

Heavy quarks as probes of QGP transport properties and hadronization dynamics

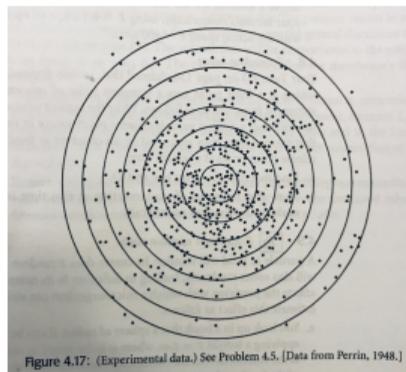
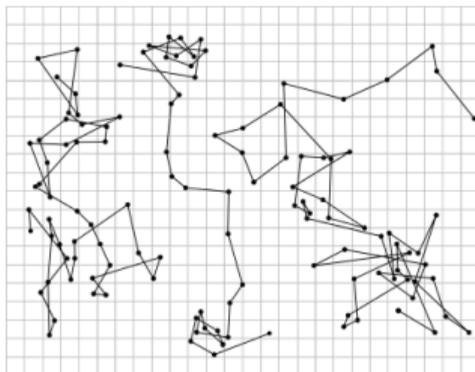
Andrea Beraudo

INFN - Sezione di Torino

SIM e PRIN meeting, Catania, 10-11 settembre 2024



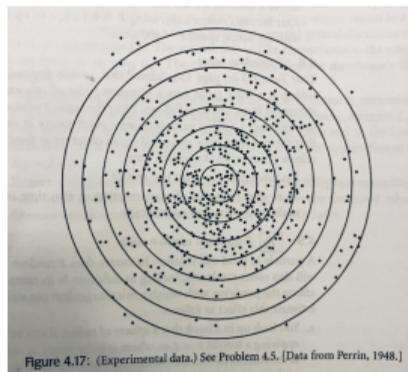
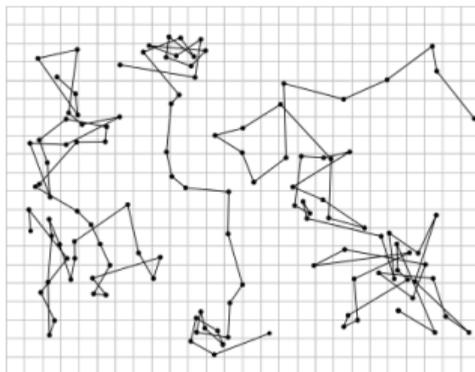
HF in HIC's: what do we want to learn? A bit of history...



Einstein (1905) and Perrin (1909) study of Brownian motion: from the random walk of small grains ($a \sim 0.5\mu\text{m}$) in water one extracts the **diffusion coefficient**

$$\langle x^2 \rangle_{t \rightarrow \infty} \sim 2D_s t$$

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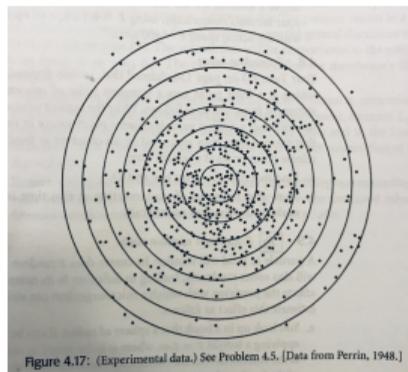
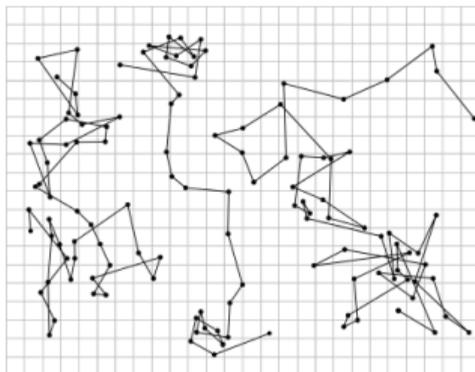
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and estimates the **Avogadro number** (proof of the *granular structure of matter*):

$$\mathcal{N}_A K_B \equiv \mathcal{R} \quad \longrightarrow \quad \mathcal{N}_A = \frac{\mathcal{R} T}{6\pi a \eta D_s}$$

Perrin obtained the values $\mathcal{N}_A \approx 5.5 - 7.2 \cdot 10^{23}$.

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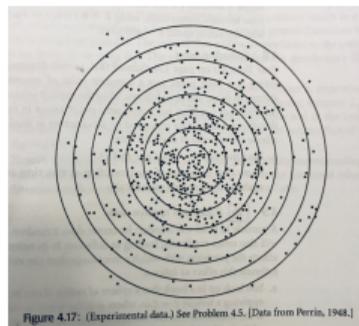
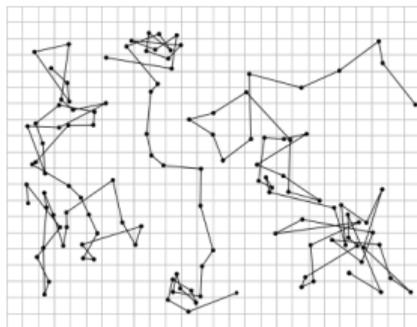
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Perrin obtained the values $\mathcal{N}_A \approx 5.5 - 7.2 \cdot 10^{23}$. We would like to **derive HQ transport coefficients in the QGP** with a comparable precision and accuracy!

HF in HIC's: what do we want to learn? A bit of history...



- “Brownian motion cannot be stopped suppressing convection currents, which are easy to recognize” (Perrin 1909): it is a **random motion superimposed to the collective flow of the fluid**. **Do HQ's in HIC's have enough time to become part of the fluid?**

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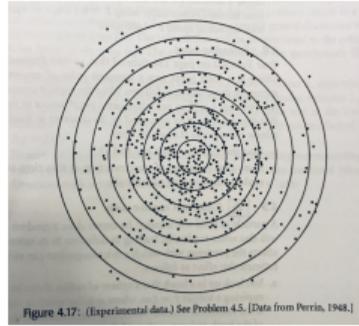
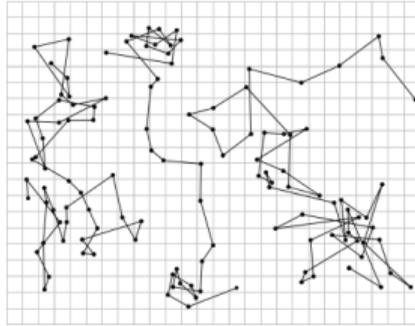
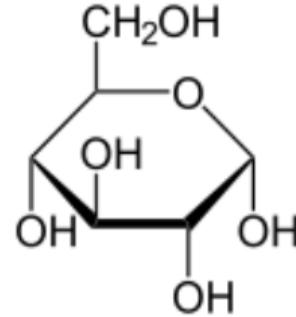
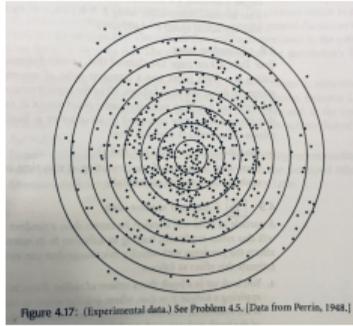
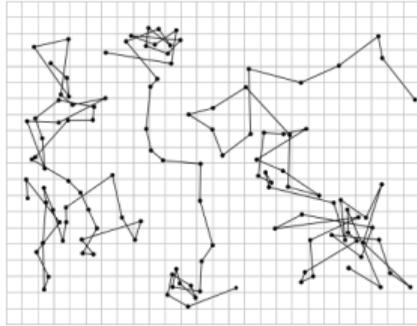


Figure 4.17: (Experimental data.) See Problem 4.5. [Data from Perrin, 1948.]

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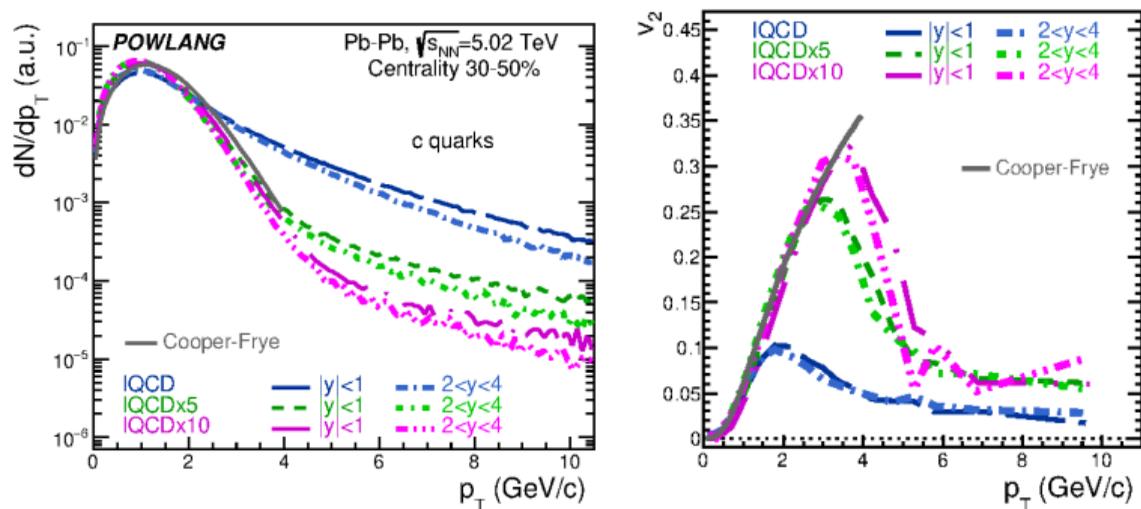


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- Experiments took time: several months to go from 1 kg of gumgutta to 10^{-4} kg of grains of the same size;
- **Equations for Brownian motion work also at the molecular level**, describing diffusion of sugar ($C_6H_{12}O_6$) in water (H_2O)

$$\mathcal{N}_A = 6.5 \cdot 10^{23}$$

Notice that $M_{\text{sugar}} \approx 10M_{\text{water}}$, as HQ to light-quasiparticle mass ratio

We do not have a microscope!

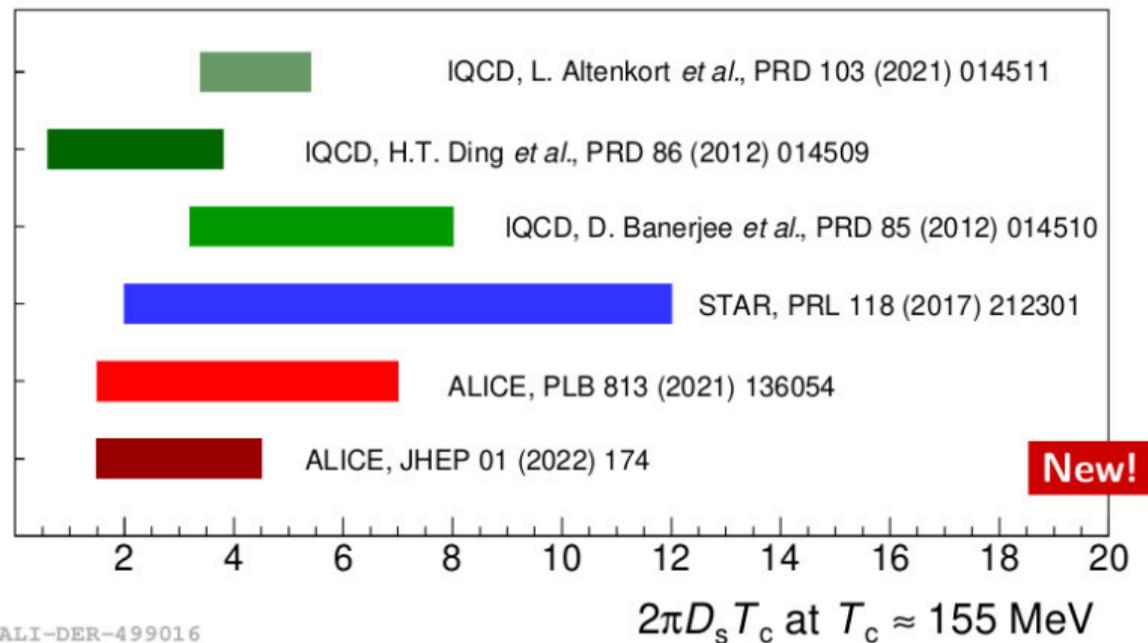


Transport coefficients can be accessed indirectly, comparing transport predictions with different values of **momentum broadening**

$$\kappa = \frac{2T^2}{D_s}$$

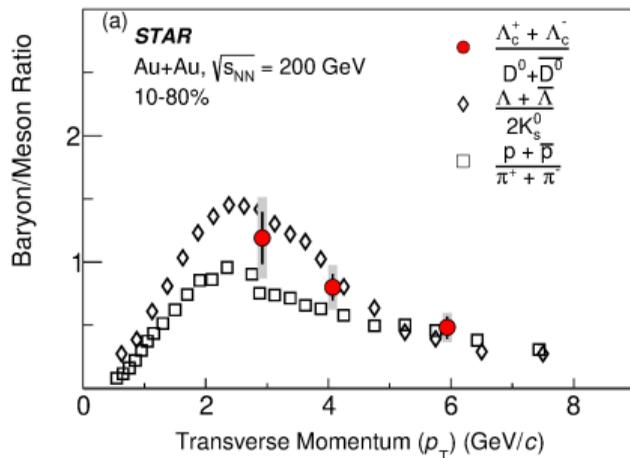
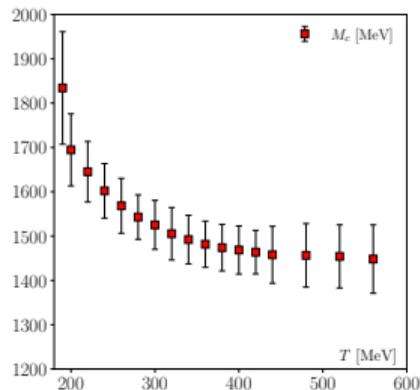
with experimental results for momentum (left) and angular (right) HF particle distributions (figure from [A.B. et al., JHEP 05 \(2021\) 279](#))

Where do we stand?



Still far from accuracy and precision of Perrin result for \mathcal{N}_A ...

