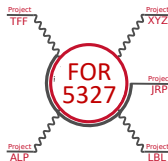
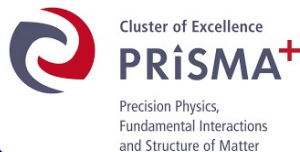


*Workshop on Flavour Changing and  
Conserving Processes (FCCP2025)  
Anacapri, September 29, 2025*



# Status of R measurements at low-energy $e^+e^-$ colliders



*Achim Denig  
Institute for Nuclear Physics  
Johannes Gutenberg University Mainz*

# *R Measurements and Hadronic Vacuum Polarization*

Marc Knecht

## Hadronic vacuum polarization

Anomalous magnetic moment of the muon  $(g-2)_\mu$

Running electromagnetic fine structure constant

$$a_\mu^{HVP} = \frac{1}{4\pi^3} \int_{4m_\pi^2}^{\infty} ds K(s) \sigma_{\text{had}}(s)$$

$$\alpha_{\text{em}}(M_Z^2) = \frac{1}{1 - \Delta\alpha(M_Z^2)};$$

$$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2) \sim \int_{4\pi^2}^{\infty} ds \frac{R_{\text{had}}(s)}{s(s - M_Z^2)}$$

$$\sigma_{\text{had}}(s) = \sigma_{\text{tot}}(e^+e^- \rightarrow \text{Hadrons})$$

$$R_{\text{had}} = \frac{\sigma_{\text{had}}(s)}{\sigma_{ee \rightarrow \mu\mu}(s)}$$

# R Measurements and Hadronic Vacuum Polarization

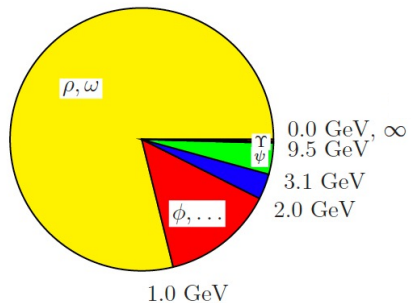
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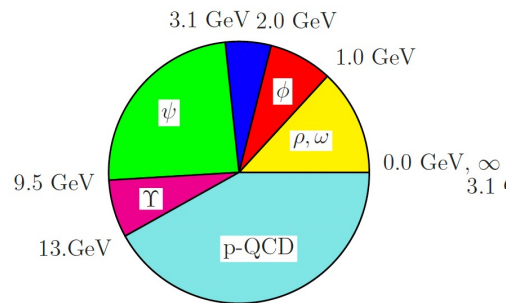
→ relevant mass range < 2...3 GeV  
leading channel:  $e^+e^- \rightarrow \pi^+\pi^-$   
>70% contribution to  $a_\mu^{HVP}$

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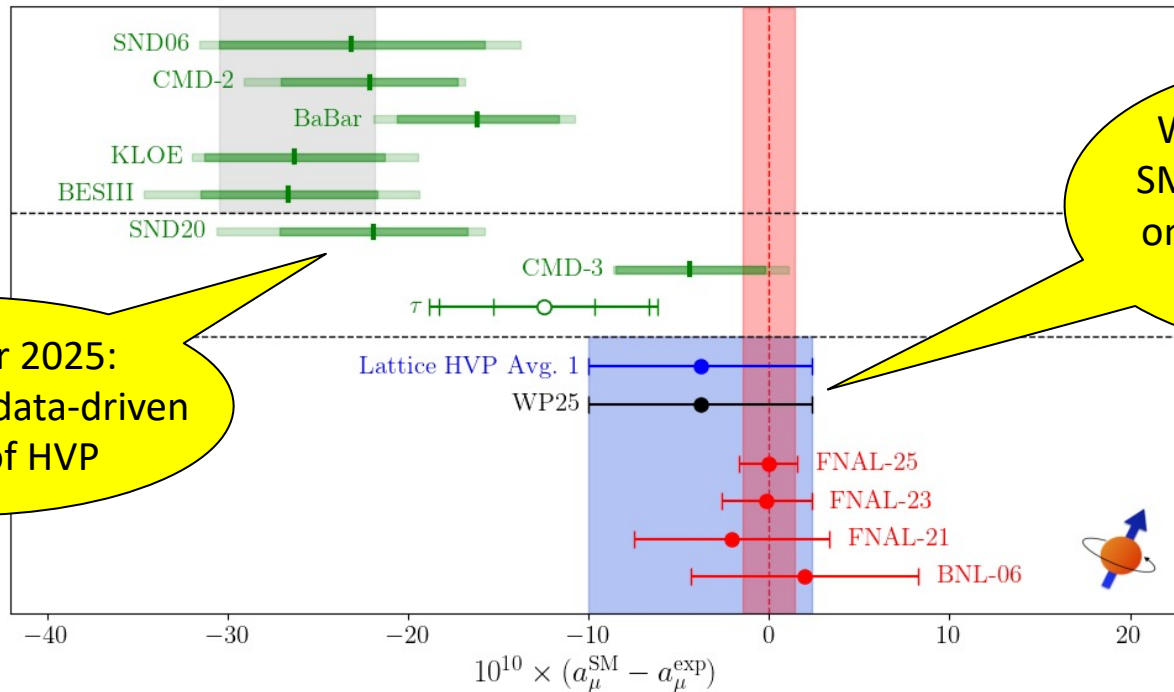


→ relevant mass range  
< 13 GeV

# Whitepaper '25: Lattice QCD-based SM-Prediction for $(g-2)_\mu$

Davide Giusti

After decades of SM  $g-2$  calculations, for the first time dispersive determination not used any more



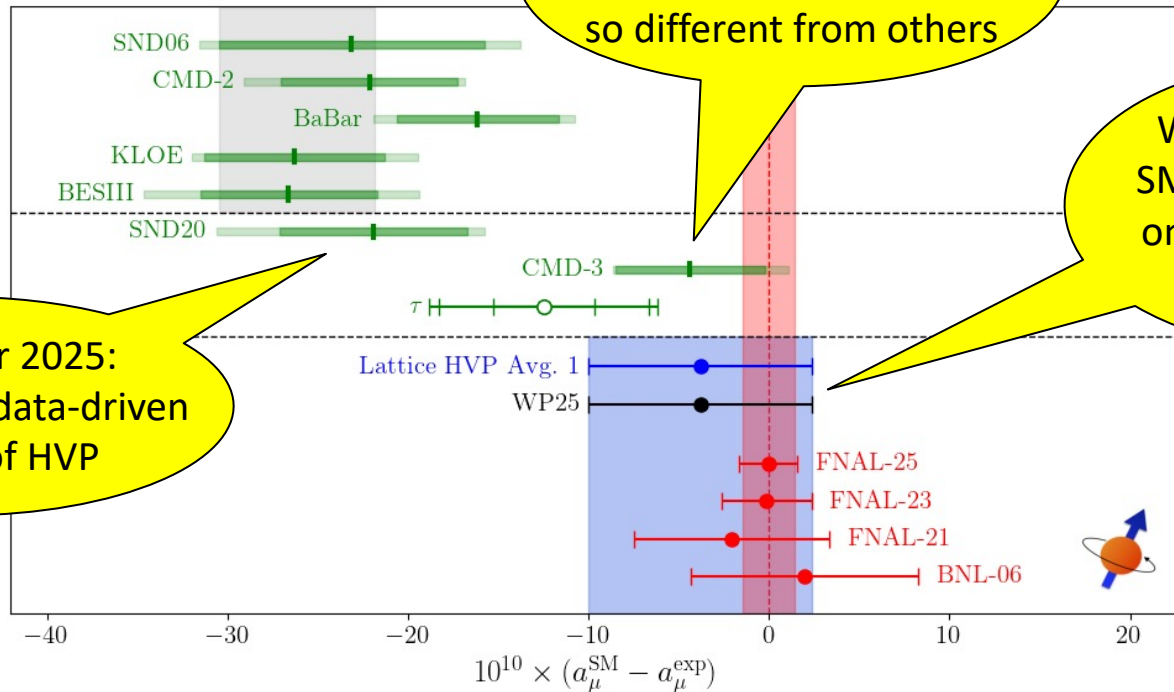
Whitepaper 2025:  
no average for data-driven  
estimate of HVP

Whitepaper 2025:  
SM prediction based  
on LQCD calculation  
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# Whitepaper '25: Lattice QCD-based SM-Prediction for $(g-2)_\mu$

After decades of SM  $g-2$  calculations, for the first time a prediction is not used any more



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CMD-3 measurement  
of  $e^+e^- \rightarrow \pi^+\pi^-$   
so different from others

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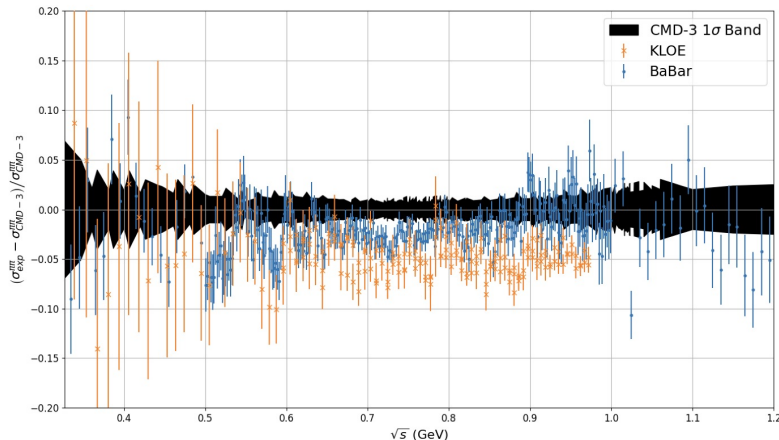
# 2023 Shock: CMD-3 @ Novosibirsk $e^+e^- \rightarrow \pi^+\pi^-$

- New result from CMD-3 collaboration @ VEPP-2000 collider in Novosibirsk
  - Energy scan (from threshold up to 1.2 GeV) method, no ISR!
  - Form factor extraction via selection of  $\pi\pi/\text{ee}$  ratio
  - **Highest statistics data sample** of all experiments, systematic uncertainty 0.7% on  $\rho$  peak
- **Significant deviation from previous ISR and energy scan experiments (CMD-2)! Why?**

PRL 132 (2024) 231903  
PRD 109 (2024) 112002

$$|F_\pi|^2 = \left( \frac{N_{\pi^+\pi^-}}{N_{e^+e^-}} - \Delta^{bg} \right) \cdot \frac{\sigma_{e^+e^-}^0 \cdot (1 + \delta_{e^+e^-}) \cdot \varepsilon_{e^+e^-}}{\sigma_{\pi^+\pi^-}^0 \cdot (1 + \delta_{\pi^+\pi^-}) \cdot \varepsilon_{\pi^+\pi^-}}$$

Courtesy Aidan Wright



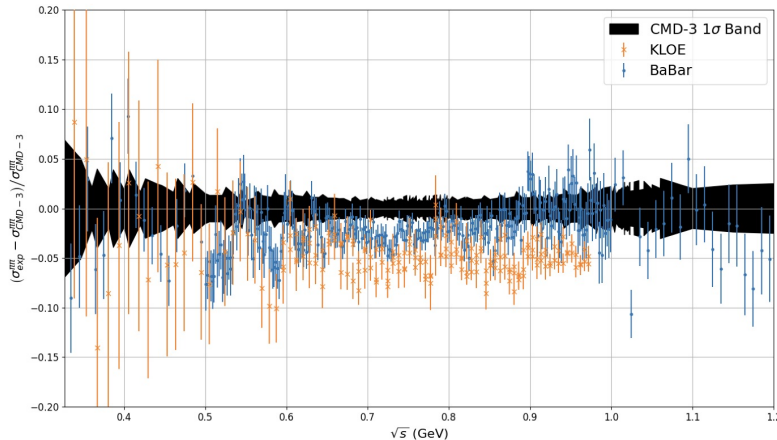
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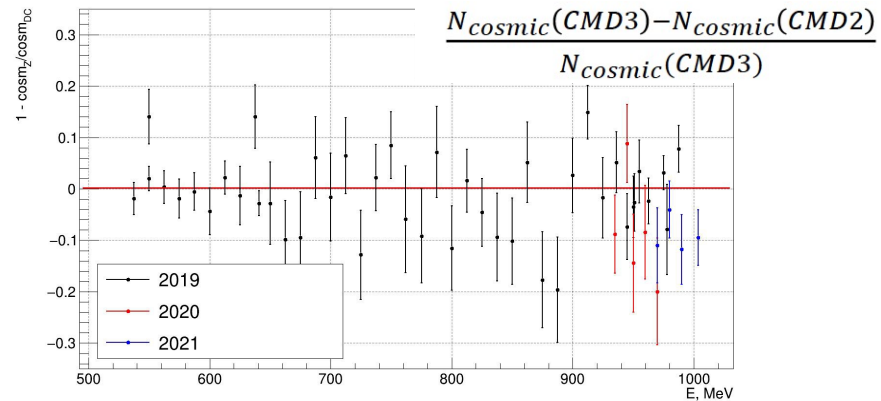
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Courtesy Aidan Wright



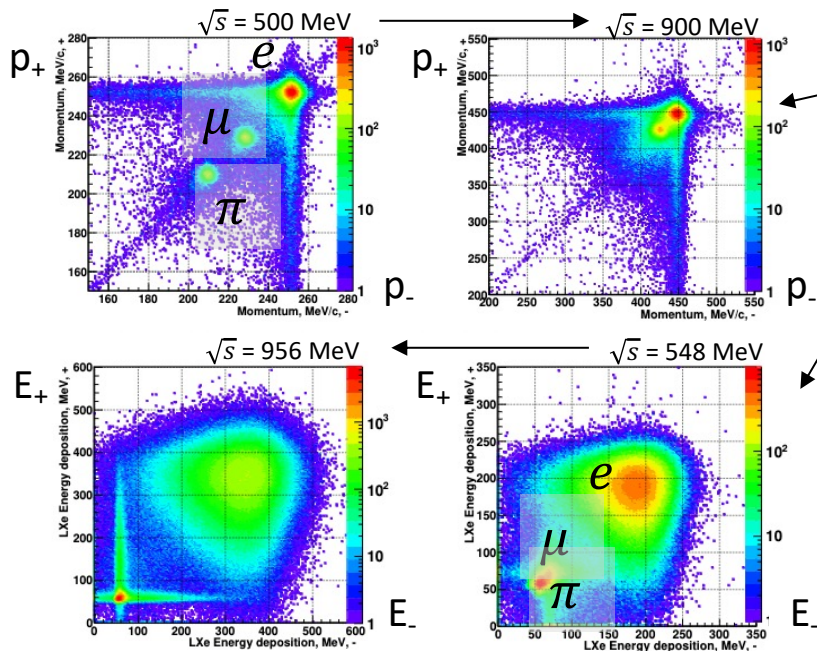
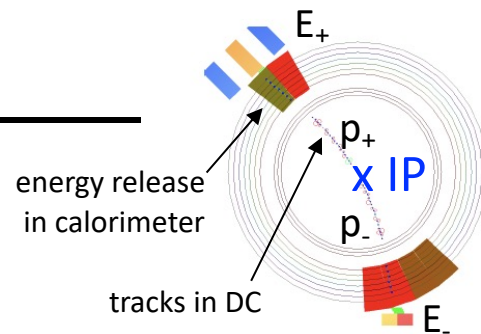
Background from cosmic ray events  
as a possible explanation for CMD-2/CMD-3 difference?



# 2023 Shock: CMD-3 @ Novosibirsk $e^+e^- \rightarrow \pi^+\pi^-$

## Scrutiny of CMD-3 result within the Theory Initiative

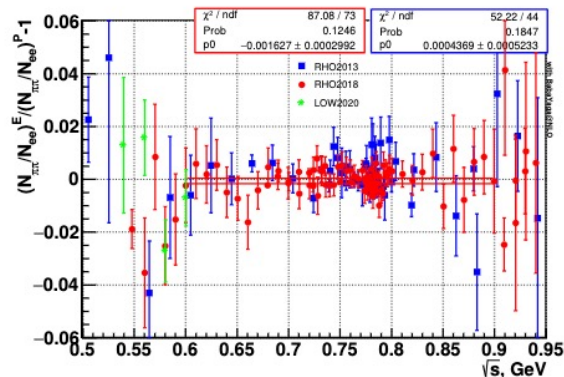
- Very open replies by F. Ignatov  $\rightarrow$  no major showstopper observed
- Very powerful analysis with many and impressive internal cross checks
- Monte-Carlo generator for energy scan cannot be independently verified



Most impressive feature:  $\pi\pi/ee$  ratio determined independently by two complementary methods

- Momentum based
- Calorimetric

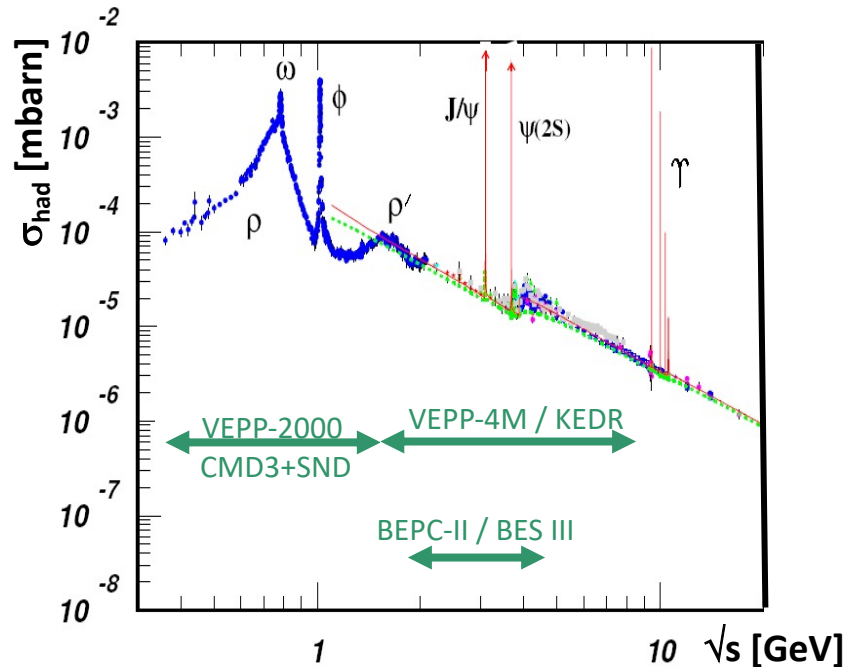
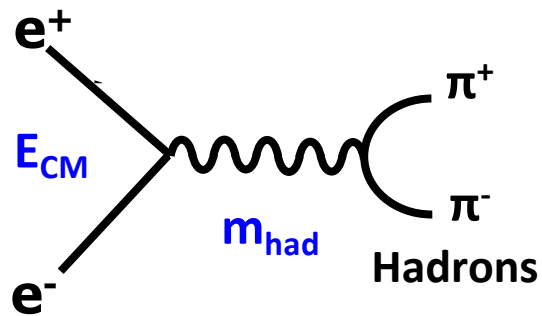
agreement  $\sim 0.2\%$  around rho peak



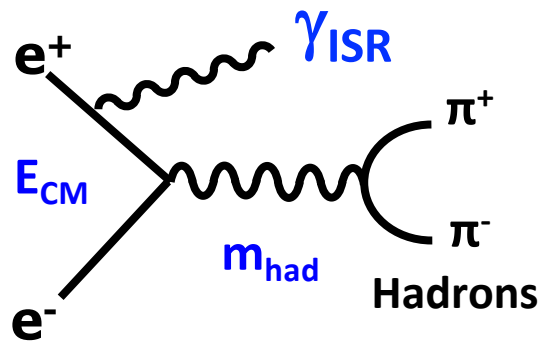
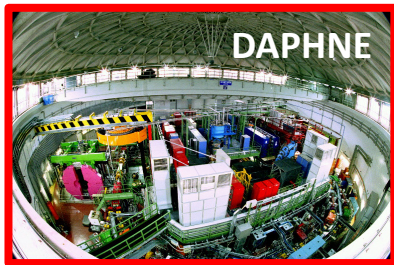


