

Dynamic models of Gentrification

Giovanni Mauro, Nicola Pedreschi, Luca Pappalardo, Renaud Lambiotte



Gentrification

“**One by one**, many of the **working class quarters** of London have been **invaded** by the middle classes – upper and lower (...)

Once this process of ‘**gentrification**’ starts in a district it goes on **rapidly** until all or most of the original **working** class occupiers are **displaced**” (...)

Ruth Glass, 1964



What is Gentrification?

“The process of **improving** an area of a town or city so that it attracts people of a **higher** social class than before”

Oxford Advanced Learner's Dictionary



“The process by which a place, especially part of a city, changes from being a **poor** area to a **richer** one, where people from a higher social class live”

Cambridge Dictionary



How to measure Gentrification?

- “Measuring the invisible”¹
 - Replacement or displacement?
 - Do we even have correct data?
 - Hard to retrieve them²
- We need a Digital Twin (*of data that does not exist!*)

[1] Atkinson, R. (2000). Measuring gentrification and displacement in Greater London.

[2] Easton, S., Lees, L., Hubbard, P., & Tate, N. (2020). Measuring and mapping displacement: The problem of quantification in the battle against gentrification.

[3] Wachsmuth, D., & Weisler, A. (2018). Airbnb and the rent gap: Gentrification through the sharing economy.

[4] Zukin, S., Lindeman, S., & Hurson, L. (2017). The omnivore's neighborhood? Online restaurant reviews, race, and gentrification.

[5] Bunten, D. M., Preis, B., & Aron-Dine, S. (2024). Re-measuring gentrification.

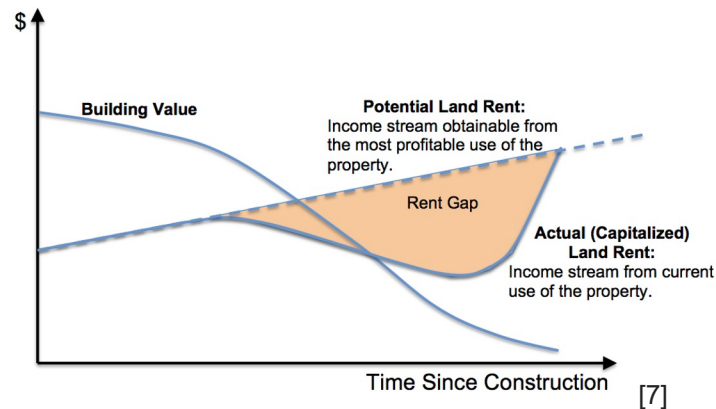
Theories of Gentrification

- **Several** economic and social **theories**.

1. Economic theories (rent gap)
2. Social theories (demand-side)

- The **Rent Gap**:

- "... between the actual capitalized **ground rent** of a plot of land given its **present** use and the **potential** ground rent that might be gleaned under a "**higher and better**" use"⁶.



[6]Smith, N. (1987). Gentrification and the rent gap.

[7] Illustration of how a rent gap grows over time. By Daniel Herriges, based on a similar chart by Neil Smith in "Toward a Theory of Gentrification A Back to the City Movement by Capital, not People", 1979

Theories of Gentrification Drivers

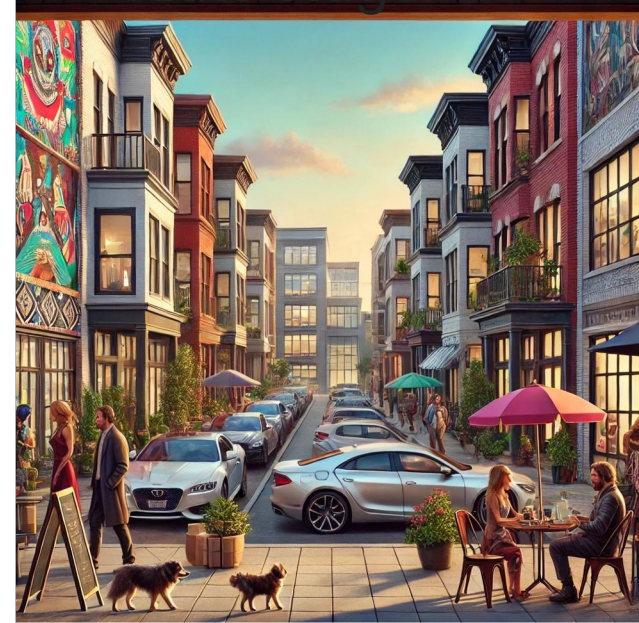
Early Stage



Transitional Stage



Late Stage



Inspired by
Caulfield, J., & Peake, L. (Eds.). (1996). *City Lives and City Forms: Critical Research and Canadian Urbanism*. University of Toronto Press.
Ley, D. (2003). Artists, aestheticisation and the field of gentrification. *Urban studies*, 40(12), 2527-2544.
Images: DALL-E

How to model Gentrification?

Rent Gap

- Deriving theoretical equations ⁸
- Transactions of owners-buyers ⁹

[8] Redfern, P. A. (1997). A new look at gentrification: 2. A model of gentrification.

[9] O'Sullivan, D. (2002). Toward micro-scale spatial modeling of gentrification.

Demand Side

- As a contagious process ¹¹
- Theory and data informed model ¹²

[11] Liu, C., & O'Sullivan, D. (2016). An abstract model of gentrification as a spatially contagious succession process.

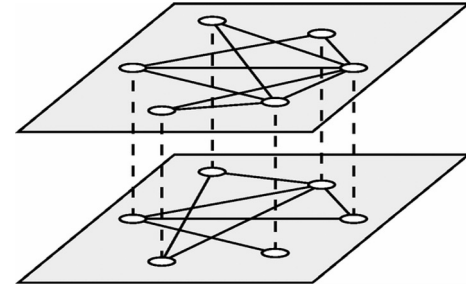
[12] Torrens, P. M., & Nara, A. (2007). Modeling gentrification dynamics: A hybrid approach.

How to model Gentrification?

1. Low-parameter (ABM) simulation

2. Based on **people** choices and **economic** conditions

3. Output: temporal **multilayer** network of relocations



Gomez, S., et al. Diffusion dynamics on multiplex networks.

Journal of Mathematical Sociology
1971, Vol. 1, pp 143–186

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Printed in Birkenhead, England

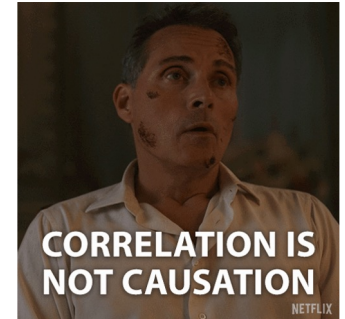
DYNAMIC MODELS OF SEGREGATION†

THOMAS C. SCHELLING
Harvard University



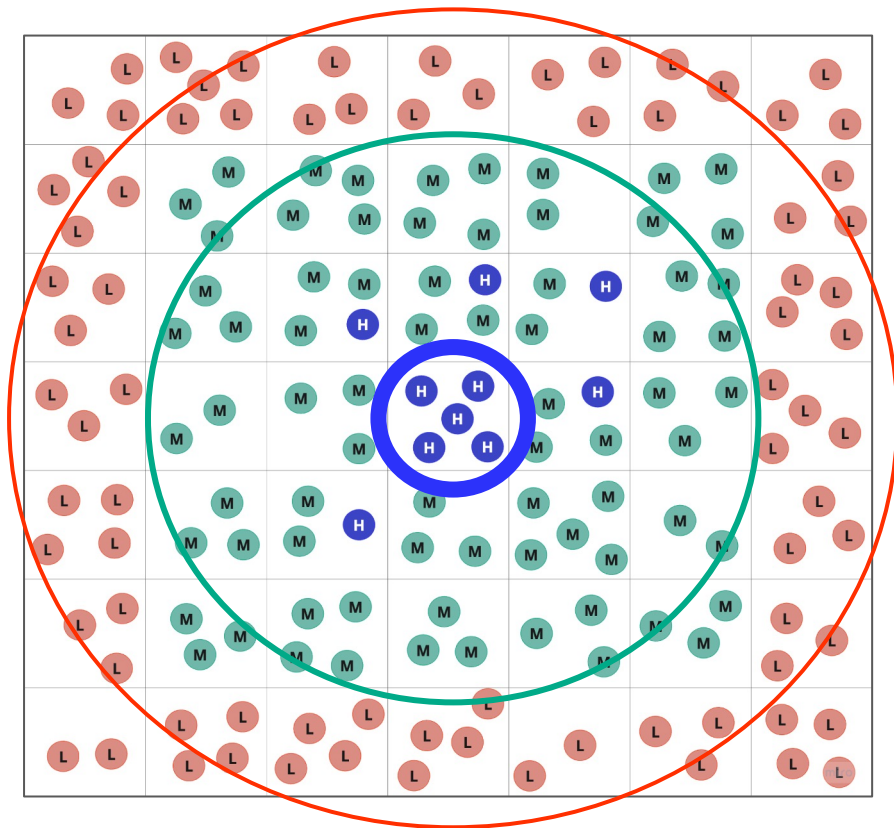
KISS

Keep. It. Simple. Stupid.