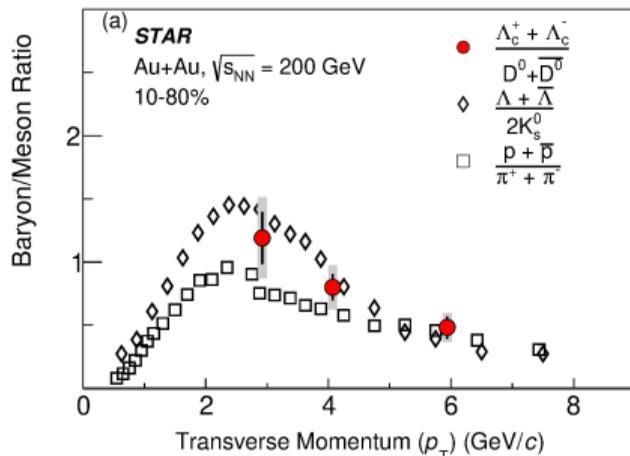
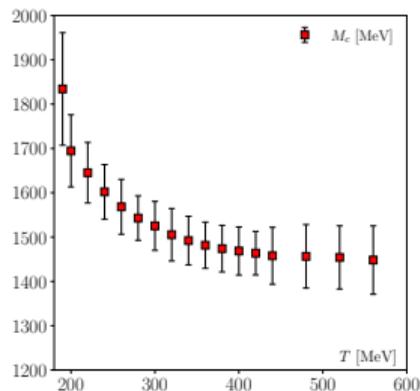
A crucial difference



In HF studies in nuclear collisions the **nature of the Brownian particle changes** during its propagation through the medium

- possible thermal mass-shift, see [2311.01525 \[hep-lat\]](#) (here neglected)
- **hadronization** (impossible to neglect)

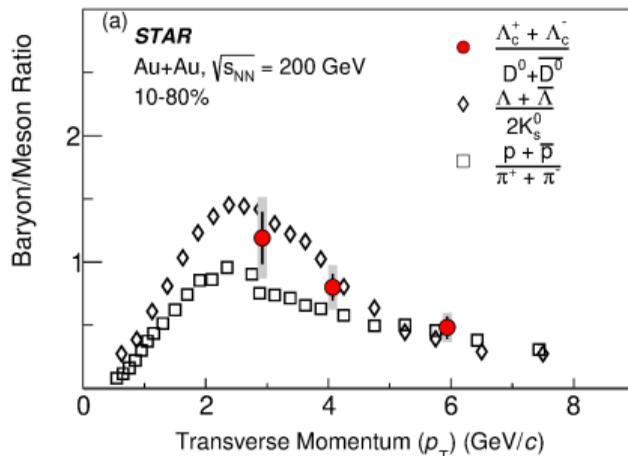
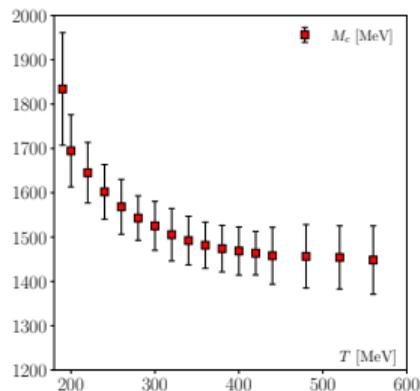
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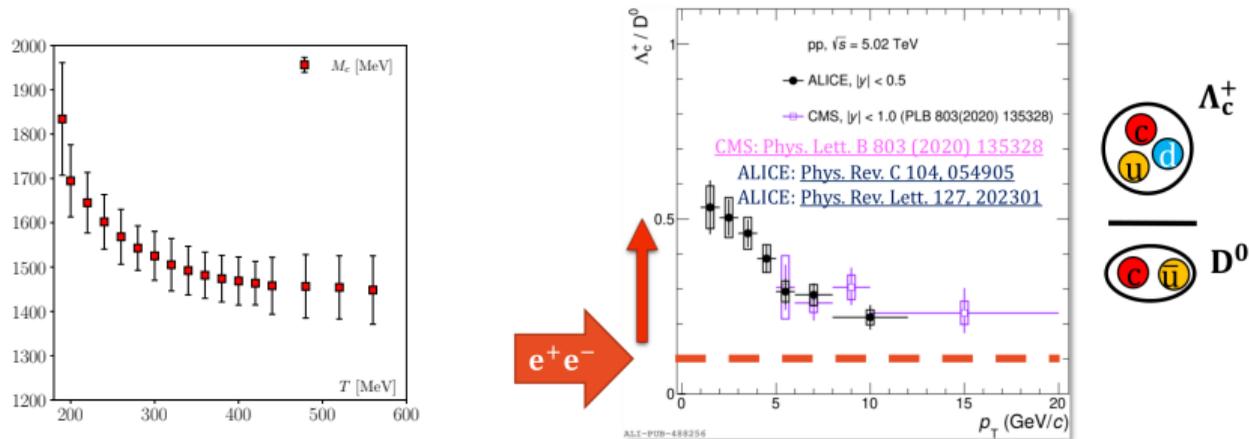
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 - an issue of interest in itself: how **quark \rightarrow hadron transition changes in the presence of a medium** (one of the topics of this talk). **How big should the medium be?**

HQ dynamics in the fireball

To model the HQ propagation in an expanding fireball one develops a **relativistic Langevin equation**, obtained from the soft-scattering limit of the Boltzmann equation (A.B. et al., Nucl.Phys. A831 (2009) 59)

$$\frac{\Delta p^i}{\Delta t} = - \underbrace{\eta_D(\mathbf{p}) p^i}_{\text{determ.}} + \underbrace{\xi^i(t)}_{\text{stochastic}},$$

with the properties of the noise encoded in

$$\langle \xi^i(\mathbf{p}_t) \rangle = 0 \quad \langle \xi^i(\mathbf{p}_t) \xi^j(\mathbf{p}_{t'}) \rangle = b^{ij}(\mathbf{p}) \frac{\delta_{tt'}}{\Delta t} \quad b^{ij}(\mathbf{p}) \equiv \kappa_{\parallel}(\mathbf{p}) \hat{p}^i \hat{p}^j + \kappa_{\perp}(\mathbf{p}) (\delta^{ij} - \hat{p}^i \hat{p}^j)$$

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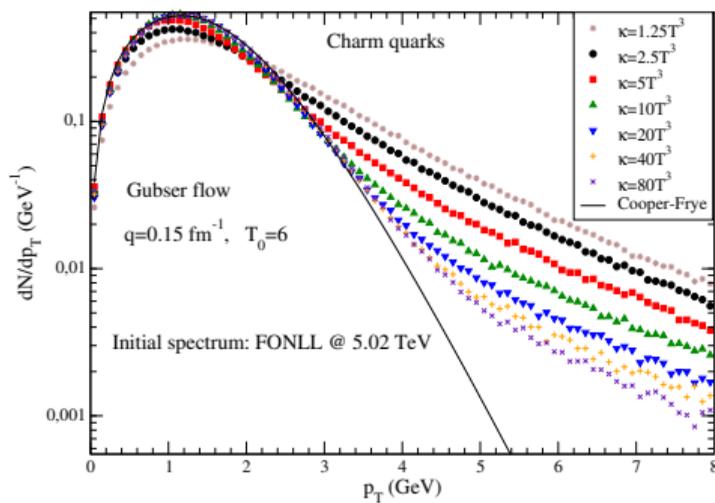
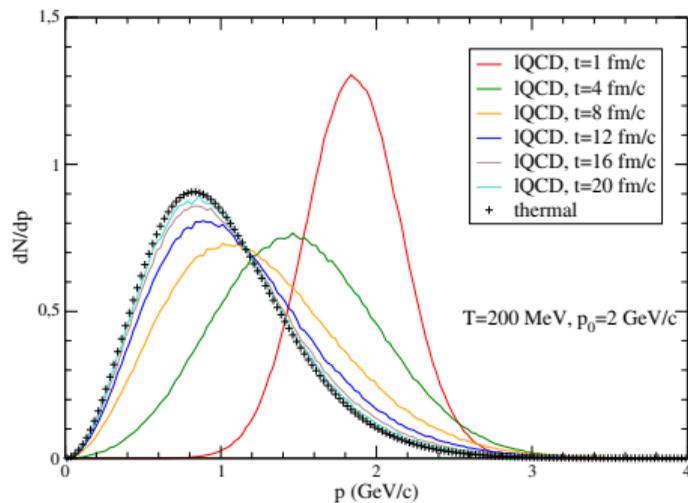
Transport coefficients describe the HQ-medium coupling

- **Momentum diffusion** $\kappa_{\perp} \equiv \frac{1}{2} \frac{\langle \Delta p_{\perp}^2 \rangle}{\Delta t}$ and $\kappa_{\parallel} \equiv \frac{\langle \Delta p_{\parallel}^2 \rangle}{\Delta t}$;
- **Friction** term (dependent on the **discretization scheme!**)

$$\eta_D^{\text{Ito}}(\mathbf{p}) = \frac{\kappa_{\parallel}(\mathbf{p})}{2TE_p} - \frac{1}{E_p^2} \left[(1 - v^2) \frac{\partial \kappa_{\parallel}(\mathbf{p})}{\partial v^2} + \frac{d-1}{2} \frac{\kappa_{\parallel}(\mathbf{p}) - \kappa_{\perp}(\mathbf{p})}{v^2} \right]$$

fixed in order to assure approach to equilibrium (**Einstein relation**)

Asymptotic approach to thermalization

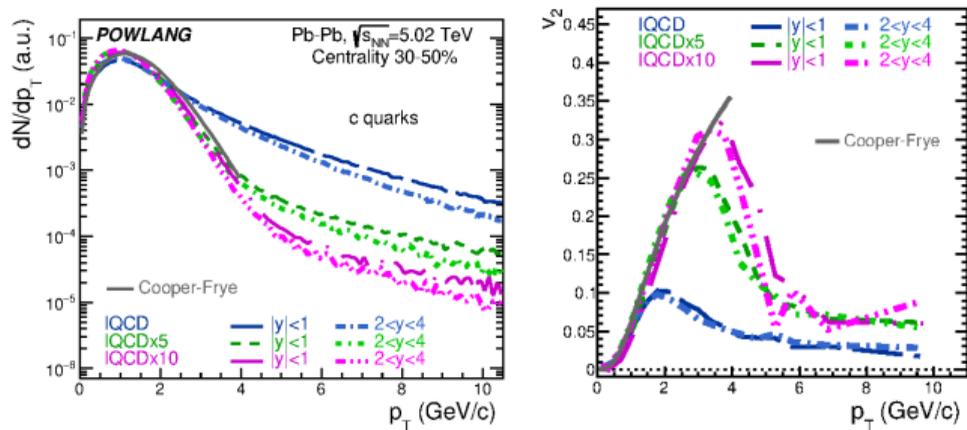


Validation of the model (figures adapted from [Federica Capellino master thesis](#)):

- Left panel: evolution in a static medium
- Right panel: decoupling from expanding medium at $T_{FO} = 160$ MeV

For late times or very large transport coefficients HQ's approach local kinetic equilibrium with the medium. For an expanding medium high- p_T tail remains off equilibrium.

Which information can one extract from the data?



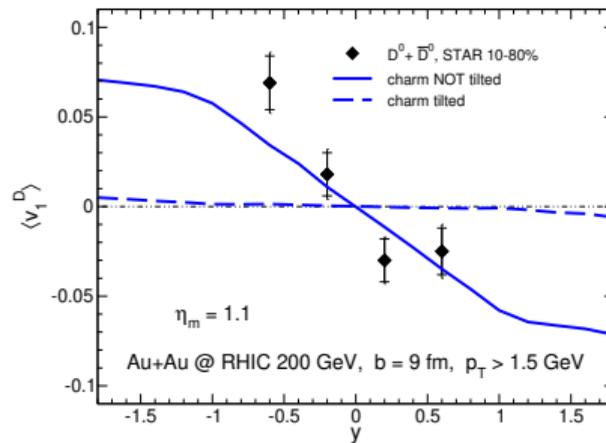
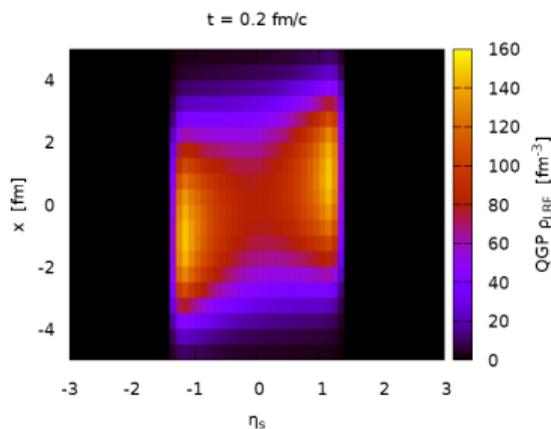
$$D_s \sim \kappa^{-1} \sim \tau_R^{\text{kin}}$$

HQ evolve maximizing the entropy:

- Momentum distribution approaches local kinetic equilibrium $e^{-p \cdot u/T} = e^{-E_p^*/T}$
- Spatial diffusion cancels any local quark-number excess

However, **very efficient kinetic equilibration entails very inefficient spatial equilibration and viceversa.** Can one exploit this to **extract a richer information on transport coefficients from properly chosen observables?**

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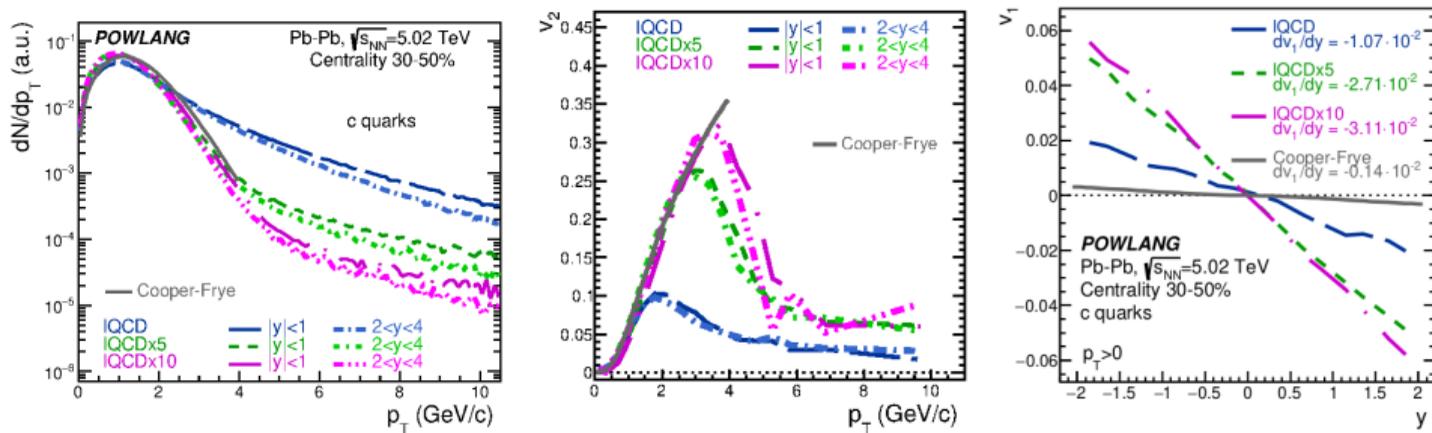


Initial off-equilibrium HQ distribution

- in momentum space: $d\sigma/d\vec{p}_T dy \neq e^{-p \cdot u/T}$
- in coordinate space: $n_{\text{coll}}(\vec{x}_\perp) \neq s_0(\vec{x}_\perp, \eta_s)$

