



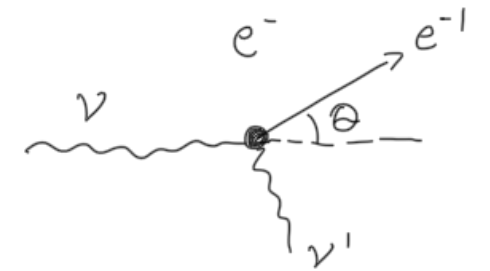
Feasibility of a directional solar neutrino measurement with the CYGNO/INITIUM experiment

Samuele Torelli

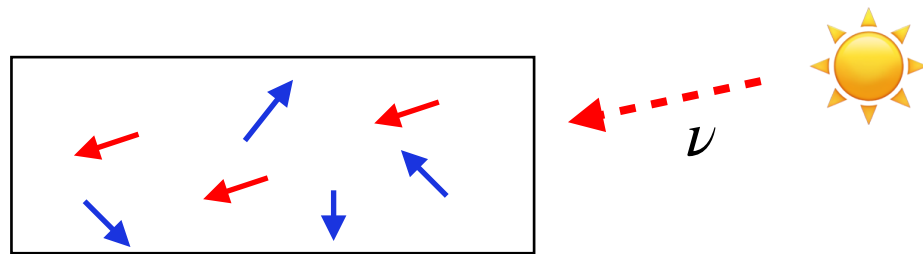
Prof. Elisabetta Baracchini



Why a directional measurement



- Capability of discriminating signal from background from source direction



Introduction of a much stronger signature than the only energy spectrum

Signal peaked distribution over flat bkg in angle

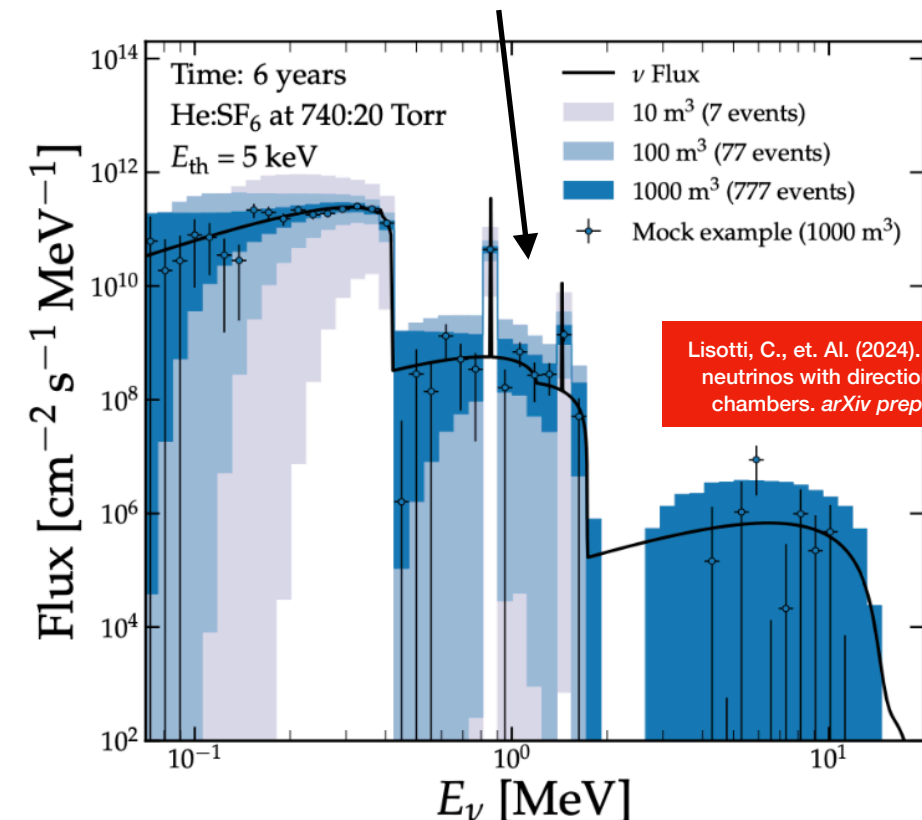
- Interests in:
 - Improve precision on the pp flux (Solar luminosity constraints)
 - Improve precision in CNO flux measurement (Metallicity problem)

- Possibility of event by event neutrino energy reconstruction (closed kinematic)

$$E_{\nu, Reco} = \frac{-m_e T_e - \sqrt{T_e^2 m_e^2 \cos(\theta)^2 + 2T_e m_e^3 \cos(\theta)^2}}{(T_e - T_e \cos(\theta)^2 - 2m_e \cos(\theta)^2)}$$

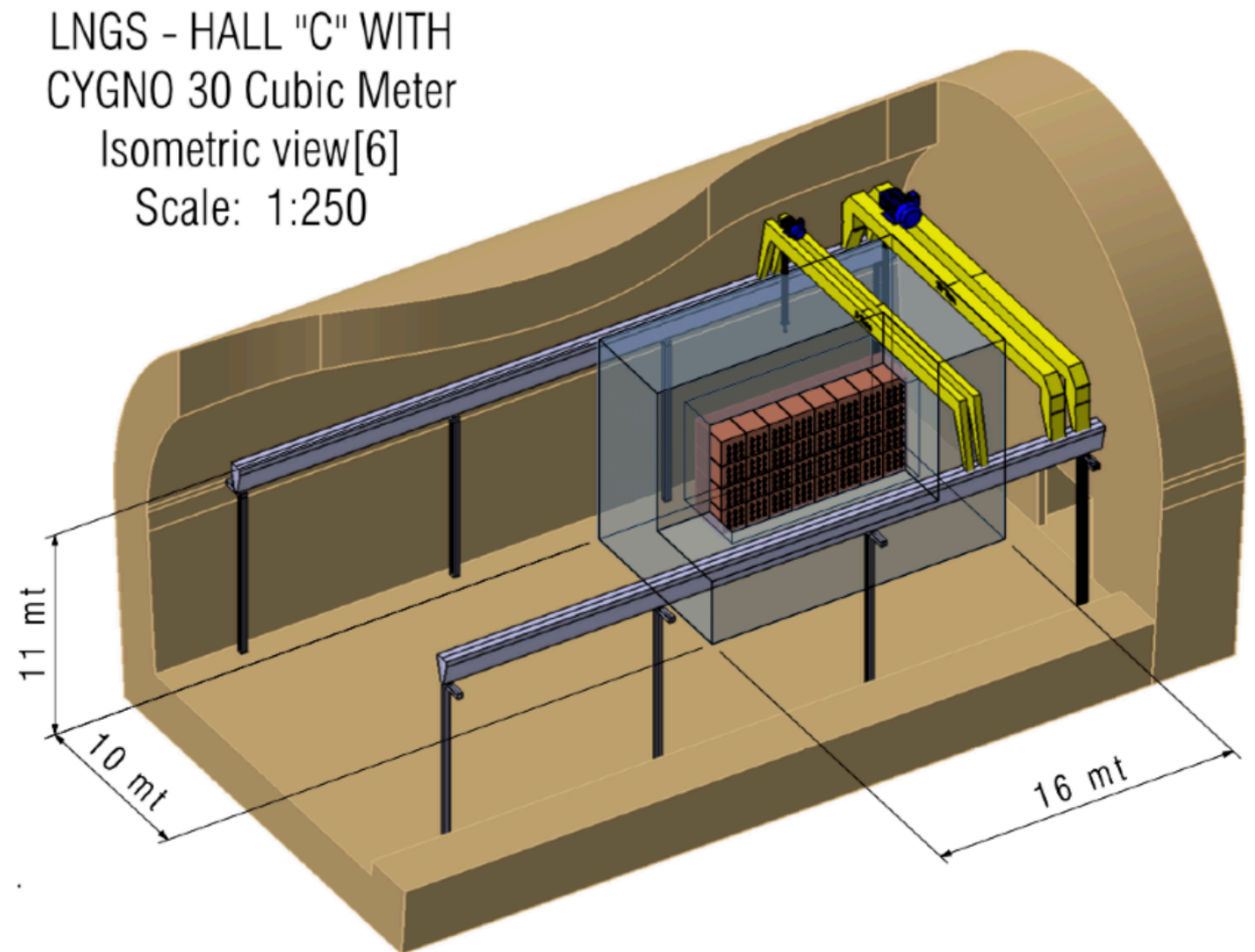
Reconstruction of the original neutrino energy spectrum

Remove the spectral degeneracy of pep, ⁷Be and CNO



With a *CYGNO* 30 detector

- *CYGNO* 30 m³ detector proposed to be suitable for this measurement
- Modular approach: at the moment composed by 75 *CYGNO_04* modules
- Significant contribution in DM searches for SI and SD couplings
- Proposed additionally to be suitable for a directional measurement of solar neutrino from pp chain



Feasibility study of a directional neutrino measurement

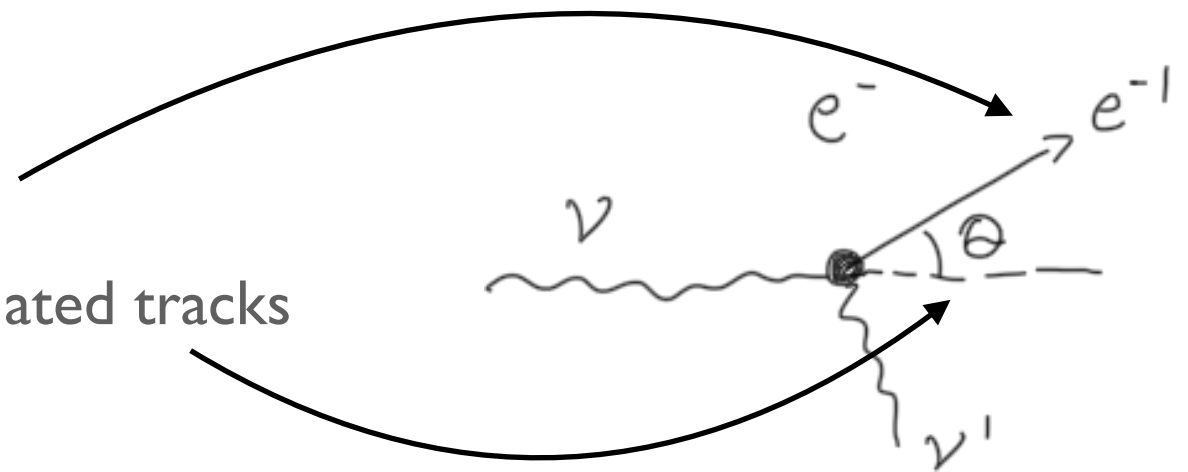
The purpose of my PhD thesis has been to evaluate the feasibility of a directional measurement of solar neutrino produced in the pp chain with a 30 m³ CYGNO detector

For this study 2 key elements critical to asses:

O'Hare, C. A. J.,... S.Torelli..., et al. *arXiv:2203.05914*

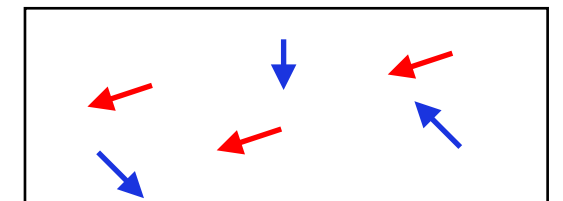
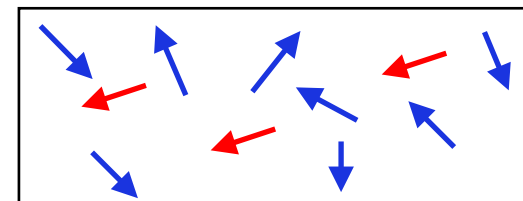
1. Detector performances (energy and angular resolution)

- CYGNO-30 will be composed by many CYGNO-04 modules, similar to LIME
- Detector performances assessed on LIME
 - **Energy resolution** on X-Ray data in LIME
 - **Angular resolution** studies on LIME simulated tracks



2. Electromagnetic background expected in the detector

- CYGNO-30 conceptual design
- Material and geometry optimization
- GEANT4 simulation

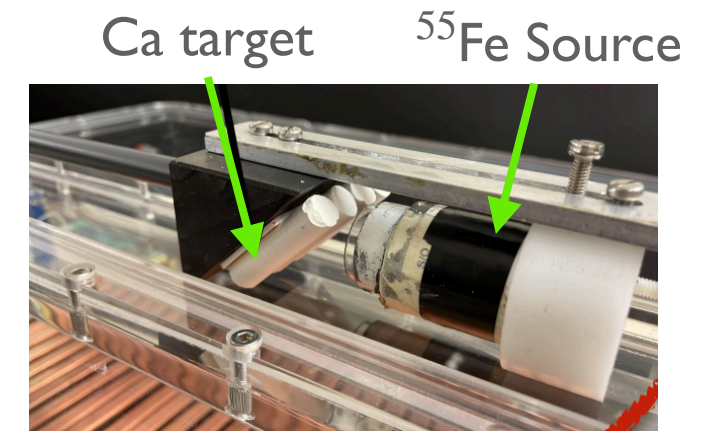
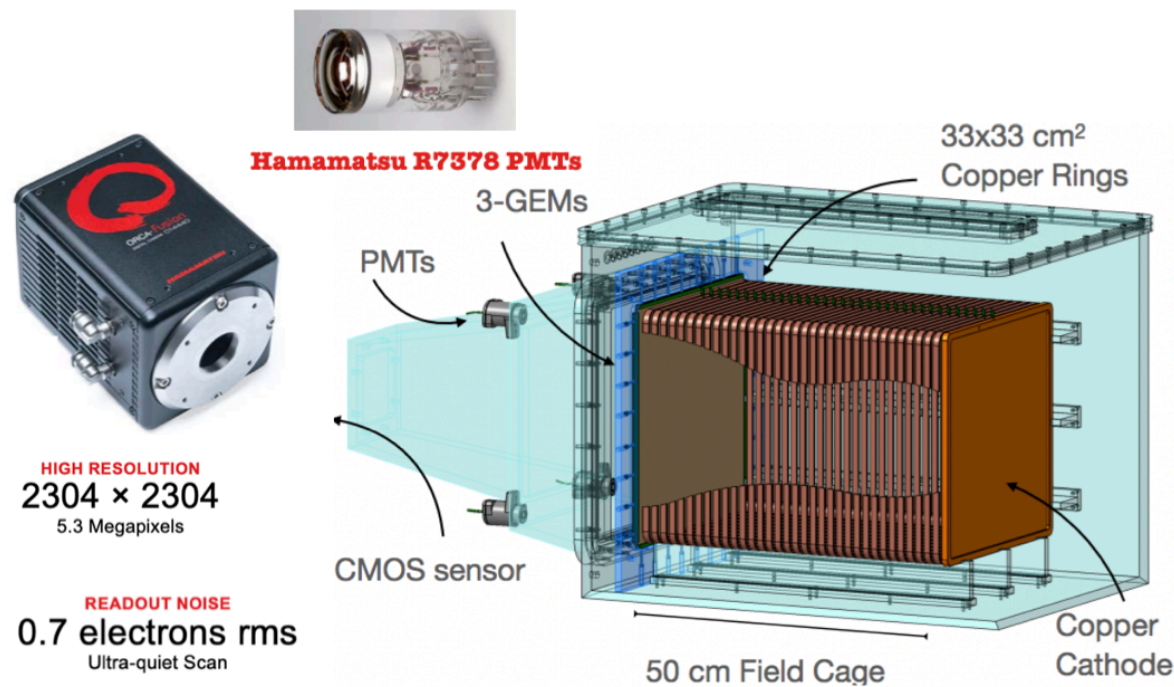


