

# $b \rightarrow c\tau^-\bar{\nu}_\tau$ semileptonic decays

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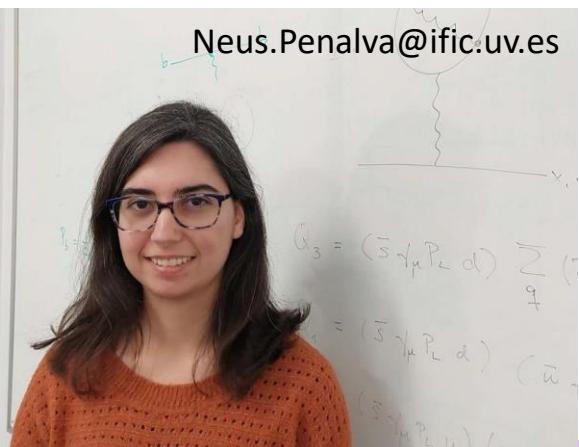
IFIC (CSIC-UV)

Welcome day, UniTo  
Sunday, 3 November 2024



# Who am I?

- I'm from Crevillent, a small city near Alacant
- Master and PhD student at Instituto de Física Corpuscular in Valencia (2019-2023)
- Postdoc at Universitat de Barcelona (2024)
- Now, postdoc at IFIC and INFN Torino (Spanish grant CIAPOS)



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# Who am I?

But I am much more than my work!



Things that I like:

- Embroidery (and textile arts in general)
- Traditional dances
- Music
- Videogames



*at*



Things that I love (and miss so much):

- Chispitas



# Outline

1. Introduction
  - i. The SM and LFU
  - ii.  $b \rightarrow c\tau\bar{\nu}_\tau$  decays and New Physics
2. New observables in  $b \rightarrow c\tau\bar{\nu}_\tau$  decays
  - i. Formalism
  - ii. Observables
  - iii. Tau decay
3. Final remarks



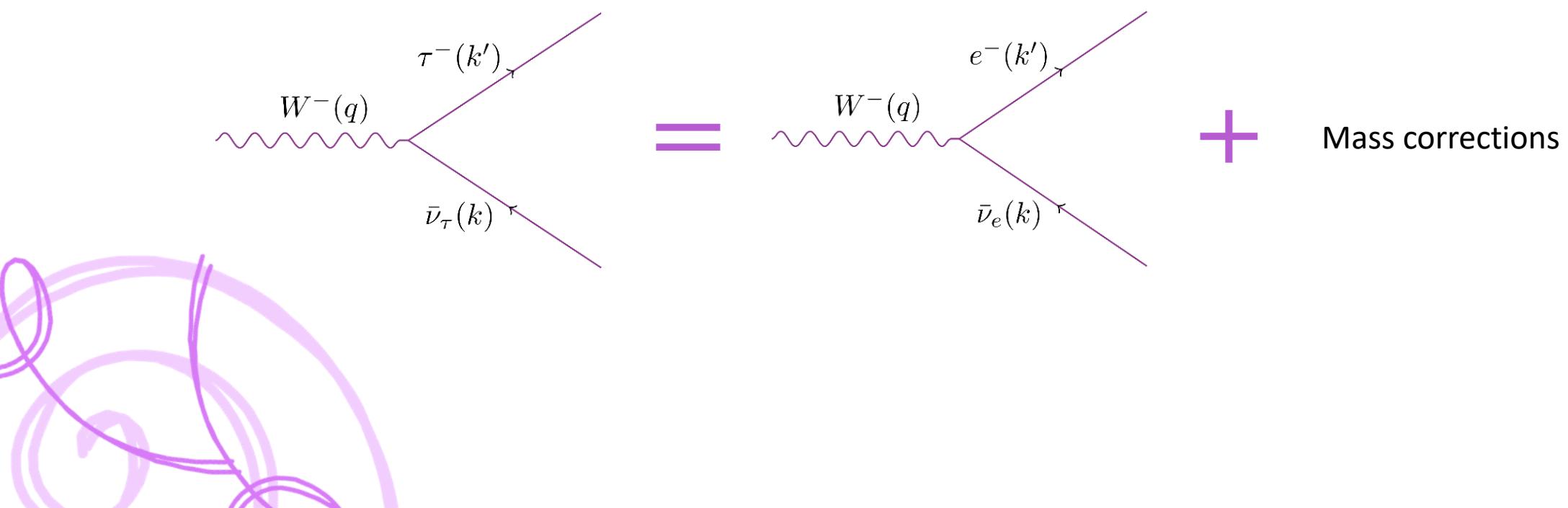
# Standard model

- Describes all known fundamental particles in nature and their interactions.
- Elementary particles
  - Fermions:
    - Three families of quarks and leptons
  - Bosons
    - Gluons (strong force mediators)
    - Photon (electromagnetism mediator)
    - Z and W (weak force mediators)
    - Higgs boson

