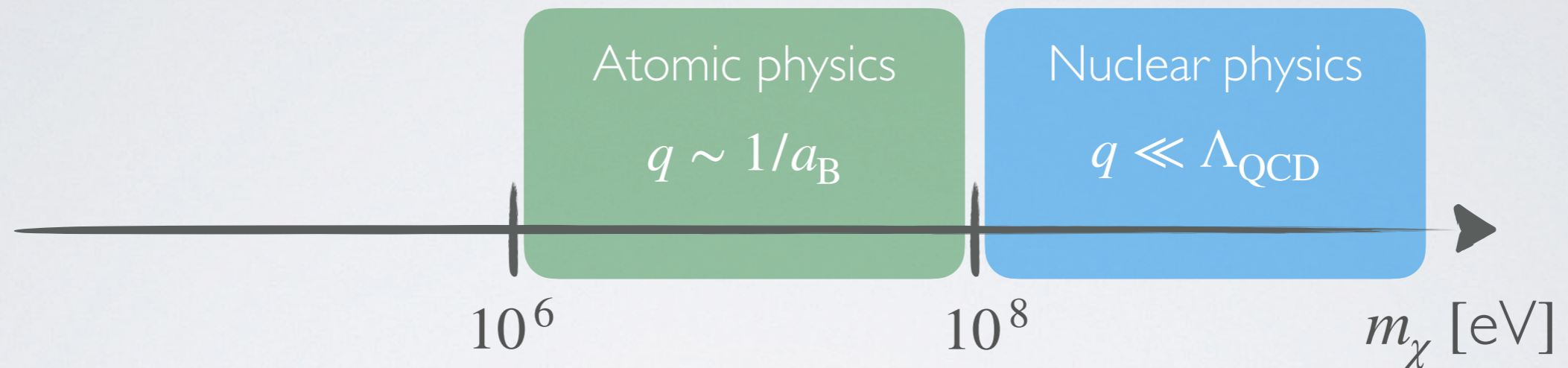
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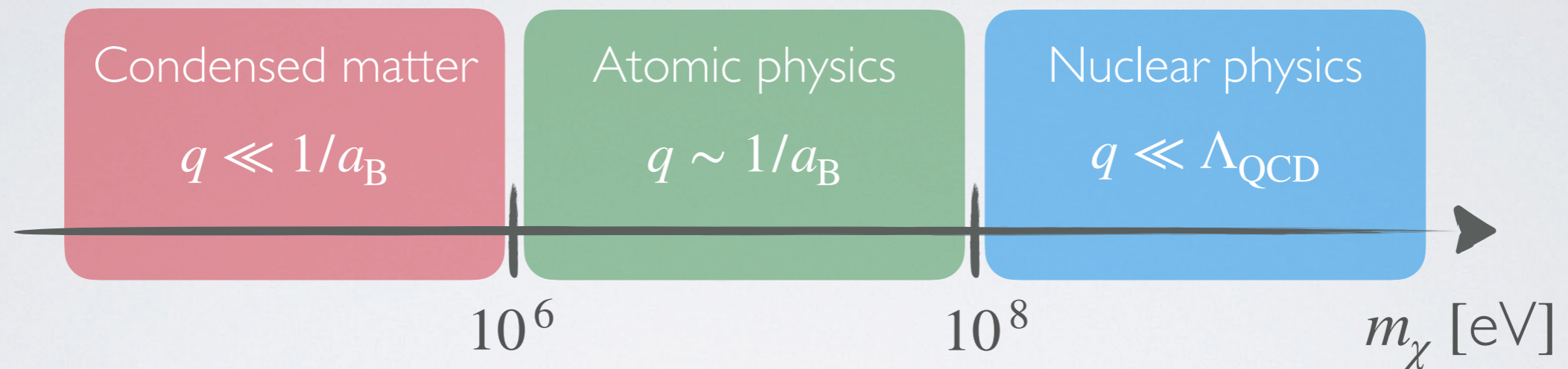
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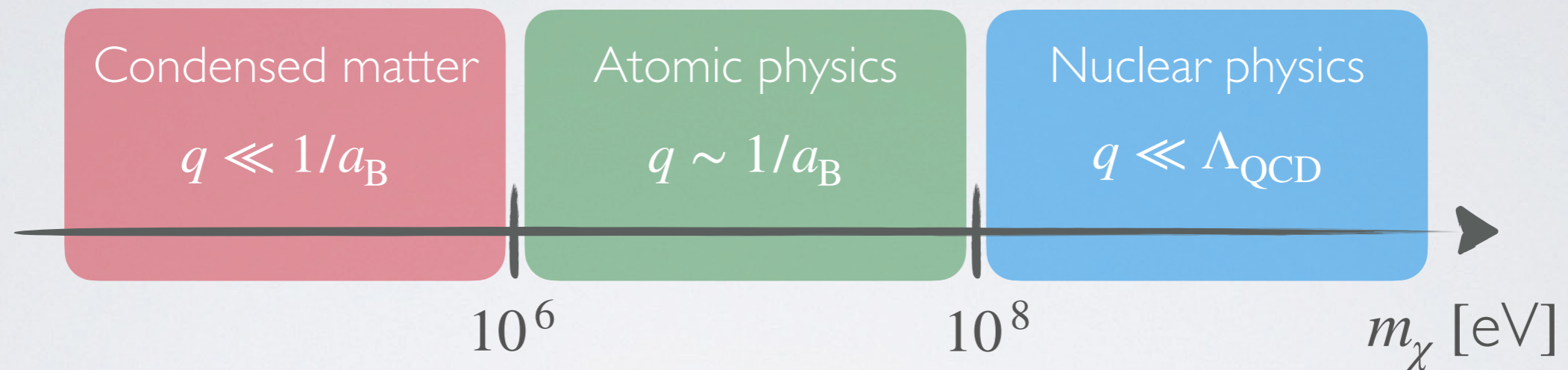
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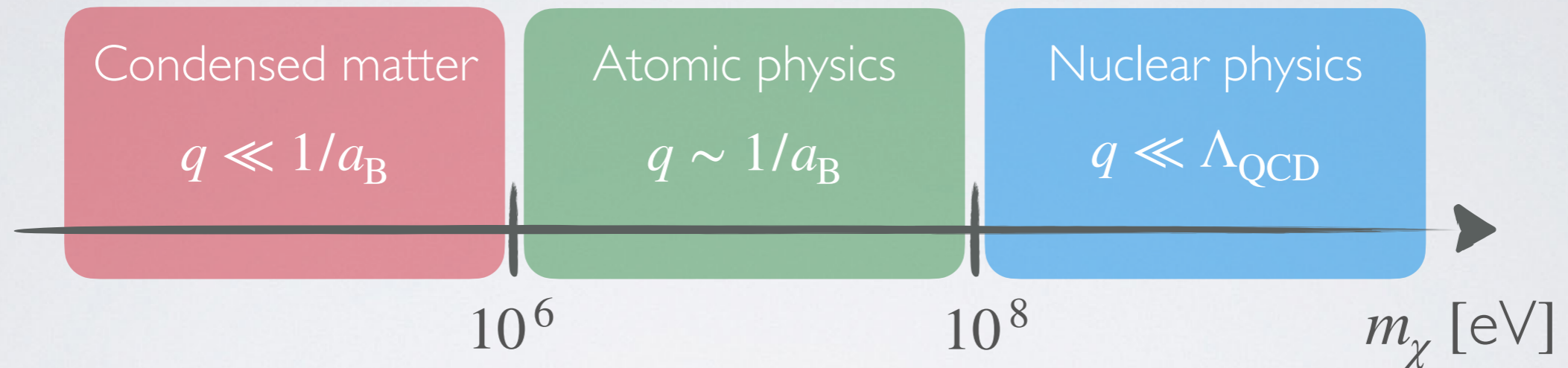
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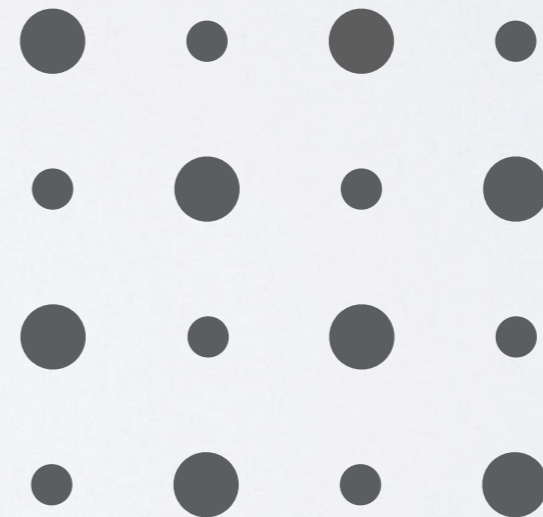
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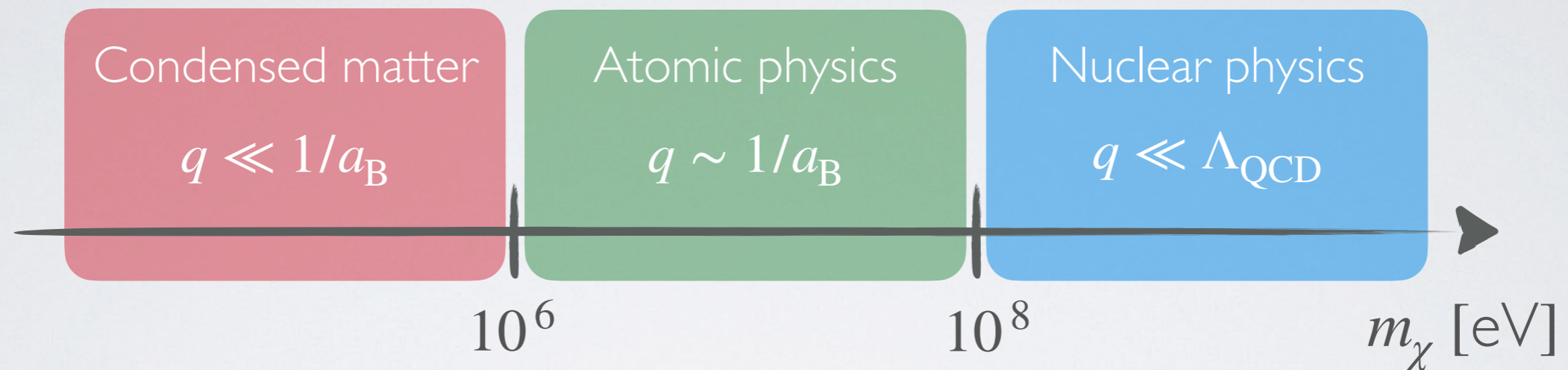


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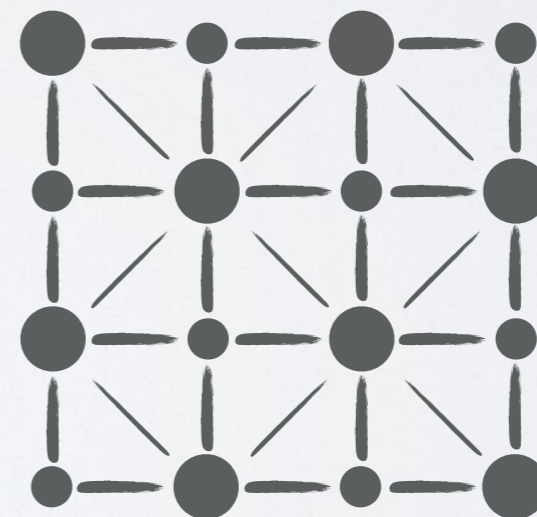


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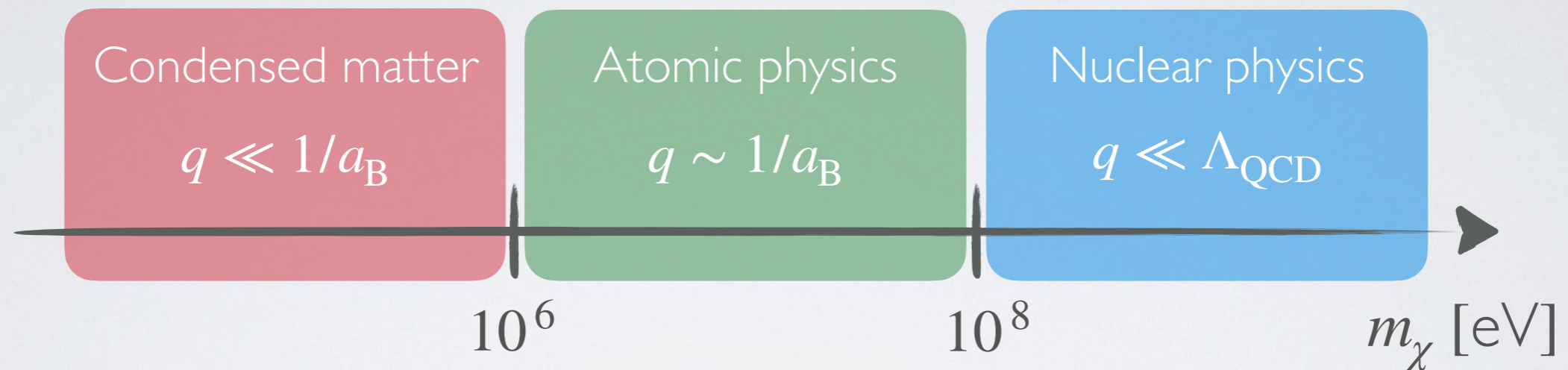


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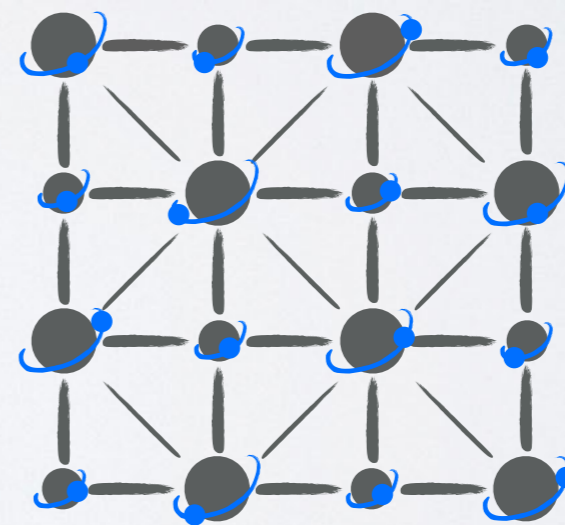


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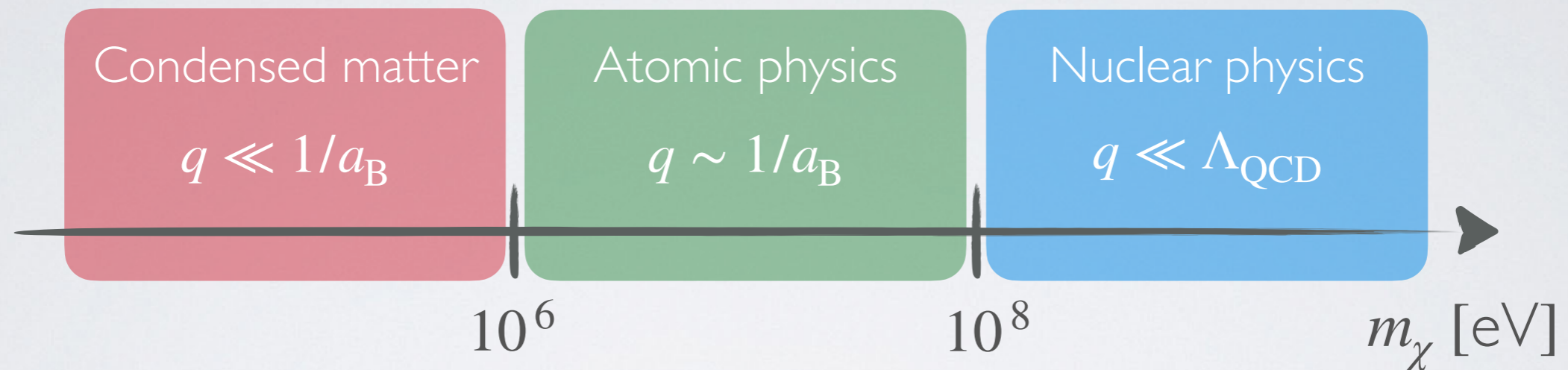


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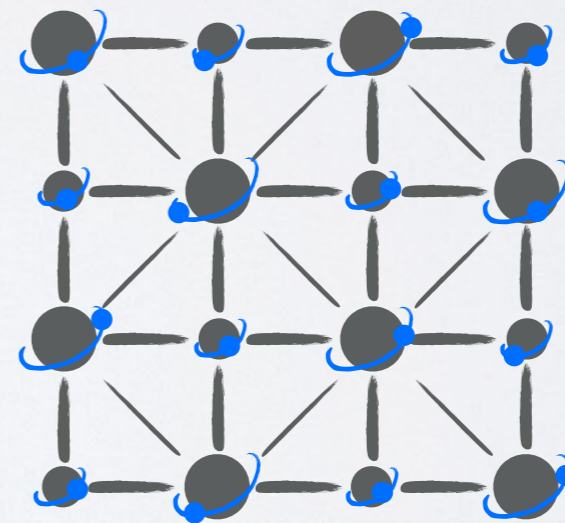


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- Need theoretical tools** that allow to solve or bypass these problems

