

Recent results within the sd and fpg shells

J.M. Allmond – ORNL

*On behalf of the CLARION2-TRINITY
and FDSi@FRIB Collaborations*

ORNL is managed by UT-Battelle, LLC for the US Department of Energy

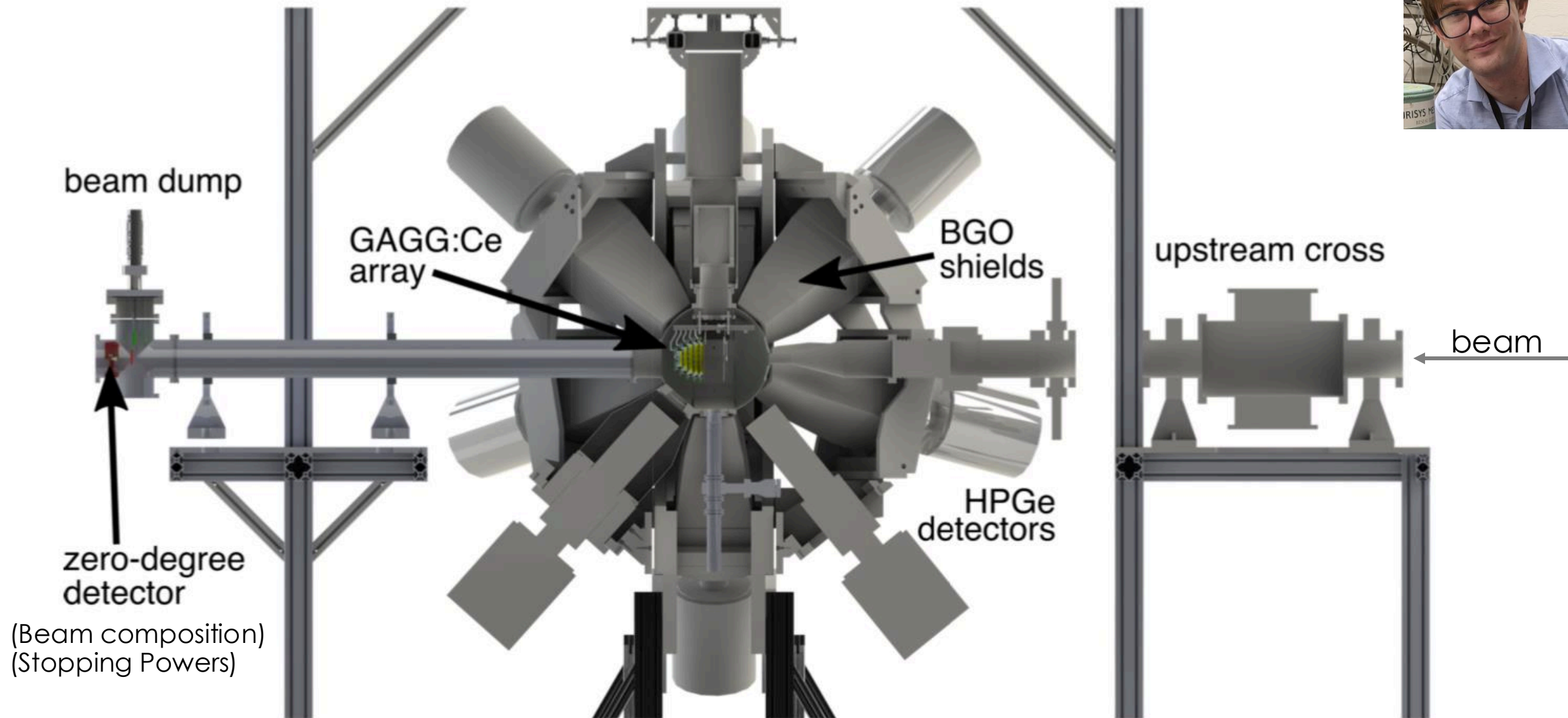


U.S. DEPARTMENT OF
ENERGY

Tim Gray



CLARION2-TRINITY @ FSU



Liquid Drop Representation of Shape

$$r = R(1 + \beta_2 Y_{20} + \beta_3 Y_{30} + \dots)$$

Monopole term (volume)

$R = 1.2A^{1/3}$ or from other theory

~ 0 for, e.g., Ti isotopes

$$\beta_2^2 \sim \langle Q^2 \rangle$$

Liquid Drop Representation of Shape

$$\begin{aligned}\langle r^2 \rangle &= \langle r^2 \rangle_{\text{sph}} + \langle r^2 \rangle_Q \\ &= (3/5)R^2 + (4\pi / 3Z^2R^2)\langle Q^2 \rangle\end{aligned}$$

$$\begin{aligned}\delta \langle r^2 \rangle &= \delta \langle r^2 \rangle_{\text{sph}} + \delta \langle r^2 \rangle_Q \\ &\sim \delta \langle r^2 \rangle_{\text{sph}} + (4\pi / 3Z^2R^2)\delta \langle Q^2 \rangle\end{aligned}$$

Liquid Drop Representation of Shape

$$\begin{aligned} \overset{\text{Measurable}}{\langle r^2 \rangle} &= \langle r^2 \rangle_{\text{sph}} + \overset{\text{Measurable}}{\langle r^2 \rangle_Q} \\ &= (3/5)R^2 + (4\pi / 3Z^2R^2)\langle Q^2 \rangle \end{aligned}$$

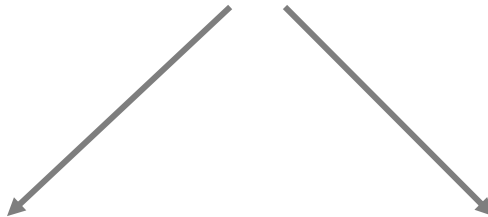
$$\begin{aligned} \overset{\text{Measurable}}{\delta \langle r^2 \rangle} &= \delta \langle r^2 \rangle_{\text{sph}} + \overset{\text{Measurable}}{\delta \langle r^2 \rangle_Q} \\ &\sim \delta \langle r^2 \rangle_{\text{sph}} + (4\pi / 3Z^2R^2)\delta \langle Q^2 \rangle \end{aligned}$$

Ground-State Deformation $\langle Q^2 \rangle$

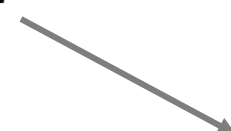
Couple E2 operators to a frame-invariant quantity

$$\{E2 \times E2\}^0 = \frac{1}{\sqrt{5}} Q^2$$

Ground State


$$\langle s | \{E2 \times E2\}^0 | s \rangle = \frac{1}{\sqrt{2s+1}} \langle s || \{E2 \times E2\}^0 || s \rangle$$

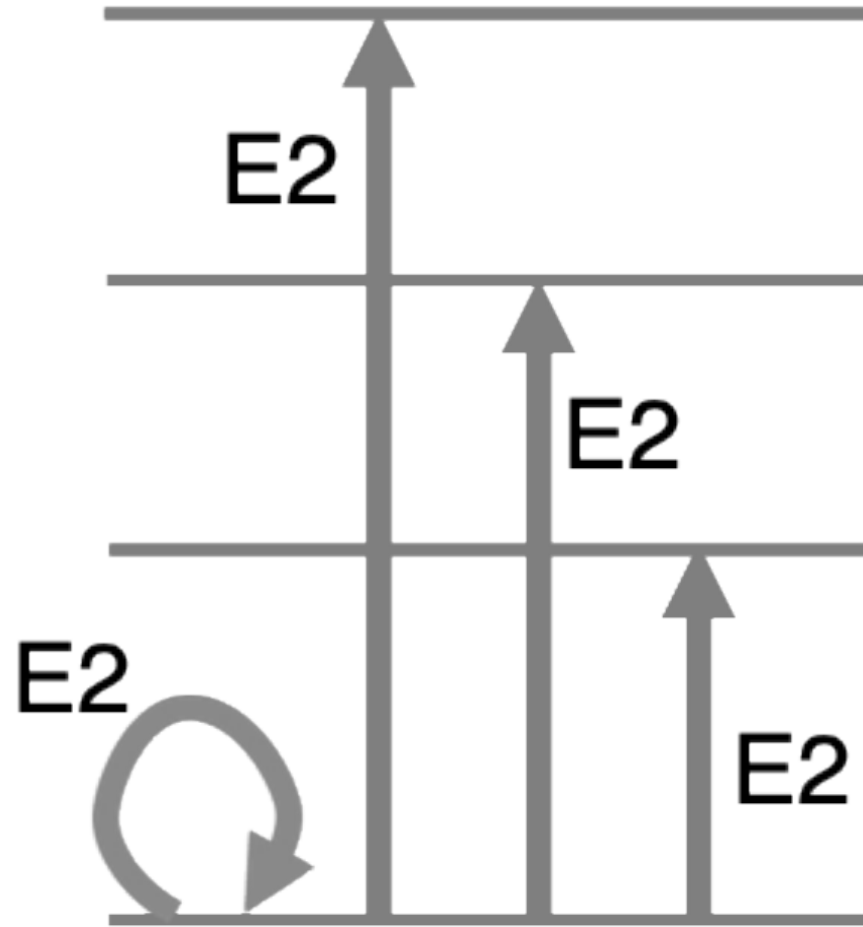
$$= \frac{1}{\sqrt{2s+1}} (-1)^{2s} \sum_r \langle s || E2 || r \rangle \langle r || E2 || s \rangle \left\{ \begin{matrix} 2 & 2 & 0 \\ s & s & r \end{matrix} \right\},$$



Sum over intermediate states

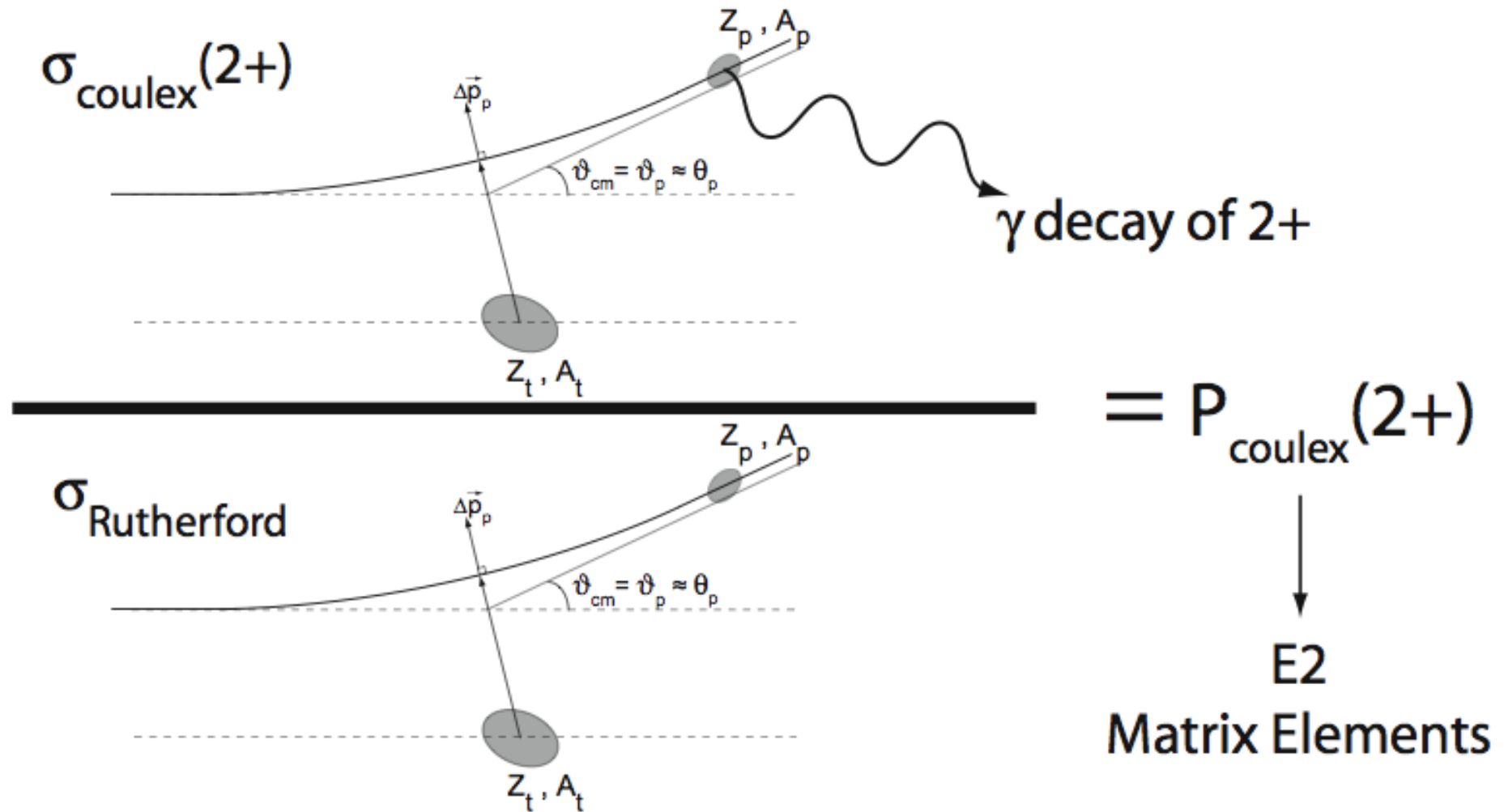
Ground-State Deformation $\langle Q^2 \rangle$

Essentially the $B(E2)$ sum, with addition of **ground-state moment** term if spin is non-zero



Coulomb Excitation – E2 Moments

Coulomb excitation cross sections or probabilities let us determine E2 M.E.s and B(E2)s.



