

# Report on LNS **theory group (GR4)** activity

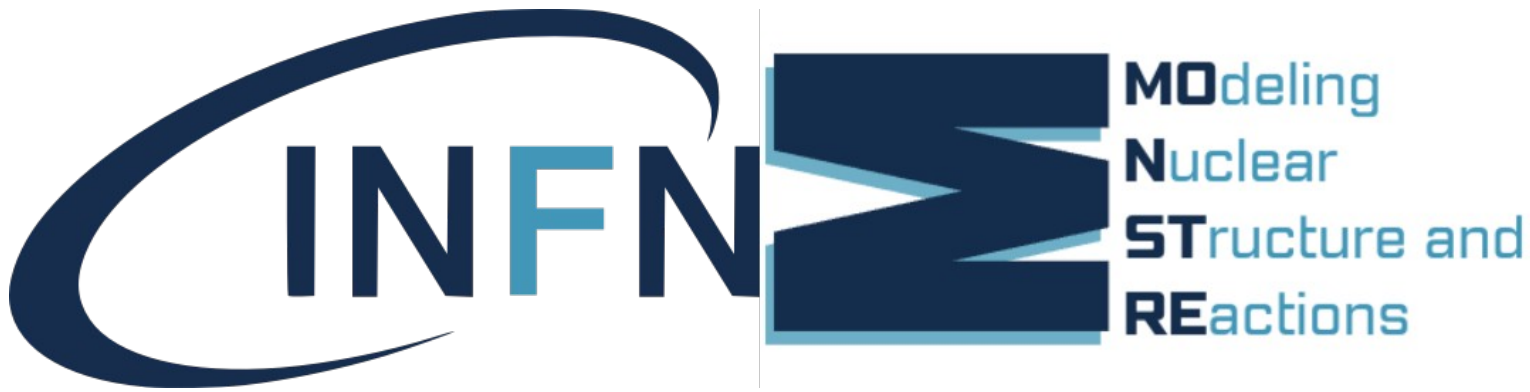


**Danilo Gambacurta**  
Laboratori Nazionali del Sud (Catania)

Presentazione Attività e Preventivi 2024  
18 e 19 Luglio 2024

## **Iniziative Specifiche di CSN4:**

- MONSTRE
- SIM



# MONSTRE

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*Unità: LNS, Bologna, CT, Milano, Padova, Trento*  
*FTE totale: ≈30, FTE (LNS) ≈4.5*

**Responsabile Nazionale:** Danilo Gambacurta (LNS)

**Responsabile Locale:** Maria Colonna

Collaborazioni: LNS+CT (Chimera, Medea, NUMEN, ASFIN), Firenze, Napoli, Genova, IPN-Orsay, GANIL, GSI, Monaco, Bucharest, Giessen, Darmstadt, Siviglia, MSU, Pechino, Lanzhou, Rio de Janeiro, RIKEN, ...

# Obiettivi generali:

Modeling nuclear structure and reaction properties

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## Four WorkPackages (WPs)

- **WP1: *Ab initio* many body methods for nuclei and nuclear matter:** increasing the accuracy and predictive power
- **WP2: Advanced theoretical studies of nuclear phenomena:** addressing the experimental challenges
- **WP3: Nuclear matter under extreme conditions:** from nuclear dynamics to compact objects
- **WP4: Emerging computational technologies:** quantum information and machine learning techniques

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# LNS Activities: Nuclear Structure Studies

## Theoretical Models and Techniques

- ✓ **Energy Density Functional Framework (Skyrme, Gogny, Covariant)**
- ✓ **Ground state: HF, HF+BCS, HFB**
- ✓ **Excited states: RPA, QRPA, Second RPA, TDHF**
- ✓ **Transport theories based on EDF**
- ✓ **Extending models: including clusters d.o.f. , short range correlations, bridge with ab-initio theories, ...**

## Main Physical Cases of Interest

- ✓ **Collective nuclear excitations, especially in neutron-rich and exotic nuclei**  
(Giant Resonances, Pygmy Dipole Resonance, ...)
- ✓ **EoS of asymmetric matter (symmetry energy, ...)**
- ✓ **Charge exchange excitations (Gamow-Teller, Fermi, etc,) and Beta Decay (single and double)**
- ✓ **Interdisciplinary aspects between nuclear and neutrino physics**

# LNS activities: Nuclear Reaction Studies

## Theoretical Models and Techniques

- ✓ *Semi-classical transport theories, incorporating many-body correlations*
- ✓ *DWBA and/or coupled channel calculations*
- ✓ *Formulation of scattering theories and methods*

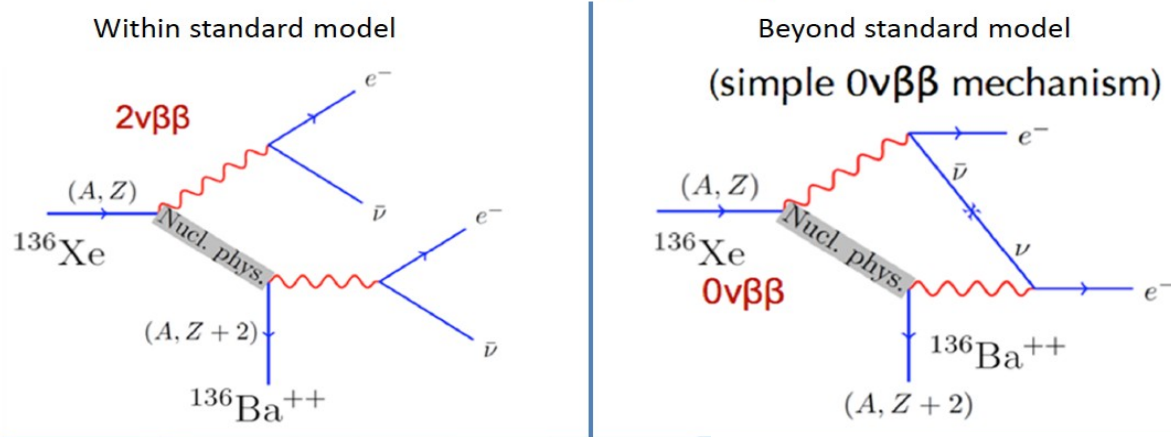
## Main Physical Cases of Interest

- ✓ *Nuclear reactions at Fermi/intermediate energies*
- ✓ *Direct reaction (transfer, charge exchange, probing spin-isospin channels)*
- ✓ *Fragmentation reactions, also for medical applications*
- ✓ *Impact of Eos on nuclear reactions*
- ✓ *Double Charge Excitations and the connection to double beta decay*
- ✓ *Reactions for astrophysical studies (light systems, cluster structure)*

# Theoretical part of NUMEN project (Resp. M. Colonna)

For *single charge exchange (SCE)* Nuclear Reactions are a well tested approach to probe single  $\beta$  decay... MAGNEX at LNS allow to access *double charge exchange (DCE)*

## Double $\beta$ -decay



$$T_{\beta\alpha}^{(2)} = \langle \chi_p^{(-)} | (b | V_{res} G_c V_{res} | a) | \chi_d^{(+)} \rangle =$$

**Double**

$$= \sum_c \int \frac{d^3k}{(2\pi)^3} \langle \chi_p^{(-)} | (b | V_{res} | c) | \chi_d^{(+)} \rangle \cdot \frac{1}{\epsilon_2 - \epsilon_1 + i\eta}$$

**Single**

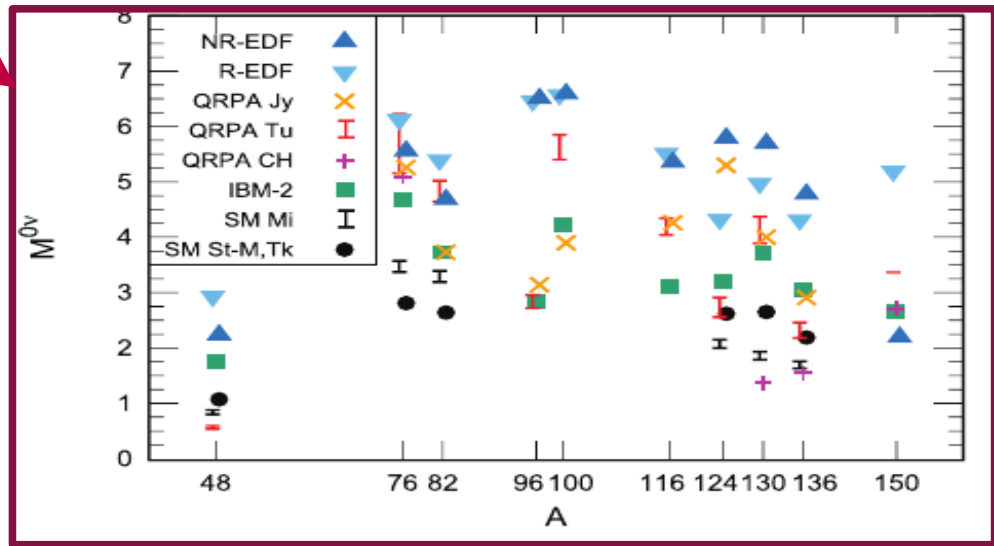
$$\cdot \langle \tilde{\chi}_y^{(+)} | (c | V_{res} | a) | \chi_d^{(+)} \rangle \quad \text{Single}$$

$$1/T_{\frac{1}{2}}^{0\nu}(0^+ \rightarrow 0^+) = G_{0\nu} |M^{\beta\beta 0\nu}|^2 \left| \frac{\langle m_\nu \rangle}{m_e} \right|^2$$

**Nuclear Matrix Element (NME)!**

$$|M_\epsilon^{\beta\beta 0\nu}|^2 = \left| \langle \Psi_f | \hat{O}_\epsilon^{\beta\beta 0\nu} | \Psi_i \rangle \right|^2$$

- ➔ Modellizzazione meccanismo di reazione
- ➔ Sviluppo di Codici numerici
- ➔ Multi-Channel approach
- ➔ Modelli di struttura nucleare per meccanismi SCE/DCE





*Article*



## Theory of Majorana-Type Heavy Ion Double Charge Exchange Reactions by Pion–Nucleon Isotensor Interactions

Horst Lenske <sup>1,\*</sup>, Jessica Bellone <sup>2,†</sup>, Maria Colonna <sup>2,†</sup> and Danilo Gambacurta <sup>2,†</sup>



*Article*

## Induced Isotensor Interactions in Heavy-Ion Double-Charge-Exchange Reactions and the Role of Initial and Final State Interactions

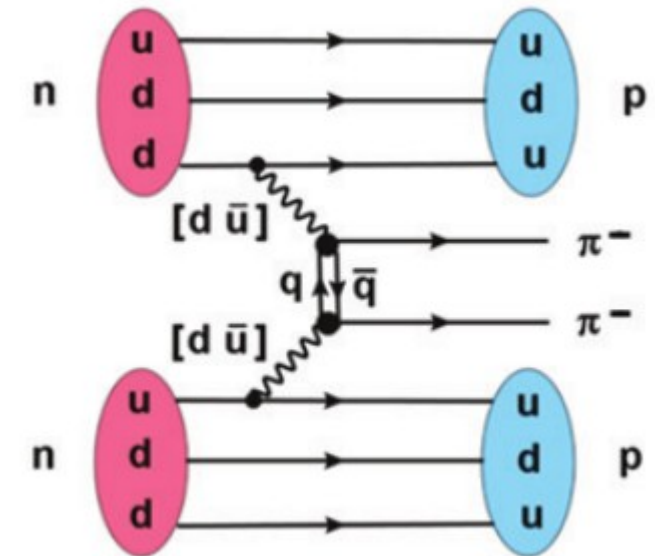
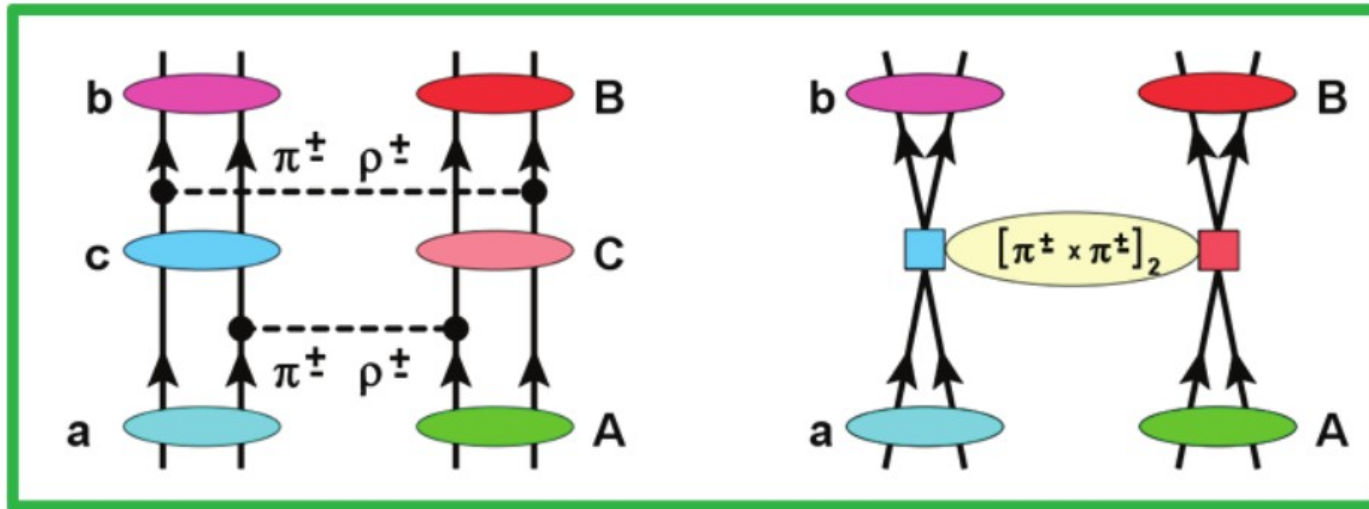
Horst Lenske <sup>1,\*</sup>, Jessica Bellone <sup>2,†</sup>, Maria Colonna <sup>2,†</sup>, Danilo Gambacurta <sup>2,†</sup> and José-Antonio Lay <sup>3,4,†</sup>



The role of **initial state (ISI)** and **final state (FSI)** ion–ion interactions for double single-charge-exchange (DSCE) reactions has been investigated.

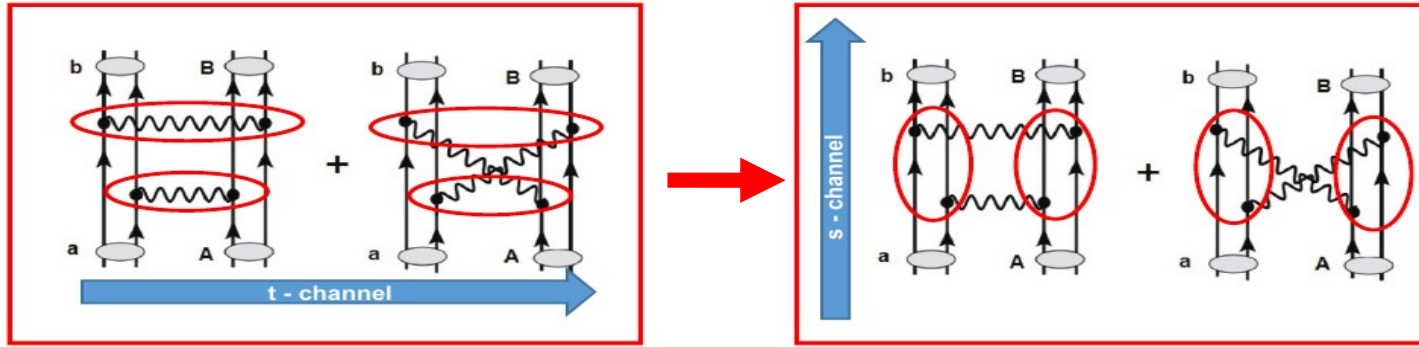
Virtual pion–nucleon charge exchange interactions are investigated as the source for induced isotensor interactions, giving rise to the **Majorana DCE (MDCE) reactions** in the projectile and target nucleus.

**Connections to neutrinoless Majorana double beta decay (MDBD)** are also discussed at various levels of the dynamics, from the underlying fundamental electro-weak and QCD scales to the physical scales of nuclear MDBD and MDCE physics.