Step 1: Characterization of the detector
response to low energy electron recoil

Multi-energy X-Ray data

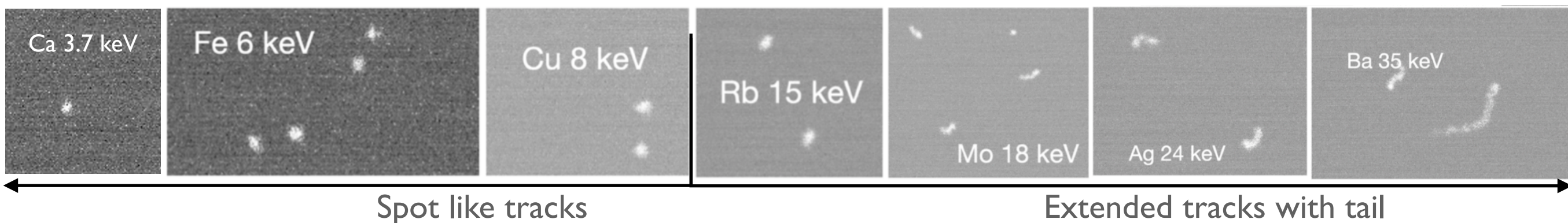
Data taken overground at LNF: High pileup

- Study of linearity and energy resolution performed overground with different X-Ray sources
- LIME detector used $33 \times 33 \text{ cm}^2$ with 50 cm drift



Target	Energy (keV)	Photon Yield	
Selected K_alpha K_beta (#/sec/steradian)			
Cu	8.04	8.91	2,500
Rb	13.37	14.97	8,800
Mo	17.44	19.63	24,000
Ag	22.10	24.99	38,000
Ba	32.06	36.55	46,000
Tb	44.23	50.65	76,000

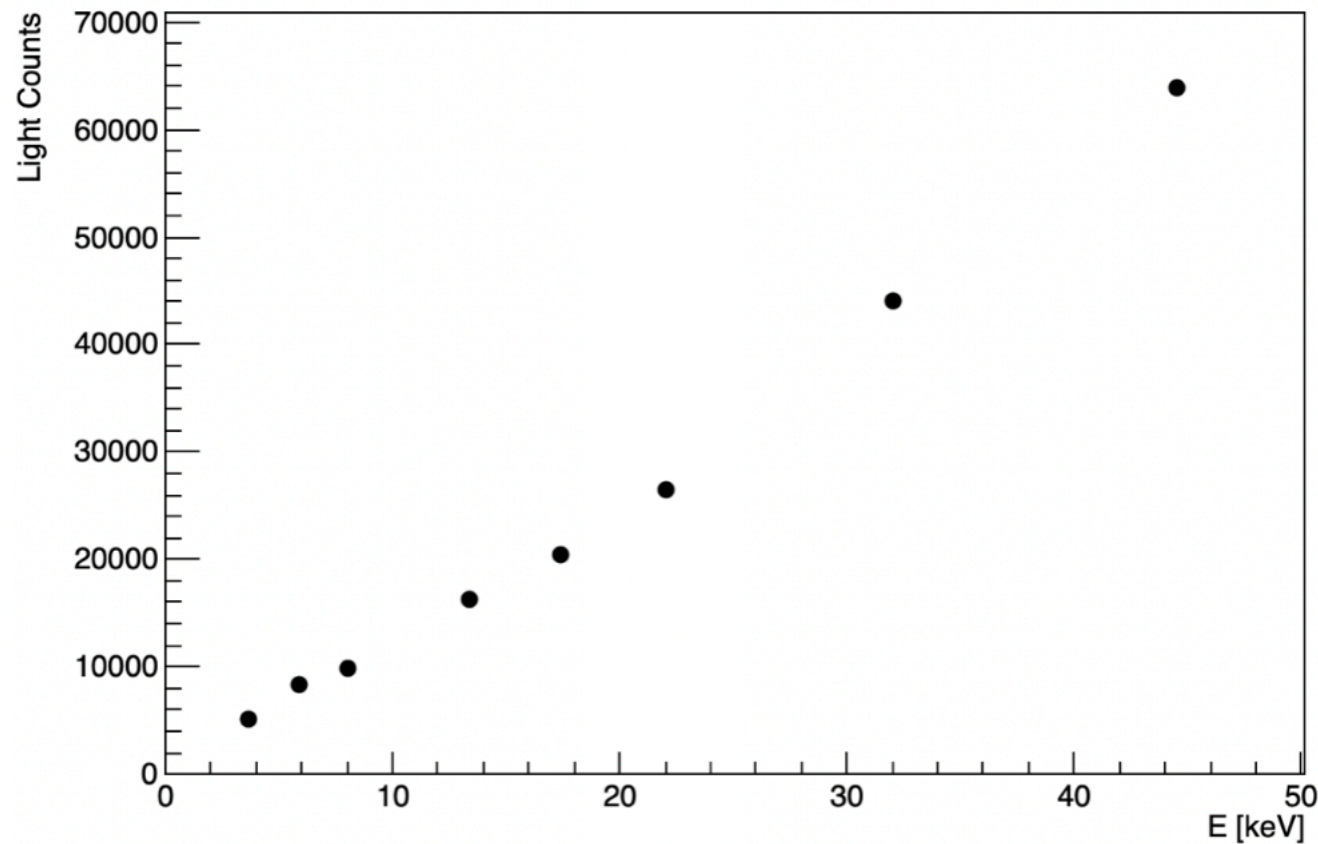
- How tracks appear:



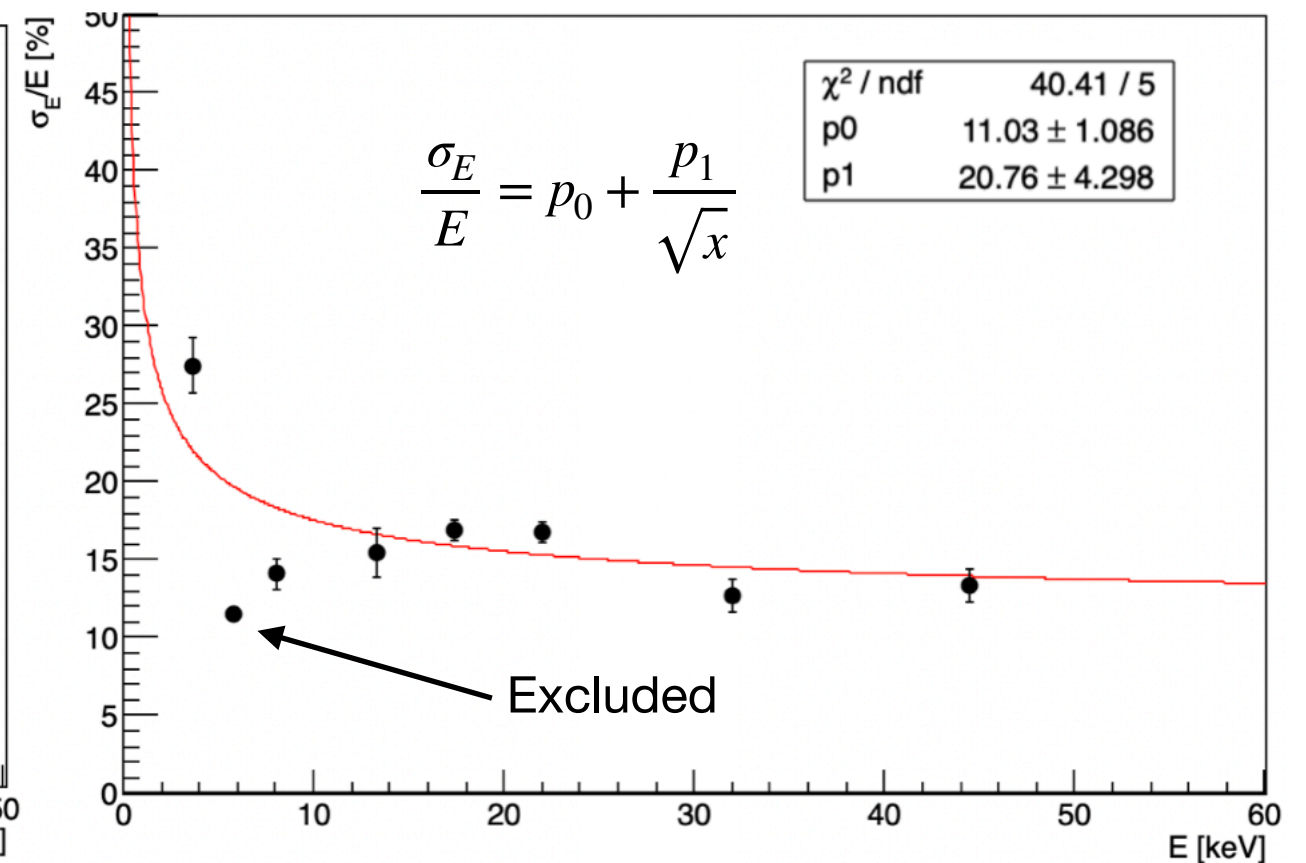
Light response and energy resolution

- From the data analysis the detector response and the energy resolution:

Detector light response vs E



Energy resolution vs E



- Response expected to be subject to saturation at very low E and less saturated at high E
- Energy resolution behaviour compatible with typical resolution of a gas detector

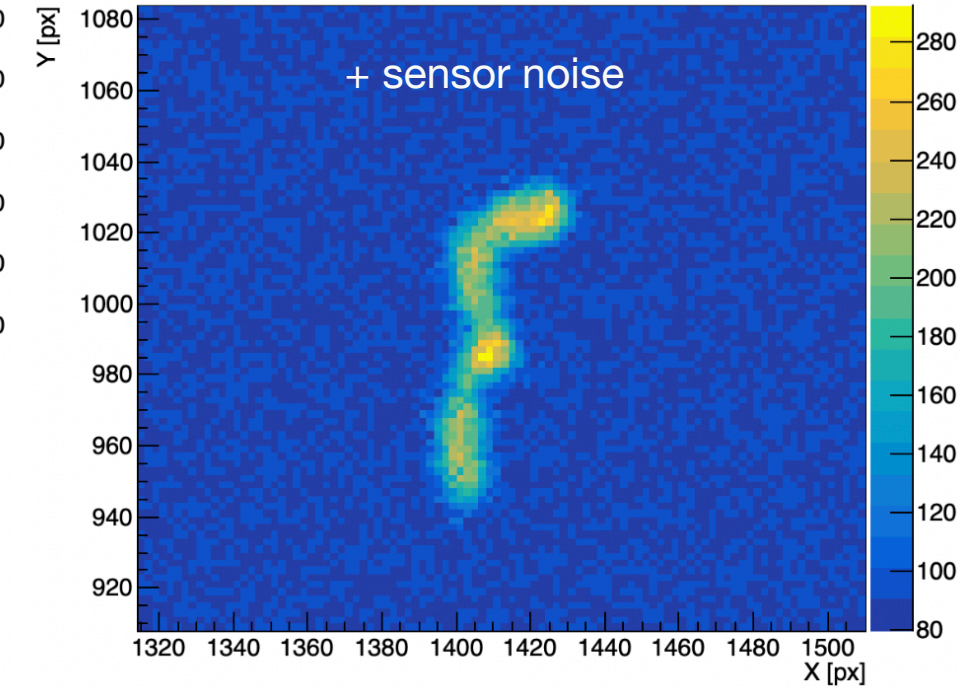
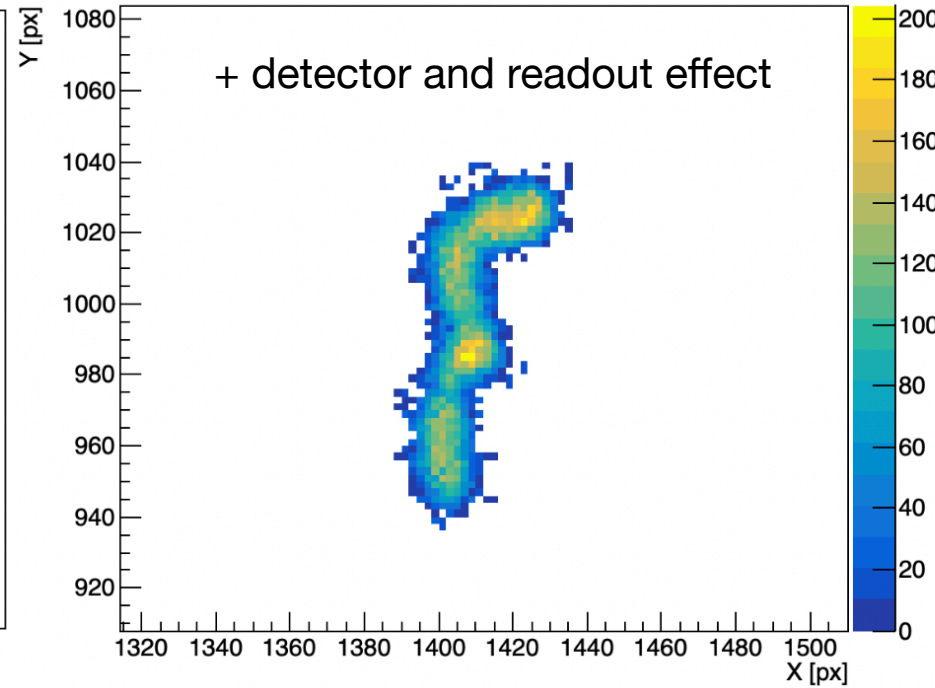
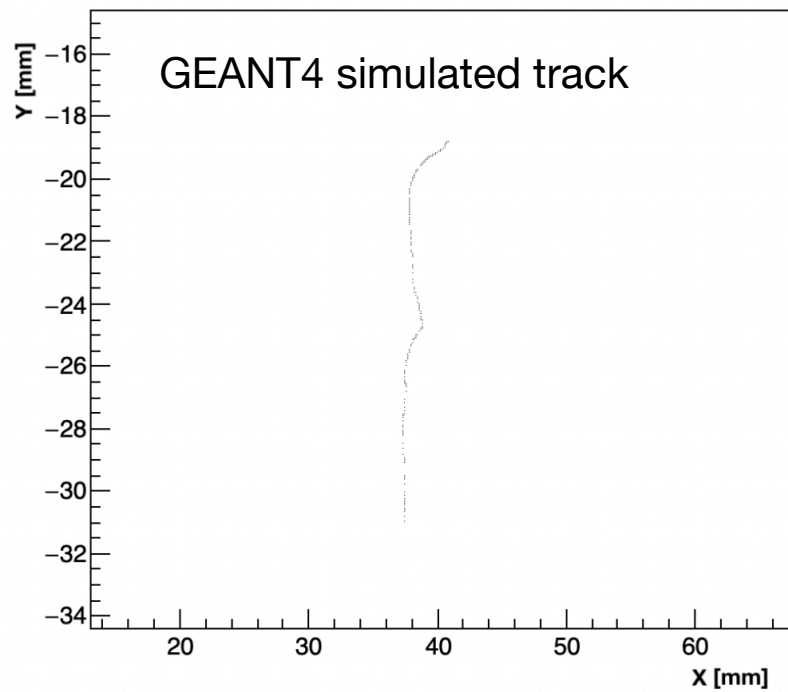
Step 2: Development of a simulation to
produce low energy electron recoil
sCMOS images