# **The alternative Method: Initial State Radiation (ISR)**

# Measurements on $R$ – Energy Scan vs. Initial State Radiation

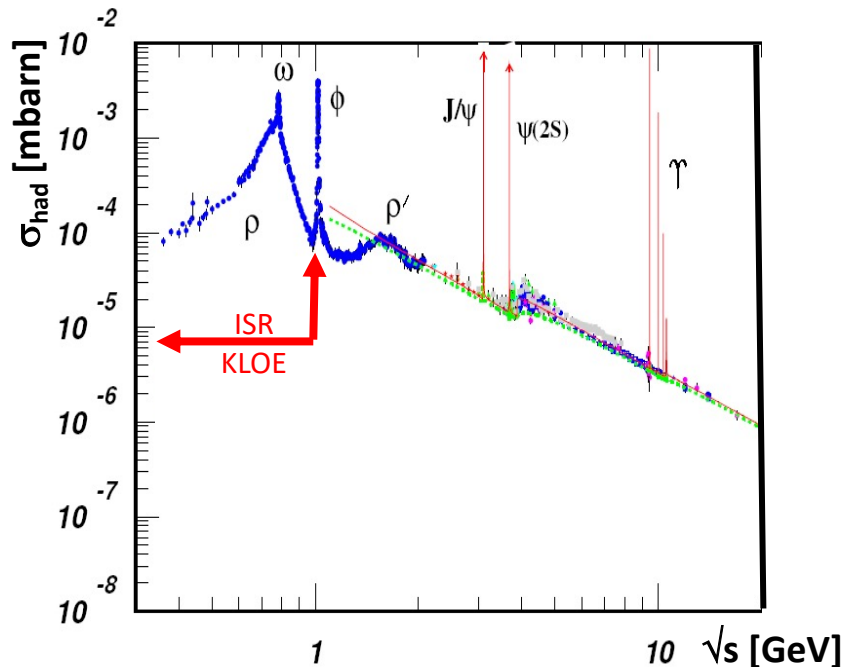


# Measurements on $R$ – Energy Scan vs. Initial State Radiation



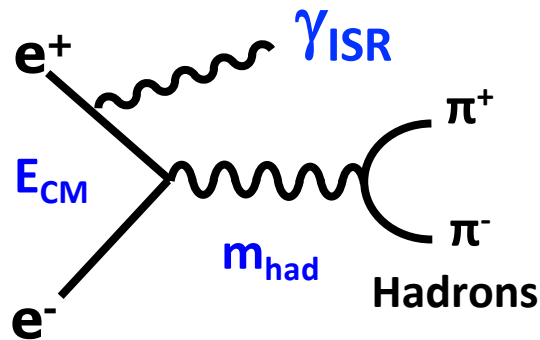
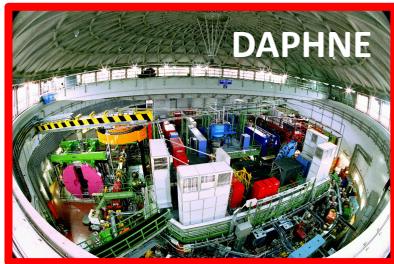
- No systematic variation of  $E_{\text{beam}}$
- High statistics thanks to high luminosity
- Radiative corrections ( $H_{\text{rad}}$ )

PHOKHARA event generator



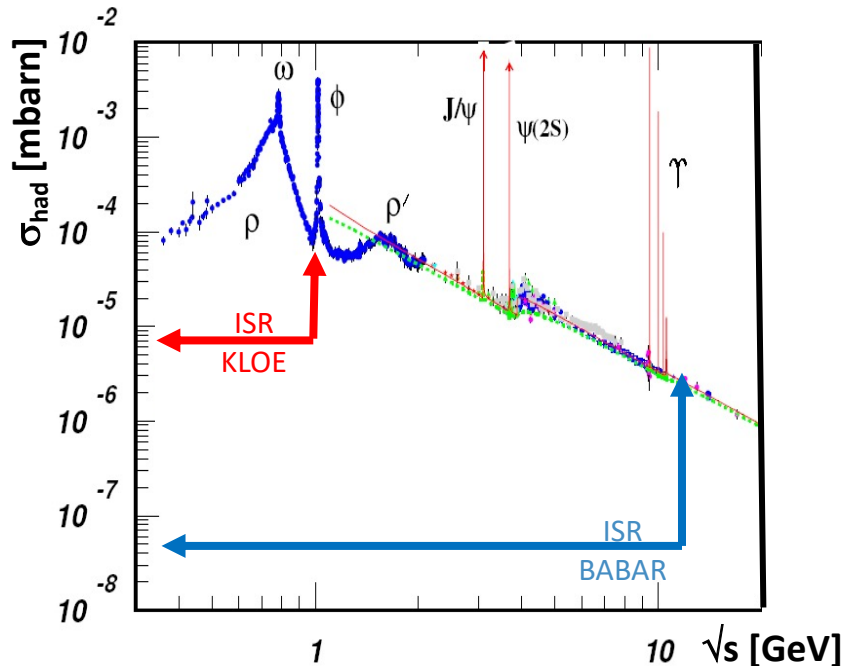


# Measurements on $R$ – Energy Scan vs. Initial State Radiation



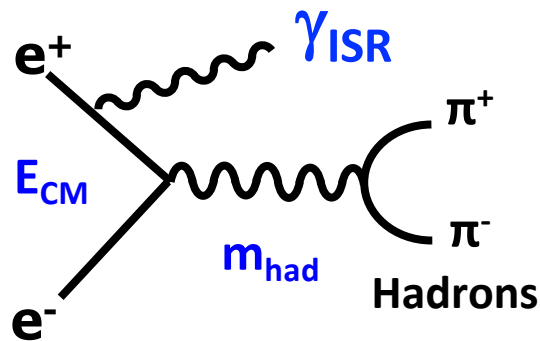
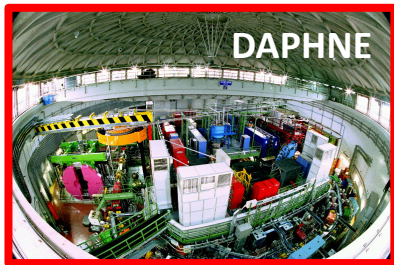
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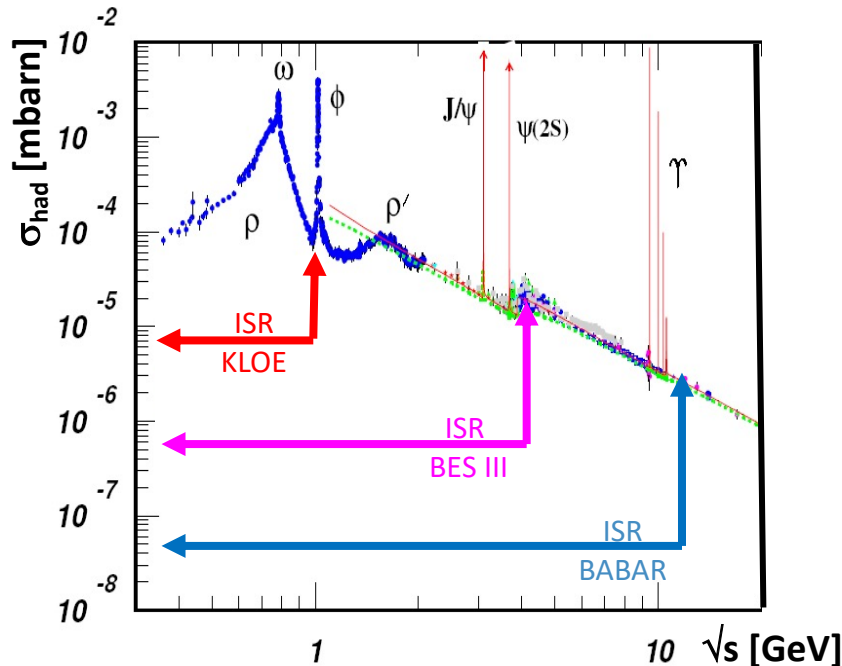


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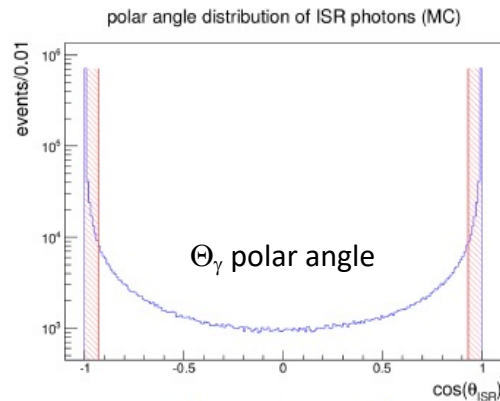


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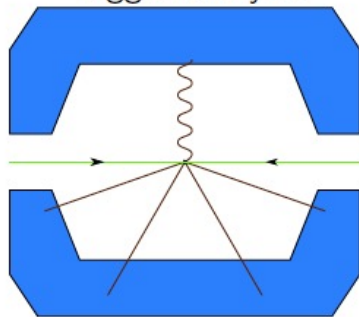
# Initial State Radiation – tagged vs. untagged



**Tagged analysis:**  
ISR photon measured in Calorimeter

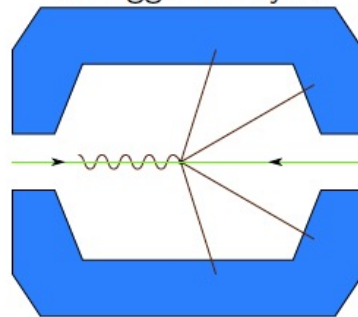
**Untagged analysis:**  
No ISR detection; cut on missing momentum

Tagged analysis



- + exclusive reconstruction
- increased background
- reduced statistics
- + mass range  $\sqrt{s'} < E_{CM}$

Untagged analysis



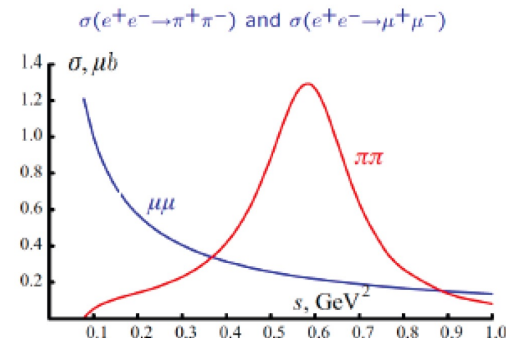
- + reduced background
  - + very high statistics (x5)
  - mass range  $E_{th} < \sqrt{s'} < E_{CM}$
- KLOE:  $E_{th} = \sim 0.6$  GeV  
 BESIII:  $E_{th} = \sim 1$  GeV  
 BABAR:  $E_{th} = \sim 3$  GeV

# Initial State Radiation - Normalization

## Two independent normalization methods:

1) normalization to  $L_{\text{int}}$  (obtained from Bhabha events) and  $H_{\text{rad}}$ ; subtraction of background ( $\mu^+\mu^-\gamma$ , ...)

$$\sigma_{\text{bare}}(e^+e^- \rightarrow \pi^+\pi^-) = \frac{N_{\pi\pi\gamma}/\epsilon_{\text{exp}}}{L_{\text{int}} \cdot H_{\text{rad}} \cdot \delta_{\text{vac}} \cdot (1 + \delta_{\text{FSR}})}$$



# Initial State Radiation - Normalization

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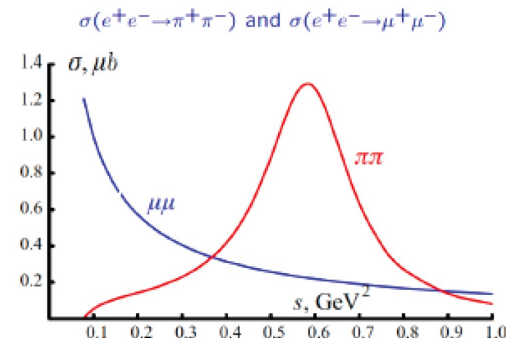
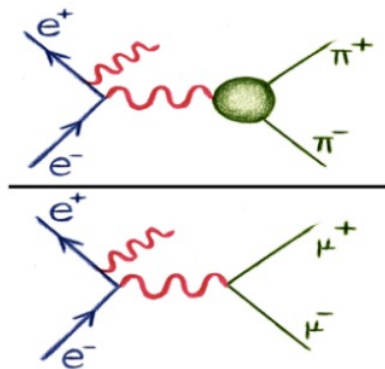
$$\sigma_{bare}(e^+e^- \rightarrow \pi^+\pi^-) = \frac{N_{\pi\pi\gamma}/\epsilon_{exp}}{L_{int} \cdot H_{rad} \cdot \delta_{vac} \cdot (1 + \delta_{FSR})}$$

2) **normalization to  $\mu^+\mu^-\gamma$  events, i.e. R ratio ( $\pi\pi\gamma/\mu\mu\gamma$ )**

→  $L_{int}$ ,  $H_{rad}$ ,  $\delta_{vac}$  cancel in ratio!

→ requires high statistics of  $\mu^+\mu^-\gamma$

$$R = \frac{N_{\pi^+\pi^-}}{N_{\mu^+\mu^-}} \cdot \frac{\epsilon_{\mu^+\mu^-} \cdot (1 + \delta_{\mu^+\mu^-}^{FSR})}{\epsilon_{\pi^+\pi^-} \cdot (1 + \delta_{\pi^+\pi^-}^{FSR})}$$

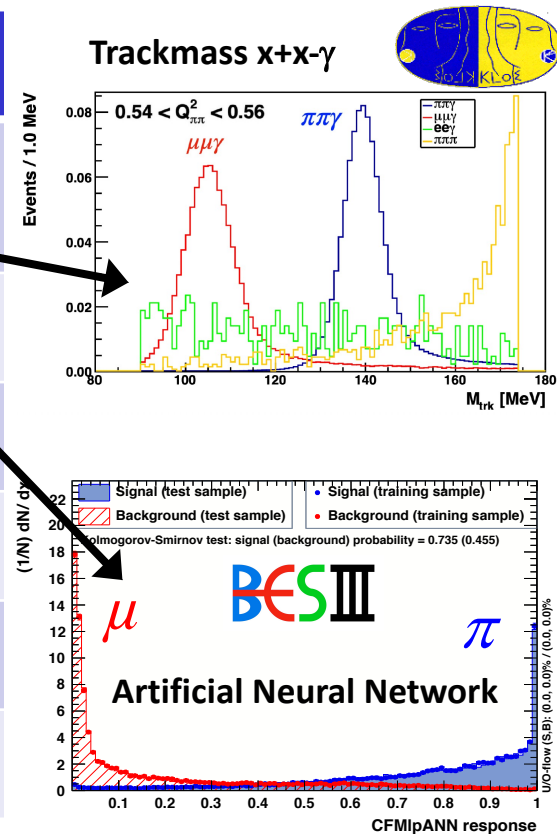


# Overview Experiments

Experiment	Published Method	Normalization	Separation $\pi - \mu$
KLOE $\sqrt{s} \sim 1$ GeV	ISR untagged ISR tagged ISR untagged	Luminosity + $H_{\text{rad}}$ Luminosity + $H_{\text{rad}}$ $\mu + \mu - \gamma$	Kinematics Track Kinematics Track Kinematics Track
BABAR $\sqrt{s} \sim 10$ GeV	ISR tagged	$\mu + \mu - \gamma$	Particle ID
BESIII $\sqrt{s} \sim 4$ GeV	ISR tagged	Luminosity + $H_{\text{rad}}$	Particle ID (ML)
BELLE-II $\sqrt{s} \sim 10$ GeV			
CMD-2/CMD-3	Scan $< \sim 1$ GeV	$e + e -$	Kinematics Track Kinematics EMC
SND	Scan $< \sim 1$ GeV	$e + e -$	Kinematics EMC

# Overview Experiments

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SND	Scan $< \sim 1$ GeV	$e + e -$	Kinematics EMC

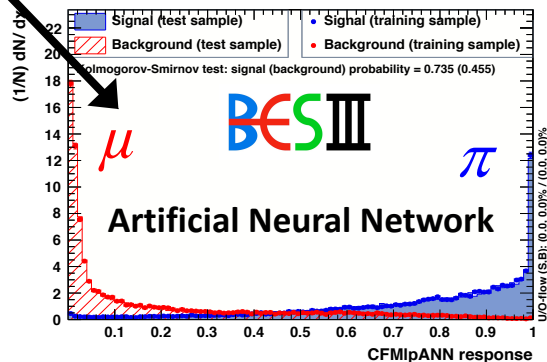
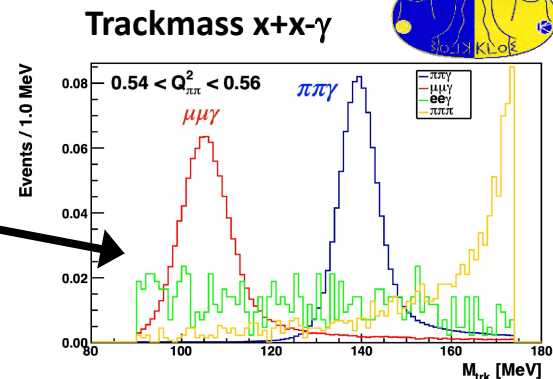


# Overview Experiments



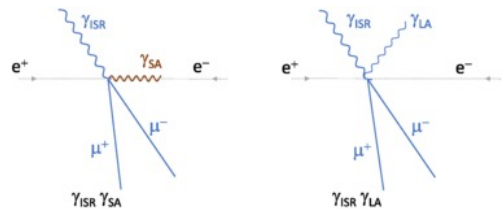
**Diverse set of methods,  
cms energies,  
normalizations, selections**

Experiment	Publication	Normalization	Separation $\pi - \mu$
KLOE		Luminosity + $H_{\text{rad}}$ Luminosity + $H_{\text{rad}}$ $\mu\mu\gamma$	Kinematics Track Kinematics Track Kinematics Track
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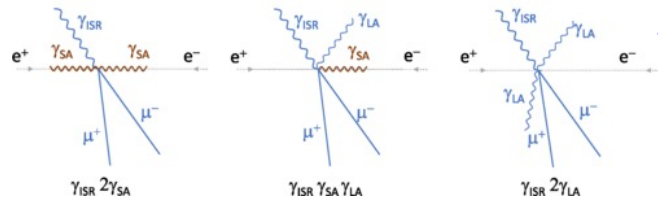


# BABAR Radiative Correction Studies (2023)

NLO



NNLO



BABAR analysis requires  
1 photon at large angle

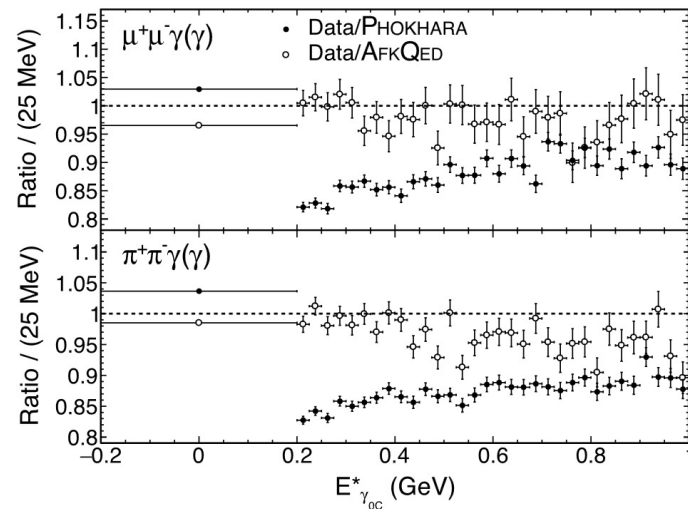
## Detailed study of NLO and NNLO radiative corrections

- Kinematic fits for  $\pi^+\pi^-\gamma_{ISR,LA}\gamma(\gamma)$ ,  $\mu^+\mu^-\gamma_{ISR,LA}\gamma(\gamma)$
- Comparison with PHOKHARA (NLO full correction) and AfkQED (collinear approximation beyond LO) generators

→ NNLO radiation observed at 3.5% level (missing in PHOKHARA)

→ Phokhara prediction for small angle ISR photons at NLO too high by ~25% (AfkQED fits better to data)

Phys. Rev. D 108, L111103





# Possible Consequences from BABAR Findings (?)

Eur. Phys. J. C 84, 721 (2024)

- BABAR:**
- rather inclusive selection and therefore weak dependence from PHOKHARA
    - small effect on published BABAR result due to PHOKHARA NLO limitations
  - however: in original BABAR  $2\pi$  paper 2% correction applied to AfkQED due to statement that PHOKHARA provides better NLO correction → only valid for acceptance (?)