QUARKS		GAUGE BOSONS	
mass →	$\approx 2.3 \text{ MeV}/c^2$	mass →	$\approx 126 \text{ GeV}/c^2$
charge →	2/3	charge →	0
spin →	1/2	spin →	0
	u		g
	charm		Higgs boson
	t		
	top		
	d		
	strange		
	b		
	bottom		
	γ		
	photon		
mass →	$\approx 4.8 \text{ MeV}/c^2$	mass →	$\approx 95 \text{ MeV}/c^2$
charge →	-1/3	charge →	-1
spin →	1/2	spin →	1/2
	e		Z
	electron		Z boson
	μ		
	tau		
mass →	$\approx 105.7 \text{ MeV}/c^2$	mass →	$\approx 1.777 \text{ GeV}/c^2$
charge →	-1	charge →	-1
spin →	1/2	spin →	1/2
	τ		W
	tau		W boson
mass →	$\approx 0.511 \text{ MeV}/c^2$	mass →	$\approx 91.2 \text{ GeV}/c^2$
charge →	-1	charge →	0
spin →	1/2	spin →	1
	e		
	electron		
	μ		
	τ		
mass →	$< 2.2 \text{ eV}/c^2$	mass →	$\approx 80.4 \text{ GeV}/c^2$
charge →	0	charge →	±1
spin →	1/2	spin →	1
	ν <sub>e</sub>		
	electron neutrino		
	ν <sub>μ</sub>		
	muon neutrino		
	ν <sub>τ</sub>		
	tau neutrino		

# Lepton Flavour Universality

- Lepton Flavour Universality:
  - The coupling of the gauge bosons to the leptons is flavour independent.
  - The SM predictions should be the same for all 3 families of leptons except for mass effects.

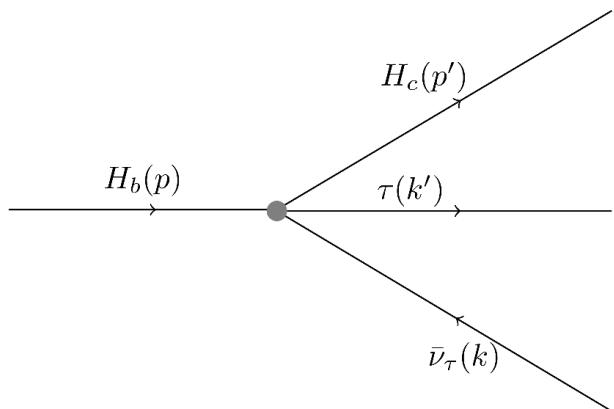


# LFU in $b \rightarrow c\tau\bar{\nu}_\tau$ decays

Quarks live in hadrons → Look into hadronic decays of  $\Lambda_b$  baryons and  $B$ -mesons



Let's focus only on the exclusive decays.



$$\mathcal{R}(H_c) = \frac{\Gamma(H_b \rightarrow H_c \tau \bar{\nu}_\tau)}{\Gamma(H_b \rightarrow H_c \ell \bar{\nu}_\ell)} = 1 + \text{mass corrections};$$

$H_b \rightarrow H_c = \bar{B} \rightarrow D, \bar{B} \rightarrow D^*, \Lambda_b \rightarrow \Lambda_c \dots$

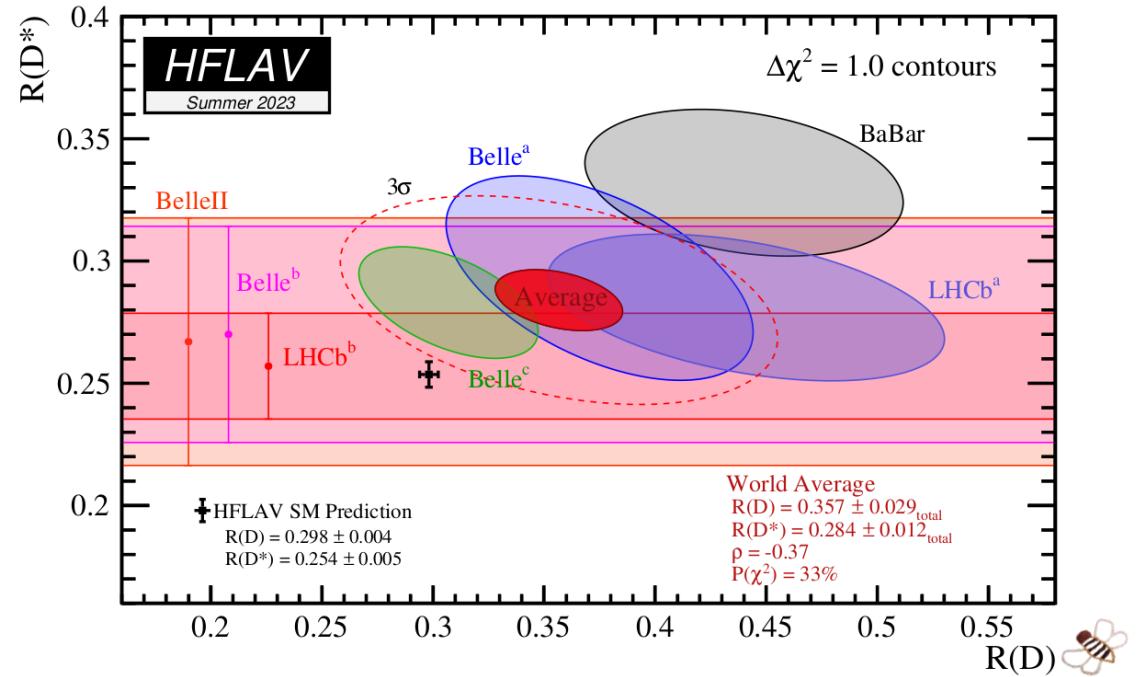
$\ell = e, \mu$

# LFU Violation?

- Combined results for  $\mathcal{R}(D), \mathcal{R}(D^*)$  show a  $\sim 3\sigma$  deviation from the SM.<sup>1</sup>
- Deviations also in  $\mathcal{R}(\Lambda_c)$  and other observables as  $P_\tau(D^*)$  and  $F_L^{D^*}$ .

