

Seismic Isolation of GW detectors



V. Boschi

valerio.boschi@pi.infn.it

Istituto Nazionale di Fisica Nucleare (INFN)

Introduction

Virgo and LIGO sensitivity

Imagine to drop a glass of wine (or water) in the ocean.....

Ocean Surface (S):

$$70\% \times 4\pi \times R_{\text{terra}}^2 =$$
$$0.7 \times 4 \times 3.14 \times (6.37e6 \text{ m})^2$$
$$\sim 3.6e14 \text{ m}^2$$

Volume of the glass (V):

$$\sim 0.25e-3 \text{ m}^3$$



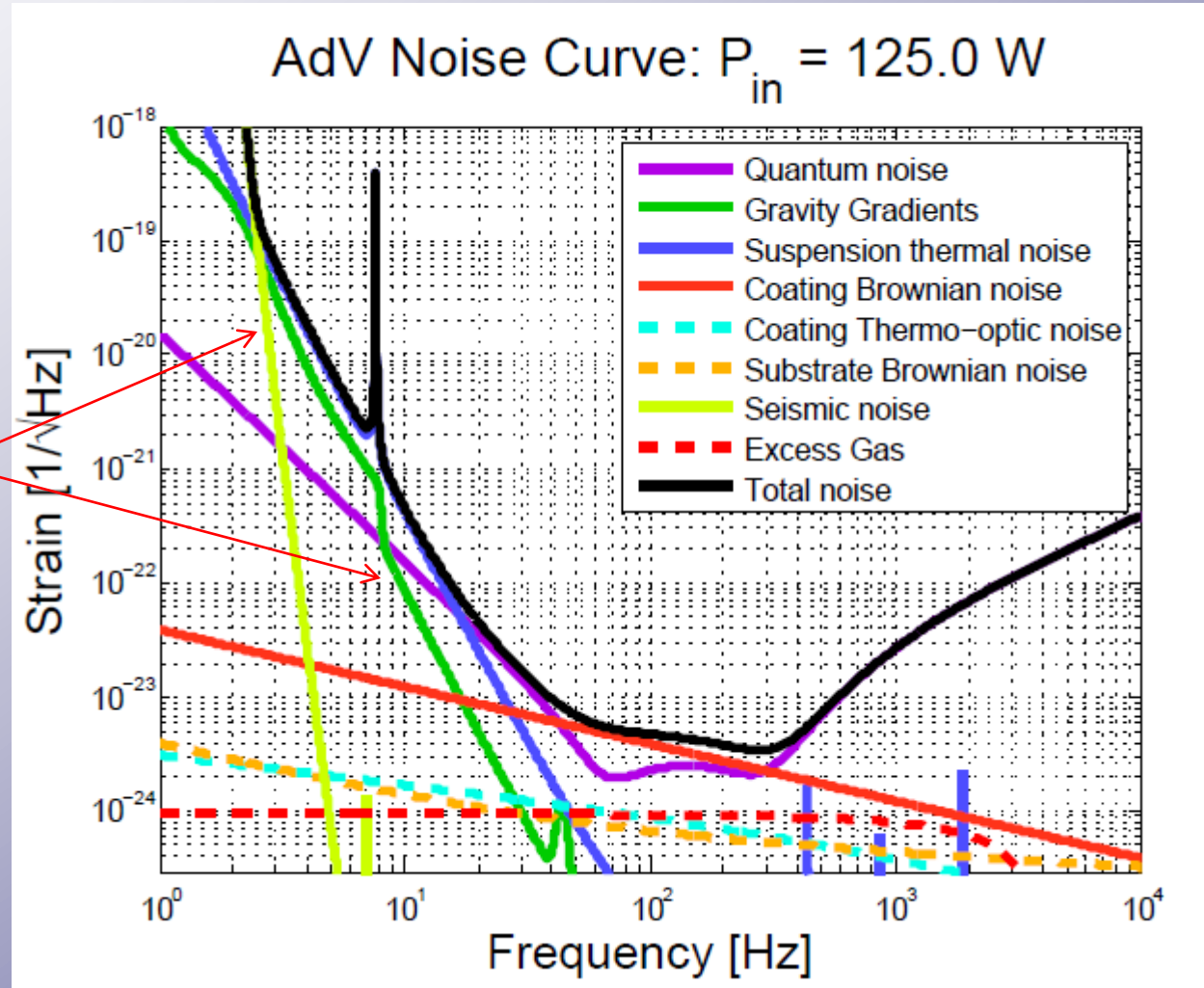
Increase of the global sea level:
 $h \sim V / S \sim 1e-18 \text{ m}$

This is the level of sensitivity we need to reach with GW detectors !!

Introduction

AdVirgo Noise Budget

Newtonian and Seismic noise dominate at low frequency



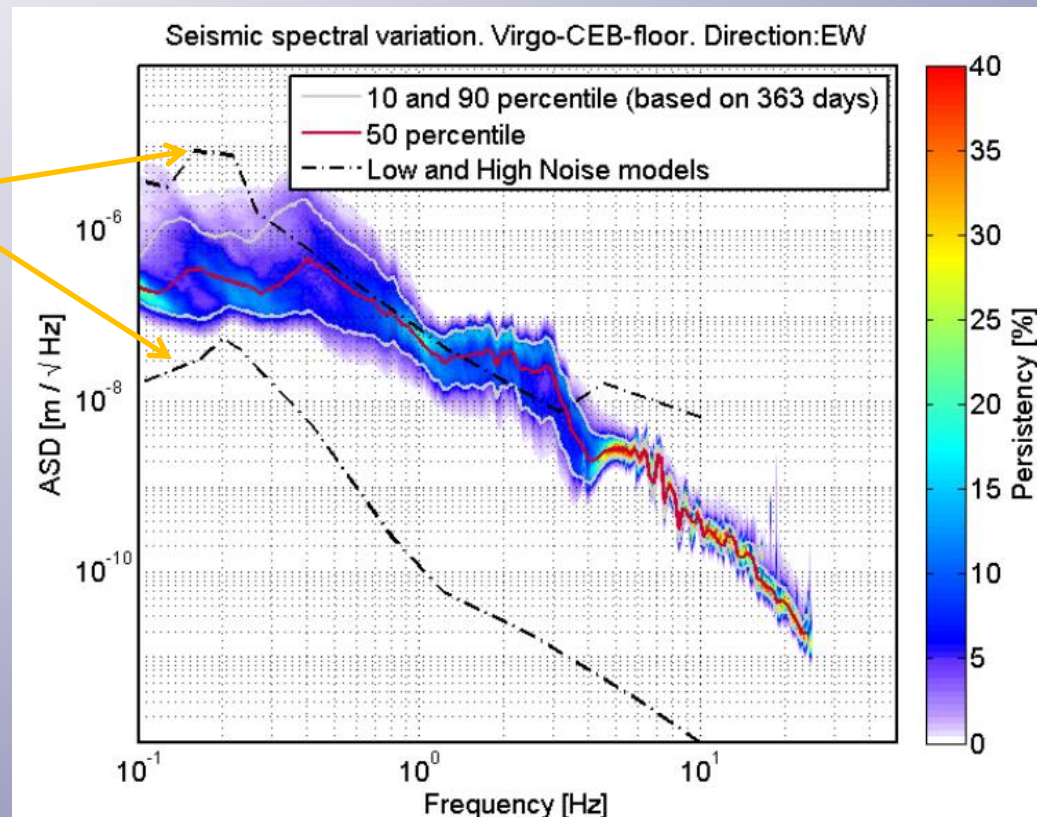
Introduction

Seismic Noise on Earth

- Seismic noise has both natural and human origins and can vary by few orders of magnitude from site to site.
- All ground motion displacement spectra observed worldwide share some common characteristics: they have essentially the same amplitude in all three orthogonal space directions and they exhibit a low pass behavior that follows the empirical law for $f > 0.1$ Hz

$$x(f) \sim A (1 \text{ Hz}/f)^2 \text{ m}/\sqrt{\text{Hz}}$$

Peterson's
High and Low
Noise Models

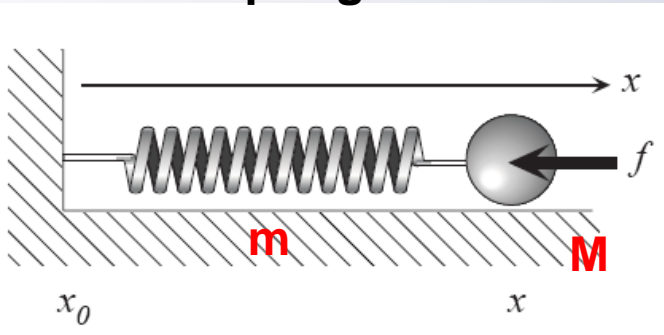


Introduction

Harmonic Oscillators as Mechanical filters

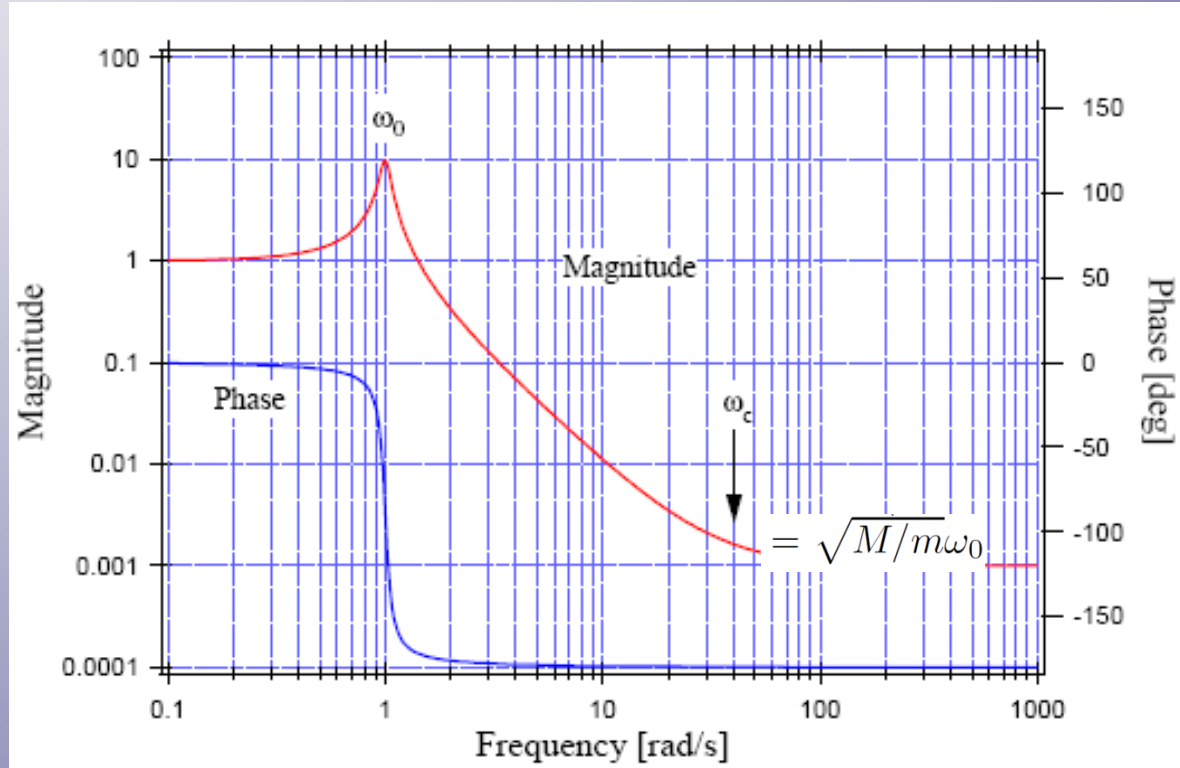
At frequencies higher than the oscillator resonance, the transfer function of an harmonic oscillator is equivalent to a second-order low pass filter.