Single-Step Coulomb Excitation of $^{46,48,49,50}\text{Ti}$

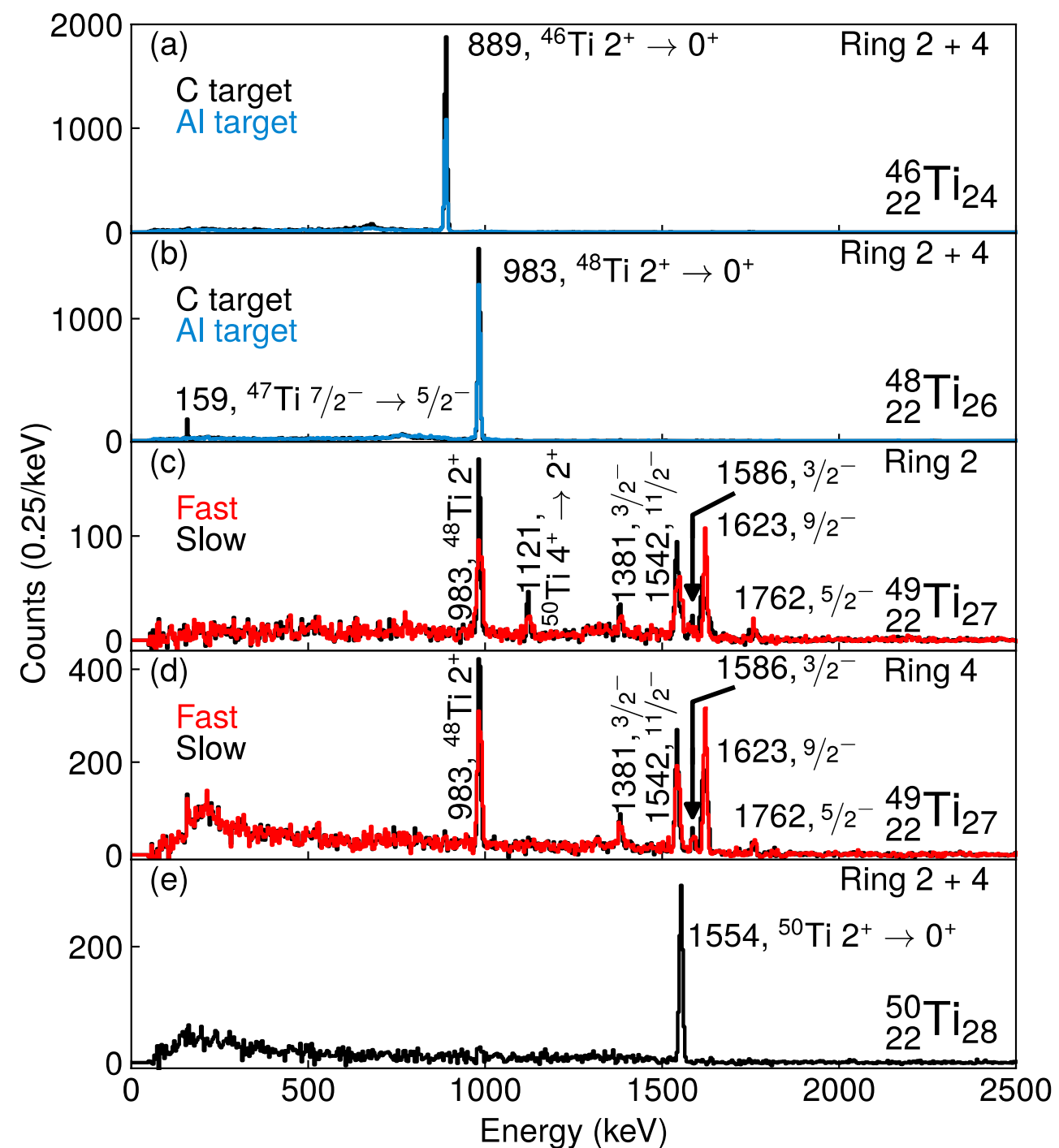
Measurements for B(E2):

- Particle-Gamma / Particle
- Absolute Gamma efficiency
- Beam composition
- Stopping powers

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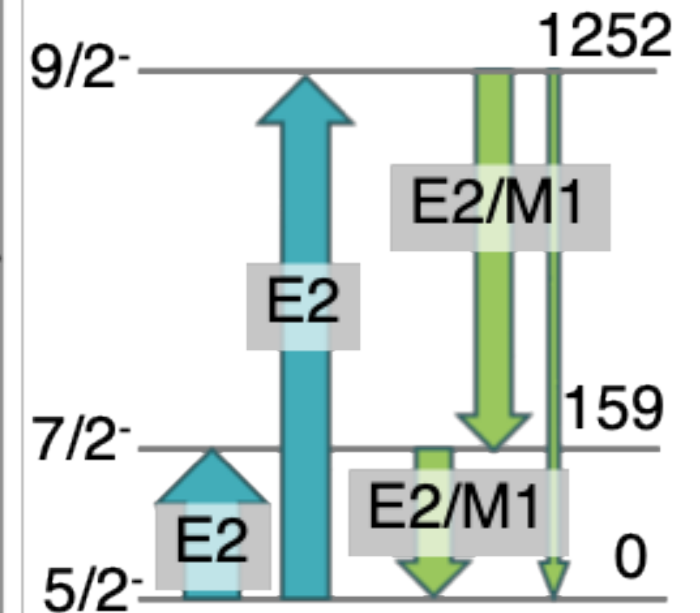
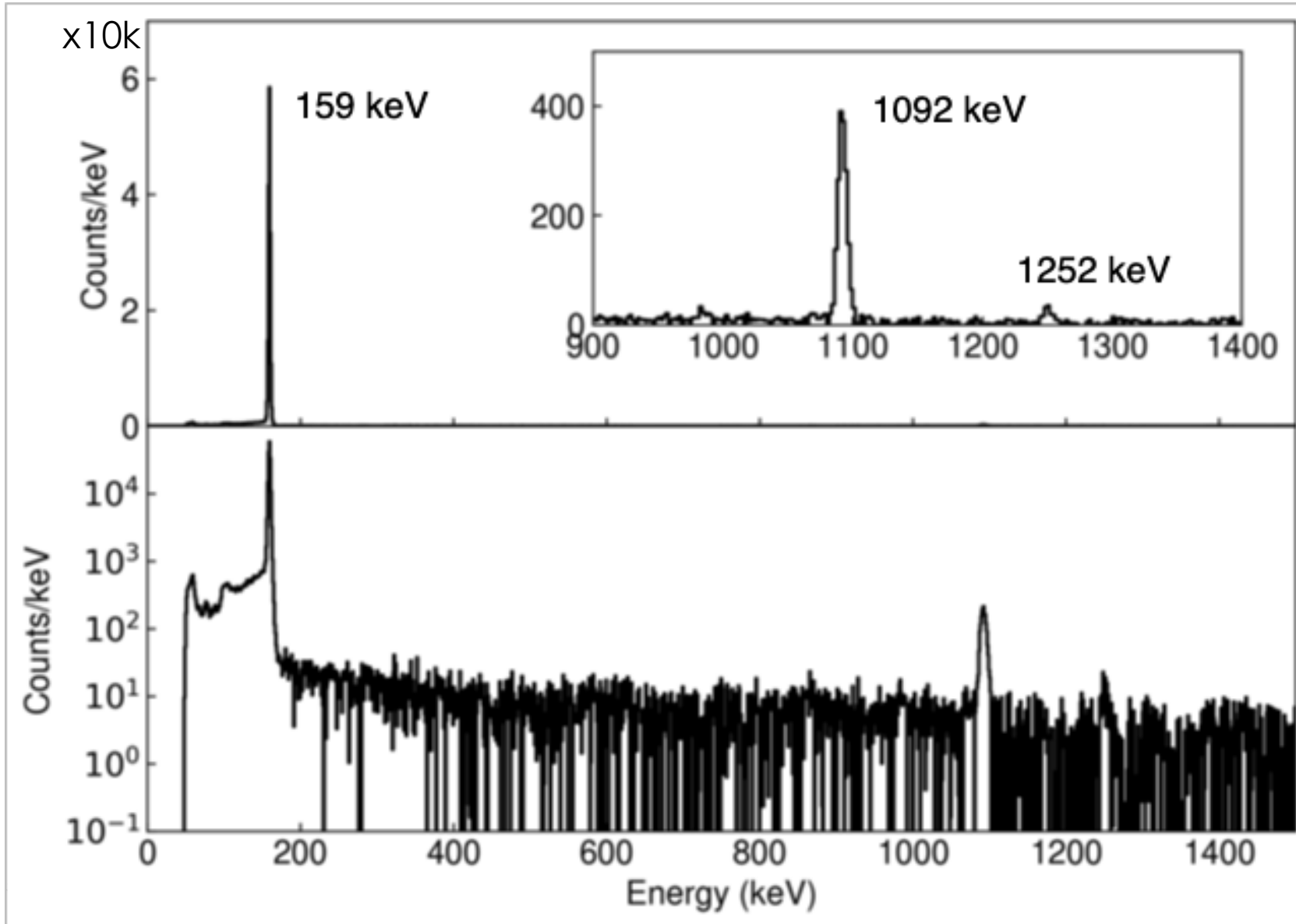


T.J. Gray *et al.*, PLB **855**, 138856 (2024)
w/ some calculations by Angela and Takayuki!