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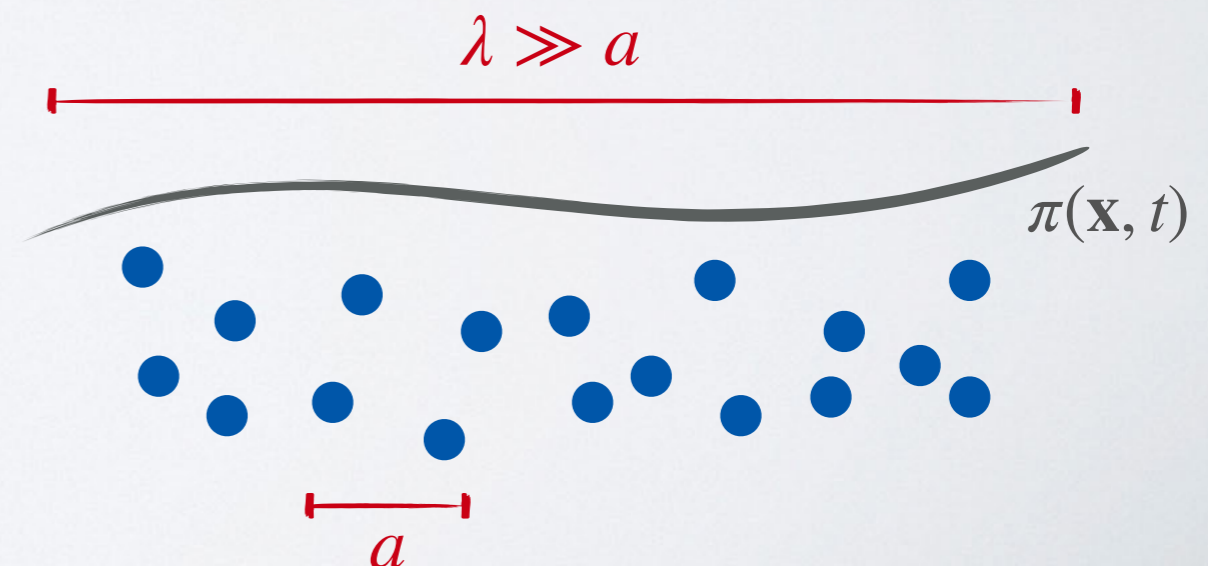
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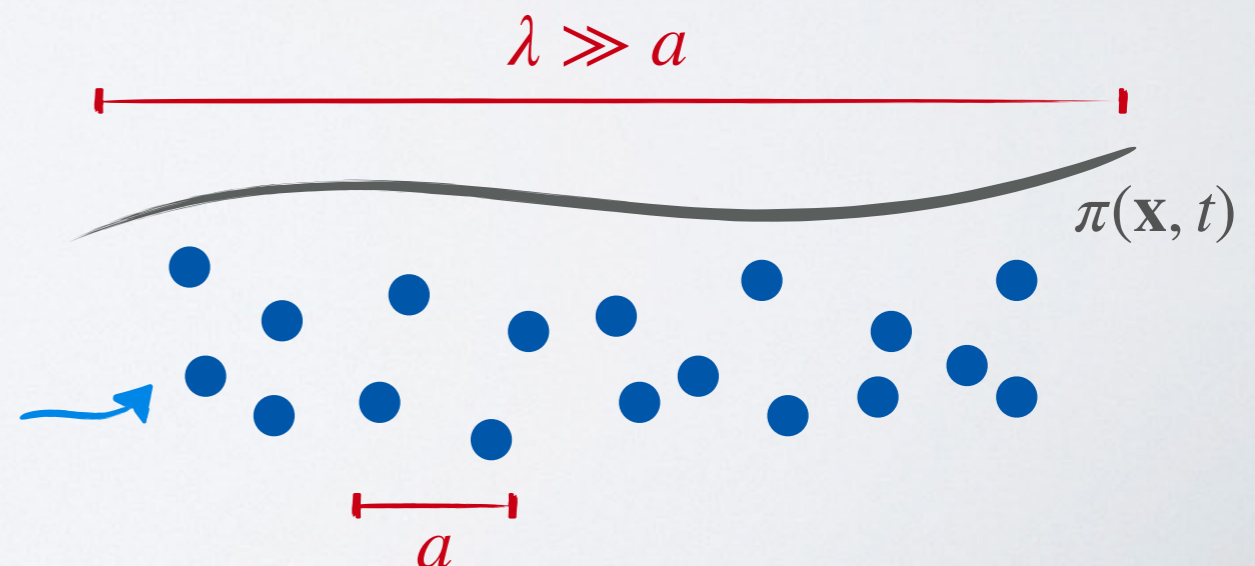
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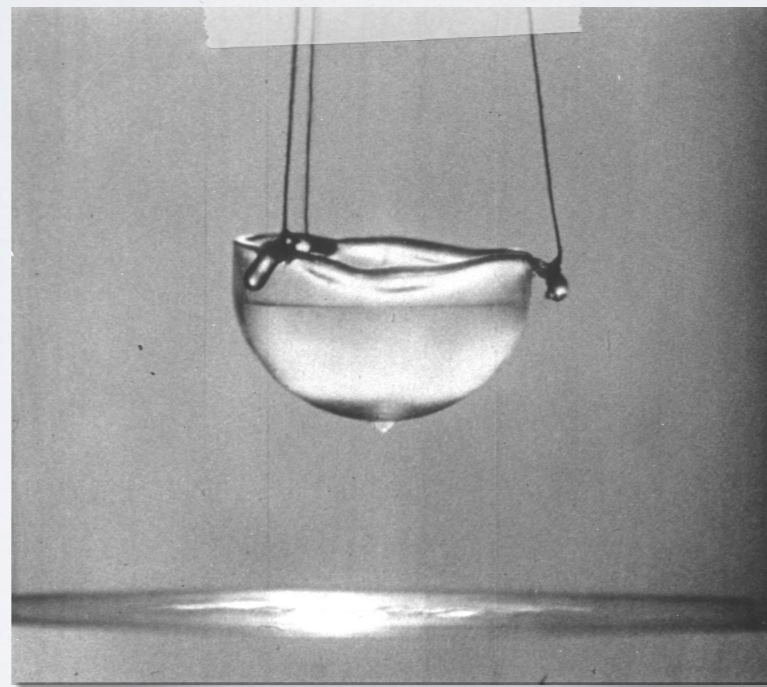
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complicated microscopic physics encoded here



Spin-independent interactions: superfluid ^4He



[w/ Acanfora, Caputo, Geoffray,
Piccinini, Polosa, Rossi, Sun]

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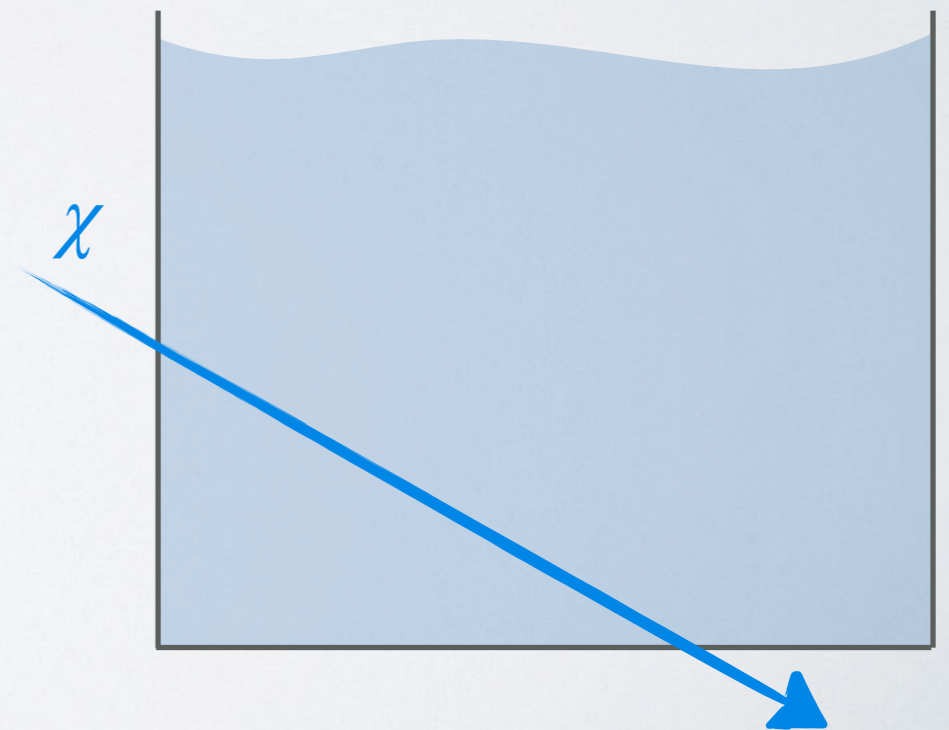
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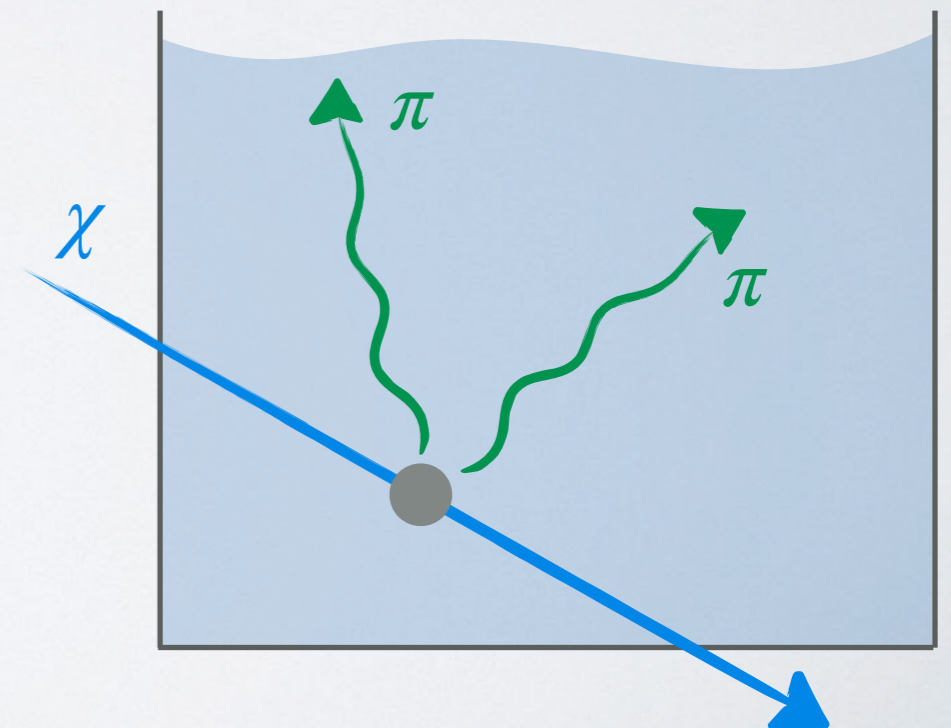
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- Not enough modes to lose energy/momentum into

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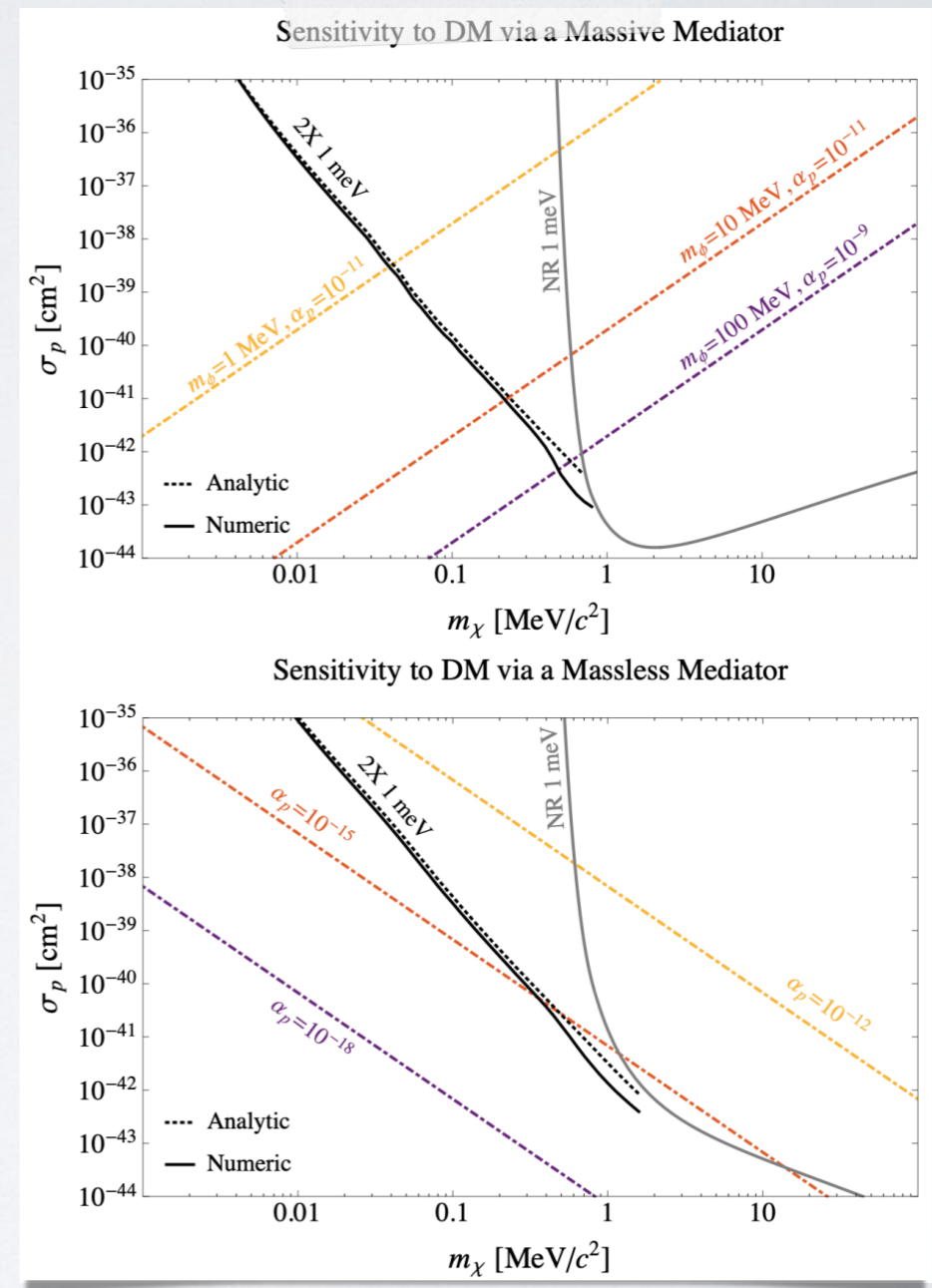


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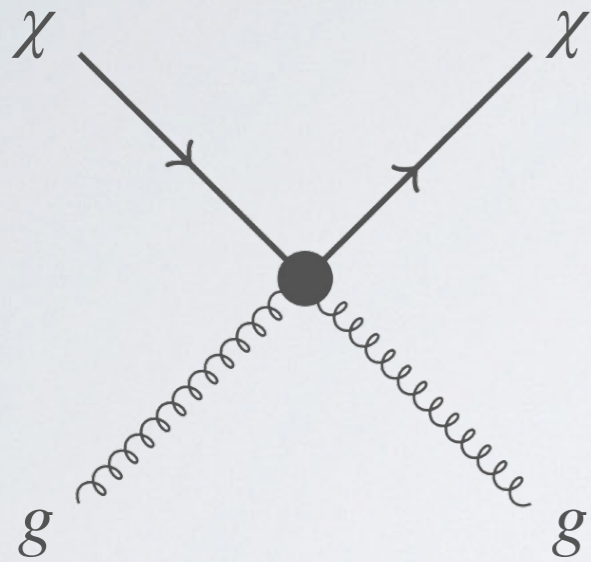
effective coefficients
are given by the
equation of state:

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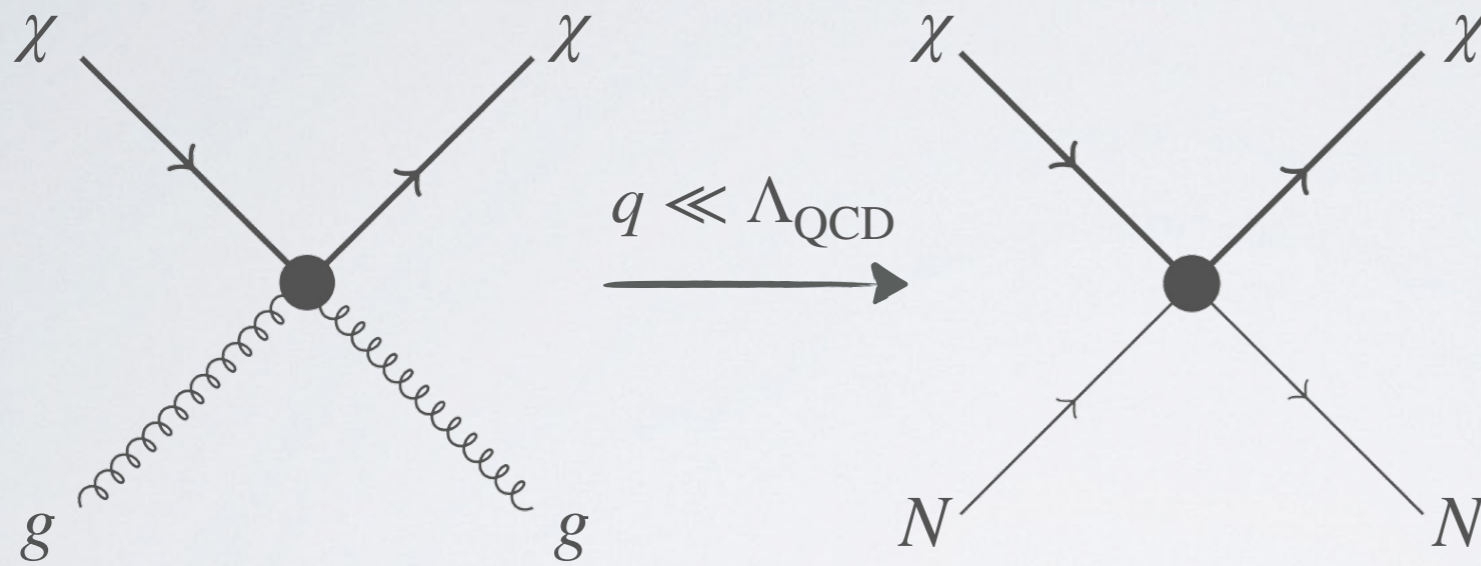
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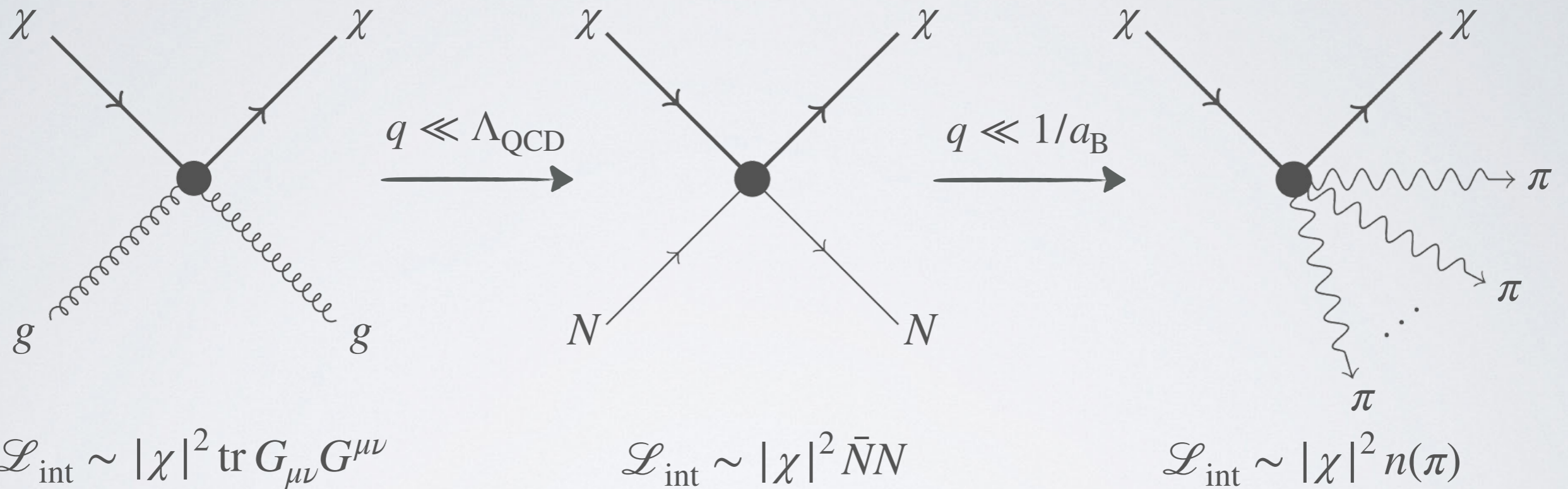


