



UNIVERSITY of
ROCHESTER

LABORATORY FOR
LASER ENERGETICS
UNIVERSITY OF ROCHESTER 

Overview on tests and applications of strong-field QED with multi PW lasers

Antonino Di Piazza

Workshop on “Fundamental research and applications
with the EuPRAXIA facility at LNF”
Frascati, December 05, 2024

Outline

- The electromagnetic interaction
- The quantum vacuum and the critical fields of QED
- Strong-field QED in an intense laser field
- Radiation reaction in a nutshell
- Vacuum-polarization effects in a nutshell
- Flying-focus beams: a new tool to study strong-field QED
- The multipetawatt laser facility NSF OPAL
- Conclusions
- Reviews on strong-field QED:
 1. A. Di Piazza et al., Rev. Mod. Phys. **84**, 1177 (2012)
 2. B. King and T. Heinzl, High Power Laser Sci. Eng. **4**, e5 (2016)
 3. T. G. Blackburn, Rev. Mod. Plasma Phys. **4**, 5 (2020)
 4. F. Karbstein, Particles **3**, 39 (2020)
 5. A. Gonoskov et al., Rev. Mod. Phys. **94**, 045001 (2022)
 6. A. M. Fedotov et al., Phys. Rep. **1010**, 1 (2023)

The electromagnetic interaction

- Quantum electrodynamics (QED) is the relativistic quantum theory describing the interaction among electric charges
- By considering the lightest electric charges, electrons and positrons, the basic scales of QED are obtained by combining the electron charge e and mass m , together with c and \hbar :

Strength: $\alpha = e^2 / 4\pi\epsilon_0 \hbar c = 7.3 \times 10^{-3}$ (Fine-structure constant)	Energy: $mc^2 = 0.51 \text{ MeV}$ (Electron rest energy)
Length: $\lambda_C = \hbar / mc = 3.9 \times 10^{-11} \text{ cm}$ (Compton wavelength)	Electromagnetic field: $E_{cr} = m^2 c^3 / \hbar e = 1.3 \times 10^{16} \text{ V/cm}$ $B_{cr} = m^2 c^3 / \hbar e = 4.4 \times 10^{13} \text{ G}$ (Critical fields of QED)

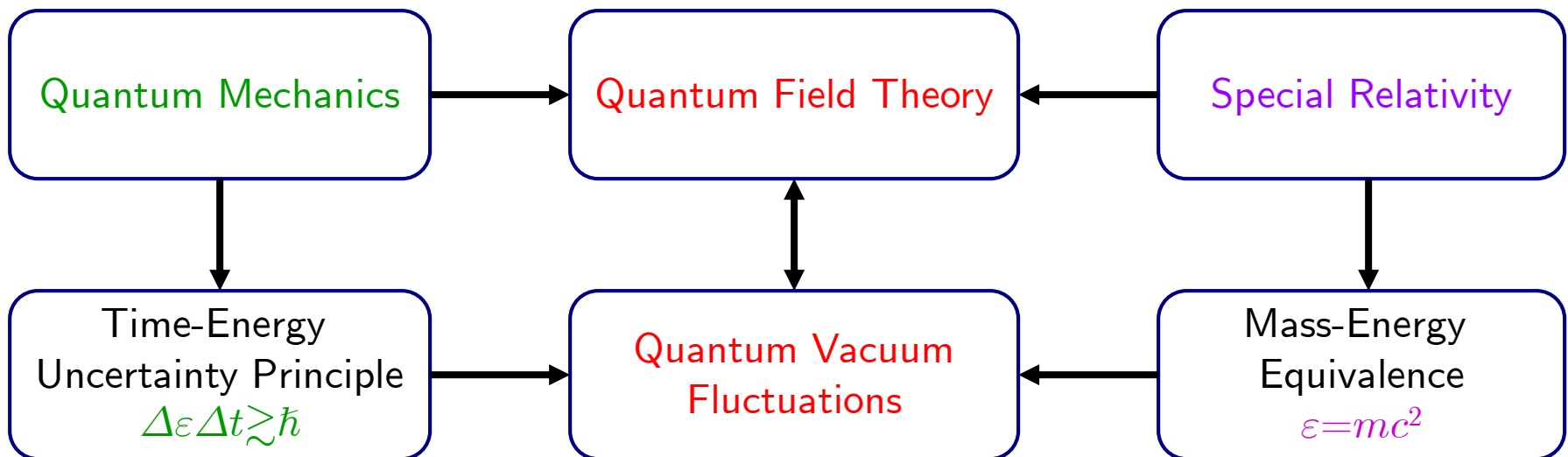
- Critical laser intensity of QED:

$$I_{cr} = cE_{cr}^2 = 4.6 \times 10^{29} \text{ W/cm}^2$$

World-record intensity: 10^{23} W/cm^2 (Yoon et al. 2021)

