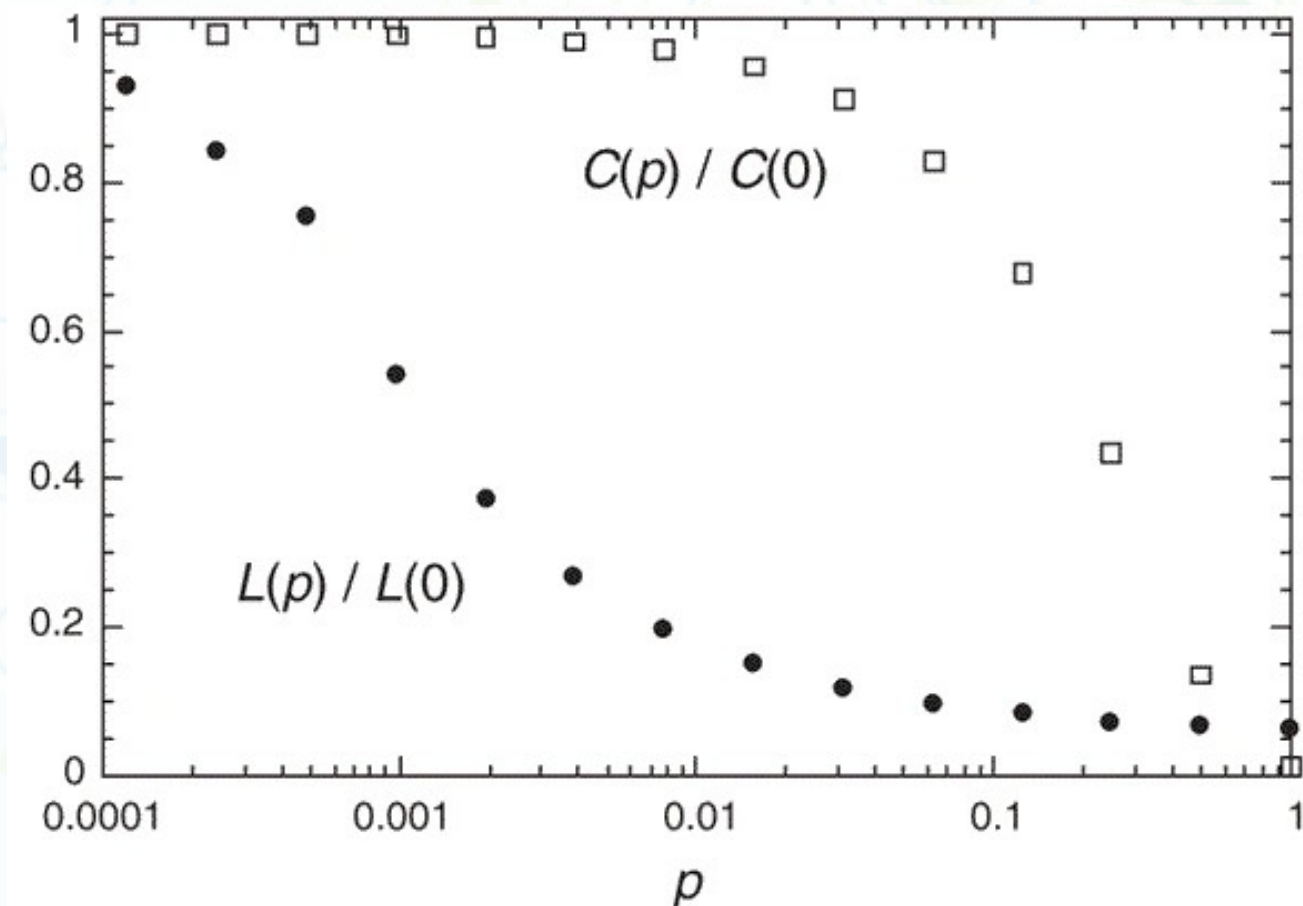


The background of the slide is a complex network diagram. It consists of numerous nodes, represented by circles of varying sizes and colors (blue, green, yellow, and grey), interconnected by a dense web of thin lines. Some nodes are highlighted with larger, semi-transparent colored circles around them. The overall structure suggests a complex system of interactions, likely representing an ecological community.

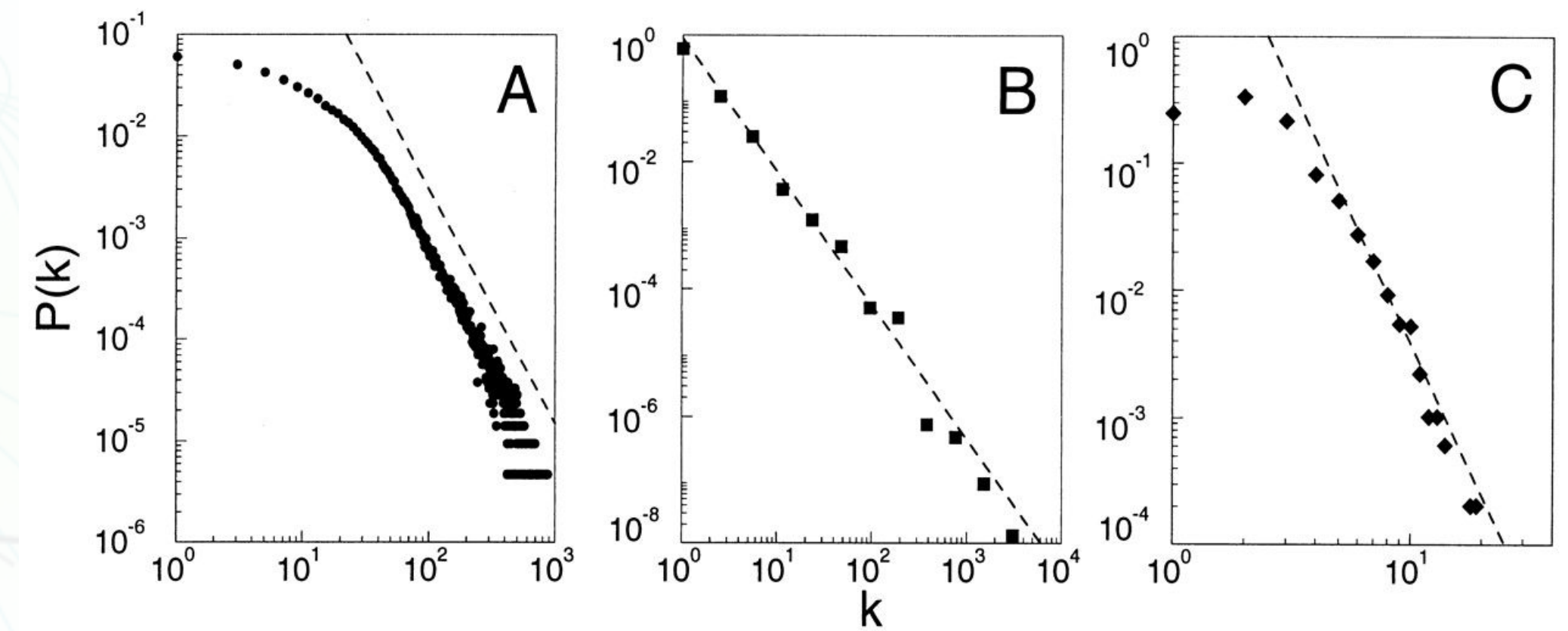
HIGHER-ORDER INTERACTIONS AND THE STABILITY OF COMPETITIVE ECOLOGICAL COMMUNITIES

Sandro Meloni

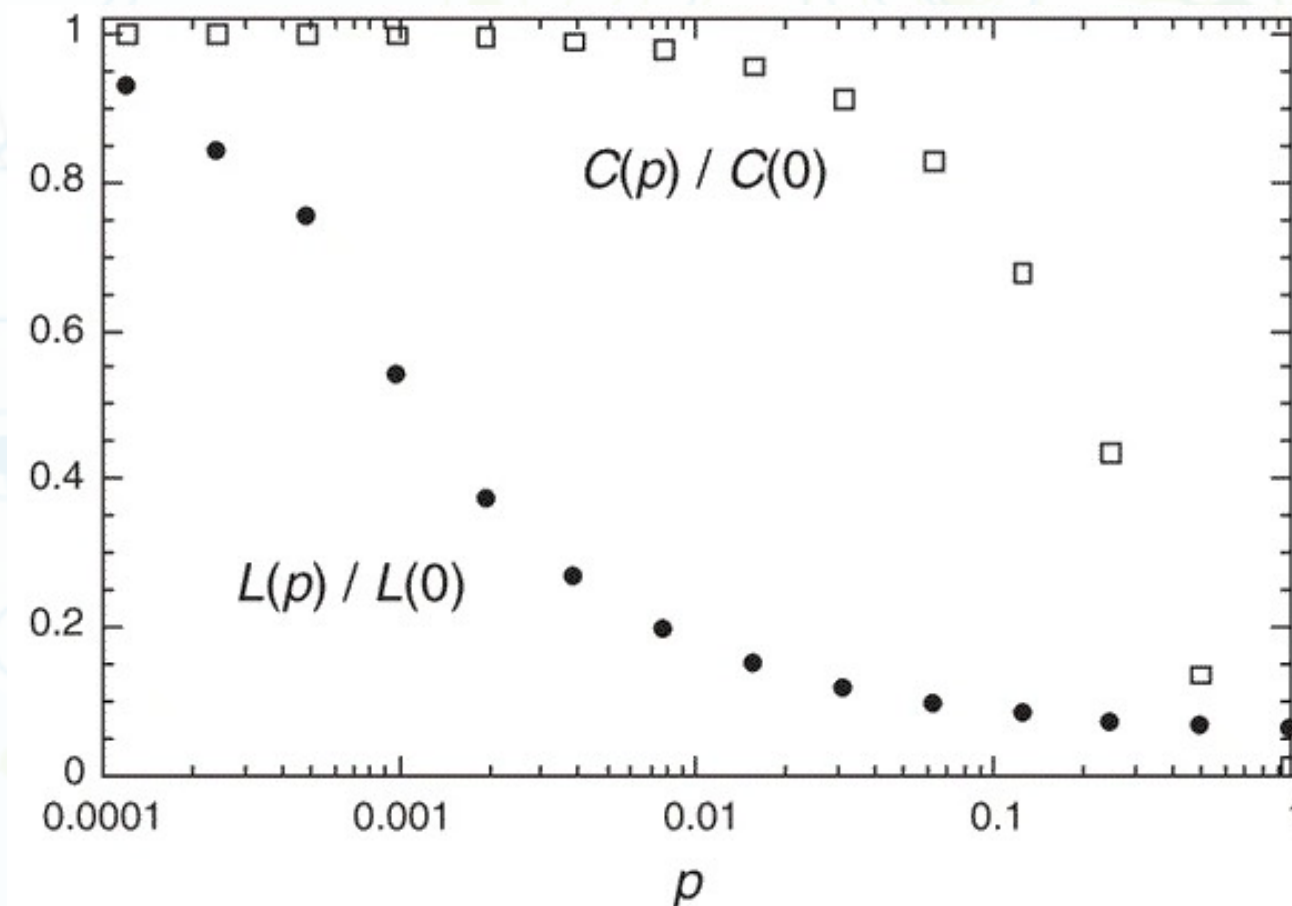
CCS/Italy 2025 - Bari, September 15th 2025



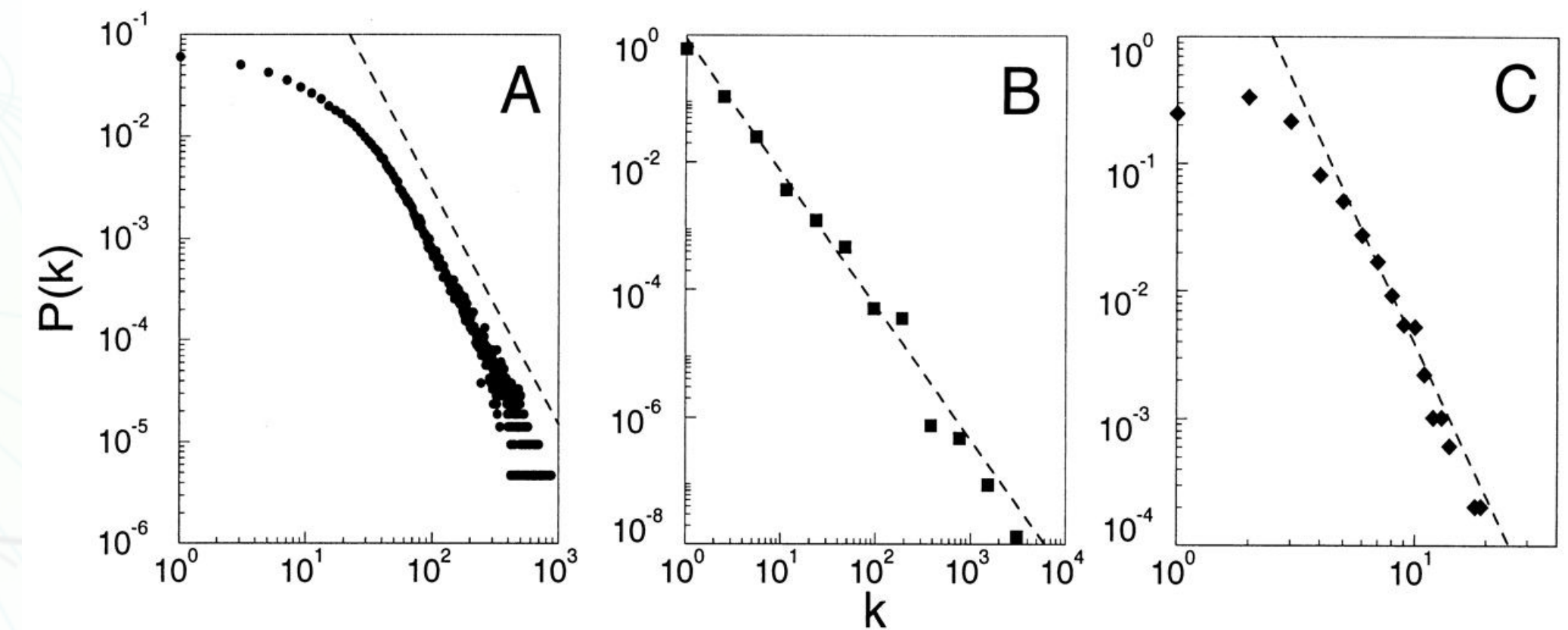
Watts D., Strogatz S. *Nature* 393, 440–442 (1998)



Barabási A.-L., Albert R. *Science* 286, 509–512 (1999)

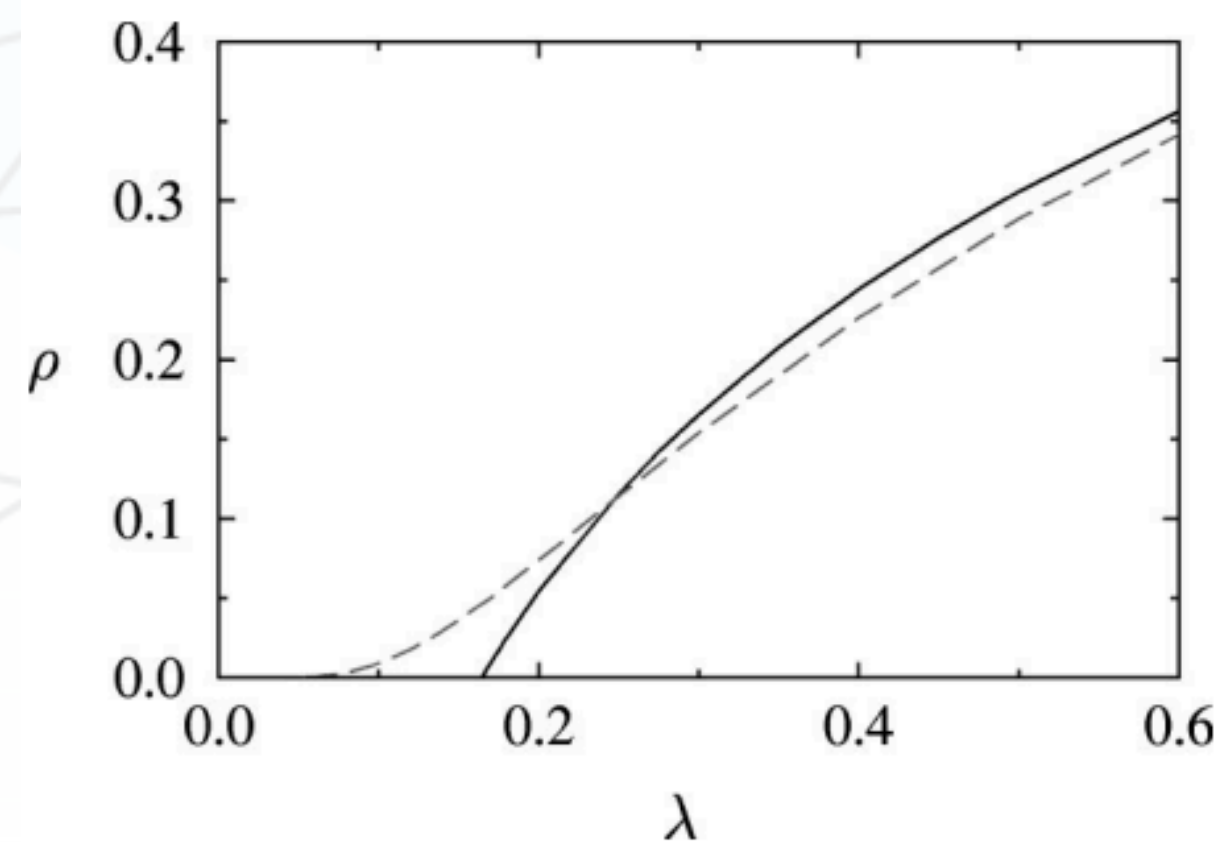


Watts D., Strogatz S. *Nature* 393, 440-442 (1998)

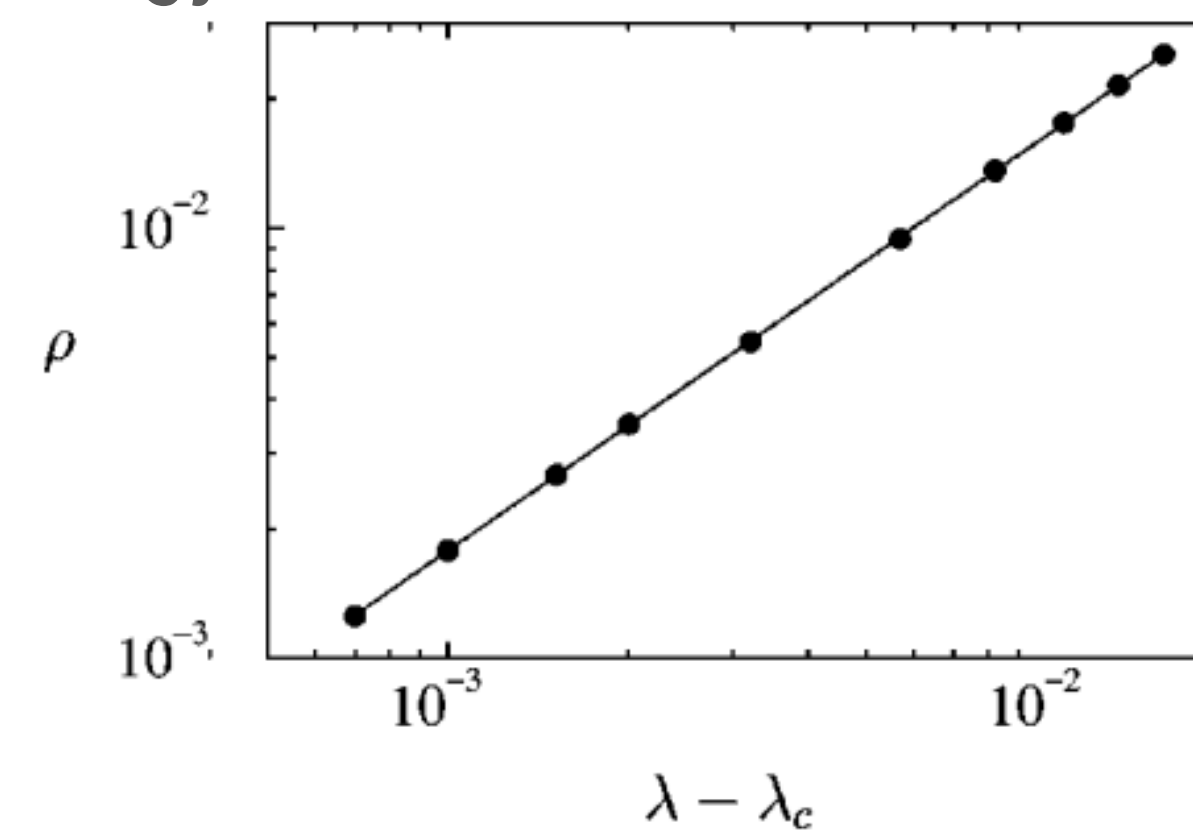


Barabási A.-L., Albert R. *Science* 286, 509-512 (1999)