- KLOE/BESIII:**
- less inclusive selection regarding NLO
    - claim: large effects due PHOKHARA NLO limitations of up to 3.2% in the case of BESIII

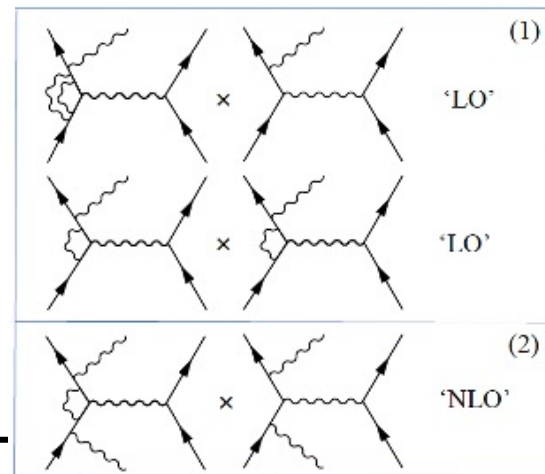
However, scenarios need to be taken into account:

1: NNLO interference terms (1) dominate → large effects

2: NNLO interference terms (2) dominate

→ significantly reduced effects on experimental analyses

So far no explicit calculation of these NNLO interference effects



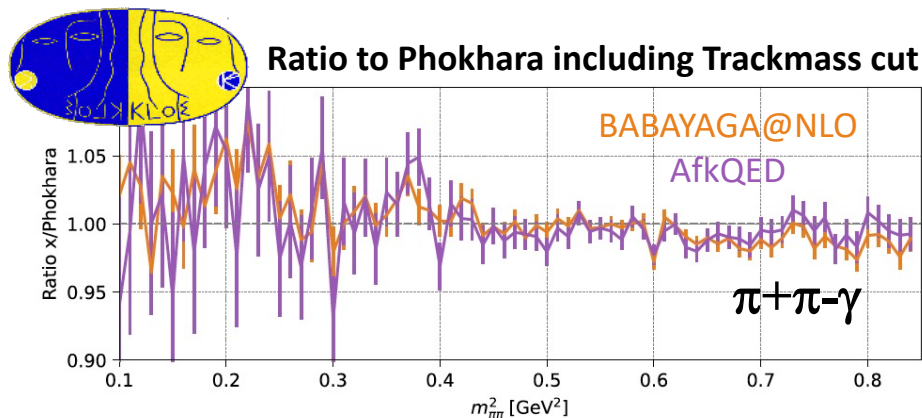
# KLOE / BESIII Response to PHOKHARA Shortcomings

Investigation of kinematic cuts, which are sensitive to NLO corrections: Trackmass (KLOE),  $\chi^2$  (BESIII)

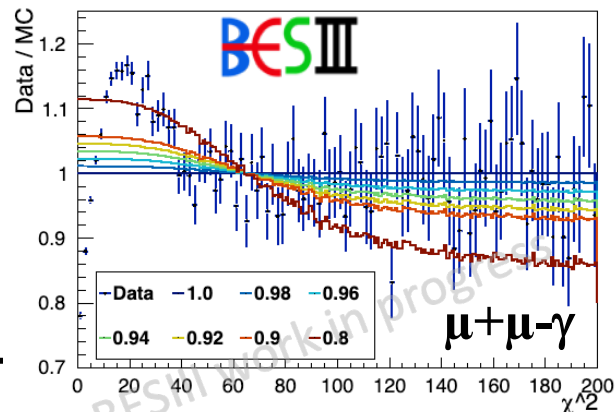
Radio-MonteCarlow Initiative with detailed comparisons

- KLOE has presented a **good agreement between various MC generators** for realistic acceptance cuts and also in the case of the kinematic trackmass cut for KLOE-10
- BESIII has carried out a **full detector simulations for various MC generators** and a **data-PHOKHARA comparison for  $e^+e^- \rightarrow \mu^+\mu^-\gamma$  in the  $\chi^2$  distribution**; furthermore it has been demonstrated that the published analysis is **largely inclusive in higher order corrections**

→ **scenario 2 from DHLM223 paper strongly preferred**



Data-Phokhara comparison for  $\chi^2$  distribution



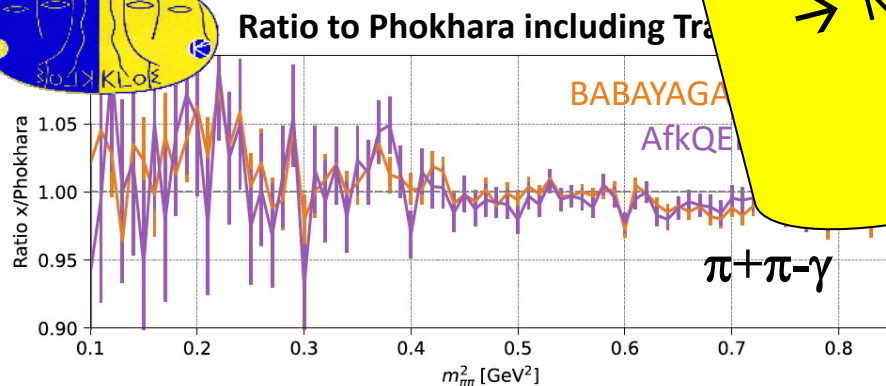
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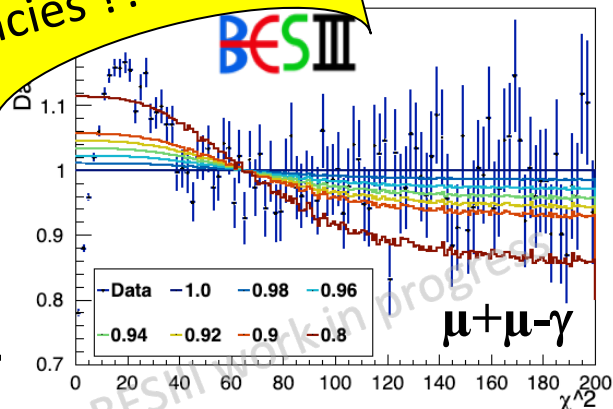
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→ **scenario 2 from DHLM223 paper strongly**



**News from 2024 KEK workshop:**  
Phokhara limitations likely not impacting KLOE/BESIII  
→ No viable explanation for discrepancies ?!



**NEW**

# *The need for improved radiative corrections*

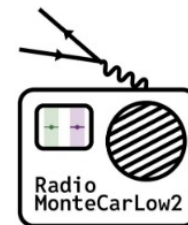
Andrea Gurgone

Fulvio Piccini

ISR: for hadronic channels (especially two-pion channel) no independent cross check to Phokhara !

Energy scan: no independent cross check to MCGPJ generator !

- **Development of new MC generators of utmost importance for the field**  
PHOKHARA@NNLO, McMule, Sherpa, BABAYAGA@NLO ( including  $\pi^+\pi^-\gamma$  )
- **Controlled treatment of Final State Radiation effects**
- **Efforts coordinated within the RadioMontecarlo initiative**
- **Strong interplay between Theory and Experiment**



**NEW**

# *The need for improved radiative corrections*

Andrea Gurgone

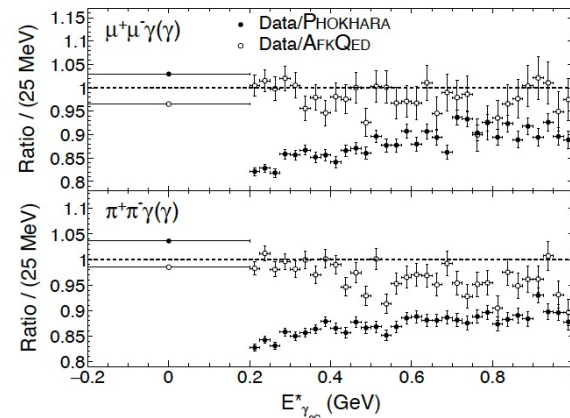
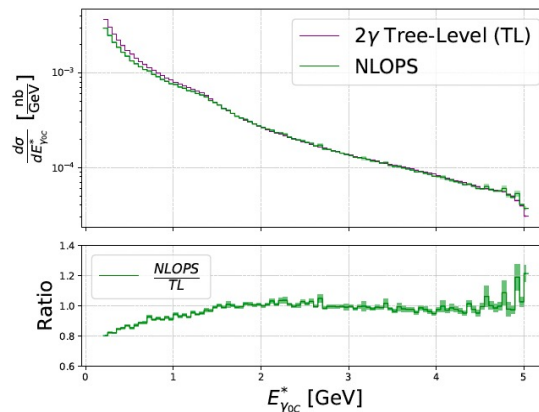
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- **Strong interplay between Theory and Experiment**



Fulvio Piccini @ Orsay

First results from new BABAYAGA@NLO  
→ seems to confirm findings of BABAR  
regarding PHOKHARA liminations





# **Breaking News from 2025 Orsay Workshop and Outlook**

## New BABAR ISR Measurement of $e^+e^- \rightarrow \pi^+\pi^-$

Andrés Pinto

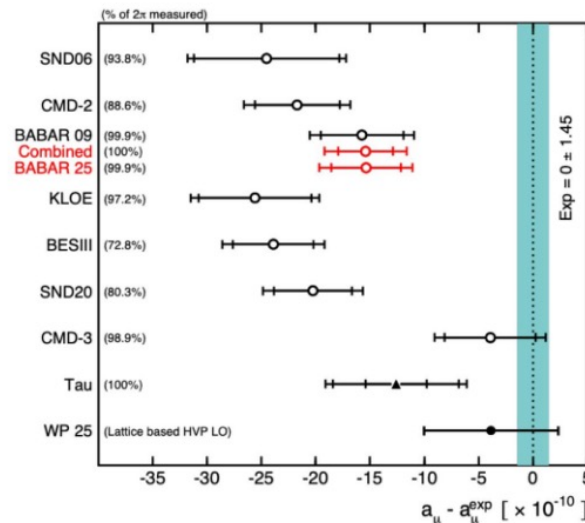
Andreas Pinto @ Orsay

**New analyses :**  
Factor x2 more statistics  
Independent  $\pi - \mu$  separation

- New **blind BaBar analysis** ( $460 \text{ fb}^{-1}$ ) confirms the  $\pi^+\pi^-$  contribution to  $a_\mu$ .
- Independent method (angular fits, no PID) removes dominant 2009 systematic.
- Unblinded  $\mu\mu\gamma$  spectrum agrees with QED, validating the approach.
- $\pi\pi$  cross section consistent with 2009, with **reduced systematics** in 0.5–1.4 GeV.

- Results:
  - Below 0.5 GeV:  $a_\mu^{\pi\pi} = (58.0 \pm 5.5 \text{ (stat.)} \pm 1.7 \text{ (syst.)}) \times 10^{-10}$
  - 0.5–1.4 GeV:  $a_\mu^{\pi\pi} = (456.2 \pm 2.2 \text{ (stat.)} \pm 1.7 \text{ (syst.)}) \times 10^{-10}$
- Robustness shown by excellent agreement with 2009.

- Central region: systematic error 0.37%, statistical error (from fit) similar to 2009 analysis
- Statistical error dominates in threshold region







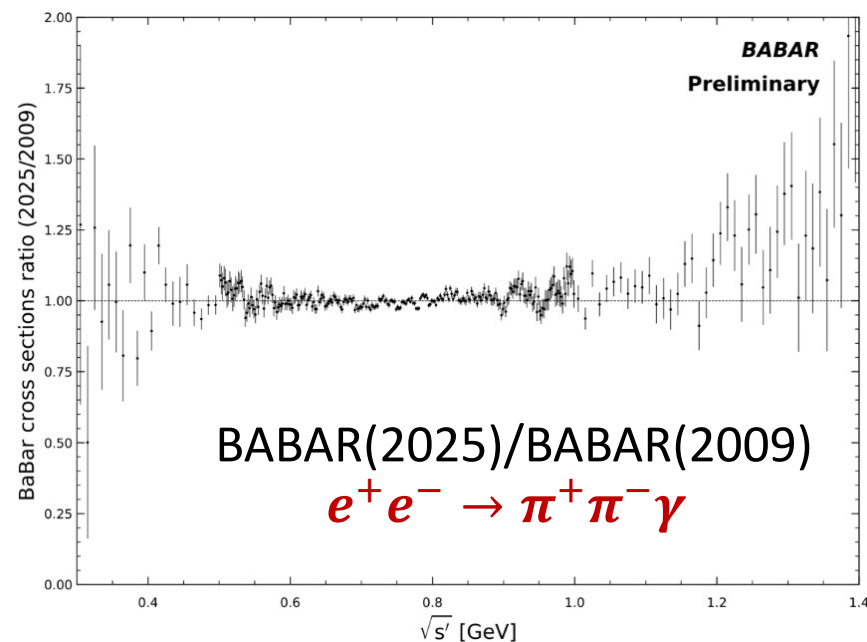
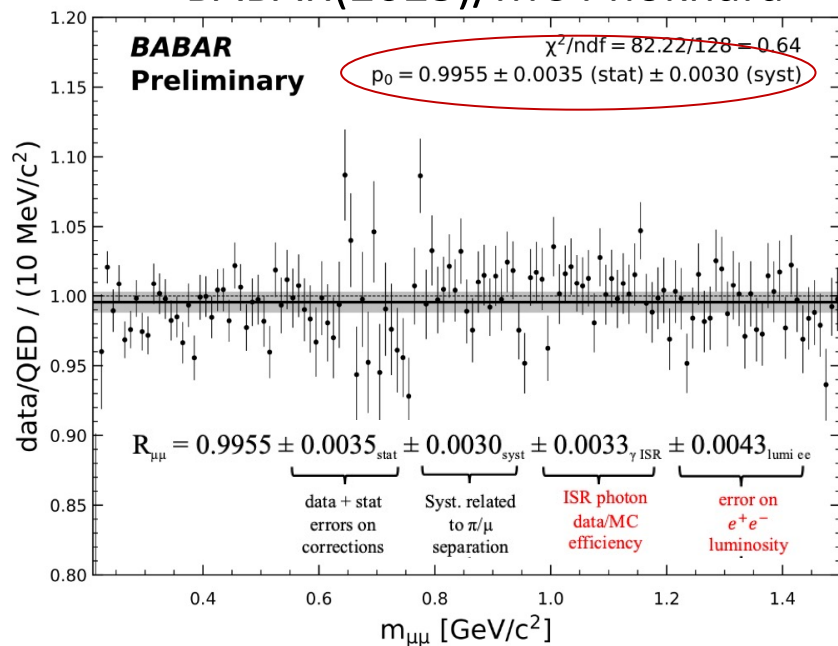
# New BABAR ISR Measurement of $e^+e^- \rightarrow \pi^+\pi^-$

28

Andrés Pinto @ Orsay

$$e^+e^- \rightarrow \mu^+\mu^- \gamma$$

BABAR(2025)/MC Phokhara







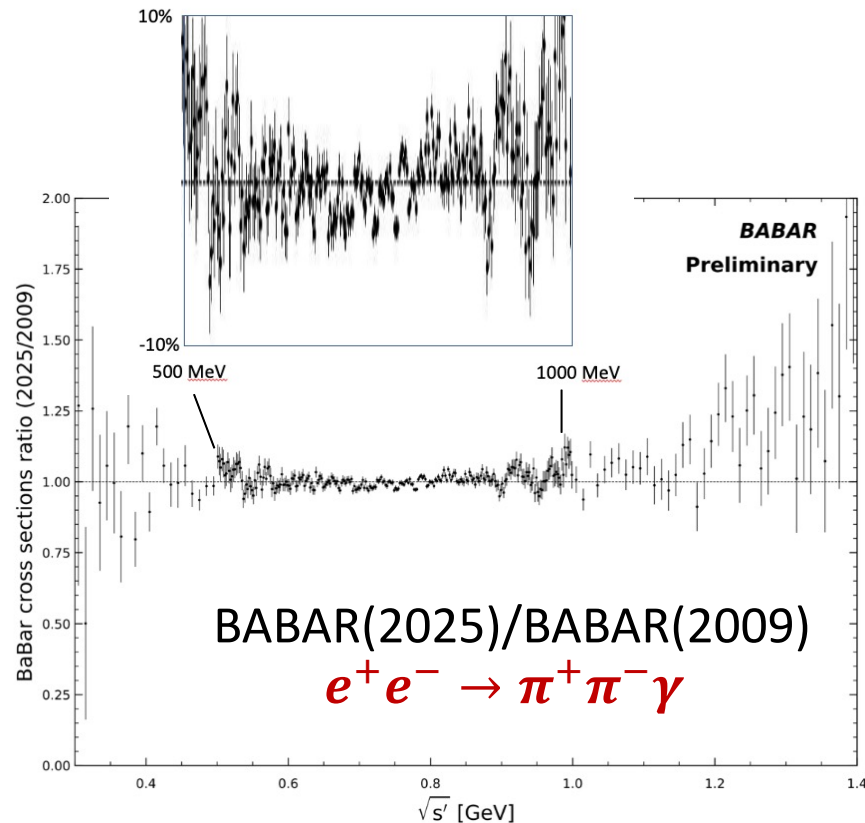
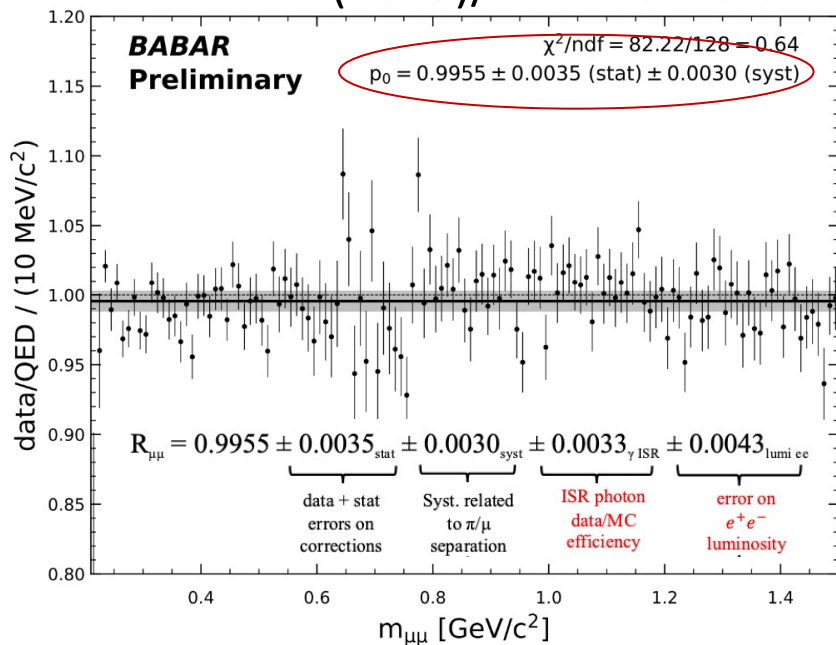
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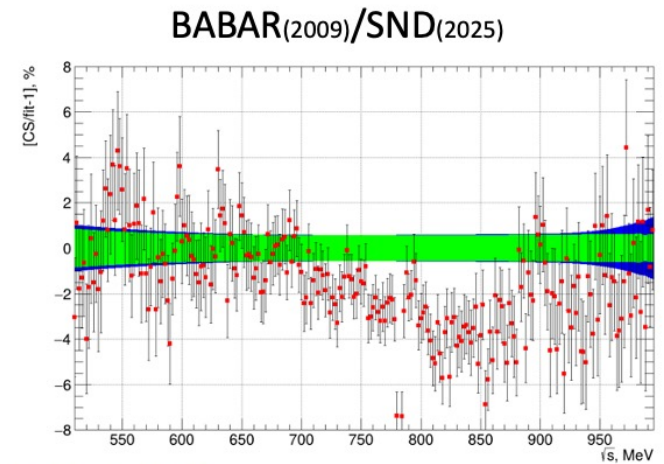
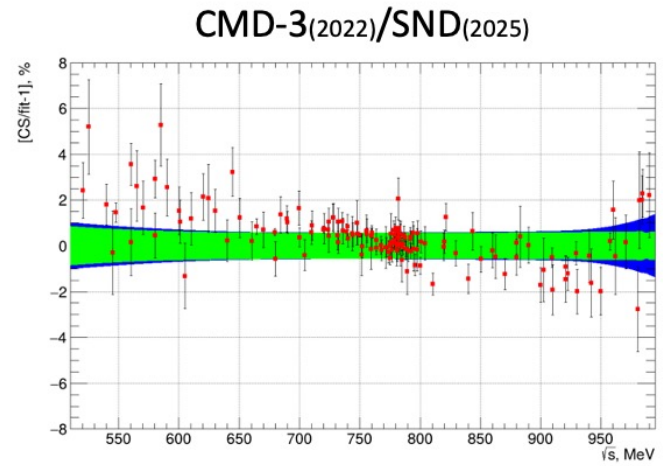


**NEW**

# New SND Measurement of $e^+e^- \rightarrow \pi^+\pi^-$ (energy scan)

30

- New SND analysis based on 90/pb of data collected in 2018 (factor x20 compared to SND20)
- New selection algorithm, systematic uncertainty of 0.7%
  - higher cross section compared to previous analysis (SND20)
  - „ application of the current analysis techniques to (previous) data results in better agreement“
- Cross check on 2% level with 2019 data
- In dispersion integral  $-0.6\sigma$  wrt. CMD-3  $+1.8\sigma$  wrt. BABAR(09)



**-0.6  $\sigma$**

CMD-3:  $a_\mu \times 10^{10} = 433.62 \pm 3.76$

$a_\mu \times 10^{10} = 431.11 \pm 3.52$  vs.