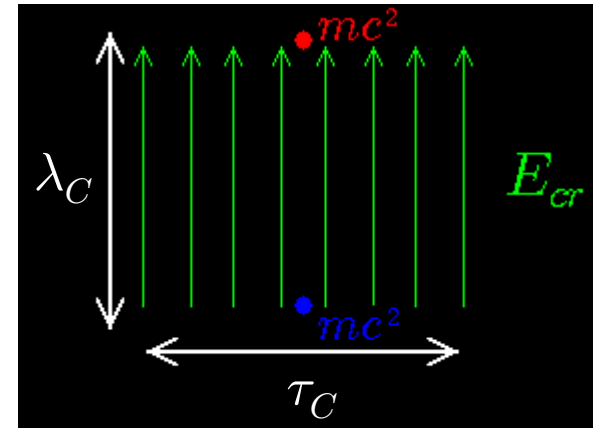
The quantum vacuum and the critical fields of QED

- The vacuum state is the lowest-energy state of the theory, where no particles are present
- In quantum field theory
 - “Fluctuations” of particles-antiparticles are present in the vacuum
 - They cover a very short distance and annihilate again after a very short time (in the case of electrons and positrons $\lambda_C = \hbar/mc \sim 10^{-11}$ cm and $\tau_C = \lambda_C/c = \hbar/mc^2 \sim 10^{-21}$ s, respectively)



- Physical meaning of the critical fields:

$$|e|E_{cr} \times \frac{\hbar}{mc} = mc^2$$



- Vacuum instability and electromagnetic cascades (Bell et al., PRL 2008, Bulanov et al., PRL 2010, Fedotov et al., PRL 2010)
- The interaction energy of a Bohr magneton with a magnetic field of the order of B_{cr} is of the order of the electron rest energy
- In the presence of background electromagnetic fields of the order of the critical ones a new regime of QED, **the strong-field QED regime**, opens:
 - where **the properties of the vacuum are substantially altered by the fields**
 - where a tight interplay unavoidably exists between collective (plasma-like) and quantum effects
 - which is **unaccessible to conventional accelerators because it requires coherent fields**

Strong-field QED in an intense laser field

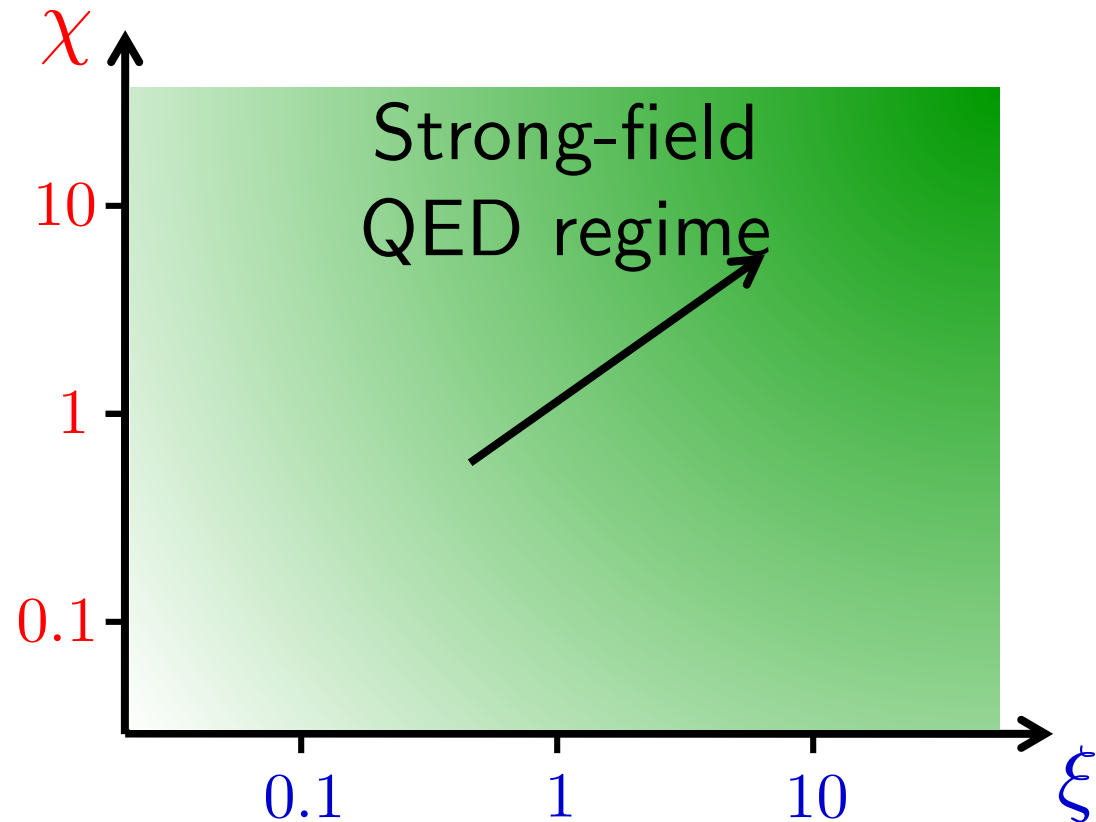
- An electron with energy ε collides head-on with a plane wave with amplitude E_L and angular frequency ω_L (wavelength λ_L)



