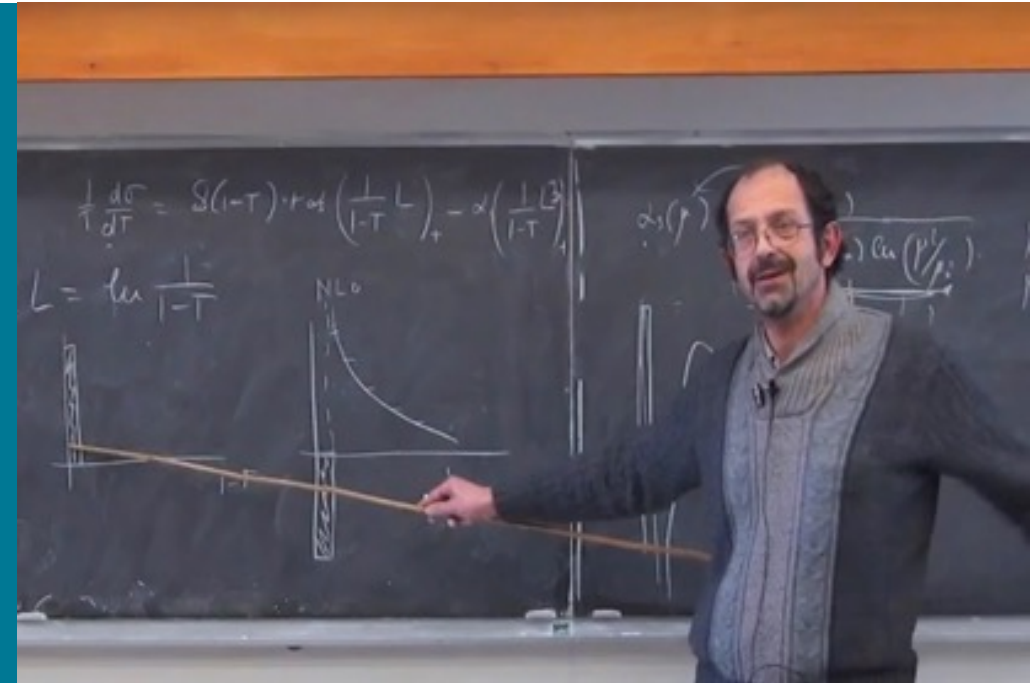


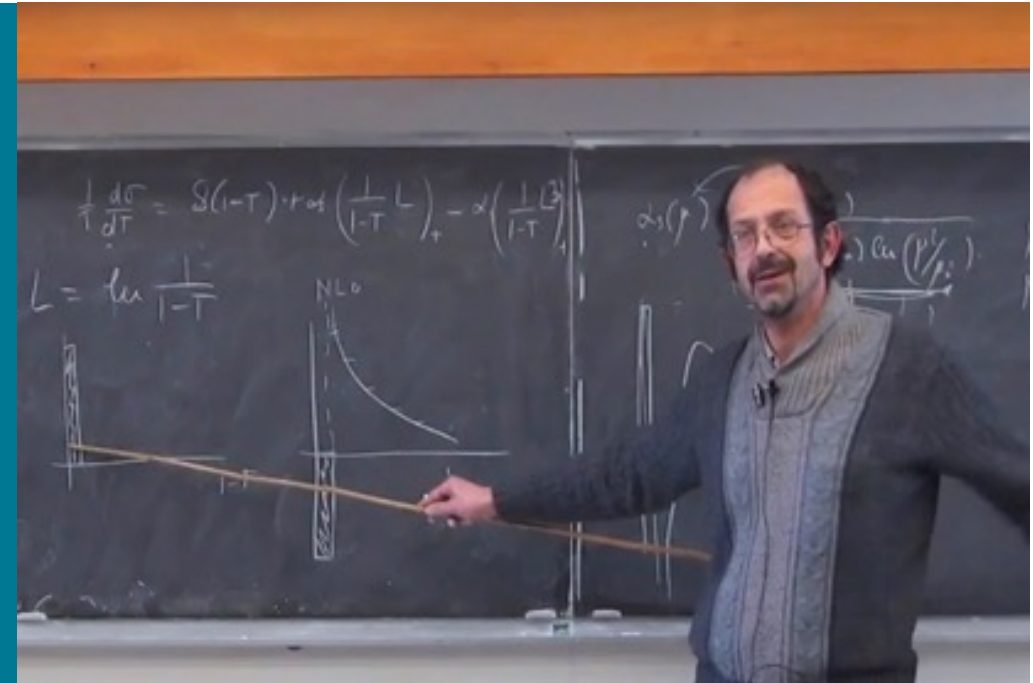
Precision is important

Prof. Dr. Günther Dissertori
ETH Zurich

9 January 2025, S. Catani Memorial Symposium
Firenze



Precision of measurements and Accuracy of theoretical predictions are important

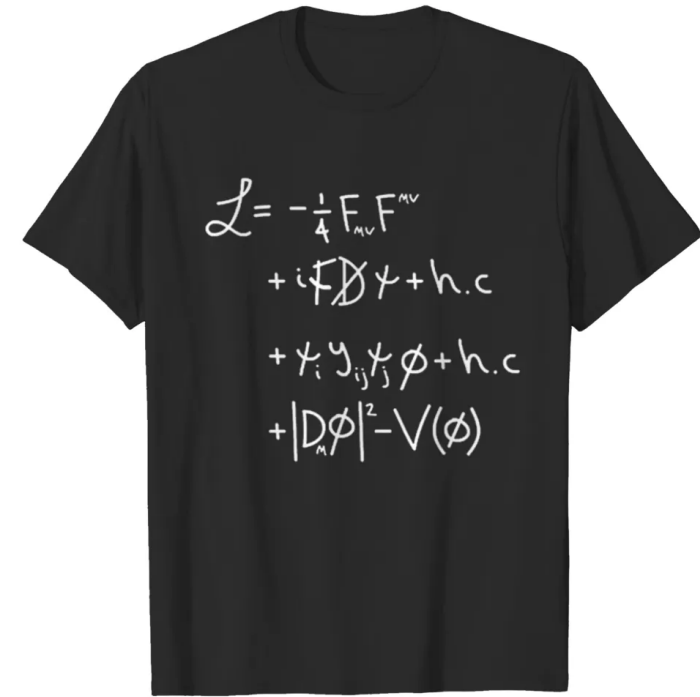
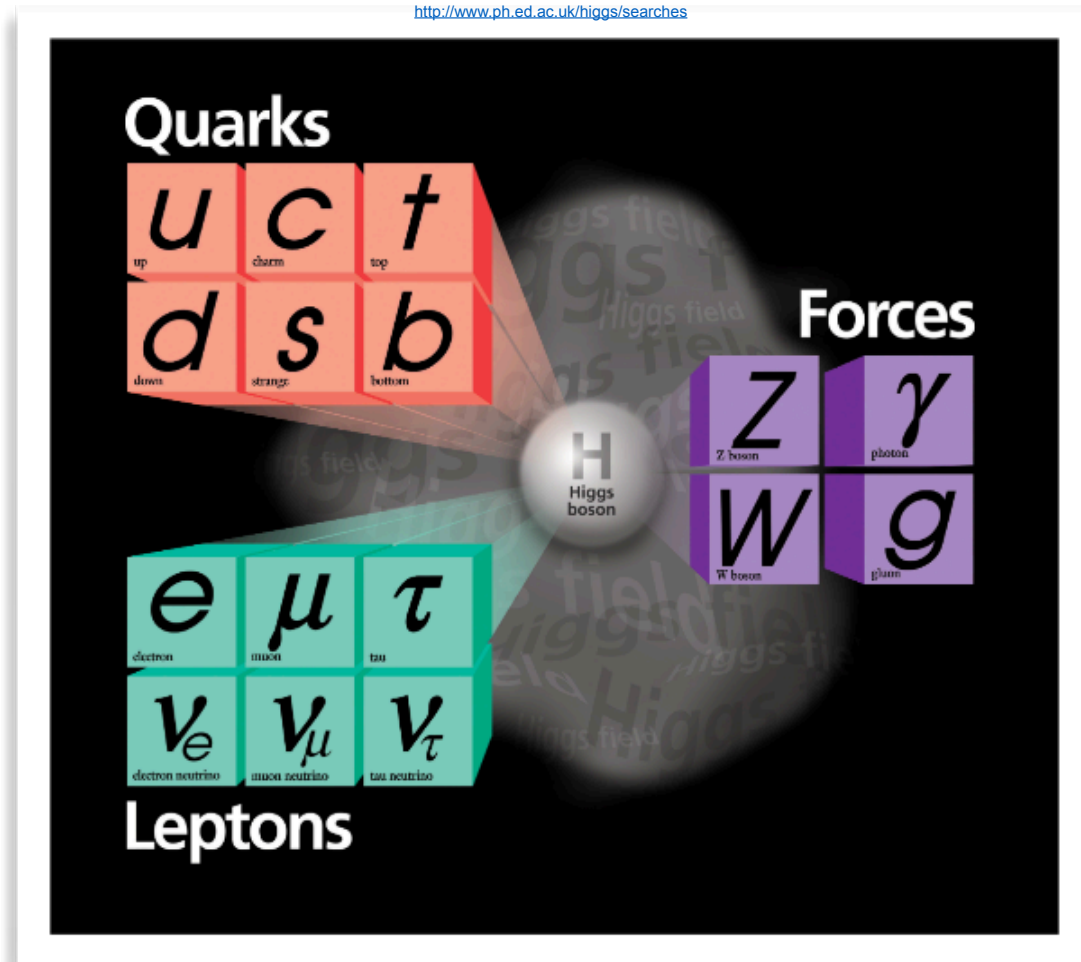


Some preliminary remarks

The state of the nation

The Standard Model of Particle Physics

<http://www.ph.ed.ac.uk/higgs/searches>



A renormalizable **Quantum Field Theory**,
built on the powerful principle of **gauge theories**,
with great predictive power

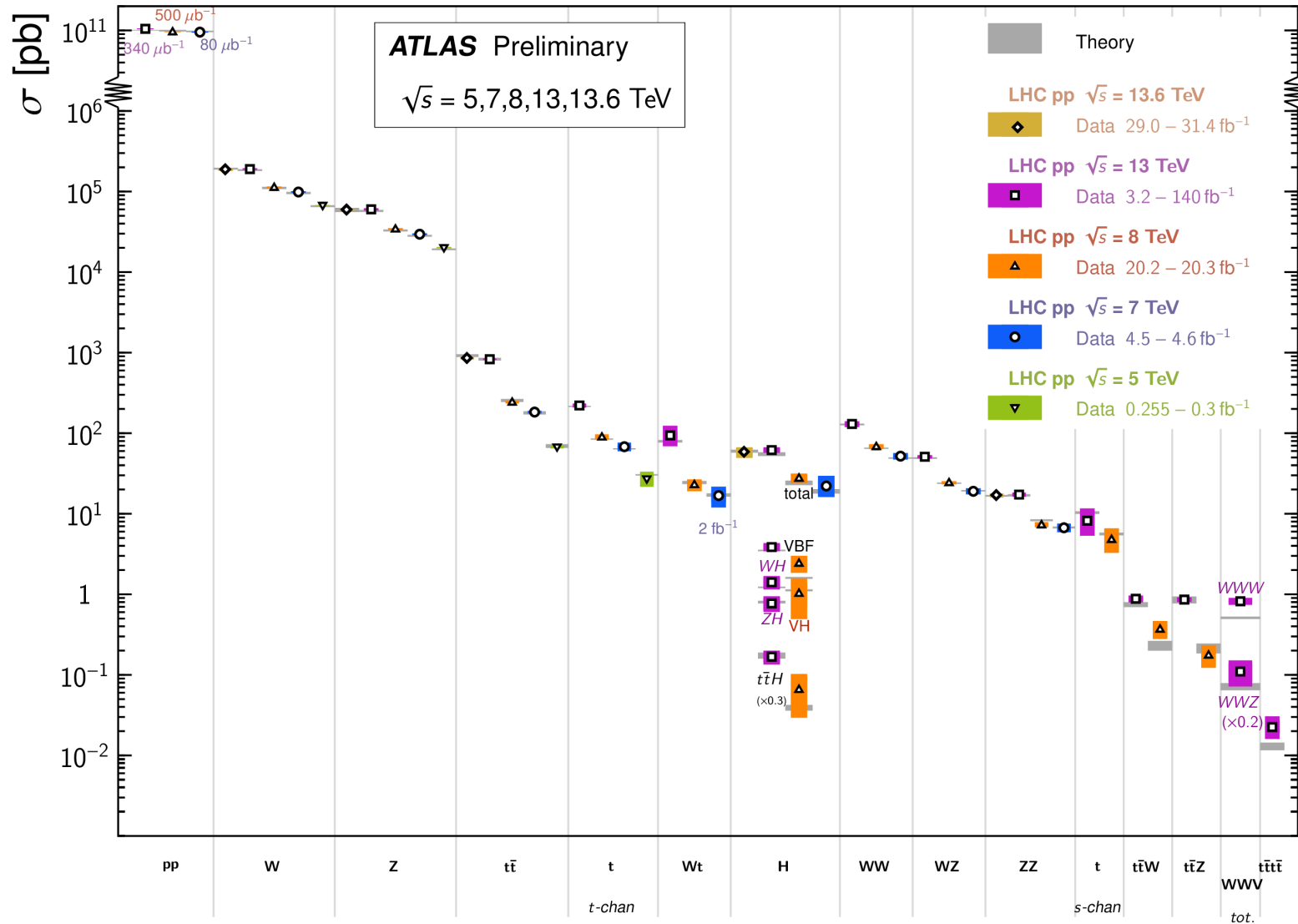
“It works”

as shown, eg. by the results from the first decade
of the LHC

The SM: Tested to greatest precision (EW sector)

Standard Model Total Production Cross Section Measurements

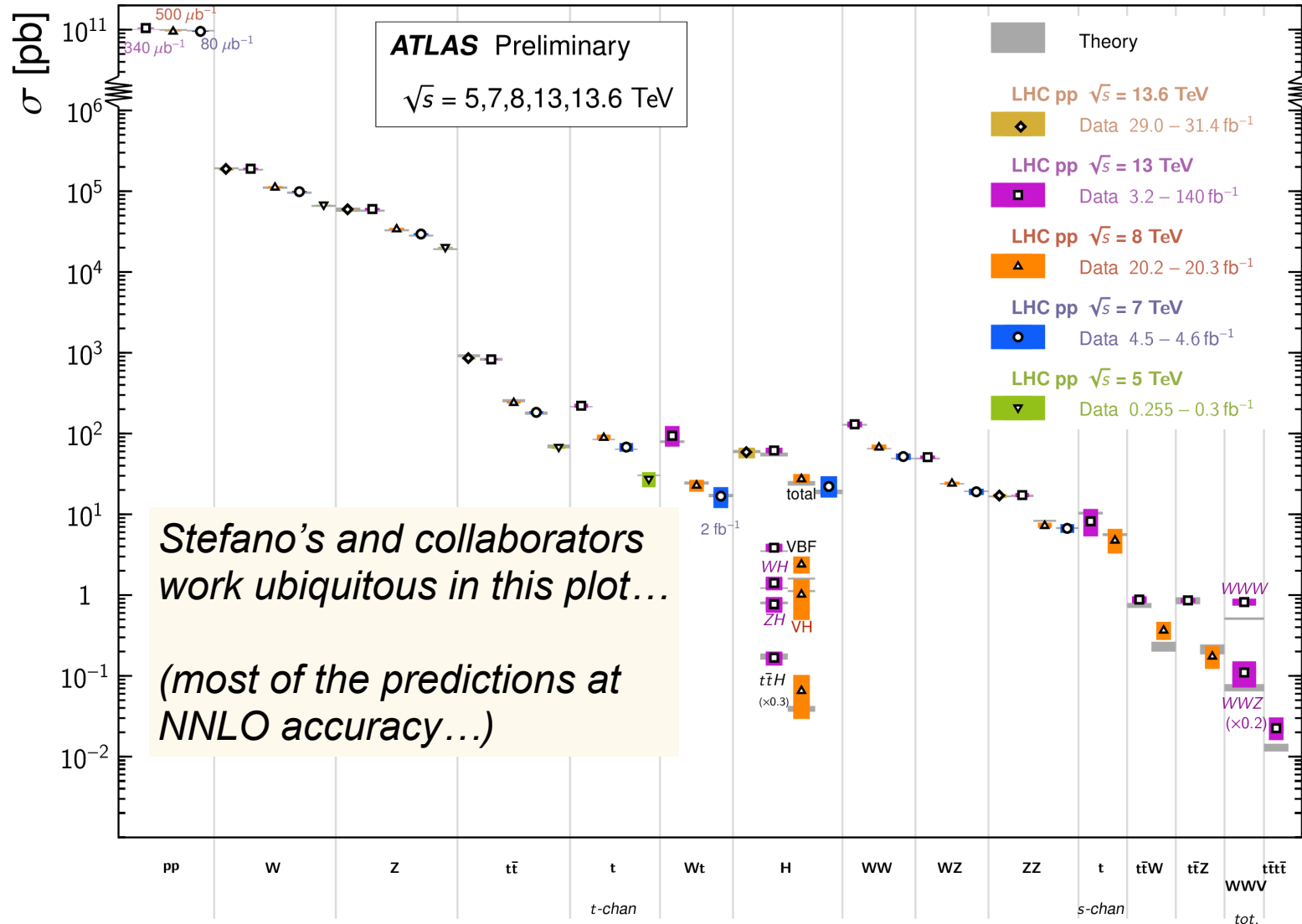
Status: June 2024



The SM: Tested to greatest precision (EW sector)

Standard Model Total Production Cross Section Measurements

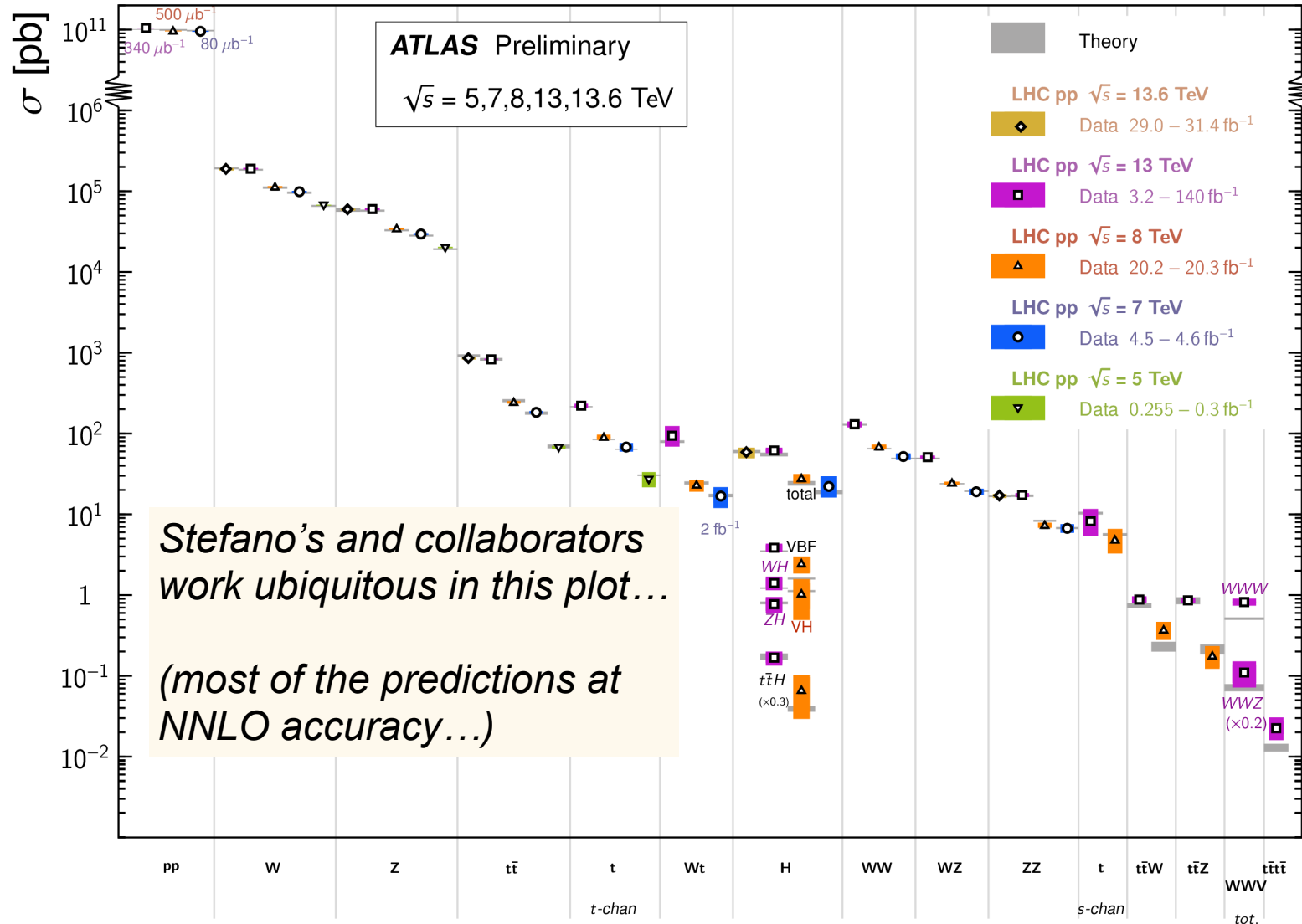
Status: June 2024



The SM: Tested to greatest precision (EW sector)

Standard Model Total Production Cross Section Measurements

Status: June 2024



CMS Preliminary

LEP combination

Phys. Rep. 532 (2013) 119

D0

PRL 108 (2012) 151804

CDF

Science 376 (2022) 6589

LHCb

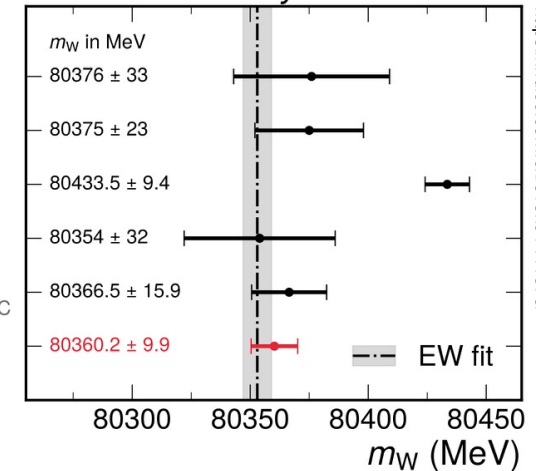
JHEP 01 (2022) 036

ATLAS

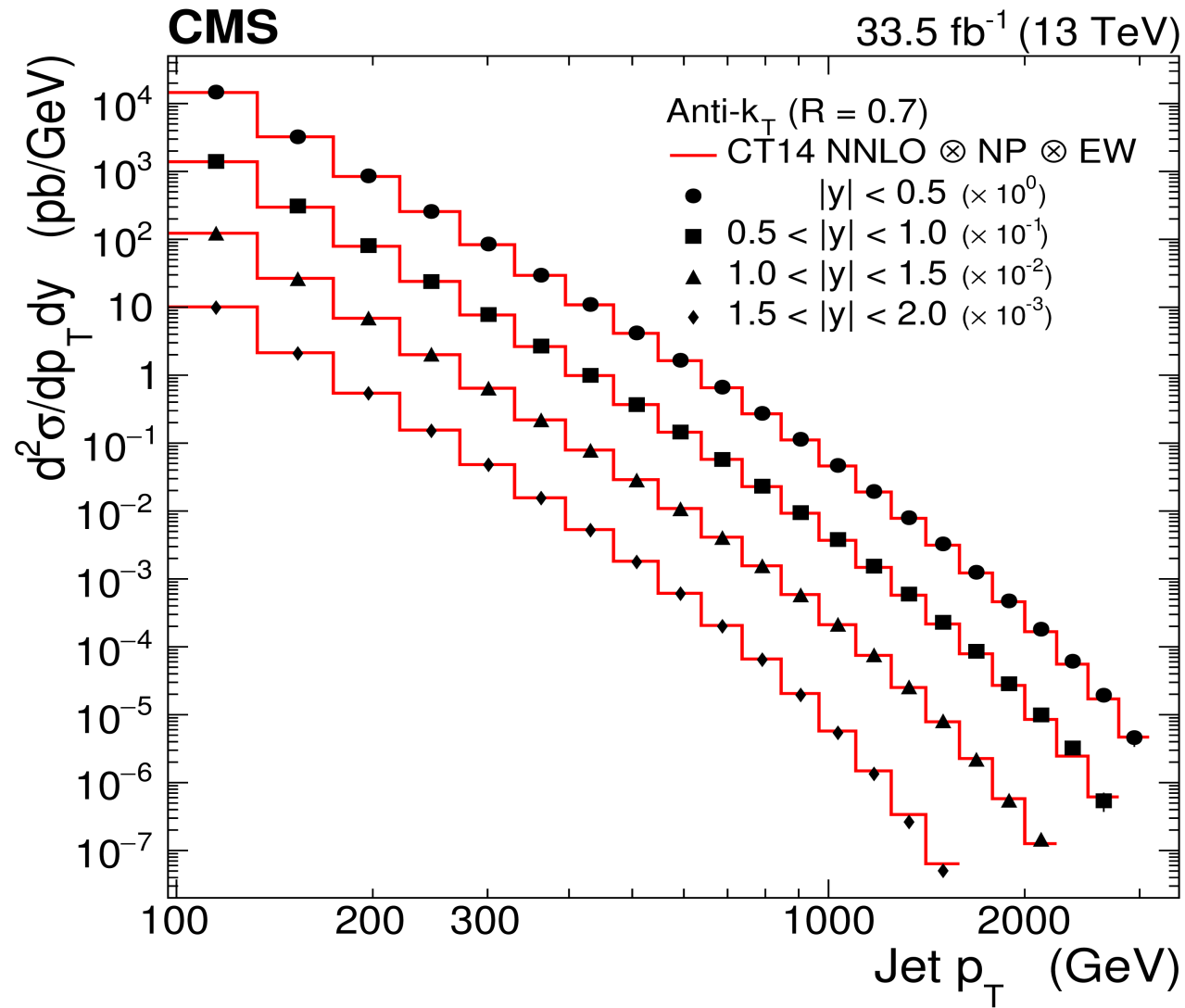
arxiv:2403.15085, subm. to EPJC

CMS

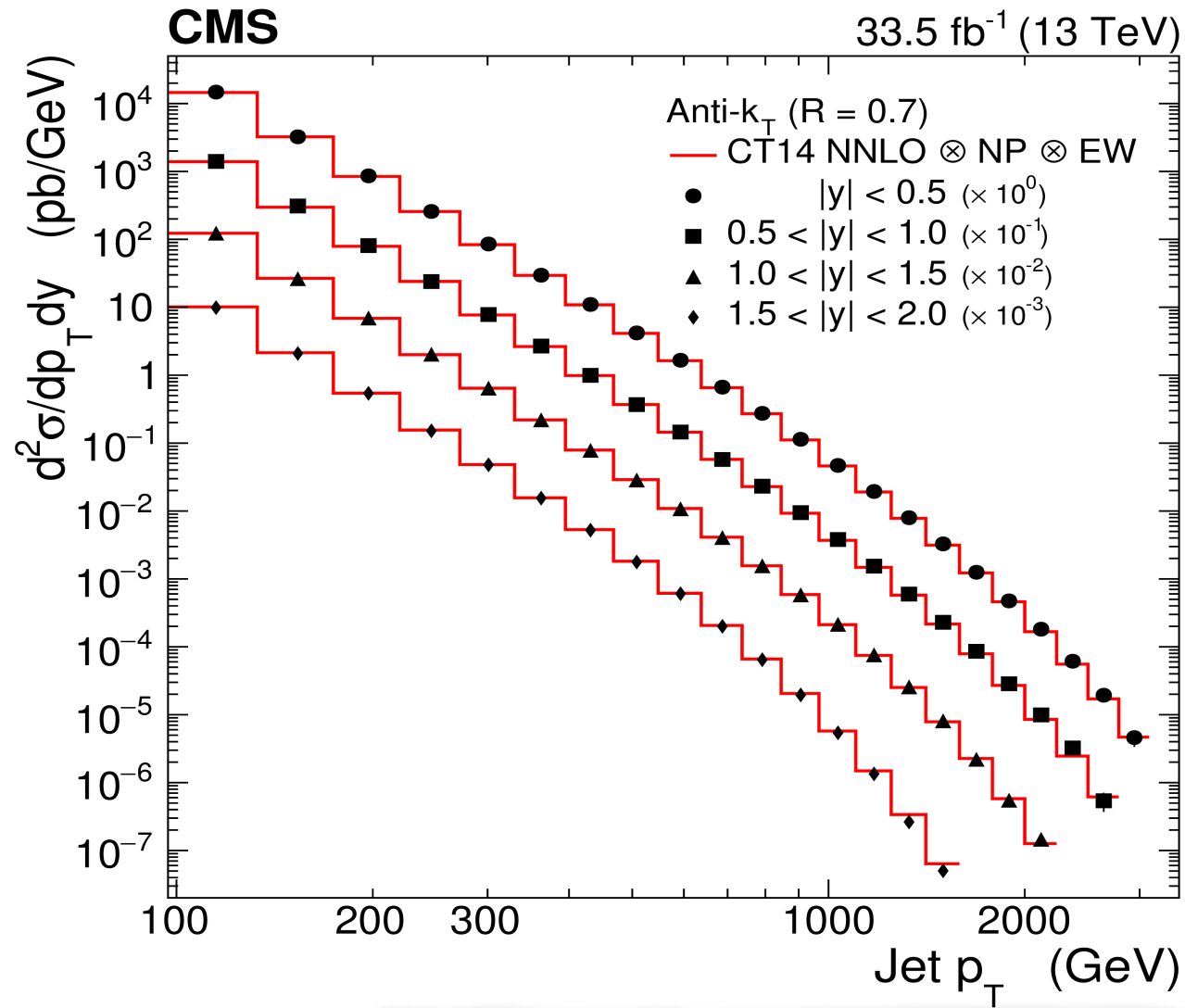
This Work



The SM: Tested to greatest precision (QCD sector)

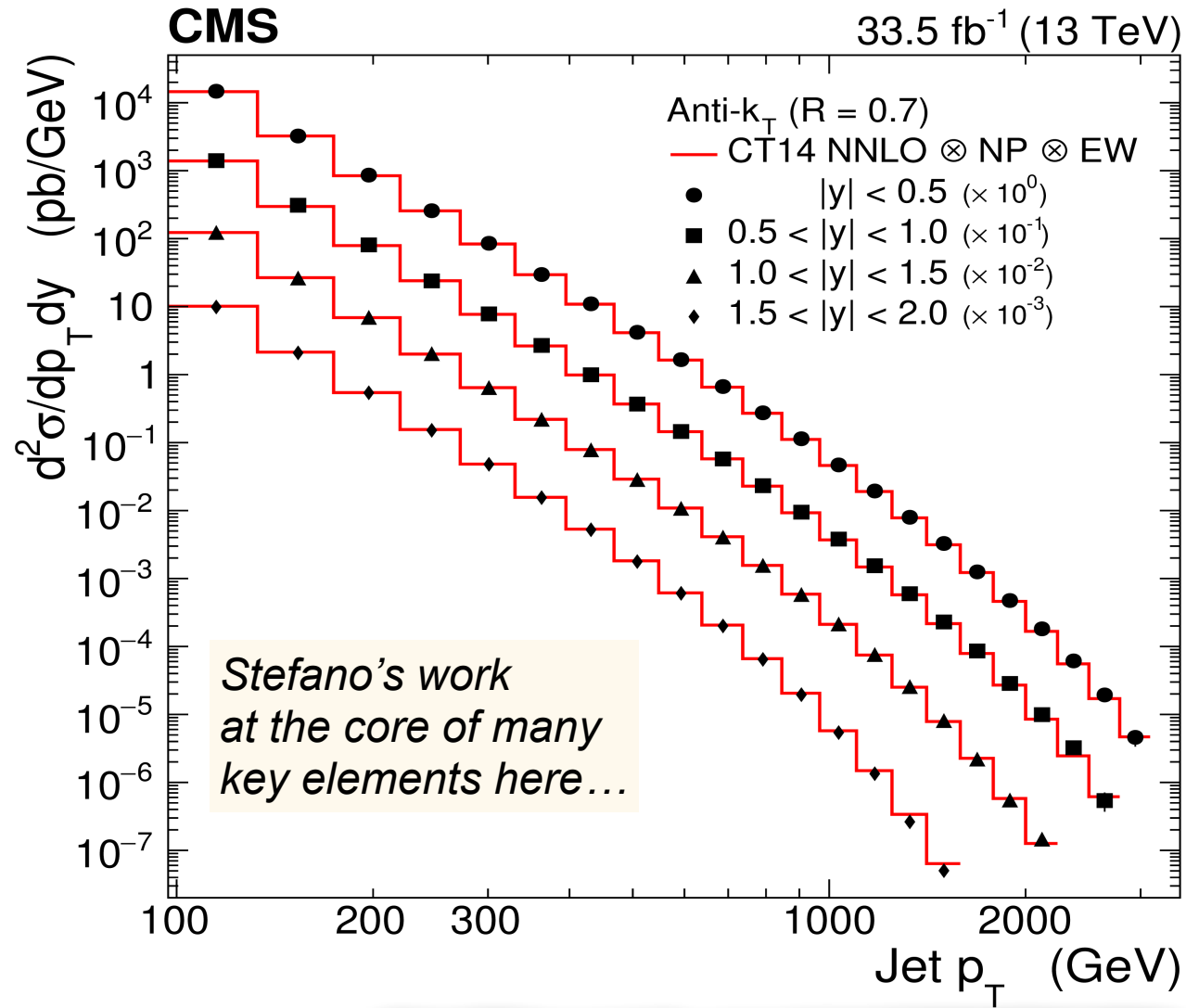


The SM: Tested to greatest precision (QCD sector)



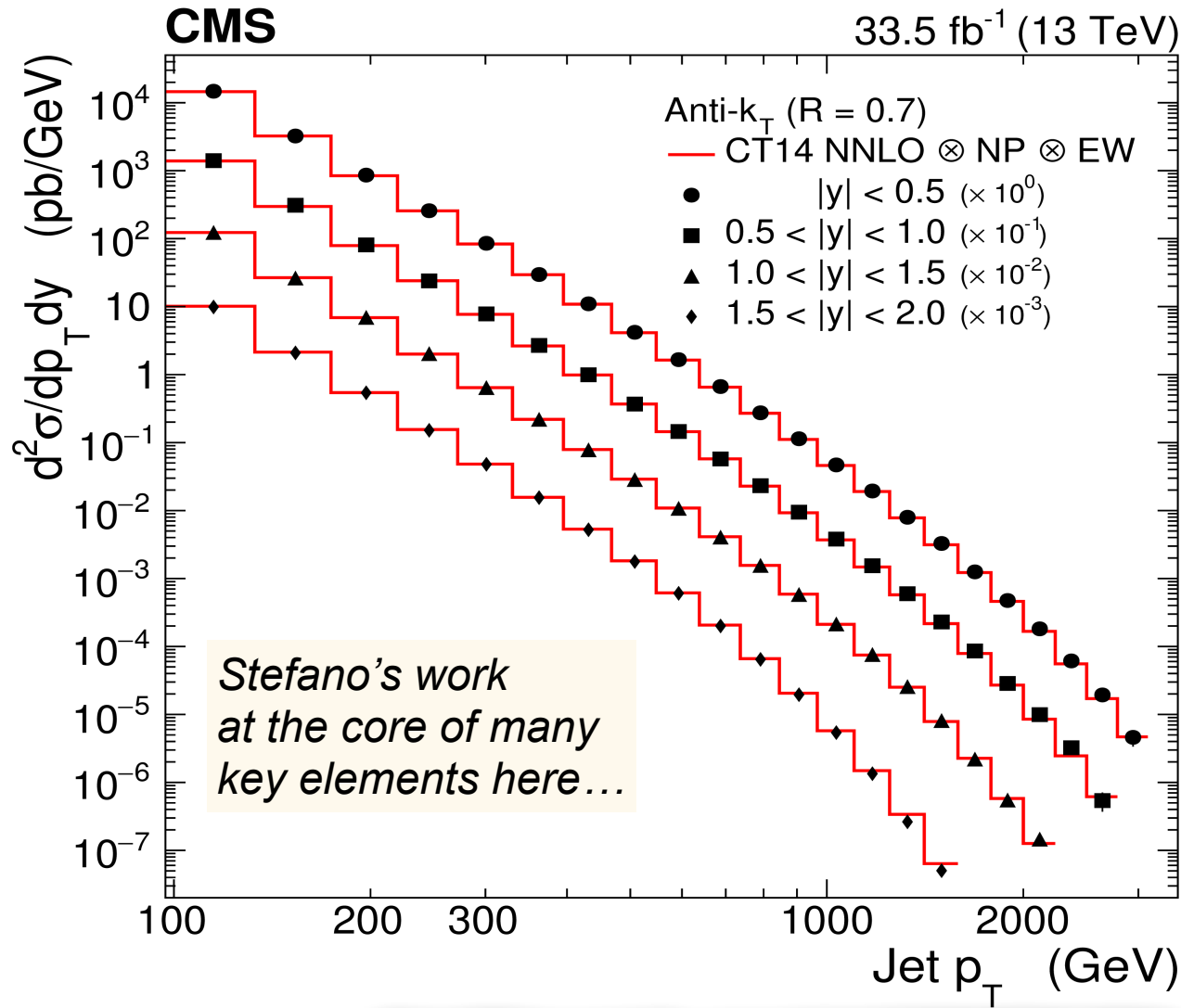
probing distance scales of 10^{-19} m !

