

# Observation of the $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ decay and measurement of its branching ratio

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on behalf of the NA62 collaboration

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## Contents:

- The golden modes  $K \rightarrow \pi \nu \bar{\nu}$  in the SM and beyond
- NA62 after LS2: detector upgrades & performance
- New measurement of  $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$

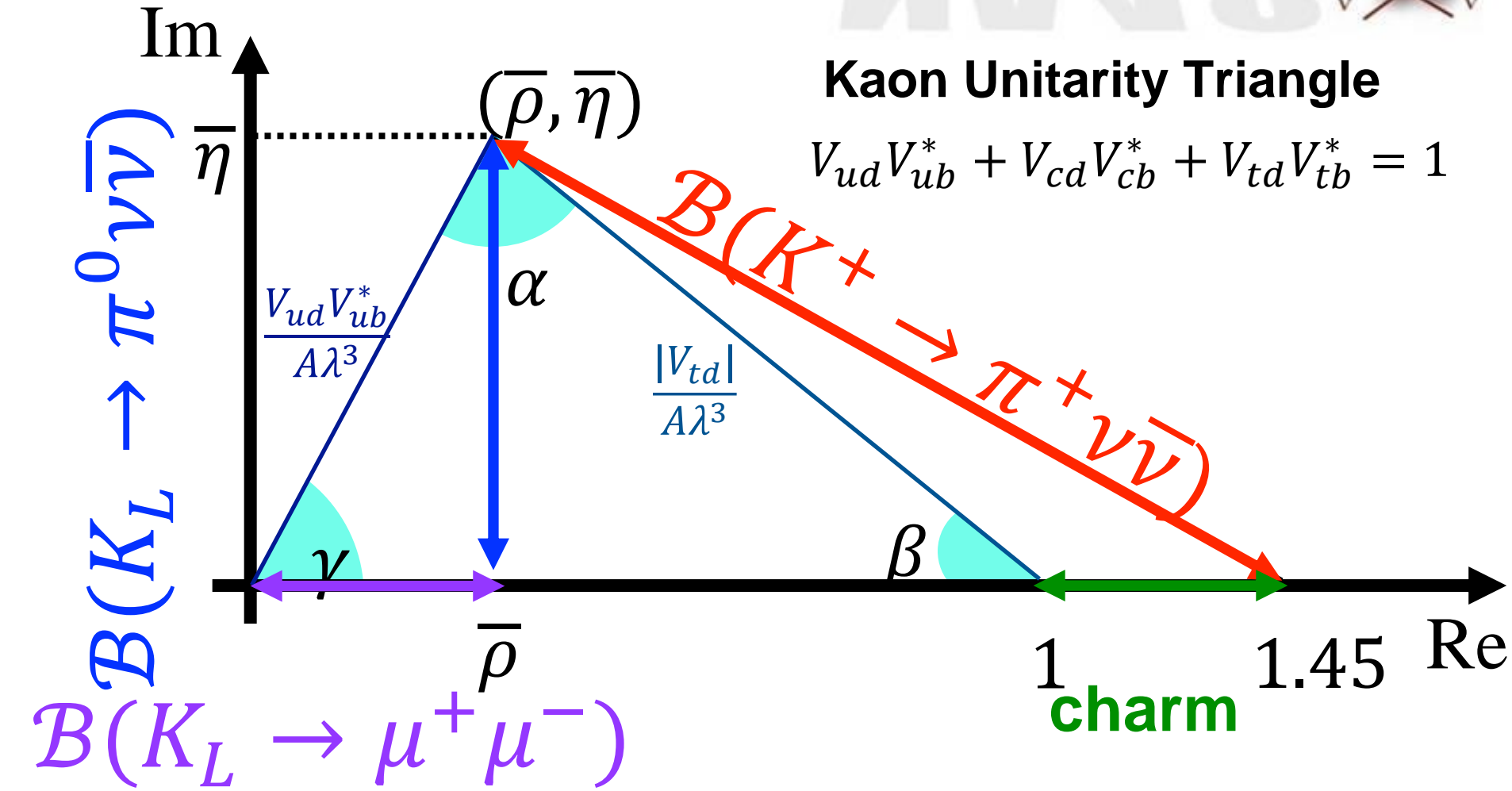
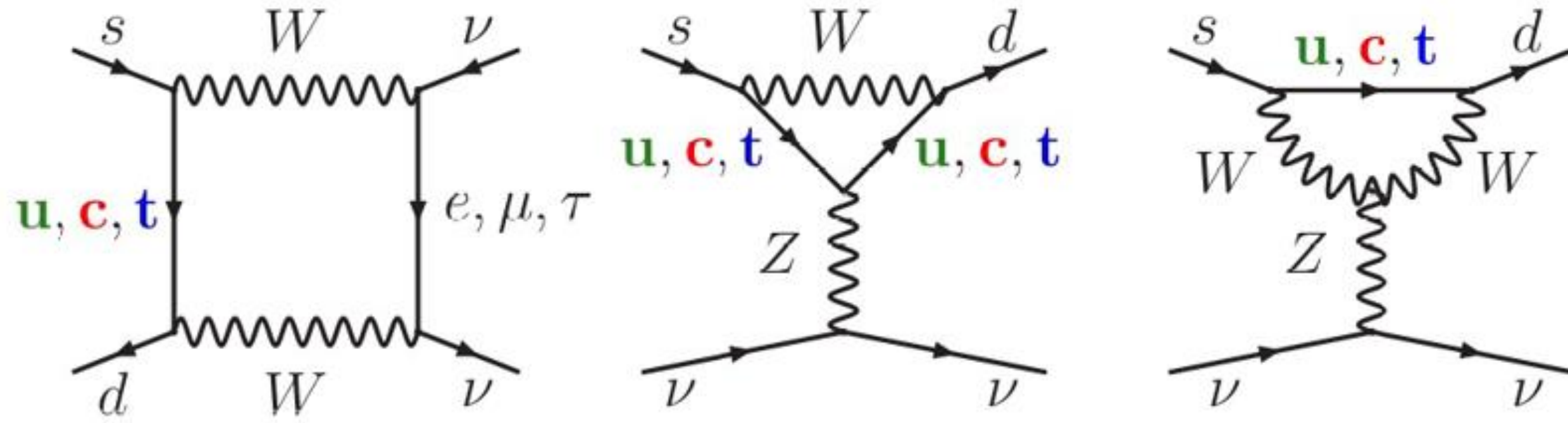
# Rare Kaon Decays: SM and Beyond

The golden modes  $K \rightarrow \pi \nu \bar{\nu}$

# $K \rightarrow \pi \nu \bar{\nu}$ : Precision test of the SM



## SM: Z-penguin & box diagrams



### Kaon Unitarity Triangle

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 1$$

- $\mathcal{B}(K \rightarrow \pi \nu \bar{\nu})$  highly suppressed in SM

- GIM mechanism & maximum CKM suppression  $s \rightarrow d$  transition:  $\sim \frac{m_t}{m_W} |V_{ts}^* V_{td}|$

- Theoretically clean  $\Rightarrow$  high precision SM predictions

- Dominated by short distance contributions.

- Hadronic matrix element extracted from  $\mathcal{B}(K \rightarrow \pi l \nu)$  decays via isospin rotation.

Decay Mode BR	SM [ <a href="#">Buras et al. EPJC 82 (2022) 7, 615</a> ]	SM [ <a href="#">D'Ambrosio et al. JHEP 09 (2022) 148</a> ]	Experimental Status
$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	$(8.60 \pm 0.42) \times 10^{-11}$	$(7.86 \pm 0.61) \times 10^{-11}$	$(10.6_{-3.5}^{+4.1}) \times 10^{-11}$ (NA62)
$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$	$(2.94 \pm 0.15) \times 10^{-11}$	$(2.68 \pm 0.30) \times 10^{-11}$	$< 2 \times 10^{-9}$ (KOTO)

# $K \rightarrow \pi \nu \bar{\nu}$ : Beyond the SM



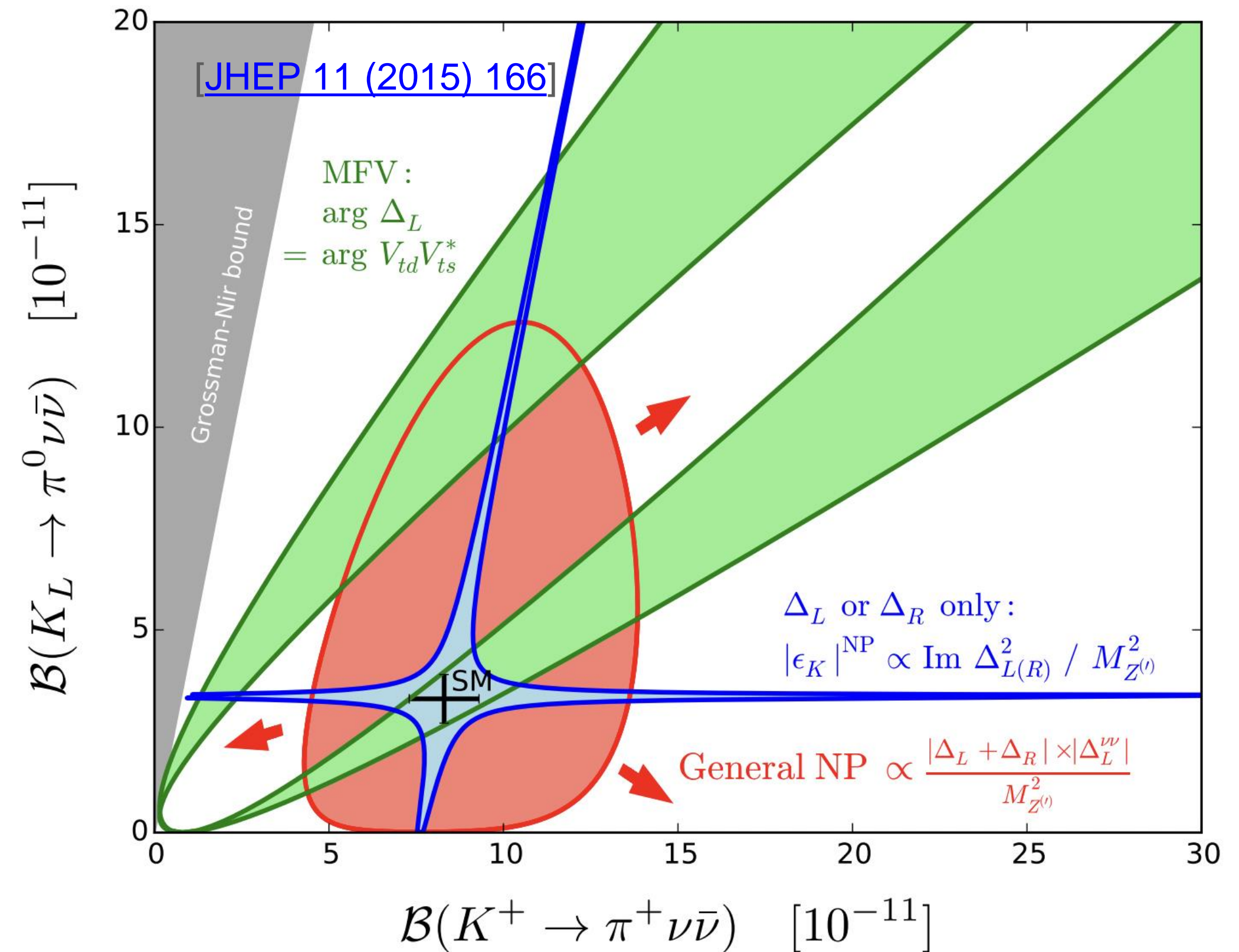
- Correlations between BSM contributions to BRs of  $K^+$  and  $K_L$  modes [[JHEP 11 \(2015\) 166](#)].
  - Must measure both to discriminate between BSM scenarios.
- Correlations with other observables ( $\epsilon'/\epsilon$ ,  $\Delta M_B$ , B-decays) [[JHEP 12 \(2020\) 097](#)][[PLB 809 \(2020\) 135769](#)].
- Leptoquarks [[EPJ.C 82 \(2022\) 4, 320](#)], Interplay between CC and FCNC [[JHEP 07 \(2023\) 029](#)], NP in neutrino sector [[EPJ.C 84 \(2024\) 7, 680](#)] and additional scalar/tensor contributions [[JHEP 12 \(2020\) 186](#)][[arXiv:2405.06742](#)] ...

- **Green:** CKM-like flavour structure
  - Models with Minimal Flavour Violation
- **Blue:** new flavour-violating interactions where LH or RH currents dominate
  - $Z'$  models with pure LH/RH couplings
- **Red:** general NP models without above constraints
- **Grossman-Nir Bound:** model-independent relation

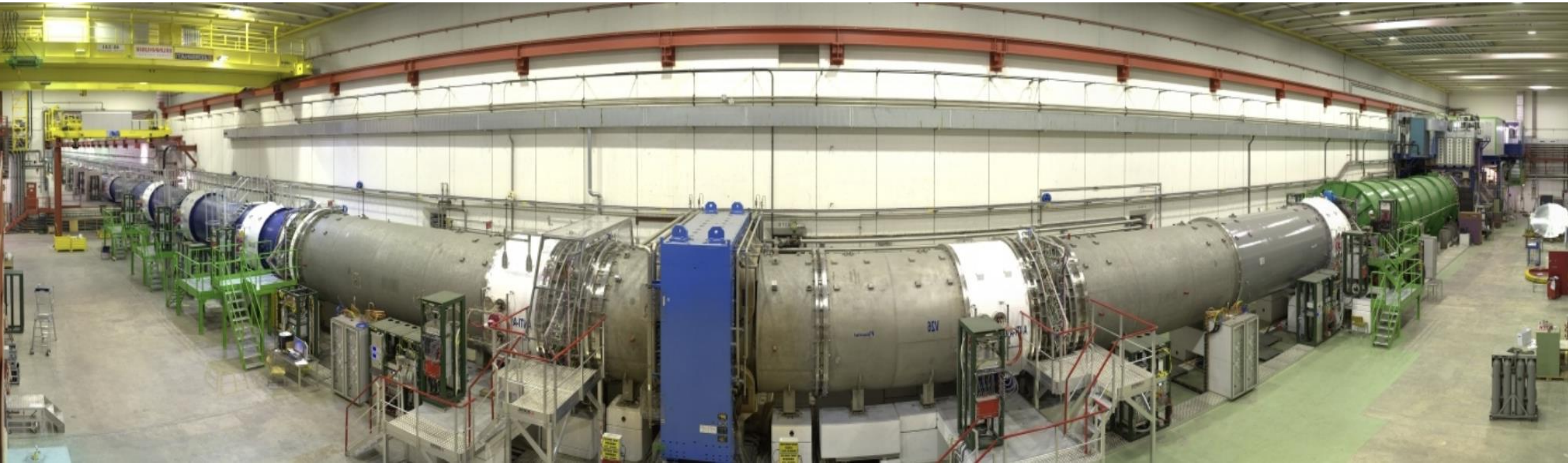
[[PLB 398 \(1997\) 163-168](#)]

$$\frac{\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \tau_{K^+}}{\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \tau_{K_L}} \simeq 1$$

$$\Rightarrow \mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \lesssim 4.3 \cdot \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$$



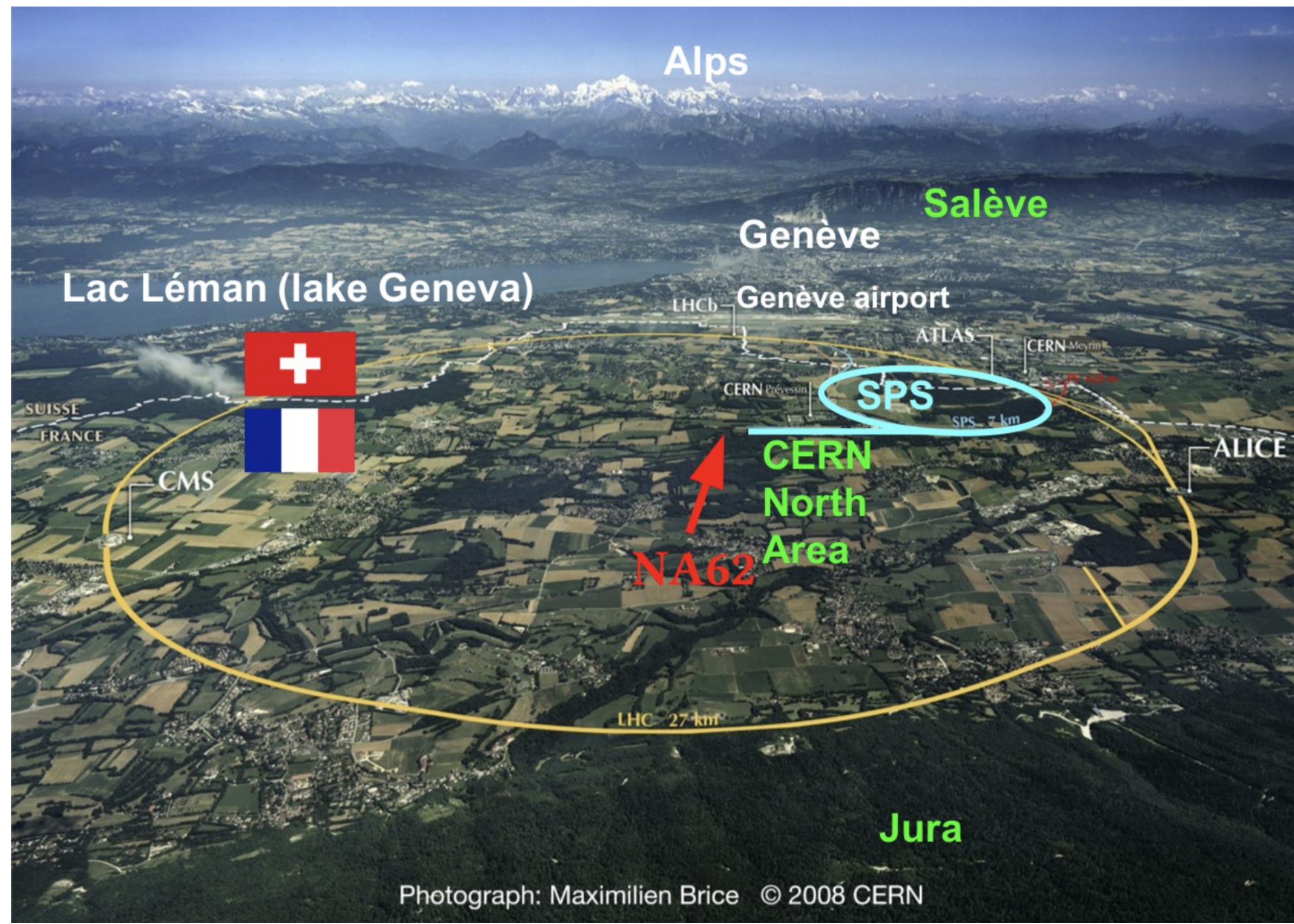
# NA62: The $K^+$ factory at the CERN North Area



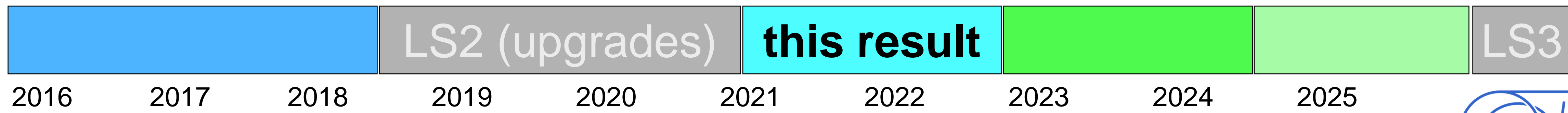
# The NA62 Experiment at CERN



~200 collaborators from ~30 institutions.



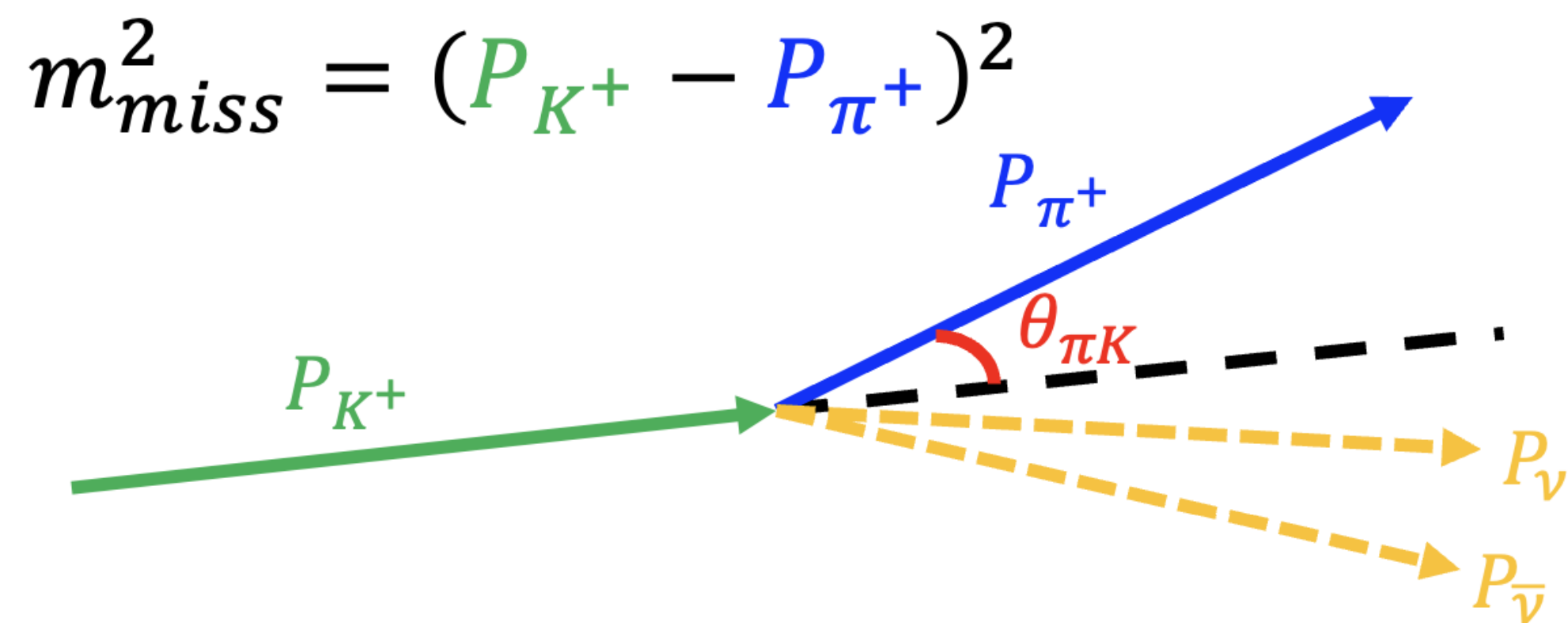
- Primary goal: measurement of  $B(K^+ \rightarrow \pi^+ \nu \bar{\nu})$
- New Technique:  $K^+$  decay-in-flight
- Results: [\[PLB 791 \(2019\) 156\]](#) [\[JHEP 11 \(2020\) 042\]](#) [\[JHEP 06 \(2021\) 093\]](#)
- Broader physics programme:
  - Rare  $K^+$  decays (e.g.  $K^+ \rightarrow \pi^+ \gamma \gamma$  [\[PLB 850 \(2024\) 138513\]](#))
  - LNV/LFV decays (e.g.  $K^+ \rightarrow \pi^- (\pi^0) e^+ e^+$  [\[PLB 830 \(2022\) 137172\]](#))
  - Exotics (e.g. Dark photon [\[PRL 133 \(2024\) 11, 111802\]](#))
- Data taking
  - 2016 Commissioning + Physics run (45 days).
  - 2017 Physics run (160 days).
  - 2018 Physics run (217 days).
  - 2021 Physics run (85 days [10 beam dump]).
  - 2022 Physics run (215 days).
  - 2023 Physics run (150 days [10 beam dump]).
  - 2024 Physics run ongoing ...



# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ at NA62

## NA62 Strategy:

- Tag  $K^+$  and measure momentum.
- Identify  $\pi^+$  and measure momentum.
- Match  $K^+$  and  $\pi^+$  in time & form vertex.
- Determine  $m_{miss}^2 = (P_K - P_\pi)^2$
- Reject any additional activity.



## NA62 Performance Keystones:

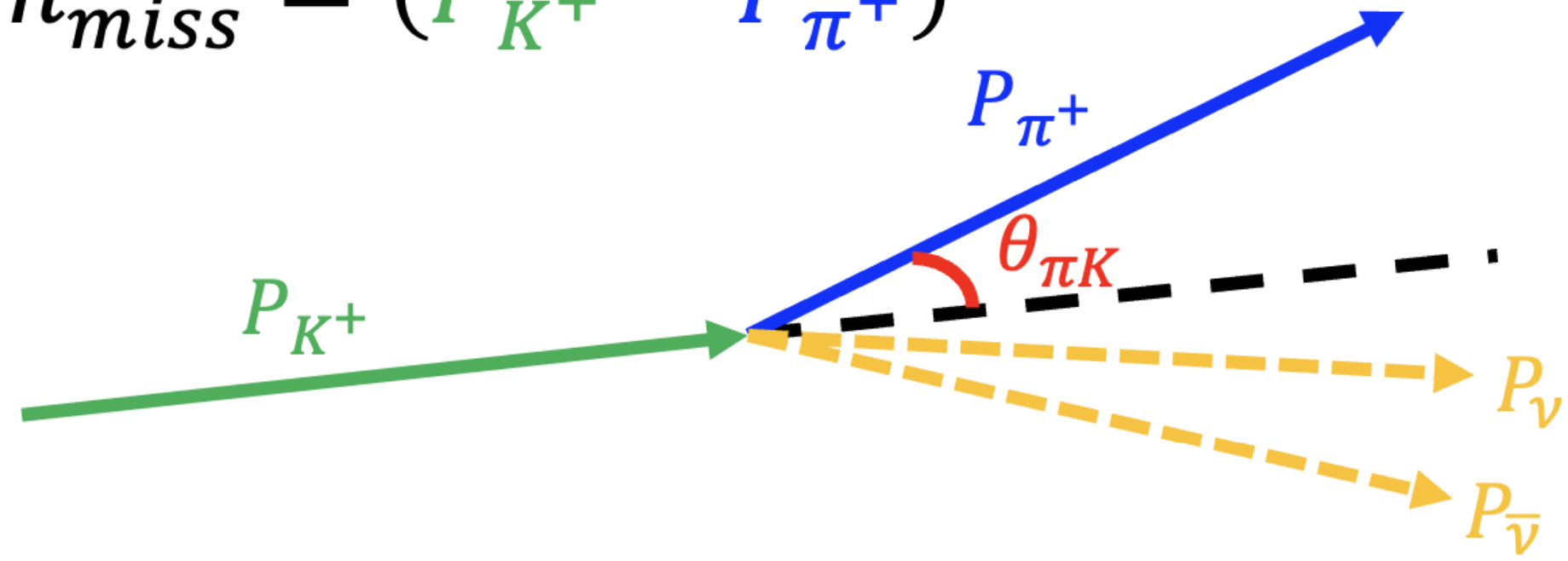
- $\mathcal{O}(100)ps$  timing between detectors
- $\mathcal{O}(10^4)$  background suppression from kinematics
- $> 10^7$  muon rejection
- $> 10^7$  rejection of  $\pi^0$  from  $K^+ \rightarrow \pi^+ \pi^0$  decays

Decay mode	Branching Ratio [PDG]
$K^+ \rightarrow \mu^+ \nu_\mu$	$(63.56 \pm 0.11)\%$
$K^+ \rightarrow \pi^+ \pi^0$	$(20.67 \pm 0.08)\%$
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	$(5.583 \pm 0.024)\%$
$K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$	$(4.247 \pm 0.024) \times 10^{-5}$

$K^+ \rightarrow \pi^+ \nu \bar{\nu} \approx 10^{-10}$

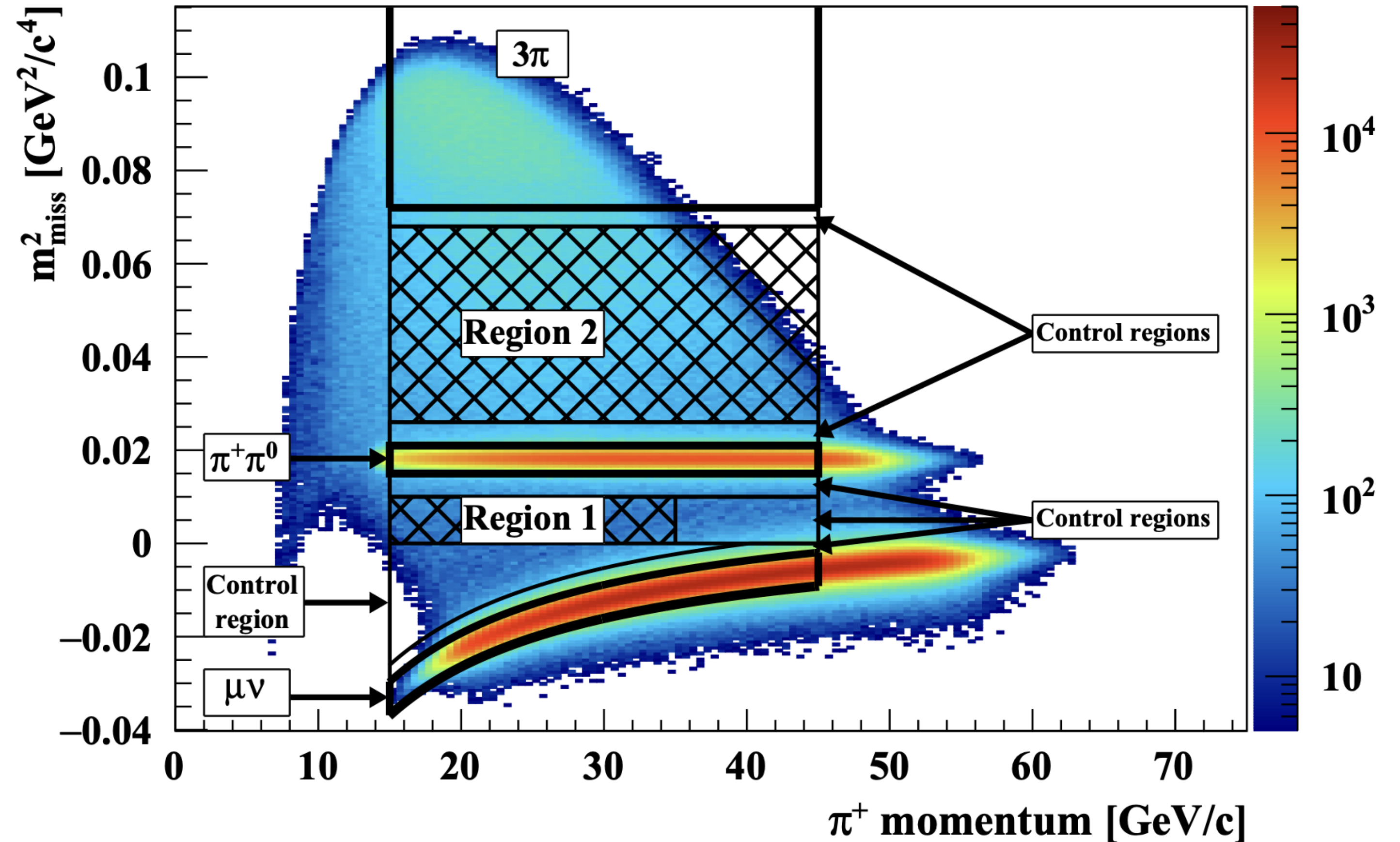
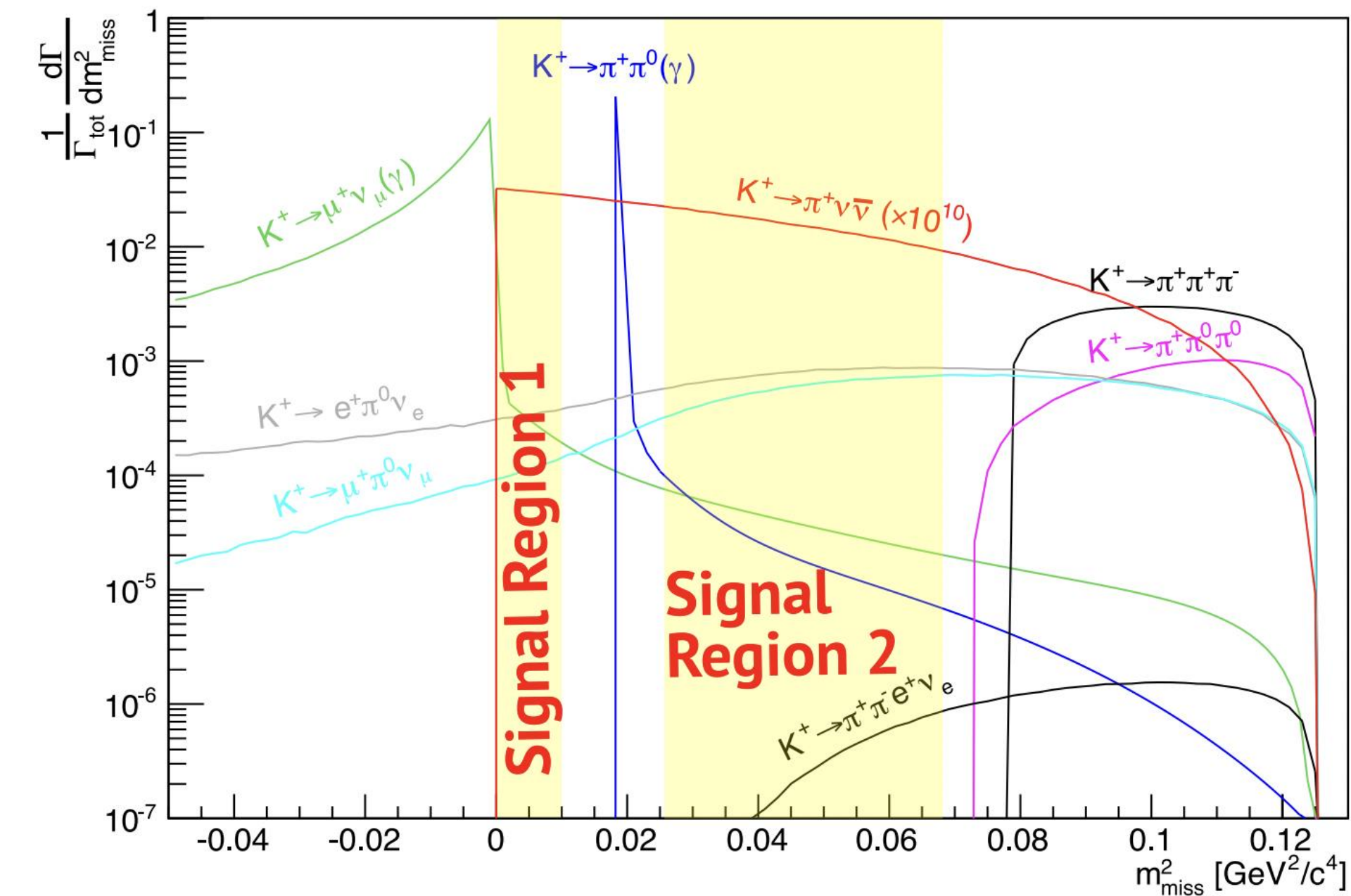
# Kinematic constraints & signal regions

