Higgs & BSM at lepton colliders

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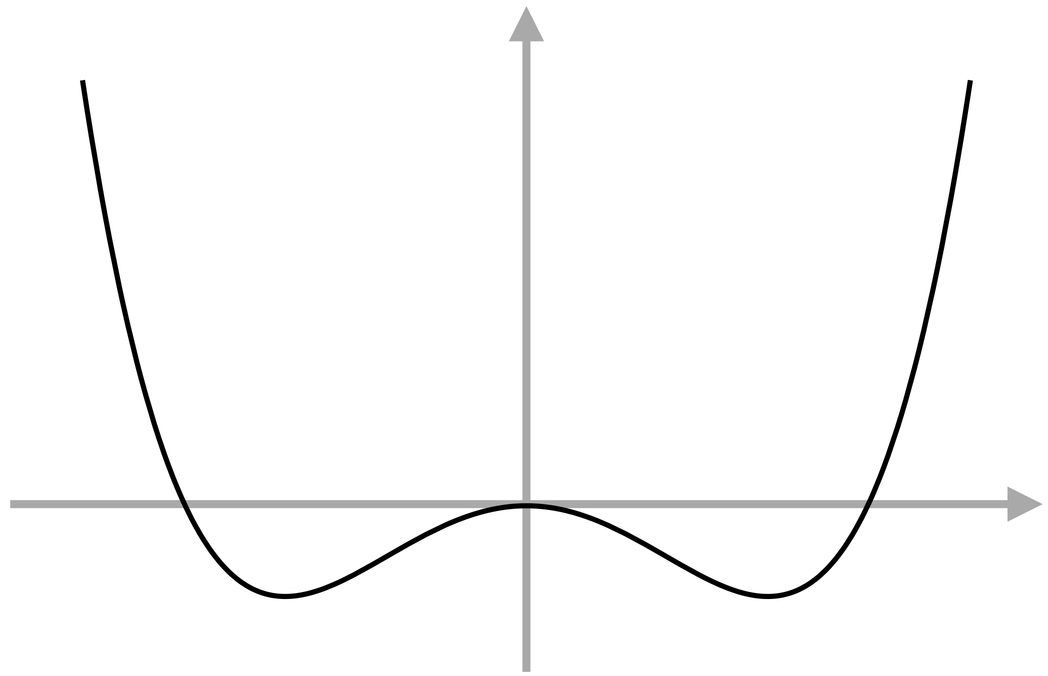
Workshop on FCC-ee and Lepton Colliders — LNF, 23.01.2025

Why colliders?

Goal: explore physics at least up to $M \approx 10\,\mathrm{TeV}$

- ✦ What is the Higgs made of? What is its *size*? What causes EWSB?

we don't know…



$$V(\Phi) = \alpha(T - T_c)\,\Phi^2 + \beta\,\Phi^4$$

~ Landau-Ginzburg theory for superconductivity

… We still **lack the microscopic description** (BCS)!

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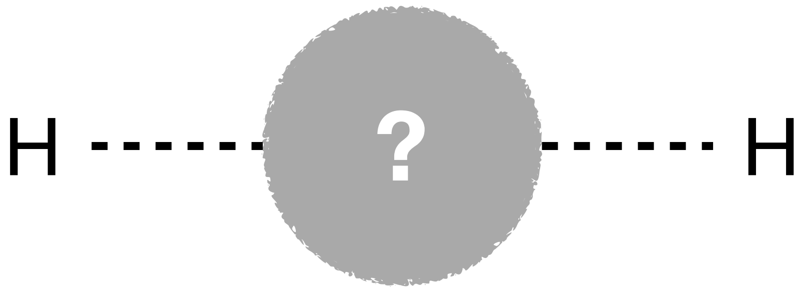

→ $M_{\mathrm{NP}} \lesssim 4\pi v \approx 3\,\mathrm{TeV}$

rough estimate! there can easily be some O(1) factor

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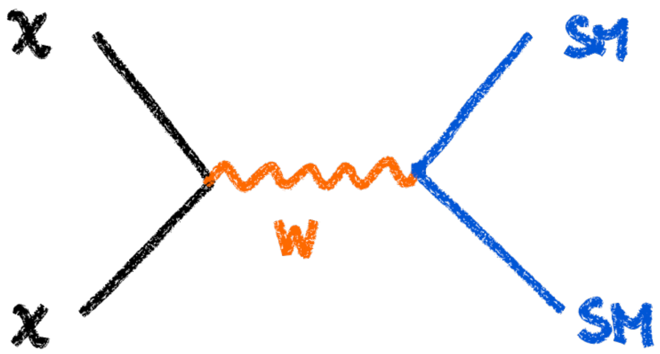
- ✦ What is dark matter? Is it a WIMP?

we have no idea…



$$\longrightarrow \quad M_{\mathrm{DM}} \approx 1 - 15\,\mathrm{TeV}$$

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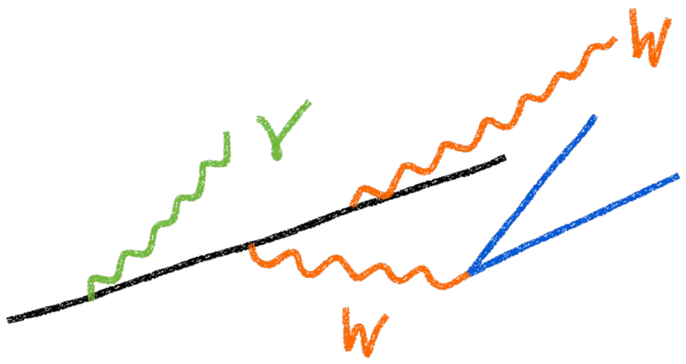
- Electroweak radiation: new phenomena *in the SM*

  Restoration of EW symmetry and radiation of "massless" EW bosons

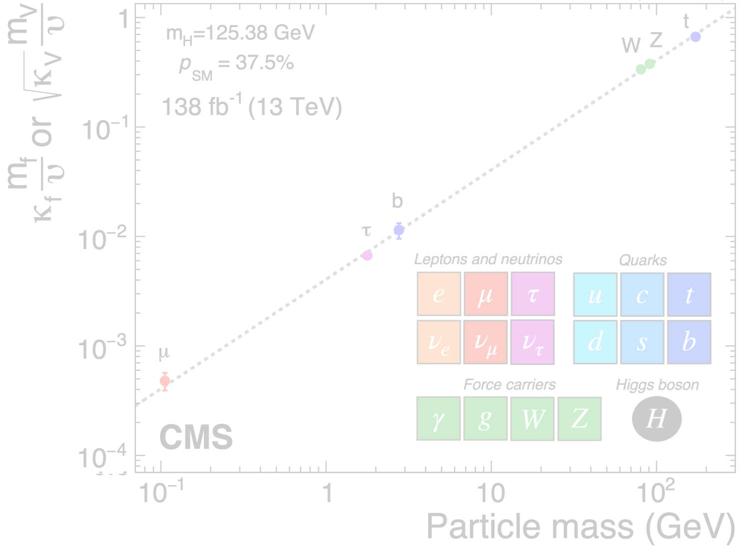


$\longrightarrow$ $E \approx 10\,\mathrm{TeV}$

we have never observed this…

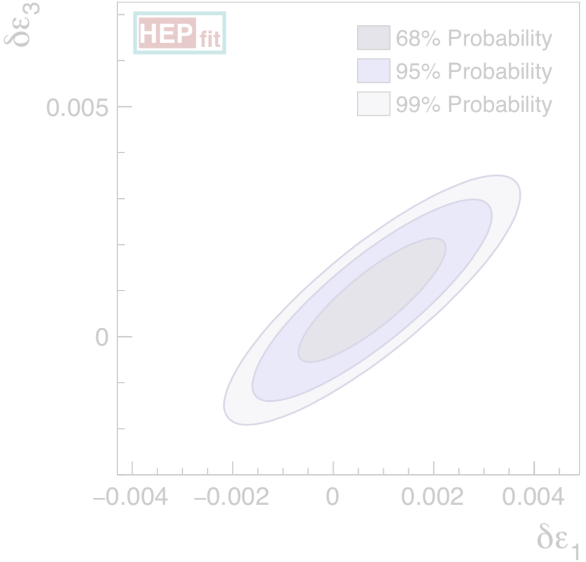
Where do we stand?

- The SM works well at the TeV scale: → $M_{\rm NP} \gtrsim$ few TeV directly



- The Higgs boson is SM-like:

$$\delta\kappa \sim \frac{v^2}{M_{\rm NP}^2} g_\star^2 \lesssim 5\,\% \quad \longrightarrow \quad M_{\rm NP} \gtrsim g_\star\,\text{TeV}$$



- The EW sector is SM-like:

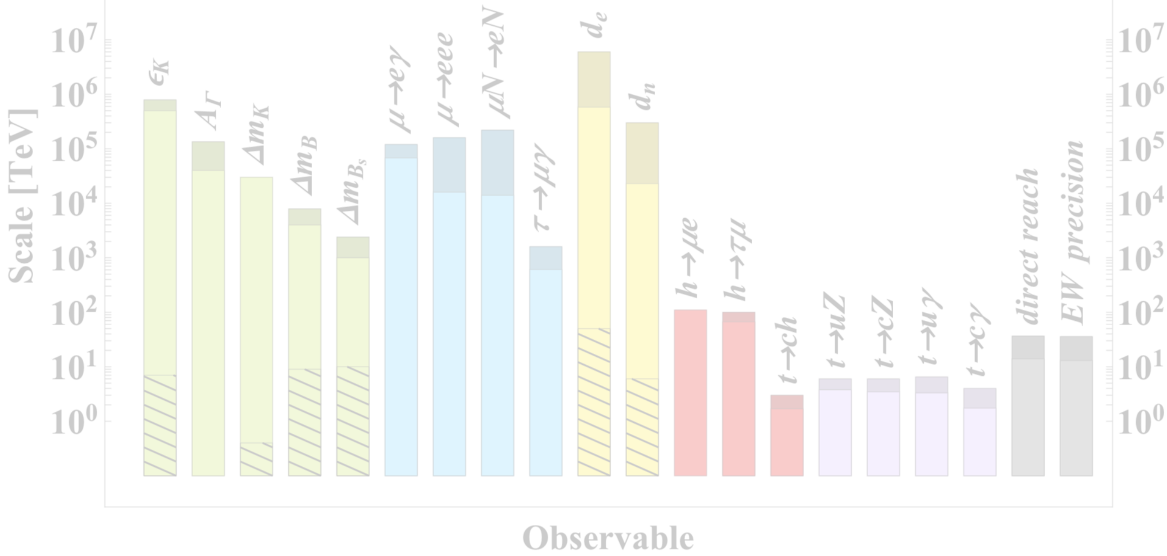
$$\delta\varepsilon \sim \frac{m_W^2}{M_{\rm NP}^2} \lesssim \text{few} \times 10^{-3} \quad \longrightarrow \quad M_{\rm NP} \gtrsim 2\,\text{TeV}$$

- The CKM picture of flavor and CP works well; lepton flavor is conserved

$$\frac{\delta\mathcal{O}_{ij}}{\mathcal{O}_{ij}^{\rm SM}} \sim \frac{v^2}{M_{\rm NP}^2}\frac{4\pi}{\alpha}\frac{c_{ij}}{\xi_{ij}} \lesssim 10\,\%$$

flavor suppression of the SM

$$\longrightarrow \quad M_{\rm NP} \gtrsim 3\,\text{TeV}\left(\frac{c_{ij}}{\xi_{ij}}\right)^{1/2}$$



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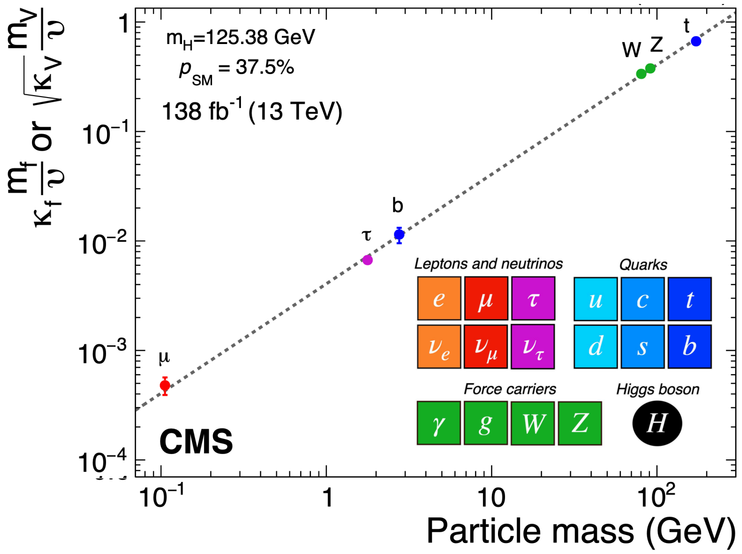

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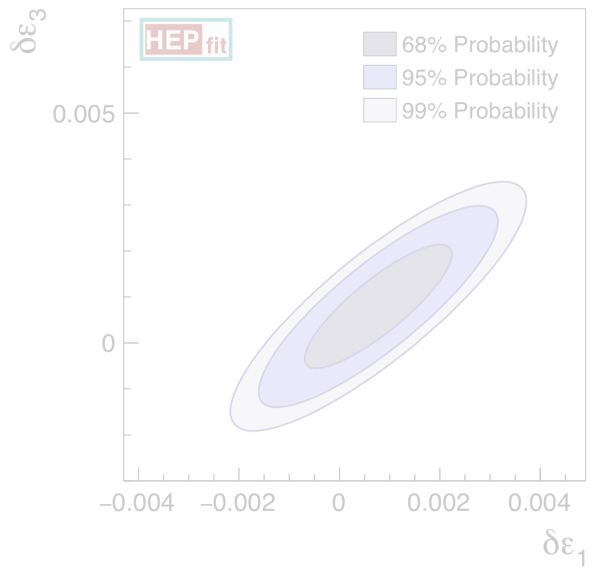

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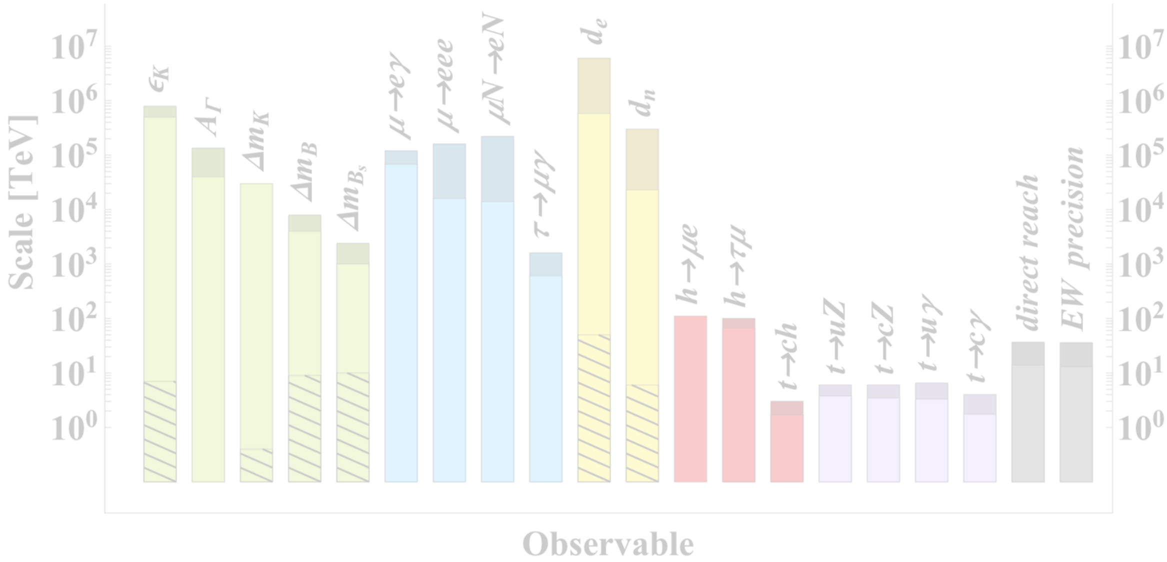

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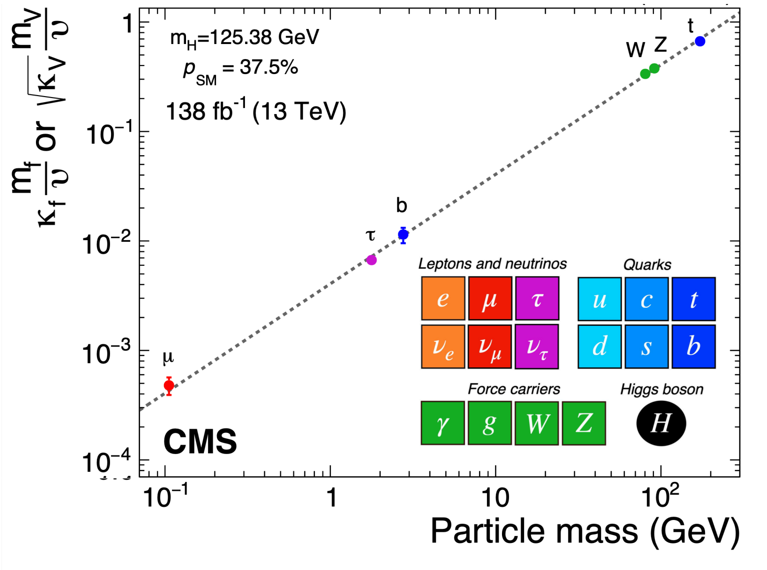

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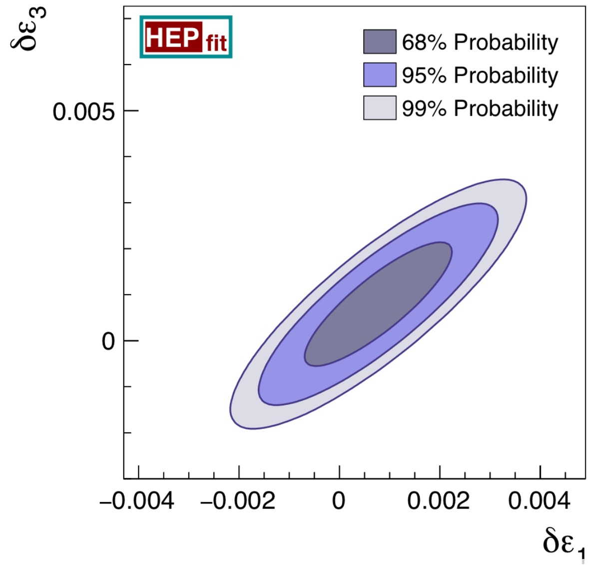

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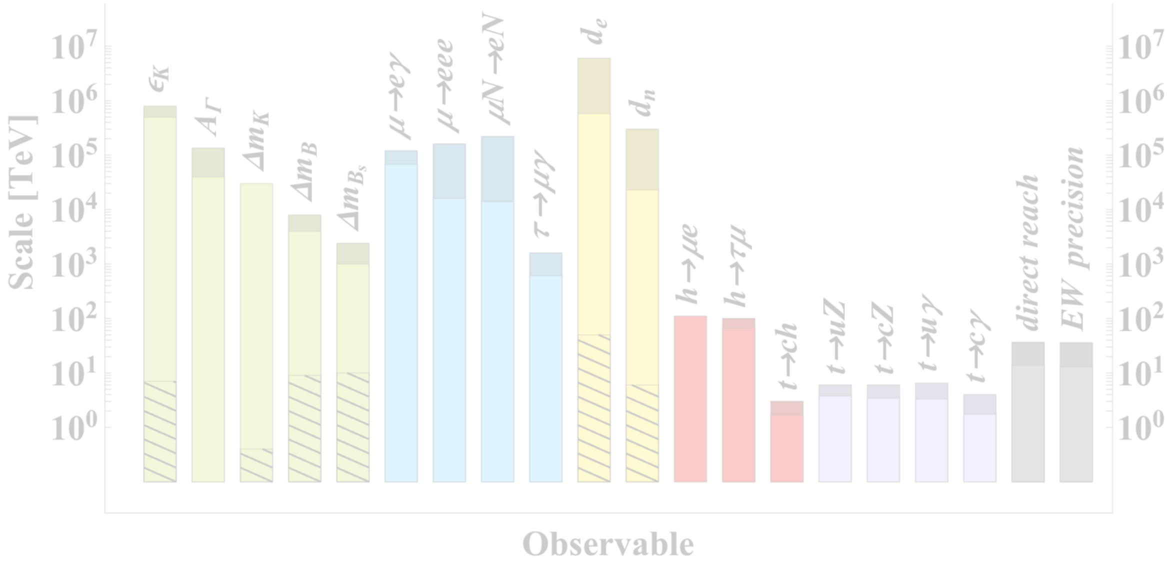

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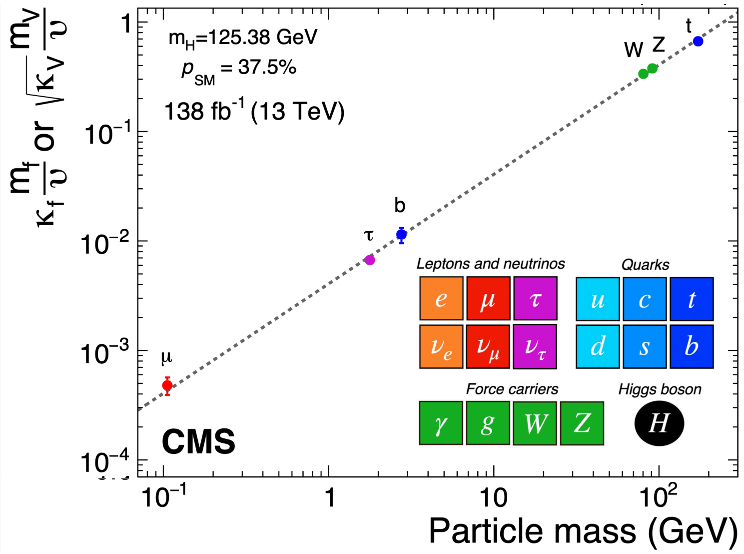

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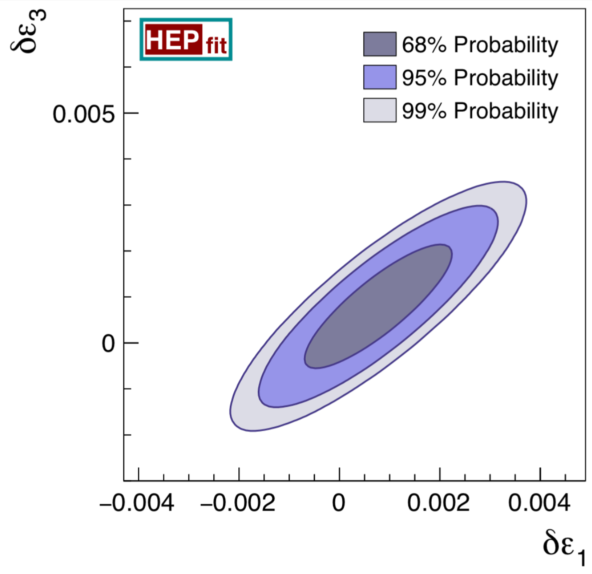

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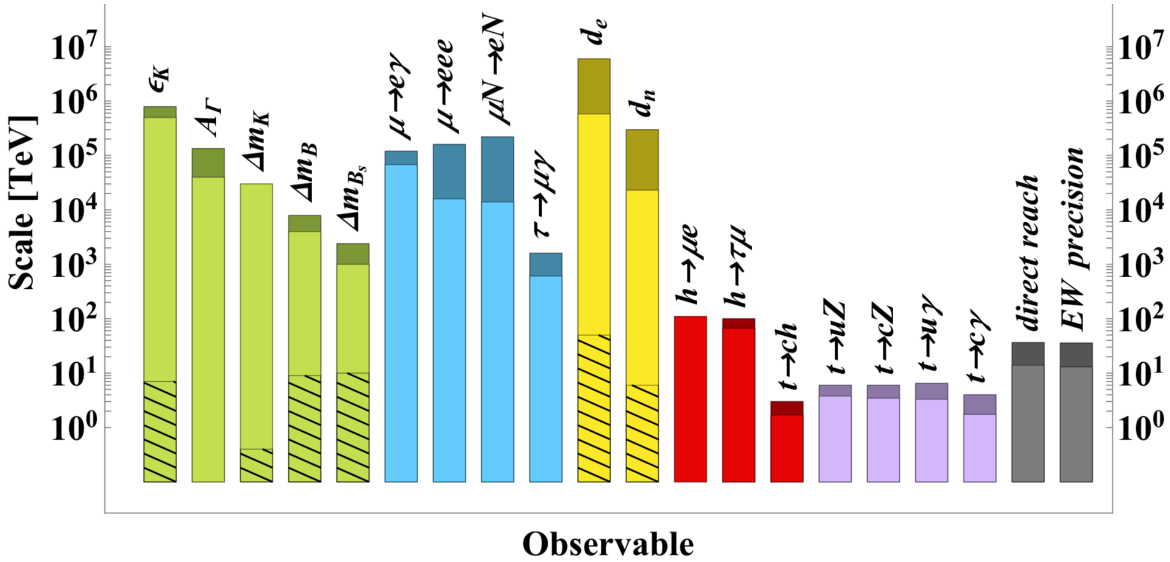


Where do we stand?

- SMEFT with CKM-like suppression ($U(2)^3$ flavor symmetry):
- + mild suppression of light gen. interactions
- + some flavor alignment

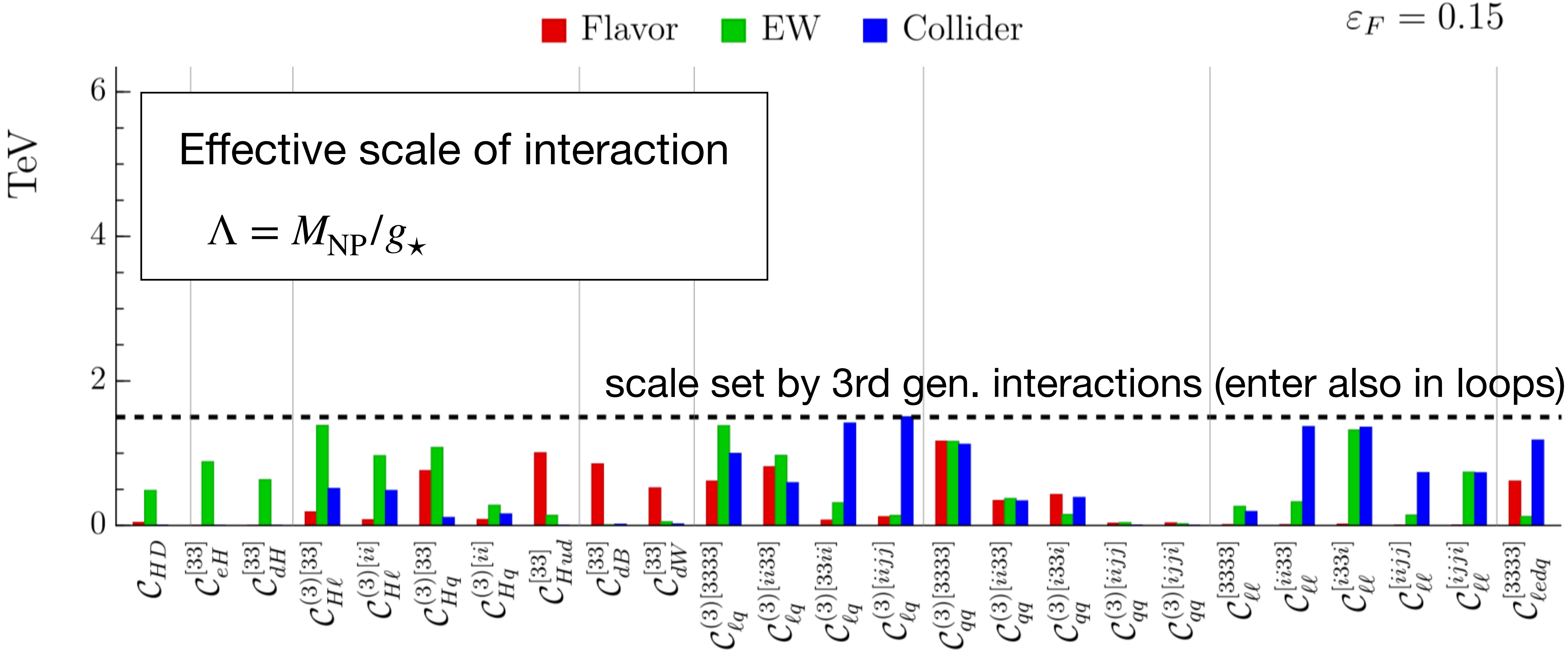
$$\varepsilon_{\rm loop} = \frac{g_i}{16\pi^2}$$

$$\varepsilon_Q = 0.16$$

$$\varepsilon_L = 0.40$$

$$\varepsilon_H = 0.31$$

$$\varepsilon_F = 0.15$$



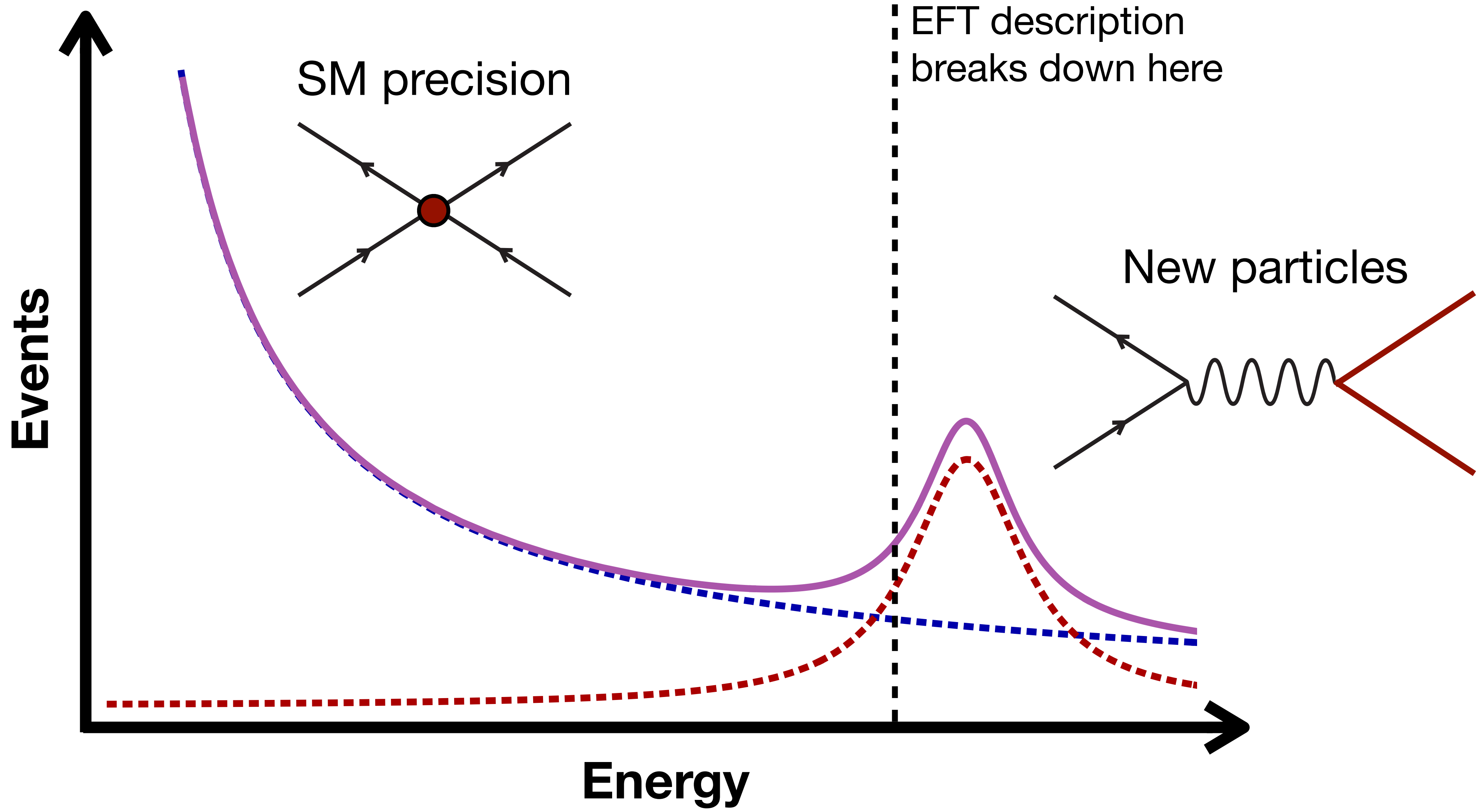
Effective scale of interaction

$$\Lambda = M_{\rm NP}/g_\star$$

scale set by 3rd gen. interactions (enter also in loops)

Allwicher, Cornella, Isidori, Stefanek 2311.00020

Two paths forward



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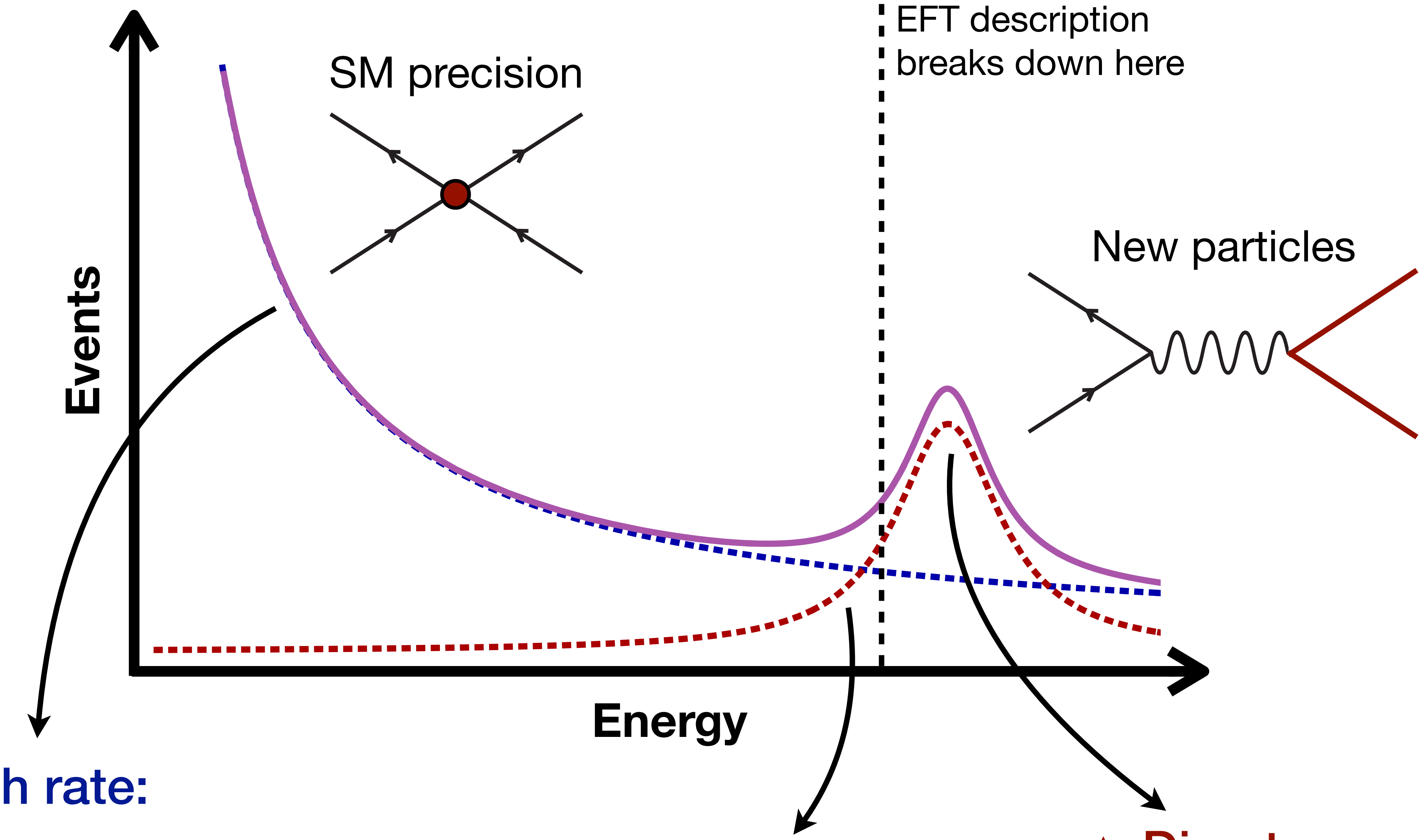


- **High rate:**

  More events

  = Better precision

- **High energy precision:**

  New physics effects

  grow ~ E^2

  $\sigma_{\text{SM}} \sim 1/E^2$

- **Direct searches:**

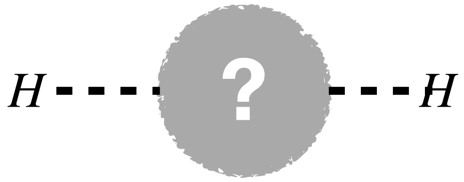
  Look for new

  particles/resonances

The next step: Higgs

- Big open questions in the SM involve Higgs:

  study it with the precision of Z!



- All proposed future colliders will be able to produce millions of Higgses

  ➔ study single Higgs couplings with below percent precision!