Initialization

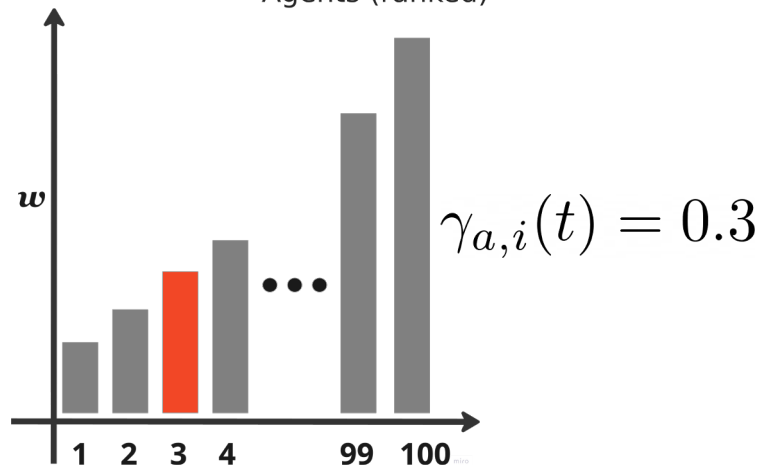
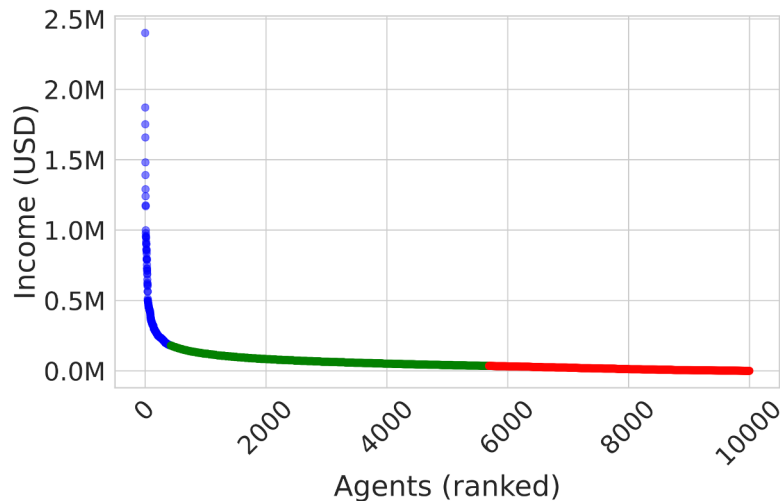
- City as a **lattice**
- **3** types of agents:
 1. **Low** income
 2. **Middle** income
 3. **High** income
- Each cell starts ~75% full



Income and class

- The **fixed income** w of an agent a is **sampled** from US 2022 Social Security Administration data ¹³
- The income **percentile** of an agent a in node i at time t is indicated as

$$\gamma_{a,i}(t)$$



[13] Mantzaris, A. V. (2020). Incorporating a monetary variable into the Schelling model addresses the issue of a decreasing entropy trace.

Segregation.png



maxwatsongeography.wordpress.com

Gentrification.avi

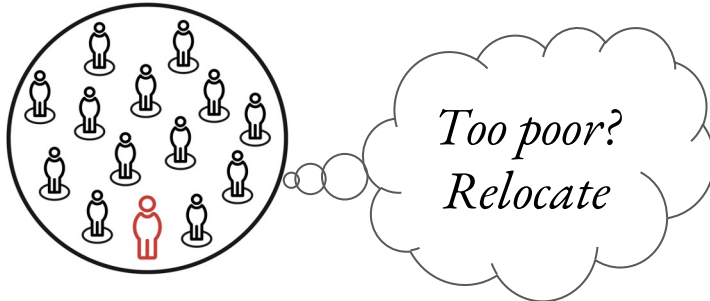
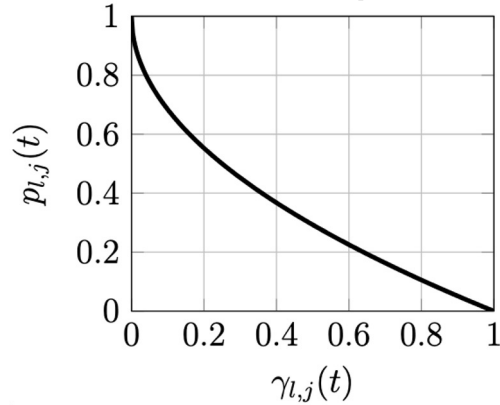


artfcity.com

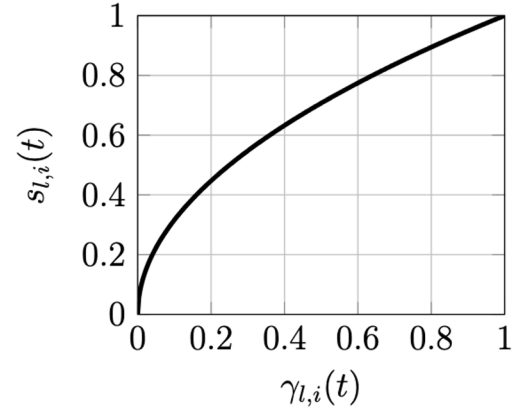
1) **Low** income agent l :

~38%

Evaluation phase



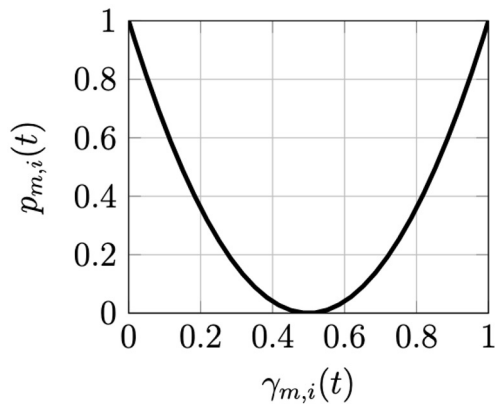
Movement phase



2) Middle income agent m :

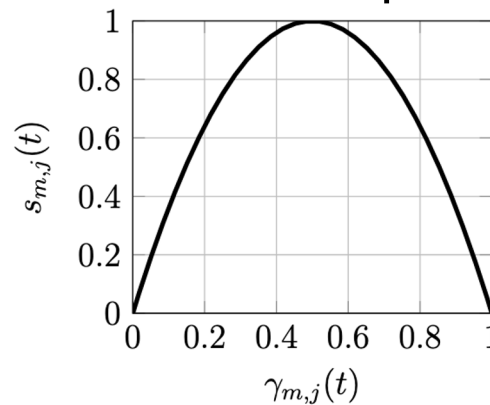
~57%

Evaluation phase



*I want to
stay
middle!*

Movement phase



*I said I want
to stay middle.*

3) High income agent h :