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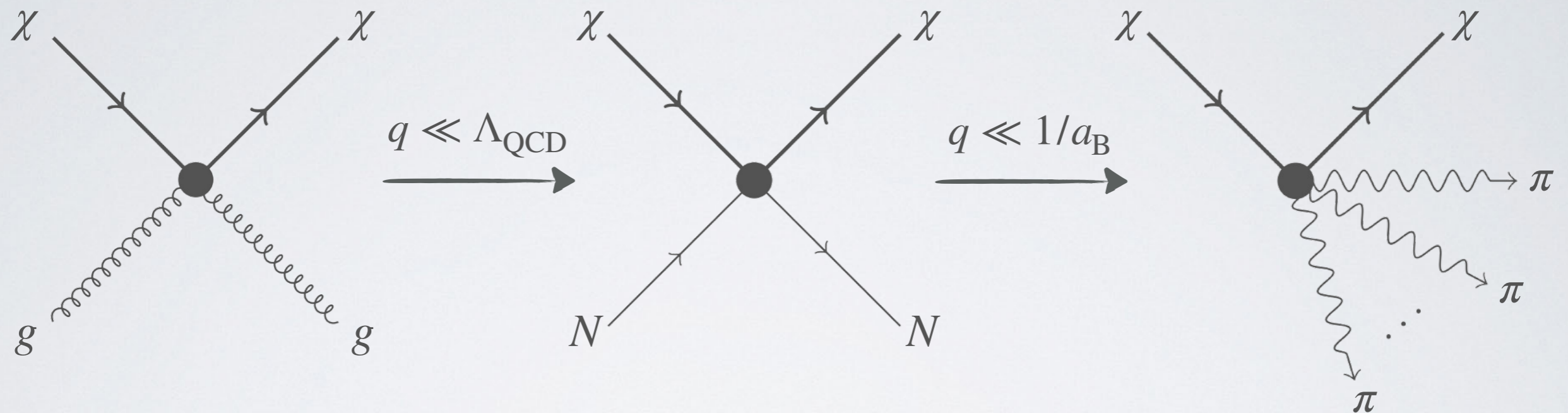
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$$\mathcal{L}_{\text{int}} \sim |\chi|^2 \text{tr} G_{\mu\nu} G^{\mu\nu}$$

$$\mathcal{L}_{\text{int}} \sim |\chi|^2 \bar{N}N$$

$$\mathcal{L}_{\text{int}} \sim |\chi|^2 n(\pi)$$

- Obtain from the $U(1)$ Noether current within the EFT

$$\mathcal{L}_{\text{int}} \propto |\chi|^2 J^0 \sim |\chi|^2 \left(g\dot{\pi} + g'\dot{\pi}^2 + g''(\nabla\pi)^2 + \dots \right)$$

[see, e.g., Acanfora, **AE**, Polosa – EPJC 2019, 1902.02361]

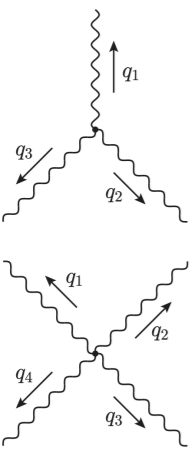
IDEAL REACH

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- We can now use [standard QFT methods](#) to compute event rates

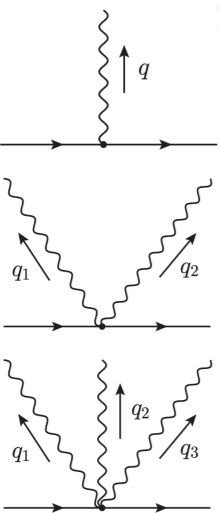
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$$= g_1 (\omega_1 \mathbf{q}_2 \cdot \mathbf{q}_3 + \omega_2 \mathbf{q}_1 \cdot \mathbf{q}_3 + \omega_3 \mathbf{q}_1 \cdot \mathbf{q}_2) + g_2 \omega_1 \omega_2 \omega_3,$$

$$= i\lambda_1 (\mathbf{q}_1 \cdot \mathbf{q}_2 \mathbf{q}_3 \cdot \mathbf{q}_4 + \mathbf{q}_1 \cdot \mathbf{q}_3 \mathbf{q}_2 \cdot \mathbf{q}_4 + \mathbf{q}_1 \cdot \mathbf{q}_4 \mathbf{q}_2 \cdot \mathbf{q}_3) + i\lambda_2 (\omega_1 \omega_2 \mathbf{q}_3 \cdot \mathbf{q}_4 + \omega_1 \omega_3 \mathbf{q}_2 \cdot \mathbf{q}_4 + \omega_1 \omega_4 \mathbf{q}_2 \cdot \mathbf{q}_3 + \omega_2 \omega_3 \mathbf{q}_1 \cdot \mathbf{q}_4 + \omega_2 \omega_4 \mathbf{q}_1 \cdot \mathbf{q}_3 + \omega_3 \omega_4 \mathbf{q}_1 \cdot \mathbf{q}_2) + i\lambda_3 \omega_1 \omega_2 \omega_3 \omega_4,$$



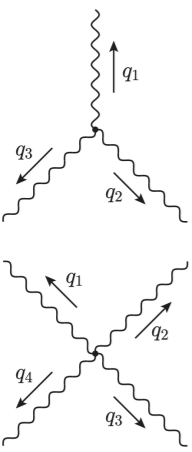
$$= G_\chi m_\chi \alpha \omega,$$

$$= iG_\chi m_\chi (\beta_1 \mathbf{q}_1 \cdot \mathbf{q}_2 + \beta_2 \omega_1 \omega_2),$$

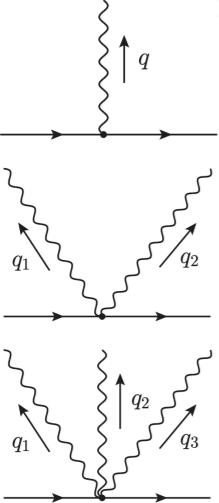
$$= G_\chi m_\chi [\gamma_1 (\omega_1 \mathbf{q}_2 \cdot \mathbf{q}_3 + \omega_2 \mathbf{q}_1 \cdot \mathbf{q}_3 + \omega_3 \mathbf{q}_1 \cdot \mathbf{q}_2) + \gamma_2 \omega_1 \omega_2 \omega_3].$$

IDEAL REACH

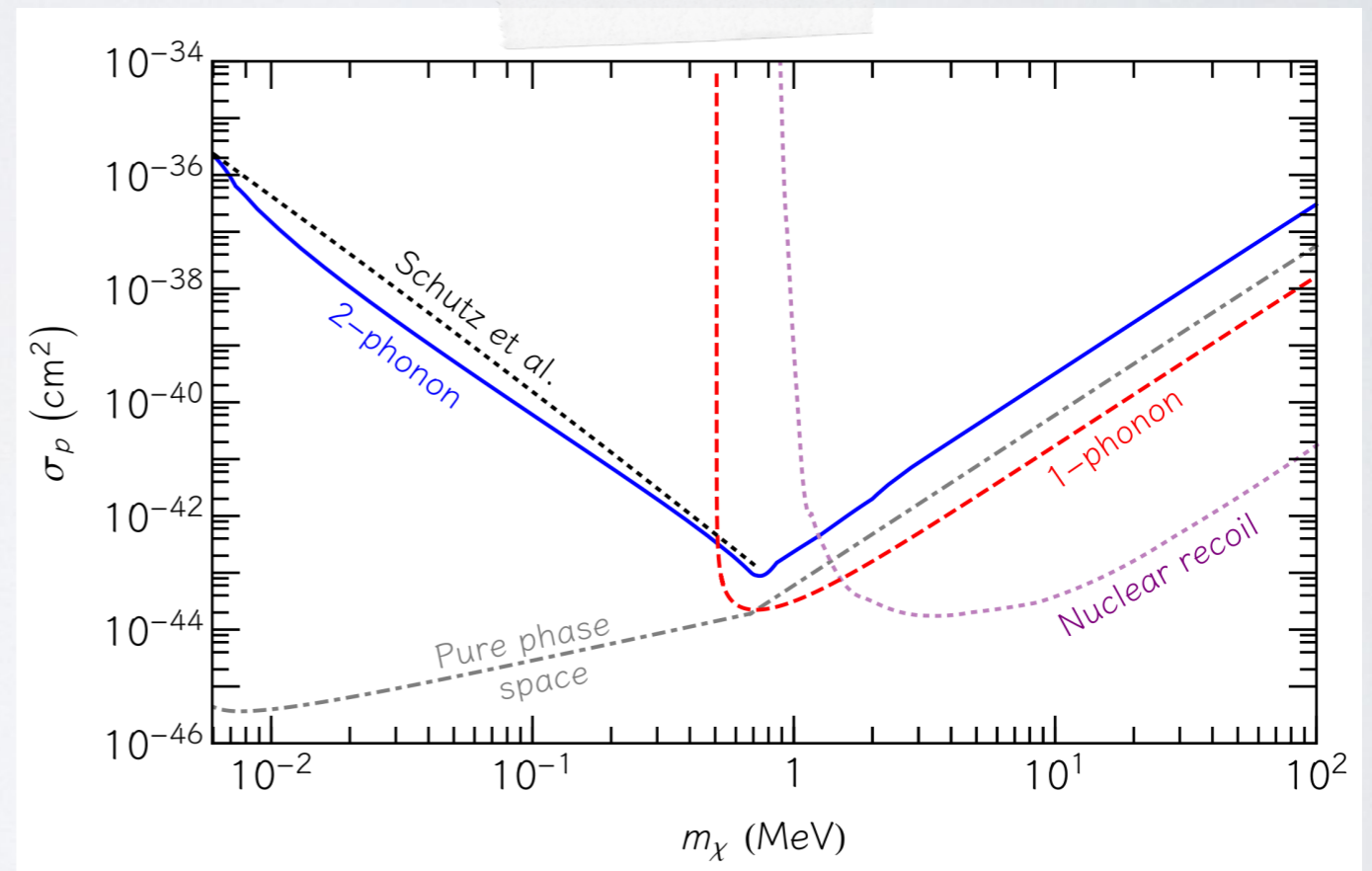
- We can now use **standard QFT methods** to compute event rates



$$\begin{aligned}
 &= g_1 (\omega_1 \mathbf{q}_2 \cdot \mathbf{q}_3 + \omega_2 \mathbf{q}_1 \cdot \mathbf{q}_3 + \omega_3 \mathbf{q}_1 \cdot \mathbf{q}_2) \\
 &\quad + g_2 \omega_1 \omega_2 \omega_3, \\
 &= i\lambda_1 (\mathbf{q}_1 \cdot \mathbf{q}_2 \mathbf{q}_3 \cdot \mathbf{q}_4 + \mathbf{q}_1 \cdot \mathbf{q}_3 \mathbf{q}_2 \cdot \mathbf{q}_4 \\
 &\quad + \mathbf{q}_1 \cdot \mathbf{q}_4 \mathbf{q}_2 \cdot \mathbf{q}_3) \\
 &\quad + i\lambda_2 (\omega_1 \omega_2 \mathbf{q}_3 \cdot \mathbf{q}_4 + \omega_1 \omega_3 \mathbf{q}_2 \cdot \mathbf{q}_4 \\
 &\quad + \omega_1 \omega_4 \mathbf{q}_2 \cdot \mathbf{q}_3 + \omega_2 \omega_3 \mathbf{q}_1 \cdot \mathbf{q}_4 \\
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 &\quad + i\lambda_3 \omega_1 \omega_2 \omega_3 \omega_4,
 \end{aligned}$$



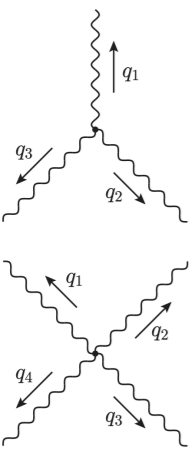
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 &\quad + \omega_3 \mathbf{q}_1 \cdot \mathbf{q}_2) + \gamma_2 \omega_1 \omega_2 \omega_3].
 \end{aligned}$$



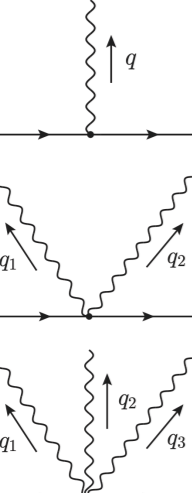
[Acanfora, **AE**, Polosa – EPJC 2019, 1902.02361;
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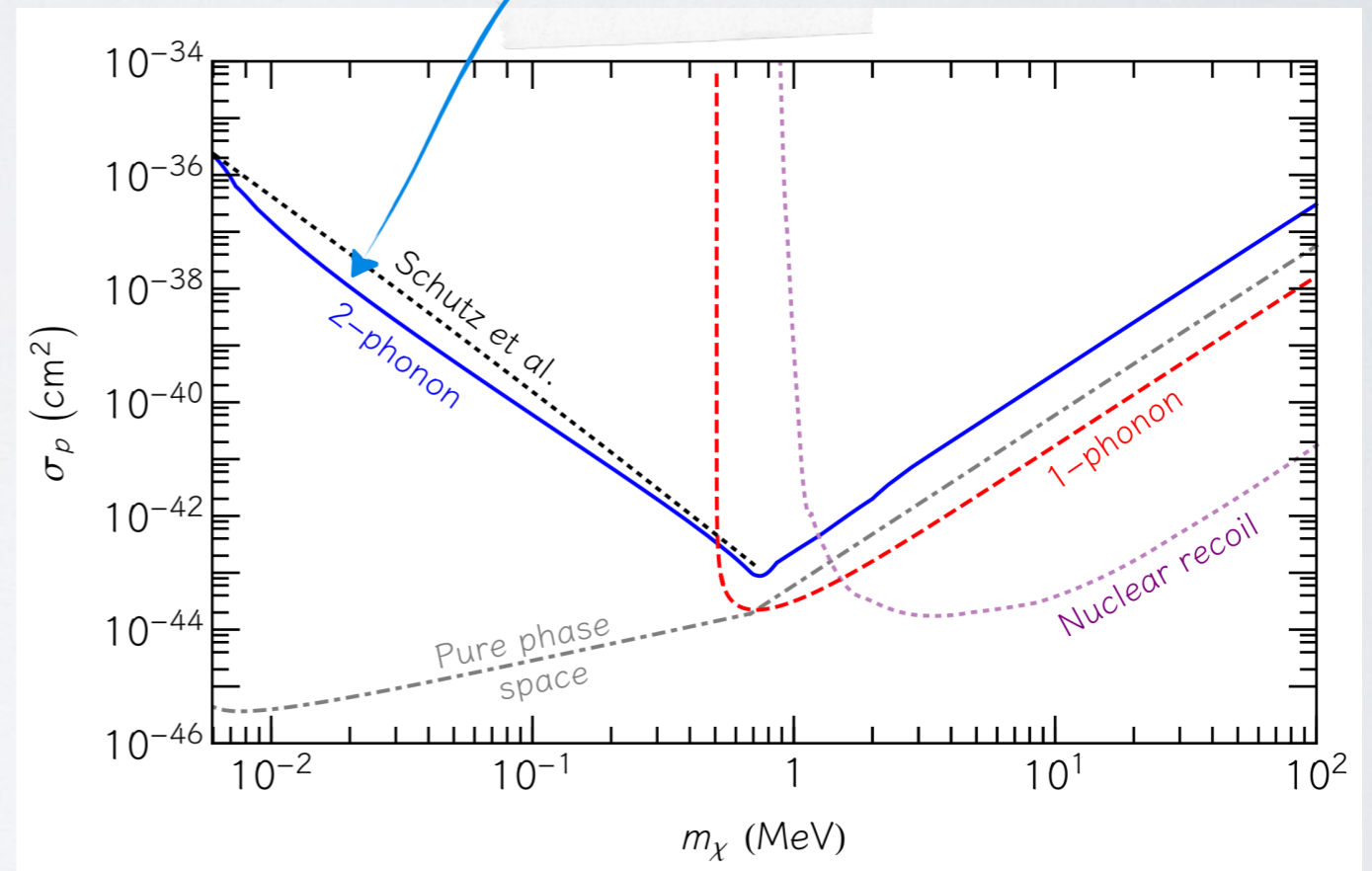


$$\begin{aligned}
 &= g_1 (\omega_1 \mathbf{q}_2 \cdot \mathbf{q}_3 + \omega_2 \mathbf{q}_1 \cdot \mathbf{q}_3 + \omega_3 \mathbf{q}_1 \cdot \mathbf{q}_2) \\
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 &= i\lambda_1 (\mathbf{q}_1 \cdot \mathbf{q}_2 \mathbf{q}_3 \cdot \mathbf{q}_4 + \mathbf{q}_1 \cdot \mathbf{q}_3 \mathbf{q}_2 \cdot \mathbf{q}_4 \\
 &\quad + \mathbf{q}_1 \cdot \mathbf{q}_4 \mathbf{q}_2 \cdot \mathbf{q}_3) \\
 &\quad + i\lambda_2 (\omega_1 \omega_2 \mathbf{q}_3 \cdot \mathbf{q}_4 + \omega_1 \omega_3 \mathbf{q}_2 \cdot \mathbf{q}_4 \\
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 \end{aligned}$$

revise results obtained with traditional methods



[Acanfora, **AE**, Polosa – EPJC 2019, 1902.02361;
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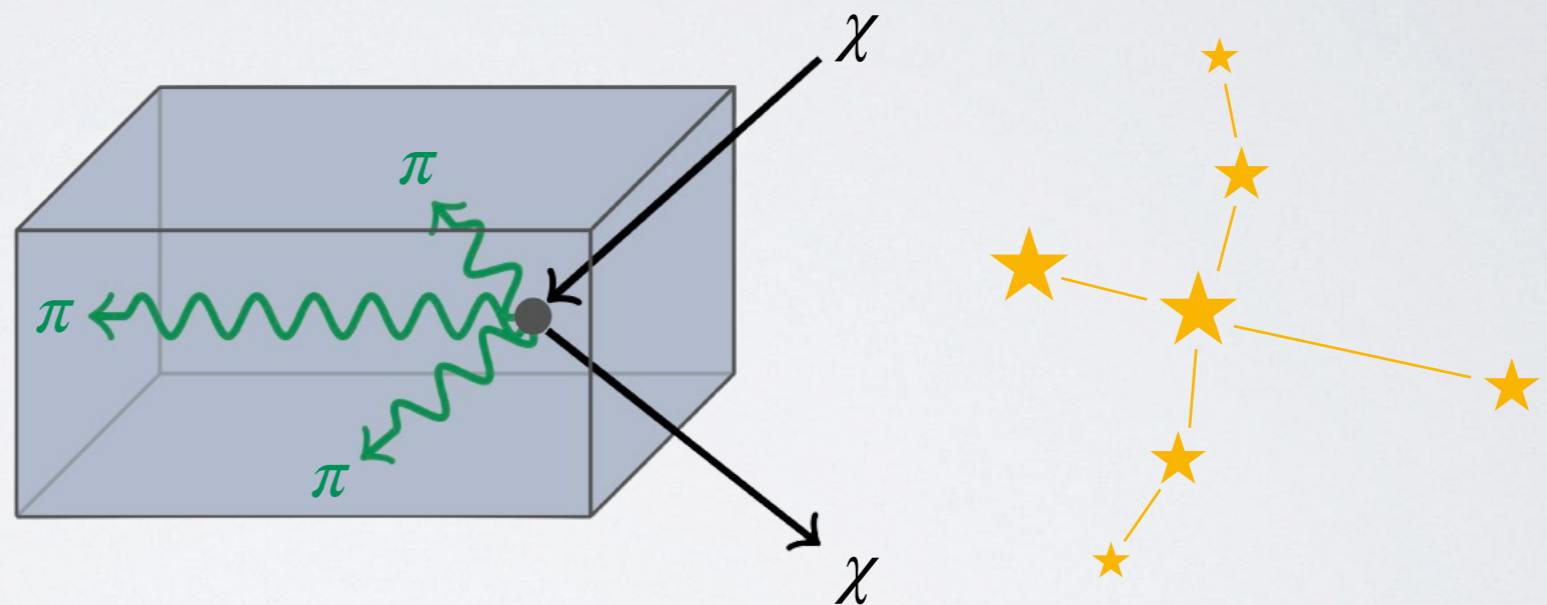
DIRECTIONALITY