Massive Spring



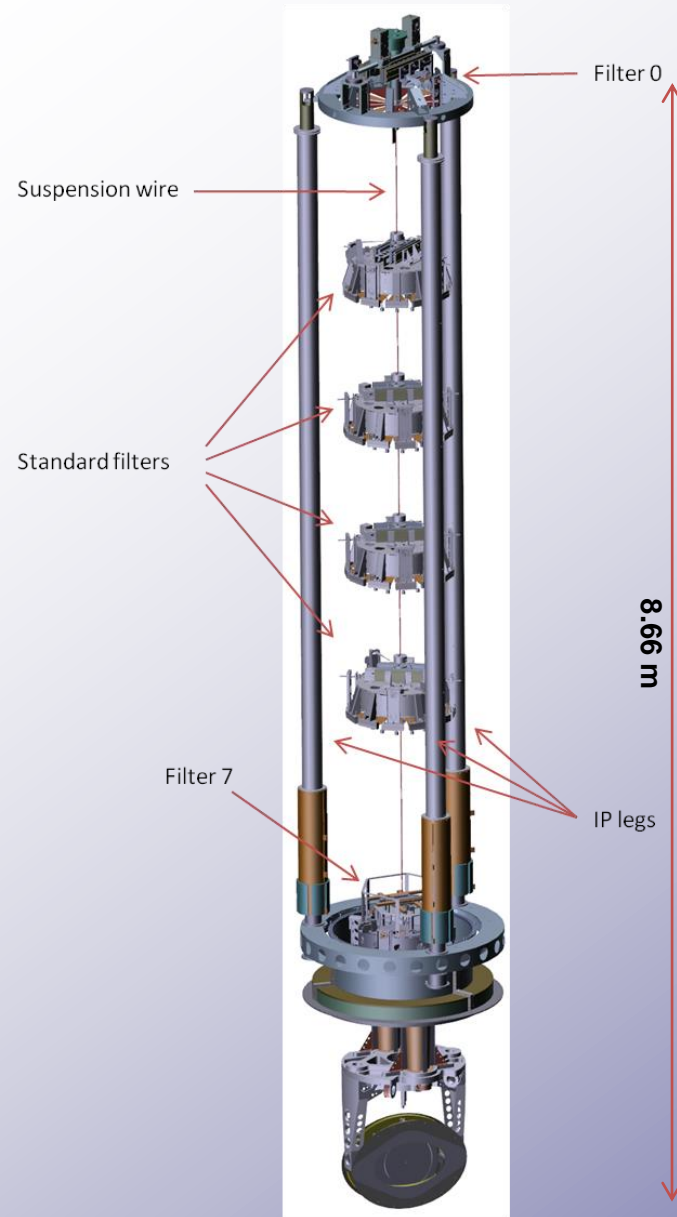
$$H_X = \frac{\omega_0^2(1 + i\phi) + \frac{m}{M}\omega^2}{\omega_0^2(1 + i\phi) - \omega^2 + i\frac{\gamma}{M}\omega}$$

Transfer Function



AdVirgo Superattenuator

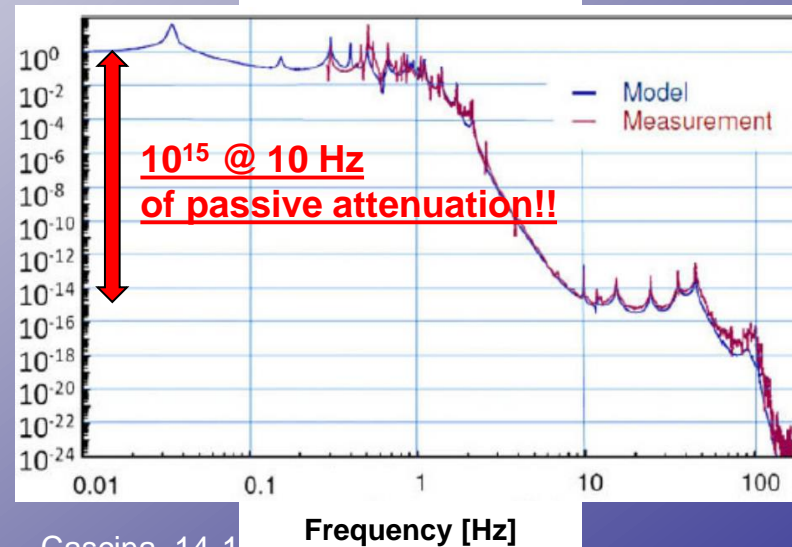
The superattenuator (SA)



The AdVirgo superattenuator (SA) is a complex mechanical device capable of providing more than **10 orders of magnitude of passive seismic isolation in all six degrees of freedom above a few Hz**

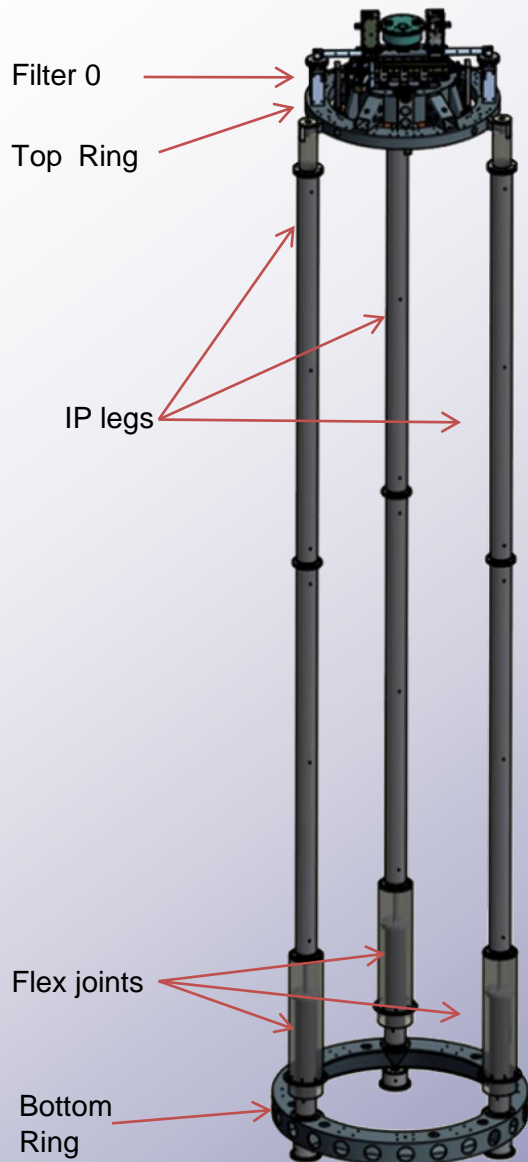
- The SA is a passive mechanical system constituted by a 5 stage pendulum supported by a 3-leg elastic pre-isolator called inverted pendulum (IP).
- All the normal mode resonance frequencies of the SA are kept below 2 Hz.
- The SA mechanical structure, consists of three fundamental parts: the inverted pendulum, the chain of standard filters, the payload.
- Mechanical design for AdVirgo is essentially the same of Virgo except for the payload.

Transfer function



AdVirgo Superattenuator

The inverted pendulum

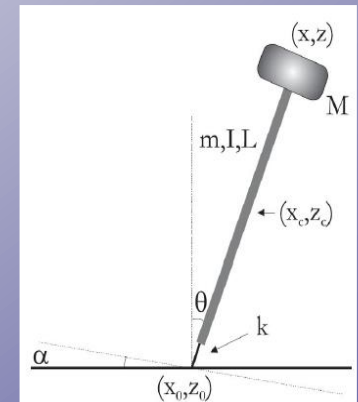


- A low frequency pre-isolator constituted of three 6 m-long hollow legs, each one connected to the ground through a flexible joint and supporting an interconnecting structure (the top ring) on its top.
- The structure horizontal normal modes are tuned at about 30-40 mHz.
- A simple mechanical model such as this

Gravitational Anti-spring

gives

$$\omega_0 = \frac{k - (M + m/2)g/L}{M + m/4 + I/L^2}$$

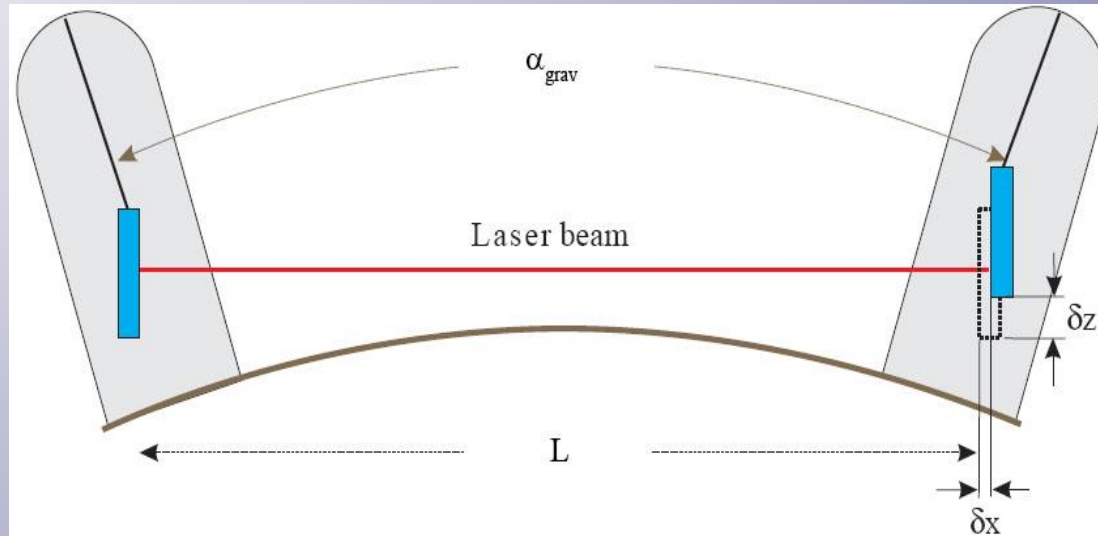


- Since the system is very soft, it requires very low forces to be moved:
for $f \ll f_0$ $F \simeq M\omega_0^2 x$
- The top ring is a mechanical support for an additional seismic filter, called filter 0, similar to those used in the chain.
- The filter 0 is equipped with a set of sensors and actuators, placed in a pinwheel configuration, that are used to actively damp the IP resonance modes.