$$m_{miss}^2 = (P_{K^+} - P_{\pi^+})^2$$



$\mathcal{O}(10^4)$  background suppression from kinematics

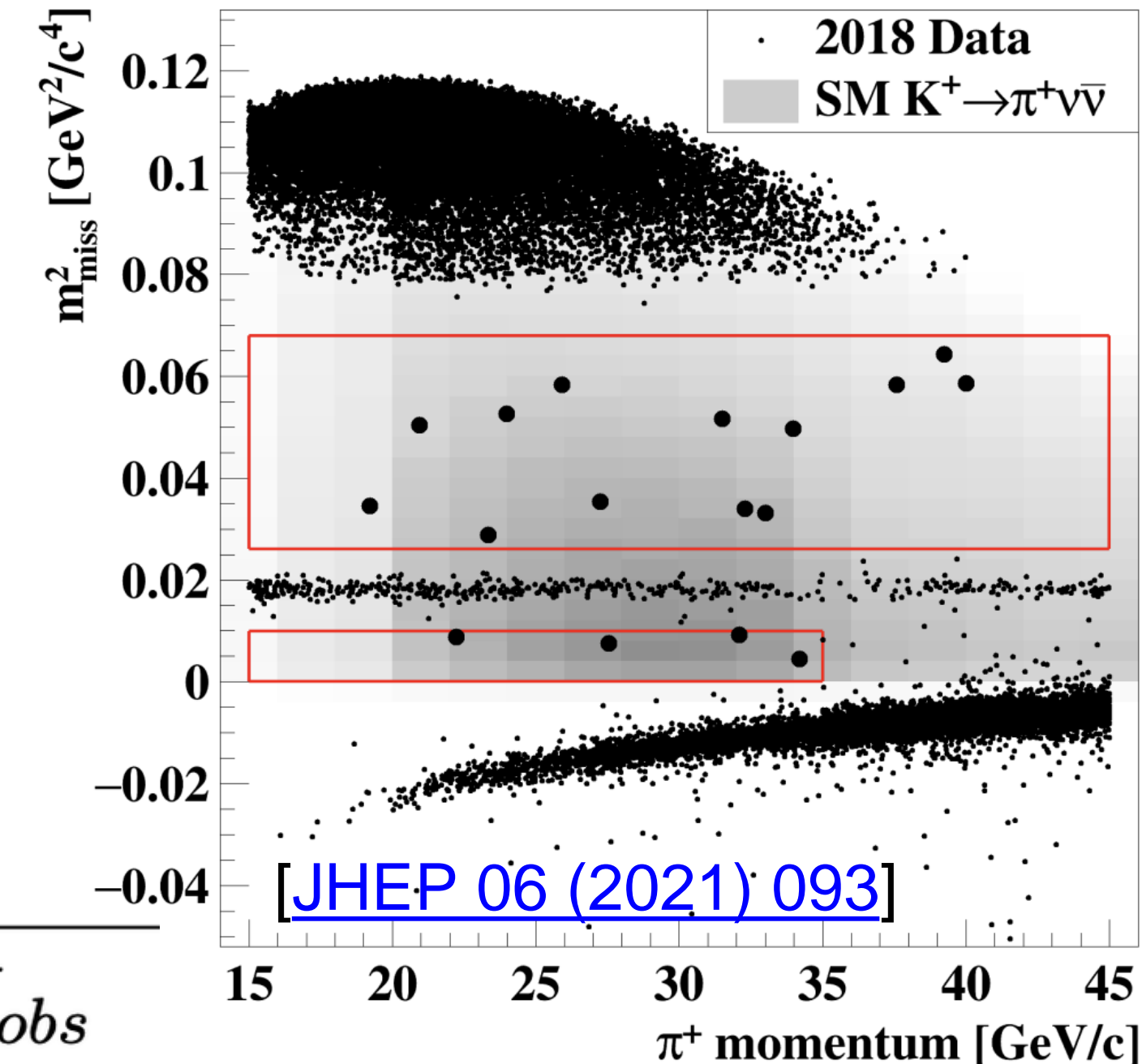
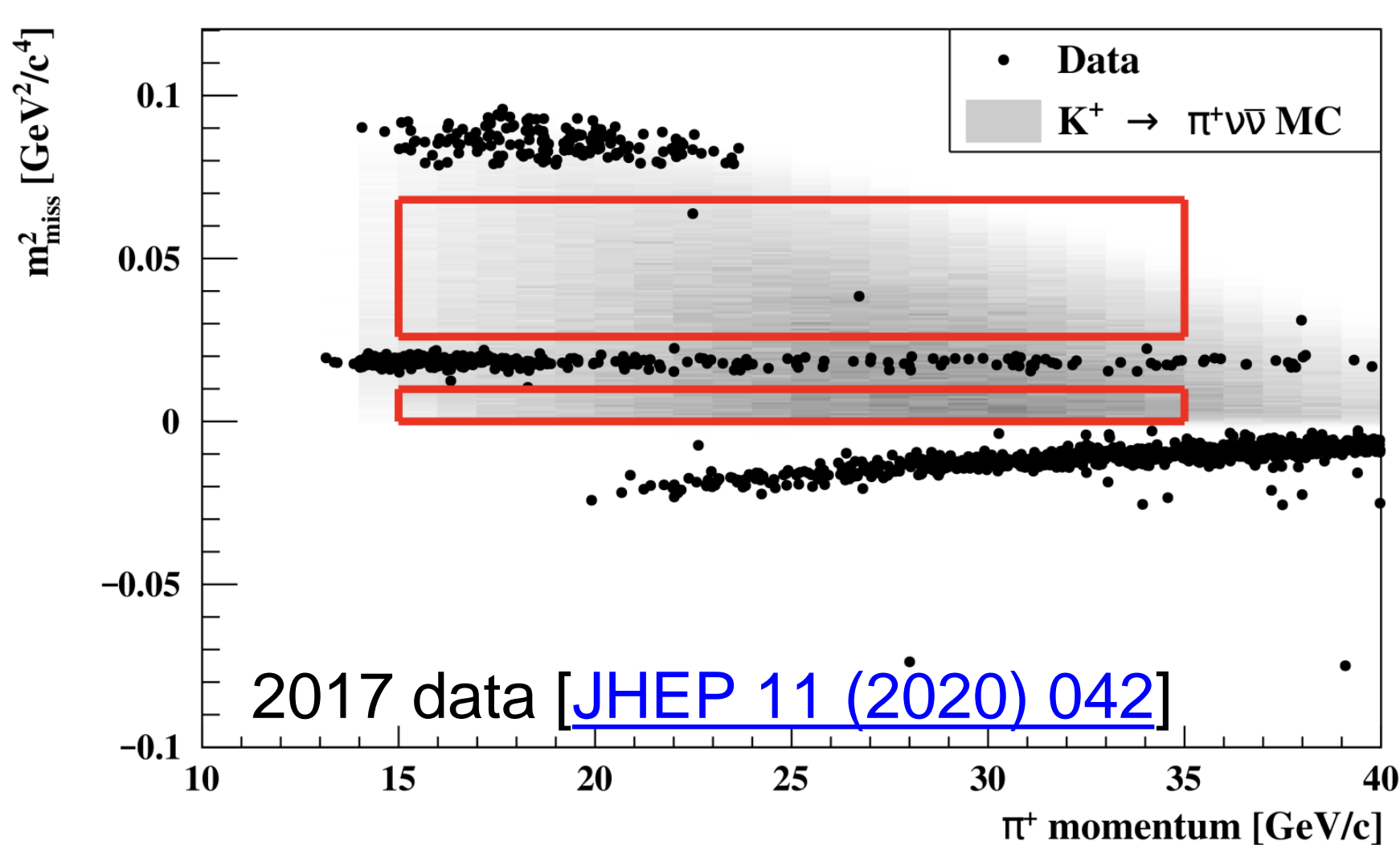
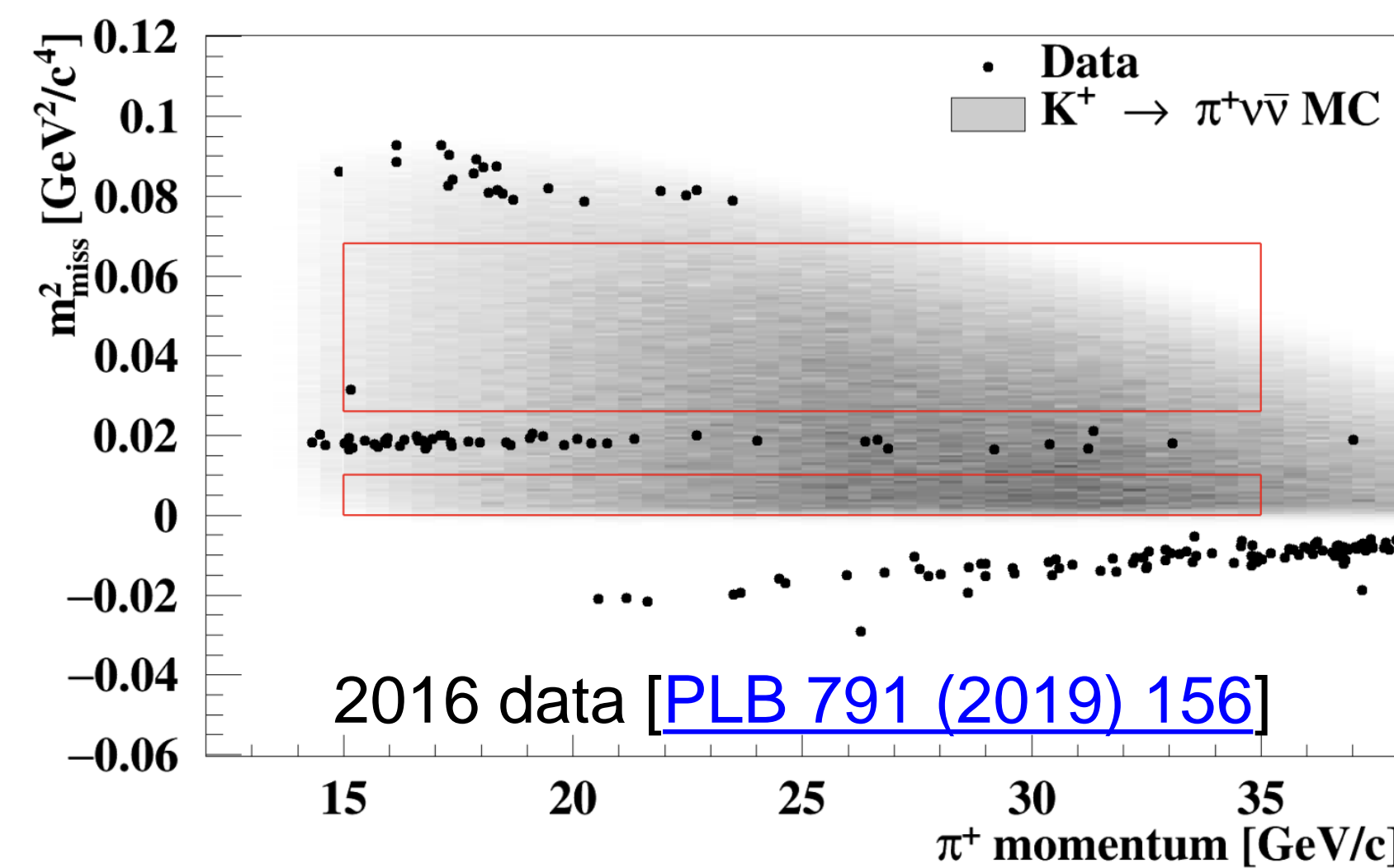
[JHEP 06 (2021) 093]



$\pi^+$  momentum range: 15—45 GeV/c



# The story so far: $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ with 2016–18 data



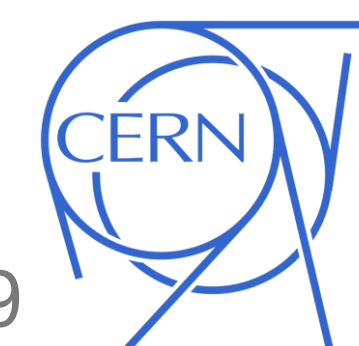
Data-taking year	[Reference]	$N_{bg}$	$N_{\pi\nu\bar{\nu}}^{SM,exp}$	$N_{obs}$
2016	[PLB 791 (2019) 156]	$0.152^{+0.093}_{-0.035}$	$0.267 \pm 0.020$	1
2017	[JHEP 11 (2020) 042]	$1.46 \pm 0.33$	$2.16 \pm 0.13$	2
2018	[JHEP 06 (2021) 093]	$5.42^{+0.99}_{-0.75}$	$7.58 \pm 0.40$	17
2016–18	[JHEP 06 (2021) 093]	$7.03^{+1.05}_{-0.82}$	$10.01 \pm 0.42$	20

$N_{\pi\nu\bar{\nu}}^{SM,exp}$  assumes:  
 $B_{\pi\nu\bar{\nu}}^{SM} = 8.4 \times 10^{-11}$

Statistical combination:

$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (10.6^{+4.0}_{-3.4}|_{stat} \pm 0.9_{syst}) \times 10^{-11} @ 68\% CL$$

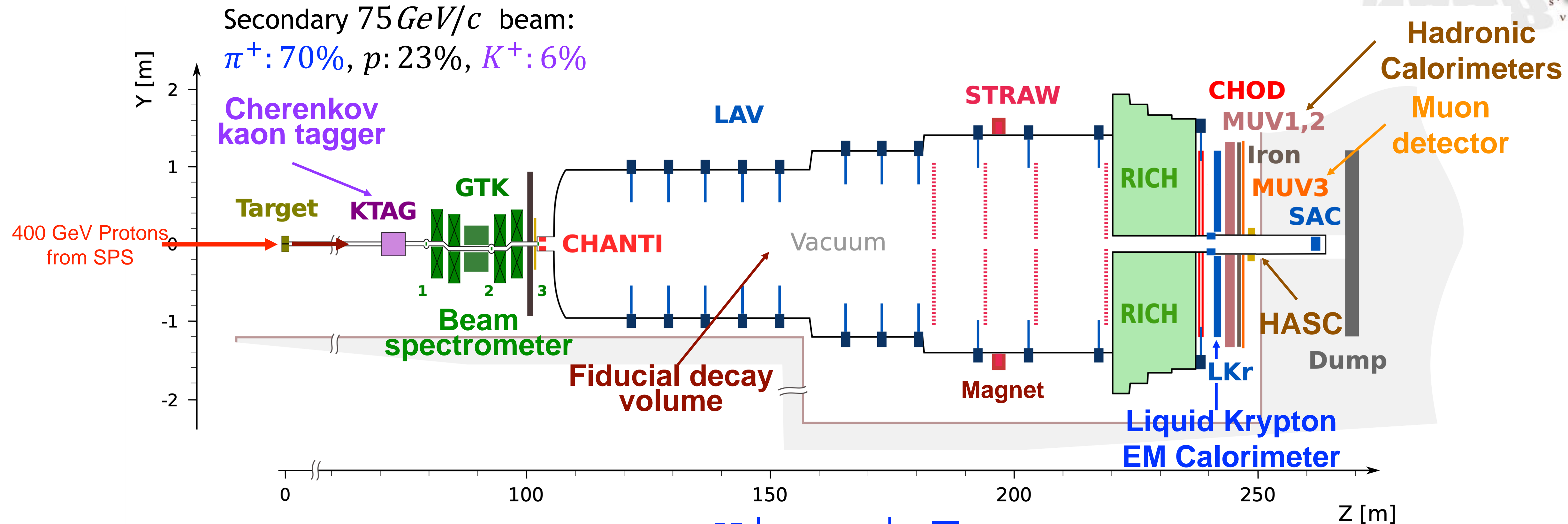
$$\text{Background-only hypothesis: } p = 3.4 \times 10^{-4} \Rightarrow \text{significance} = 3.4\sigma$$



# NA62 Detector, Upgrades & Performance

# NA62 beamline & detector

[JINST 12 (2017) 05, P05025]



- Designed & optimised for study of  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  :
  - Particle tracking: beam particle (GTK) & downstream tracks (STRAW)
  - PID:  $K^+$  - KTAG,  $\pi^+$  - RICH, Calorimeters (LKr, MUV1,2), MUV3 ( $\mu$  detector)
  - Comprehensive veto systems: CHANTI (beam interactions), LAV, LKr, IRC, SAC ( $\gamma$ )

# Particle ID performance : 2021–22 data

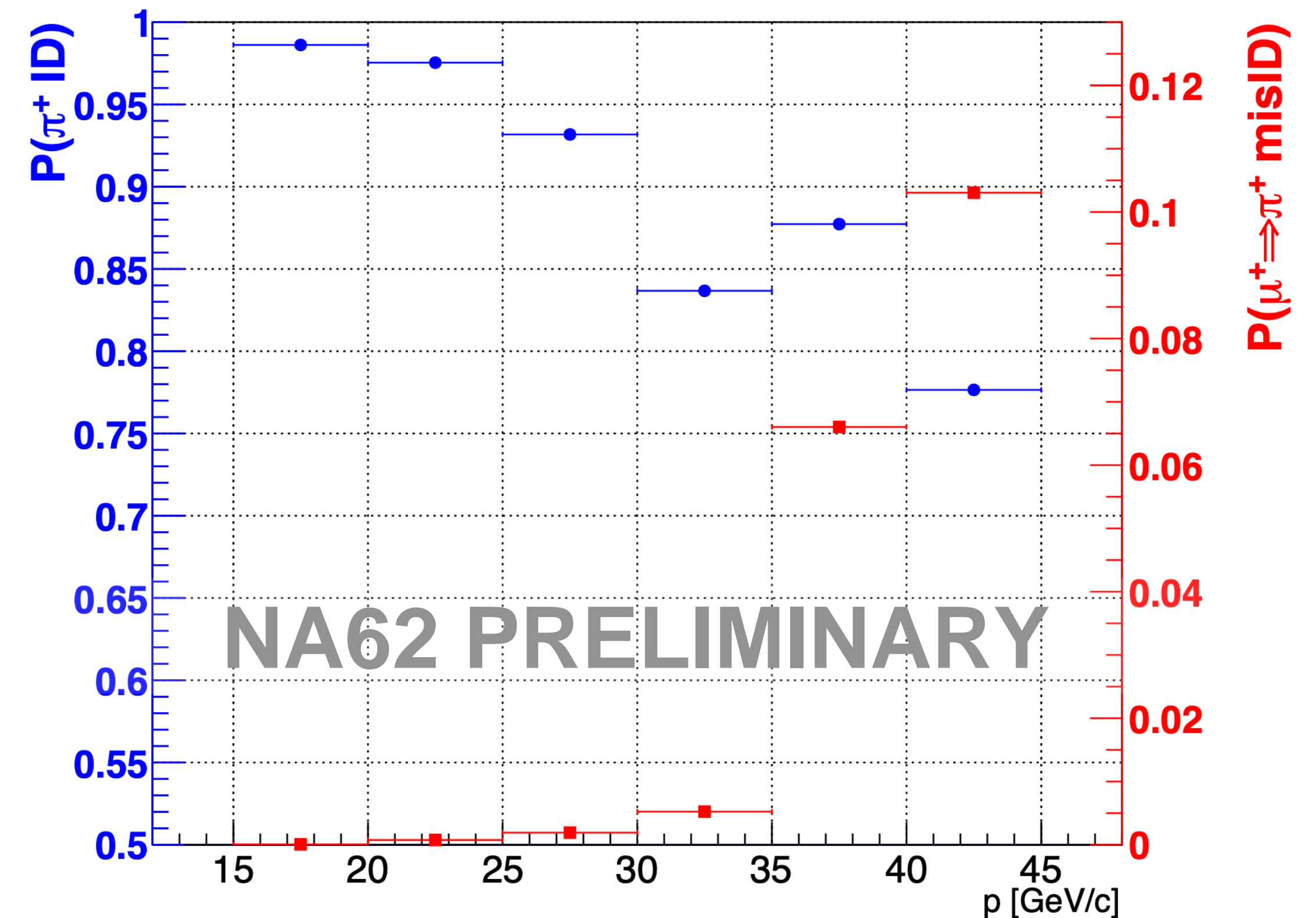
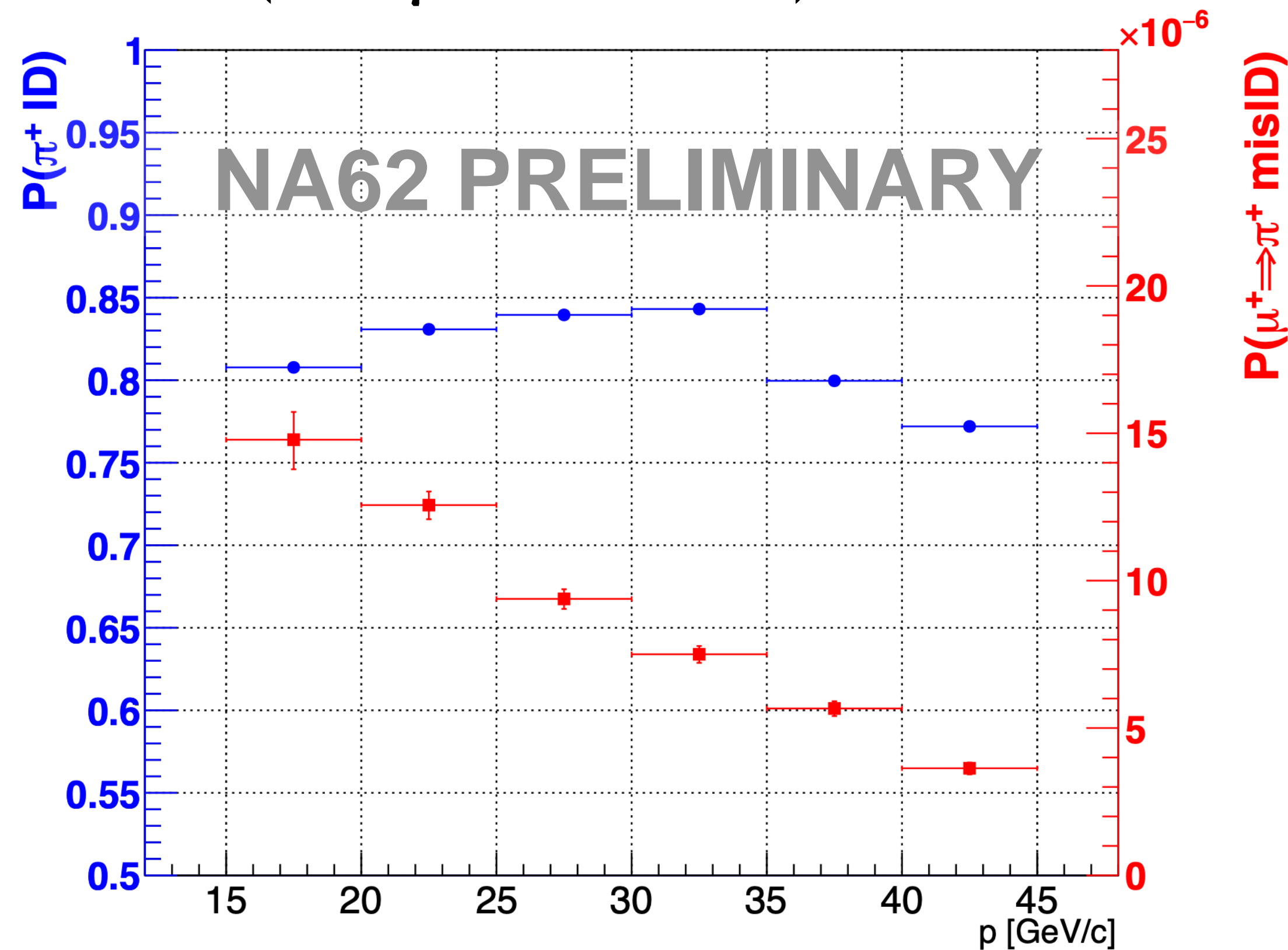


## Calorimeters

## RICH

- Use BDT classifier for LKr & MUV1,2
- + MUV3 (fast  $\mu^+$  detector)

Designed to distinguish between  $\pi^+ / \mu^+$  with 15 – 35  $GeV/c$



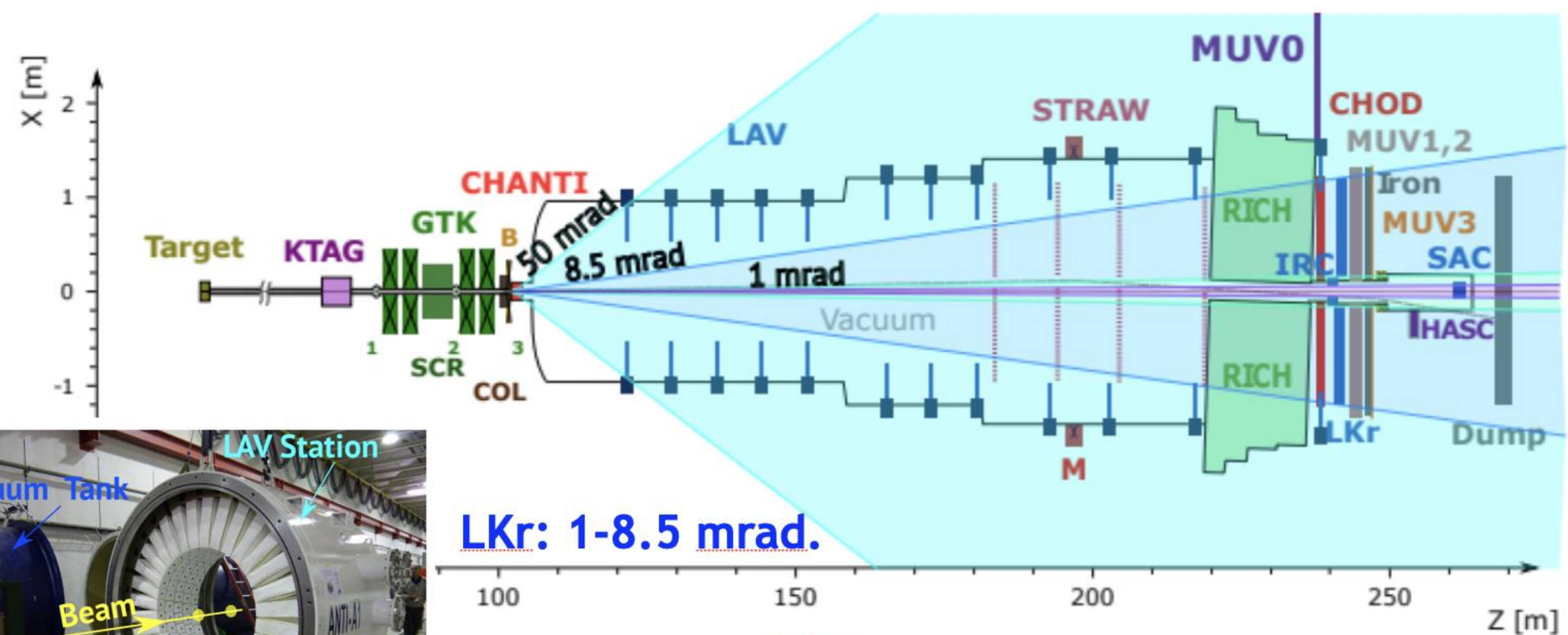
$$P(\pi^+) = 73 \%$$

$$P(\mu^+ \Rightarrow \pi^+) = (1.3 \pm 0.2) \times 10^{-8}$$

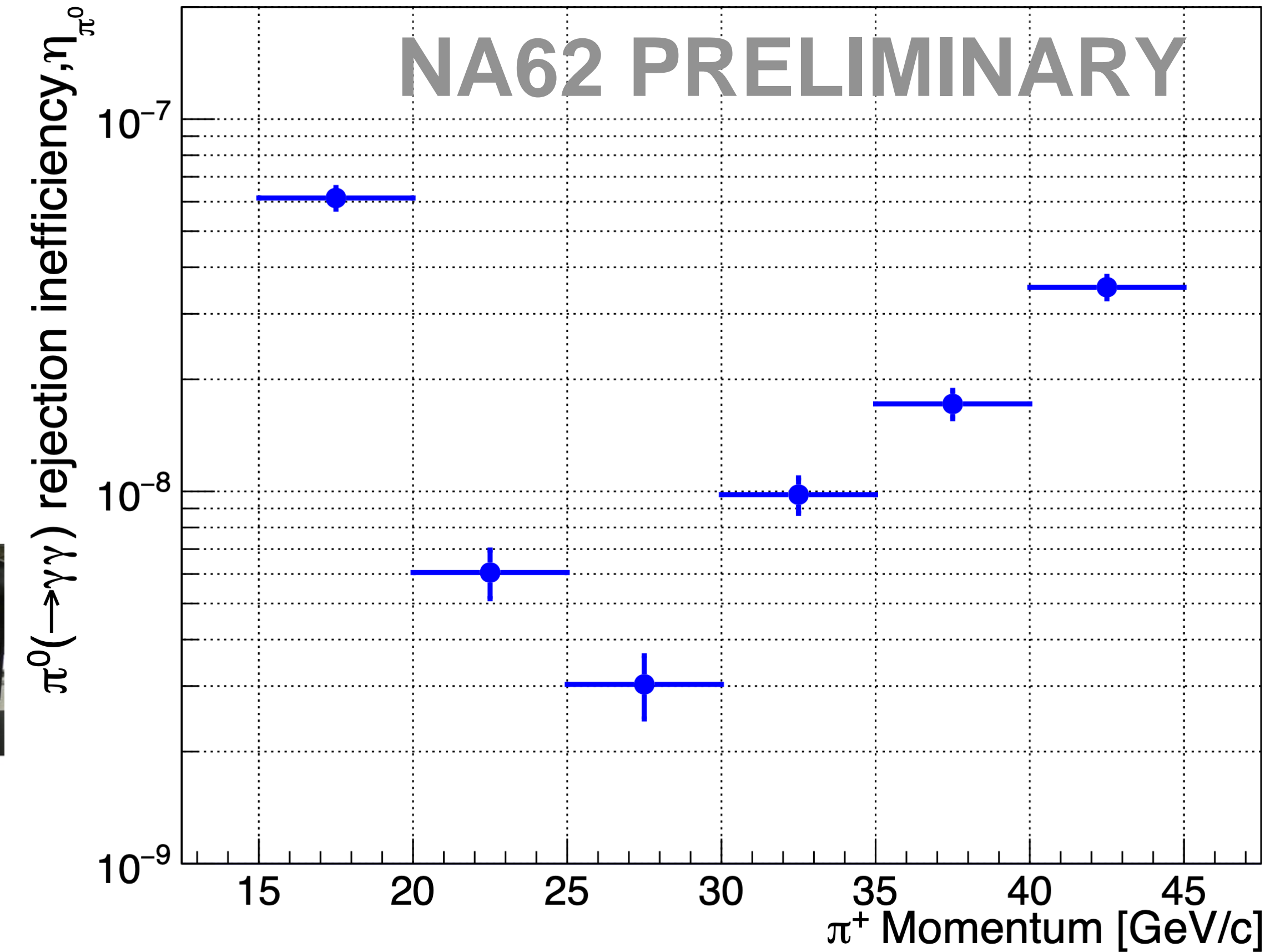
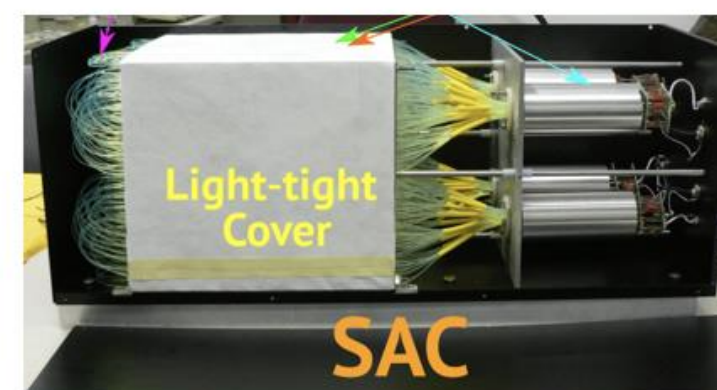
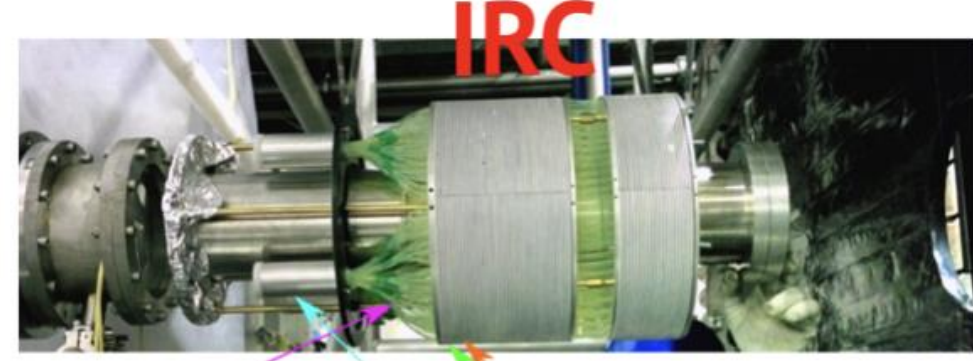
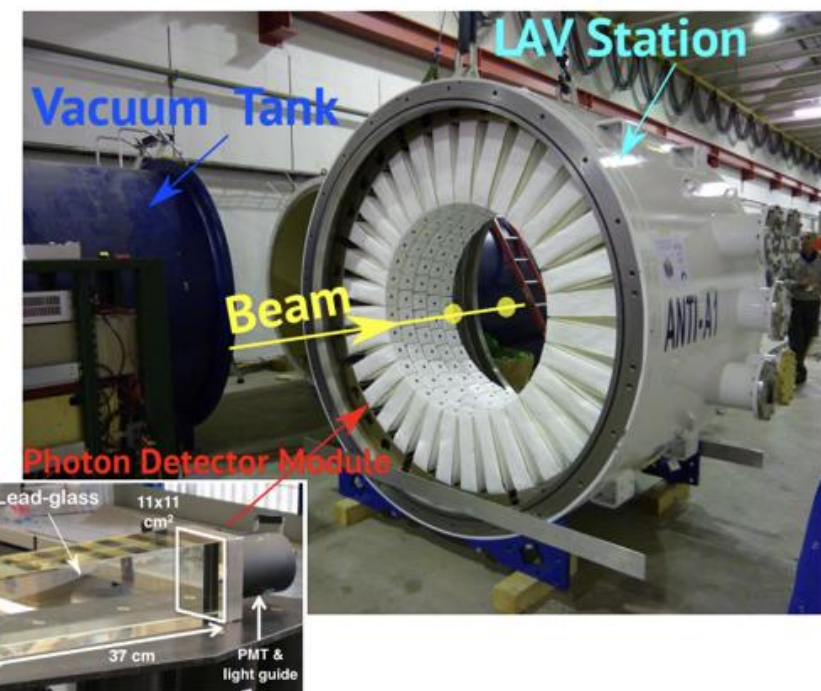
# Comprehensive photon veto system: 21–22



Control sample of  $K^+ \rightarrow \pi^+ \pi^0$



LKr: 1-8.5 mrad.



- Probability of  $K^+ \rightarrow \pi^+ \pi^0$ ,  $\pi^0 \rightarrow \gamma\gamma$  events passing all photon veto conditions:

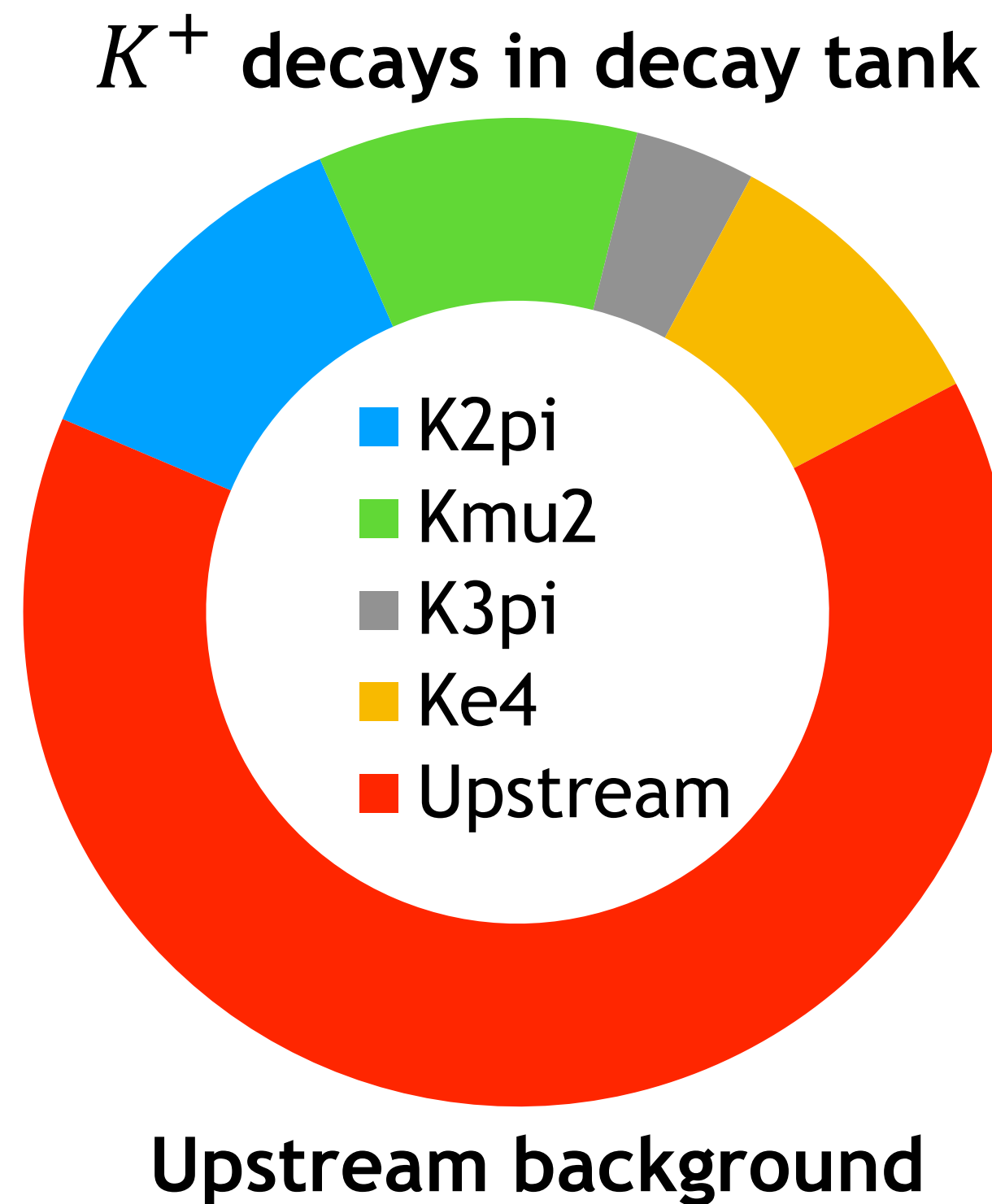
$$\eta_{\pi^0} = (1.72 \pm 0.07) \times 10^{-8}$$

- Meets target: combined  $\gamma/\pi^0$  rejection of  $\mathcal{O}(10^8)$

# Upgrading NA62

- 2016–18 analysis proved NA62 technique.
- **Limitation: tight cuts to reject backgrounds  $\Rightarrow$  reduces signal efficiency.**
- To improve: need new tools to control background.

Background	N(exp) 2018 (S2)
Upstream	$2.76^{+0.90}_{-0.70}$
$K^+ \rightarrow \pi^+ \pi^0$	$0.52 \pm 0.05$
$K^+ \rightarrow \mu^+ \nu$	$0.45 \pm 0.06$
$K^+ \rightarrow \pi^+ \pi^- e^+ \nu$	$0.41 \pm 0.10$
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	$0.17 \pm 0.08$
Total	$4.31^{+0.91}_{-0.72}$



**Largest backgrounds:**

1. **Upstream**
2.  $K^+ \rightarrow \pi^+ \pi^0$

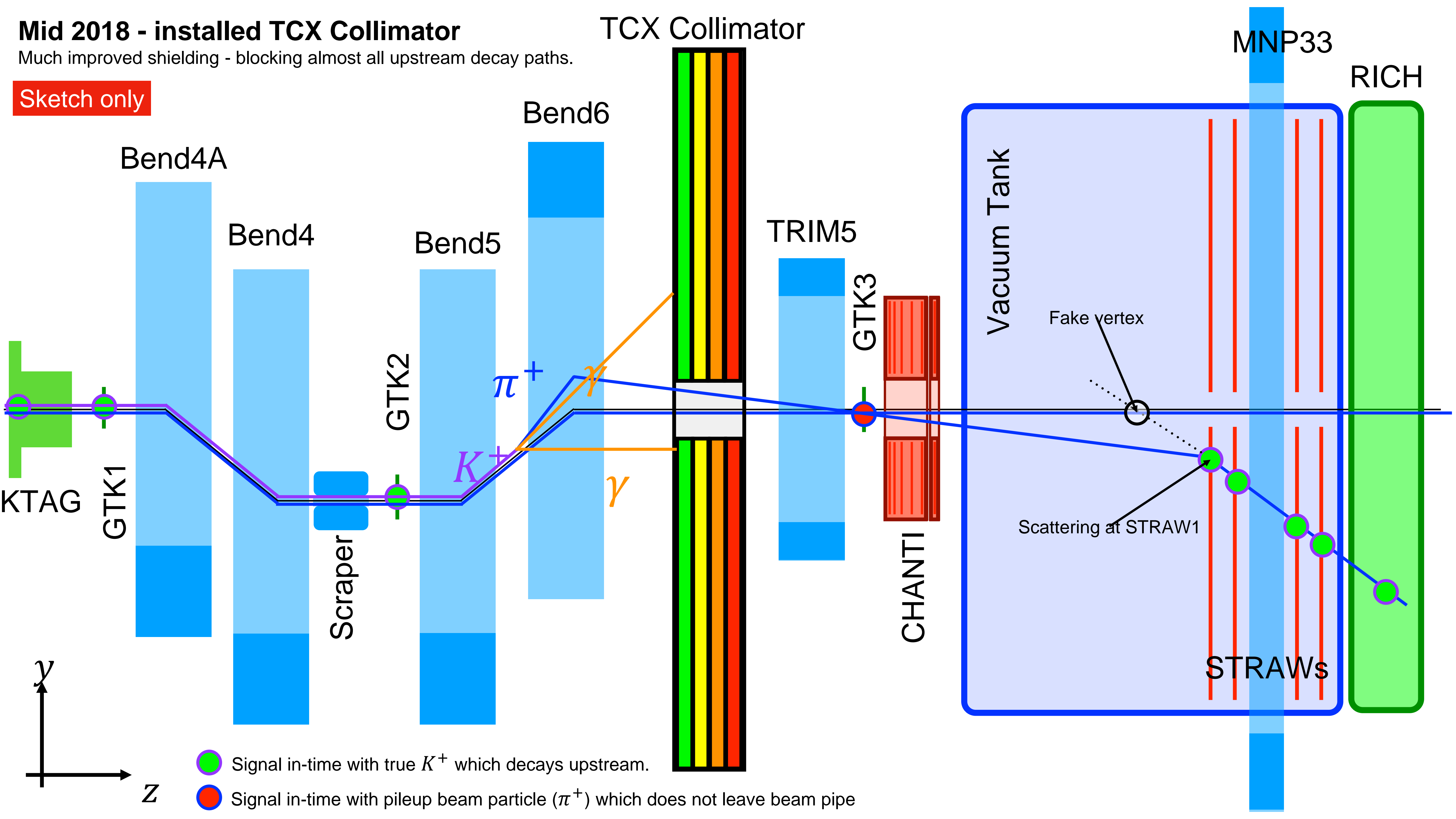
**Veto by detecting previously missed particles...**

# Mid 2018 - installed TCX Collimator

Much improved shielding - blocking almost all upstream decay paths.