Most studies focused only on approach to *kinetic* equilibrium. However, observables sensitive to **spatial inhomogeneity** of HQ distribution, like the **directed flow** v_1 , can provide a richer information on HF transport coefficients (S. Chatterjee and P. Bozez, PRL 120 (2018) 19, 192301, A.B. et al., JHEP 05 (2021) 279, L. Oliva et al., JHEP 05 (2021) 034)

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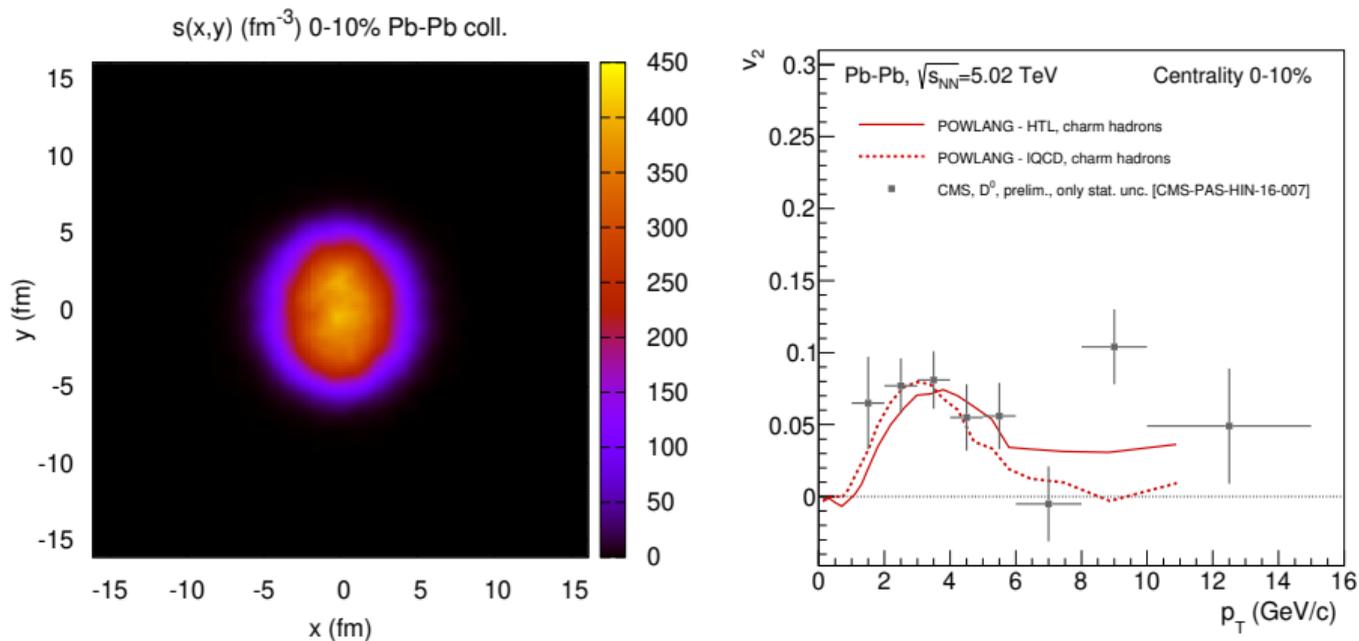


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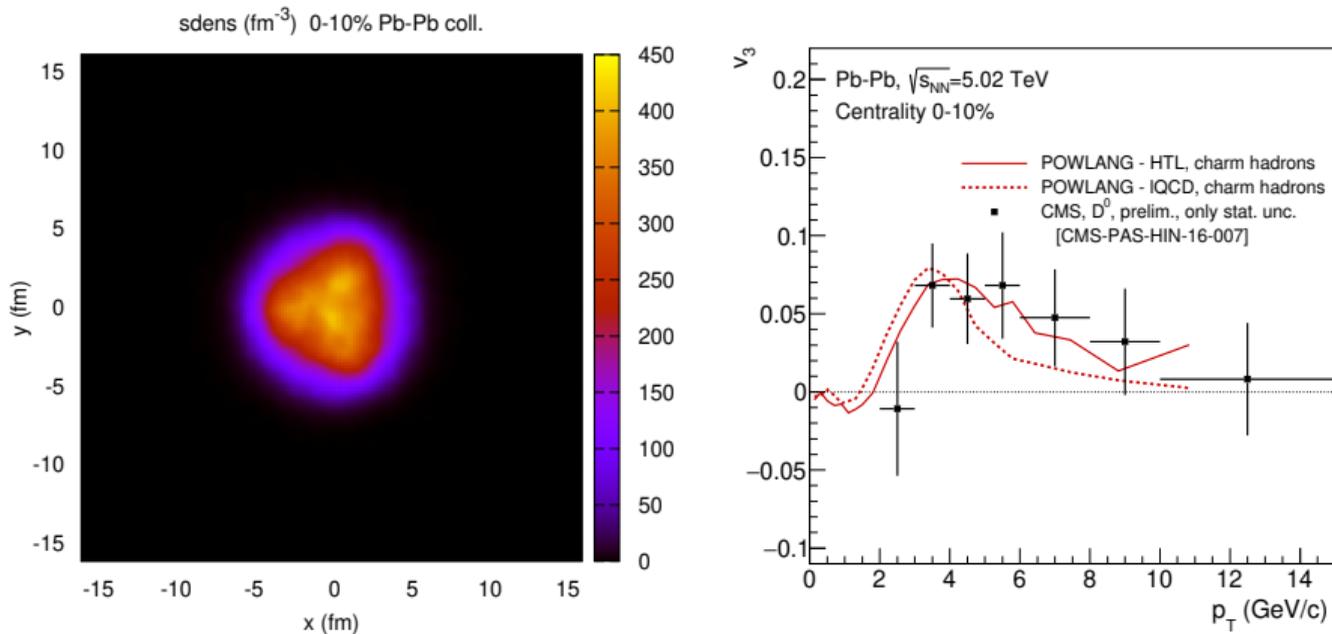
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Some results: D -meson v_2 and v_3 in Pb-Pb



Transport calculations carried out in [JHEP 1802 \(2018\) 043](#), with hydrodynamic background calculated via the [ECHO-QGP code \(EPJC 73 \(2013\) 2524\)](#) starting from [EBE](#) Glauber Monte-Carlo initial conditions: $v_2 \neq 0$ in central collisions, $v_3 \neq 0$

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HQ momentum diffusion: lattice-QCD

From the **non-relativistic limit** of the Langevin equation one gets

$$\frac{dp^i}{dt} = -\eta_D p^i + \xi^i(t), \quad \text{with} \quad \langle \xi^i(t) \xi^j(t') \rangle = \delta^{ij} \delta(t - t') \kappa$$

$$\text{hence} \quad \kappa = \frac{1}{3} \int_{-\infty}^{+\infty} dt \langle \xi^i(t) \xi^i(0) \rangle_{\text{HQ}} = \frac{1}{3} \int_{-\infty}^{+\infty} dt \underbrace{\langle F^i(t) F^i(0) \rangle_{\text{HQ}}}_{\equiv D^>(t)}$$

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From $D_E(\tau)$ one extracts the **spectral density** according to

$$D_E(\tau) = \int_0^{+\infty} \frac{d\omega}{2\pi} \frac{\cosh(\tau - \beta/2)}{\sinh(\beta\omega/2)} \sigma(\omega)$$

The direct extraction of the spectral density from the euclidean correlator

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is a ill-posed problem, since the latter is known for a **limited set** (~ 20) of points $D_E(\tau_i)$, and one wishes to obtain a **fine scan** of the the spectral function $\sigma(\omega_j)$. A direct χ^2 -fit is not applicable.

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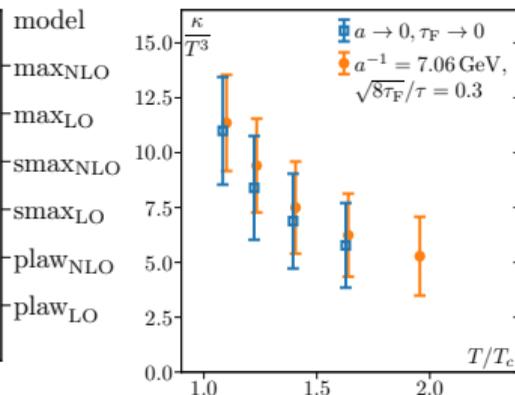
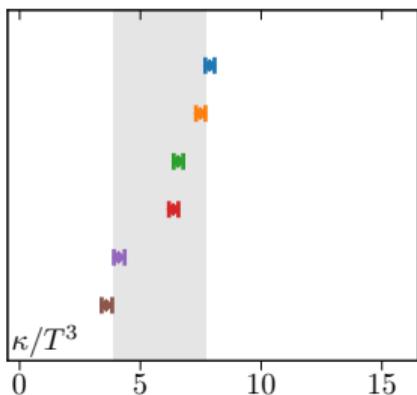
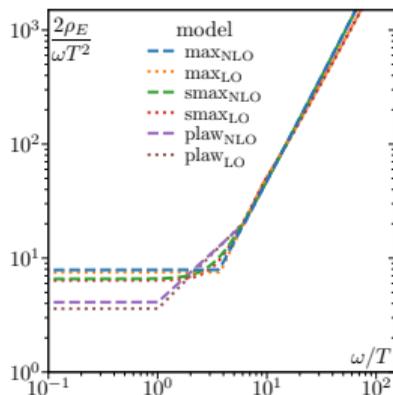
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Possible strategies:

- Bayesian techniques (Maximum Entropy Method)
- Theory-guided ansatz for the behaviour of $\sigma(\omega)$ to constrain its functional form (new results for $N_f=2+1$ [O. Kaczmarek et al., 2302.08501 \[hep-lat\]](#))



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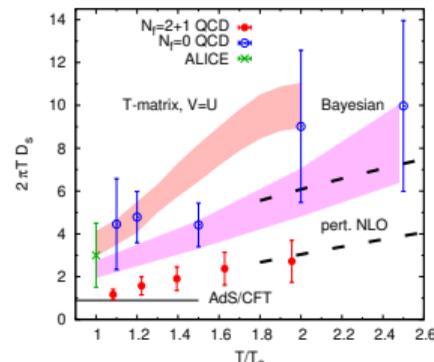
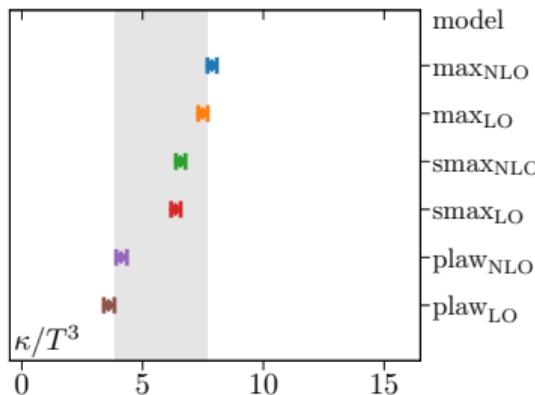
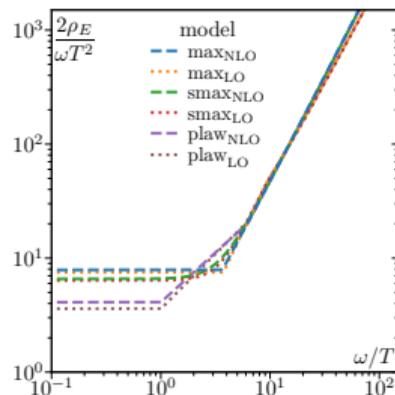
The direct extraction of the spectral density from the euclidean correlator

$$D_E(\tau) = \int_0^{+\infty} \frac{d\omega}{2\pi} \frac{\cosh(\tau - \beta/2)}{\sinh(\beta\omega/2)} \sigma(\omega)$$

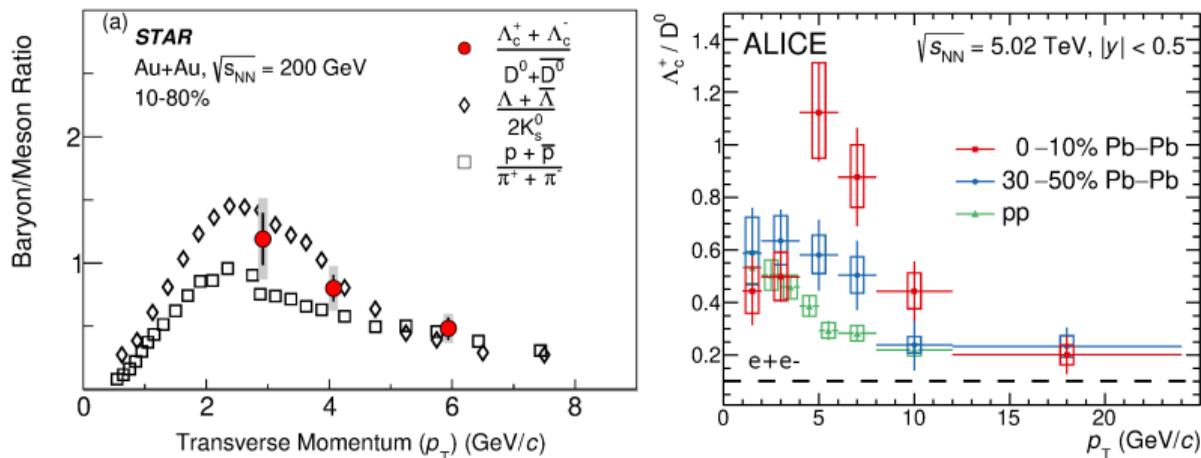
is a ill-posed problem, since the latter is known for a **limited set** (~ 20) of points $D_E(\tau_i)$, and one wishes to obtain a **fine scan** of the the spectral function $\sigma(\omega_j)$. A direct χ^2 -fit is not applicable.