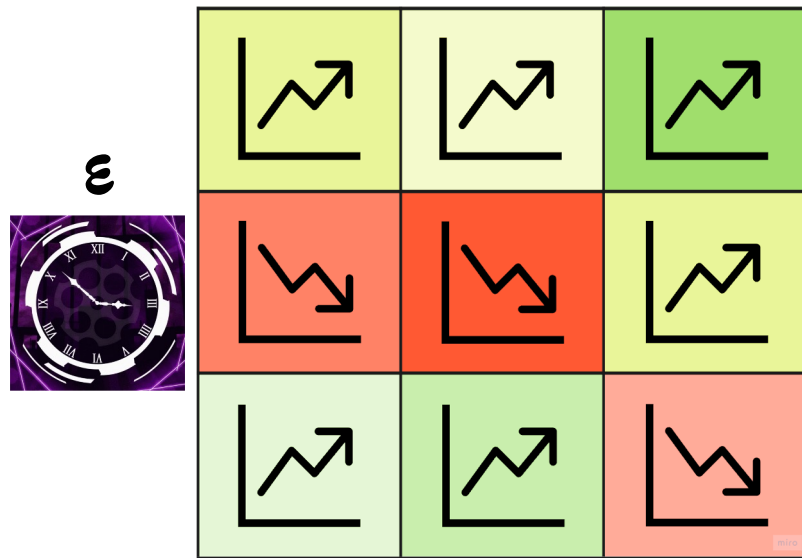
~5%

Evaluation phase



p_h

Movement phase

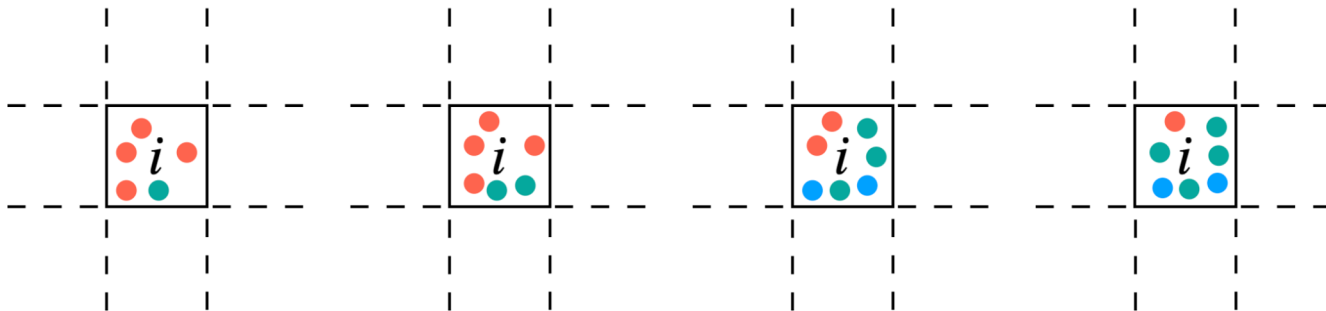


$p(x) \propto \text{trend}_\epsilon(x)$

MEASURING GENTRIFICATION

$\mathcal{G}_{count}$

$n_L^i(t)$ $n_M^i(t)$ $n_H^i(t)$



$t = t_k$

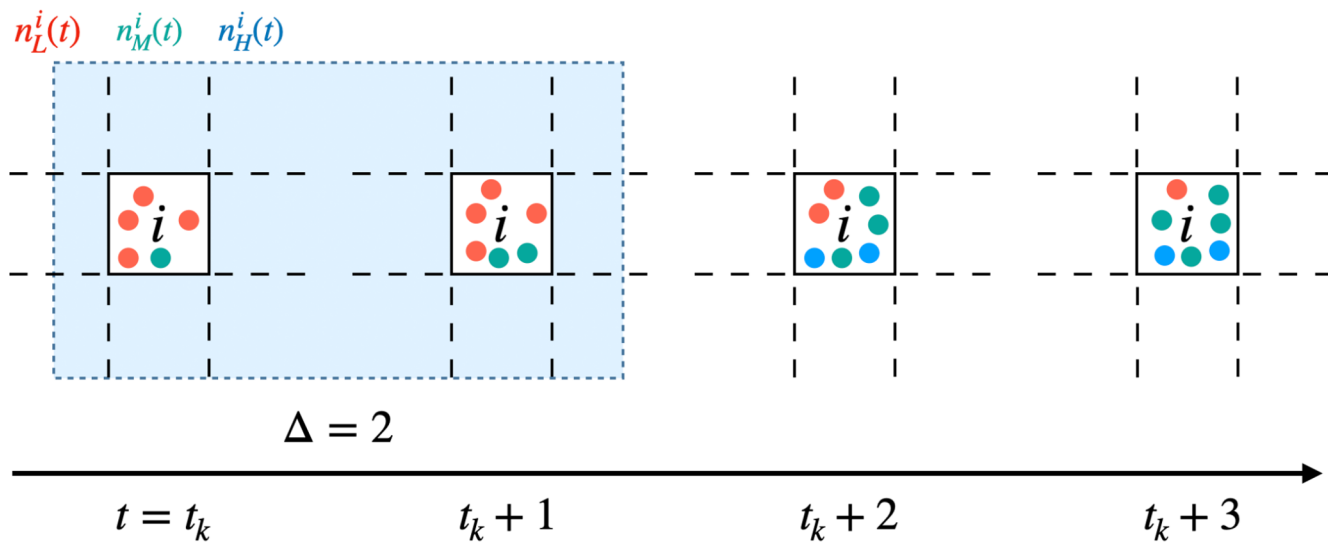
$t_k + 1$

$t_k + 2$

$t_k + 3$

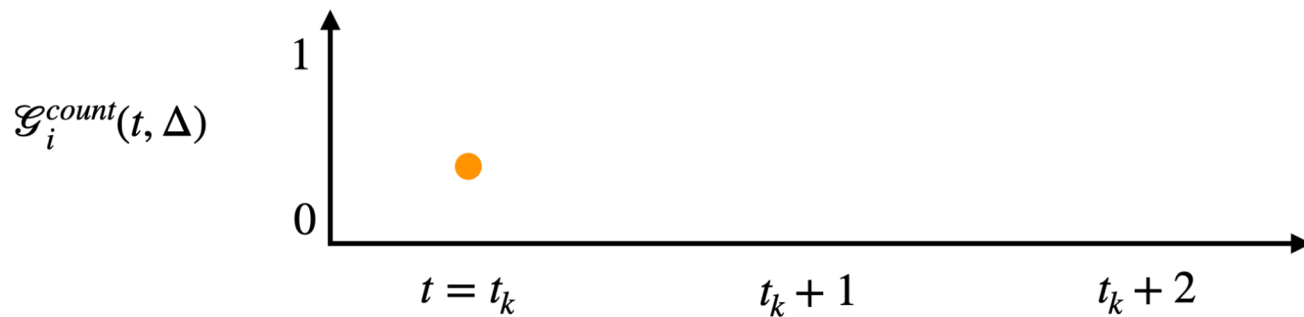
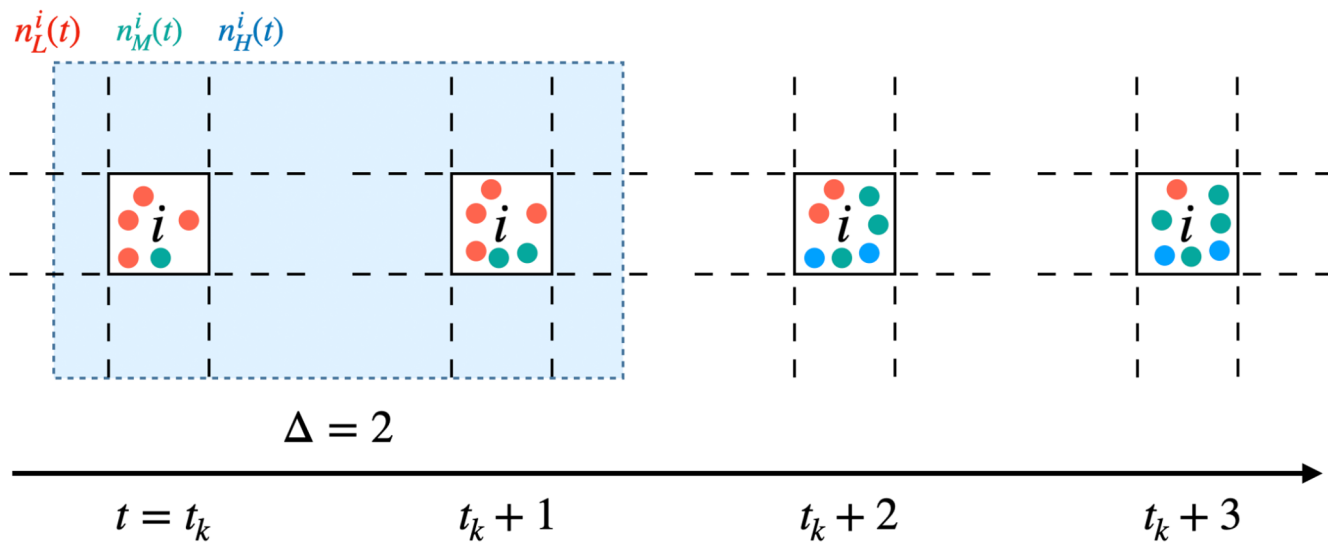


$\mathcal{G}_{count}$

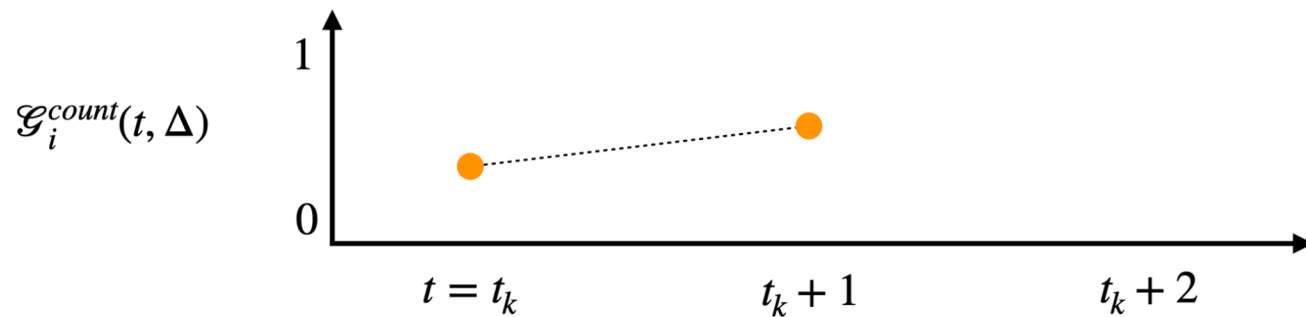
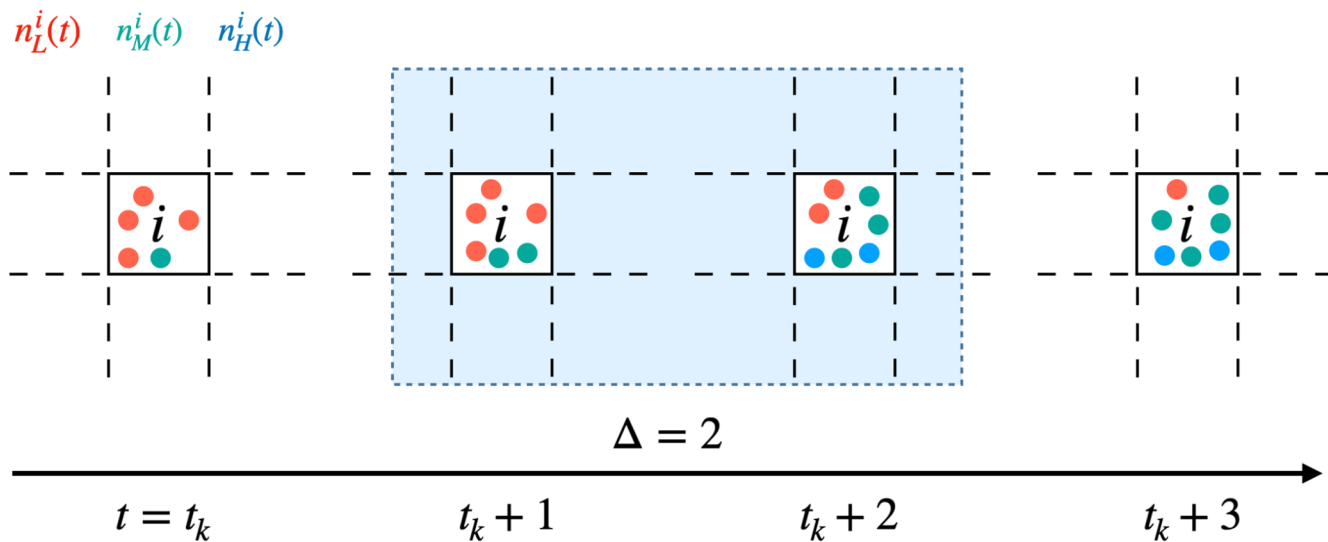