Sketch only

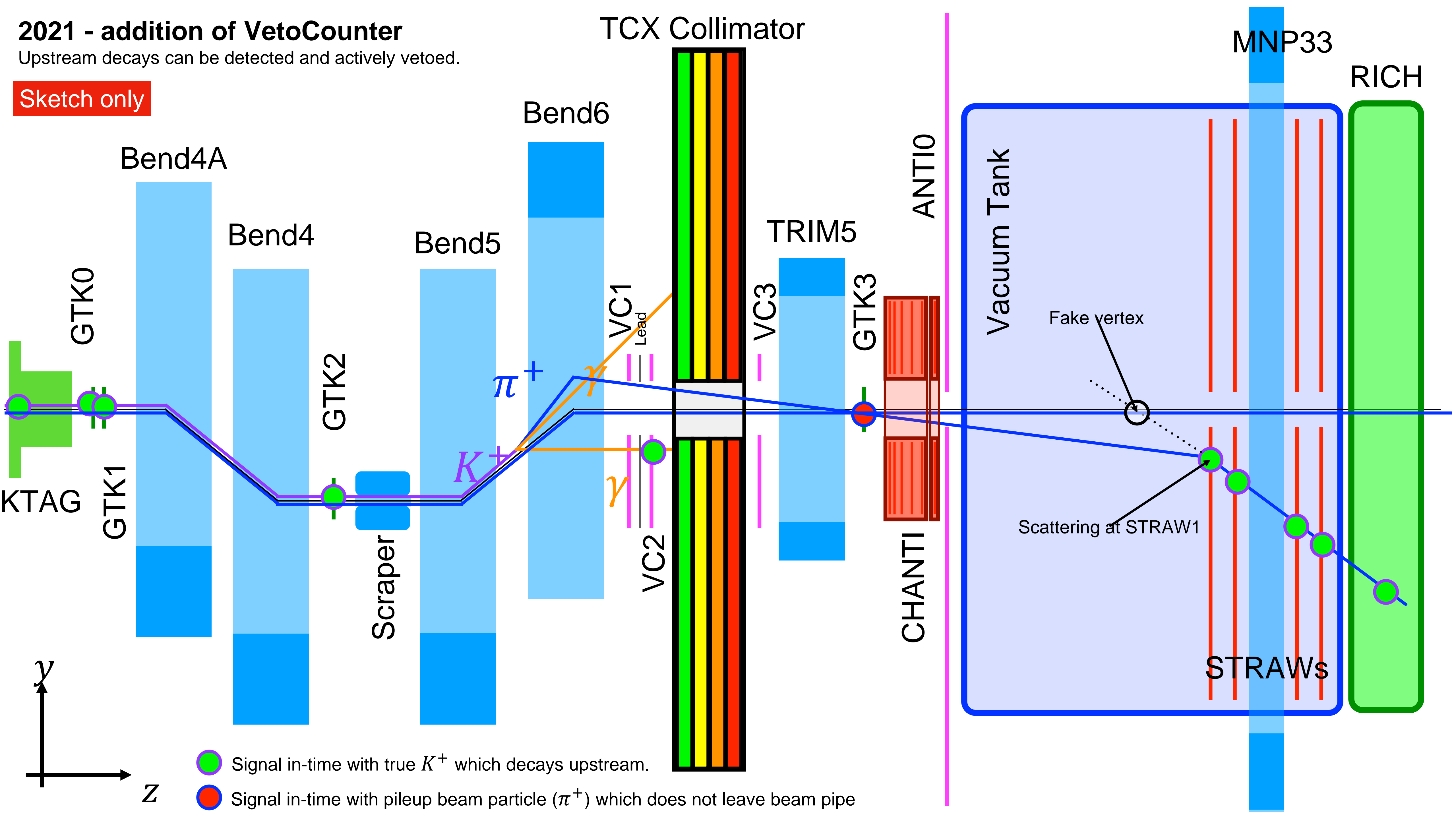
## TCX Collimator



# 2021 - addition of VetoCounter

Upstream decays can be detected and actively vetoed.

Sketch only

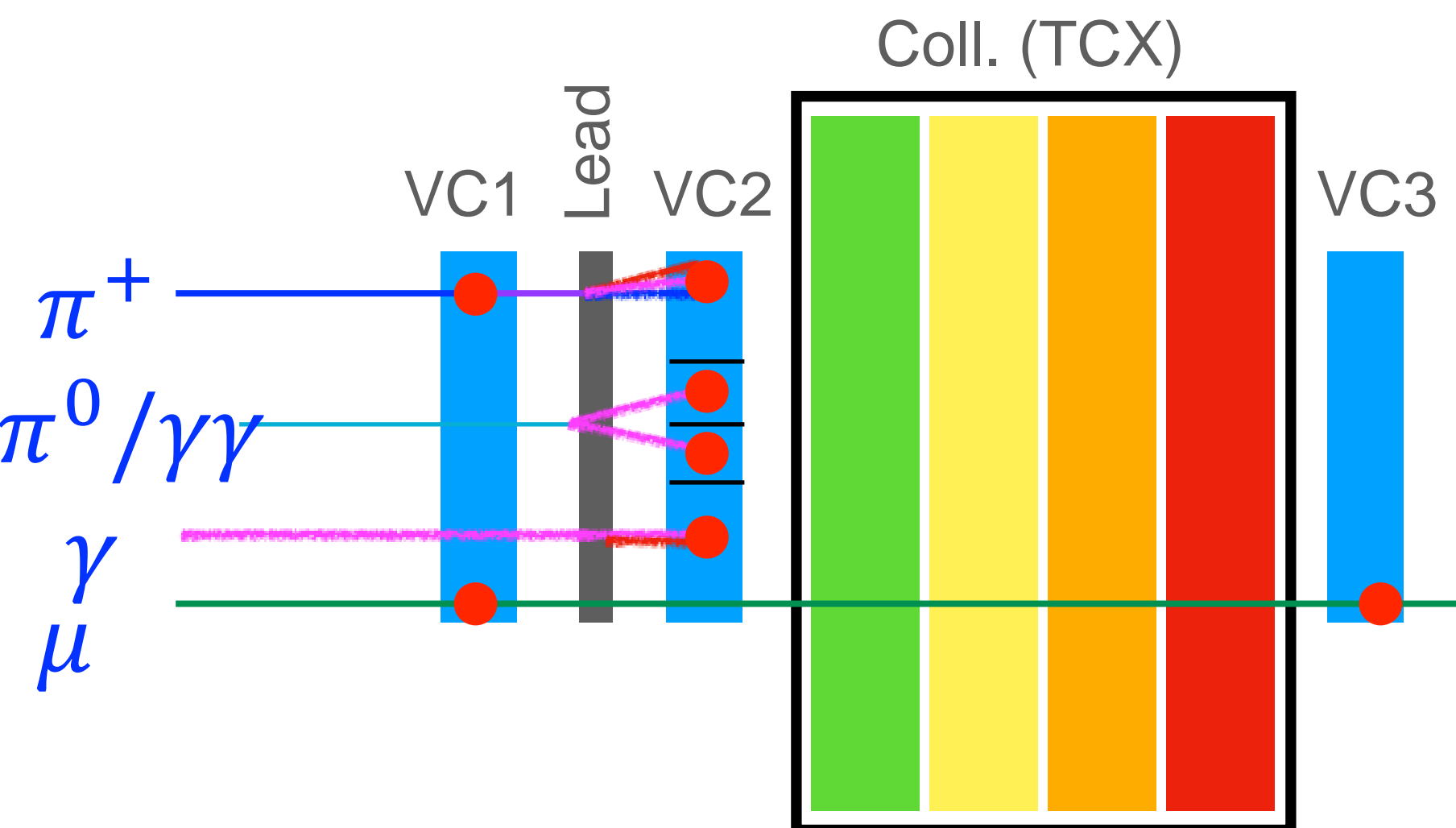




# New upstream vetos: VetoCounter & ANTI0 P326 NA62



[FELIX readout: [Streaming Readout Workshop talk 2021](#)]



## VetoCounter

- Detect particles from decays upstream of final collimator.
- **Factor ~3 rejection** with ~2% accidental veto.

## ANTI0

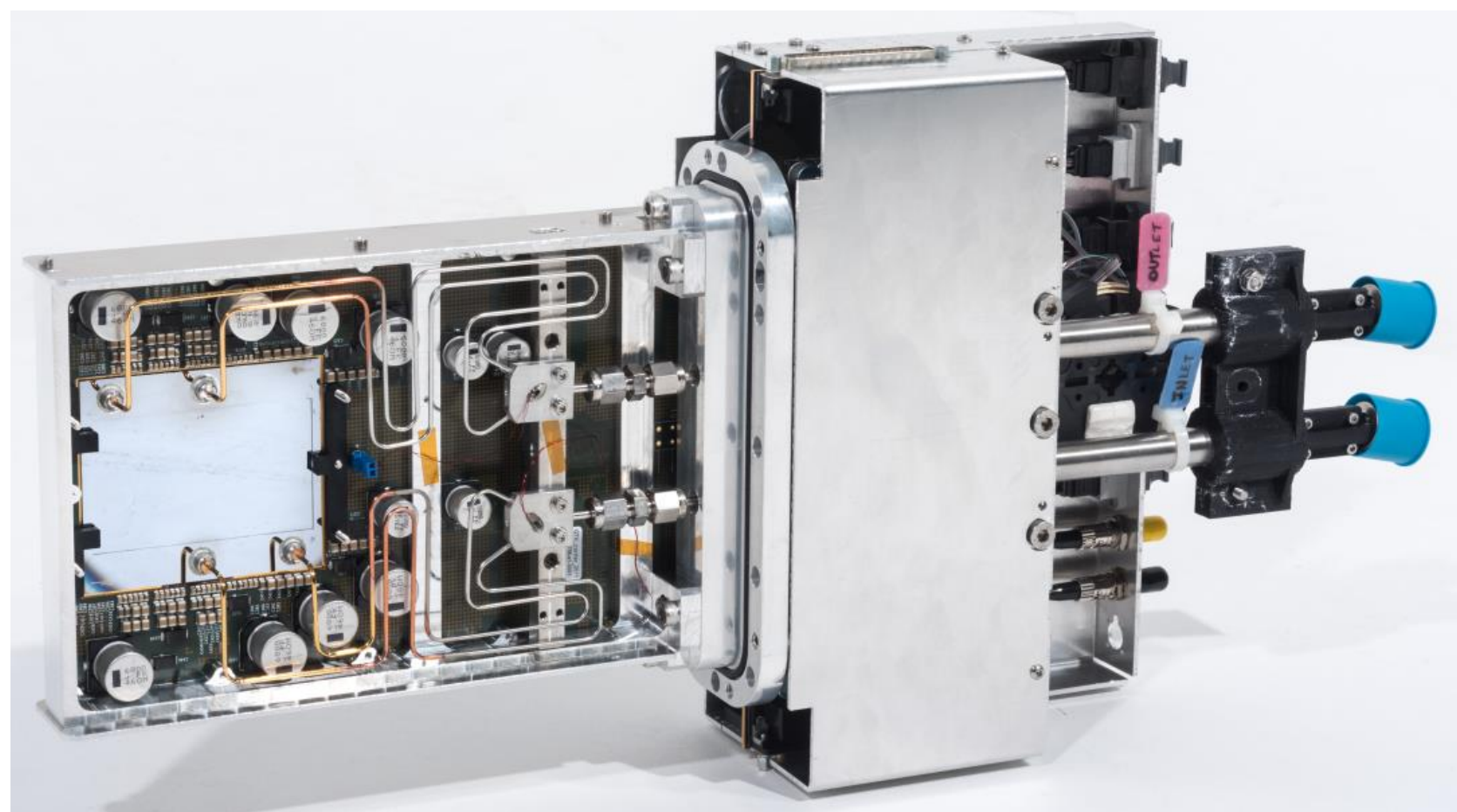
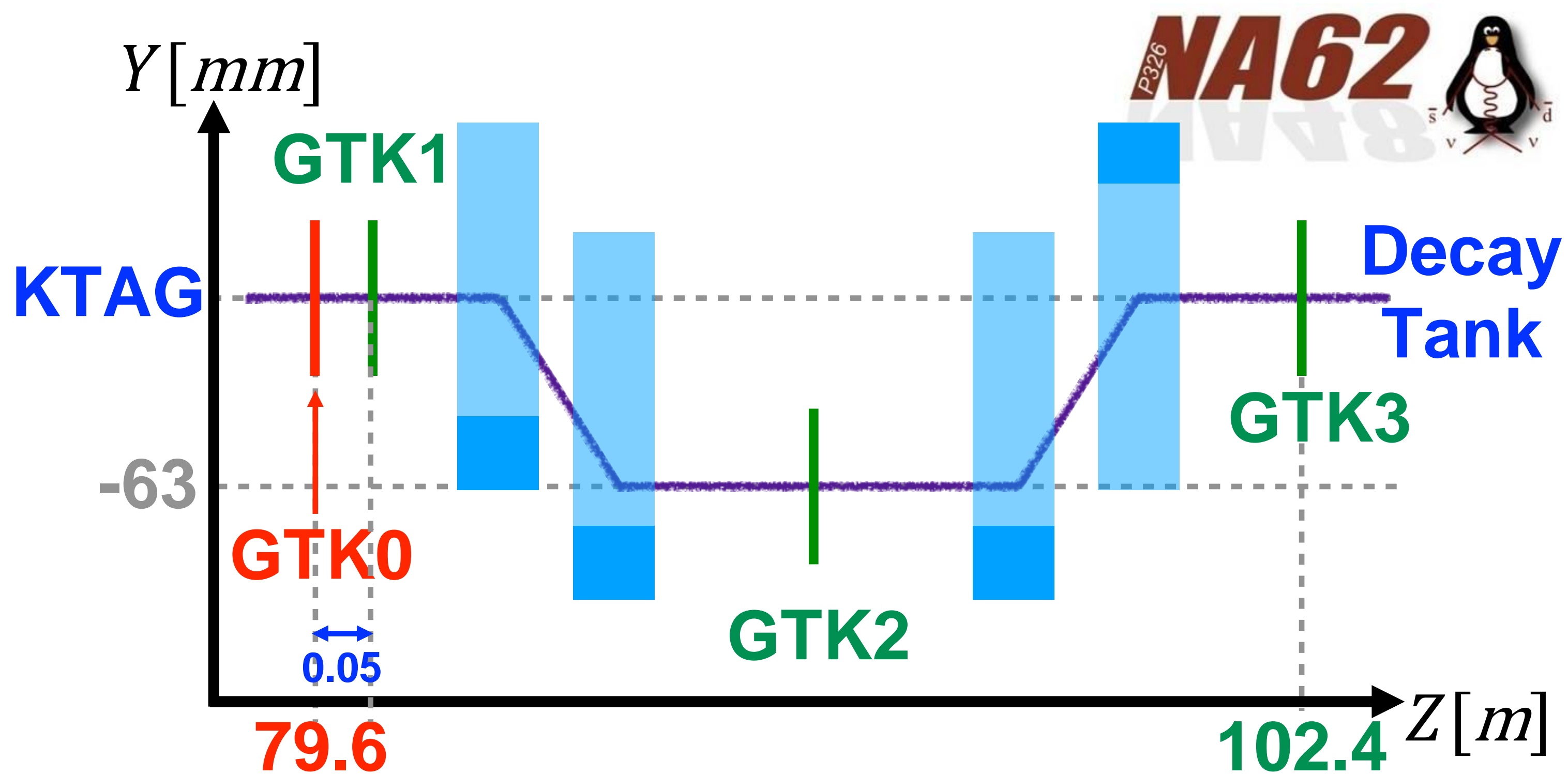
- Detect particles up to ~1 m from beam line.
- **Reject ~20% of upstream background** with <1% signal loss.

[SPSC report 2023][EP Newsletter, Dec21]

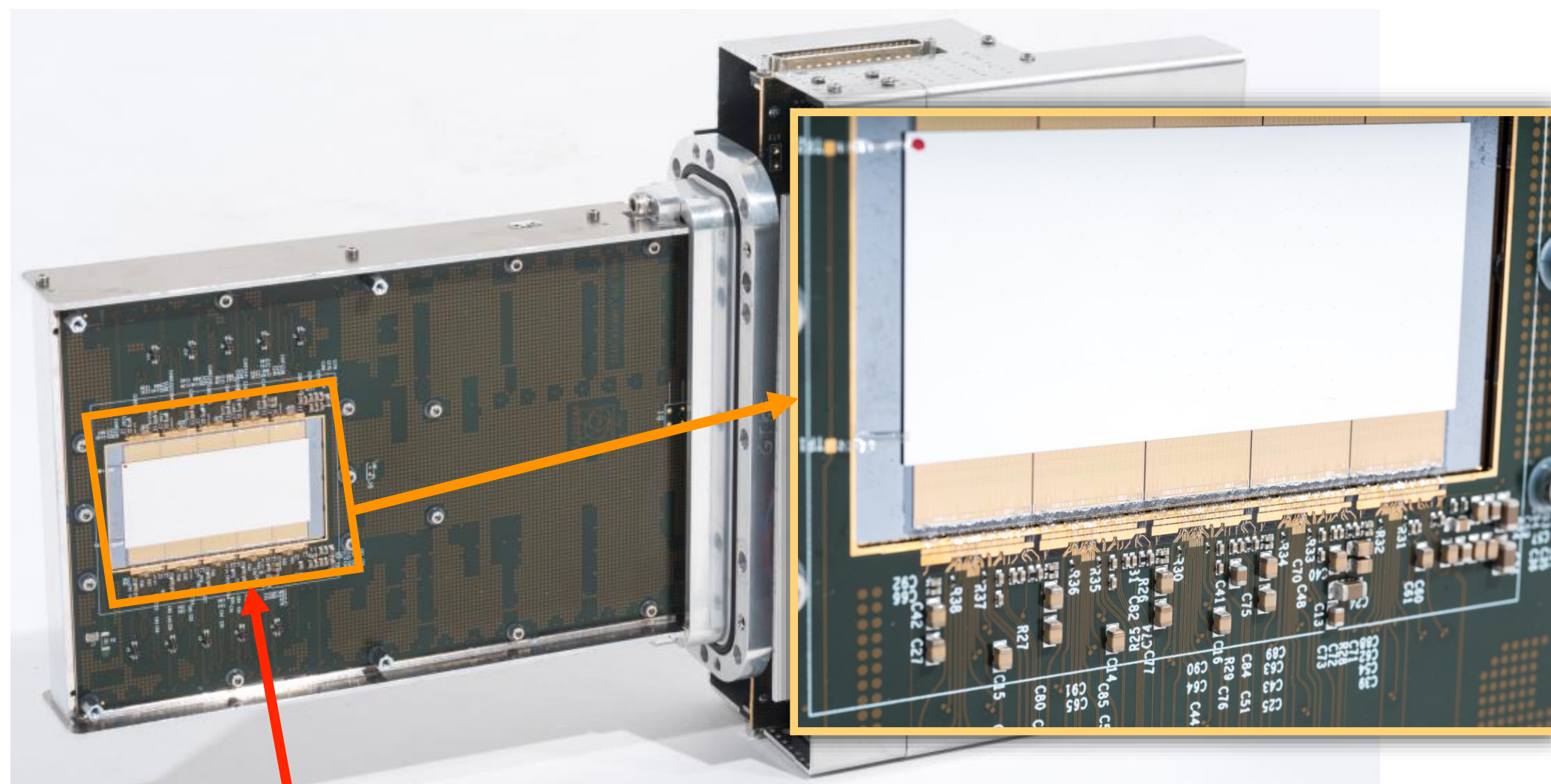


# 4th GTK station

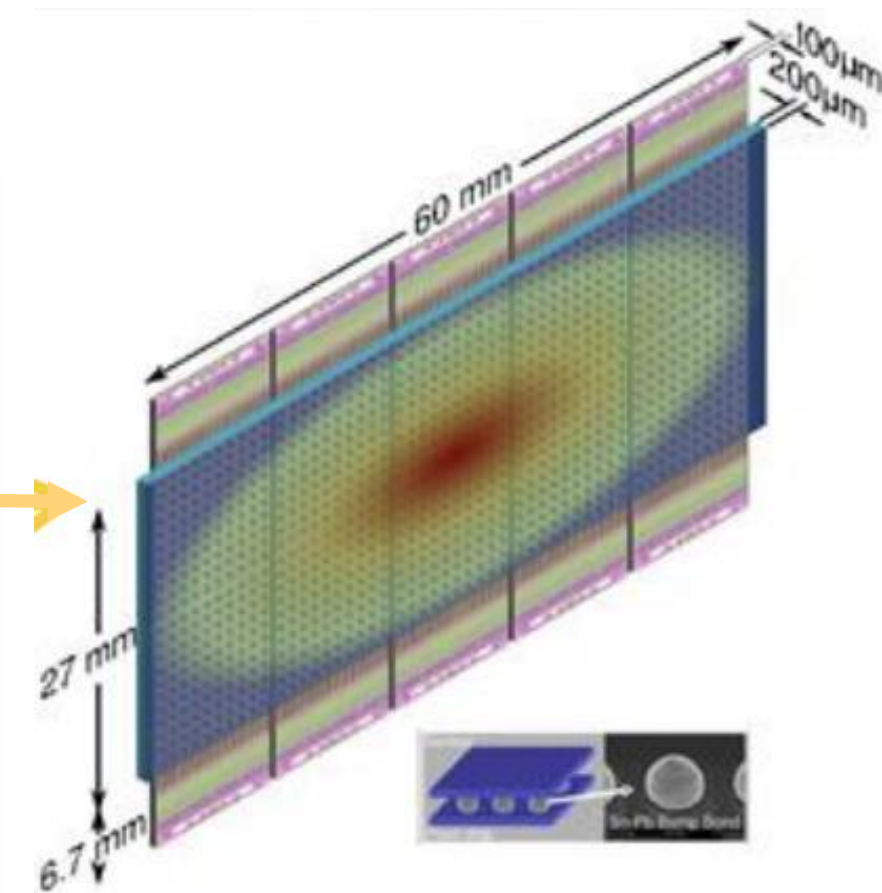
- Si Pixel detector exposed to  $\sim 1\text{GHz}$  beam.
- Essential for  $K^+ - \pi^+$  matching.
  - Measures  $K^+$  3-mom. & time
- 4th GTK station improves efficiency & pileup resilience.

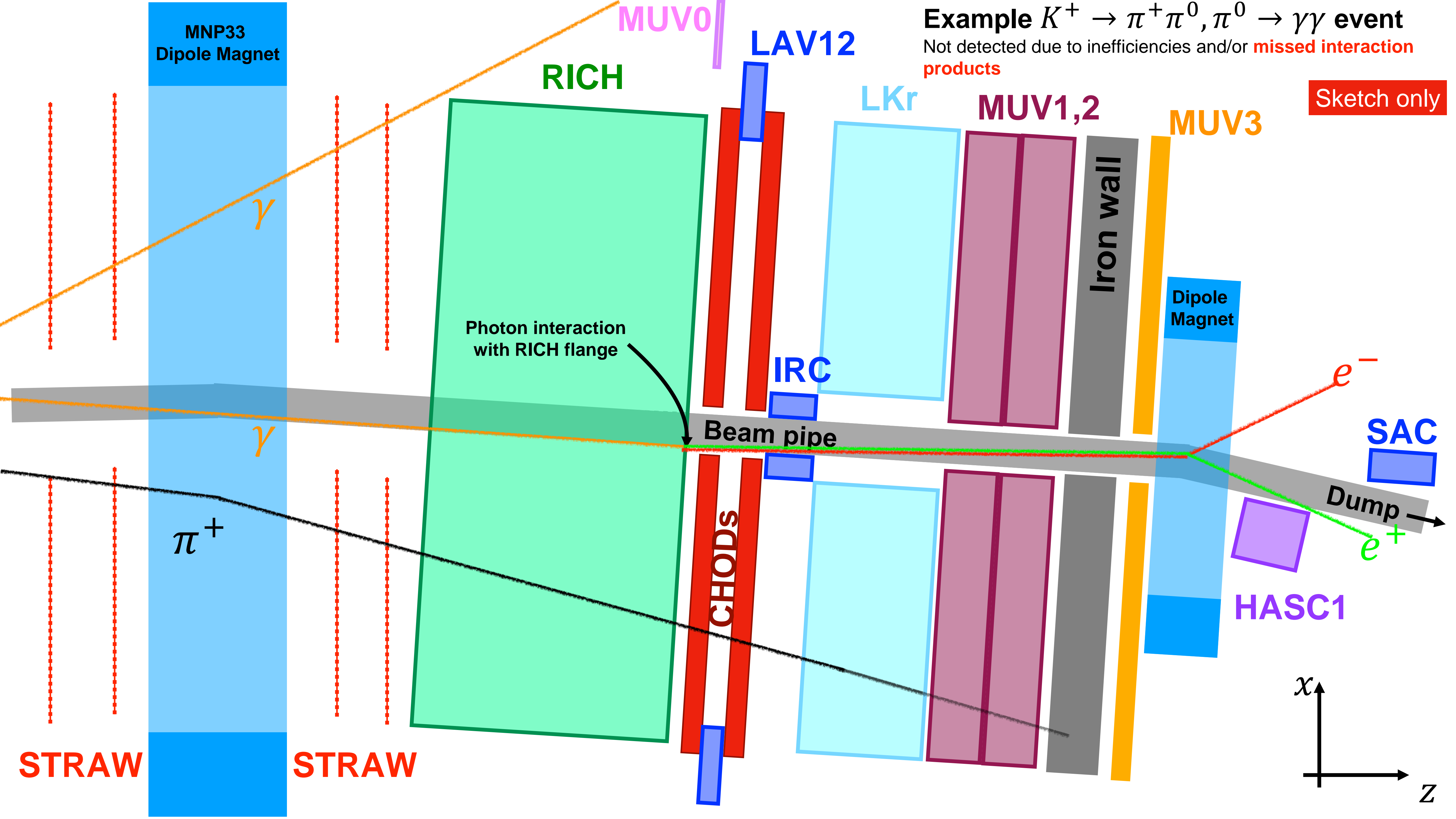


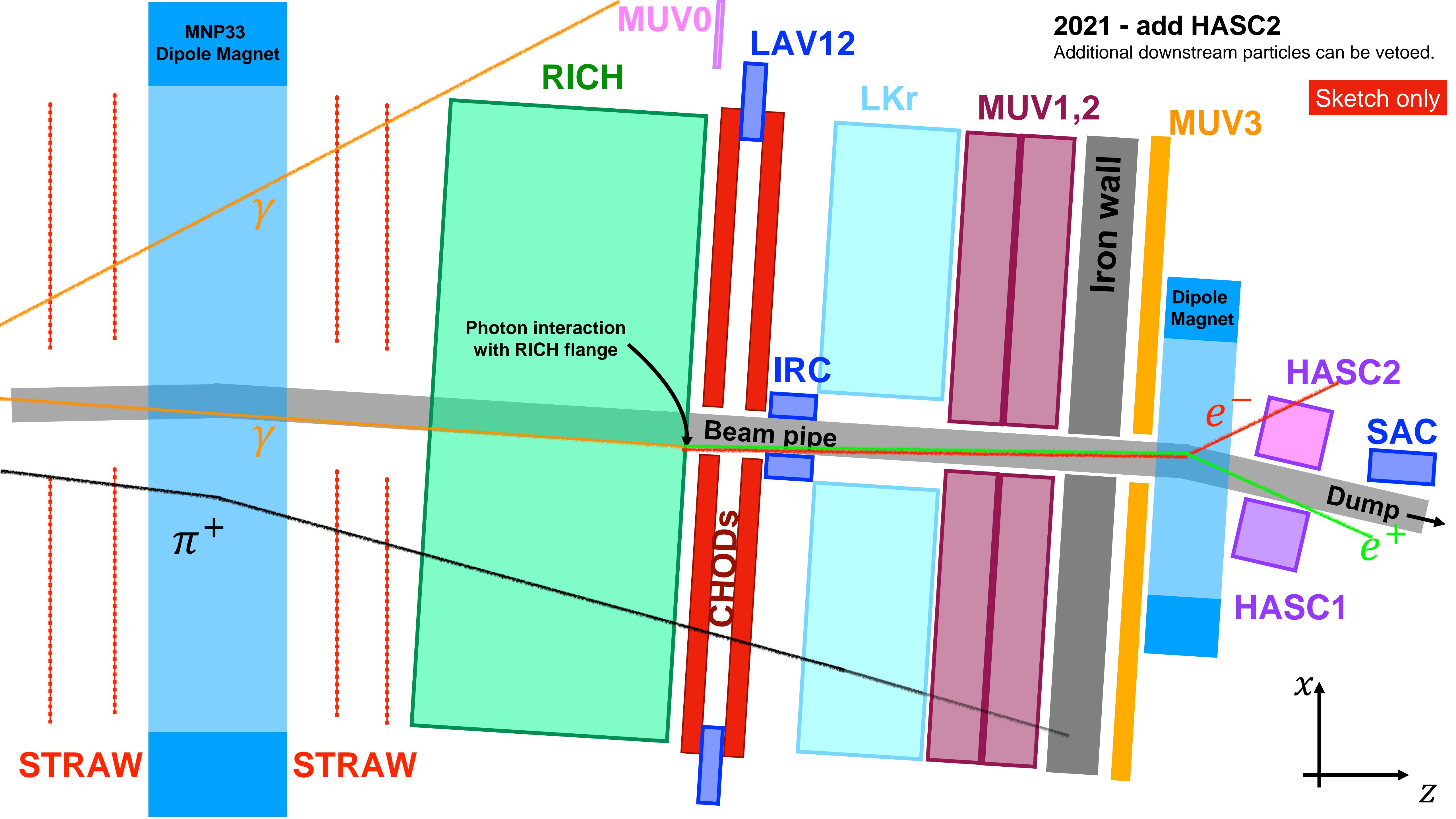
Cooling plate



Si Pixels  $\sim (30 \times 60 \text{ mm active area})$





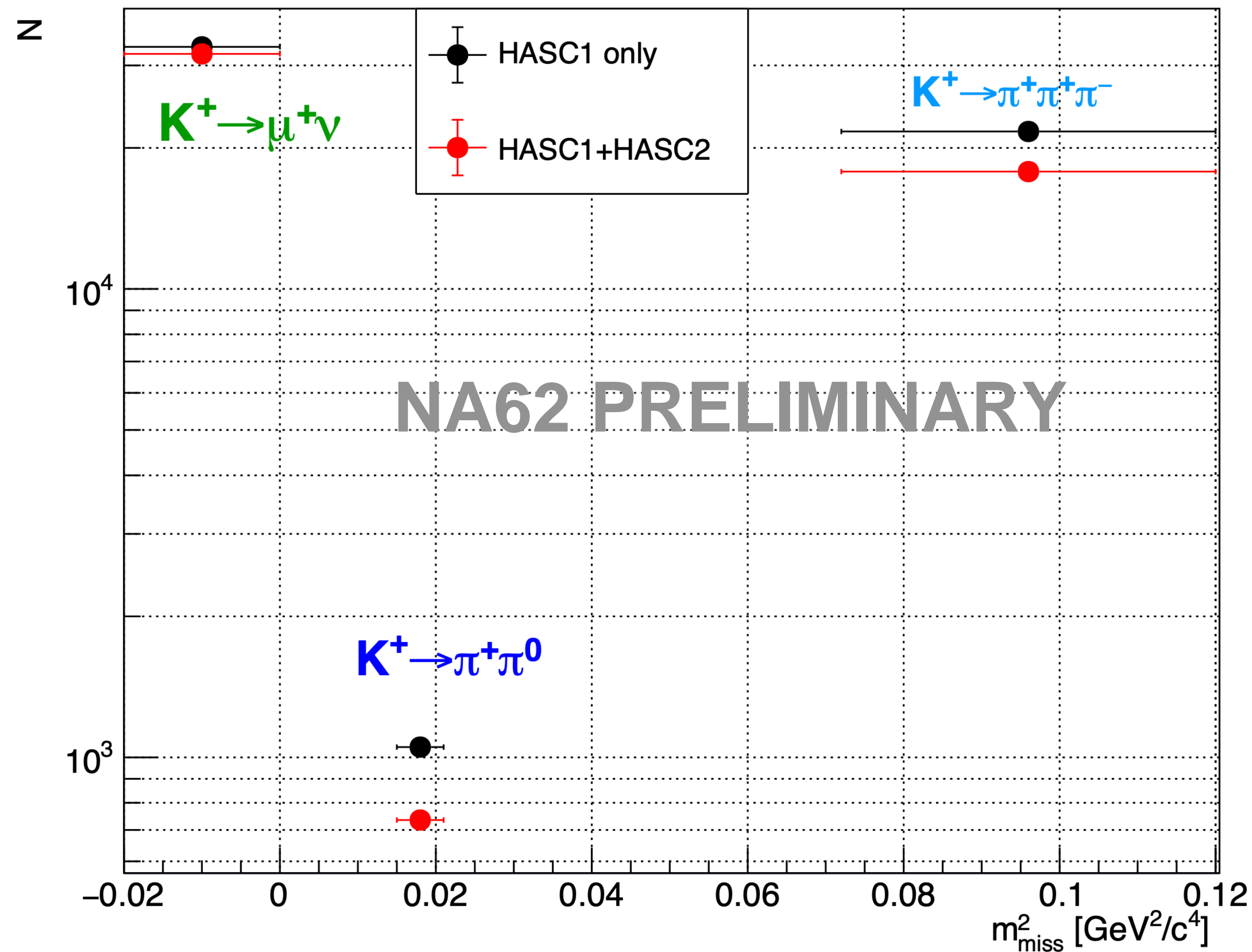


# HASC2 veto

Events passing  $\pi^+ \nu \bar{\nu}$  selection

(modifying HASC veto: study integral of background regions)

- $K^+ \rightarrow \pi^+ \pi^0$  was 2<sup>nd</sup> largest background for 2018 analysis.



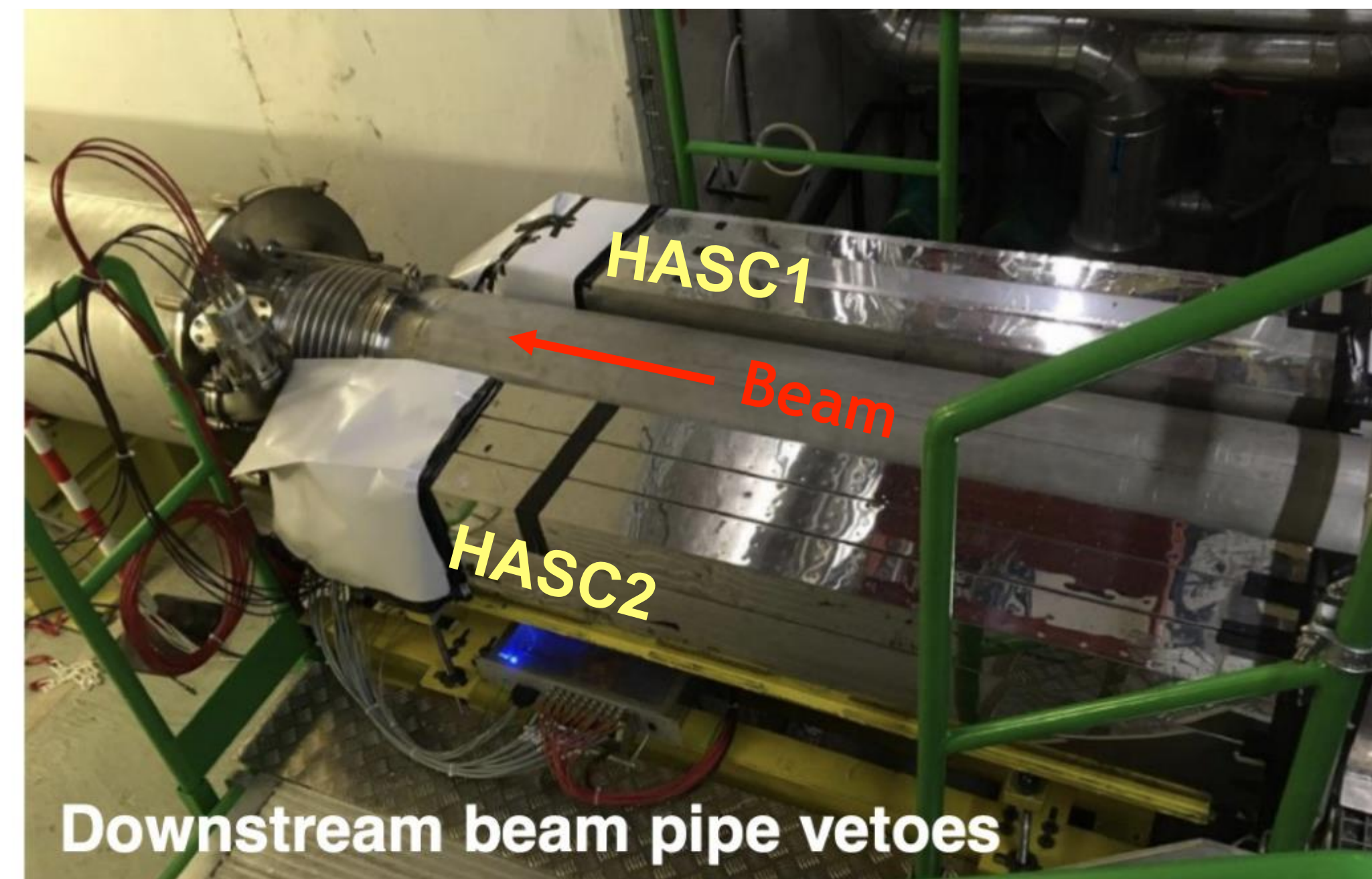
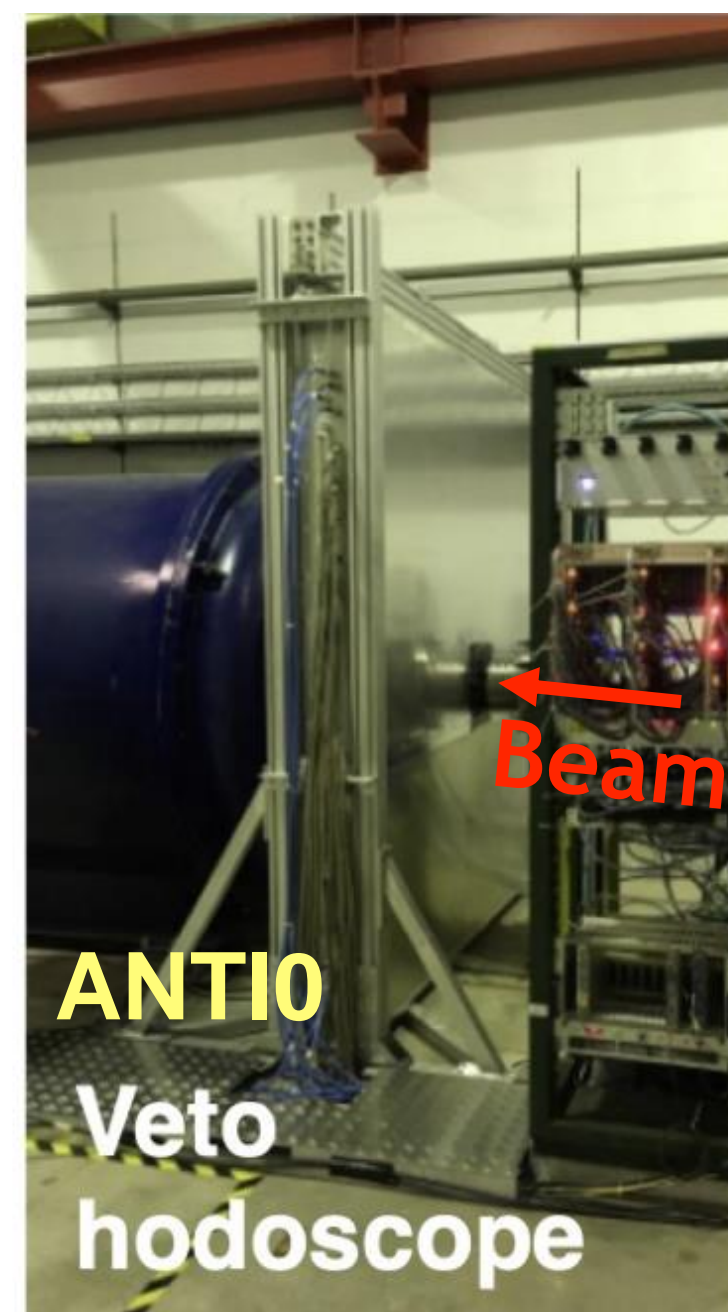
- Addition of HASC2:

- 30% less  $K^+ \rightarrow \pi^+ \pi^0$
- 18% less  $K^+ \rightarrow \pi^+ \pi^+ \pi^-$
- 3.5% less  $K^+ \rightarrow \mu^+ \nu$
- with only 1.5% signal loss

# Summary of NA62 upgrades

- New detectors, installed during LS2:
  - 4th **GTK** (Kaon beam tracker) & rearrange GTK achromat (GTK2 upstream of scraper).
  - New upstream veto (**VetoCounter**) & veto hodoscope (**ANTI0**) upstream of decay volume.
  - Additional veto detector (**HASC2**) at end of beam-line.
- Intensity increased by  $\sim 35\%$  with respect to 2018 [450  $\rightarrow$  600 MHz].
- Improvements to the trigger configuration.