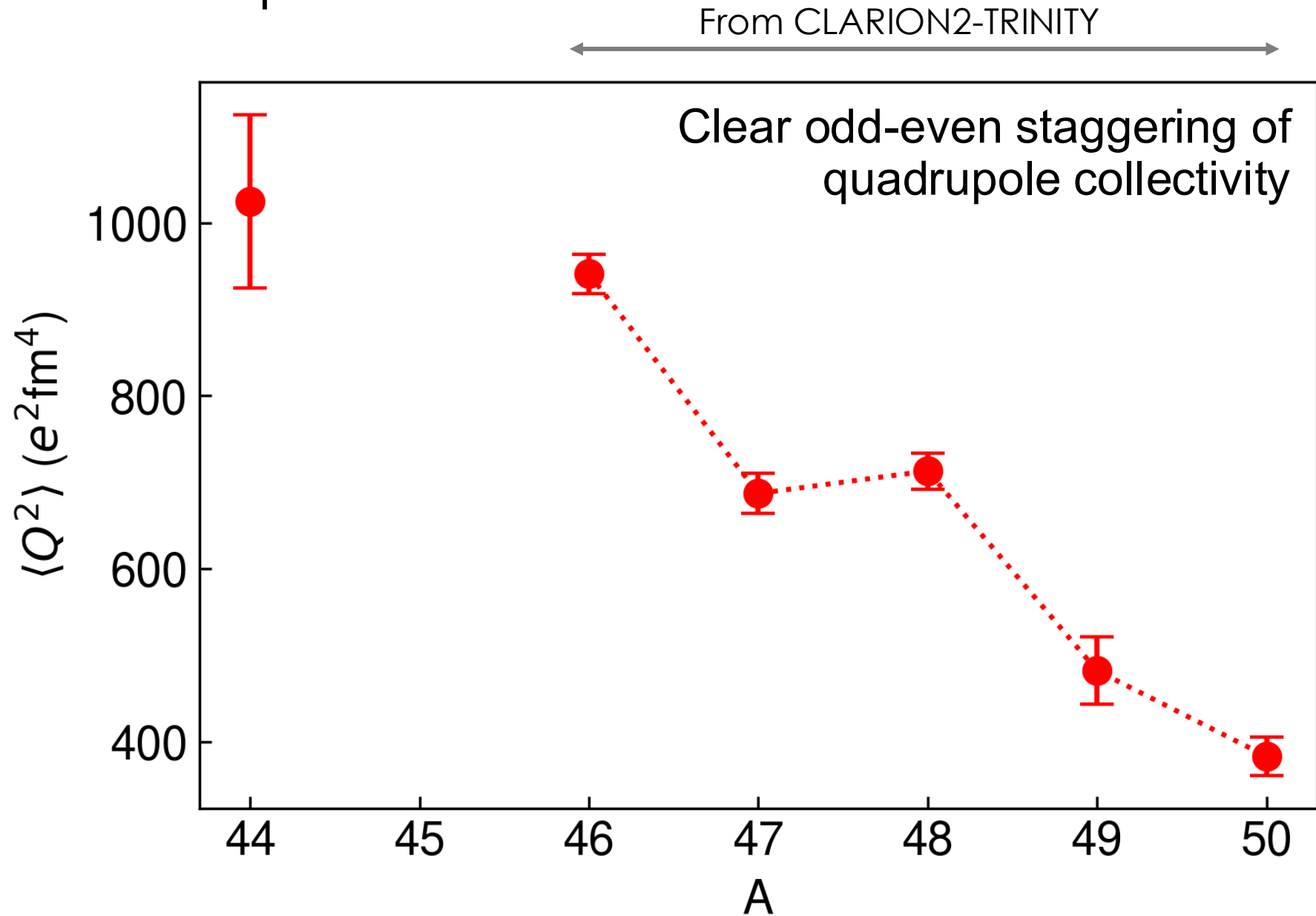


Finish the Ti Chain with Addition of ^{47}Ti

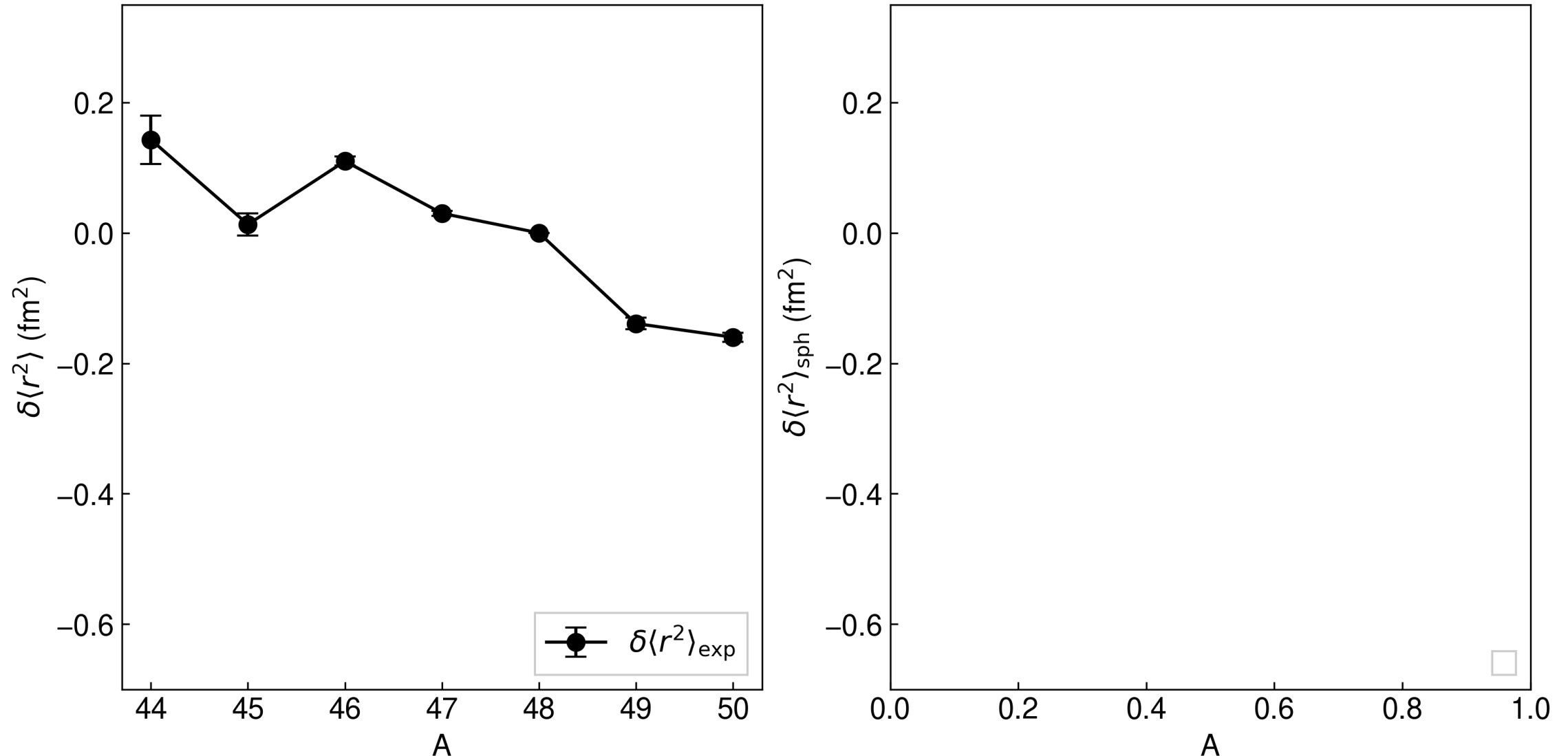
From Summer 2024 with all 5 Rings of TRINITY



