Entanglement and time paradoxes in neutral kaons at KLOE:

from past to future or from future to past?



Antonio Di Domenico Dipartimento di Fisica, Sapienza Università di Roma and INFN sezione di Roma, Italy on behalf of the KLOE-2 collaboration and Jose Bernabeu





XXVI Roma Tre Topical Seminar on Subnuclear Physics "Testing quantum mechanics at colliders"

Dipartimento di Matematica e Fisica, Università Roma Tre - 3 December 2024

Entangled neutral kaons at a \$\phi-factory



Production of the vector meson ϕ in e⁺e⁻ annihilations:

- $e^+e^- \rightarrow \phi \quad \sigma_{\phi} \sim 3 \ \mu b$ W = $m_{\phi} = 1019.4 \ MeV$
- BR($\phi \rightarrow K^0 \overline{K}^0$) ~ 34%
- ~10⁶ neutral kaon pairs per pb⁻¹ produced in an antisymmetric quantum state with $J^{PC} = 1^{--}$:

 $p_{\rm K} = 110 \ {\rm MeV/c} \\ \lambda_{\rm S} = 6 \ {\rm mm} \quad \lambda_{\rm L} = 3.5 \ {\rm m}$



$$\begin{aligned} \left|i\right\rangle &= \frac{1}{\sqrt{2}} \left[\left|K^{0}\left(\vec{p}\right)\right\rangle \left|\overline{K}^{0}\left(-\vec{p}\right)\right\rangle - \left|\overline{K}^{0}\left(\vec{p}\right)\right\rangle \left|K^{0}\left(-\vec{p}\right)\right\rangle \right] \\ &= \frac{N}{\sqrt{2}} \left[\left|K_{s}\left(\vec{p}\right)\right\rangle \left|K_{L}\left(-\vec{p}\right)\right\rangle - \left|K_{L}\left(\vec{p}\right)\right\rangle \left|K_{s}\left(-\vec{p}\right)\right\rangle \right] \\ &N &= \sqrt{\left(1 + \left|\varepsilon_{s}\right|^{2}\right)\left(1 + \left|\varepsilon_{L}\right|^{2}\right)} \left/ \left(1 - \varepsilon_{s}\varepsilon_{L}\right) \approx 1 \end{aligned}$$

KLOE and KLOE-2 at the Frascati φ-factory DAΦNE



KLOE detector





- ~ 3 x10⁸ η's
- ⇒ the largest sample ever collected at the $\phi(1020)$ peak in e⁺e⁻ collisions

KLOE and KLOE-2 at the Frascati φ-factory DAΦNE















Same final state for both kaons: $f_1 = f_2 = \pi^+\pi^-$ (this specific channel is suppressed by CP viol. $|\eta_{+-}|^2 = |A(K_L - >\pi^+\pi^-)/A(K_S - >\pi^+\pi^-)|^2 \sim |\epsilon|^2 \sim 10^{-6}$)





Same final state for both kaons: $f_1 = f_2 = \pi^+ \pi^-$ (this specific channel is suppressed by CP viol. $|\eta_{+-}|^2 = |A(K_L - >\pi^+ \pi^-)/A(K_S - >\pi^+ \pi^-)|^2 \sim |\varepsilon|^2 \sim 10^{-6}$)

EPR correlation:

no simultaneous decays ($\Delta t=0$) in the same final state due to the fully destructive quantum interference











$$|i\rangle = \frac{1}{\sqrt{2}} \left[\left| K^{0} \right\rangle \left| \overline{K}^{0} \right\rangle - \left| \overline{K}^{0} \right\rangle \right] K^{0} \right]$$

The EPR correlation suggested a simple test of quantum coherence

$$I\left(\pi^{+}\pi^{-},\pi^{+}\pi^{-};\Delta t\right) = \frac{N}{2} \left[\left| \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \left| K^{0}\overline{K}^{0}(\Delta t) \right\rangle \right|^{2} + \left| \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \left| \overline{K}^{0}K^{0}(\Delta t) \right\rangle \right|^{2} -2\Re \left(\left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \left| K^{0}\overline{K}^{0}(\Delta t) \right\rangle \right\rangle \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \left| \overline{K}^{0}K^{0}(\Delta t) \right\rangle^{*} \right) \right]$$



$$|i\rangle = \frac{1}{\sqrt{2}} \left[\left| K^{0} \right\rangle \left| \overline{K}^{0} \right\rangle - \left| \overline{K}^{0} \right\rangle \right] K^{0} \right]$$

The EPR correlation suggested a simple test of quantum coherence

$$I(\pi^{+}\pi^{-},\pi^{+}\pi^{-};\Delta t) = \frac{N}{2} \left[\left| \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \right| K^{0}\overline{K}^{0}(\Delta t) \right\rangle \right|^{2} + \left| \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \right| \overline{K}^{0}K^{0}(\Delta t) \right\rangle \right|^{2} - \left(1 - \zeta_{00}\right) \cdot 2\Re \left(\left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \right| K^{0}\overline{K}^{0}(\Delta t) \right\rangle \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \left| \overline{K}^{0}K^{0}(\Delta t) \right\rangle^{*} \right) \right]$$

 $\left|i\right\rangle = \frac{1}{\sqrt{2}} \left[\left|K^{0}\right\rangle \left|\overline{K}^{0}\right\rangle - \left|\overline{K}^{0}\right\rangle \left|K^{0}\right\rangle\right]$



The EPR correlation suggested a simple test of quantum coherence

$$I\left(\pi^{+}\pi^{-},\pi^{+}\pi^{-};\Delta t\right) = \frac{N}{2} \left[\left| \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \left| K^{0}\overline{K}^{0}(\Delta t) \right\rangle \right|^{2} + \left| \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \left| \overline{K}^{0}K^{0}(\Delta t) \right\rangle \right|^{2} \right] \right]$$

$$-(1-\zeta_{0\overline{0}})\cdot 2\Re\left(\left\langle\pi^{+}\pi^{-},\pi^{+}\pi^{-}\left|K^{0}\overline{K}^{0}(\Delta t)\right\rangle\left\langle\pi^{+}\pi^{-},\pi^{+}\pi^{-}\left|\overline{K}^{0}K^{0}(\Delta t)\right\rangle^{*}\right)\right]$$

Decoherence parameter:

$$\xi_{0\overline{0}} = 0 \implies QM$$

 $\begin{aligned} \zeta_{0\overline{0}} = 1 & \rightarrow \text{ total decoherence} \\ & \text{(also known as Furry's hypothesis} \\ & \text{ or spontaneous factorization)} \\ & \text{W.Furry, PR 49 (1936) 393} \end{aligned}$

Bertlmann, Grimus, Hiesmayr PR D60 (1999) 114032 Bertlmann, Durstberger, Hiesmayr PRA 68 012111 (2003)

 $\left|i\right\rangle = \frac{1}{\sqrt{2}} \left[\left|K^{0}\right\rangle \left|\overline{K}^{0}\right\rangle - \left|\overline{K}^{0}\right\rangle \left|K^{0}\right\rangle\right]$



The EPR correlation suggested a simple test of quantum coherence

$$I(\pi^{+}\pi^{-},\pi^{+}\pi^{-};\Delta t) = \frac{N}{2} \left[\left| \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \middle| K^{0}\overline{K}^{0}(\Delta t) \right\rangle \right|^{2} + \left| \left\langle \pi^{+}\pi^{-},\pi^{+}\pi^{-} \middle| \overline{K}^{0}K^{0}(\Delta t) \right\rangle \right|^{2} \right|^{2}$$

$$I(\Delta t) \quad (a.u.)$$

$$Decoherence parameter: \qquad \zeta_{0\overline{0}} = 0 \qquad \rightarrow \qquad QM$$

$$\zeta_{0\overline{0}} = 0 \qquad \rightarrow \qquad QM$$

$$\zeta_{0\overline{0}} = 0 \qquad \rightarrow \qquad total \ decoherence (also known as Furry's hypothesis or spontaneous factorization) W.Furry, PR 49 (1936) 393$$
Bertlmann, Grimus, Hiesmayr PR D60 (1999) 114032 Bertlmann, Durstberger, Hiesmayr PRA 68 012111 (2003)



KLOE-2 JHEP 04 (2022) 059

$$\zeta_{0\overline{0}} = \left(-0.5 \pm 8.0_{stat} \pm 3.7_{syst}\right) \times 10^{-7}$$

CP violating process: terms $\zeta_{00}/|\eta_{+-}|^2$ with $|\eta_{+-}|^2 \sim |\epsilon|^2 \sim 10^{-6}$ => high sensitivity to ζ_{00} ; CP violation in kaon mixing acts as amplification mechanism





KLOE-2 JHEP 04 (2022) 059

$$\zeta_{0\overline{0}} = (-0.5 \pm 8.0_{stat} \pm 3.7_{syst}) \times 10^{-7}$$

CP violating process: terms $\zeta_{00}/|\eta_{+-}|^2$ with $|\eta_{+-}|^2 \sim |\epsilon|^2 \sim 10^{-6}$ => high sensitivity to ζ_{00} ; CP violation in kaon mixing acts as amplification mechanism

In the B-meson system, BELLE coll. (PRL 99 (2007) 131802) obtains:

$$\zeta_{00}^{B} = 0.029 \pm 0.057$$





KLOE-2 JHEP 04 (2022) 059

$$\zeta_{0\overline{0}} = \left(-0.5 \pm 8.0_{stat} \pm 3.7_{syst}\right) \times 10^{-7}$$

CP violating process:

terms $\zeta_{00}/|\eta_{+-}|^2$ with $|\eta_{+-}|^2 \sim |\epsilon|^2 \sim 10^{-6}$ => high sensitivity to ζ_{00} ; CP violation in kaon mixing acts as amplification mechanism