(as a comparison: 1.7 x 10^7 Z bosons @ LEP)

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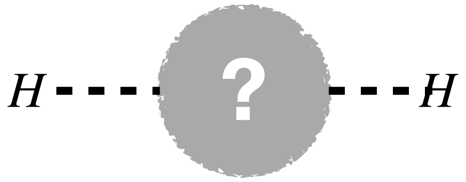

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Low energy
e^+e^- factories
(FCC-ee, CEPC,
ILC, CLIC380)

TeV-scale
e^+e^- factories
(CLIC, ILC1000)

LHC: few x 10^7

HL-LHC: few x 10^8

FCC-hh:
few x 10^{10}

Muon colliders: 10^6 – 10^8

\# of Higgses

clean environment:
can measure “large” Higgs
BR w/ almost 10^{-3} precision

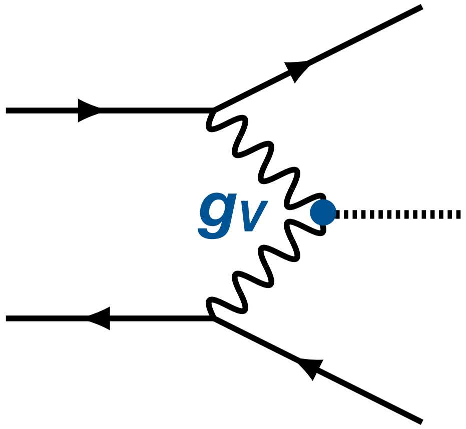
large QCD backgrounds:
only rare modes (BR < 10^{-3})
easily accessible

Higgs factories

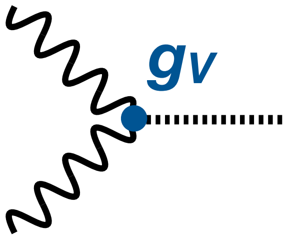
- Low-energy e+e- factories: $e^+e^- \to Zh$ @ 240 GeV

- measure the recoil (missing mass) of h against Z
- *direct* measurement of gV ⟶ other couplings + width

- A high-energy lepton collider is a “vector boson collider”

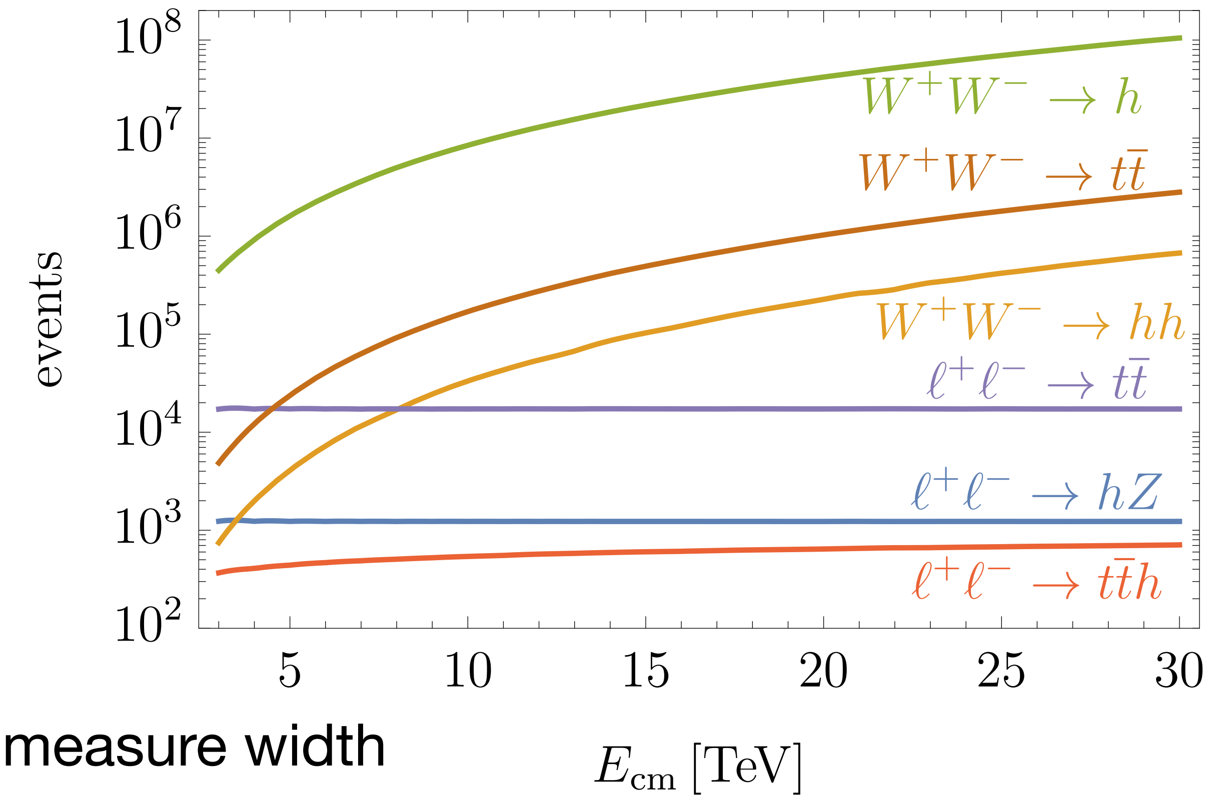


$$\approx \frac{s}{\hat{s}} \log \frac{s}{\hat{s}}$$



For “soft” SM final state $\hat{s} \sim m_{\rm EW}^2$

cross-section is enhanced



- potentially huge single H production

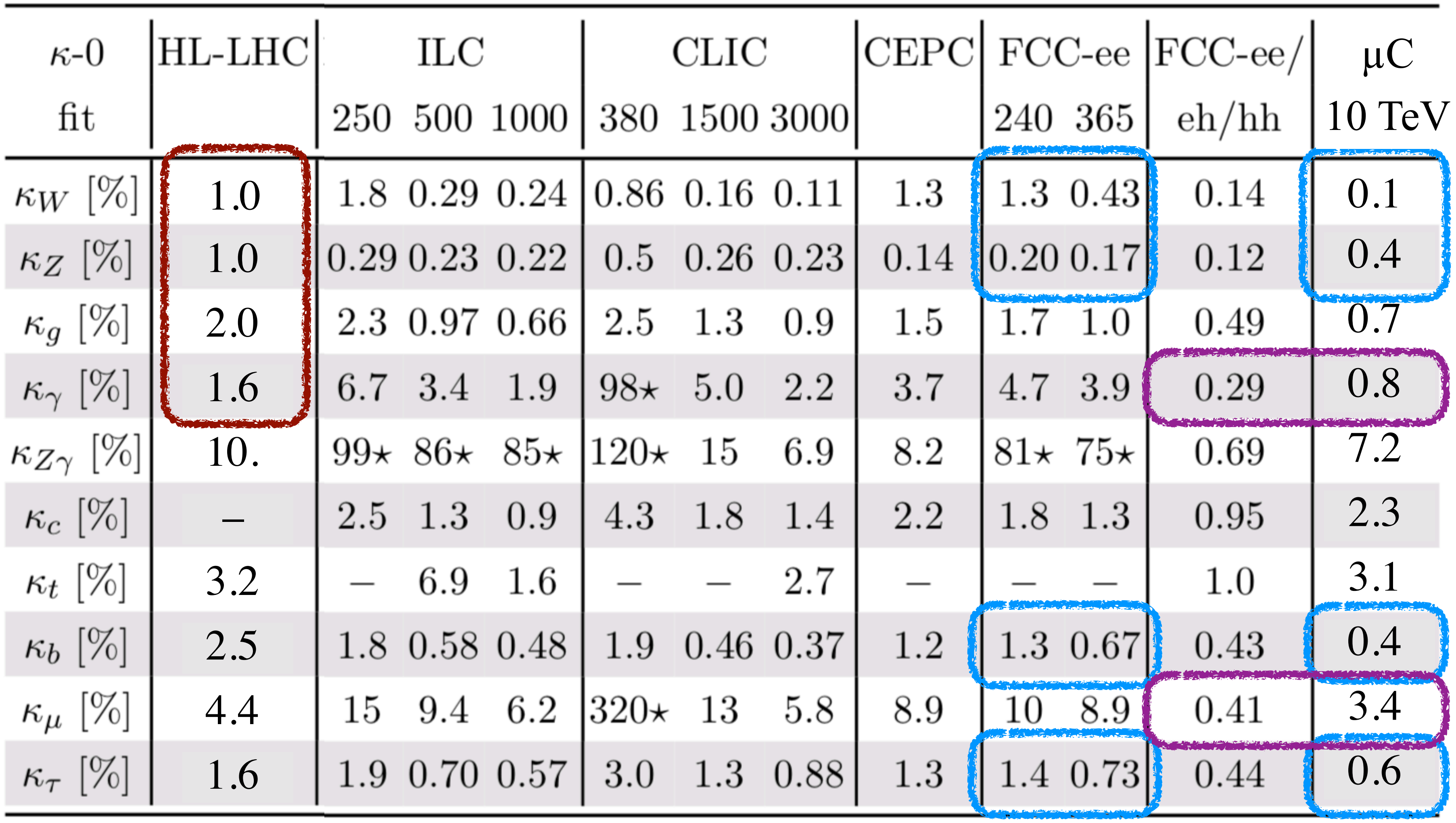
  (10^7-10^8 at 10-30 TeV)

- hard neutrinos from W-fusion not seen

  ZZ fusion (forward lepton tagging) could still measure width

Higgs factories

High-lumi LHC is already a Higgs factory!



κ-0	HL-LHC	ILC			CLIC			CEPC	FCC-ee		FCC-ee/	μC
fit		250	500	1000	380	1500	3000		240	365	eh/hh	10 TeV
κ_W [%]	1.0	1.8	0.29	0.24	0.86	0.16	0.11	1.3	1.3	0.43	0.14	0.1
κ_Z [%]	1.0	0.29	0.23	0.22	0.5	0.26	0.23	0.14	0.20	0.17	0.12	0.4
κ_g [%]	2.0	2.3	0.97	0.66	2.5	1.3	0.9	1.5	1.7	1.0	0.49	0.7
κ_γ [%]	1.6	6.7	3.4	1.9	98⋆	5.0	2.2	3.7	4.7	3.9	0.29	0.8
$\kappa_{Z\gamma}$ [%]	10.	99⋆	86⋆	85⋆	120⋆	15	6.9	8.2	81⋆	75⋆	0.69	7.2
κ_c [%]	–	2.5	1.3	0.9	4.3	1.8	1.4	2.2	1.8	1.3	0.95	2.3
κ_t [%]	3.2	–	6.9	1.6	–	–	2.7	–	–	–	1.0	3.1
κ_b [%]	2.5	1.8	0.58	0.48	1.9	0.46	0.37	1.2	1.3	0.67	0.43	0.4
κ_μ [%]	4.4	15	9.4	6.2	320⋆	13	5.8	8.9	10	8.9	0.41	3.4
κ_τ [%]	1.6	1.9	0.70	0.57	3.0	1.3	0.88	1.3	1.4	0.73	0.44	0.6

2103.14043

dominant
channels:
~ few ‰

rare modes:
high rate
needed!

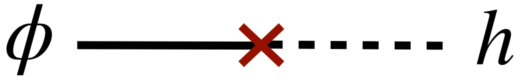
What NP scales will we test with the Higgs?

$$\delta\kappa \sim \frac{v^2}{M_{\rm NP}^2} g_\star^2 \lesssim \mathbf{0.2\%} \quad \rightarrow \quad M_{\rm NP} \gtrsim g_\star \times \mathbf{6\ TeV}$$

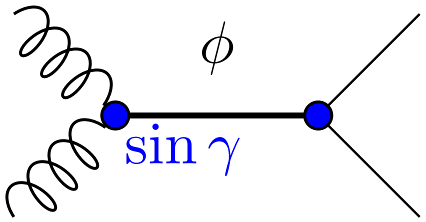
Direct vs indirect

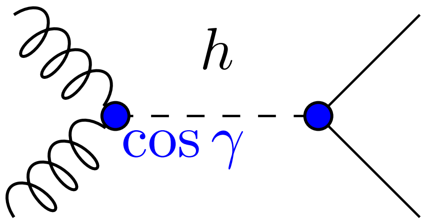
Compare single Higgs couplings measurements with reach of direct searches

- **Example: singlet scalar** $\mathscr{L}_{\text{int}} \sim \phi|H|^2$

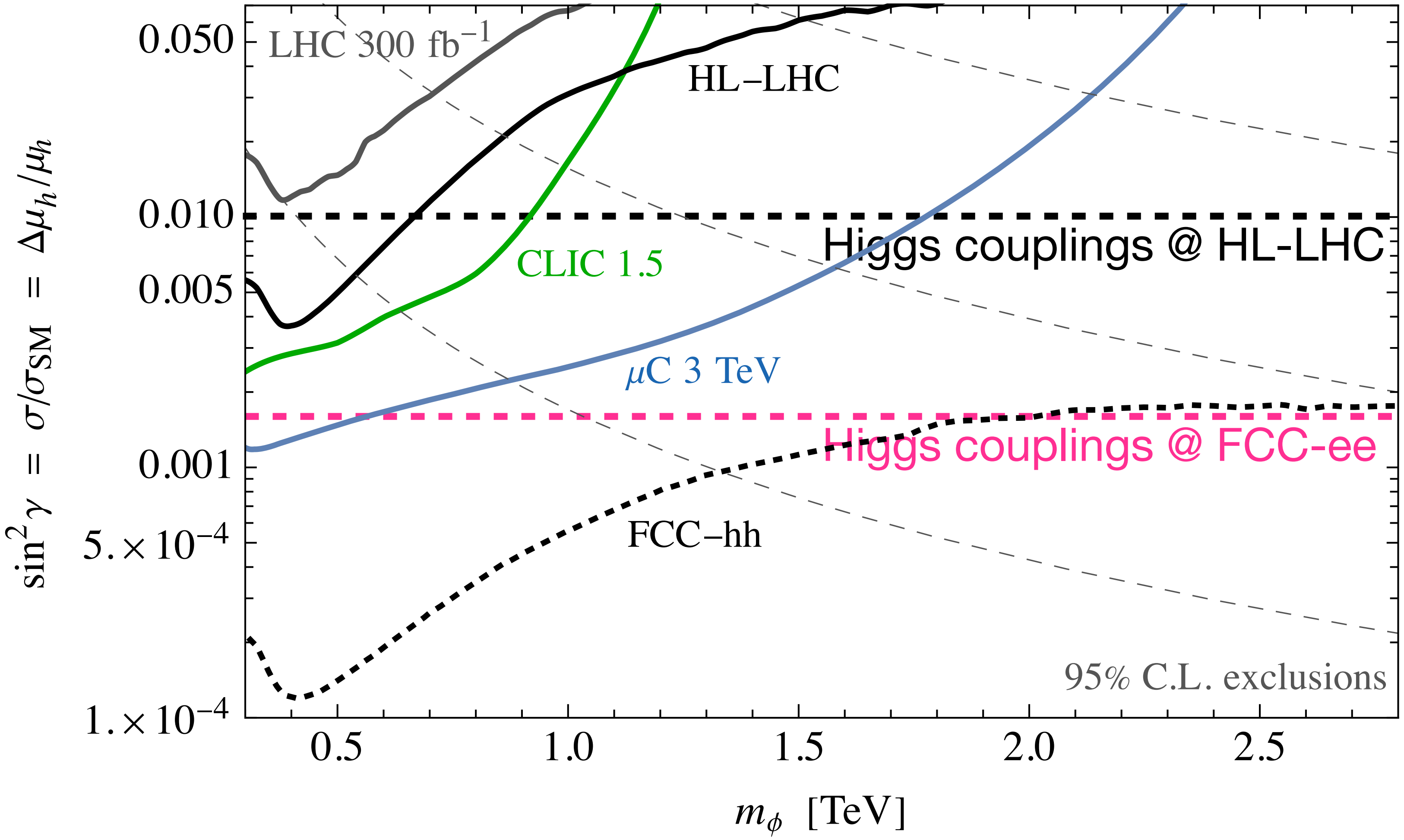


ϕ is like a heavy Higgs with narrow width + hh decay





one single parameter controls resonance production, decay, & Higgs coupling modifications



B, Redigolo, Sala, Tesi 1807.04743

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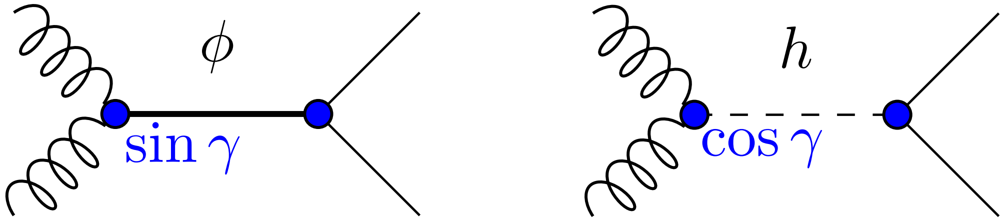

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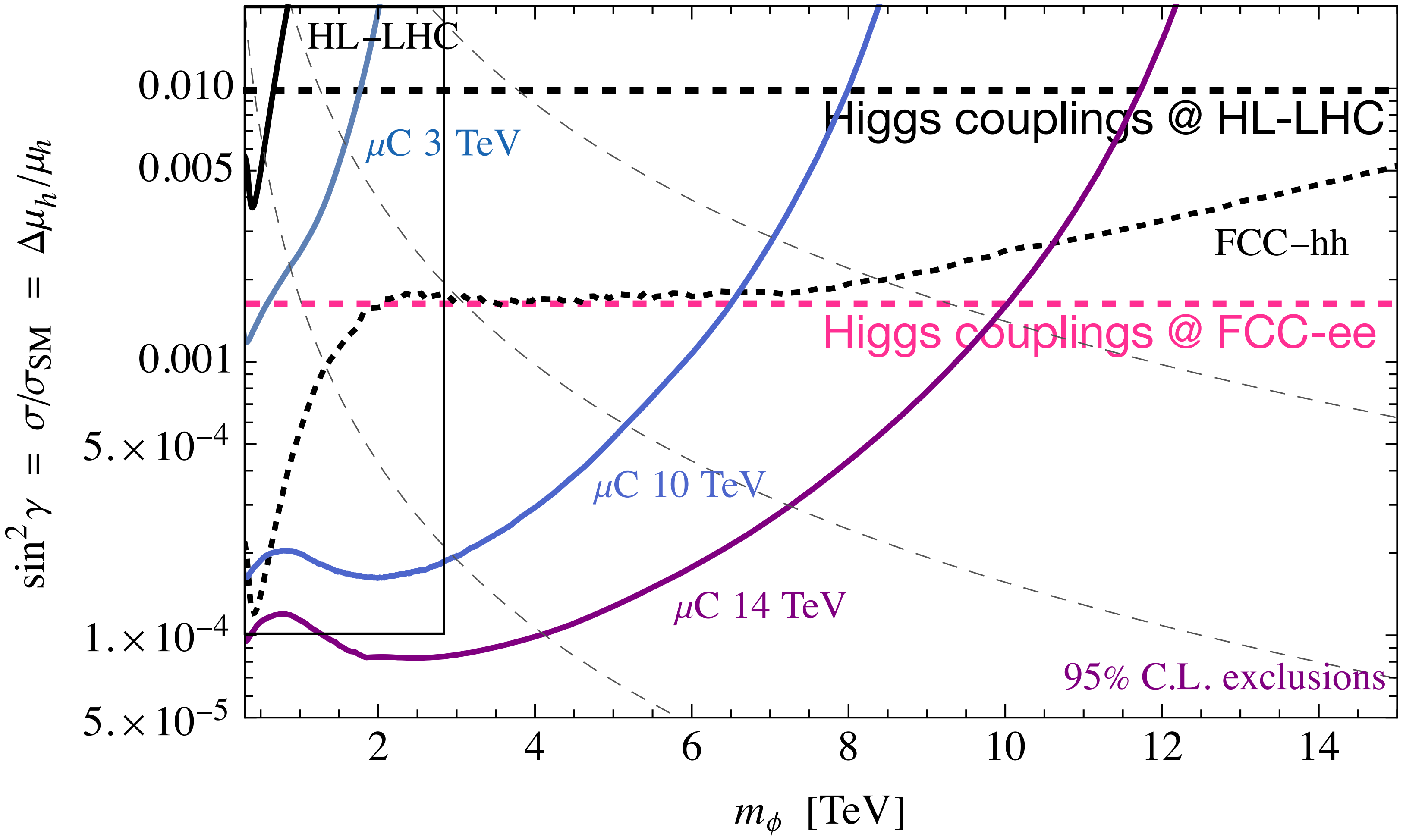


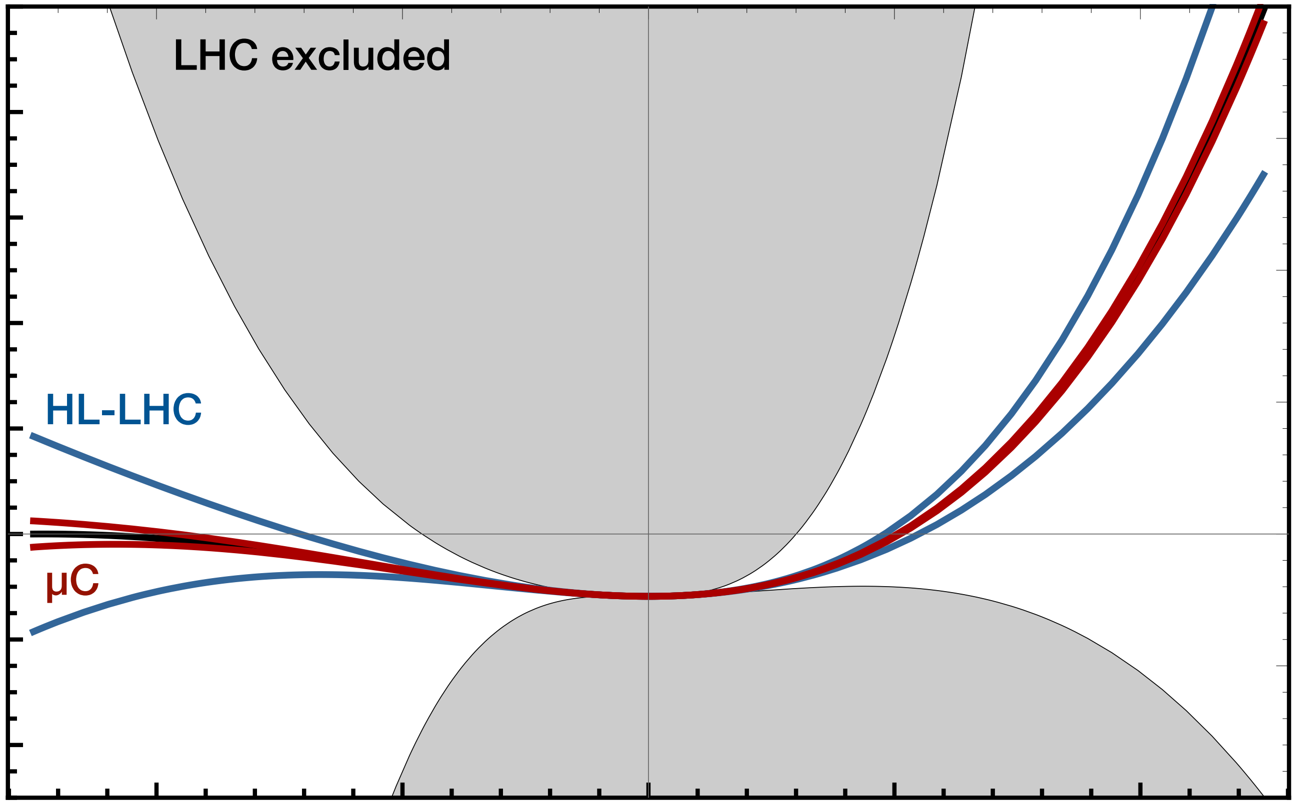
B, Redigolo, Sala, Tesi 1807.04743

Higgs self-coupling

- Measurement of trilinear coupling: access to the Higgs potential

Uncertainty scenario	κ_λ 68% CI	κ_λ 95% CI
No syst. unc.	[0.7, 1.4]	[0.3, 1.9]
Baseline	[0.5, 1.6]	[0.0, 2.5]
Theoretical unc. halved	[0.3, 2.2]	[−0.3, 5.5]
Run 2 syst. unc.	[0.1, 2.4]	[−0.6, 5.6]

- very poorly known today!
- HL-LHC will only reach 50% precision on SM value



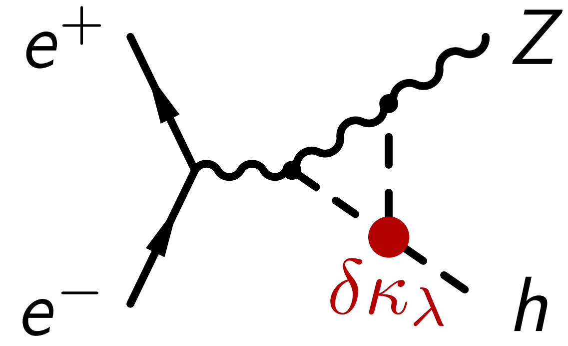
credits: Craig, Petrossian-Byrne

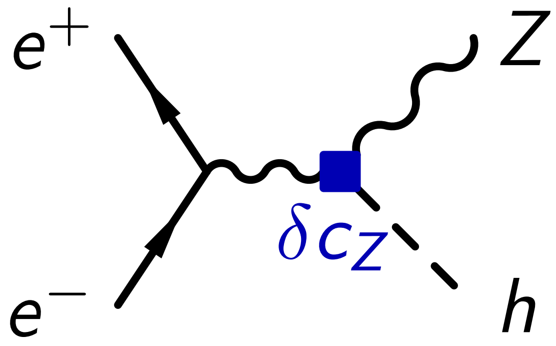
Higgs self-coupling

- Indirect sensitivity to $\delta\kappa_\lambda$ from single H production at low-energy e^+e^-

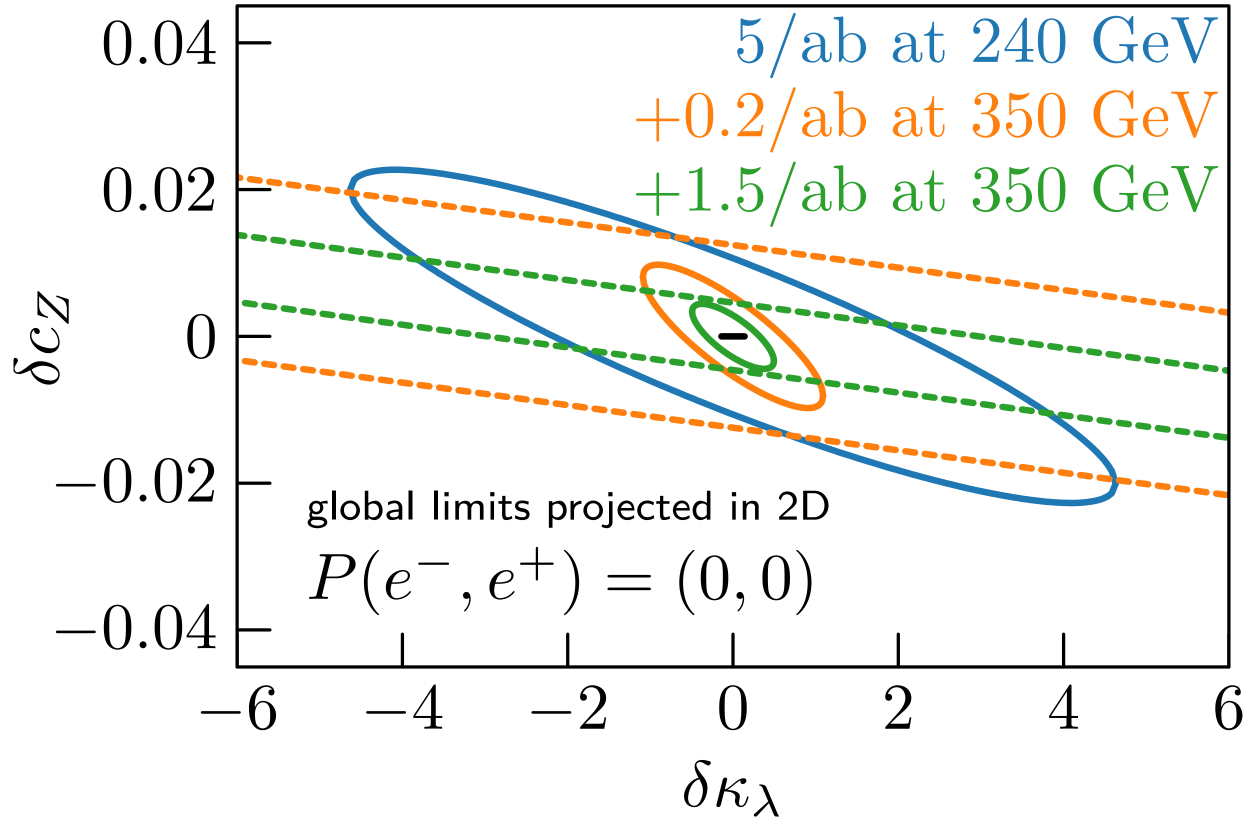
  one loop effect

- Degeneracy between trilinear and Z coupling: need measurements at at different energies





Di Vita et al. 1711.03978



- Individual limit: $\delta\kappa_\lambda \sim 15\,\%$
- Global fit: $\delta\kappa_\lambda \sim 50-100\,\%$

Double Higgs production

- Precise determination of $\delta\kappa_\lambda$ requires double Higgs production

- *Only* possible at high-energy machines: need high rate!

  100 TeV FCC-hh or multi-TeV lepton collider

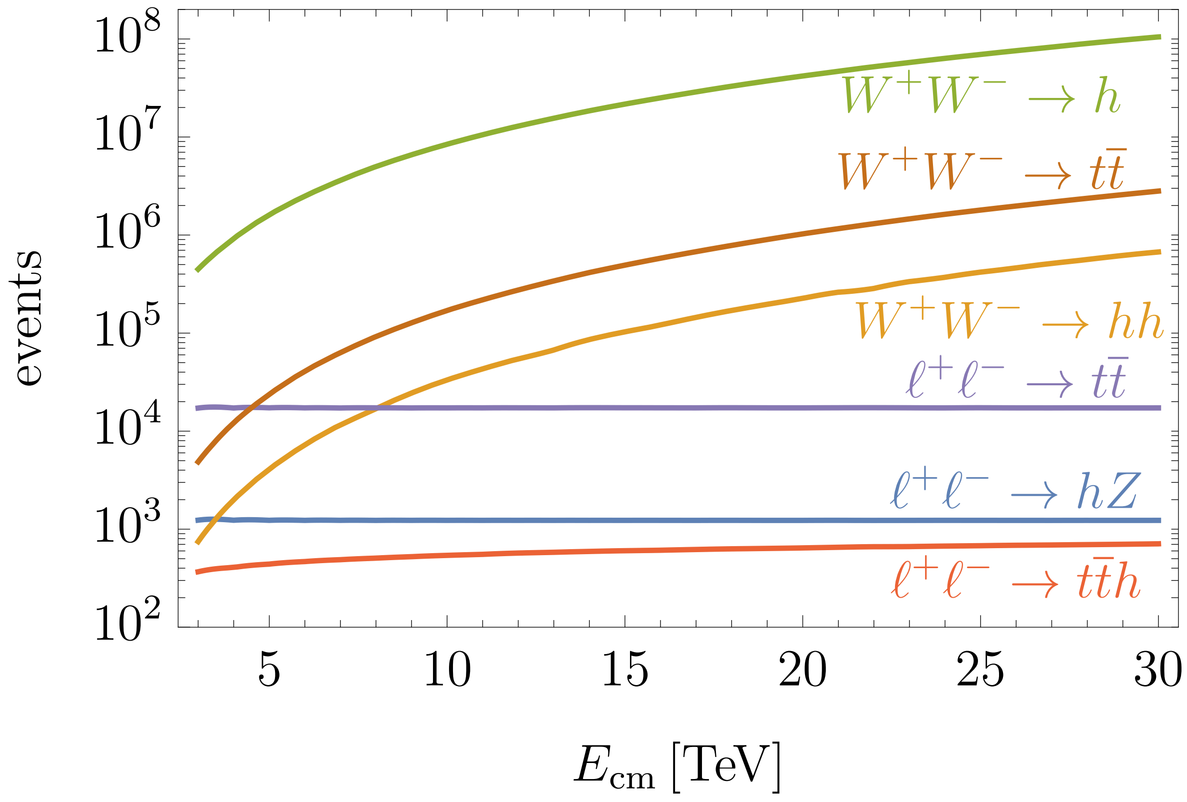
CLIC 1901.05897

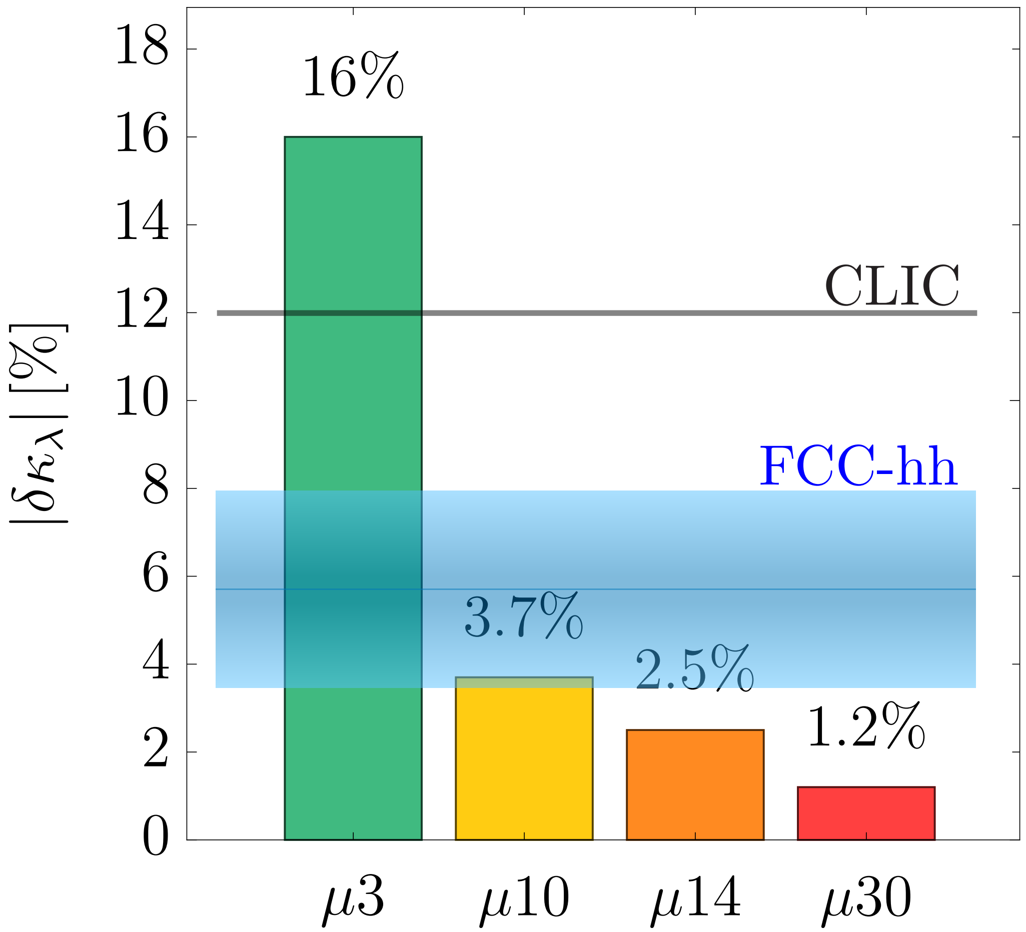
B, Franceschini, Wulzer 2012.11555
Costantini et al. 2005.10289
Han et al. 2008.12204

Mangano et al. 2004.03505

- A high-energy lepton collider is a

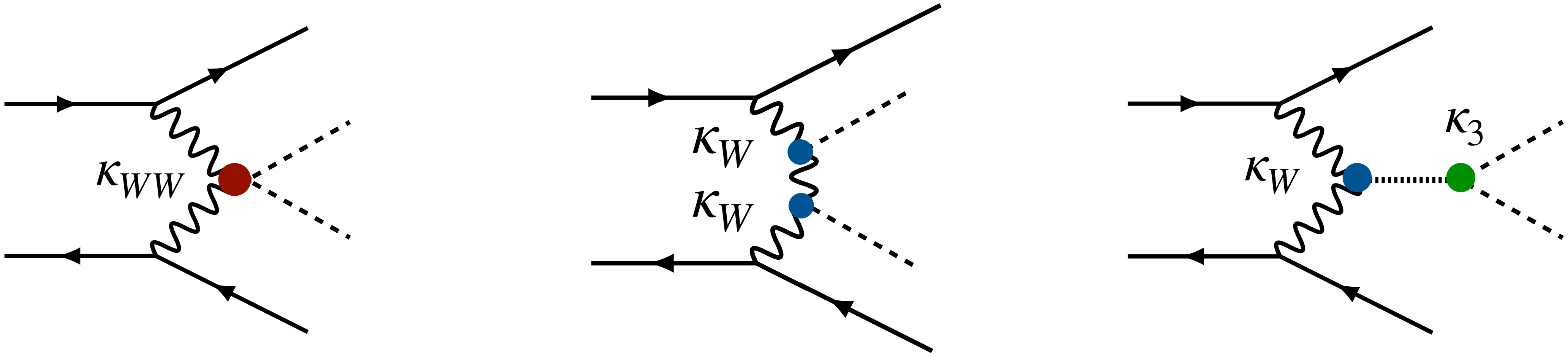
  “vector boson collider”

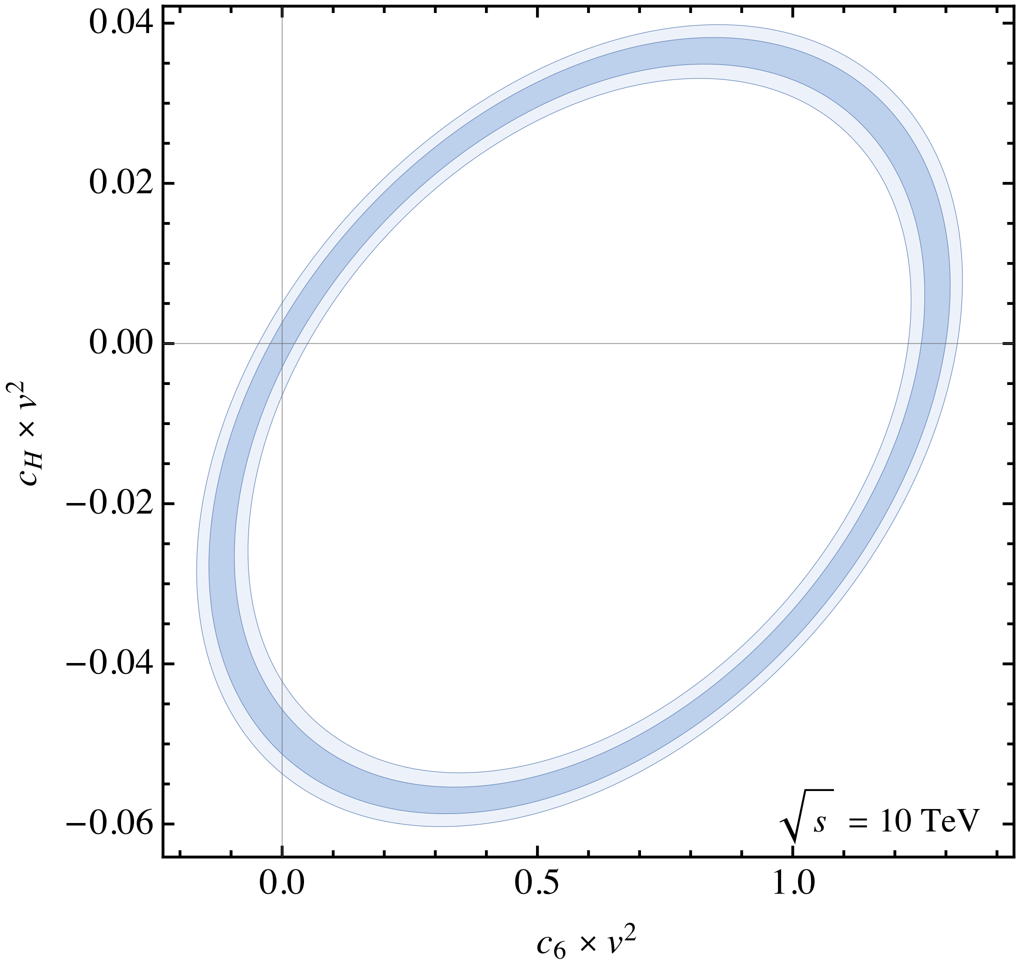




Double Higgs production

- Double Higgs production depends on trilinear coupling κ_3 but also on W-boson couplings κ_W, κ_{WW} that enter the production cross-section





large degeneracy in total cross-section

- Two dim. 6 operators:

$$\mathcal{O}_6 = -\lambda |H|^6 \qquad \mathcal{O}_H = \frac{1}{2}\left(\partial_\mu |H|^2\right)^2$$

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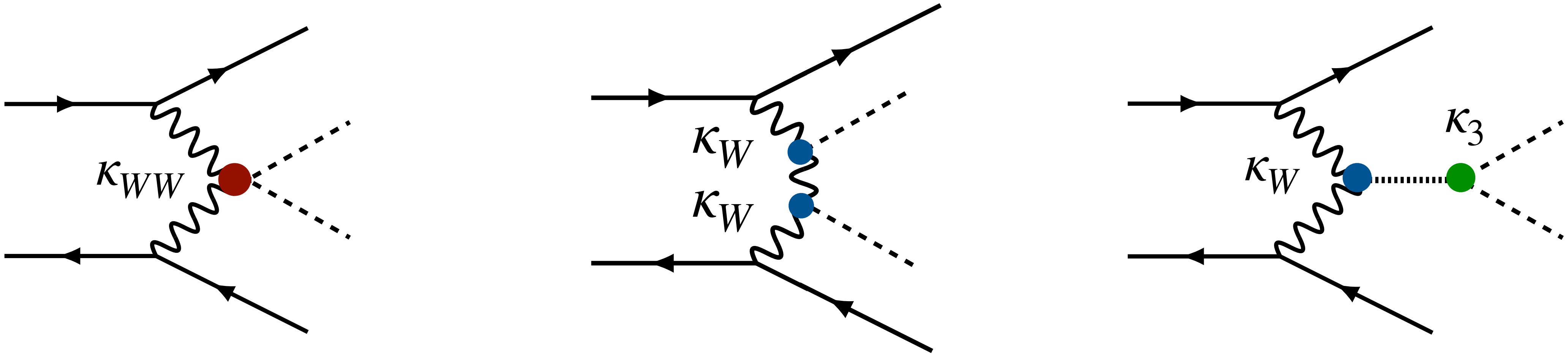
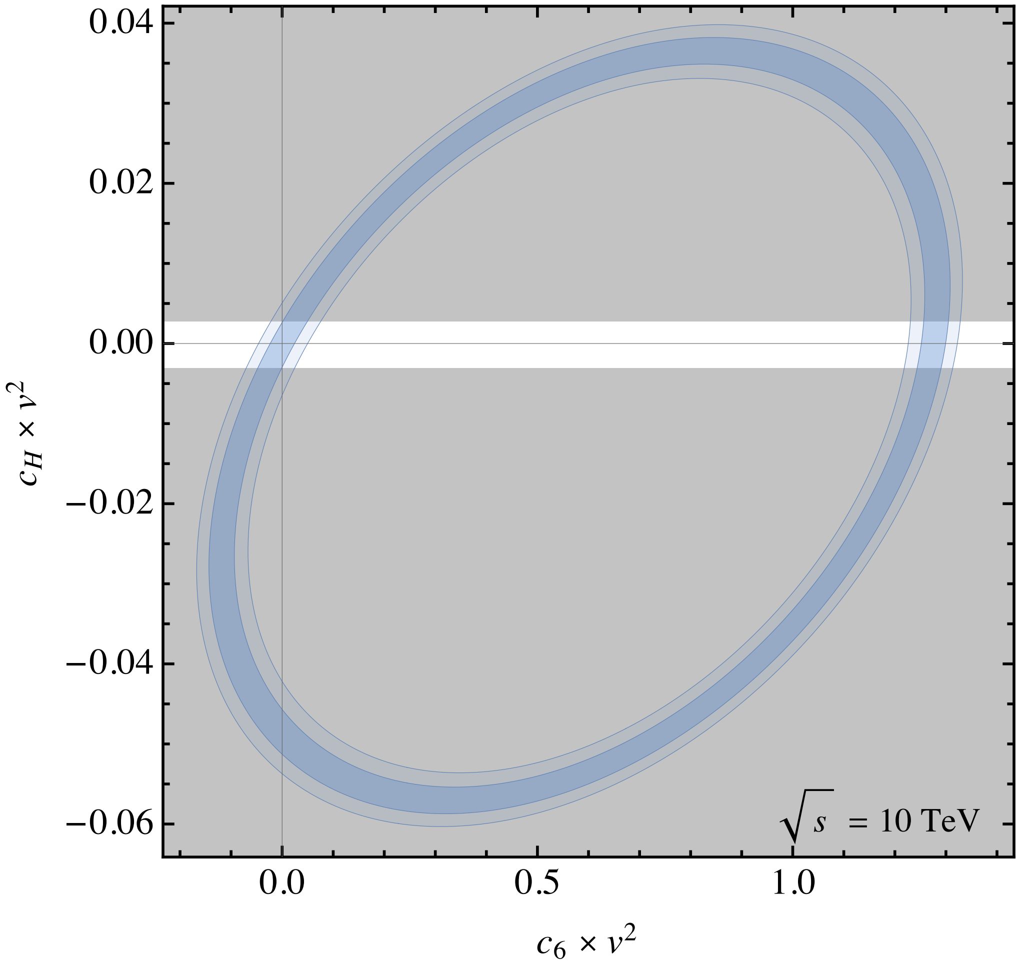




large degeneracy in total cross-section

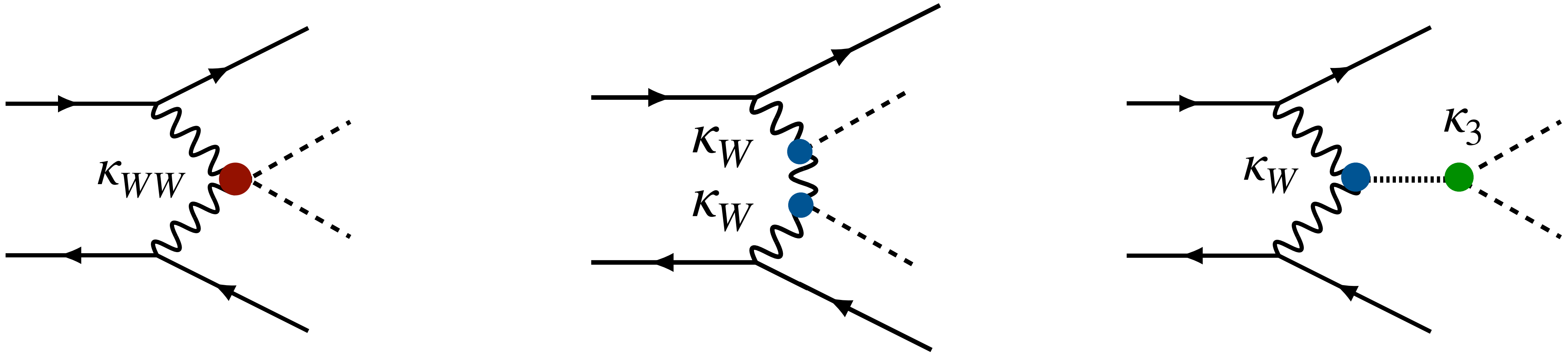
- Two dim. 6 operators:

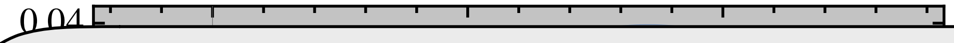
$$\mathcal{O}_6 = -\lambda |H|^6 \qquad \mathcal{O}_H = \frac{1}{2}\left(\partial_\mu |H|^2\right)^2$$

C_H can be constrained from Higgs couplings (but indirect measurement)

Double Higgs production

- Double Higgs production depends on trilinear coupling κ_3 but also on W-boson couplings κ_W, κ_{WW} that enter the production cross-section



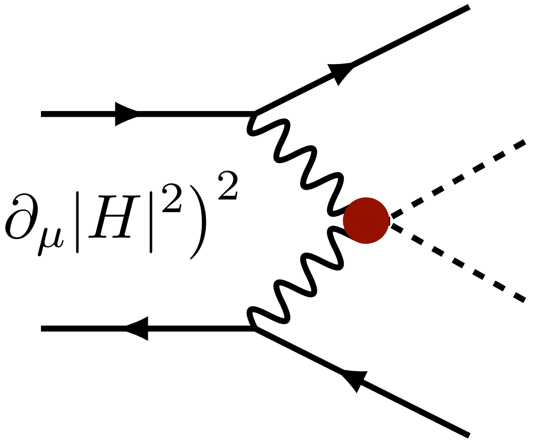


Higgs physics doesn't mean just couplings. There's much more information in the energy dependence of the interactions! (form factors)

Double Higgs at high mass

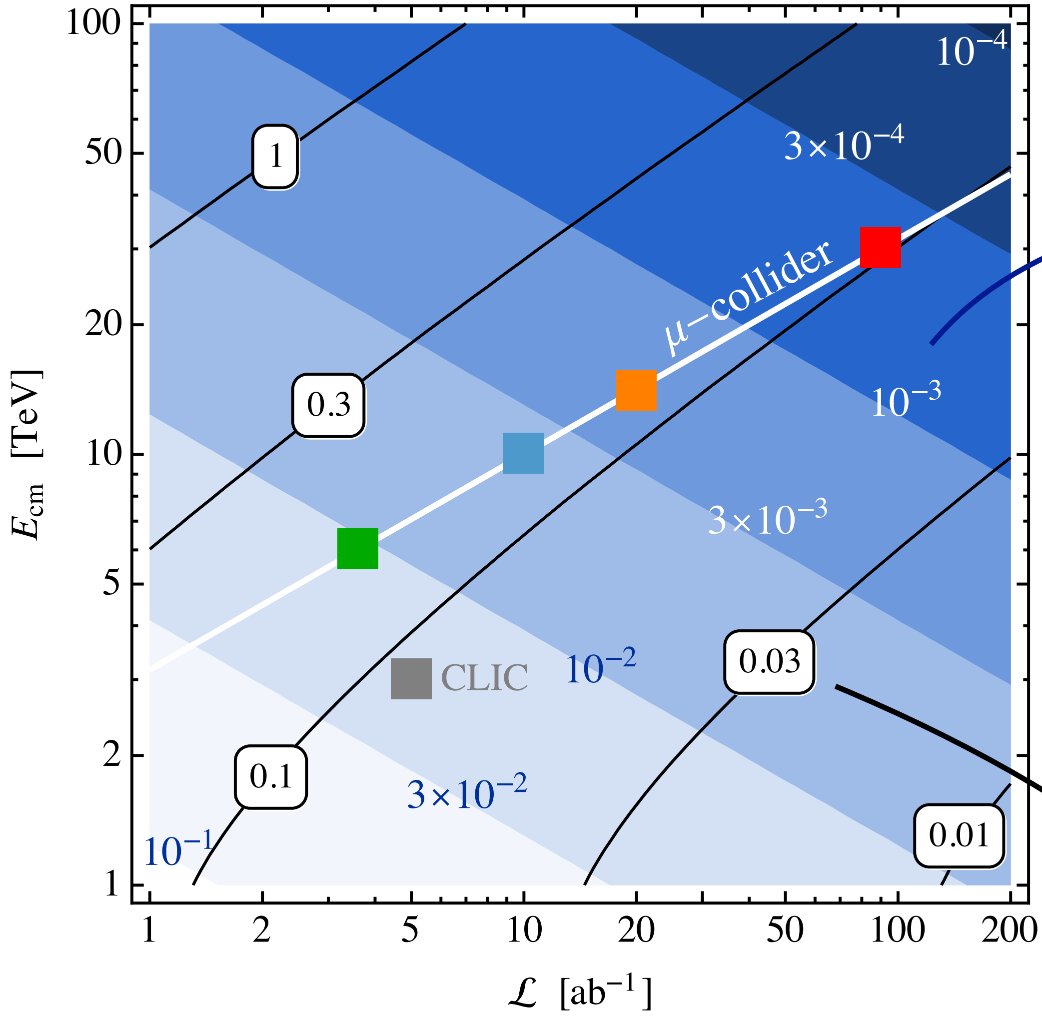
- NP contribution from $\mathscr{O}_H$ (equivalently κ_W, κ_{WW}) grows as E^2: high mass tail gives a *direct* measurement of C_H

High-energy WW → *hh* more sensitive than Higgs pole physics at energies ≳ 10 TeV



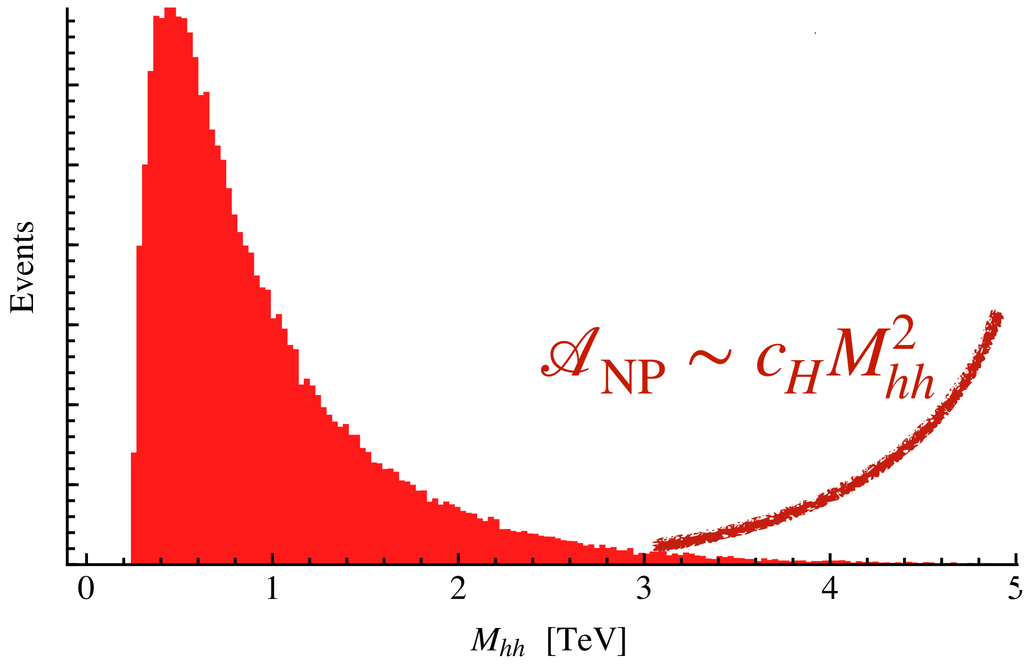
$$\mathcal{O}_H = \frac{1}{2}\left(\partial_\mu |H|^2\right)^2$$

B, Franceschini, Wulzer 2012.11555



$\xi \equiv C_H v^2$

$\mu^+\mu^- \to hh\nu\bar{\nu}$



(see also Contino et al. 1309.7038)

S/B low-precision measurement

EW precision

- Higgs & EWSB physics ⟷ EW precision measurements

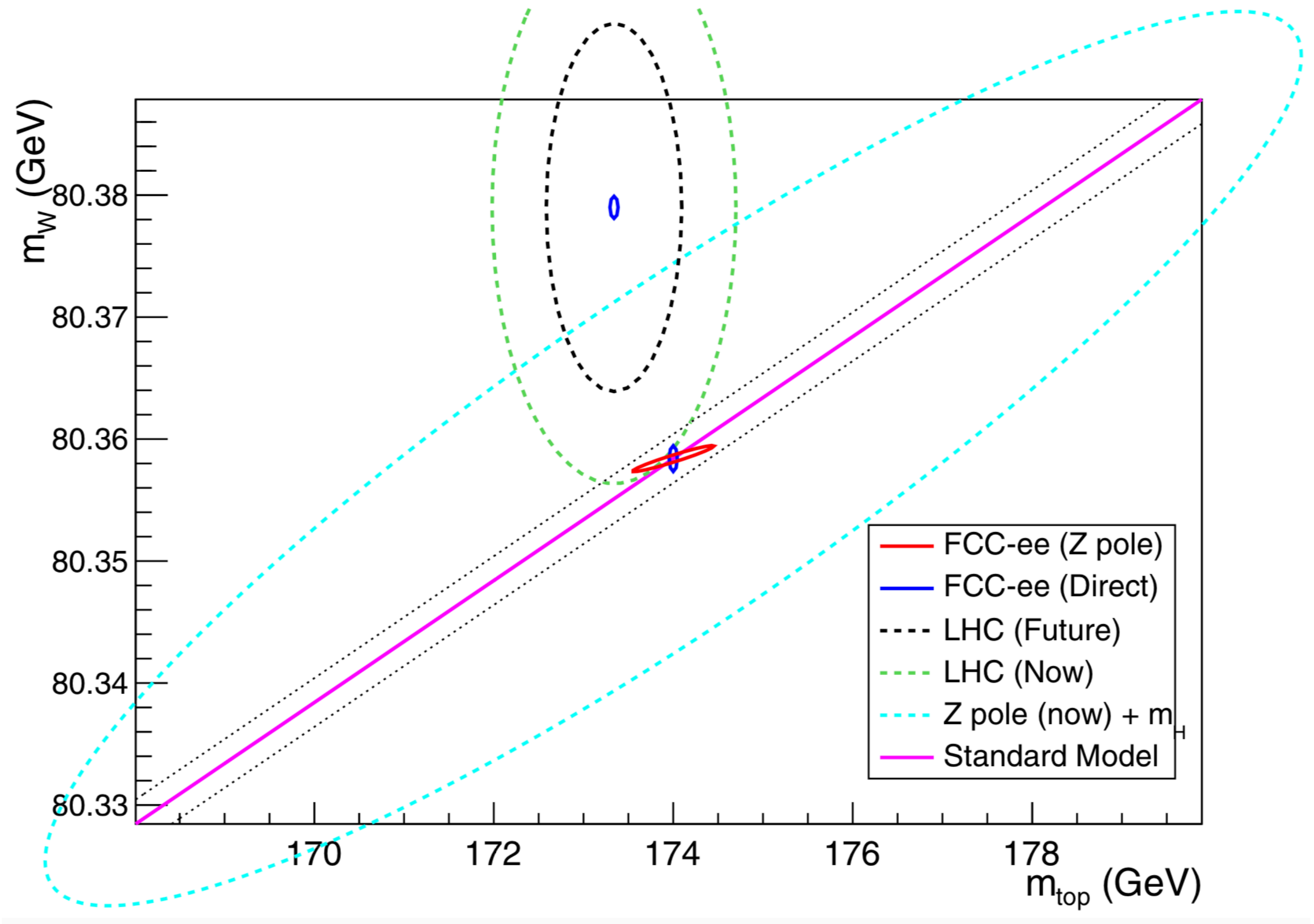
$\Delta\rho$

$$\mathcal{O}_T = \left(H^\dagger D^\mu H\right)^2$$

$\sin^2\theta_{\text{eff}}$

$$\mathcal{O}_W = \left(H^\dagger \sigma^a D^\mu H\right) D^\nu W^a_{\mu\nu}$$

$$\mathcal{O}_B = \left(H^\dagger D^\mu H\right) \partial^\nu B_{\mu\nu}$$



- **FCC-ee: 6 x 10^{12} Z bosons**

ultimate precision at the Z pole, limited by syst. and th. errors

$$\Delta\hat{S} \sim \frac{m_W^2}{M_{\text{NP}}^2} \lesssim \text{few} \times 10^{-5}$$

$\longrightarrow$ $M_{\text{NP}} \gtrsim$ **12 TeV**

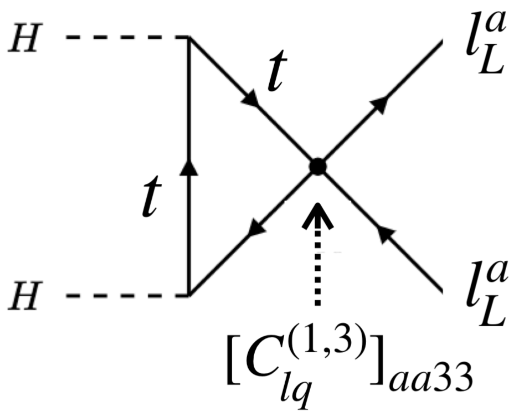
No other machine can reach this precision in Z, W physics

EW precision

- In general, several more operators enter the EW fit

4-fermion interactions affect EW observables through one loop RGE

2311.00020, 1704.04504



$\dashrightarrow$ $[C^{(1,3)}_{Hl}]_{aa}$

rates and asymmetries
in $Z \to \ell\ell$

$b \to c\ell\nu$ decays,
LH current

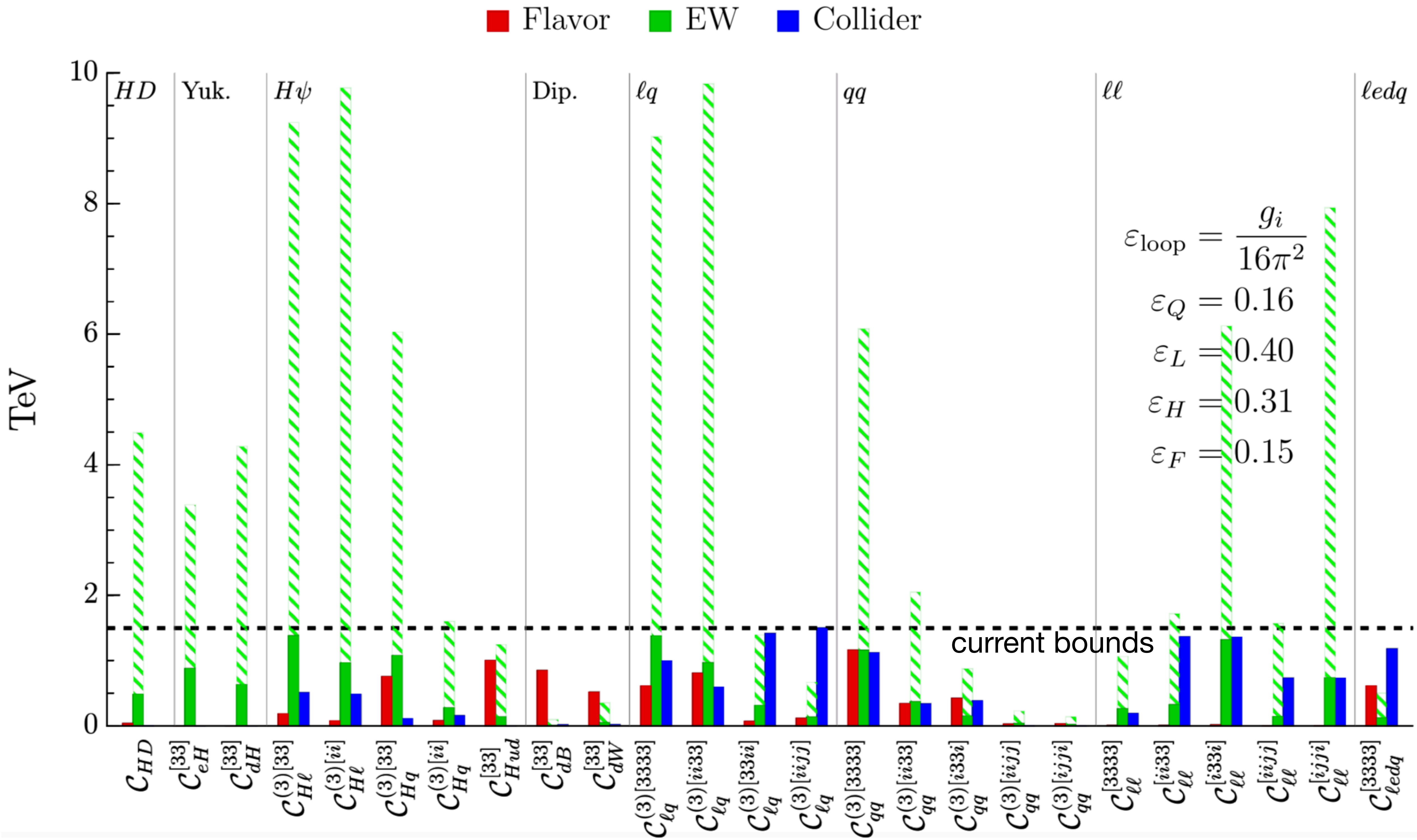
Why 10^{12} Z bosons?

- Lepton asymmetries are small: $N_{\text{events}} = N_Z \times \text{BR}(Z \to \ell^+\ell^-) \times A_\ell \sim 3 \times 10^{-4}\, N_Z$

$\Longrightarrow$ $N_Z \approx 10^{12}$ for 10^{-4} precision.

EW precision

- ✦ U(2)³ flavor symmetry + suppression of light gen. + some flavor alignment



Allwicher, Cornella, Isidori, Stefanek 2311.00020

The need for a high-energy collider

Eventually we'll need to measure physics at higher energy to improve!

- High-rate measurements eventually limited by **systematics**
- Precision measurements need to be matched with **SM theory** predictions of comparable precision $\Delta\hat{S} \lesssim 10^{-5} \longrightarrow$ NNLO EW

If a deviation is seen indirectly

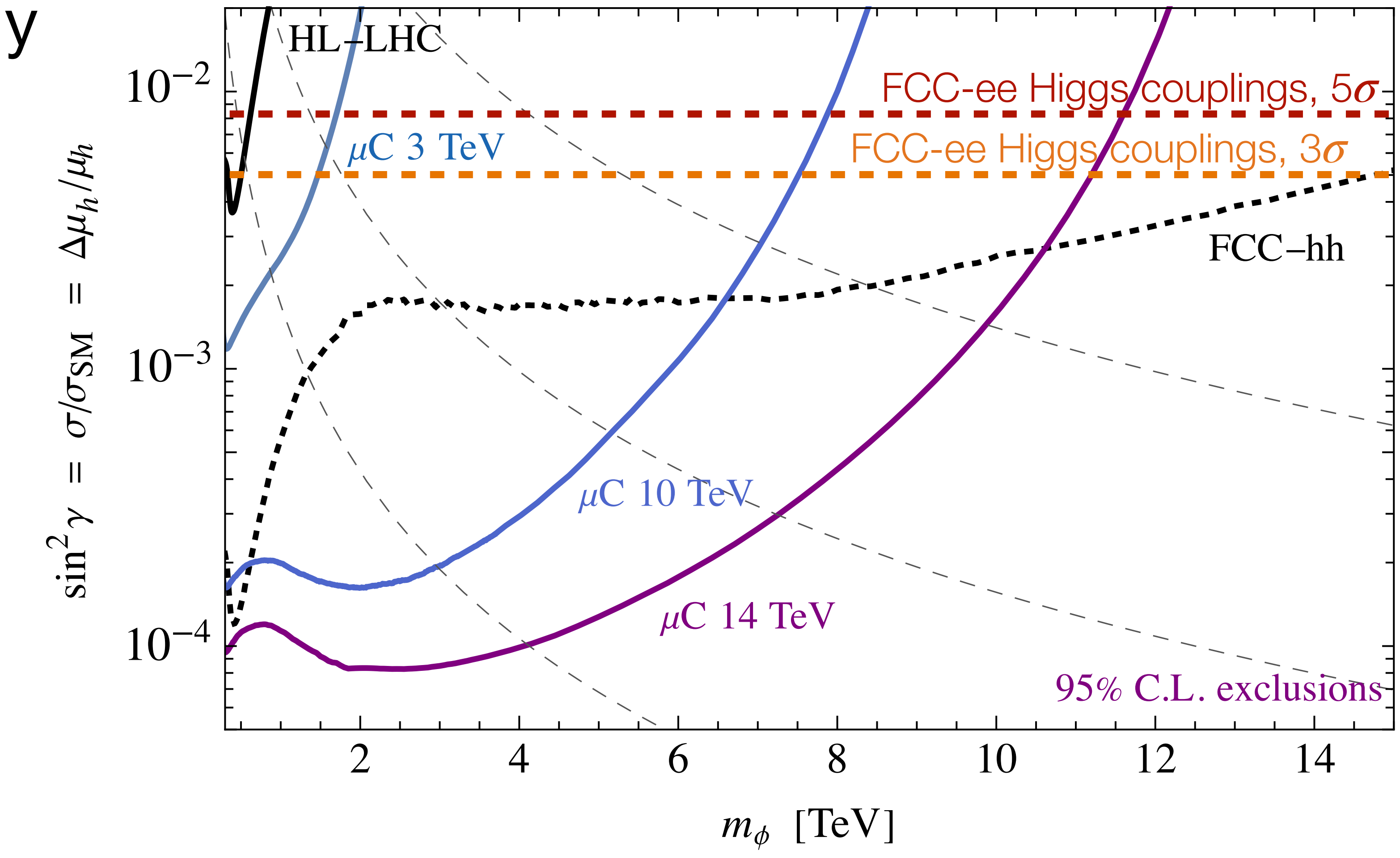
(in Higgs, EW, flavor…),

it will be crucial to be able

to study the related

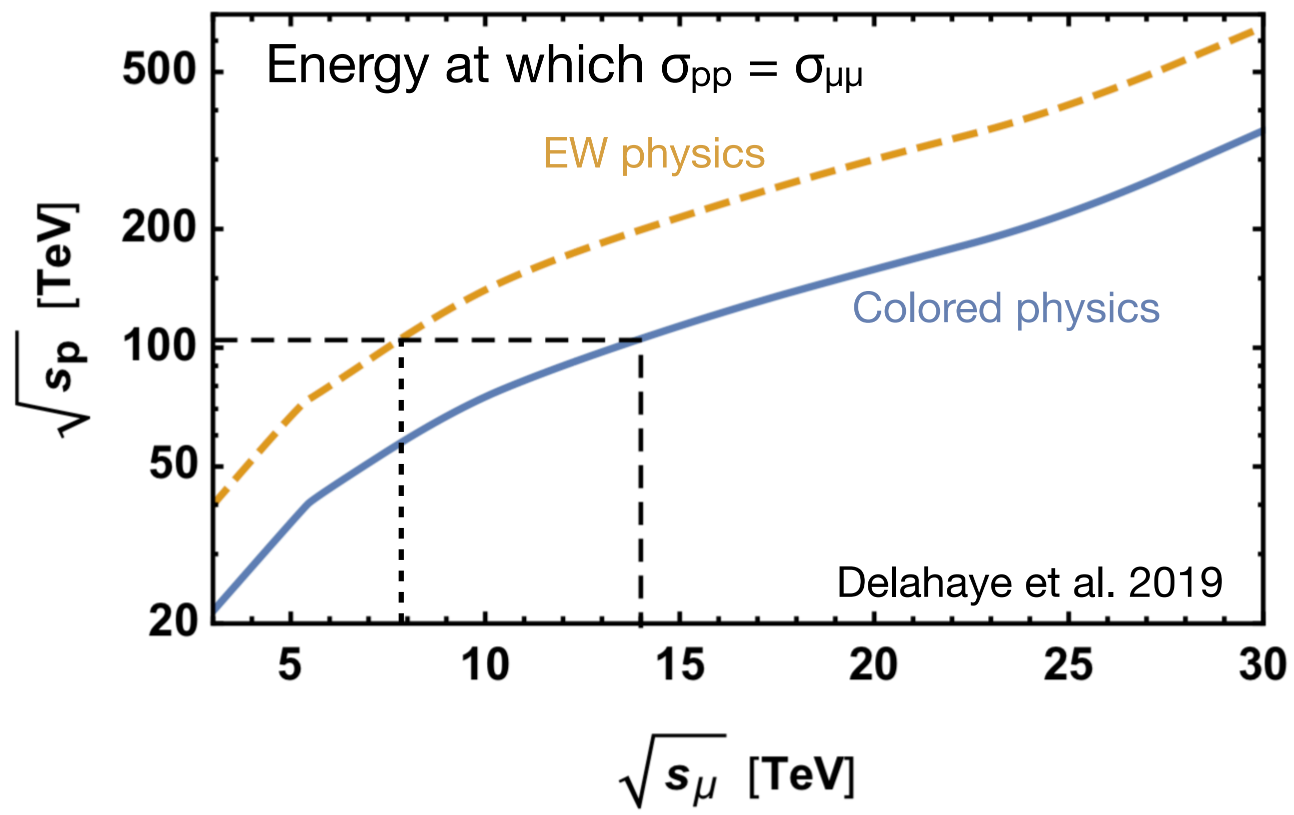
new physics directly!

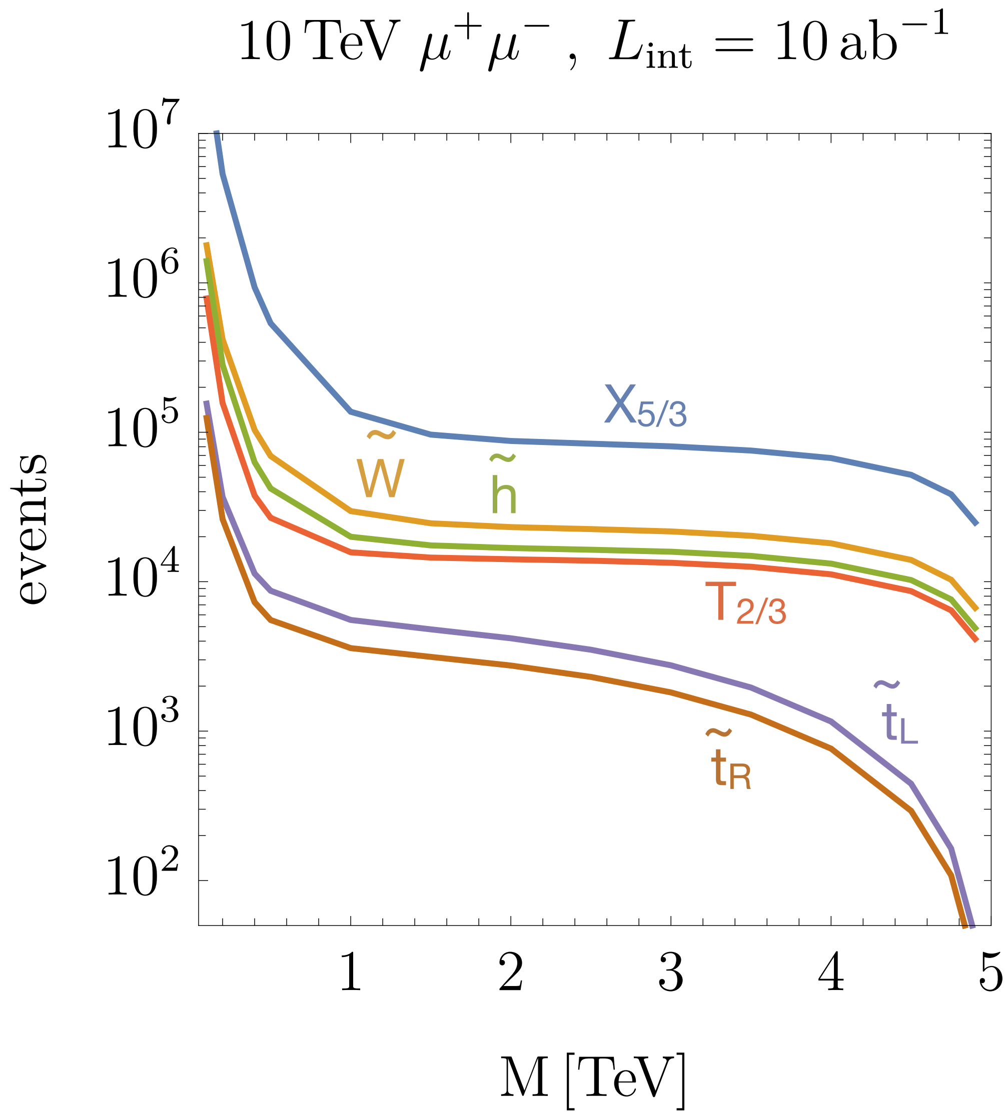
Higgs + Singlet scalar 1807.04743

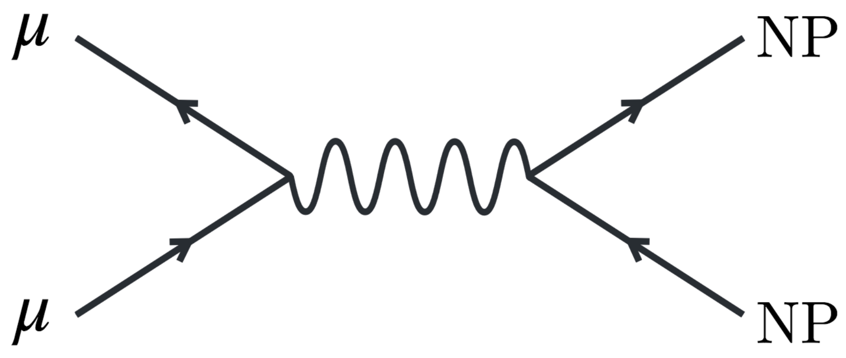


Direct searches

- Main motivation for a high energy lepton collider: produce pairs of EW particles *up to kinematical threshold* (no loss of energy due to parton distribution functions)



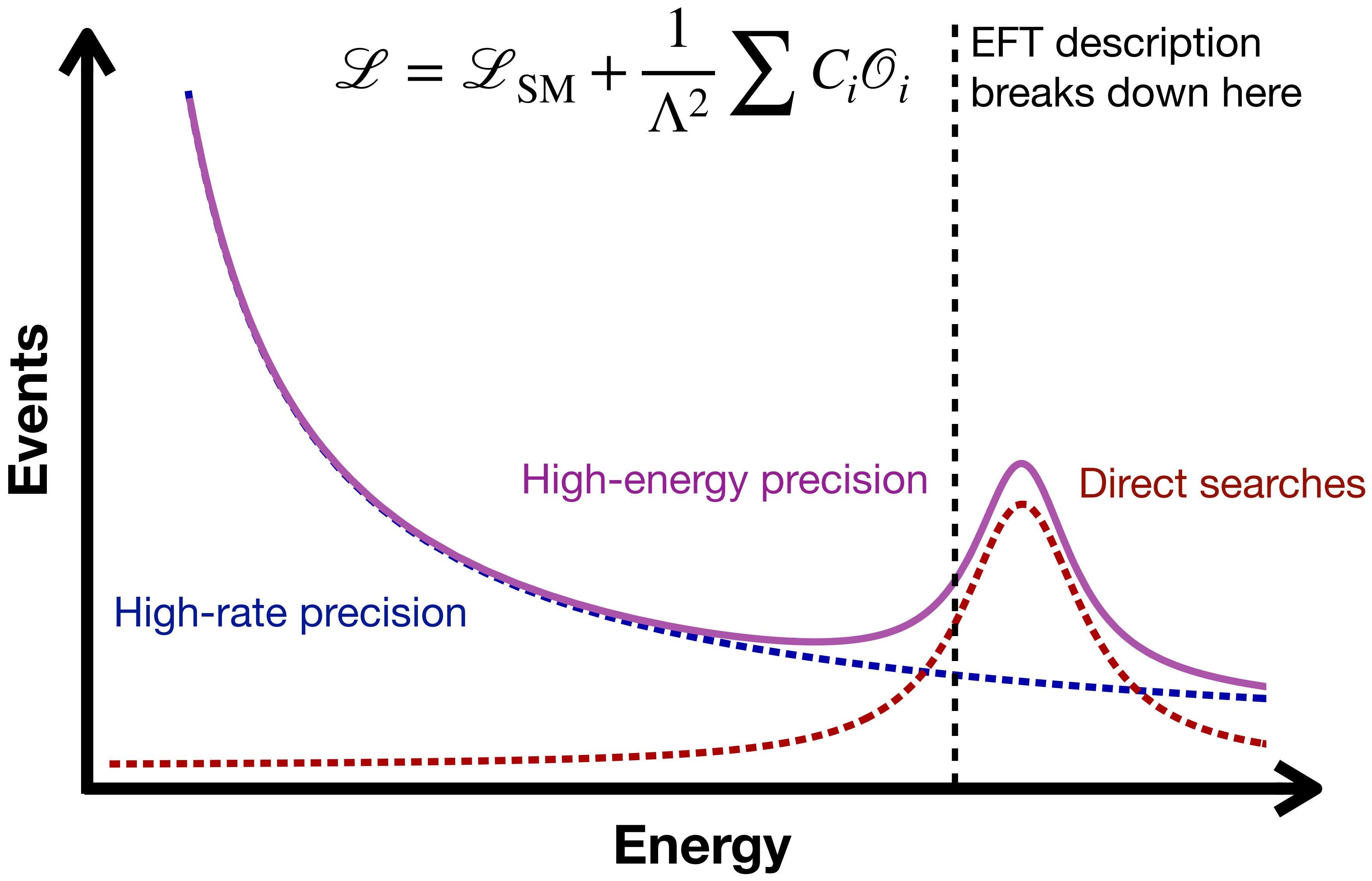




☛ **Directly explore physics at 10+ TeV!**

EW precision at high-energy

- NP effects are more important at high energies: *energy helps accuracy*

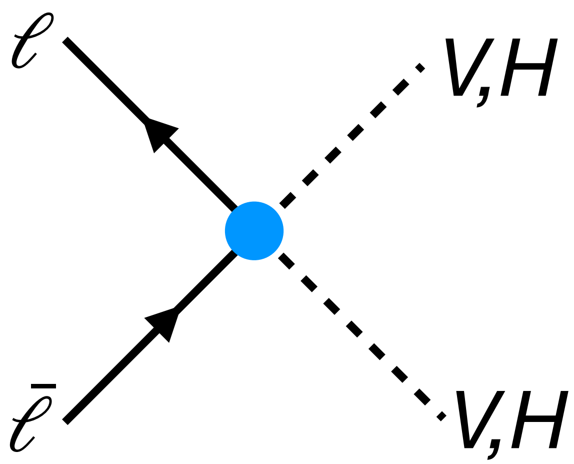


$$\frac{\Delta\sigma(E)}{\sigma_{SM}(E)} \propto \frac{E^2}{\Lambda^2_{BSM}} \approx \begin{cases} 10^{-6}, & E \sim 100\,\mathrm{GeV} \\ 10^{-2}, & E \sim 10\,\mathrm{TeV} \end{cases}$$

Farina et al. 1609.08157
Franceschini et al. 1712.01310
B, Franceschini, Wulzer 2012.11555

Example: high-energy di-bosons

- Longitudinal 2 → 2 scattering amplitudes at high energy:



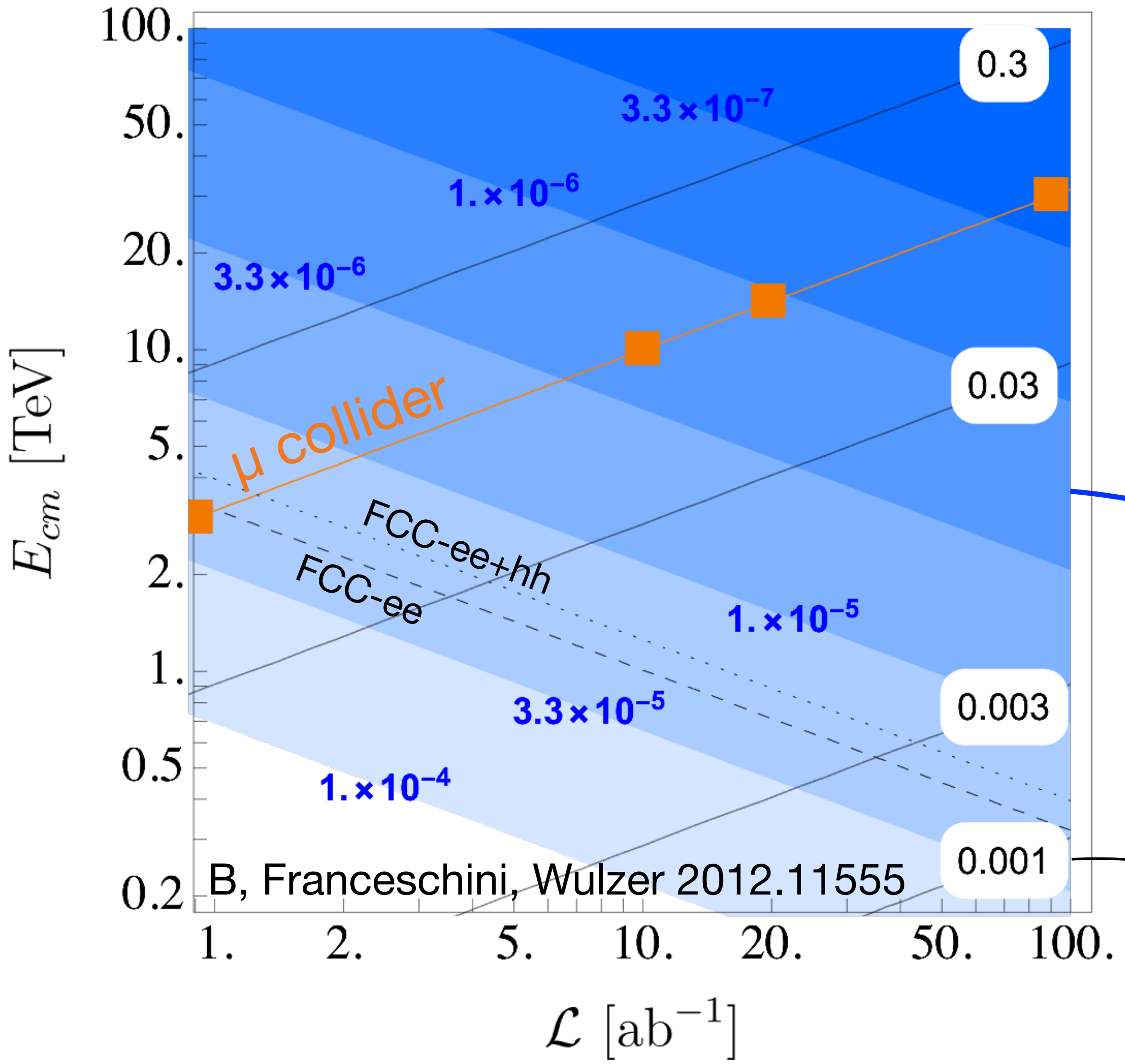
$$\ell^+\ell^- \to W_L^+W_L^-$$

$$\ell^+\ell^- \to Z_L H$$

Determined by the same two operators that affect also EWPT (in flavor-universal theories):

$$\mathcal{O}_W = \left(H^\dagger \sigma^a D^\mu H\right) D^\nu W^a_{\mu\nu}$$

$$\mathcal{O}_B = \left(H^\dagger D^\mu H\right) \partial^\nu B_{\mu\nu}$$



B, Franceschini, Wulzer 2012.11555

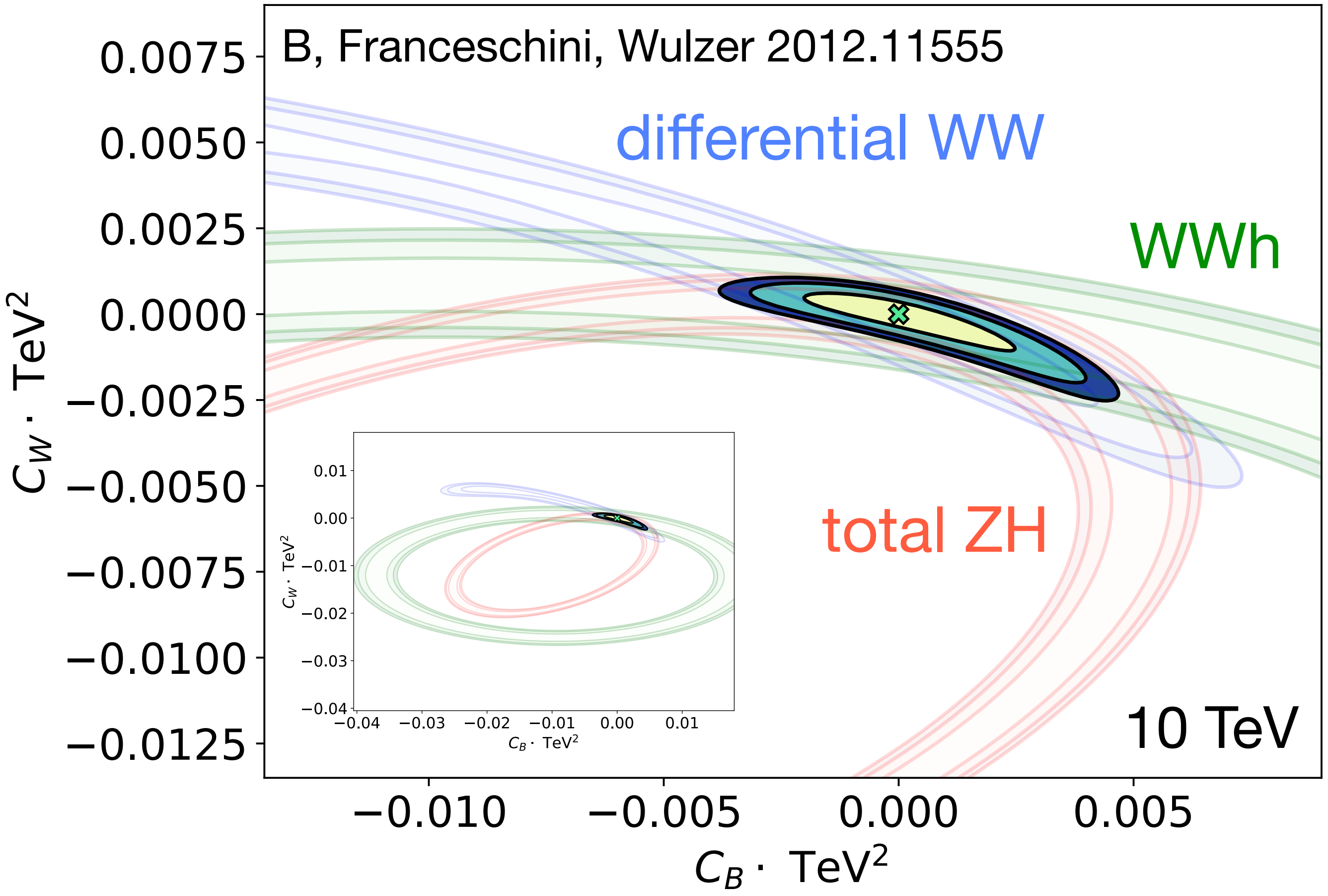
related with Z-pole observables

$$\hat{S} = m_W^2 (C_W + C_B)$$

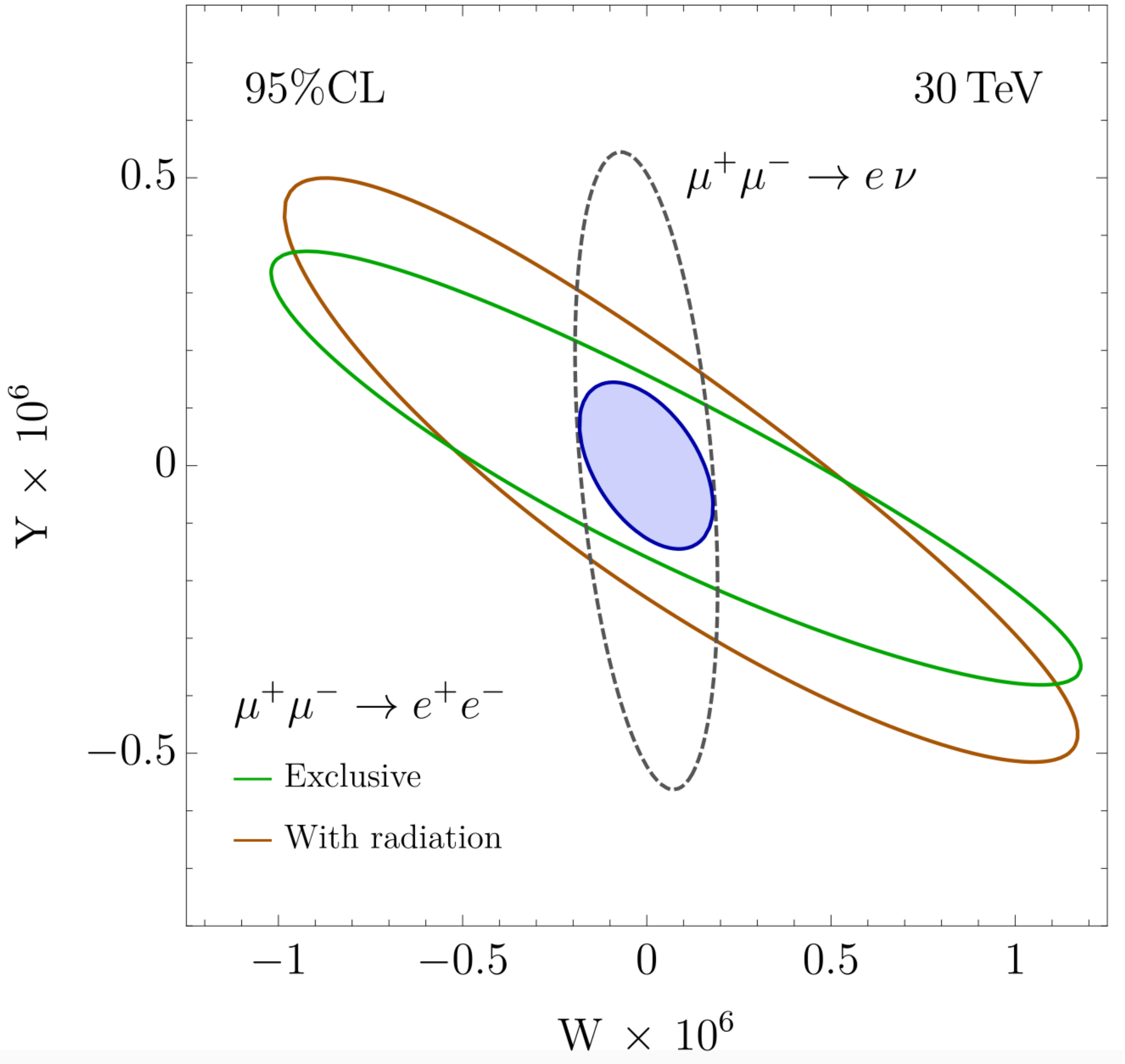
LEP: 10^{-3}, FCC: few 10^{-5} **MuC:** 10^{-6}

precision of measurement

EW radiation



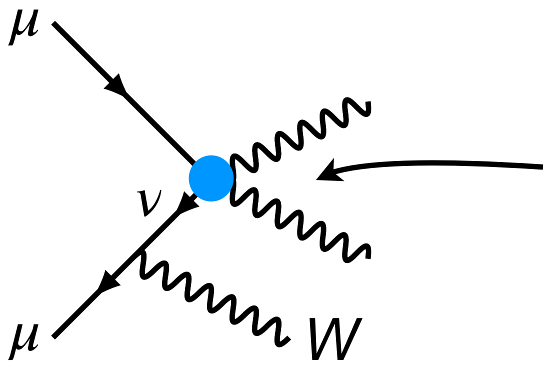
Chen, Glioti, Rattazzi, Ricci, Wulzer 2202.10509



Gauge boson radiation important:

soft W emission allows to access

charged processes $\ell\nu \to W^\pm Z, W^\pm H$

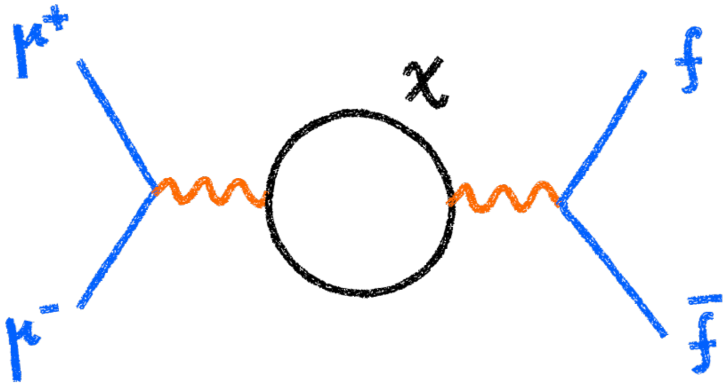


independent measurement of C_W

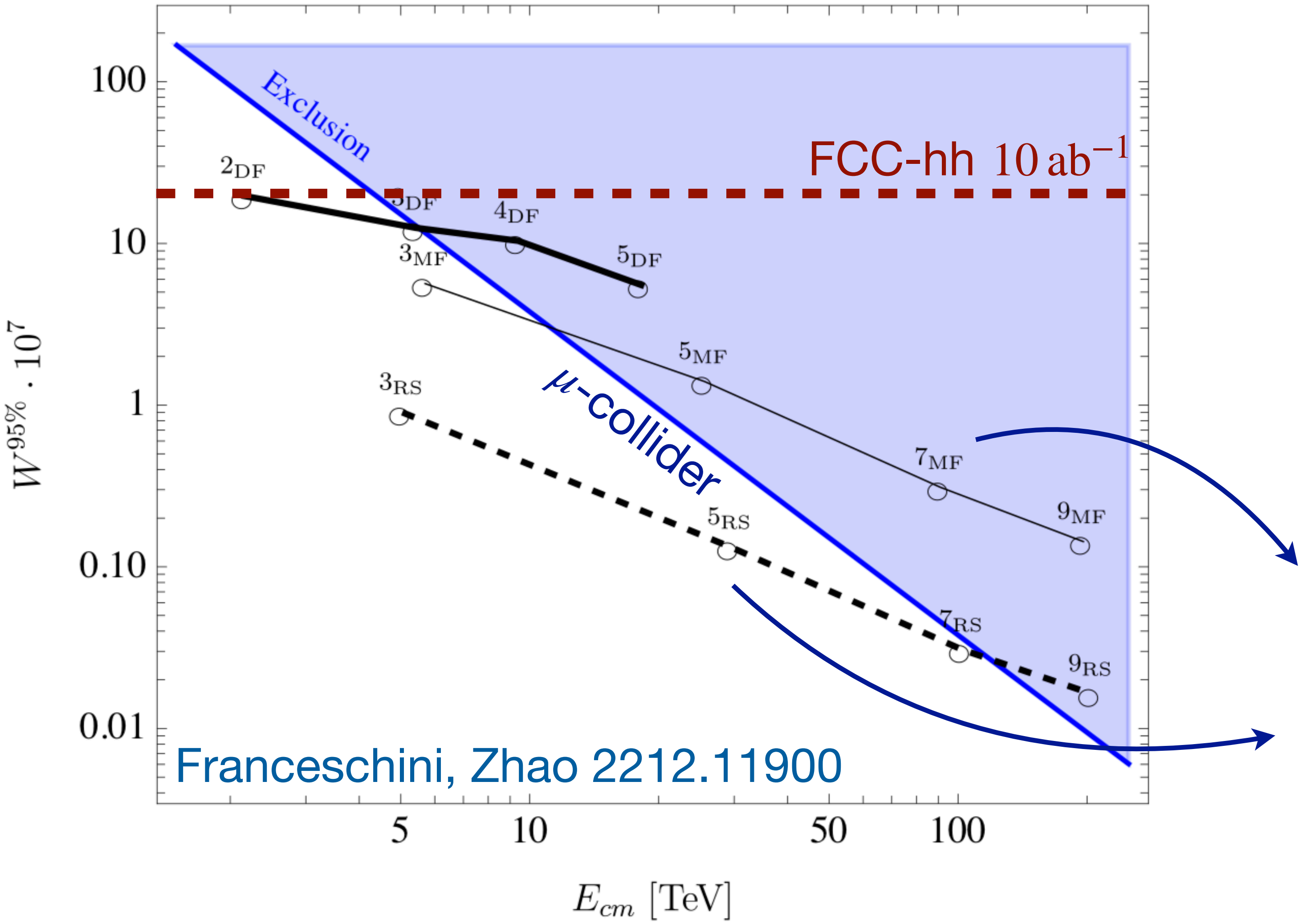
- contains new physical information!
- need to properly define inclusive observables, resummation of logs, …

EW-charged matter

- All EW multiplets contribute to high-energy 2 → 2 fermion scattering: effects that grow with energy, can be tested at μ collider



can be WIMP dark matter if M ~ few TeV



Franceschini, Zhao 2212.11900

$$\hat W \approx 10^{-7}\times\left(\frac{1\,\mathrm{TeV}}{M_{\rm DM}}\right)^2 n^3 \propto 1/n^2$$

$$\hat Y \approx 10^{-7}\times\left(\frac{1\,\mathrm{TeV}}{M_{\rm DM}}\right)^2 Y^2 n \propto 1/n^4$$

right of blue line: can be tested indirectly

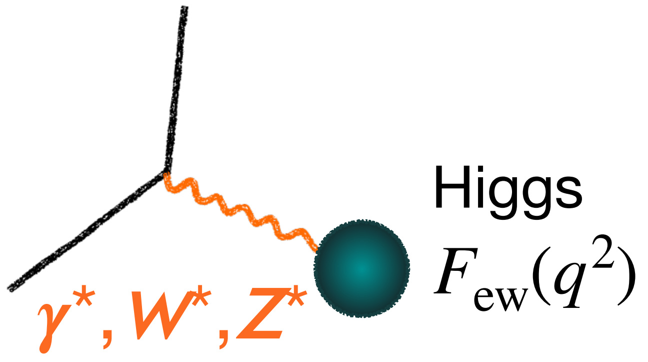
left of blue line: can be tested directly

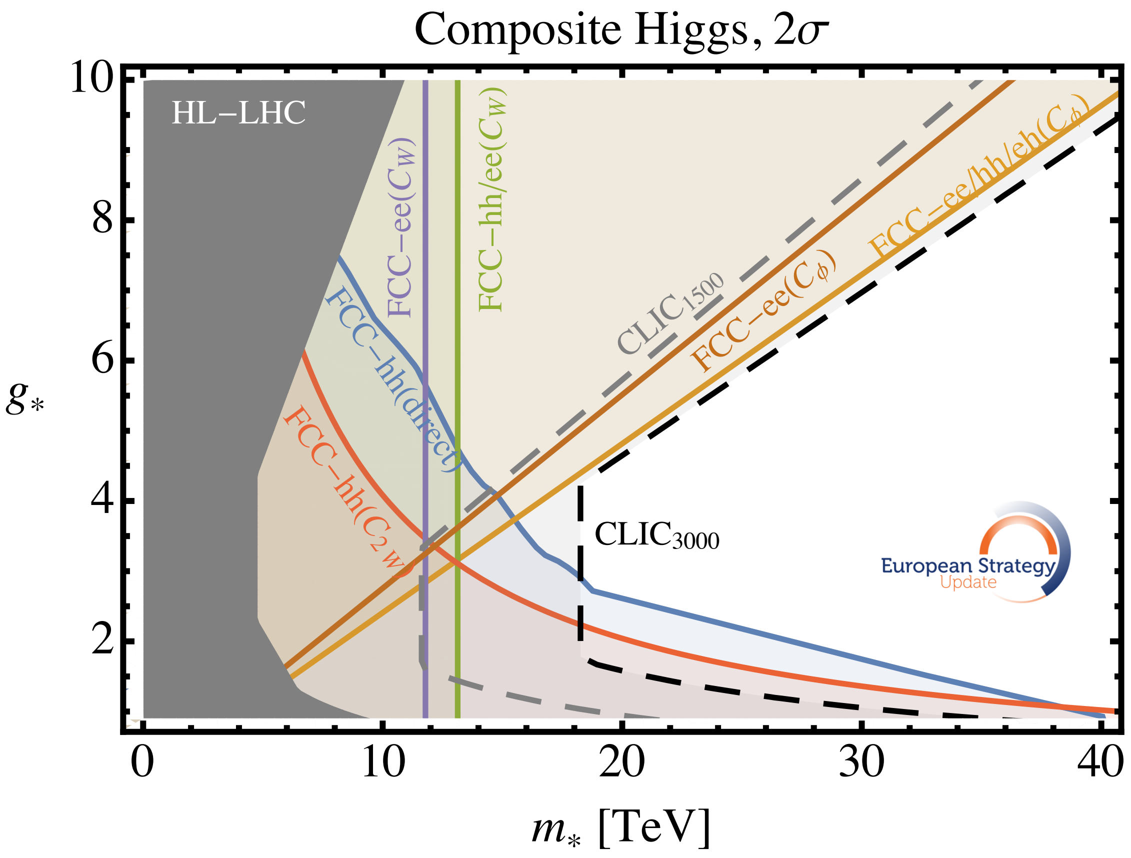
High-energy probes: EW & Higgs physics

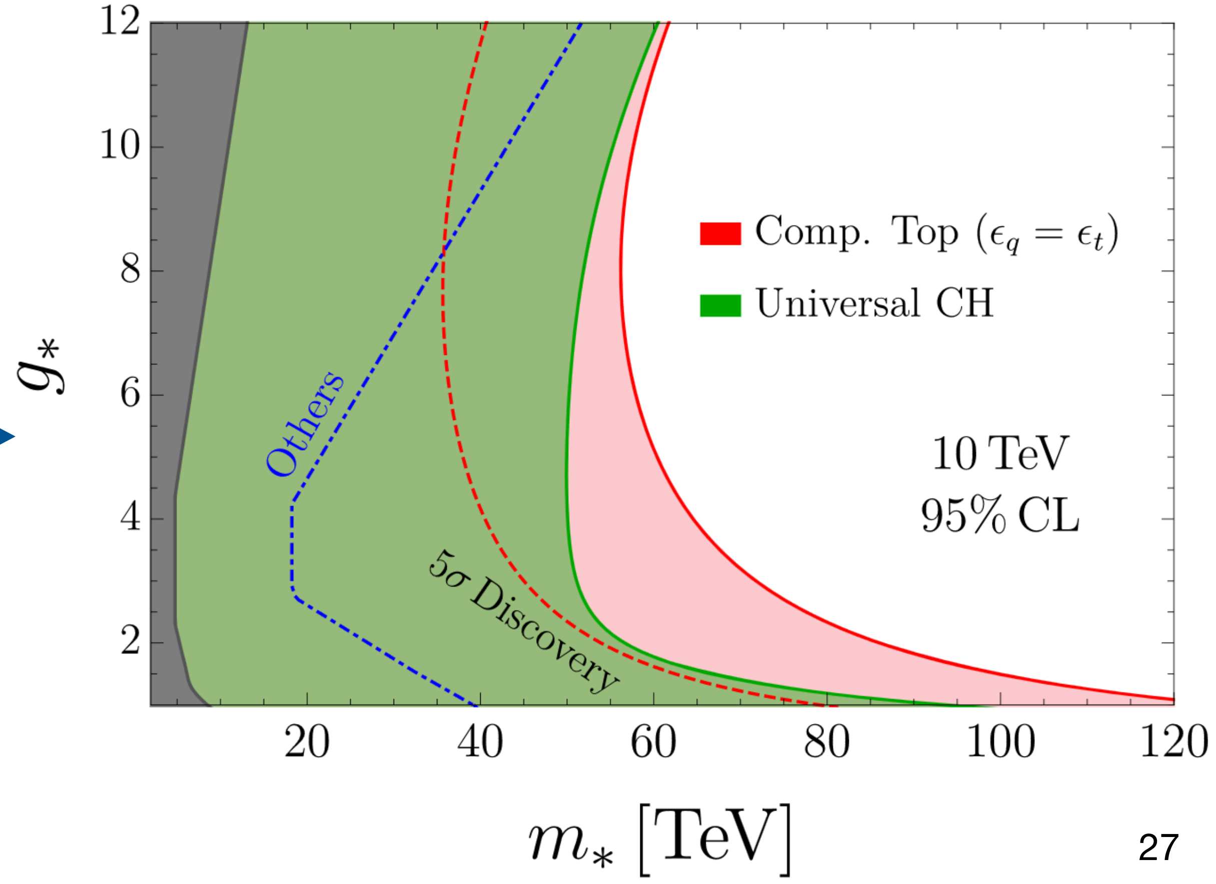
- Ultimate precision at the Z pole + Higgs couplings: the quickest way to probe new physics coupled to Higgs/EW at scales of ~ 10 TeV

- High-energy processes at a 10–30 TeV lepton collider are able to reach scales of ~ 100 TeV.

Example: new physics with mass m⋆ and coupling g⋆



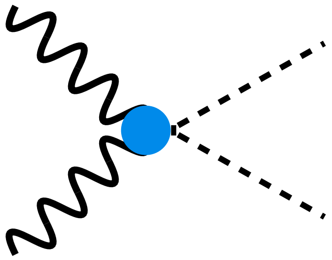




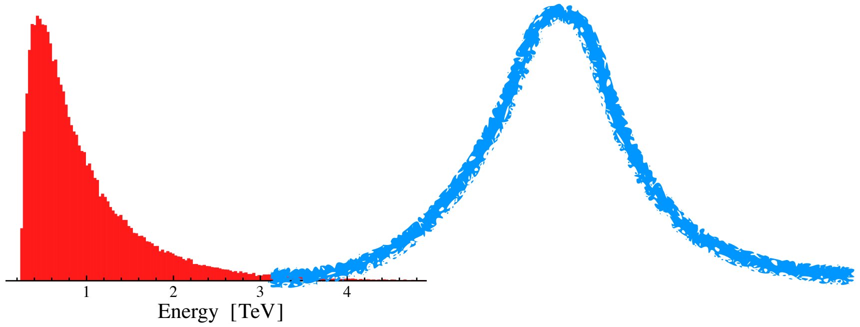
Summary

- One of the priorities for our field in the next decades will be to **explore the 10+ TeV scale.** Precision measurements might be the quickest way…

- Two complementary paths forward:



High rate



High energy

- **Low-energy e^+e^- collider:** Higgs physics at 10^{-3}, EW physics at 10^{-5}, flavor.

  The easiest way to reach 10 TeV (indirectly)

- **High-energy $\mu^+\mu^-$ collider:** collide elementary particles at the energy frontier.

  VBF: Higgs physics at 10^{-3}, Higgs self-coupling.

  High-energy: EWPT at 10^{-7}, i.e. scales > 100 TeV; EW particles at 10+ TeV.

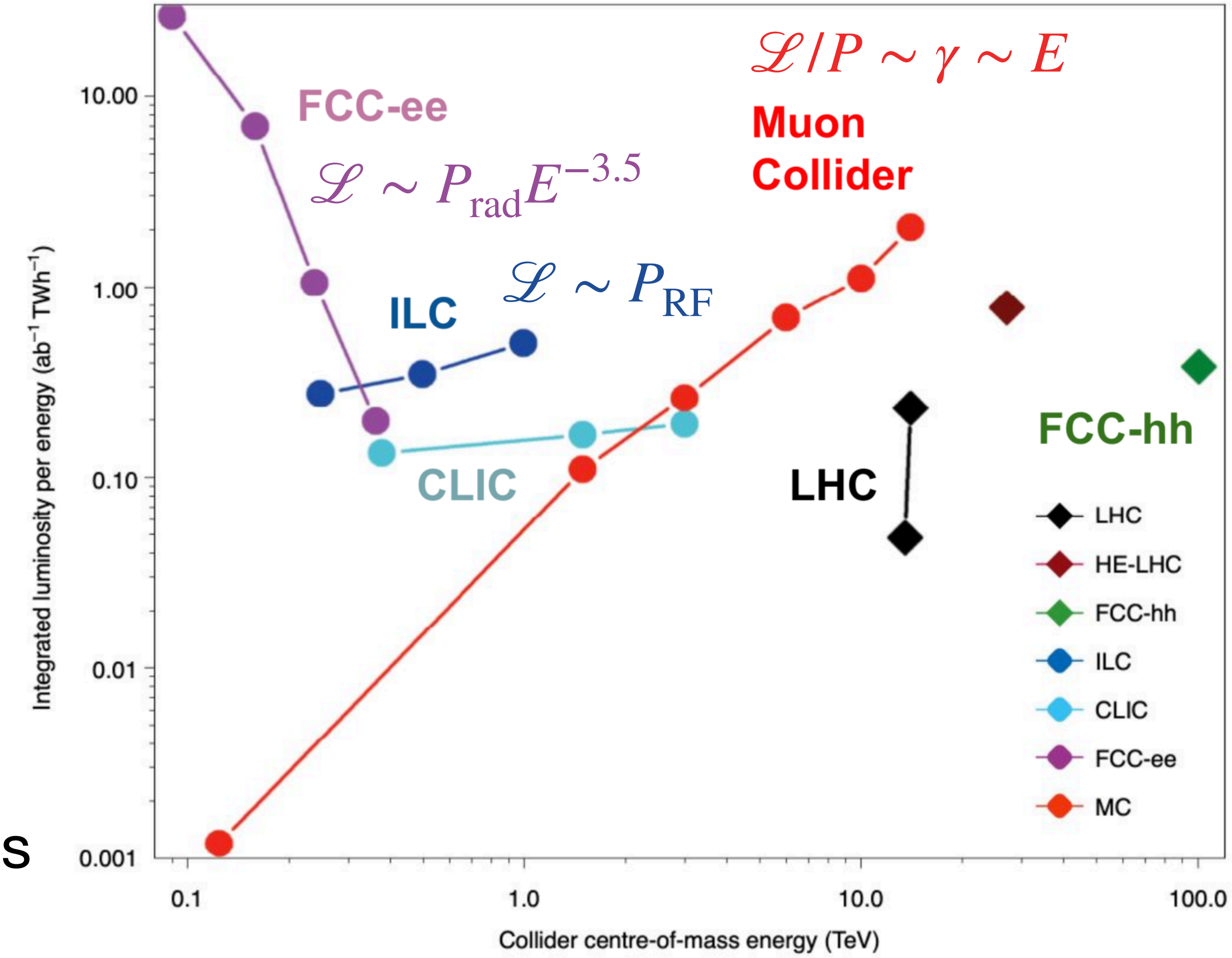
Backup

Lepton colliders

- ✦ Lepton colliders are ideal probes of short-distance physics
- ✦ Muons are elementary and heavy (207 x electrons)
  - negligible energy loss in synchrotron radiation
  - negligible beamstrahlung

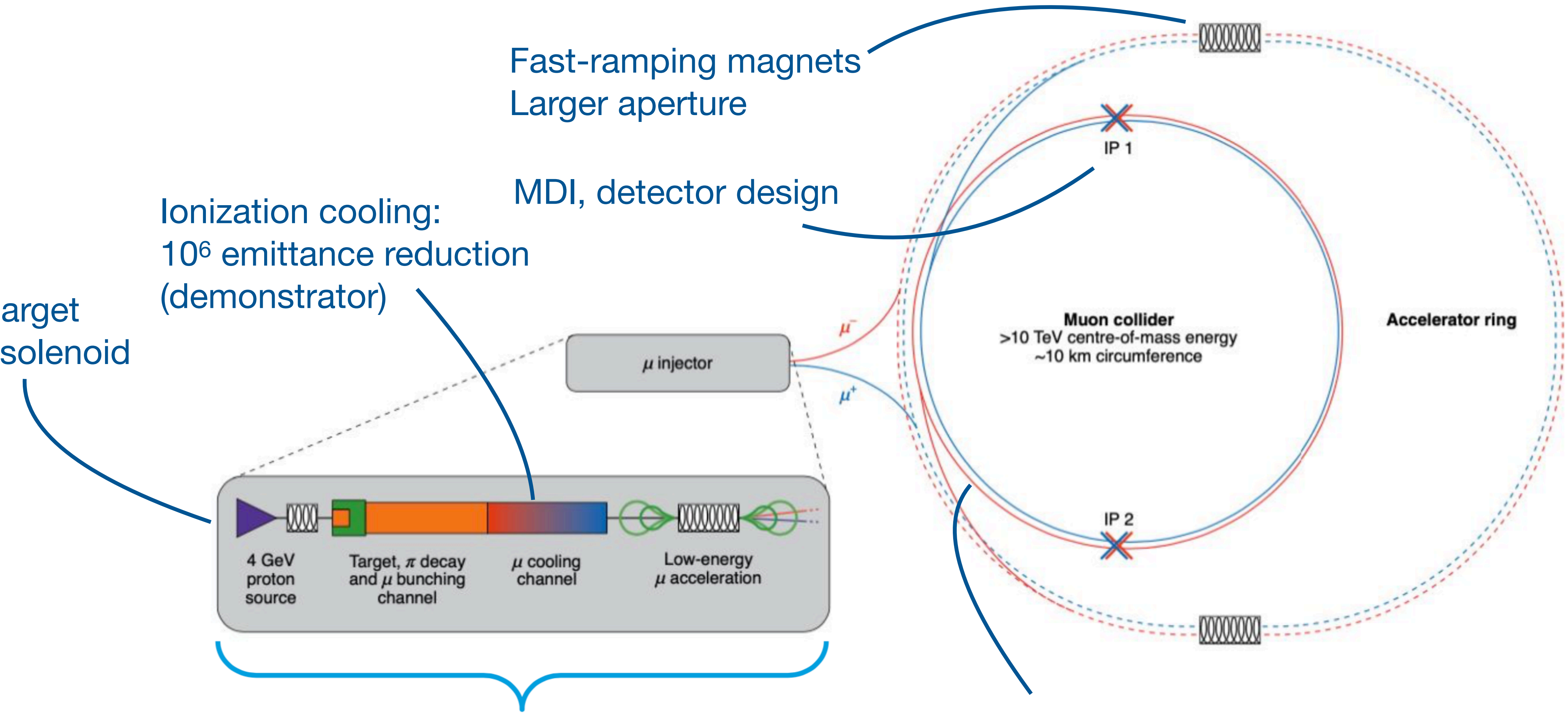
But they decay…

- ✦ Luminosity increases with the square of beam energy
  - muon lifetime increases
  - transverse emittance decreases



Muon colliders!

- A muon collider is *not science-fiction*!
- Several technical challenges that require major R&D effort



Fast-ramping magnets
Larger aperture

MDI, detector design

Ionization cooling:
10^6 emittance reduction
(demonstrator)

Few-MW target
High-field solenoid

Proton-driven scheme

Accelerator design,
mitigation systems

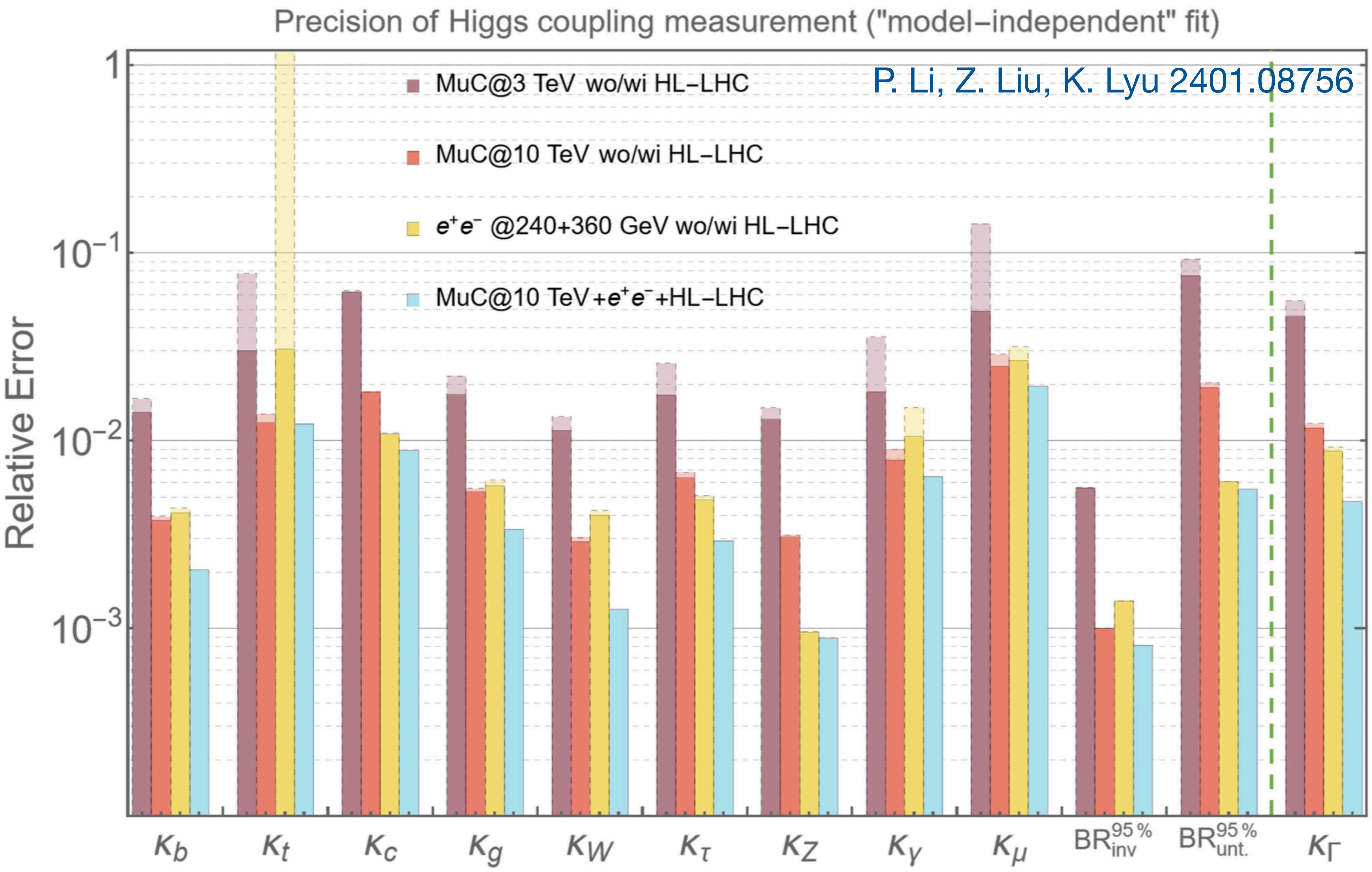
High energy lepton collider (10 TeV or more) is a dream for particle physics…

… dedicated R&D program crucial to establish feasibility in the next years!