New effects from topology

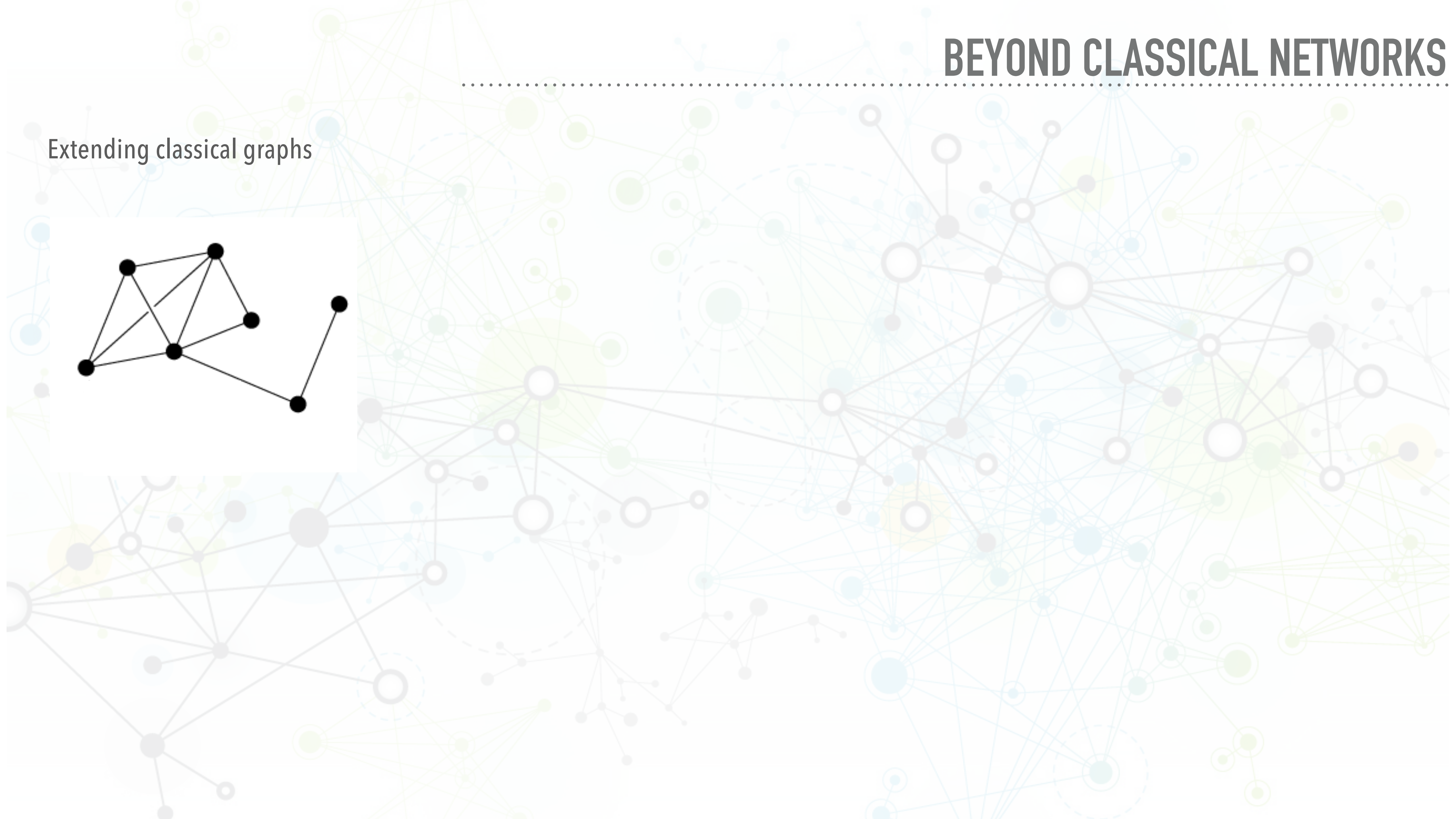
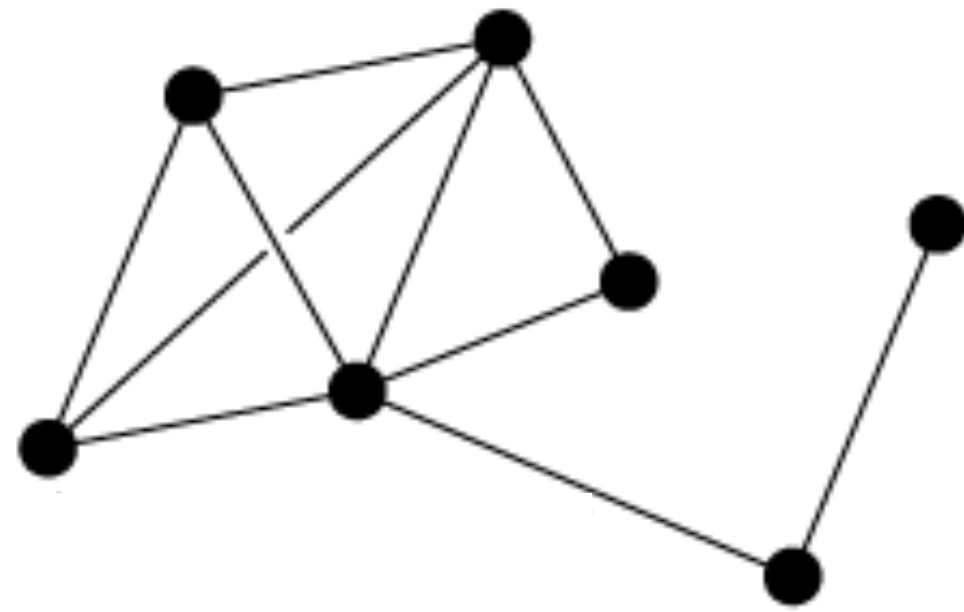


Pastor-Satorras R., Vespignani A. *Physical Review E* 63, 066117 (2001)



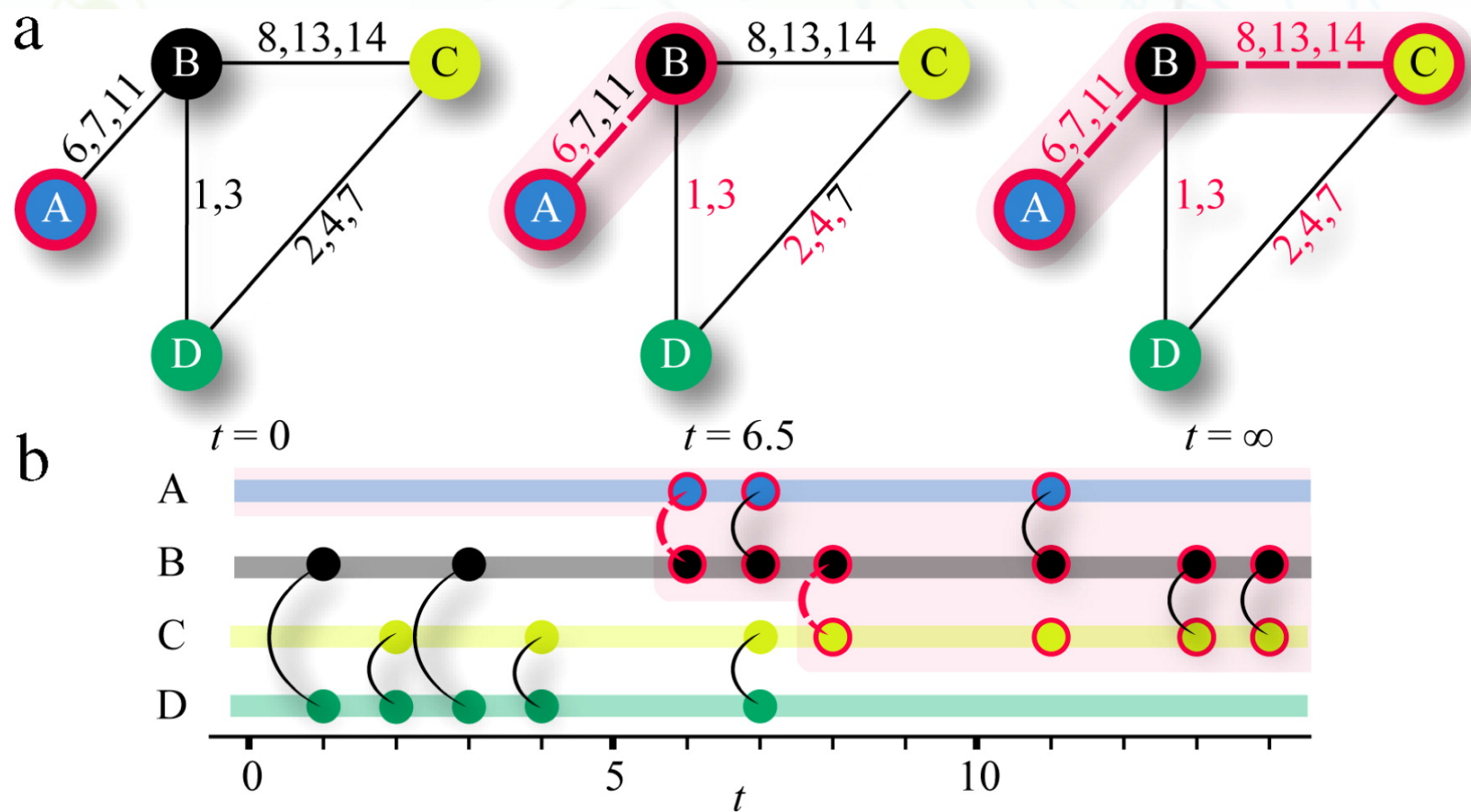
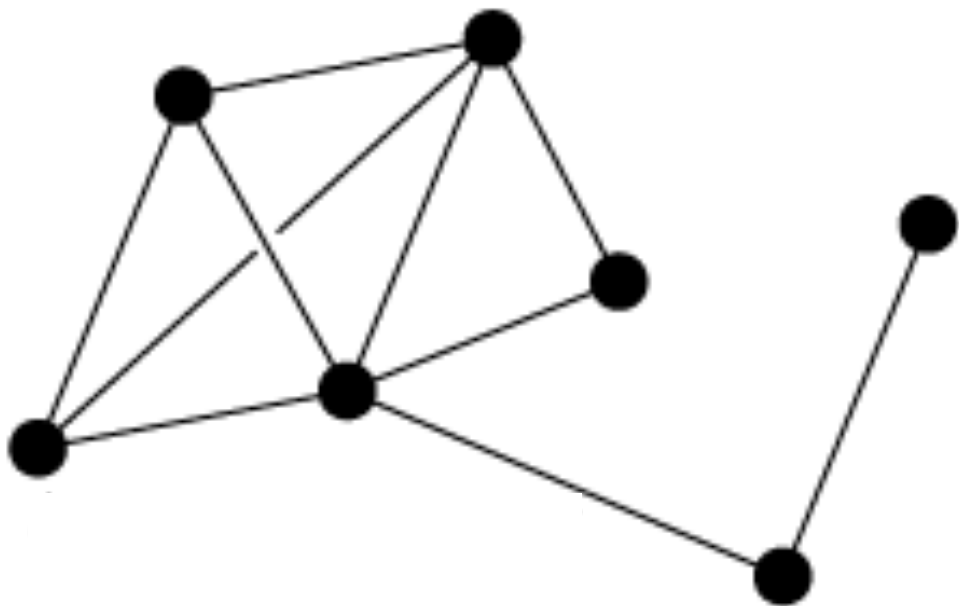
BEYOND CLASSICAL NETWORKS

Extending classical graphs



BEYOND CLASSICAL NETWORKS

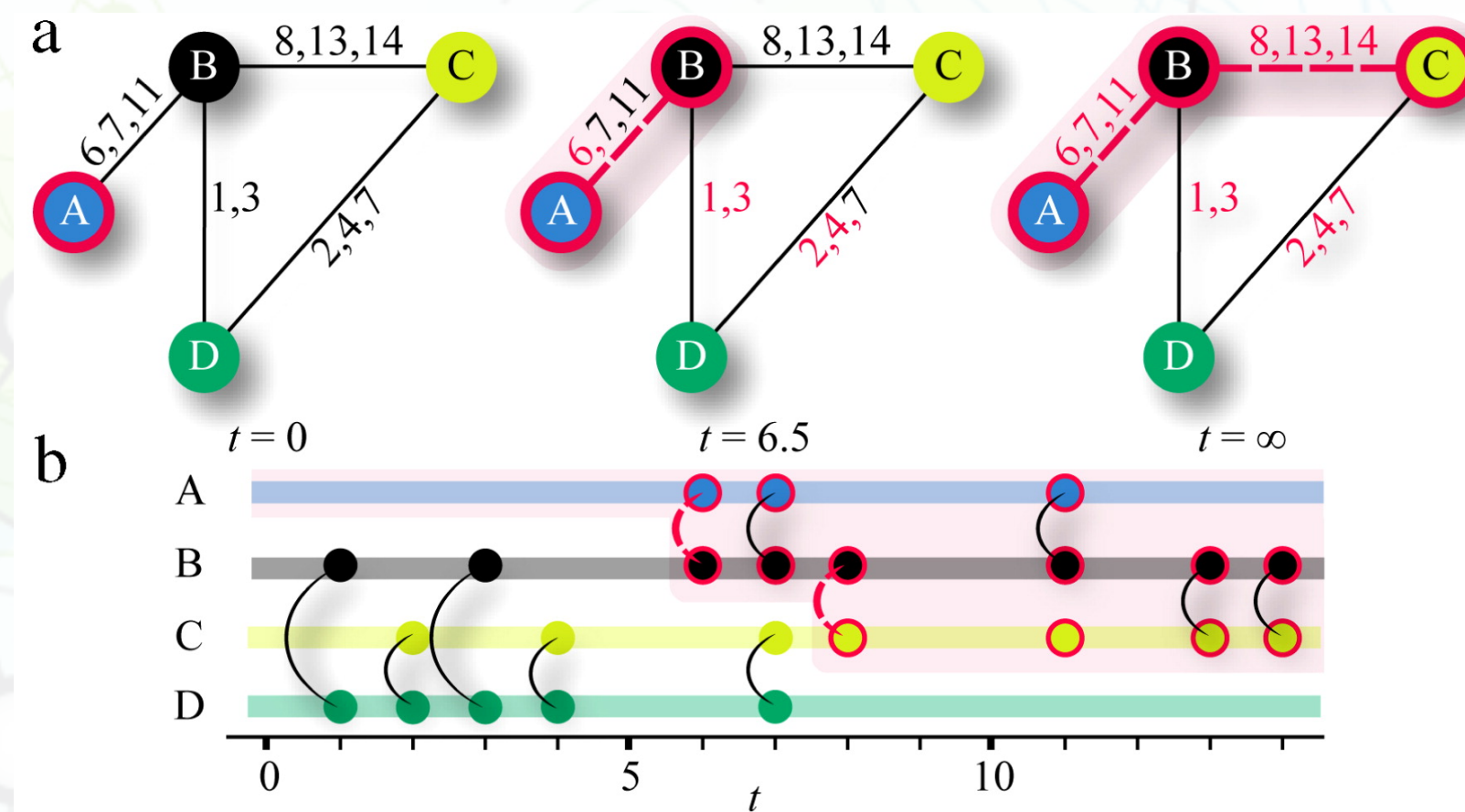
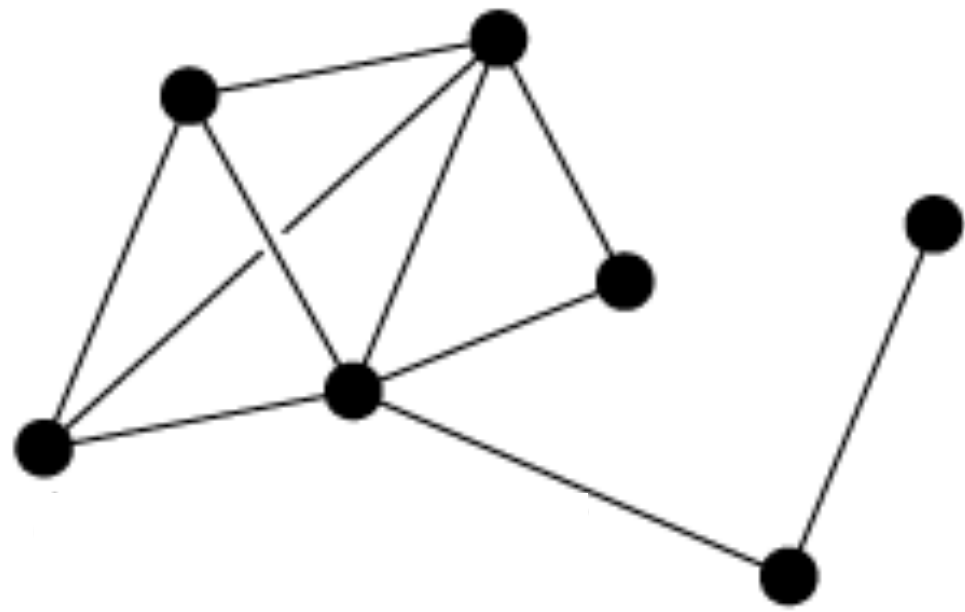
Extending classical graphs



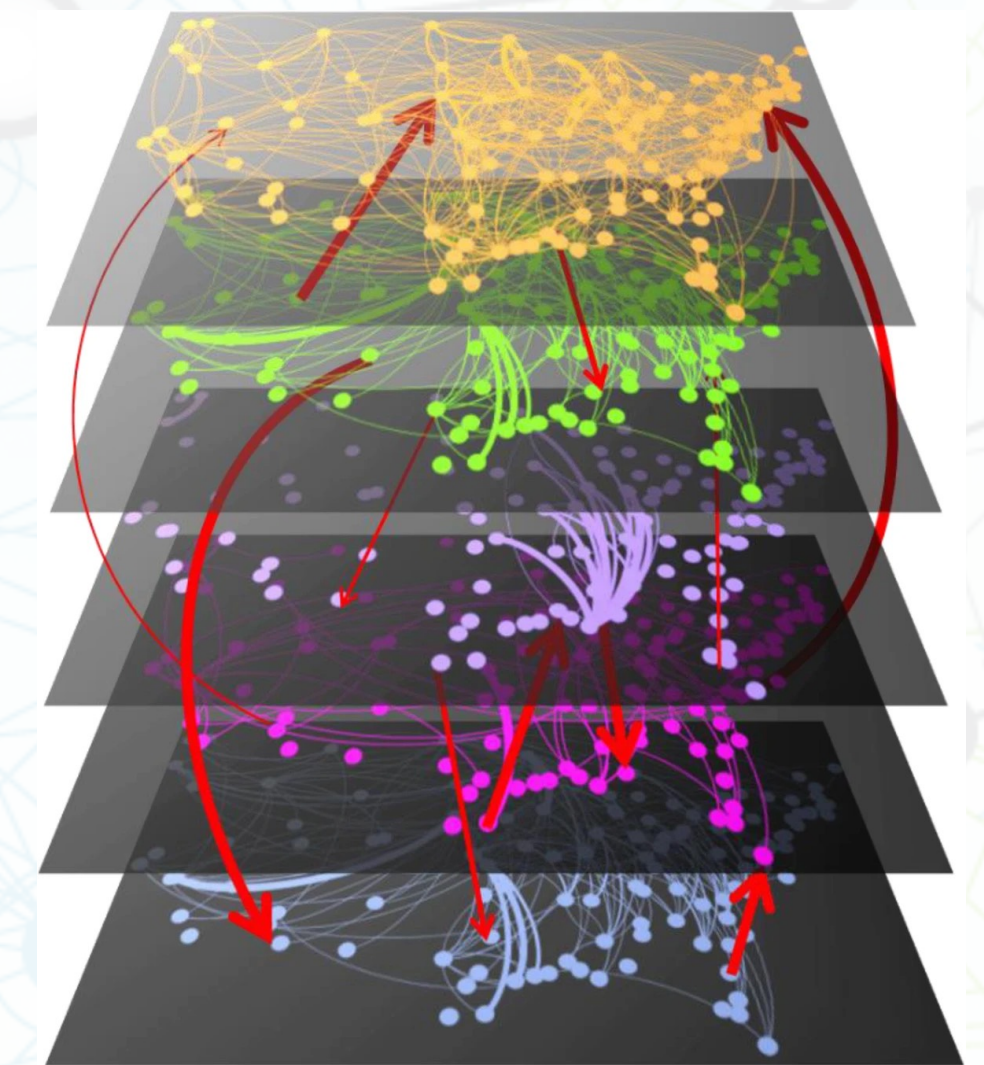
Temporal Networks

BEYOND CLASSICAL NETWORKS

Extending classical graphs



Temporal Networks



Multiplex/Multilayer Networks



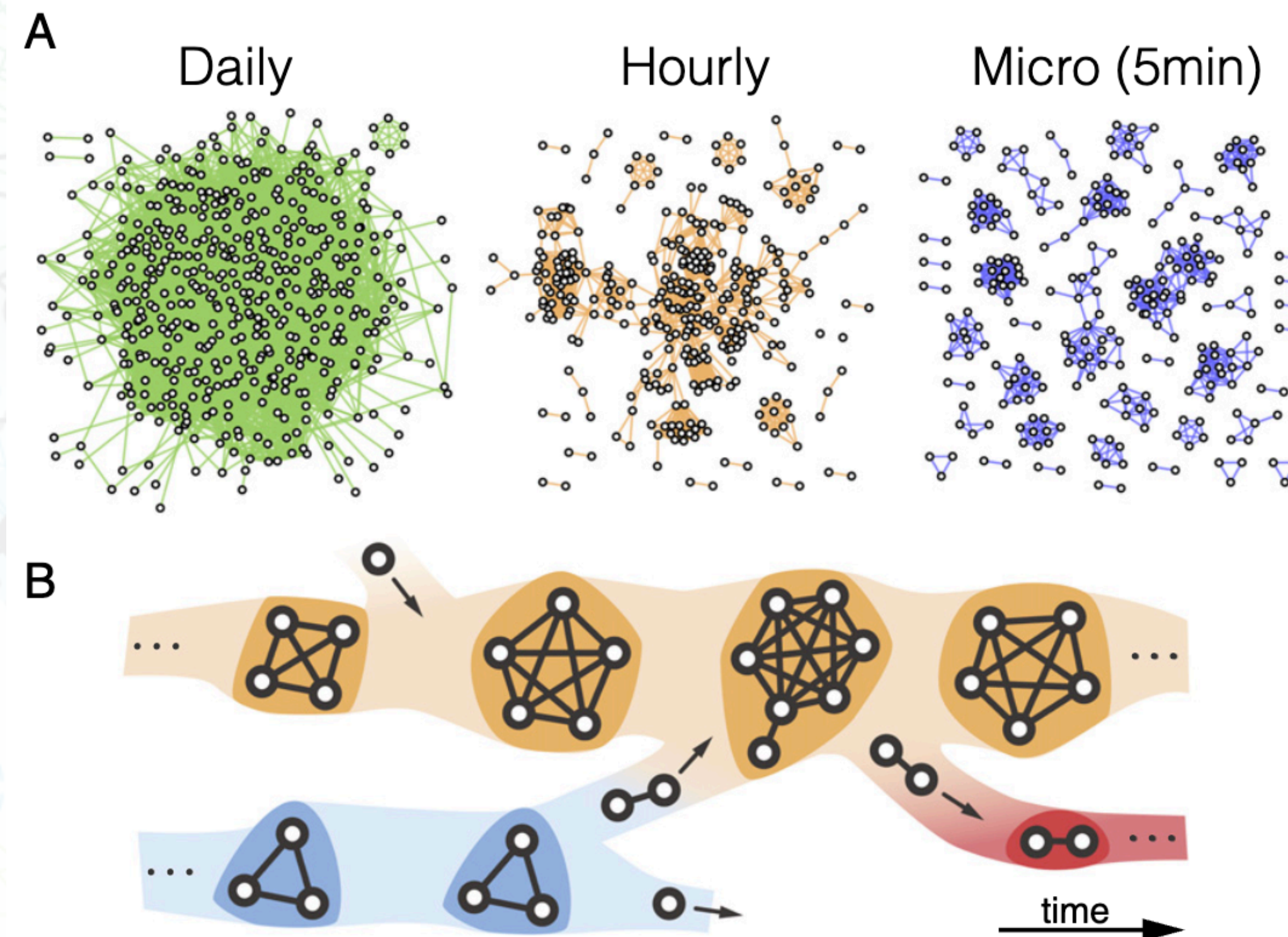
Fundamental structures of dynamic social networks