In the B-meson system, BELLE coll. (PRL 99 (2007) 131802) obtains:

$$\zeta_{00}^{B} = 0.029 \pm 0.057$$

Possible decoherence due quantum gravity effects (apparent loss of unitarity) implying also **CPT** violation => modified Liouville – von Neumann equation for the density matrix of the kaon system depends on a CPTV parameter γ [J. Ellis et al. PRD53 (1996) 3846]



In this scenario γ can be at most: $O(m_K^2/M_{PLANCK}) = 2 \times 10^{-20} \text{ GeV}$

KLOE-2 result

$$\gamma = (1.3 \pm 9.4_{stat} \pm 4.2_{syst}) \times 10^{-22} \text{ GeV}$$



From past to future

Entanglement as a tool for discrete symmetries tests



In QM the entangled state can be expressed in any base:



- In maximally entangled systems the complete knowledge of the system as a whole is encoded in the entangled state, the single subsystems are undefined.
- When the decay measurement to *f* is performed, the partner is instantaneously informed and tagged as $K_{\Rightarrow f}$ and the decay filters (projects) its orthogonal for the decayed meson.





























the future partner kaon state at t_2 before its decay;

<u>THE RELEVANT TIME DEPENDENCE</u> HERE IS IN $\Delta t = t_2 - t_1$

i.e. from the preparation of the tagged state until its decay





The past (kaon decay at t_1) tags the future partner kaon state at t_2 before its decay;

<u>THE RELEVANT TIME DEPENDENCE</u> HERE IS IN $\Delta t = t_2 - t_1$

i.e. from the preparation of the tagged state until its decay





Double decay intensity calculation





QM calculation of double decay intensity:

two alternatives

(I) Time History approach (TH), from past to future

FUTURE

- (1) The time evolution of the state $|i\rangle$ from time t = 0 to time $t = t_1$, with definite total width Γ ;
- (2) The projection of the state $|i(t = t_1)\rangle$ onto the orthogonal pair $|K_{\neq f_1}^{\perp}\rangle|K_{\neq f_1}\rangle$, filtered by the decay f_1 , times the decay amplitude of the state $|K_{\Rightarrow f_1}^{\perp}\rangle$ into the f_1 channel;
- (3) The time evolution of the surviving (single) kaon state $|K_{\neq f_1}\rangle$ from time $t = t_1$ to time $t = t_2$;
- (4) The projection at time $t = t_2$ of the evolved state $|K_{\neq f_1}(\Delta t)\rangle$ onto the state $|K_{\neq f_2}^{\perp}\rangle$ filtered by the decay f_2 , times the decay amplitude of the state $|K_{\neq f_2}^{\perp}\rangle$ into the f_2 channel.

$$I(f_{1}, t_{1}; f_{2}, t_{2})_{\mathrm{TH}} = \left| \langle f_{2} | T | \mathbf{K}_{\neq f_{2}}^{\perp} \rangle \langle \mathbf{K}_{\neq f_{2}}^{\perp} | \mathbf{K}_{\neq f_{1}} (\Delta t) \rangle \langle f_{1} | T | \mathbf{K}_{\neq f_{1}}^{\perp} \rangle \langle \mathbf{K}_{\neq f_{1}}^{\perp} \mathbf{K}_{\neq f_{1}} | i(t = t_{1}) \rangle \right|^{2}$$

$$(4) \qquad (3) \qquad (2) \qquad (1)$$

Double decay intensity calculation





PAST

QM calculation of double decay intensity: two alternatives

(I) Time History approach (TH), from past to future

FUTURE

- (1) The time evolution of the state $|i\rangle$ from time t = 0 to time $t = t_1$, with definite total width Γ ;
- (2) The projection of the state $|i(t = t_1)\rangle$ onto the orthogonal pair $|K_{\Rightarrow f_1}^{\perp}\rangle|K_{\Rightarrow f_1}\rangle$, filtered by the decay f_1 , times the decay amplitude of the state $|K_{\Rightarrow f_1}^{\perp}\rangle$ into the f_1 channel;
- (3) The time evolution of the surviving (single) kaon state $|K_{\Rightarrow f_1}\rangle$ from time $t = t_1$ to time $t = t_2$;
- (4) The projection at time $t = t_2$ of the evolved state $|K_{\neq f_1}(\Delta t)\rangle$ onto the state $|K_{\neq f_2}^{\perp}\rangle$ filtered by the decay f_2 , times the decay amplitude of the state $|K_{\neq f_2}^{\perp}\rangle$ into the f_2 channel.

 $I(\pi^{+}\ell^{-}\bar{\nu}, t_{1}; 3\pi^{0}, t_{2})_{TH} = |\langle 3\pi^{0}|T|K_{-}\rangle\langle K_{-}|K^{0}(\Delta t)\rangle\langle \pi^{+}\ell^{-}\bar{\nu}|T|\overline{K}^{0}\rangle\langle \overline{K}^{0}K^{0}|i(t_{1})\rangle|^{2}$ (4)
(3)
(2)
(1)

Double decay intensity calculation





QM calculation of double decay intensity: two alternatives

(I) Time History approach (TH), from past to future

FUTURE

- (1) The time evolution of the state $|i\rangle$ from time t = 0 to time $t = t_1$, with definite total width Γ ;
- (2) The projection of the state $|i(t = t_1)\rangle$ onto the orthogonal pair $|K_{\neq f_1}^{\perp}\rangle|K_{\neq f_1}\rangle$, filtered by the decay f_1 , times the decay amplitude of the state $|K_{\Rightarrow f_1}^{\perp}\rangle$ into the f_1 channel;
- (3) The time evolution of the surviving (single) kaon state $|K_{\neq f_1}\rangle$ from time $t = t_1$ to time $t = t_2$;
- $K^0 \rightarrow K_{-}$ (4) The projection at time $t = t_2$ of the evolved state $|K_{\neq f_1}(\Delta t)\rangle$ onto the state $|K_{\neq f_2}^{\perp}\rangle$ filtered by the decay f_2 , times the decay amplitude of the state $|K_{\neq f_2}^{\perp}\rangle$ into the f_2 channel.

 $I(\pi^{+}\ell^{-}\bar{\nu}, t_{1}; 3\pi^{0}, t_{2})_{TH} = |\langle 3\pi^{0}|T|K_{-}\langle K_{-}|K^{0}(\Delta t)\rangle \langle \pi^{+}\ell^{-}\bar{\nu}|T|\overline{K}^{0}\rangle \langle \overline{K}^{0}K^{0}|i(t_{1})\rangle|^{2}$ (4)(3)(1)(2)

T,CP, CPT tests in transitions





T,CP, CPT tests in transitions







Direct test of CPT symmetry in neutral kaon transitions

CPT symmetry test

Reference		CPT-conjugate	
Transition	Decay products	Transition	Decay products
$\overline{K^0 \to K_+}$	$(\ell^-, \pi\pi)$	$K_+ \to \bar{K}^0$	$(3\pi^0,\ell^-)$
$K^0 \rightarrow K$	$(\ell^{-}, 3\pi^{0})$	$\mathrm{K}_{-}\to \bar{\mathrm{K}}^{0}$	$(\pi\pi,\ell^-)$
$\bar{K}^0 \to K_+$	$(\ell^+, \pi\pi)$	$\mathrm{K}_+ \to \mathrm{K}^0$	$(3\pi^0, \ell^+)$
$\bar{\mathrm{K}}^{0} \rightarrow \mathrm{K}_{-}$	$(\ell^+, 3\pi^0)$	$K_{-} \rightarrow K^{0}$	$(\pi\pi,\ell^+)$

One can define the following ratios of probabilities:

$$R_{1,C\mathcal{PT}}(\Delta t) = P \left[\mathbf{K}_{+}(0) \to \bar{\mathbf{K}}^{0}(\Delta t) \right] / P \left[\mathbf{K}^{0}(0) \to \mathbf{K}_{+}(\Delta t) \right]$$
$$R_{2,C\mathcal{PT}}(\Delta t) = P \left[\mathbf{K}^{0}(0) \to \mathbf{K}_{-}(\Delta t) \right] / P \left[\mathbf{K}_{-}(0) \to \bar{\mathbf{K}}^{0}(\Delta t) \right]$$
$$R_{3,C\mathcal{PT}}(\Delta t) = P \left[\mathbf{K}_{+}(0) \to \mathbf{K}^{0}(\Delta t) \right] / P \left[\bar{\mathbf{K}}^{0}(0) \to \mathbf{K}_{+}(\Delta t) \right]$$
$$R_{4,C\mathcal{PT}}(\Delta t) = P \left[\bar{\mathbf{K}}^{0}(0) \to \mathbf{K}_{-}(\Delta t) \right] / P \left[\mathbf{K}_{-}(0) \to \mathbf{K}^{0}(\Delta t) \right]$$

Any deviation from $R_{i,CPT}$ =1 constitutes a violation of CPT-symmetry

J. Bernabeu, A.D.D., P. Villanueva, JHEP 10 (2015) 139

Direct test of T symmetry in neutral kaon transitions



T symmetry test

Reference		T-conjugate	
Transition	Final state	Transition	Final state
$\bar{K}^0 \to K$	$(\ell^+,\pi^0\pi^0\pi^0)$	$K \to \bar{K}^0$	$(\pi^0\pi^0\pi^0,\ell^-)$
${\rm K}_+ \rightarrow {\rm K}^0$	$(\pi^0\pi^0\pi^0,\ell^+)$	${\rm K}^0 \to {\rm K}_+$	$(\ell^-,\pi\pi)$
$\bar{K}^0 \to K_+$	$(\ell^+,\pi\pi)$	$K_+ \to \bar{K}^0$	$(\pi^0\pi^0\pi^0,\ell^-)$
$\mathrm{K}_{-} \to \mathrm{K}^{0}$	$(\pi\pi, \ell^+)$	${\rm K}^0 ightarrow {\rm K}$	$(\ell^-,\pi\pi)$