The SM: Tested to greatest precision (QCD sector)



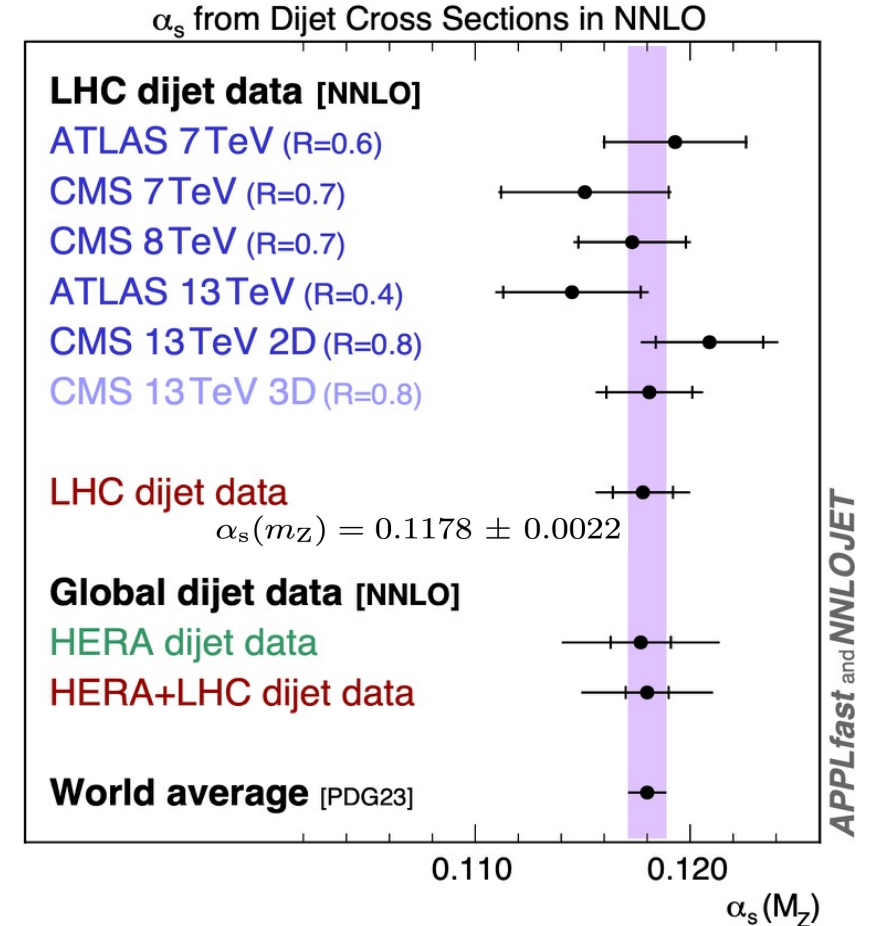
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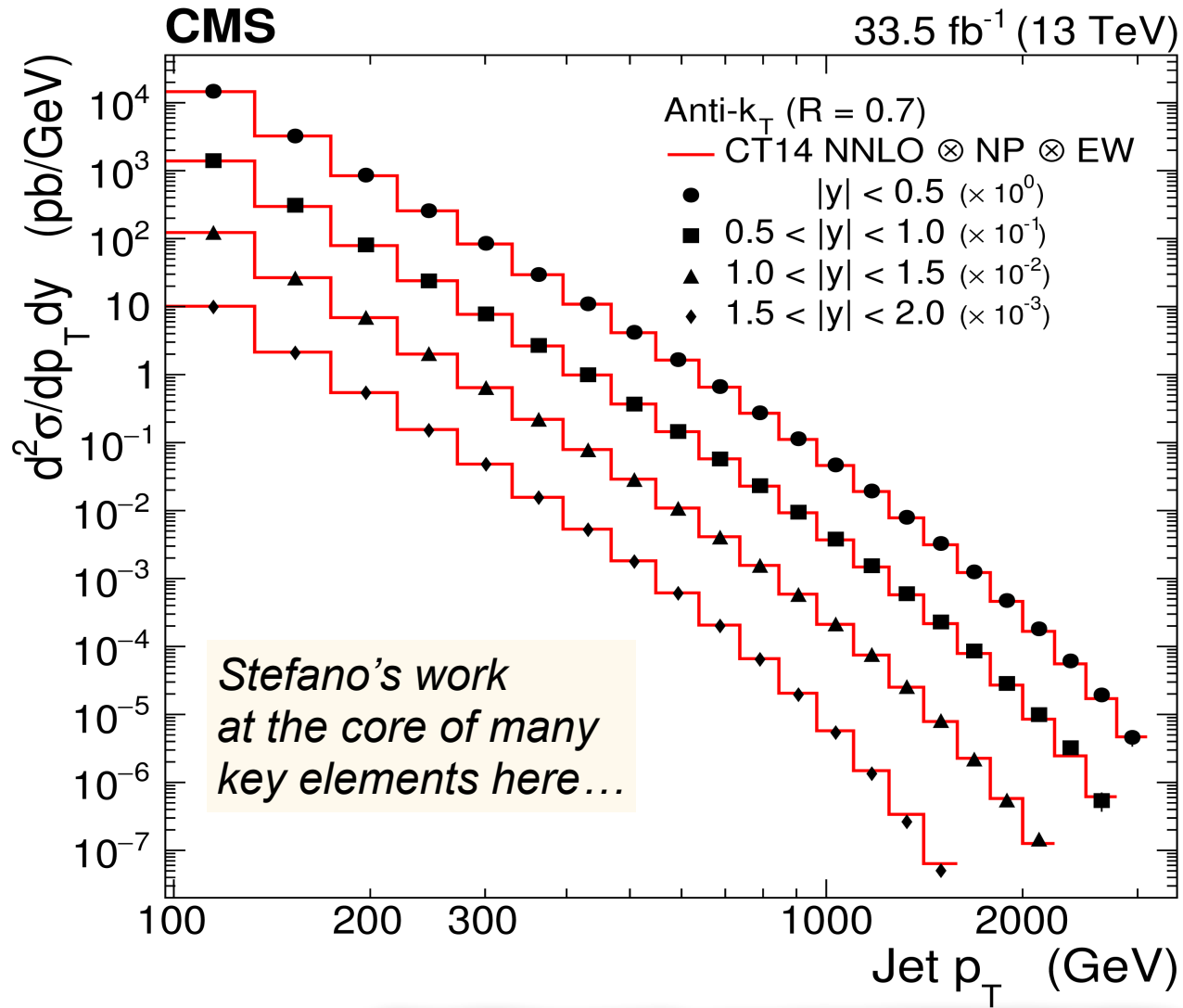


probing distance scales of 10^{-19} m !

<https://arxiv.org/pdf/2412.21165>

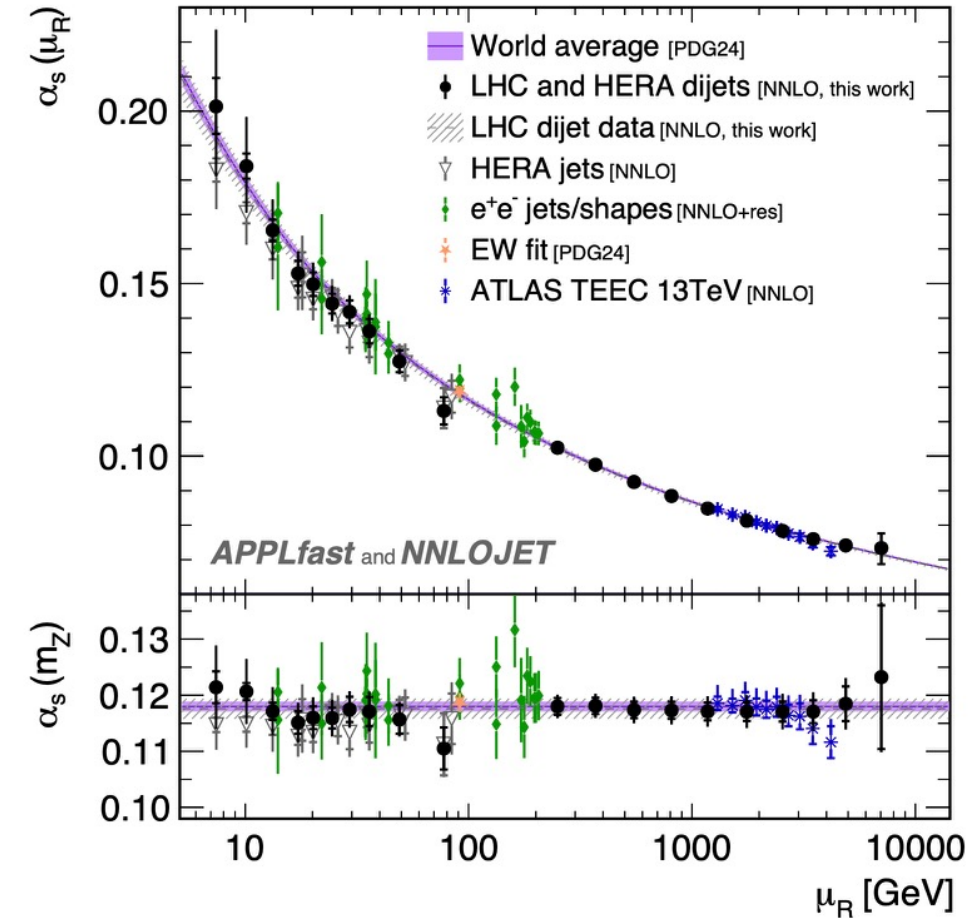


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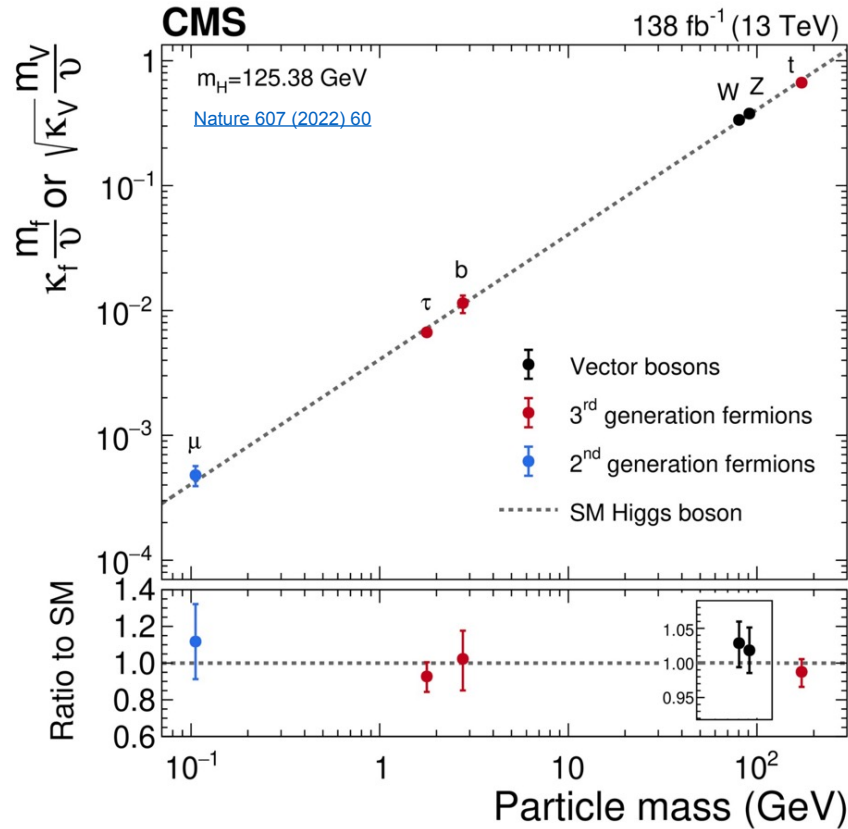
<https://arxiv.org/pdf/2412.21165>



The Higgs boson: a fundamentally new tool and future “precision probe”

$$-\frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

$$+ \psi_i \gamma_{ij} \psi_j \phi + h.c$$



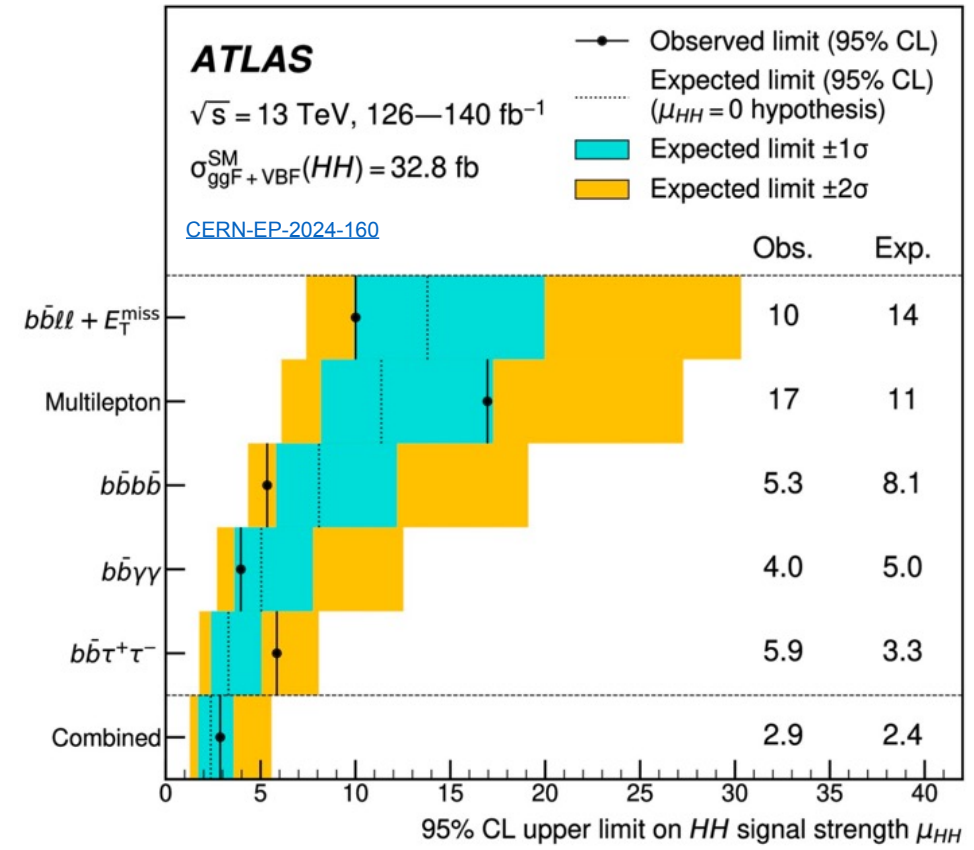
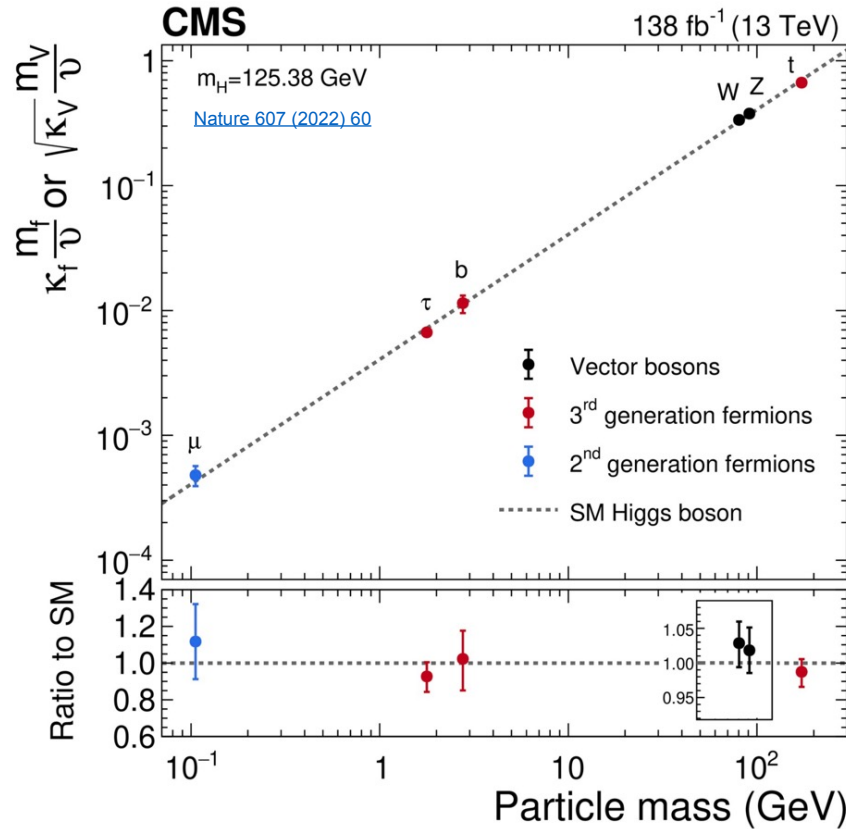
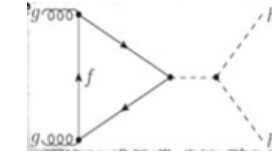
Again, the amazing precision and accuracy achieved “already” at this stage is also thanks to Stefano’s (and collaborators) work

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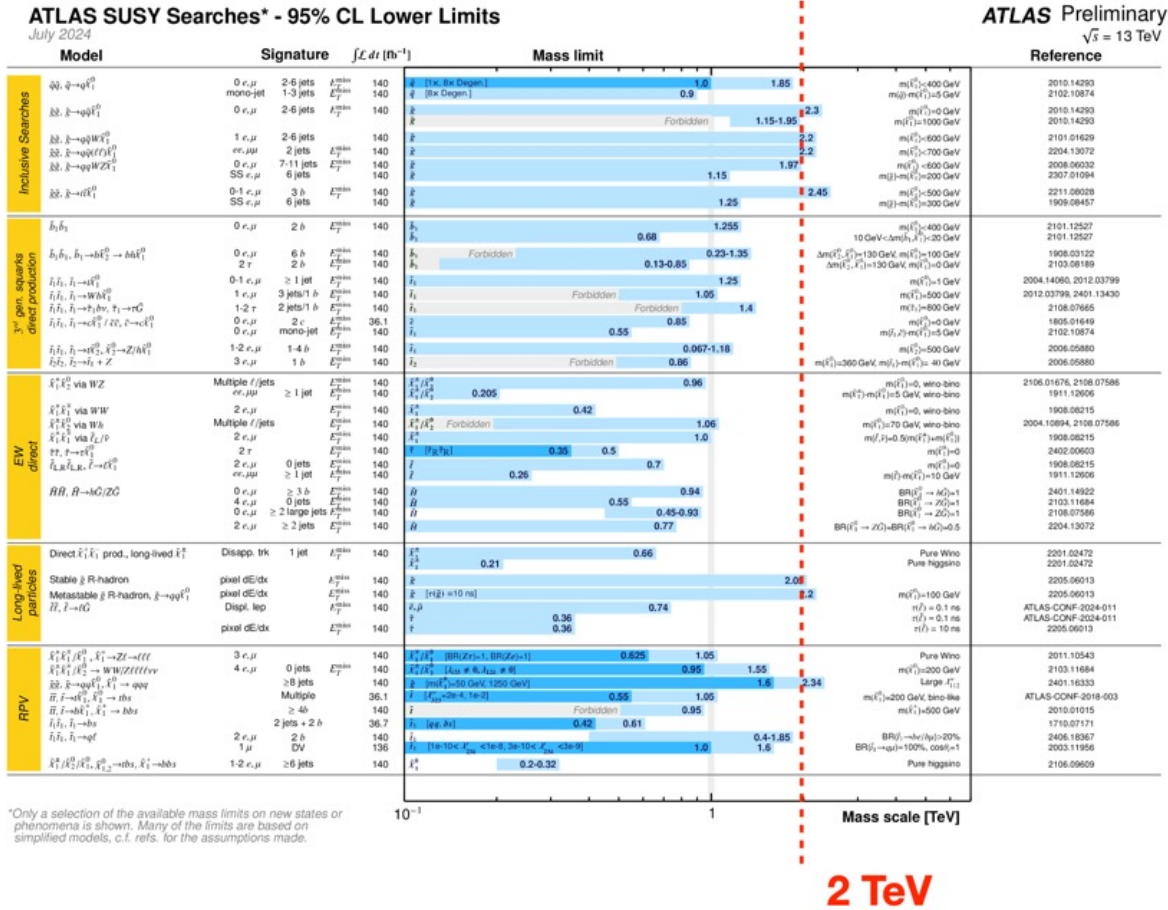
$$+|D_\mu \phi|^2 - V(\phi)$$



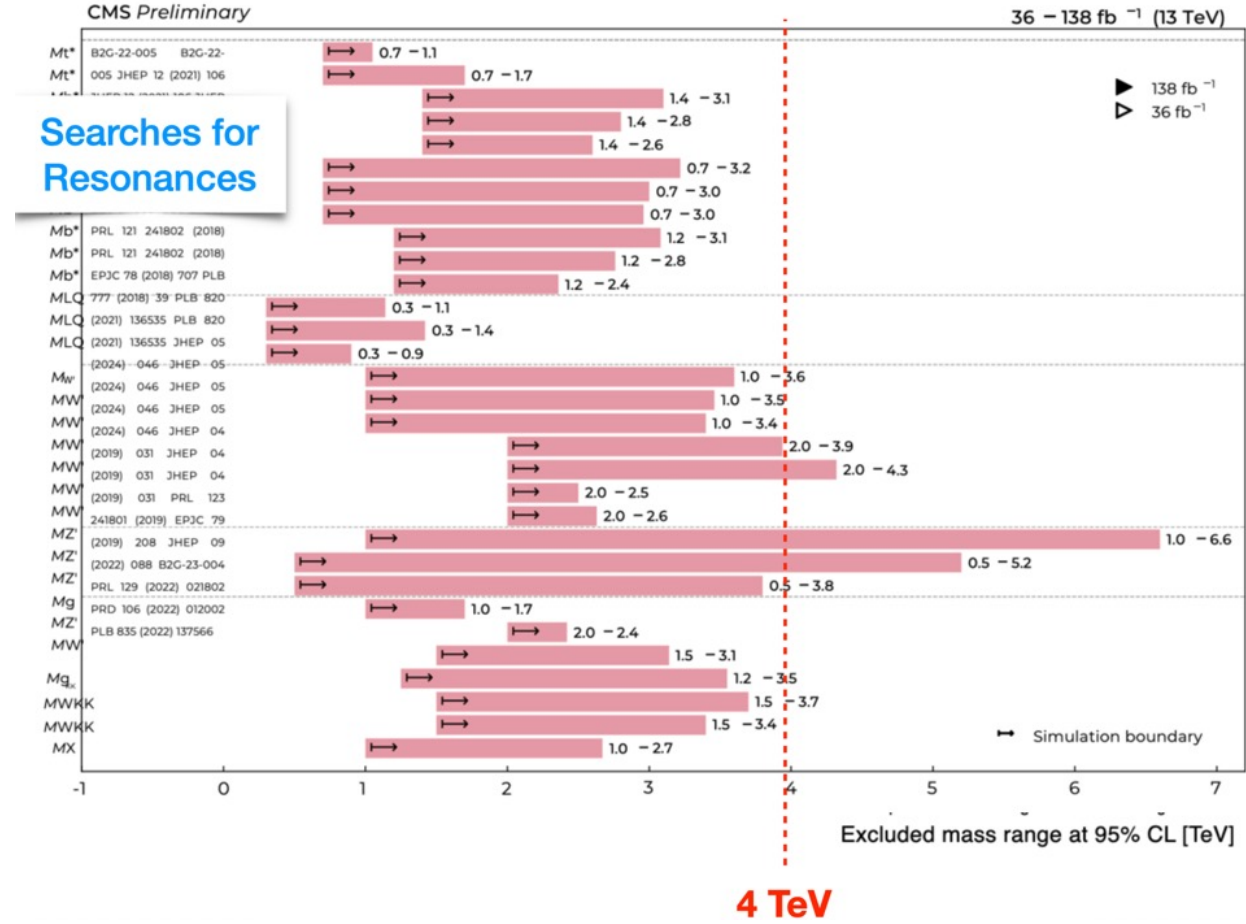
Again, the amazing precision and accuracy achieved “already” at this stage is also thanks to Stefano’s (and collaborators) work

Enormous „clean up“ of Beyond-SM model/parameter space: an achievement probably not valued enough

See talks by Livia Soffi and Marumi Kado, ICHEP 2024



*Only a selection of the available mass limits on new states or phenomena is shown. Many of the limits are based on simplified models, c.f. refs. for the assumptions made.



The SM: Highly successful, **but....**

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi} \not{D} \psi + h.c$$

Simplicity, governed by symmetries, few free parameters

$$+ \chi_i y_{ij} \chi_j \phi + h.c + |D_\mu \phi|^2 - V(\phi)$$

Not governed by symmetries
many (!) parameters
set by the “hand” of experiments!

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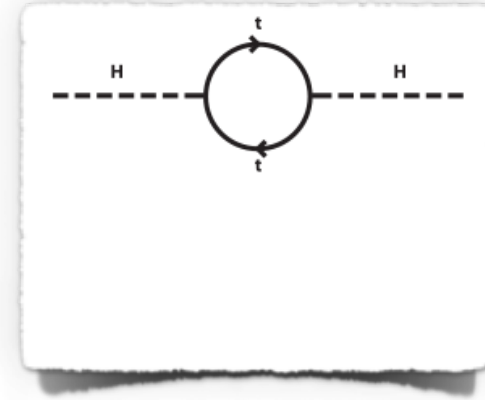
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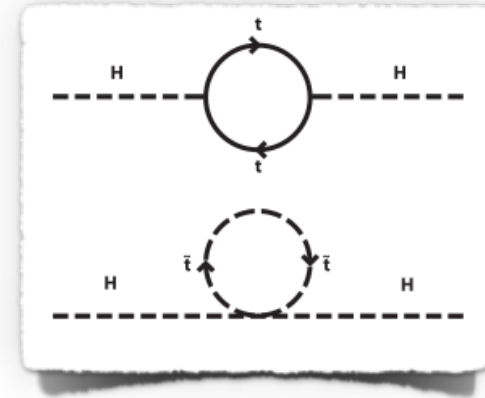
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No dark matter candidate in the model on the left !

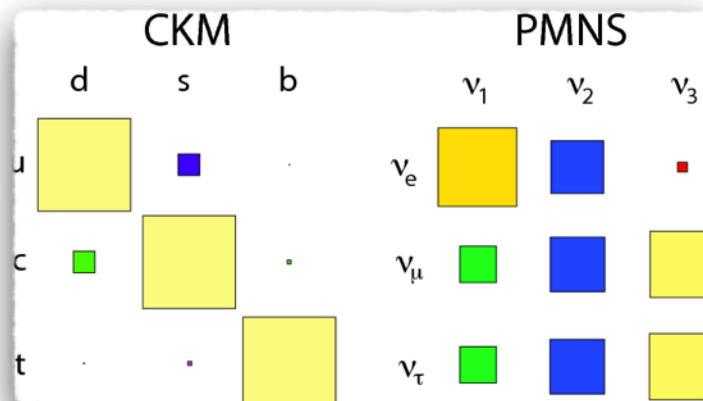
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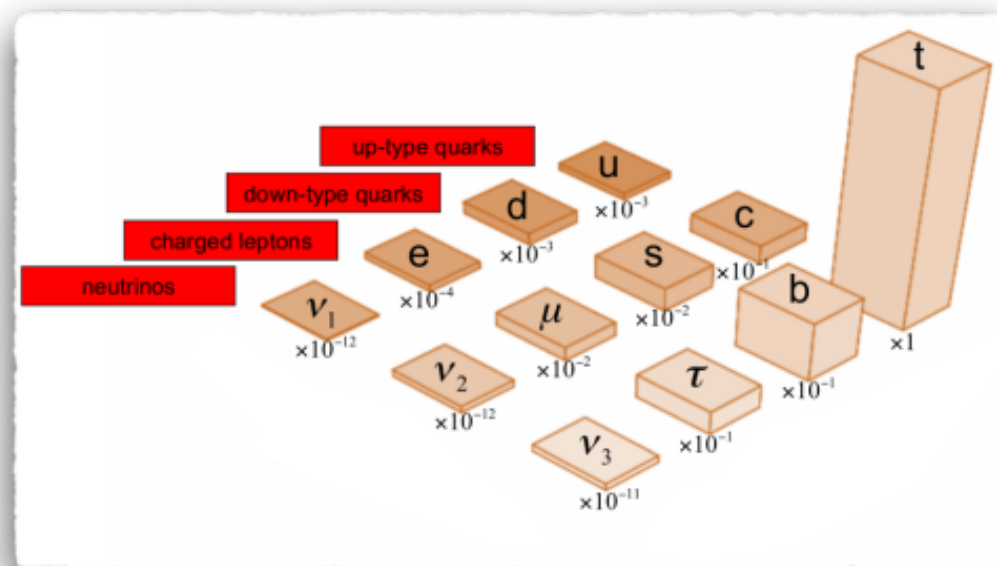
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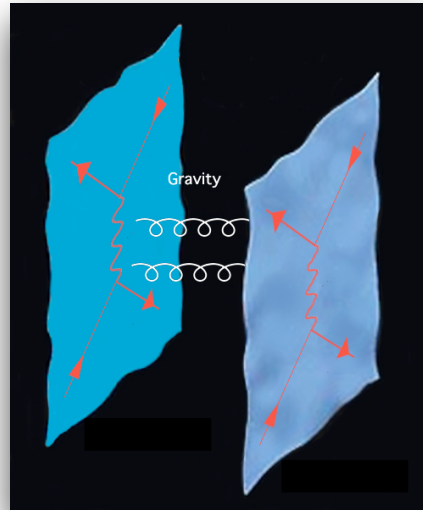
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Why is gravity so much weaker?