ER sCMOS images simulation

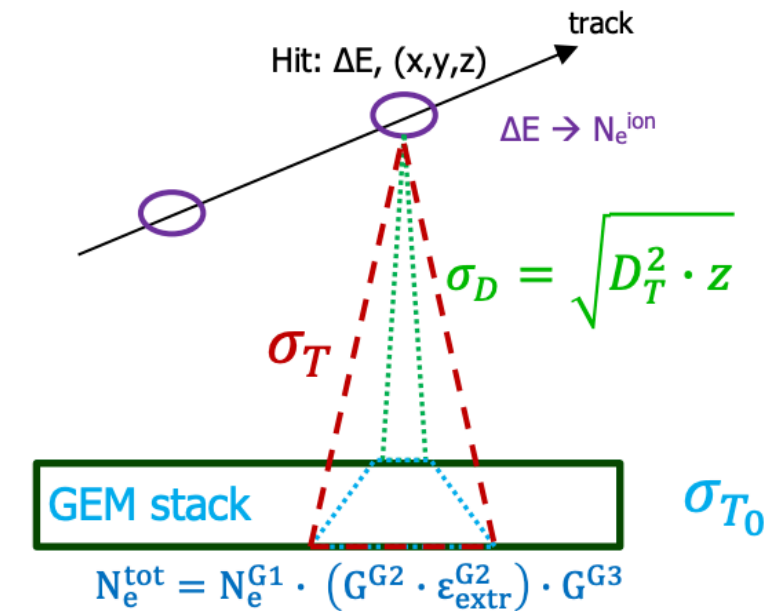
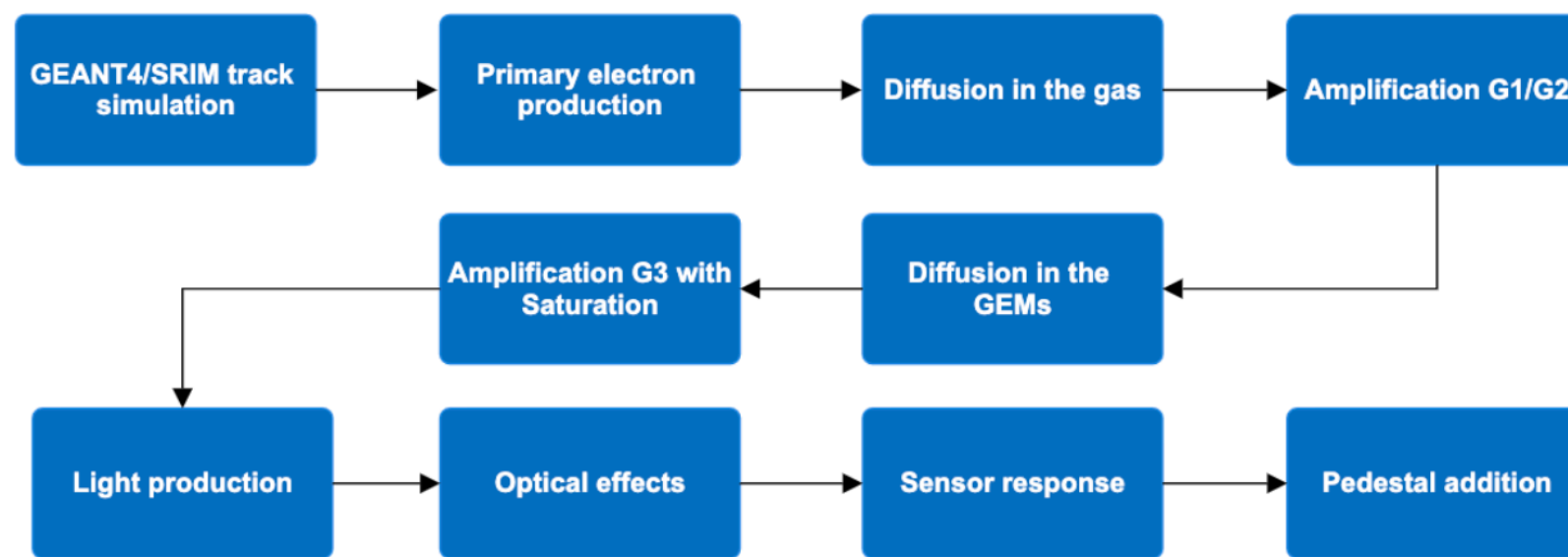
Detector response

From a GEANT4 track

To a sCMOS-like image



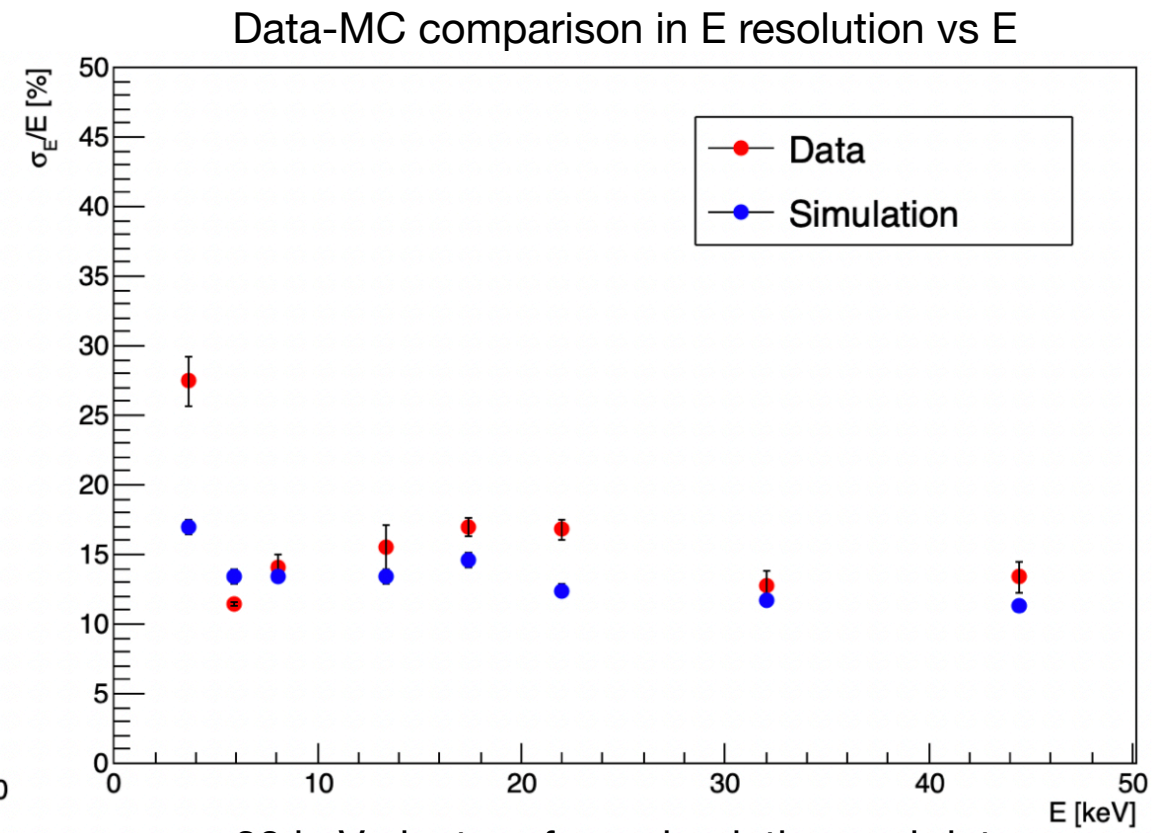
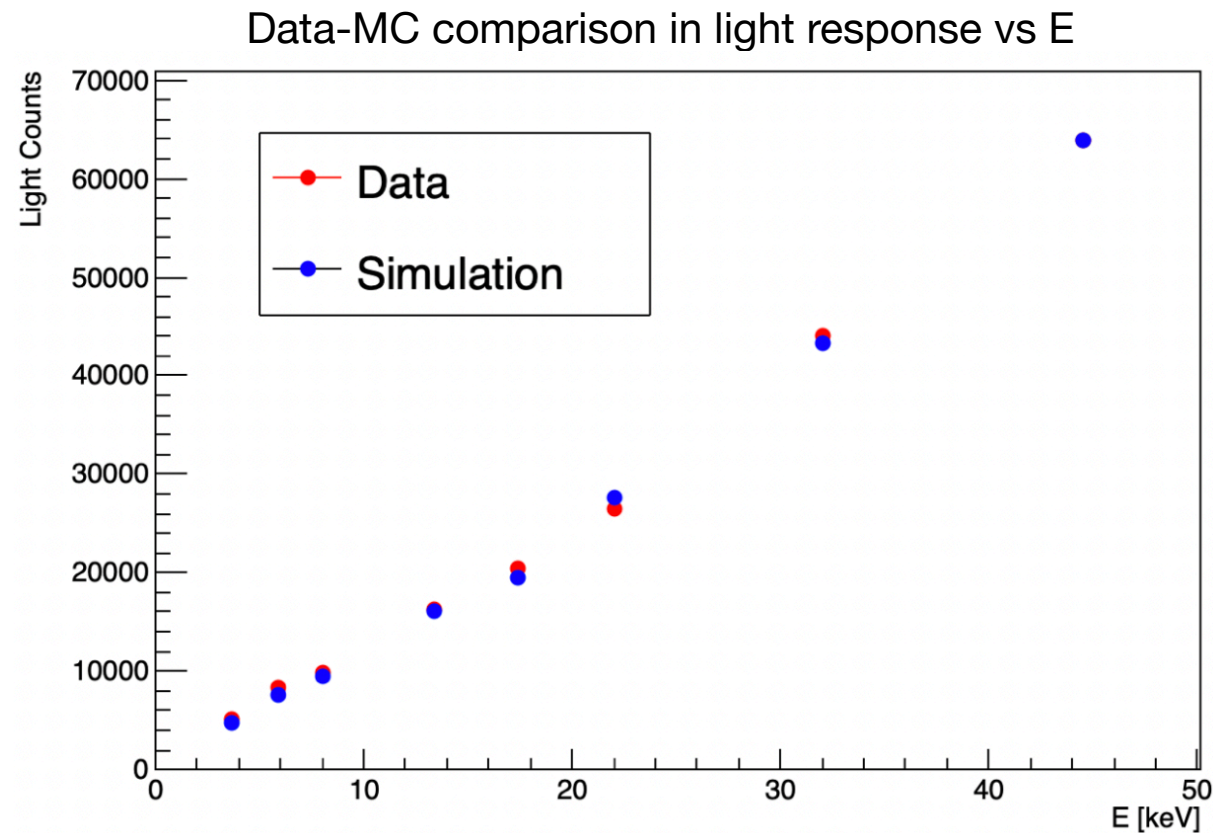
Working flow of the simulation (statistical effects are considered)



- Simulation parameters optimized on ^{55}Fe data

Data MC comparison

- Set of data produced at the same energies of the multi-energy X-ray data
- Parameters at the operative condition on LIME

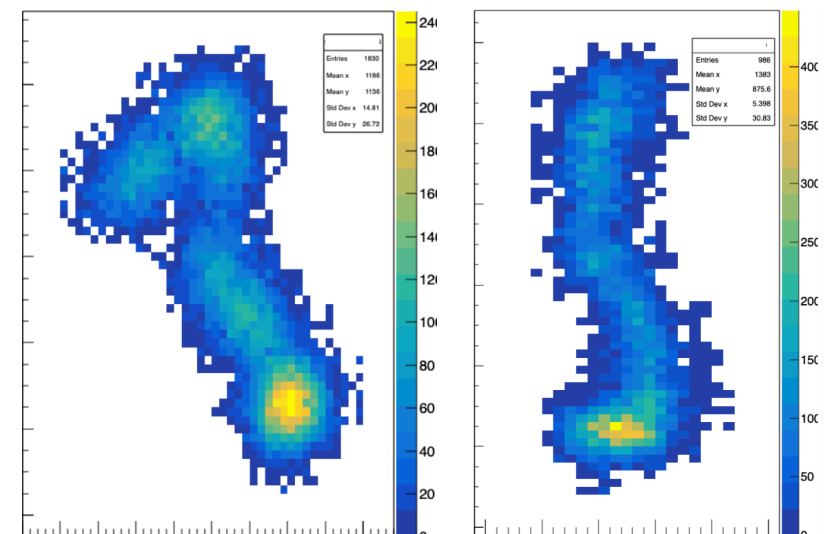


- Satisfactory level of agreement in light response and energy resolution
- Additionally a set of 9 topological track shape variables has been compared in Data and MC

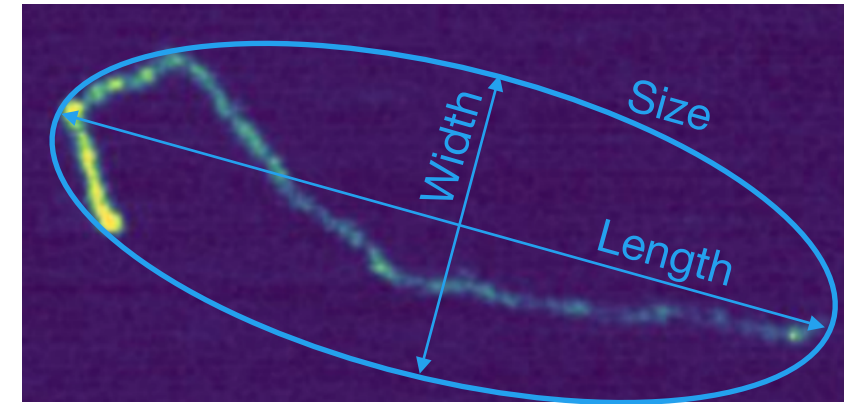


Signal/Background separation done with $sPlot$ technique

30 keV electron from simulation and data



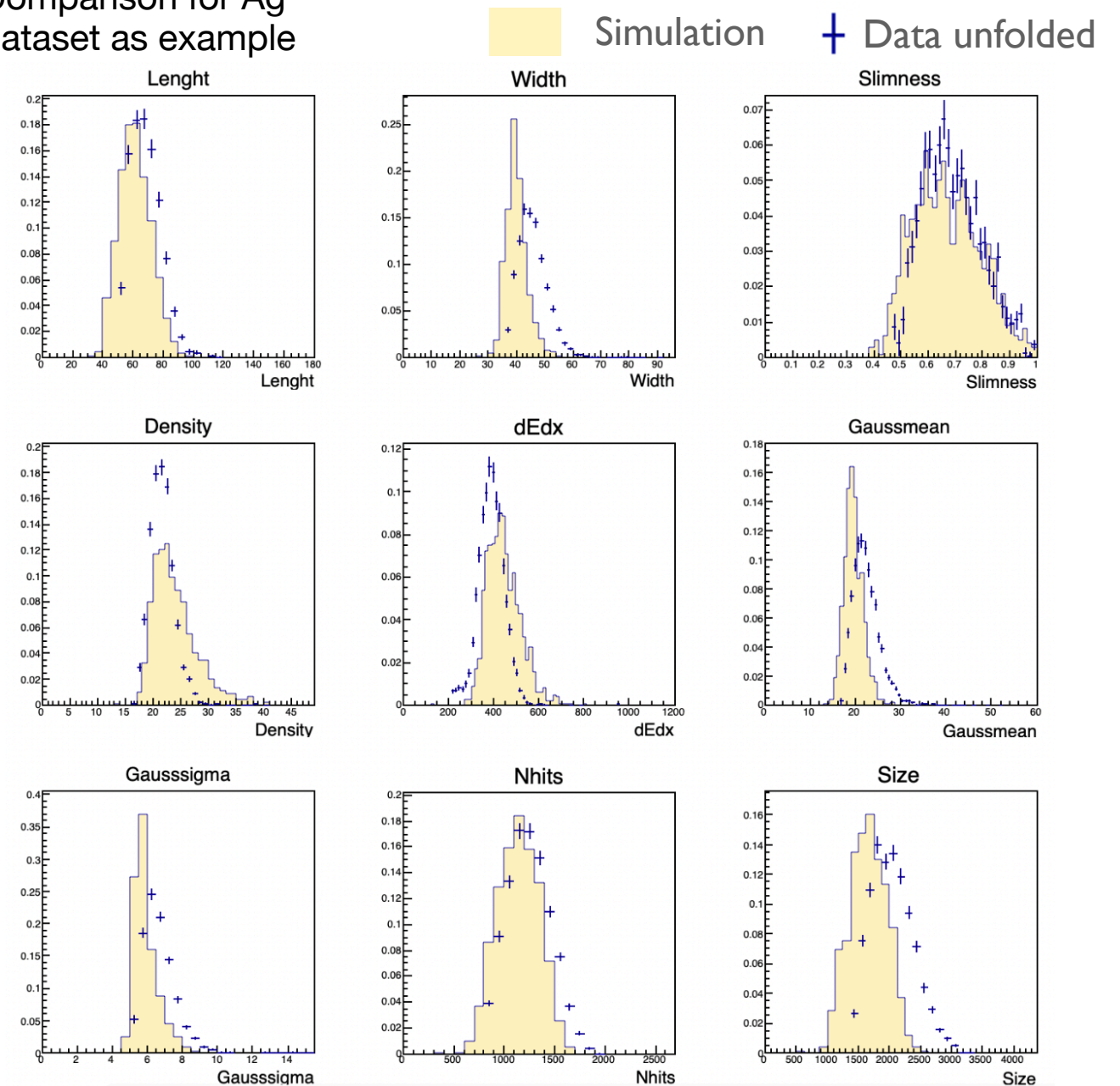
Track shape parameters comparison



- Shape variables compared for every energy dataset:

- Track length
- Track width
- Ratio width/length (slimness)
- Ratio light/npixels (density)
- Ratio light/length
- Mean transversal projection of the light distribution
- Sigma transversal projection of the light distribution
- Number of pixels
- Size of the cluster

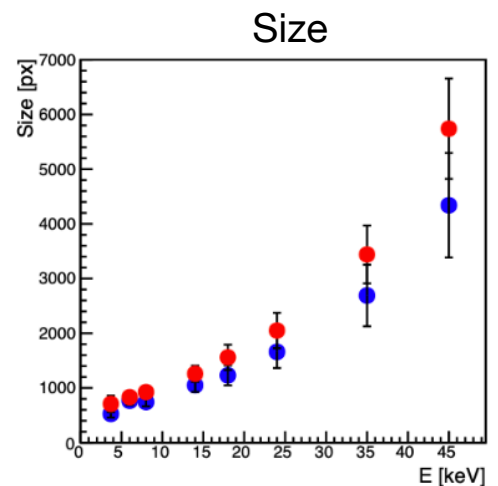
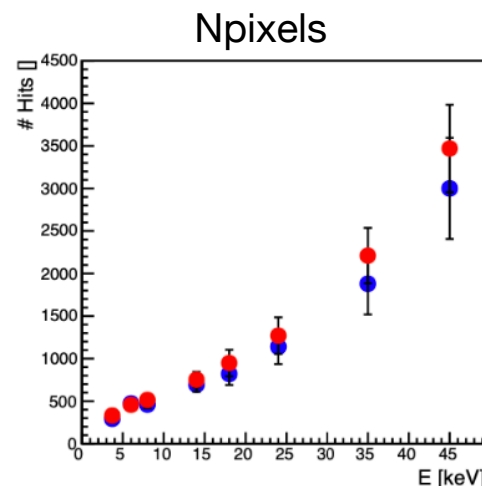
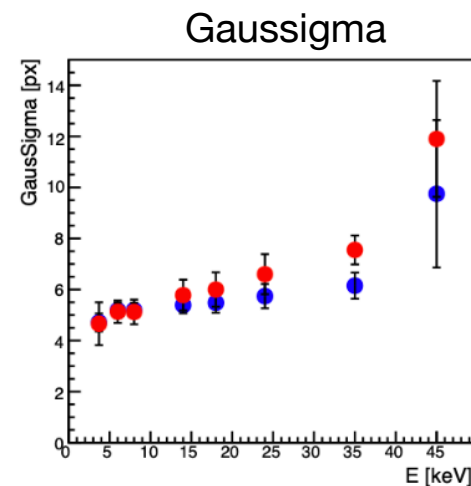
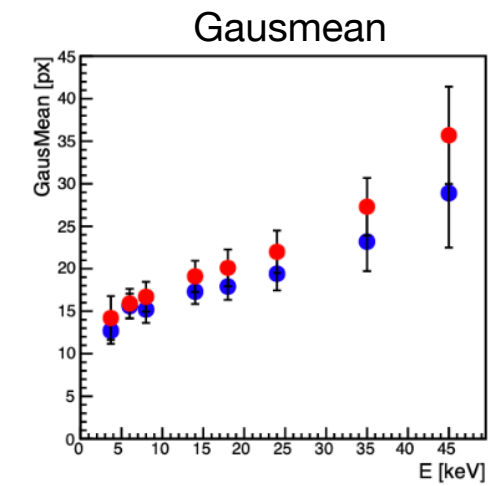
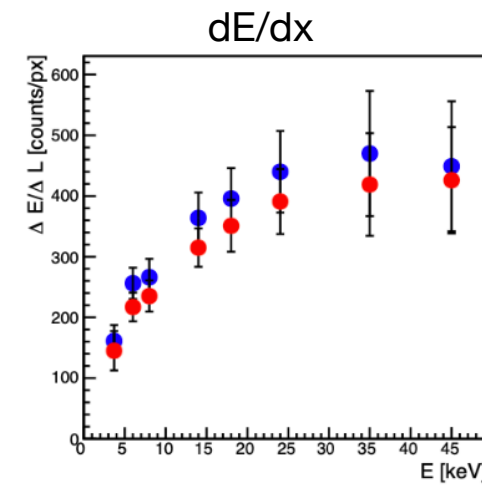
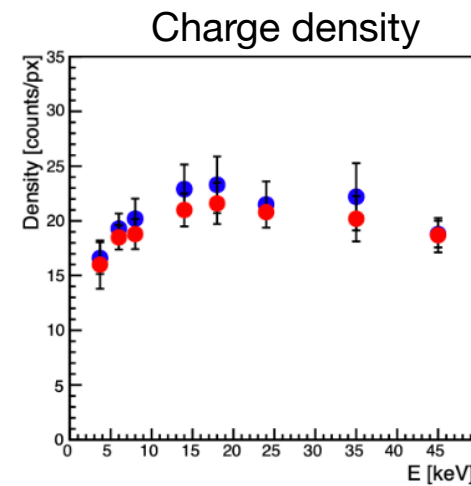
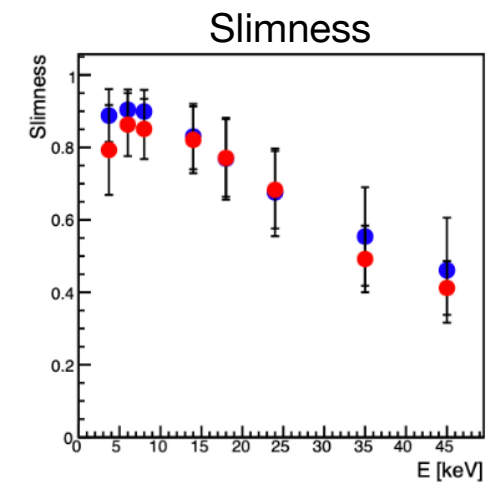
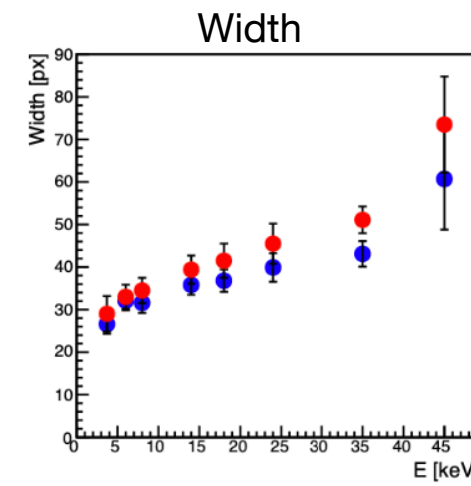
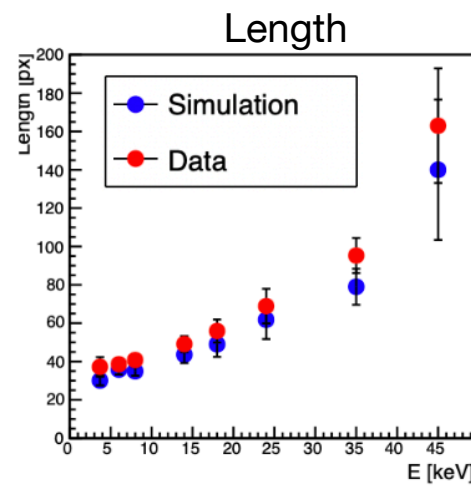
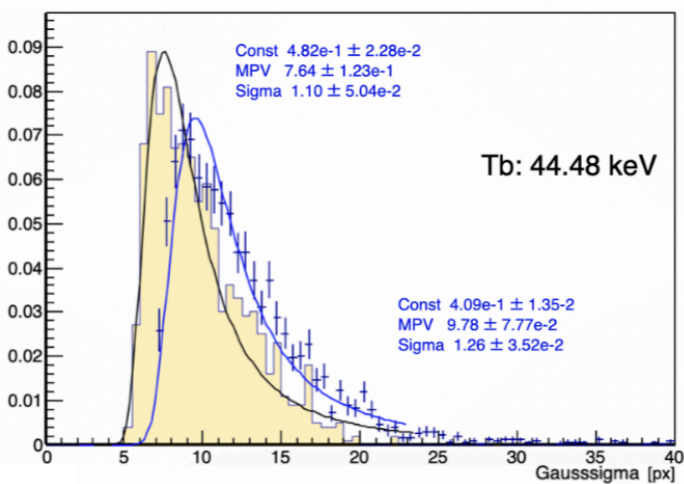
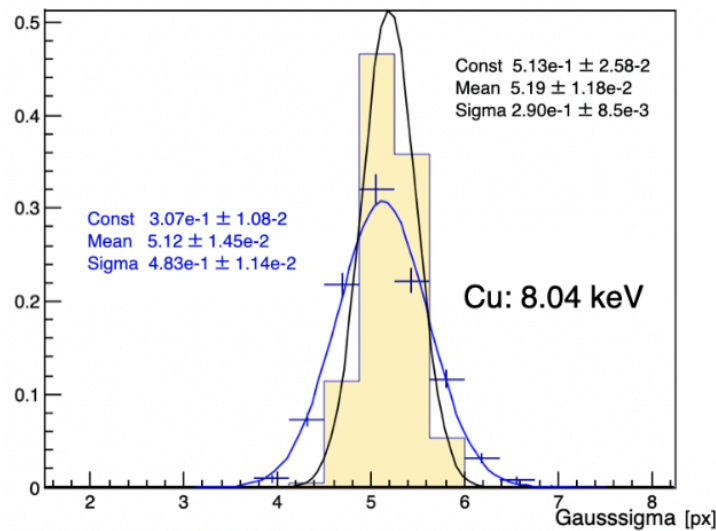
Comparison for Ag dataset as example



Track shape parameters comparison

Paper in preparation

- Mean and Sigma of the variable reported as a function of the energy for the different variables

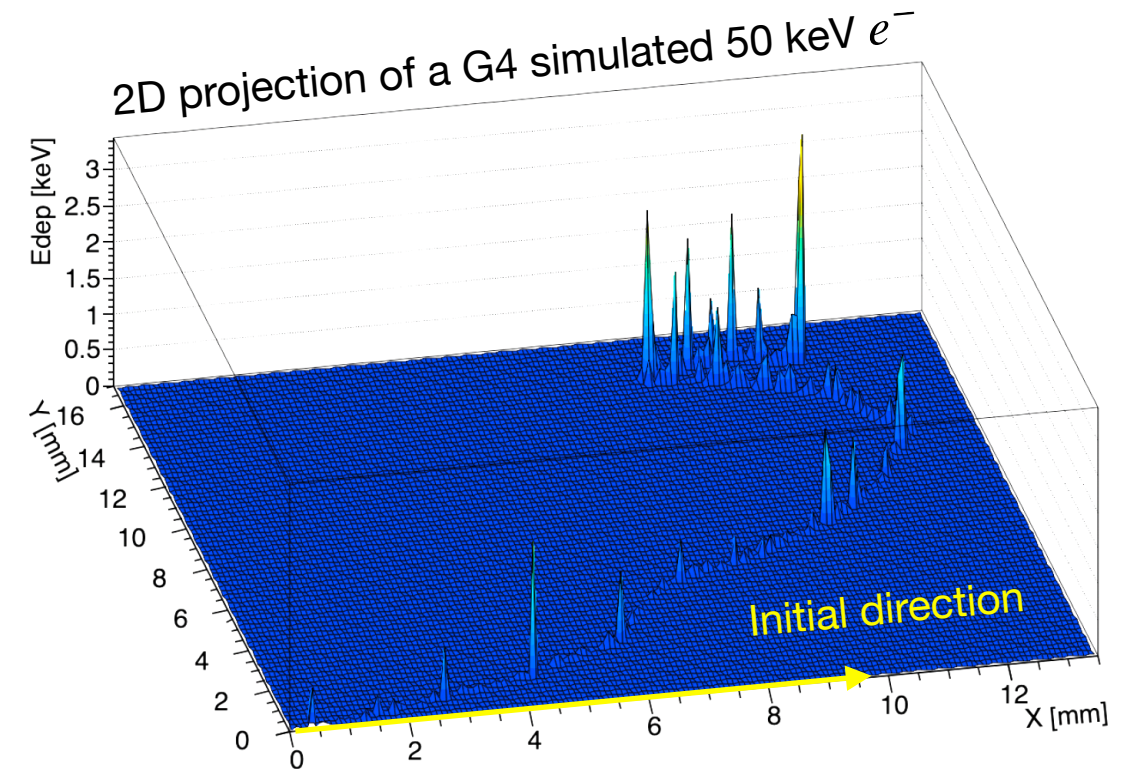


- Satisfactory agreement reached given the complexity of the simulation

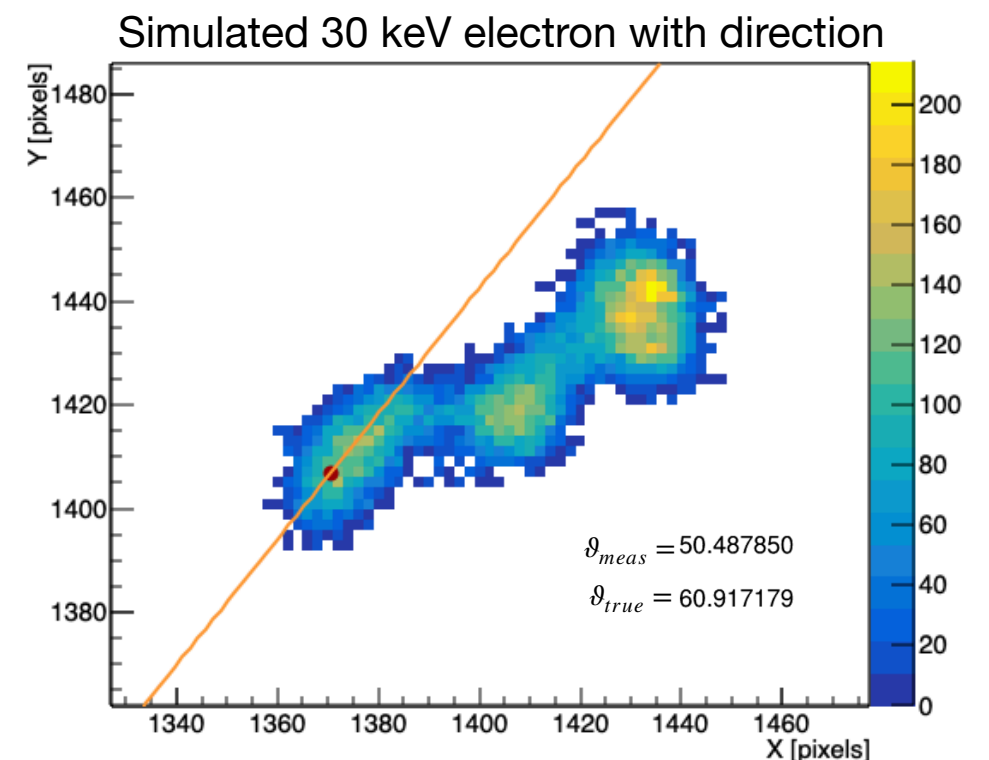
Step 3: Study the 2D angular resolution performances on electron recoils

Directionality of low energy electron recoil

- Measuring the electron recoil direction is one of the key points to study the feasibility of this measurement
- Electrons in gas undergo multiple scattering, thus the directional information is rapidly lost
- Only connecting the beginning of the track with the end is not enough to determine the diffusion
→Dedicated algorithm needed

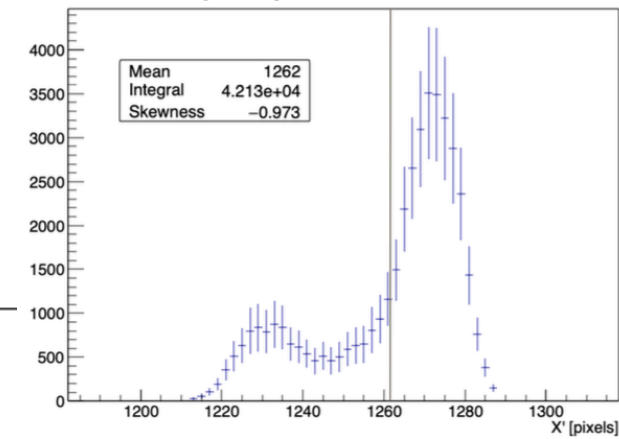


- Given the absence of ER with known direction the algorithm has been optimized and tested on simulated tracks
- Studied on 2D tracks projection, PMT for 3rd coordinate will be introduced in the future