DIRECTIONALITY

- EFT allows to also study more complicated signals

DIRECTIONALITY

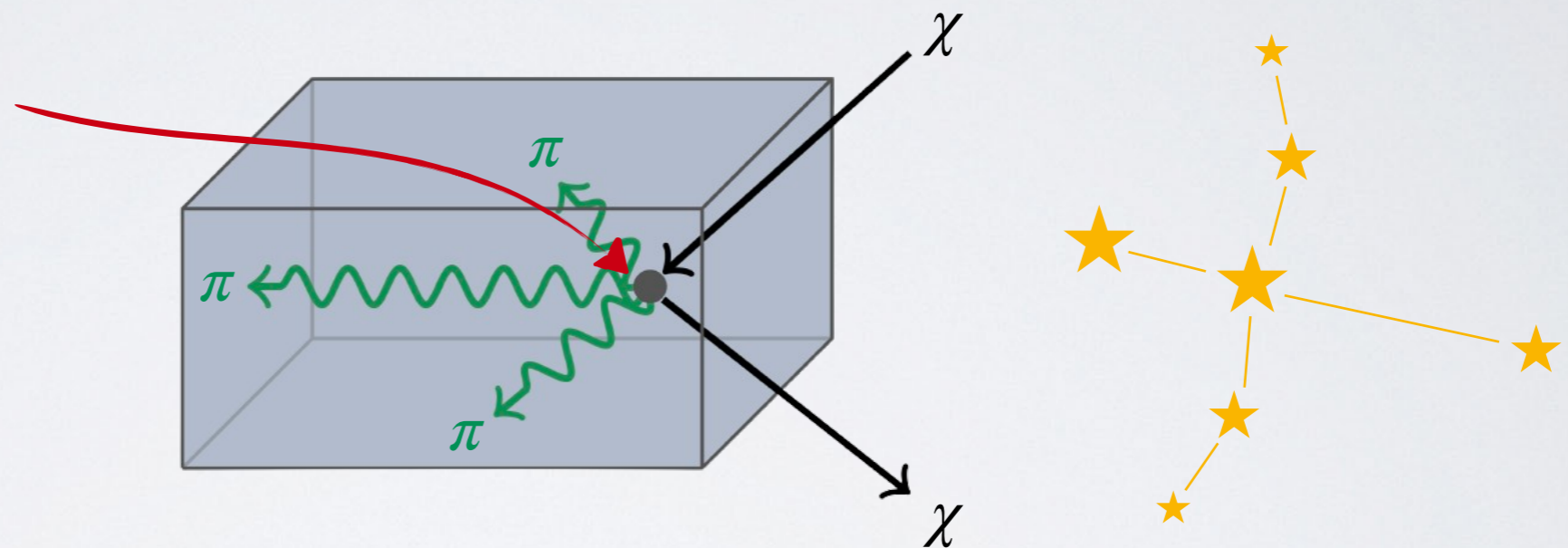
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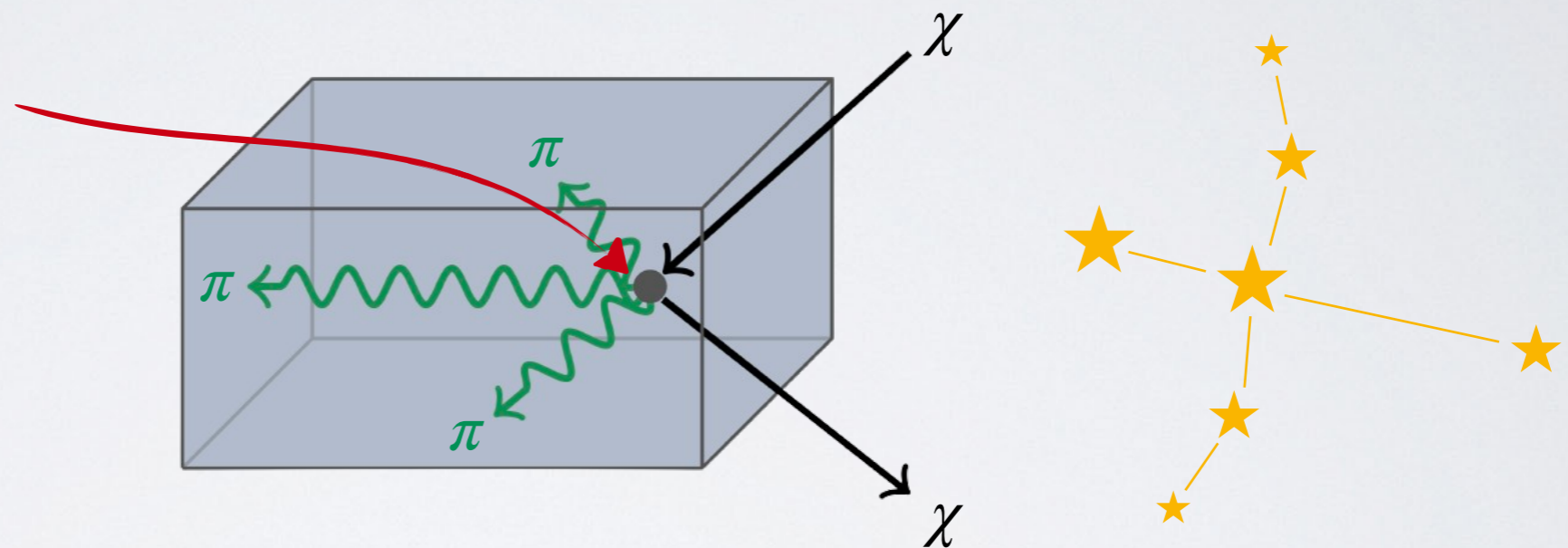
impossible with traditional methods, but very simple within EFT



DIRECTIONALITY

- EFT allows to also study more complicated signals

impossible with traditional methods, but very simple within EFT



- If not completely suppressed, this configuration would provide a coincident, directional signal \rightarrow optimal for background rejection

DIRECTIONALITY

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- We compute the 4-body, non-Lorentz invariant phase space using Monte Carlo techniques again borrowed from particle physics

DIRECTIONALITY

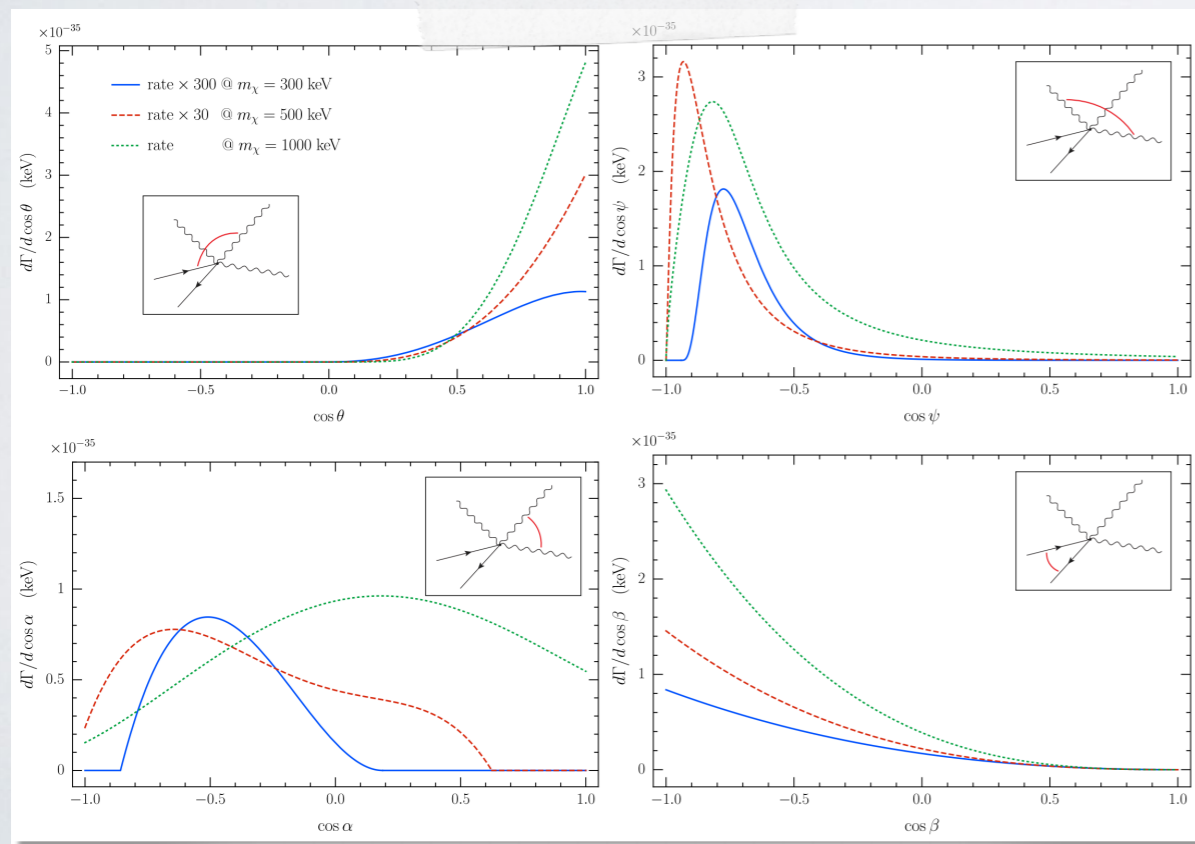
- We compute the 4-body, non-Lorentz invariant phase space using Monte Carlo techniques again borrowed from particle physics

$$d\Phi_4 \sim d^3p_f \prod_{i=1}^3 d^3q_i \delta\left(\frac{p_i^2}{2m_\chi} - \frac{p_f^2}{2m_\chi} - c_s q_1 - c_s q_2 - c_s q_3\right) \delta^{(3)}(\mathbf{p}_i - \mathbf{p}_f - \mathbf{q}_1 - \mathbf{q}_2 - \mathbf{q}_3)$$

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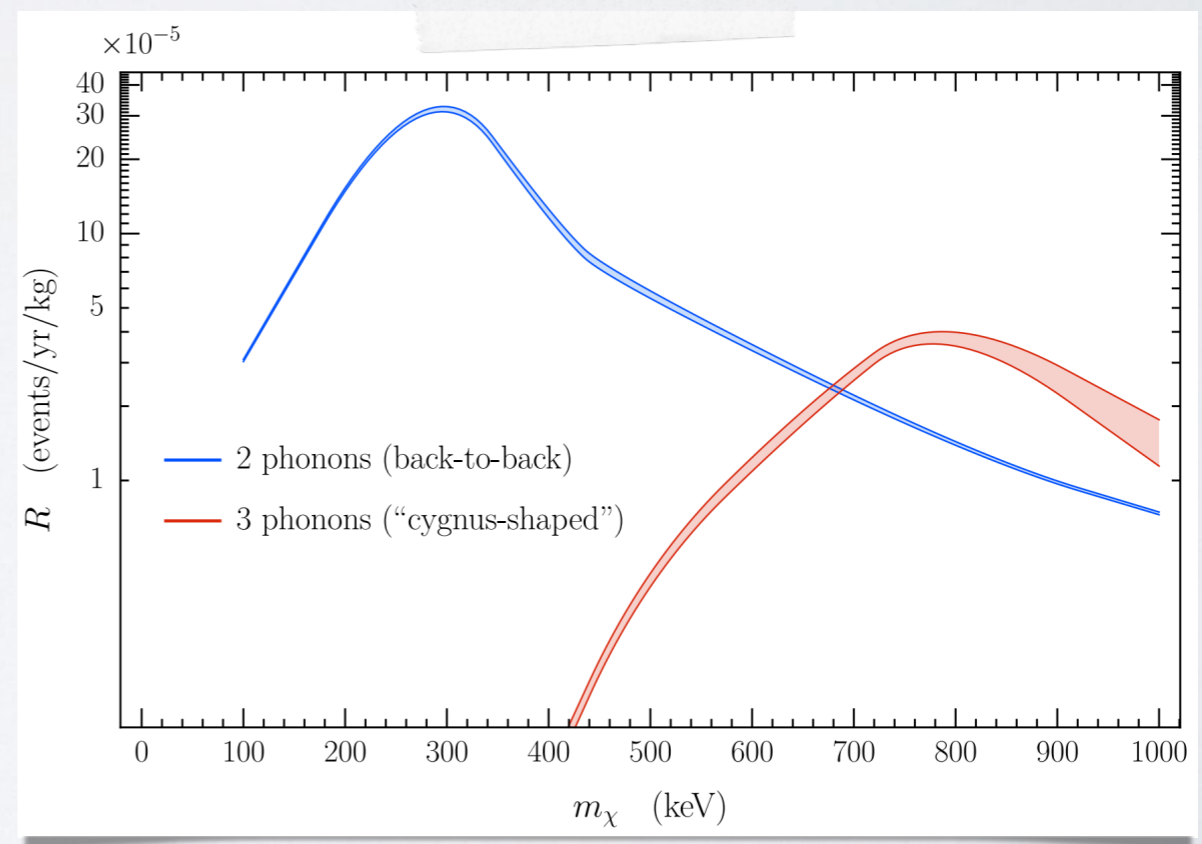
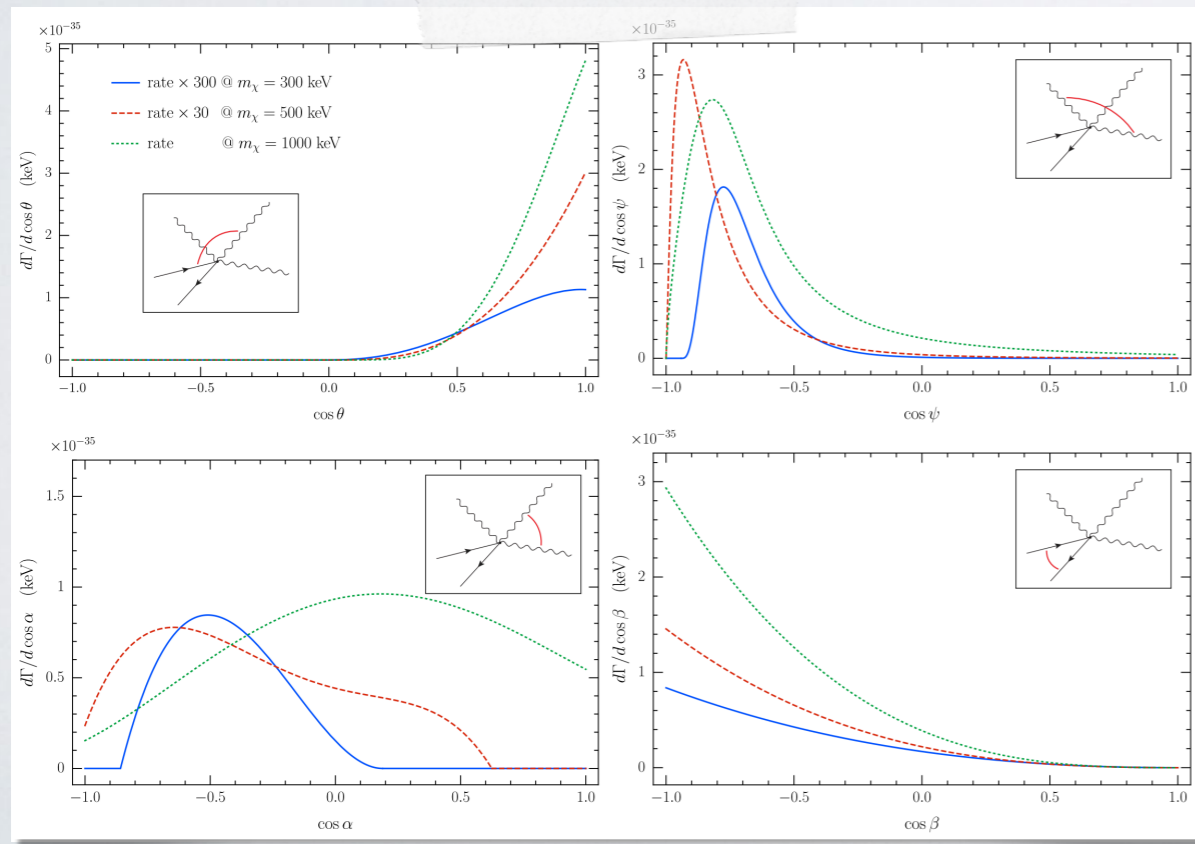
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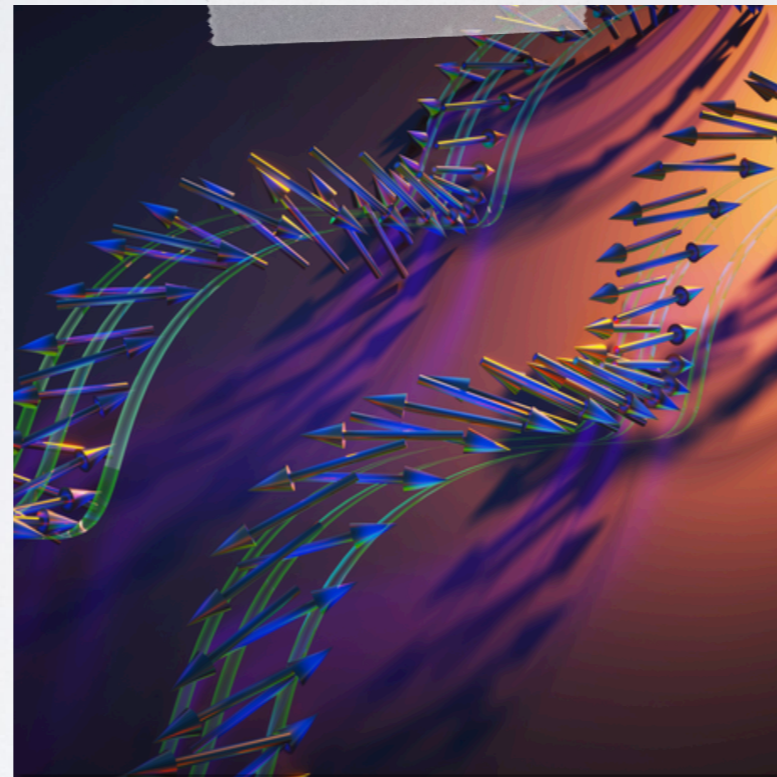
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[Caputo, **AE**, Piccini, Polosa, Rossi – PRD 2021, 2012.014321]

Spin-dependent interactions: anti-ferromagnets



[w/ Catinari, Pavaskar]

(ANTI-)FERROMAGNETS

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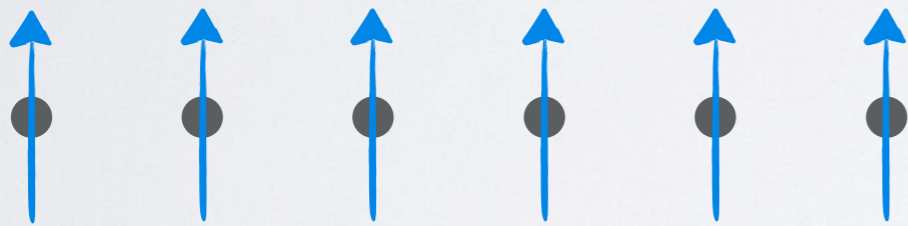
- How about dark matter with *spin-dependent interactions*?