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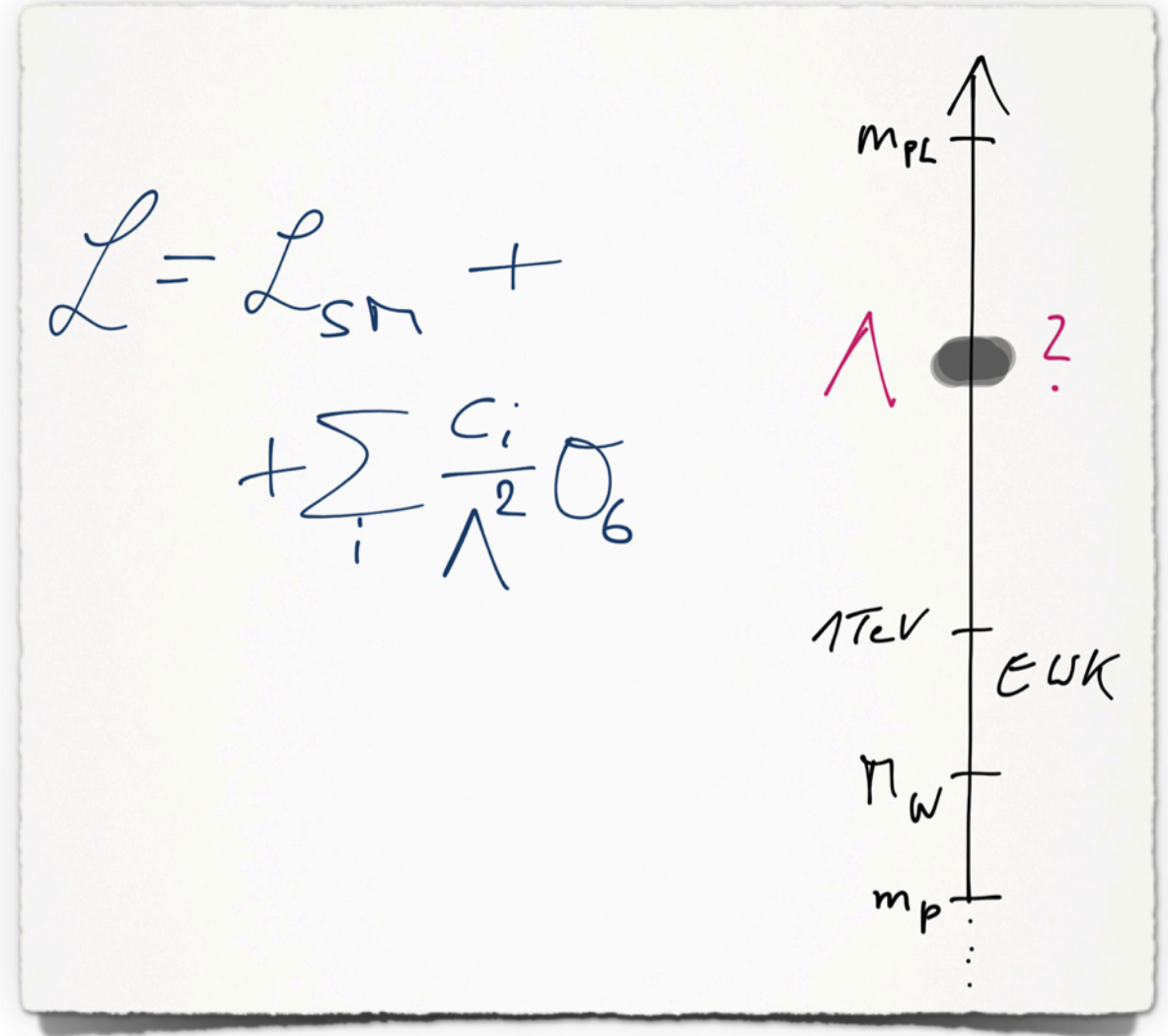
Why is gravity so much weaker?

Why are neutrinos so light?

Matter-Antimatter asymmetry?

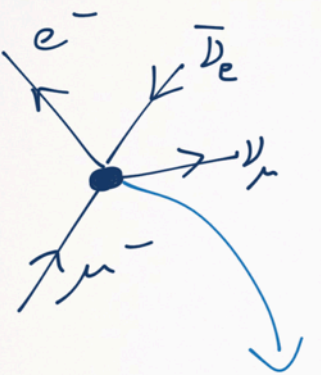
New physics needed, but where is it?

i.e. what is the scale of New Physics?

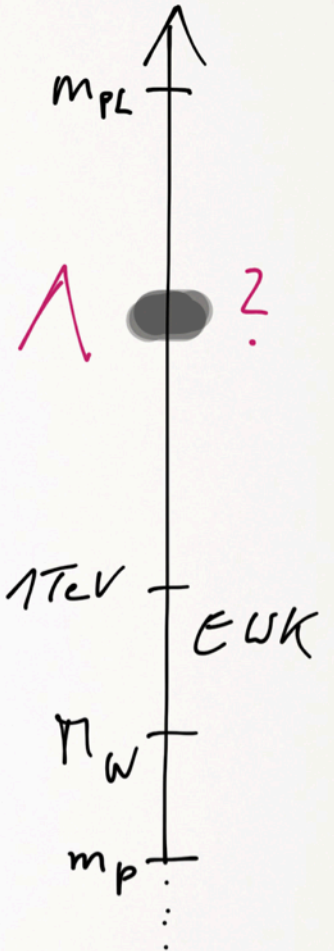


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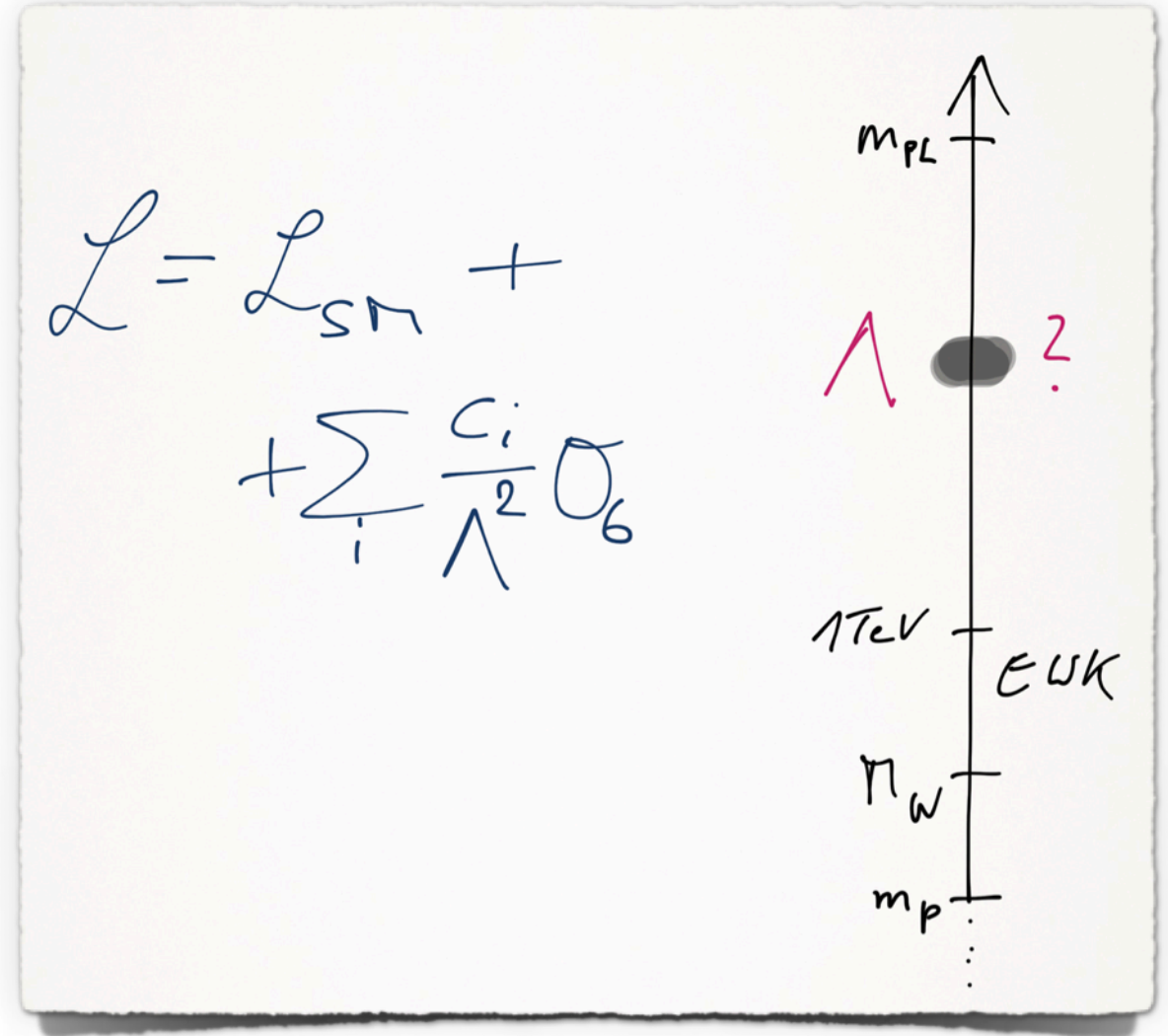
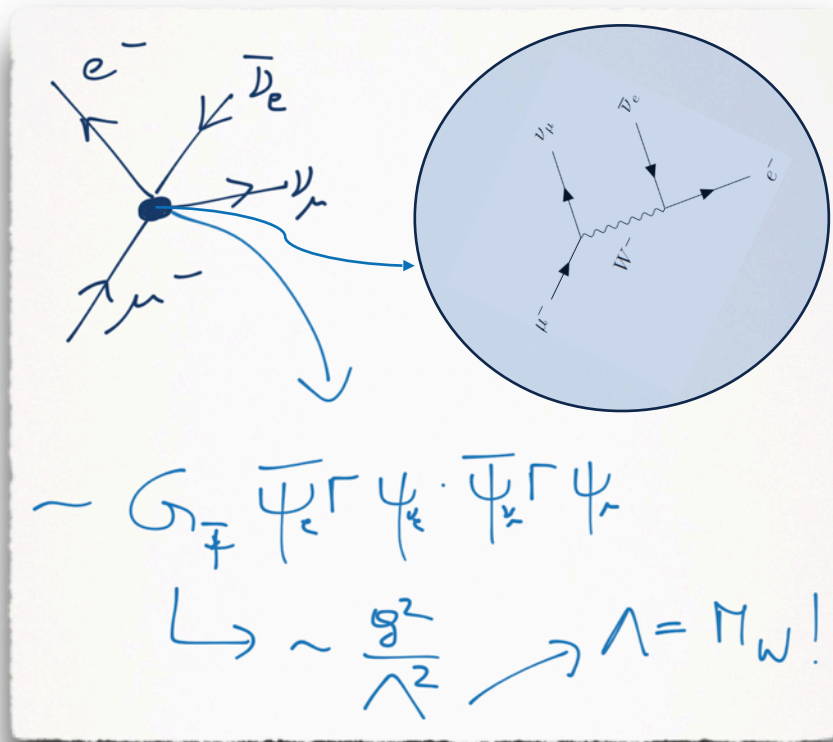
$\sim G_F \bar{\Psi}_e \Gamma \Psi_\mu \cdot \bar{\Psi}_\nu \Gamma \Psi_e$
 $\hookrightarrow \sim \frac{g^2}{\Lambda^2} \rightarrow \Lambda = M_W!$

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda^2} \mathcal{O}_6$$


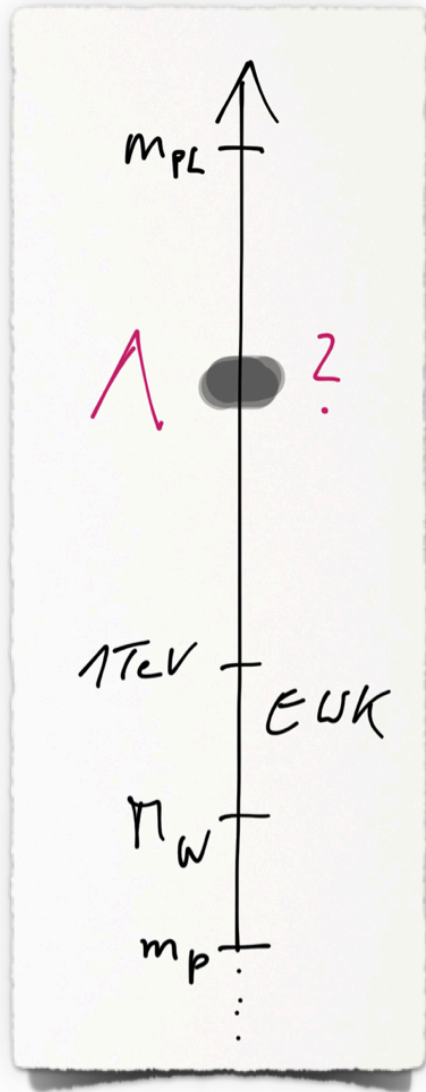
Energy scale diagram showing m_{PL} , Λ , 1TeV , M_W , m_p , and dots. The Λ scale is marked with a red question mark. The 1TeV scale is labeled EWK .

New physics needed, but where is it?

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New physics needed, but where is it?

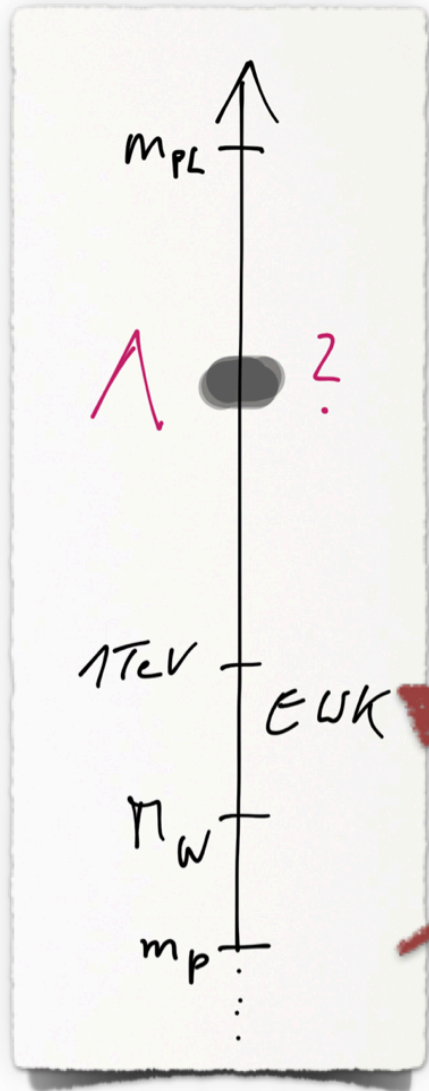


$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_6^{\text{th}} \dots$$

↙ ↘

$$\frac{d\sigma^{\text{exp}}}{dx} \Leftrightarrow \frac{d\sigma^{\text{th}}}{dx} (\alpha_i, m_j, c_k)$$

New physics needed, but where is it?

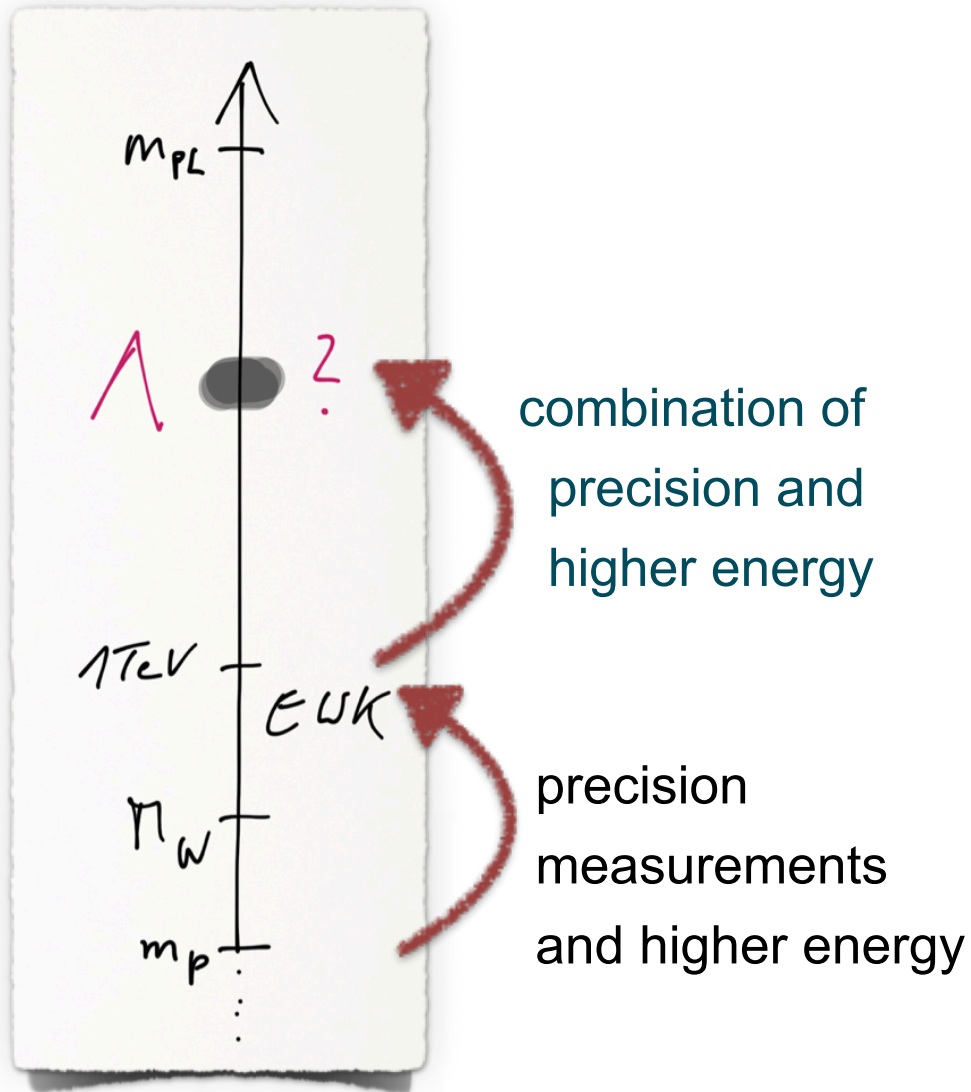


precision
measurements
and higher energy

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_6^t \dots$$

$$\frac{d\sigma^{exp}}{dx} \Leftrightarrow \frac{d\sigma^{th}}{dx} (\alpha_i, m_j, c_k)$$

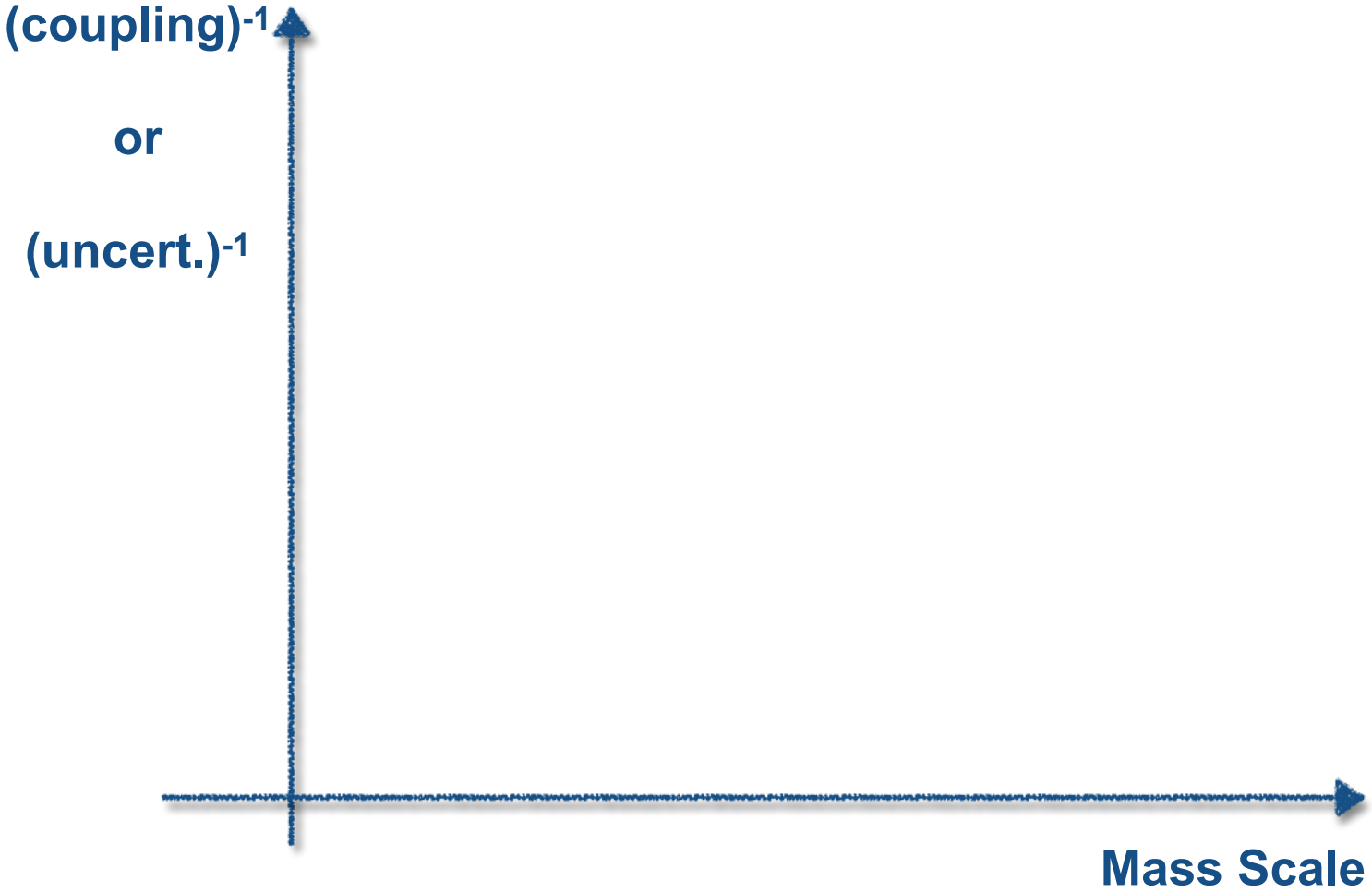
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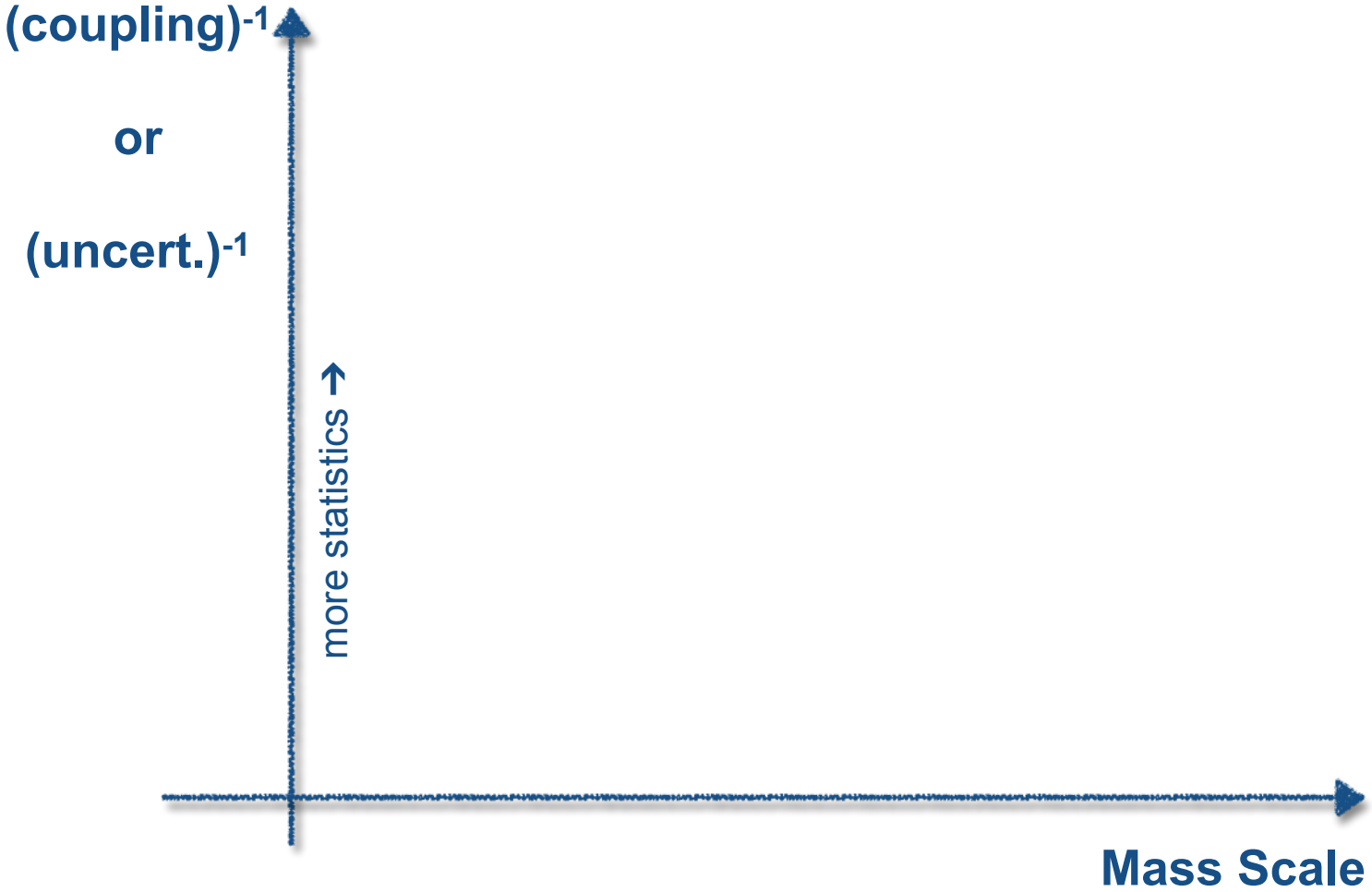
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How to explore the unknown



How to explore the unknown



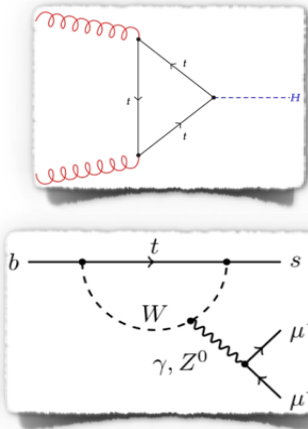
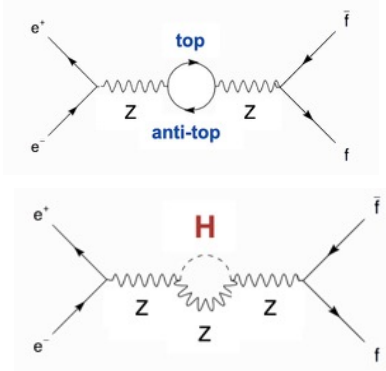
How to explore the unknown

$(\text{coupling})^{-1}$

or

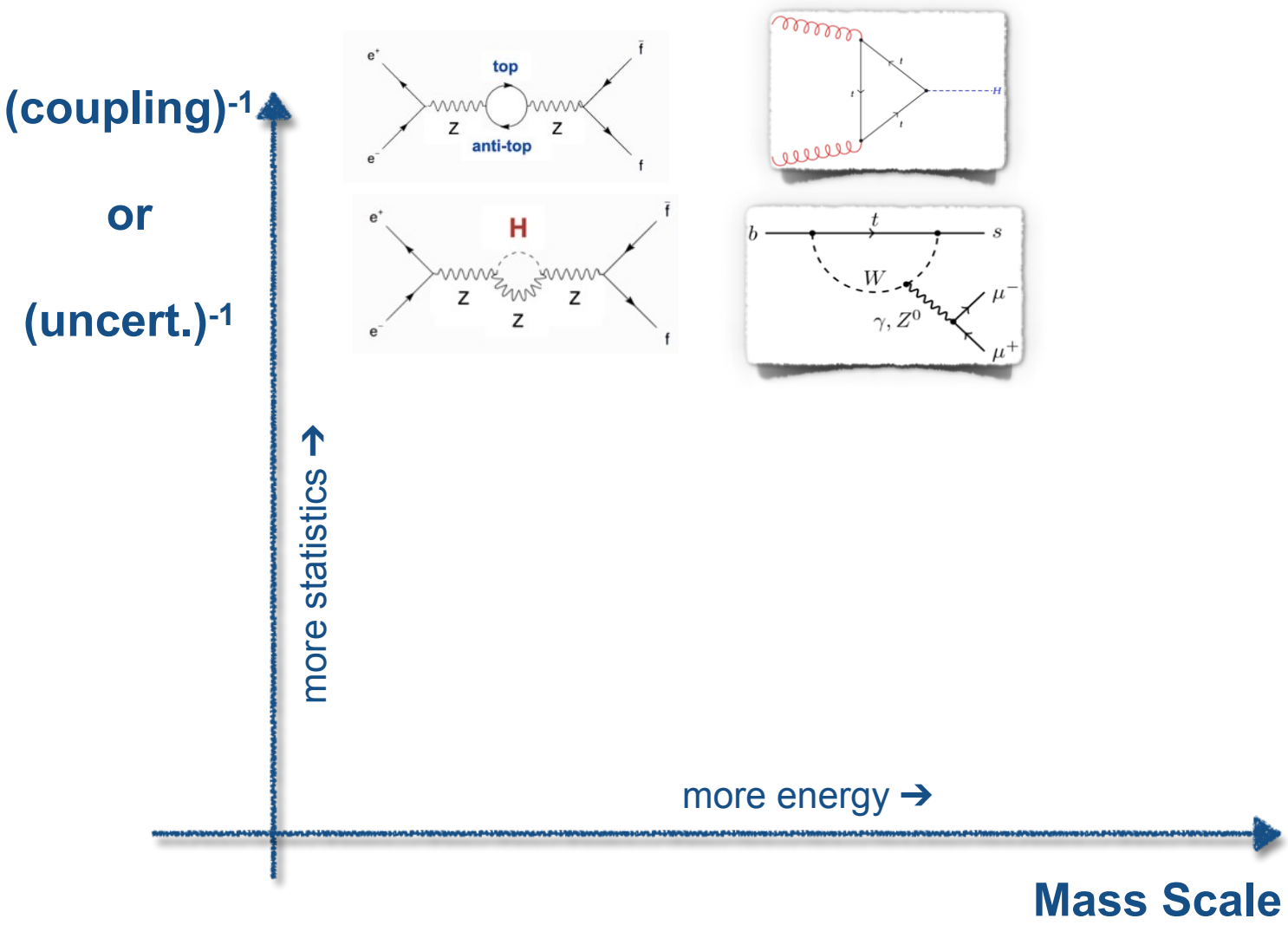
$(\text{uncert.})^{-1}$

more statistics \rightarrow

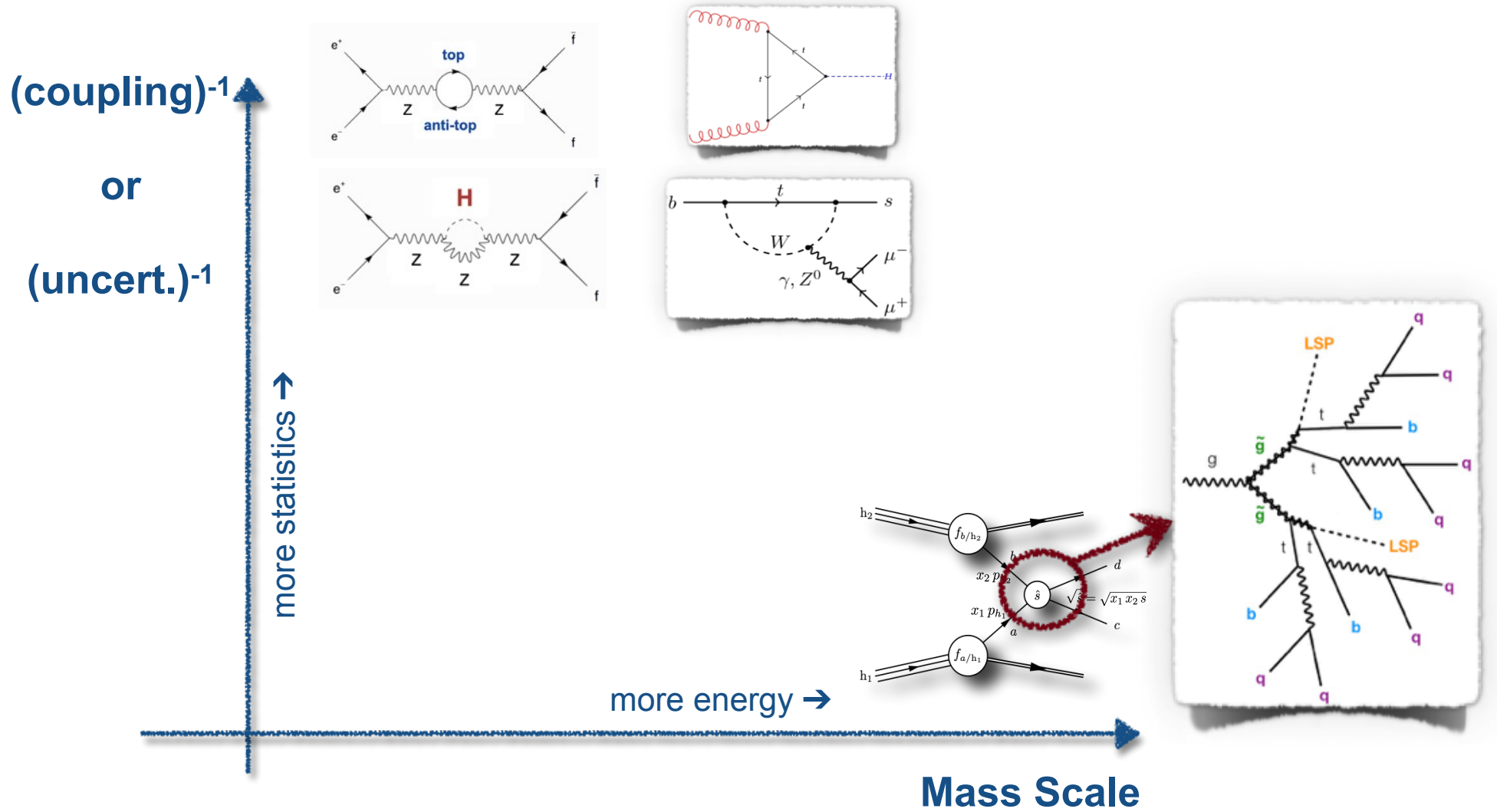


Mass Scale \rightarrow

How to explore the unknown

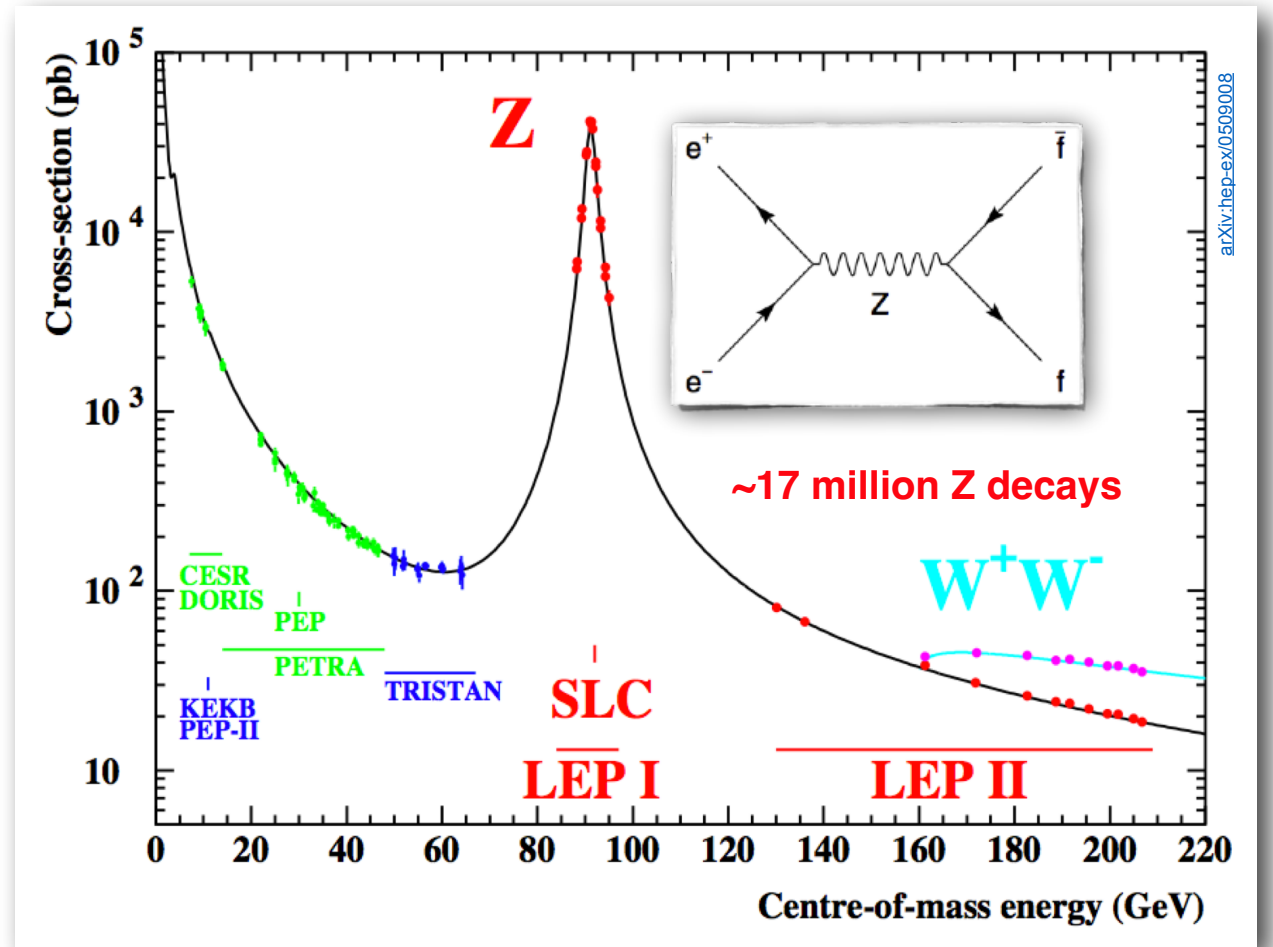
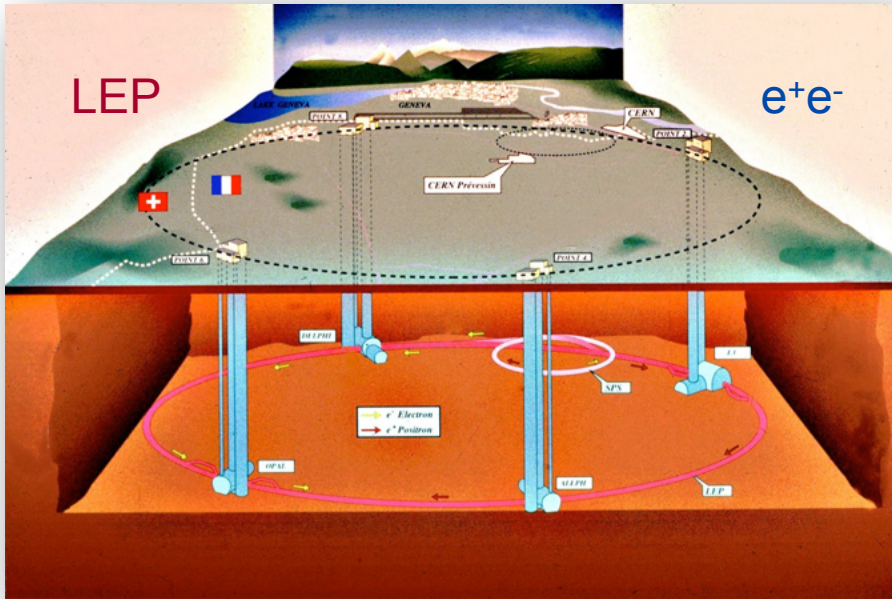