Possible strategies:

- Bayesian techniques (Maximum Entropy Method)
- Theory-guided ansatz for the behaviour of $\sigma(\omega)$ to constrain its functional form (new results for $N_f=2+1$ [O. Kaczmarek et al., 2302.08501 \[hep-lat\]](#))

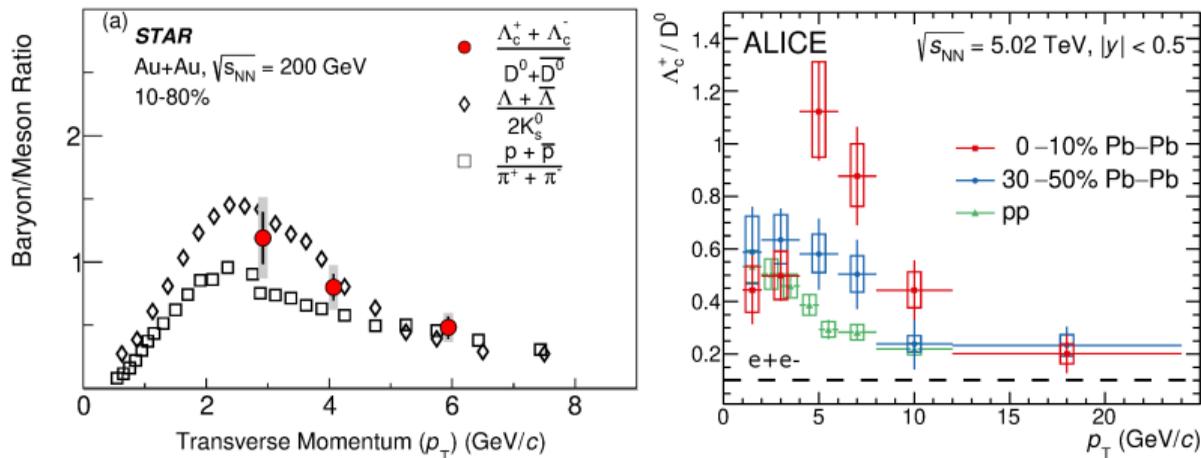


HF hadronization: experimental findings



Strong **enhancement of charmed baryon/meson ratio**, incompatible with hadronization models tuned to reproduce e^+e^- data

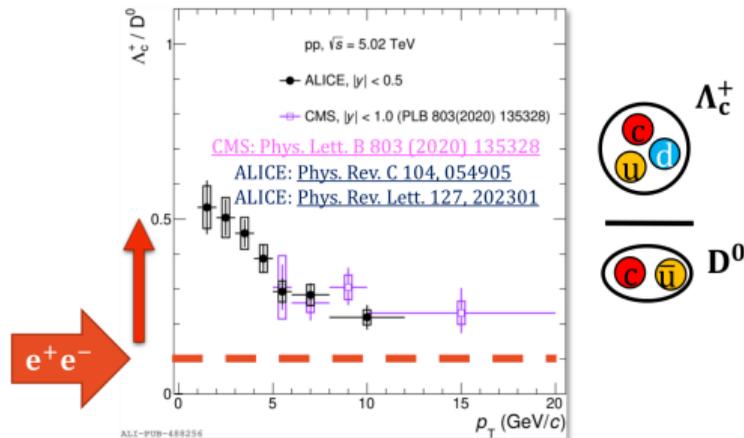
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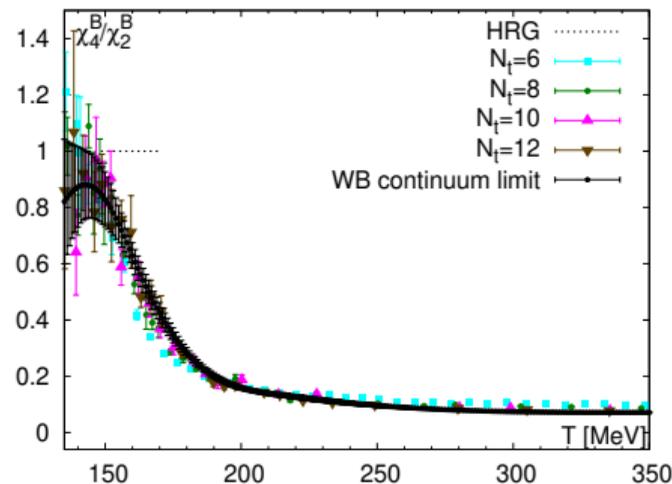
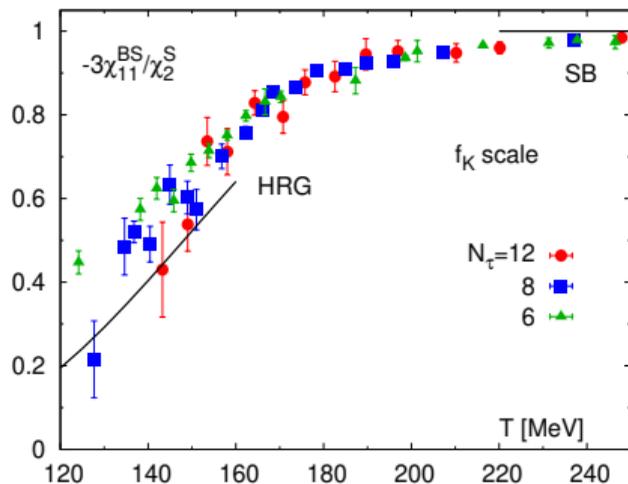


Strong **enhancement of charmed baryon/meson ratio**, incompatible with hadronization models tuned to reproduce e^+e^- data

- pattern similar to light hadrons
- baryon **enhancement observed also in pp collisions**: is a dense medium formed also there?
Breaking of factorization description in pp collisions

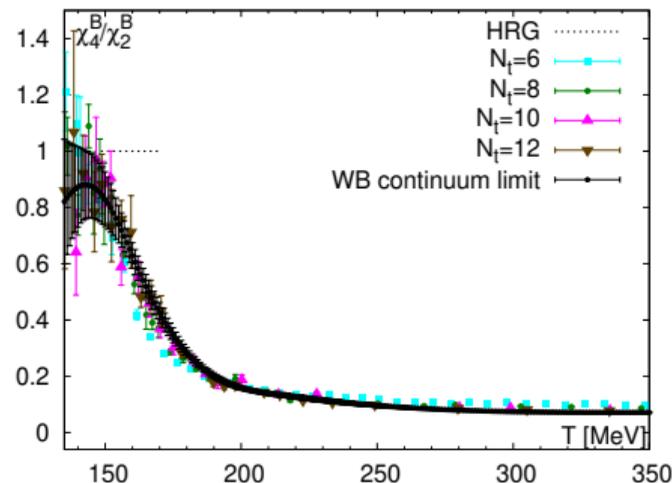
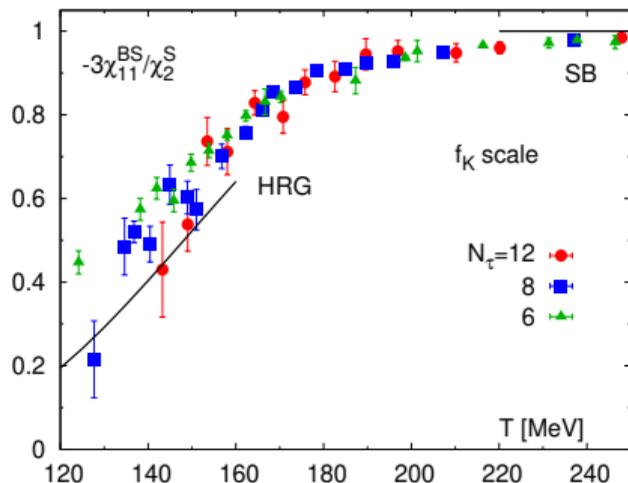
$$d\sigma_h \neq \sum_{a,b,X} f_a(x_1) f_b(x_2) \otimes d\hat{\sigma}_{ab \rightarrow c\bar{c}X} \otimes D_{c \rightarrow h_c}(z)$$

Premise: which are the carriers of conserved charges?



- In the QGP strangeness carried by quarks with $|B|=1/3$, PRD 86, 034509 (2012)
- $\chi_4^B/\chi_2^B = B^2$, with $|B|=1$ (HG) or $|B|=1/3$ (QGP), PRL 111, 062005 (2013)

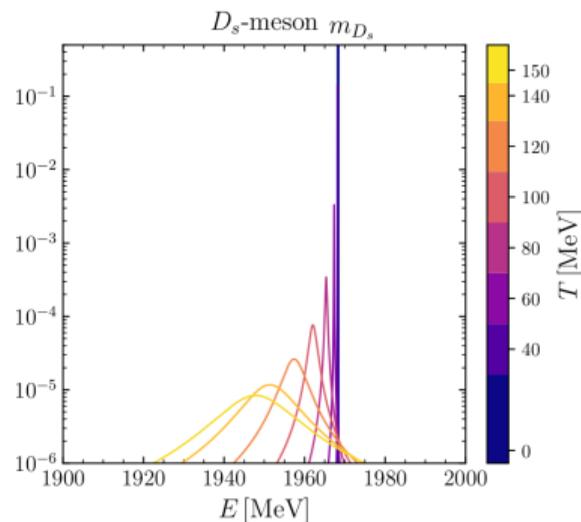
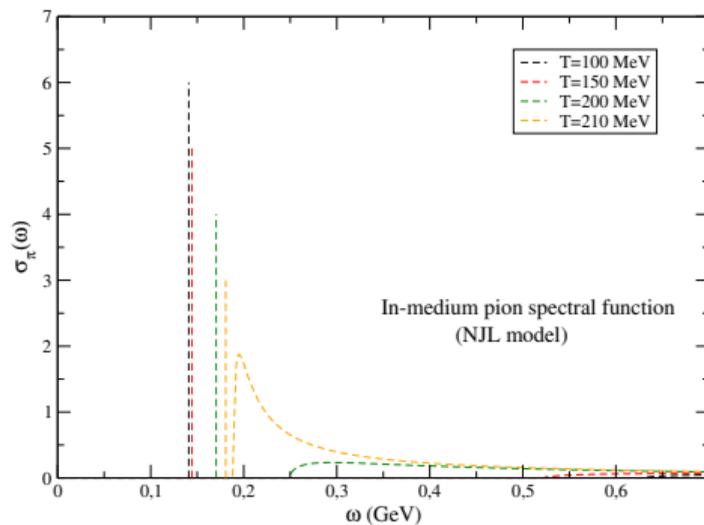
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One would expect a sharp change in the nature of these carriers...
However, IQCD data show that also this change is **very smooth!**

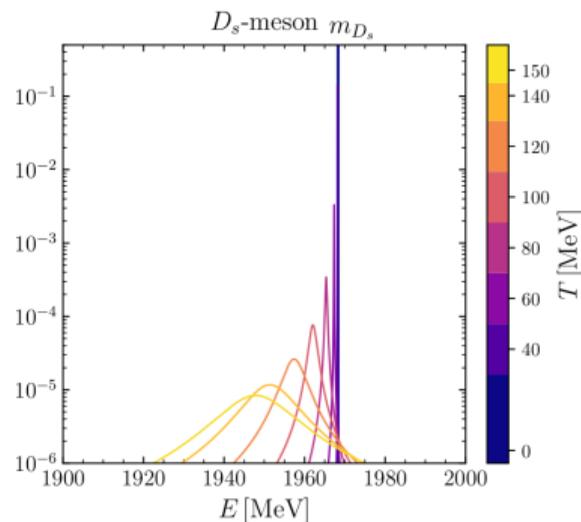
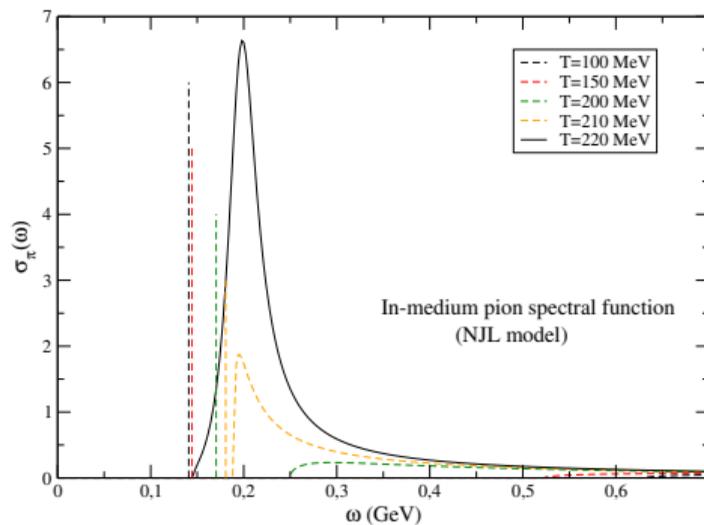
What is a hadron around the QCD crossover?



- At $T=0$ hadrons are **stable eigenstates of H_{QCD}**
- At $T \neq 0$ effective Lagrangians predict **much richer structure of hadronic spectral functions** (broadening, mass shift), both for light (NJL model) and heavy (non-linear chiral $SU(3)$ model) hadrons¹

¹G. Montana et al., PLB 806 (2020)