AdVirgo Superattenuator

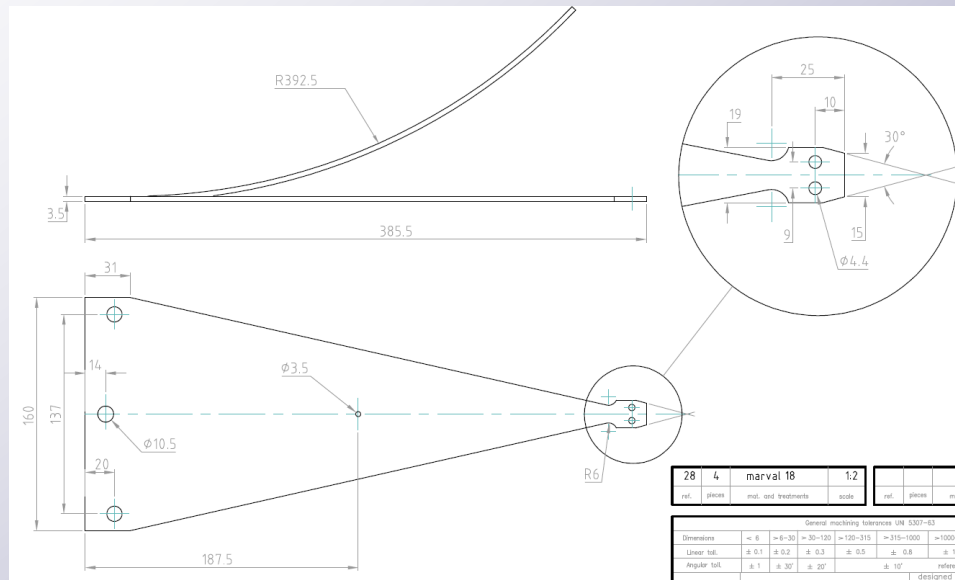
Why vertical attenuation ?

- The input and output mirrors of a Fabry-Perot cavity form an angle $\alpha_{\text{grav}} = L/r = 5 \cdot 10^{-4}$ rad (where $L = 3$ km is the cavity length and r is the Earth radius) with the global vertical direction. Therefore vertical displacement Δz has effect along the beam direction, producing a variation $\alpha_{\text{grav}} \cdot \Delta z$ of the optical path.
- The suspension system causes even larger mechanical couplings (1%), due to structural reasons.



AdVirgo Superattenuator

Vertical attenuation: Blades

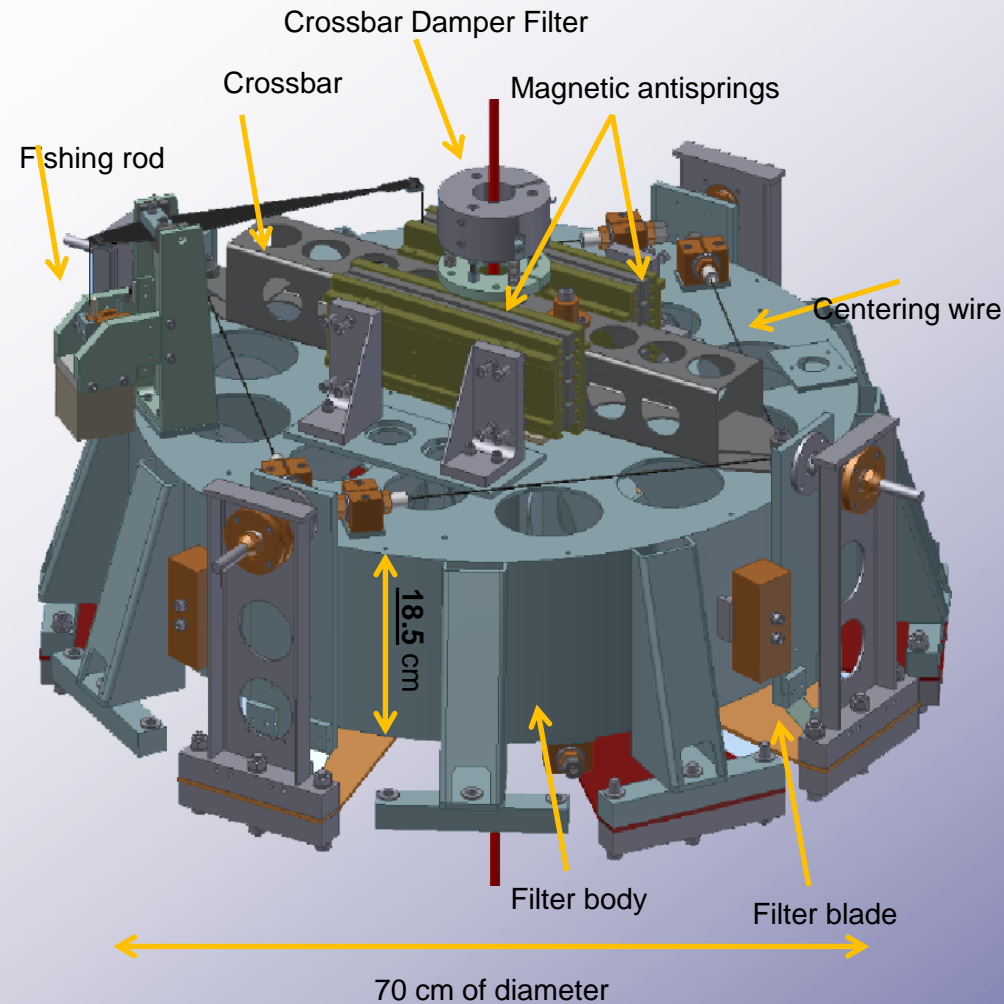


- All the maraging steel blades have a thickness of 3.5 mm, a length of 385.5 mm, while the width of the triangular base changes according with the load to be supported.
- The number of blades ranges from 12 (in the first filter of the chain) to 4 (in the filter 7) according to the suspended load. A total of 52 blades is needed for a long tower.
- The load M depends by the base width b , by the thickness t and length l with this law

$$M = \frac{Ebt^3}{12R_c gl}$$

AdVirgo Superattenuator

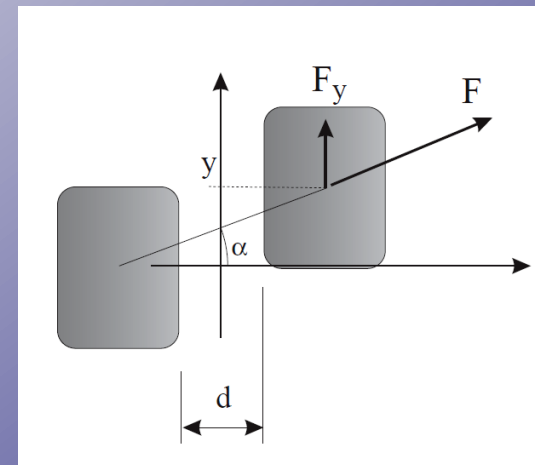
Vertical Attenuation: Standard filters



The first four pendulum stages of the SA are denominated Standard Filters (SFs).

The SF is essentially a rigid steel cylinder supporting a set of maraging steel cantilevered triangular blades clamped along the outer surface of the filter body.

A magnetic anti-spring system, assembled on each filter, is designed to reduce its fundamental vertical frequency from about 1.5 Hz down below 0.5 Hz.