How to explore the unknown



A look back at the "good old" LEP times

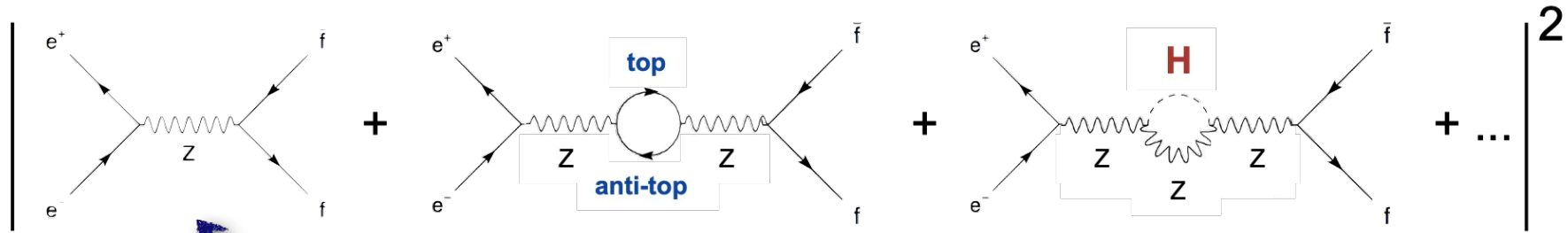
Physics at LEP



Z mass: relative precision of **0.02 per-mille**
 “Height” of the Z resonance : **~ 1 per-mille**

Sensitivity to quantum loops, thanks to precision and accuracy

$$\sigma(e^+e^- \rightarrow f\bar{f}) =$$



$$\propto M_t^2$$

% level correction

$$\propto \log M_H^2$$

sub-% level correction

Observable \mathcal{O}

$$\Rightarrow \mathcal{O}_{\text{theo}} = \mathcal{O}_{\text{LO}} \times (1 + \Delta r) \quad \longleftrightarrow \text{compare} \quad \mathcal{O}_{\text{meas}}$$

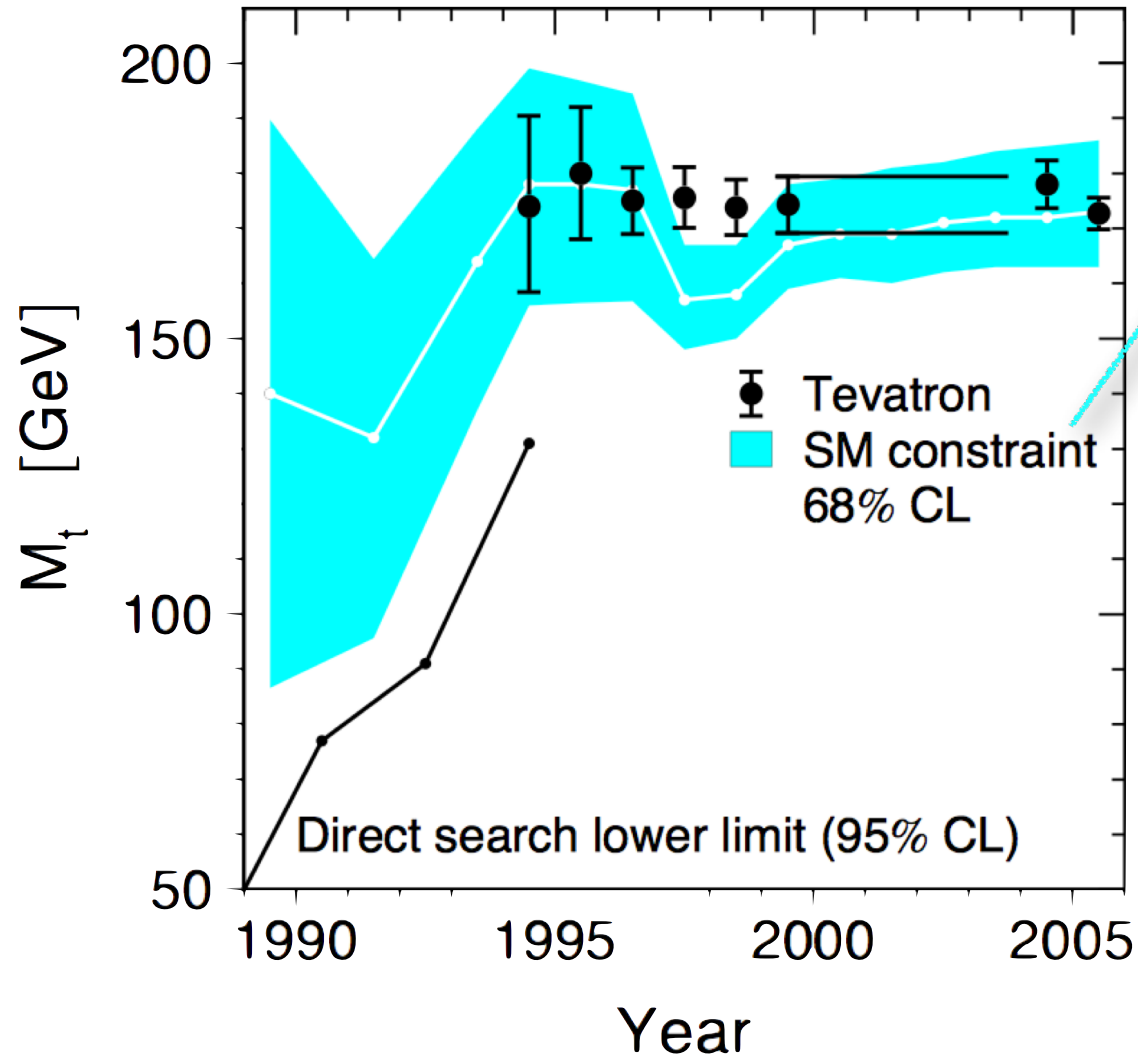
“loop” corrections: $\Delta r = f(M_t^2, \log M_H^2)$

👉 with per-mille level precision measurements sensitivity to heavy particles in the loops!

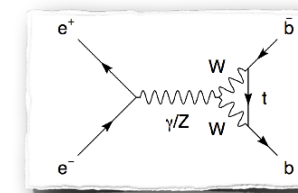
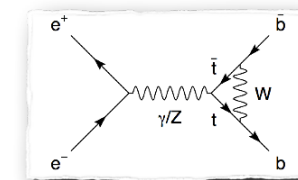
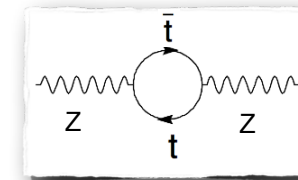
Proof of principle

“prediction” of the top quark mass and comparison to the direct measurement

from [arXiv:hep-ex/0509008](https://arxiv.org/abs/hep-ex/0509008)



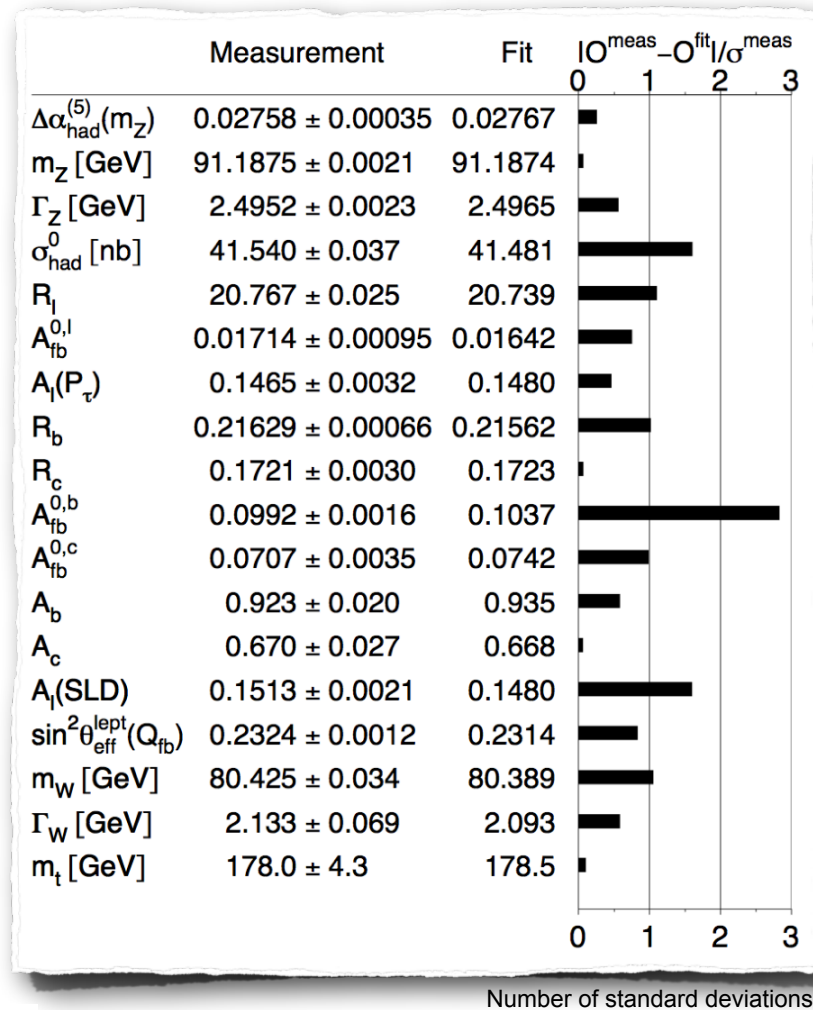
$M_t = 173^{+13}_{-10} \text{ GeV}$



And then the “Higgs prediction”

Vary a few input parameters, including M_H , in a global fit to:

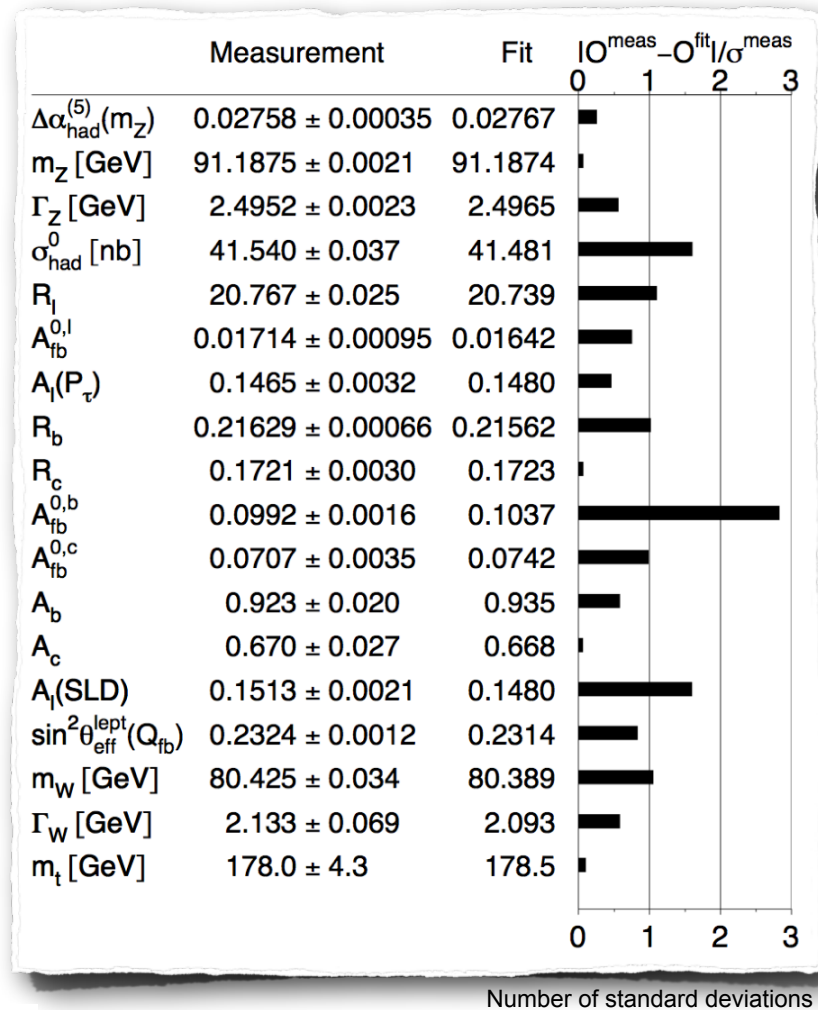
Z-pole data, direct measurements of m_W , Γ_W , m_{top} and the hadr. vac. pol.



And then the “Higgs prediction”

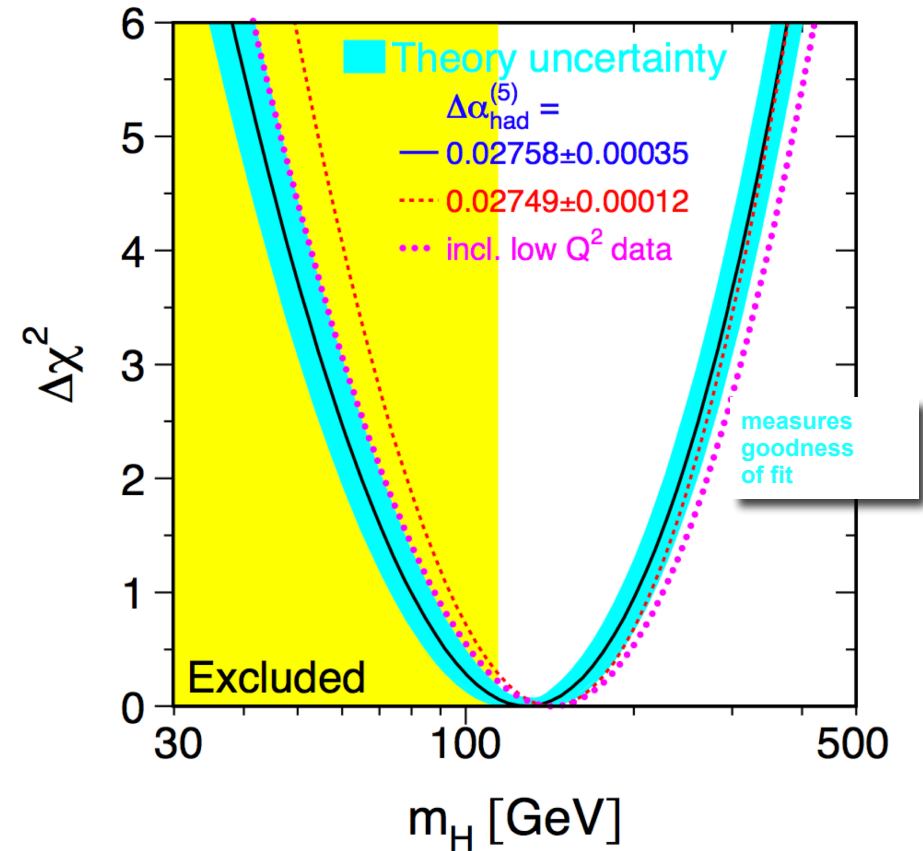
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Example taken from LEP EWK combination early 2006

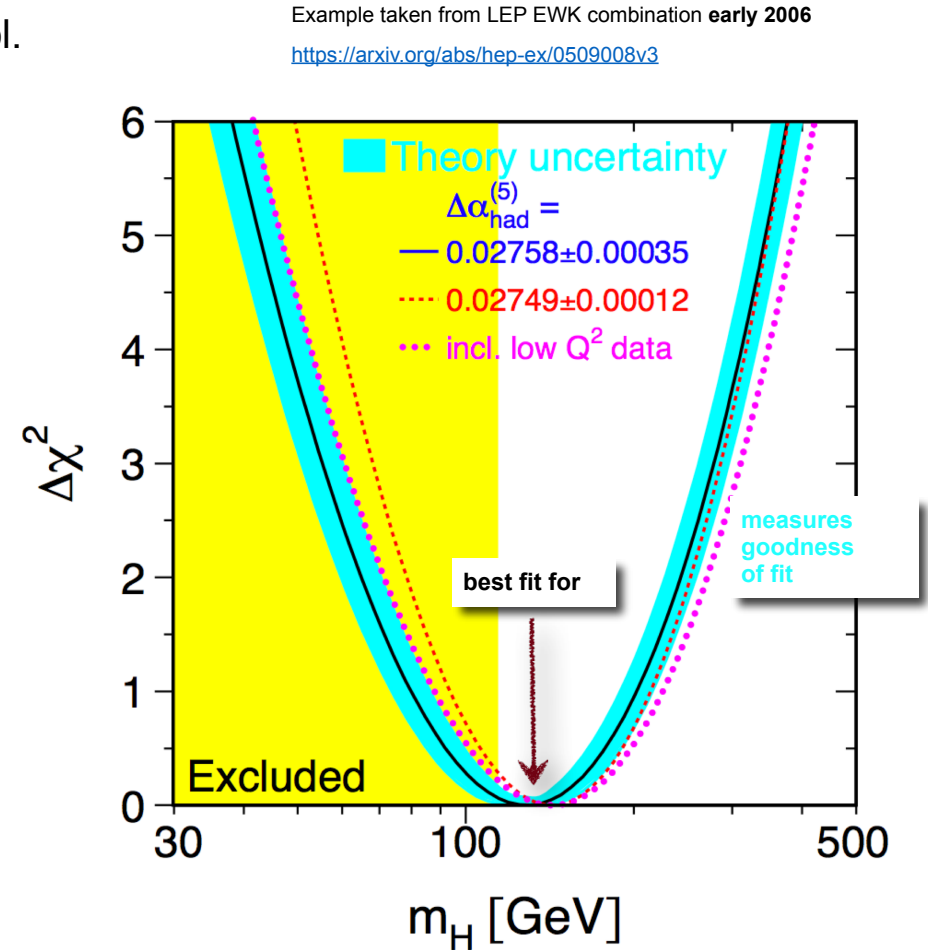
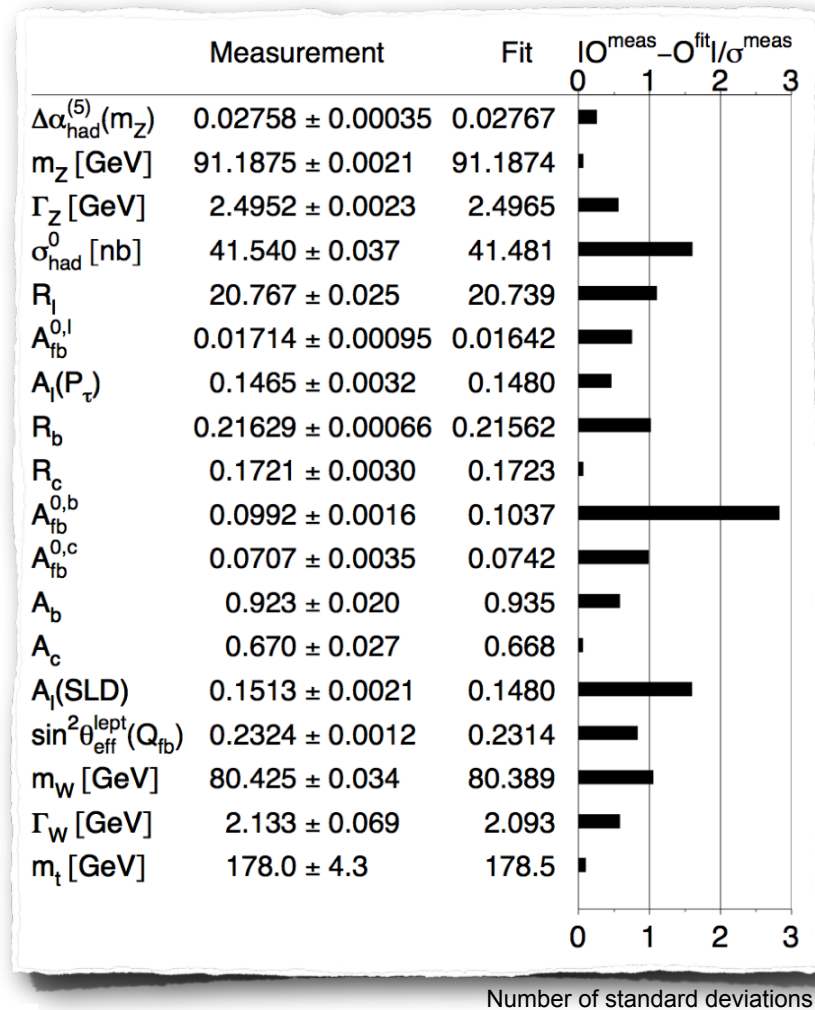
<https://arxiv.org/abs/hep-ex/0509008v3>



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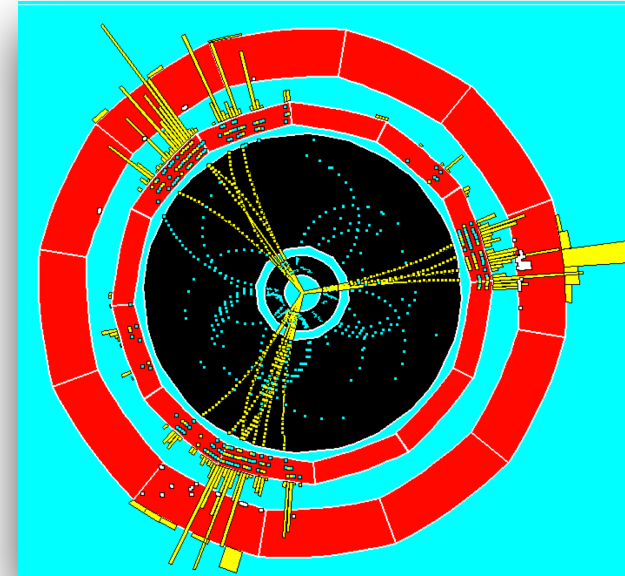
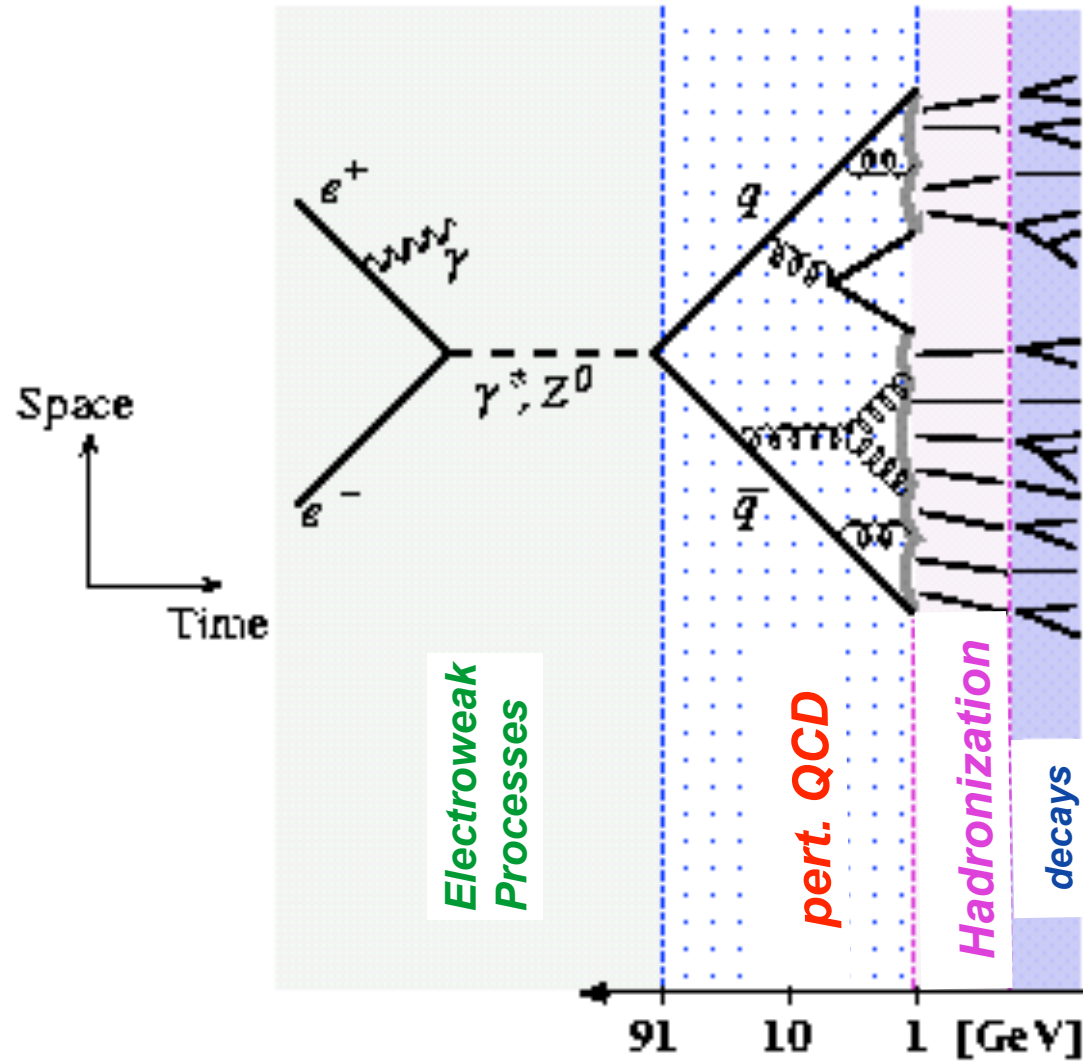
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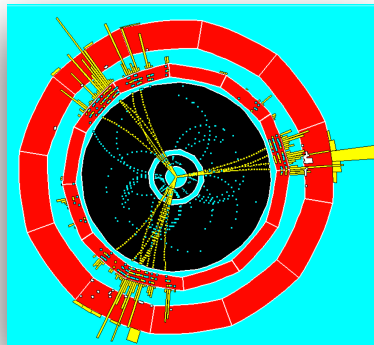
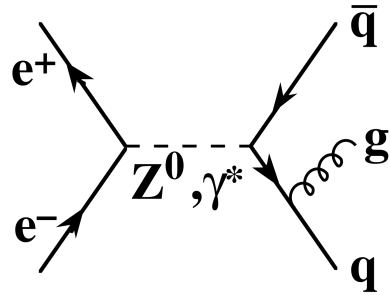


$M_H = 129_{-49}^{+74} \text{ GeV}$
 $M_H < 285 \text{ GeV}$ at 95% C.L.

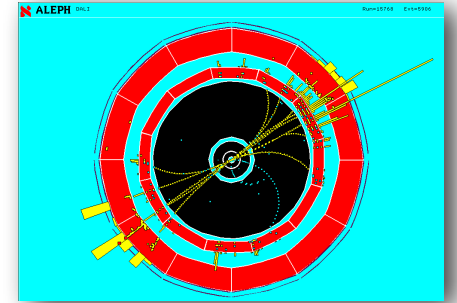
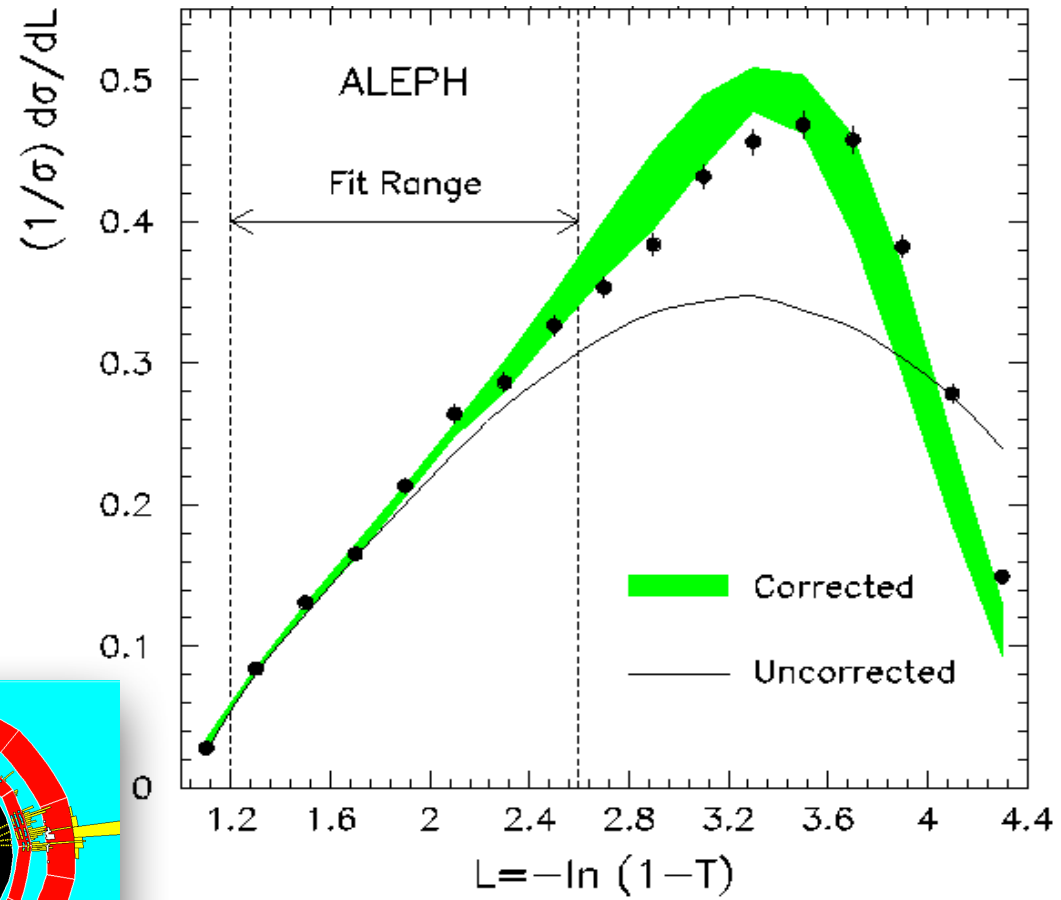
LEP: Also a wonderful tool for precision QCD studies...