Vedran Sekara^a, Arkadiusz Stopczynski^{a,b}, and Sune Lehmann^{a,c,1}

^aDepartment of Applied Mathematics and Computer Science, Technical University of Denmark, DK-2800 Kongens Lyngby, Denmark, ^bMedia Lab, Massachusetts Institute of Technology, Cambridge, MA 02139; and ^cThe Niels Bohr Institute, University of Copenhagen, DK-2100 Copenhagen, Denmark

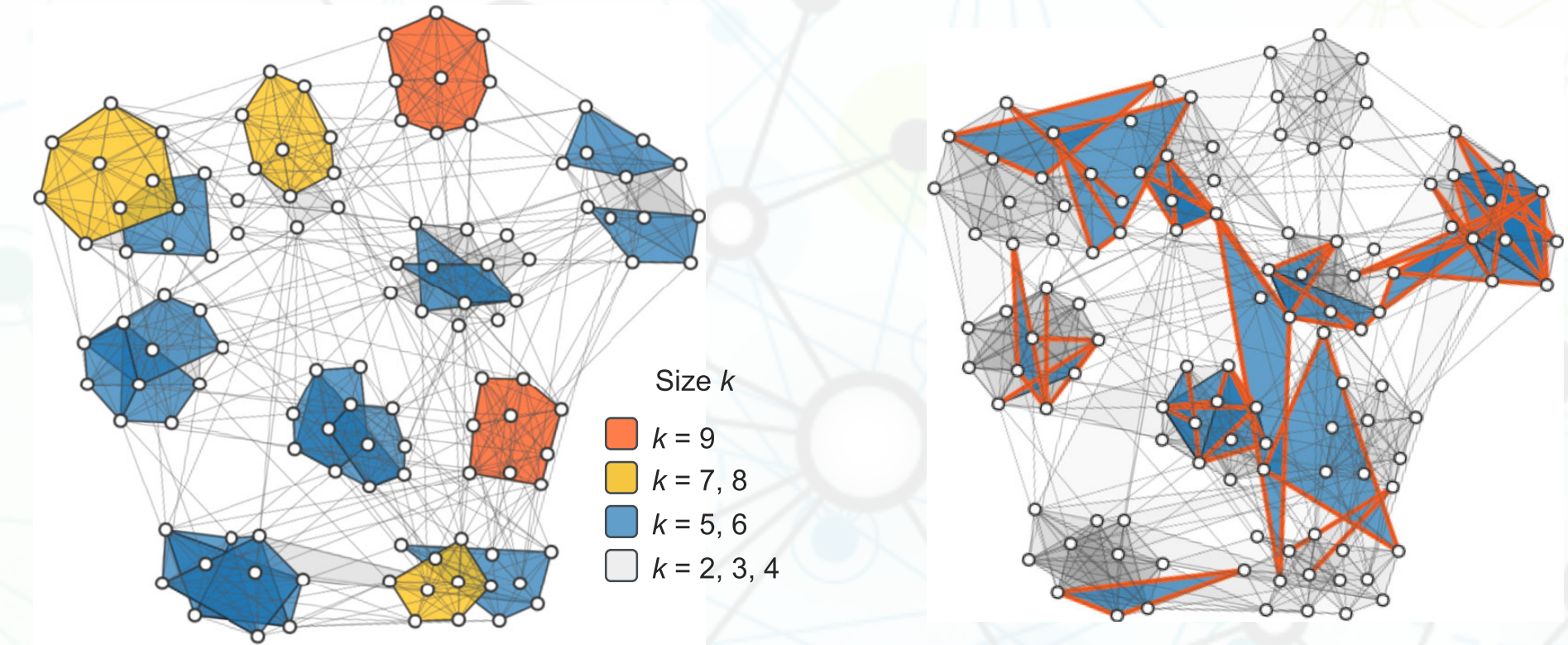
Edited by Albert-Laszlo Barabasi, Northeastern University, Boston, MA, and accepted by Editorial Board Member Kenneth W. Wachter July 12, 2016 (received for review March 9, 2016)

From pairwise to Higher-Order Interactions

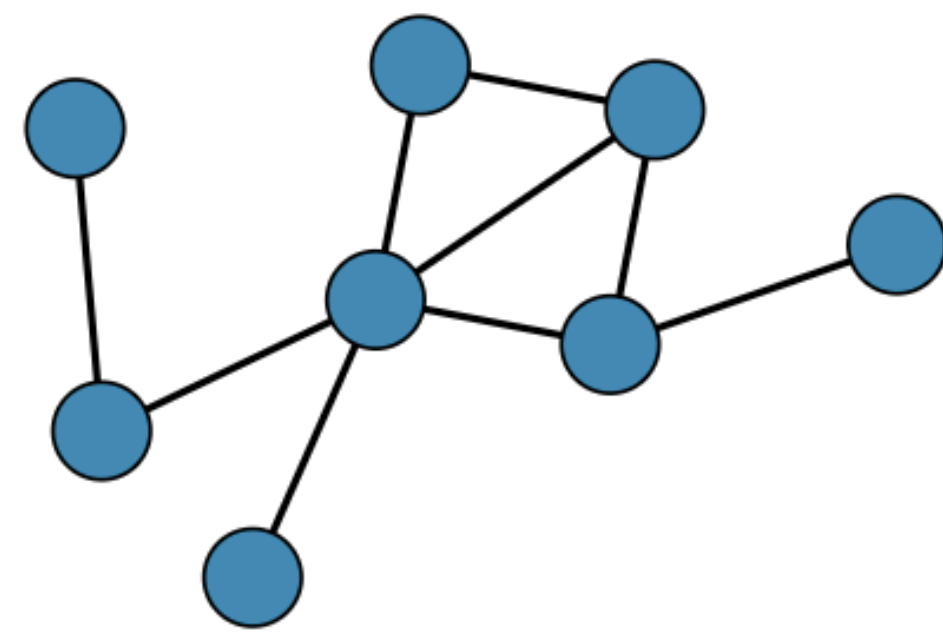


The physics of higher-order interactions in complex systems

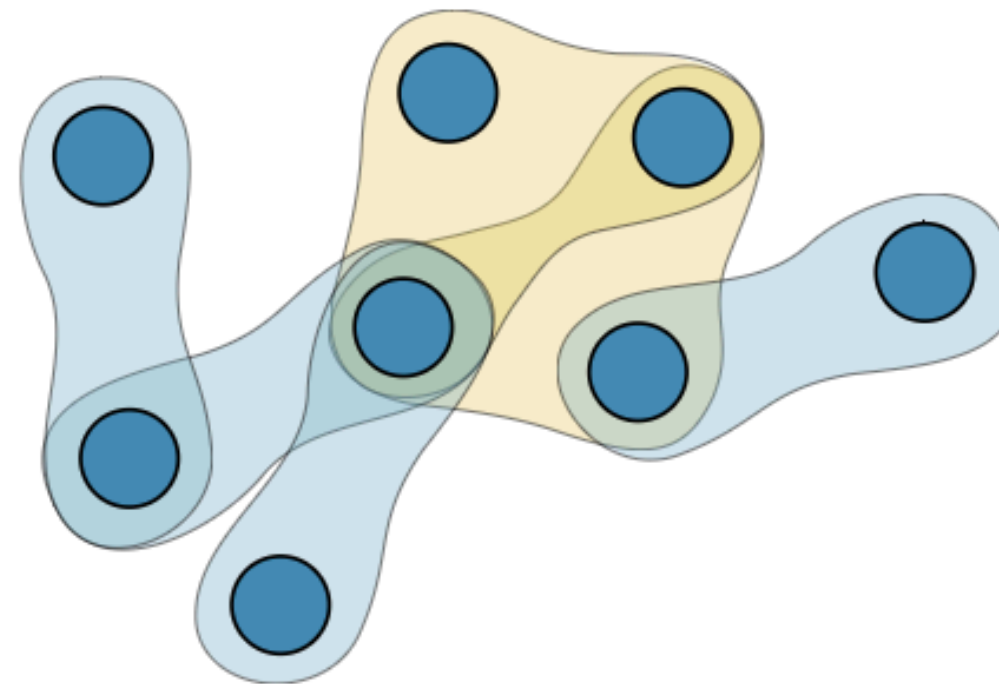
Federico Battiston¹✉, Enrico Amico^{2,3}, Alain Barrat^{4,5}, Ginestra Bianconi^{6,7},
Guilherme Ferraz de Arruda⁸, Benedetta Franceschiello^{9,10}, Iacopo Iacopini¹, Sonia Kéfi^{11,12},
Vito Latora^{6,13,14,15}, Yamir Moreno^{8,15,16,17}, Micah M. Murray^{9,10,18}, Tiago P. Peixoto^{1,19},
Francesco Vaccarino^{10,20} and Giovanni Petri^{8,21}✉



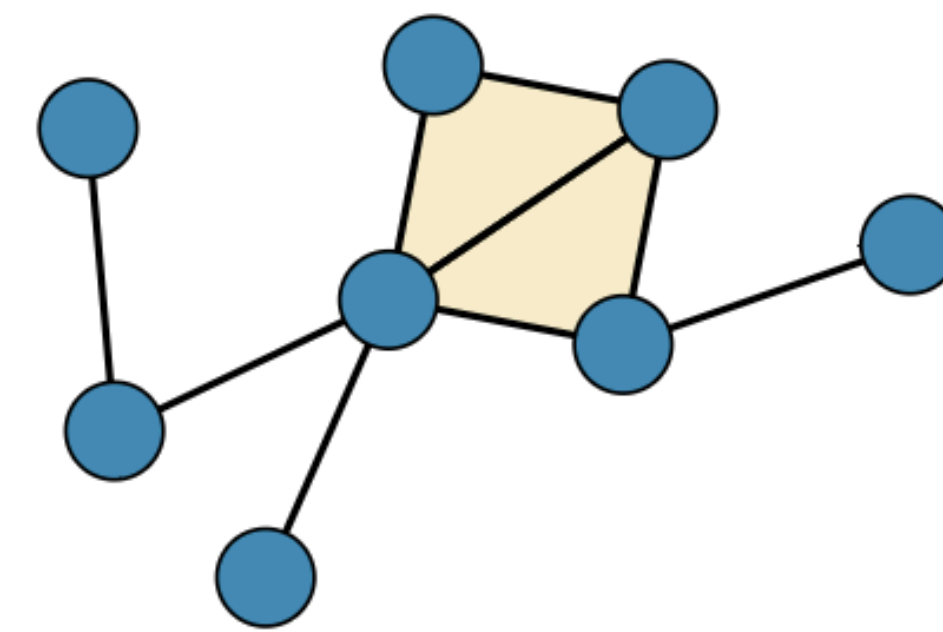
a Network



b Hypergraph



c Simplicial complex

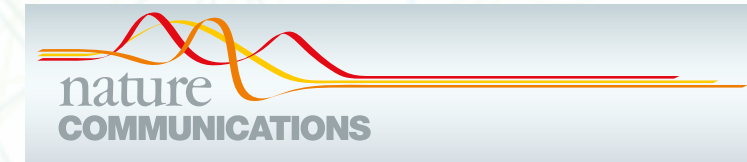


DYNAMICS WITH HIGHER ORDER INTERACTIONS

Social Contagion

ARTICLE

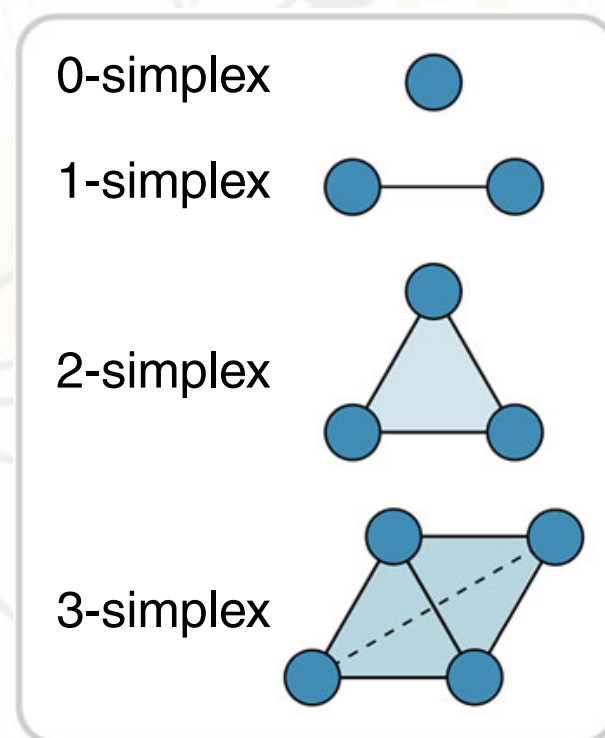
<https://doi.org/10.1038/s41467-019-10431-6>



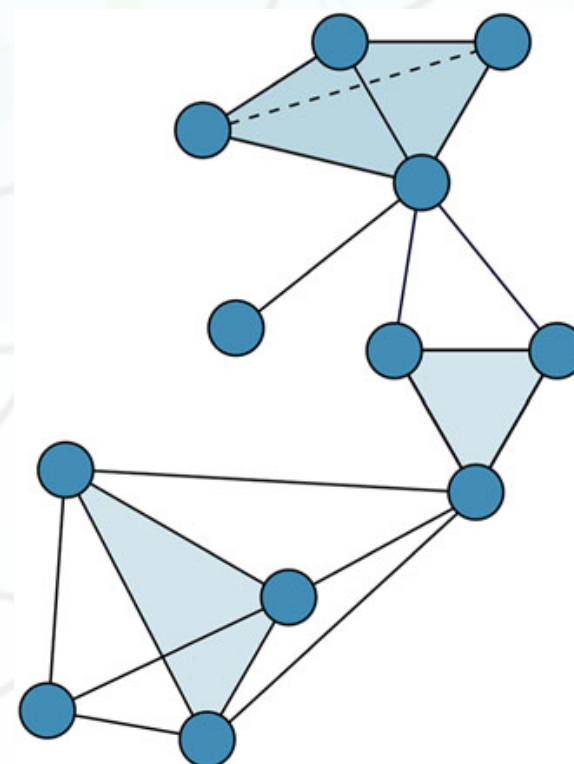
Simplicial models of social contagion

Iacopo Iacopini^{1,2}, Giovanni Petri^{3,4}, Alain Barrat^{3,5} & Vito Latora^{1,2,6,7}