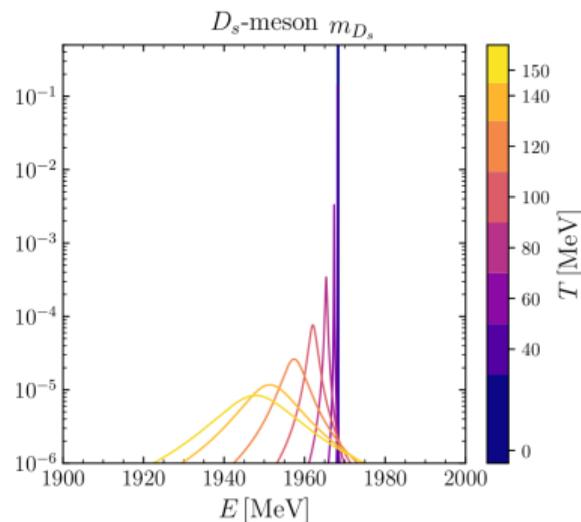
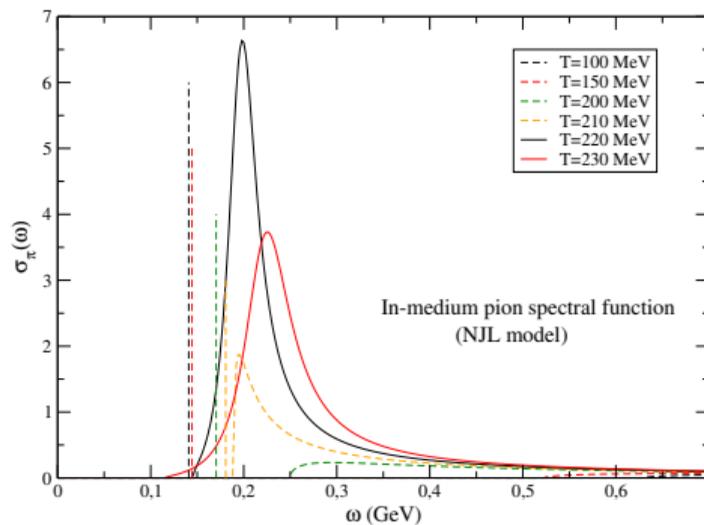
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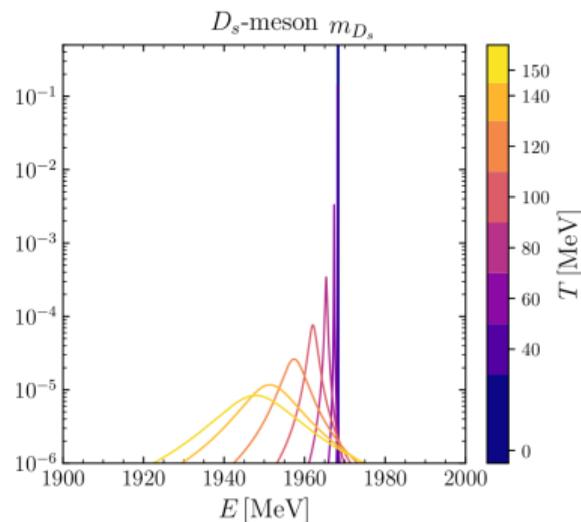
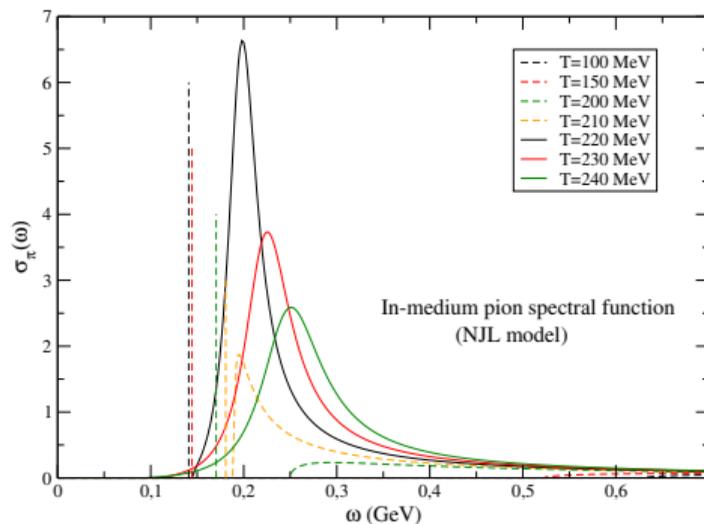
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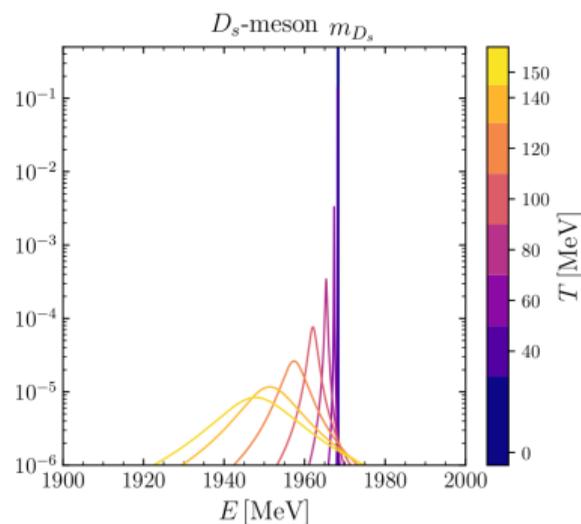
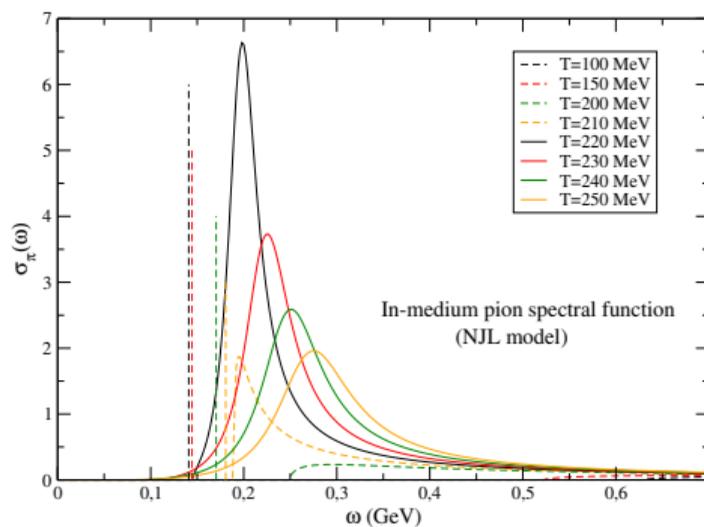
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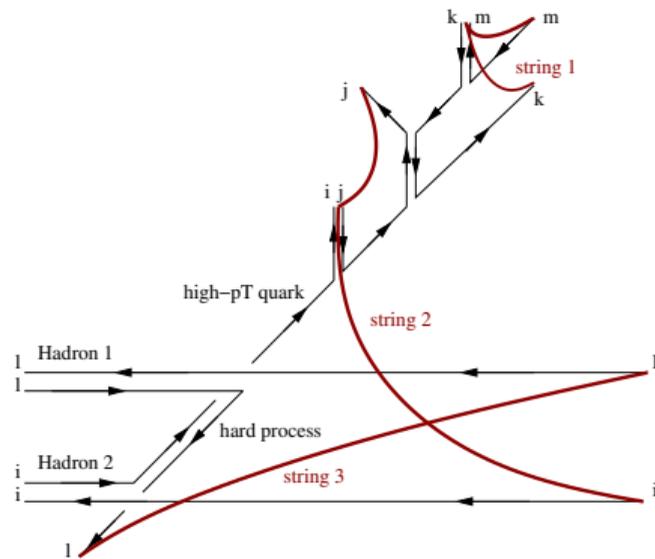
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Grouping colored partons into color-singlet structures: strings (PYTHIA), clusters (HERWIG), hadrons/resonances (coalescence).

Hadronization models: common features

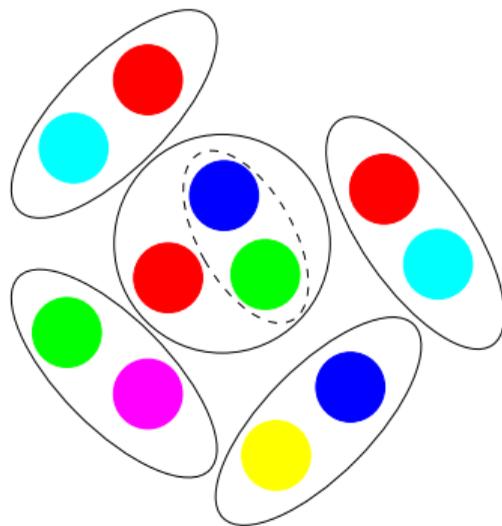
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- in “elementary collisions”: from the hard process, shower stage, underlying event and beam remnants;

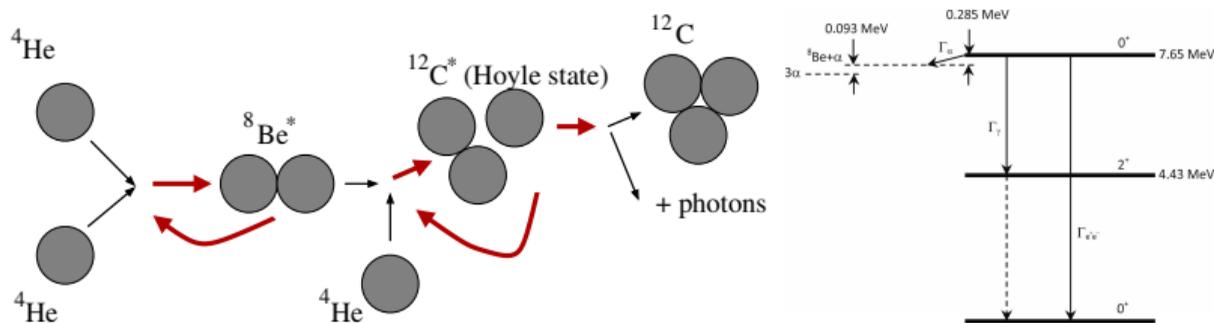
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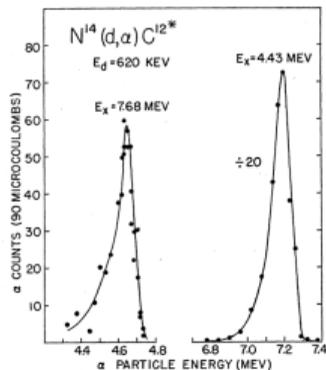
- in “elementary collisions”: from the hard process, shower stage, underlying event and beam remnants;
- in heavy-ion collisions: from the hot medium produced in the collision. NB Involved **partons closer in space** in this case and this has deep consequence!

A warning from nucleosynthesis



- Final yields in **stellar nucleosynthesis** *extremely sensitive* to **existence of excited states just above threshold** (not a simple $N \rightarrow 1$ process);

A warning from nucleosynthesis



PRL 106, 192501 (2011) Selected for a Viewpoint in Physics
PHYSICAL REVIEW LETTERS week ending
13 MAY 2011

Ab Initio Calculation of the Hoyle State

Evgeny Epelbaum,¹ Hermann Krebs,¹ Dean Lee,² and Ulf-G. Meißner^{3,4}

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²Department of Physics, North Carolina State University, Raleigh, North Carolina 27695, USA

³Helmholtz-Institut für Strahlen- und Kernphysik and Bethe Center for Theoretical Physics,
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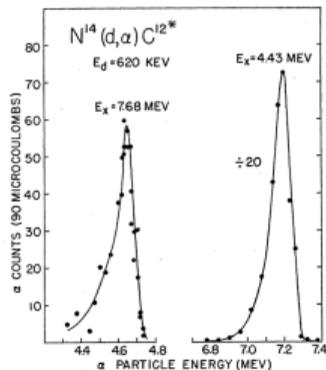
⁴Institut für Kernphysik, Institute for Advanced Simulation and Jülich Center for Hadron Physics,
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(Received 24 February 2011; published 9 May 2011)

The Hoyle state plays a crucial role in the helium burning of stars heavier than our Sun and in the production of carbon and other elements necessary for life. This excited state of the carbon-12 nucleus was postulated by Hoyle as a necessary ingredient for the fusion of three alpha particles to produce carbon at stellar temperatures. Although the Hoyle state was seen experimentally more than a half century ago nuclear theorists have not yet uncovered the nature of this state from first principles. In this Letter we report the first *ab initio* calculation of the low-lying states of carbon-12 using supercomputer lattice simulations and a theoretical framework known as effective field theory. In addition to the ground state and excited spin-2 state, we find a resonance at $\sim 85(3)$ MeV with all of the properties of the Hoyle state and in agreement with the experimentally observed energy.

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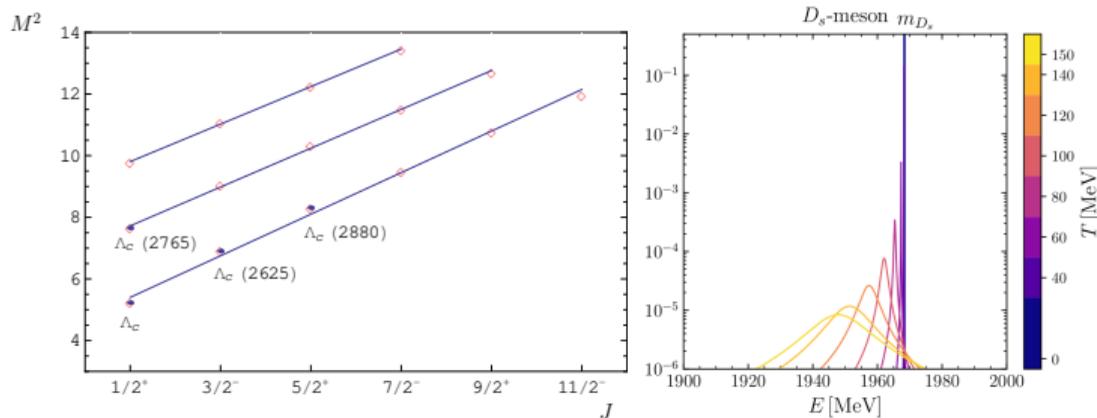
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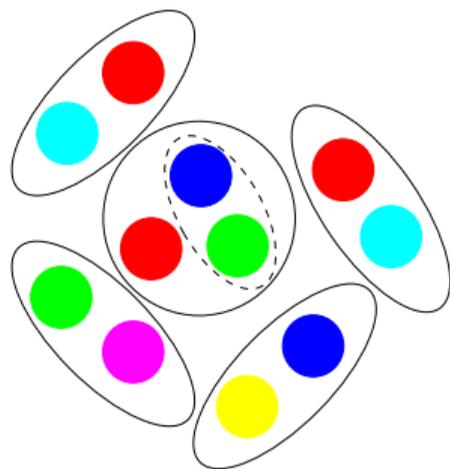
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None of the above conditions is fully under control in the quark to hadron transition: PDG states $<$ RQM states (D. Ebert *et al.*, PRD 84, 014025 (2011)), what is a hadron around T_c ?

Local Color Neutralization (LCN): basic ideas

Both in AA and pp collision a **big/small deconfined fireball** is formed. Around the QCD crossover temperature quarks undergoes **recombination with the *closest* opposite color-charge** (antiquark or diquark).

- Why? screening of color-interaction, **minimization of energy stored in confining potential**
- Implication: recombination of particles *from the same fluid cell* → **Space-Momentum Correlation (SMC)**, recombined partons tend to share a common collective velocity



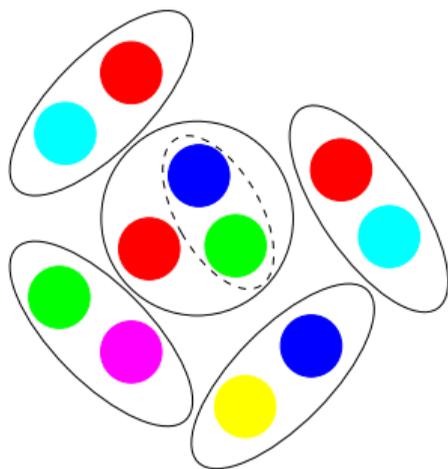
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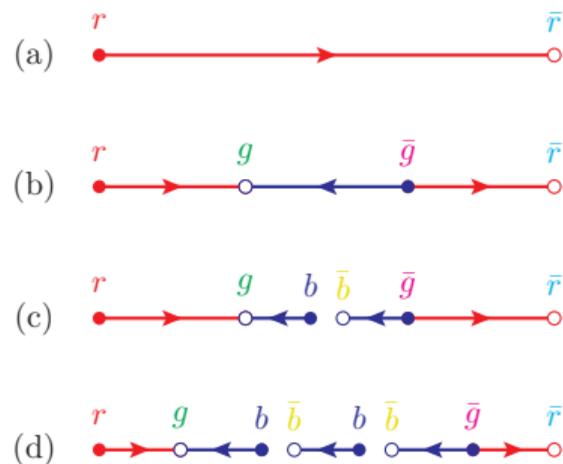
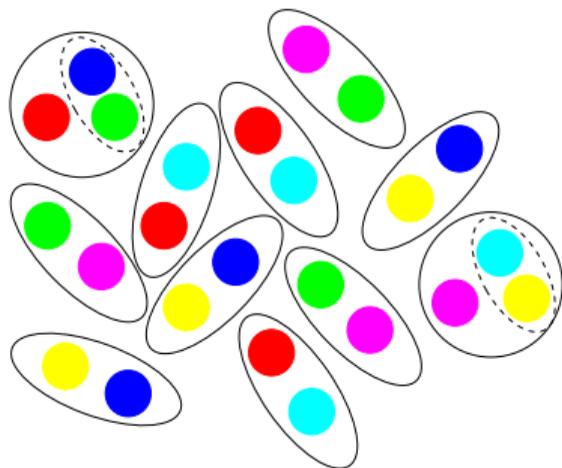
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Color-singlet structures are thus formed, eventually undergoing **decay into the final hadrons**: $2 \rightarrow 1 \rightarrow N$ process, usually a **charmed hadron plus a very soft particle**