(ANTI-)FERROMAGNETS

- How about dark matter with *spin-dependent interactions*?
- A possibility is to look for the interaction between dark matter and *spin-ordered systems*

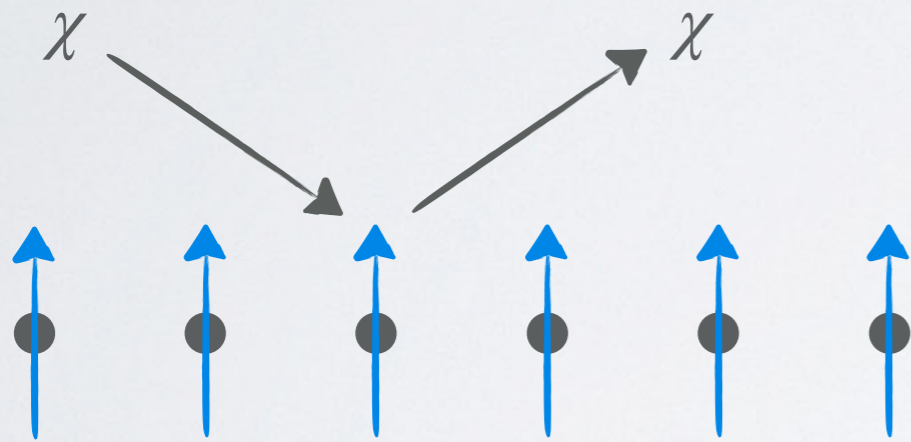
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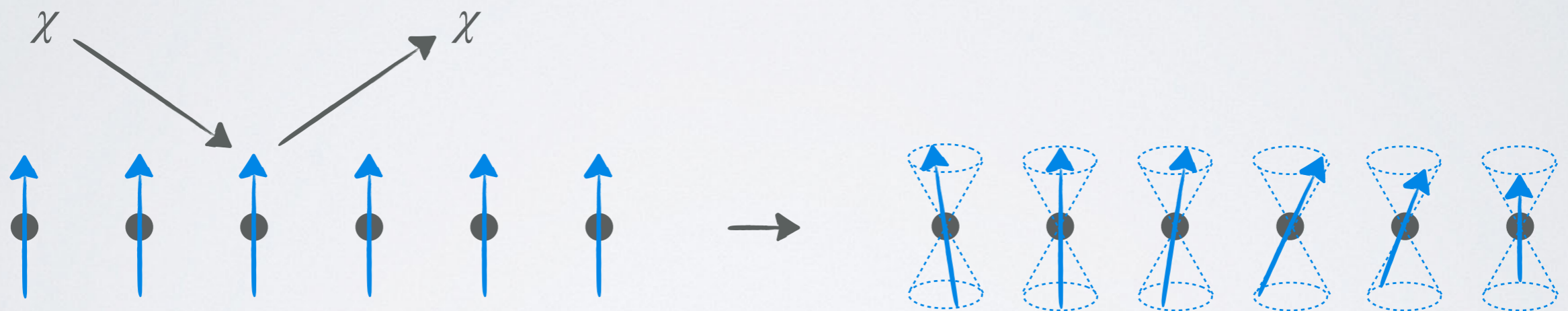
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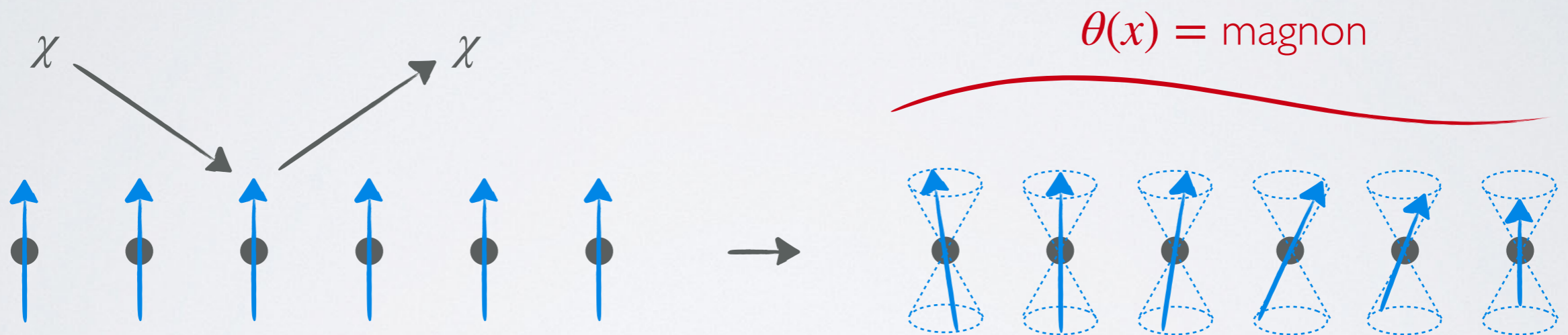
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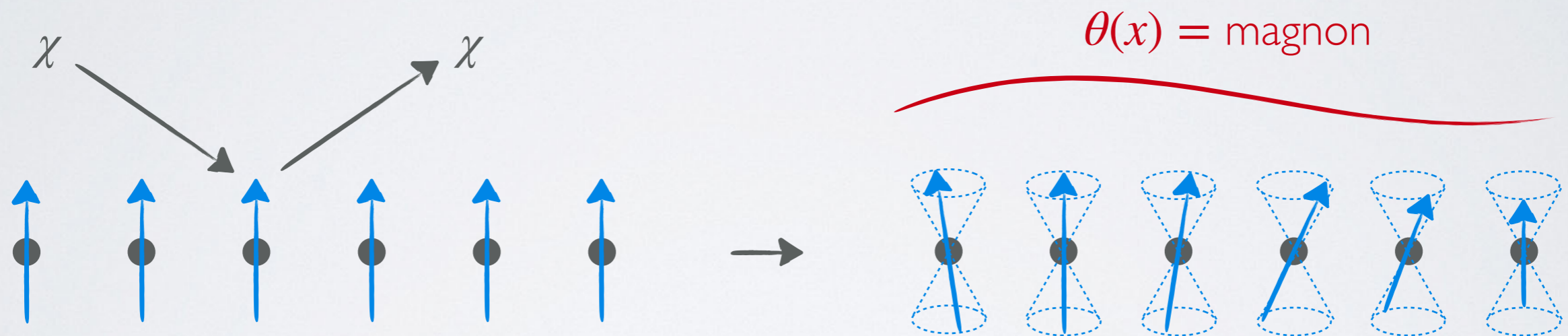
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- How about dark matter with *spin-dependent interactions*?
- A possibility is to look for the interaction between dark matter and *spin-ordered systems*



- Ways to detect few magnons have been proposed (TES? SQUIDs? quantum sensors? cavities?)

[Trickle, Zhang, Zurek – PRL 2020, 1905.13744; Lachance-Quirion et al. – Science Advances 2017; Lachance-Quirion et al. – Science 2020]

DM-SPIN INTERACTION

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- At low energies **dark matter couples to *spin density field***
- Two benchmark models:

$$\mathcal{L}_{\text{m.d.}} \sim V_{\mu\nu} \bar{\chi} \sigma^{\mu\nu} \chi + V_{\mu} \bar{e} \gamma^{\mu} e$$

[e.g., Sigurdson et al. – PRD 2004, astro-ph/0406355; Chang, Weiner, Yavin – PRD 2010, 1007.4200]

$$\mathcal{L}_{\text{p.m.}} \sim \phi \bar{\chi} \chi + \phi \bar{e} i \gamma^5 e$$

[e.g., Banks, Fortin, Thomas – 1007.5515; Bagnasco, Dine, Thomas – PLB 1994, hep-ph/9310290]

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- For a non-relativistic system, at low energies:

$$\mathcal{L}_{\text{m.d.}} \rightarrow \chi^{\dagger} \sigma^i \chi (\delta^{ij} - \nabla^{-2} \nabla^i \nabla^j) s_i$$

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spin density



FERROMAGNETS

FERROMAGNETS

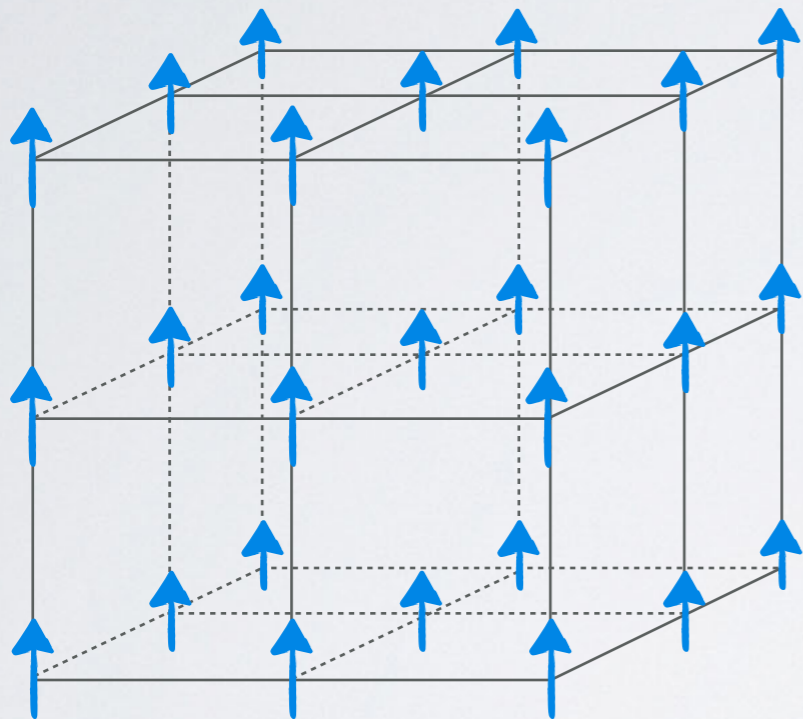
- First proposed to use ferromagnets

[Trickle, Zhang, Zurek – PRL 2020, 1905.13744; Mitridate et al. – PRD 2020, 2005.10256;
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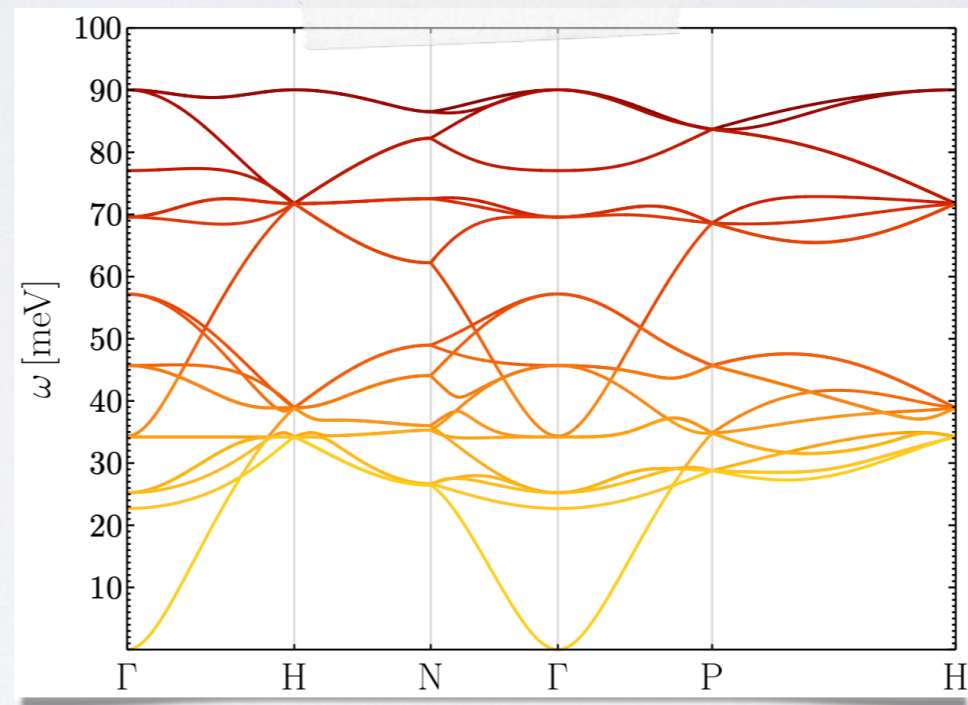
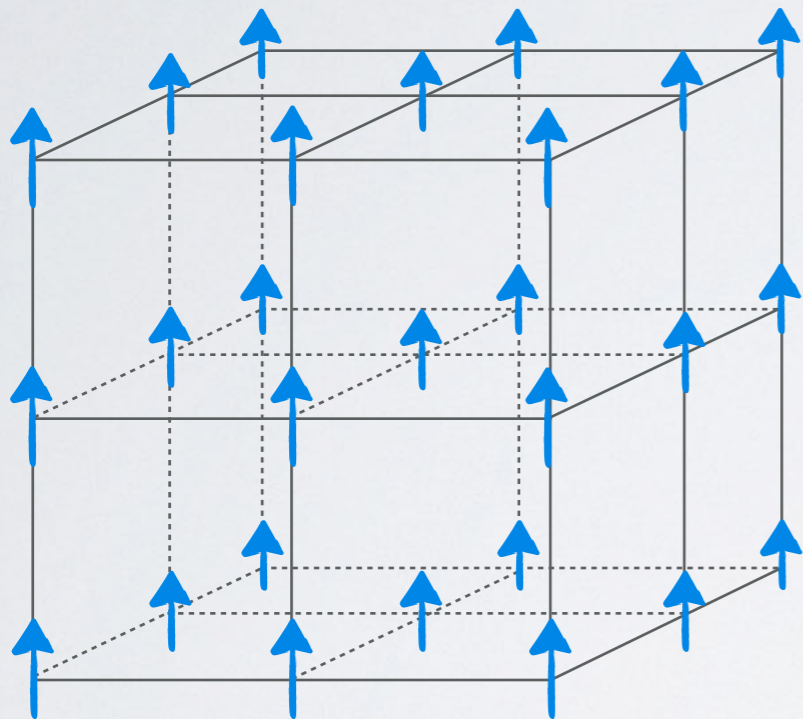
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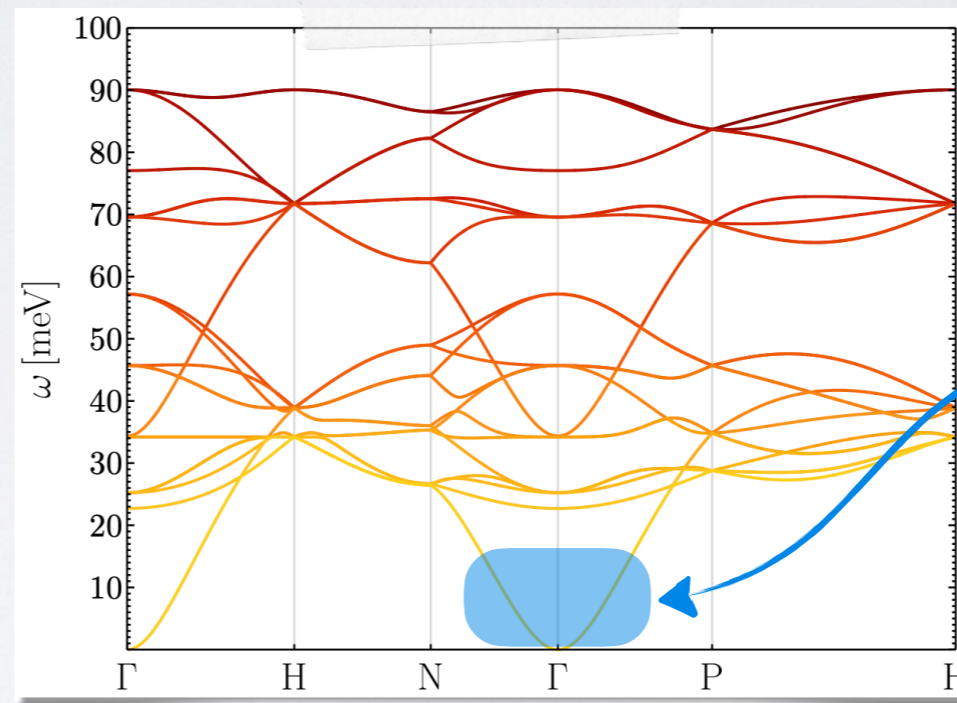
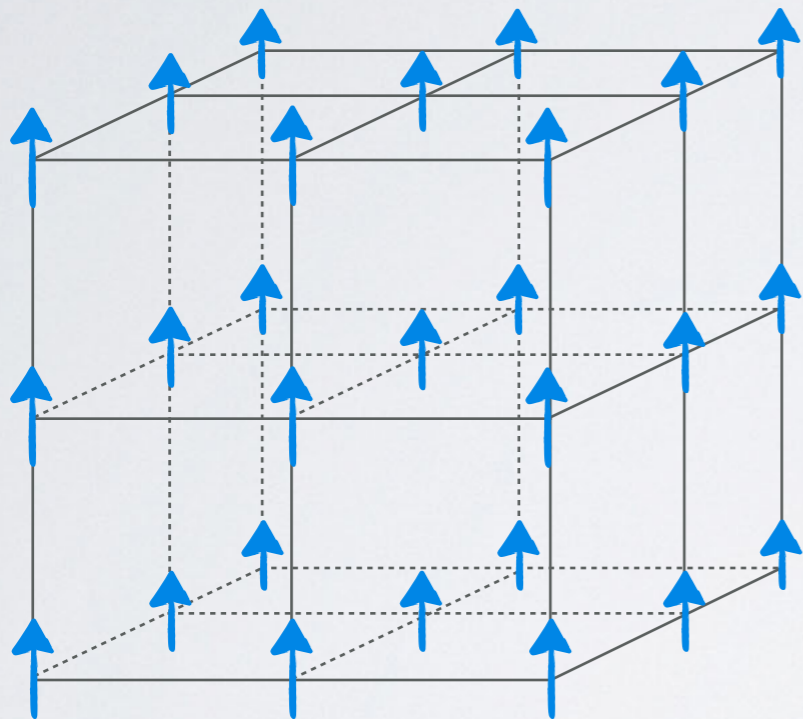
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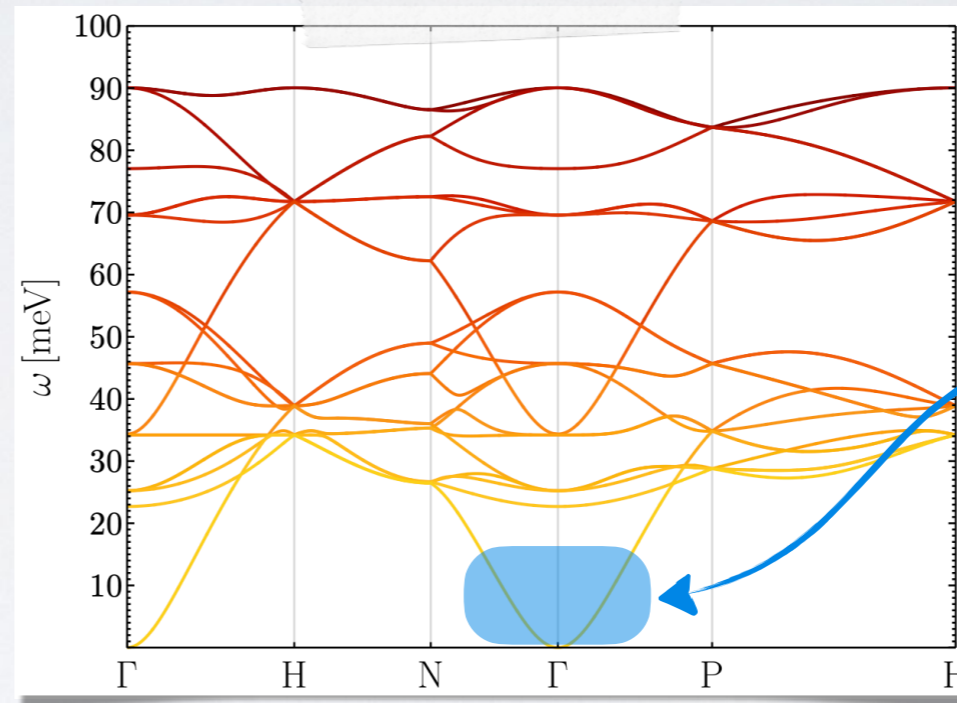
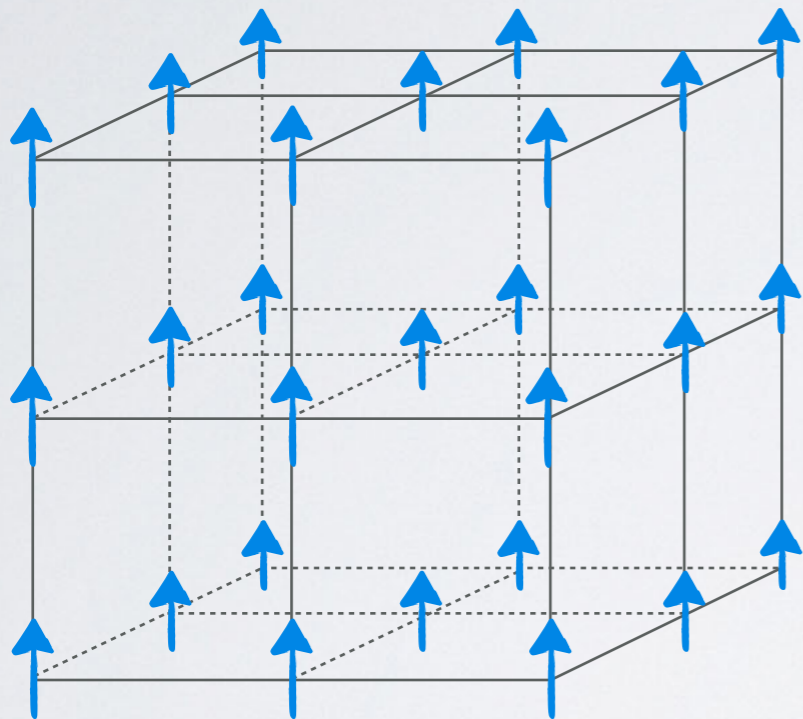