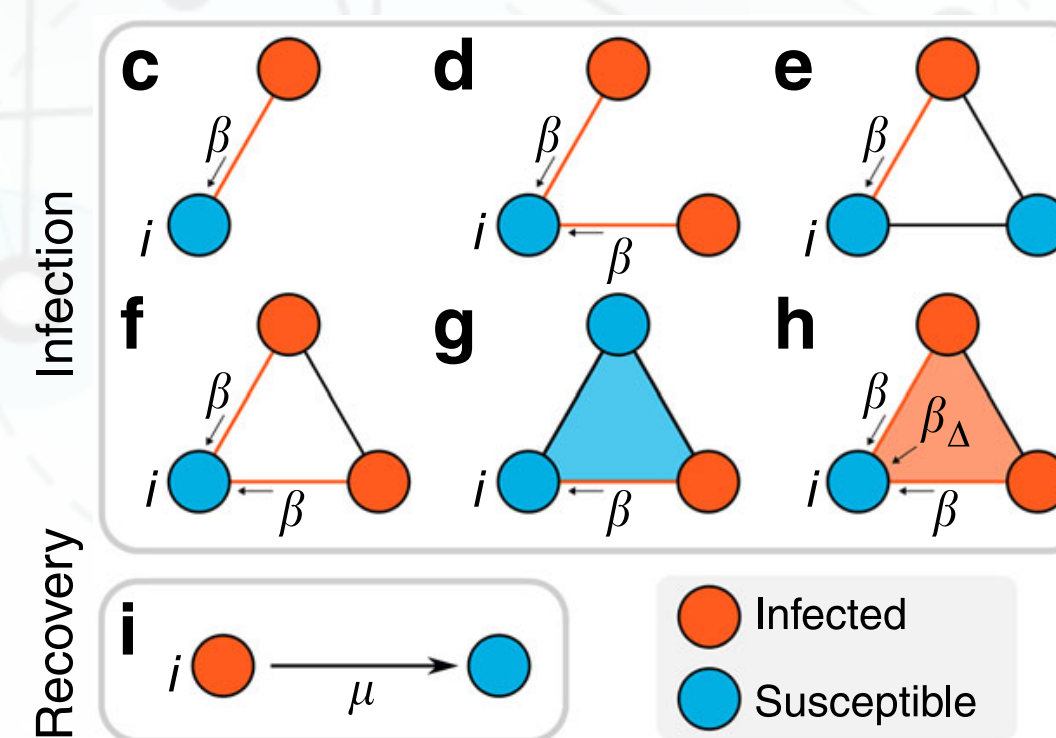
a d-dimensional group interactions



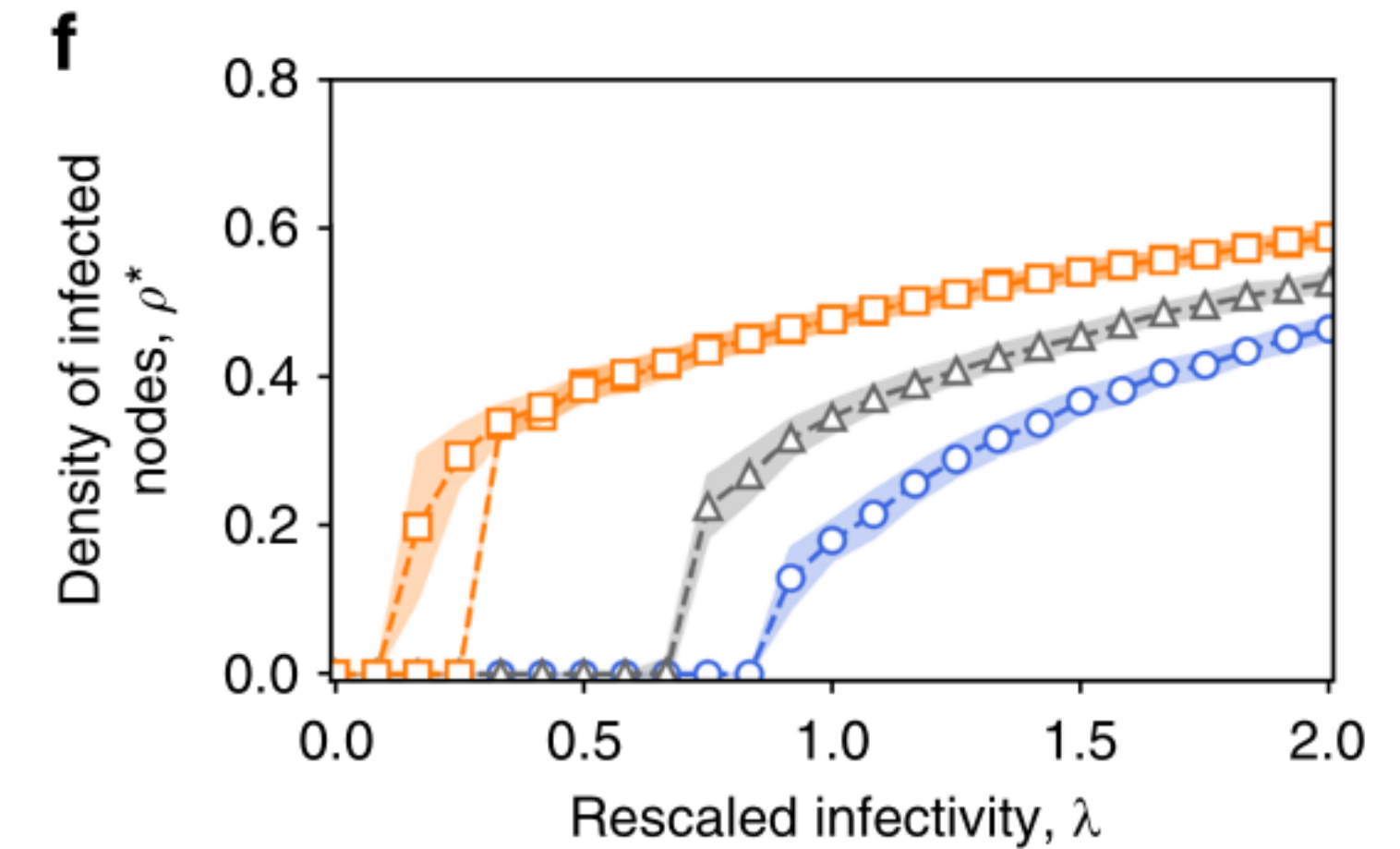
b Social structure: simplicial complex



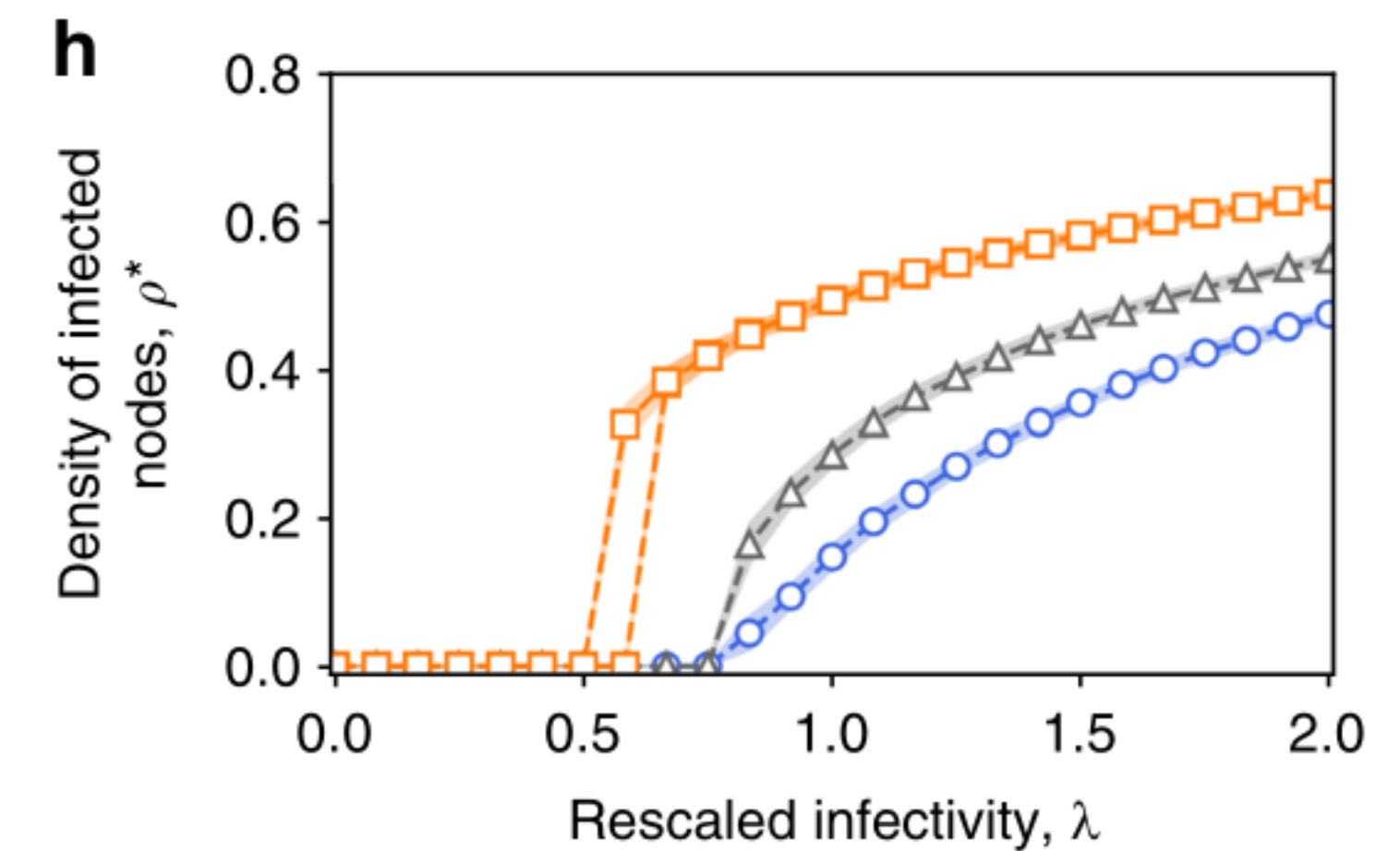
Simplicial contagion



Hospital

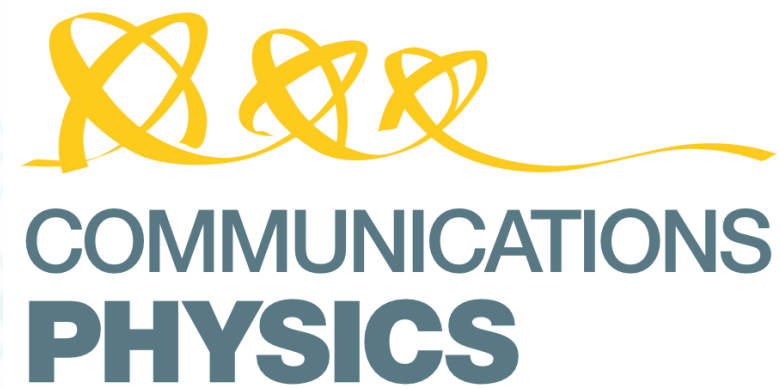


High school



DYNAMICS WITH HIGHER ORDER INTERACTIONS

Synchronization



ARTICLE

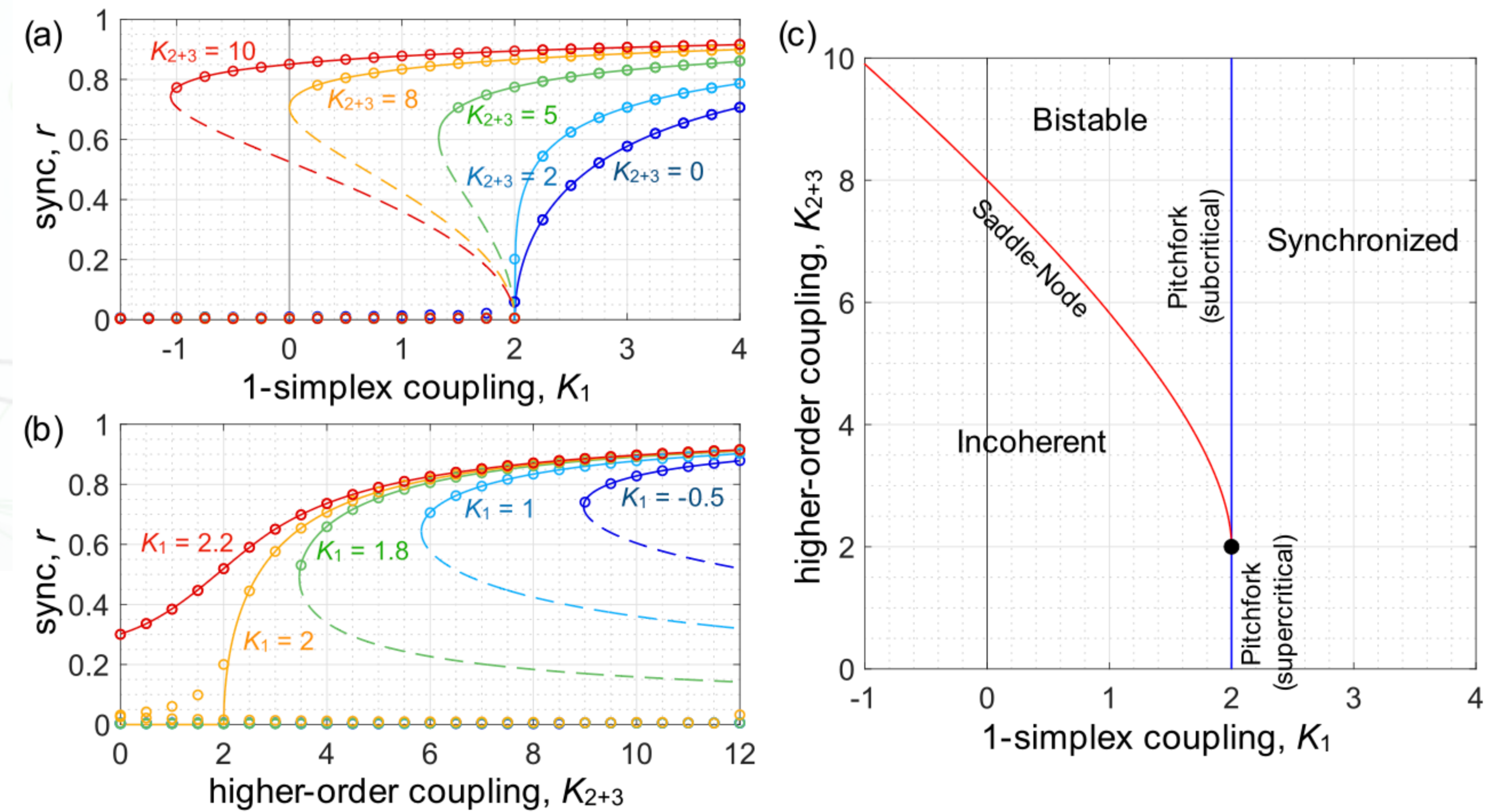
<https://doi.org/10.1038/s42005-020-00485-0>

OPEN

Higher order interactions in complex networks of phase oscillators promote abrupt synchronization switching

Per Sebastian Skardal¹ & Alex Arenas²

$$\begin{aligned}\dot{\theta}_i = & \omega_i + \frac{K_1}{\langle k^1 \rangle} \sum_{j=1}^N A_{ij} \sin(\theta_j - \theta_i) \\ & + \frac{K_2}{2\langle k^2 \rangle} \sum_{j=1}^N \sum_{l=1}^N B_{ijl} \sin(2\theta_j - \theta_l - \theta_i) \\ & + \frac{K_3}{6\langle k^3 \rangle} \sum_{j=1}^N \sum_{l=1}^N \sum_{m=1}^N C_{ijlm} \sin(\theta_j + \theta_l - \theta_m - \theta_i),\end{aligned}$$



DYNAMICS WITH HIGHER ORDER INTERACTIONS

Rumor spreading

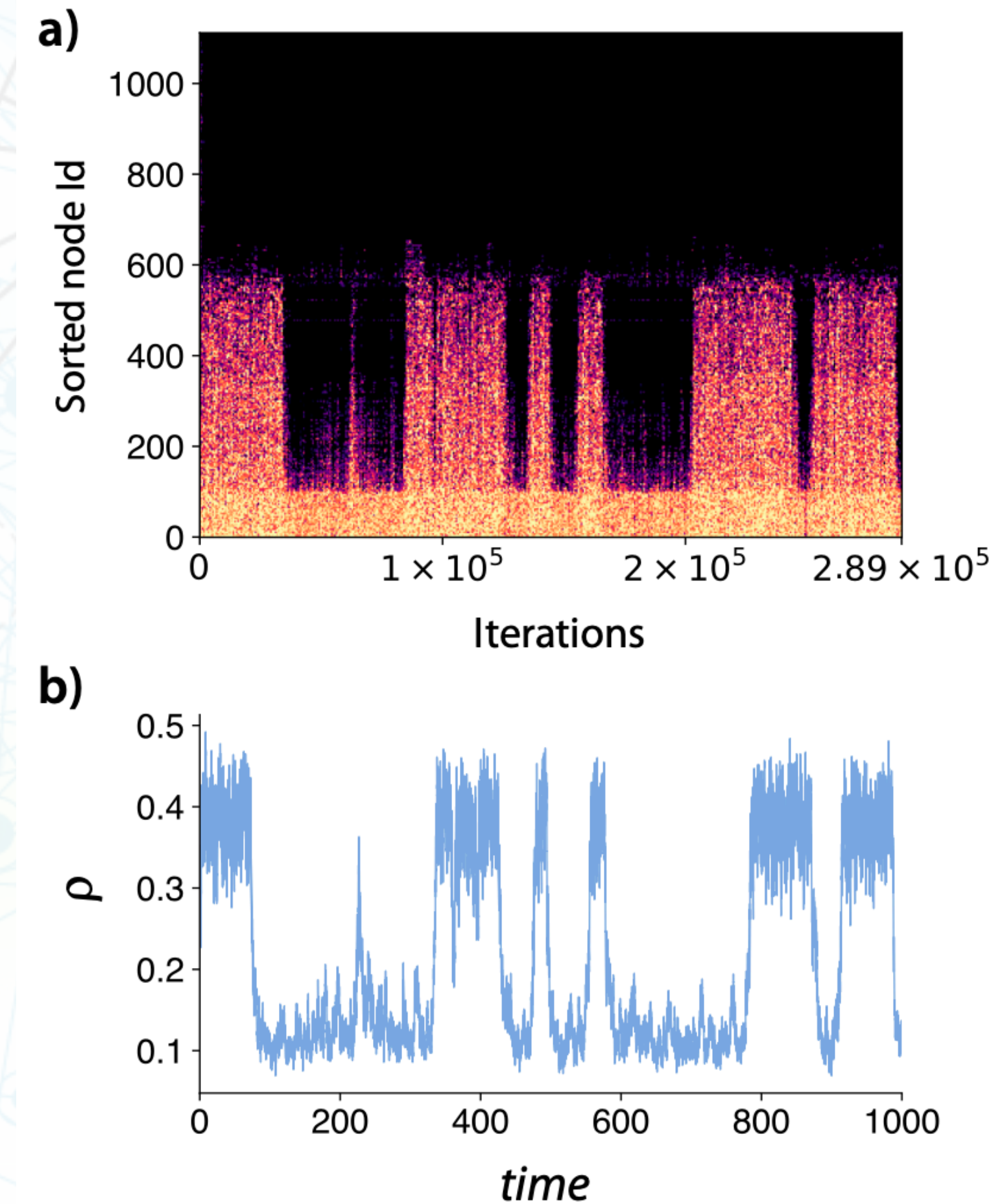
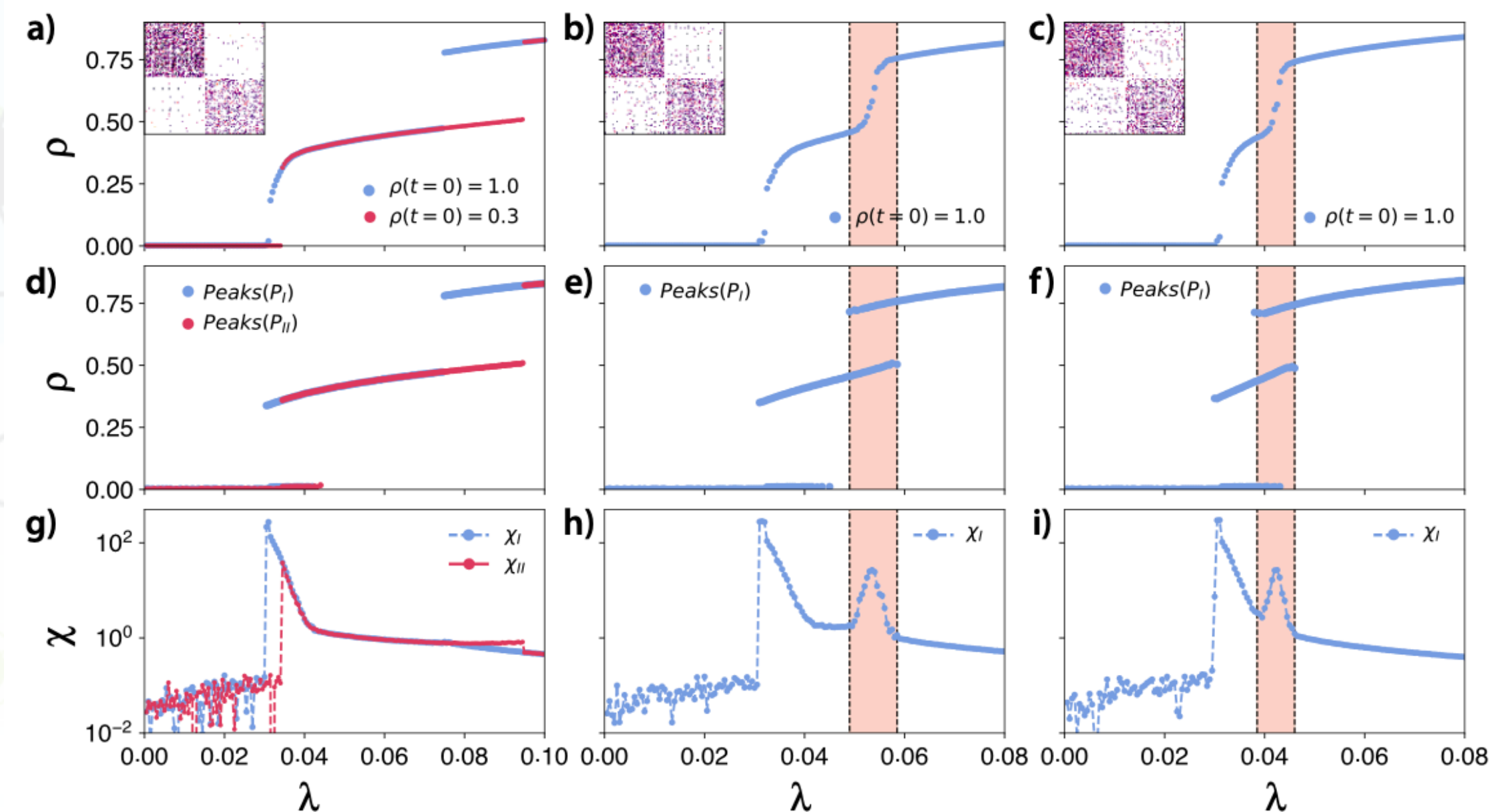
nature communications



Article

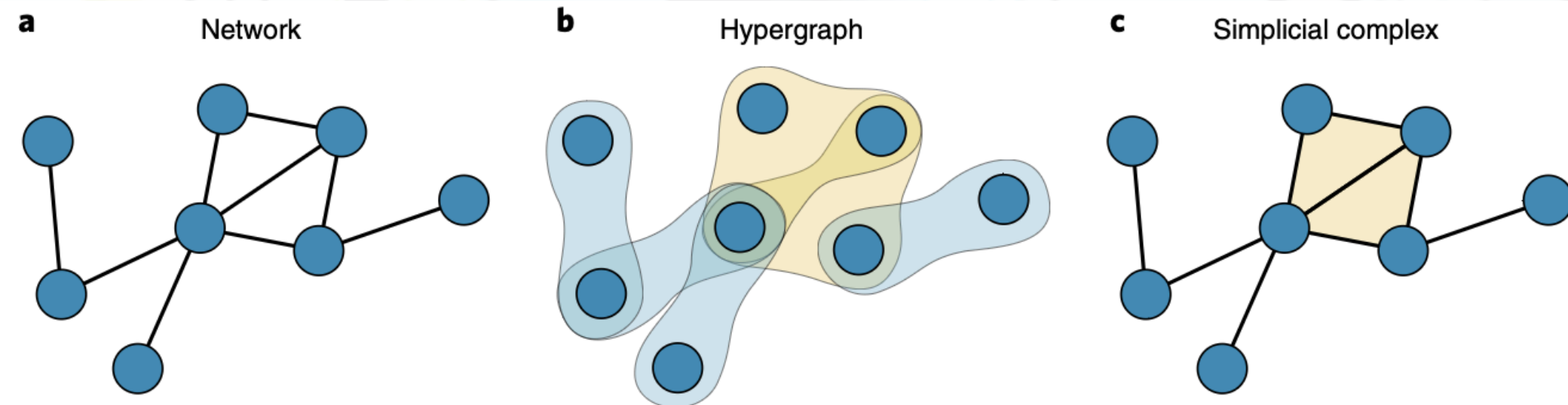
<https://doi.org/10.1038/s41467-023-37118-3>

Multistability, intermittency, and hybrid transitions in social contagion models on hypergraphs



The physics of higher-order interactions in complex systems

Federico Battiston¹✉, Enrico Amico^{2,3}, Alain Barrat^{4,5}, Ginestra Bianconi^{6,7},
Guilherme Ferraz de Arruda⁸, Benedetta Franceschiello^{9,10}, Iacopo Iacopini¹, Sonia Kéfi^{11,12},
Vito Latora^{6,13,14,15}, Yamir Moreno^{8,15,16,17}, Micah M. Murray^{9,10,18}, Tiago P. Peixoto^{1,19},
Francesco Vaccarino^{10,20} and Giovanni Petri^{8,21}✉



The idea of higher-order interactions is well-known in the setting of many-body physics, for example in strong interactions^{24,25} or van der Waals interactions²⁶, as well as in statistical mechanics²⁷. However, in all these cases, representations of higher-order interactions are simple in the sense that they do not contribute to the emerging complexity of the problem. In complex systems, typically described as networks, the story is different, and in many cases these interactions must be taken into account using more advanced mathematical structures, such as hypergraphs and simplicial complexes⁹. Several investigations have already shown that the presence of higher-order interactions may substantially impact the dynamics on networked systems, from diffusion^{28,29} and synchronization^{30,31} to social^{32–34} and evolutionary processes³⁵, possibly leading to the emergence of abrupt (explosive) transitions between states. Furthermore, although most research in complex systems focuses on the dynamical evolution of the states of the nodes, it is natural to consider that higher-order structures (described by hyperedges) could themselves possess a dynamical state, leading to a whole new panorama of dynamical processes. Finally, although many datasets can be easily visualized as networks, very few are readily described using a hypergraph representation. The challenge of going from the dynamics of units, and possibly information about their pairwise interactions, to a meaningful pattern of higher-order interactions between these units, remains substantial. In this Perspective, we outline the main signatures of new physics arising in higher-order systems, and we propose three key directions for future research.

Questions:

- How these new results are related with classical theory?
- Are there equivalent pairwise models?
- Do we always need them?

UNDERSTANDING HOIS

Ref. • "Higher-order contagion processes in 1.99 dimensions"

SM, Andrea Gabrielli, Pablo Villegas

arXiv:2502.18004

• "On the stability of competitive ecological communities with pairwise and higher-order interactions"

Marc Duran-Sala, SM, Violeta Calleja-Solanas.

arXiv:2501.09172

• "Demystifying HOI in ecology: is this description worth it?"

Santiago Lamata-Otín, Carlos Gómez Ambrosi, Violeta Calleja-Solanas, Jesús Gómez Gardeñes, SM.

in preparation

People



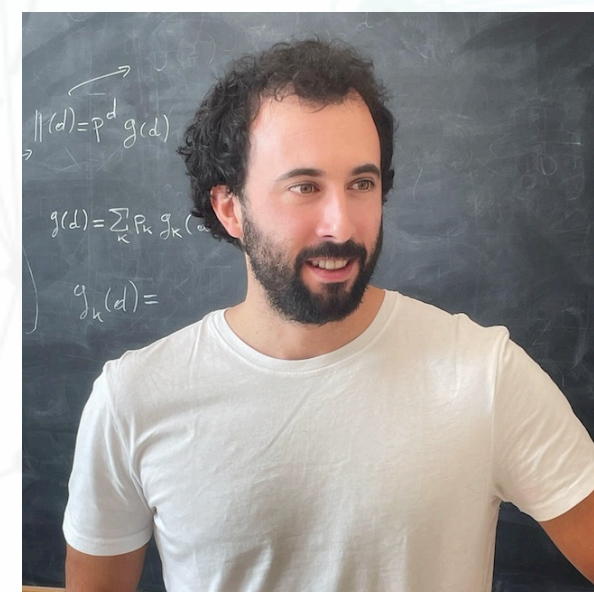
Carlos Gómez, UNIZAR



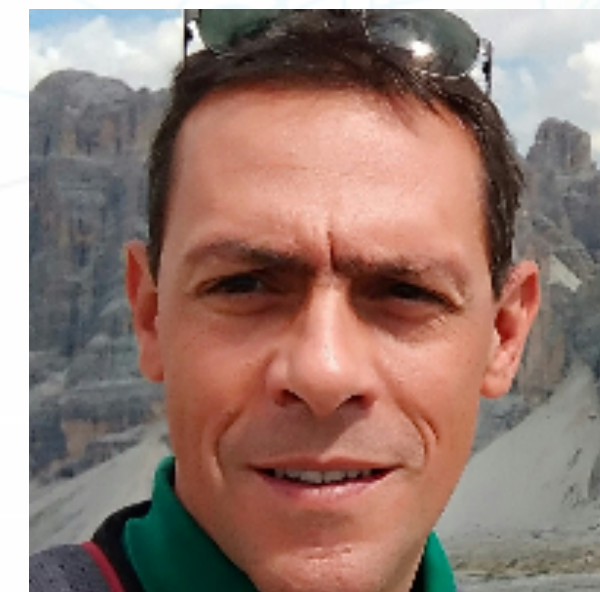
Jesús Gómez, UNIZAR



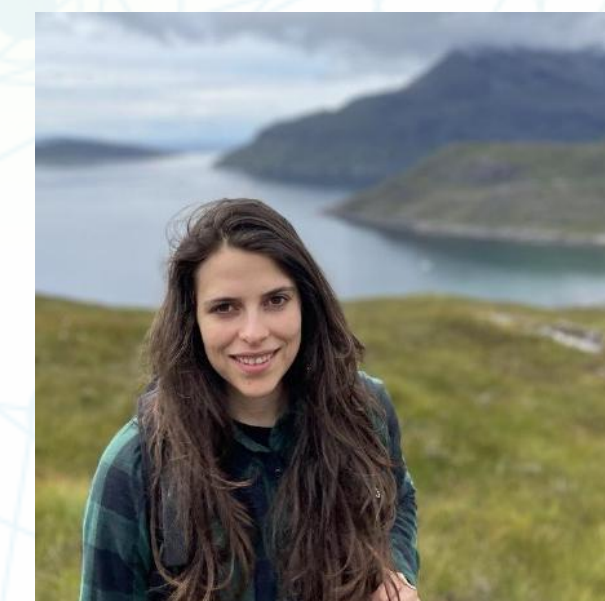
Santiago Lamata, UNIZAR



Pablo Villegas, CREF



Andrea Gabrielli, Roma TRE



Violeta Calleja, EBD CSIC



Marc Duran, EPFL

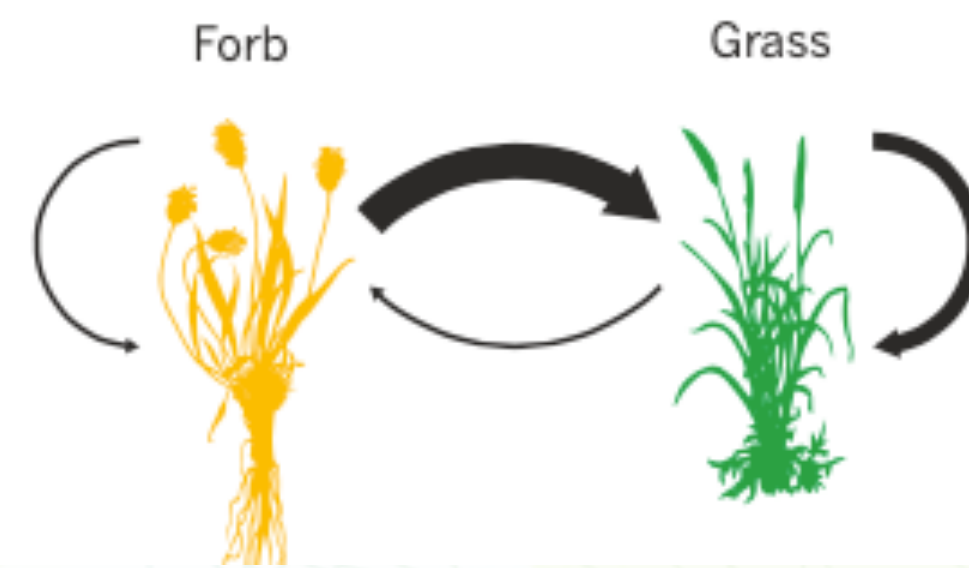


DO WE ALWAYS NEED THEM?