Possible explanations:

- Experimental results
- Hadronic inputs (form factors)
- New physics!



# New physics effects

One way of adding NP effects is considering the most general effective Hamiltonian:

$$H_{\text{eff}} = \frac{4G_F V_{cb}}{\sqrt{2}} \left[ \underbrace{(1 + C_{LL}^V) \mathcal{O}_{LL}^V + C_{RL}^V \mathcal{O}_{RL}^V}_{\text{(axial-)vector}} + \underbrace{C_{LL}^S \mathcal{O}_{LL}^S + C_{RL}^S \mathcal{O}_{RL}^S}_{\text{(pseudo-)scalar}} + \underbrace{C_{LL}^T \mathcal{O}_{LL}^T}_{\text{tensor}} \right. \\ \left. + \underbrace{C_{LR}^V \mathcal{O}_{LR}^V + C_{RR}^V \mathcal{O}_{RR}^V + C_{LR}^S \mathcal{O}_{LR}^S + C_{RR}^S \mathcal{O}_{RR}^S + C_{RR}^T \mathcal{O}_{RR}^T}_{\text{right-handed neutrinos}} \right] + h.c.,$$

- $\mathcal{R}(D), \mathcal{R}(D^*)$  expressions depend on these  $C_{ij}^\Gamma$ .
- Different sets of  $C_{ij}^\Gamma$  (NP models) are, in general, fitted to the anomalies observed in the semileptonic B-meson decays.
- We need more observables/measures to distinguish among these models.

# What can we do?

- Propose NP models and try to adjust them.
- Do global fits
- Defining new observables
- Sensibility studies of the observables



- 1.- General formalism for studying  $b \rightarrow c$  exclusive semileptonic decays
- 2.- Studying different angular and spin asymmetries
- 3.- Look to the  $\tau$  decay products.



# 1.- Formalism

## Squared amplitude

The observable quantities will be proportional to the squared amplitude of the decay

$$\Gamma, \frac{d\Gamma}{d\omega ds_{13}}, A_{FB} \propto |\mathcal{M}|^2$$

$$\mathcal{M} = \left( J_H^\alpha J_\alpha^L + J_H J^L + J_H^{\alpha\beta} J_{\alpha\beta}^L \right)_{\bar{\nu}_\ell L} + \left( J_H^\alpha J_\alpha^L + J_H J^L + J_H^{\alpha\beta} J_{\alpha\beta}^L \right)_{\bar{\nu}_\ell R}$$

### Hadronic matrix elements

- Depend on the considered hadrons
- Difficult to compute: Form Factor parametrization

### Leptonic currents

- Have into account the lepton polarization
- Easy to compute

What we do: We separate the squared amplitude in leptonic and hadronic tensors

$$\overline{\sum} |\mathcal{M}|^2 = \sum_{\chi=L,R} \left[ \sum_{(\alpha\beta)(\rho\lambda)} L_{(\alpha\beta)(\rho\lambda)}(k, k', h_\chi) W_\chi^{(\alpha\beta)(\rho\lambda)}(p, q) \right]$$

# 1. Formalism

## Hadronic tensors

$$\overline{\sum} |\mathcal{M}|^2 = \sum_{\chi=L,R} \left[ \sum_{(\alpha\beta)(\rho\lambda)} L_{(\alpha\beta)(\rho\lambda)}(k, k', h_\chi) \underline{W_\chi^{(\alpha\beta)(\rho\lambda)}(p, q)} \right]$$

The hadronic tensors can be decomposed in linear combinations of Lorentz structures using Lorentz, parity and time-reversal transformations.

- This decomposition is **general** for all decays.
- At most **quadratic** in  $q$  and  $p$ .
- The coefficients multiplying the Lorentz tensors are scalars ( $W_i(q^2)$ ) called **structure functions (SFs)**.
- There are **16 SFs for each neutrino chirality** and are functions of  $q^2$  or  $\omega$  and the WCs.

# 1.- Formalism

## Observables and Structure functions

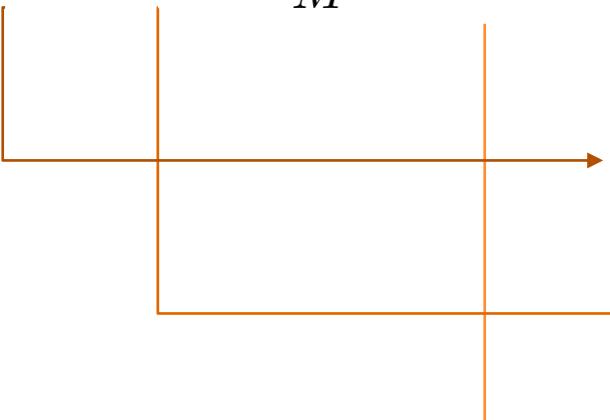
The observables depend on the structure functions and are general.