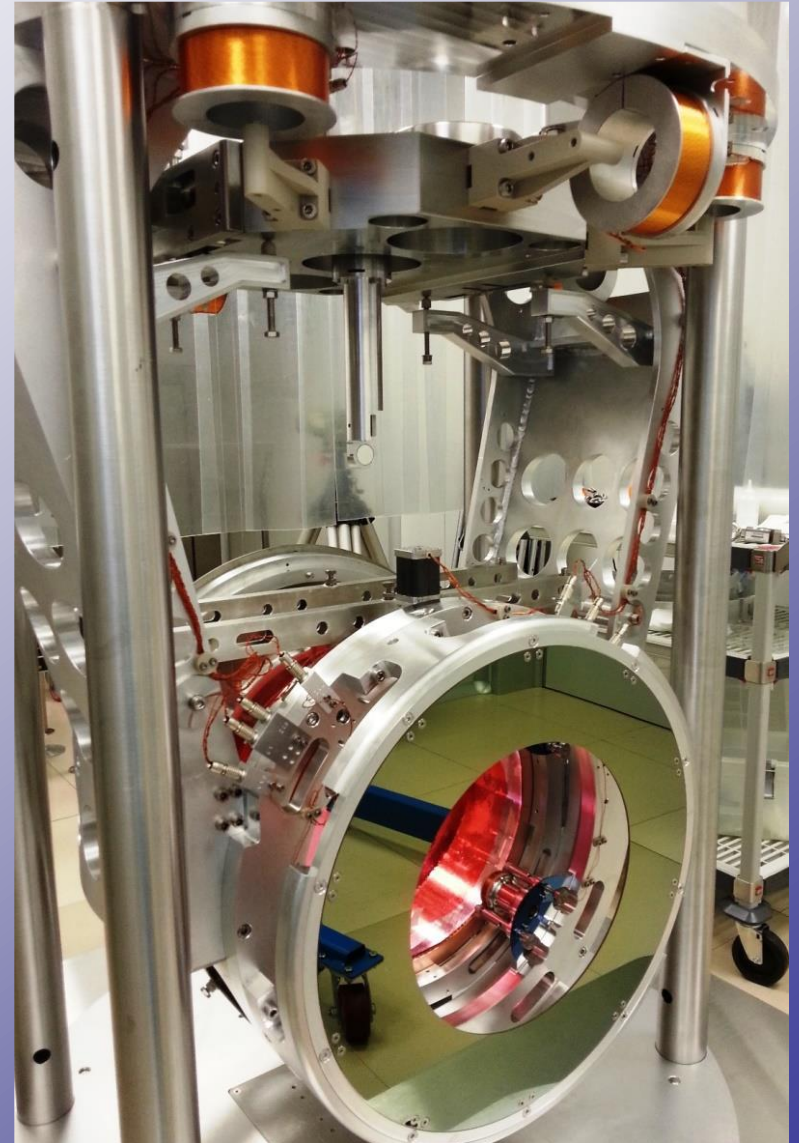
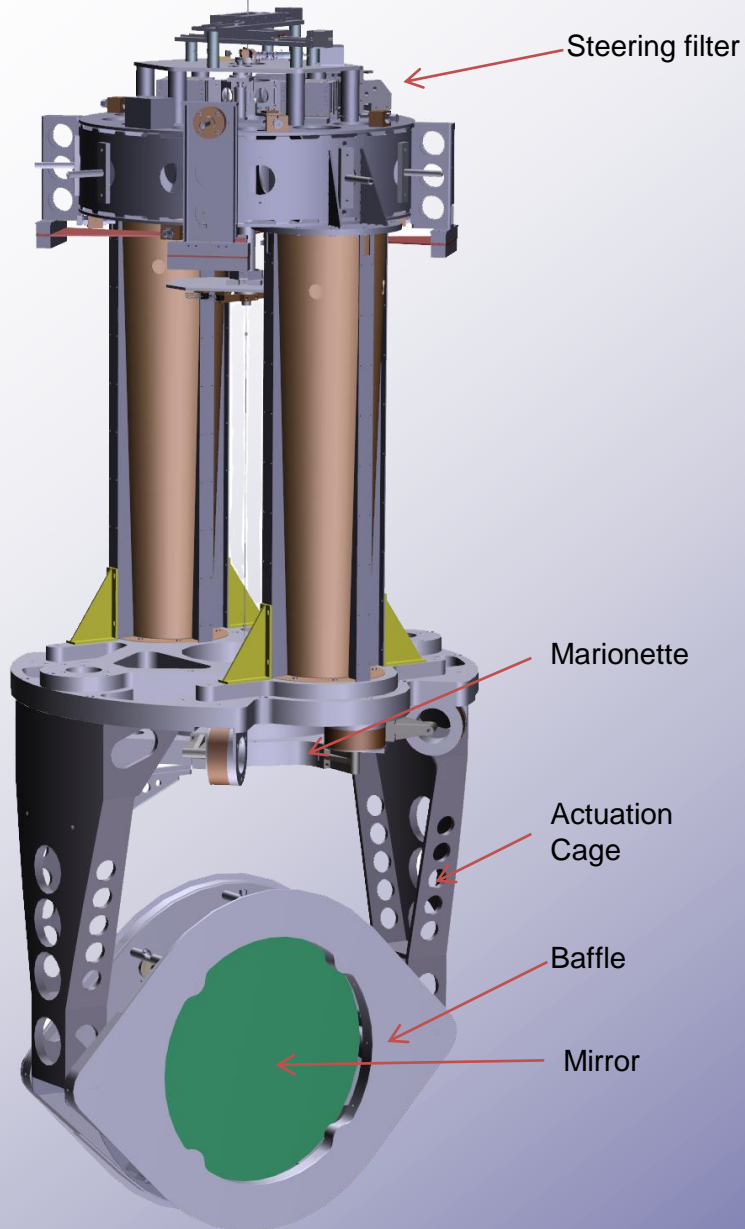


Magnetic antispring working principle

**10^2 for $f > 2$ Hz
of passive attenuation
in both horizontal and vertical
direction !!**

AdVirgo Superattenuator

The payload

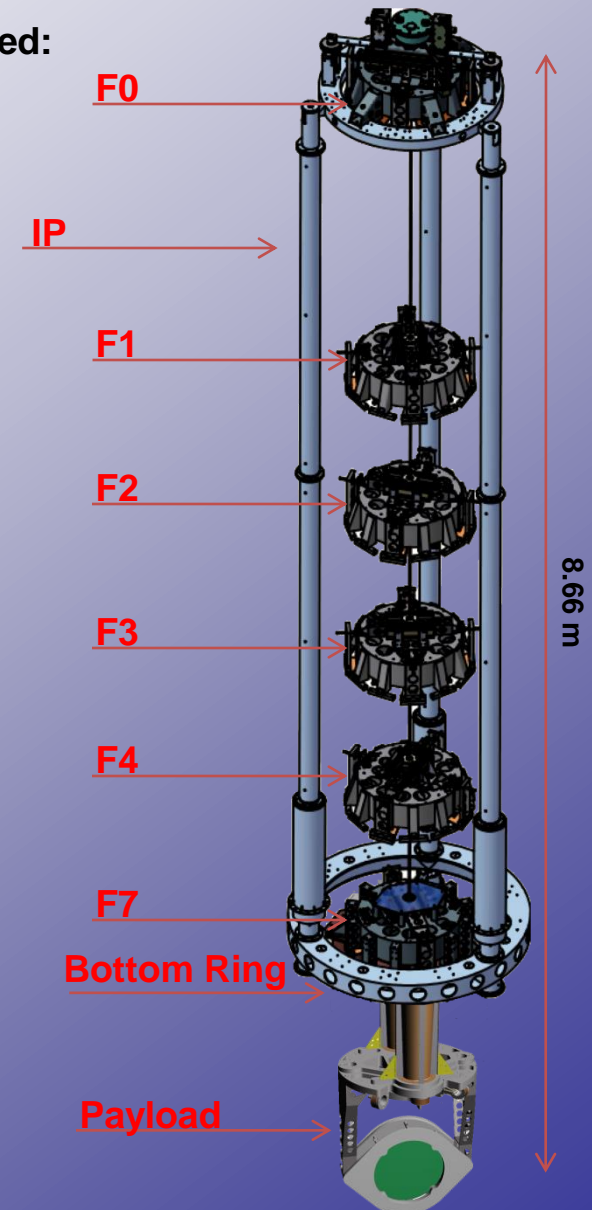


AdVirgo Superattenuator

Control system setup

On long superattenuators (BS, NI, NE, WI, WE, PR, SR) are installed:

- **18 LVDTs** of 3 different types
 - 9 Vertical LVDTs (F0 – F7 Crossbar, Bottom Ring)
 - 3 F0 Horizontal LVDT
 - 6 F7 LVDTs
- **5 Accelerometers** of 2 different types installed on F0:
 - 3 Horizontal Accs
 - 2 Vertical Accs
- **23 Coils** of 4 different types
 - 5 F0 Coils
 - 6 F7 Coils
 - 8 Marionette coils
 - 4 Mirror coils
- **3 Piezos** on bottom ring
- **21 Motors**
 - 1 Top screw F0 vertical motor
 - 3 F0 trolley motors
 - 6 Fishing rod motors
 - 2 Marionette motors
 - 4 F7 motors
 - 5 Accelerometer motors



AdVirgo Superattenuator

Control system hardware

- **Electronics Design based on Texas Instruments DSP**

- TMS320C6678

- Eight TMS320C66x DSP Core Subsystems
 - 320 GMAC/160 GFLOP @ 1.25GHz
 - Four Lanes of SRIO 2.1 - 5 Gbaud Per Lane Full Duplex
 - Two Lanes PCIe Gen2 - 5 Gbaud Per Lane Full Duplex
 - Ethernet MAC Subsystem - Two SGMII Ports w/ 10/100/1000 Mbps operation
 - 64-Bit DDR3 Interface (DDR3-1600)