- Exact four-momentum conservation;
- No direct bound-state formation, hence no need to worry about overlap between the final hadron and the parent parton wave-functions



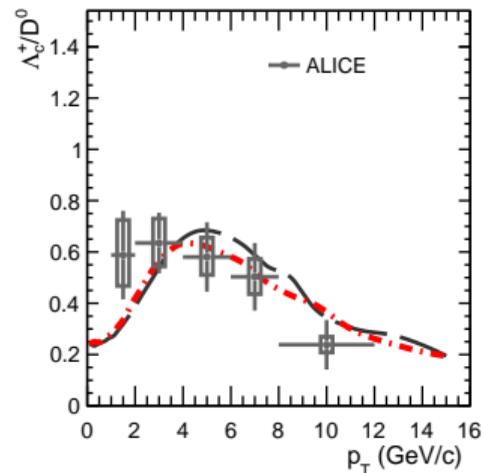
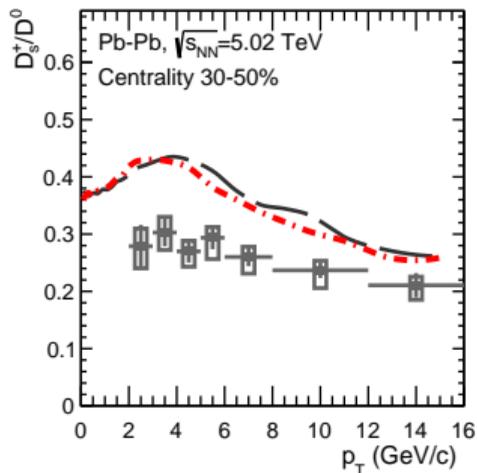
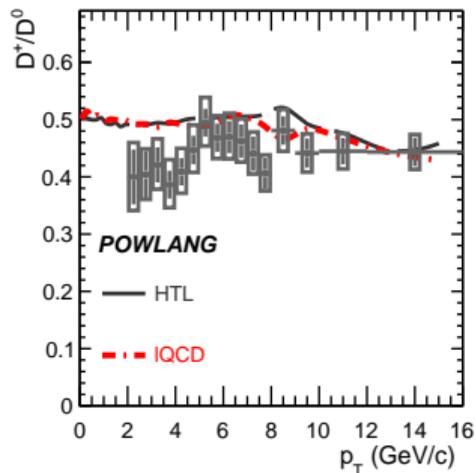
Implementation of global conservation laws



- In **LCN** and similar *recombination approaches* baryon number (and other charges as well) can be **conserved over a very large volume**;
- On the other hand in **PYTHIA string-breaking** (and possibly pop-corn) mechanism **charge conservation occurs locally**²

²L. Lonnblad and H. Shah, EPJC 83 (2023) 12, 1105

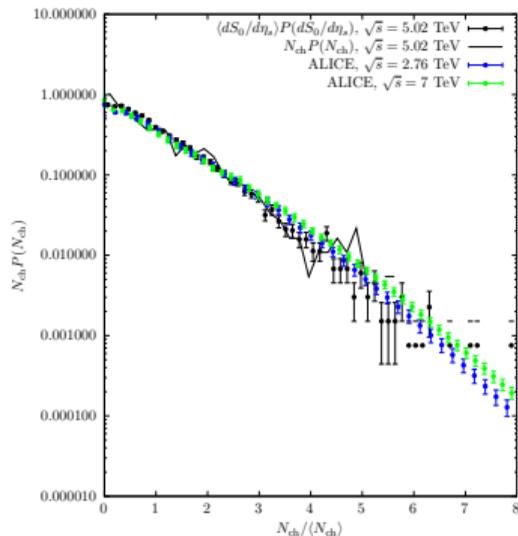
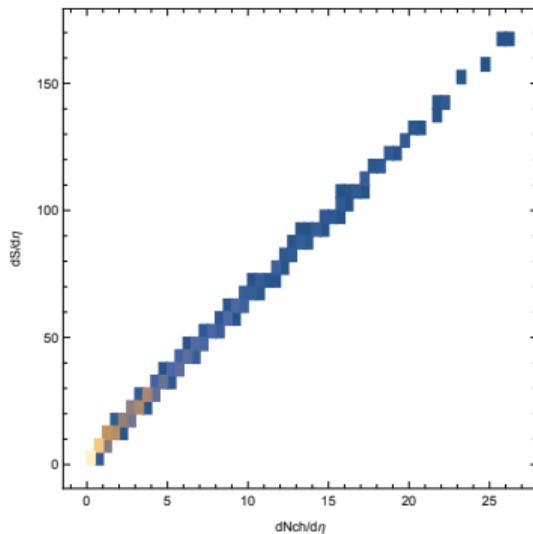
Results in AA collisions



- Enhanced HF baryon-to-meson ratios up to intermediate p_T nicely reproduced, thanks to formation of *small invariant-mass charm+diquark clusters*
- Smooth approach to e^+e^- limit ($\Lambda_c^+/D^0 \approx 0.1$) at high p_T : high- M_c clusters fragmented as Lund strings, as in the vacuum

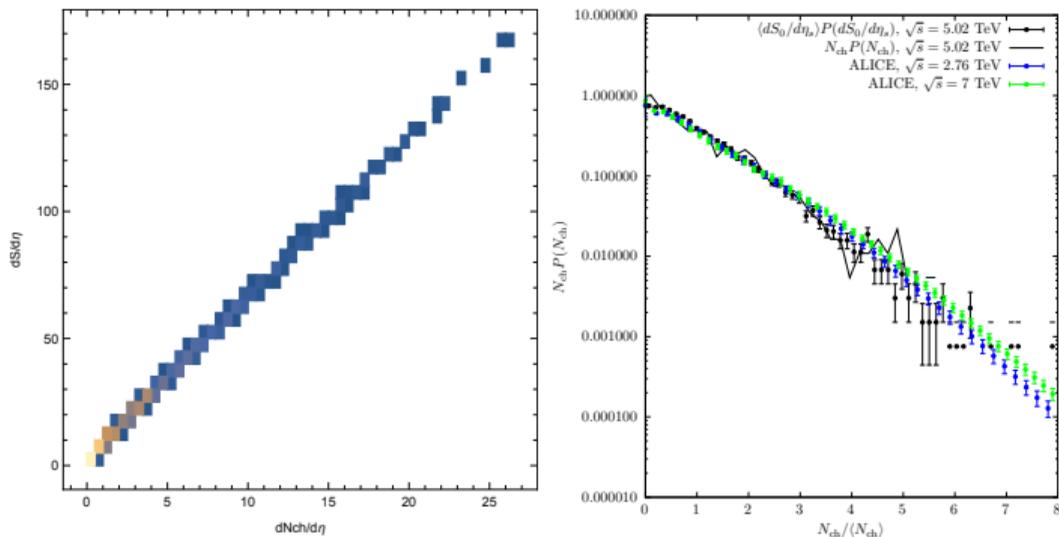
For more details see [A.B. et al., EPJC 82 \(2022\) 7, 607.](#)

Addressing pp collisions...



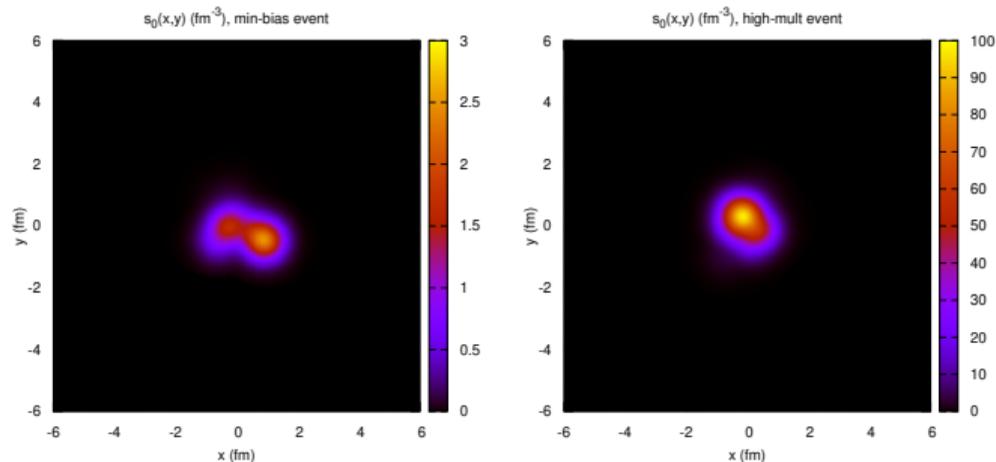
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Addressing pp collisions...



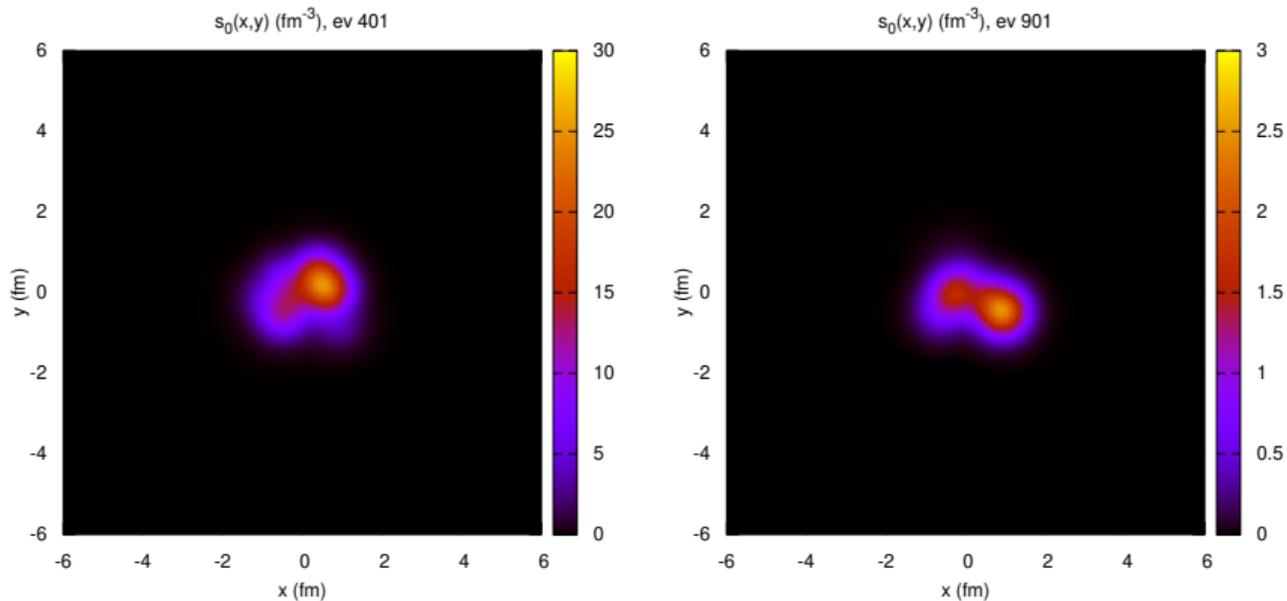
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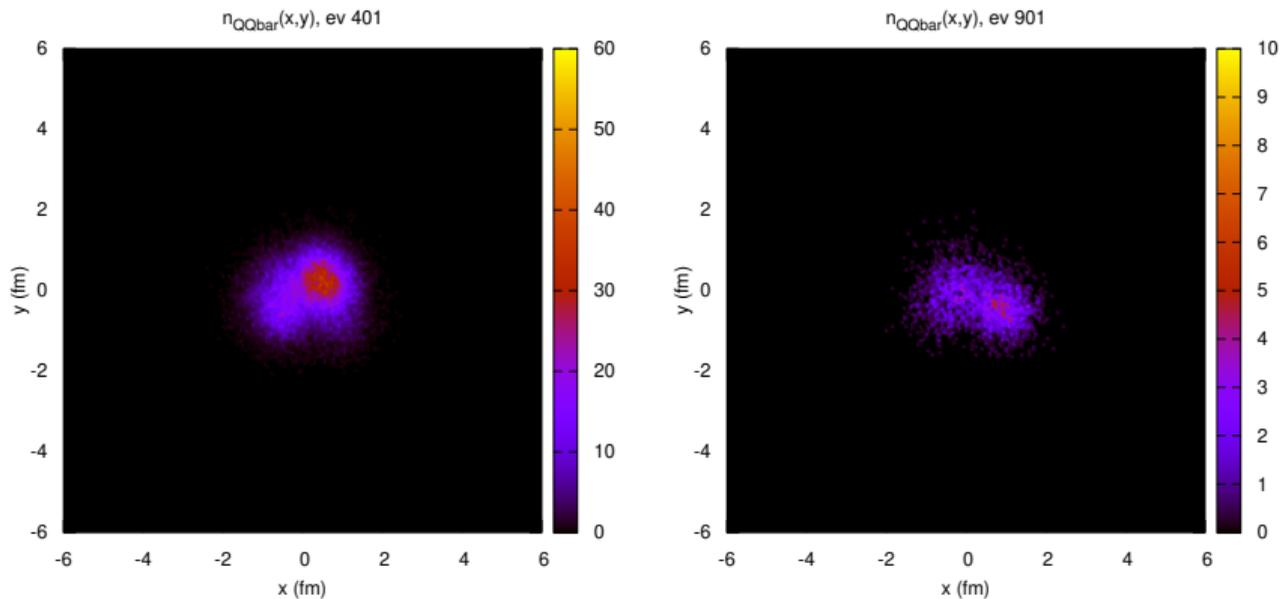
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- Samples of 10^3 minimum-bias ($\langle dS/dy \rangle_{\text{mb}} \approx 37.6$, tuned to experimental $\langle dN_{\text{ch}}/d\eta \rangle$) and high-multiplicity ($\langle dS/dy \rangle_{0-1\%} \approx 187.5$) events used to simulate HQ transport and hadronization.

Why in-medium hadronization also in pp?