For example in the SM:

$$W^{\mu\nu}(p, q) = -g^{\mu\nu}W_1 + \frac{p^\mu p^\nu}{M^2}W_2 + i\epsilon^{\mu\nu\alpha\beta}p_\alpha q_\beta \frac{W_3}{2M^2} + \frac{q^\mu q^\nu}{M^2}W_4 + \frac{p^\mu q^\nu + p^\nu q^\mu}{2M^2}W_5,$$

An therefore the square matrix element:

$$\frac{2 \sum |\mathcal{M}|^2}{M^2} = \frac{1}{2} \left[ \mathcal{A}(\omega) + \mathcal{B}(\omega) \frac{(k \cdot p)}{M^2} + \mathcal{C}(\omega) \frac{(k \cdot p)^2}{M^4} \right]$$



$$\mathcal{A}(\omega) = \frac{q^2 - m_\ell^2}{M^2} \left\{ 2W_1 - W_2 + \frac{M_\omega}{M} W_3 + \frac{m_\ell^2}{M^2} W_4 \right\},$$

$$\mathcal{B}(\omega) = -\frac{2q^2}{M^2} W_3 + \frac{4M_\omega}{M} W_2 + \frac{2m_\ell^2}{M^2} W_5,$$

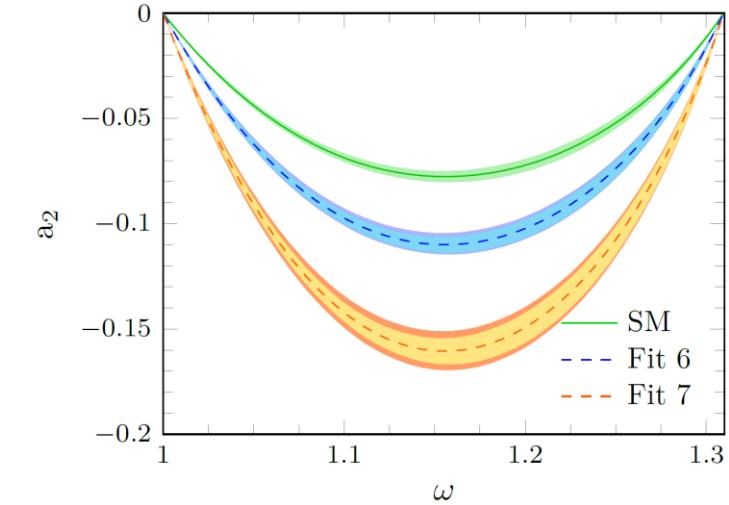
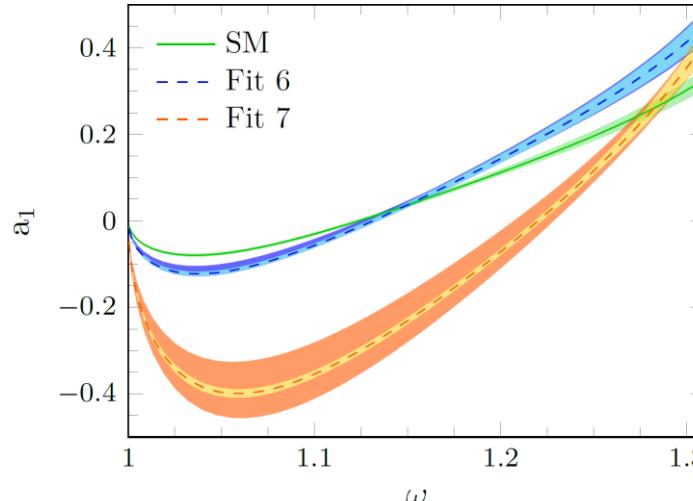
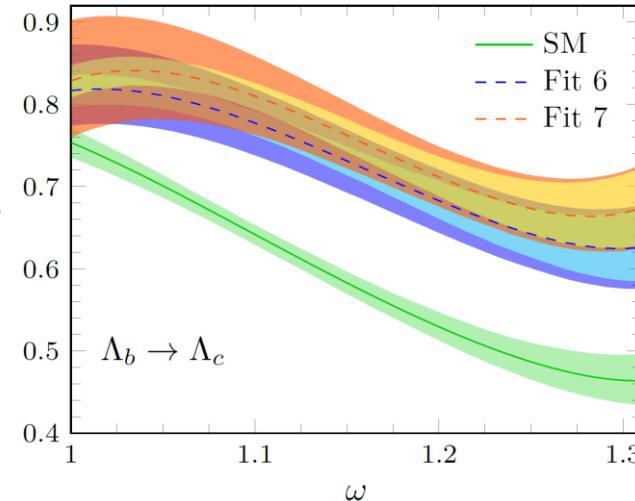
$$\mathcal{C}(\omega) = -4W_2.$$

## 2.- Observables

### CM frame

$$\frac{d\Gamma}{d\omega ds_{13}} \xrightarrow[\substack{\text{CM} \\ (\vec{p} - \vec{p}' = 0)}]{} \frac{d^2\Gamma}{d\omega d\cos\theta_\ell} = \frac{\Gamma_0 M^3 M'}{2} \sqrt{\omega^2 - 1} \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left\{ a_0(\omega) + a_1(\omega) \cos\theta_\ell + a_2(\omega) \cos^2\theta_\ell \right\},$$

We can measure  $a_0$ ,  $a_1$  and  $a_2$  which are related to the forward-backward asymmetry.