$\langle Q^2 \rangle$ of Ti Isotopes

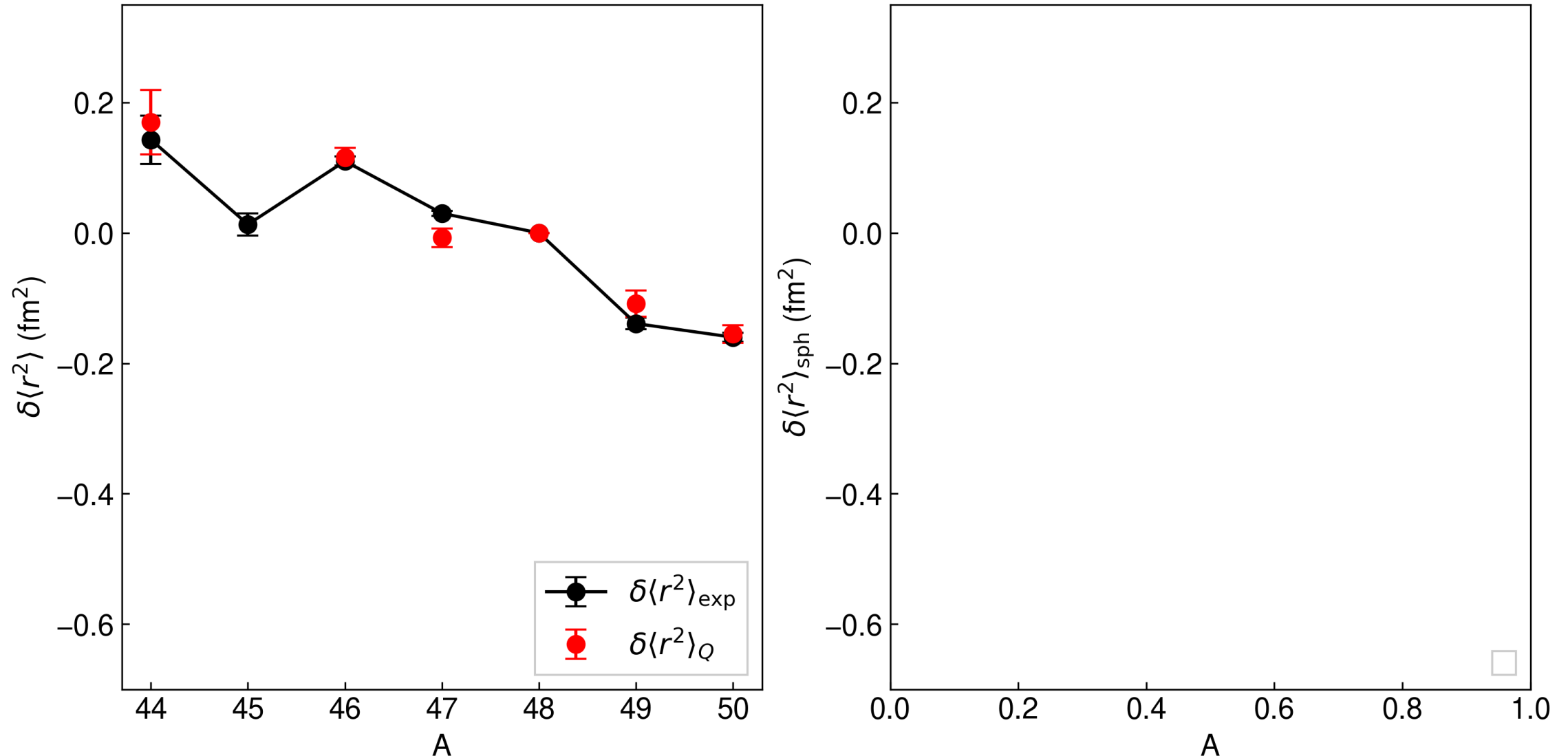


Ti Isotope Shifts $\rightarrow$ Differences in $\langle r^2 \rangle$



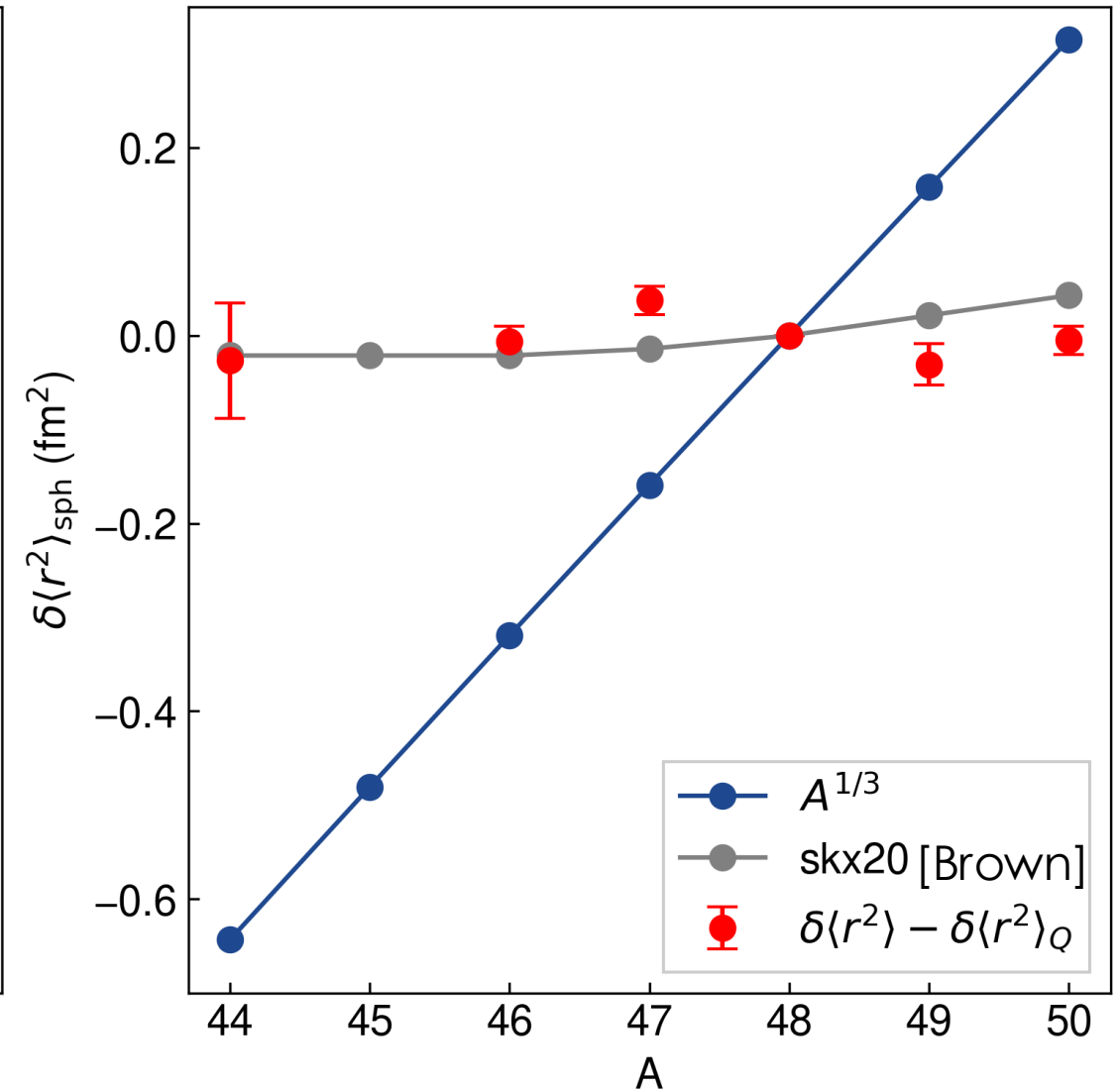
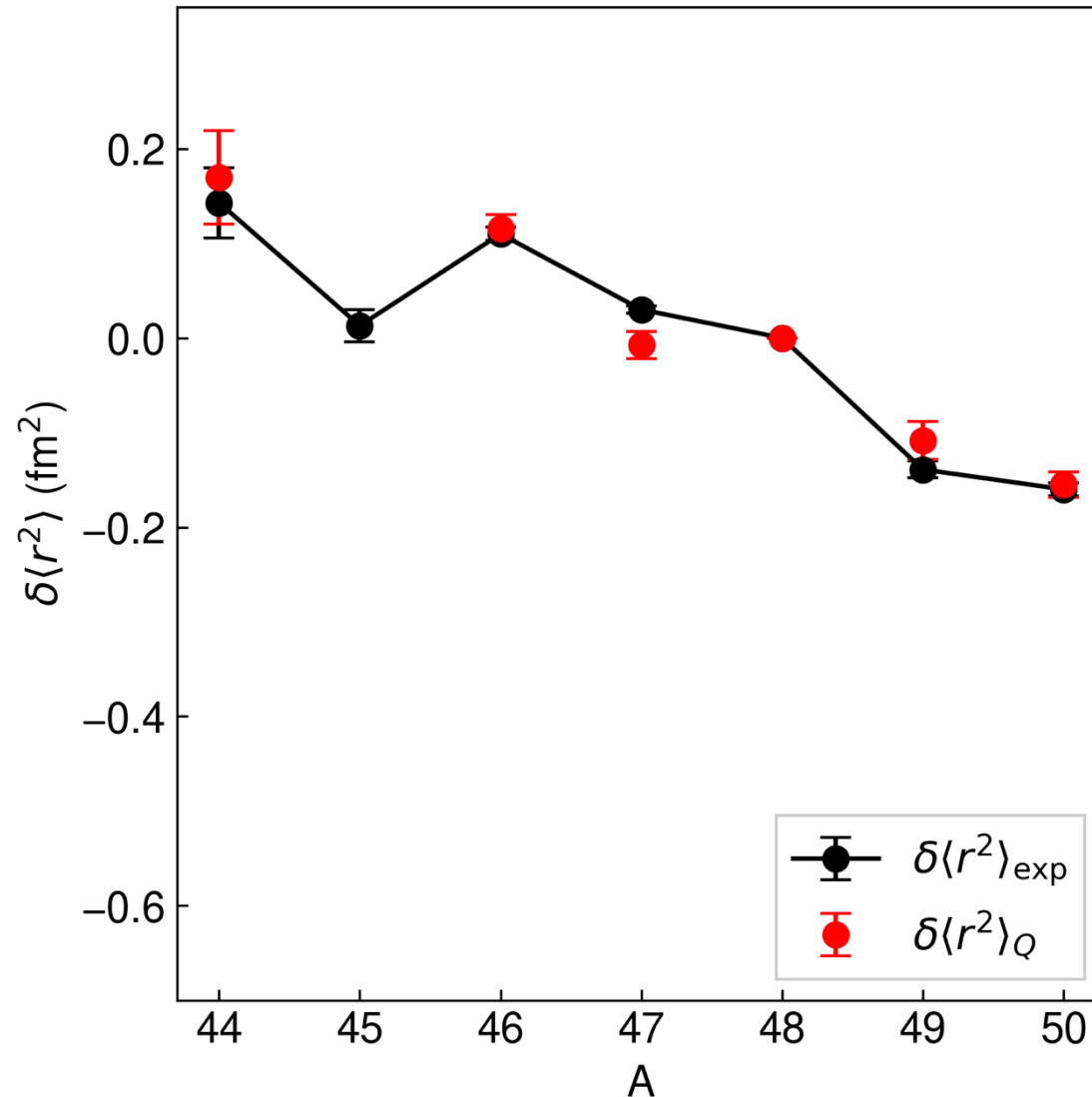
[Atomic Data and Nuclear Data Tables 99 (2013) 69–95] [Phys. Rev. C **102**, 054302]

Ti Isotope Shifts $\rightarrow$ Differences in $\langle r^2 \rangle$



[Atomic Data and Nuclear Data Tables 99 (2013) 69–95] [Phys. Rev. C **102**, 054302]

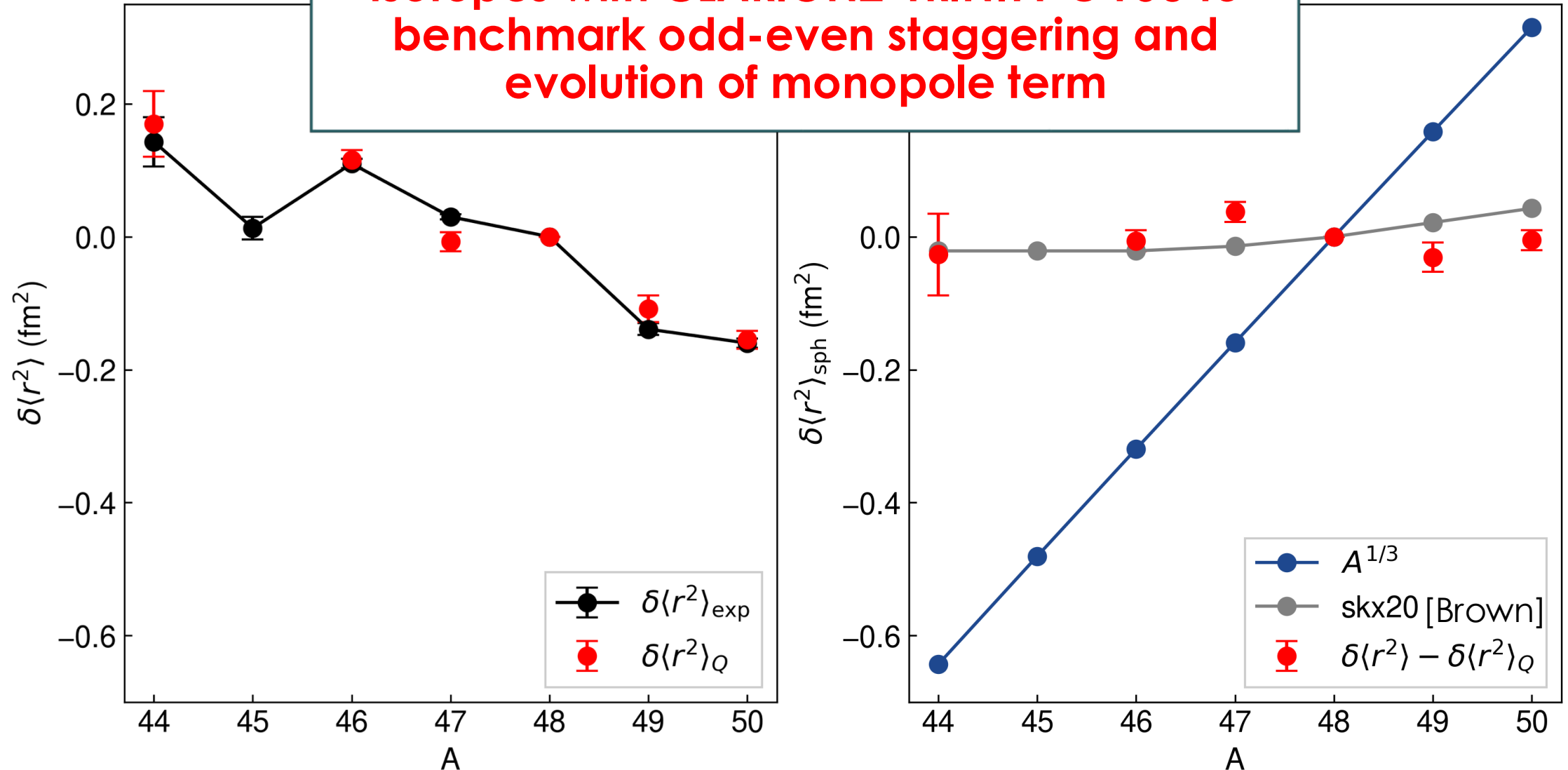
Ti Isotope Shifts $\rightarrow$ Differences in $\langle r^2 \rangle$



[Atomic Data and Nuclear Data Tables 99 (2013) 69–95] [Phys. Rev. C **102**, 054302]

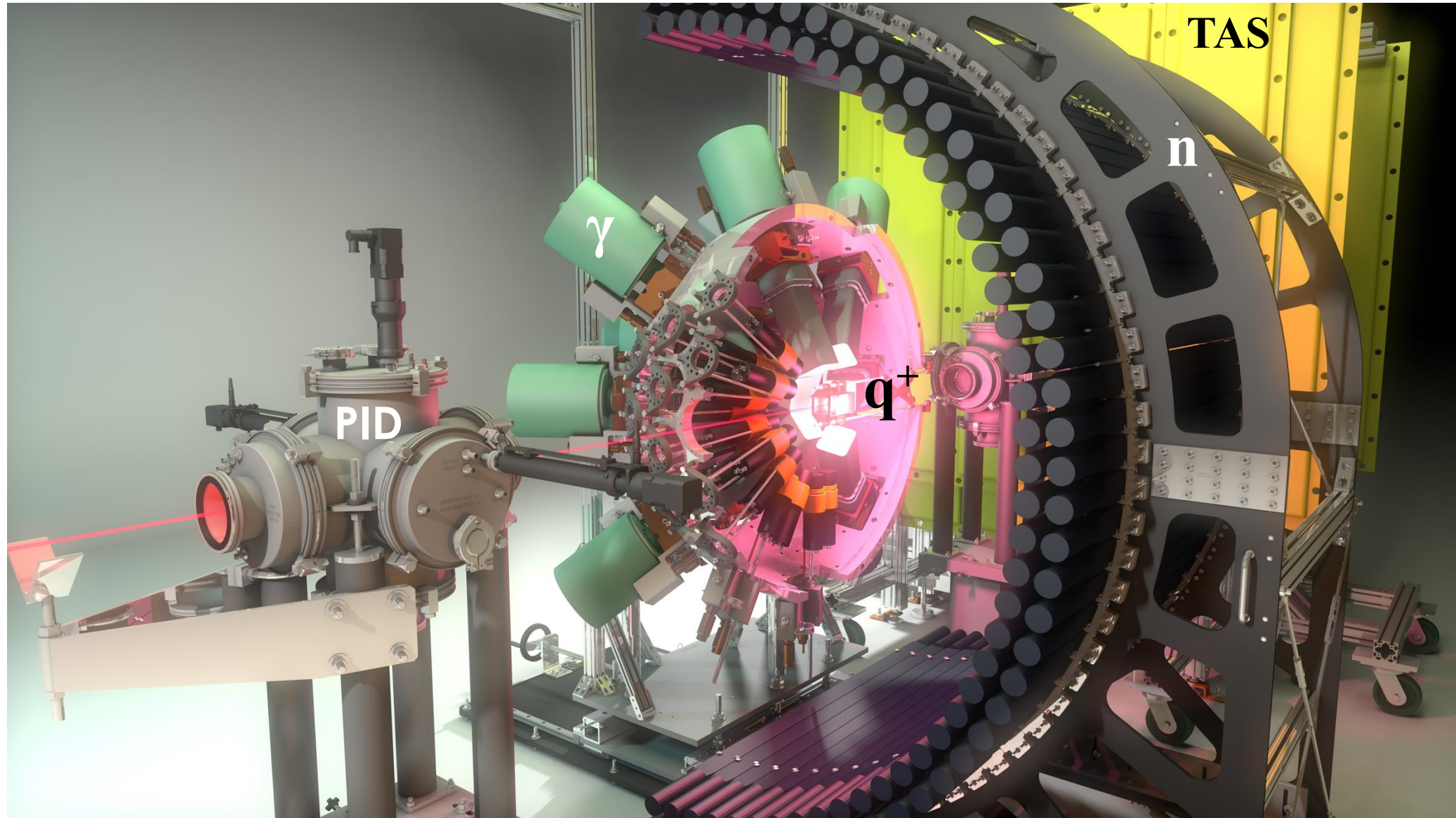
Ti Isotope Shift

Will measure all stable Ca, Cr, Fe, Ni isotopes with CLARION2-TRINITY @ FSU to benchmark odd-even staggering and evolution of monopole term



[Atomic Data and Nuclear Data Tables 99 (2013) 69–95] [Phys. Rev. C **102**, 054302]