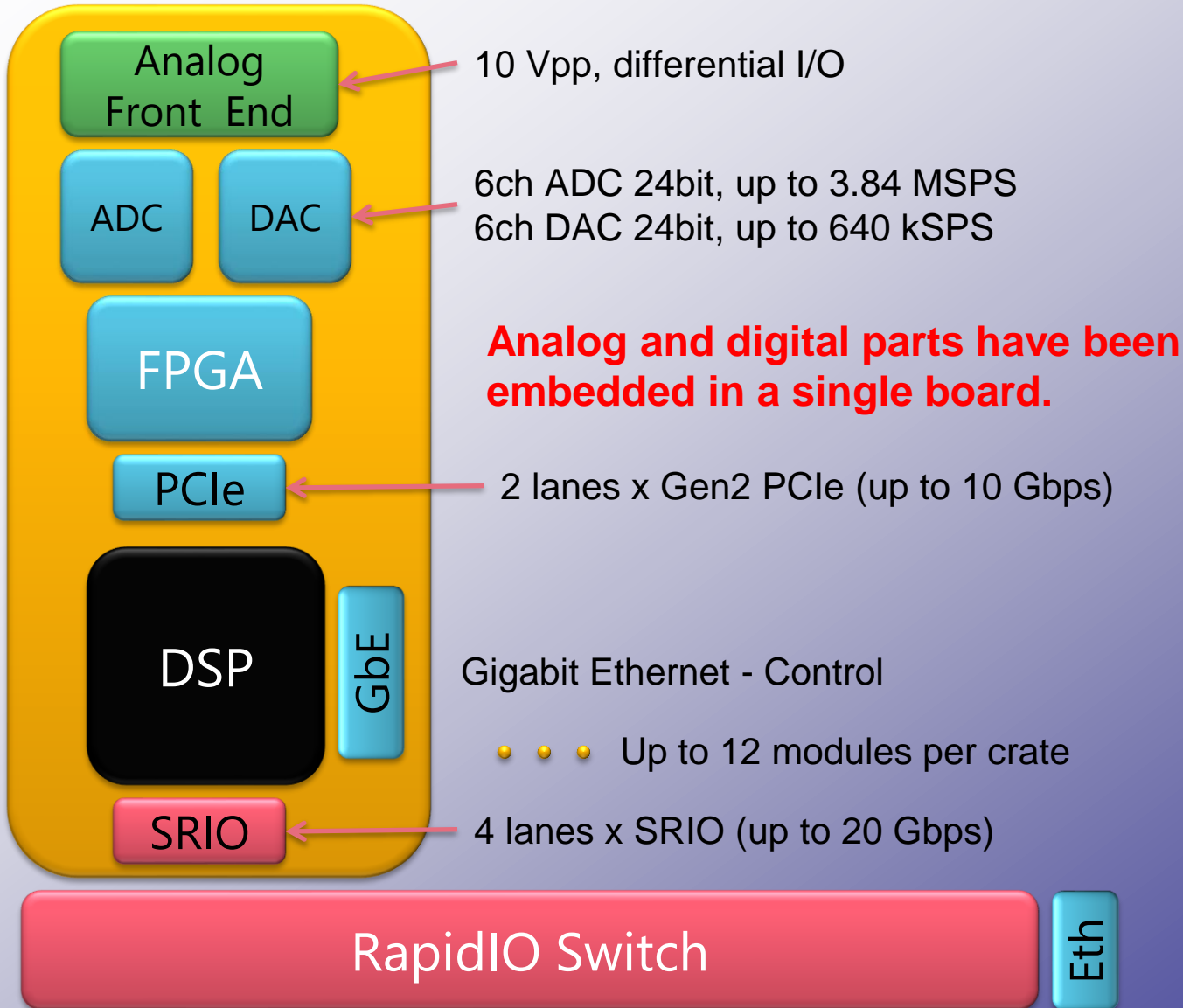


Computing power of a high-end GPU but extremely energy efficient and specifically designed for hard real-time applications

Platform		Effective Time to complete 1024 complex to complex FFT (single precision) μ s	Power (Watts)	Energy per FFT (μ J)
GPU	nVidia Tesla C2070	0.16	225	36
GPU	nVidia Tesla C1060	0.3	188	56.4
GPP	Intel Xeon Core Duo @ 3 GHz	1.8	95	171
GPP	Intel Nehalem Quad Core @ 3.2 GHz	1.2	130	156
DSP	TI C6678 @ 1.2 GHz	0.86	10	8.6

AdVirgo Superattenuator

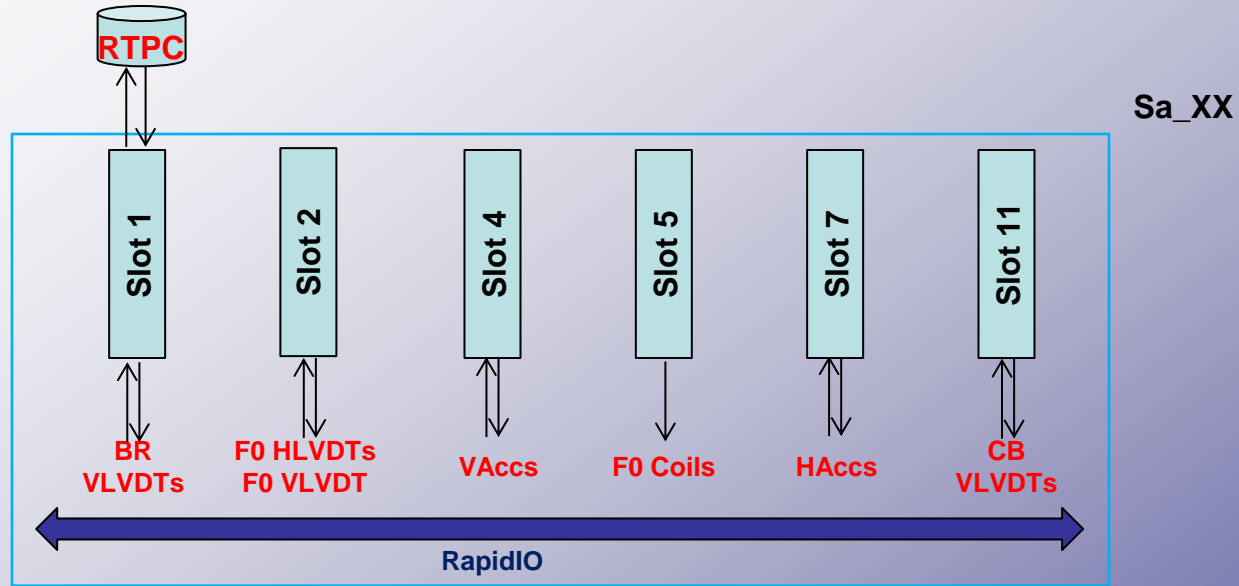
Control system hardware



AdVirgo Superattenuator

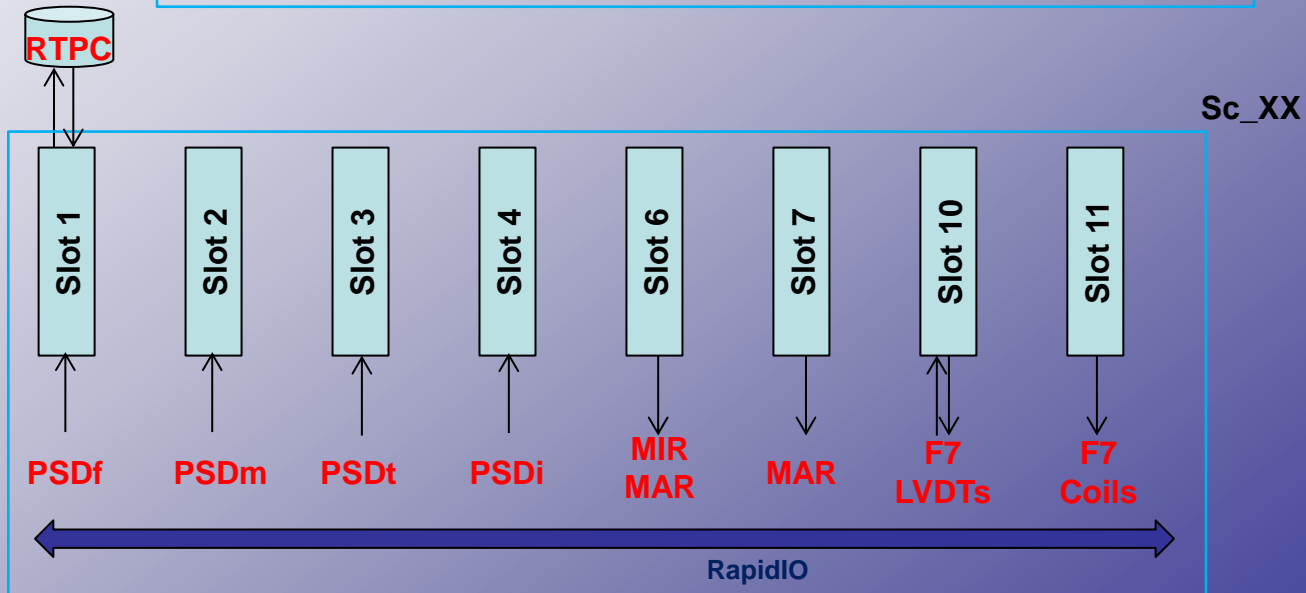
Control system hardware

- A total of 14 boards, each one equipped with an 8-core TMS320C6678 DSP, are connected to each long suspension:



Total computing power of each SA :

> 2.2 TFLOPs !!



AdVirgo Superattenuator

Control system software

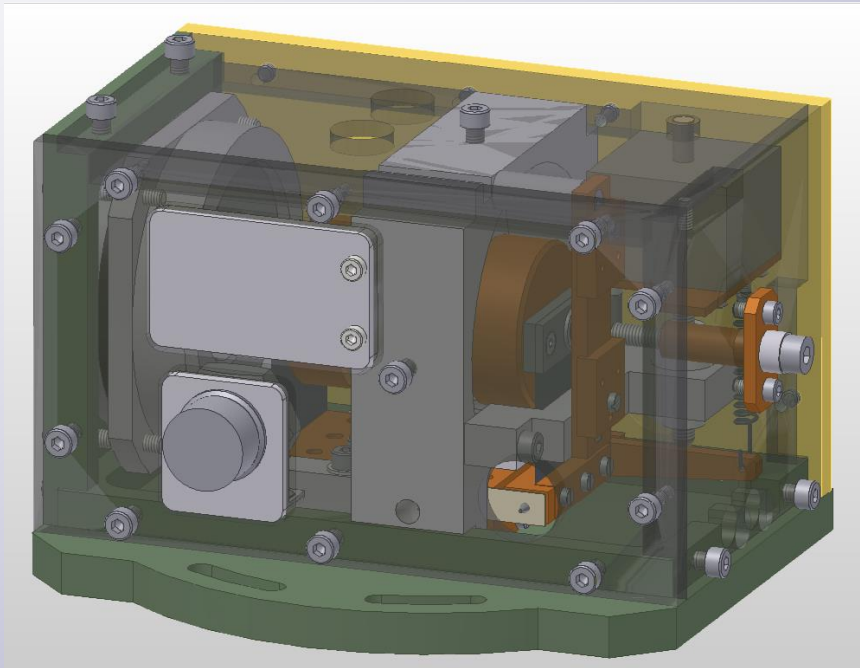
SA control is an extremely complex system:

- **131** DSP boards are installed on BPC, BS, IB, MC, PR, NI, NE, WI, WE, SR, OB
- **185** control code files are running at the same time on the DSP cores at 10 kHz (IP, F7, LC controls), 40 kHz (Global signals oversampling) and 320 kHz (Digital demodulation of sensors)
- All the DSP software (code, generated assembler and binaries) is archived in an SVN repo that can be browsed:
https://svn.ego-gw.it/svn/satsw/DSPCode_Adv/