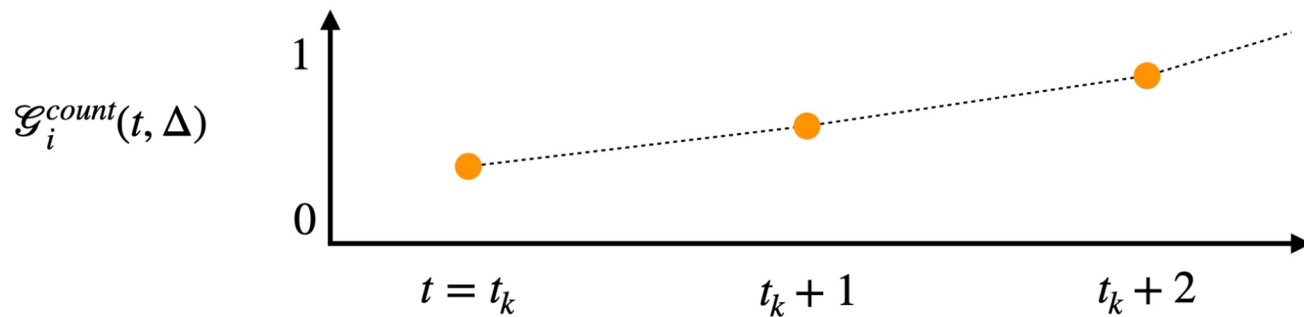
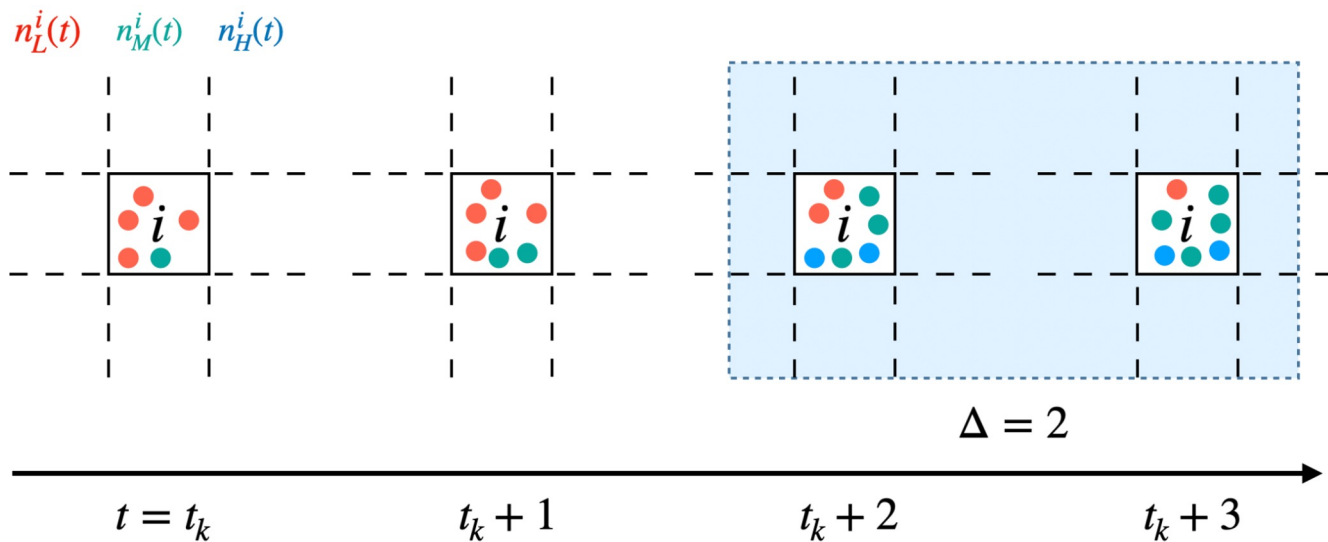
$$\mathcal{G}_i^{count}(t, \Delta) = \frac{1}{\Delta} \sum_{\tau=t}^{t+\Delta} \frac{n_H^i(\tau) + n_M^i(\tau)}{n_H^i(\tau) + n_M^i(\tau) + n_L^i(\tau)}$$

$\mathcal{G}_{count}$

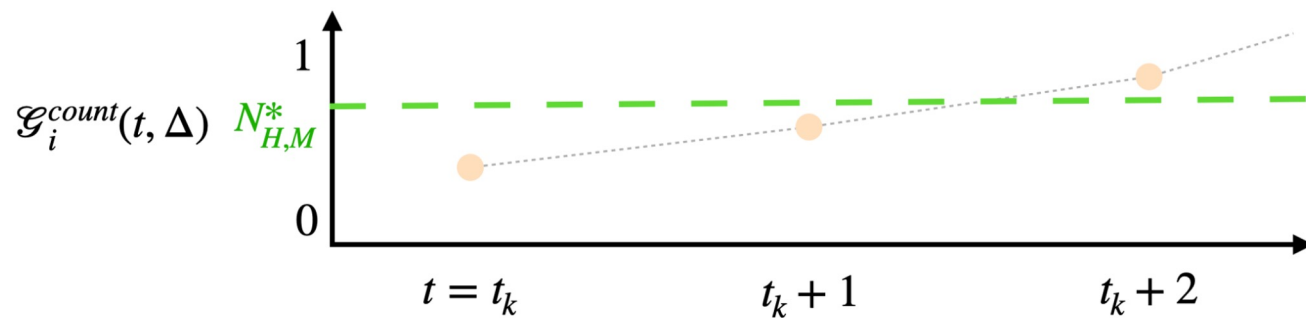
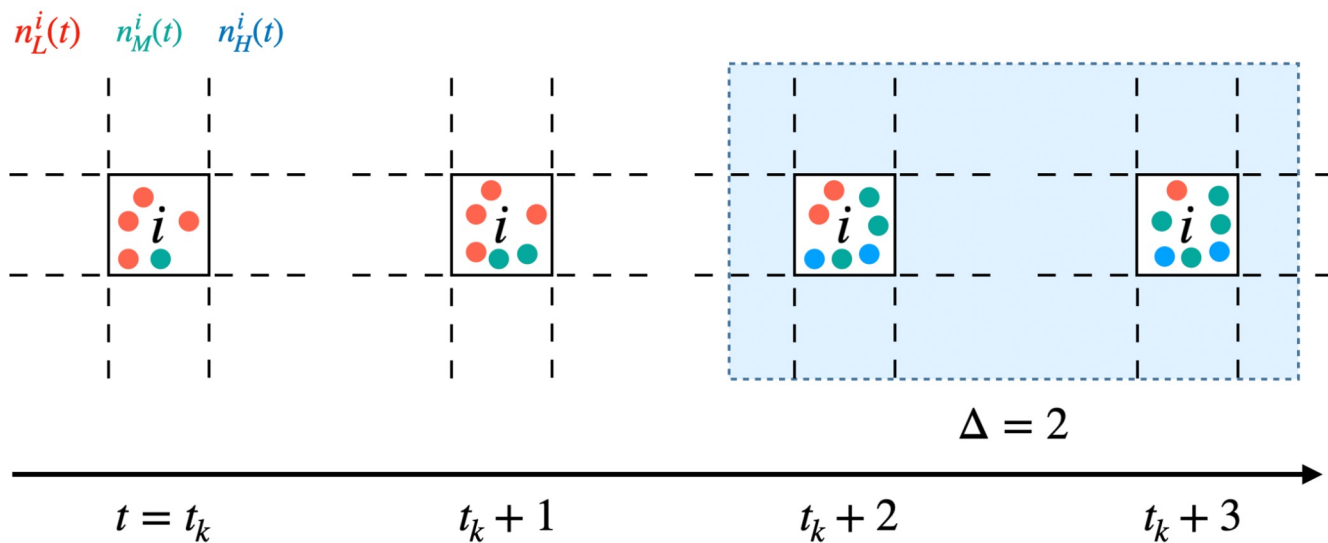


$\mathcal{G}_{count}$

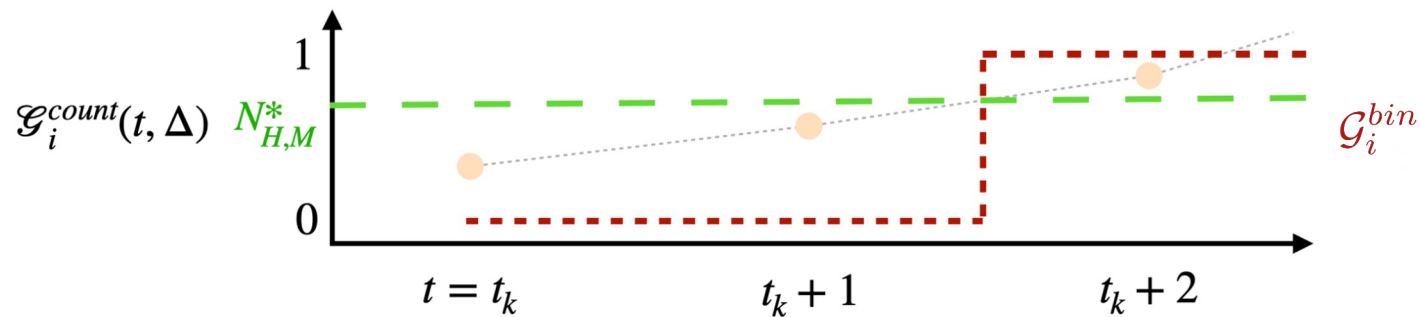
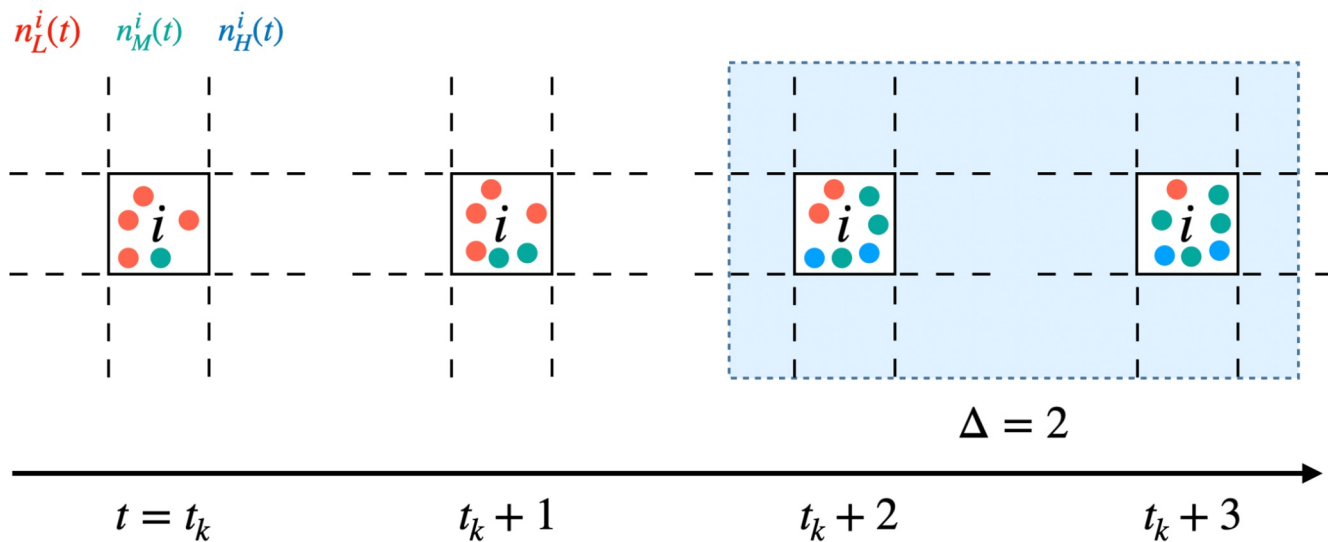