One can define the following ratios of probabilities:

$$\begin{aligned} R_1(\Delta t) &= P\left[\mathrm{K}^0(0) \to \mathrm{K}_+(\Delta t)\right] / P\left[\mathrm{K}_+(0) \to \mathrm{K}^0(\Delta t)\right] \\ R_2(\Delta t) &= P\left[\mathrm{K}^0(0) \to \mathrm{K}_-(\Delta t)\right] / P\left[\mathrm{K}_-(0) \to \mathrm{K}^0(\Delta t)\right] \\ R_3(\Delta t) &= P\left[\bar{\mathrm{K}}^0(0) \to \mathrm{K}_+(\Delta t)\right] / P\left[\mathrm{K}_+(0) \to \bar{\mathrm{K}}^0(\Delta t)\right] \\ R_4(\Delta t) &= P\left[\bar{\mathrm{K}}^0(0) \to \mathrm{K}_-(\Delta t)\right] / P\left[\mathrm{K}_-(0) \to \bar{\mathrm{K}}^0(\Delta t)\right] .\end{aligned}$$

Any deviation from R_i=1 constitutes a violation of T-symmetry

J. Bernabeu, A.D.D., P. Villanueva: NPB 868 (2013) 102

T, CP, CPT tests in neutral kaon transitions at KLOE

CP observables

 $\rho = \overline{\nu} \cdot \Lambda t^{\gamma}$

$$R_{2,\mathcal{CPT}}^{\exp}(\Delta t) \equiv \frac{I(\ell^-, 3\pi^0; \Delta t)}{I(\pi\pi, \ell^-; \Delta t)} \qquad \qquad R_{2,\mathcal{T}}^{\exp}(\Delta t) \equiv \frac{I(\ell^-, 3\pi^0; \Delta t)}{I(\pi\pi, \ell^+; \Delta t)} \qquad \qquad R_{2,\mathcal{CP}}^{\exp}(\Delta t) \equiv \frac{I(\ell^-, 3\pi^0; \Delta t)}{I(\ell^+, 3\pi^0; \Delta t)}$$

$$R_{4,\mathcal{CPT}}^{\exp}(\Delta t) \equiv \frac{I(\ell^+, 3\pi^0; \Delta t)}{I(\pi\pi, \ell^+; \Delta t)} \qquad R_{4,\mathcal{T}}^{\exp}(\Delta t) \equiv \frac{I(\ell^+, 3\pi^0; \Delta t)}{I(\pi\pi, \ell^-; \Delta t)} \qquad R_{4,\mathcal{CP}}^{\exp}(\Delta t) \equiv \frac{I(\pi\pi, \ell^+; \Delta t)}{I(\pi\pi, \ell^-; \Delta t)} \\ \mathcal{D}_{\mathcal{R}_{\mathcal{CPT}}}^{\mathcal{CPT}}(\Delta t \gg \tau_S) \equiv \frac{R_{2,\mathcal{CPT}}^{\exp}(\Delta t \gg \tau_S)}{R_{4,\mathcal{CP}}^{\exp}(\Delta t \gg \tau_S)} \qquad \mathcal{D}_{\mathcal{R}_{\mathcal{T},\mathcal{CP}}}(\Delta t \gg \tau_S) \equiv \frac{R_{2,\mathcal{T}}^{\exp}(\Delta t \gg \tau_S)}{R_{4,\mathcal{CP}}^{\exp}(\Delta t \gg \tau_S)} \equiv \frac{R_{2,\mathcal{CP}}^{\exp}(\Delta t \gg \tau_S)}{R_{4,\mathcal{CP}}^{\exp}(\Delta t \gg \tau_S)}$$

Corresponding to study the following processes at KLOE:

CPT



T, CP, CPT tests in neutral kaon transitions at KLOE





Measured double kaon decay intensities

• residual background subtraction for $\pi e^{\pm} v \ 3\pi^0$ channel

• MC selection efficiencies corrected from data with 4 independent control samples



Testing Quantum Mechanics at colliders – 3 December 2024 – Roma Tre University
T, CP, CPT tests in neutral kaon transitions at KLOE



ure 6: Ratios Af Di Domenico y rates of entangled K Testing Quantum Mechanics and 3 December 2024; AonBathe, UNIversity ta, G. Corradi and G. Pa³⁷



From future to past

Further studies of the properties of entanglement for neutral K mesons

Double decay intensity calculation





QM calculation of double decay intensity: two alternatives

(I) Time History approach (TH), from past to future

FUTURE

- (1) The time evolution of the state $|i\rangle$ from time t = 0 to time $t = t_1$, with definite total width Γ ;
- (2) The projection of the state $|i(t = t_1)\rangle$ onto the orthogonal pair $|K_{\neq f_1}^{\perp}\rangle|K_{\neq f_1}\rangle$, filtered by the decay f_1 , times the decay amplitude of the state $|K_{\Rightarrow f_1}^{\perp}\rangle$ into the f_1 channel;
- (3) The time evolution of the surviving (single) kaon state $|K_{\neq f_1}\rangle$ from time $t = t_1$ to time $t = t_2$;
- (4) The projection at time $t = t_2$ of the evolved state $|K_{\neq f_1}(\Delta t)\rangle$ onto the state $|K_{\neq f_2}^{\perp}\rangle$ filtered by the decay f_2 , times the decay amplitude of the state $|K_{\neq f_2}^{\perp}\rangle$ into the f_2 channel.

$$I(f_{1}, t_{1}; f_{2}, t_{2})_{\mathrm{TH}} = \left| \langle f_{2} | T | \mathbf{K}_{\neq f_{2}}^{\perp} \rangle \langle \mathbf{K}_{\neq f_{2}}^{\perp} | \mathbf{K}_{\neq f_{1}} (\Delta t) \rangle \langle f_{1} | T | \mathbf{K}_{\neq f_{1}}^{\perp} \rangle \langle \mathbf{K}_{\neq f_{1}}^{\perp} \mathbf{K}_{\neq f_{1}} | i(t = t_{1}) \rangle \right|^{2}$$

$$(4) \qquad (3) \qquad (2) \qquad (1)$$

Double decay intensity calculation





QM calculation of double decay intensity: two alternatives

(II) T.D. Lee and C.N. Yang (LY) two decay times state formalism (1961) [see e.g. T.Day PR121, 1204 (1961), D. Inglis RMP 33, 1 (1961)]

 $|i(t)\rangle = \frac{\mathcal{N}}{\sqrt{2}} \{|\mathbf{K}_{\mathrm{S}}\rangle e^{-i\lambda_{S}t}|\mathbf{K}_{\mathrm{L}}\rangle e^{-i\lambda_{L}t} - |\mathbf{K}_{\mathrm{L}}\rangle e^{-i\lambda_{L}t}|\mathbf{K}_{\mathrm{S}}\rangle e^{-i\lambda_{S}t} \}$ $|i_{t_{1},t_{2}}\rangle = \frac{\mathcal{N}}{\sqrt{2}} \{|\mathbf{K}_{\mathrm{S}}\rangle e^{-i\lambda_{S}t_{1}}|\mathbf{K}_{\mathrm{L}}\rangle e^{-i\lambda_{L}t_{2}} - |\mathbf{K}_{\mathrm{L}}\rangle e^{-i\lambda_{L}t_{1}}|\mathbf{K}_{\mathrm{S}}\rangle e^{-i\lambda_{S}t_{2}} \}$ $I(f_{1}, t_{1}; f_{2}, t_{2})_{\mathrm{LY}} = |\langle f_{1}f_{2}|T|i_{t_{1},t_{2}}\rangle|^{2}$



Double decay intensity calculation





QM calculation of double decay intensity: two alternatives

(II) T.D. Lee and C.N. Yang (LY) two decay times state formalism (1961) [see e.g. T.Day PR121, 1204 (1961), D. Inglis RMP 33, 1 (1961)]

$$|i(t)\rangle = \frac{\mathcal{N}}{\sqrt{2}} \{|\mathbf{K}_{\mathrm{S}}\rangle e^{-i\lambda_{S}t}|\mathbf{K}_{\mathrm{L}}\rangle e^{-i\lambda_{L}t} - |\mathbf{K}_{\mathrm{L}}\rangle e^{-i\lambda_{L}t}|\mathbf{K}_{\mathrm{S}}\rangle e^{-i\lambda_{S}t}\}$$

$$|i_{t_{1},t_{2}}\rangle = \frac{\mathcal{N}}{\sqrt{2}} \{|\mathbf{K}_{\mathrm{S}}\rangle e^{-i\lambda_{S}t_{1}}|\mathbf{K}_{\mathrm{L}}\rangle e^{-i\lambda_{L}t_{2}} - |\mathbf{K}_{\mathrm{L}}\rangle e^{-i\lambda_{L}t_{1}}|\mathbf{K}_{\mathrm{S}}\rangle e^{-i\lambda_{S}t_{2}}\}$$

$$TH \text{ and LY approaches are fully equivalent}}$$

$$I(f_{1}, t_{1}; f_{2}, t_{2})_{\mathrm{LY}} = |\langle f_{1}f_{2}|T|i_{t_{1},t_{2}}\rangle|^{2}$$

$$I(f_{1}, t_{1}; f_{2}, t_{2})_{\mathrm{TH}} = I(f_{1}, t_{1}; f_{2}, t_{2})_{\mathrm{TH}} \equiv I(f_{1}, t_{1}; f_{2}, t_{2})_{\mathrm{LY}} \equiv I(f_{1}, t_{1}; f_{2}, t_{2})$$





If past tags the future, the t_1 , t_2 symmetry of the correlated state in the LY approach demands the exploration of the question: can future post-tag the past?





If past tags the future, the t_1 , t_2 symmetry of the correlated state in the LY approach demands the exploration of the question: can future post-tag the past?





<u>The future (kaon decay at t_2) post-tags</u> <u>the past partner kaon state at t_1 , before the</u> <u>decay, when it was entangled !</u> If past tags the future, the t_1 , t_2 symmetry of the correlated state in the LY approach demands the exploration of the question: can future post-tag the past?