**Figure 1.** Schematic representation of the collisional processes contributing to a DCE reaction  $A(Z, N) \rightarrow B(Z \pm 2, N \mp 2)$ . The DSCE reaction scenario of second-order in the isovector NN T-matrix (left) competes with the direct MDCE mechanism proceeding by an isotensor interaction induced by off-shell pion–nucleon DCE scattering.

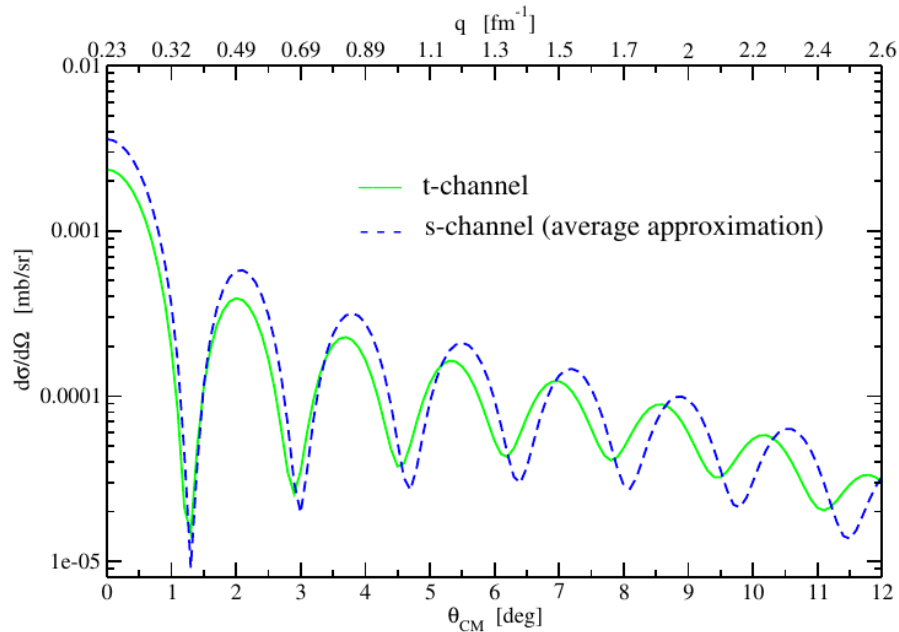
# From t- to s-channel representation



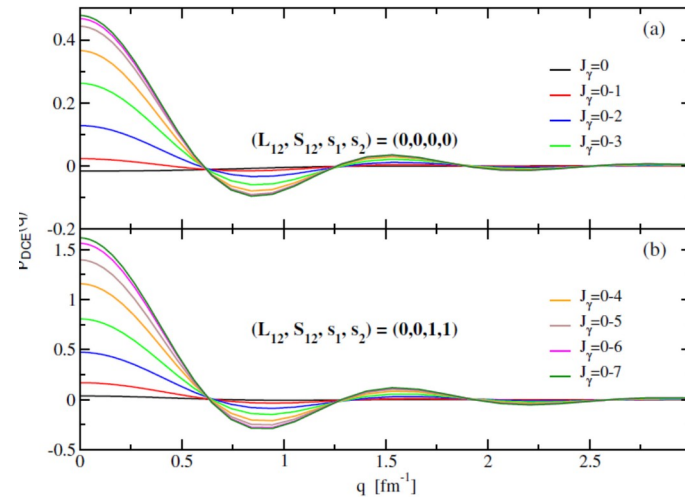
S-channel: separation and factorization of the 2-step process in target and projectile => Selective information on target and projectile

Two-body transition densities

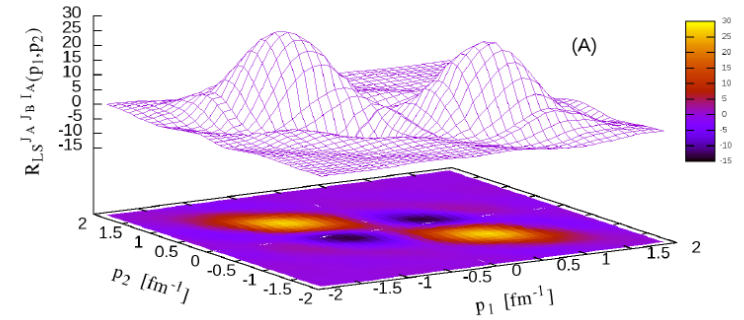
➤ DSCE Cross Section -  $^{76}\text{Se}(^{18}\text{O}, ^{18}\text{Ne}_{g.s.})^{76}\text{Ge}_{g.s.}$  vs.  $^{76}\text{Ge}(^{20}\text{Ne}, ^{20}\text{O}_{g.s.})^{76}\text{Se}_{g.s.}$



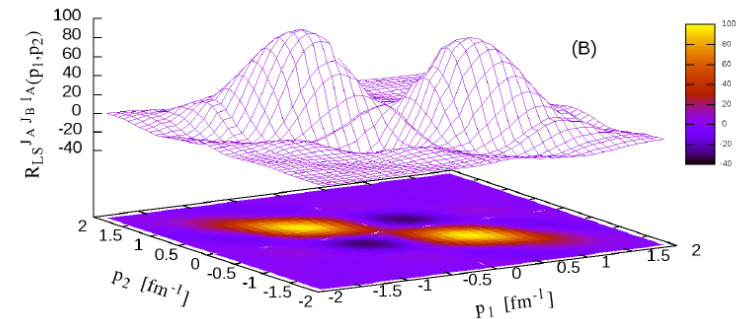
2BTDs  $^{76}\text{Se} \rightarrow ^{76}\text{Ge}_{g.s.}$



$^{76}\text{Se}(\tau^+\tau^+)$   $(L,S,S_1,S_2) = (0,0,0,0)$

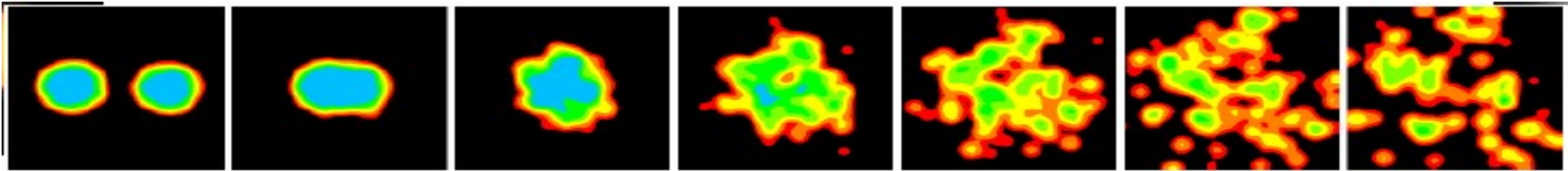


$^{76}\text{Se}(\tau^+\tau^+)$   $(L,S,S_1,S_2) = (0,0,1,1)$



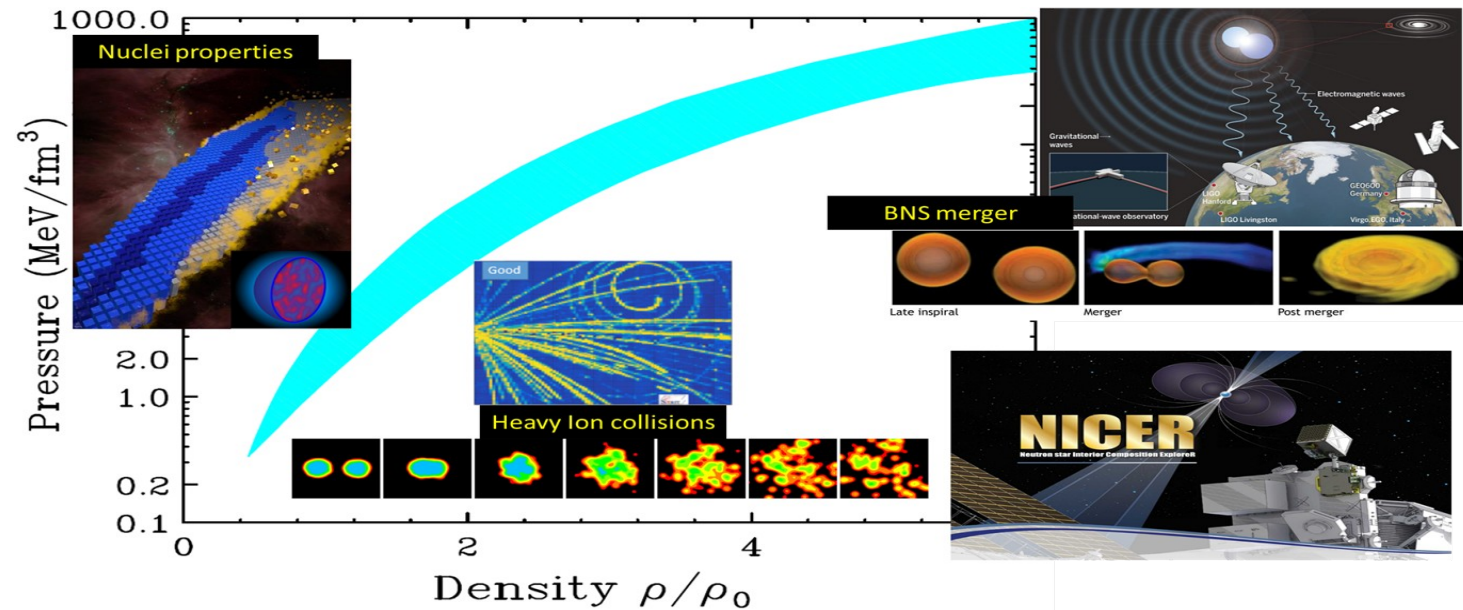
# Dissipative reactions provide a unique opportunity to create nuclear matter in several conditions of density and temperature in laboratory

*Femto-nova explosion created by heavy ion collisions !*



*from A. Ono*

- Explore the nuclear matter **phase diagram** and access the nuclear **Equation of State (EOS)**



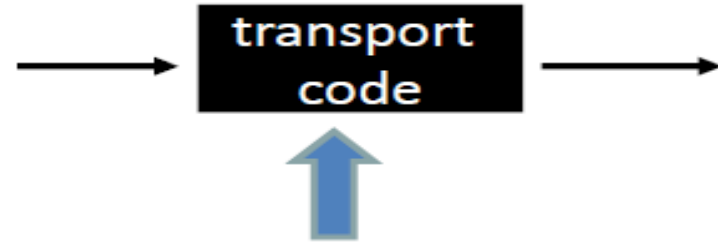
*The EOS of asymmetric nuclear matter*



# Semi-classical approx: from ETDHF to *transport theories*

## Challenges for transport theories: TMEP

physical input  
(EOS,  $\sigma_{inmed}$ ,  
 $\pi\Delta$  physics, ..)



observables

- Quite complex: simulations with many technical details
- Model dependence for some observables

→ Establish a sort of systematical theoretical error

→ **Transport Model Evaluation (Comparison) Project -- TMEP**

- About 30 participants

### Core group:

MC (Catania)

Dan Cozma (Bucharest)

Pawel Danielewicz & Betty Tsang (MSU)

C-M Ko and Z.Zhang (Texas A&M)

Akira Ono (Sendai)

Jun Xu (Shanghai)

Herman Wolter (Munich)

Yingxun Zhang (Beijing)

### ☑ Calculations of Nuclear Matter

(box with periodic boundary conditions)

test separately ingredients in a transport approach:

a) collision term without and with blocking (Cascade)

Y.X. Zhang, et al., Phys. Rev. C 97, 034625 (2018)

b) mean field propagation (Vlasov)

c) pion,  $\Delta$  production in Cascade

d) instabilities, fragmentation

e) momentum dependent fields

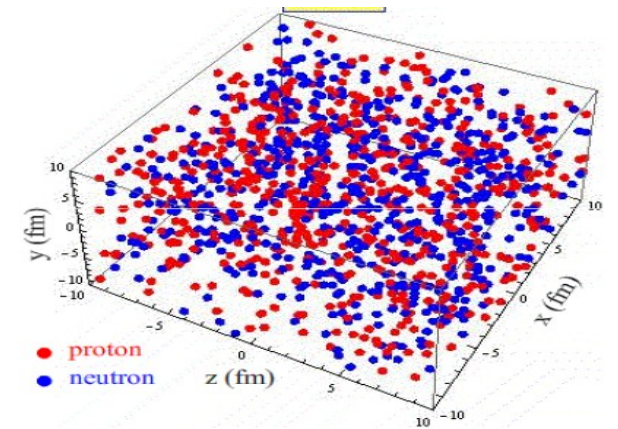
.....

} A.Ono et al., PRC 100, 044617 (2019)

} M. Colonna et al., PRC, 104, 024603 (2021)

} **PI in progress**

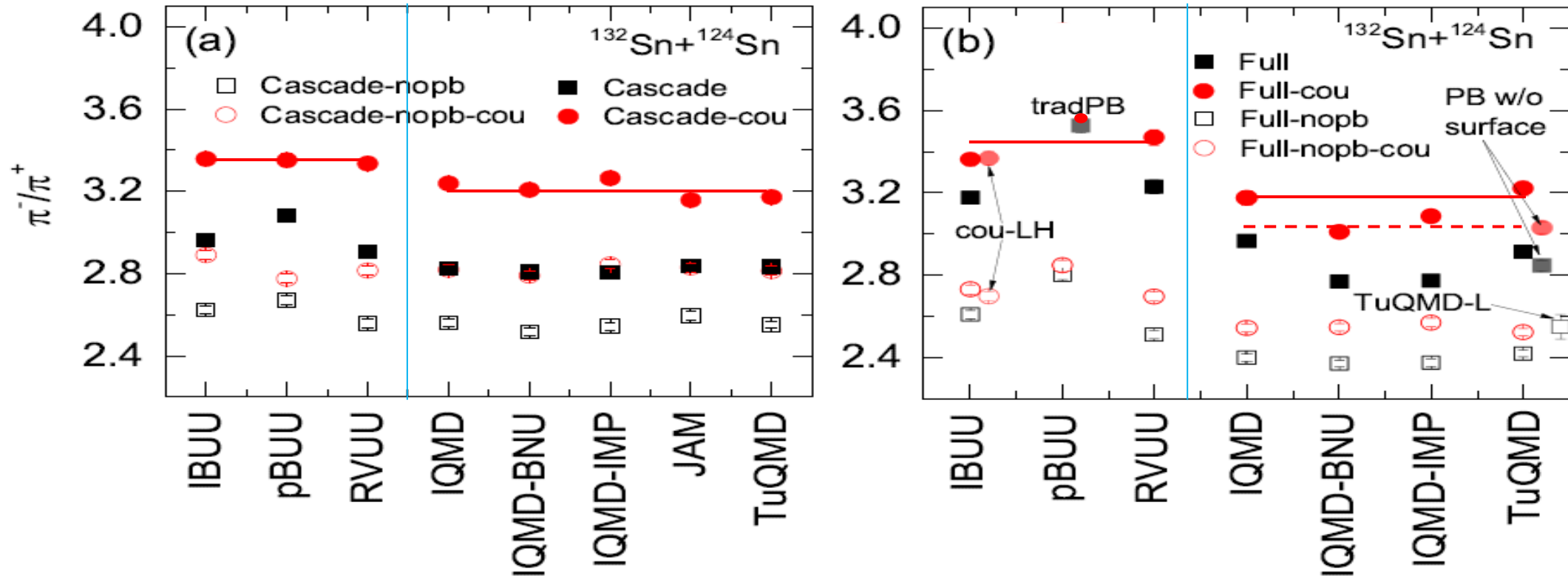
H.Wolter et al, PPNP 125 (2022)



### Comparing pion production in transport simulations of heavy-ion collisions at 270A MeV under controlled conditions

Jun Xu<sup>1,\*</sup> Hermann Wolter<sup>2,†</sup> Maria Colonna<sup>3,‡</sup> Mircea Dan Cozma<sup>4,§</sup> Pawel Danielewicz<sup>5,6,||</sup> Che Ming Ko<sup>7,¶</sup>  
 Akira Ono<sup>8,#</sup> ManYee Betty Tsang<sup>5,6,\*\*</sup> Ying-Xun Zhang<sup>9,10,††</sup> Hui-Gan Cheng<sup>11</sup> Natsumi Ikeno<sup>12,13</sup> Rohit Kumar<sup>5</sup>  
 Jun Su<sup>14</sup> Hua Zheng<sup>15</sup> Zhen Zhang<sup>14</sup> Lie-Wen Chen<sup>16</sup> Zhao-Qing Feng<sup>11</sup> Christoph Hartnack<sup>17</sup> Arnaud Le Fèvre<sup>18</sup>  
 Bao-An Li<sup>19</sup> Yasushi Nara<sup>20</sup> Akira Ohnishi<sup>21,‡‡</sup> and Feng-Shou Zhang<sup>22,23</sup>  
 (TMEP Collaboration)