- The physical observables depend on the two Lorentz- and gauge-invariant parameters

$$\xi = \frac{1}{2\pi} \frac{|e|E_L\lambda_L}{mc^2} = \frac{|e|E_L\lambda_C}{\hbar\omega_L}$$

$$\chi = \frac{E_L}{E_{cr}} \Big|_{\text{rest frame}} \approx \frac{2\varepsilon}{mc^2} \frac{E_L}{E_{cr}}$$



Optical laser technology

Optical laser technology ($\hbar\omega_L \sim 1$ eV, $\lambda_L \sim 1$ μm)	Energy (J)	Pulse duration (fs)	Spot radius (μm)	Intensity (W/cm ²)
Experiments (Astra Gemini, CoReLS)	10	40	2.5	4×10^{20}
Facilities (APOLLON, ELI Beamlines, ELI-NP, ZEUS etc...)	10 ÷ 100	10 ÷ 20	1	$10^{21} \div 10^{22}$
Record intensity (CoReLS, 2021)	50	20	1.1	1.1×10^{23}
Future projects (NSF OPAL)	2×500	20	1.3	5×10^{23}

Electron accelerator technology

Electron accelerator technology	Energy (GeV)	Beam duration (fs)	Spot radius (μm)	Number of electrons
Conventional accelerators (SLAC)	50	3×10^3	1	4×10^{10}
Laser-plasma accelerators (LBNL)	7.8	35	40	3×10^7

Message: Present technology allows for the experimental investigation of strong-field QED

$$\xi = 7.5 \frac{\sqrt{I_L [10^{20} \text{ W/cm}^2]}}{\hbar\omega_L [\text{eV}]}$$

$$\chi = 5.9 \times 10^{-2} \varepsilon [\text{GeV}] \sqrt{I_L [10^{20} \text{ W/cm}^2]}$$

Radiation reaction in a nutshell

Units with $\epsilon_0 = \hbar = c = 1$

- Accelerated electric charges emit electromagnetic radiation (relativistic Larmor formula, s is the electron's proper time)

$$\frac{d\mathcal{E}}{dt} = -\frac{2}{3} \frac{e^2}{4\pi} \frac{du^\mu}{ds} \frac{du_\mu}{ds}$$
- The exact dynamics of the electron in an external field includes the effects of this energy loss (and of the related momentum loss)
- By adding an extra force to the Lorentz equation due to the field produced by the electron itself, one can obtain the Lorentz-Abraham-Dirac (LAD) equation