<u>The future (kaon decay at t_2) post-tags</u> <u>the past partner kaon state at t_1 , before the</u> <u>decay, when it was entangled !</u>



$$\begin{split} \begin{split} \left| \begin{matrix} \mathbf{K}^{(1)}(t=t_{1}) \\ \mathbf{FAST} \end{matrix} \right| &= & \frac{\mathcal{N}}{\sqrt{2}} \{ \langle f_{2} | T | \mathbf{K}_{\mathrm{L}} \rangle e^{-i\lambda_{L}t_{2}} e^{-i\lambda_{S}t_{1}} | \mathbf{K}_{\mathrm{S}} \rangle - \langle f_{2} | T | \mathbf{K}_{\mathrm{S}} \rangle e^{-i\lambda_{S}t_{2}} e^{-i\lambda_{L}t_{1}} | \mathbf{K}_{\mathrm{L}} \rangle \} \\ &= & \frac{\mathcal{N}}{\sqrt{2}} \langle f_{2} | T | \mathbf{K}_{\mathrm{S}} \rangle \{ e^{-i\lambda_{S}t_{1}} \left[\eta_{2} \ e^{-i\lambda_{L}t_{2}} | \mathbf{K}_{\mathrm{S}} \rangle \right] - e^{-i\lambda_{L}t_{1}} \left[e^{-i\lambda_{S}t_{2}} \mathbf{K}_{\mathrm{L}} \rangle \right] \} . \\ &= & \mathbf{FUTURE} \end{split}$$





<u>The future (kaon decay at t_2) post-tags</u> <u>the past partner kaon state at t_1 , before the</u> <u>decay, when it was entangled !</u>





From past to future:

The state of the last decaying particle (particle-2) is tagged (prepared) at $t = t_1$ as:

 $|K^{(2)}(t = t_1)\rangle = \mathcal{N}_2[|K_L\rangle - \eta_1|K_S\rangle]$ a state which depends on η_1 of particle-1.

From future to past:

The state of the first decaying particle (particle-1) is **post-tagged** at t = 0 as:

 $|K^{(1)}(t=0)\rangle = \mathcal{N}_1\{\eta_2 e^{-i\lambda_L t_2}|\mathbf{K}_S\rangle - e^{-i\lambda_S t_2}|\mathbf{K}_L\rangle\}$ a state which depends on η_2 and t_2 of particle-2.

The explicit dependence on the future time t_2 , and the other unique features of neutral kaons with respect to other physical systems, like $\Delta\Gamma \neq 0$ and $\langle K_L | K_S \rangle \neq 0$, naturally lead to this peculiar quantum effect:

a definite time correlation (not symmetric comparing "from past to future" to "from future to past") between the outcome at a given future time of the observed decay and the state of the unobserved partner in the past, at entanglement time.

J. Bernabeu and A.D.D., Phys. Rev. D 105, 116004 (2022)



see Bernabeu's

From past to future:

The state of the last decaying particle (particle-2) is tagged (prepared) at $t = t_1$ as:

 $|K^{(2)}(t = t_1)\rangle = \mathcal{N}_2[|K_L\rangle - \eta_1|K_S\rangle]$ a state which depends on η_1 of particle-1.

From future to past:

The state of the first decaying particle (particle-1) is **post-tagged** at t = 0 as:

 $|K^{(1)}(t=0)\rangle = \mathcal{N}_1\{\eta_2 e^{-i\lambda_L t_2}|\mathbf{K}_S\rangle - e^{-i\lambda_S t_2}|\mathbf{K}_L\rangle\}$ a state which depends on η_2 and t_2 of particle-2.

The explicit dependence on the future time t_2 , and the other unique features of neutral kaons with respect to other physical systems, like $\Delta\Gamma \neq 0$ and $\langle K_L | K_S \rangle \neq 0$, naturally lead to this peculiar quantum effect:

a definite time correlation (not symmetric comparing "from past to future" to "from future to past") between the outcome at a given future time of the observed decay and the state of the unobserved partner in the past, at entanglement time.

K_s tag: due to CP violation $\langle K_L | K_S \rangle \neq 0$, the time correlation "from future to past" with condition $e^{-\Delta\Gamma\Delta t/2}/\eta_2 \ll 1$ is the only known method to *post-tag* a K_s beam with arbitrary high purity.

J. Bernabeu and A.D.D., Phys. Rev. D 105, 116004 (2022)

From past to future:

The state of the last decaying particle (particle-2) is tagged (prepared) at $t = t_1$ as:

 $|K^{(2)}(t = t_1)\rangle = \mathcal{N}_2[|K_L\rangle - \eta_1|K_S\rangle]$ a state which depends on η_1 of particle-1.

From future to past:

 $|K^{(1)}(t=0)\rangle = \mathcal{N}_1\{\eta_2 e^{-i\lambda_L t_2}|\mathbf{K}_{\mathbf{S}}\rangle - e$

The explicit dependence on the function kaons with respect to other physical peculiar quantum effect:

a definite time correlation (not symmost") between the outcome at a give

unobserved partner in the past, at entanglement time.

K_S tag: due to CP violation $\langle K_L | K_S \rangle \neq 0$, the time correlation "from future to past" with condition $e^{-\Delta\Gamma\Delta t/2}/\eta_2 \ll 1$ is the only known method to *post-tag* a K_S beam with arbitrary high purity.

J. Bernabeu and A.D.D., Phys. Rev. D 105, 116004 (2022)

as:

 $_2$ and t_2 of particle-2.

ures of neutral aturally lead to this

offective for the state of t

^{see} Bernabeu's

Back from the future





post-tagged state: $|K^{(1)}(t_1 = 0)\rangle = \mathcal{N}\{|K_S\rangle - \rho(t_2)|K_L\rangle\}$ in the case $f = f_1 = f_2$ at fixed t₂: $\rho(t_2) = e^{-i(\lambda_S - \lambda_L)t_2}$

$$\begin{aligned} \left| \langle f | K^{(1)}(t_1) \rangle \right|^2 &= \left| \mathcal{N} \right|^2 \left| \langle f | K_S(t_1) \rangle - \rho(t_2) \langle f | K_L(t_1) \rangle \right|^2 \\ &= \left| \mathcal{N} \right|^2 \left\{ e^{-\Gamma_S t_1} + \left| \rho(t_2) \right|^2 e^{-\Gamma_L t_1} - 2e^{-\frac{\Gamma_S + \Gamma_L}{2} t_1} [\Re \rho(t_2) \cos \Delta m \, t_1 + \Im \rho(t_2) \sin \Delta m \, t_1] \right\} \end{aligned}$$

Experimentally t_2 is averaged on a bin width => e.g. bin width $\frac{1}{2} \tau_s$



"Back from the future": observable effects





















"Back from the future" effect at KLOE-2



- Analysed data: 1.7 fb⁻¹ selection of $K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ events as for search for decoherence/CPTV effects [KLOE-2 - JHEP 04 (2022) 059];
- Fit of t_1 distribution with QM theory taking into account resolution and efficiency through a 4-dimensional smearing matrix

 $(t_{1,true}, t_{1,reco}, t_{2\,true}, t_{2,reco});$

- Negligible background from $e^+e^- \rightarrow 4\pi$ process and regeneration on beam pipe;
- histogram normalization as single fit parameter.





Testing Quantum Mechanics at colliders - 3 December 2024 - Roma Tre University

"Back from the future" effect at KLOE-2



• normalizing the distributions to unity at $t_1=0$, we get a first evidence of the effect



- The analysis to extract the ρ parameter as a function of t_2 is being finalized

Conclusions



- The entanglement of neutral kaon pairs at a ϕ -factory has unique features.
- <u>Search for decoherence and CPT violation effects in $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ at KLOE/KLOE-2 => stringent limits on model parameters (quantum gravity inspired), in some cases with a precision reaching the interesting Planck's scale region.</u>

FROM PAST TO FUTURE:

- Exploiting the maximal entanglement of the initial state for the necessary exchange of *in* and *out* states, it is possible to directly test T and CPT in transition processes.
- The KLOE-2 collaboration performed the first direct test of T and CPT in neutral kaon transitions with a precision of few percent on the corresponding observables.
- No CPT violation observed, T violation at limit, CP violation is observed with a significance of 5.2σ.

FROM FUTURE TO PAST:

- Novel time quantum correlation effect in the entangled kaon system [PRD 105, 116004 (2022)].
- <u>This surprising "Back from the future</u>" effect is fully observable at KLOE/KLOE-2 and naturally leads to the tagging of the K_S state, and to the definition of new observables.
- A preliminary analysis of the φ->K_SK_L -> π⁺π⁻π⁺π⁻ events with KLOE data shows a first evidence of this effect. Finalization of the analysis to extract the ρ parameter as a function of t₂.
- The Back from the future effect cannot be a causal influence, independently of time-like or space-like intervals. This result seems to confirm the counterintuitive feature of time in quantum mechanics, and goes beyond other phenomena, like delayed choice experiments with entangled photon systems, that are stationary at all times, and have the result independent on whether the choice is made in the past or in the future.



Thank you!