$^{132}\text{Sn} + ^{124}\text{Sn}$ ,  $b=4$  fm  $E/A = 270$  MeV/A



- CASCADE**: difference **BUU/QMD** due to better treatment of Pauli-Blocking in **BUU**

- FULL**: difference **BUU/QMD** due to «softer» effective interaction in **QMD**

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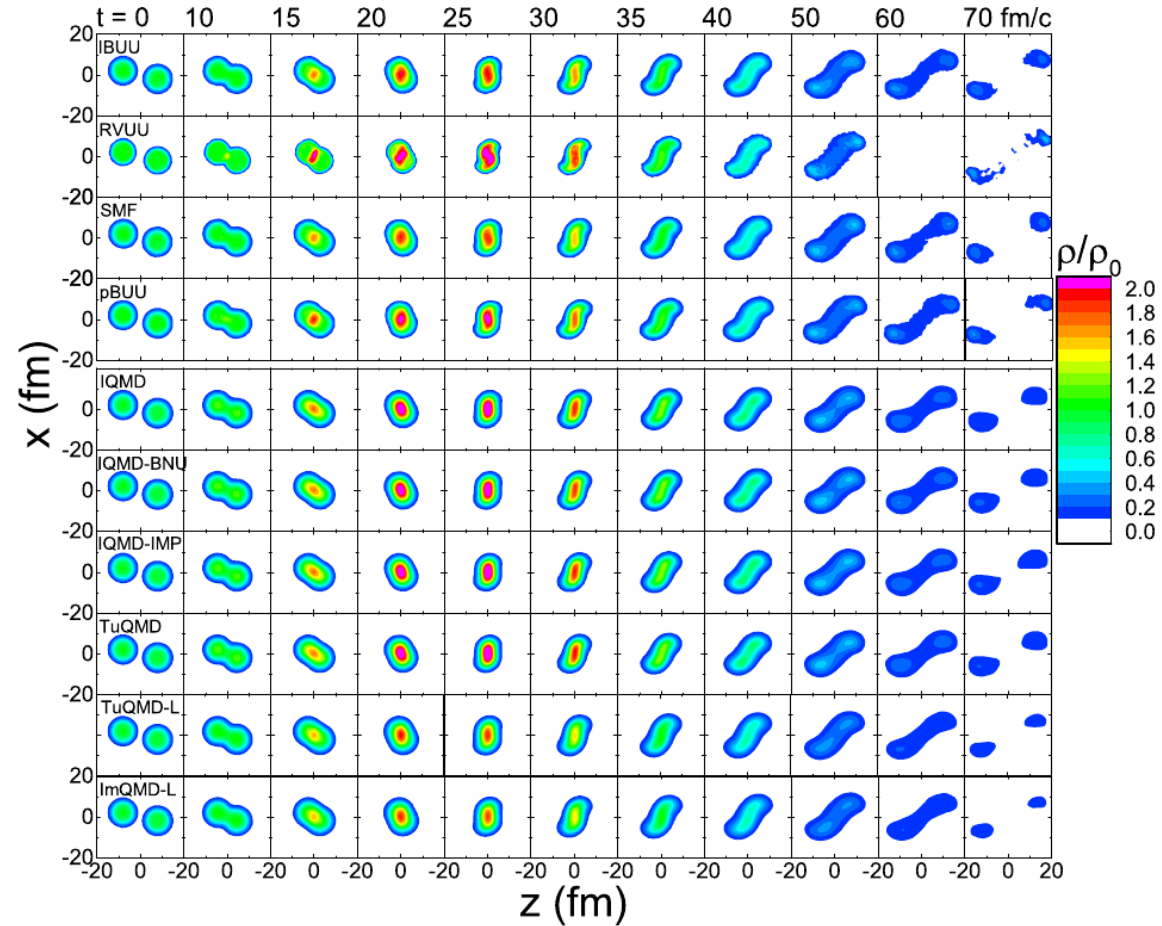


FIG. 2. Contours of reduced densities  $\rho/\rho_0$  in the  $x$ - $z$  plane at different indicated times in the Full-nopb mode.

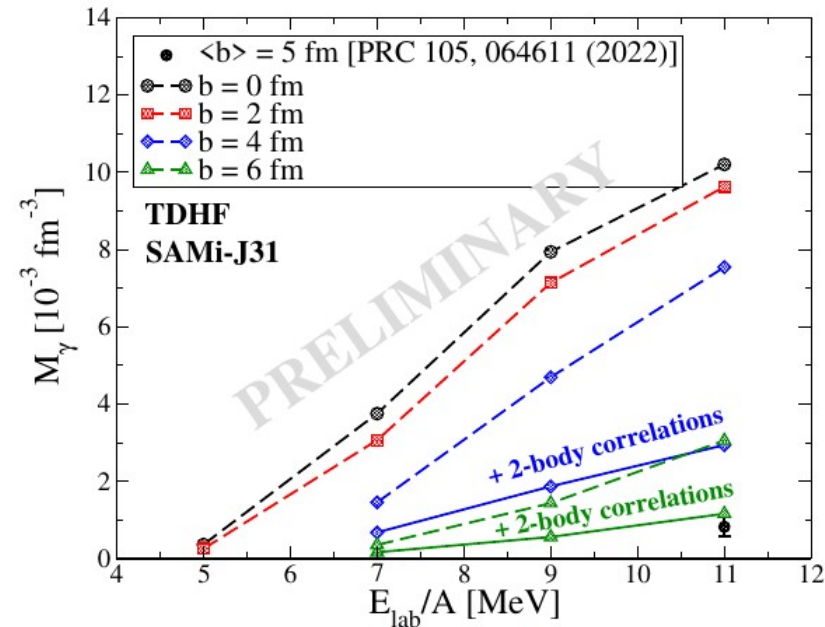
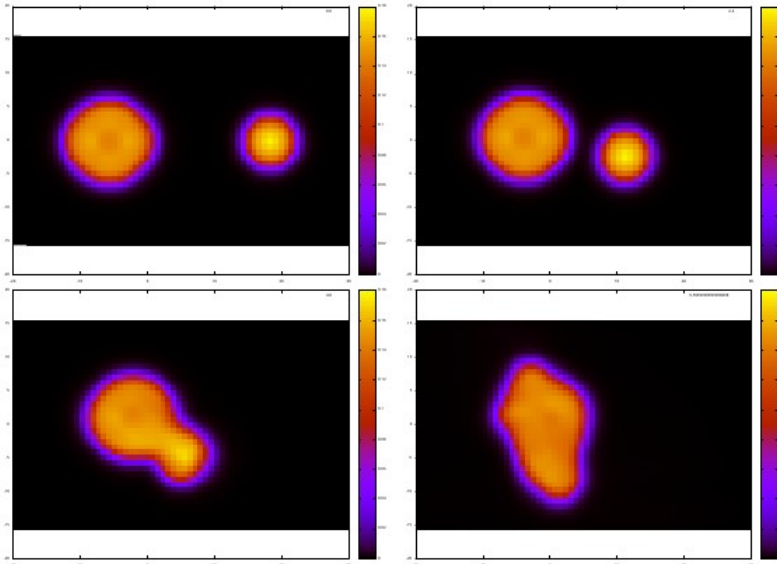
# Dynamics of low-energy heavy-ion collisions (HIC)

- Mean-field models based on (**Skyrme-like**) energy density functionals (**EDFs**)
  - Time-Dependent Hartree-Fock (**TDHF**) theory (or **semi-classical** counterpart)

$$i\hbar\dot{\hat{\rho}}(t) + [\hat{\rho}, \hat{H}_{eff}[\rho]] = 0$$

- **Equilibration** mechanisms in **charge-asymmetric** reactions around **Coulomb** barrier
  - **Pre-equilibrium** emission in  $^{40}\text{Ca} + ^{152}\text{Sm}$  at  $E_{beam} = 11 \text{ A MeV} \Rightarrow$  **Dynamical dipole**

[L. Shvedov, S. Burrello, M. Colonna, H. Zheng, in preparation]



- Understanding **microscopic** processes underlying complex HIC **dynamics**
- Unraveling connection between **effective interaction** and equation of state (**EOS**)
- Crucial **insights** on mechanism for the formation of **super-heavy** elements



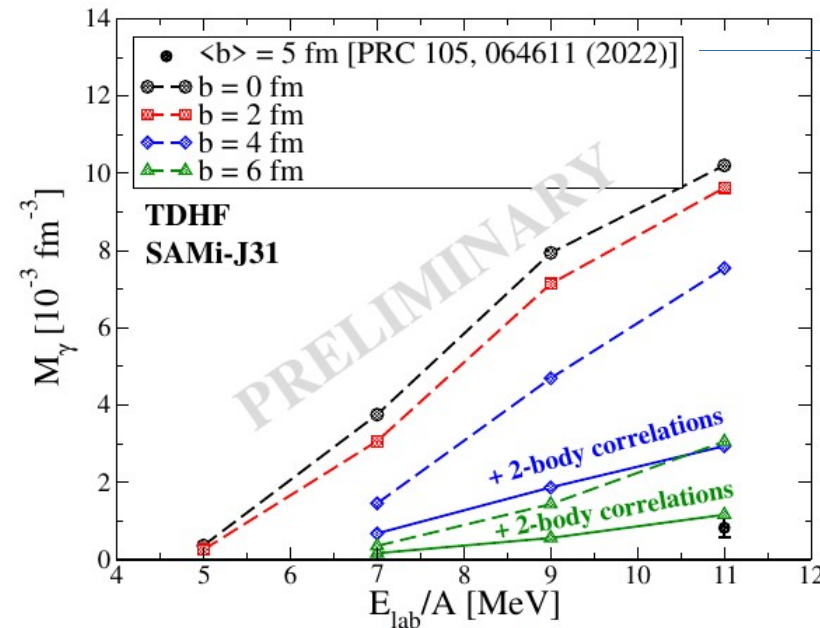
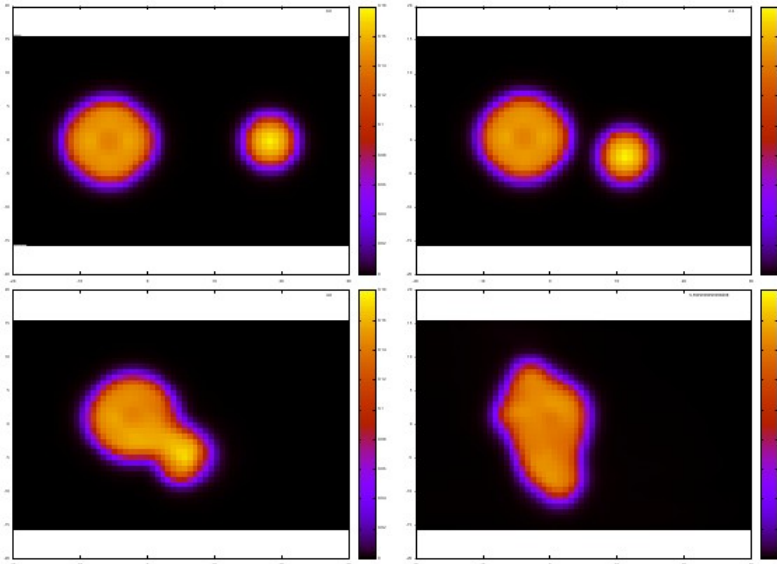
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Parascandolo et al., @LNS

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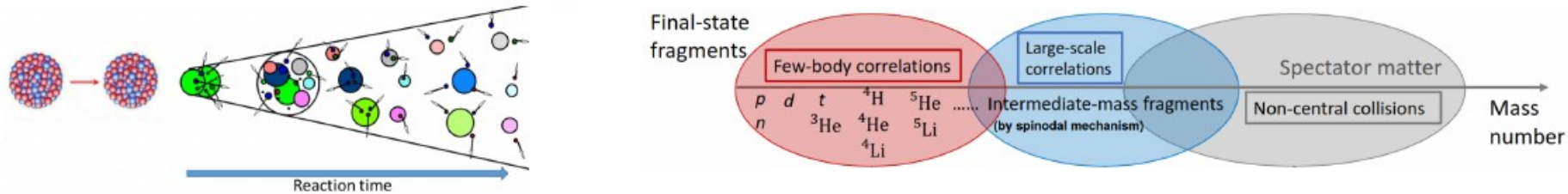


# Improving models for HIC at intermediate energies

- Kinetic approach for **HIC** at  $E_{\text{beam}} \approx (30 - 300) \text{ AMeV} \Rightarrow$  (beyond) Boltzmann eqs.

$$(\partial_t + \nabla_{\mathbf{p}} \varepsilon_{\tau} \cdot \nabla_{\mathbf{r}} - \nabla_{\mathbf{r}} \varepsilon_{\tau} \cdot \nabla_{\mathbf{p}}) f_{\tau} = I_{\tau}^{\text{coll}}[f_n, f_p, \dots], \quad \tau = n, p, d, t, h, \alpha$$

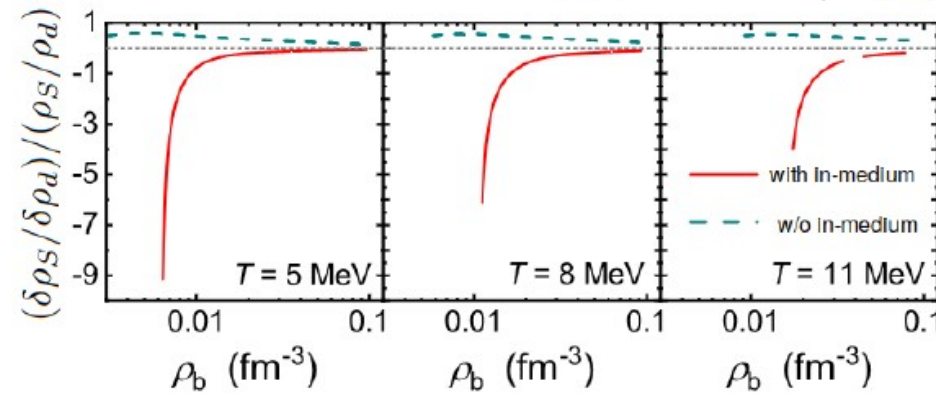
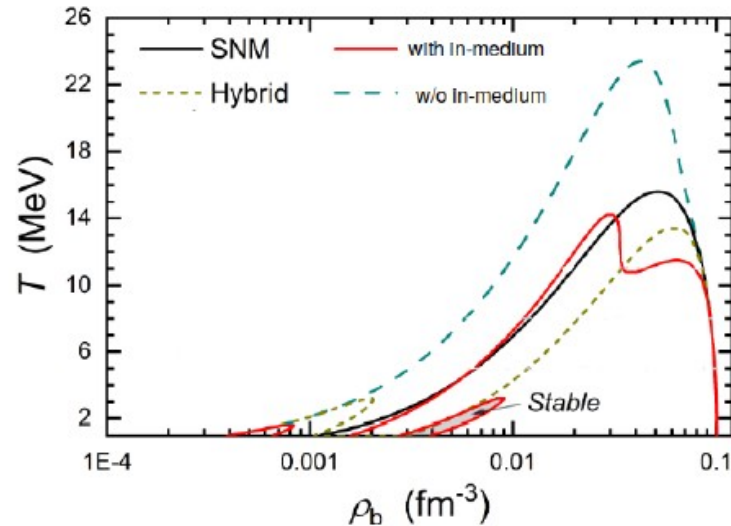
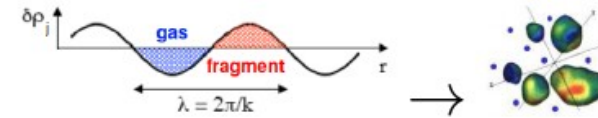
- **Consistent** description of **light** clusters (+ in-medium effects) and **fragments**



- **Linear** response to **collision-less** Boltzmann  $\Rightarrow$  linearized **Vlasov** eqs. ( $\omega = \omega(k)$ )

