Maria Lucia Sambataro





Relativistic transport approach for charm and bottom toward a phenomenological determination of Ds

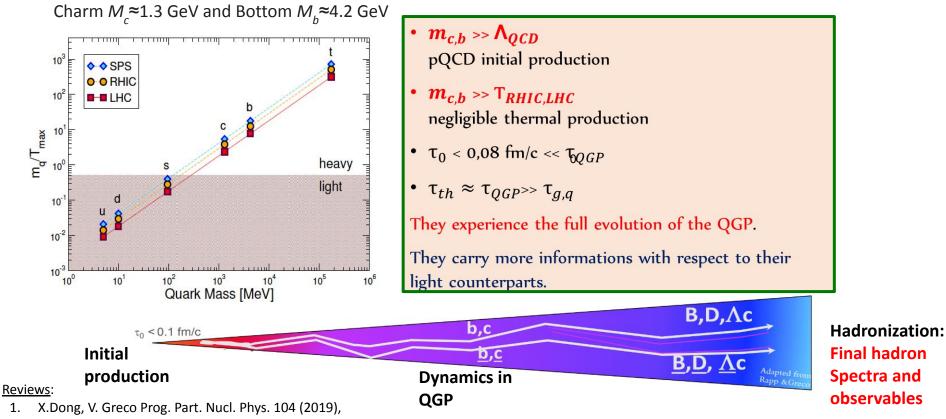
In collaboration with: V. Minissale, Y. Sun, S. Plumari, G. Parisi, V. Greco

Dipartimento di Fisica e Astronomia 'E.Majorana'- Università degli Studi di Catania

INFN -Laboratori Nazionali del Sud (LNS)

Meeting SIM - Catania INFN (LNS) - 10-11 Settembre 2024

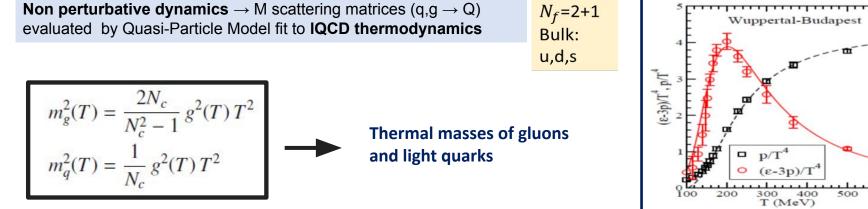
Basic scales of charm and bottom quarks



2. A.Andronic EPJ C76 (2016), 3) R.Rapp, F.Prino J.Phys. G43 (2016)

CATANIA MODEL: QUASI-PARTICLE MODEL AND TRANSPORT THEORY

Quasi Particle Model (QPM) fitting IQCD



g(T) from a fit to ϵ from lQCD data \rightarrow good reproduction of P, $\epsilon\text{-}3P$

$$g^{2}(T) = \frac{48\pi^{2}}{(11N_{c} - 2N_{f})\ln\left[\lambda\left(\frac{T}{T_{c}} - \frac{T_{s}}{T_{c}}\right)\right]^{2}}$$

 λ =2.6 T_s =0.57 T_c

QPM Thermal Masses [GeV]

2

T/T_C [GeV]

Larger than pQCD especially as T \rightarrow T $_c$

S. Plumari et al, *Phys.Rev.D* 84 (2011) 094004 H. Berrehrah,, PHYSICAL REVIEW C **93**, 044914 (2016) 600

Relativistic Boltzmann equation at finite η/s

Bulk evolution

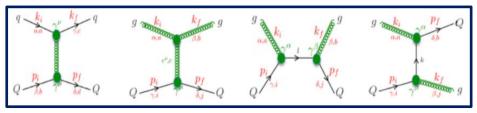
$$p^{\mu}\partial_{\mu}f_{q}(x,p)+m(x)\partial_{\mu}^{x}m(x)\partial_{p}^{\mu}f_{q}(x,p)=C[f_{q},f_{g}]$$

$$p^{\mu}\partial_{\mu}f_{g}(x,p)+m(x)\partial_{\mu}^{x}m(x)\partial_{p}^{\mu}f_{g}(x,p)=C[f_{q},f_{g}]$$
Free-streaming
field interaction
 $\varepsilon - 3p \neq 0$
Free-streaming
Collision term
gauged to some $\eta/s \neq 0$
Free-streaming
Collision term
gauged to some $\eta/s \neq 0$
Free-streaming
Free-streaming
Collision term
gauged to some $\eta/s \neq 0$
Free-streaming
Free

$$p^{\mu}\partial_{\mu}f_Q(x,p)=C[f_q,f_g,f_Q]$$

$$C[f_{q}, f_{g}, f_{Q}] = \frac{1}{2E_{1}} \int \frac{d^{3}p_{2}}{2E_{2}(2\pi)^{3}} \int \frac{d^{3}p_{1}'}{2E_{1}'(2\pi)^{3}} \times [f_{Q}(p_{1}')f_{q,g}(p_{2}') - f_{Q}(p_{1})f_{q,g}(p_{2})] \times |M_{(q,g) \rightarrow Q}(p_{1}p_{2} \rightarrow p_{1}'p_{2}')| \times (2\pi)^{4} \delta^{4}(p_{1}+p_{2}-p_{1}'-p_{2}')$$

Feynman diagrams at first order pQCD for HQs-bulk interaction:



Scattering matrices $M_{q,q}$ by QPM fit to IQCD thermodynamics

HADRONIZATION: hybrid Coalescence + fragmentation

Relativistic Boltzmann equation at finite η/s

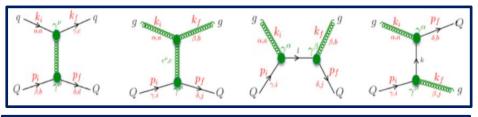
Bulk evolution $p^{\mu}\partial_{\mu}f_{q}(x,p)+m(x)\partial_{\mu}^{x}m(x)\partial_{p}^{\mu}f_{q}(x,p)=C[f_{q},f_{g}]$ $p^{\mu}\partial_{\mu}f_{g}(x,p)+m(x)\partial_{\mu}^{x}m(x)\partial_{p}^{\mu}f_{g}(x,p)=C[f_{q},f_{g}]$ Free-streaming field interaction $\varepsilon - 3p \neq 0$ Collision term gauged to some n/s $\neq 0$

HQ evolution

$$p^{\mu}\partial_{\mu}f_Q(x,p)=C[f_q,f_g,f_Q]$$

$$C[f_{q}, f_{g}, f_{Q}] = \frac{1}{2E_{1}} \int \frac{d^{3}p_{2}}{2E_{2}(2\pi)^{3}} \int \frac{d^{3}p_{1}}{2E_{1}'(2\pi)^{3}} \times [f_{Q}(p_{1}')f_{q,g}(p_{2}') - f_{Q}(p_{1})f_{q,g}(p_{2})] \times |M_{(q,g) \rightarrow Q}(p_{1}p_{2} \rightarrow p_{1}'p_{2}')| \times (2\pi)^{4} \delta^{4}(p_{1}+p_{2}-p_{1}'-p_{2}')$$

Feynman diagrams at first order pQCD for HQs-bulk interaction:



Scattering matrices $M_{g,q}$ by QPM fit to IQCD thermodynamics

HADRONIZATION: hybrid Coalescence + fragmentation

Information from non-equilibrium: anisotropic flows $v_n(p_T)$

Elliptic flow

Triangular flow

$$E\frac{\mathrm{d}^{3}N}{\mathrm{d}p_{\mathrm{T}}} = \frac{1}{2\pi} \frac{\mathrm{d}^{2}N}{p_{\mathrm{T}}\mathrm{d}p_{\mathrm{T}}\mathrm{d}y} \left\{ 1 + \sum_{i=1}^{\infty} v_{\mathrm{n}} \cos[\mathrm{n}(\varphi - \Psi_{\mathrm{n}})] \right\}$$

Elliptic flow v₂

 asymmetry between the in-plane and out-of-plane directions

Triangular flow v₃

 event-by-event fluctuations in the initial distributions of nucleons

$$\epsilon_{n} = \frac{\langle r_{\perp}^{n} \cos[n(\varphi - \Phi_{n})] \rangle}{\langle r_{\perp}^{n} \rangle} \qquad \Phi_{n} = \frac{1}{n} \arctan \frac{\langle r_{\perp}^{n} \sin(n\varphi) \rangle}{\langle r_{\perp}^{n} \cos(n\varphi) \rangle}$$
$$r_{n} = \sqrt{x^{2} + y^{2}} \qquad \varphi = \arctan(y/y)$$

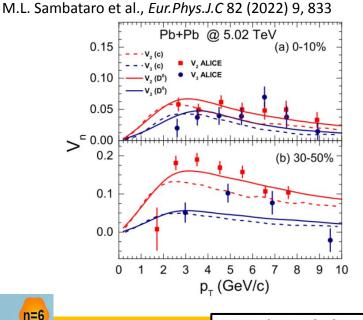
 y^2 , $\varphi = \arctan(y/x)$

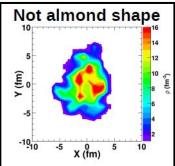
Azimuthal anisotropies depend on

- □ the interaction and coupling of heavy quarks with the medium;
- □ the initial conditions of the system, i.e.geometry of the collision;
- the fluctuations in the distributions of nucleons and gluons within the nuclei

Monte Carlo Glauber for initial condition of partons

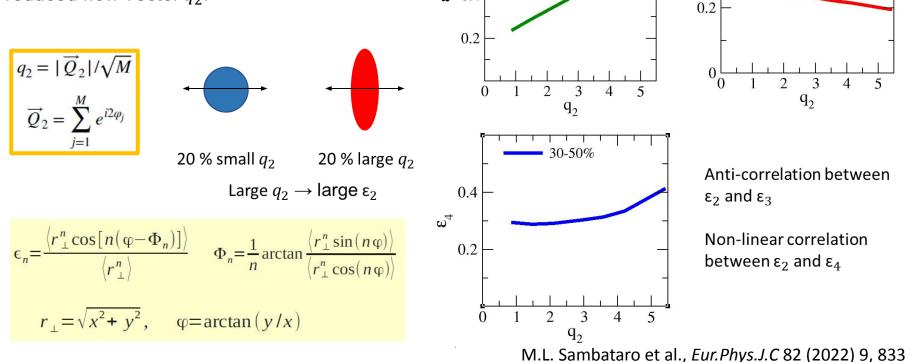
S.Plumari et al, *Phys.Rev.C* 92 (2015) 5





Event-Shape-Engeenering technique

Selection of events with the same centrality but different initial geometry on the basis of the magnitude of the second-order harmonic reduced flow vector q_2 .



0.8

0.6

ພິ 0.4

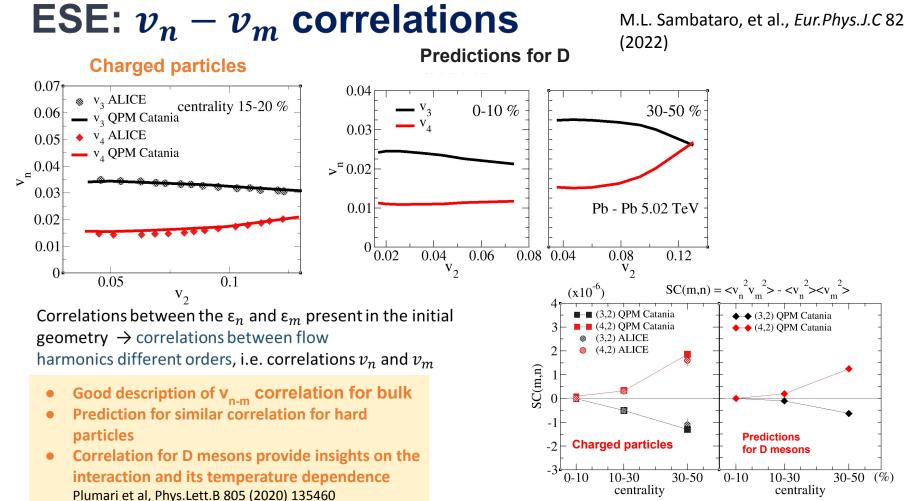
30-50%

Pb-Pb 5,02 TeV

0.4

 $\tilde{\epsilon}$

30-50%



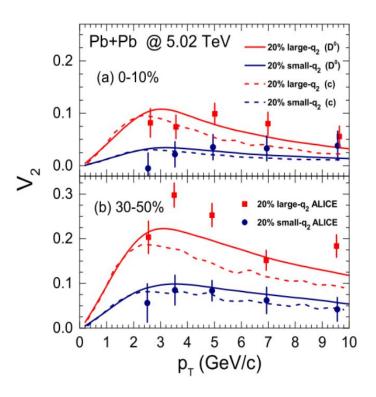
Data taken from: S. Mohapatra Nucl. Phys. A 956 (2016) 59-66

Event-shape-engeenering

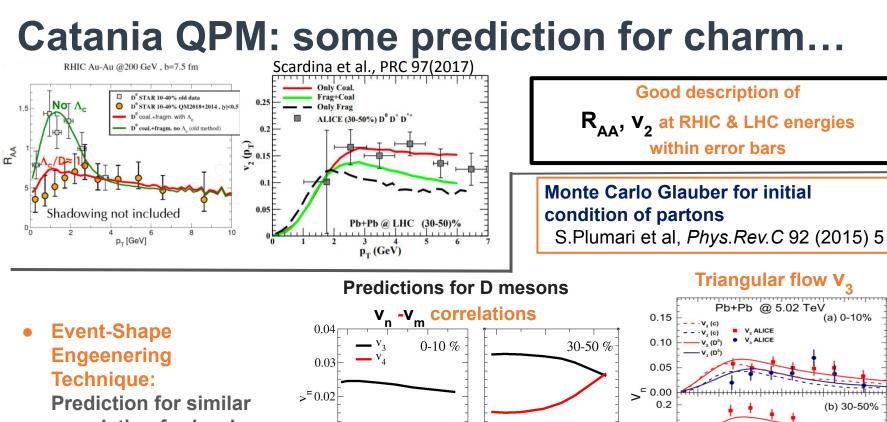
Selection of events with the same centrality but different initial geometry on the basis of the magnitude of the second-order harmonic reduced flow vector q_2 .