SPARE SLIDES

The neutral kaon two-level oscillating system in a nutshell

 K^0 and $\overline{K^0}$ can decay to common final states due to weak interactions: strangeness oscillations



H is the effective hamiltonian (non-hermitian), decomposed into a Hermitian part (mass matrix **M**) and an anti-Hermitian part (i/2 decay matrix Γ):

$$\mathbf{H} = \mathbf{M} - \frac{i}{2} \Gamma = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{21} & \Gamma_{22} \end{pmatrix}$$

Diagonalizing the effective Hamiltonian:

eigenstates: physical states

eigenvalues

$$\lambda_{S,L} = m_{S,L} - \frac{i}{2}\Gamma_{S,L} \qquad |K_{S,L}\rangle = \frac{1}{\sqrt{2(1+|\varepsilon_{S,L}|)}} \left[(1+\varepsilon_{S,L}) |K^0\rangle \pm (1-\varepsilon_{S,L}) |\overline{K}^0\rangle \right]$$

$$|K_{1,2}\rangle \text{ are } CP = \pm 1 \text{ states}$$

$$K_L \to \pi\pi \text{ violates CP} \qquad \left[|K_{1,2}\rangle + \varepsilon_{S,L}| |K_{2,1}\rangle \right] \qquad \left[|K_{1,2}\rangle + \varepsilon_{S,L}| |K_{2,1}\rangle \right]$$

$$|K_{1,2}\rangle \text{ are } CP = \pm 1 \text{ states}$$

$$\left[\langle K_S | K_L \rangle \cong \varepsilon_S^* + \varepsilon_L \neq 0 \right] \text{ small CP impurity } \sim 2 \times 10^{-3}$$

The neutral kaon two-level oscillating system in a nutshell

$$|K_{S,L}\rangle \propto \left[\left(1+\varepsilon_{S,L}\right)|K^{0}\rangle\pm\left(1-\varepsilon_{S,L}\right)|\overline{K}^{0}\rangle\right]$$

CP violation:

T violation:

$$\varepsilon_{S,L} = \varepsilon \pm \delta$$

$$\varepsilon = \frac{H_{12} - H_{21}}{-i\Im M_{12}} = \frac{-i\Im M_{12}}{-i\Im M_{12}} = \frac{-i\Im M_{12}}{-i}$$

$$\frac{H_{12} - H_{21}}{2(\lambda_s - \lambda_L)} = \frac{-i\Im M_{12} - \Im \Gamma_{12}/2}{\Delta m + i\Delta \Gamma/2}$$

CPT violation:

$$\delta = \frac{H_{11} - H_{22}}{2(\lambda_S - \lambda_L)} = \frac{1}{2} \frac{\left(m_{\overline{K}^0} - m_{K^0}\right) - (i/2)\left(\Gamma_{\overline{K}^0} - \Gamma_{K^0}\right)}{\Delta m + i\Delta\Gamma/2}$$

- $\delta \neq 0$ implies CPT violation
- $\varepsilon \neq 0$ implies T violation
- $\epsilon \neq 0$ or $\delta \neq 0$ implies CP violation

```
(with a phase convention \Im \Gamma_{12} = 0)
```

$$\Delta m = m_L - m_S , \quad \Delta \Gamma = \Gamma_S - \Gamma_L$$
$$\Delta m = 3.5 \times 10^{-15} \text{ GeV}$$
$$\Delta \Gamma \approx \Gamma_S \approx 2\Delta m = 7 \times 10^{-15} \text{ GeV}$$

The neutral kaon two-level oscillating system in a nutshell

$$|K_{S,L}\rangle \propto \left[\left(1+\varepsilon_{S,L}\right)|K^{0}\rangle\pm\left(1-\varepsilon_{S,L}\right)|\overline{K}^{0}\rangle\right]$$

CP violation:

T violation:

$$\varepsilon_{S,L} = \varepsilon \pm \delta$$

$$\varepsilon = \frac{H_{12} - H_{21}}{2(\lambda_s - \lambda_L)} = \frac{-i\Im M_{12} - \Im\Gamma_{12}/2}{\Delta m + i\Delta\Gamma/2}$$

CPT violation:

$$\delta = \frac{H_{11} - H_{22}}{2(\lambda_S - \lambda_L)} = \frac{1}{2} \frac{\left(m_{\overline{K}^0} - m_{K^0}\right) - (i/2)\left(\Gamma_{\overline{K}^0} - \Gamma_{K^0}\right)}{\Delta m + i\Delta\Gamma/2}$$

huge amplification factor!!

- $\delta \neq 0$ implies CPT violation
- $\epsilon \neq 0$ implies T violation
- $\epsilon \neq 0$ or $\delta \neq 0$ implies CP violation

```
(with a phase convention \Im\Gamma_{12} = 0)
```

$$\Delta m = m_L - m_S \quad , \qquad \Delta \Gamma = \Gamma_S - \Gamma_L$$

$$\Delta m = 3.5 \times 10^{-15} \text{ GeV}$$

$$\Delta \Gamma \approx \Gamma_{\rm s} \approx 2\Delta m = 7 \times 10^{-15} {\rm GeV}$$



	<m></m> (GeV)	∆m (GeV)	<Γ> (GeV)	ΔΓ/2 (GeV)
K ⁰	0.5	3x10 ⁻¹⁵	3x10 ⁻¹⁵	3x10 ⁻¹⁵
D^0	1.9	6x10 ⁻¹⁵	2x10 ⁻¹²	1x10 ⁻¹⁴
B ⁰ _d	5.3	3x10 ⁻¹³	4x10 ⁻¹³	O(10 ⁻¹⁵) (SM prediction)
$B^0_{\ s}$	5.4	1x10 ⁻¹¹	4x10 ⁻¹³	3x10 ⁻¹⁴

$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$: CPT violation in entangled K states

In presence of decoherence and CPT violation induced by quantum gravity (CPT operator "ill-defined") the definition of the particle-antiparticle states could be modified. This in turn could induce a breakdown of the correlations imposed by Bose statistics (EPR correlations) to the kaon state:

[Bernabeu, et al. PRL 92 (2004) 131601, NPB744 (2006) 180].

I(π⁺π⁻, π⁺π⁻;Δt) (a.u.)

$$|i\rangle \propto \left(|K^{0}\rangle|\bar{K}^{0}\rangle - |\bar{K}^{0}\rangle|K^{0}\rangle\right) + \omega(K^{0}\rangle|\bar{K}^{0}\rangle + |\bar{K}^{0}\rangle|K^{0}\rangle\right) \stackrel{1.2}{\underset{D.8}{\overset{0.6}{\overset{0.4}{\overset{0}{}}}} = 3 \times 10^{-3}$$

at most one expects:
$$|\omega|^{2} = O\left(\frac{E^{2}/M_{PLANCK}}{\Delta\Gamma}\right) \approx 10^{-5} \Rightarrow |\omega| \sim 10^{-3}$$

In some microscopic models of space-time foam arising from non-critical string theory [Bernabeu, Mavromatos, Sarkar PRD 74 (2006) 045014]: $|\omega| \sim 10^{-4} \div 10^{-5}$

The maximum sensitivity to ω is expected for $f_1=f_2=\pi^+\pi^-$ (terms: $|\omega|/|\eta_{+-}|$) All CPTV effects induced by QG ($\alpha,\beta,\gamma,\omega$) could be simultaneously disentangled.

$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$: CPT violation in entangled K states

In presence of decoherence and CPT violation induced by quantum gravity (CPT operator "ill-defined") the definition of the particle-antiparticle states could be modified. This in turn could induce a breakdown of the correlations imposed by Bose statistics (EPR correlations) to the kaon state:

[Bernabeu, et al. PRL 92 (2004) 131601, NPB744 (2006) 180].

 $|i\rangle \propto \left(|K^{0}\rangle|\overline{K}^{0}\rangle - |\overline{K}^{0}\rangle|K^{0}\rangle\right) + \omega(|K^{0}\rangle|\overline{K}^{0}\rangle + |\overline{K}^{0}\rangle|K^{0}\rangle)$ $\propto \left(|K_{S}\rangle|K_{L}\rangle - |K_{L}\rangle|K_{S}\rangle\right) + \omega(|K_{S}\rangle|K_{S}\rangle - |K_{L}\rangle|K_{L}\rangle)$ at most one expects: $\left|\omega\right|^{2} = O\left(\frac{E^{2}/M_{PLANCK}}{\Delta\Gamma}\right) \approx 10^{-5} \Rightarrow |\omega| \sim 10^{-3}$

I(π⁺π⁻, π⁺π⁻;Δt) (a.u.)



In some microscopic models of space-time foam arising from non-critical string theory [Bernabeu, Mavromatos, Sarkar PRD 74 (2006) 045014]: $|\omega| \sim 10^{-4} \div 10^{-5}$

The maximum sensitivity to ω is expected for $f_1=f_2=\pi^+\pi^-$ (terms: $|\omega|/|\eta_{+-}|$) All CPTV effects induced by QG ($\alpha,\beta,\gamma,\omega$) could be simultaneously disentangled.

$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$: CPT violation in entangled K states



Testing Quantum Mechanics at colliders - 3 December 2024 - Roma Tre University

A. Di Domenico

Decoherence and CPT violation

Possible decoherence due quantum gravity effects (BH evaporation) (apparent loss of unitarity): Black hole information loss paradox => Possible decoherence near a black hole. "like candy rolling on the

Hawking [1] suggested that at a microscopic level, in a quantum gravity picture, non-trivial space-time fluctuations (generically <u>space-time foam</u>) could give rise to decoherence effects, which would necessarily entail a violation of CPT [2].

Modified Liouville – von Neumann equation for the density matrix of the kaon system with 3 new CPTV parameters α , β , γ [3]:

$$\dot{\rho}(t) = \underbrace{-iH\rho + i\rho H^{+}}_{QM} + L(\rho;\alpha,\beta,\gamma)$$

extra term inducing decoherence: pure state => mixed state







tongue" J. Wheeler



A. Di Domenico

Decoherence and CPT violation

Possible decoherence due quantum gravity effects (BH evaporation) (apparent loss of unitarity): Black hole information loss paradox => Possible decoherence near a black hole. "like candy rolling on the

Hawking [1] suggested that at a microscopic level, in a quantum gravity picture, non-trivial space-time fluctuations (generically <u>space-time foam</u>) could give rise to decoherence effects, which would necessarily entail a violation of CPT [2].