Directionality algorithm in a nutshell

Track light profile distribution

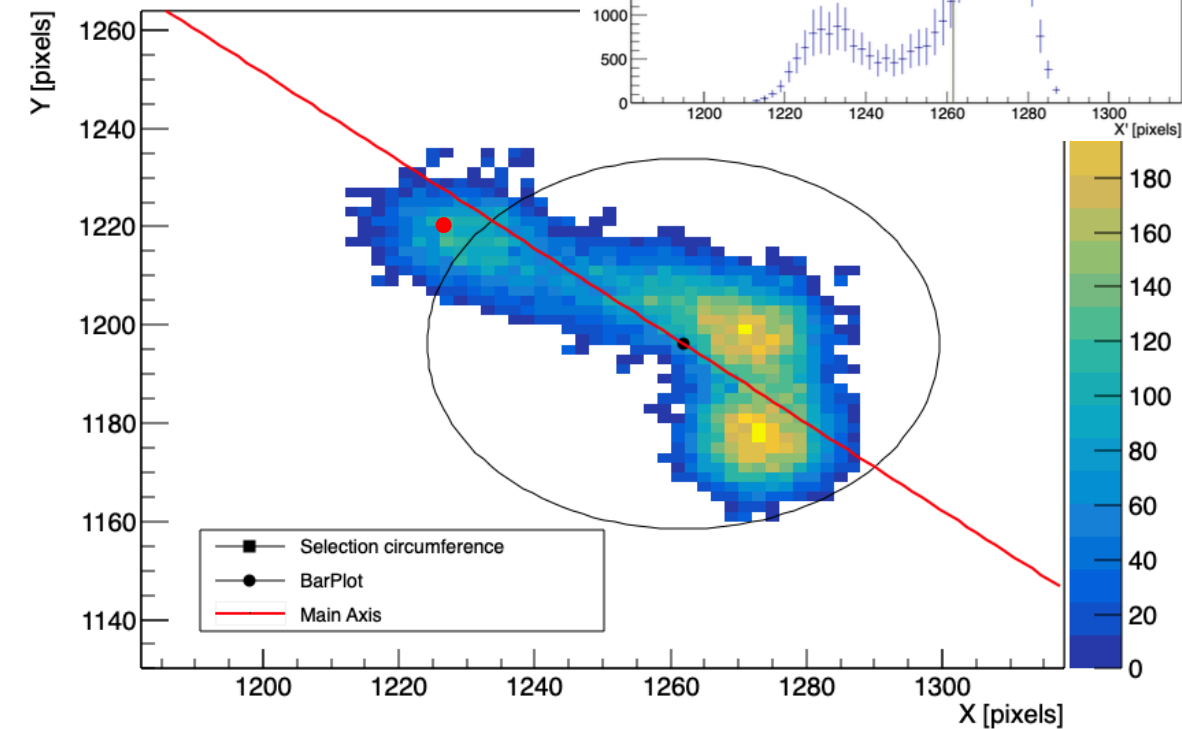


- Algorithm adapted from X-ray polarimetry:

Soffitta, Paolo, et al. Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment 700 (2013): 99-105.

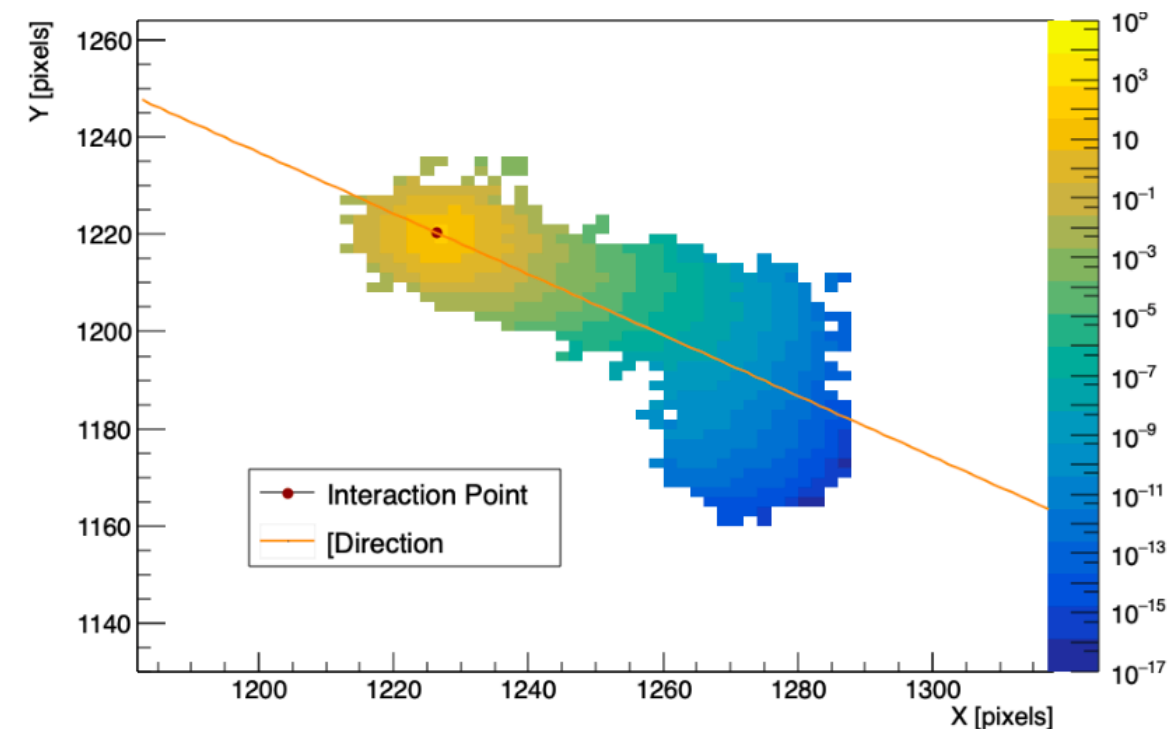
- Searching for the beginning of the track with:

- Skewness
- Distance of pixels from barycenter (farthest pixels)
- Selection of a region with fixed number of points N_{pt}



- Find the track direction:

- Track point intensity rescaled with the distance from the interaction point: $W(d_{ip}) = \exp(-d_{ip}/w)$
- Direction taken as the main axis of the rescaled track passing from the interaction Point
- Orientation given following the light in the Pixels



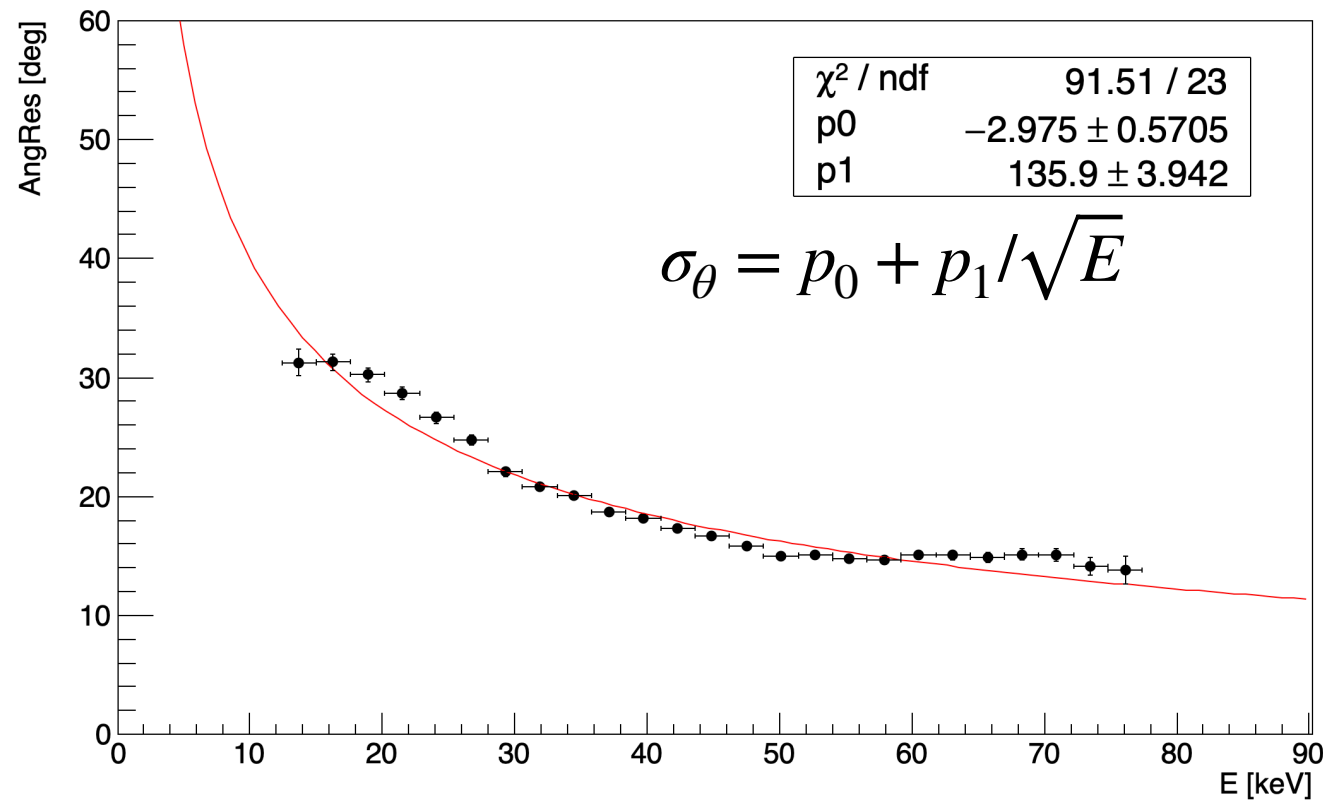
- Two parameters of the algorithm: N_{pt} and w

Results on angular resolution

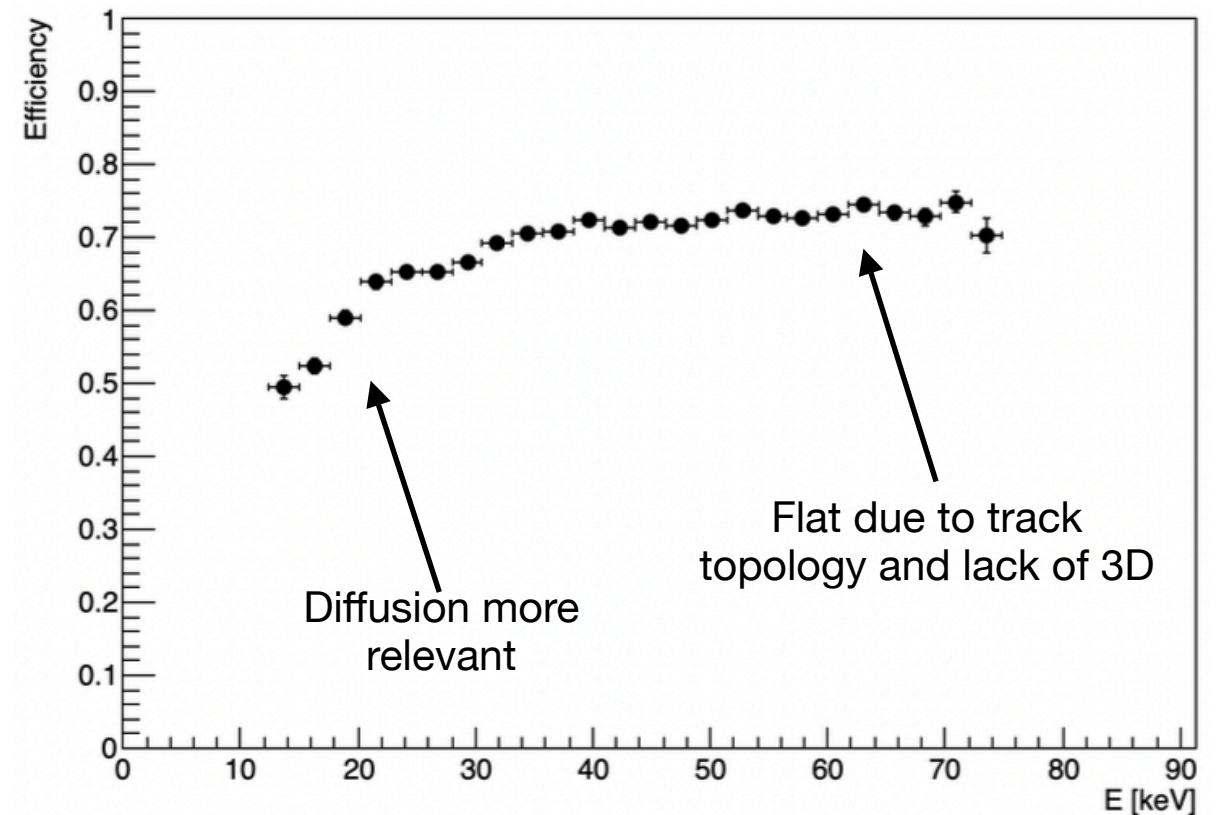
Paper in preparation

- Angular resolution performances evaluated on a dataset with uniform energy tracks [16-70] keV