[R. Wang, S. Burrello, M. Colonna, F. Matera, arXiv:2405.02157, accepted on PRC Letter]

- $\omega = \text{Im}(\omega) \Leftrightarrow$  **unstable** mode (**spinodal region**)



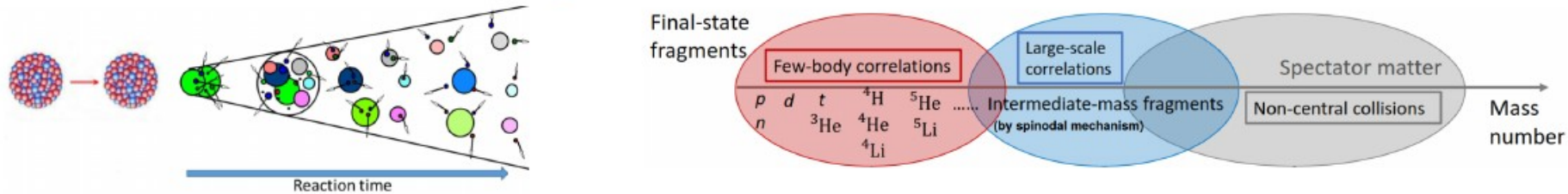
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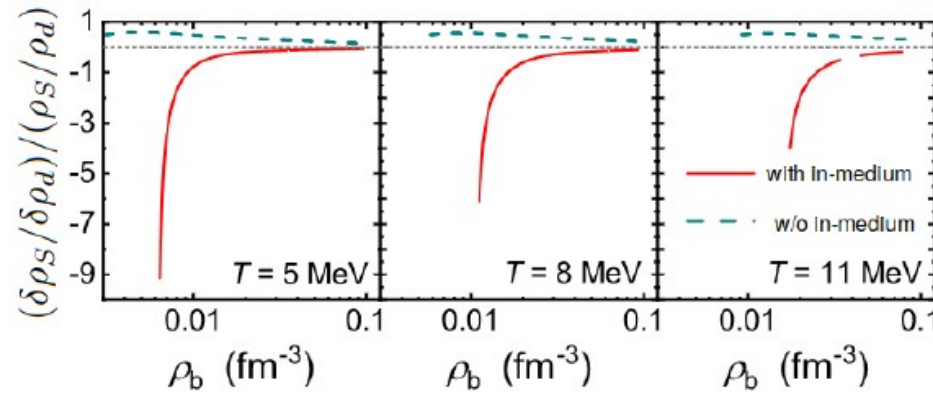
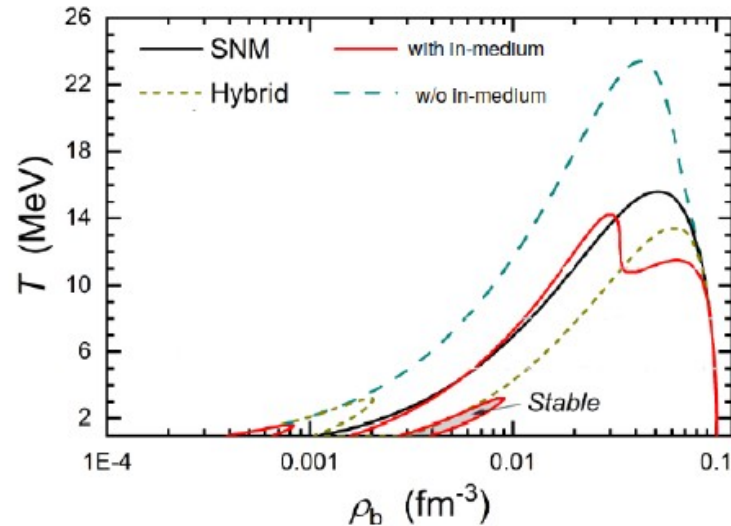
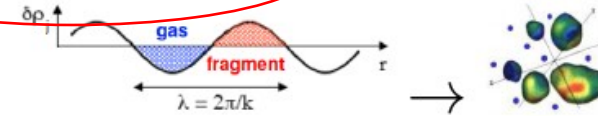
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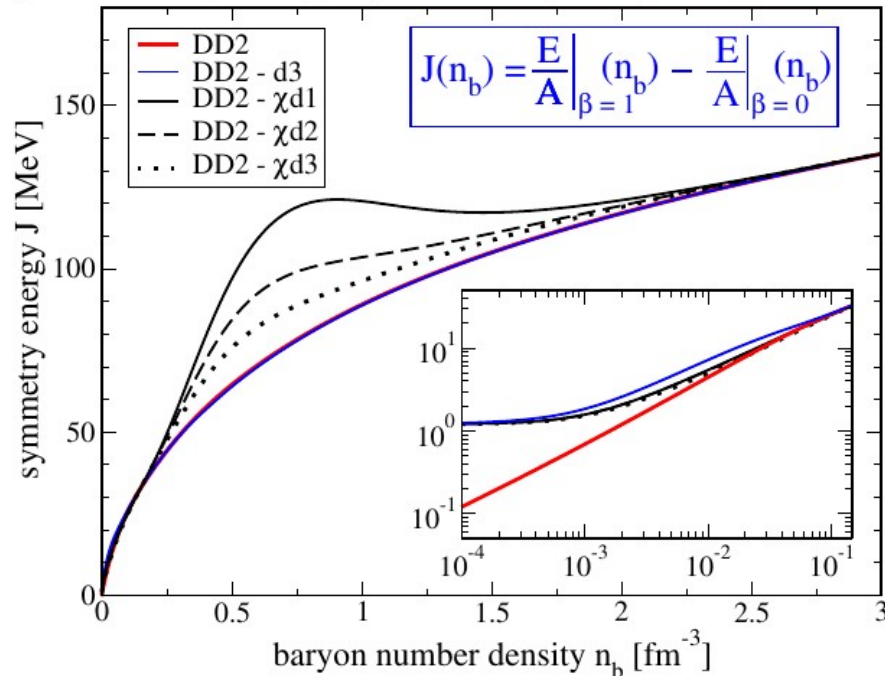
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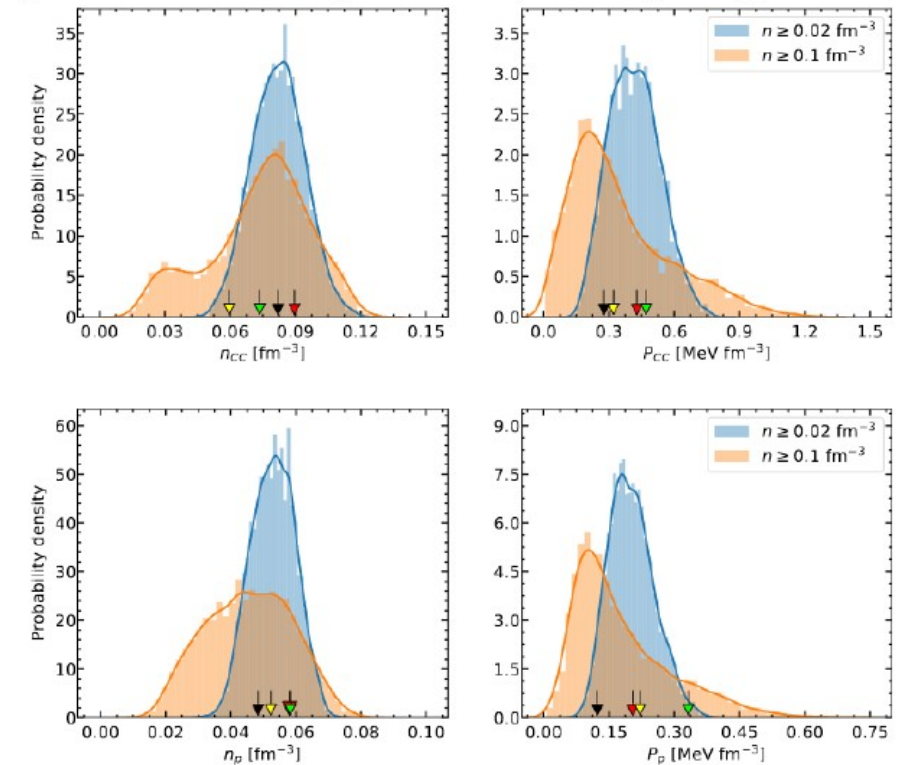
# EOS and modelization of compact stellar object

- Embedding **clusters** and **short-range correlations** in EDFs [coll. G. Röpke & S. Typel]
- Treatment of **low-density** matter in **meta-modeling** approach [coll. F. Gulminelli]
- **EFT**-inspired & **ab-initio** benchmarked **EDFs** [S. Burrello & M. Grasso, EPJA 58:2 (2022)]

[S. Burrello, S. Typel, EPJA 58, 120 (2022)]



[H. Dinh Thi et al., A&A 654, A114 (2021)]

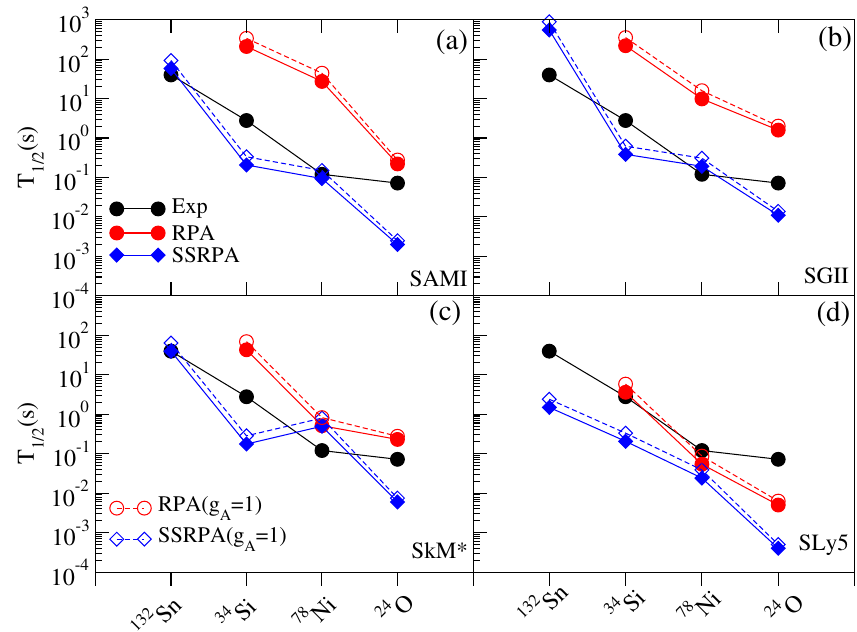


- Development of **emulators** to provide **inputs** on **EOS** from **heavy-ion physics**
- **Theoretical** support for interpretation of **GW** signals for **Einstein Telescope**

## Gamow-Teller Strength in $^{48}\text{Ca}$ and $^{78}\text{Ni}$ with the Charge-Exchange Subtracted Second Random-Phase Approximation

D. Gambacurta<sup>1</sup>, M. Grasso<sup>2</sup> and J. Engel<sup>3</sup>

### Improving beta decay half lives description



D.G and M. Grasso in preparation

- Implications for NME in neutrino-less double- $\beta$  decay, **PANDORA** and **NUMEN** project

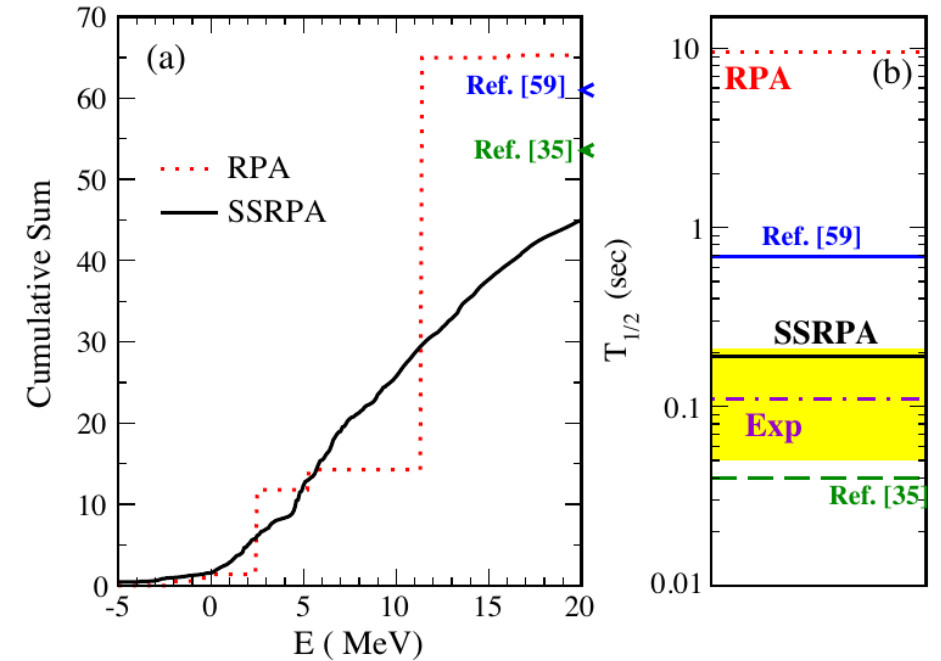


FIG. 4. (a) Cumulative sum for different models (see legend and text) for the nucleus  $^{78}\text{Ni}$ ; (b)  $\beta$ -decay half-life for  $^{78}\text{Ni}$  predicted by SSRPA, compared with predictions of other models and the experimental value [58]. The yellow band represents the experimental uncertainty.

## Symmetry-restored Skyrme-random-phase-approximation calculations of the monopole strength in deformed nuclei

A. Porro<sup>1,2,3,\*</sup>, G. Colò<sup>4,5,†</sup>, T. Duguet<sup>1,6,‡</sup>, D. Gambacurta<sup>7,8</sup> and V. Somà<sup>1,||</sup>

### A. Angular momentum projection

$$P_{MK}^J \equiv \frac{2J+1}{8\pi^2} \int d\Omega \mathcal{D}_{MK}^{J*}(\Omega) \mathcal{R}(\Omega),$$