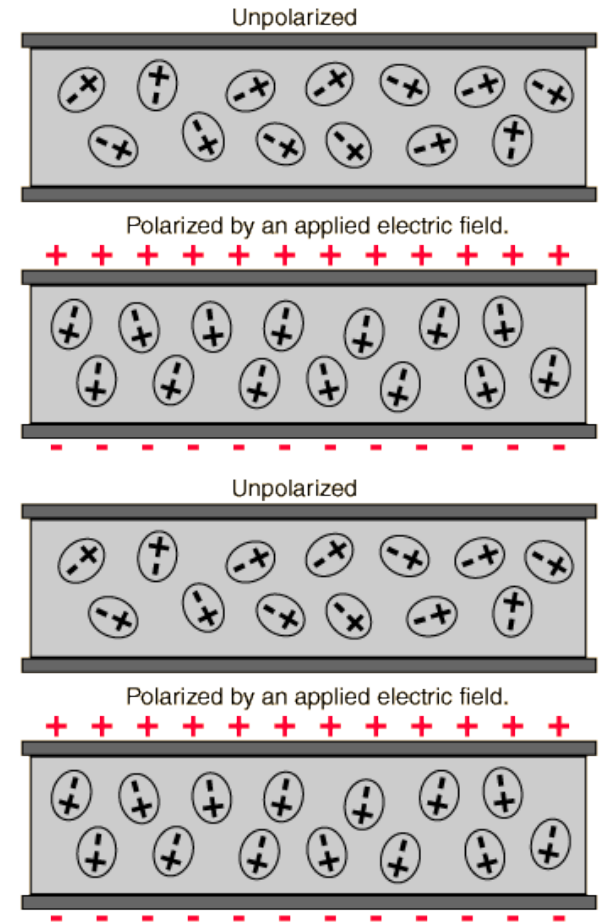
$$m \frac{du^\mu}{ds} = e F^{\mu\nu} u_\nu + \frac{2}{3} \frac{e^2}{4\pi} \left(\frac{d^2 u^\mu}{ds^2} + \frac{du^\nu}{ds} \frac{du_\nu}{ds} u^\mu \right)$$
- The LAD equations features physical inconsistencies (runaway solutions, violation of causality) essentially due to the Schott term
- Landau and Lifshitz noticed that within classical electrodynamics a “reduction of order” can be carried out:

$$\frac{du^\mu}{ds} \approx \frac{e}{m} F^{\mu\nu} u_\nu \quad \text{in} \quad \frac{2}{3} \frac{e^2}{4\pi} \left(\frac{d^2 u^\mu}{ds^2} + \frac{du^\nu}{ds} \frac{du_\nu}{ds} u^\mu \right)$$
- One obtains the Landau-Lifshitz (LL) equation

$$m \frac{du^\mu}{ds} = e F^{\mu\nu} u_\nu + \frac{2}{3} \frac{e^2}{4\pi} \left[\frac{e}{m} (\partial_\alpha F^{\mu\nu}) u^\alpha u_\nu - \frac{e^2}{m^2} F^{\mu\nu} F_{\alpha\nu} u^\alpha + \frac{e^2}{m^2} (F^{\alpha\nu} u_\nu) (F_{\alpha\lambda} u^\lambda) u^\mu \right]$$
- Experiments on radiation reaction in intense laser fields: Cole et al., 2018, Poder et al., 2018, Los et al., 2024

Vacuum-polarization effects in a nutshell

- Due to the presence of the virtual electron-positron pairs, the vacuum according to QED behaves as a birefringent medium
- Dichroic/absorptive effects come into play when pair production becomes sizable
- For fields with wavelengths much larger than the $\lambda_C \approx 3.9 \times 10^{-7} \mu\text{m}$, vacuum-polarization effects are local
- They can be described as if the vacuum features two refractive indexes depending on the mutual polarization of polarizing and probe fields
- Examples of vacuum refractive indexes for a background electromagnetic field (\mathbf{E}, \mathbf{B}) and a probe propagating along the direction \mathbf{n} and polarized either along \mathcal{E} or along \mathcal{B} ($I_{cr} \sim 10^{29} \text{ W/cm}^2$)



$$\mathcal{E} = \mathbf{E} - (\mathbf{n} \cdot \mathbf{E})\mathbf{E} + \mathbf{n} \times \mathbf{B}$$

$$n_{\mathcal{E}} = 1 + \frac{4\alpha}{90\pi} \frac{(\mathbf{n} \times \mathbf{E})^2 + (\mathbf{n} \times \mathbf{B})^2 - 2\mathbf{n} \cdot (\mathbf{E} \times \mathbf{B})}{I_{cr}}$$

$$\mathcal{B} = \mathbf{B} - (\mathbf{n} \cdot \mathbf{B})\mathbf{B} - \mathbf{n} \times \mathbf{E}$$