 $q_2 = |\vec{Q}_2| / \sqrt{M}$ $\vec{Q}_2 = \sum_{j=1}^{M} e^{i2\varphi_j}$ 20 % small q_2 20 % large q_2 Large $q_2 \rightarrow \text{large } \epsilon_2$ $\epsilon_{n} = \frac{\langle r_{\perp}^{n} \cos[n(\varphi - \Phi_{n})] \rangle}{\langle r_{\perp}^{n} \rangle} \qquad \Phi_{n} = \frac{1}{n} \arctan \frac{\langle r_{\perp}^{n} \sin(n\varphi) \rangle}{\langle r_{\perp}^{n} \cos(n\varphi) \rangle}$ $r_{\perp} = \sqrt{x^2 + y^2}, \quad \varphi = \arctan(y/x)$

M.L. Sambataro et al., *Eur.Phys.J.C* 82 (2022) 9, 833



Discrepancy between selected v_2 and unbiased one ~ 50%



0.08 0.04

Pb - Pb 5.02 TeV

0.08

v₂

0.12

0.1

0.0

0

2 3

8

p₊ (GeV/c)

9 10

0.01

0.02

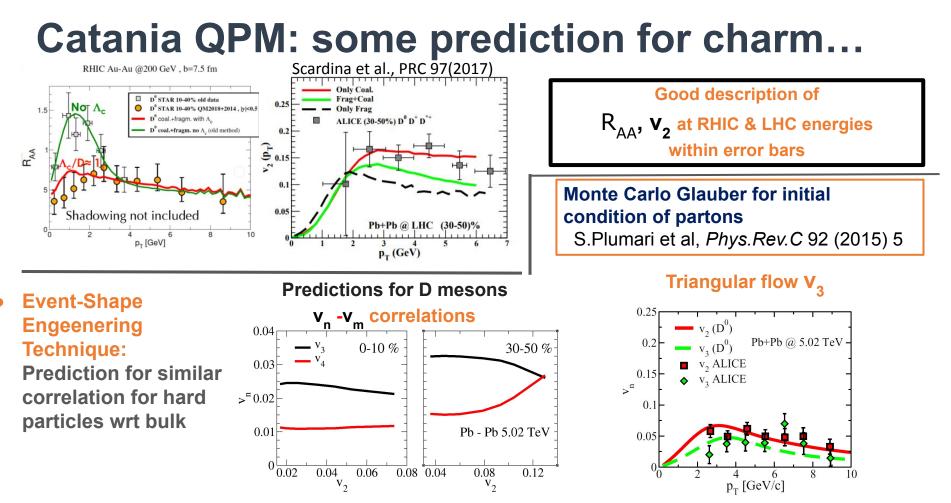
0.04

v₂

0.06

correlation for hard particles wrt bulk

ALICE collaboration, *Phys.Lett.B* 813 (2021) 136054 M.L. Sambataro, et al., *Eur.Phys.J.C* 82 (2022)



ALICE collaboration, *Phys.Lett.B* 813 (2021) 136054 M.L. Sambataro, et al., *Eur.Phys.J.C* 82 (2022)

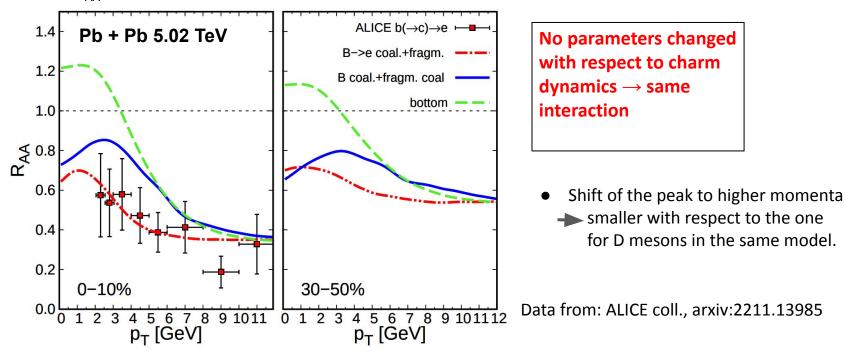
[See S. Bass Overview on transport model (03 June 15.15)]

Extension to bottom dynamics: R_{AA}

Hadronization with coalescence + fragmentation model

 \succ Prediction for B meson R_{AA}

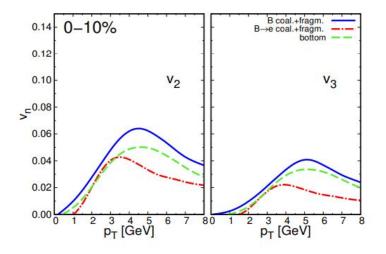
R_{AA} of electrons from semileptonic B meson decay



M.L. Sambataro et al., *Phys.Lett.B* 849 (2024) 138480

Extension to bottom dynamics: v_(n=2,3)

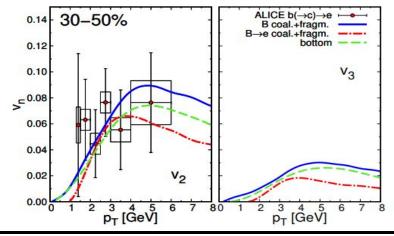
- Prediction for B meson
- electrons from semileptonic B meson decay within a coal + fragm model



No parameters changed with respect to charm dynamics

M.L. Sambataro et al., *Phys.Lett.B* 849 (2024) 138480

Data from ALICE, PRL 126, 162001 (2021)



Compared to charm quark

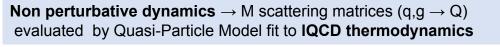
- Efficiency of conversion of ε_2 :
- ► 15% smaller for v_2 in most central collisions. ↓ 40% smaller for v_2 at 30–50% centrality.
- Efficiency of conversion of ε_3 :
- ► 30% smaller for v_3 at both 0-10% and 30-50% centralities.

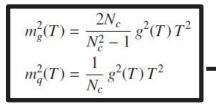
From central to peripheral

- enhancement of v₂ (ϵ_2 (0-10%) \approx 0.13 and ϵ_2 (30-50%) \approx 0.42)
- similar v₃ ($\epsilon_3(0-10^{5}\%)^{-2}0.11$ and $\epsilon_3(30-50\%)^{-2}0.21$)

MOMENTUM DEPENDENT Quasi Particle Model: <u>QPM vs QPMp</u>

Going back to Quasi Particle Model (QPM)... Equation of State and Susceptibilities





Thermal masses of gluons and light quarks

N_f=2+1 Bulk: u,d,s

QPM Standard

no momentum dependence

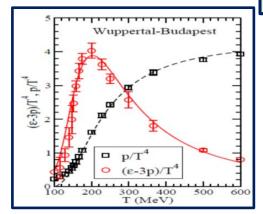


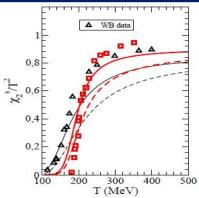


 $g^{2}(T) = \frac{48\pi^{2}}{(11N_{c} - 2N_{f})\ln\left[\lambda\left(\frac{T}{T_{c}} - \frac{T_{s}}{T_{c}}\right)\right]^{2}} \qquad \lambda = 2.6 \\ T_{s} = 0.57 T_{c}$