Modified Liouville – von Neumann equation for the density matrix of the kaon system with 3 new CPTV parameters α, β, γ [3]: at most (e.g., in non-critical string models):

$$\dot{\rho}(t) = \underbrace{-iH\rho + i\rho H^{+}}_{QM} + L(\rho; \alpha, \beta, \gamma) \qquad \alpha, \beta, \gamma = O\left(\frac{M_{K}^{2}}{M_{PLANCK}}\right) \approx 2 \times 10^{-20} \text{ GeV}$$

[1] Hawking, Comm.Math.Phys.87 (1982) 395; [2] Wald, PR D21 (1980) 2742; [3] Ellis et. al, NP B241 (1984) 381; Ellis, Mavromatos et al. PRD53 (1996)3846; Handbook on kaon interferometry [hep-ph/0607322],
M. Arzano PRD90 (2014) 024016 => Theories with Planck scale deformed symmetries can induce decoherence





tongue" J. Wheeler



$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$: decoherence and CPT violation



$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$: decoherence & CPTV limits



$$\begin{split} \zeta_{0\overline{0}} &= (-0.5 \pm 8.0_{stat} \pm 3.7_{syst}) \times 10^{-7} \\ \zeta_{SL} &= (0.1 \pm 1.6_{stat} \pm 0.7_{syst}) \times 10^{-2} \\ \gamma &= (1.3 \pm 9.4_{stat} \pm 4.2_{syst}) \times 10^{-22} \text{ GeV} \\ \Re \omega &= (-2.3^{+1.9}_{-1.5stat} \pm 0.6_{syst}) \times 10^{-4} \\ \Im \omega &= (-4.1^{+2.8}_{-2.6stat} \pm 0.9_{syst}) \times 10^{-4} \\ |\omega| &= (4.7 \pm 2.9_{stat} \pm 1.0_{syst}) \times 10^{-4} \\ \phi_{\omega} &= -2.1 \pm 0.2_{stat} \pm 0.1_{syst} \text{ rad} \end{split}$$

$$\lambda \cong \frac{\zeta_{SL}}{\Gamma_s} = (0.1 \pm 1.2_{stat} \pm 0.5_{syst}) \times 10^{-16} \text{ GeV}$$

BR($\phi \to K_S K_S, K_L K_L$) < 2.4×10⁻⁷ at 90% C.L.

KLOE-2 JHEP 04 (2022) 059

[improvement x2 wrt KLOE PLB 642(2006) 315]

Systematic uncertainties

	$\delta \zeta_{ m SL}$	$\delta \zeta_{0 \bar{0}}$	$\delta\gamma$	$\delta \Re \omega$	$\delta\Im\omega$	$\delta \omega $	$\delta \phi_{\omega}$
	$\cdot 10^2$	$\cdot 10^7$	$\cdot 10^{21}{ m GeV}$	$\cdot 10^4$	$\cdot 10^4$	$\cdot 10^4$	(rad)
Cut stability	0.56	2.9	0.33	0.53	0.65	0.78	0.07
4π background	0.37	1.9	0.22	0.32	0.19	0.32	0.04
Regeneration	0.17	0.9	0.10	0.06	0.63	0.58	0.05
Δt resolution	0.18	0.9	0.10	0.15	0.09	0.15	0.02
Input phys. const.	0.04	0.2	0.02	0.03	0.09	0.07	0.01
Total	0.71	3.7	0.42	0.64	0.93	1.04	0.10

$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$: test of quantum coherence



The decoherence parameter ζ depends on the basis in which the spontaneous factorization mechanism is specified:

 $\xi = 0$ (QM) $\xi = 1$ (total decoherence)

$$\begin{aligned} & \mathsf{K}_{\mathsf{S}}\mathsf{K}_{\mathsf{L}} & |i\rangle = \frac{1}{\sqrt{2}} \Big[\big| K_{s} \big\rangle \big| K_{L} \big\rangle - \big| K_{L} \big\rangle \big| K_{s} \big\rangle \Big] & \Rightarrow \quad \big| K_{s} \big\rangle \big| K_{L} \big\rangle \quad \text{or} \quad \big| K_{L} \big\rangle \big| K_{s} \big\rangle \\ & |\eta_{+-}| = \frac{\big| \langle \pi^{+}\pi^{-} | T | K_{L} \rangle \big|}{\langle \pi^{+}\pi^{-} | T | K_{s} \rangle} \Big|_{\sim 10^{-3}} & \mathbf{I} \propto \big| \langle \pi^{+}\pi^{-}, \pi^{+}\pi^{-} | T | i \rangle \big|^{2} & \mathbf{I} \propto \big| \langle \pi^{+}\pi^{-} | T | K_{s} \big\rangle \big\langle \pi^{+}\pi^{-} | T | K_{L} \big\rangle \big|^{2} \\ & \text{suppressed by CP violation} & \text{suppressed by CP violation} \end{aligned}$$

$$\begin{split} K^{0}\overline{K}^{0} & |i\rangle = \frac{1}{\sqrt{2}} \Big[|K^{0}\rangle |\overline{K}^{0}\rangle - |\overline{K}^{0}\rangle |K^{0}\rangle \Big] \implies |K^{0}\rangle |\overline{K}^{0}\rangle \quad \text{or} \quad |\overline{K}^{0}\rangle |K^{0}\rangle \\ \text{basis} & I \propto \left| \langle \pi^{+}\pi^{-}, \pi^{+}\pi^{-}|T|i\rangle \right|^{2} & I \propto \left| \langle \pi^{+}\pi^{-}|T|K^{0}\rangle \langle \pi^{+}\pi^{-}|T|\overline{K}^{0}\rangle \right|^{2} \\ \frac{\langle \pi^{+}\pi^{-}|T|\overline{K}^{0}\rangle}{\langle \pi^{+}\pi^{-}|T|\overline{K}^{0}\rangle} |\sim^{1} \text{ suppressed by CP violation} & \text{not suppressed by CP violation} \\ => \text{ intuitive explanation of the high sensitivity to } \zeta_{0\overline{0}} \end{split}$$


- CPT theorem holds for any QFT formulated on flat space-time which assumes: (1) Lorentz invariance (2) Locality (3) Unitarity
- Extension of CPT theorem to a theory of quantum gravity far from obvious (e.g. CPT violation appears in several QG models)
- Consequences of CPT symmetry: equality of masses, lifetimes, |q| and $|\mu|$ of a particle and its anti-particle.
- Is it possible to test the CPT symmetry directly in transition processes between kaon states, rather than comparing masses, lifetimes, or other intrinsic properties of particle and anti-particle states?
- CPT violating effects may not appear at first order in diagonal mass terms (survival probabilities) while they can manifest at first order in transitions (non-diagonal terms).
- Clean formulation required. Possible spurious effects induced by CP violation in the decay and/or a violation of the ΔS = ΔQ rule have to be well under control. Genuine effect must be independent of ΔΓ, i.e. not requiring the decay as an essential ingredient.

Probing CPT: J. Bernabeu, A.D.D., P. Villanueva, JHEP 10 (2015) 139 Time-reversal violation: J. Bernabeu, A.D.D., P. Villanueva, NPB 868 (2013) 102

Time Reversal



•The transformation of a system corresponding to the inversion of events in time, or reversed dynamics, with the formal substitution $\Delta t \rightarrow -\Delta t$, is usually called 'time reversal', but a more appropriate name would actually be motion reversal.



•Exchange of in \leftrightarrow out states and reversal of all momenta and spins tests time reversal, i.e. the symmetry of the responsible dynamics for the observed process under time reversal (transformation implemented in QM by an antiunitary operator)

•Similarly for CPT tests: the exchange of in \leftrightarrow out states etc.. is required.



Defenses	Terrete	CD contracto	CDT contracto
Reference	1-conjugate	CP-conjugate	CP1-conjugate
$\mathrm{K}^{0} \rightarrow \mathrm{K}^{0}$	$\mathrm{K}^{0} \rightarrow \mathrm{K}^{0}$	$\bar{K}^0 \to \bar{K}^0$	$\bar{K}^0 \to \bar{K}^0$
$K^0 \to \bar{K}^0$	$\bar{K}^0 \to K^0$	$\bar{K}^0 \to K^0$	$K^0 \to \bar{K}^0$
$\mathrm{K}^{0} \to \mathrm{K}_{+}$	$\mathrm{K}_+ \to \mathrm{K}^0$	$\bar{\rm K}^0 \to {\rm K}_+$	${\rm K}_+ \to \bar{\rm K}^0$
$\mathrm{K}^{0} \rightarrow \mathrm{K}_{-}$	$\mathrm{K}_{-} \to \mathrm{K}^{0}$	$\bar{K}^0 \to K$	$K \to \bar{K}^0$
$\bar{K}^0 \to K^0$	${\rm K}^0 \to \bar{\rm K}^0$	$K^0 \to \bar{K}^0$	$\bar{K}^0 \to K^0$
$\bar{K}^0 \to \bar{K}^0$	$\bar{K}^0 \to \bar{K}^0$	$\mathrm{K}^{0} \rightarrow \mathrm{K}^{0}$	$\mathrm{K}^{0} \rightarrow \mathrm{K}^{0}$
$\bar{K}^0 \to K_+$	$K_+ \to \bar{K}^0$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{+}$	$\mathrm{K}_+ \to \mathrm{K}^0$
$\bar{K}^0 \to K$	$K \to \bar{K}^0$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{-}$	$\mathrm{K}_{-} \to \mathrm{K}^{0}$
$\mathrm{K}_+ \to \mathrm{K}^0$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{+}$	$K_+ \to \bar{K}^0$	$\bar{\mathrm{K}}^{0} \rightarrow \mathrm{K}_{+}$
$K_+ \to \bar{K}^0$	$\bar{K}^0 \to K_+$	$\mathrm{K}_+ \to \mathrm{K}^0$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{+}$
$\mathrm{K}_+ \to \mathrm{K}_+$	$\mathrm{K}_+ \to \mathrm{K}_+$	$\mathrm{K}_+ \to \mathrm{K}_+$	$\mathrm{K}_+ \to \mathrm{K}_+$
$\mathrm{K}_+ \to \mathrm{K}$	$\mathrm{K}_{-} \rightarrow \mathrm{K}_{+}$	$\mathrm{K}_+ \to \mathrm{K}$	$\mathrm{K}_{-} \to \mathrm{K}_{+}$
$\mathrm{K}_{-} \to \mathrm{K}^{0}$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{-}$	$K\to \bar{K}^0$	$\bar{K}^0 \to K$
$K\to \bar K^0$	$\bar{K}^0 \to K$	$\mathrm{K}_{-} \to \mathrm{K}^{0}$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{-}$
$\mathrm{K}_{-} \to \mathrm{K}_{+}$	$\mathrm{K}_+ \to \mathrm{K}$	$\mathrm{K}_{-} \to \mathrm{K}_{+}$	$\mathrm{K}_+ \rightarrow \mathrm{K}$
$\mathrm{K}_{-} \to \mathrm{K}_{-}$	$\mathrm{K}_{-} \rightarrow \mathrm{K}_{-}$	$\mathrm{K}_{-} \to \mathrm{K}_{-}$	$\mathrm{K}_{-} \rightarrow \mathrm{K}_{-}$