## 2.- Observables

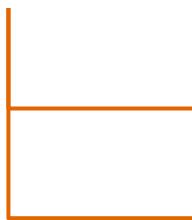
### Lab frame and polarization

Similarly, we could go to the LAB frame ( $\vec{p} = 0$ ) and study the tau-energy distribution.



$c_0, c_1, c_2$  with the same information as the functions before

Or consider the polarized distributions in both cases.



3 new functions for the angular distribution.

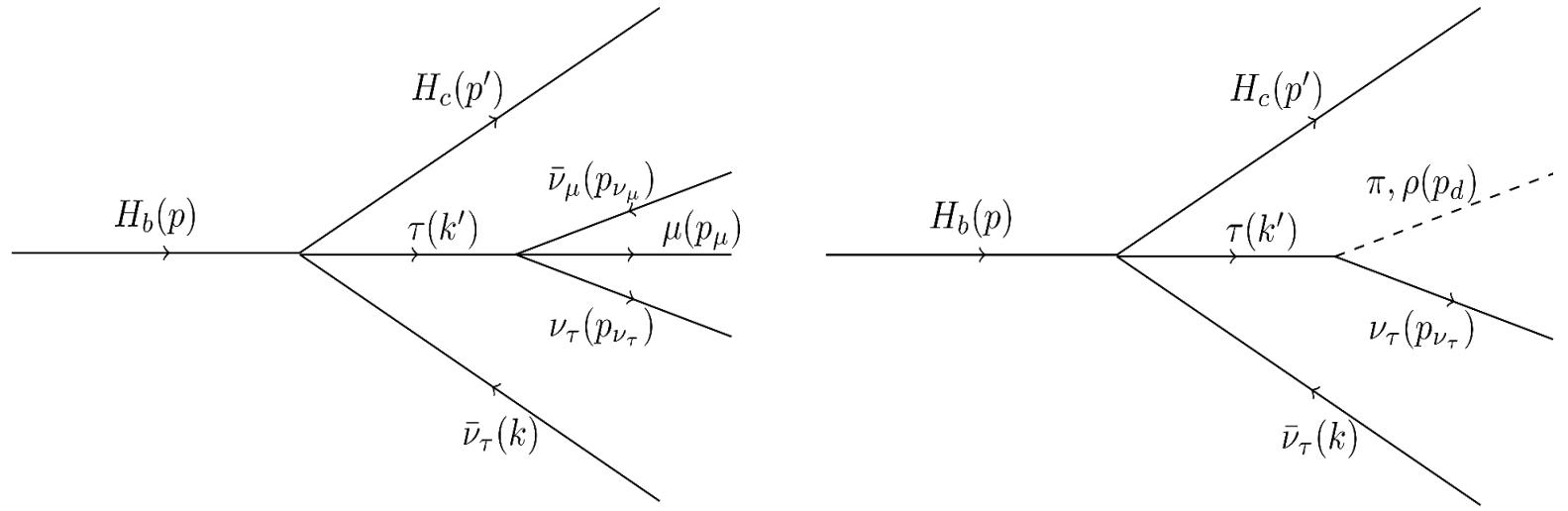
4 new functions for the energy distribution.



### 3.- Tau decay

#### Visible kinematics

- One would need to measure the outgoing  $\tau$  4-momentum and polarization state.
- The  $\tau$  does not travel far and in any case determining the polarization is challenging.
- Its decay involves at least one more neutrino  $\rightarrow$  Difficult to reconstruct.
- **Solution:** relying on the variables of the  $\tau$  decay charged products.



### 3.- Tau decay

#### Visible kinematics in the CM frame

We rely on the kinematical variables of the visible products ( $\mu$ ,  $\pi$  and  $\rho$ )