O2 SOFTWARE MAP				
SA	BOARD IP	CONNECTED DEVICES	SOFTWARE RUNNING (Core4, 10 kHz)	SOFTWARE RUNNING (Core1, 320 kHz)
BPC	172.16.2.104	PSD	/virgoDev/Sa/DSPCode_Adv/BPC/BPC_PSD	
BPC	172.16.2.141	PIEZO	/virgoDev/Sa/DSPCode_Adv/BPC/BPC_CD	
Sa_BS	172.16.2.62	BR LVDTs	/virgoDev/Sa/DSPCode_Adv/BS/LVDT/BS_MASTER	/virgoDev/Sa/DSPCode_Adv/BS/LVDT/BS_BR_LVDT_Demod
Sa_BS	172.16.2.53	F0 LVDTs	/virgoDev/Sa/DSPCode_Adv/BS/LVDT/BS_LVDT_HS_SRIO	/virgoDev/Sa/DSPCode_Adv/BS/LVDT/BS_LVDT_HG2
Sa_BS	172.16.2.32	F0 VAccs	/virgoDev/Sa/DSPCode_Adv/BS/Accs/BS_vAcc_LQG	/virgoDev/Sa/DSPCode_Adv/BS/Accs/BS_vAcc_Demod
Sa_BS	172.16.2.33	F0 Coils	/virgoDev/Sa/DSPCode_Adv/BS/InertialDamping/BS_ID_Diag	
Sa_BS	172.16.2.133	F0 HAccs	/virgoDev/Sa/DSPCode_Adv/BS/Accs/BS_Acc_LQG	/virgoDev/Sa/DSPCode_Adv/BS/Accs/BS_Acc_Demod
Sa_BS	172.16.2.52	F1-F7 VLVDTS	/virgoDev/Sa/DSPCode_Adv/BS/LVDT/BS_VLVDT_SRIO	/virgoDev/Sa/DSPCode_Adv/BS/LVDT/BS_VLVDT
Sc_BS	172.16.2.80	PSD	/virgoDev/Sa/DSPCode_Adv/BS/LC/BS_PSDf	
Sc_BS	172.16.2.108	PSD	/virgoDev/Sa/DSPCode_Adv/BS/LC/BS_PSDm	
Sc_BS	172.16.2.110	PSD	/virgoDev/Sa/DSPCode_Adv/BS/LC/BS_PSDt	
Sc_BS	172.16.2.84	PSD	/virgoDev/Sa/DSPCode_Adv/BS/LC/BS_PSDi	
Sc_BS	172.16.2.181	MIR, MAR Coils	/virgoDev/Sa/DSPCode_Adv/BS/LC/BS_Mir	
Sc_BS	172.16.2.179	MAR Coils	/virgoDev/Sa/DSPCode_Adv/BS/LC/BS_Mar	
Sc_BS	172.16.2.139	F7 LVDT	/virgoDev/Sa/DSPCode_Adv/BS/LVDT/BS_F7_LVDT	/virgoDev/Sa/DSPCode_Adv/BS/LVDT/BS_F7_LVDT_Demod
Sc_BS	172.16.2.120	F7 Coils	/virgoDev/Sa/DSPCode_Adv/BS/F7/BS_F7_CD	
Sa_IB	172.16.2.28	BR LVDTs	/virgoDev/Sa/DSPCode_Adv/IB/LVDT/IB_MASTER	/virgoDev/Sa/DSPCode_Adv/IB/LVDT/IB_BR_LVDT_Demod
Sa_IB	172.16.2.130	F0, F4, F7 LVDTs	/virgoDev/Sa/DSPCode_Adv/IB/LVDT/IB_LVDT	/virgoDev/Sa/DSPCode_Adv/IB/LVDT/IB_LVDT_Demod
Sa_IB	172.16.2.9	F0 VAccs	/virgoDev/Sa/DSPCode_Adv/IB/Accs/IB_vAcc_LQG	/virgoDev/Sa/DSPCode_Adv/IB/Accs/IB_vAcc_Demod
Sa_IB	172.16.2.121	F0 Coils	/virgoDev/Sa/DSPCode_Adv/IB/InertialDamping/IB_ID_Diag	
Sa_IB	172.16.2.23	F0 HAccs	/virgoDev/Sa/DSPCode_Adv/IB/Accs/IB_Acc_LQG	/virgoDev/Sa/DSPCode_Adv/IB/Accs/IB_Acc_Demod
Sc_IB	172.16.2.118	PSD	/virgoDev/Sa/DSPCode_Adv/IB/LC/IB_PSDf	
Sc_IB	172.16.2.86	PSD	/virgoDev/Sa/DSPCode_Adv/IB/LC/IB_PSDi	
Sc_IB	172.16.2.107	PSD	/virgoDev/Sa/DSPCode_Adv/IB/LC/IB_PSDt	
Sc_IB	172.16.2.173	MAR Coils	/virgoDev/Sa/DSPCode_Adv/IB/LC/IB_Mar1	
Sc_IB	172.16.2.174	MAR Coils	/virgoDev/Sa/DSPCode_Adv/IB/LC/IB_Mar2	
Sa_MC	172.16.2.128	BR LVDTs	/virgoDev/Sa/DSPCode_Adv/MC/LVDT/MC_MASTER	/virgoDev/Sa/DSPCode_Adv/MC/LVDT/MC_BR_LVDT_Demod
Sa_MC	172.16.2.51	F0, F4, F7 LVDTs	/virgoDev/Sa/DSPCode_Adv/MC/LVDT/MC_LVDT	/virgoDev/Sa/DSPCode_Adv/MC/LVDT/MC_LVDT_Demod
Sa_MC	172.16.2.158	F0 VAccs	/virgoDev/Sa/DSPCode_Adv/MC/Accs/MC_vAcc_LQG	/virgoDev/Sa/DSPCode_Adv/MC/Accs/MC_vAcc_Demod
Sa_MC	172.16.2.103	F0 Coils	/virgoDev/Sa/DSPCode_Adv/MC/InertialDamping/MC_ID_Diag	
Sa_MC	172.16.2.14	F0 HAccs	/virgoDev/Sa/DSPCode_Adv/MC/Accs/MC_Acc_LQG	/virgoDev/Sa/DSPCode_Adv/MC/Accs/MC_Acc_Demod
Sa_MC	172.16.2.150	PIEZO	/virgoDev/Sa/DSPCode_Adv/MC/tilt/Piezo_Test	
Sc_MC	172.16.2.101	PSD	/virgoDev/Sa/DSPCode_Adv/MC/LC/MC_PSDf	
Sc_MC	172.16.2.168	PSD	/virgoDev/Sa/DSPCode_Adv/MC/LC/MC_PSDi	
Sc_MC	172.16.2.88	PSD	/virgoDev/Sa/DSPCode_Adv/MC/LC/MC_PSDTf	
Sc_MC	172.16.2.109	PSD	/virgoDev/Sa/DSPCode_Adv/MC/LC/MC_PSDTi	
Sc_MC	172.16.2.171	MAR Coils	/virgoDev/Sa/DSPCode_Adv/MC/LC/MC_Mar1	
Sc_MC	172.16.2.172	MAR Coils	/virgoDev/Sa/DSPCode_Adv/MC/LC/MC_Mar2	
Sc_MC	172.16.2.176	MIR Coils	/virgoDev/Sa/DSPCode_Adv/MC/LC/MC_Mir	
Sa_NE	172.16.2.37	BR LVDTs	/virgoDev/Sa/DSPCode_Adv/NE/LVDT/NE_MASTER	/virgoDev/Sa/DSPCode_Adv/NE/LVDT/NE_BR_LVDT_Demod
Sa_NE	172.16.2.40	F0 LVDTs	/virgoDev/Sa/DSPCode_Adv/NE/LVDT/NE_LVDT	/virgoDev/Sa/DSPCode_Adv/NE/LVDT/NE_LVDT_Demod

AdVirgo Superattenuator Sensors

- There is a total of 5 Accelerometer (Accs) installed on the suspension F0 of 2 different types with sensitivity of about $3 \cdot 10^{-10}$ m/s²/sqrt(Hz) for $f < 3$ Hz
- There are 18 LVDTs installed on long tower suspensions of 3 different types with a sensitivity of about 10^{-8} m/sqrt(Hz) for $f > 0.1$ Hz
- All the LVDTs are operated using a digital demodulation scheme at 320 kHz sampling frequency



AdVirgo Superattenuator Sensors

- There are 18 LVDTs installed on long tower suspensions of 3 different types
 - 9 Vertical LVDTs (F0 – F7 Crossbar, Bottom Ring)
 - 3 F0 Horizontal LVDT
 - 6 F7 LVDTs
- Each sensors have been characterized and calibrated
- All the LVDTs are operated using a digital demodulation scheme at 320 kHz sampling frequency:

```

Level: Top
Virgo Inertial damping on [ 172.16.2.14 ] Page 1
Hardware implementation
BS_VLVD_00.hrd
Ramp Time [100.00] Downsampling Factor [1]
Sampling Frequency [320000.00] Oversampling Factor [1]

Input Output Filename GUARD Gain Gname @Frequency When
-----
ADCI sc1 NULL no 1
ADC2 sc2 NULL no 1
ADC3 sc3 NULL no 1
ADC4 sc4 NULL no 1
ADC5 sc7 NULL no 1
SIG_GEN pr1 sine1 no 1
SIG_GEN pr2 sine2 no 1
SIG_GEN pr3 sine3 no 1
SIG_GEN pr4 sine4 no 1
SIG_GEN pr7 sine7 no 1
ADD phase1_1 no -83.44
ADD phase1_2 no 6.56
ADD phase2_1 no -85.32
ADD phase2_2 no 4.68
ADD phase3_1 no -83.76
ADD phase3_2 no 6.24
ADD phase4_1 no -82.06
ADD phase4_2 no 7.94
ADD phase7_1 no -75.95
ADD phase7_2 no 14.05
SIG_GEN mod_sin1 mod_sin1 no 1
SIG_GEN mod_cos1 mod_cos1 no 1
SIG_GEN mod_sin2 mod_sin2 no 1
SIG_GEN mod_cos2 mod_cos2 no 1
SIG_GEN mod_sin3 mod_sin3 no 1
SIG_GEN mod_cos3 mod_cos3 no 1
SIG_GEN mod_sin4 mod_sin4 no 1
SIG_GEN mod_cos4 mod_cos4 no 1
SIG_GEN mod_sin7 mod_sin7 no 1
SIG_GEN mod_cos7 mod_cos7 no 1
pr1 DAC1 NULL no 5
pr2 DAC2 NULL no 5
pr3 DAC3 NULL no 5
pr4 DAC4 NULL no 5
pr7 DAC5 NULL no 5
MIX mm1_sin mix_sin1 no 1.0
    
```