Conjugate= reference

Reference	T-conjugate	CP-conjugate	CPT-conjugate
$\mathrm{K}^{0} \rightarrow \mathrm{K}^{0}$	$\mathbf{K}_{0} \rightarrow \mathbf{K}_{0}$	$\bar{K}^0 \to \bar{K}^0$	$\bar{K}^0 \to \bar{K}^0$
$K^0 \to \bar{K}^0$	$\bar{K}^0 \to K^0$	$\bar{K}^0 \to K^0$	\mathbf{K}^{0} $\overline{\mathbf{K}}^{0}$
$\mathrm{K}^{0} \rightarrow \mathrm{K}_{+}$	$\mathrm{K}_+ \to \mathrm{K}^0$	$\bar{K}^0 \to K_+$	$K_+ \to \bar{K}^0$
$\mathrm{K}^{0} \to \mathrm{K}_{-}$	$\mathrm{K}_{-} \to \mathrm{K}^{0}$	$\bar{K}^0 \to K$	$K \to \bar{K}^0$
$\bar{K}^0 \to K^0$	$K^0 \to \bar{K}^0$	$K^0 \to \bar{K}^0$	$\bar{\mathbf{k}}^0$, \mathbf{k}^0
$\bar{K}^0 \to \bar{K}^0$	$\overline{\mathbf{X}}^{0} \longrightarrow \overline{\mathbf{X}}^{0}$	$\mathrm{K}^{0} \rightarrow \mathrm{K}^{0}$	$\mathrm{K}^{0} \rightarrow \mathrm{K}^{0}$
$\bar{K}^0 \to K_+$	$K_+ \to \bar{K}^0$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{+}$	$\mathrm{K}_+ \to \mathrm{K}^0$
$\bar{K}^0 \to K$	$K\to \bar K^0$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{-}$	$\mathrm{K}_{-} \to \mathrm{K}^{0}$
$K_+ \to K^0$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{+}$	$K_+ \to \bar{K}^0$	$\bar{K}^0 \to K_+$
$K_+ \to \bar{K}^0$	$\bar{K}^0 \to K_+$	$\mathrm{K}_+ \to \mathrm{K}^0$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{+}$
$\mathrm{K}_+ \to \mathrm{K}_+$	$K \rightarrow K$	\mathbf{K}_{+} \mathbf{K}_{+}	K_{+}
$\mathrm{K}_+ \to \mathrm{K}$	$\mathrm{K}_{-} \to \mathrm{K}_{+}$	\mathbf{V}_{+}	$\mathrm{K}_{-} \to \mathrm{K}_{+}$
$\mathrm{K}_{-} \to \mathrm{K}^{0}$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{-}$	$K\to \bar{K}^0$	$\bar{K}^0 \to K$
$K \to \bar{K}^0$	$\bar{K}^0 \to K$	$\mathrm{K}_{-} \to \mathrm{K}^{0}$	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{-}$
$\mathrm{K}_{-} \to \mathrm{K}_{+}$	$\mathrm{K}_+ \to \mathrm{K}$	$\mathbf{V} \rightarrow \mathbf{V}_+$	$\mathrm{K}_+ \to \mathrm{K}$
$\mathrm{K}_{-} \to \mathrm{K}_{-}$			K K



• • ·				
Conjugate=	Reference	<i>T</i> -conjugate	CP-conjugate	CPT-conjugate
reference	$K^0 \to K^0$	$\mathbf{K}_{0} \rightarrow \mathbf{K}_{0}$	$\bar{K}^0 \to \bar{K}^0$	$\bar{K}^0 \to \bar{K}^0$
	$K^0 \to \bar{K}^0$	$\bar{\mathrm{K}}^{0} \rightarrow \mathrm{K}^{0}$	$\bar{K}^0 \to K^0$	$\mathbf{K}^{0} \rightarrow \mathbf{K}^{0}$
	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{+}$	$K_+ \to K^0$	$\bar{K}^0 \to K_+$	$K_+ \to \bar{K}^0$
already in the table with	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{-}$	$K_{-} \rightarrow K^{0}$	$\bar{K}^0 \to K$	$K \to \bar{K}^0$
	$\bar{K}^0 \to K^0$	\mathbf{K}_0 \mathbf{K}_0	$\mathbf{k}_0 \cdot \mathbf{k}_0$	$\bar{\mathbf{K}}^0$, \mathbf{K}^0
	$\bar{K}^0 \to \bar{K}^0$	$\overline{\mathbf{X}}^0 \longrightarrow \overline{\mathbf{X}}^0$	$\overline{\mathbf{K}^0} \rightarrow \overline{\mathbf{K}}^0$	$\overline{\mathbf{K}^0} \rightarrow \overline{\mathbf{K}^0}$
reference	$\bar{K}^0 \to K_+$	$K_+ \to \bar{K}^0$		$\mathrm{K}_+ \to \mathrm{K}^0$
	$\bar{K}^0 \to K$	$K_{-} \rightarrow \bar{K}^{0}$	$\mathbf{K}^0 \rightarrow \mathbf{K}$	$\mathrm{K}_{-} \to \mathrm{K}^{0}$
	$K_+ \rightarrow K^0$	$K^0 \rightarrow K$	$K_+ \to \bar{K}^0$	$\bar{\mathbf{K}}^0$, $\mathbf{K}_{\mathbf{k}}$
	$K_+ \to \bar{K}^0$	$\overline{\mathbf{K}}^{0}$ $\overline{\mathbf{K}}$		\mathbf{K}^{0} \mathbf{K}_{+}
	$\mathrm{K}_+ \to \mathrm{K}_+$	K K		K K
	$\mathrm{K}_+ \to \mathrm{K}$	$K_{-} \rightarrow K_{+}$		$\mathrm{K}_{-} \to \mathrm{K}_{+}$
	$K_{-} \rightarrow K^{0}$	K ⁰ K	$K \to \bar{K}^0$	K ⁰ K
	$K \to \bar{K}^0$	KO K		
	$\mathrm{K}_{-} \to \mathrm{K}_{+}$			
	$\mathrm{K}_{-} \to \mathrm{K}_{-}$	K K		K K



Conjugata				
Conjugate=	Reference	T-conjugate	CP-conjugate	CPT-conjugate
reference	$K^0 \to K^0$	K K	$\bar{K}^0 \to \bar{K}^0$	$\bar{K}^0 \rightarrow \bar{K}^0$
already in the table with conjugate as reference	$K^0 \to \bar{K}^0$	$\bar{K}^0 \to K^0$	$\bar{\mathrm{K}}^{0} \rightarrow \mathrm{K}^{0}$	$\mathbf{K}^0 \rightarrow \mathbf{\bar{K}}^0$
	$\mathrm{K}^{0} \rightarrow \mathrm{K}_{+}$	$\mathrm{K}_+ \to \mathrm{K}^0$	$\bar{K}^0 \to K_+$	$K_+ \to \bar{K}^0$
	$\mathrm{K}^{0} \to \mathrm{K}_{-}$	$\mathrm{K}_{-} \to \mathrm{K}^{0}$	$\bar{K}^0 \to K$	$\mathrm{K}_{-} \to \bar{\mathrm{K}}^{0}$
	$\bar{K}^0 \to K^0$	K^0 \bar{K}^0	\mathbf{K}^0 $\mathbf{\bar{K}}^0$	$\mathbf{\bar{k}}^0 \setminus \mathbf{k}^0$
	$\bar{K}^0 \to \bar{K}^0$	$\overline{\mathbf{X}}^{0} \rightarrow \overline{\mathbf{X}}^{0}$	$\overline{\mathbf{K}}^0 \rightarrow \overline{\mathbf{K}}^0$	$\overline{\mathbf{N}} \xrightarrow{0} \overline{\mathbf{N}}$
	$\bar{K}^0 \to K_+$	$K_+ \to \bar{K}^0$	\mathbf{K}^{0} \mathbf{K}_{+}	$K_+ \rightarrow K^0$
	$\bar{K}^0 \to K$	$K \to \bar{K}^0$		$\mathrm{K}_{-} \rightarrow \mathrm{K}^{0}$
	$\mathrm{K}_+ \to \mathrm{K}^0$	$K^0 \rightarrow K$	$K_+ \to \bar{K}^0$	<u>ko</u> k
Two identical conjugates for one reference	$K_+ \to \bar{K}^0$	$\bar{\mathbf{K}}^0$ - K_{\mp}	\mathbf{H}_{+} \mathbf{H}_{0}	\mathbf{K}^{0} \mathbf{K}_{+}
	$\mathrm{K}_+ \to \mathrm{K}_+$	$K \rightarrow K$	\mathbf{K}_{+} \mathbf{K}_{+}	K K
	$\mathrm{K}_+ \to \mathrm{K}$	$K_{-} \rightarrow K_{+}$	$\mathbf{K} \to \mathbf{K}$	$K_{-} \rightarrow K_{+}$
	$\mathrm{K}_{-} \to \mathrm{K}^{0}$	\mathbf{V}^0 \mathbf{V}	$K \to \bar{K}^0$	K ⁰ K
	$K \to \bar{K}^0$		$\mathbf{H} \rightarrow \mathbf{H}^0$	
	$\mathrm{K}_{-} \to \mathrm{K}_{+}$			
	$\mathrm{K}_{-} \to \mathrm{K}_{-}$		$V \to V_{-}$	K K