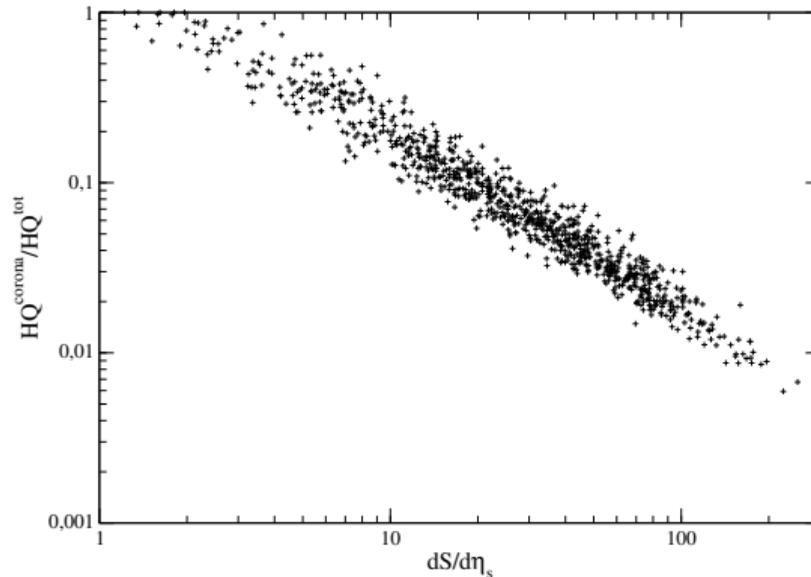
$Q\bar{Q}$ production biased towards hot spots of highest multiplicity events

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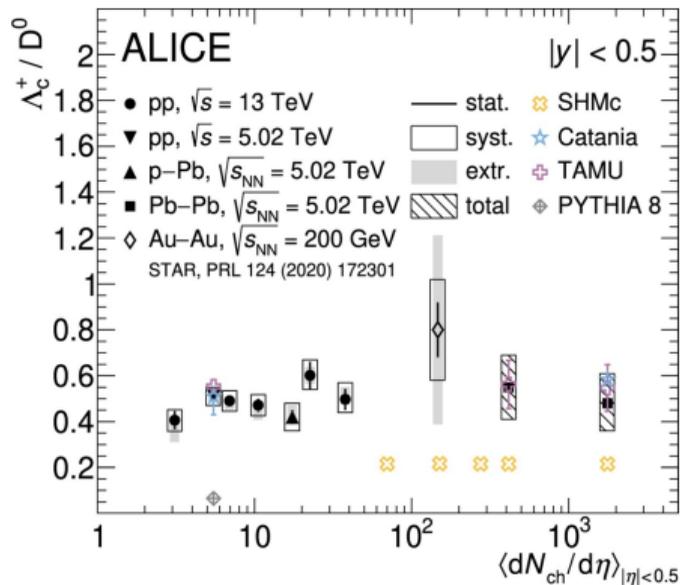
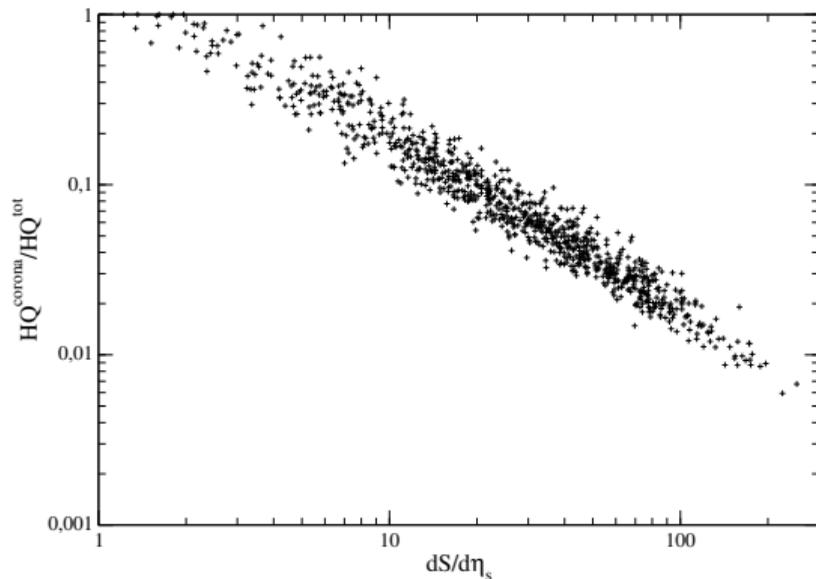
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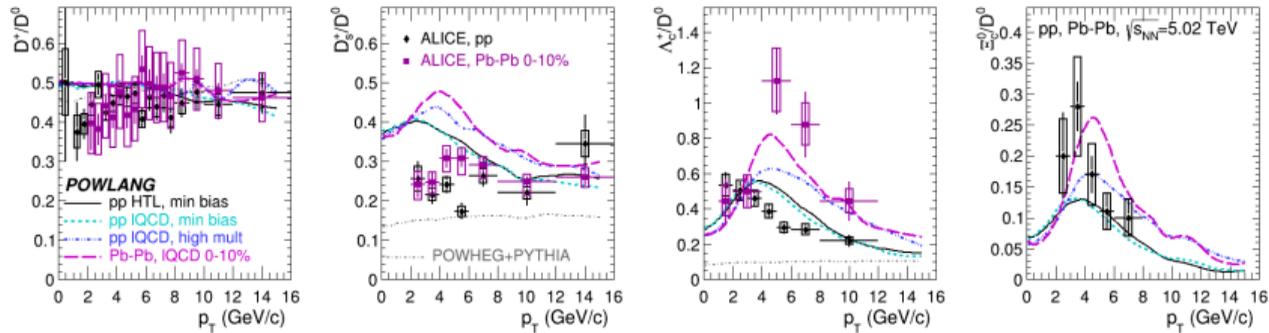
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Why in-medium hadronization also in pp?



$Q\bar{Q}$ production biased towards **hot spots of highest multiplicity events** \rightarrow only about 5% of $Q\bar{Q}$ pairs initially found in fluid cells below T_c . Studies of **charmed-hadron production in low-multiplicity pp events** of great interest! Would one recover the e^+e^- fragmentation fractions?

Results in pp: particle ratios

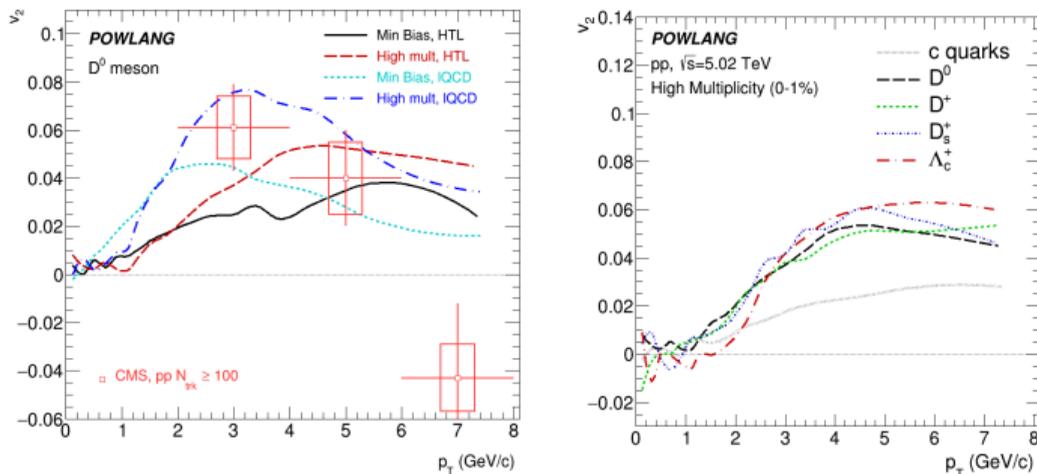


First results for particle ratios³:

- POWHEG+PYTHIA standalone strongly underpredicts baryon-to-meson ratio
- Enhancement of charmed baryon-to-meson ratio qualitatively reproduced if propagation+hadronization in a small QGP droplet is included
- Multiplicity dependence of radial-flow peak position (just a reshuffling of the momentum, without affecting the yields): $\langle u_{\perp} \rangle_{pp}^{mb} \approx 0.33$, $\langle u_{\perp} \rangle_{pp}^{hm} \approx 0.53$, $\langle u_{\perp} \rangle_{PbPb}^{0-10\%} \approx 0.66$

³In collaboration with D. Pablos, A. De Pace, F. Prino et al., Phys.Rev.D 109 (2024) 1, L011501

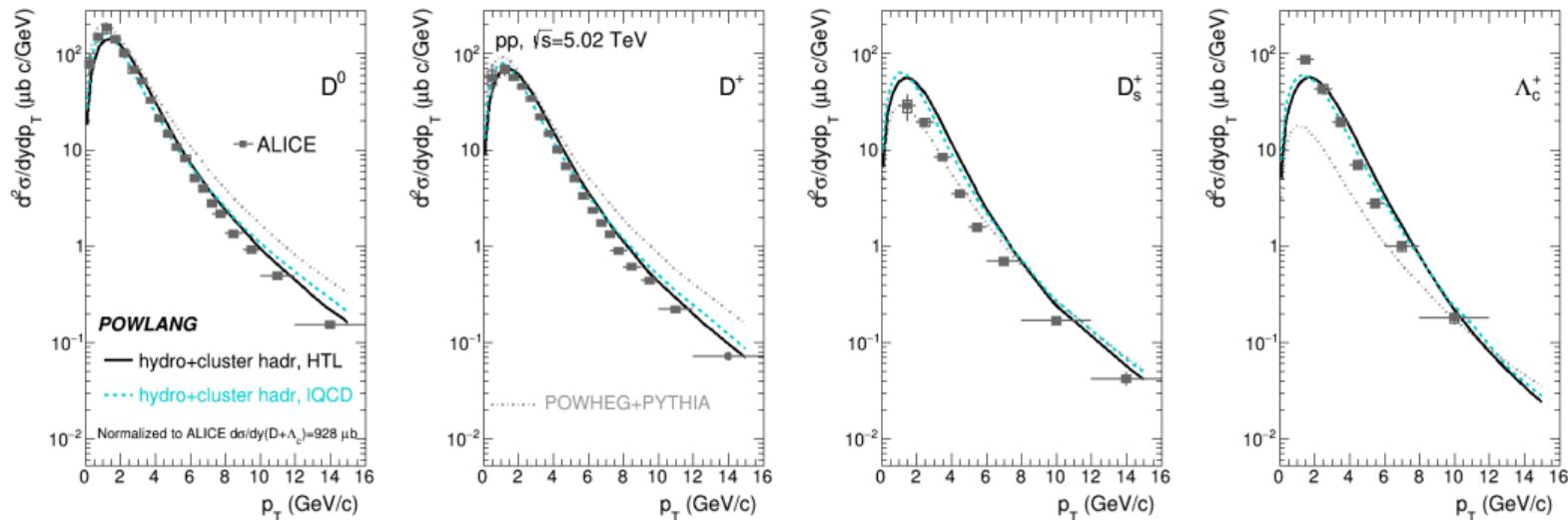
Results in pp: elliptic flow



Response to **initial elliptic eccentricity** ($\langle \epsilon_2 \rangle^{\text{mb}} \approx \langle \epsilon_2 \rangle^{\text{mh}} \approx 0.31$) \longrightarrow **non-vanishing v_2 coefficient**

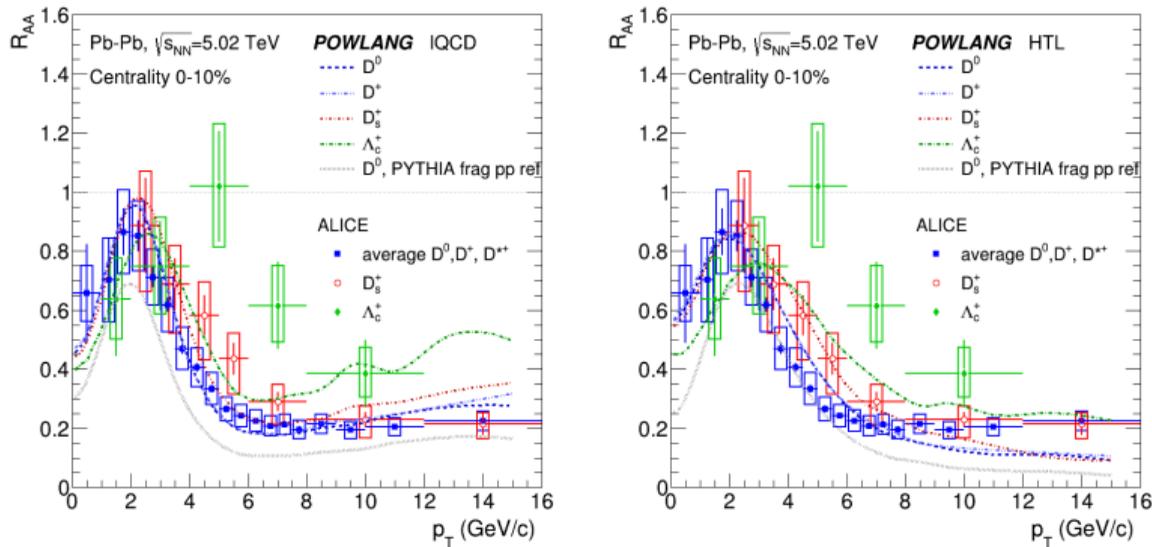
- Differences between minimum-bias and high-multiplicity results only due to longer time spent in the fireball ($\langle \tau_H \rangle^{\text{mb}} \approx 1.95$ fm/c vs $\langle \tau_H \rangle^{\text{hm}} \approx 2.92$ fm/c)
- Mass ordering at low p_T ($M_{qq} > M_q$)
- **Sizable fraction of v_2 acquired at hadronization**

Relevance to quantify nuclear effects



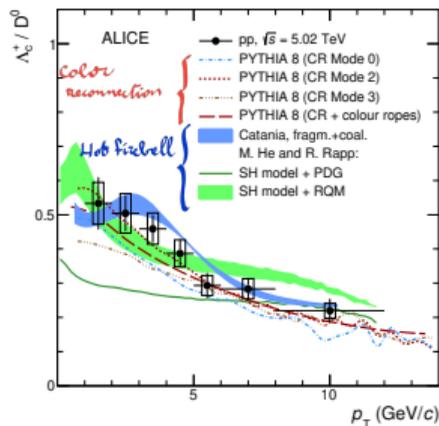
- Slope of the spectra in pp collisions better described including medium effects

Relevance to quantify nuclear effects



- Slope of the spectra in pp collisions better described including medium effects
- Inclusion of **medium effects in minimum-bias pp benchmark** fundamental to better describe **charmed hadron R_{AA}** , both the **radial-flow peak** and the **species dependence**

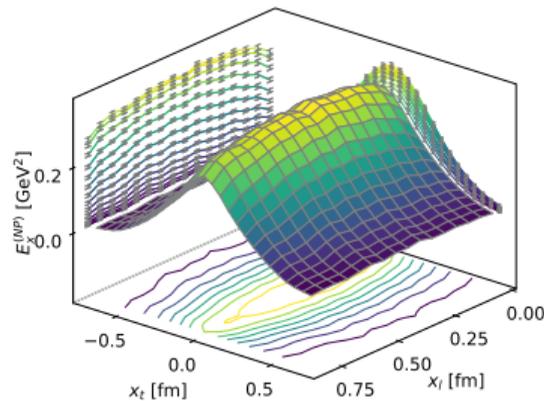
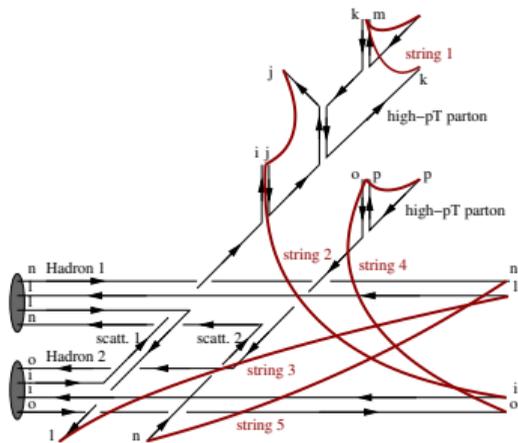
Looking for alternative (?) explanations: Color Reconnection (CR)



Charmed baryon enhancement in pp collisions can be accounted for *either* assuming the formation of a **small fireball** *or*, in **PYTHIA**, introducing the possibility of **color-reconnection** (CR).