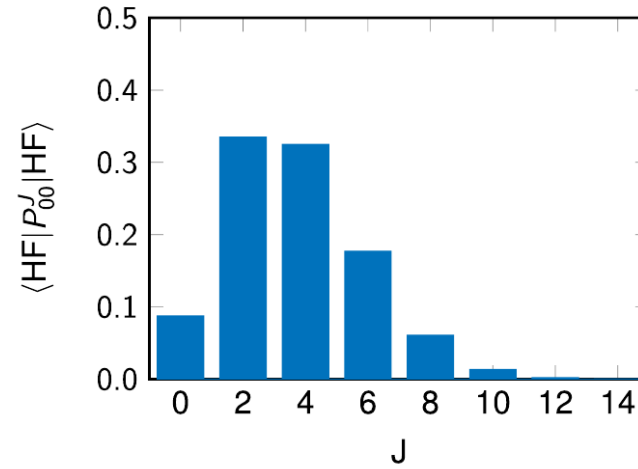
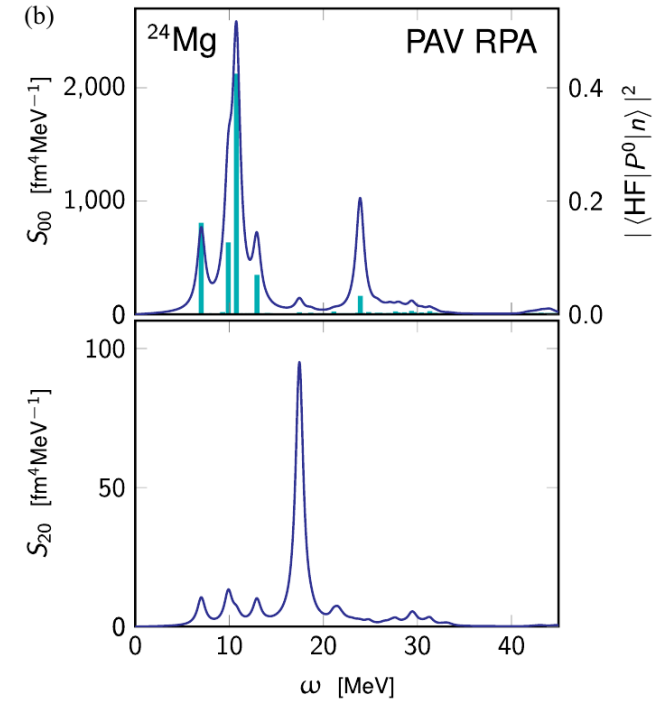
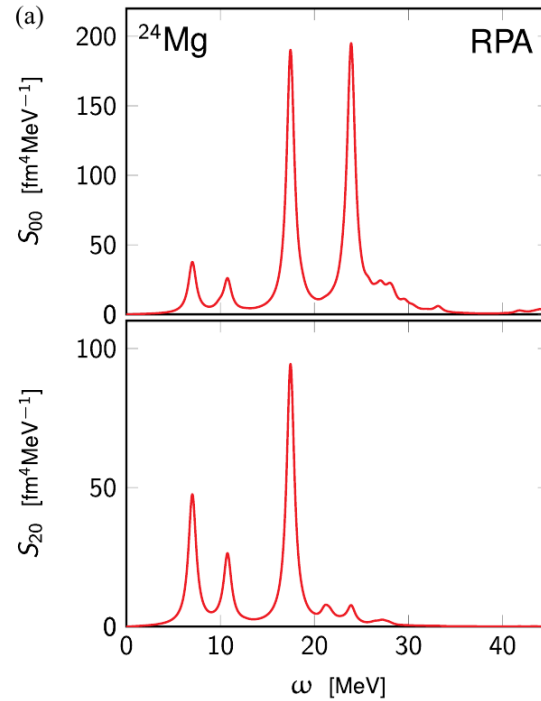
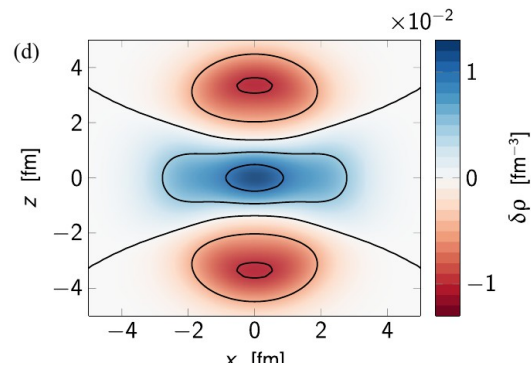
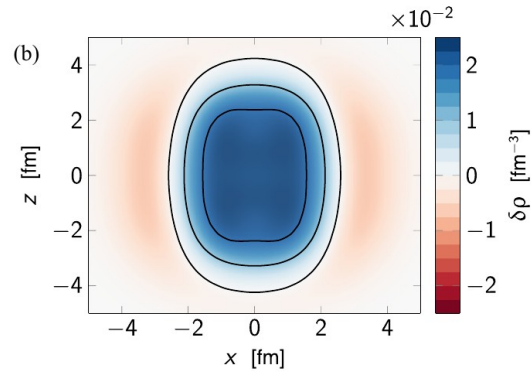


FIG. 2. Angular momentum decomposition of the HF ground state in  $^{24}\text{Mg}$  ( $N_{\text{sh}} = 11$ ).



## Symmetry-restored Skyrme-random-phase-approximation calculations of the monopole strength in deformed nuclei

A. Porro<sup>1,2,3,\*</sup>, G. Colò<sup>4,5,†</sup>, T. Duguet<sup>1,6,‡</sup>, D. Gambacurta<sup>7,8</sup> and V. Somà<sup>1,||</sup>

### A. Angular momentum projection

$$P_{MK}^J \equiv \frac{2J+1}{8\pi^2} \int d\Omega \mathcal{D}_{MK}^{J*}(\Omega) \mathcal{R}(\Omega),$$

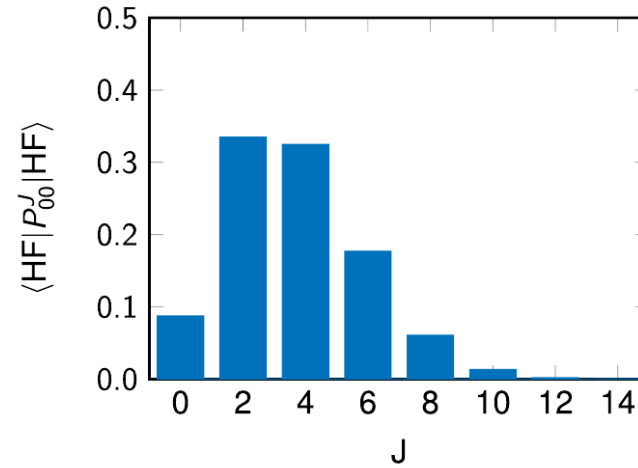
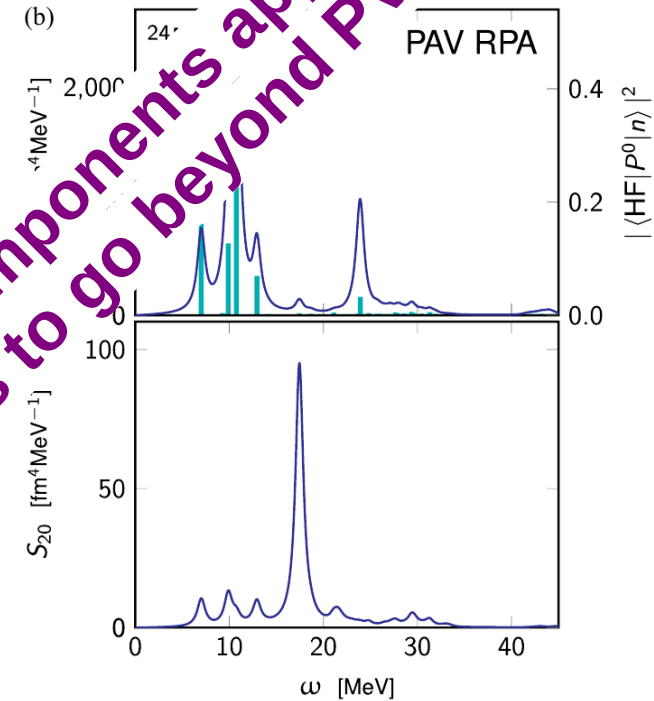
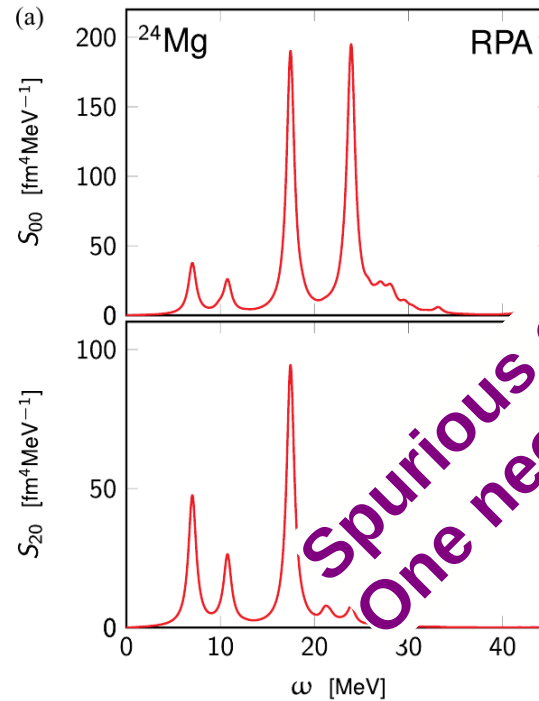
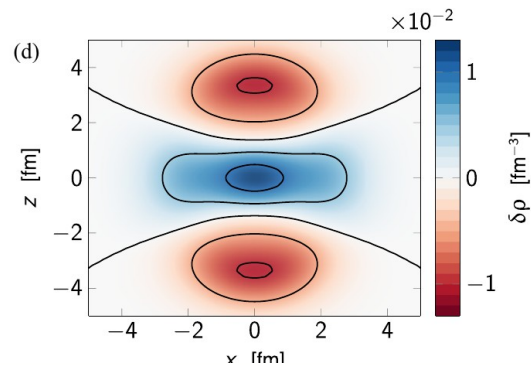
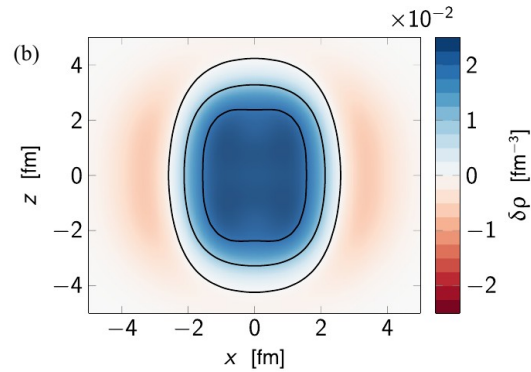


FIG. 2. Angular momentum decomposition of the state in  $^{24}\text{Mg}$  ( $N_{\text{sh}} = 11$ ).



Spurious components appear  $\Rightarrow$   
One needs to go beyond PVA-RPA

# Attività 2025: MONSTRE

## Nuclear Structure

- Single and double beta decay studies (RPA, QRPA and Second RPA), *in progress*
- Nuclear excitations in deformed nuclei and link with Equation of State
- Transport theories: formation of light clusters, treated as explicit degrees of freedom
- Equation of State including light clusters, *Short Range Correlations*  
(important also for the modeling of compact stellar objects=>Einstein Telescope physics)

## Nuclear Reactions

- Charge Exchange: Compare the results of different structure models (shell model vs. QRPA), *in progress*
  - Consistent description of competing channels (multi-nucleon transfer) and, more in general, of all open reaction channels (multi-channel approach)
  - Correlated Double Charge Exchange mechanism (*short-range correlations*) and interference with DSCE
- **Theoretical support** to LNS experiments (Numen project, ASFIN, PANDORA, ...)

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# FTE: MONSTRE (4.4)<sup>4.7 in 2023</sup>

cognome	nome	contratto	profilo	perc	sezione
<b>Bonaccorso</b>	<b>Angela</b>	Associato	Associazione Senior	0%	Pisa
<b>Bonasera</b>	<b>Aldo</b>	Associato	Associazione Senior	50%	LNS
<b>Burrello</b>	<b>Stefano</b>	Dipendente	Ricercatore	70%	LNS
<b>Colonna</b>	<b>Maria</b>	Dipendente	Dirigente di Ricerca	60%	LNS
<b>Gambacurta</b>	<b>Danilo</b>	Dipendente	Primo Ricercatore	80%	LNS
<b>Greco</b>	<b>Vincenzo</b>	Associato	Prof. Ordinario	10%	LNS
<b>Gargano</b>	<b>Angelina</b>	Dipendente	Primo Ricercatore	70%	Napoli
<b>Shvedov</b>	<b>Leonid</b>	Dipendente	Assegno di Ricerca	100%	LNS

# **SIM: Strongly Interacting Matter at high density and temperature**

*Units: Catania, Firenze, **LNS**, Torino,*

*FTE totale:  $\approx 20$*

**FTE (LNS)  $\approx 6.6$**

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**Responsabile Nazionale:** Andrea Beraudo (TO)

**Responsabile Locale:** Enzo Greco

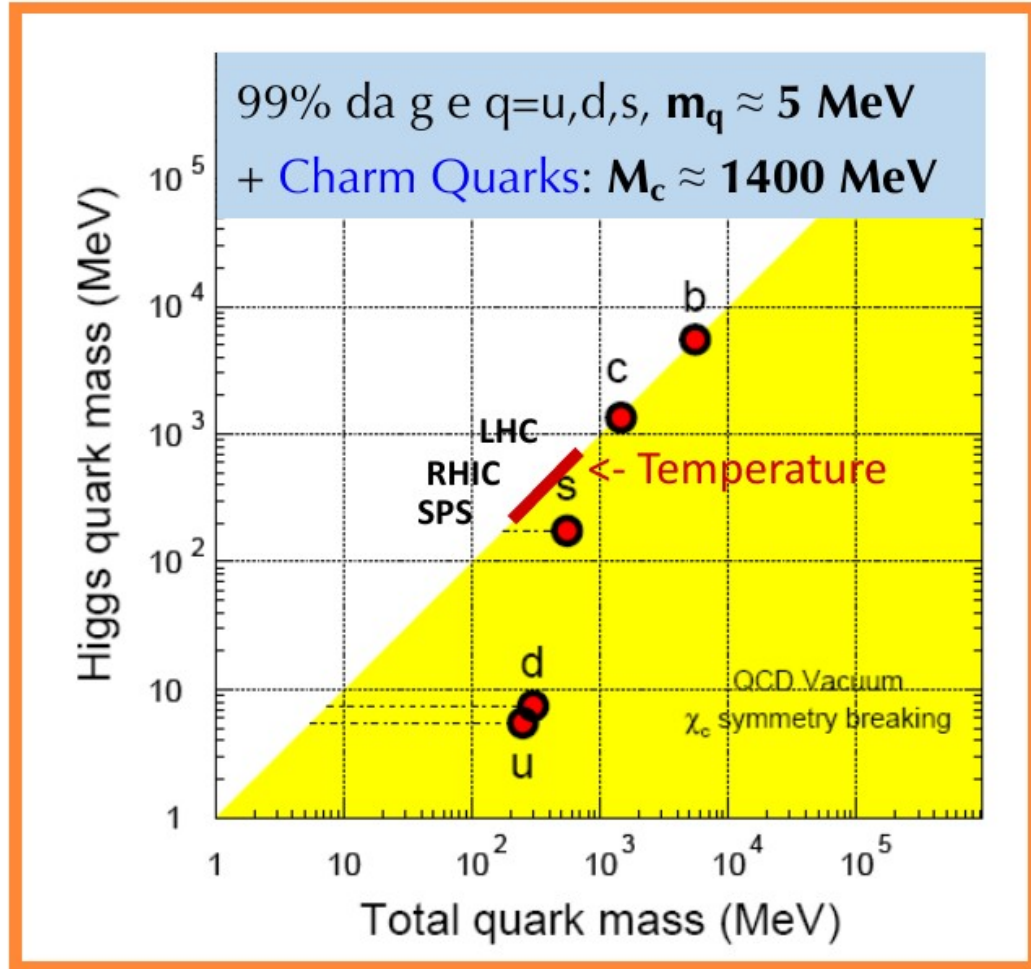
Collaborazioni: CT, TO, Francoforte, Nantes, CERN, Berkeley LBL, Texas A&M, Duke U., Lanzhou University, University of Barcellona, IIT Goa, Jyväskylä , ...