Conjugate= Reference T-conjugate CP-conjugate *CPT*-conjugate reference $K^0 \rightarrow K^0$ $\bar{\mathrm{K}}^0 \rightarrow \bar{\mathrm{K}}^0$ $\bar{K}^0 \rightarrow \bar{K}^0$ $\bar{K}^0 \rightarrow K^0$ $\bar{K}^0 \to K^0$ $K^0 \rightarrow \bar{K}^0$ $K^0 \rightarrow K_+$ $K_+ \rightarrow \bar{K}^0$ $K_+ \rightarrow K^0$ $\bar{\mathrm{K}}^0 \to \mathrm{K}_+$ $K^0 \rightarrow K_ K_{-} \rightarrow K^{0}$ $K_{-} \rightarrow \bar{K}^{0}$ $\bar{\mathrm{K}}^{0} \rightarrow \mathrm{K}_{-}$ already in the \mathbf{K}^0 $\mathbf{\bar{K}}^0$ $\bar{\mathbf{k}}_0$ \mathbf{k}_0 $\bar{\mathrm{K}}^{0} \rightarrow \mathrm{K}^{0}$ \underline{K}_{0} \underline{K}_{0} table with $\overline{\mathbf{R}}^{0} \rightarrow \overline{\mathbf{R}}^{0}$ $\bar{\mathrm{K}}^0 \to \bar{\mathrm{K}}^0$ $R^{0} \rightarrow R^{0}$ conjugate as $\bar{\mathrm{K}}^0 \to \mathrm{K}_+$ $K_+ \rightarrow \bar{K}^0$ $K_+ \rightarrow K^0$ reference $\bar{\mathrm{K}}^0 \to \mathrm{K}_- \mid \mathrm{K}_- \to \bar{\mathrm{K}}^0$ $K_{-} \rightarrow K^{0}$ K^0 K $K_+ \to \bar{K}^0$ $\overline{\mathbf{V}^0}$ V $K_+ \rightarrow K^0$ $K_+ \to \bar{K}^0$ $\overline{\mathbf{v}}_{0}$ $K_+ \rightarrow K_+$ K V Two identical $\mathrm{K}_+ \rightarrow \mathrm{K}_ \mathbf{V} \longrightarrow \mathbf{V}$ $K_{-} \rightarrow K_{+}$ $\rightarrow K_{\perp}$ conjugates **1**70 $K \rightarrow K^0$ TZ. $K_{-} \rightarrow \bar{K}^{0}$ for one reference $K_{-} \rightarrow \bar{K}^{0}$ **T**Z0 V_{+} $K_{-} \rightarrow K_{+}$ LZ. $K_{-} \rightarrow K_{-}$ \mathbf{V} \mathbf{V} V

4 distinct tests of T symmetry

4 distinct tests of CP symmetry

4 distinct tests of CPT symmetry

Direct test of CPT symmetry in neutral kaon transitions

Two observable ratios of double decay intensities at ϕ -factory

for
$$\Delta t < 0$$
 for $\Delta t > 0$

$$R_{2,CPT}^{exp}(\Delta t) \equiv \frac{I(\ell^{-}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{-}; \Delta t)} = R_{1,CPT}(|\Delta t|) \times D_{CPT} = R_{2,CPT}(\Delta t) \times D_{CPT}$$

$$R_{4,CPT}^{exp}(\Delta t) \equiv \frac{I(\ell^{+}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{+}; \Delta t)} = R_{3,CPT}(|\Delta t|) \times D_{CPT} = R_{4,CPT}(\Delta t) \times D_{CPT}$$
with D_{CPT} constant
$$D_{CPT} = \frac{BR(K_{L} \rightarrow 3\pi^{0})}{BR(K_{S} \rightarrow \pi\pi)} \frac{\Gamma_{L}}{\Gamma_{S}}$$
for visualization purposes, plots with
$$R_{e(\delta)=3.3} 10^{4} Im(\delta)=1.6 10^{5}$$

Testing Quantum Mechanics at colliders - 3 December 2024 - Roma Tre University

Direct test of CPT symmetry in neutral kaon transitions

Two observable ratios of double decay intensities at ϕ -factory

for
$$\Delta t < 0$$
 for $\Delta t > 0$

$$R_{2,CPT}^{exp}(\Delta t) \equiv \frac{I(\ell^{-}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{-}; \Delta t)} = R_{1,CPT}(|\Delta t|) \times D_{CPT} = R_{2,CPT}(\Delta t) \times D_{CPT}$$

$$R_{4,CPT}^{exp}(\Delta t) \equiv \frac{I(\ell^{+}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{+}; \Delta t)} = R_{3,CPT}(|\Delta t|) \times D_{CPT} = R_{4,CPT}(\Delta t) \times D_{CPT}$$
with D_{CPT} constant
$$D_{CPT} = \frac{BR(K_{L} \rightarrow 3\pi^{0})}{BR(K_{S} \rightarrow \pi\pi)} \frac{\Gamma_{L}}{\Gamma_{S}}$$
for visualization purposes, plots with
$$R_{e(\delta)=3.3} 10^{4} Im(\delta)=1.6 10^{5}$$

Direct test of T symmetry in neutral kaon transitions



Two observable ratios of double decay intensities at ϕ -factory

$$R_{2,\mathcal{T}}^{\exp}(\Delta t) \equiv \frac{I(\ell^{-}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{+}; \Delta t)}$$
$$R_{4,\mathcal{T}}^{\exp}(\Delta t) \equiv \frac{I(\ell^{+}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{-}; \Delta t)}$$

for
$$\Delta t < 0$$
 for $\Delta t > 0$
= $R_{1,T}(|\Delta t|) \times D_T$ = $R_{2,T}(\Delta t) \times D_T$

 $= R_{3,\mathrm{T}}(|\Delta t|) \times D_{\mathrm{T}} = R_{4,\mathrm{T}}(\Delta t) \times D_{\mathrm{T}}$



for visualization purposes, plots with CP violation in the mixing from PDG and CPT invariance



The region $\Delta t > 0$ is statistically most populated at KLOE

A. Di Domenico

Testing Quantum Mechanics at colliders – 3 December 2024 – Roma Tre University

Direct test of T symmetry in neutral kaon transitions



Two observable ratios of double decay intensities at ϕ -factory

$$R_{2,\mathcal{T}}^{\exp}(\Delta t) \equiv \frac{I(\ell^{-}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{+}; \Delta t)}$$
$$R_{4,\mathcal{T}}^{\exp}(\Delta t) \equiv \frac{I(\ell^{+}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{-}; \Delta t)}$$

for
$$\Delta t < 0$$
 for $\Delta t > 0$
= $R_{1,T}(|\Delta t|) \times D_T$ = $R_{2,T}(\Delta t) \times D_T$

$$= R_{3,\mathrm{T}}(|\Delta t|) \times D_{\mathrm{T}} = R_{4,\mathrm{T}}(\Delta t) \times D_{\mathrm{T}}$$

with
$$D_{T} = D_{CPT}$$
 constant
 $D_{CPT} = \frac{BR (K_{L} \rightarrow 3\pi^{0})}{BR (K_{S} \rightarrow \pi\pi)} \frac{\Gamma_{L}}{\Gamma_{S}}$

for visualization purposes, plots with CP violation in the mixing from PDG and CPT invariance



The region $\Delta t > 0$ is statistically most populated at KLOE

A. Di Domenico

Testing Quantum Mechanics at colliders – 3 December 2024 – Roma Tre University

Direct test of T symmetry in neutral kaon transitions



Two observable ratios of double decay intensities at ϕ -factory

$$R_{2,\mathcal{T}}^{\exp}(\Delta t) \equiv \frac{I(\ell^{-}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{+}; \Delta t)}$$
$$R_{4,\mathcal{T}}^{\exp}(\Delta t) \equiv \frac{I(\ell^{+}, 3\pi^{0}; \Delta t)}{I(\pi\pi, \ell^{-}; \Delta t)}$$

with $D_T = D_{CPT}$ constant

 $D_{\rm CPT} = \frac{{\rm BR} \left({\rm K}_{\rm L} \to 3\pi^0 \right)}{{\rm BR} \left({\rm K}_{\rm S} \to \pi\pi \right)} \frac{\Gamma_L}{\Gamma_S}$

$$= R_{1,T}(|\Delta t|) \times D_T \qquad = R_{2,T}(\Delta t) \times D_T$$

$$= R_{3,\mathrm{T}}(|\Delta t|) \times D_{\mathrm{T}} = R_{4,\mathrm{T}}(\Delta t) \times D_{\mathrm{T}}$$



The region $\Delta t > 0$ is statistically most populated at KLOE

for visualization purposes, plots with CP violation in the mixing from PDG and CPT invariance

Impact of the approximations on the tests



In general K_+, K_- and K^0, \overline{K}^0 can be non-orthogonal bases

T test

Assumes $\Delta S = \Delta Q$ rule and negligible direct CP/CPT violation. In the limit $\Delta t \gg \tau_S$ negligible contaminations from direct CP violation.

CPT test

Assumes $\Delta S = \Delta Q$ rule and negligible direct CP/CPT violation. In the limit $\Delta t \gg \tau_S$ negligible contaminations from direct CP violation. The double ratio constitutes one of the most robust observables for the proposed CPT test. In the limit $\Delta t \gg \tau_S$ it exhibits a pure and genuine CPT violating effect, without assuming negligible contaminations from direct CP violation and/or $\Delta S = \Delta Q$ rule violation.

$$\mathsf{DR}_{\mathsf{CPT}} = \frac{R_{2,\mathrm{CPT}}^{\mathrm{exp}}(\Delta t \gg \tau_S)}{R_{4,\mathrm{CPT}}^{\mathrm{exp}}(\Delta t \gg \tau_S)} = 1 - 8\Re\delta - 8\Re x_-$$

CLEANEST MODEL INDEPENDENT CPT OBSERVABLE