$\mathcal{G}_{count}$ 

$\mathcal{G}_{count}$



$\mathcal{G}_{count}$



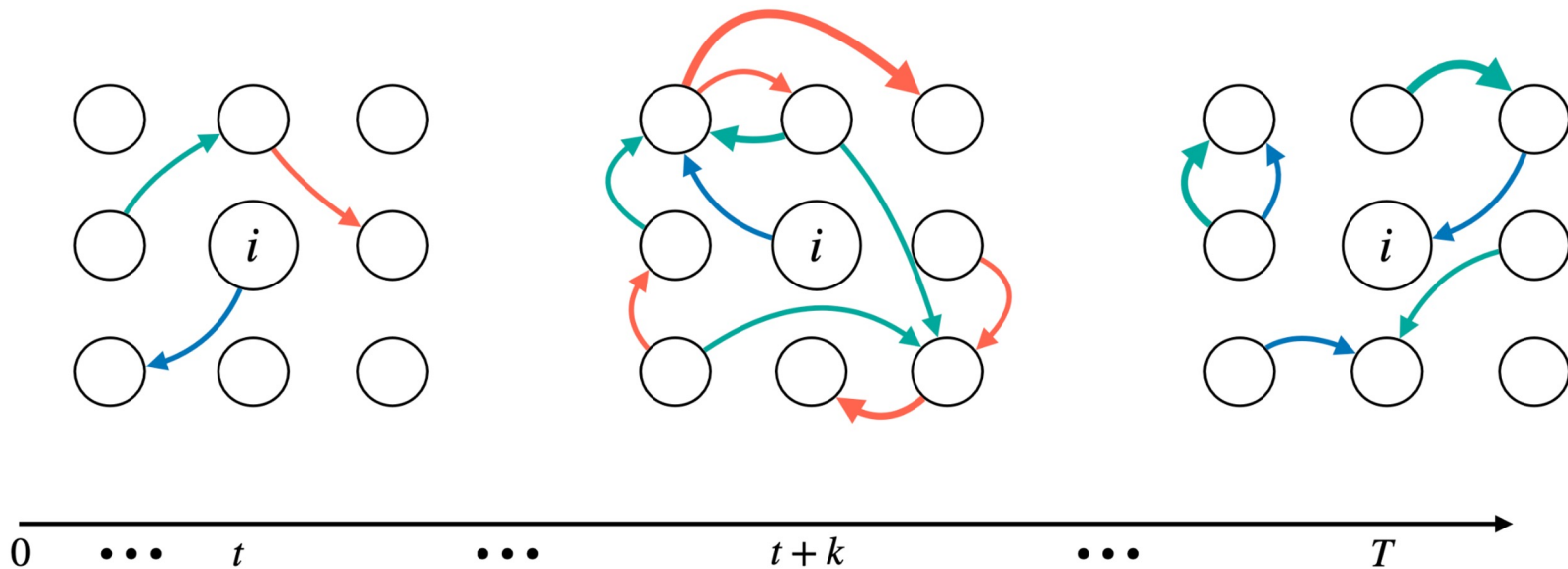
Where's the network?

- **Temporal**, Multilayer network of flows
- **Nodes**: neighborhoods
- **Edges**: #agents moving at time t

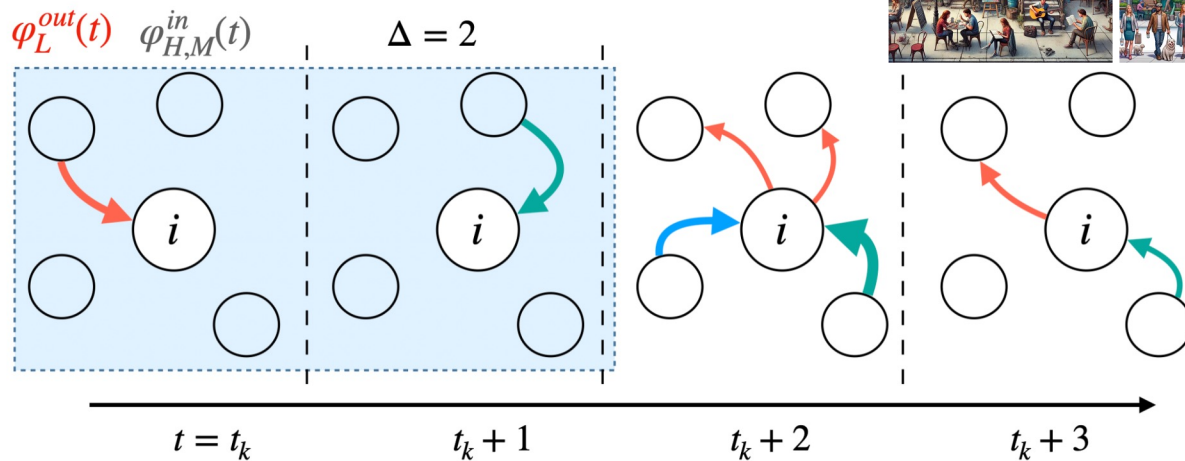
L

M

H



$\mathcal{G}_{net}$



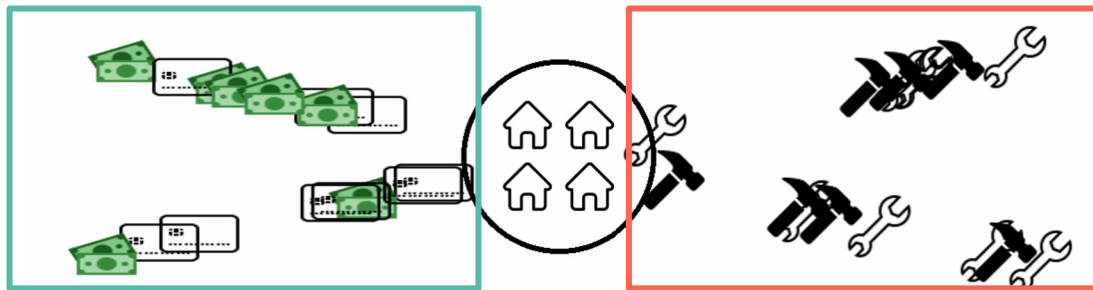
$$\mathcal{G}_i^{net}(t, \Delta) \equiv \left(\frac{1}{\Delta} \sum_{\tau=t-\Delta}^t \varphi_i^{out}(\tau) \right) \cdot \left(\frac{1}{\Delta} \sum_{\tau=t-\Delta}^t \varphi_i^{in}(\tau) \right)$$