# Obiettivi generali: Study of strongly interacting matter at high density and temperature

---

- Fenomenologia del Quark Gluon Plasma (QGP)
- Dinamica dei quarks e meccanismi di adronizzazione
- Equazioni del trasporto per i partoni (beyond hydrodynamics):
- Dinamica dei quark pesanti: charm e bottom
- Early stage, dinamica di non-equilibrio AA, pA e pp

# An elephant in the liquid: Heavy Charm Quark



Heavy because:

✧  $M \gg \Lambda_{\text{QCD}}$  (particle physics)

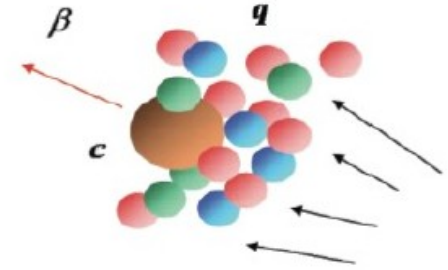
✧  $M \gg T$  (plasma physics)

Fokker-Planck Equation – Brownian motion

$$\frac{\partial f_{c,b}}{\partial t} = \underbrace{\gamma}_{\langle p \rangle} \frac{\partial (p f_{c,b})}{\partial p} + \underbrace{D}_{\langle \Delta p^2 \rangle} \frac{\partial^2 f_{c,b}}{\partial p^2}$$

$\langle p \rangle$   
Drag

$\langle \Delta p^2 \rangle$   
Diffusion



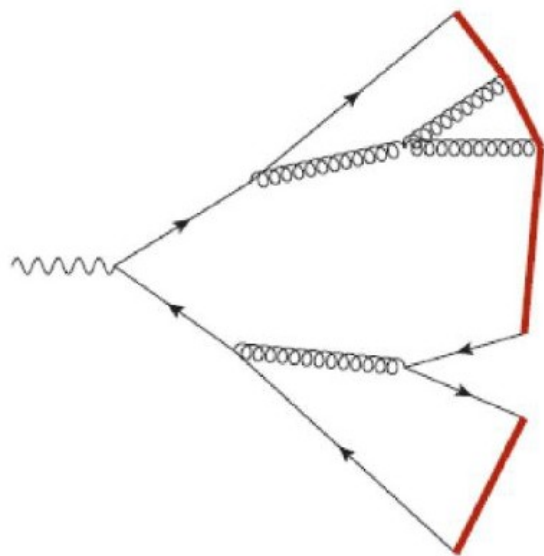
→ Poorly dragged & long thermalization time (!?)

$$\tau_{C,\text{therm}} \approx O(10^2) \gg \tau_{\text{QGP}} \gg \tau_{q,\text{therm}} \approx O(1) \text{ fm/c}$$

Goal : determine strength of QCD interaction and thermalization time of Heavy quarks

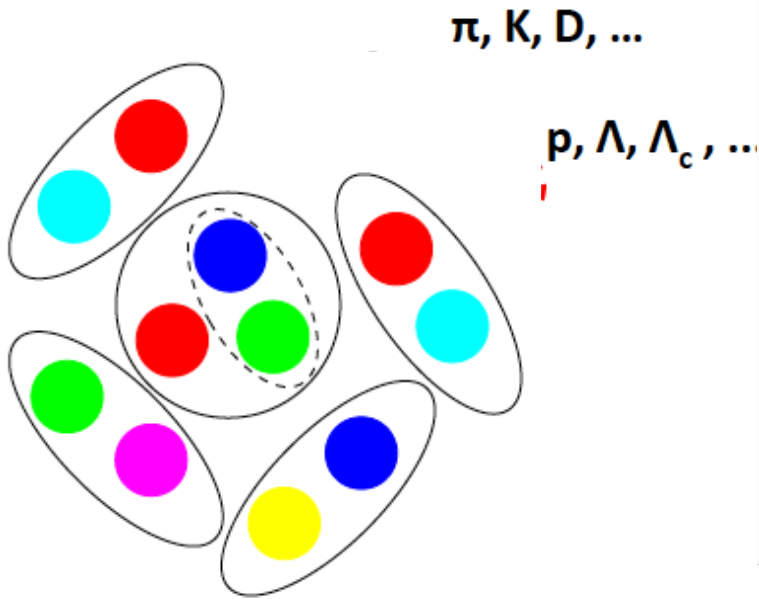
Long stand problem → reproduce both  $p_T$  spectra ( $R_{AA}$ ) and elliptic flow ( $v_2$ )

# Hadronization from $e^+e^-$ to pp and AA



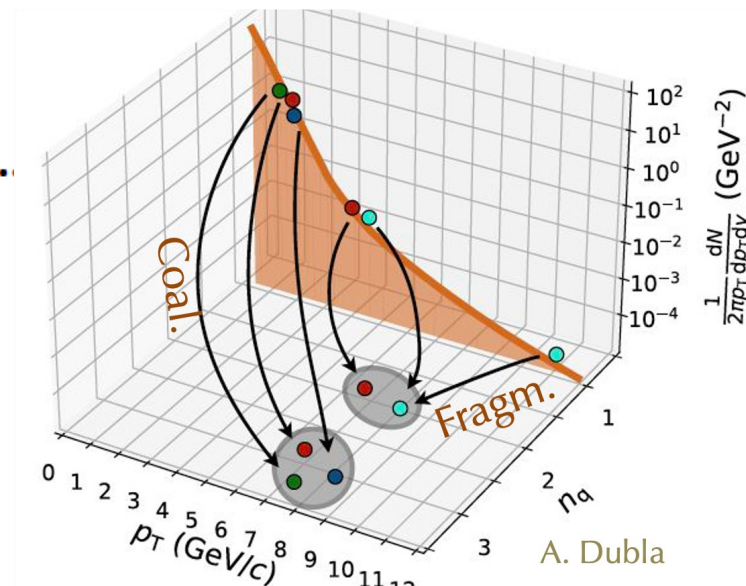
Fragmentation

$$f_H(P_H = zp_T) = f_{q,g}(p_T) \otimes D_{q,g \rightarrow H}(z) \quad , z < 1$$



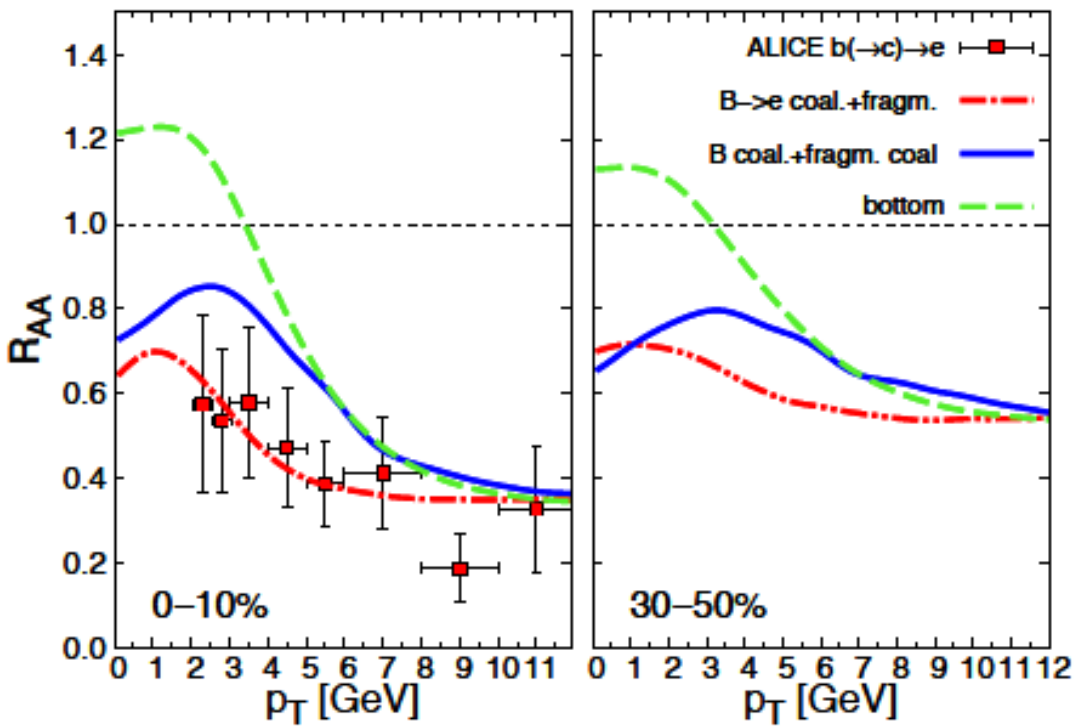
Coalescence

$$f_M \approx f_q \otimes f_{\bar{q}} \otimes \Phi_M \cdot \delta(\vec{p}_M - \vec{p}_q - \vec{p}_{\bar{q}})$$

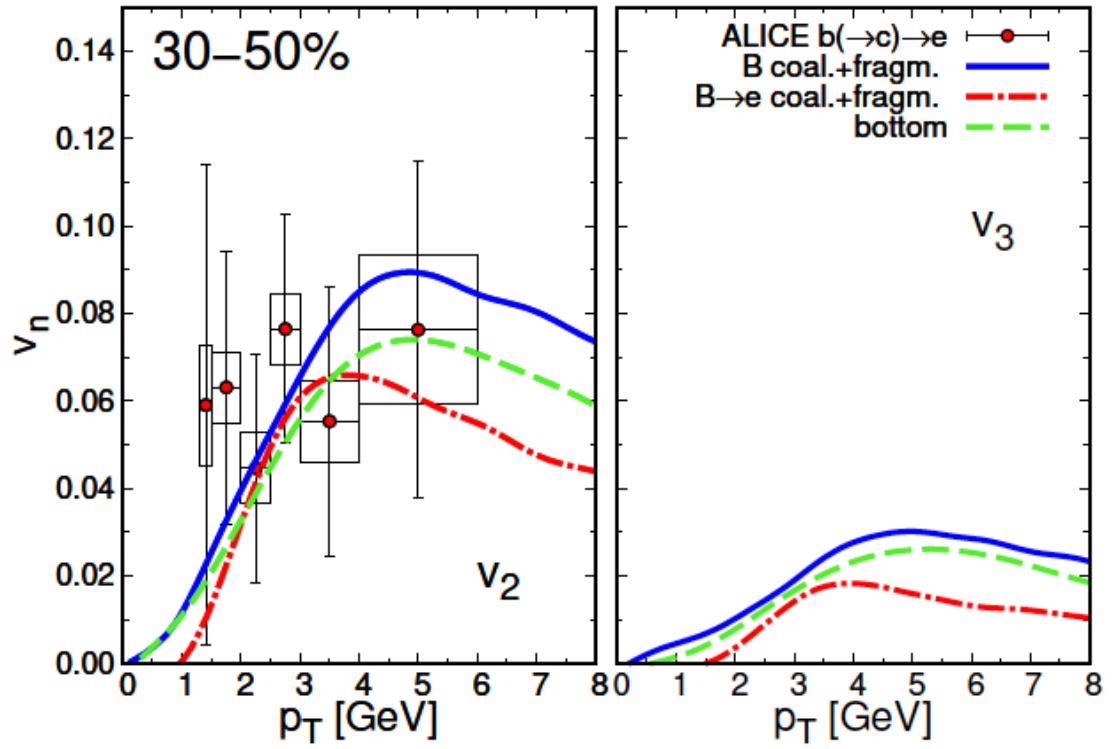


# Extension to b quark dynamics

## Ratio $p_T$ spectra AA/pp collision



## Elliptic $v_2$ and triangular $v_3$ flow



- Extension of QPM-Catania model employed for charm quarks to bottom quarks: no parameter adjustment!
- Comparison to electrons for semileptonic decays of B mesons: OK! (large error bars)



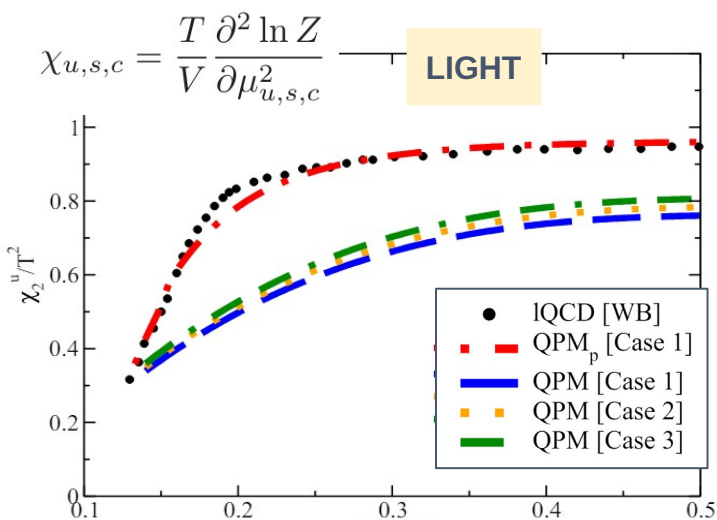
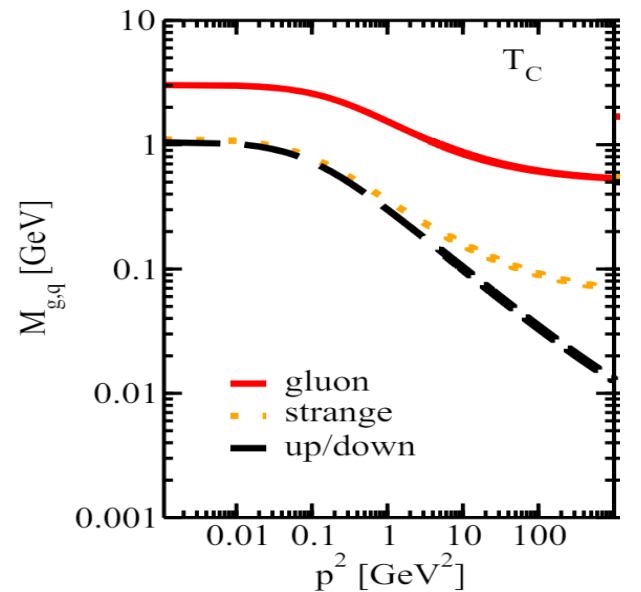
# New: QPM ( $N_f=2+1$ ) extension to QPMp ( $N_f=2+1+1$ )

Momentum dependent masses :  $p \gg \Lambda_{\text{QCD}} \rightarrow m_{u,d,s} \rightarrow$  current masses

$$M_g(T, \mu_q, p) = \left(\frac{3}{2}\right) \left( \frac{g^2(T^*/T_c(\mu_q))}{6} \left[ \left(N_c + \frac{1}{2}N_f\right) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \left[ \frac{1}{1 + \Lambda_g(T_c(\mu_q)/T^*) p^2} \right] \right] \right)^{1/2} + m_{\chi_8}$$

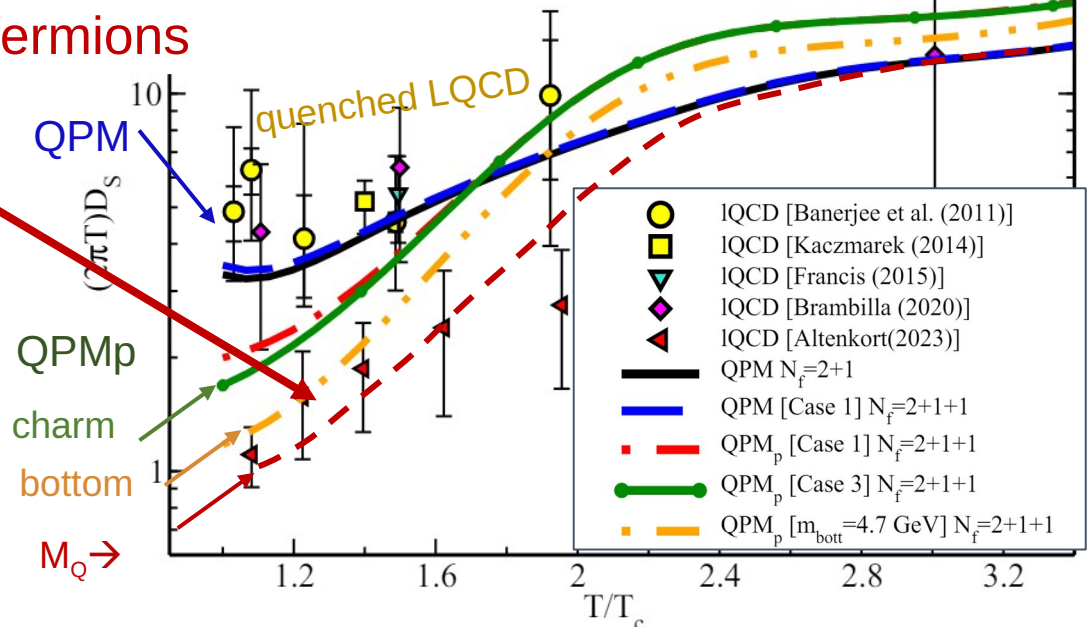
$$M_{q,\bar{q}}(T, \mu_q, p) = \left( \frac{N_c^2 - 1}{8N_c} g^2(T^*/T_c(\mu_q)) \left[ T^2 + \frac{\mu_q^2}{\pi^2} \left[ \frac{1}{1 + \Lambda_q(T_c(\mu_q)/T^*) p^2} \right] \right] \right)^{1/2} + m_{\chi_q}$$

$m_{u,d,s}(p)$  expected on theoretical ground  $\rightarrow$  susceptibilities...