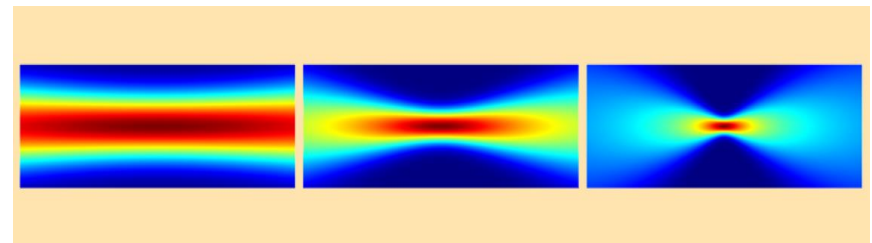
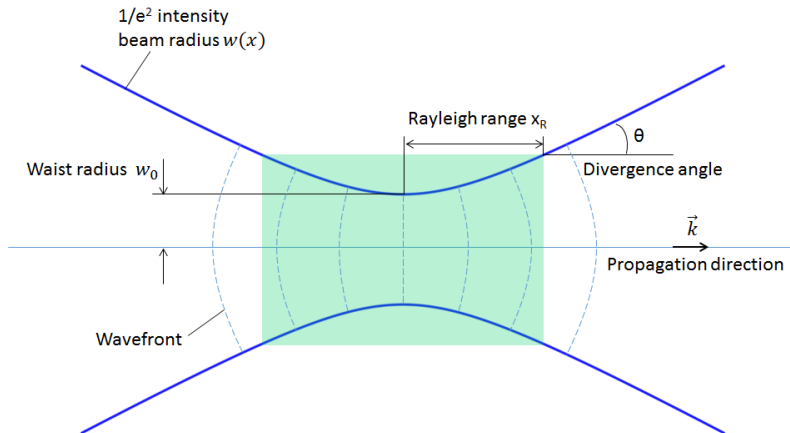
$$n_{\mathcal{B}} = 1 + \frac{7\alpha}{90\pi} \frac{(\mathbf{n} \times \mathbf{E})^2 + (\mathbf{n} \times \mathbf{B})^2 - 2\mathbf{n} \cdot (\mathbf{E} \times \mathbf{B})}{I_{cr}}$$

A limitation of Gaussian beams for SFQED

- The expressions of the classical and quantum nonlinearity parameters show that strong-field QED effects benefit from **high laser intensities**
- Interesting effects, like radiation reaction and vacuum birefringence, also depend on **how long particles experience strong fields**
- Gaussian laser beams feature an **intrinsic limitation**: at a given power, the more one focuses the beam to increase the intensity, the shorter becomes the longitudinal region where the field is strong

$$\xi = \frac{1}{2\pi} \frac{|e|E_L \lambda_L}{mc^2} = \frac{|e|E_L \lambda_C}{\hbar\omega_L}$$

$$\chi = \frac{E_L}{E_{cr}} \Big|_{\text{rest frame}} \approx \frac{2\varepsilon}{mc^2} \frac{E_L}{E_{cr}}$$



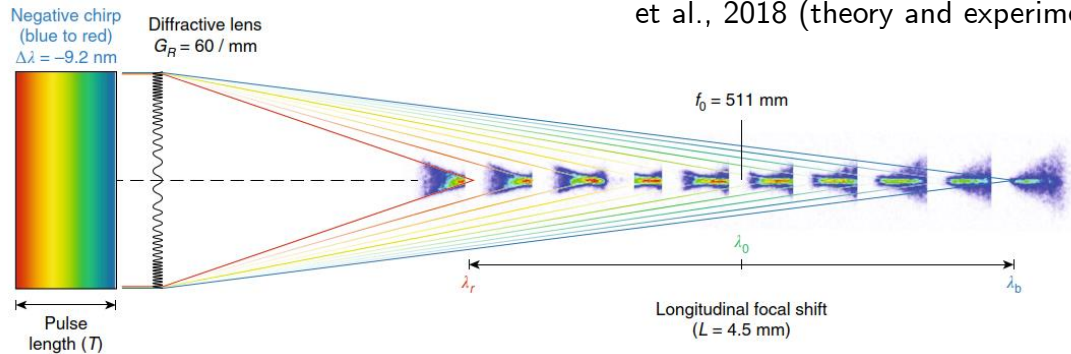
$$E_y(t, \mathbf{r}) = B_z(t, \mathbf{r})$$

$$= E_0 \frac{e^{-r_{\perp}^2/w^2(x)}}{w(x)} \sin \left[\omega(t - x) - \frac{\omega x r_{\perp}^2}{x^2 + x_R^2} + \psi_0 \right]$$