Angular resolution vs energy



Directionality efficiency vs Energy

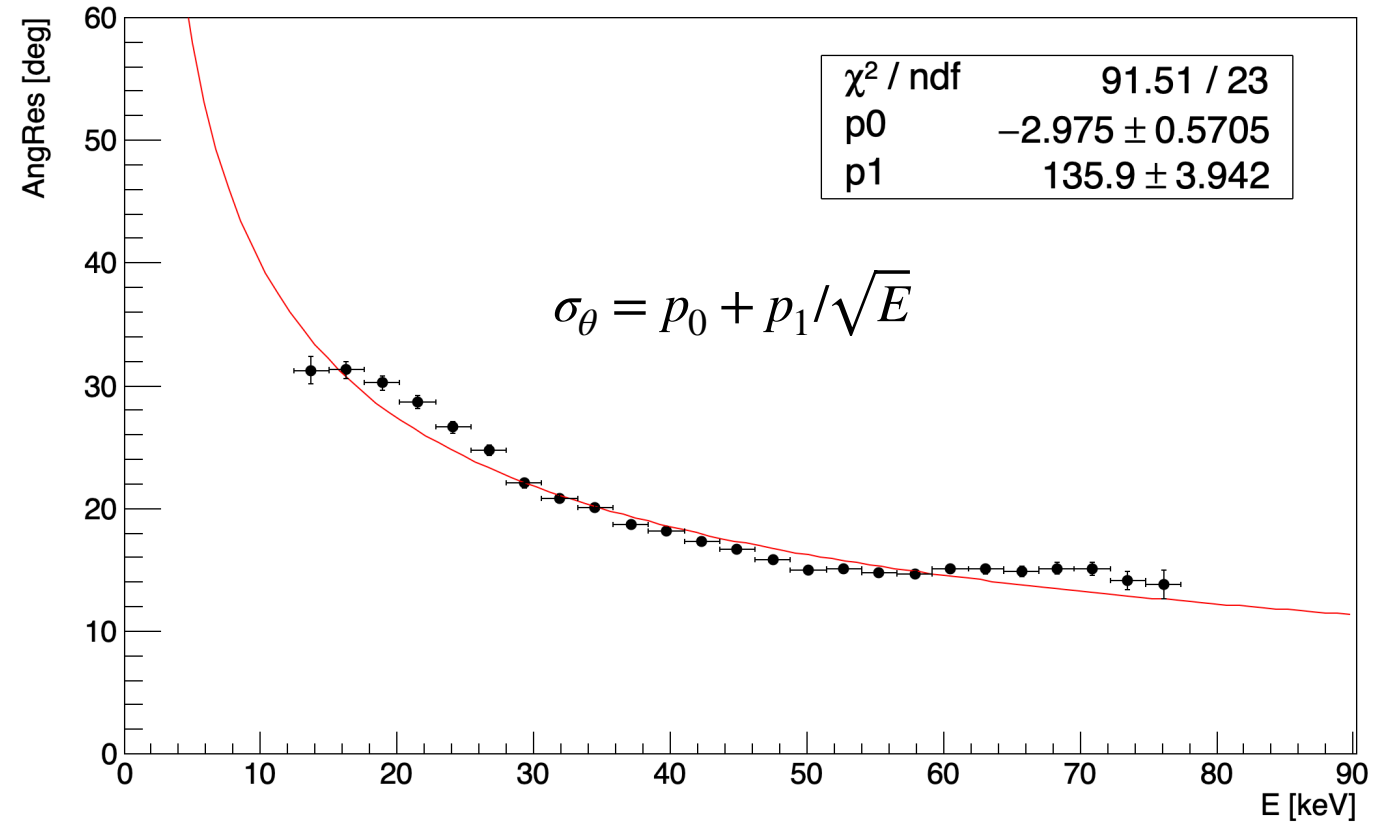
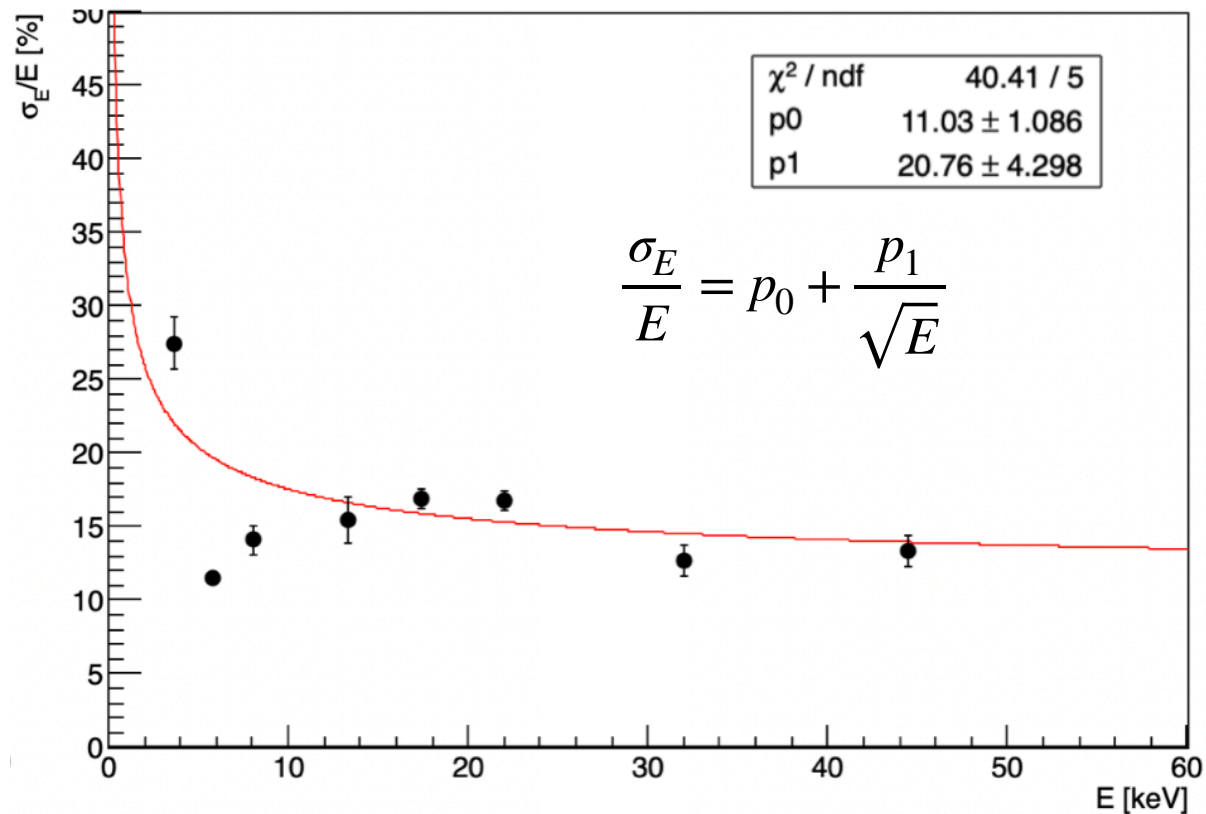


- First angular resolution result in this energy range
- Negative coefficient p_0 but it is expected to saturate at a value $\neq 0$ at higher energy

Step 4: Sensitivity studies for solar pp
neutrinos with CYGNO 30 m³

Resolutions and assumptions

- LIME resolutions will be assumed for the analysis



- Assumptions:

- Same resolution in both theta (on the GEM plane) and phi (with respect to the perpendicular to the GEM plane) given the PMT time resolution.
- Linear detector response
- Threshold on electron energy of 10 keV (55 keV on ν energy)

In CYGNO gas mixture:
 expected $1 \text{ ev}/\text{y}/\text{m}^3$
 (Oscillation included)

Bayesian approach for sensitivity studies

- Sensitivity studies on solar neutrino detection performed within a Bayesian framework:

$$p(\mu_s, \mu_b | D) = \frac{\mathcal{L}(D | \mu_s, \mu_b) \cdot \pi(\mu_s) \cdot \pi(\mu_b)}{p(D)}$$

Posterior probability \rightarrow $p(\mu_s, \mu_b | D)$
 Likelihood \rightarrow $\mathcal{L}(D | \mu_s, \mu_b)$
 Prior probabilities \rightarrow $\pi(\mu_s) \cdot \pi(\mu_b)$
 Normalization \rightarrow $p(D)$

$$\mathcal{L} = \prod_{i,j} \frac{\lambda_{i,j}^{n_{i,j}} e^{-\lambda_{i,j}}}{n_{i,j}!}$$

Binned likelihood \rightarrow \mathcal{L}

$$p(H_1 | D) = \frac{\mathcal{L}(D | H_1) \cdot \pi(H_1)}{p(D)}$$

$$p(H_0 | D) = \frac{\mathcal{L}(D | H_0) \cdot \pi(H_0)}{p(D)}$$

- Strategy:

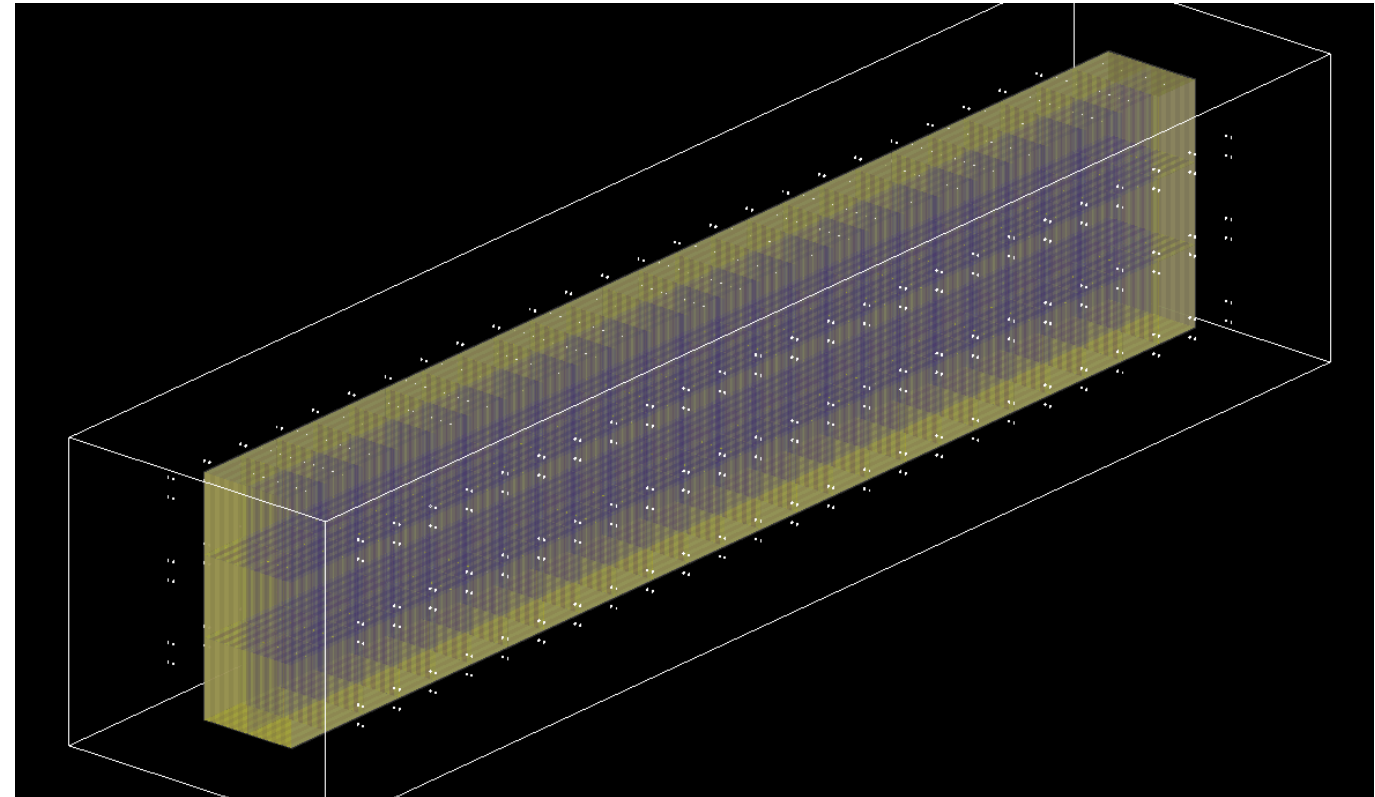
- Theoretical model for signal and background with the detector resolution included
- ToyMC production
- Likelihood fit for S+B model (H_1) and only B model (H_0)

$$\frac{p(H_1 | D)}{p(H_0 | D)} = \frac{\mathcal{L}(D | H_1) \cdot \pi(H_1)}{\mathcal{L}(D | H_0) \cdot \pi(H_0)} = B_f \frac{\pi(H_1)}{\pi(H_0)}$$

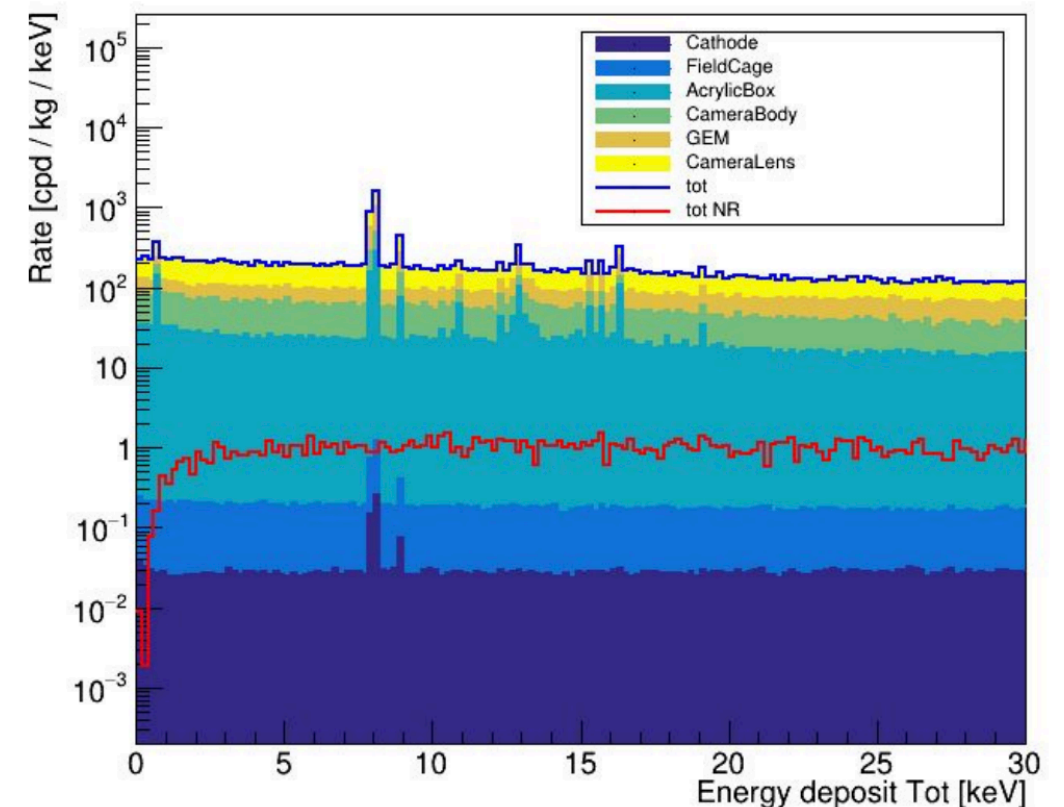
- Calculation of the Bayes factor and discovery probability vs exposure

Background studies

- Bkg simulation of the full detector geometry
- Three rows stack on each other with 25 CYGNO-04 modules
- All 75 modules enclosed in a common vessel
- Most critical detector element from CYGNO-04 background studies included in the simulation:
 - Field cage
 - Cathode
 - GEMs
 - Detector body (Vessel)
 - Resistors
 - Camera lenses
 - Camera sensor
- Simulation done with most ultrapure materials available now → detector to be realized in ~ 6y
- Shielding thick and pure enough such that the level of the external background is less than the internal one



CYGNO-04 internal background spectrum



Material choice

Reference:

- Electroformed copper by Majorana Collaboration:

MAJORANA Collaboration • N. Abgrall (LBNL, NSD and Shanghai Jiao Tong U.) et al. Nucl.Instrum.Meth.A 828 (2016), 22-36

- Acrylic insulator from SNO:

Systematic study of trace radioactive impurities in candidate construction materials for EXO-200
D.S. Leonard (Alabama U.), et al. Nucl.Instrum.Meth.A 591 (2008), 490-509

- SMD Resistors from XENON-IT:

Material radioassay and selection for the XENON1T dark matter experiment. XENON
Collaboration • E. Aprile (Columbia U.) et al. Eur.Phys.J.C 77 (2017) 12, 890

- Suprasil lenses and camera sensor:

Measurement performed @ LNGS - low radioactivity lab.