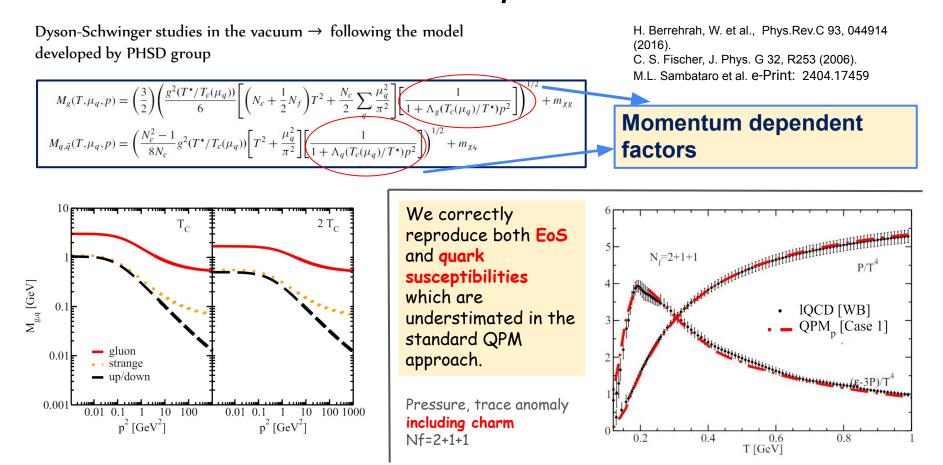


S. Plumari et al, *Phys.Rev.D* 84 (2011) 094004 H. Berrehrah, PHYSICAL REVIEW C **93**, 044914 (2016)





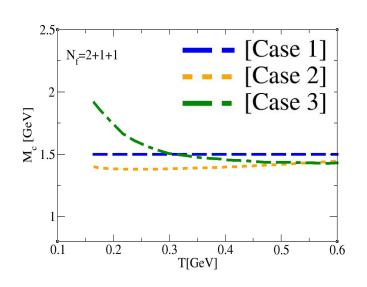
QPM extension: QPMp(N_f=2+1+1)



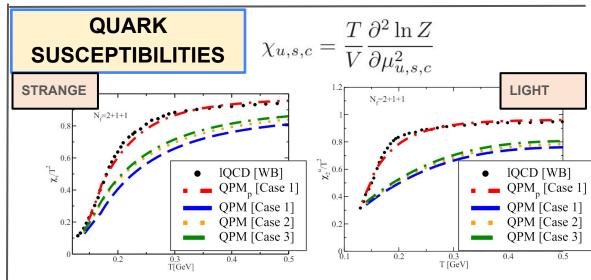
QPM extension: $QPMp(N_f=2+1+1)$ and $m_c(T)$

we have also extended our quasi-particle model approach for Nf = 2+1 to Nf = 2 + 1 + 1 where the charm quark is included Temperature parametrization for charm mass:

Case 1: $m_c = 1.5 \ GeV$ **Case 2:** $m_c^2 = m_{c0}^2 + \frac{N_c^2 - 1}{8N_c} g^2 [T^2 + \frac{\mu_c^2}{\pi^2}]$ with $m_{c0} = 1.3 \ GeV$ **Case 3:** m_c fixed by charm fluctuation $\chi_2^c = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_i^2}$



M.L. Sambataro et al. e-Print: 2404.17459

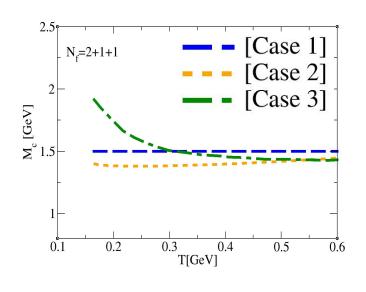


QPM understimates the IQCD data;

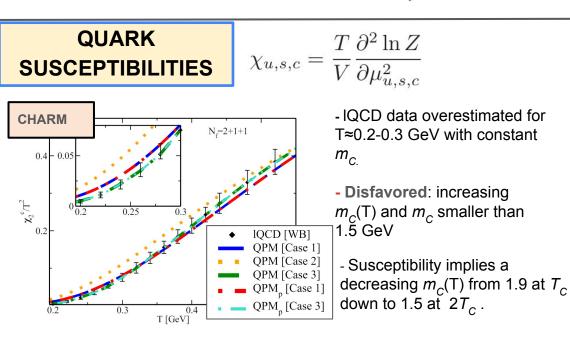
QPMp -> smaller 'thermal average mass' -> extra contribution in susceptibility

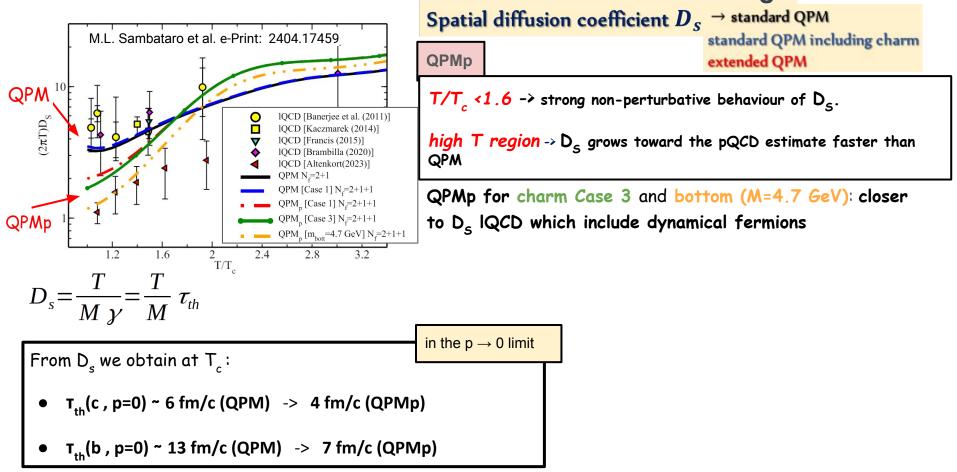
QPM extension: $QPMp(N_f=2+1+1)$ and $m_c(T)$