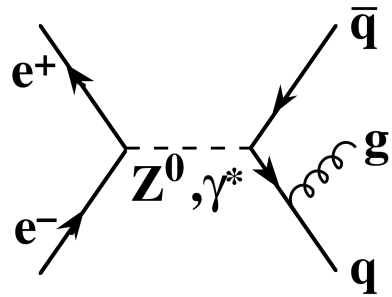
Measurements of the strong coupling



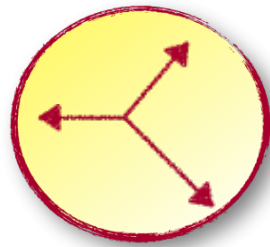
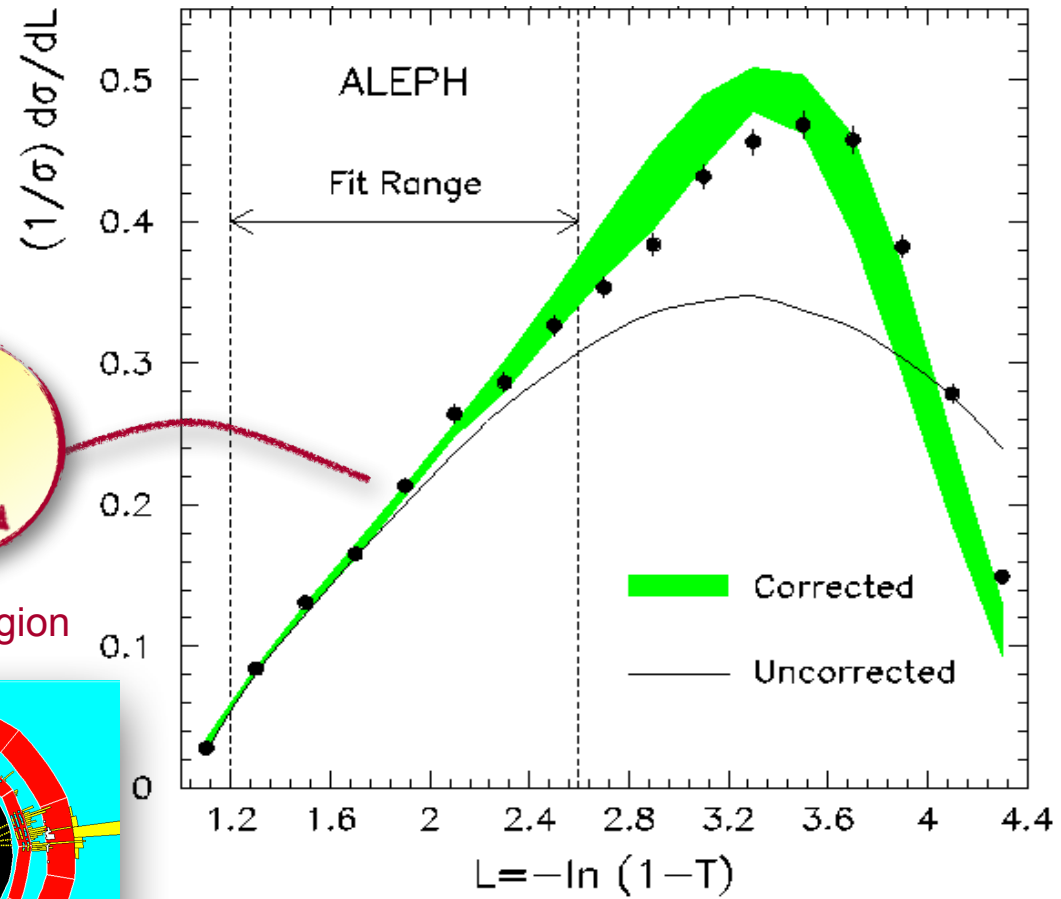
1/2 ← Thrust → 1



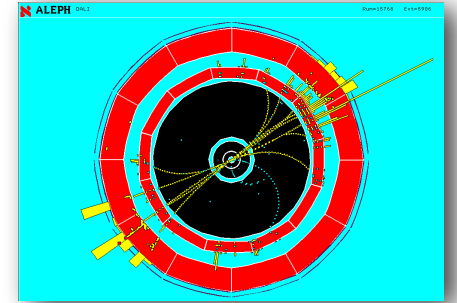
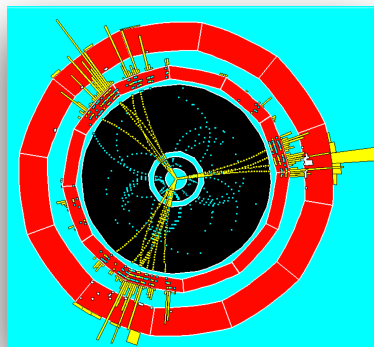
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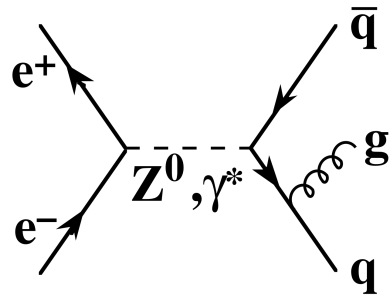
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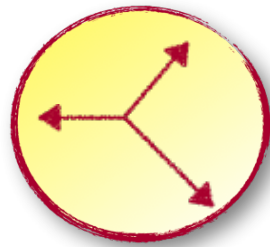
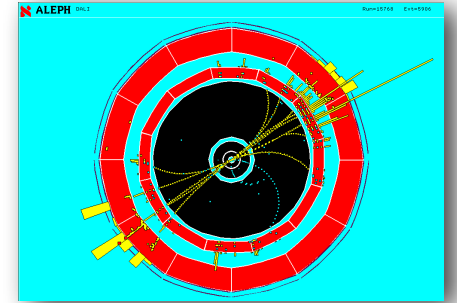
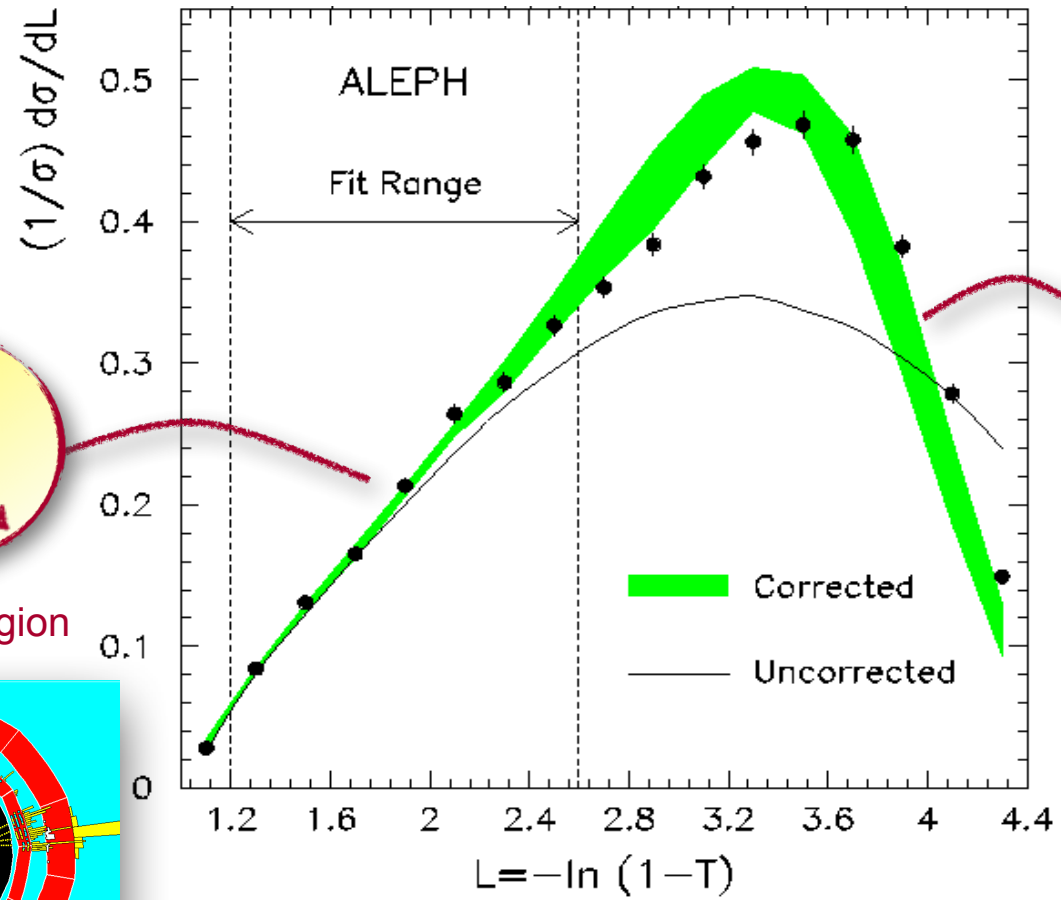
3 (4,5) jet region



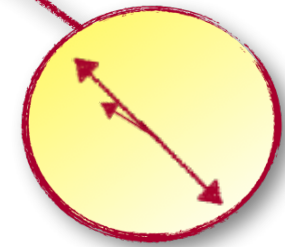
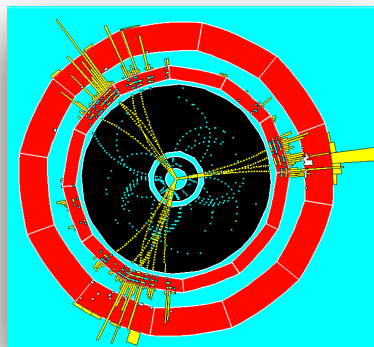
Measurements of the strong coupling



1/2 ← Thrust → 1

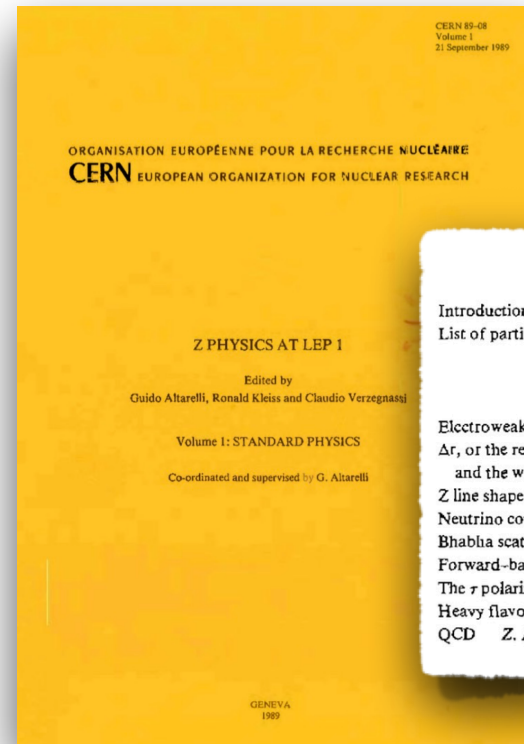
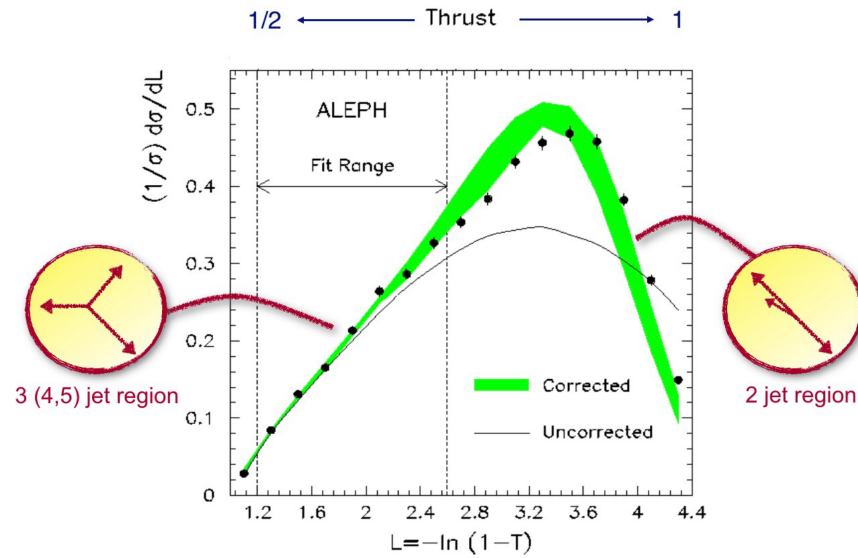


3 (4,5) jet region



2 jet region

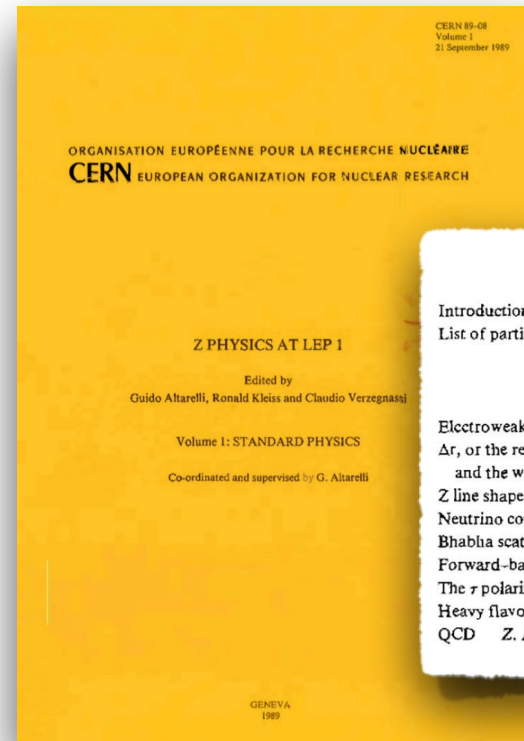
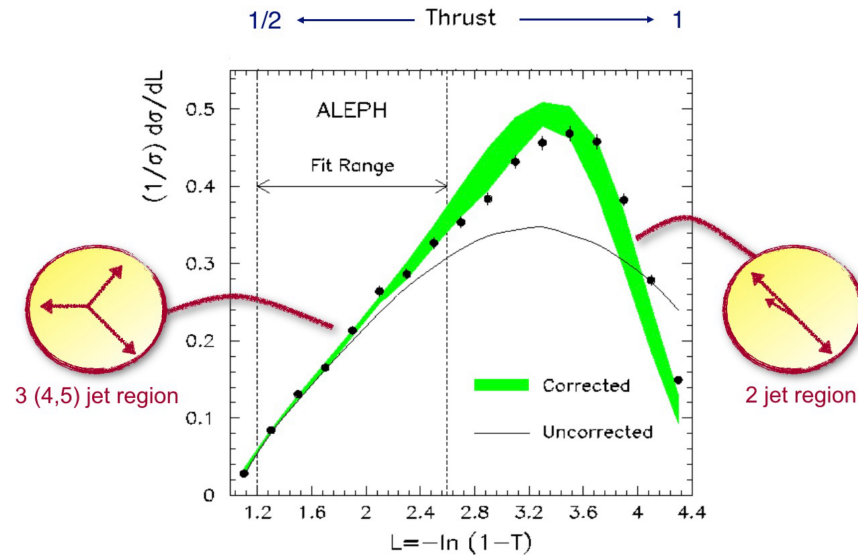
Measurements of the strong coupling



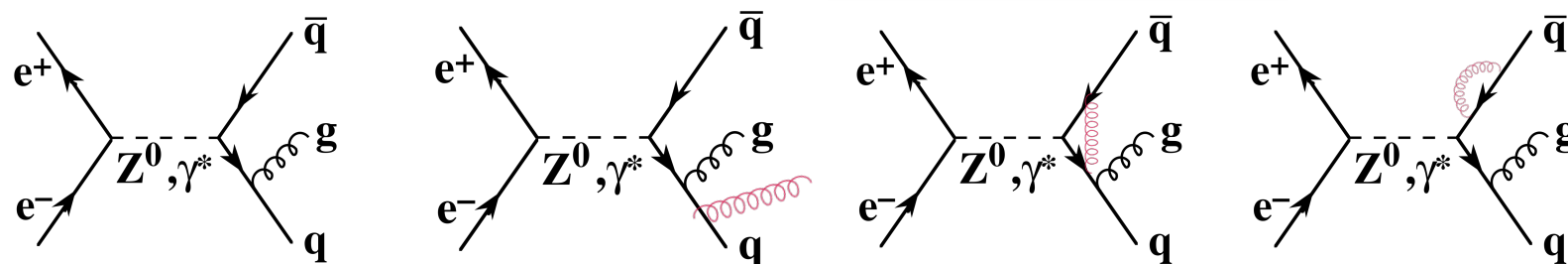
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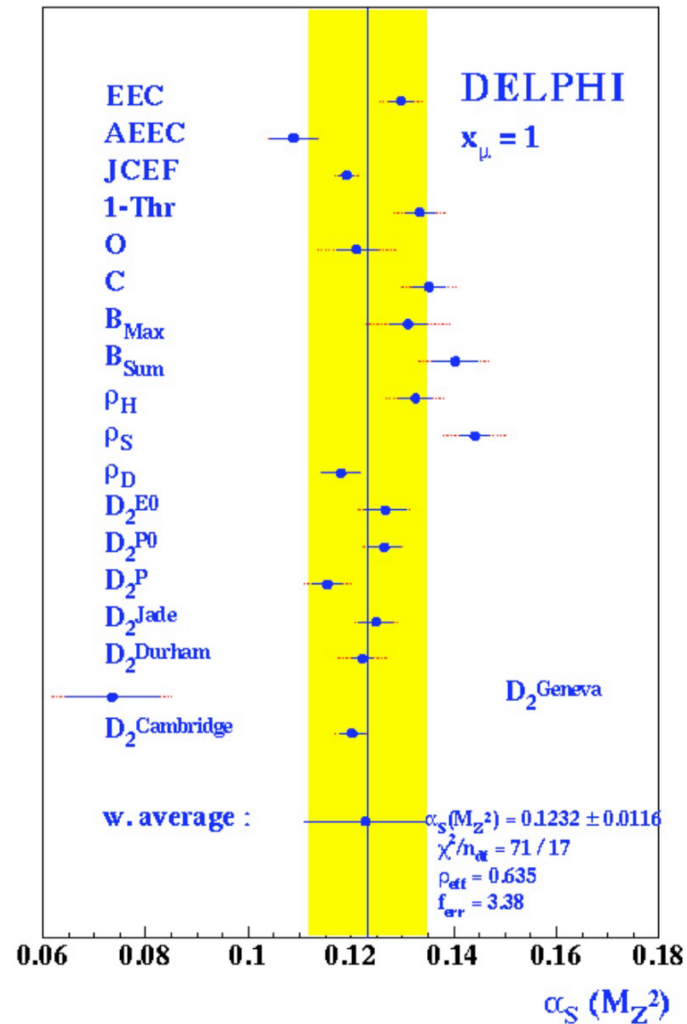


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$$\sigma_{\text{NLO}}^{\text{pert}} = \alpha_s(\mu^2) A + \alpha_s^2(\mu^2) \left[B + \beta_0 A \ln \frac{\mu^2}{Q^2} \right]$$

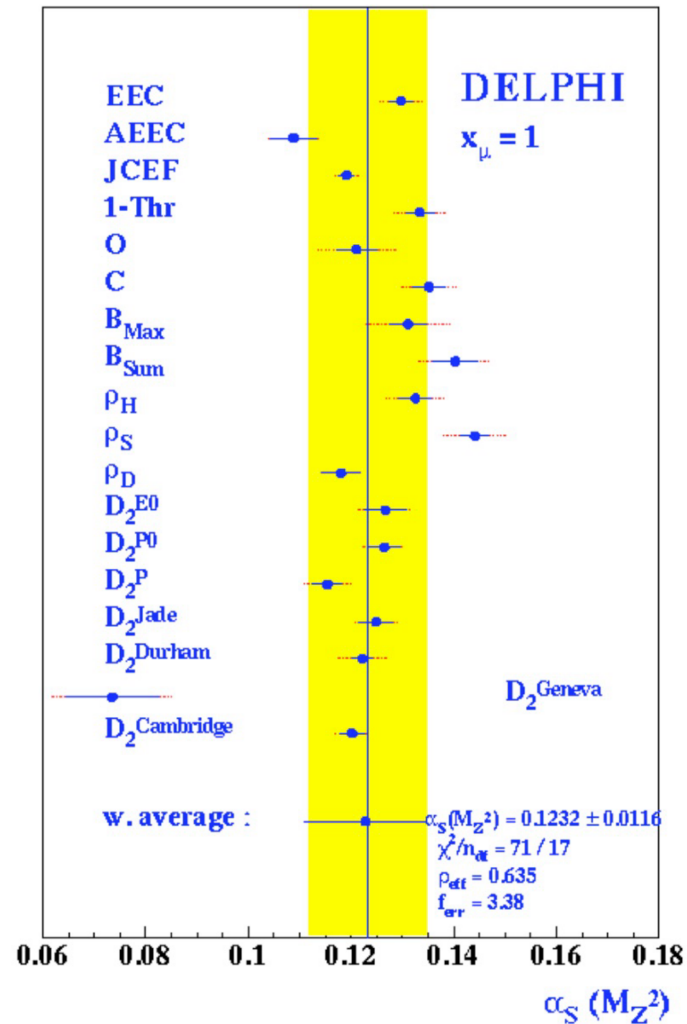
The path from NLO to NLO+NLL



NLO only, typical results

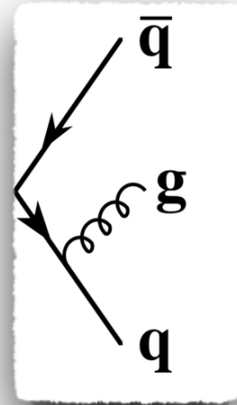
$$\alpha_s(M_Z) \approx 0.125 \pm 0.010$$

The path from NLO to NLO+NLL



NLO only, typical results

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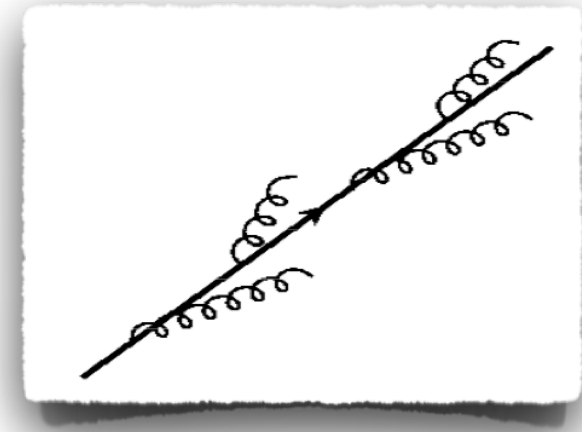


α_s

$$E_G (1 - \cos \theta_{QG})$$

$$\Rightarrow \alpha_s \ln^2 y_{cut}$$

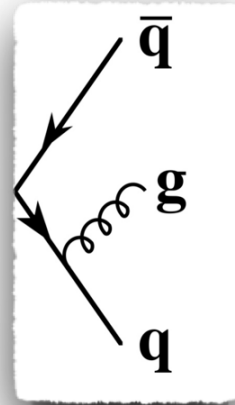
The path from NLO to NLO+NLL



$$\alpha_s^n \ln^{2n} y_{\text{cut}}$$

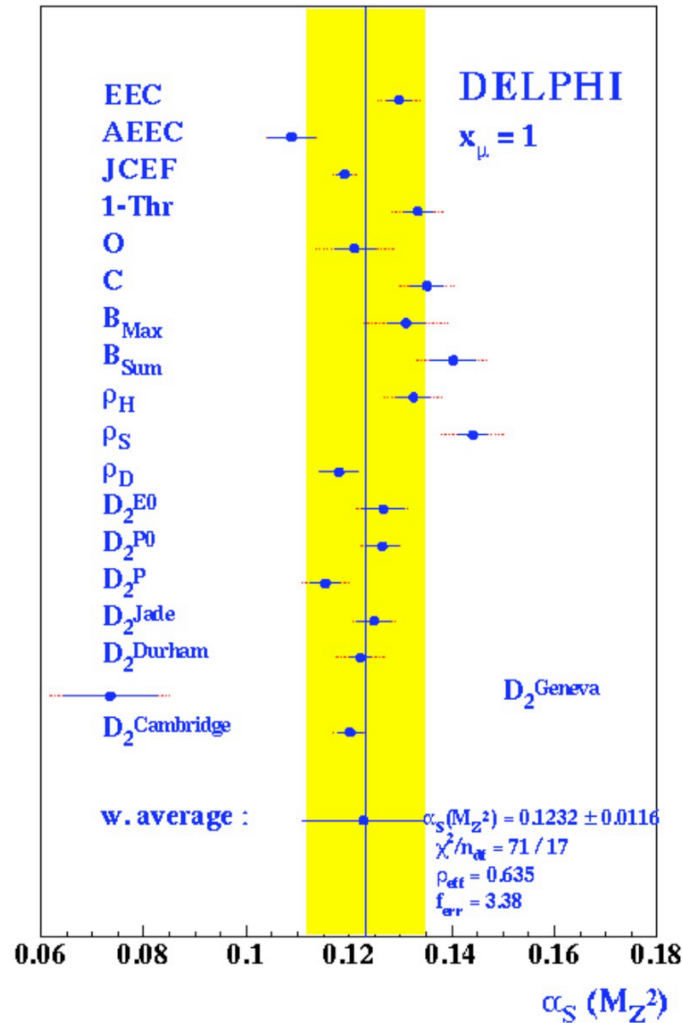
$$\sigma \propto \sigma_{\text{NLO}} + \sum_{n,m} c_{n,m} \alpha_s^n \ln^m y_{\text{cut}}$$

“the rise of resummation”



α_s

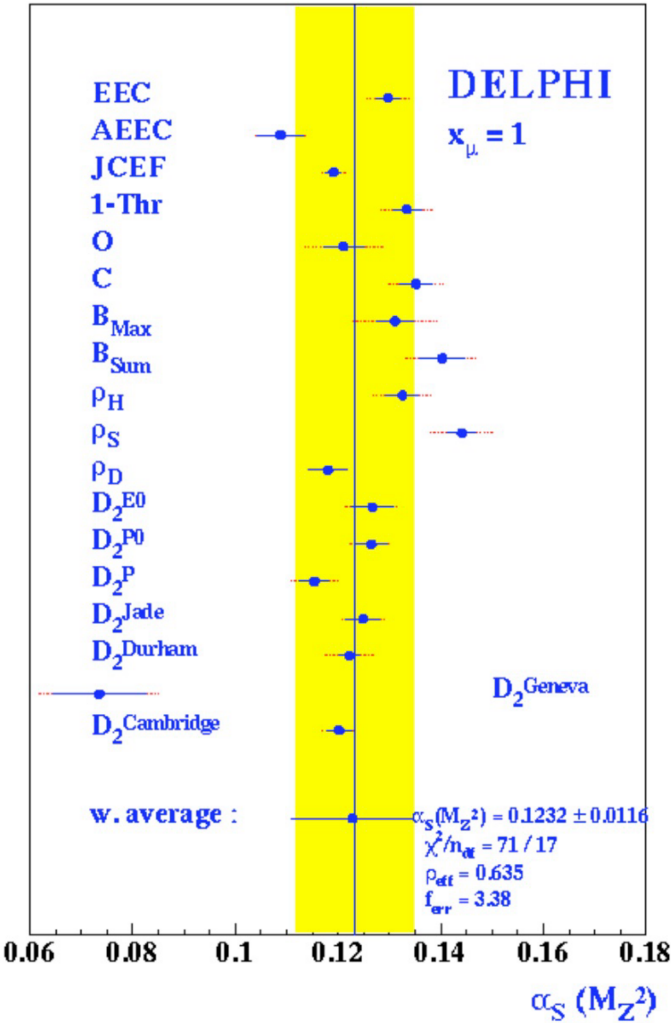
$$\frac{E_G (1 - \cos \theta_{\text{QG}})}{\Rightarrow \alpha_s \ln^2 y_{\text{cut}}}$$



NLO only, typical results

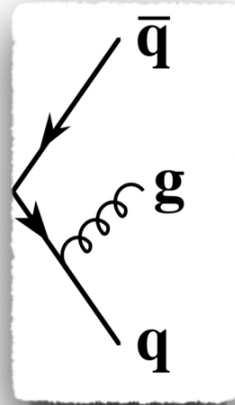
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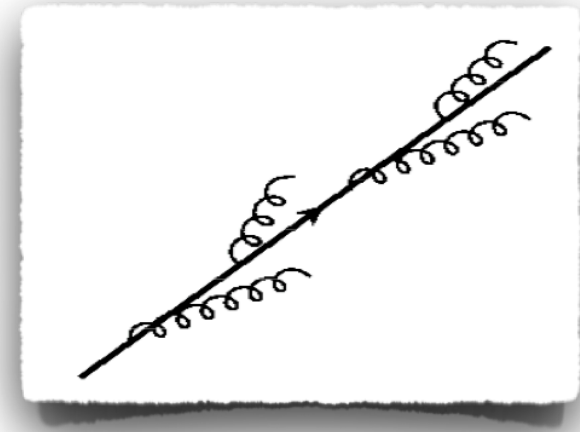
NLO only, typical results

$$\alpha_s(M_Z) \approx 0.125 \pm 0.010$$



α_s

$$\frac{E_G (1 - \cos \theta_{QG})}{\Rightarrow \alpha_s \ln^2 y_{cut}}$$



$$\alpha_s^n \ln^{2n} y_{cut}$$

$$\sigma \propto \sigma_{NLO} + \sum_{n,m} c_{n,m} \alpha_s^n \ln^m y_{cut}$$

“the rise of resummation”

$$R_2(y_{cut}) = \frac{\sigma_2(y_{cut})}{\sigma_{tot}}$$

$$R_2 = \exp \left\{ - \int_{sy_{cut}}^s \frac{dq^2}{q^2} \frac{C_F \alpha_s(q^2)}{2\pi} \left[\ln \frac{s}{q^2} - \frac{3}{2} \right] \right\} \approx 1 - \int_{sy_{cut}}^s \frac{dq^2}{q^2} \frac{C_F \alpha_s(q^2)}{2\pi} \ln \dots + \dots \approx 1 - \frac{C_F \alpha_s}{2\pi} \ln^2 y_{cut} + \dots$$

$$R_2(y_{cut} \rightarrow 0) = 0$$

Resummation

Thrust distribution in e^+e^- annihilation \star

S. Catani ^{a,b}, G. Turnock ^a, B.R. Webber ^a and L. Trentadue ^c

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Received 18 April 1991

We calculate the thrust distribution in e^+e^- annihilation including resummation of leading and next-to-leading logarithms of $1-T$ to all orders in QCD perturbation theory. This enables us to predict the distribution up to the largest values of T and reduces the renormalization scale dependence relative to the leading order at both large and small T . From a comparison with experimental data, we find $A_{\text{had}}^{(3)} = 200 \pm 140$ MeV, corresponding to $\alpha_s(m_Z^2) = 0.116 \pm 0.012$.

1. Introduction

The detailed experimental data on event shapes in e^+e^- annihilation at LEP energies [1] and below [2-5] provide both a challenge to QCD and a good opportunity for accurate determinations of the strong coupling constant α_s . Of the various possible event shape measures (see ref. [6] for a recent review), one of the earliest and most widely-used is the thrust, T [7], defined as

$$T = \text{Max} \frac{\sum_i |p_i \cdot n|}{\sum_i |p_i|}, \quad (1)$$

where the sum is over all final-state particles i and the maximum is with respect to the direction of the vector n (the thrust axis). It can be seen from this definition that the thrust is an infrared and collinear safe quantity, that is, it is insensitive to the emission of zero-momentum particles and to the splitting of one particle into two collinear ones. Thus the cross section

$$\sigma(\tau) = \int_{1-\tau}^1 \frac{d\sigma}{dT} dT \quad (2)$$

is finite order-by-order in QCD perturbation theory, and the experimental data on this quantity should be

\star Research supported in part by the UK Science and Engineering Research Council and in part by the Italian Ministero della Pubblica Istruzione.

directly comparable with perturbative calculations at the parton level, after small corrections for non-perturbative hadronization effects.

So far, comparisons between the theoretical and experimental thrust distributions have been performed [1-8] using theoretical predictions based on the relevant QCD matrix elements evaluated to second order in the strong coupling α_s [9]. As long as the thrust is not too large, the fixed-order perturbative calculations should be reliable. At large values of T , however, there are terms in higher order that become enhanced by powers of $\ln(1-T)$. In this kinematical region the real expansion parameter is the large effective coupling $\alpha_s \ln^2(1-T)$ and therefore any finite-order perturbative calculation cannot give an accurate evaluation of the cross section. The logarithmic terms need to be identified and resummed to all orders in α_s before a reliable prediction can be made.

The appearance of large double logarithmic terms is a common feature of any hard process in the semi-inclusive or Sudakov region, where emission of radiation is inhibited by the kinematics. In the case of jet cross sections at $1-T \ll 1$, the jet invariant masses are constrained to be so small as to allow only emission of gluons that are soft and collinear with respect to the parton generating the jet. The double logarithmic terms $\alpha_s \ln^2(1-T)$ are due to such soft and collinear gluons.

α_s). These are normally classified as *leading* logarithms when $n < m \leq 2n$, *next-to-leading* when $m = n$, and *sub-dominant* when $m < n$. In the next section we

resum all leading and next-to-leading terms, neglecting only the sub-dominant logarithms.