■ out

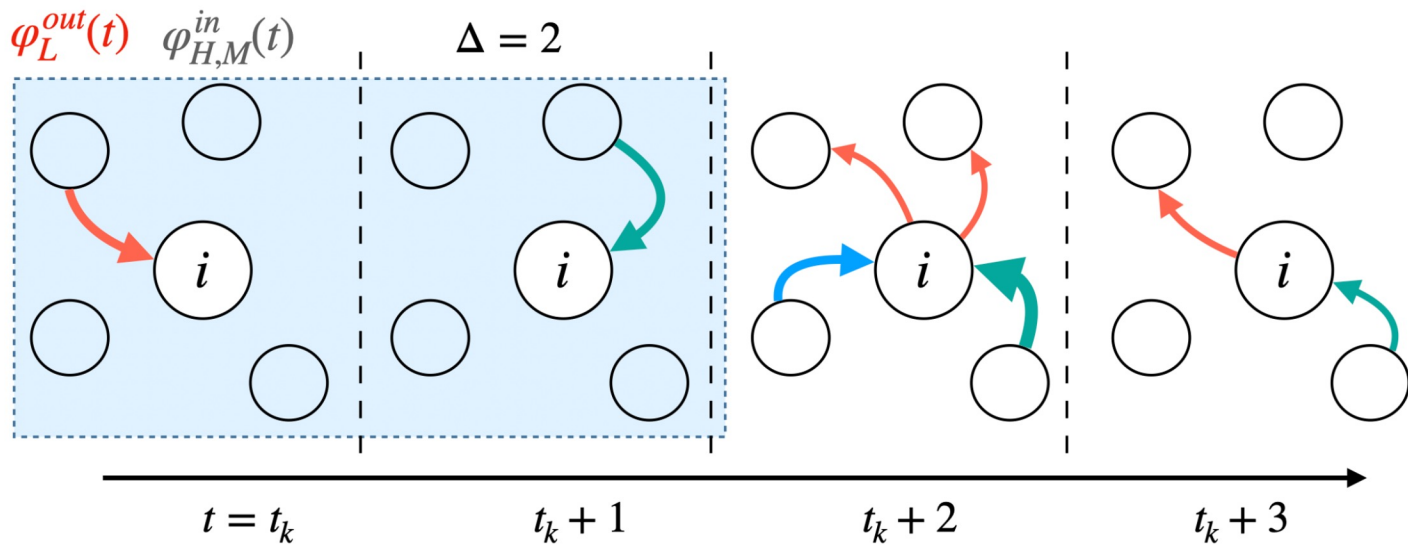
■
■ in

$\mathcal{G}_{net}$

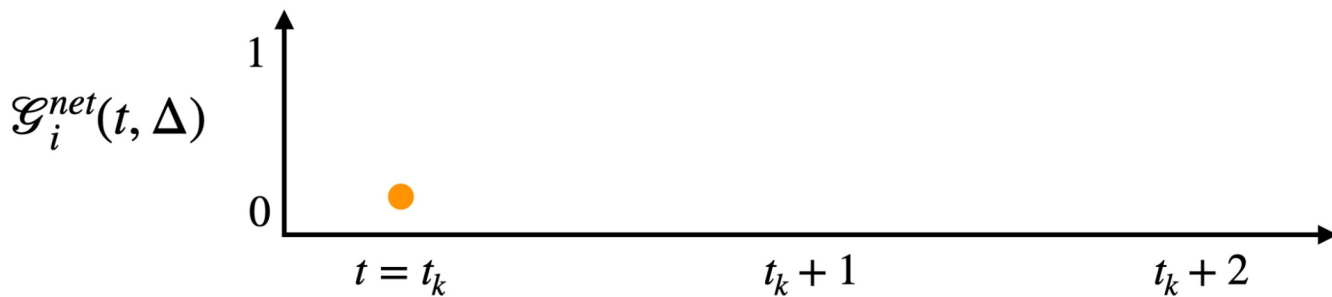
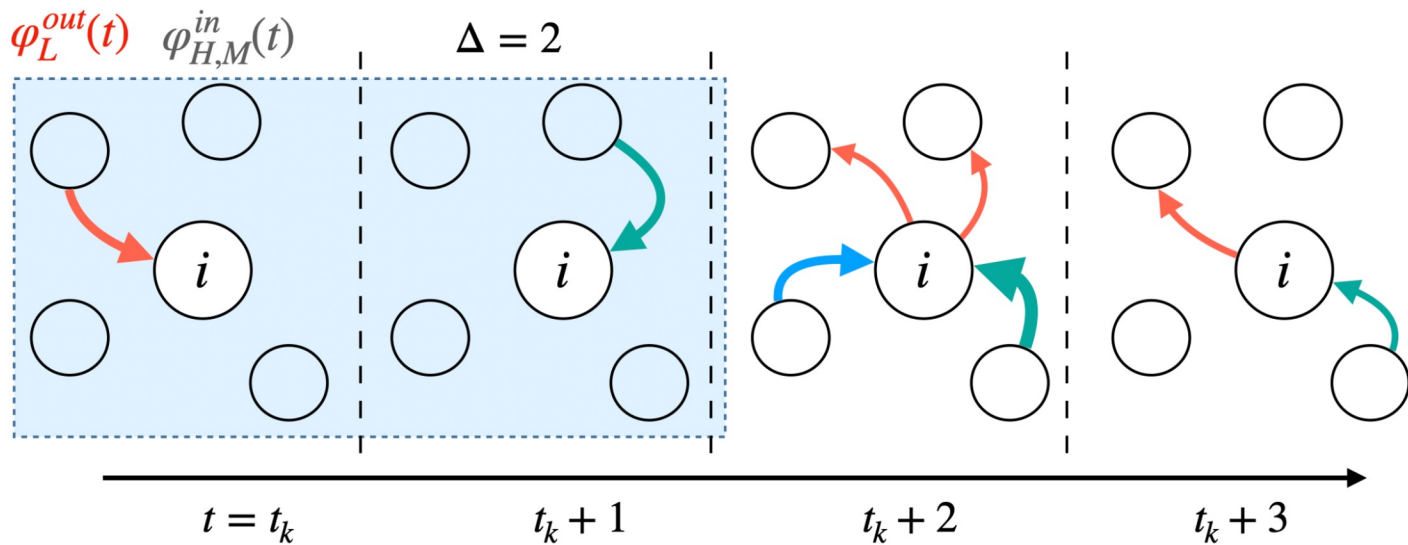
$$\mathcal{G}_i^{\text{net}}(t, \Delta) \equiv \left(\frac{1}{\Delta} \sum_{\tau=t-\Delta}^t \varphi_i^{\text{in}}(\tau) \right) \cdot \left(\frac{1}{\Delta} \sum_{\tau=t-\Delta}^t \varphi_i^{\text{out}}(\tau) \right)$$

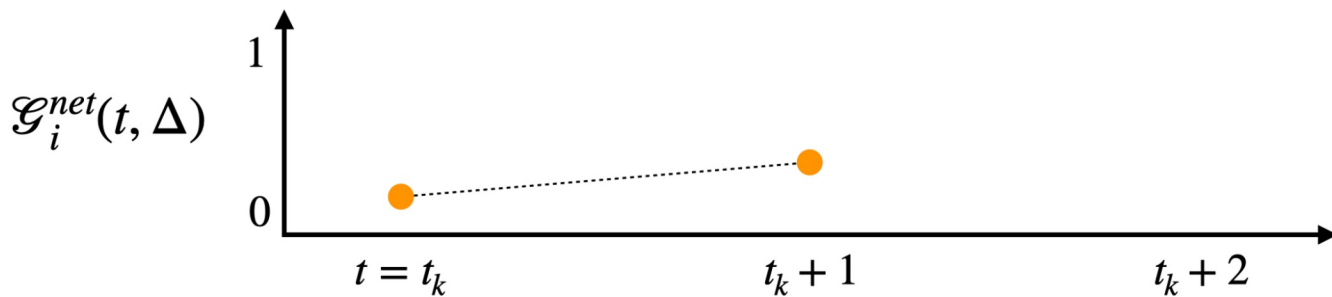
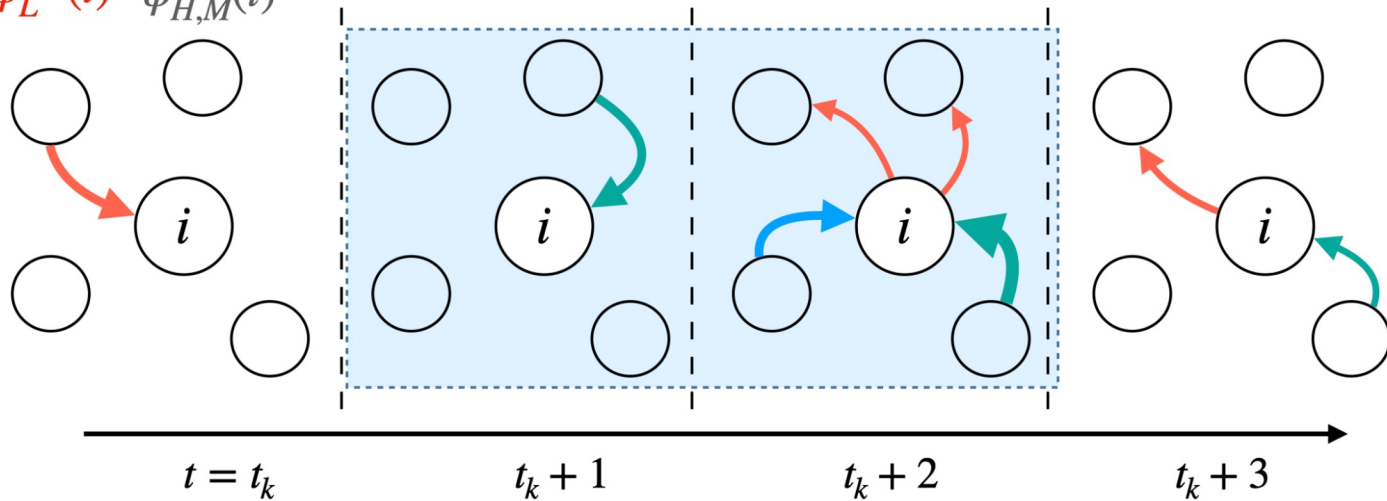


$\mathcal{G}_{net}$

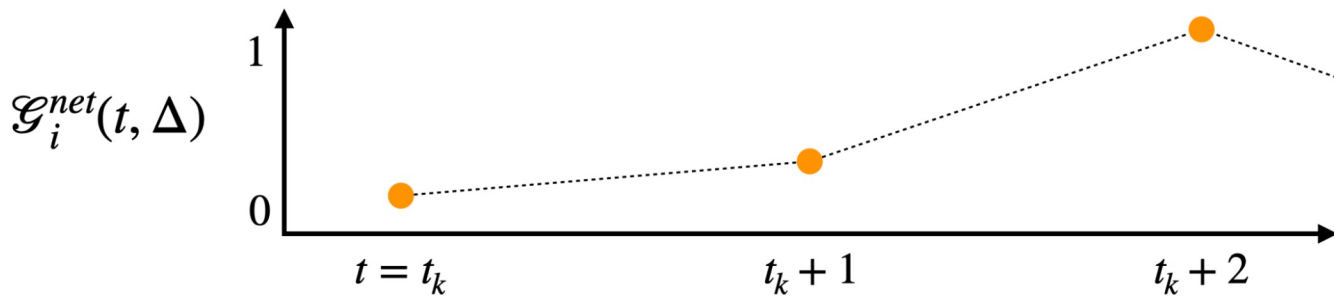
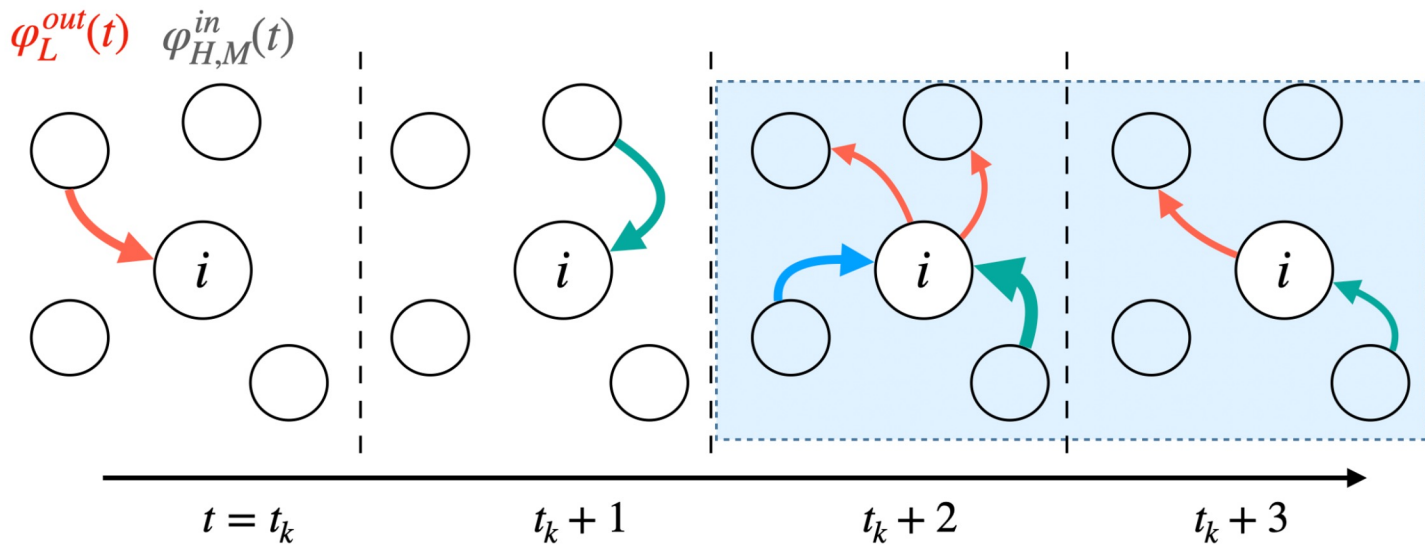