BaBar:  $a_\mu \times 10^{10} = 423.87 \pm 2.06$

**+1.8  $\sigma$**

# Overview Experiments – Past and Future

Experiment	Published Method	Normalization	Separation $\pi - \mu - e$	Future
KLOE	ISR untagged ISR tagged ISR untagged	Luminosity Luminosity $\mu + \mu - \gamma$	Kinematics Track Kinematics Track Kinematics Track	ISR untagged $\mu + \mu - \gamma$ statistics x 7
BABAR	ISR tagged	$\mu + \mu - \gamma$	Particle ID	ISR tagged, separation by polar angle, statistics x 2
BESIII	ISR tagged	Luminosity	Particle ID (ML)	ISR tagged, $\mu + \mu - \gamma$ , statistics x 7, 1C kin. fit
BELLE-II				ISR tagged, $\mu + \mu - \gamma$ , Particle ID
CMD-3	Energy scan	$e + e -$	Kinematics Track Kinematics EMC	overall improvements
SND	Energy scan	$e + e -$	Kinematics EMC	overall improvements ML for $\pi - e$ separation

# Overview Experiments – Past and Future

Experiment	Published Method	Normalization	Separation $\pi - \mu - e$	Future	
KLOE	ISR untagged ISR tagged ISR untagged	Luminosity Luminosity $\mu + \mu - \gamma$	Kinematics Track Kinematics Track Kinematics Track	ISR untagged $\mu + \mu - \gamma$ statistics x 7	0.4%
BABAR	ISR tagged	$\mu + \mu - \gamma$	Particle ID	ISR tagged, separation by polar angle, statistics x 2	0.5%
BESIII	ISR tagged	Luminosity	Particle ID (ML)	ISR tagged, $\mu + \mu - \gamma$ , statistics x 7, 1C kin. fit	0.5%
BELLE-II				ISR tagged, $\mu + \mu - \gamma$ , Particle ID	0.5%
			Kinematics Track Kinematics EMC	overall improvements	0.3%
	energy scan	$e + e -$	Kinematics EMC	overall improvements ML for $\pi - e$ separation	0.7%

**New analyses in preparation:**  
New MC generators, new techniques,  
awareness to (N)NLO issues, ...

# Upcoming new ISR BESIII Measurement of $e^+e^- \rightarrow \pi^+\pi^-$

Existing BESIII tagged ISR result based on 2.9/fb of data at  $\sqrt{s}=3.77$  GeV - 4C kinematic fit  
0.9% systematic uncertainty

sources	Uncertainty (%)
Photon efficiency	0.2
Tracking efficiency	0.3
Pion ANN efficiency	0.2
Pion e-PID efficiency	0.2
Angular acceptance	0.1
Background subtraction	0.1
Unfolding	0.2
FSR correction $\delta_{\text{FSR}}$	0.2
Vacuum polarization correction $\delta_{\text{vac}}$	0.2
Radiator function	0.5
Luminosity $\mathcal{L}_{\text{int}}$	0.5
<b>Sum</b>	<b>0.9</b>

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0.9% systematic uncertainty



First half next year: expect new result!  
adding 3.1/fb of data at  $\sqrt{s}=4.18$  GeV;  
**1C kinematic fit  $\rightarrow$  much less sensitive  
towards MC limitations of rad. corrections,  
some minor additional improvements (0.7%)**

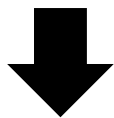
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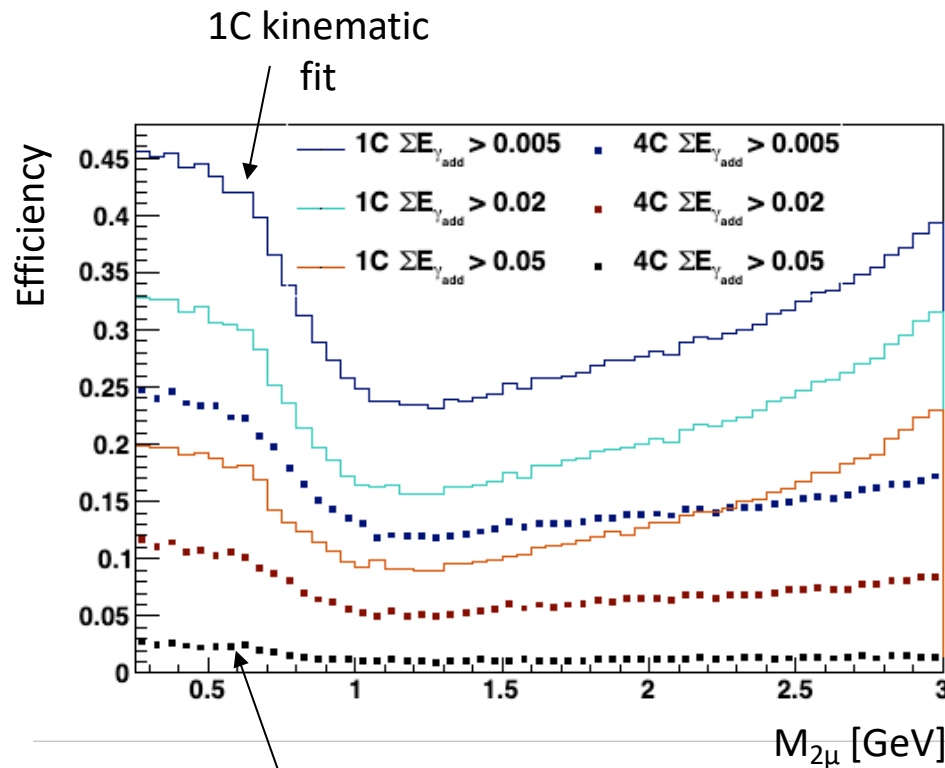
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**1C kinematic fit  $\rightarrow$  much less sensitive  
towards MC limitations of rad. corrections,**  
some minor additional improvements (0.7%))



Next years: final result based on existing  
data set of 20/fb of data at  $\sqrt{s}=3.77$  GeV;  
**1C kinem. fit and normal. to  $\mu\mu\gamma$  (<0.5%)**

sources	Uncertainty (%)
Photon efficiency	0.2 $\rightarrow$ 0.0
Tracking efficiency	0.3 $\rightarrow$ 0.2
Pion ANN efficiency	0.2
Pion e-PID efficiency	0.2 $\rightarrow$ 0.0
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# Upcoming new ISR BESIII Measurement of $e^+e^- \rightarrow \pi^+\pi^-$

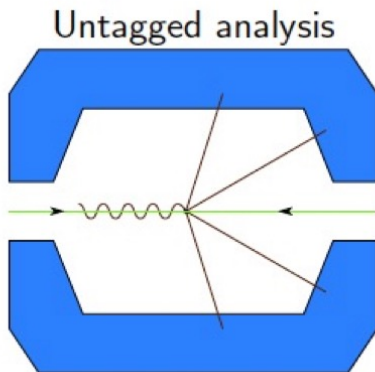


**1C kinematic fit with much (x4)  
improved efficiency for NLO ISR photons  
→ more inclusive for (N)NLO photons**

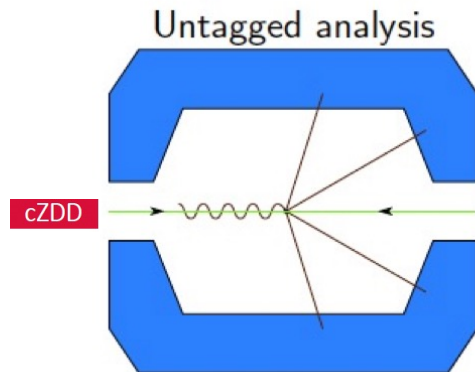
4C kinematic fit (published result)



# *Installation of a Tagging Detector at BESIII: $cZDD$*



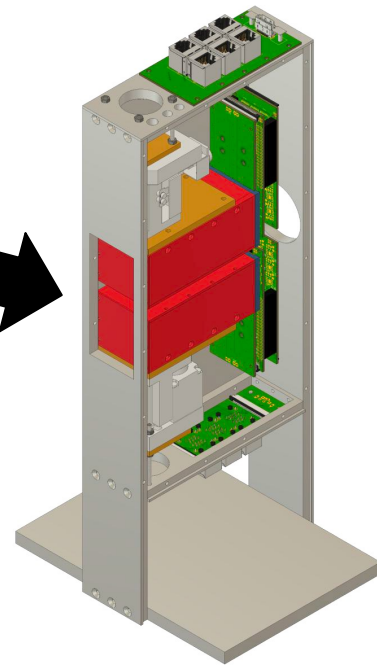
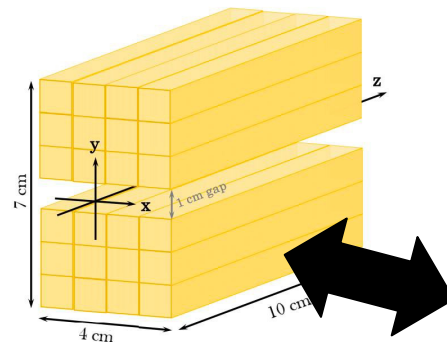
# Installation of a Tagging Detector at BESIII: $cZDD$



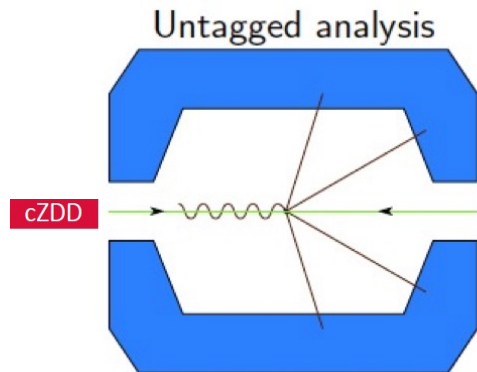
## crystal Zero Degree Detector

$cZDD$

- 2 half detectors with 12 LYSO crystals each (SiPM) (on both sides), retractable
- PANDA sampling ADC for SiPM readout
- can also be used as luminosity detector



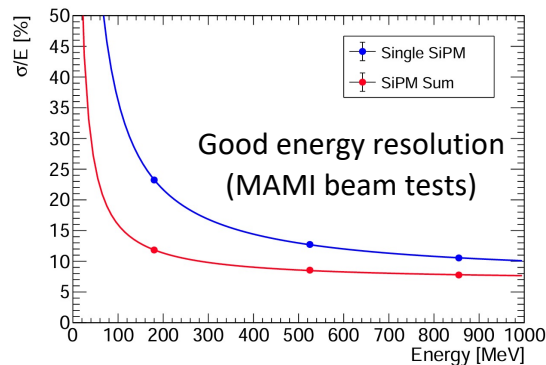
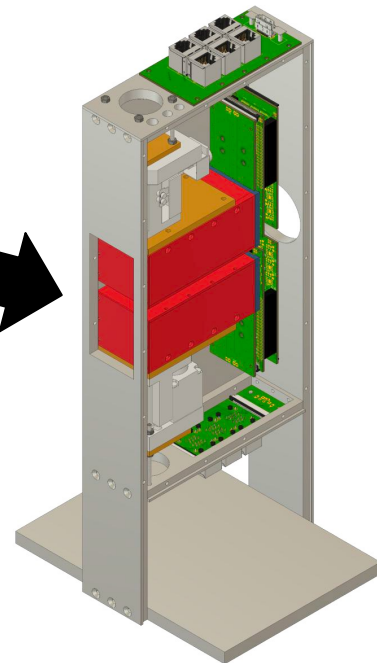
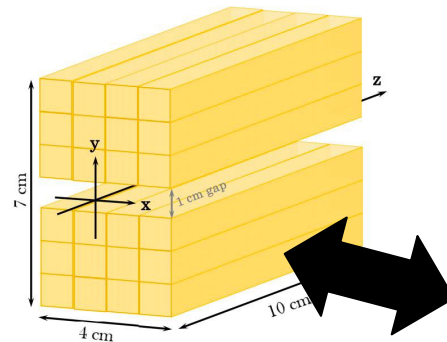
# Installation of a Tagging Detector at BESIII: $cZDD$



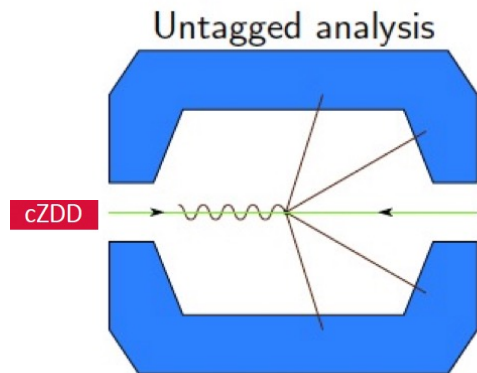
**crystal Zero Degree Detector**

cZDD

2 half detectors with 12  
LYSO crystals each (SiPM)  
(on both sides), retractable  
→ PANDA sampling ADC for SiPM readout  
→ can also be used as luminosity detector



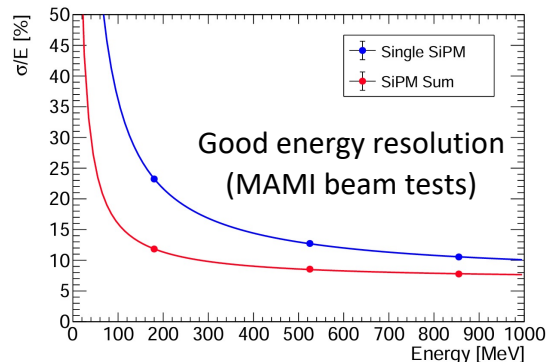
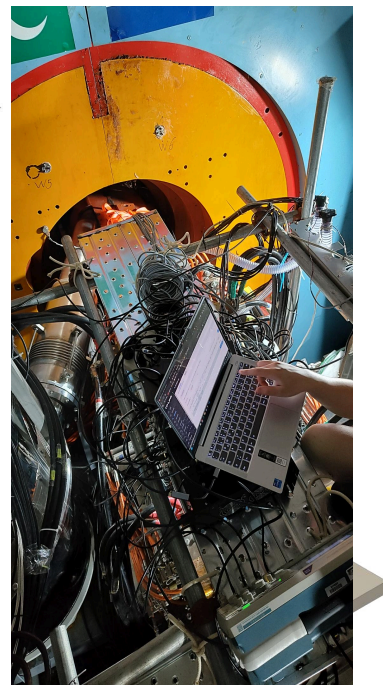
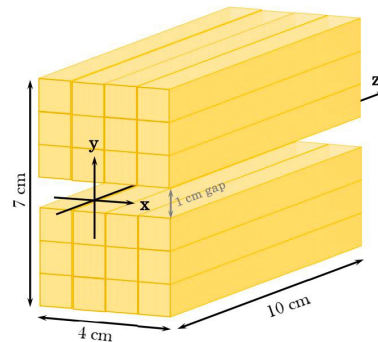
# Installation of a Tagging Detector at BESIII: $cZDD$



## crystal Zero Degree Detector

cZDD

2 half detectors with 12  
LYSO crystals each (SiPM)  
(on both sides), retractable  
→ PANDA sampling ADC for SiPM readout  
→ can also be used as luminosity detector



Installed in BESIII on Sept. 10th

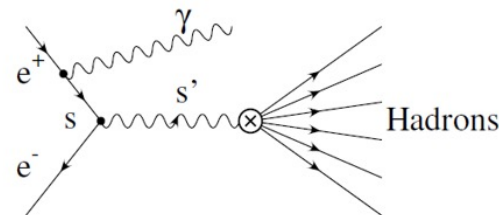
→ cZDD detector will improve our capabilities for ISR physics  
(tagging of ISR photon, background subtraction, ...)



# Conclusions

# Conclusions

- New Lattice as well as CMD-3 results challenging previous  $e^+e^-$  data
  - difference in  $\pi^+\pi^-$  between CMD-3 and other expts. to be understood
  - brand new BABAR data confirms previous result (in conflict with FNAL g-2)
  - will be exciting to see next upcoming new results (BESIII)
- Radiative corrections are a key issue → RadioMonteCarlow initiative!  
Comparison of existing MC codes should be possible shortly (finally!)  
New analysis algorithms designed to be resilient against MC limitations
- Have not covered other hadronic channels beyond  $\pi^+\pi^-$  - puzzles there as well
- Have not covered new inclusive ISR analysis at BESIII (with great potential for BELLE-II!)