2. Calculation

For a final-state configuration corresponding to a large value of the thrust, eq. (1) can be approximated by

$$1-T \approx (k_1^2 + k_2^2)/Q^2, \quad (5)$$

where k_1^2 and k_2^2 are the invariant masses-squared of two back-to-back jets. Thus the key to the evaluation of the thrust distribution is its relation to the jet mass distribution, which was introduced in refs. [11,12] and calculated to next-to-leading logarithmic accuracy in ref. [17]. If $J(Q^2, k^2)$ denotes the probability distribution of jet invariant mass-squared k^2 at scale Q^2 , then to this accuracy the thrust fraction R takes the form

$$R(\tau, \alpha_s(Q^2)) = \Sigma(\tau, \alpha_s(Q^2)) \\ = \int_0^\infty dk_1^2 dk_2^2 J(Q^2, k_1^2) J(Q^2, k_2^2) \\ \times \Theta(\tau Q^2 - k_1^2 - k_2^2), \quad (6)$$

where Θ is the Heaviside step function. It can be shown [18] that corrections to eq. (5), as well as kinematic correlations between the jet masses and overlap between the jets, give only contributions that are sub-dominant in the sense defined above. Introducing the Laplace transform of the jet mass distribution,

$$\tilde{J}_i(Q^2) = \int_0^\infty dk^2 J(Q^2, k^2) e^{-\nu k^2}, \quad (7)$$

and using the integral representation

$$\Theta(\tau Q^2 - k^2) = \int_{-\infty}^{\tau Q^2 - k^2} \frac{dN}{2\pi i} \frac{e^{N\tau}}{N} e^{-Nk^2/Q^2}, \quad (8)$$

we find that

$$\Sigma(\tau, \alpha_s(Q^2)) = \int_{-\infty}^{\tau Q^2} \frac{dN}{2\pi i} \frac{e^{N\tau}}{N} [\tilde{J}_{N/Q^2}(Q^2)]^2, \quad (9)$$

Resummation of large logarithms in e^+e^- event shape distributions \star

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We describe a method for the resummation of leading and next-to-leading large logarithms to all orders in QCD perturbation theory, applicable to e^+e^- event shape distributions that have the property of exponentiation near the two-jet region. After a general discussion of the conditions for exponentiation and the evaluation of matrix elements and phase space to next-to-leading logarithmic accuracy, we give details of the application of the method to the thrust and heavy jet mass distributions. We show how the resummed expressions can be matched with known second-order results to obtain improved predictions throughout the whole of phase space, and how to suppress spurious higher-order terms generated by resummation outside the physical region. We also give the necessary ingredients for the improvement of third-order predictions by resummation when they become available.

1. Introduction

The measurement of hadronic event shape parameters in e^+e^- annihilation is one of the most important ways in which QCD can be tested and its coupling constant α_s determined. The recent flood of very accurate data from the LEP experiments has brought about a situation in which the theoretical uncertainties

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¹ On leave of absence from INFN, Sezione di Firenze, Italy.

² On leave of absence from Cavendish Laboratory, University of Cambridge, UK

when α_s is small, a perturbative treatment of the shape distribution only appear to make sense when $\alpha_s L^2$ is also small, which excludes a large part of the two-jet configuration, where most of the events occur. Whenever $\alpha_s L^2$ is still small, we can improve the range and accuracy of perturbative predictions by identifying these logarithmically-enhanced terms and resumming them to all orders.

A full understanding of logarithmically-enhanced terms now exists for a class of shape variables, namely those for which the leading logarithmic terms exponentiate. By this we mean that at small y the logarithm of the cross section takes the form

$$\ln R(y) \sim L g_1(\alpha_s L), \quad (4)$$

where the function g_1 has a power series expansion in $\alpha_s L$. More precisely, the exponentiation of QCD matrix elements in the two-jet region implies that, in phase space by which $R(y)$ is defined also has factorization properties which shall specify, then

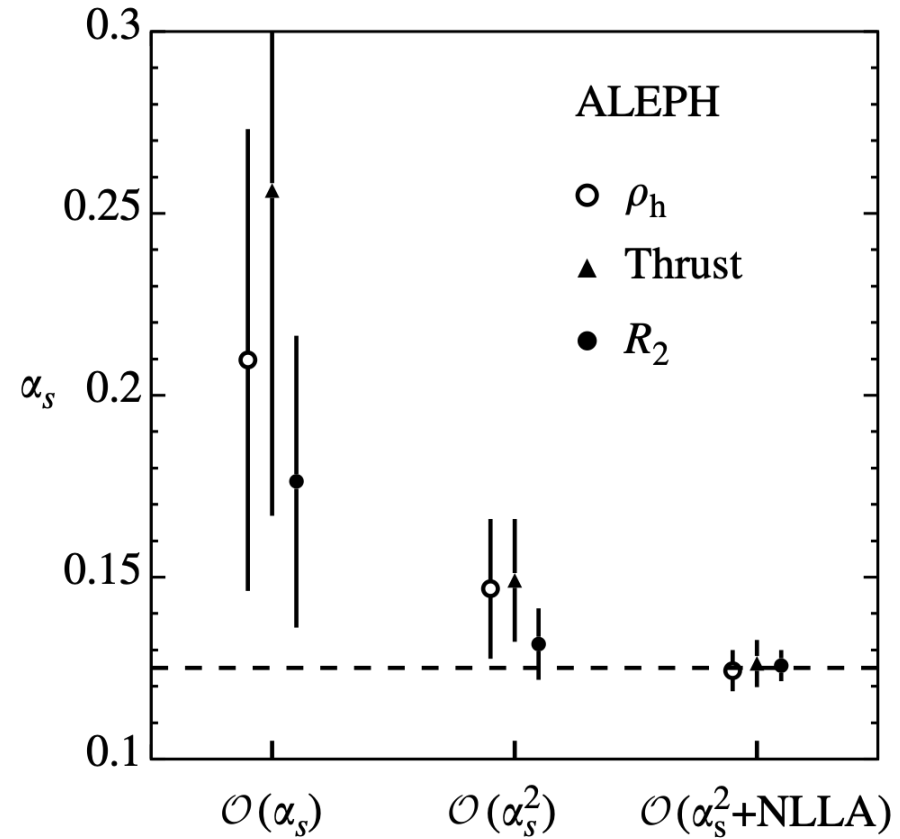
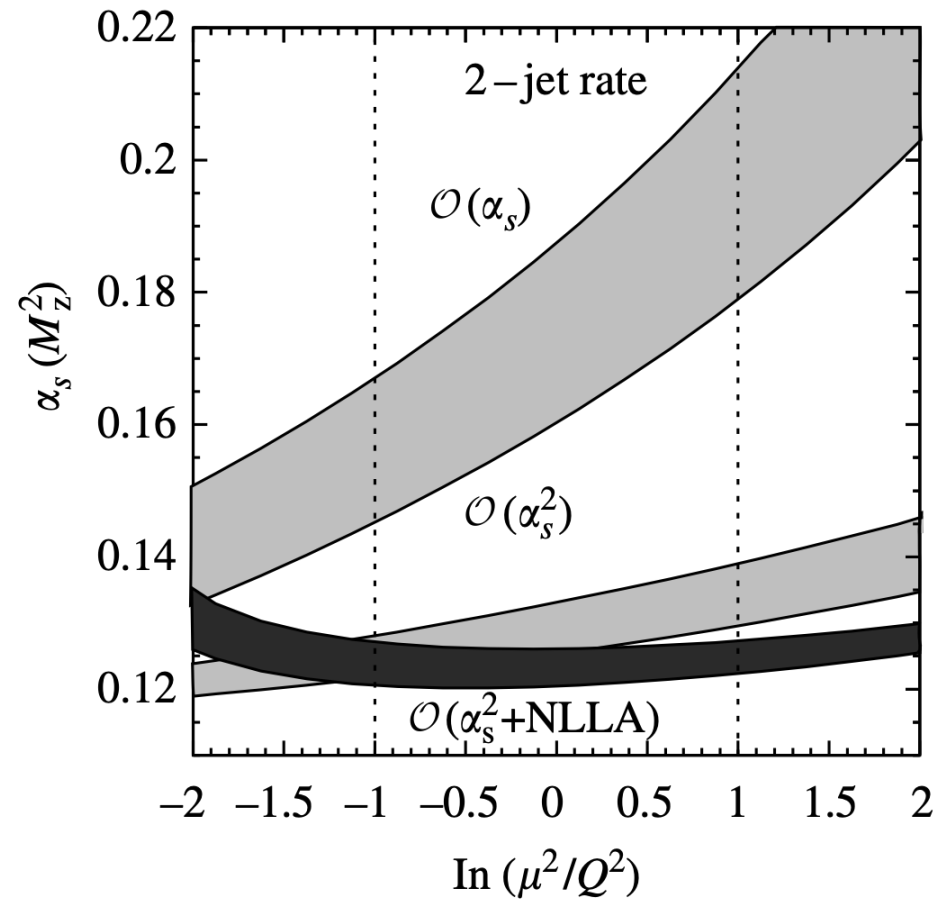
$$R(y) = C(\alpha_s) \Sigma(y, \alpha_s) + D(y, \alpha_s), \quad (5)$$

$$C(\alpha_s) = 1 + \sum_{n=1}^{\infty} C_n \alpha_s^n, \\ \ln \Sigma(y, \alpha_s) = \sum_{n=1}^{\infty} \sum_{m=1}^{n+1} G_{nm} \alpha_s^n L^m \\ = L g_1(\alpha_s L) + g_2(\alpha_s L) + \alpha_s g_3(\alpha_s L) + \dots, \quad (6)$$

where C_n vanishes as $y \rightarrow 0$ order-by-order in perturbation theory. For later convenience we have defined $\tilde{\alpha}_s = \alpha_s/2\pi$ in the expansions. The word exponentiation refers to the fact that the terms $\alpha_s^n L^m$ with $m > n+1$ are absent from $\Sigma(y, \alpha_s)$ whereas they do appear in $R(y)$ itself. The function g_1 resums all the contributions $\alpha_s^n L^{n+1}$, while g_2 contains the *next-to-leading* logarithmic terms $\alpha_s^n L^n$, and g_3 etc. represent the remaining *subdominant* logarithmic corrections $\alpha_s^n L^m$ with $0 < m < n$. All the functions g_i vanish at $L = 0$ since they resum terms with $m > 0$.

Eq. (6) represents an improved perturbative expansion in the small- y region. If we can find the form of the functions g_i , then we shall have a systematic perturbative treatment of the shape distribution throughout the region of y in which $\alpha_s L \lesssim 1$, which is much larger than the domain $\alpha_s L^2 \ll 1$ in which the non-exponentiated perturbation series was applicable. Furthermore, the resummed expression (6) can be consistently matched with fixed-order calculations. In particular, one can evaluate the leading and next-to-leading functions g_1 and g_2 and combine them with the known order- α_s^2 results on the shape cross section,

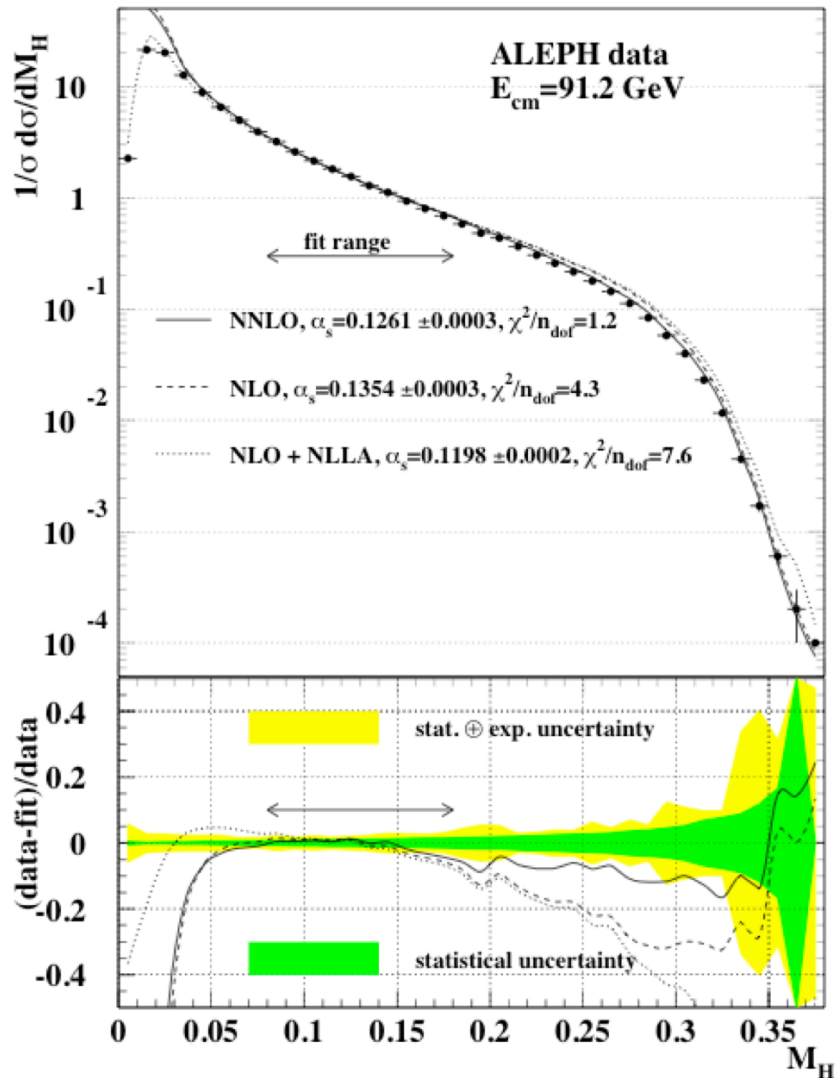
The path from NLO to NLO+NLL



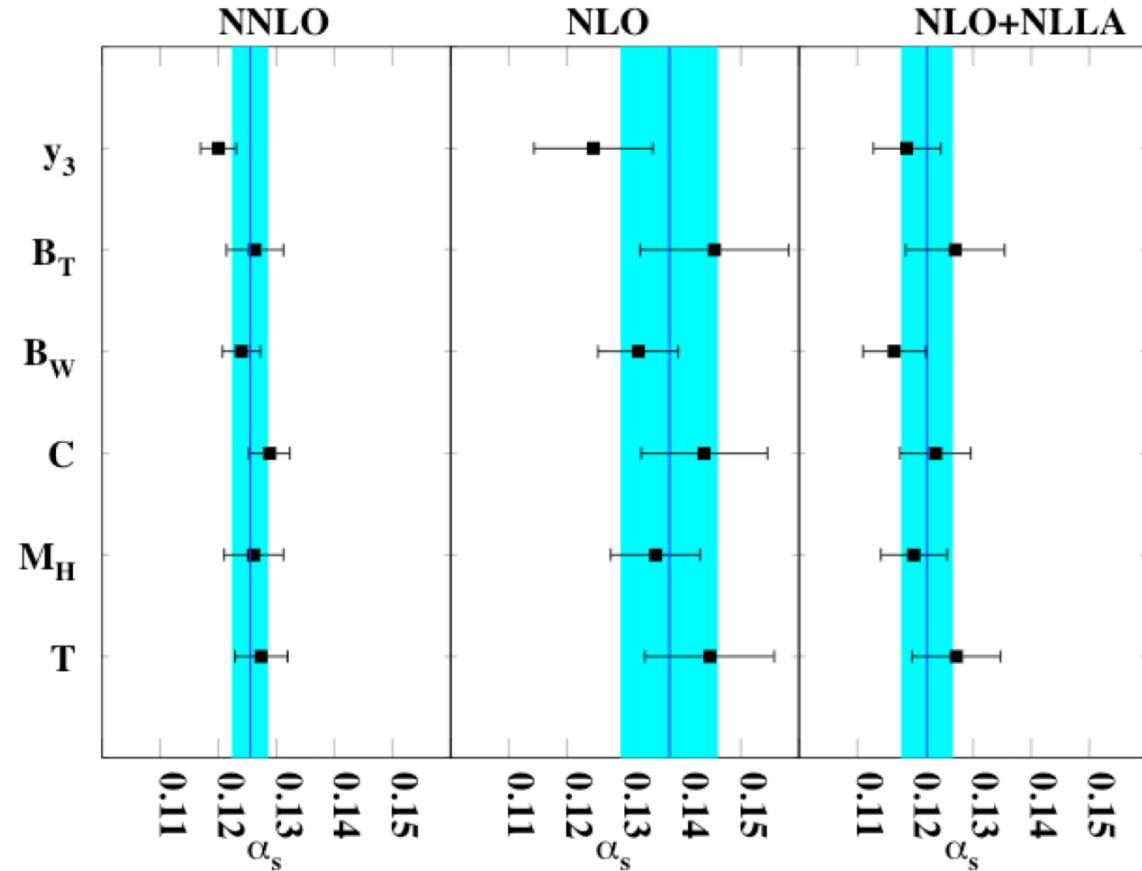
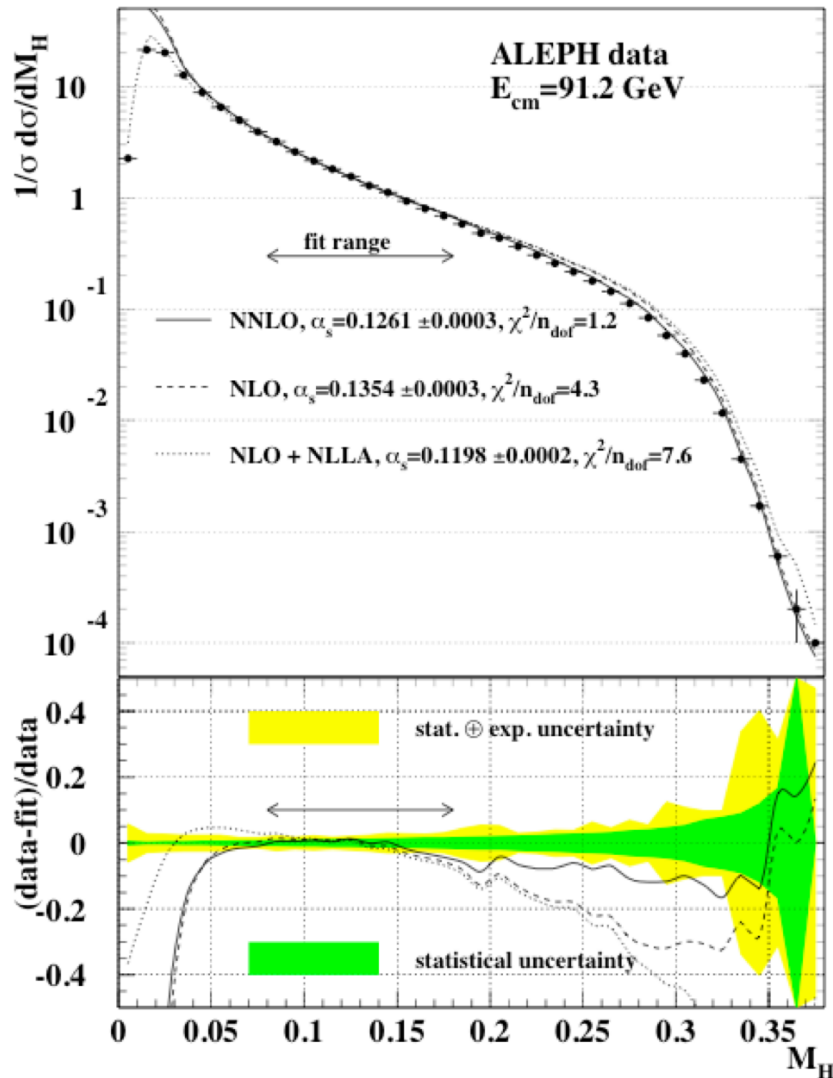
Resummation matched to NLO, typical results

$$\alpha_s(M_Z) \approx 0.120 \pm 0.005$$

The path from NLO to NLO+NLL, and the dawn of the NNLO era



The path from NLO to NLO+NLL, and the dawn of the NNLO era

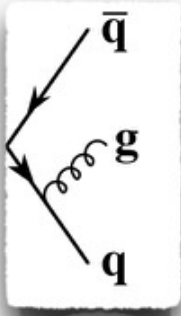


much less scatter at NNLO, reduced pert. uncertainty : 0.003

$$\alpha_s(M_Z^2) = 0.1240 \pm 0.0008 \text{ (stat)} \pm 0.0010 \text{ (exp)} \pm 0.0011 \text{ (had)} \pm 0.0029 \text{ (theo)}$$

Th. Gehrmann, A. Gehrmann-DeRidder, G. Heinrich, N. Glover, H. Stenzel, GD, JHEP 2008, 040, arXiv:0712.0327

Jet algorithms



$$y_{ij} = \frac{2 \min(E_i^2, E_j^2) (1 - \cos \theta_{ij})}{E_{\text{cm}}^2} \approx \frac{k_{\perp}^2}{E_{\text{cm}}^2} \quad \text{"Durham" Jet Algo}$$

$$\frac{\alpha_s}{E_G (1 - \cos \theta_{QG})}$$

1420 citations

Physics Letters B 269 (1991) 432–438
North-Holland

PHYSICS LETTERS B

**New clustering algorithm
for multijet cross sections in e^+e^- annihilation[☆]**

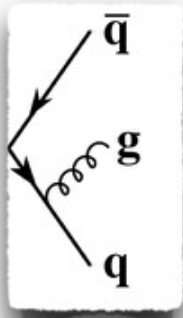
S. Catani^{a,b,1}, Yu.L. Dokshitzer^{c,d}, M. Olsson^d, G. Turnock^a and B.R. Webber^a

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^d Department of Theoretical Physics, University of Lund, Sölvegatan 14A, S-22362 Lund, Sweden

Received 2 August 1991

Cross sections for $e^+e^- \rightarrow n$ -jets, as functions of the jet resolution parameter y_{cut} , are computed according to a new clustering algorithm. The jet multiplicity n is defined in such a way that jets i and j with energies E_i and E_j at relative angle θ_{ij} are resolved if $y_{ij} = 2(1 - \cos \theta_{ij}) \min(E_i^2, E_j^2) / s > y_{\text{cut}}$, where s is the centre-of-mass energy squared. Using this algorithm, large higher-order corrections at small values of y_{cut} can easily be evaluated. Our calculations include resummation of leading and next-to-leading logarithms of y_{cut} to all orders in QCD perturbation theory. This enables us to predict the jet cross sections at small y_{cut} for arbitrary n . Simple analytical results for $n \leq 5$ are presented.

Jet algorithms



$$\frac{\alpha_s}{E_G (1 - \cos \theta_{QG})}$$

$$y_{ij} = \frac{2 \min(E_i^2, E_j^2) (1 - \cos \theta_{ij})}{E_{cm}^2} \approx \frac{k_{\perp}^2}{E_{cm}^2} \quad \text{“Durham” Jet Algo}$$

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**New clustering algorithm
for multijet cross sections in e^+e^- annihilation[☆]**

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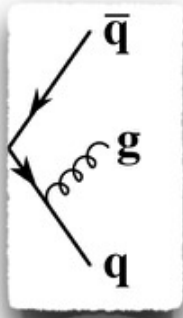
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In the next section we describe a new jet algorithm^{#1} in which relative transverse momentum replaces the invariant mass of the original JADE algorithm as the jet resolution variable. To emphasize this change of variable, we call the new algorithm the k_{\perp} -algorithm. The use of transverse momentum to resolve jets is suggested by the coherence properties of QCD soft emission [20,21] in order to preserve exponentiation and LPHD.

The results of our calculation are presented in section 3. We study the behaviour of multijet cross sections at small values of the resolution parameter y_{cut} using the k_{\perp} -algorithm. We show that leading and next-to-leading logarithms can be resummed to all orders in α_s for any number of jets and give simple results up to five jets.

^{#1} This algorithm arose from discussions at the Durham Workshop on Jet Studies at LEP and HERA, December 1990, and is sometimes referred to as the Durham algorithm.

Jet algorithms



$$\frac{\alpha_s}{E_G (1 - \cos \theta_{QG})}$$

Nuclear Physics B
Volume 406, Issues 1-2, 27 September 1993, Pages 187-224

ELSEVIER

Longitudinally-invariant k_{\perp} -clustering algorithms for hadron-hadron collisions ☆

S. Catani **, Yu.L. Dokshitzer ^{a,b}, M.H. Seymour, B.R. Webber ***

$$y_{ij} = \frac{2 \min(E_i^2, E_j^2) (1 - \cos \theta_{ij})}{E_{cm}^2} \approx \frac{k_{\perp}^2}{E_{cm}^2} \quad \text{“Durham” Jet Algo}$$

We propose a version of the QCD-motivated “ k_{\perp} ” jet-clustering algorithm for hadron-hadron collisions which is invariant under boosts along the beam directions. This leads to improved factorization properties and closer correspondence to experimental practice at hadron colliders. We examine alternative definitions of the resolution variables and cluster recombination scheme, and show that the algorithm can be implemented efficiently on a computer to provide a full clustering history of each event. Using simulated data at $\sqrt{s} = 1.8$ TeV, we study the effects of calorimeter segmentation, hadronization and the soft underlying event, and compare the results with those obtained using a conventional cone-type algorithm.

In the past few years, a suite of IRC safe algorithm has become widely used

k_t	SR $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ hierarchical in rel p_t	Catani et al '91 Ellis, Soper '93
Cambridge/ Aachen	SR $d_{ij} = \Delta R_{ij}^2 / R^2$ hierarchical in angle	Dokshitzer et al '97 Wengler, Wobish '98
anti- k_t	SR $d_{ij} = \min(k_{ti}^{-2}, k_{tj}^{-2}) \Delta R_{ij}^2 / R^2$ gives perfectly conical hard jets	MC, Salam, Soyez '08 (Delsart, Loch)
SISCone	Seedless iterative cone with split-merge gives 'economical' jets	Salam, Soyez '07

1420 citations

Physics Letters B 269 (1991) 432-438
North-Holland

PHYSICS LETTERS B

New clustering algorithm for multijet cross sections in e^+e^- annihilation ☆

S. Catani ^{a,b,1}, Yu.L. Dokshitzer ^{c,d}, M. Olsson ^d, G. Turnock ^a and B.R. Webber ^a

^a Cavendish Laboratory, University of Cambridge, Madingley Road, Cambridge CB3 0HE, UK
^b INFN, Sezione di Firenze, Largo Fermi 2, I-50125 Florence, Italy
^c Leningrad Nuclear Physics Institute, Gatchina, SU-188 350 Leningrad, USSR
^d Department of Theoretical Physics, University of Lund, Sölvegatan 14A, S-22362 Lund, Sweden

Received 2 August 1991

Cross sections for $e^+e^- \rightarrow n$ -jets, as functions of the jet resolution parameter y_{cut} , are computed according to a new clustering algorithm. The jet multiplicity n is defined in such a way that jets i and j with energies E_i and E_j at relative angle θ_{ij} are resolved if $y_{ij} = 2(1 - \cos \theta_{ij}) \min(E_i^2, E_j^2) / s > y_{cut}$, where s is the centre-of-mass energy squared. Using this algorithm, large higher-order corrections at small values of y_{cut} can easily be evaluated. Our calculations include resummation of leading and next-to-leading logarithms of y_{cut} to all orders in QCD perturbation theory. This enables us to predict the jet cross sections at small y_{cut} for arbitrary n . Simple analytical results for $n \leq 5$ are presented.

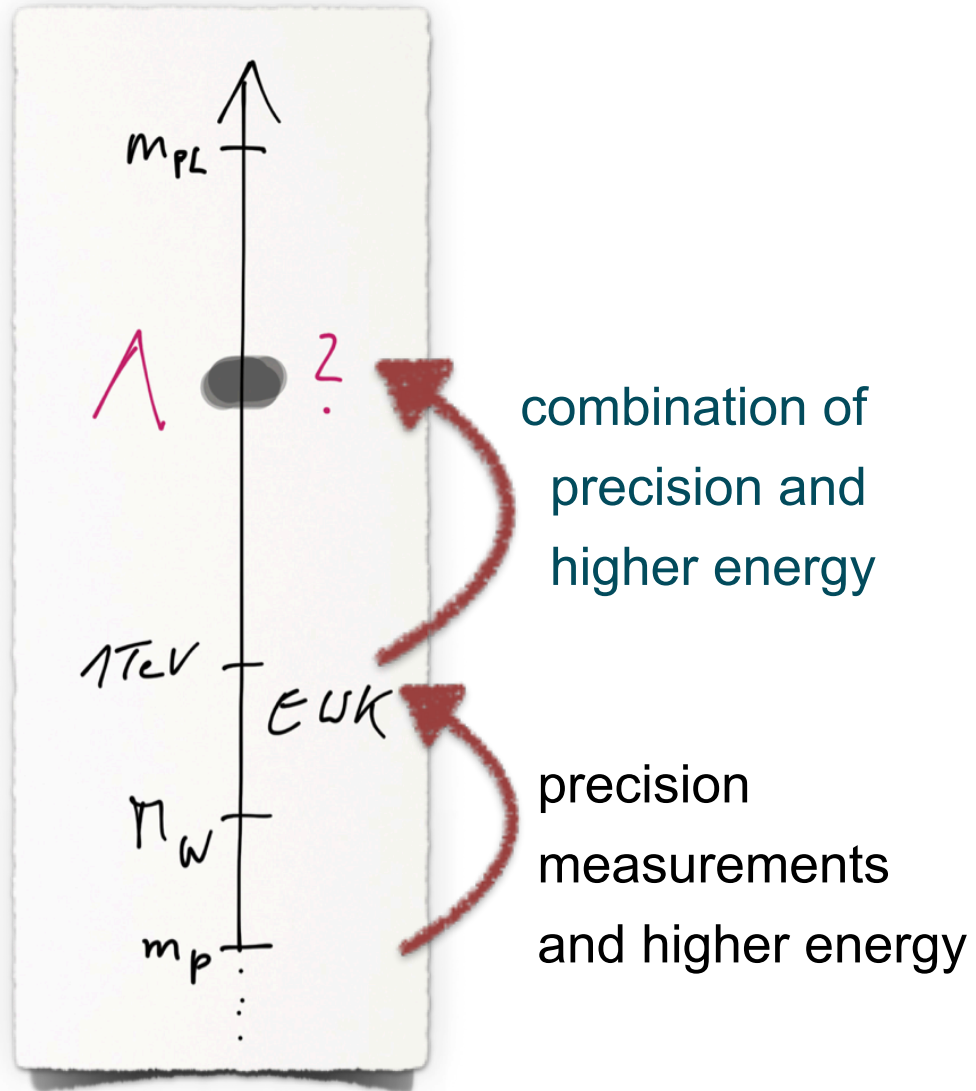
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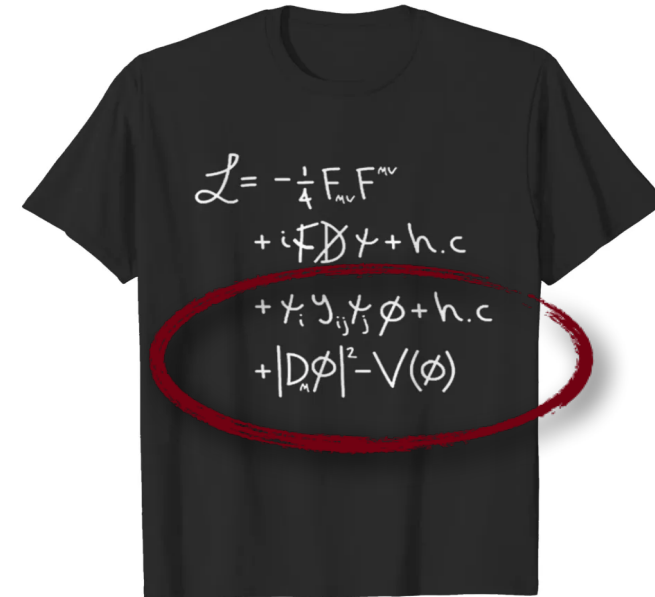
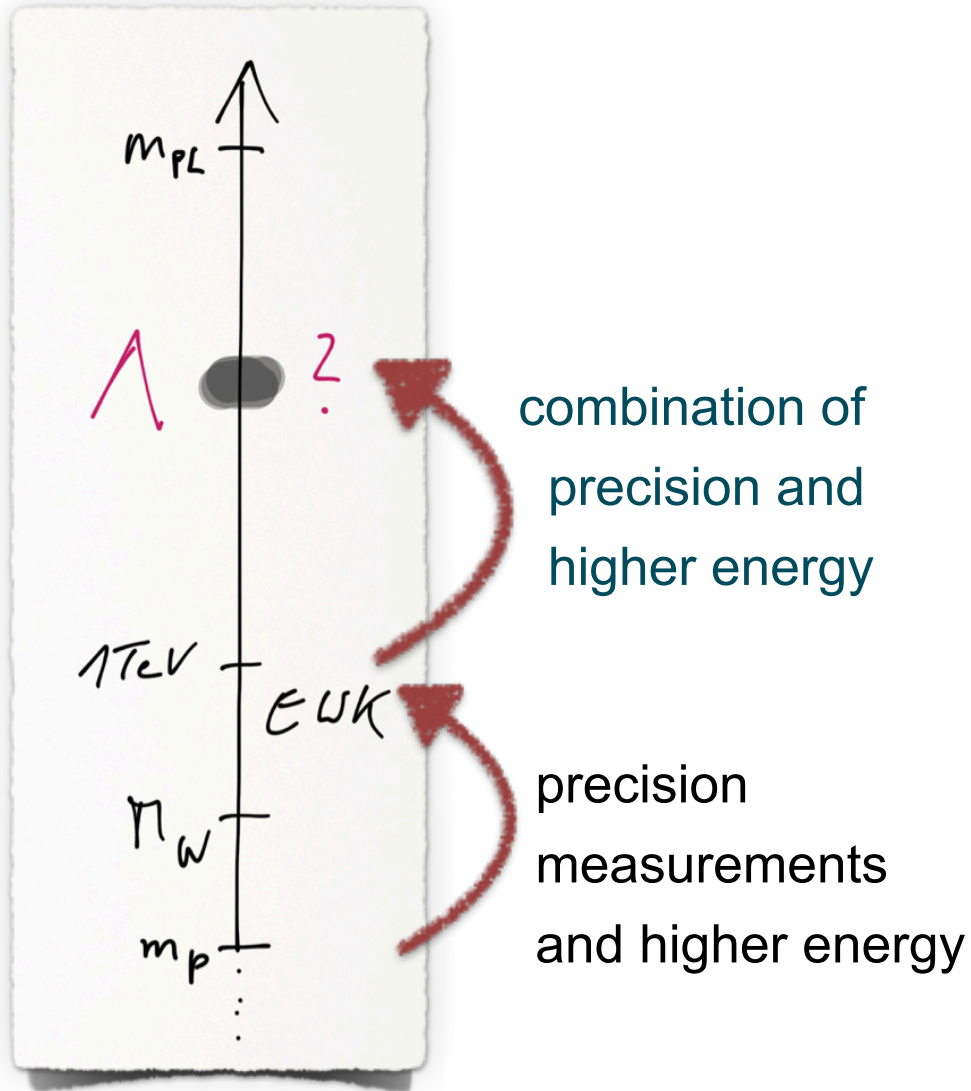
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Now back to our current
LHC times...

New physics needed, but where is it?