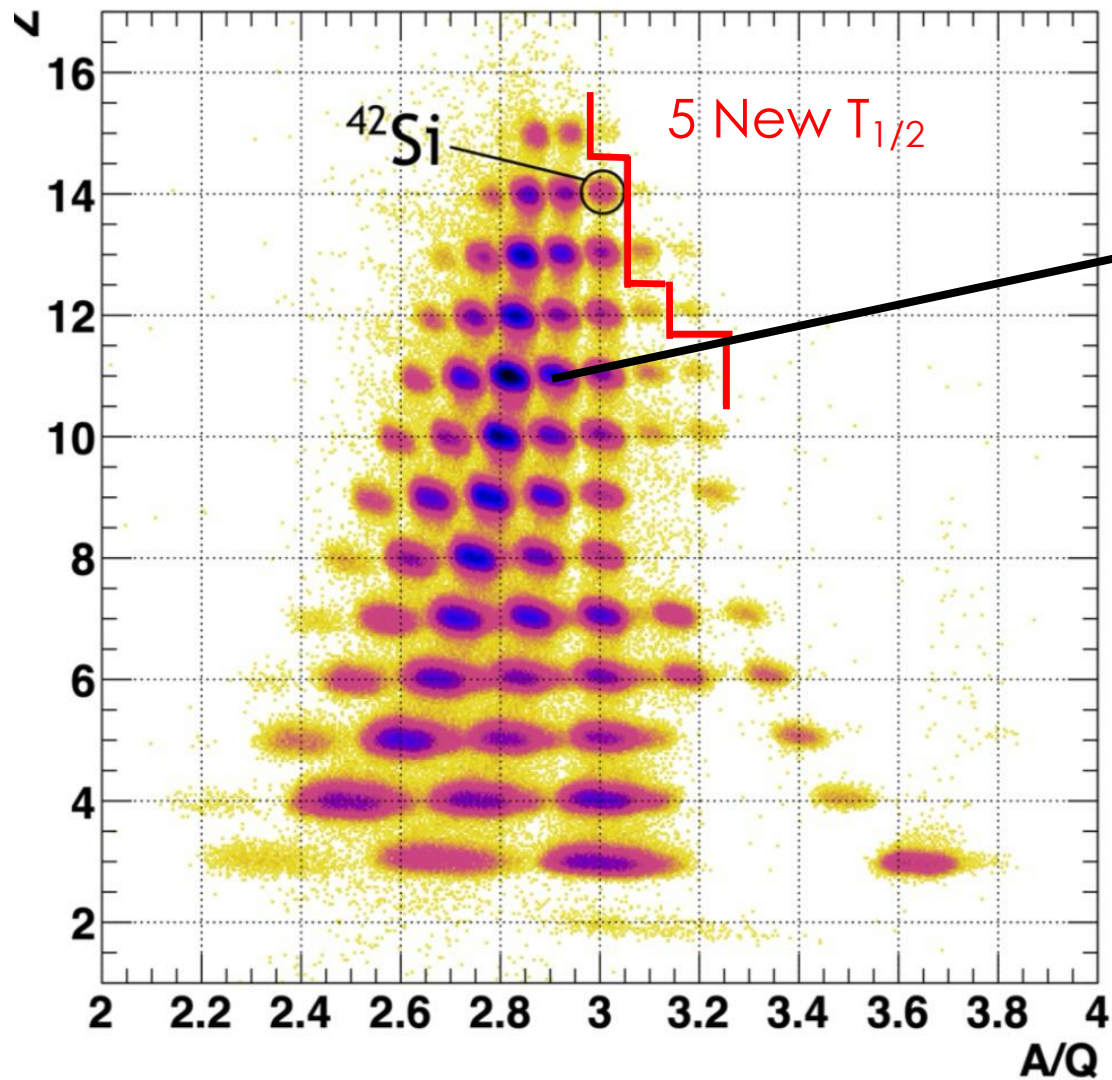
FDSi @ FRIB



Exotic N=20-28 Region

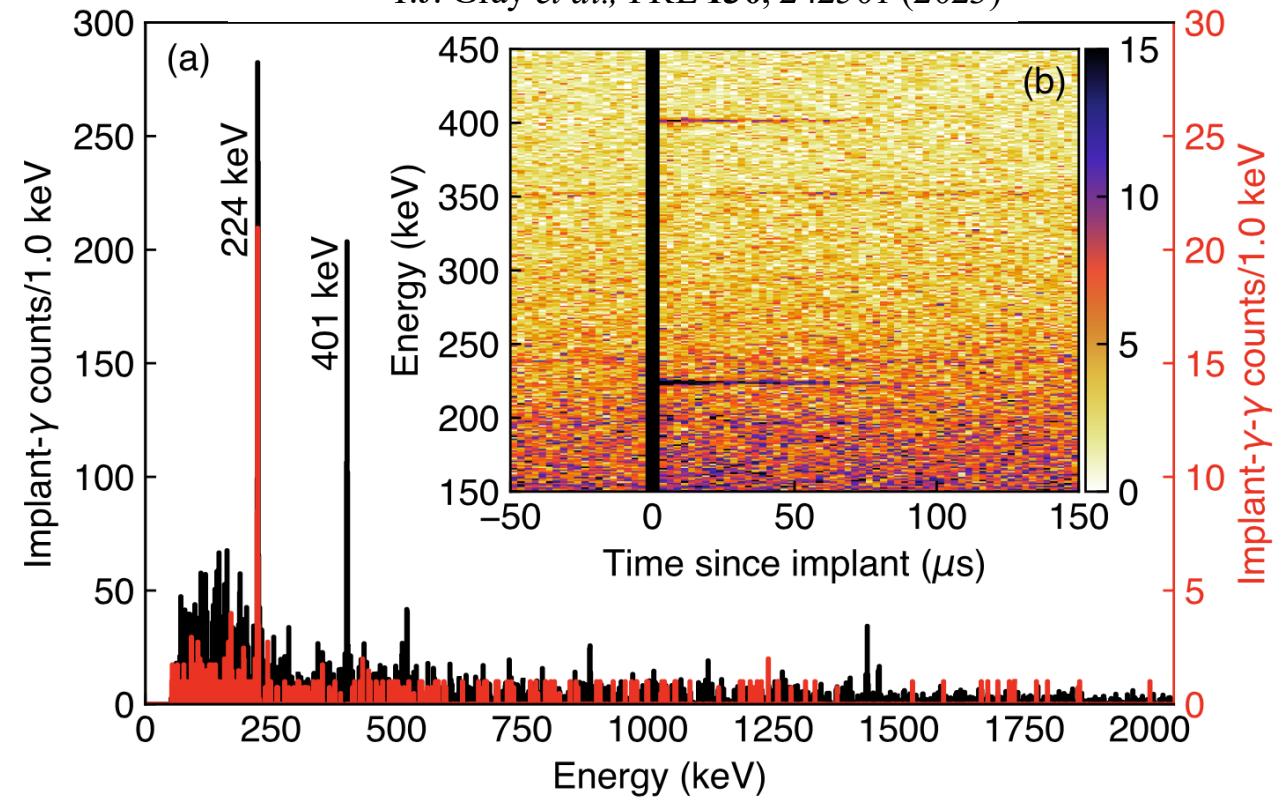
PI = Heather Crawford (LBNL)

H.L Crawford *et al.*, PRL **129**, 212501 (2022)



New Beam Isomer in ^{32}Na

T.J. Gray *et al.*, PRL **130**, 242501 (2023)



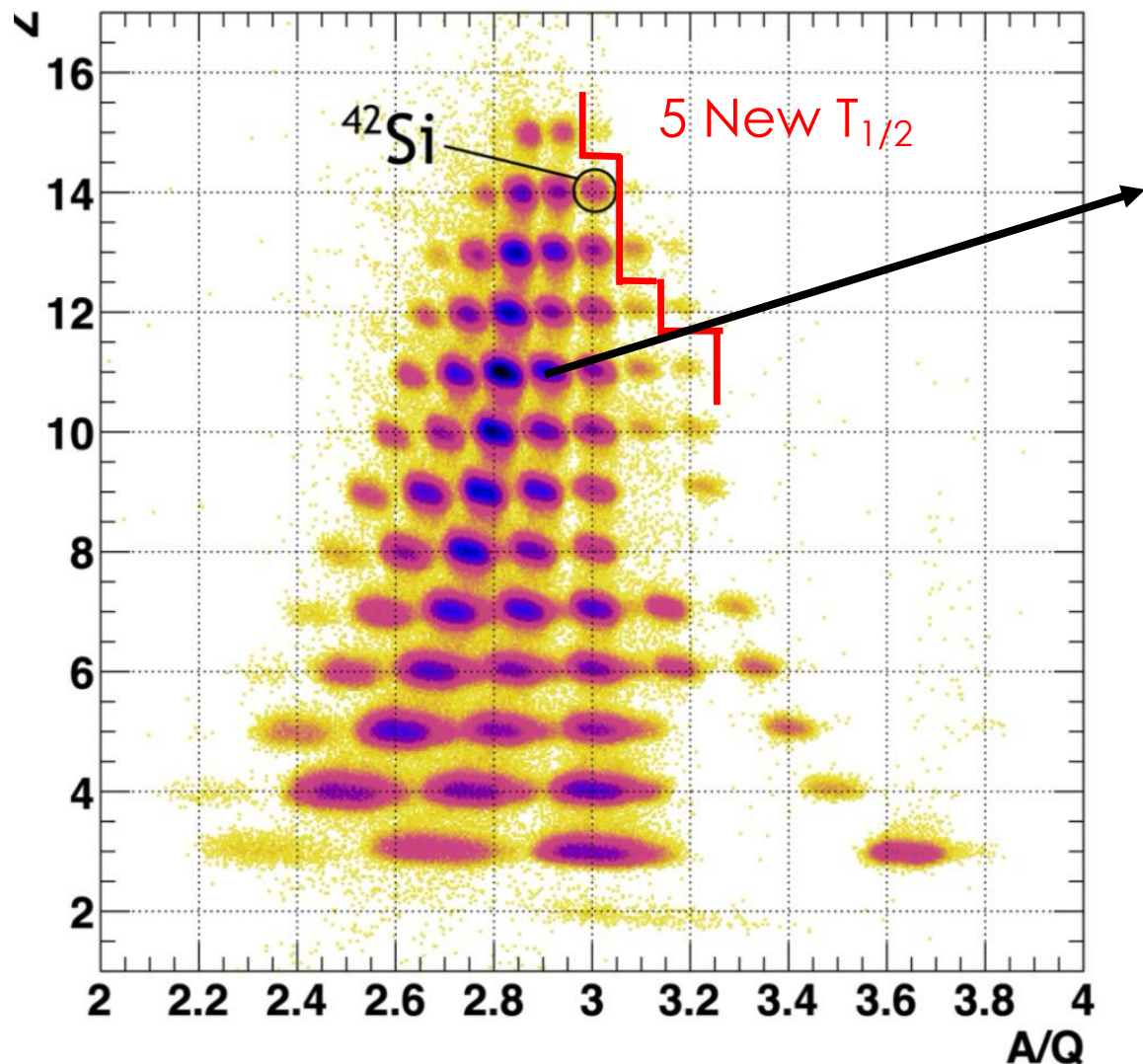
delayed gamma singles

gammas gated on 401 keV

Exotic N=20-28 Region

PI = Heather Crawford (LBNL)

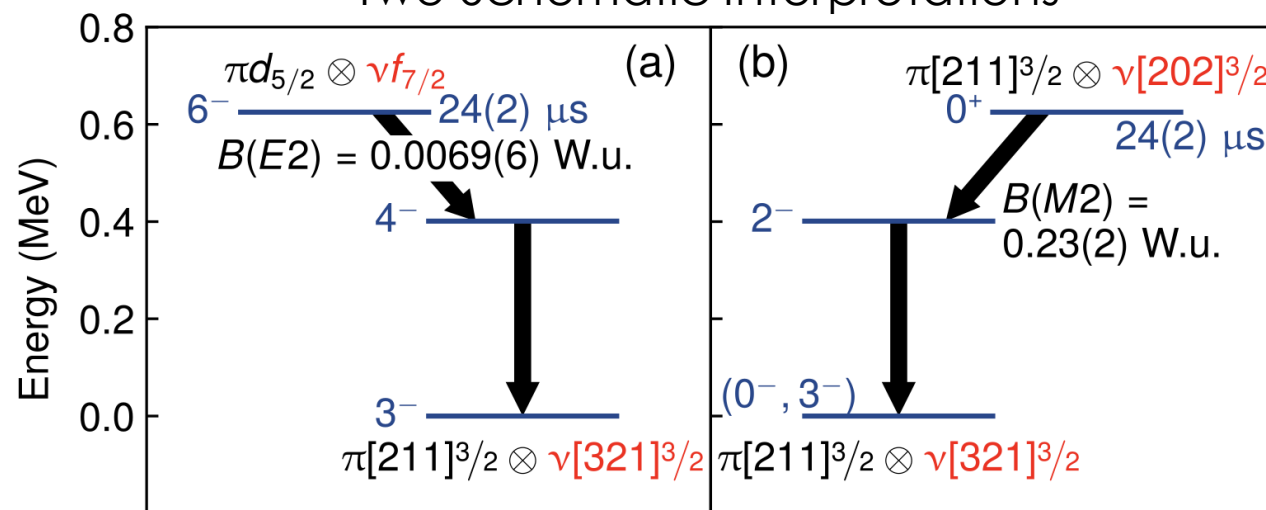
H.L Crawford *et al.*, PRL **129**, 212501 (2022)