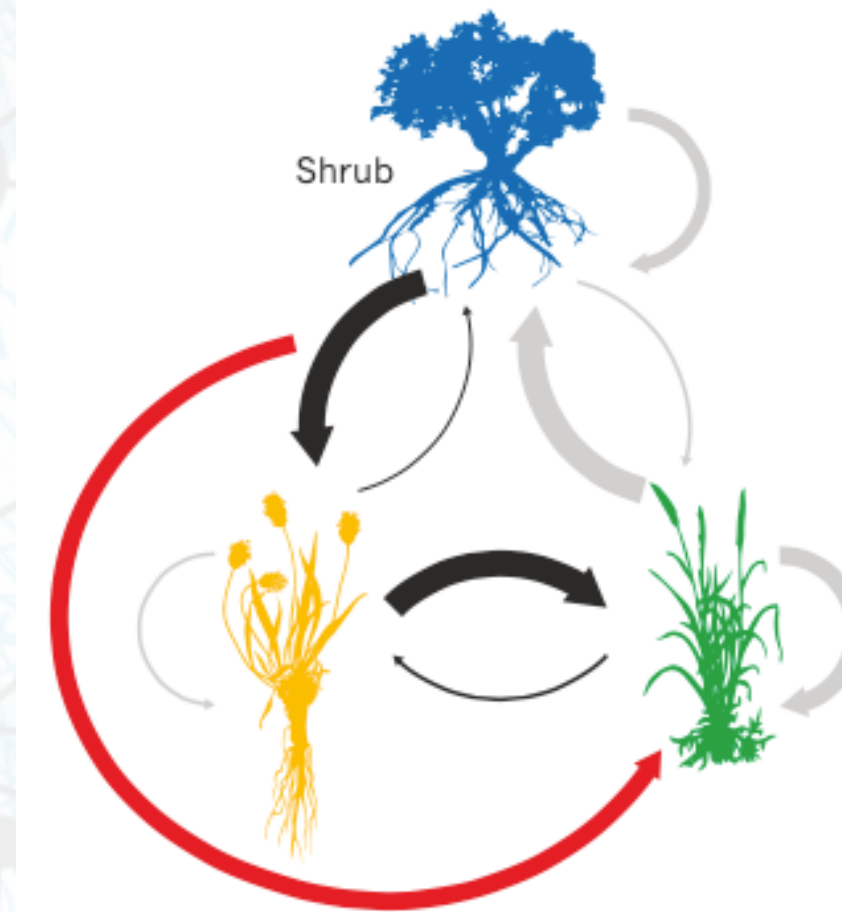
BEYOND PAIRWISE INTERACTIONS IN ECOLOGY

Ecological dynamics

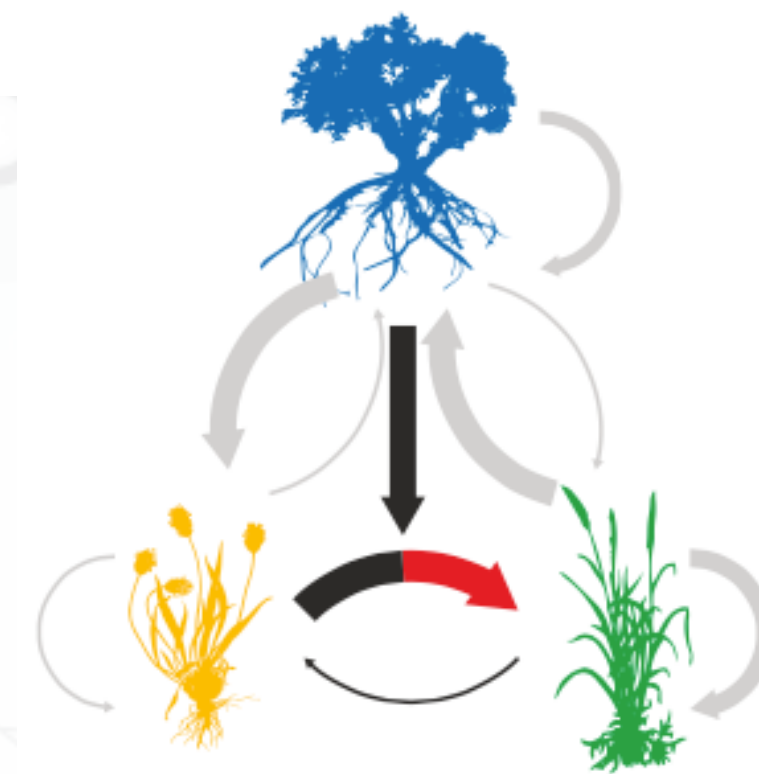
Pairwise



Interaction chain



Higher-Order Interaction



REVIEW

doi:10.1038/nature22898

Beyond pairwise mechanisms of species coexistence in complex communities

Jonathan M. Levine¹, Jordi Bascompte², Peter B. Adler³ & Stefano Allesina⁴

Received: 2 December 2021 | Revised: 6 April 2022 | Accepted: 14 April 2022

DOI: 10.1111/ele.14022

PERSPECTIVE

ECOLOGY LETTERS  WILEY

Detecting and interpreting higher-order interactions in ecological communities

Andrew R. Kleinhesslink¹ | Nathan J. B. Kraft¹ | Stephen W. Pacala² |
Jonathan M. Levine² 

Levine et al. Nature 546, 56–64 (2017)

HOIs and the stability of ecological communities

LETTER

doi:10.1038/nature23273

Higher-order interactions stabilize dynamics in competitive network models

Jacopo Grilli¹, György Barabás¹, Matthew J. Michalska-Smith¹ & Stefano Allesina^{1,2,3}

nature
ecology & evolution

ARTICLES

PUBLISHED: 17 FEBRUARY 2017 | VOLUME: 1 | ARTICLE NUMBER: 0062

Higher-order interactions capture unexplained complexity in diverse communities

Margaret M. Mayfield^{1*} and Daniel B. Stouffer^{2*}

ARTICLE

Received 16 Jan 2016 | Accepted 20 Jun 2016 | Published 2 Aug 2016

DOI: 10.1038/ncomms12285

OPEN

High-order species interactions shape ecosystem diversity

Eyal Bairey¹, Eric D. Kelsic^{2,†} & Roy Kishony^{2,3}

VOL. 203, NO. 4 THE AMERICAN NATURALIST APRIL 2024

Multitrophic Higher-Order Interactions Modulate Species Persistence

Lisa Buche,^{1,*} Ignasi Bartomeus,² and Oscar Godoy^{2,3}

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INTERFACE

royalsocietypublishing.org/journal/rsif

Ecological models: higher complexity in, higher feasibility out

Mohammad AlAdwani and Serguei Saavedra

ARTICLE

Received 16 Jan 2016 | Accepted 20 Jun 2016 | Published 2 Aug 2016

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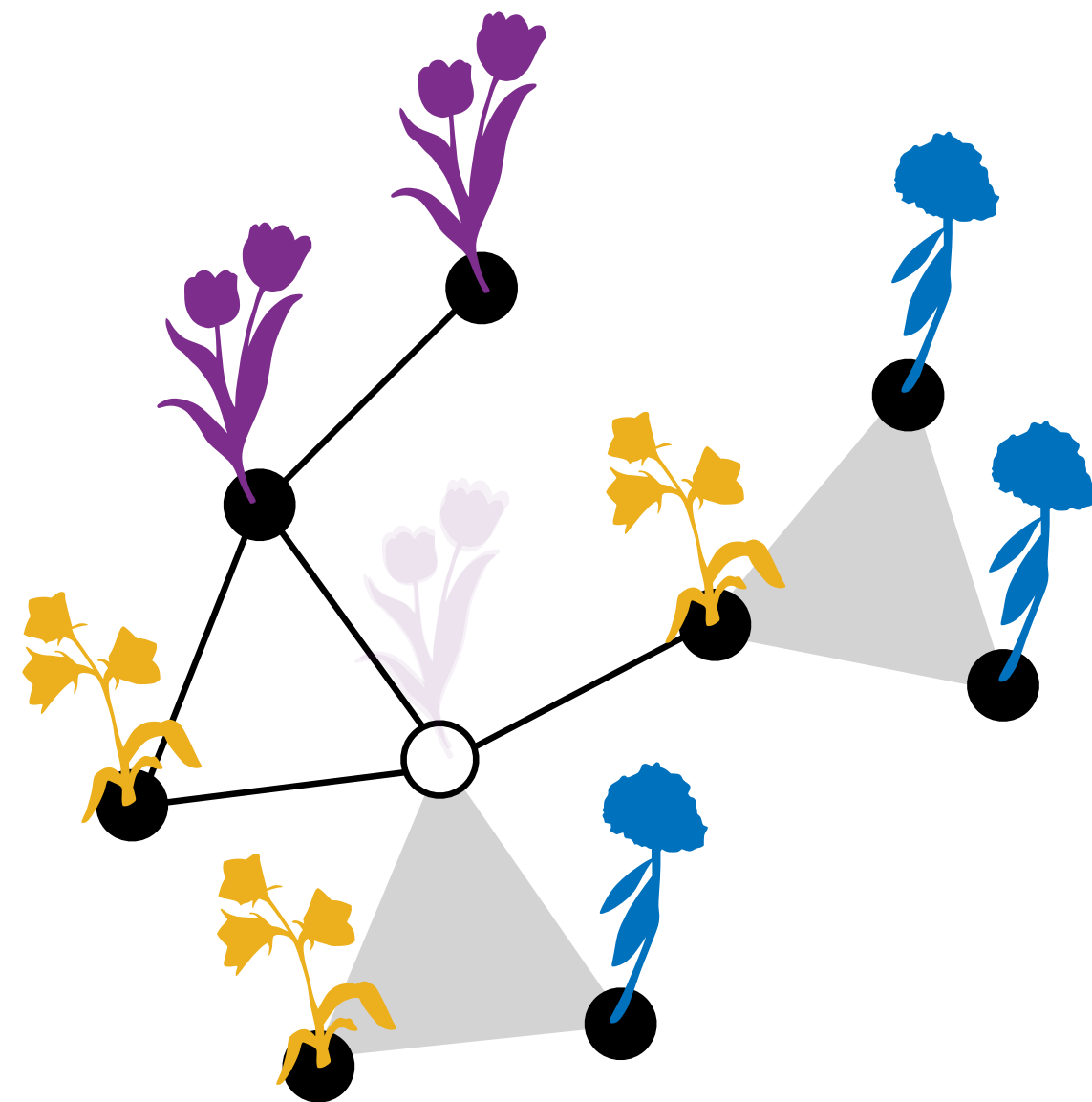
ECOLOGY LETTERS

Ecology Letters, (2019) 22: 423–436

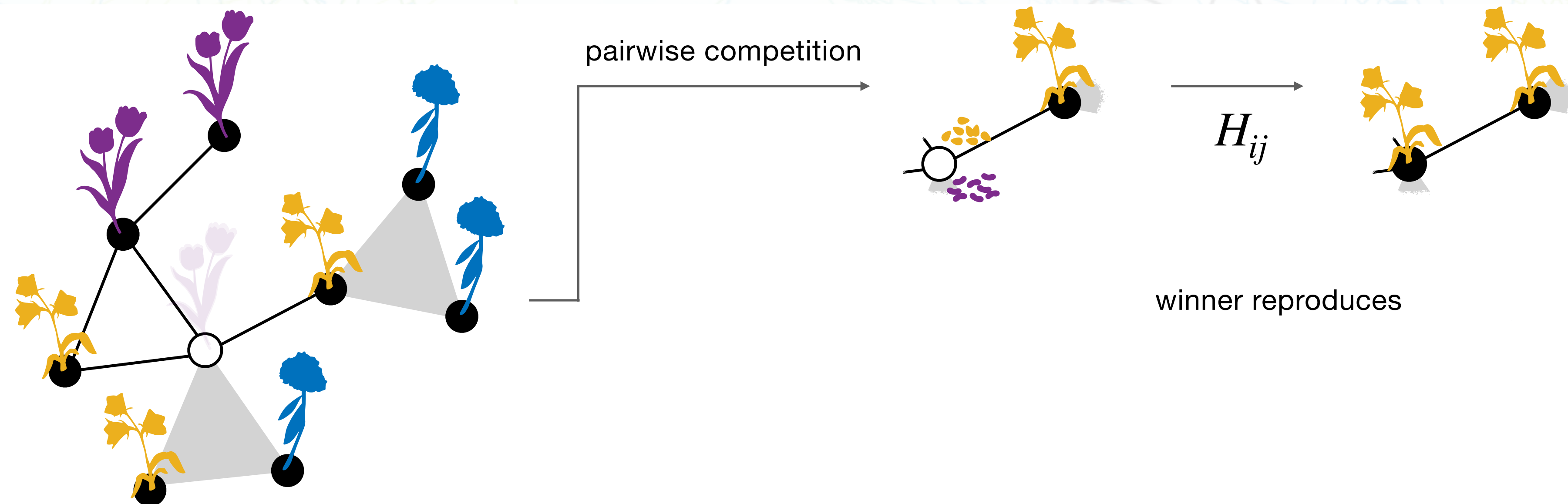
doi: 10.1111/ele.13211

The mechanistic basis for higher-order interactions and non-additivity in competitive communities

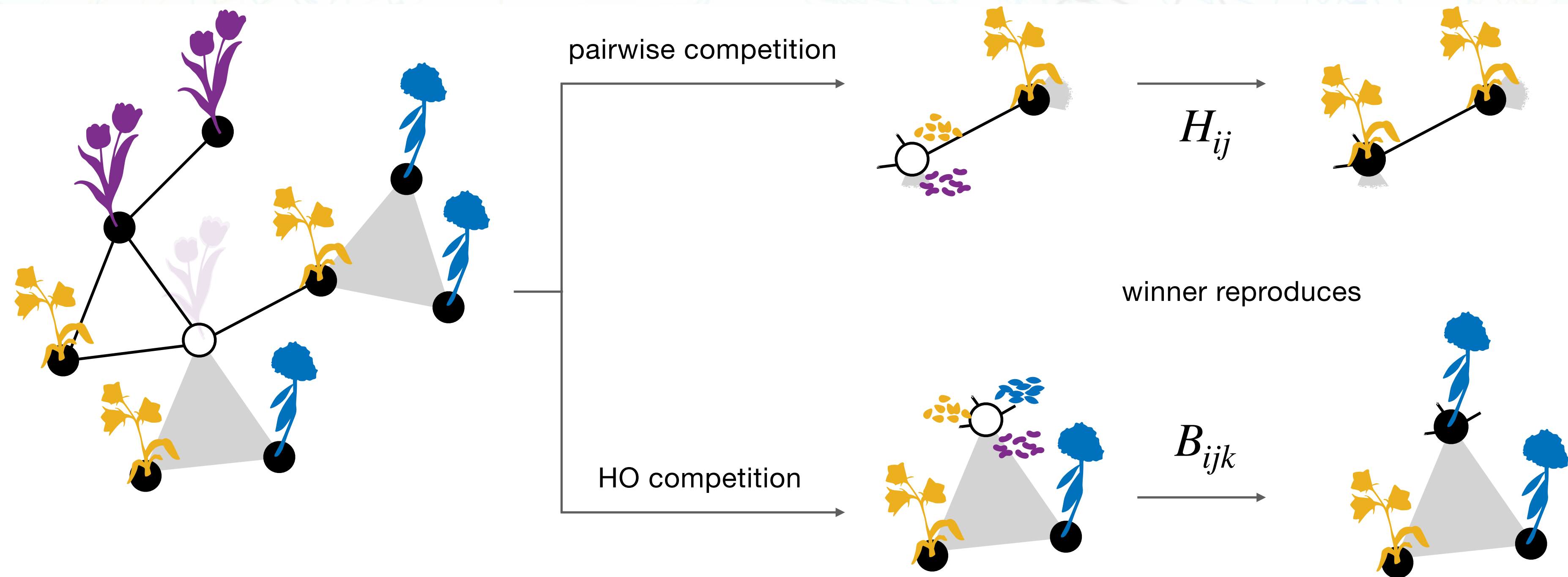
COMPETITIVE COMMUNITY MODEL



COMPETITIVE COMMUNITY MODEL



COMPETITIVE COMMUNITY MODEL



Higher-order interactions stabilize dynamics in competitive network models

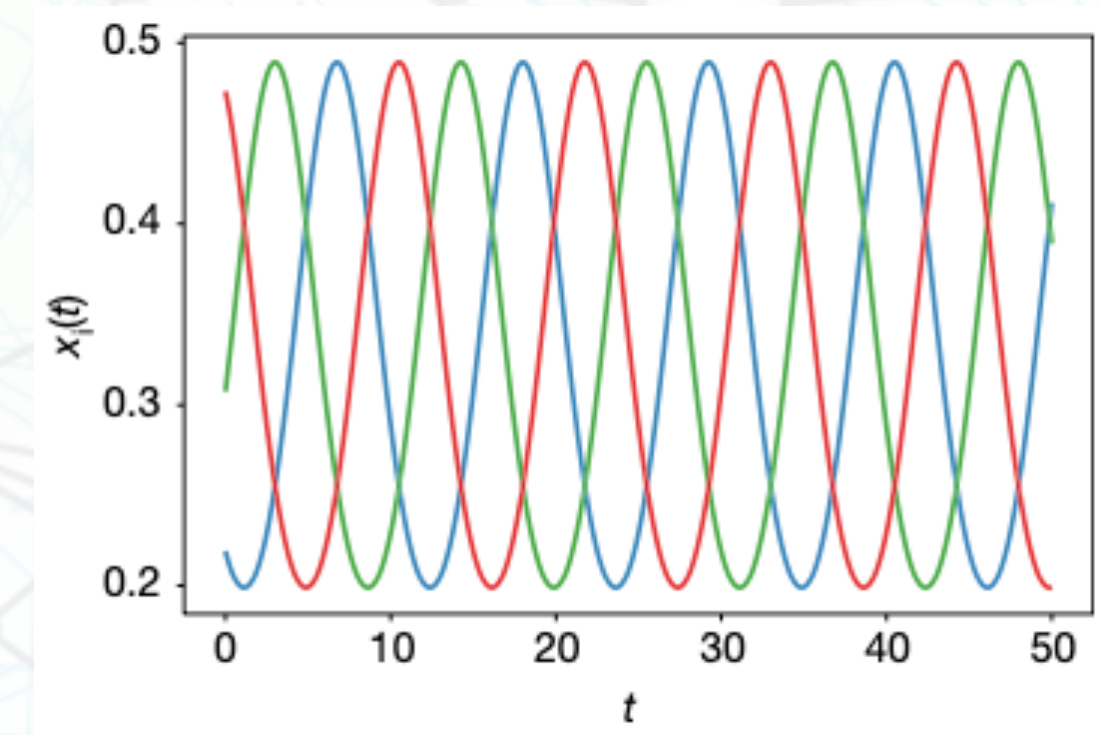
Jacopo Grilli¹, György Barabás¹, Matthew J. Michalska-Smith¹ & Stefano Allesina^{1,2,3}

Described by a Replicator Equation (well mixed case)

Pairwise interactions

$$\frac{dx_i}{dt} = x_i \left(\frac{D(x)}{F(x)^2} f_i \sum_j 2H_{ij} f_j x_j - d_i \right)$$