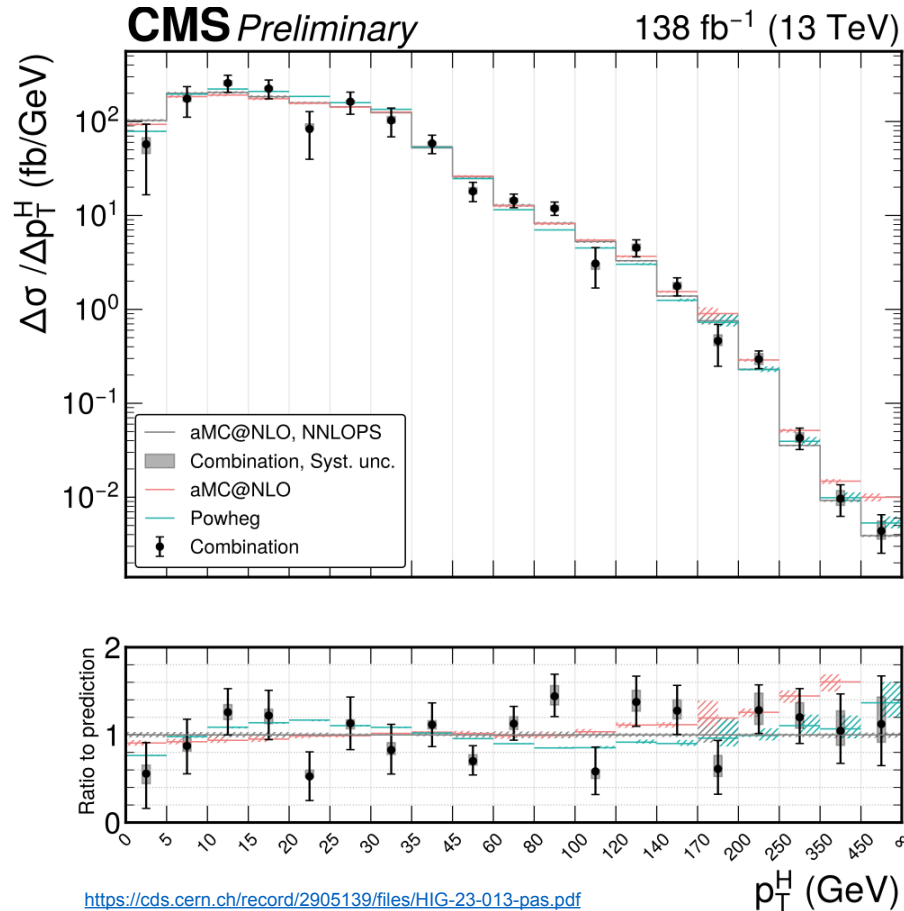
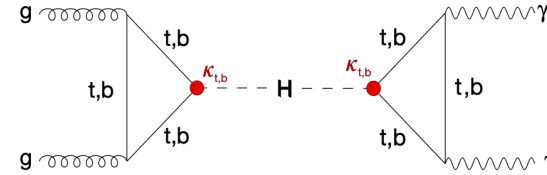
New physics needed, but where is it?



Could the Higgs boson be a gateway to it?

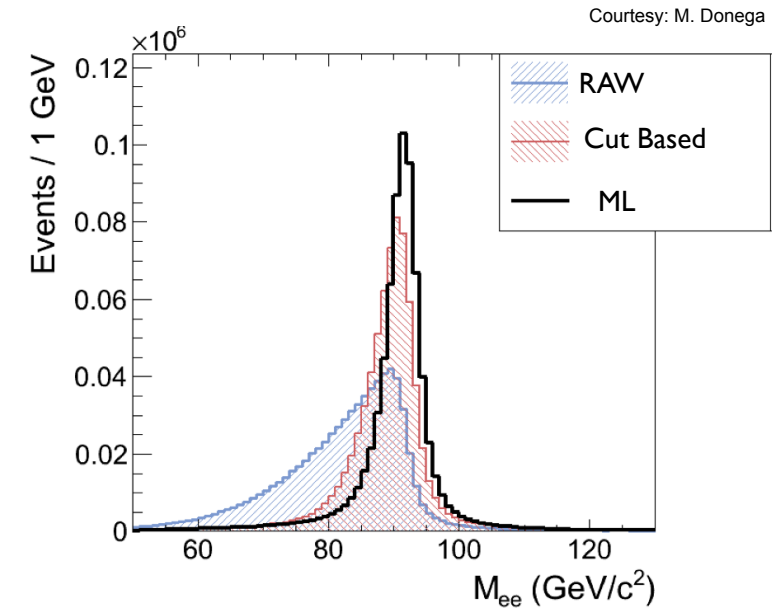
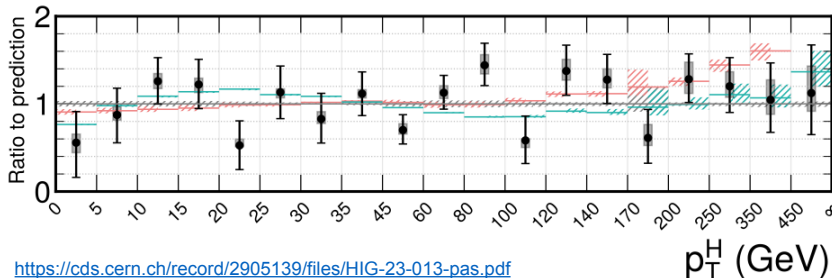
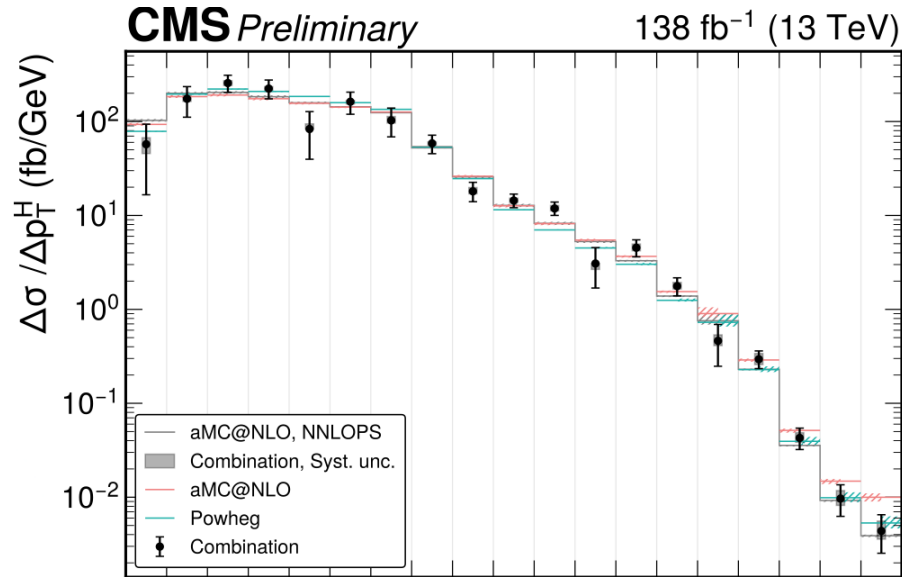
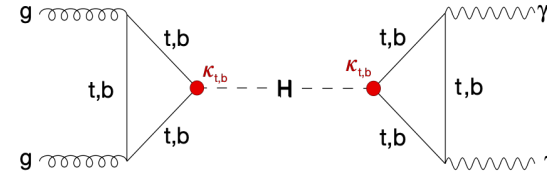
Differential cross sections and importance of exp. precision and tools

Besides incl. cross sections/couplings,
new physics could also
modify the *differential* cross sections



Differential cross sections and importance of exp. precision and tools

Besides incl. cross sections/couplings, new physics could also modify the *differential* cross sections



Thanks to **Machine Learning tools**:
improvements in resolution \rightarrow increases S/\sqrt{B} ,
that can be directly translated to a luminosity gain:

- improve the resolution by 20%
- equivalent to a gain in sensitivity of 10%
- equivalent to a gain in luminosity of 20%

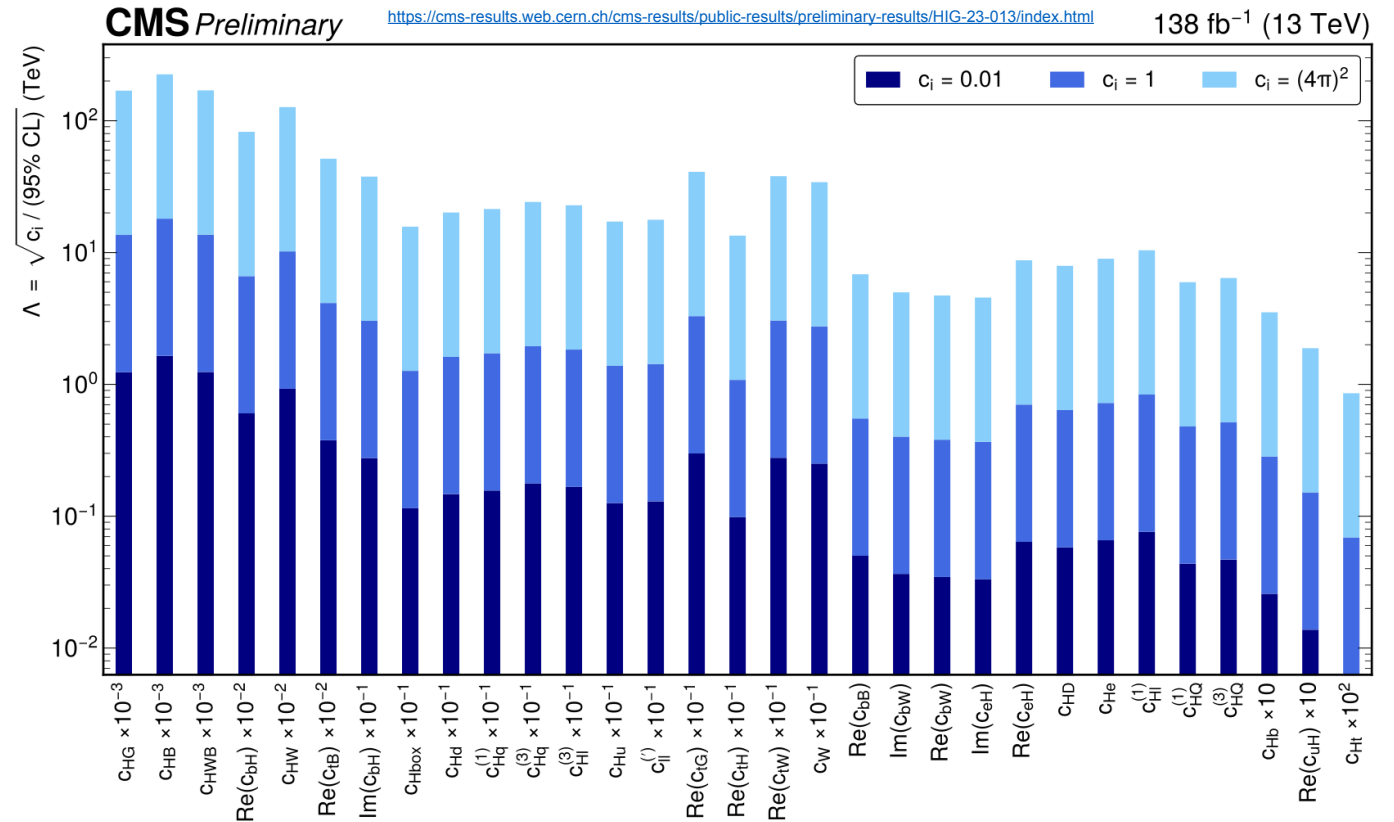
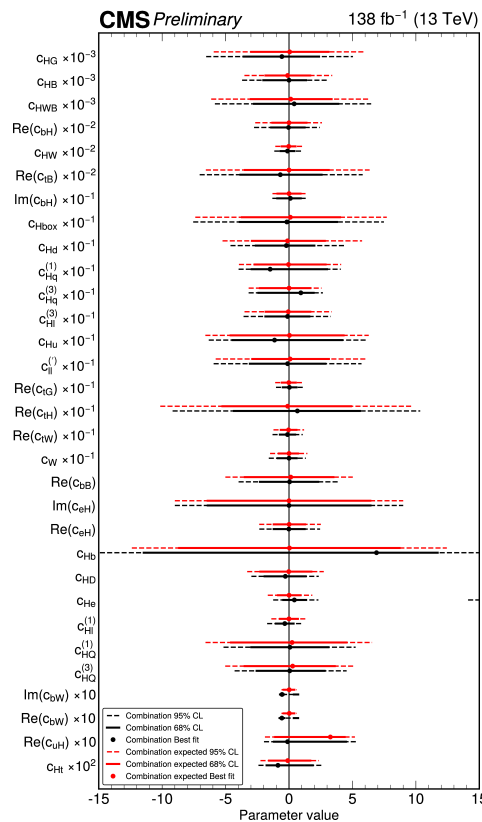
i.e. equivalent to running the LHC for 20% longer time

The Higgs boson is used as a „search tool“, already now

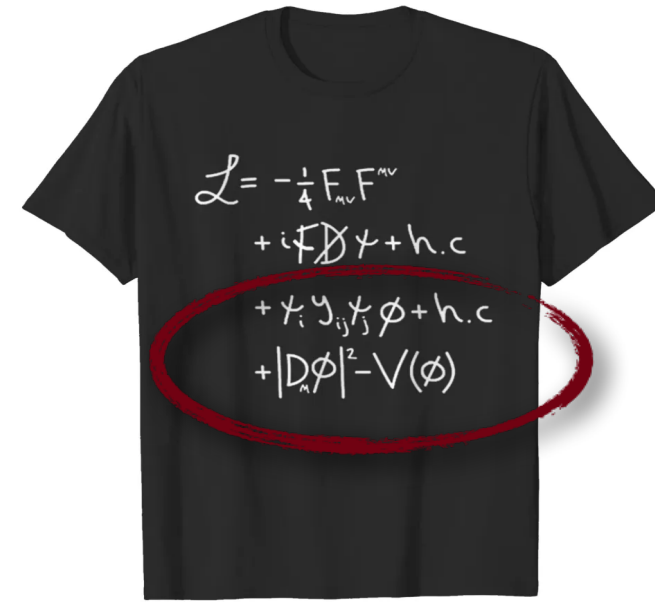
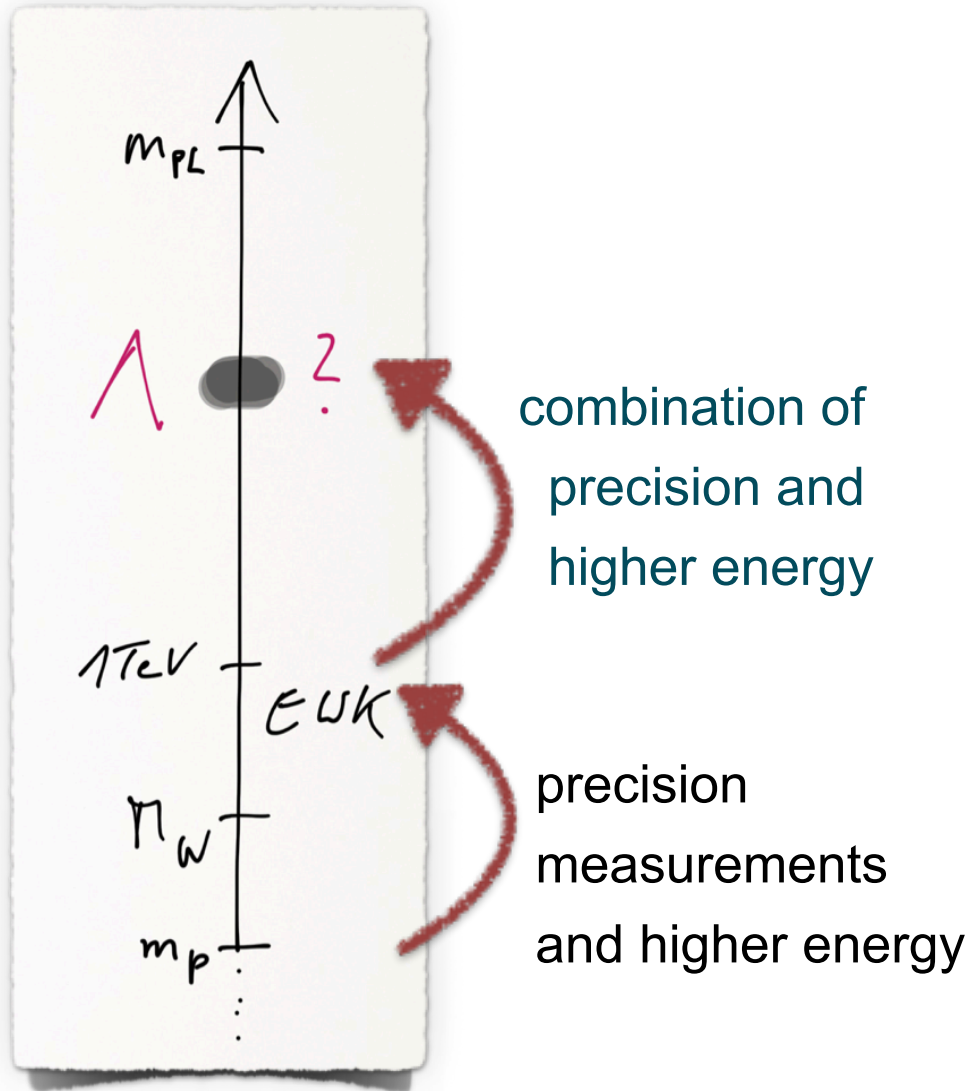
Example from CMS PAS HIG-23-013

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{j=0}^{2499} \frac{c_j^{(6)}}{\Lambda^2} O_j^{(6)}$$

$$L(\vec{x}|\vec{\mu}, \vec{\nu}) = \prod_n p\left(\vec{x} \left| \sum_{if} \mu_{if}(\vec{c}) S_{if,n}(\vec{\nu}) + B(\vec{\nu}) \right.\right) \cdot \prod_j p(\vec{y}_j|\vec{\nu}_j)$$

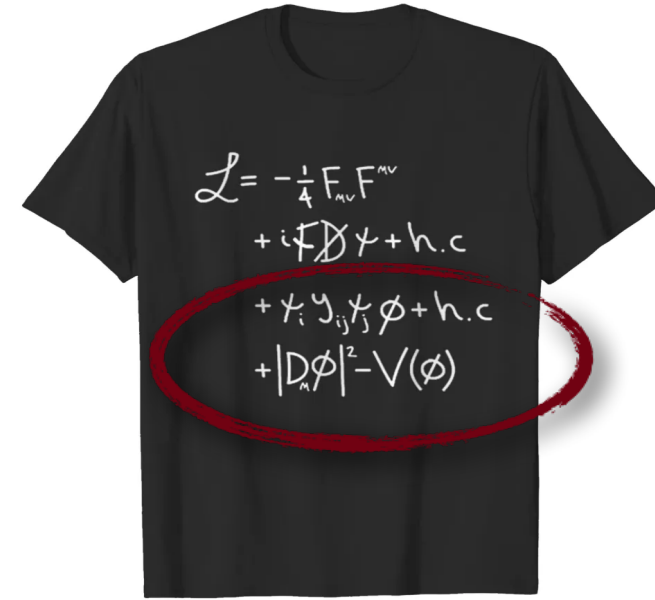
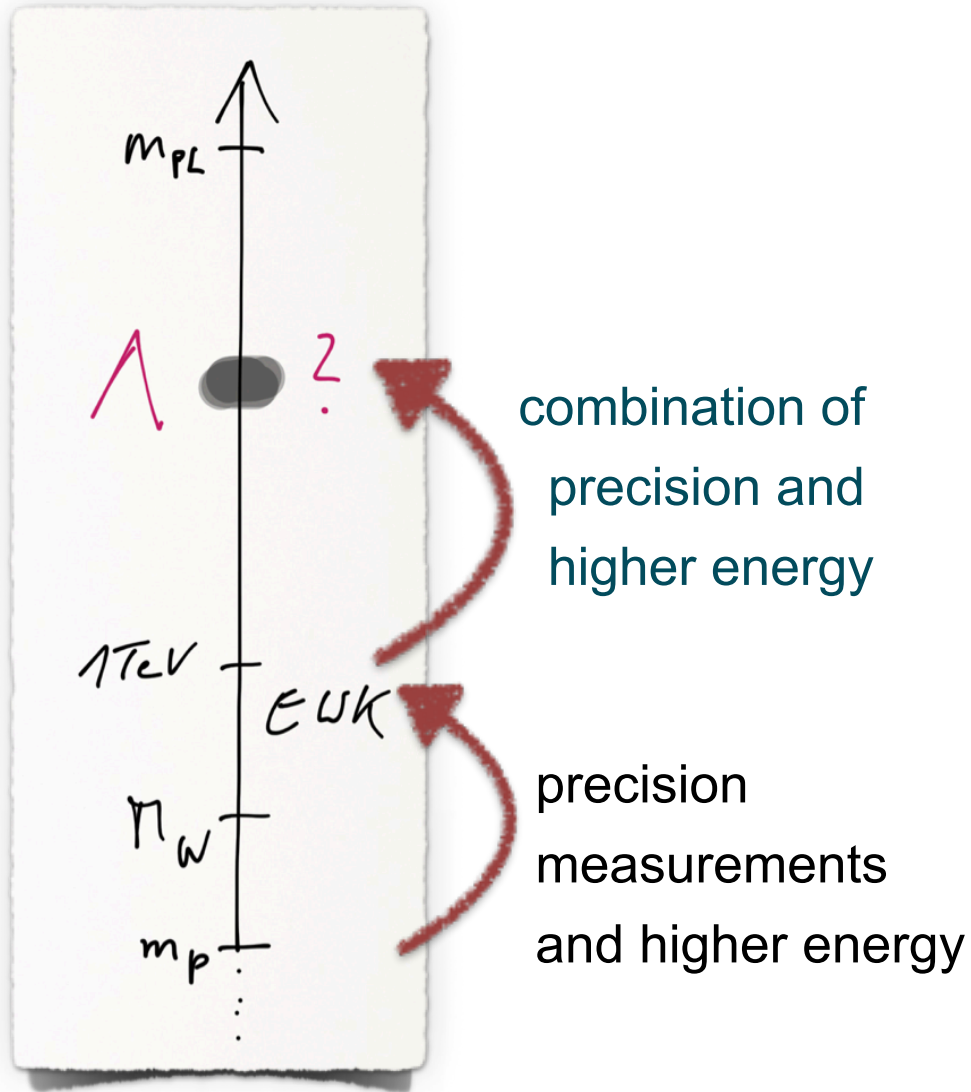


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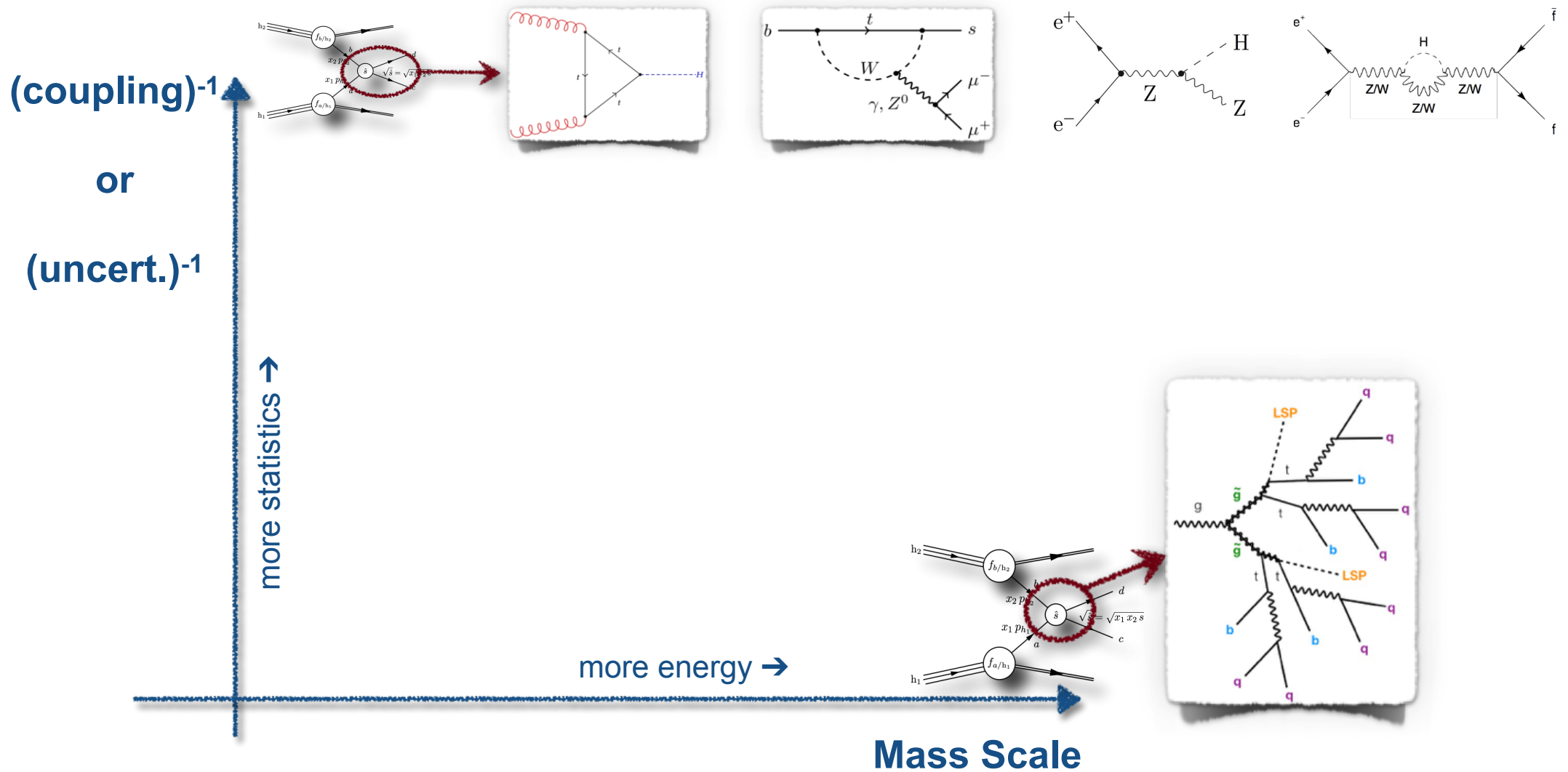
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Consensus (?) regarding a e^+e^- Higgs factory as next step, beyond HL-LHC

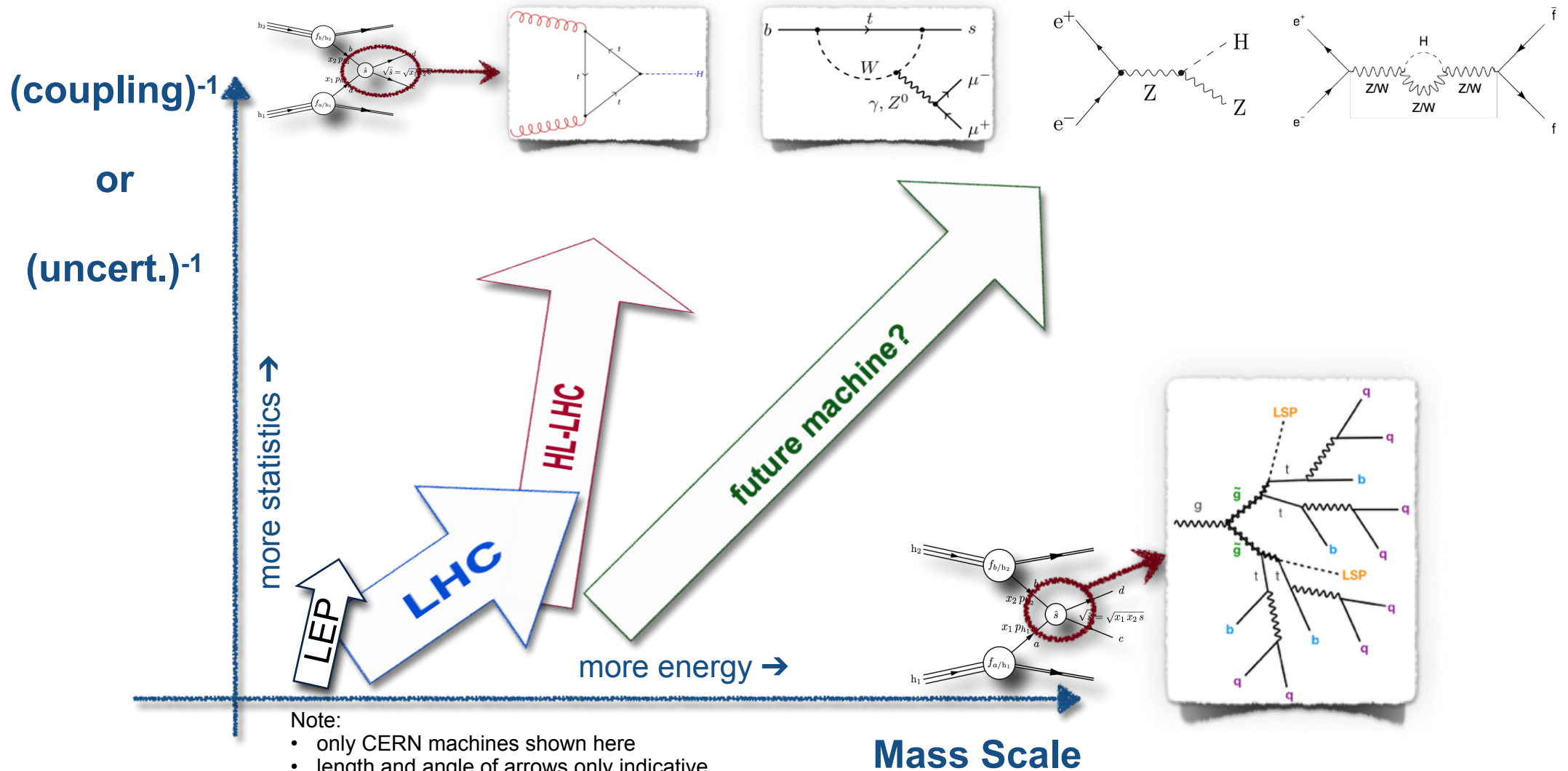
In any case: We are in an exploratory phase!

Actually, this is the "normal" case...

Remember: How to explore the unknown

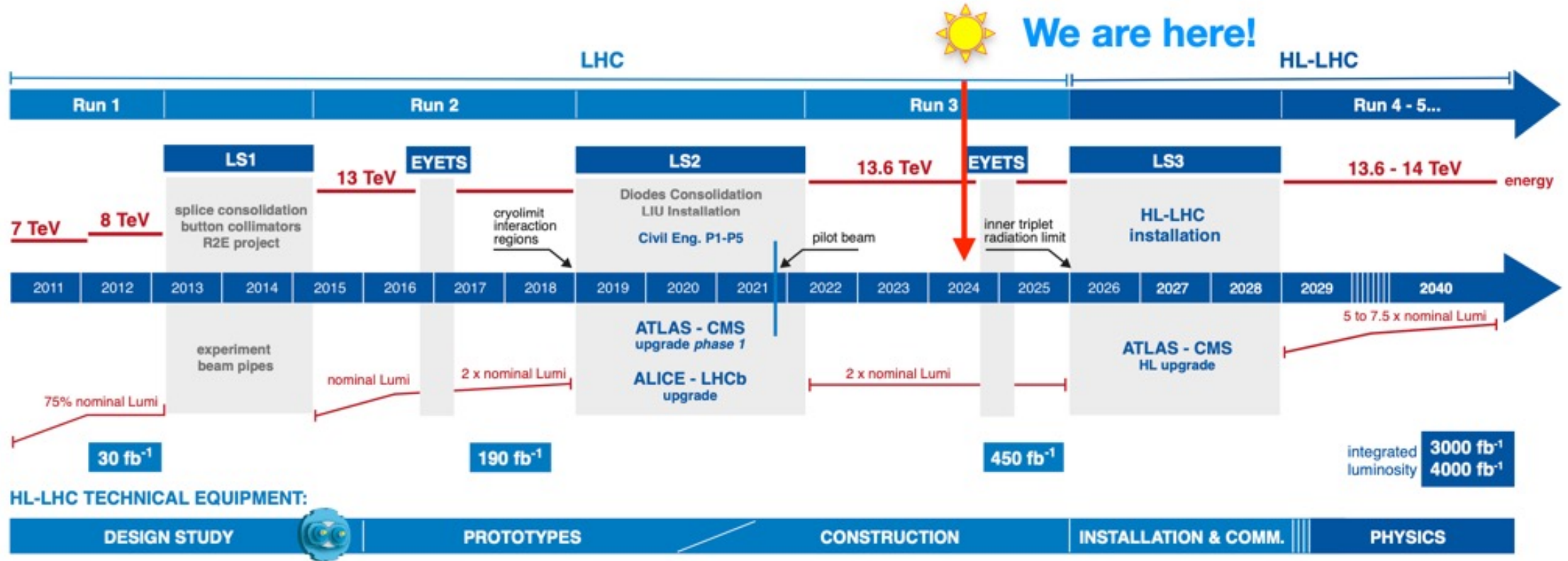


Remember: How to explore the unknown



The future (?)