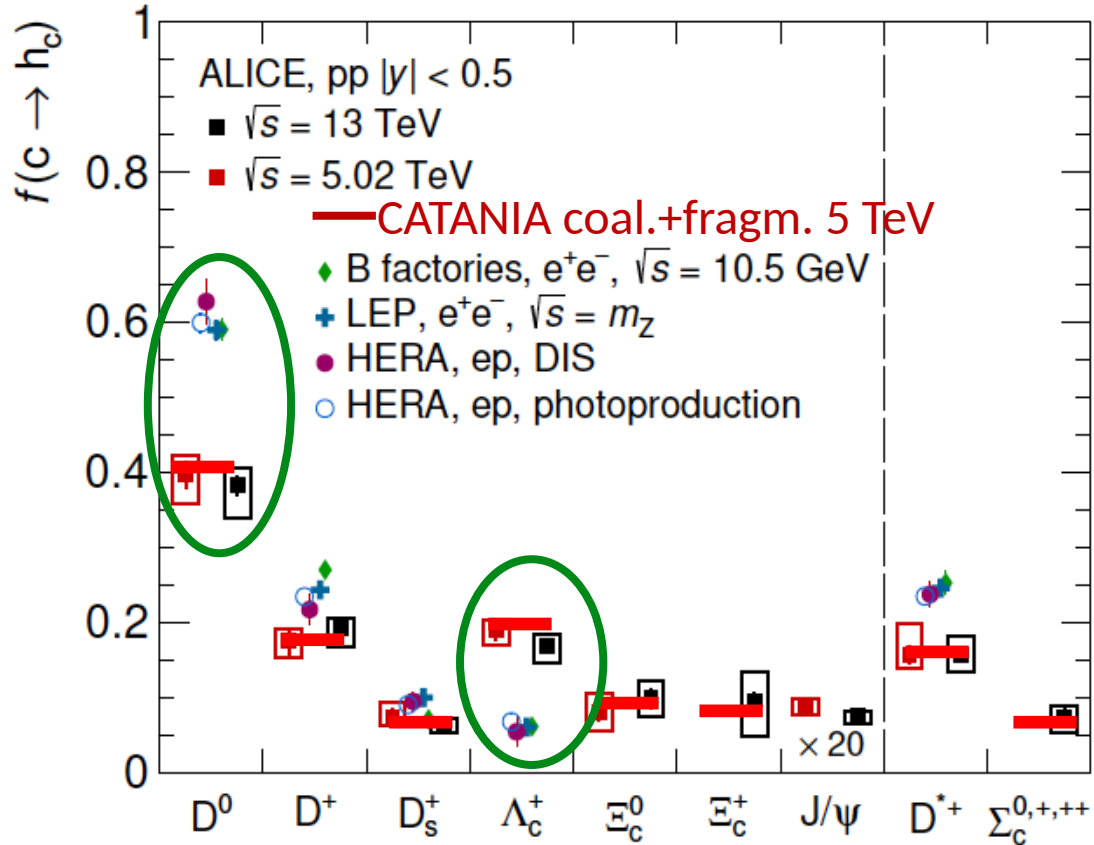
$\triangleright$  QPMp describes  $\epsilon, P, \chi_q, \chi_s$  of LQCD  
 + closer than QPM to  $D_s$  to new LQCD with dynamical fermions

$$D_s = \frac{T}{M \gamma} = \frac{T}{M} \tau_{th}$$



$\triangleright$  Can this new  $D_s(T)$  generate predictions for  $R_{AA}, v_2, v_3$  in agreement with experimental data?

# “Fragmentation” Fractions in pp Catania Coalescence

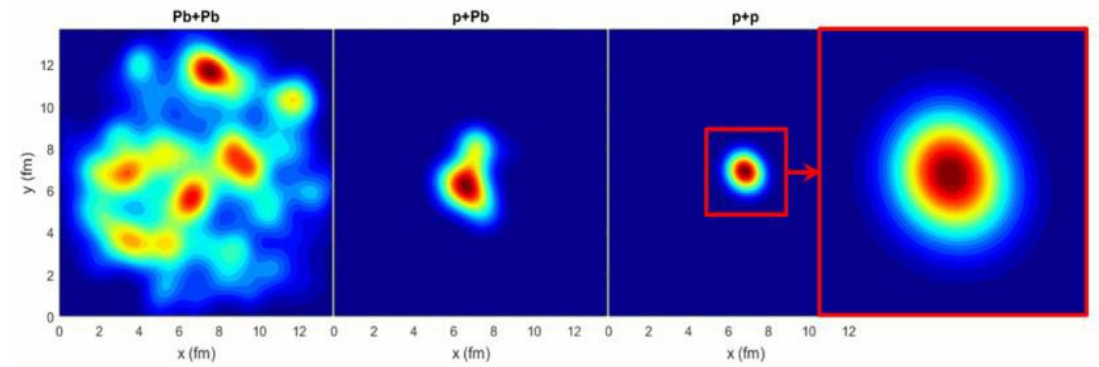


Altmann, Dubla, Greco, Rossi & Skands, [arXiv:2405.19137](https://arxiv.org/abs/2405.19137)

- Evidence of different “Fragmentation” Fractions in pp at LHC wrt  $e^+e^-$  ( $e-p$ ) collisions while very similar to AA collisions
- Catania Coal+Fragm. : same approach to pp and AA: pp@TeV like a little drop of AA

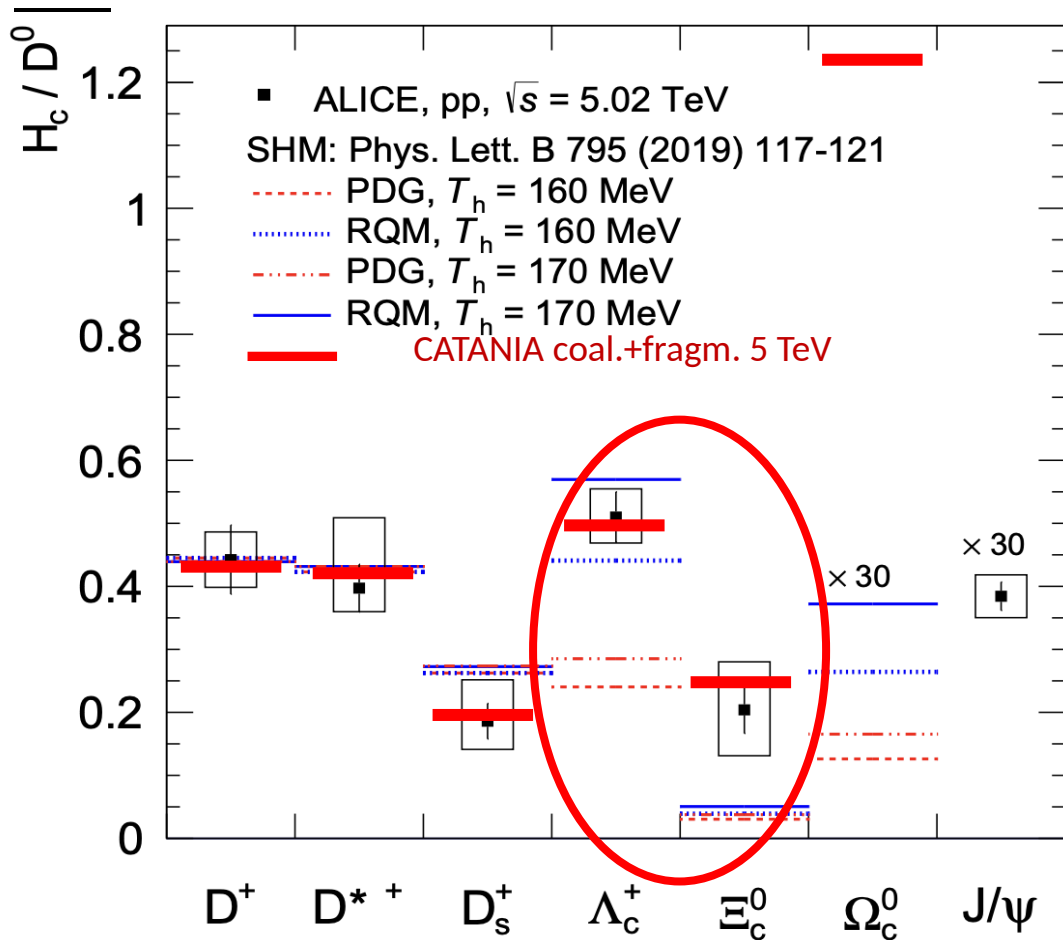
Coalescence  $f_M \approx f_q \otimes f_{\bar{q}} \otimes \Phi_M \cdot \delta(\vec{p}_M - \vec{p}_q - \vec{p}_{\bar{q}})$

**Daring** to assume a small fireball according **viscous hydro** applied to pp as in AA, but **size,time, flow given by hydro for pp**





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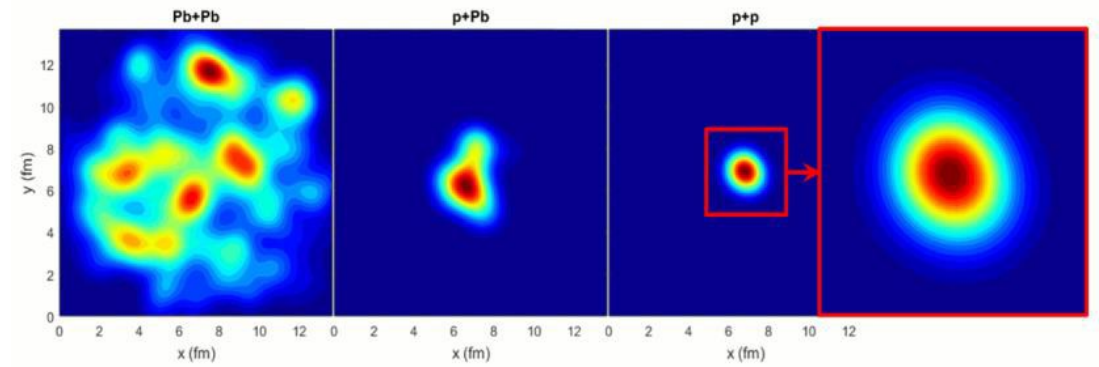


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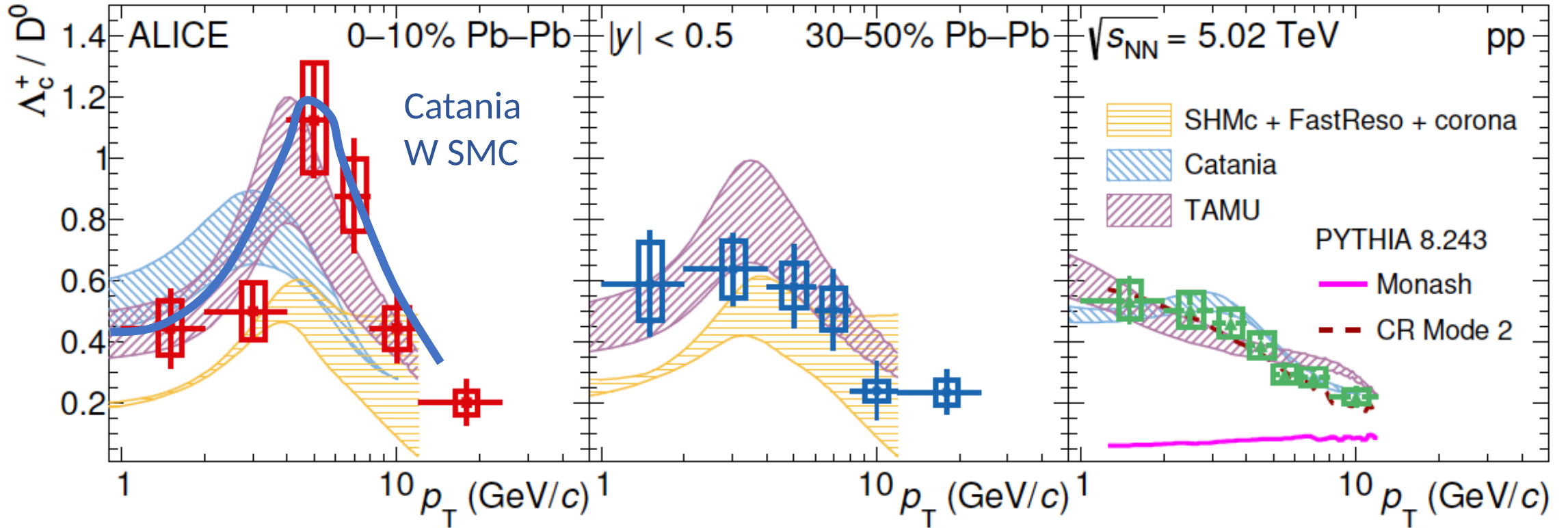
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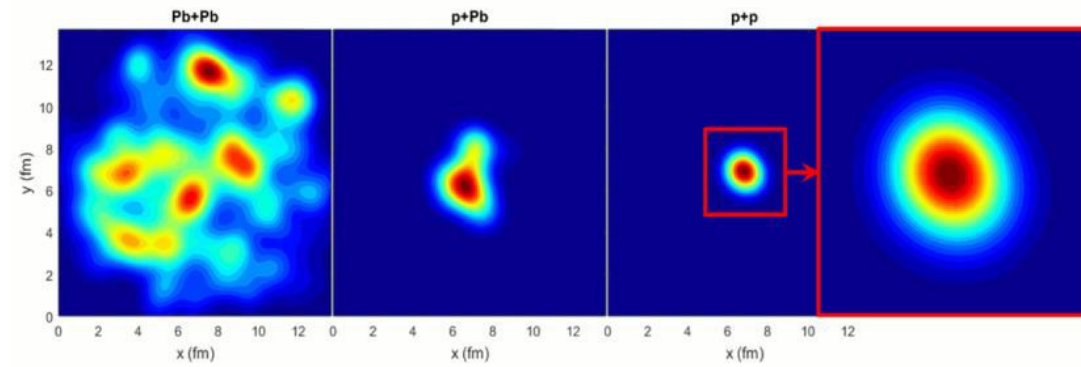