⁴M. Baker et al., EPJC 80 (2020) 6, 514; C. Bierlich et al., EPJC 84 (2024) 3, 231

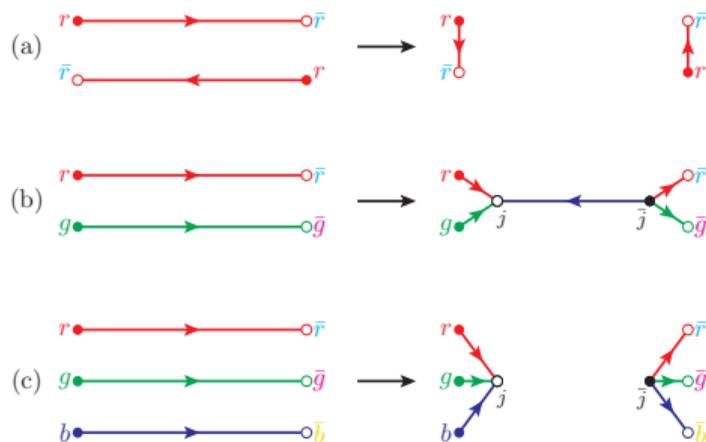
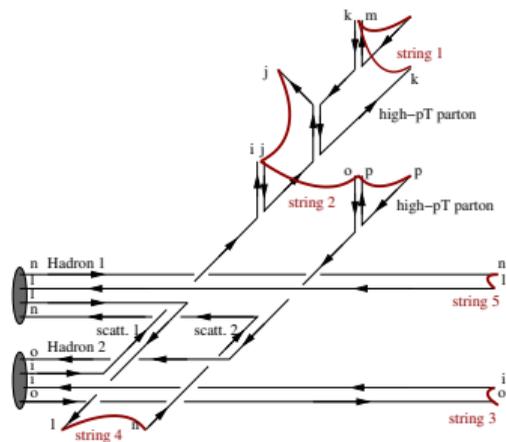
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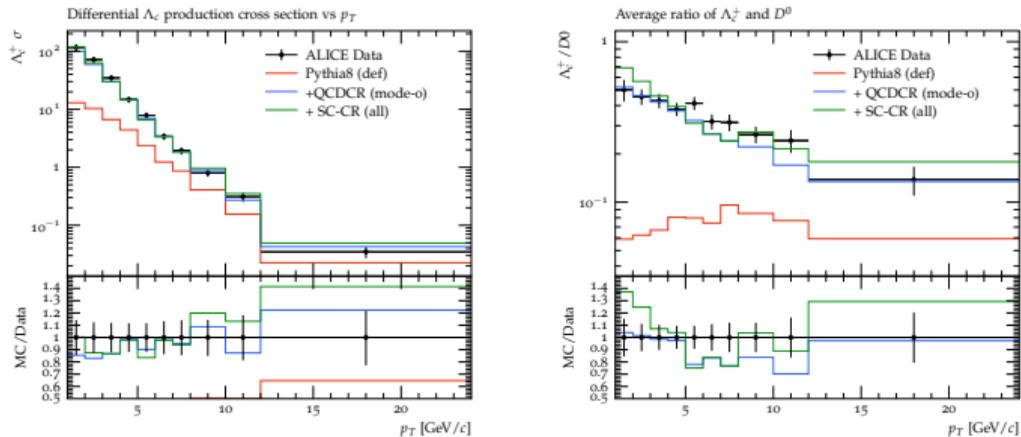
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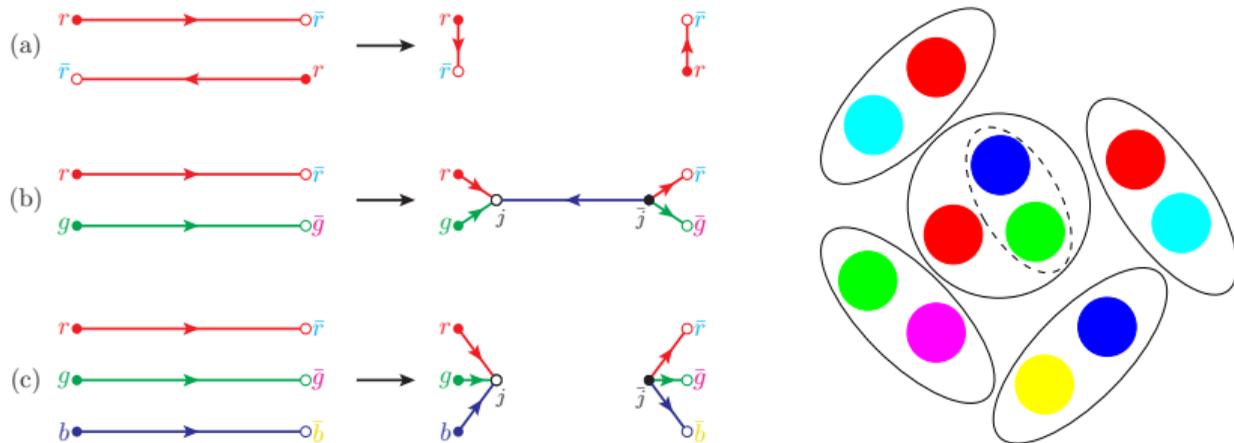
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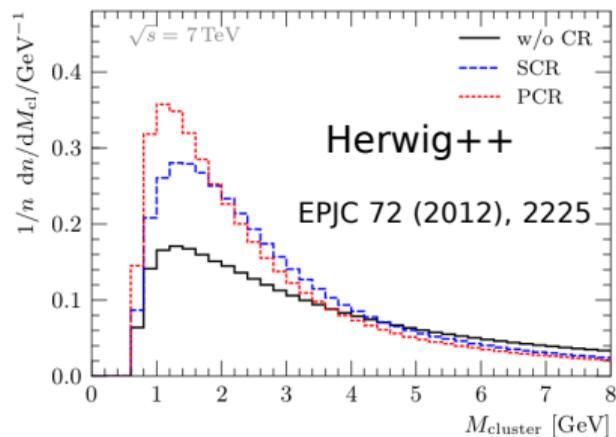
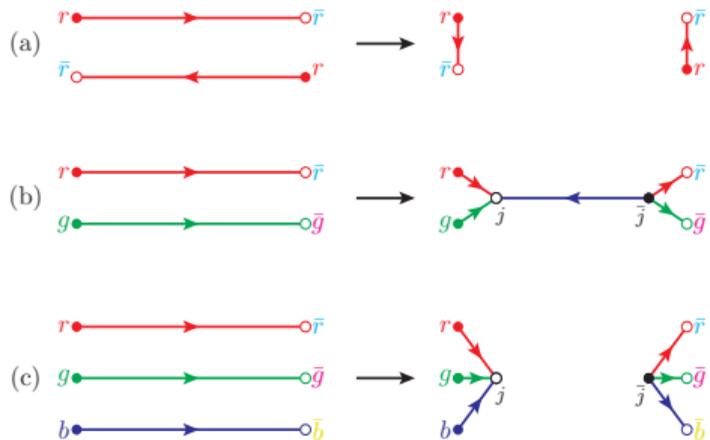
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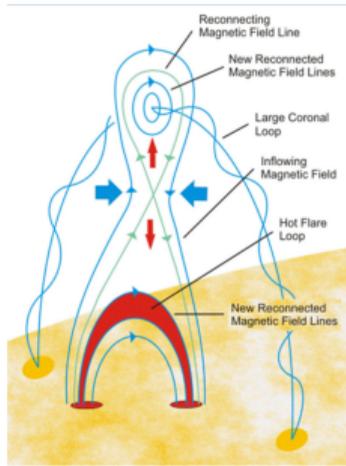
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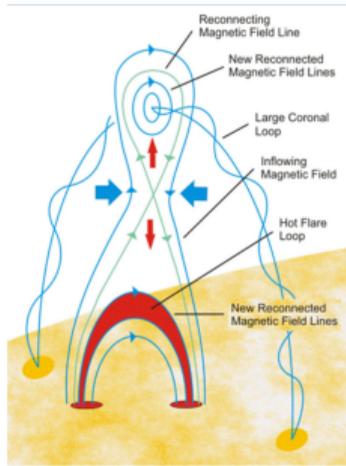
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Most violent phenomena astrophysical phenomena associated to **magnetic reconnections**: sudden **conversion of energy stored in the B-field into kinetic energy of the plasma particles**

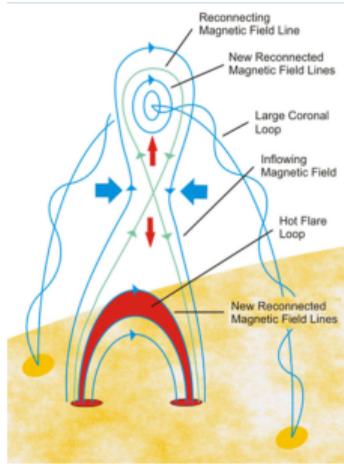
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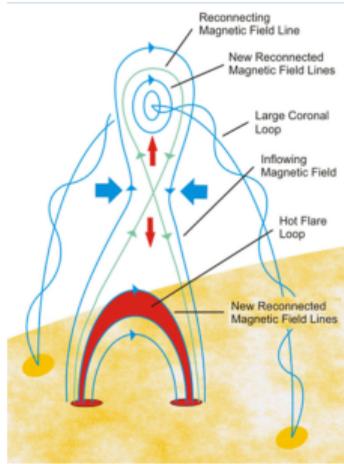
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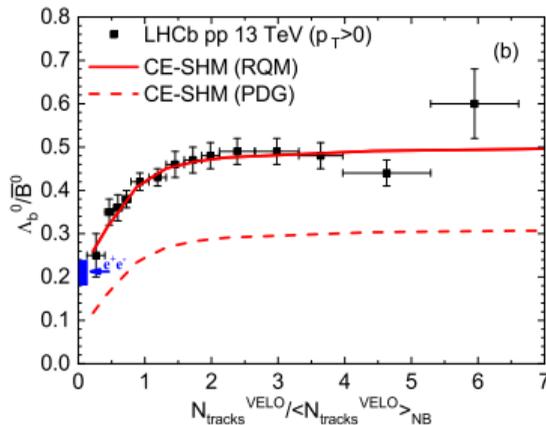
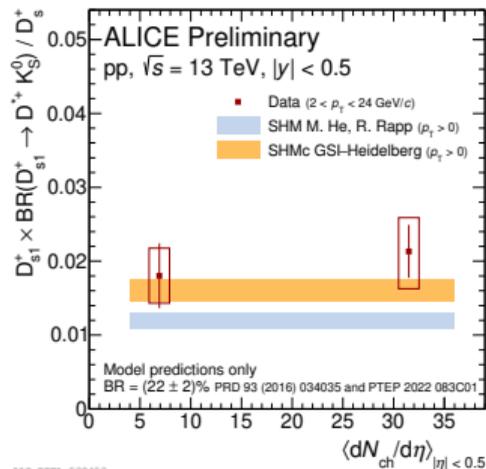


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Is CR possible without the formation of a QGP with *finite color conductivity*?

HF statistical hadronization

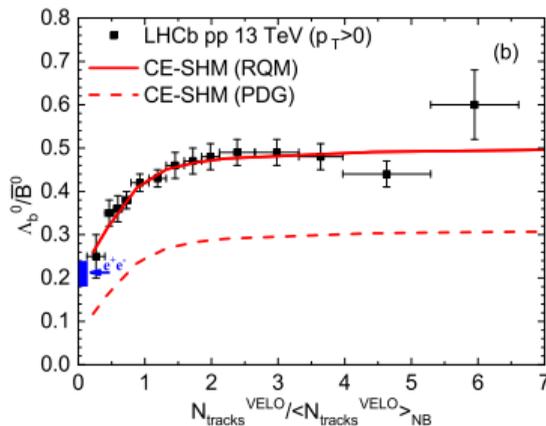
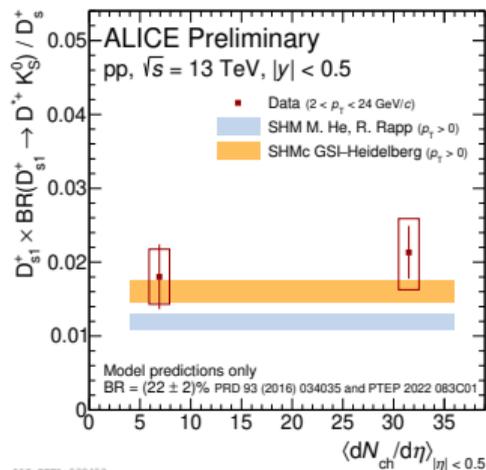


$$Z(\vec{Q}) = \int_0^{2\pi} \frac{d^5\phi}{(2\pi)^5} e^{i\vec{Q}\cdot\vec{\phi}} \exp\left[\sum_j \gamma_s^{N_{sj}} \gamma_c^{N_{cj}} \gamma_b^{N_{bj}} e^{-i\vec{q}_j\cdot\vec{\phi}} z_j\right], \quad \text{with} \quad z_j = (2J_j + 1) \frac{VT_H}{2\pi^2} m_j^2 K_2\left(\frac{m_j}{T_H}\right)$$

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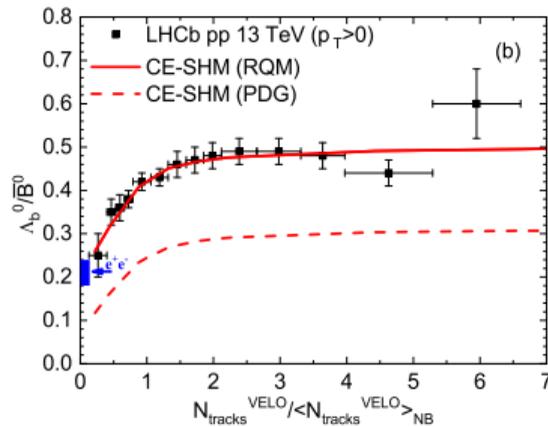
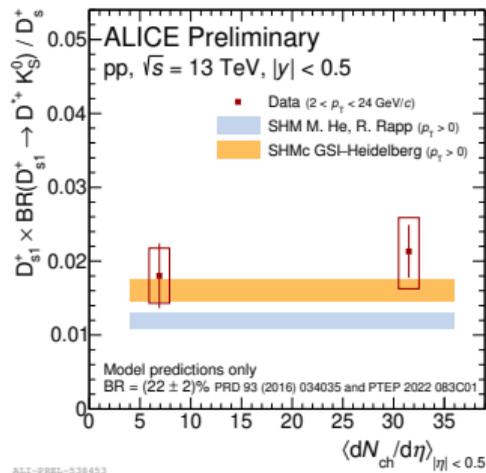


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