New Beam Isomer in ^{32}Na

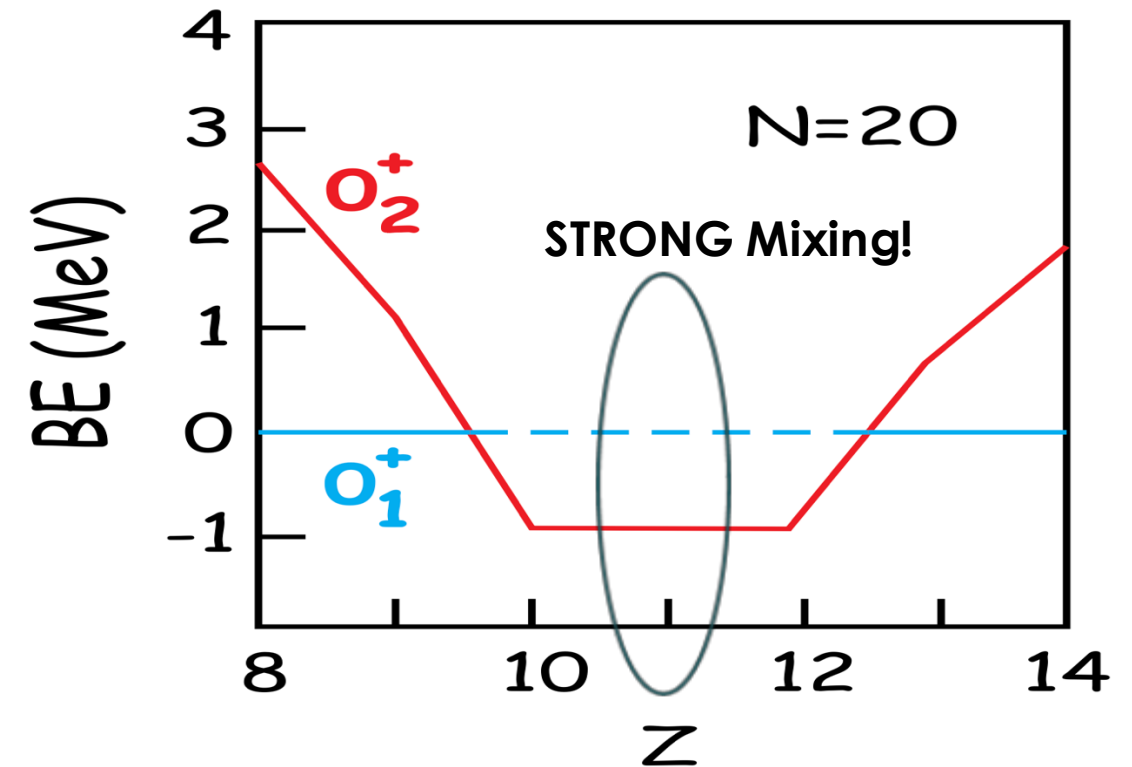
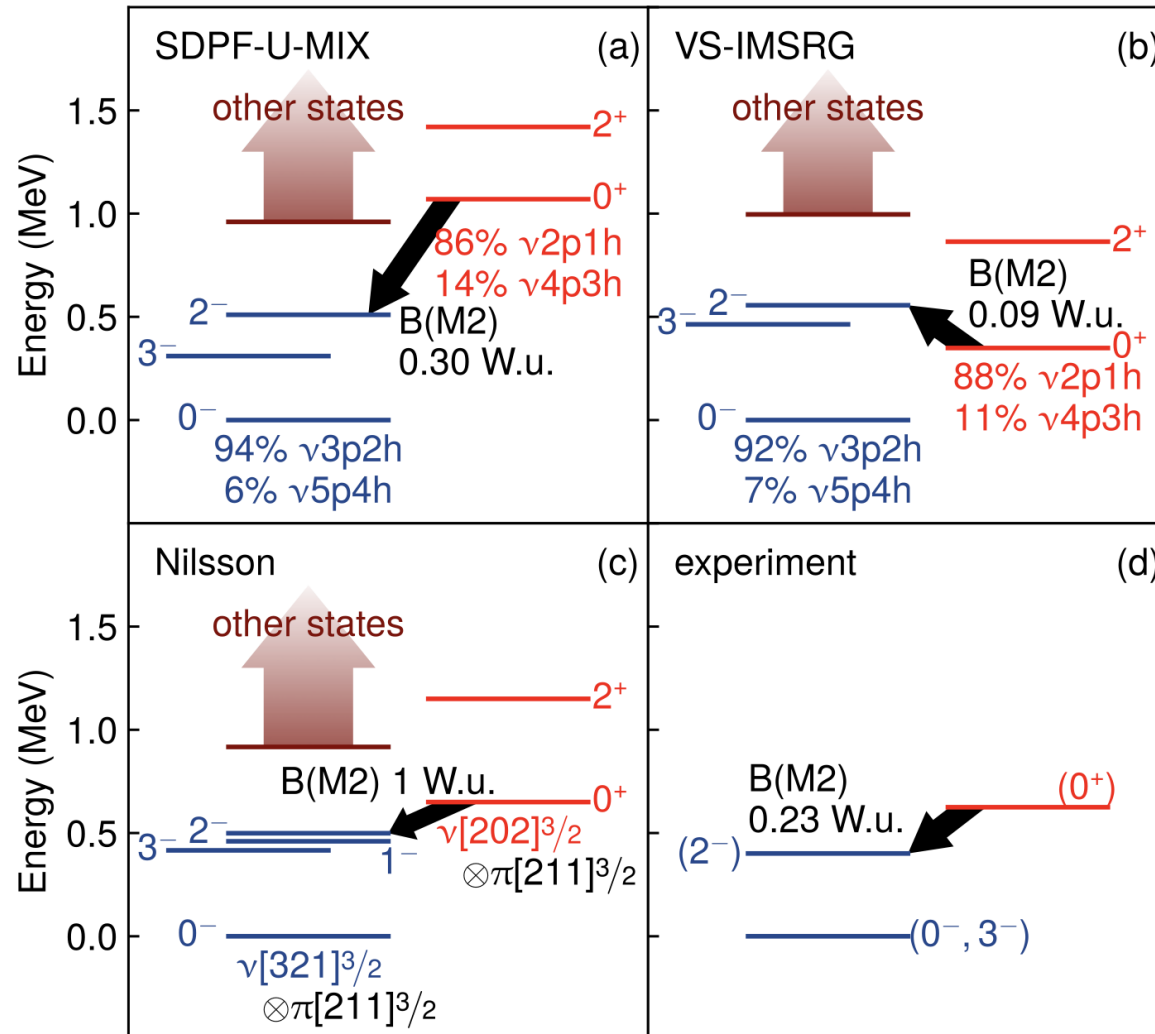
T.J. Gray *et al.*, PRL **130**, 242501 (2023)

Two Schematic Interpretations

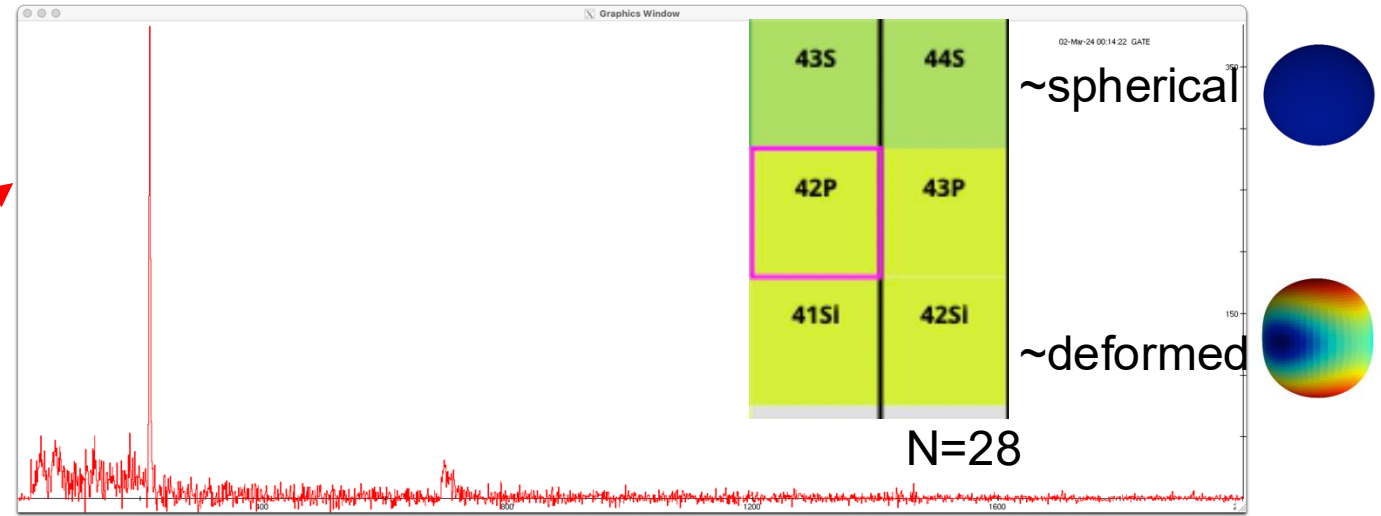
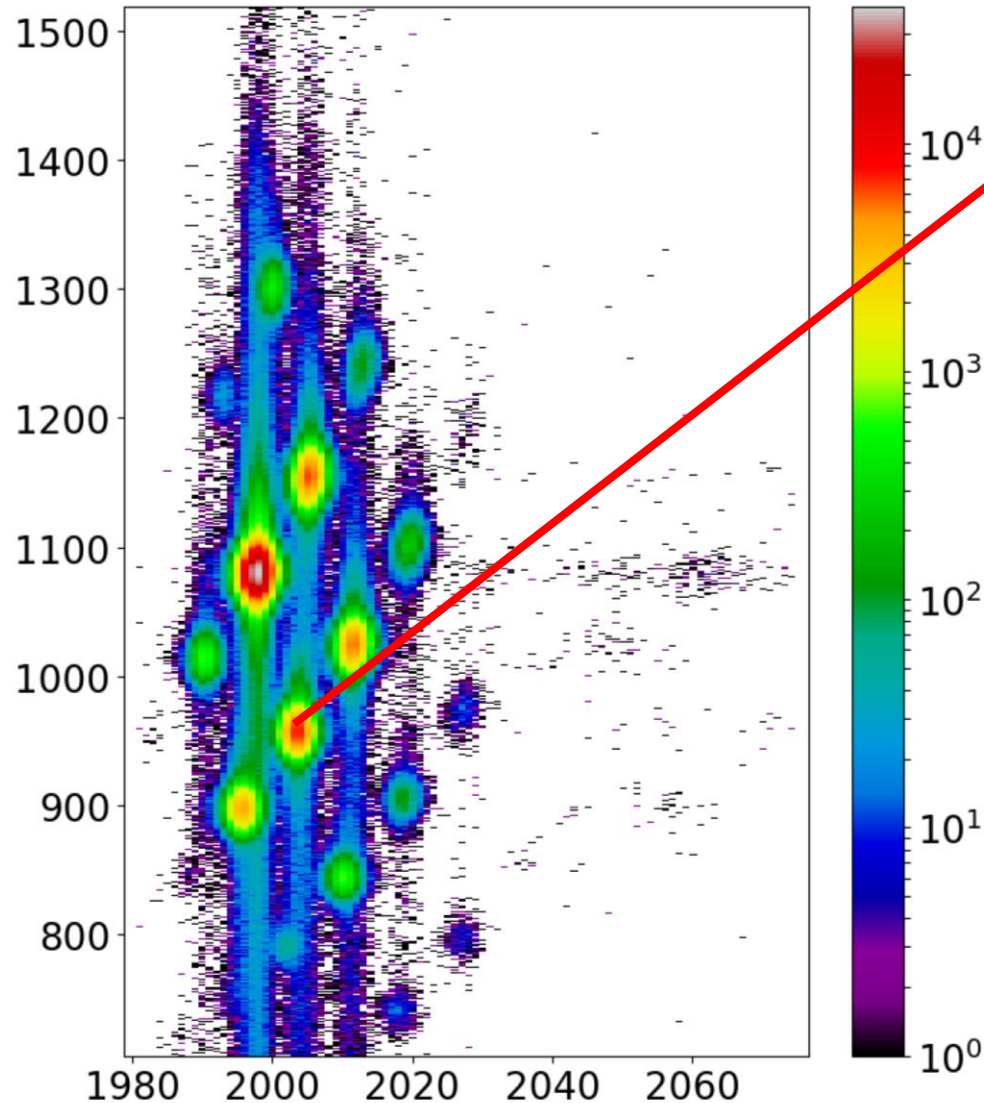