Higgs couplings at muon collider

- A full-fledged Higgs-physics program is possible at a μC

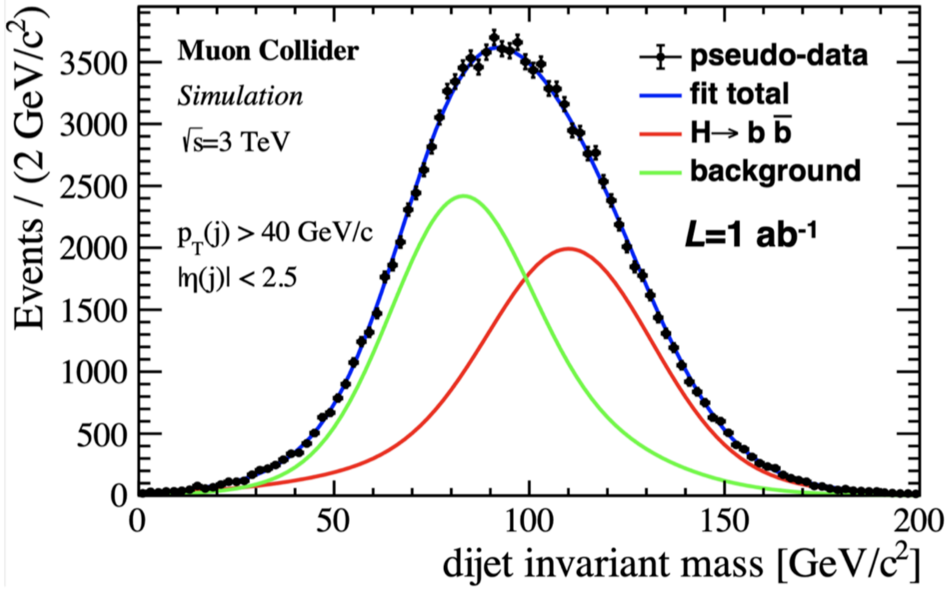
- Single Higgs couplings can more easily be studied at e+e- factory! *(most likely before a μC!)*



Single Higgs: backgrounds

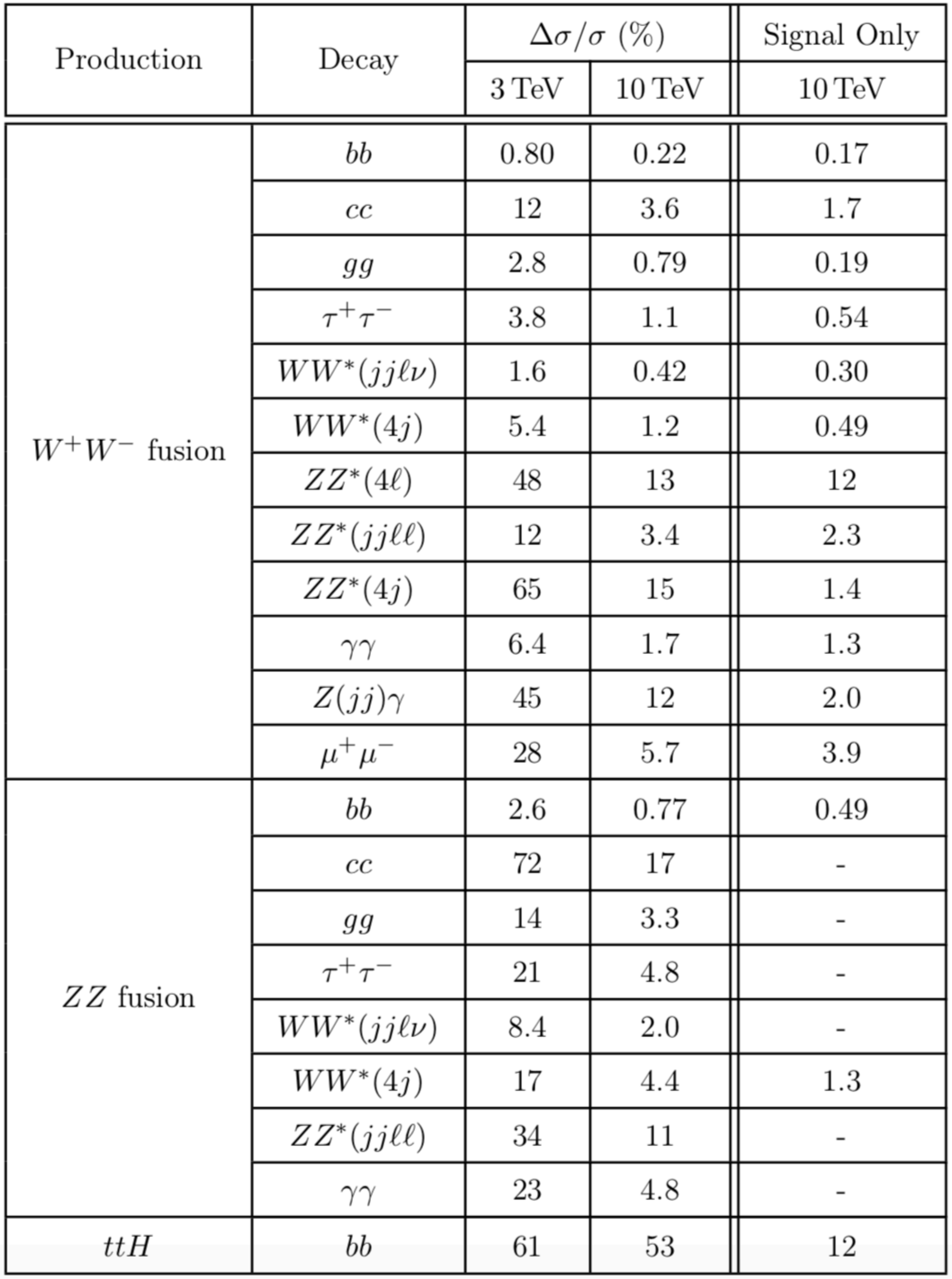
- Physics backgrounds (including the Higgs itself!)
- Beam-induced background

L. Sestini et al.



- Detector performance
  - “soft” and forward particles

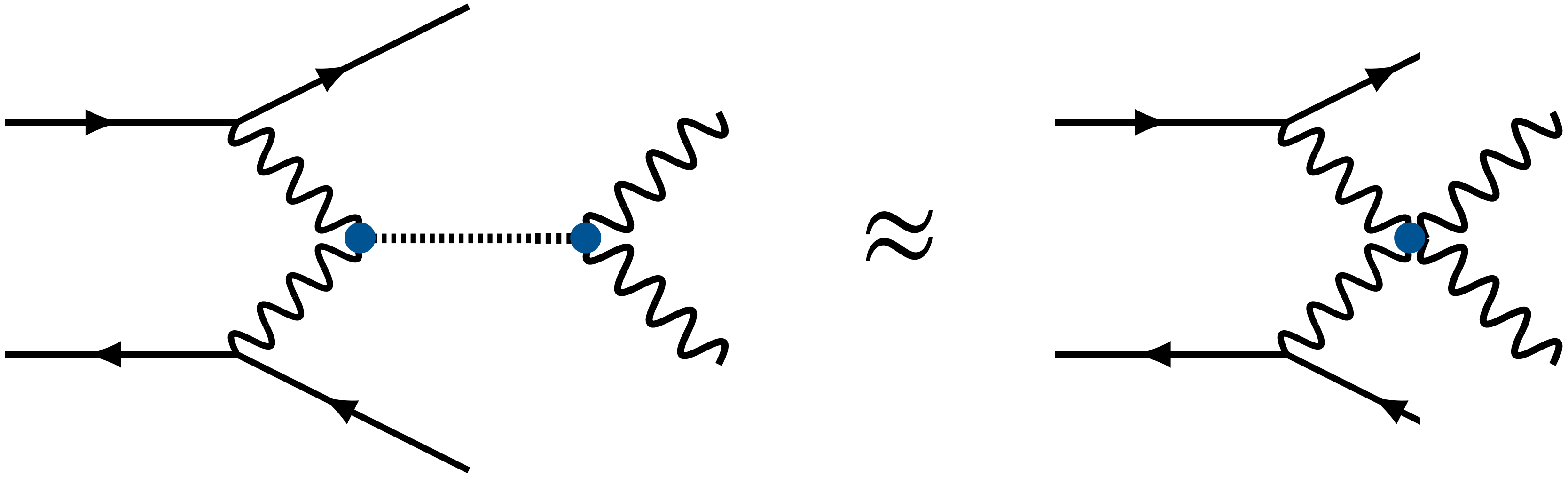
Forslund, Meade
2203.09425



Production	Decay	$\Delta\sigma/\sigma$ (%)		Signal Only
		3 TeV	10 TeV	10 TeV
W^+W^- fusion	bb	0.80	0.22	0.17
	cc	12	3.6	1.7
	gg	2.8	0.79	0.19
	$\tau^+\tau^-$	3.8	1.1	0.54
	$WW^*(jj\ell\nu)$	1.6	0.42	0.30
	$WW^*(4j)$	5.4	1.2	0.49
	$ZZ^*(4\ell)$	48	13	12
	$ZZ^*(jj\ell\ell)$	12	3.4	2.3
	$ZZ^*(4j)$	65	15	1.4
	$\gamma\gamma$	6.4	1.7	1.3
	$Z(jj)\gamma$	45	12	2.0
	$\mu^+\mu^-$	28	5.7	3.9
ZZ fusion	bb	2.6	0.77	0.49
	cc	72	17	-
	gg	14	3.3	-
	$\tau^+\tau^-$	21	4.8	-
	$WW^*(jj\ell\nu)$	8.4	2.0	-
	$WW^*(4j)$	17	4.4	1.3
	$ZZ^*(jj\ell\ell)$	34	11	-
	$\gamma\gamma$	23	4.8	-
ttH	bb	61	53	12

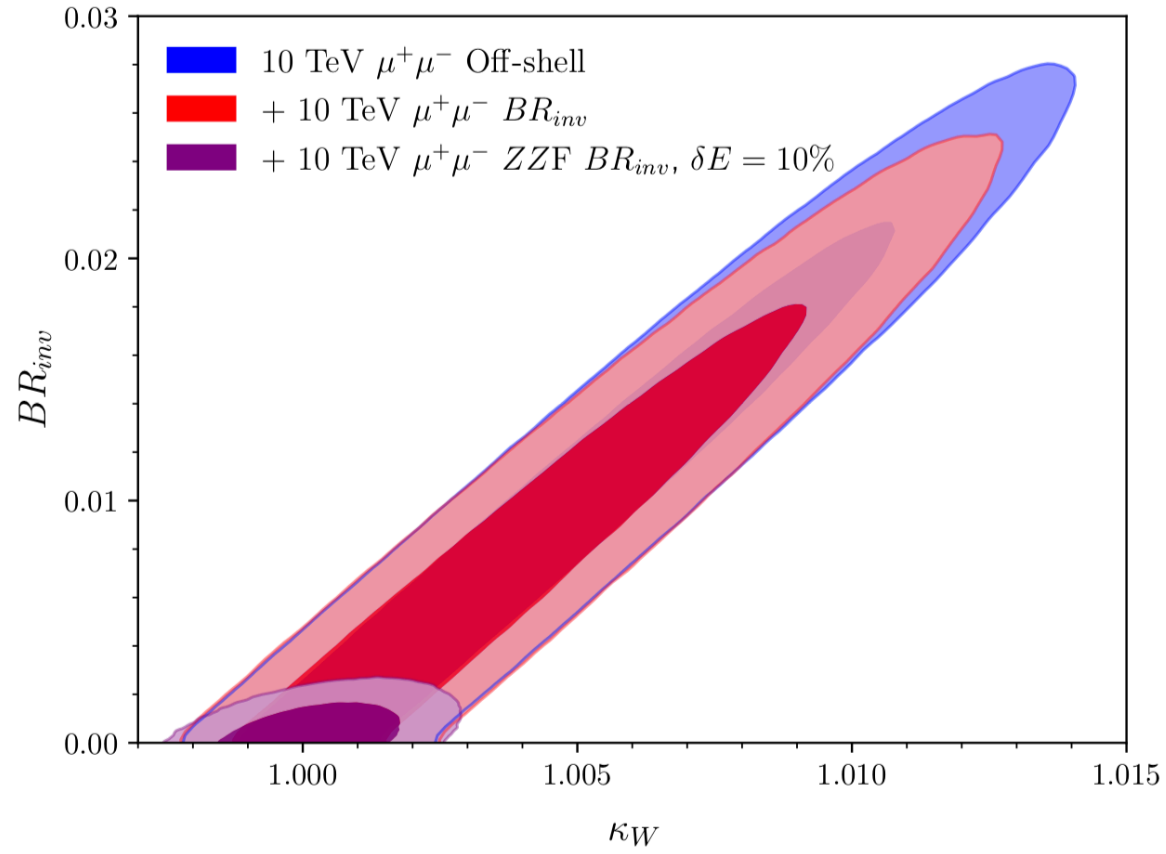
Single Higgs at high mass (off-shell)

- Off-shell single Higgs production: independent of width



$$\sim \frac{E^2}{\Lambda^4}$$

Forslund, Meade 2308.02633

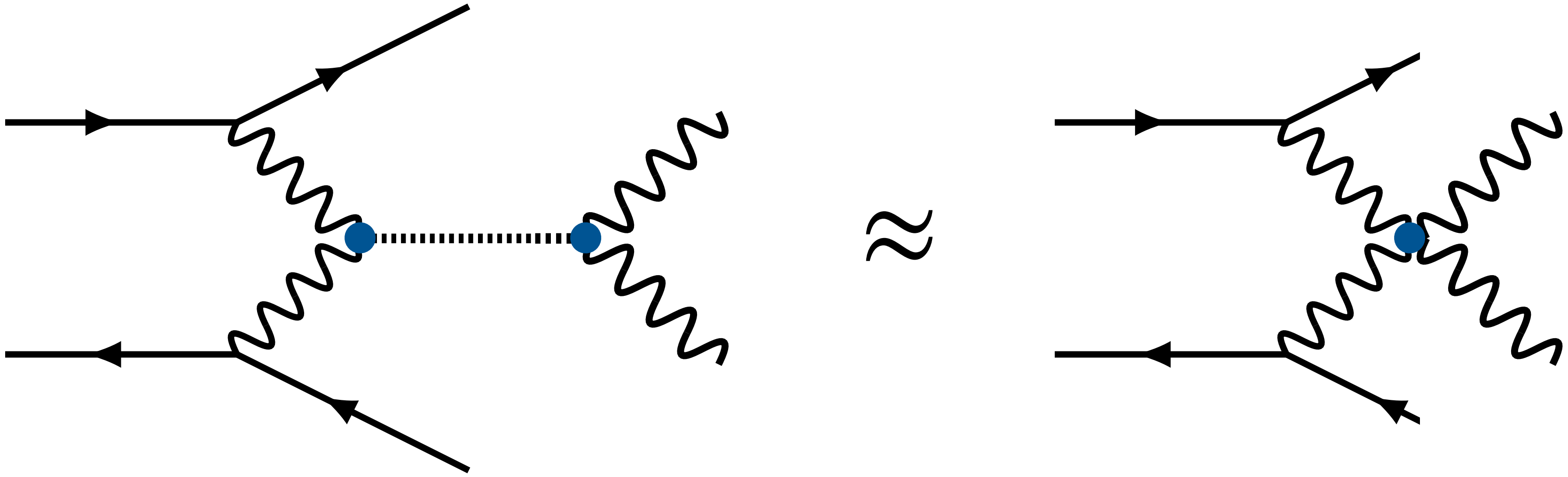


precision limited (~ 3%) due to backgrounds: not possible to determine κ_W precisely through WW scattering

➔ correlation width vs. coupling

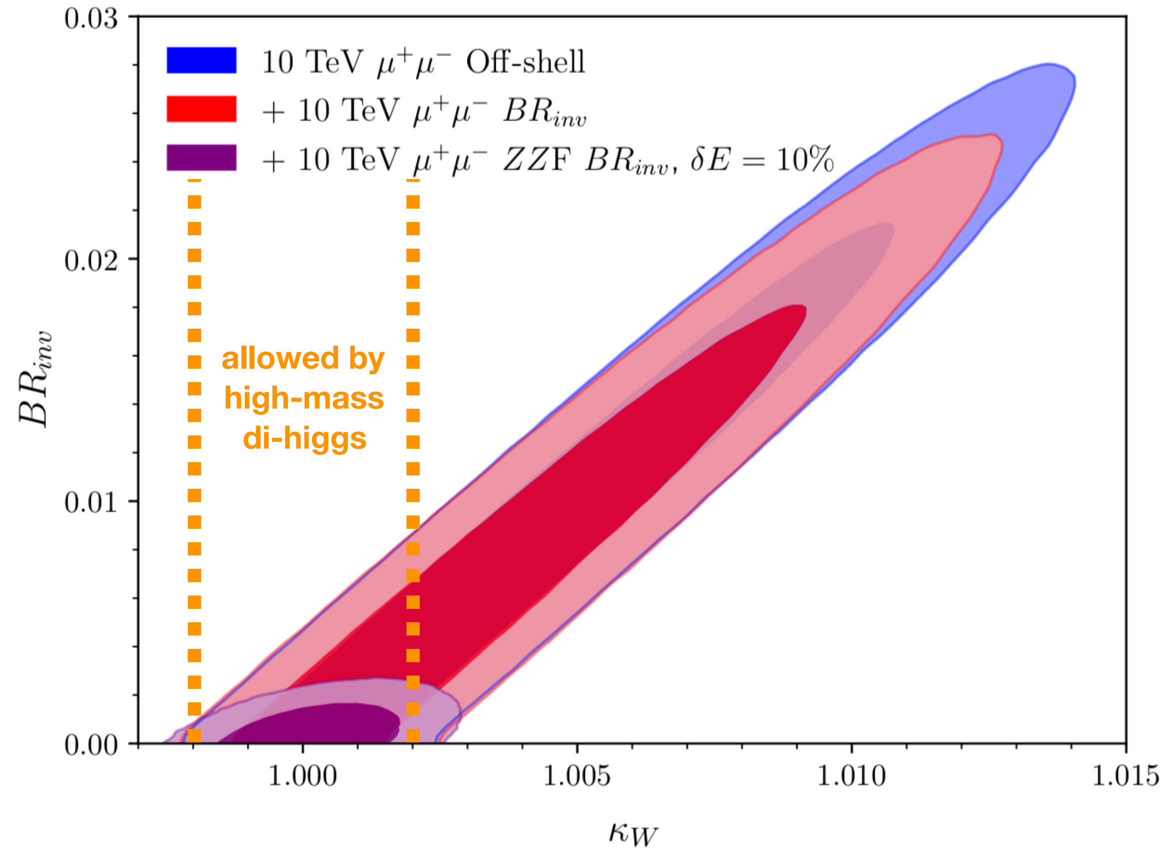
Single Higgs at high mass (off-shell)

- Off-shell single Higgs production: independent of width



$$\sim \frac{E^2}{\Lambda^4}$$

Forslund, Meade 2308.02633



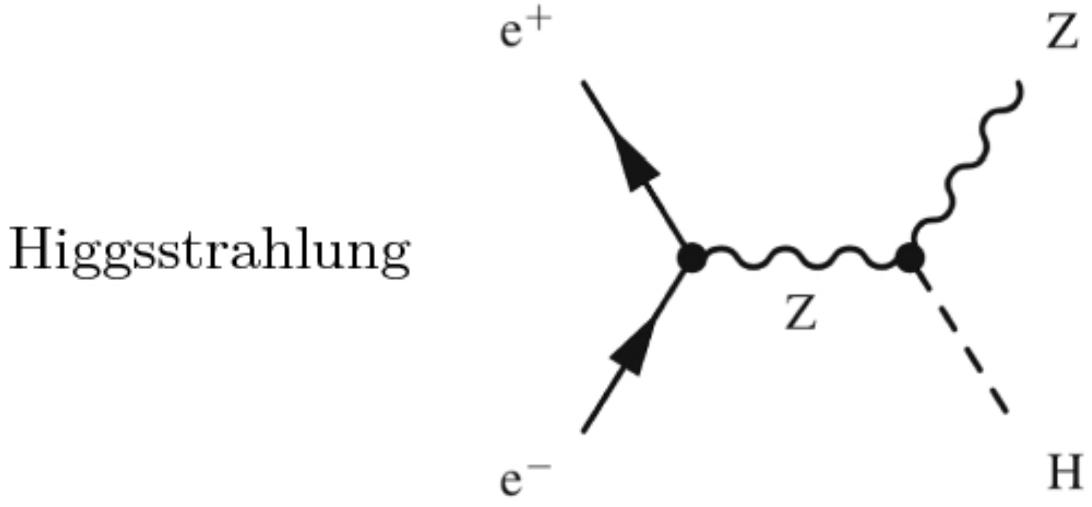
precision limited (~ 3%) due to backgrounds: not possible to determine κ_W precisely through WW scattering

➔ correlation width vs. coupling

Inclusive Higgs search

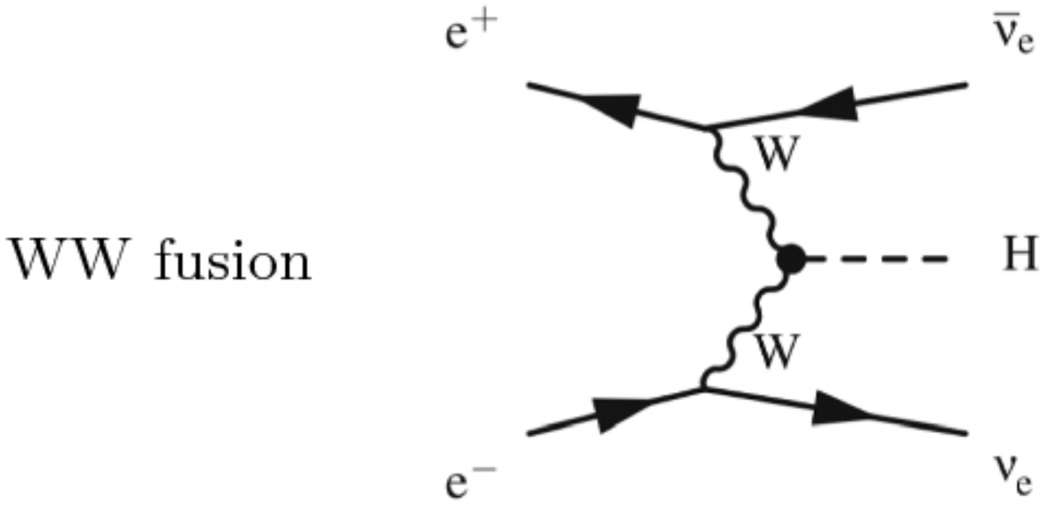
- Caveat: single Higgs at μC can access only

$$\mu_f = \sigma_h \times \mathrm{BR}_{h\to f} \sim \frac{g_W^2 \times g_f^2}{\Gamma_h}$$ (similar to LHC)



$s = (p_h + p_Z)^2$

Inclusive measurement, $\sigma_h \sim g_Z^2$



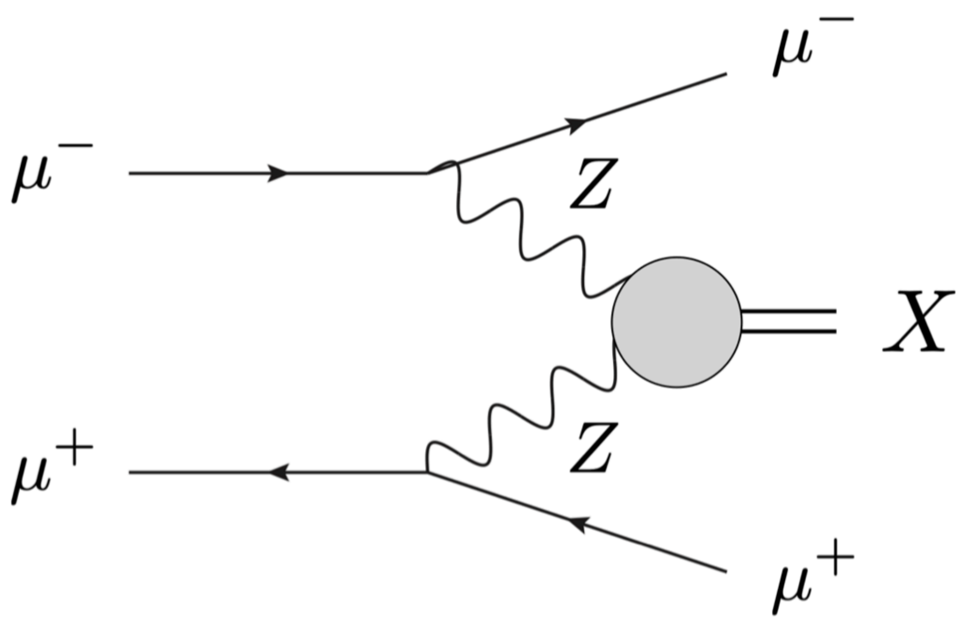
Hard neutrinos not seen,

WW → h → WW depends on g_W and Γ

cannot disentangle deviations in the couplings from modifications of total width

Inclusive Higgs search

- Try to do an inclusive single Higgs measurement with ZZ → h



- cross-section ~ 10x lower than WW
- **needs forward muon detection!**

$$s = (p_h + p_{\mu 1} + p_{\mu 2})^2$$

- Untagged: % sensitivity

  if muons detected at $\eta \gtrsim 6$

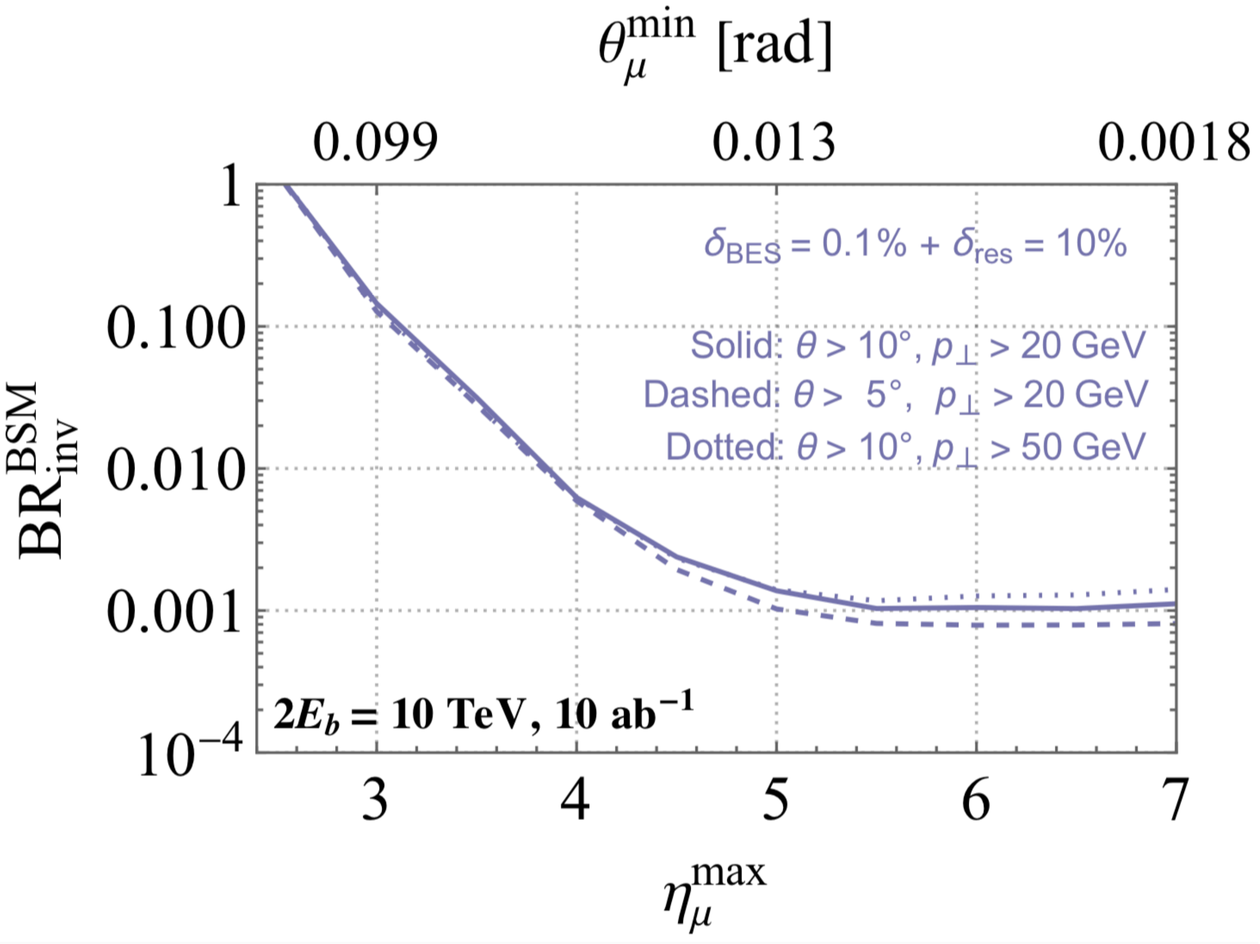
  P. Li, Z. Liu, K. Lyu 2401.08756

- Invisible: 10^{-3} sensitivity

  if muons detected at $\eta \gtrsim 5$

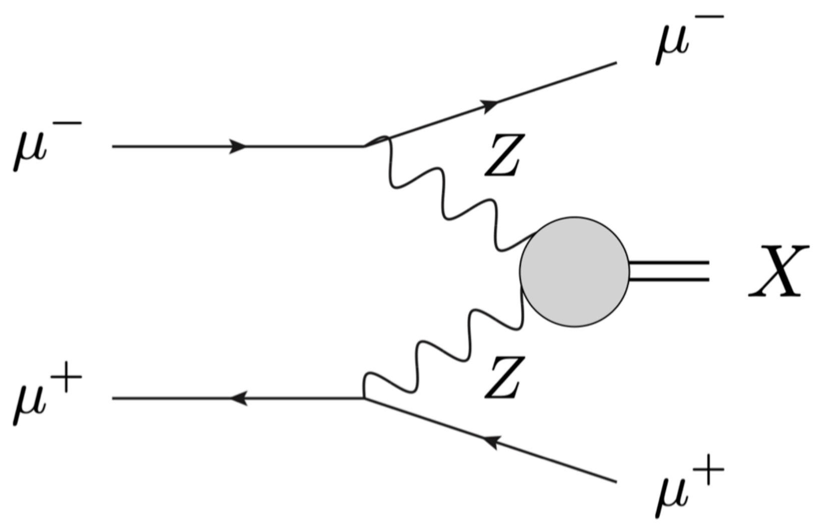
  Ruhdorfer, Salvioni, Wulzer 2303.14202

  Forslund, Meade 2308.02633



Invisible Higgs @ muon collider

- Invisible BSM Higgs Branching Ratio can be one of the contributions to total width Γ.

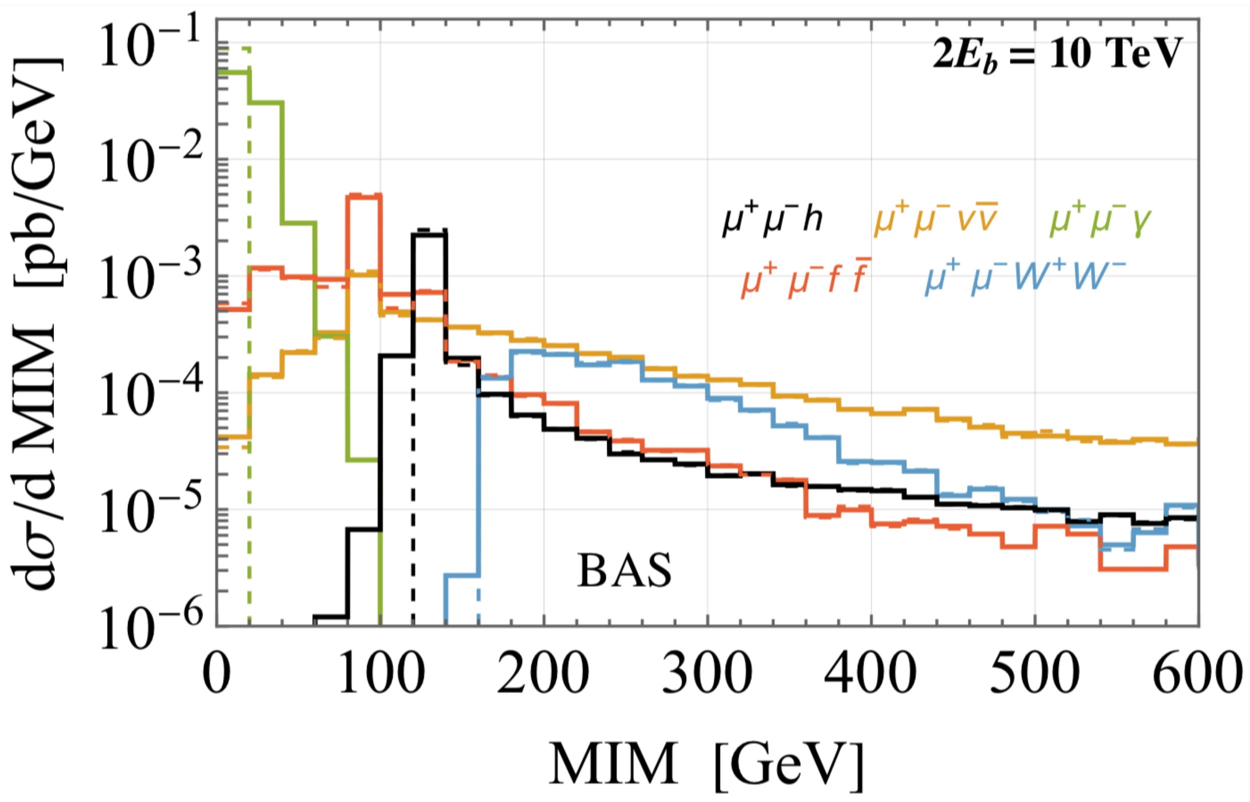


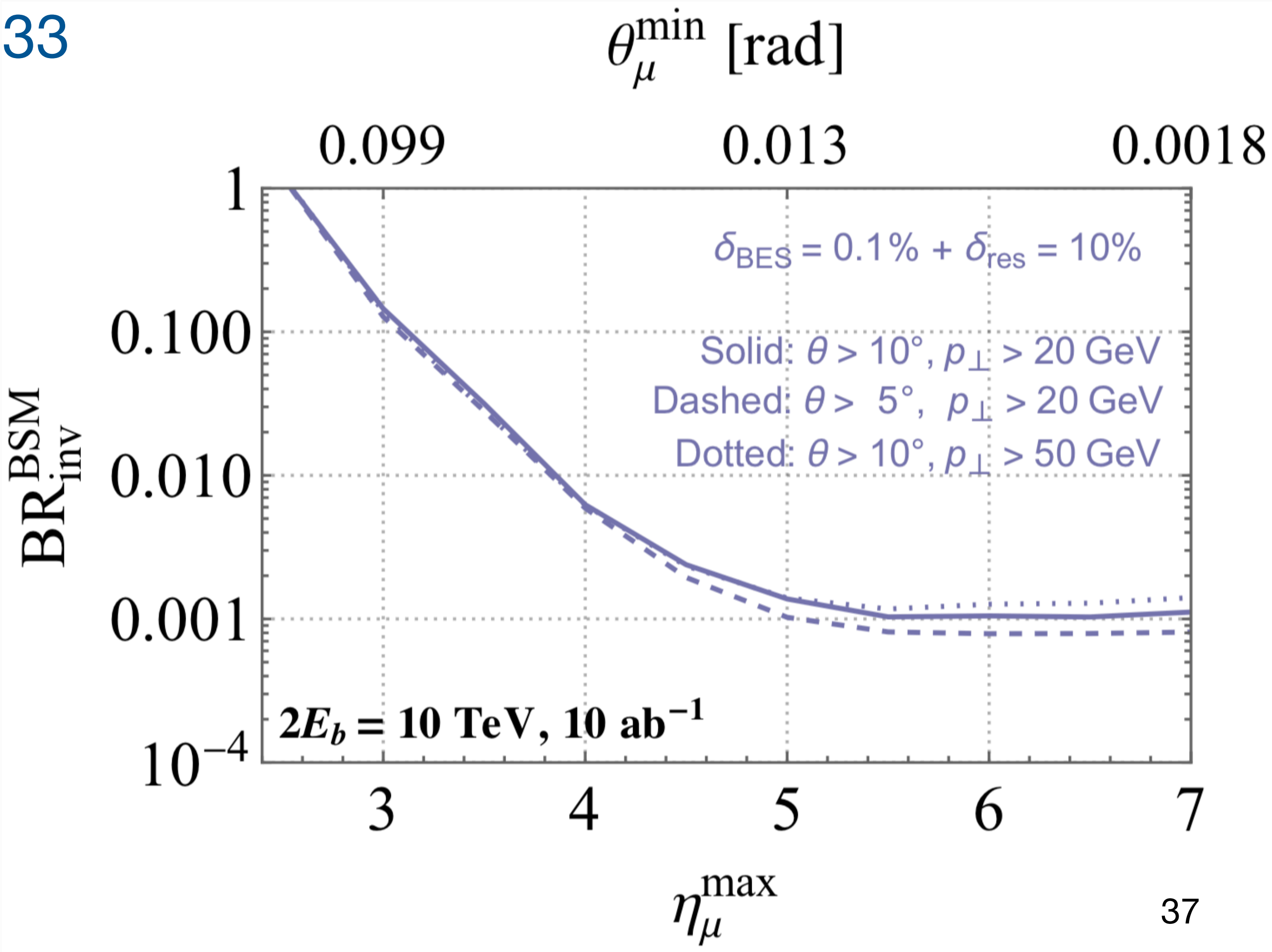
- Can also be studied in ZZ-fusion:

  10^{-3} sensitivity *if muons detected at* $\eta \gtrsim 5$

Ruhdorfer, Salvioni, Wulzer 2303.14202

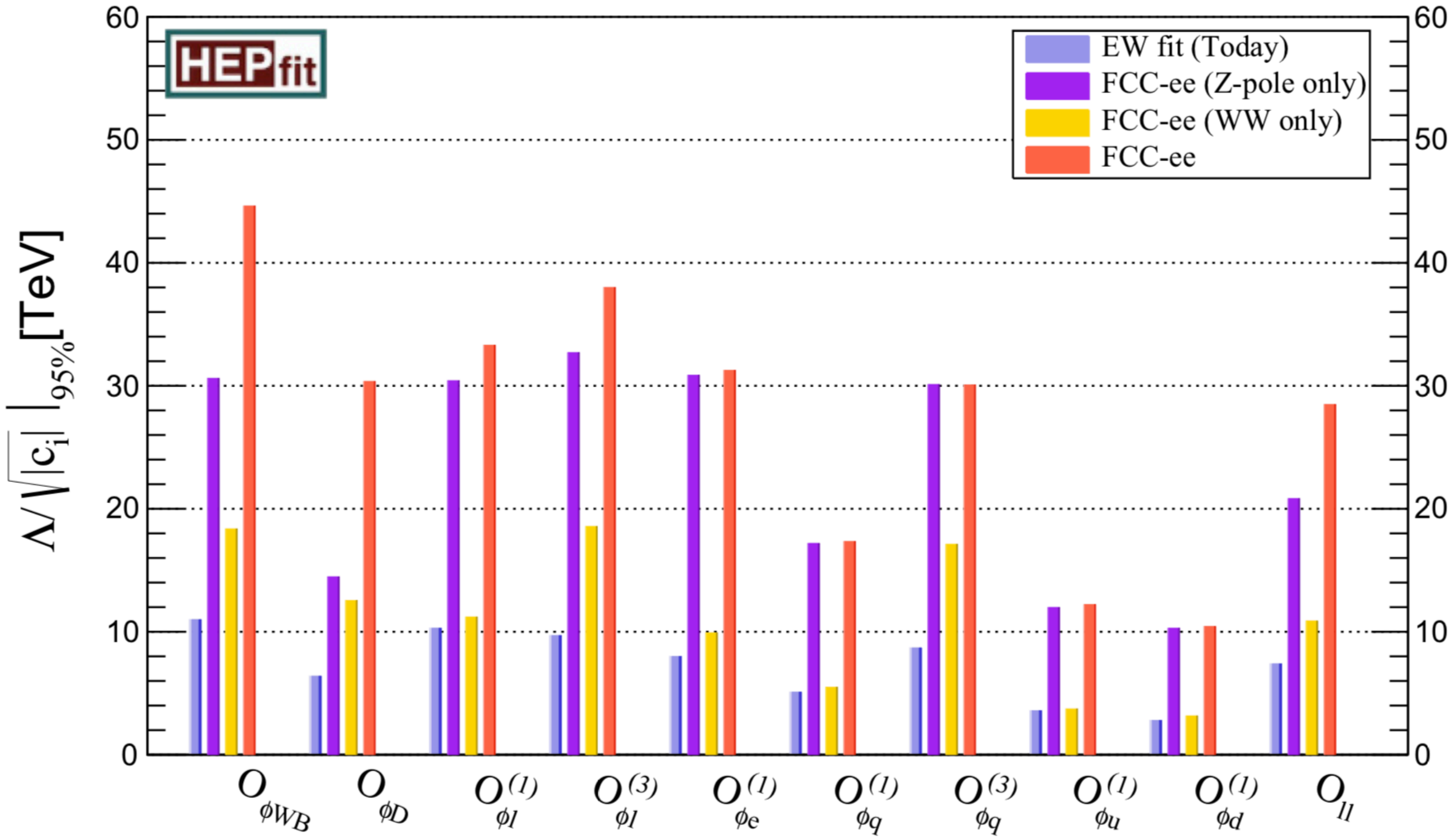
Forslund, Meade 2308.02633





EW precision

- In general, several more operators enter the EW fit

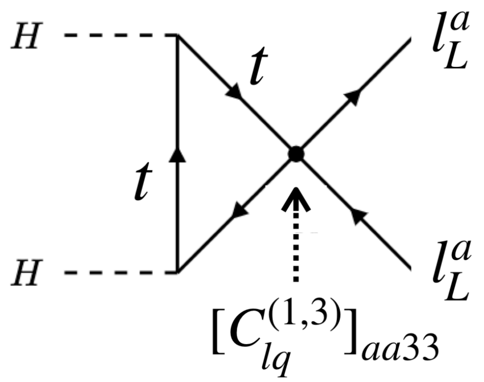


effective scales ~ 30 TeV

$$M_{\rm NP}^{\rm EW} = \Lambda \times g_\star \approx 12\,{\rm TeV}\left(\frac{g_\star}{g_2}\right)$$

Several 4-fermion interactions enter through one loop RGE

2311.00020, 1704.04504



$$\dashrightarrow \quad [C_{Hl}^{(1,3)}]_{aa}$$

$$M_{\rm NP}^{4f} \gtrsim 10\,{\rm TeV} \times g_\star$$

Example: WIMP Dark Matter

✦ Weakly Interacting Massive Particle: most general EW multiplet with DM candidate that is

(a) stable,

(b) without coupling to γ & Z,

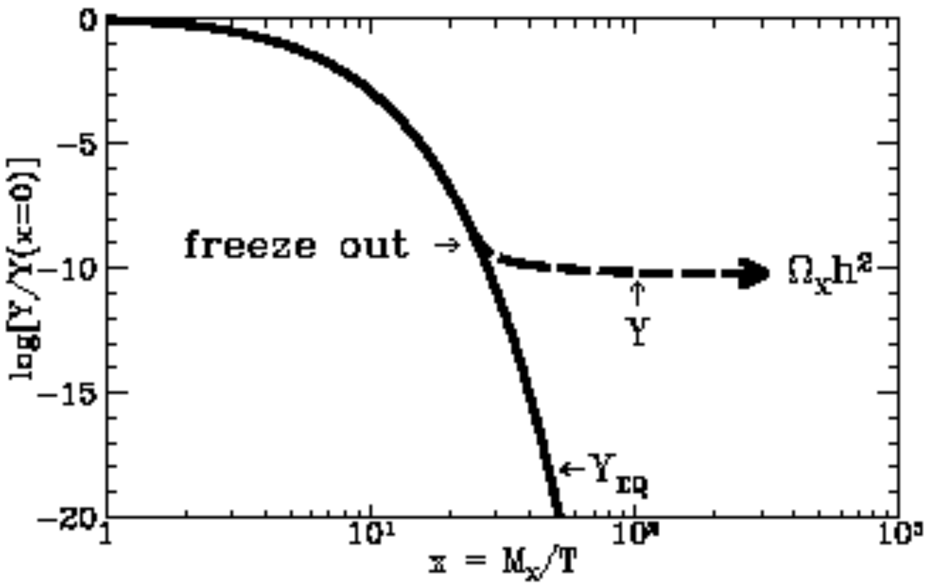
(c) calculable (perturbative).

