## From Spins to Strings

Jacob M. Leedom WISPs in String Cosmology 24XX.XXXX,24XX.XXXX, PRL 130 (2023) 18, 181801 w/Carl Beadle, Diego Blas, Itay Bloch, Jeff Dror, Sebastian Ellis, Stefania Gori, & Nicholas Rodd



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  - Axions
  - Dark Photons
  - Gravitons

[Talks by: Andreas, Federico, Joao, Nicole, Margherita, Gonzalo]

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- WISPy States:
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  - Gravitons
- As Cosmic Backgrounds:
  - Cosmic axion Background (CaB) relic density of relativistic ultralight axions
  - hidden CMB (hCMB) population of ultralight dark photons
  - Gravitational Wave Background (GWB)



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[Svrcek,Witten;'06] [Arvanitaki,Dimopoulos,Dubovsky, Kaloper,March-Russel;'09] [Cicoli,Goodsell,Ringwald;'12] [Cicoli,Guidetti,Righi,Westphal;'21]



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How can we detect them?

• Purely Gravitationally:  $\Delta N_{eff}$ 



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- This would indicate existence
- How can we get some more fine-grained information?

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WISPs manifest as effective magnetic fields  
Can be probed via spin-based experiments





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## Basics of NMR



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• One can start from Schrödinger equation for spins to find magnetization....or use the Bloch Equations:

$$\frac{d\mathsf{M}}{dt} = \mathsf{M} \times \gamma \mathsf{B} - \frac{M_x \hat{\mathsf{x}} + M_y \hat{\mathsf{y}}}{T_2} - \frac{(M_z - M_0)\hat{\mathsf{z}}}{T_1}$$

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- Magnetic field & magnetization composed of two pieces

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Perturbative expansion and decouple the equations

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$$\ddot{\mathcal{M}}_{x} + \frac{2}{T_{2}}\dot{\mathcal{M}}_{x} + \omega_{0}^{2}\mathcal{M}_{x} = \gamma\omega_{0}\mathcal{M}_{0}(\hat{x}\cdot\vec{B}_{w}) - \gamma\mathcal{M}_{0}\frac{d}{dt}(\hat{y}\cdot\vec{B}_{w})$$

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• Perturbative expansion and decouple the equations

$$\ddot{M}_{x} + \frac{2}{T_{2}}\dot{M}_{x} + \omega_{0}^{2}M_{x} = 2g_{N}M_{0}\omega_{0}(\hat{x}\cdot\nabla a) - 2g_{N}M_{0}\frac{d}{dt}(\hat{y}\cdot\nabla a)$$

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• Damped & Driven SHO – general solution via Green's function:

$$M_{x}(t) = C_{1}e^{-t/T_{2}}\cos(\omega_{0}t) + C_{2}e^{-t/T_{2}}\sin(\omega_{0}t) + \int_{0}^{t}G(t-s)F(s)ds$$

• 
$$G(t) = \frac{1}{\Omega} e^{-t/T_2} \sin[\Omega t]$$
 •  $\Omega^2 = \omega_0^2 - T_2^{-2}$ 

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• From here can get the power spectral density (PSD) of signal

$$P_k := rac{\Delta t}{T} \langle \widetilde{M}_k^2 
angle \qquad \qquad \widetilde{M}_k := \sum_{n=0}^{N-1} M(n\Delta t) e^{-2\pi i k n/N}$$

• NMR used in CASPEr searches for QCD axion dark matter

[Graham,Rajendran,'13] [Budker,Graham,Ledbetter, Rajendran,Sushkov,'13] [Jackson Kimball et al.,'17]



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  - Realize sufficiently long  $T_2$
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  - Elucidate scan strategy
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$$\nabla a(t) = \sqrt{\frac{2\rho_a}{N_a\bar{\omega}}} \sum_{i=1}^{N_a} \frac{\vec{k_i}}{\sqrt{\omega_i}} \sin[\omega_i t + \phi_i] \qquad \qquad \bullet \omega_i \approx m_a (1 + v_i^2/2) \\ \bullet \vec{k_i} \approx m_a \vec{v_i} \\ \bullet \phi_i \in [0, 2\pi)$$

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• Assume CaB couples to nucleons:  $\mathcal{L} \supset g_N^{(a)}(\partial_\mu a) \bar{N} \gamma^\mu \gamma^5 N$ 

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- Assume CaB couples to nucleons:  $\mathcal{L} \supset g_N^{(a)}(\partial_\mu a) \bar{N} \gamma^\mu \gamma^5 N$
- Can leverage the hard work above to map QCD axion projections to CaB projections:

$$\rho_{a} = \rho_{\rm DM} \sqrt{\frac{T_2}{\tau_a}} \left(\frac{g_N^{\rm (DM)}}{g_N^{(a)}}\right)^2 \left(\frac{v_{\rm DM}}{v_a}\right)^2$$

- Assume C<sub>a</sub>B couples to nucleons:  $\mathcal{L} \supset g_N^{(a)}(\partial_\mu a) \bar{N} \gamma^\mu \gamma^5 N$
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Define

$$\Omega_{a} := \frac{1}{\rho_{c}} \frac{d\rho_{a}}{d\ln\omega}$$

• Assume CaB couples to photons:  $\mathcal{L} \supset \frac{g_{ga\gamma\gamma}}{A}F_{\mu\nu}\widetilde{F}^{\mu\nu}$ 



[Dror,Murayama,Rodd, '21]

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## NMR Application: Dark Photons



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## NMR Application: Gravitational Waves

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