Neutral circles



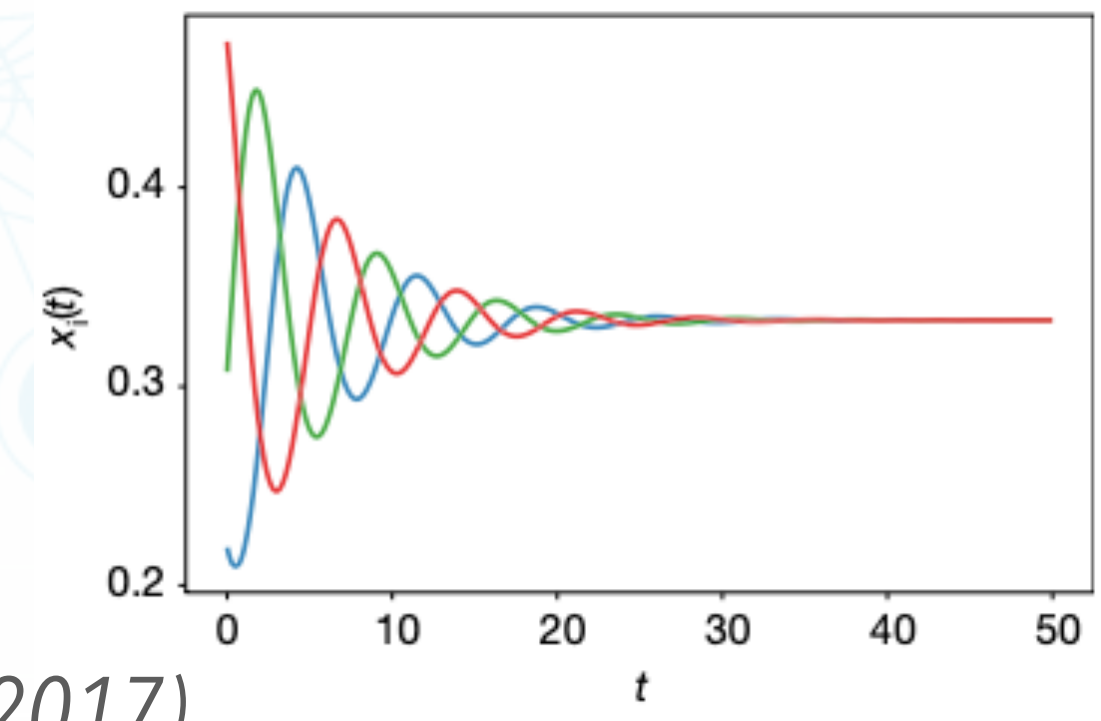
With:

f_i birth rate
 d_i death rate

Higher-order interactions

$$\frac{dx_i}{dt} = x_i \left(\frac{D(x)}{F(x)^3} f_i \sum_{j,k} B_{ijk} f_j x_j f_k x_k - d_i \right)$$

Fixed point



$$F(x) = \sum_i f_i x_i$$
$$D(x) = \sum_i d_i x_i$$

Higher-order interactions stabilize dynamics in competitive network models

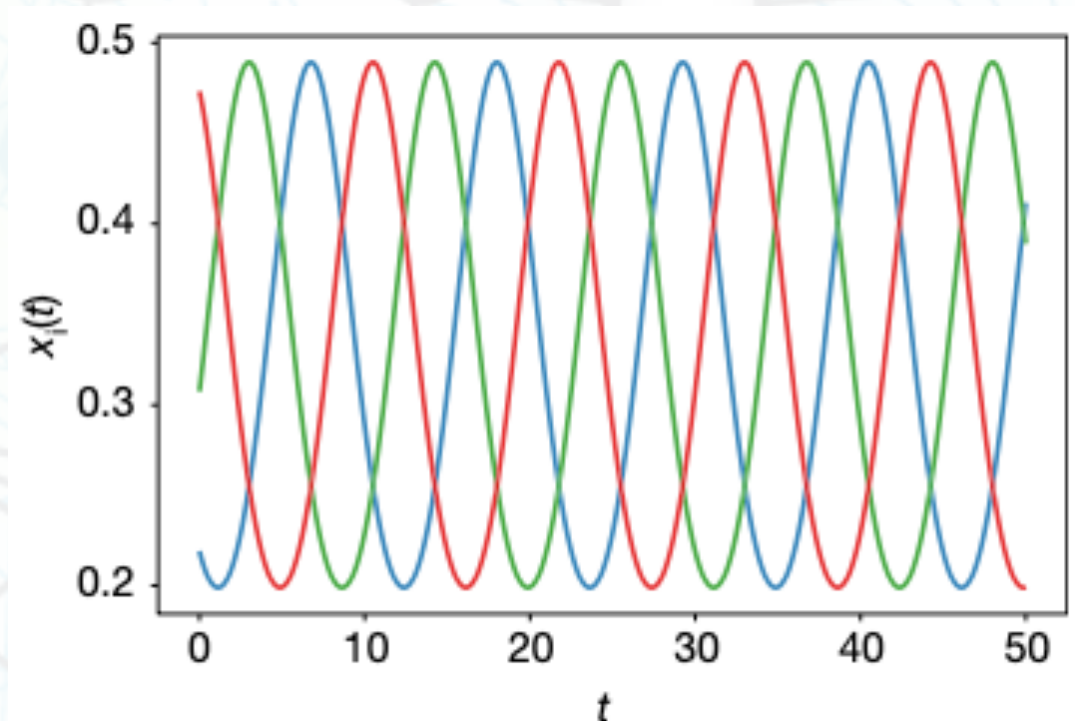
Jacopo Grilli¹, György Barabás¹, Matthew J. Michalska-Smith¹ & Stefano Allesina^{1,2,3}

Described by a Replicator Equation (well mixed case)

Pairwise interactions

$$\frac{dx_i}{dt} = x_i \left(\frac{D(x)}{F(x)^2} f_i \sum_j 2H_{ij} f_j x_j - d_i \right)$$

Neutral circles



With:

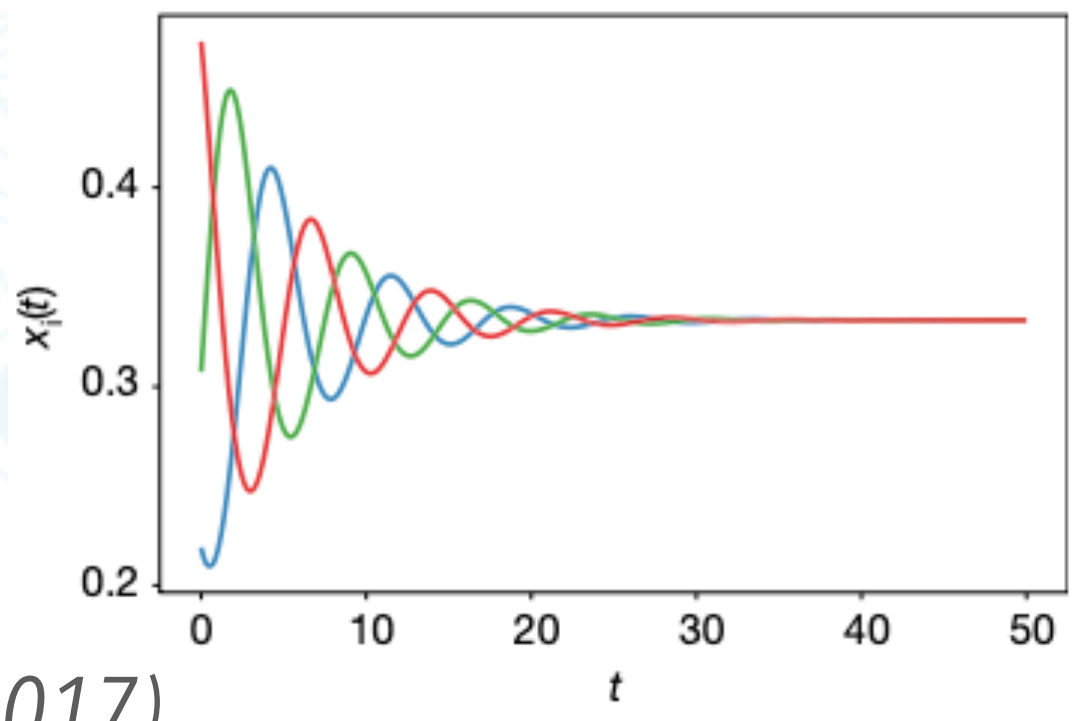
f_i birth rate
 d_i death rate

What happens in more realistic scenarios?

Higher-order interactions

$$\frac{dx_i}{dt} = x_i \left(\frac{D(x)}{F(x)^3} f_i \sum_{j,k} B_{ijk} f_j x_j f_k x_k - d_i \right)$$

Fixed point



$$F(x) = \sum_i f_i x_i$$
$$D(x) = \sum_i d_i x_i$$

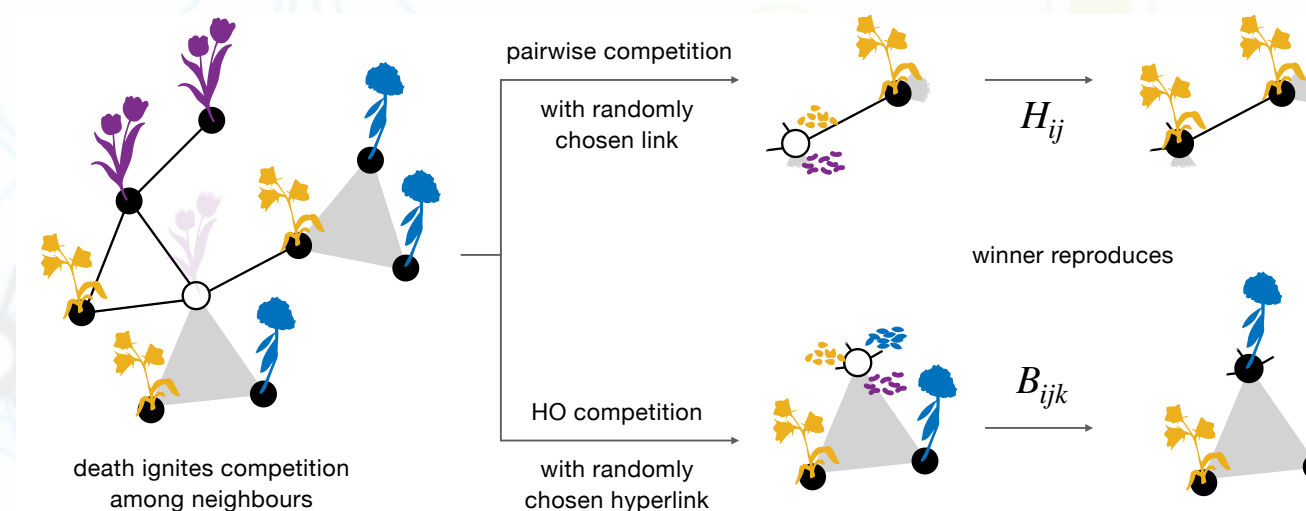
COMPETITIVE COMMUNITY MODEL

Described by a Replicator Equation (well mixed case)

Full model

$$\frac{dx_i}{dt} = (1 - \alpha) \left[x_i \left(\frac{D(x)}{F(x)^2} f_i \sum_j 2H_{ij} f_j x_j - d_i \right) \right] + \alpha \left[x_i \left(\frac{D(x)}{F(x)^3} f_i \sum_{j,k} B_{ijk} f_j x_j f_k x_k - d_i \right) \right]$$

α intensity of H0Is



With:

f_i birth rate
 d_i death rate

$$F(x) = \sum_i f_i x_i$$

$$D(x) = \sum_i d_i x_i$$

IDENTICAL PHYSIOLOGICAL RATES

Special case:
Identical physiological rates

$$\begin{aligned} f_i \text{ birth rate} &= 1 \\ d_i \text{ death rate} &= 1 \end{aligned} \quad \begin{aligned} F(x) &= \sum f_i x_i = 1 \\ D(x) &= \sum_i d_i x_i = 1 \end{aligned}$$

It reduces to:

$$\frac{dx_i}{dt} = (1 - \alpha) \left(-x_i + 2 \sum_j H_{ij} x_i x_j \right) + \alpha \left(-x_i + \sum_{j,k} B_{ijk} x_i x_j x_k \right)$$

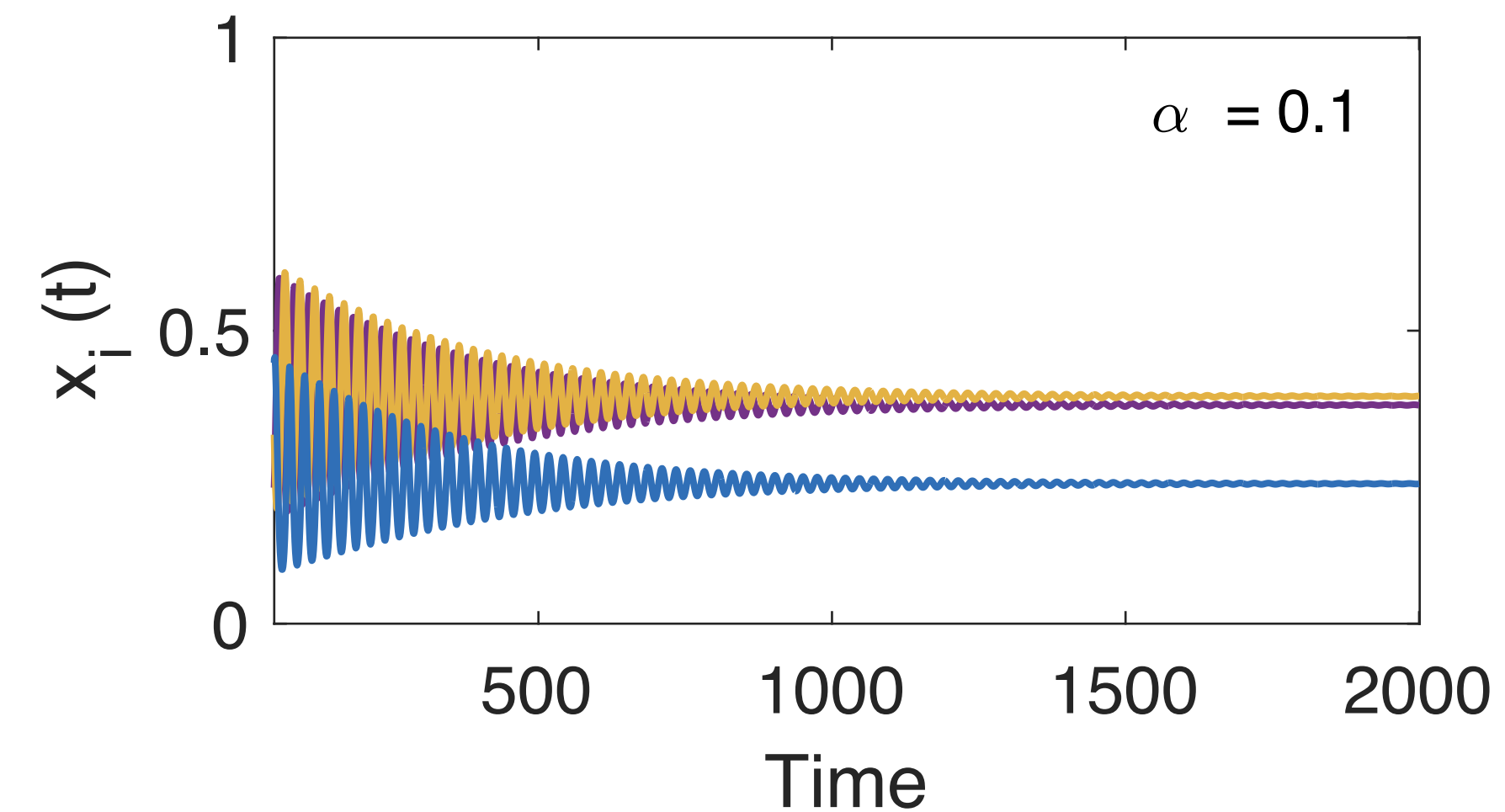
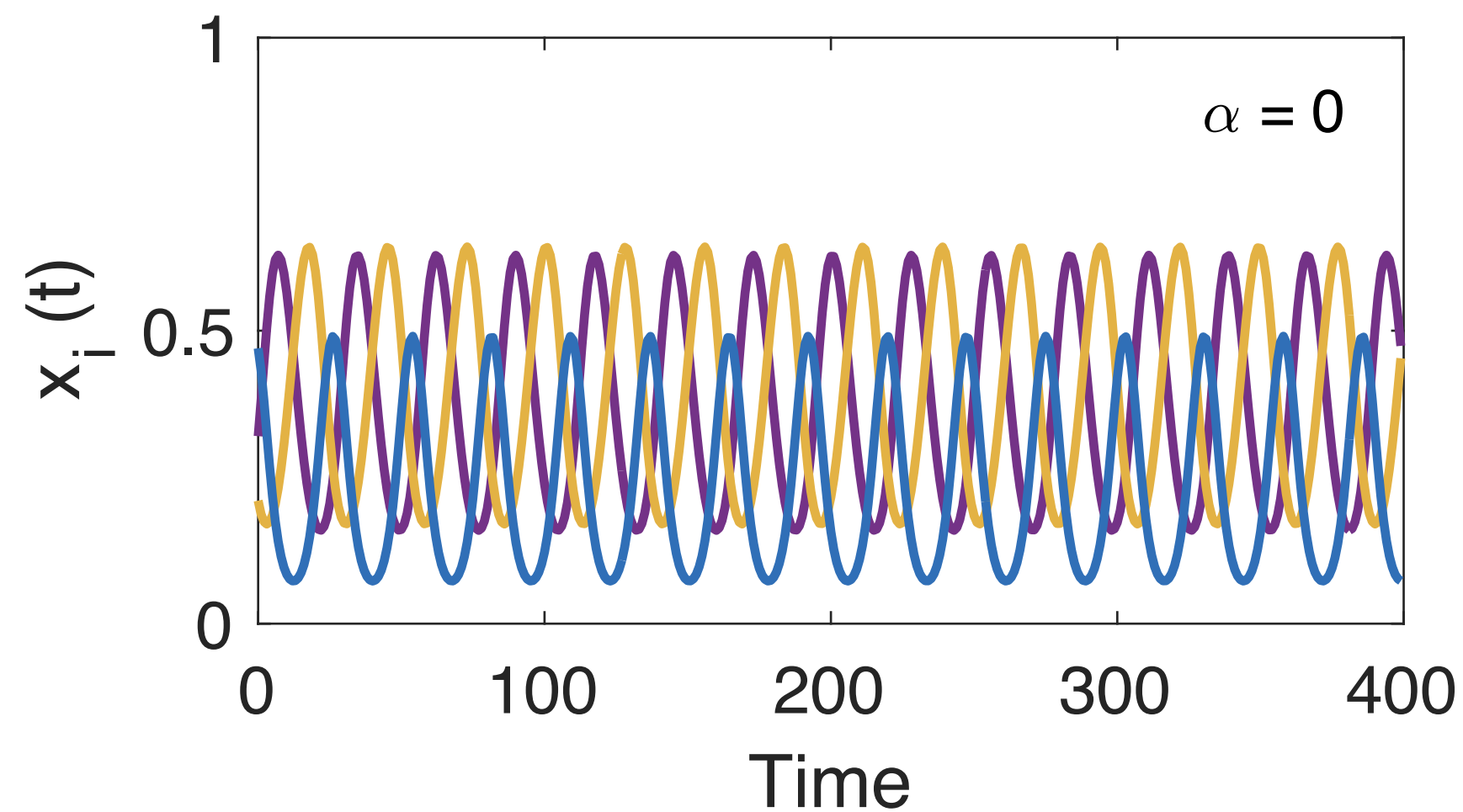
IDENTICAL PHYSIOLOGICAL RATES

Special case:
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It reduces to:

$$\frac{dx_i}{dt} = (1 - \alpha) \left(-x_i + 2 \sum_j H_{ij} x_i x_j \right) + \alpha \left(-x_i + \sum_{j,k} B_{ijk} x_i x_j x_k \right)$$



IDENTICAL PHYSIOLOGICAL RATES

Special case:
Identical physiological rates

Lyapunov function

$$V(x) = - \sum_i x_i^* \log \frac{x_i}{x_i^*}$$

$$\frac{dV}{dt} = \alpha \left[-2 \sum_i x_i^* \left(\sum_j H_{ij} \xi_j \right)^2 \right]$$

f_i birth rate = 1

d_i death rate = 1

$$F(x) = \sum_i f_i x_i = 1$$

$$D(x) = \sum_i d_i x_i = 1$$

IDENTICAL PHYSIOLOGICAL RATES

Special case:
Identical physiological rates

f_i birth rate = 1

d_i death rate = 1

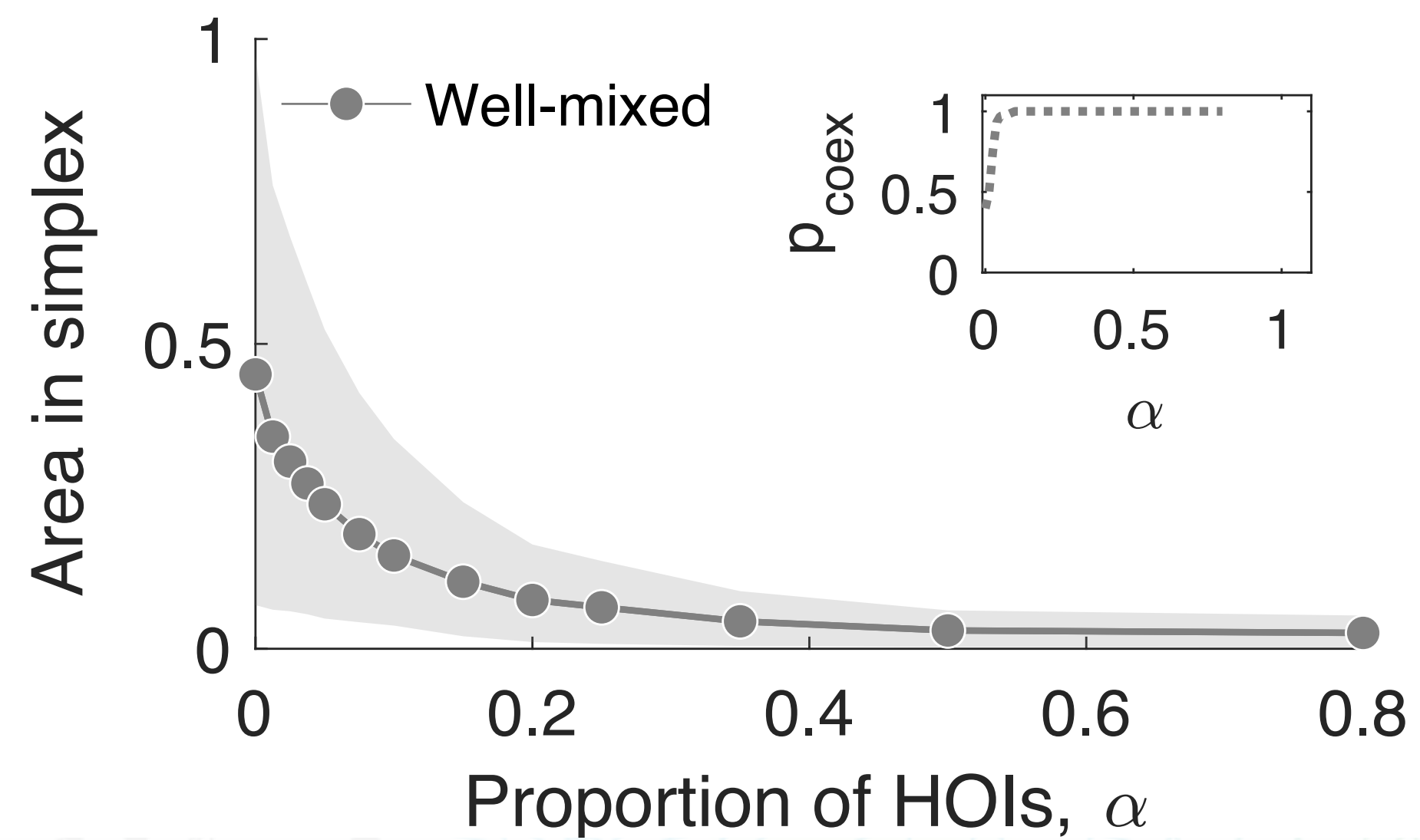
$$F(x) = \sum_i f_i x_i = 1$$

$$D(x) = \sum_i d_i x_i = 1$$

Lyapunov function

$$V(x) = - \sum_i x_i^* \log \frac{x_i}{x_i^*}$$

$$\frac{dV}{dt} = \alpha \left[-2 \sum_i x_i^* \left(\sum_j H_{ij} \xi_j \right)^2 \right]$$