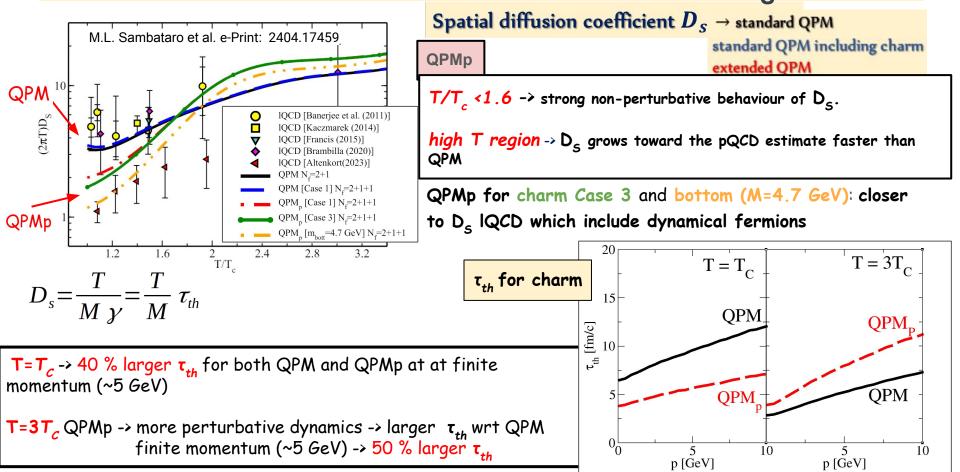
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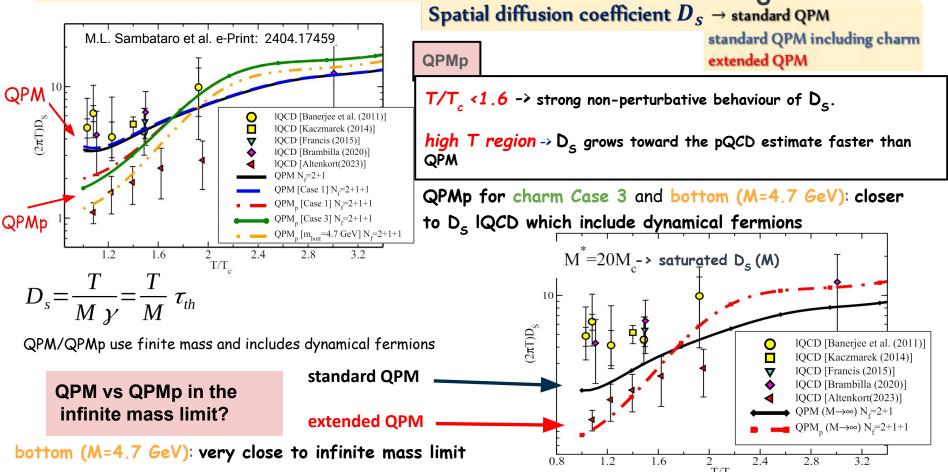


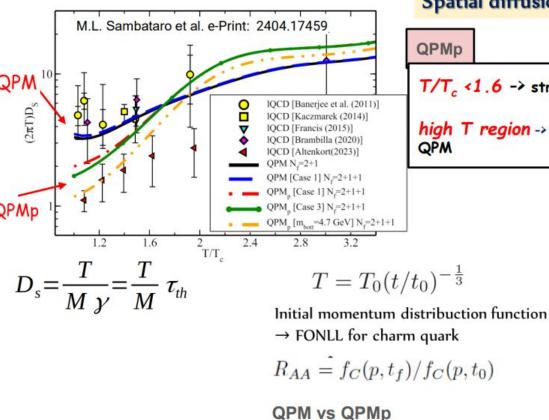
M.L. Sambataro et al. e-Print: 2404.17459









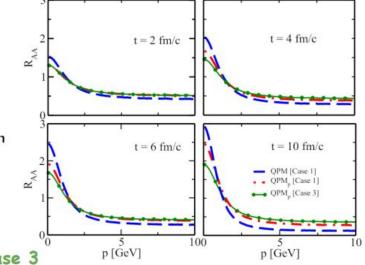


-> RAA reduction especially for Case 3

Spatial diffusion coefficient $D_s \rightarrow \text{standard QPM}$ QPMpstandard QPM including charm
extended QPM

 $T/T_c < 1.6 \rightarrow$ strong non-perturbative behaviour of D_s .

high T region -> D₅ grows toward the pQCD estimate faster than QPM



Conclusions

- Extension to bottom quark dynamics in standard QPM: good description of R_{AA} and v_2 of electrons from semileptonic B meson decay and prediction for v_2 and v_3
- Charm mass [T] parametrization: charm susceptibility as function of T implies a decreasing $m_c(T)$ from 1.9 at T_c down to 1.5 at $2T_c$ getting closer to IQCD data for Ds.
- QPMp

Good reproduction of both EoS and susceptibilities -> decrease of D_s at small T. Bottom D_s very close to the new IQCD data for M-> ∞ .

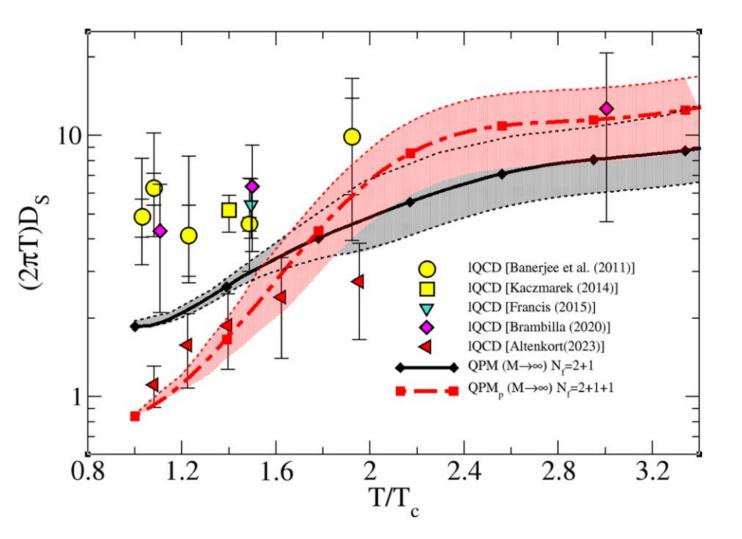
- Spatial diffusion coefficient D_s(T) in the infinite mass limit -> satisfactory agreement with the IQCD calculations that include dynamical fermions, differently from previous IQCD data in quenched approximation.
 - Perspectives: Effect on observables for realistic simulations.

Thanks for the attention!

25

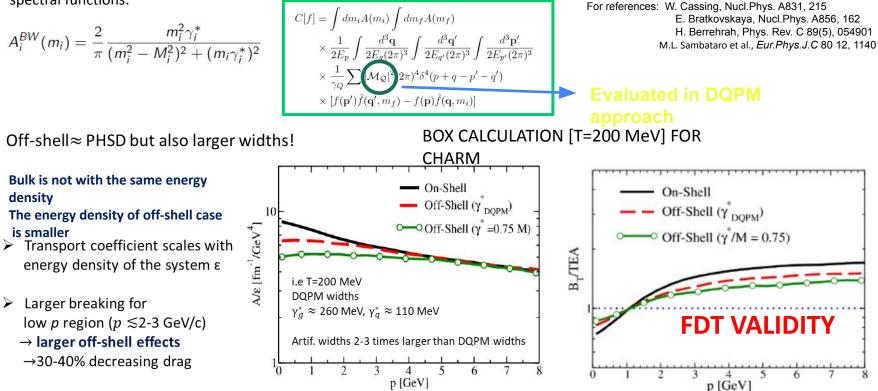
Back up slides

26



Non-perturbative effects: impact of off-shell dynamics QPM vs. DQPM

Partons are dressed by non-perturbative spectral functions:

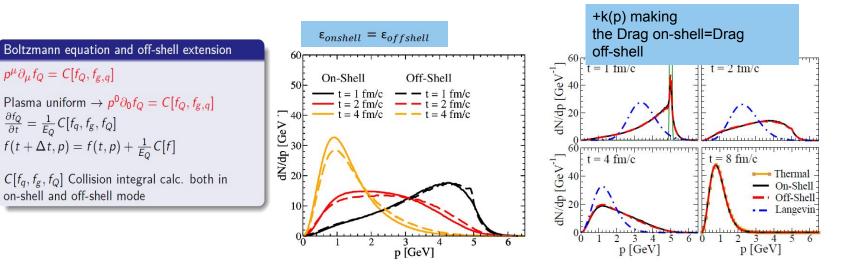


On-shell vs Off-shell energy loss

Partons are dressed by non-perturbative spectral functions:

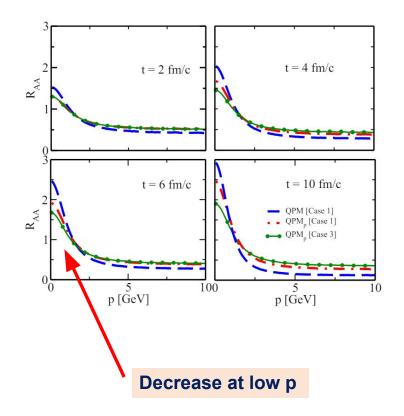
$$A_i^{BW}(m_i) = \frac{2}{\pi} \frac{m_i^2 \gamma_i^*}{(m_i^2 - M_i^2)^2 + (m_i \gamma_i^*)^2}$$

BOX CALCULATION [T=200 MeV] FOR CHARM



The difference between on-shell and off-shell mode can be adsorbed by multiplying scattering matrix for a *k* factor

$QPMp - D_s and R_{AA}$



1+1D system $T = T_0 (t/t_0)^{-\frac{1}{3}}$

Initial momentum distribuction function \rightarrow FONLL for charm quark $R_{AA} = f_C(p, t_f) / f_C(p, t_0)$

QPM vs QPMp -> R_{AA} reduction especially for Case 3

Momentum dependent QPM approach

- Better description of recent IQCD data.
- Effects on the global χ^2 coming from the comparison to the experimental data of R_{AA} , v_n ?

QPM extended – QPMp + m_c (T)

we have also extended our quasi-particle model approach for Nf = 2+1 to Nf = 2 + 1 + 1 where the charm quark is included Temperature parametrization for charm mass Case 1: $m_c = 1.5 \ GeV$ Case 2: $m_c^2 = m_{c0}^2 + \frac{N_c^2 - 1}{8N_c}g^2[T^2 + \frac{\mu_c^2}{\pi^2}]$ with $m_{c0} = 1.3 \ GeV$ Case 3: m_c fixed by charm fluctuation $\chi_2^c = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_i^2}$

The following expression for the quark fluctuations:

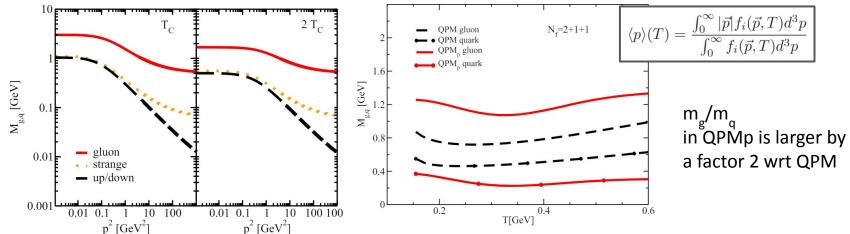
$$c_2^q = \frac{\chi_2^q}{2} = \frac{1}{2} \frac{6}{\pi^2} \left(\frac{m_q}{T}\right)^2 \sum_{l=1}^{\infty} (-1)^{l+1} K_2(lm_q/T)$$

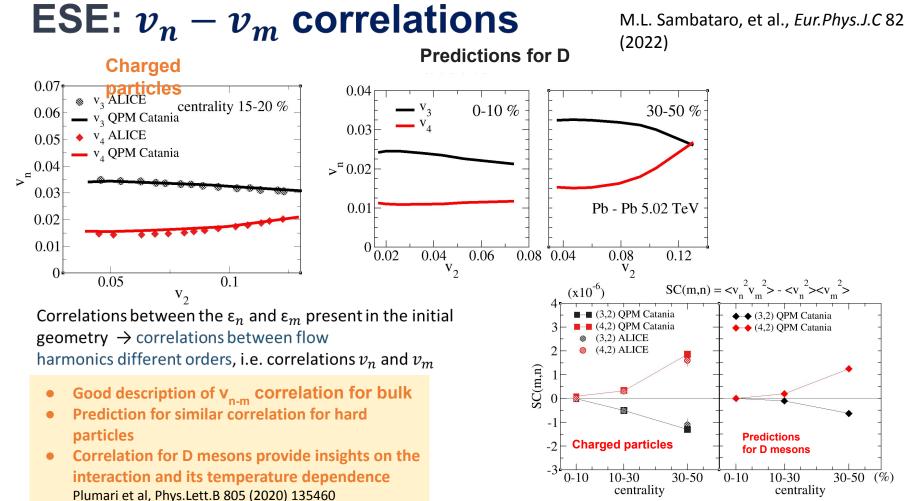
can be solved in terms of mq/T, with the χ values numerically obtained in IQCD. We then fit the resulting temperature dependence of charm mass

QPM extended – QPMp

Dyson-Schwinger studies in the vacuum \rightarrow following the model developed by PHSD group $M_{g}(T,\mu_{q},p) = \left(\frac{3}{2}\right) \left(\frac{g^{2}(T^{*}/T_{c}(\mu_{q}))}{6} \left[\left(N_{c} + \frac{1}{2}N_{f}\right)T^{2} + \frac{N_{c}}{2}\sum_{q}\frac{\mu_{q}^{2}}{\pi^{2}}\right] \left[\frac{1}{1 + \Lambda_{g}(T_{c}(\mu_{q})/T^{*})p^{2}}\right]^{1/2} + m_{\chi g}\right]$ $M_{q,\bar{q}}(T,\mu_{q},p) = \left(\frac{N_{c}^{2} - 1}{8N_{c}}g^{2}(T^{*}/T_{c}(\mu_{q}))\left[T^{2} + \frac{\mu_{q}^{2}}{\pi^{2}}\right] \left[\frac{1}{1 + \Lambda_{q}(T_{c}(\mu_{q})/T^{*})p^{2}}\right]^{1/2} + m_{\chi g}$ $M_{q,\bar{q}}(T,\mu_{q},p) = \left(\frac{N_{c}^{2} - 1}{8N_{c}}g^{2}(T^{*}/T_{c}(\mu_{q}))\left[T^{2} + \frac{\mu_{q}^{2}}{\pi^{2}}\right] \left[\frac{1}{1 + \Lambda_{q}(T_{c}(\mu_{q})/T^{*})p^{2}}\right]^{1/2} + m_{\chi g}$ $M_{q,\bar{q}}(T,\mu_{q},p) = \left(\frac{N_{c}^{2} - 1}{8N_{c}}g^{2}(T^{*}/T_{c}(\mu_{q}))\left[T^{2} + \frac{\mu_{q}^{2}}{\pi^{2}}\right] \left[\frac{1}{1 + \Lambda_{q}(T_{c}(\mu_{q})/T^{*})p^{2}}\right]^{1/2} + m_{\chi g}$

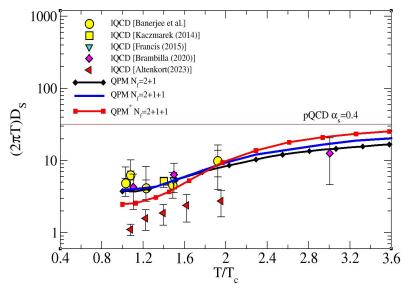
We correctly reproduce both **EoS** and **quark susceptibilities** which are understimated in the standard QPM approach.