$$\mathcal{G}_i^{net}(t, \Delta) \equiv \sqrt{\left(\frac{1}{\Delta} \sum_{\tau=t-\Delta}^t \varphi_i^{out}(\tau) \right) \cdot \left(\frac{1}{\Delta} \sum_{\tau=t-\Delta}^t \varphi_i^{in}(\tau) \right)}$$

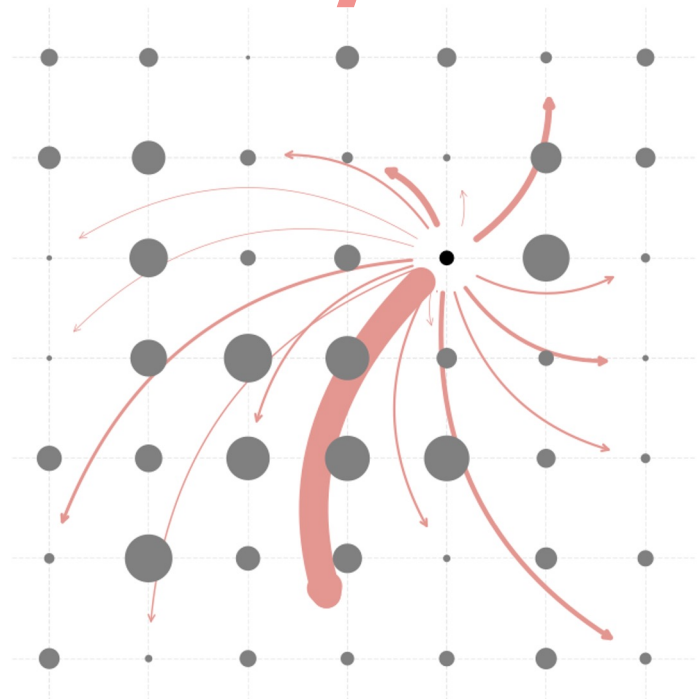
$\mathcal{G}_{net}$ 

$\mathcal{G}_{net}$
 $\varphi_L^{out}(t)$
 $\varphi_{H,M}^{in}(t)$


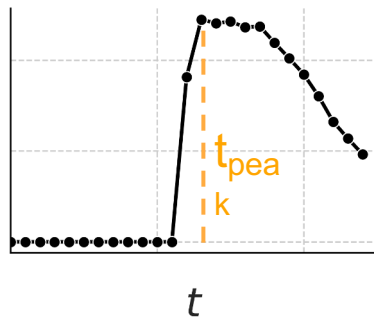
$\mathcal{G}_{net}$



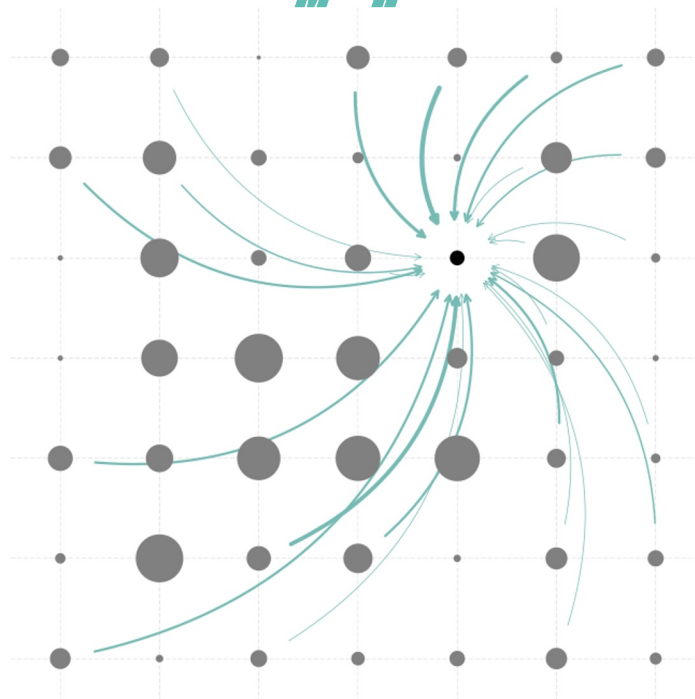
L

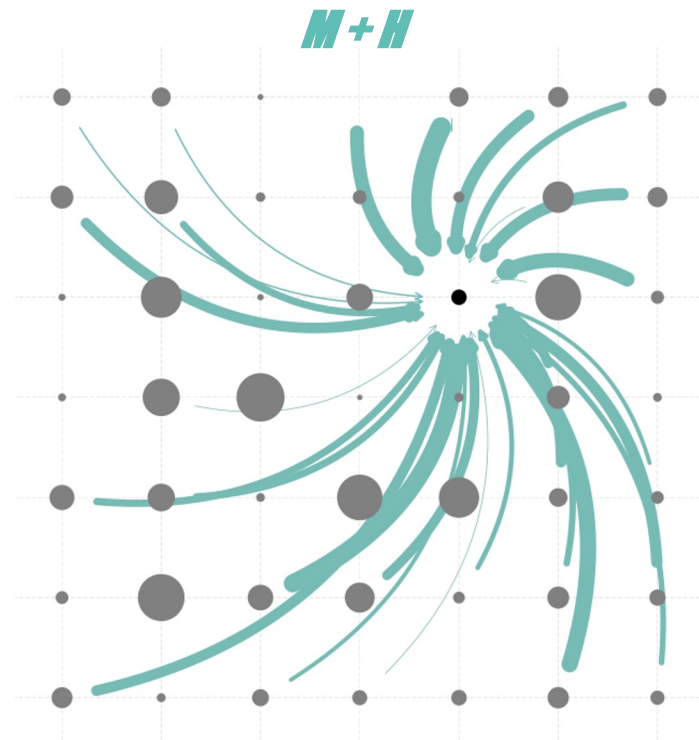
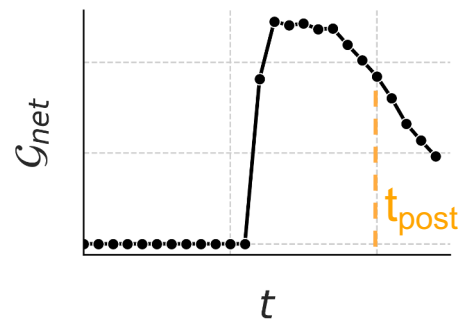
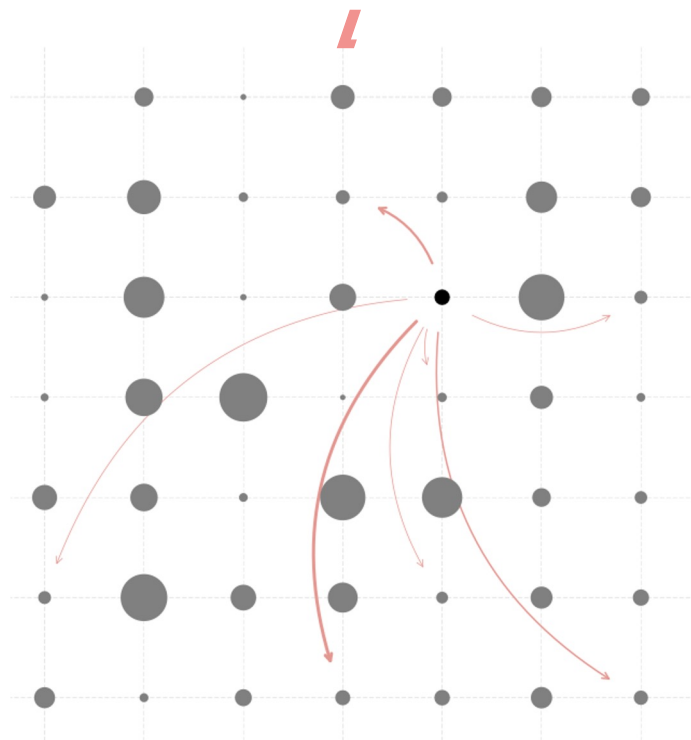