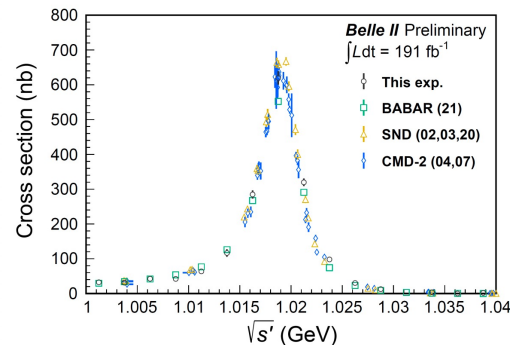
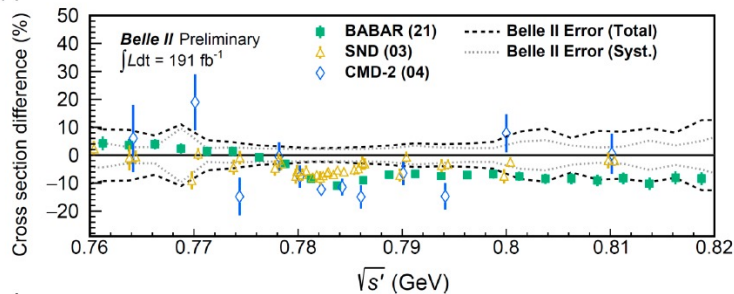
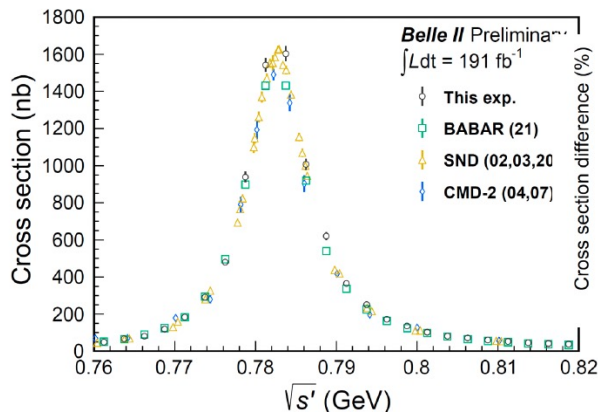
**Thank you !**

# New BELLE-II Analysis of $e^+e^- \rightarrow \pi^+\pi^-\pi^0$

44



- First BELLE-II ISR analysis of hadronic process:  $\pi^+\pi^-\pi^0$  channel, ( $0.62 < \sqrt{s} < 1.8$ ) GeV  
 → systematic uncertainty: >2.2%  
 → integral value higher by 2.5 sigma than BABAR
- Main limitation (~1.2% uncertainty): NLO radiative correction  
 → confirmation of BABAR findings, however with limited consequences



5% ... 10% higher cross section than BABAR in  $\omega$  region





# CMD-3: $e^+e^- \rightarrow K_S K_L$

- Measurement 1.004 – 1.070 GeV
- 1.8% systematic uncertainty (BABAR 2.9%)
- Reconstruction of  $K_S \rightarrow \pi^+ \pi^-$
- Fit to cross section:

$$\sigma_{e^+e^- \rightarrow K_S^0 K_L^0}(s) = \frac{8\pi\alpha}{3s^{5/2}} p_{K^0}^3 \left| \frac{g_{\rho\gamma} g_{\rho KK}}{D_\rho(s)} + \frac{g_{\omega\gamma} g_{\omega KK}}{D_\omega(s)} + \frac{g_{\phi\gamma} g_{\phi KK}}{D_\phi(s)} + A_{\rho', \omega', \phi'} \right|^2$$

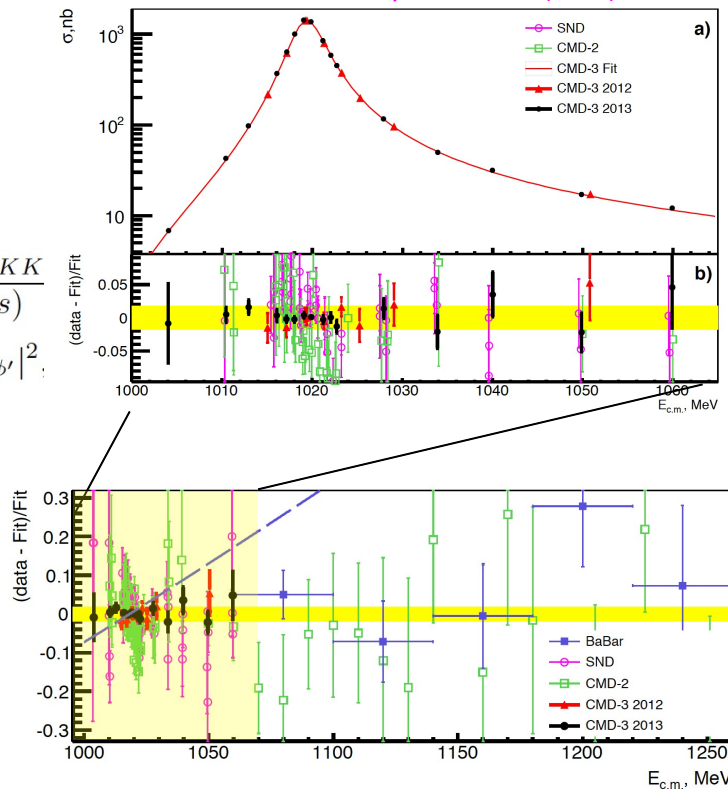
$$|g_{V\gamma}| = \sqrt{\frac{3m_V^3 \Gamma_{Vee}}{4\pi\alpha}}; |g_{VKK}| = \sqrt{\frac{6\pi m_V^2 \Gamma_V B_{VKK}}{p_{K^0}^3(m_V)}}$$

$$D_V(s) = m_V^2 - s - i\sqrt{s}\Gamma_V(s)$$

$$\Gamma_V(s) = \Gamma_V \sum_{V \rightarrow f} B_{V \rightarrow f} \frac{P_{V \rightarrow f}(s)}{P_{V \rightarrow f}(m_V^2)}$$

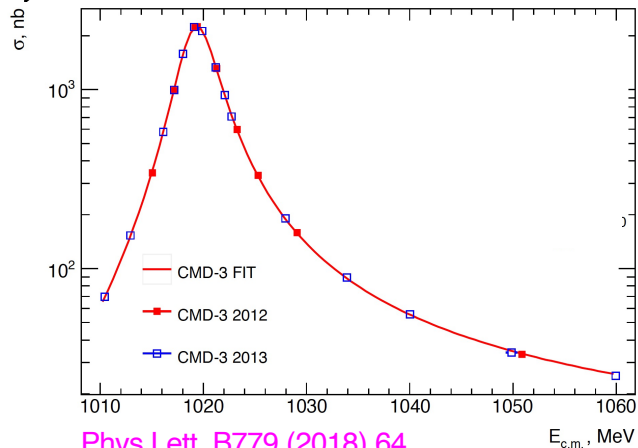
- Overall good agreement

Phys.Lett. B760 (2016) 314



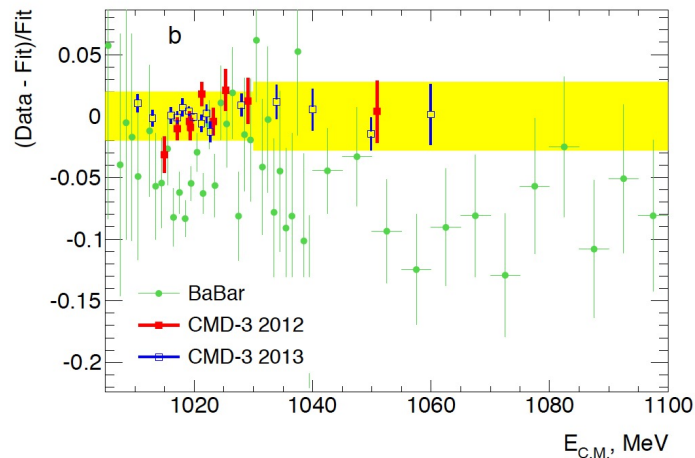
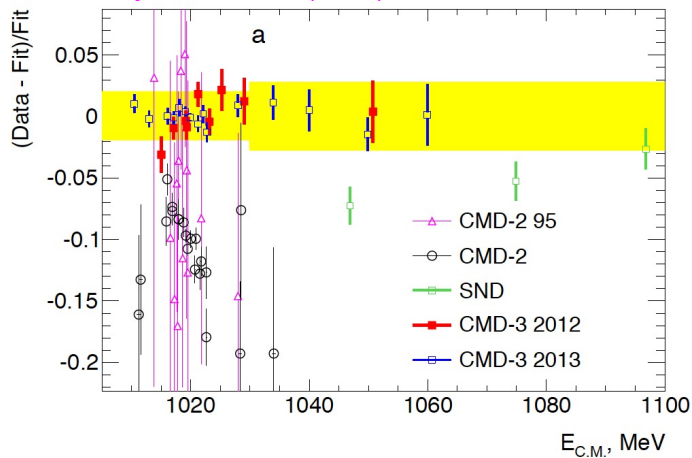


# CMD-3: $e^+e^- \rightarrow K^+K^-$



Phys.Lett. B779 (2018) 64

- Measurement 1.010 – 1.060 GeV
- 2.0% systematic uncertainty (BABAR 0.72 – 1.41 % in that range)
- Similar fit to cross section as for  $K_S K_L$
- Parameters:
- New CMD-3 data above CMD-2 / BABAR ???



# $R_{incl}$ Measurement BESIII (2022)

Phys. Rev. Lett. 128 (2022) 062004

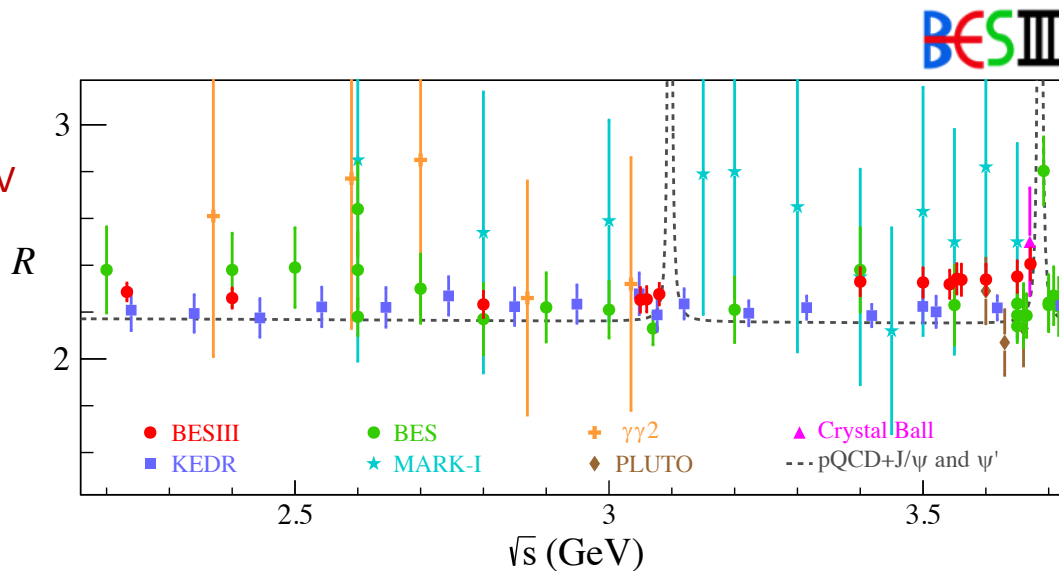
$$R_{\text{had}}(s) = \frac{1}{\sigma_{\mu^+\mu^-}} \cdot \frac{N_{\text{had}} - N_{\text{bkg}}}{\mathcal{L} \cdot \epsilon_{\text{had}} \cdot (1 + \delta)}$$

**Analysis strategy: select all events with  $\geq 2$  tracks**

- Reject back-to-back 2-prong events (Bhabha,  $\mu^+\mu^-$ )
- Remaining background from ISR and QED events subtracted from MC

- Energy range covered:  $2.2 < \sqrt{s} < 3.7$  GeV
- Statistical uncertainty  $< 0.5\%$   
Systematic uncertainty  $< 2.6\%$  below 3.1 GeV  
 $\sim 3.0\%$  above
- Above 3.4 GeV deviation observed with:
  - KEDR/Novosibirsk on the level of  $1.9\sigma$
  - pQCD theory on the level of  $2.7\sigma$

**World's most precise  $R_{incl}$  measurement !**  
**Some deviations from pQCD seen ?!**  
**Much more data will be published shortly !**

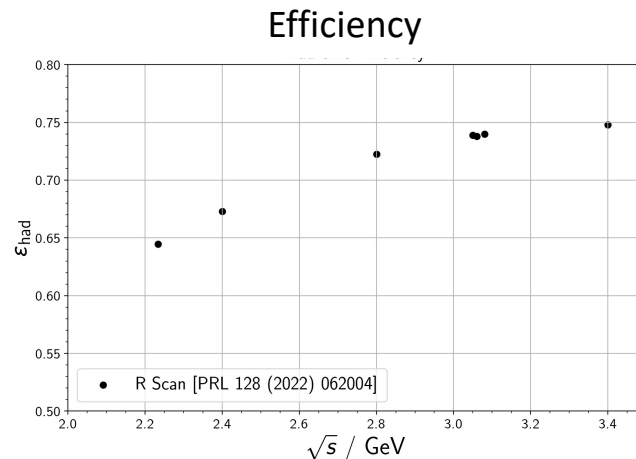


# Messages learnt from Inclusive R Measurement

- Selection requires  $\geq 2$  tracks, which are not back-to-back
- Detector acceptance starts **above  $21^\circ$**

→ For low-multiplicity final hadronic states ( $\pi^+\pi^-$ ,  $\pi^+\pi^-\pi^0$ ,  $\pi^+\pi^-\pi^0\pi^0$ , ...), the probability to be not selected large relatively large

→ Total event efficiency at 60% .... 70% level

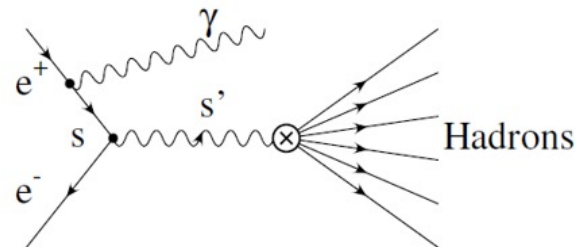


For the determination of the event efficiency, a precise MC generator for  $e^+e^- \rightarrow \text{Hadrons}$  is needed (possible model dependence difficult to estimate)



Inclusive ISR with detection of ISR photon only

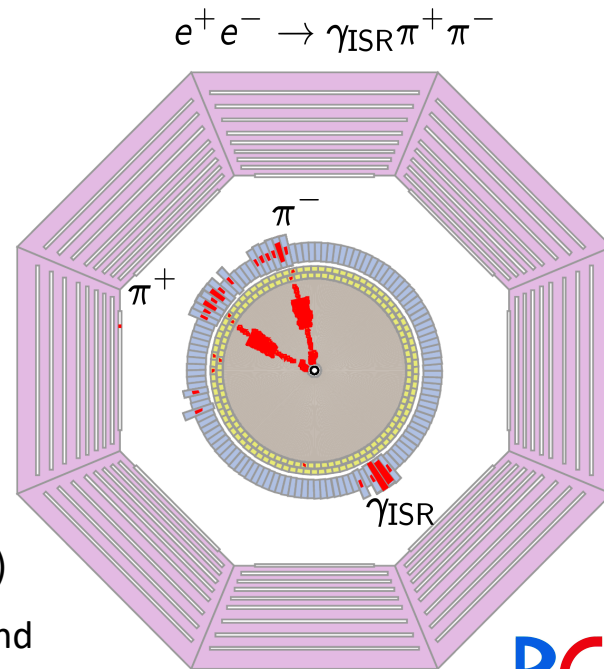
$$s' = m_{\text{had}}^2 = s - 2E_\gamma \sqrt{s}$$



# New Inclusive Approach using ISR

## Event selection:

- **Select 1 high-energetic photon  $> 1.2 \text{ GeV} \equiv \text{ISR photon}$  at large polar angle  $[\cos\Theta_{\text{ISR}}] < 0.8$**   
 → Restricts hadronic mass spectrum  $< 2.7 \text{ GeV}$
- **Require (for time being)  $\geq 1$  charged track in the event**  
 → Does currently not include fully neutral states ( e.g.  $e^+e^- \rightarrow \pi^0\gamma$  )
- ISR boost confines particles into narrow cone  
 → Very high detection efficiency
- Less reliant on description of hadronic MC  
 → ISR description in MC under control
- Single measurement down to threshold (does not need scan)
- Measurement fully inclusive for Final State Radiation (FSR) and higher order corrections of ISR
- In principle able to measure fully neutral channels



**BESIII**

# New Inclusive Approach using ISR: Efficiency

## Event selection:

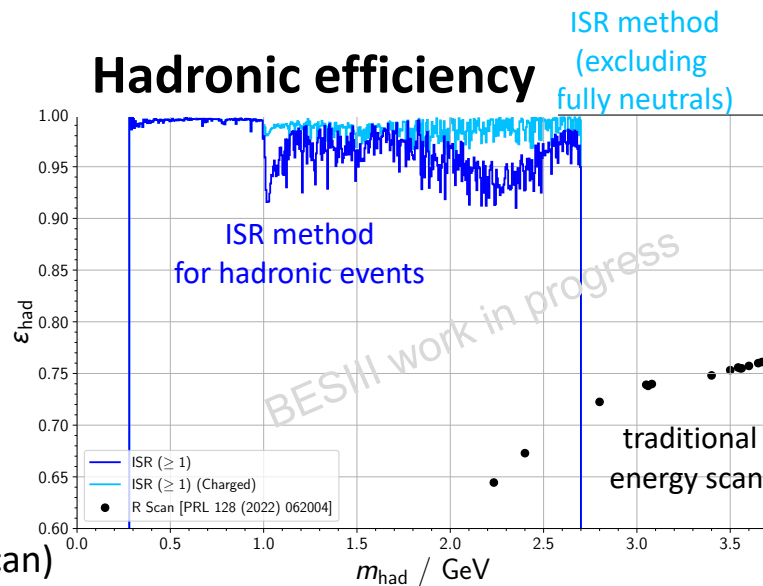
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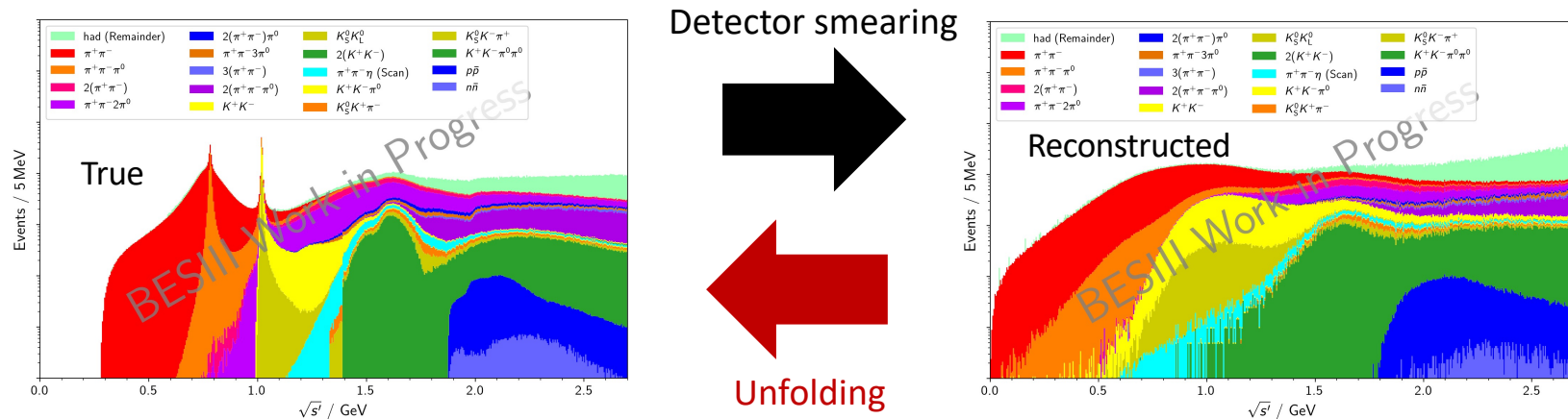
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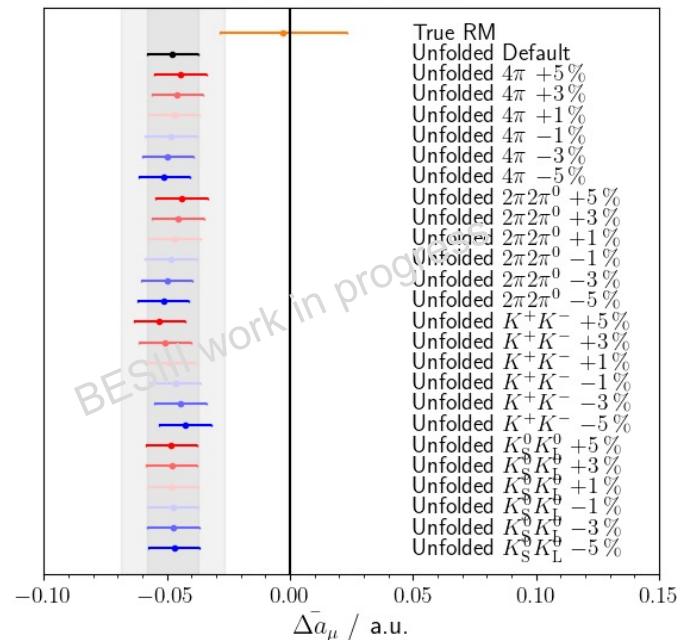
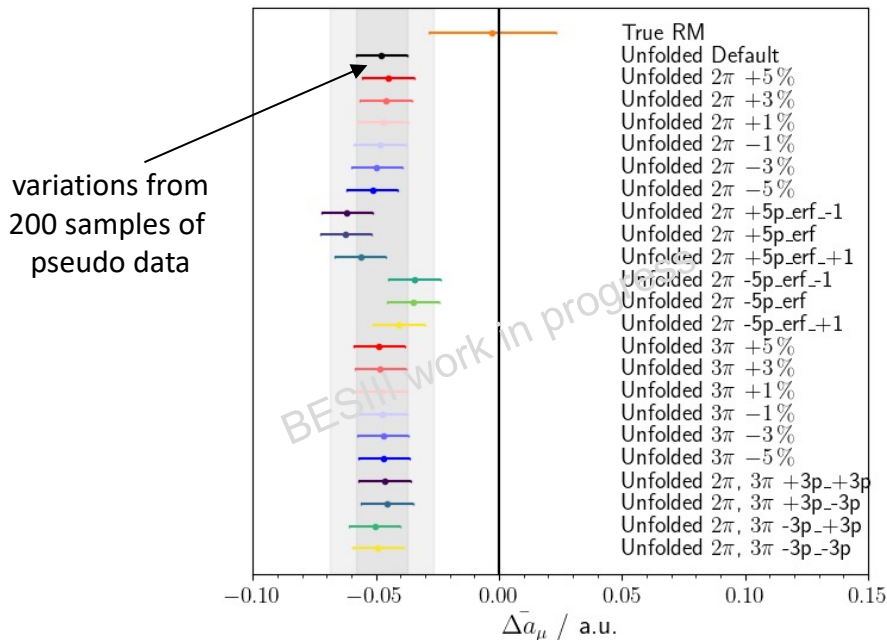
# Unfolding from Detector Mass Resolution