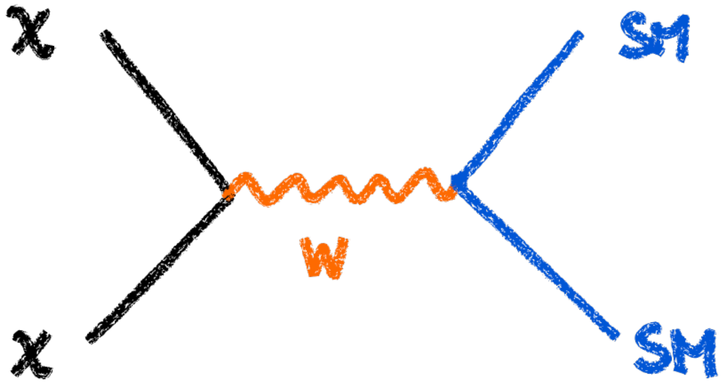
similar to Minimal DM:
Cirelli, Fornengo, Strumia hep-ph/0512090

$$\chi_n = (\cdots, \chi^-, \boxed{\chi^0}, \chi^+, \cdots)$$

✦ Mass fixed by freeze-out DM abundance

Bottaro, DB, Costa, Franceschini, Panci, Redigolo, Vittorio 2107.09688, 2205.04486





EW n-plet	Mass [TeV]
$2_{1/2}$	1.08
3_0	2.86
$4_{1/2}$	4.8
5_0	13.6
5_1	9.9
$6_{1/2}$	31.8
7_0	48.8
9_0	113

☛ talks by Raki and Paolo

Energies of several TeV crucial to probe these WIMP candidates!

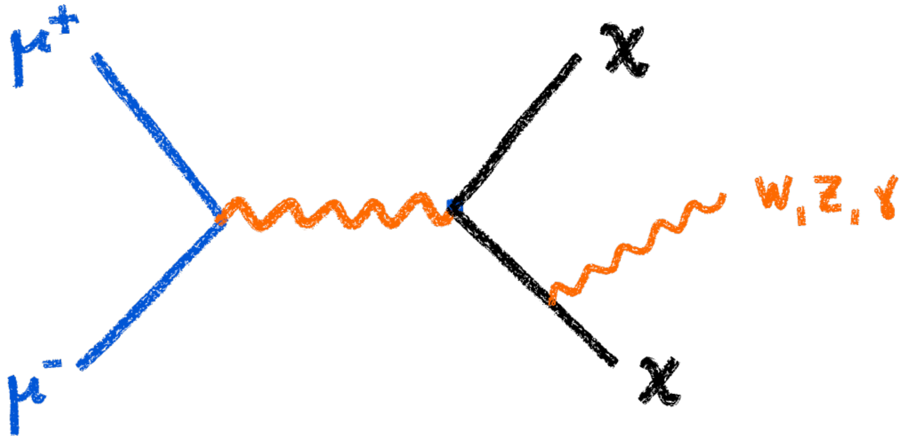
Example: WIMP Dark Matter

- Mono-γ/W/Z signals: $\mu\bar{\mu} \to \chi\bar{\chi} + X$

  DM pair production + EW radiation

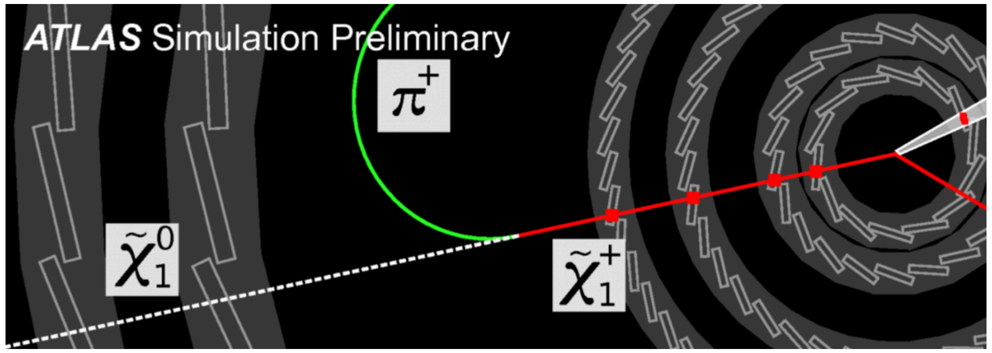
  Han et al. 2009.11287

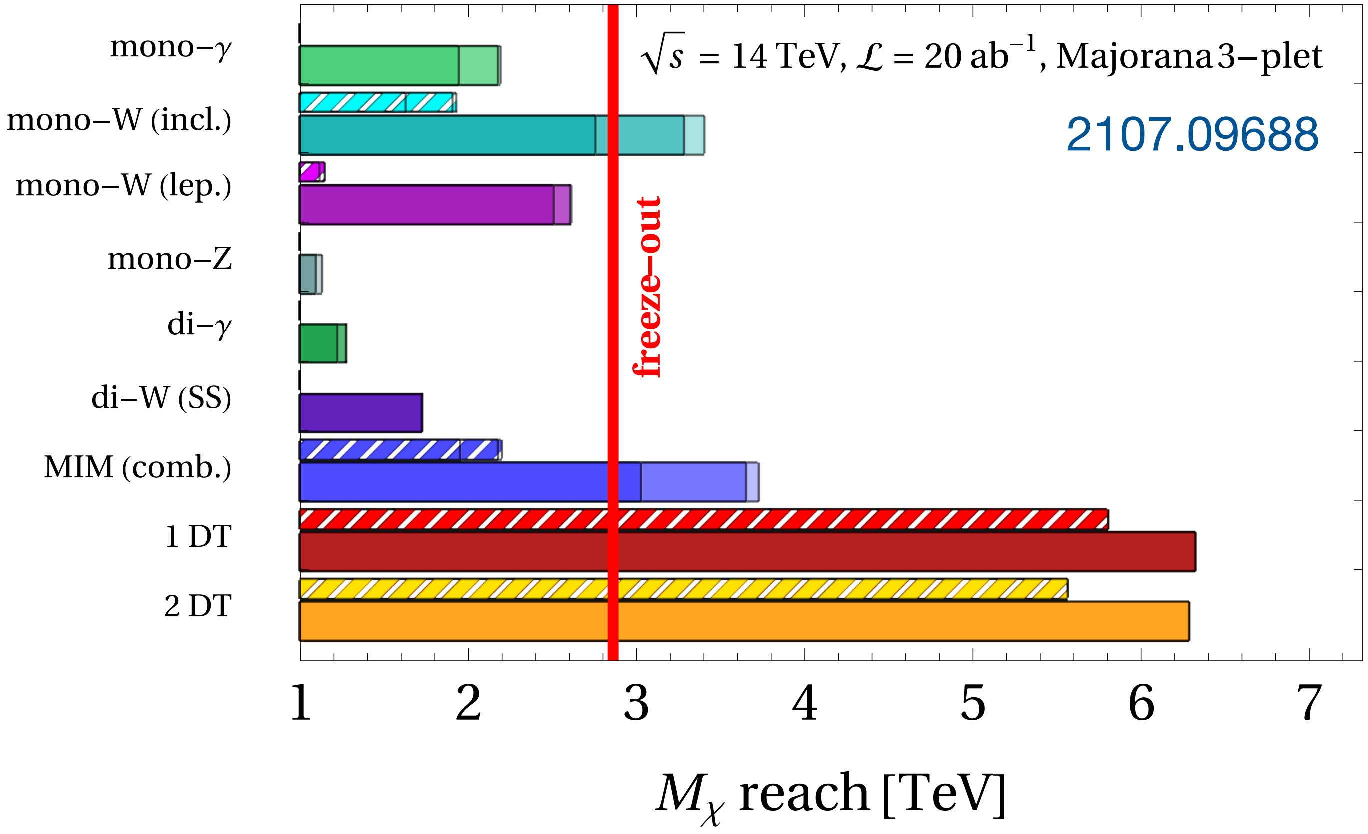
  Bottaro et al. 2107.09688, 2205.04486



- Disappearing tracks: charged components of χ can be long-lived $\chi^\pm \to \chi^0\pi^\pm$

  Capdevilla et al. 2102.11292





μC can probe all relevant WIMP candidates!

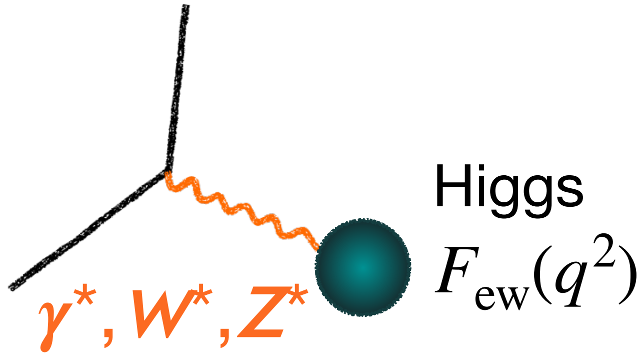
More difficult at hadron colliders, due to PDF suppression

FCC physics study

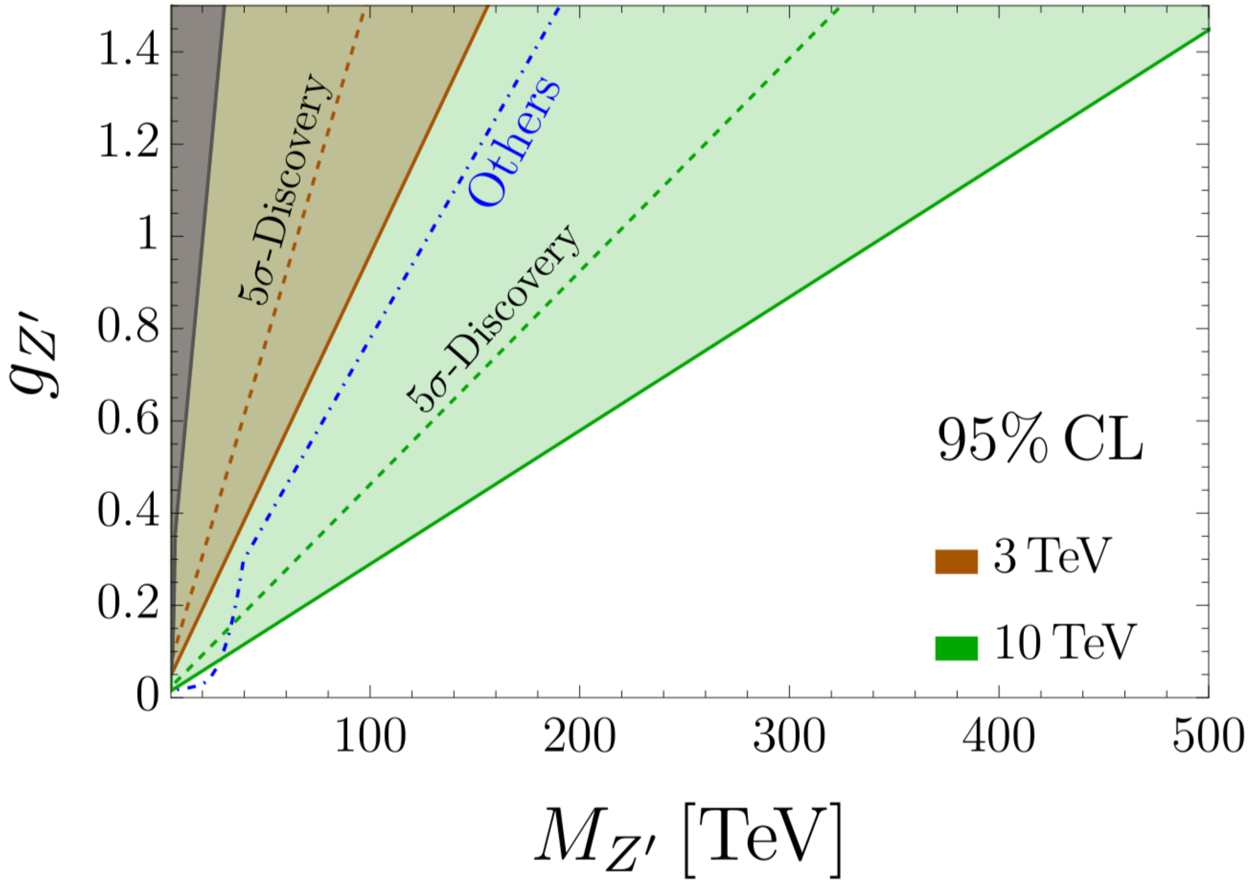
Cirelli, Sala, Taoso 1407.7058

High-energy probes: EW & Higgs physics

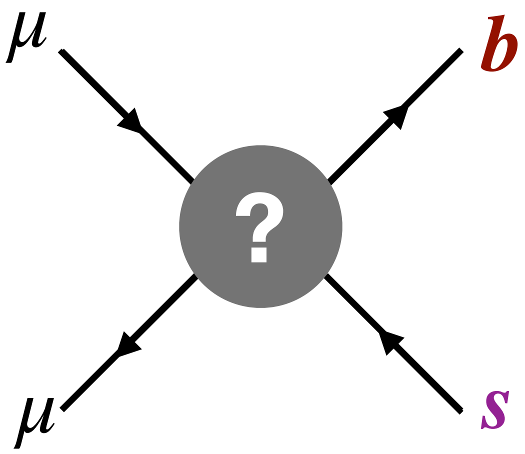
- High-energy processes at a 10–30 TeV lepton collider are able to probe EW new physics scales of 100 TeV or more.
  - 10x higher than ultimate precision at Z pole



- Example: heavy resonance with mass $m_{Z'}$ and coupling $g_{Z'}$ to fermions



Quark flavor violation



Four-fermion interactions: muon current coupled to flavor-violating bilinear

$$\frac{c_{bs}}{\Lambda^2}(\bar{b}_{L,R}\gamma^{\rho}s_{L,R})(\bar{\mu}_{L,R}\gamma_{\rho}\mu_{L,R})$$

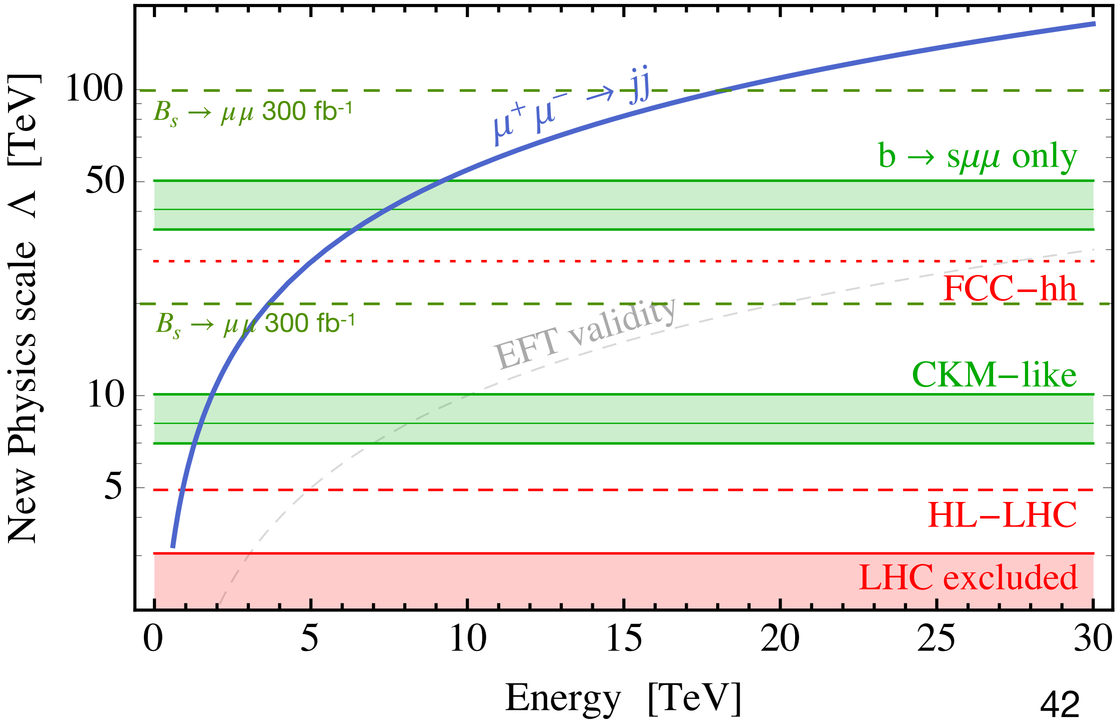
- Contributes to (semi-)leptonic rare B decays $b \to s\mu\mu$: branching ratios & angular observables of various hadronic processes

$$B_s \to \mu\mu, \qquad B \to K^{(*)}\mu\mu, \qquad B_s \to \phi\mu\mu, \qquad \Lambda_b \to \Lambda\mu\mu$$

- Theory uncertainties: cannot improve indefinitely with rare decays

$$\mathrm{BR}(B \to K\mu\mu) \sim \frac{m_W^4}{\Lambda^4}, \quad \sigma(\mu\bar{\mu} \to jj) \sim \frac{E^2}{\Lambda^4}$$

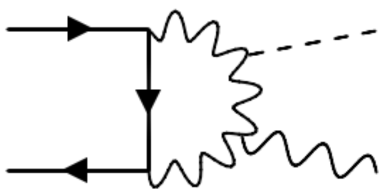
Azatov, Garosi, Greljo, Marzocca, Salko, Trifinopoulos 2205.13552



Muon g-2 @ muon collider

- SM irreducible bakground is small: $\sigma^{(\mathrm{SM})}_{\mu^+\mu^-\to h\gamma} \approx 10^{-2}\,\mathrm{ab}\left(\frac{30\,\mathrm{TeV}}{\sqrt{s}}\right)^2$

  tree-level is suppressed by muon mass; loop contribution dominant

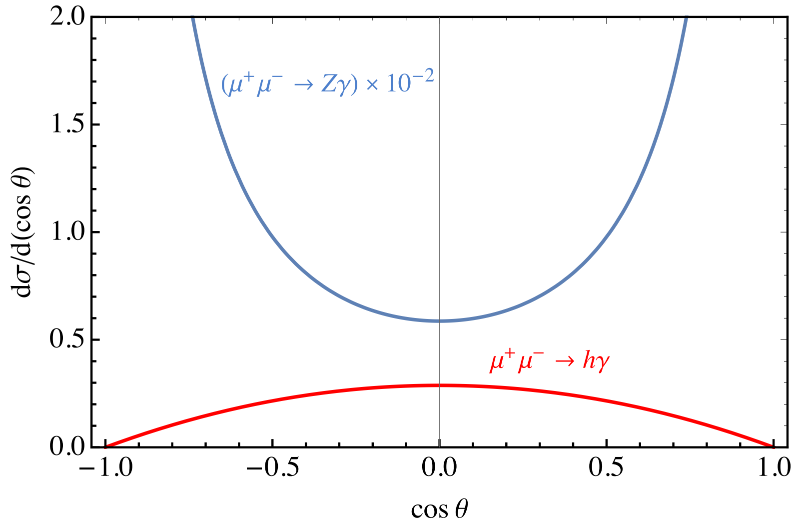


- Main background from *μμ* → Z*γ* (where Z is mistaken for H)

  (large due to transverse Z polarizations)

$$\frac{d\sigma_{\mu\mu\to h\gamma}}{d\cos\theta} = \frac{|C^{\mu}_{e\gamma}(\Lambda)|^2}{\Lambda^4}\frac{s}{64\pi}(1-\cos^2\theta)$$

$$\frac{d\sigma_{\mu\mu\to Z\gamma}}{d\cos\theta} = \frac{\pi\alpha^2}{4s}\frac{1+\cos^2\theta}{\sin^2\theta}\frac{1-4s_W^2+8s_W^4}{s_W^2c_W^2}$$



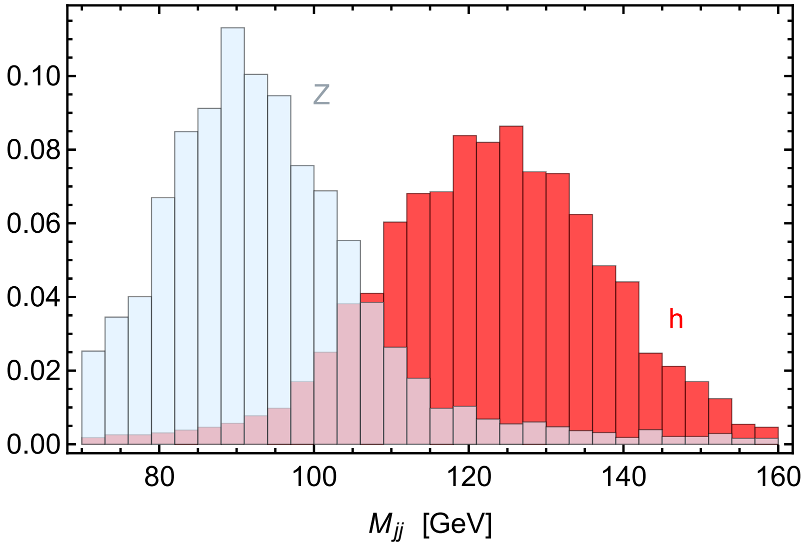
Search in h → bb channel:

$\epsilon_b \approx 80\,\%$ $\quad |\cos\theta_{\mathrm{cut}}| < 0.6$ $\quad \mathrm{BR}_{h\to b\bar{b}} = 58\,\%$

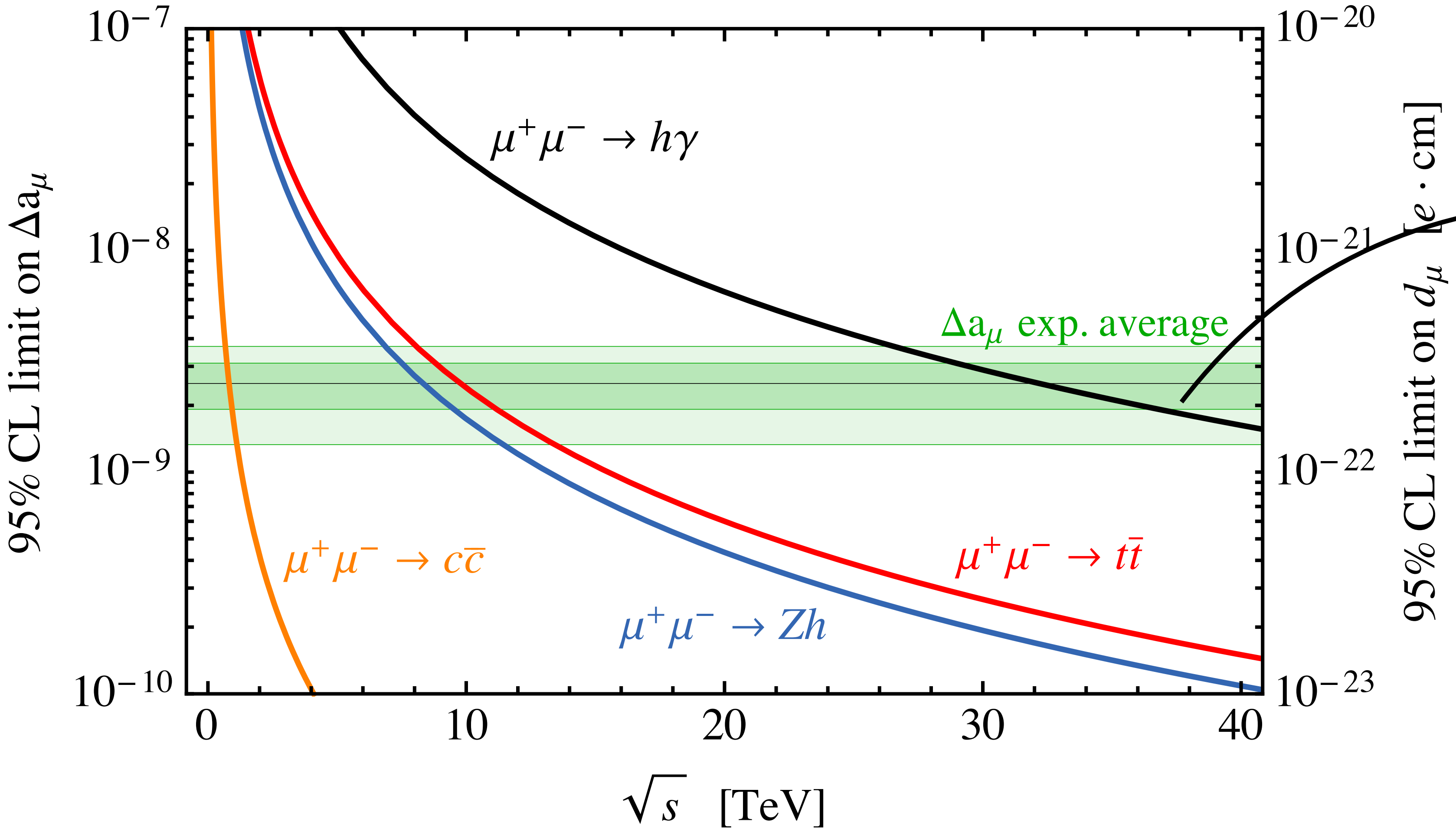
At 30 TeV, 90 ab^{-1}, for $\Delta a_\mu = 3\times 10^{-9}$:

$$N_S = 22, \quad N_B = 886 \times p_{Z\to h}$$

Δa$_\mu$ can be tested at 95% CL at a 30 TeV collider if Z→h mistag probability < 10-15%



Muon g-2 @ muon collider



Exp. value of Δa_μ can be tested at 95% CL at a 30 TeV collider!

(with reasonable assumptions on detector performance)

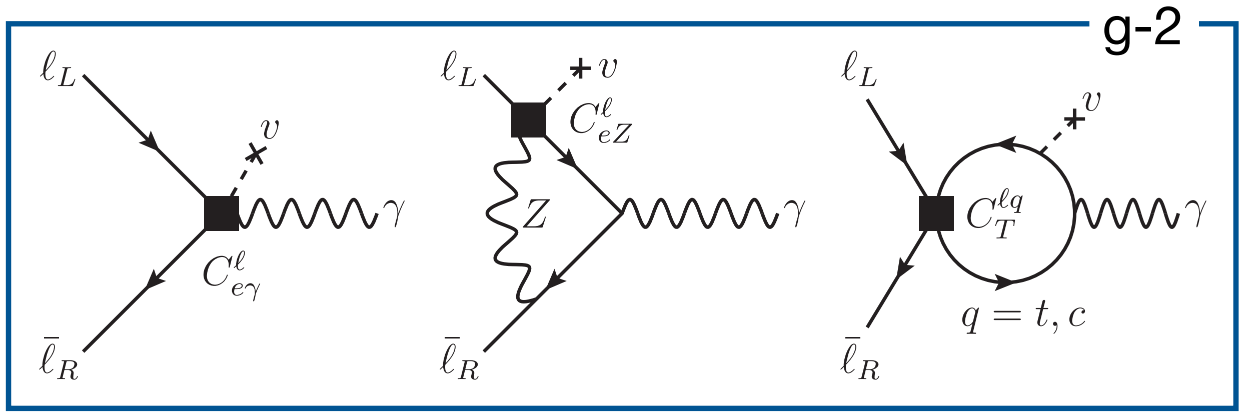
This result is completely model-independent!

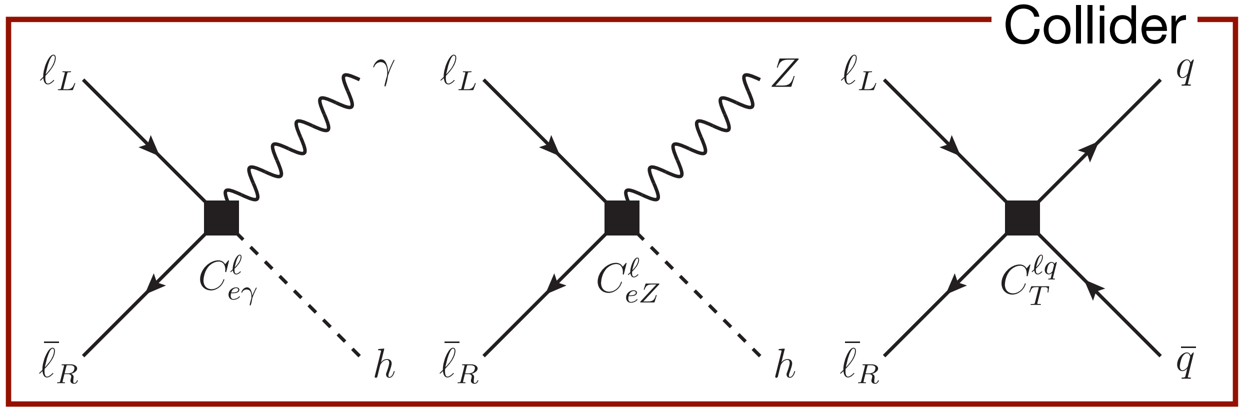
B, Paradisi 2012.02769

- Other operators enter g-2 at 1 loop:

$$\Delta a_\mu \approx \left(\frac{250\,\text{TeV}}{\Lambda^2}\right)^2 \left(C_{e\gamma} - \frac{C_{Tt}}{5} - \frac{C_{Tc}}{1000} - \frac{C_{eZ}}{20}\right)$$

- Full set of operators with $\Lambda \gtrsim 100$ TeV can be probed at a high-energy muon collider





Lepton g-2 from rare Higgs decays

- Tau magnetic dipole moment: enhanced due to the larger mass

$$\Delta a_\tau = \frac{4v\, m_\tau}{\Lambda^2} C^\tau_{e\gamma} \approx \Delta a_\mu \frac{m_\tau^2}{m_\mu^2} \approx 10^{-6}$$

if $C^\ell_{e\gamma}$ scales as y_ℓ

Present bound: $\Delta a_\tau \lesssim 10^{-2}$

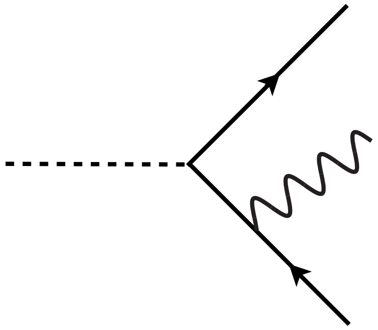
from LEP $e^+e^- \to e^+e^-\tau^+\tau^-$

hep-ex/0406010

Can be improved to few 10-3

at HL-LHC 1908.05180

- Contribution to h → $\tau\tau\gamma$ decays:

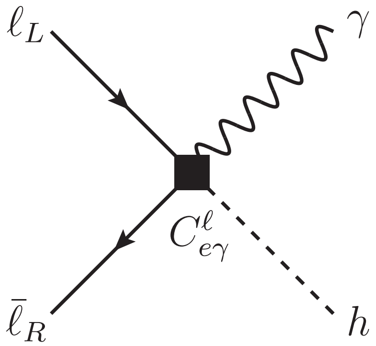


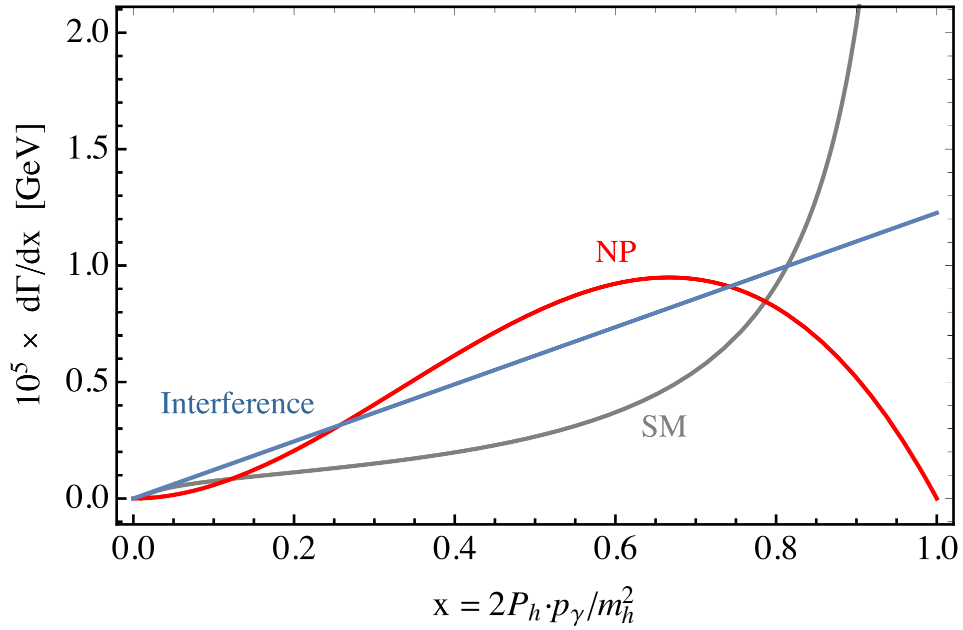
$$\mathrm{BR}^{(\mathrm{SM})}_{h\to\tau^+\tau^-\gamma} \approx 5\times 10^{-4}$$

(with cut on soft collinear photon)

could be measured at few % level by Higgs factory

$$\mathrm{BR}^{(\mathrm{NP})}_{h\to\tau^+\tau^-\gamma} \approx 0.2\times \Delta a_\tau$$



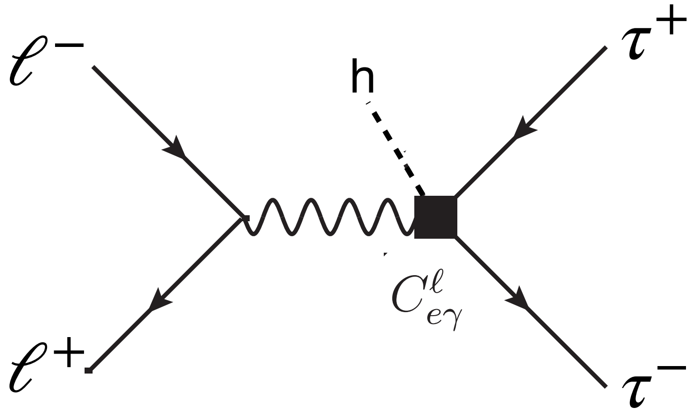


Tau g-2 from high-energy probes

Further possibilities to measure Δa_τ precisely from high-energy probes

- $H\tau\tau$ associated production

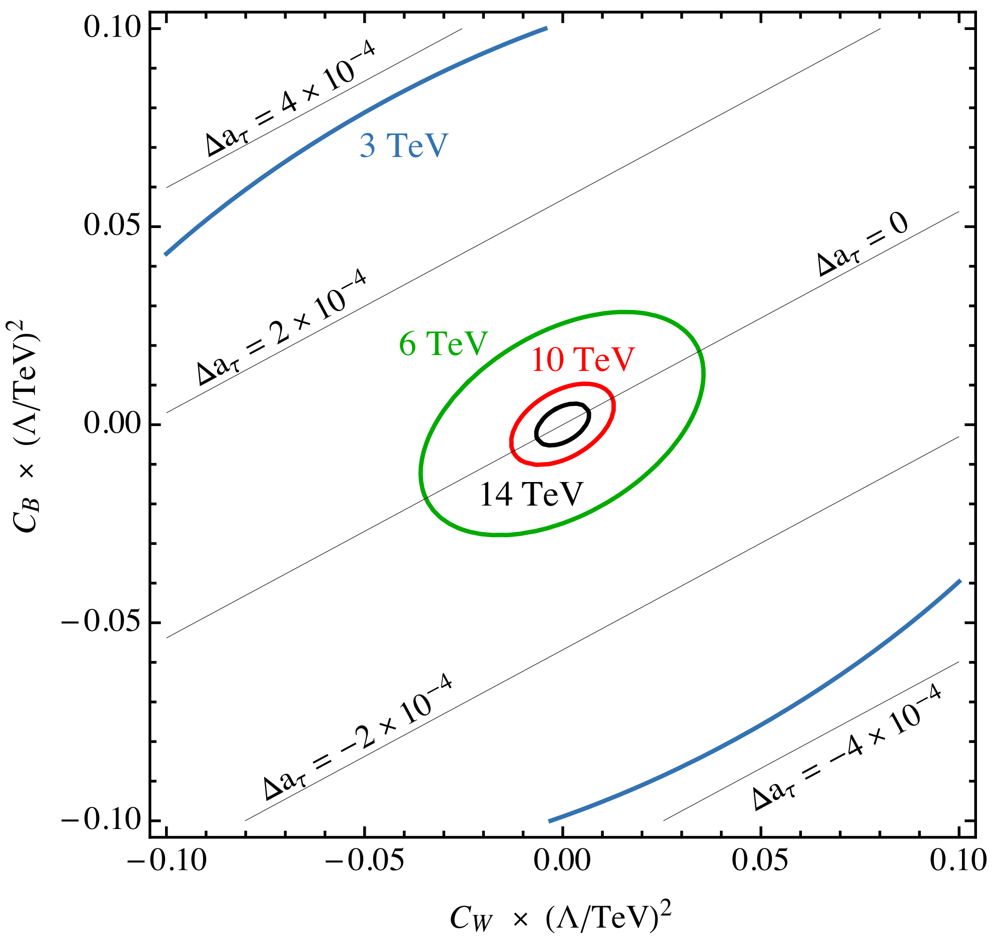
work in progress with Levati, Paradisi, Maltoni, Wang

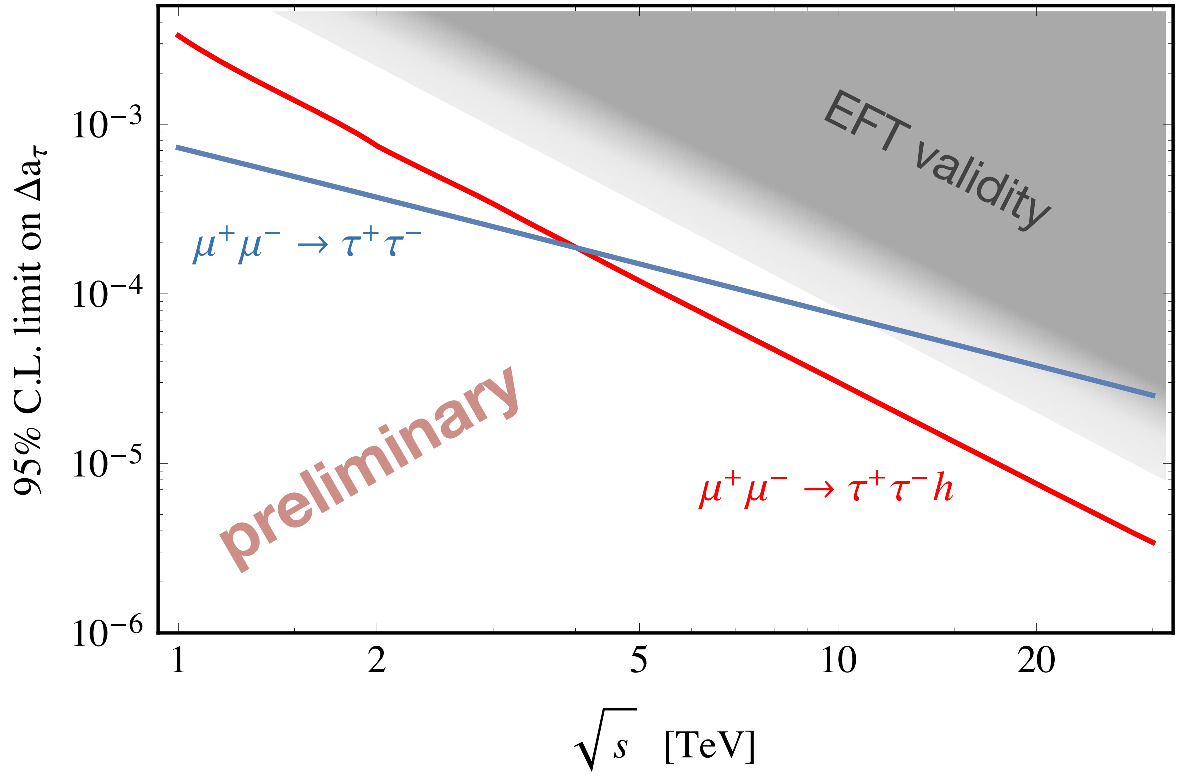


- Main background from μμ → $Z\gamma$

(where Z is mistaken for H)

Could probe $\Delta a_\tau \sim 10^{-5}$ @ 10 TeV





also a bound on tau EDM!