Secondary signals
Modulation signals

Demodulation phases

Demodulation signals

```

Level: Top
Virgo Inertial damping on [ 172.16.2.14 ] Page 2
Hardware implementation
BS_VLVD_00.hrd
Ramp Time [100.00] Downsampling Factor [1]
Sampling Frequency [320000.00] Oversampling Factor [1]

Input Output Filename GUARD Gain Gname @Frequency When
-----
MIX mm1_cos mix_cos1 no 1.0
MIX mm2_sin mix_sin2 no 1.0
MIX mm2_cos mix_cos2 no 1.0
MIX mm3_sin mix_sin3 no 1.0
MIX mm3_cos mix_cos3 no 1.0
MIX mm4_sin mix_sin4 no 1.0
MIX mm4_cos mix_cos4 no 1.0
MIX mm7_sin mix_sin7 no 1.0
MIX mm7_cos mix_cos7 no 1.0
mm1_sin lvd11 lpflt no 600 0.0 after
mm1_cos lvd11_cos lpflt no 600 0.0 after
mm2_sin lvd12 lpflt no 600 0.0 after
mm2_cos lvd12_cos lpflt no 600 0.0 after
mm3_sin lvd13 lpflt no 600 0.0 after
mm3_cos lvd13_cos lpflt no 600 0.0 after
mm4_sin lvd14 lpflt no 600 0.0 after
mm4_cos lvd14_cos lpflt no 600 0.0 after
mm7_sin lvd17 lpflt no 600 0.0 after
mm7_cos lvd17_cos lpflt no 600 0.0 after
lvd11 PROBE F1_VLVD 1.0
lvd12 PROBE F2_VLVD 1.0
lvd13 PROBE F3_VLVD 1.0
lvd14 PROBE F4_VLVD 1.0
lvd17 PROBE F7_VLVD 1.0
    
```

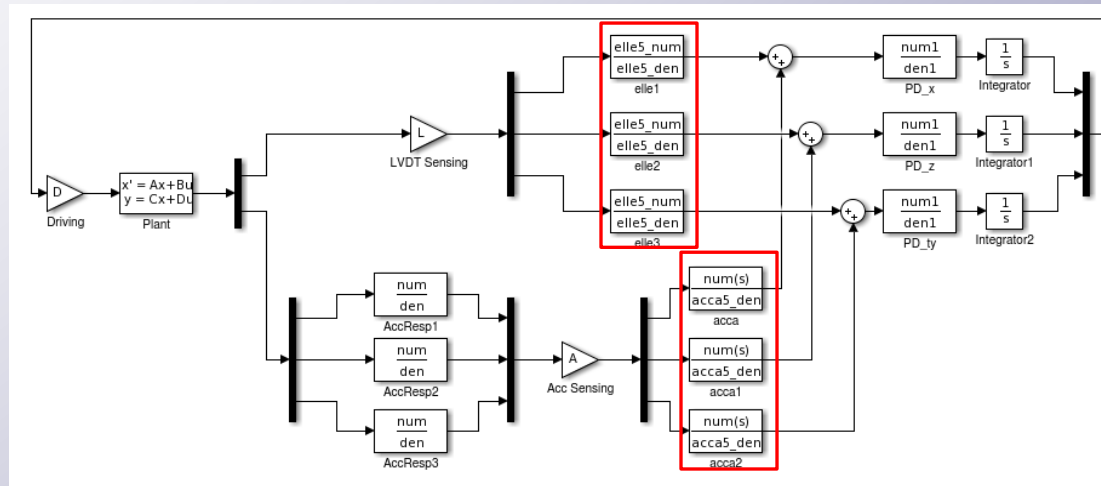
Low pass output filter
(5th order Butterworth at 1 kHz)

AdVirgo Superattenuator

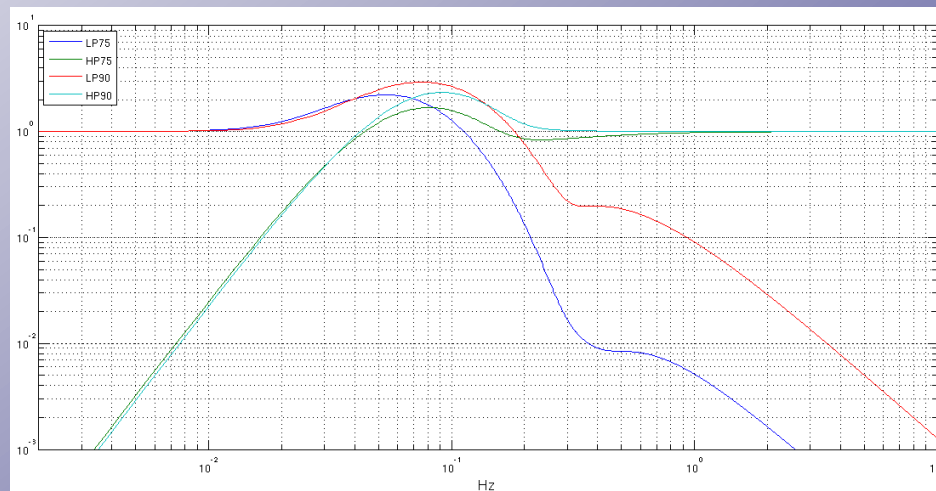
Inertial Damping

Two Accelerometer-LVDT blending filters are used (High Pass for Accs and Low Pass for LVDTs)

- 75 mHz crossover frequency used for standard operation
- 90 mHz crossover frequency used for robustness (High microseism or windy conditions)