$\alpha_c = 0$. Any amount of HOs stabilizes the dynamics

DIFFERENT PHYSIOLOGICAL RATES

General case (well mixed)

$$\frac{dx_i}{dt} = (1 - \alpha) \left[x_i \left(\frac{D(x)}{F(x)^2} f_i \sum_j 2H_{ij} f_j x_j - d_i \right) \right] + \alpha \left[x_i \left(\frac{D(x)}{F(x)^3} f_i \sum_{j,k} B_{ijk} f_j x_j f_k x_k - d_i \right) \right]$$

The equilibrium depends of the fraction of H0Is

$$\alpha_c = \frac{-\frac{1}{F^2 D^*} (F^* D - F D^*)^2}{2D \frac{F^*}{F} - \sum_i x_i^* T_2 - \frac{F^{*2}}{F^2} \frac{D}{D^*} \sum_i x_i T_2^*}$$

With:

f_i birth rate

d_i death rate

$$F(x) = \sum f_i x_i$$

$$D(x) = \sum_i d_i x_i$$

With $T_2(\vec{x}) = \frac{D}{F^3} f_i \sum_j \sum_k f_j f_k (2H_{ij} H_{ik} + H_{ij} H_{jk} + H_{ik} H_{kj}) x_j x_k$

DIFFERENT PHYSIOLOGICAL RATES

Adding noise:



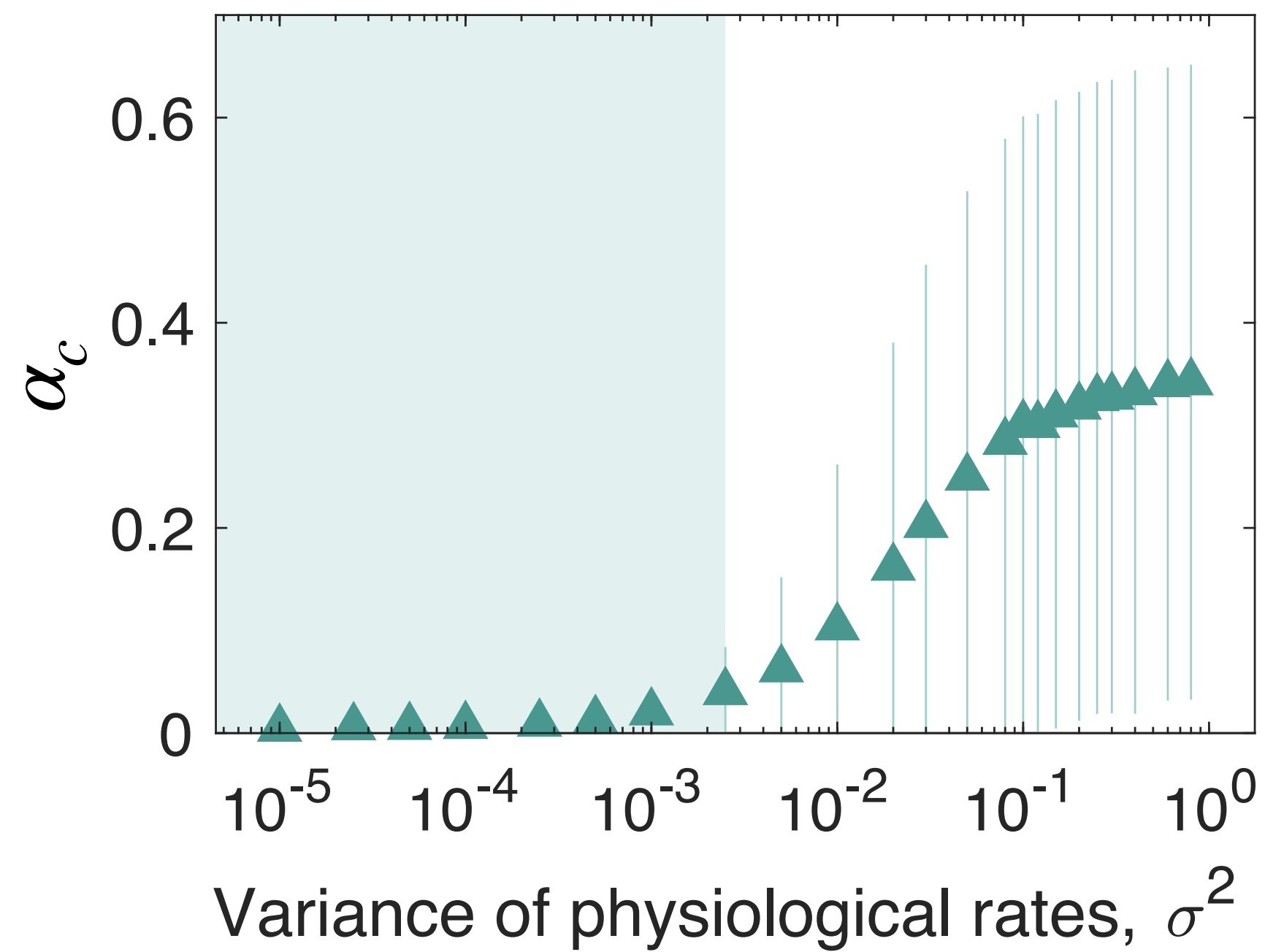
f_i and d_i normally distributed with mean $\mu = 1$

DIFFERENT PHYSIOLOGICAL RATES

Adding noise:



f_i and d_i normally distributed with mean $\mu = 1$

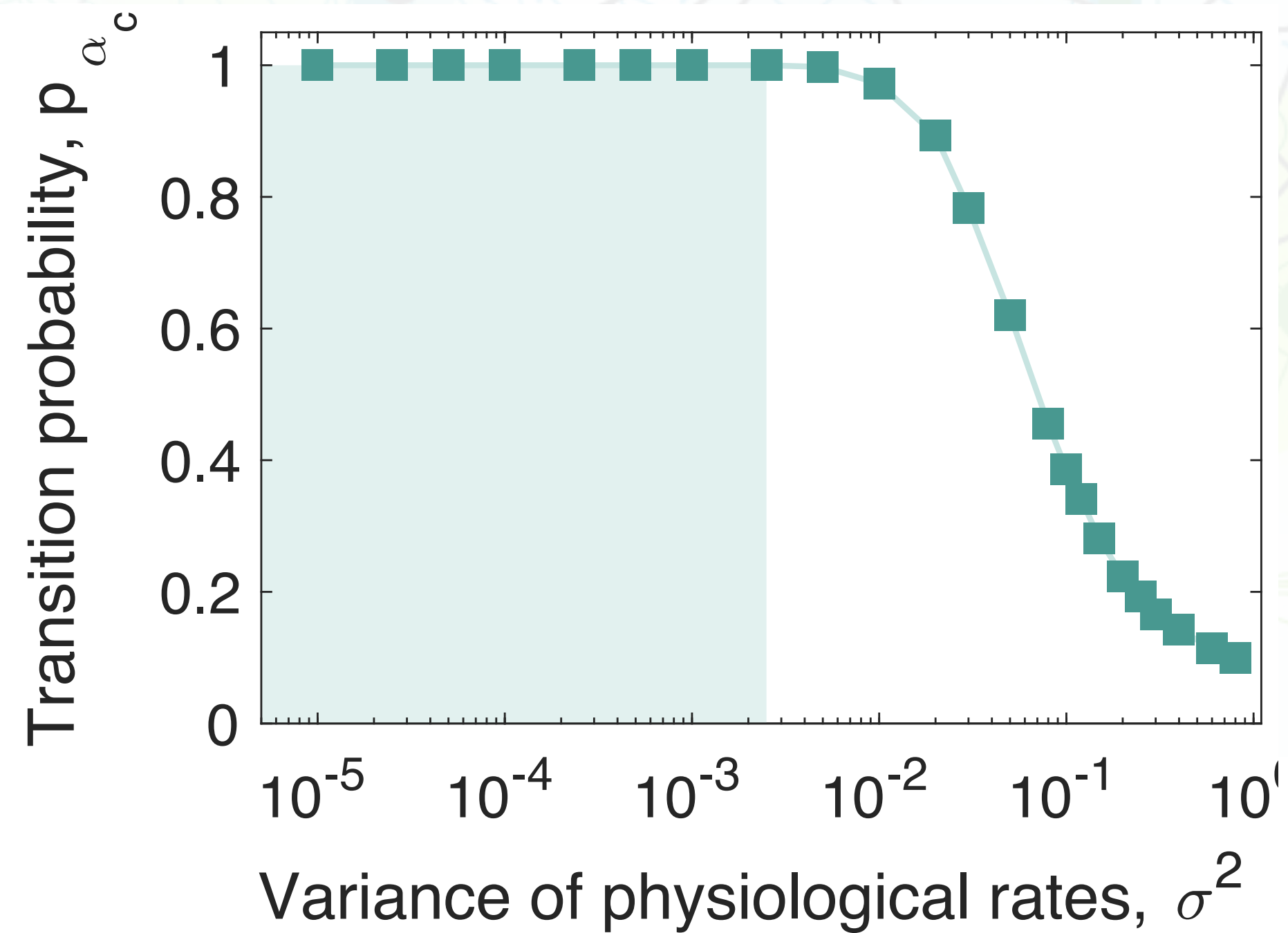
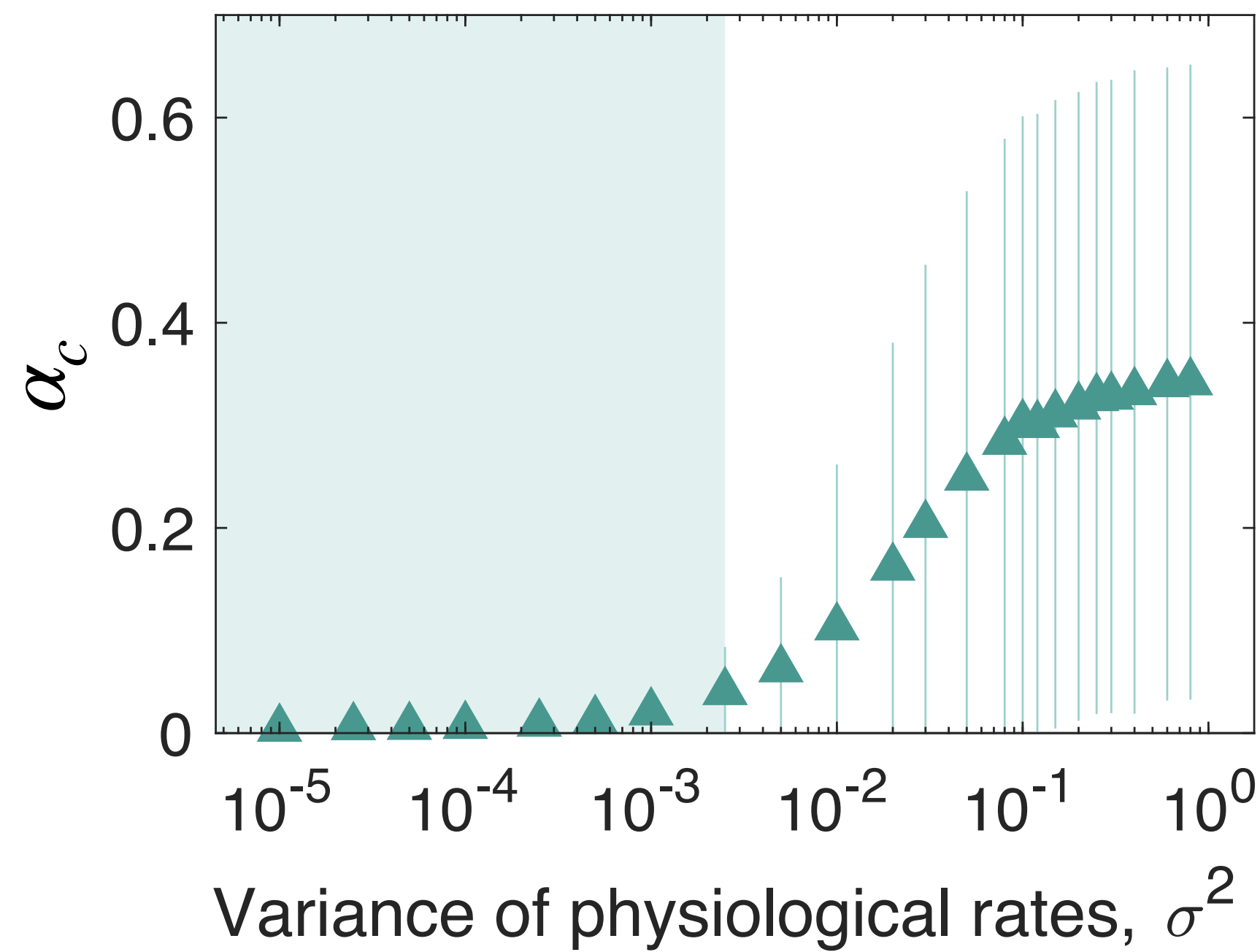


DIFFERENT PHYSIOLOGICAL RATES

Adding noise:



f_i and d_i normally distributed with mean $\mu = 1$



Heterogeneity affects stability

Real data

Allometric scaling of plant life history

Núria Marbà*, Carlos M. Duarte, and Susana Agustí

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Edited by James H. Brown, University of New Mexico, Albuquerque, NM, and approved August 1, 2007 (received for review April 15, 2007)

Plant mortality and birth rates are critical components of plant life history affecting the stability of plant populations and the ecosystems they form. Although allometric theory predicts that both plant birth and mortality rates should be size-dependent, this prediction has not yet been tested across plants ranging the full size spectrum. Here we show that both population mortality and population birth rates scale as the $-1/4$ power and plant lifespan as the $1/4$ power of plant mass across plant species spanning from the tiniest phototrophs to the largest trees. Whereas the controls on plant lifespans are as yet poorly understood, our findings suggest

Our data set confirms that a similar $-1/4$ scaling relationship applies to the scaling of plant birth rate (B , d^{-1}) and M (1). A general balance between plant lifespan and birth rate required to achieve a balanced population size and density that a proportional scaling between plant lifespan and birth rate is expected. Indeed, there was a strong positive scaling between D and B (Fig. 3), but the slope was significantly lower (slope, 95% c.i. 0.78–0.87; Fig. 3), indicating that plants tended to exceed mortality for the smallest phototrophs. If the slope of the scaling relationship closely approached a

Plant type	<i>n</i>	Individual mass, grams dry weight	Mortality rate, d ^{−1}	Life span, d	Birth rate, d ^{−1}
Phytoplankton	48	3.5 ± 2.4 × 10 ^{−9} (3.4 × 10 ^{−15} –8.3 × 10 ^{−8})	39 ± 7.0 × 10 ^{−2} (1.2 × 10 ^{−3} –2.5)	2.3 ± 1.2 × 10 ¹ (2.8 × 10 ^{−1} –5.8 × 10 ²)	15 ± 2.5 × 10 ^{−1} (4.0 × 10 ^{−2} –3.7)
Macroalgae	37	7.2 ± 4.6 × 10 ¹ (7.3 × 10 ^{−4} –1.5 × 10 ³)	7.6 ± 1.8 × 10 ^{−3} (2.2 × 10 ^{−4} –5.8 × 10 ^{−2})	4.0 ± 1.2 × 10 ² (1.2 × 10 ^{−1} –3.1 × 10 ³)	1.4 ± 0.63 × 10 ^{−2} (2.6 × 10 ^{−4} –3.8 × 10 ^{−2})
Mosses	7	2.1 ± 0.26 × 10 ^{−2} (1.6 × 10 ^{−2} –3.3 × 10 ^{−2})	1.8 ± 0.27 × 10 ^{−3} (6.7 × 10 ^{−4} –2.8 × 10 ^{−3})	4.8 ± 1.0 × 10 ² (2.5 × 10 ² –1.0 × 10 ³)	
Ferns	3		2.6 ± 1.0 × 10 ^{−4} (1.3 × 10 ^{−4} –4.6 × 10 ^{−4})	3.4 ± 1.1 × 10 ³ (1.5 × 10 ³ –5.2 × 10 ³)	2.0 ± 0.32 × 10 ^{−4} (1.2 × 10 ^{−4} –2.8 × 10 ^{−4})
Seagrasses	151	3.1 ± 0.37 × 10 ^{−1} (7.0 × 10 ^{−3} –2.5)	2.5 ± 0 – 35 × 10 ^{−3} (5.6 × 10 ^{−5} –4.1 × 10 ^{−2})	13 ± 1.4 × 10 ² (1.7 × 10 ¹ –1.2 × 10 ⁴)	1.9 ± 0.20 × 10 ^{−3} (3.9 × 10 ^{−5} –1.2 × 10 ^{−2})
Land and salt marsh herbs	190	4.9 ± 2.4(1.8 × 10 ^{−2} –1.2 × 10 ²)	5.8 ± 1.5 × 10 ^{−3} (1.4 × 10 ^{−5} –2.2 × 10 ^{−1})	16 ± 3.0 × 10 ² (3.2–5.0 × 10 ⁴)	2.1 ± 0.44 × 10 ^{−3} (1.1 × 10 ^{−5} –2.0 × 10 ^{−2})
Succulent plants	12	2.9 ± 1.4 × 10 ³ (4.4 × 10 ² –6.1 × 10 ³)	8.9 ± 2.2 × 10 ^{−3} (2.6 × 10 ^{−5} –2.0 × 10 ^{−2})	7.6 ± 3.3 × 10 ³ (3.5 × 10 ¹ –2.7 × 10 ⁴)	2.1 ± 0.8 × 10 ^{−5} (6.7 × 10 ^{−6} –3.6 × 10 ^{−5})
Shrubs and lianas	20	5.9 ± 3.2 × 10 ¹ (4.5–1.8 × 10 ²)	1.1 ± 0.6 × 10 ^{−2} (1.1 × 10 ^{−4} –1.2 × 10 ^{−1})	14 ± 4.1 × 10 ² (6.0–6.5 × 10 ³)	
Mangroves	30	2.8 ± 1.3 × 10 ¹ (6.4 × 10 ^{−1} –3.2 × 10 ²)	3.5 ± 0.94 × 10 ^{−3} (2.4 × 10 ^{−5} –2.3 × 10 ^{−2})	1.8 ± 0.94 × 10 ³ (3.0 × 10 ¹ –2.8 × 10 ⁴)	
Trees	230	7.7 ± 1.2 × 10 ⁵ (11–11 × 10 ⁶)	2.9 ± 0.53 × 10 ^{−4} (2.8 × 10 ^{−7} –5.2 × 10 ^{−3})	1.1 ± 0.2 × 10 ⁵ (1.3 × 10 ² –2.5 × 10 ⁶)	4.1 ± 0.65 × 10 ^{−5} (3.0 × 10 ^{−6} –3.1 × 10 ^{−4})
Overall	728	23 ± 4.2 × 10 ⁴ (3.4 × 10 ^{−15} –11 × 10 ⁶)	2.9 ± 0.58 × 10 ^{−2} (2.8 × 10 ^{−7} –2.5)	37 ± 6.7 × 10 ³ (2.8 × 10 ^{−1} –2.5 × 10 ⁶)	1.3 ± 0.32 × 10 ^{−1} (3.0 × 10 ^{−6} –3.7)

From N. Marbà, et al. , Proc. Natl. Acad. Sci. U.S.A. 104 (40) 15777-15780 (2007)

REAL PHYSIOLOGICAL RATES

Real data

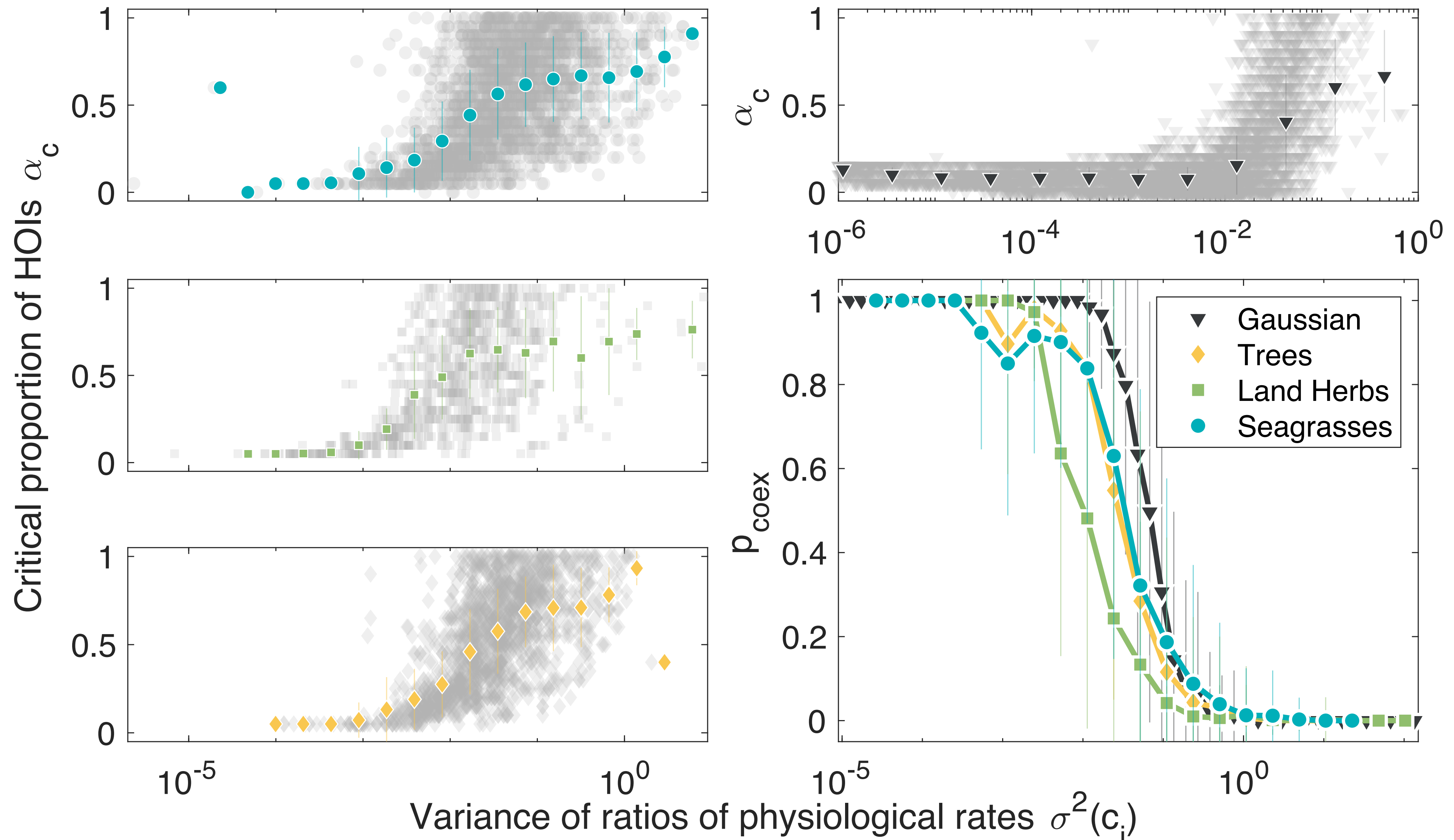
Allometric scaling of plant

Núria Marbà*, Carlos M. Duarte, and Susana Agustí

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Edited by James H. Brown, University of New Mexico, Albuquerque, NM, and