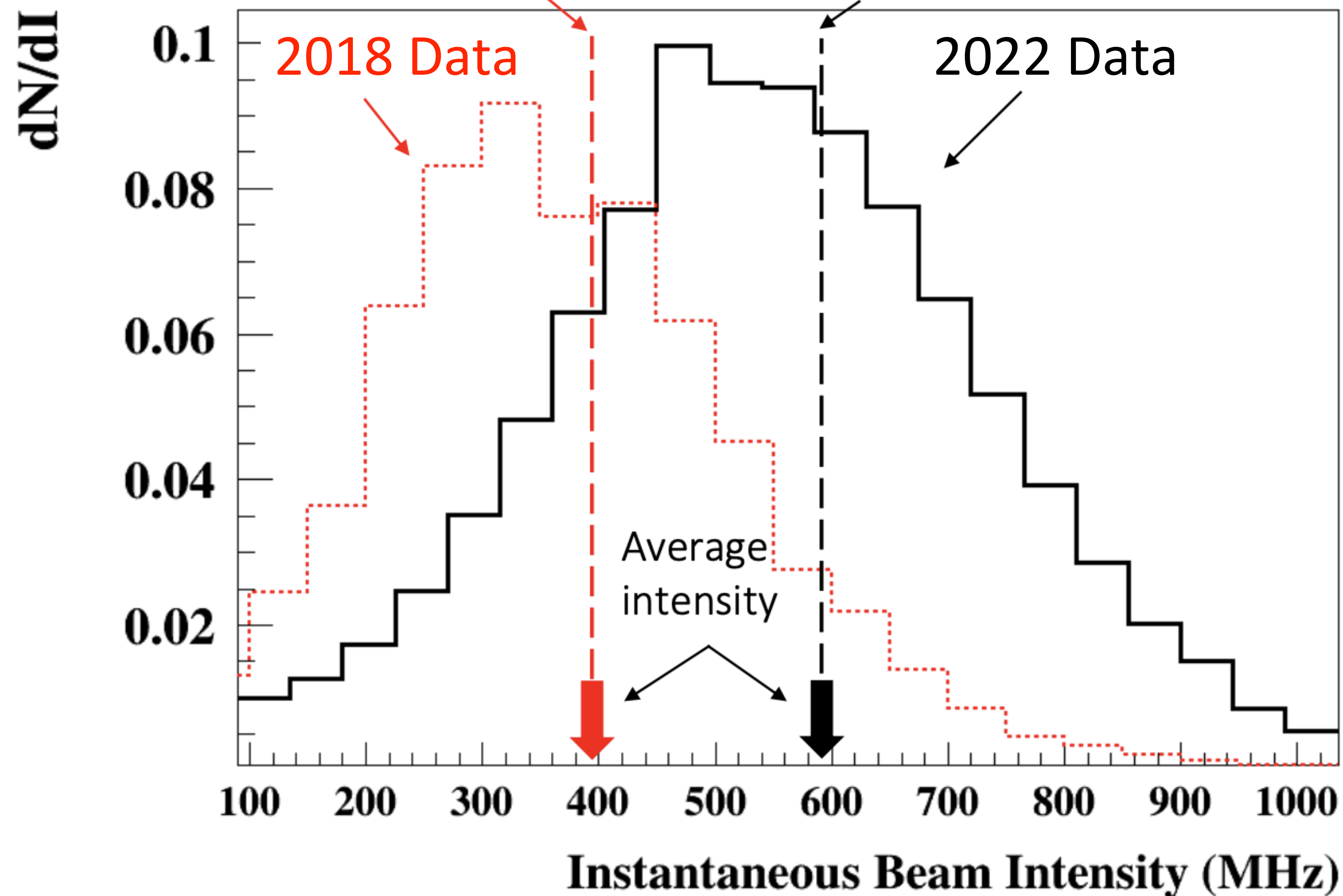
## New detectors installed in 2021:



# Beam intensity: 2018 vs 2022

$\sim 20 \times 10^{11}$  ppp on T10

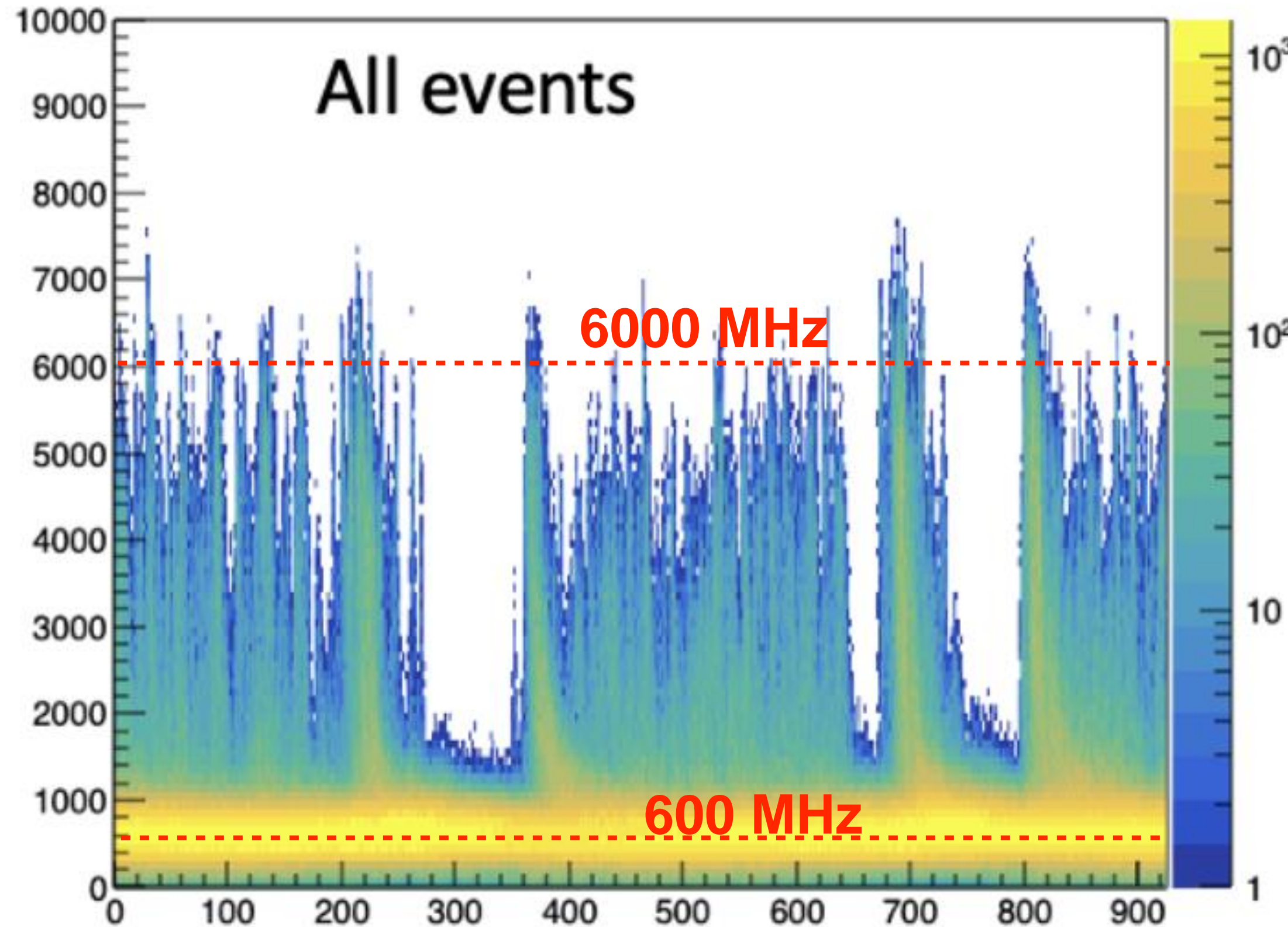
$\sim 30 \times 10^{11}$  ppp on T10



- Average beam intensity increased.
- NA62 “Full intensity” with 4.8s spill = 600 MHz

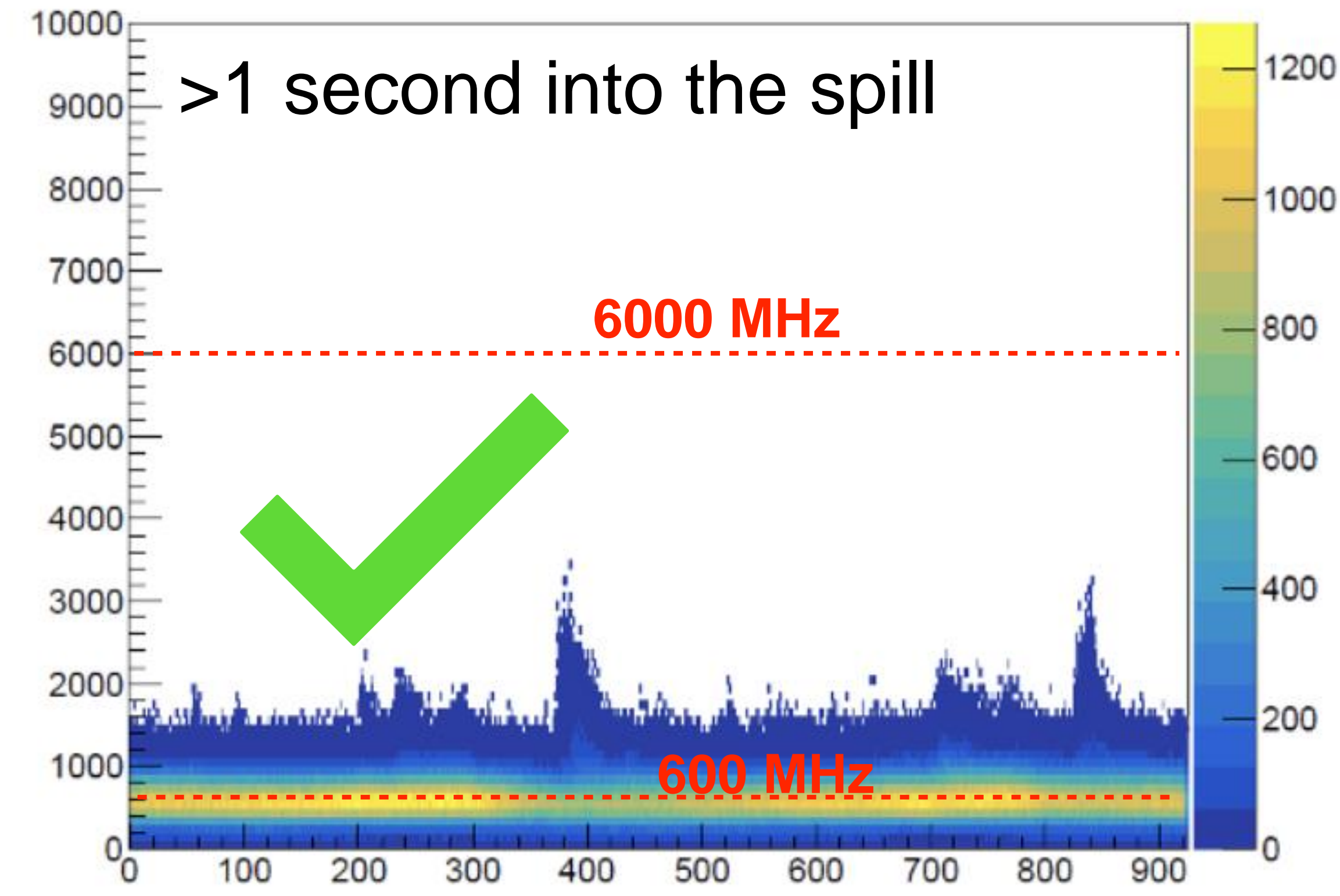
# 2021 instantaneous beam intensity

Instantaneous beam intensity [MHz]



Folded event timestamp [25ns]

Instantaneous beam intensity [MHz]



Folded event timestamp [25ns]

- Remove events in first 1s of 4.8s spill for 2021 data only.
- DAQ overwhelmed by instantaneous rates up to 10x higher than design.



# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ : Analysis of new data

2021–2022 data : **Signal Sensitivity**

# Analysis strategy

## Triggers:

- **Minimum Bias:**  $K^+ \rightarrow \mu^+ \nu$
- **Normalisation:**  $K^+ \rightarrow \pi^+ \pi^0$
- **Signal:**  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  candidates

- RICH multiplicity (reference time)
- Signal in CHODs
- No signal in MUV3 ( $\mu$  veto)
- Tag  $K^+$  ( $\geq 5$  KTAG sectors)
- $<40$  GeV in LKr ( $\pi^0 / \gamma / e$  veto)
- LAV veto (downstream of vertex)

Common conditions

+ add more conditions

## Selection:

- **Normalisation**  $K^+ \rightarrow \pi^+ \pi^0$ : 1 downstream track (only); identified as  $\pi^+$ ;  $K^+ - \pi^+$  matching (space & time); upstream vetos.
- **Signal**  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  candidates: same as normalisation selection + full photon and detector multiplicity cuts (reject all extra activity).

# Bayesian classifier for $K^+ - \pi^+$ matching

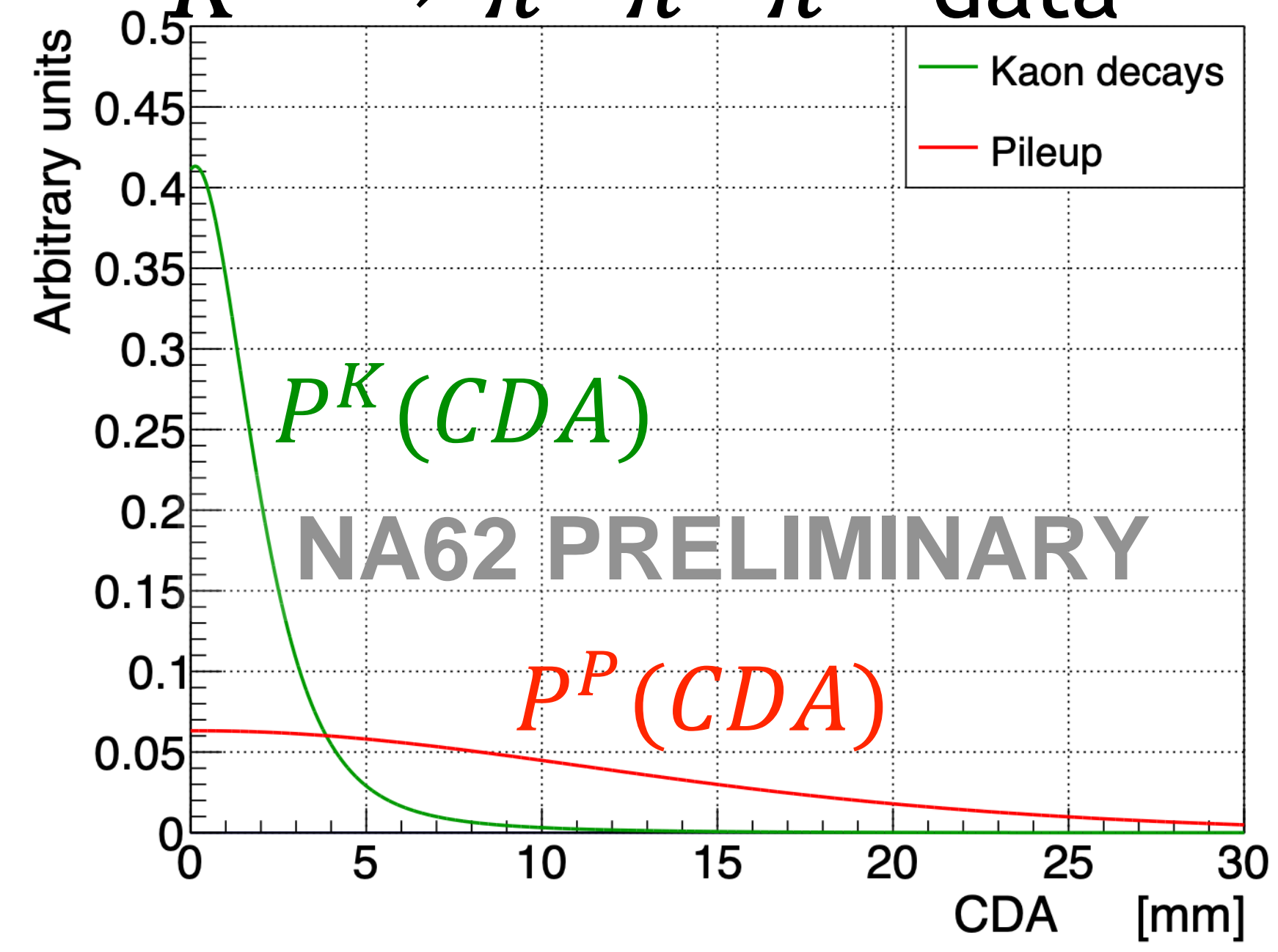
Example of selection update



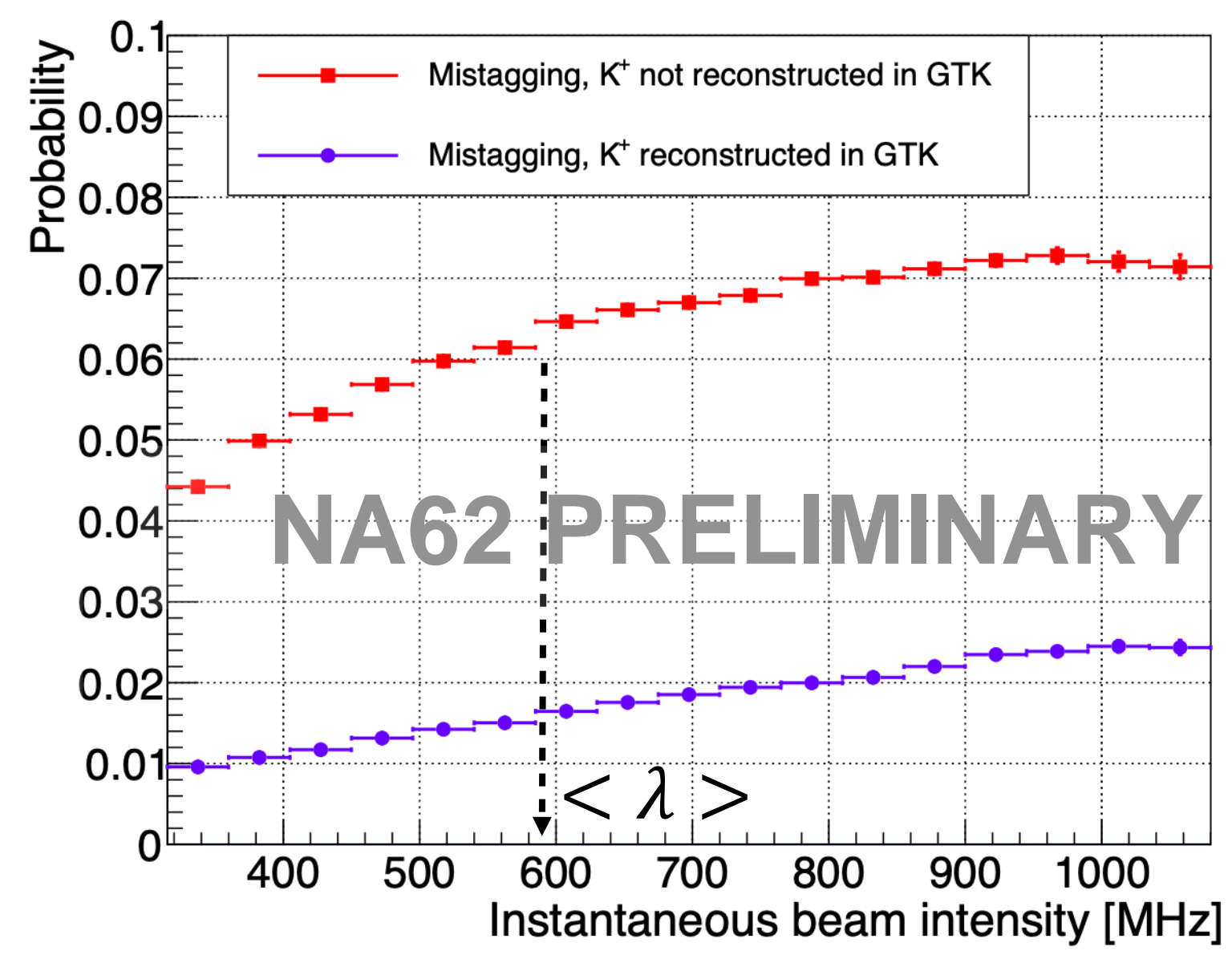
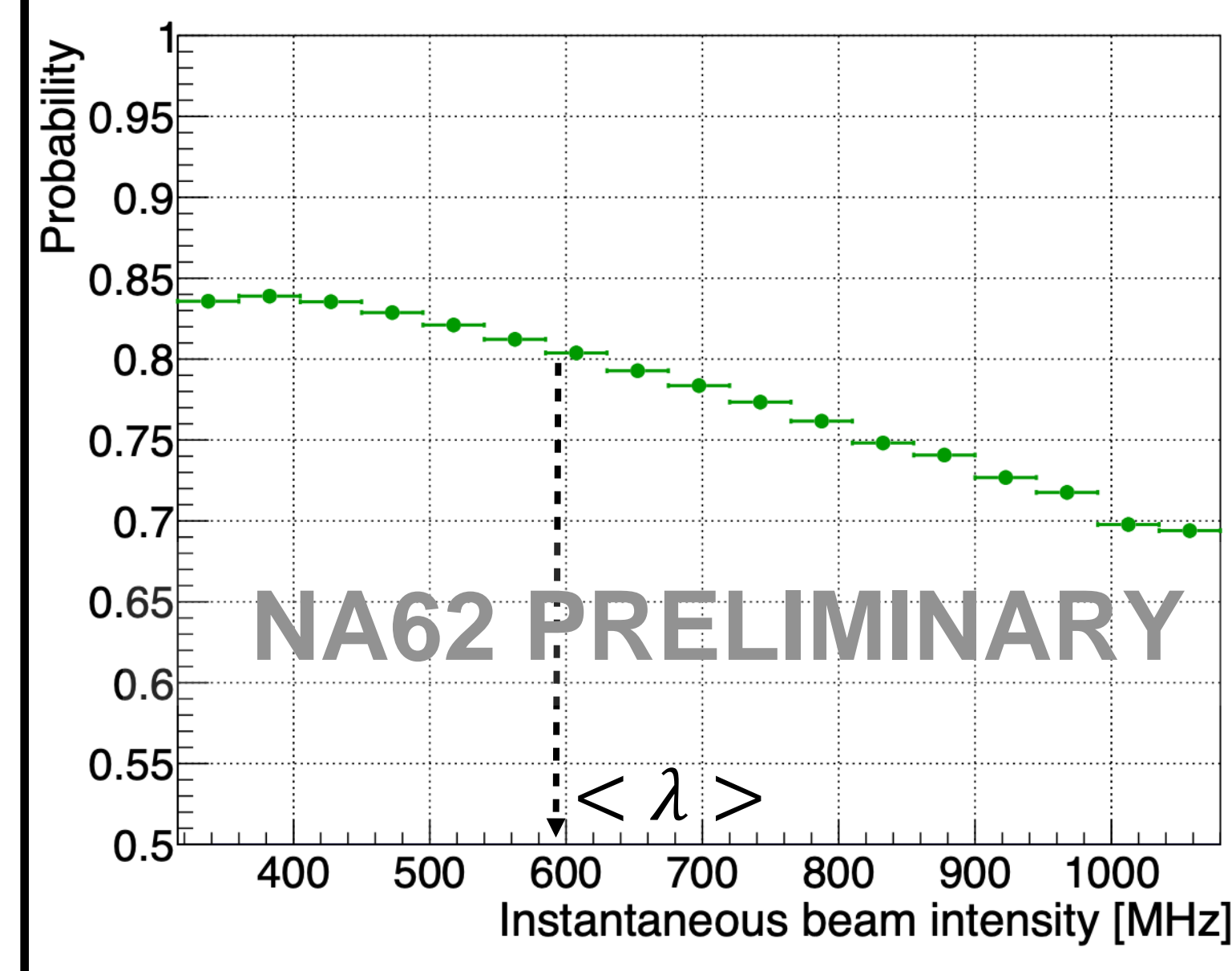
- **Inputs:** spatial (CDA) & time ( $\Delta T_+$ ) matching, intensity/pileup ( $N_{GTK}$ ) [prior]

- **Output:** posterior probability of GTK track = true  $K^+$ 
  - Use likelihoods of kaons (K) and pileup (P)
  - Likelihood ratio used to select true match when  $N_{GTK} > 1$

- Models for PDFs/Prior from  $K^+ \rightarrow \pi^+ \pi^+ \pi^-$  data



$\epsilon = 80\%$       $P^P_{mistag} = 6\%$       $P^K_{mistag} = 2\%$



- Efficiency improved (+10%) and mistagging probability maintained.



# Signal sensitivity

- Normalisation channel:  $K^+ \rightarrow \pi^+ \pi^0$ , momentum range  $p \in [15, 45] \text{ GeV}/c$ .

Effective number of  $K^+$  decays,  $N_K$ :

$$N_K = \frac{N_{\pi\pi} D_0}{B_{\pi\pi} A_{\pi\pi}}$$

Number of normalisation events  $\rightarrow N_{\pi\pi} D_0$   
 Downscaling factor of normalisation trigger (generally 400)  $\rightarrow D_0$   
 Branching ratio of  $K^+ \rightarrow \pi^+ \pi^0$  decay  $\rightarrow B_{\pi\pi}$   
 Acceptance of normalisation selection  $\rightarrow A_{\pi\pi}$

Single event sensitivity:

(Branching ratio corresponding to expectation of 1 event)

$$B_{SES} = \frac{1}{N_K \epsilon_{RV} \epsilon_{trig} A_{\pi\nu\bar{\nu}}}$$

Random veto efficiency  $\rightarrow \epsilon_{RV}$

Trigger efficiency (ratio)  $\rightarrow \epsilon_{trig}$

Signal selection acceptance  $\rightarrow A_{\pi\nu\bar{\nu}}$

Number of expected SM events:

(For comparison to previous results use  $B_{\pi\nu\bar{\nu}}^{SM} = 8.4 \times 10^{-11}$  but results are independent of this choice)

$$N_{\pi\nu\bar{\nu}}^{SM} = \frac{B_{\pi\nu\bar{\nu}}^{SM}}{B_{SES}}$$

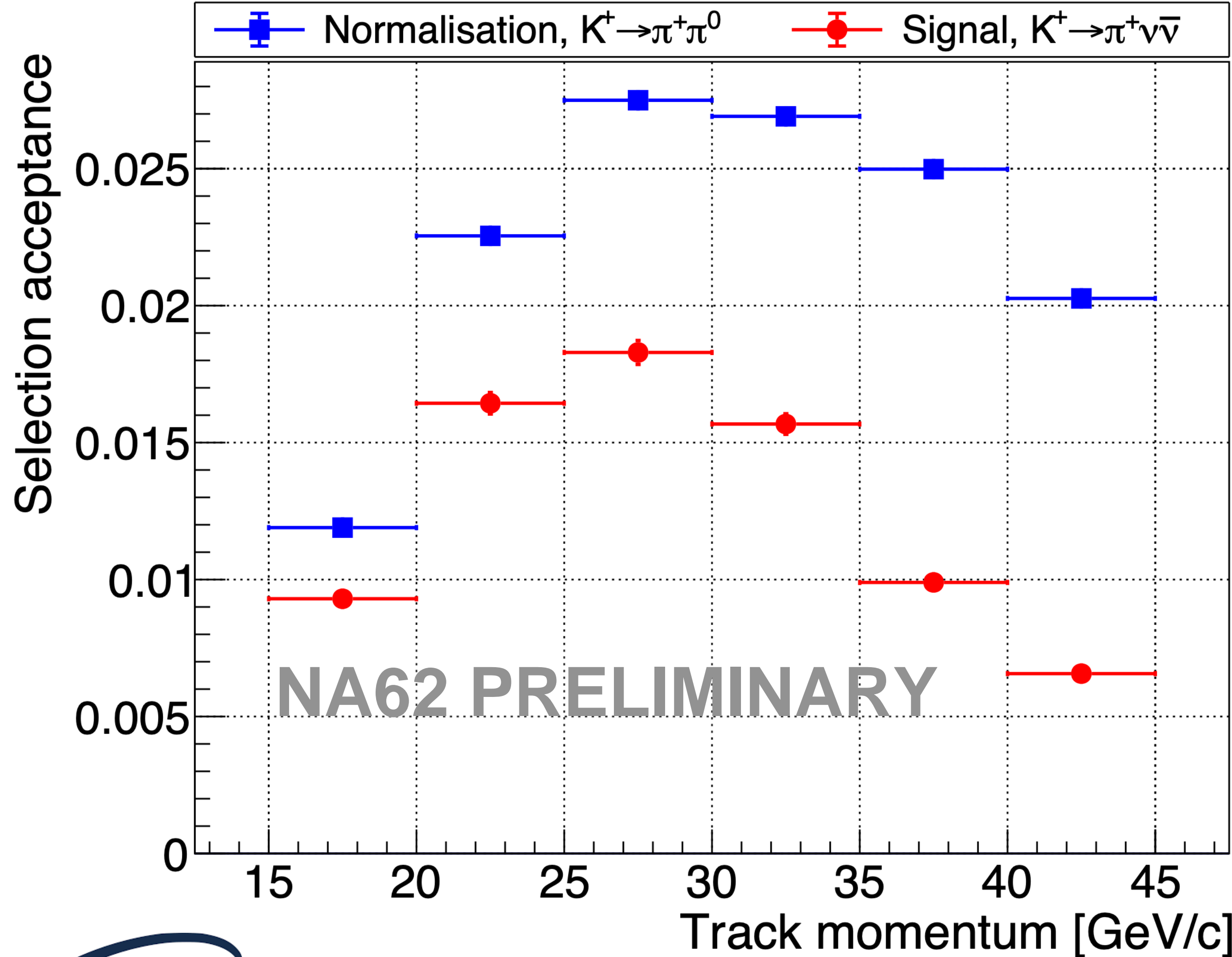
# Acceptances

Acceptances



Analysis is performed in (5 GeV/c) bins of momentum:

$$N_{\pi\nu\bar{\nu}}^{exp}(p_i) = \frac{B_{\pi\nu\bar{\nu}}^{SM}}{B_{SES}(p_i)} = \frac{B_{\pi\nu\bar{\nu}}^{SM}}{B_{\pi\pi}} \frac{A_{\pi\nu\bar{\nu}}(p_i)}{A_{\pi\pi}(p_i)} D_0 N_{\pi\pi}(p_i) \varepsilon_{trig}(p_i) \varepsilon_{RV}$$



Case	OLD 2018 (S2)	NEW 2021-22	
Norm.	11.8%	13.4%	+15%
Signal	(6.37±0.64)%	(7.61±0.18)%	+20%

- Increased selection efficiencies.
  - New K-pi matching technique.
  - Re-tuned vertex conditions.
  - Relaxation of some vetos.
- Improved precision (plus improved systematic uncertainty evaluation).

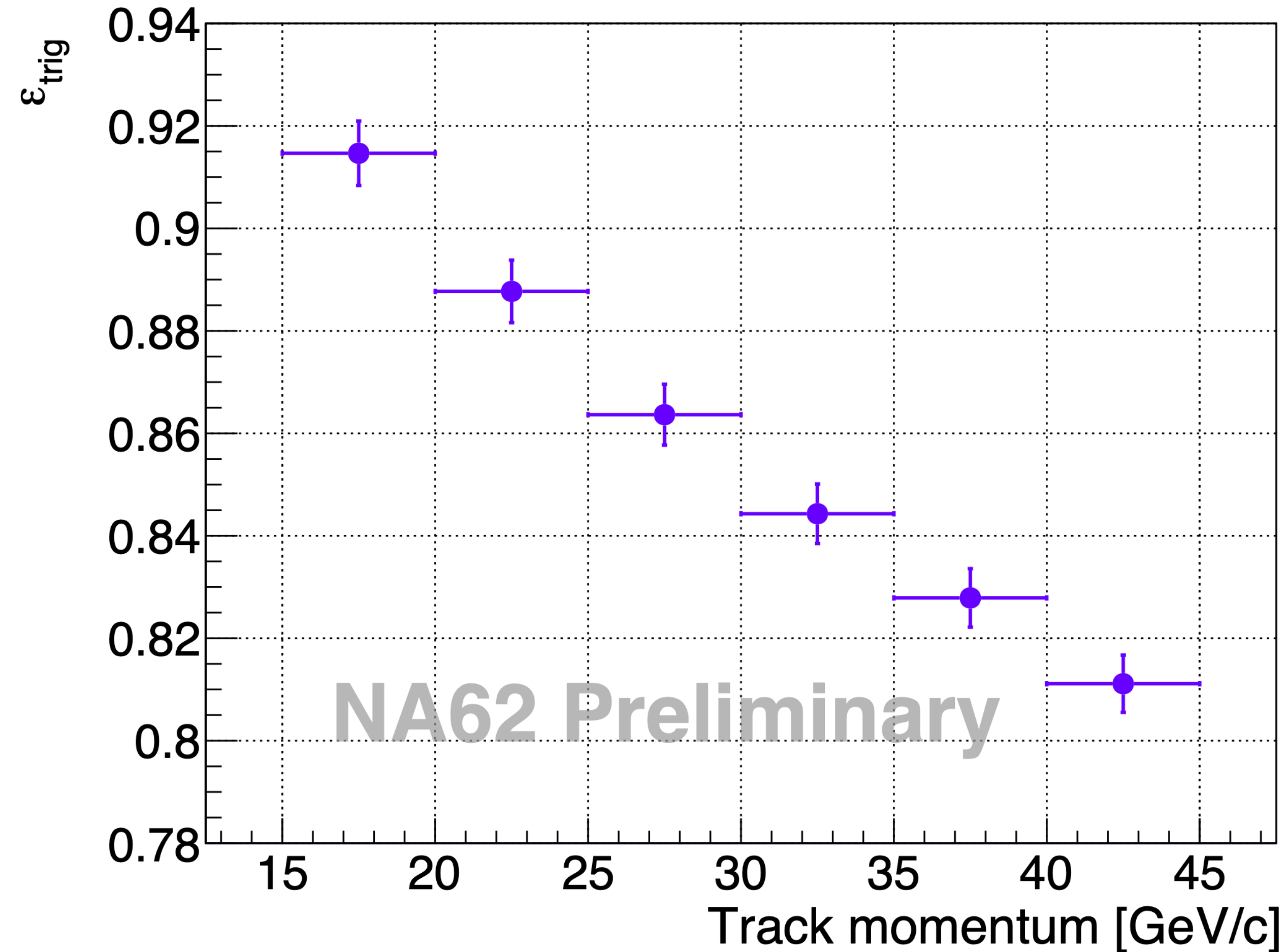
Acceptances evaluated at 0 intensity.  
Intensity dependence captured in  $\varepsilon_{RV}$

# Trigger efficiencies



Analysis is performed in (5 GeV/c) bins of momentum:

$$N_{\pi\nu\bar{\nu}}^{exp}(p_i) = \frac{B_{\pi\nu\bar{\nu}}^{SM}}{B_{SES}(p_i)} = \frac{B_{\pi\nu\bar{\nu}}^{SM}}{B_{\pi\pi}} \frac{A_{\pi\nu\bar{\nu}}(p_i)}{A_{\pi\pi}(p_i)} D_0 N_{\pi\pi}(p_i) \epsilon_{trig}(p_i) \epsilon_{RV}$$



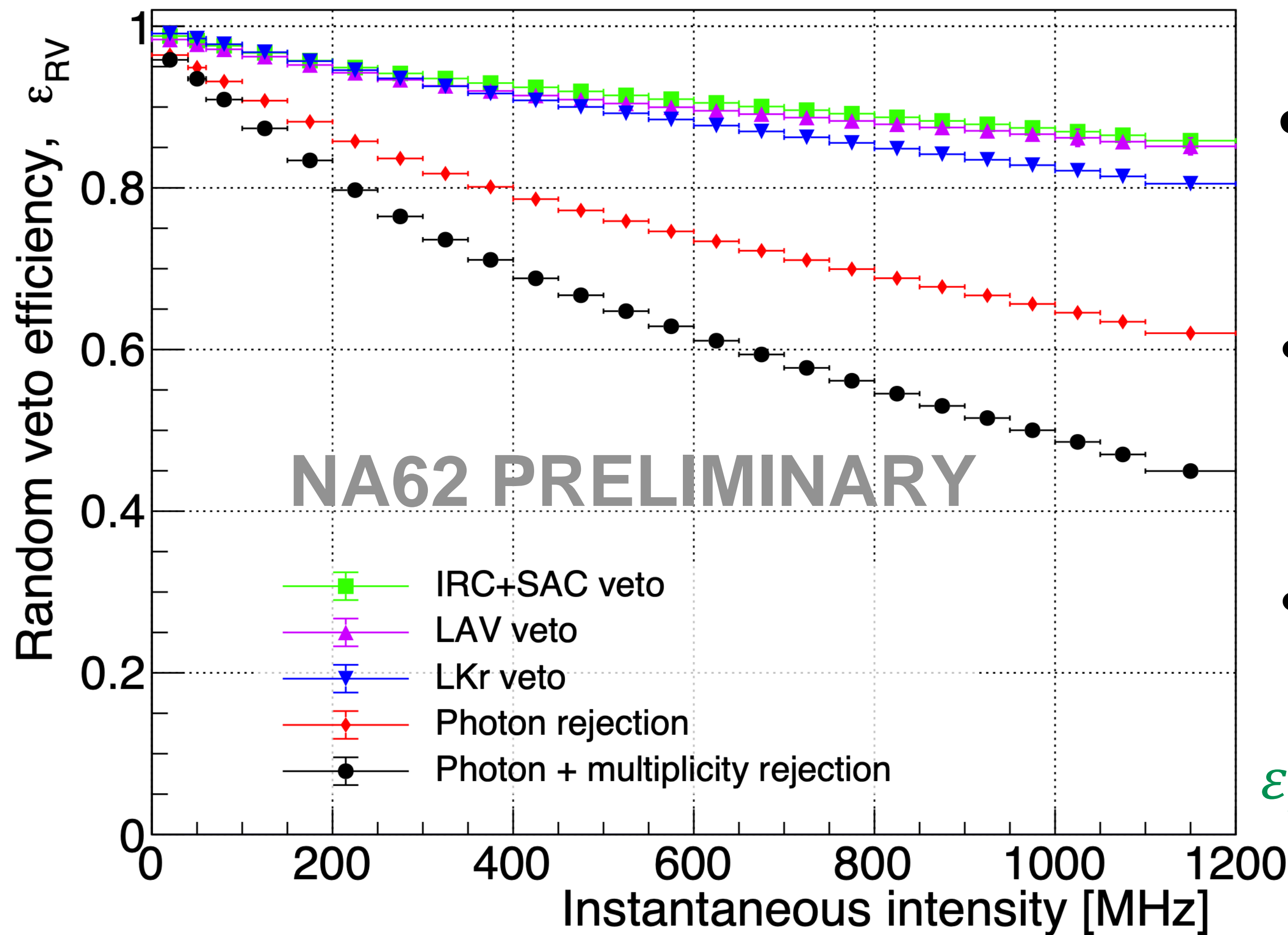
$$\epsilon_{trig} = \frac{\epsilon_{sig}}{\epsilon_{norm}} \quad \begin{aligned} \epsilon_{trig}(new) &= (85.9 \pm 1.4)\% \\ \epsilon_{trig}(2018) &= (89 \pm 5)\% \end{aligned}$$

- Trigger efficiency ratio:
  - **New:** several components in both normalisation & signal triggers: **partial cancellation**.
  - **Old:** in 2016–18 data normalise with fully independent min bias trigger (**no cancellation**).
- Improved precision by factor 3 with reduced systematic uncertainty.