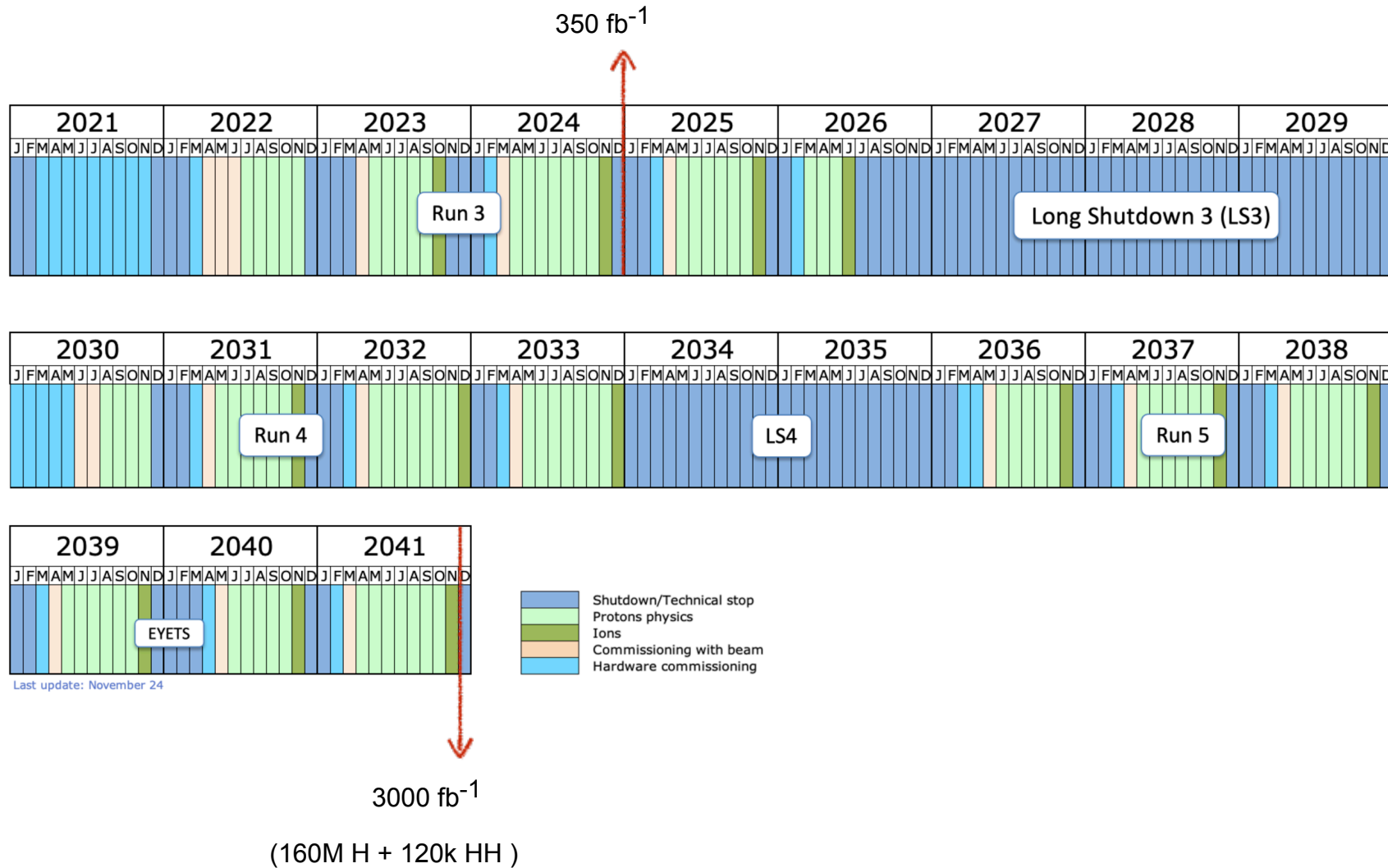
The imminent future, HL-LHC: Failure is not an option....



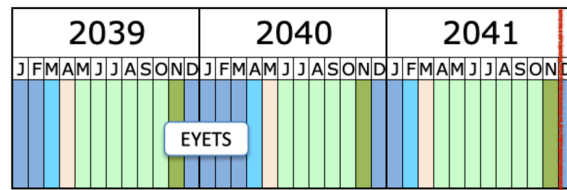
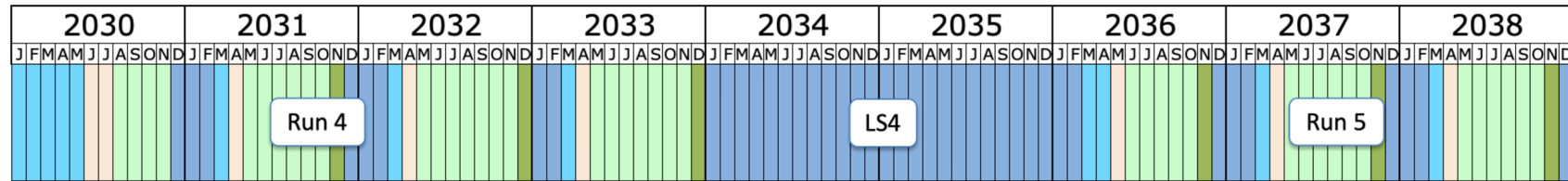
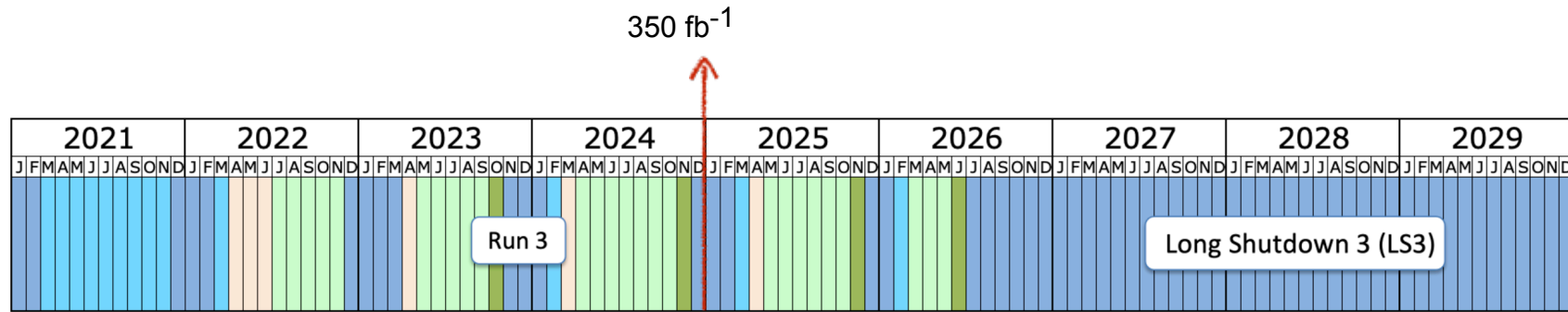
Marumi Kado, ICHEP 2024

Current challenge: in parallel data taking, data analyses and upgrades

The imminent future, HL-LHC: Latest schedule update



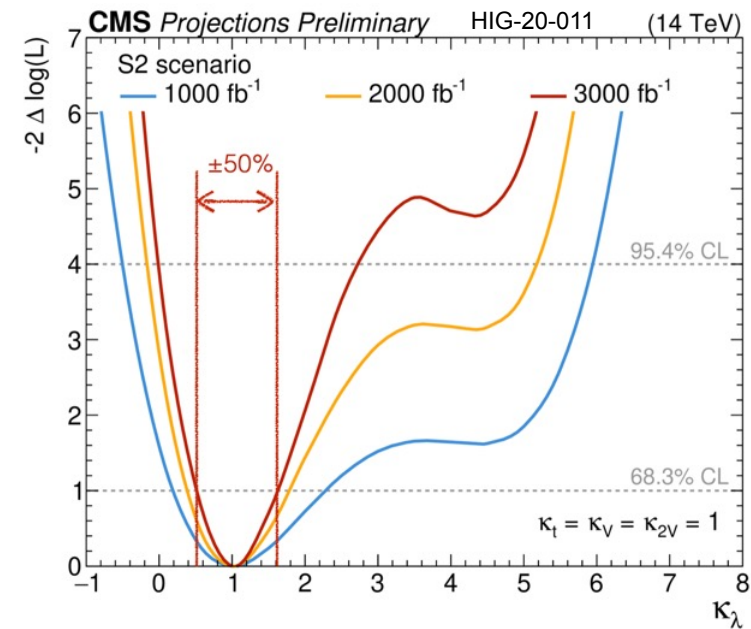
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Last update: November 24

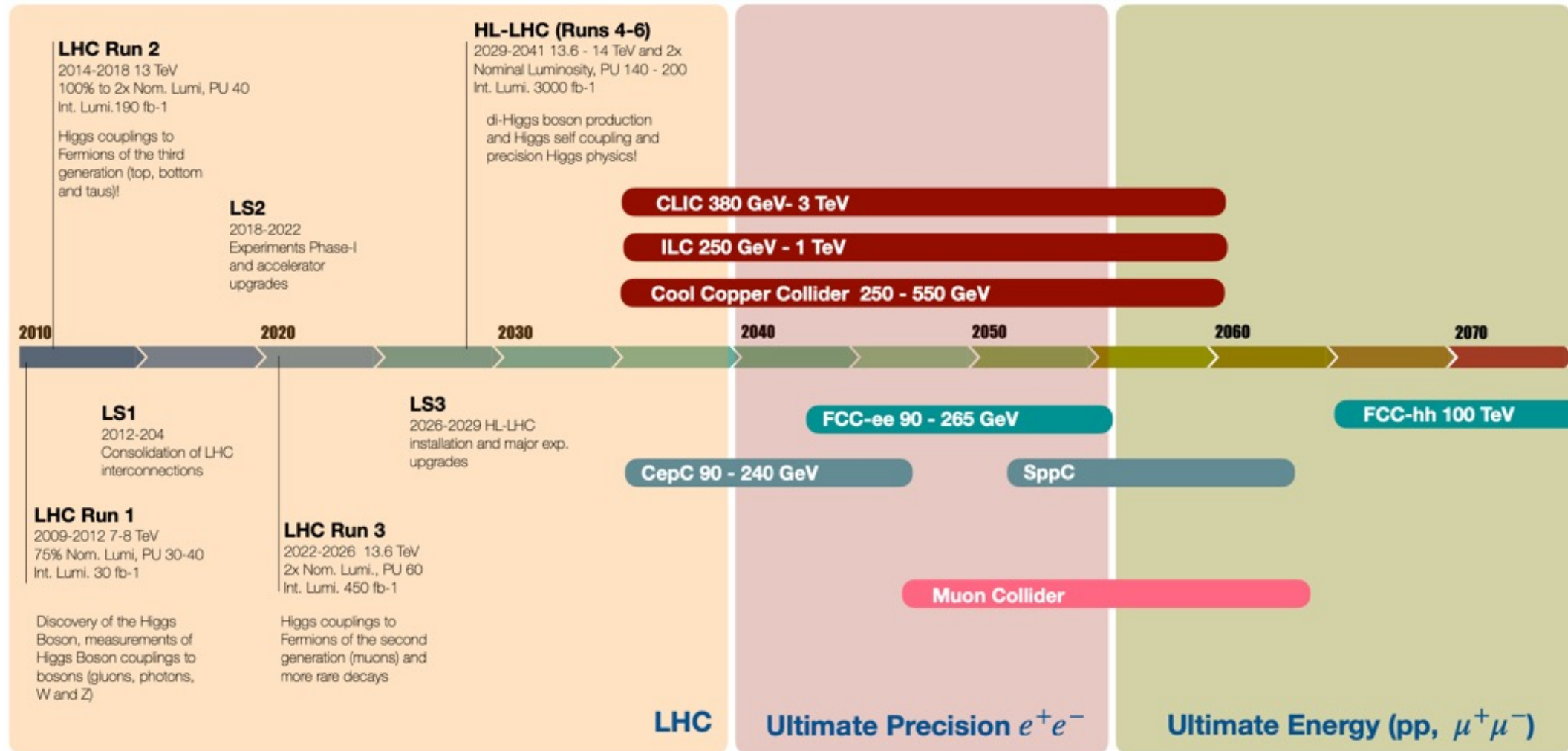
- Shutdown/Technical stop
- Protons physics
- Ions
- Commissioning with beam
- Hardware commissioning

3000 fb⁻¹
(160M H + 120k HH)



A Scientific Mission for the 21st Century

Rende Steerenberg



If you are in an exploratory regime....



If you are in an exploratory regime....



or



?

If you are in an exploratory regime....



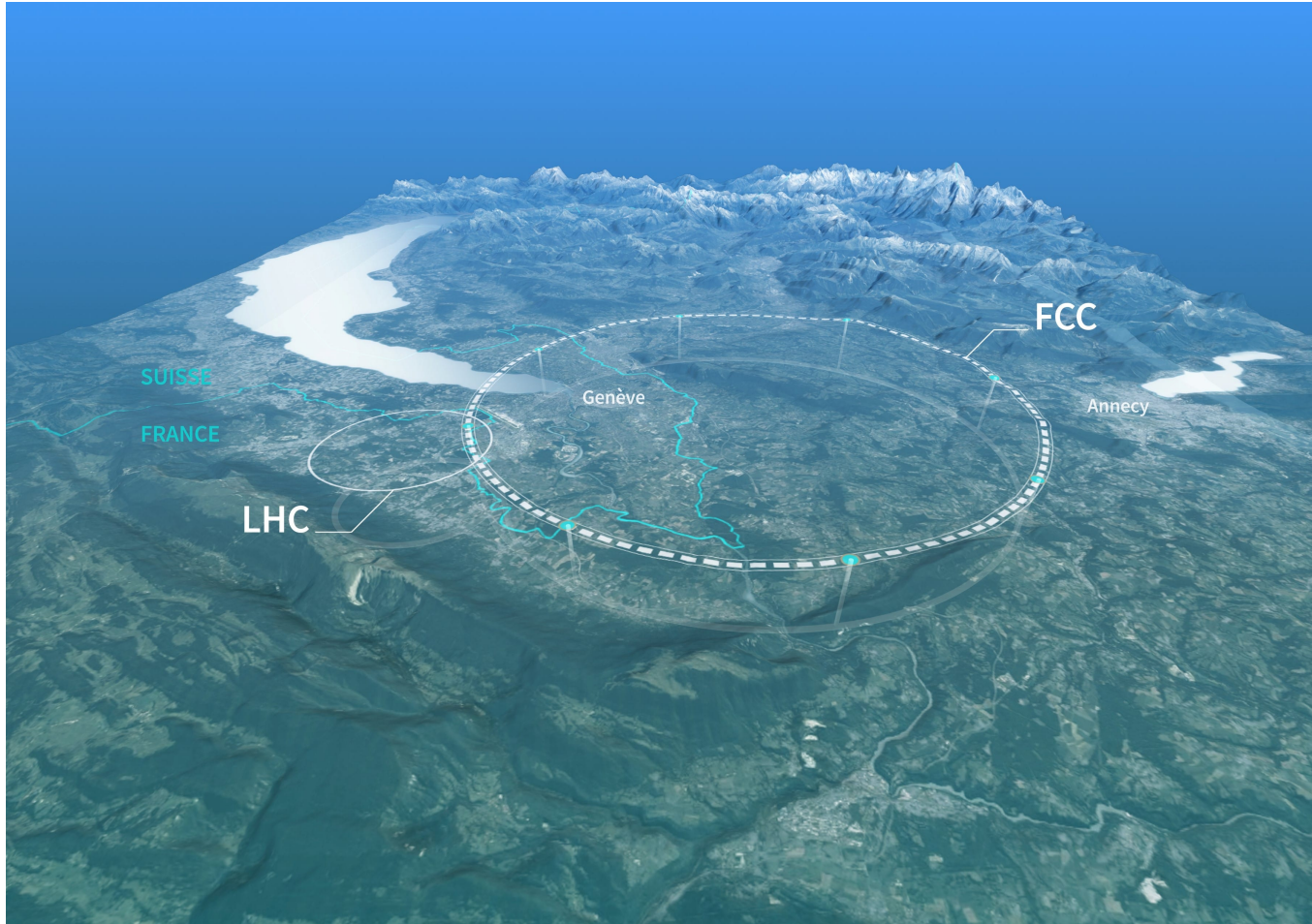
or



?

The **full FCC programme** (ee then hh, and more than one experiment) is the most versatile toolbox among all options on the table!

The FCC programme



<https://home.cern/science/accelerators/future-circular-collider>

FCC IN A NUTSHELL

Timeline

- **2025:** Completion of the FCC Feasibility Study
- **2027–2028:** Decision by CERN Member States and international partners

Tunnel

- **90.7 km** circumference
- **200 m** average depth
- **8 surface points** (7 in France, 1 in Switzerland)

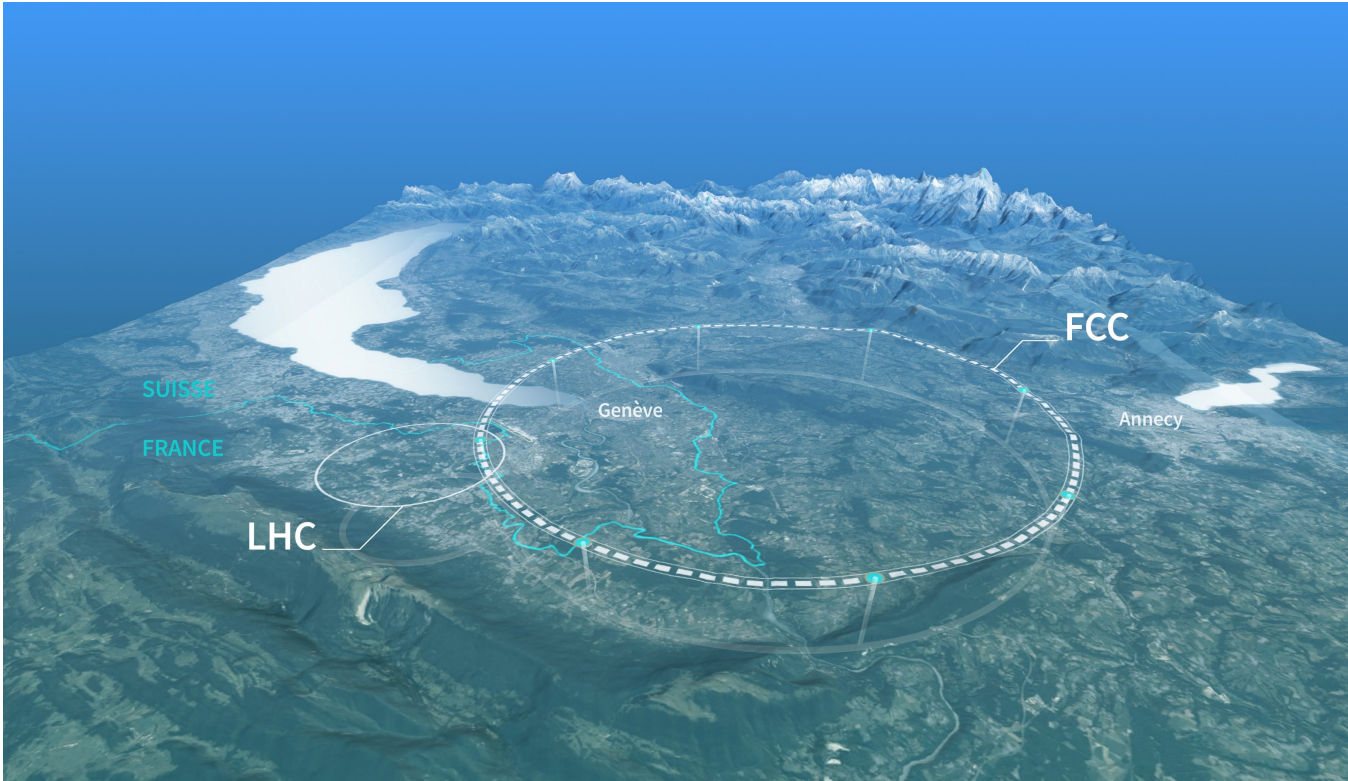
Two stages

- **FCC-ee** (precision measurements) about 15 years from the **mid-2040s**
- **FCC-hh** (high energy) about 25 years from the **2070s**

Costs/benefits

- **15 billion CHF**, spread over at least **15 years** for FCC-ee with four experiments
- Estimated benefit–cost ratio of **1.66**
- About **800 000** person-years of employment created

The FCC programme



- Stage 1: **FCC-ee** (Z, W, H, $t\bar{t}$) as a **Higgs factory**, electroweak & top factory at highest luminosities
- Stage 2: **FCC-hh** (~100 TeV) as natural continuation at energy frontier, **proton-proton** with options



Rende Steernberg, ICHEP 2024

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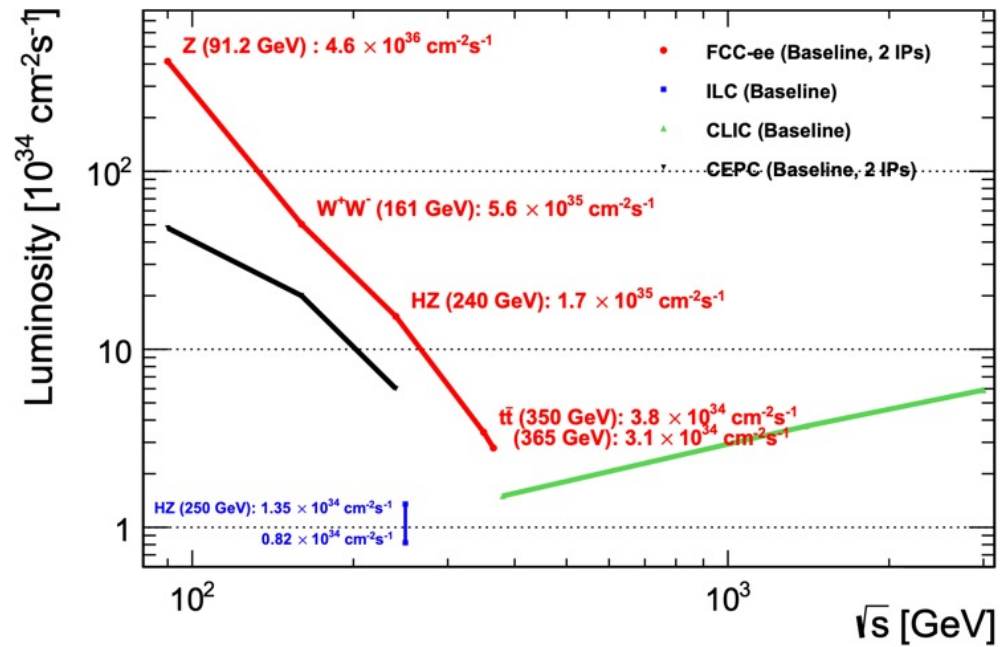
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FCC: promises and challenges

Some examples taken from

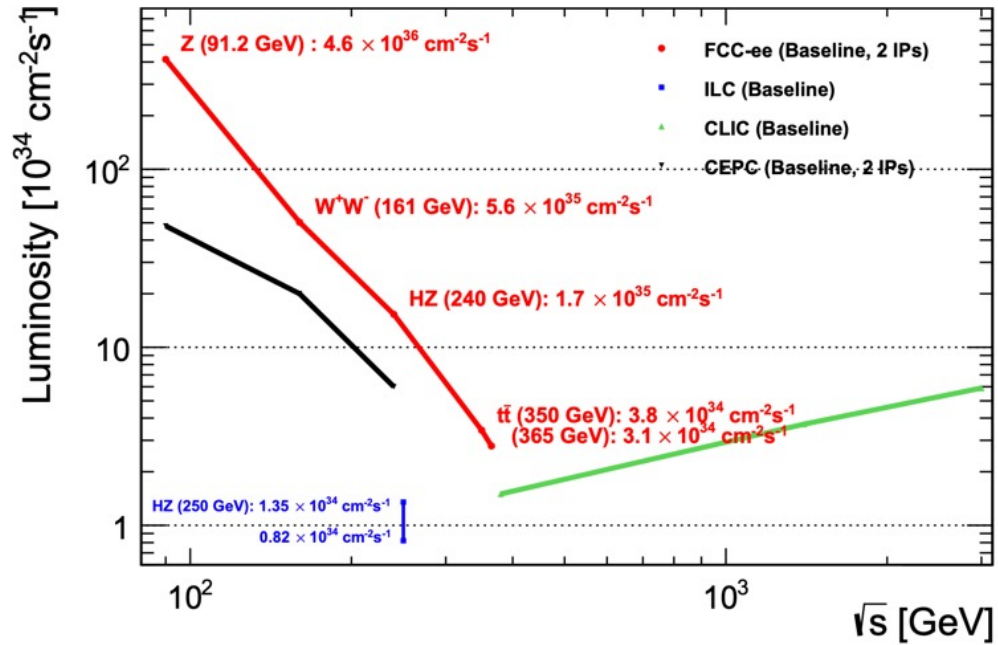
Blondel & Janot, <https://inspirehep.net/literature/1870513>



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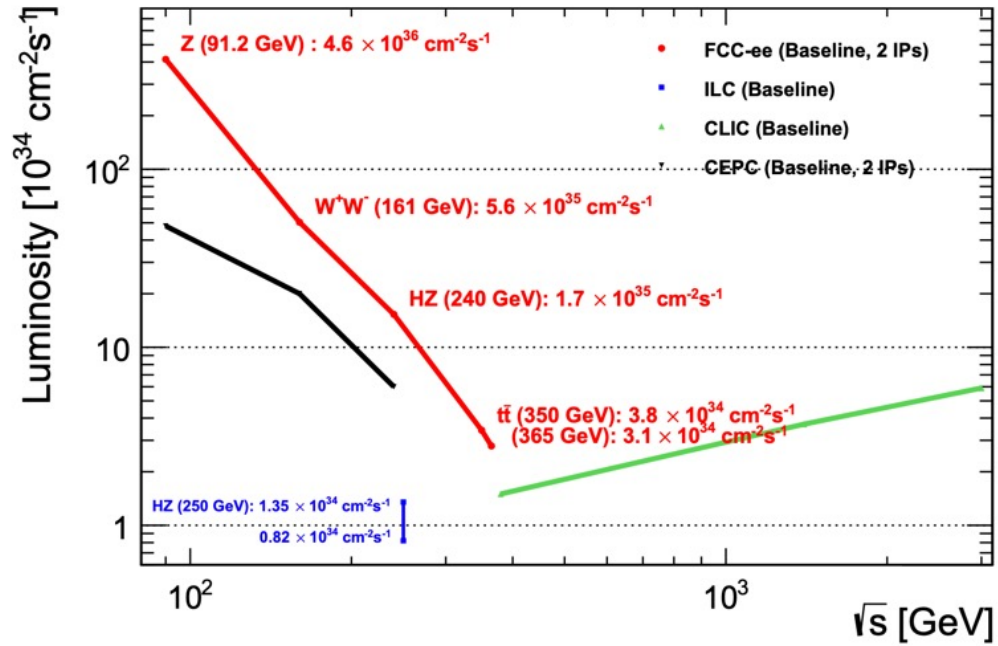
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Collider	HL-LHC	FCC-ee _{240→365}	FCC-INT
Lumi (ab ⁻¹)	3	5 + 0.2 + 1.5	30
Years	10	3 + 1 + 4	25
g_{HZ} (%)	1.5	0.18/0.17	0.17/0.16
g_{HHH} (%)	50	44/33 27/24	3–4
Γ_H (%)	SM	1.1	0.91

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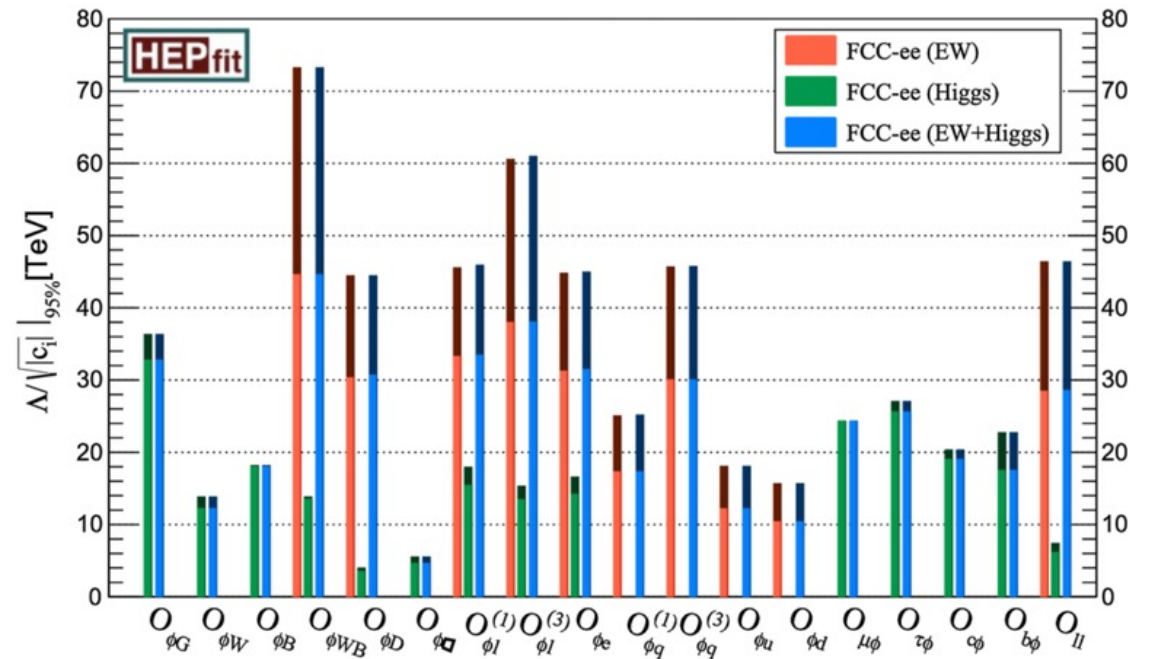
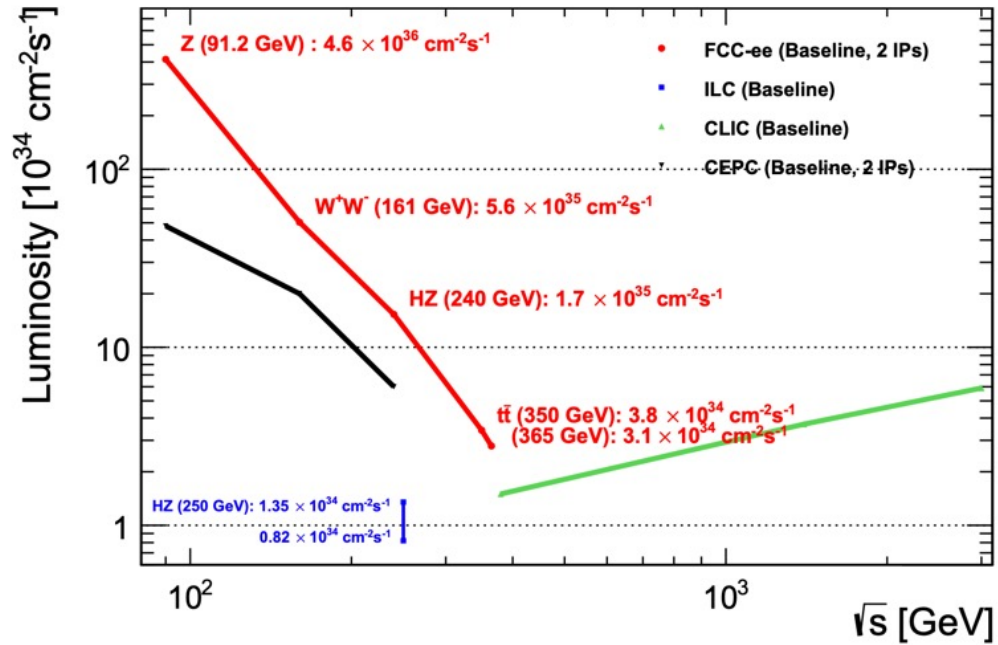


Fig. 5 Electroweak (red) and Higgs (green) constraints from FCC-ee, and their combination (blue) in a global EFT fit. The constraints are presented as the 95% probability bounds on the interaction scale, $\Lambda/\sqrt{c_i}$, associated to each EFT operator. Darker shades of each colour indicate the results when neglecting all SM theory uncertainties

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Call for new generation(s) of brave theorists to tackle the new challenges...

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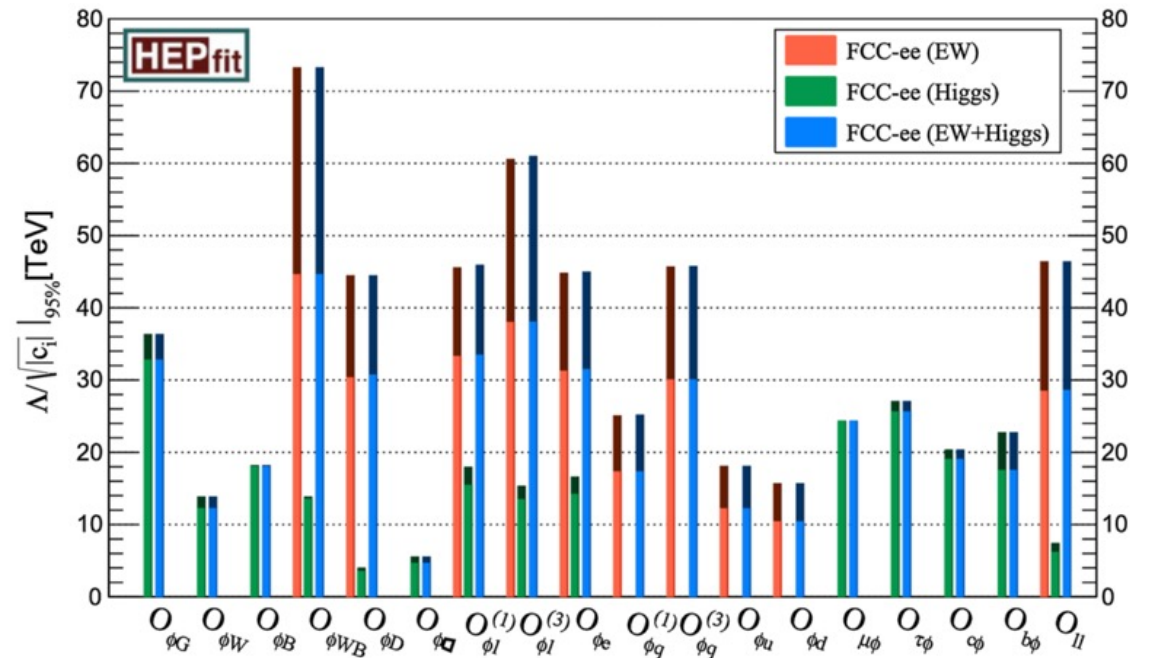


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- Make sure that, besides such a (timely) flagship project, there remains an **attractive portfolio of other projects at CERN** (like in the past).

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Timeline for the update of the European Strategy for Particle Physics



<https://home.cern/news/news/knowledge-sharing/updating-european-strategy-particle-physics>

A remark regarding the upcoming **European Strategy exercise**:

There is only one question to be answered: **do you envision a bright future for CERN?**
No need to repeat the entire discussions of the last time – the physics situation is clear, basically no change since last time. Fight the entropy.

Conclusion(s)

Concluding statements

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Thank you for the invitation!