- Large smearing introduced by limited detector resolution
- Application of unfolding algorithms to recover the *true* spectrum
- Requires Monte-Carlo program to construct unfolding matrix – Response Matrix (RM)
- Systematically testing the bias in the unfolding procedure due to wrong input Monte-Carlo Pseudo Data (PD)

# Unfolding from Detector Mass Resolution

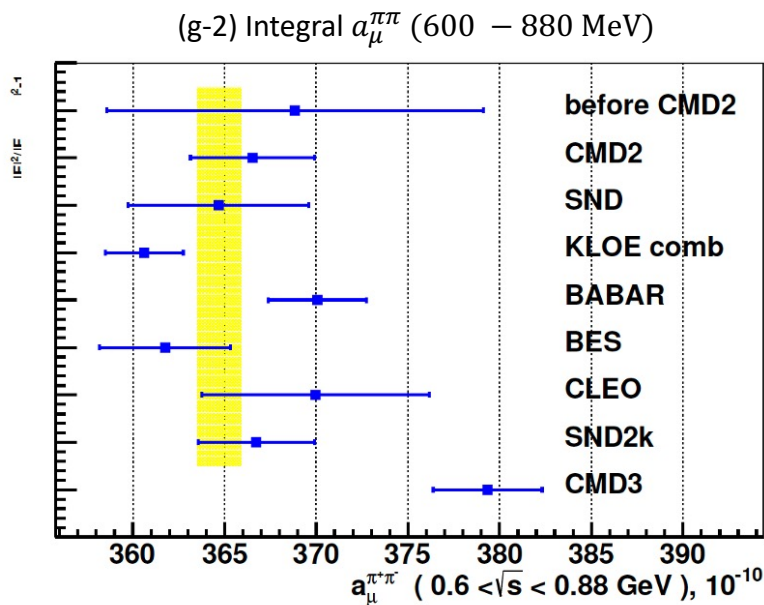
- More than 50 cross section variations in input MC tested (e.g. up to  $\pm 5\%$  variation of  $2\pi$  cross section)  
**→ Very stable result for unfolded spectrum → variation well within percent level (=precision goal)**



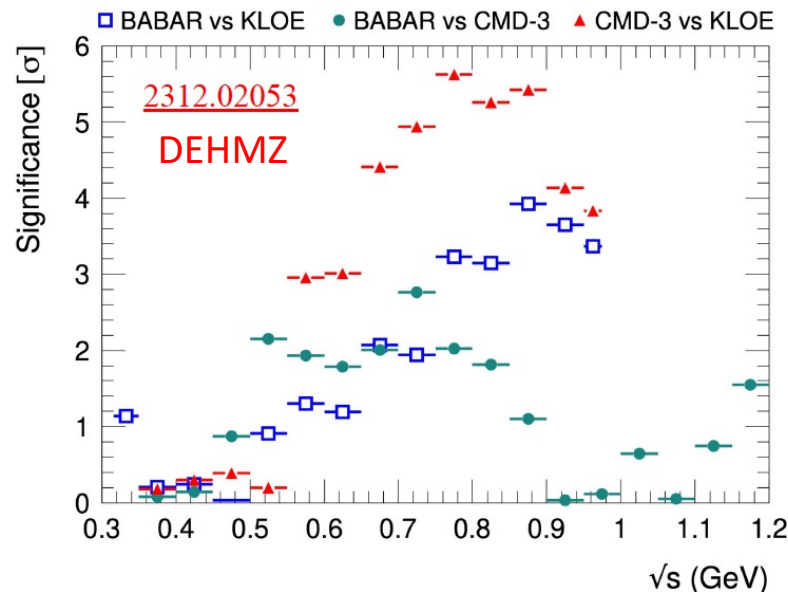
- With larger data sets also conversion events might be used to significantly improve mass resolution**



# CMD-3 Compatibility with other Experiments for HVP Integral

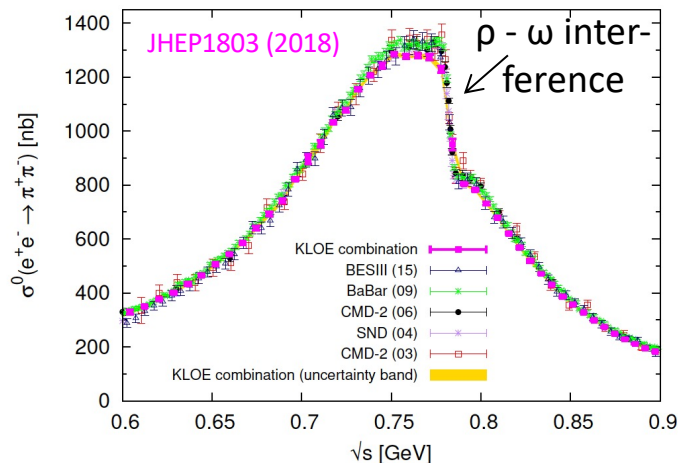


Deviation between data sets (in statistical significance)



→ Significant deviation from previous ISR and energy scan experiments (CMD-2)! Why?

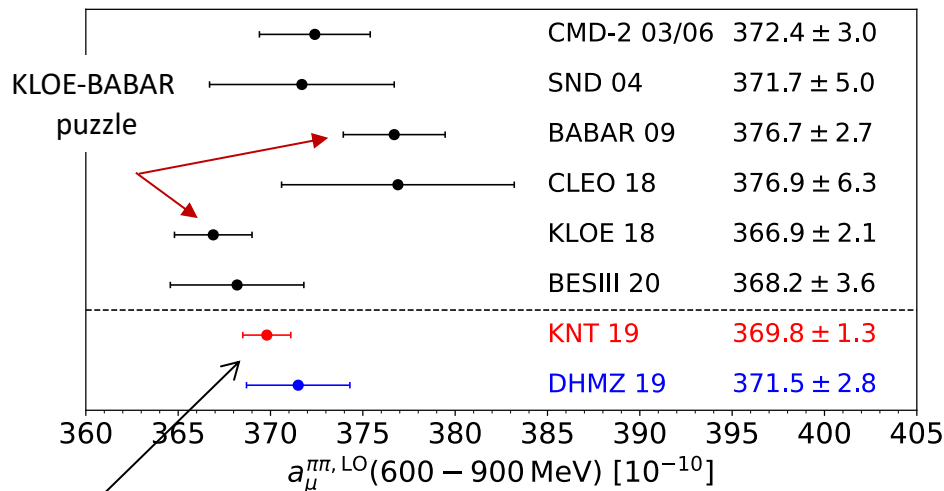
# Most relevant Channel: $e^+e^- \rightarrow \pi^+\pi^-$ (until 2023)



## Systematic Uncertainties on $\rho(770)$ peak

- ISR BABAR 0.5%
- ISR KLOE 0.6%
- ISR BESIII 0.9%
- Energy Scan CMD-2 0.8%\*

\* limited in addition by statistics



## Most recent evaluations of HVP:

- Davier, Höcker, Malaescu, Zhang (DHMZ)
  - averaging via 2<sup>nd</sup> ord. polynomial interpolation
  - systematic correlat. propagated via pseudo-data (MC)
- Keshavarzi, Nomura, Teubner (KNT)
  - data subjected to a clustering procedure
  - fit over all data sets taking into account correlations

# 2020 Whitepaper Estimate of HVP

Merging of **KNT**, **DHMZ** estimate with **ChPT/dispersive fits**: **CHHKs** for  $2\pi$ ,  $3\pi$  channels;

**Big debate up to 2023:**  
Who is right? KLOE or BABAR?

	DHMZ19	KNT19	Difference
$\pi^0\gamma$	507.85(0.83)(3.23)(0.55)	504.23(1.90)	3.62 :-)
	46.21(0.40)(1.10)(0.86)	46.63(94)	-0.42
	13.68(0.03)(0.27)(0.14)	13.99(19)	-0.31
	18.03(0.06)(0.48)(0.26)	18.15(74)	-0.12
	23.08(0.20)(0.33)(0.21)	23.00(22)	0.08
	12.82(0.06)(0.18)(0.15)	13.04(19)	-0.22
	4.41(0.06)(0.04)(0.07)	4.58(10)	-0.17
Sum of the above	626.08(0.95)(3.48)(1.47)	623.62(2.27)	2.46
[1.8, 3.7] GeV (without $c\bar{c}$ )	33.45(71)	34.45(56)	-1.00
$J/\psi, \psi(2S)$	7.76(12)	7.84(19)	-0.08
[3.7, $\infty$ ) GeV	17.15(31)	16.95(19)	0.20
Total $a_\mu^{\text{HVP, LO}}$	694.0(1.0)(3.5)(1.6)(0.1) $_{\psi(0.7)\text{D}+\text{QCD}}$	692.8(2.4)	1.2 reasonable agreement

$$\rightarrow a_\mu^{\text{HVP, LO}} = 693.1(2.8)_{\text{exp}}(2.8)_{\text{syst}}(0.7)_{\text{pQCD}} = 693.1(4.0) \times 10^{-10} \text{ Whitepaper estimate}$$

experimental uncertainties:  
dominated by  $2\pi$  uncertainty

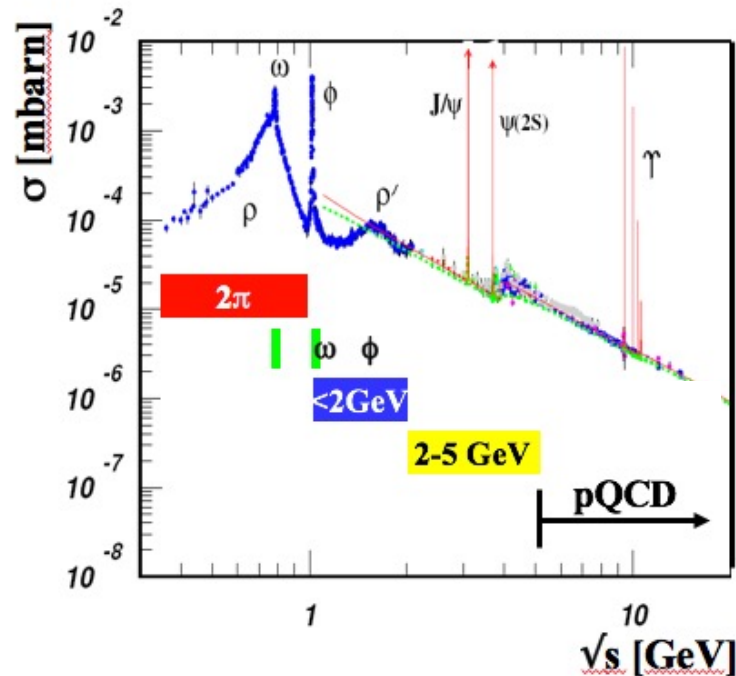
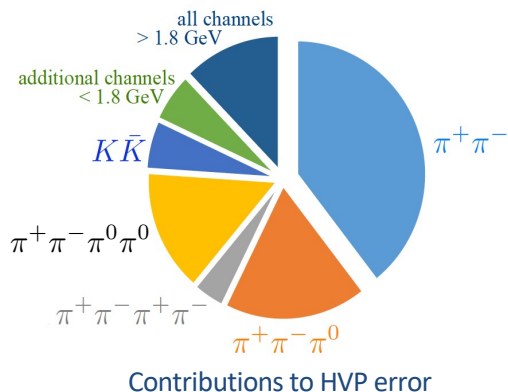
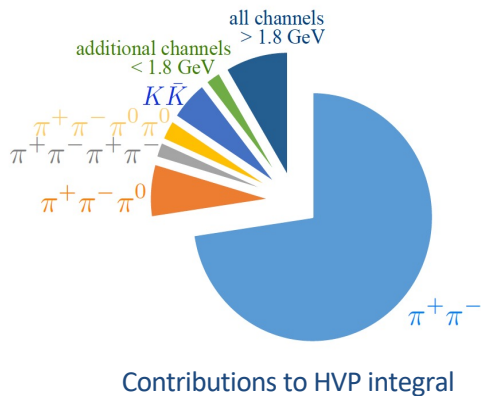
KLOE/BABAR tension:  
leaving out KLOE or  
BABAR, respectively

energy region [1.8;3.7] GeV; usage of pQCD by  
DHMZ, while KNT follows data-driven approach

# Hadronic Vacuum Polarization Contribution to $(g-2)_\mu$

## Anomalous magnetic moment of the muon $(g-2)_\mu$

$$a_\mu^{HVP} = \frac{1}{4\pi^3} \int_{4m_\pi^2}^{\infty} ds K(s) \sigma_{\text{had}}(s)$$



# Overview Experiments – Past and Future

Experiment	Published Method	Normalization	Separation $\pi - \mu - e$	Future	
KLOE	ISR untagged ISR tagged ISR untagged	Luminosity Luminosity $\mu + \mu - \gamma$	Kinematics Track Kinematics Track Kinematics Track	ISR untagged $\mu + \mu - \gamma$ statistics x 7	0.4%
BABAR	ISR tagged	$\mu + \mu - \gamma$	Particle ID	ISR tagged, separation by polar angle, statistics x 2	<0.5%
BESIII	ISR tagged	Luminosity	Particle ID (ML)	ISR tagged, $\mu + \mu - \gamma$ , statistics x 7, 1C kin. fit	0.5%
BELLE-II				ISR tagged, $\mu + \mu - \gamma$ , Particle ID	0.5%
			Kinematics Track Kinematics EMC	overall improvements	0.3%
	energy scan	$e + e -$	Kinematics EMC	overall improvements ML for $\pi - e$ separation	0.6%

**New analyses in preparation:**  
New MC generators, new techniques,  
awareness to (N)NLO issues, ...



- **BESIII  $\pi^+\pi^-$**  ( $600 < \sqrt{s} < 900$ ) MeV, update of covariance matrix  $\rightarrow$  central value unchanged
- Energy scan measurements above 2 GeV of multi-hadronic channels (spectroscopy)
- **Total hadronic cross section** measurement above 2 GeV



- New SND scans of  **$\pi^+\pi^-4\pi^0$  above 1 GeV ( $> 3\%$  uncertainty)**
- New **SND scan of  $\pi^+\pi^-$**  channel, ( $525 < \sqrt{s} < 883$ ) MeV  
 $\rightarrow$  systematic uncertainty  $> 600$  MeV: 0.8%; after publications issues found



- New **BABAR ISR data on  $\pi^+\pi^-4\pi^0$ ,  $2(\pi^+\pi^-)3\pi^0$ ,  $KK\pi\pi\pi$**
- New **BABAR ISR analysis of  $\pi^+\pi^-\pi^0$  channel**, ( $0.62 < \sqrt{s} < 3.5$ ) GeV  
 $\rightarrow$  systematic uncertainty:  $> 1.3\%$   
 $\rightarrow$  fit to  $M_{3\pi}$  including  $\omega(782)$ ,  $\omega(1420)$ ,  $\omega(1680)$ ,  $\phi(1020)$ ,  $\rho(770)$



- First **BELLE-II ISR analysis of hadronic process:  $\pi^+\pi^-\pi^0$  channel**, ( $0.62 < \sqrt{s} < 1.8$ ) GeV  
 $\rightarrow$  systematic uncertainty:  $> 2.2\%$   
 $\rightarrow$  integral value higher by 2.5 sigma than BABAR
- Main limitation ( $\sim 1.2\%$  error): NLO rad. correction  $\rightarrow$  confirmation of BABAR findings

# Inclusive R Measurement

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Above cms energies of  $\sim 2$  GeV inclusive measurement of  $R_{\text{had}}$   
(large QED background below, low multiplicities)

Master formula:

$$R_{\text{had}}(s) = \frac{1}{\sigma_{\mu^+\mu^-}} \cdot \frac{N_{\text{had}} - N_{\text{bkg}}}{\mathcal{L} \cdot \epsilon_{\text{had}} \cdot (1 + \delta)}$$

## CMS Energy

- 14 points
- 2.2 GeV to 3.7 GeV
- $> 10^5$  had. events

## Luminosity

Determined with large angle Bhabha scattering

## Efficiency

Ratio of generated and reconstructed events from Monte-Carlo

## Background Contributions

- Evaluated with MC:
  - BabaYaga@NLO, Phokhara, KKMC  
 $e^+e^- \rightarrow e^+e^-, \mu^+\mu^-, \gamma\gamma, \tau^+\tau^-$
  - BdkRC, Diag36, Galuga, Ekhar  
 $e^+e^- \rightarrow e^+e^-X$
- Beam related background

## Radiative Corrections

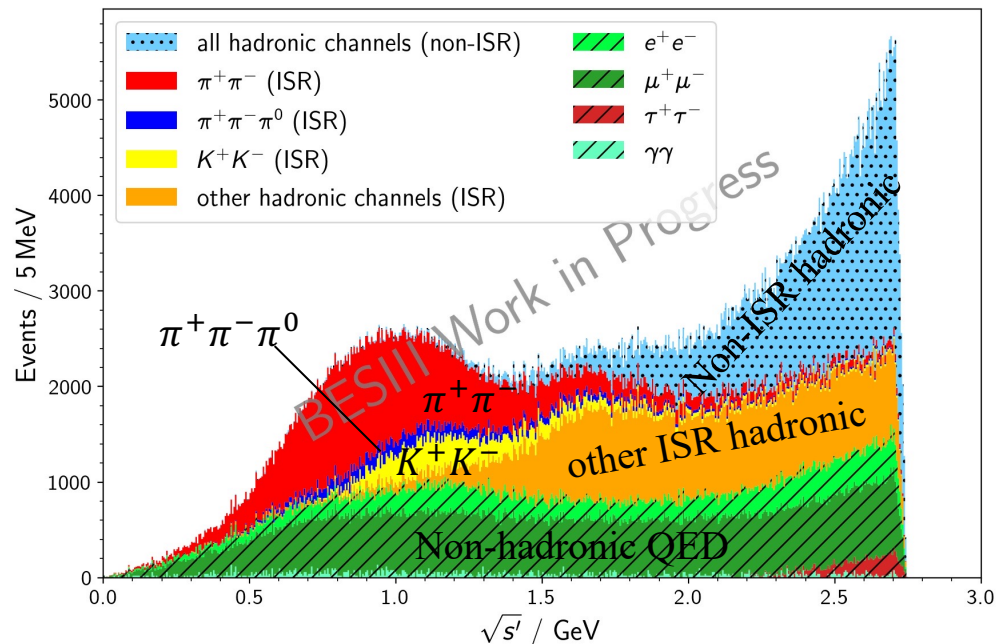
- Two schemes tested
  - Feynman diagram
  - Structure functions
- Agreement within 1.2 %

**Analysis strategy: select all events with  $\geq 2$  tracks**

- Reject back-to-back 2-prong events (Bhabha, Di-Muons)
- Remaining background from ISR and QED events ( $e^+e^- \rightarrow e^+e^- / \mu^+\mu^-$ ) subtracted from MC

# Hadronic Mass Spectrum

## Mass spectrum after application of PID and meson veto



- Plots for  $\sqrt{s} = 4.180$  GeV (3.1 / fb)
- No additional cuts using Muon Detector or other selection cuts

- Significant yield of hadronic events over QED background; hadronic non-ISR event yield small < 1.5 GeV
- However ... due to limited energy resolution of ISR photon, huge smearing effects (no  $\rho$ ,  $\omega$ ,  $\phi$  visible)