for $m_\chi \lesssim 10$ MeV only
 gapless magnons
 $\omega(q) = q^2 / (2m_\theta)$

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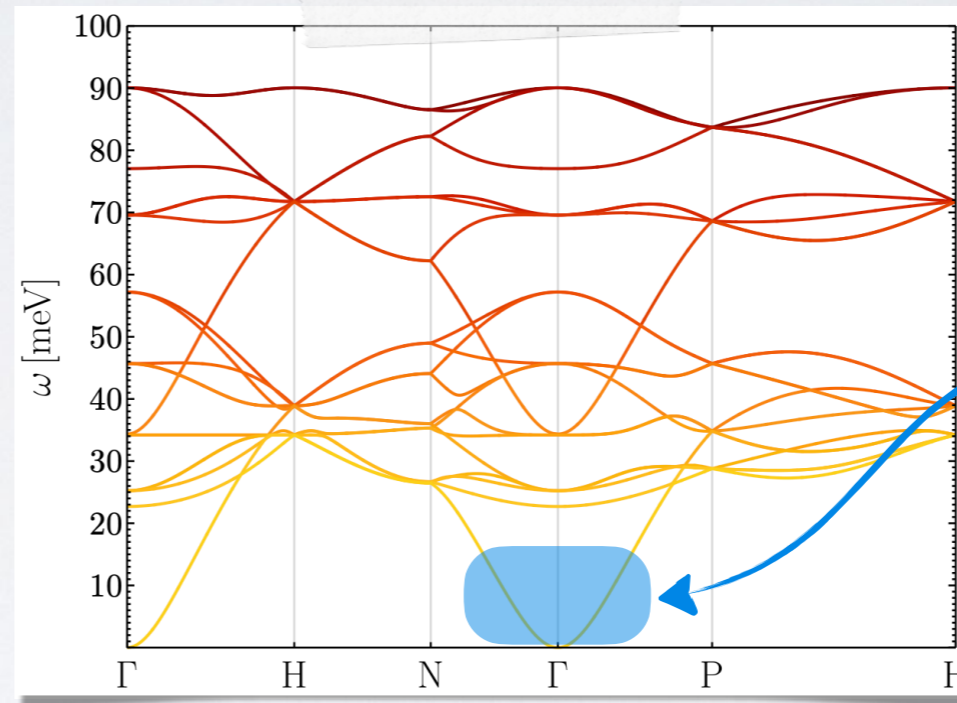
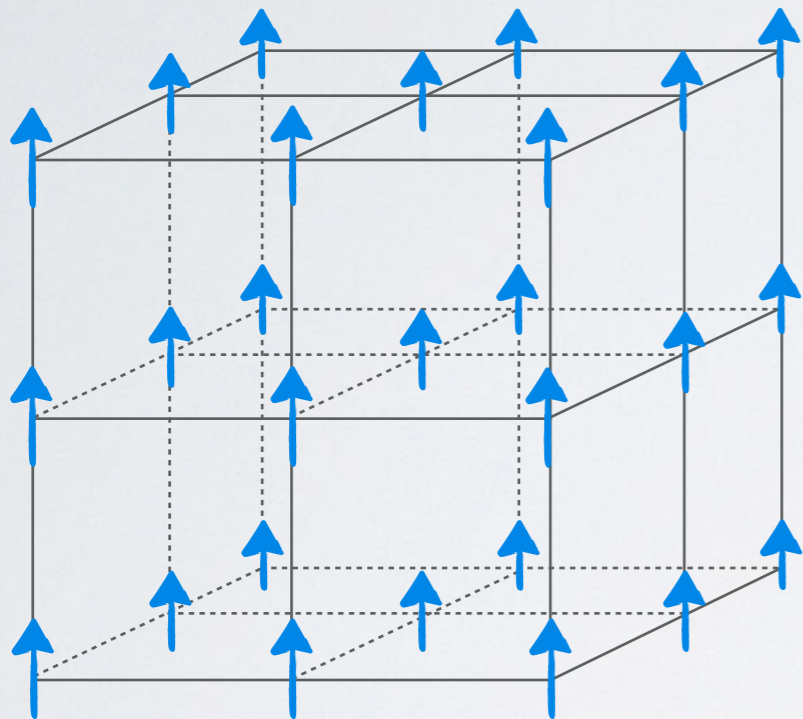
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- Conservation of magnetization → only one magnon emitted

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for $m_\chi \lesssim 10$ MeV only
gapless magnons
 $\omega(q) = q^2 / (2m_\theta)$

- Conservation of magnetization \rightarrow only one magnon emitted

$$\omega_{\max} \simeq 4 \frac{m_\theta}{m_\chi} E_\chi \quad \text{with} \quad m_\theta \sim 1 \text{ MeV}$$

\rightarrow inefficient for
 $m_\chi \lesssim 1$ MeV

FERROMAGNETS

FERROMAGNETS

- Compute the magnon emission rate

FERROMAGNETS

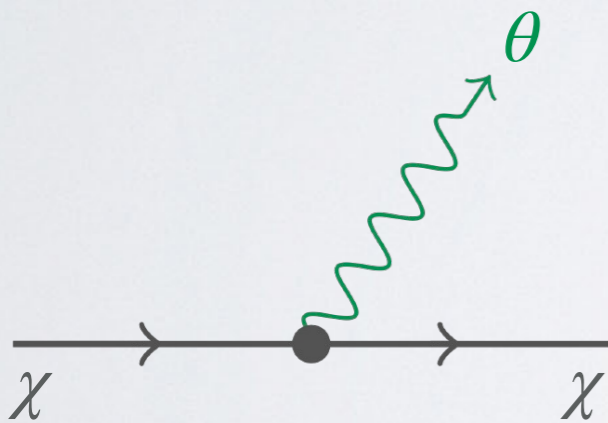
- Compute the magnon emission rate
- **Traditional approach:** quantize the Heisenberg model

$$H = \frac{1}{2} \sum_{\ell, \ell'}^N \sum_{j, j'}^n J_{\ell \ell' j j'} \mathbf{S}_{\ell j} \cdot \mathbf{S}_{\ell' j'} \rightarrow \sum_{\nu=1}^n \sum_{\mathbf{q} \in 1\text{BZ}} \omega_{\nu, \mathbf{q}} b_{\nu, \mathbf{q}}^\dagger b_{\nu, \mathbf{q}}$$

FERROMAGNETS

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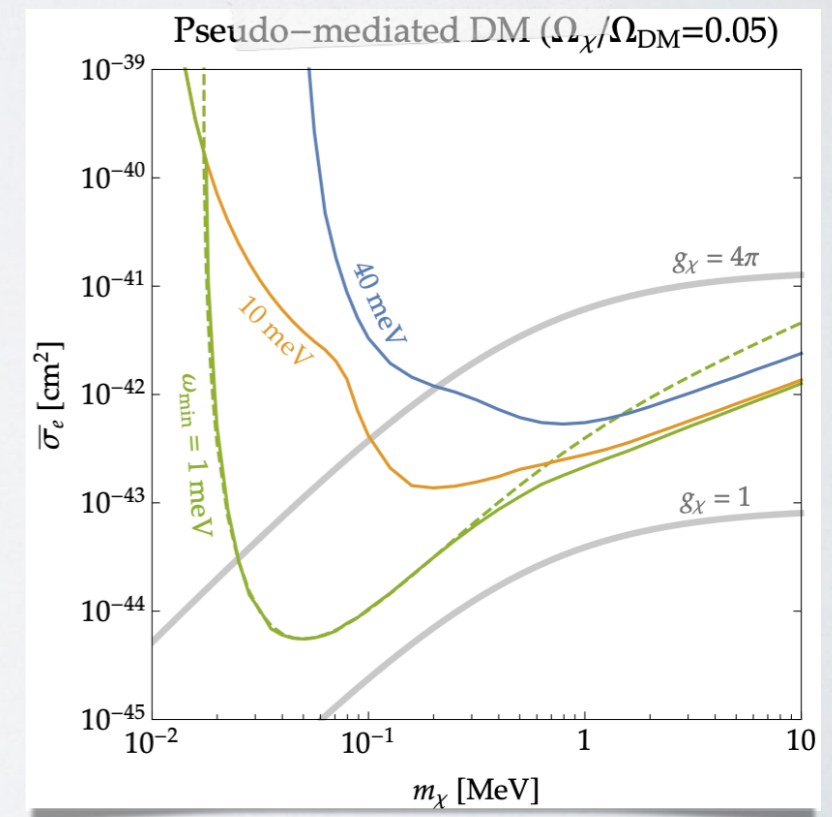
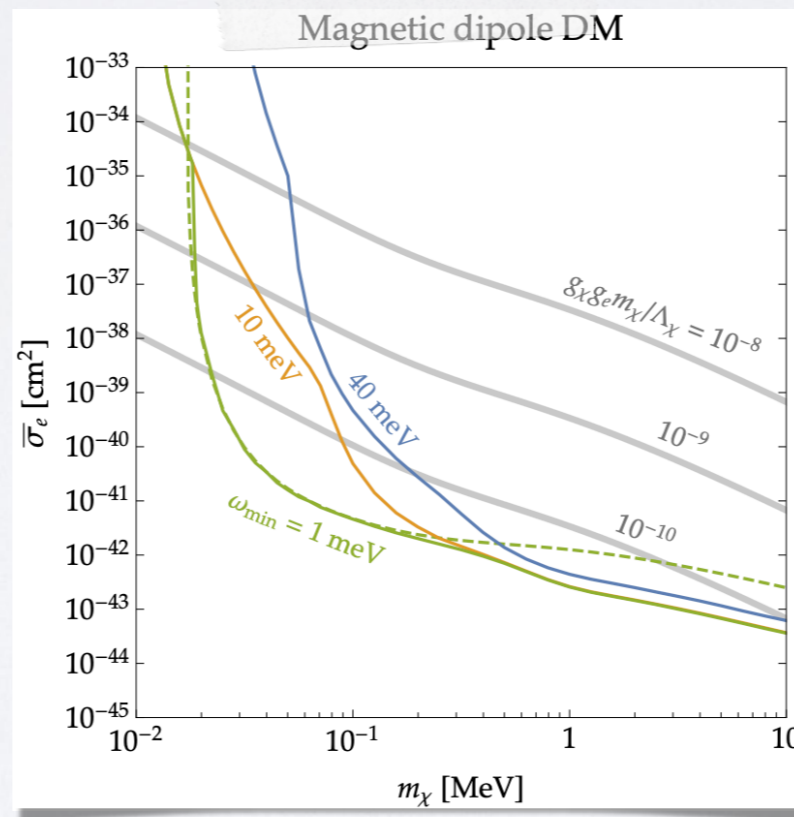
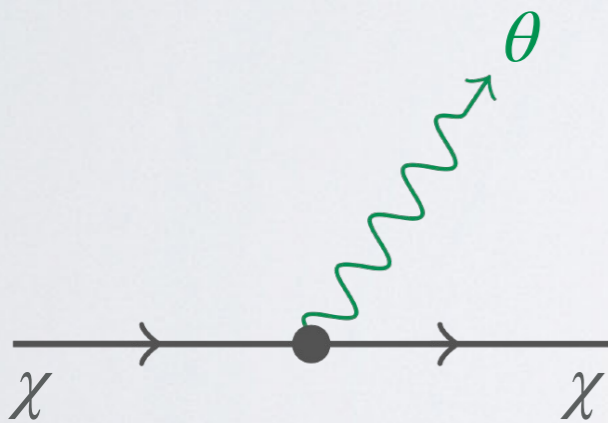
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FERROMAGNETS

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[Trickle, Zhang, Zurek – PRL 2020, 1905.13744]

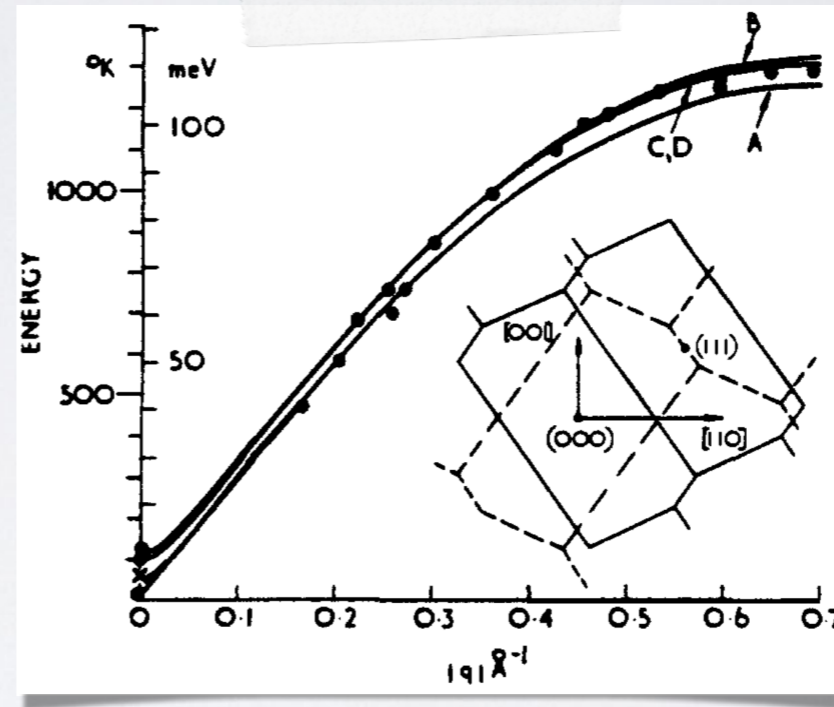
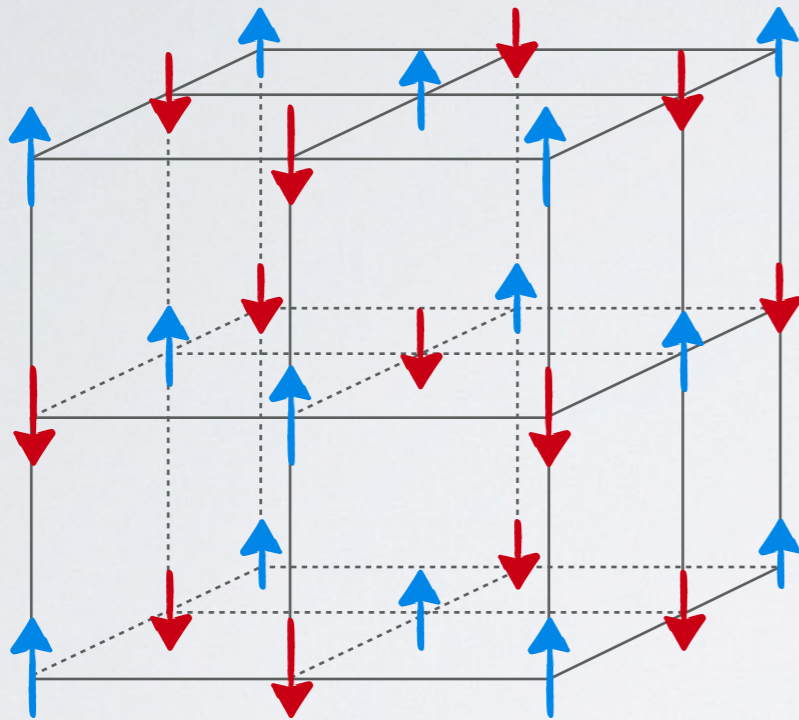
ANTI-FERROMAGNETS