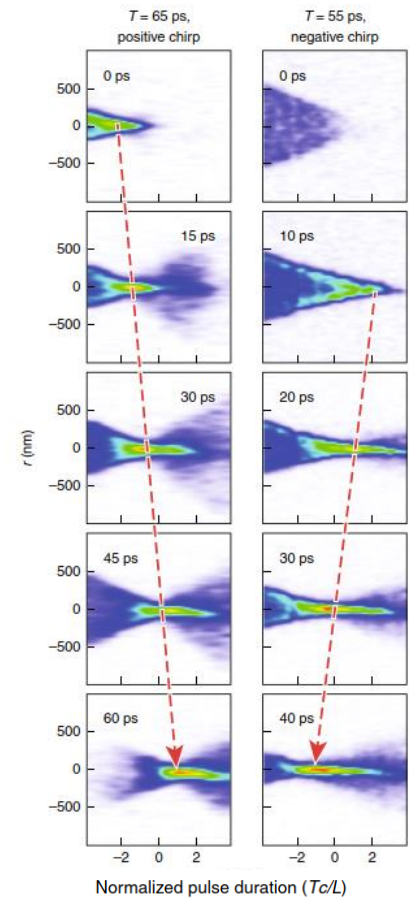
$$r_{\perp} = \sqrt{y^2 + z^2}, \quad w(x) = w_0 \sqrt{1 + \frac{x^2}{x_R^2}}, \quad x_R = \frac{\omega w_0^2}{2}$$

Flying-focus beams

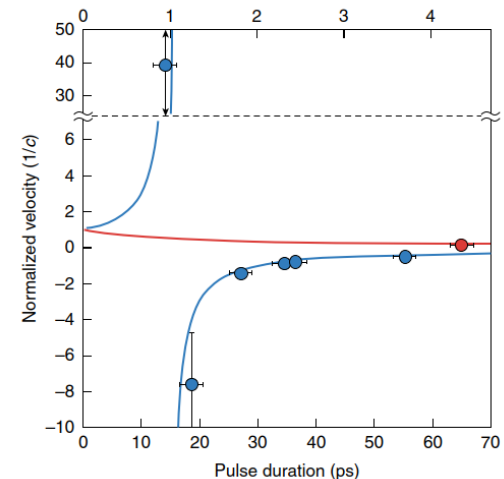
- One can overcome the limitation of a Gaussian beam and **control the focal position by using**, e.g., a **chirped pulse** (the frequency content of the pulse depends on time) and a **chromatic lens** (different frequencies are focused at different points)



Saint-Marie et al., 2017 (theory) and Froula et al., 2018 (theory and experiment)



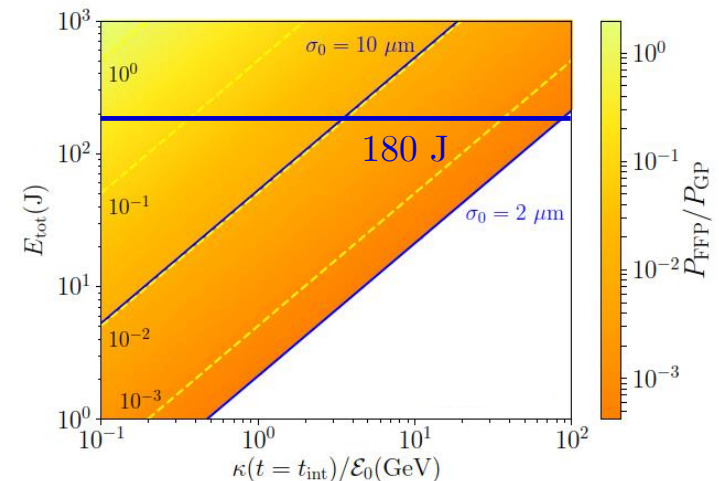
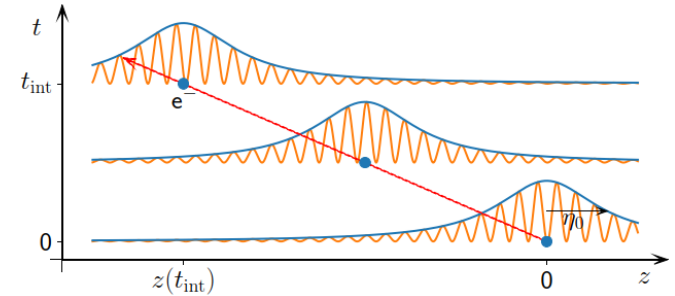
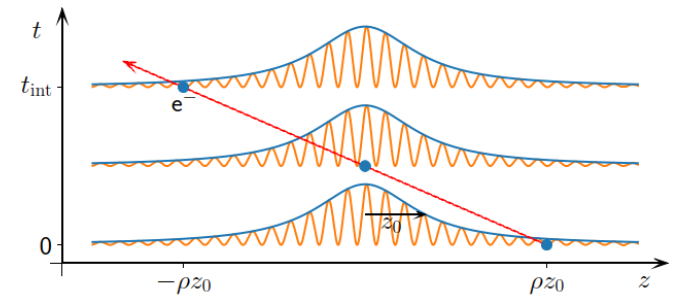
- The velocity of such a “flying-focus” pulse can be controlled, can be either positive or negative and the case $v_f \approx -1$ was demonstrated experimentally
- To sustain the pulse over a long length high energies are required