# Improve Mass Resolution by using Photon Conversion Events

- Utilize conversion of ISR photon in detector material, especially the beam pipe

Reduction of statistics

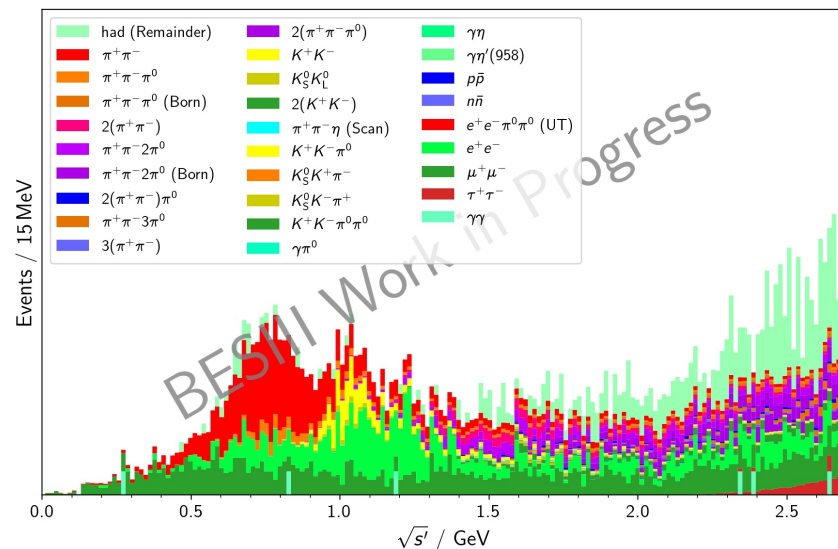
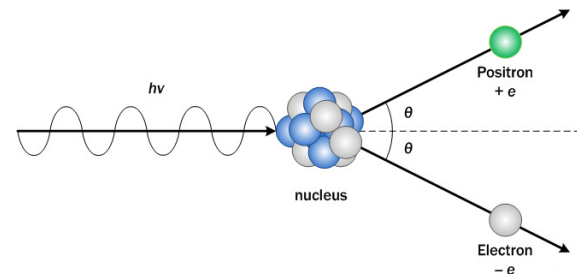
- Tracks of produced  $e^+e^-$  pair to be reconstructed in the MDC

- Improvement of mass resolution by large factors

→ Narrow resonances now separately visible

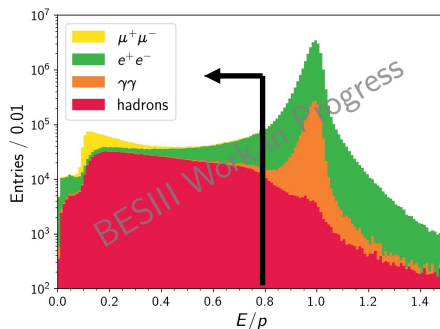
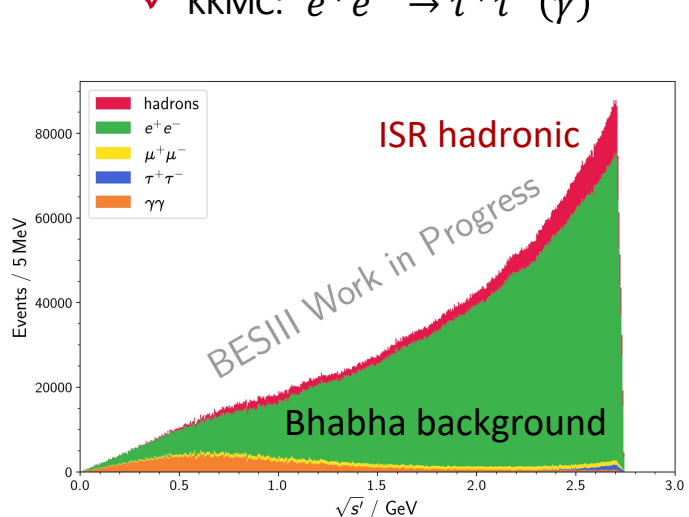
- High potential for the new high-statistics data sets at BESIII, especially the 20/fb data sample being currently collected

→ allows for cross checks between different analysis approaches

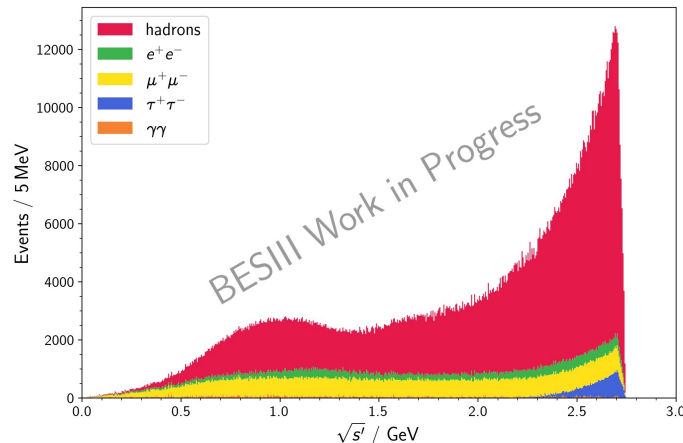


# Challenge 1: Subtraction of QED Background

- Apply dedicated PID cuts, e.g.  $E_{EMC} / |\vec{p}|$
- Subtract remaining QED events using MC simulation  $\rightarrow$  High precision QED MC needed
  - Babar@NLO  $\sim 0.1\%$ :  $e^+e^- \rightarrow e^+e^-(\gamma), \gamma\gamma(\gamma)$
  - Phokhara  $\sim 0.5\%$ :  $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$
  - KKMC:  $e^+e^- \rightarrow \tau^+\tau^-(\gamma)$

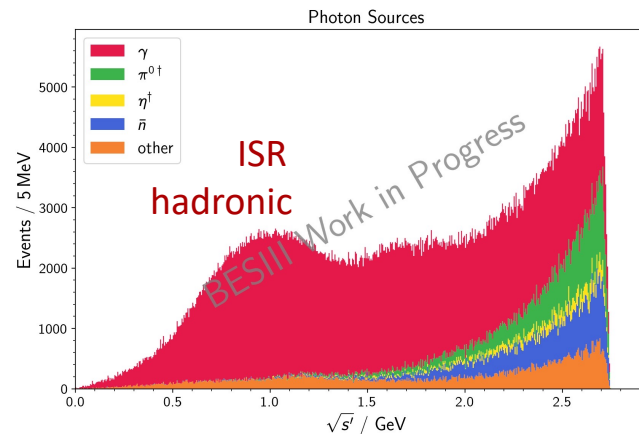
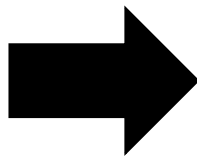
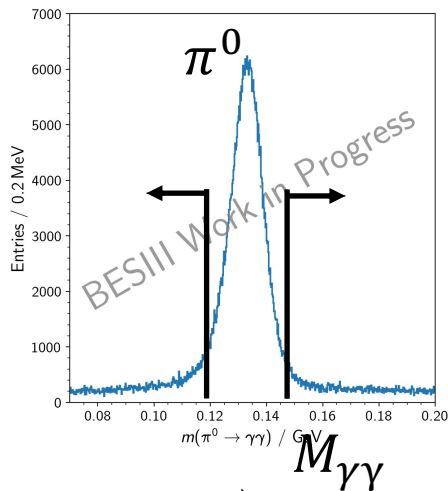
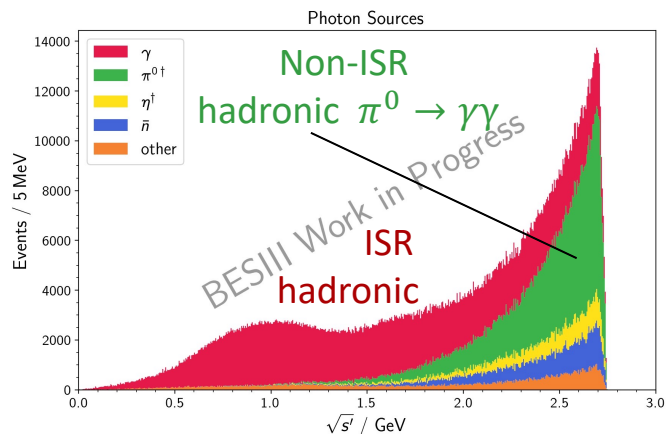


Dramatic reduction of Bhabha background



# Challenge 2: Subtraction of Hadronic Non-ISR Events

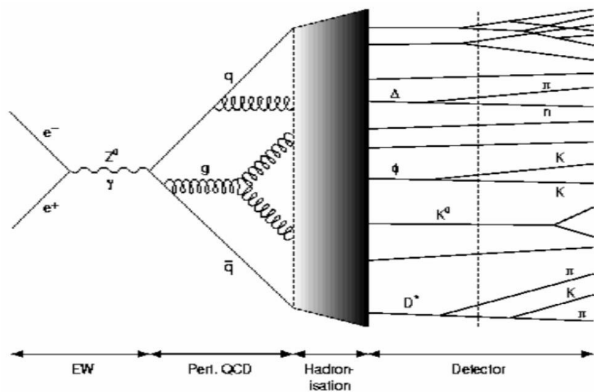
- Very asymmetric two-photon decays of  $\pi^0$  mesons,  $\pi^0 \rightarrow \gamma\gamma$ , can produce high-energetic photons
- Veto events, in which  $\gamma\gamma$  invariant masses peaks around the  $\pi^0$ ,  $\eta$ ,  $\eta'$  mass



# Two independent inclusive Monte-Carlo Generators

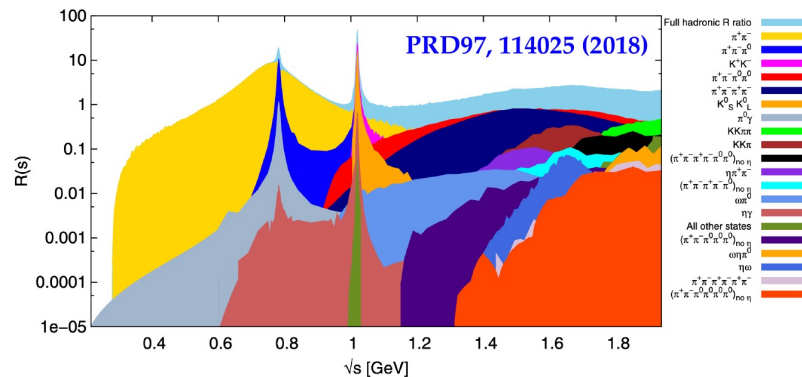
## Fully theoretical MC production

- Development based on Jetset for low-energy experiments (LundAreaLaw)
- Simulation of resonances and continuum
- ISR and vacuum polarization implemented
- Kinematics of final hadrons tuned by experimental distributions ( $N_{\text{trk}}$ ,  $N_\gamma$ ,  $\cos\Theta$ , ...)



## MC generator almost entirely based on exptl. data

- PHOKHARA** event generator (10 low-multiplicity channels  $2\pi$ ,  $3\pi$ ,  $4\pi$ ,  $N\bar{N}$ , ...) fitted to exptl. data
- CONEXC** based purely on exptl. data (phase space), 47 channels



- Remaining channels simulated by **LUARLW**

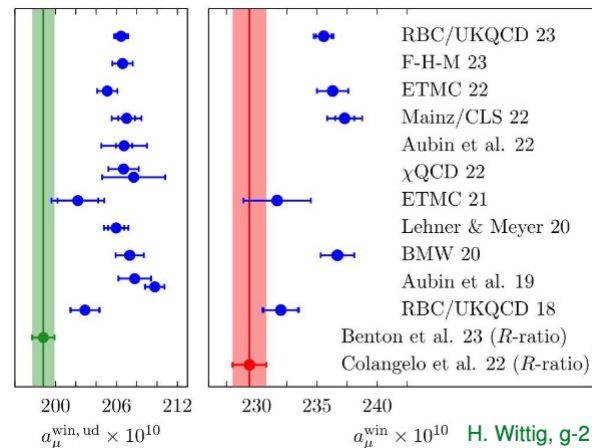


After years of developments, tuning, and cross checks a deviation of better than 2.3% (including ISR) between the hybrid generator and LUARLW is found (major achievement)

# Lattice QCD Windows Estimates

Serious deviation between data-driven evaluation of  $a_\mu^{HVP}$  and intermediate-distance Lattice-QCD window

- weight function allows to relate Lattice-QCD window to total hadronic cross section
- weight function peaked at  $\sim 1.5$  GeV
- ca. 1/3 of total  $a_\mu^{HVP}$ , of which 60% given by  $\pi^+\pi^-$
- selects  $\sim 28\%$  of absolute  $\pi^+\pi^-$  contribution
- need to explain deviation of  $7 \dots 8 \times 10^{-10}$



H. Wittig, g-2 TI Workshop

Explanation 1: Upscale  $\pi^+\pi^-$  data by  $>5\%$  (flat), however this causes some conflict with BMW result for full  $a_\mu^{HVP}$

Explanation 2: Underestimated contributions  $> 1$  GeV (higher multipl.), however would need to be large effect; hadronic particle not being observed by experiment, e.g. Sexaquark? [arxiv:2206.13460](https://arxiv.org/abs/2206.13460)

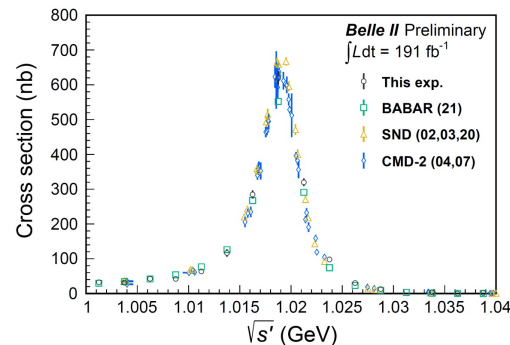
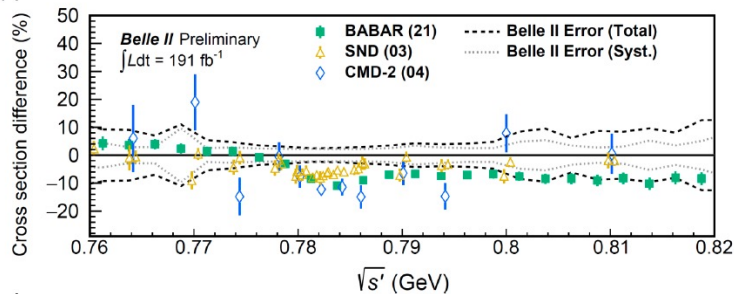
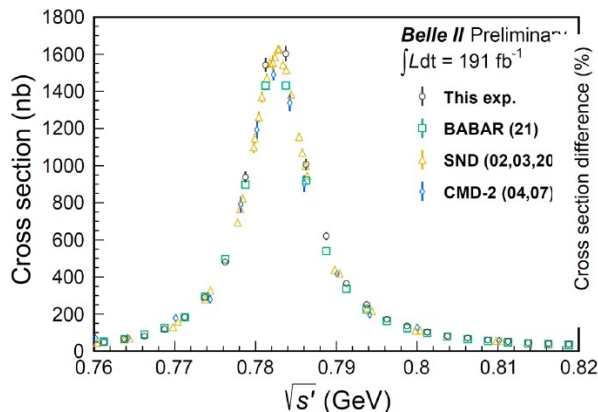
Explanation 3: Common systematic effect in Lattice-QCD and/or underestimated BMW21 result for full  $a_\mu^{HVP}$

# New BELLE-II Analysis of $e^+e^- \rightarrow \pi^+\pi^-\pi^0$

66



- First BELLE-II ISR analysis of hadronic process:  $\pi^+\pi^-\pi^0$  channel, ( $0.62 < \sqrt{s} < 1.8$ ) GeV  
 → systematic uncertainty: >2.2%  
 → integral value higher by 2.5 sigma than BABAR
- Main limitation (~1.2% uncertainty): NLO radiative correction  
 → confirmation of BABAR findings, however with limited consequences



5% ... 10% higher cross section than BABAR in  $\omega$  region

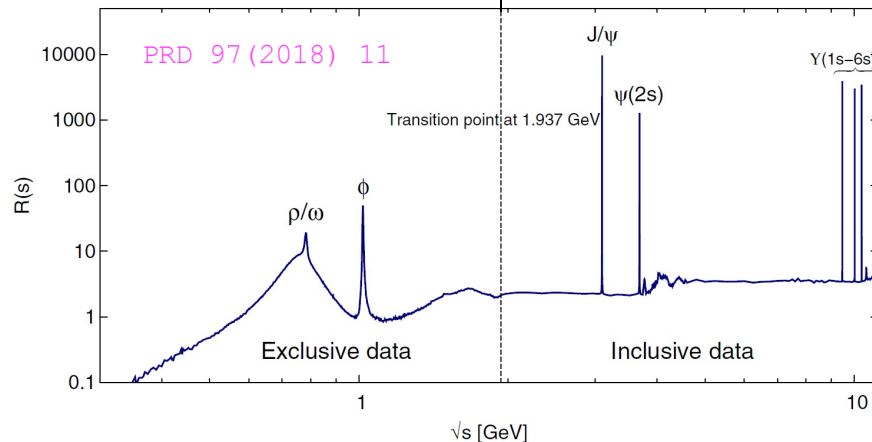
# Measurements on $R$ – Exclusive vs. Inclusive

## Exclusive measurements (<2 GeV)

- Individually highly precise
- Energy scan or initial state radiation
- Large number of channels at higher energies
- Sum over multiple channels

## Inclusive measurements (>2 GeV)

- Covers all possible channels
- Reliant on good Monte Carlo generator
- Only energy scan measurements
- Subtract QED background

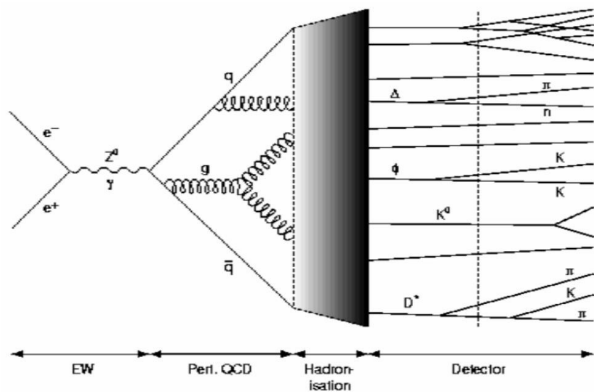


Some tension with KEDR data in the transition region around 2 GeV

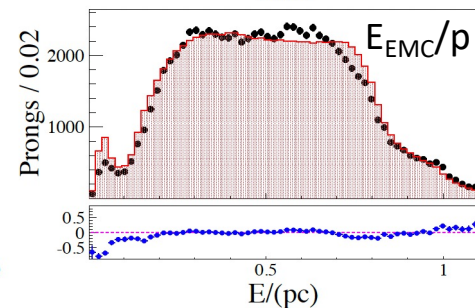
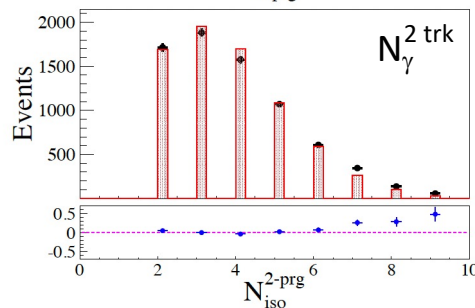
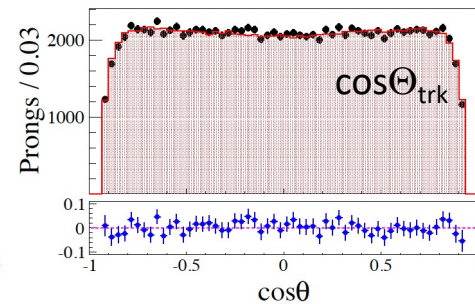
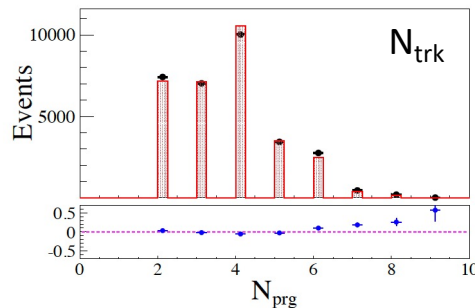
# Inclusive Monte-Carlo Production LUARLW

## Fully theoretical MC production

- Development based on Jetset for low-energy experiments (LundAreaLaw)
- Simulation of resonances and continuum
- ISR and vacuum polarization implemented
- Kinematics of final hadrons tuned by experimental distributions



- Data
- ▨ LUARLW Monte Carlo

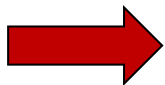
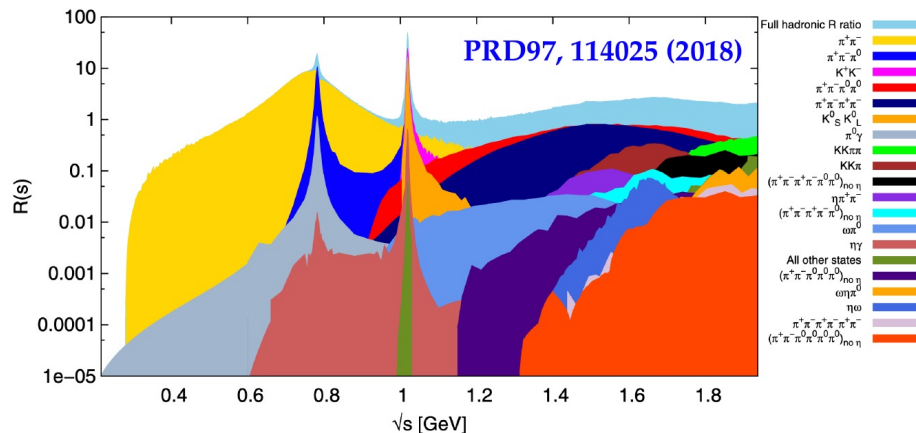




# Hybrid Monte-Carlo Generator

## MC generator based on experimental data (as much as possible)

- PHOKHARA event generator (10 low-multiplicity channels  $2\pi$ ,  $3\pi$ ,  $4\pi$ ,  $N\bar{N}$ , ...) fitted to exptl. data
- CONEXC based purely on exptl. data (phase space), 47 channels
- Remaining channels simulated by LUARLW



After years of developments, tuning, and cross checks a deviation of better than 2.3% (including ISR) between the hybrid generator and LUARLW is found (major achievement)

# Whitepaper Estimate of HVP

- Merging of **KNT**, **DHMZ** estimates + input from **ChPT/dispersive fits**: **CHHKs** for  $2\pi$ ,  $3\pi$  channels; determinations from FJ17 and BDJ10 (assuming hadronic models in global fit) not considered
- Observation that averaging procedures in KNT and DHMZ lead to large differences for individual channels (especially  $2\pi$ ) although total average in good agreement, which is accidental!