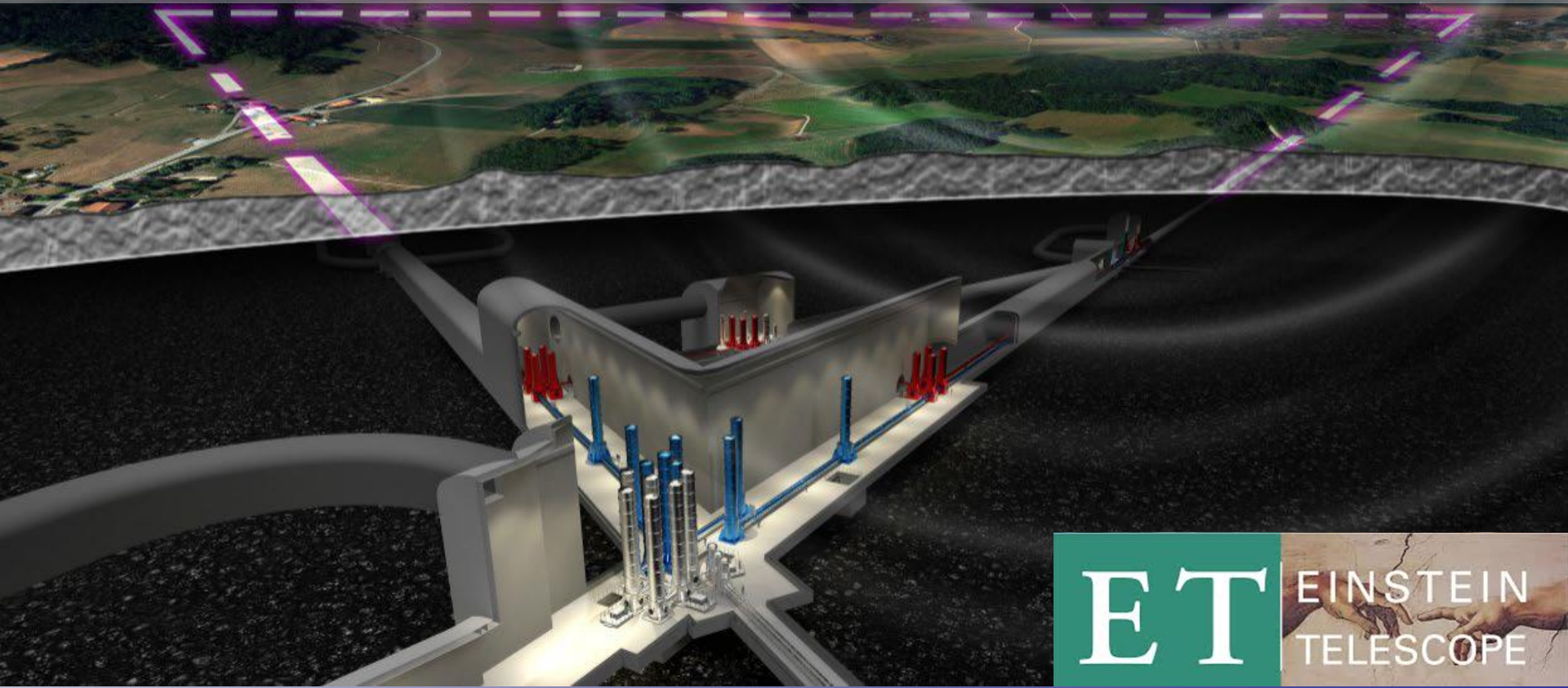
Standard Blending filters



The future of gravitational wave astronomy

Einstein Telescope

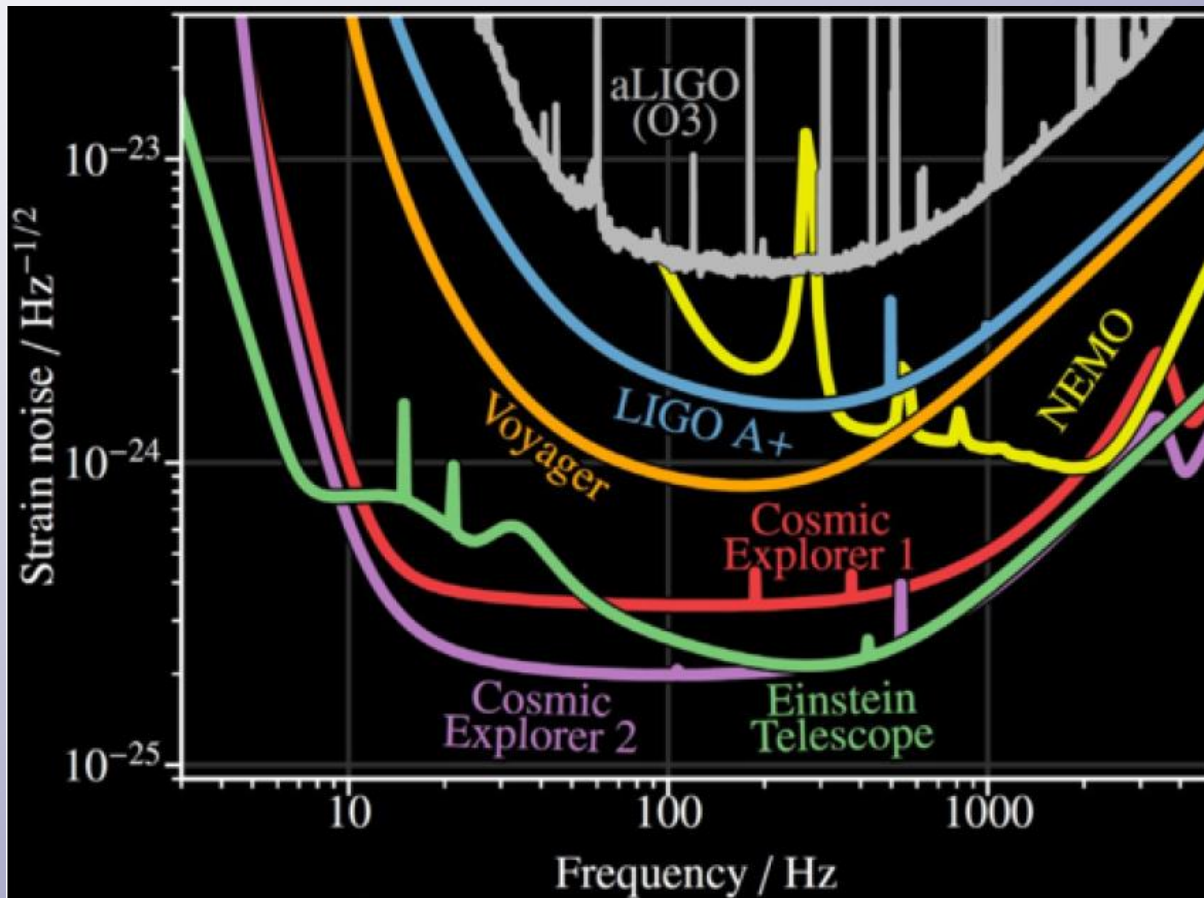
- [Einstein Telescope](#) (ET) is expected to have a triangular configuration, with 10 km of length for each side, in order to host two detectors with different bandwidths, and, to drastically reduce the effects of ground motion, will be built underground, making the needed infrastructural works very complex and expensive.
- In Europe three candidate sites have been identified for ET: an area in the Nuoro province, in Sardinia, Italy, the Meuse-Rhine euroregion at the border between Netherlands, Belgium and Germany, and a location in Saxony, Germany.



Einstein Telescope

Seismic isolation

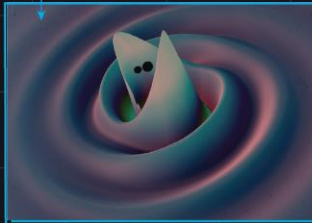
- The gravitational-wave interferometers of next generation, Einstein and Cosmic Explorer, aim at gaining a factor of 10 in noise level, respect to Virgo and LIGO, but also extending at low frequency their detection band.
- Even in a site with very low seismicity, the sensitivity increase in the low frequency region will put challenging constraints on the suppression of seismic noise: **new designs should be studied.**



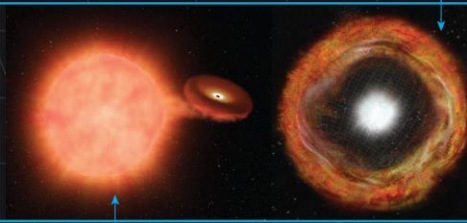
Laser Interferometer Lunar Antenna

<https://www.vanderbilt.edu/lunarlabs/lila/>

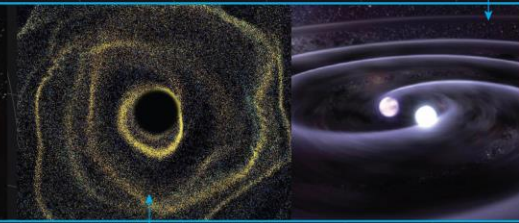
Multi-band test of General Relativity
at cosmological scales
with IMBH binaries



White dwarf mergers
as progenitors of Type Ia SNe;
Emissions from Core collapse SNe



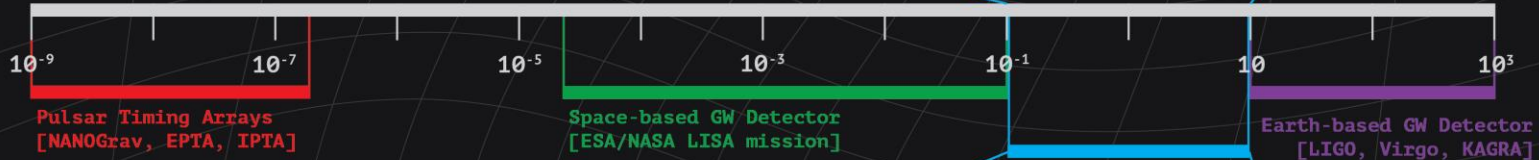
Early-warning alert of days
to months for binary
neutron star mergers



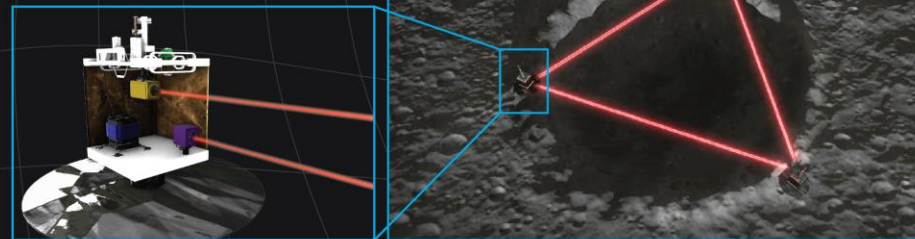
Multi-messenger observation
of IMRIs as tidal
disruption events

Superradiance of axion-like particles
around primordial black holes;
Sub-atomic dark matter emissions

Gravitational-Wave Frequency Spectrum



Moon-based GW Detector
[LILA]

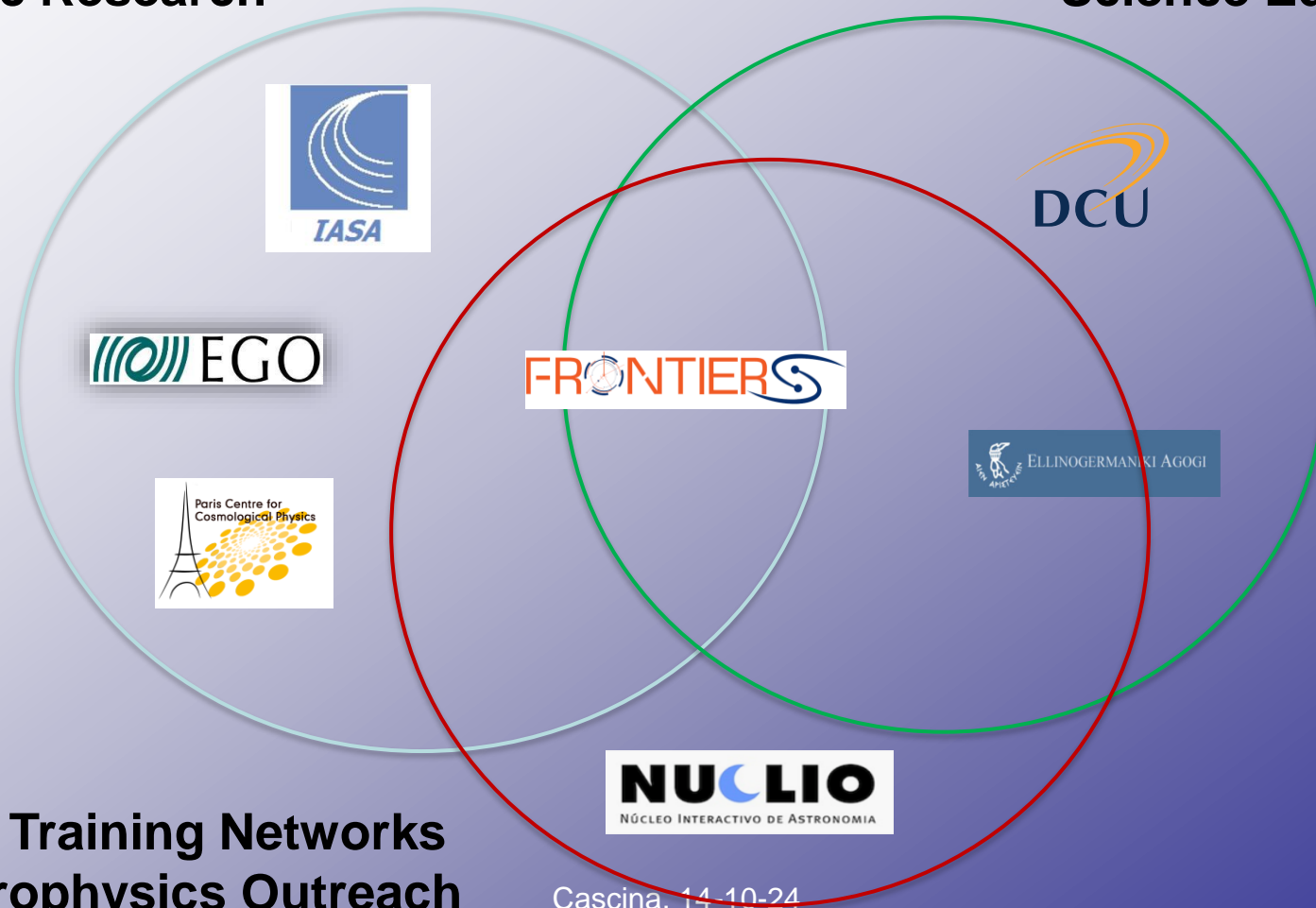


Frontiers (<https://frontiers-project.eu/>)

was an EU funded project bringing together **research** and **educational** institutions from all over **Europe** (2018-2021)

Scientific Research

Science Education



**Teacher Training Networks
and Astrophysics Outreach**

Thank you for your attention!!