- The idea of using a flying-focus pulse with focus moving at the speed of light in the opposite direction of the phase velocity can be exploited in different contexts
- Classical radiation reaction sizable at relatively low laser powers (Formanek et al. PRA 2022)
- Energy loss due to radiation reaction:

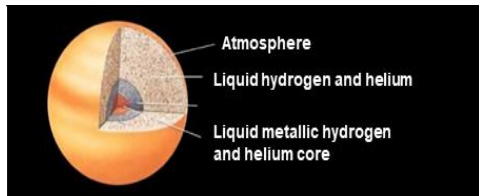
$$\varepsilon(t) \approx \frac{\varepsilon_0}{1 + \frac{4\varepsilon_0}{3m} r_e \omega_0^2 \int_0^t g^2(t') \xi^2(t') dt'} = \frac{\varepsilon_0}{1 + \kappa(t)}$$

- The energy loss depends on the laser energy per unit surface ($\kappa(t) \sim \xi_0^2 t$)
- A flying-focus allows for the same energy losses than a Gaussian beam but at much lower power
- Numerical results for $t_{\text{int}} = 100$ ps (corresponding to $\sim 60,000$ oscillations)
- Similar conclusions hold for vacuum-polarization effects

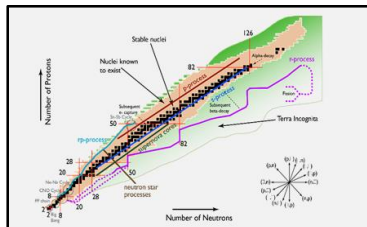


NSF OPAL: a laser design project funded by NSF and guided by the most pressing scientific questions in the four research areas

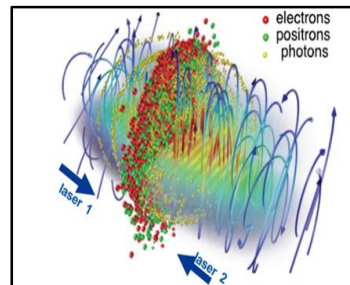
Laboratory Astrophysics and Planetary Physics (LAPP)



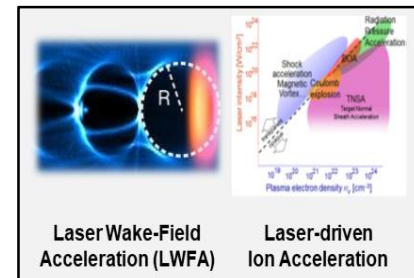
Laser-Driven Nuclear Physics (LDNP)