Data taken from: S. Mohapatra Nucl. Phys. A 956 (2016) 59-66

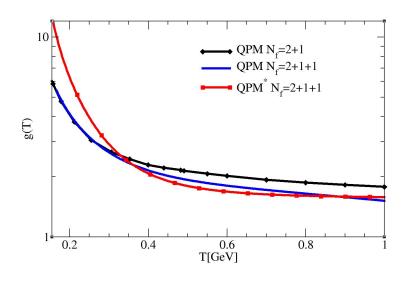
QPM extended – **Preliminary** D_s and R_{AA}



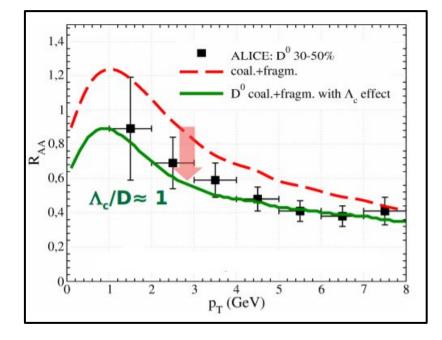
coupling g(T)

Spatial diffusion coefficient $D_s \xrightarrow{\rightarrow}$ standard QPM standard QPM including charm extended QPM $T/T_c < 2 \xrightarrow{\rightarrow}$ strong non-perturbative behaviour near to T_c .

high T region \rightarrow the D_s reaches the pQCD limit quickly than the standard QPM.

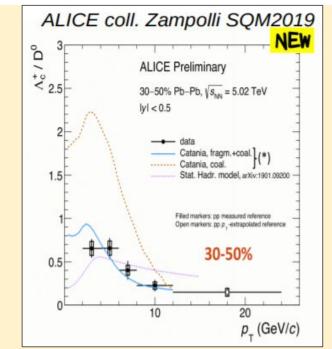


D meson: Impact of large Λ_c production on R_{AA}



 $D_s(\mathbf{T})$ of charm quark that reproduces R_{AA} and v_2 gives good description of

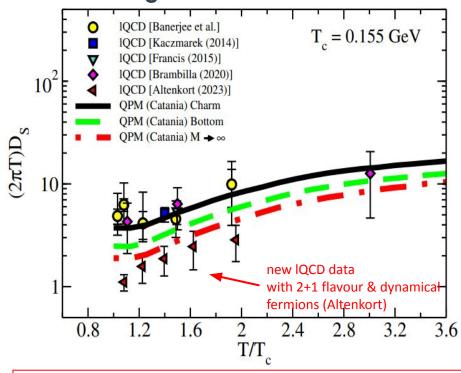
- > Impact of Λ_c/D^0
- > Triangular flow $v_3(p_T)$.
- \succ q_2 selected anisotropic flow and spectra.



> With the same coalescence plus fragmentation model we describe the Λ_c/D^0

S. Plumari, et al., Eur. Phys. J. C78 no. 4, (2018) 348

$(2\pi T)D_s$: Charm quark vs Bottom quark



From D_s we obtain (in the 1-2T_c range):

- $T_{th}(c) \sim 5 \text{ fm/c}$
- $T_{th}^{(i)}(b) \sim 11 \text{ fm/c}$ breaking w.r.t. the relation: $T_{th}(b) = (M_b/M_c)T_{th}(c) \sim 3.3 T_{th}(c) \sim 16.5 \text{ fm/c}$

- IQCD data are in $M_Q \rightarrow \infty$, so the D_s evaluated is mass independent + quenched medium
- QPM use finite mass and includes dynamical fermions

$$D_s = \frac{T}{M \gamma} = \frac{T}{M} \tau_{th}$$

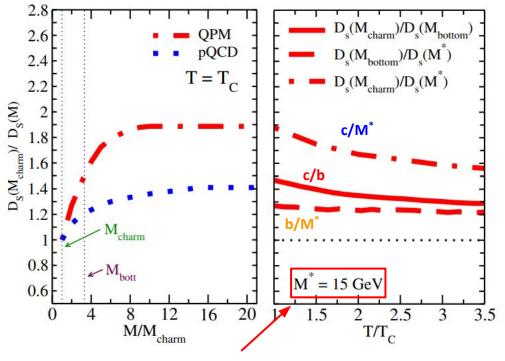
From kinetic theory is expected that: $au_{th}(b) / \tau_{th}(c) \approx \gamma_c / \gamma_b \approx M_b / M_c$

In QPM approach $\rightarrow D_s(c)$ is 30-40% larger than $D_s(b)$ (no mass independence)

 $M{\rightarrow}$ ∞ limit is not reached for charm

M.L. Sambataro et al., e-Print: 2304.02953

$(2\pi T)D_s$ ratios: Charm quark vs Bottom quark



fictitious super-heavy quark staying in the $\rm M_Q \rightarrow \infty$ limit

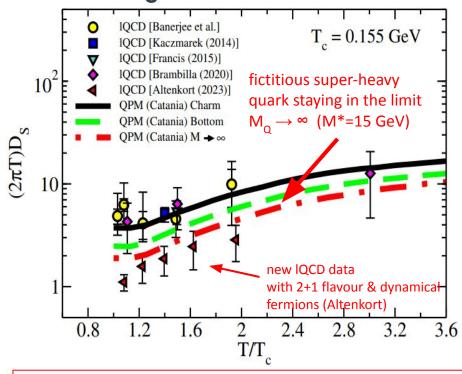
> $D_s(M_{charm})/D_s(M)$ as a function of M/M_{charm} at T_c :

Saturation scale of Ds for $M_Q \sim 8 M_{charm} \gtrsim 10 \text{ GeV}$ Ds $(M_{charm})/Ds(M \rightarrow \infty) = 1.9 \text{ for QPM}.$ Ds $(M_{charm})/Ds(M \rightarrow \infty) \simeq 1.4 \text{ for pQCD}.$

- Ratios at fixed mass as a function of T:
 - **b/M^{*}: about 25% in all T range**
 - c/b: about 50% at $\rm T_{c}\,$ and not smaller than 30%
 - c/M*: factor 1.5-2

M.L. Sambataro et al., e-Print: 2304.02953

$(2\pi T)D_s$: Charm quark vs Bottom quark



- From D_v we obtain (in the 1-2T_v range):
- $T_{th}(c) \sim 5 \text{ fm/c}$
- $T_{th}^{(i)}(b) \sim 11 \text{ fm/c}$ breaking w.r.t. the relation: $T_{th}(b) = (M_b/M_c)T_{th}(c) \sim 3.3 T_{th}(c) \sim 16.5 \text{ fm/c}$

IQCD data are in M_Q→∞ so D_s is mass independent

$$D_s = \frac{T}{M \gamma} = \frac{T}{M} \tau_{th}$$

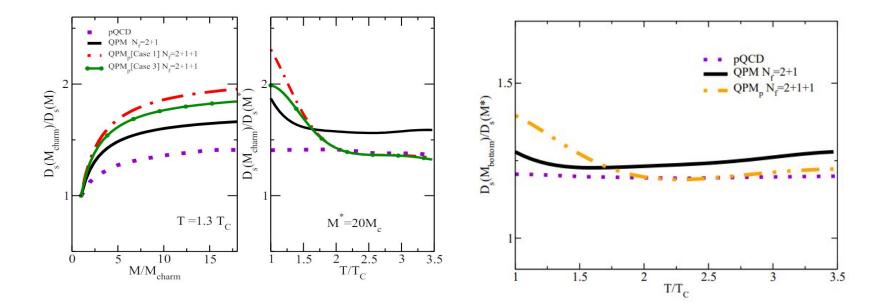
• QPM use finite mass and includes dynamical fermions