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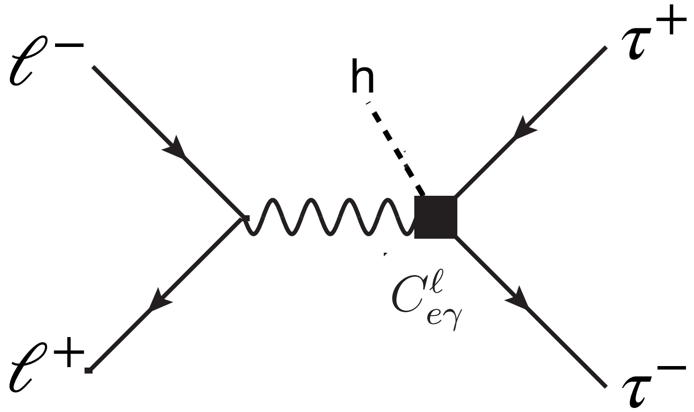

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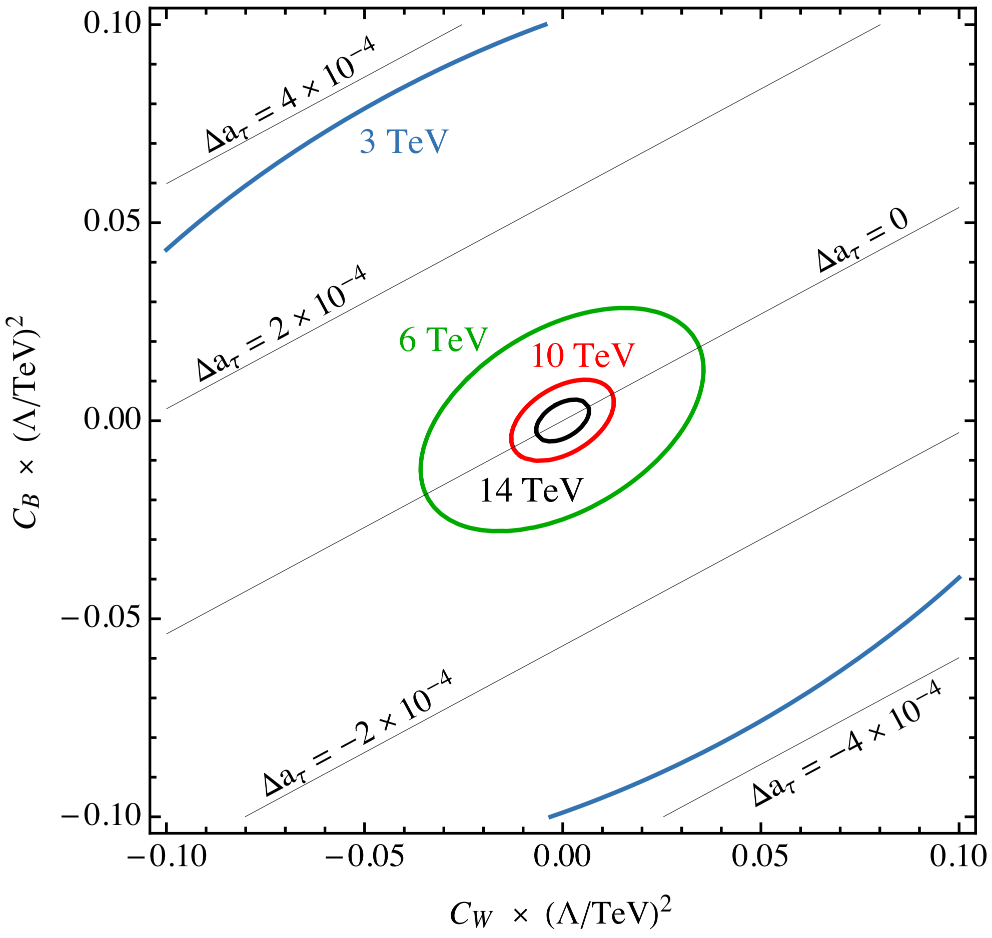
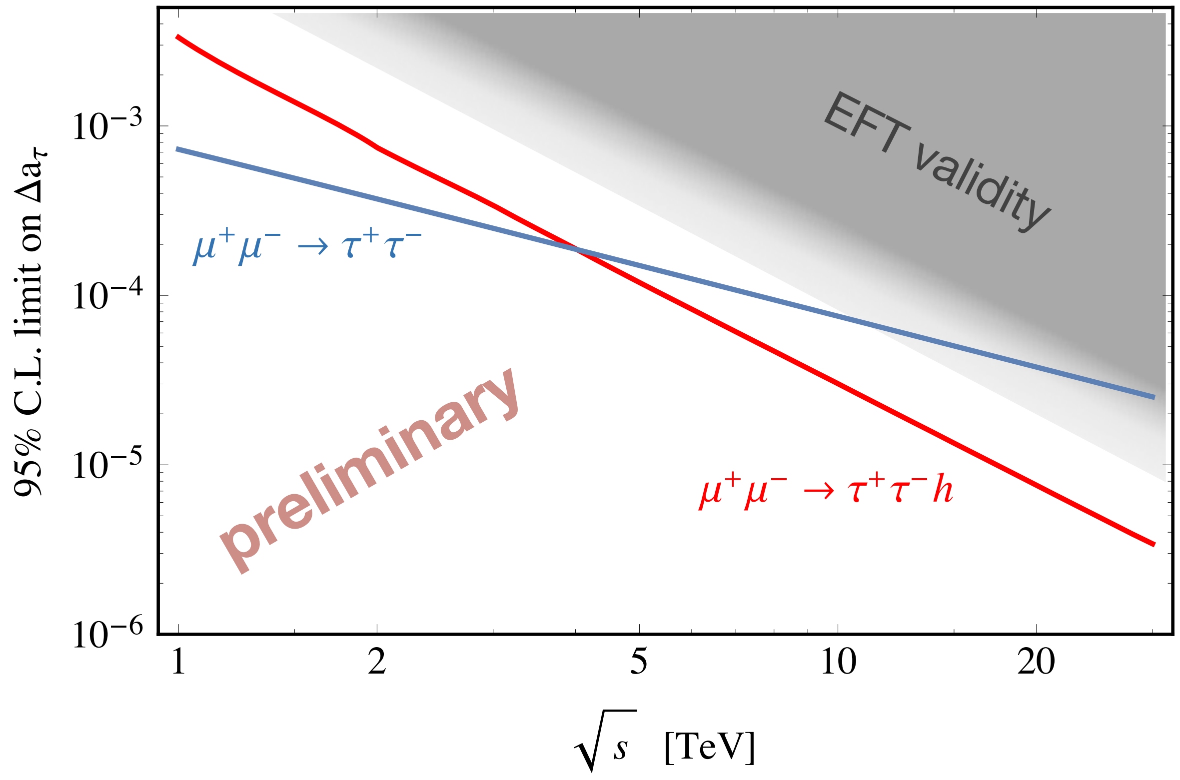




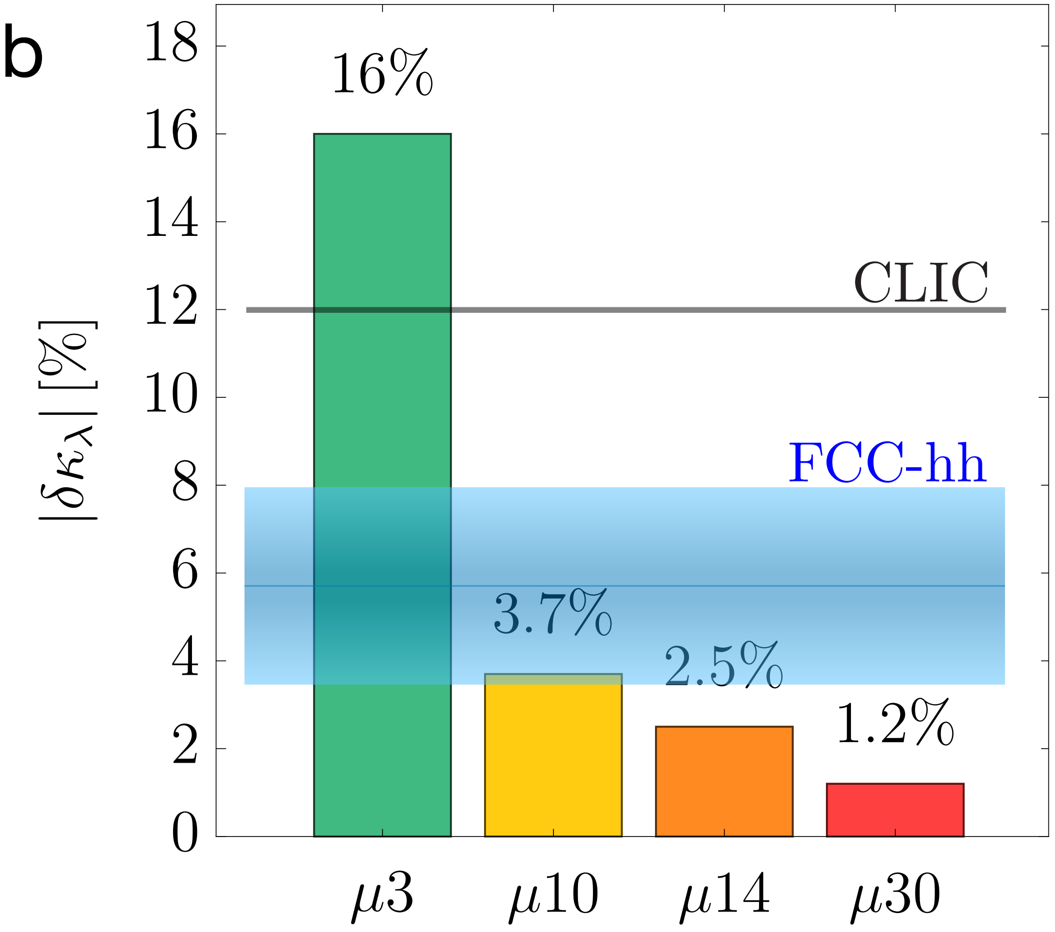
also a bound on tau EDM!

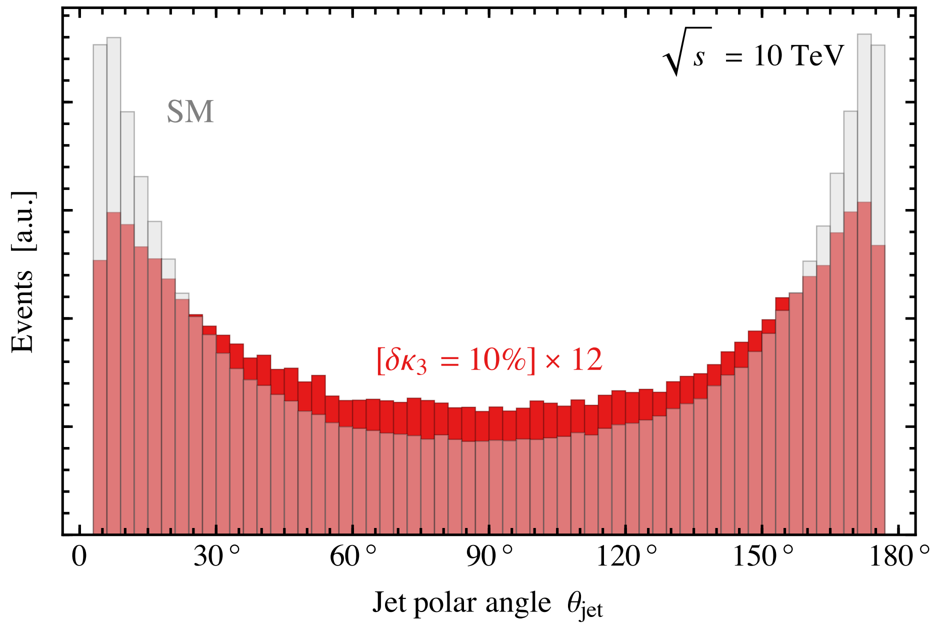
Double Higgs production

- Reach on Higgs trilinear coupling: hh → 4b

E [TeV]	$\mathscr{L}$ [ab^{-1}]	N_{rec}	$\delta\kappa_3$
3	5	170	~ 10%
10	10	620	~ 4%
14	20	1340	~ 2.5%
30	90	6'300	~ 1.2%

B, Franceschini, Wulzer 2012.11555,
Han et al. 2008.12204, Costantini et al. 2005.10289





- Weak dependence on angular acceptance (signal is in the central region)
- Some dependence on detector resolution (to remove backgrounds)

B, Franceschini, Wulzer 2012.11555
see also CLIC study 1901.05897

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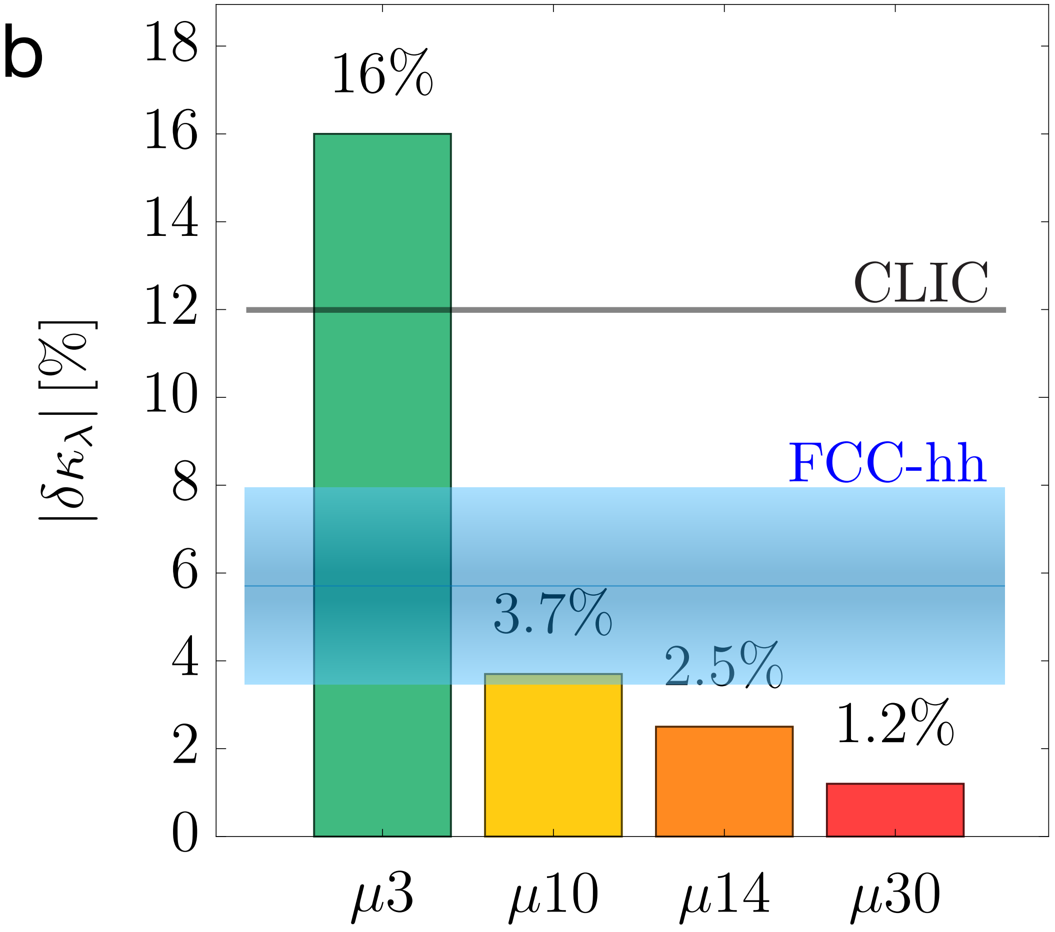

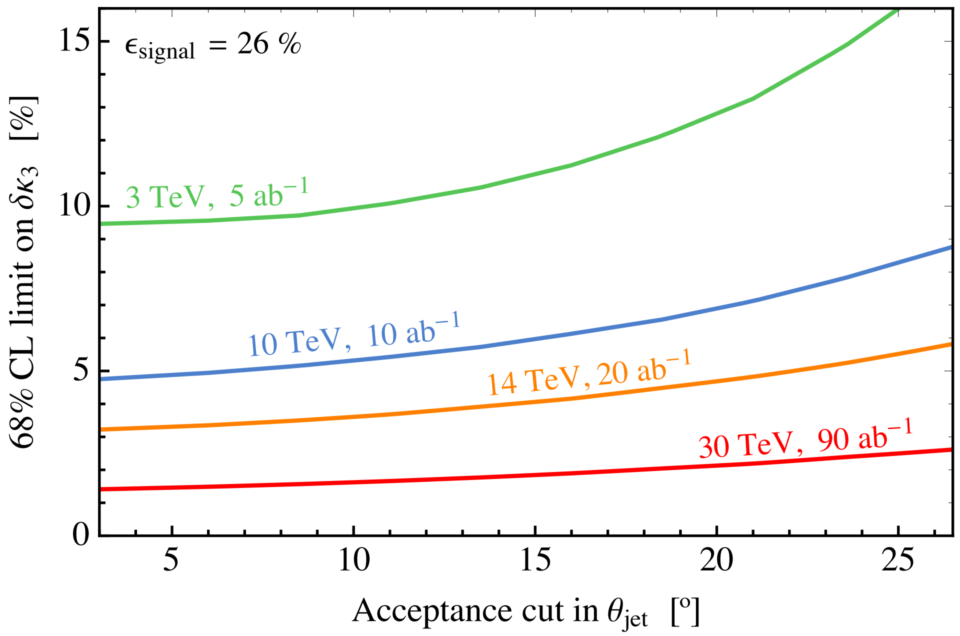

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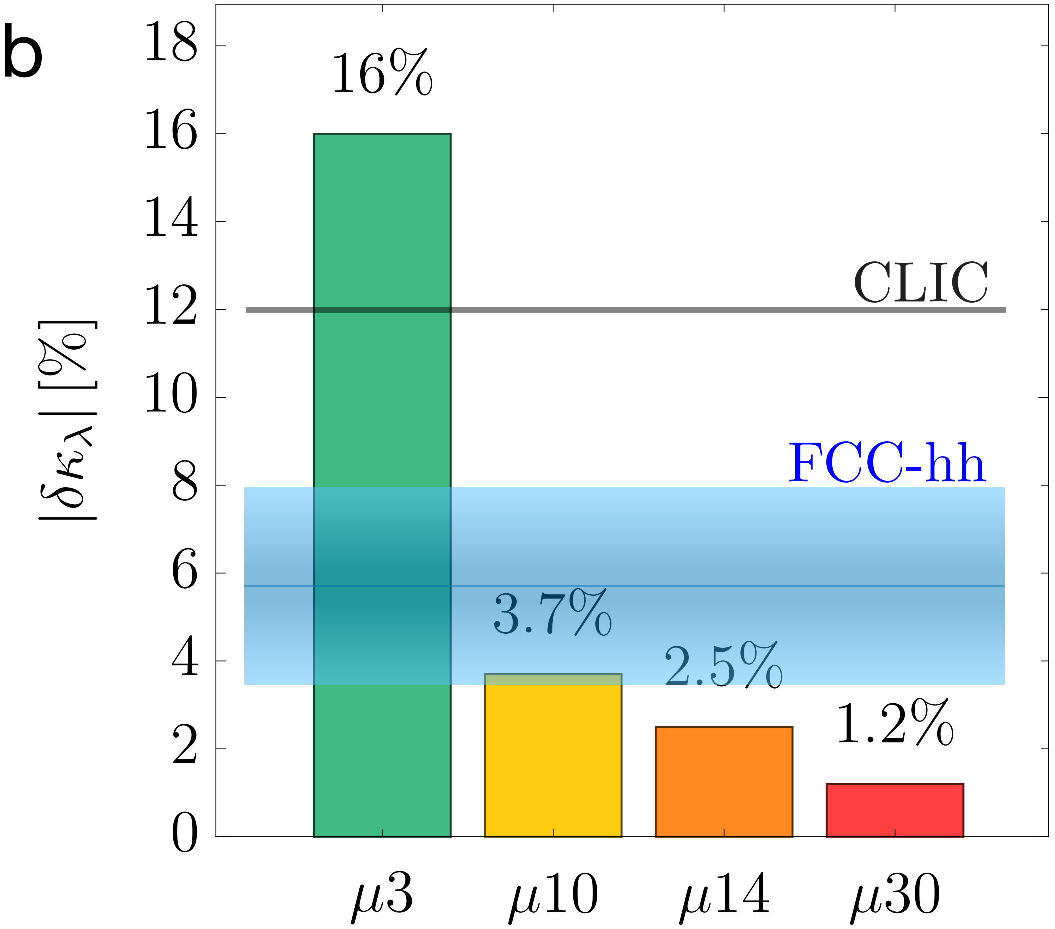

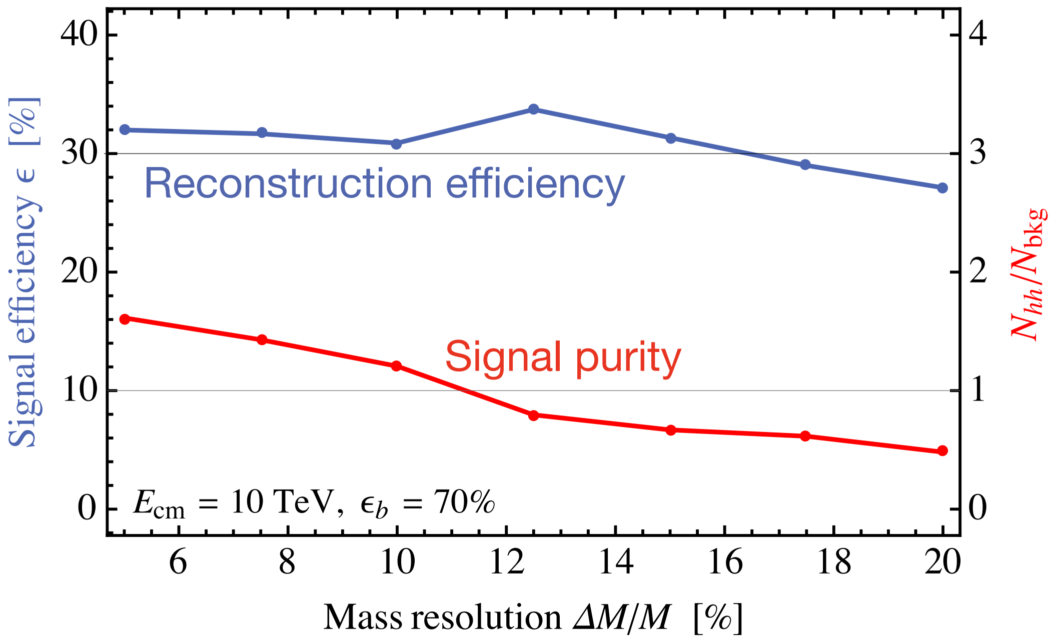

- ‣ Weak dependence on angular acceptance (signal is in the central region)
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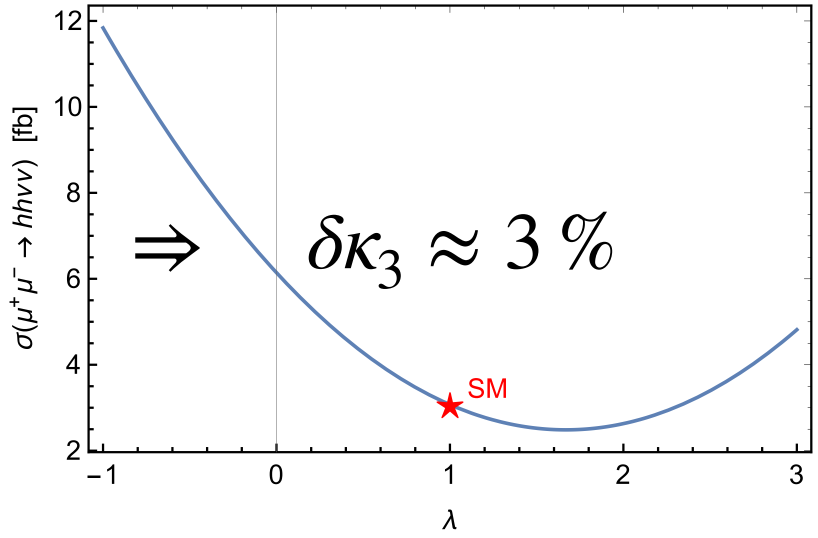
B, Franceschini, Wulzer 2012.11555
see also CLIC study 1901.05897

Double Higgs production

Number of events $\sim s\log(s/m_h^2) \approx 10^5$ at 14 TeV

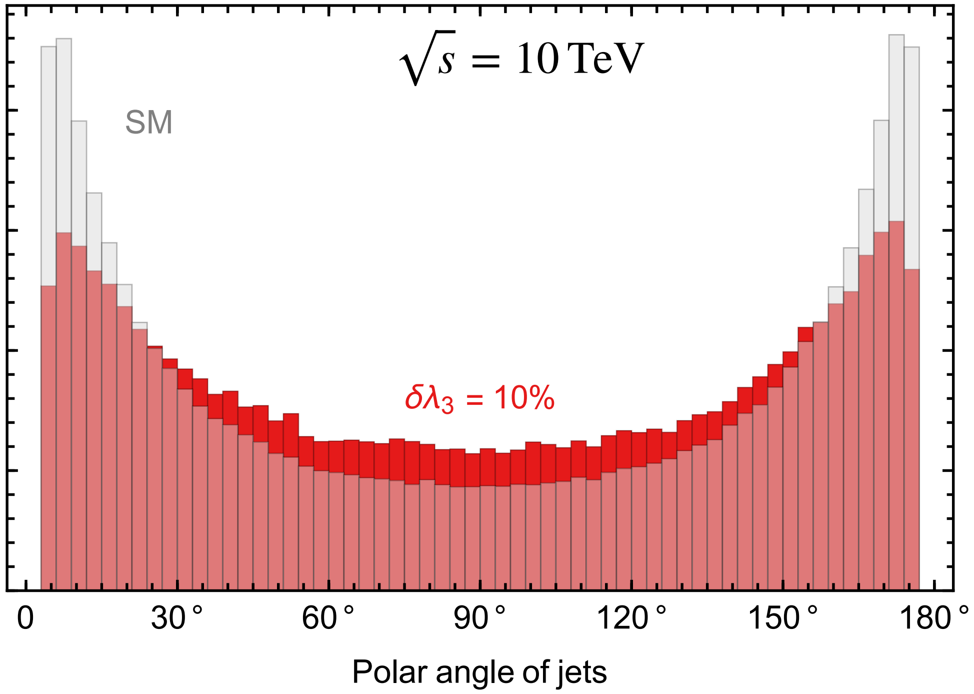
Naïve estimate of the reach: $\delta\sigma \sim (N\times\epsilon)^{-1/2} \approx 1\,\%$

$$\left.\begin{array}{r}\text{reconstruction eff.} \sim 30\,\% \\ \text{BR}(hh\to 4b) = 34\,\%\end{array}\right\}\ \epsilon \sim 10\,\%$$

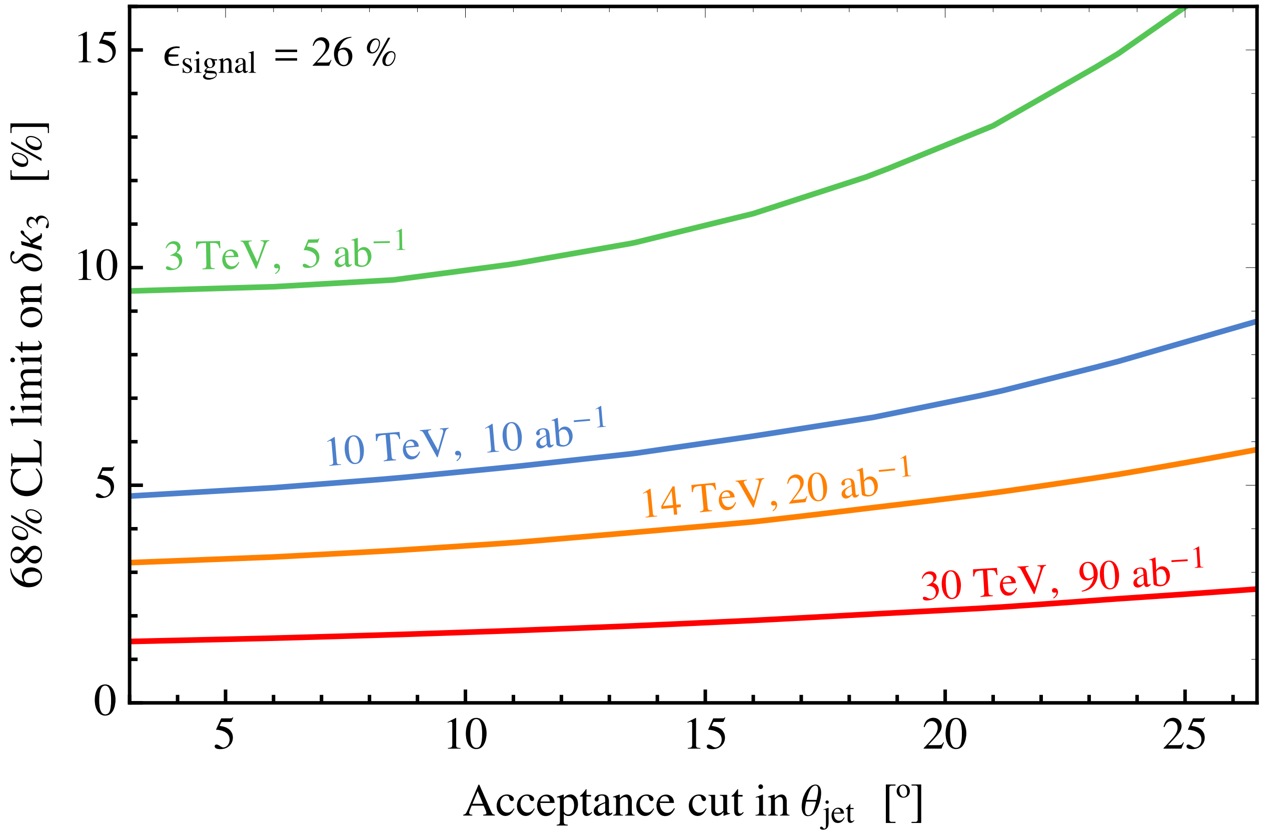


$\Rightarrow\ \delta\kappa_3 \approx 3\,\%$

- **Acceptance cuts** in polar angle θ and p_T of jets:
  - *hh* signal is strongly peaked in forward region



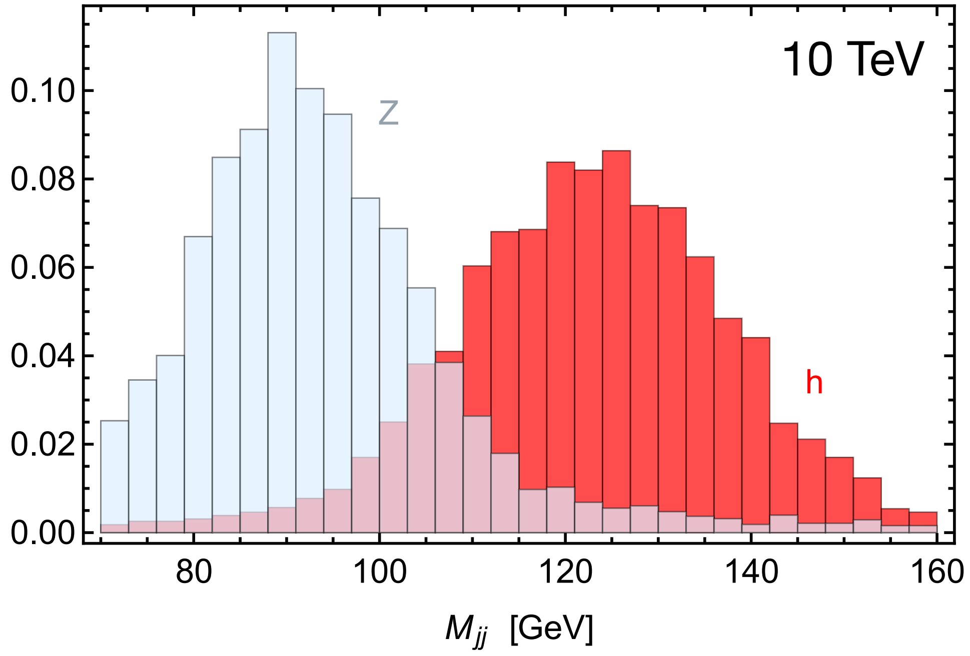
B, Franceschini, Wulzer 2012.11555

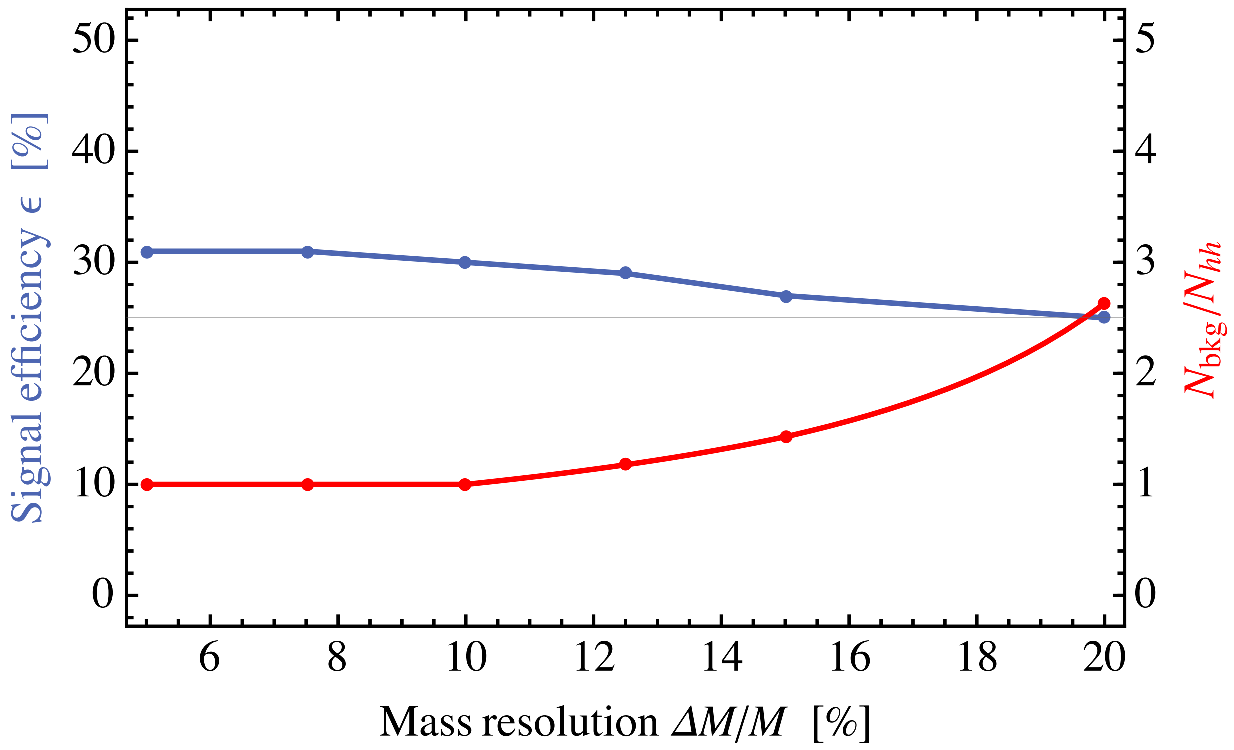


  - Contribution from trilinear coupling is more central: loss due to angular cut is less important

Double Higgs production

- **Backgrounds are important** and cannot be neglected
  (see also CLIC study 1901.05897)
  - Mainly VBF di-boson production:
    Zh & ZZ, but also WW, Wh, WZ…
  - Precise invariant mass reconstruction
    is crucial to isolate signal





NB: (Very!) simplified background analysis *(at parton level!)*

All this should be done properly with a detector simulation

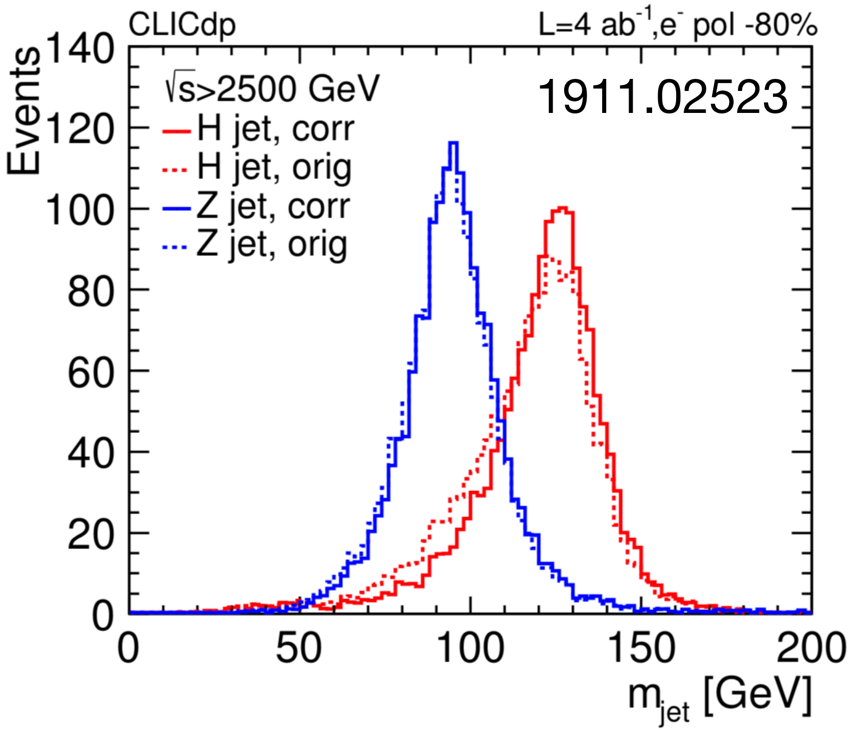
However, perfect agreement with 1901.05897! (3 TeV CLIC)

B, Franceschini, Wulzer 2012.11555

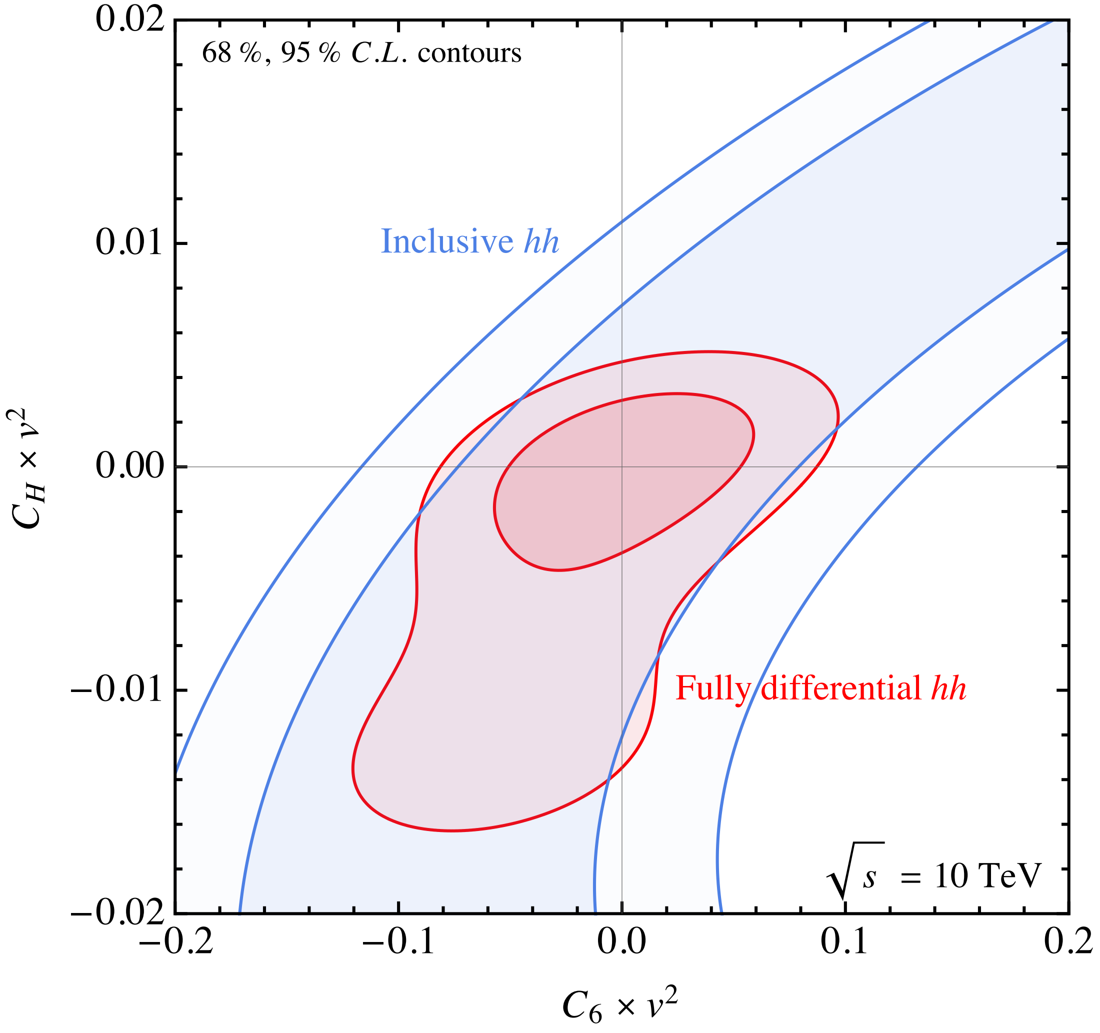
Double Higgs at high mass

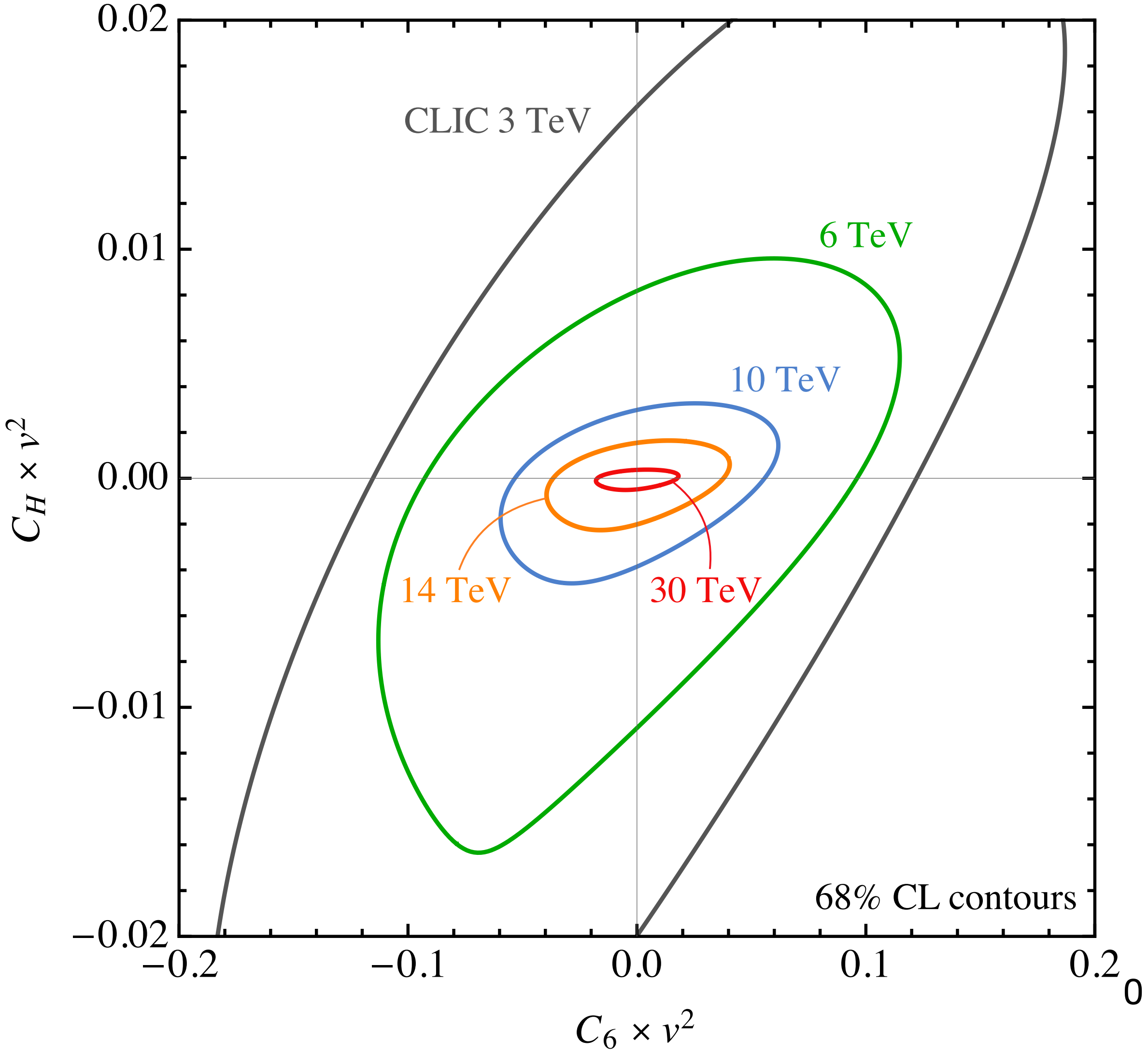
- Fully differential analysis in p_T and M_{hh} to optimize combined sensitivity to C_H and C_6
- Very boosted Higgs bosons: treat them as a single h-jet, without reconstructing the 4 b's.