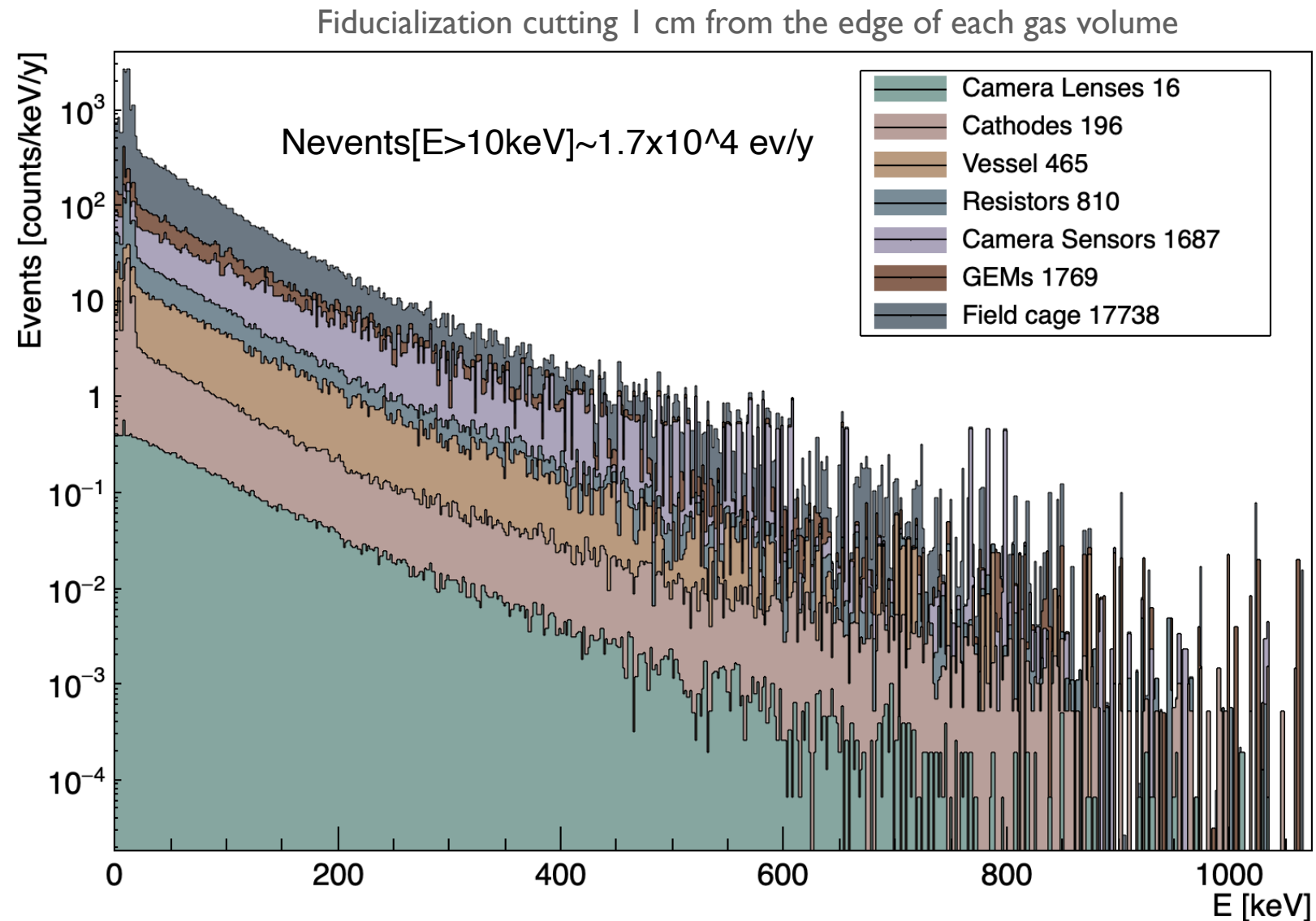
Detector element	Material	^{238}U	^{232}Th	^{40}K	^{235}U	^{226}Ra	^{228}Th
GEM core	Acrylic	< 296.0 $\mu\text{Bq/Kg}$	< 56.9 $\mu\text{Bq/Kg}$	< 71.2 $\mu\text{Bq/Kg}$	x	eq	eq
GEM armor	EFCu	0.131 $\mu\text{Bq/Kg}$	0.034 $\mu\text{Bq/Kg}$	x	x	eq	eq
Field cage support	Acrylic	< 296.0 $\mu\text{Bq/Kg}$	< 56.9 $\mu\text{Bq/Kg}$	< 71.2 $\mu\text{Bq/Kg}$	x	eq	eq
Field cage strip	EFCu	0.131 $\mu\text{Bq/Kg}$	0.034 $\mu\text{Bq/Kg}$	x	x	eq	eq
Cathode	EFCu	0.131 $\mu\text{Bq/Kg}$	0.034 $\mu\text{Bq/Kg}$	x	x	eq	eq
Vessel	EFCu	0.131 $\mu\text{Bq/Kg}$	0.034 $\mu\text{Bq/Kg}$	x	x	eq	eq
Camera sensor	Silicon	2 mBq/Kg	2.8 mBq/Kg	9 mBq/Kg	x	eq	eq
Camera lenses	Suprasil	123 $\mu\text{Bq/Kg}$	40.7 $\mu\text{Bq/Kg}$	0.3 mBq/Kg	x	eq	eq
Resistors	Al_2O_3	1 $\mu\text{Bq/pc}$	0.14 $\mu\text{Bq/pc}$	1.2 $\mu\text{Bq/pc}$	0.04 $\mu\text{Bq/pc}$	0.18 $\mu\text{Bq/pc}$	0.13 $\mu\text{Bq/pc}$

- Purest material available employed for detector realization

- GEMs with acrylic core from:

S.E. Vahsen(Hawaii U.), et. Al. ADS Abstract
Service - arXiv:2008.12587

Final background spectrum



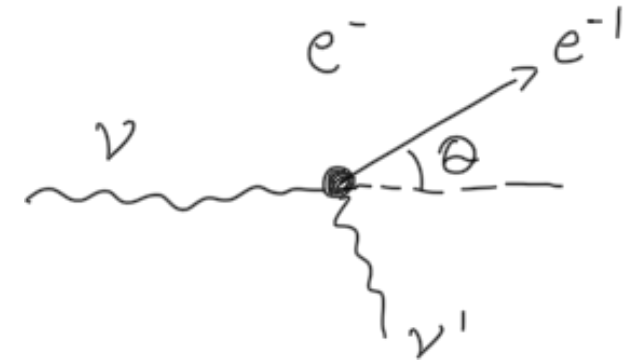
- Field cage acrylic is the dominant contribution ($\times 10$)
- Very recently we found a more suitable insulator

Arnquist, Isaac J., et al. "Ultra-low radioactivity Kapton and copper-Kapton laminates." *Nuclear Instruments and Methods*

Material	^{238}U	^{232}Th	^{40}K
Acrylic	$< 296.0 \mu\text{Bq/Kg}$	$< 56.9 \mu\text{Bq/Kg}$	$< 71.2 \mu\text{Bq/Kg}$
Kapton	$\sim 10 \mu\text{Bq/Kg}$	$\sim 10 \mu\text{Bq/Kg}$	X

- $\times 10$ less radioactive than the SNO acrylic

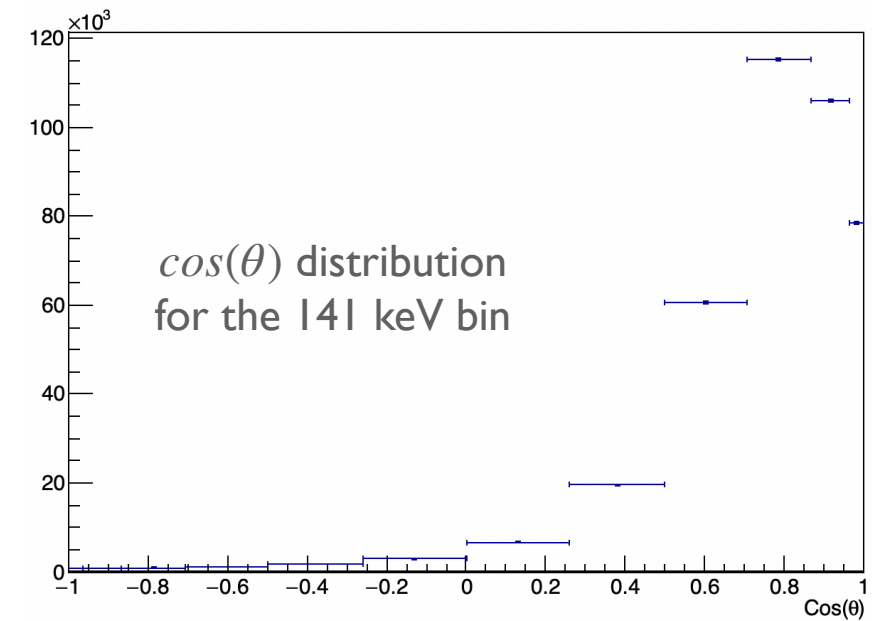
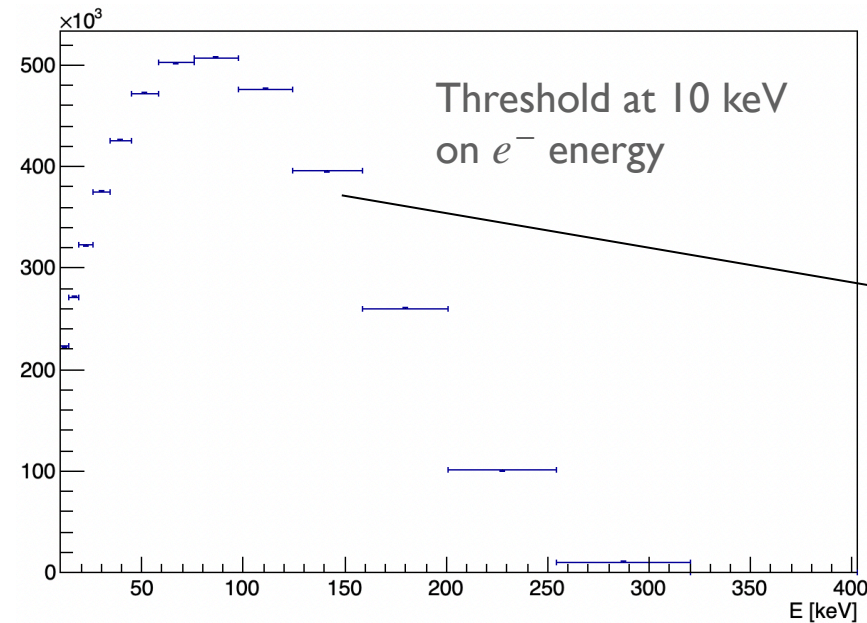
Template for bayesian analysis



- Template produced starting from the expected distribution adding the detector resolution
 - Both the energy and angular spectrum in the Sun's reference frame are considered
 - For each energy bin the $\cos(\theta)$ distribution is produced

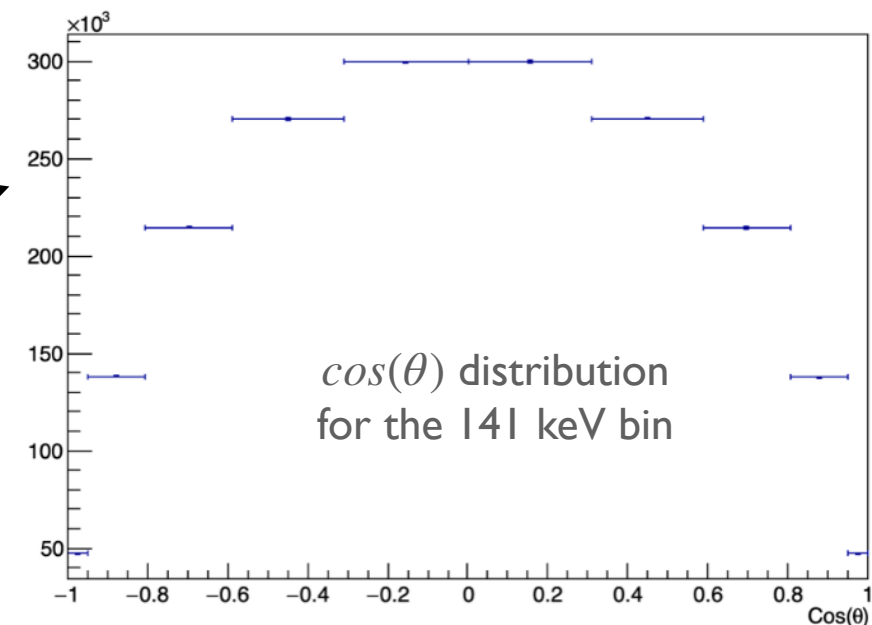
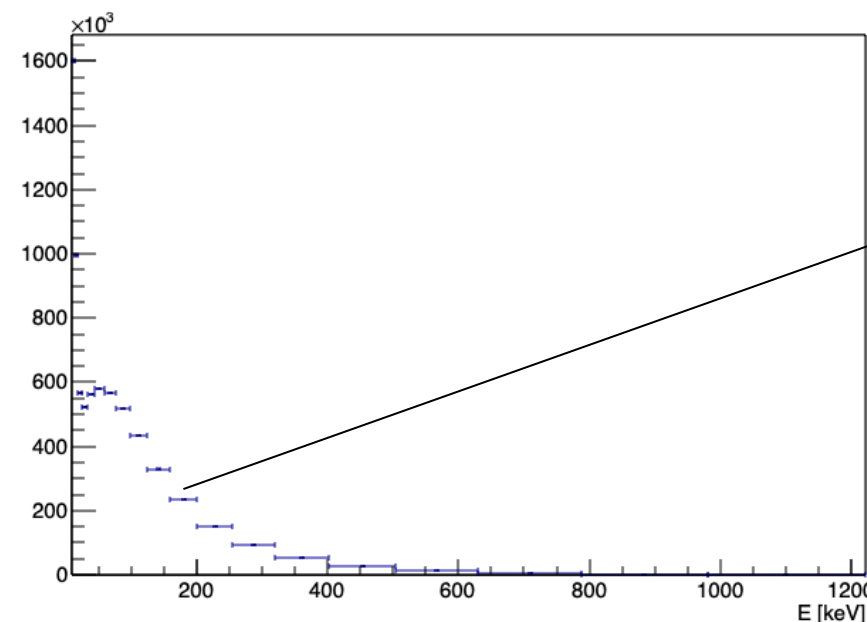
• Signal

Produced starting from the pp chain neutrino spectrum, simulating the interaction and adding the detector resolution



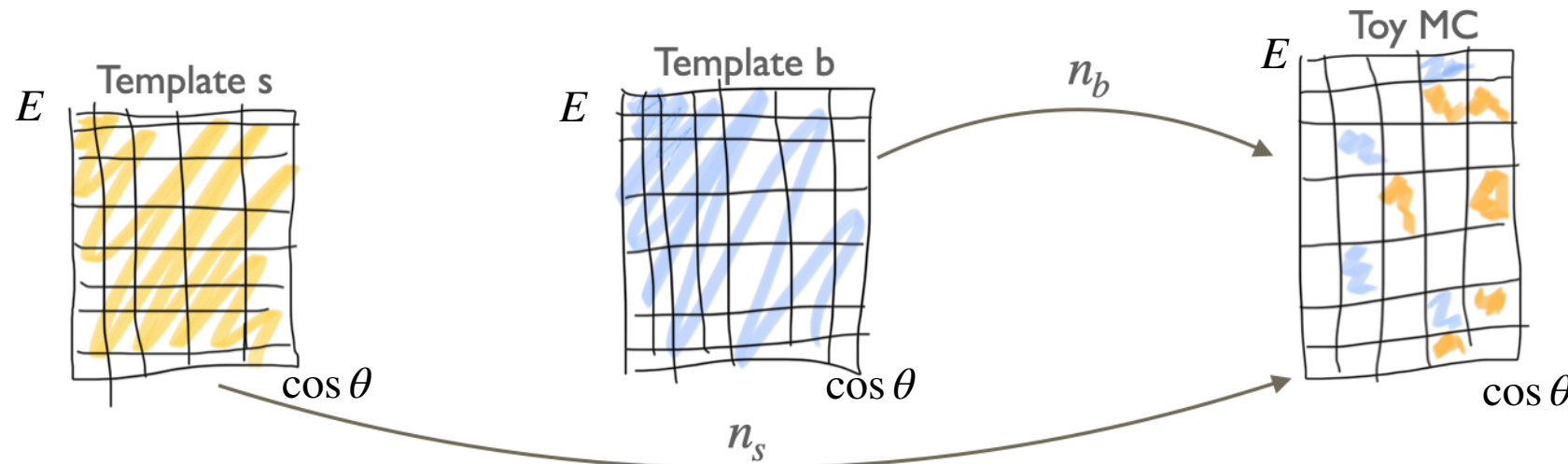
• Background

From CYGNO_30 background simulation, assuming an isotropic angular distribution



Toy-MC analysis

- Toy-MC generated by a hypothesis of expected number of events, extracting poissonianly the values of n_s and n_b , and filling an E-cos(θ) histogram with the extracted events from the templates



$$\bar{N}_s = 30 \text{ ev/y} \cdot \text{exp}$$

$$\bar{N}_b = 1.78 \cdot 10^4 \text{ ev/y} \cdot \text{exp} / R_f$$

- Each toyMC fit with B (H_0) model and S+B (H_1) model

0.5/0.5

- Calculation of the Bayes factor:
$$\frac{p(H_1|D)}{p(H_0|D)} = \frac{\int \mathcal{L}(D | \mu_b, \mu_s, H_1) \pi(\mu_b) \pi(\mu_s) d\mu_b d\mu_s}{\int \mathcal{L}(D | \mu_b, H_0) \pi(\mu_b) d\mu_b} \cdot \frac{\pi(H_1)}{\pi(H_0)} = B_f \frac{\pi(H_1)}{\pi(H_0)}$$