# From AA to pp baryon/meson vs $p_T$



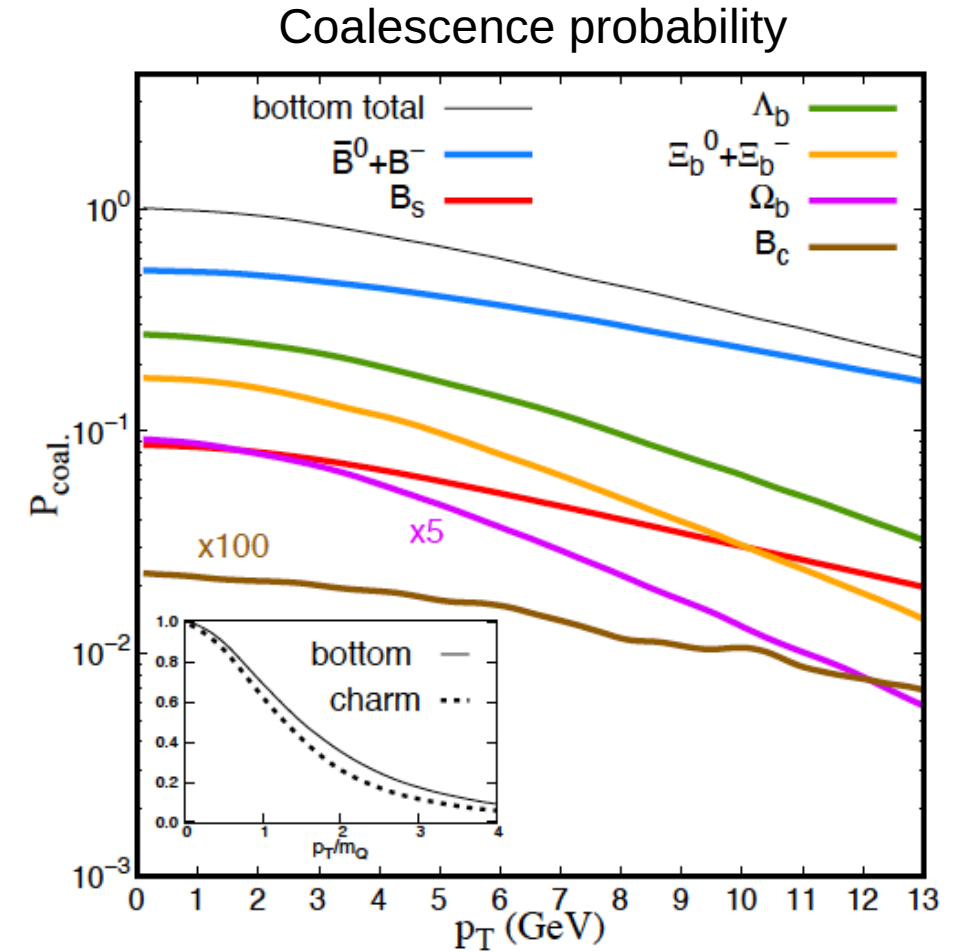
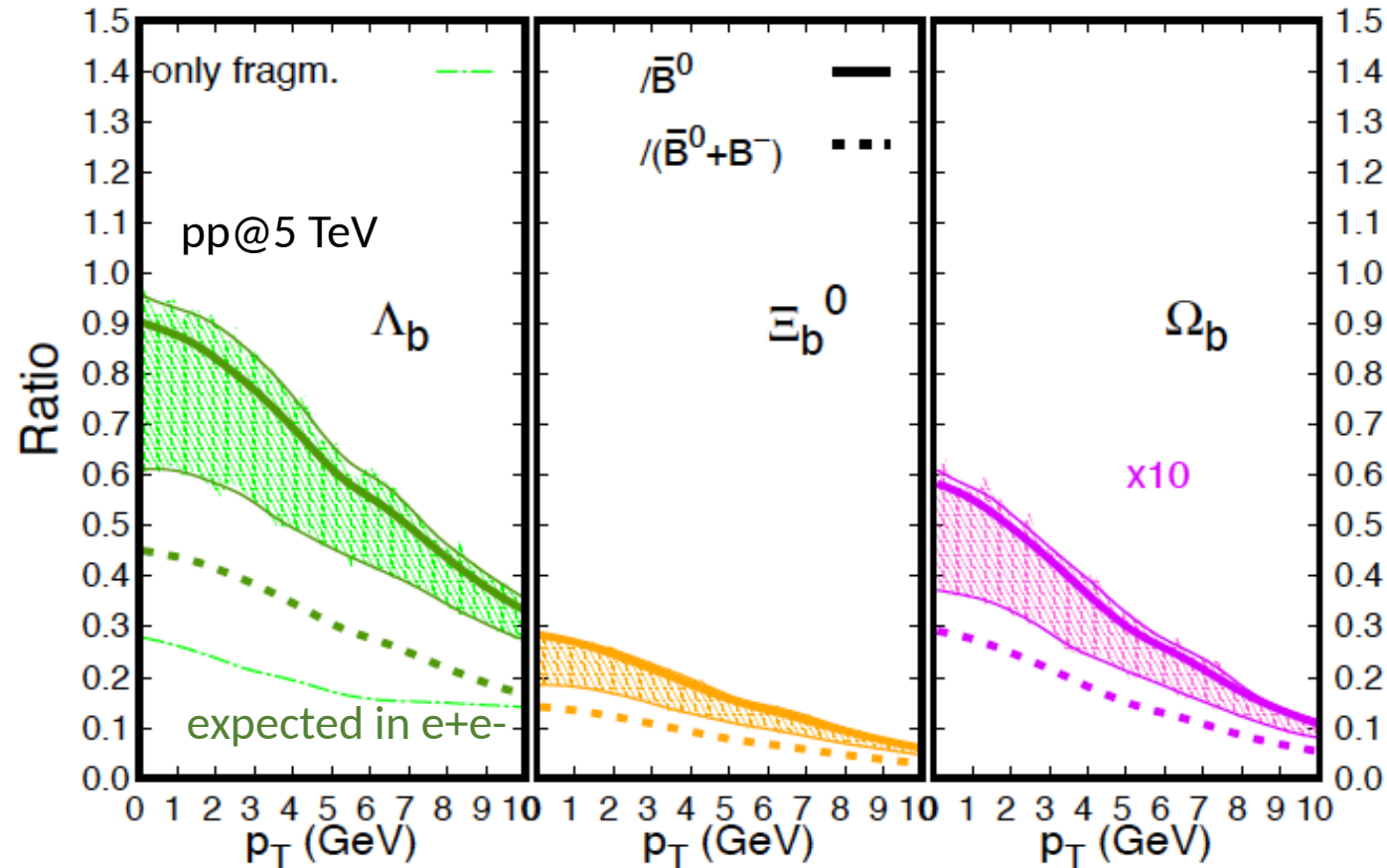
Same hadronization approach in pp and AA:  
pp@TeV like a drop of AA with smaller size & radial flow

SMC: Space-Momentum correlation



# “Extension to bottom baryons

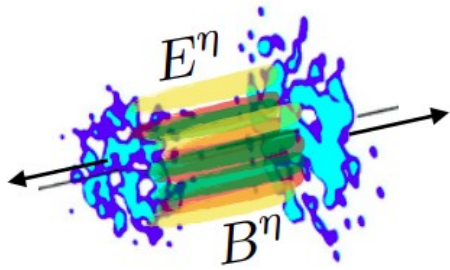
V. Minissale et al., [2405.19244](#) [hep-ph]



➤ Similar but even larger  $\Lambda_b/B$  than  $\Lambda_c/D$

➤ Extension of coalescence probability in  $p_T$  about proportional to the heavy quark mass

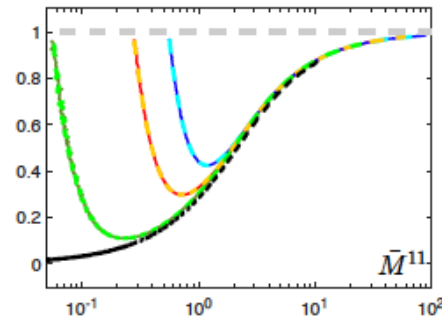
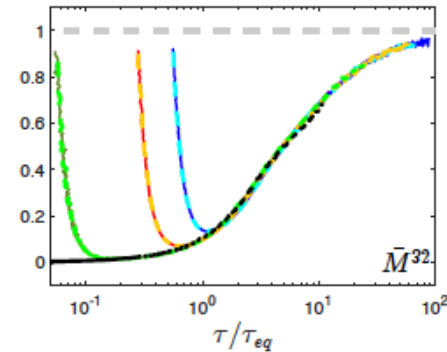
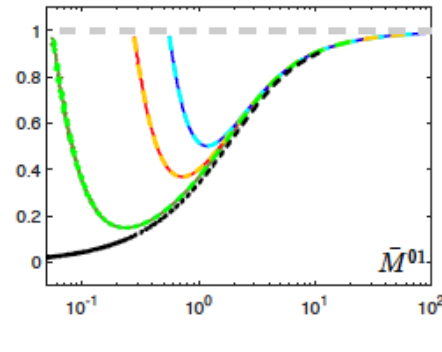
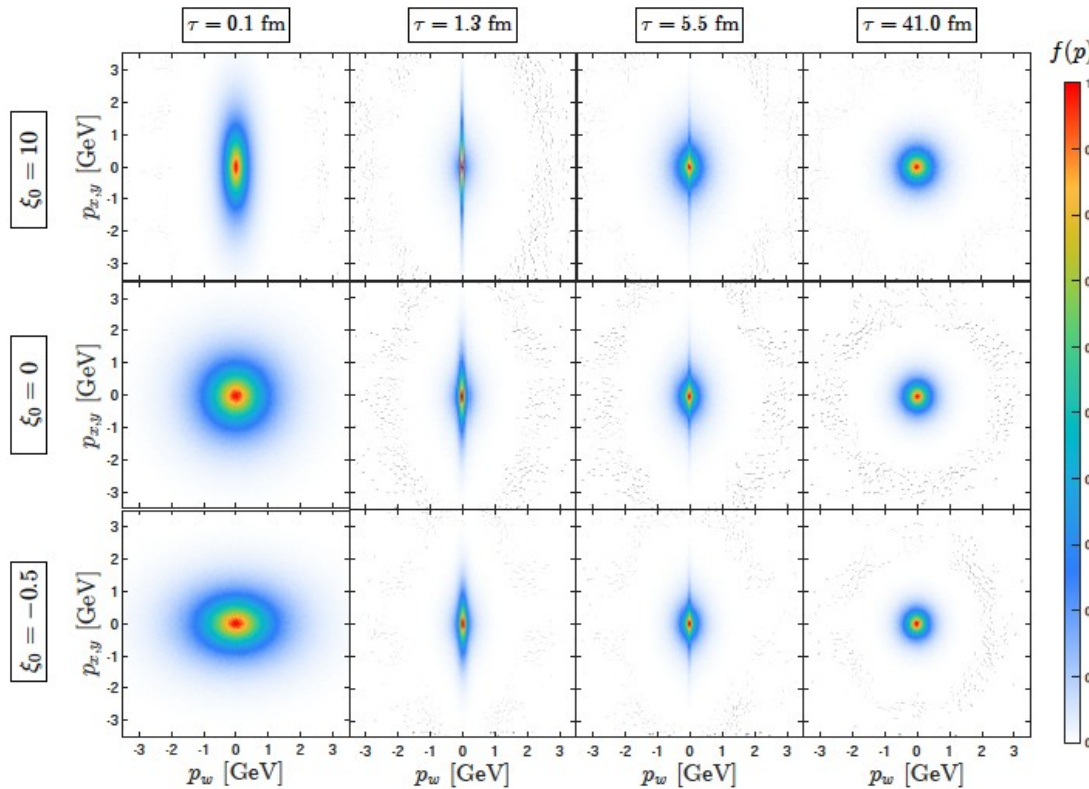
# Very early stage dynamics



$$p^\mu \partial_u f_a(x, p) + m(x) \partial_u^x m(x) \partial_\nu^\mu f_q(x, p) = C[f_q, f_g]$$

$$\mathcal{M}^{mn}(\tau) = \int dP (p \cdot u)^n (p \cdot z)^{2m} f(\tau, p).$$

transverse to flow\* longitudinal



	$4\pi\eta/s$	$\tau_0$ [fm]	ratio[fm]
—	1	0.1	0.1
- - -	2	0.2	0.1
—	4	0.2	0.05
- - -	2	0.1	0.05
—	10	0.1	0.01
- - -	5	0.05	0.01
—	attractor		

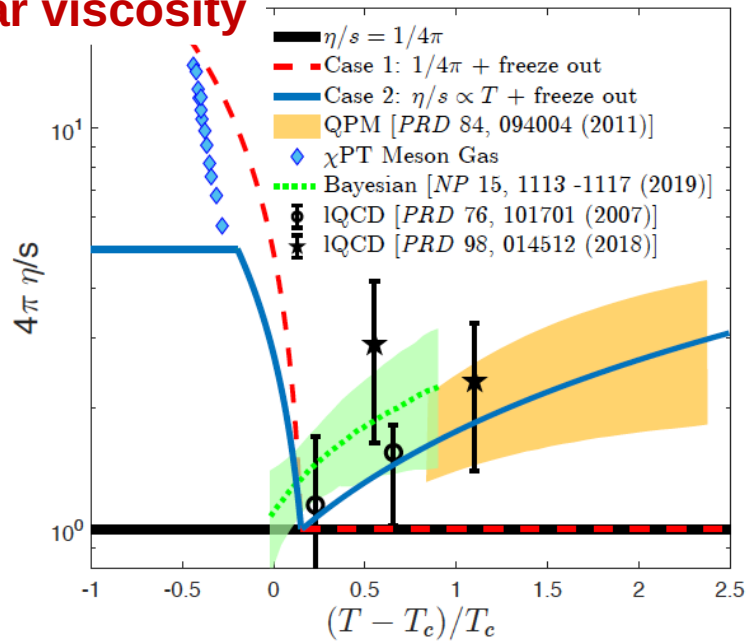
Evolution of the moments of the distribution function

Simulation in 1+1D

How sensitive we are to “unknown” initial conditions and early stage attractions?

# Impact of transition to hadronic matter

## Shear viscosity



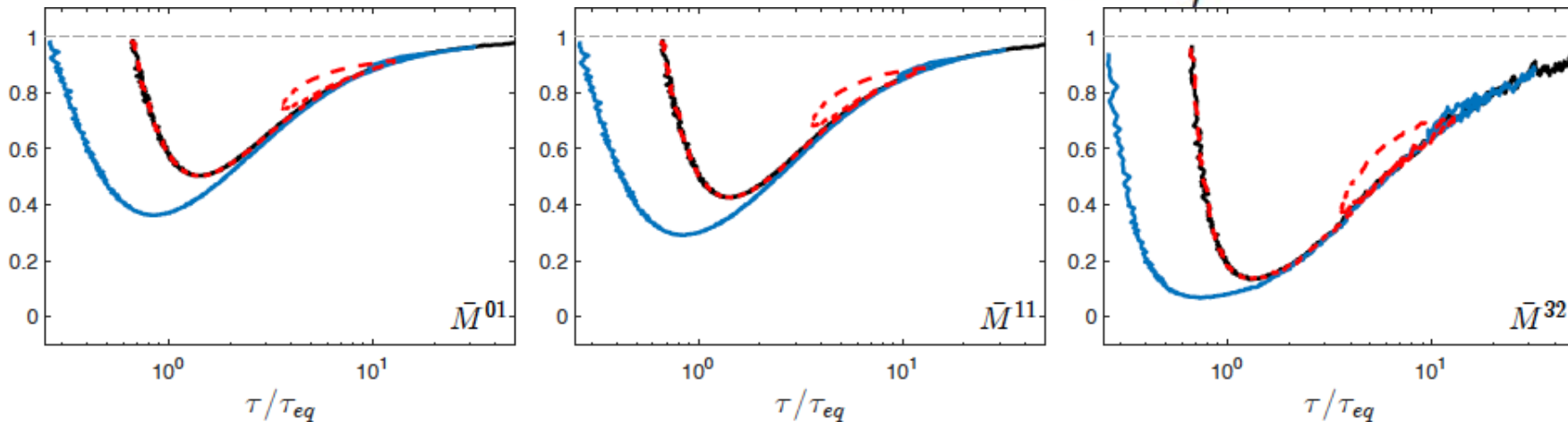
Even the strong rise of the shear viscosity at the transition to hadronic matter ( $\rightarrow$  increase of equil. time) does not break the evolution toward equilibration

$$\tau_{eq} = 5(\eta/s)/T(\tau)$$

V. Nugara et al., 2311.11921 [hep-ph]

## Moments $M^{mn}$ normalized to equilibrium values

$$\mathcal{M}^{mn}(\tau) = \int dP (p \cdot u)^n (p \cdot z)^{2m} f(\tau, p).$$





# Attività SIM 2024-26

- ❖ Develop a relativistic event-by-event transport theory suitable to perform realistic simulations of relativistic HIC's from AA to pA collisions.
  - Study the existence of dynamical attractors in 3+1 D
  - Heavy Quark dynamics in a unified frameworks in pA and AA(extension to b quarks)
  - Early stage Heavy Quark in the Glasma (collaboration with INFN-CT)
- ❖ Hadronization: coalescence+fragmentation to predict different charmed hadrons like D mesons  $\Lambda_c$ ,  $\Xi_c$  and  $\Omega_c$  baryons as well as multi-charm baryons ( $\Xi_{cc}$ ,  $\Omega_{cc}$  and  $\Omega_{ccc}$ )
  - to different colliding systems from Pb+Pb to Kr+Kr, Ar+Ar and pA collisions (ALICE3)
- Explore impact of open quantum system techniques in high energy physics on quantum computing (NQSTI – PNRR)

# FTE: SIM (6.0)<sup>5.9 in 2023</sup>

---

cognome	nome	contratto	profilo	perc	sezione
<b>Asta</b>	<b>Angelo</b>	Associato	Dottorando III (proroga)	100%	LNS
<b>Coci</b>	<b>Gabriele</b>	Associato	RTDA-PNRR	10%	LNS
<b>Greco</b>	<b>Vincenzo</b>	Associato	Prof. Ordinario	90%	LNS
<b>Nugara</b>	<b>Vincenzo</b>	Associato	Dottorando III	100%	LNS
<b>Parisi</b>	<b>Gabriele</b>	Associato	Dottorando III	100%	LNS
<b>Plumari</b>	<b>Salvatore</b>	Associato	Prof. Associato	100%	LNS
<b>Sambataro</b>	<b>Maria Lucia</b>	Associato	Assegnista	100%	LNS

# Budget (in k€)

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	Missioni	Inviti	Seminari	Consumi	Inventariabile	Totale
<b>Dotazioni</b>	<b>9</b>	<b>5</b>	<b>4</b>	<b>4</b>	<b>7</b>	<b>29</b>
<b>MONSTRE</b>	<b>9</b>	<b>-</b>	<b>-</b>	<b>-</b>	<b>-</b>	<b>9</b>
<b>SIM</b>	<b>14</b>	<b>-</b>	<b>-</b>	<b>-</b>	<b>-</b>	<b>14</b>
<b>Totale</b>	<b>30</b>	<b>5</b>	<b>4</b>	<b>4</b>	<b>7</b>	<b>52</b>