From kinetic theory is expected that: $\tau_{th}(b) / \tau_{th}(c) \approx \gamma_c / \gamma_b \approx M_b / M_c$

D_s(T) from QPM in the infinite mass limit is the more pertinent to compare to IQCD simulations evaluated taking into account dynamical fermions

M.L. Sambataro et al., e-Print: 2304.02953

Ds mass dependence: QPM vs QPMp



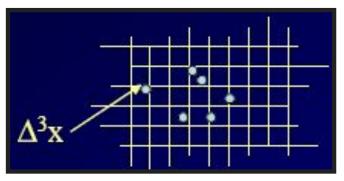
Numerical solution of Boltzmann Equation

Use Test-Particle Method to sample the phase space distribution function

 $f(\vec{x}, \vec{p}, t) = \omega \sum_{i=1}^{N_{test}} \delta^{(3)}(\vec{x} - \vec{r}_i(t)) \delta^{(3)}(\vec{p} - \vec{p}_i(t))$

 \mathbf{F}_{i} solution of Boltzmann eq. $\rightarrow~$ Test particles solve classical Hamilton eq. of motion

$$\begin{cases} \vec{p}_i(t + \Delta t) = \vec{p}_i(t - \Delta t) + 2\Delta t \cdot \left(\frac{\partial \vec{p}_i}{\partial t}\right)_{coll} \\ \vec{r}_i(t + \Delta t) = \vec{r}_i(t - \Delta t) - 2\Delta t \cdot \left[\frac{\vec{p}_i(t)}{E_i(t)}\right] \end{cases}$$



Collision Integral mapped through a Stochastic Al

$$P_{22} = \frac{\Delta N_{coll}^{2 \to 2}}{\Delta N_1 \Delta N_2} = v_{rel} \sigma_{22} \frac{\Delta t}{\Delta^3 x}$$

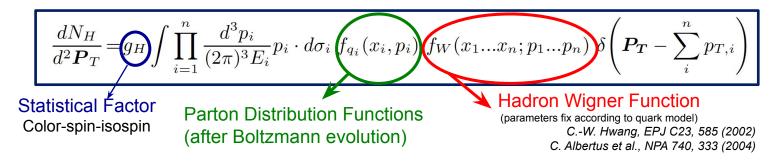
 $\Delta t \square 0$ and $\Delta^3 x \square 0$: exact solution

Final phase-space of HQ + bulk parton scattering sampled according to $|M_{QCD}|^2 \square$ code test through simulations in a "box"

[Scardina, Colonna, Plumari, and Greco PLB v.724, 296 (2013)] [Xu and Greiner PRC v. 71, (2005)]

Hybrid Hadronization Model for HQs

COALESCENCE: Formula developed for the light sector [Greco, Ko, Levai PRL 90 (2003)]



FRAGMENTATION: HQs that do not undergo to Coalescence

$$\frac{dN_H}{d^2 \boldsymbol{P}_T} = \sum_f \int dz \frac{dN_f}{d^2 p_T} \frac{D_{f \to H}(z)}{z^2}$$

We use Peterson parametrization: $D_H(z) \propto \left[z \left(1 - \frac{1}{z} - \frac{\epsilon_c}{1-z} \right)^2 \right]^{-1}$

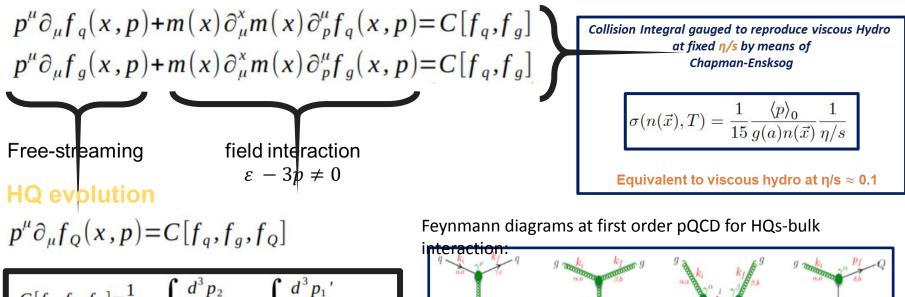
Peterson et al. PRD 27 (1983) 105

Parameter ε_{c} tuned to reproduce *D* and *B* meson spectra in pp collisions.

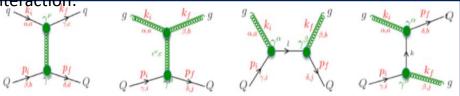
Plumari, Minissale, Das, Coci, Greco, EPJ C 78 (2018) no.4

Relativistic Boltzmann equation at finite η/s

Bulk evolution

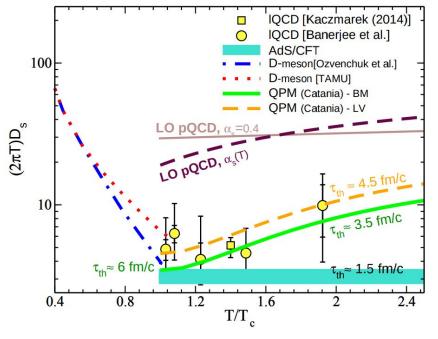


$$C[f_{q}, f_{g}, f_{Q}] = \frac{1}{2E_{1}} \int \frac{d^{3}p_{2}}{2E_{2}(2\pi)^{3}} \int \frac{d^{3}p_{1}'}{2E_{1}'(2\pi)^{3}} \times [f_{Q}(p_{1}')f_{q,g}(p_{2}') - f_{Q}(p_{1})f_{q,g}(p_{2})] \times |M_{(q,g) \rightarrow Q}(p_{1}p_{2} \rightarrow p_{1}'p_{2}')| \times (2\pi)^{4} \delta^{4}(p_{1} + p_{2} - p_{1}' - p_{2}')$$



Scattering matrices $M_{a,a}$ by QPM fit to IQCD thermodynamics

Spatial diffusion coefficient of charm quark



<u>Reviews :</u>

- F. Prino and R. Rapp, JPG(2019)
- X. Dong and V. Greco, Prog.Part.Nucl.Phys. (2019)
- Jiaxing Zhao et al., arXiv:2005.08277

Not a model fit to IQCD data, but $\rm D_{s}$ estimate that comes from results of $\rm R_{AA}~(p_{T})$ and $\rm v_{2}~(p_{T})$

We have a probe with $\tau_{therm}\approx\tau_{QGP}$

$$\tau_{th} = \frac{M}{2\pi T^2} (2\pi T D_s) \cong 1.8 \frac{2\pi T D_s}{(T/T_c)^2} \text{ fm/c}$$

FUTURE:

- -Access low p and precision data (detector
- upgrade)
- -Better insight into hadronization
- -New observables
- -Bottom Main focus of this talk