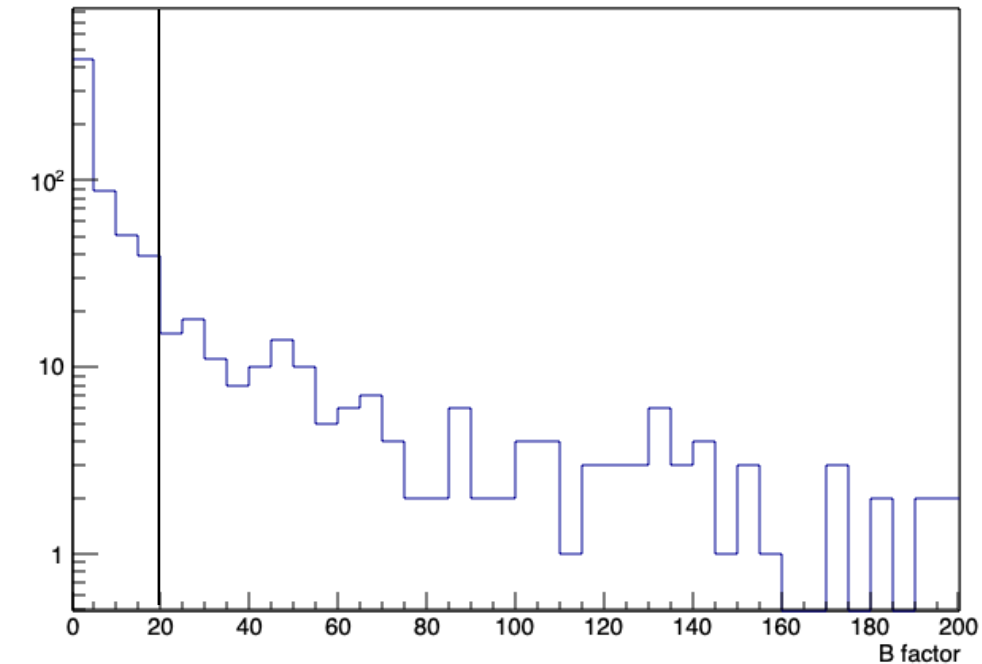
- Discovery probability with a BF>20 (=3 σ confidence level):

$$DP(\text{exp}, R_f) = \frac{N_{\text{toy}}(\text{BF} > 20)}{N_{\text{toy}}}$$

- Sensitivity studied as a function of detector exposure from 0.5 to 10 years.
- Given possible future reduction of materials radiopurity, not possible to predict today, sensitivity evaluated in various background reduction scenario

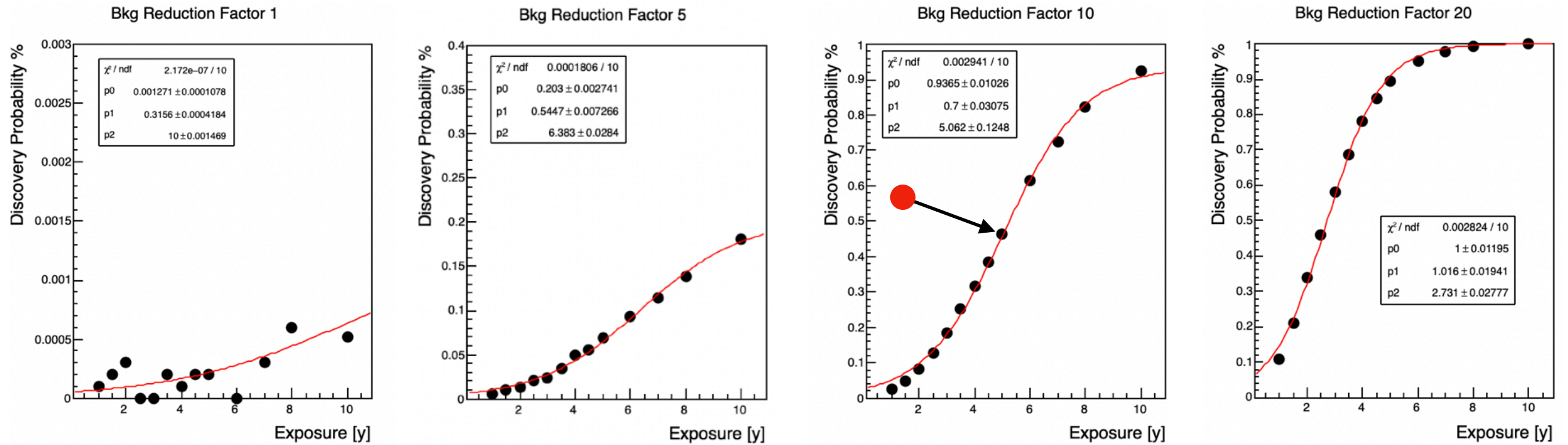
- 10000 Toy MC produced for each configuration

Bayes factor distribution for 1000 toy MC



Sensitivity results

- Plot of the **discovery probability with $BF > 20$** as a function of the exposure for different **further** background reduction



- With a further bkg reduction of a factor 10, in 5.5 y there is a 50% probability of collecting data for which the S+B model is at least 20 times (3σ) more probable than the only B model

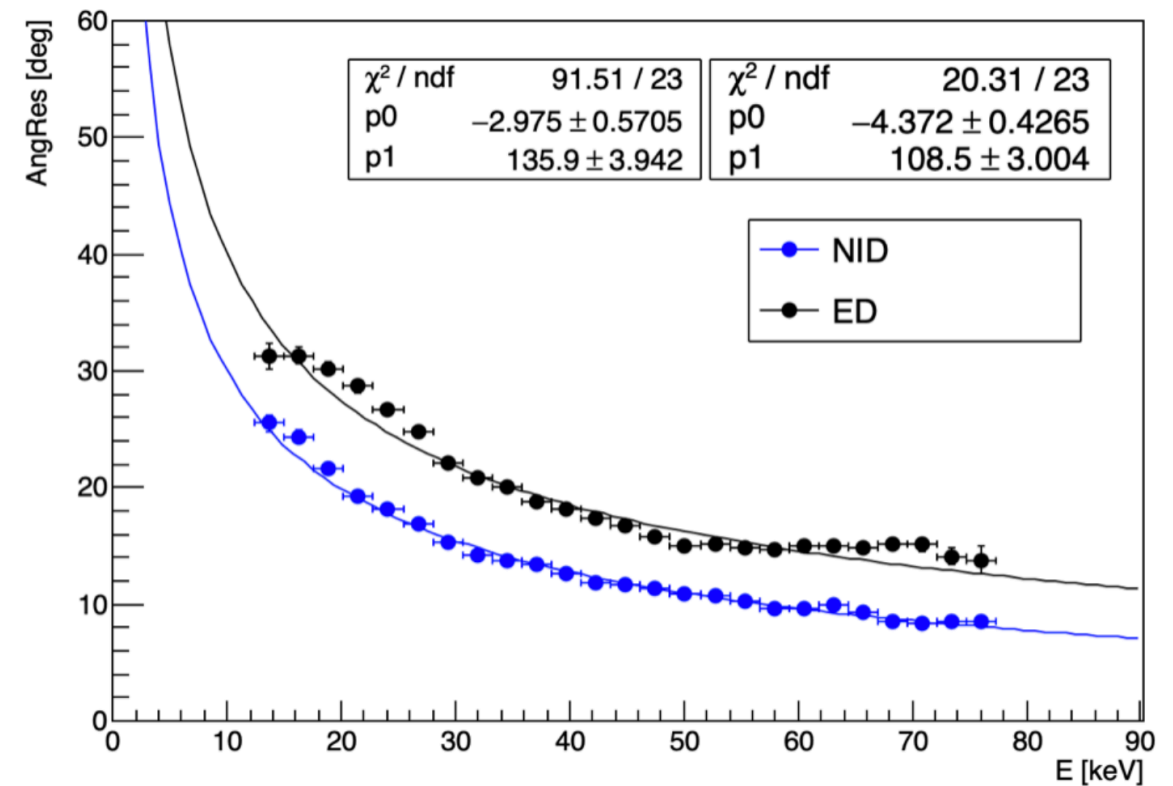
\bar{B}_{10}	$\ln \bar{B}_{10}$	sigma	category
2.5	0.9	2.0	
2.9	1.0	2.1	'weak' at best
8.0	2.1	2.6	
12	2.5	2.7	'moderate' at best
21	3.0	3.0	
53	4.0	3.3	
150	5.0	3.6	'strong' at best
43000	11	5.0	

- Exposure corresponding to 65 neutrino signal over 9790 ev. of background
- Equivalent to a rate $B_{\text{gk}}/\text{Signal} \simeq 60$, very strong background toleration
- Borexino in the pp measurement had a ratio $B_{\text{gk}}/\text{Signal} \simeq 2.3$

Trotta, Roberto. "Bayes in the sky: Bayesian inference and model selection in cosmology." *Contemporary Physics* 49 (2008): 104 - 71.

Sensitivity results with NID angular resolution

- Same study repeated with NID angular resolution assuming the same energy resolution
- No significant improvement obtained with only reduced diffusion:
 1. Sensitivity dominated by the energy resolution (improvement in both needed)
 2. Angular distribution of the scattered ER dominates

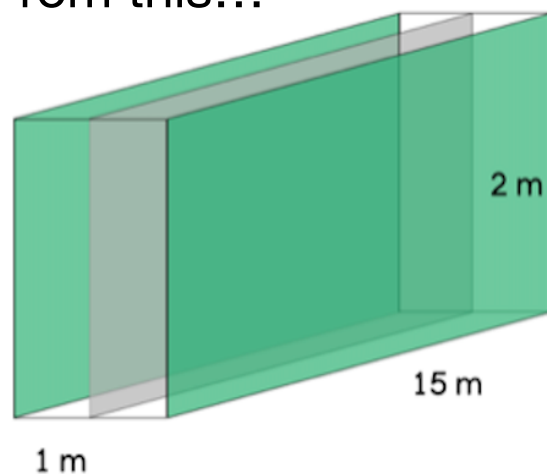


- However NID would allow to build a detector with 1.5 m drift length with still better performances than ED operation

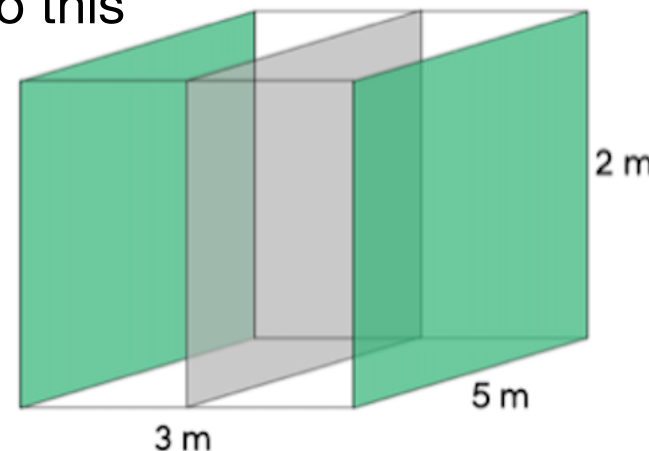


- More compact detector
- 1/3 of GEMs, cathodes, cameras...
- Less background
- Less shield required
- Much cheaper realization costs

From this...

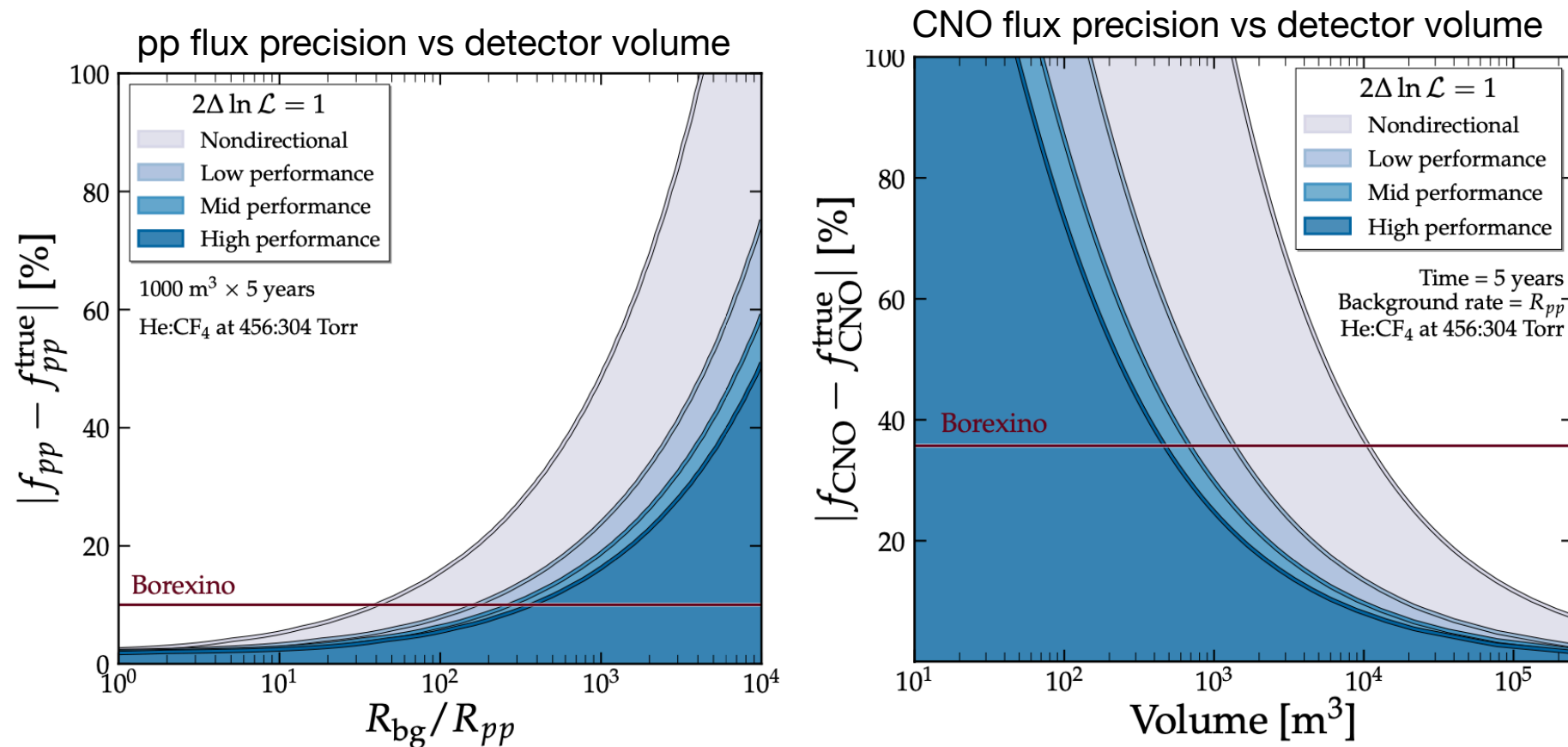


... to this



Future development in solar neutrino measurement

- Projection for the precision of a pp and CNO flux measurement in CYGNUS:



Lisotti, C., O'Hare, C. A., Baracchini, ... & Torelli, S. (2024). CYGNUS: Detecting solar neutrinos with directional gas time projection chambers. *arXiv preprint arXiv:2404.03690*.

- In the future no other experiments are expressly designed to measure pp and CNO neutrinos:
- JUNO's capability for a CNO measurement will strongly depend on the background expected (developed for reactor's neutrinos, might take 10s of years to reach the Borexino bgk level)
- DARWIN could precisely measure the pp but the Xe 2β decay might prevent CNO measurement
- It could be worth to invest on the gas TPC technology to study solar neutrino alongside with DM

Conclusions on the feasibility of a directional solar neutrino measurement

- Solar neutrinos has been proposed as object of study with directional TPC approach through $\nu - eES$
- Directionality can increase the bkg toleration and can allow for spectroscopic measurement of solar neutrinos

In my PhD thesis the feasibility of an observation of solar neutrino from the pp cycle with the CYGNO 30 m³ detector has been investigated

- The energy response and resolution of the 50L prototype have been studied and a simulation able to reproduce electron tracks has been developed
- In this context an algorithm to measure directionality of low energy electrons has been developed and optimised for CYGNO, and the angular resolution performances have been studied
- A simulation of the background expected in a CYGNO-30 detector has been performed and together with the detector performances will serve as benchmark for the whole CYGNUS collaboration
- As a result of this thesis work a CYGNO-30 experiment can perform an observation with 3σ sensitivity at 10 keV threshold in 5.5y if the background can be constrained to $\sim 10^3$ events/y
- This highlights the high discriminating power of the directionality capable of distinguishing 165 signal events over 9680 background events tolerating $R_{B/S} \sim 60$ (Borexino had 2.3 on the pp)