# Random veto

$\epsilon_{RV}$  is independent of track momentum (related to additional activity only)

$$N_{\pi\nu\bar{\nu}}^{exp}(p_i) = \frac{\mathcal{B}_{\pi\nu\bar{\nu}}^{SM}}{\mathcal{B}_{SES}(p_i)} = \frac{\mathcal{B}_{\pi\nu\bar{\nu}}^{SM}}{\mathcal{B}_{\pi\pi}} \frac{A_{\pi\nu\bar{\nu}}(p_i)}{A_{\pi\pi}(p_i)} D_0 N_{\pi\pi}(p_i) \epsilon_{trig}(p_i) \epsilon_{RV}$$



- $\epsilon_{RV}$  = Random Veto Efficiency:
  - $1 - \epsilon_{RV}$  = Probability of rejecting a signal event due to additional activity.
- Balance:
  - Strict vetos  $\Rightarrow$  lower efficiency
  - Loose vetos  $\Rightarrow$  higher background
- Operational intensity higher but re-tuning vetos means  $\epsilon_{RV}$  is comparable:

$$\epsilon_{RV}(new, \overline{\lambda_{21-22}} \approx 600 MHz) = (63.6 \pm 0.6)\%$$

$$\epsilon_{RV}(old, \overline{\lambda_{2018}} \approx 400 MHz) = (66 \pm 1)\%$$

# Signal sensitivity results



$$N_K = \frac{N_{\pi\pi} D_0}{B_{\pi\pi} A_{\pi\pi}} \quad \mathcal{B}_{SES} = \frac{1}{N_K \varepsilon_{RV} \varepsilon_{trig} A_{\pi\nu\bar{\nu}}}$$

- Display integrals (15–45 GeV/c, 2021+22) for summary tables.
- \* Acceptances evaluated at 0 intensity.

$$N_{\pi\nu\bar{\nu}}^{exp} = \frac{\mathcal{B}_{\pi\nu\bar{\nu}}^{SM}}{\mathcal{B}_{SES}}$$

Assuming  $\mathcal{B}_{\pi\nu\bar{\nu}}^{SM} = 8.4 \times 10^{-11}$  :

2021–22:  $N_{\pi\nu\bar{\nu}} = 10.00 \pm 0.34$

c.f. 2016–18 :  $N_{\pi\nu\bar{\nu}} = 10.01 \pm 0.42$

↓

Double expected signal by including 21–22 data.

$N_{\pi\pi}$	Normalisation $K^+ \rightarrow \pi^+ \pi^0$	$2.0 \times 10^8$
$A_{\pi\pi}$	Normalisation acceptance	$(13.410 \pm 0.005)\%$
$N_K$	Effective $K^+$ decays	$2.9 \times 10^{12}$
$A_{\pi\nu\bar{\nu}}$	Signal acceptance	$(7.6 \pm 0.2)\%$
$\varepsilon_{trig}$	Trigger efficiency	$(85.9 \pm 1.4)\%$
$\varepsilon_{RV}$	Random veto efficiency	$(63.6 \pm 0.6)\%$
$\mathcal{B}_{SES}$	Single event sensitivity	$(0.84 \pm 0.03) \times 10^{-11}$

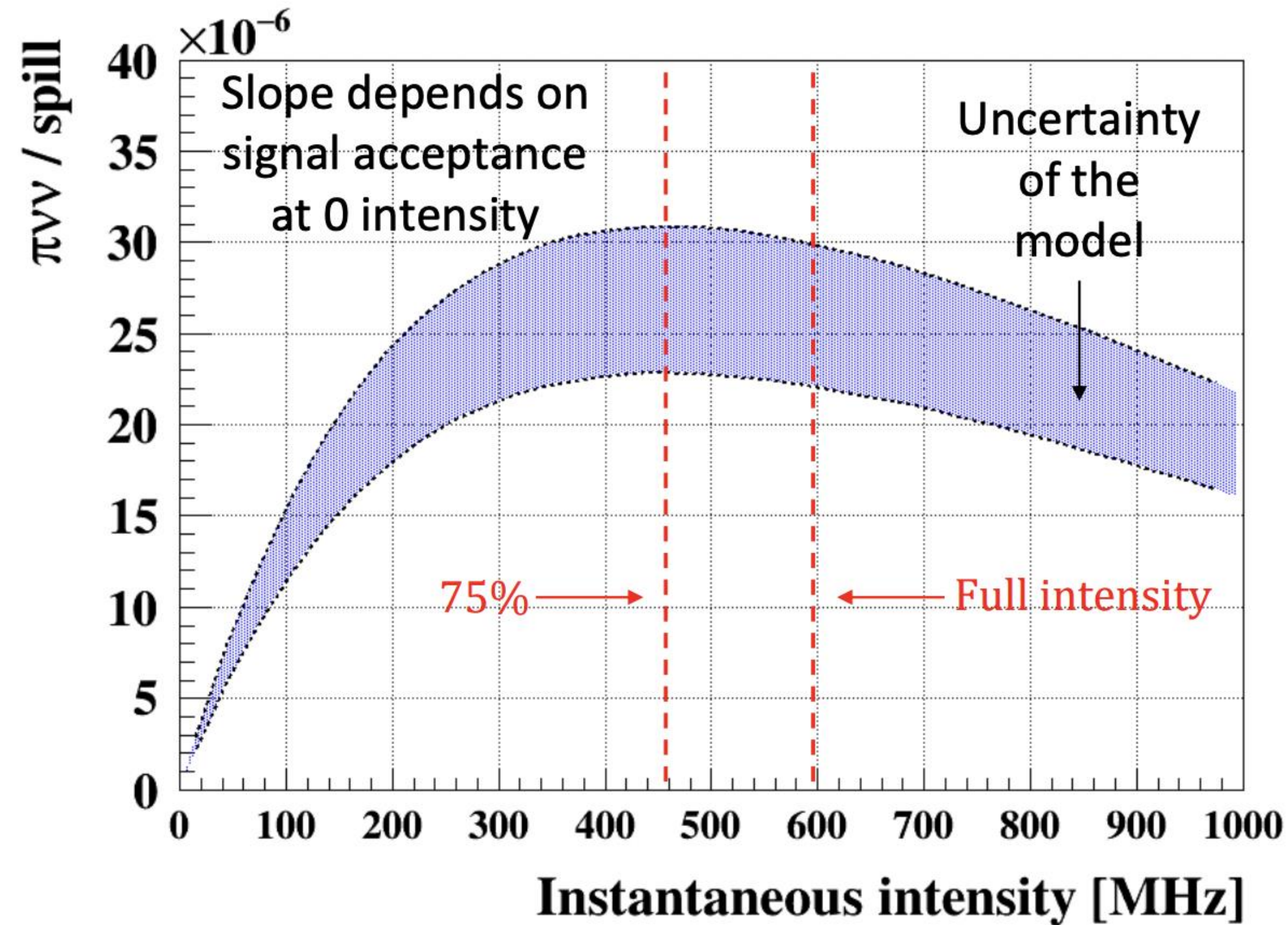
- **Significant improvement in SES uncertainty:**
  - old: 6.3% → new: 3.5%. Due to:
    - trigger efficiency cancellations
    - improved procedures for evaluation of acceptances and  $\varepsilon_{RV}$



# Optimum NA62 intensity



## Selected signal yield vs intensity



- Saturation of expected signal yield with intensity. Mainly due to:
  - Paralyzable effects from TDAQ dead time and trigger veto windows.
  - Offline selection, due to veto conditions.
- Main sources of uncertainty for model:
  - Online time-dependent mis-calibrations.
  - Fit uncertainty.
- **From August 2023 operate at optimal intensity (~75% of full) to maximise  $\pi V V$  sensitivity**
  - Maximise signal yield
  - lower expected background
  - Higher DAQ efficiency

Studies of **2021—22 data** at high intensity **were crucial** to establish optimal intensity

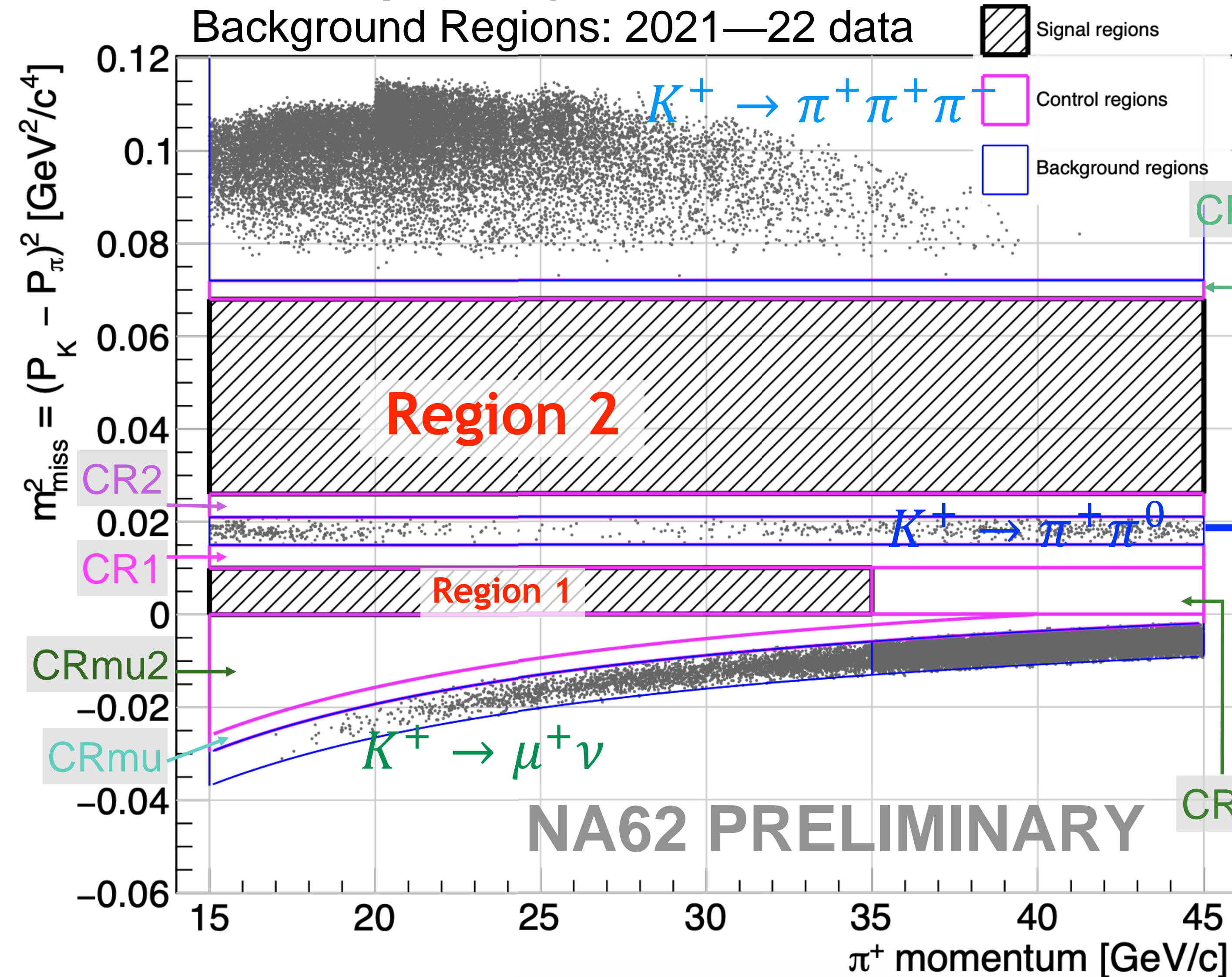
# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ : Analysis of new data

2021—2022 data : **Background Evaluation**

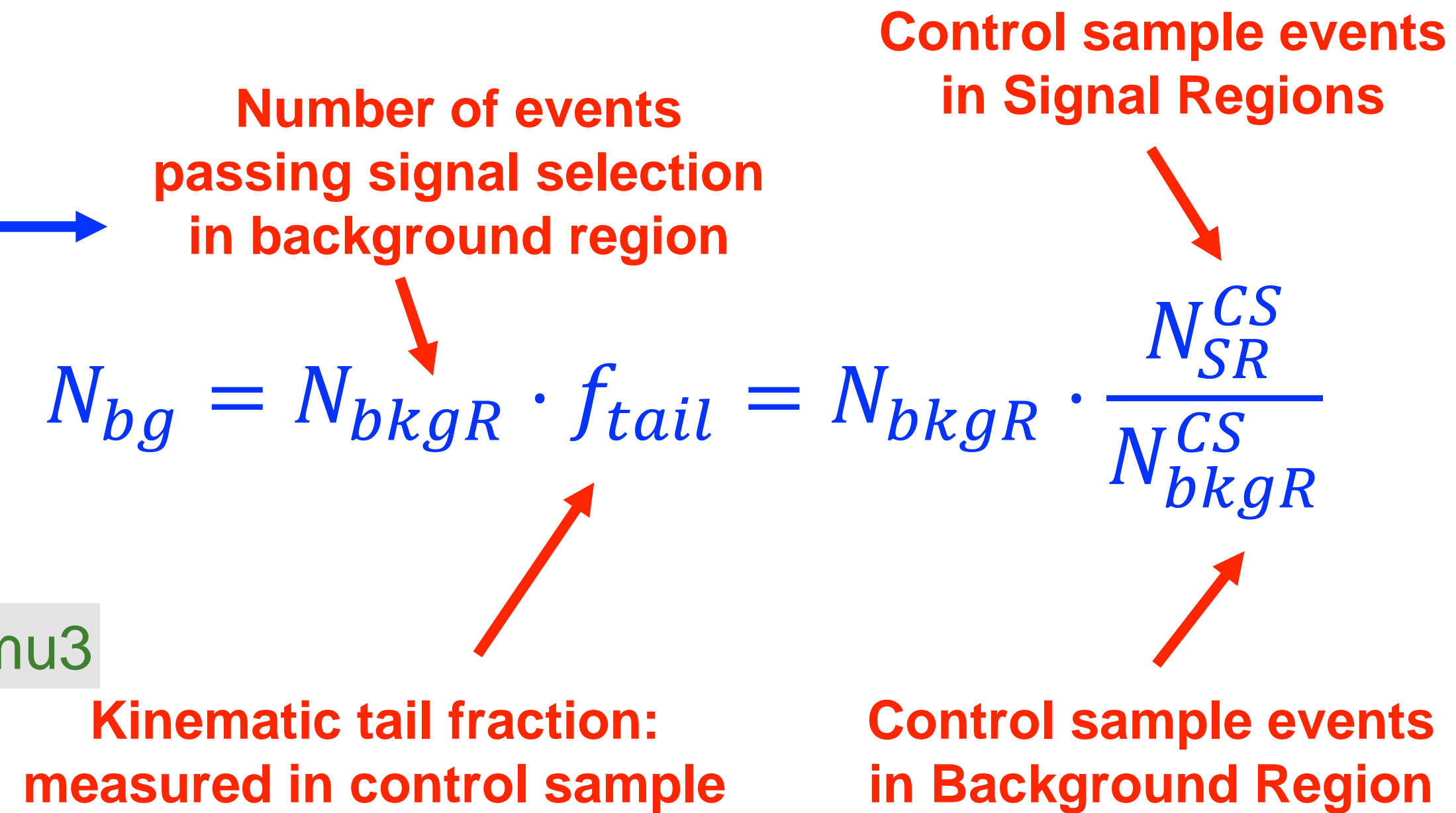
# Background regions & estimations

Events passing  $\pi V V$  selection

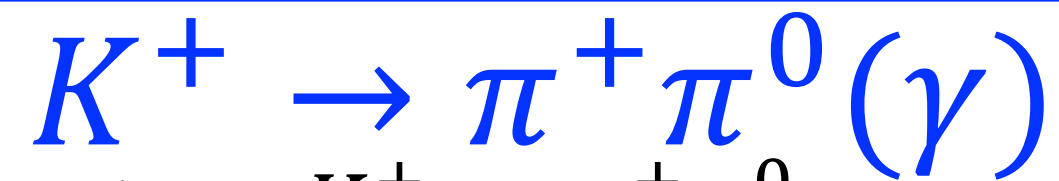
Background Regions: 2021—22 data



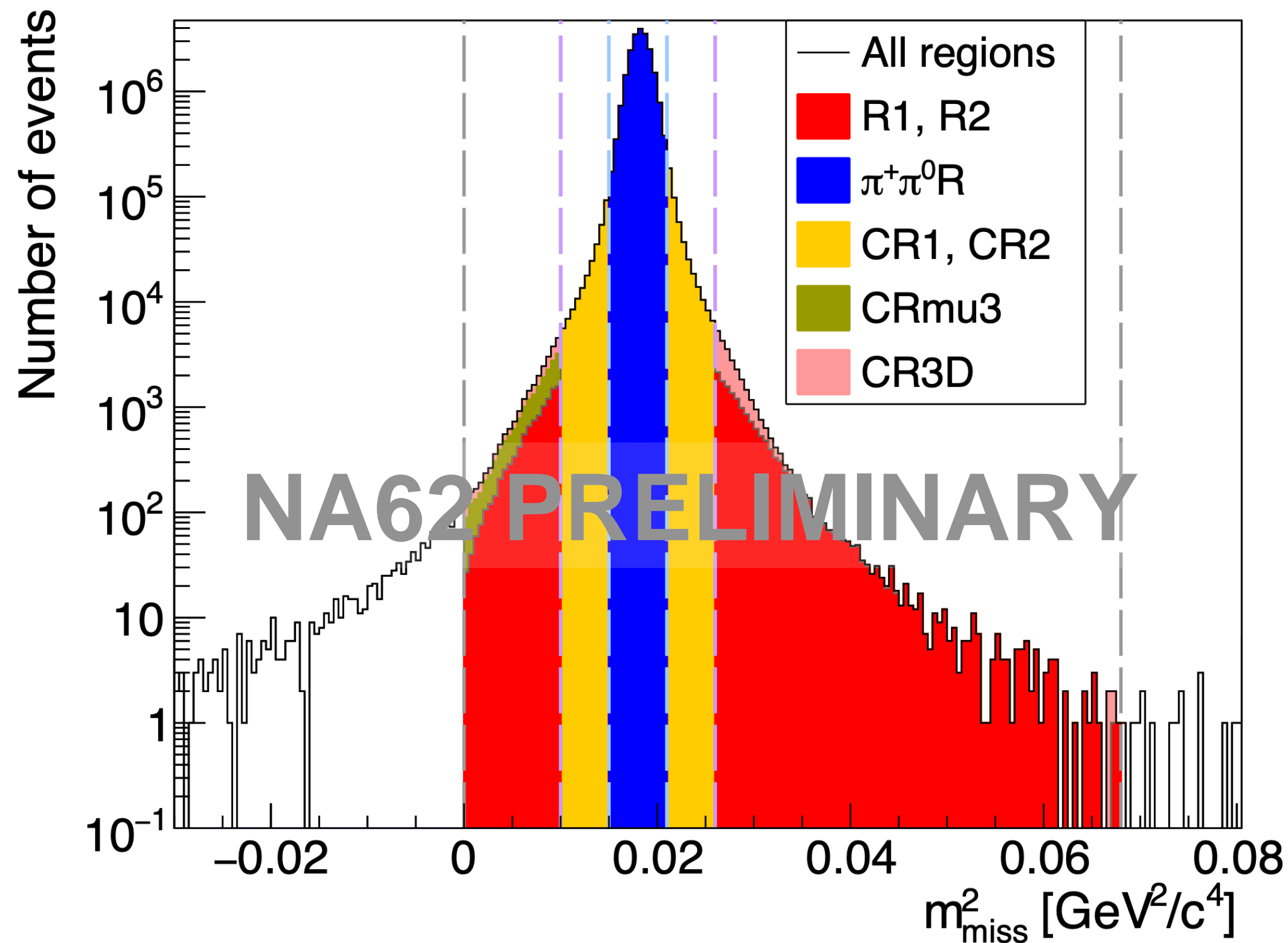
Backgrounds from kinematic misconstruction tails in  $m_{miss}^2$



# Backgrounds from kinematic tails



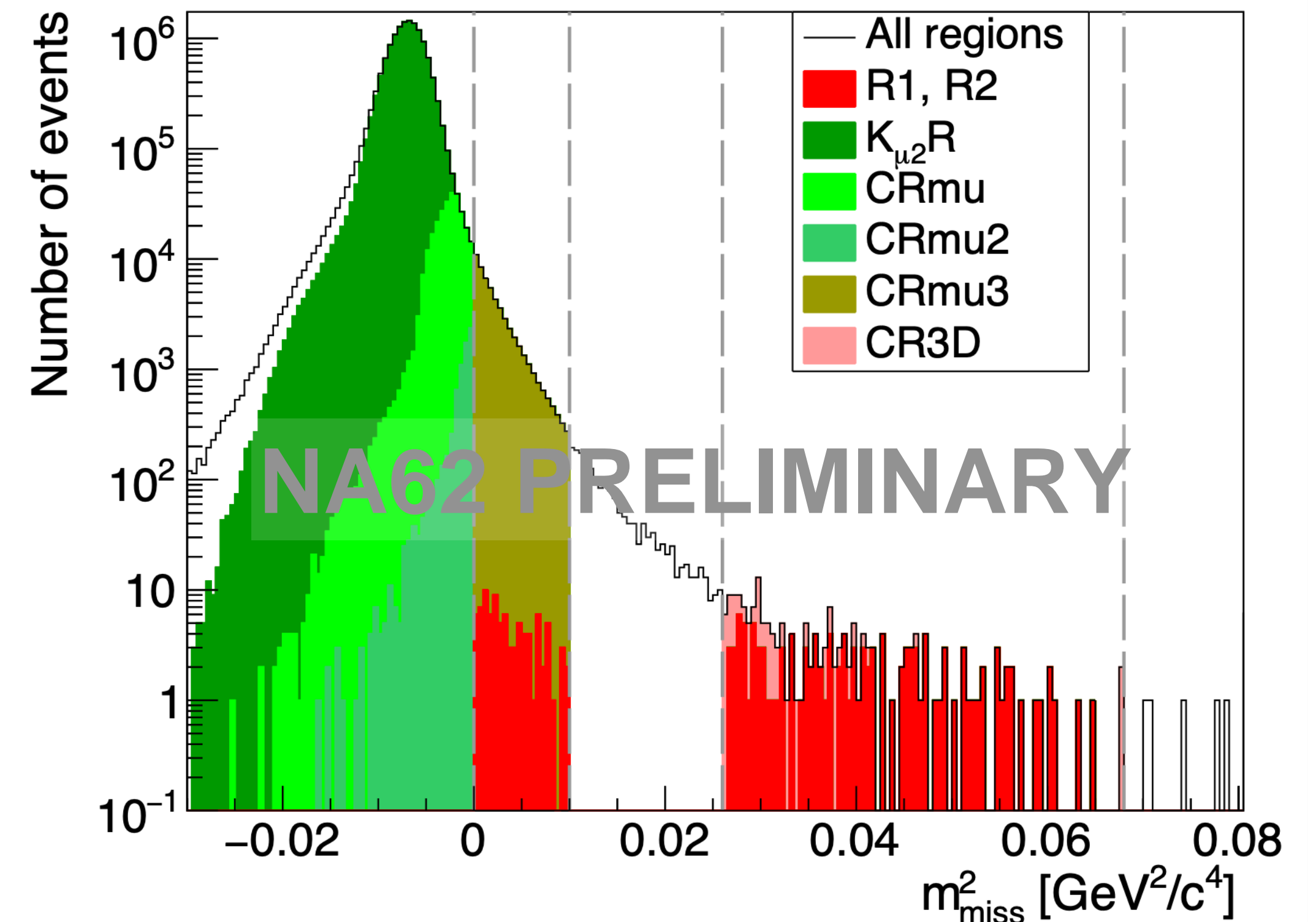
control sample of  $K^+ \rightarrow \pi^+ \pi^0$  events with  $\pi^0 \rightarrow \gamma\gamma$  and 2 photons detected in LKr:



$$N_{bg}(K^+ \rightarrow \pi^+ \pi^0 (\gamma)) = 0.83 \pm 0.05$$

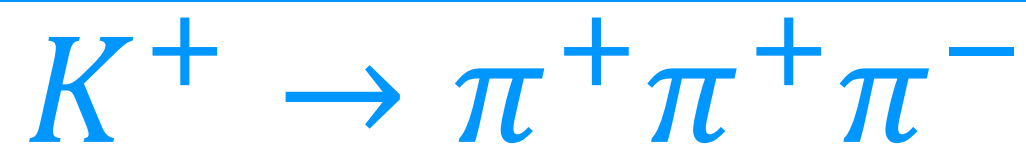


control sample of  $K^+ \rightarrow \mu^+ \nu$  events with RICH PID= $\pi^+$  and Calo PID= $\mu^+$ :



- <1% contribution from  $K^+ \rightarrow \mu^+ \nu$  followed by  $\mu^+ \rightarrow e^+ \nu \nu$

$$N_{bg}(K^+ \rightarrow \mu^+ \nu) = 0.9 \pm 0.2$$



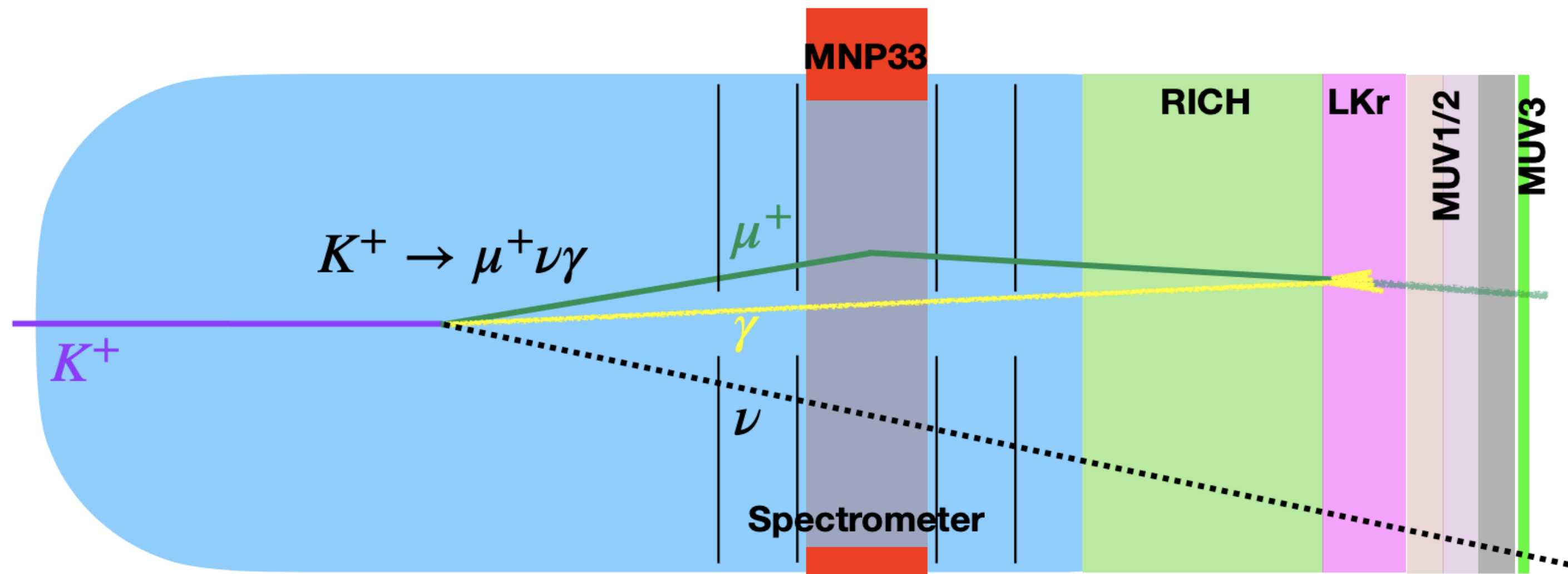
- Use MC to measure  $f_{tail}$ :

$$N_{bg}(K^+ \rightarrow \pi^+ \pi^+ \pi^-) = 0.11 \pm 0.03$$

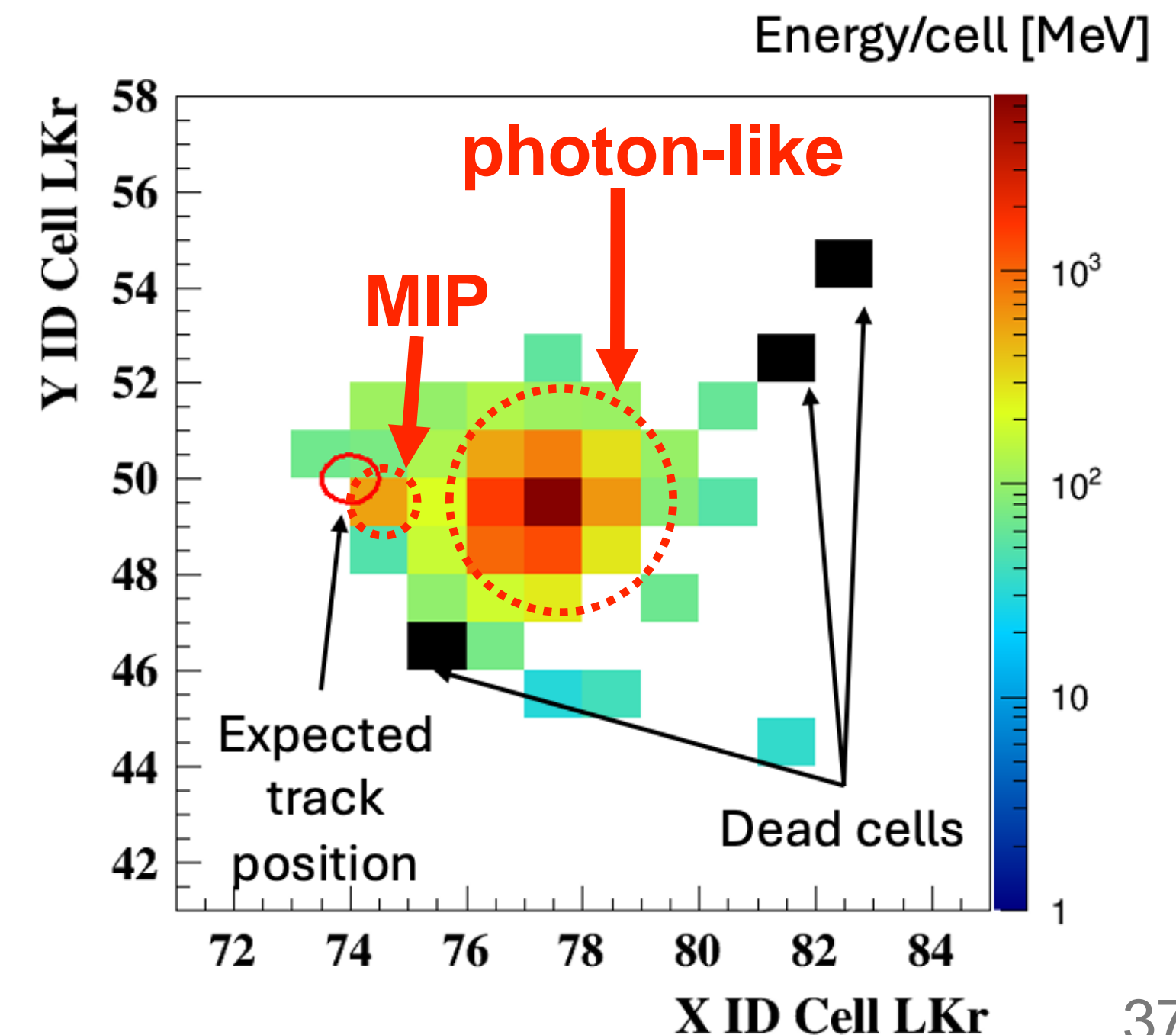
# Radiative decays: $K^+ \rightarrow \pi^+ \pi^0 \gamma$ & $K^+ \rightarrow \mu^+ \nu \gamma$



- $K^+ \rightarrow \pi^+ \pi^0 \gamma$  : included with “kinematic tails” estimation.
  - Suppression: photon vetos, rejection with additional  $\gamma$  is 30x stronger.
  - Estimation: MC + measured single photon rejection efficiency :  $N_{bg}(K^+ \rightarrow \pi^+ \pi^0 \gamma) = 0.07 \pm 0.01$
  - Validation:  $m_{miss}^2$  control regions (CR1,2 - see later)
- $K^+ \rightarrow \mu^+ \nu \gamma$  : not included in “kinematic tails” estimation if  $\gamma$  overlaps  $\mu^+$  at LKr (leading to misID as  $\pi^+$ )
  - Suppression: based on  $(P_K - P_\mu - P_\gamma)^2$  and  $E_\gamma$  with  $\gamma =$  LKr cluster (mis)associated to muon.
    - Necessary for 2021–22 data, since Calorimetric PID degraded at higher intensities.
  - Estimation: min. Bias data control sample with signal in MUV3 :  $N_{bg}(K^+ \rightarrow \mu^+ \nu \gamma) = 0.8 \pm 0.4$
  - Validation: data sample without  $K^+ \rightarrow \mu^+ \nu \gamma$  veto and PID = “less pion-like” (Calo BDT bins below  $\pi^+$  bin).



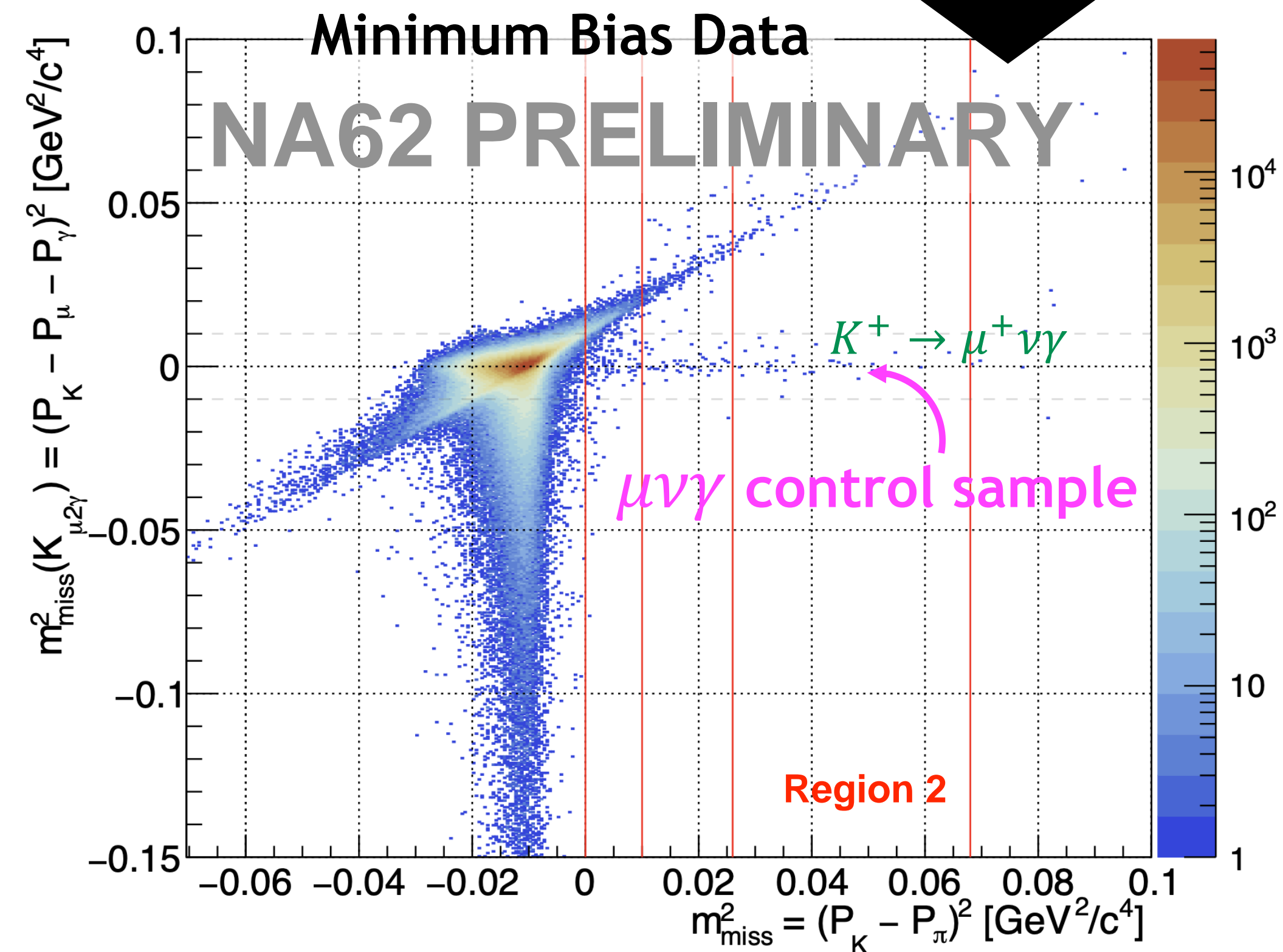
Sketch only



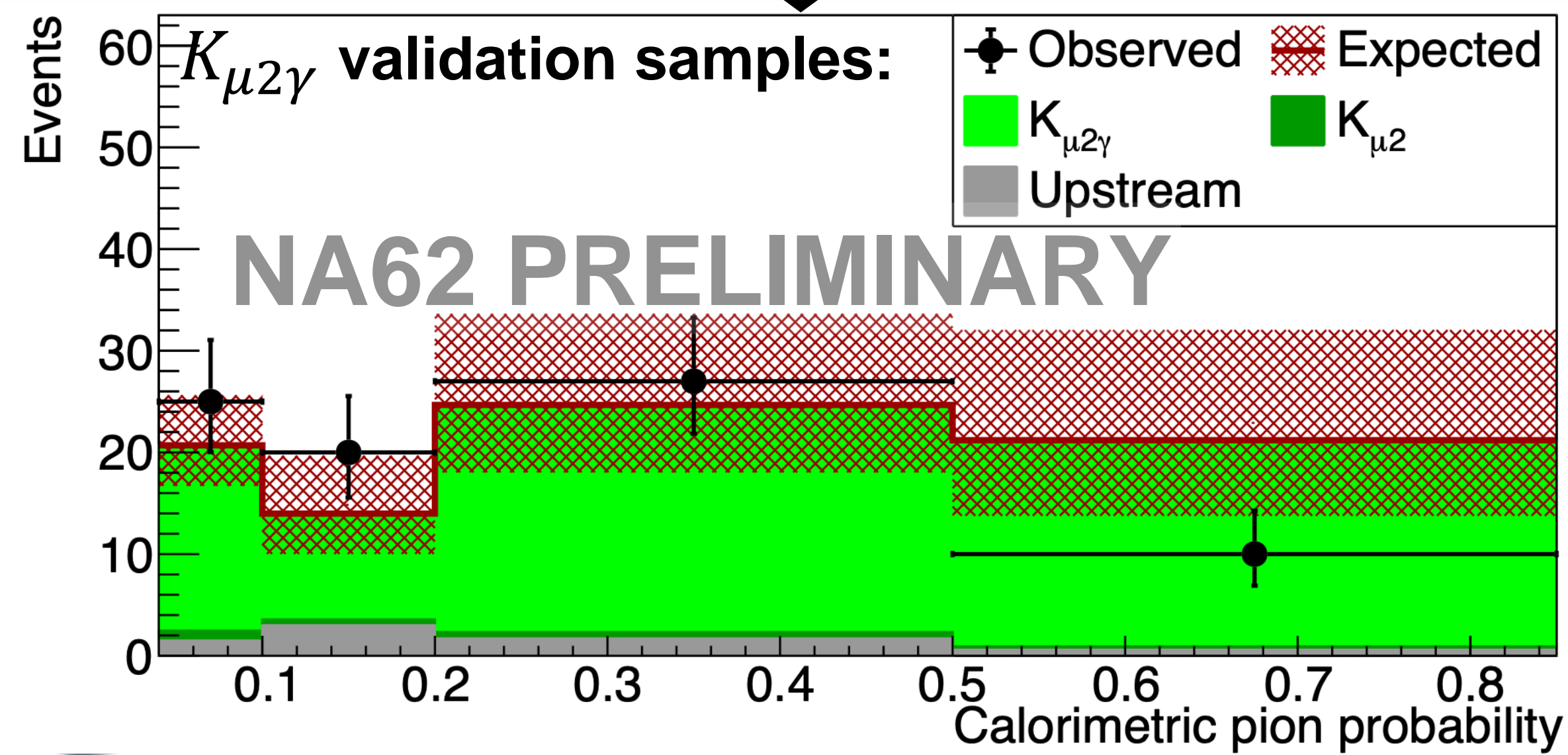
# $K^+ \rightarrow \mu^+ \nu \gamma$ Background

- Kinematically select  $K^+ \rightarrow \mu^+ \nu \gamma$  events:  $m_{miss}^2(K_{\mu 2\gamma}) = (P_K - P_\mu - P_\gamma)^2$ 
  - $P_K$  : 4-momentum of  $K^+$  from GTK (as normal)
  - $P_\mu$  : 4-momentum of track with  $\mu^+$  mass hypothesis.
  - $P_\gamma$  : reconstructed from energy and position of LKr cluster (and position of  $K^+ - \mu^+$  vertex).