  We assumed a boosted-H tagging efficiency ~ 50%



B, Franceschini, Wulzer 2012.11555





High-energy di-bosons

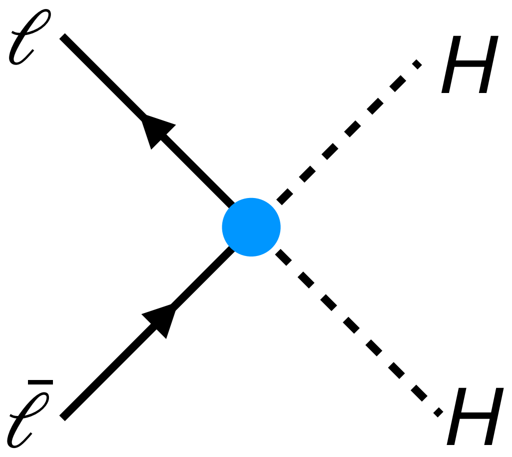
- Longitudinal 2 → 2 scattering amplitudes at high energy:

Process	BSM Amplitude
$\ell_L^+\ell_L^- \to Z_0 h$ $\bar{\nu}_L\nu_L \to W_0^+W_0^-$	$s\,(G_{3L}+G_{1L})\sin\theta_\star$
$\ell_L^+\ell_L^- \to W_0^+W_0^-$ $\bar{\nu}_L\nu_L \to Z_0 h$	$s\,(G_{3L}-G_{1L})\sin\theta_\star$
$\ell_R^+\ell_R^- \to W_0^+W_0^-\,,Z_0 h$	$s\,G_{lR}\sin\theta_\star$
$\bar{\nu}_L\ell_L^- \to W_0^-Z_0\,/\,W_0^-h$ $\nu_L\ell_L^+ \to W_0^+Z_0\,/\,W_0^+h$	$\sqrt{2}\,s\,G_{3L}\sin\theta_\star$

Determined by 3 fermion/scalar current-current interactions (Warsaw):

$$\boxed{\begin{aligned}
\mathcal{O}_{3L} &= \left(\bar{\mathrm{L}}_L\gamma^\mu\sigma^a\mathrm{L}_L\right)\left(iH^\dagger\sigma^a\overleftrightarrow{D}_\mu H\right),\\
\mathcal{O}_{1L} &= \left(\bar{\mathrm{L}}_L\gamma^\mu\mathrm{L}_L\right)\left(iH^\dagger\overleftrightarrow{D}_\mu H\right),\\
\mathcal{O}_{lR} &= \left(\bar{l}_R\gamma^\mu l_R\right)\left(iH^\dagger\overleftrightarrow{D}_\mu H\right).
\end{aligned}}$$

“high-energy primary effects”



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$\boxed{\ell^+_R\ell^-_R \to W_0^+W_0^-\,,Z_0 h}$	$s\,G_{lR}\sin\theta_\star$
$\bar\nu_L\ell^-_L \to W_0^-Z_0\,/\,W_0^-h$ $\nu_L\ell^+_L \to W_0^+Z_0\,/\,W_0^+h$	$\sqrt{2}\,s\,G_{3L}\sin\theta_\star$

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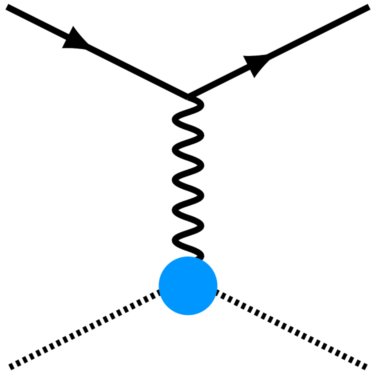
"high-energy primary effects"

- In flavor-universal theories, they are generated by SILH operators (via e.o.m.):



$$G_{1L} = \frac{1}{2}G_{lR} = \frac{g'^2}{4}(C_B + C_{HB})$$

$$G_{3L} = \frac{g^2}{4}(C_W + C_{HW})$$

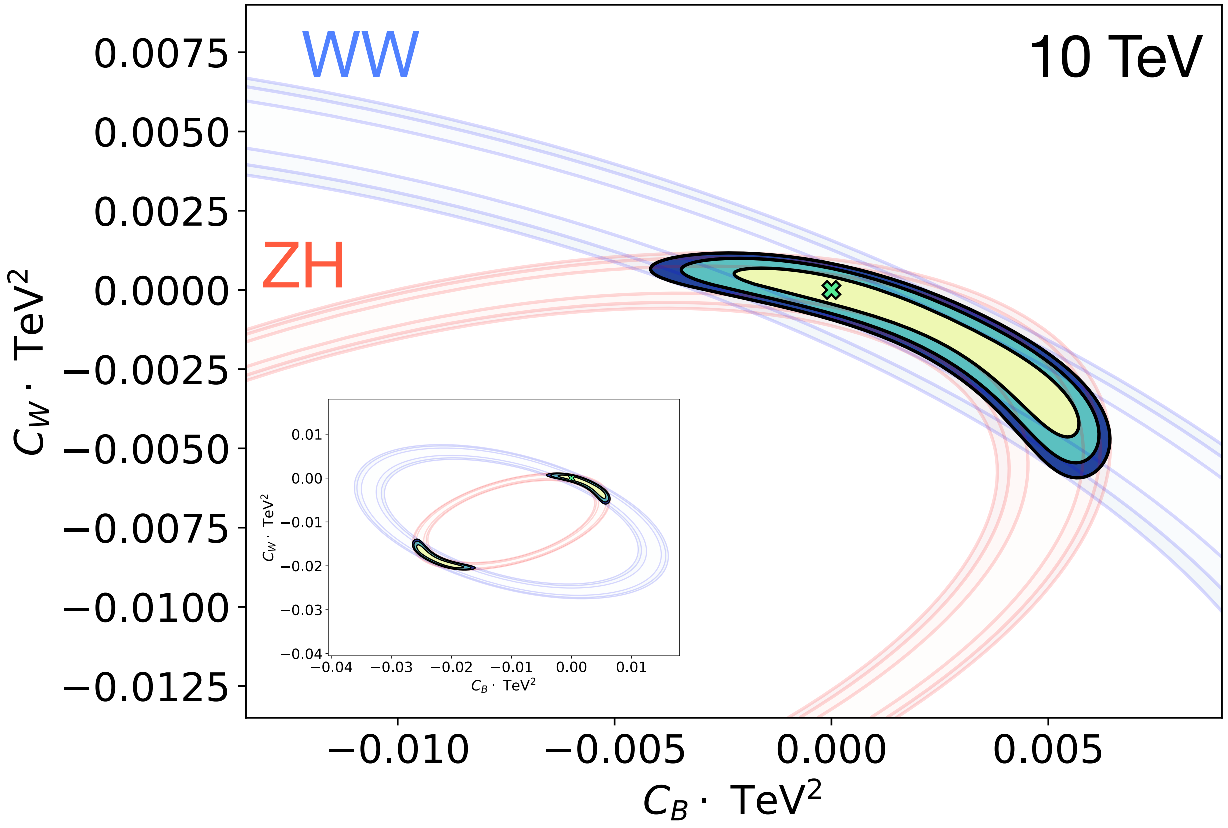
$$\boxed{\begin{aligned}\mathcal{O}_W &= \frac{ig}{2}\left(H^\dagger\sigma^a\overleftrightarrow{D}^\mu H\right)D^\nu W^a_{\mu\nu}\\ \mathcal{O}_B &= \frac{ig'}{2}\left(H^\dagger\overleftrightarrow{D}^\mu H\right)\partial^\nu B_{\mu\nu}\\ \mathcal{O}_{HW} &= ig(D^\mu H)^\dagger\sigma^a(D^\nu H)W^a_{\mu\nu}\\ \mathcal{O}_{HB} &= ig'(D^\mu H)^\dagger(D^\nu H)B_{\mu\nu}\end{aligned}}$$

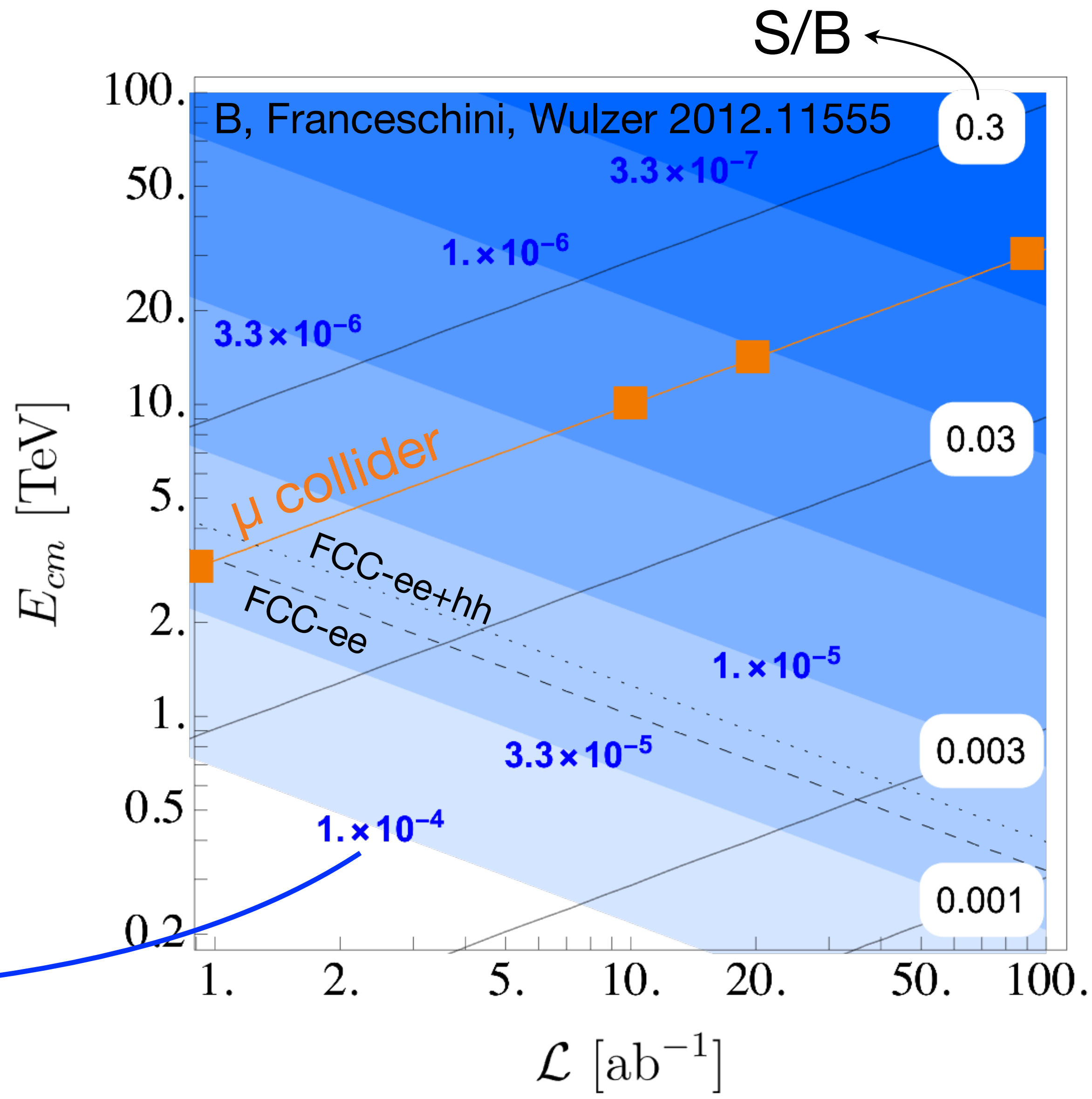
High-energy di-bosons

- C_W and C_B determined from high-energy $\mu^+\mu^- \to ZH$, W^+W^- total cross-sections

Limits on $C_{W,B}$ scale as E^2

$$\sigma_{\mu\mu\to ZH} \approx 122\,\text{ab}\left(\frac{10\,\text{TeV}}{E_{\text{cm}}}\right)^2\left[1+\#\,E_{\text{cm}}^2 C_W+\#\,E_{\text{cm}}^4 C_W^2\right]$$





- In universal theories, $C_{W,B}$ related with Z-pole and other EW observables

$$\hat{S} = m_W^2(C_W + C_B)$$

Muon collider:

$$10\,\text{TeV}: \quad C_W \lesssim (40\,\text{TeV})^{-2}, \quad \hat{S} \lesssim 10^{-6}$$

$$30\,\text{TeV}: \quad C_W \lesssim (120\,\text{TeV})^{-2}, \quad \hat{S} \lesssim 10^{-7}$$

LEP : $\hat{S} \lesssim 10^{-3}$

FCC : $\hat{S} \lesssim 10^{-5}$ ⟵ ultimate precision at Z pole

High-energy WW: angular analysis

- $O_{W,B}$ contribute to longitudinal scattering amplitudes:

$$\mathscr{A}_{00}^{(\mathrm{NP})} = s\,(G_{1L} - G_{3L})\,\sin\theta_\star$$

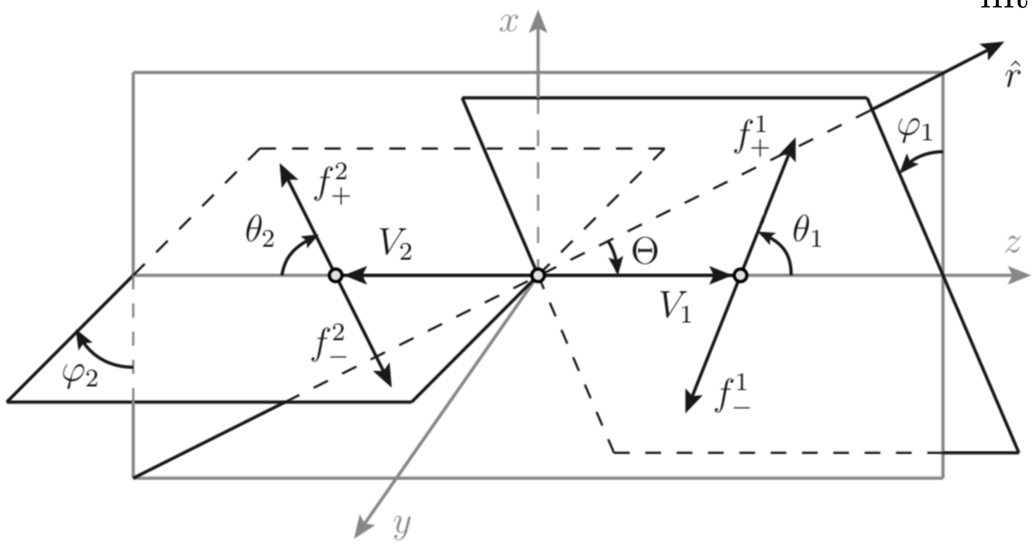
$$\mathscr{A}_{-+} = -\frac{g^2}{2}\sin\theta_\star$$

$$\mathscr{A}_{+-} = g^2\cos^2\frac{\theta_\star}{2}\cot^2\frac{\theta_\star}{2}$$

- In the SM, large contribution to $\mu^+\mu^- \to W^+W^-$ from transverse polarizations.

Interference between ±∓ and 00 helicity amplitudes cancels in the total cross-section ⇒ signal suppressed!

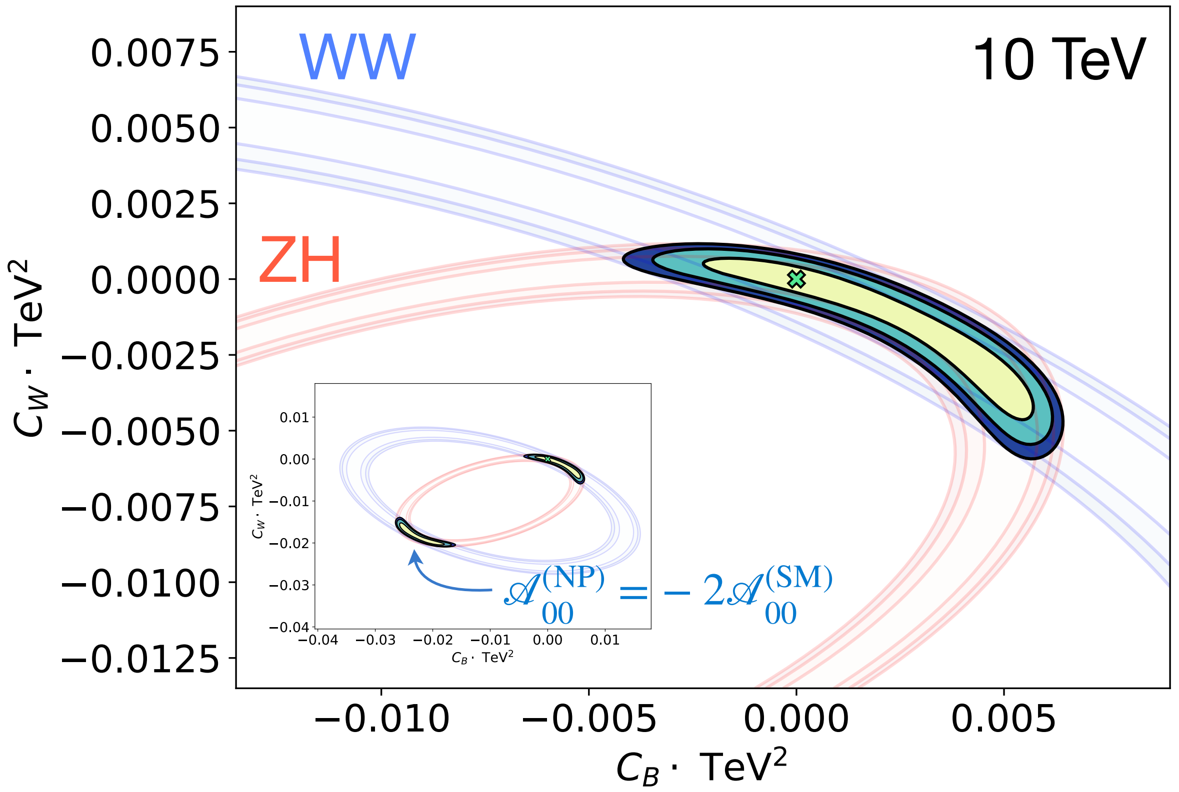
see also Panico et al. 1708.07823, 2007.10356



$$d\sigma_{\text{int}} \propto \mathcal{M}_{00}\mathcal{M}_{+-}\cos(\varphi_+ - \varphi_-)\sin\theta_+(1+\cos\theta_+)\sin\theta_-(1-\cos\theta_-)$$
$$+\mathcal{M}_{00}\mathcal{M}_{-+}\cos(\varphi_+ - \varphi_-)\sin\theta_+(1-\cos\theta_+)\sin\theta_-(1+\cos\theta_-)$$

($\theta_\pm, \varphi_\pm$ polar and azimuthal angle of $W^\pm$ decay products)

- Can exploit the SM/BSM interference by looking at fully differential WW cross-section in scattering and decay angles!



B, Franceschini, Wulzer 2012.11555

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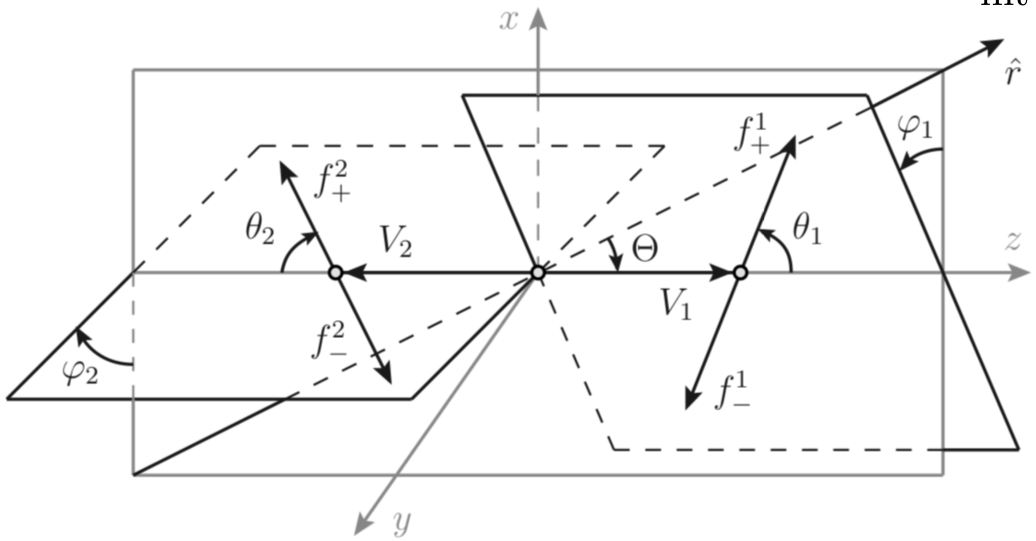

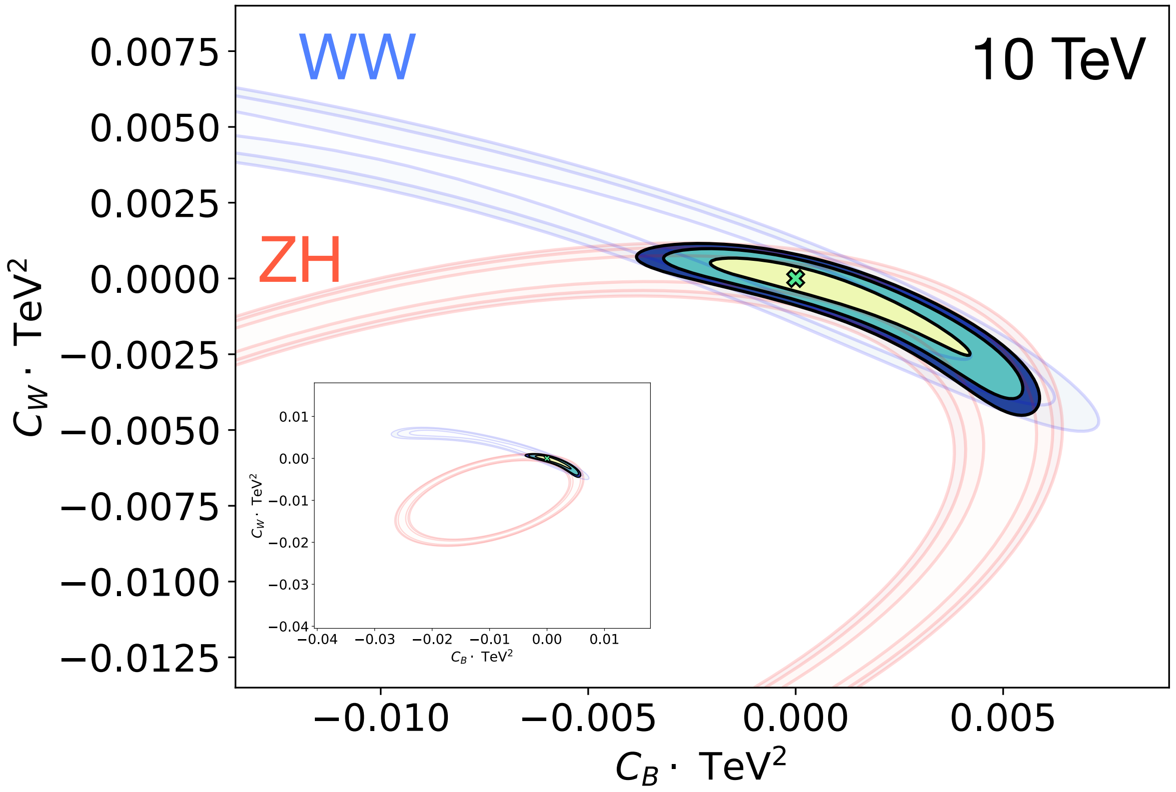

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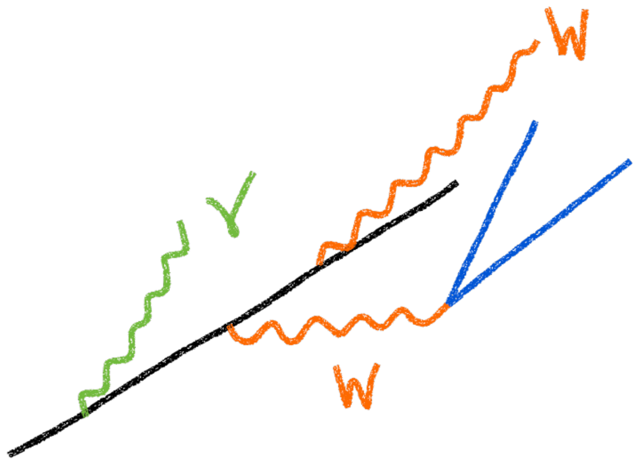
B, Franceschini, Wulzer 2012.11555

EW radiation



EW radiation becomes important at multi-TeV energies!

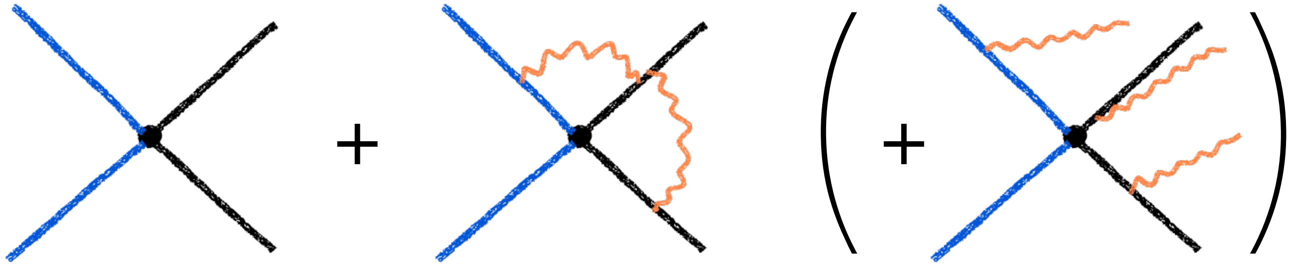
Especially relevant for muon collider, but also FCC-hh…

- ✦ $m_{W,Z} \ll E$: γ, W, Z are all similar!
- ✦ Multiple gauge boson emission is not suppressed

Sudakov factor $\frac{\alpha}{4\pi}\log^2\left(\frac{E^2}{m_W^2}\right) \times$ Casimir ≈ 1 for E ~ 10 TeV

- ☛ Which cross-section? Exclusive, (semi-)inclusive, depending on amount of radiation included

see Chen, Glioti, Rattazzi, Ricci, Wulzer 2202.10509



- ☛ Initial state is EW-charged:

(Precise) resummation of double logs needed. Goal: % or ‰ precision

- ☛ Could one define EW jets? Neutrino “jet tagging”?

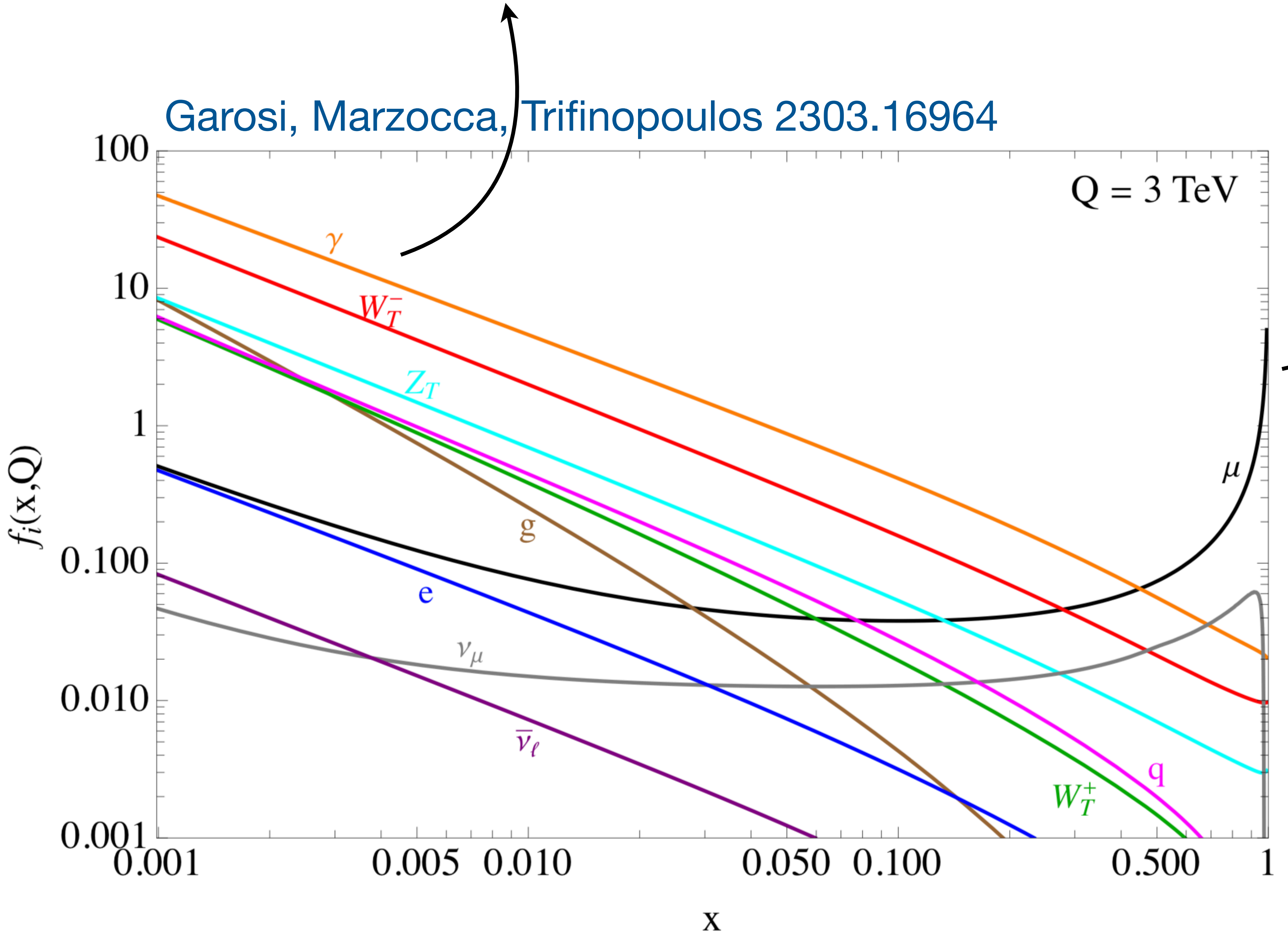
EW radiation

- Resummation of large logarithms: lepton PDF

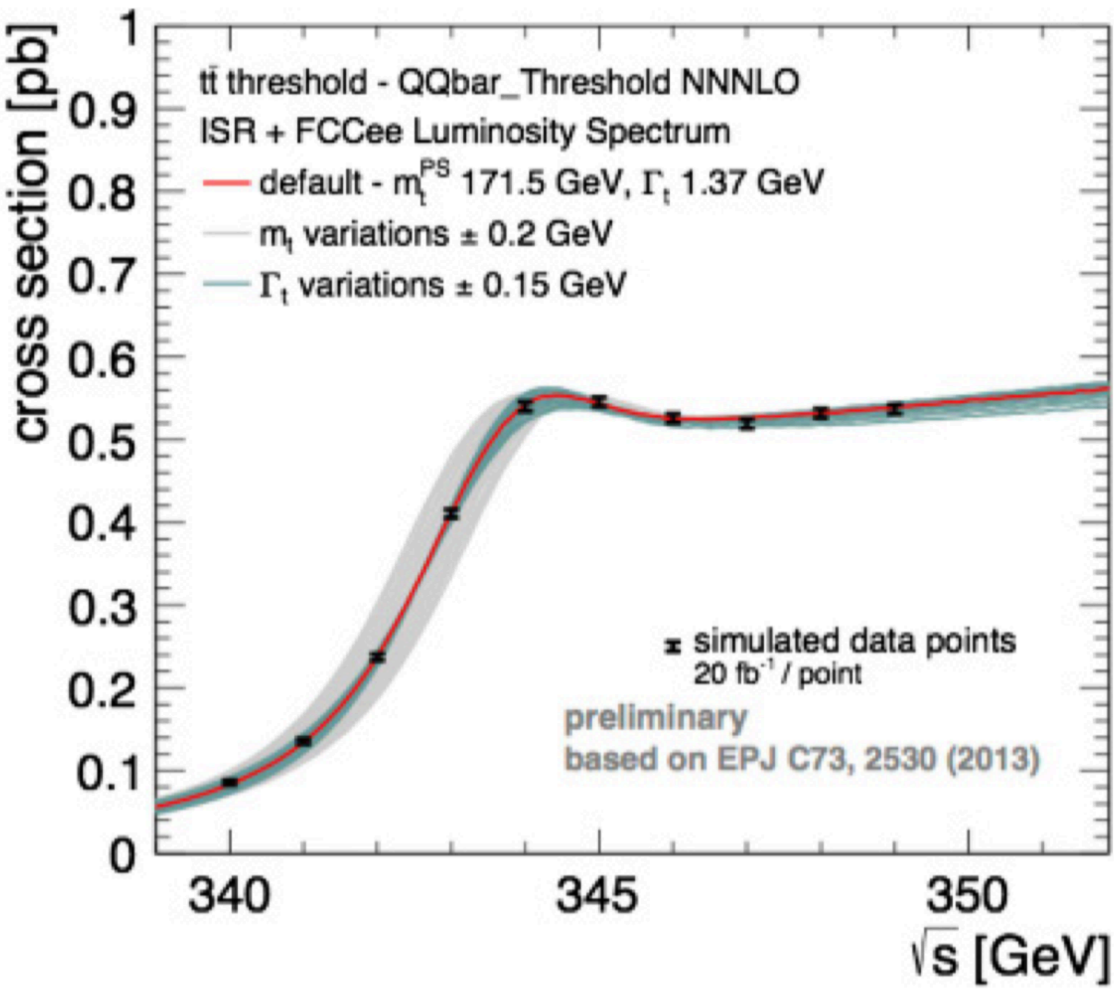
Soft + collinear
radiation: VBF

Elementary leptons:
hard 2 → 2 scattering

Garosi, Marzocca, Trifinopoulos 2303.16964

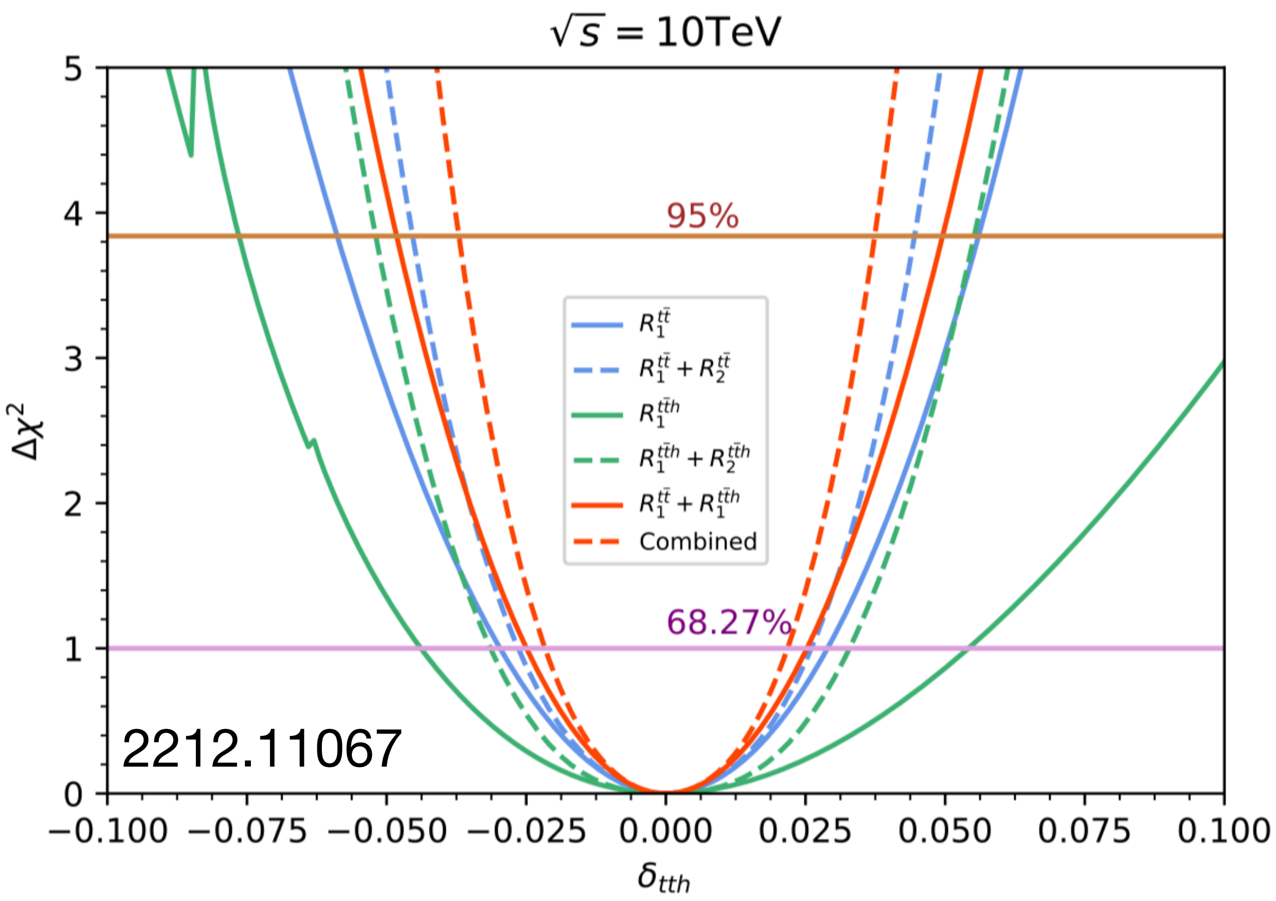


Top quark Yukawa



threshold scan @ FCC

tth @ muon collider



2212.11067

(a) $\mu^+\mu^- \to t\bar{t}\nu\bar{\nu}$ with $\sqrt{s} = 10$ TeV and $L = 10\,\mathrm{ab}^{-1}$.