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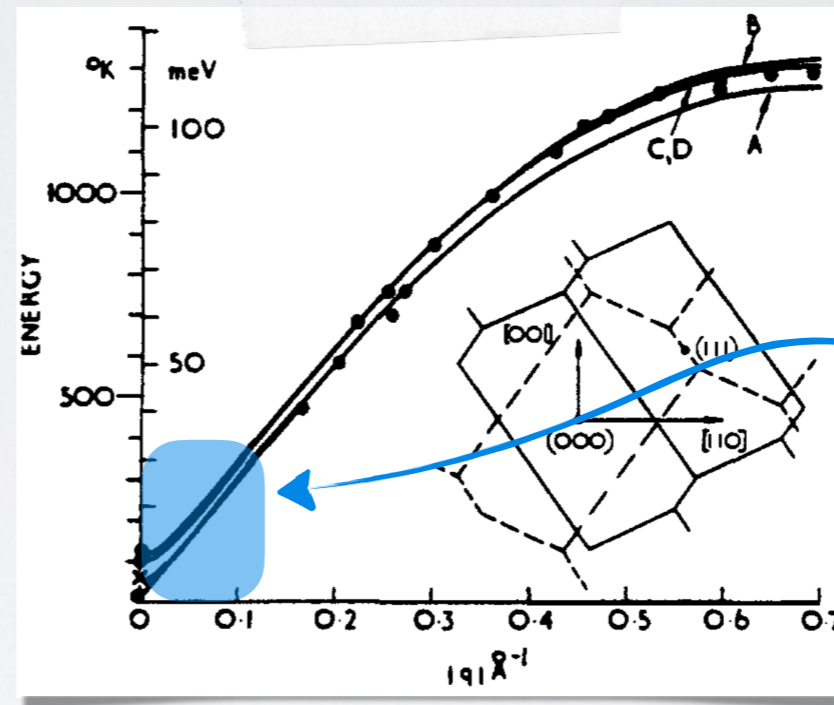
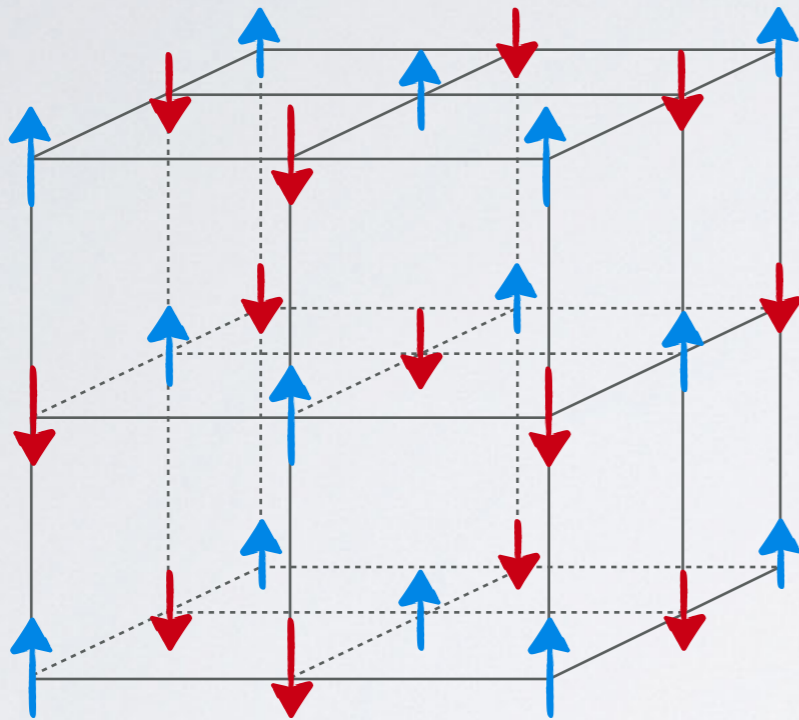
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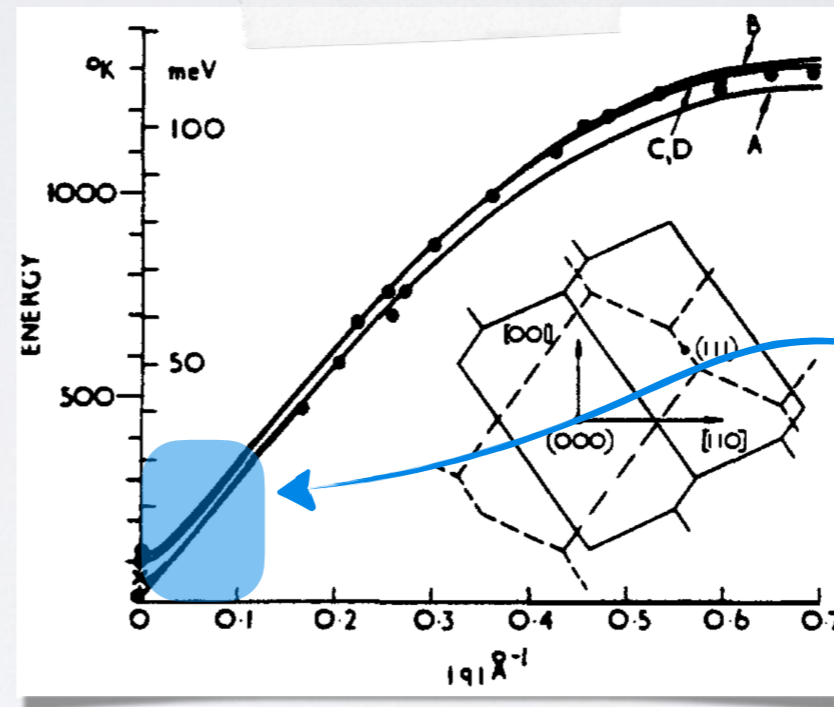
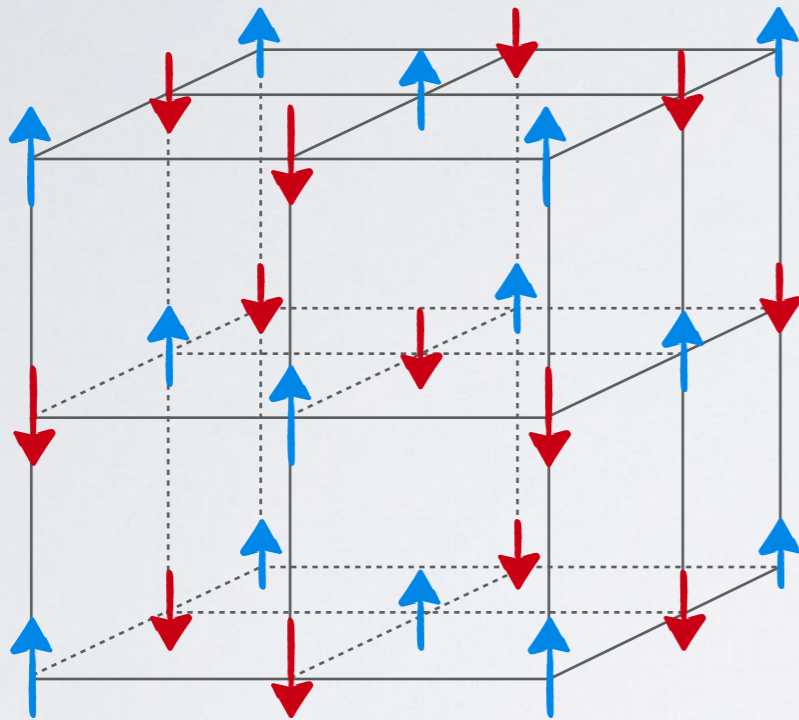
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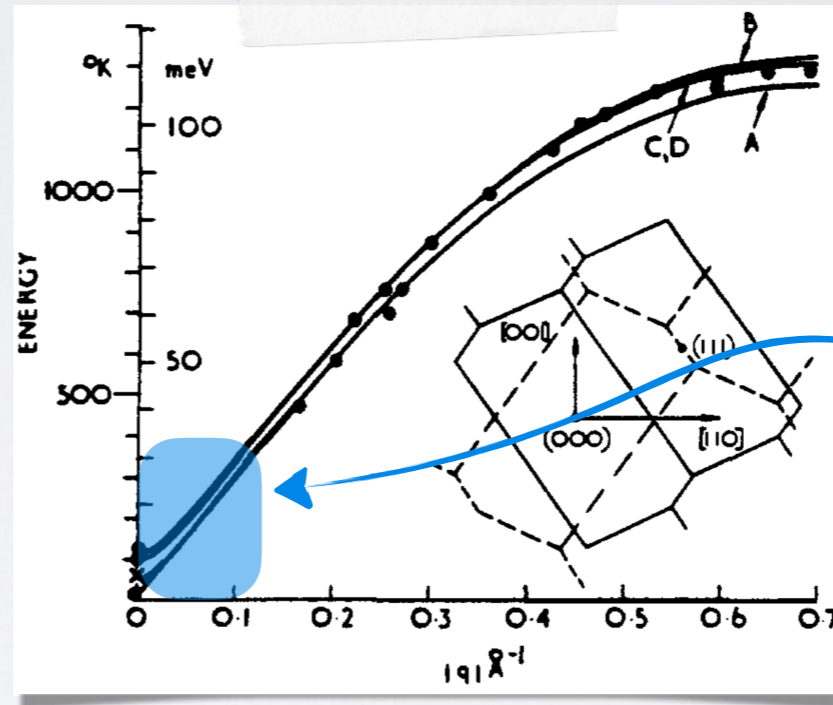
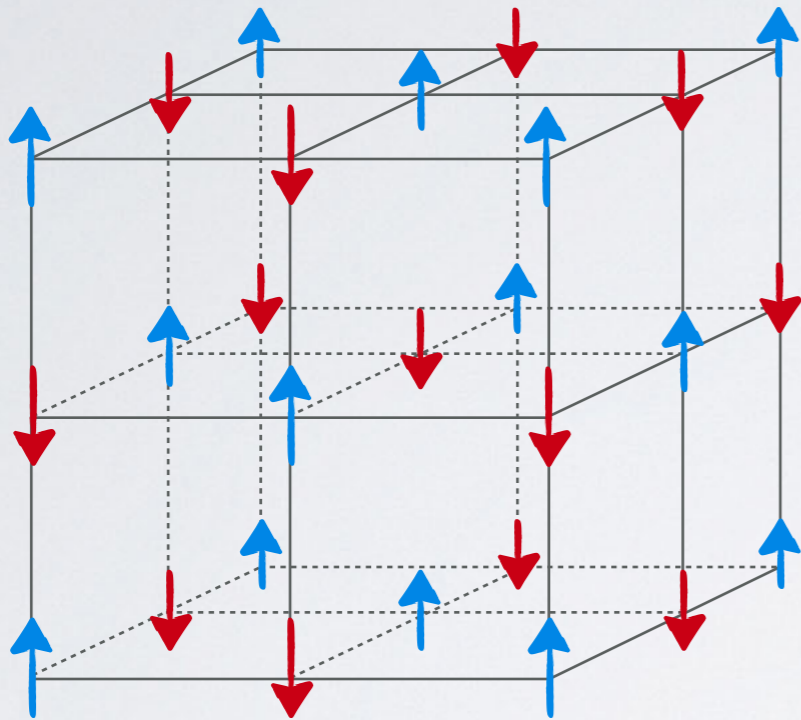


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- Nickel-oxide has $v_\theta \sim 0.1 v_\chi \rightarrow$ very efficient at absorbing dark matter energy

[AE, Pavaskar – PRD (2023), 2210.13516]

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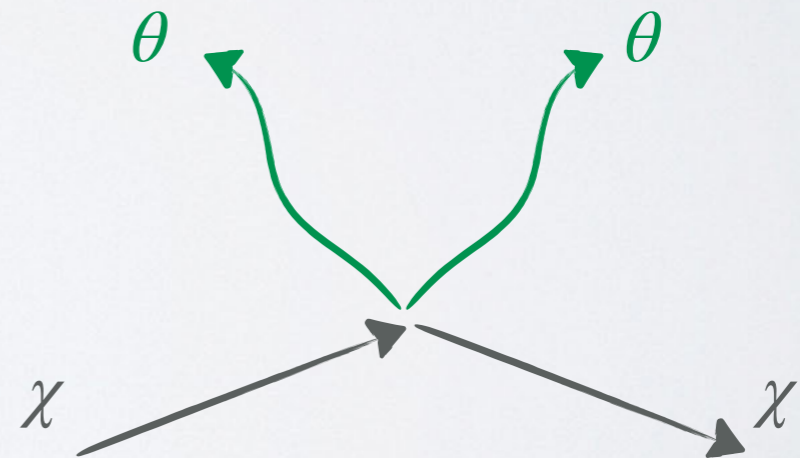
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- **Multi-magnon emission process** evade the kinematical constraints and **get down to $m_\chi \sim \mathcal{O}(\text{keV})$**



MAGNONS

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- Anti-ferromagnets spontaneously break internal spin symmetry

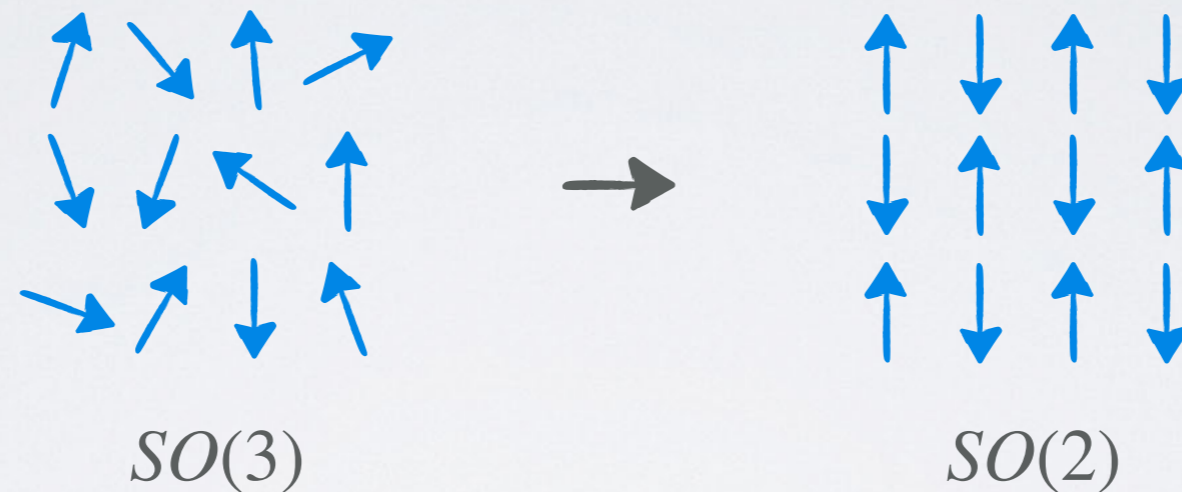
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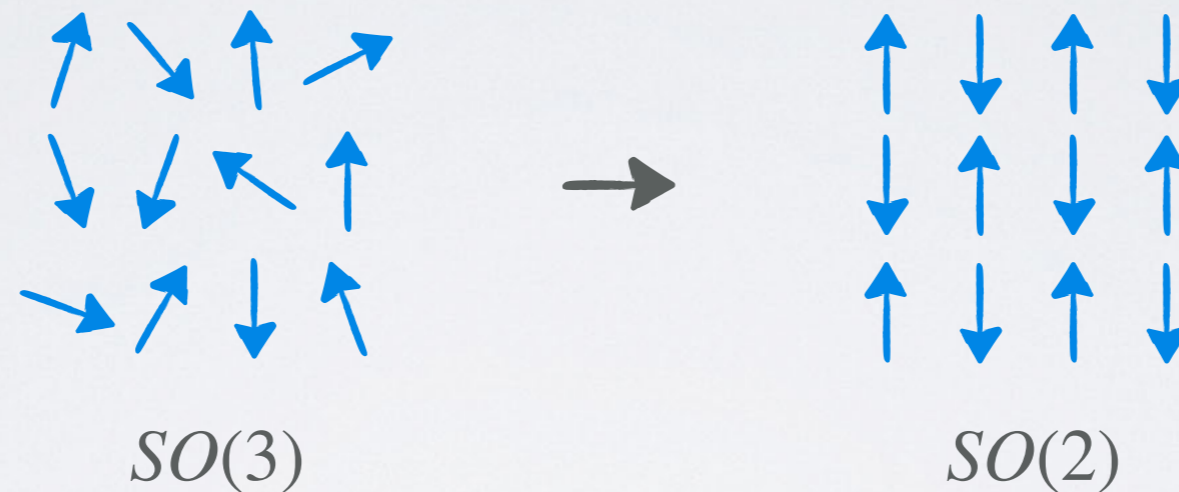
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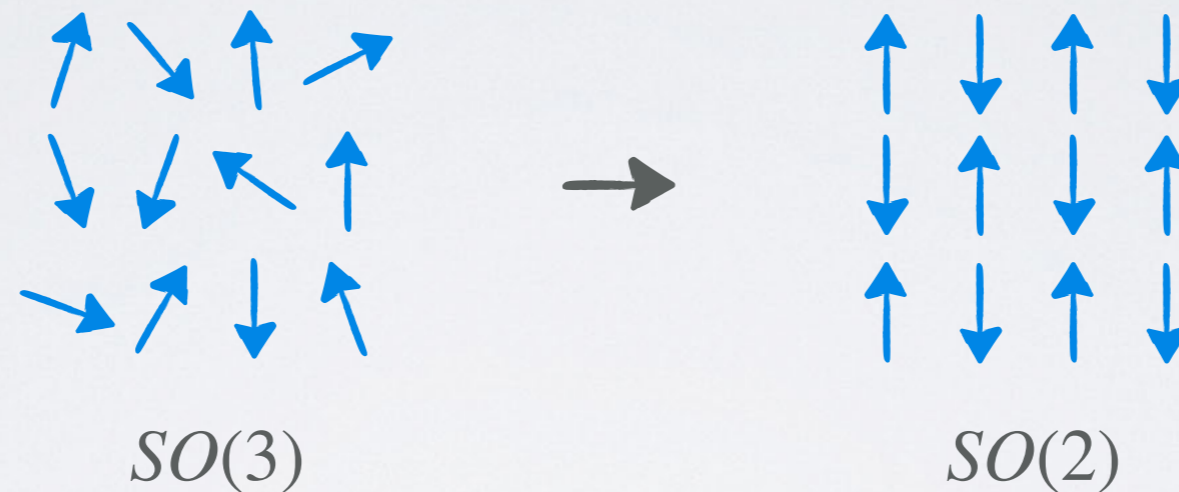
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Gapless magnon = Goldstone

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- At low energies/momenta magnons can be described by an EFT, invariant under the full symmetry group

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can be extracted from
dispersion relation +
neutron scattering data

$$v_\theta = c_2/c_1$$

$$\sigma_n \propto c_1$$

[Pavaskar, Penco, Rothstein – SciPost Phys. (2022), 2112.13873; **AE**, Pavaskar – PRD (2023), 2210.13516]

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- Structure **completely dictated by symmetry** \rightarrow just need c_1
- This allows to **bypass difficulties in the standard treatment** (failure of the Holsten-Primakoff approach) [Dyson – Phys. Rev. 1956]

IDEAL REACH

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[[AE](#), Pavaskar – PRD (2023), 2210.13516]