Evaluate background expectation using  $\mu\nu\gamma$  control sample from MinimumBias trigger, not applying Calorimetric BDT classifier and MUV3 signal:

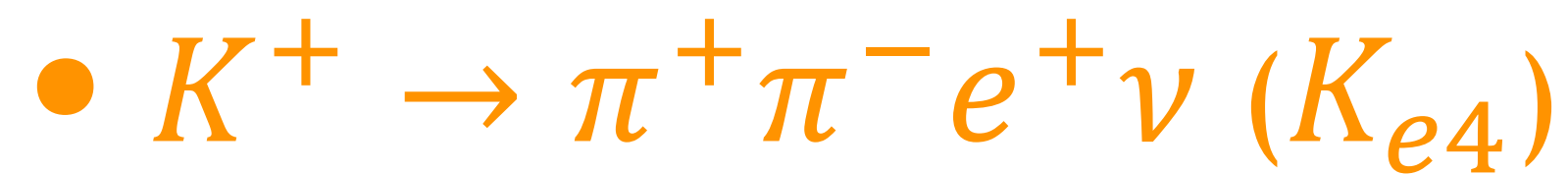


Validation: data sample with PID = “less pion-like” (Calo BDT bins below  $\pi^+$  bin).



- Before  $K^+ \rightarrow \mu^+ \nu \gamma$  veto: found excess of events at  $p > 35$  GeV/c in Region 2 relative to 2016–18 data.
- Additional background identified and studied in data control samples & MC.
- $K^+ \rightarrow \mu^+ \nu \gamma$  veto added to selection criteria for final analysis.

# Other backgrounds



- No clean control samples for  $K_{e4}$  in data: Use  $2 \times 10^9$  simulated decays.

Acceptance :  $A_{K_{e4}} = \frac{N_{MC}^{sel}}{N_{MC}^{gen}} = (1.3 \pm 0.3_{stat}) \times 10^{-8}$

Effective # of  $K^+$       Random veto & trigger efficiencies

$$N_{bg}(K^+ \rightarrow \pi^+ \pi^- e^+ \nu) = N_K \varepsilon_{RV} \varepsilon_{trig} \mathcal{B}_{K_{e4}} A_{K_{e4}}$$

$$N_{bg}(K^+ \rightarrow \pi^+ \pi^- e^+ \nu) = 0.89^{+0.34}_{-0.28}$$

Branching ratio of  $K_{e4}$   
(from PDG)



- Evaluated with simulations.
- **Negligible contributions to total background.**

$$N_{bg}(K^+ \rightarrow \pi^0 \ell^+ \nu) < 1 \times 10^{-3}$$

$$N_{bg}(K^+ \rightarrow \pi^+ \gamma \gamma) = 0.01 \pm 0.01$$

# Upstream background evaluation

$$N_{bg} = \sum_i N_i f_{cda} P_i^{match}$$

$N$  Upstream Reference Sample:  
signal selection but invert CDA cut (CDA > 4mm)

$f_{cda}$  Scaling factor : bad cda  $\rightarrow$  good cda

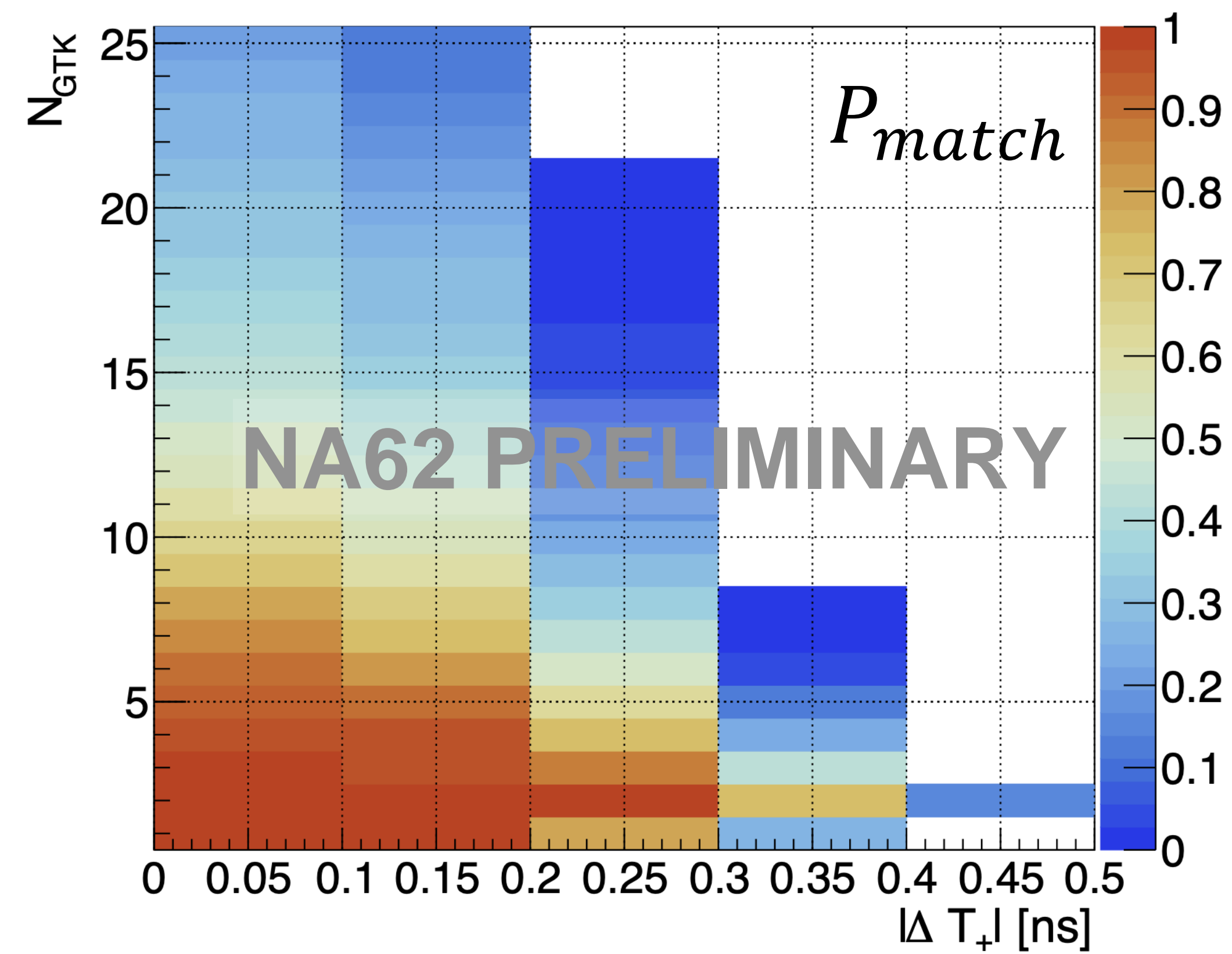
$P_{match}$  Probability to pass  $K^+ - \pi^+$  matching

Calculate using bins (i) of  $(\Delta T_+, N_{GTK})$   
[Updated to fully data-driven procedure]

$$N = 51 \quad f_{CDA} = 0.20 \pm 0.03 \quad \langle P_{match} \rangle = 73\%$$

$$N_{bg}(Upstream) = 7.4^{+2.1}_{-1.8}$$

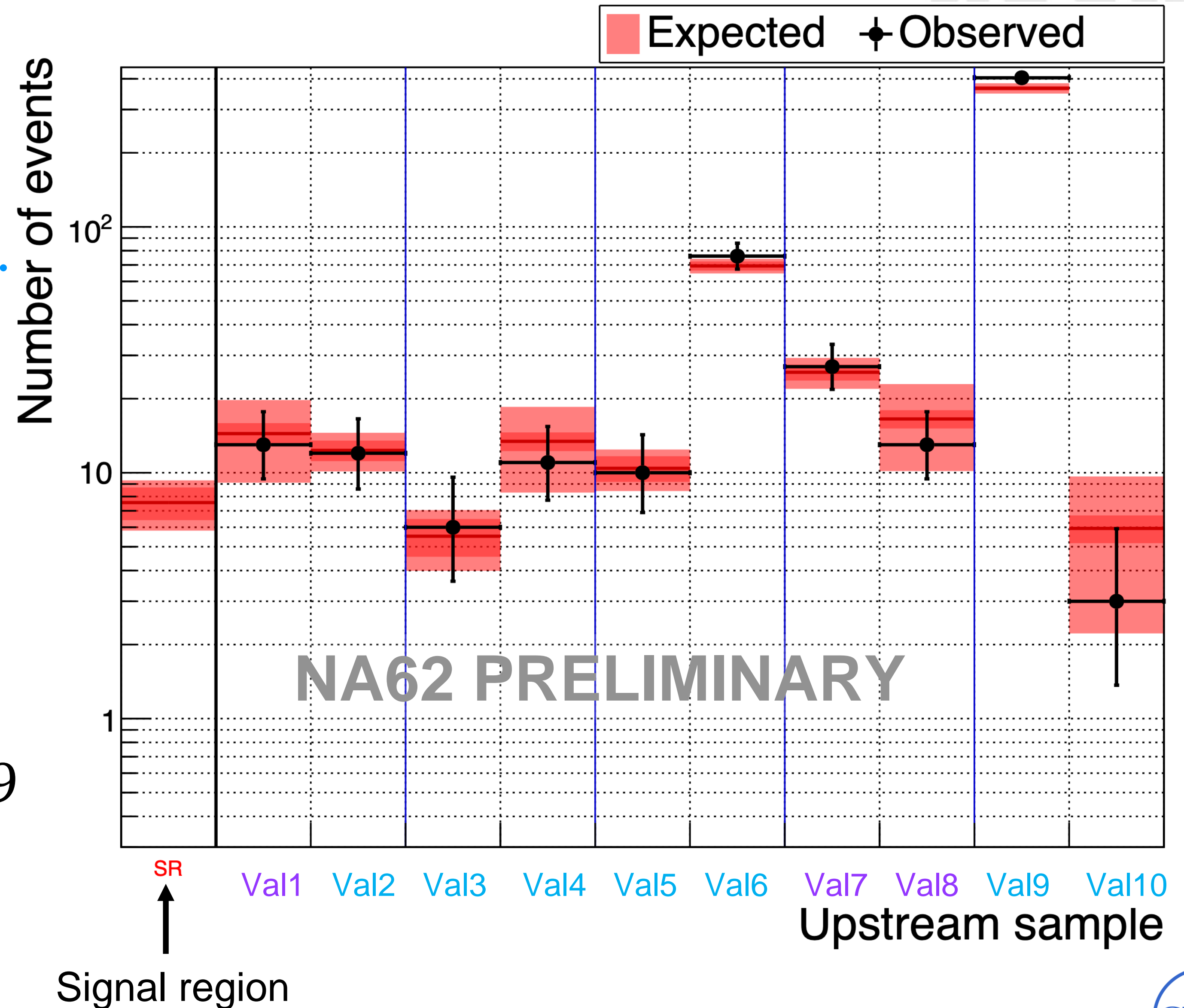
- Upstream reference sample contains all known upstream mechanisms.
  - $N$  provides normalisation.
- $f_{CDA}$  depends only on geometry.
- $P_{match}$  depends on  $(\Delta T_+, N_{GTK})$ .





# Upstream background validation

- Invert & loosen upstream vetos to enrich with different mechanisms:
  - Interaction-enriched: Val1,2,7,8
  - Accidental-enriched: Val3,4,5,6,9,10.
- All independent.
- Expectations and observations are in good agreement.
- Number of events rejected by VetoCounter:
  - (i.e. events in signal region with associated VC signal)
  - $N_{exp}^{VCrej.} = 6.9 \pm 1.4$  ,  $N_{obs}^{VCrej.} = 9$
- VetoCounter is essential to control upstream background.



# Summary of expectations

## Backgrounds

$K^+ \rightarrow \pi^+ \pi^0 (\gamma)$	$0.83 \pm 0.05$
$K^+ \rightarrow \pi^+ \pi^0$	$0.76 \pm 0.04$
$K^+ \rightarrow \pi^+ \pi^0 \gamma$	$0.07 \pm 0.01$
$K^+ \rightarrow \mu^+ \nu (\gamma)$	$1.70 \pm 0.47$
$K^+ \rightarrow \mu^+ \nu$	$0.87 \pm 0.19$
$K^+ \rightarrow \mu^+ \nu \gamma$	$0.82 \pm 0.43$
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	$0.11 \pm 0.03$
$K^+ \rightarrow \pi^+ \pi^- e^+ \nu$	$0.89^{+0.34}_{-0.28}$
$K^+ \rightarrow \pi^0 \ell^+ \nu$	$< 0.001$
$K^+ \rightarrow \pi^+ \gamma \gamma$	$0.01 \pm 0.01$
Upstream	$7.4^{+2.1}_{-1.8}$
Total	$11.0^{+2.1}_{-1.9}$

## Signal Sensitivity

$$\mathcal{B}_{SES} = (0.84 \pm 0.03) \times 10^{-11}$$

$$N_{\pi\nu\bar{\nu}}^{SM,exp} = \frac{\mathcal{B}_{\pi\nu\bar{\nu}}^{SM}}{\mathcal{B}_{SES}}$$

Assuming  $\mathcal{B}_{\pi\nu\bar{\nu}}^{SM} = 8.4 \times 10^{-11}$  :

2021–22:  $N_{\pi\nu\bar{\nu}} = 10.00 \pm 0.34$

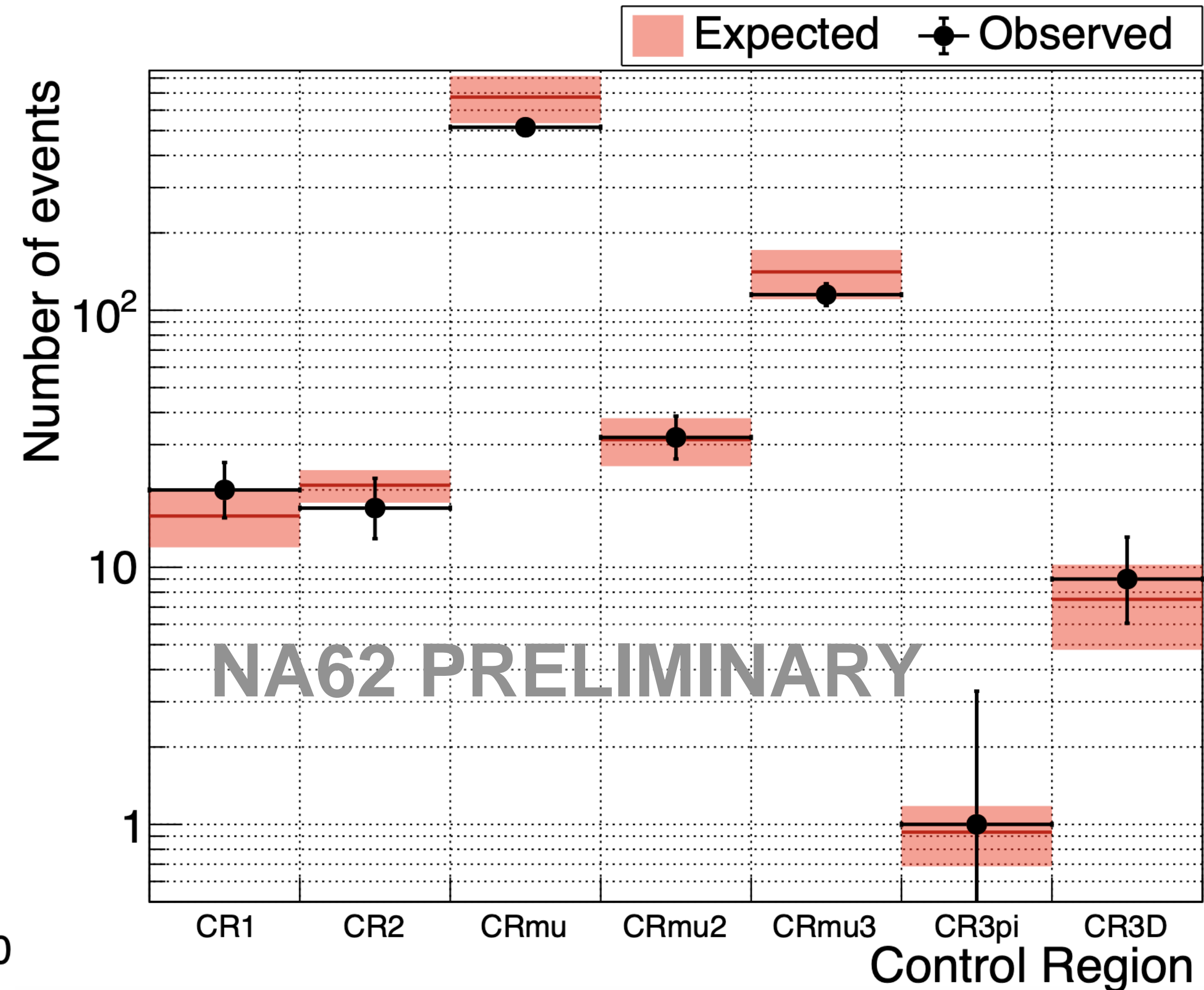
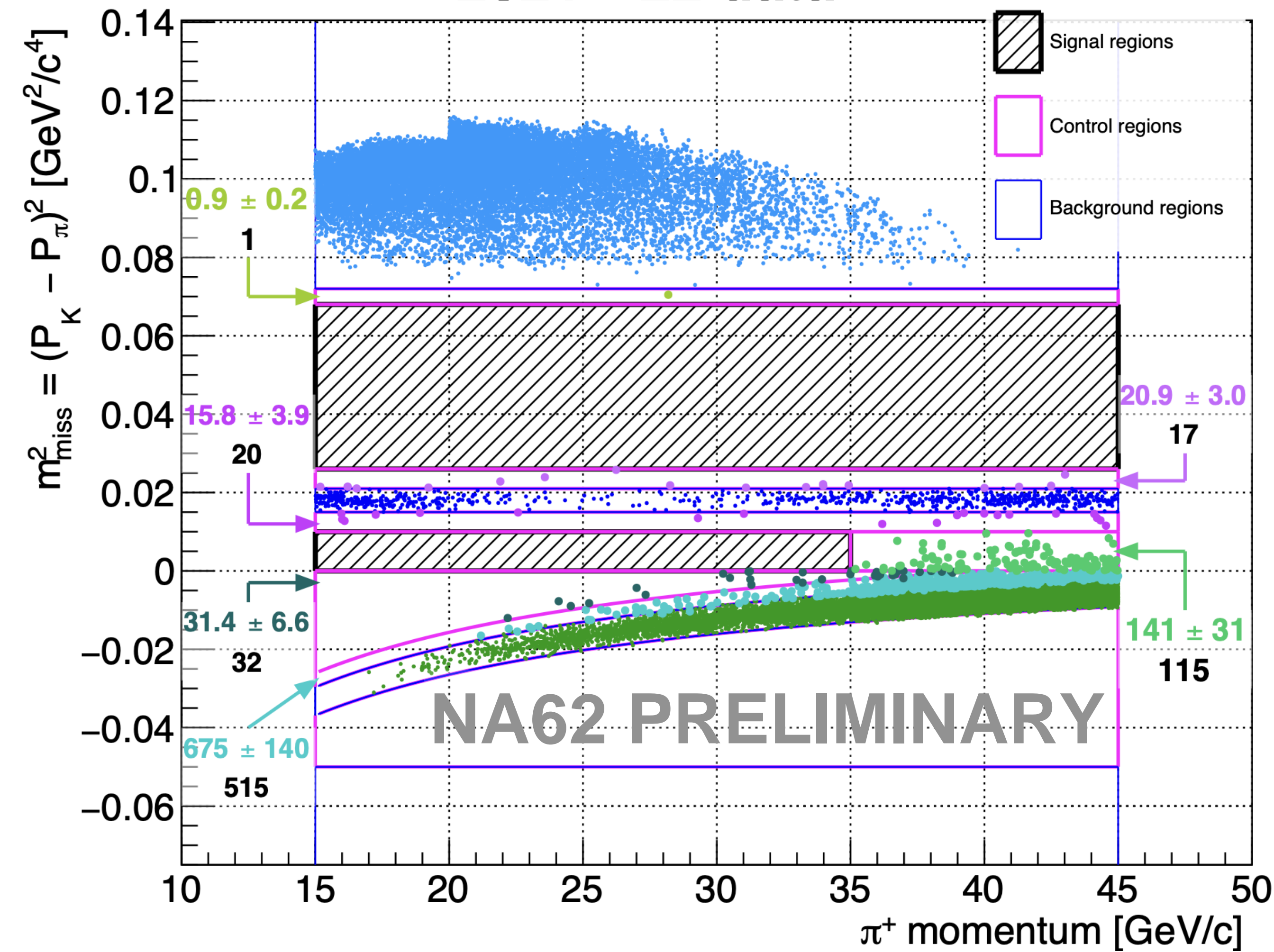
c.f. 2016–18 :  $N_{\pi\nu\bar{\nu}} = 10.01 \pm 0.42$

Expected signal doubled by including 2021–22 data

- $N_{\pi\nu\bar{\nu}}^{SM}$  per SPS burst:  $2.5 \times 10^{-5}$  in 2022
  - c.f.  $1.7 \times 10^{-5}$  in 2018.  $\Rightarrow$  signal yield increased by 50%
- Sensitivity for BR  $\sim \sqrt{S + B}/S$  similar but improved with respect to 2018 analysis, for same amount of data

# Control regions: 2021–22 Data

2021–22 data



- Good agreement in control regions validates background expectations.

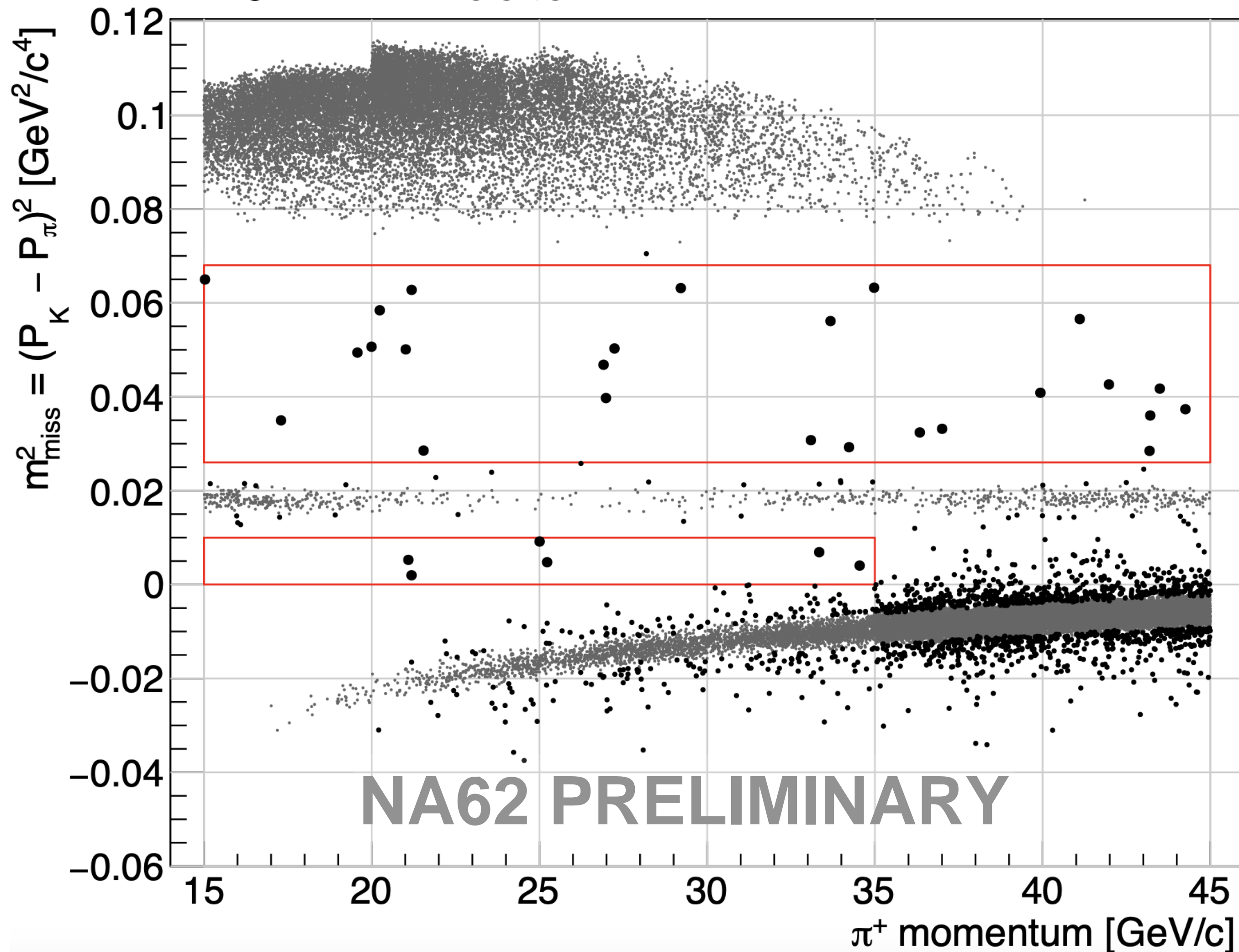
# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ : New NA62 Results

2021—22 data  
and combined 2016—22 data

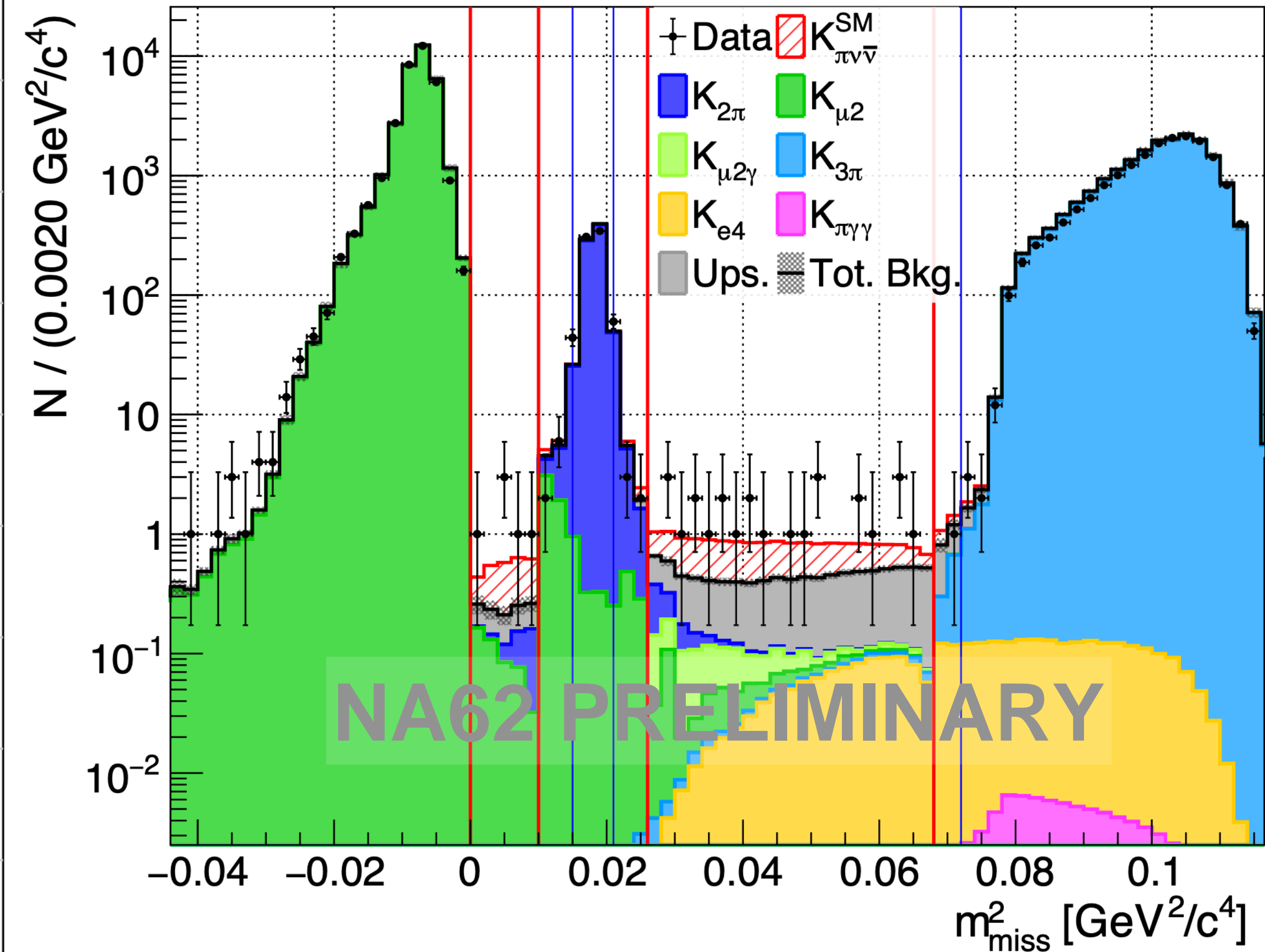
# Signal regions: 2021–22 Data



2021–22 data



1D projection with differential background predictions & SM signal expectation [not a fit]:



Expected SM signal:  $N_{\pi\nu\bar{\nu}}^{SM} \approx 10$

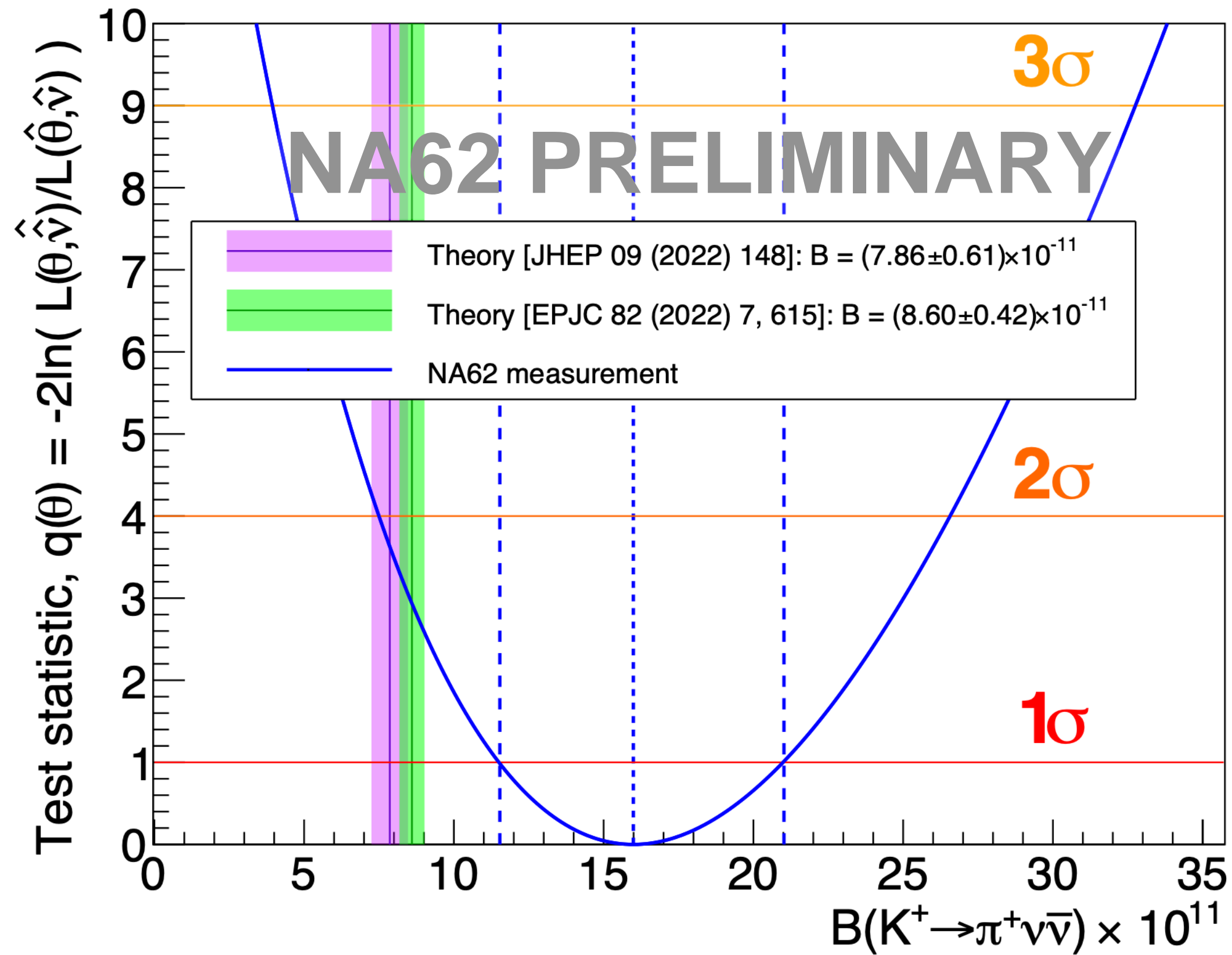
Expected background:  $N_{bg} = 11.0^{+2.1}_{-1.9}$

Observed:  $N_{obs} = 31$

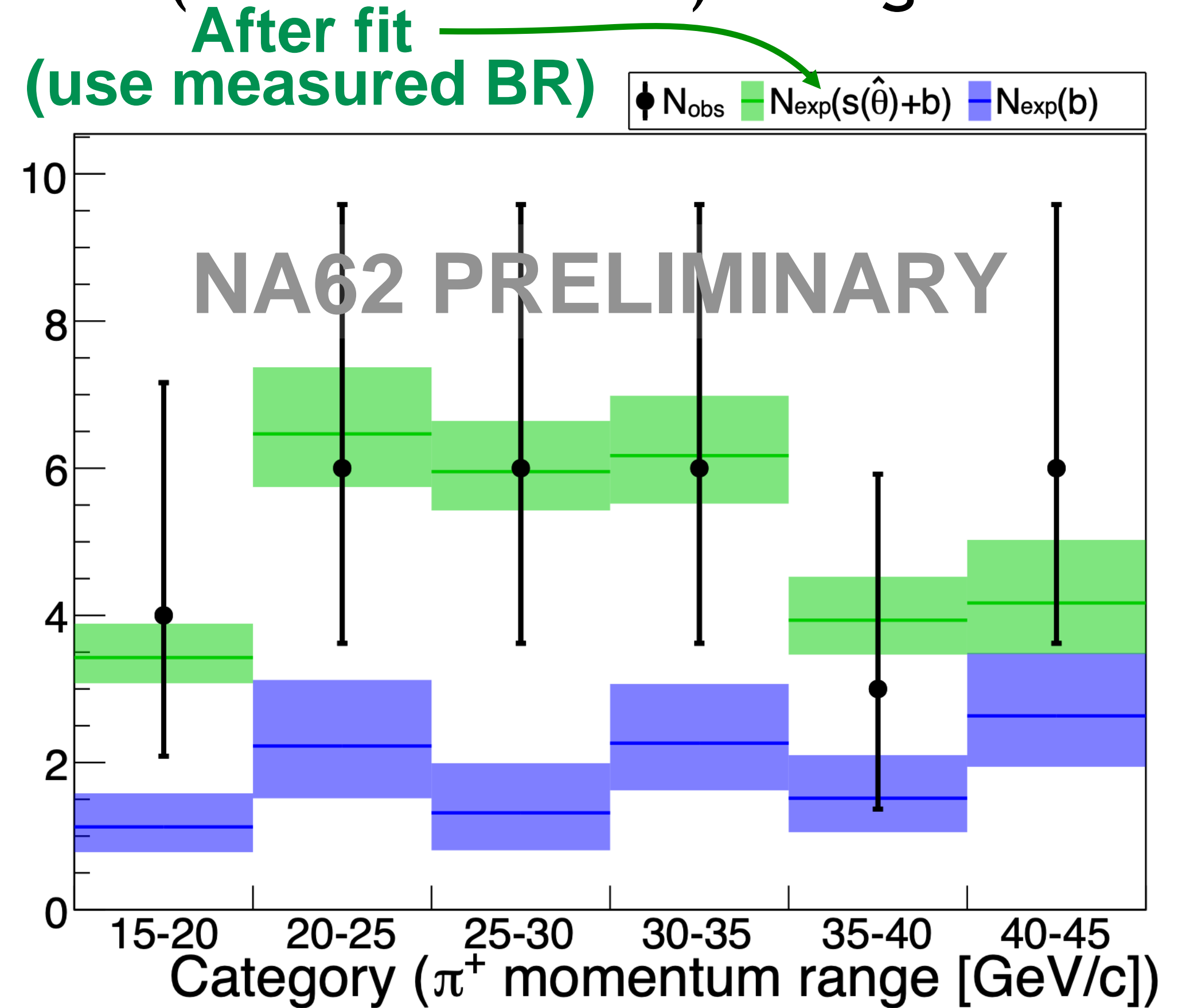
# Results: 2021–22 Data



- Measure  $\mathcal{B}_{\pi\nu\bar{\nu}}$  and 68% ( $1\sigma$ ) confidence interval using a profile likelihood ratio test statistic  $q(\theta)$