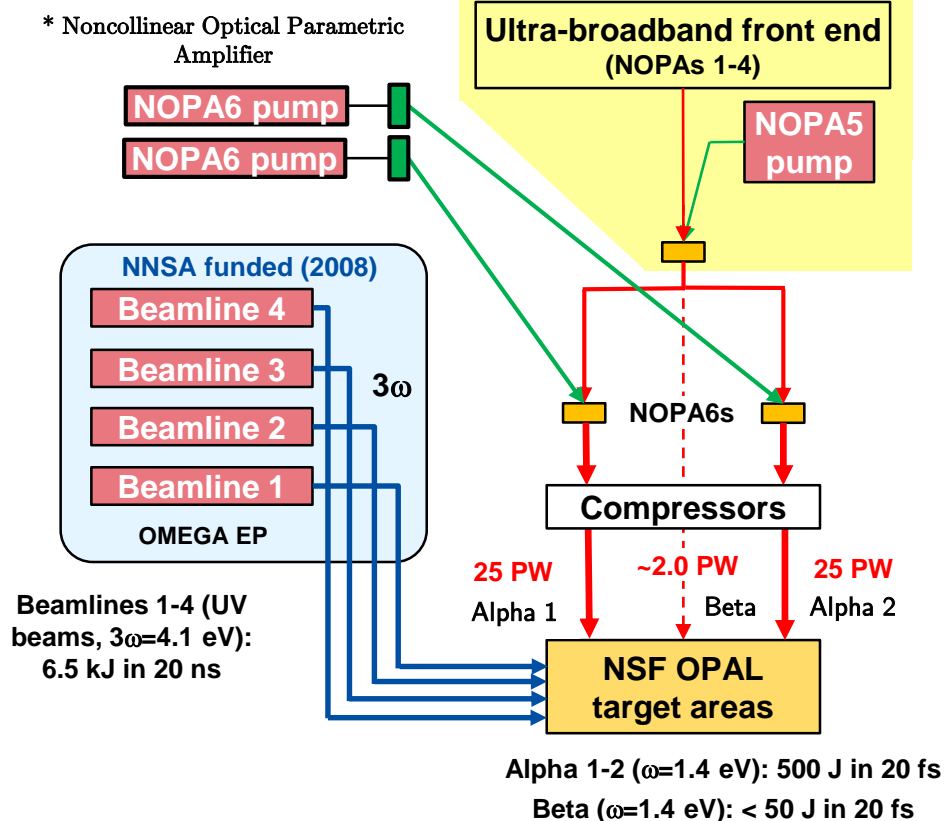
High-Field Physics and Quantum Electrodynamics (HFP/QED)



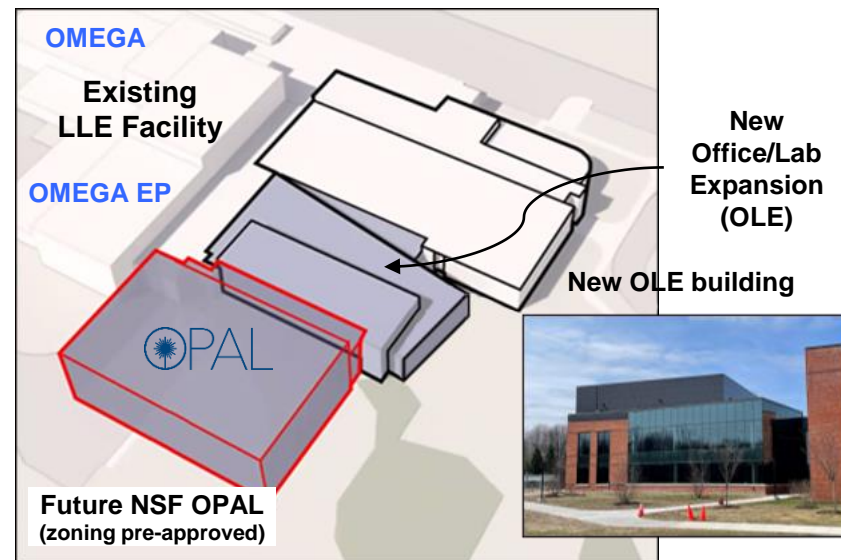
Particle Acceleration and Advanced Light Sources (PAALS)



Laser system



Construction site



The two buildings would house NSF OPAL, plus labs and offices for new research

Conclusions

- Modern lasers offer a unique possibility to access new extreme regimes of interaction of light with matter and can be used **as a new tool, alternative to conventional accelerators, for investigating fundamental physics and quantum electrodynamics in still uncharted regimes**
- **Flying-focus beams** are laser beams where the focus moves with controllable velocity
- We have proposed to exploit the unique properties of **flying-focus beams as a tool to test strong-field effects like radiation-reaction and vacuum-polarization** effects under controlled conditions at relatively low laser powers/intensities
- NSF has awarded funding to design **NSF OPAL**: a two, 25-PW laser system at the LLE for investigating plasma physics, nuclear physics, strong-field QED etc...

A post-doc position is available in my group at the University of Rochester starting at any time



If you are interested, please contact me at
a.dipiazza@rochester.edu