$$\frac{d^3\Gamma_d}{d\omega d\xi_d d \cos \theta_d}$$

$\cos \theta_d$ : angle between the charged particle and the final hadron

$\xi_d$ : proportional to the energy of the charged particle in the CM frame

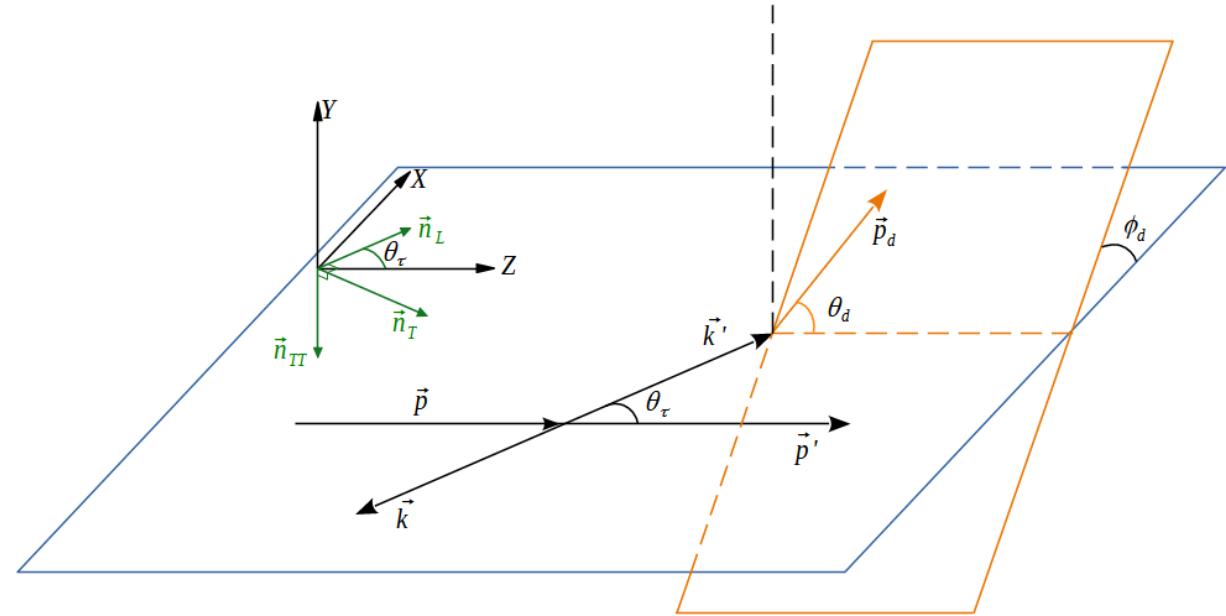
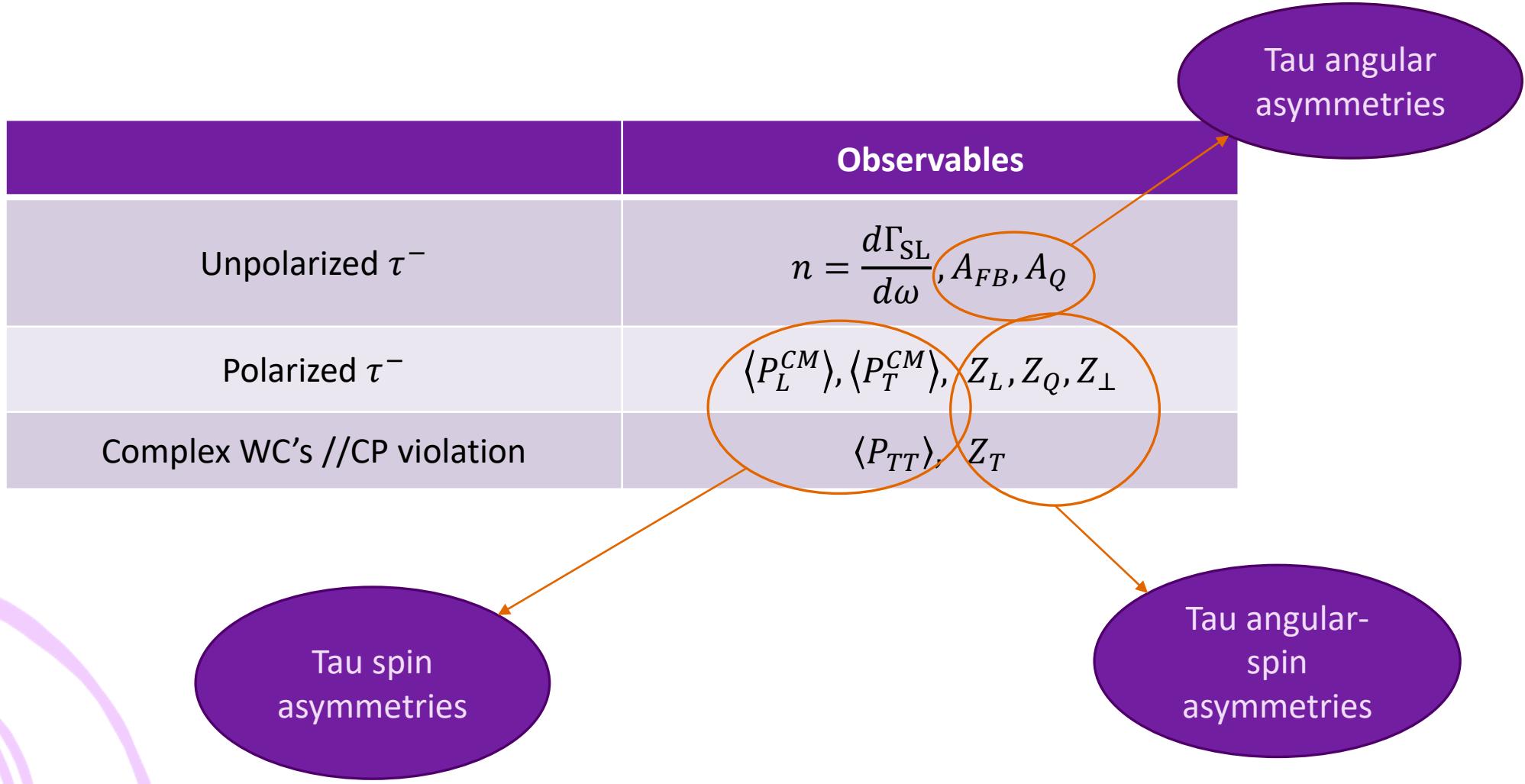


Figure: Kinematics in the  $\tau^- \bar{\nu}_\tau$  CM reference system and the unit vectors ( $\vec{n}_L$ ,  $\vec{n}_T$  and  $\vec{n}_{TT}$ ).