ζ_{net}



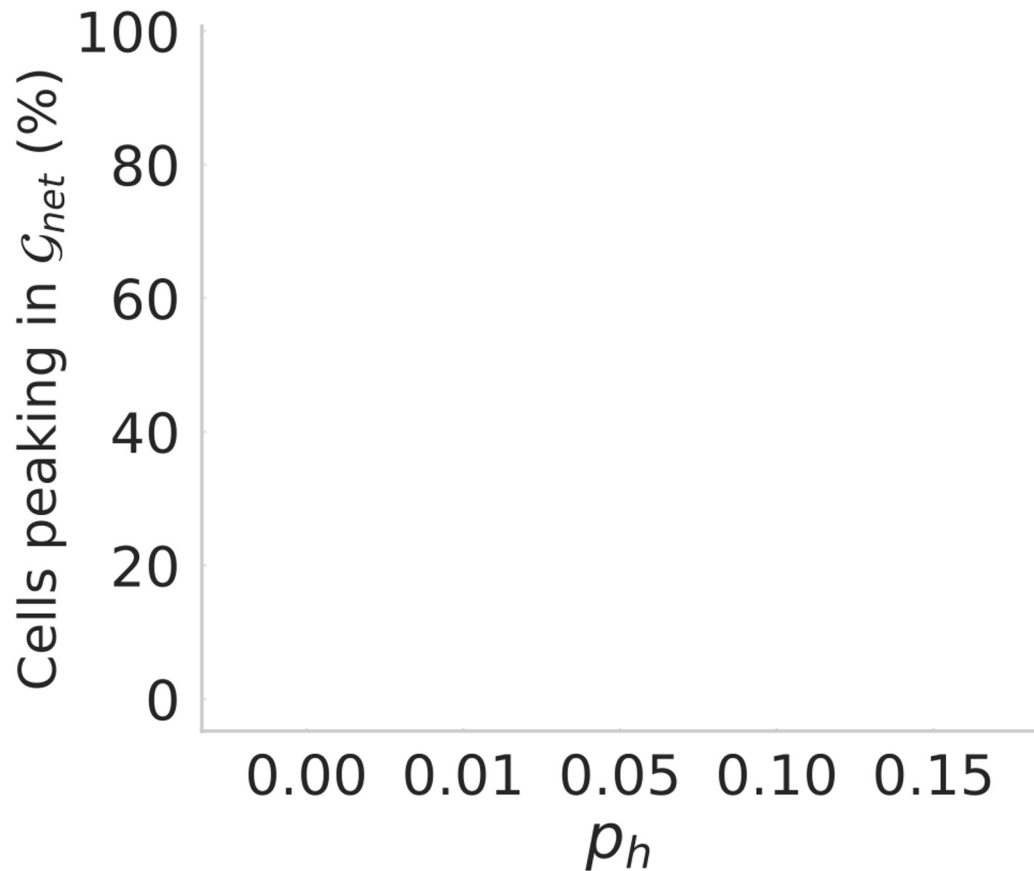
M+H





Results I

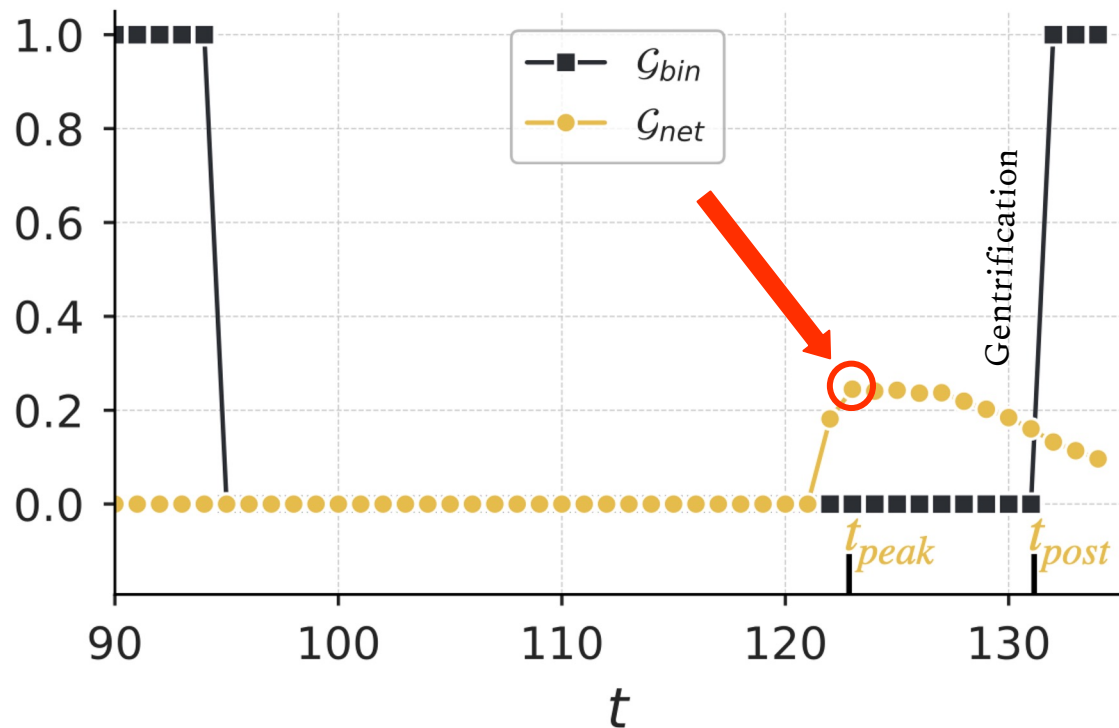
No rich = No gentrification



150 rep x box

Results II

$\mathcal{G}_{net}$ is an early-warning of $\mathcal{G}_{bin}$



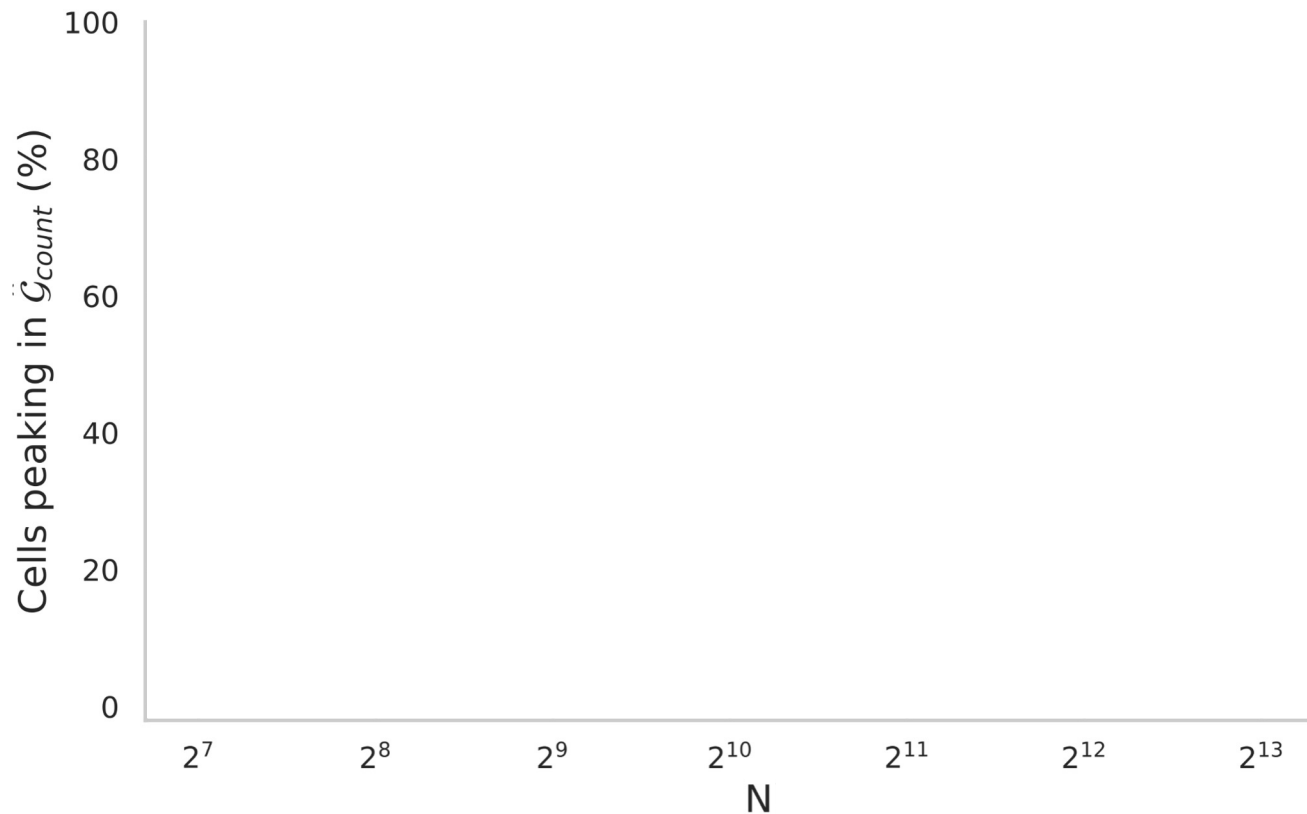
  Threshold
 Abrupt change

  Threshold
 Abrupt change

Coordinated flows **peak**
before population
“proportions”

Results III

Denser cities = Higher Gentrification



Results

1. Super **High**-Income citizen are the drivers

1. **Middle**-Income citizen are the triggers

2. **Low**-income citizen are the displaced

2. **Coordinated flows** reveals **early-warning** signals of Gentrification

1. Residential **mobility** is key

3. **Bigger** and **denser** cities experience more Gentrification

Limitations

1. **Simplistic** urban **form**
2. **Fixed** population, income bracket, and city size
3. Not considering important **factors**
 1. Housing **prices**, mortgages, city council **interventions**
etc.
4. **High-Income** especially can have **more houses**

Ongoing works

1. **Validation** on relocation datasets
 1. Parameter **fitting**
 2. Measure **significance**
2. Correlation with Gentrification proxies
 1. **AirBnB**, Idealista, Yelp...
3. Redundant/Synergistic **CAUSES** of Gentrification



Paper

Dynamic models of Gentrification



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