- Use 6 (momentum bin) categories

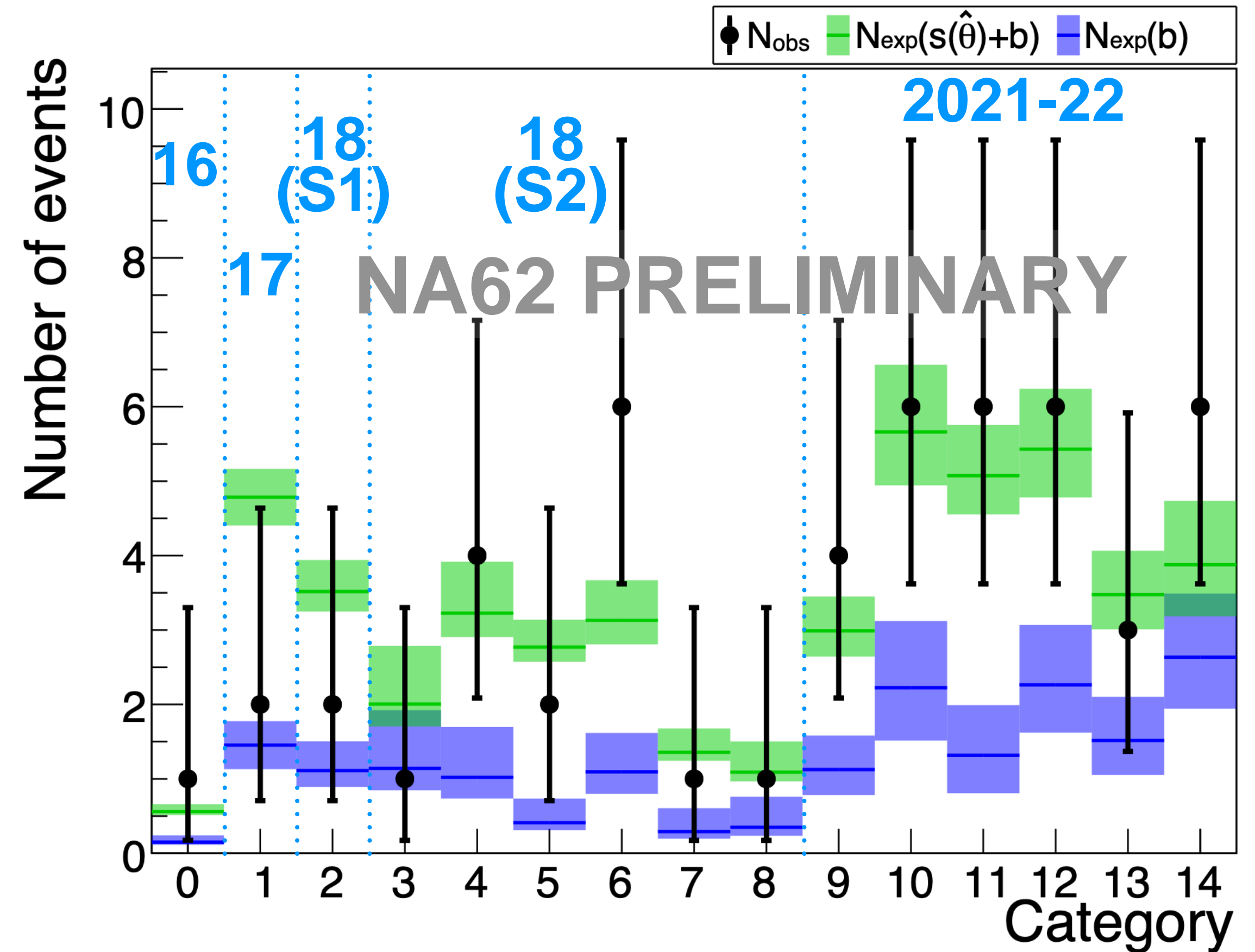
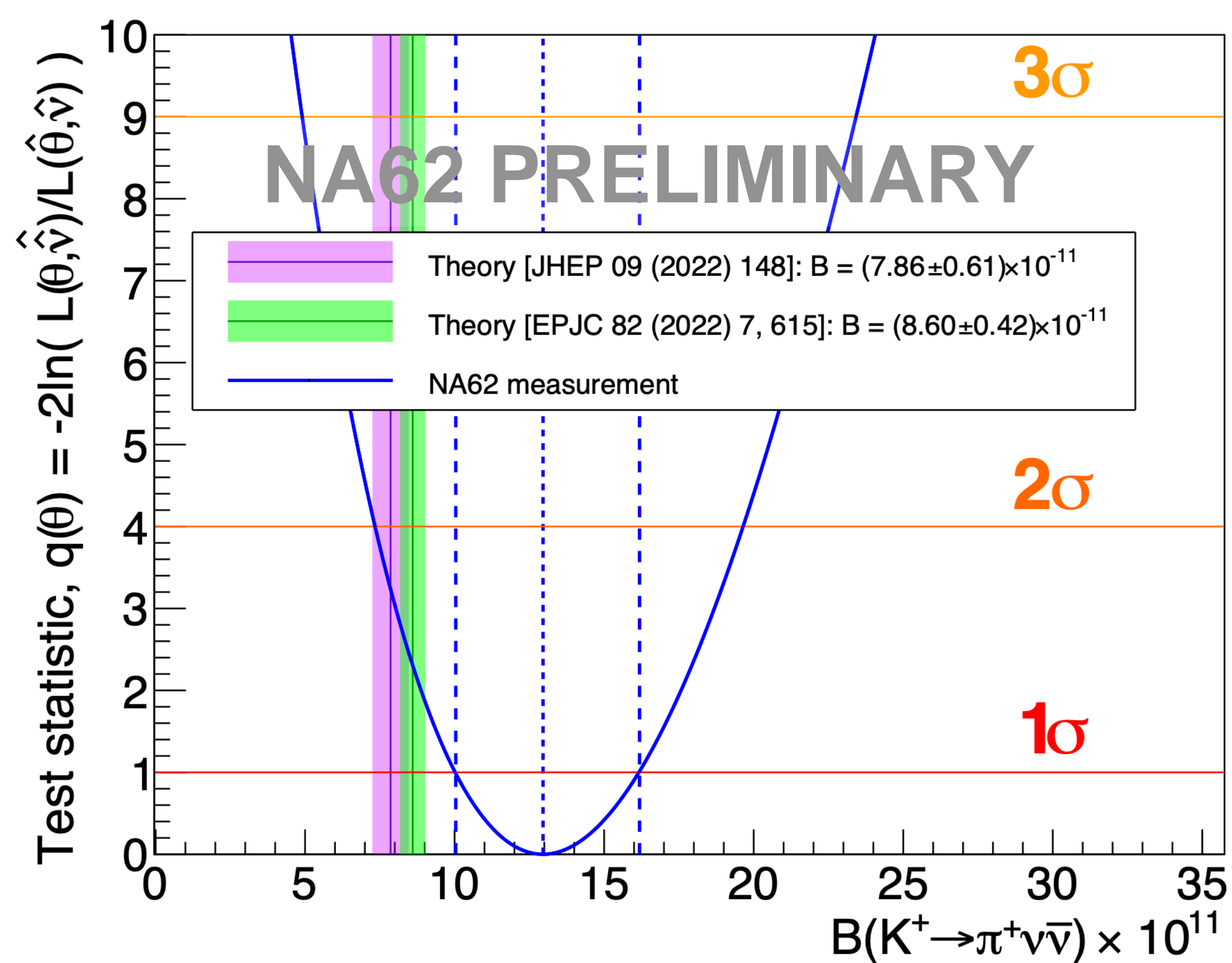


$$\mathcal{B}_{21-22}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (16.0_{-4.5}^{+5.0}) \times 10^{-11} = (16.0 ({}_{-4.2}^{+4.8})_{\text{stat}} ({}_{-1.3}^{+1.4})_{\text{syst}}) \times 10^{-11}$$

# Combining NA62 results: 2016–22



- Integrating 2016–22 data:  $N_{bg} = 18_{-2}^{+3}$ ,  $N_{obs} = 51$ .
- Background-only hypothesis **p-value** =  $2 \times 10^{-7} \Rightarrow$  **significance**  $Z > 5$



$$B_{16-22}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (13.0_{-2.9}^{+3.3}) \times 10^{-11} = (13.0 ({}_{-2.7}^{+3.0})_{stat} ({}_{-1.2}^{+1.3})_{syst}) \times 10^{-11}$$

# Results in context

BNL E787/E949 experiment  
[\[Phys.Rev.D 79 \(2009\) 092004\]](#)

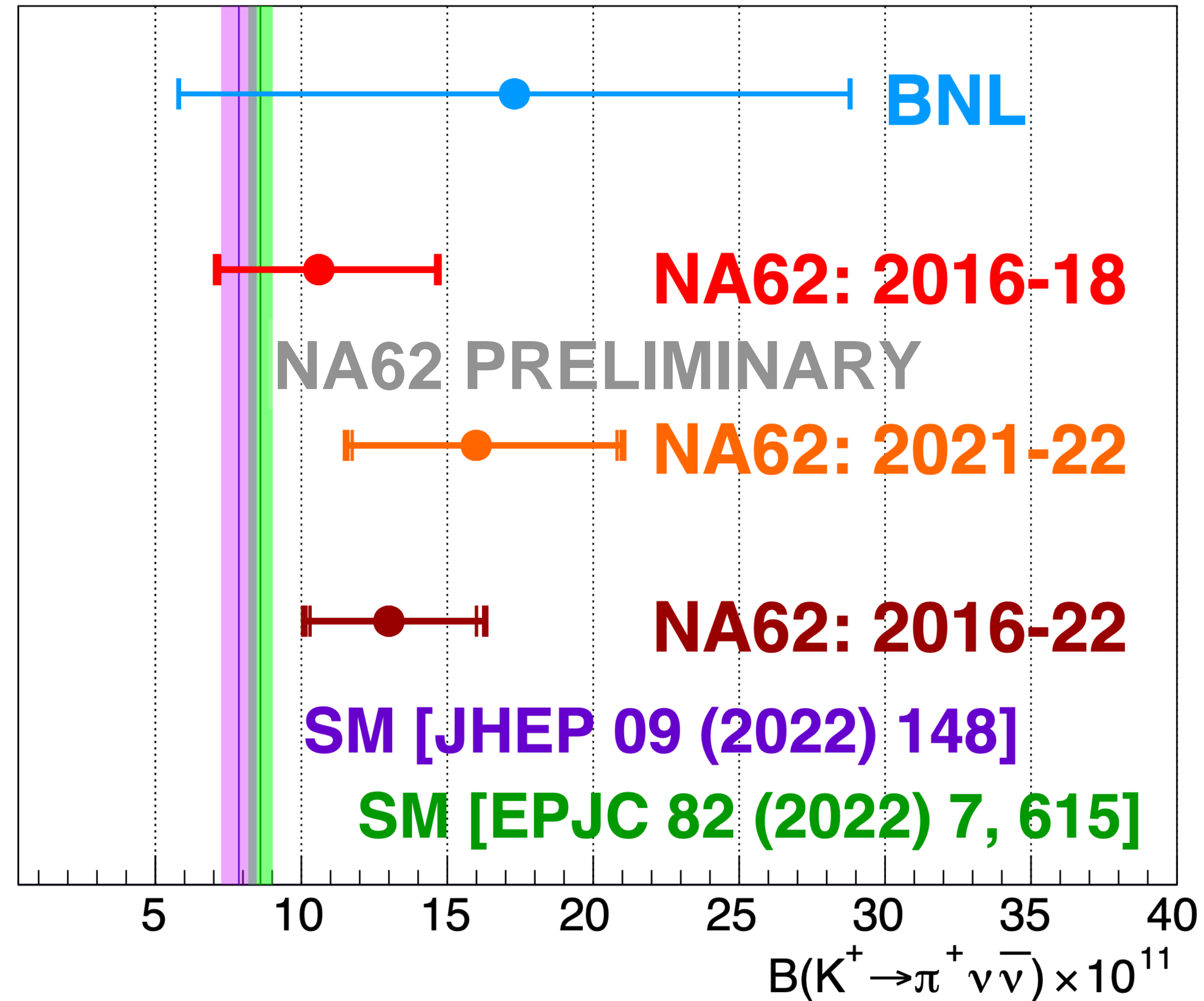
$$\mathcal{B}_{\pi\nu\bar{\nu}}^{16-18} = \left(10.6^{+4.1}_{-3.5}\right) \times 10^{-11}$$

[JHEP 06 (2021) 093]

$$\mathcal{B}_{\pi\nu\bar{\nu}}^{21-22} = \left(16.0^{+5.0}_{-4.5}\right) \times 10^{-11}$$

$$\mathcal{B}_{\pi\nu\bar{\nu}}^{16-22} = \left(13.0^{+3.3}_{-2.9}\right) \times 10^{-11}$$

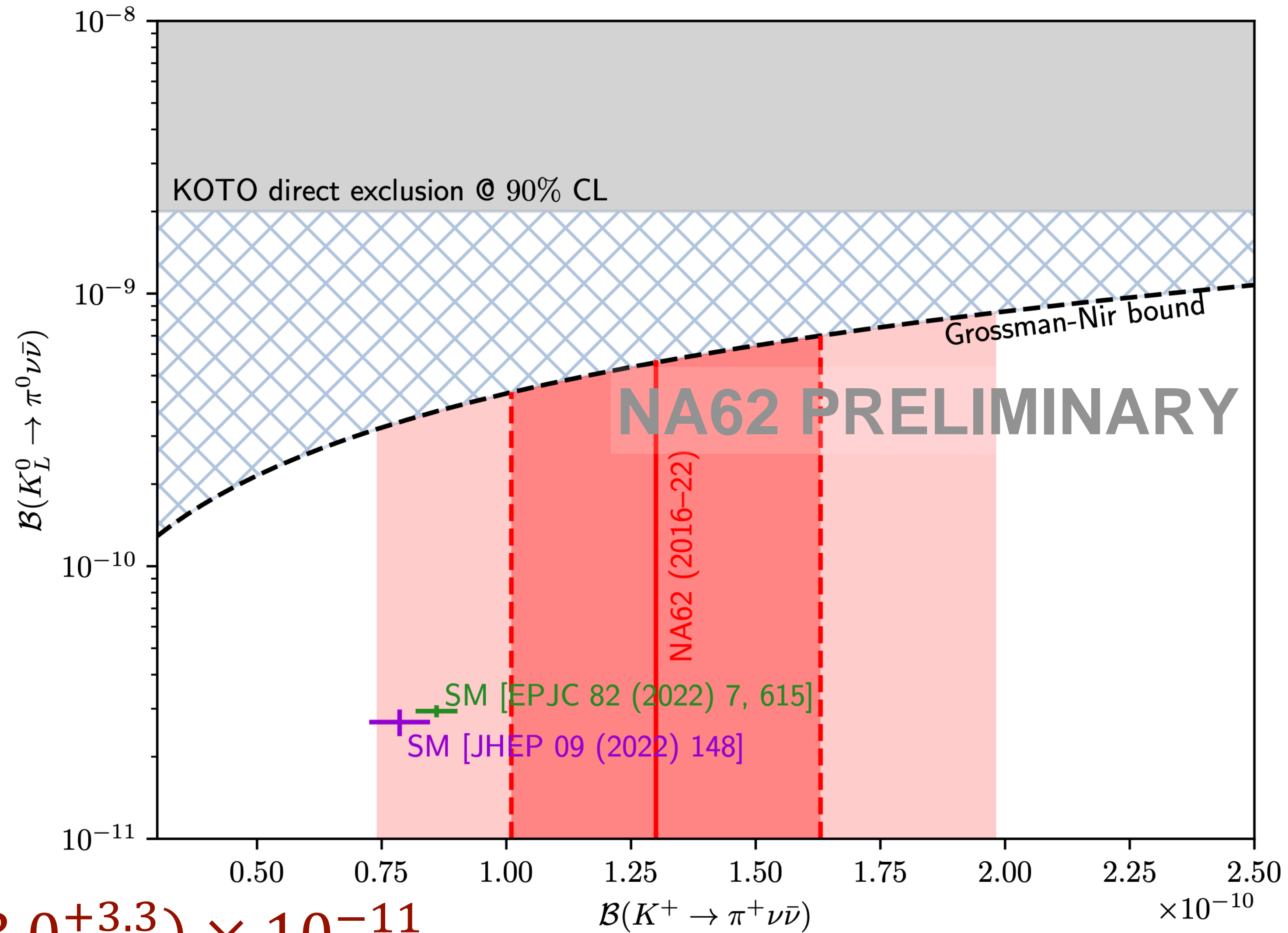
- NA62 results are consistent
- Central value moved up (now 1.5–1.7 $\sigma$  above SM)
- Fractional uncertainty decreased: 40% to 25%
- Bkg-only hypothesis rejected with significance  $Z > 5$





# Results in context

- Fractional uncertainty: 25%
- Bkg-only hypothesis rejected with significance  $Z > 5$
- Observation of the  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  decay with BR consistent with SM prediction, within  $1.7\sigma$
- Need full NA62 data-set to clarify SM agreement or tension



$$\mathcal{B}_{\pi\nu\bar{\nu}}^{16-22} = (13.0_{-2.9}^{+3.3}) \times 10^{-11}$$

$$2\sigma \text{ range : } [7.4 - 19.7] \times 10^{-11}$$

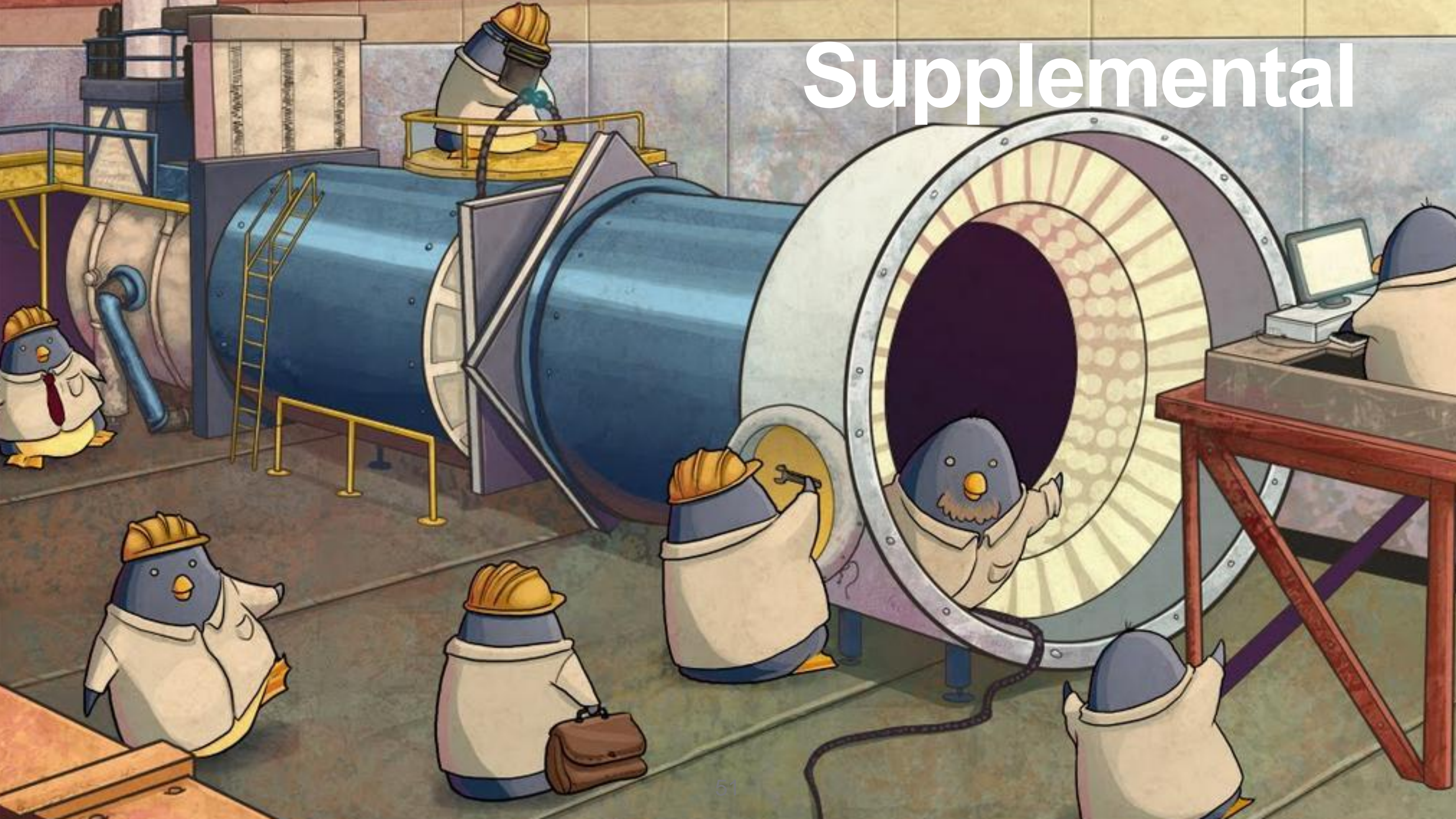
# Conclusions



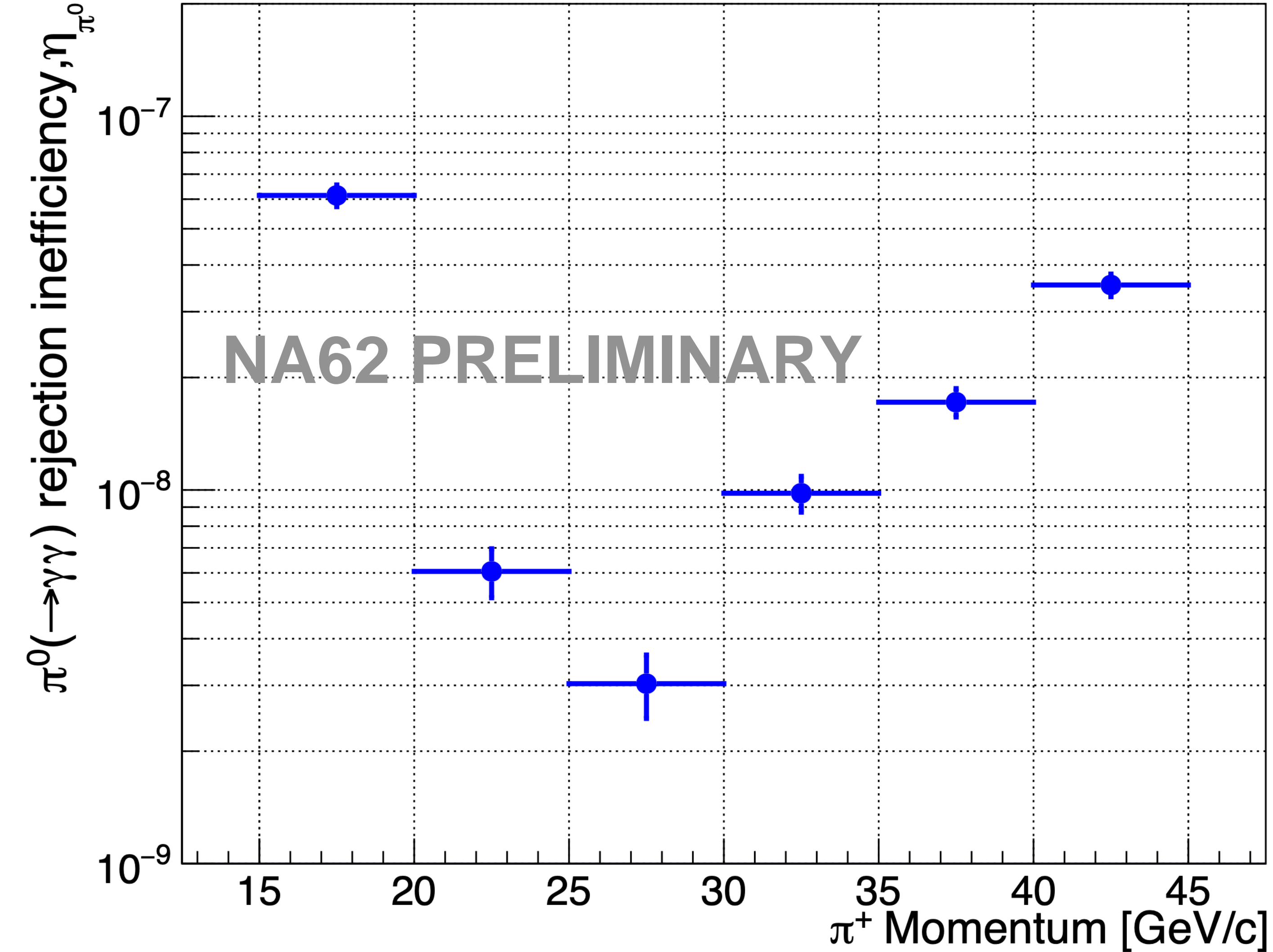
- New study of  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  decay using NA62 2021–22 dataset:
  - Improved signal yield per SPS spill by 50%.
  - $N_{bg} = 11.0_{-1.9}^{+2.1}$  ,  $N_{obs} = 31$
  - $\mathcal{B}_{21-22}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (16.0_{-4.5}^{+5.0}) \times 10^{-11} = (16.0 \text{ }_{-4.2}^{+4.8})_{stat} \text{ }_{-1.3}^{+1.4})_{syst} \times 10^{-11}$
- Combining with 2016–18 data for full 2016–22 results:
  - $N_{bg} = 18_{-2}^{+3}$  ,  $N_{obs} = 51$  (using 9+6 categories for BR extraction)
  - $\mathcal{B}_{16-22}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (13.0_{-2.9}^{+3.3}) \times 10^{-11} = (13.0 \text{ }_{-2.7}^{+3.0})_{stat} \text{ }_{-1.2}^{+1.3})_{syst} \times 10^{-11}$
  - Background-only hypothesis rejected with significance  $Z > 5$ .
- **First observation of  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  decay: BR consistent with SM prediction within  $1.7\sigma$** 
  - Need full NA62 data-set to clarify SM agreement or tension.

2023–LS3 data-set collection & analysis in progress...

# Supplemental



# Photon veto performance



- Probability of  $K^+ \rightarrow \pi^+ \pi^0$  events with  $\pi^0 \rightarrow \gamma\gamma$  passing full photon vetos:

Number of events passing full  $\pi^+ \nu \bar{\nu}$  selection in  $\pi^+ \pi^0$  region

$$\eta_{\pi^0} = \frac{N_{sel.}^{\pi^+ \pi^0 R}}{N_{\pi\pi} D_0 \epsilon_{trig} \epsilon_{RV}}$$

Number of selected normalisation events

Normalisation trigger downscaling and efficiency

Random veto efficiency

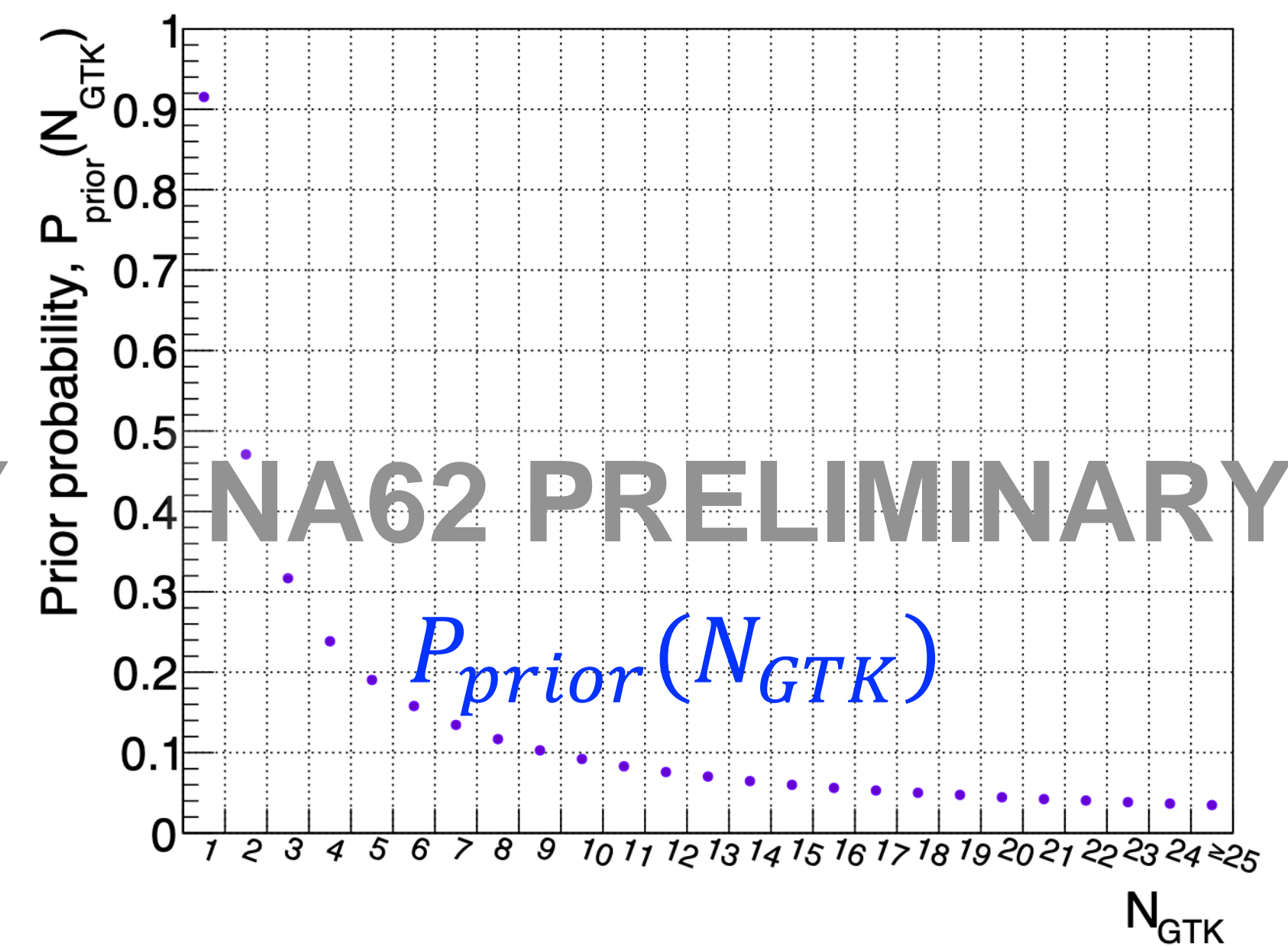
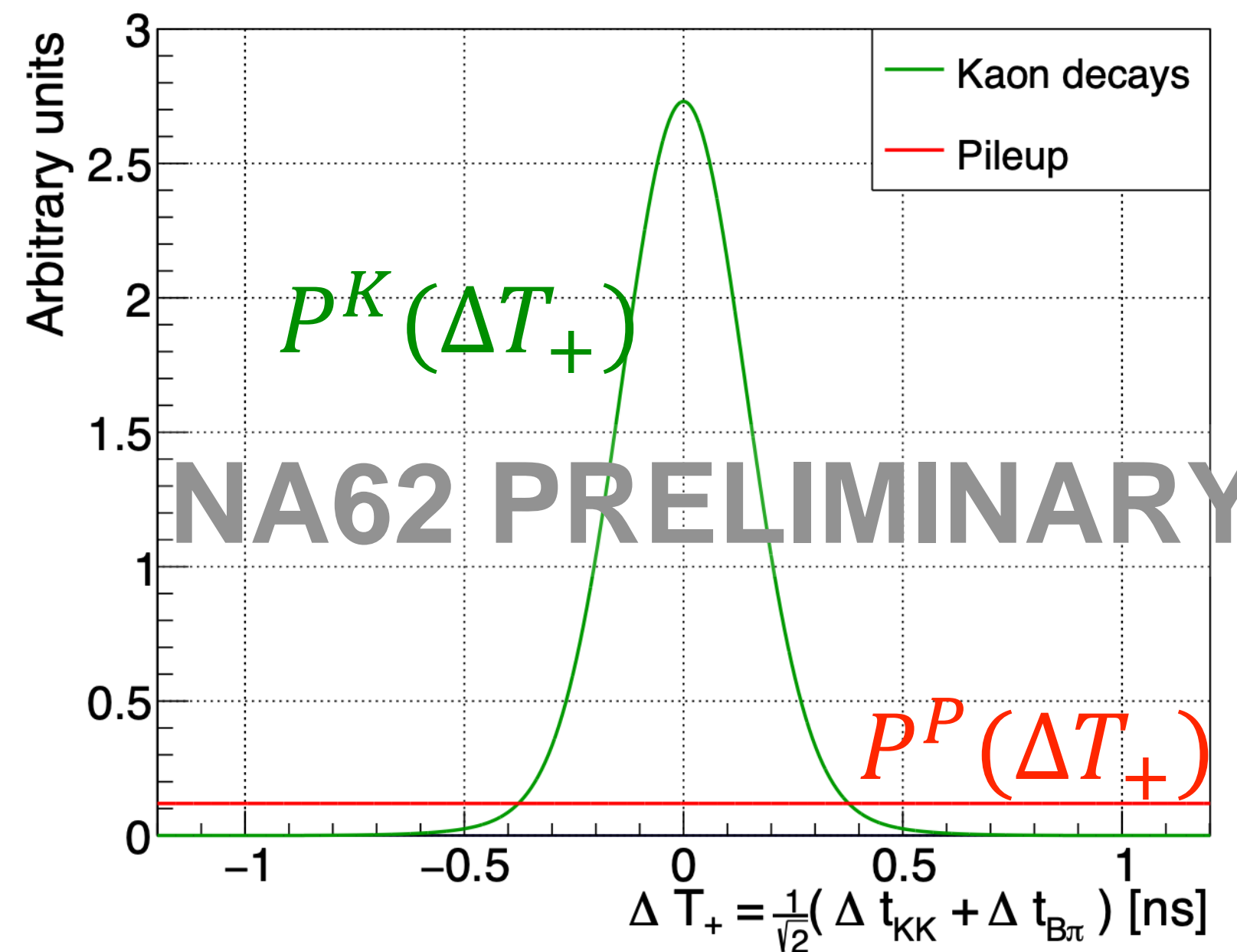
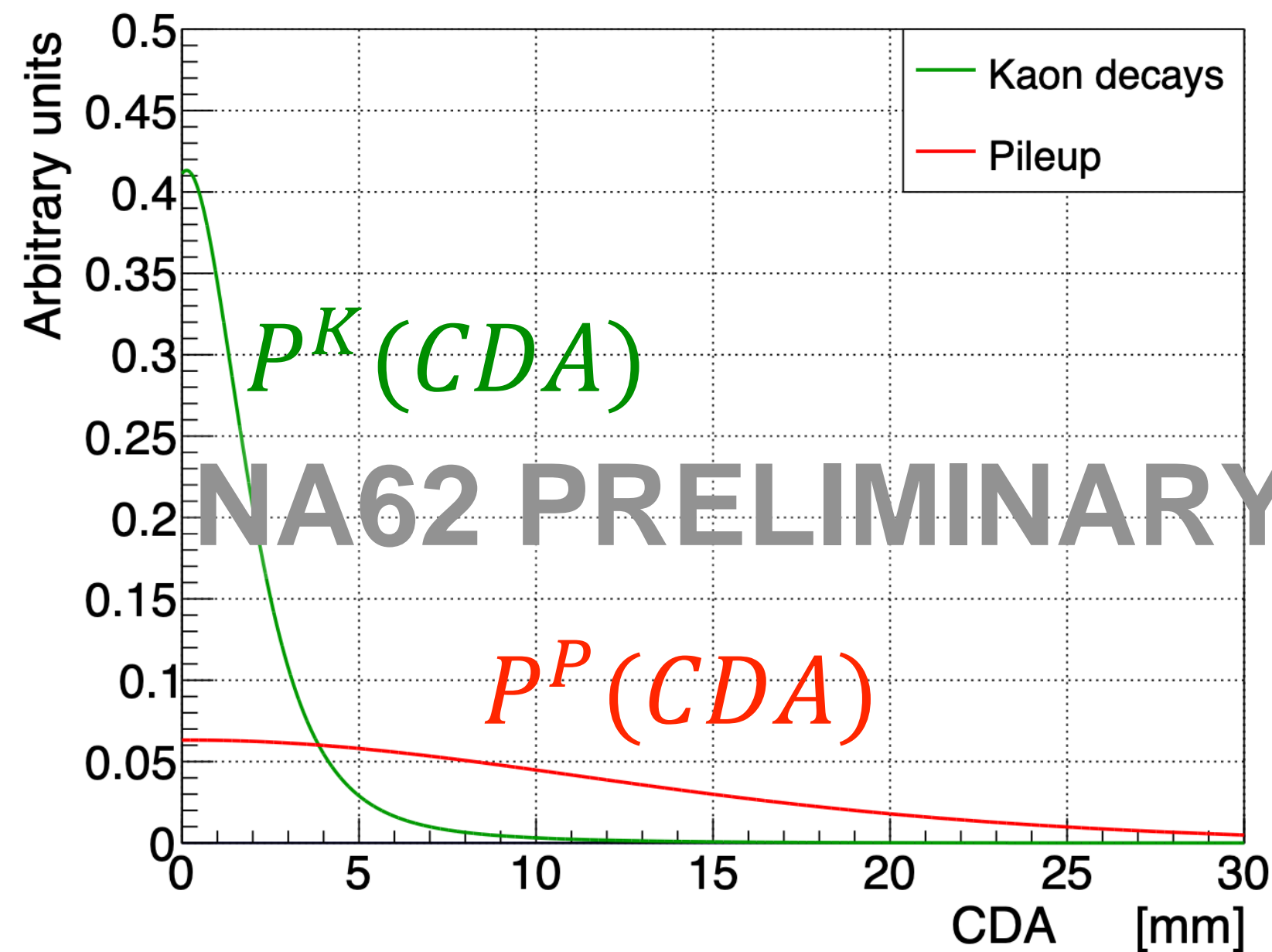
$$\eta_{\pi^0} = (1.72 \pm 0.07) \times 10^{-8}$$

- Combined  $\gamma/\pi^0$  rejection of  $\mathcal{O}(10^8)$ .