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Special case:
Identical physiological rates

Random networks (Erdős-Rényi) with tunable fraction of HOIs



$\alpha = 0$

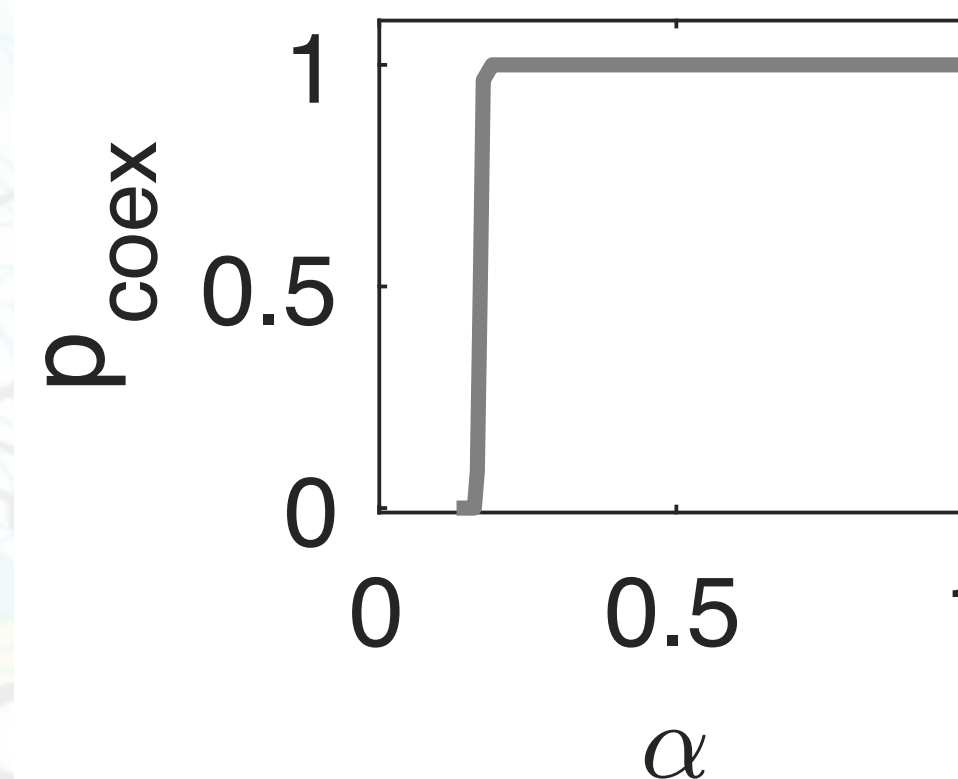
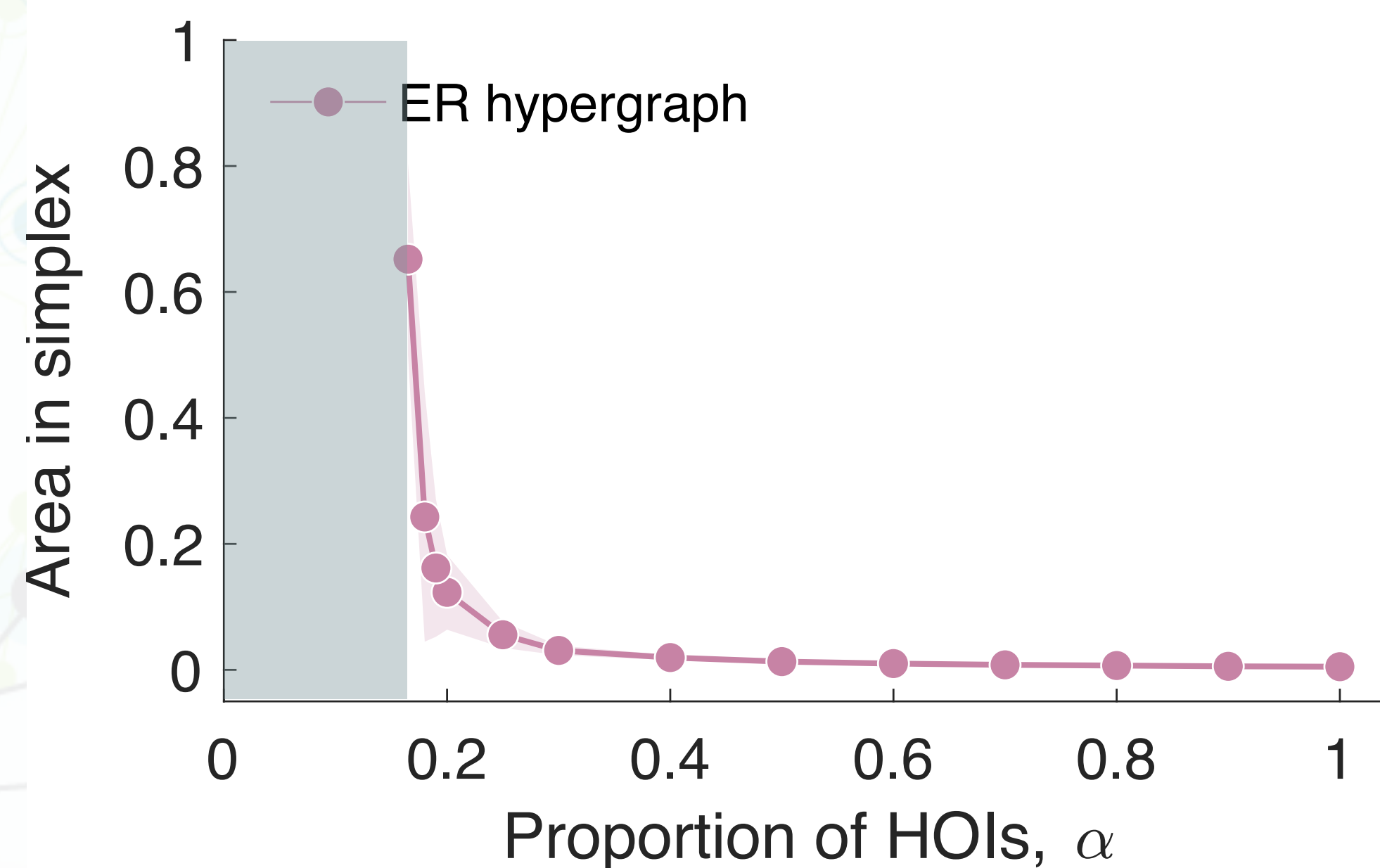
$\alpha = 1$

α fraction of hyperlinks

Special case:

Identical physiological rates

Random networks (Erdős-Rényi) with tunable fraction of HOIs



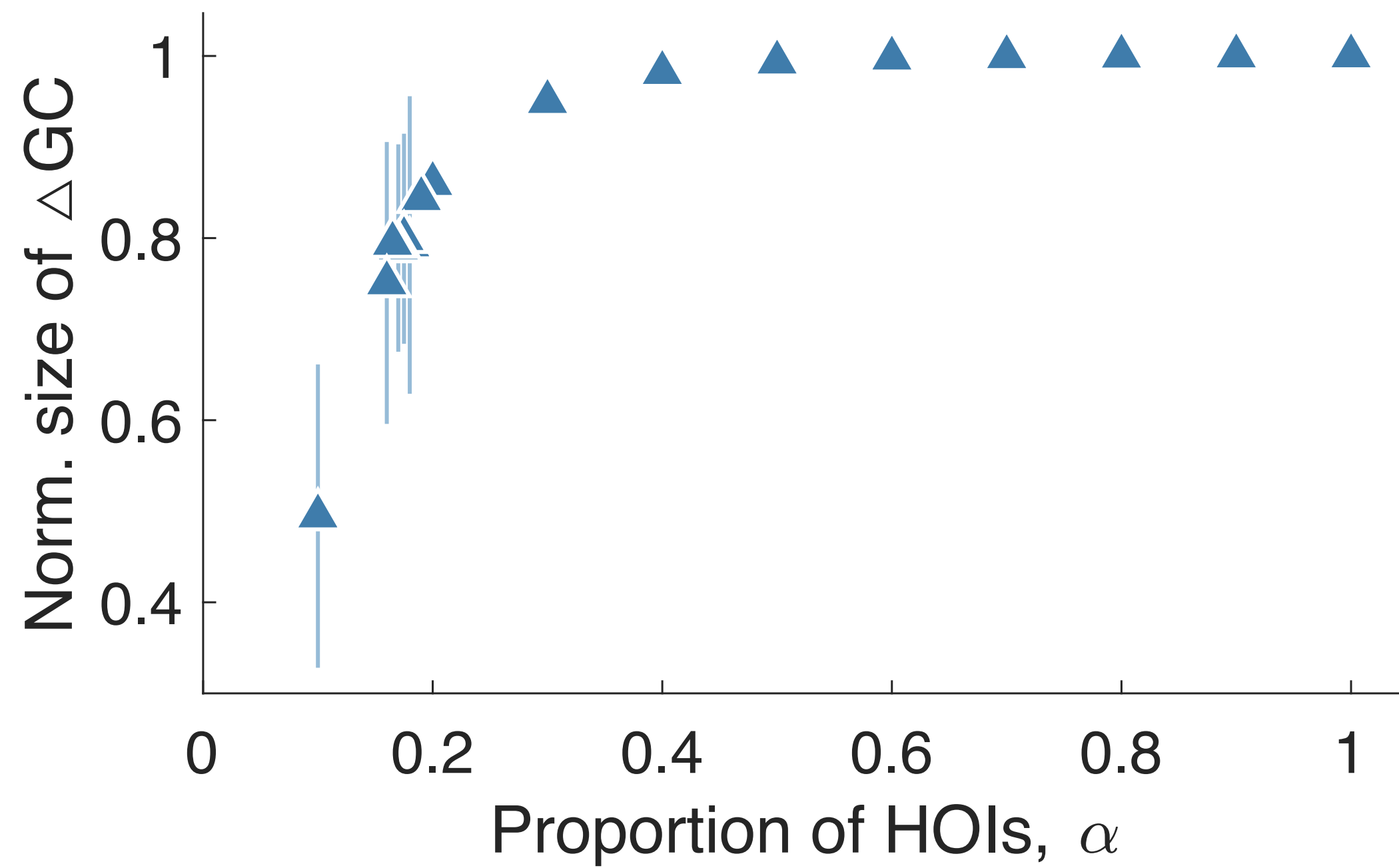
Sharp transition in Coexistence

Special case:

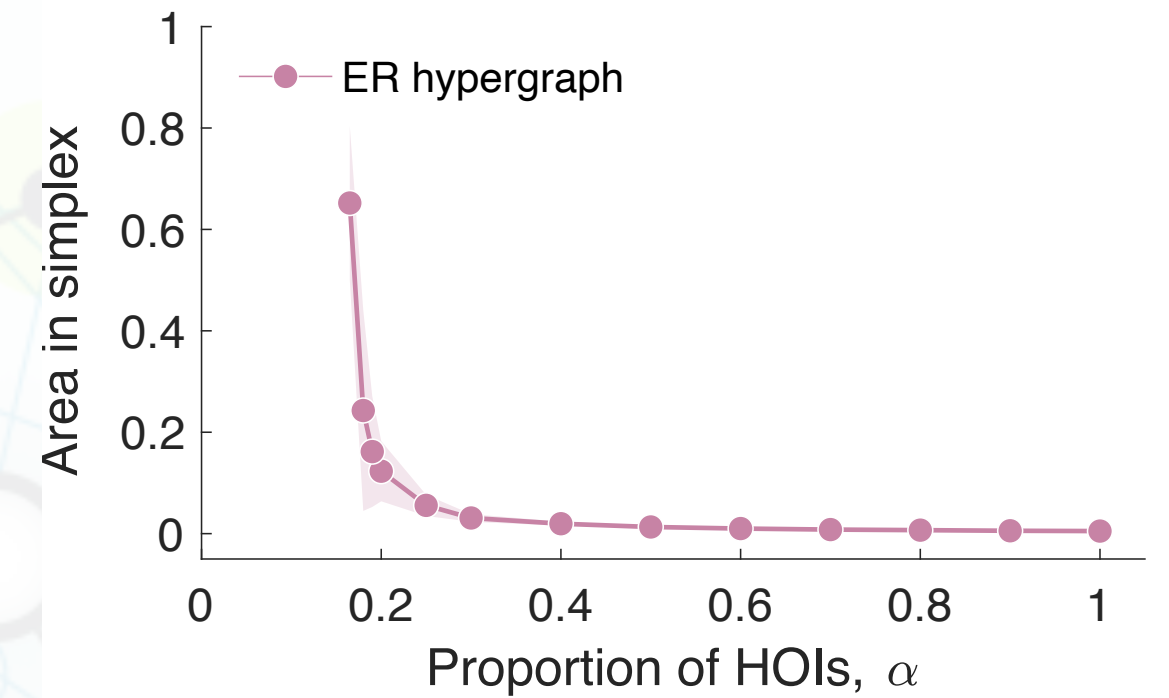
Identical physiological rates

Random networks (Erdős-Rényi) with tunable fraction of HOIs

Sharp transition in coexistence: how?



Percolating cluster of HOIs

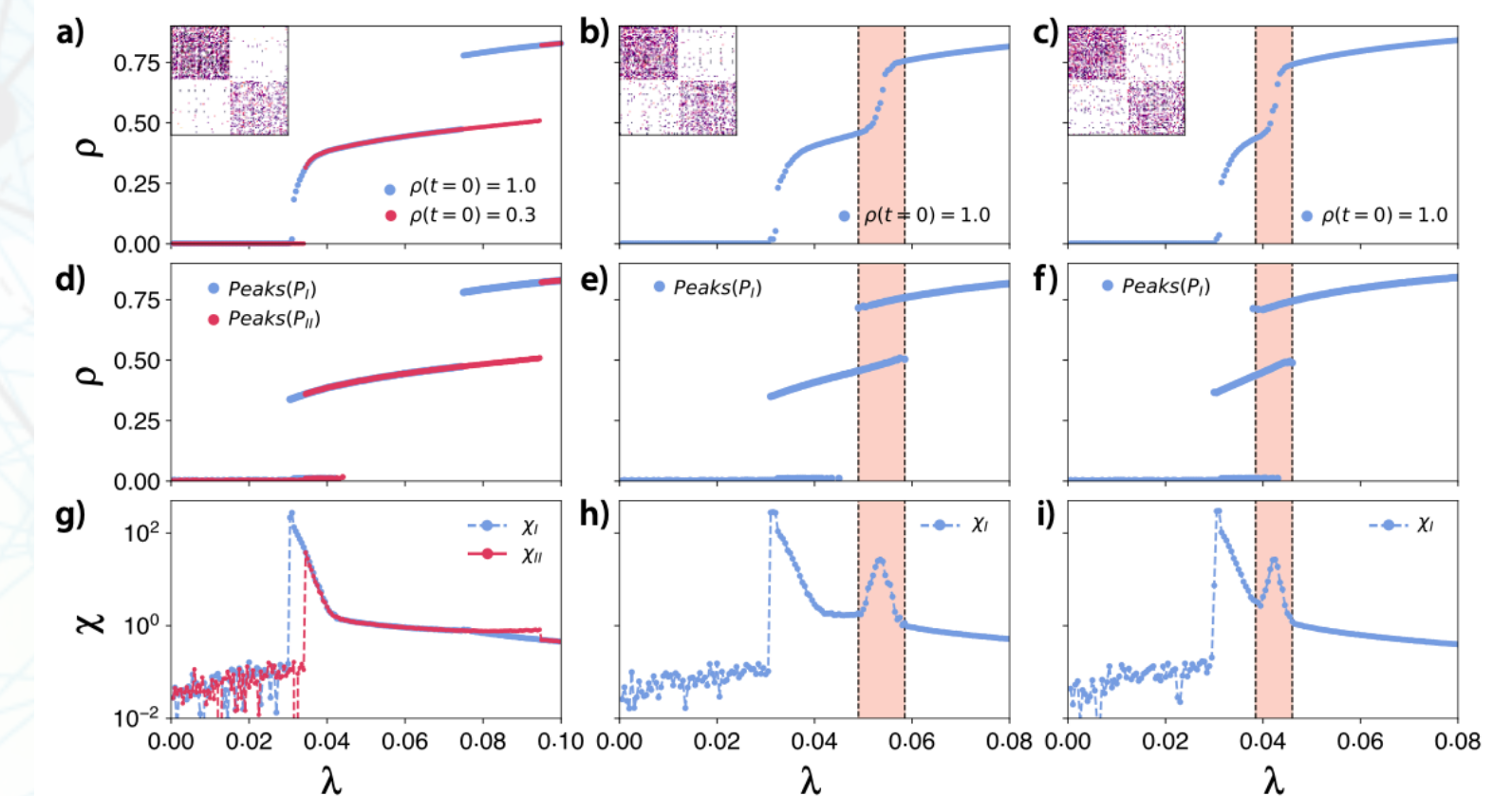


ΔGC
size of the giant component
considering only HO connections

Higher-order interactions can be a framework to study dynamical systems on networks

However:

- Rethink their study at the light of Network Theory and Statistical Mechanics
- Leave the "new physics" behind and put efforts in systematize these new results



Ref. • "Higher-order contagion processes in 1.99 dimensions"
SM, Andrea Gabrielli, Pablo Villegas
arXiv:2502.18004

• "On the stability of competitive ecological communities with pairwise and higher-order interactions"
Marc Duran-Sala, SM, Violeta Calleja-Solanas.
arXiv:2501.09172

• "Demystifying HOI in ecology: is this description worth it?"
Santiago Lamata-Otín, Carlos Gómez Ambrosi, Violeta Calleja-Solanas, Jesús Gómez Gardeñes, SM.
in preparation

Acks.

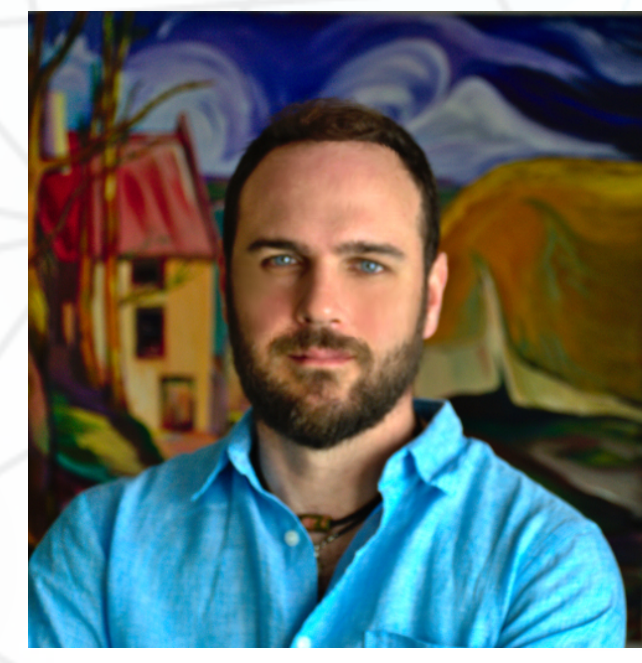
Project APASOS (PID2021-122256NB-C21/C22) - funded under Fondo Europeo de Desarrollo Regional (FEDER, UE) and the María de Maeztu Program (CEX2021-001164-M) for units of Excellence in R&D.

Project "CODE – Coupling Opinion Dynamics with Epidemics", funded under PNRR Mission 4 "Education and Research" - Component C2 - Investment 1.1 - Next Generation EU "Fund for National Research Program and Projects of Significant National Interest" PRIN 2022 PNRR, grant code P2022AKRZ9, CUP B53D23026080001.

People



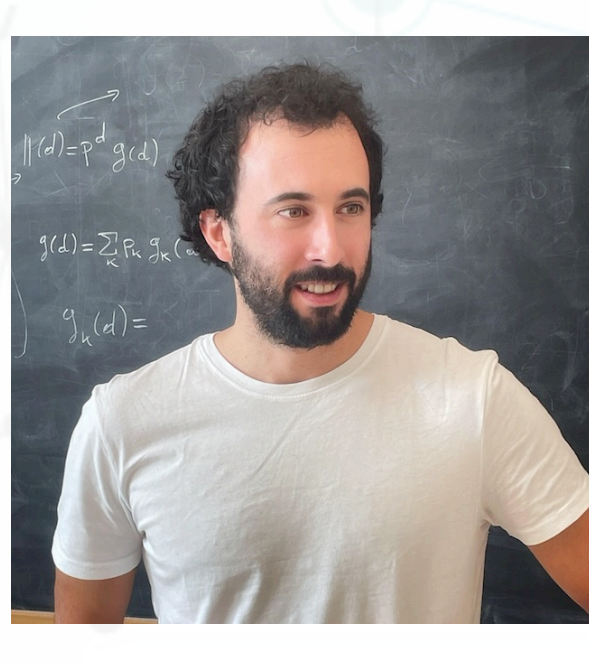
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