Spherical-Deformed or Deformed-Deformed

Theory on ^{32}Na Consistent with Deformed Spin/K Isomer

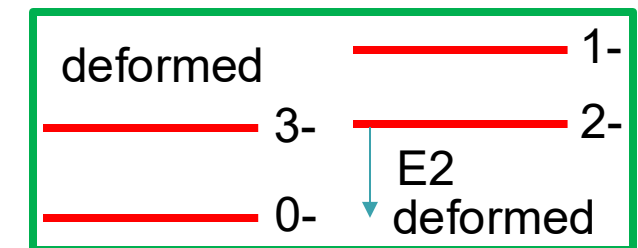
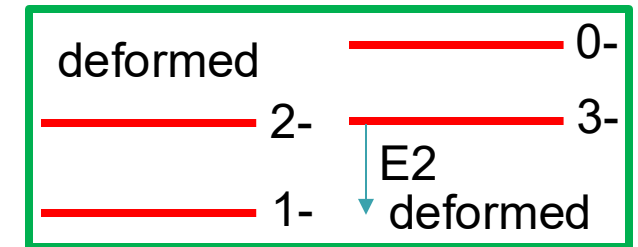
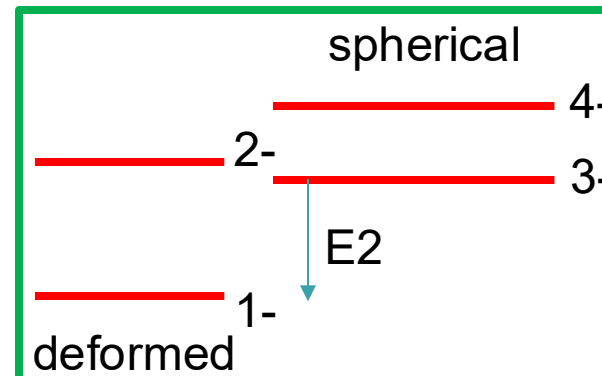


New μ s Isomer at N=28 Shape Crossing – $^{42}\text{P}_{27}$



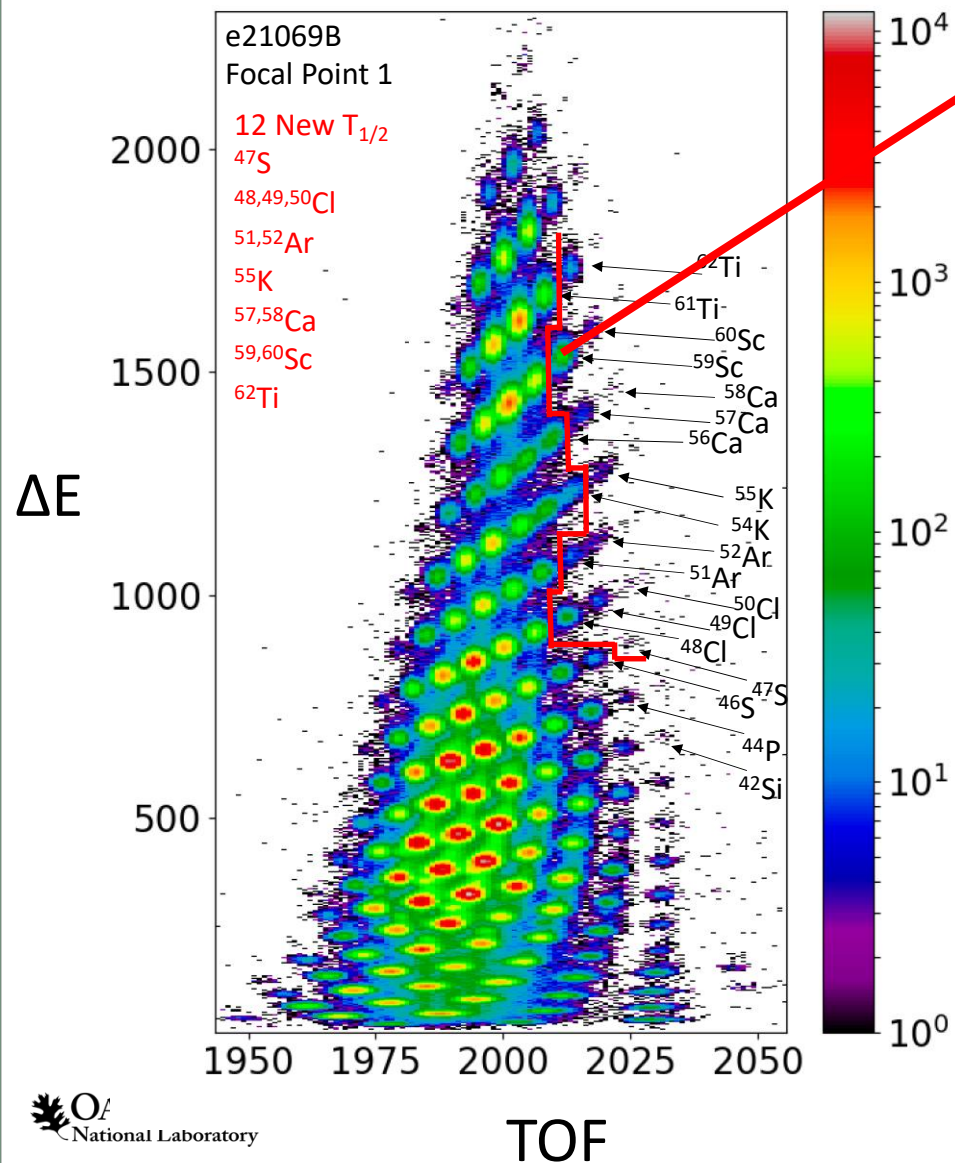
Schematic Scenarios

- Need Calculations!
- Strong Shape mixing like N=20 region?

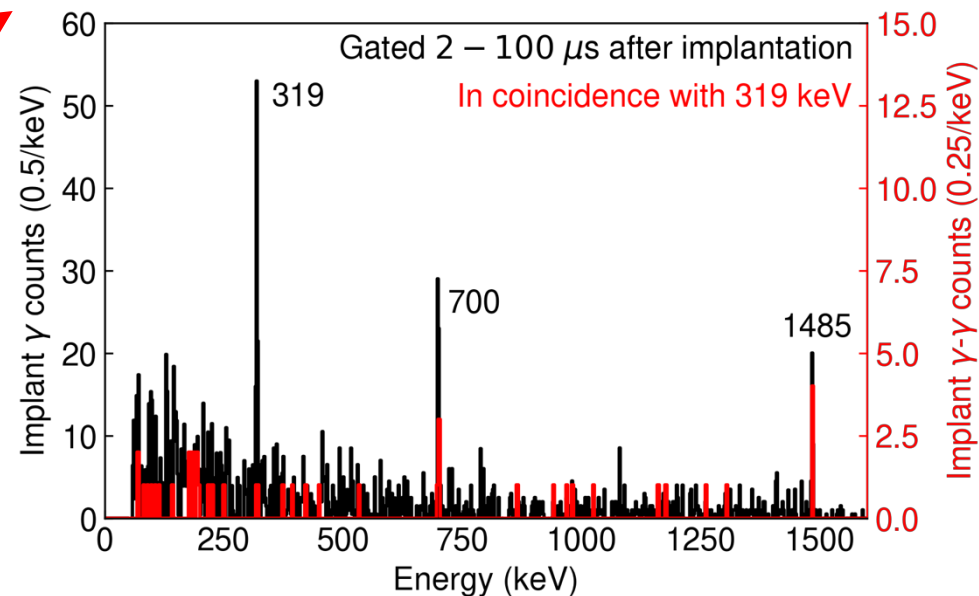


Exotic Ca Region

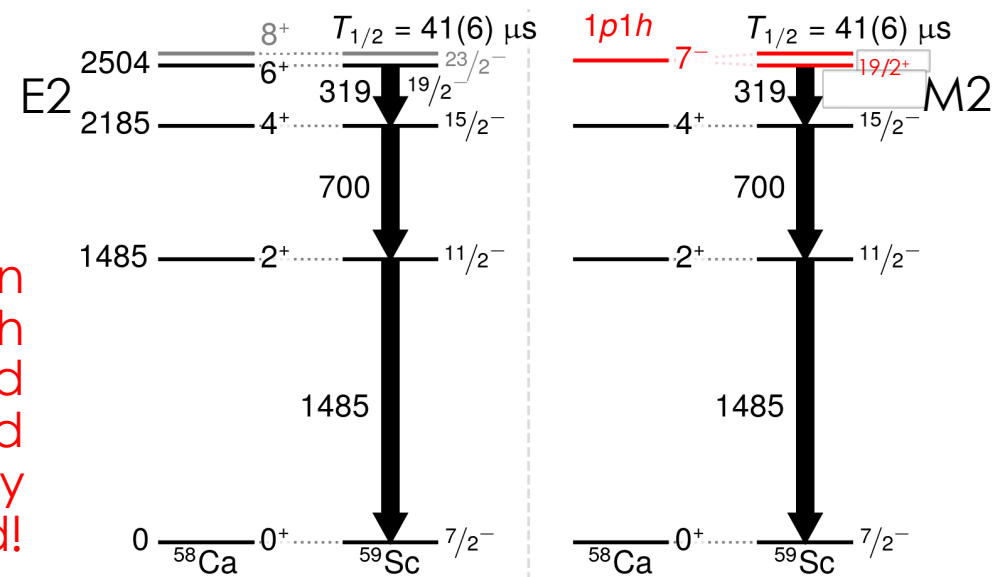
PI = Wei Jia Ong (LLNL)



New Beam Isomer in $^{59}\text{Sc}_{38}$



$\nu g_{9/2}$ seniority isomer OR $\nu g_{9/2}$ 1p-1h isomer

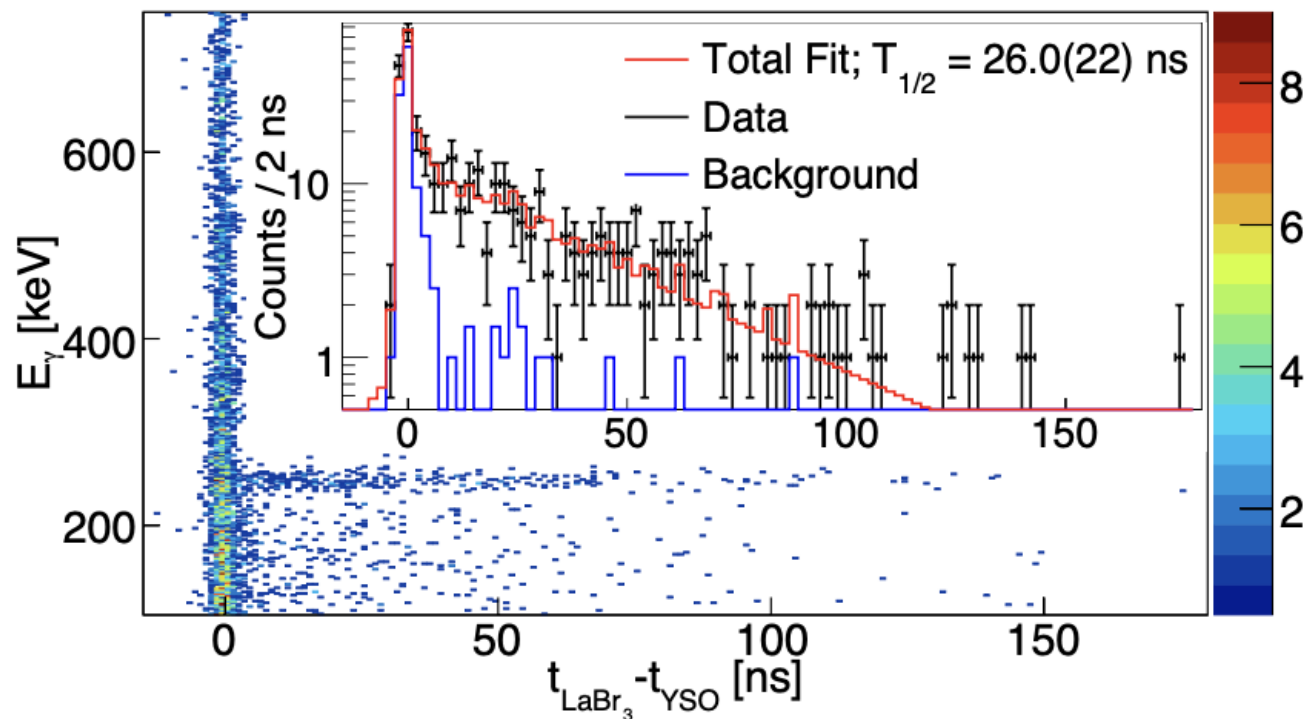


Theory in progress with 1p-1h and weakened $N=40$ currently favored!