### 3.- Tau decay

#### Observables



### 3.- Tau decay

#### Partially integrated visible distributions

We integrate some of the variables  
to increase statistics

The diagram illustrates the process of integrating variables to simplify the decay rate. It starts with the full three-dimensional distribution  $\frac{d^3\Gamma_d}{d\omega d\xi_d d\cos\theta_d}$ , which is shown as a purple wavy line. This is integrated over  $d\xi_d$  to obtain the two-dimensional distribution  $\frac{d^2\Gamma_d}{d\omega d\cos\theta_d}$ , represented by an orange wavy line. This distribution is then integrated over  $d\cos\theta_d$  to get the one-dimensional distribution  $\frac{d\Gamma_d}{d\cos\theta_d}$ . Finally, it is integrated over  $d\omega$  to obtain the distribution  $\frac{d\Gamma_d}{dE_d} = \mathcal{B}_d \frac{d\Gamma_{SL}}{d\omega}$ , represented by a black wavy line.

$$\frac{d^3\Gamma_d}{d\omega d\xi_d d\cos\theta_d} \xrightarrow{\int d\xi_d} \frac{d^2\Gamma_d}{d\omega d\cos\theta_d} \xrightarrow{\int d\cos\theta_d} \frac{d\Gamma_d}{d\cos\theta_d}$$

$$\xrightarrow{\int d\omega} \frac{d\Gamma_d}{dE_d} = \mathcal{B}_d \frac{d\Gamma_{SL}}{d\omega}$$

### 3.- Tau decay

#### The normalized $d\Gamma/dE_d$ distribution

The only surviving term is:

$$\widehat{F}_0^d(E_d) = \frac{1}{\Gamma_{\text{SL}}} \int_1^{\omega_{\text{sup}}(E_d)} \frac{1}{\gamma} \frac{d\Gamma_{\text{SL}}}{d\omega} \left\{ C_n^d(\omega, E_d) + C_{P_L}^d(\omega, E_d) \langle P_L^{\text{CM}} \rangle(\omega) \right\} d\omega,$$

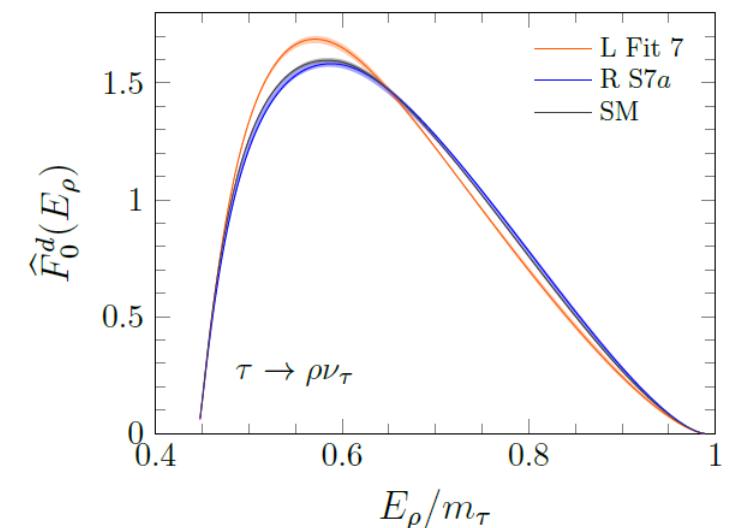
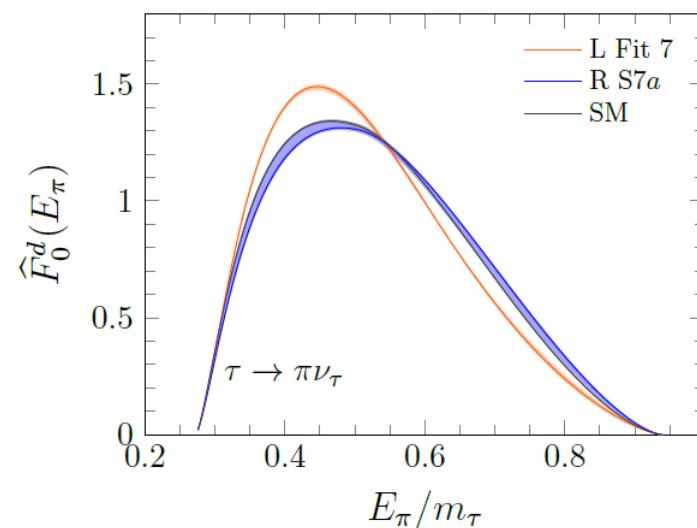
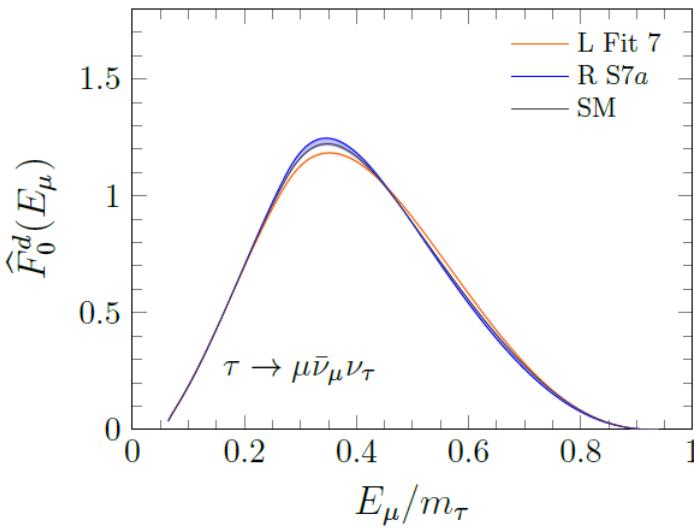


Figure: Energy  $d\Gamma/dE_d$  distribution for the  $\Lambda_b \rightarrow \Lambda_c \tau \bar{\nu}_\tau$  decay and each of the  $\tau$  decay modes.