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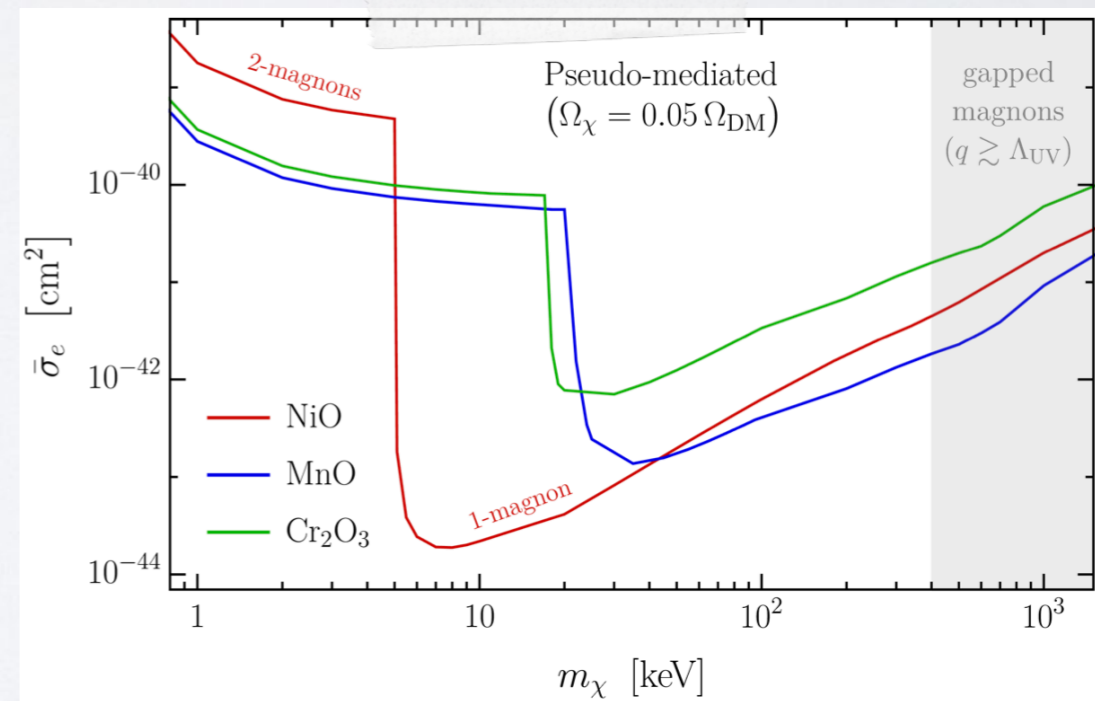
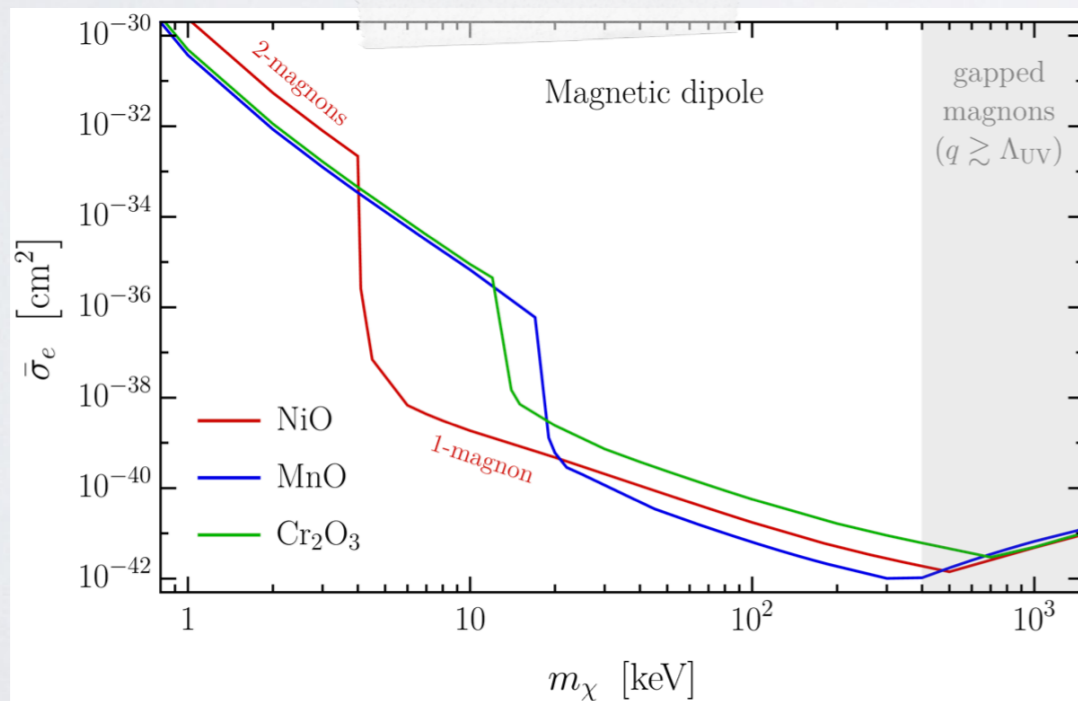
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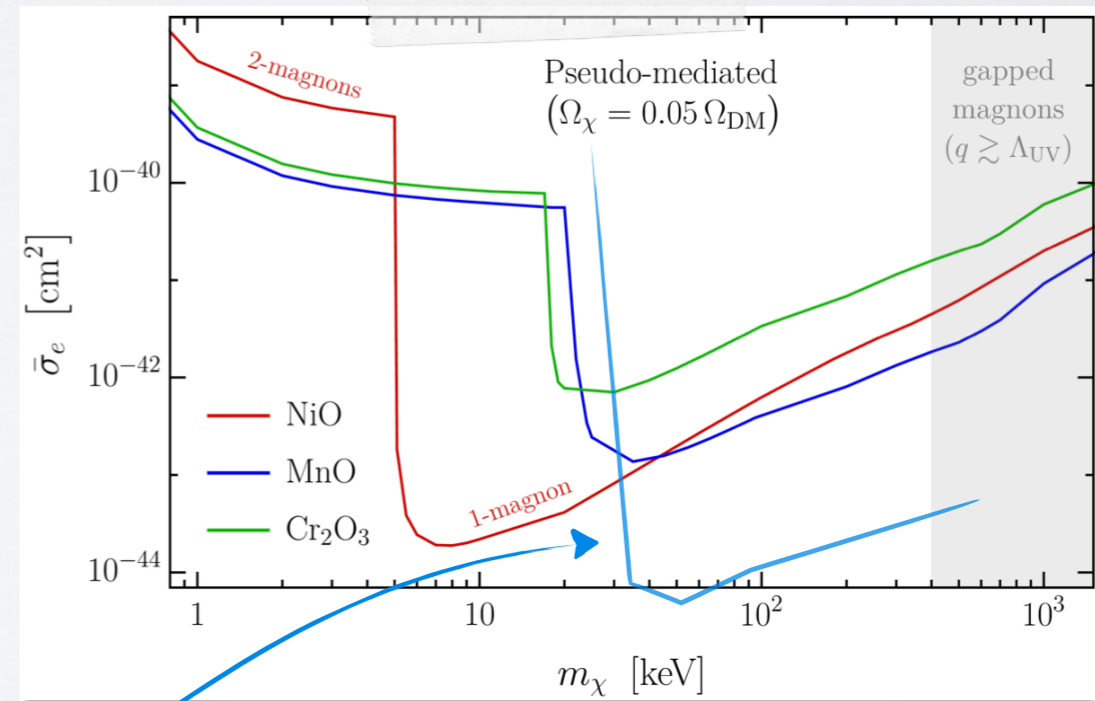
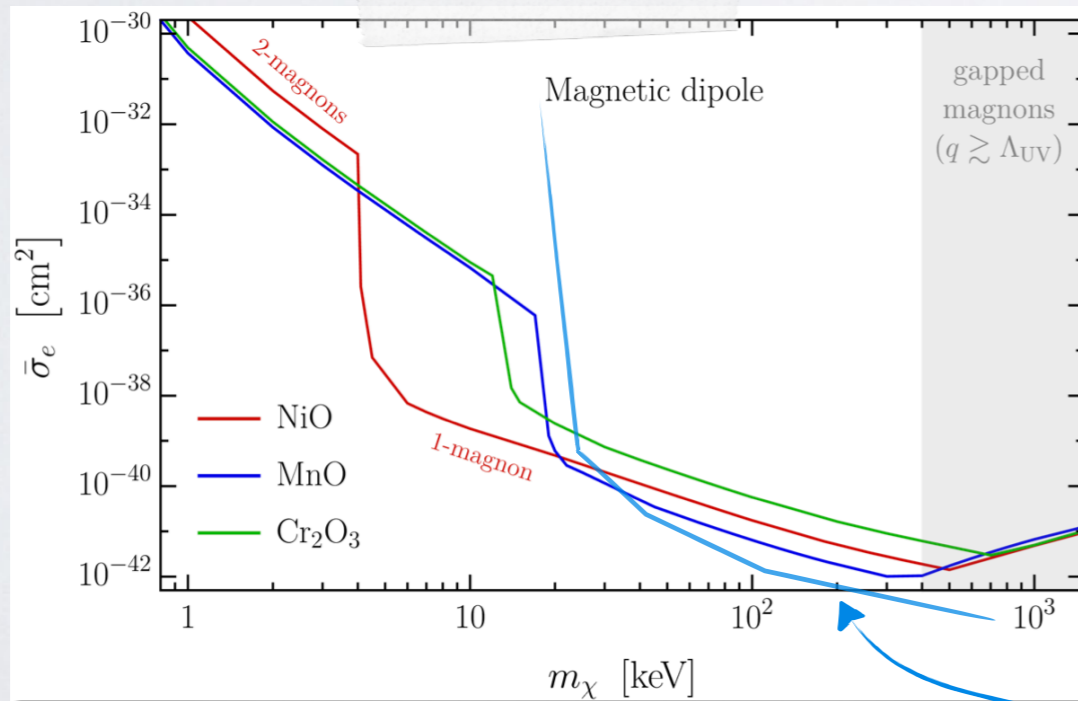


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ferromagnets

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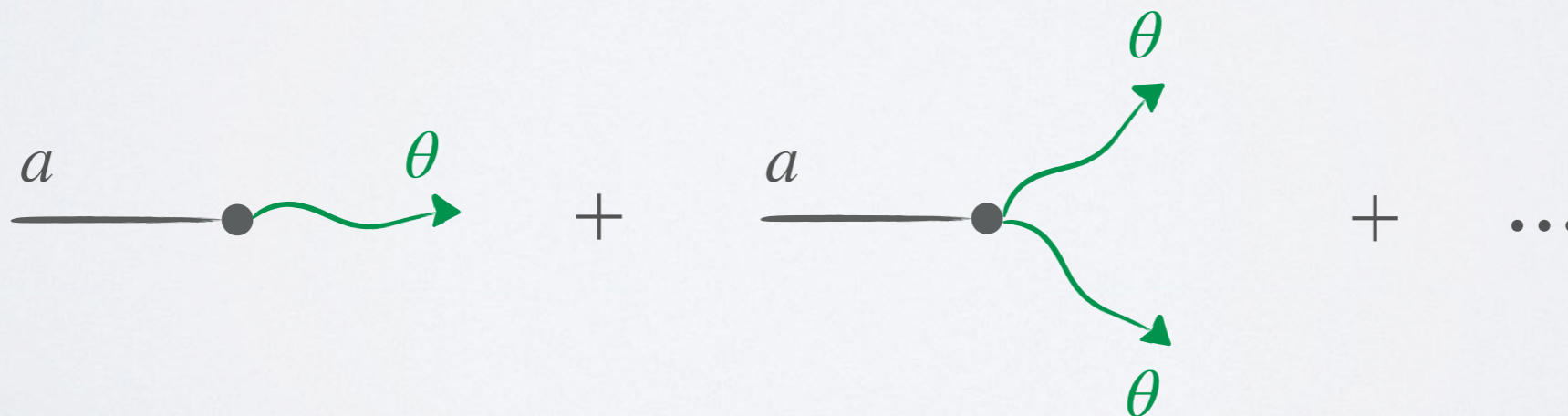
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[Catinari, **AE**, Pavaskar – 2411.09761]

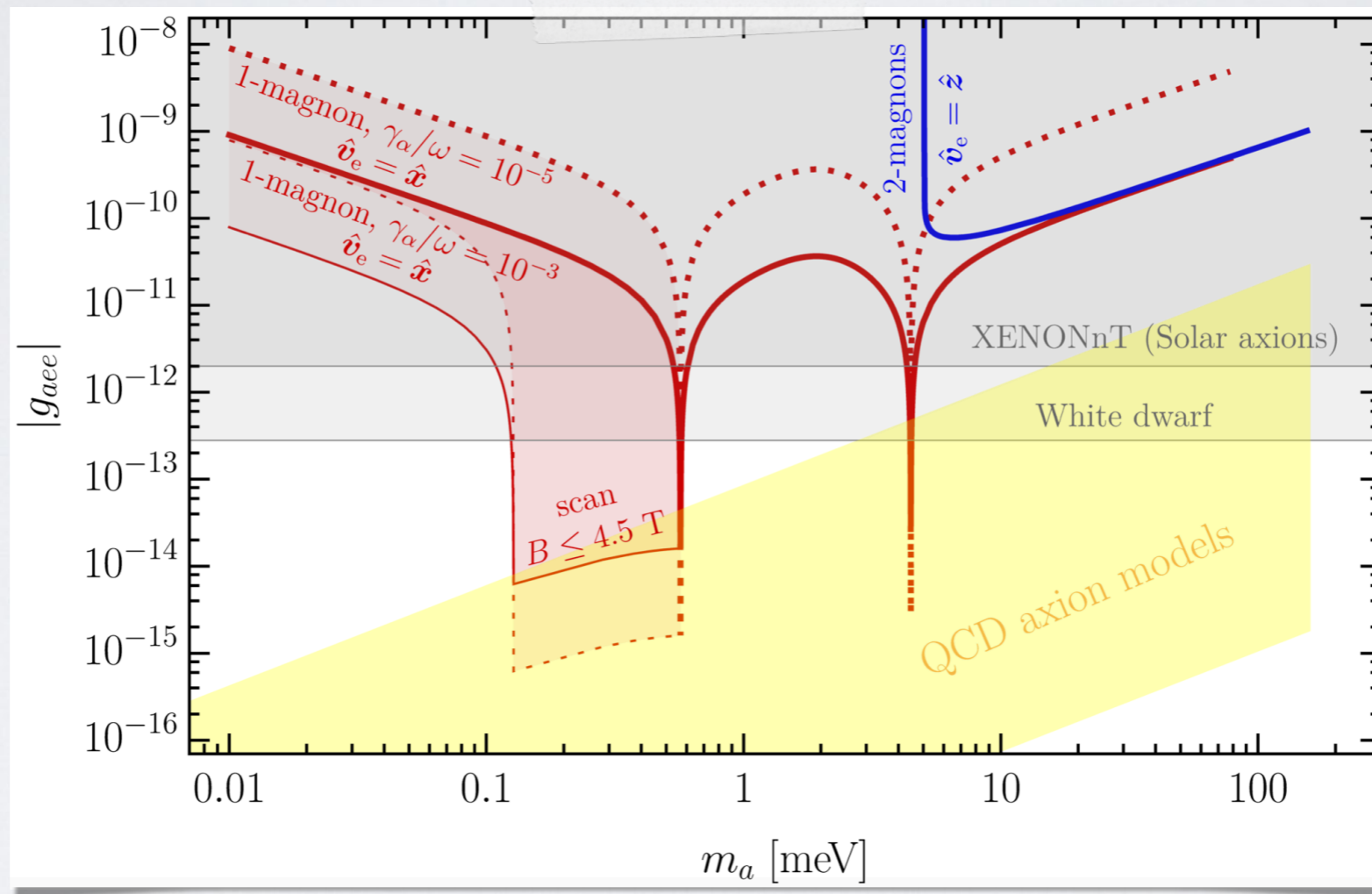
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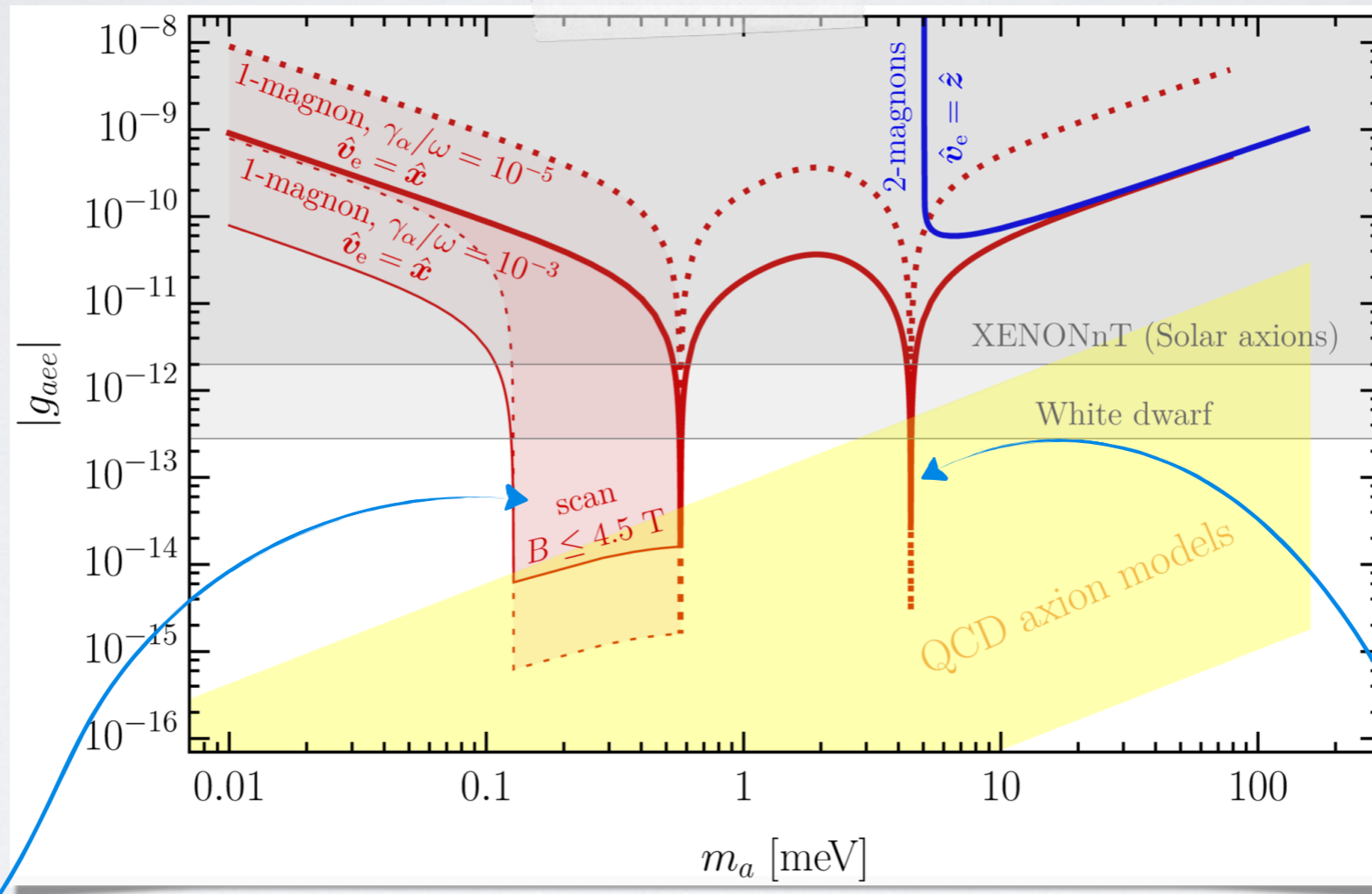
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[Catinari, **AE**, Pavaskar – 2411.09761]

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B-field scan

higher magnon branch

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- The superfluid helium idea is more advanced, with some **projects already in the R&D phase (HeRALD, DELight)** → *see next talk!*
- For anti-ferromagnets there is a plethora of open questions:
 - ▶ is any other good material out there? [Marocco, Wheeler – 2501.18120]
 - ▶ what is the **actual observable**? How do we see magnons? (SQUIDs? cavities?)

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Thank you for the attention!