# Bayesian classifier for $K^+ - \pi^+$ matching



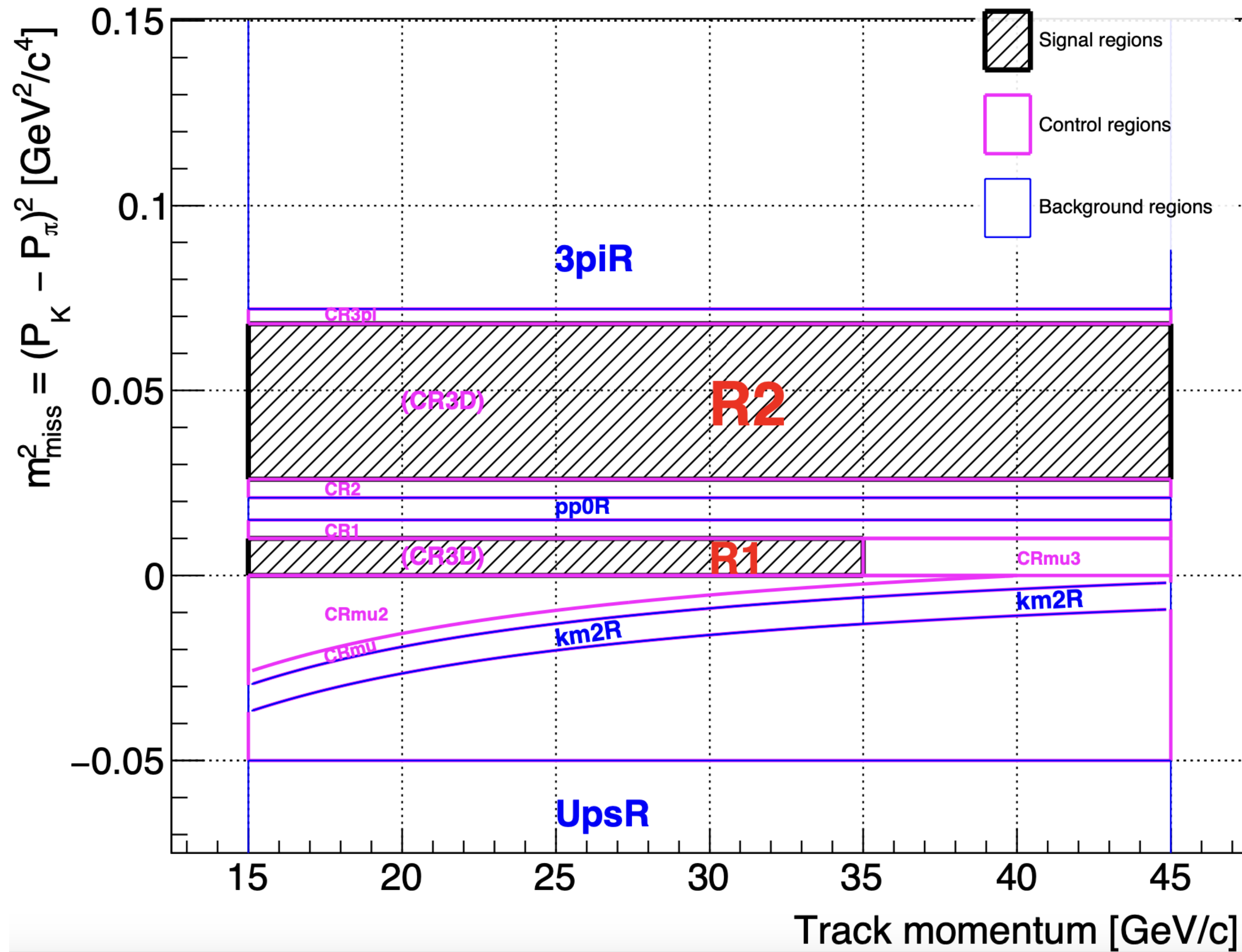
- **Inputs:** spatial (CDA) & time ( $\Delta T_+$ ) matching, intensity/pileup ( $N_{GTK}$ ) [prior]
  - Models for PDFs/Prior from  $K^+ \rightarrow \pi^+ \pi^+ \pi^-$  data.



Example of selection update

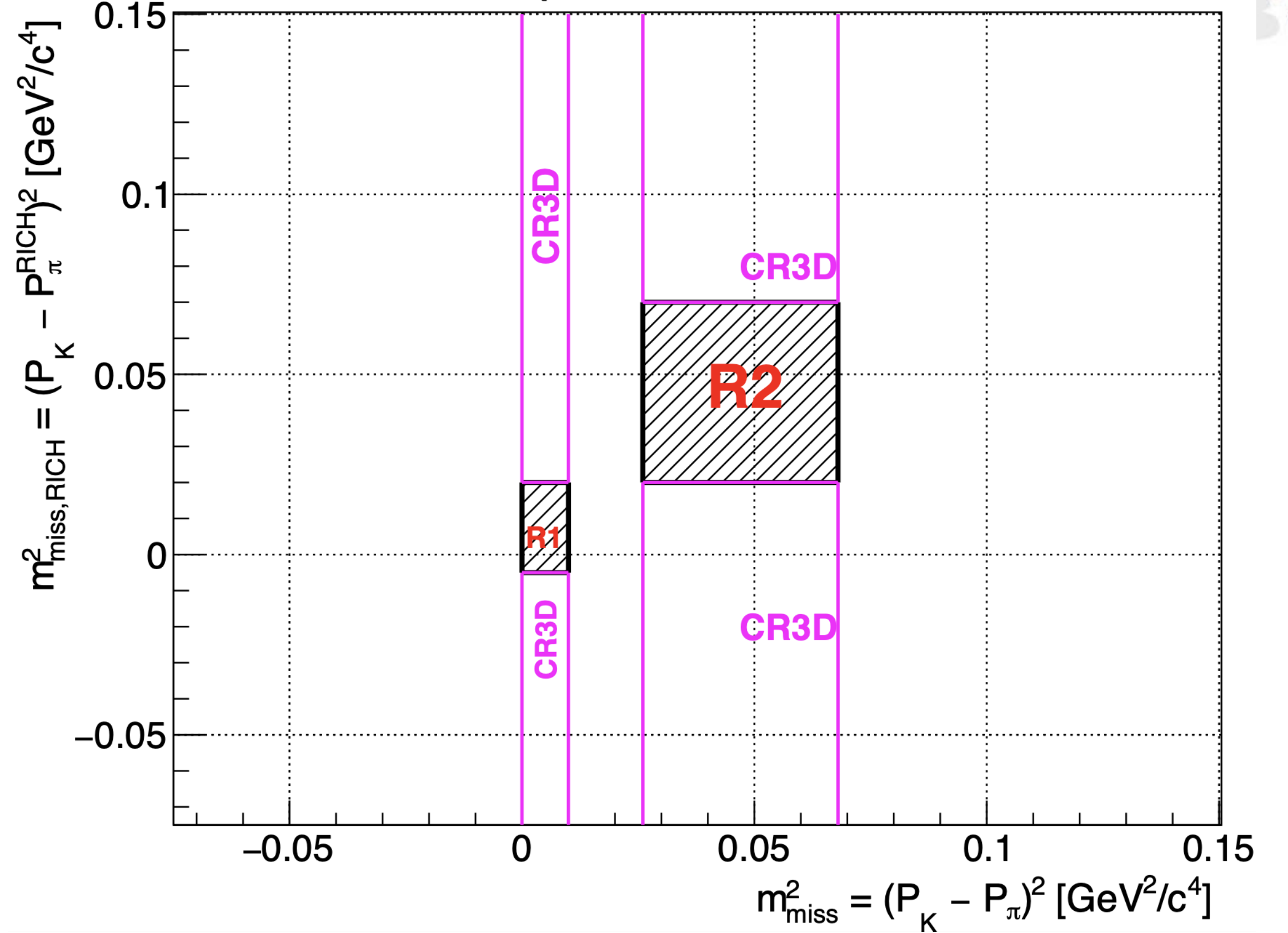
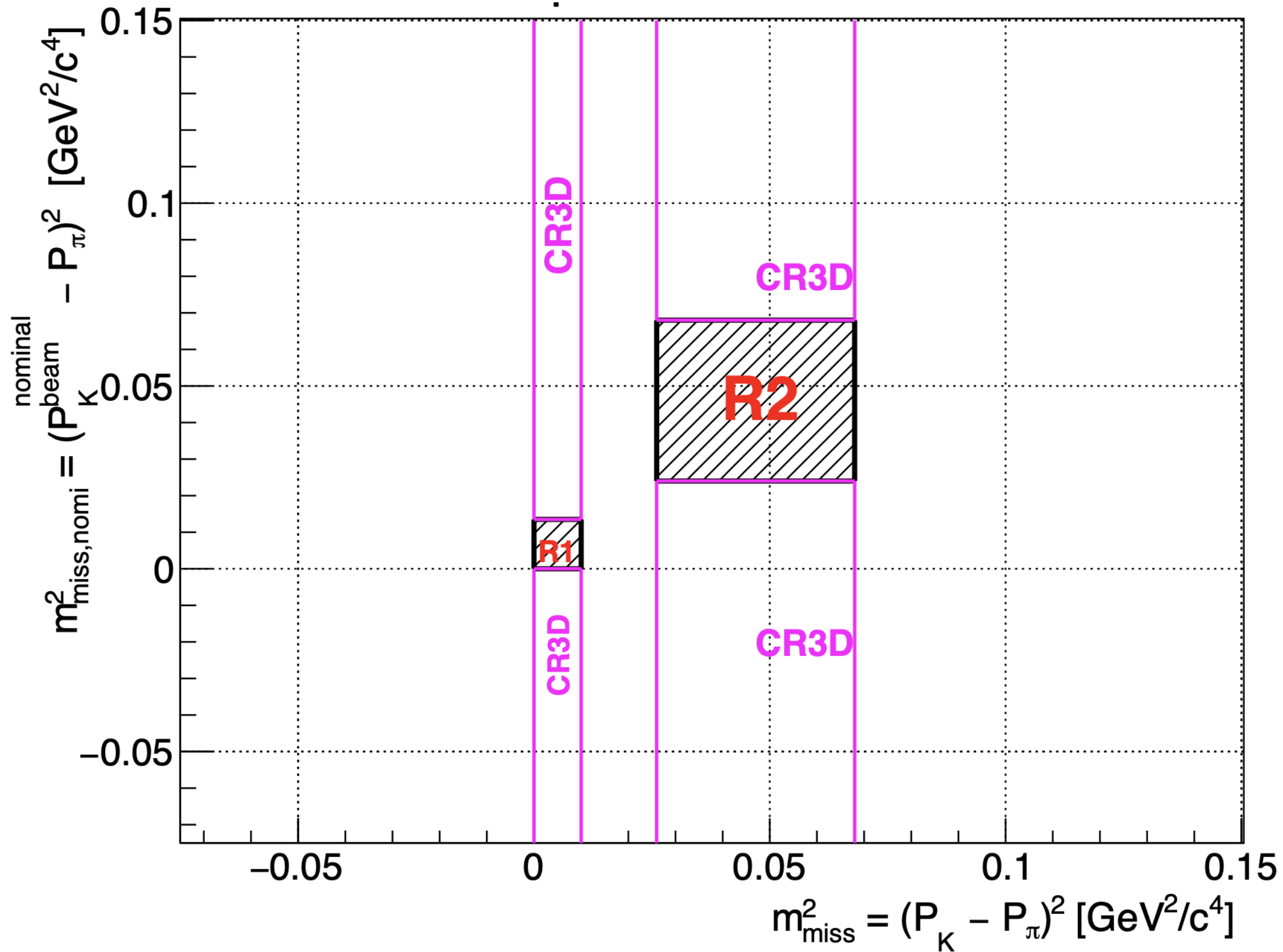
- **Output:** posterior probability of GTK track = true  $K^+$ 
  - Use likelihoods of kaons (K) and pileup (P)
  - Likelihood ratio used to select true match when  $N_{GTK} > 1$
  - Efficiency improved (+10%) and mistagging probability maintained.

# Kinematic regions



- **Signal regions:**
- **Control regions:**
  - Used to validate background predictions.
- **Background regions:**
  - Used as “reference samples” for some background estimates.

# 3D signal regions definition



**CR3D**: control region for events in SR in 2 out of 3 dimensions.

$$m^2_{miss} = (P_K - P_\pi)^2$$

Default: GTK

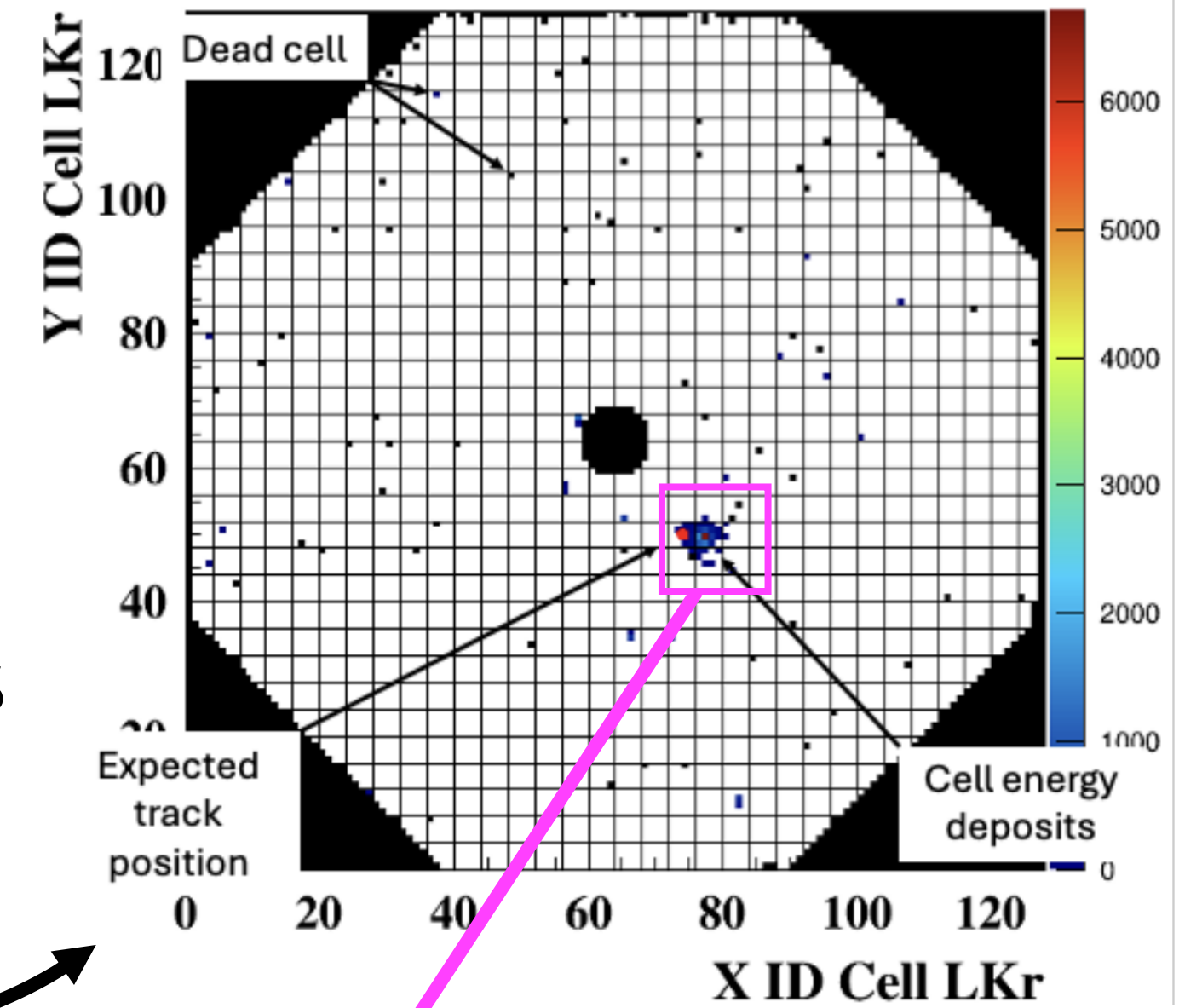
Alternative: Nominal beam =  $m^2_{miss,nom}$

Default: STRAW

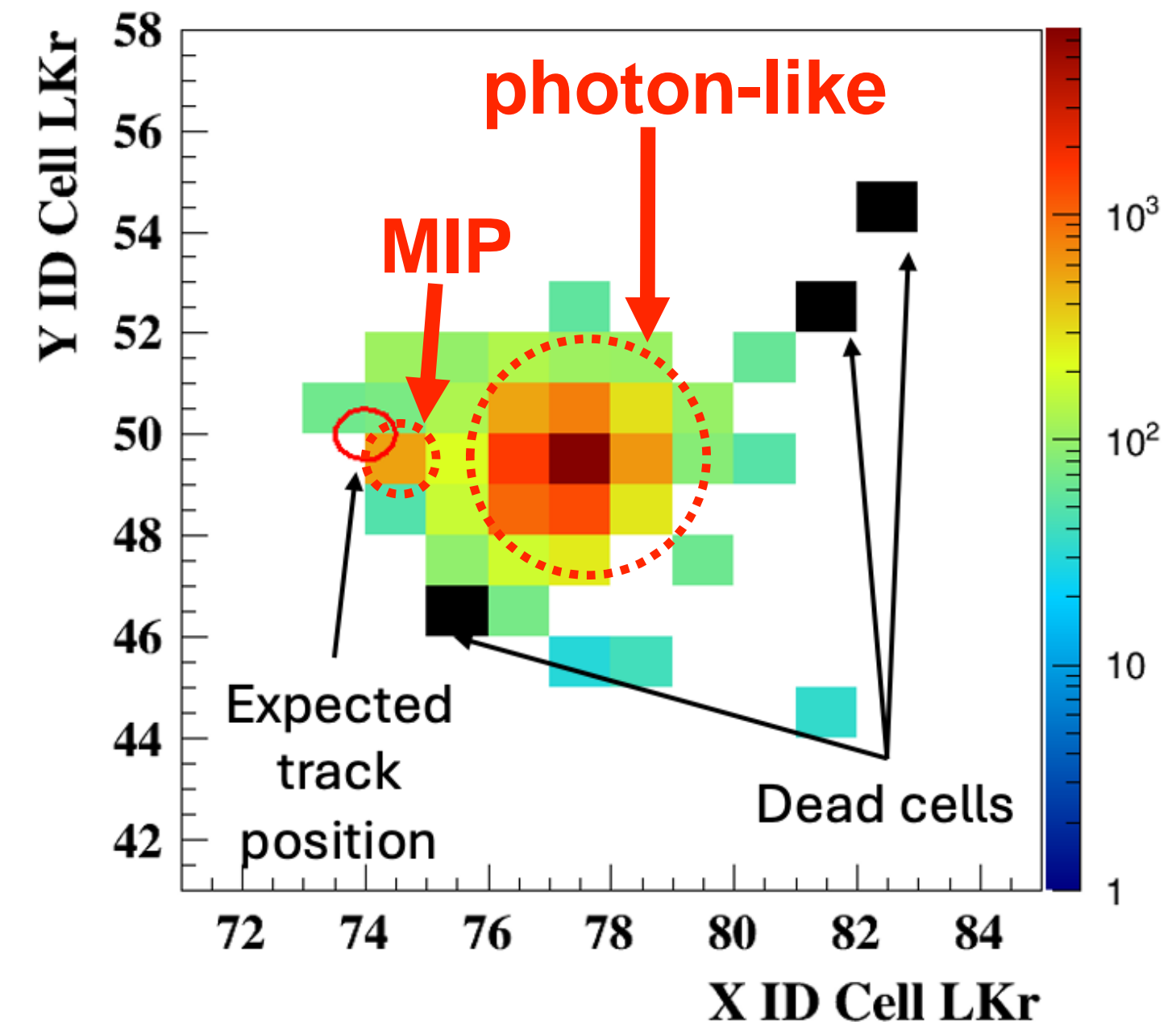
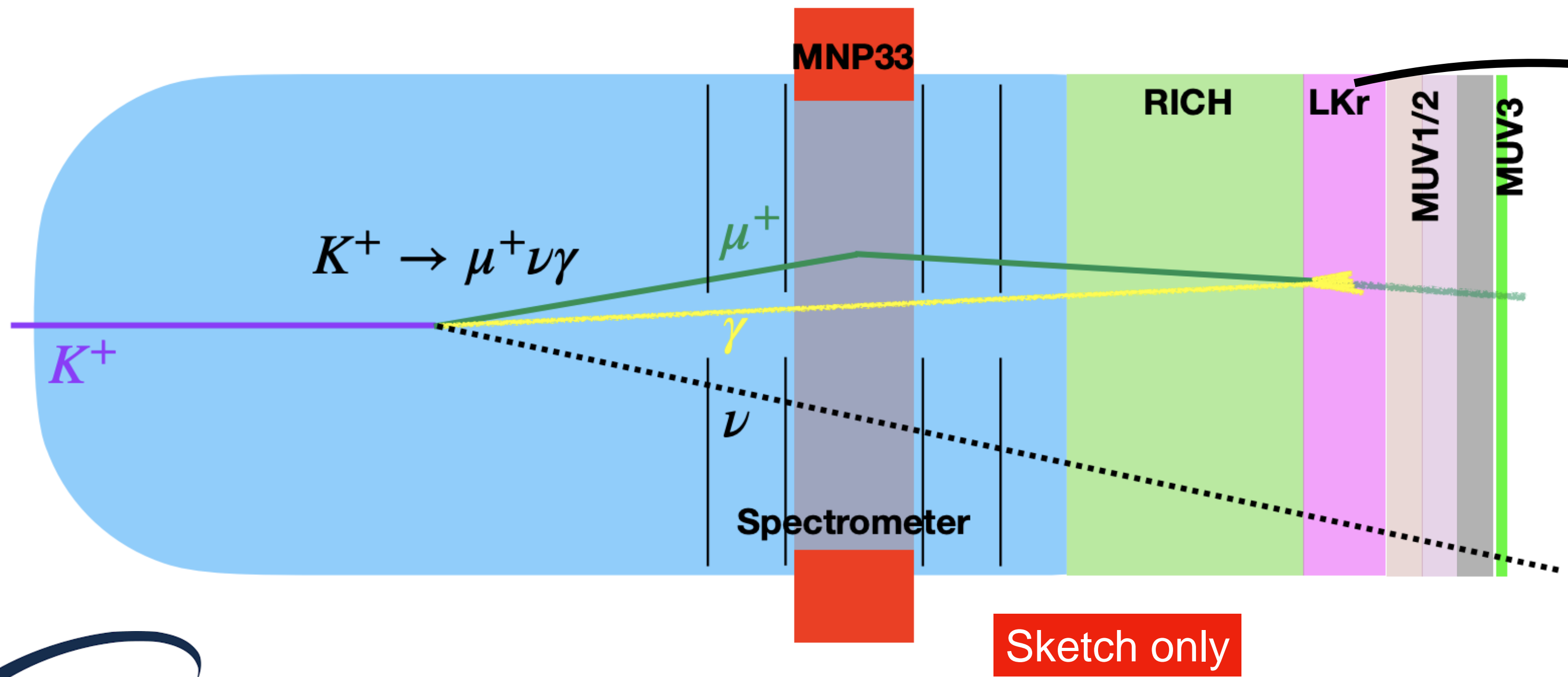
Alternative:  $|p|$  from RICH (use as a velocity spectrometer) =  $m^2_{miss,RICH}$

# Background mechanism: $K^+ \rightarrow \mu^+ \nu \gamma$

Example event (2022 data):



- $K^+ \rightarrow \mu^+ \nu \gamma$  decay with fairly energetic photon ( $E_\gamma > 5 GeV$ ) and high momentum  $\mu^+$  ( $p \gtrsim 35 GeV/c$ ).
- $\gamma$  and  $\mu^+$  hit LKr together and are misidentified as a  $\pi^+$ .
- No rejection power from photon vetos (LKr  $\gamma$  cluster associated to track).
- Additional  $\gamma$  naturally shifts  $m_{miss}^2 = (P_K - P_\pi)^2$  towards higher values (i.e. towards signal regions).



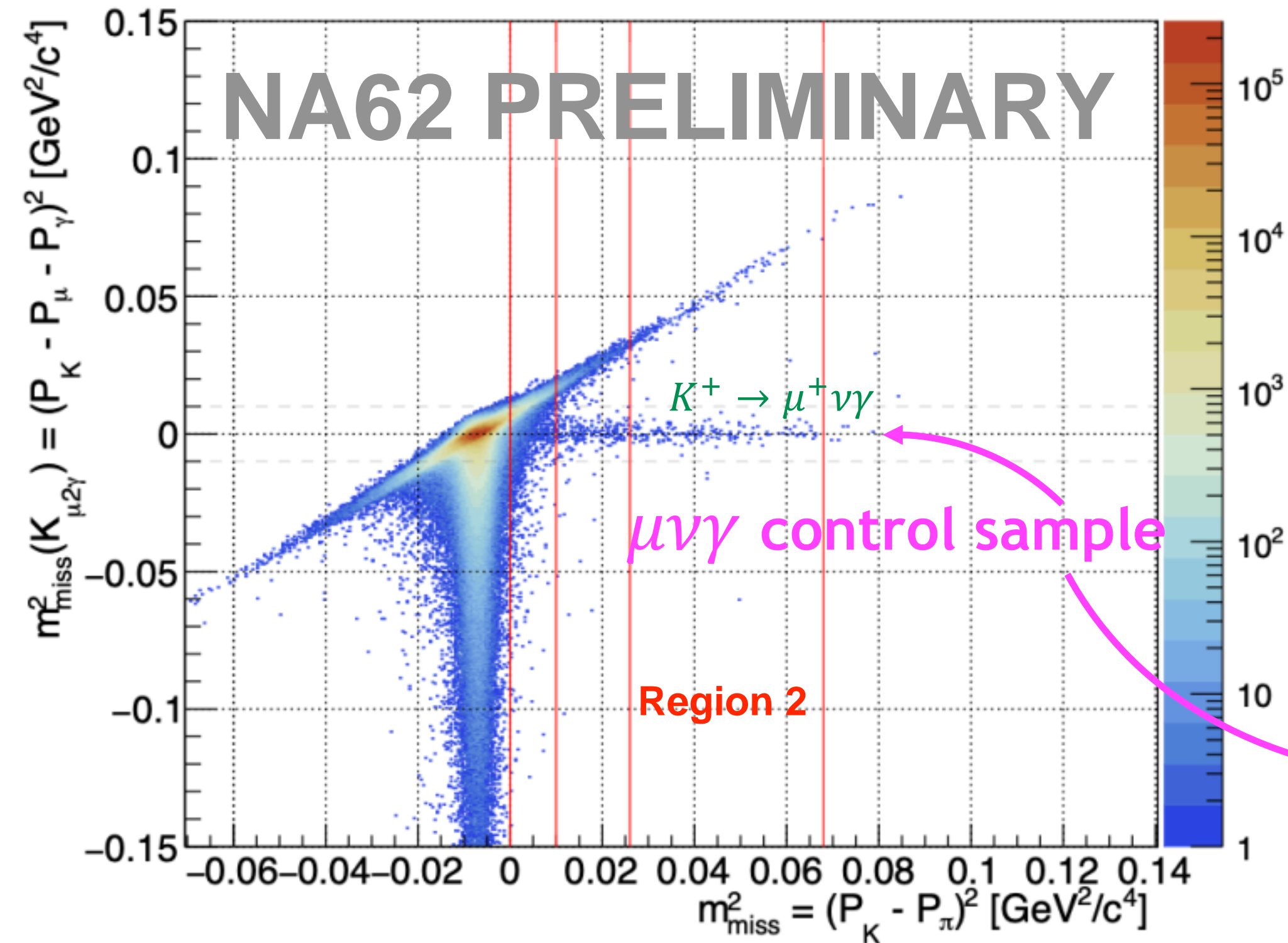


# Background evaluation: $K^+ \rightarrow \mu^+ \nu \gamma$



- Evaluate background expectation using  $\mu\nu\gamma$  control sample from MinimumBias (MB) trigger.
  - Not applying Calorimetric BDT classifier and a signal in MUV3.

Minimum Bias Data



- Kinematically select  $K^+ \rightarrow \mu^+ \nu \gamma$  events:  $m_{miss}^2(K_{\mu 2\gamma}) = (P_K - P_\mu - P_\gamma)^2$ 
  - $P_K$  : 4-momentum of  $K^+$  from GTK (as normal)
  - $P_\mu$  : 4-momentum of track with  $\mu^+$  mass hypothesis.
  - $P_\gamma$  : reconstructed from energy (subtracting MIP energy deposit) and position of LKr cluster (and position of  $K^+ - \mu^+$  vertex).

$$N_{bg}(K^+ \rightarrow \mu^+ \nu \gamma) = N_{\mu\nu\gamma}^{MB} D_{MB} \frac{\epsilon_{signal}}{\epsilon_{MB}} P_{misID}$$

Downscaling of MB trigger

Ratio of  $\pi^+ \nu \bar{\nu}$  and MB trigger efficiencies

probability of  $\gamma + \mu^+$  being misidentified as a  $\pi^+$

Not included in kinematic tails calculation because the tails sample imposes Calorimetric PID= $\mu^+$ , while here there is misID of  $\mu^+ \gamma \Rightarrow \pi^+$ .

# Background rejection: $K^+ \rightarrow \mu^+ \nu \gamma$

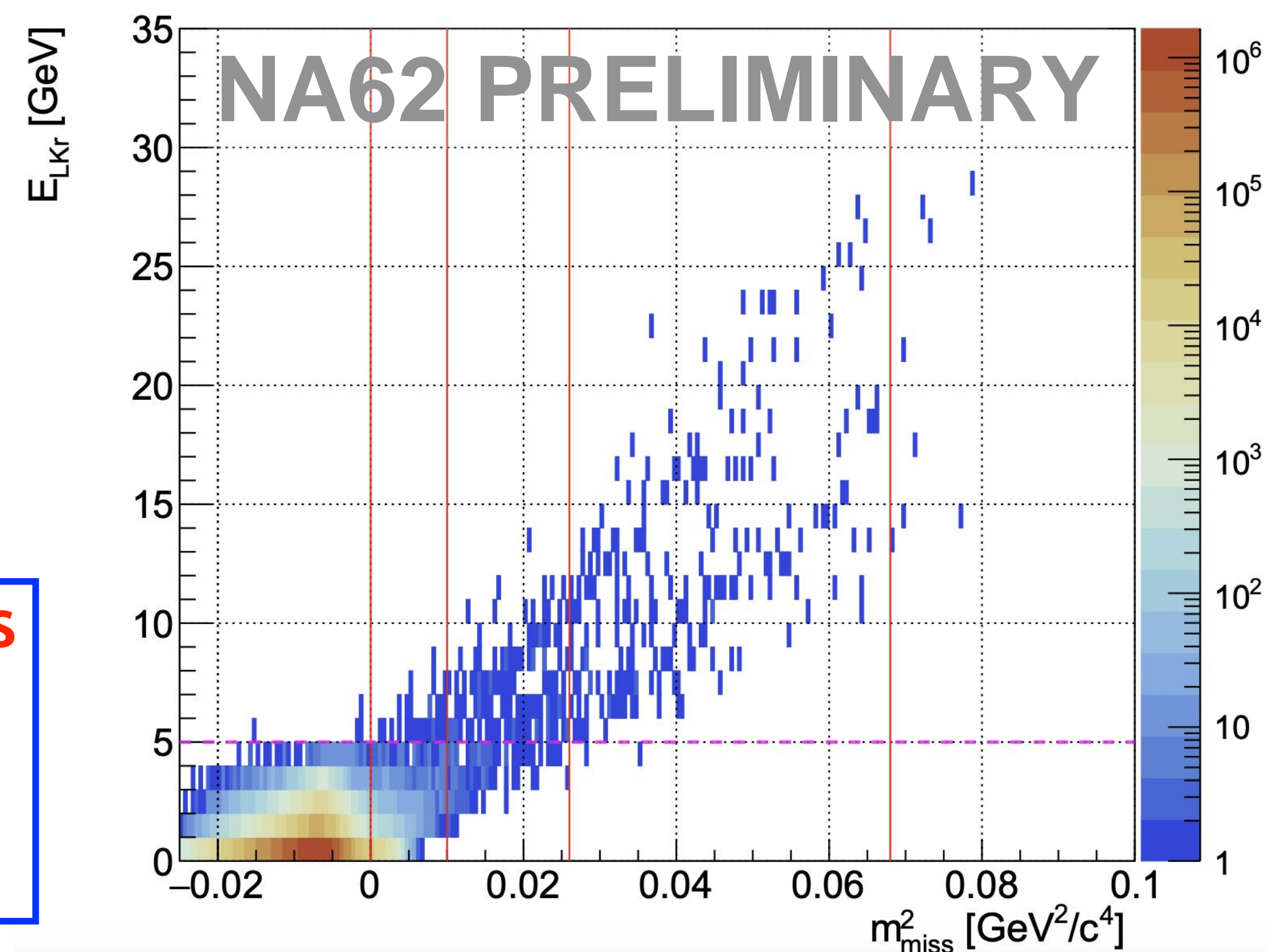
Minimum Bias Data

Events with MUV3 association and  $|m_{miss}^2(K_{\mu 2\gamma})|^2 < 0.01 \text{ GeV}^2/c^4$

veto  $K^+ \rightarrow \mu^+ \nu \gamma$  events with:

- $|m_{miss}^2(K_{\mu 2\gamma})|^2 < 0.01 \text{ GeV}^2/c^4$   $\rightarrow$  c.f. resolution  $\sim 0.0025 \text{ GeV}^2/c^4$
- $E_\gamma > 5 \text{ GeV}$
- $\mu^+$ -like RICH PID.

- Veto conditions established using data control samples and MC.
- $K^+ \rightarrow \mu^+ \nu \gamma$  Veto  $\Rightarrow$  20x background suppression with 0.4% signal loss.



- Why different to 2016–18 analysis?
  - Calorimetric PID degraded:
    - Higher intensity in 2021–22 data (in particular, affects MUV1,2).
    - Training of BDT classifier.

# Upstream background evaluation

$$N_{bg} = \sum_i N_i f_{cda} P_i^{match}$$

$N$   
 $f_{cda}$   
 $P_{match}$

Upstream Reference Sample:  
signal selection but invert CDA cut (CDA > 4mm)

Scaling factor : bad cda  $\rightarrow$  good cda

Probability to pass  $K^+ - \pi^+$  matching

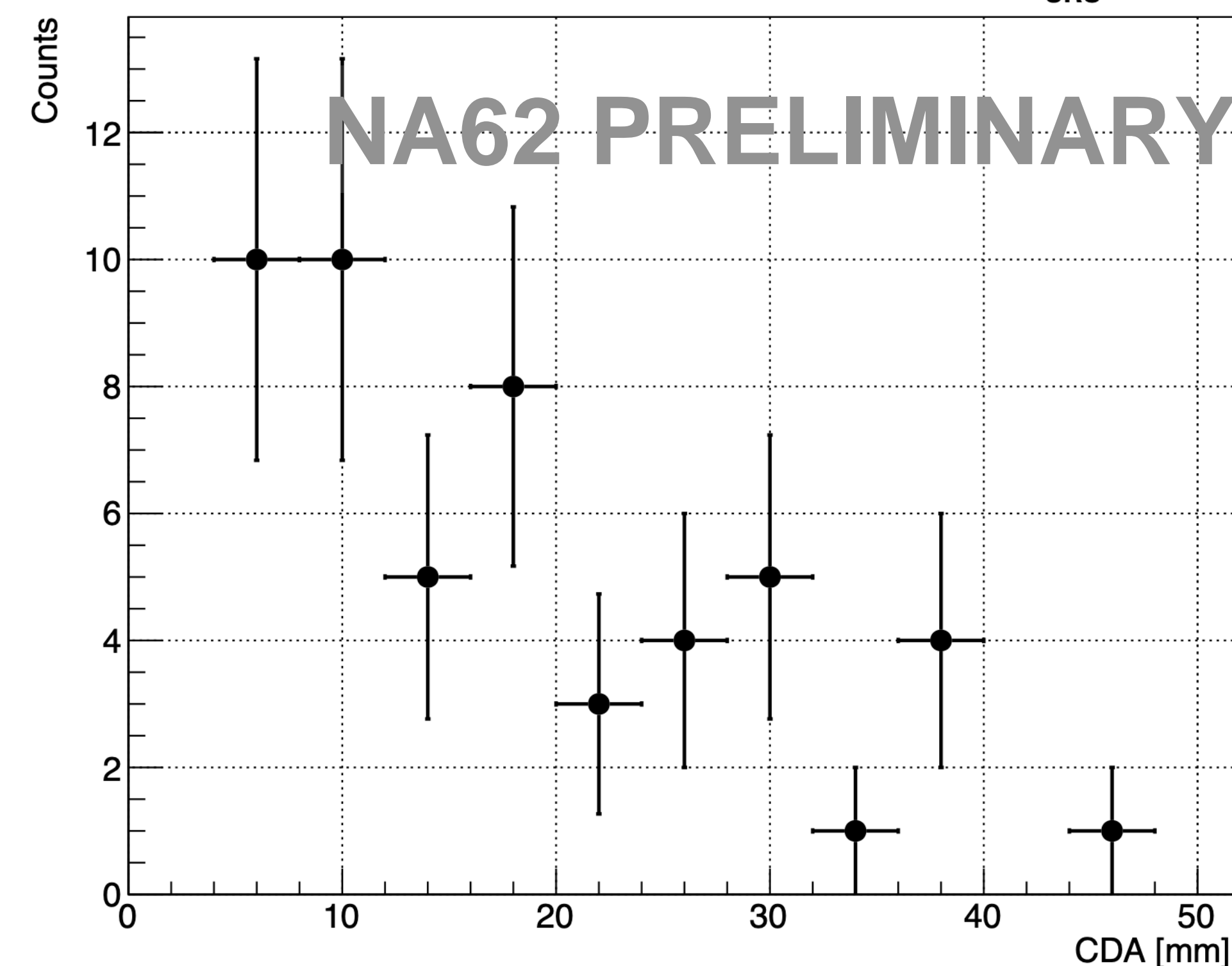
- Upstream reference sample contains all known upstream mechanisms.
  - $N$  provides normalisation.
- $f_{CDA}$  depends only on geometry.
- $P_{match}$  depends on  $(\Delta T_+, N_{GTK})$ .

$N_{URS} = 51$

Calculate using bins (i) of  $(\Delta T_+, N_{GTK})$   
[Updated to fully data-driven procedure]

$$N = 51 \quad f_{CDA} = 0.20 \pm 0.03 \quad \langle P_{match} \rangle = 73\%$$

$$N_{bg}(Upstream) = 7.4^{+2.1}_{-1.8}$$



# Results in context: the long story of $K^+ \rightarrow \pi^+ \nu \bar{\nu}$



- Experimental measurements:
  - Camerini et al. [[PRL 23 \(1969\) 326-329](#)]
  - Klems et al. [[PRD 4 \(1971\) 66-80](#)]
  - Ljung et al. [[PRD 8 \(1973\) 1307-1330](#)]
  - Cable et al. [[PRD 8 \(1973\) 3807-3812](#)]
  - Asano et al. [[PLB 107 \(1981\) 159](#)]
  - E787 :
    - [[PRL 64 \(1990\) 21-24](#)]
    - [[PRL 70 \(1993\) 2521-2524](#)]
    - [[PRL 76 \(1996\) 1421-1424](#)]
    - [[PRL 79 \(1997\) 2204-2207](#)]
    - [[PRL 84 \(2000\) 3768-3770](#)]
    - [[PRL 88 \(2002\) 041803](#)]
  - E949 (+E787)
    - [[PRL 93 \(2004\) 031801](#)]
    - [[PRL 101 \(2008\) 191802](#)]
  - NA62:
    - 2016 data: [[PLB 791 \(2019\) 156](#)]
    - 2016+17 data: [[JHEP 11 \(2020\) 042](#)]
    - 2016–18 data: [[JHEP 06 \(2021\) 093](#)]
    - 2016–22 data : this result.
- Theory:
  - [[Phys.Rev. 163 \(1967\) 1430-1440](#)]
  - [[PRD 10 \(1974\) 897](#)]
  - [[Prog.Theor.Phys. 65 \(1981\)](#)]
  - [[PLB 133 \(1983\) 443-448](#)]
  - [[PLB 192 \(1987\) 201-206](#)]
  - [[Nucl.Phys.B 304 \(1988\) 205-235](#)]
  - [[PRD 54 \(1996\) 6782-6789](#)]
  - [[PRD 76 \(2007\) 034017](#)]
  - [[PRD 78 \(2008\) 034006](#)]
  - [[PRD 83 \(2011\) 034030](#)]
  - [[JHEP 11 \(2015\) 033](#)]
  - [[JHEP 09 \(2022\) 148](#)]