### 3.- Tau decay

#### The $d\Gamma/(d \cos \theta_d)$ distribution

We loose the information on  $\langle \mathcal{P}_L^{\text{CM}} \rangle$  but not in the remaining asymmetries.

$$\frac{d\Gamma_d}{d \cos \theta_d} = \mathcal{B}_d \Gamma_{\text{SL}} \left[ \frac{1}{2} + \hat{F}_1^d \cos \theta_d + \hat{F}_2^d P_2(\cos \theta_d) \right].$$

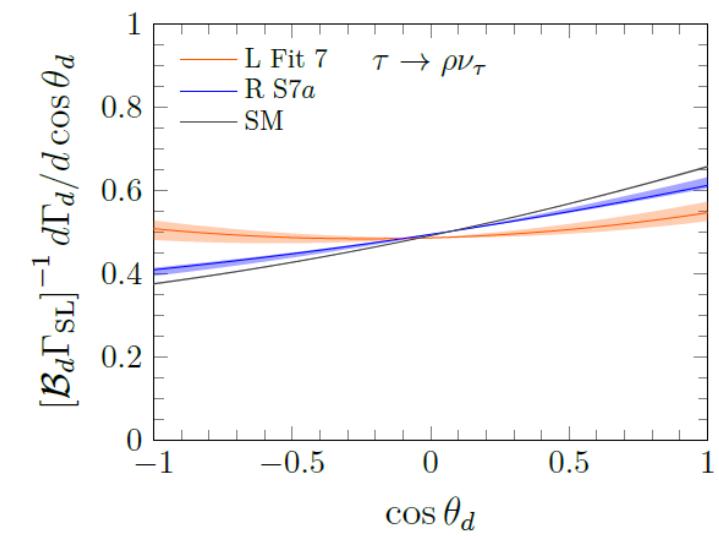
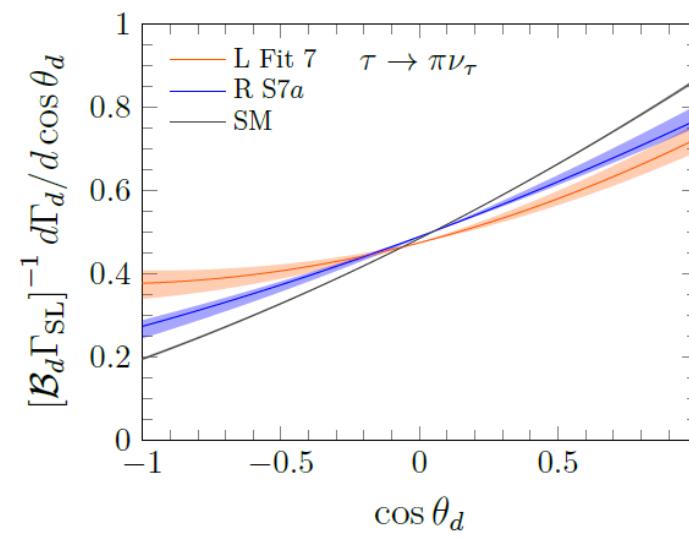
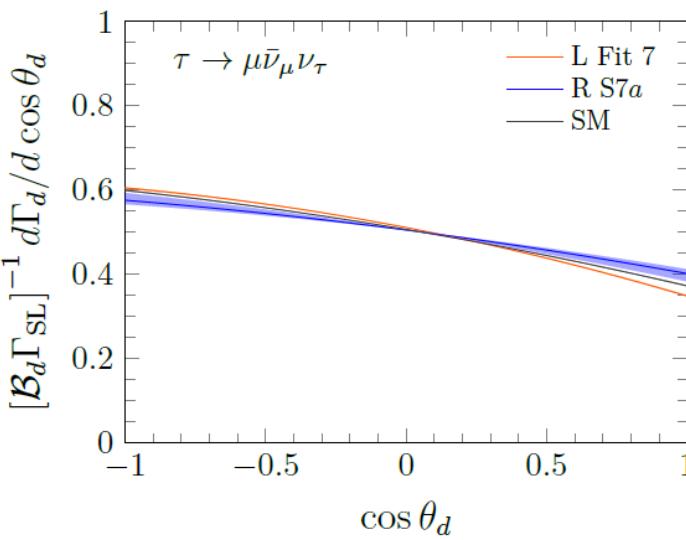


Figure: Angular  $d\Gamma/d \cos \theta_d$  distribution for the  $\Lambda_b \rightarrow \Lambda_c$  decay and each of the  $\tau$  decay modes.

## Final remarks

- We have proposed different observables that are sensitive to NP effects, which we have computed for different extensions of the SM.
- If the LFU anomalies observed in semileptonic B meson decays are confirmed, we still need to combine as many observables and decays as possible, in order to determine the preferred NP extension of the SM.

GRAZIE!!