T.J. Gray
et al., in prep

B(E2;1⁺→3⁺) in ⁵⁴Sc and Universal sd + fp Effective Charges

$\pi f_{7/2} \otimes \nu f_{5/2} \rightarrow \pi f_{7/2} \otimes \nu p_{1/2} = \nu f_{5/2} \rightarrow \nu p_{1/2}$ in weak coupling limit

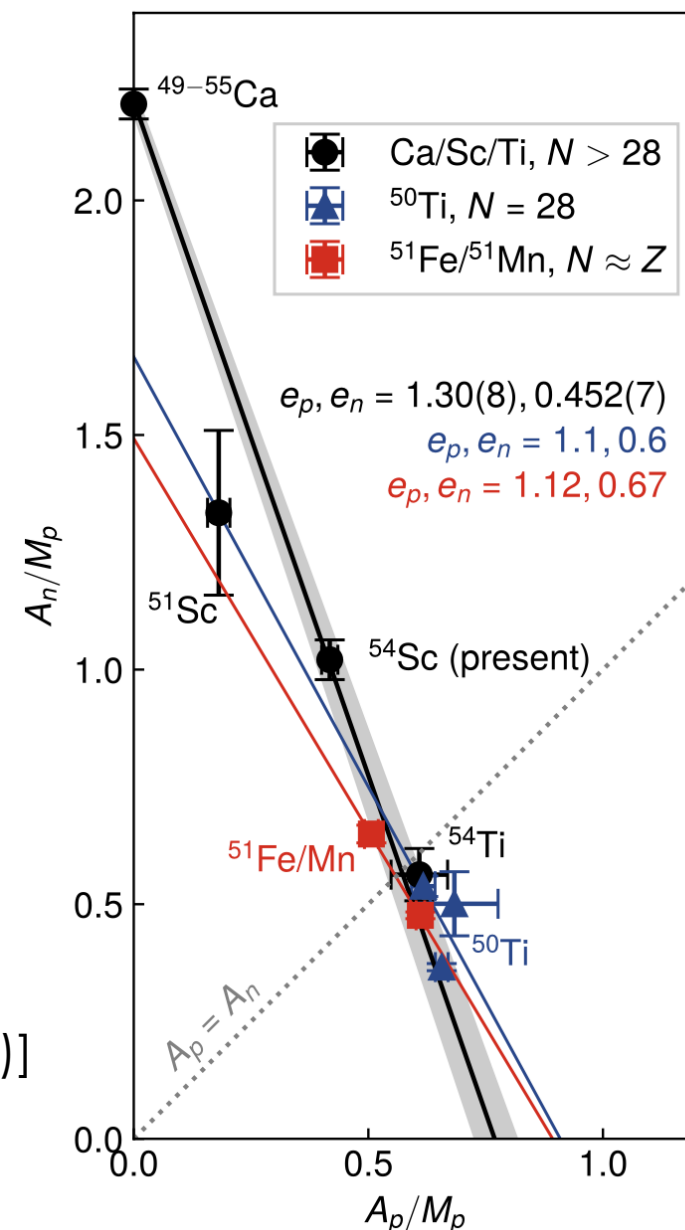


“No evidence for changes in the effective charges due to an isospin or orbital dependence is found.”



fp shell charges = 1.30(8), 0.452(7)
sd shell charges = 1.36(5), 0.45(5)
Microscopic Thy = 1.31, 0.46

[present]
[PRC **78**, 064302 (2008)]
[PRC **54**, 1641 (1996)]

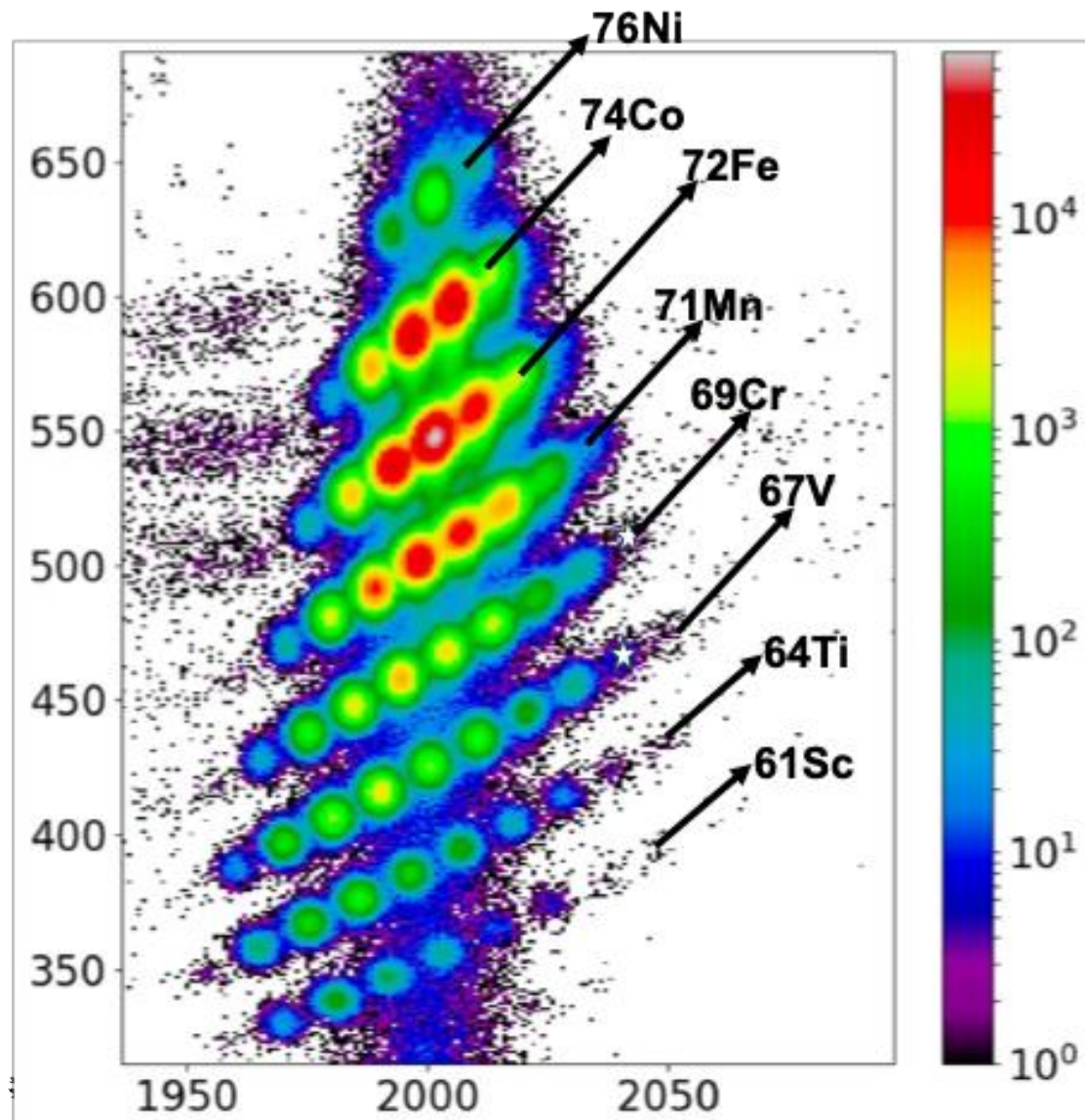


T.H. Ogunbeku *et al.*,

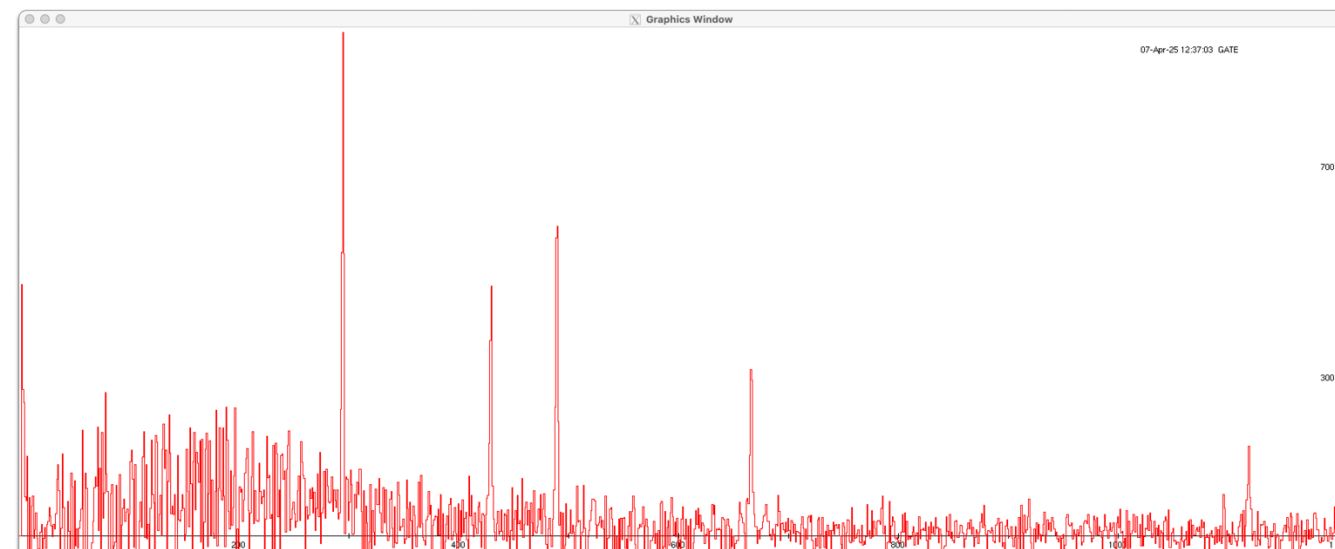
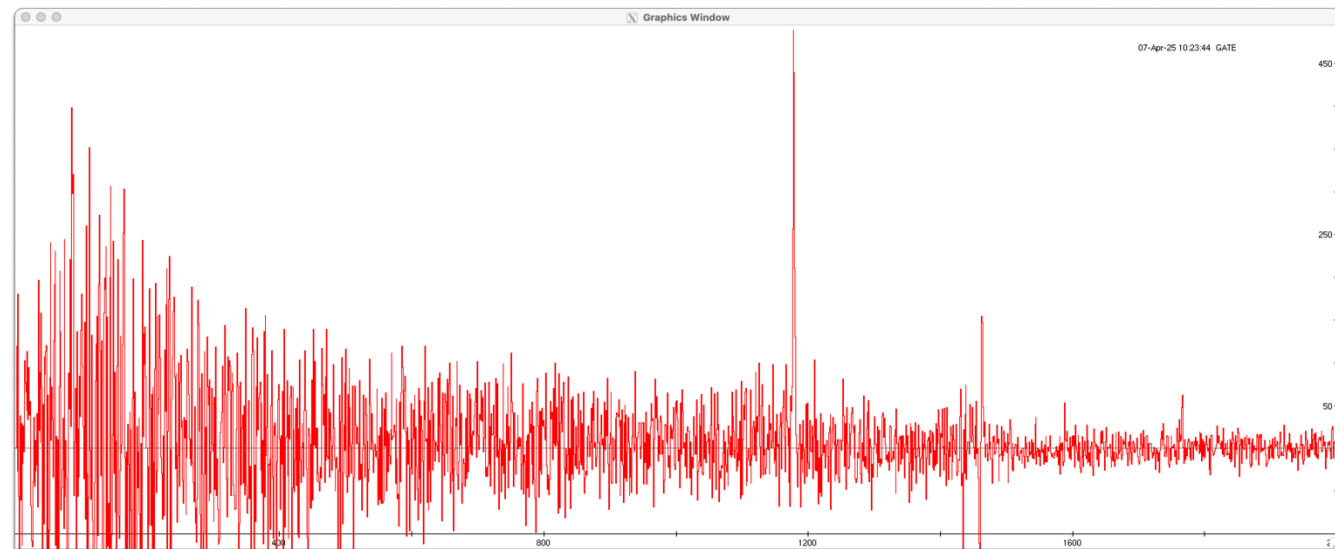
Submitted to PRL (2025), w/ some calculations by Angela, Takayuki, and Alex

Exotic N=40 Region

PI = Ben Crider – Miss. State



New Beam Isomers from March 2025 Experiment!



D. Scriven
et al., in prep

Thank you

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with the U.S. Department of Energy