→  $a_\mu^{HVP,LO} = 693.1(2.8)_{\text{exp}}(2.8)_{\text{syst}}(0.7)_{\text{pQCD}} = 693.1(4.0) \times 10^{-10}$  **Whitepaper estimate**

- **exp**: experimental uncertainties:  $2.8 \times 10^{-10}$   
dominated by  $2\pi$  channel uncertainty

$$2.8 \times 10^{-10}$$

- **syst**: KLOE/BABR tension taken into account by estimating HVP leaving out KLOE or leaving out BABAR in evaluation:

$$2.8 \times 10^{-10}$$

- pQCD: difference in energy region [1.8;3.7] GeV btw. KNT and DHMZ; usage of pQCD by DHMZ, while KNT follows data-driven approach:  $.7 \times 10^{-10}$

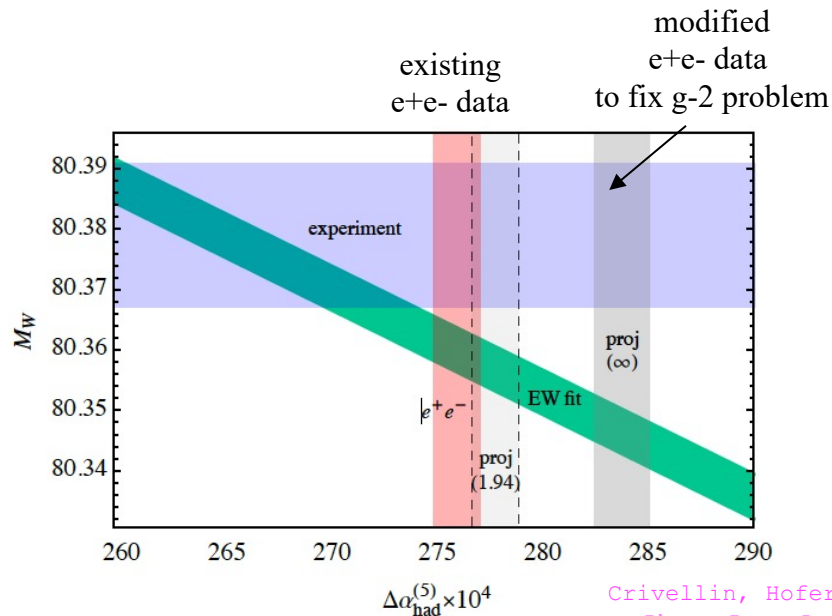
	DHMZ19	KNT19	Difference
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$\pi^+\pi^-\pi^0$	46.21(0.40)(1.10)(0.86)	46.63(94)	-0.42
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$K_S K_L$	12.82(0.06)(0.18)(0.15)	13.04(19)	-0.22
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Sum of the above	626.08(0.95)(3.48)(1.47)	623.62(2.27)	2.46
[1.8, 3.7] GeV (without $c\bar{c}$ )	33.45(71)	34.45(56)	-1.00
$J/\psi, \psi(2S)$	7.76(12)	7.84(19)	-0.08
[3.7, $\infty$ ] GeV	17.15(31)	16.95(19)	0.20
Total $a_\mu^{HVP,LO}$	694.0(1.0)(3.5)(1.6)(0.1) $_{\psi(0.7)_{\text{DV+QCD}}}$	692.8(2.4)	1.2

# HVP and Electroweak Precision Physics

Artificially increasing  $e^+e^-$  cross sections (over full energy range) to match  $a_\mu^{\text{exp}}$

→ Impact on running of fine structure constant  $\Delta\alpha_{\text{had}}(M_Z^2)$

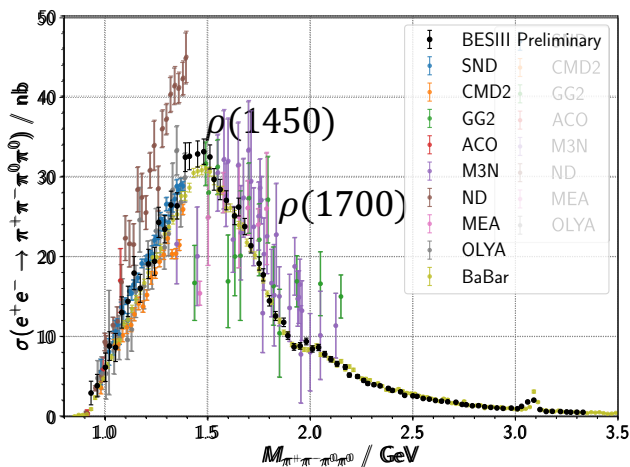
→ increasing deviation btw. EW fit and EW measurements (e.g.  $M_H$ ,  $M_W$ , ...) ?!



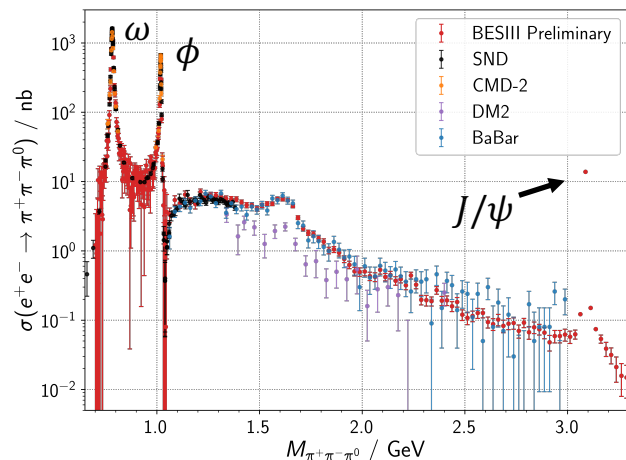
Crivellin, Hoferichter, Manzari, Montull  
Phys. Rev. Lett. 125, 091801 (2020)

# ISR: $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ , $e^+e^- \rightarrow \pi^+\pi^-2\pi^0$

Cross section  $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$



Cross section  $e^+e^- \rightarrow \pi^+\pi^-\pi^0$



	$\text{fb}^{-1}$	$a_\mu^{4\pi} [10^{-10}]$
Before		$16.76 \pm 1.31 \pm 0.20_{\text{rad}}$
BABAR	450	$17.9 \pm 0.1 \pm 0.06$
BESIII (prel.)	2.9	$18.63 \pm 0.27 \pm 0.57$

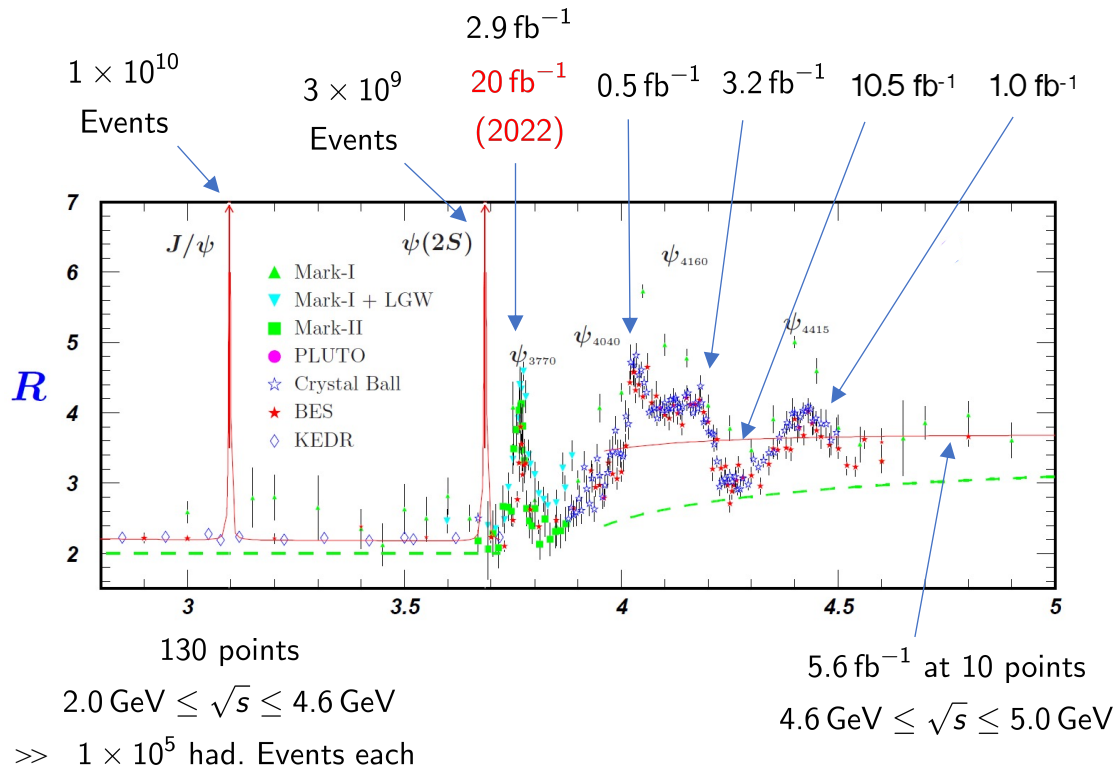
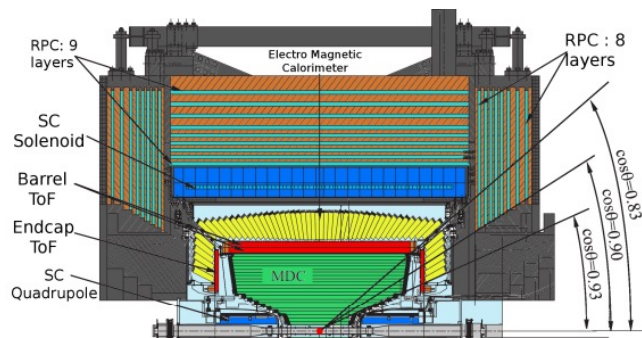
	$a_\mu^{3\pi} [10^{-10}]$
Before <sub>KNT18</sub> (<2 GeV)	$47.79 \pm 0.89$
BESIII (prel.)	$49.15 \pm 0.56 \pm 0.58$

Meson2021: Bastian Kubis

# BESIII Experiment at the tau-charm Factory BEPC-II

## World's by far largest $\tau$ -charm dataset in $e^+e^-$ annihilation:

- Symmetric  $e^+e^-$  collider
- Located at the BEPCII collider (Beijing, China)
- CMS energy: 2 GeV to 5 GeV
- Maximum luminosity:  $1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
- 93% coverage of the solid angle



# Standard Model Prediction of $(g-2)_\mu$

$$a_\mu^{SM} = a_\mu^{QED} + a_\mu^{weak} + a_\mu^{had} = (11\,659\,181.0 \pm 4.3) \cdot 10^{-10}$$

Kinoshita et al. '12

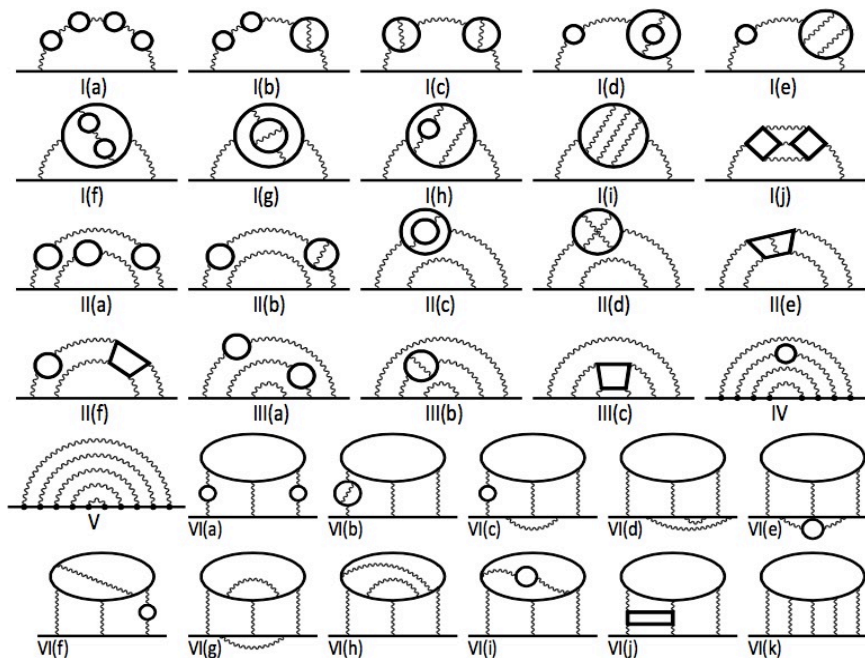
$$(11\,658\,471.808 \pm 0.015) \cdot 10^{-10}$$

Czarnecki et al.

$$(15.4 \pm 0.2) \cdot 10^{-10}$$

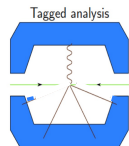
Absolute contribution dominated by QED  
Uncertainty dominated by hadronic contribution

10<sup>th</sup>  
12672  
diagrams



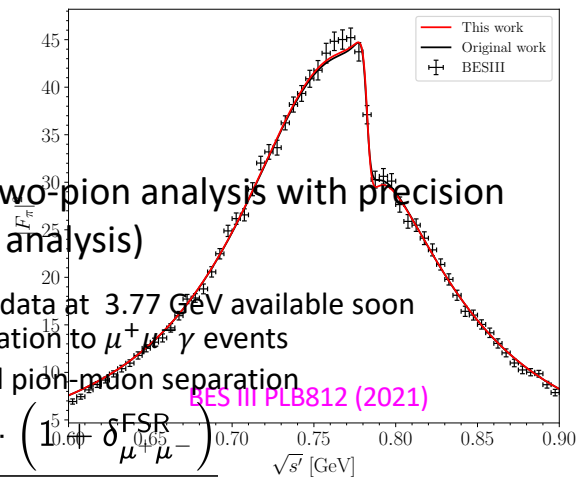
# BESIII Analysis $e^+e^- \rightarrow \pi^+\pi^-\gamma_{ISR}$

- BESIII aims for new two-pion analysis with precision goal of 0.5% (tagged analysis)



- 20/fb of data at 3.77 GeV available soon
- Normalization to  $\mu^+\mu^-\gamma$  events
- Improved pion-muon separation

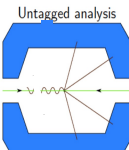
BES III PLB812 (2021)



$$R = \frac{N_{\pi^+\pi^-}}{N_{\mu^+\mu^-}} \cdot \frac{\epsilon_{\mu^+\mu^-} \cdot \left(1 + \delta_{\mu^+\mu^-}^{\text{FSR}}\right)}{\epsilon_{\pi^+\pi^-} \cdot \left(1 + \delta_{\pi^+\pi^-}^{\text{FSR}}\right)}$$

CMD-2 03,06 372.4 ± 3.0

- BESIII aims for an improved measurement of the mass range above 1 GeV (untagged analysis)



BESIII 16 superseded by this work

CLEO 18

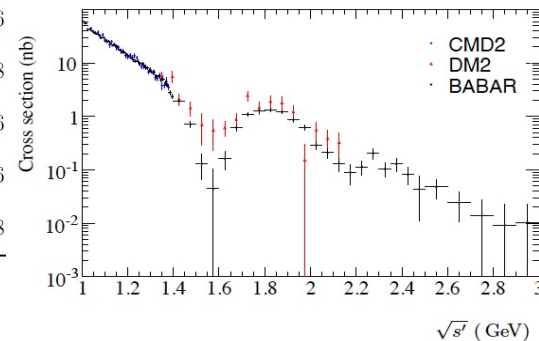
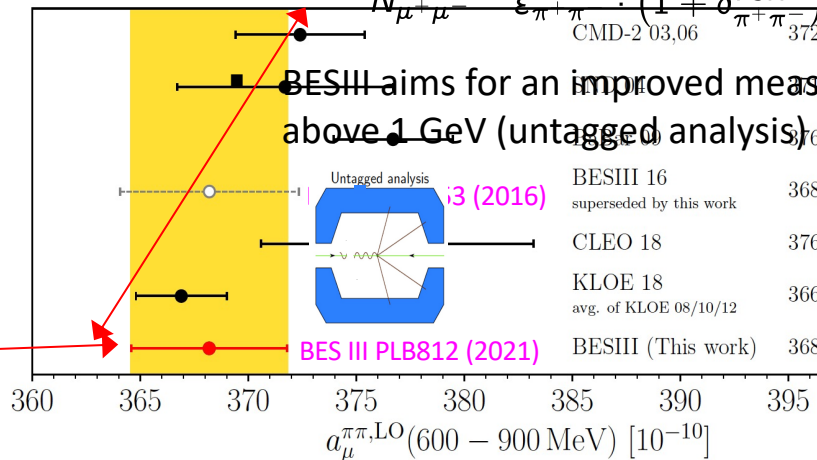
KLOE 18

avg. of KLOE 08/10/12

BESIII (This work)

$a_{\mu}^{\pi\pi, \text{LO}}(600 - 900 \text{ MeV}) [10^{-10}]$

Source	BESIII 2016 2.9/fb (Update)
Photon efficiency	0.2
Pion tracking efficiency	0.3
Pion ANN efficiency	0.2
Pion e-PID efficiency	0.2
Angular acceptance	0.1
Background subtraction	0.1
Unfolding procedure	0.2
Luminosity $\mathcal{L}$	0.5
FSR correction	0.2
Vacuum polarization	0.2
Radiator function	0.5
<b>Sum Systematics</b>	<b>0.9</b>
<b>Statistical error</b>	<b>0.4</b>



# Whitepaper 2025: KLOE LA-Analysis

